Heavy Ion Physics Lecture 2

Thomas K Hemmick Stony Brook University

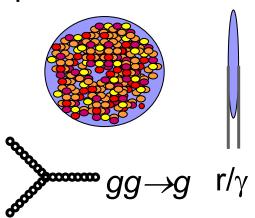
CMS Preliminary GLV. div dy - 400 **Outline of Lecture** GI₂V: dN₂/dy = 1400 PbPby 533 (2.76) TeV STA What have we done? SPS **Energy Density** CMS preliminary **Initial Temperature** Systematic uncertainty **Chemical & Kinetic Equilibrium System Size** 3020490 50 601070 Is There a There There? p_ Photon E_ (GeV) Strong co CMS PbPb $\sqrt{s_{NN}}$ = 2.76 TeV The Medium & The Probe Ldt = 7.2 ub ", > 10 GeV/c, |\eta"| < 2.4 **High Pt Suppression Control Experiments:** γ_{direct} CMS PbPb 7.2 µb⁻¹ at √s_{sex} = 2.76 Te What is It Like? **Azimuthally Anisotropic Flow Hydrodynamic Limit Heavy Flavor Modification Recombination Scaling** slirninary10% Is the matter exotic? **Quarkonia, Jet Asymmetry, Color Glass Condensate** What does the Future Hold? Stony Brook University

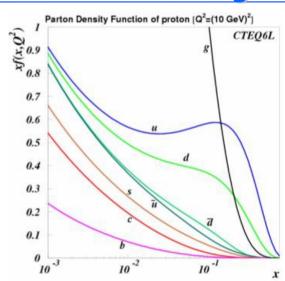
LHC Experiments



Could Suppression be Merely from the PDFs?

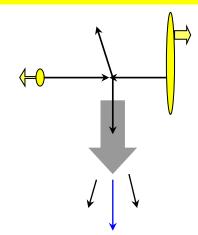
probe rest frame

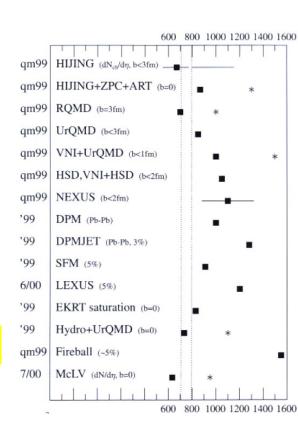




- The lower in x one measures, the more gluons you find.
- At some low enough x, phase space saturates and gluons swallow one another.
- Another novel phase:Color GlassCondensate

Control Experiment



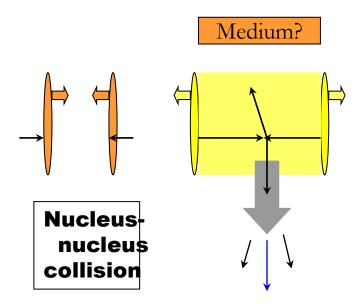






STONY d+Au Control Experiment 5 BROWK



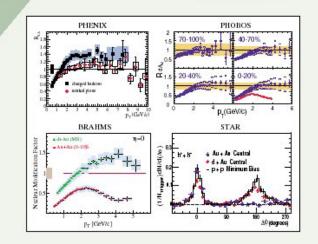


- Collisions of small with large nuclei qui
- Small + Large distinguishes all initial a

PHYSICAL REVIEW **ETTERS**

Articles published week ending 15 AUGUST 2003

Volume 91, Number 7

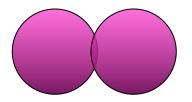


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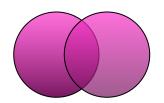


Terminology

Peripheral Collision



Semi-Central Collision



Central Collision

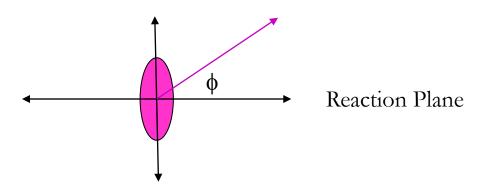


100%

Centrality

0%

- Centrality and Reaction Plane determined on an Event-by-Event basis.
- N_{part}= Number of Participants
 - \Box 2 \rightarrow 394
- □ N_{coll} = # Collisions
 - □ **1→1000**



Fourier decompose azimuthal yield:

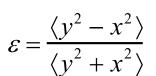
$$\frac{d^3N}{d\phi dp_{T_6}dy} \propto \left[1 + 2v_1\cos(\phi) + 2v_2\cos(2\phi) + \dots\right]$$

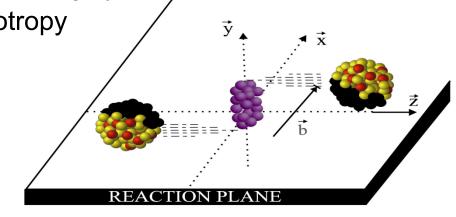
What is it Like? "elliptic flow"

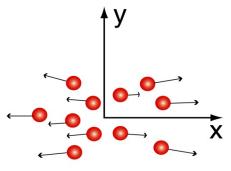
Origin: spatial anisotropy of the system when created, followed by multiple scattering of particles in the evolving system spatial anisotropy → momentum anisotropy

v₂: 2nd harmonic *Fourier* coefficient in azimuthal distribution of particles with respect to the reaction plane

Almond shape overlap region in coordinate space



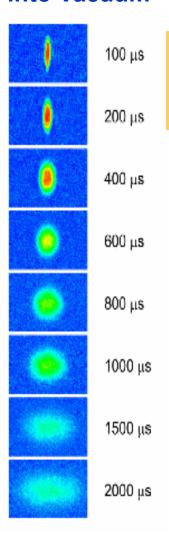




$$v_2 = \langle \cos 2\phi \rangle$$
 $\phi = \arctan \frac{p_y}{p_x}$

Anisotropic Flow

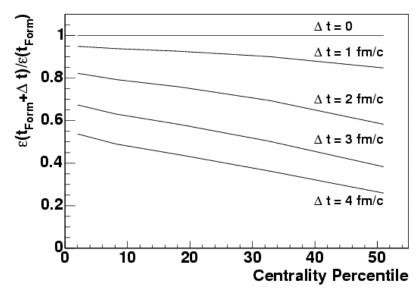
Liquid Li Explodes into Vacuum



Position Space anisotropy (eccentricity) is transferred to a momentum space anisotropy visible to experiment

- Gases explode into vacuum uniformly in all directions.
- Liquids flow violently along the short axis and gently along the long axis.
- We can observe the RHIC medium and decide if it is more liquid-like or gas-like

Process is SELF-LIMITING Sensitive to the initial time



Delays in the initiation of anisotropic flow not only change the magnitude of the flow but also the centrality dependence increasing the sensitivity of the results to the initial time.

Fourier Expansion

$$\frac{1}{p_{T}} \frac{d^{3}N}{dp_{T} d\phi dy} = \frac{1}{2\pi p_{T}} \frac{d^{2}N}{dp_{T} dy} \left[1 + 2v_{1}(p_{T}, y) \cos(\phi) + 2v_{2}(p_{T}, y) \cos(2\phi) + \dots \right]$$

here the sin terms are skipped by symmetry agruments.

□ For a symmetric system (AuAu, CuCu) at y=0, v_{odd} vanishes

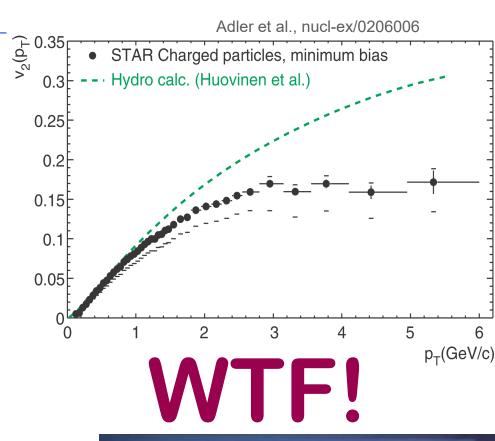
$$\frac{1}{p_T} \frac{d^3 N}{dp_T d\phi dv} = \frac{1}{2\pi p_T} \frac{d^2 N}{dp_T dv} \left[1 + 2v_2(p_T) \cos(2\phi) + 2v_4(p_T) \cos(4\phi) + \dots \right]$$

 v₄ and higher terms are non-zero and measured but will be neglected for this discussion.

$$\frac{1}{p_{T}} \frac{d^{3}N}{dp_{T} d\phi dv} = \frac{1}{2\pi p_{T}} \frac{d^{2}N}{dp_{T} dv} [1 + 2v_{2}(p_{T})\cos(2\phi)]$$

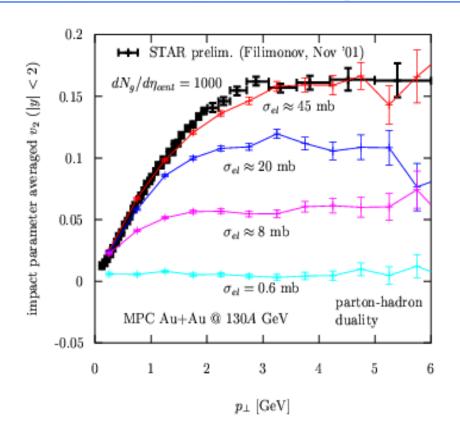
Huge v₂!

- Hydrodynamic limit exhausted at RHIC for low p_T particles.
- Can microscopic models work as well?
- Flow is sensitive to thermalization time since expanding system loses spatial asymmetry over time.
- Hydro models require thermalization in less than τ=1 fm/c





What is needed, partonically for v₂?



parton transport solutions via

MPC 1.6.0 [D.M. & Gyulassy, NPA 697 ('02)]

$$p^{\mu}\partial_{\mu}f_{i} = S_{i} + C_{i}^{2 \to 2}[f] + \dots$$

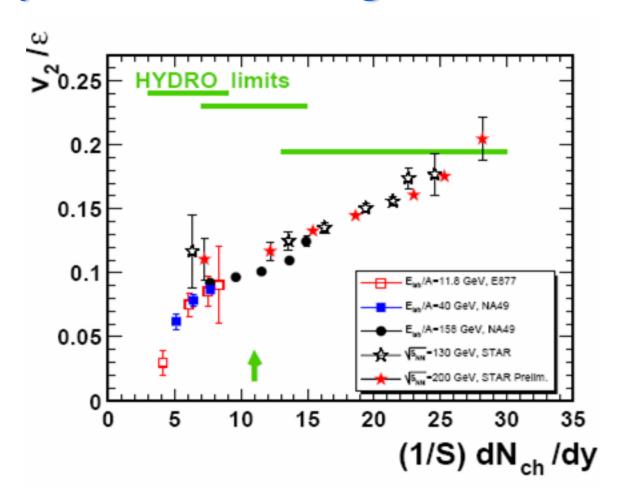
minijet initial conditions $1g
ightarrow 1\pi$ hadronization

Huge cross sections!!

- saturation pattern can be reproduced with elastic $2 \to 2$ interactions, requires large opacities $\sigma_{el} \times dN_g/d\eta \approx 45000$ mb \gg pQCD (3 mb $\times 1000$)
 - large opacities also suggested by pion HBT data [D.M & Gyulassy, nucl-th/0211017]

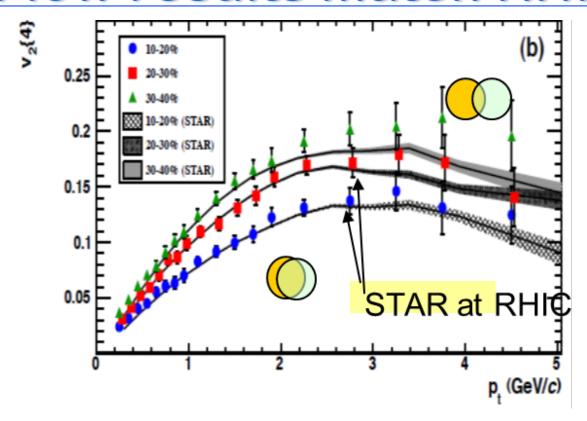
if
$$(\pi r^3 = 45 \text{ mb}) \{r = 1.2 \text{ fm}\};$$

Comparison to Hydro Limit



- Hydro limit drops with energy.
- RHIC "exhausts" hydro limit.
- Does the data flatten to LHC or rise?

LHC Flow results match RHIC

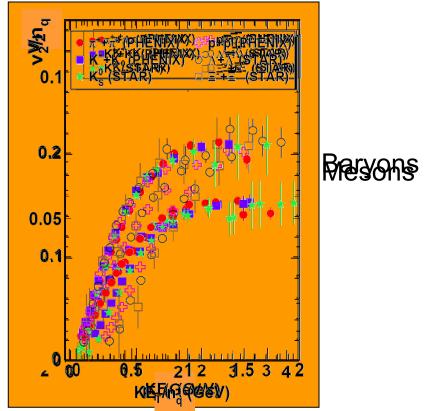


- Magnitude of flow as a FUNCTION of p_T is nearly exactly the same as at RHIC.
- LHC data reach to very high moments (v₆).

What else we can get from Hydro?

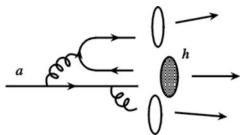
So far we have tracked the hydrodynamic evolution of the system back in time to the initial state. Let now Hydro do something good for us.

Approximately: $\partial_{\nu} T^{\mu\nu} = 0 \rightarrow \int \nabla P \, dV = \Delta E_{K} \cong m_{T} - m_{0} \equiv \Delta K E_{T} = \sqrt{p_{T}^{2} + m_{0}^{2}}$



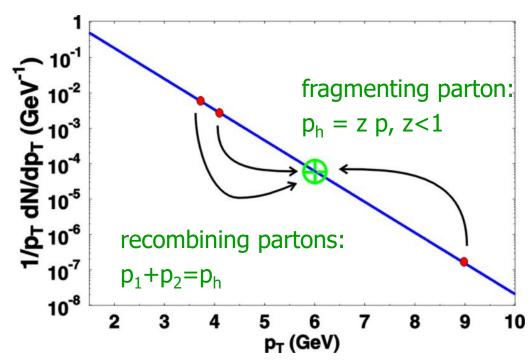
v₂ for different m₀ shows good agreement with "ideal fluid" hydrodynamics An "ideal fluid" which knows about quarks!

Recombination Concept

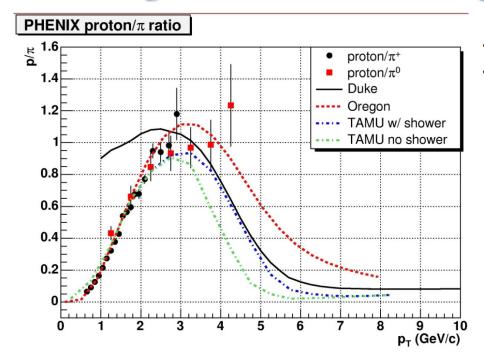


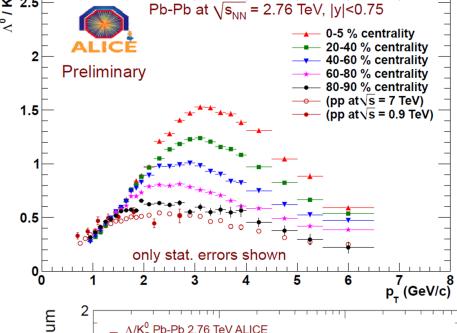
$$E \frac{dN_{\rm h}}{d^3P} = \int_0^1 \frac{dz}{z^2} \frac{E}{z} \frac{dN_a}{d^3(P/z)} D_{\alpha \to h}(z)$$

- for exponential parton spectrum, recombination is more effective than fragmentation
- baryons are shifted to higher p_t than mesons, for same quark distribution
- understand behavior of protons!

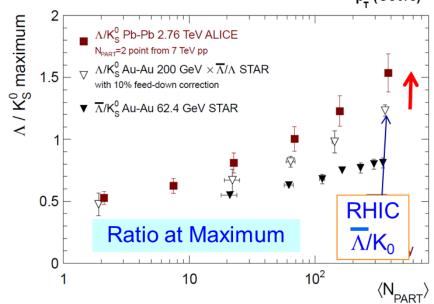


Baryon Anomaly

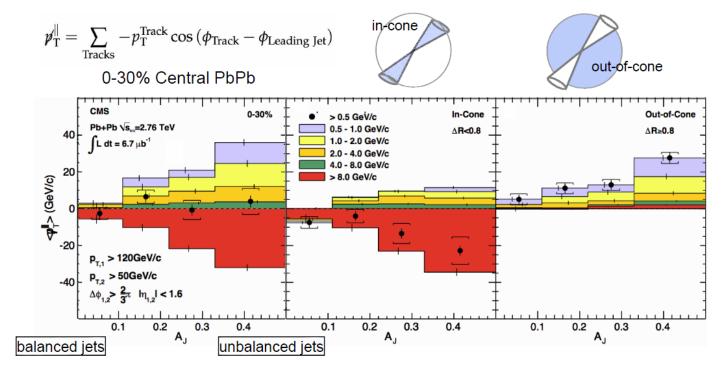




- Recombination models assume particles are formed by the coalescence of "constituent" quarks.
- Explain baryon excess by simple counting of valence quark content.



Where does the Energy: LHC

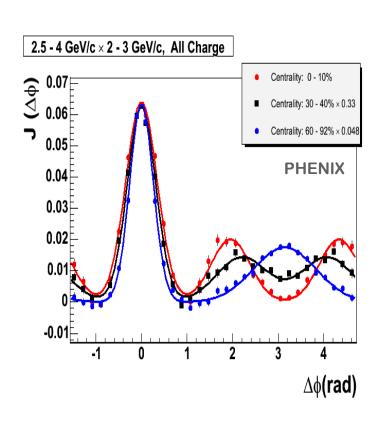


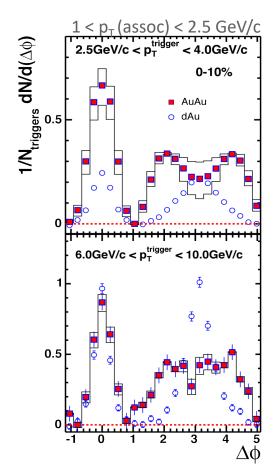
Low p_T, full acceptance Momentum is balanced In-cone large momentum Out-off-cone low p_T particles imbalance at high p_T Consistent with calorimetry

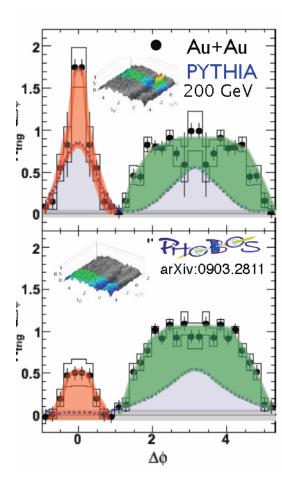
balance the complete event

- **Outside of large cone (R=0.8)**
- **Carried by soft particles**

Away Jet cannot "Disappear"





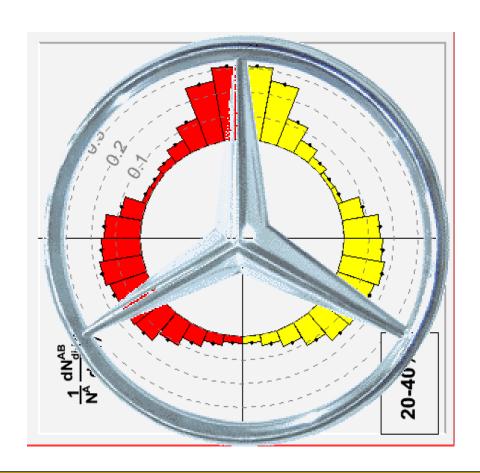


- Energy conservation says "lost" jet must be found.
- "Loss" was seen for partner momenta just below the trigger particle...Search low in momentum for the remnants.

Correlation of soft ~1-2 GeV/c jet partners

Emergence of a Volcano Shape

"split" of away side jet!







Strings: Duality of Theories that Look Different

Tool in string theory for 10 years

Strong coupling in one theory corresponds to weak

coupling in other theory

Theory A

AdS/CFT duality (Anti deSitter Space/ Conformal field theory)

QGP (in QCD)





Finite temperature gauge theory ⇔ Black hole in AdS space at strong coupling (N=4 SYM)



 $\pi T x_{\perp}$ -15 $\pi T x_{\rm H}$

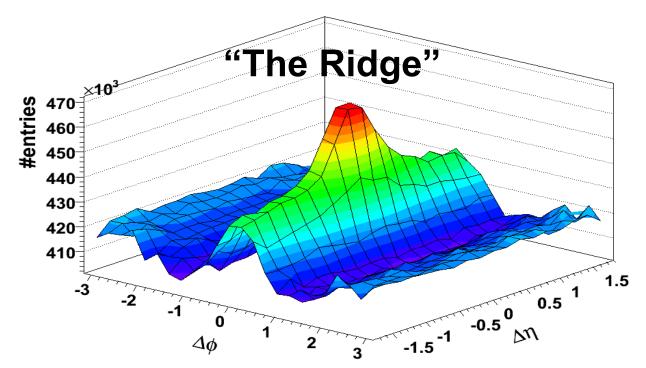
Calculated from AdS/CFT Duality





thermal due to the Hawking radiation

Another Exotic Structure: Ridge



Is this bulk response to stimulus...long range flux tubes...v₃?

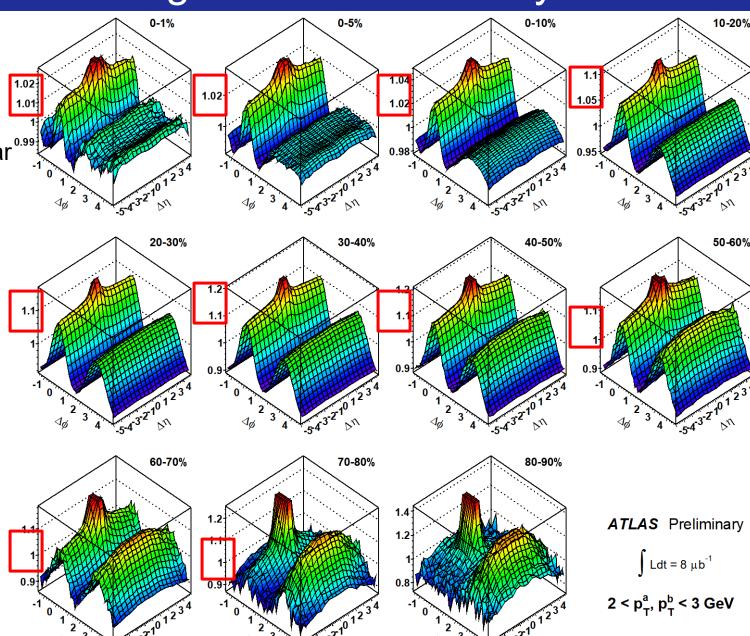
- 1. p_T spectra similar to bulk (or slightly harder)
- 2. baryon/meson enhancement similar to bulk
- 3. Scales per trigger like Npart similar to bulk

Rise and fall of "ridge/cone"—Centrality evolution

Pay attention to how long-range structures disappear and clear jet-related peaks emerge on the away-side

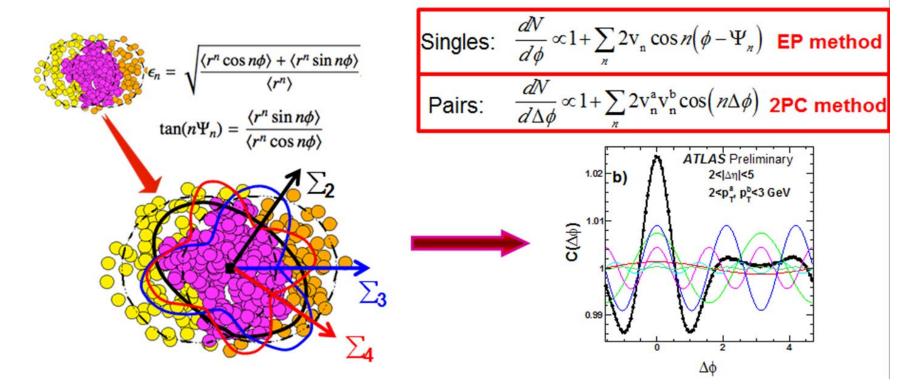
Strength of soft component increase and then decrease

Near-side jet peak is truncated from top to better reveal long range structure

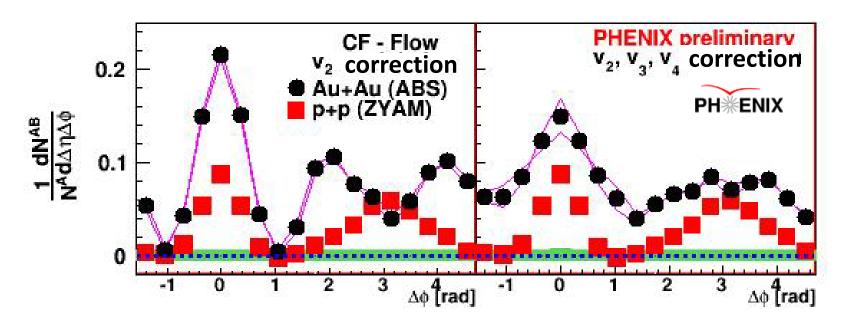


Ridge and Cone = v₃???

- Event Plane method yields <v_n> (v_{odd}=0).
- 2-particle yields SQRT(<v_n²>) (v_{odd}>0).
- How to disentangle:
 - □ PHENIX = EP method + factorization.
 - □ ATLAS = Rapidity OUTSIDE other Jet.
 - □ Everyone else = Factorization.



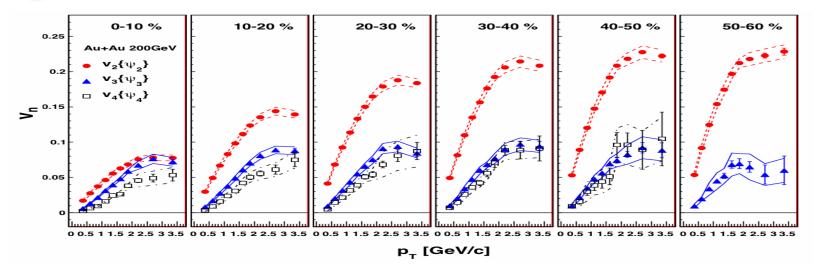
v₃ explains double-hump



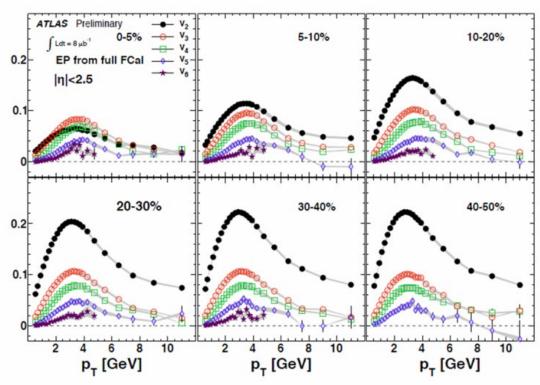
- \square V_2 correction only
 - double-hump

- $\square V_2, V_3, V_4$ correction
 - double-hump disappeared
 - Peak still broadened

Higher order moments

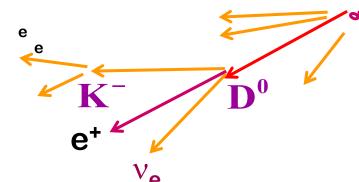


- Higher order moments can be measured WRT their own "reaction plane".
- Determines how initial state fluctuations are carried by fluid to final state.
- Higher order moments will serve to provide strong constraint on viscosity.



How can charm (bottom) be measured?

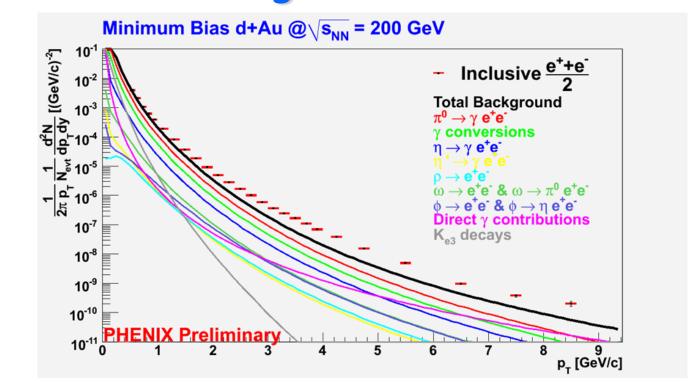
- ideal (but challenging)
 - \Box direct reconstruction of charm decays (e.g. $D^0 \to K^-\pi^+$)
 - much easier if displaced vertex is measured (PHENIX upgrade)
- □ alternative (but indirect)
 - contribution of semi leptonic charm decays to
 - single lepton spectra
 - lepton-pair spectra



$$\frac{D^0 \to K^- \ell^+ \nu_e}{D^0 \to K^+ \ell^- \overline{\nu_\ell}}$$

$$\frac{D^0 \to K^- \ell^+ \nu_e}{\overline{D^0} \to K^+ \ell^- \overline{\nu_\ell}} \quad \left\{ \begin{array}{l} D^0 \overline{\overline{D^0}} \to e^+ e^- K^+ K^- \nu_e \overline{\nu_e} \\ \overline{D^0} \overline{\overline{D^0}} \to e^- \mu^+ K^+ K^- \overline{\nu_e} \nu_\mu \\ \overline{D^0} \overline{\overline{D^0}} \to \mu^+ \mu^- K^+ K^- \nu_\mu \overline{\nu_\mu} \end{array} \right.$$

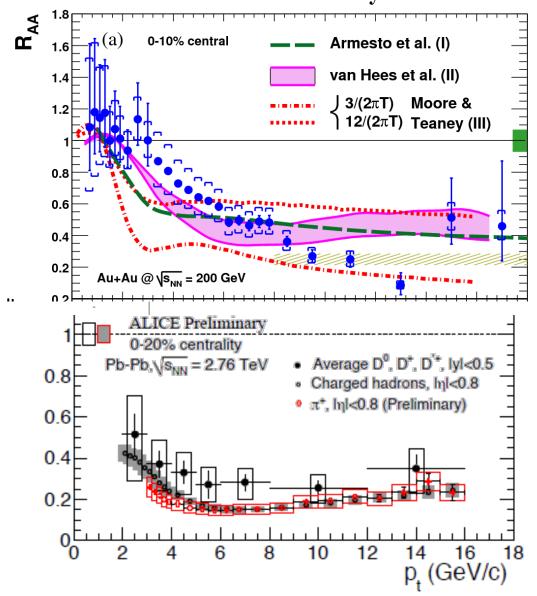
Inferred Heavy Flavor



- Measurement inclusive e[±].
- □ **Measure** π^0 , η^0
- Construct "Cocktail" of electron sources other than c/b
 - light hadron decays
 - photon conversions
- Subtract e[±] "cocktail" leaves e from c/b.

Hard Probes: Open Heavy Flavor

Electrons from c/b hadron decays



Calibrated probe?

pQCD now predicts cross section well Total charm follows binary scaling

Strong medium effects

Significant suppression

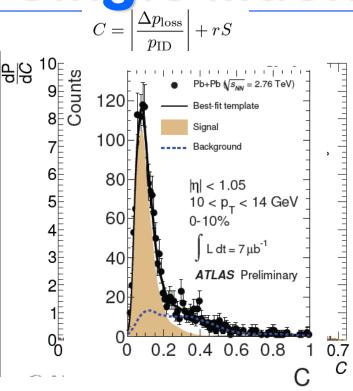
Upper bound on viscosity!

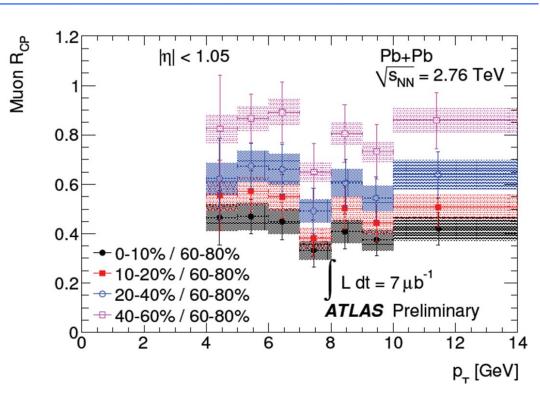
Little room for bottom production

Limited agreement with energy loss calculations



Single Muons from ATLAS



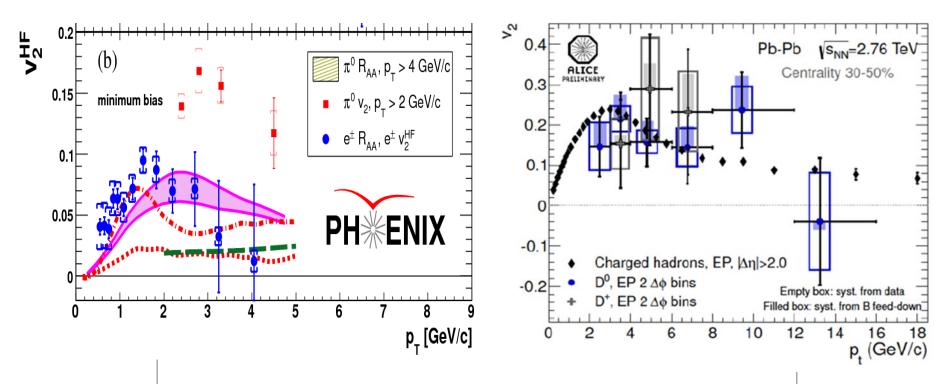


- High Momentum muons dominantly from heavy flavor.
- Eliminate unwanted background by statistical method.
- At these high momenta, the muons are likely dominated by bottom.
- Is there a limit to the power of the river?...Stay tuned.

Stony Brook University

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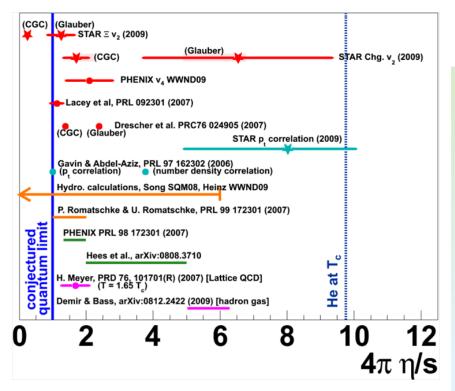
Heavy Flavor Quarks are Flowing!

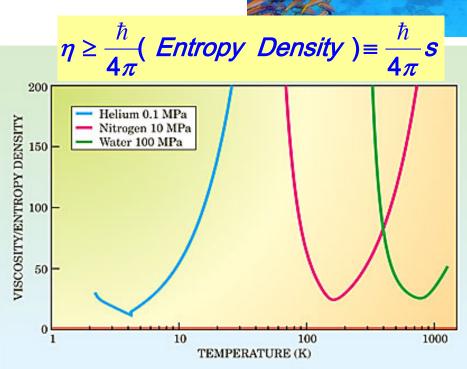


- We can imagine that the flowing QGP is a river that sweeps quarks.
- A "perfect fluid" is like a school of fish...all change direction at once.
- Our QGP river carries off heavy stones (not BOTTOM???)
- Requiring a model to SIMULTANEOUSLY fit R_{AA} and v_2 "measures" the η/s of the QGP fluid.



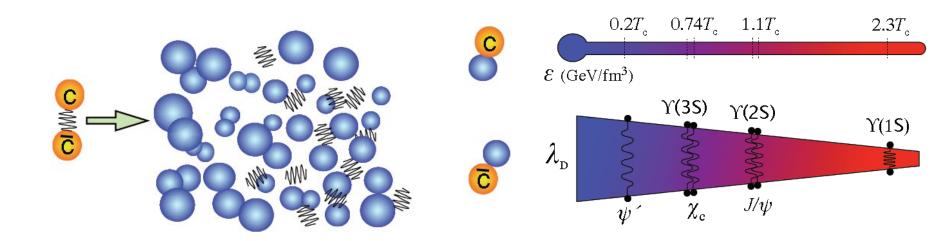
How Perfect is "Perfect"?





- □ RHIC "fluid" is at ~1-3 on this scale (!)
- The Quark-Gluon Plasma is, within preset error, the most perfect fluid possible in nature.
- High order v_n measurements to yield superb precision!

Quarkonia Production

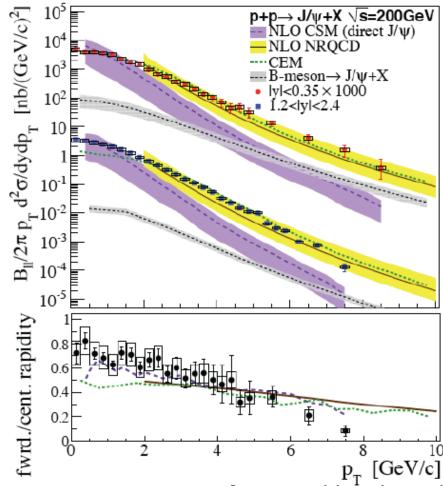


- J/psi Suppression by Quark-Gluon Plasma Formation,
 T. Matsui and H. Satz, Phys.Lett.B178:416,1986.
- If cc dissolved, unlikely to pair with each other.
- $\ \ \square$ Suppression of J/ Ψ and Y.
- Suppression driven by size of the meson as compared to the Debye Radius (radius of color conductivity)

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How is J/ψ formed in pp?

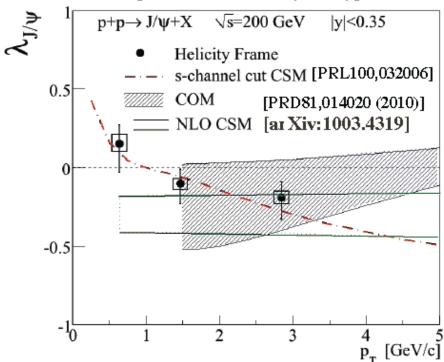
[arXiv:1105.1966]



• new measurement of J/ψ yield in the mid and forward rapidities

- only models with color octet formation describe the data
- \circ J/ ψ polarization measured to be small

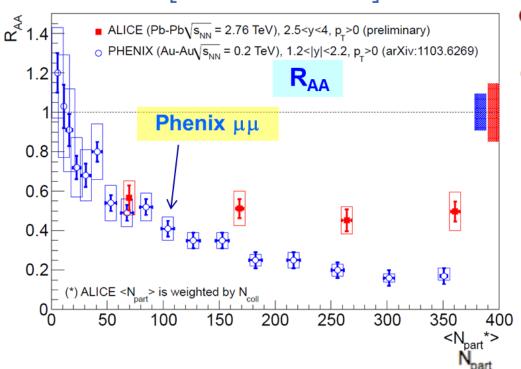
[PRD82,012001 (2010)]



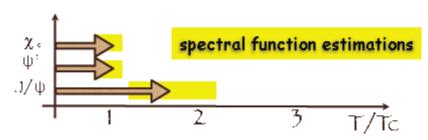
O color octet state may cross part of the nuclear matter as a pre-resonant state

J/ψ is suppressed (everywhere)

[arXiv:1103.6269v1]

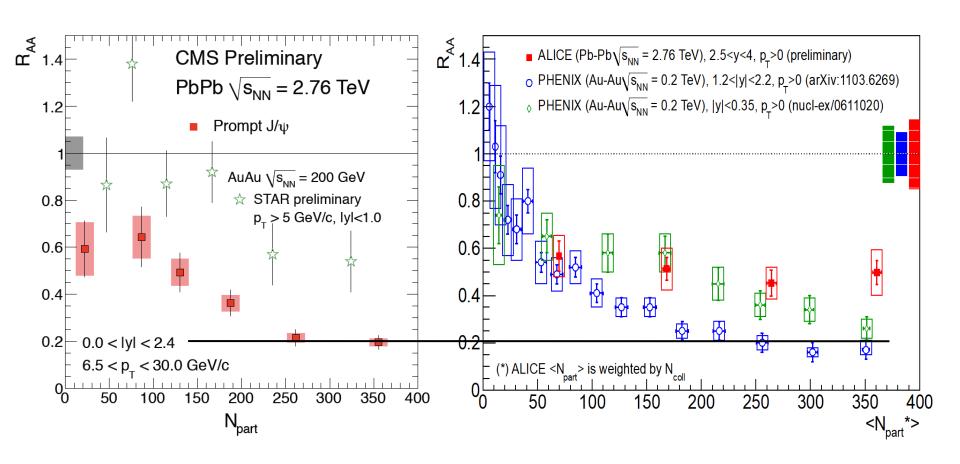


- Tc ~ 170 MeV
- inverse slope of thermal photons measured by PHENIX is
 221±28MeV [PRL104, 132301 (2010)]
- hydro models fitted to the thermal photon data suggest T_{init} ~300-600 MeV
- who survives?



 \circ if J/ ψ from ψ ' and χ_c fully suppressed R_{AA} drops to 0.6

LHC/RHIC comparison

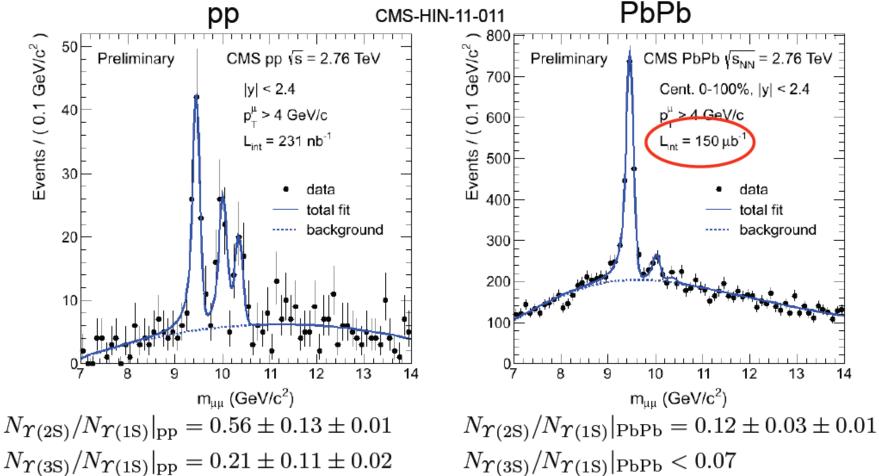


STAR (p_T >5 GeV) versus CMS (6.5< p_T <30 GeV)

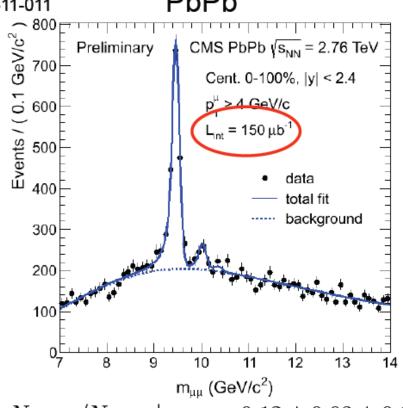
PHENIX ($p_T>0$ GeV) versus ALICE ($p_T>0$ GeV)

Caveat: Different beam energy and rapidity coverage; $dN_{ch}/d\eta(N_{part})^{LHC} \sim 2.1 \text{ x } dN_{ch}/d\eta(N_{part})^{RHIC}$

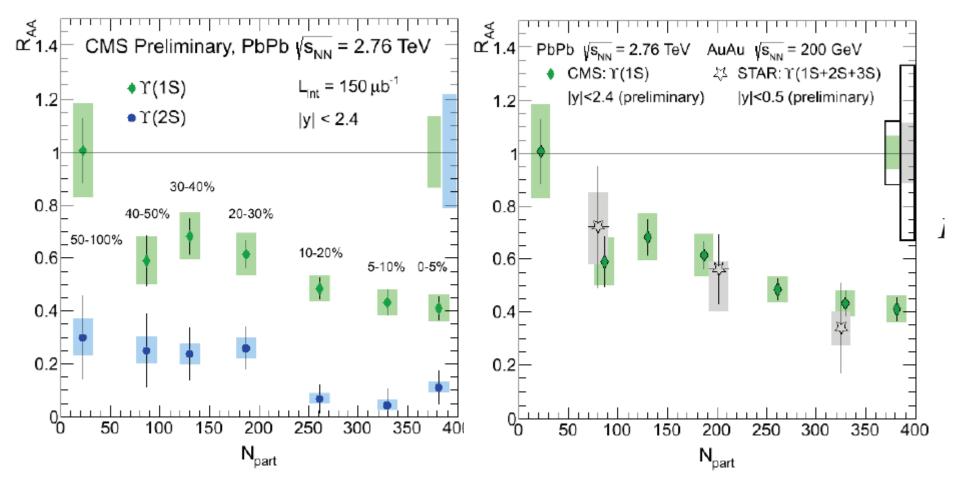
CMS: all the Y states separately.



- The data show that the 2s/3s are reduced compared to the 1s.
- This is first strong indication of sequential melting in QGP.
- Should yield screening length of our color conductor!



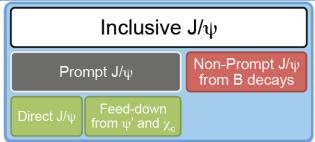
Upsilon Suppression



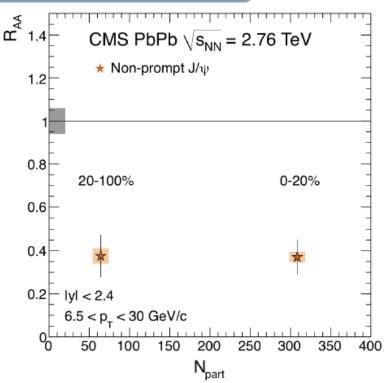
- Upsilon system is "cleaner" than the J/Psi.
- □ 1s state suffers from feed-down (~50%).
- Consistent with melting all Y except feeddown.

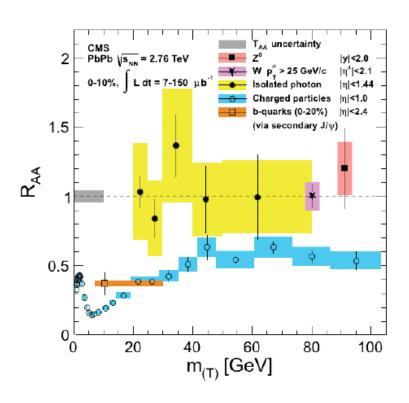
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J/Psi as Bottom Suppression?



CMS can separate out J/Psi which are daughter states of decays from B mesons.

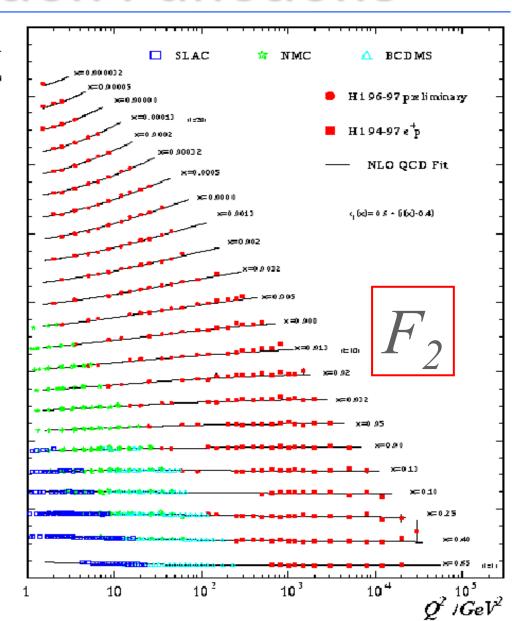




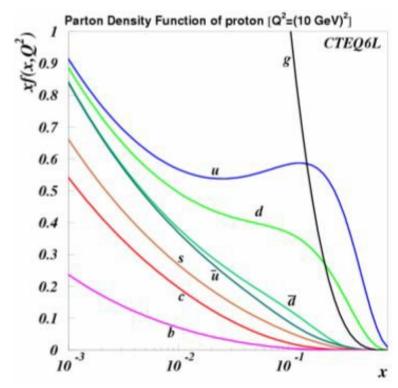
- These are a surrogate for a bottom quark.
- **Suppression same or less than \pi/charm?**

Parton Distribution Functions

- PDFs are measured by e-p scattering.
- Calculations (PYTHIA)
 use theoretically
 inspired forms guided
 by the data:
 - □ CTEQ 5M
 - □ others...
- Unitarity requires that the integral under the PDF adds up to the full proton momentum.
- Dirty Little Secret: The sum of the parts exceeds the whole!



Crisis in Parton Distributions!

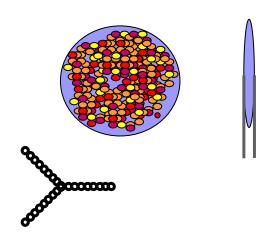


What happens if you pack too many gluons inside a box? probe rest frame Gluon Density Grows High Energy ANSWER: They eat each other.

Parton Distributions explode at low x.

The rise must be capped.

Glass at the Bottom of the Sea?



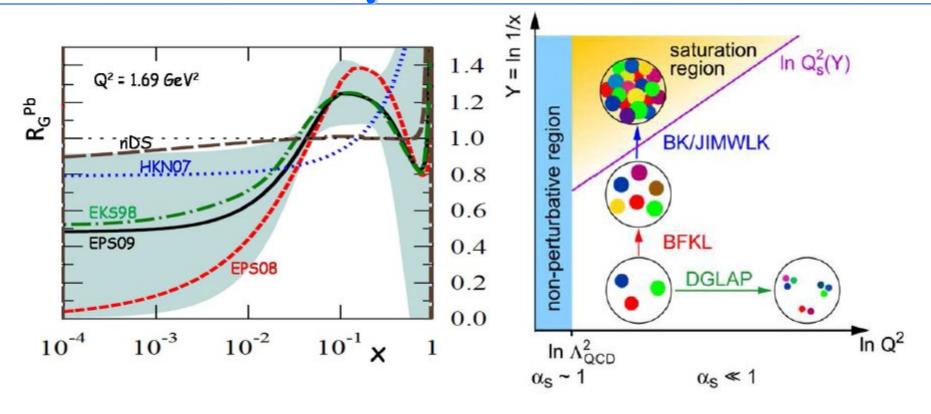
- Note that the gluon fusion reaction, g+g→g, "eats gluons".
- Its kind of like a fish tank:
 - When the fish eat their young, the tank never overfills with fish.

This implies that

nature has a maximal gluon density.

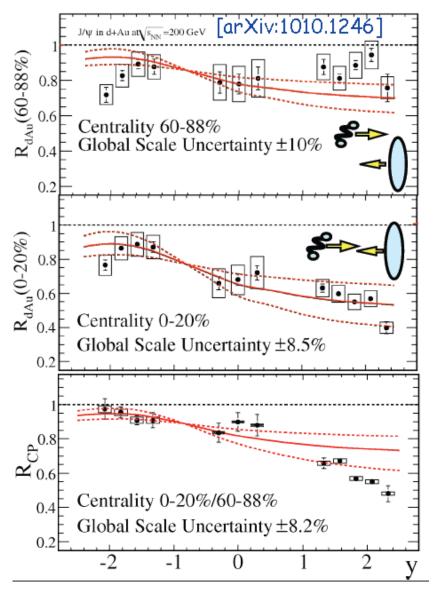
- Material exhibiting nature's ultimate gluon density is called Color Glass Condensate.
- The existence of this material would cap the gluon growth at low x, restoring unitarity
- The Bottom of the Sea Fuses Into Color Glass.

Nuclear Oomph...



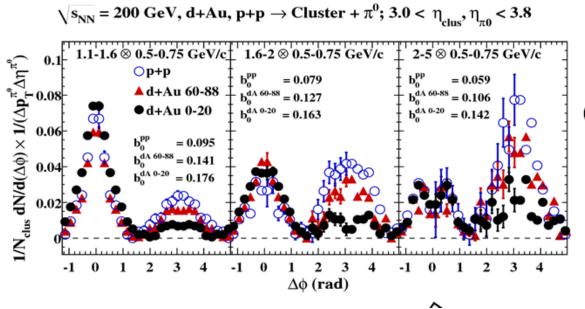
- A nucleus compresses more matter and makes the CGC easily accessible.
- Shadowing competes with CGC.
- Many believe that shadowing is simply "parameterized" CGC.

J/y complicated by CNM effects



- Electron-nucleus collisions are the most promising way to find CGC.
- Proton (deuteron)
 collisions are the best
 we have for now.
- A depletion in the low-x wave function of a Au nucleus decreases the number of scatterings in the deuteron direction.
- EPS09 shadowing fails.

Jets distinguish CGC from shadowing.

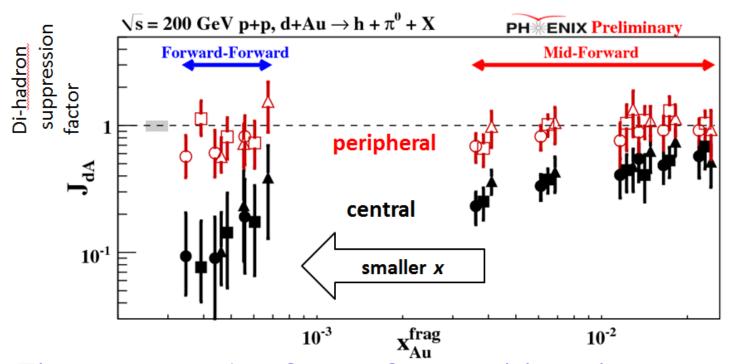


Color Glass Condensate?

new forward EM calorimeter $|\eta| = 3.0-3.8$

- The fundamental difference between the CGC model of cold nuclear matter and the shadowing model is the number of partons that scatter.
- Shadowing changes the PDF, but still does all physics as 1-on-1 parton scatterings.
- CGC allows one (from deuteron) against many (from glass), and thereby splits away-side jet into many small pieces.

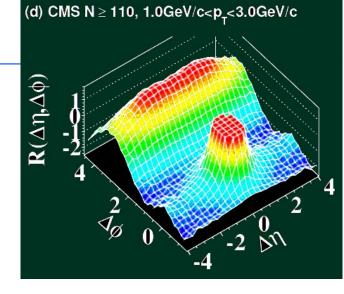
HUGE suppression in low X.



- □ The suppression factor from cold nuclear matter is a factor of ~10!
- The away-side jet "decorrelates".
- Jury still out:
 - Nearly all measurements follow CGC predictions.
 - Predictions are often qualitative.
- Electron-ion collisions will find the truth.

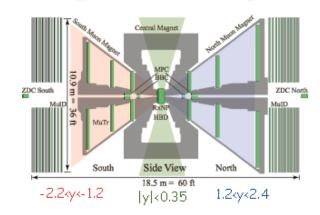
Summary

- Nuclear Collisions provide access to the collective color interaction.
- These provide a glimpse at aspects of the color force inaccessible through elementary collisions.



- Partonic matter just beyond the phase transition is a strongly-coupled plasma exhibiting explosive flow into the vacuum.
- String-theory has provided "Nature's lower bound" on η/s...a limit realized within error by sQGP.
- Nuclear collisions can provide access to dense color fields in cold nuclear matter that may exhibit CGC.
- Short time scales for thermalization challenge theory.

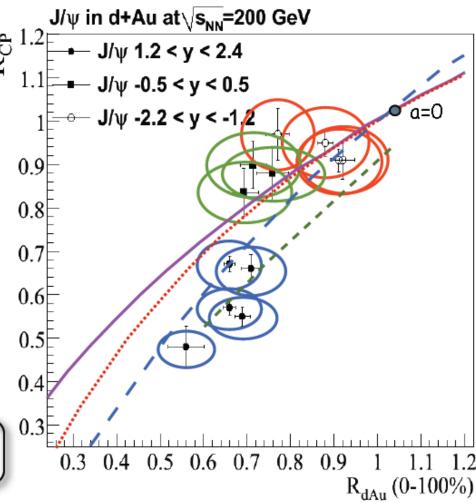
Length dependence of J/\psi



scan different values for the strength "a" in R_{dAu} formula

$$R_{dAu,i}(a) = \int f_i\left(r_T\right) M\left(r_T;a\right) dr_T$$
 $M(r_T;a) = e^{-a\Lambda(r_T)}$ exponential
 $M(r_T;a) = 1 - a\Lambda\left(r_T\right)$ linear
 $M(r_T;a) = 1 - a\Lambda\left(r_T\right)^2$ quadratic

nuclear modification requires a quadratic or higher order dependence



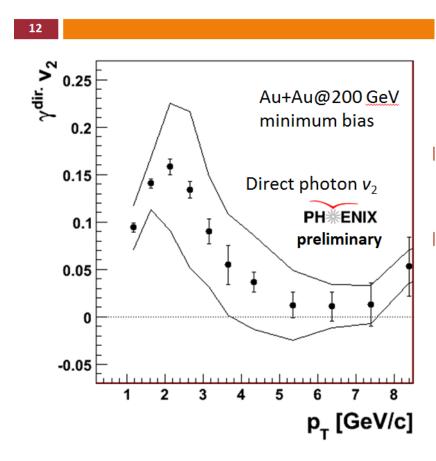
 by the way, reasonable agreement with CGC model as well

[Kharzeev and Tuchin, Nucl. Phys. A770, 40 (2006)]

SURPRISE!

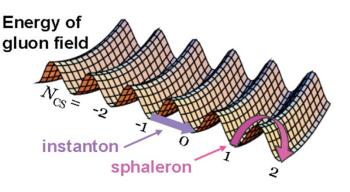
- The direct virtual photons measured by PHENIX have been associated with early stage thermal radiation.
- If true, they should show little flow.
- Surprise...they flow.
- We must take care in interpreting these photons...

Direct Photon v_2



Gauge fields possess non-trivial topology CHARACTERISTIC FORMS $TP_1(\theta) = rac{1}{4\pi^2} \{ heta_{12} \wedge \theta_{13} \wedge heta_{23} + heta_{12} \wedge \Omega_{12} + heta_{13} \wedge \Omega_{13} + heta_{23} \wedge \Omega_{23} \}$. Dima Kharzeev. QM2011

QCD vacuum is a superposition of states with different topology

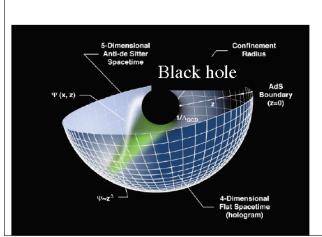


Transitions between such states create the local imbalance of chirality

Topological transitions are frequent in sQGP

Chern-Simons number diffusion rate at strong coupling

$$\Gamma = rac{(g_{
m YM}^2 N)^2}{256\pi^3} T^4$$
 D.Son,
A.Starinets hep-th/
020505



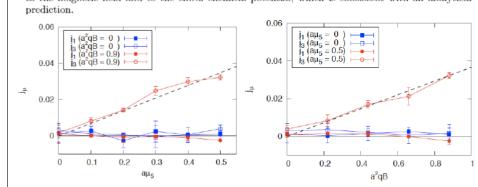
NB: This calculation is completely analogous to the calculation of shear viscosity that led to the "perfect liquid"

arXiv:1105.0385, May 3, 2011 Chiral magnetic effect in lattice QCD with chiral chemical potential

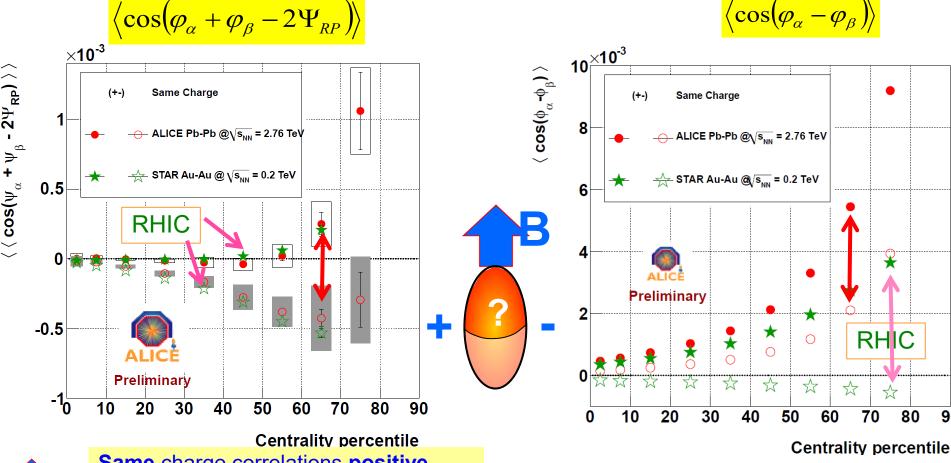
Arata Yamamoto

Department of Physics, The University of Tokyo, Tokyo 113-0033, Japan (Dated: May 3, 2011)

We perform a first lattice QCD simulation including two-flavor dynamical fermion with chiral chemical potential. Because the chiral chemical potential gives rise to no sign problem, we can exactly analyze a chirally asymmetric QCD matter by the Monte Carlo simulation. By applying an external magnetic field to this system, we obtain a finite induced current along the magnetic field, which corresponds to the chiral magnetic effect. The obtained induced current is proportional to the magnetic field and to the chiral chemical potential, which is consistent with an analytical



Chiral Magnetic Effect ('strong parity violation')



Same charge correlations positive

may decrease with √s

Opposite charge correlations negative RHIC: (++), (+-) different sign and magnitude

RHIC ≈ LHC

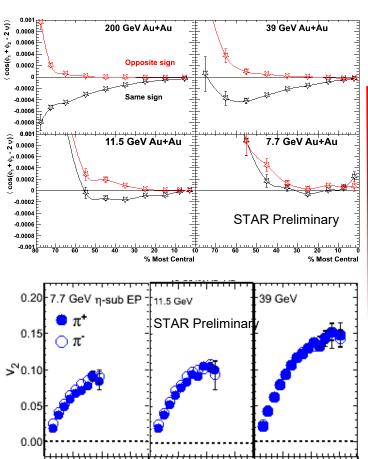
Local Parity Violation in 10¹⁷ Gauss magnetic Field?

LHC: (++),(+-) **same sign**, similar magnitude

Backup Slides

Dynamical Charge Correlations

Possible interpretations:



(A) If linked to LPV effect - de-confinement and chiral symmetry restoration. Absence of difference in correlations means absence of phase transition.

K. Fukushima et al, PRD 78, 074033 (2008)

Alternate Observables

(B) Charge asymmetry

LPV: $\langle A_+ A_- \rangle_{UD} < \langle A_+ A_- \rangle_{LR}$



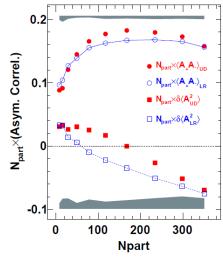
Reaction plane dependence balance function ~ difference between opposite and same charge correlations.

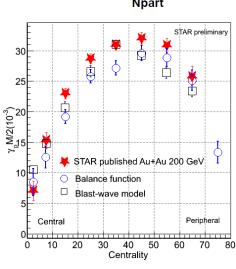
A. Bzdak, et al., PRC 83 (2011) 014905

S. Schlichting et al., PRC 83 (2011) 014913

Y. Burnier et al., arXiv:1103.1307

How to reconcile (A) with the fact $v_2(\pi^+) < v_2(\pi^-)$ at 7.7 GeV





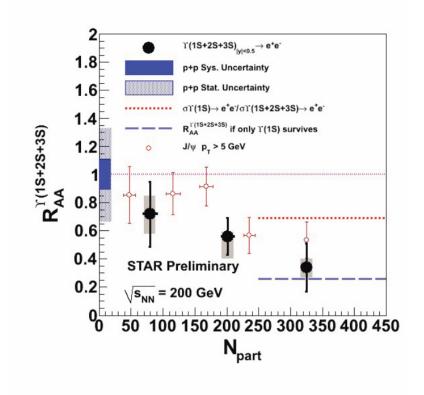
නෙහිතු)

p_{_} (GeV/c)

Suppression.

- 1s state should be too large to melt in the plasma.
- 2s/3s could be melted.
- Data are above bluedashed which would be consistent with only 1s survival and removal of nearly all 2s/3s.

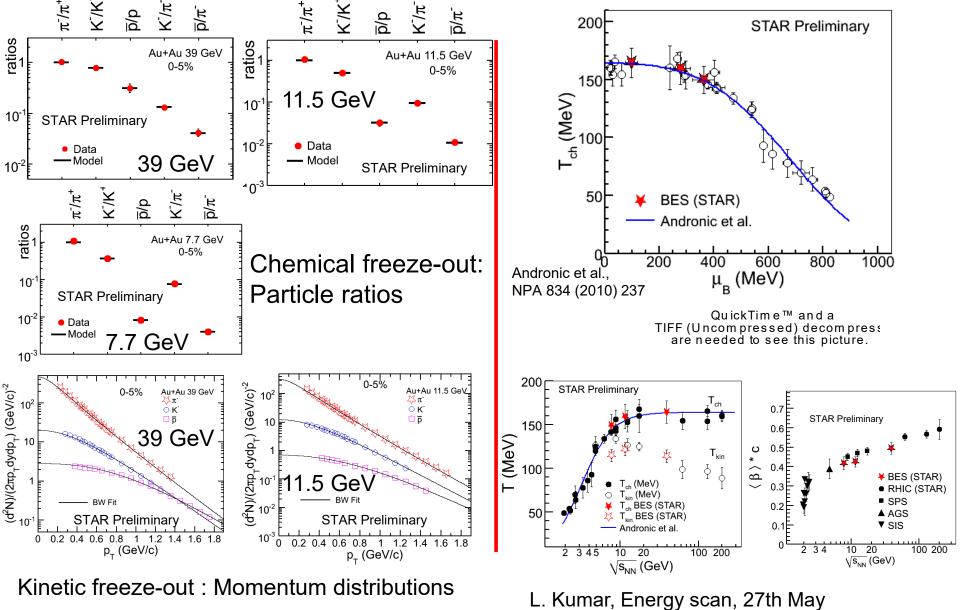
Y RAA





Freeze-out Conditions

QuickTime™ and a TIFF (Uncompressed) decompressor are needed to see this picture.

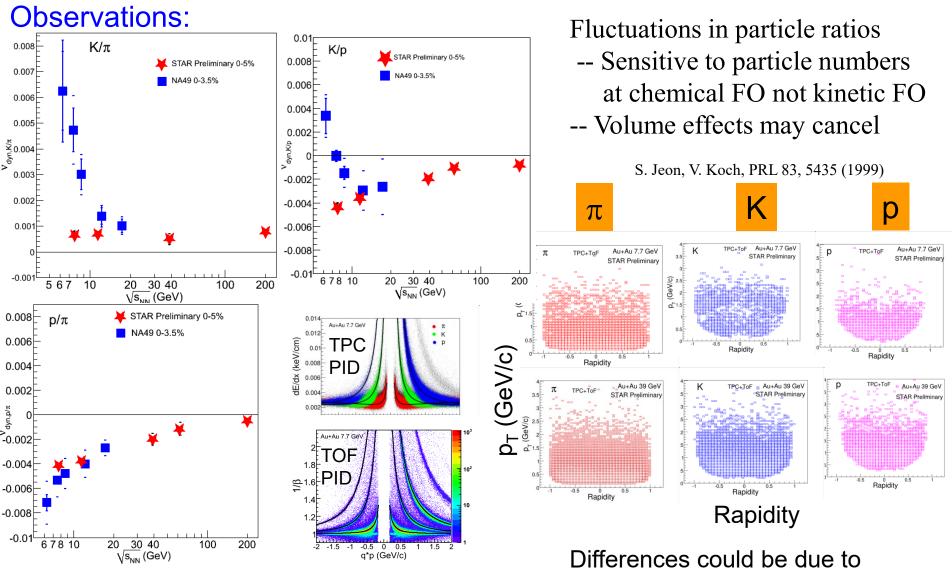


QM2011

Bedanga Mohanty



Particle Ratio Fluctuations



Constant or monotonic trends observed

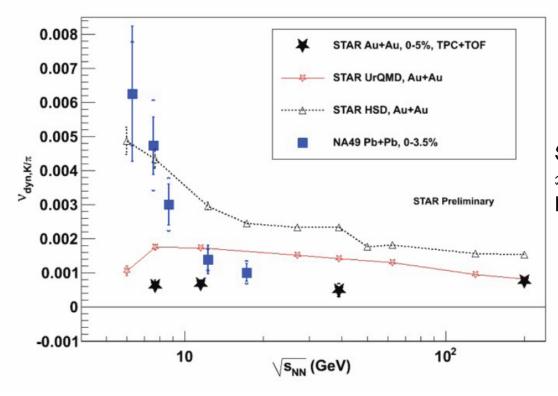
Apparent differences (results with Kaons) with SPS

QM2011 Bedanga Mohanty

Differences could be due to difference in acceptance and/or PID selections --- under discussion

fluct.

Particle ratio fluctuations

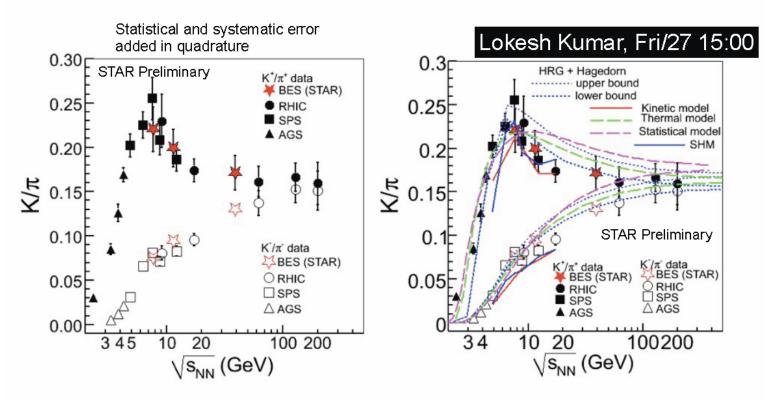


Terence Tarnowsky, Mon/23 16:00

STAR TPC+TOF π: 0.2 < p_T < 1.4 GeV/c K; 0.2 < p_T < 1.4 GeV/c

Data are still "horny"

K/π ratio

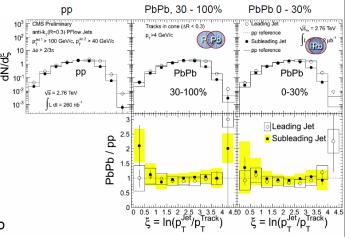


□ Can be naturally explained by change of strangeness production from \(\Lambda \text{K} \) to KK...

Fragmentation Function at LHC

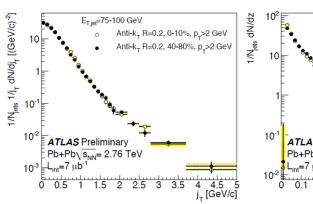


$$\xi = \ln \left(\frac{p_T^{Jet}}{p_T^{Track}} \right)$$



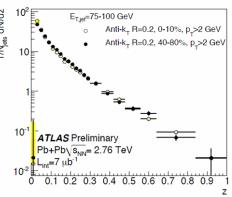
Fragmentation Functions

Compare PbPb to pp



p_T cut to suppress underlying event, and background subtracted using region outside jet cone

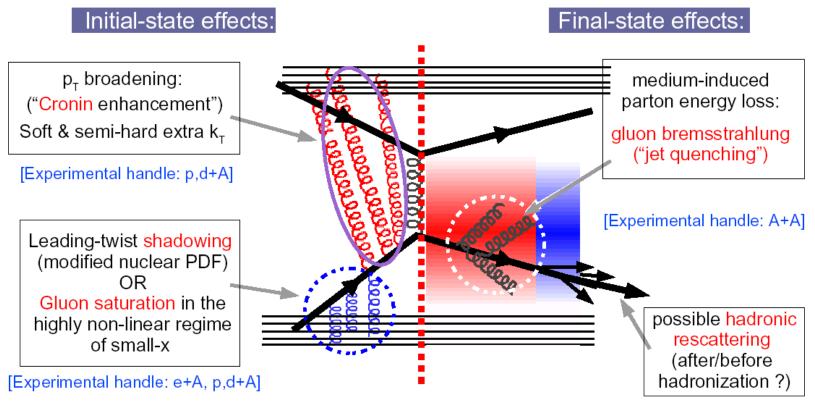
Yellow bands represent uncertainties from background subtraction



No strong modification of fragmentation functions between peripheral and central: surprising in a radiative energy loss scenario?

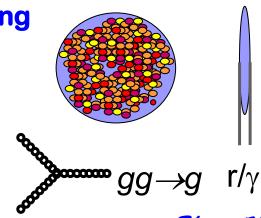
- Not modified!
- Need to be more quantitative to really understand differences from RHIC.





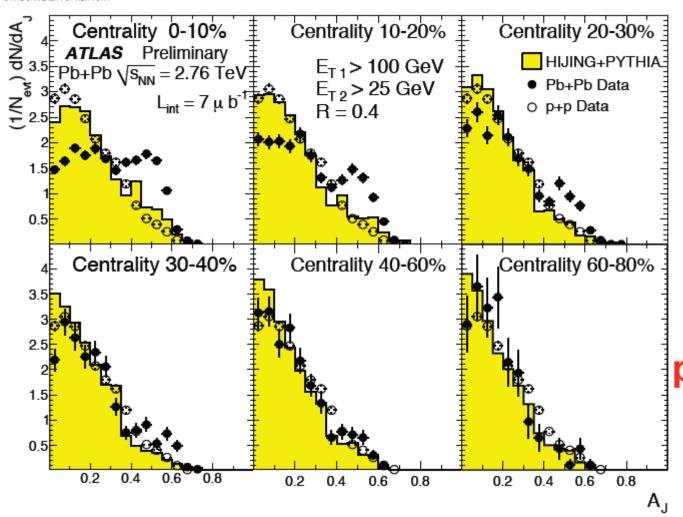
- Color Glass Condensate
- Gluon fusion reduces number of scattering centers in initial state.
- Theoretically attractive; limits DGLAP evolution/restores unitarity

probe rest frame









$$A_J = \frac{E_T^1 - E_T^2}{E_T^1 + E_T^2}$$

$$E_{T1} > 100 \ GeV$$

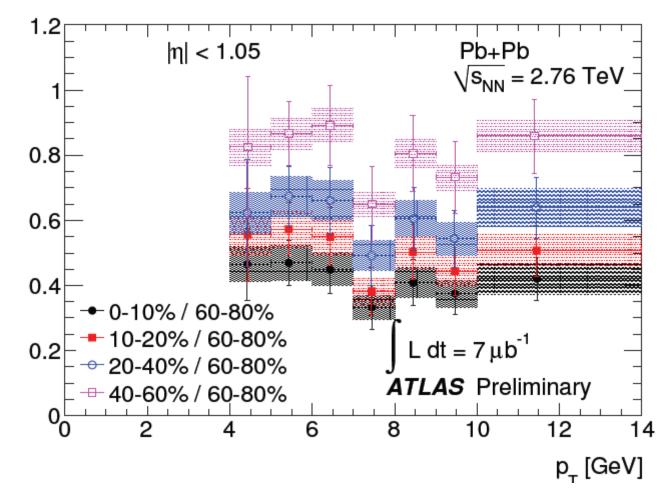
 $E_{T2} > 25 \ GeV$

Updated from published result



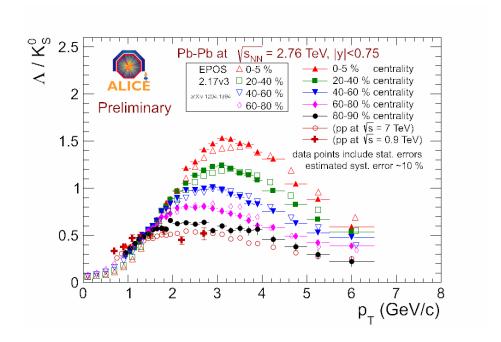






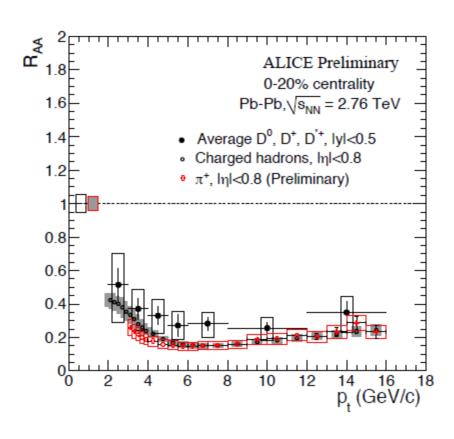






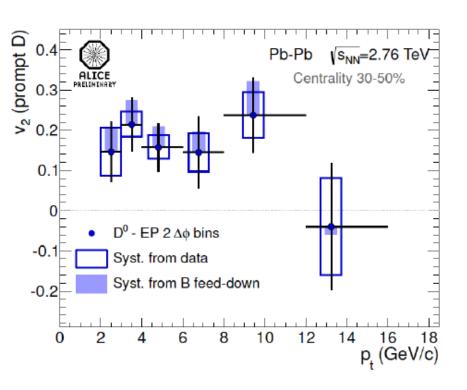


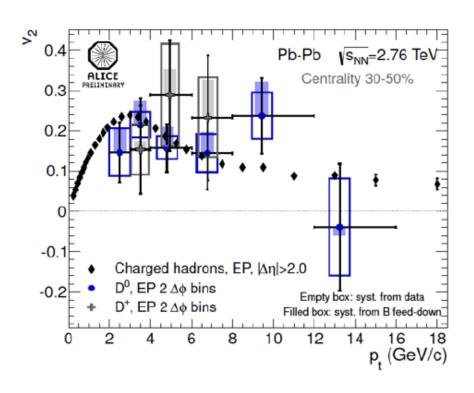






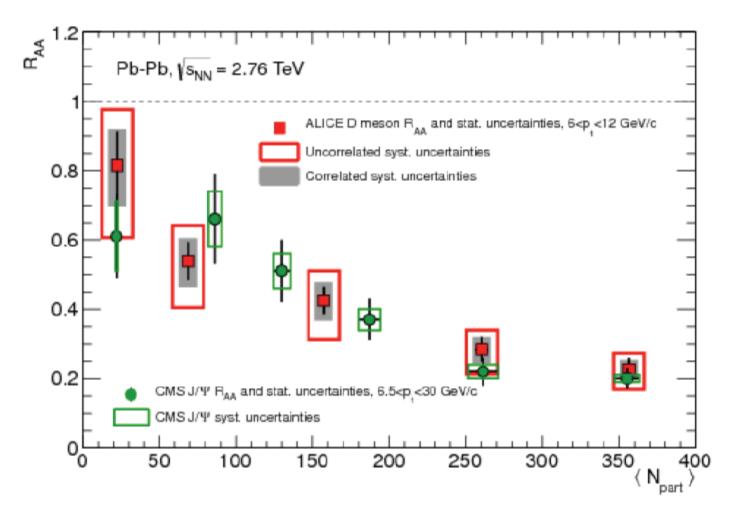






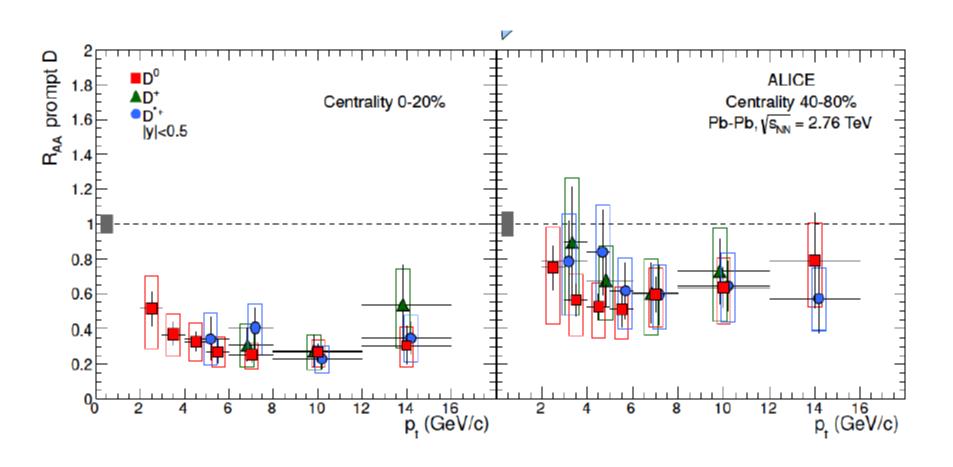






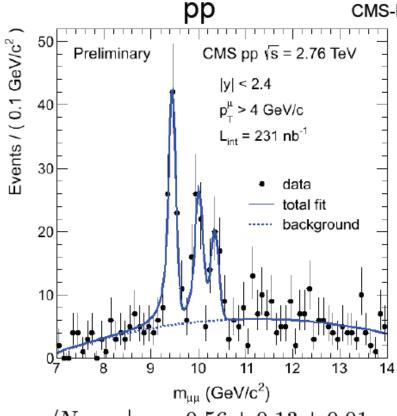




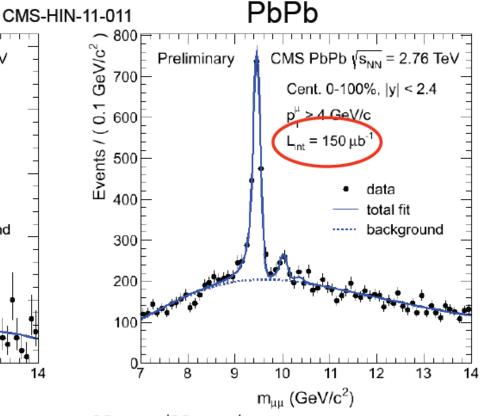








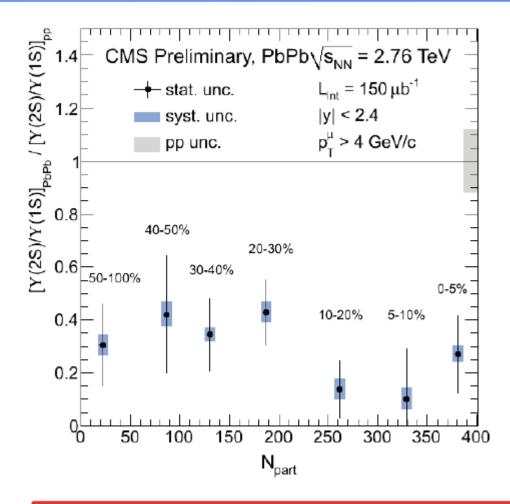
 $N_{\Upsilon(2S)}/N_{\Upsilon(1S)}|_{pp} = 0.56 \pm 0.13 \pm 0.01$ $N_{\Upsilon(3S)}/N_{\Upsilon(1S)}|_{pp} = 0.21 \pm 0.11 \pm 0.02$



 $N_{\Upsilon(2S)}/N_{\Upsilon(1S)}|_{\text{PbPb}} = 0.12 \pm 0.03 \pm 0.01$ $N_{\Upsilon(3S)}/N_{\Upsilon(1S)}|_{\text{PbPb}} < 0.07$







$$\frac{N_{\Upsilon(2S)}/N_{\Upsilon(1S)}|_{\text{PbPb}}}{N_{\Upsilon(2S)}/N_{\Upsilon(1S)}|_{\text{pp}}} = 0.21 \pm 0.07 \pm 0.02$$





