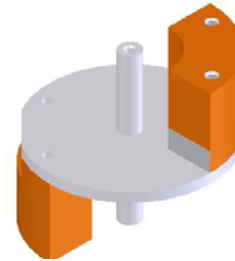


# How I Spent my Summer Vacation



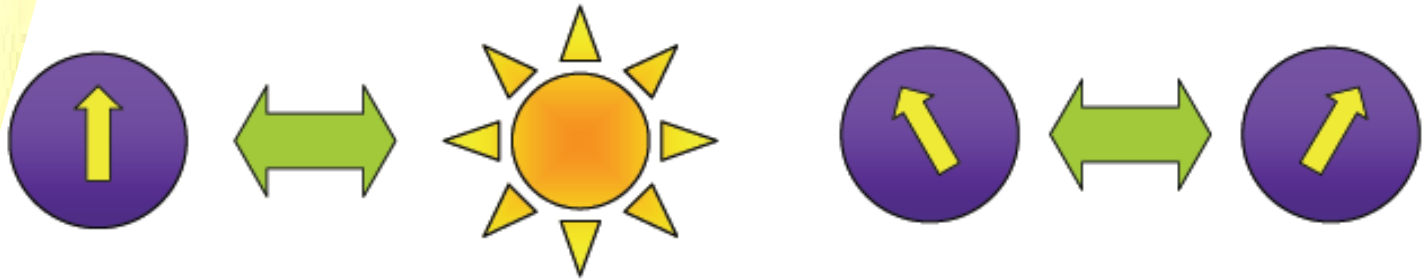
*Searching for gravitational force violations  
and a theoretical 5th force.*

# Overview

- **Better Understanding of Forces**
  - Spin-Coupled Force
  - Inverse Square Law
  - Weak Equivalence Principle
- **Eöt-Wash Instrumentation**
- **Contributions and Improvements**
  - Magnetic Flux Detection
  - Pendulum for Sensitive Detection of Gravity Gradients

# Spin-Coupled Force

- Theoretical 5<sup>th</sup> force coupling to fermion spin
- Force mediated by a new particle (axions?)



$$V_{\text{md}} \propto \sigma_e \cdot \mathbf{r} \quad \text{spin couples to point mass}$$

$$V_{\text{dd}} \propto \sigma_1 \cdot \sigma_2 \quad \text{spins of two spin sources couple}$$

# Inverse Square Law Violation

$$F = \frac{Gm_1m_2}{r^2}$$

*What if gravity is mediated by the exchange of a graviton  
AND another particle?*

$$F = \frac{Gm_1m_2}{r^2} \left[ 1 + \alpha (1 + r/\lambda) e^{-r/\lambda} \right]$$

*2<sup>nd</sup> term called Yukawa interaction*

*Consequence:  $1/r^2$  is a large-scale limit on gravity*

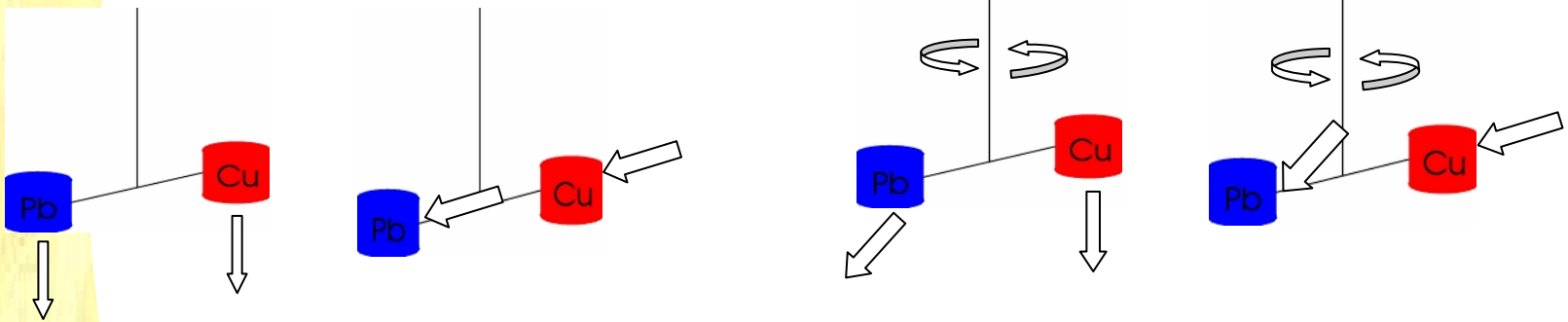
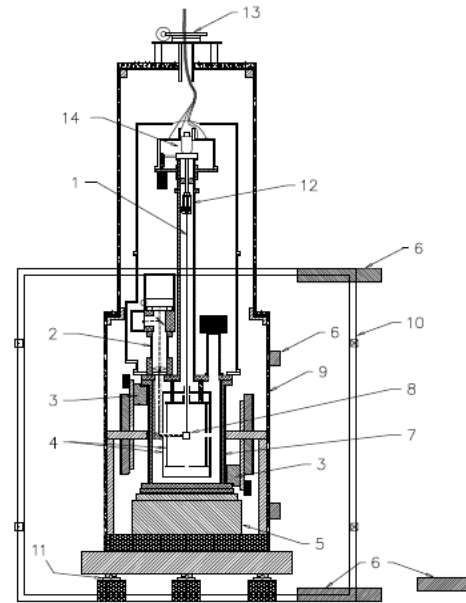
# Weak Equivalence Principle Violation

- WEP says inertial mass = gravitational mass

$$\left. \begin{array}{l} F = m_G g \\ F = m_I a \end{array} \right\} a = \frac{m_G}{m_I} g$$

- What if  $\mathbf{F}_G \neq \mathbf{F}_I$ ?
- Two materials with same *weight* won't necessarily have the same  $F_I$

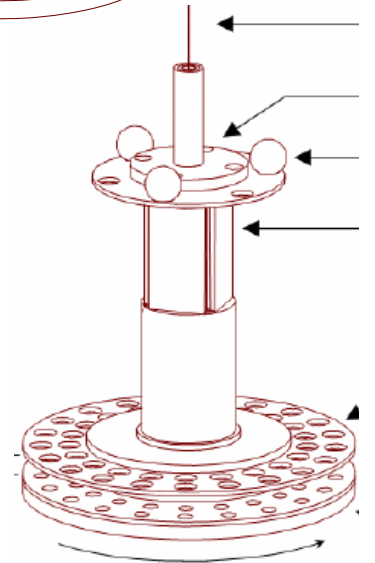
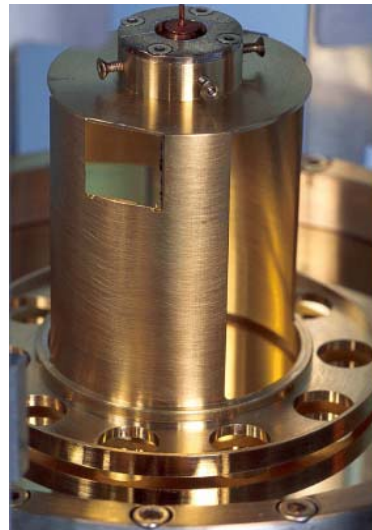
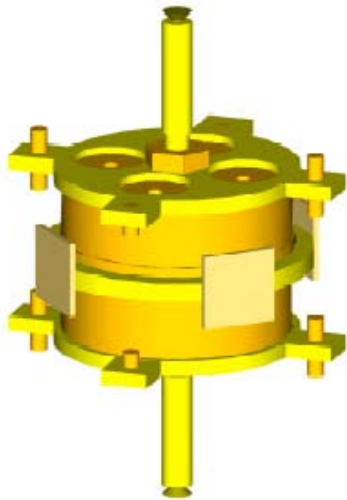
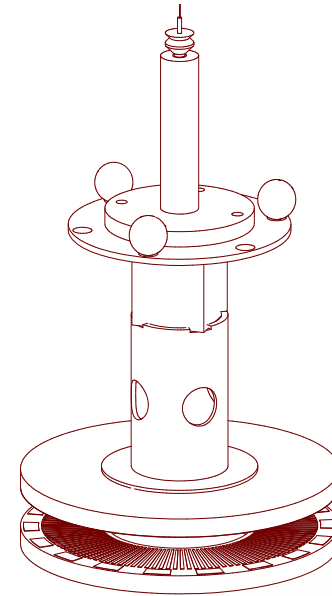
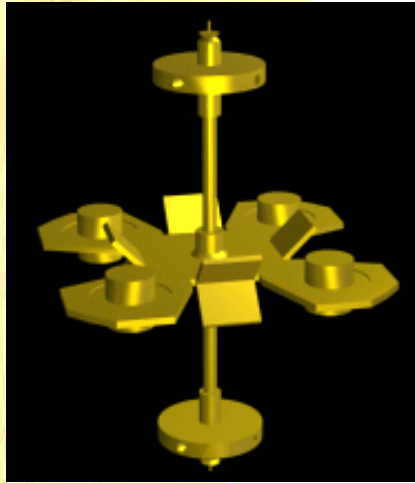
# Torsion Balance



Uneven forces create torque on pendulum

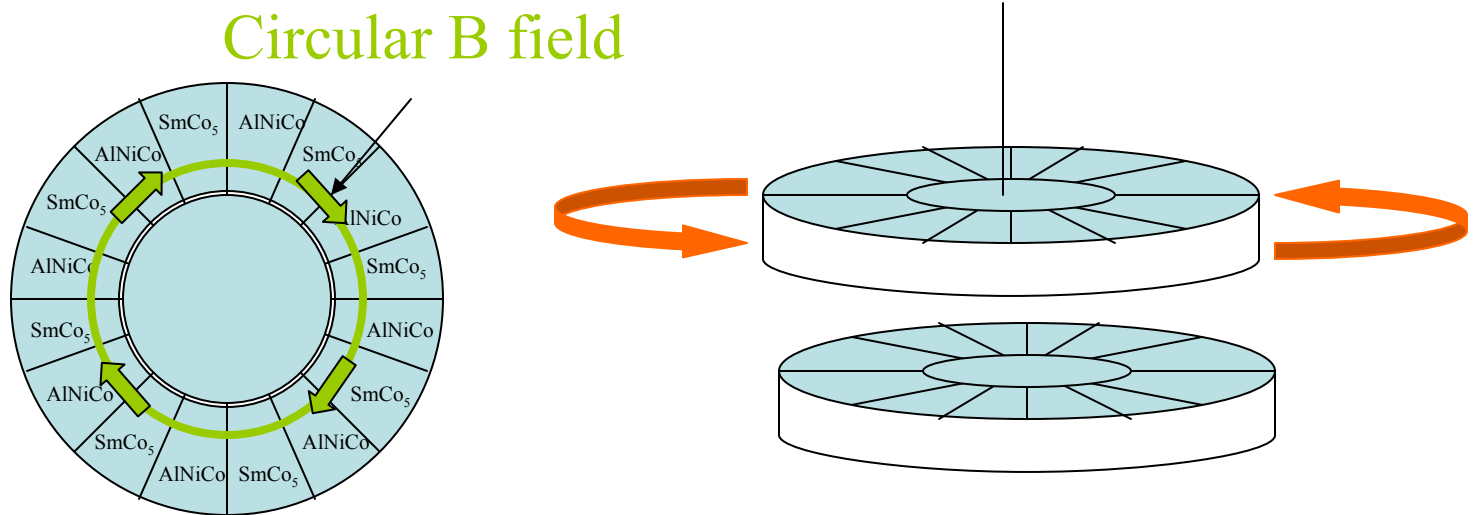
$$\Theta = T / \kappa$$

# Eot-Wash Pendulums



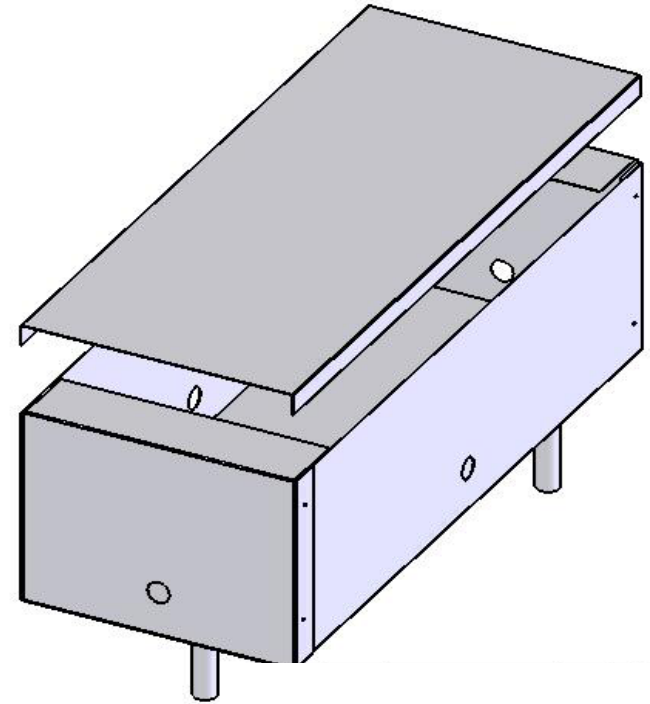
# Spin Force: Experimental Setup

- Trapezoidal magnets form 10 spin dipoles
- Spin moments align to minimize  $V_{dd} \rightarrow$  Torsion of pendulum
- Must evenly magnetize spin pendulum to minimize external flux





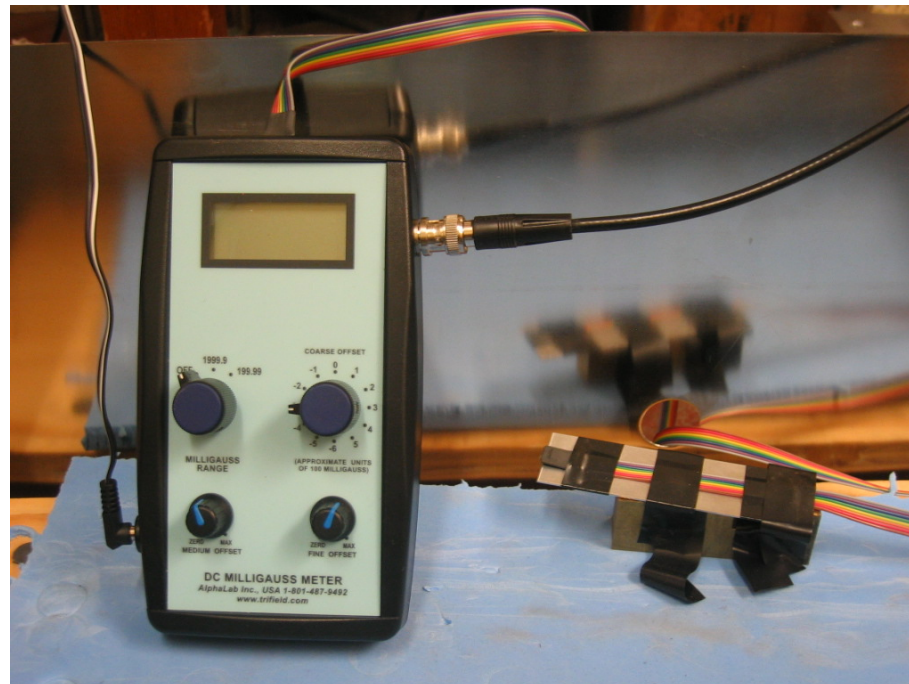
# Magnetic Shield Box



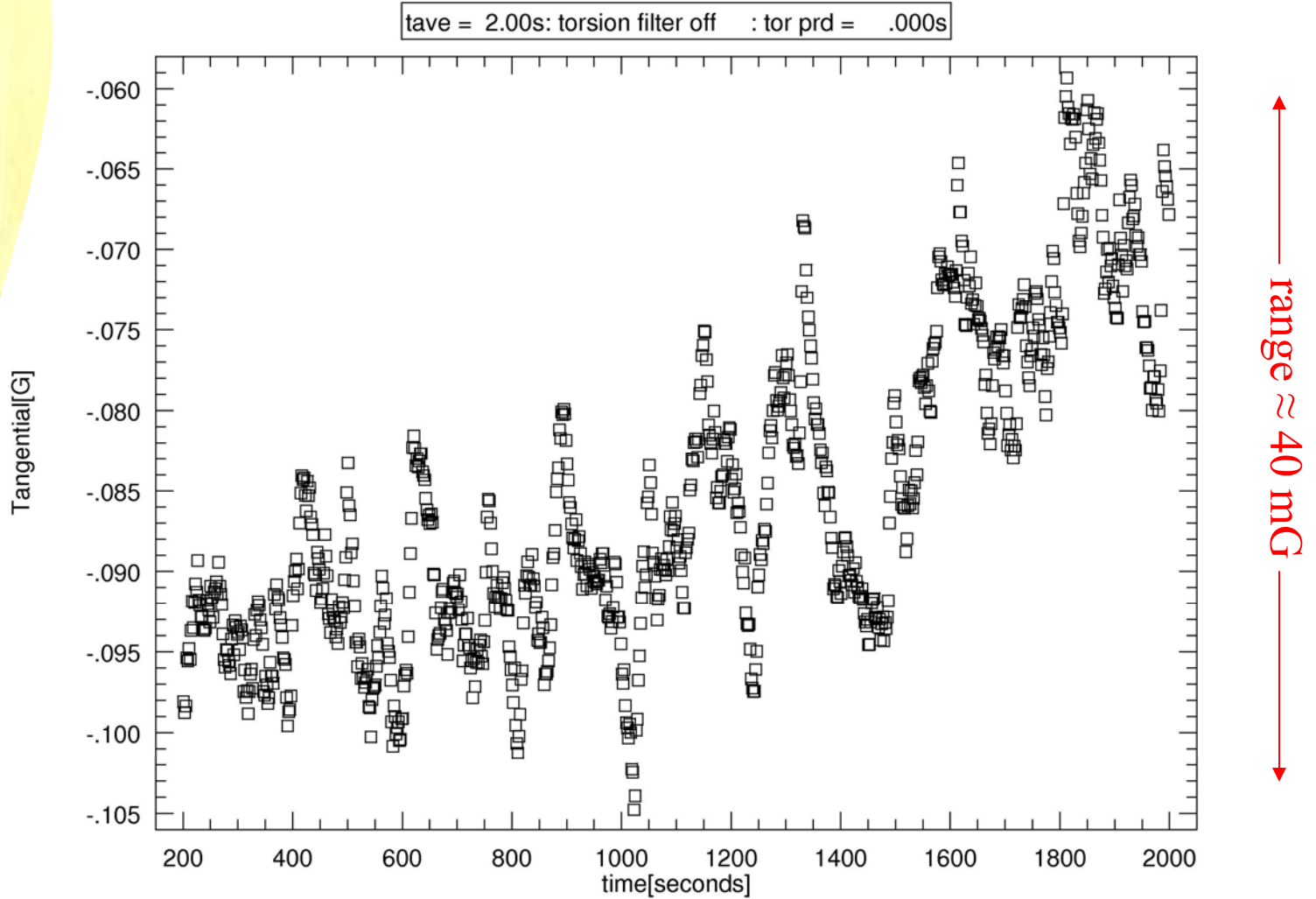
*Permits us to determine external magnetic flux of the spin pendulum and make appropriate corrections.*

# Magnetoresistance Magnetometer

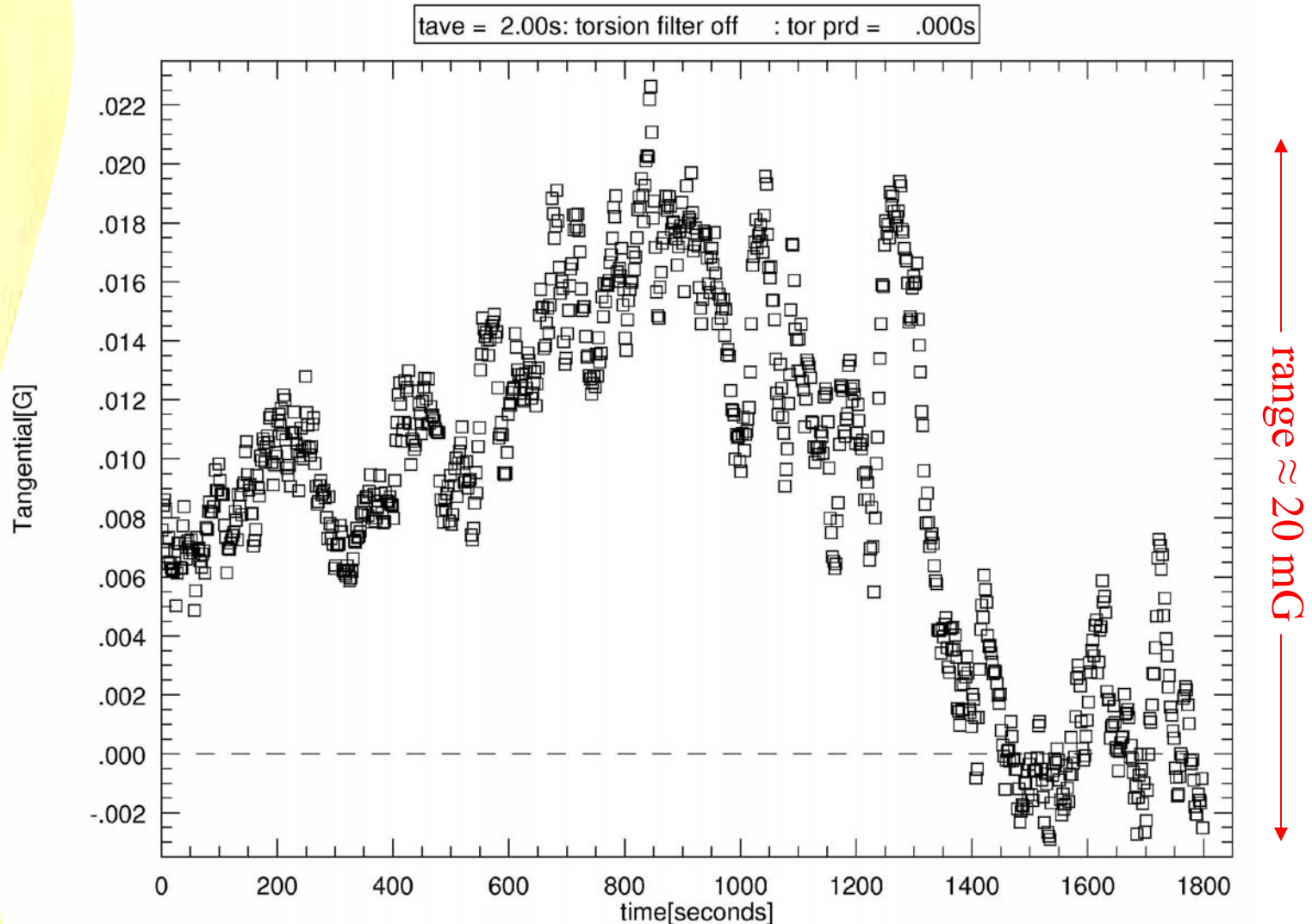
- Range of 2000 milligauss
- Resolution of 0.01 milligauss
- Ideal size



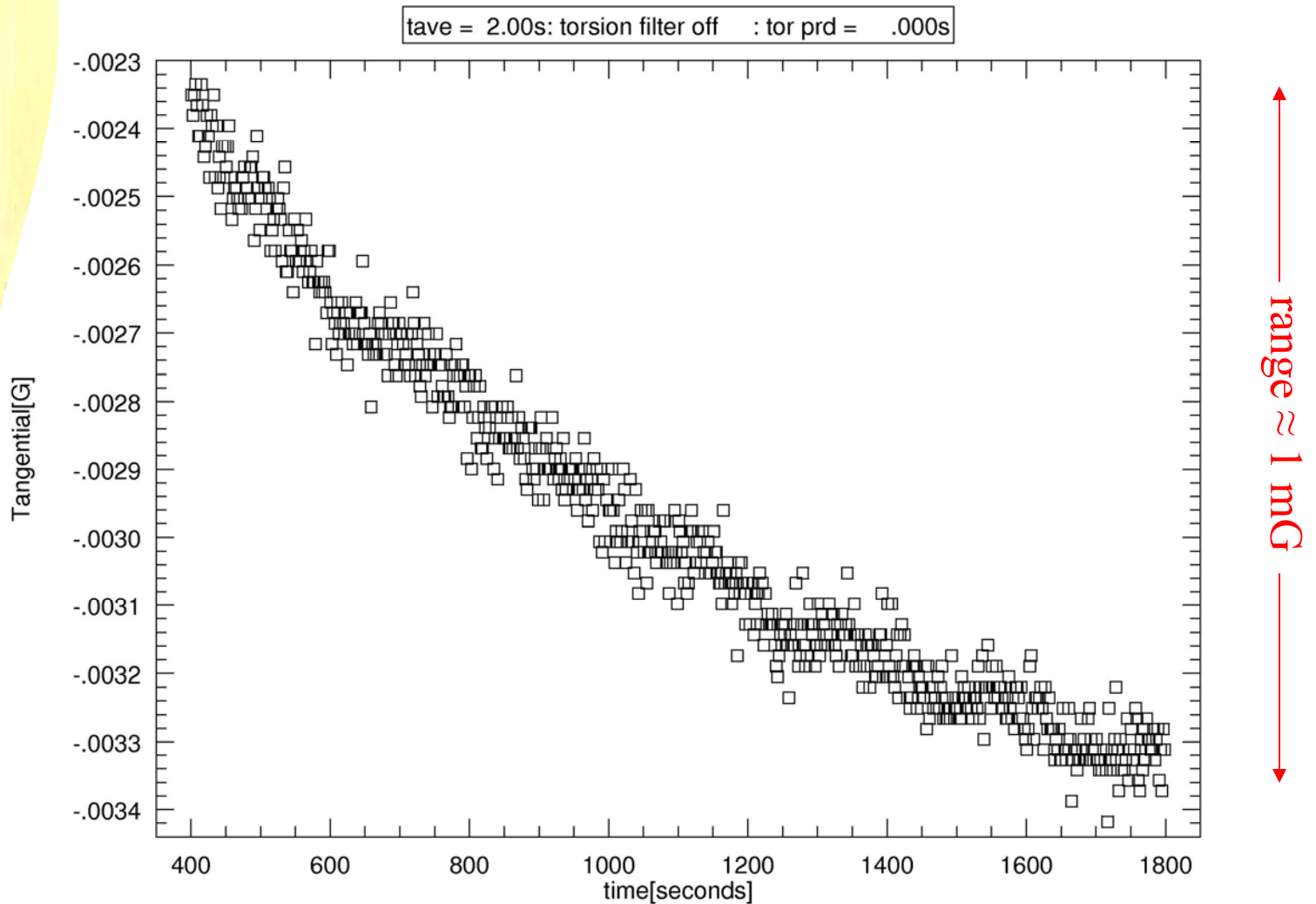
# Noise Run: Old Shield, Old Magnetometer



# Noise Run: New Shield, Old Magnetometer



# Noise Run: New Shield, New Magnetometer



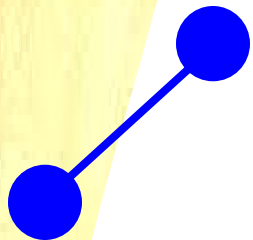
# Gravity Gradient Pendulum:

*Why do it?*

- Eot-Wash pendulums study fundamental forces
  - Spin-coupled force
  - Different law of gravity
- Pendulums highly sensitive to changing gravitational fields
- Measure effects of known gravitational forces and subtract from pendulum measurements

# Pendulum Design: The Gravitational Quadrupole Moment

$$q_{lm} = \int \rho_p(r) r^l Y_{lm}^*(r) d^3r$$



large  $q_{21}$

$$q_{21} = \frac{-1}{2} \sqrt{\frac{15}{2\pi}} \int \rho_p(r) r^2 \sin\theta \cos\theta e^{-i\varphi} d^3r$$

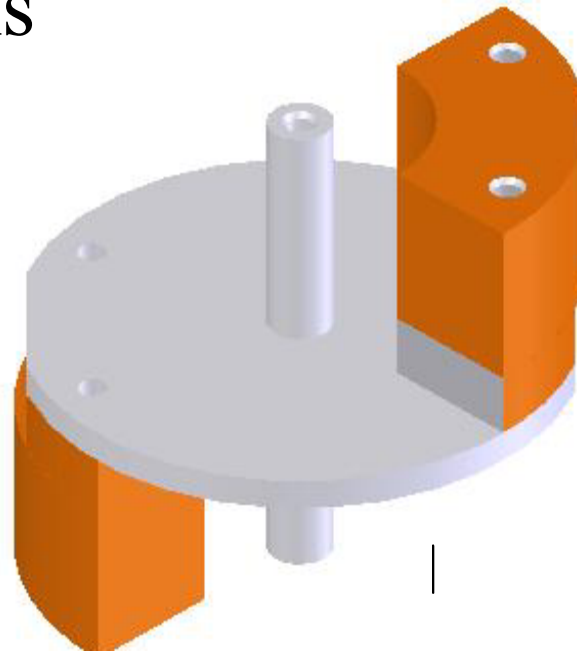


large  $q_{22}$

$$q_{22} = \frac{1}{4} \sqrt{\frac{15}{2\pi}} \int \rho_p(r) r^2 \sin^2\theta e^{-2i\varphi} d^3r$$

# q2 Pendulum

- $q_{21} = -110.02 \text{ gcm}^2$  (10000x greater than normal)
- $q_{22} = 62.79 \text{ gcm}^2$
- Mass and dimensions similar to other pendulums





# Effect of Gravity Gradients on Pendulum

Pendulum angle of deflection:

$$\Theta_g = T_g / \kappa = -4\pi i G / \kappa \sum \frac{1}{2l+1} \sum \bar{m} q_{lm} Q_{lm} \times e^{-im\omega t}$$

Gravitational Multipole Field caused by Environmental Factors:

$$Q_{lm} = \int \rho_s(r') r'^{-(l+1)} Y_{lm}(r') d^3r$$

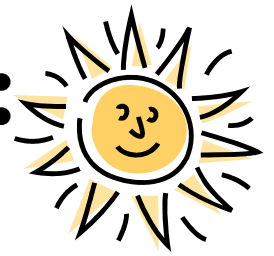
Torsion balance is capable of detecting  $\Theta_g \geq 5$  nrad/day

$$\rightarrow Q_{2m} \geq 2 \times 10^{-5} \text{ g/cm}^3$$



# Possible $Q_{2m}$ Contributors:

## Sun and Moon



Time of Day	$\Theta$ sun	$Q_{21}$ ( $\times 10^{-7}$ )	$Q_{22}$ ( $\times 10^{-7}$ )	$\Theta$ moon	$Q_{21}$ ( $\times 10^{-7}$ )	$Q_{22}$ ( $\times 10^{-7}$ )
6:00 AM	90	0	2.2	150	4	1.16
8:00 AM	66	-1.64	1.84	129	4.52	2.79
10:00 AM	41	-2.18	0.947	105	2.31	4.31
12:00 PM	20	-1.41	0.257	83	-1.12	4.55
2:00 PM	-25	1.68	0.393	63	-3.74	3.67
4:00 PM	-48	2.19	1.22	50	-4.55	2.71
6:00 PM	-73	1.23	2.01	141	4.52	1.83
8:00 PM	-96	-0.458	2.18	156	3.43	0.764
Closest approach r (sun) = $1.497E13$ cm r (moon) = 35639888500 m	90	0	2.29	90	0	6.27



# Possible $Q_{2m}$ Contributors: Daily Traffic



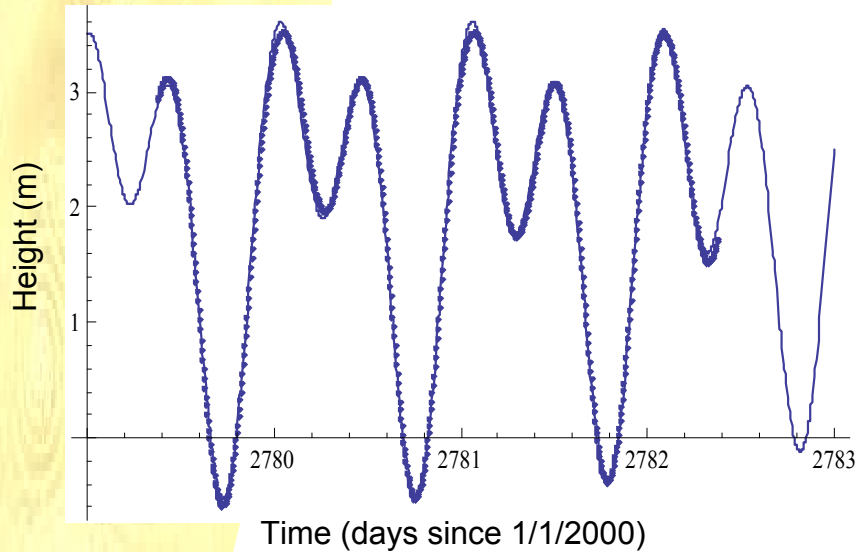
Location	Mass (g)	Distance (cm)	$\Theta$ (degrees)	$Q_{21}$	$Q_{22}$
Alex 1m away	54431.08	100	90	0	$2.10 \times 10^{-2}$
Alex 2m away	54431.08	200	90	0	$2.63 \times 10^{-3}$
Nikolai's office	74842.74	320.79	18.16	$-5.19 \times 10^{-4}$	$8.51 \times 10^{-5}$
Office next to Nikolai's	217724.34	476.11	50.19	$-7.67 \times 10^{-4}$	$4.60 \times 10^{-4}$
Parking Lot - Cars	7801788	3000	7	$-2.70 \times 10^{-5}$	$1.66 \times 10^{-6}$
Parking Lot - UPS Delivery Truck	4082331	2700	2	$-5.59 \times 10^{-6}$	$9.76 \times 10^{-8}$
Parking Lot - GMC Delivery Truck	4082331	2000	3	$-2.06 \times 10^{-5}$	$5.40 \times 10^{-7}$

# Possible $Q_{2m}$ Contributors: Puget Sound Tides

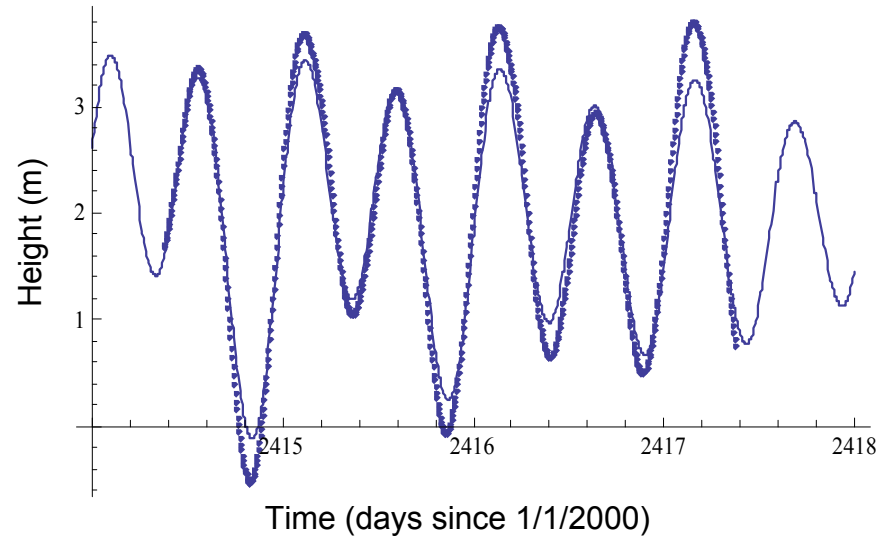
Location	Mass-HT (g)	Mass-LT (g)	Distance (cm)	$Q_{22}$ - HT	$Q_{22}$ - LT	$\Delta Q_{22}$
All mass centered in middle of Elliot Bay	$9.31 \times 10^{14}$	$8.80 \times 10^{14}$	$7.83 \times 10^5$	$7.49 \times 10^{-4}$	$7.08 \times 10^{-4}$	$4.10 \times 10^{-5}$
All mass centered farthest from UW	$9.31 \times 10^{14}$	$8.80 \times 10^{14}$	$1.00 \times 10^6$	$3.60 \times 10^{-4}$	$3.40 \times 10^{-4}$	$2.00 \times 10^{-5}$



# Mapping the Tides



Curve fit to 2007/2008 data



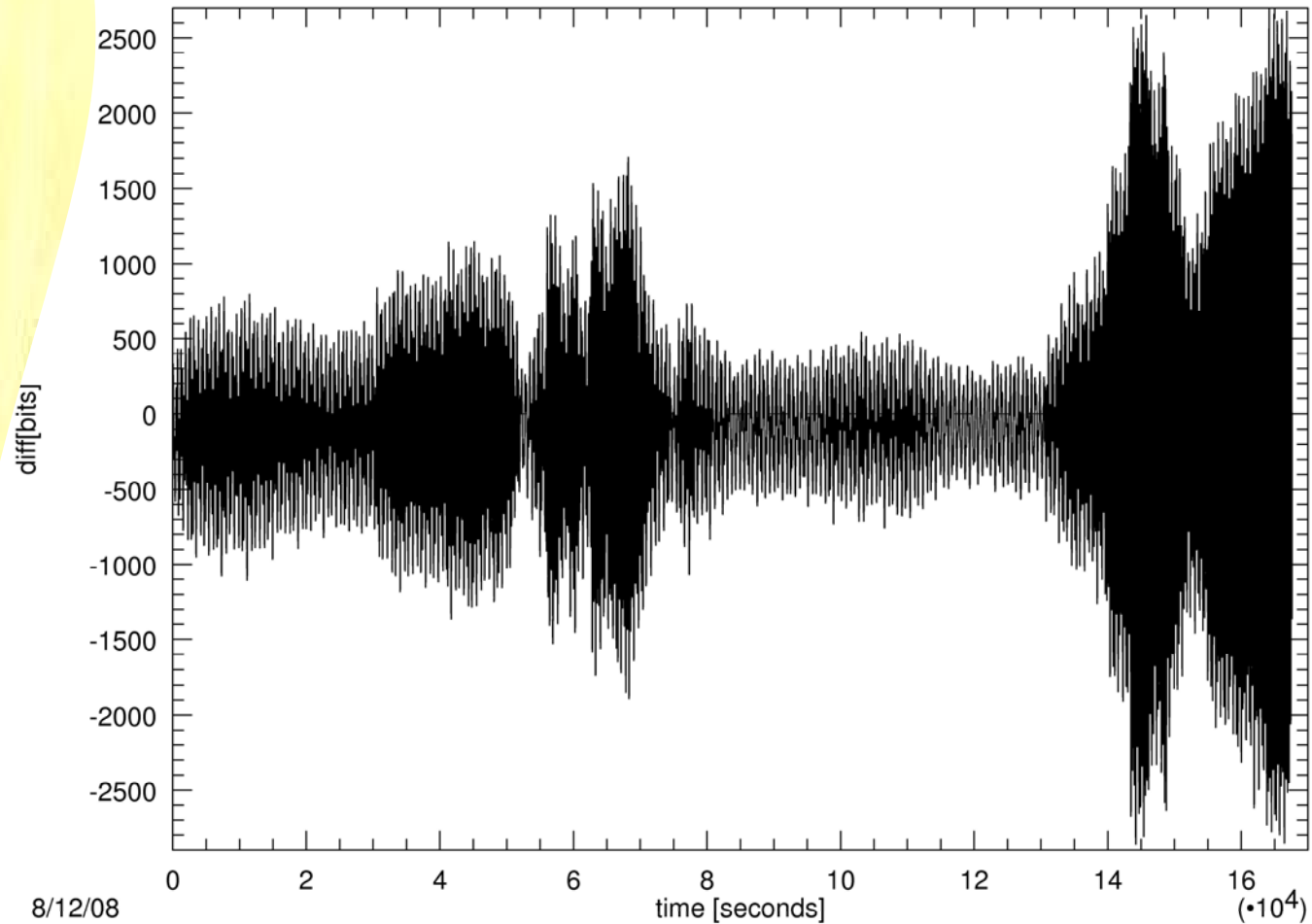
Compared with 2006 data

## Puget Sound Tides Function

$$\begin{aligned} h(t) = & 1.405 \sin [(2\pi (1.00274) x + 2.98127)] + 0.548 \sin [(2\pi (0.92954) x + 5.60001)] \\ & + -0.978 \sin [(2\pi (1.93227) x + 0.61891)] + 0.282 \sin [(2\pi (2) x + 0.875285)] \\ & + 0.138 \sin [(2\pi (1.89598) x + 1.90958)] + 0.709 \sin [(2\pi (0.99726) x + 1.52675)] \\ & + 0.022 \sin [(2\pi (3.86455) x + 2.41113)] + 1.96 \end{aligned}$$

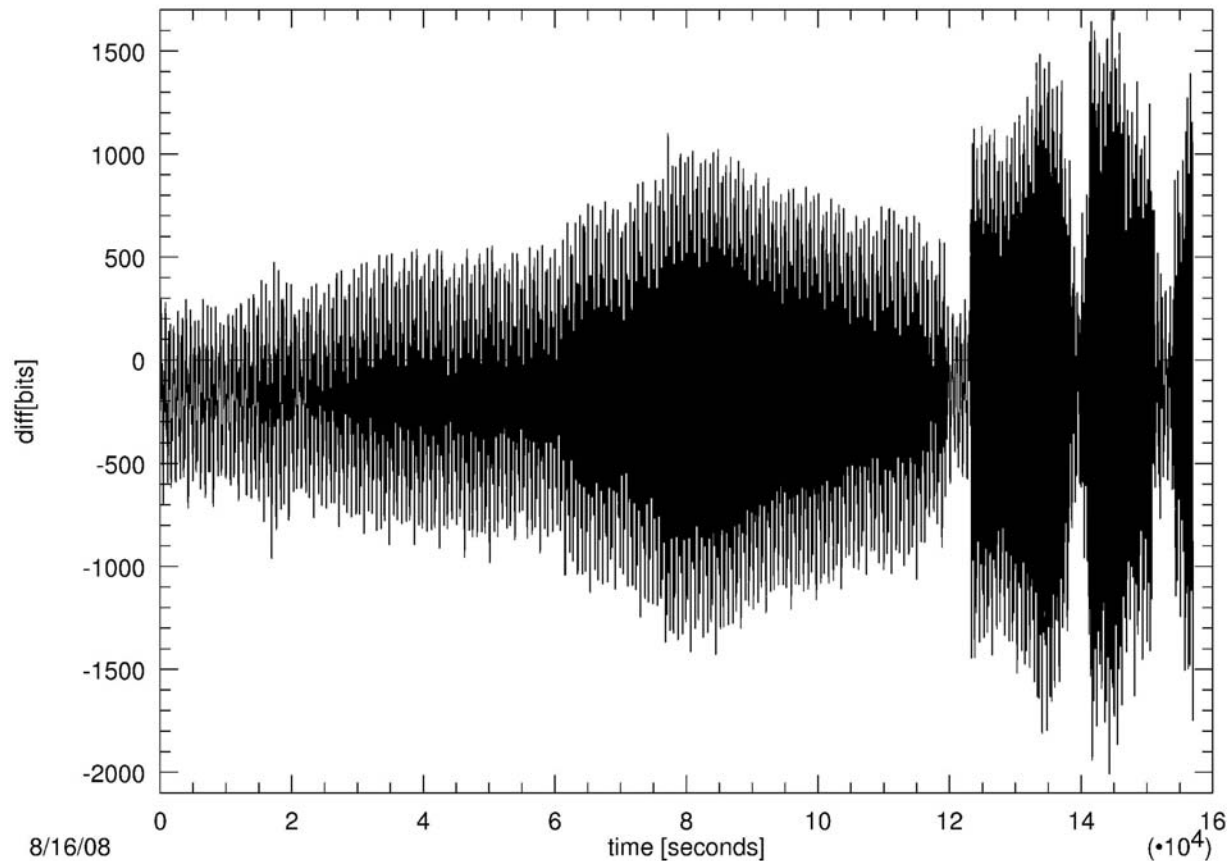
# Sample Pendulum Run

RPLOT: run9932 Q22data



*Over the course of 2 days: 8/12/08 – 8/14/08*

# Daily Fluctuations



*Data taken from Saturday, 8/16 through Monday, 8/18*

**Program detects daily modulation in theta:**

**Direction 1:  $-91.32 \pm 15.92$  nrad**

**Direction 2:  $84.48 \pm 15.92$  nrad**

# Daily Fluctuations

## Weekday Amplitude:

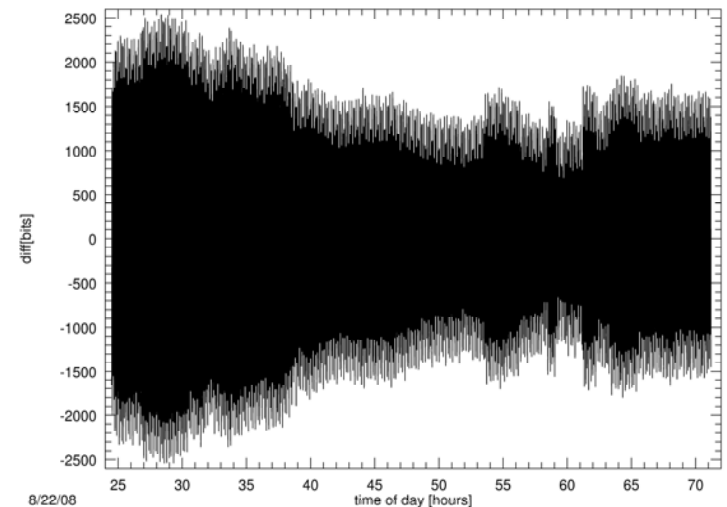
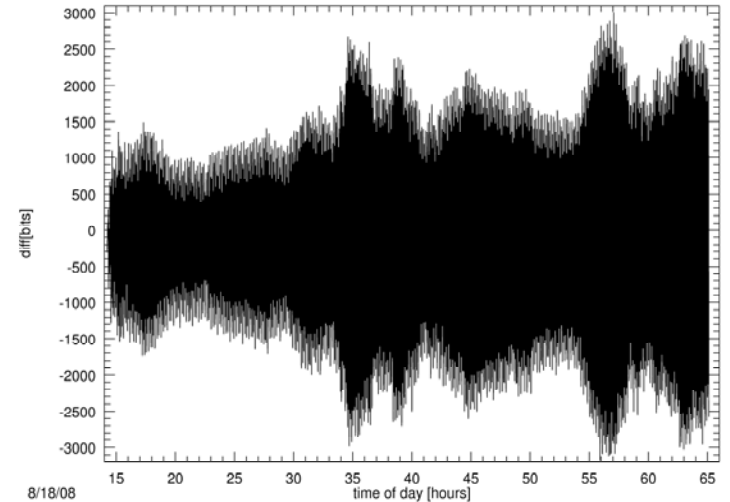
Direction 1 =  $146 \pm 44$  nrad

Direction 2 =  $125 \pm 44$  nrad

## Weekend Amplitude:

Direction 1 =  $6.3 \pm 3.2$  nrad

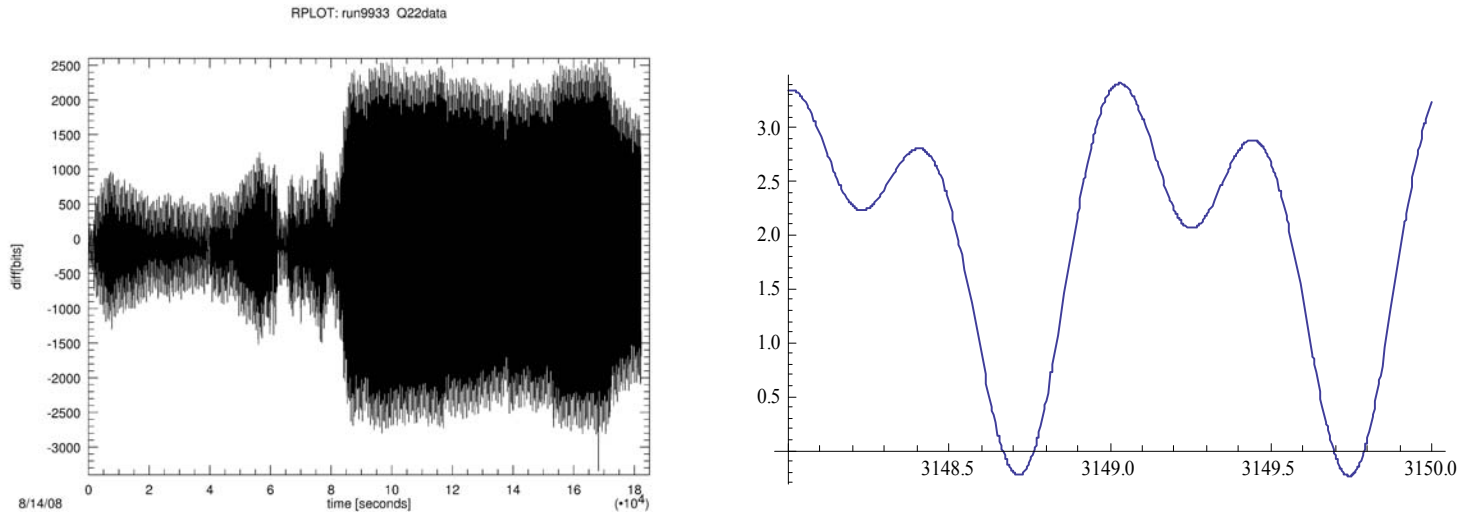
Direction 2 =  $41 \pm 3.2$  nrad





# Tidal Fluctuations

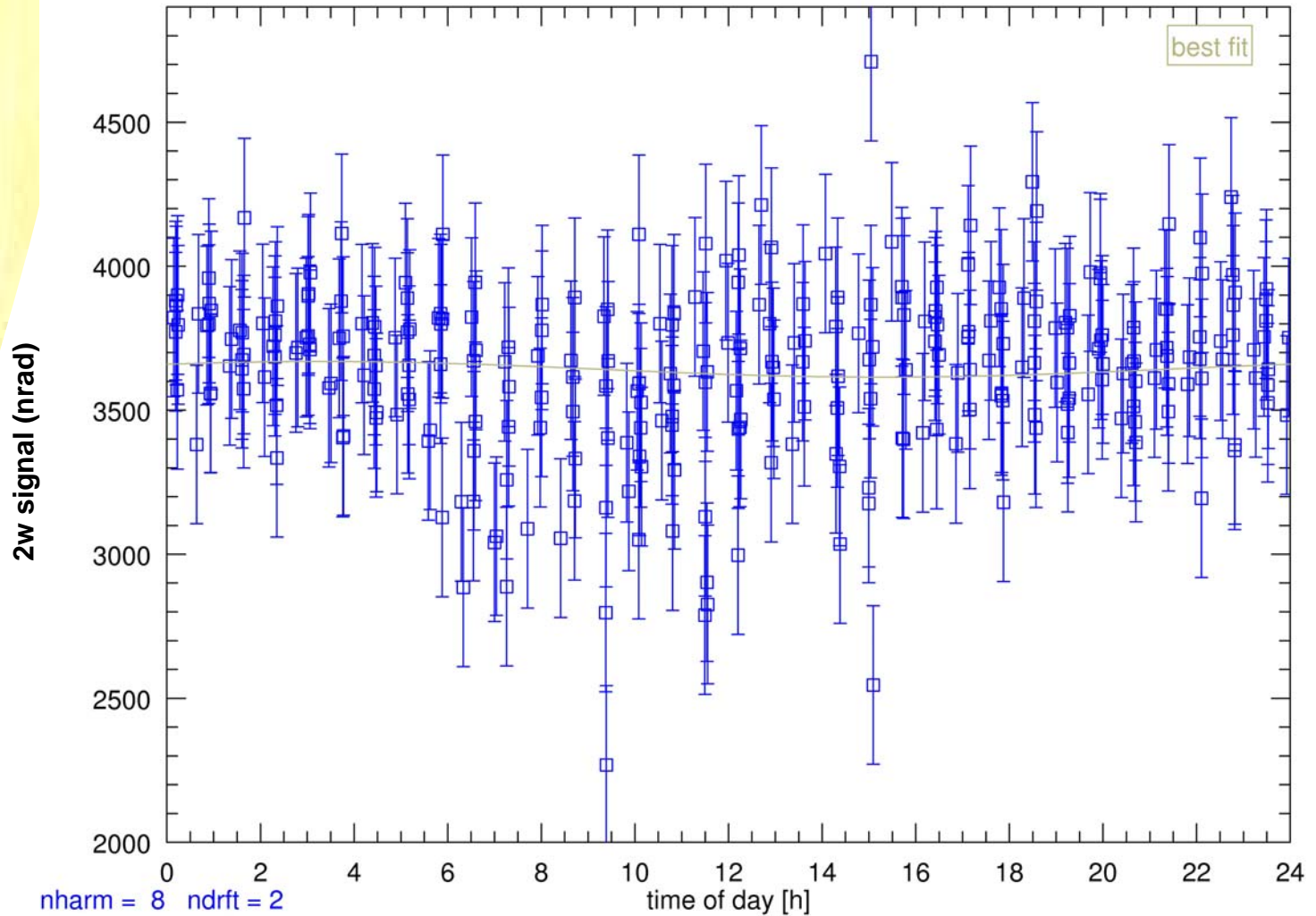
- Pendulum movement tracked for 10 days
- Program used to compare Pendulum Run data to Puget Sound Tidal Function



Modulation in theta due to tidal forces:

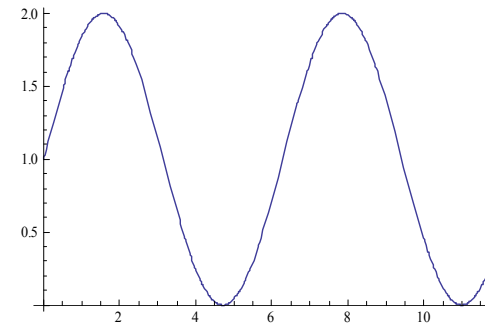
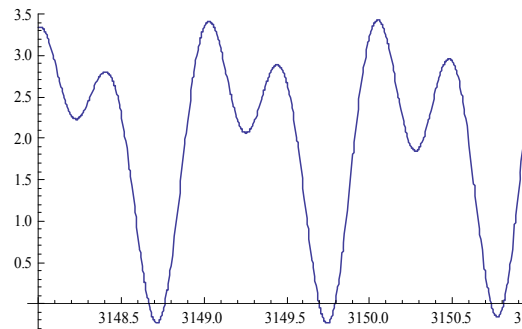
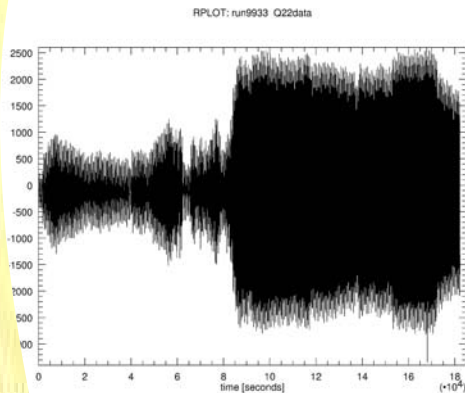
$$34 \pm 14 \text{ nrad}$$

# Solar Fluctuations



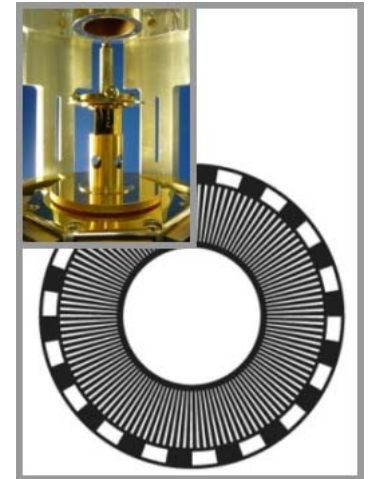
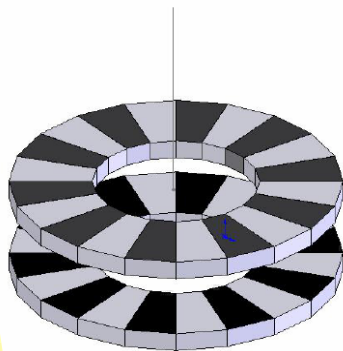
# Conclusions

- Strong correlation between signal and lab traffic
- Evidence of tidal influence
- No noticeable solar interference



# What's Left?

- Magnetize and test Spin Pendulum
- Lunar interference for q2 Pendulum
- More conclusive tidal evidence
- Apply q2 Pendulum results to other Eöt-Wash pendulums



# Thanks

*Special thanks to past and present members of the CENPA Gravity Group, especially*

Blayne Heckel

Eric Adelberger

William Terrano

Todd Wagner

Ted Cook

Frank Fleischer

Claire Cramer

Yue Su

*Thanks also to Warren Buck, Wick Haxton, and the NSF for a wonderful summer!*

# Appendix

## Spin-Coupled Potentials

$$V_{md}(r) = \frac{g_p^e g_s^N}{\hbar c} \frac{\hbar^2}{8\pi m_e} \frac{(\boldsymbol{\sigma}_e \cdot \hat{\mathbf{r}})}{m_e} \left( \frac{1}{r\lambda} + \frac{1}{r^2} \right) e^{-r/\lambda}$$

$$V_{dd}(r) = \frac{g_p^e g_p^e}{4\pi \hbar c} \frac{\hbar^3}{4m_e^2 c} \left[ (\boldsymbol{\sigma}_1 \cdot \boldsymbol{\sigma}_2) \left( \frac{1}{\lambda r^2} + \frac{1}{r^3} \right) - (\boldsymbol{\sigma}_1 \cdot \hat{\mathbf{r}})(\boldsymbol{\sigma}_2 \cdot \hat{\mathbf{r}}) \left( \frac{1}{\lambda^2 r} + \frac{3}{\lambda r^2} + \frac{3}{r^3} \right) \right] e^{-r/\lambda}$$

## Spherical Harmonics

$$Y_2^1(\theta, \varphi) = \frac{-1}{2} \sqrt{\frac{15}{2\pi}} \sin \theta \cos \theta e^{i\varphi}$$

$$Y_2^2(\theta, \varphi) = \frac{1}{4} \sqrt{\frac{15}{2\pi}} \sin^2 \theta e^{2i\varphi}$$