

Electron-Ion Collider

NNPSS Lectures 2017 (Day 2) Rik Yoshida, Jefferson Lab

July 2017

NNPSS Lectures 2017



PLAN FOR THE LECTURES

Day 1:

- Prologue
- Some History
- Deep Inelastic Scattering and Parton Distributions (I)

Day 2:

- **DIS and PDF (II)**
- **Beyond parton distributions.**

Day 3:

- EIC accelerator and detector realizations
- Other facilities and EIC physics topics.
- EIC and physics topic at other facilities.
- EIC and the future of Nuclear Physics.
- Epilogue

DEEP INELASTIC SCATTERING AND PARTON DISTRIBUTION (II).

Quarks and Gluons as partons

$u(x)$: up quark distribution

$\bar{u}(x)$: up anti-quark distribution

etc.

Momentum has to add up to 1 (“momentum sum rule”)

$$\int x[u(x) + \bar{u}(x) + d(x) + \bar{d}(x) + s(x) + \bar{s}(x) + \dots] dx = 1$$

Quantum numbers of the nucleon has to be right

So for a proton:

$$\int [u(x) - \bar{u}(x)] dx = 2$$

$$\int [d(x) - \bar{d}(x)] dx = 1$$

$$\int [s(x) - \bar{s}(x) + \dots] dx = 0$$

e-p Neutral Current (NC) cross-section:

We'll come back
to these

Has to do with
long. photon.
Only large at
largest y

Has to do with
Z₀ exchange:
small for Q << M_Z

$$\frac{d^2\sigma}{dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4} [Y_+ F_2(x, Q^2) - y^2 F_1(x, Q^2) + Y_- x F_3(x, Q^2)]$$

$$Y_{\pm} = 1 \pm (1-y)$$

$$y = Q^2/xs \quad 0 \leq y \leq 1 \quad \text{"inelasticity"}$$

So for now:

$$\frac{d^2\sigma}{dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4} Y_+ F_2(x, Q^2)$$

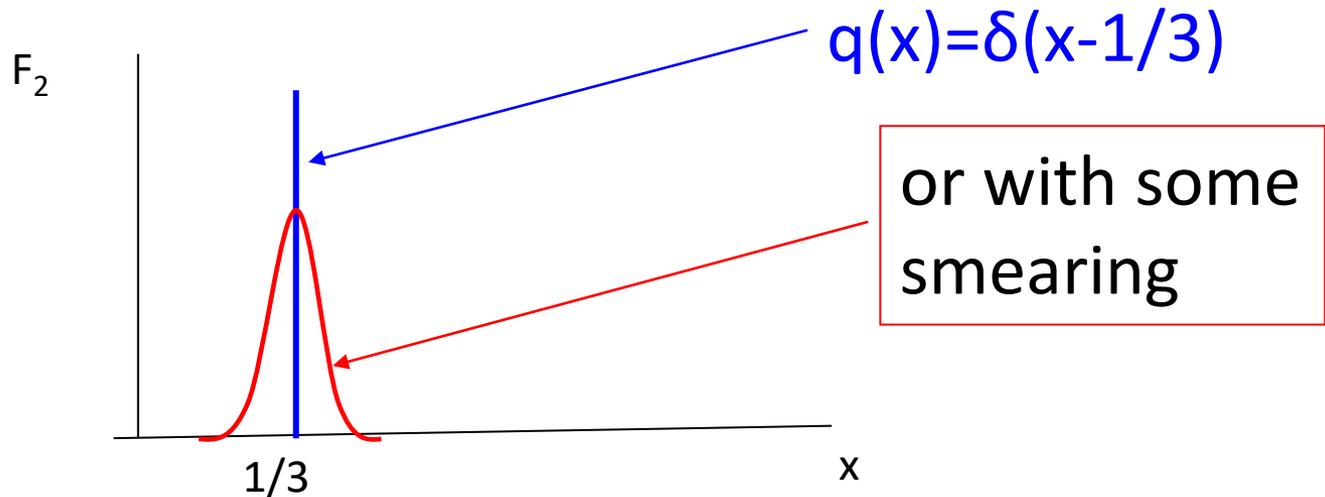
quark charge

$$F_2 = x \sum (q + \bar{q}) e_q^2 + Z\text{-exchange}$$

If, proton was made of 3 quarks each with 1/3 of proton's momentum:

$$F_2 = x \sum (q(x) + \bar{q}(x)) e_q^2$$

no anti-quark!

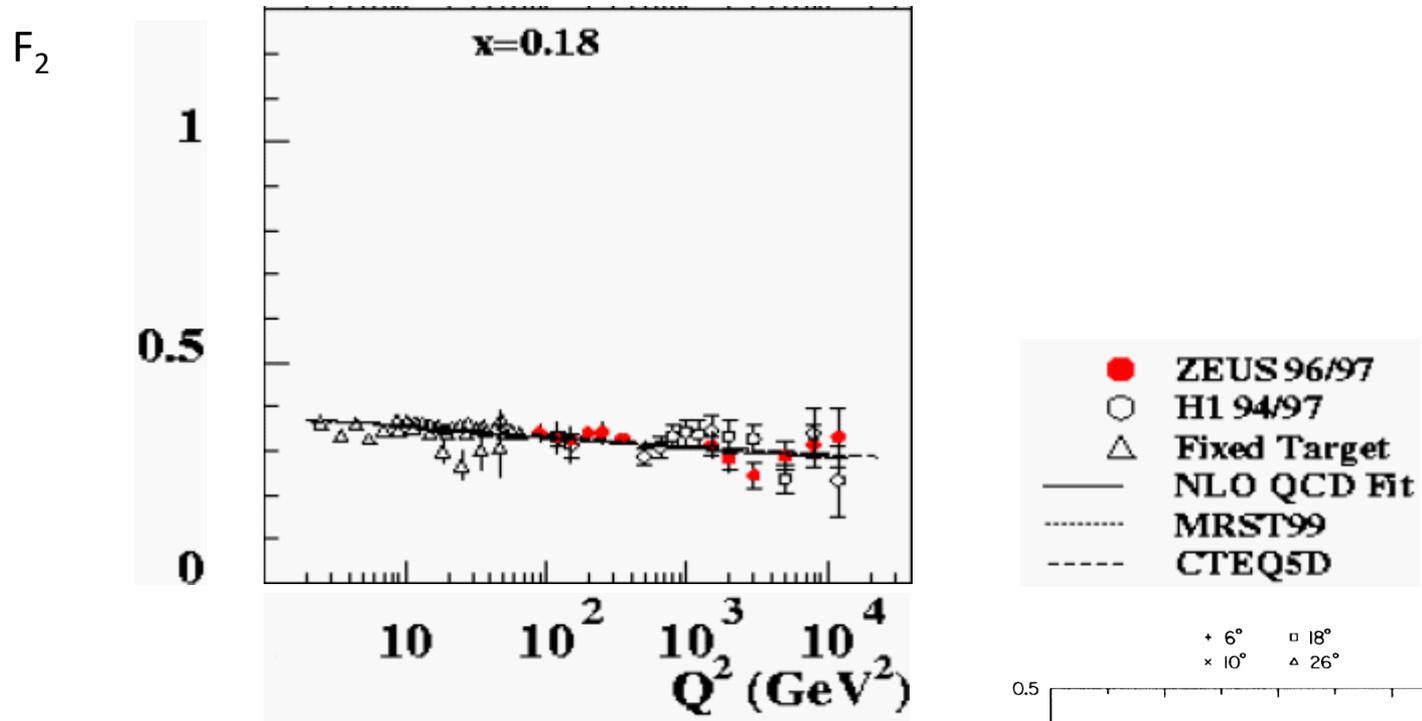


The partons are point-like and incoherent then Q^2 shouldn't matter.

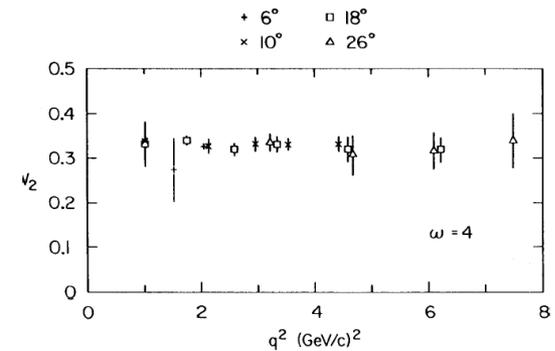
→ **Bjorken scaling**: F_2 has no Q^2 dependence.

Let's look at some data →

Proton Structure Function F_2



Seems to be.... **NOT**



So far:

$F_2 \sim \sum(q+\bar{q}) \approx S$ (sea quarks) measured directly in
NC DIS

Scaling violations

$dF_2/d\ln Q^2 \sim \alpha_s \bullet g$ Scaling violations gives gluons
(times α_s). DGLAP equations.

What about valence quarks?

$\sum(q-q) = u_v + d_v$ can we determine them separately?

Can we decouple α_s and g ?

Return to Neutral Current (NC) cross-section:

Now write out the e^+p and e^-p separately
(keep ignoring F_L for now..)

$$Y_{\pm} = 1 \pm (1-y)$$

$$\frac{d^2\sigma(e^{\pm}p)}{dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4} [Y_+ F_2(x, Q^2) \mp Y_- xF_3(x, Q^2)]$$

$$xF_3 = \sum (q(x, Q^2) - \bar{q}(x, Q^2)) xB_q \sim \text{The valence quarks!}$$

$$B_q = -2e_q a_q a_e \chi_Z + 4v_q a_q v_e a_e \chi_Z^2$$

$$\chi_Z = \frac{1}{\sin 2\theta_W} \left(\frac{Q^2}{M_Z^2 + Q^2} \right) \quad \text{Keeps } xF_3 \text{ small if } Q < M_Z$$

Return to Neutral Current (NC) cross-section:

Now write out the e^+p and e^-p separately
(keep ignoring F_L for now..)

$$Y_{\pm} = 1 \pm (1-y)$$

$$\frac{d^2\sigma(e^{\pm}p)}{dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4} [Y_+ F_2(x, Q^2) \mp Y_- xF_3(x, Q^2)]$$

$xF_3 = \sum (q(x, Q^2) - \bar{q}(x, Q^2)) xB_q \sim$ The valence quarks!

$$B_q = \underbrace{-2e_q a_q a_e}_{\gamma\text{-Z interference}} x_Z + \underbrace{4v_q a_q v_e a_e}_{\text{Z-exchange}} x_Z^2$$

e_q : electric charge of a quark

$a_q v_q$: axial-vector and vector couplings of a quark

$a_e v_e$: axial-vector and vector couplings of an electron

Return to Neutral Current (NC) cross-section:

Now write out the e^+p and e^-p separately
(keep ignoring F_L for now..)

$$Y_{\pm} = 1 \pm (1-y)$$

$$\frac{d^2\sigma(e^{\pm}p)}{dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4} [Y_+ F_2(x, Q^2) \mp Y_- xF_3(x, Q^2)]$$

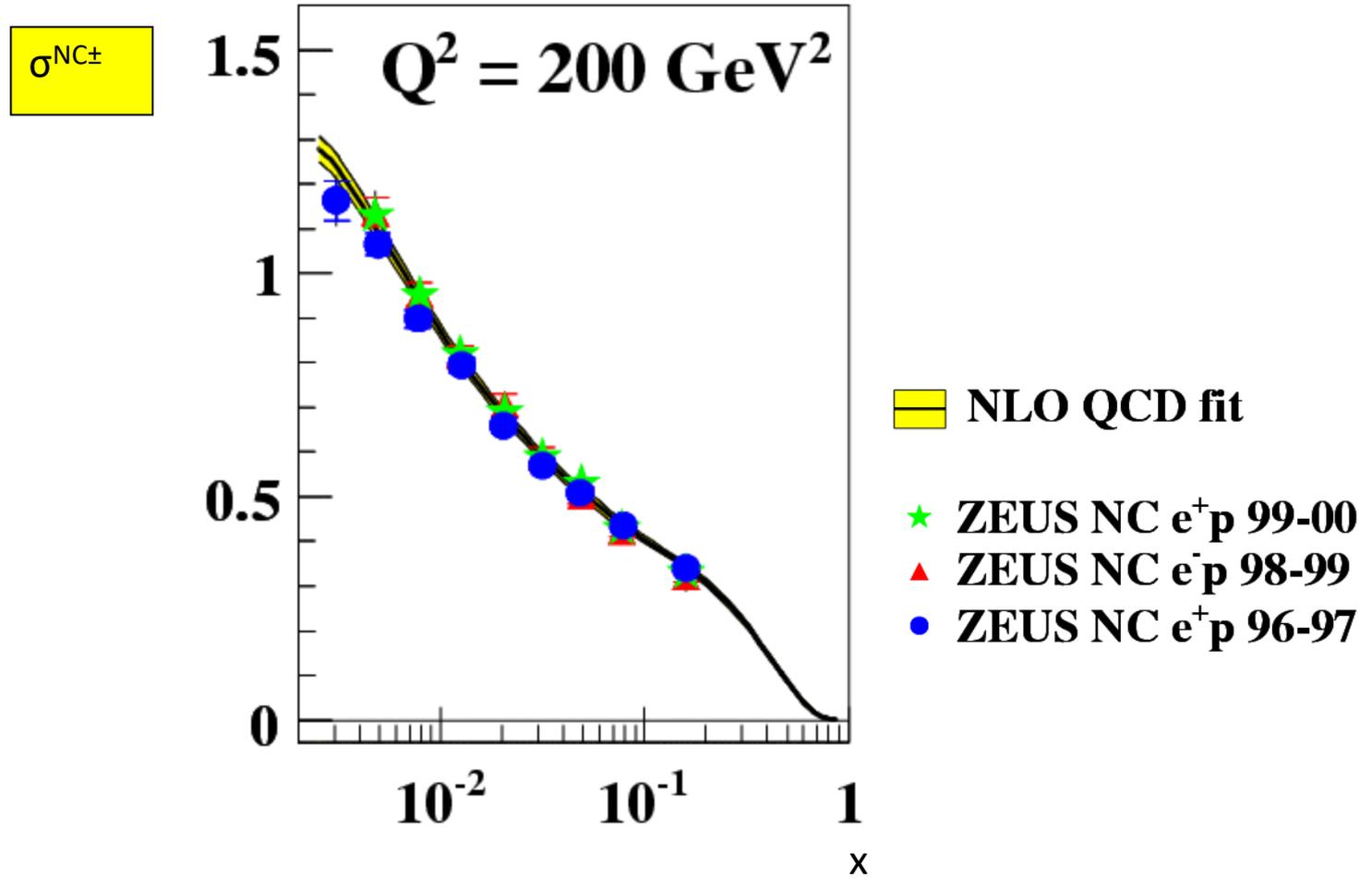
$$xF_3 = \sum (q(x, Q^2) - \bar{q}(x, Q^2)) xB_q \sim \text{The valence quarks!}$$

Let's look at the "reduced NC cross-section"

$$\sigma^{NC\pm} = F_2(x, Q^2) \mp (Y_- / Y_+) \bullet xF_3(x, Q^2)$$

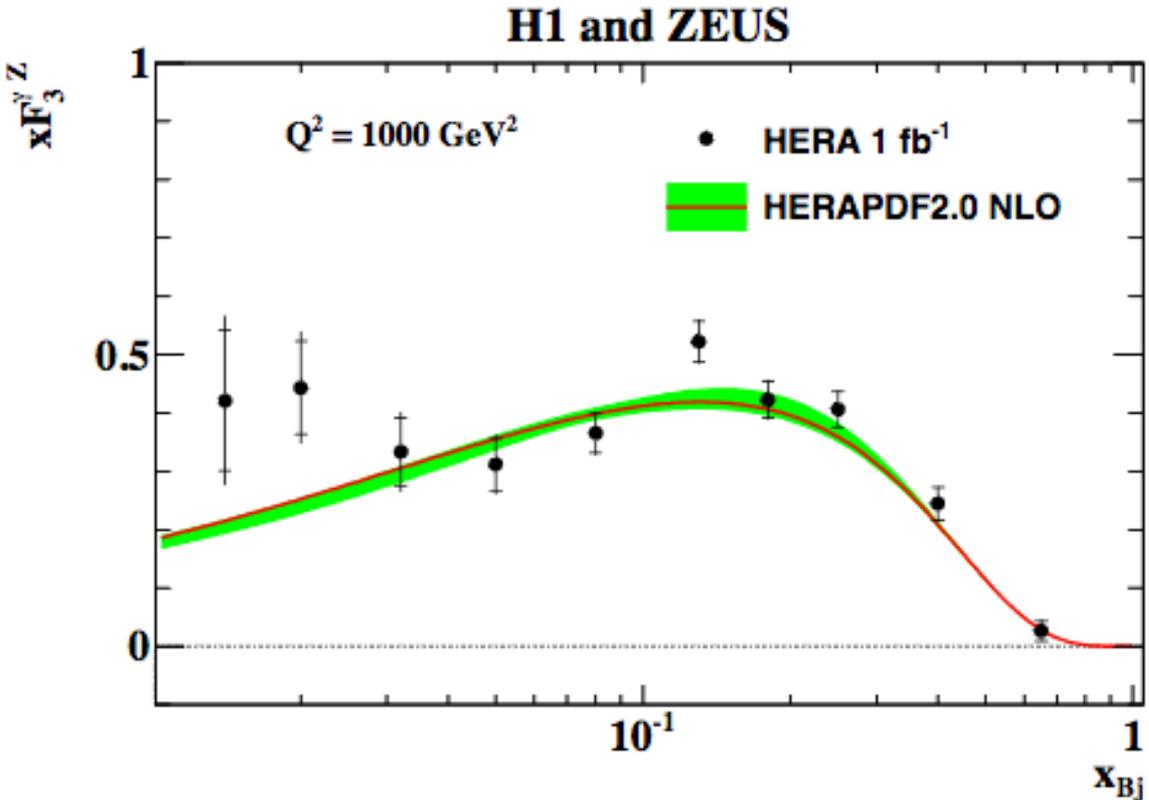
Note the change of sign from e^+p to e^-p

Reduced Neutral Current Cross-section

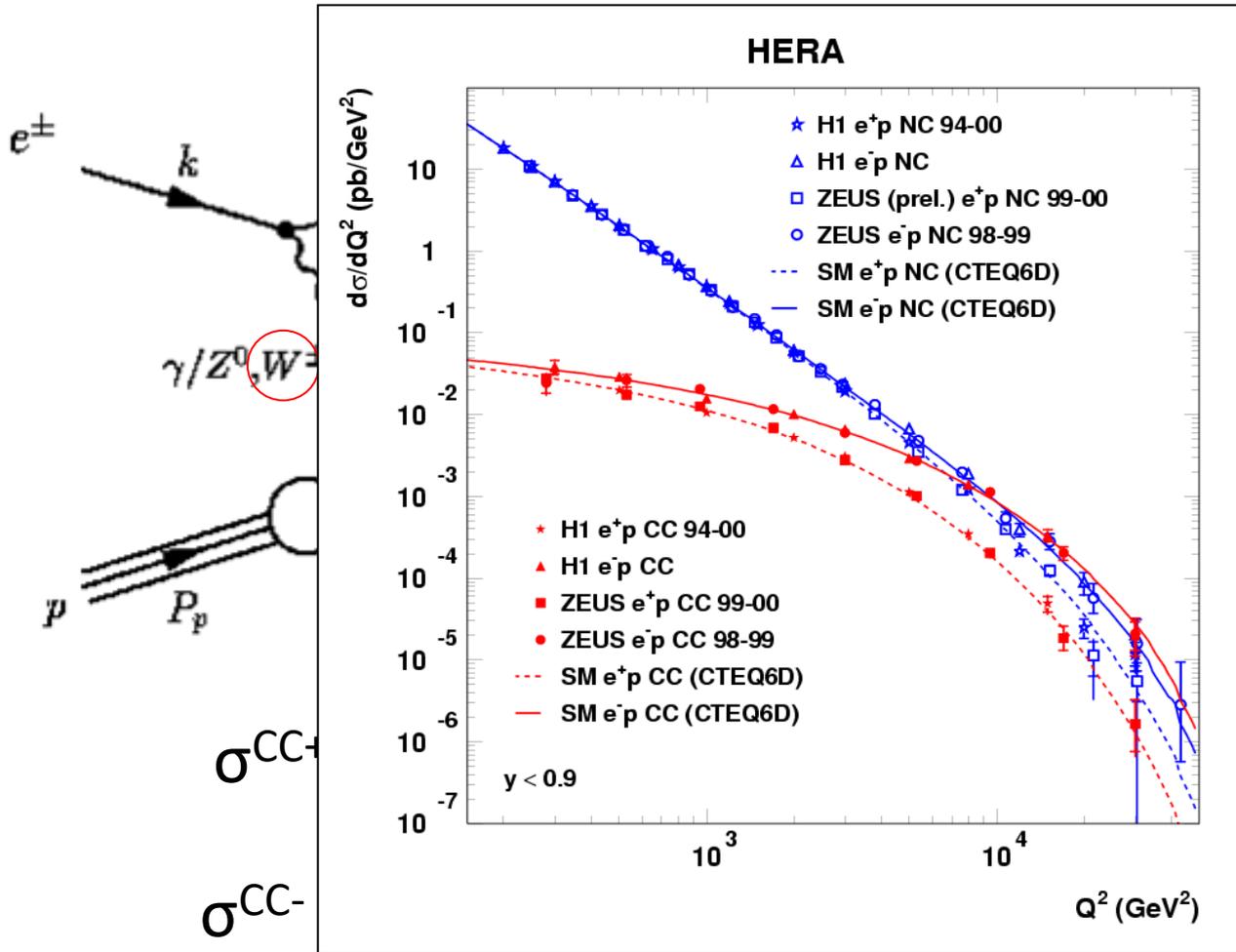


Measurements are at relatively high x

Final result from HERA



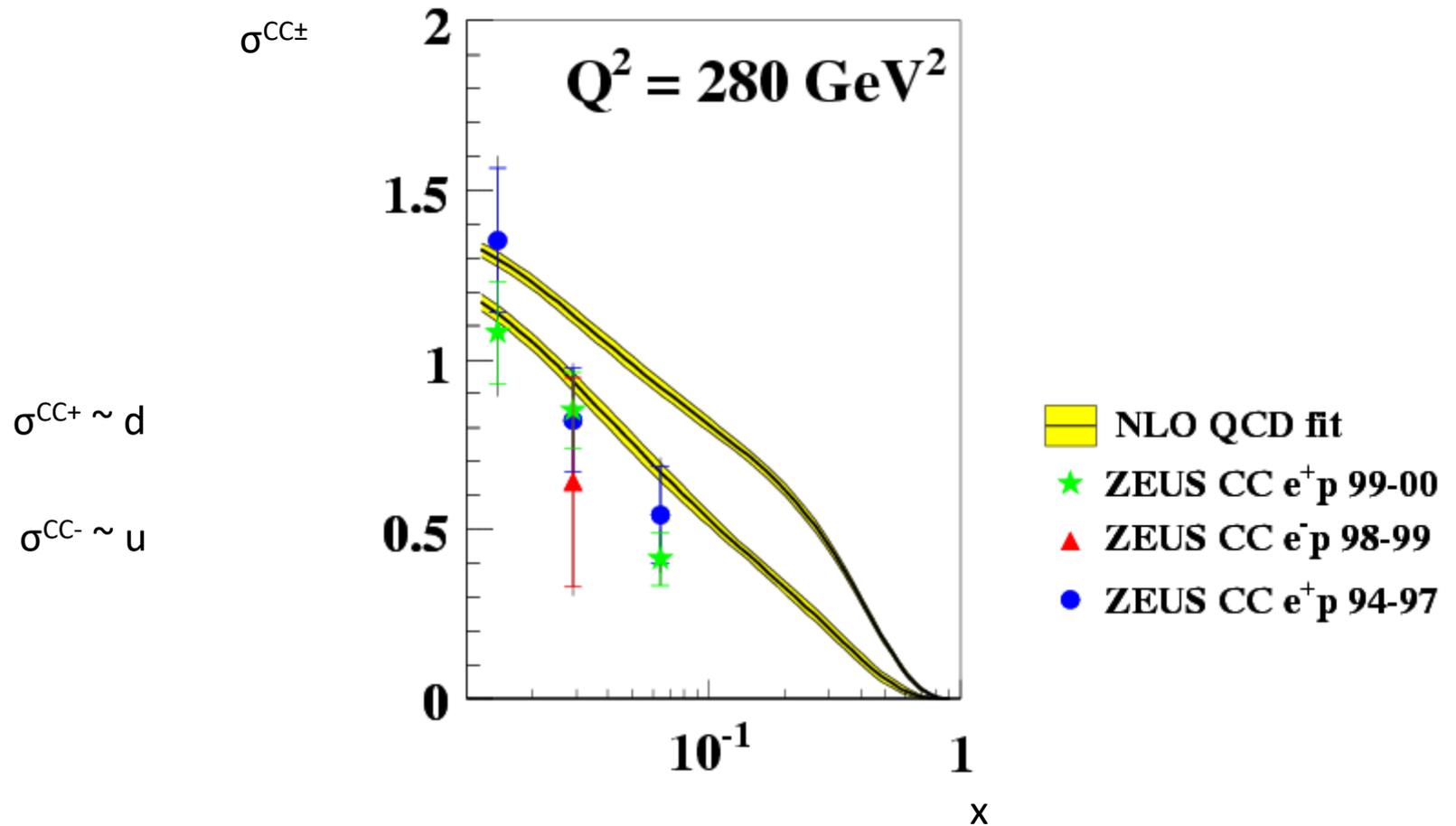
Charged Current Cross-Sections



$$\left[\frac{M_W^2}{M_W^2 + Q^2} \right]^2 \sigma^{CC\pm}$$

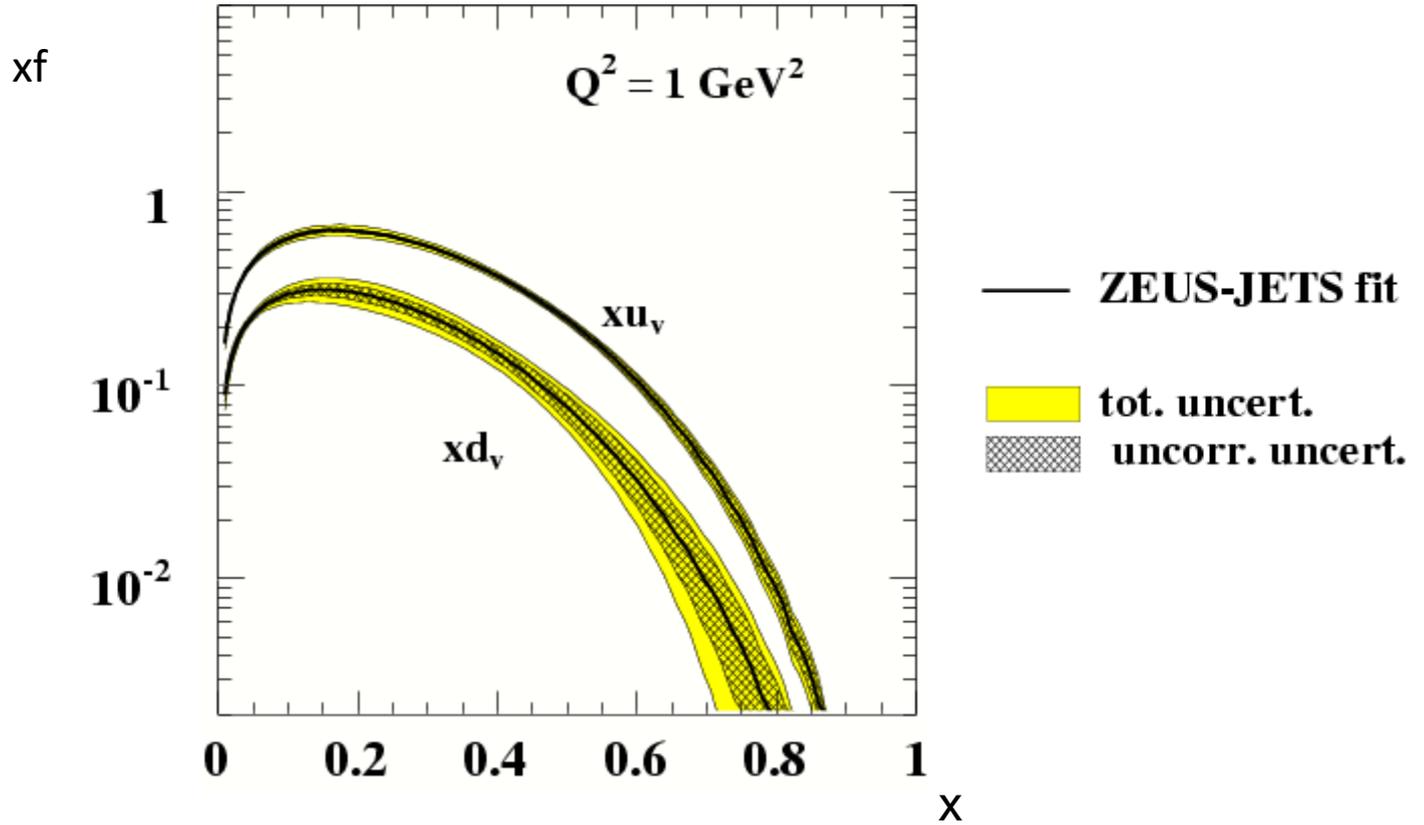
charm

Reduced Charged-Current Cross-Section



Now let's look at the valence quarks from the QCD fits →

Valence PDFs

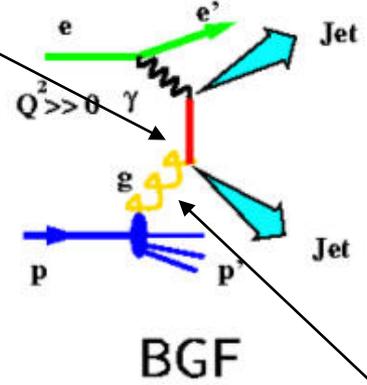
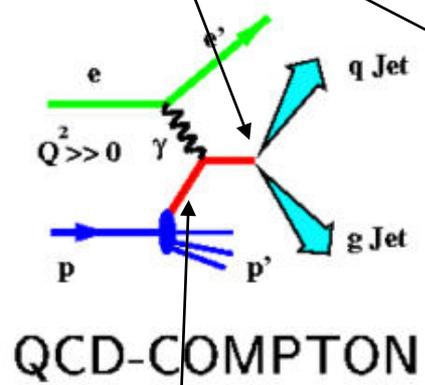


The momenta from valence quarks are producing gluons and sea quarks at low x

Jet production in DIS (HERA)

Sensitive to α_s

$$\sigma_{\text{jet}} \sim \alpha_s \cdot f(x)$$



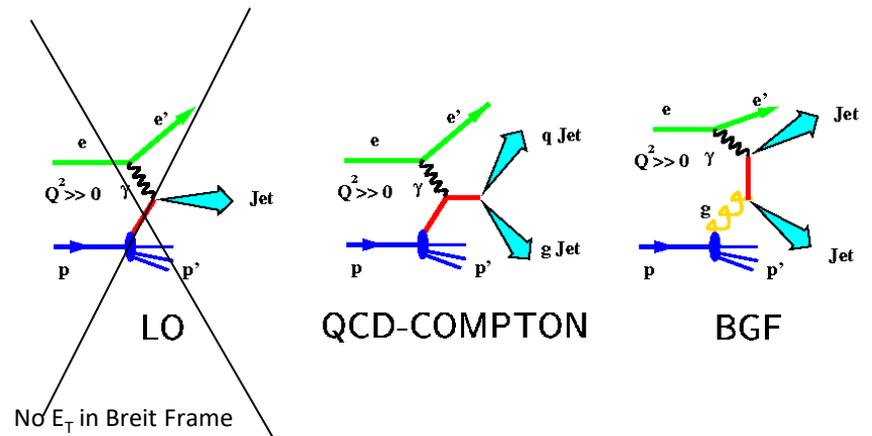
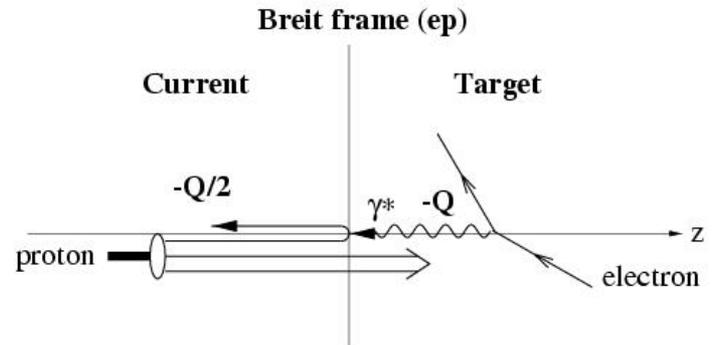
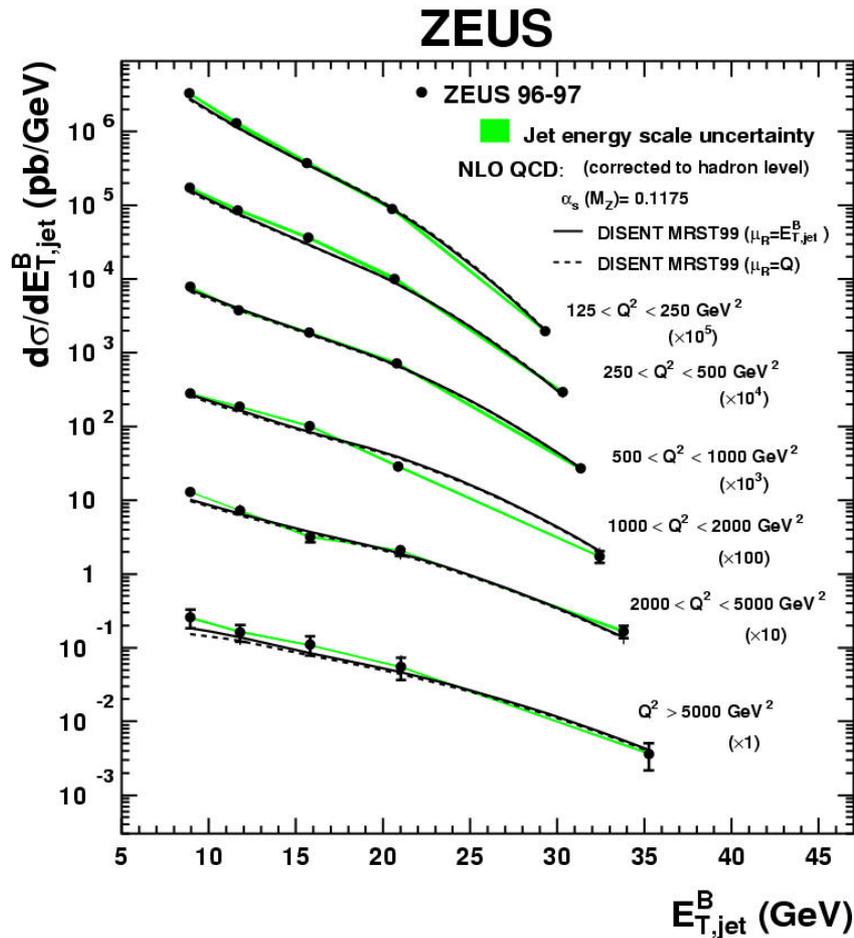
Sensitive to quarks
 $\sim 10^{-2} < x < \sim 10^{-1}$

Sensitive to gluon
 $\sim 10^{-3} < x < \sim 10^{-2}$

Same range as NC and CC

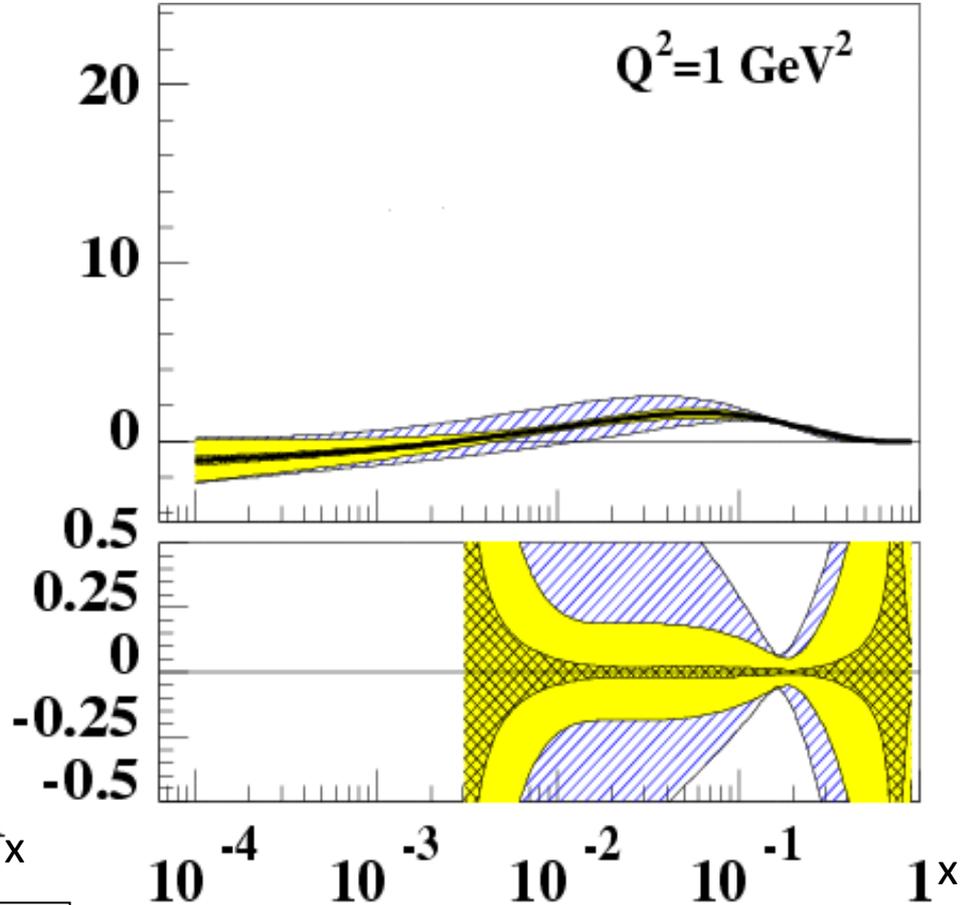
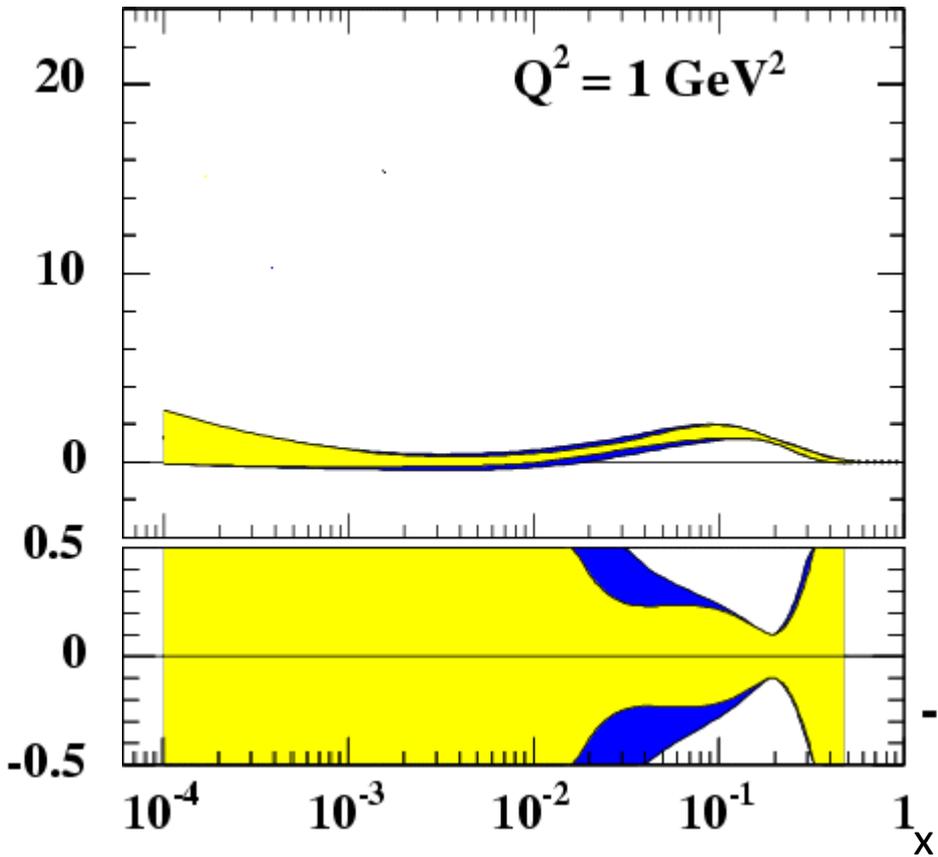
complementary to gluon from F_2

Jet measurements in Breit frame



Jet production cross-section used in QCD fit →

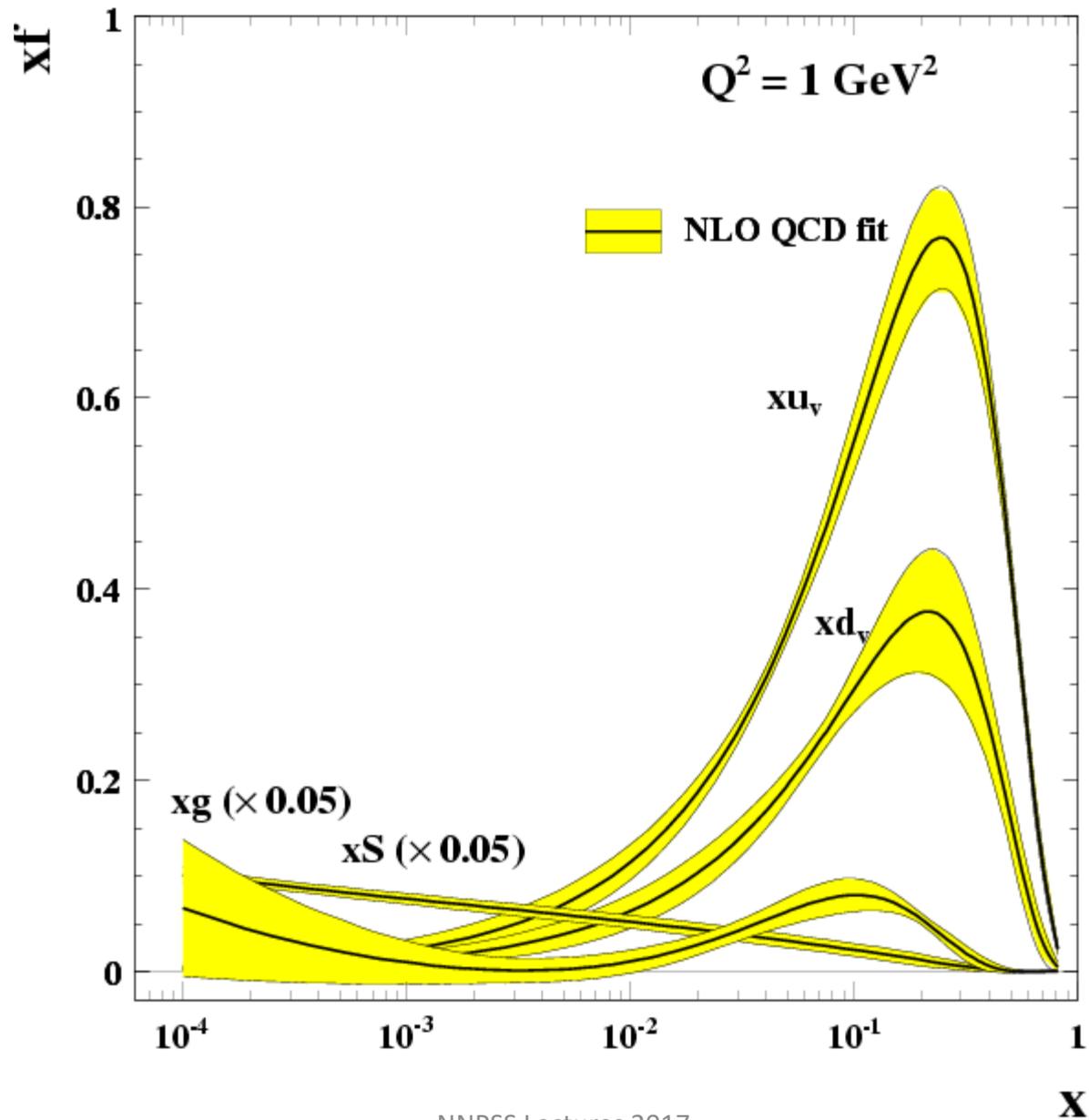
Gluon distributions



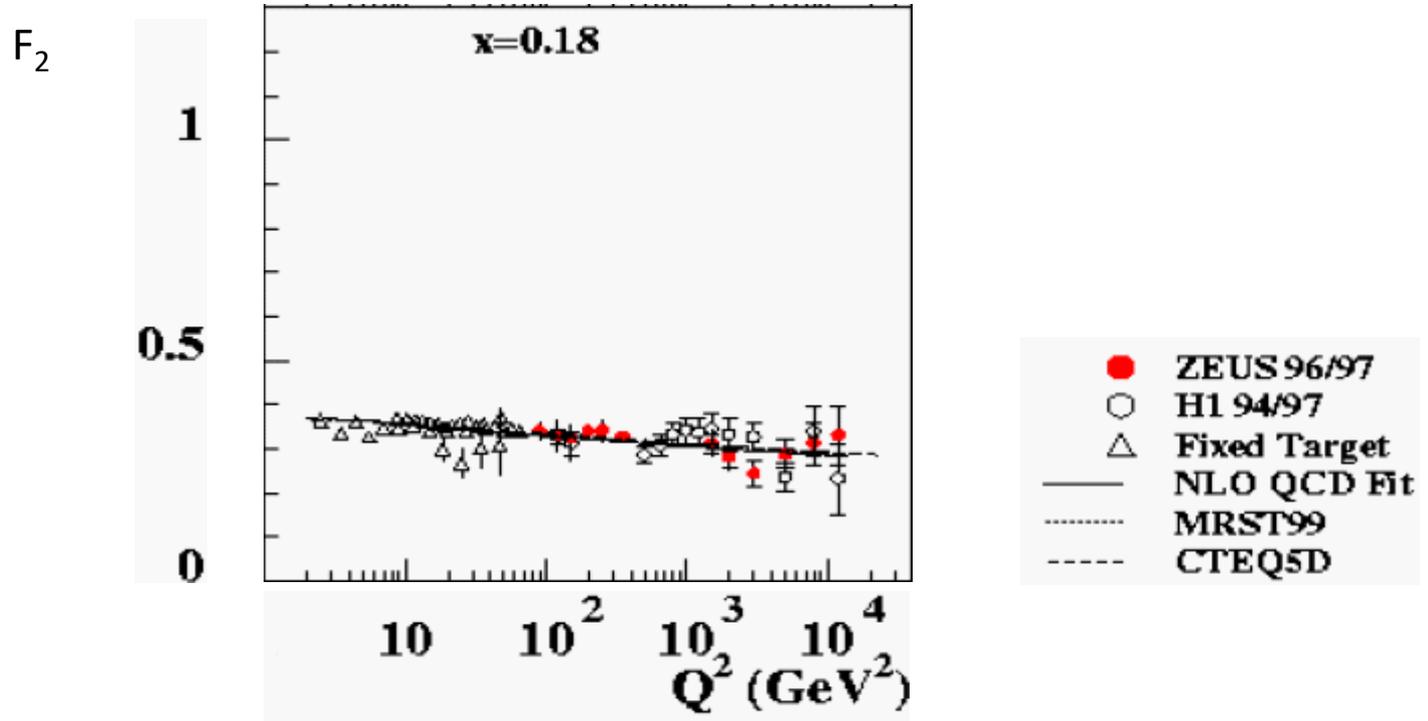
Using only HERA (ZEUS) data including NC, CC and jets

Using HERA (ZEUS) F_2 data and FNAL, CERN fixed tgt

Finally...



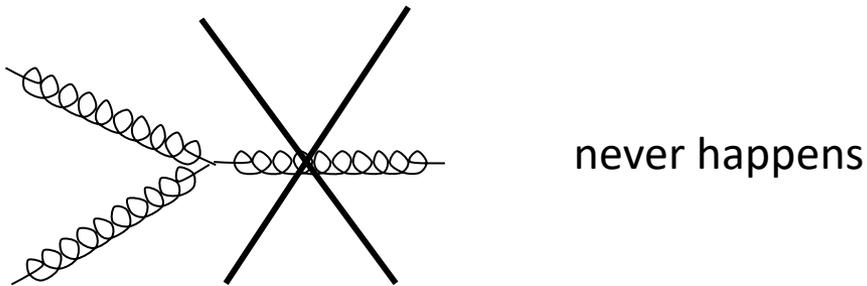
Proton Structure Function F_2



Now we understand what is happening here.

Some remarks about DGLAP equations:

The “**incoherence**” of the original parton model is preserved. i.e. a parton doesn't know anything about its neighbor.

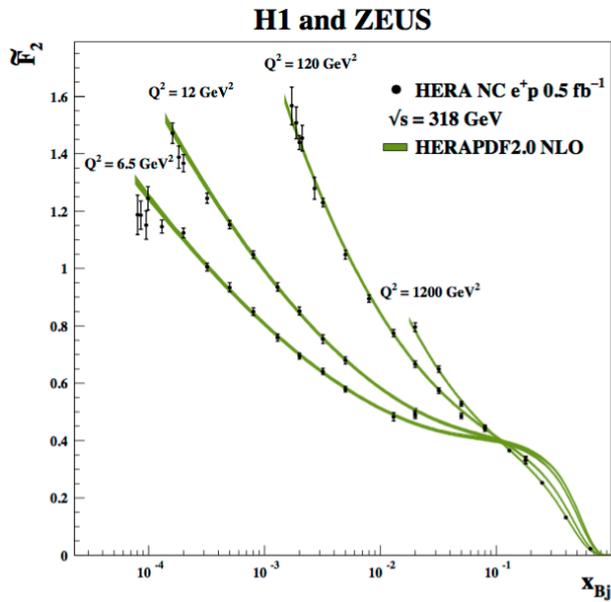


The “**process independent**” partons also survive.

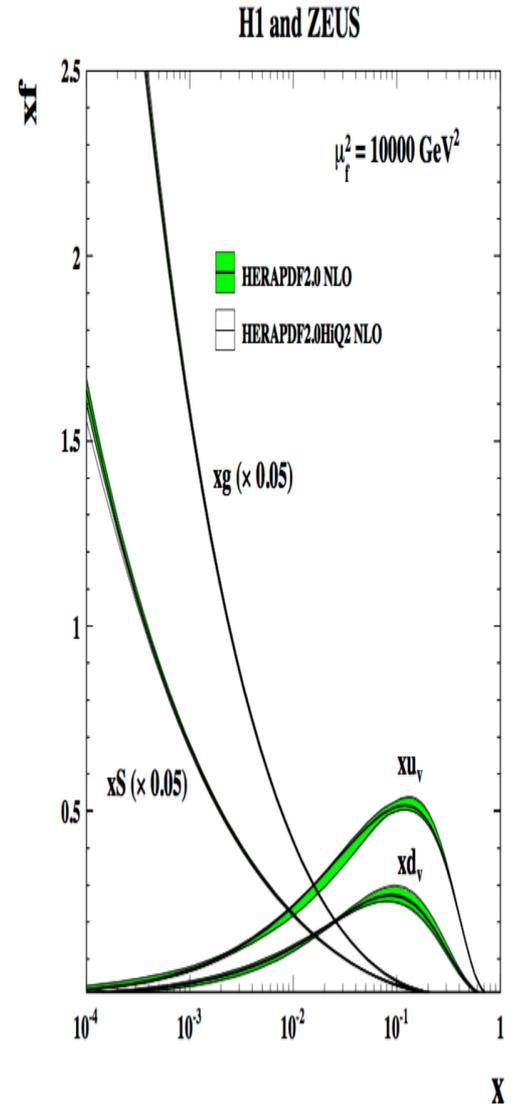
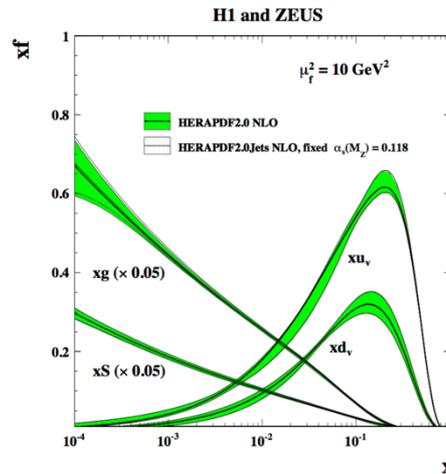
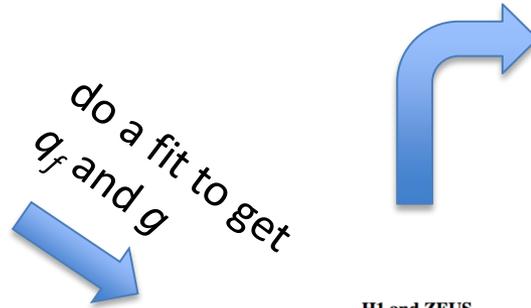
But now parton densities must be “evolved” in Q^2 .

What does this mean? →

How this works



Q^2 (or μ^2) evolution



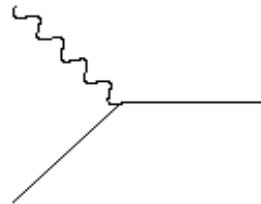
Structure function F_L

Longitudinal cross-section

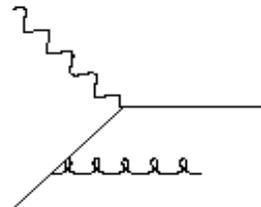
- F_L corresponds to absorption of longitudinally polarized virtual photon.

$$F_L = (Q^2/4\pi^2\alpha) \sigma_L$$

- Spin 1/2 quarks (with no transverse momentum) cannot absorb a longitudinally polarized boson.



LO: $\mathbf{k}_T=0$, $F_L=0$



NLO: $\mathbf{k}_T \neq 0$, $F_L \neq 0$

$$F_L = \frac{\alpha_s}{4\pi} x^2 \int_x^1 \frac{dz}{z^3} \left[\frac{16}{3} F_2 + 8 \sum e_q^2 \left(1 - \frac{x}{z}\right) zg \right]$$

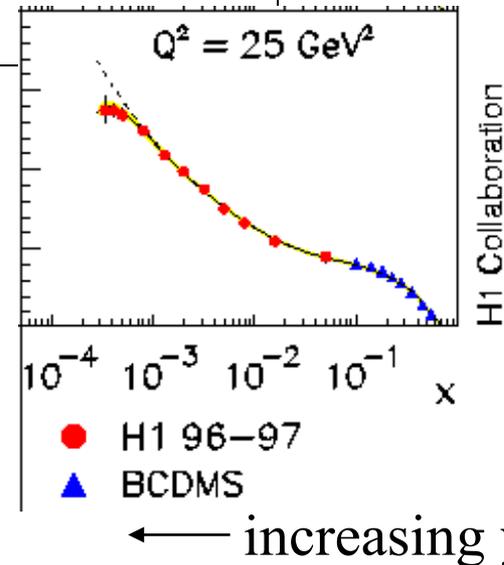
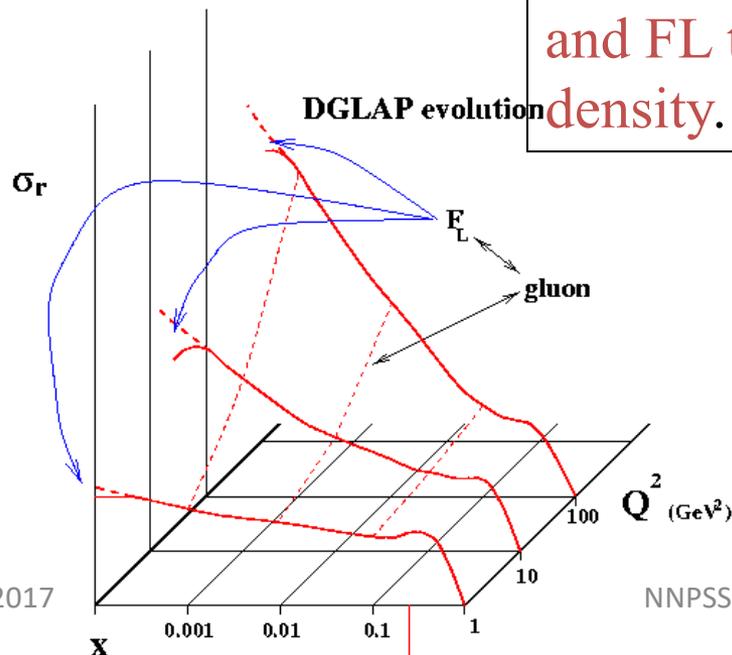
- At higher orders, quarks have transverse momentum (k_T), and therefore $F_L \neq 0$.
- F_L is related to the gluon density in the proton.

$$\frac{d\sigma^2}{dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4} (Y_+ F_2 - y^2 F_L \pm Y_- x F_3)$$

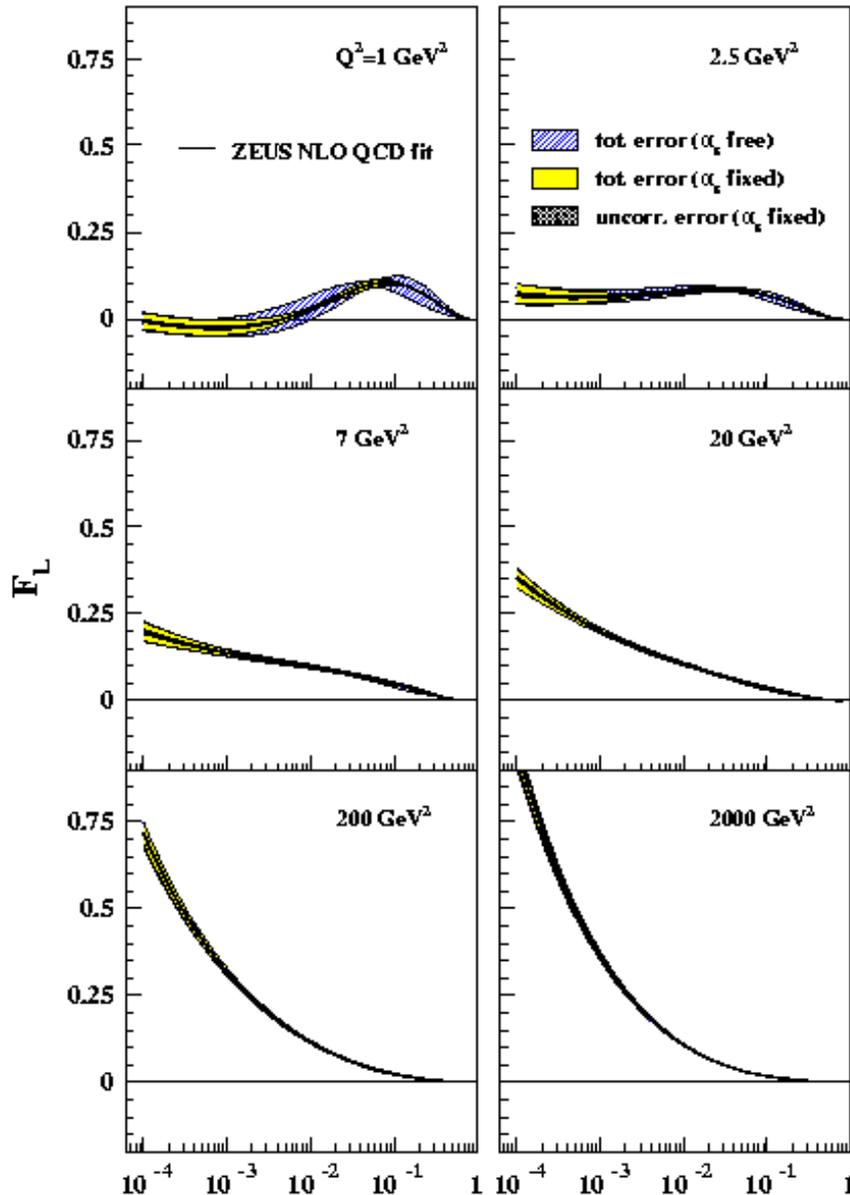
$y = Q^2/xs$: need to measure at different \sqrt{s} to get F_L (or indeed F_2 , in principle).

But...

QCD predicts a relationship between scaling violations and FL through the gluon density.



ZEUS



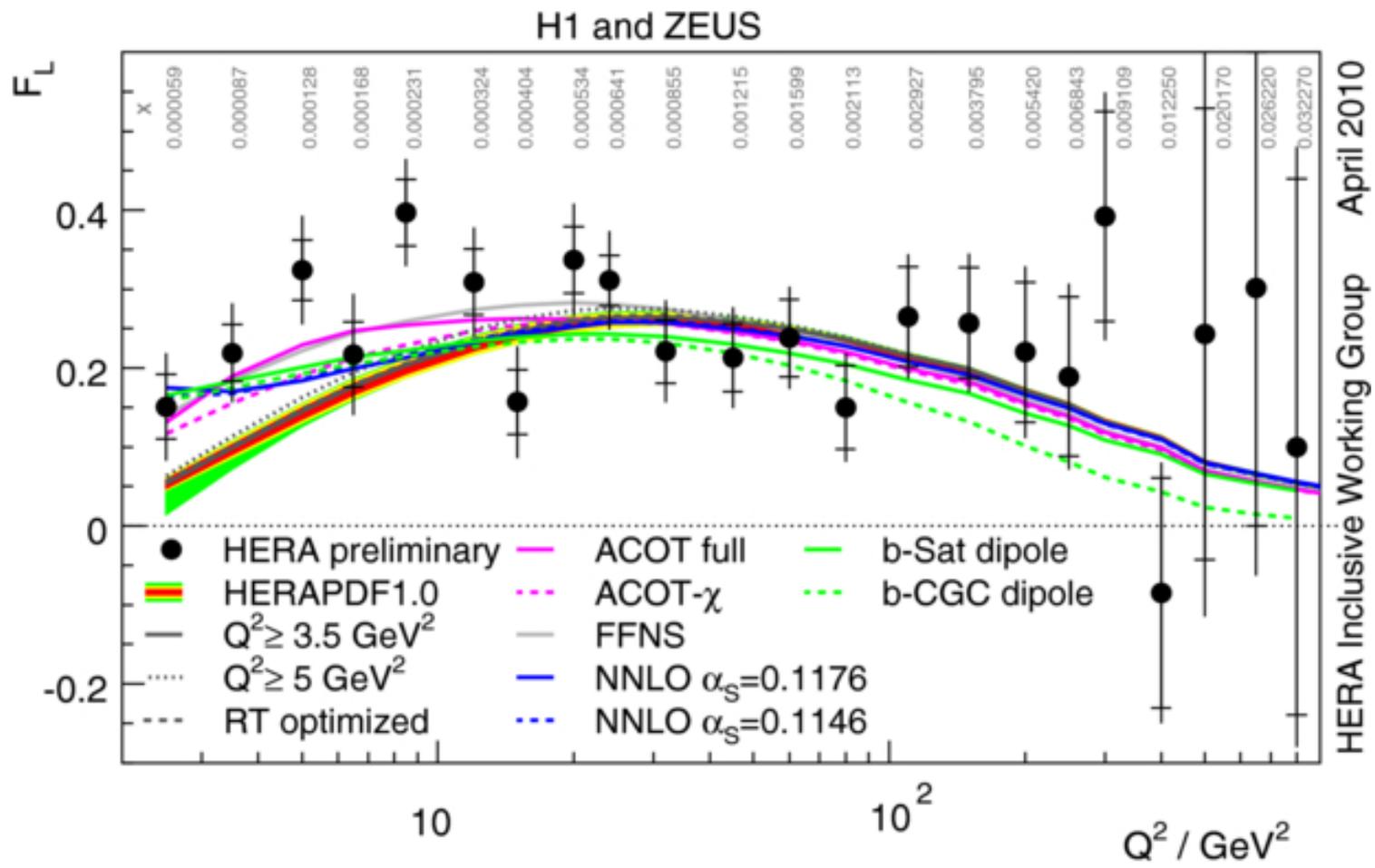
You can **determine**
 F_L from a NLO DGLAP
 fit to NC cross-section.

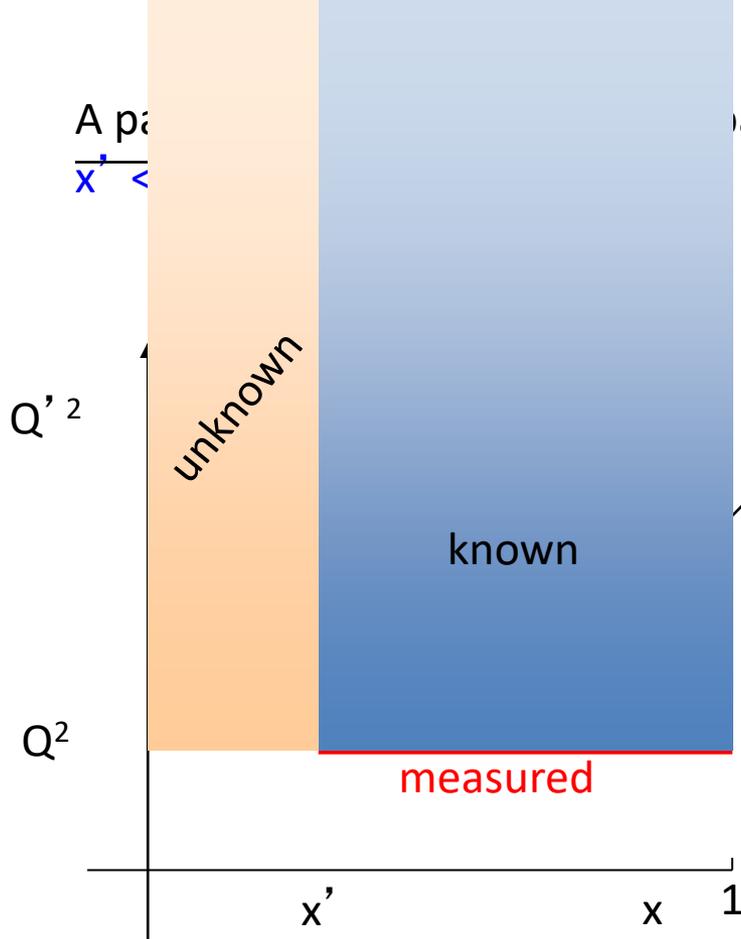
Indeed, we also only determine
 F_2 the same way, in principle:

$$\frac{d\sigma^2}{dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4} (Y_+ F_2 - y^2 F_L \pm Y_- x F_3)$$

We measure this only







In fact, any parton at $x > x'$ at Q^2 is a source.

To know the parton density at x' , Q'^2 it's necessary (and sufficient) to know the parton density in the range: $x' \leq x \leq 1$ at some lower Q^2 .

If you know the partons in range $x' \leq x \leq 1$ at some Q^2 , then you know the partons in the range $x' \leq x \leq 1$ for all $Q'^2 > Q^2$.

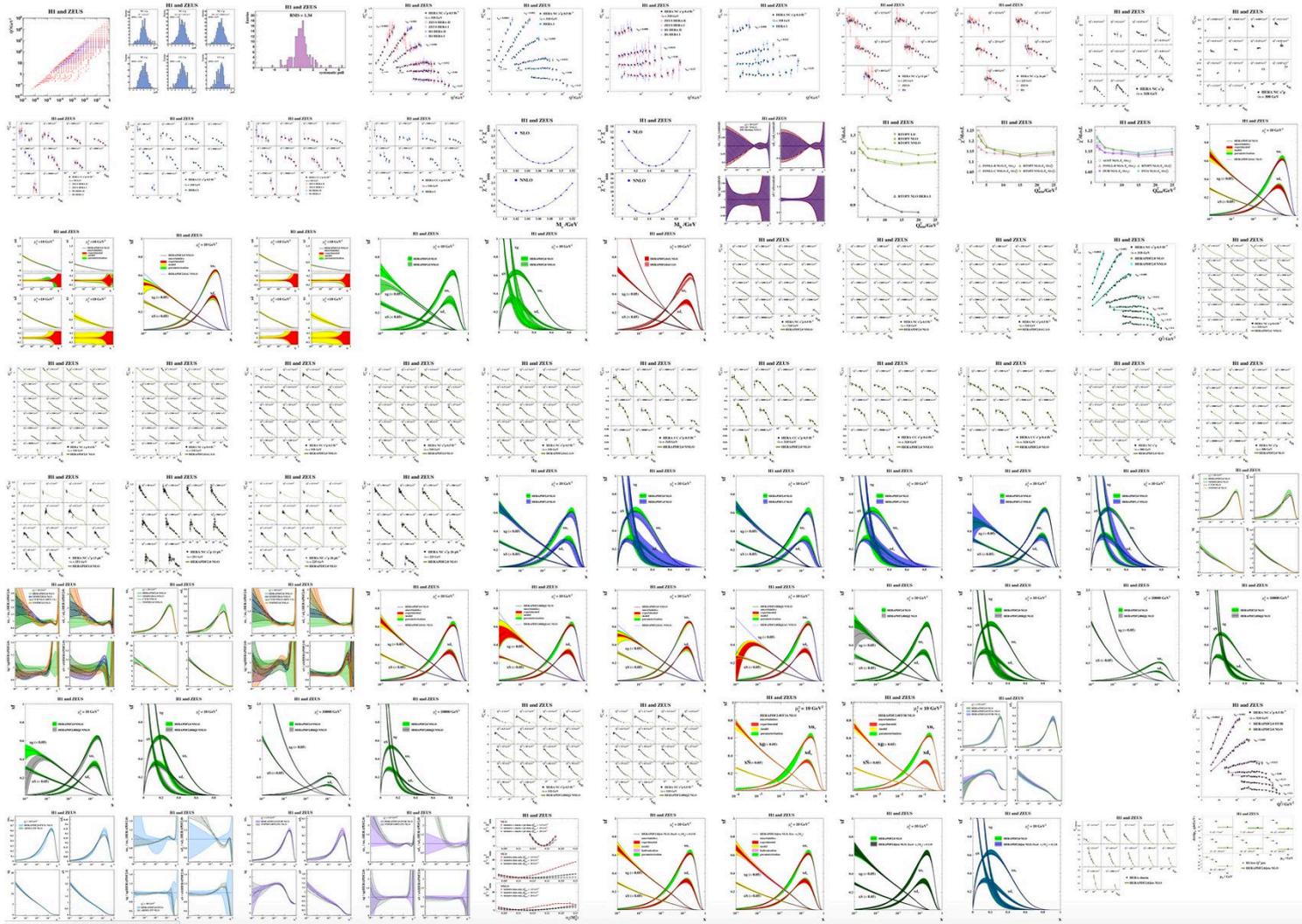
Some remarks I

- We've just gone through an informal tour of **QCD-improved parton model** and its application to data from **ep** Deep Inelastic Scattering.
- **Some health warnings:**
 - Most of what I talked about is a **leading-order** picture. In practice, most things are done at least to **next-to-leading** order. At NLO, the interpretation of the results are not as straight-forward.
 - Many people worry about whether we are not missing something fundamentally with the picture of **DGLAP equations**.
 - Much of the data are at very low x : **DGLAP** is a **$\ln Q^2$** approximation. Why aren't **$\ln(1/x)$** terms important...or are they?
→ **BFKL equations**.
 - The density of the partons, especially that of the **gluons** is getting very high. When and where should we worry about **“shadowing”**, **“gluon recombination”** etc.
 - The idea of **incoherence** of partons may be breaking down in some kinematic regions: phenomenon of **“hard diffraction”** is difficult to understand in terms of partons without correlations to each other.
 - We'll cover some of this in the next section.

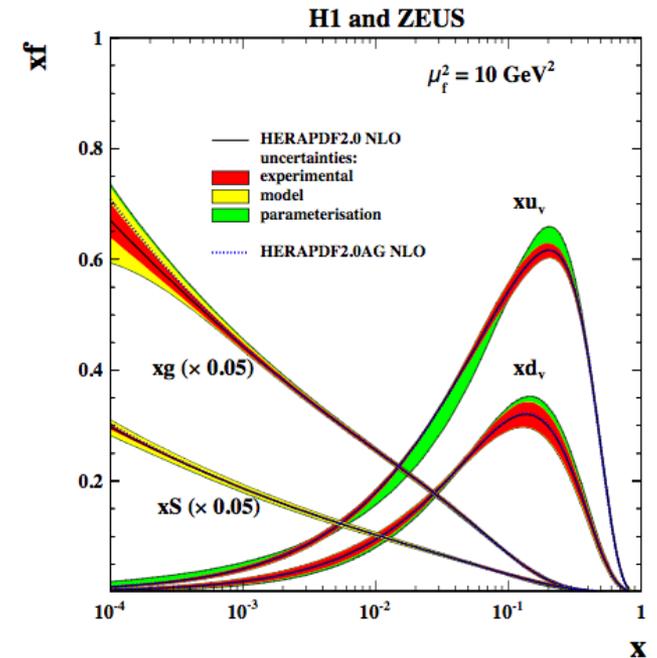
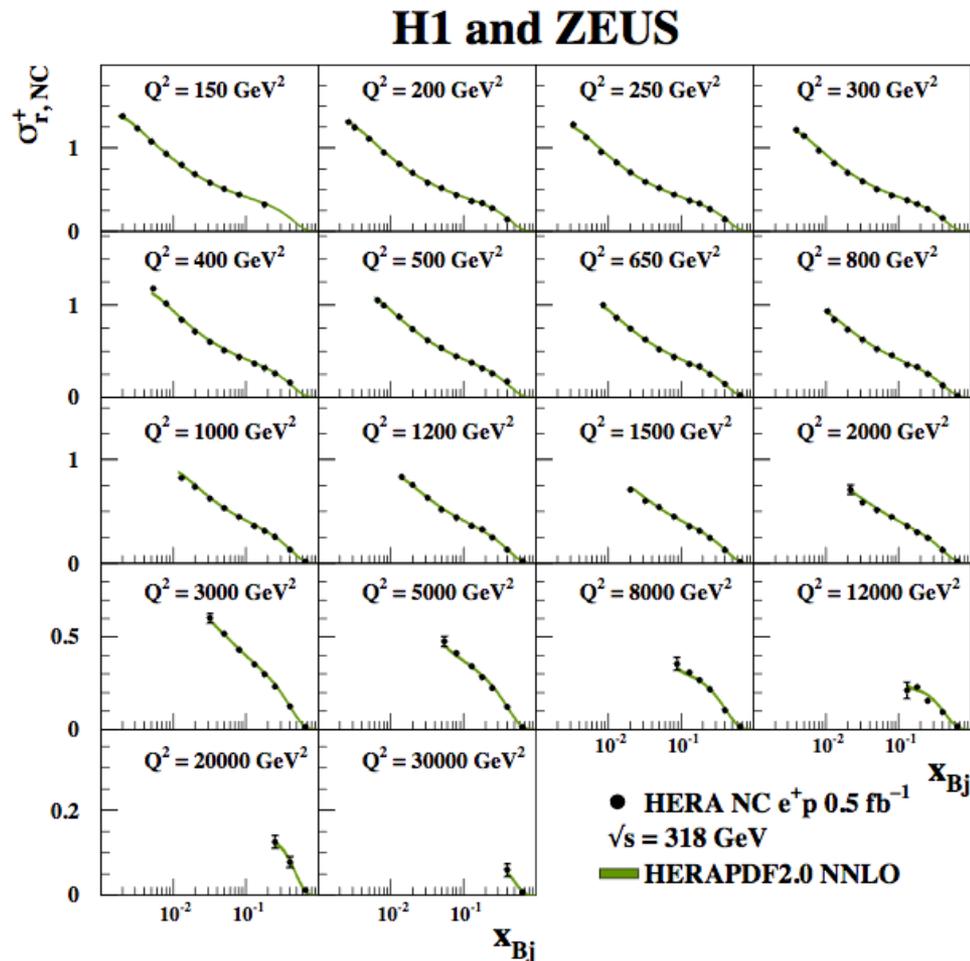
Some remarks II

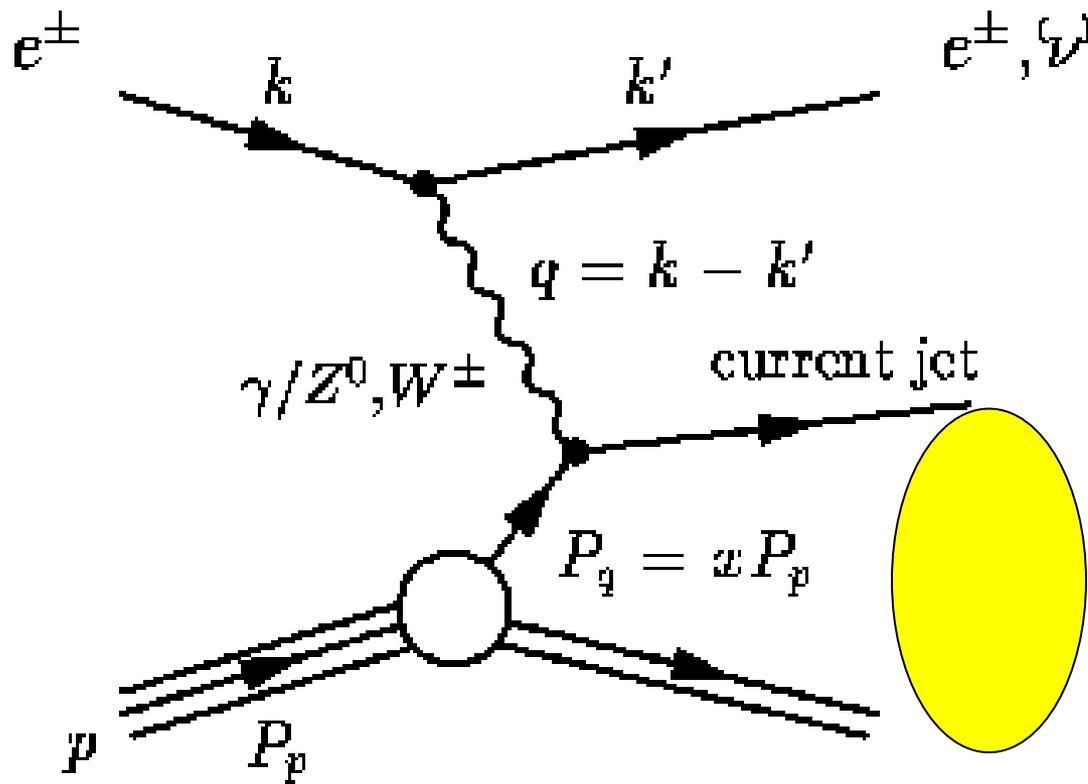
- Thanks to [Claire Gwenlan](#) for preparing some of the plots animation for me.
- However, the data used were relatively old.
- Final HERA (combined H1 and ZEUS) structure function data are summarized in the publication: **Eur.Phys.J. C75 (2015) no.12, 580**

Final St. Fcn. Results from HERA



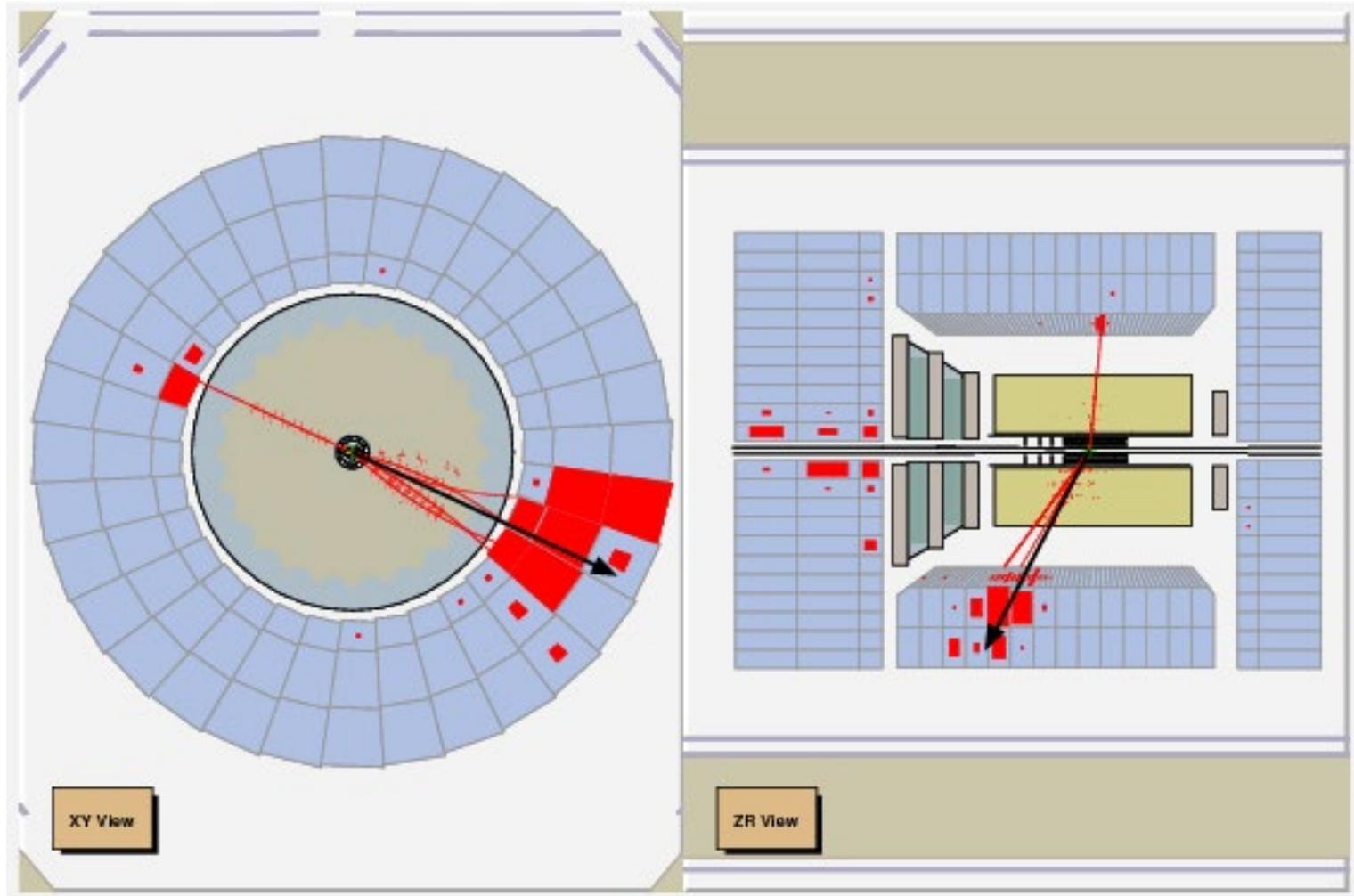
A small portion of the data.





color
 connection
 leads to
 particles
 in "gap".

DIS Event in the ZEUS Detector



NEXT

- We learned about parton distribution functions of the proton.
- Things are similar for polarized PDFs and Fragmentation Functions.
- Did we learn something about the proton?
- What is missing?

Now we enter areas without too many answers

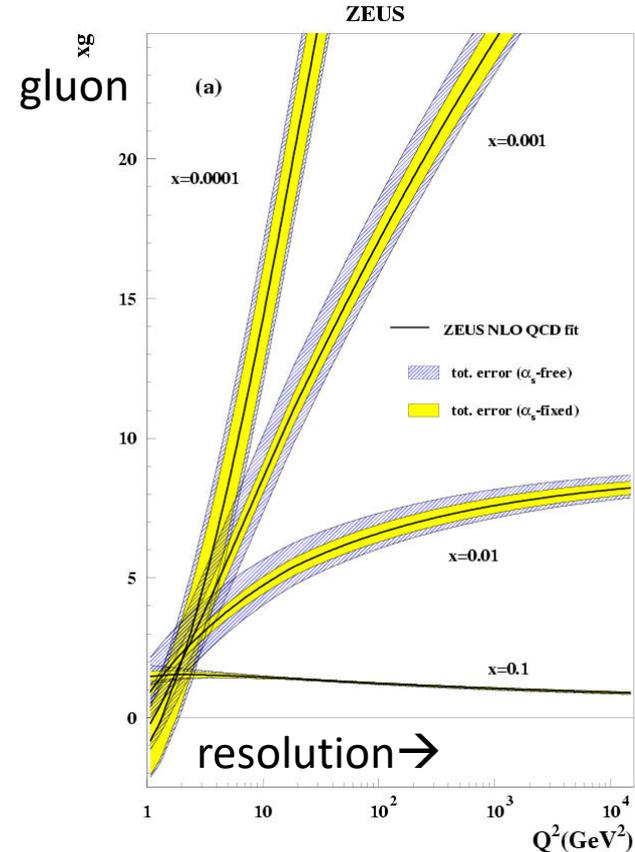
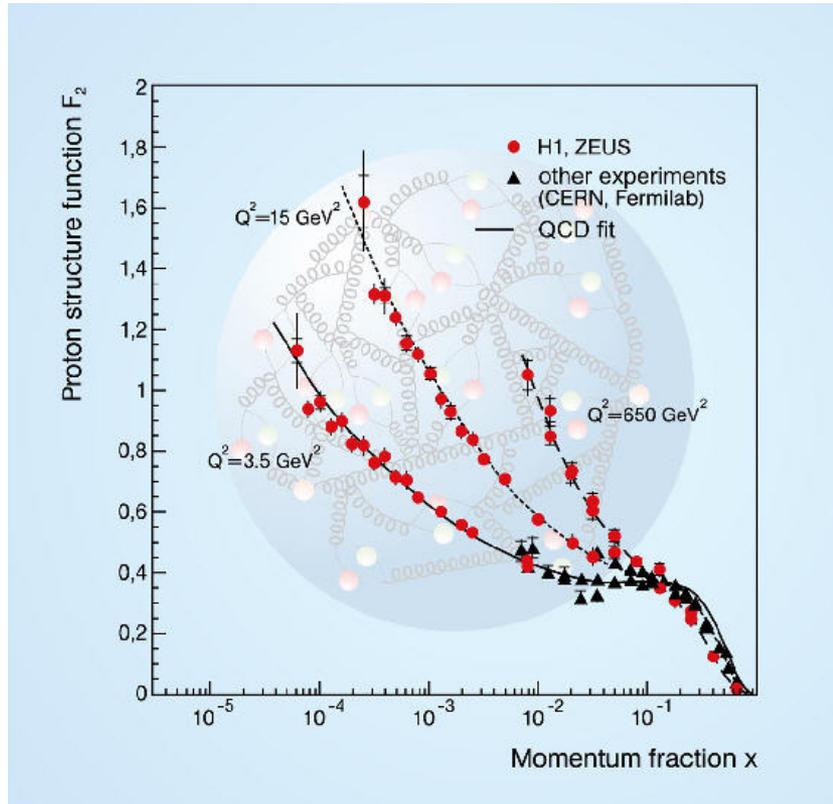
BEYOND PARTON DISTRIBUTIONS

Where we are...

- We were interested in how protons and neutrons (nucleons) and hadrons “work”.
 - How do they acquire their characteristics.
 - Intrinsic characteristics such as mass, spin arise.
 - Interactions with other hadrons.
 - Bind into nuclei. How does that lead to the characteristics of the nuclei.
- We’ve found out that nucleons (all hadrons) are made of quarks and gluons.
- We’ve extracted proton pdf’s (longitudinal distributions)
- We’ve verified the perturbative QCD describe the evolution of pdf’s.
- It seems like we should be able to answer some of the initial questions in terms of quarks, gluons and pQCD... But..
- In the last two lectures, we talked about answers. Now we talk about questions..
 - Part I: Is all really well? Are we sure the this pQCD+pdf edifice is correct?
 - Part II: How do we move ahead beyond pdf’s and start to answer some of those questions.

PART I: DIFFRACTION, BFKL, SATURATION

Triumph of perturbative QCD

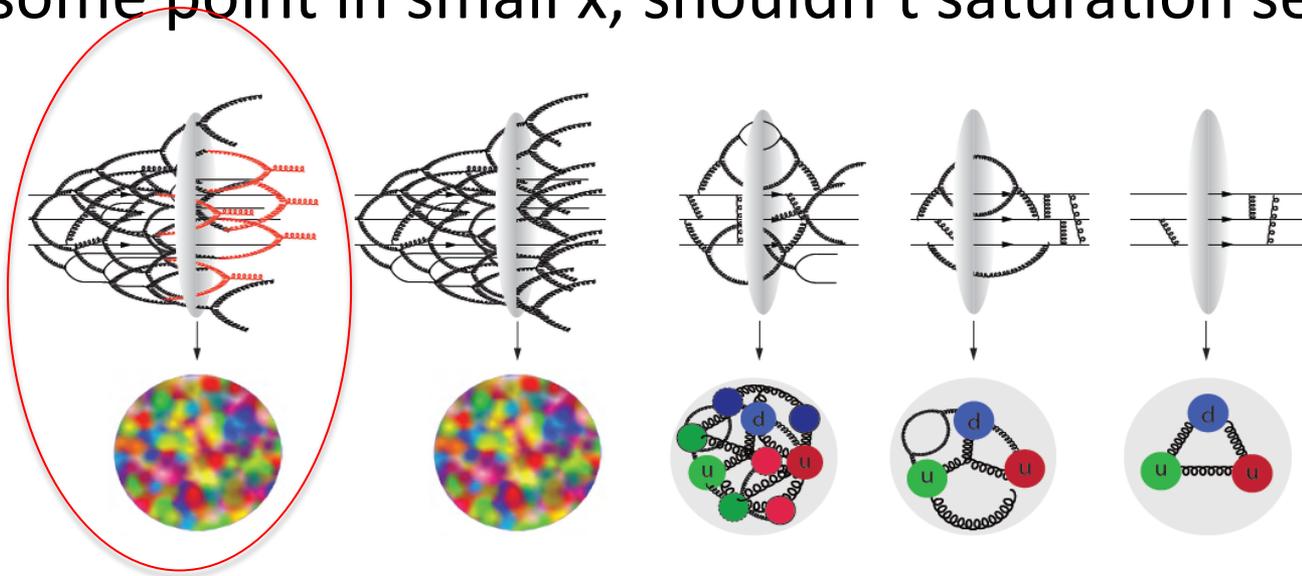


A part of Wilczek's comments upon the Nobel Prize announcement

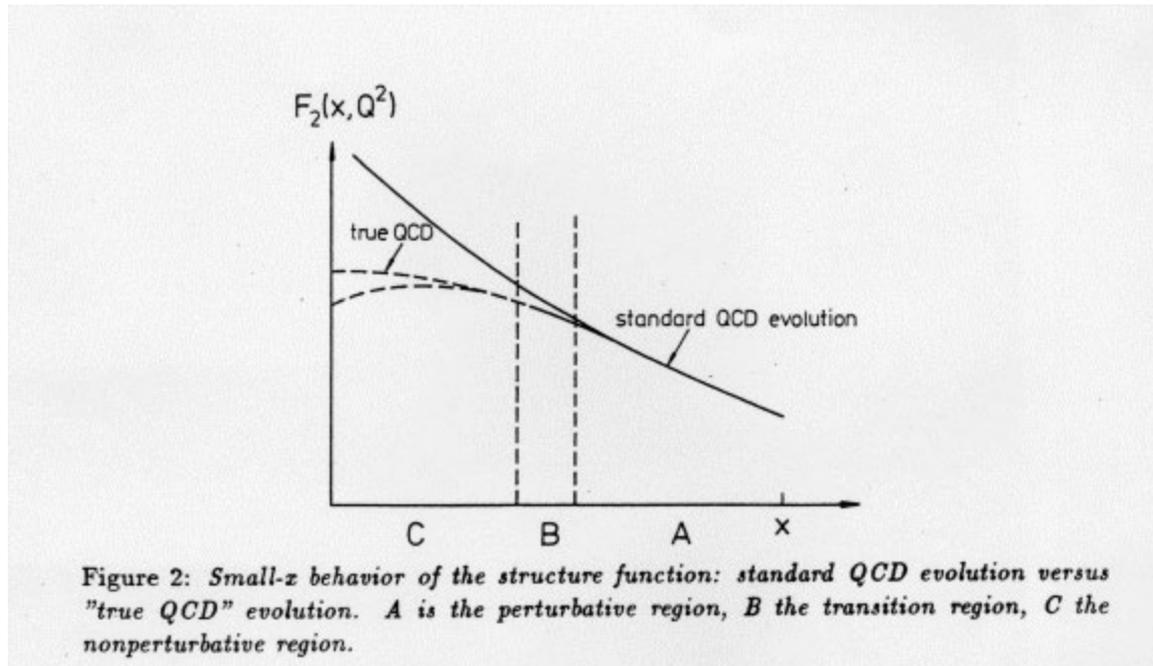
proposed specific experimental tests of our ideas. In the fourth paper some technical objections to the theory were cleared up, and in the fifth and sixth papers further experimental consequences, regarding the pointwise evolution of structure functions, were derived. The most dramatic of these, that protons viewed at ever higher resolution would appear more and more as field energy (soft glue), was only deeply verified at HERA twenty years later.

Beyond DGLAP: BFKL and Saturation

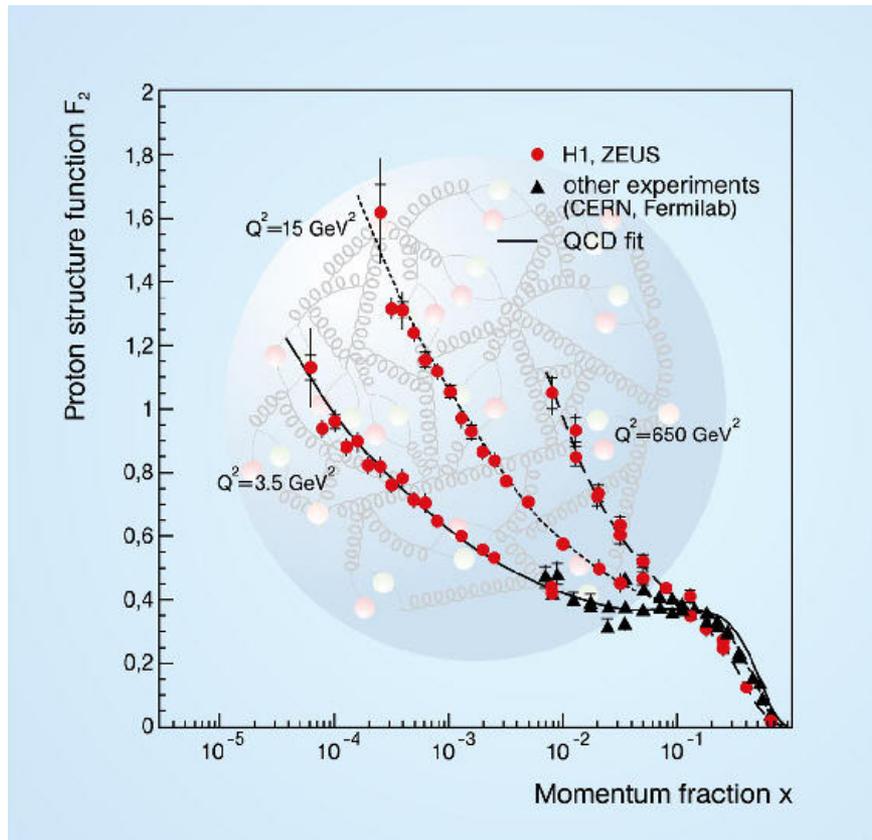
- DGLAP is an expansion in $\alpha_s(\ln Q^2)$. Terms proportional to $\alpha_s \ln(1/x)$ are neglected.
- If $x < 0.001$ then should DGLAP still work?
- $\ln(1/x)$ evolution is called BFKL.
- At some point in small x , shouldn't saturation set in?



From 1991 HERA Workshop proceedings

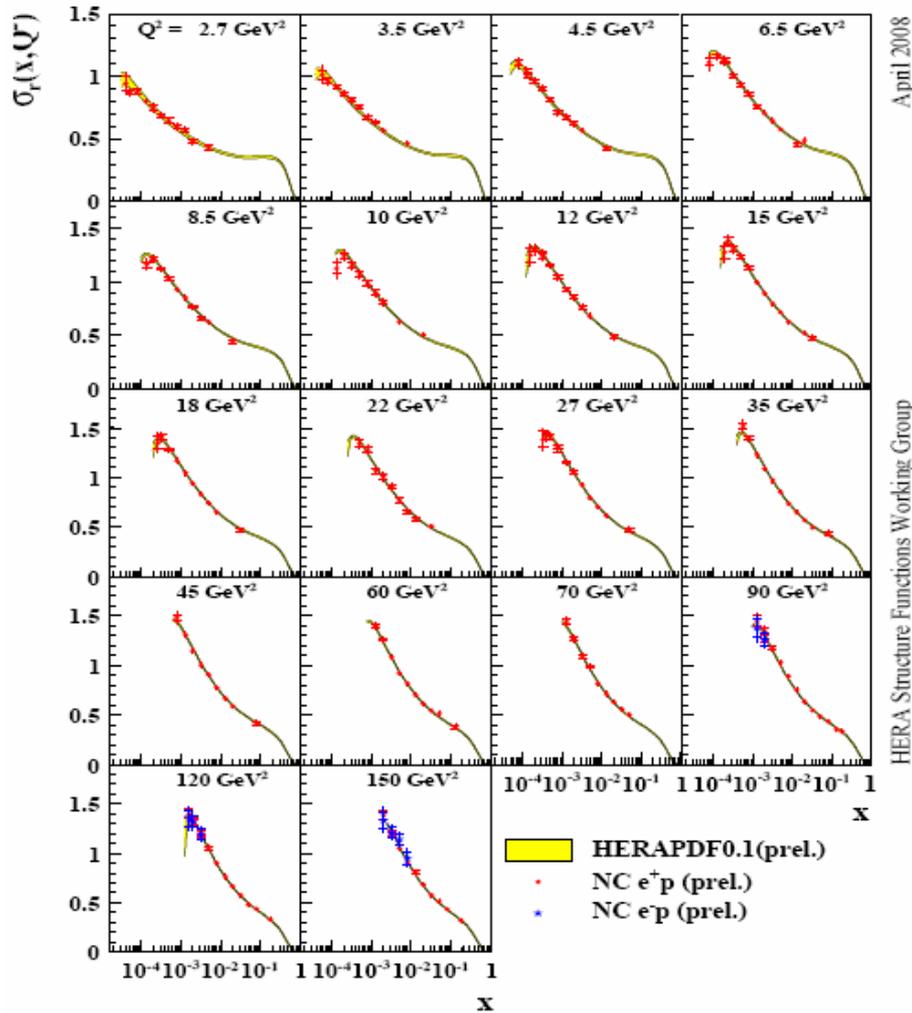


- A: Standard pQCD
- B: Modified by GLR (saturation)
- C: non-perturbative region.



- In early 1990's when we started to measure the F_2 structure function at HERA, most of the experimentalists thought of gluon saturation as visibly changing the behaviour of F_2 at low- x (for a fixed Q^2).
- DGLAP fits achieved excellent fits to the data, and precision PDFs began to be extracted.
- There seemed to be no “need” for low- x theory. We did not find a smoking gun for BFKL, much less saturation.
- This remains the view of many HERA experimentalists today.

H1 and ZEUS Combined PDF Fit

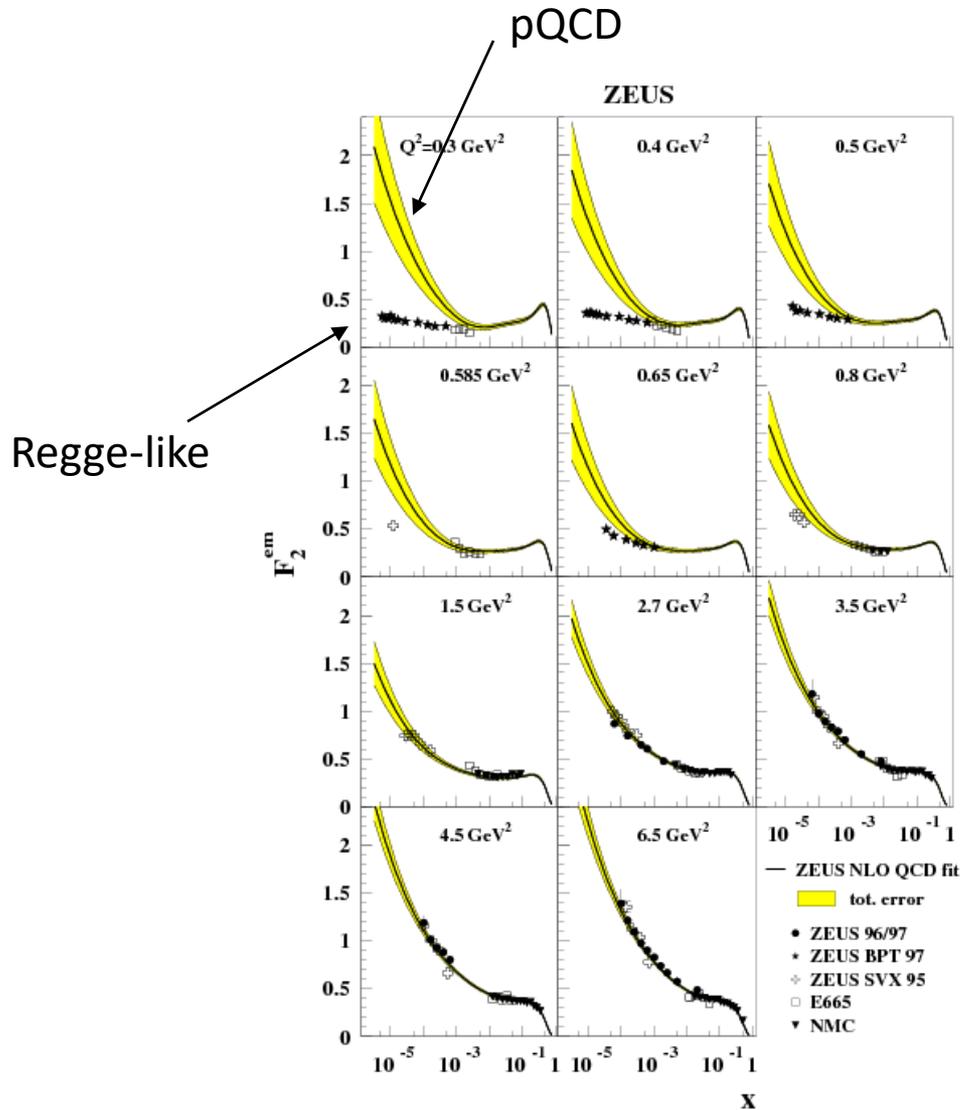


April 2008

HERA Structure Functions Working Group

Recent HERAPDF0.1 fit

Remarkably good fit to very precise data using DGLAP alone.



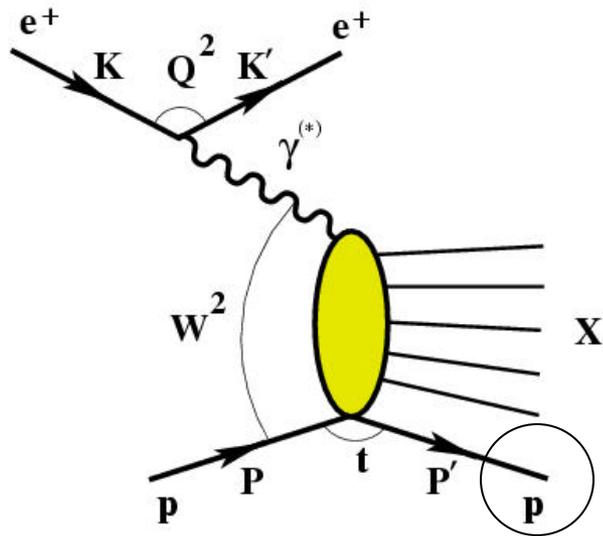
The only visible failure of DGLAP happens at low- Q^2 below 1 GeV^2 .

This seems reasonable as a limit of perturbation theory.

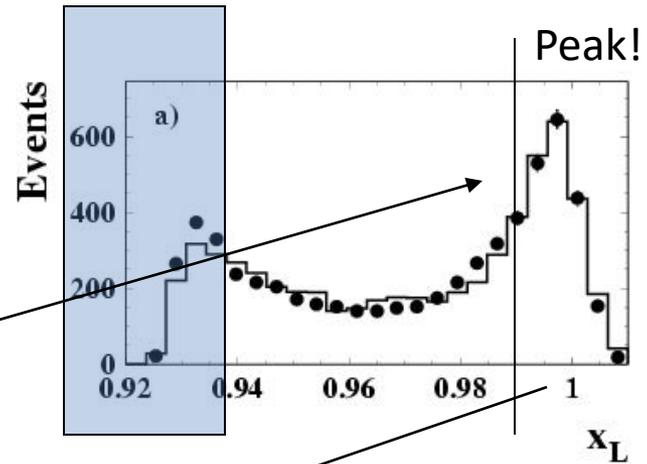
(Note, however but the failures begin at low- x)

Diffraction

Has the hadronic proton completely vanished (only manifestation in the parton densities) ?



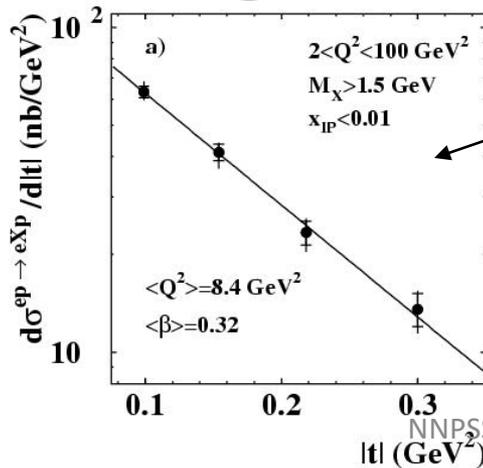
Look for leading protons in the final state



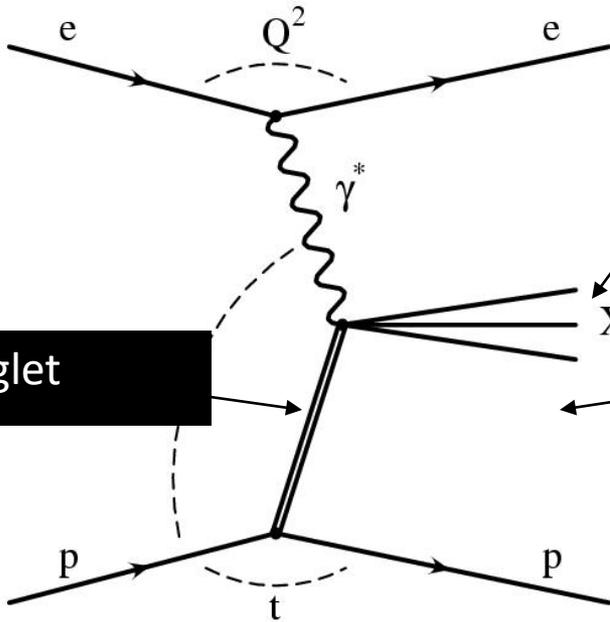
carries most of the beam momentum

If proton carries most of the beam momentum and t is small \rightarrow

t is small



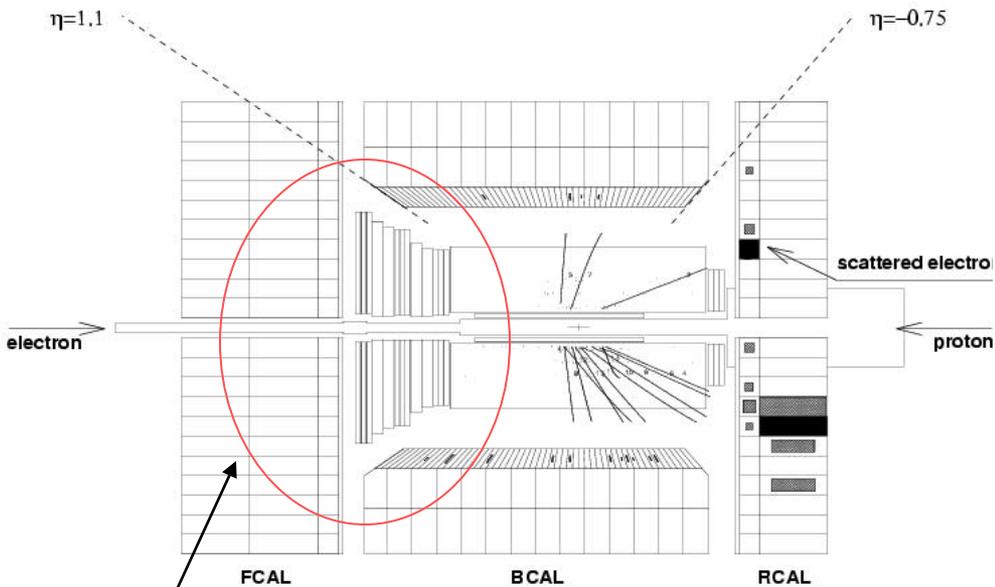
...then



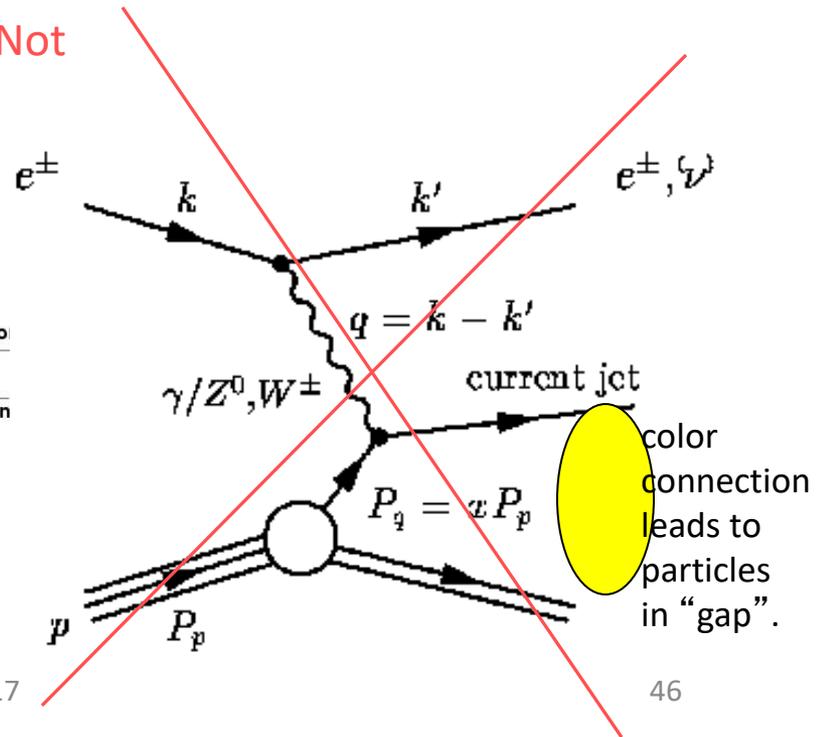
Mass of X, M_X , must be small with respect to W

X is far away in rapidity from the proton \rightarrow a rapidity gap

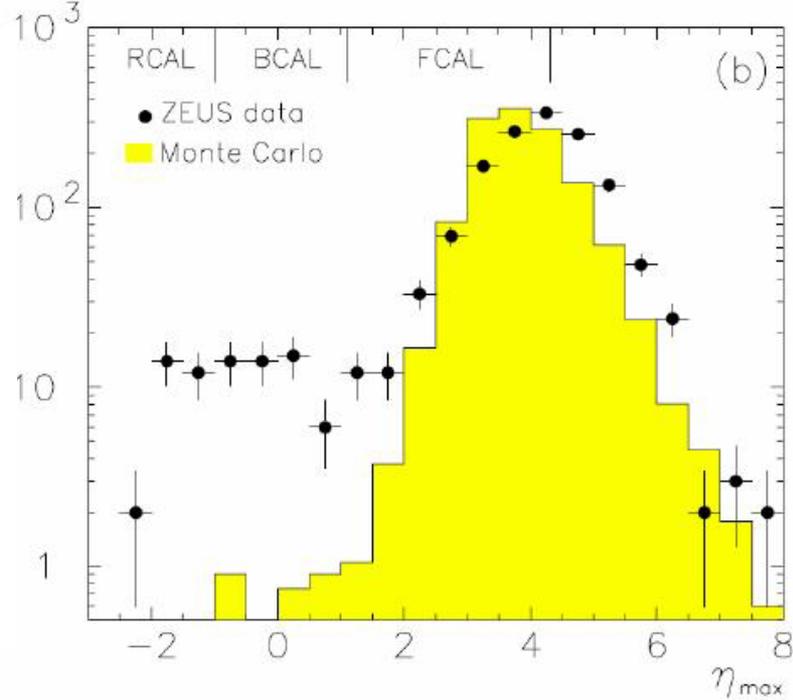
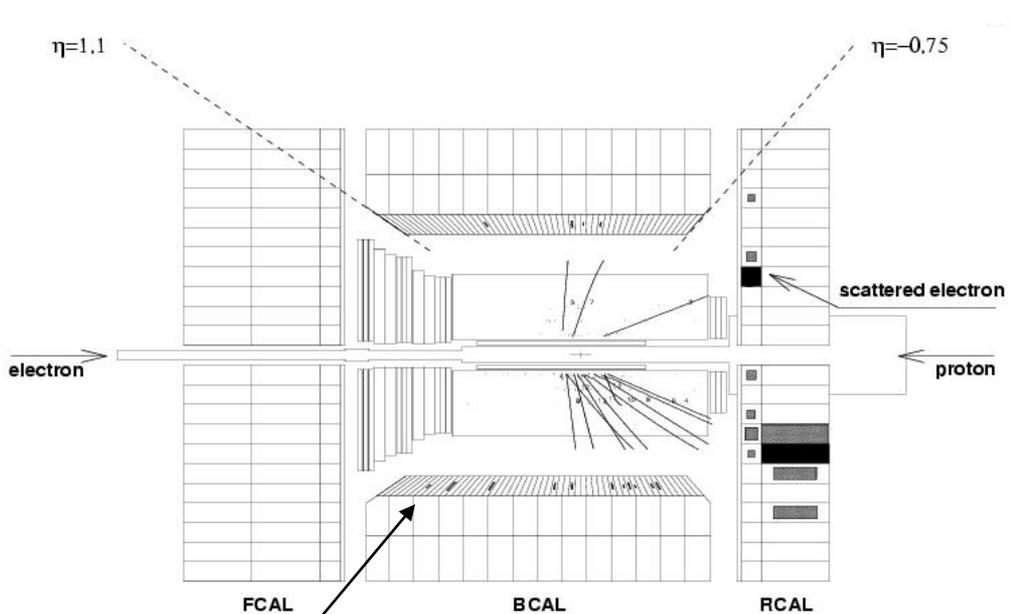
color singlet



Not



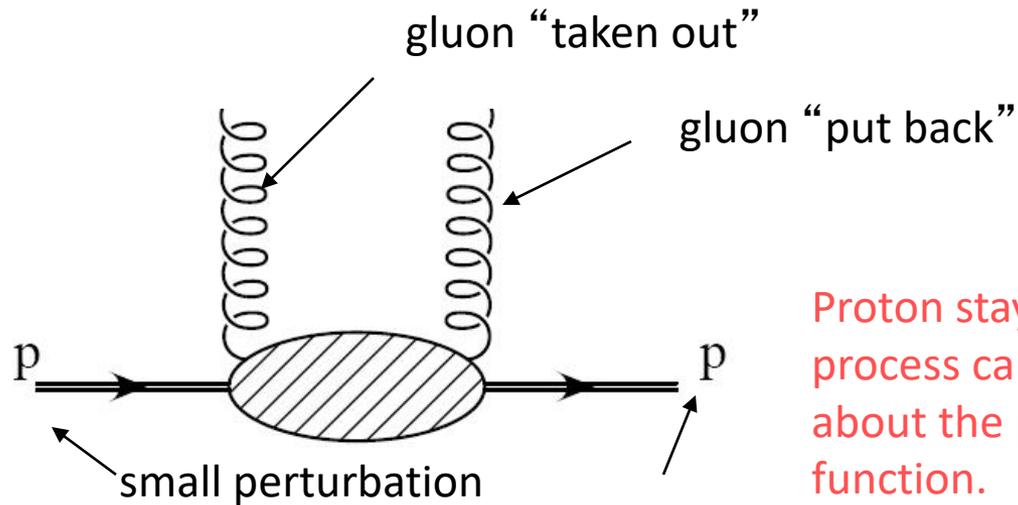
No particles in the proton direction



η_{max} , the most forward energy deposit

~10% of DIS events are “rapidity gap” events

In the simplest interpretation 2 gluons in a color singlet state are exchanged:



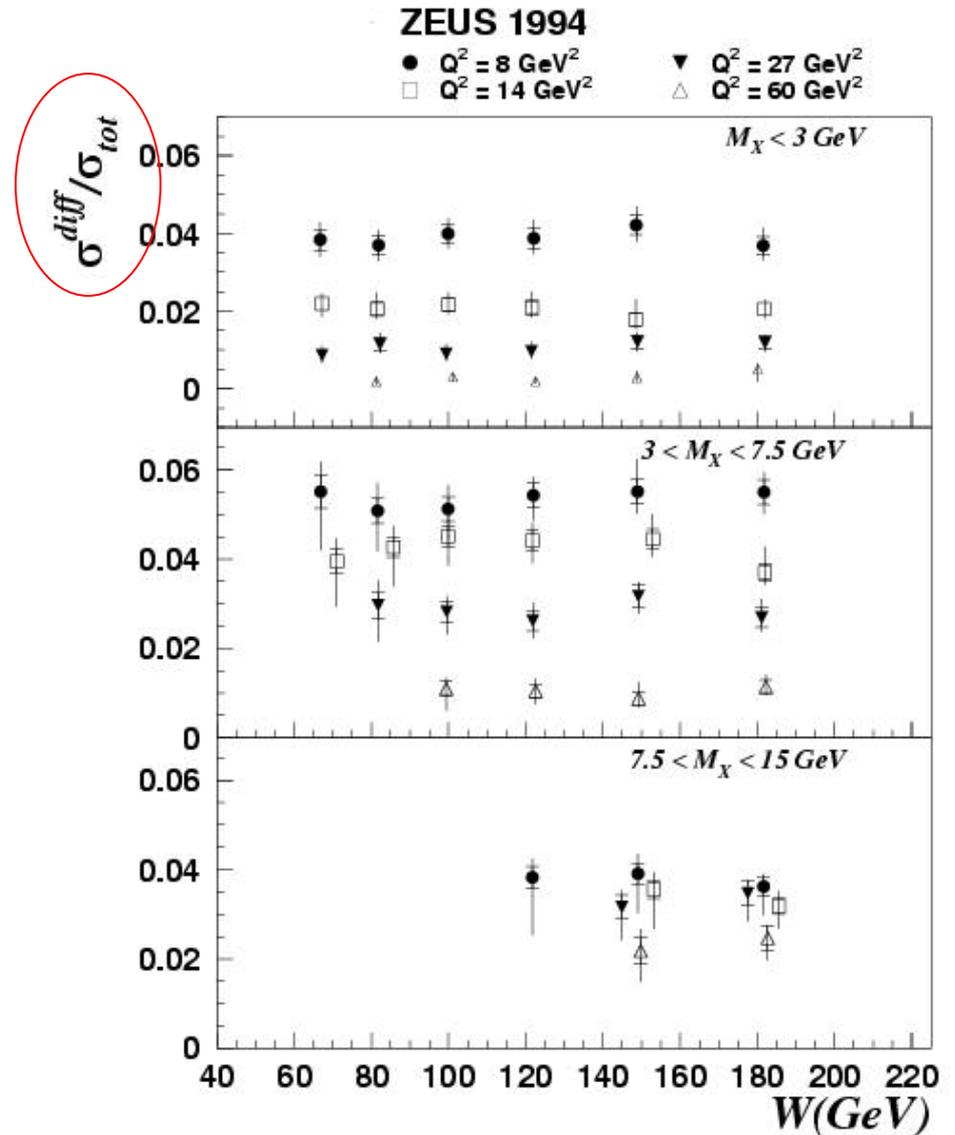
Proton stays intact: this process carries information about the proton wave function.

Here, proton is behaving as a hadron!

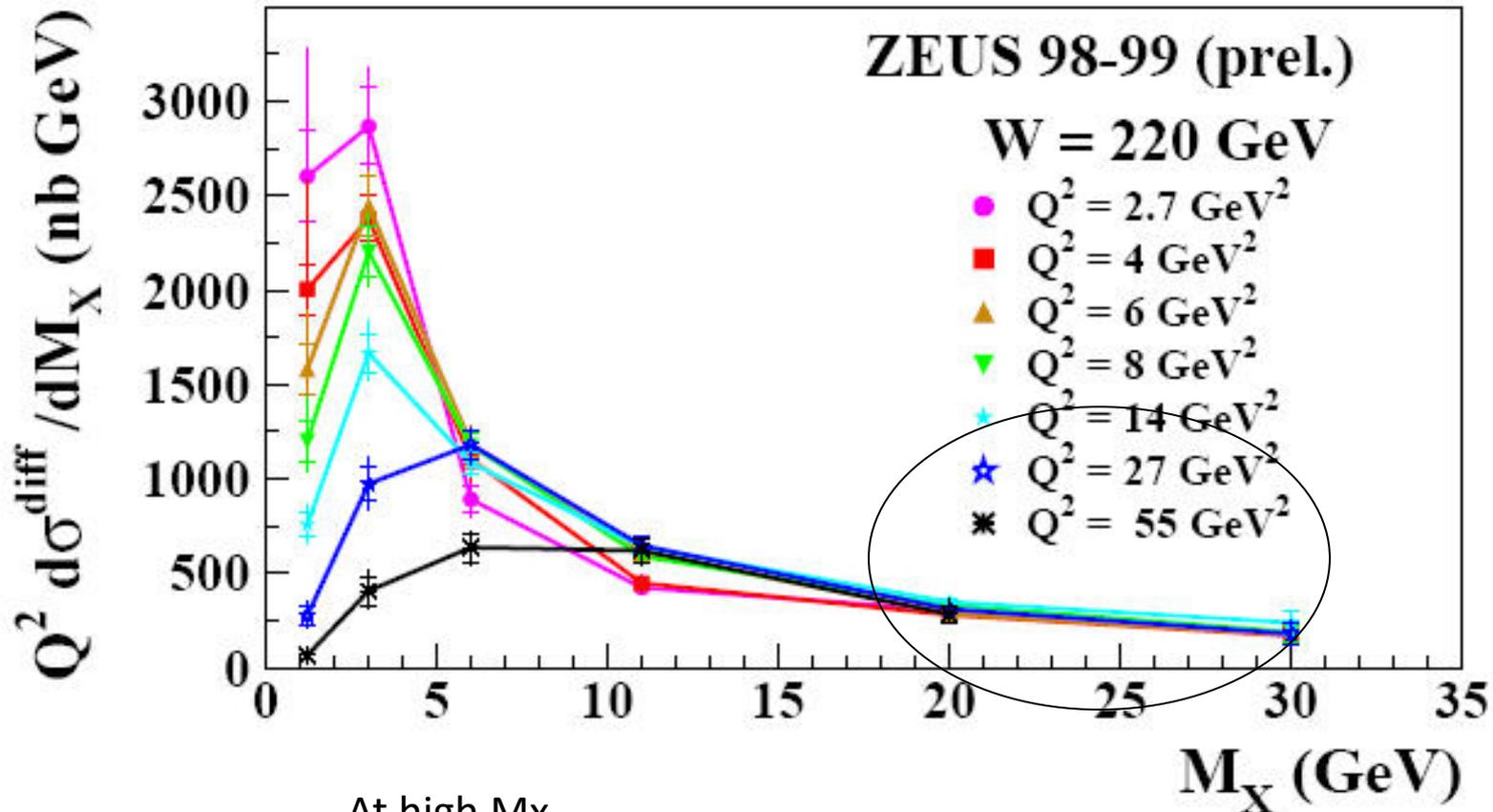
This is “diffraction” familiar from hadronic physics: however, with some peculiarities

- Sizable part of F_2 even at high Q^2 ($\sim 10\%$ at 30 GeV^2). \rightarrow High Q^2 means interpretable in terms of pQCD(?)

- Ratio to total cross section is flat with W (or x). How is this possible? If
 - $\sigma_{\text{tot}} \sim$ gluon density
 - $\sigma_{\text{diff}} \sim (\text{gluon density})^2$
 (Naively...)



ZEUS



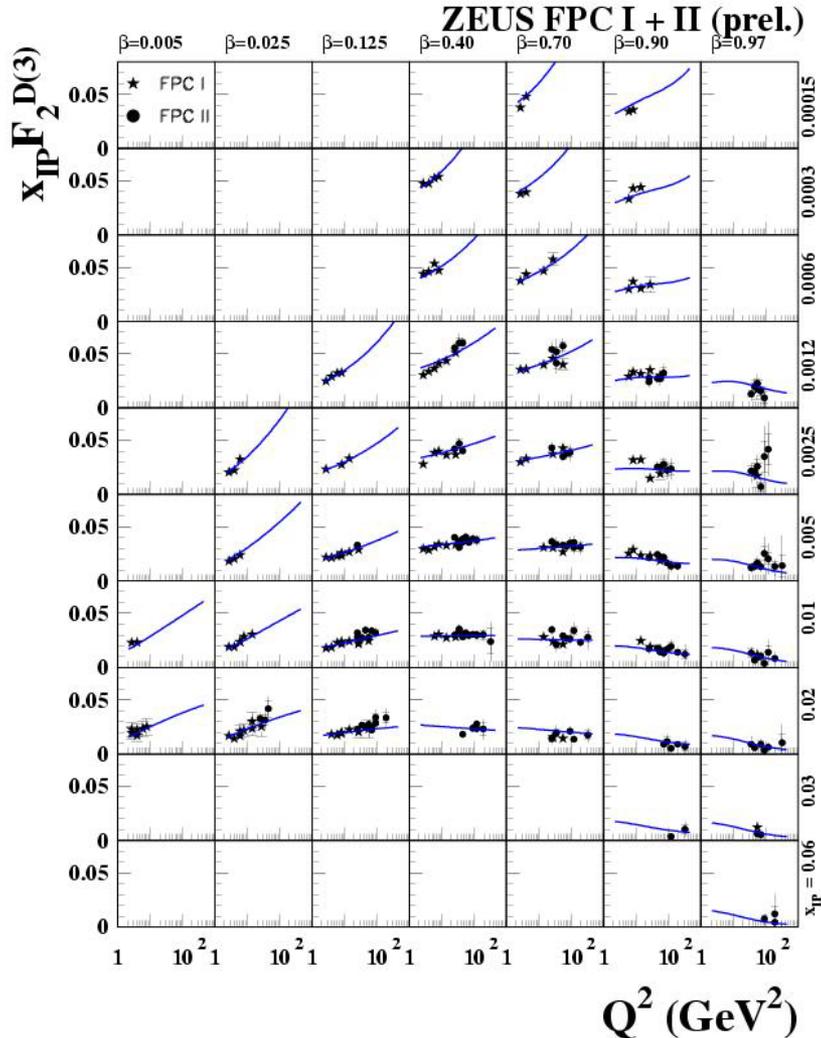
At high M_X ,
diffractive DIS is
not vanishing
at high Q^2 . — “leading
twist” in pQCD
language.

Proton as a hadron

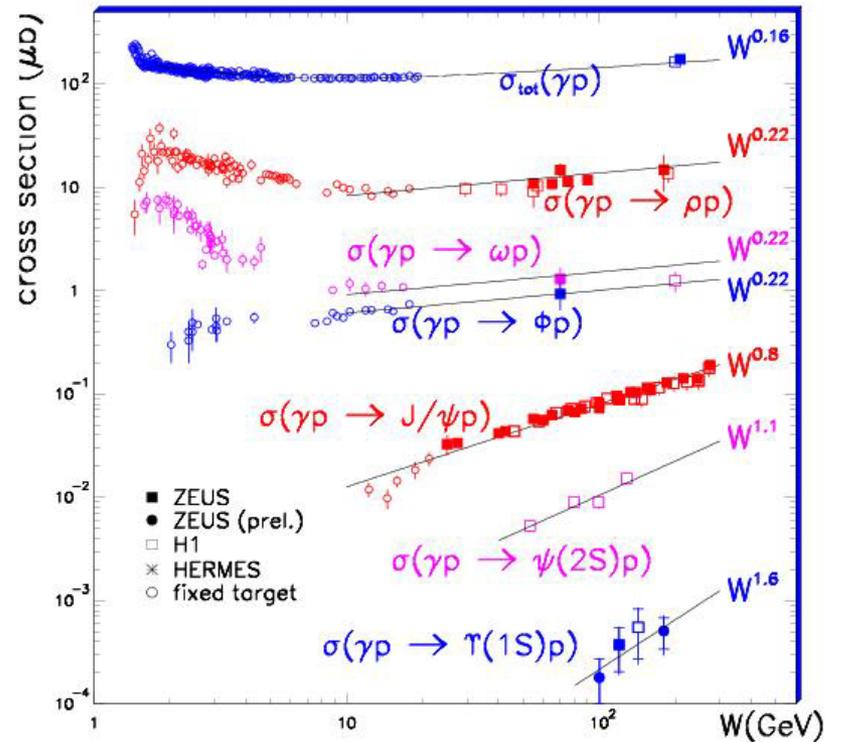
- In DIS diffraction we have:
 - A phenomenon that is clearly related to the hadronic nature of the proton—i.e. that of confined color.
 - that exists at 10% level at high Q^2 —where perturbative QCD should be usable.
 - that does not conform to the expectation from the hadronic phenomenology.
 - that does not conform to the naïve expectation of 2 gluon exchange.
- Plenty of mysteries:
 - We observe protons as hadrons clearly in the kinematic region where asymptotic freedom+partons appears to give a good description of data.
 - Do we, then, truly understand the evolution of partons in the proton—especially at low x ?
 - Is diffractive DIS the opportunity to finally begin to unravel confinement from a perturbative point of view?

July 2017 A lot of high precision data from HERA exists → NNPSS Lectures 2017

Diffractive DIS cross-section



Elastic VM production



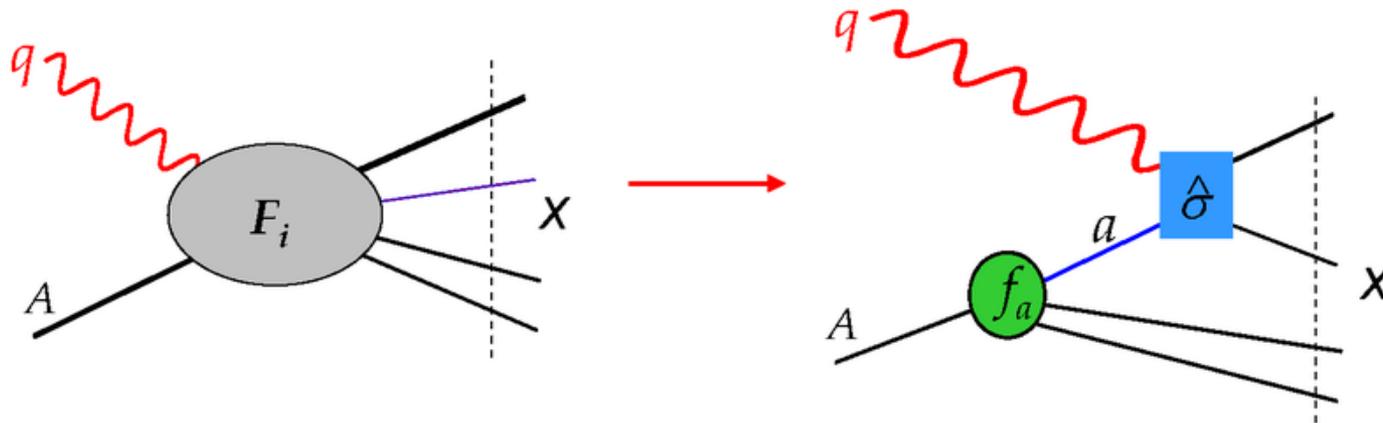
So far, no true understanding of this phenomenon

PART II: TOWARDS 3D STRUCTURES OF THE NUCLEI AND NUCLEON

What are we missing?

- We discovered that (nearly) massless quarks and gluons make up the nucleon and that QCD governs their interactions.
- We had hoped to find out how quarks and gluons and their interactions give rise to the characteristics of the nucleons.
 - Spin
 - Mass
 - Bulk
- We also hoped that we would be able to find out how NN interactions work in terms of QCD.
 - How nuclear forces arise.
 - How nuclear characteristics come about
- We were able to do this kind of things with EM and atoms.
- So far we have failed..

What longitudinal factorization did

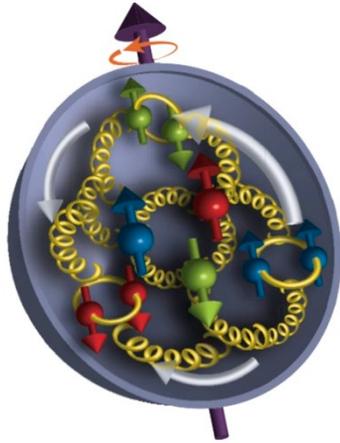


$$\lim_{Q^2 \rightarrow \text{large}, x \text{ fixed}} F_i(x, Q^2) = f_a \otimes \sigma$$

Function only of x (i.e. longitudinal momentum)

Our quarks and gluons as constituents of the proton only exist longitudinally.

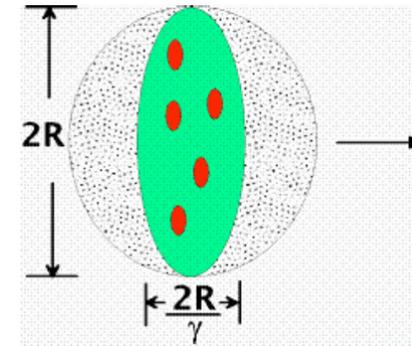
Limits of Longitudinal Information



infinite
momentum
frame



What we know



What is the quark and gluon structure of the proton?

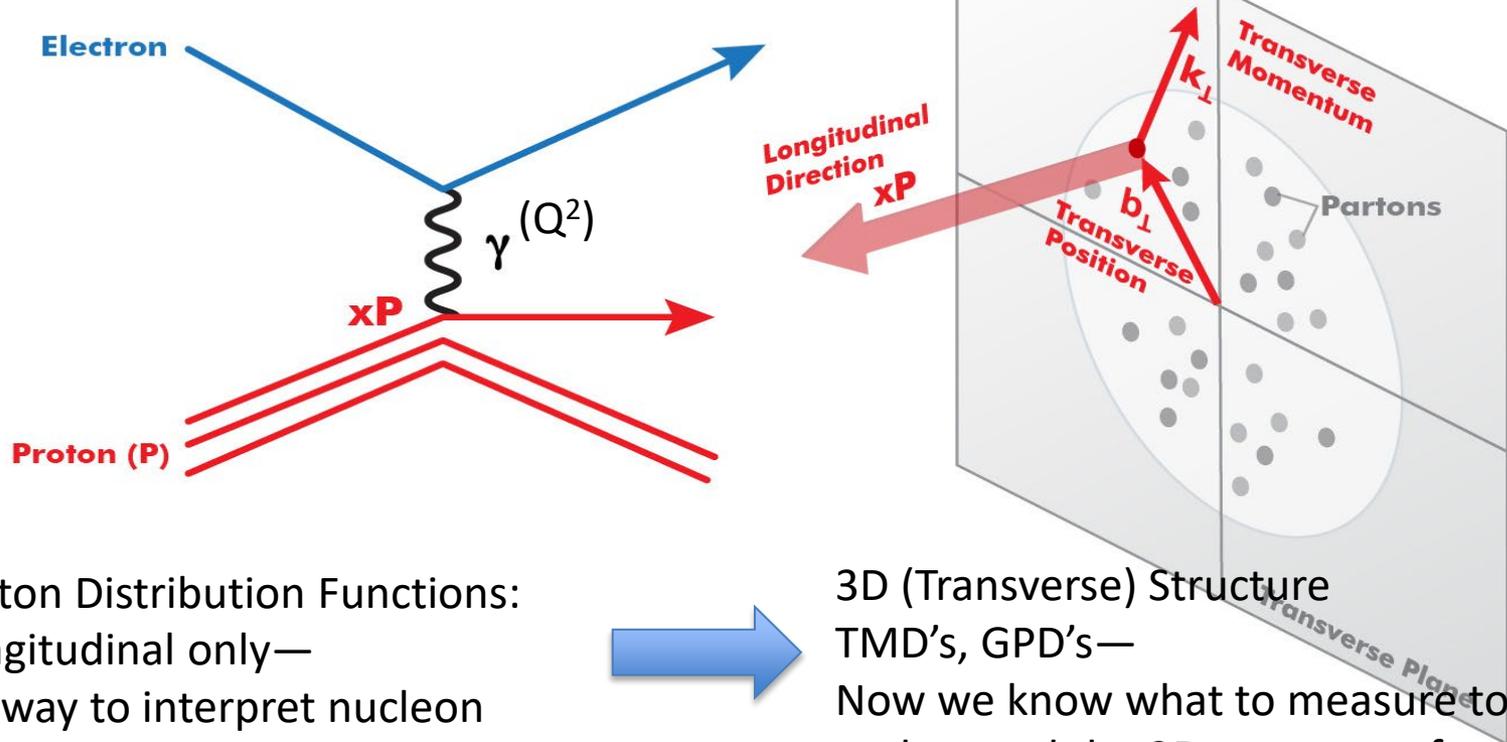
- orbital motion?
- color charge distribution?
- how does the mass come about?
- origin of nucleon-nucleon interaction?

Parton frozen transversely. Framework does not incorporate any transverse information.

But this was the only way to define quark-gluon structure of proton in pQCD.

Progress in pQCD Theory (~1980-~2010)

Factorization II



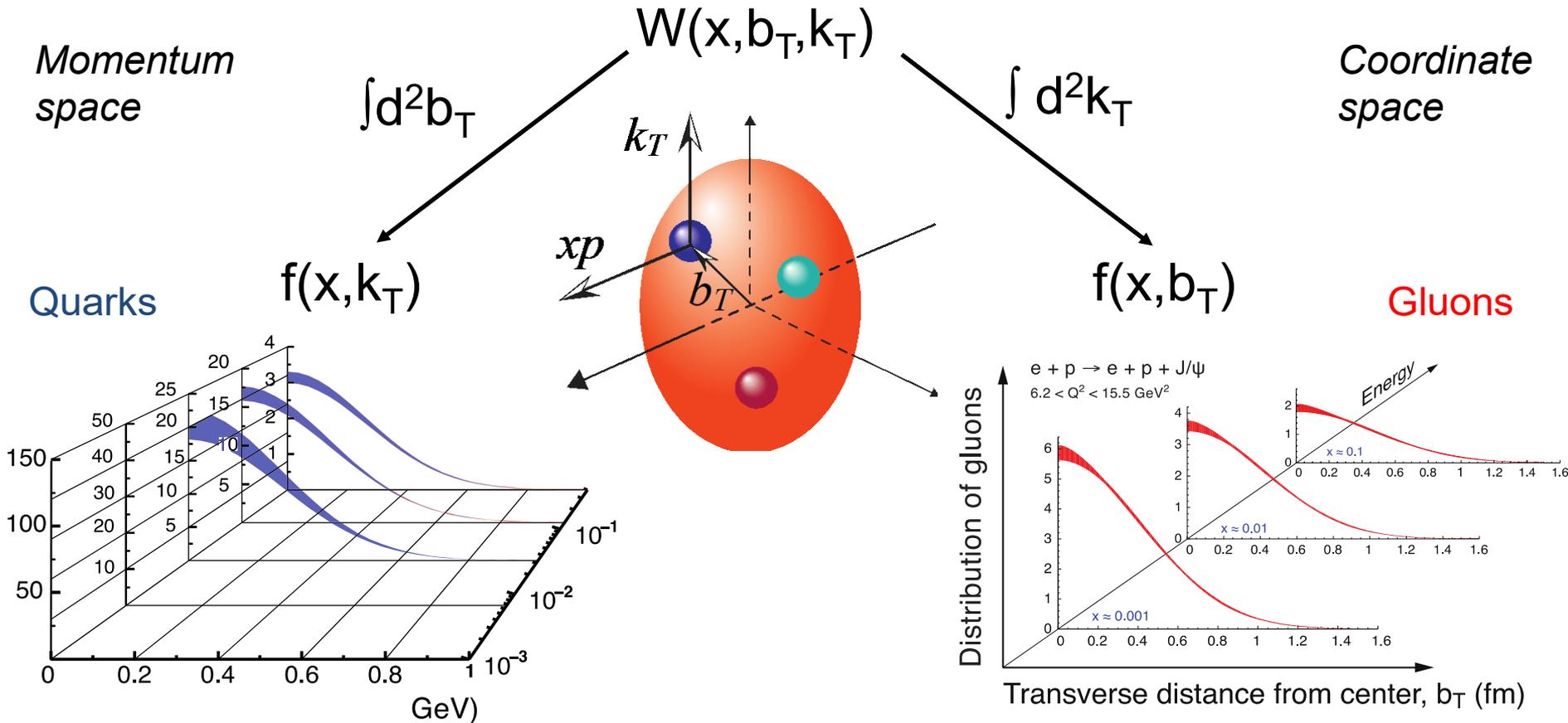
Parton Distribution Functions:
Longitudinal only—
No way to interpret nucleon
partonic structure in rest frame



3D (Transverse) Structure
TMD's, GPD's—
Now we know what to measure to
understand the 3D structure of nucleons

Transverse Momentum Dependent Distributions (TMD): k_t
Generalized Parton Distributions (GPD): b_t

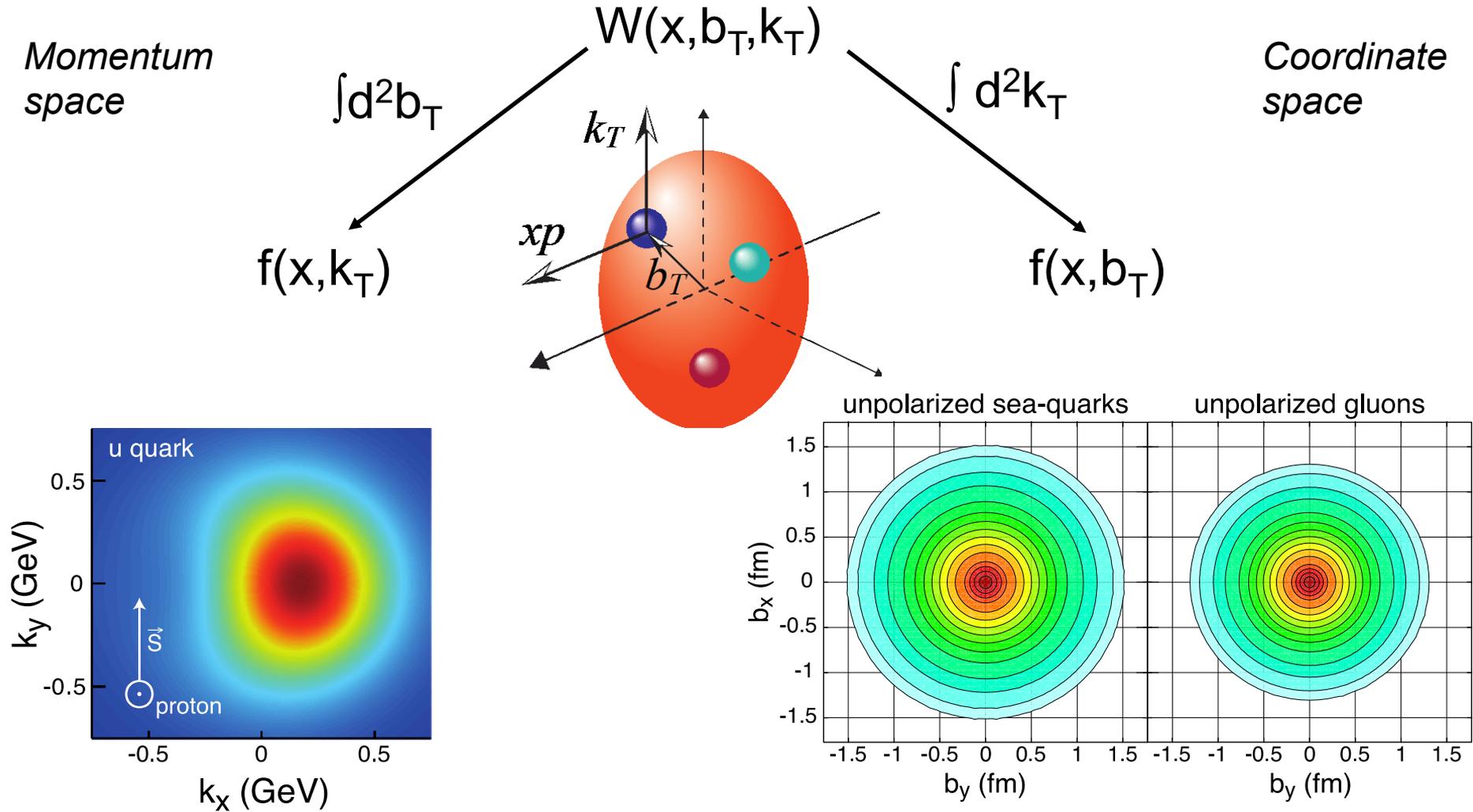
3D Imaging of Quarks and Gluons



Spin-dependent 3D momentum space images from semi-inclusive scattering

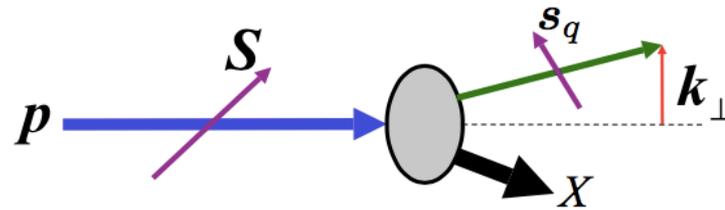
Spin-dependent 2D (transverse spatial) + 1D (longitudinal momentum) coordinate space images from exclusive scattering

3D Imaging of Quarks and Gluons

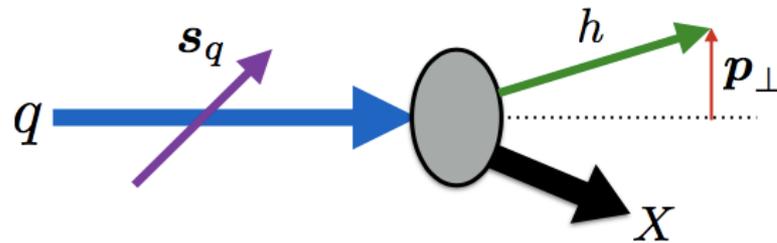


Position $r \cdot p \rightarrow$ Orbital Motion of Partons

Some TMD examples



$S \cdot (p \times k_{\perp})$ $s_q \cdot (p \times k_{\perp})$ $S \cdot s_q$
 "Sivers effect" "Boer-Mulders effect"

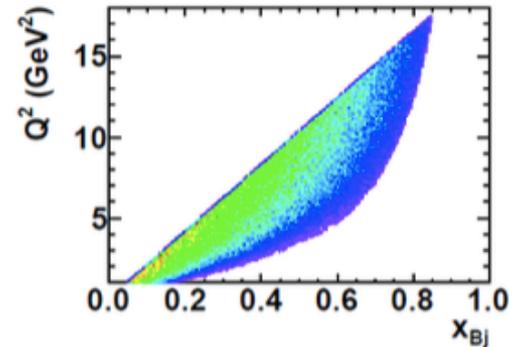
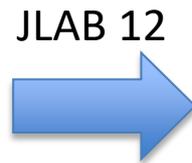
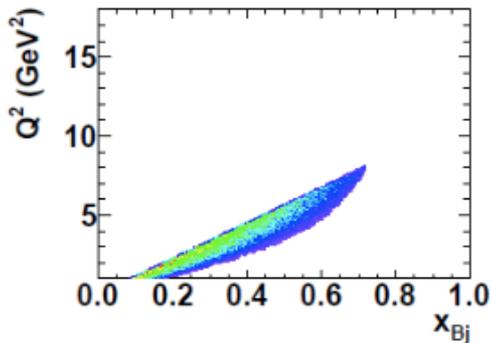
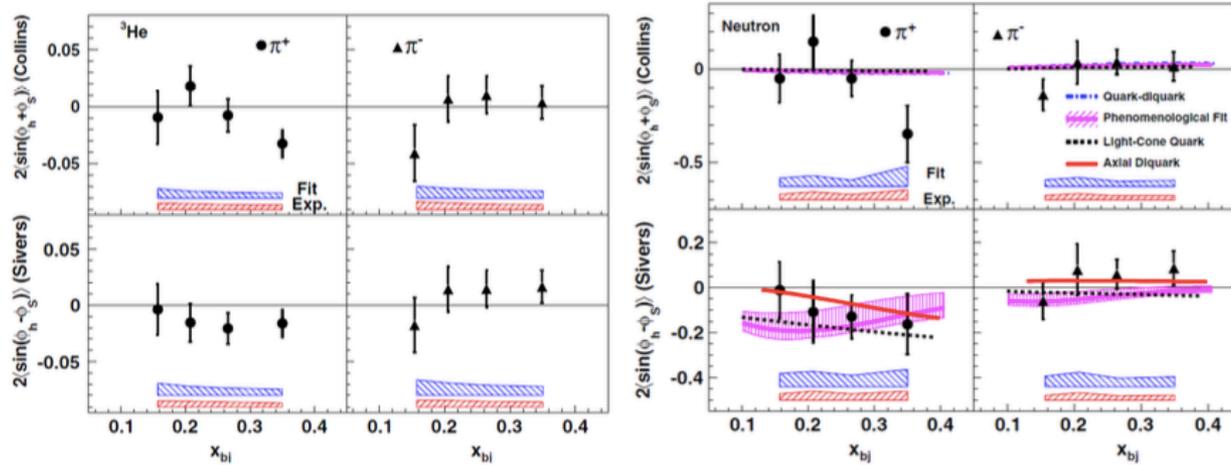


$s_q \cdot (p_q \times p_{\perp})$ "Collins effect"

Courtesy of M. Anselmino

JLab Program on TMDs and GPDs

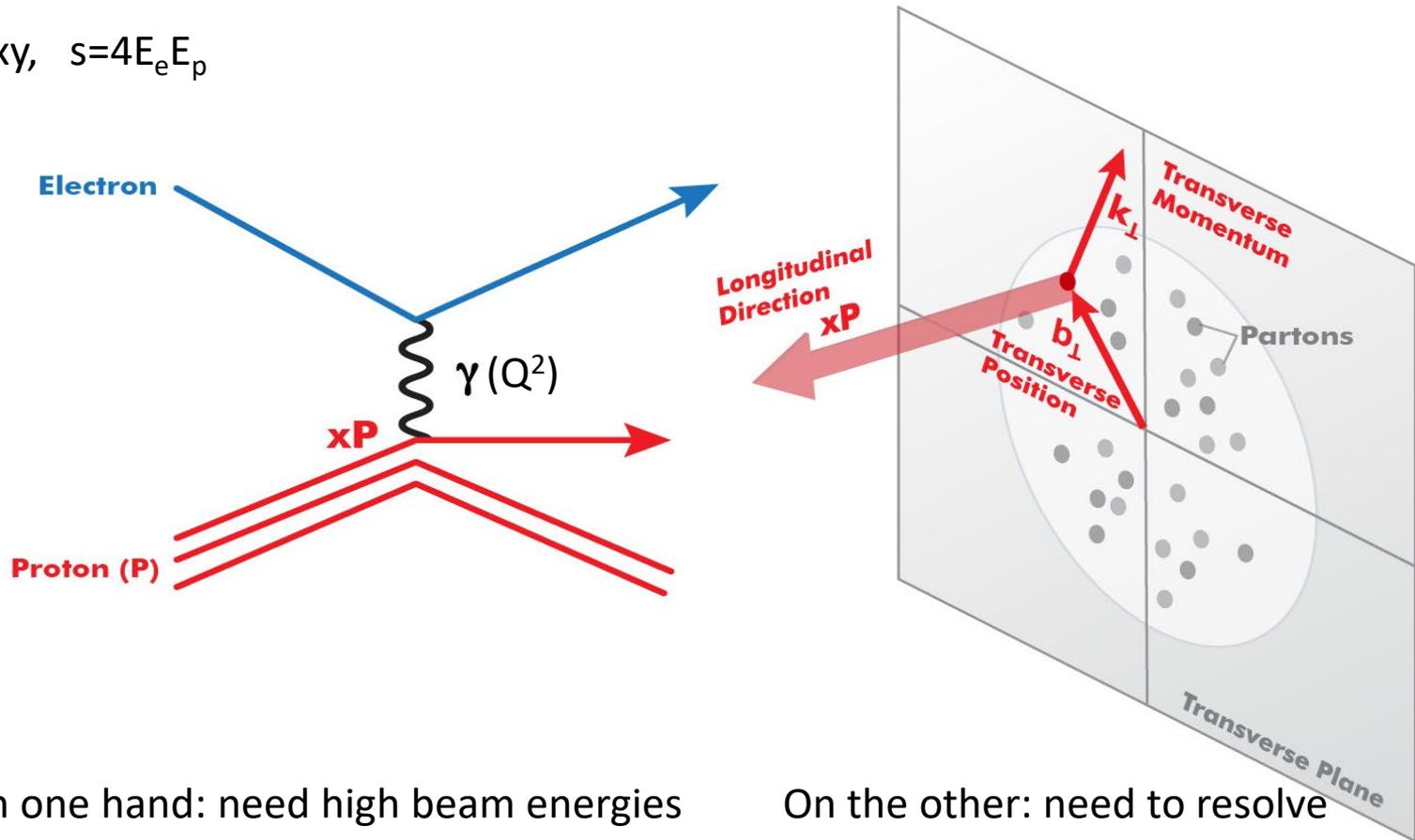
Collins and Sivers effects: *PRL 107, 072003 (2011)*



THE NEXT LEAP FORWARD: EIC

Experimental Challenge of the EIC

$$Q^2 = sxy, \quad s = 4E_e E_p$$



On one hand: need high beam energies to resolve partons in nucleons.

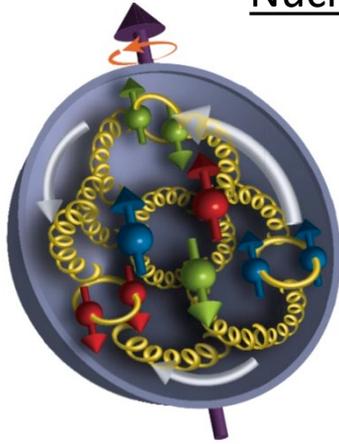
Q^2 needs to be up to $\sim 1000 \text{ GeV}^2$

On the other: need to resolve quantities (k_t , b_t) of **order a few hundred MeV** in the proton. Limits proton beam energy. High Lumi needed.

Electron-Ion Collider: Cannot be HERA or LHeC: proton energy (TeV) too high

Understanding the Nucleon at the Next Level

Nucleon: A many-body system with challenging characteristics



Relativistic ($M_{\text{proton}} \gg M_{\text{quark}}$)

Strongly Coupled (QCD)

Quantum Mechanical (Superposition of configurations)

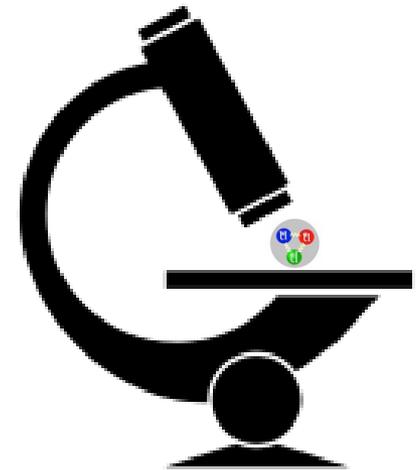
Measure in the Multi-Body regime:

- Region of quantum fluctuation + non-perturbative effects \rightarrow dynamical origin of mass, spin.

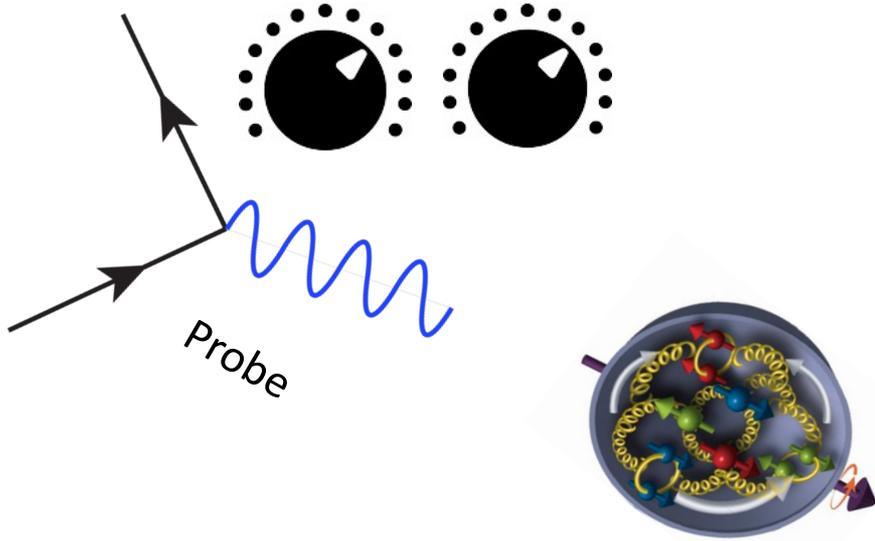
For the first time, get (almost?) all relevant information about quark-gluon structure of the nucleon

Designing EIC \rightarrow Designing the right probe

- Resolution appropriate for quarks and gluons
- Ability to project out relevant Q.M. configurations



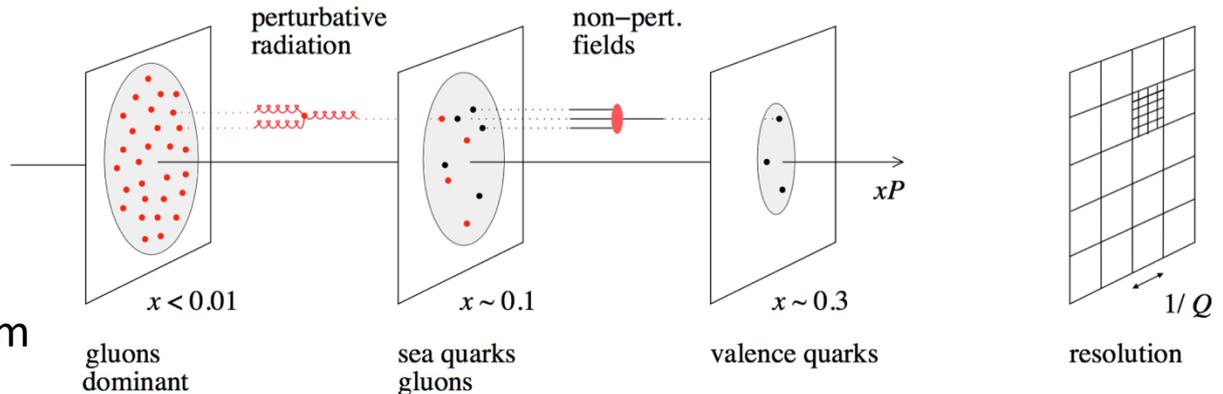
Parameters of the Probe



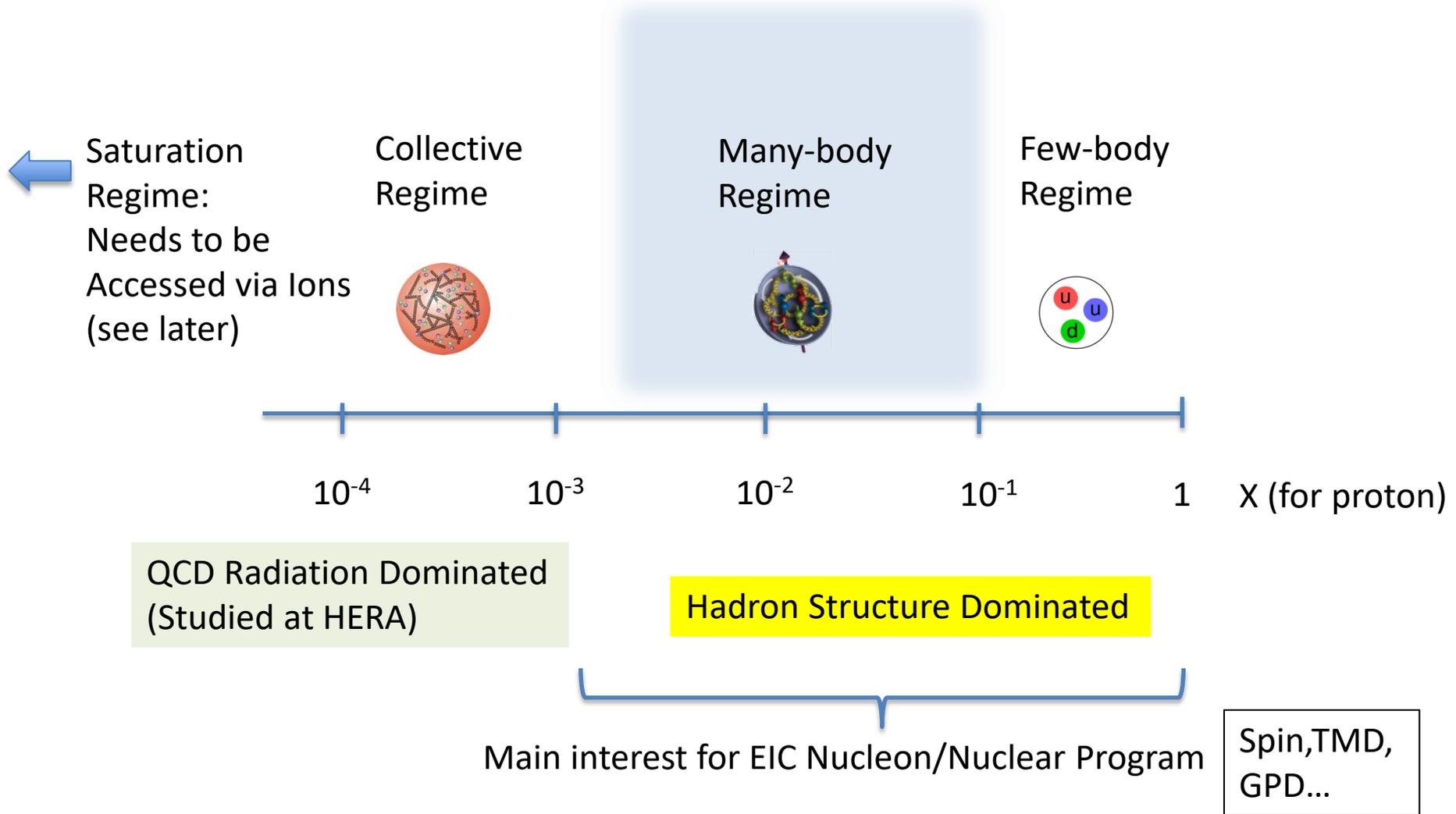
Ability to change x projects out different configurations where different dynamics dominate

Ability to change Q^2 changes the resolution scale

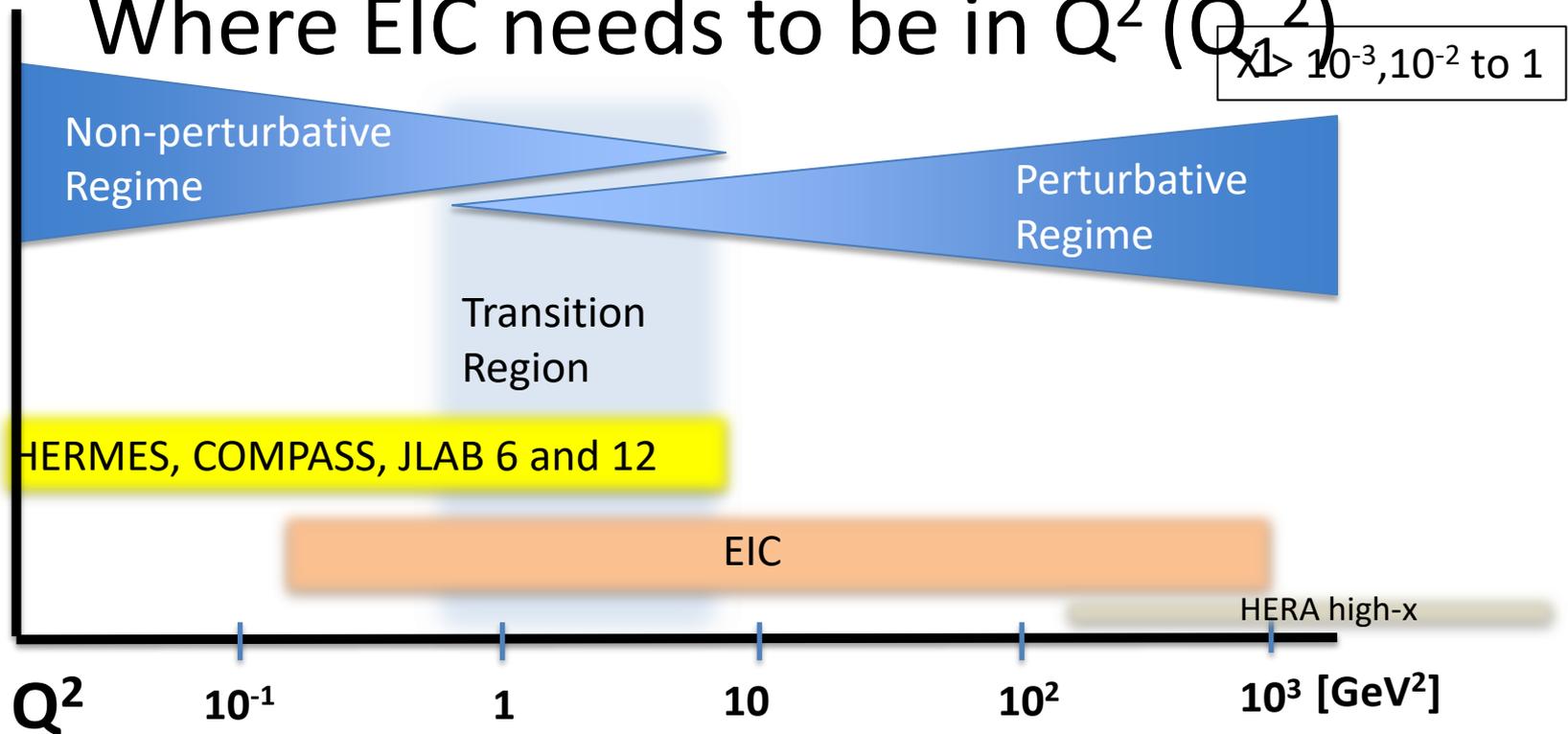
$Q^2 = 400 \text{ GeV}^2 \Rightarrow 1/Q = .01 \text{ fm}$



Where EIC Needs to be in x (nucleon)



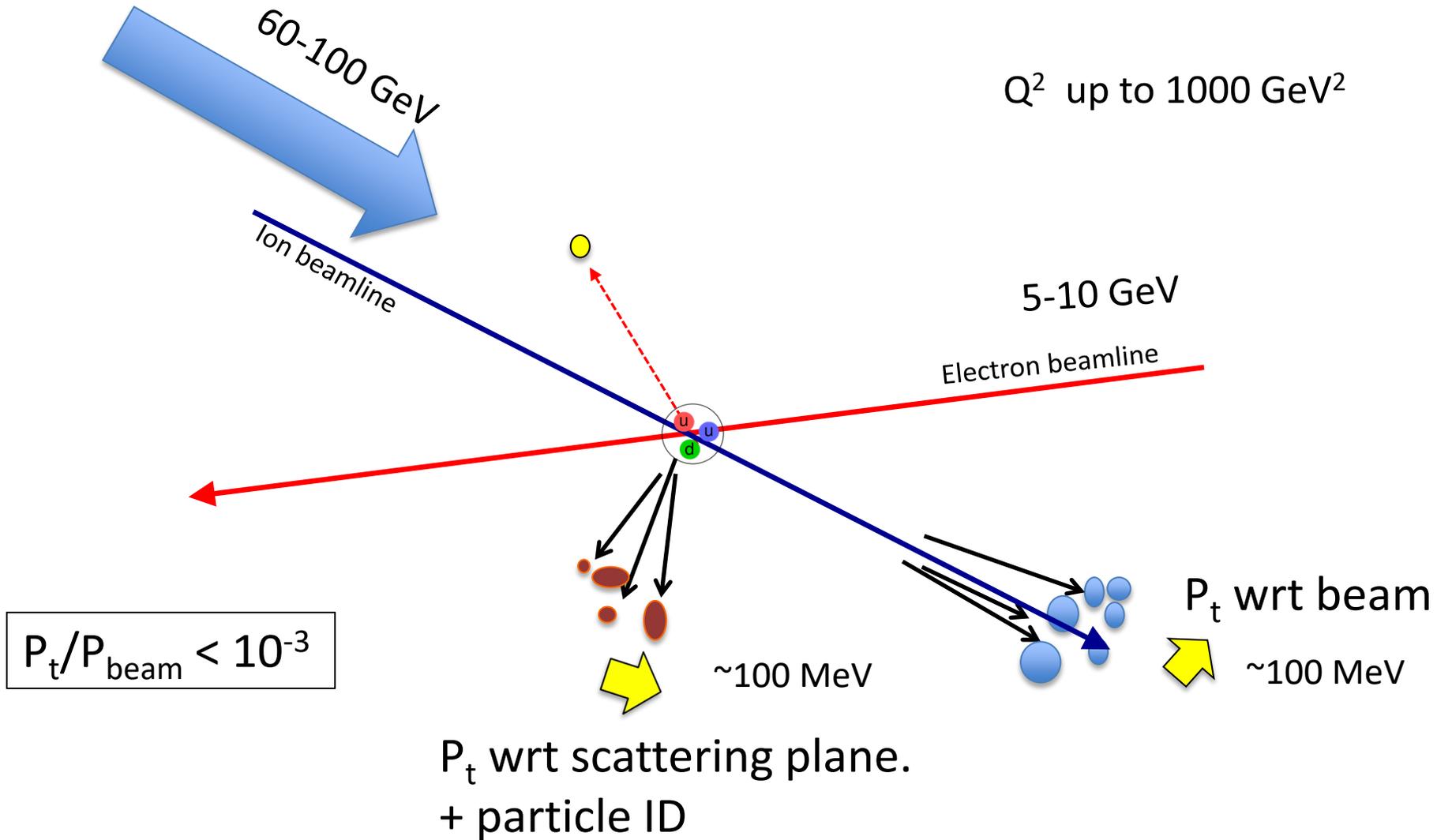
Where EIC needs to be in Q^2 (Q^2)



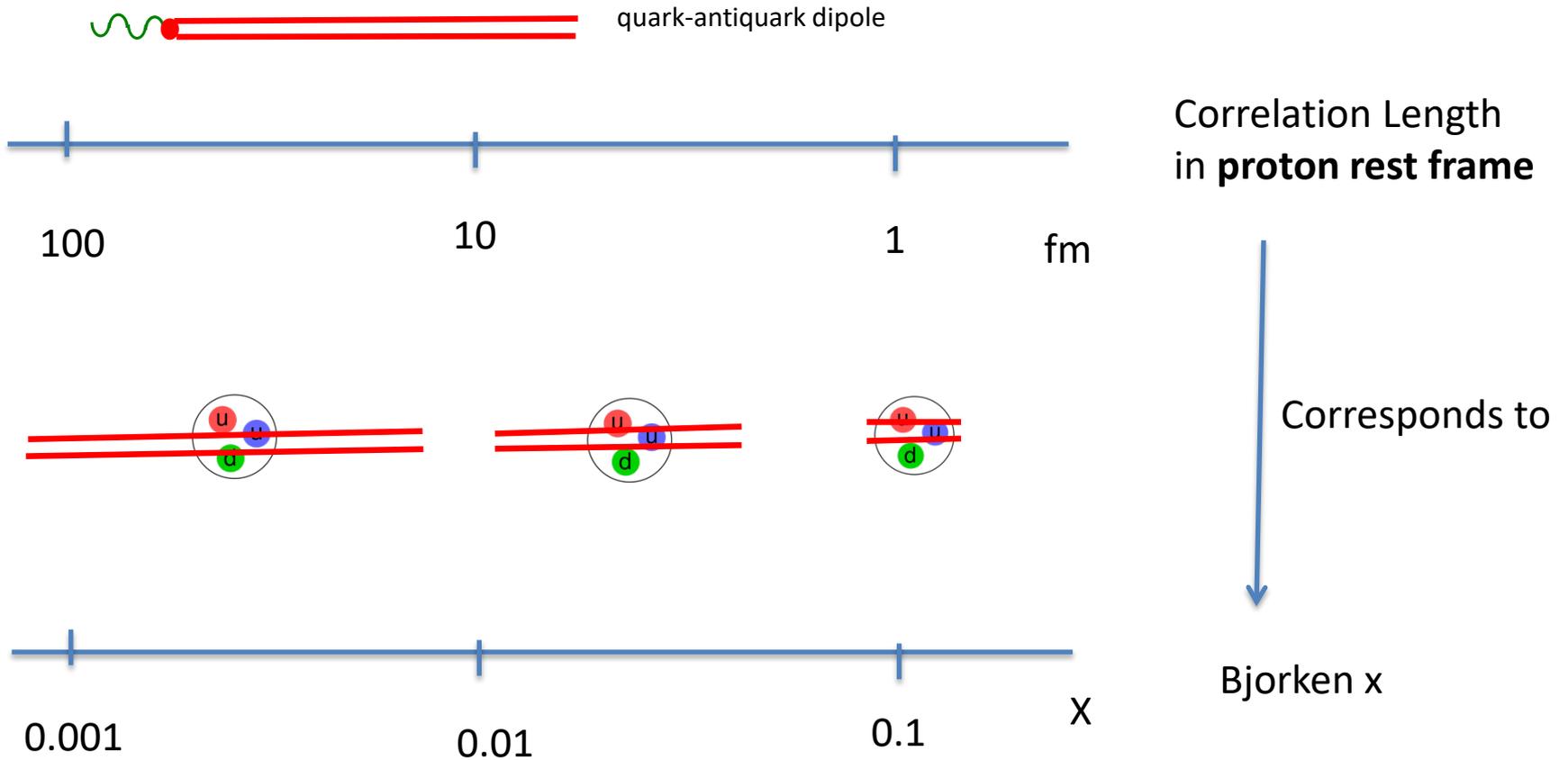
- Include non-perturbative, perturbative and transition regimes
- Provide long evolution length and up to Q^2 of ~ 1000 GeV² ($\sim .005$ fm)
- Overlap with existing measurements

Disentangle Pert./Non-pert., Leading Twist/Higher Twist

Measuring k_t and b_t

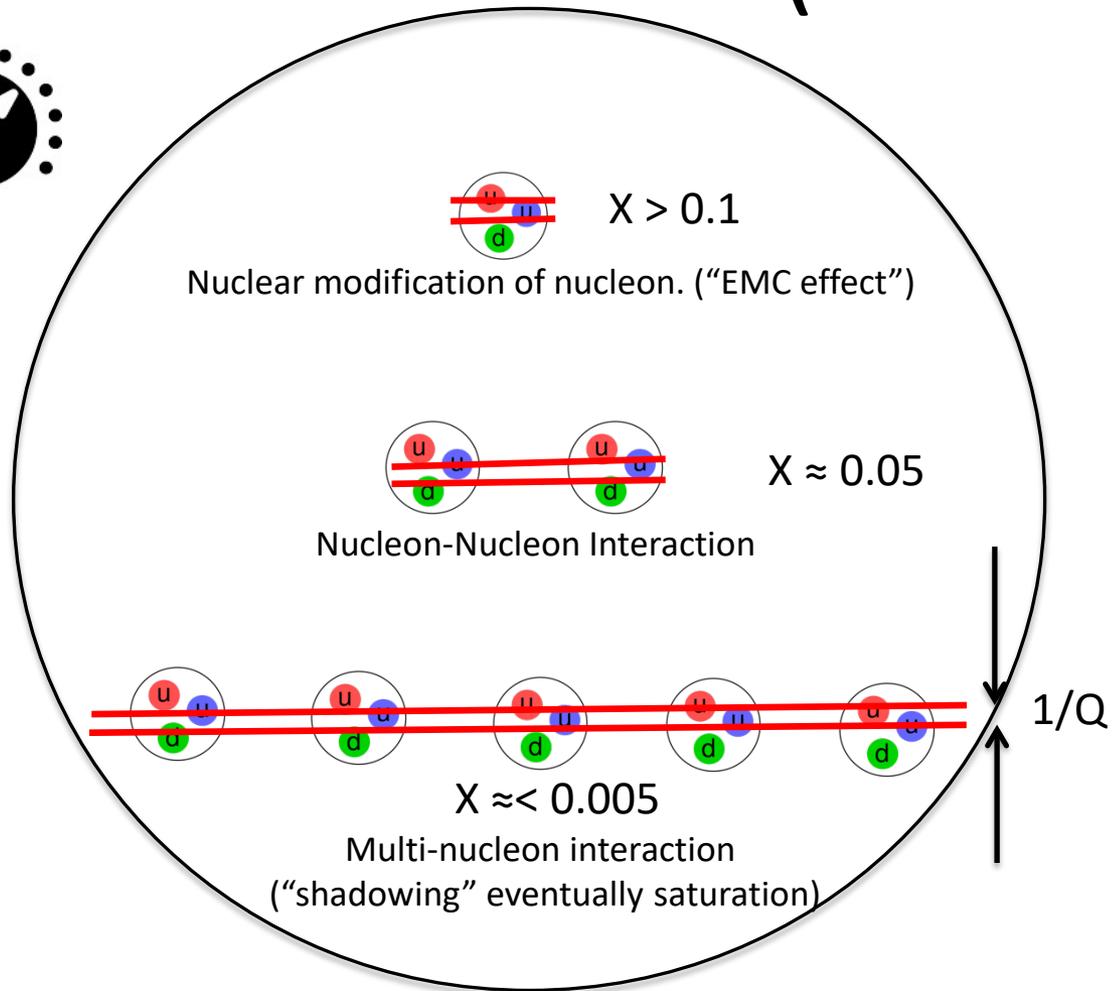
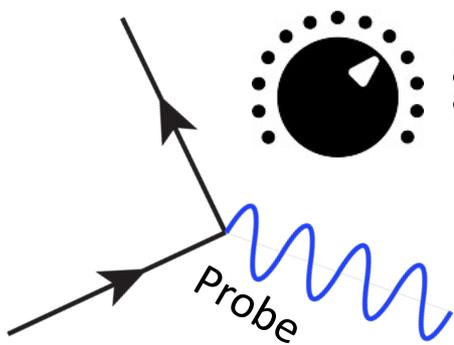


Bjorken x and length scale



In the proton rest frame, dipole lifetime ($x < 0.1$) extends far beyond the proton charge radius

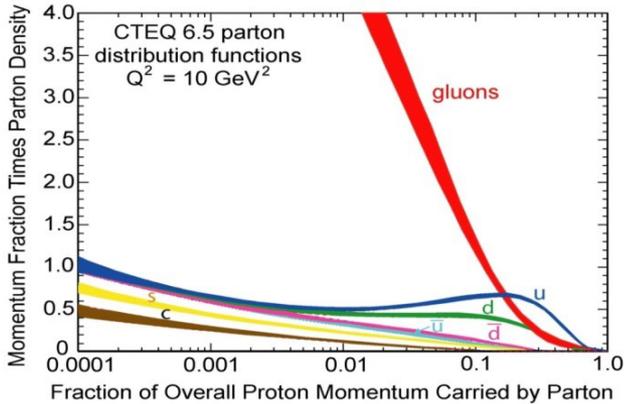
Parameters of the Probe (Nuclei)



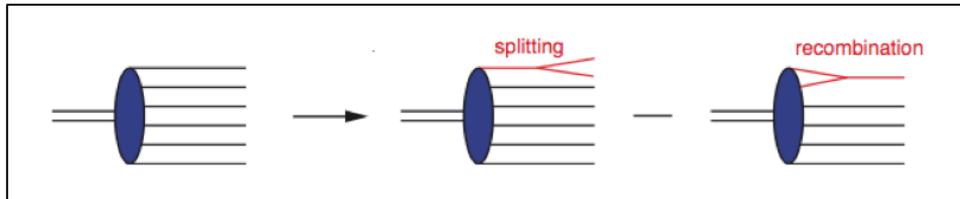
Probing the nucleon interaction in the nuclei (note this is different from correlation measurements)

Note: the x range for nuclear exploration is similar to the nucleon exploration

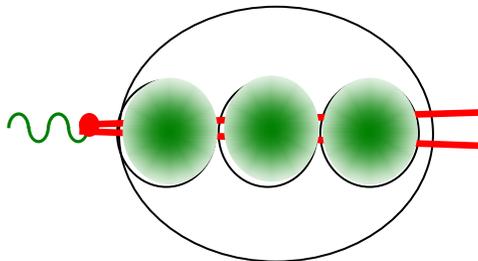
QCD at Extremes: Parton Saturation



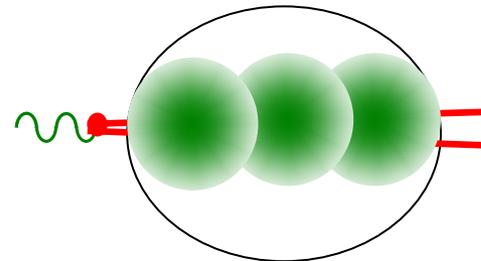
HERA discovered a dramatic rise in the number of gluons carrying a small fractional longitudinal momentum of the proton (i.e. small- x).



This cannot go on forever as x becomes smaller and smaller: parton recombination must balance parton splitting. i.e. Saturation—**unobserved at HERA for a proton. (expected at extreme low x)**

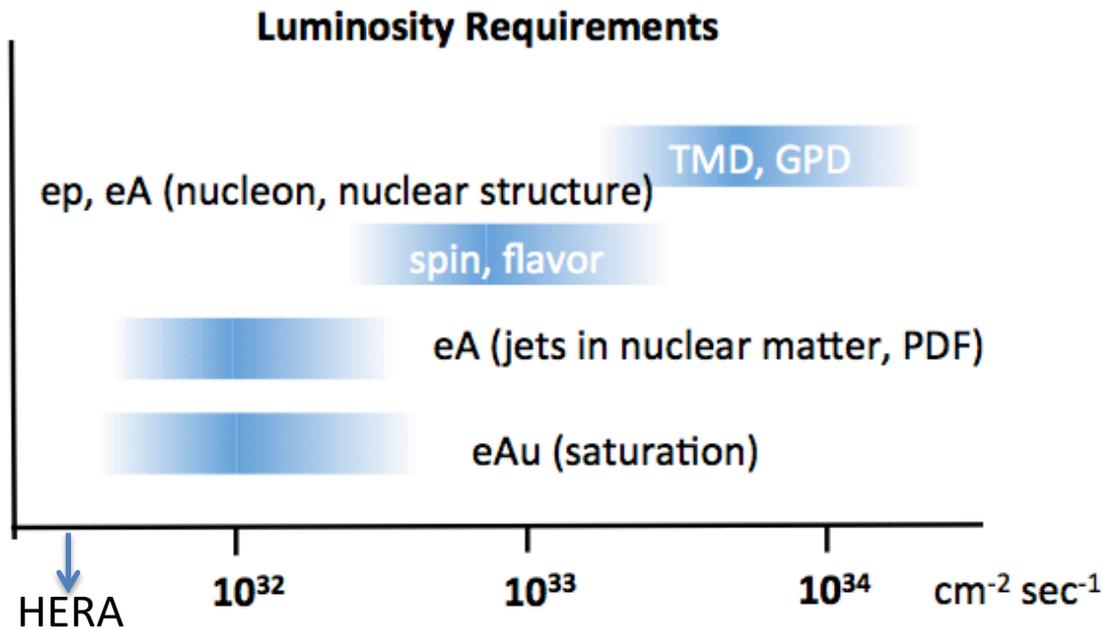


In nuclei, the interaction probability enhanced by $A^{1/3}$



Will nuclei saturate faster as color leaks out of nucleons?

Luminosity/Polarization Needed

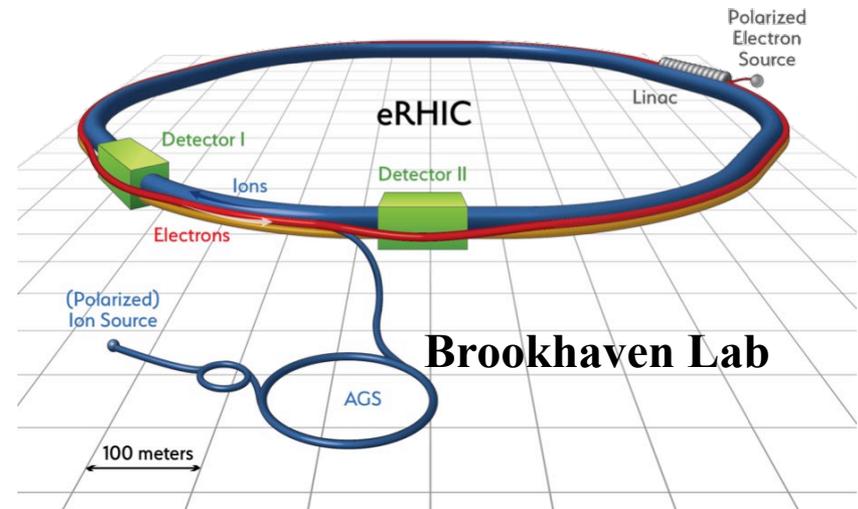
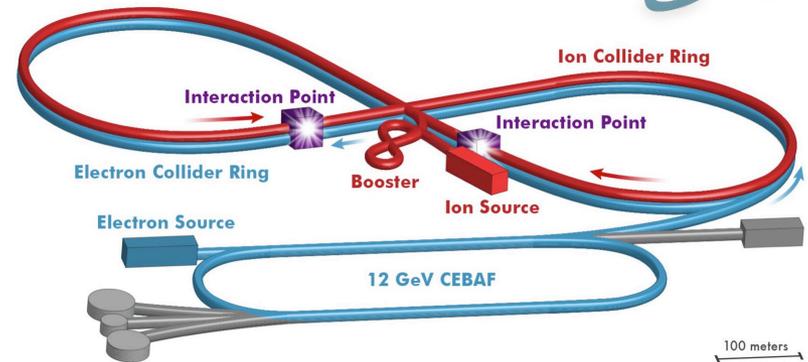


Central mission of EIC (nuclear and nucleon structure) requires high luminosity and polarization (>70%).

EIC Parameters

- US EIC Machine design aims from the [EIC Whitepaper](#)
 - **Highly polarized** (~70%) electron and nucleon beams.
 - **Ion beams** from deuterons to the heaviest nuclei (uranium or lead).
 - **Variable** center of mass energies from ~20 - ~100 GeV, upgradable to ~140 GeV.
 - High luminosity: $\sim 10^{33-34} \text{ cm}^{-2} \text{ s}^{-1}$
 - Possibility of having more than one interaction region.
- Two proposed realization plans
 - Jefferson Lab: building on the existing 12 GeV CEBAF. [JLEIC Design](#).
 - BNL: building on the existing RHIC. [eRHIC Design](#).
 - [Recent review of acc. R&D](#)
- Similar performances, cost according to LRP assessment.
- US EIC will likely be down-selected from one of these proposals.

Jefferson Lab 



END OF DAY 2

Day 3:

- EIC accelerator and detector realizations
- Other facilities and EIC physics topics.
- EIC and physics topic at other facilities.
- EIC and the future of Nuclear Physics.
- Epilogue