

# **Effects of variation of fundamental constants from Big Bang to atomic clocks**

## **Contributors:**

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The possibility for the fundamental constants to vary is suggested by theories unifying **gravity** with **other** interactions.

Fine structure constant  $\alpha = e^2/\hbar c$ ,  
 $e$  -electron charge,  $c$  -speed of light.

Quark mass  $m_q$ /Strong interaction scale  $\Lambda_{QCD}$ .

The search goes in:

- (1) Quasar absorption spectra (QAS)
- (2) Big Bang Nucleosynthesis (BBN)
- (3) Oklo natural nuclear reactor
- (4) Atomic clocks

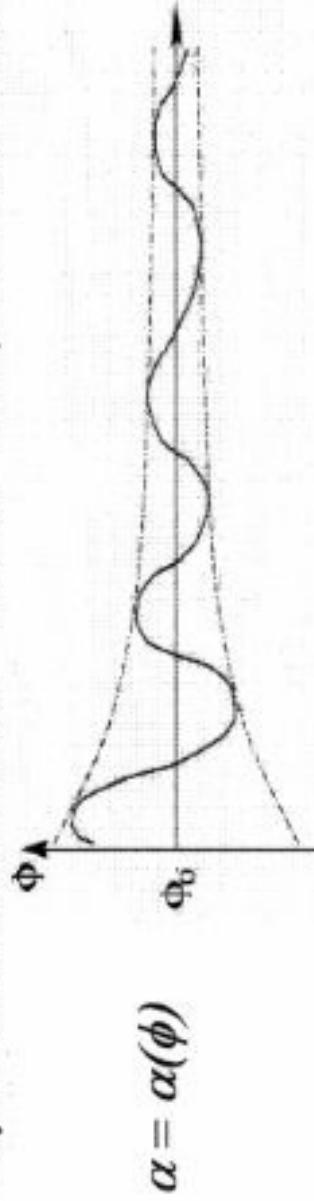
	Constants	Result
QAS	$\alpha \frac{m_q}{\Lambda_{QCD}}$	$\Delta \neq 0 !?$
BBN	$\alpha \frac{m_q}{\Lambda_{QCD}} \frac{\Lambda_{QCD}}{M_{Plank}}$	$\Delta \neq 0 !?$
Oklo	$\alpha \frac{m_q}{\Lambda_{QCD}}$	$\Delta \neq 0 !?$
Clocks	$\alpha \frac{m_{q,e}}{\Lambda_{QCD}}$	$\Delta < \delta$

## “Motivating” comments from the literature:

- “Unified theories applied to cosmology suffer generically from a problem of predicting time-dependent coupling constants.” – Fujii Y., Omote M., Nishakoa T., 1994, Prog. Theor. Phys., 92, 3
- “ ... in cosmology with extra dimensions people try to find solutions with the external dimensions expanding while the extra dimensions remain static. But at present no mechanism for keeping the internal spatial scale static has been found.” – Li L.-X., Gott J.

$$R_{\text{III}}, 1998, \text{Phys. Rev. D}, 58, 103513 \quad \alpha \propto G / R_{\text{KK}}^2$$

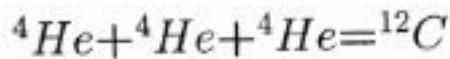
- “ ...  $dR_{\text{KK}}/dt \neq 0$  ... could give rise to observable time variations in the fundamental “constants” of our four-dimensional world and thereby provide a window to the extra dimensions.” – Marciano W. J., 1984, Phys. Rev. Lett., 52, 489
- “ ... all coupling constants and masses of elementary particles, being dependent on the dilaton scalar field, should be, generally speaking, space and time dependent, and influenced by local circumstances.” – Damour T., Polyakov A. M., 1994, Nucl. Phys. B, 423, 532



- $\alpha = e^2/hc$  - “The minimal varying- $c$  theory is of interest because it offers a means of solving the so-called cosmological problems: the horizon, flatness, cosmological constant, entropy, and homogeneity problems.” – Barrow J. D., Magueijo J., 1998, Phys. Lett. B, 443, 104

Some special “tuning” of fundamental constants is needed for humans to exist.

Example: low-energy resonance in carbon production reaction in stars:

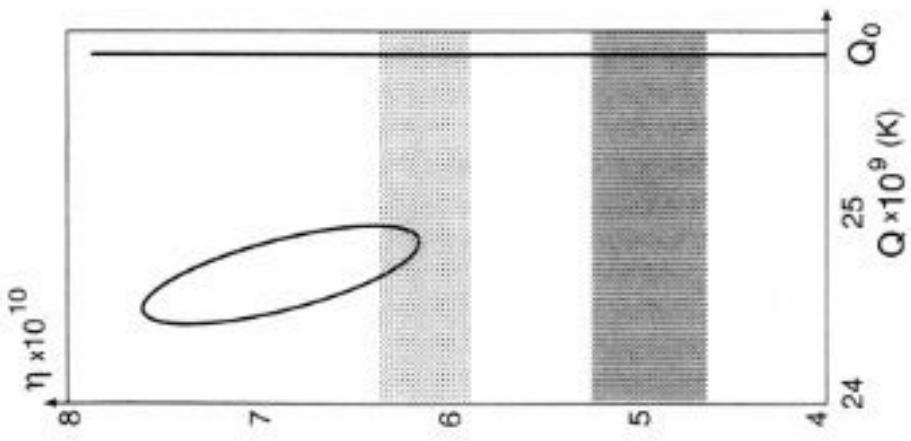


Different coupling constants  $\rightarrow$  no low-energy resonance  $\rightarrow$  no carbon  $\rightarrow$  no life.

Variation of coupling constants in space could provide a natural explanation of “fine tuning”: we appeared in area of the Universe where values of fundamental constants are consistent with our existence.

# Big Bang Nucleosynthesis

(Dmitriev, Flambaum, Webb)

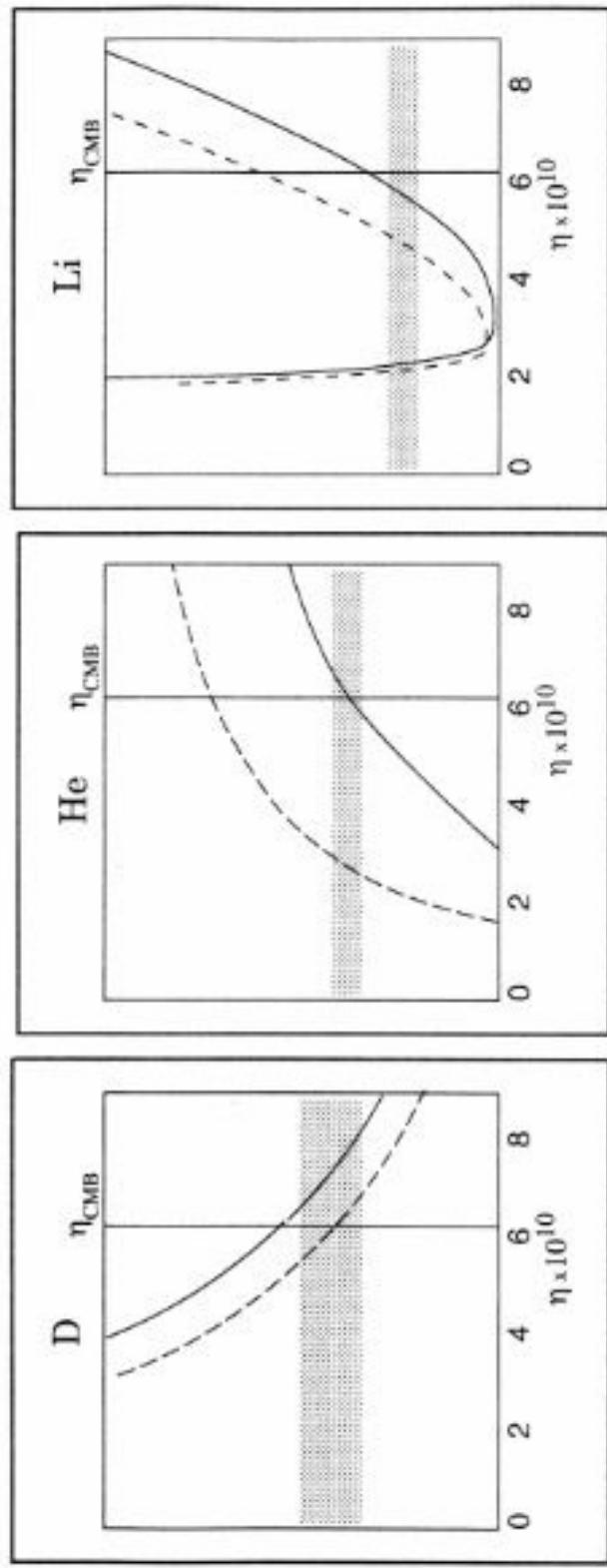


$$p + n \rightarrow d + \gamma, \quad 3 \text{ sec} \leq t \leq 6 \text{ min}$$

Productions of D,  $^4\text{He}$ ,  $^7\text{Li}$  are exponentially sensitive to deuteron binding energy  $E_d$

- $\eta$  from cosmic microwave background fluctuations ( $\eta$  - baryon to photon ratio).

- $\eta$  from BBN for present value of  $Q$  ( $Q = |E_d|$ )



$$\frac{\delta E_d}{E_d} = -0.019 \pm 0.005$$

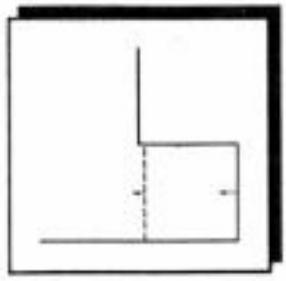
Comparison with observations gives

$$\eta(BBN) \approx \eta(CMB)$$

This also leads to agreement

Flambaum, Shuryak: Deuteron Binding Energy is very sensitive to variation of *strange* quark mass (4 factors of enhancement):

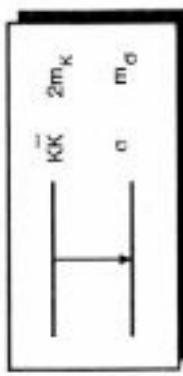
1. Deuteron is a shallow bound level.



Virtual level in  $n+p \rightarrow d+\gamma$  is even more sensitive to the variation of the potential.

2. Strong compensation between  $\sigma$ -meson and  $\omega$ -meson exchange in potential (Walecka model):  $4\pi r V = -g_s^2 e^{-m_\sigma r} + g_v^2 e^{-m_\omega r}$

3.  $\sigma = \frac{1}{\sqrt{3}}(u\bar{u} + d\bar{d} + s\bar{s})$ ,  $m_\sigma \approx \frac{2}{3}m_s + 2\lambda_{qCD}$



4. Repulsion of  $\sigma$  from  $K\bar{K}$  threshold

Total  $\frac{\delta E_d}{E_d} \approx -17 \frac{\delta m_s}{m_s}$  and  $\frac{\delta(m_s/\Lambda_{QCD})}{m_s/\Lambda_{QCD}} = (+1.1 \pm 0.3) \times 10^{-3}$

Sensitivity of  $E_d$  to variation of  
of the light quark mass  $m_q$

Pion mass  $m_\pi \sim \sqrt{m_q \cdot \Lambda_{QCD}}$

$$\frac{\delta E_d}{E_d} = K_\pi \frac{\delta m_\pi}{m_\pi} = K_\pi \cdot \frac{1}{2} \cdot \frac{\delta m_q}{m_q}$$

Flambauer, Shuryak 2002

$$-18 < K_\pi < 3$$

Epelbaum  
Meißner, Glöckle

$$\frac{\partial E_d}{\partial m_\pi} = -0.075 \pm 0.023$$

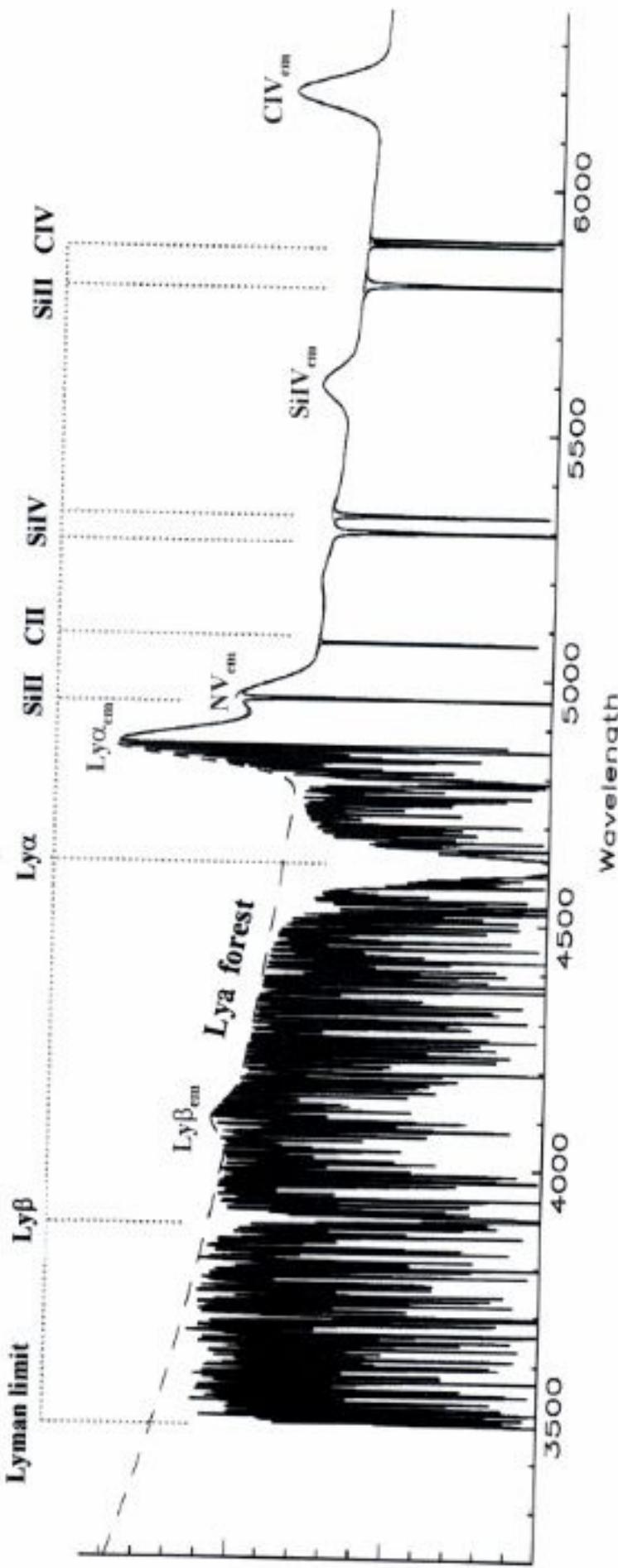
$$\rightarrow K_\pi = -5 \quad (1 \pm 0.3)$$

$$\frac{\delta E_d}{E_d} \approx -2.5 \quad - \frac{\delta (m_q / \Lambda_{QCD})}{(m_q / \Lambda_{QCD})}$$



## 4.2 Astrophysical constraints:

Quasars - probing the universe back to much earlier times



## Many-Multiplet Method

Relativistic correction to electron energy  $E_n$ :

$$\Delta_n = \frac{E_n}{\nu} (Z\alpha)^2 \left[ \frac{1}{j + 1/2} - C(Z, j, l) \right] \quad C \approx 0.6$$

1. Increases with nuclear charge  $Z$ .
2. Changes sign for higher angular momentum  $j$ .

Probing the variability of  $\alpha$  with QSO absorption lines

## Procedure:

1. Compare heavy ( $Z \sim 30$ ) and light ( $Z < 10$ ) atoms, OR
2. Compare  $s \rightarrow p$  and  $d \rightarrow p$  transitions in heavy atoms.

Shifts can be of opposite sign.

Basic formula:

$$E_{z=0} = E_{z=0} + q \left[ \left( \frac{\alpha_z}{\alpha_0} \right)^2 - 1 \right]$$

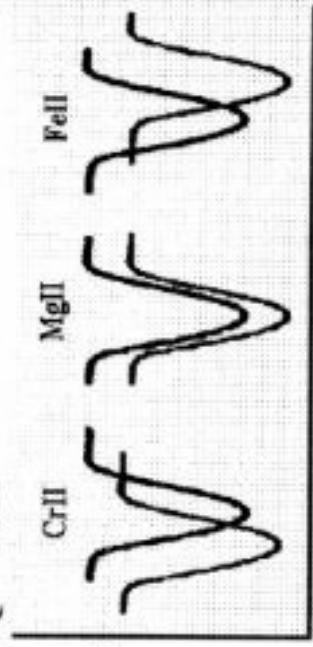
$E_{z=0}$  is the laboratory frequency. 2<sup>nd</sup> term is non-zero only if  $\alpha$  has changed.  $q$  is derived from atomic calculations.

Relativistic shift of the central line in the multiplet  $\frac{q = Q + K(L \cdot S)}{K}$   
Numerical examples: (units = cm<sup>-1</sup>)

$K$  is the spin-orbit splitting parameter.  $Q \sim 10K$

$Z=26$ ( $s \rightarrow p$ )	FeII 2383A: $\omega_0 = 38458.987(2) + 1449x$
$Z=12$ ( $s \rightarrow p$ )	MgII 2796A: $\omega_0 = 35669.298(2) + 120x$
$Z=24$ ( $d \rightarrow p$ )	CrII 2066A: $\omega_0 = 48398.666(2) - 1267x$

$$x = (\alpha_z/\alpha_0)^2 - 1$$



MgII "anchor"

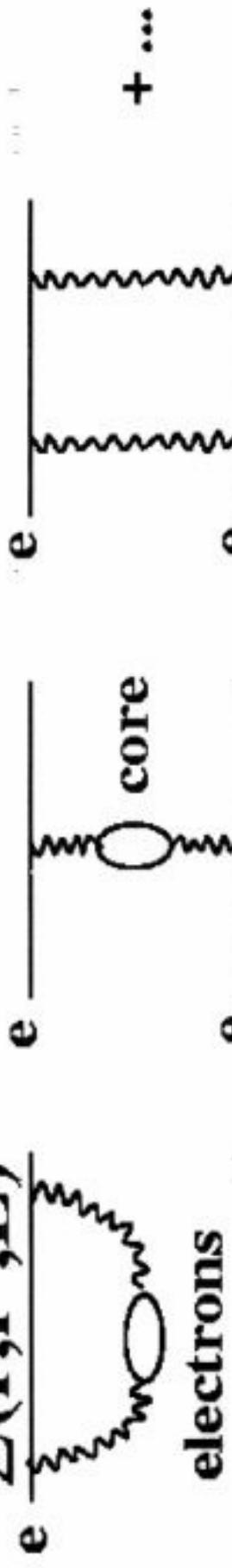
To find dependence of atomic transition frequencies on  $\alpha$  we have performed calculations of atomic transition frequencies for different values of  $\alpha$ .

1. Zero Approximation – Relativistic Hartree-Fock method:  
energies, wave functions, Green's functions

2. Many-body perturbation theory to calculate effective

Hamiltonian for valence electrons including self-energy operator and screening; perturbation  $\longrightarrow V = H - H_{HF}$

$$\sum(\mathbf{r}, \mathbf{r}', \mathbf{E})$$



3. Diagonalization of the effective Hamiltonian

**Test:** Energy levels in Mg II to 0.2% accuracy

## Lines used in the analysis ( cm<sup>-1</sup>)

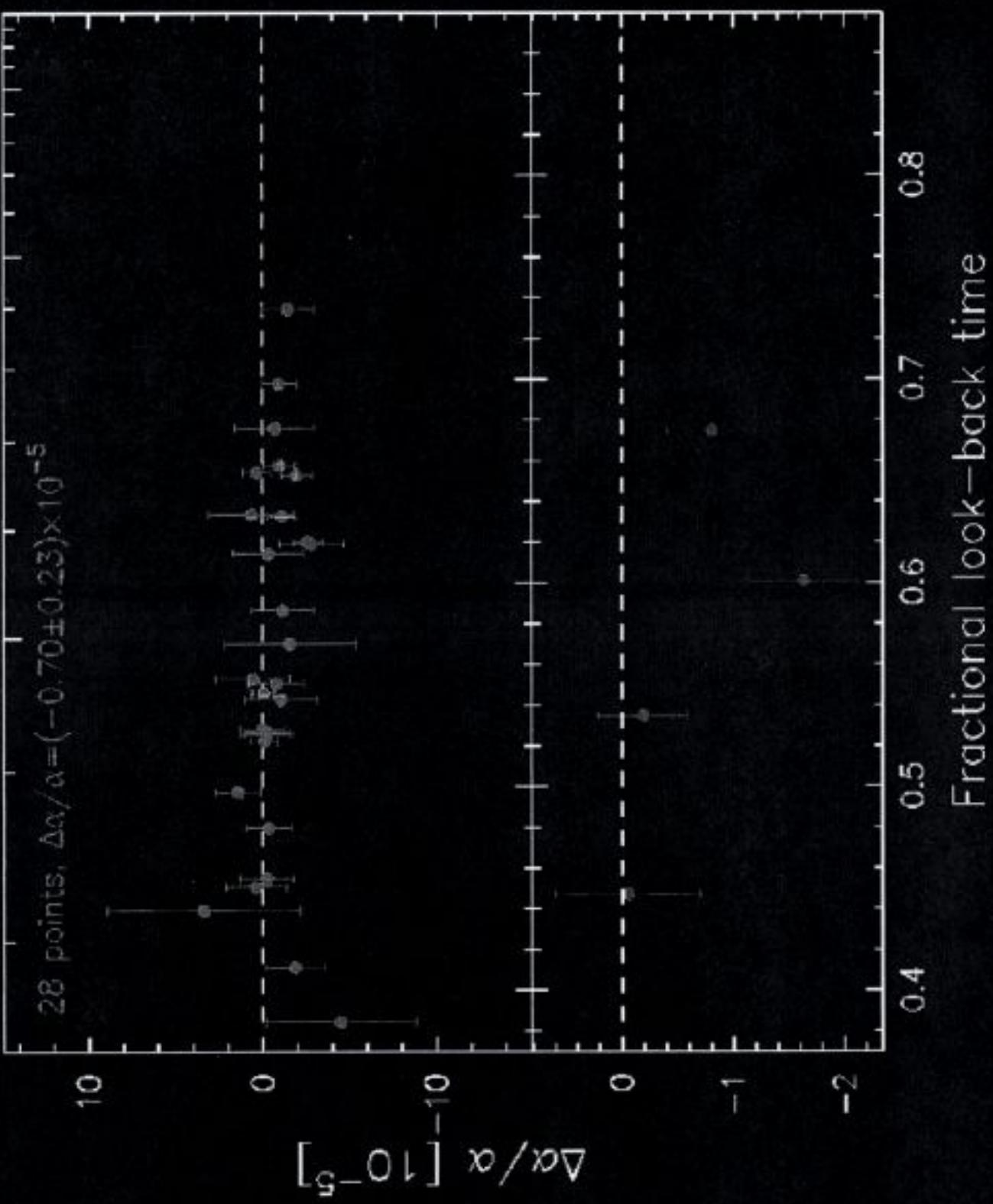
	Anchor lines		Negative shifters	
MgI	35051.277(1)	+	86x	57420.013(4)
MgII	35760.848(2)	+	211x	57080.373(4)
MgII	35669.298(2)	+	120x	48632.055(2)
SII	55309.3365(4)	+	520x	48491.053(2)
SII	65500.4492(7)	+	50x	48398.868(2)
AIII	59851.924(4)	+	270x	62171.625(4)
AIII	53916.540(1)	+	464x	
AIII	53682.880(2)	+	216x	62065.528(3)
AIII	58493.071(4)	-	20x	42658.2404(2)
NIII				42114.8329(2)
				Fell
				41968.0642(2)
				Fell
				38660.0494(2)
				Fell
				38458.9871(2)
				ZnII
				49355.002(2)
				ZnII
				48481.077(2)
				1400x
				700x
				1110x
				1280x
				1360x
				1300x
			Positive shifters	
				+ 1100x
				+ 1210x
				+ 1590x
				+ 1460x
				+ 1490x
				+ 1330x
				+ 2490x
				+ 1584x

# Results:

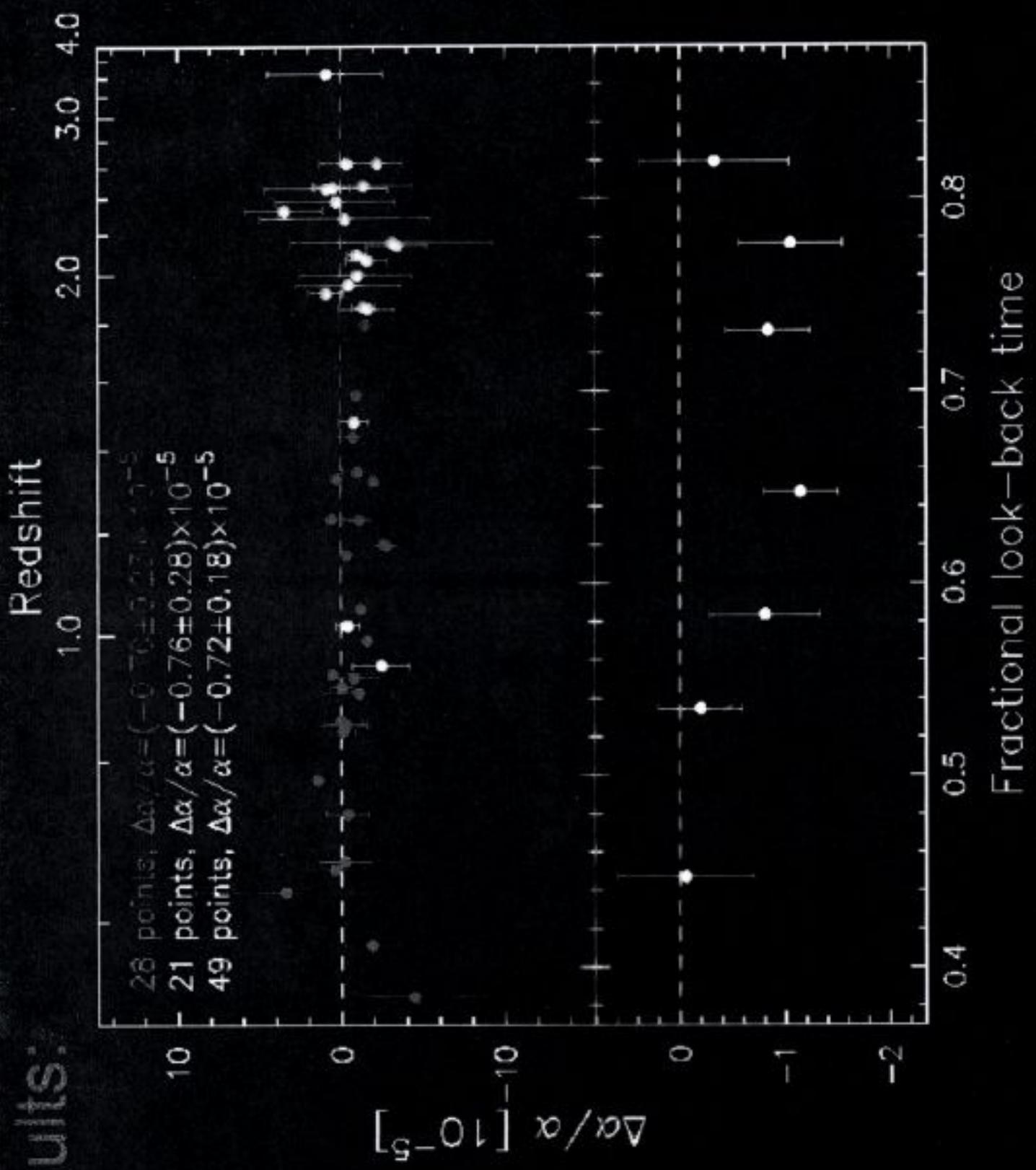
Redshift

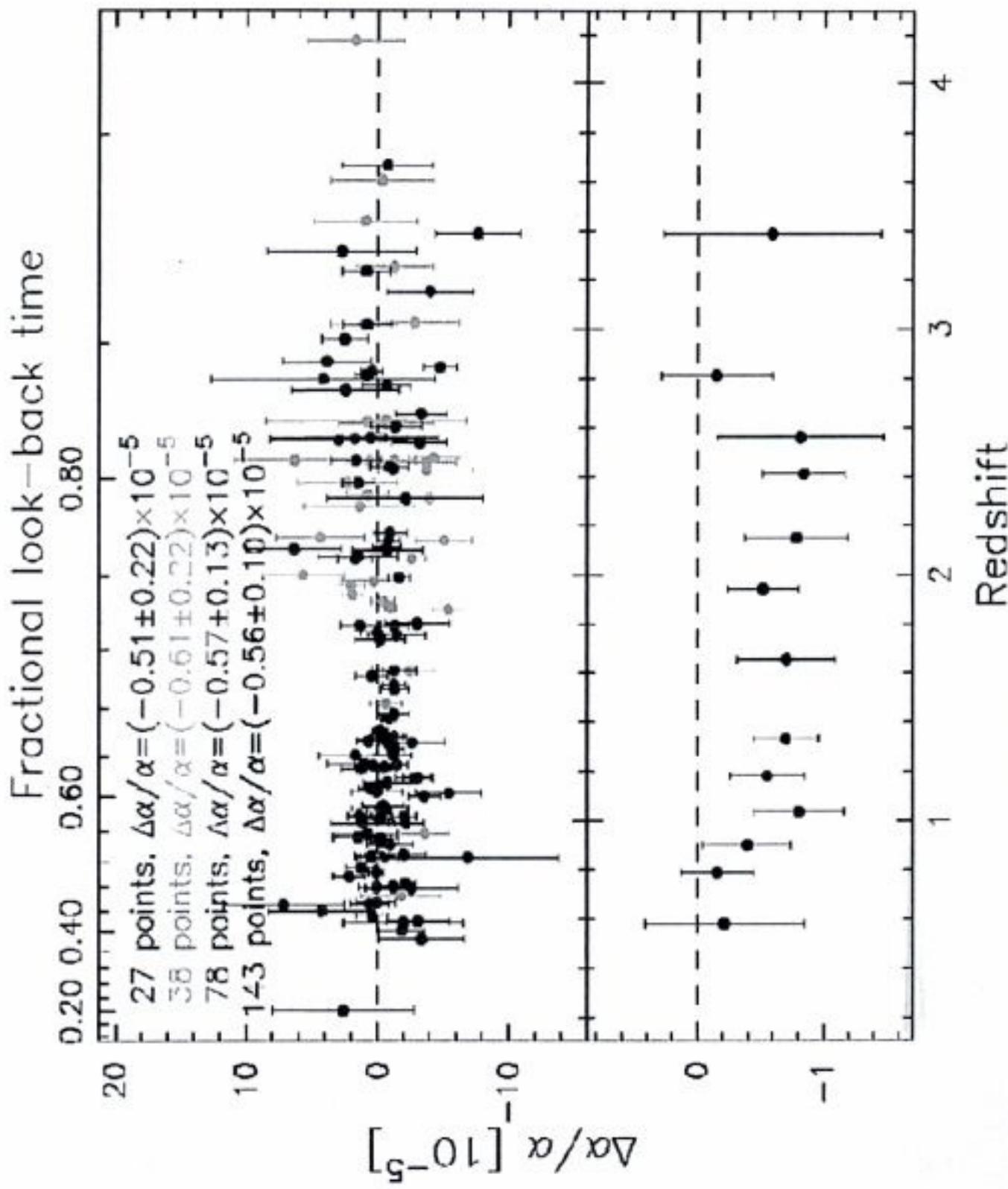
2.0  
3.0  
4.0

28 points,  $\Delta\alpha/\alpha = (-0.70 \pm 0.23) \times 10^{-5}$



# Results:





# Potential systematic effects:

- (: Wavelength calibration errors
- (: Laboratory wavelength errors
- (: Heliocentric velocity variation
- (: Temperature changes during observations
- (: Line blending
- (: Differential isotopic saturation
- (: Hyperfine structure effects
- (: Instrumental profile variations
- (: ... and of course, Magnetic fields
- (: ~~Atmospheric dispersion effects~~
- (: Isotopic ratio evolution

# UVES QSO Sample 2004

*Wilfred Walsh, John Webb, Victor Flambaum*  
[wwalsh@phys.unsw.edu.au](mailto:wwalsh@phys.unsw.edu.au)

UNIVERSITY OF NEW SOUTH WALES  
SYDNEY AUSTRALIA

UNSW, September 2004

Results:

1998-2003, Keck telescope, Hawaii, red shift  $0.2 < z < 4.3$ ,  
143 absorption systems, 23 transitions,

3 independent samples:

$$\frac{\delta\alpha}{\alpha} = (-0.543 \pm 0.116) \cdot 10^{-5}$$

Statistical significance  $4.7 \sigma$  from zero.

2004, VLT-UVES, Chile (different hemisphere), red shift  
 $0.4 < z < 2.8$

full sample, 74 systems  $\frac{\delta\alpha}{\alpha} = (-0.020 \pm 0.092) \cdot 10^{-5}$

clean sample, 52 systems  $\frac{\delta\alpha}{\alpha} = (-0.004 \pm 0.098) \cdot 10^{-5}$

Strianand et al sample, 23 systems  $\frac{\delta\alpha}{\alpha} = (-0.061 \pm 0.126) \cdot 10^{-5}$

VLT:  $|\frac{\delta\alpha}{\alpha}| < 0.1 \cdot 10^{-5}$  Zero!

Too large scatter, more realistic preliminary result

$$\frac{\delta\alpha}{\alpha} = (-0.05 \pm 0.29) \cdot 10^{-5}$$

Other groups results from VLT-UVES:

Strianand, Chand, Petitjean, Aracil (2004), 23 systems, 12  
transitions,  $0.4 < z < 2.3$ :

$$\frac{\delta\alpha}{\alpha} = (-0.06 \pm 0.06) \cdot 10^{-5}$$

Quast, Reimer, Levshakov (2004): 1 system, Fe II only, 6  
transitions,  $z = 1.15$ :

$$\frac{\delta\alpha}{\alpha} = (-0.04 \pm 0.19 \pm 0.27_{syst}) \cdot 10^{-5}$$

Difference between Keck and VLT data:

Undiscovered systematic effect?

Spatial variation of  $\alpha$ ?

*C. L. Steinhardt, Phys. Rev. D, 71, 043509 (2005):*

It might be spatial variation!

*Srianand et al* use data from Southern Hemisphere only

$$\left(\frac{\Delta\alpha}{\alpha}\right)_{\text{South}} = (-0.06 \pm 0.06) \times 10^{-5}$$

*Murphy et al* use both:

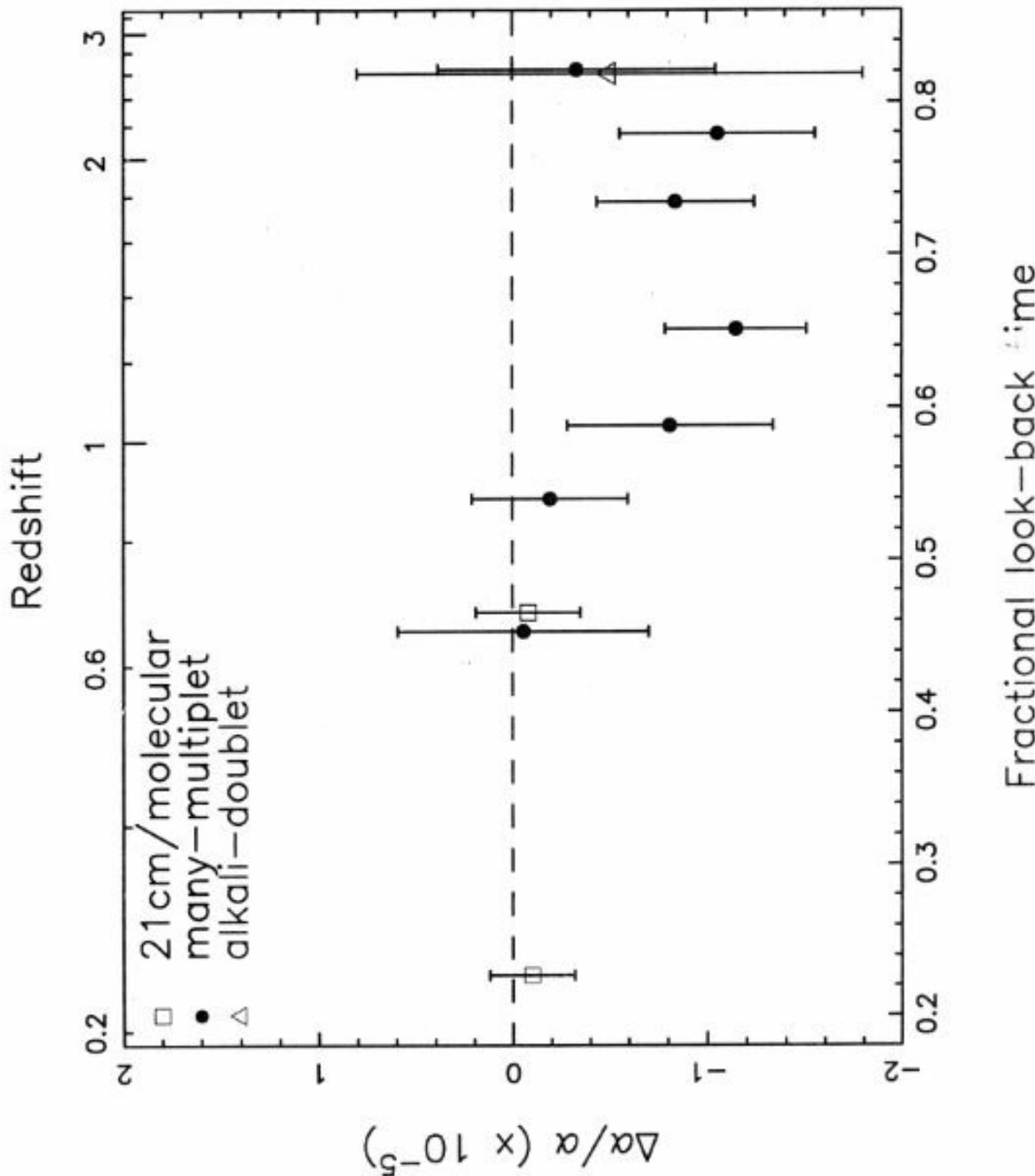
$$\left(\frac{\Delta\alpha}{\alpha}\right)_{\text{South}} = (-0.36 \pm 0.19) \times 10^{-5}$$

$$\left(\frac{\Delta\alpha}{\alpha}\right)_{\text{North}} = (-0.66 \pm 0.12) \times 10^{-5}$$

## Radio constraints:

- Hydrogen hyperfine transition at  $\lambda_H = 21\text{cm}$ .
- Molecular rotational transitions CO, HCO<sup>+</sup>, HCN, HNC, CN, CS ...
- $\omega_H/\omega_M \propto \alpha^2 g_P$  where  $g_P$  is the proton magnetic g-factor.

$$g_P = g_p \left( \frac{m_q}{\Lambda_{QED}} \right)$$



## 45 Measurements

$$\frac{\langle g_p \rangle}{g_p} = \frac{\delta X}{X} = (-0.16 \pm 0.54) \cdot 10^{-5}$$

$Z \approx 0.7$  , 6 bn years ago

$$X = \alpha^2 \left( \frac{m_q}{\Lambda_{QCD}} \right)^{-0.09}$$

Flambaum  
Leinweber  
Thomas  
Young

GUT models :

Calmet, Fritzsch; Langecker, Segre, Strassl

$$\frac{\delta(m/\Lambda_{QCD})}{m/\Lambda_{QCD}} \sim 35 \frac{\delta \alpha}{\alpha}$$

weak / strong variation  
may be more important !

## **Measurements of $m_e/m_p \sim m_e/\Lambda_{QCD}$**

Tsanavaris, Webb, Murphy, Flambaum, Curran  
Phys. Rev. Lett. 2005

hyperfine 21 cm H/optical

Mg, Ca, Mn, Ti, C, Si, Zn, Cr, Fe, Ni

8 quasar absorption systems,  $0.24 < z < 2.04$

Measured  $X = \alpha^2 g_p m_e / m_p$

$$\frac{\delta X}{X} = (1.17 \pm 1.01) 10^{-5}$$

$$\frac{d \ln X}{dt} = (-1.43 \pm 1.27) 10^{-15} / \text{year}$$

No variation.

Combined with measurements of  $\alpha$ -variation

$$\frac{\delta(m_e/m_p)}{(m_e/m_p)} = (2.31 \pm 1.03) 10^{-5}$$

$$\frac{\delta(m_e/m_p)}{(m_e/m_p)} = (1.29 \pm 1.01) 10^{-5}$$

Recent result based on  $H_2$  measurements

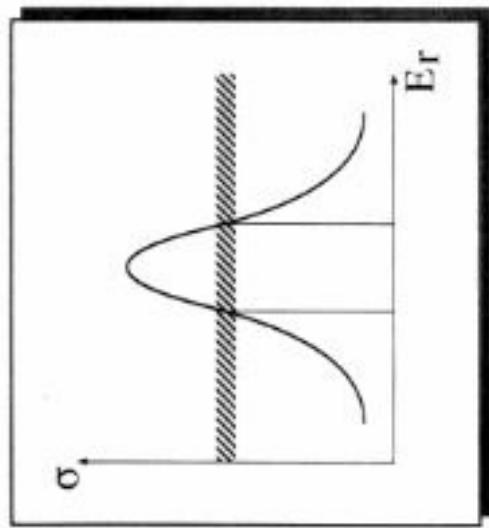
Reinhold, Bunning, Hollenstein, Ivanchik, Petitjean,  
Ubach 2005.

$$\frac{\delta(m_e/m_p)}{(m_e/m_p)} = (-2.4 \pm 0.6) 10^{-5}$$

Variation  $4\sigma$ !

# Oklo natural nuclear reactor

S. Lamoreaux and J. Torgerson, nucl-th/0309048 PRD(2004)



$n + ^{149}\text{Sm} \rightarrow ^{150}\text{Sm}$  cross-section.

Two solutions for the change of the resonance position  $E_r$ :

1.  $\Delta E_r = (-135 \pm 5) \times 10^{-3}$  eV
2.  $\Delta E_r = (-58 \pm 5) \times 10^{-3}$  eV

V. Flambaum and E. Shuryak, hep-ph/0212403: PRD (2004)

$$\Delta E_r = 1.7 \times 10^8 \text{ eV} \frac{\delta(m_s/\Lambda)}{m_s/\Lambda}$$

1.  $\frac{\delta(m_s/\Lambda)}{m_s/\Lambda} = (-0.80 \pm 0.03) \times 10^{-9}$
2.  $\frac{\delta(m_s/\Lambda)}{m_s/\Lambda} = (-0.34 \pm 0.03) \times 10^{-9}$

$1.8 \cdot 10^{-9}$  years ago

## **LABORATORY EXPERIMENTS - ATOMIC CLOCKS**

There are two types of atomic clocks:

1. Microwave (e.g.  $^{133}\text{Cs}$ , 6s hfs  $F=3 - F=4$  transition serves as definition of metric second; also Rb, Yb $^+$ , etc.).
2. Optical (Ca, Sr, Hg  $^1\text{S}_0 - ^3\text{P}_1$ , etc.)

Comparing rates of different clocks allows to study variation of fundamental constants.

Advantages:

1. Very narrow lines, sensitivity in  $\frac{\Delta\alpha}{\alpha}$  up to  $10^{-18}$  per year.
2. Larger  $Z$ ,  $q$  up to 60000 cm $^{-1}$ .
3. Simple interpretation ( $\dot{c}/c \mid_{t=today}$ ).

# Optical atomic clocks

TABLE II: Experimental energies and calculated  $q$  coefficients for transitions from the ground state to the state shown.

Atom/Ion	Z	State	Wavelength, Å	$q$ ( $\text{cm}^{-1}$ )	Reference
			Experiment		
Al II	13	$3s3p$	$^3P_0$	2674.30	146
		$3s3p$	$^3P_1$	2669.95	211
		$3s3p$	$^3P_2$	2661.15	343
		$3s3p$	$^1P_1$	1670.79	278
Ca I	20	$4s4p$	$^3P_0$	6597.22	125
		$4s4p$	$^3P_1$	6574.60	180
		$4s4p$	$^3P_2$	6529.15	294
		$4s4p$	$^1P_1$	4227.92	250
Sr I	38	$5s5p$	$^3P_0$	6984.45	443
		$5s5p$	$^3P_1$	6894.48	642
		$5s5p$	$^3P_2$	6712.06	1084
		$5s5p$	$^1P_1$	4608.62	924
Sr II	38	$4d$	$^3D_{3/2}$	6870.07	2828
		$4d$	$^3D_{5/2}$	6740.25	3172
In II	49	$5s5p$	$^3P_0$	2365.46	3787
		$5s5p$	$^3P_1$	2306.86	4860
		$5s5p$	$^3P_2$	2182.12	7767
		$5s5p$	$^1P_1$	1586.45	6467
Ba II	56	$5d$	$^3D_{3/2}$	20644.74	5844
		$5d$	$^3D_{5/2}$	17621.70	5976
Dy I	66	$4f^{10}5d6s$	$^3[10]_{10}$	5051.03	6008
		$4f^95d^26s$	$^3K_{10}$	5051.03	-23708
Yb I	70	$6s6p$	$^3P_0$	5784.21	2714
		$6s6p$	$^3P_1$	5558.02	3527
		$6s6p$	$^3P_2$	5073.47	5883
		$6s6p$	$^1P_1$	3989.11	4951
Yb II	70	$4f^{14}5d$	$^3D_{3/2}$	4355.25	10118
		$4f^{14}5d$	$^3D_{5/2}$	4109.70	10397
		$4f^{13}6S^2$	$^2F_{7/2}$	4668.81	-56737
Yb III	70	$4f^{13}5d$	$^3P_0$	2208.63	-27800
Hg I	80	$6s6p$	$^3P_0$	2656.39	15299
		$6s6p$	$^3P_1$	2537.28	17584
		$6s6p$	$^3P_2$	2270.51	24908
		$6s6p$	$^1P_1$	1849.50	22789
Hg II	80	$5d^36s^2$	$^2D_{5/2}$	2815.79	-56671
		$5d^46s^2$	$^2D_{3/2}$	1978.16	-44003
Tl II	81	$6s6p$	$^3P_0$	2022.20	16267
		$6s6p$	$^3P_1$	1872.90	18845
		$6s6p$	$^3P_2$	1620.09	33268
		$6s6p$	$^1P_1$	1322.75	29418
Ra II	88	$6d$	$^3D_{3/2}$	8275.15	18785
		$6d$	$^3D_{5/2}$	7276.37	17941

**Table 99.1.** Relative sensitivity of the hyperfine relativistic factors to the variation of  $\alpha$  (parameter  $\kappa$ ) and nuclear magnetic moments on the variation of the quark mass/strong interaction scale  $m_q/\Lambda_{QCD}$  (parameter  $\beta$ ) for atoms involved in microwave standards.

Z	Atom	$\kappa$	$\beta$
1	$^1\text{H}$	0.00	-0.100
1	$^2\text{H}$	0.00	-0.063
37	$^{87}\text{Rb}$	0.34	-0.074
48	$^{111}\text{Cd}^+$	0.6	-0.117
55	$^{133}\text{Cs}$	0.83	0.127
70	$^{171}\text{Yb}^+$	1.5	-0.117
80	$^{199}\text{Hg}^+$	2.3	-0.117

Using parameters  $\kappa$  and *beta* we can present dependence of the microwave standards on the fundamental constants:

$$\frac{\partial \ln f}{\partial t} = \frac{\partial \ln V}{\partial t} \quad (99.5)$$

$$V = cR_\infty \cdot \frac{m_e}{m_p} \cdot \alpha^{2+\kappa} \cdot \left(\frac{m_q}{\Lambda_{QCD}}\right)^\beta \quad (99.6)$$

In comparison of two microwave standards the factors  $cR_\infty$  and  $m_e/m_p$  are cancelled out. However, in comparison of optical and microwave standards the factor  $m_e/m_p$  survives. Its dependence on the fundamental constants is the following

$$\partial \ln \frac{m_e}{m_p} = \partial \ln \left[ \frac{m_e}{\Lambda_{QCD}} \cdot \left(\frac{m_q}{\Lambda_{QCD}}\right)^{-0.048} \right] \quad (99.7)$$

We may assume that the electron mass and all quark masses have the same relative variation. This assumption seems to be natural if the Higgs mechanism of mass generation is correct.

Comparing atomic clocks one can study:

Atomic	optical/optical	$\alpha^2$
	optical/hyperfine	$\alpha^2, m_{e,q}/\Lambda_{QCD}$
	hyperfine/hyperfine	" "
Molecular	hyperfine/rotational	" "
	hyperfine/ $\Lambda$ -doubling	" "
	rotational/optical	" "

		Experiment	$\frac{1}{\alpha} \frac{d\alpha}{dt} (10^{-15}/\text{year})$
Marion et al	2003	$\frac{\text{Rb(hfs)}}{\text{Cs(hfs)}}$	$(0.05 \pm 1.3)^a$
Bize et al	2003	$\frac{\text{Hg}^+(\text{opt})}{\text{Cs(hfs)}}$	$(-0.03 \pm 1.2)^a$
Fisher et al	2004	$\frac{\text{H(opt)}}{\text{Cs(hfs)}}$	$(-1.1 \pm 2.3)^a$
Peik et al	2004	$\frac{\text{Yb}^+(\text{opt})}{\text{Cs(hfs)}}$	$(-0.2 \pm 2.0)$
Bize et al	2004	$\frac{\text{Rb(hfs)}}{\text{Cs(hfs)}}$	$(0.1 \pm 1)^a$

<sup>a</sup> assuming  $m_q/\Lambda = \text{Const.}$

Combined results:

$$\frac{\partial \ln \alpha}{\partial t} = (-0.9 \pm 2.9) \times 10^{-15} \text{yr}^{-1}$$

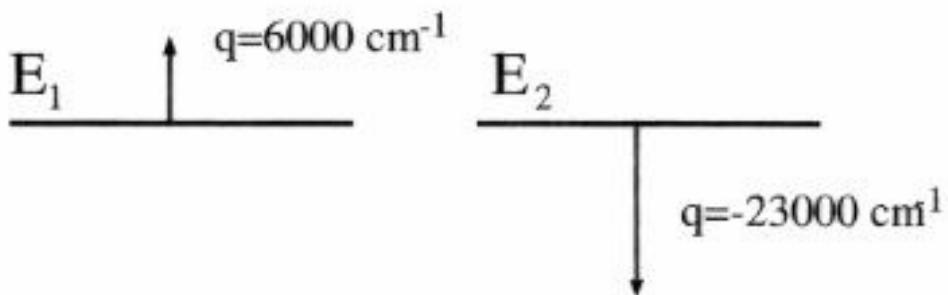
$$\frac{\partial \ln (m_q/\Lambda_{QCD})}{\partial t} = (-4 \pm 10) \times 10^{-15} \text{yr}^{-1}$$

There is a possibility of  $10^{10}$  times enhancement due to “degenerate” energy levels of different nature! Example: Dy atom.

$$1. \text{ } 4f^{10}5d6s, \quad E_1 = 19797.96\ldots \text{ cm}^{-1}$$

$$2. \text{ } 4f^95d^26s, \quad E_2 = 19797.96\ldots \text{ cm}^{-1}$$

$$\text{Interval } \omega = E_2 - E_1 \sim 10^{-4} \text{ cm}^{-1} \sim 10^{-9} E_1.$$



$$\omega = \omega_0 + (q_1 - q_2) 2 \frac{\Delta \alpha}{\alpha} =$$

$$= 10^{-4} \text{ cm}^{-1} + 60000 \text{ cm}^{-1} \frac{\Delta \alpha}{\alpha}$$

$$\frac{\Delta \omega}{\omega} (1 \text{ year})_{\text{Lab}} \sim \frac{\Delta \omega}{\omega} (10^{10} \text{ years})_{\text{astro}}$$

Preliminary result: UC Berkely

$$|\frac{\partial \ln \alpha}{\partial t}| < 4.3 \times 10^{-15} \text{ yr}^{-1}$$

## CONCLUSIONS

BBN/CMB data may be interpreted as variation of  $m_q/\Lambda_{QCD}$ .

MM method provided sensitivity increase  $\sim 100$  times. Many lines, positive and negative shifters - control of systematics.

Keck data- 3 independent optical samples, 143 systems- variation of  $\alpha$ .

VLT data- no variation.

Undiscovered systematics or spatial variation?

$m_e/m_p$ : 21 cm H/optical- no variation;  
 $H_2$  (Paris-Amsterdam-Peterburg)-variation!

Oklo data: variation of  $m_q/\Lambda_{QCD}$  !?

- Atomic clocks are very sensitive to present time variation of  $\alpha$  and  $m_q/\Lambda_{QCD}$ . Transition between close levels - a billion times enhancement.