Low-Energy Nuclear Experiments Lecture 2: Ground States and Excitation Spectra

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## The (Second) Plan

- Other ground-state properties
  - Magnetic dipole moments and electric quadrupole moments
- Trends in excitation spectra
  - Collective vs. single-particle
  - Vibration, rotation, ...
- Nuclear decay measurements and more
  - Gamma-decay
  - Beta-decay
  - Alpha-decay



## Other Ground State Properties



# Other Ground State Properties Radii and moments



### Nuclear radii and nuclear shapes

A fundamental property of the ground state is the shape and size of the nucleus – the nuclear radius provides insight into nuclear extent (matter and charge).





The nuclear shape can deviate from spherical, but usually maintains symmetry with quadrupole deformation.



### Nuclear radii definitions

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$$\langle \boldsymbol{r_c^2} \rangle = \frac{\int_{0}^{R} \rho(\boldsymbol{r}) \boldsymbol{r}^2 \, d\boldsymbol{r}}{\int_{0}^{R} \rho(\boldsymbol{r}) \, d\boldsymbol{r}}$$

(m)

Consider RMS radii (matter and neutron)

Nuclear quadrupole deformation

$$R = R_0 \left[ 1 + \sum_{\mu = -2}^2 a_{2\mu} Y_{2\mu}(\theta, \phi) \right]$$

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VOLUME 30, NUMBER 2

Near stability we know:  $R = r_0 A^{1/3}$ 



### Matter radii: total interaction cross-sections

Be beam production target

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### Skins and halos





### Laser spectroscopy for radii --> isotope shifts





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The finite size and mass of the atomic nucleus has a distinct influence on the optical spectrum, which can be probed with high precision using laser spectroscopy.

R.F. Garcia Ruiz *et al.*, arXiv:1504.04474v1

http://www.euroschoolonexoticbeams.be/site/files/nlp/LNP879\_Chapter6.pdf



### Ground state nuclear moments



### Magnetic moments

$$\mu = \int \psi_{J,M}^{*}(\vec{\mu})_{z}\psi_{J,M}$$
$$\vec{\mu} = \sum_{k=1}^{A} g_{L}^{(k)}\vec{L}^{(k)} + \sum_{k=1}^{A} g_{S}^{(k)}\vec{S}^{(k)},$$
$$\mu_{s.p.} = j \left[ g_{l} \pm \frac{g_{s} - g_{l}}{2l + 1} \right] \text{ for } j = l \pm \frac{1}{2}$$





### Physics in magnetic moments



 g-factors are sensitive to proton/neutron contributions to nuclear states – where collective properties may vary smoothly, proton and neutron contributions can vary substantially

G. J. Kumbartzki et al., Phys. Rev. C 85, 044322 (2012).





### Hyperfine structure

Hyperfine structure refers to the splitting of a single electronic level for nuclei with I > 0

$$\Delta E_{mag} = \left| \boldsymbol{g}_{I} \right| \cdot \boldsymbol{\mu}_{N} \cdot \boldsymbol{B} + \frac{1}{2} \boldsymbol{Q} \cdot \boldsymbol{V}_{zz}$$

**Derived properties of nuclei:** - Spin (orbital+intrinsic angular momentum), parity ( $I^{\pi}$ ) - Nuclear **g-factor** and magnetic dipole moment ( $g_I$  and  $\mu_I$ ) - Electric quadrupole moment (Q) -Charge radius (  $\langle r^2 \rangle$  )

Give information on: - Configuration of neutrons and protons in nucleus - Size and form of nucleus





### β-NMR/NQR technique

#### Beta-Nuclear Magnetic Resonance:

Use decay (β-/β+) as a detection tool; asymmetric emission for spin-polarized nuclei

Measured decay asymmetry:

 $A = \frac{N(0^{\circ}) - N(180^{\circ})}{N(0^{\circ}) + N(180^{\circ})}$ 





### Laser polarization

One method to achieve nuclear polarization is using lasers to create atomic polarization, which then couples to the nucleus.



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Facilities around the world (i.e. TRIUMF) have or are commissioning laser systems to expand their experimental capabilities.

### $\beta$ -NQR of <sup>11</sup>Li at TRIUMF



www.triumf.ca/laser-spectroscopy/β-nqr-lithium-isotopes



## **Excitation Spectra**



### Level schemes – collective vs. single particle

### Level Schemes Contain Structural Information





4811

4403

408 keV

404 keV

#### Single particle excitations

Within a independent particle model, a subset of nuclear excitations correspond to different configurations of protons and neutrons



p<sub>3/2</sub>

 $f_{7/2}$ 

d<sub>3/2</sub>

 $S_{1/2}$ 

d<sub>5/2</sub>

28

8

Neutrons



 Within a independent particle model, a subset of nuclear excitations correspond to different configurations of protons and neutrons

d<sub>3/2</sub>

۶<sub>1/2</sub>

d<sub>5/2</sub>

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Protons

8

(e)

2014 keV







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June 15 – 25, 2015

#### **Collective excitations**

- Many nucleons outside a closed shell contribute coherently to excitations
- Vibrations and rotations (for nonspherical nuclei) have excitation energies comparable to single-particle energy excitations

The nucleus can quiver, ring or even "breathe"; the coordinated motion of the nuclear particles reveals much about the forces between them. Six modes of vibration have been detected so far





### Nuclear vibration

Treat nuclear vibrations as time-dependent deformation

$$R(\theta,\phi) = R_0 \left( 1 + \sum_{\lambda=0}^{\infty} \sum_{\mu=-\lambda}^{\lambda} \alpha_{\lambda\mu}^* Y_{\lambda\mu}(\theta,\phi) \right)$$
$$H_{\text{vib}} = \frac{1}{2} \sum_{\lambda\mu} \left( B_\lambda |\dot{\alpha}_{\lambda\mu}|^2 + C_\lambda |\alpha_{\lambda\mu}|^2 \right)$$



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- Give rise to characteristic excitation spectra – vibration phonons couple as angular momenta
  - i.e. Quadrupole vibrations



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### Nuclear rotation



Deformed nuclei can also undergo collective rotational motion; nuclear rotation is parameterized in the same way as classical rotors



From A. Bohr and B. R. Mottelson. *Nuclear structure*, volume 2

$$E_{rot}(J) = \hbar^2/2I \times J(J+1)$$
  
I = Moment of inertia



### Deformation and the Nilsson model



- Nuclear rotation is a collective excitation, but interfaces to single-particle structure
- Nilsson model is a shell-model description in a deformed basis, which provides a good description in well-deformed nuclei

### Moment of inertia in nuclei



- Rigid body
  estimate for the
  moment of inertia
  is consistently
  larger than
  experimental data
- Irrotational flow value (like a liquid drop...) is too small
- Data puts the nuclear moment of inertia between these two limits; moment of inertia dynamic



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### Excitations in the real world

Nuclei are not limited to a single type of excitation – vibration, rotation and single-particle configurations all coexist at similar excitation energies.

States near in energy with the same spin interact and interfere – nuclear wavefunctions are complex superpositions of 'pure'





### Simple patterns still tell us about structure





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## $R_{4/2}$ – A powerful ratio





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### Question!

- In <sup>42</sup>Si, a gamma-ray from 2+ to 0+ is observed at 742 keV, and a gamma-ray from the 4+ state to the 2+ state is observed at 2032 keV. What can we say about the excitation?
  - (A) Nothing
  - (B) It's pretty rotational deformed
  - (C) It seems vibrational
  - (D) It's unbound





### Question!

- In <sup>42</sup>Si, a gamma-ray from 2+ to 0+ is observed at 742 keV, and a gamma-ray from the 4+ state to the 2+ state is observed at 1431 keV. What can we say about the excitation?
  - (A) Nothing
  - (B) It's pretty rotational *deformed*
  - (C) It seems vibrational
  - (D) It's unbound

E(4+)/E(2+) = (1431 + 742)keV / 742 keV = 2.9

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## Studying Level Schemes



## Studying Level Schemes Nuclear Decay



### Nuclear ground-state decay

Nuclei decay toward stability (and a lower energy state) via one of four basic decay modes:

- Alpha decay ( --> Z-2, N-2)
- Beta(-) decay ( --> Z+1, N-1)
- Beta(+) decay ( --> Z-1, N+1)
- Fission (--> 2 fragments + n)
- 1p & 2p radioactivity



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### Decay observables

- Nuclear decay measurements allow access to a number of observables
  - Half-life information for decaying state
  - Energies for emitted particles (spectroscopic information in daughter nucleus)
  - Gamma-rays de-exciting daughter states populated in decay
    - Excited state spins and parities based on selection rules for primary decay and subsequent gamma decay


## **Decay half-lives**

All radioactive decay modes obeys Poisson statistics and are described by straight-forward differential equations.



$$A = -dN/dt = \lambda N$$

$$t_{1/2} = \ln(2) / \lambda$$



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### Nuclear excited state decay

- Excited states in nuclei can decay in a number of ways:
  - $β^+$ ,  $β^-$ , electron capture (EC) -- <sup>177</sup>Lu<sup>m</sup>
  - Particle emission -- <sup>53</sup>Co<sup>m</sup>, <sup>211</sup>Po<sup>m</sup>
  - Fission <sup>239</sup>Pu<sup>m</sup>
  - Internal conversion
  - Gamma-ray emission



### **Dominant Excited State Decay**

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Nuclear properties from gamma-ray studies

- Coincidence relation --> Level schemes
- Angular distribution/correlation --> Multipolarity, spin
- Doppler shifts --> excited state lifetimes
- Linear polarization --> E/M, parity
- Intensity of transitions --> B(E2)











The transition probability for at state decaying by transition of multipole order L is:

$$T_{fi}(\lambda L) = \frac{8\pi (L+1)}{\hbar L ((2L+1)!!)^2} \left(\frac{E_{\gamma}}{\hbar c}\right)^{2L+1} B(\lambda L: J_i \to J_f)$$





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*Reduced matrix element* – i.e.

$$B(E2: J_i \to J_f) = \frac{1}{2J_i + 1} \langle \psi_f || E2 || \psi_i \rangle^2$$







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The transition probability for at state decaying by transition of multipole order L is:

$$\begin{split} T_{fi}(\lambda L) &= \frac{8\pi (L+1)}{\hbar L ((2L+1)!!)^2} \left(\frac{E_{\gamma}}{\hbar c}\right)^{2L+1} B(\lambda L:J_i \to J_f) \\ & \text{Reduced matrix element-i.e.} \\ & \text{Weisskopf estimates} \\ B(E2:J_i \to J_f) &= \frac{1}{2J_i+1} \langle \psi_f || E2 || \psi_i \rangle^2 \\ T(E1) &= 1.03 \times 10^{24} A^{2/3} E_{\gamma}^3 \\ T(E2) &= 7.28 \times 10^7 A^{4/3} E_{\gamma}^5 \\ & \text{T}(M1) = 3.15 \times 10^{13} E_{\gamma}^3 \\ & \text{T}(M2) = 2.24 \times 10^7 A^{4/3} E_{\gamma}^5 \end{split}$$

...



- The bulk of electromagnetic (gamma) transitions have lifetimes of 10<sup>-15</sup> – 10<sup>-13</sup> s
  - Explains why excited states primarily undergo gamma decay (compare to beta-decay lifetimes » ms, or alpha decay » s)



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- Occasionally longer lifetimes are observed, i.e. ns or longer --> Isomerism
  - Isomers arise for many reasons



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## Question!

- What would you expect to be the dominant character of the gamma-ray transition linking the second 0<sup>+</sup> excited state at 1.06 MeV in <sup>32</sup>Mg with the ground state (0<sup>+</sup>)?
   (A) E1
  - (B) M2
  - (C) No gamma transition(D) M1



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   (A) E1
  - (B) M2
    (C) No gamma transition
    (D) M1

 Gamma rays must carry at least one ~ of angular momentum – cannot link two 0+ states
 When gamma transition is not possible, internal conversion is an alternative electromagnetic transition.



• Energies --> spacing between nuclear levels



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- Lifetimes --> information about transition probabilities, links to nuclear matrix elements (structure!)



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Knowledge of J<sub>i</sub> and J<sub>f</sub> limit the multipolarity (L) of gamma-ray transitions



- Energies --> spacing between nuclear levels
- Lifetimes --> information about transition probabilities, links to nuclear matrix elements (structure!)
- Intensities --> experiment dependent generally relates to transition probabilities (branching ratios)

- Knowledge of J<sub>i</sub> and J<sub>f</sub> limit the multipolarity (L) of gamma-ray transitions
- To measure multipole order (L) we can measure angular distributions
- To determine E vs. M we need to measure polarization of the transition



## Gamma-Ray Angular Distributions

 Angular distribution of a gamma-ray depends on the values of m<sub>i</sub> and m<sub>f</sub>





## Gamma-Ray Angular Distributions

- Angular distribution of a gamma-ray depends on the values of  $m_{\rm i}$  and  $m_{\rm f}$ 





## Gamma-Ray Angular Distributions

If we produce unequal populations p(m<sub>i</sub>) angular distributions
 W(θ) will be non-constant

#### Nuclear Orientation





## Gamma-Ray Angular Correlations

Observation of a previous radiation selects an unequal mixture of populations p(m<sub>i</sub>)





- First gamma defines z-axis --  $\theta_1 = 0$ 
  - p(m<sub>m</sub>) = 0 for m<sub>m</sub> = 0
- Distribution of  $\gamma_2$  relative to  $\gamma_1$  is

• 
$$W(\theta) -> 1 + \cos^2 \theta$$





## Back to $\beta$ decay...

- The majority of nuclides on the chart decay via  $\beta^+$  or  $\beta^-$  decay
  - $\circ \quad n \dashrightarrow p + \beta^{-} + v_{e}$
  - $\circ \quad p \dashrightarrow n + \beta^+ + \overline{\nu}_e$
- We can consider β-decay (and other decays) as a tool to populate excited states in daughter nuclei, but with a unique selectivity



Forbiddenness	$\Delta J$	Δπ
Superallowed	$0^+ \rightarrow 0^+$	no
Allowed	0, 1	no
First forbidden	0, 1, 2	yes
Second forbidden	1, 2, 3	no
Third forbidden	2, 3, 4	yes

# β-decay half-lives

 even with the most limited statistics, half-lives can be extracted

 the equations of exponential decay are well known and can be applied using statistical techniques such as maximum likelihood to obtain half-lives from tens of observed decays



D. Bazin et al., PRL 101, 252501 (2008).F. Bosch et al., Int. J. Mass Spectr. 251, 212 (2006).

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# Implantation β decay spectroscopy

#### β-Delayed Gamma Spectroscopy



 gamma rays following decay events provide information on lowlevel structure of daughter nuclei

#### **Isomeric Decay**

 depending on the production mechanism, nuclei may be produced in long-lived excited states (isomeric states)

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• a TAC for implantation-gamma provides the possibility for isomer lifetime determination, if you look for gammas following an implantation



## Implant-decay correlation technique



The use of highly-segmented detectors (usually Si) allows temporal and spatial correlations between implanted nuclei, and their subsequent decays → detect the implant and the decay to obtain half-lives and information on levels in the daughter relative to the parent ground state





## <u>β-decay</u> spectroscopy set-up: NSCL



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# β-decay spectroscopy: complex example

A. Look at the gamma-rays in coincidence with the nucleus of interest (<sup>56</sup>Sc) implantations – by fitting half-lives of the isomer, and through gammagamma correlations, build up a level scheme, and can get relative spinparities for the states in <sup>56</sup>Sc



HLC et al., PRC 82, 014311 (2010).



## β-decay spectroscopy: complex example





# β-decay spectroscopy: complex example



D. Gate on implantations that came in coincidence with isomer gamma-rays and look at half-life  $\rightarrow$ determine which state the isomer populates, and fix the spin/parity



= 30 ms

## Alpha decay

- α decay occurs only in heavier systems on the nuclear chart
- Alpha decay however probes different aspects of the nuclear forces



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 Different selectivity in the process --> favour low L alpha emission

## Alpha decay – heavy element structure



Yu. Ts. Oganessian et al., PRL 104, 142502 (2010).



The heaviest nuclei decay via emission of 'heavy' particles – alpha decay – or by spontaneous fission

Since alphas and fission products are relatively easy to detect, even a single nucleus can provide significant information

Decay properties of element 117 alone, from only 6 events, provide experimental evidence supporting enhanced stability beyond Z = 111
## The heaviest nuclei – patience required!



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Experiment ran for 70 days, <sup>48</sup>Ca at 7 x 10<sup>12</sup> ions/second on <sup>249</sup>Bk → 5 observed decay chains for <sup>293</sup>117 and 1 for <sup>294</sup>117, corresponding to cross-sections of 0.5pb and 1.1pb





# Spectroscopy of heavy elements



#### Spectroscopy from element 115





#### Proton dripline





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## Proton decay



Even when the Q value for proton removal becomes positive, proton emission is hindered due to the Coulomb (and centrifugal) barriers --> radioactivity





### 2p decay





## Summary

- Nuclear excitation spectra (energies, spins and parities of excited states) are fundamental experimental observables
- Patterns of excitation provide insight into symmetries and collective properties of nucleus
  - Vibrational spectra
  - Rotational spectra
  - Single-particle excitations
- Nuclear decay provides access to excitation spectra, as well as fundamental observable such as half-life

