

# The Neutrino Mass from Tritium $\beta$ Decay

Ernst Wilhelm Otten

Email: ernst.otten@uni-mainz.de



- Introduction
- Tritium  $\beta$  decay experiments in Mainz
- The improved Mainz Experiment
- Analysis and Discussion
- Summary and Outlook

Present group members:

Jochen Bonn  
Uta Bornschein  
Beate Degen  
Christian Weinheimer  
E. O.

Visitors: from Troitzk:

Vladimir Lobashev  
Oleg Kazachenko  
Juli Yerashkin

from Oubna/Prague:

Alois Kovalik

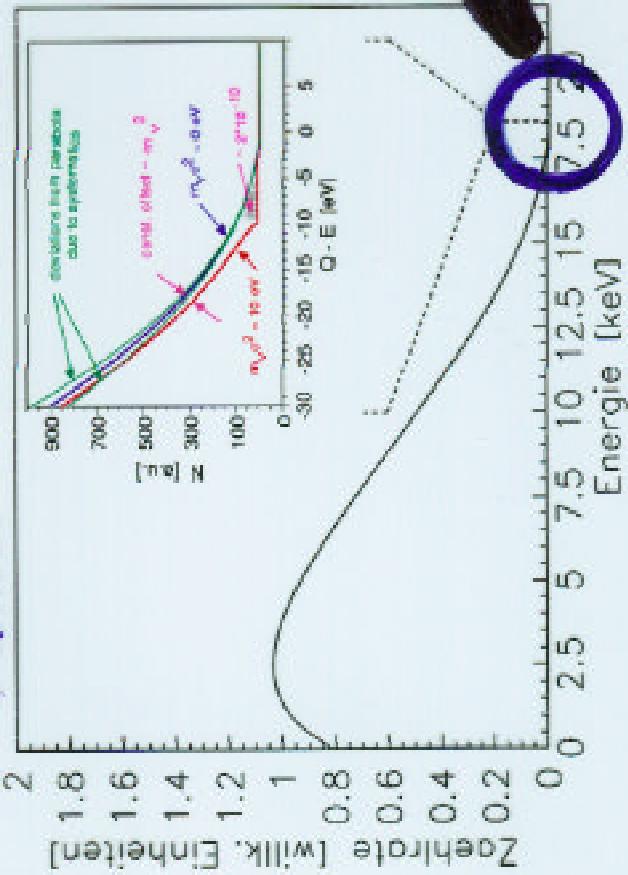
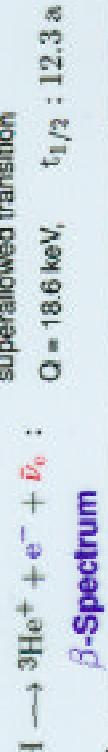
Collaborator in  $T_2$ -film physics:

Paul Leidner (Konstanz)

Fresh Diploma Students as from 1999:

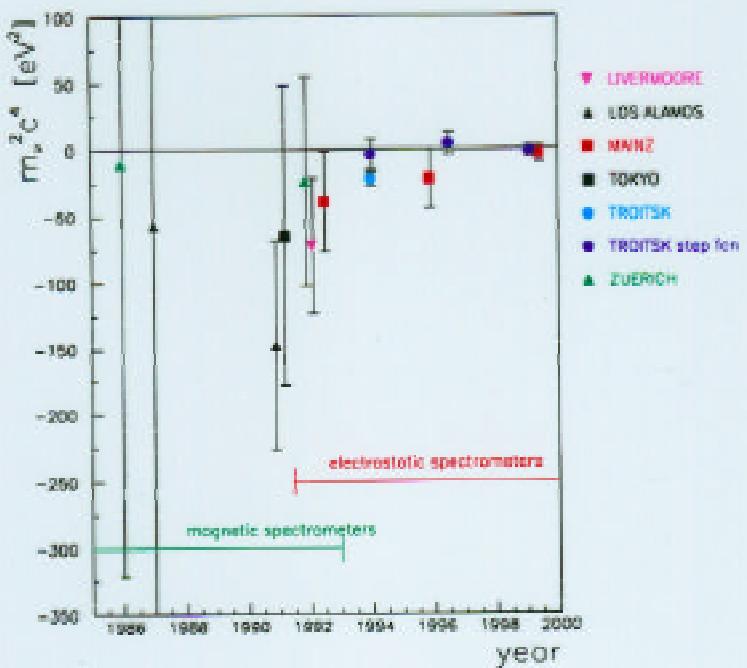
Lars Fickinger  
Christine Krämer  
Holger Ullrich

## Direct measurement of $m_{\nu_e}$



if more than one mass eigenstate contributes (not resolved):  $\overline{m_\nu^2} := \sum_i |U_{ei}|^2 \cdot m_i^2$

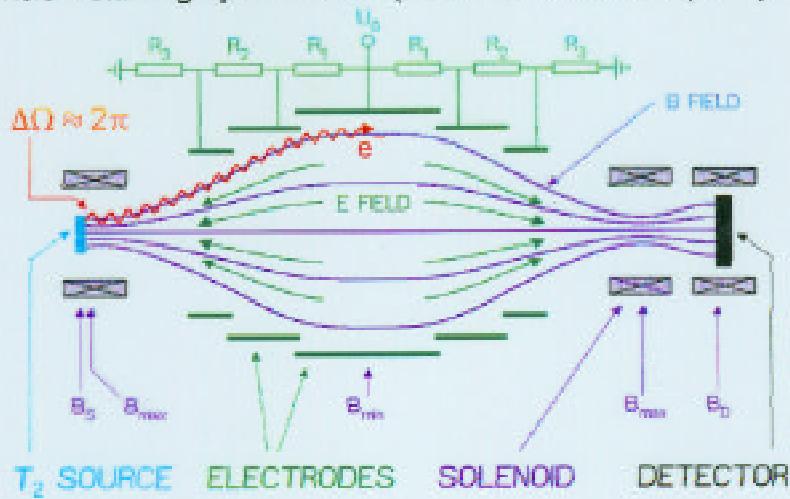
## Tritium $\beta$ decay: last decade



- 2 running experiments: Mainz, Troitsk
- Mainz 1991/1994 and Troitsk 1994::
  - only data close to endpoint:  $m_{\nu}^2 \approx 0$
  - down to 500 eV below endpoint:  $m_{\nu}^2 \approx -100 eV^2$
  - undetected additional energy loss

## Magnetic Adiabatic Collimation + Electrostatic filter

"Solenoid Retarding Spectrometer" (Nucl. Inst. Meth. B63 (1992) 345)



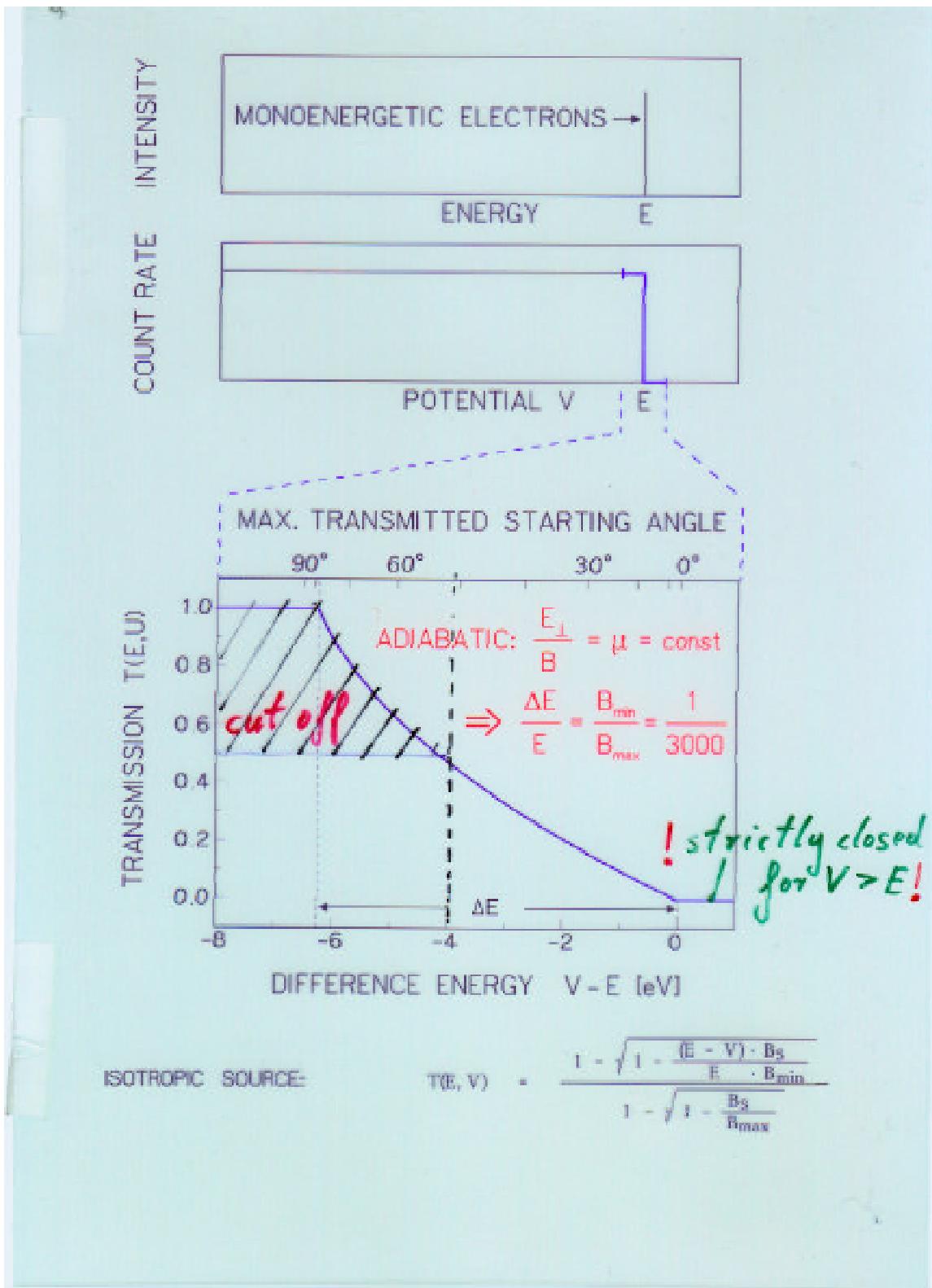
$$\vec{F} = (\vec{\mu} \vec{\nabla}) \vec{B} + q \vec{E} \quad \mu = \frac{E}{B} = \text{constant}$$

WITHOUT E FIELD:

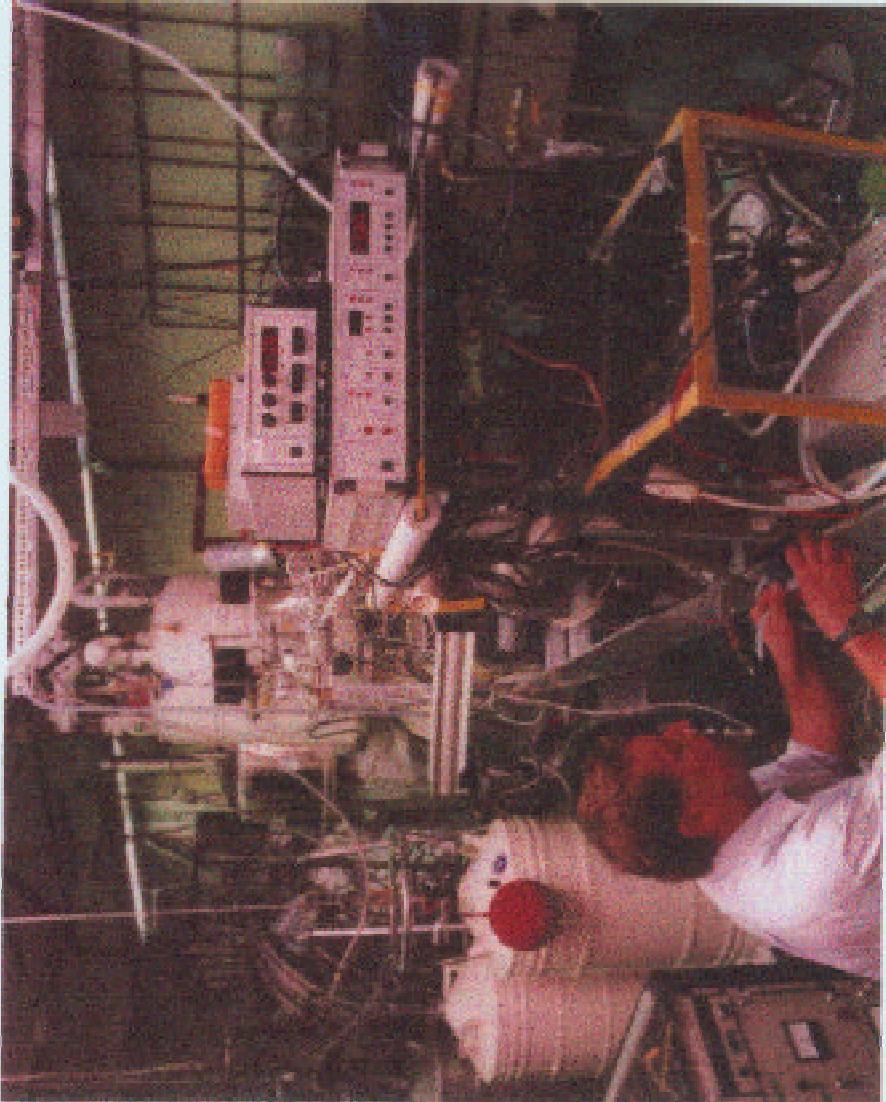


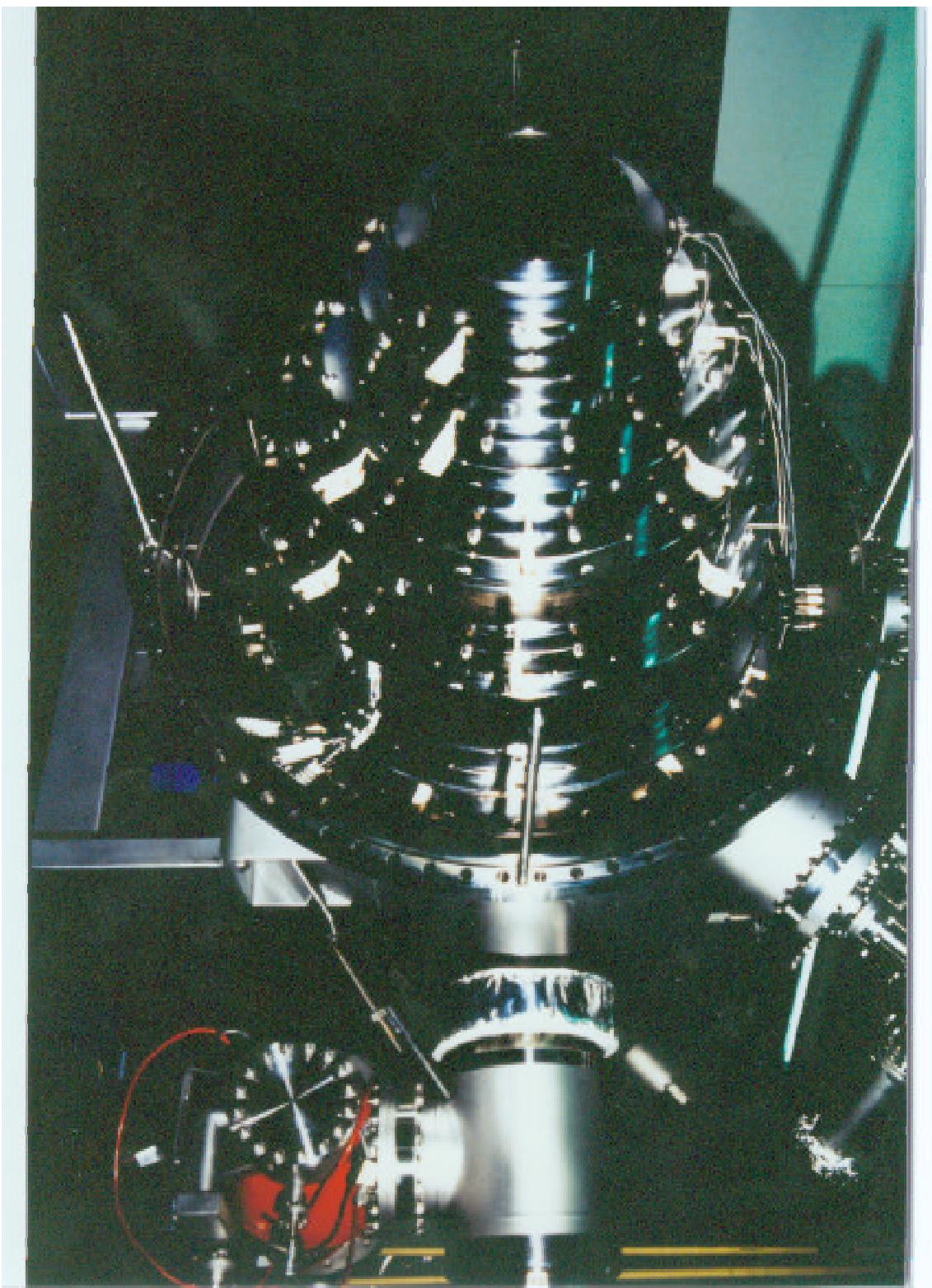
- magnetic guiding field  
→  $\Delta\Omega \approx 2\pi$
- adiabatic trans. $E_{\perp} \rightarrow E_{||}$  + electrostatic retardation  
→  $\Delta E \approx 4 - 6 \text{ eV}$

- performs point to point image
- keeps off background originating outside flux tube

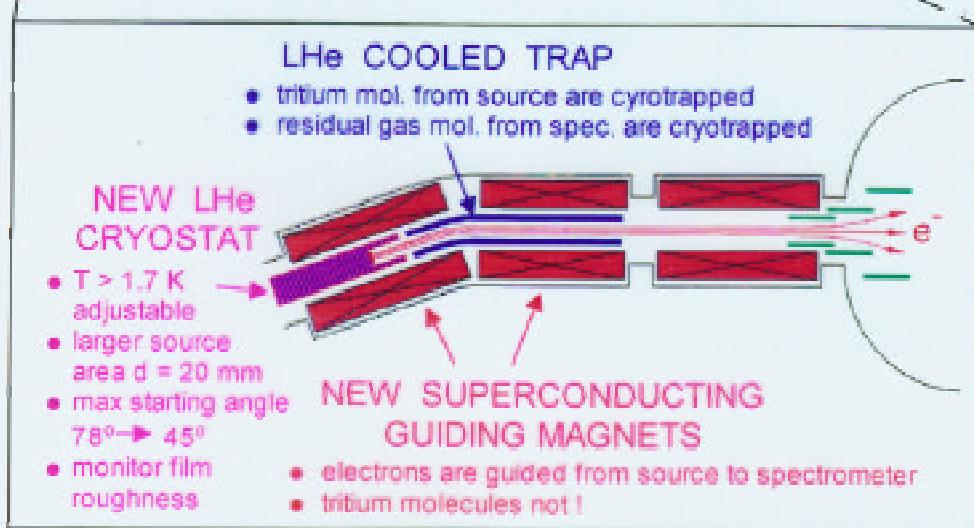
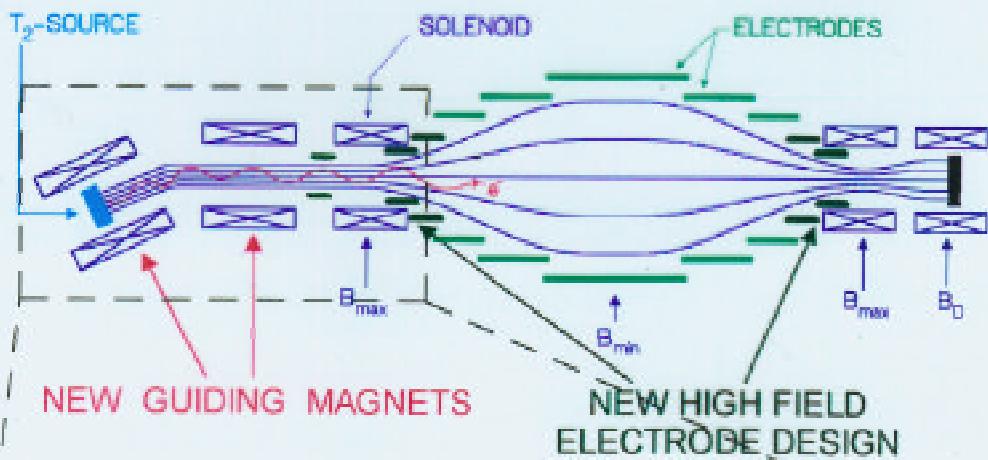






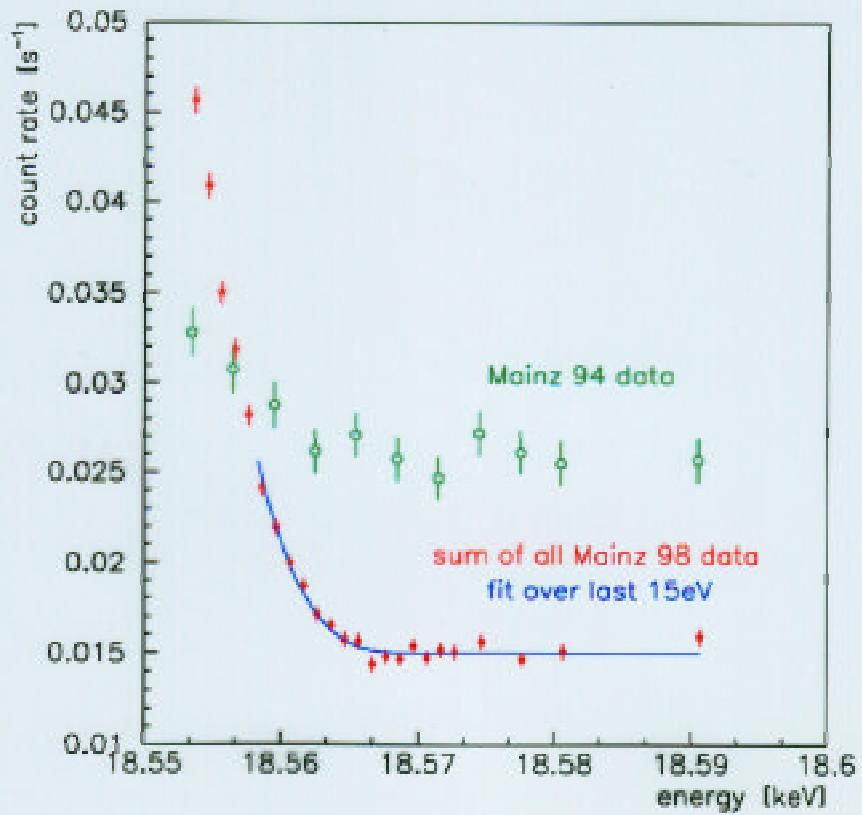


## IMPROVEMENTS OF THE EXPERIMENTAL SETUP



## Summing up all 1998 data

Q3+Q4+Q5



## The Fitfunction

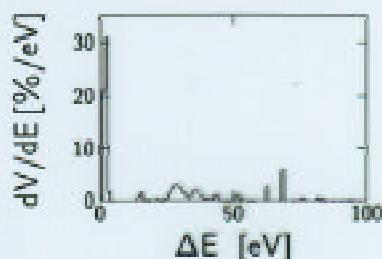
$$N(E) = \text{amp} \sum_i P_i \epsilon_i^2 \sqrt{1 - \frac{m_\nu^2 c^4}{\epsilon_i^2}} \otimes f_{\text{response}} + BG$$

$f_{\text{resp}}$   $\equiv$  Charging  $\otimes$  TF  $\otimes$  EL  $\otimes$  BS  $\otimes$  I,  
with  $\epsilon_i = E_0 - V_i - E$ : final states

final states:

sudden approx.

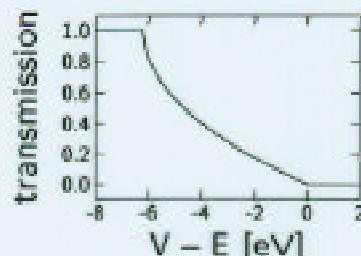
(Kolos, Fackler)



TF:

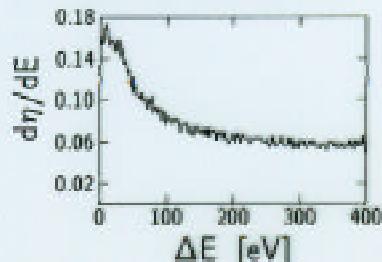
transmission fcn

(analytically known)



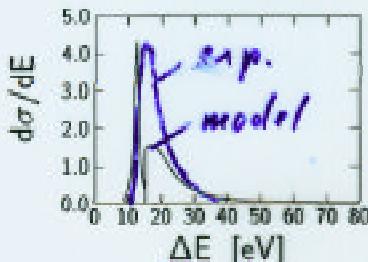
BS: backscatter:

MC-calculations



EL: energy-loss:

$^{83m}\text{Kr}$ -measurements



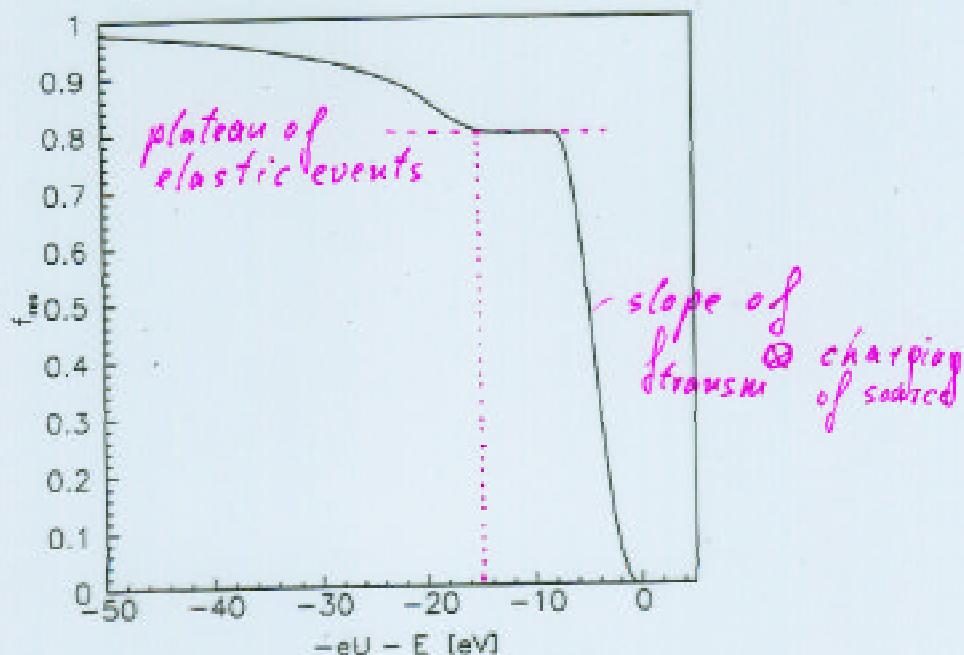
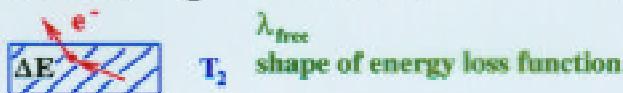


Figure 2. Normalised response function of the spectrometer  $f_{res}$  for a monoenergetic electron source of energy  $E$  in dependence on the retarding energy  $-eU$ . The energy loss  $f_{loss}$  and the charging effect  $f_{charge}$  are calculated for a source thickness of 490 Å as used for measurements Q3-Q5.

## Systematic uncertainties

- Inelastic Scattering      film thickness      (49 %)



- Final states      (effects due to solid state)      (37 %)

spectator excitation  
changes of excited states energy levels

- $T_2$  film charging up      (new)      (14 %)



- $T_2$  film roughness      (avoided)      (-)



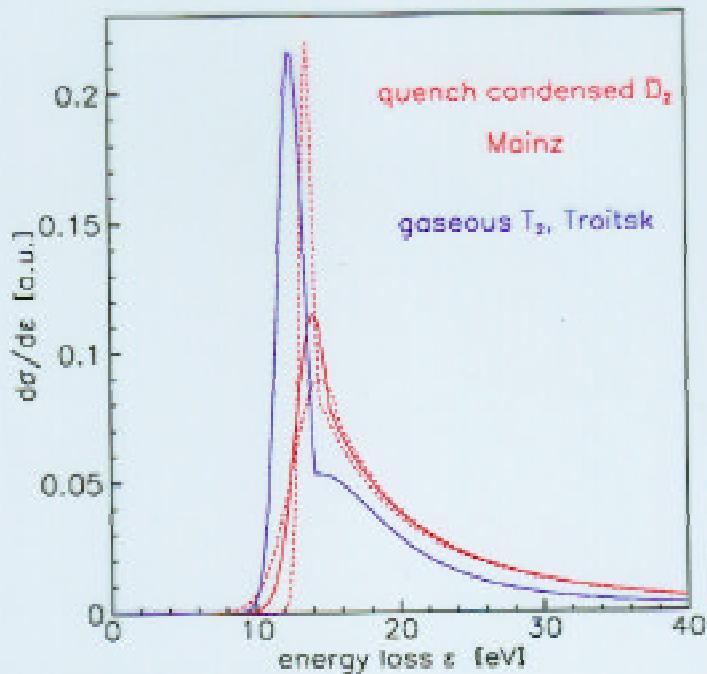
- Backscattering      (small)      (< 1%)



- Detector efficiency      (small)      (-)

(contribution to systematic uncertainty for Q5, last 70 eV  $\leftrightarrow$ )

## Energy loss function



Determination with conversion  $e^-$  through  $D_2$  films:

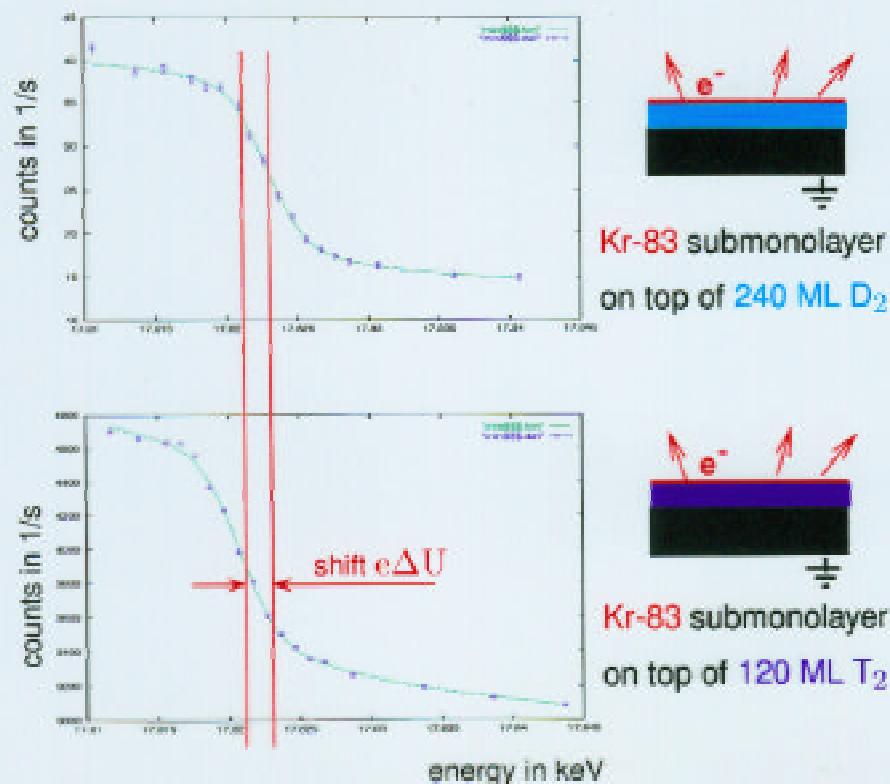
- → shape for quench condensed film is significantly different to shape for gas!  
Influence of Pauli blocking for excited molecular states!
- →  $\sigma_{tot} = 3.00 \pm 0.16 \cdot 10^{-18} \text{ cm}^2$ ;  
14% smaller than expected  
Influence of Pauli blocking for excited molecular states!

## Charging up of T<sub>2</sub> film

Shift of endpoint energy (run 1997)

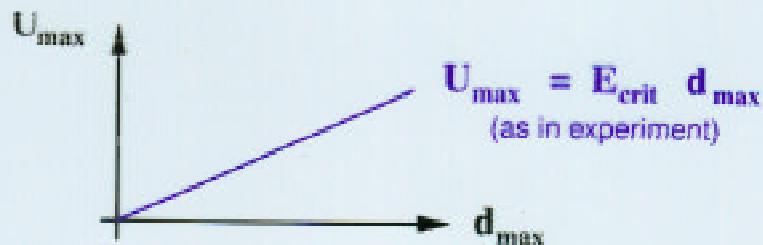
Charging up of the T<sub>2</sub> film (40 mCi)

→ Measurements with K conversion electrons of Kr-83



## Does microscopic picture fit?

1) Expectation from picture:



2) Measured critical field  $E_{\text{crit}}$ :

$$E_{\text{crit}} = 6 \text{ V} / 288 \text{ Monolagen}$$

$$\rightarrow W_{\text{pass}} = e \cdot E_{\text{crit}} \cdot d_{\text{ML}} \approx 250 \text{ K}$$

(right order of magnitude !)

⊕ charging up effect probably understood

⊖ deterioration of energy resolution

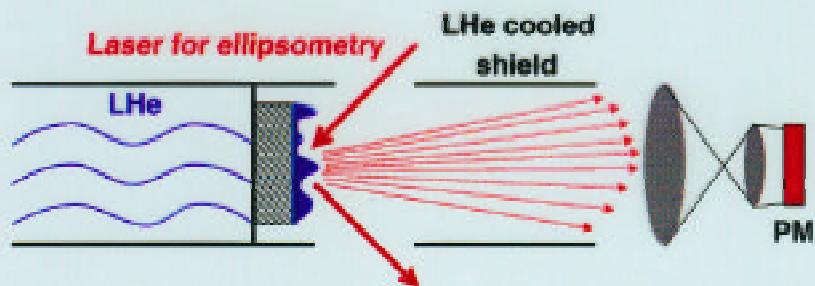
(10% – 90% : 3.5 eV → 6.0 eV)

• take effect into account in analysis

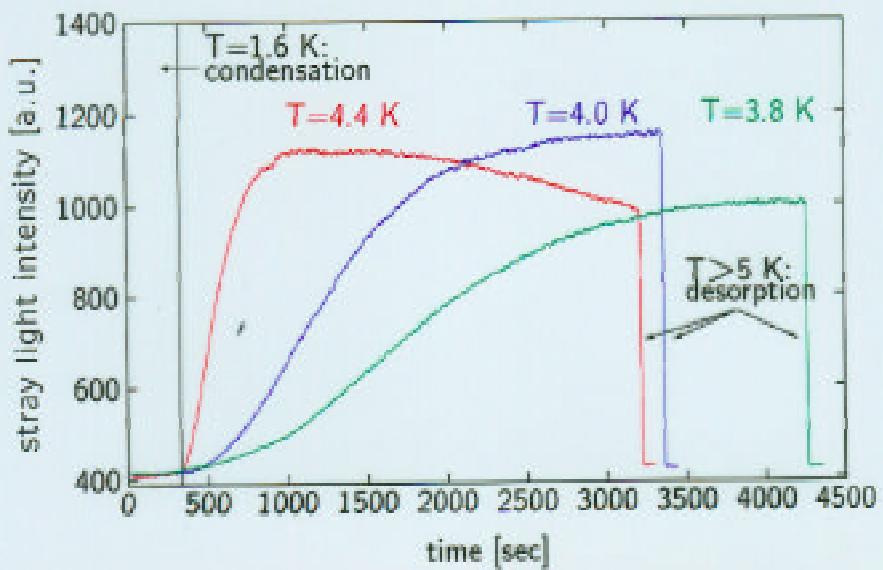
estimate for uncertainty:  $\approx 50\%$  of total effect

## Detection of Roughening Transition

### Observation of stray light

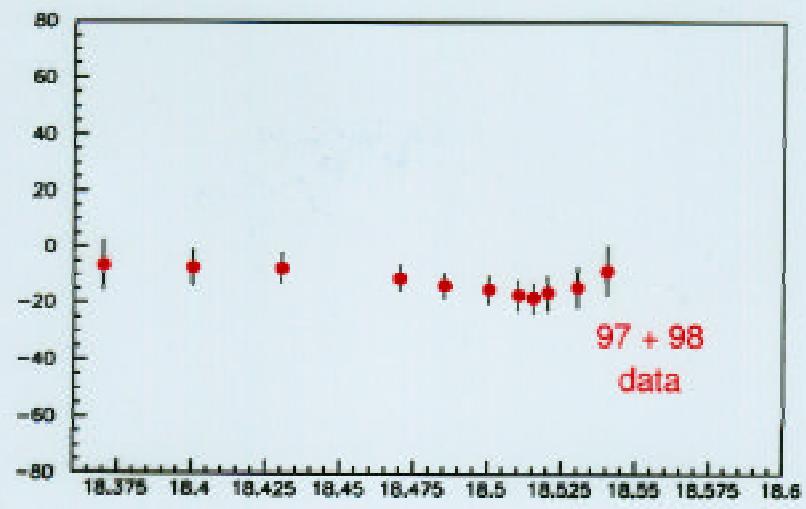


## Temperature Dependence of Roughening Transition

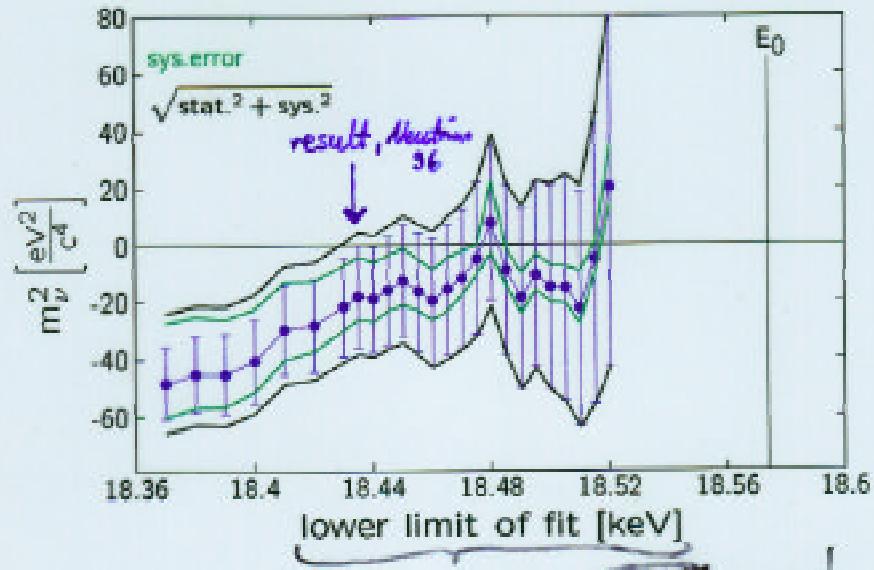


**Extrapolated time constants for  $T_2$**   
(ok, if  $T_2$  decays do not matter)

$T$	$4.2$ K	$2.8$ K	$1.6$ K
$\tau$	hours	days	years



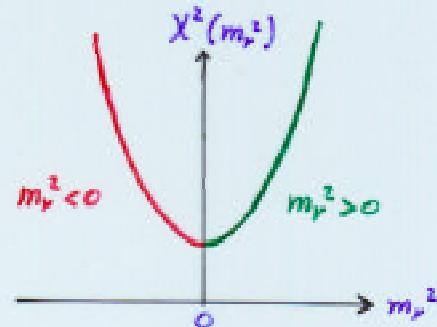
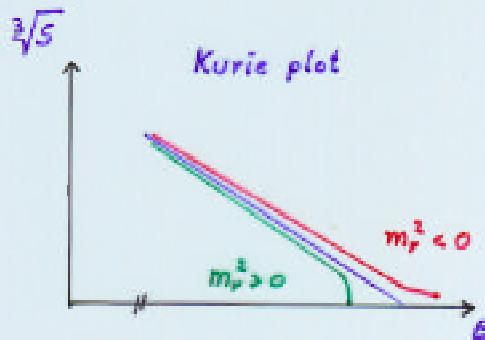
## Result 1994



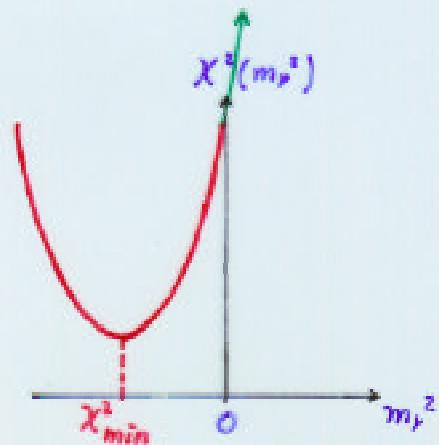
- fit abuses fit parameter  $m_{\nu}^2$  to compensate systematic discrepancies between data and fit function
- trend explainable by missing energy loss

## How to treat negative $m_\nu^2$ - values in the fit function ?

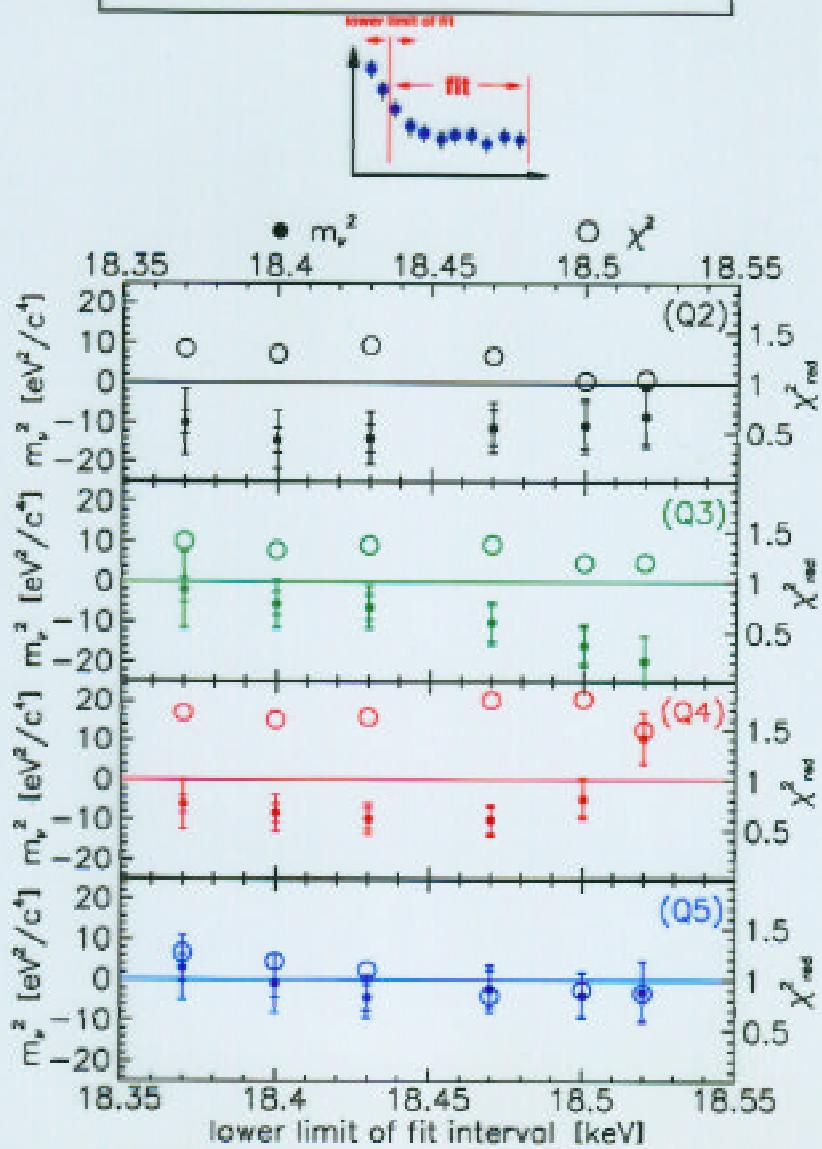
Find a suitable analytical continuation of  $\beta$ -spectrum beyond  $E_0$  which produces a parabolic  $\chi^2(m_\nu^2)$  - curve around  $m_\nu^2 = 0$  to accomodate statistical fluctuations of excess count rate



However:  
systematic distortion of  
spectrum, e.g. by under-  
estimated fraction of  
inelastic processes  
produce significant but  
unphysical negative  
 $m_\nu^2$ -values



## $m_\nu^2(\text{fit})$ versus fit interval



## Mainz upper limits on neutrino mass 2

### 2.) If one believes in step as correct solution:

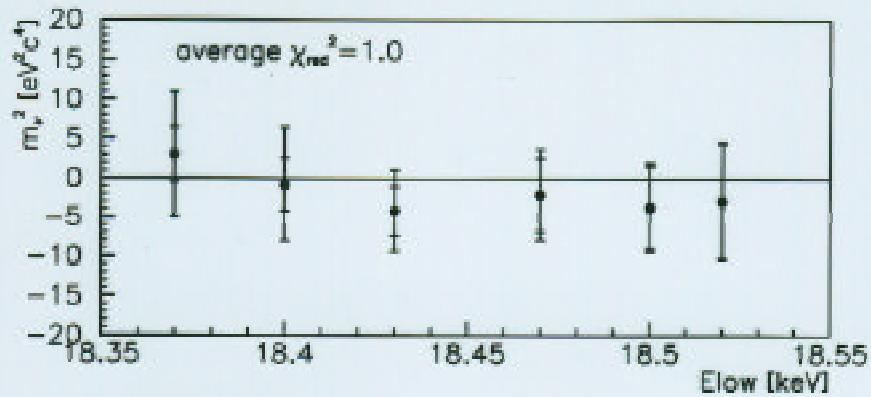
→ fit step and subtract it (only possible for Q4):

last 70 eV (Q4, 1998 run II):

$$m_\nu^2 c^4 = -1.8 \pm 5.1 \pm 2.0 \text{ eV}^2$$

$$\rightarrow m_\nu c^2 \leq 3.0 \text{ eV} \quad (95\% \text{C.L., unified approach})$$

### 3.) Considering Q5, 1998 run III alone:



→ Standardanalysis:

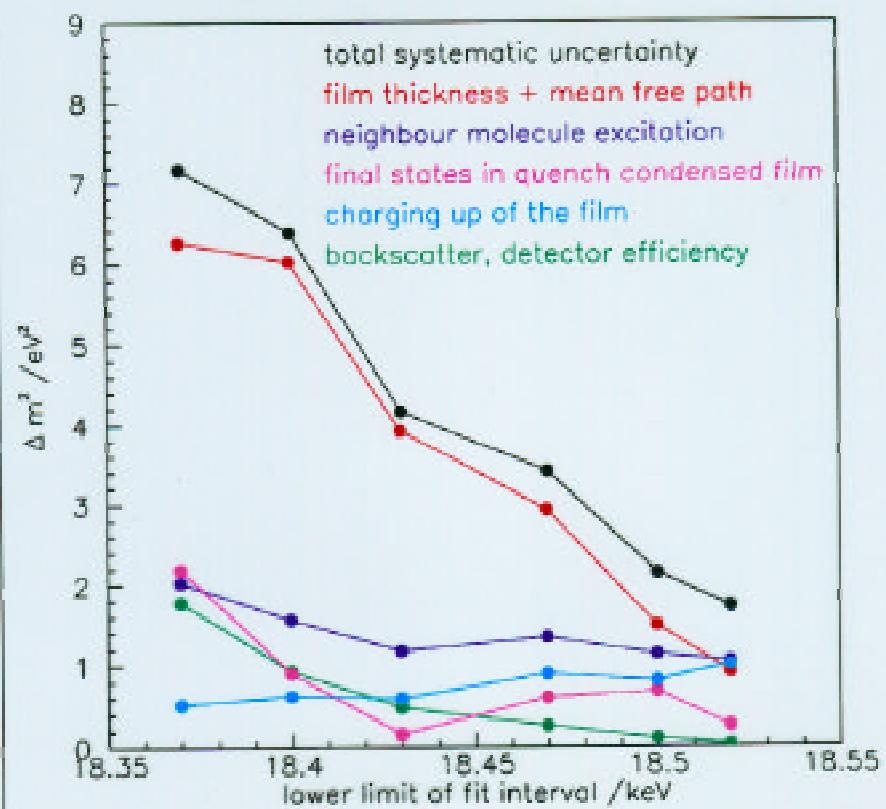
last 70 eV (Q5, 1998 run III):

$$m_\nu^2 c^4 = -3.7 \pm 5.3 \pm 2.1 \text{ eV}^2$$

$$\rightarrow m_\nu c^2 \leq 2.8 \text{ eV} \quad (95\% \text{C.L., unified approach})$$

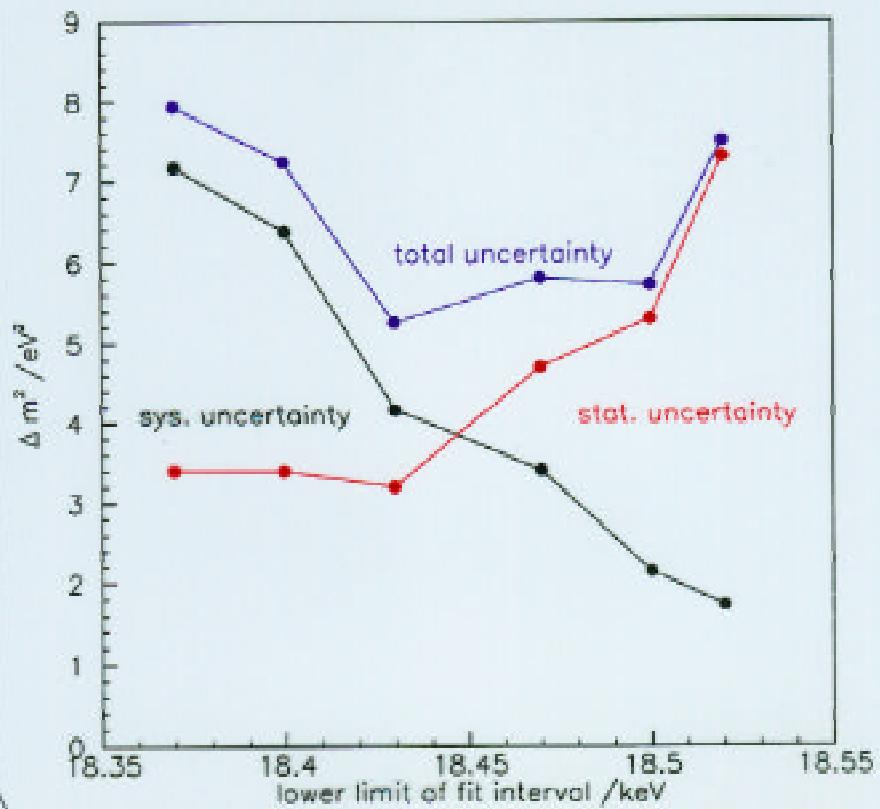
## Systematic uncertainties

1998 run III: Q5



## Statistical and systematic uncertainties

1998 run III: Q5

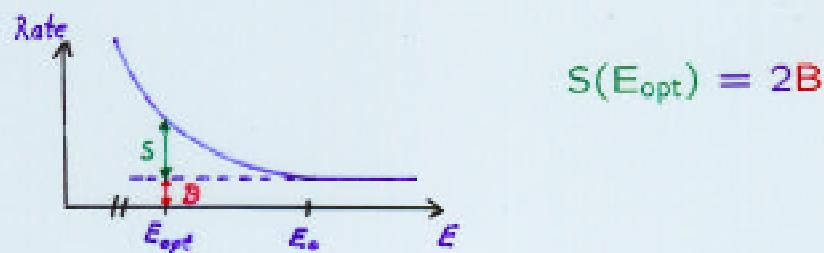


## Statistical Error $\delta m_\nu^2$

given:  $S = \text{Signal rate}$   
 $B = \text{Background rate}$

$$\delta m_\nu^2(E) = \frac{2}{3c^4} (E_0 - E)^2 \sqrt{\frac{(S + B)/t}{S}}$$

Optimal point in the spectrum



There the dependence on

- source strength R
- background rate B
- measuring time t

is given as

$$\delta m_\nu^2 \propto R^{-\frac{2}{3}} \cdot B^{\frac{1}{6}} \cdot t^{-\frac{1}{2}}$$

## Correlation of errors

- of  $(\text{mass})^2$  :  $\delta m_\nu^2$  and
- Endpoint  $E_0$ :  $\delta E_0$

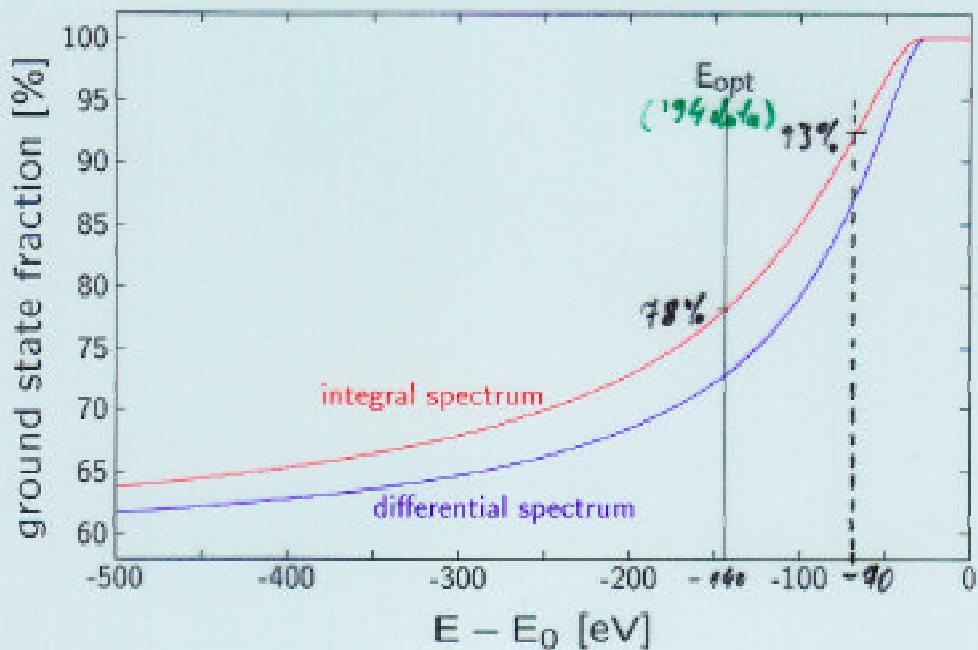
as function of point of measurement  $E$

$$\delta m_\nu^2(E) = \frac{2}{c^4}(E_0 - E)\delta E_0$$

Example (1): Introduce an **external** value of  $E_0$  from some other measurement into the fit which is **too large**, then the fit finds:  $m_\nu^2 > 0$  (Ljubimov effect)

Example (2):  $E_0$  is determined from fitting the experimental spectrum, but found **too low**, because the fraction of inelastic events has been underestimated than the fit yields:  $m^2 < 0$  (Mainz effect and others)

## Fraction of Ground State Transitions in $T_2$ $\beta$ -Decay

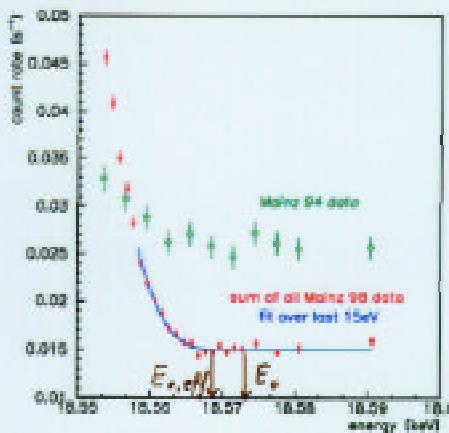


## Mainz upper limits on neutrino mass 1

### 1.) Decorrelate $m_\nu^2$ from systematics:

Sum of all 1998 data (Q3+Q4+Q5) (taken under same conditions)

- Take last 15 eV of  $\beta$  spectrum
  - free of systematics (atomic physics thresholds)
  - no influence from "Troitsk-like" anomaly as observed in Q4
- Add two data points at 18470 eV and 18500 eV
  - to decorrelate  $m_\nu^2$  from endpoint  $E_0$  and amplitude
  - minor influence of systematics
  - minor influence from "Troitsk-like" anomalies



$$m_\nu^2 c^4 = -0.1 \pm 3.8 \pm 1.8 \text{ eV}^2 \quad (\chi^2/\text{d.o.f.} \approx 1)$$

$$\rightarrow m_\nu c^2 \leq 2.9 \text{ eV} \quad (95\% \text{C.L., unified approach})$$

## Summary

- Present MAC-E-filters have reached mass limit  $m_\chi$  well below 3eV
- Old puzzle of "negative"  $m_\chi^2$  has been solved: tricky excess of energy losses!
- Residual anomalies show up on a much finer scale, so close to the end point that they can hardly be caused by misinterpreting energy losses. They seem to vary in time
- Mainz is shortcircuiting this difficulty by choosing for the evaluation either "clean runs" or a data interval  $\leq 15\text{eV}$  below  $E_0$
- Present instruments in Troitzk and Mainz will eventually reach the mass limit of 2eV will probably be able to decide whether residual anomaly is a physics or an instrumental effect
- We need stronger instruments to break the astrophysically relevant 1eV limit and to resolve residual anomalies in the spectrum or search for new ones