

# Low-Energy Nuclear Experiments

## Lecture 1: The Basics

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# The Plan

- Some basics
  - Energy scales etc.
  - Nuclear landscape and how we get there
  - ABC's of nuclear structure – nuclear shell model
- Nuclear binding and masses
  - Mass measurements
  - Cross-sections and the most exotic systems

# Why study nuclear structure?

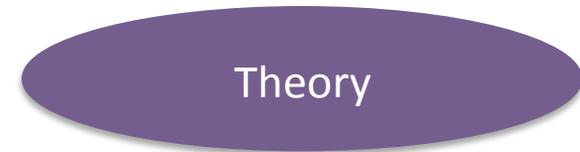
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**Goal:** Establish the physical properties of exotic nuclei and their interactions (reactions) to constrain theory and improve predictive power

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## Physical properties

Mass, decay lifetime, production cross-section, electric and magnetic moments, excited state properties (moments, energies, lifetimes), etc...

*Note --> the observables in an experiment may or may not require interpretation to relate to physical properties*

# Observables

Ultimately, we would like to understand the wavefunction of nuclear states. But these are **not** observable quantities.

## Observables:

Half-life, mass, decay modes, electric/magnetic moments, cross-sections, momentum distributions, transition probabilities, ....

# Challenges for radioactive nuclei

The observables we're interested in for stable nuclei are the same ones we're interested in for exotic systems.

Most techniques translate as well...but radioactive nuclei add some experimental challenges.

## Biggest challenges:

Half-life --> how do you study an isotope that lives for a fraction of a second (ms timescale for beta-unstable nuclei)

Production --> how do you study nuclei you only see once a week, or less?

# Scales: Energy and size

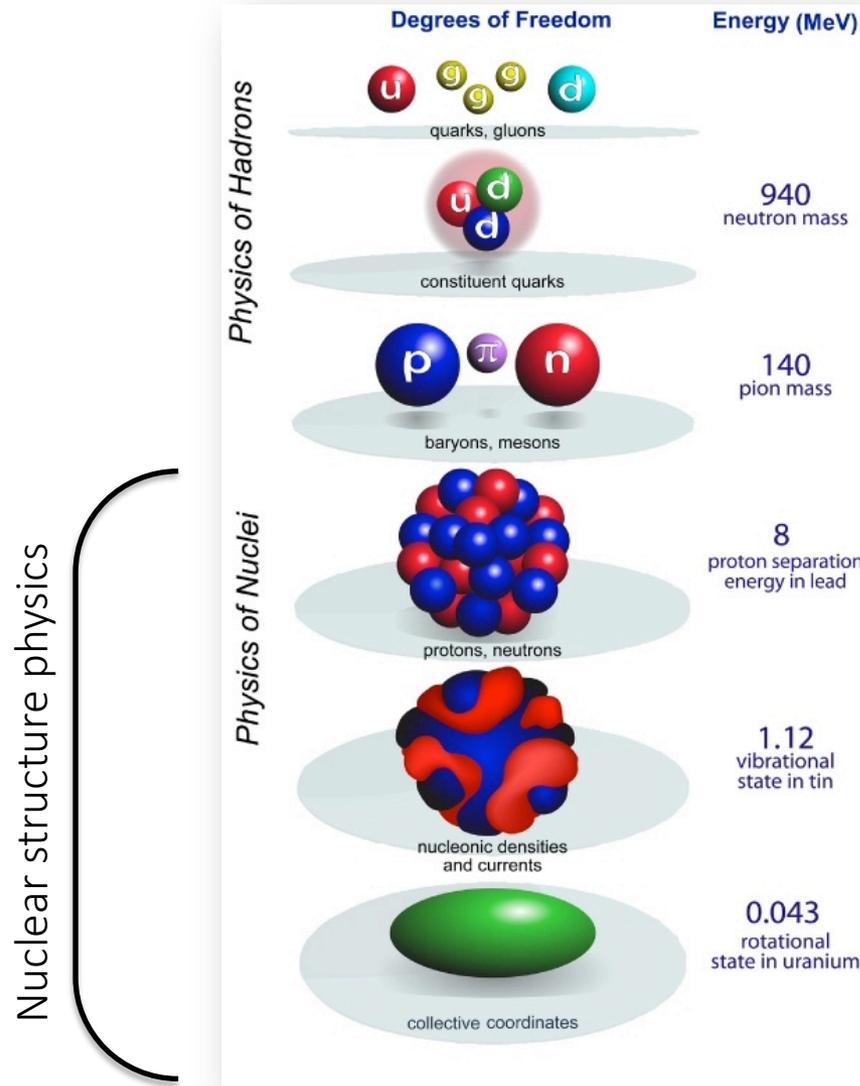
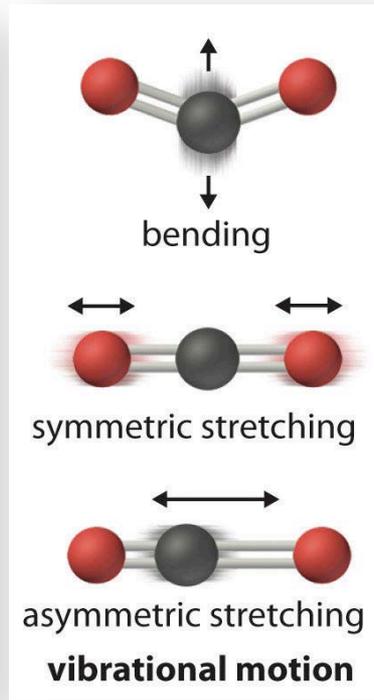
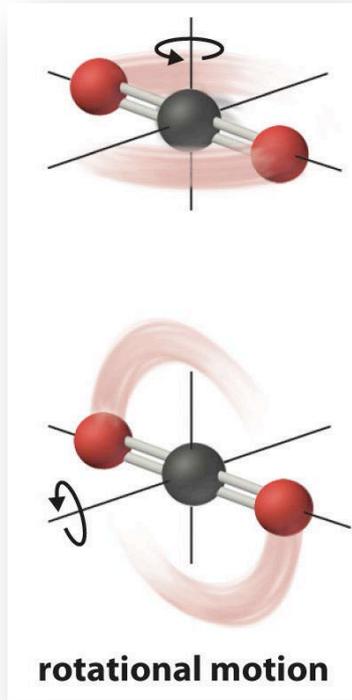
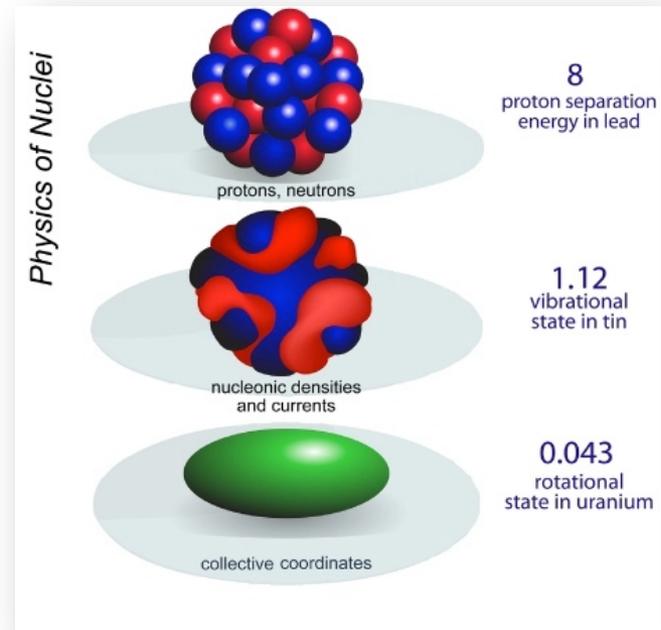


Figure: R J Furnstahl and K Hebeler 2013 Rep. Prog. Phys. 76 126301 doi:10.1088/0034-4885/76/12/126301

# Scales: Energy and size



Nuclear structure physics



Molecular excitations:

- $E_{\text{rot}} \ll E_{\text{vib}} \ll E_{\text{electric}}$   
( $\mu\text{eV} \ll \text{meV} \ll \text{eV}$ )

Molecular excitations are separable –  
wavefunctions can be treated as product of terms

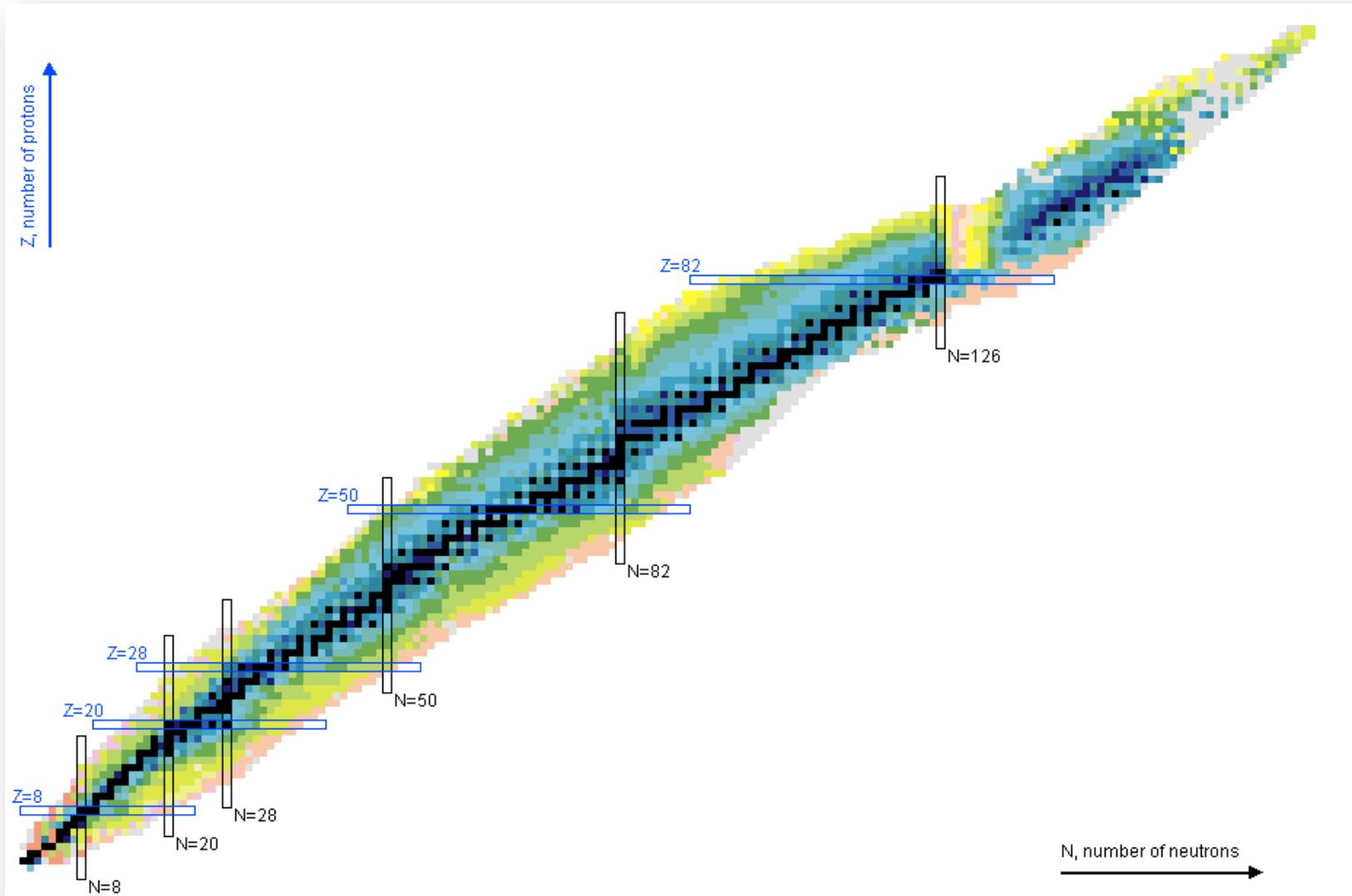
Nuclear excitations:

- $E_{\text{rot}} \sim E_{\text{vib}} \sim E_{\text{electric}}$   
(all MeV)

Collective and single-particle excitations  
are all of a similar energy scale and  
interact

Figure: R J Furnstahl and K Hebeler 2013 Rep. Prog. Phys. 76 126301 doi:10.1088/0034-4885/76/12/126301

# Nuclear landscape



# Nuclear landscape basics

A given nucleus is a bound system of  $N$  neutrons and  $Z$  protons, with a total mass number  $A = N + Z$

Shorthand:  ${}^A_Z X_N$

Isotopes: same  $Z$ , but different  $N$

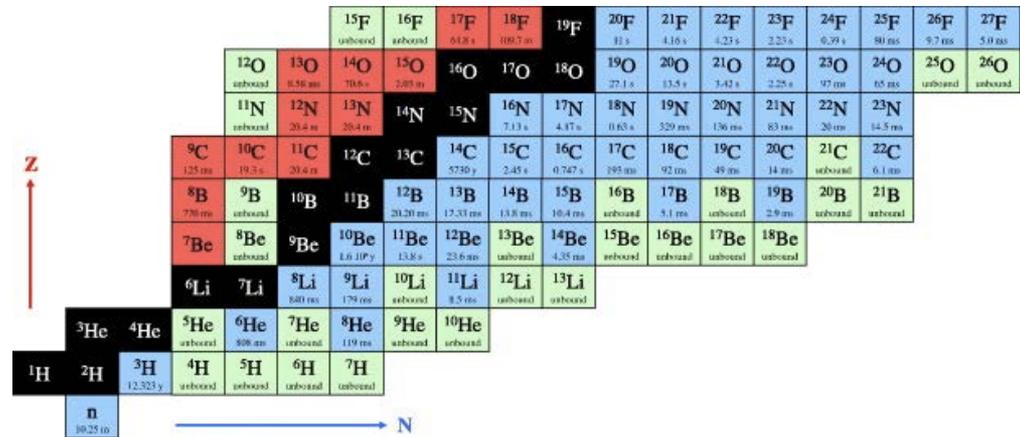
${}^9\text{C}$ ,  ${}^{10}\text{C}$ ,  ${}^{11}\text{C}$ ,  ${}^{12}\text{C}$ , ...

Isotones: Same  $N$ , but different  $Z$

${}^{12}\text{C}$ ,  ${}^{11}\text{B}$ ,  ${}^{10}\text{Be}$ ,  ${}^9\text{Li}$ ,  ${}^8\text{He}$ , ...

Isobars: Nuclei with the same mass number  $A$

${}^{12}\text{N}$ ,  ${}^{12}\text{C}$ ,  ${}^{12}\text{B}$ ,  ${}^{12}\text{Be}$ , ...



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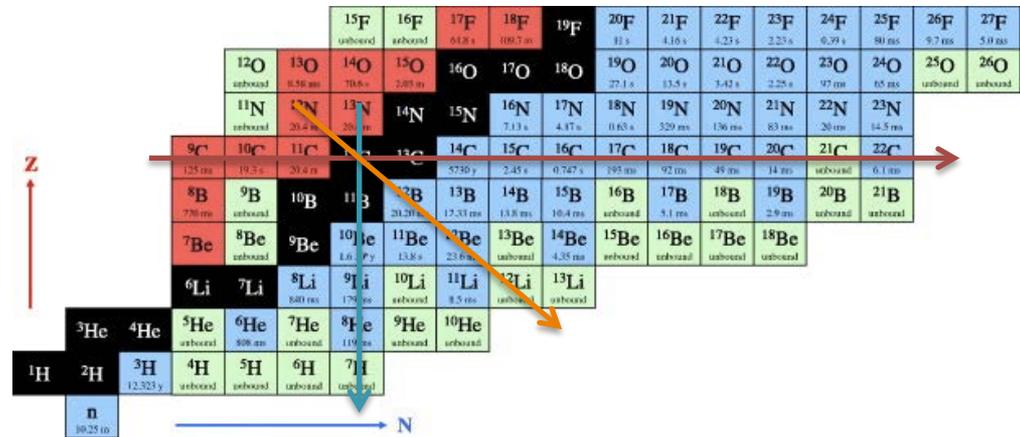
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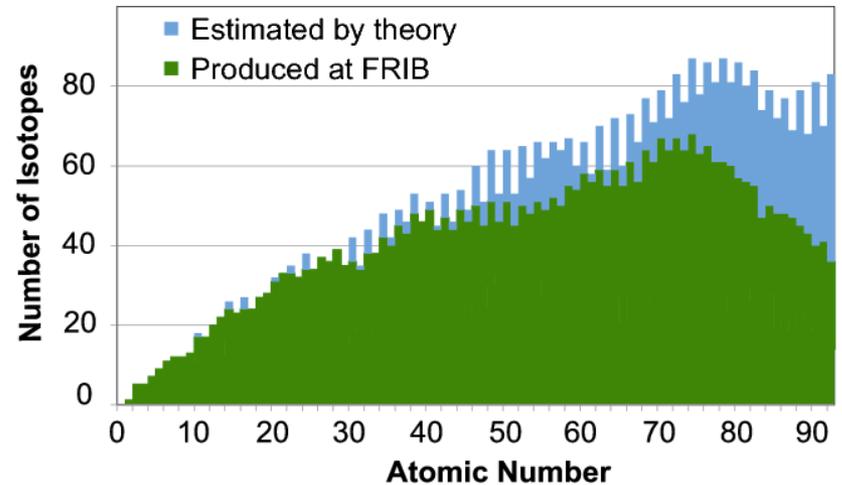
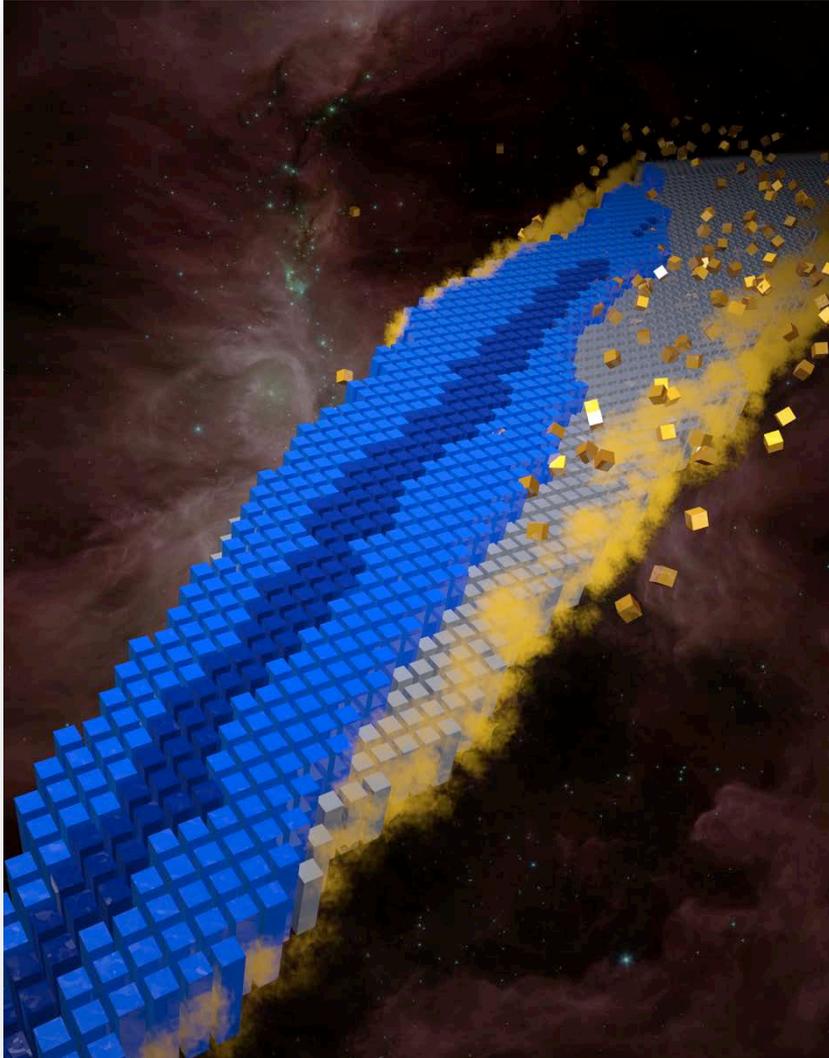
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Isobars: Nuclei with the same mass number  $A$

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# Nuclear landscape limits



- 254 stable isotopes have been observed;
- more than 3000 isotopes have been made in laboratories;
- as many as 6000-8000 are expected to possibly exist

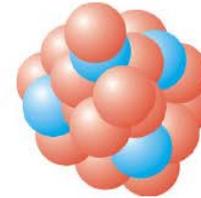
# “Exotic” nuclei

## Normal Nucleus:



6 neutrons  
6 protons (carbon)  
 $^{12}\text{C}$   
Stable, found in nature

## Exotic Nucleus:



16 neutrons  
6 protons (carbon)  
 $^{22}\text{C}$   
Radioactive, at the limit of  
nuclear binding

“Exotic” nuclei are those which will undergo radioactive decay towards a lower-energy system  
They are characterized by:

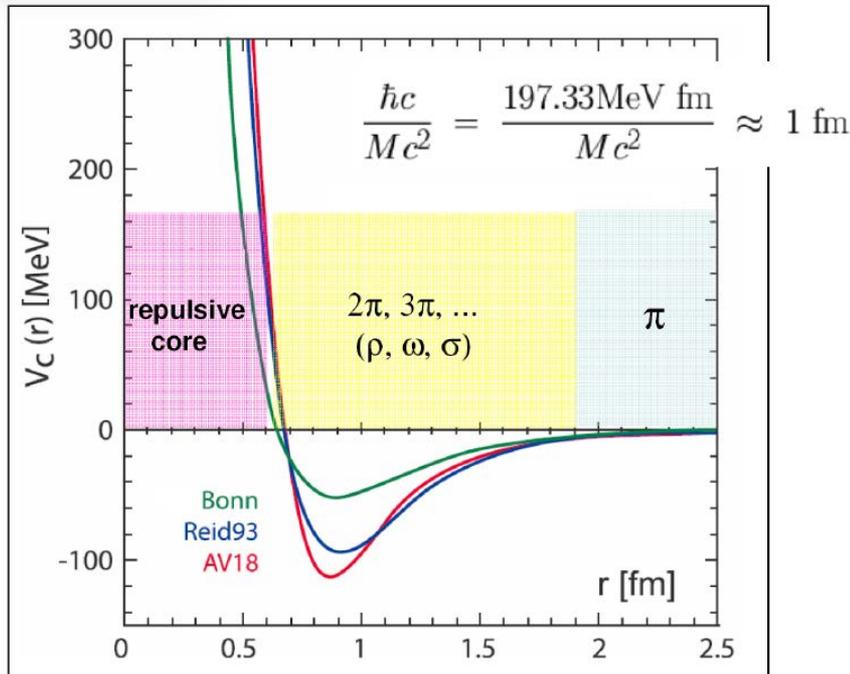
- excess of protons or neutrons
- short half-lives
- neutron/proton dominated surface
- low binding of nucleons

# What binds the nuclear system?



Protons and neutrons are bound together by the *strong* force

The strong (colour) force between quarks in one proton, and quarks in another proton is sufficient to overcome the electromagnetic repulsion



From T. Hatsuda (Oslo 2008)



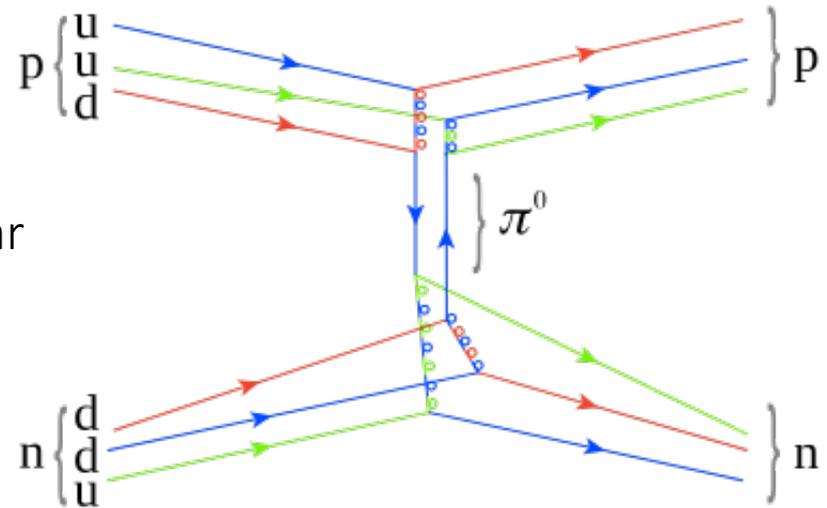
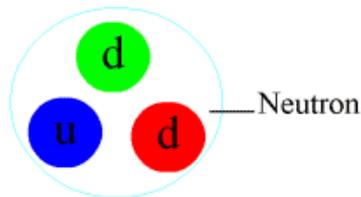
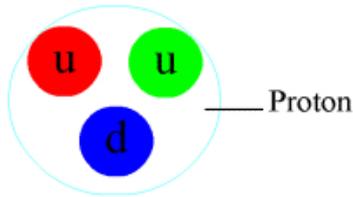
Consider the nuclear binding force as:

- a residual strong interaction, or
- the exchange of mesons

# Pion exchange model

Can interpret the nuclear strong force as an exchange force involving neutral pions,  $\pi^0$

Hideki Yukawa judged the range of the nuclear force to be about 1 fm, and calculated the range of the exchange particle to be of order  $100 \text{ MeV}/c^2$  – led to discovery of the pion



--> For a proton to interact with another proton, it must exchange something with it, but quarks are confined, thus exchange quark-antiquark pair (meson); lightest is pion, defining the upper range for the nuclear strong force

# Binding energy and mass

Mass  $M(N,Z)$  of neutral atom (of order GeV)

Mass excess:

$$\Delta(N,Z) = M(N,Z) - uA \text{ (of order MeV)}$$

$$\text{Atomic mass unit } u = M(^{12}\text{C})/12 = 931.5 \text{ MeV}/c^2$$

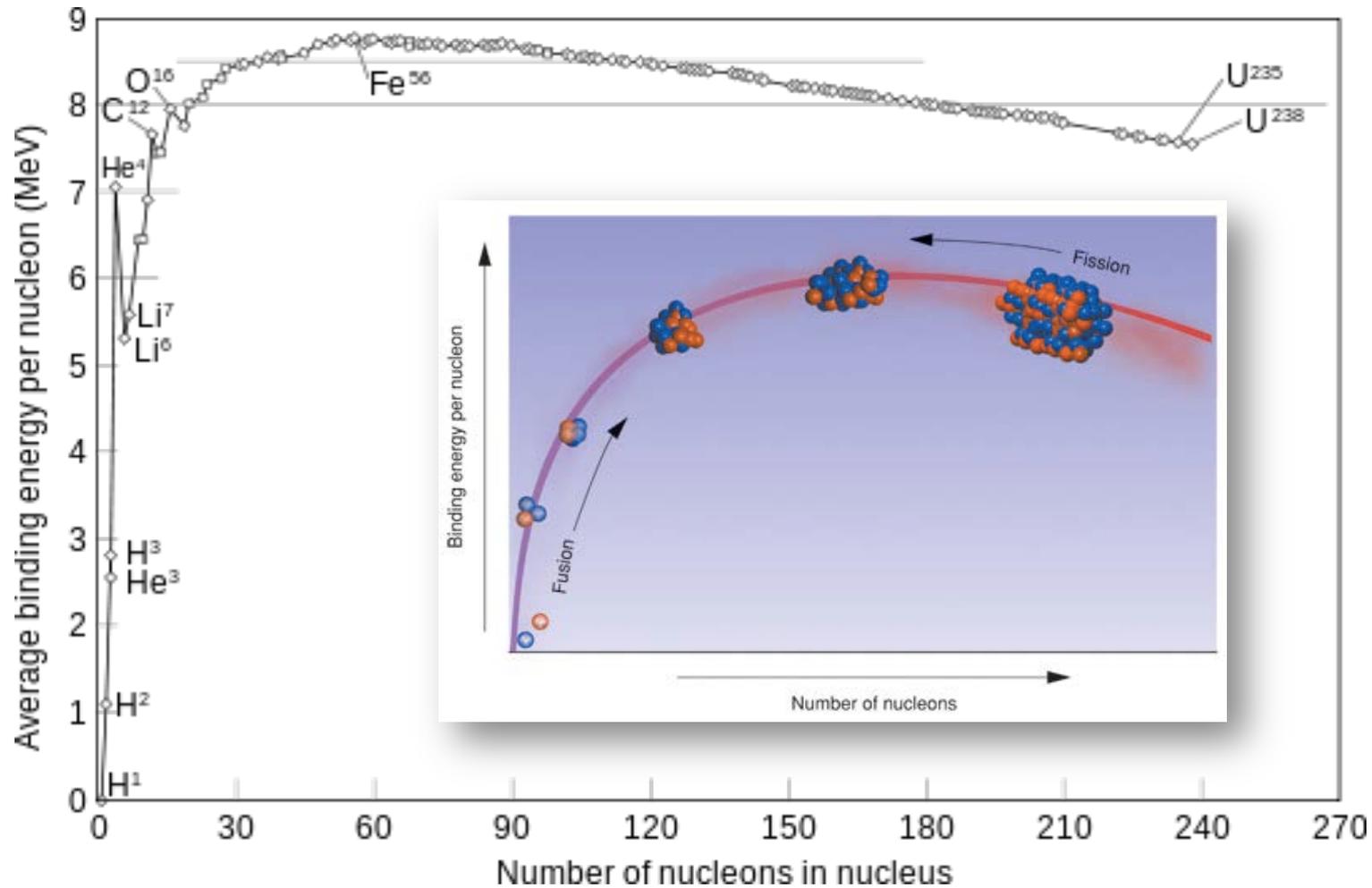
$$\rightarrow \Delta(^{12}\text{C}) = 0$$

Binding energy:

$$B(N,Z) = ZM_{\text{H}}c^2 + NM_{\text{n}}c^2 - M(N,Z)c^2$$

$$B(N,Z) = Z\Delta_{\text{H}}c^2 + N\Delta_{\text{n}}c^2 - \Delta(N,Z)c^2$$

# Binding of nuclei – Fission and fusion



# The liquid-drop model for nuclear binding

$$B(Z,A) = a_v A + a_s A^{2/3} + a_c Z^2/A^{1/3} + a_A (N-Z)^2/A - a_p/A^{1/2}$$

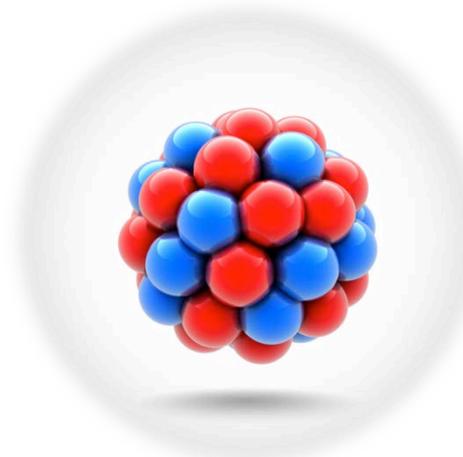
Volume term  
 $a_v = -15.68 \text{ MeV}$

Surface term  
 $a_s = 18.56 \text{ MeV}$

Coulomb term  
 $a_c = 0.717 \text{ MeV}$

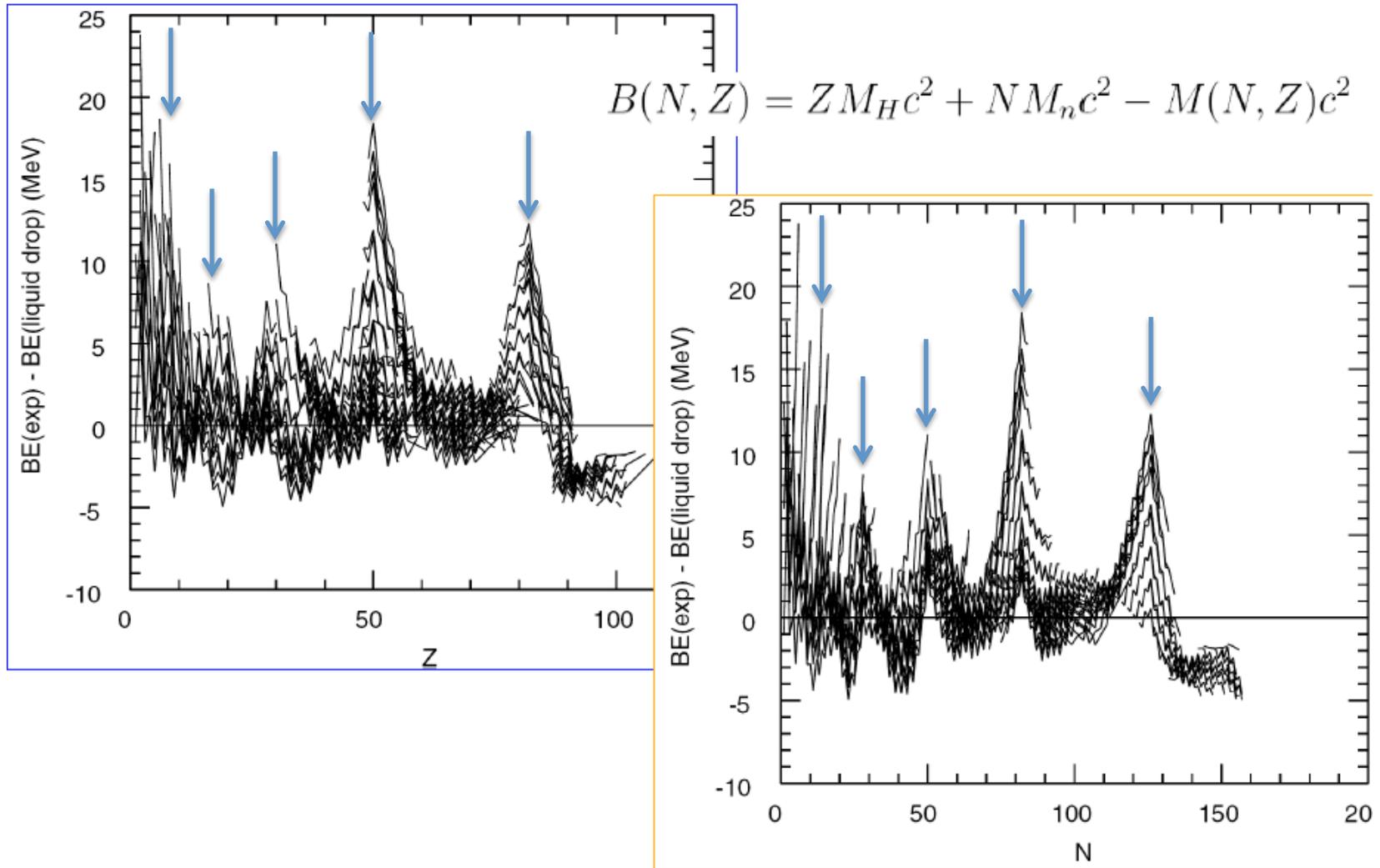
Asymmetry term  
 $a_A = 28.1 \text{ MeV}$

Pairing term  
 $a_p = 12.0 \text{ MeV}$   
(+) even-even  
(-) odd-odd  
(0) even-odd



$$R = r_0 A^{1/3}$$

# Semi-empirical mass vs. reality



# Nucleon separation energies

Ground state masses directly are large; changes in trends are obscured

More useful are differences in masses, the energy required to remove nucleons from a given system

$$S_{2n} = B(N,Z) - B(N-2,Z) = M(N-2,Z) + 2M_n - M(N,Z)$$

# Question!

- Why would mass evaluations produce plots of  $S_{2n}$  rather than  $S_n$ ?
  - (A) Removal of a single neutron is not allowed in any nuclear system
  - (B) Mass differences between even-N and odd-N systems are large
  - (C) Neutrons provide more information than protons for nuclear structure
  - (D)  $S_n$  is more difficult to calculate

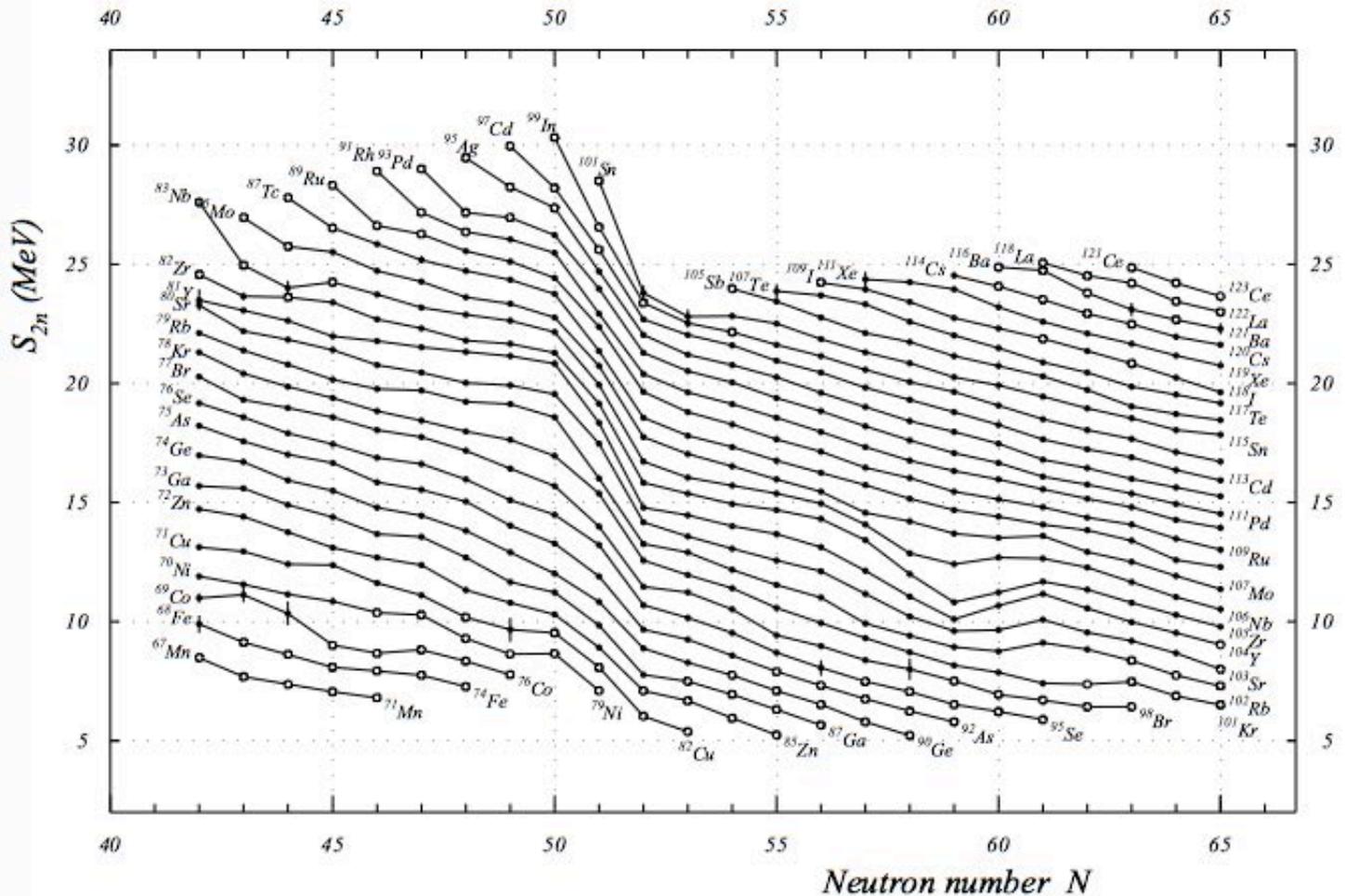


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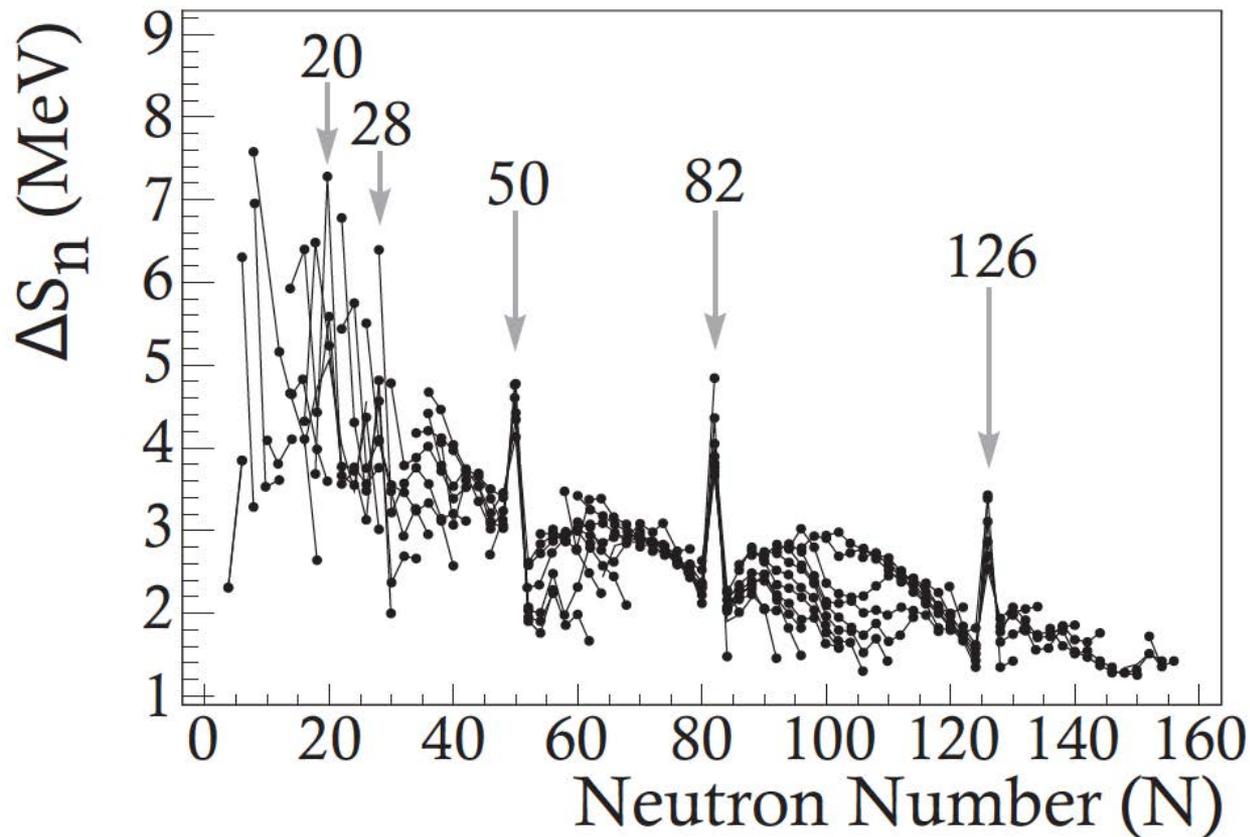


# Nucleon separation energies

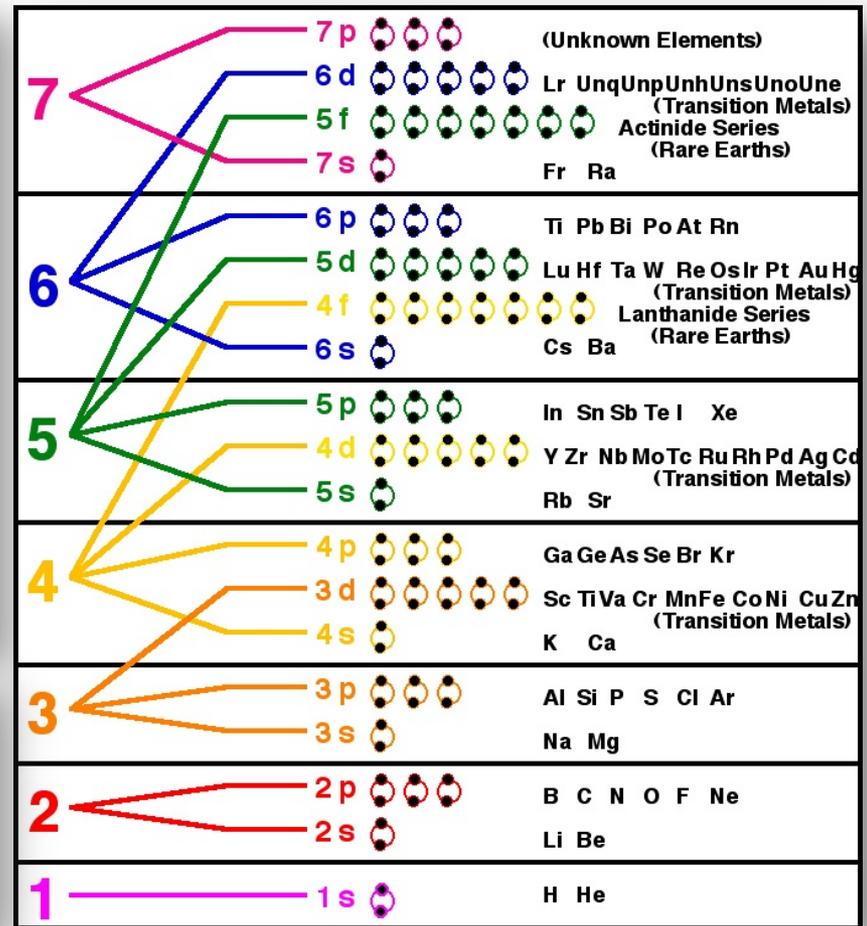
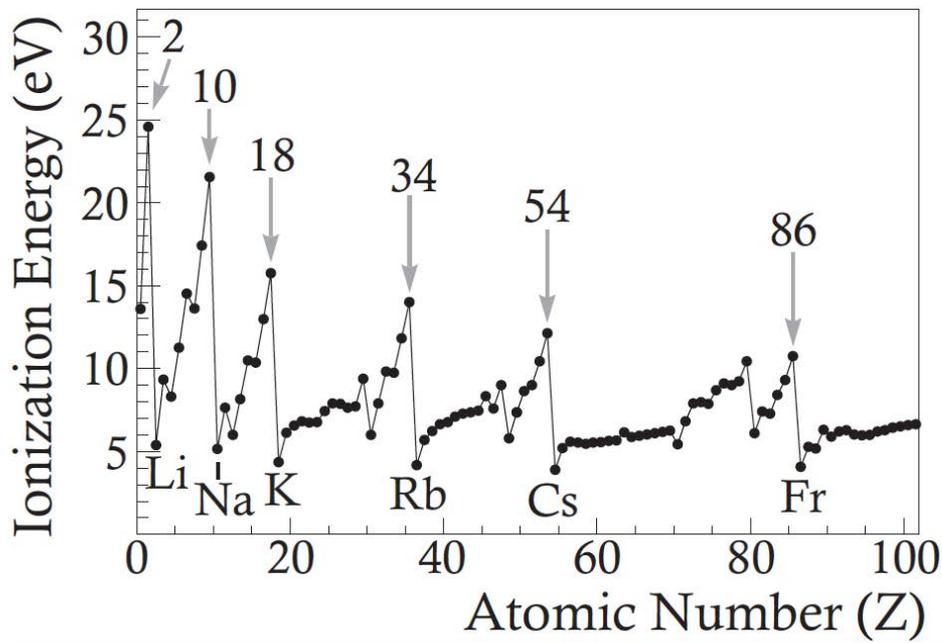


2012 AME Mass evaluation

# Nucleon separation energies



# Ionization energies in atoms...

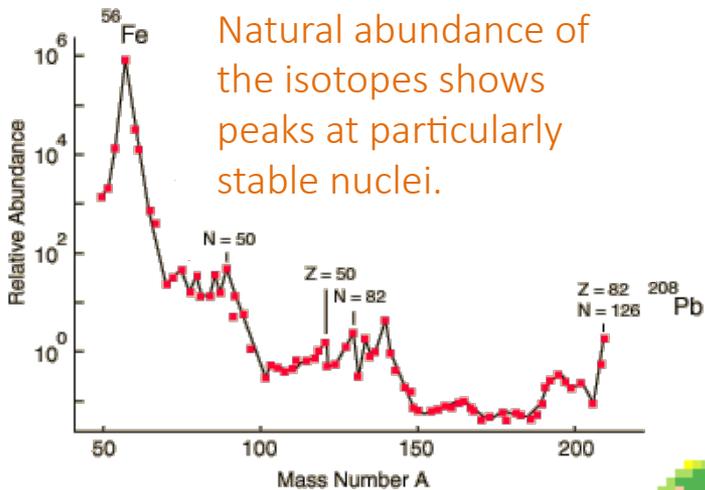


Hydrogen Emission Spectrum

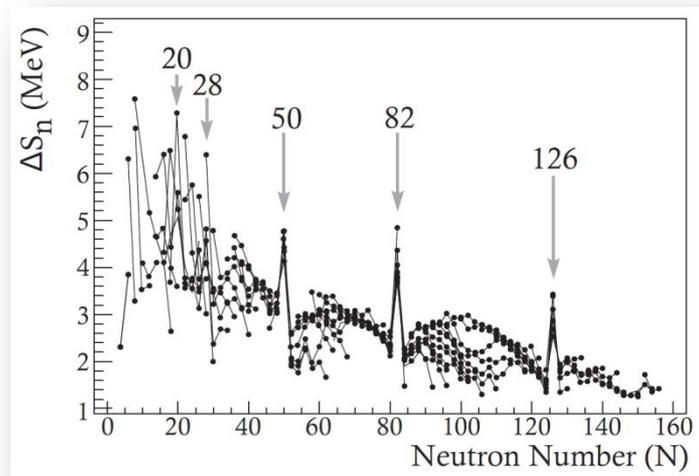
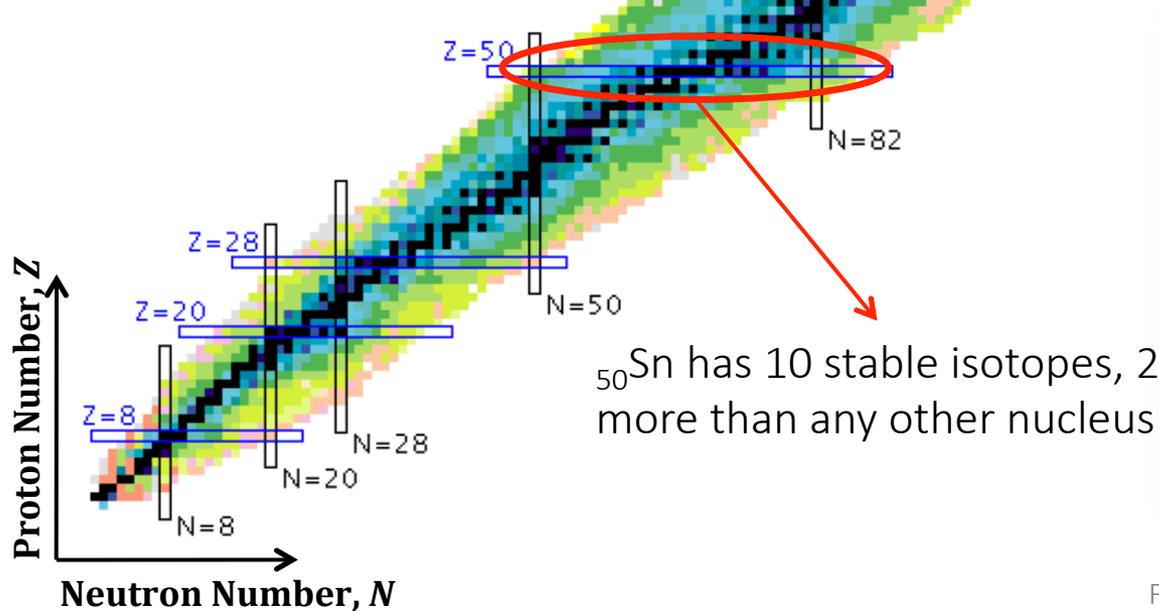


# Nuclear magic numbers

Natural abundance of the isotopes shows peaks at particularly stable nuclei.

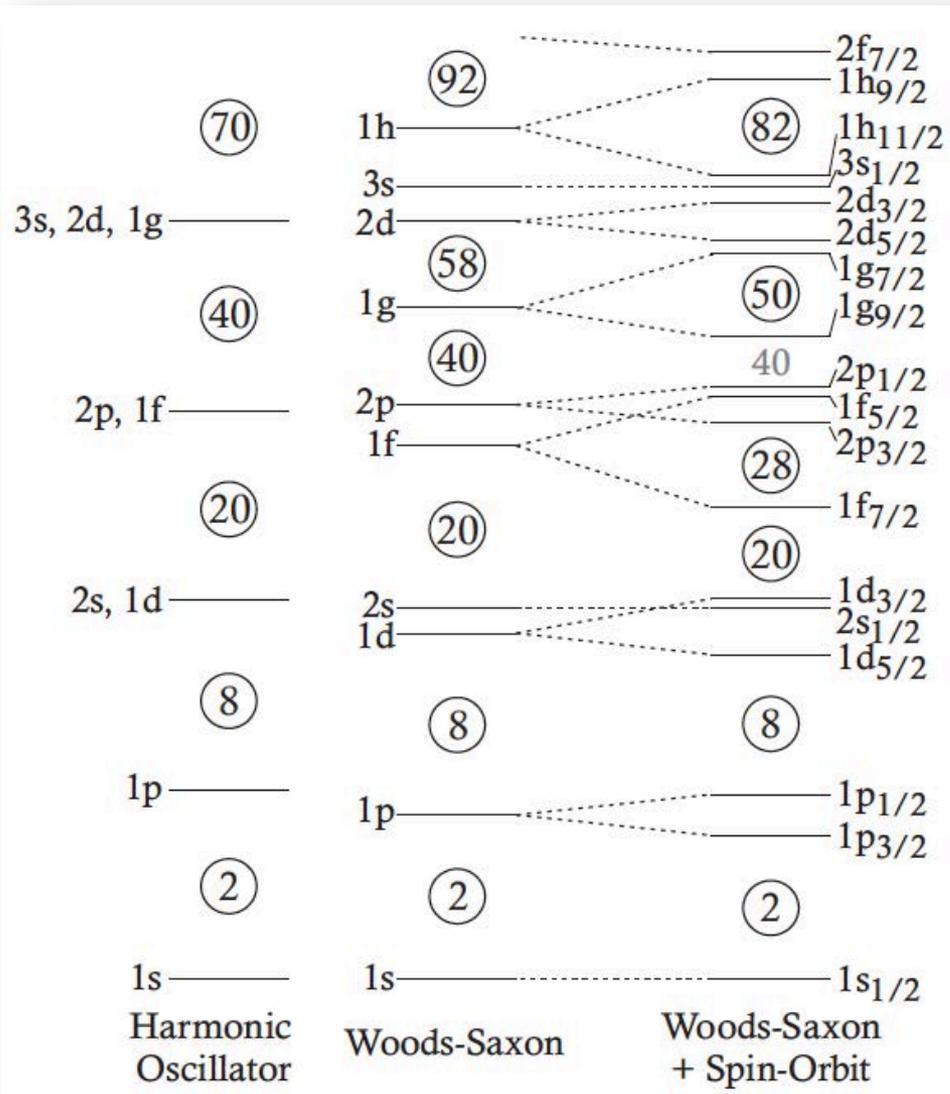


Similar indicators are found across the nuclear landscape, suggesting a nuclear shell structure.



Firestone, R.B. *Table of Isotopes*. Wiley, New York, 1996.

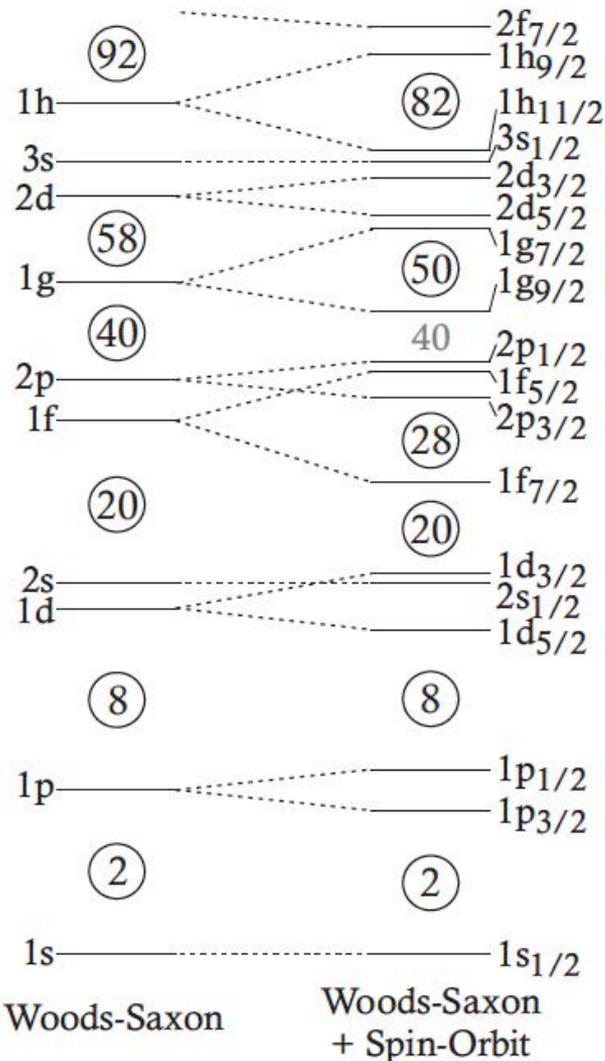
# Nuclear shell structure



Maria Goeppert-Mayer  
 & Hans D. Jensen  
 1963

Maria Goeppert-Mayer, Phys. Rev. 75, 1969 (1949).  
 O. Haxel, Phys. Rev. 75, 1766 (1949).

# Nuclear shell structure

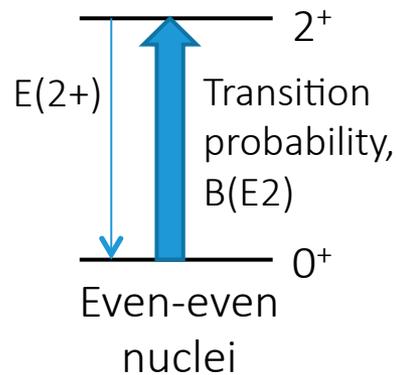


- Single-particle levels in nuclei
  - Single-particle levels in the fermionic system are grouped into shells, with stabilizing gaps between groups of states at certain occupation numbers with “magic numbers” of protons and neutrons
- Magic numbers
  - Magic numbers correspond to particularly stable structures (2, 8, 20, 28, 50, 82,...)

$$H = H_0 + H_{res} = \sum_{i=1}^A \left[ \frac{\mathbf{p}_i^2}{2m_i} + U_i(\mathbf{r}) \right] + H_{res}$$

# Nuclear shell structure signatures

To improve our understanding and descriptions of nuclei far from stability, we need to identify the location of shell gaps, and ideally the spacing between single-particle states in the most exotic nuclei.

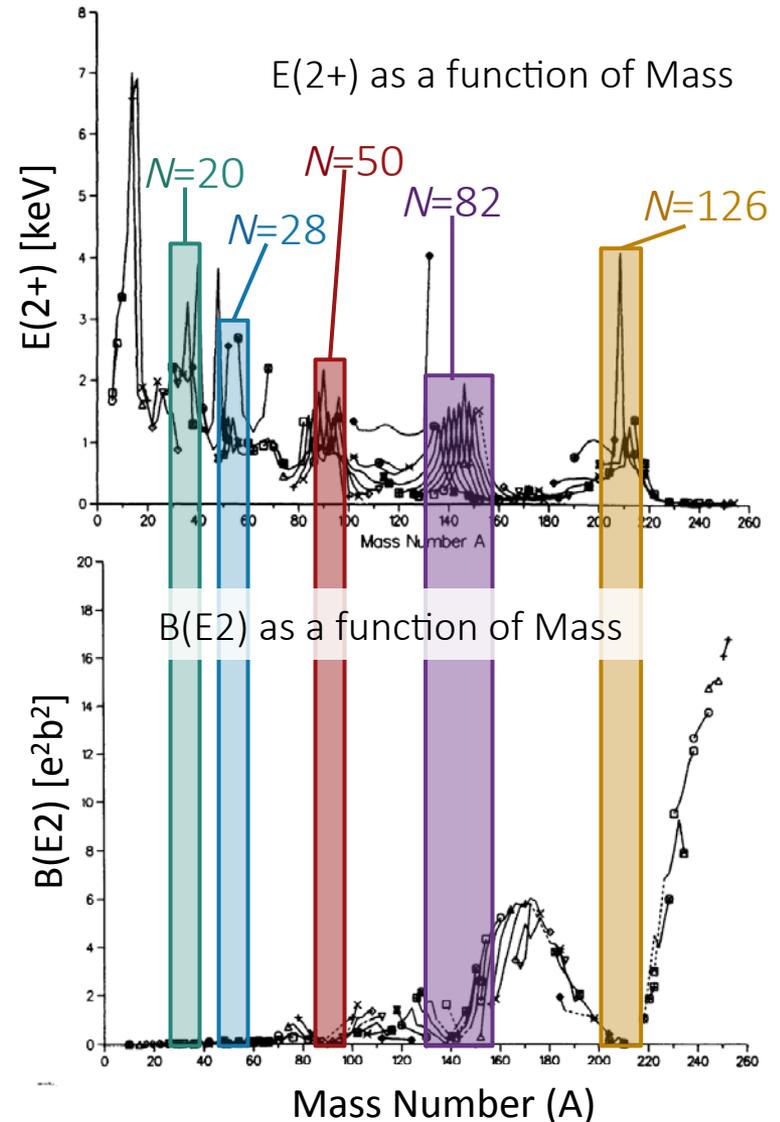


## Structure of Even-Even Nuclei

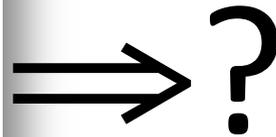
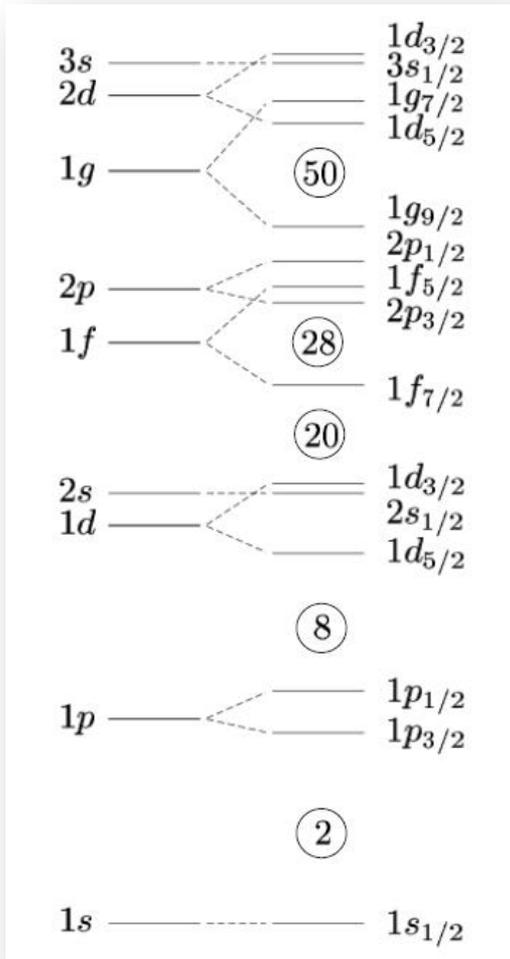
The ground state of even-even nuclei is always  $0^+$ , while the first excited state is usually a  $2^+$  state. The energy of this state, and the cross-section to populate it are sensitive to details of the nuclear structure.

$$B(E2; i \rightarrow f) = \frac{1}{2J_i + 1} \langle \lambda_f J_f || E2 || \lambda_i J_i \rangle^2$$

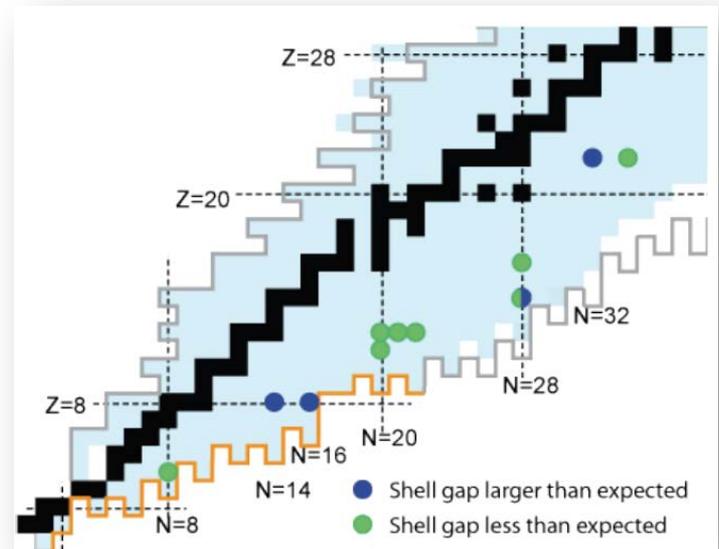
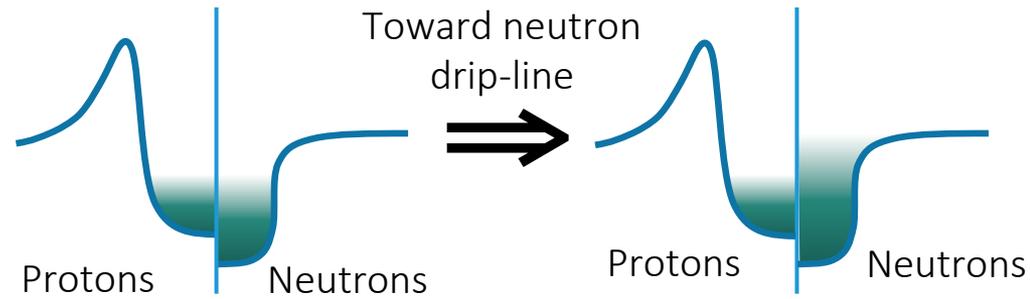
$$B(E2) \uparrow = \frac{(2.57)Z^2}{EA^{2/3}} [e^2 b^2]$$



# “Exotic” shell structure



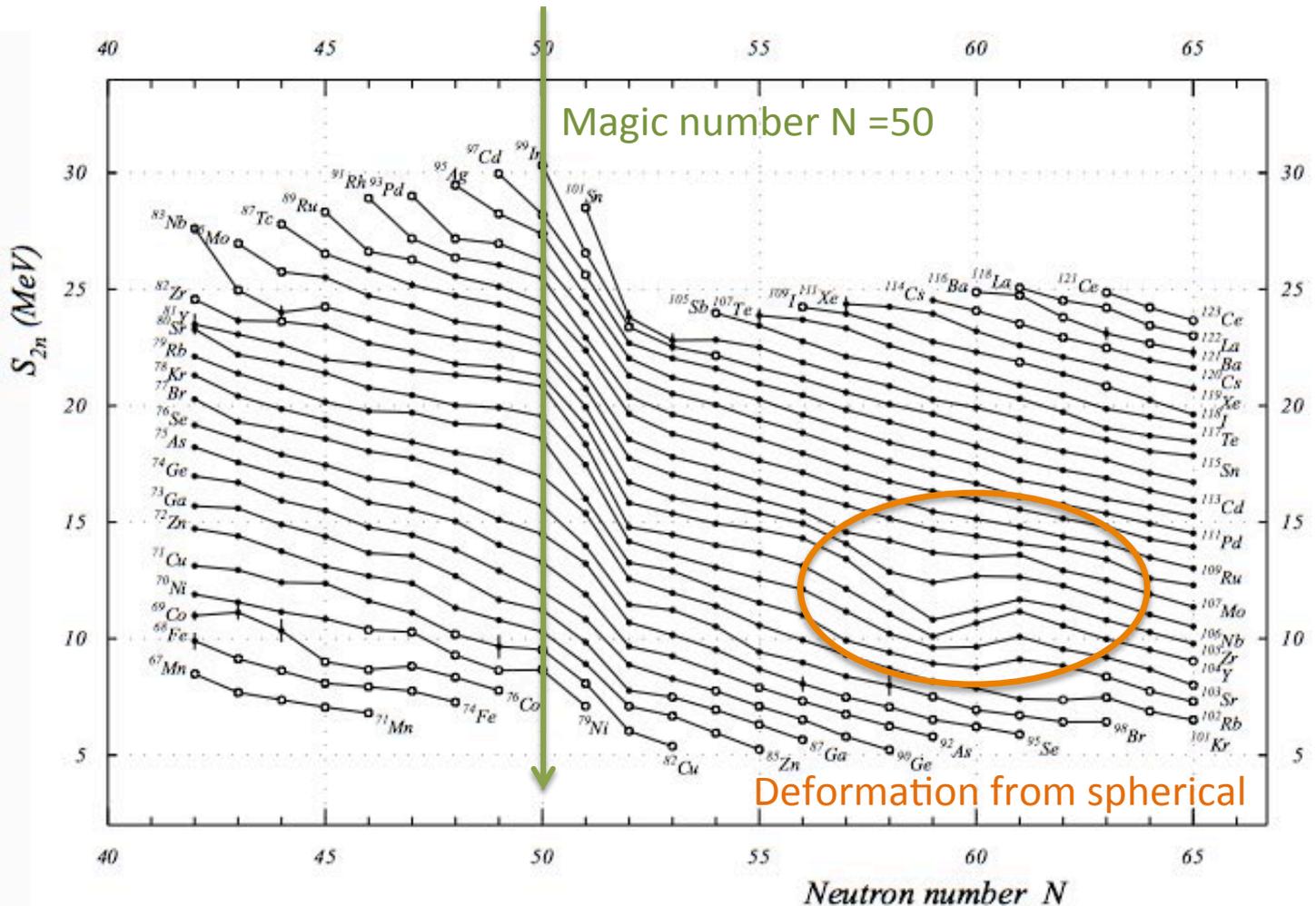
A driving question in nuclear science:  
Is the shell-model description static across the entire chart of nuclides?



Near the valley of  $\beta$  stability

Approaching the drip-lines

# Masses and shells



# Mass observables

$$S_{2n} = B(N,Z) - B(N-2,Z) = M(N-2,Z) + 2M_n - M(N,Z)$$

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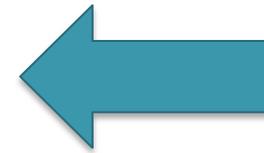
$$S_{2p} = B(N,Z) - B(N,Z-2) = M(N,Z-2) + 2M_H - M(N,Z)$$



Measure nuclear masses as for first insight to exotic nuclei. But we need to produce them.

# Making exotic nuclei

To study the most exotic nuclei we must first produce them. Using stable beam facilities and different combinations of targets + beams, a wide variety of exotic nuclei can be produced and studied.



However, there are a finite # of combinations of stable beams + targets → make radioactive beams, and use these

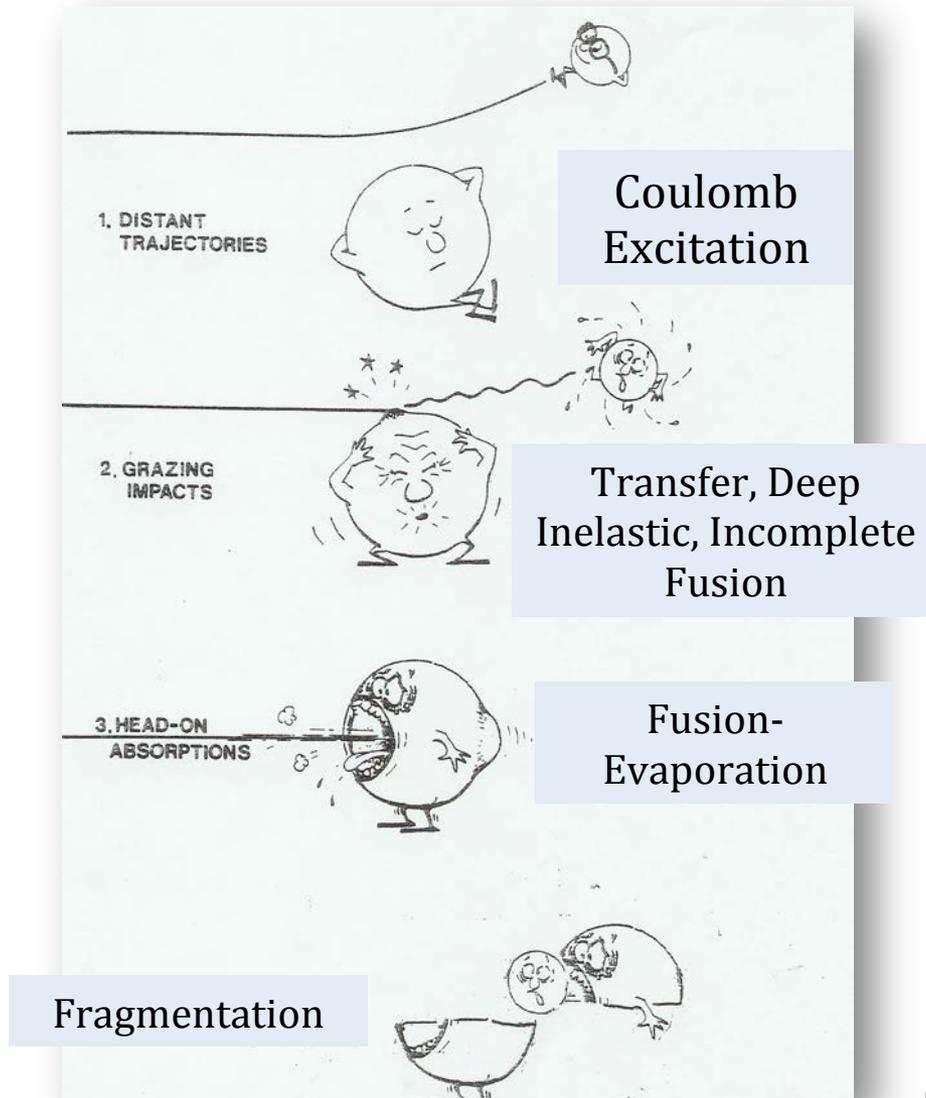
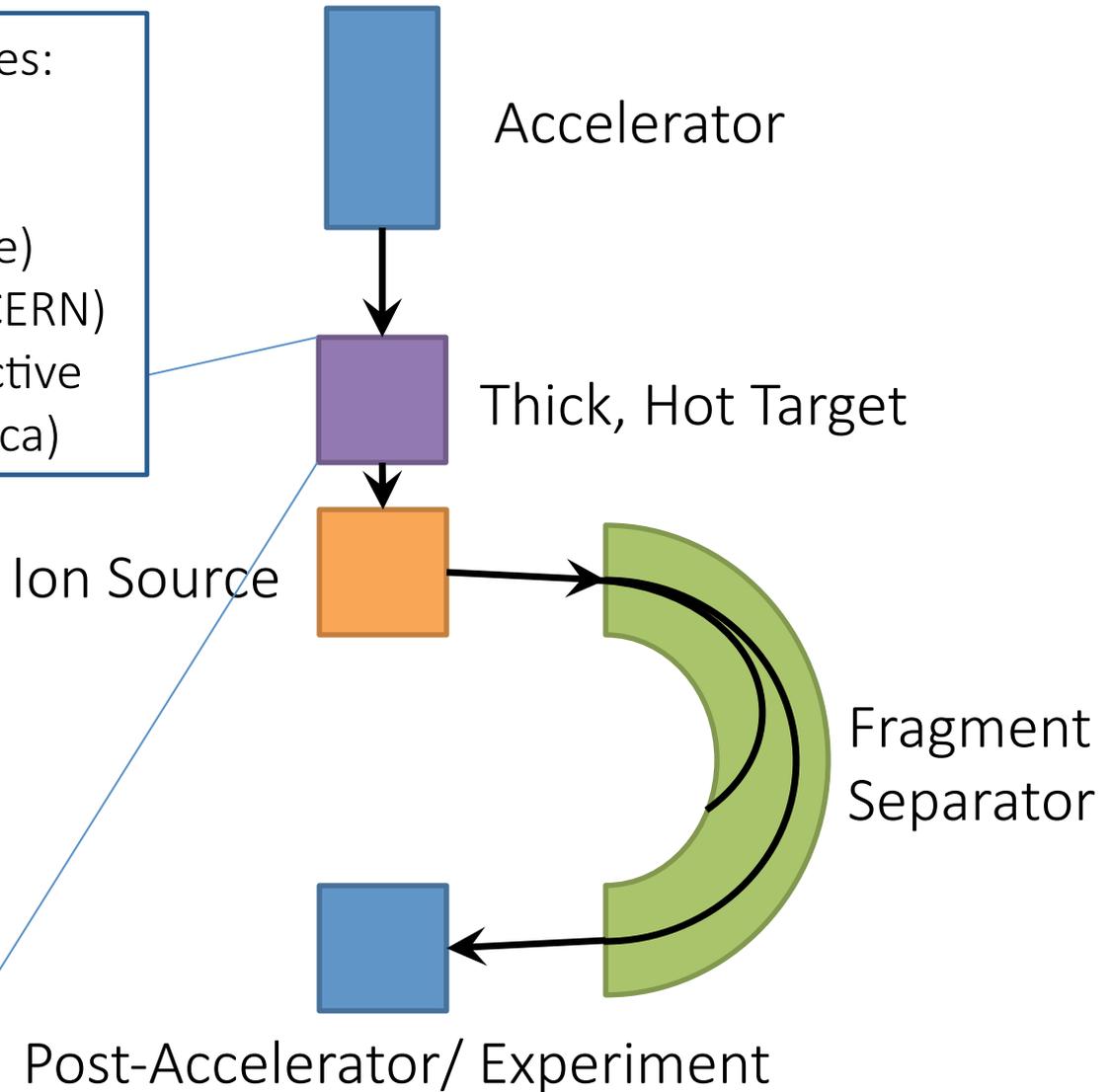
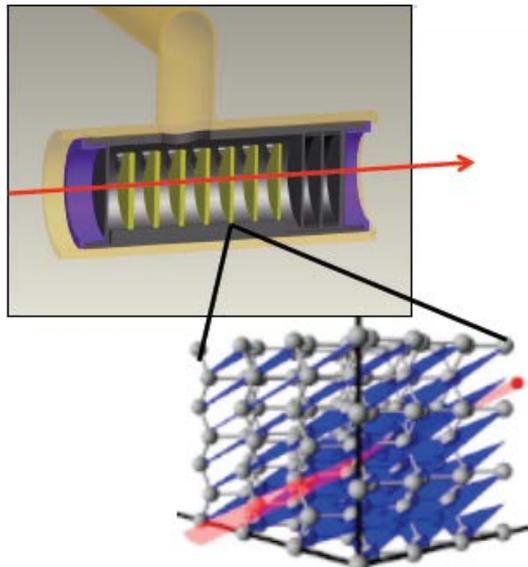


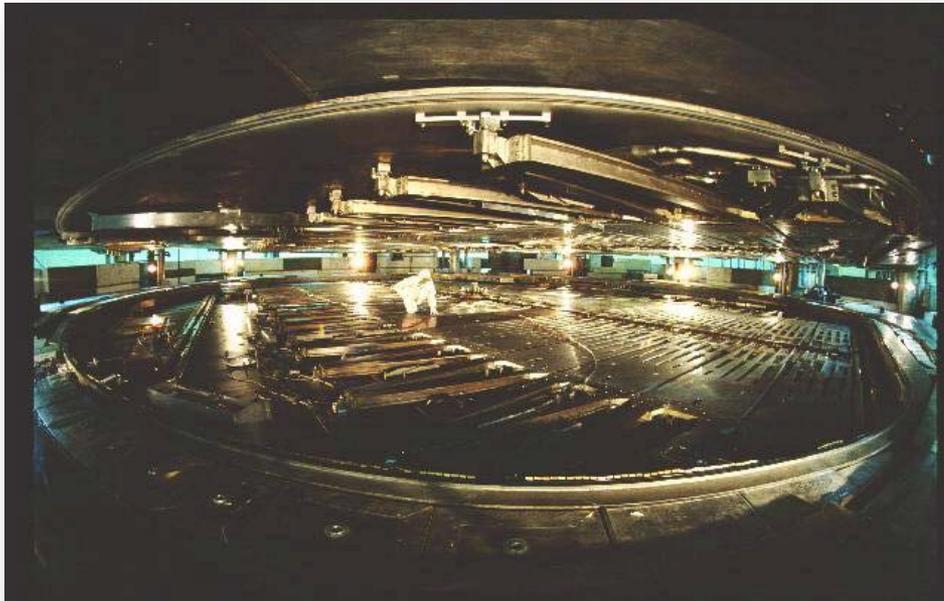
Figure: Borrowed from R.M. Clark, 2007 RIA Summer School

# Isotope Separation On-Line (ISOL)

Examples of ISOL facilities:  
TRIUMF (Canada)  
HRIBF (USA)  
SPIRAL/SPIRAL2 (France)  
REX-ISOLDE/HIE-ISOLDE (CERN)  
iTHEMBA - future radioactive  
beam facility (South Africa)



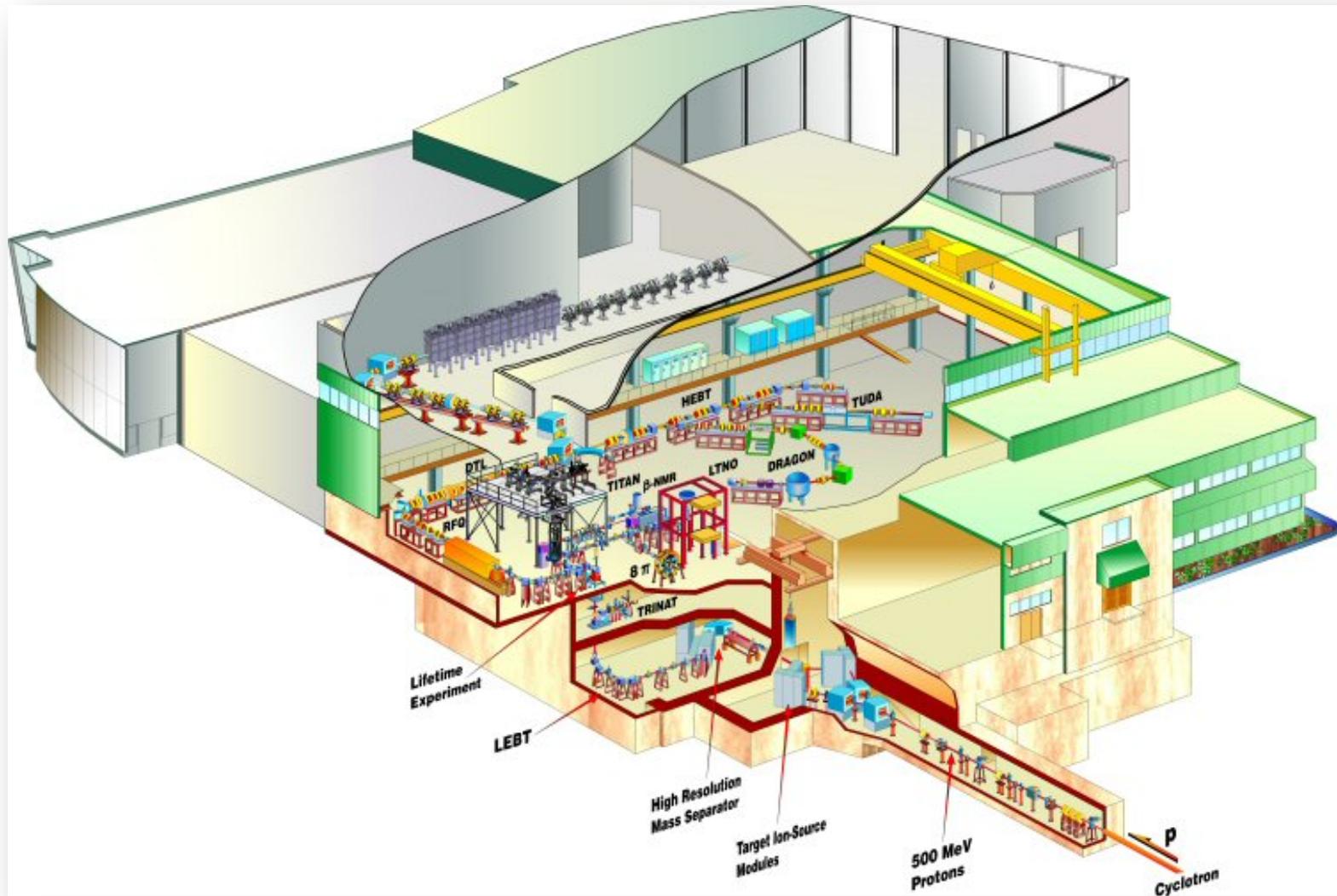
# ISOL Facilities - TRIUMF



TRIUMF is home to the world's largest cyclotron – accelerates  $H^-$  to 520 MeV, extracts as proton beam

Proton beam is sent into target hall, and interacts with thick targets (materials such as UC)

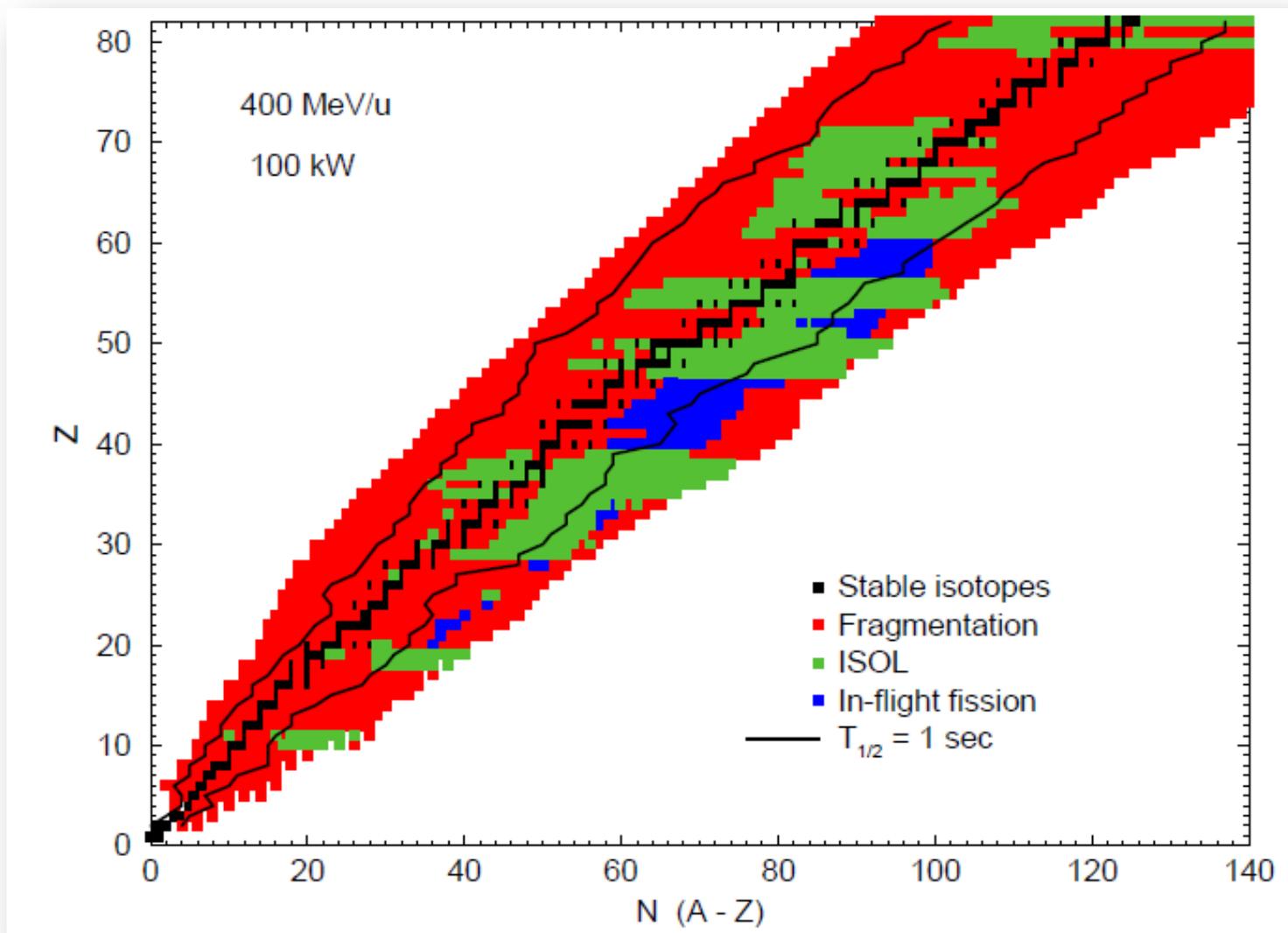
# ISOL Facilities - TRIUMF



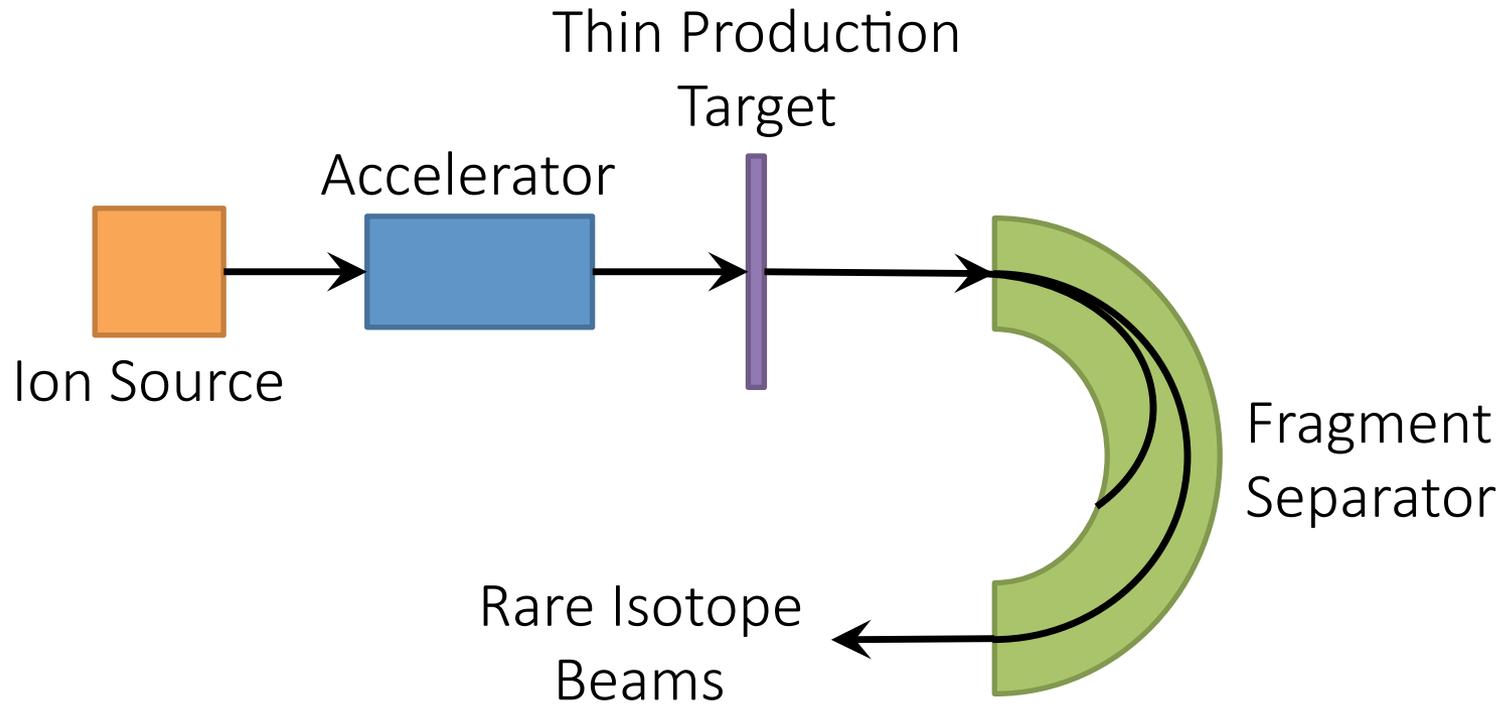
# ISOL - Considerations

- Nuclei produced within the crystal lattice of the target must migrate to the surface → very chemically selective process
- Due to extraction time, limited isotopes with long lifetimes →  $\tau > 1s$
- Beam ions lose a LOT of energy in the target → targets must withstand very high temperatures, which limits materials available
- Products that diffuse to the surface must still be ionized before they can be used in an experiment → again, chemically selective
- Chemically selectivity results in good Z purity of radionuclides, but you need mass separator ionization to isolate according to A – with this though, can obtain isotopically pure beams
- Reaccelerate rare-isotopes so beams are often very good quality, and for certain elements, very high intensity (i.e. alkali earth)

# What can we make? – ISOL



# Fragmentation + In-flight separation



Examples of fragmentation facilities:

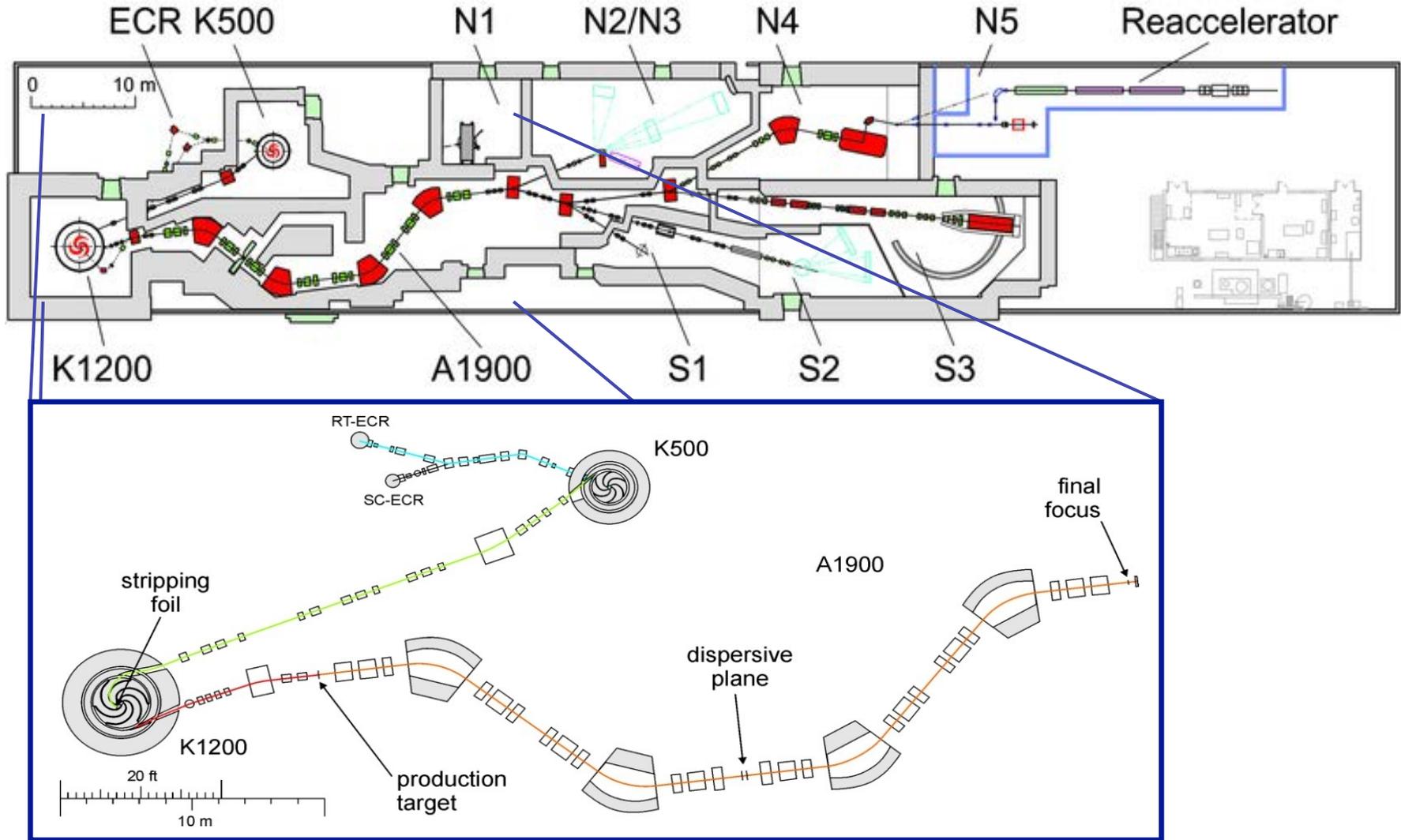
NSCL (USA) --> FRIB

RIKEN (Japan)

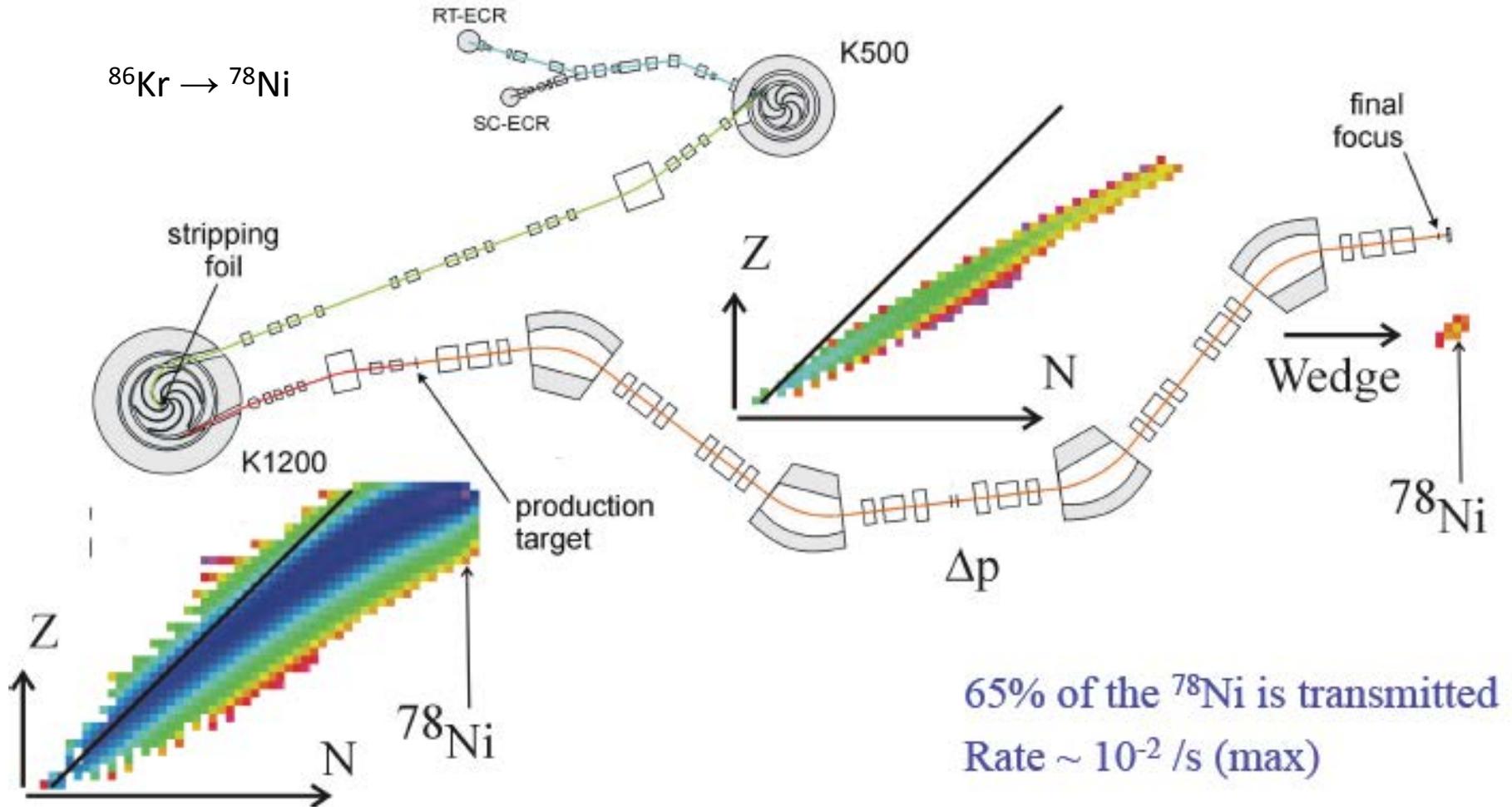
GANIL (France)

GSI (Germany)

# Fragmentation facilities - NSCL



# Fragmentation + separation: Example



# Fragmentation - Considerations

- Production of nuclei is chemically independent – you make everything lighter than your primary beam, and it's moving FAST
- NEED in-flight separation to obtain clean secondary beams, and will still usually not obtain 100% beam purity
- Beams are high energy, momentum spread in reactions means they can have large emittances, etc.
- Certain experimental techniques are either NOT possible, or need to be significantly altered for fast beams

# What can we make? – Fragmentation

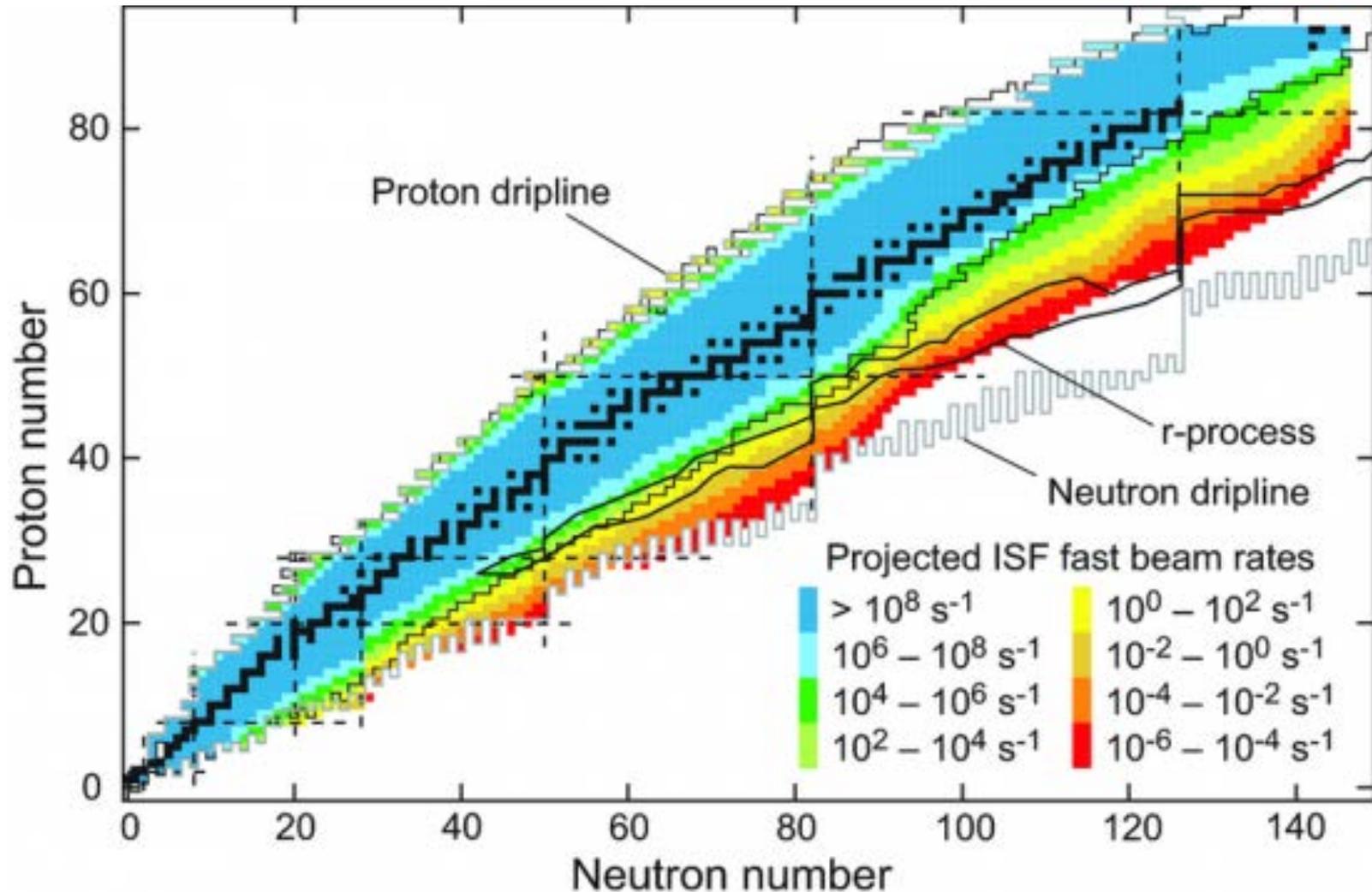
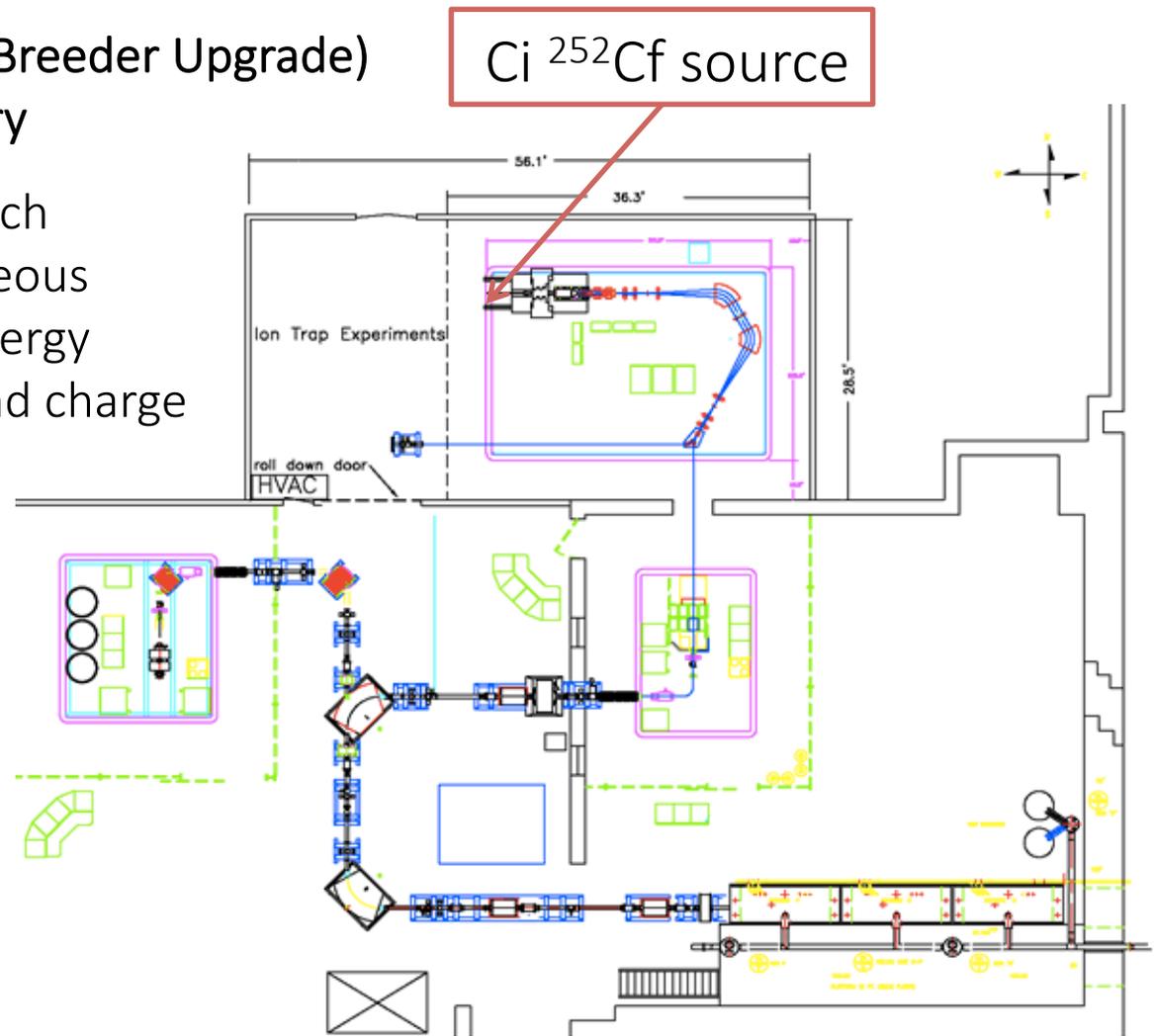


Figure: NSCL White Paper, 2006

# Fission-fragment accelerator

## CARIBU (Californium Rare Ion Breeder Upgrade) @ Argonne National Laboratory

Turns a source of neutron-rich isotopes, such as a spontaneous fission source, into a low-energy beam using a gas catcher and charge breeder



CARIBU: [www.phy.anl.gov/atlas/caribu.html](http://www.phy.anl.gov/atlas/caribu.html)

# Fission fragment yields

Production has inherent selectivity – cannot produce all nuclei, but will provide an intense source of certain species.

Due to reacceleration, beams should, like in ISOL facilities be of very high quality.

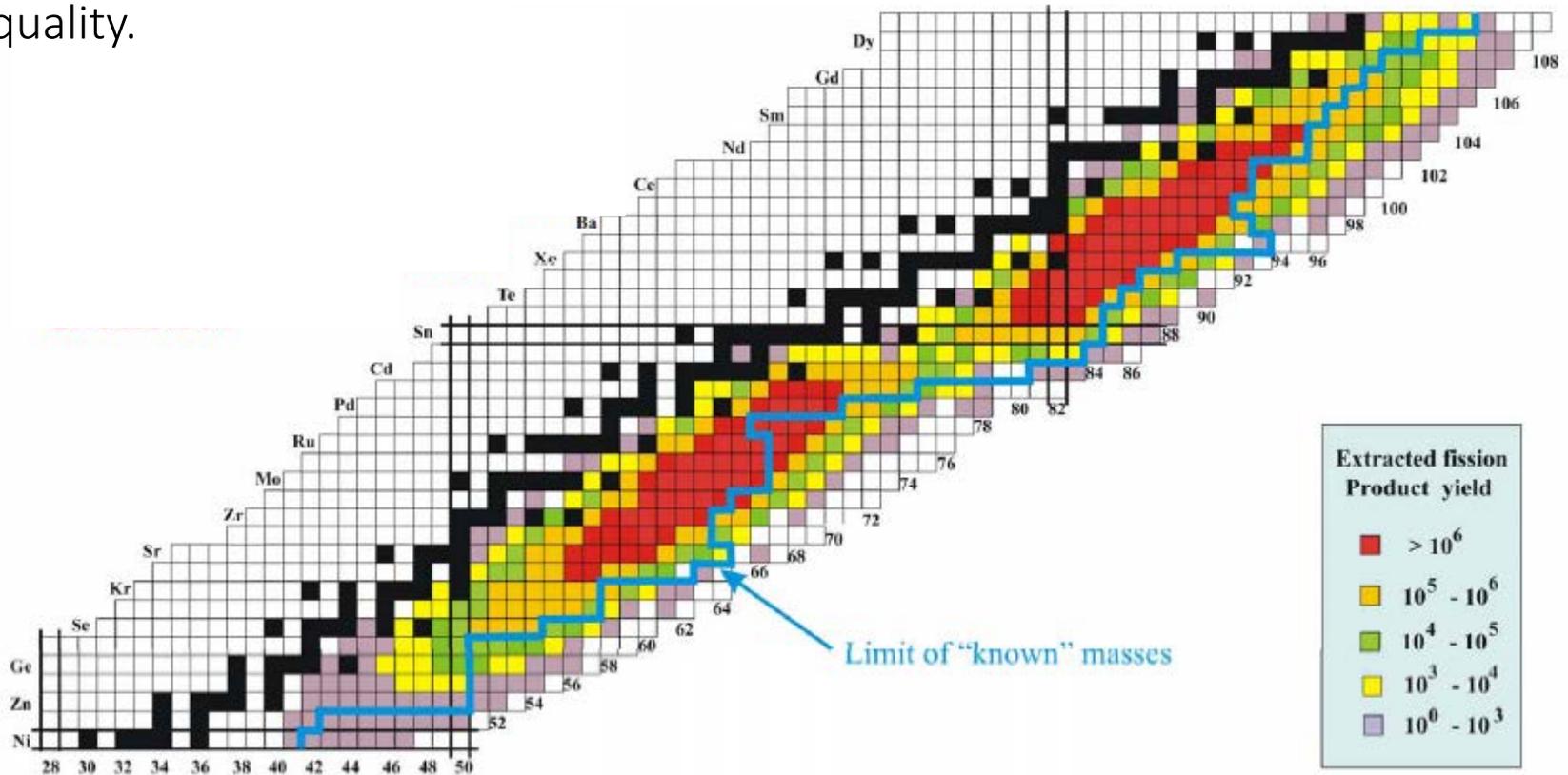
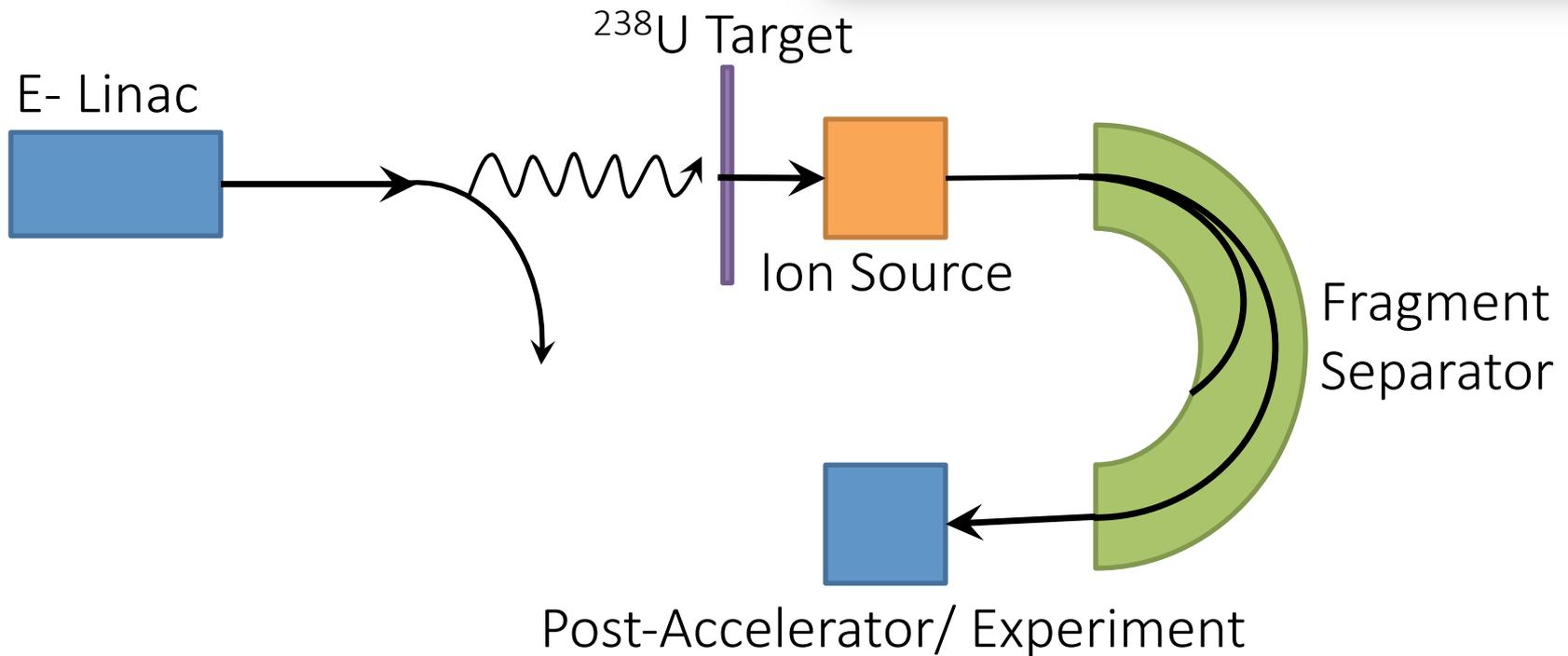
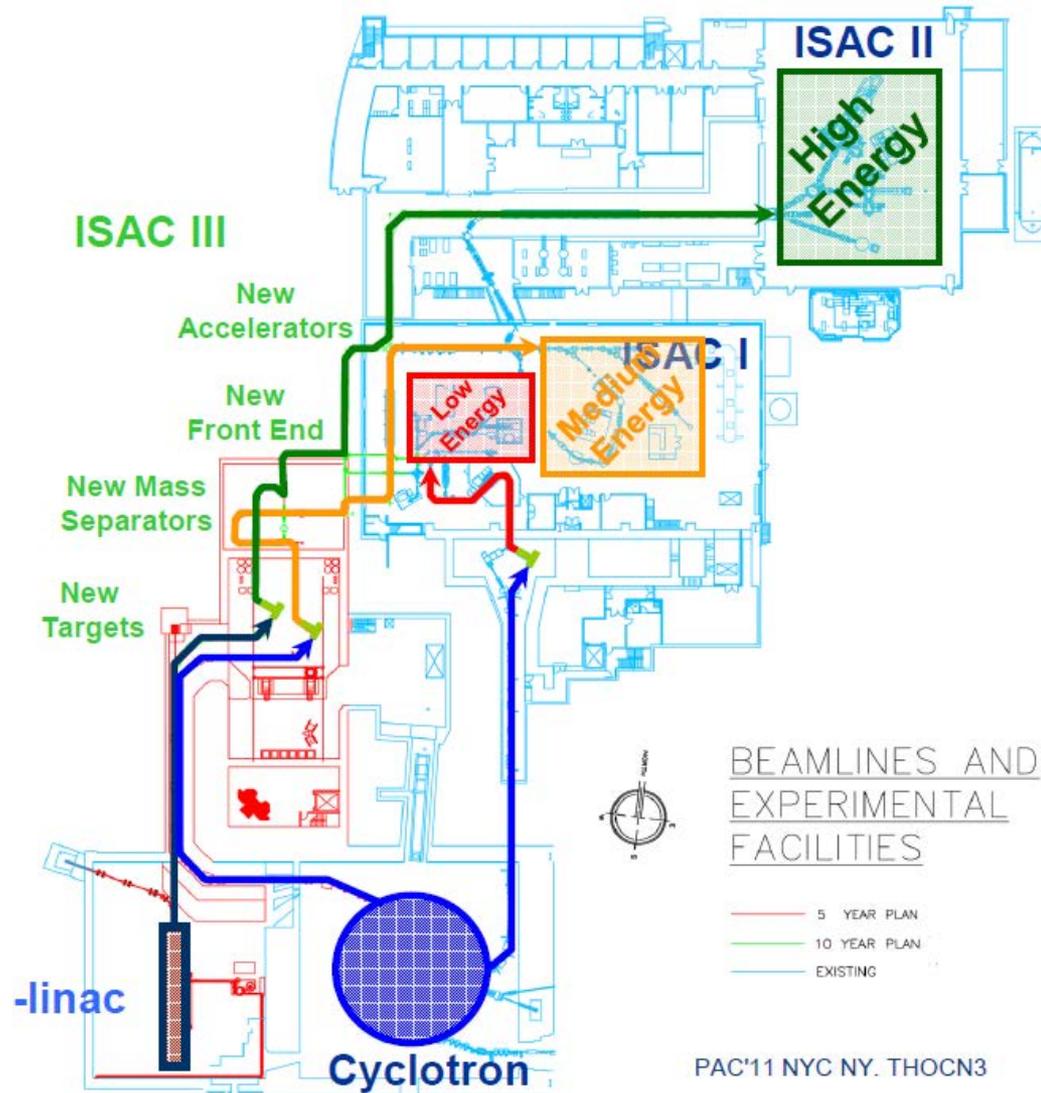


Figure: CARIBU Upgrade presentation @ ATLAS User Group Workshop, 2004

# On the horizon: Photo-fission production

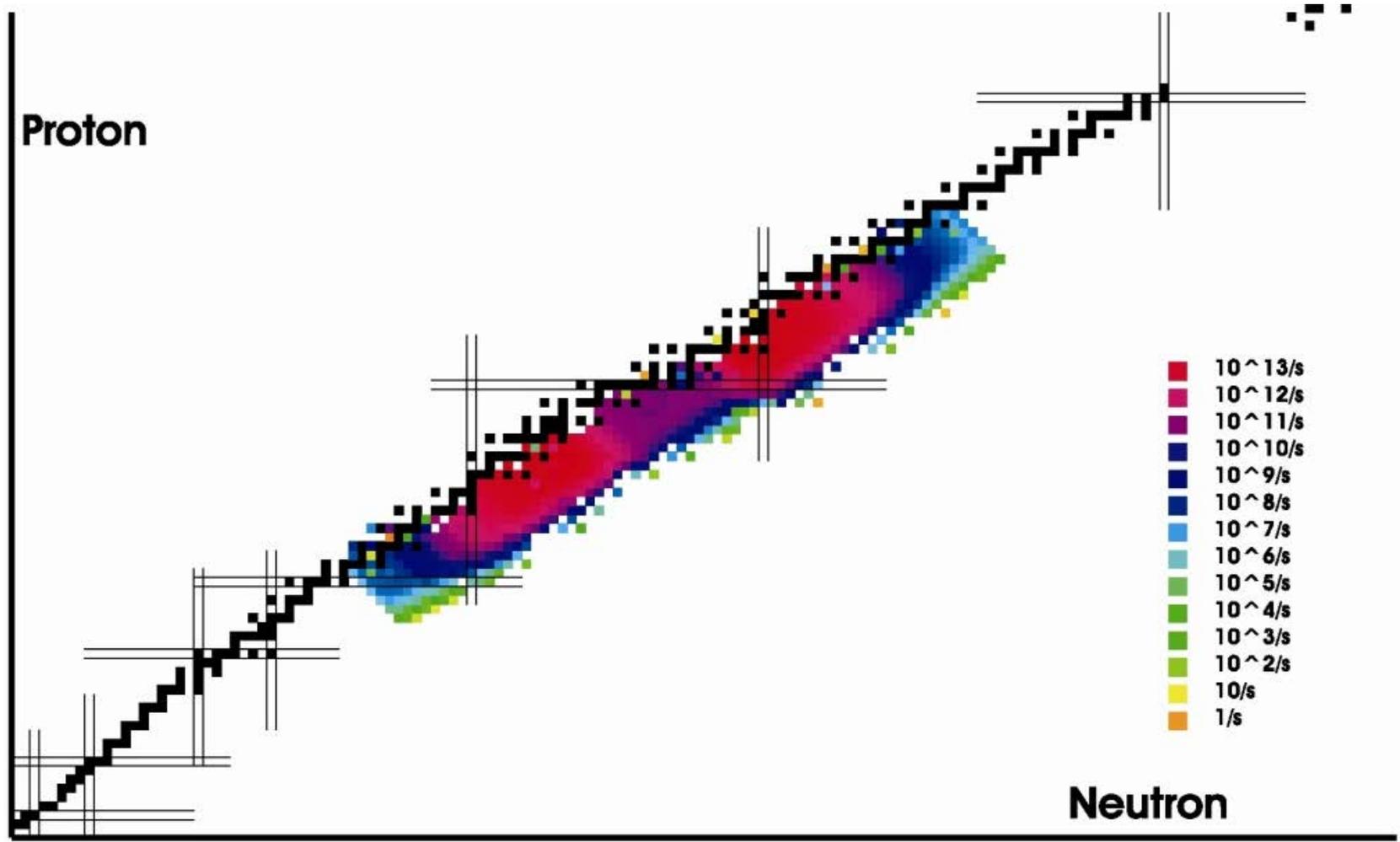


# Photo-fission facility: ARIEL @ TRIUMF



ARIEL: [www.triumf.ca/ariel](http://www.triumf.ca/ariel)

# Photo-fission facility: ARIEL @ TRIUMF



ARIEL: [www.triumf.ca/ariel](http://www.triumf.ca/ariel)

# Question!

- If you wanted to run an experiment on  $^{42}\text{Ar}$ , where would you go to make the measurement?
  - (A) TRIUMF (ISOL facility)
  - (B) NSCL (fragmentation facility)
  - (C) CARIBU (fission fragments)
  - (D) RIKEN RIBF (fragmentation facility)



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  - (A) TRIUMF (ISOL facility)
  - (B) NSCL (fragmentation facility)
  - (C) CARIBU (fission fragments)
  - (D) RIKEN RIBF (fragmentation facility)

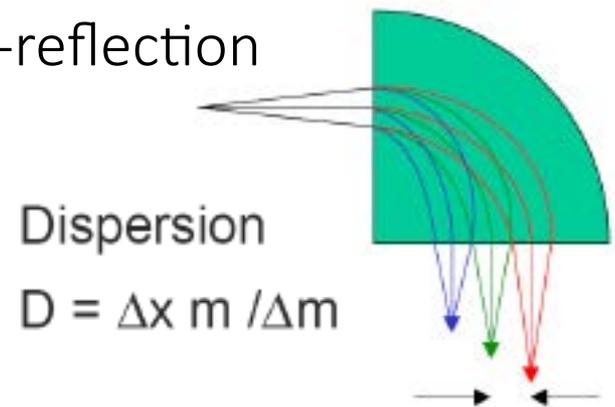


# Mass Measurements

# Mass measurements – Direct vs. indirect

- Indirect measurements
  - Q-value measurements – decay and kinematics from two-body reactions
- Direct measurements
  - Conventional mass spectrometry
  - Time-of-flight measurements
    - Spectrometer, multi-turn or multi-reflection
  - Frequency measurements
    - Penning traps, storage rings

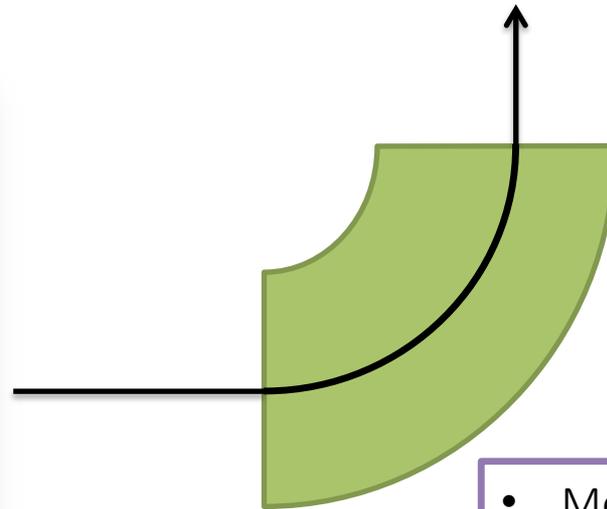
$$A(a, b)B$$
$$Q = M_A + M_a - M_b - M_B$$



# TOF mass measurements

Obtain mass based on equations of motion for charged particles through a magnetic system.

$$\begin{aligned} F_{\text{Lorentz}} &= F_{\text{centrifugal}} \\ \rightarrow qvB \sin(\theta) &= \frac{mv^2}{\rho} \\ m &= \gamma m_0 \\ v &= \frac{L_{\text{path}}}{\text{TOF}} \\ \Rightarrow m_0 &= \frac{\text{TOF} \cdot q(B\rho)}{L_{\text{path}} \cdot \gamma} \end{aligned}$$



- Measure multiple masses simultaneously
- Accuracy  $\Delta m/m \rightarrow 10^{-6}$
- Lifetimes down to ms

Measurement requires precision knowledge of TOF and magnetic rigidity ( $B\rho$ ).

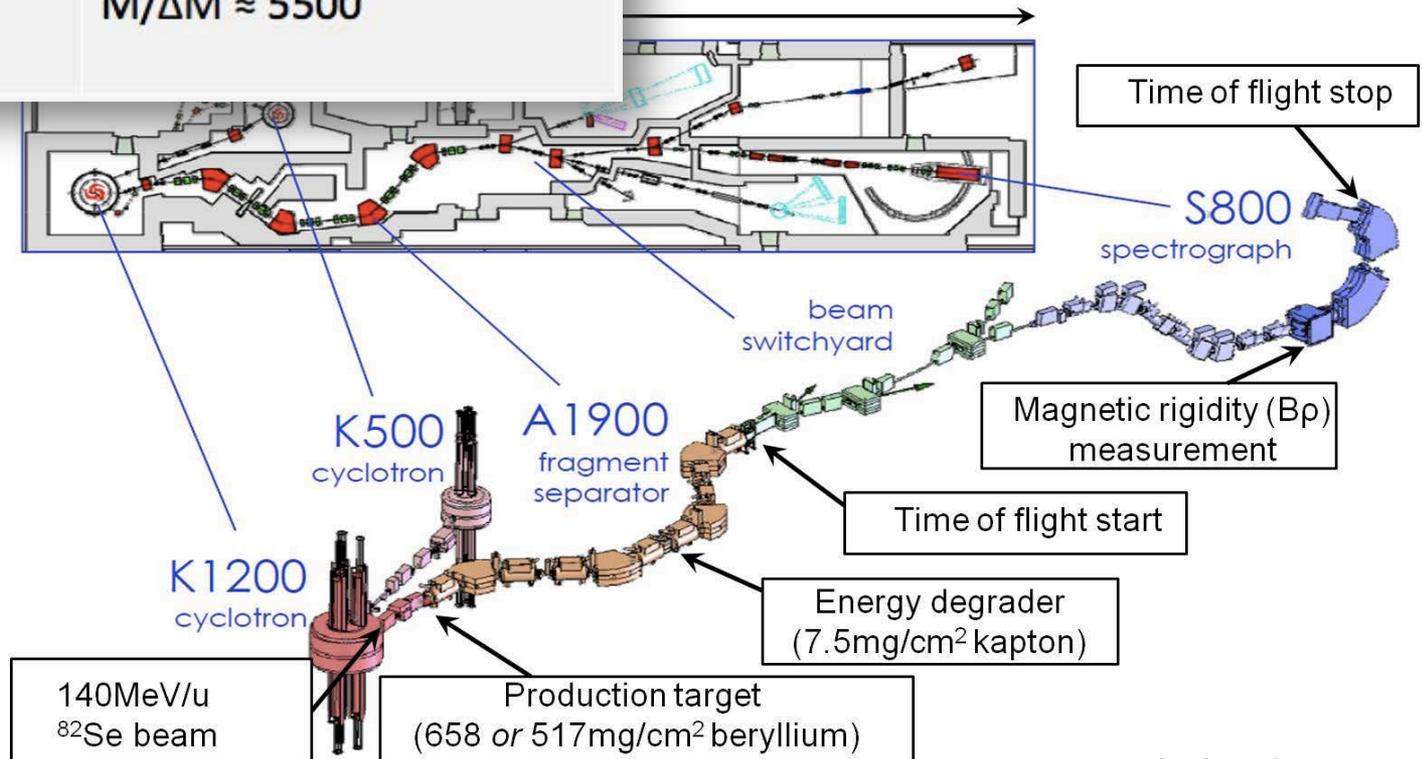
--> In practice, measure known masses to calibrate TOF measurements

Experimental equipment – long flight-path magnetic separator

--> TOFI @ LANL, SPEG @ GANIL, A1900+S800 @ NSCL...

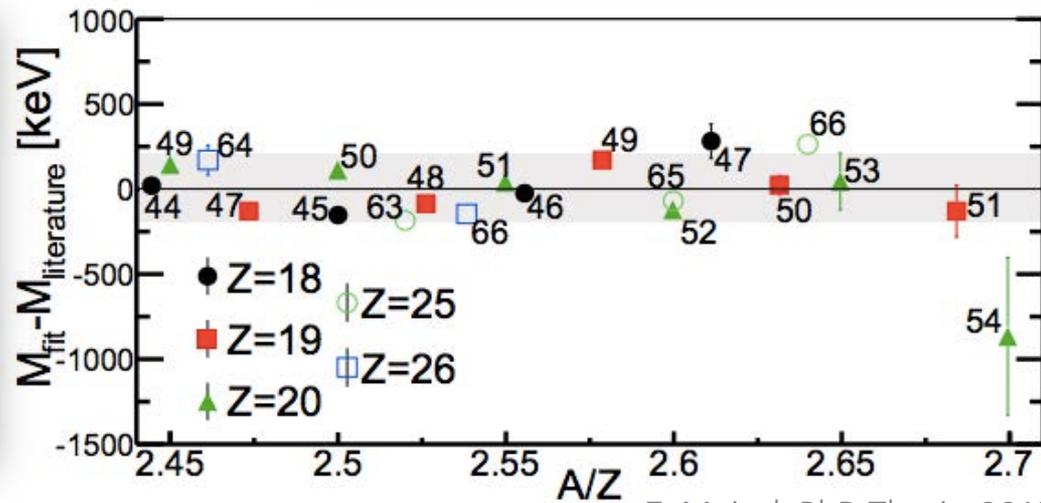
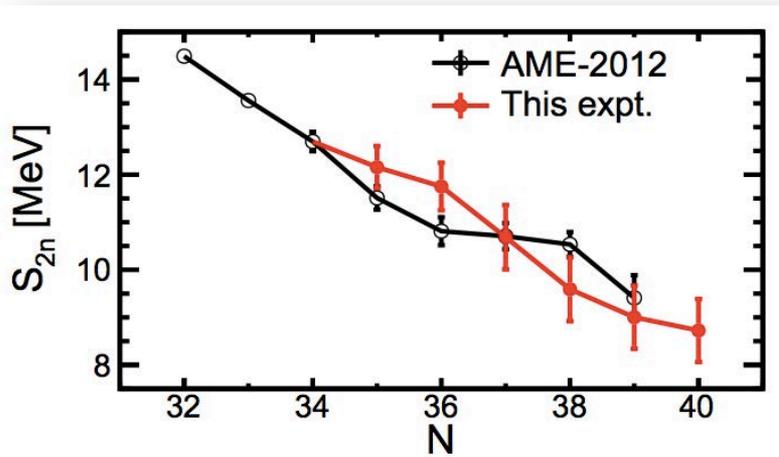
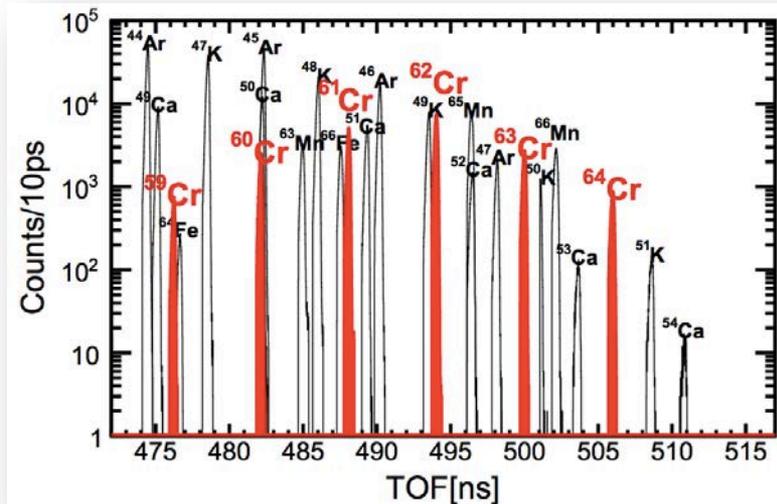
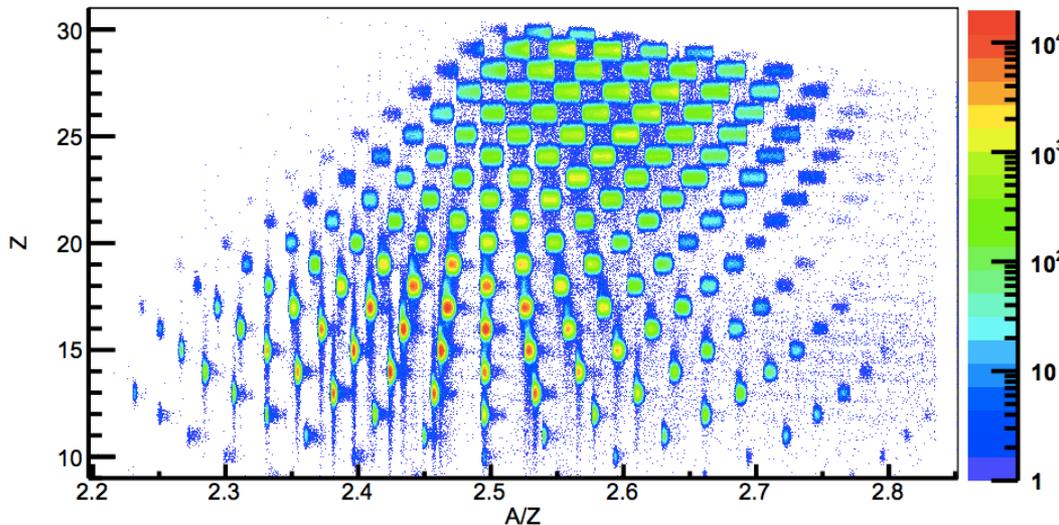
# TOF mass measurements

Solid angle	$\Omega = 20\text{msr}$
Momentum acceptance	$\delta p/p \approx 1\%$ (due to MCP)
Max Rigidity	$B\rho \approx 4\text{Tm}$
Central flight Path	$L_0 = 59\text{m}$
Achieved Mass Resolution	$M/\Delta M \approx 5500$



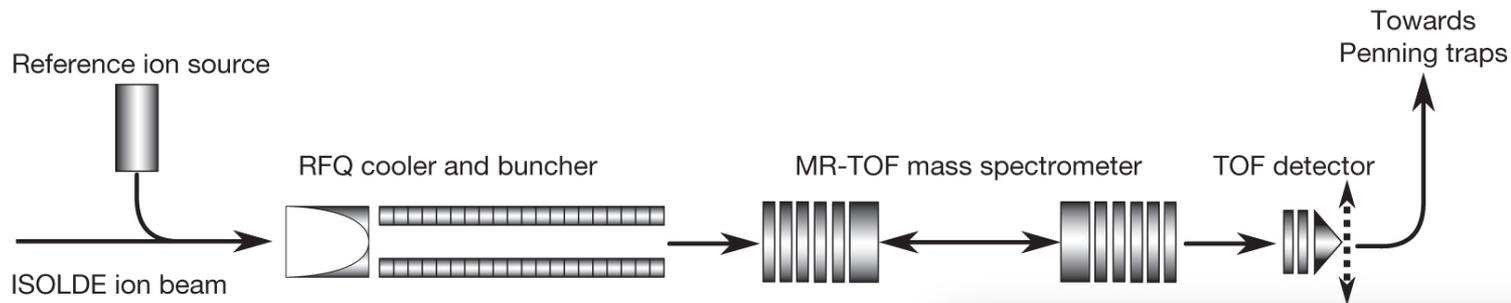
Z. Meisel, PhD Thesis, 2015.

# TOF mass measurements



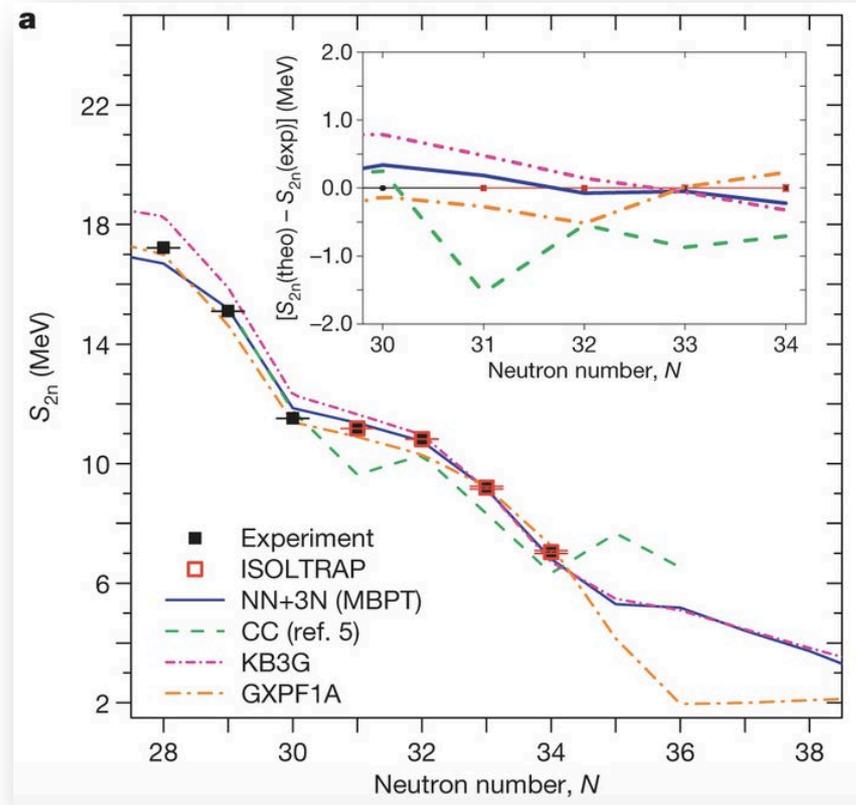
Z. Meisel, PhD Thesis, 2015.

# MR-TOF – $^{54}\text{Ca}$ at ISOLDE



TOF measurements require long flight path lengths; a method around this is to “reuse” the same flight distance –

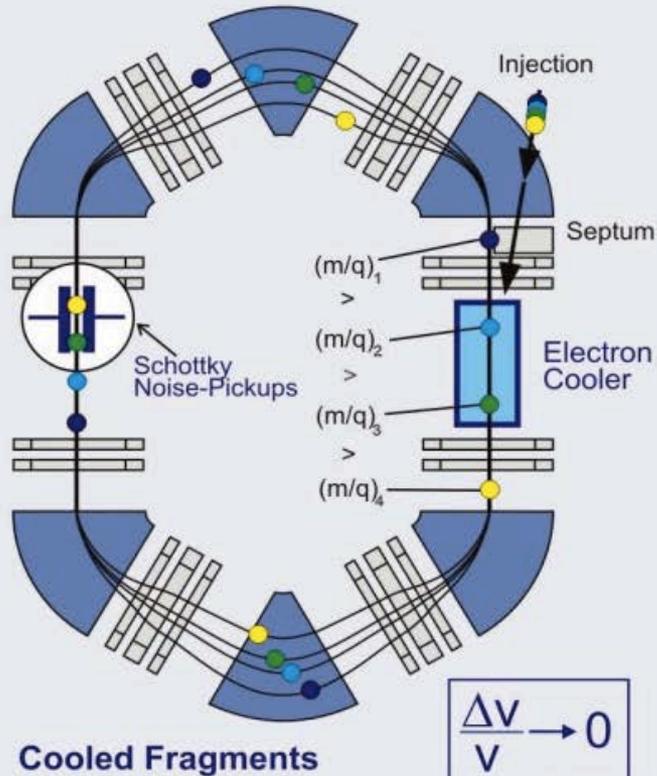
**multi-reflection TOF**



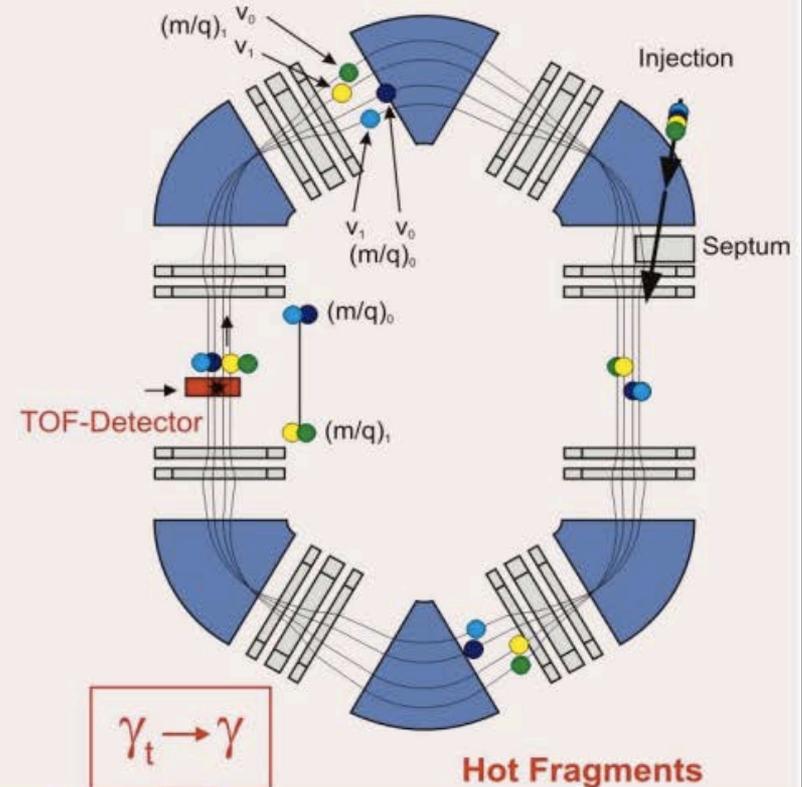
F Wienholtz et al. Nature **498**, 346-349 (2013).

# Storage ring mass measurement

## SCHOTTKY MASS SPECTROMETRY

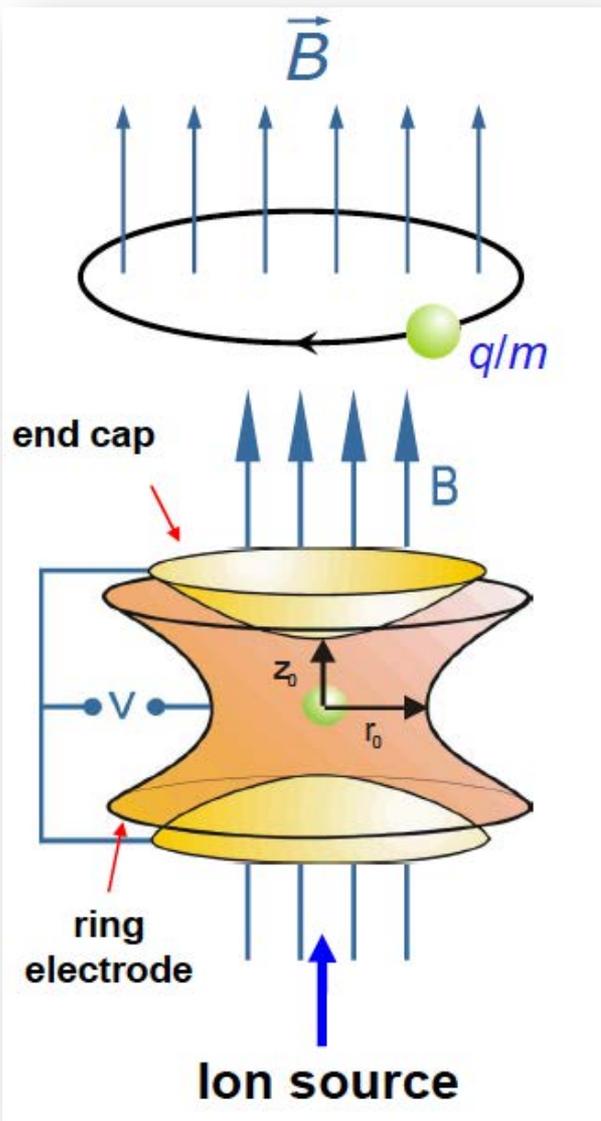


## ISOCRONOUS MASS SPECTROMETRY



$$\frac{\Delta f}{f} = -\frac{1}{\gamma_t^2} \frac{\Delta(m/q)}{m/q} + \frac{\Delta v}{v} \left(1 - \frac{\gamma^2}{\gamma_t^2}\right)$$

# Penning trap mass measurements

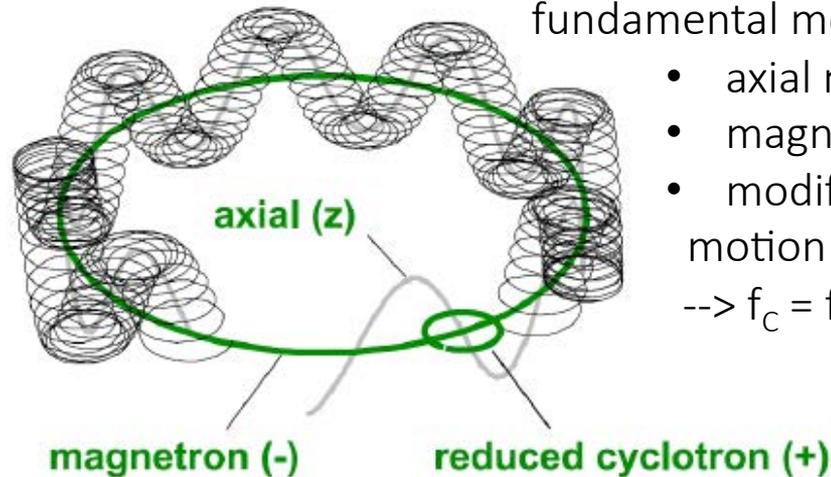


Mass measurement comes from determination of the cyclotron frequency for the characteristic motion of the stored ions

$$f_c = \frac{1}{2\pi} \cdot \frac{q}{m} \cdot B$$

Motion is superposition of three fundamental motions:

- axial motion ( $f_z$ )
  - magnetron motion ( $f_-$ )
  - modified cyclotron motion ( $f_+$ )
- >  $f_c = f_+ + f_-$



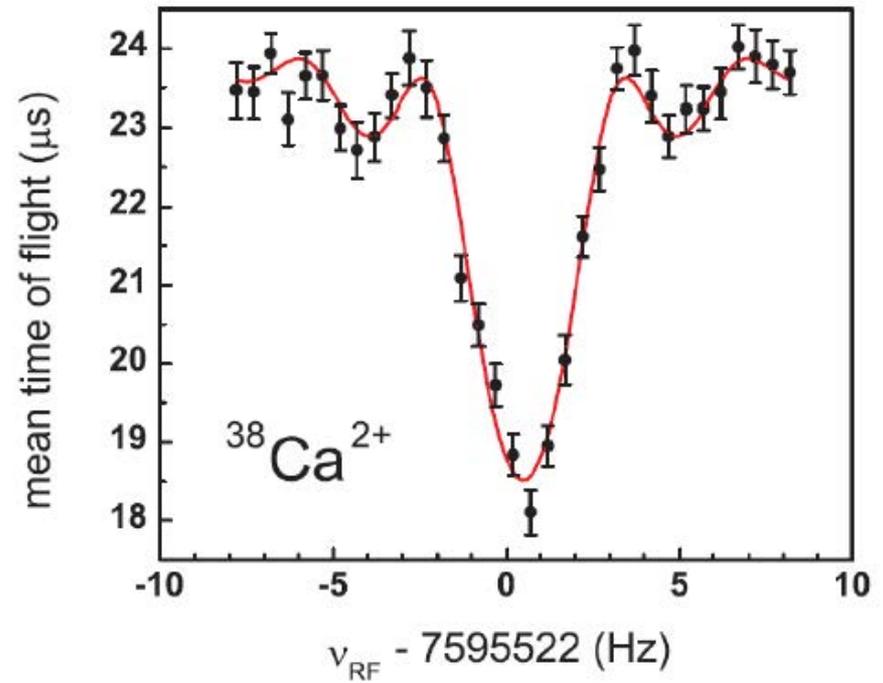
# Penning trap mass measurements

Strong homogenous B field provides radial confinement; weak electric quadrupole field provides axial confinement

Excite cyclotron motion with multipolar RF (to excite cyclotron motion resonance)

Transform radial to axial energy and eject ions toward particle detector

Measure TOF to detector



Constantly measure reference ions as well to reduce systematic error in measurements (varying B field, etc.)

G. Bollen *et al.*, Phys. Rev. Lett. 96, 152501 (2006).



# Penning traps around the world



K. Blaum *et al.*, J. Phys. B 42, 154015 (2009).

# Describing masses

## Algebraic descriptions:

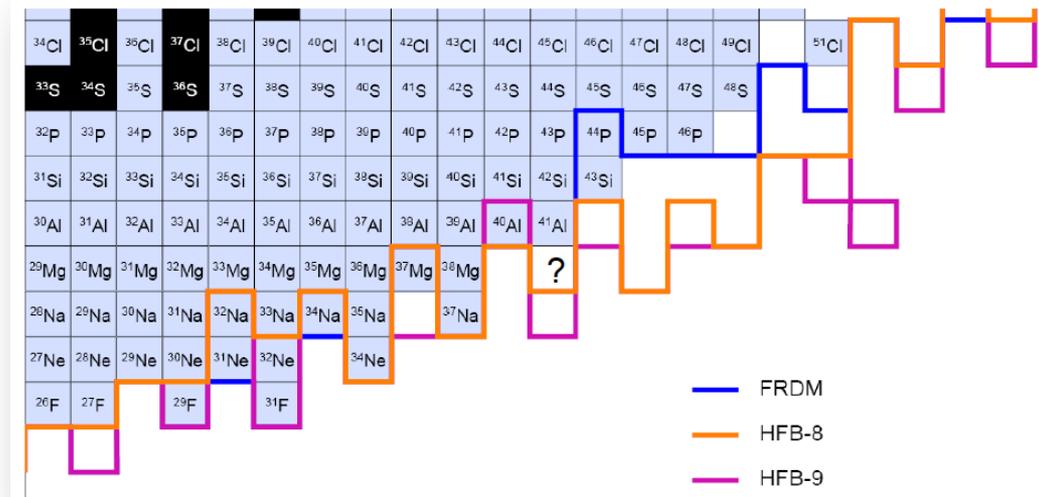
- Garvey-Kelson (GK) relationships between sums and differences between masses

## Microscopic-macroscopic:

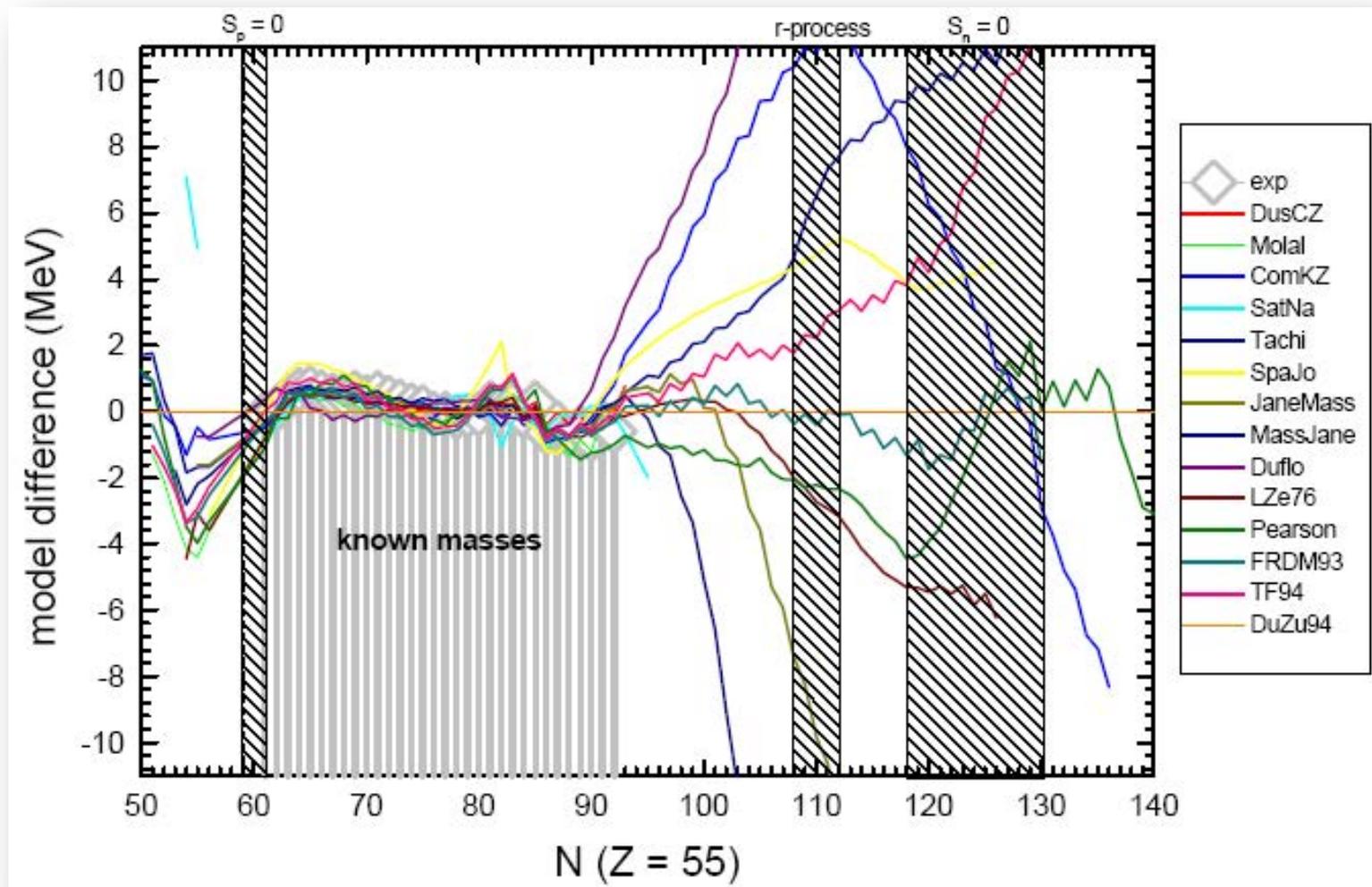
- Finite-range droplet model (FRDM) – 31 parameters fit to data
  - Bulk part from liquid drop + shell and pairing corrections

## Microscopic:

- Relativistic mean-field (RMF) and Hartree-Fock Bogoliubov (HFB); use effective nucleon-nucleon interactions



# What can we predict?



Away from available data, predictions still vary widely.

# Question!

- What technique would be best suited for measuring the (most accurate) mass of an exotic nucleus with a lifetime of about 10 ms?
  - (A) Penning trap mass spectroscopy
  - (B) TOF measurement at ISOL facility
  - (C) TOF measurement at fragmentation facility
  - (D) Decay Q-value measurement



# Question!

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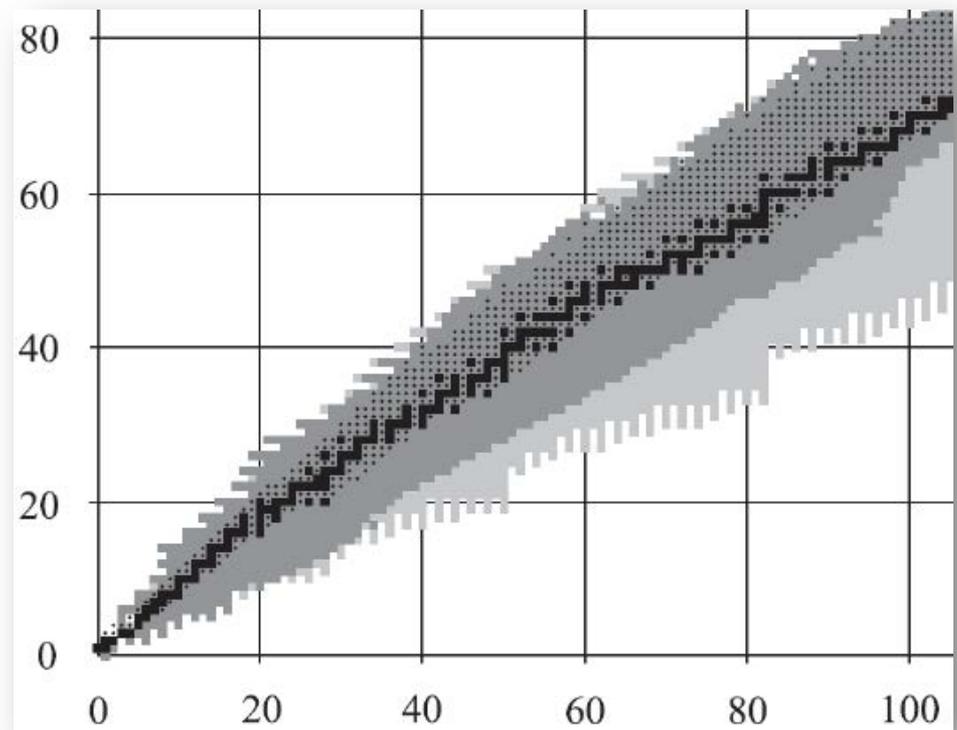


# Locating the driplines

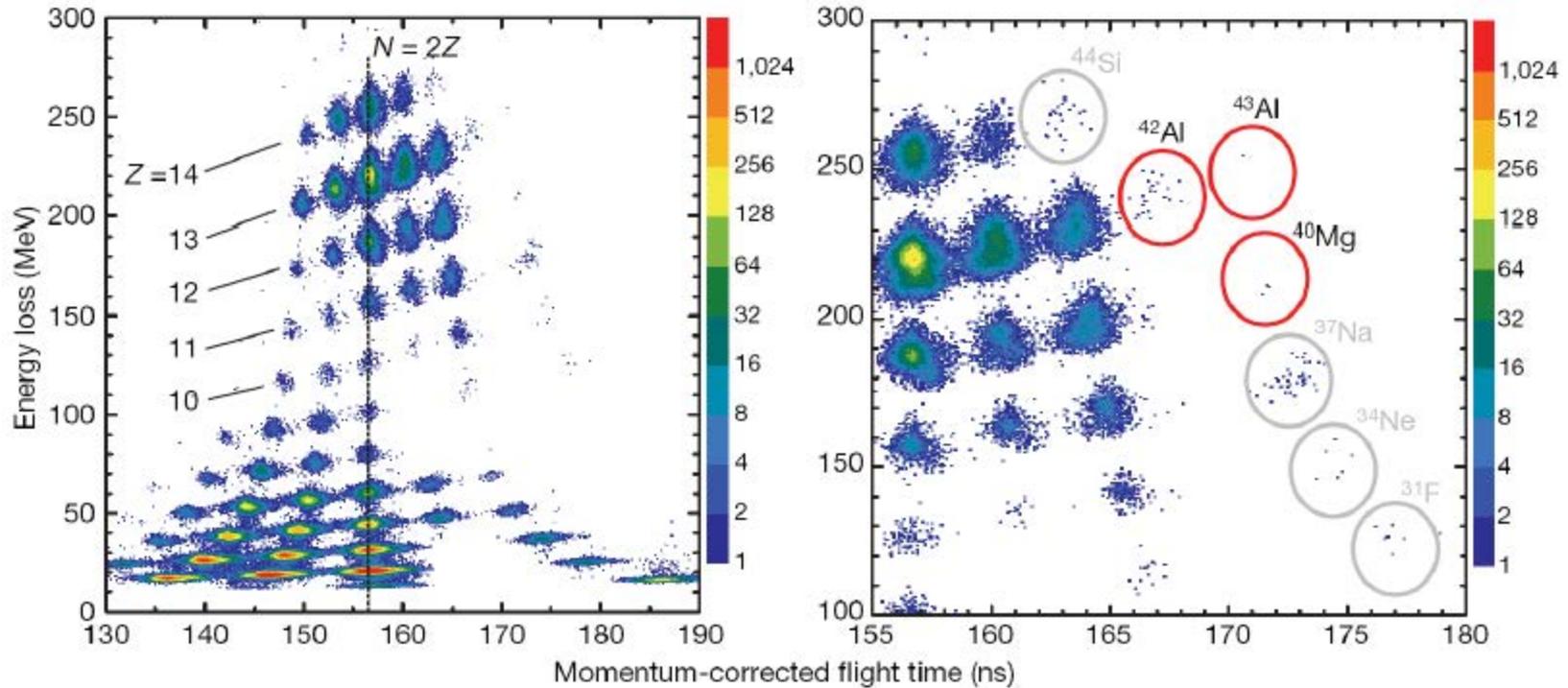
The limits of existence are defined by the proton and neutron driplines

$S_n$  (or  $S_p$ ) become positive  $\rightarrow$  neutron/proton are not bound; emission does not require energy input

At the neutron dripline, the definition is fairly straightforward – proton dripline, a little more complicated...



# Production of $^{40}\text{Mg}$



7.6 days of data at a primary beam rate of  $5 \times 10^{11}$  particles/second  
→ 3  $^{40}\text{Mg}$ , 23  $^{42}\text{Al}$  and 1  $^{43}\text{Al}$

Absence of a nucleus also provides information –  $^{26}\text{O}$  and  $^{28}\text{O}$   
for instance, or even  $^8\text{Be}$

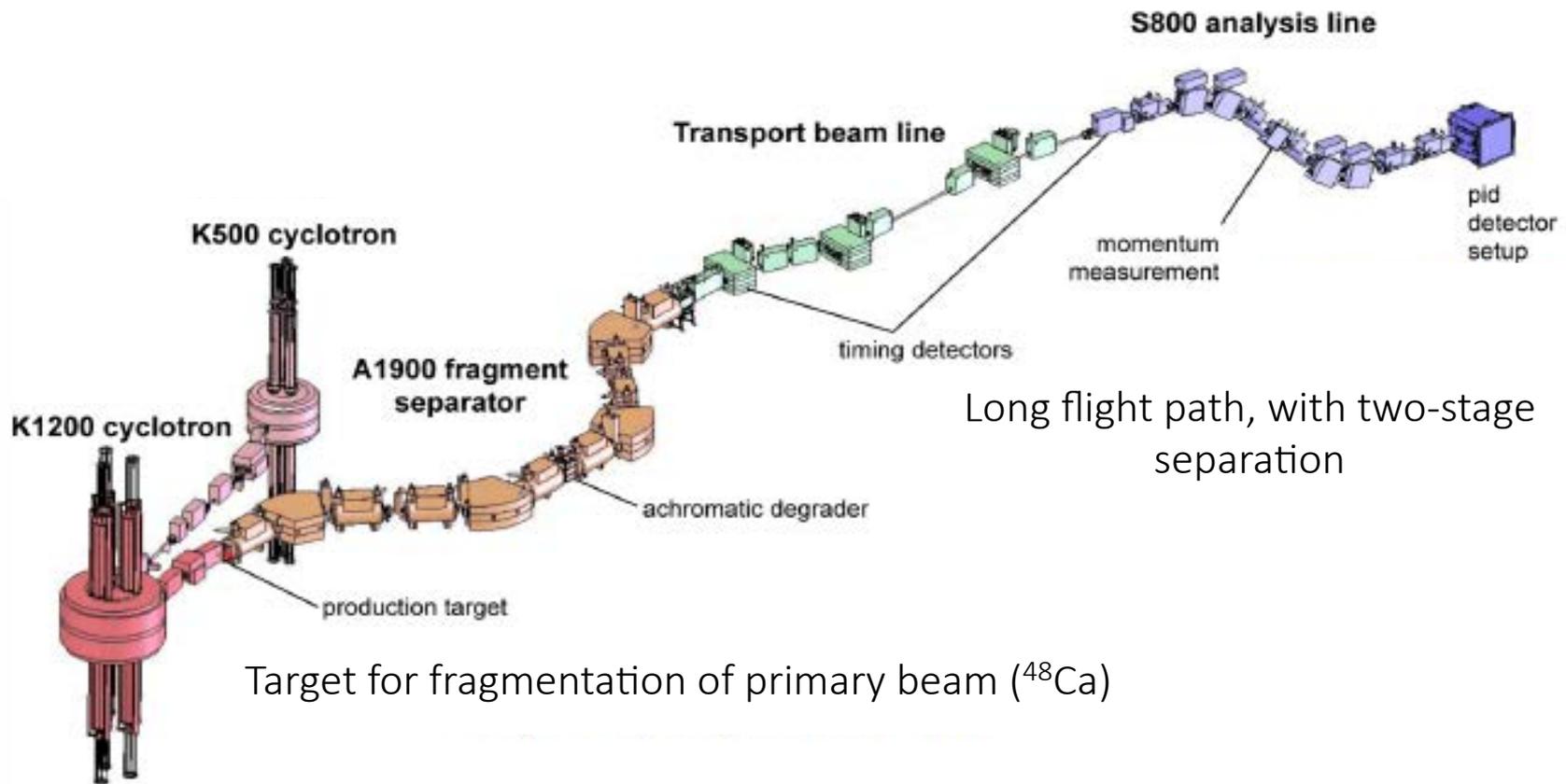
T. Baumann et al., Nature 449, 1022 (2007)

# How was it done?

Need to make and uniquely identify the nucleus – most often use a combination of time-of-flight, and energy loss.

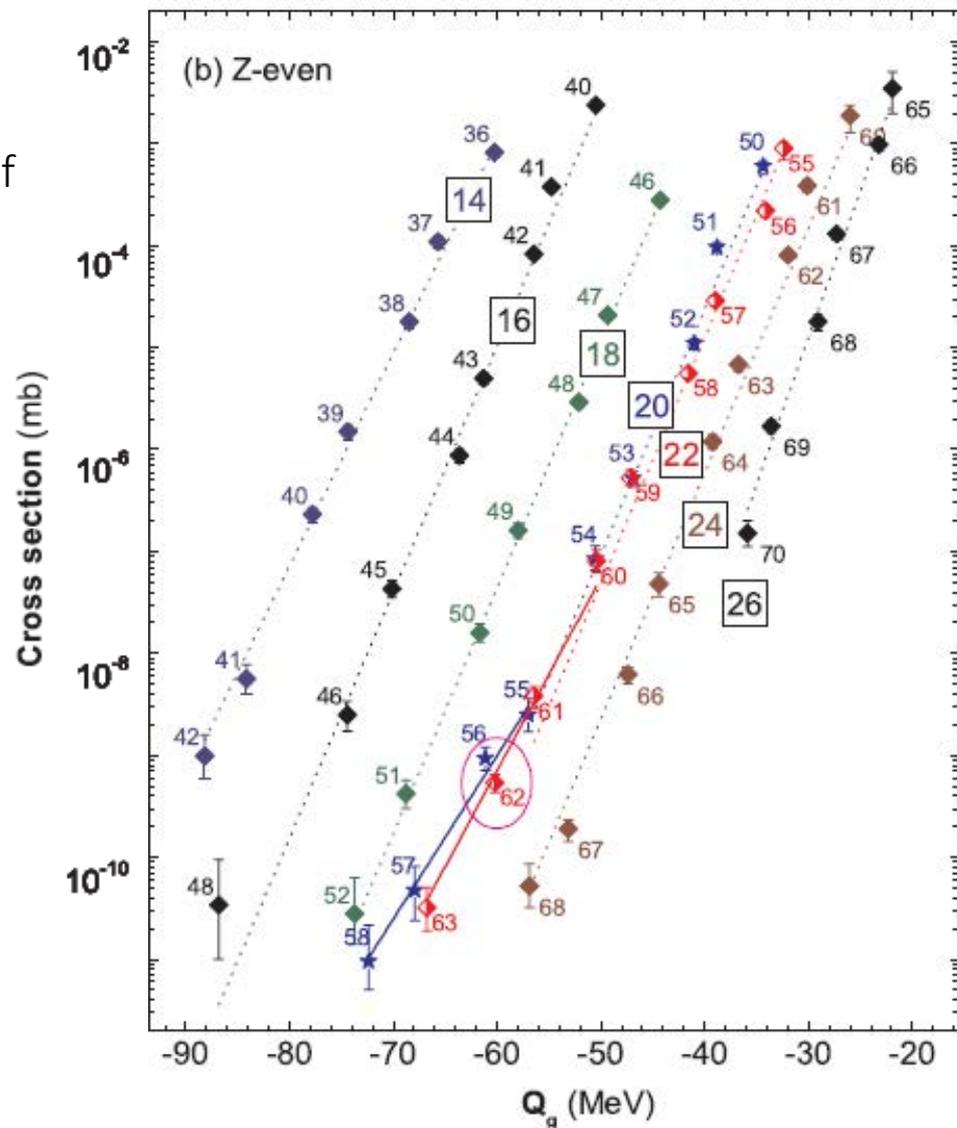
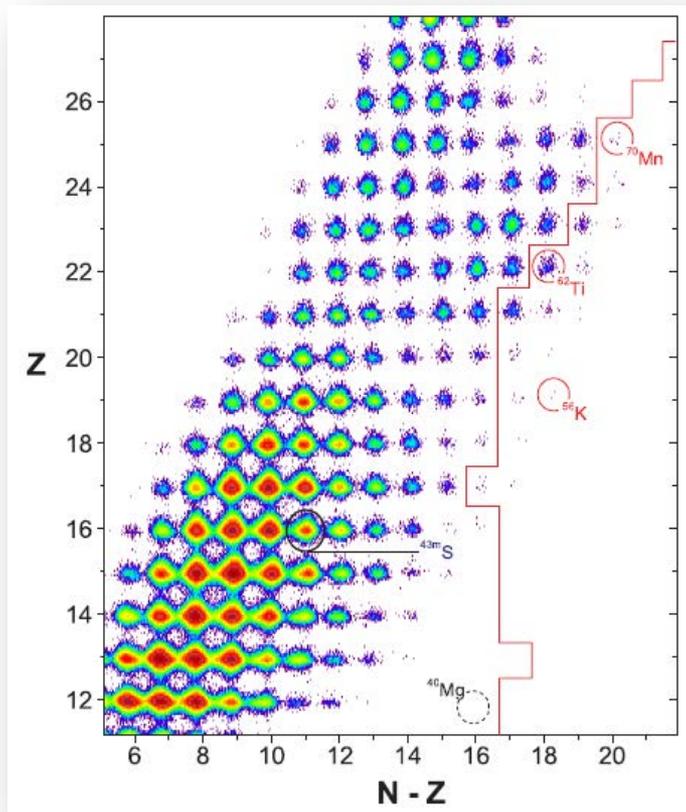
$$\text{Energy Loss} \propto Z^2$$

$$\text{Time of flight} \propto A/Z, \text{ flight path length and magnetic rigidities}$$



# Fragmentation cross-sections

A change in the trend of fragmentation cross-sections indicates a change in the binding – enhanced binding suggestive of a change in nuclear structure?



O. Tarasov et al., PRL 102, 142501 (2009)

# Summary

- Nuclear masses are a fundamental observable (and physical quantity) characterizing a nucleus, and systematics can indicate changes in nuclear shell structure
- Exotic nuclei away from stability can be produced in a number of techniques, each with different pros and cons
  - ISOL (Isotope separation online)
  - Fragmentation
  - Fission sources
- Nuclear masses can be measured in a variety of techniques, more appropriate to certain lifetime regimes, etc.