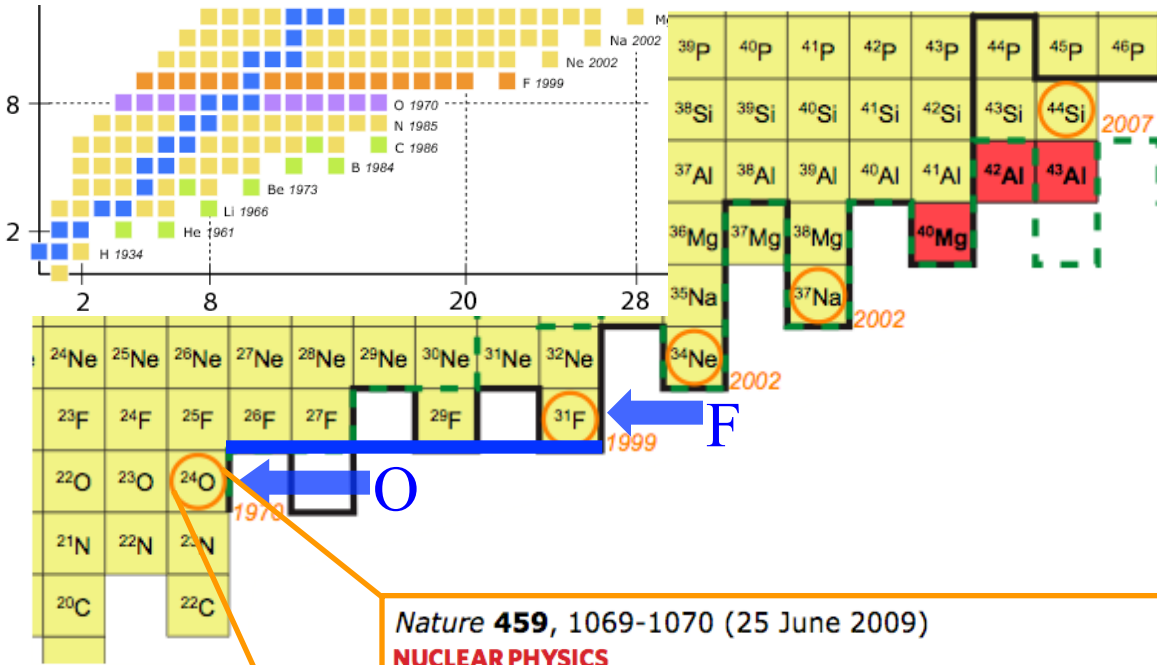


The oxygen anomaly



Nature **459**, 1069-1070 (25 June 2009)

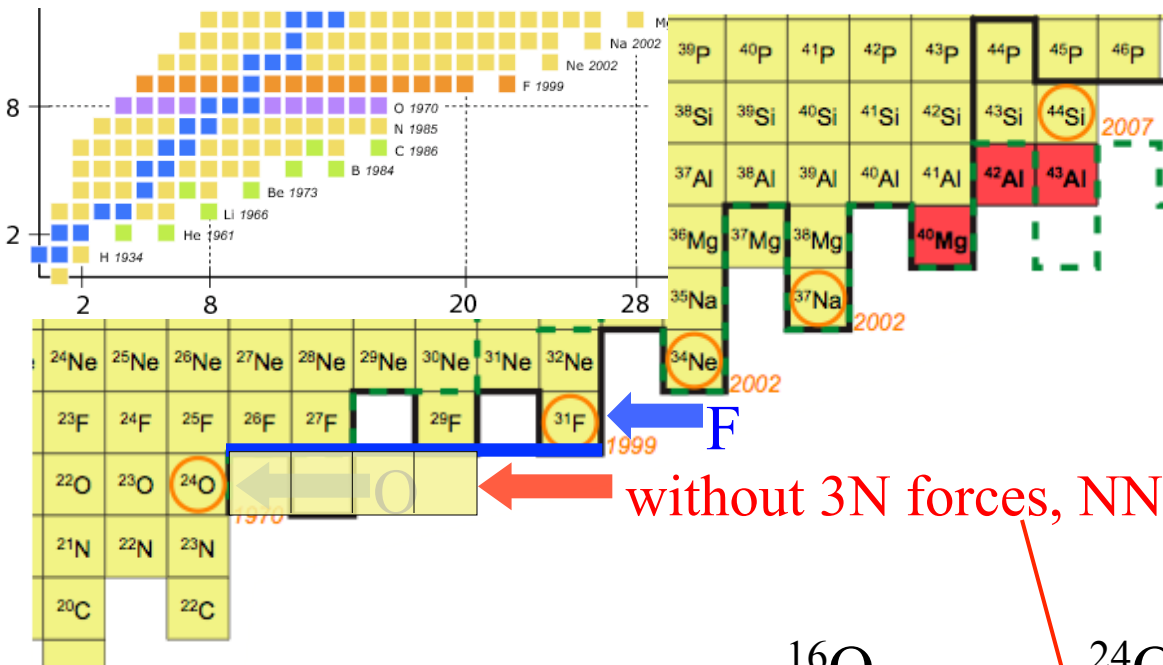
NUCLEAR PHYSICS

Unexpected doubly magic nucleus

Robert V. F. Janssens

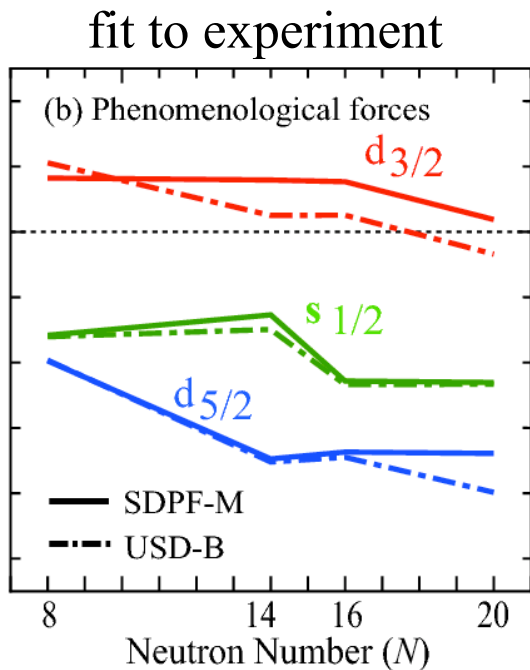
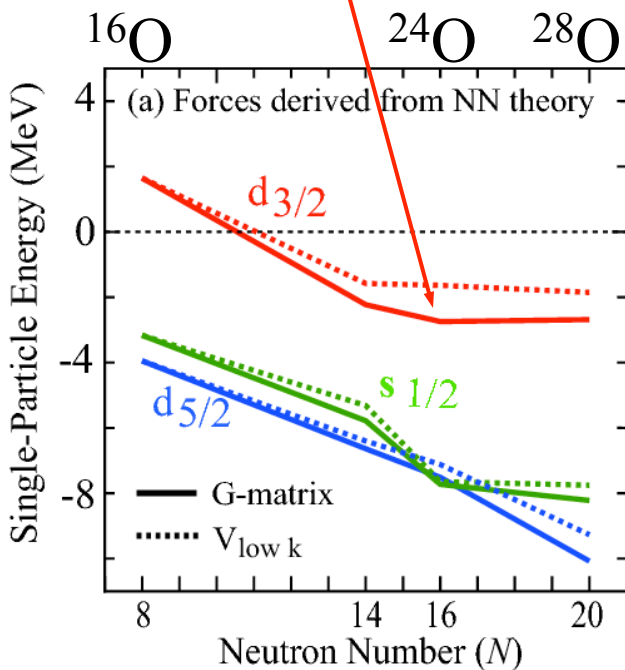
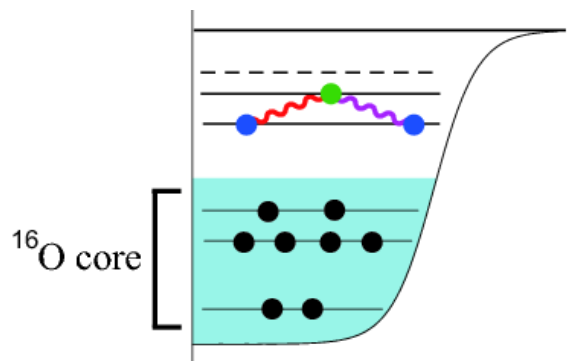
Nuclei with a 'magic' number of both protons and neutrons, dubbed doubly magic, are particularly stable. The oxygen isotope ^{24}O has been found to be one such nucleus — yet it lies just at the limit of stability.

The oxygen anomaly - not reproduced without 3N forces



without 3N forces, NN interactions too attractive

many-body theory based on two-nucleon forces:
drip-line incorrect at ^{28}O



The shell model - impact of 3N forces

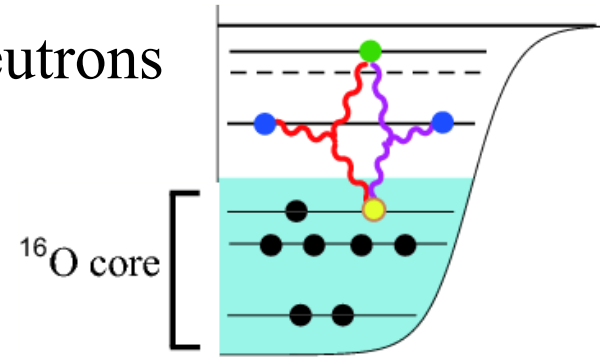
include 'normal-ordered' 2-body part of 3N forces (enhanced by core A)

leads to repulsive interactions between valence neutrons

contributions from residual three valence-nucleon interactions suppressed by $E_{\text{ex}}/E_{\text{F}} \sim N_{\text{valence}}/N_{\text{core}}$

Friman, AS (2011)

residual 3N amplified in most neutron-rich nuclei



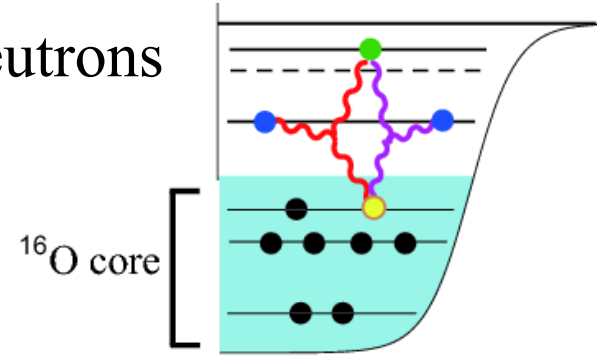
Oxygen isotopes - impact of 3N forces

include ‘normal-ordered’ 2-body part of 3N forces (enhanced by core A)

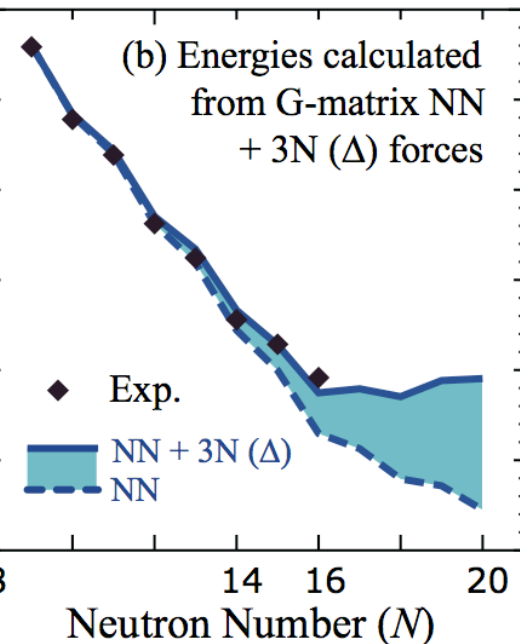
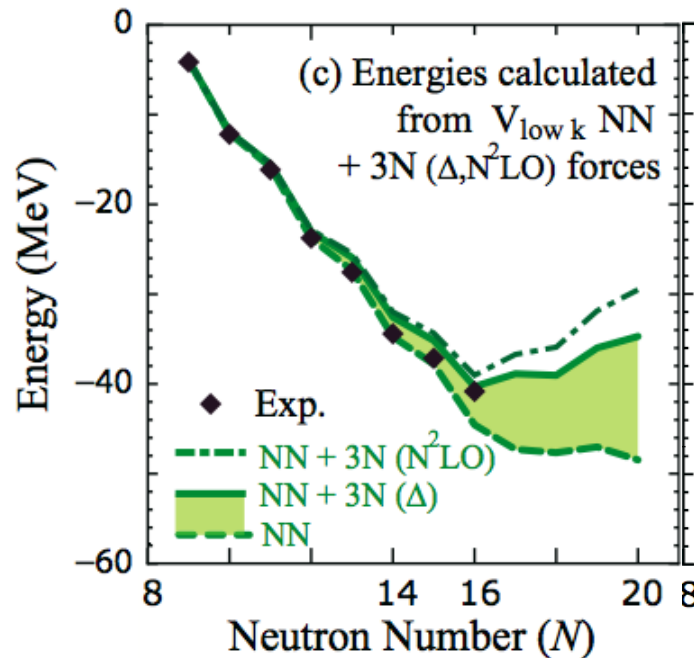
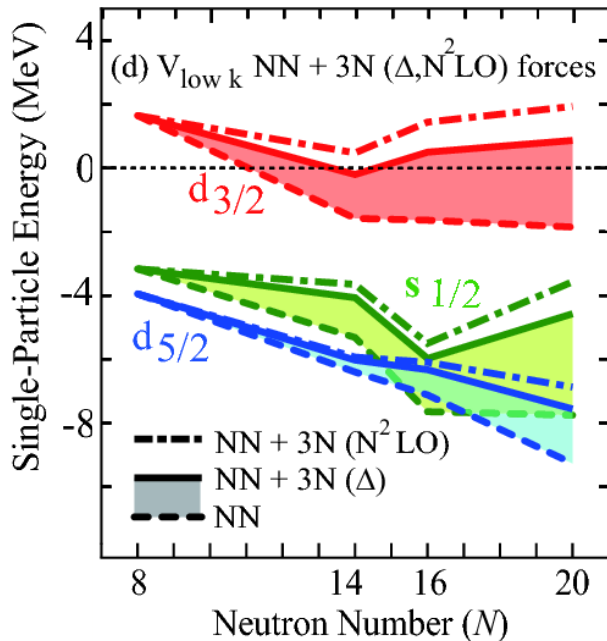
leads to repulsive interactions between valence neutrons

contributions from residual three valence-nucleon interactions suppressed by $E_{\text{ex}}/E_{\text{F}} \sim N_{\text{valence}}/N_{\text{core}}$

Friman, AS (2011)



$d_{3/2}$ orbital remains unbound from ^{16}O to ^{28}O



microscopic explanation of the oxygen anomaly Otsuka et al. (2010)

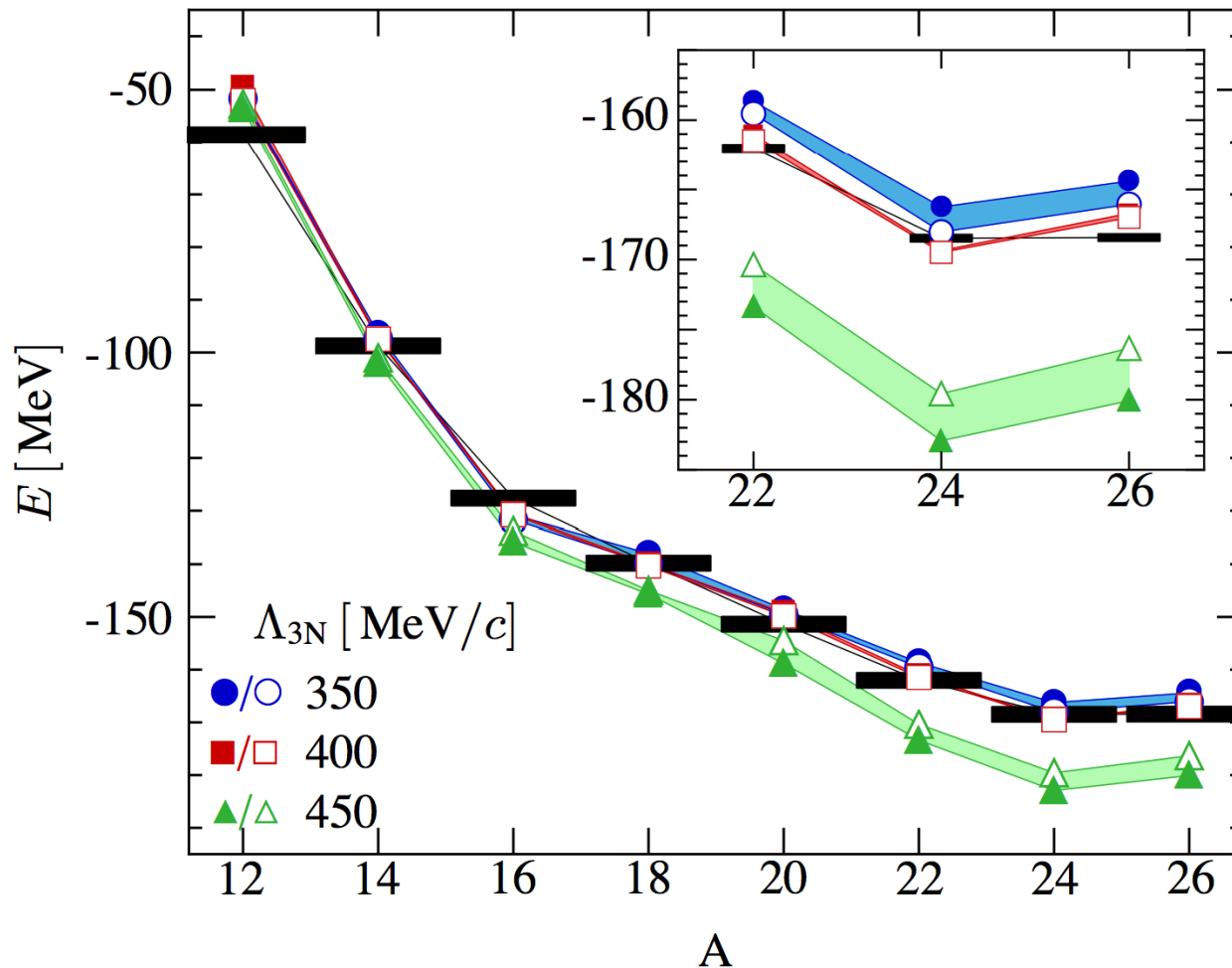
New ab-initio methods extend reach

impact of 3N forces confirmed in large-space calculations:

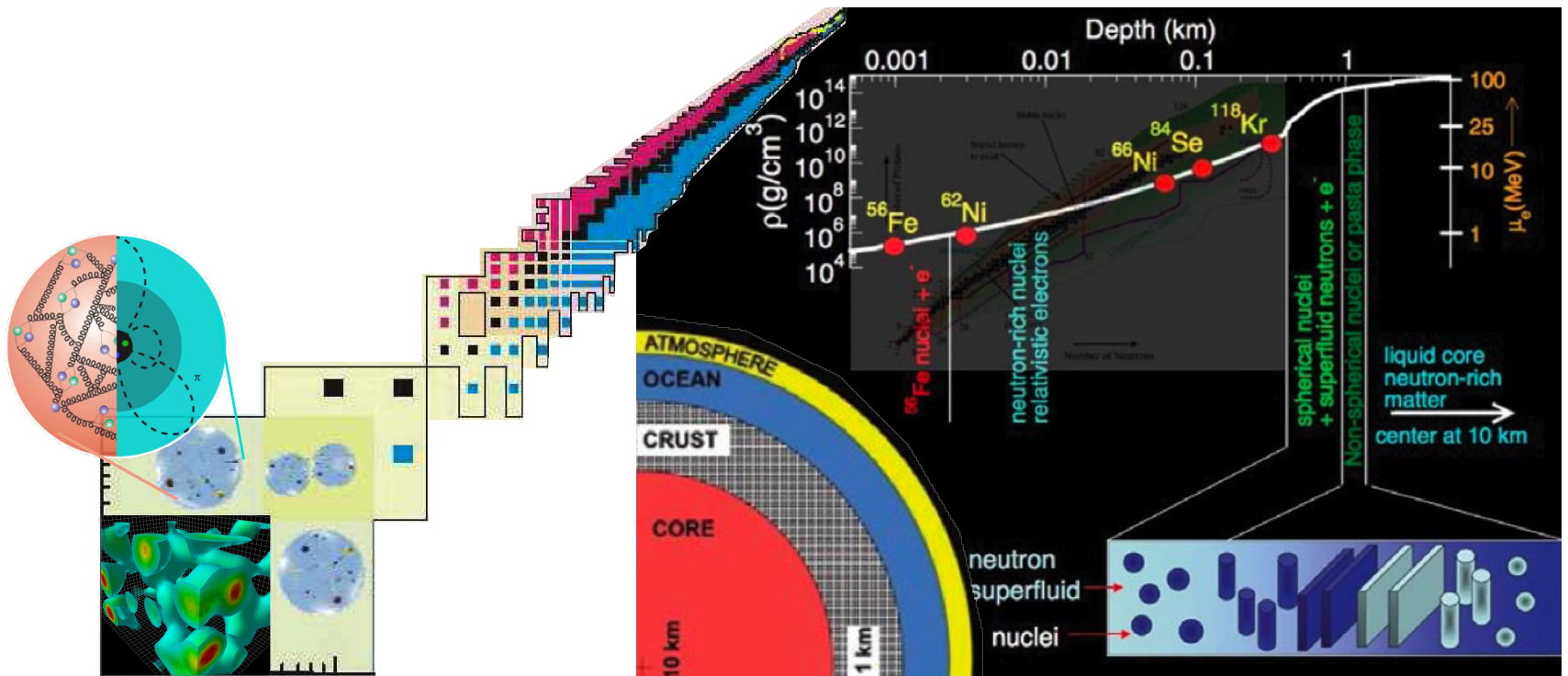
Coupled Cluster theory with phenomenological 3N forces [Hagen et al. \(2012\)](#)

In-Medium Similarity RG based on chiral NN+3N [Hergert et al. \(2013\)](#)

Green's function methods based on chiral NN+3N [Cipollone et al. \(2013\)](#)



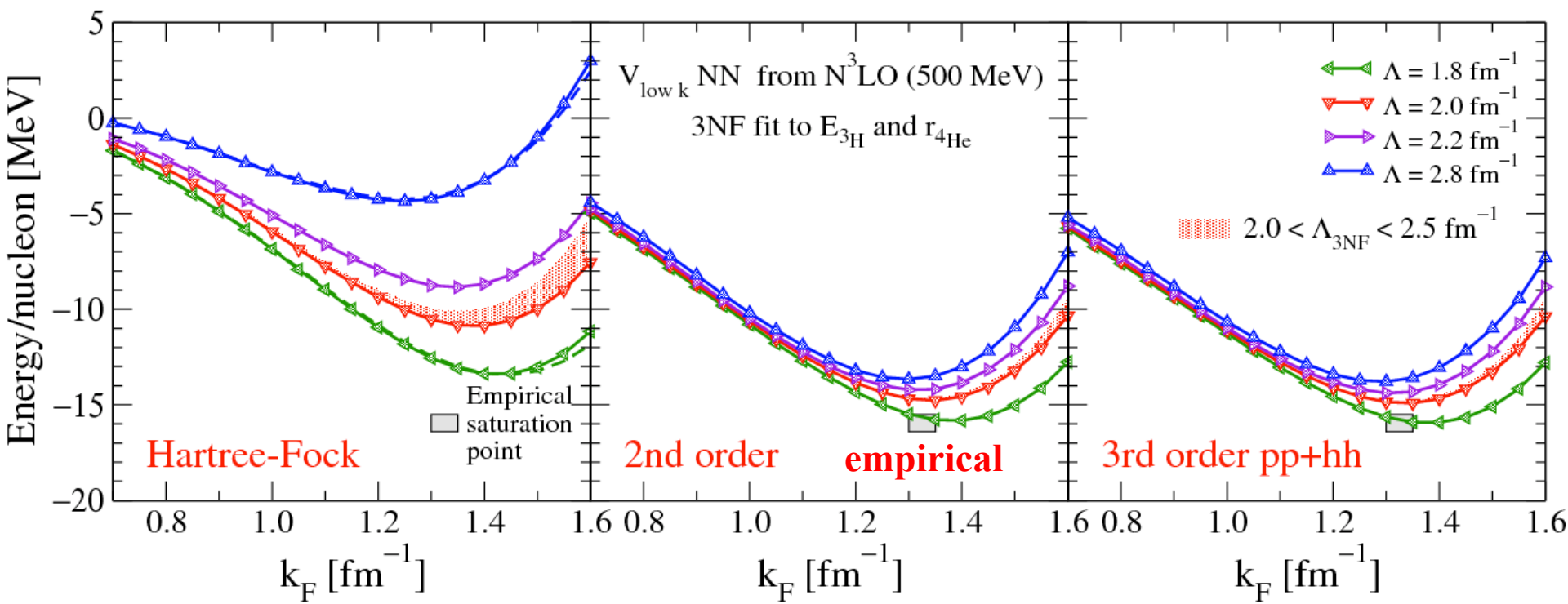
Neutron matter and neutron stars



Impact of 3N forces on nuclear matter

chiral 3N forces fit to light nuclei
predict nuclear matter saturation
with theoretical uncertainties

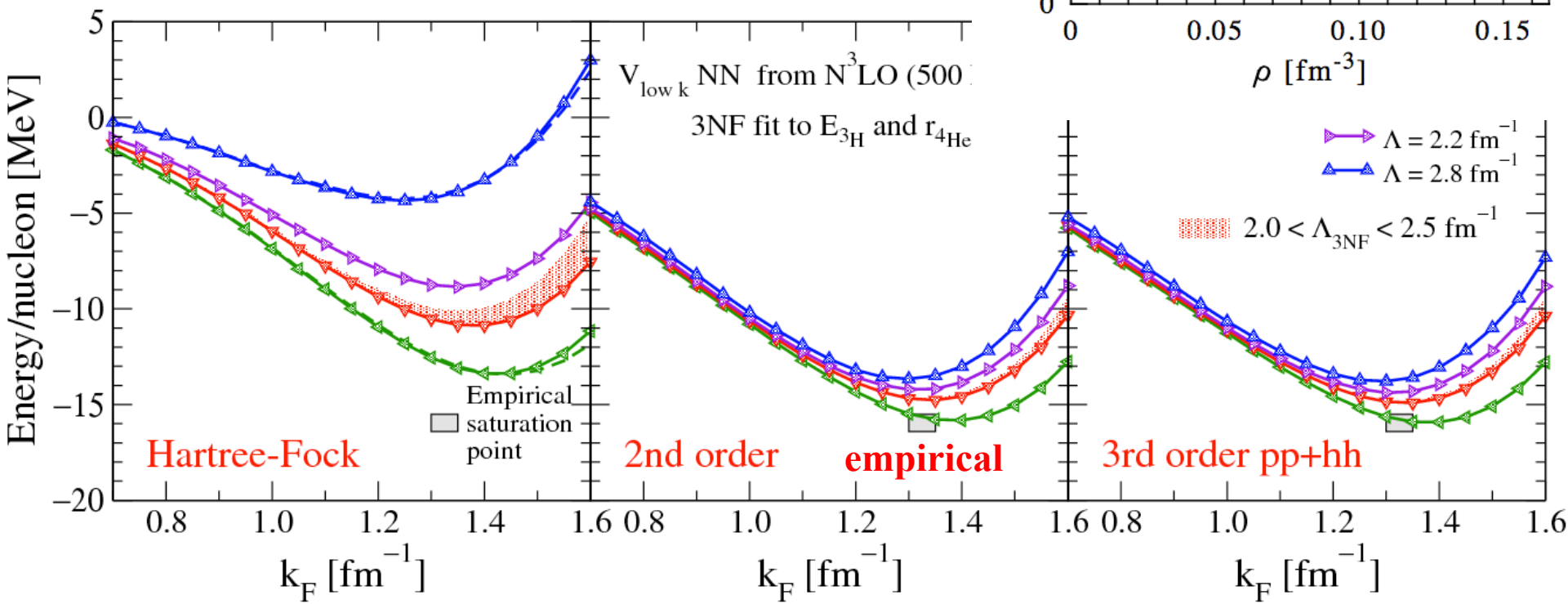
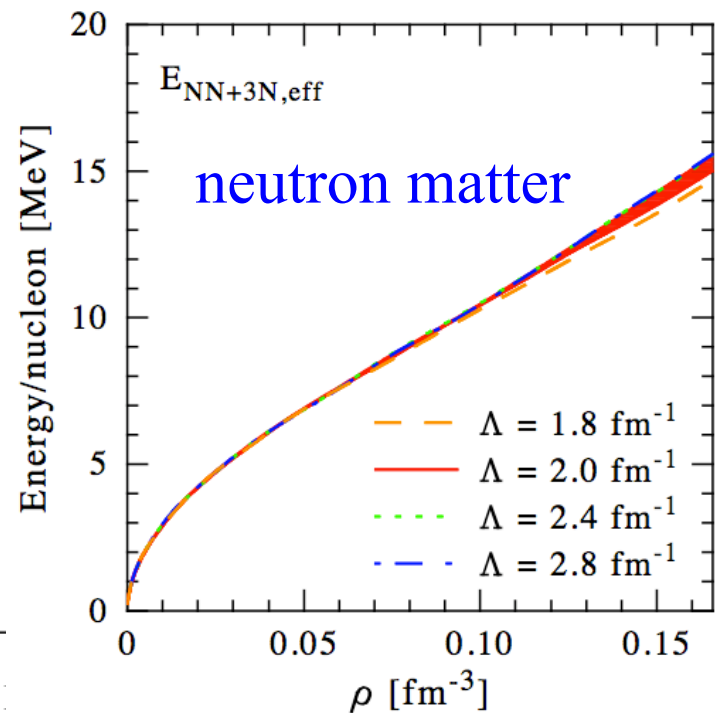
Bogner et al. (2005), Hebeler et al. (2011)



Impact of 3N forces on neutron matter

neutron matter is simpler system,
 tensor forces and 3N forces weaker

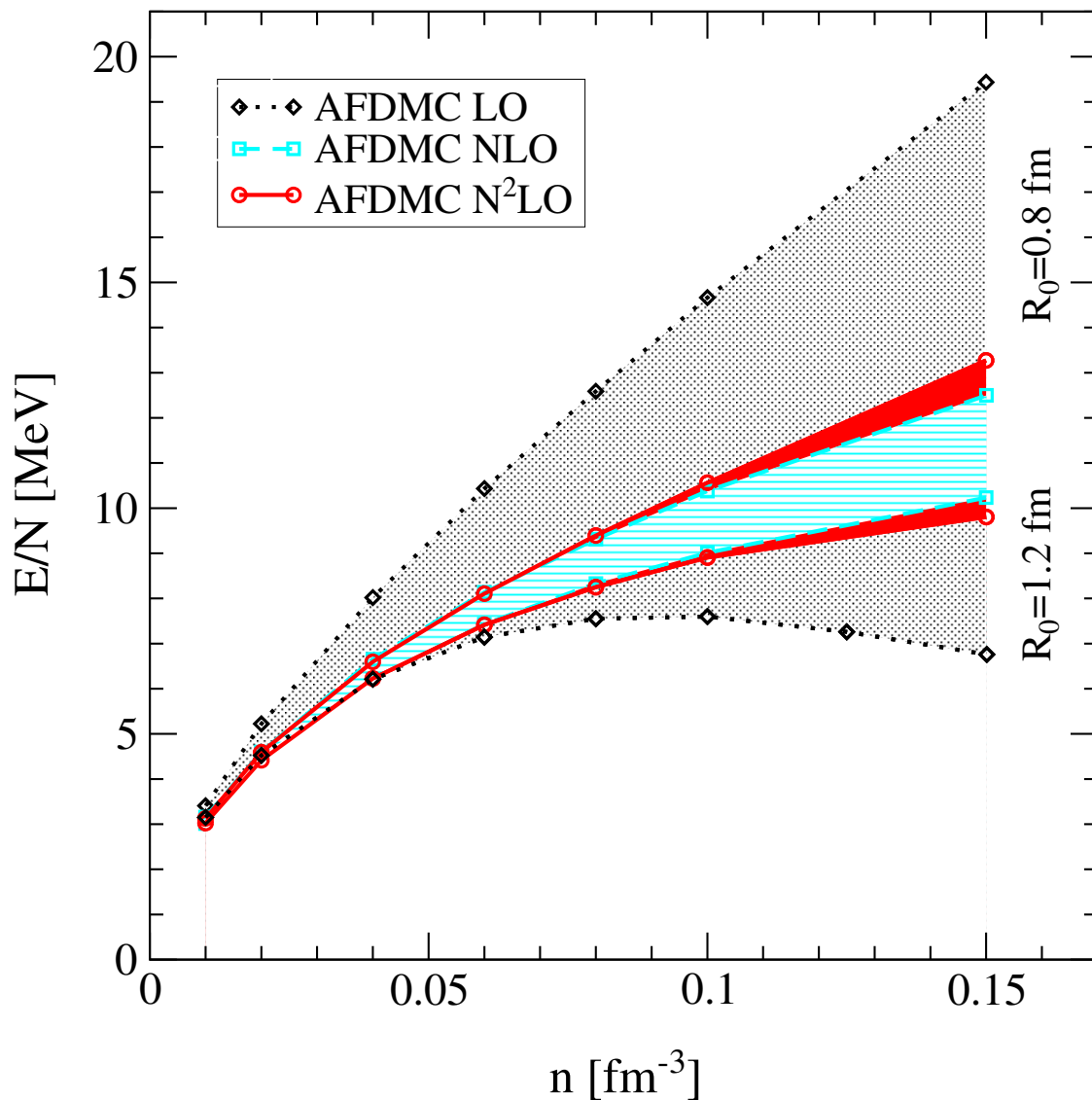
Hebeler, AS (2010)



AFDMC results for neutron matter

Gezerlis et al., arXiv:1303.6243, PRL in press.

order-by-order convergence up to saturation density (NN only)

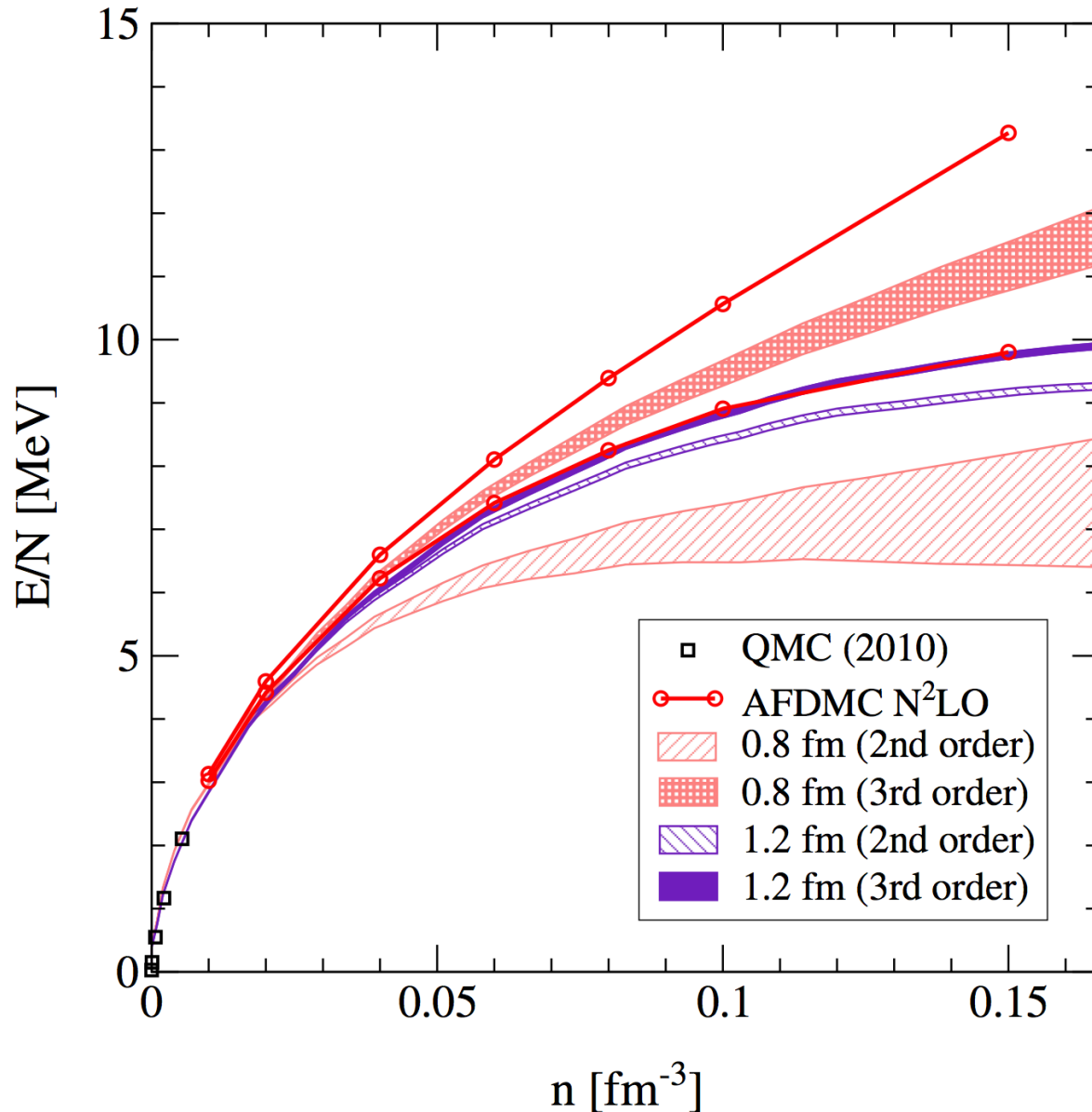


bands similar to
phase shift bands

N^2 LO \sim NLO
due to missing
higher-order contacts

Comparison to perturbative calculations at N²LO

Hartree-Fock +2nd order +3rd order (pp+hh), same as for N³LO calcs.



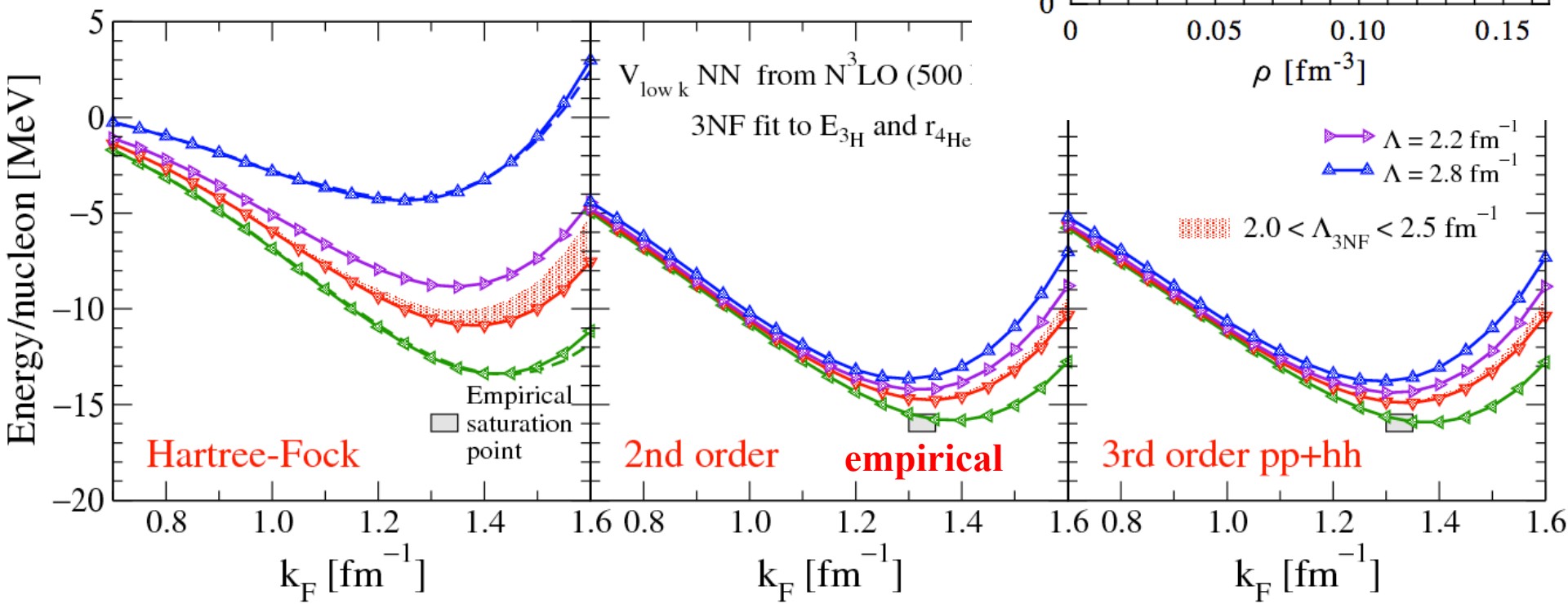
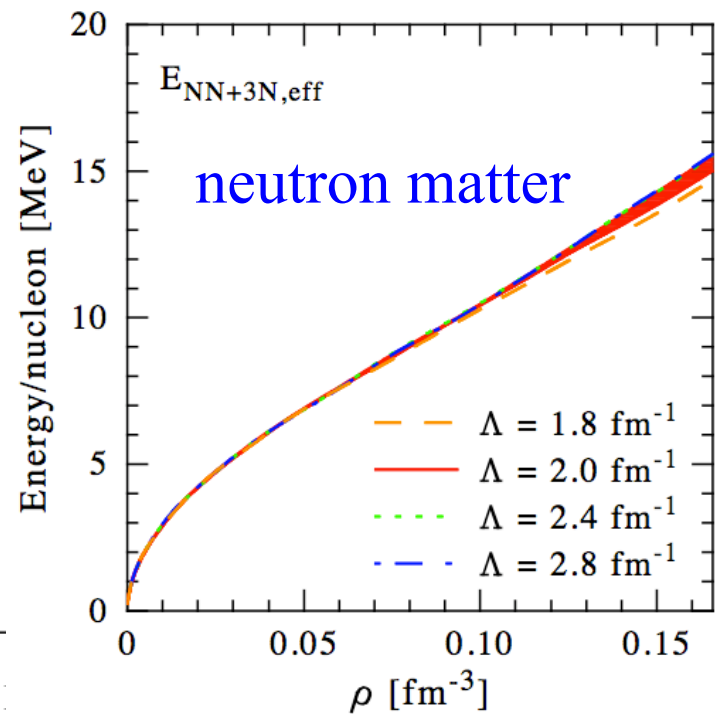
band at each order from
free to HF spectrum

low cutoffs (400 MeV)
3rd order corr. small,
excellent agreement
with AFDMC

Impact of 3N forces on neutron matter

neutron matter is simpler system,
only long-range parts of 3N forces
contribute (c_1 and c_3)

Hebeler, AS (2010)



Chiral effective field theory and many-body forces

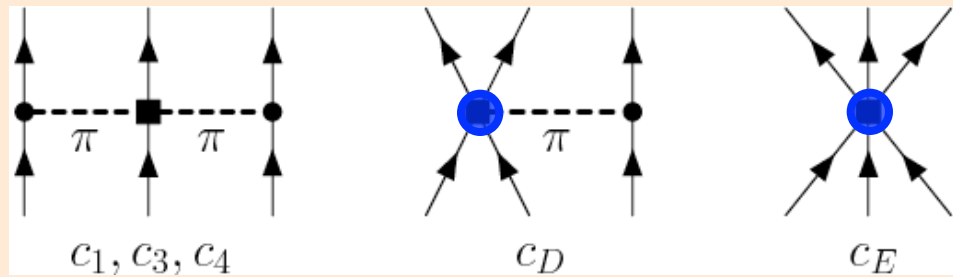
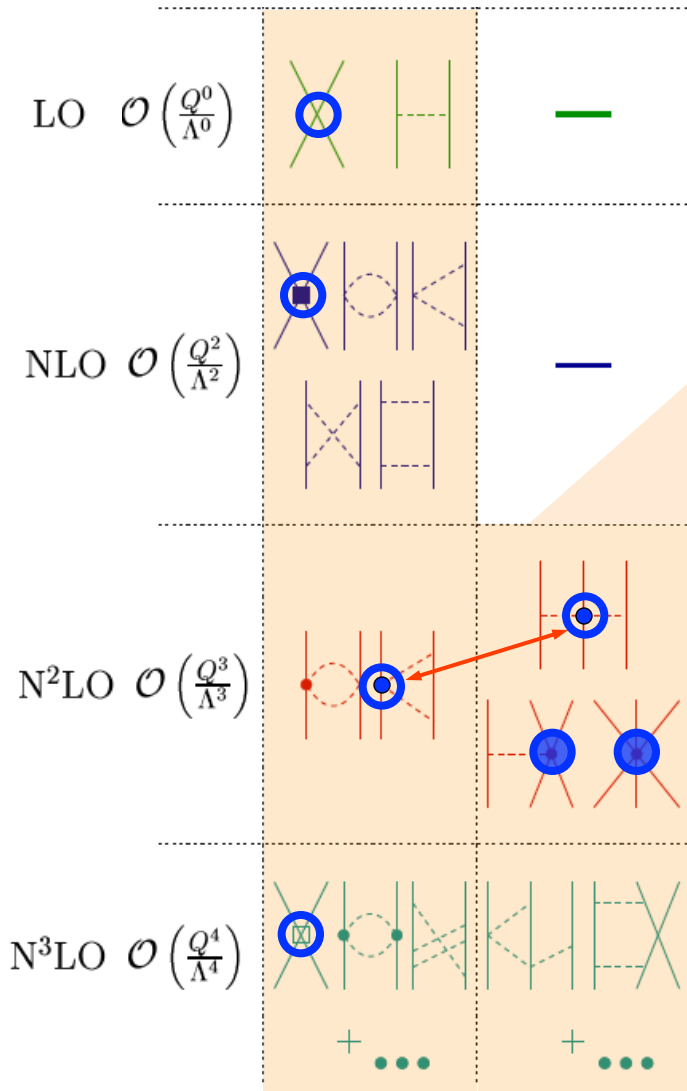
Separation of scales: low momenta $\frac{1}{\lambda} = Q \ll \Lambda_b$ breakdown scale ~ 500 MeV

NN

3N

consistent NN-3N interactions

3N,4N: only 2 new couplings to N³LO



c_i from π N and NN [Meissner et al. \(2007\)](#)

$$c_1 = -0.9_{-0.5}^{+0.2}, \quad c_3 = -4.7_{-1.0}^{+1.2}, \quad c_4 = 3.5_{-0.2}^{+0.5}$$

single- Δ : $c_1=0, c_3=-c_4/2=-3 \text{ GeV}^{-1}$

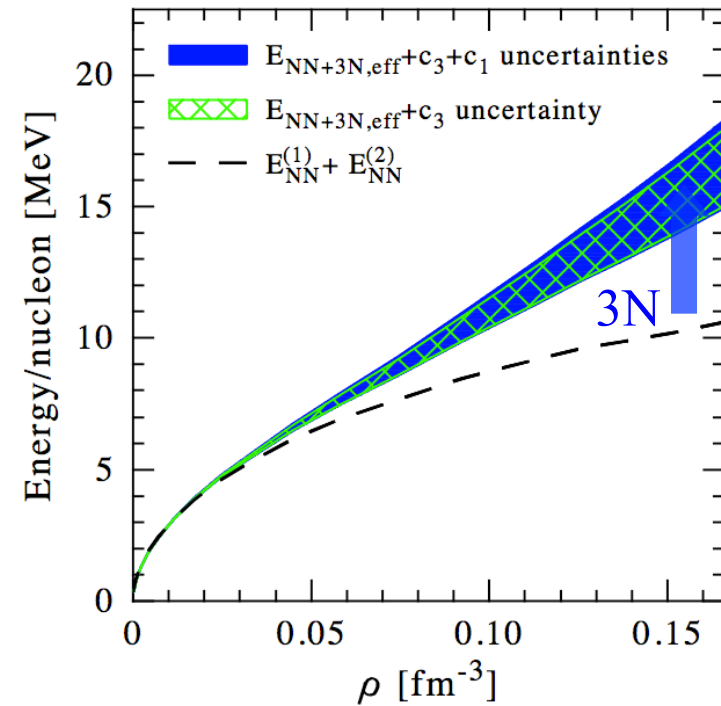
c_D, c_E fit to ${}^3\text{H}, {}^4\text{He}$ properties only

Impact of 3N forces on neutron matter

neutron matter uncertainties

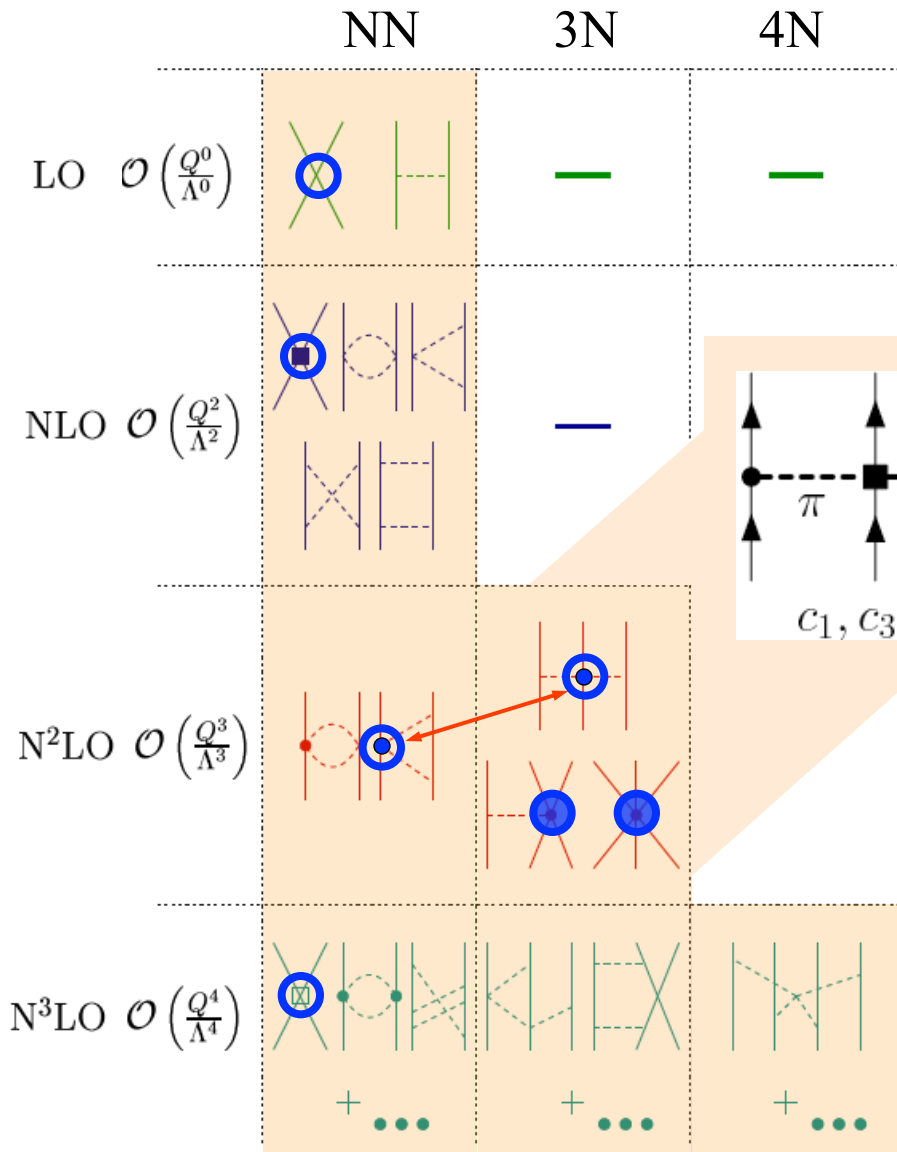
dominated by 3N forces (c_3 coupling)

Hebeler, AS (2010)



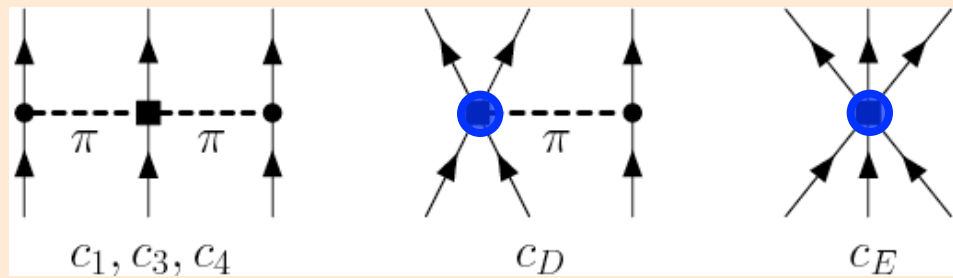
Chiral effective field theory for nuclear forces

Separation of scales: low momenta $\frac{1}{\lambda} = Q \ll \Lambda_b$ breakdown scale ~ 500 MeV



c_D, c_E don't contribute for **neutrons** because of Pauli principle and pion coupling to spin, also for c_4

Hebeler, AS (2010)



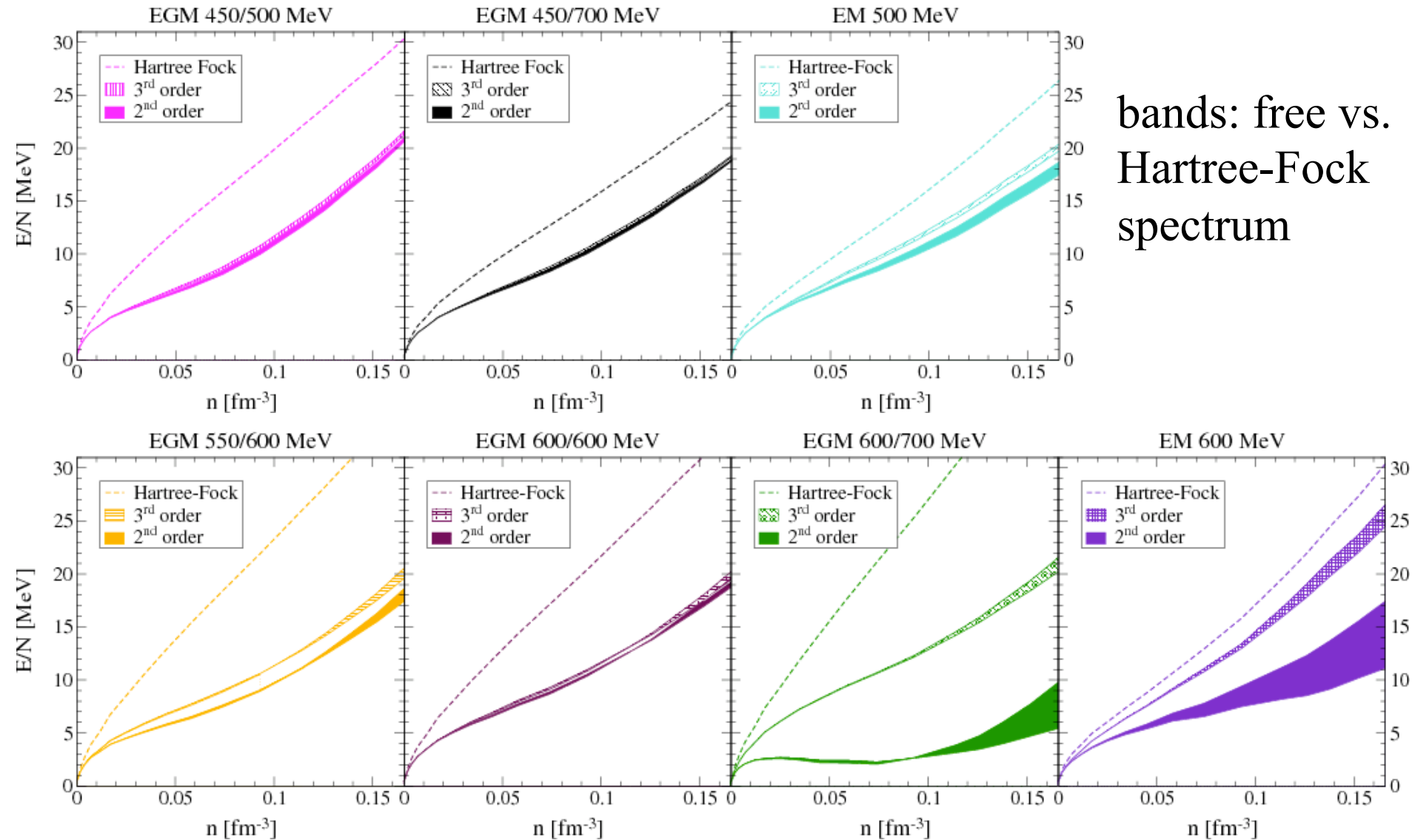
all 3- and 4-neutron forces are predicted to N³LO!

study 3N and 4N in neutron matter

Tews, Krüger, Hebeler, AS (2013)

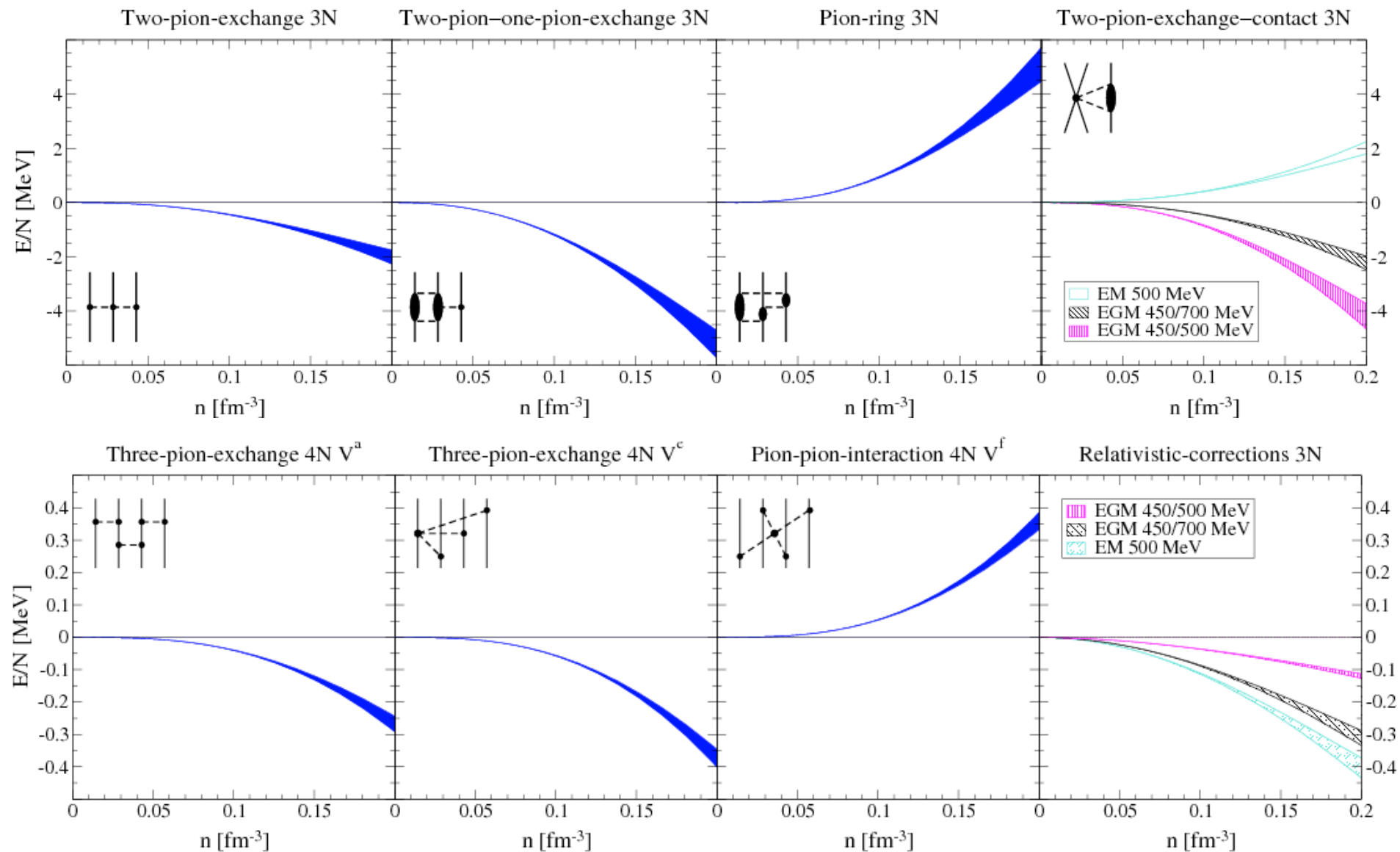
Neutron matter from chiral EFT interactions

direct calculations without RG/SRG evolution, 3N to N²LO only



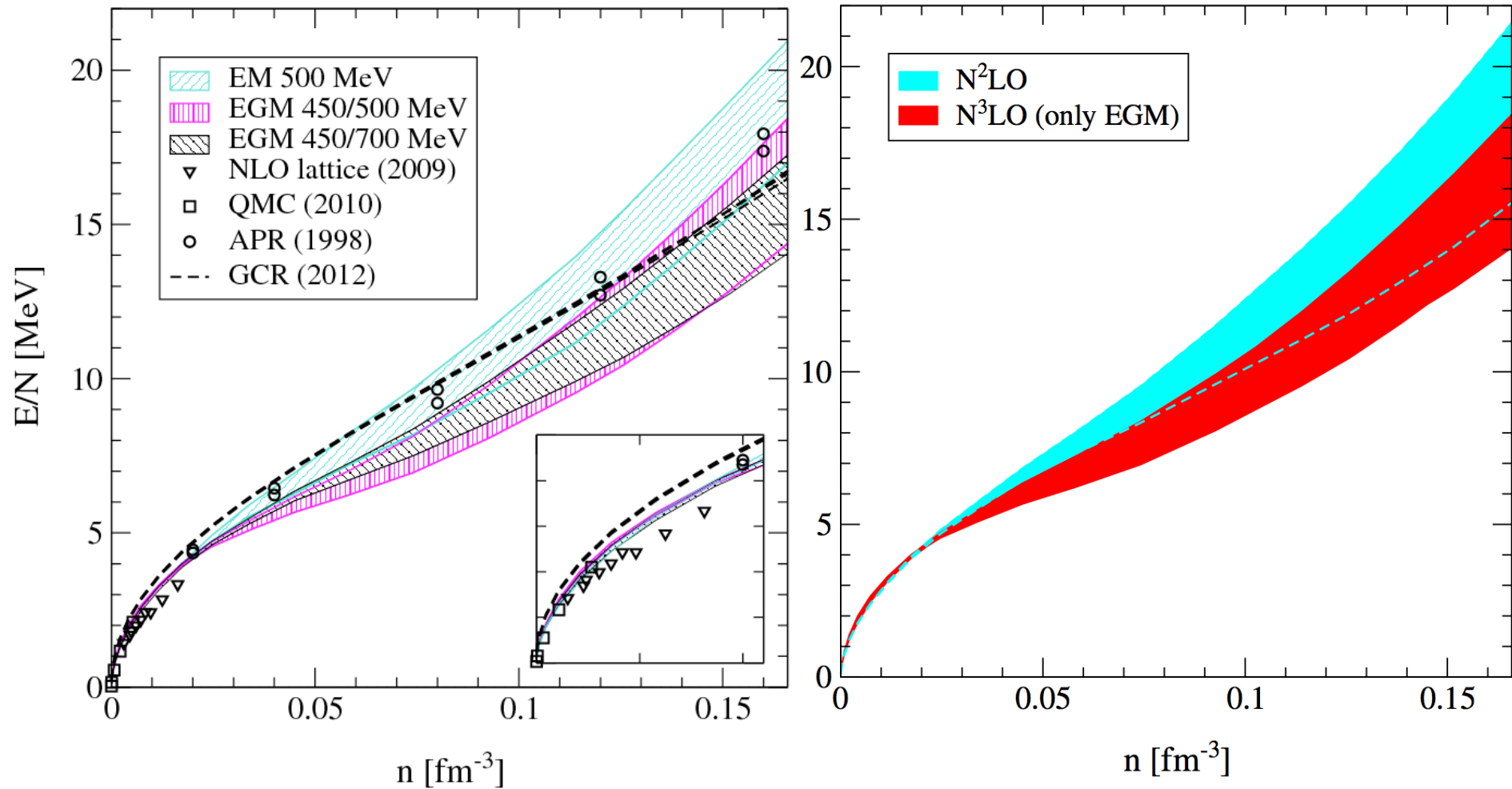
$N^3\text{LO}$ 3N and 4N interactions in neutron matter

evaluated at Hartree-Fock level



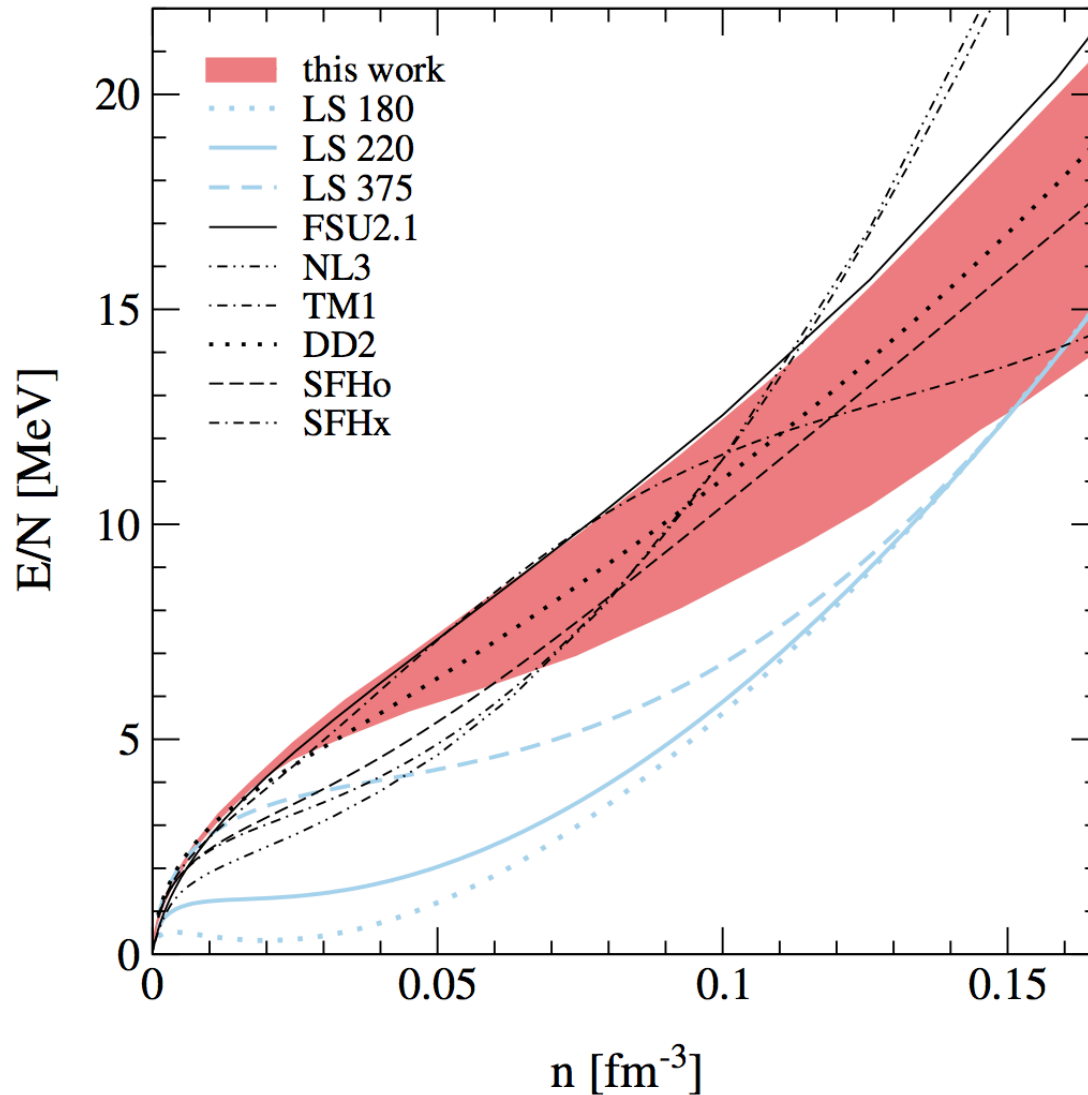
Complete N³LO calculation of neutron matter

first complete N³LO result, Hartree-Fock +2nd order +3rd order (pp+hh)
includes uncertainties from NN, 3N (dominates), 4N



Comparisons to equations of state in astrophysics

many equations of state used in supernova simulations not consistent with neutron matter results

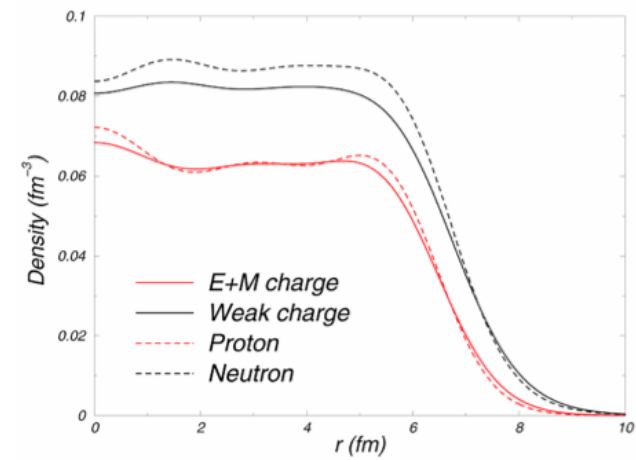


Neutron skin of ^{208}Pb

probes neutron matter energy/pressure,
neutron matter band predicts

neutron skin of ^{208}Pb : 0.17 ± 0.03 fm ($\pm 18\%$!)

Hebeler et al. (2010)

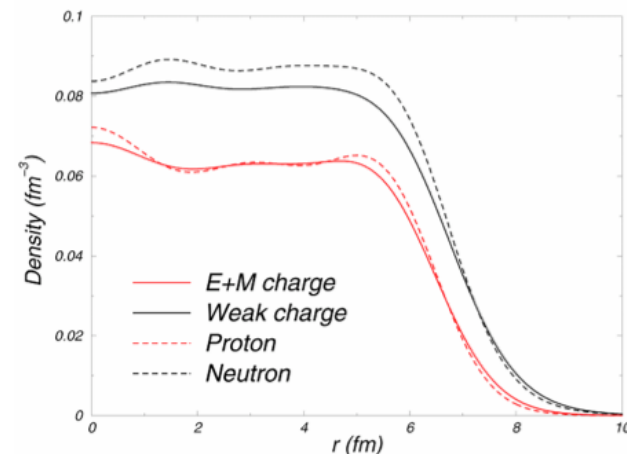


Neutron skin of ^{208}Pb

probes neutron matter energy/pressure,
neutron matter band predicts

neutron skin of ^{208}Pb : 0.17 ± 0.03 fm ($\pm 18\%$!)

Hebeler et al. (2010)



in excellent agreement with extraction from complete E1 response

$0.156 + 0.025 - 0.021$ fm

PRL 107, 062502 (2011)

PHYSICAL REVIEW LETTERS

week ending
5 AUGUST 2011

Complete Electric Dipole Response and the Neutron Skin in ^{208}Pb

A benchmark experiment on ^{208}Pb shows that polarized proton inelastic scattering at very forward angles including 0° is a powerful tool for high-resolution studies of electric dipole (E1) and spin magnetic dipole (M1) modes in nuclei over a broad excitation energy range to test up-to-date nuclear models. The extracted E1 polarizability leads to a neutron skin thickness $r_{\text{skin}} = 0.156^{+0.025}_{-0.021}$ fm in ^{208}Pb derived within

PREX: neutron skin from parity-violating electron-scattering at JLAB

electron exchanges Z-boson, couples preferentially to neutrons

goal II: ± 0.06 fm

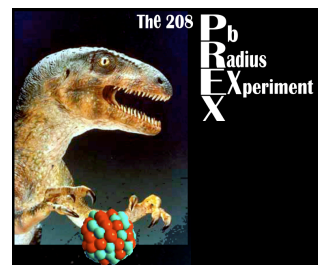
PRL 108, 112502 (2012)

PHYSICAL REVIEW LETTERS

week ending
16 MARCH 2012

Measurement of the Neutron Radius of ^{208}Pb through Parity Violation in Electron Scattering

We report the first measurement of the parity-violating asymmetry A_{PV} in the elastic scattering of polarized electrons from ^{208}Pb . A_{PV} is sensitive to the radius of the neutron distribution (R_n). The result $A_{\text{PV}} = 0.656 \pm 0.060(\text{stat}) \pm 0.014(\text{syst})$ ppm corresponds to a difference between the radii of the neutron and proton distributions $R_n - R_p = 0.33^{+0.16}_{-0.18}$ fm and provides the first electroweak observation of the neutron skin which is expected in a heavy, neutron-rich nucleus.



Symmetry energy and pressure of neutron matter

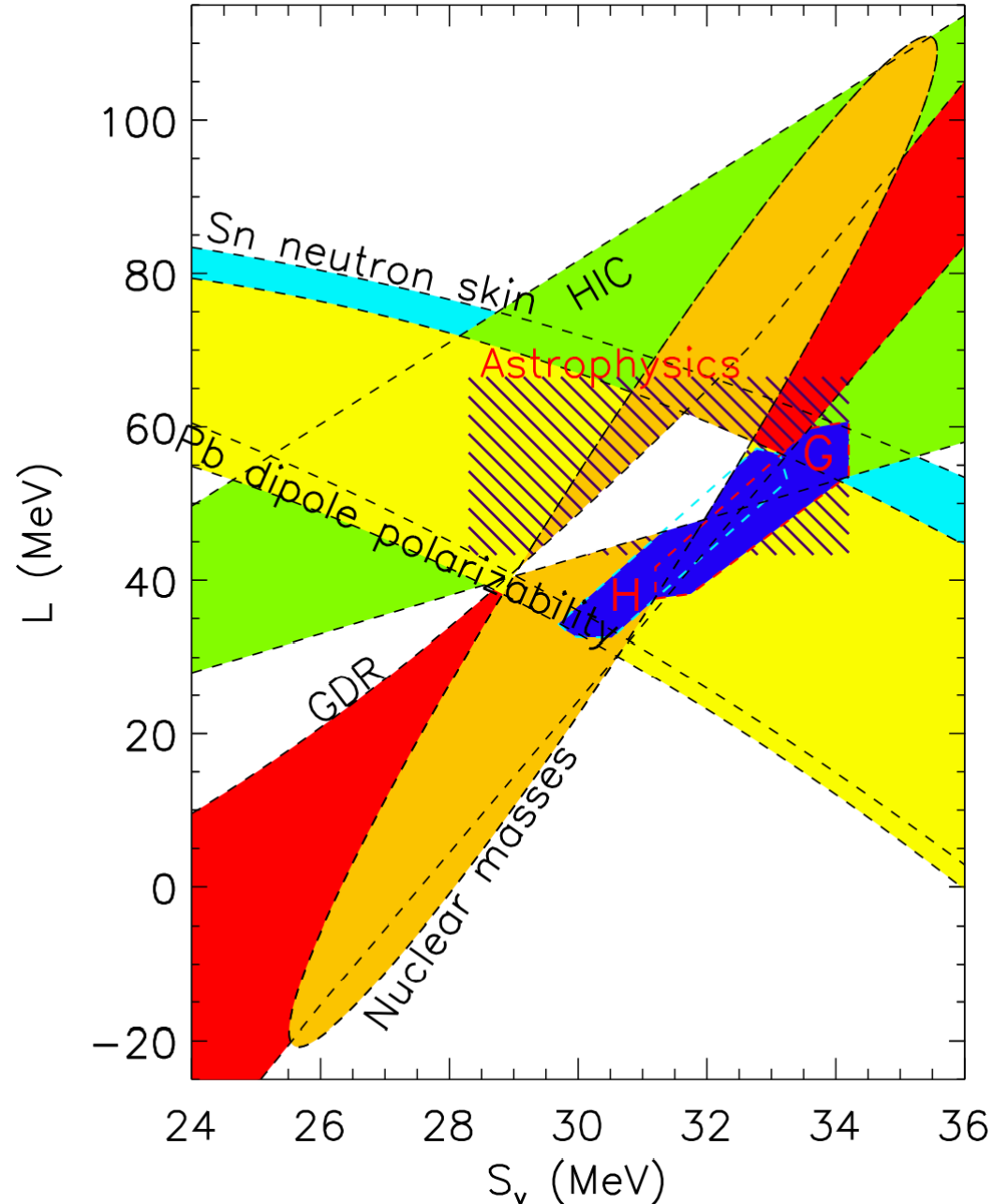
neutron matter band predicts
symmetry energy S_v and
its density derivative L

comparison to experimental
and observational constraints
Lattimer, Lim (2012)

neutron matter constraints
H: Hebeler et al. (2010, 2013)

G: Gandolfi et al. (2011)

microscopic calculations
provide tight constraints!



Discovery of the heaviest neutron star

A two-solar-mass neutron star measured using Shapiro delay

P. B. Demorest¹, T. Pennucci², S. M. Ransom¹, M. S. E. Roberts³ & J. W. T. Hessels^{4,5}

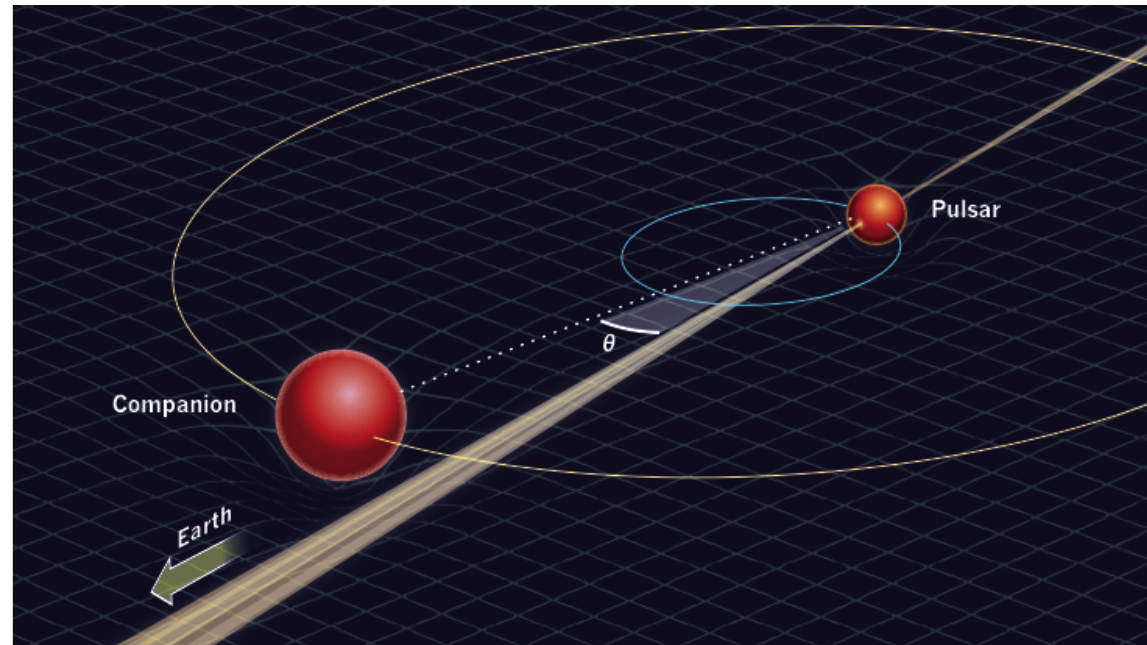
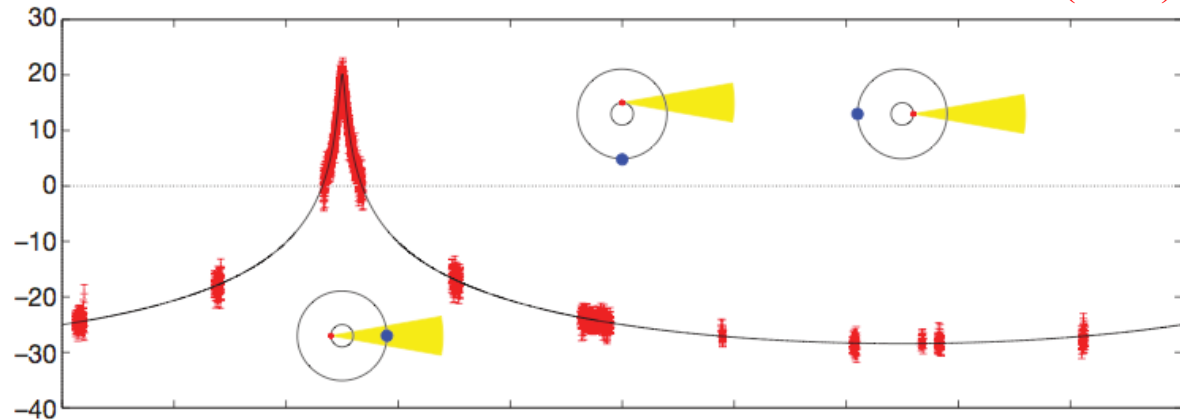
Nature (2010)

direct measurement of
neutron star mass from
increase in signal travel
time near companion

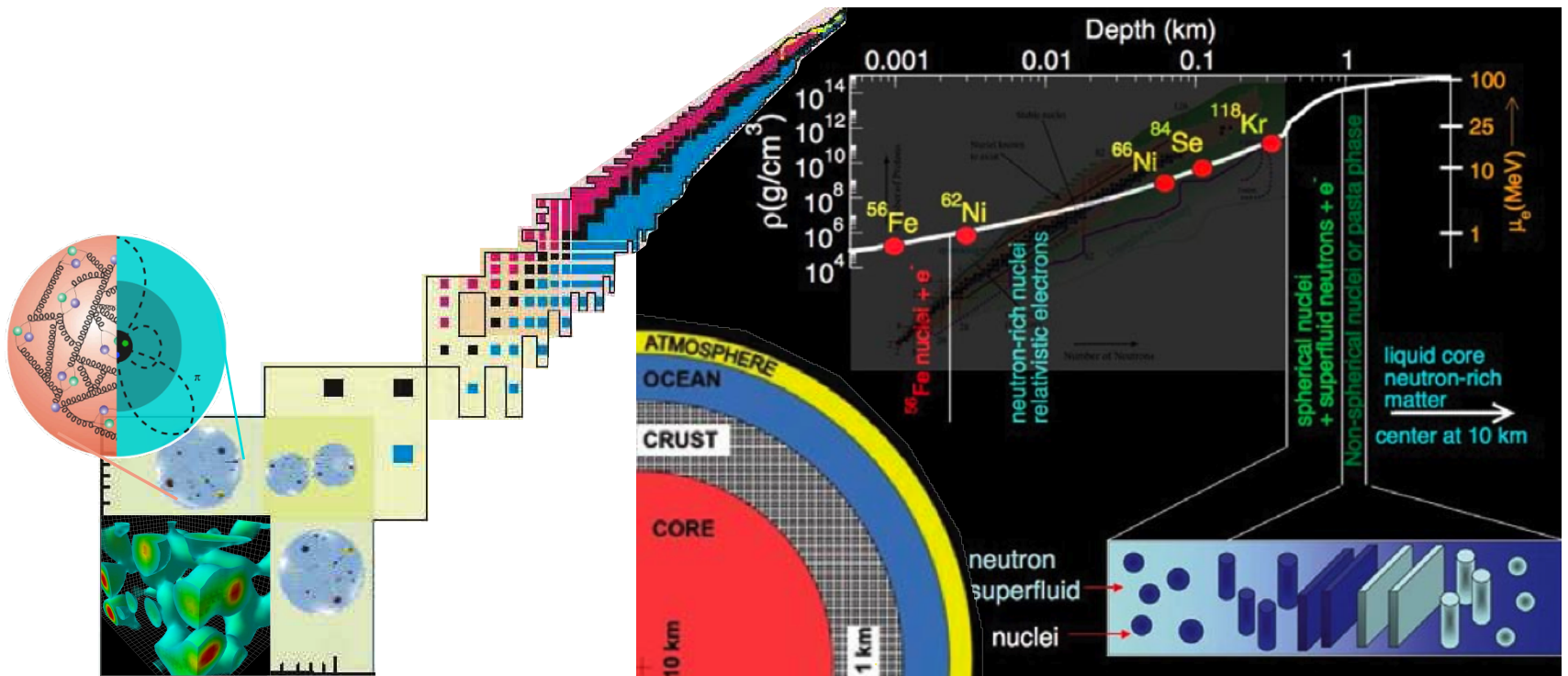
J1614-2230

most edge-on binary
pulsar known (89.17°)
+ massive white dwarf
companion ($0.5 M_{\text{sun}}$)

heaviest neutron star
with $1.97 \pm 0.04 M_{\text{sun}}$

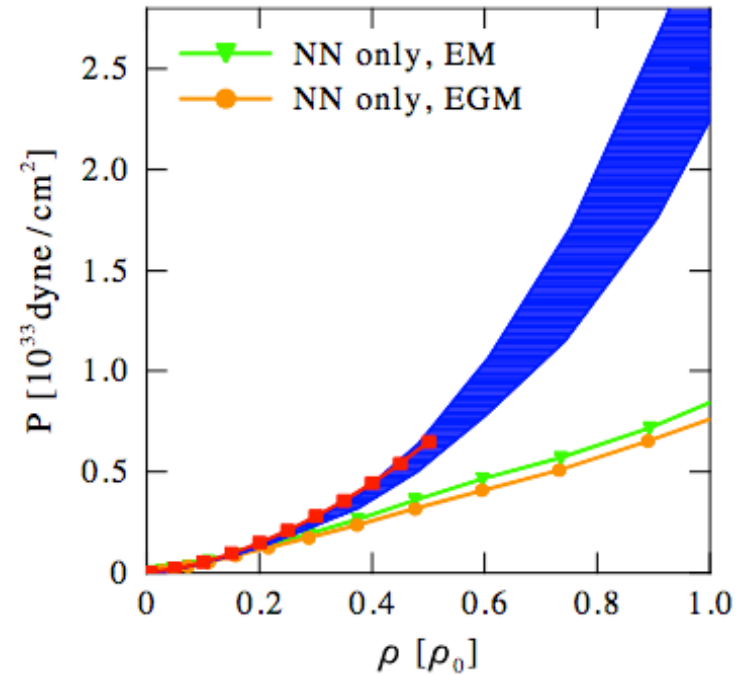


Neutron matter and neutron stars



Impact on neutron stars Hebeler et al. (2010, 2013)

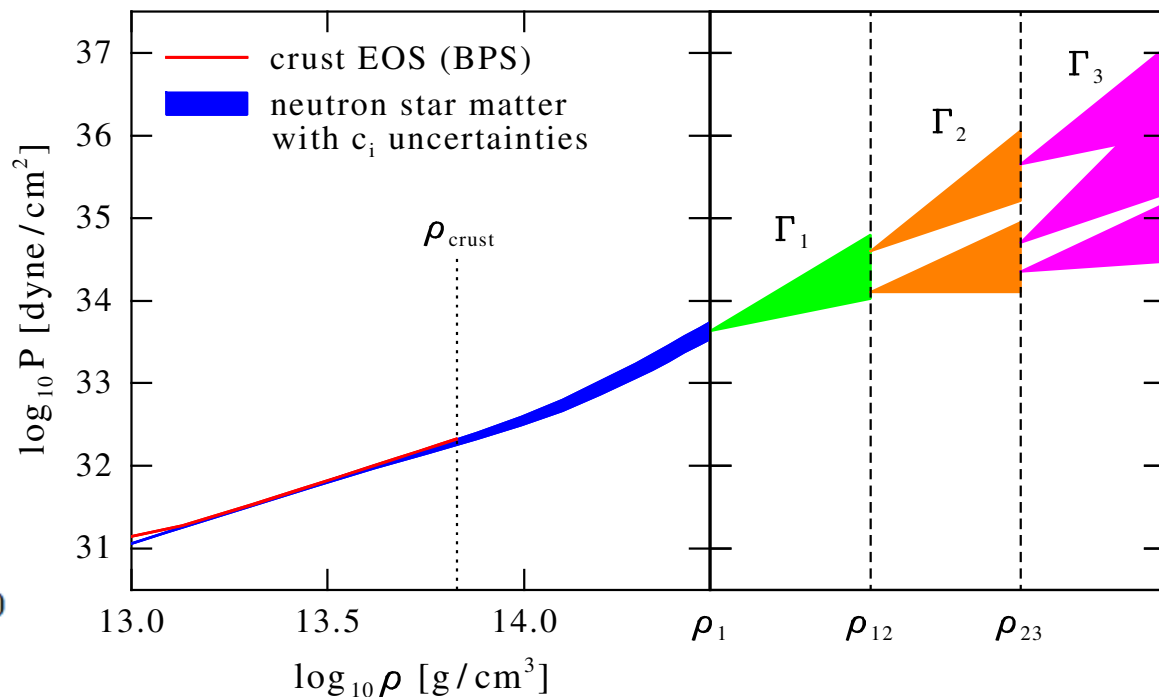
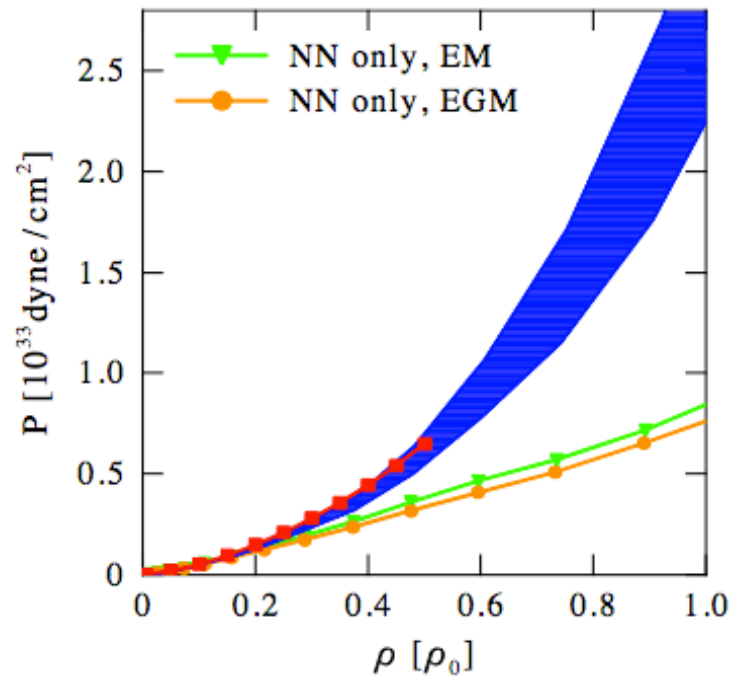
Equation of state/pressure for **neutron-star matter** (includes small $Y_{e,p}$)



pressure below nuclear densities agrees with standard crust equation of state only after 3N forces are included

Impact on neutron stars Hebeler et al. (2010, 2013)

Equation of state/pressure for **neutron-star matter** (includes small $Y_{e,p}$)



pressure below nuclear densities agrees with standard crust equation of state only after 3N forces are included

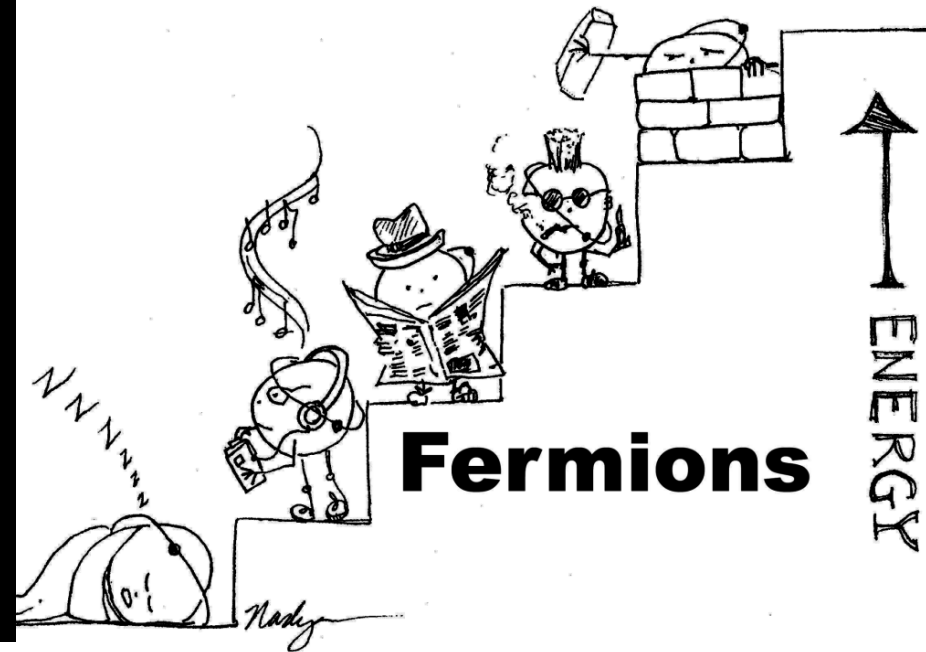
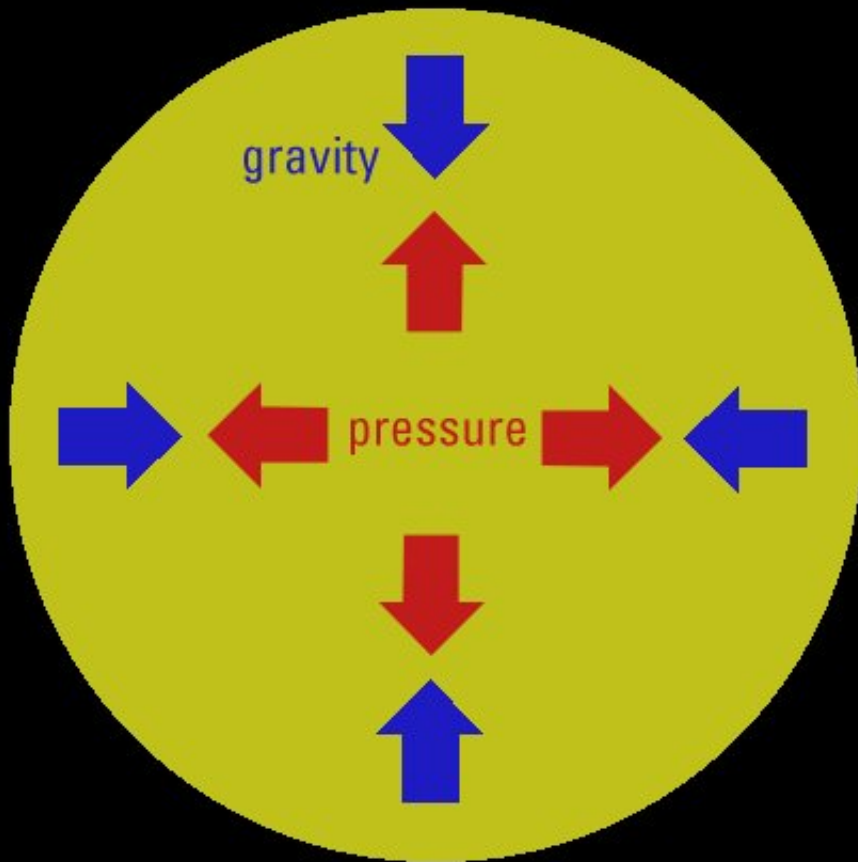
extend uncertainty band to higher densities using piecewise polytropes
allow for soft regions

Why are (neutron) stars stable?

equilibrium between pressure of matter and gravity

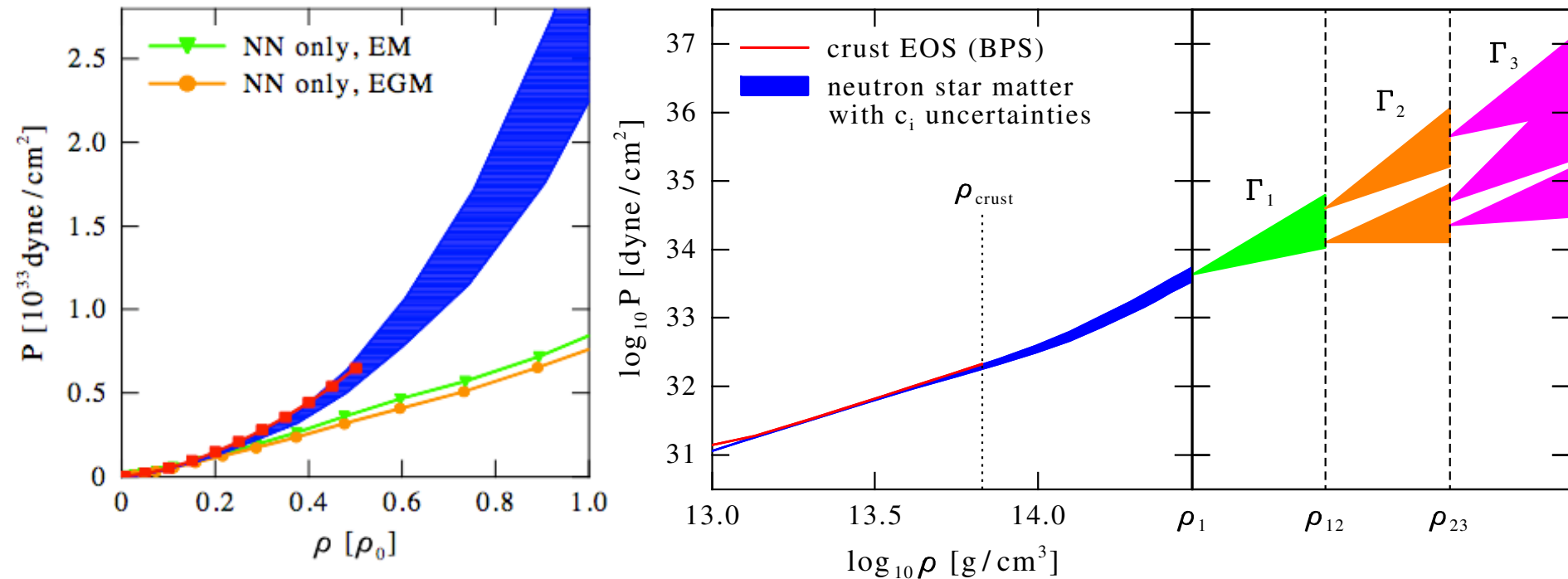
leads to Tolman-Oppenheimer-Volkov equations for neutron stars:
solve for enclosed $M(r)$, total M and R , only input: equation of state

pressure for neutrons:
Fermi pressure plus
 NN , $3N$,... interactions



Impact on neutron stars Hebeler et al. (2010, 2013)

Equation of state/pressure for **neutron-star matter** (includes small $Y_{e,p}$)

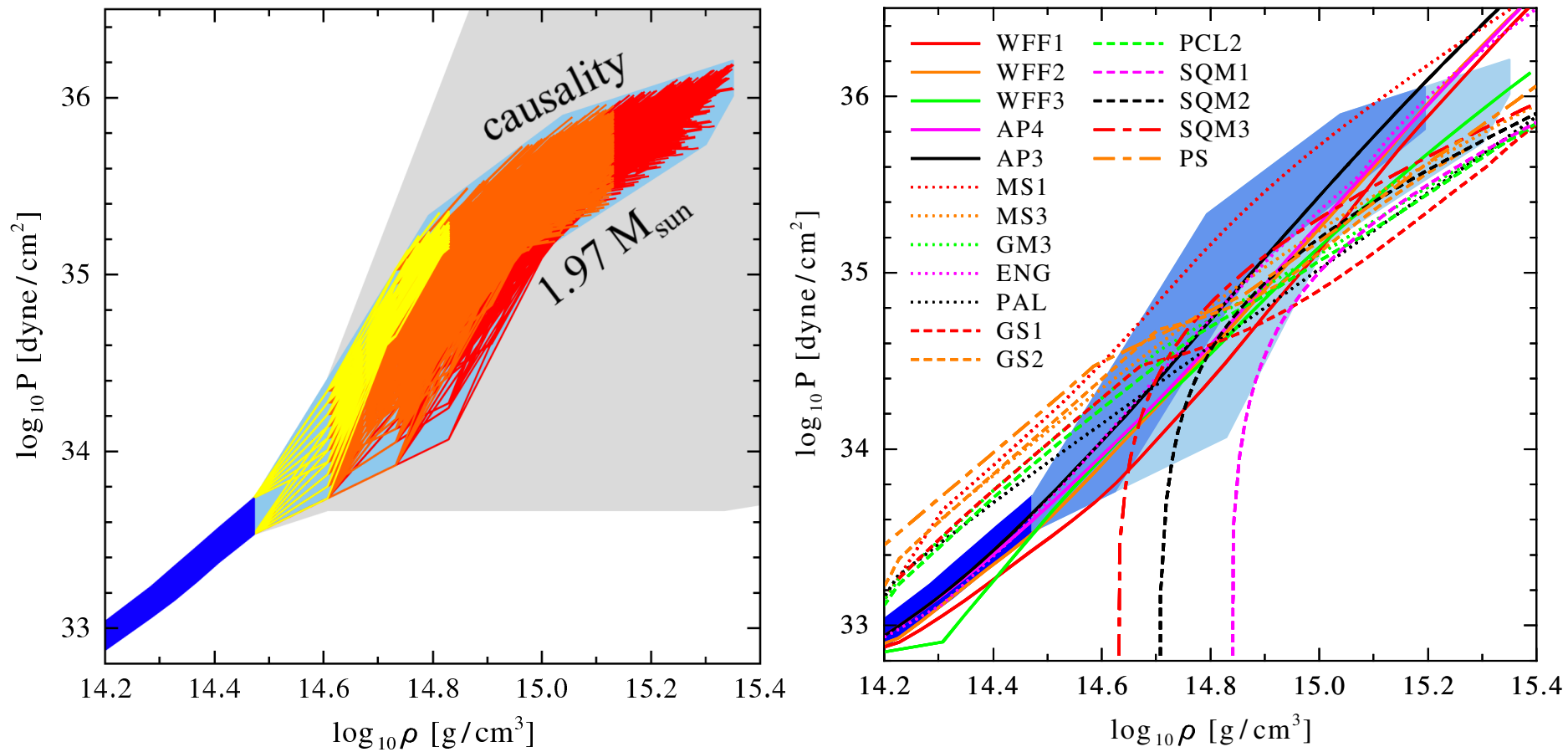


pressure below nuclear densities agrees with standard crust equation of state only after 3N forces are included

extend uncertainty band to higher densities using piecewise polytropes
allow for soft regions

Pressure of neutron star matter

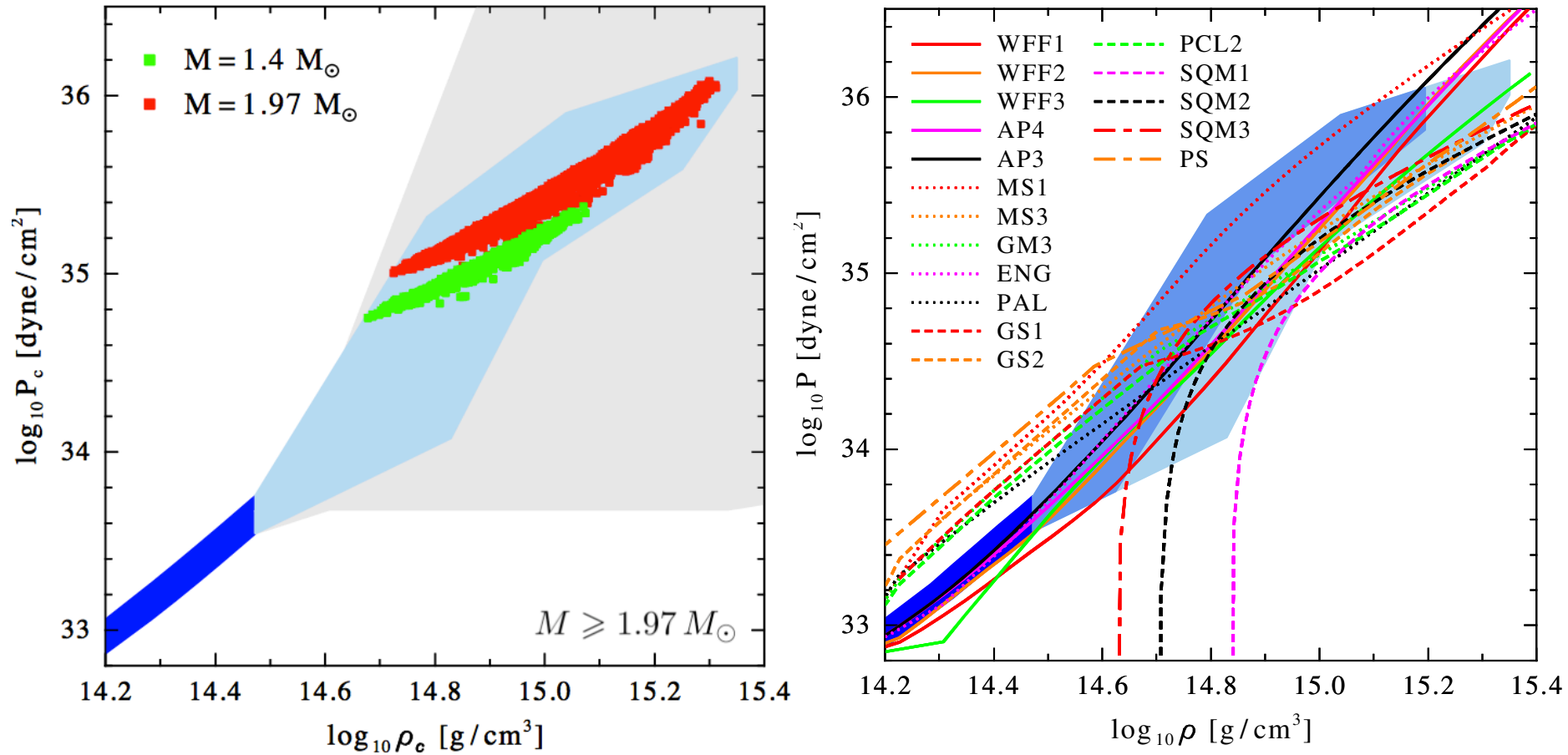
constrain polytropes by causality and require to support $1.97 M_{\text{sun}}$ star



low-density pressure sets scale, chiral EFT interactions provide strong constraints, ruling out many model equations of state

Pressure of neutron star matter

constrain polytropes by causality and require to support $1.97 M_{\text{sun}}$ star

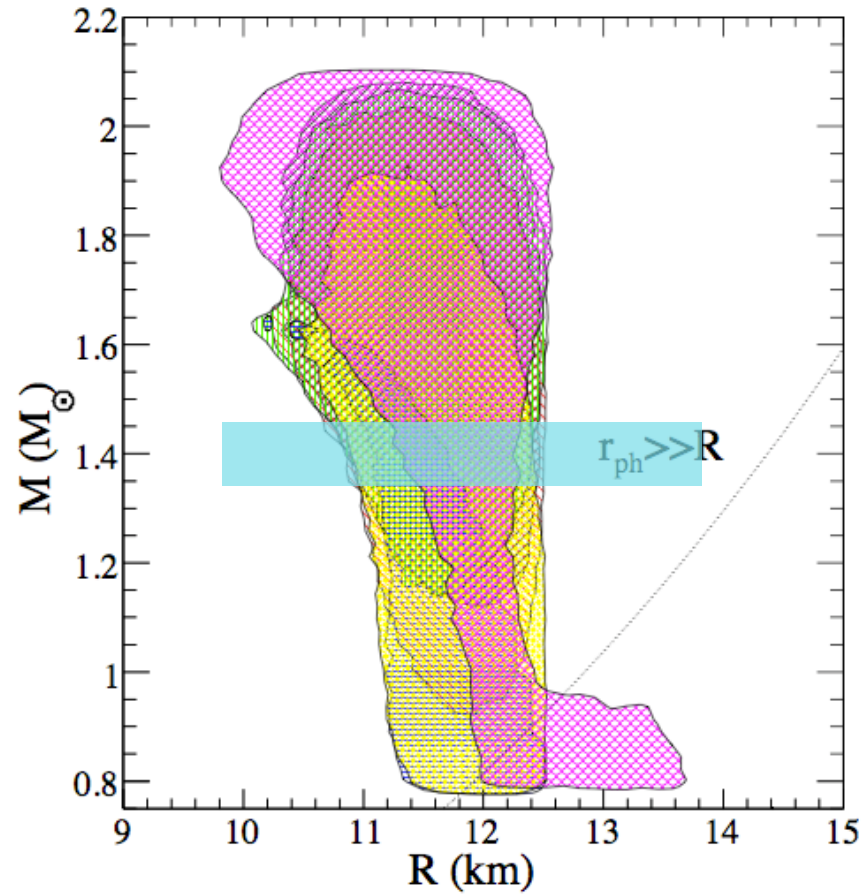
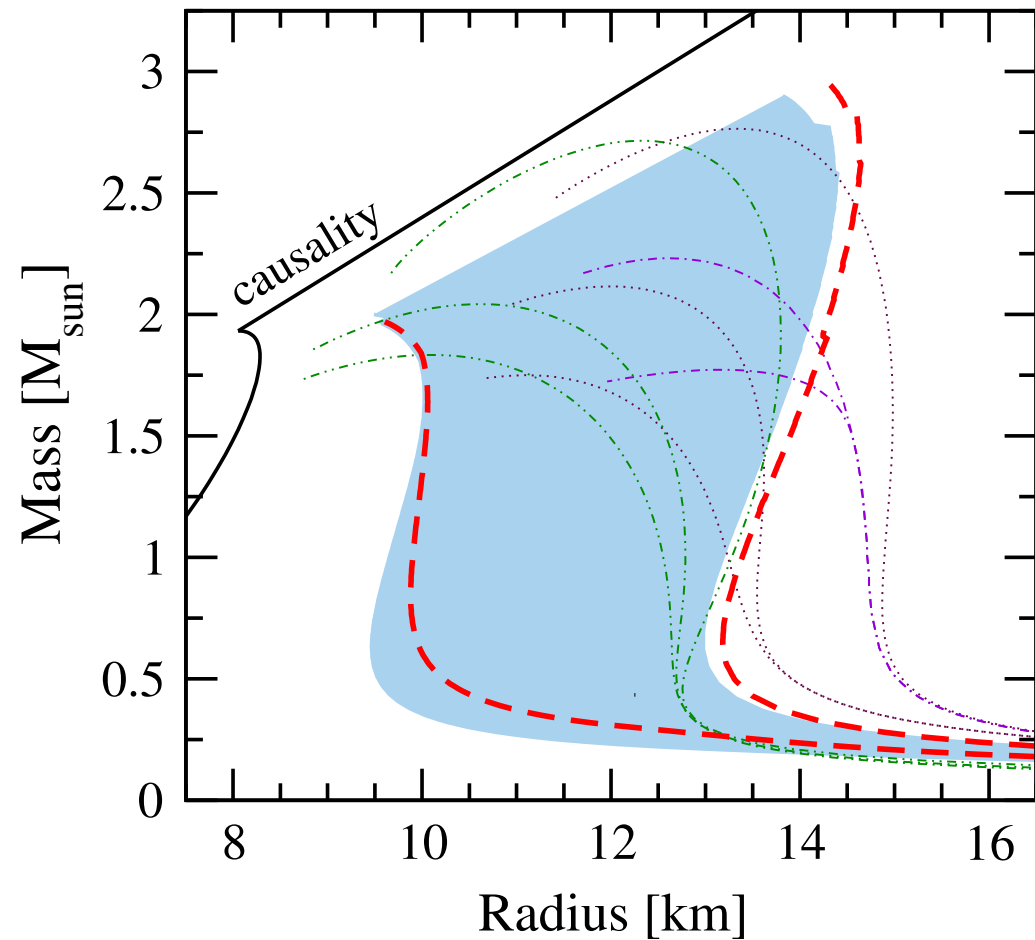


low-density pressure sets scale, chiral EFT interactions provide strong constraints, ruling out many model equations of state

central densities for $1.4 M_{\text{sun}}$ star: $1.8-4.4 \rho_0$

Neutron star radius constraints

uncertainty from many-body forces and general extrapolation



constrains neutron star radius: 9.7-13.9 km for $M=1.4 M_{\text{sun}}$ ($\pm 18\%$!)

consistent with extraction from X-ray burst sources [Steiner et al. \(2010\)](#)

Neutron-star mergers and gravitational waves

explore sensitivity to neutron-rich matter in neutron-star merger and gw signal

Bauswein, Janka (2012), Bauswein, Janka, Hebeler, AS (2012).

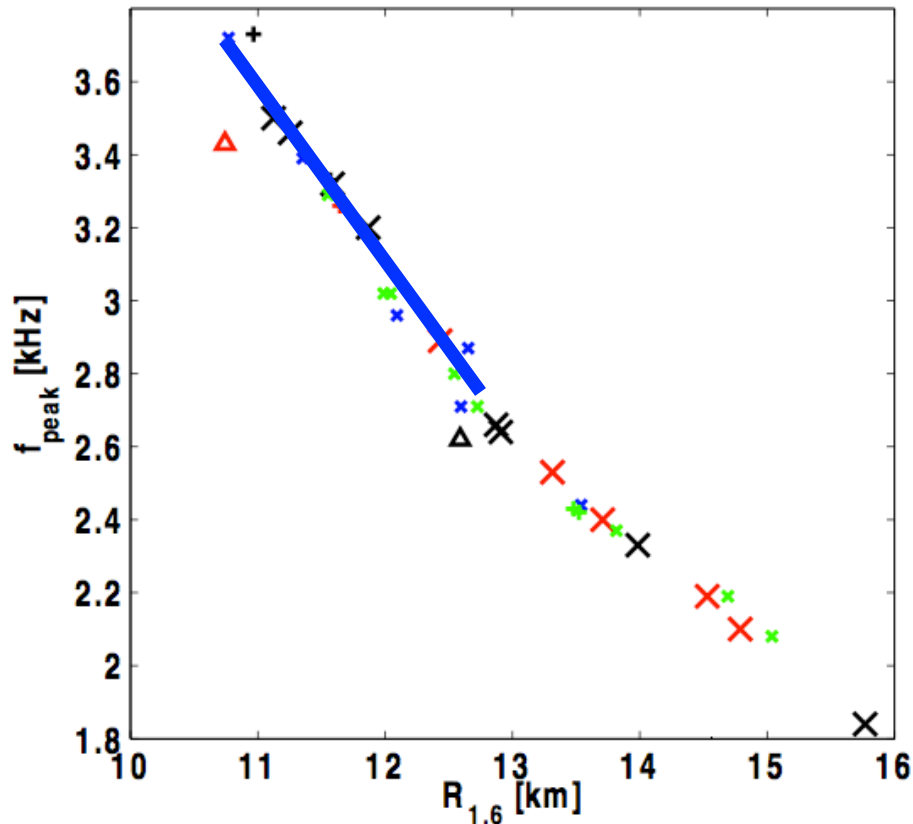


FIG. 10: Peak frequency of the postmerger GW emission versus the radius of a nonrotating NS with $1.6 M_{\odot}$ for different EoSs. Symbols have the same meaning as in Fig. 8.

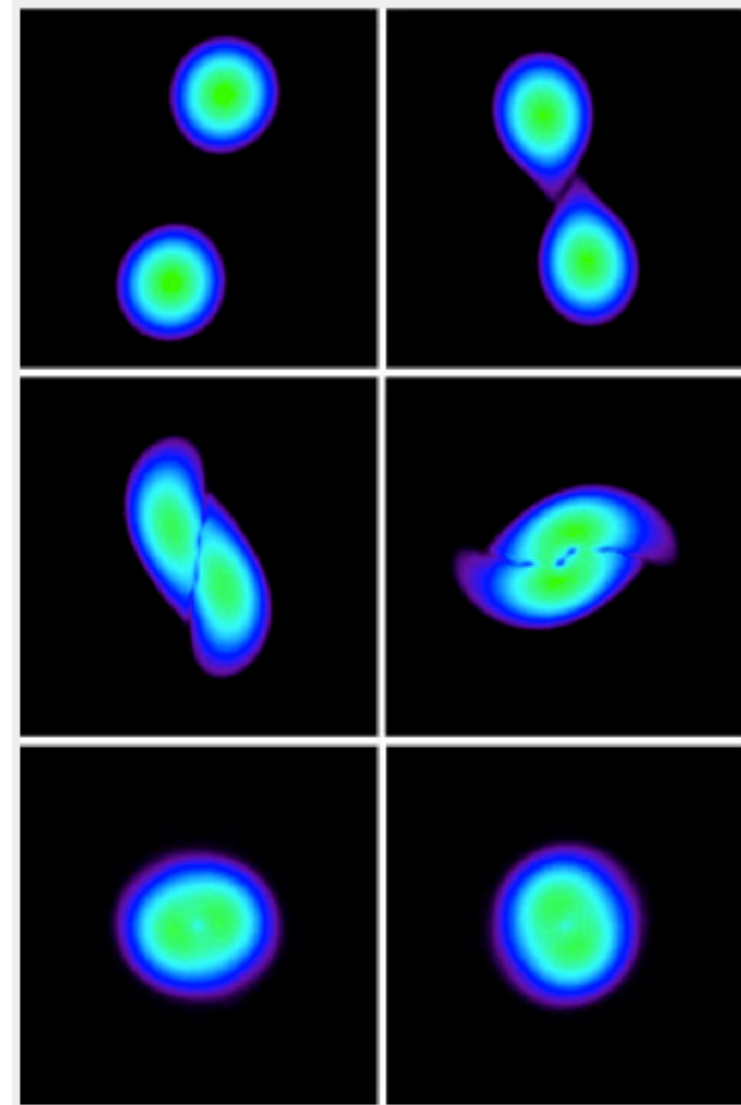


Fig. 1: Various snapshots of the collision of two neutron stars initially revolving around each other. The sequence simulated by the computer covers only 0.03 seconds. The two stars orbit each other counterclockwise (top left) and quickly come closer (top right). Finally they collide (centre left), merge (centre right), and form a dense, superheavy neutron star (bottom). Strong vibrations of the collision remnant are noticeable as deformations in east-west direction and in north-south direction (bottom panels). (Simulation: Andreas Bauswein and H.-Thomas Janka/MPA)