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# Fundamental Symmetries - 2

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#### Flow of the lectures

- Review symmetry and symmetry breaking
- Introduce the Standard Model and its symmetries
- Beyond the SM: an effective theory perspective and overview
- Discuss a number of "worked examples"
  - Precision measurements: charged current (beta decays); neutral current (PVES); muon g-2, ..
  - Symmetry tests: CP (T) violation and EDMs; Lepton Flavor and Lepton Number violation

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Today I.5 lectures

lectures

# The Standard Model and its symmetries (Part 2)

#### Towards a realistic model

- Identified gauge group as SU(3)xSU(2)xU(1)
- But pure gauge Lagrangian unrealistic:
  - massless fermions and gauge bosons
  - no SU(2)xU(1)- invariant mass term can be written
- Solution: add a new scalar EW doublet, the Higgs

#### The Standard Model



#### The Standard Model

• Gauge group:



#### • Building blocks: fermions and Higgs

	SU(3) <sub>c</sub> x SU(2) <sub>W</sub> x U(1) <sub>Y</sub> representation: (dim[SU(3) <sub>c</sub> ], dim[SU(2) <sub>W</sub> ], Y)	SU(2)w transformation
$l = \left(\begin{array}{c} \nu_L \\ e_L \end{array}\right)$	(1,2,-1/2)	$l \to V_{SU(2)} l$
$e = e_R$	(  ,  , - )	
$q^i = \left(\begin{array}{c} u_L^i \\ d_L^i \end{array}\right)$	( <mark>3,2,1/6</mark> )	$q \to V_{SU(2)} q$
$u^i = u^i_R$	( <mark>3</mark> , <b>1</b> , 2/3)	
$d^i = d_R^i$	<b>(3,  , -  /3)</b>	
$\varphi = \left(\begin{array}{c} \varphi^+ \\ \varphi^0 \end{array}\right)$	( <b> </b> ,2, <b> </b> /2)	$\varphi \to V_{SU(2)} \varphi$
$\tilde{\varphi} = \epsilon \varphi^* = \begin{pmatrix} \varphi \\ -\varphi \\ -\varphi \end{pmatrix}$	(1,2,-1/2)	$\tilde{\varphi} \to V_{SU(2)} \tilde{\varphi}$

• SM Lagrangian:



• SM Lagrangian:  $\mathcal{L}_{SM} = \mathcal{L}_{Gauge} + \mathcal{L}_{Higgs} + \mathcal{L}_{Yukawa}$ 

$$\mathcal{L}_{\text{Gauge}} = -\frac{1}{4} G^A_{\mu\nu} G^{A\mu\nu} - \frac{1}{4} W^I_{\mu\nu} W^{\mu\nu} - \frac{1}{4} B_{\mu\nu} B^{\mu\nu} + i\bar{\ell} \not{D} \ell + i\bar{e} \not{D} e + i\bar{q} \not{D} q + i\bar{u} \not{D} u + i\bar{d} \not{D} d$$

$$D_{\mu} = I \partial_{\mu} - ig_s \frac{\lambda^A}{2} G^A_{\mu} - ig \frac{\sigma^a}{2} W^a_{\mu} - ig' Y B_{\mu}$$

• SM Lagrangian:  $\mathcal{L}_{SM} = \mathcal{L}_{Gauge} + \mathcal{L}_{Higgs} + \mathcal{L}_{Yukawa}$ 

$$\mathcal{L}_{\text{Higgs}} = (D_{\mu}\varphi)^{\dagger} (D^{\mu}\varphi) - \lambda (\varphi^{\dagger}\varphi - v^{2})^{2} \xrightarrow{\text{EVVSB}} \langle \varphi \rangle = \begin{pmatrix} 0 \\ v \end{pmatrix}$$
$$\langle \tilde{\varphi} \rangle = \begin{pmatrix} v \\ 0 \end{pmatrix}$$
$$\langle \tilde{\varphi} \rangle = \begin{pmatrix} v \\ 0 \end{pmatrix}$$
$$v = 174 \,\text{GeV}$$

$$D_{\mu} = I \partial_{\mu} - ig_s \frac{\lambda^A}{2} G^A_{\mu} - ig \frac{\sigma^a}{2} W^a_{\mu} - ig' Y B_{\mu}$$

 $SU(2)_W \times U(1)_Y \rightarrow U(1)_{EM}$ 

• Expand around the minimum of the potential

$$\mathcal{L}_{\text{Higgs}} = (D_{\mu}\varphi)^{\dagger} (D^{\mu}\varphi) - \lambda (\varphi^{\dagger}\varphi - v^2)^2$$

$$\phi(x) = e^{i\pi_i(x)\sigma_i/v} \begin{pmatrix} 0\\ v + \frac{h(x)}{\sqrt{2}} \end{pmatrix}$$

 Generalization of the abelian Higgs model discussed in detail earlier on



•  $Q = T_3 + Y$  annihilates the vacuum  $\rightarrow$  unbroken U(1)<sub>EM</sub>. Photon remains massless, other gauge bosons (W<sup>±</sup>, Z) acquire mass

 $SU(2)_W \times U(1)_Y \rightarrow U(1)_{EM}$ 

• Expand around the minimum of the potential

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$$\mathcal{L}_{\text{Higgs}} = (D_{\mu}\varphi)^{\dagger}(D^{\mu}\varphi) - \lambda(\varphi^{\dagger}\varphi - v^{2})^{2} \qquad \phi(x) = e^{i\pi_{i}(x)\sigma_{i}/v} \begin{pmatrix} 0 \\ v + \frac{h(x)}{\sqrt{2}} \end{pmatrix}$$
$$\boxed{m_{W}^{2}W_{\mu}^{+}W_{\mu}^{-} + \frac{1}{2}m_{Z}^{2}Z_{\mu}Z_{\mu}](1 + \frac{1}{\sqrt{2}v}h)^{2}}$$
$$\frac{1}{2}(\partial_{\mu}h)^{2} - \frac{1}{2}m_{h}^{2}h^{2} - \sqrt{\frac{\lambda}{2}}m_{h}h^{3} - \frac{\lambda}{4}h^{4}}$$

 $m_h = 2\sqrt{\lambda}v$ 

Higgs mass controlled by v and Higgs self-coupling

$$G_F^{-1} = 2\sqrt{2}v^2$$

#### Fermion-Higgs sector: LYukawa

$$\mathcal{L}_{\text{Yukawa}} = \bar{e}_L Y_e e_R \left( v + \frac{h}{\sqrt{2}} \right) + \bar{d}_L Y_d d_R \left( v + \frac{h}{\sqrt{2}} \right) + \bar{u}_L Y_d u_R \left( v + \frac{h}{\sqrt{2}} \right) + \text{h.c.}$$

Fermion mass matrices diagonalized by bi-unitary transformation

$$Y_f = V_{f_L}^{\dagger} Y_f^{\text{diag}} V_{f_R} \qquad f = e, d, u \qquad \longrightarrow \qquad m_{f,i} = v \left( Y_f^{\text{diag}} \right)_{ii}$$

Higgs coupling to fermions is flavor-diagonal and proportional to mass

$$\mathcal{L}_{\text{Yukawa}} = \sum_{f=e,d,u} m_f \bar{f} f \left( 1 + \frac{h}{\sqrt{2}v} \right)$$
$$f = f_L + f_R$$

# Fermion-gauge sector: $\mathcal{L}_{int} = g A_{\mu}^{a} J^{\mu,a}$

• Neutral current

$$\mathcal{L}_{\text{int}} = -\frac{g}{2\cos\theta} Z^{\mu} \bar{\psi}_f \left( g_V^{(f)} \gamma_{\mu} - g_A^{(f)} \gamma_{\mu} \gamma_5 \right) \psi_f \qquad \begin{array}{l} \theta = \arctan\frac{g'}{g} \\ e = g\sin\theta, \end{array}$$
$$g_V^{(f)} = T_3^{(f)} - 2\sin^2\theta Q^{(f)} \qquad g_A^{(f)} = T_3^{(f)}$$

- Flavor diagonal
- Both V and A: expect P-violation



# Fermion-gauge sector: $\mathcal{L}_{int} = g A_{\mu}^{a} J^{\mu,a}$

Charged current



 $g_2 V_{ii}$ 

Cabibbo-Kobayashi-Maksawa matrix

- CKM matrix is unitary:
  - 9 real parameters, but redefinition of quark phases reduces physical parameters to 4: 3 mixing angles and 1 phase

$$V_{ij} \rightarrow V_{ij} e^{i((\phi_d)_j - (\phi_u)_i)}$$

5 independent parameters (phase differences)

• Irreducible phase implies CP violation:

- CKM matrix and  $m_q$  govern the pattern of flavor and CPV in the SM

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5 independent parameters (phase differences)

• Irreducible phase implies CP violation:

$$g_2 V_{ij} W^+_{\mu} \bar{u}^i_L \gamma^{\mu} d^j_L + g_2 V^*_{ij} W^-_{\mu} \bar{d}^j_L \gamma^{\mu} u^i_L$$

$$\int \mathbf{CP \ transformation}$$

$$g_2 V_{ij} W^-_{\mu} \bar{d}^j_L \gamma^{\mu} u^i_L + g_2 V^*_{ij} W^+_{\mu} \bar{u}^i_L \gamma^{\mu} d^j_L$$



• CKM matrix and  $m_q$  govern the pattern of flavor and CPV in the SM

# Symmetries of the Standard Model

- Now pause and take stock of what is the fate of symmetries in the SM (besides Poincare', which is built in)
  - Gauge symmetry is hidden (spontaneously broken)
  - Global (flavor) symmetries: all explicitly broken<sup>\*\*</sup> except for U(1) associated with B, L, and  $L_{\alpha}$  (individual lepton families)
  - Impact of anomalies: only B-L is conserved (but no worries at T=0)
  - P, C maximally violated by Weak interactions
  - CP (and T): violated by CKM (and QCD theta term)

\*\* Approximate SU(2) and SU(3) vector and axial symmetries of QCD play key role in strong interactions

# Symmetries of the Standard Model

- Most symmetries are broken
- However, SM displays approximate discrete (C, P, T) and global symmetries (B, L) observed in nature
- Not an input in the model, rather an outcome that depends on the assigned gauge quantum numbers (+ renormalizability)

- Standard Model tested at the quantum (loop) level in both electroweak and flavor sector
- Precision EW tests are at the 0.1% level. Examples of global fits:



• A few "tensions" and "anomalies": g-2, ... (will discuss it later on)

• Flavor physics and CP violation: K, B, D meson physics well described by CKM matrix, in terms of 3 mixing angles and a phase!



Some recent "anomalies" in B decays

• Higgs boson: discovered in  $H \rightarrow \gamma \gamma$  mode





- Higgs boson: discovered in  $H \rightarrow \gamma \gamma$  mode
- So far Higgs properties are compatible with the Standard Model



- Couplings to W, Z, γ,g and t, b, T known at 20-30% level
- But couplings to light flavors much less constrained
- Still room for deviations: is this the SM Higgs? Key question at LHC Run 2 & important target for low energy experiments

# Beyond the Standard Model

### The quest for "new physics"

• The SM is remarkably successful, but can't be the whole story



Tev

# The quest for "new physics"

The SM is remarkably successful, but can't be the whole story
 ⇒ new degrees of freedom (Heavy? Light & weakly coupled? Both?)



 Two approaches, both needed to reconstruct BSM dynamics (structure, symmetries, and parameters of L<sub>BSM</sub>)

# Models of new physics

- Extended gauge group  $(SU(2)_L \times SU(2)_R \times U(1), ...)$ , Grand Unified group (SU(5), SO(10), ...)
- Extended particle content (2HDM, ...)
- New symmetry: Supersymmetry
- Composite models (QCD-like EWSB)
- Dark sector
- Combinations of the above
- •

In the following, I will assume that new physics originates above the electroweak scale and discuss its low-energy footprints in the framework of effective field theory

#### The low-energy footprints of L<sub>BSM</sub>



• At energy scales  $E \le M_{BSM}$ , new physics shows up as local operators



### The low-energy footprints of L<sub>BSM</sub>



• EFT expansion in E/M<sub>BSM</sub>, M<sub>W</sub>/M<sub>BSM</sub>

 Each model generates its own pattern of operators: experiments at E<< M<sub>BSM</sub> can *discover* and *tell apart* new physics scenarios

#### Role of low-E experiments

• Comment #I: O<sub>i</sub><sup>(d)</sup> can be roughly divided in two classes



(ii) Those that violate (approximate)
SM symmetries: mediate rare/
forbidden processes (qFCNC, LFV, LNV, BNV, EDMs)



#### Role of low-E experiments

• Comment #1:  $O_i^{(d)}$  can be roughly divided in two classes

(i) Those that give corrections to SM "allowed" processes: probe them with precision measurements ( $\beta$ -decays, muon g-2, Q<sub>W</sub>,...)

(ii) Those that violate (approximate)
SM symmetries: mediate rare/
forbidden processes (qFCNC, LFV, LNV, BNV, EDMs)

 Comment #2: each UV model generates its own pattern of operators / couplings → different signatures in LE experiments

Therefore, LE measurements provide the opportunity to both <u>discover</u> BSM effects & <u>discriminate</u> among BSM scenarios (maximal impact in combination with the LHC)

#### A guided tour of $L_{eff}$

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{SM} + \frac{C^{(5)}}{\Lambda} O^{(5)} + \sum_{i} \frac{C_{i}^{(6)}}{\Lambda^{2}} O_{i}^{(6)} + \dots$$

• Dim 5: only one operator

Weinberg 1979

$$\hat{O}_{\text{dim}=5} = \ell^T C \epsilon \varphi \ \varphi^T \epsilon \ell \qquad C = i \gamma_2 \gamma_0$$



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- Violates total lepton number  $(| \rightarrow e^{i\alpha} |, e \rightarrow e^{i\alpha} e)$
- Generates Majorana mass for L-handed neutrinos (after EWSB)

$$\frac{1}{\Lambda}\hat{O}_{\text{dim}=5} \xrightarrow{\langle\varphi\rangle = \begin{pmatrix} 0\\v \end{pmatrix}} \frac{1}{\Lambda}\nu_L^T C\nu_L$$

## A guided tour of $L_{eff}$

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$$\frac{1}{\Lambda}\hat{O}_{\text{dim}=5} \qquad \xrightarrow{\langle\varphi\rangle = \begin{pmatrix} 0 \\ v \end{pmatrix}} \qquad \frac{v^2}{\Lambda}\nu_L^T C\nu_L$$

• "See-saw":  $m_{\nu} \sim 1 \,\mathrm{eV} \rightarrow \Lambda \sim 10^{13} \,\mathrm{GeV}$
Explicit realization of dimension-5 operator in models with heavy R-handed Majorana neutrinos



$$\mathcal{L}_5 = g_{\alpha\beta} \ \ell_{\alpha}^T C \epsilon \varphi \ \varphi^T \epsilon \ell_{\beta}$$

• Or with triplet Higgs field:



$$\mathcal{L}_5 = \mathbf{g}_{\alpha\beta} \ \ell_{\alpha}^T C \epsilon \varphi \ \varphi^T \epsilon \ell_{\beta}$$

### A guided tour of $L_{eff}$

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{SM} + \frac{C^{(5)}}{\Lambda} O^{(5)} + \sum_{i} \frac{C_{i}^{(6)}}{\Lambda^{2}} O_{i}^{(6)} + \dots$$

• Dim 6: affect many processes



### A guided tour of $L_{eff}$

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{SM} + \frac{C^{(5)}}{\Lambda} O^{(5)} + \sum_{i} \frac{C_{i}^{(6)}}{\Lambda^{2}} O_{i}^{(6)} + \dots$$

- Dim 6: affect many processes
  - B violation

Weinberg 1979 Wilczek-Zee1979 Buchmuller-Wyler 1986, .... Grzadkowski-Iskrzynksi-Misiak-Rosiek (2010)

- Gauge and Higgs boson couplings
- CPV, LFV, qFCNC, ...
- g-2, Charged Currents, Neutral Currents, ...

This equation at work

$$\delta O_{\rm BSM}(\Lambda) \lesssim (O_{\rm exp} - O_{\rm SM})$$





- Caveat: horizontal axis is  $\Lambda/C^{(5)}$ ,  $\Lambda/[C_i^{(6)}]^{1/2}$ , ....
- So beware of couplings, loop factors, approximate symmetries , etc



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- So beware of couplings, loop factors, approximate symmetries , etc

### Challenges

• Precision experiments

Theory: control physics over many scales and hadronic / nuclear environment



#### Next steps

- "Worked examples" that connect to NP experimental program
- Precision measurements: beta decays, PV electron scattering, muon g-2





Qweak



muon g-2

• Symmetry tests: Electric Dipole moments, LFV in muon processes,  $0\nu\beta\beta$  and LNV





Mu<sub>2</sub>e



Majorana

# Precision measurements as probes of new physics



# Charged Current













## β-decays and BSM physics

• In the SM, W exchange (V-A, universality)



# β-decays and BSM physics

In the SM, W exchange (V-A, universality)



- Broad band sensitivity to BSM physics
- Name of the game: precision! To probe BSM scale  $\Lambda$ , need expt. & th. at the level of  $(v / \Lambda)^2$ : therefore 10<sup>-3</sup> is a well motivated target
- Precision at or approaching 0.1%. Probe scale  $\Lambda \sim 5-10$  TeV

• Effect of any new physics encoded in ten quark-level couplings

$$\begin{aligned} \mathcal{L}_{CC} &= -\frac{G_F^{(0)} V_{ud}}{\sqrt{2}} \times \left[ (1 + \epsilon_L) \ \bar{e}\gamma_\mu (1 - \gamma_5) \nu_\ell \cdot \bar{u}\gamma^\mu (1 - \gamma_5) d \right. \\ &+ \epsilon_R \ \bar{e}\gamma_\mu (1 - \gamma_5) \nu_\ell \cdot \bar{u}\gamma^\mu (1 + \gamma_5) d \\ &+ \epsilon_S \ \bar{e}(1 - \gamma_5) \nu_\ell \cdot \bar{u}q d \\ &- \epsilon_P \ \bar{e}(1 - \gamma_5) \nu_\ell \cdot \bar{u}\gamma_5 d \\ &+ \epsilon_T \ \bar{e}\sigma_{\mu\nu} (1 - \gamma_5) \nu_\ell \cdot \bar{u}\sigma^{\mu\nu} (1 - \gamma_5) d \right] + \text{h.c.} \end{aligned}$$

$$\begin{aligned} &+ \epsilon_i \longrightarrow \tilde{\epsilon}_i \quad (1 - \gamma_5) \nu_\ell \longrightarrow (1 + \gamma_5) \nu_\ell \end{aligned}$$

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n

8α

 $\langle p|\bar{u}\Gamma d|n\rangle = g_{\Gamma}\bar{\psi}_{p}\Gamma\psi_{n}$ 

 To connect experiment to (B)SM couplings, need radiative corrections + hadronic & nuclear matrix elements

#### How do we probe the E's?

- Rich phenomenology, two classes of observables:
  - I. Differential decay rates (probe non V-A via "b" and correlations)

$$d\Gamma \propto F(E_e) \left\{ 1 + \frac{b}{E_e} \frac{m_e}{E_e} + \frac{a}{E_e} \frac{\vec{p_e} \cdot \vec{p_\nu}}{E_e E_\nu} + \langle \vec{J} \rangle \cdot \left[ A \frac{\vec{p_e}}{E_e} + B \frac{\vec{p_\nu}}{E_\nu} + \cdots \right] \right\}$$

Lee-Yang, Jackson-Treiman-Wyld



#### $a(\epsilon_{\alpha}), A(\epsilon_{\alpha}), B(\epsilon_{\alpha}), ...$

isolated via suitable experimental asymmetries

#### How do we probe the E's?

- <u>Rich phenomenology</u>, two classes of observables:
  - I. Differential decay rates (probe non V-A via "b" and correlations)
  - 2. Total decay rates (probe mostly V, A via extraction of  $V_{ud}$ ,  $V_{us}$ )



# Summary of low energy constraints

- This table summarizes a large number of measurements and th. input
- Already quite impressive. Effective scales in the range  $\Lambda$ = 1-10 TeV ( $\Lambda_{SM} \approx 0.2$  TeV)

VC, S.Gardner, B.Holstein 1303.6953 Gonzalez-Alonso & Naviliat-Cuncic 1304.1759



Non-standard coupling	Observable	Current sensitivity	Prospective sensitivity
$\operatorname{Re}(\epsilon_L + \epsilon_R)$	$\Delta_{ m CKM}$	$\sim 0.05\%$	< 0.05% *
$\operatorname{Im}(\epsilon_R)$	$D_n$	$\sim 0.05\%$	
$\epsilon_P, \ \tilde{\epsilon}_P$	$R_{\pi} = \frac{\Gamma(\pi \to e\nu)}{\Gamma(\pi \to \mu\nu)}$	$\sim 0.05\%$	
$\operatorname{Re}(\epsilon_S)$	$b,\ B,\ [ ilde{a},\  ilde{A},\  ilde{G}]$	$\sim 0.5\%$	< 0.3%
$\operatorname{Im}(\epsilon_S)$	$R_n$	$\sim 10\%$	
$\operatorname{Re}(\epsilon_T)$	$b, \ B, \ [\tilde{a}, \ \tilde{A}, \ \tilde{G}], \ \ \pi \to e \nu \gamma$	$\sim 0.1\%$	< 0.03%
$\operatorname{Im}(\epsilon_T)$	$R_{^{8}Li}$	$\sim 0.2\%$	$\sim 0.05\%$
$\tilde{\epsilon}_{\alpha \neq P}$	a, b, B, A	$\sim 5-10\%$	

# Summary of low energy constraints

- This table summarizes a large number of measurements and th. input
- Already quite impressive. Effective scales in the range  $\Lambda$ = 1-10 TeV ( $\Lambda_{SM} \approx 0.2$  TeV)
- Focus on probes that depend on the ε's *linearly*

$$\tilde{Y}(E_e) = \frac{Y(E_e)}{1 + b \, m_e/E_e + \dots}$$

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#### CKM unitarity: input

$$|\bar{V}_{ud}|^2 + |\bar{V}_{us}|^2 + |\bar{V}_{us}|^2 = 1 + \Delta_{\text{CKM}}(\epsilon_i)$$



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• Extraction dominated by  $0^+ \rightarrow 0^+$  transitions



$$|V_{ud}|^2 + |V_{us}|^2 + |V_{us}|^2 = 1 + \Delta_{\mathrm{CKM}}(\epsilon_i)$$



• Extraction dominated by  $0^+ \rightarrow 0^+$  transitions

• Not yet competitive:

$$V_{ud} = \left[\frac{4908.7(1.9) \ s}{\tau_n \left(1 + 3g_A^2\right)}\right]^{1/2}$$

Czarnecki, Marciano, Sirlin 2004

#### $V_{ud}$ from $0^+ \rightarrow 0^+$ nuclear $\beta$ decays

$$\frac{1}{t} = \frac{G_{\mu}^2 |V_{ud}|^2 m_e^5}{\pi^3 \log 2} f(Q) \ (1 + \frac{RC}{}) \longrightarrow ft \ (1 + \frac{RC}{}) = \frac{2984.48(5) \ s}{|V_{ud}|^2}$$



 $\langle f | \tau_+ | i \rangle = \sqrt{2} (1 - \delta_C/2)$ Coulomb distortion of wave-functions

 $\delta_C \sim 0.5\%$ 

Towner-Hardy Ormand-Brown Nucleus-dependent rad. corr. (Z, E<sup>max</sup> ,nuclear structure)

$$\delta_R \sim 1.5\%$$

Sirlin-Zucchini '86 Jaus-Rasche '87 Nucleus-independent short distance rad. corr.

$$\Delta_R \sim 2.4\%$$

Marciano-Sirlin '06



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$$\frac{1}{t} = \frac{G_{\mu}^2 |V_{ud}|^2 m_e^5}{\pi^3 \log 2} f(Q) \ (1 + \frac{RC}{}) \longrightarrow \frac{f t}{t} \ (1 + \frac{RC}{}) = \frac{2984.48(5) s}{|V_{ud}|^2}$$







• New LQCD calculations have led to smaller  $V_{us}$  from  $K \rightarrow \pi I v$ 

#### CKM unitarity test

$$|\bar{V}_{ud}|^2 + |\bar{V}_{us}|^2 + |\bar{V}_{bi}|^2 = 1 + \Delta_{\text{CKM}}(\epsilon_i)$$



- No longer perfect agreement:
  - New physics?
  - Underestimated th. errors? [ $\delta_C$  (A,Z), f<sub>+</sub>(0), F<sub>K</sub>/F<sub> $\pi$ </sub> ]

#### CKM unitarity: opportunities

- Given high stakes (0.05% EW test), it is highly desirable to
  - Assess robustness of  $\delta_C$ : nucl. str. calculations + expt. validation
  - Pursue  $V_{ud}$  @ 0.02% through neutron decay

$$V_{ud} = \left[\frac{4908.7(1.9) \ s}{\tau_n \left(1 + 3g_A^2\right)}\right]^{1/2}$$

$$\frac{\delta \tau_n}{\delta \tau_n} \sim 0.35 \text{ s}$$

$$\frac{\delta \tau_n}{\tau_n} \sim 0.04 \%$$

BL2, BL3 (cold beam), UCNT, ...

 $\delta g_A/g_A \sim 0.025\%$ (δa/a , δA/A ~ 0.1%)

aCORN, Nab, UCNA+, ...



\*\* For global analysis see Wauters et al, 1306.2608



\*\* For global analysis see Wauters et al, 1306.2608

#### Scalar and tensor couplings

FUTURE

- Several precision measurements on the horizon (neutron & nuclei)
- For definiteness, study impact of b<sub>n</sub>, B<sub>n</sub> @ 10<sup>-3</sup>; b<sub>GT</sub> (<sup>6</sup>He, ...) @10<sup>-3</sup>



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• Can greatly improve existing limits on  $\varepsilon_T$ , probing  $\Lambda_T \sim 10 \text{ TeV}$ 

# High energy constraints

- The new physics that contributes to  $\varepsilon_{\alpha}$  affects other observables!
- Relative strength of constraints depends on the specific model
- Model-independent statements possible in "heavy BSM" limit:  $M_{BSM} > TeV \rightarrow new physics looks point-like at the weak scale$





<u>Vertex corrections</u> strongly constrained by Z-pole observables ( $\Delta_{CKM}$  is at the same level)

 $\frac{Four-fermion\ interactions}{\sigma_{had}\ at\ LEP\ would\ allow\ \Delta_{CKM}\ \sim 0.01\ and\ non\ V-A} structures\ at\ \epsilon_i\ \sim\ 5\%.$  What about LHC?

VC, Gonzalez-Alonso, Jenkins 0908.1754

#### LHC constraints

Heavy BSM limit: all ε<sub>α</sub> couplings contribute to the process

 $p p \rightarrow e v + X$ 



T. Bhattacharya, VC, et al, 1110.6448 VC, Gonzalez-Alonso, Graesser, 1210.4553

### LHC constraints

• Heavy BSM limit: all  $\epsilon_{\alpha}$  couplings contribute to the process  $p p \rightarrow e v + X$ 

- No excess events at high  $m_T$  $\Rightarrow$  bounds on  $\varepsilon_{\alpha}$
- Current bounds at the level of 0.3%-1%, depending on the operator




### β decays vs LHC reach



VC, Gonzalez-Alonso, Graesser, 1210.4553

### β decays vs LHC reach



Unmatched lowenergy sensitivity and future reach

LHC limits close to low-energy. Interesting interplay in the future LHC reach already stronger than low-energy

VC, Gonzalez-Alonso, Graesser, 1210.4553

• Scalar and tensor operators:  $\beta$ -decays can probe deeper than the LHC!



#### Connection to models

- A given model  $\rightarrow$  set overall size and pattern of  $\epsilon_{\alpha}$  couplings
- Beta decays can play very useful diagnosing role. Qualitative picture:

		٤L	٤ <sub>R</sub>	٤ <sub>P</sub>	٤s	٤ <sub>T</sub>	
	LRSM	x	√	x	x	x	$\sim$
Can be made quantitative	LQ	√	x	√	√	√	u e d LQ v
	2HDM	x	x	√	√	x	$H^{+}$
Bauman, Erler, Ramsey-Musolf, arXiv:1204.0035	MSSM	√	1	√	4	V	$u \xrightarrow{\chi_k^+} \nu_I$ $d_i \xrightarrow{\tilde{d}_i^-} \ell_I$ $d \xrightarrow{\chi_m^0} \ell_I$
Musolf, Tulin hep-ph/0608064	YOUR FAVORITE MODEL		•••		•••		$W^+ \chi_i^0 \qquad \nu_I$ $\chi_j^- \qquad \ell_I$

### Neutral Current

# Neutral analogue of V-A CC interaction?

 Speculation by Zel'dovic before the incorporation within the SU(2)xU(1) model of electroweak interactions

σ · p < 0) can differ by 0.1 to 0.01 percent. Such

an effect is a specific test for an interaction not

A magnetized iron plate can served as a source

conserving parity

	PARILI NONCON	SERVATION IN THE
	FIRST ORDER IN	THE WEAK-INTER-
682 LETTERS 1	TO THE EDIT ACTION CONSTAN	NT IN FLECTRON
PARITY NONCONSERVATION IN THE FIRST ORDER IN THE WEAK-INTER- ACTION CONSTANT IN ELECTRON SCATTERING AND OTHER EFFECTS	ing electrons SCATTERING ANI	O OTHER EFFECTS
Ya. B. ZEL' DOVICH	the electron levels of different parities in the free	
Submitted to JETP editor December 25, 1958	atom.	
J. Exptl. Theoret. Phys. (U.S.S.R.) 36, 964-966 (March, 1959) We assume that besides the weak interaction	stable transition $2S_{1/2} \rightarrow 1S_{1/2}$ , which appears on account of the admixture of $2P_{1/2}$ to the $2S_{1/2}$ , still turns out to be even smaller that the transition probability on account of the meaning formation	1958
that causes beta decay,	the electron, and is less than the probability of the	1700
$g(\overline{PON})(\overline{e}^{*}O_{*}) + \text{Herm. conj.},$ (1)	two-quantum transition 25 - 18 by a factor of more than 10". Finally, the interaction (3) leads	
there exists an interaction	to a rotation of the plane of polarization of visible	
(POP) (COC) (23	light by any substance not containing molecules	
with $g \approx 10^{-60}$ and the operator $Q = \infty (1 \pm i\infty)$	optically active in the ordinary sense of the words.	
characteristic' of processes in which parity is not	because the weak interaction mixes atomic elec-	
conserved.*	tronic states of different parity. A calculation of	▼
Then in the scattering of electrons by protons	the effect gives an expression of the form	·
scattering, and the nonconservation of parity will	aright - Alen :	
appear in terms of the first order in the small	$\sim N_{*}(\sigma^{*}(x), \sigma) d_{\pi}(0) = d_{\pi}(0) + (4E_{\pi} - E_{\pi})$ (3)	Discovery of
quantity g. Owing to this it becomes possible to	$= \sum_{i=1}^{n} \sum_{j=1}^{n} \varphi_i(\phi_j) \varphi_i(\phi_j) \gamma(e_F - e_S),  (a)$	. /
to determine the sign of g.	where n is the index of refraction for circularly polarized light: $N_s \approx a^{-3}$ is the number density of	neutral currents
The matrix element of the Coulomb scattering	the atoms; a is the linear dimension of an atom;	incuti ai cui i ciits
is of the order of magnitude e <sup>2</sup> /k <sup>2</sup> , where k is	$\lambda$ is the wavelength of the light; $ \phi_S(0)  \sim 1/a^{3/2}$ ;	
quently, the ratio of the interference term to the	in  cp(0)  there are nonvanishing "small com-	In $v_{\mu}e \rightarrow v_{\mu}e$
Coulomb term is of the order of gk2/e2. Substi-	where $\varphi$ are the "large components"; $ \phi_D(0)  \sim$	۳ ۳
tuting $g = 10^{-6}/M^2$ , where M is the mass of the	$(h/mc)a^{-1/2}$ , so that	would be made in
conservation effects can be of the order of 0.1 to		
0.01 percent.	$ n_{\text{sight}} - n_{\text{teft}}  \sim (g/a^{-}\Delta E_{SP})(\Delta/m_{c}r) \sim 10^{-40}.$ (4)	1072
In the scattering of fast (~ 10 <sup>9</sup> ev) longitudi-	Rotation of the plane of polarization by fradian	9/3
unpolarized terret made it can be amounted that	occurs in a length of the order $\frac{1}{10^{-20}} = 10^{12}$ cm.	
the cross-sections for right-hand and left-hand	so that even in the first order in g the effect ob-	
electrons (i.e., for electrons with $\sigma \cdot p > 0$ and	viously cannot be observed.	

DADITY MONCONCEDUATION IN THE

How plausible is the assumption that the interaction (2) exists? Let us regard as a shablet

#### PARITY NONCONSERVATION IN THE FIRST ORDER IN THE WEAK-INTER-ACTION CONSTANT IN ELECTRON SCATTERING AND OTHER EFFECTS

WE assume that besides the weak interaction that causes beta decay,

$$g(\overline{PON})(\overline{e}^{-}Ov) + \text{Herm. conj.},$$
 (1)

there exists an interaction

$$g(\overline{P}OP)(\overline{e}^{-}Oe^{-})$$
(2)

with  $g \approx 10^{-49}$  and the operator  $O = \gamma_{\mu} (1 + i\gamma_5)$ characteristic<sup>1</sup> of processes in which parity is not conserved.\*

Then in the scattering of electrons by protons the interaction (2) will interfere with the Coulomb scattering, and the nonconservation of parity will appear in terms of the first order in the small quantity g. Owing to this it becomes possible to test the hypothesis used here experimentally and to determine the sign of g.

In the scattering of fast (~10<sup>9</sup> ev) longitudinally polarized electrons through large angles by unpolarized target nuclei it can be expected that the cross-sections for right-hand and left-hand electrons (i.e., for electrons with  $\sigma \cdot p > 0$  and  $\sigma \cdot p < 0$ ) can differ by 0.1 to 0.01 percent. Such an effect is a specific test for an interaction not conserving parity.





Parity violating

$$A_{\rm PV} = \frac{\sigma_{\rm I} - \sigma_{\rm I}}{\sigma_{\rm I} + \sigma_{\rm I}}$$

• A<sub>PV</sub> violates parity:



• A<sub>PV</sub> violates parity:



• Expected size of the effect:

The matrix element of the Coulomb scattering is of the order of magnitude  $e^2/k^2$ , where k is the momentum transferred ( $\hbar = c = 1$ ). Consequently, the ratio of the interference term to the Coulomb term is of the order of  $gk^2/e^2$ . Substituting  $g = 10^{-5}/M^2$ , where M is the mass of the nucleon, we find that for  $k \sim M$  the parity nonconservation effects can be of the order of 0.1 to 0.01 percent.



• Through 4 decades of technical progress, parity-violating electron scattering (PVES) has become a precision tool



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### A<sub>PV</sub> in the Standard Model

• Neutral currents predicted in the Standard Model

$$\mathcal{L}_{\text{int}} = -\frac{g}{2\cos\theta} Z^{\mu} \bar{\psi}_f \left( g_V^{(f)} \gamma_{\mu} - g_A^{(f)} \gamma_{\mu} \gamma_5 \right) \psi_f \qquad \begin{array}{l} \theta = \arctan\frac{g'}{g} \\ e = g\sin\theta, \end{array}$$
$$g_V^{(f)} = T_3^{(f)} - 2\sin^2\theta Q^{(f)} \qquad g_A^{(f)} = T_3^{(f)} \qquad \boxed{Q_W^{(f)} = 2 g_V^{(f)}} \qquad \begin{array}{l} \text{Weak charge of the fermion} \end{array}$$

~

### A<sub>PV</sub> in the Standard Model

• Neutral currents predicted in the Standard Model

• Through  $g_V$ ,  $A_{PV}$  provides a handle on weak mixing angle

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$$g_V^{(f)} = T_3^{(f)} - 2\sin^2\theta Q^{(f)} \qquad g_A^{(f)} = T_3^{(f)} \qquad Q_W^{(f)} = 2g_V^{(f)} \qquad \text{Weak charge of the fermion}$$

$$\stackrel{e}{\longrightarrow} \stackrel{e}{\longrightarrow} \stackrel{e}{\longrightarrow$$

#### Experimental processes







Courtesy of P. Reimer and R. Arnold

#### Impact of PVES

• Precise LE measurements of  $\theta_W$  & constraints on BSM



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### Effective Lagrangian and $A_{\text{PV}}$

• At low-energy PV in neutral current described by effective Lagrangian

SM

$$\mathcal{L}_{\mathsf{PV}}^{eq} = \frac{G_{\mu}}{\sqrt{2}} \sum_{q} \left[ C_{1q} \overline{e} \gamma^{\mu} \gamma_{5} e \overline{q} \gamma_{\mu} q + C_{2q} \overline{e} \gamma^{\mu} e \overline{q} \gamma_{\mu} \gamma_{5} q \right]$$

$$C_{1u} = -\frac{1}{2} + \frac{4}{3} \sin^2 \theta_W \approx -0.19$$
  

$$C_{1d} = \frac{1}{2} - \frac{2}{3} \sin^2 \theta_W \approx 0.35$$
  

$$C_{2u} = -\frac{1}{2} + 2 \sin^2 \theta_W \approx -0.04$$
  

$$C_{2d} = \frac{1}{2} - 2 \sin^2 \theta_W \approx 0.04$$

$$\begin{array}{c} e & A \\ e & Z^{0} \\ q & Z^{0} \\ q & V \end{array} \qquad e & e \\ Q & Q \\ C_{1i} \equiv 2g_{A}^{e}g_{V}^{i} \qquad C_{2i} \equiv 2g_{V}^{e}g_{A}^{i} \end{array}$$

BSM

$$\mathcal{L}_{eq} = \sum_{i,j=L,R} \frac{g_{ij}^2}{\Lambda^2} \overline{e}_i \gamma_\mu e_i \, \overline{q}_j \gamma^\mu q_j$$

+ purely leptonic

$$\frac{\overline{x}}{x} + \frac{\overline{y}}{e} + \frac{\overline{z}}{e} + \frac{\overline$$

• Operators probed & NP sensitivity:

$$\mathsf{SM} \qquad \mathcal{L}_{\mathsf{PV}}^{eq} = \frac{G_{\mu}}{\sqrt{2}} \sum_{q} \left[ C_{1q} \overline{e} \gamma^{\mu} \gamma_{5} e \overline{q} \gamma_{\mu} q + C_{2q} \overline{e} \gamma^{\mu} e \overline{q} \gamma_{\mu} \gamma_{5} q \right]$$



 Improved precision on quark couplings

$$C_{1u} = -0.1835 \pm 0.0054$$
$$C_{1d} = 0.3355 \pm 0.0050$$

• Operators probed & NP sensitivity:

$$\mathsf{SM} \qquad \mathcal{L}_{\mathsf{PV}}^{eq} = \frac{G_{\mu}}{\sqrt{2}} \sum_{q} \left[ C_{1q} \overline{e} \gamma^{\mu} \gamma_{5} e \overline{q} \gamma_{\mu} q + C_{2q} \overline{e} \gamma^{\mu} e \overline{q} \gamma_{\mu} \gamma_{5} q \right]$$



• Operators probed & NP sensitivity:

BSM 
$$\mathcal{L}_{eq} = \sum_{i,j=L,R} \frac{g_{ij}^2}{\Lambda^2} \overline{e}_i \gamma_\mu e_i \overline{q}_j \gamma^\mu q_j$$

+ purely leptonic (Moller)

Sensitivities to new physics •  $\Lambda_{\text{new}} \simeq [\sqrt{2} \text{ GF } \Delta \text{Qw}]^{-1/2} = 246.22 \text{ GeV} / \sqrt{\Delta} \text{Qw}$ •  $\Lambda_{\text{new}} \simeq 3.4 \text{ TeV}$  (Qw<sup>e</sup> from E158) •  $\Lambda_{new} \simeq 4.6 \text{ TeV} (Qw^{p} \text{ from Qweak})$  Anew ≃ 2.5 TeV (C<sub>ij</sub> from SoLID) •  $\Lambda_{\text{new}} \simeq 7.5 \text{ TeV}$  (Qw<sup>e</sup> from MOLLER) •  $\Lambda_{new} \simeq 6.3 \text{ TeV} (Q_W^p \text{ from } P2@Mainz)$ •  $\Lambda_{new} \simeq 3.7 \text{ TeV} (g_R^2 \text{ from NuTeV})$ •  $\Lambda_{new} \approx 5.2 \text{ TeV} (Q_W^n \text{ from APV in Cs})$ 

Best contactinteraction reach for leptonic operators, at low OR high-energy

J. Erler

# Muon "g-2"



### Lepton magnetic moments

$$\vec{\mu} = g \frac{e}{2mc} \vec{s}, \qquad \vec{s} = \frac{\hbar}{2} \vec{\sigma}$$

- Dirac predicts g=2 in 1928
- 1947: Measurements find  $g_e \neq 2$
- Schwinger calculated  $g_e = 2(1+a_e)$   $a_e = \frac{(g_e-2)}{2} = \frac{\alpha}{2\pi} \approx 0.00116$



Great success of QED

- Current experimental precision:  $\Delta g_e = 5.2 \times 10^{-13}$  and  $\Delta g_{\mu} = 1.2 \times 10^{-9}$ 
  - g<sub>e</sub> used to extract electromagnetic coupling
  - $g_{\mu}$  used to challenge the SM!

- How is  $g_{\mu}(a_{\mu})$  measured?
  - Exploit the fact that momentum and spin do not precess in the same way in a B field
  - Relative frequency ω<sub>a</sub> proportional to (g-2)\*B



$$\omega_S = \frac{geB}{2mc} + (1-\gamma)\frac{eB}{\gamma mc}$$

- Current experimental precision:  $\Delta g_e = 5.2 \times 10^{-13}$  and  $\Delta g_{\mu} = 1.2 \times 10^{-9}$ 
  - g<sub>e</sub> used to extract electromagnetic coupling
  - $g_{\mu}$  used to challenge the SM!
- At this level of precision,  $g_{\mu}(a_{\mu})$  depends on loops from all Standard Model particles that couple to the muon



Known to 5 loops! Kinoshita et al 2012

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	VALUE ( $\times 10^{-11}$ ) UNITS
QED $(\gamma + \ell)$	$116584718.853\pm 0.022\pm 0.029_{\alpha}$
HVP(lo)*	$6923\pm42$
HVP(ho)	$-98.4\pm0.7$
H-LBL	$105 \pm 26$
EW	$154\pm1\pm2$
Total SM	$116591802 \pm 42_{\rm H\text{-}LO} \pm 26_{\rm H\text{-}HO} \pm 2_{\rm other}(\pm 49_{\rm tot})$

• Anatomy:

#### Where are we?

• Serious hint of new physics



#### Where are we?

• Serious hint of new physics







New g-2 at Fermilab will improve uncertainty factor of 4

#### Where are we?

Serious hint of new physics

 $a_{\mu} = (g_{\mu} - 2)/2$  $a_{\mu}(\text{Expt}) = 116592089(54)(33) \times 10^{-11}$ BNL E821 (2006)  $a_{\mu}(SM) = 116591802(42)(26)(02) \times 10^{-11}$  $\Delta a_{\mu} = 287(80) \times 10^{-11}$  3.6 $\sigma$  discrepancy Dominant uncertainties: ongoing efforts to improve these results using Lattice QCD

Probe BSM mag. dipole operators  $\mathcal{L} \xrightarrow{\text{EWSB}} y_{\mu} \frac{v}{\Lambda^2} \bar{\mu} \sigma^{\alpha\beta} \mu F_{\alpha\beta}$ 

3.6 $\sigma$  discrepancy  $\Rightarrow \Lambda/\sqrt{y_{\mu}} \sim 140 \text{ TeV}$  ( $\Lambda \sim 3.5 \text{ TeV}$ ). Strong "boundary condition" for TeV extensions of the SM



## Backup

#### BSM: dimension 5

• Construct all possible dim=5 effective operators in detail: this illustrates the method and leads to a physically interesting result

- Fermions only (and derivatives)? No: Use [Ψ]=3/2 and gauge invariance [Ψ's belong to chiral representations]
- Scalars only, vectors only? No: use [φ] = [V] = I and gauge invariance
- Vectors + Fermions & Vectors + scalars? No
- So, we are lead to consider operators with fermions (2) and scalars
   (2) and no derivatives

- If scalars are  $\phi$  and  $\phi^* \Rightarrow$ 
  - total hypercharge Y of fermions  $\Psi_1$  and  $\Psi_2$  is 0
  - need a multiplet and its charge-conjugate
  - but cannot make non-vanishing Lorentz scalar of dim3 (  $ar{\psi}\psi=0$  )

- We are left with building blocks  $\varphi, \varphi, \Psi_1, \Psi_2$ 
  - Forming SU(2) w invariants:  $\varphi^{\mathsf{T}} \epsilon \varphi = 0 \Rightarrow \Psi_1, \Psi_2$  must be doublets (so we are left with I or q)

Recall: 
$$\epsilon = \begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$$

- If scalars are  $\phi$  and  $\phi^* \, \Rightarrow \,$ 
  - total hypercharge Y of fermions  $\Psi_1$  and  $\Psi_2$  is 0
  - need a multiplet and its charge-conjugate
  - but cannot make non-vanishing Lorentz scalar of dim3 (  $ar{\psi}\psi=0$  )

- We are left with building blocks  $\varphi, \varphi, \Psi_1, \Psi_2$ 
  - Forming SU(2)<sub>W</sub> invariants:  $\varphi^{\mathsf{T}} \epsilon \varphi = 0 \Rightarrow \Psi_1, \Psi_2$  must be doublets (so we are left with I or q)
  - $| {}^{\mathsf{T}} \epsilon \phi$  and  $\phi {}^{\mathsf{T}} \epsilon |$  are SU(2)<sub>W</sub> and U(1)<sub>Y</sub> invariant
  - Connect them to make Lorentz scalar:

$$\hat{O}_{\text{dim}=5} = \ell^T C \epsilon \varphi \ \varphi^T \epsilon \ell$$

 $C = i\gamma_2\gamma_0$
• Could one replace I with q? No: invariance under  $SU(3)_c$  and  $U(1)_Y$ 

• Conclusion: there is only one dim=5 operator (Weinberg '79)

$$\hat{O}_{\text{dim}=5} = \ell^T C \epsilon \varphi \ \varphi^T \epsilon \ell \qquad C = i \gamma_2 \gamma_0$$

- it violates total lepton number  $( | \rightarrow e^{i\alpha} |, e \rightarrow e^{i\alpha} e)$
- it generates Majorana mass for L-handed neutrinos (after EWSB)

$$\frac{1}{\Lambda}\hat{O}_{\text{dim}=5} \qquad \xrightarrow{\langle\varphi\rangle = \begin{pmatrix} 0 \\ v \end{pmatrix}} \qquad \frac{v^2}{\Lambda}\nu_L^T C\nu_L$$

 light neutrino mass scale (≤ eV) points to high scale of lepton number breaking

$$m_{\nu} \sim 1 \,\mathrm{eV} \rightarrow \Lambda \sim 10^{13} \,\mathrm{GeV}$$

• Building blocks details: gauge fields

## $SU(3)_c \propto SU(2)_W \propto U(1)_Y$ representation

	gluons:	$G^A_\mu$ ,	$A=1\cdots 8,$	( <mark>8,   ,0</mark> )
_	-	$G^{A}_{\mu\nu} = \partial_{\mu}G^{A}_{\nu} - \partial_{\nu}G^{A}_{\mu} + g_{s}f_{ABC}G^{B}_{\mu}G^{C}_{\nu}$		
	W bosons:	$W^{I}_{\mu}$ ,	$V^I_{\mu}$ , $I=1\cdots 3$ ,	
		$W^{I}_{\mu\nu} = \partial_{\mu}W^{I}_{\nu} - \partial_{\nu}W^{I}_{\mu} + g\varepsilon_{IJK}W^{J}_{\mu}W^{K}_{\nu}$		
	B boson:	$B_{\mu}$ ,		
	$B_{\mu\nu} = \partial_{\mu}B_{\nu} - \partial_{\nu}B_{\mu} .$			(1,1,0)
Gauge transformation: $W^{I}_{\mu u}$			$\left[ W^{I}_{\mu\nu} \frac{\sigma^{I}}{2} \longrightarrow V(x) \left[ W^{I}_{\mu\nu} \frac{\sigma^{I}}{2} \right] V^{\dagger}(x) \right]$	
			$V(x) = e^{ig\beta_a(x)\frac{\sigma_a}{2}}$	

## The case for $\delta \tau_n \sim 0.3s$

• Key ingredient for  $V_{ud}$  @ 0.02%, free of nucl. structure ( $\rightarrow \Delta_{CKM}$  test)

•  $V_{ud}(n)$  and  $V_{ud}(0^+ \rightarrow 0^+)$  sensitive to different new physics!

$$\frac{\bar{V}_{ud}|_n}{\bar{V}_{ud}|_{0^+}} = 1 + c_S \epsilon_S + c_T \epsilon_T$$

$$c_{S}, c_T \sim O(1)$$

- Remove largest error in the prediction of primordial <sup>4</sup>He abundance
  - Observations may reach this level in the next decade



## Definition of D and R

$$\frac{d^3 \Gamma}{dE_e d\Omega_e d\Omega_v} = \frac{1}{(2\pi)^5} p_e E_e (E_0 - E_e)^2 \xi \left\{ 1 + b \frac{m_e}{E_e} + a \frac{\vec{p}_e \cdot \vec{p}_v}{E_e E_v} + \left\{ \frac{\vec{J}}{J} \right\} \cdot \left[ A \frac{\vec{p}_e}{E_e} + B \frac{\vec{p}_v}{E_v} + D \frac{\vec{p}_e \times \vec{p}_v}{E_e E_v} \right] + \cdots \right\}$$

$$\begin{split} &\omega(\langle \mathbf{J} \rangle, \sigma | E_e, \Omega_e) dE_e d\Omega_e = \\ & \frac{F(\pm Z, E_e)}{(2\pi)^4} p_e E_e (E_0 - E_e)^2 dE_e d\Omega_e \times \\ & \xi \left\{ 1 + b \frac{m}{E_e} + \frac{\mathbf{p}_e}{E_e} \cdot \left( A \frac{\langle \mathbf{J} \rangle}{J} + G \sigma \right) + \sigma \cdot \left[ N \frac{\langle \mathbf{J} \rangle}{J} \right. \\ & \left. + Q \frac{\mathbf{p}_e}{E_e + m} \left( \frac{\langle \mathbf{J} \rangle}{J} \cdot \frac{\mathbf{p}_e}{E_e} \right) + R \frac{\langle \mathbf{J} \rangle}{J} \times \frac{\mathbf{p}_e}{E_e} \right] \right\} \end{split}$$

$$D_{\text{BSM}} = \frac{1}{1+3\lambda^2} \left[ 4\lambda \operatorname{Im}(\epsilon_R) + 8g_S g_T \operatorname{Im}\left(\epsilon_S \epsilon_T^* + \tilde{\epsilon}_S \tilde{\epsilon}_T^*\right) \right]$$

$$R_n = \frac{1}{1+3\lambda^2} \left[ -8g_T \left( 2\lambda + 1 \right) \operatorname{Im}(\epsilon_T) - 2g_S \lambda \operatorname{Im}(\epsilon_S) \right] \qquad \qquad R_{B_{\text{Li}}} = -\frac{1}{3} \frac{8g_T}{g_A} \operatorname{Im}(\epsilon_T)$$