

# Exploring Hot Dense Matter at RHIC and LHC

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## Lecture 3: Collective Flow and Hydrodynamics

# “Hydrodynamic” flow in unusual systems

1. Cornstarch+water (“oobleck”, Non-Newtonian fluid) on an audio speaker:

<http://youtu.be/3zoTKXXNQIU>

2. Stream of sand particles striking a target in symmetric geometry:

<http://nagelgroup.uchicago.edu/Nagel-Group/Granular.html>

# Elliptic flow of a degenerate Fermi fluid

J. Thomas et al., Duke

Optically trapped atoms

→ degenerate Fermi gas

→ nanokelvin temperature (!)

Interactions magnetically tuned to Feshbach resonance

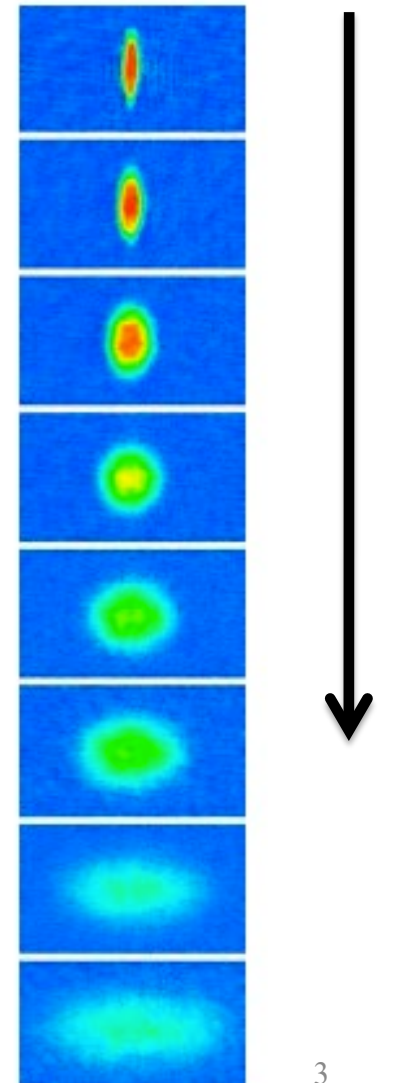
→ infinite 2-body scattering cross-section

→ prototypical “strongly-coupled” system

Prepare the system with spatial anisotropy and let it evolve

→ develops momentum anisotropy

→ **Ⓢ**elliptic flow” (!)



# What is fluid dynamics?

Fluid dynamics = Conservation of Energy+Momentum for **long wavelength** modes of excitation

breaks down for small or dilute systems

Degrees of freedom for a relativistic fluid

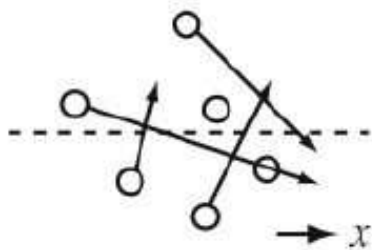
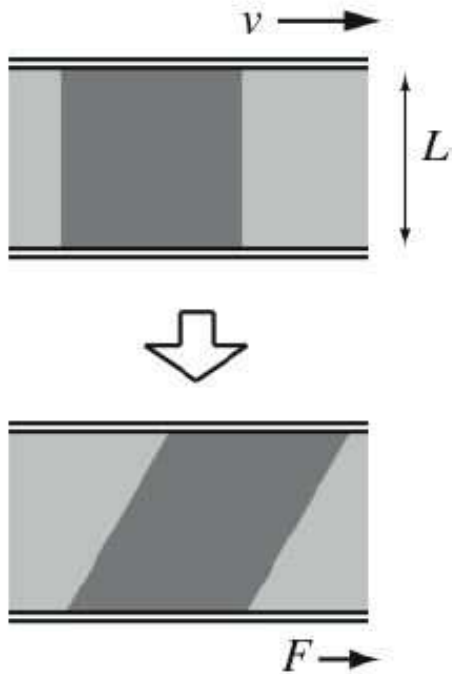
- fluid velocity  $u^\mu$  (4-vector)
- pressure  $p$  (scalar)
- energy density  $e$  (scalar)
- General relativity: metric tensor  $g_{\mu\nu}$

Quantum field theory:

- Energy-Momentum Tensor:  $T^{\mu\nu}$
- Conservation of Energy+Momentum:  $\partial_\mu T^{\mu\nu} = 0$

# Shear viscosity in fluids

Shear viscosity characterizes the efficiency of momentum transport



$$\frac{F}{A} = \eta \frac{v}{L}$$

$$\eta = \rho \langle v \rangle \lambda_{mfp} \sim \frac{1}{\sigma}$$

quasi-particle  
interaction cross  
section

Comparing relativistic fluids:  $\eta/s$

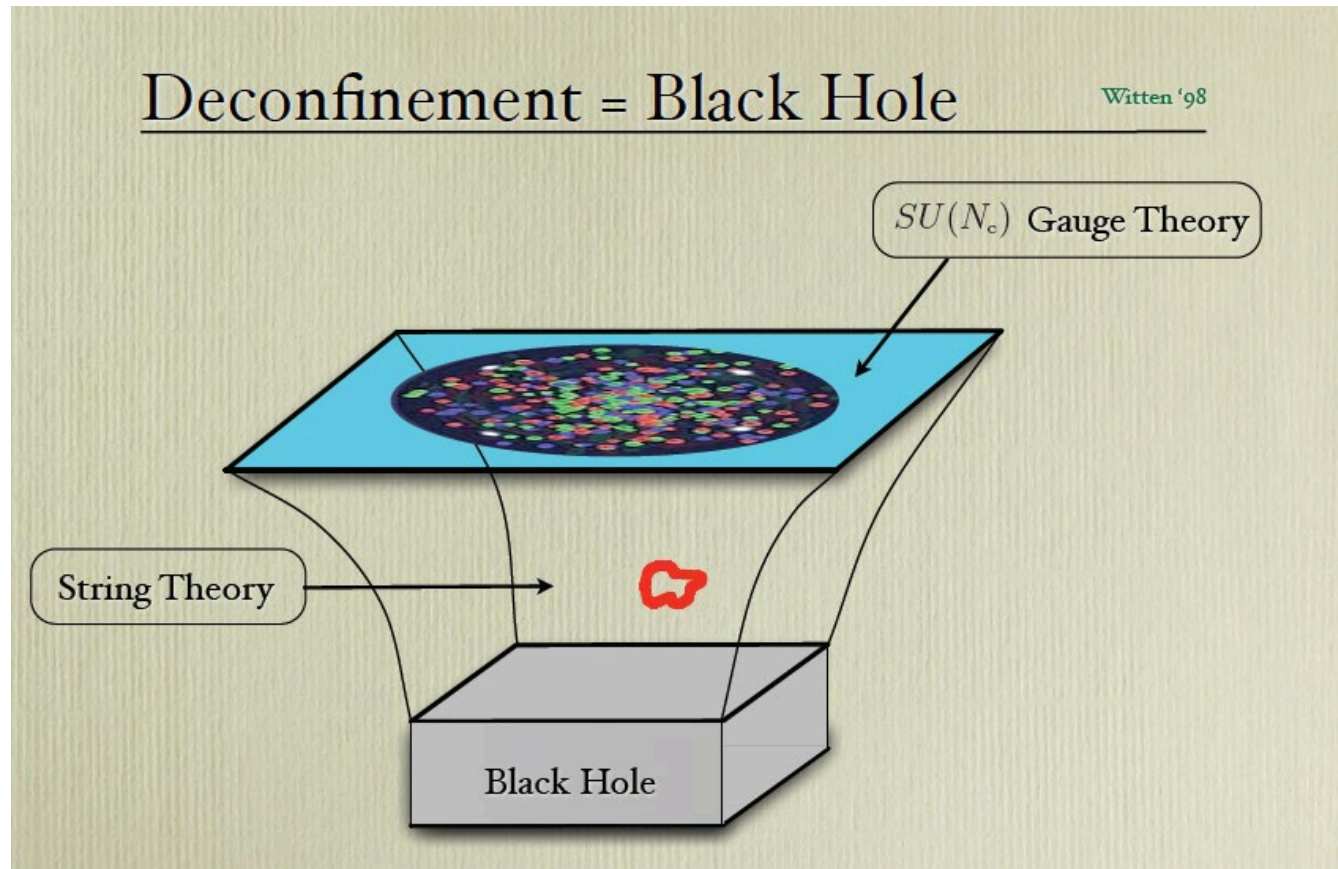
- $s$  = entropy density
- scaling param.  $\eta/s$  emerges from relativistic hydro eqns.
- generalization for non-rel. fluids:  $\eta/w$  ( $w$ =enthalpy) (Liao and Koch, Phys.Rev. C81 (2010) 014902)

Large  $\sigma \rightarrow$  small  $\eta/s$   
 $\rightarrow$  Strongly-coupled matter  
 $\rightarrow$  "perfect liquid"

# Gauge/string duality and the QGP

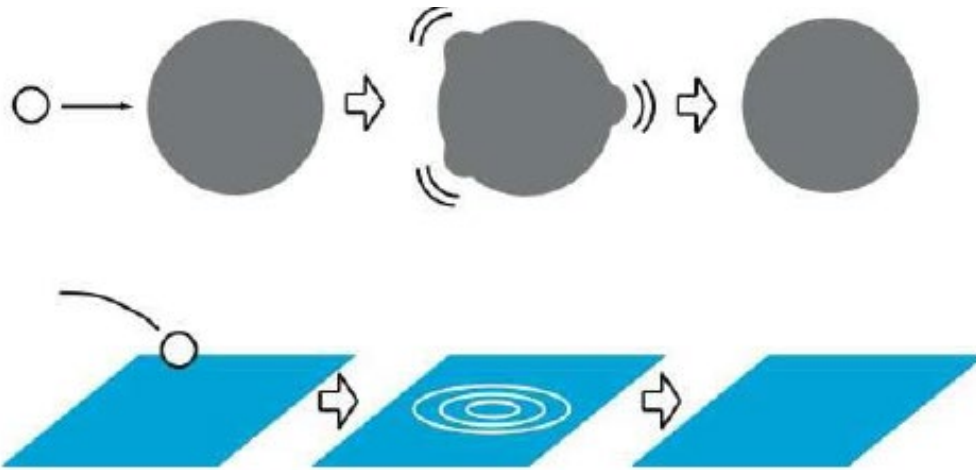
AdS/CFT correspondence (Maldacena '97): conjecture of deep connection in String Theory between strongly coupled non-abelian gauge theories and weak gravity near a (higher-dimensional) black hole

AdS/CFT correspondence = holography



# Shear viscosity and entropy in String Theory (AdS/CFT)

$\eta/s$  of a black hole (M. Natsuume, hep-ph/0700120)



Shear visc.  $\sim$  cross section:

$$\eta \propto \lim_{\omega \rightarrow 0} \sigma_{BH} = Area$$

Beckenstein entropy:

$$S_{BH} = \frac{Area}{4G\hbar} k_B$$

$$\Rightarrow \frac{\eta}{s} = \frac{\hbar}{4\pi k_B} \sim 0.1$$

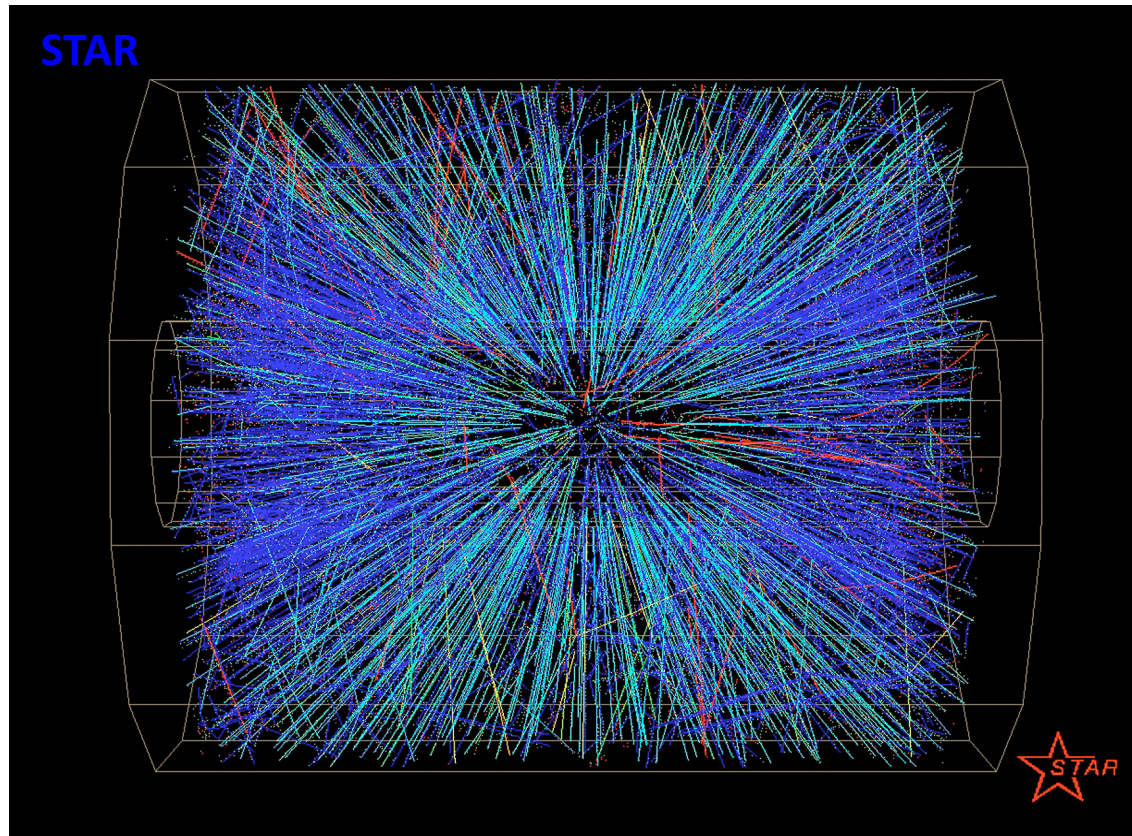
Universal result: gauge theory plasmas with gravity duals have a universal low value  $\eta/s=1/4\pi$  at strong ('t Hooft) coupling

Kovtun, Son and Starinets (KSS), PRL 94, 111601

(More precisely:  $\eta/s=1/4\pi$  is only Leading Order result for infinite coupling)



# Back to nuclear collisions...

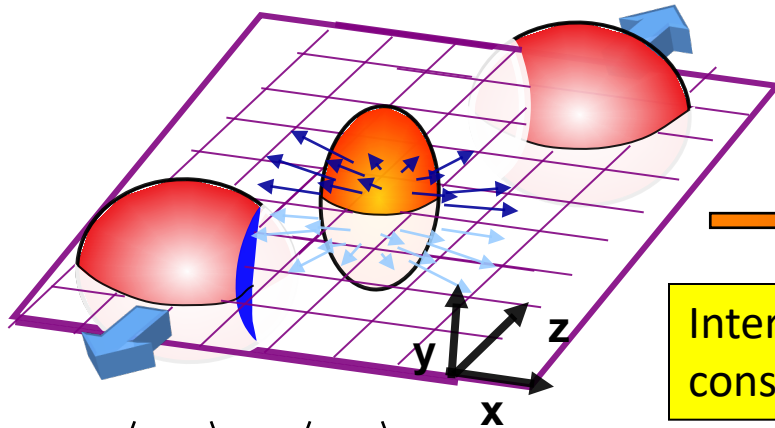




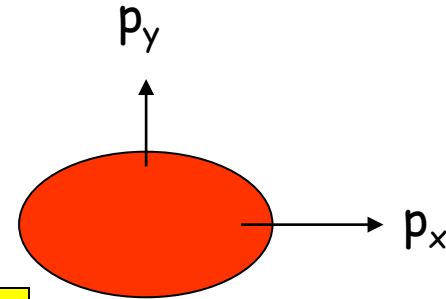
# Collective Flow of QCD Matter

Initial spatial anisotropy

Final momentum anisotropy



Interaction of constituents

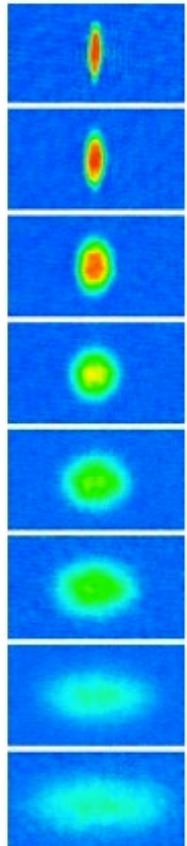


$$\varepsilon = \frac{\langle y^2 \rangle - \langle x^2 \rangle}{\langle y^2 \rangle + \langle x^2 \rangle}$$

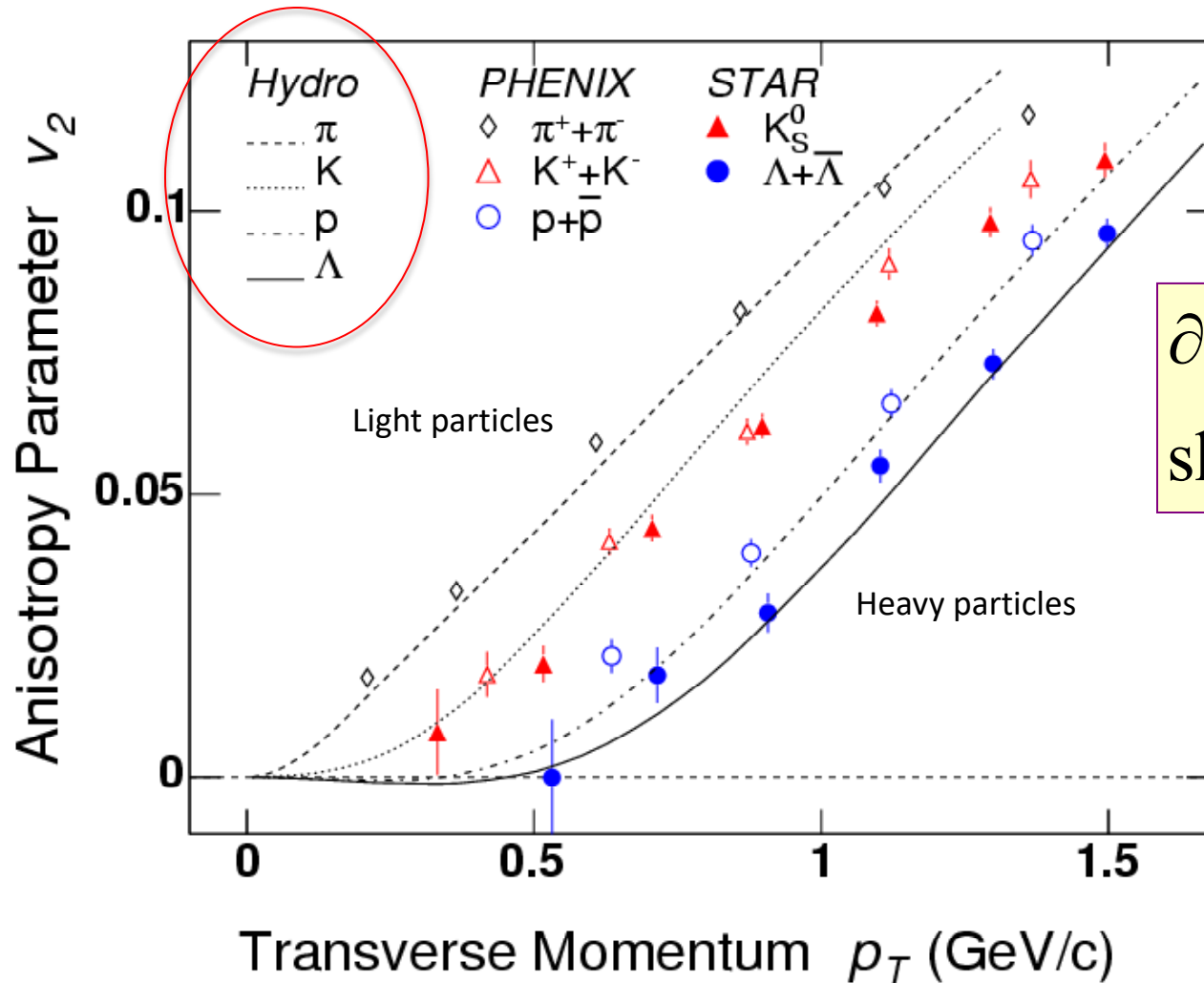
$$v_2 = \frac{\langle p_x^2 \rangle - \langle p_y^2 \rangle}{\langle p_x^2 \rangle + \langle p_y^2 \rangle}$$

Elliptic flow

$$\frac{dN}{d\phi} \propto 1 + 2v_2 \cos [2(\phi - \Psi_R)] + \dots$$



# A teaser: $v_2$ at RHIC



$v_2$  is sizable:  $\sim 10\%$  anisotropy

$$\partial_\mu T^{\mu\nu} = 0$$

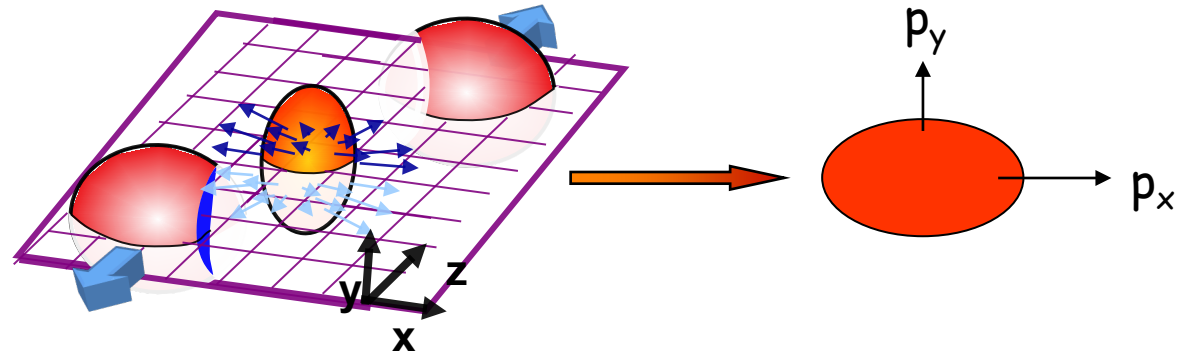
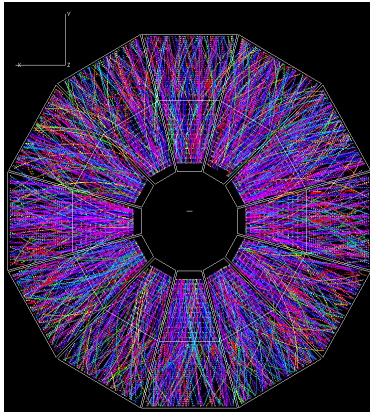
shear viscosity  $\eta = 0$

Mass hierarchy vs  
*momentum* is  
characteristic of common  
*velocity* distribution

Ideal hydro: qualitative agreement but missing the details

# How do we actually measure $v_2$ ?

STAR Heavy Ion event: Find **momentum-weighted** plane of azimuthal view in momentum space symmetry of the event (“reaction plane”  $\Psi_R$ )



Calculate the momentum-weighted azimuthal asymmetry relative to that plane:

$$v_2 = \frac{\langle p_x^2 \rangle - \langle p_y^2 \rangle}{\langle p_x^2 \rangle + \langle p_y^2 \rangle}$$

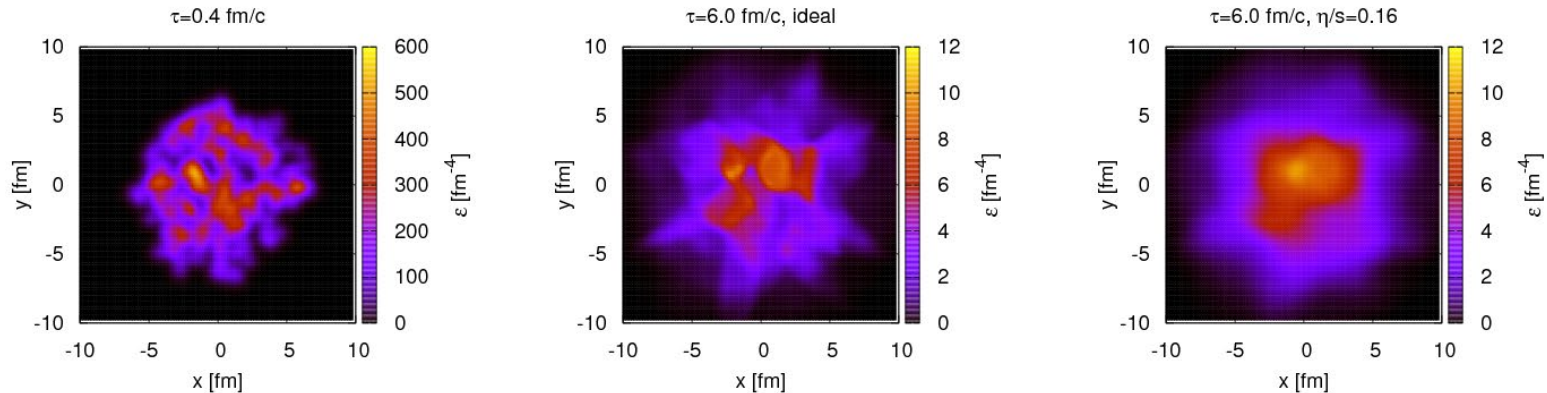
$$\frac{dN}{d\phi} \propto 1 + 2v_2 \cos [2(\phi - \Psi_R)] + \dots$$

# Wait: can it really be that simple? Actually, no.

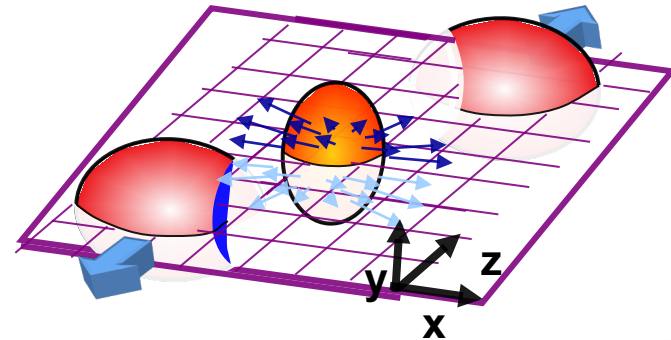
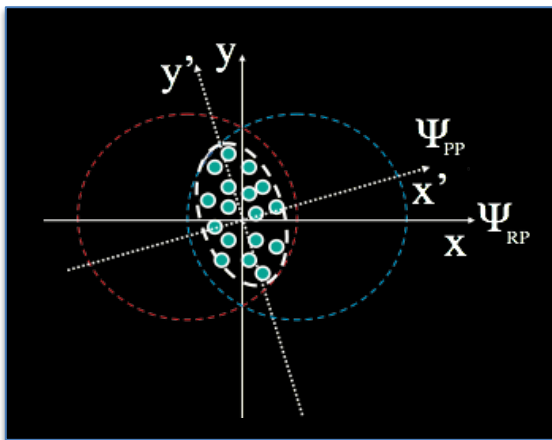
Initial state is (highly) non-uniform:

nucleon correlations, local hot spots of energy density,...

Theory calculation: Schenke, Jeon, Gale, PRL 106, 042301



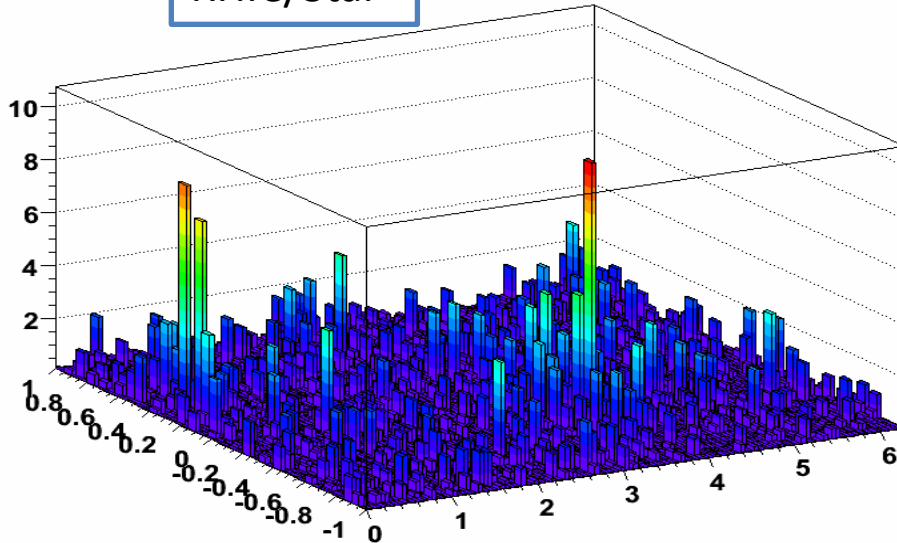
This will bias the measurement of the reaction plane orientation:



$$\frac{dN}{d\phi} \propto 1 + 2v_2 \cos [2(\phi - \Psi_R)] + \dots$$

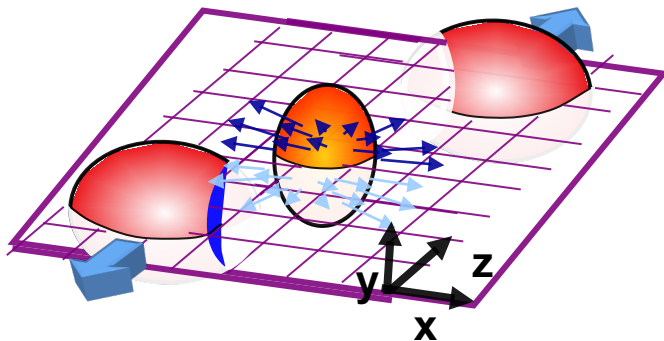
# Another complication: “non-flow” from jets

RHIC/Star

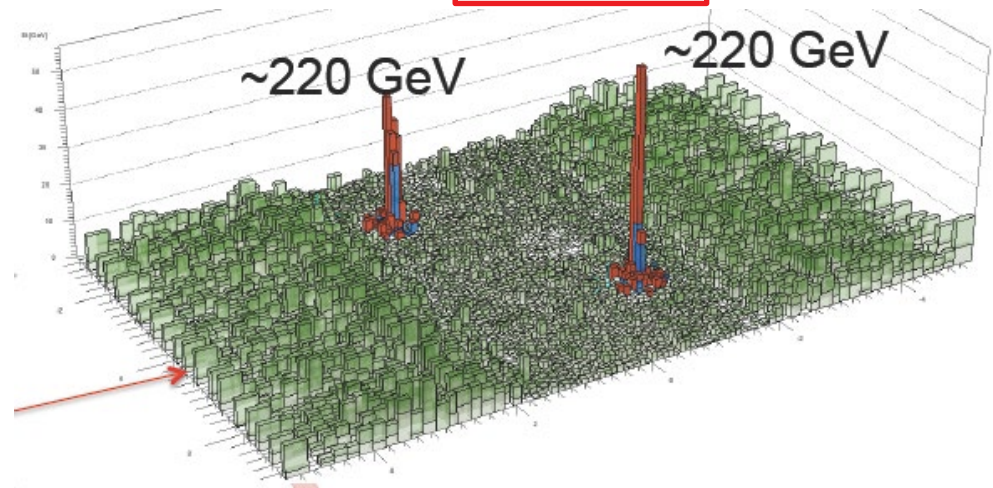


Large anisotropic contribution to momentum flow in the event

But complex and unknown correlation with reaction plane orientation



LHC/CMS



# Controlling “non-flow”

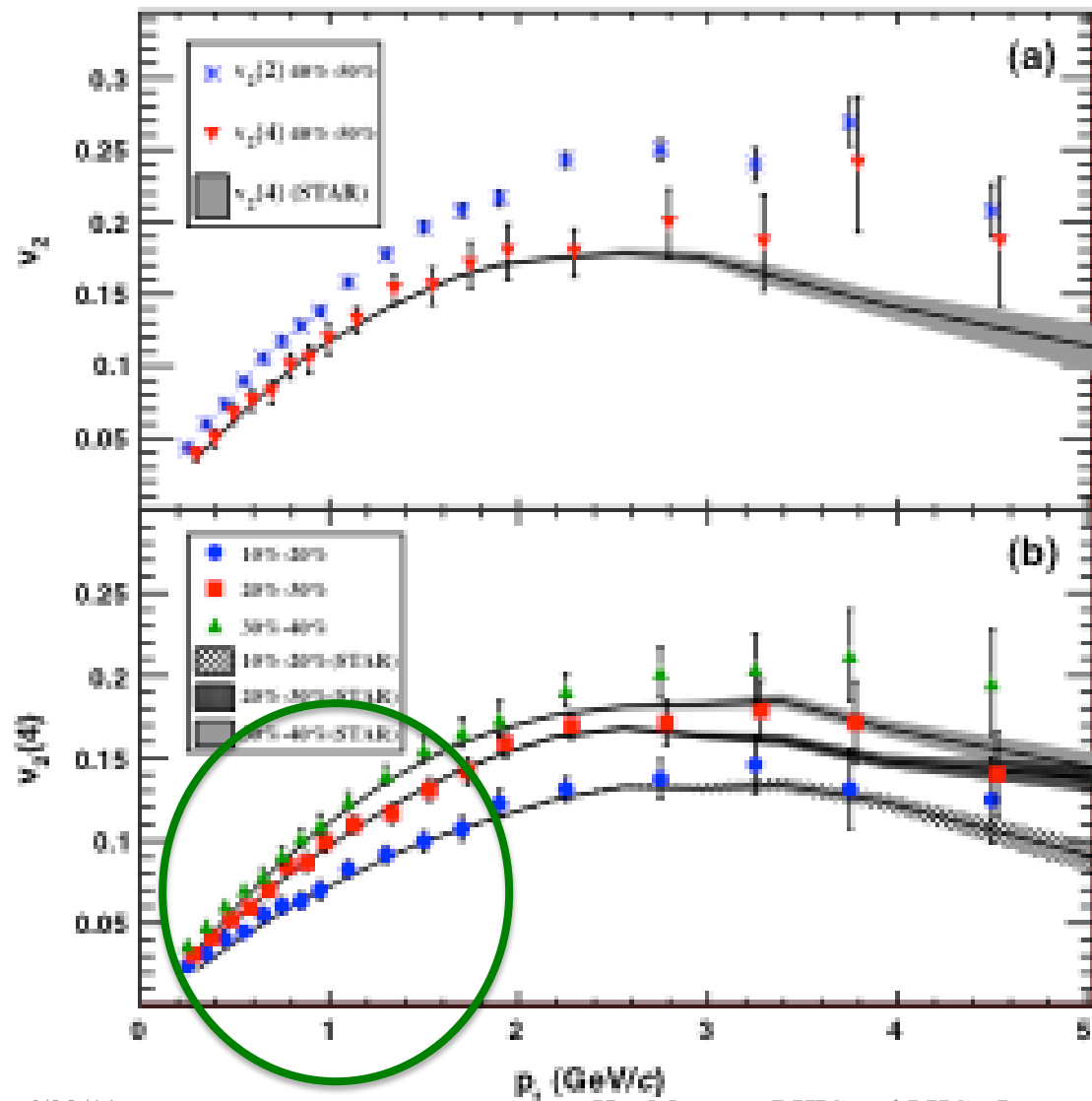
Want to remove all correlations that are not due to collective flow of many particles:

- Measure reaction plane orientation and flow signal in widely separated regions of phase space (large  $\Delta\eta$  separation)
- Compare cumulants of various order: 2,4,6,...particle
  - cumulants are well-known in statistics: isolate true n-particle correlations by removing lower order correlations (e.g. n particles can be mutually correlated due to 2-particle correlations)

Methods are under good control → small systematic uncertainties due to “non-flow” correlations

# Elliptic flow $v_2$ : LHC vs RHIC

ALICE, PRL 105, 252302 (2010)



Striking similarity of  $p_T$ -differential  $v_2$  at RHIC and LHC



# Hydrodynamic modeling of a heavy ion collision

P. Romatschke, QM11

- Need initial conditions for Hydro:  $\epsilon, u^\mu$  at  $\tau = \tau_0$
- Need equation of state  $p = p(\epsilon)$ , which gives  $c_s^2 = \frac{dp}{d\epsilon}$
- Need functions for transport coefficients  $\eta, \zeta$ .
- Need algorithm to solve (nonlinear!) hydro equations
- Need method to convert hydro information to particles (“freeze-out”)

How to include viscous effects?

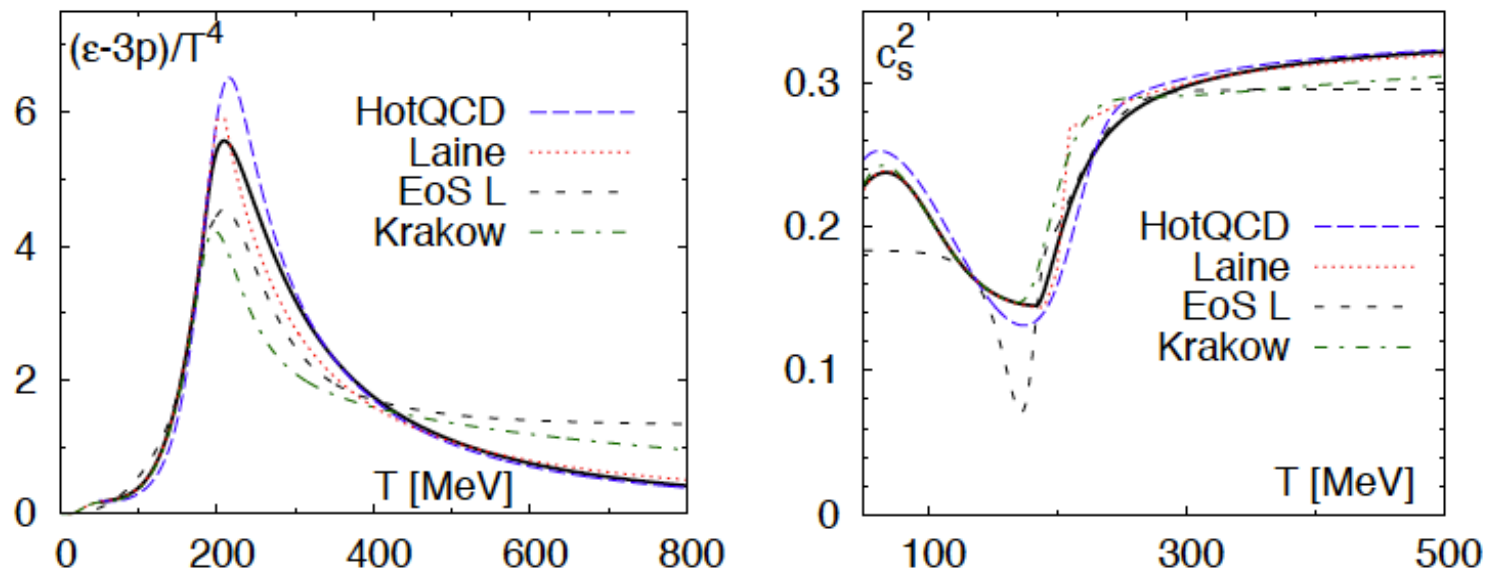
- Energy and Momentum Conservation:  $\partial_\mu T^{\mu\nu} = 0$  is exact
- But  $T^{\mu\nu} = T_{\text{id}}^{\mu\nu}$  is approximation!
- Lift approximation:  $T^{\mu\nu} = T_{\text{id}}^{\mu\nu} + \Pi^{\mu\nu}$
- Build  $\Pi^{\mu\nu}$ : Shear viscosity Bulk viscosity

$$\Pi^{\mu\nu} = \underbrace{\eta}_{\text{red circle}} \nabla^{<\mu} u^{\nu>} + \underbrace{\zeta}_{\text{green circle}} \Delta^{\mu\nu} \nabla \cdot u$$

# Equation of state

Comparison of different equations of state in hydrodynamic evolution:

P. Huovinen, P. Petreczky, Nucl.Phys.A837:26-53 (2010) see also talk by P. Huovinen, poster by W. Florkowski



Solid black: Parametrization from P. Huovinen, P. Petreczky, Nucl.Phys.A837:26-53 (2010)

HotQCD: HotQCD collaboration, Phys.Rev.D80:014504 (2009)

Laine: M. Laine and Y. Schröder, Phys. Rev. D73, 085009 (2006)

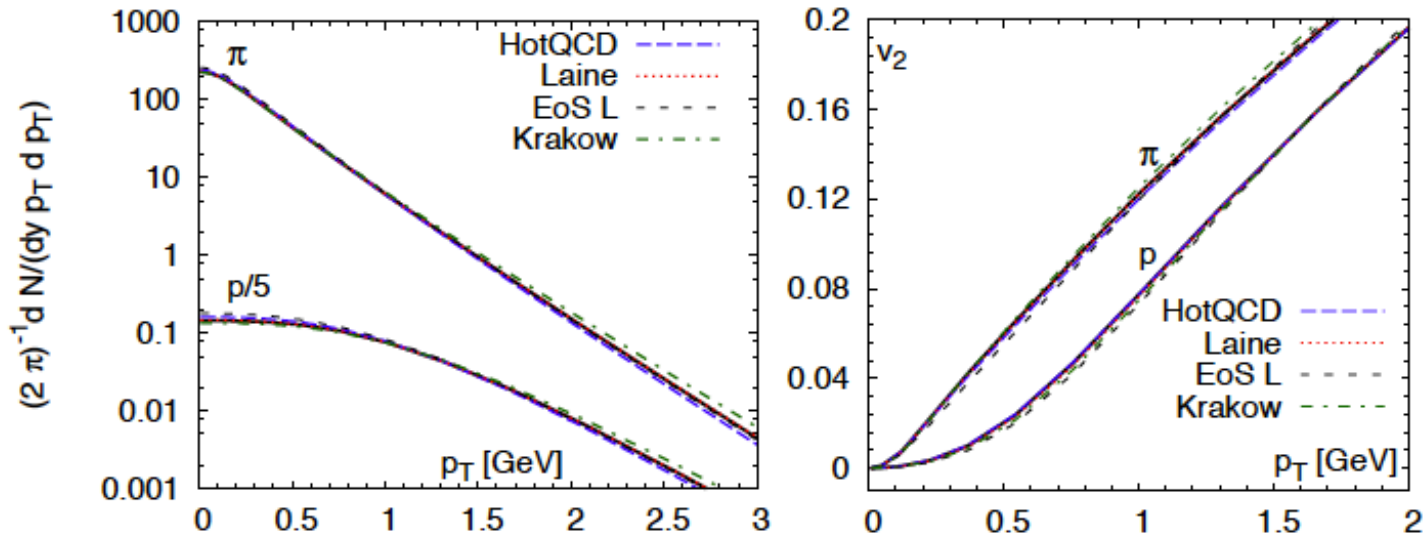
EoS L: H. Song and U. W. Heinz, Phys. Rev. C 78, 024902 (2008) using Wuppertal-Budapest results

Krakow: M. Chojnacki et al, Acta Phys. Polon. B 38, 3249 (2007) and Phys. Rev. C 78, 014905 (2008)

# Equation of state

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Conclusion:

“Differences in the lattice EoS parametrization in the literature are small and not observable in the  $p_T$ -differential elliptic flow.”

Another more recent lattice equation of state:

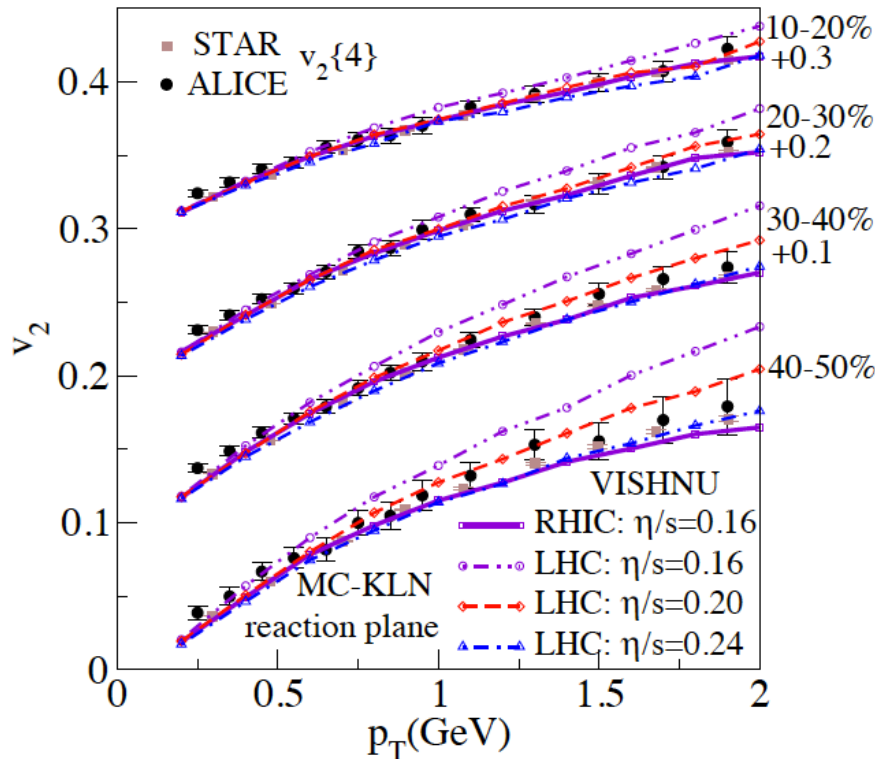
S. Borsanyi et al, JHEP 1011:077 (2010)

Wuppertal-Budapest lattice results - used in V. Roy and A.K. Chaudhuri, arXiv:1103.2870

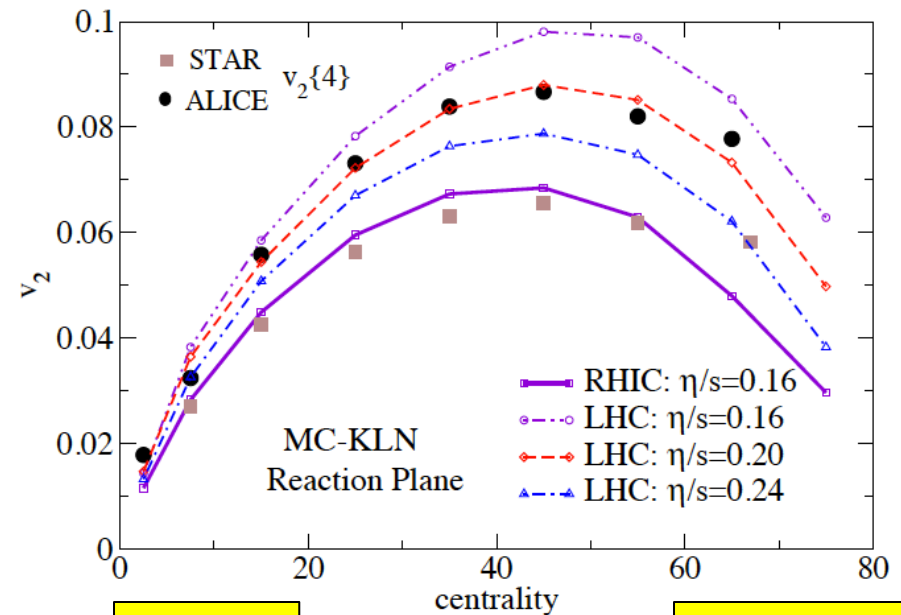
# $v_2$ : data vs. viscous hydrodynamic modeling

Song, Bass, and Heinz, arXiv:1103.2380

$p_T$ -differential



$p_T$ -integrated



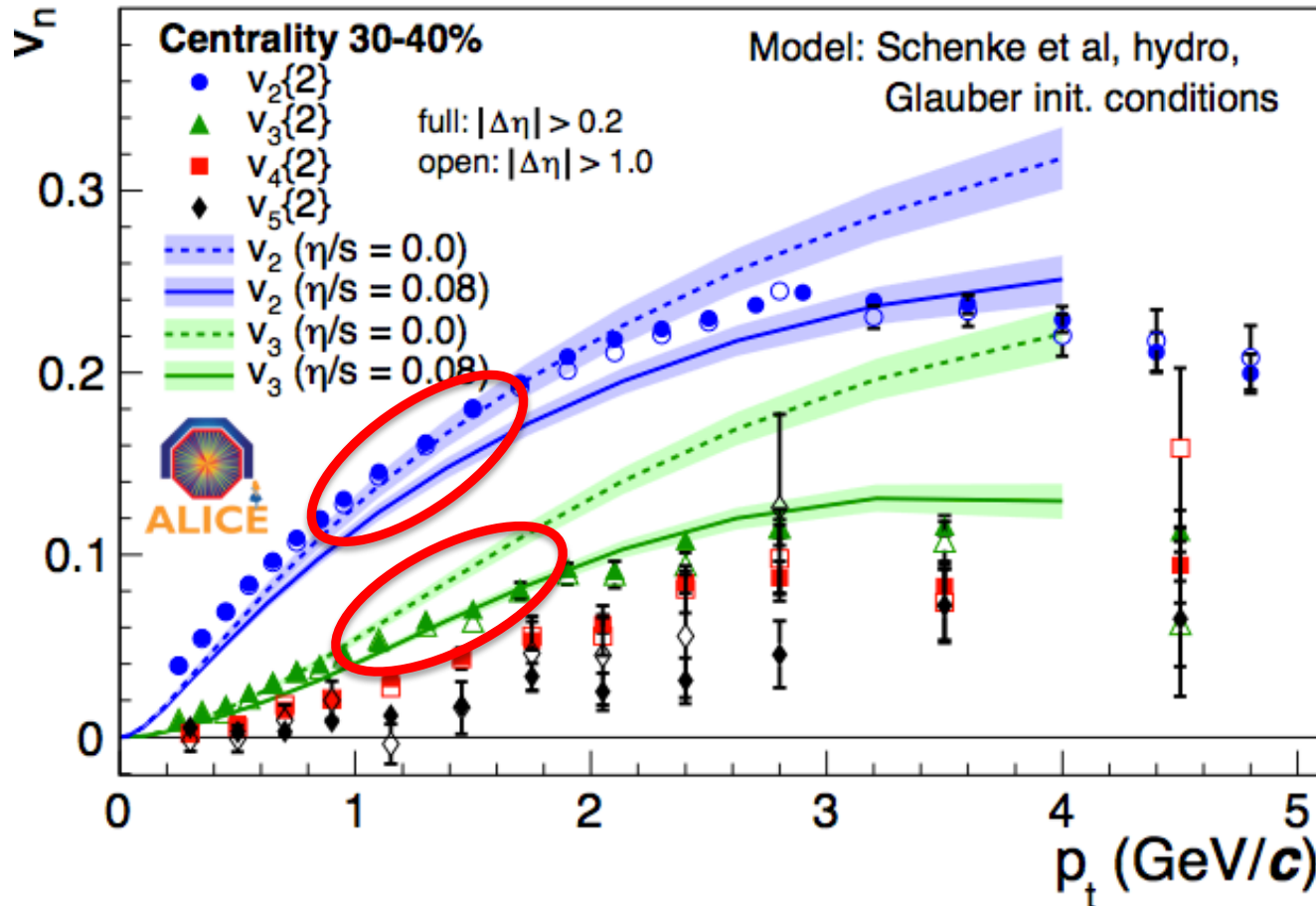
central

peripheral

Preferred values:  $\eta/s(\text{RHIC})=0.16$ ,  $\eta/s(\text{LHC})=0.20$  .....????

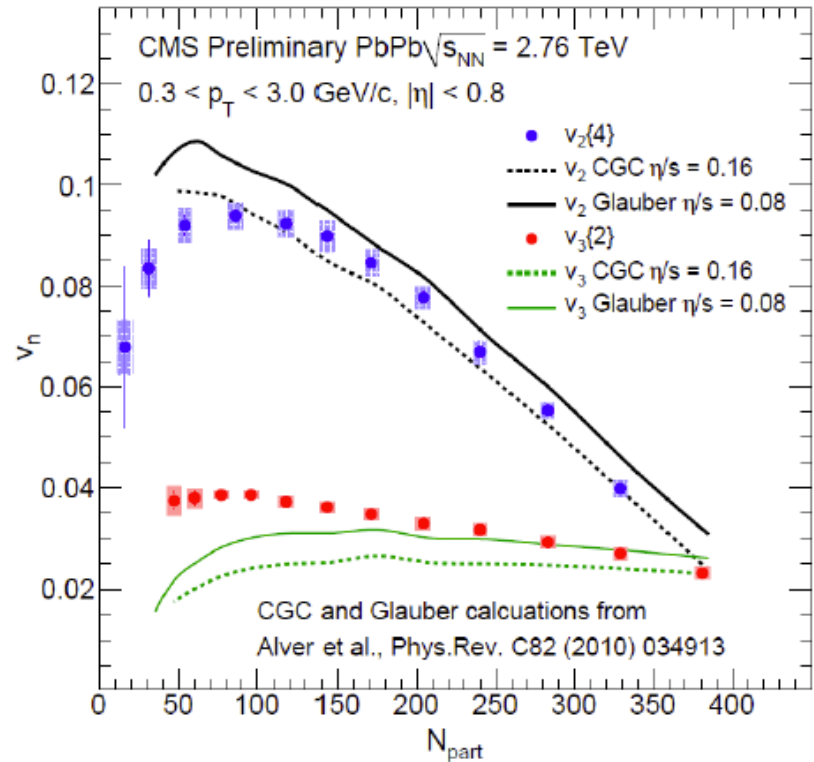
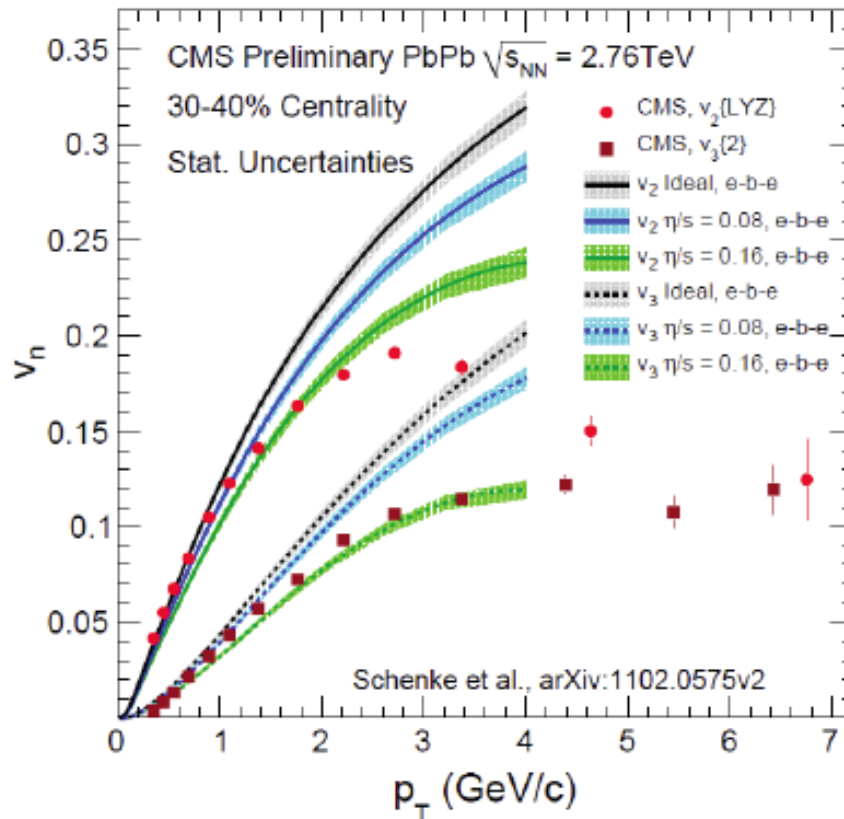
# Higher harmonics

ALICE arXiv:1105.3865



ALICE:  $v_2$  and  $v_3$  have contradictory preferences for  $\eta/s$   
→ not understood

# CMS: similar ambiguities



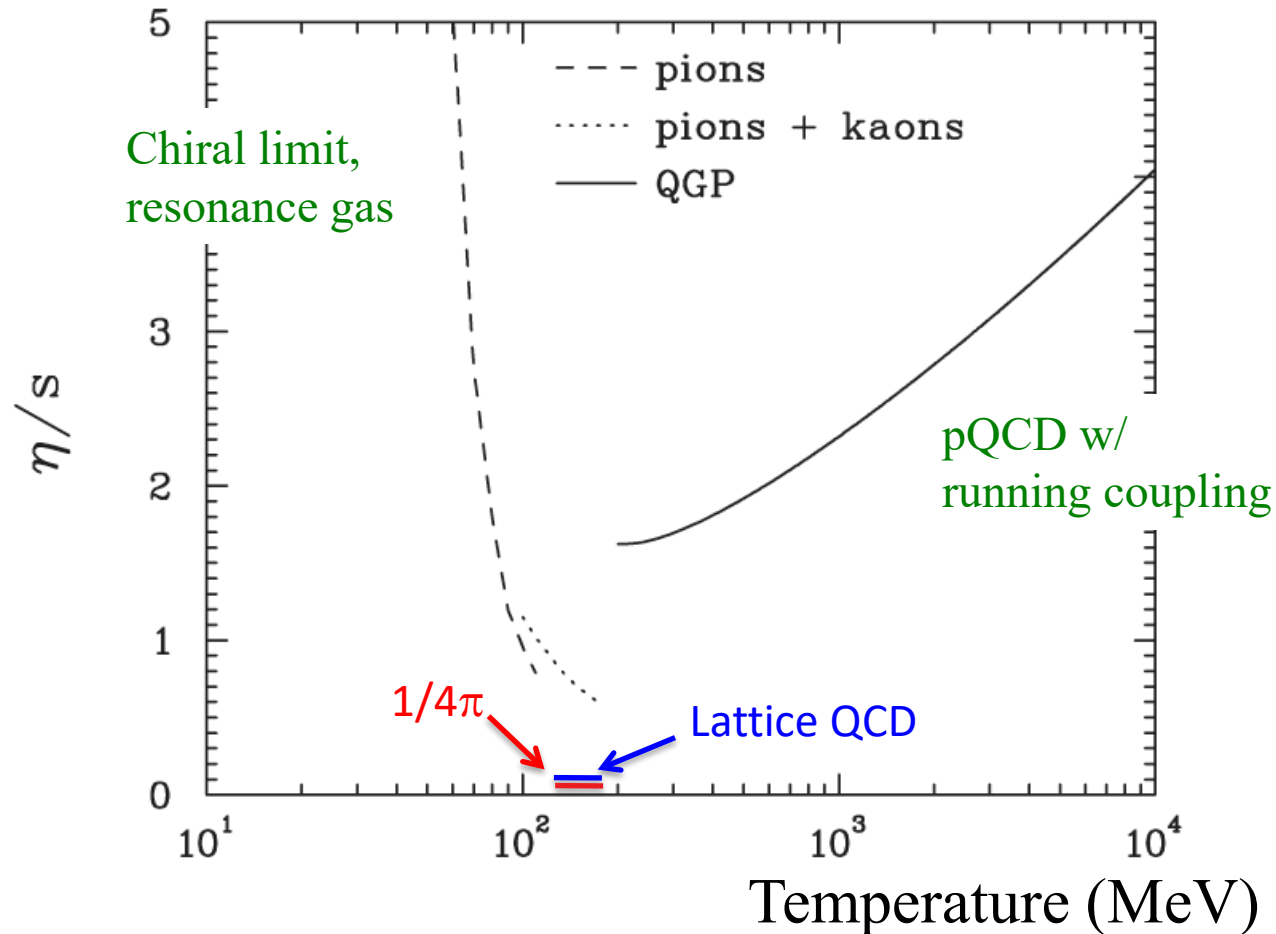
Qualitatively:  $\eta/s$  is within  $\sim 2$ -3 times  $1/4\pi$

Quantitatively: need better theoretical and experimental control for definite measurement

# Shear viscosity: expectations from QCD

Analytic: Csernai, Kapusta and McLerran PRL 97, 152303 (2006)

Lattice: H. Meyer, PR D76, 101701R (2007)



If  $T_{\text{LHC}} > T_{\text{RHIC}}$ , expect  $\eta/s(\text{LHC}) > \eta/s(\text{RHIC})$



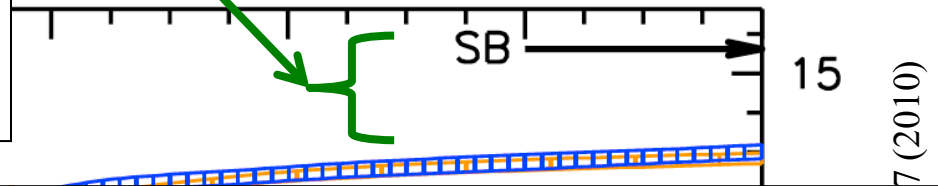
# Remember this plot:

QCD calculated on the lattice ( $\mu_B=0$ )

Slow convergence to non-interacting Steffan-Boltzmann limit  
What carries energy - complex bound states of q+g? “strongly-coupled” plasma?

Energy density

$$\varepsilon = \frac{\pi^2}{30} g_{DOF} T^4$$



Both flow measurements and Lattice QCD calculations suggest that the Quark-Gluon Plasma at high temperature is very different than a simple gas of non-interacting quarks and gluons

Why? What are the dominant degrees of freedom (“quasi-particles”)?

We don’t know yet...

Cross  
(like ionization of atomic plasma)