

Fundamental Neutron Physics III

symmetry breaking and the neutron electric dipole moment

Geoffrey Greene

University of Tennessee / Oak Ridge National Laboratory

*Parity Violation and Spontaneous Symmetry
Breaking*

"It is generally assumed on the basis of some suggestive theoretical symmetry arguments that nuclei and elementary particle can have no electric dipole moments. It is the purpose of this note to point out that although these theoretical arguments are valid when applied to molecular and atomic moments whose electromagnetic origin is well understood, their extension to nuclei and elementary particles rests on assumptions not yet tested"

E.M.Purcell and N.F.Ramsey,
Physical Review 78, 807 (1950)



Edward Purcell



Norman Ramsey

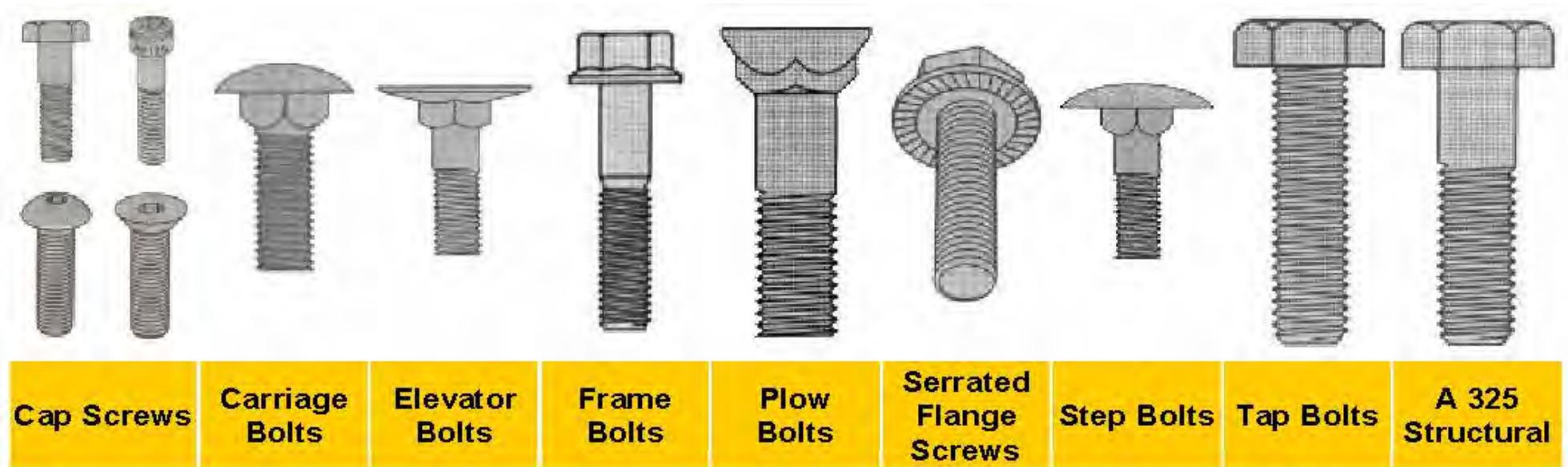
A Short History of Symmetry Violation

- 1863 (94 BP) Pasteur notes parity “violation” in organic molecules***
- 1950 (7 BP) Purcell and Ramsey suggest that parity violation must be
subject to experimental confirmation
(Ramsey gets 50-1 odds from Feynman)***
- 1951 (6 BP) First experiment specifically designed to look for a parity
violation (neutron EDM at ORNL)***
- 1956 (1 BP) Lee and Yang propose parity violation in weak interactions to
explain the “Tau-Theta” problem and suggest specific
experiments.***
- 1957 Wu, Ambler, et. al. and Garwin, et. al., Conclusively
demonstrate that parity is violated in the weak interaction
Landau suggests that CP is the “Real” symmetry***
- 1964 Christianson, et. al., demonstrate that CP is violated in K-decay***

Brief Digression

Spontaneous Symmetry breaking

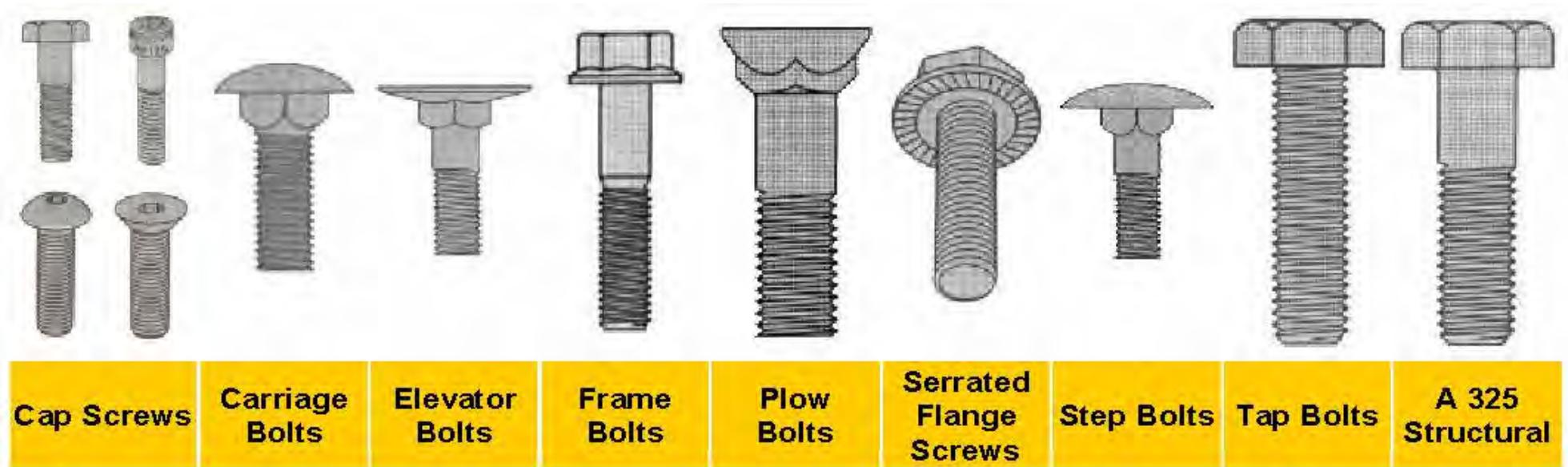
In the Universe of Nuts and Bolts



PARITY IS VIOLATED

If I randomly select a screw from the hardware bins At Home Depot...It will be RIGHT-HANDED

In the Universe of Nuts and Bolts



PARITY IS VIOLATED

***This is an example of a
“Broken Symmetry”***

Broken Symmetry

A situation in which the ground state of a many-body system has a lower symmetry than the Hamiltonian which defines the system.*

**also may apply to the vacuum state of a relativistic quantum field theory*

Some Characteristics of "Spontaneous Symmetry Breaking"

- *There is an underlying symmetry to the system.*
- *The physical state has lower symmetry than the underlying symmetry*
- *The symmetry breaking may not be complete.*
- *Incomplete symmetry breaking may be manifested by a residue of other symmetry states or domains in which the other symmetry is manifested*

Incomplete Symmetry Violation is Often an Indication of Broken Symmetry

*Threads on bicycle pedals
come in symmetric pairs*

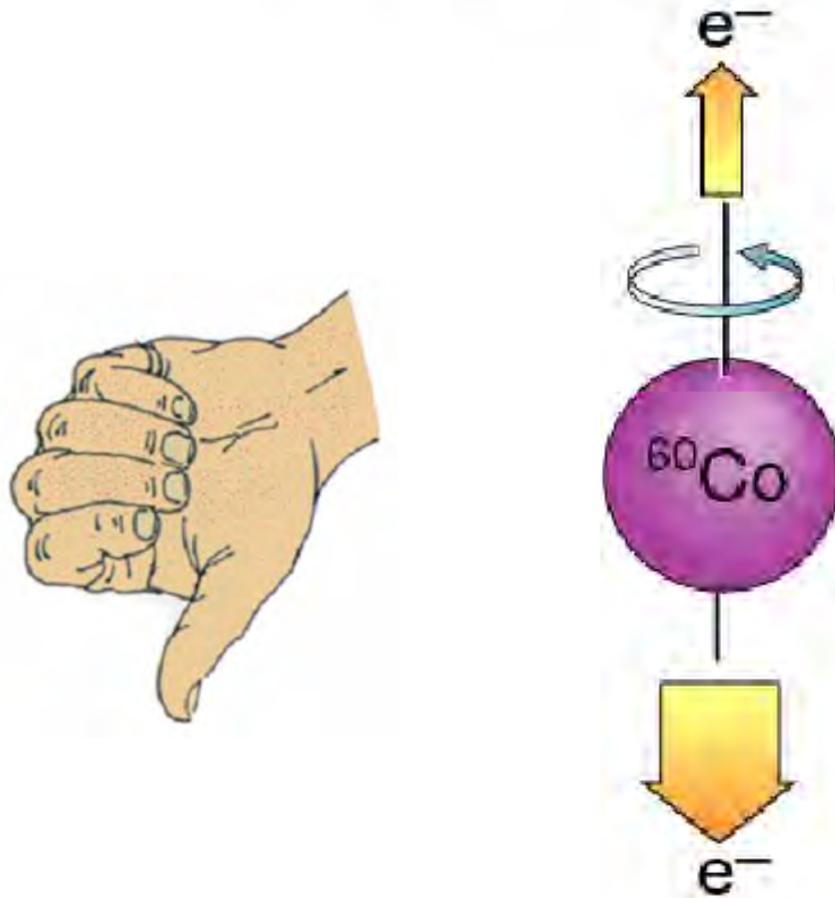


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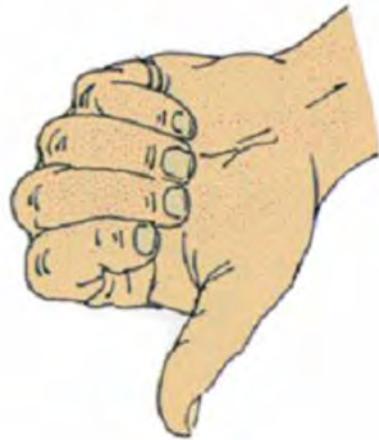
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gas bottles may be
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*Wu, Ambler, Hudson, Hoppes, Hayward
(NBS) 1957*

***At the Fundamental Level,
the Nuclear Weak Force Violates Parity***



*Wu, Ambler, Hudson, Hoppes, Hayward
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Is This a Broken symmetry?

The Cosmic Baryon Asymmetry

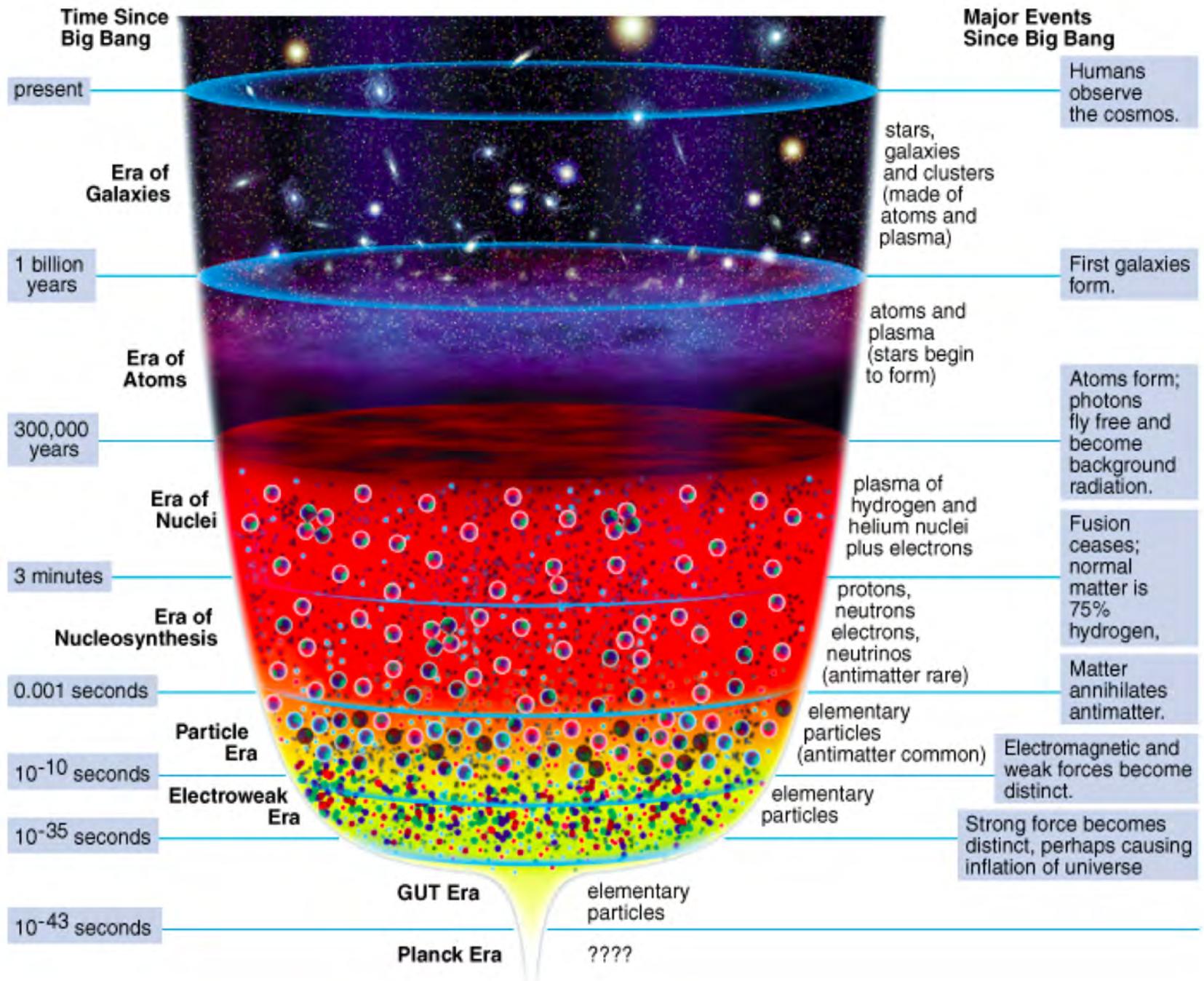
The Cosmic Baryon Asymmetry

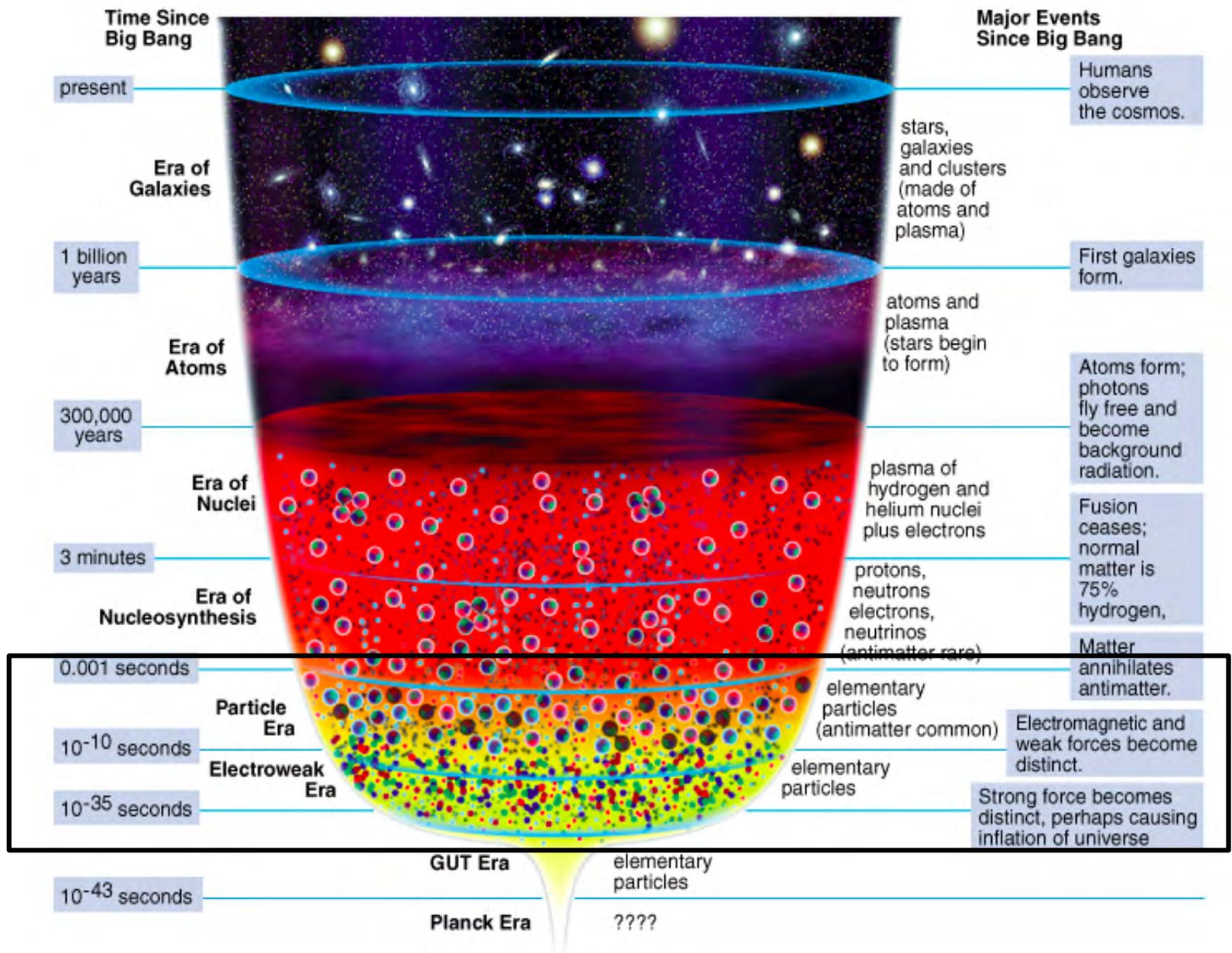
Observation:

As best we can determine, the universe consists of Matter.

There is essentially NO Antimatter.

Is This a Broken symmetry?





Just after Inflation, there were equal amounts of Matter and Antimatter.

If nothing else happened, all matter and antimatter would annihilate leaving...

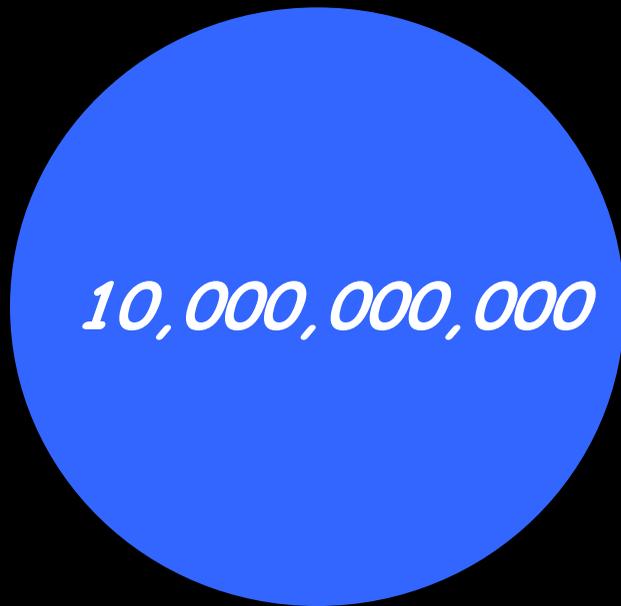
NOTHING!

***Today, the Universe consists of matter and
there is essentially NO anti-matter***

This is the

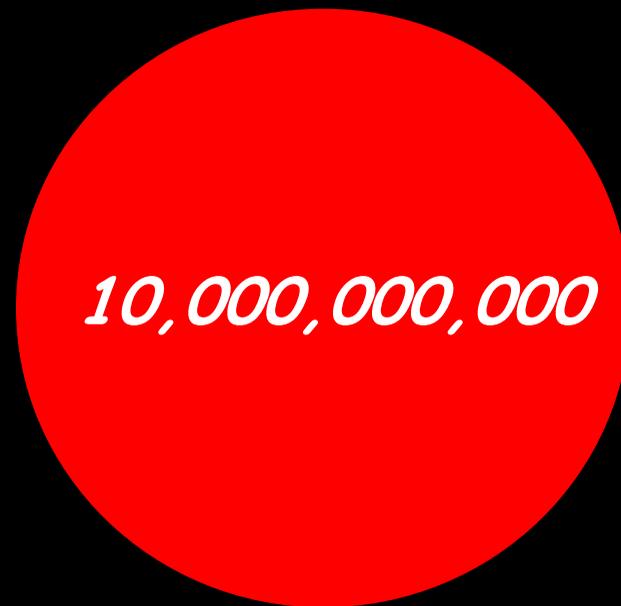
“Baryon Asymmetry Problem”

Matter and Antimatter Just After Inflation



10,000,000,000

Matter



10,000,000,000

Anti- Matter

Matter and Antimatter

$\sim 10^{-6}$ s later



10,000,000,000

Matter



9,999,999,999

Anti- Matter

Matter and Antimatter

Now

•
1

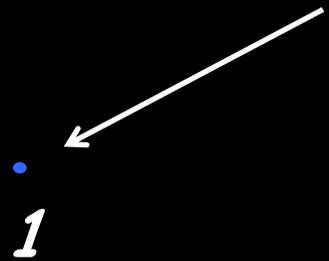
Matter

Anti- Matter

Matter and Antimatter

Now

*That's us...and
everything we can see*



1

Matter

Anti- Matter

Generating a Matter-Antimatter Asymmetry

A. D. Sakharov, JETP Lett. 5, 24 (1967)

Sakharov Process Requires Three Things:

- 1. The process must violate Baryon Number Conservation*
- 2. There must be a period of Non-Thermal Equilibrium*
- 3. The process must violate Time Reversal Non-Invariance*



A. Sakharov

Question:

Can the T violation needed to generate the matter-antimatter asymmetry when the universe was $10^{-6}s$ old be related to an observable quantity today?

The Neutron Electric Dipole Moment
An example of T violation

Discrete Symmetries

Parity:

$$\hat{P} \cdot \Psi(x, y, z) \Rightarrow \Psi(-x, -y, -z)$$

Time Reversal:

$$\hat{T} \cdot \Psi(t) \Rightarrow \Psi(-t)$$

Charge Conjugation:

$$\hat{C} \cdot \Psi_n \Rightarrow \Psi_{\bar{n}}$$

Wigner-Eckhart Theorem Implies $\vec{\mu} = \mu \frac{\vec{J}}{J}$ and $\vec{d} = d \frac{\vec{J}}{J}$

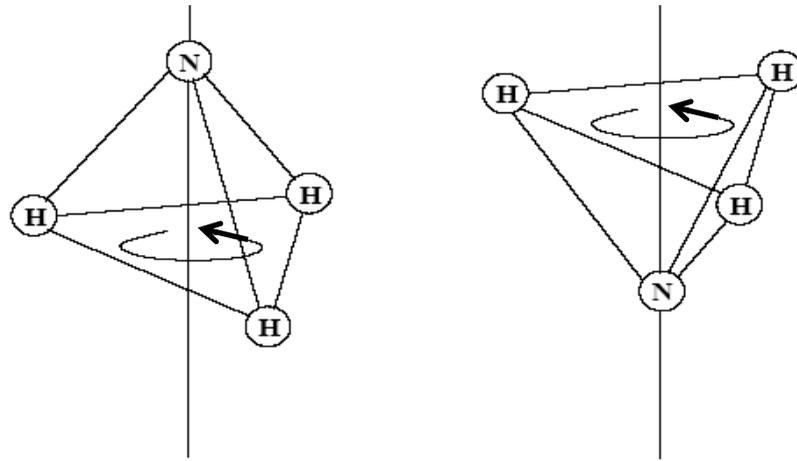
Non-Relativistic Hamiltonian

$$H = \underbrace{\vec{\mu} \cdot \vec{B}}_{\substack{\text{C-even} \\ \text{P-even} \\ \text{T-even}}} + \underbrace{\vec{d} \cdot \vec{E}}_{\substack{\text{C-even} \\ \text{P-odd} \\ \text{T-odd}}}$$

Non-zero d violates P, T, and CP

	<i>C</i>	<i>P</i>	<i>T</i>
$\vec{\mu}$	-	+	-
\vec{d}	-	+	-
\vec{E}	-	-	+
\vec{B}	-	+	-
\vec{J}	+	+	-

Non-Elementary Particles can have EDM's Without Violating Parity and Time Reversal Symmetry



If the neutron was a composite object it could also have non-zero edm without P and T.

However, it would then have a degenerate ground state Which is incompatible with observed nuclear shell structure

Non-Elementary Particles can have EDM's Without Violating Parity and Time Reversal Symmetry

Theorem:

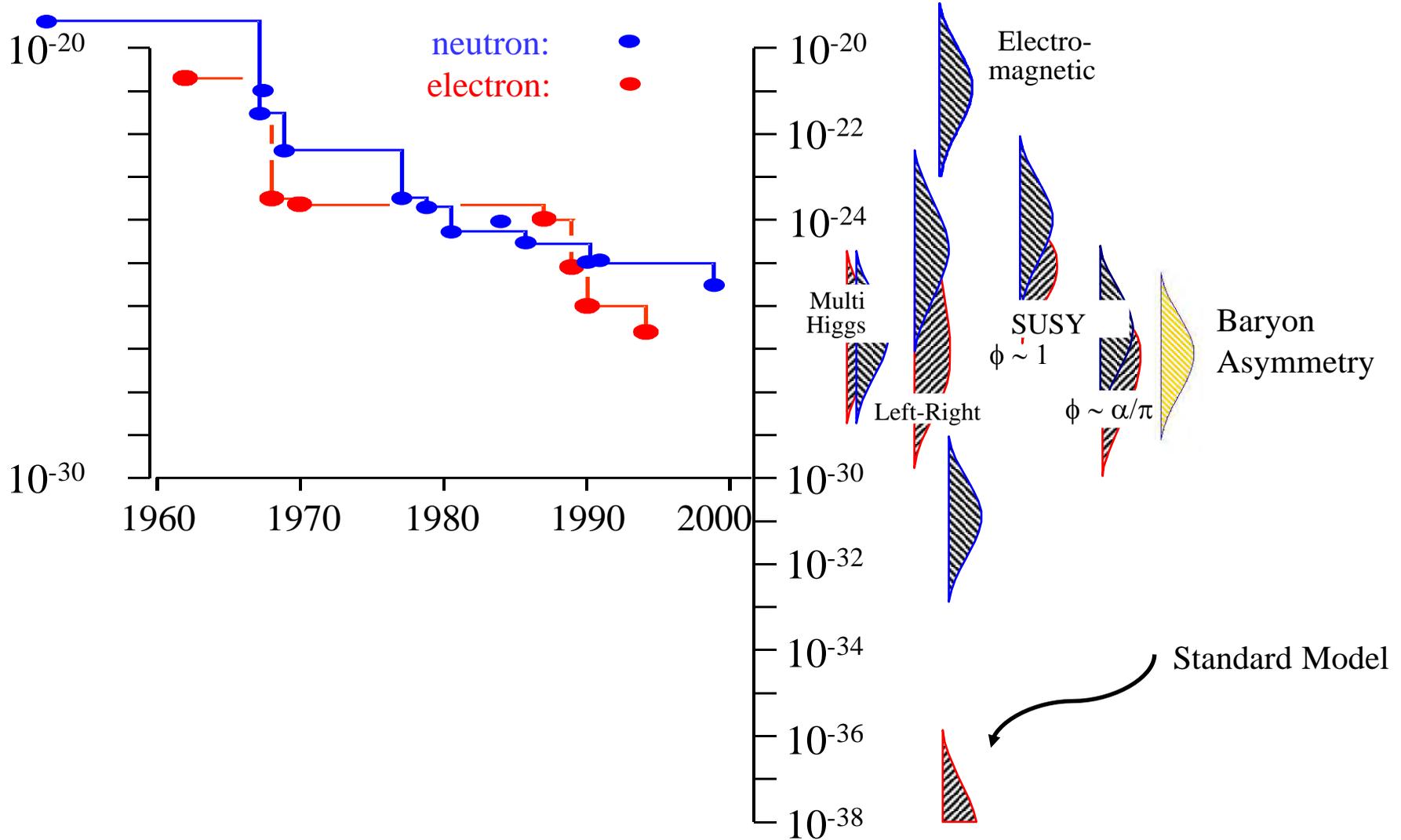
The observation of a non-zero, static, electric dipole moment for a non-degenerate elementary particle would be a direct violation of time reversal symmetry.

If the neutron was a composite object it could also have non-zero edm without P and T.

However, it would then have a degenerate ground state Which is incompatible with observed nuclear shell structure

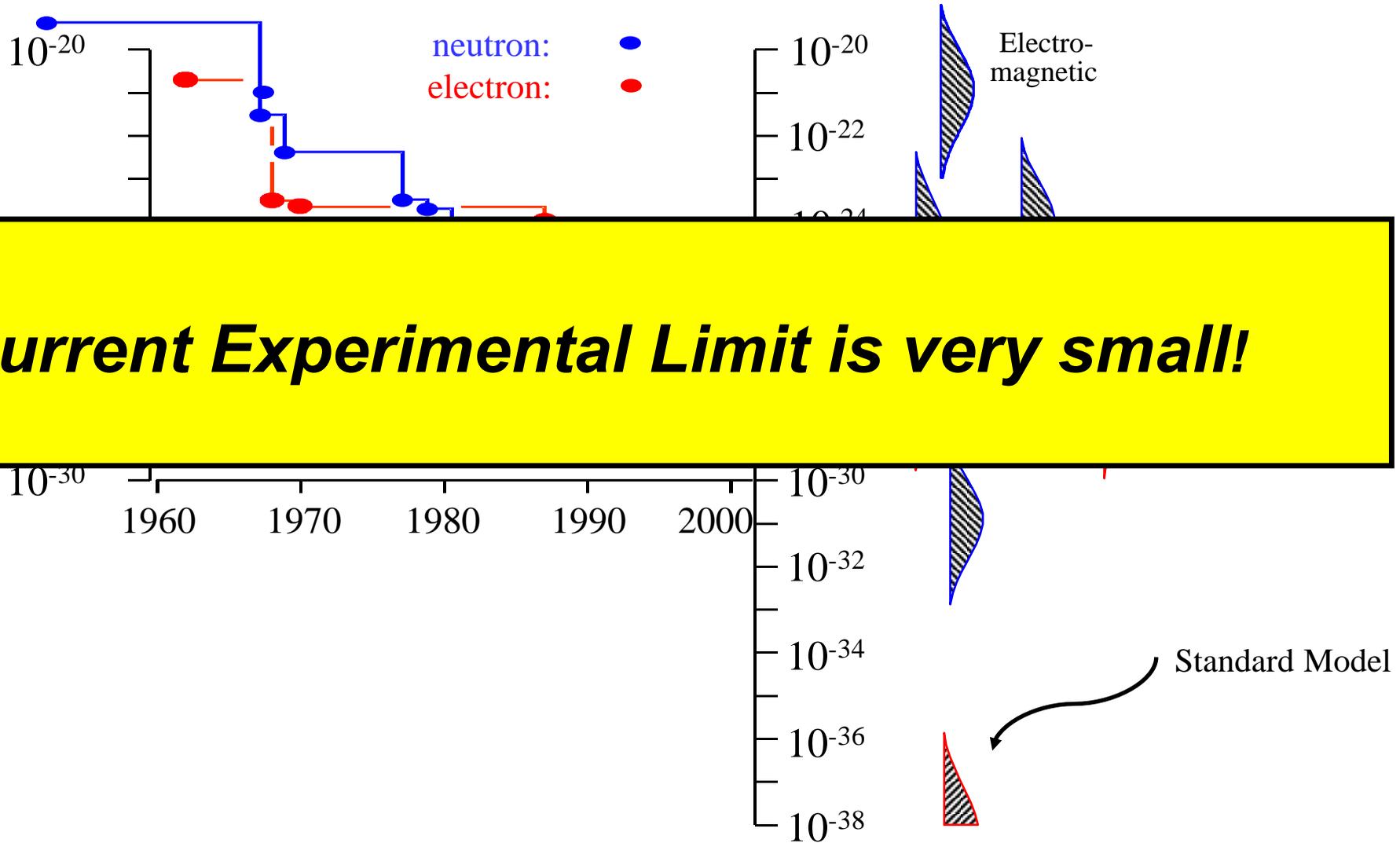
We expect a non-zero neutron EDM at some level

Experimental Limit on d (e cm)



We expect a non-zero neutron EDM at some level

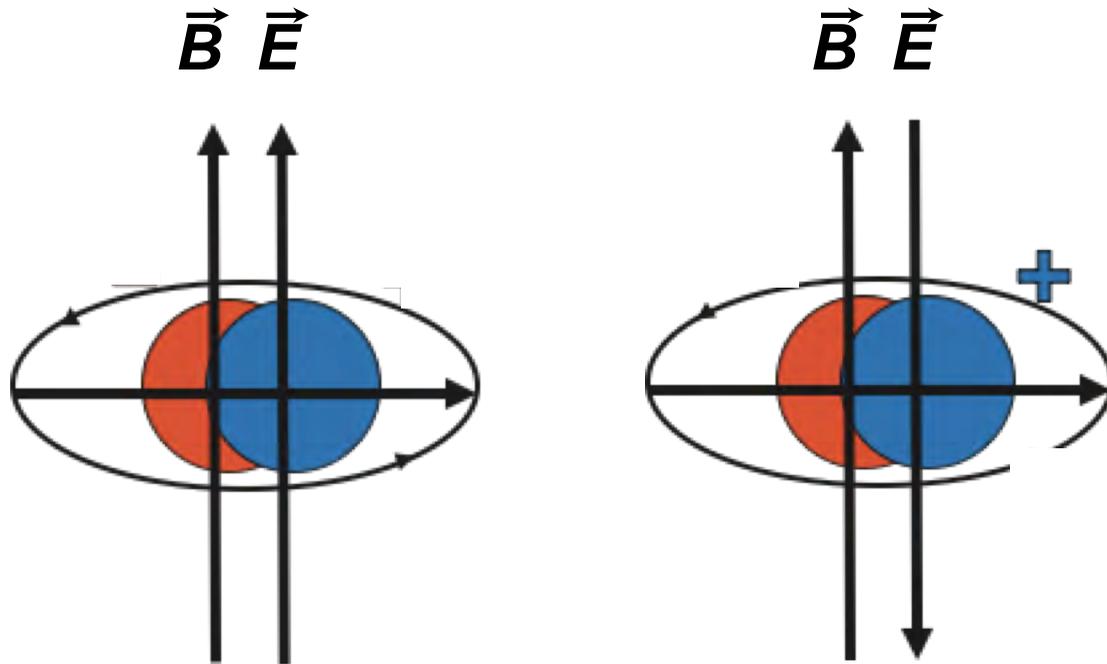
Experimental Limit on d (e cm)



If a neutron were blown up to the size of the earth, the current limit on its EDM would correspond to a displacement of + and - electron charge by $\sim 1 \mu\text{m}$



Measuring the Electric Dipole Moment



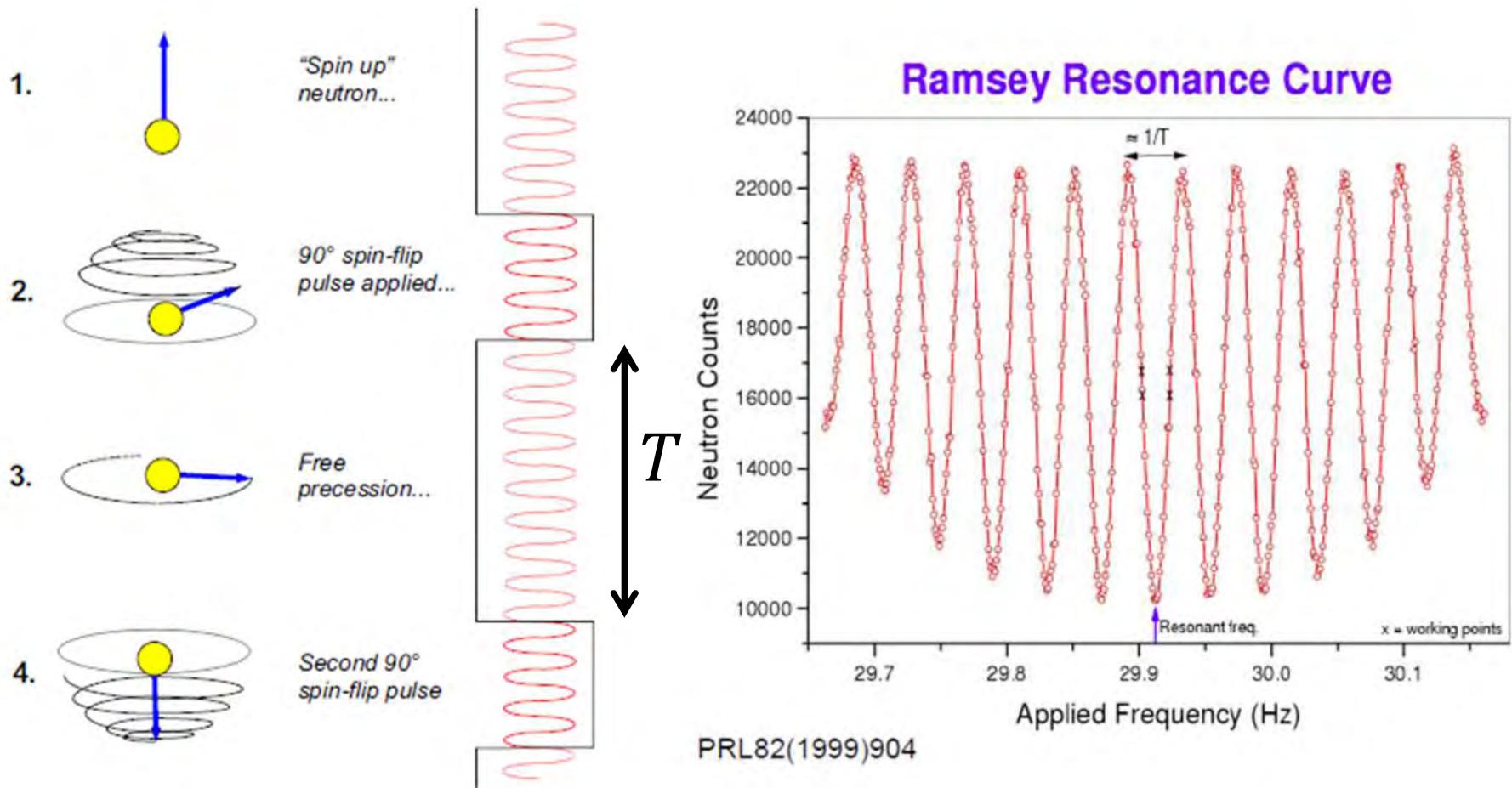
$$H = \vec{\mu} \cdot \vec{B} + \vec{d} \cdot \vec{E}$$

$$\omega = \frac{2\mu_n B}{\hbar} \pm \frac{2d_n E}{\hbar}$$

Look for a precession frequency $\hbar\omega = 2\mu_n B \pm 2d_n E$

A moment of 10^{-25} ecm in a 10 kV/cm electric field corresponds to a shift in frequency of 0.5 μ Hz!

Ramsey's Method of Separated Oscillatory Fields*



$$\Delta\omega = \frac{1}{2T}$$

*cited for Nobel Prize 1989

EDM Statistical Sensitivity

$$\sigma_{edm} \propto \frac{1}{ET\sqrt{N_n}}$$

E = Applied Electric Field

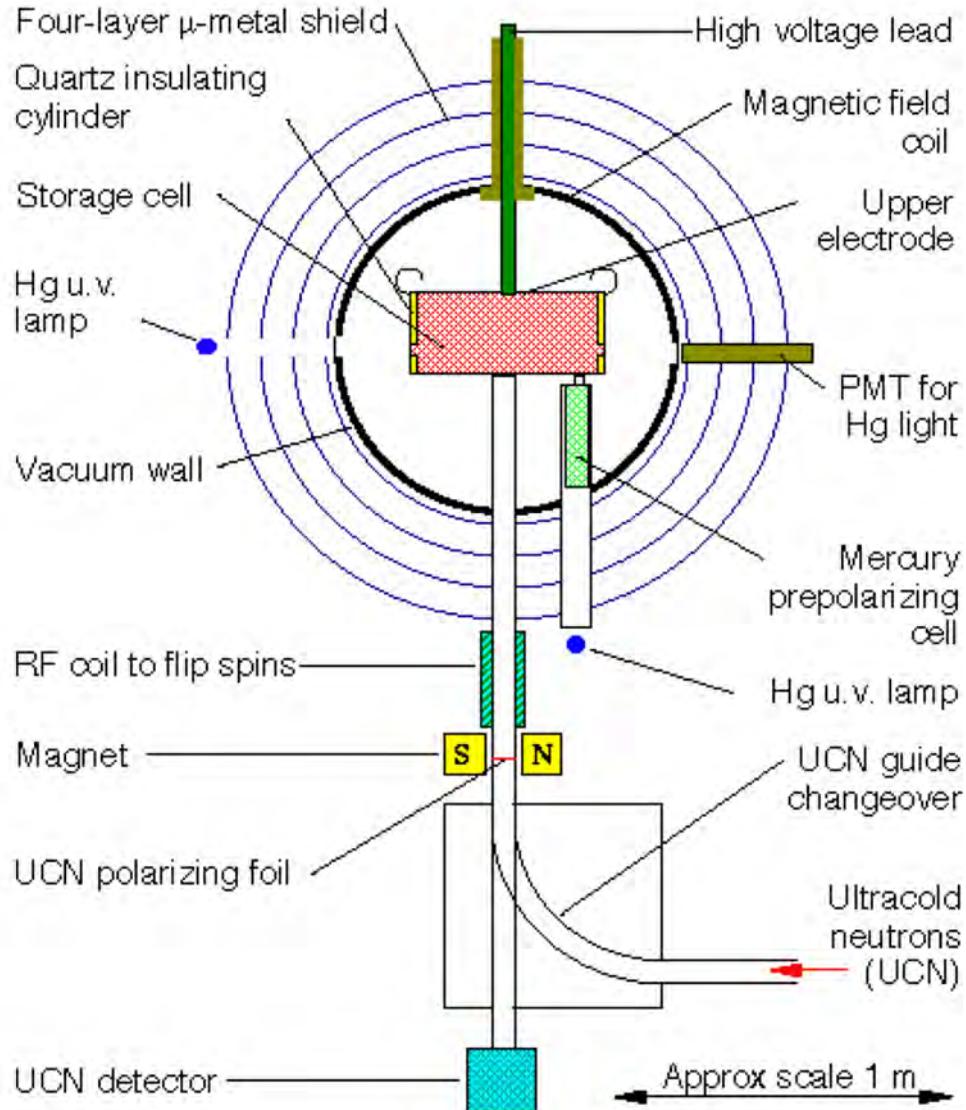
N_n = Number of neutrons observed

T = Observation Time

We want:

- 1. Highest Possible Electric Field (Limited by breakdown)*
- 2. More neutrons (limited by source strength)*
- 3. Longest possible free precession time (ultimately limited by τ_n)*

ILL- Sussex Neutron Electric Dipole Moment Experiment*

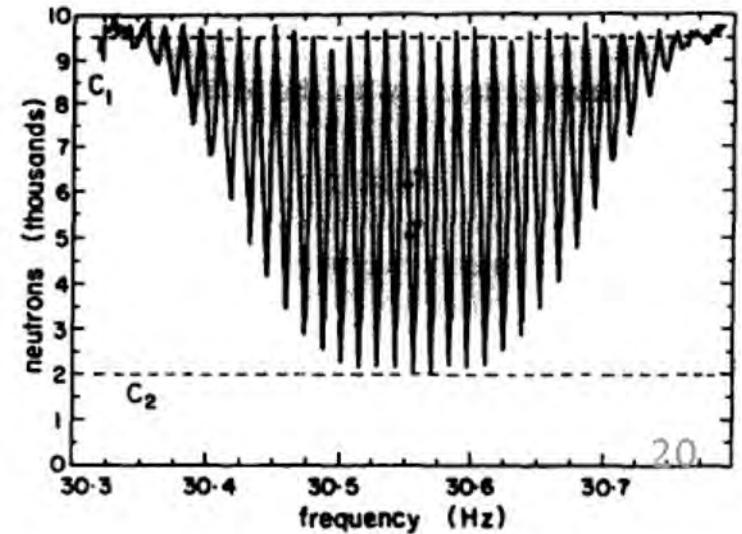


$$d = (-0.21 \pm 1.82) \times 10^{-26} \text{ ecm}$$

J.M. Pendlebury et al., PR D92 09 (2003)

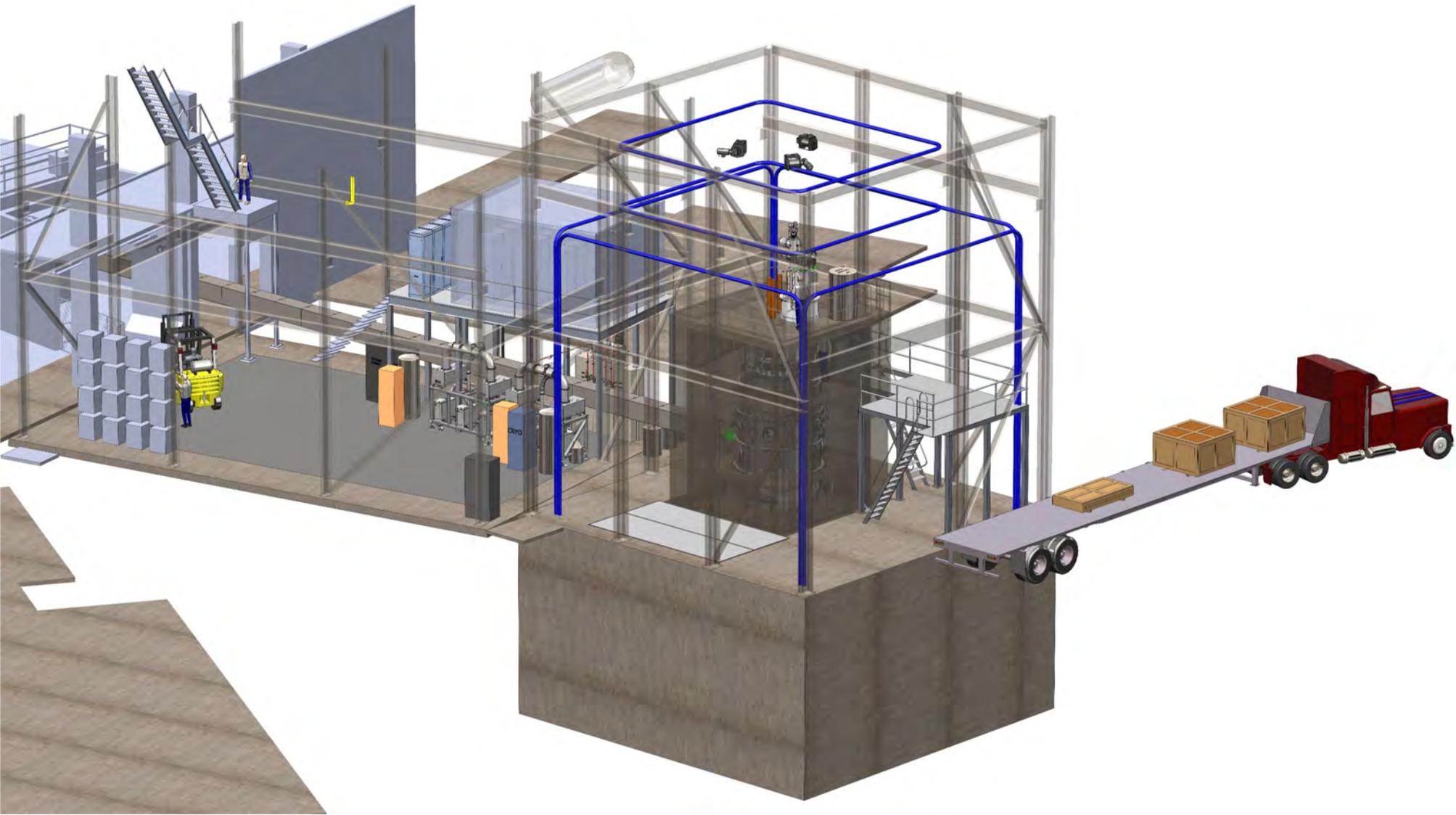
$T = 130 \text{ s}$

$E = 10 \text{ kV/cm}$



***Experiment has been upgraded and installed at PSI. New result is pending.**

The nEDM experiment at the Spallation Neutron Source



Features of the new SNS nEDM experiment:

- Double cell (common B, opposite E)
- Ultra-cold neutrons produced in-situ
 - in **superfluid Helium** below 0.7K to achieve long storage time (suppress phonon upscattering) **as a UCN source**
- Helium-3 as co-magnetometer
 - precession monitored by SQUID
 - long relaxation time in **superfluid Helium** **as a buffer gas**
- Neutron precession measured through the spin-dependent $n+^3\text{He}$ capture reaction **as a particle detector**
 - Use **liquid helium** as scintillating medium
 - Cell has to be optically transparent as a part of the light guide
 - PMT operated at cryogenic temperatures (4K)
- High dielectric strength of **superfluid helium** (>50kV/cm) **as a HV insulator**

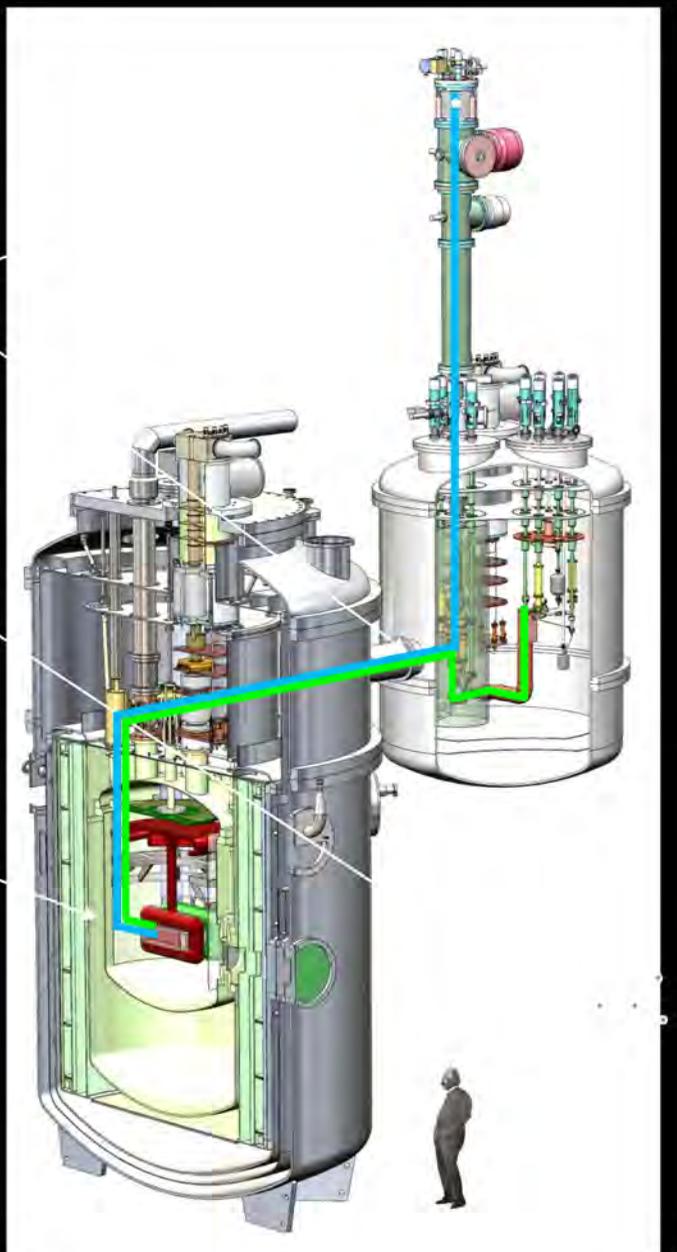
nEDM@SNS

Measurement Cycle

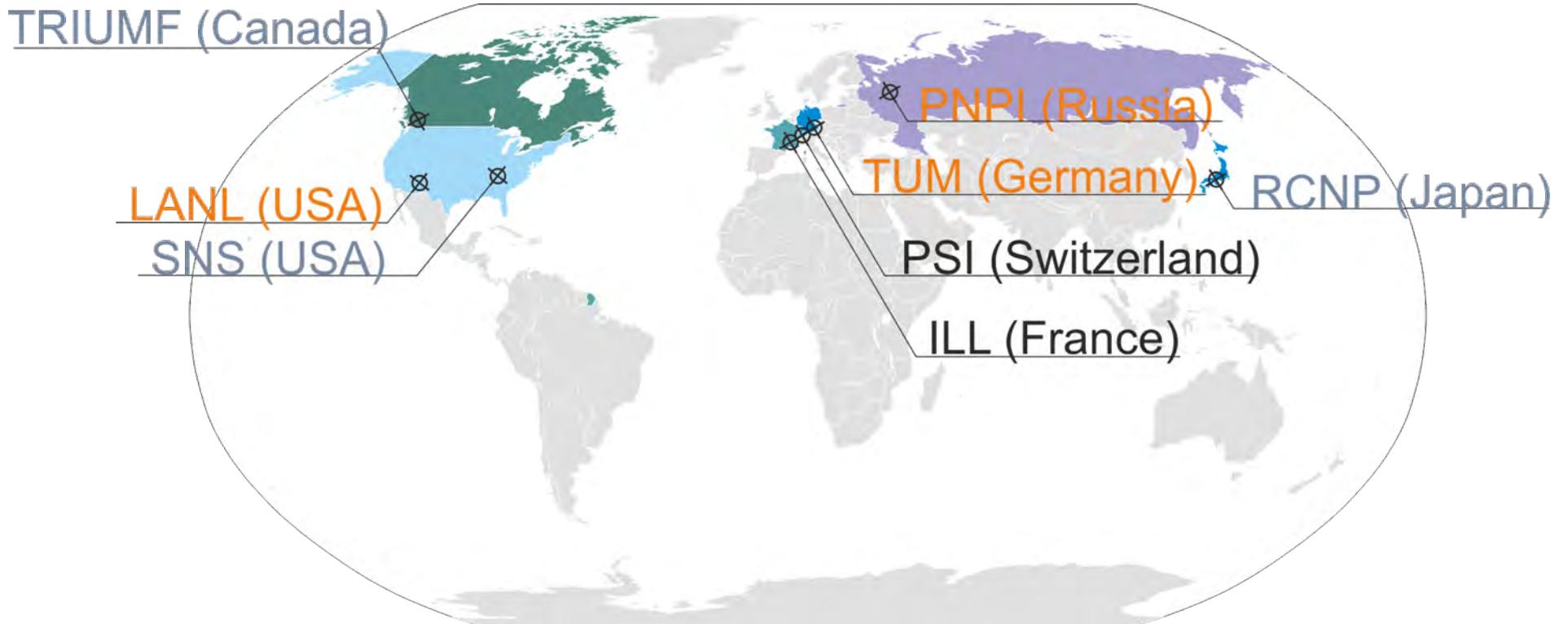
1. Load collection volume with polarized ^3He atoms
2. Transfer polarized ^3He atoms into measurement cell
3. Illuminate measurement cell with polarized cold neutrons to produce polarized UCN
4. Apply a $\pi/2$ pulse to rotate spins perpendicular to B_0
5. Measure precession frequency
6. Remove reduced polarization ^3He atoms from measurement cell
7. Flip E-field & Go to 1.



Slide thanks to Vince Cianciolo

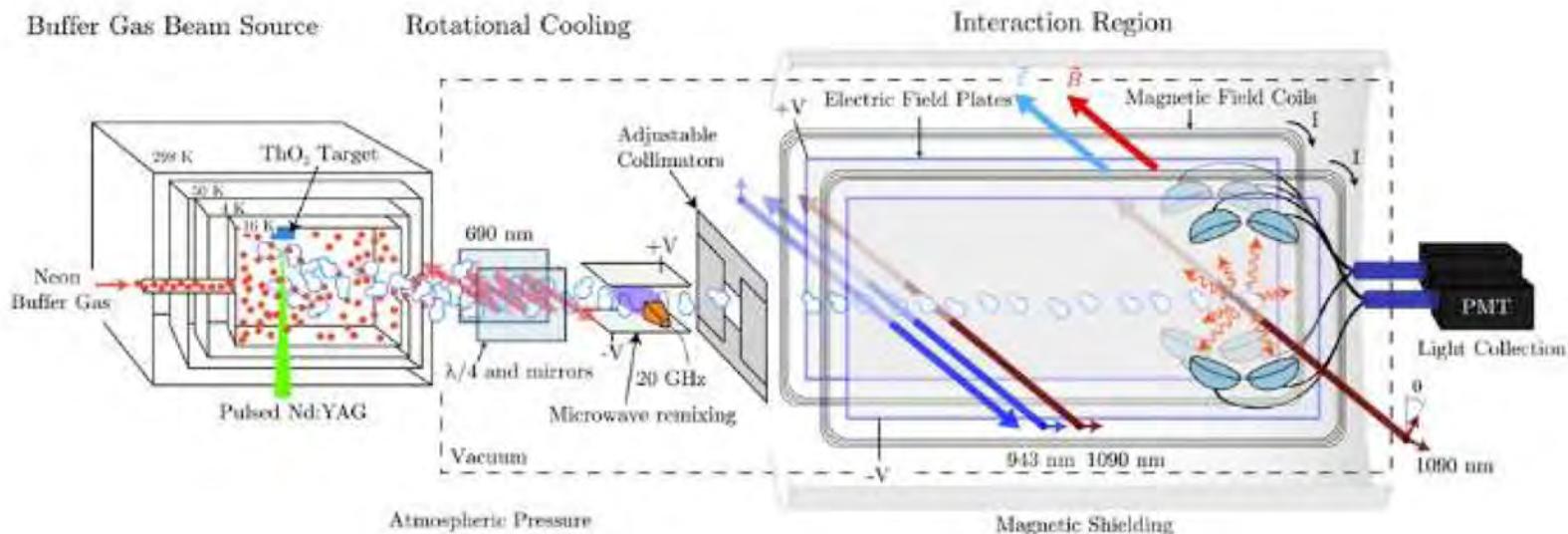


Neutron EDM searches are in progress at many facilities world wide



The Neutron EDM search is complementary to other types of EDM measurements

ACME experiment

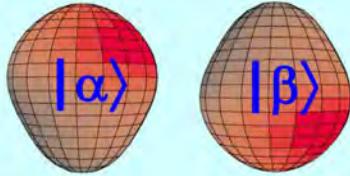


$$d_e = (-2.1 \pm 3.7_{\text{stat}} \pm 2.5_{\text{syst}}) \times 10^{-29} \text{ e} \cdot \text{cm}$$

Science 17 Jan 2014:
Vol. 343, Issue 6168, pp. 269-272



$$10 \text{ V/cm} \rightarrow 10 \cdot 10^9 \text{ V/cm},$$



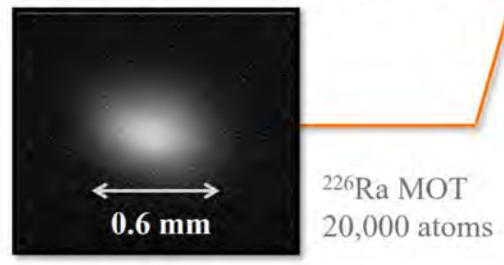
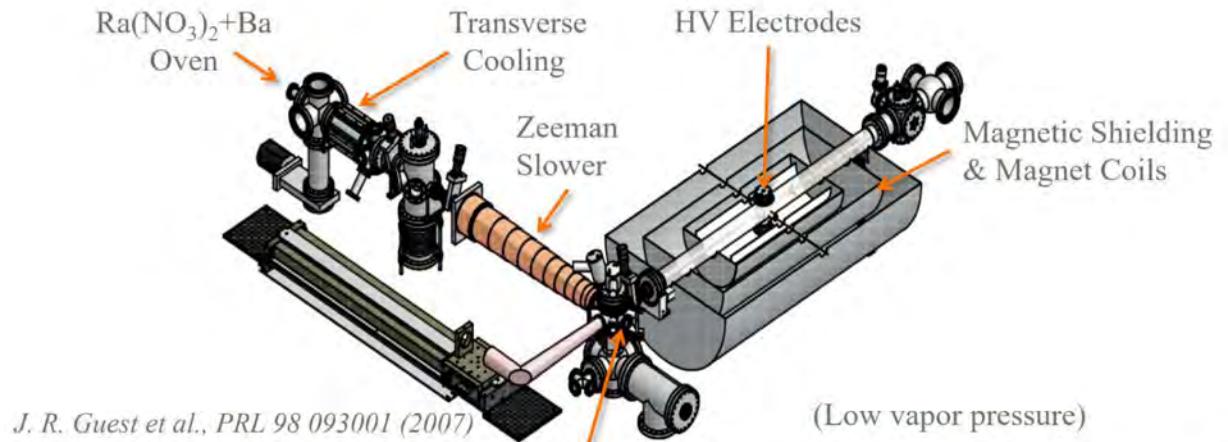
A large quadrupole and octupole deformation results in an enhanced Schiff moment
 – Auerbach, Flambaum & Spevak (1996)

Enhancement Factor: EDM (^{225}Ra) / EDM (^{199}Hg)

Skyrme Model	Isoscalar	Isovector	Isotensor
SIII	300	4000	700
SkM*	300	2000	500
SLy4	700	8000	1000

Radium-255 deformed nuclei

Collect Atoms in MOT

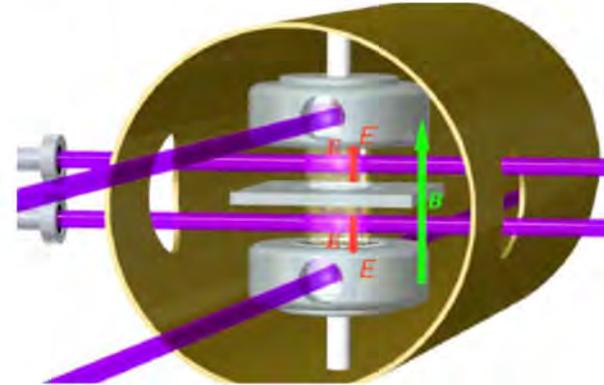


For EDM:	For Testing:
Ra-225	Ra-226
$I = 1/2, J = 0$	$I = 0, J = 0$
$t_{1/2} = 15$ days	$t_{1/2} = 1600$ yrs

The Seattle ^{199}Hg (atomic) EDM Measurement



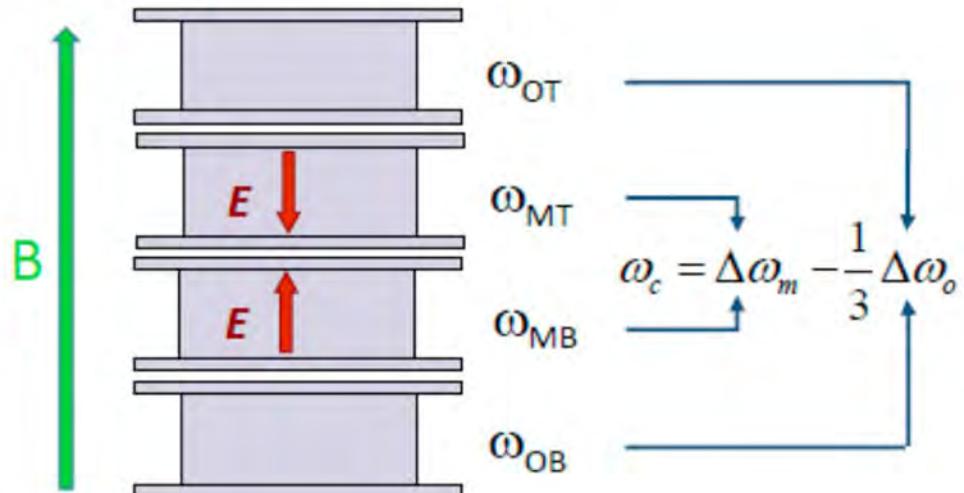
4 mercury vapor Cells:
 2 with opposite **E** fields
 2 for **B** field normalization



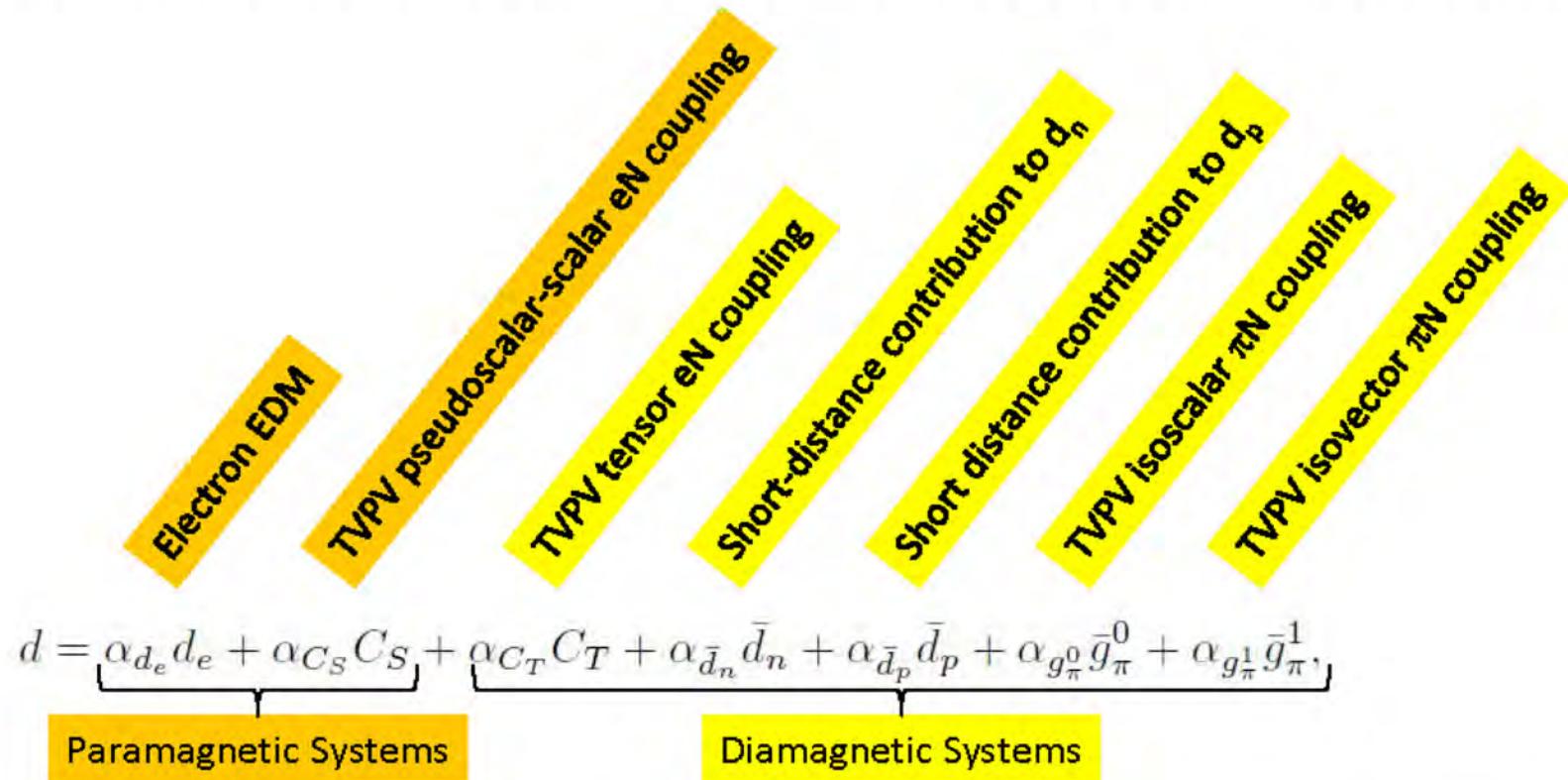
$$H = -(\vec{\mu} \cdot \vec{B} + \vec{d} \cdot \vec{E})$$

$$\omega_c = \frac{\mu}{\hbar} \left(-\frac{8}{3} \frac{\partial^3 B}{\partial z^3} \Delta z^3 \right) + \frac{4dE}{\hbar}$$

Cancels up to 2nd order gradient noise
 Same EDM sensitivity as Middle Difference



Why Do We Need So Many Experiments?



T. Chupp, M. Ramsey-Musolf, Phys. Rev. C91 035502 (2015)

End of Lecture 3

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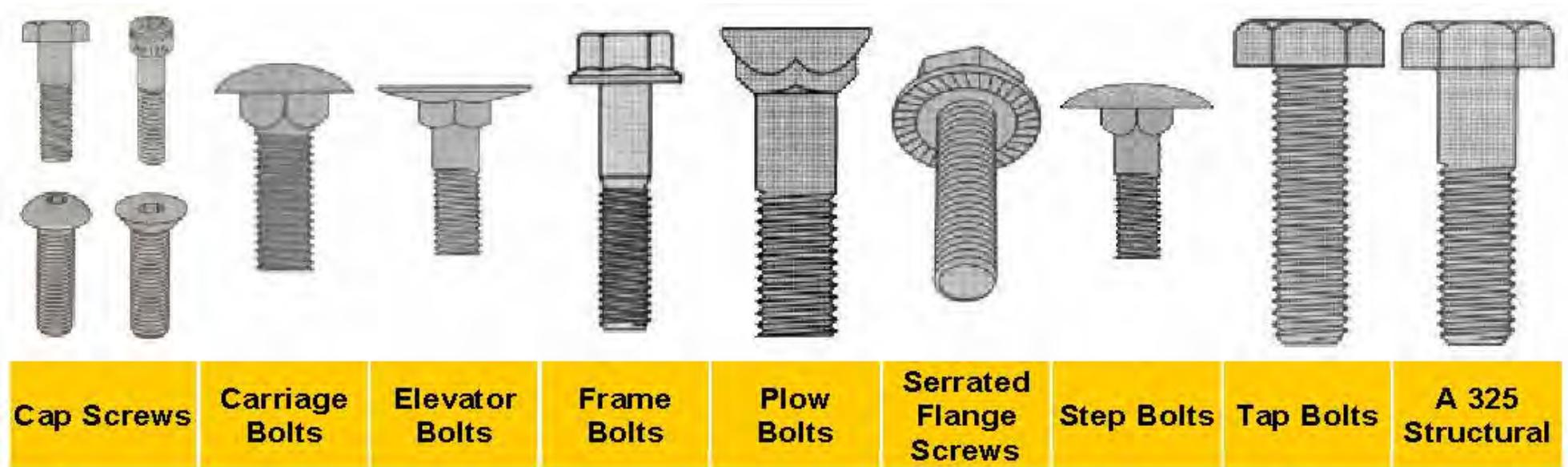
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Spontaneous Symmetry breaking

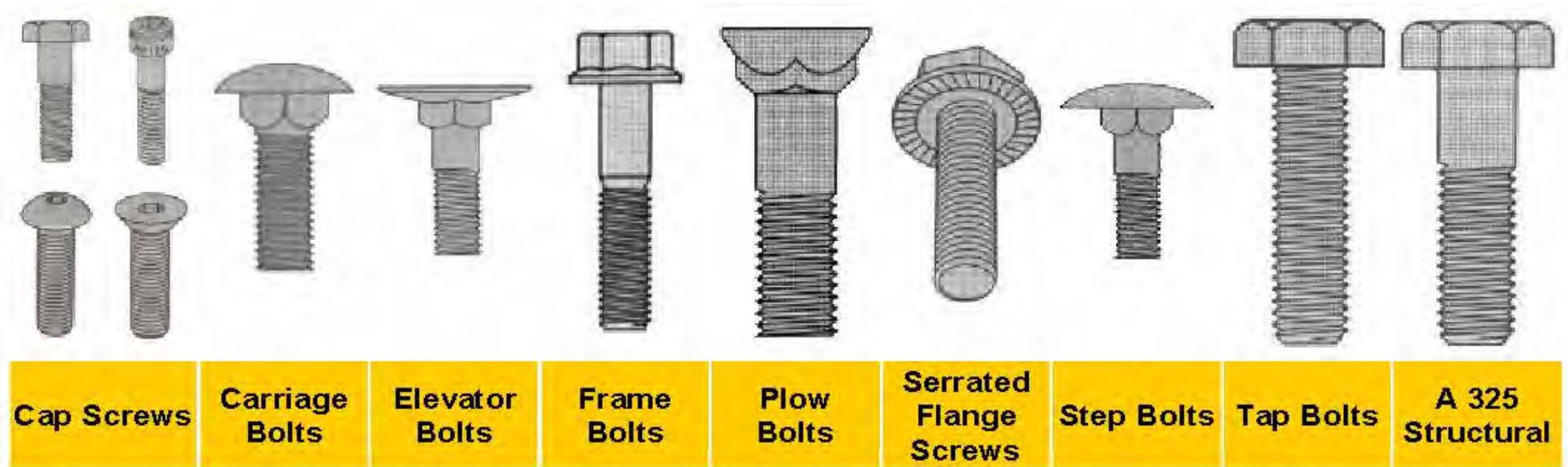
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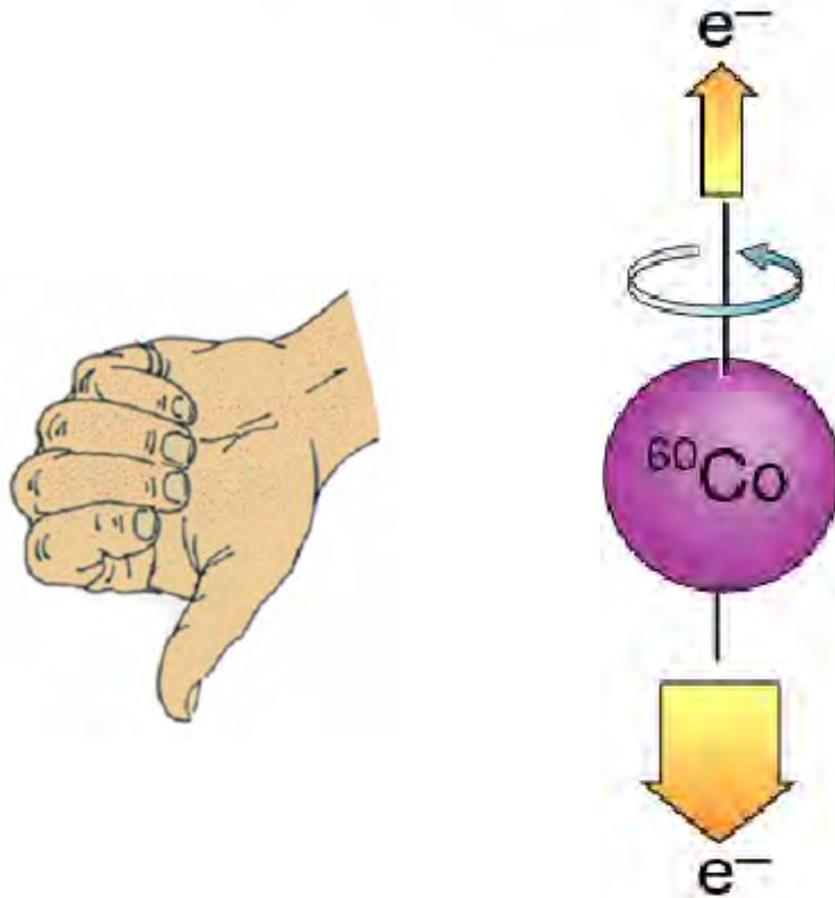


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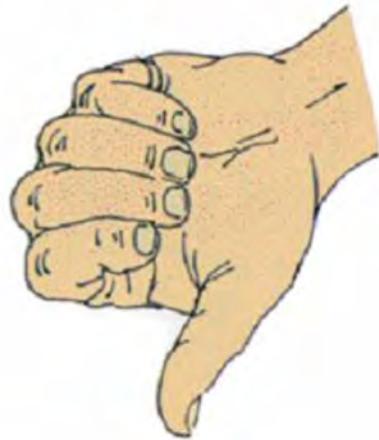
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Is This a Broken symmetry?

The Cosmic Baryon Asymmetry

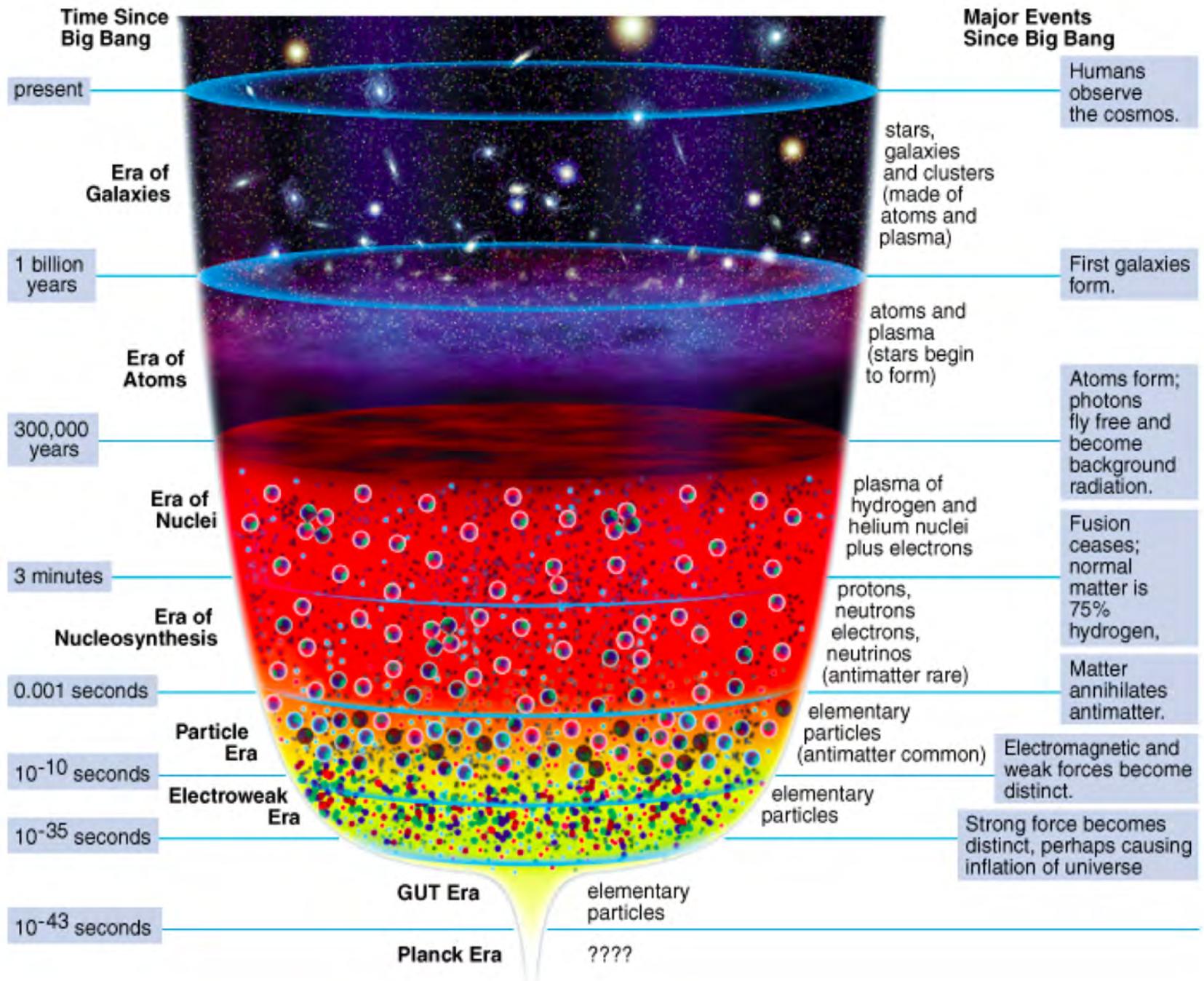
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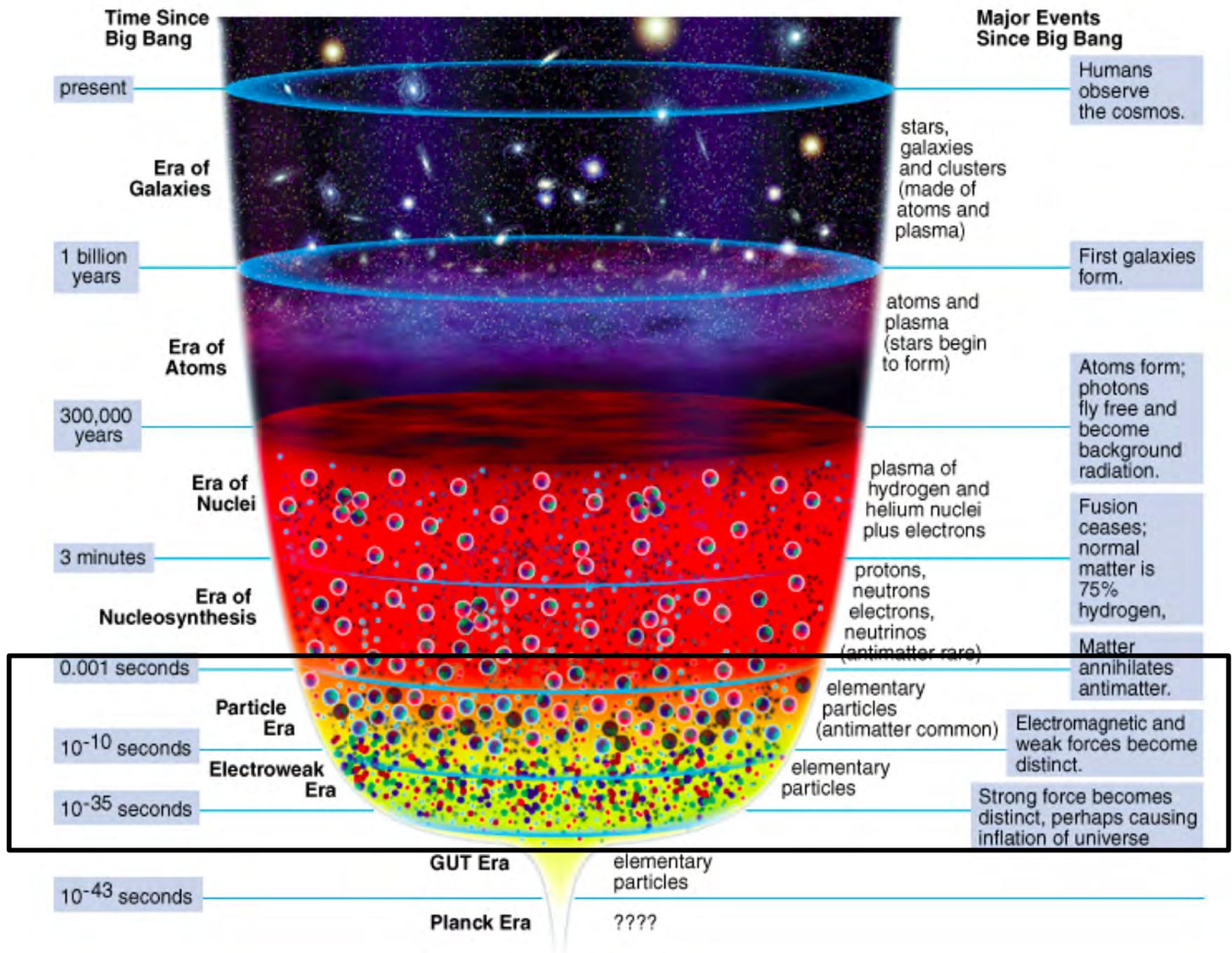
Observation:

As best we can determine, the universe consists of Matter.

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Is This a Broken symmetry?





Just after Inflation, there were equal amounts of Matter and Antimatter.

If nothing else happened, all matter and antimatter would annihilate leaving...

NOTHING!

***Today, the Universe consists of matter and
there is essentially NO anti-matter***

This is the

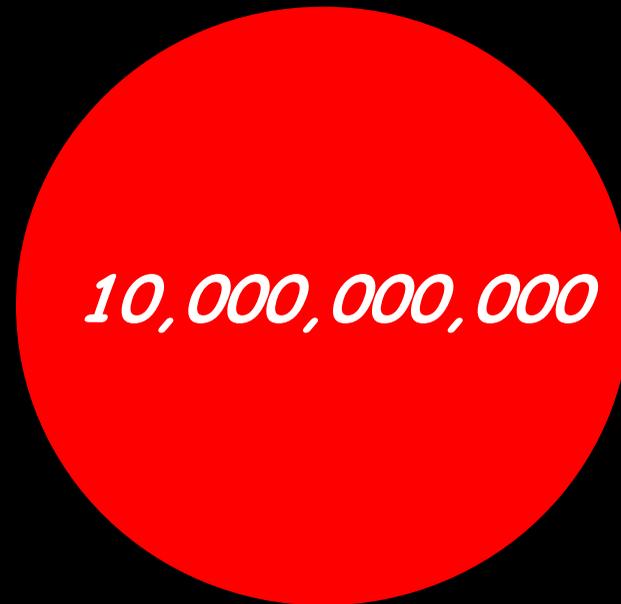
“Baryon Asymmetry Problem”

Matter and Antimatter Just After Inflation



10,000,000,000

Matter

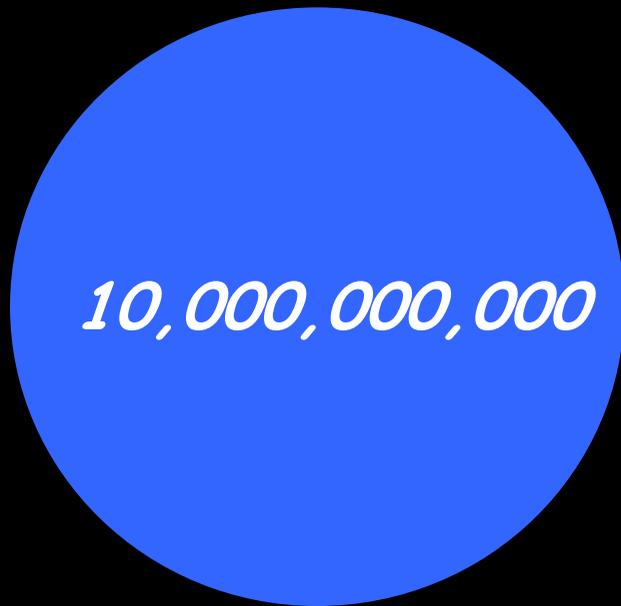


10,000,000,000

Anti- Matter

Matter and Antimatter

$\sim 10^{-6}$ s later



10,000,000,000

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9,999,999,999

Anti- Matter

Matter and Antimatter

Now

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1

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1

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An example of T violation

Discrete Symmetries

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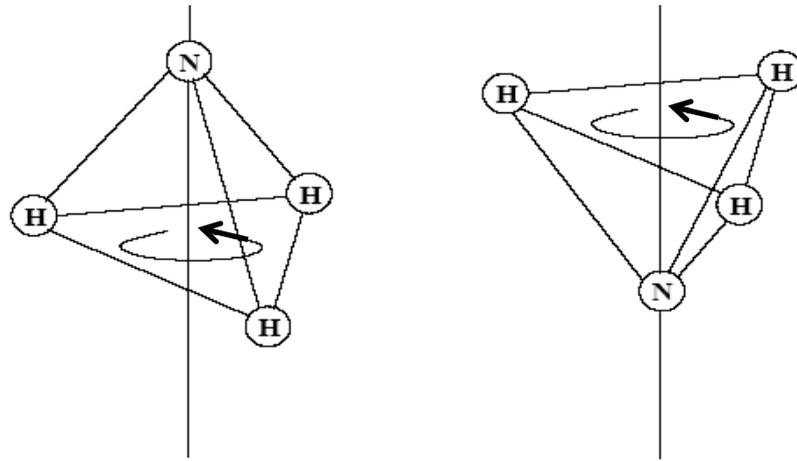
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Non-zero d violates P, T, and CP

	<i>C</i>	<i>P</i>	<i>T</i>
$\vec{\mu}$	-	+	-
\vec{d}	-	+	-
\vec{E}	-	-	+
\vec{B}	-	+	-
\vec{J}	+	+	-

Non-Elementary Particles can have EDM's Without Violating Parity and Time Reversal Symmetry



If the neutron was a composite object it could also have non-zero edm without P and T.

However, it would then have a degenerate ground state Which is incompatible with observed nuclear shell structure

Non-Elementary Particles can have EDM's Without Violating Parity and Time Reversal Symmetry

Theorem:

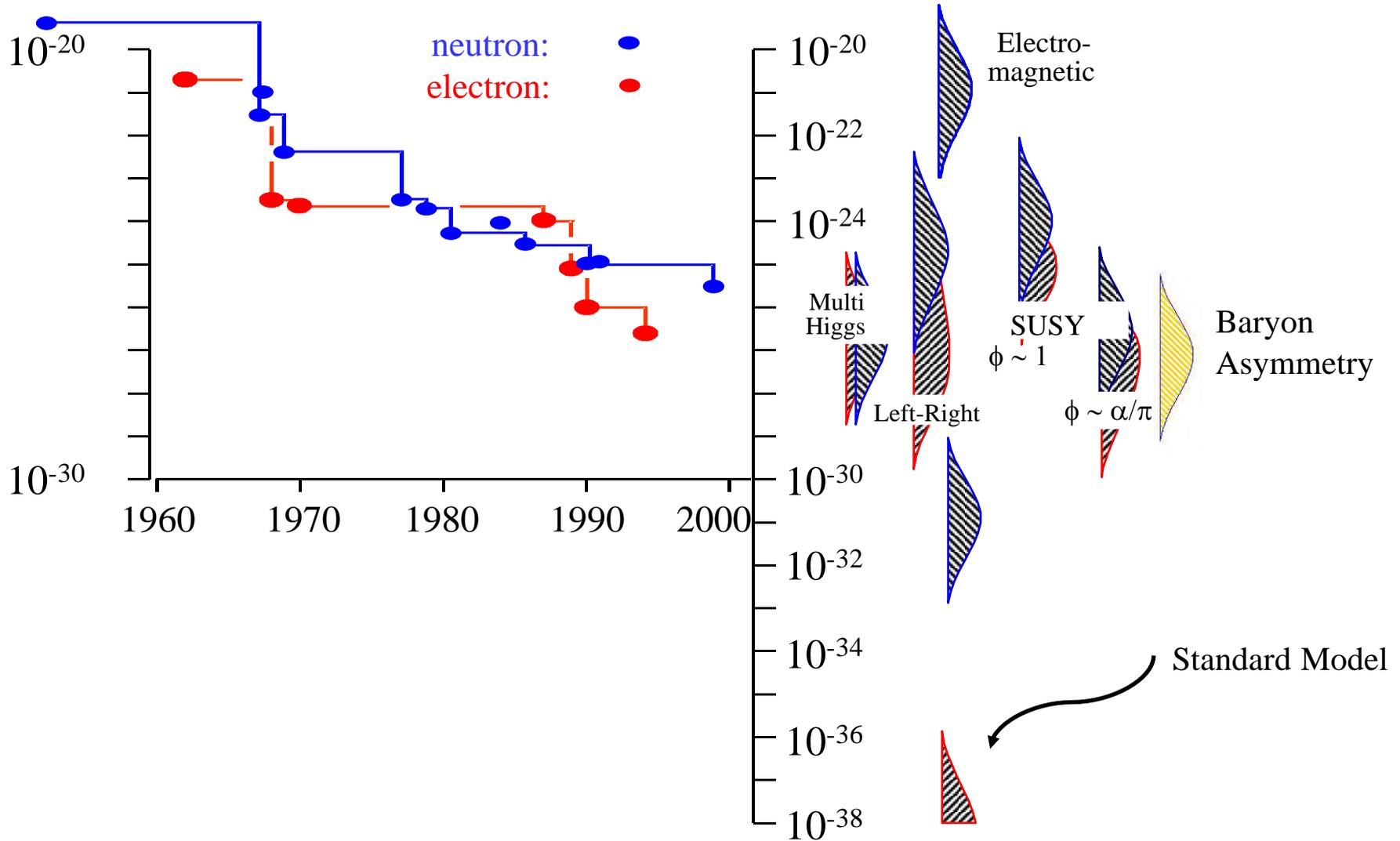
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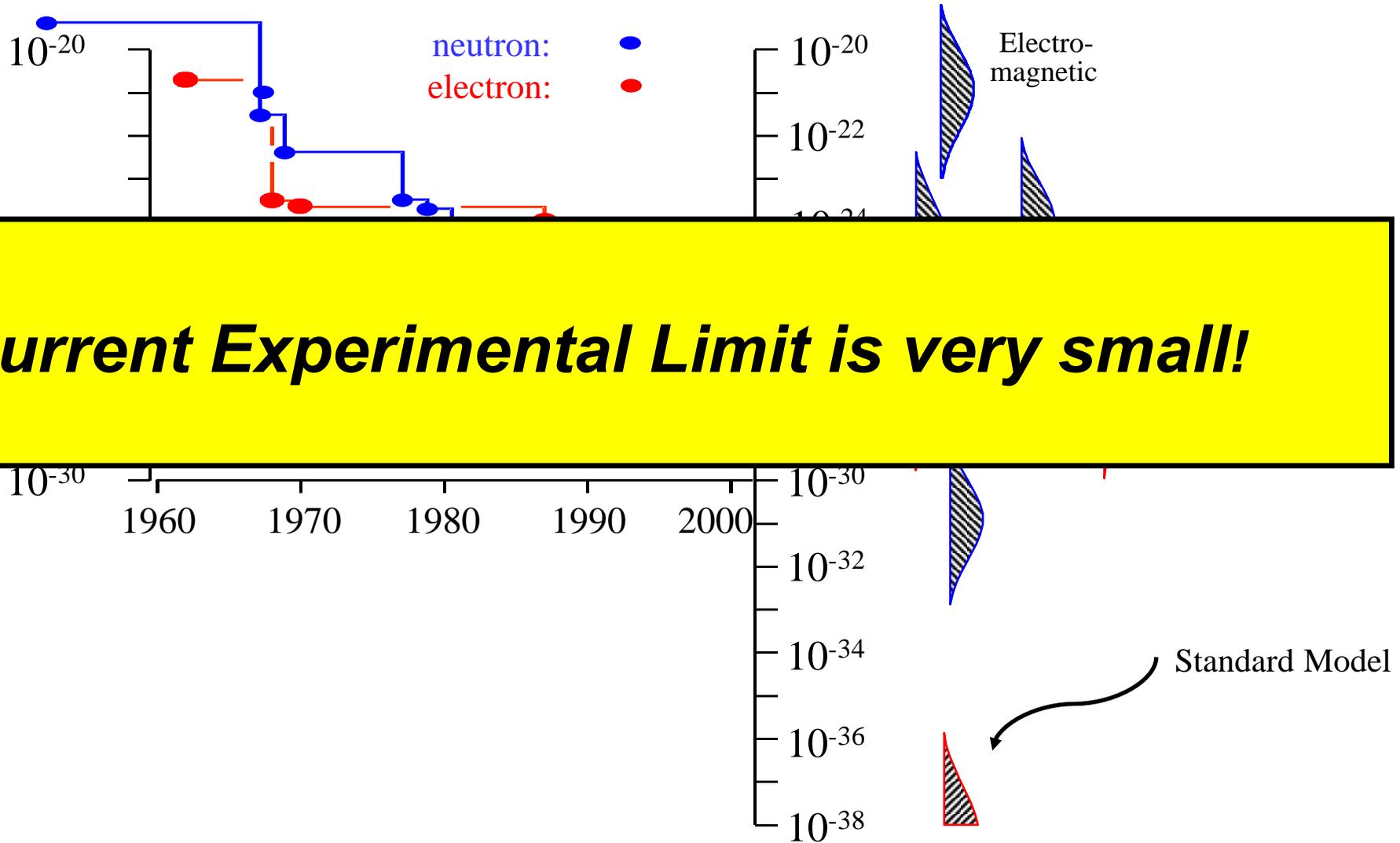
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Experimental Limit on d (e cm)



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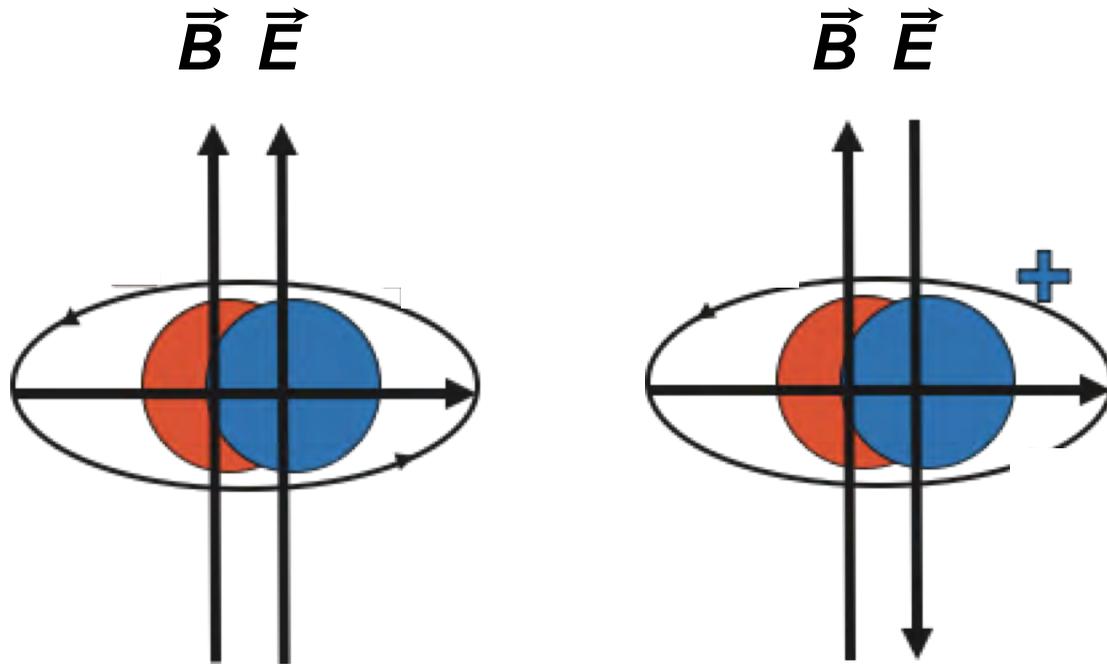
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Measuring the Electric Dipole Moment



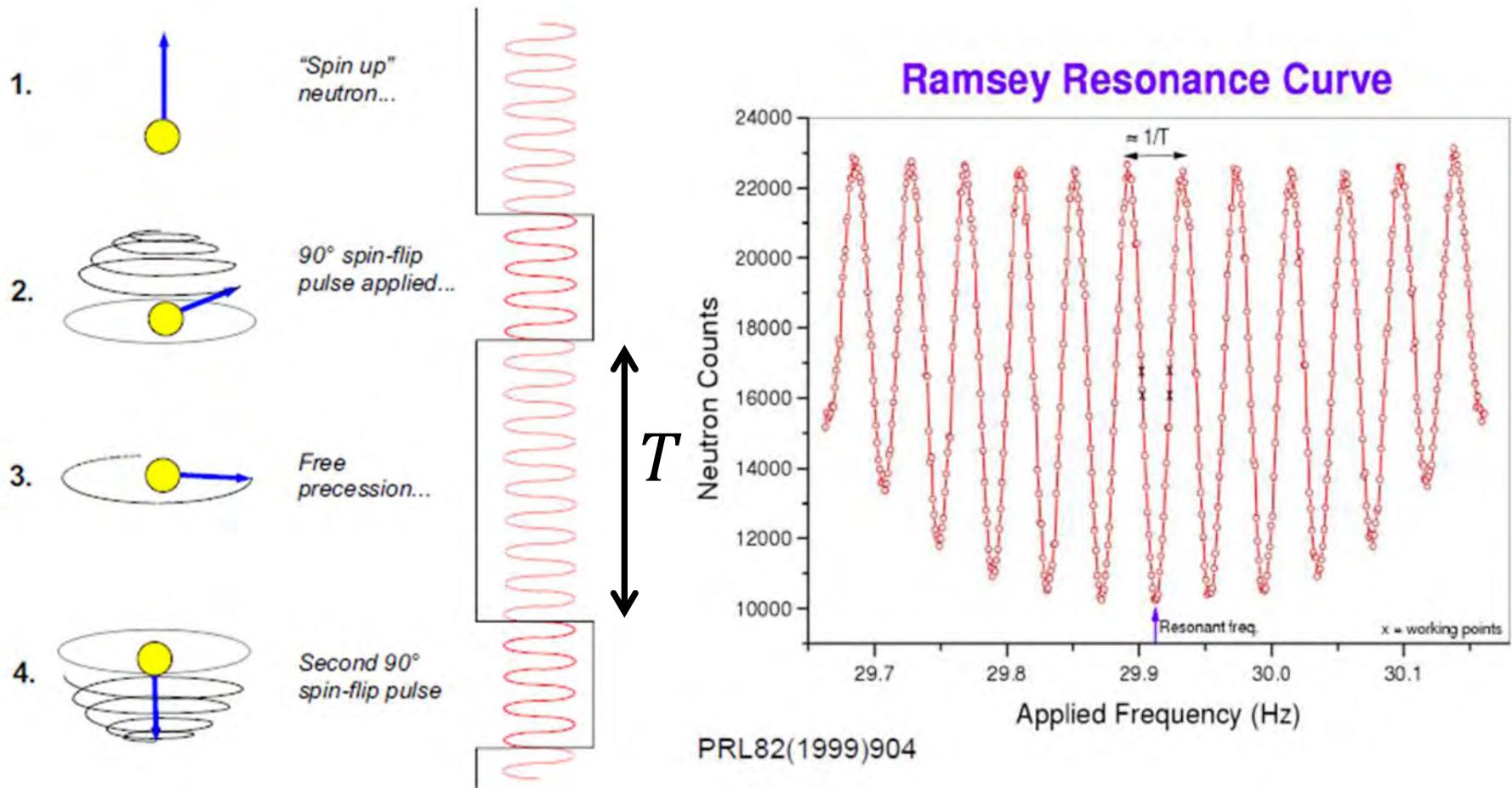
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A moment of 10^{-25} ecm in a 10 kV/cm electric field corresponds to a shift in frequency of 0.5 μ Hz!

Ramsey's Method of Separated Oscillatory Fields*



$$\Delta\omega = \frac{1}{2T}$$

EDM Statistical Sensitivity

$$\sigma_{edm} \propto \frac{1}{ET \sqrt{N_n}}$$

E = Applied Electric Field

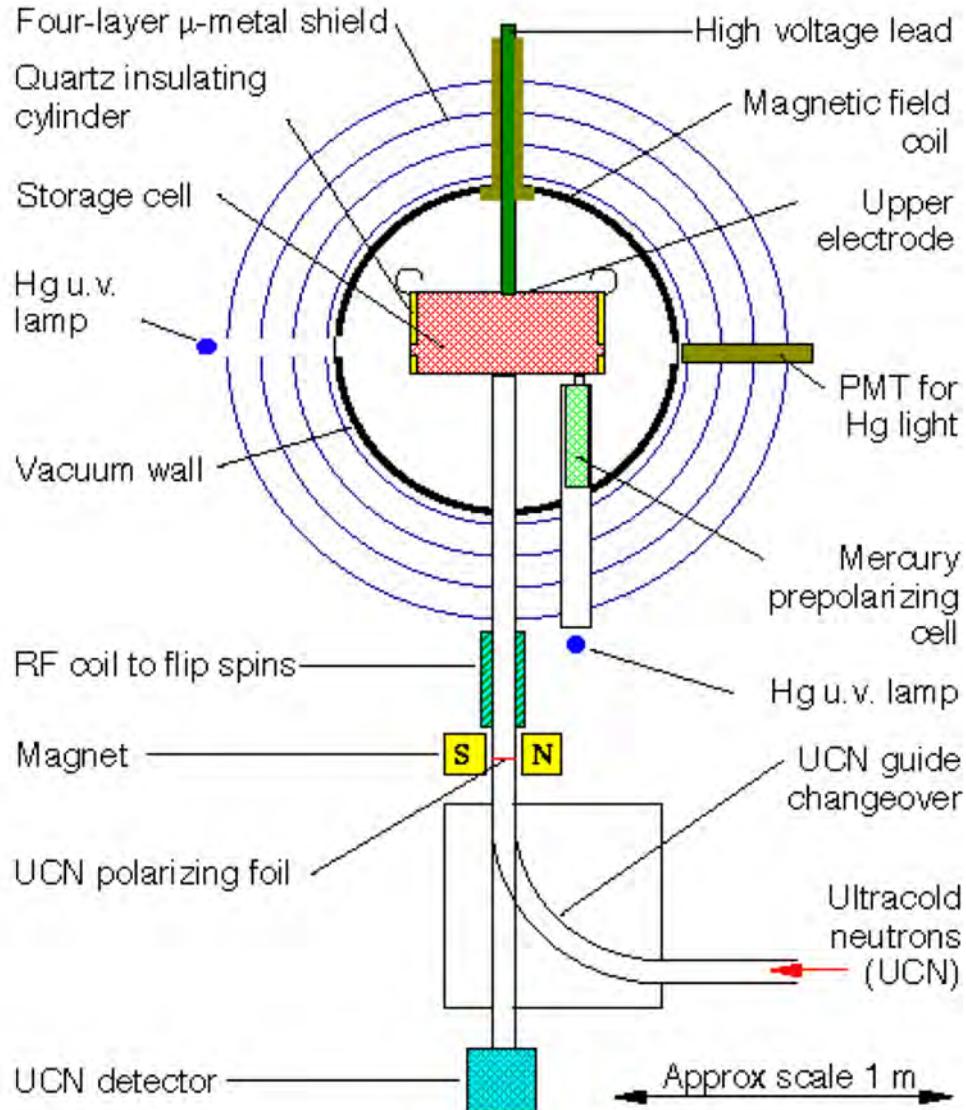
N_n = Number of neutrons observed

T = Observation Time

We want:

1. Highest Possible Electric Field (Limited by breakdown)
2. More neutrons (limited by source strength)
3. Longest possible free precession time (ultimately limited by τ_n)

ILL- Sussex Neutron Electric Dipole Moment Experiment*

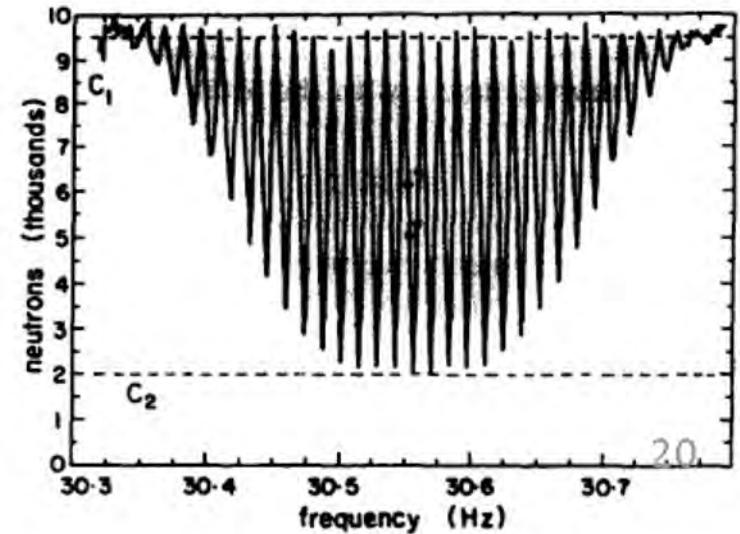


$$d = (-0.21 \pm 1.82) \times 10^{-26} \text{ ecm}$$

J.M. Pendlebury et al., PR D92 09 (2003)

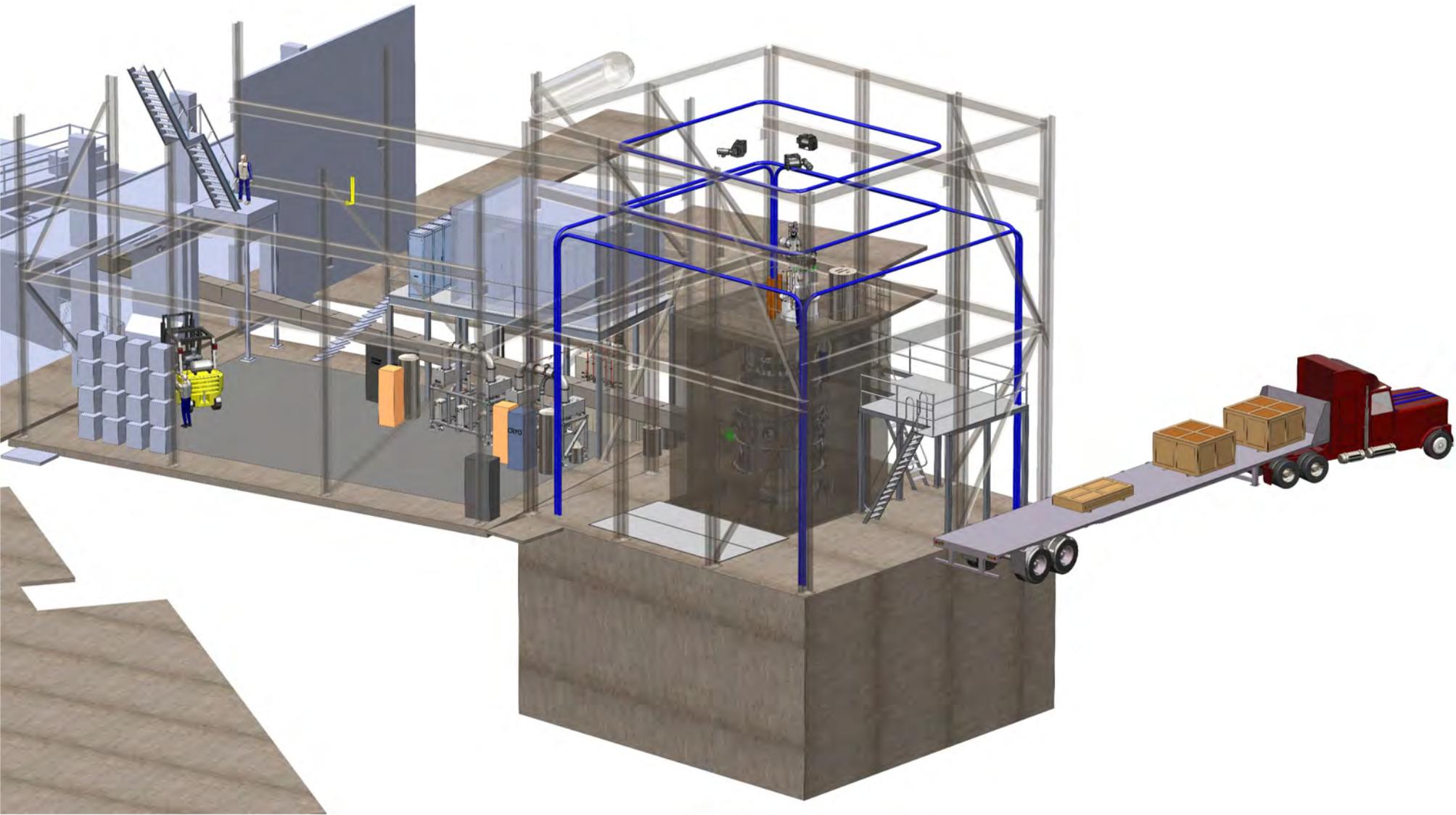
$$T = 130 \text{ s}$$

$$E = 10 \text{ kV/cm}$$



***Experiment has been upgraded and installed at PSI. New result is pending.**

The nEDM experiment at the Spallation Neutron Source



Features of the new SNS nEDM experiment:

- Double cell (common B, opposite E)
- Ultra-cold neutrons produced in-situ
 - in **superfluid Helium** below 0.7K to achieve long storage time (suppress phonon upscattering) **as a UCN source**
- Helium-3 as co-magnetometer
 - precession monitored by SQUID
 - long relaxation time in **superfluid Helium** **as a buffer gas**
- Neutron precession measured through the spin-dependent $n+^3\text{He}$ capture reaction **as a particle detector**
 - Use **liquid helium** as scintillating medium
 - Cell has to be optically transparent as a part of the light guide
 - PMT operated at cryogenic temperatures (4K)
- High dielectric strength of **superfluid helium** (>50kV/cm) **as a HV insulator**

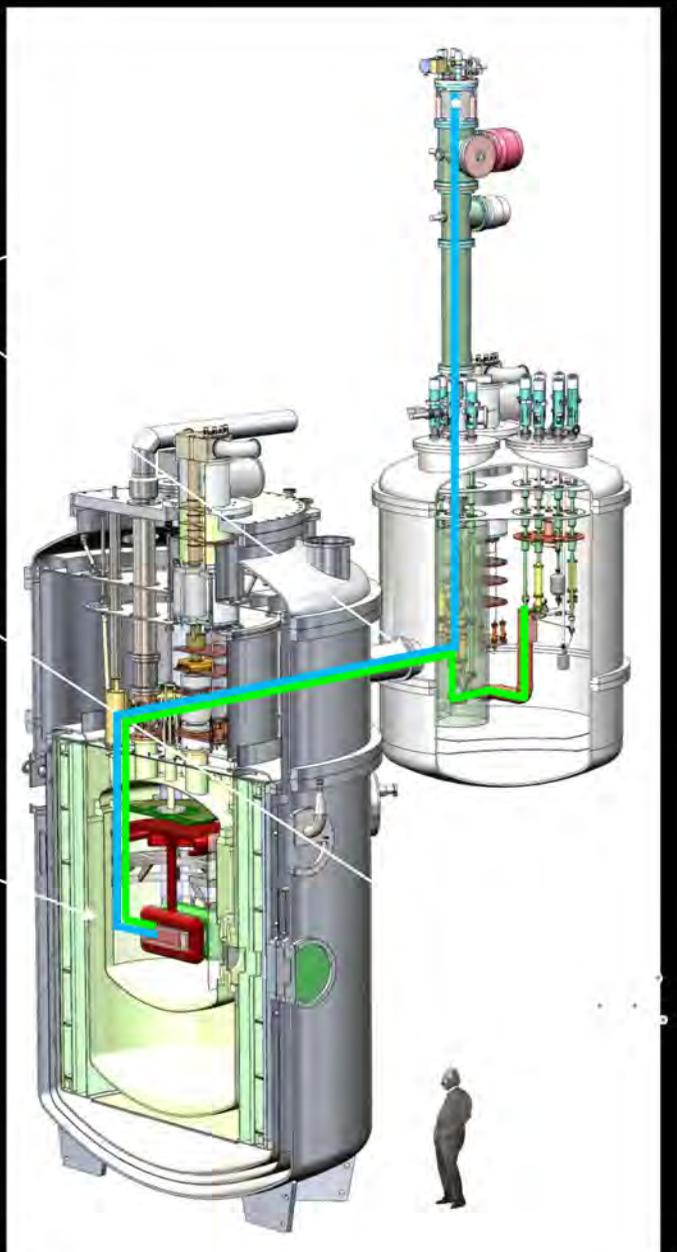
nEDM@SNS

Measurement Cycle

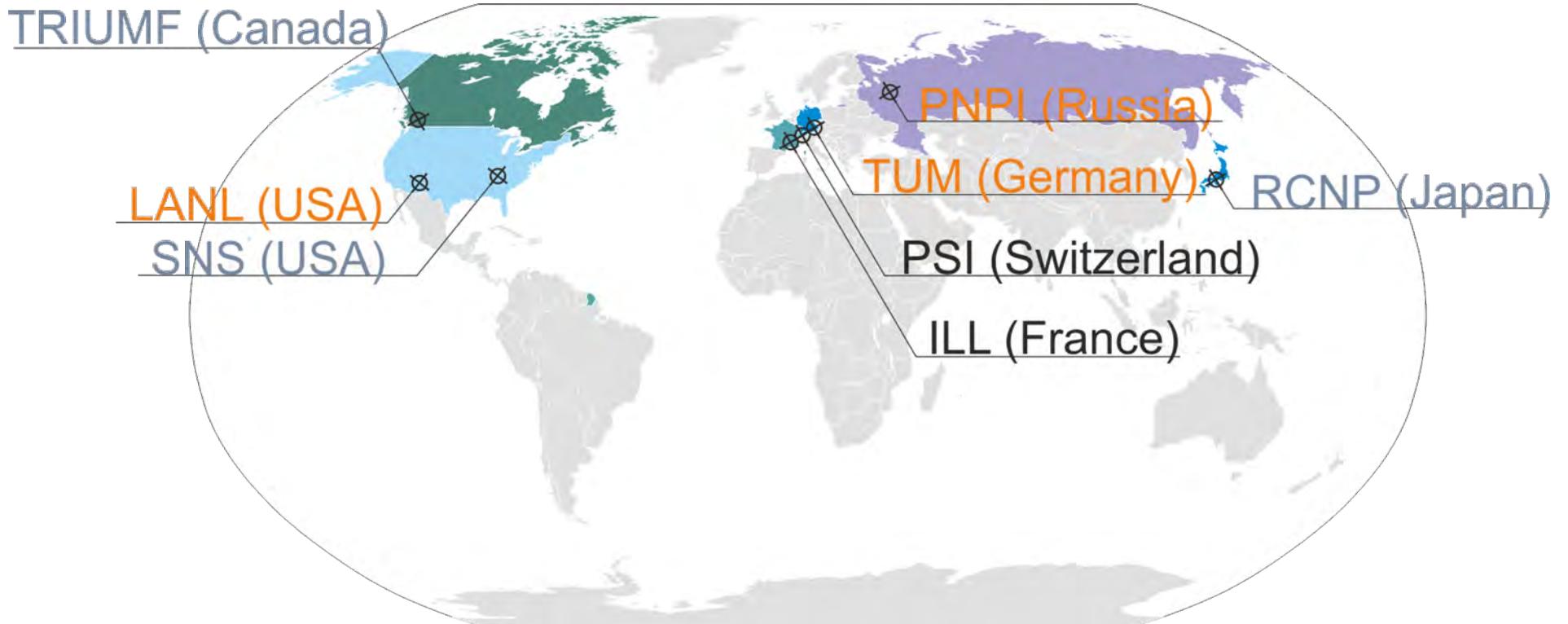
1. Load collection volume with polarized ^3He atoms
2. Transfer polarized ^3He atoms into measurement cell
3. Illuminate measurement cell with polarized cold neutrons to produce polarized UCN
4. Apply a $\pi/2$ pulse to rotate spins perpendicular to B_0
5. Measure precession frequency
6. Remove reduced polarization ^3He atoms from measurement cell
7. Flip E-field & Go to 1.



Slide thanks to Vince Cianciolo

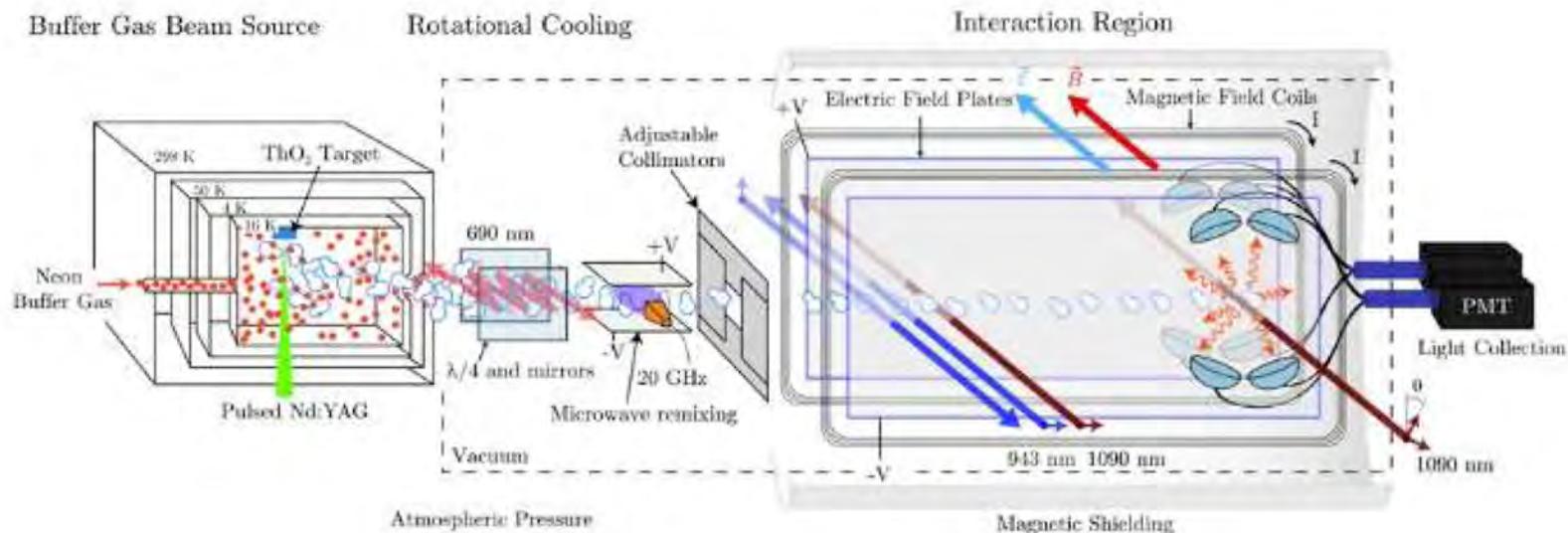


Neutron EDM searches are in progress at many facilities world wide



The Neutron EDM search is complementary to other types of EDM measurements

ACME experiment

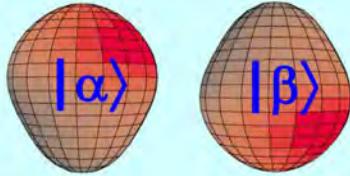


$$d_e = (-2.1 \pm 3.7_{\text{stat}} \pm 2.5_{\text{syst}}) \times 10^{-29} \text{ e} \cdot \text{cm}$$

Science 17 Jan 2014:
Vol. 343, Issue 6168, pp. 269-272



$$10 \text{ V/cm} \rightarrow 10 \cdot 10^9 \text{ V/cm},$$



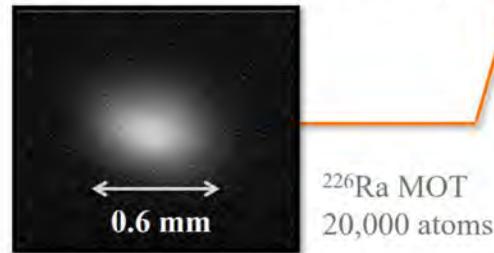
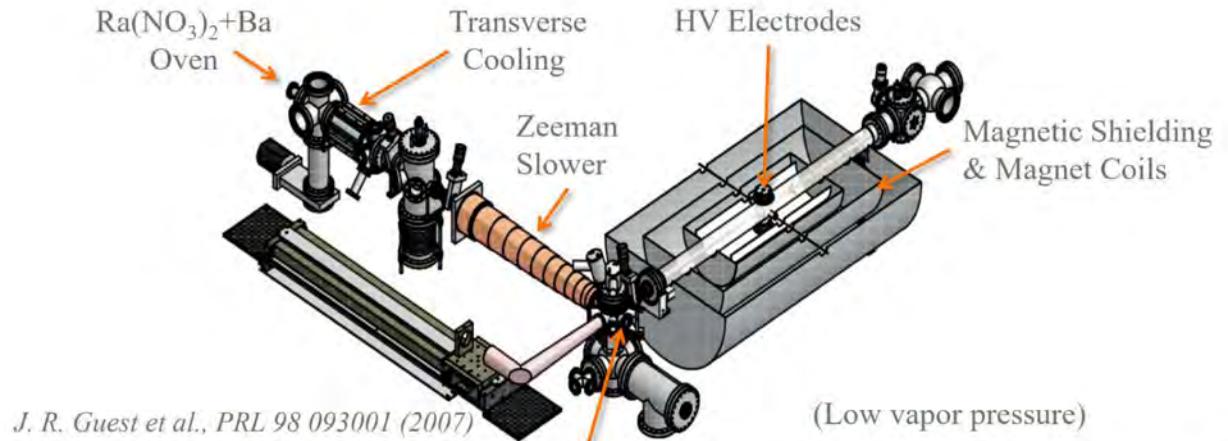
A large quadrupole and octupole deformation results in an enhanced Schiff moment
 – Auerbach, Flambaum & Spevak (1996)

Enhancement Factor: EDM (^{225}Ra) / EDM (^{199}Hg)

Skyrme Model	Isoscalar	Isovector	Isotensor
SIII	300	4000	700
SkM*	300	2000	500
SLy4	700	8000	1000

Radium-255 deformed nuclei

Collect Atoms in MOT

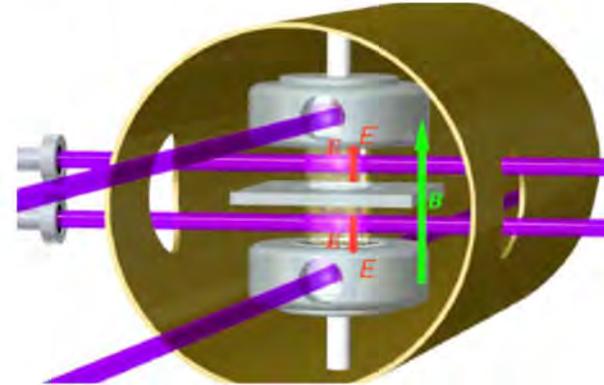


For EDM:	For Testing:
Ra-225	Ra-226
$I = 1/2, J = 0$	$I = 0, J = 0$
$t_{1/2} = 15 \text{ days}$	$t_{1/2} = 1600 \text{ yrs}$

The Seattle ^{199}Hg (atomic) EDM Measurement



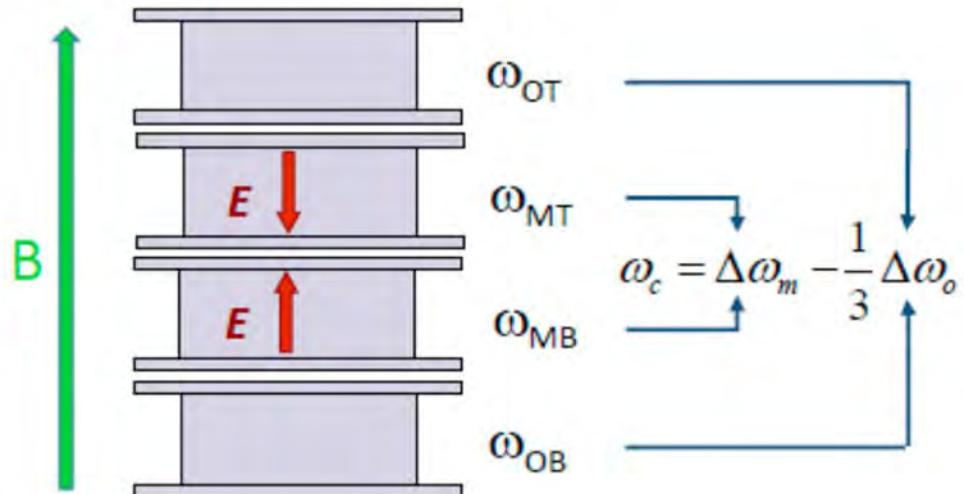
4 mercury vapor Cells:
2 with opposite **E** fields
2 for **B** field normalization



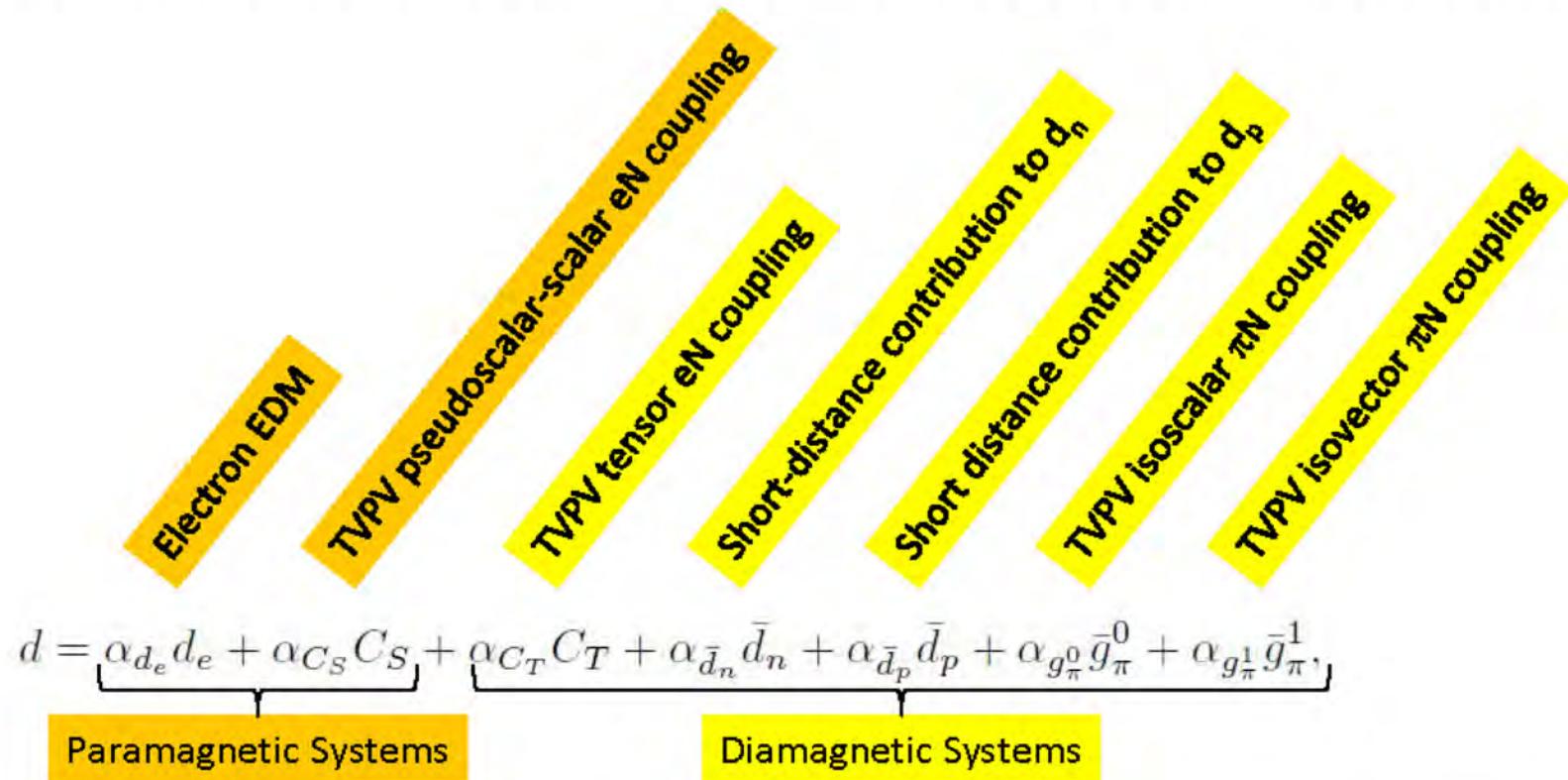
$$H = -(\vec{\mu} \cdot \vec{B} + \vec{d} \cdot \vec{E})$$

$$\omega_c = \frac{\mu}{\hbar} \left(-\frac{8}{3} \frac{\partial^3 B}{\partial z^3} \Delta z^3 \right) + \frac{4dE}{\hbar}$$

Cancels up to 2nd order gradient noise
Same EDM sensitivity as Middle Difference



Why Do We Need So Many Experiments?



T. Chupp, M. Ramsey-Musolf, Phys. Rev. C91 035502 (2015)

End of Lecture 3