



NUCLEAR ASTROPHYSICS



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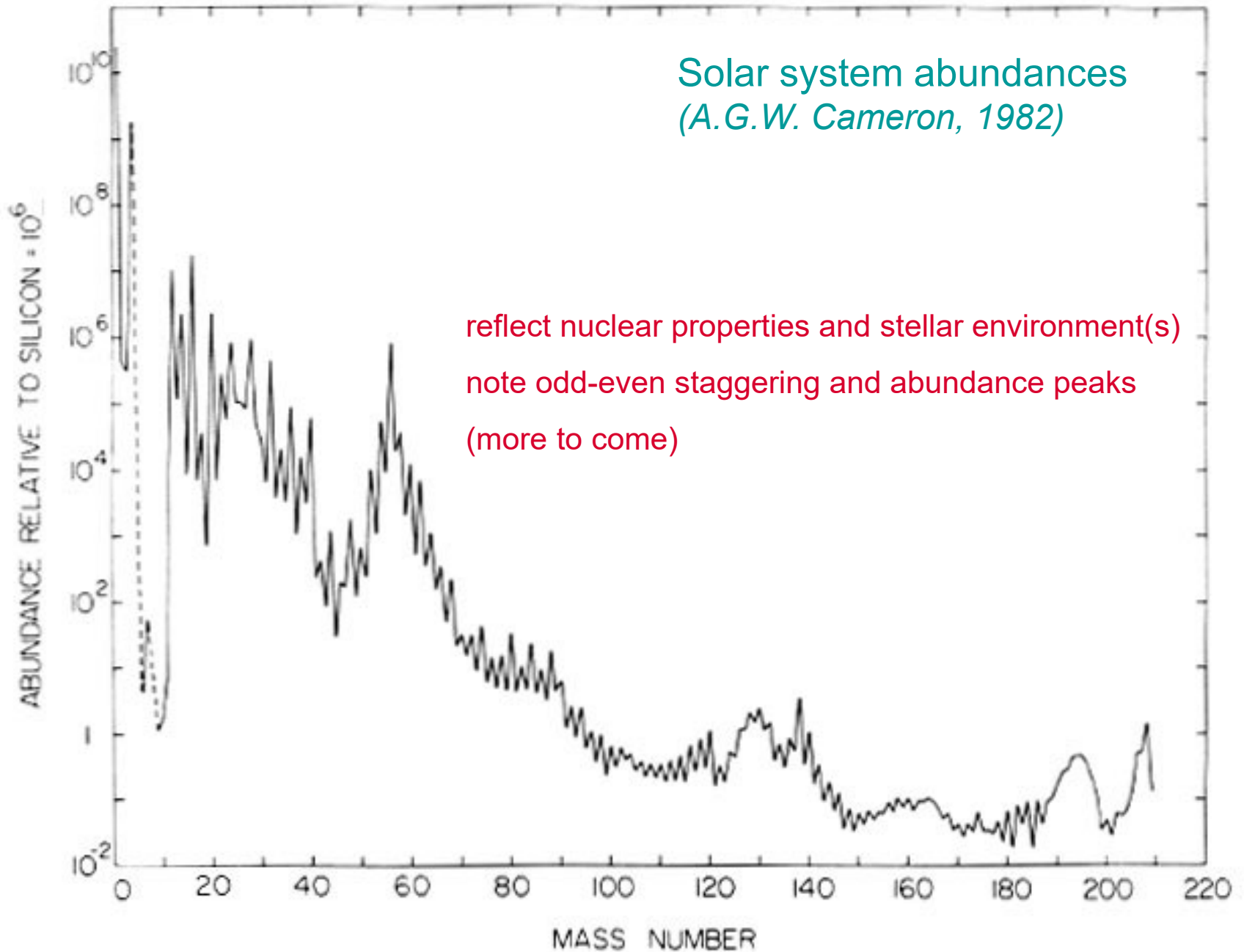




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Solar system abundances
(A.G.W. Cameron, 1982)



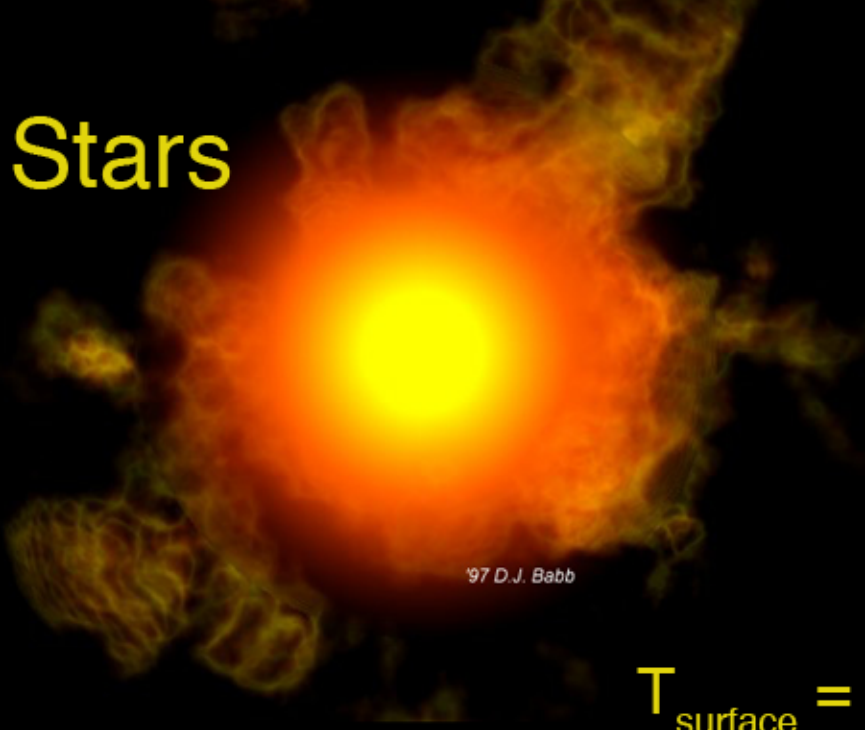
A blanket statement:

1. Almost all problems in astrophysics ultimately reduce to stars, stellar structure or stellar evolution
2. Stars evolve because of changes in their chemical composition

Basic approach:

1. Identify the astrophysical problem
2. Find an observable whose attributes depend upon a nuclear process
3. Develop a strategy for acquiring the needed nuclear information

Stars



sun:

$\sim 75\%$ H, 25% He by mass

$$M_{\odot} = 1.99 \times 10^{30} \text{ kg}$$
$$(0.1 M_{\odot} \leq M_{\text{star}} \leq 100 M_{\odot})$$

$$R_{\odot} = 6.96 \times 10^8 \text{ m}$$

$$T_{\text{surface}} = 5800 \text{ K} \quad (2500 \text{ K} \leq T_{\text{star}} \leq 25000 \text{ K})$$

$$L_{\odot} = 3.83 \times 10^{26} \text{ W} \quad (10^{-4} L_{\odot} \leq L_{\text{star}} \leq 10^5 L_{\odot})$$

[sun has $\sim 9 \times 10^{56}$ protons so L/proton (L_p) $\sim 2.8 \times 10^{-18}$ MeV/s
 E/proton (E_p) = $L_p \tau$, where $\tau = 5 \times 10^9$ y

$E_p \sim 450 \text{ keV} \longrightarrow \text{nuclear force}$]

Equations of stellar structure

1. structure

$$\frac{\partial r}{\partial m} = \frac{1}{4\pi r^2 \rho(m)} \quad (\text{defines mass as an independent variable})$$

$$\frac{\partial P}{\partial m} = -\frac{Gm}{4\pi r^4} - \frac{1}{4\pi r^2} \frac{\partial^2 r}{\partial t^2}$$

↑
sets hydrodynamic timescale
= 0 for “hydrostatic equilibrium”

see: Prialnik: “An Introduction to the Theory of Stellar Structure and Evolution”,
Kippenhahn & Weigert: “Stellar Structure and Evolution”, etc.

2. thermodynamics and chemistry

$$\frac{\partial T}{\partial m} = -\frac{GmT}{4\pi r^4 P} \nabla, \text{ where } \nabla = \left(\frac{\partial \ln T}{\partial \ln P} \right) = \nabla_{ad}, \nabla_{rad} \dots$$

adiabatic gradient
radiation

$$\frac{\partial L}{\partial m} = \epsilon_n - \epsilon_\nu - C_p \frac{\partial T}{\partial t} - \frac{1}{\rho} \left(\frac{\partial \ln \rho}{\partial \ln T} \right)_p$$

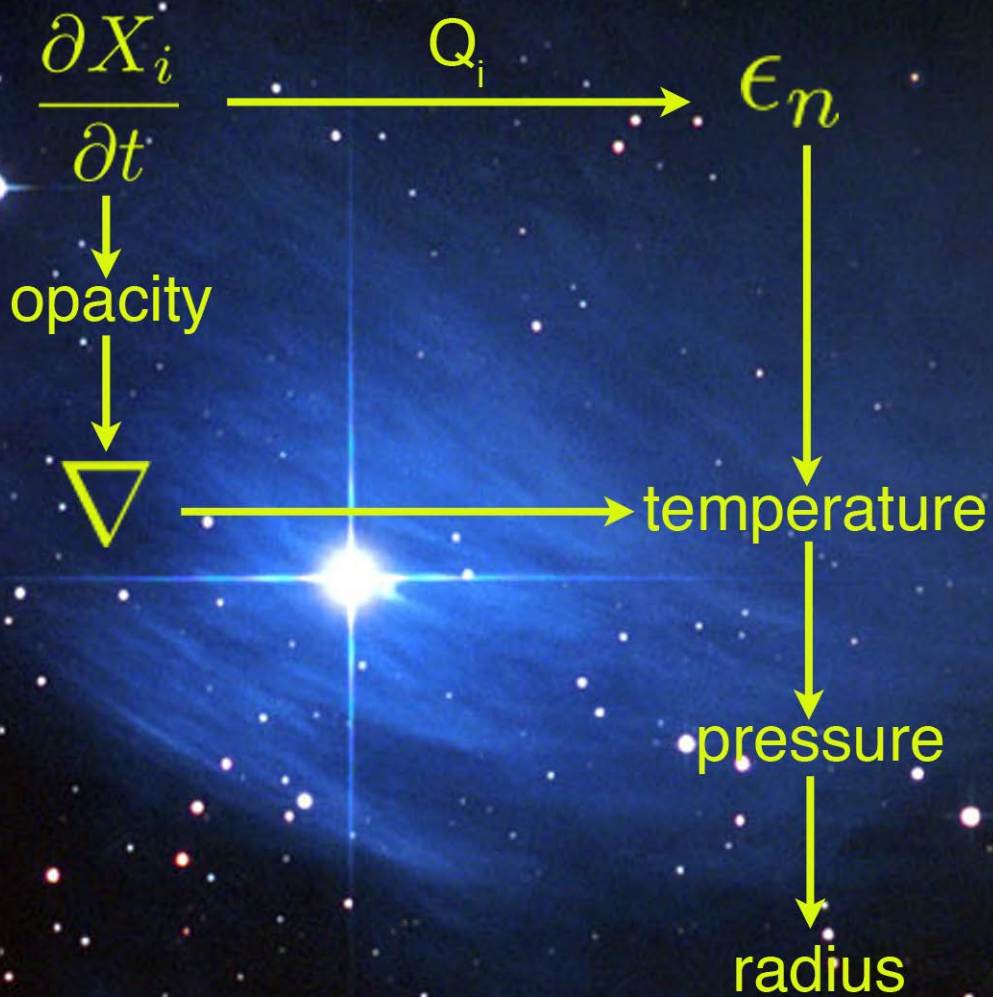
reactions and decays
neutrino losses
gravitational part (sets thermal timescale)
dU + P dV

$$\frac{\partial X_i}{\partial t} = \frac{\rho}{m_i} \left(\sum_j r_{ji} - \sum_k r_{ik} \right)$$

mass fraction of species i
production rates
destruction rates

sets nuclear timescale

given m , initial X_i :



Thermonuclear reaction rate

reaction $a + b$ with number densities N_a and N_b

number of nuclei reacting in time Δt is

$$N_b \times \sigma v \times \Delta t$$

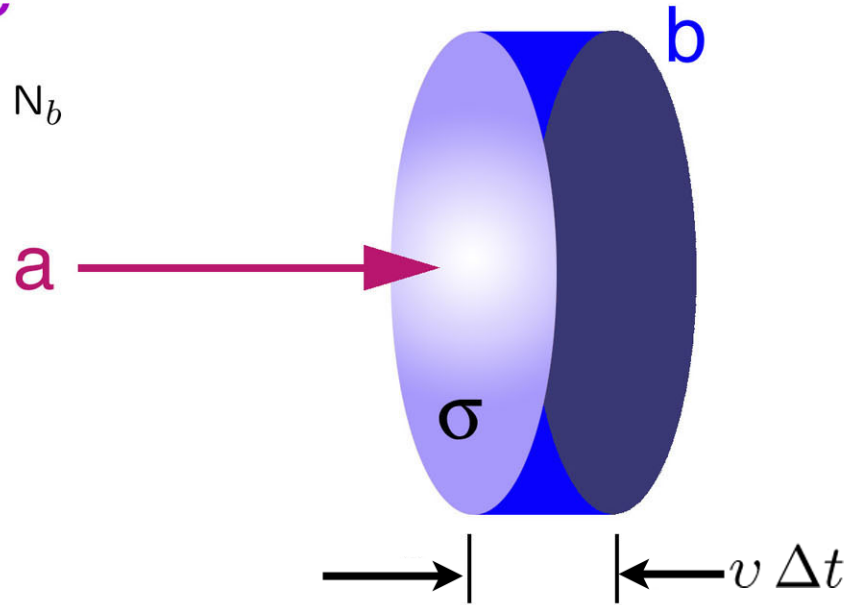
$$\text{Rate} = N_b \times \sigma v$$

$$\frac{\text{Rate}}{\text{unit volume of gas}} = \frac{N_a N_b \cdot \sigma v}{1 + \delta_{ab}}$$

(prevents double counting if $a = b$)

but there is a distribution of relative velocities

$$\text{so } R_{ab} = N_a N_b \langle \sigma v \rangle, \quad \langle \sigma v \rangle = \int_0^{\infty} \sigma(v) v \phi(v) dv$$



at thermal equilibrium*

$$\phi(v) = 4\pi v^2 \sqrt{\frac{\mu}{2\pi kT}} \exp\left(-\frac{\mu v^2}{2kT}\right)$$

$$\langle \sigma v \rangle = \sqrt{\frac{8}{\mu\pi k^3 T^3}} \int_0^\infty \sigma(E) \exp\left(-\frac{E}{kT}\right) dE$$

reaction time: in general, $N_i = \rho N_A \frac{X_i}{A_i}$, $N_A =$ Avogadro's number
 $X_i =$ mass fraction of i
 $A_i =$ atomic number of i

$$\frac{dN_b}{dt} = -\lambda N_b = \frac{N_b}{\tau_b}$$

$$R_{ab} = \frac{N_a N_b \langle \sigma v \rangle_{ab}}{1 + \delta_{ab}} = \frac{N_b}{\tau_b}$$

$$\text{so } \tau_b = (N_a \langle \sigma v \rangle_{ab})^{-1}$$

(no δ_{ab} ! if $a = b$, then 2 particles are destroyed)

*Yes, this is a good assumption. The mean-free path for a photon in the center of the sun is $\sim 10^{-3}$ cm

Properties of stellar cross sections

$$kT_{\odot} = 1.3 \text{ keV} \ll E_{\text{coul}}$$

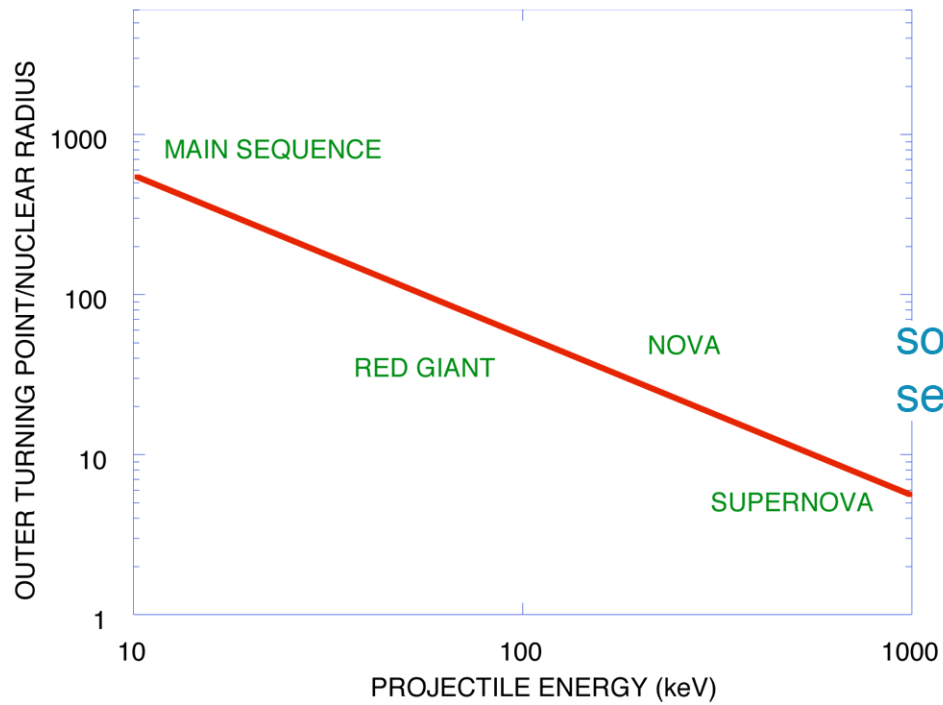
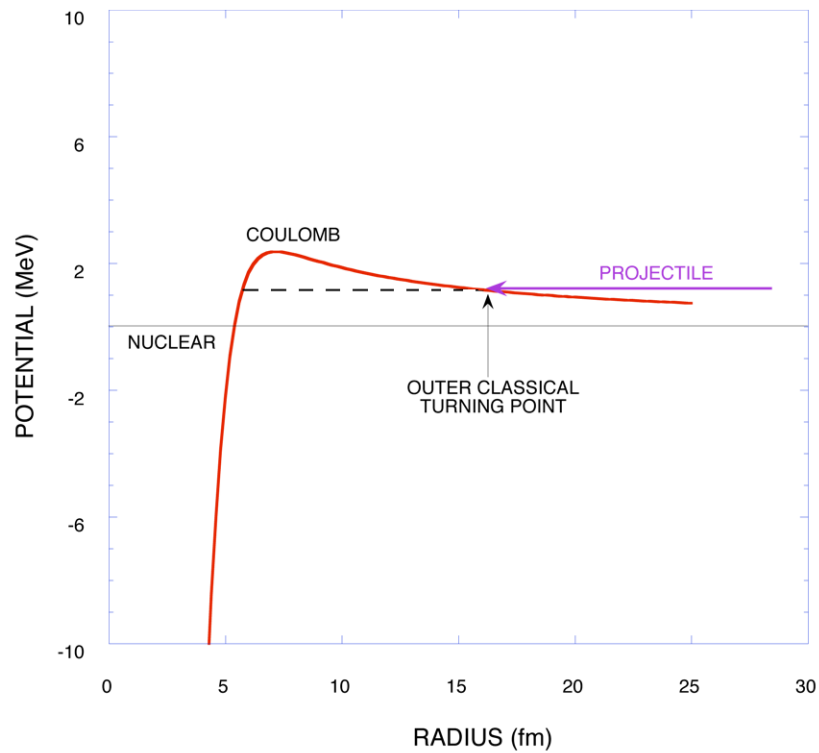
1) semi-classical scale: $\pi \lambda^2 \propto \frac{1}{E}$

2) s-wave penetration through
Coulomb barrier:

$$\propto e^{-2\pi\eta} \quad \text{or} \quad e^{-(E_G/E)^{1/2}}$$

$$\text{with } \eta = \frac{Z_1 Z_2 e^2}{\hbar} \sqrt{\frac{\mu}{2E}}, \quad E_G = \left(\frac{2\pi Z_1 Z_2 e^2}{\hbar} \right)^2 \frac{\mu}{2}$$

$$\sigma = \pi \lambda^2 e^{-2\pi\eta} \times \text{other stuff}$$

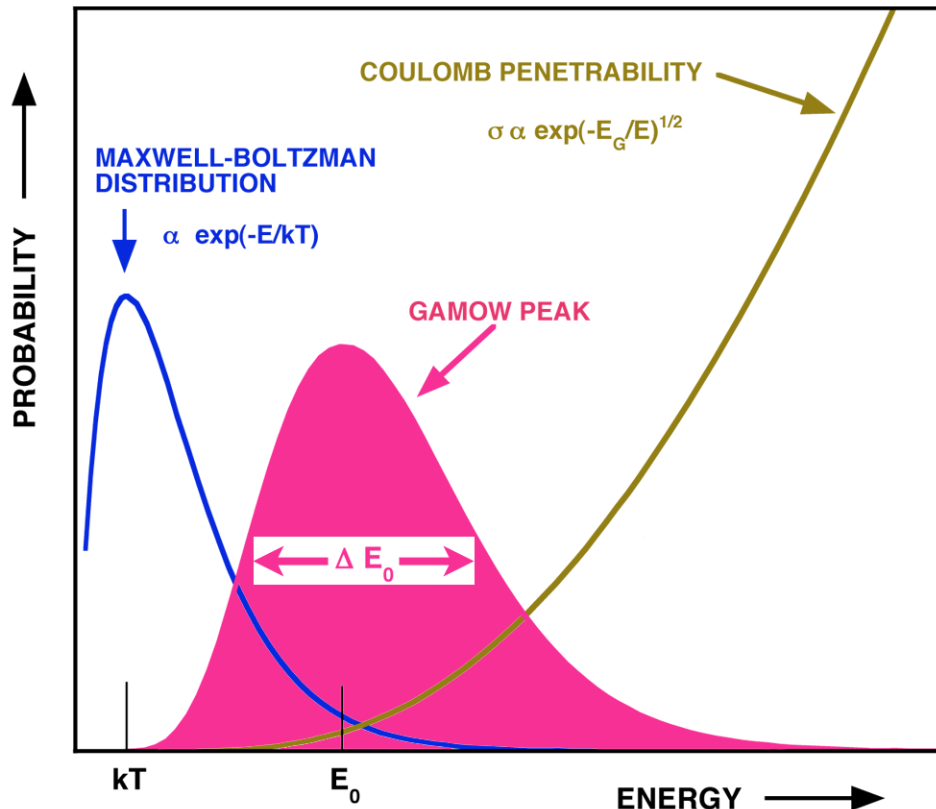


so these approximations seem appropriate

parameterize: $\sigma(E) = \frac{1}{E} e^{-2\pi\eta} S(E)$ "S-factor" S(E) contains:

- nuclear interaction
- nuclear structure
- finite-size effects
- other partial waves
- final-state phase space, etc.

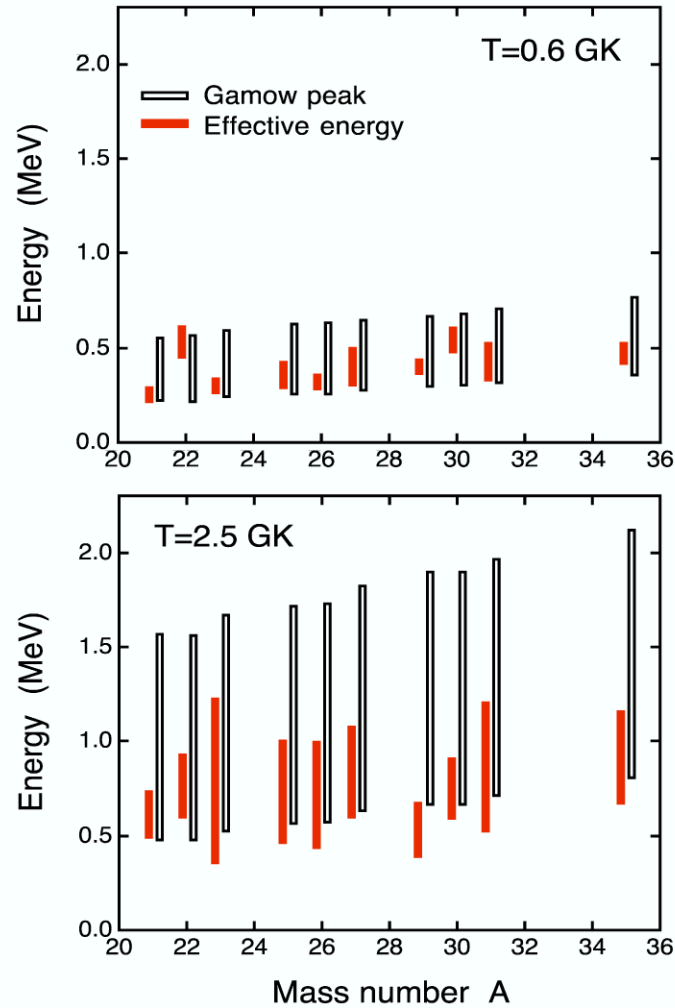
recall that: $\langle\sigma v\rangle = \sqrt{\frac{8}{\mu\pi k^3 T^3}} \int_0^\infty \sigma(E) \exp\left(-\frac{E}{kT}\right) dE$



$$\langle\sigma v\rangle = \sqrt{\frac{8}{\pi\mu k^3 T^3}} \times \int_0^\infty S(E) \exp\left[-\frac{E}{kT} - \left(\frac{E_G}{E}\right)^{1/2}\right] dE$$

$$E_0 = \left(\frac{E_G^{1/2} kT}{2}\right)^{2/3} \quad \Delta E_0 = 4 \left(\frac{E_0 kT}{3}\right)^{1/2}$$

Careful! - the Gamow peak is a useful concept, but it really pertains to non-resonant reactions. However, we tend to use it indiscriminantly. For resonances at high temp., the most effective energy may be less than E_0 !

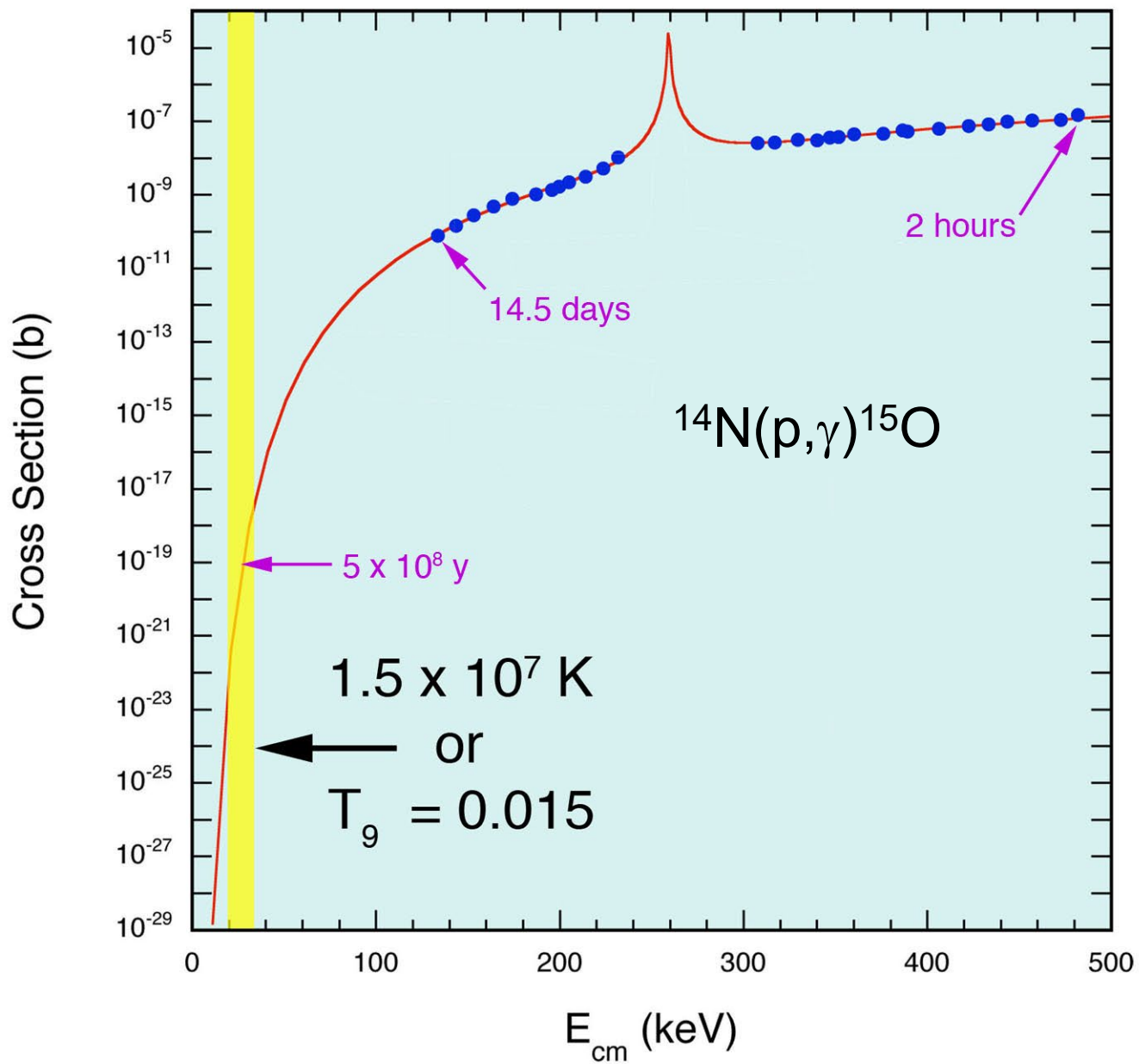


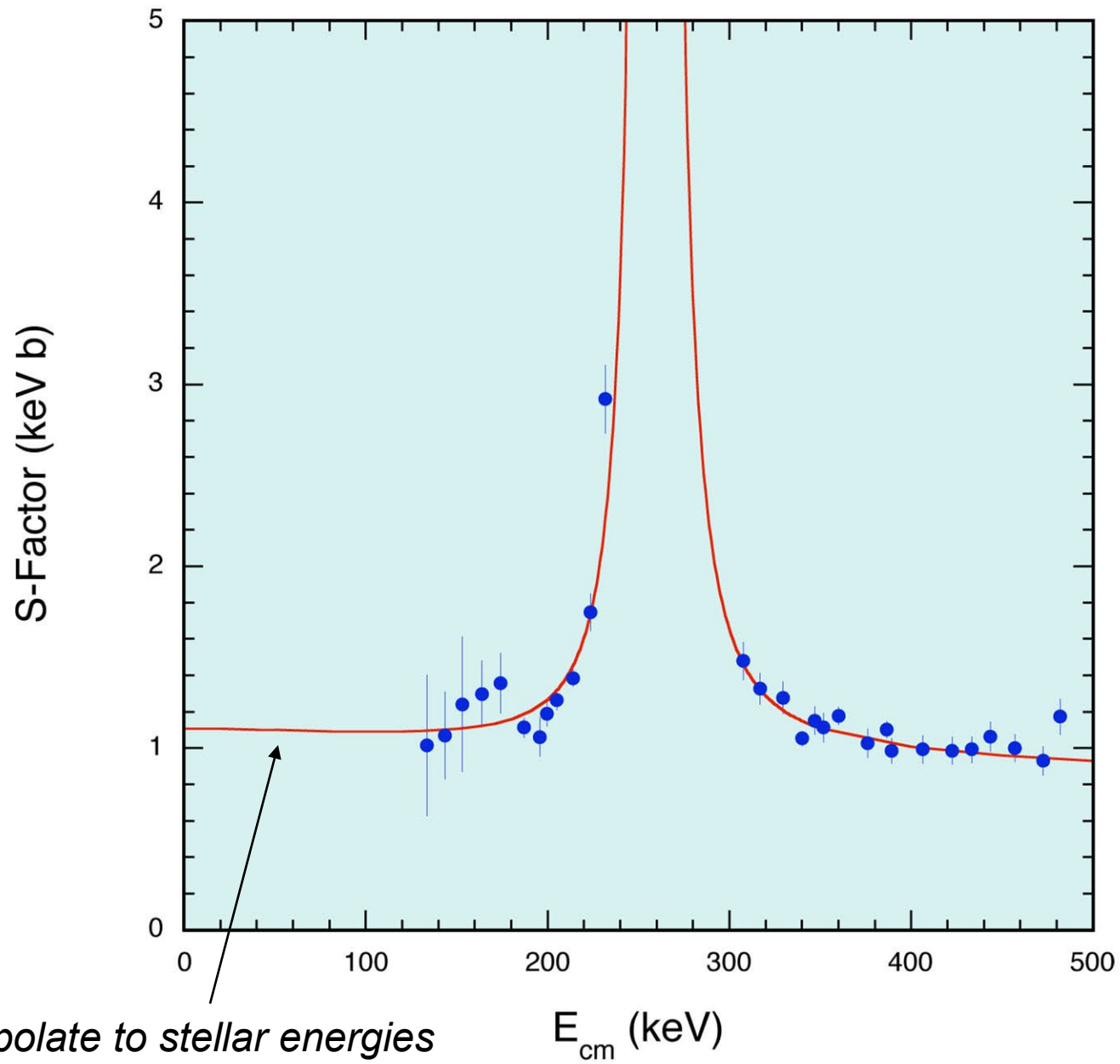
from experimental data

[J.R. Newton et al. Phys. Rev. C 75, 045801 (2007)]

| reaction | place | T_6 | E_0 (keV) |
|----------------------------|---------------|-------|-------------|
| $p + p$ | sun | 15 | 6 |
| $p + {}^{14}\text{N}$ | $3 M_{\odot}$ | 30 | 42 |
| $\alpha + {}^{12}\text{C}$ | red giant | 190 | 300 |
| $p + {}^{17}\text{F}$ | nova | 300 | 232 |
| $\alpha + {}^{30}\text{S}$ | x-ray burst | 1000 | 1793 |

- note: 1) reactions occur in a narrow window around E_0
 2) strong temperature dependence
 $\langle \sigma v \rangle \propto T^{(E_0/kT - 2/3)}$
 3) small cross sections @ E_0





extrapolate to stellar energies

Rough outline of nuclear reactions

1) compound-nuclear

$$\sigma(\alpha, \beta) = \sigma_{CN}(\alpha) \times P(\beta)$$

cross section for forming compound system from entrance channel α

probability of exit channel β

$$P(\beta) = \frac{\Gamma_\beta}{\Gamma}, \quad \Gamma = \sum_\beta \Gamma_\beta$$

a simple model for Γ_β :

decay rate = flux x emitting area

$$\lambda = \lim_{r \rightarrow \infty} v \int_\Omega |\Psi(\vec{r})|^2 r^2 d\Omega$$

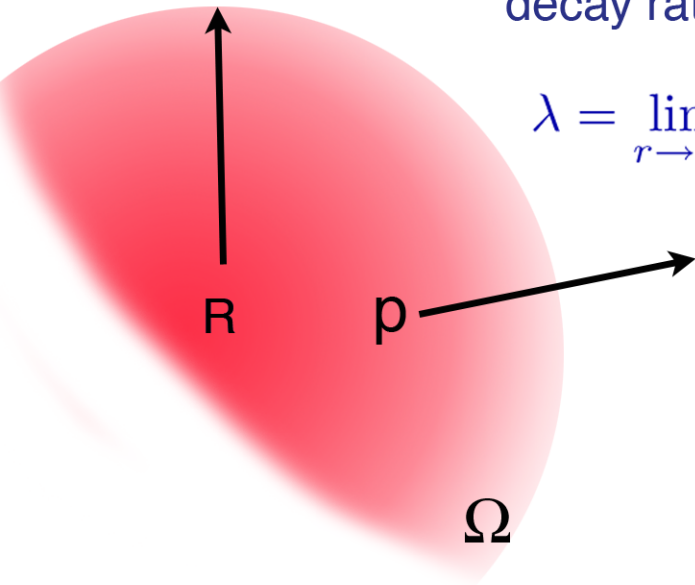
where $\Psi(\vec{r}) = \frac{U_\ell(kr)}{r} Y_{\ell m}(\theta, \phi)$

$$\lambda = \lim_{r \rightarrow \infty} v |U_\ell(kr)|^2 \int |Y_{\ell m}(\theta, \phi)|^2 d\Omega$$

$$= v |U_\ell(\infty)|^2 = \sqrt{\frac{2E}{\mu}} |U_\ell(\infty)|^2$$

define "penetrability" $P_\ell(E) \equiv kR_{nuc} \left| \frac{U_\ell(\infty)}{U_\ell(kR_{nuc})} \right|^2$

(= kR_{nuc} for s - wave neutrons; = $\frac{kR_{nuc}}{F_\ell^2(kR_{nuc}) + G_\ell^2(kR_{nuc})}$ for charged particles)



$$\begin{aligned}
\Gamma_\beta &= \lambda \hbar = \hbar \sqrt{\frac{2E}{\mu}} |U_\ell(\infty)|^2 \\
&= \frac{\hbar^2}{\mu R_{nuc}} |U_\ell(kR_{nuc})|^2 P_\ell(E) \\
&\equiv 2 \gamma_p^2 P_\ell(E) \text{ where } \gamma_p^2 = \frac{\hbar^2}{2\mu R_{nuc}} |U_\ell(kR_{nuc})|^2 \text{ "reduced width"}
\end{aligned}$$

what about $\sigma_{CN}(\alpha)$? (come back to it later)

$\ell = 0$ asymptotic wavefunction: $U_0 = e^{-\imath kr} - S_0 e^{\imath kr}$, $S_0 = e^{2\imath\delta_0}$

now equate logarithmic derivatives at $r = R$:

$$S_0 = \frac{L^I + \imath kR}{L^I - \imath kR} e^{-2\imath kR} \quad \text{and suppose that } L^I = a - \imath b \text{ (inner logarithmic deriv.)}$$

$$S_0 = - \left[\frac{(kR - b) - \imath a}{(kR + b) + \imath a} \right] e^{-2\imath kR} \longrightarrow \sigma_{reaction} = \frac{4\pi}{k^2} \left(1 - |S_0|^2 \right)$$

if you like this so far, you won't mind:

what happens if $a = 0$ at $E = E_r$? (this is equivalent to matching wavefunctions with zero slope @ $r = R$)

$$\text{near } E = E_r: a(E) \simeq \left. \frac{\partial a(E)}{\partial E} \right|_{E=E_r} (E - E_r) \quad \text{so } \frac{a}{a'} = E - E_r$$

$$\frac{a}{a'} = E - E_r \quad \text{and} \quad \Gamma_{scat} \equiv -\frac{2kR}{a'(E_r)}, \quad \Gamma_b \equiv -\frac{2b}{a'(E_r)}, \quad \Gamma = \Gamma_{scat} + \Gamma_b$$

$$\sigma_{res} = \frac{\pi}{k^2} \frac{\Gamma_{scat} \Gamma_b}{(E - E_r)^2 + \Gamma^2/4}$$

a.k.a. Breit-Wigner

for a (p,γ) reaction $\Gamma_{scat} = \Gamma_p, \quad \Gamma_b = \Gamma_\gamma$

$$\sigma_{res} = \frac{\pi}{k^2} \underbrace{\frac{2J_f + 1}{(2J_i + 1)(2J_p + 1)}}_{\omega} \frac{\Gamma_p \Gamma_\gamma}{(E - E_r)^2 + \Gamma^2/4}$$

(spin and higher partial waves included)

some comments:

- 1) Believe it or not, these (seemingly arbitrary) definitions of partial widths are equivalent to the earlier parameterization.
- 2) There's no nuclear potential anywhere in sight so this is not a calculation of the cross section, but a parameterization in terms of (hopefully) observable quantities.
- 3) If $\Gamma \ll E_r$:

$$\langle \sigma v \rangle = \left(\frac{2\pi}{\mu kT} \right)^{3/2} \hbar^2 \omega \gamma e^{-E_r/kT}, \quad \text{where } \gamma = \frac{\Gamma_p \Gamma_\gamma}{\Gamma}$$

“resonance strength”



- 4) If temperatures (energies) are high enough, then resonances are no longer isolated and narrow. Here, it's better to go back to our initial idea of a compound-nuclear cross section, but suitably averaged.

$$\sigma_{CN,l}^J(\alpha) = \frac{\pi}{k_\alpha^2} (2l+1) T_{\alpha l j}^J |\langle j m l 0 | JM \rangle|^2$$

↑
transmission coeff.

$$= \frac{16\mu^2}{\pi^2 \hbar^4} \left| \int \vec{r} j_l(kr) V_l(\vec{r}) U_l(k, \vec{r}) d^3 r \right|^2$$

↑
optical potential

from reciprocity: $P(\beta) = \frac{T_{\beta l' j'}^J}{\sum_{\alpha l j} T_{\alpha l j}^J} |\langle j' m' l' (M - m') | JM \rangle|^2$

$$\sigma(\alpha\beta) = \frac{\pi}{k_\alpha^2} \sum_J \frac{2J+1}{(2j+1)(2j'+1)} \frac{T_{\alpha l j}^J T_{\beta l' j'}^J}{\sum_{\alpha l j} T_{\alpha l j}^J}$$

this is the “Hauser-Feshbach” cross section and it’s no bargain as written $\sum_{\alpha l j} T_{\alpha l j}^J$ can contain thousands of terms (so it must be modeled)

2. direct reactions

Treat (p,γ) in perturbation theory: $\frac{d\sigma}{d\Omega} = \frac{E_\gamma}{2\pi\hbar^2 cv_i} |V_{fi}|^2$

wavefunctions? initial state: target x incident distorted wave
 final state: target x single-particle
 (photon is contained in H_{int})

$$H_{int}(E1) = \sum_m (-i) \left(\frac{4\pi}{3}\right)^{1/2} \frac{E_\gamma}{\hbar c} P \frac{m_1 m_2}{m_1 + m_2} e \left(\frac{Z_1}{m_1} - \frac{Z_1}{m_1}\right) \times D_{mP}^{(1)*} \mathcal{O}_{E1}(r) Y_{\ell m}^*(\theta\phi)$$

helicity = ± 1
rotate into $\theta_\gamma, \phi_\gamma$

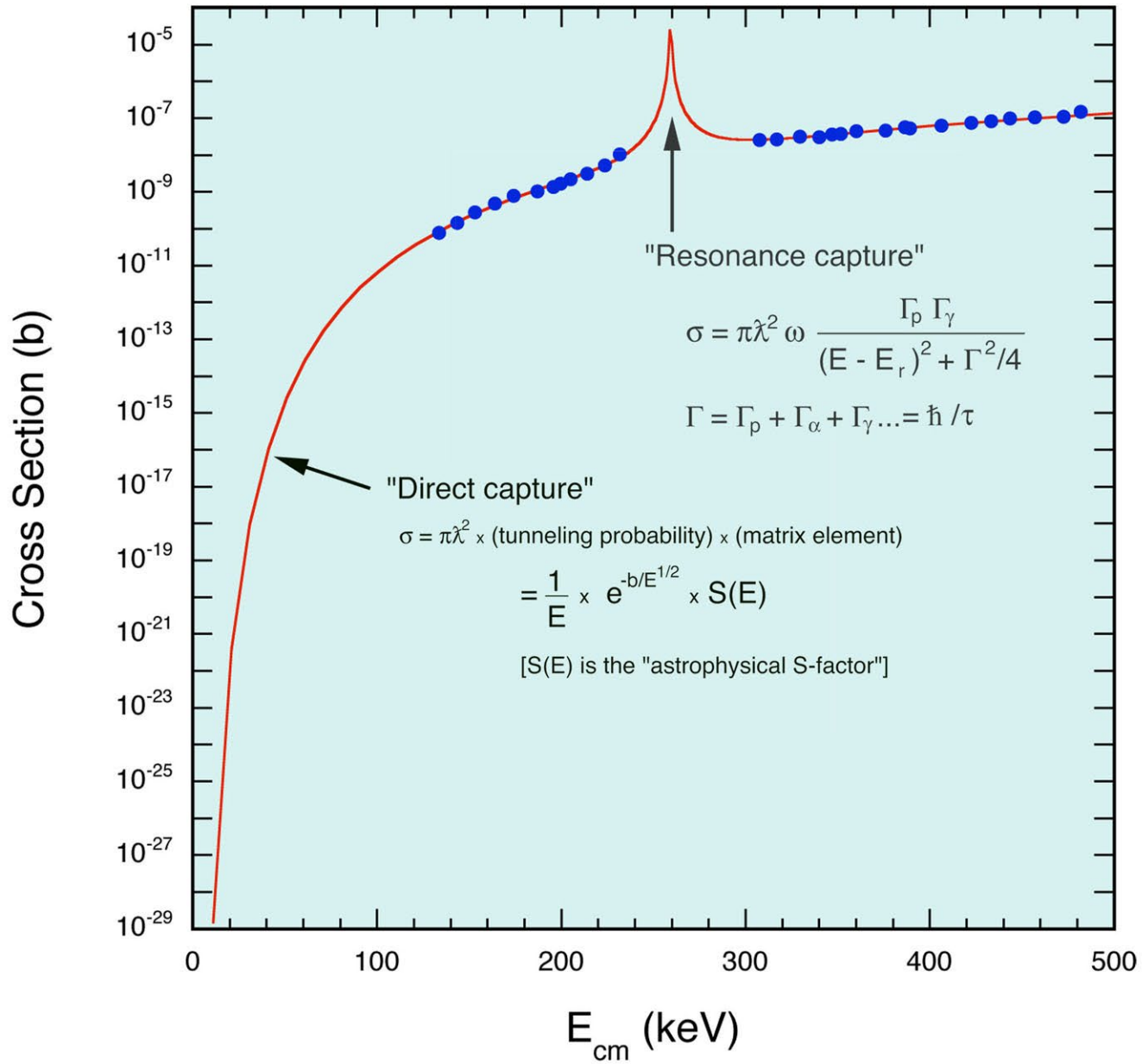
↑
↑

recoil correction
E1 radial operator

left with radial integral: $\mathcal{R}_{fi} = \int_0^\infty R_f(r) \mathcal{O}_{E1}(r) R_i(r) r^2 dr$

“direct capture” $\sigma_{DC}(exp) = \sum_{\ell f} C^2 S_{\ell f} \sigma_{DC}(th)$

$C^2 S_{\ell f}$ is a “spectroscopic factor”. Final state wavefunction assumes a pure single-particle state. Multiply this by spectroscopic amplitude θ for the “real” state. $S = n\theta^2$, where n arises when antisymmetrized wavefunctions are used. C^2 is an isospin C.G. coeff.





inverse reactions!



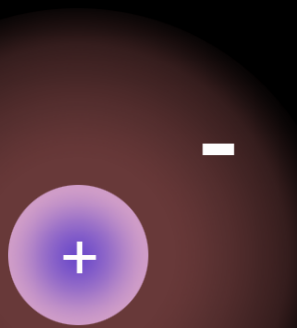
$$\frac{\sigma_{12}}{\sigma_{34}} = \frac{\mu_{12}}{\mu_{34}} \frac{E_{34}}{E_{12}} \frac{(2J_3 + 1)(2J_4 + 1)}{(2J_1 + 1)(2J_2 + 1)}$$

$$\frac{\langle \sigma v \rangle_{34}}{\langle \sigma v \rangle_{12}} = \left(\frac{\mu_{12}}{\mu_{34}} \right)^{1/2} \frac{\int_0^\infty \sigma_{34} E_{34} \exp(-E_{34}/kT) dE_{34}}{\int_0^\infty \sigma_{12} E_{12} \exp(-E_{12}/kT) dE_{12}}$$

$$E_{34} = E_{12} + Q$$

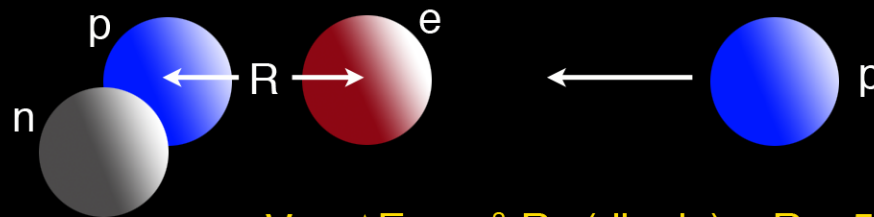
$$= \left(\frac{\mu_{12}}{\mu_{34}} \right)^{3/2} \frac{(2J_1 + 1)(2J_2 + 1)}{(2J_3 + 1)(2J_4 + 1)} e^{-Q/kT}$$

Electron screening: electron cloud shields projectile from nuclear charge in external region



reaction takes place at higher effective energy than for bare nucleus (in star and in lab)

extreme example: d+p

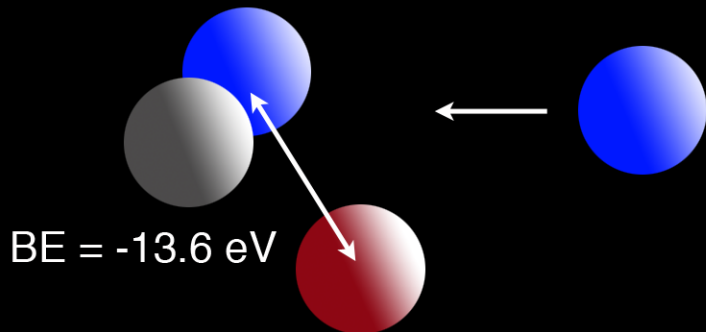


$$V_z = \Delta E = -\frac{e^2 R}{r^2} \text{ (dipole), } R \sim 5 \times 10^{-11} \text{ m}$$

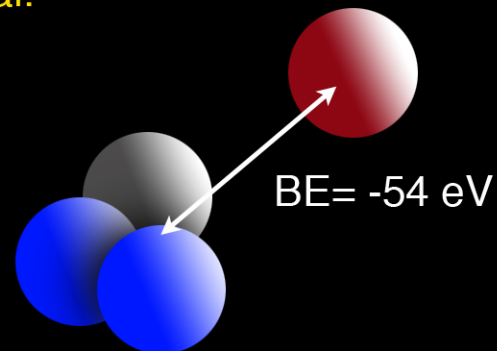
from $r = \infty$ to R , $\Delta E = 29 \text{ eV}$

a bit more realistic:

initial:



final:



(see e.g. D.D. Clayton "Principles of Stellar Evolution & Nucleosynthesis" or Rolfs & Rodney "Cauldrons in the Cosmos")

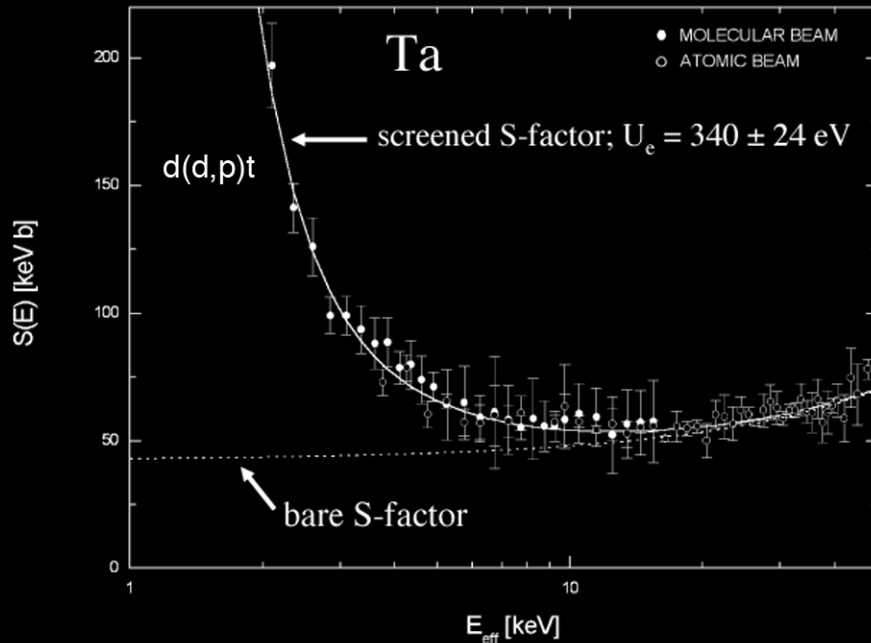
Adiabatic approx:

$\Delta(\text{binding energy}) = 40.4 \text{ eV}$, which should be an upper limit on ΔE

$$\langle \sigma v \rangle_{\text{exp}} = f(E) \langle \sigma v \rangle_{\text{nuc}} \sim \exp(-\Delta E/kT) \langle \sigma v \rangle_{\text{nuc}}$$

in a star, the situation is different: $V(r) = \frac{Z_1 Z_2 e^2}{r} e^{-r/R_D}$, where R_D is the *Debye-Hückel* radius

$$f_{\text{star}} = \exp(Z_1 Z_2 e^2 / R_D kT)$$



when do we care?

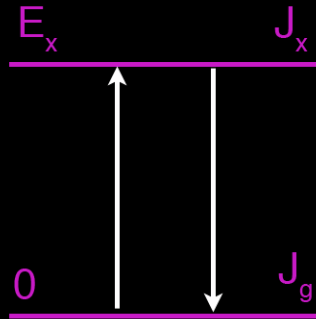
| reaction | T_6 | $\rho(\text{g/cm}^3)$ | $R_D(\text{fm})$ | f |
|----------------------------|-------|-----------------------|------------------|------|
| d+p | 15 | 140 | 2.24e+4 | 1.05 |
| p+ ¹² C | 15 | 140 | 2.24e+4 | 1.35 |
| p+ ¹⁷ F | 300 | 1000 | 3.75e+4 | 1.01 |
| α + ³⁰ S | 1000 | 1e+6 | 2.17e+3 | 1.26 |

expect $\Delta E \leq 52 \text{ eV}$ (hmm..)

[see F. Raiola et al., Phys. Lett. B547, 193 (2002)]

Other things that we sometimes ignore:

thermal population of excited states



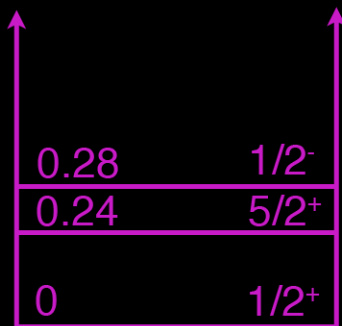
in equilibrium: $N_x \langle \sigma v \rangle_{x \rightarrow g} = N_g \langle \sigma v \rangle_{g \rightarrow x}$

$$\frac{N_x}{N_g} = \frac{\langle \sigma v \rangle_{g \rightarrow x}}{\langle \sigma v \rangle_{x \rightarrow g}} = \frac{2J_x + 1}{2J_g + 1} e^{-E_x/kT}$$

this will affect e.g. proton-capture rate: $\Gamma_p = 2\gamma_p^2 P_\ell(E)$

different core potential

different ℓ , E_r



^{19}Ne

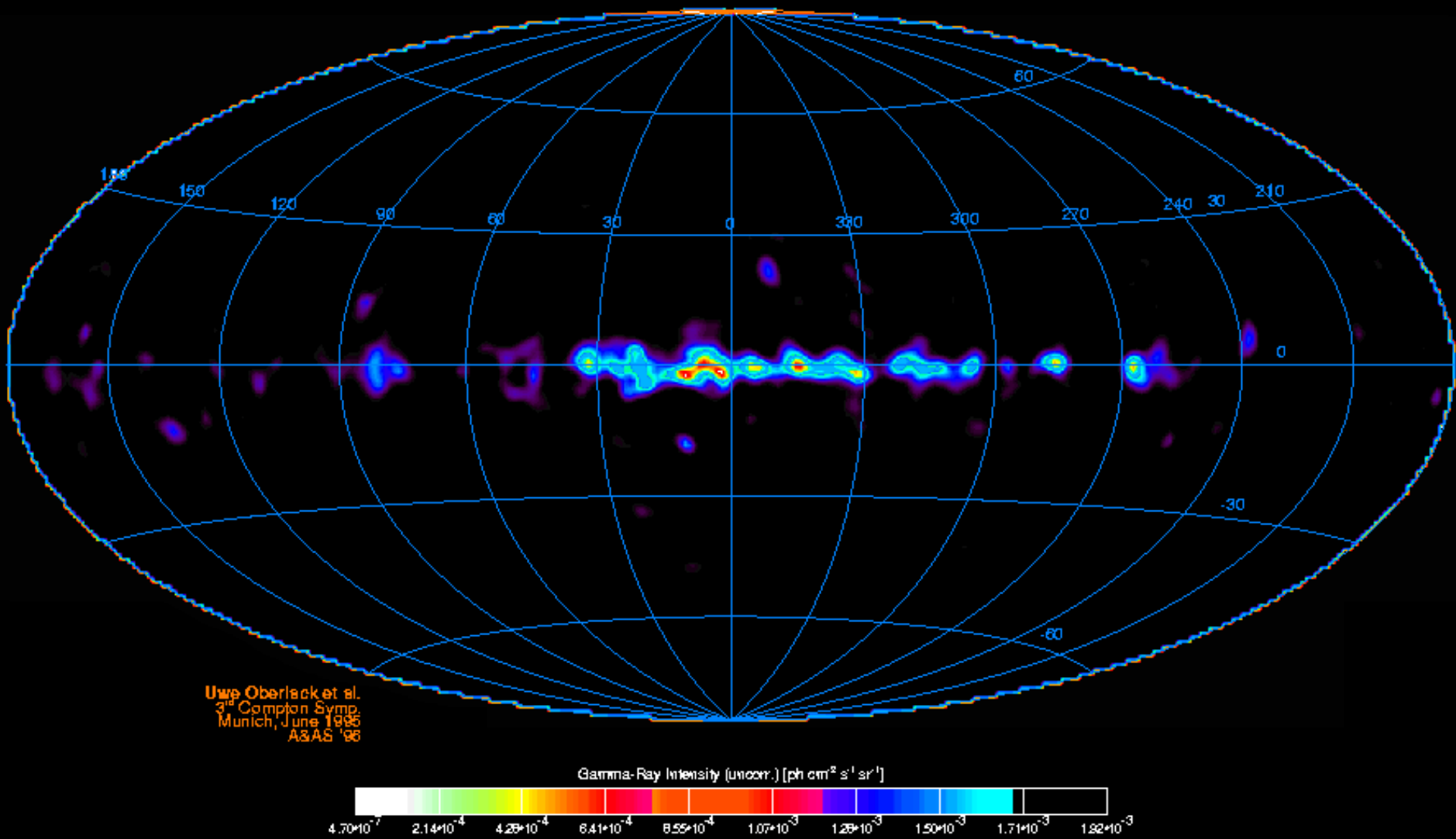
for $^{19}\text{Ne}(p,\gamma)$:

| | $T_g = 0.5$ | 1.5 |
|------|-------------|------|
| N(%) | 98.6 | 62.5 |
| 0 | 1.2 | 30.0 |
| 1 | 0.2 | 7.5 |
| 2 | | |

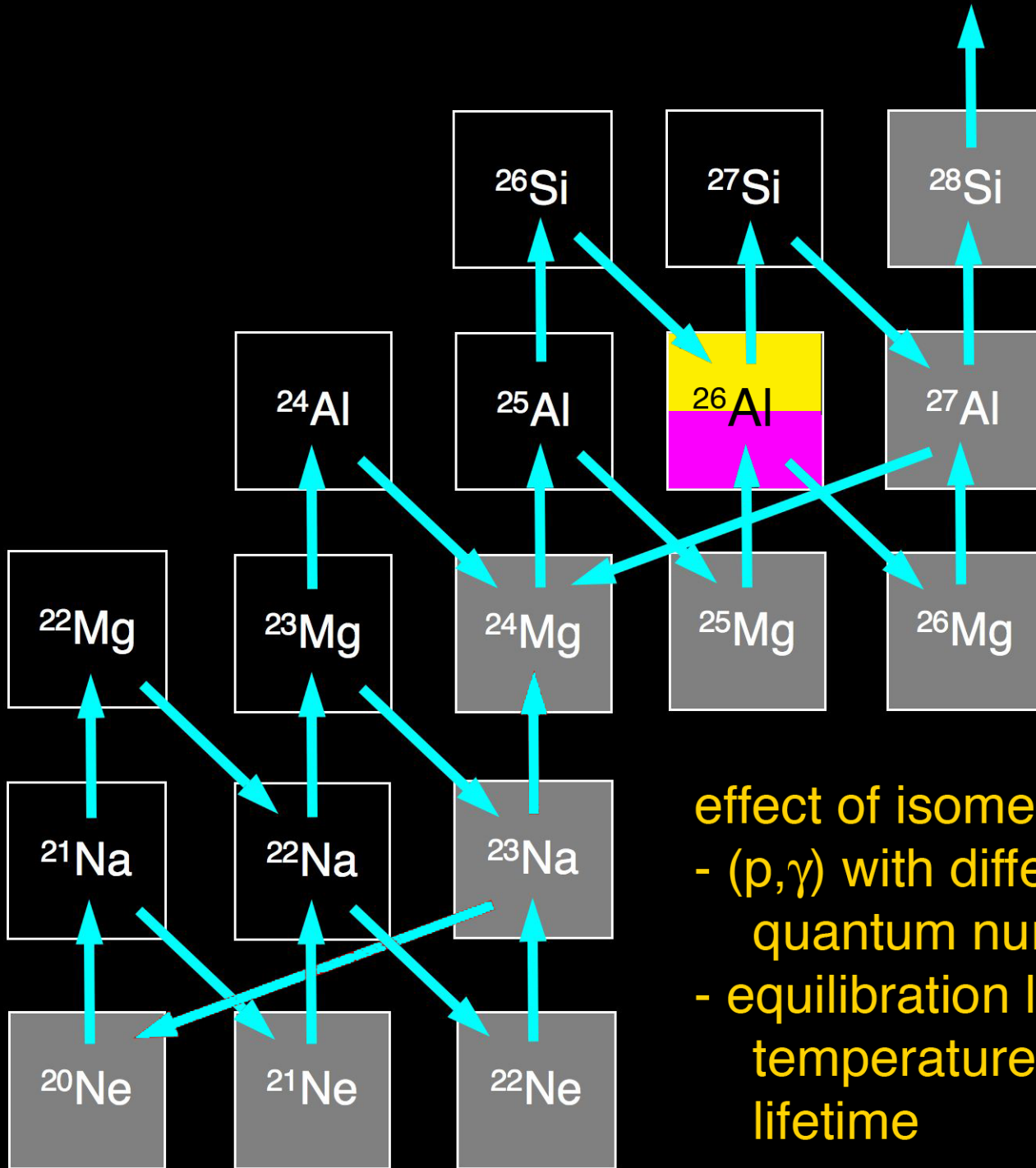
this must be calculated!

An interesting case (and my favorite nucleus) - ^{26}Al

CGRO/COMPTEL 1.8 MeV All-Sky Map

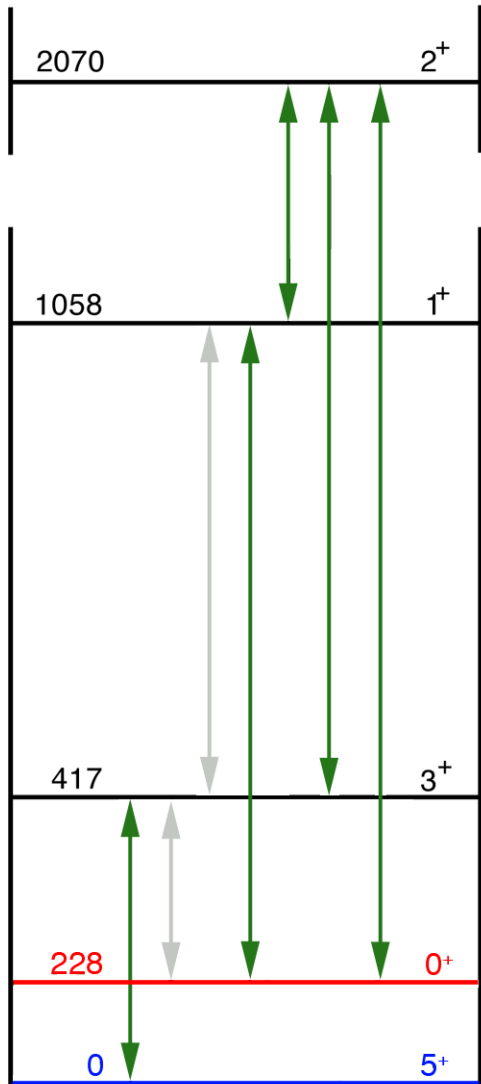


(check out Roland Diehl's web page)



effect of isomer:

- (p, γ) with different Q-value, quantum numbers
- equilibration leads to temperature-dependent lifetime



observed transition

calculated transition

β^+ / EC

$$\lambda_{if} = \frac{g_f}{g_i} \frac{\lambda_s}{e^{E_{if}/kT} - 1}$$

$$\lambda_{if} = \frac{\lambda_s}{1 - e^{-E_{if}/kT}}$$

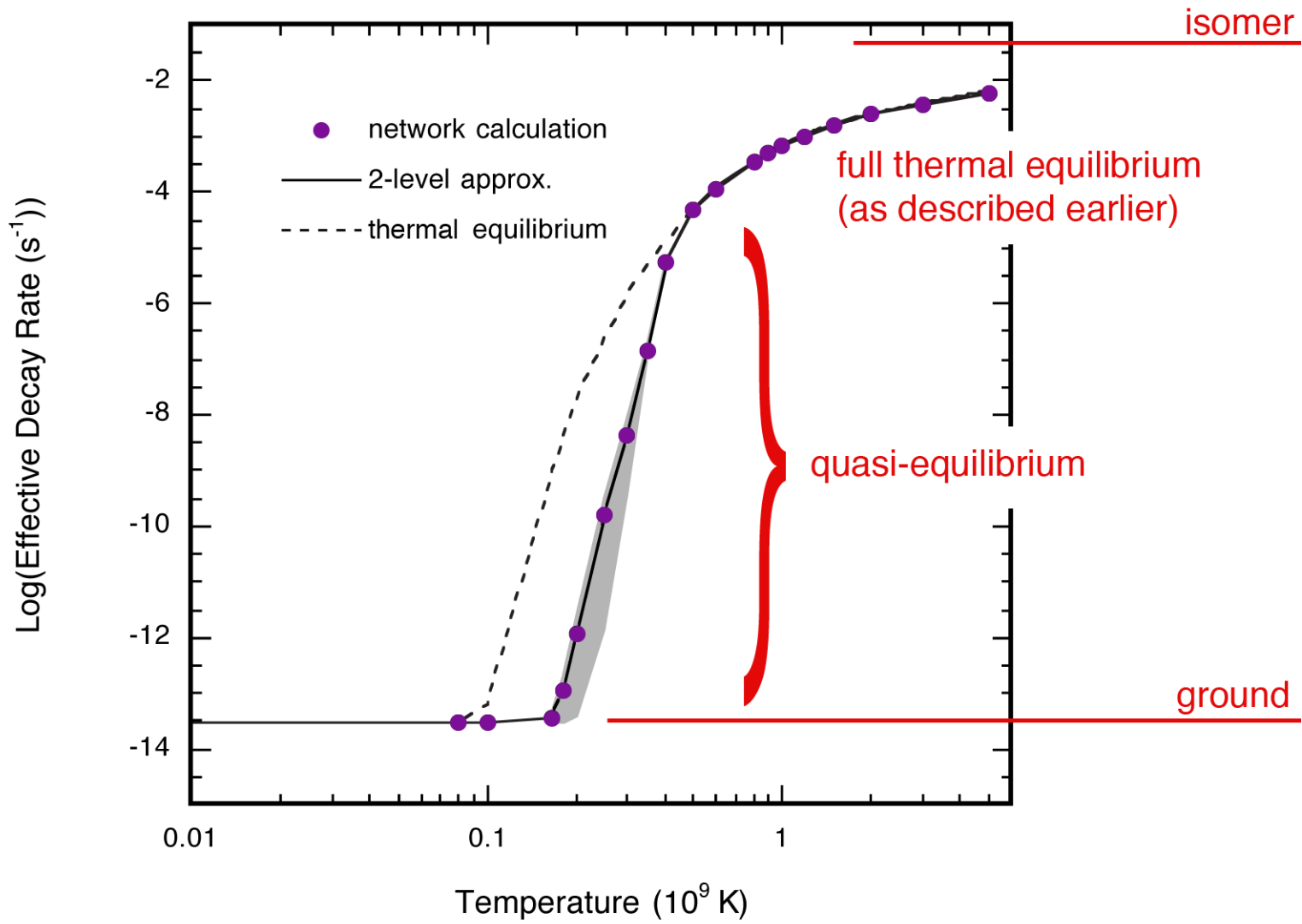
^{26}Al

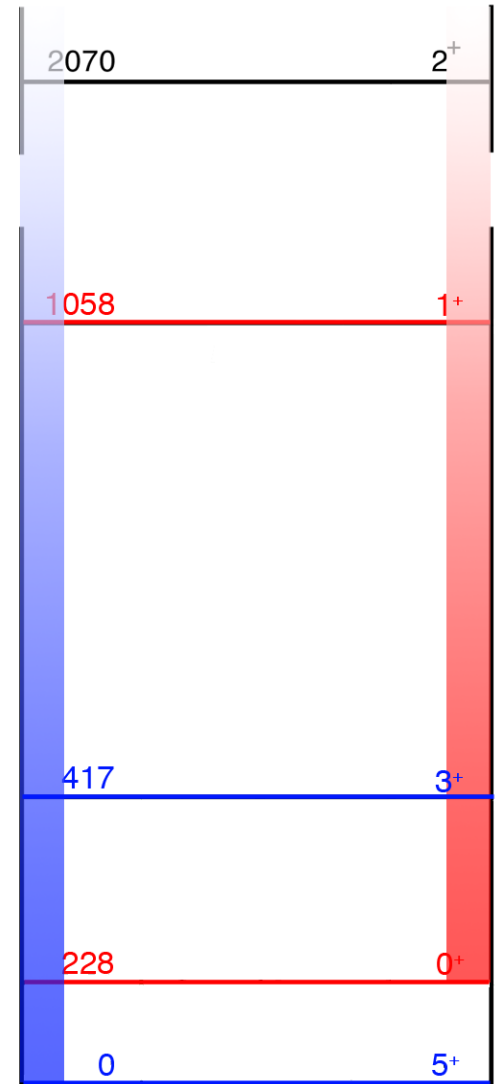
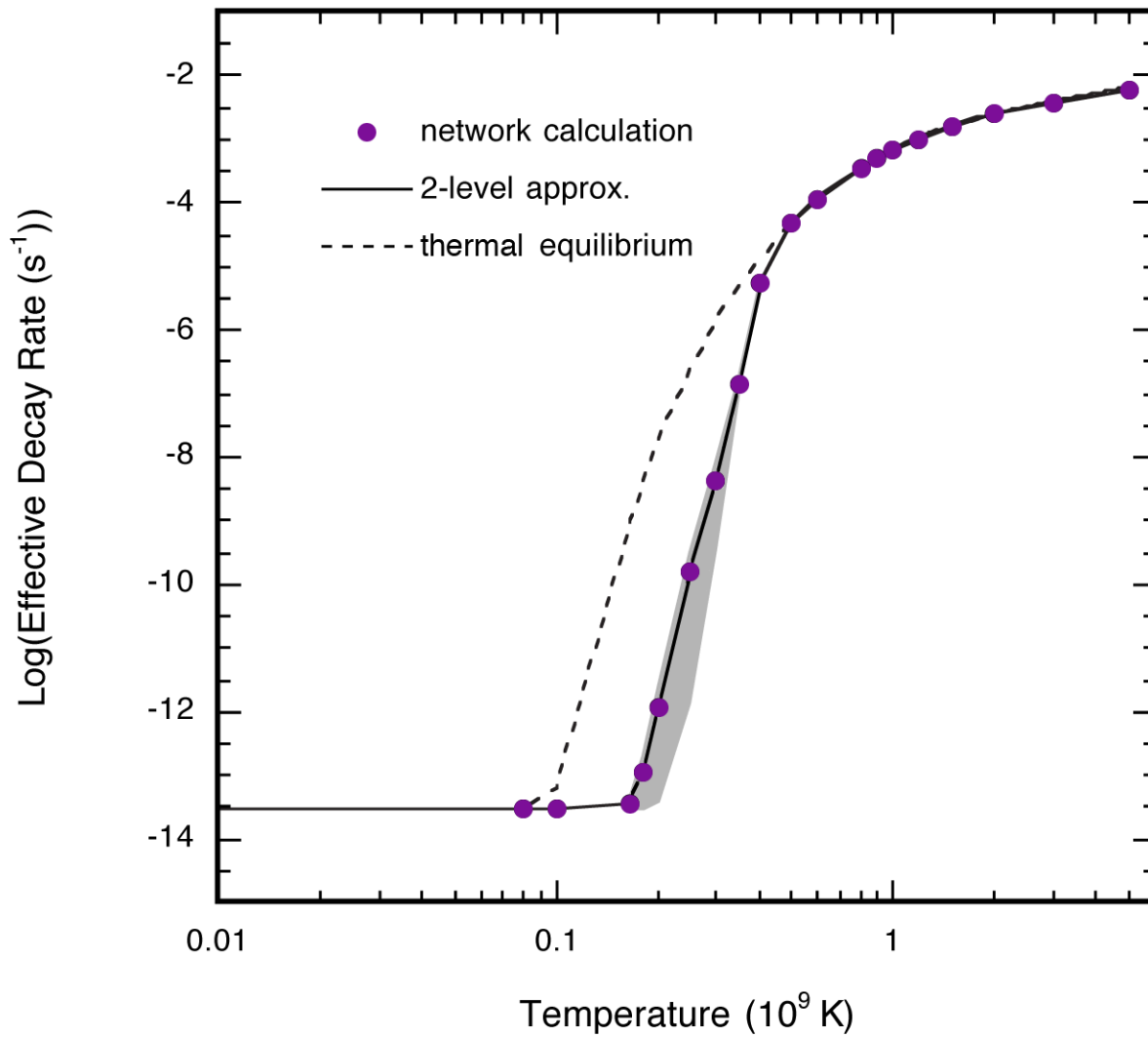
6.35 s

7.2×10^5 y

see: R.C. Runkle et al. *Ap. J.* **556**, 970 (2001)

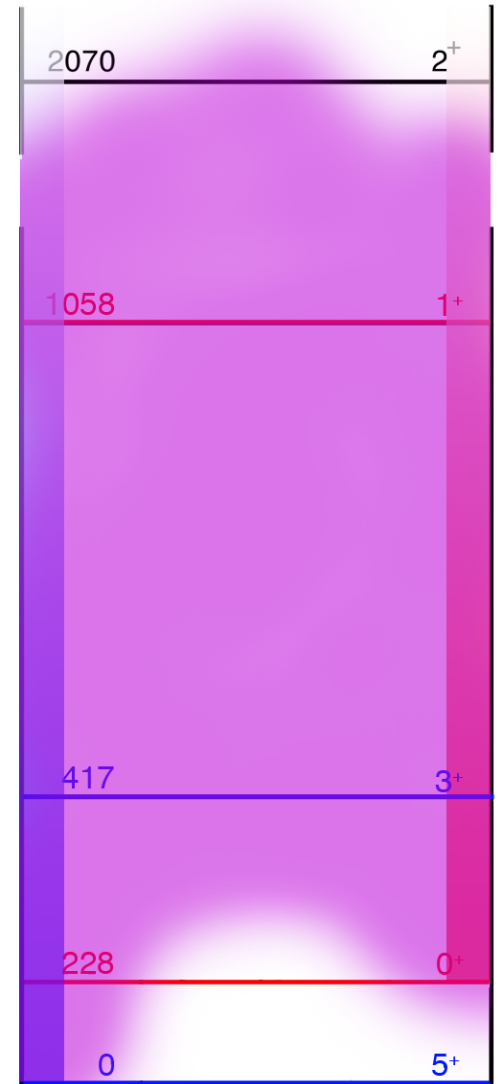
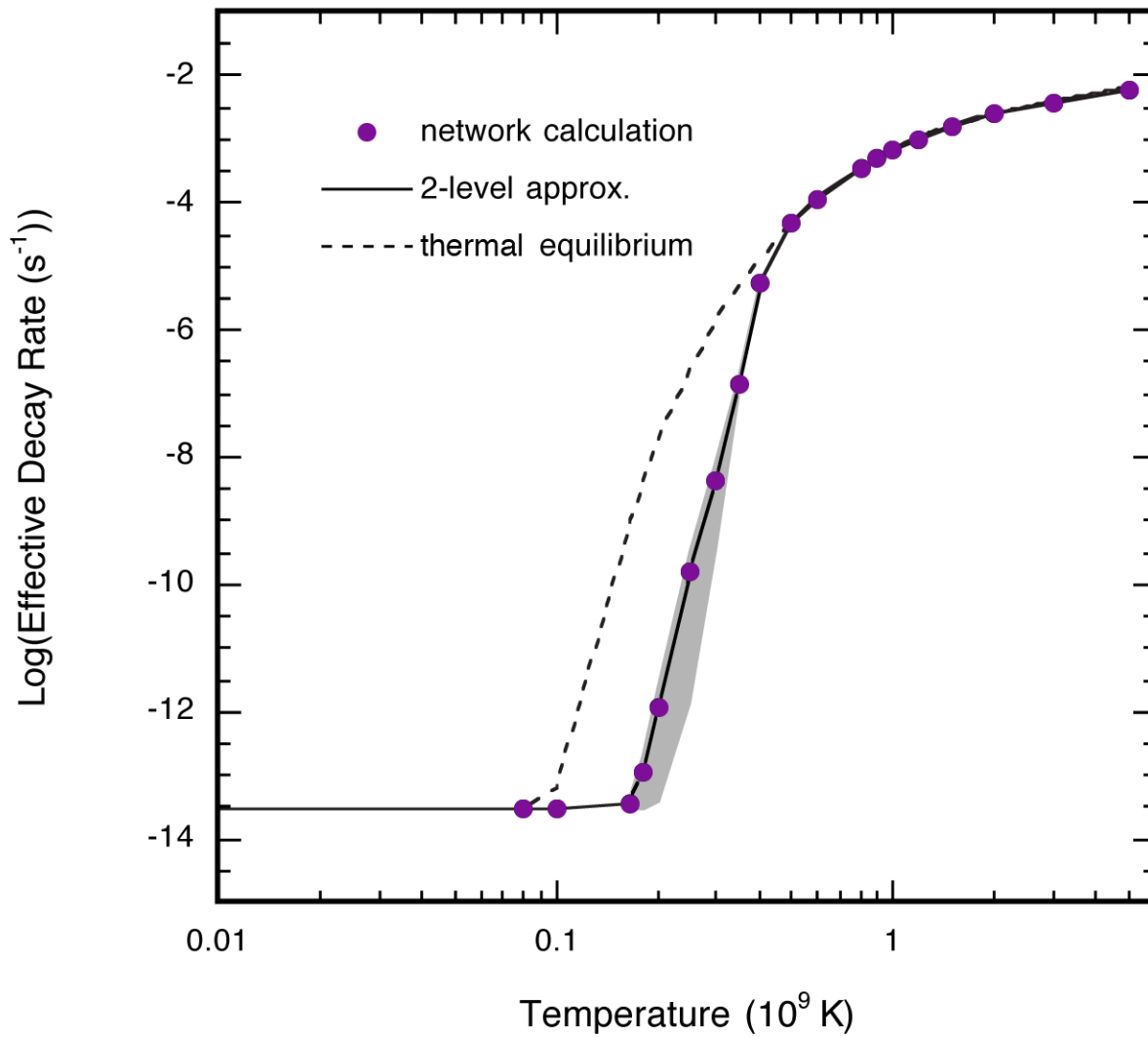
A. Coc et al., *Phys. Rev. C* **61**, 015801 (1999)





Quasi-equilibrium clusters and approach to equilibrium

^{26}Al

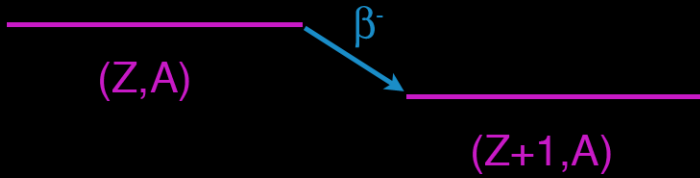


Important feature is interplay of timescales:

τ_{burning} VS. τ_{nuclear} VS. τ_{equil}

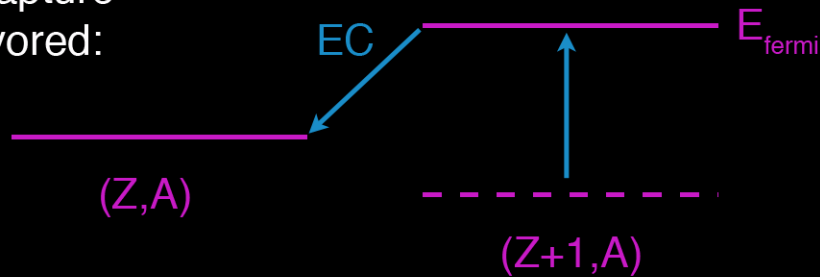
^{26}Al

β^- decay in stellar plasmas:



in a star, electron phase space depends on ρ and degree of ionization; β^- -decay is "turned off" under degenerate conditions

electron capture can be favored:



$$\frac{T_{1/2}^*}{T_{1/2}^{\text{lab}}} \sim \frac{10\mu_e Z^3}{\rho F[Z, w(T)]}$$

(however, removal of inner-shell electrons will suppress EC)

$$Q_{\beta^-} = [M(Z,A) - M(Z+1,A)]c^2 + [B_Z - B_{Z+1}]$$

$$Q_{\beta^+} = [M(Z,A) - M(Z-1,A)]c^2 - 2m_e c^2 + [B_Z - B_{Z-1}]$$

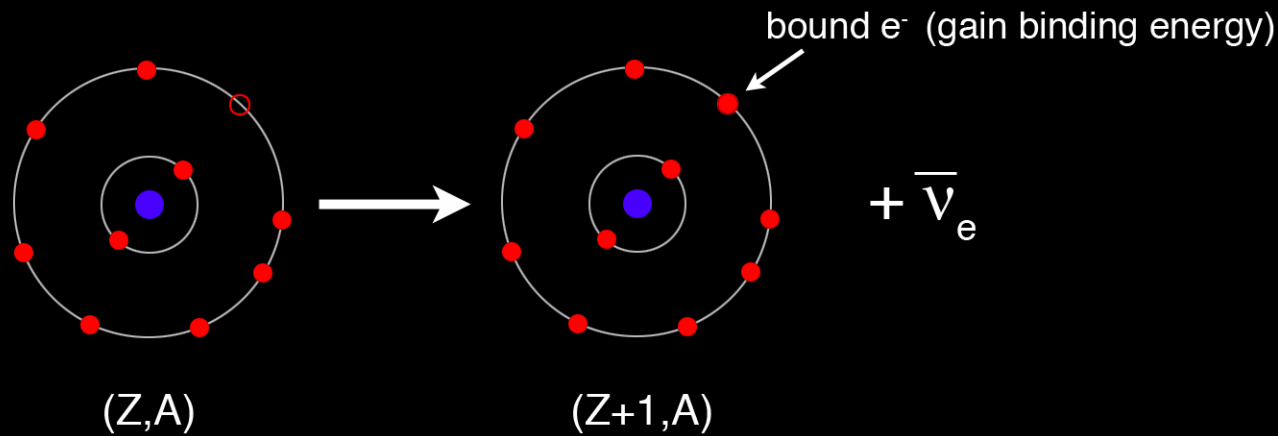
atomic masses

usually ignored

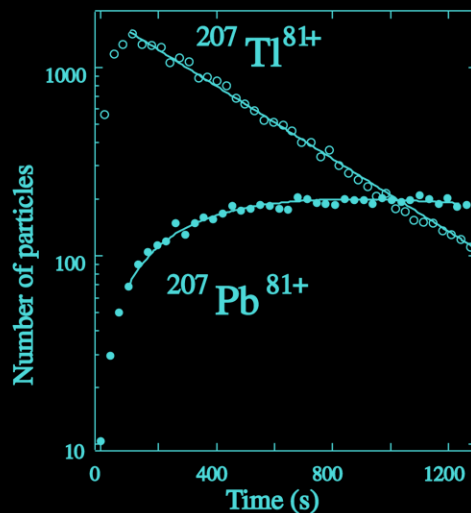
so $\left\{ \begin{array}{l} Q_{\beta^-} \downarrow \text{ as ionization } \uparrow \\ Q_{\beta^+} \uparrow \text{ as ionization } \uparrow \end{array} \right.$

[see e.g. J.N. Bahcall, *Ap. J.* **139**, 318 (1964); G.M. Fuller et al., *Ap. J. Supp.* **42**, 447 (1980) and **48**, 279 (1982); T. Kajino et al., *Nucl. Phys.* **A480**, 175 (1988)]

on the other hand, ionization can allow “bound-state β -decay” to occur:



^{163}Dy , ^{187}Re , ^{193}Ir , ^{205}Tl are stable (or nearly so) as neutral atoms, but undergo bound-state decay when fully ionized



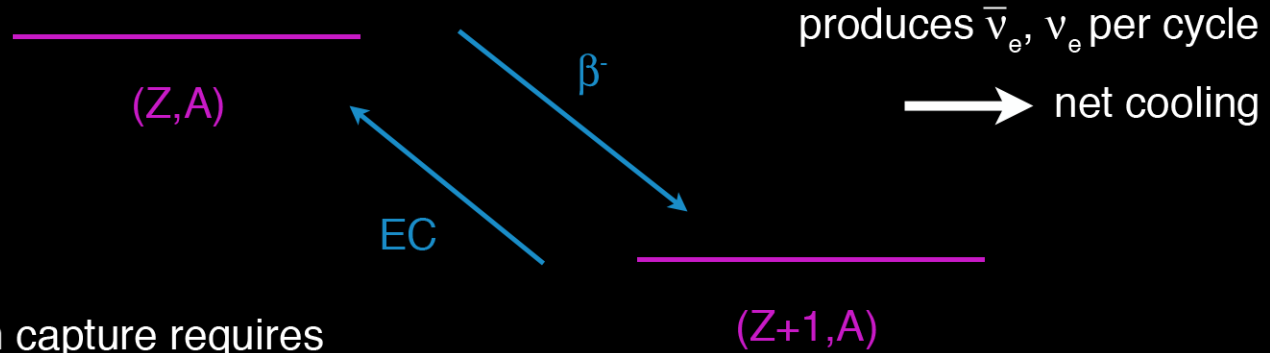
$$T_{1/2}(\text{bound} + \text{continuum}) = 264(10) \text{ s}$$

$$\text{vs. } T_{1/2}(\text{EC}) = 286(2) \text{ s}$$

FIG. 3. Number of stored bare $^{207}\text{Tl}^{81+}$ ions and their β_b daughters $^{207}\text{Pb}^{81+}$ as a function of the storage time in the ESR. The statistical errors for most data points are smaller than the size of the symbols.

Exotica: the “Urca” process*

simplest form:



upward electron capture requires energy from (\sim degenerate) electron gas

e.g. for $^{23}\text{Ne} \longleftrightarrow ^{23}\text{Na}$ pair, $\rho \geq 1.7 \times 10^9 \text{ g/cm}^3$ (important in cores of massive stars)

[see e.g., D. Arnett, “Supernovae and Nucleosynthesis”, ch. 11]

*named for a Rio de Janeiro casino



calculating nucleosynthesis

have relative isotopic abundances $Y_i = X_i/A_i$
 and reaction rates $N_A \langle \sigma v \rangle$ ($\text{cm}^3 \text{s}^{-1} \text{mole}^{-1}$)

+ = production

- = destruction

number of particles
of type i

$$\frac{dY_i}{dt} = \sum_j (\pm) N_i \lambda_j Y_j + \sum_{j,k} \underbrace{\frac{(\pm) N_i}{N_j! N_k!}}_{= (1 + \delta_{jk})} \rho N_A \langle \sigma v \rangle_{j,k} Y_j Y_k$$

decays 2-body reactions

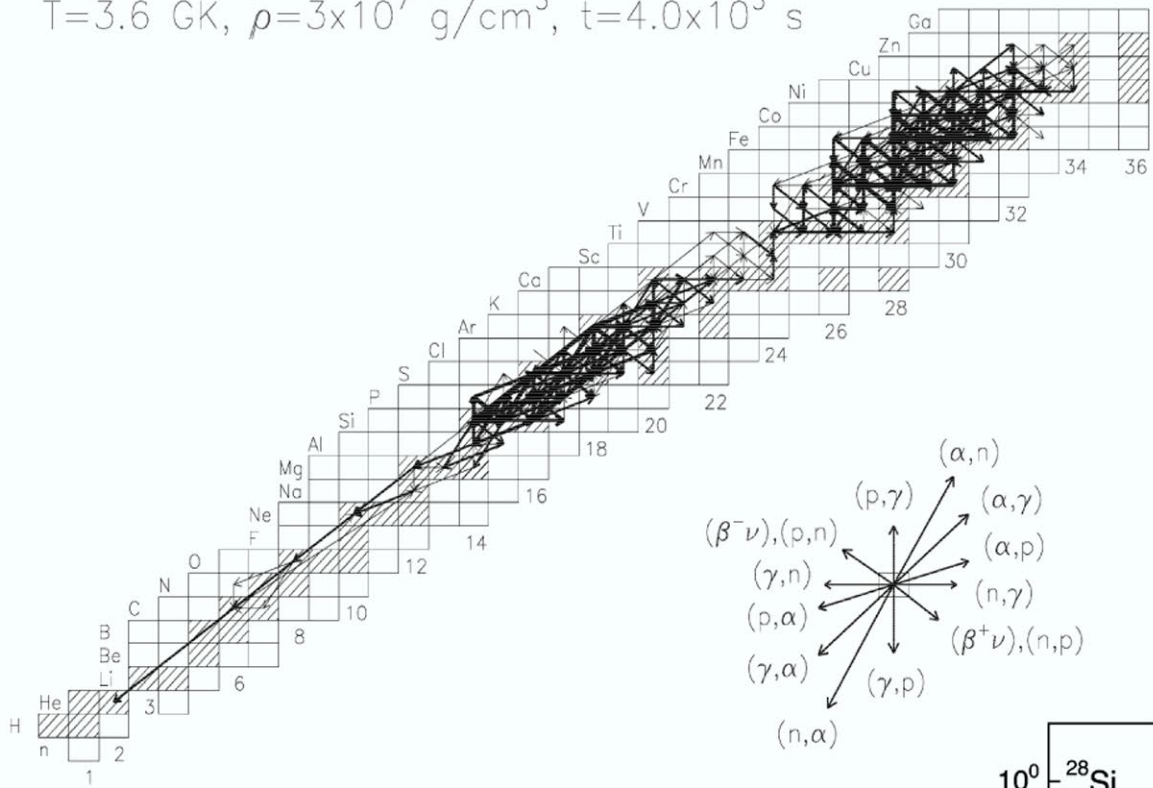
$$+ \sum_{j,k,l} \frac{(\pm) N_i}{N_j! N_k! N_l!} \rho^2 N_A^2 \langle \sigma v \rangle_{j,k,l} Y_j Y_k Y_l \quad (\text{reactions/s})$$

3-body reactions

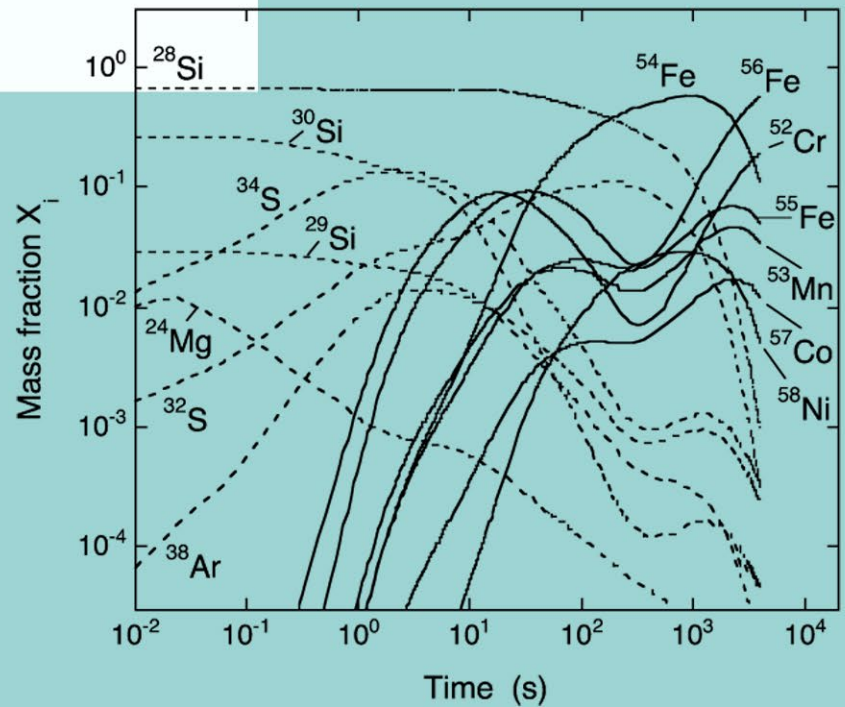
net flow $F_{i,j} = \int \left[\frac{dY_i}{dt} \Big|_{(i \rightarrow j)} - \frac{dY_j}{dt} \Big|_{(j \rightarrow i)} \right] dt$

energy released $\epsilon = \sum_{i,j} F_{i,j} Q_{i,j}$

$T=3.6 \text{ GK}$, $\rho=3 \times 10^7 \text{ g/cm}^3$, $t=4.0 \times 10^3 \text{ s}$



Core Si-burning
 $25 M_{\odot}$



(courtesy of C. Iliadis)

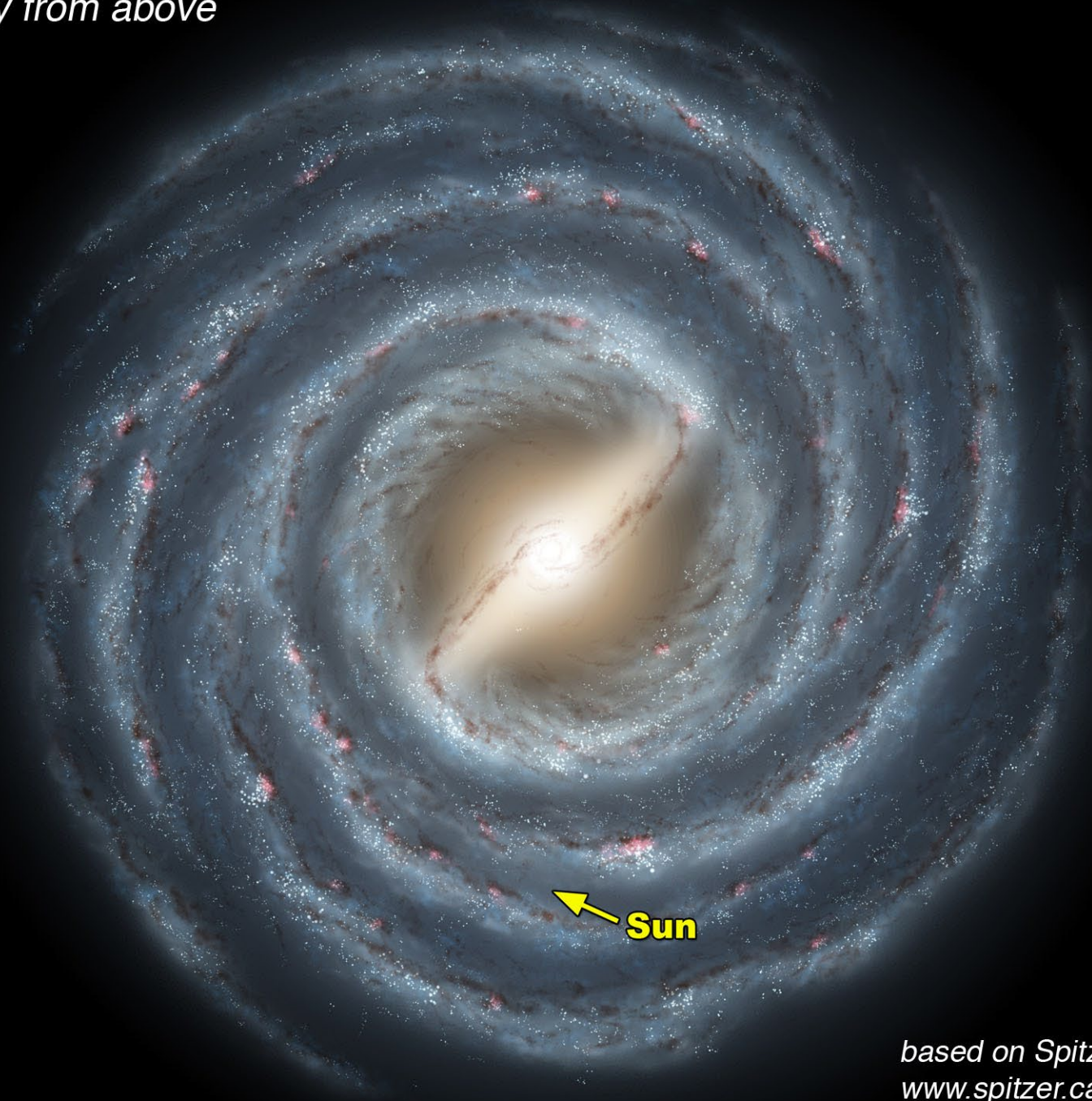
Nucleosynthesis and galactic evolution



Sombrero Galaxy • M104

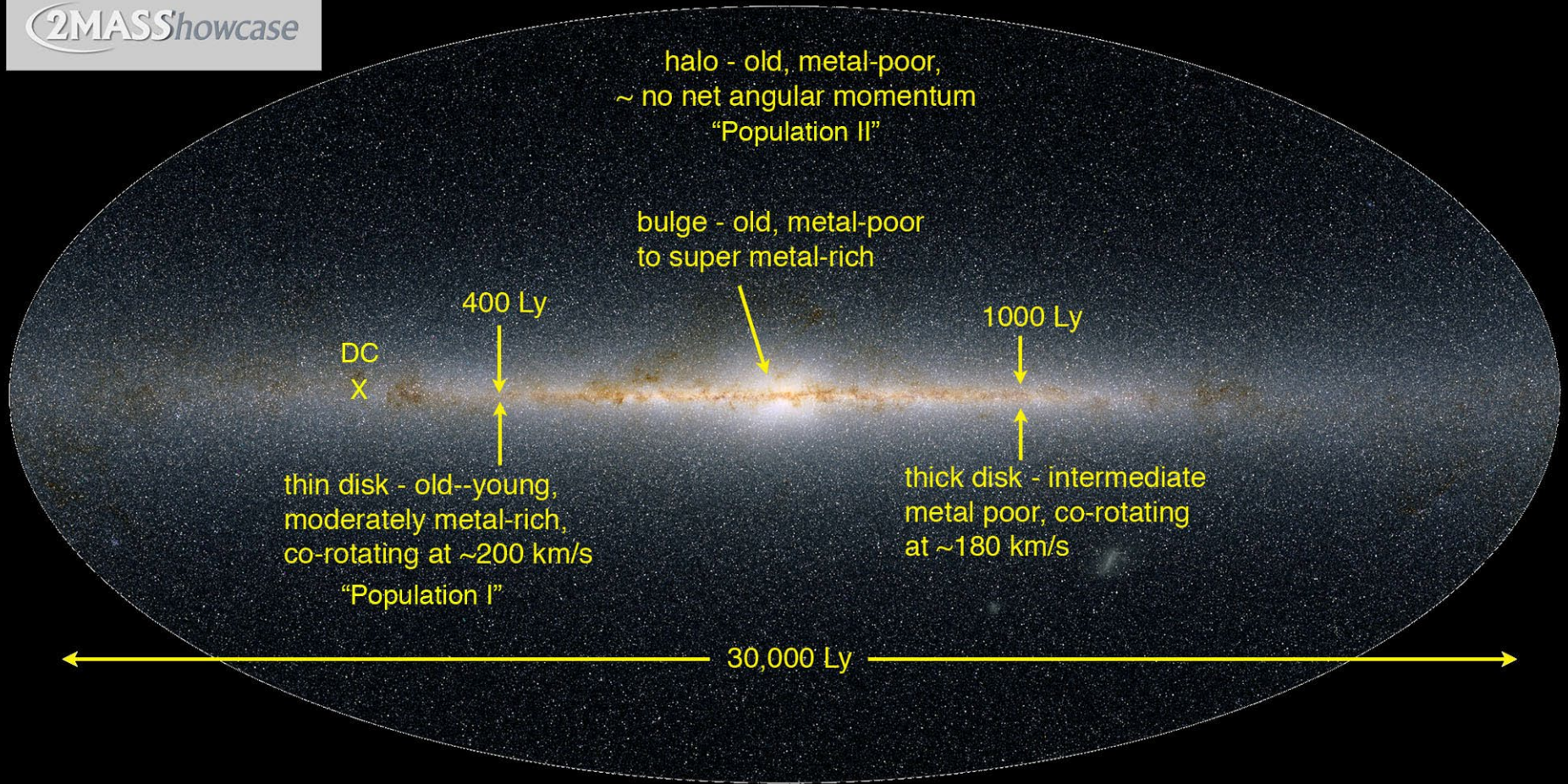
NASA and The Hubble Heritage Team (STScI/AURA) • Hubble Space Telescope ACS • STScI-PRC03-28

Milky Way from above



based on Spitzer observations
www.spitzer.caltech.edu

side view:



some interesting questions

when did the galaxy form?

how? rapid collapse of halo followed by relaxation into disk?

2 collapse episodes?

mergers?

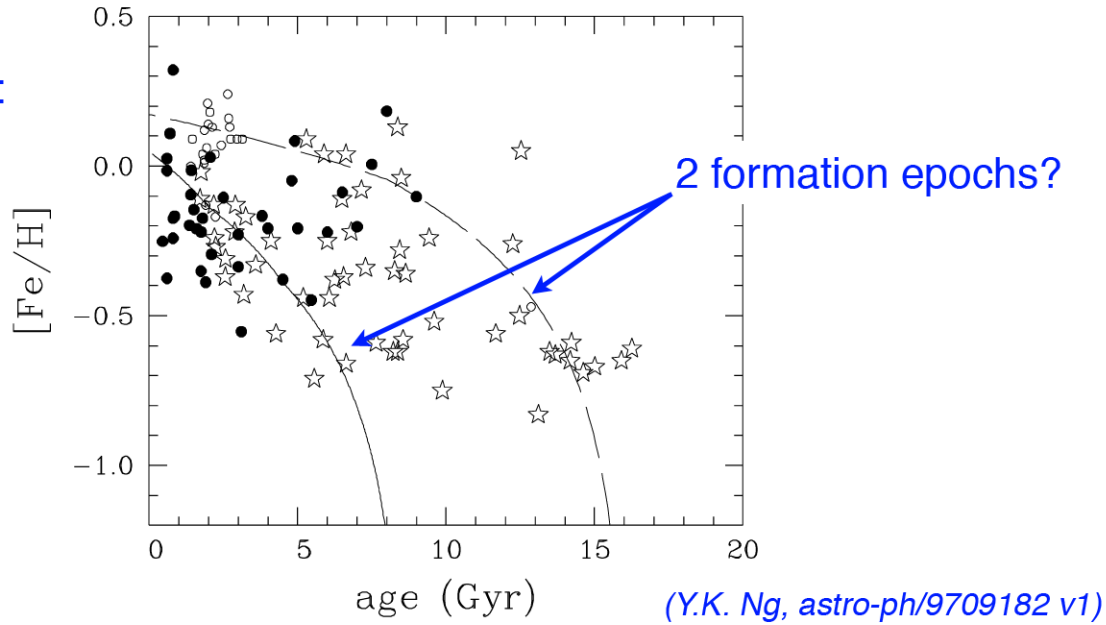
did the first stars form before the galaxy?

what is the relationship between the thin/thick disks, bulge and halo?

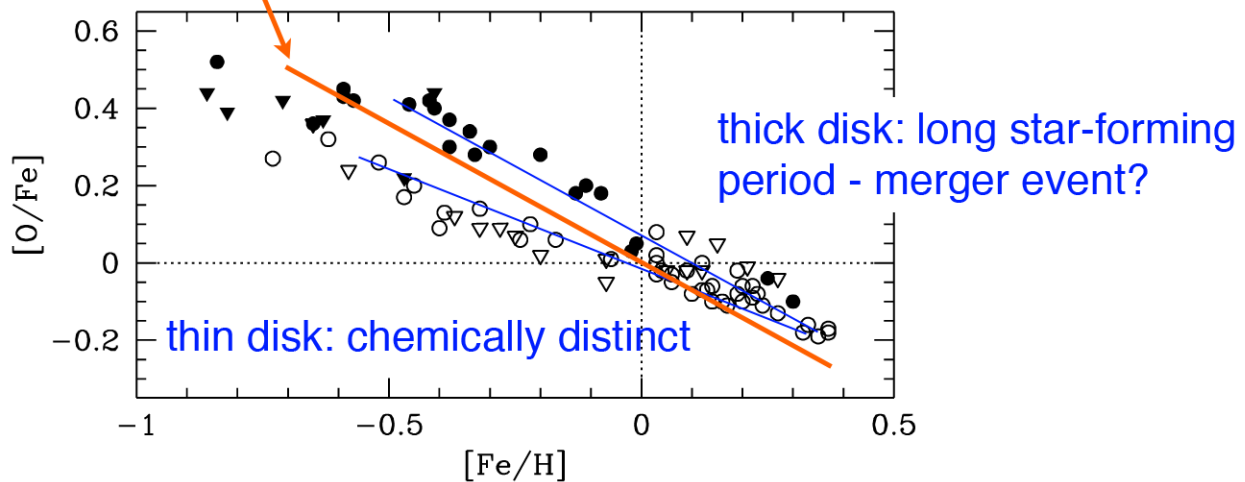
etc.

some clues from stellar evolution and nucleosynthesis
(as well as populations, kinematics, etc.)

disk:



O from short-lived, massive stars (SNII);
Fe from longer-lived, lower-mass (SNIa)

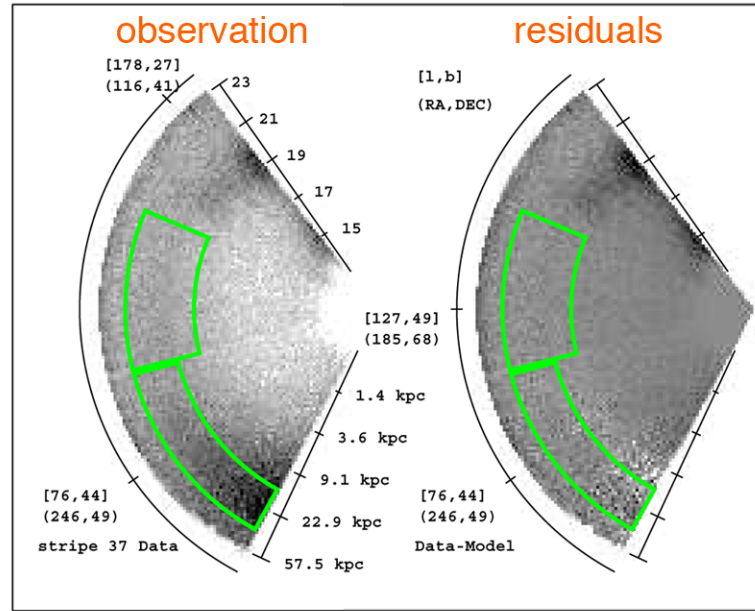
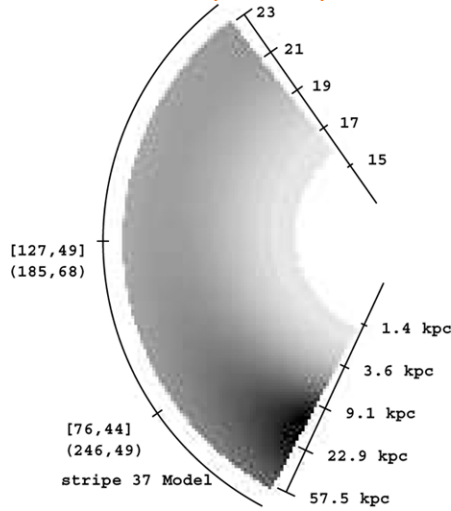


halo observations:

Sloan Digital Sky Survey Scan

[H.J. Newberg and B. Yanny, astro-ph0507671 v1 (2005)]

star density for spheroidal halo (model)

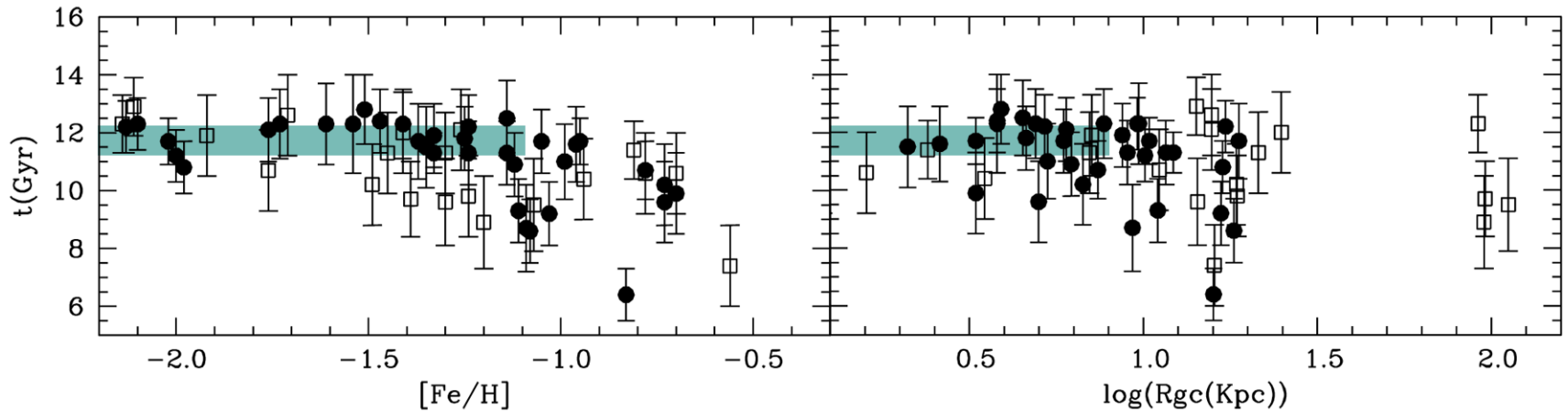


clumps and tidal streams consistent with mergers

but:

ages of 55 globular clusters:

M. Salaris and A. Weiss, *Astron & Astrophys.* **388**, 492 (2002)]



clusters with $[Fe/h] < -1.2$ and $r < 8$ kpc formed at the same time, throughout the halo

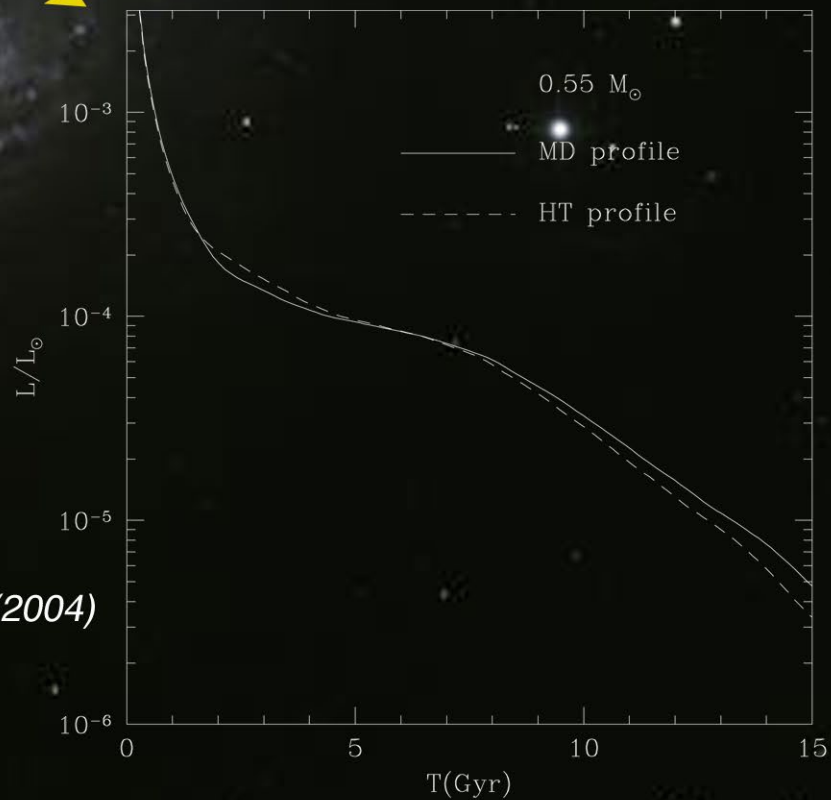
how to measure the age of the galaxy and/or galactic timescales:

1. globular clusters

2. r-process abundances in metal-poor halo stars

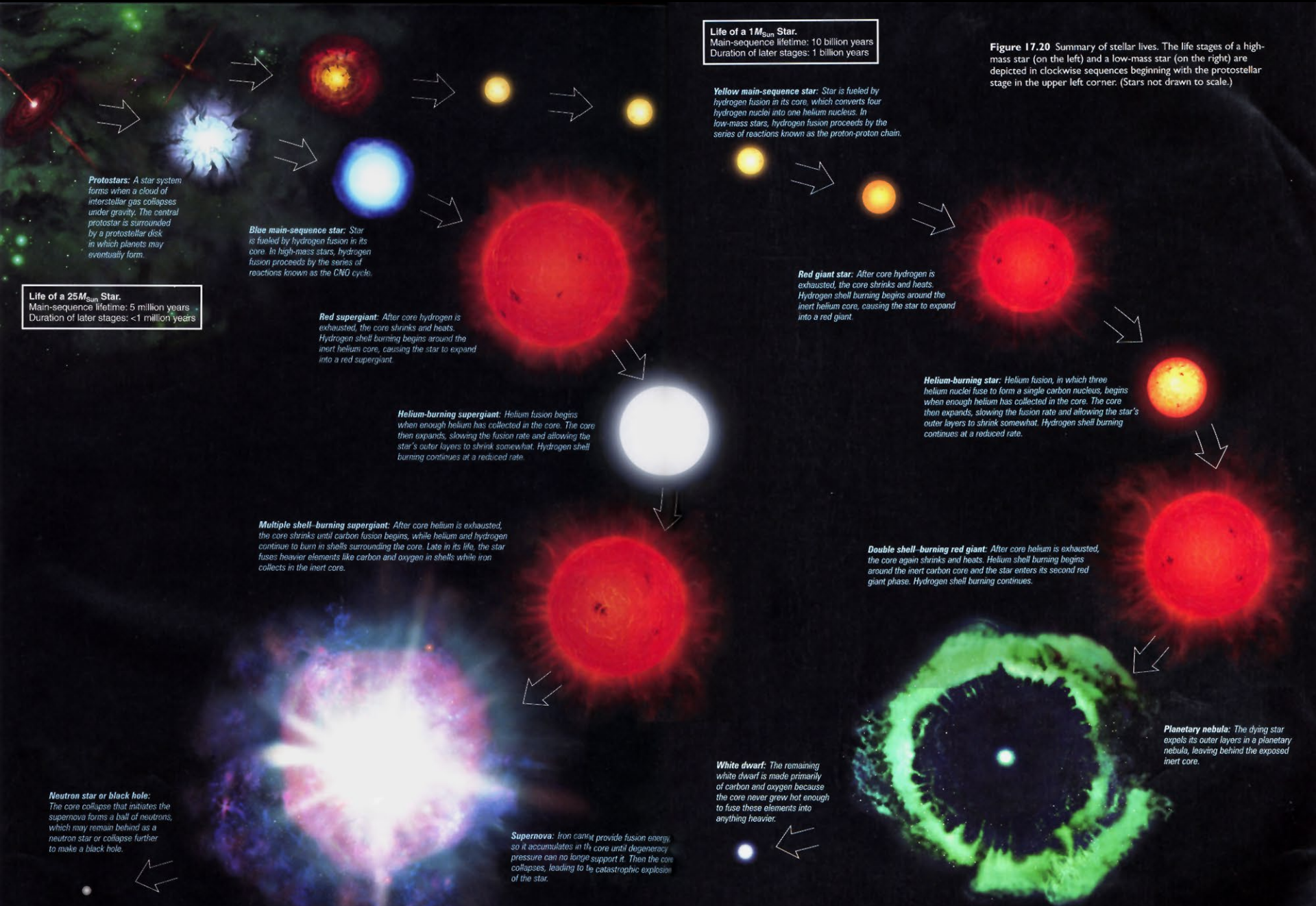
3. white dwarf cooling curves

} more to come



see B.M.S. Meyer et al., astro-ph/0401443 v1 (2004)

Quick tour of stellar evolution:



Protostars: A star system forms when a cloud of interstellar gas collapses under gravity. The central protostar is surrounded by a protostellar disk in which planets may eventually form.

Life of a $25M_{\text{sun}}$ Star.
Main-sequence lifetime: 5 million years
Duration of later stages: <1 million years

Blue main-sequence star: Star is fueled by hydrogen fusion in its core. In high-mass stars, hydrogen fusion proceeds by the series of reactions known as the CNO cycle.

Red supergiant: After core hydrogen is exhausted, the core shrinks and heats. Hydrogen shell burning begins around the inert helium core, causing the star to expand into a red supergiant.

Helium-burning supergiant: Helium fusion begins when enough helium has collected in the core. The core then expands, slowing the fusion rate and allowing the star's outer layers to shrink somewhat. Hydrogen shell burning continues at a reduced rate.

Multiple shell-burning supergiant: After core helium is exhausted, the core shrinks until carbon fusion begins, while helium and hydrogen continue to burn in shells surrounding the core. Late in its life, the star fuses heavier elements like carbon and oxygen in shells while iron collects in the inert core.

Neutron star or black hole: The core collapse that initiates the supernova forms a ball of neutrons, which may remain behind as a neutron star or collapse further to make a black hole.

Supernova: Iron cannot provide fusion energy, so it accumulates in the core until degeneracy pressure can no longer support it. Then the core collapses, leading to a catastrophic explosion of the star.

Life of a $1M_{\text{sun}}$ Star.
Main-sequence lifetime: 10 billion years
Duration of later stages: 1 billion years

Yellow main-sequence star: Star is fueled by hydrogen fusion in its core, which converts four hydrogen nuclei into one helium nucleus. In low-mass stars, hydrogen fusion proceeds by the series of reactions known as the proton-proton chain.

Red giant star: After core hydrogen is exhausted, the core shrinks and heats. Hydrogen shell burning begins around the inert helium core, causing the star to expand into a red giant.

Helium-burning star: Helium fusion, in which three helium nuclei fuse to form a single carbon nucleus, begins when enough helium has collected in the core. The core then expands, slowing the fusion rate and allowing the star's outer layers to shrink somewhat. Hydrogen shell burning continues at a reduced rate.

Double shell-burning red giant: After core helium is exhausted, the core again shrinks and heats. Helium shell burning begins around the inert carbon core and the star enters its second red giant phase. Hydrogen shell burning continues.

White dwarf: The remaining white dwarf is made primarily of carbon and oxygen because the core never grew hot enough to fuse these elements into anything heavier.

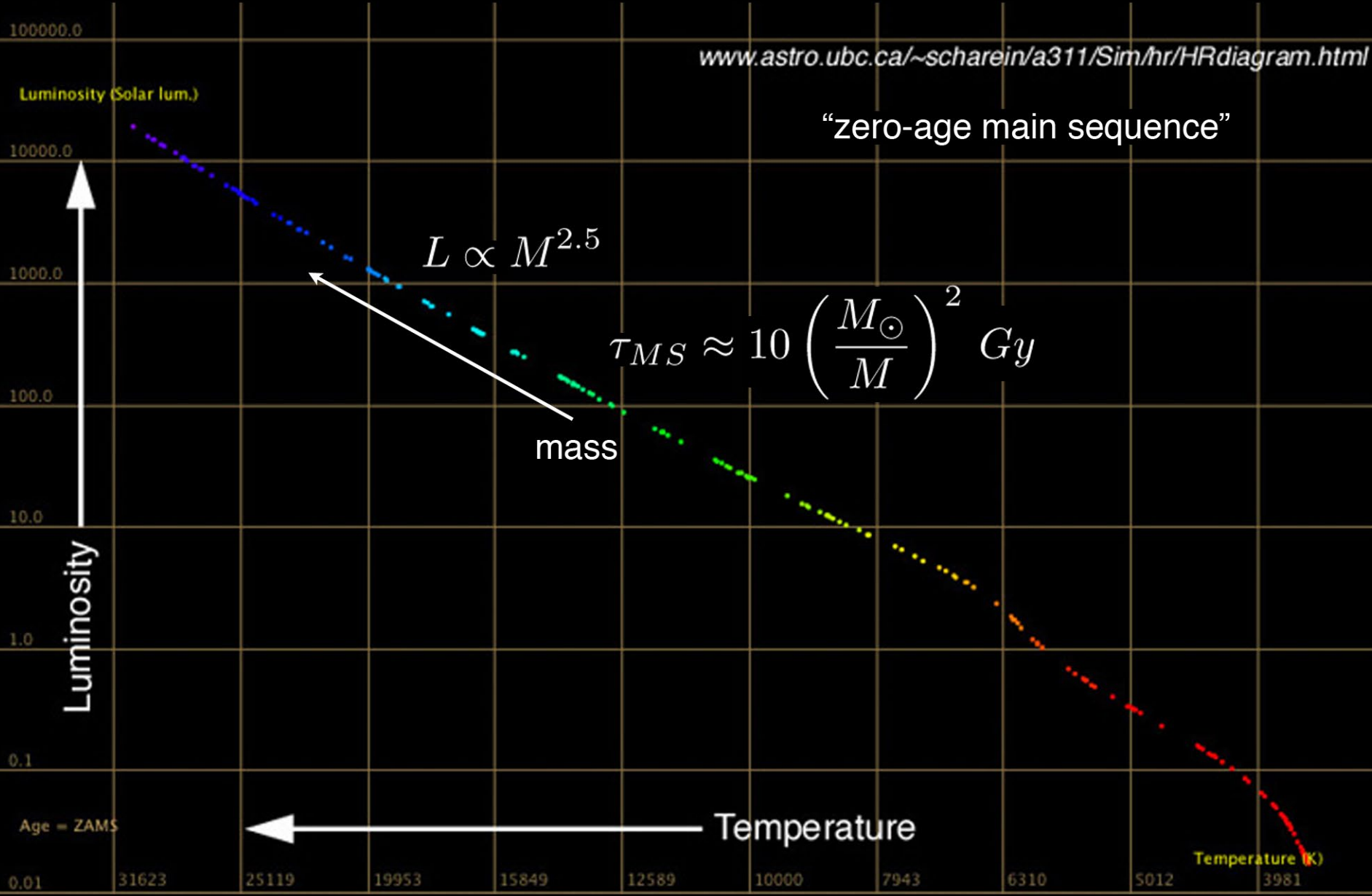
Planetary nebula: The dying star expels its outer layers in a planetary nebula, leaving behind the exposed inert core.

Figure 17.20 Summary of stellar lives. The life stages of a high-mass star (on the left) and a low-mass star (on the right) are depicted in clockwise sequences beginning with the protostellar stage in the upper left corner. (Stars not drawn to scale.)

visualizing stellar evolution

www.astro.ubc.ca/~scharein/a311/Sim/hr/HRdiagram.html

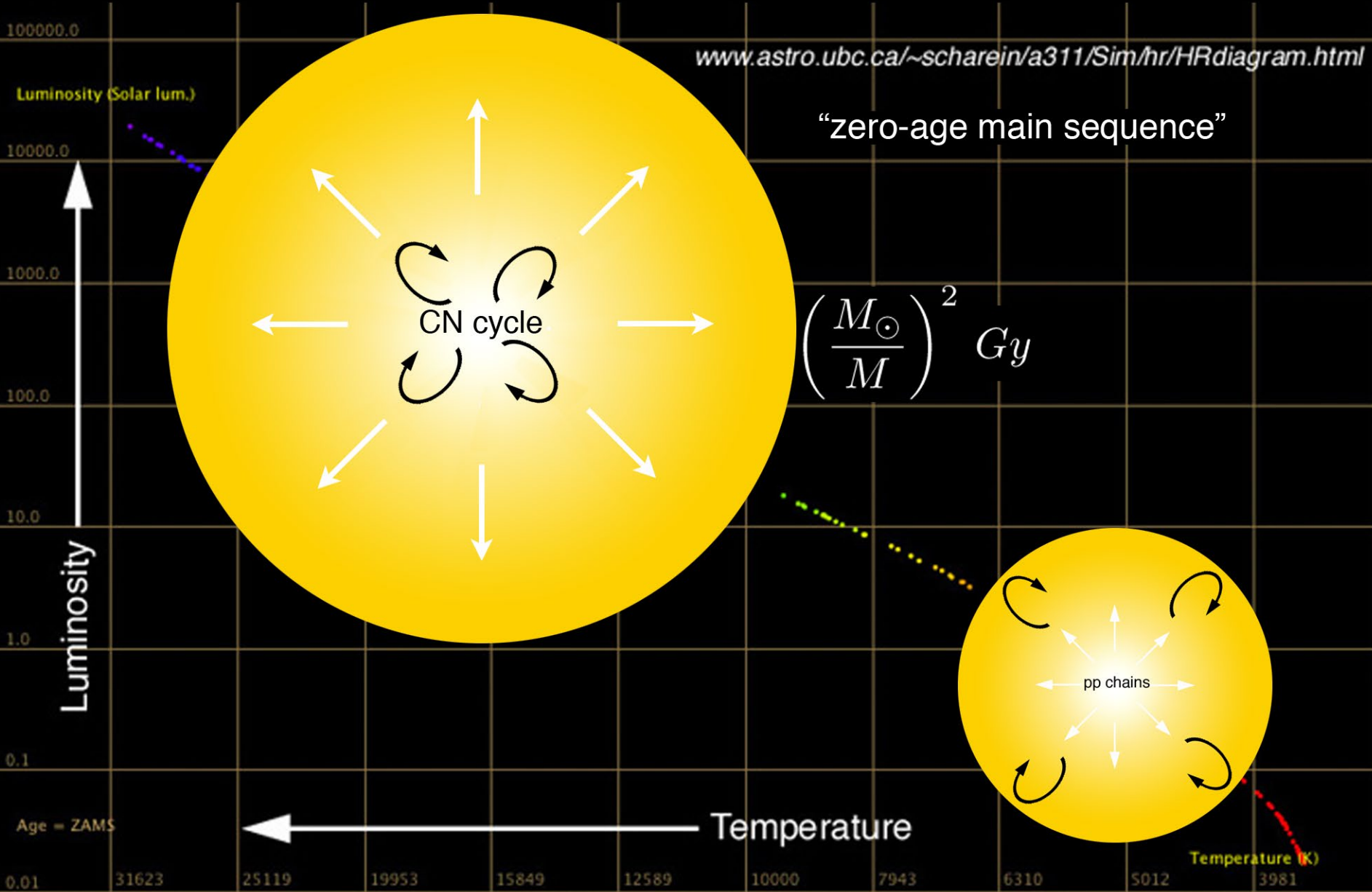
“zero-age main sequence”



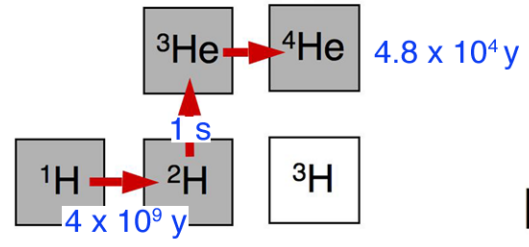
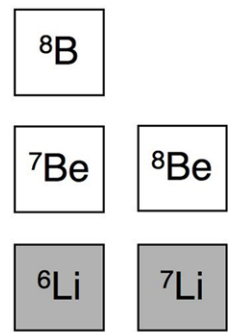
Temperature (K)

visualizing stellar evolution

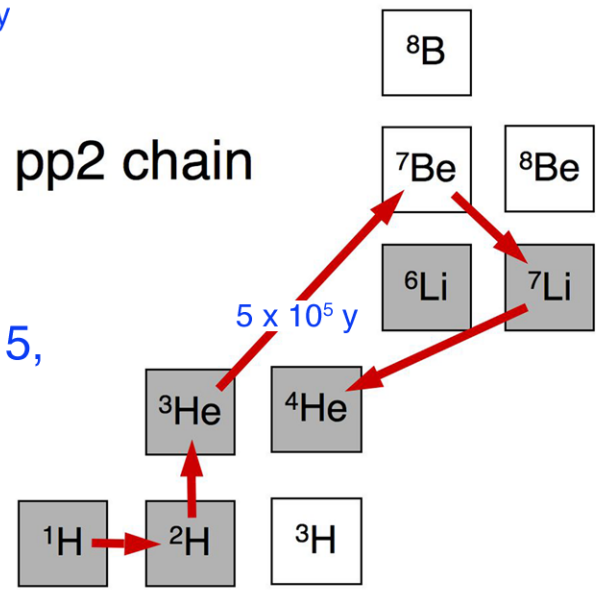
www.astro.ubc.ca/~scharein/a311/Sim/hr/HRdiagram.html



pp1 chain

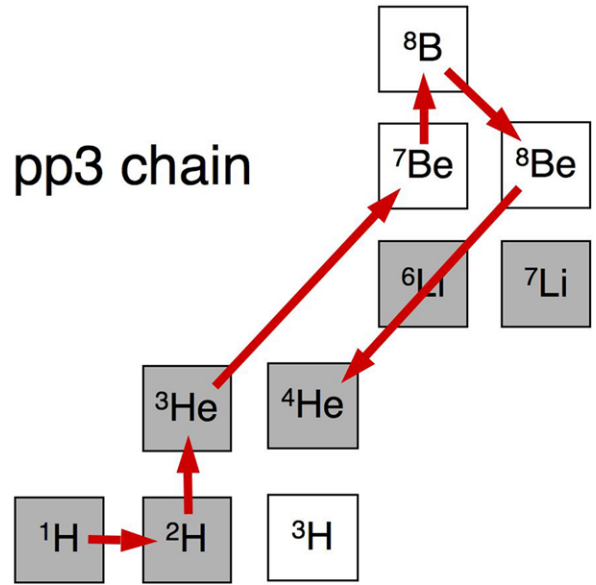


pp2 chain



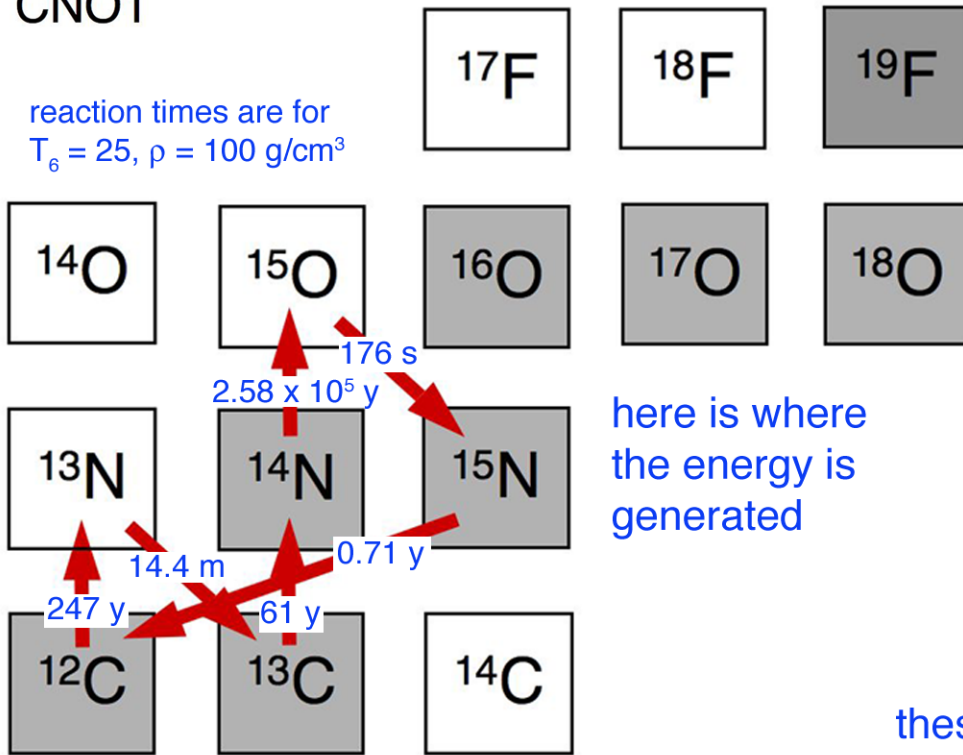
(reaction times are for $T_6 = 15$, $\rho X_H = 100 \text{ g/cm}^3$)

pp3 chain

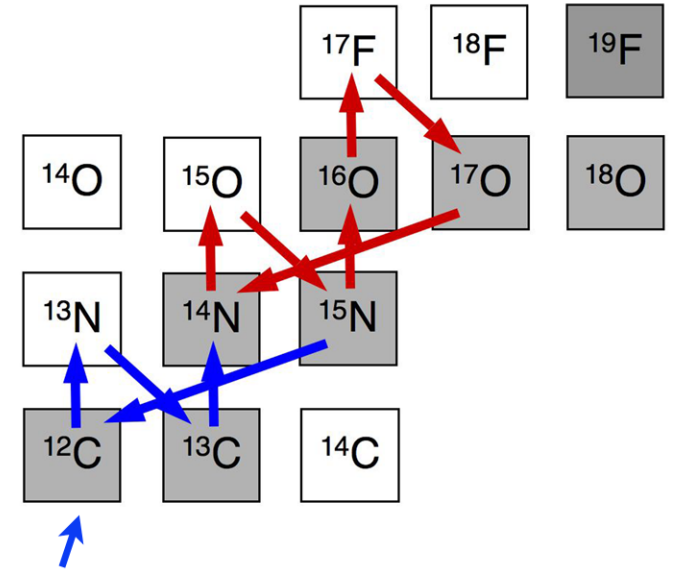


CNO1

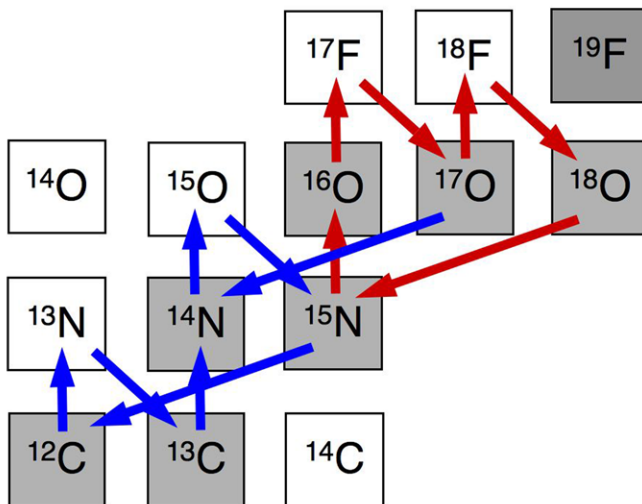
reaction times are for
 $T_6 = 25, \rho = 100 \text{ g/cm}^3$



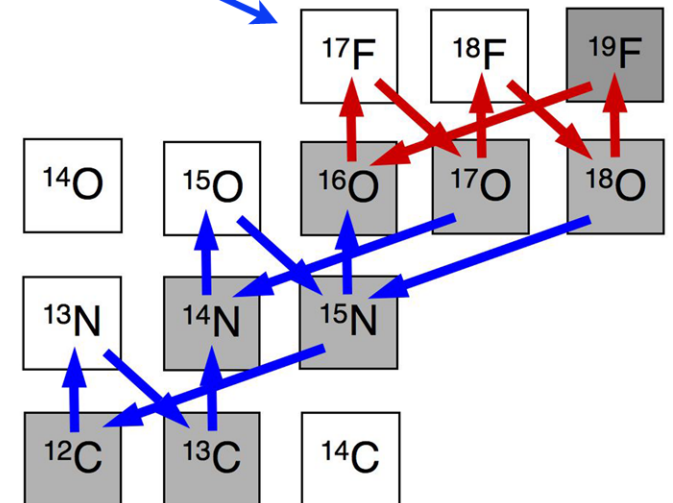
CNO2

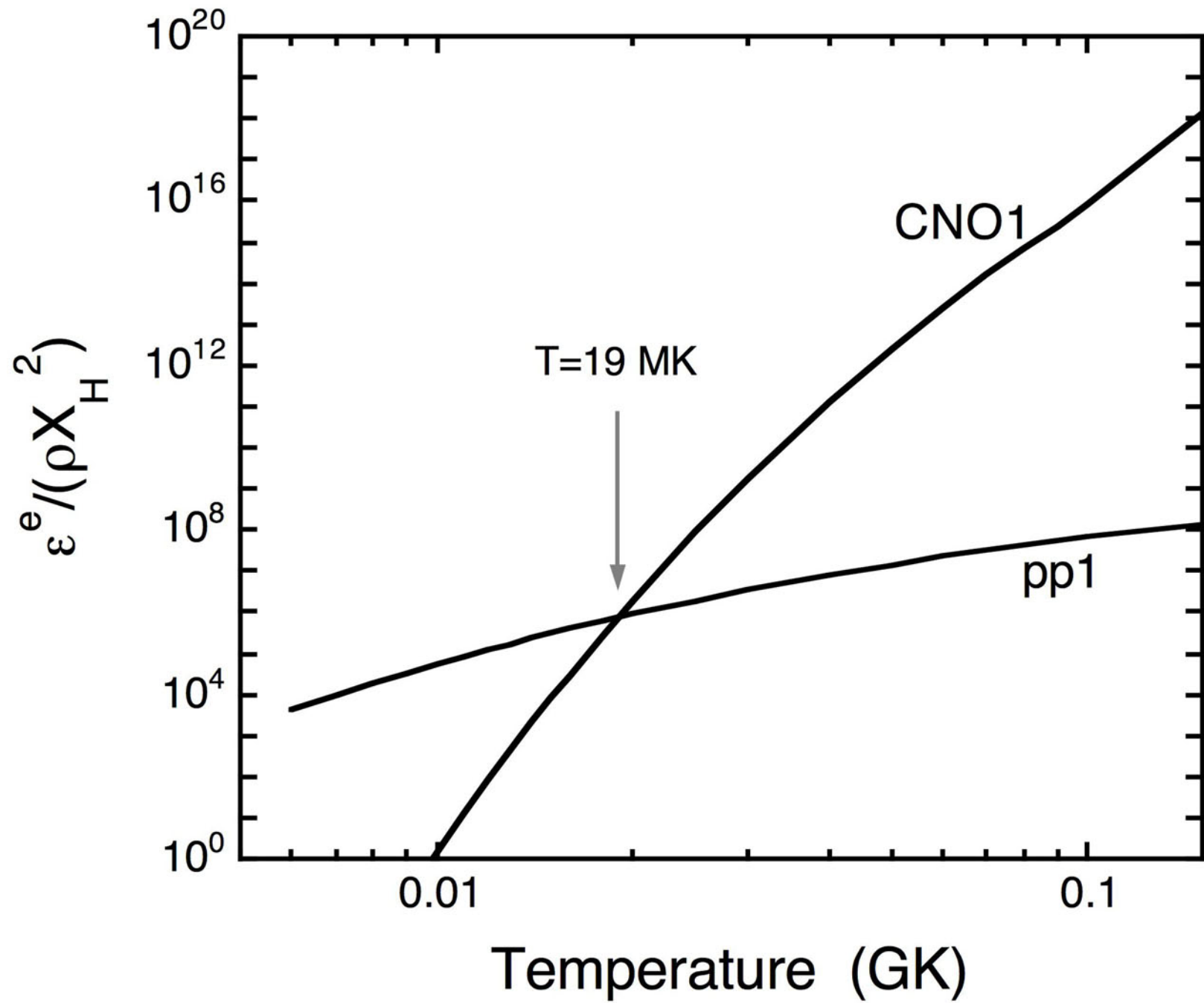


CNO3

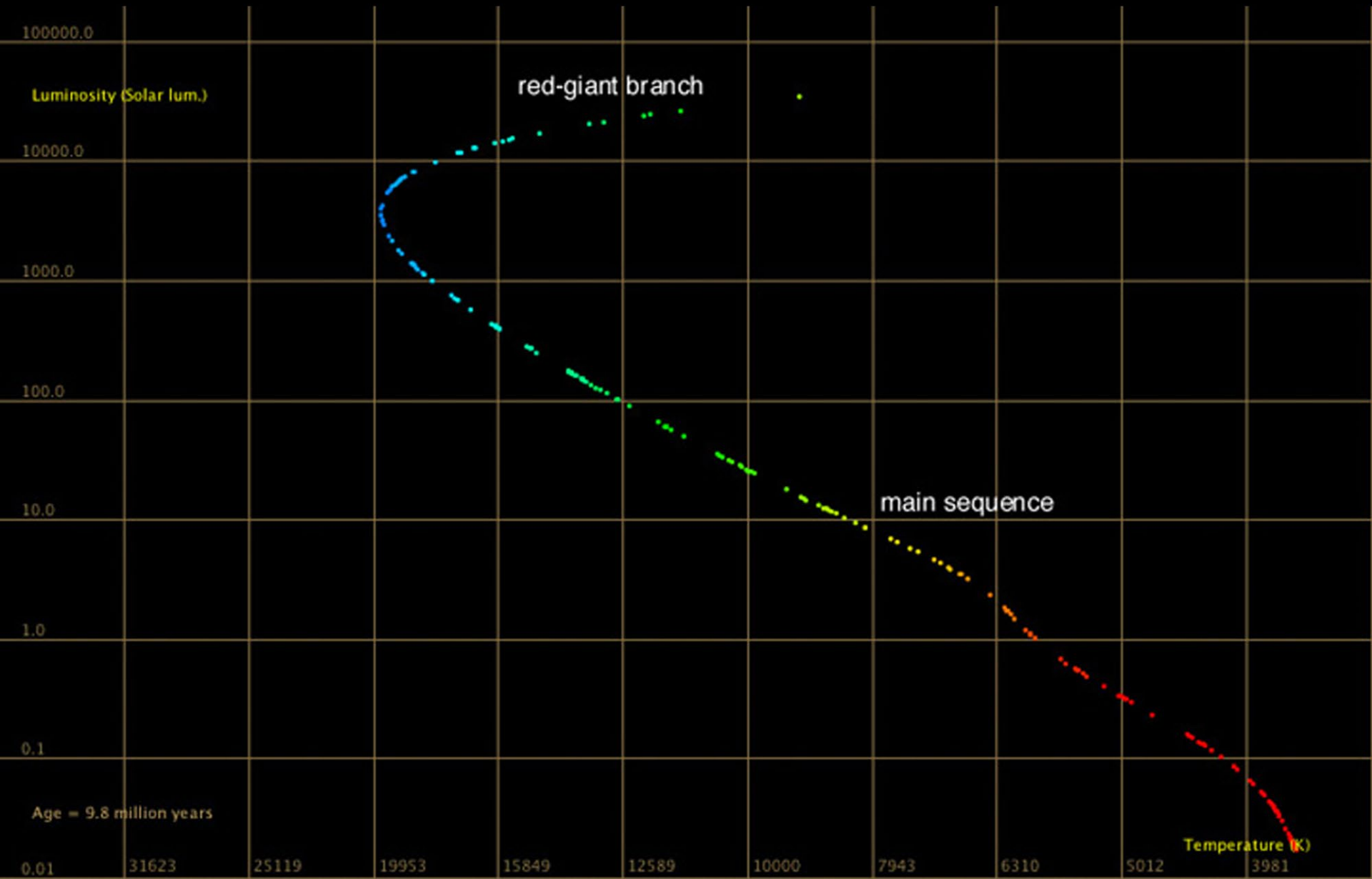


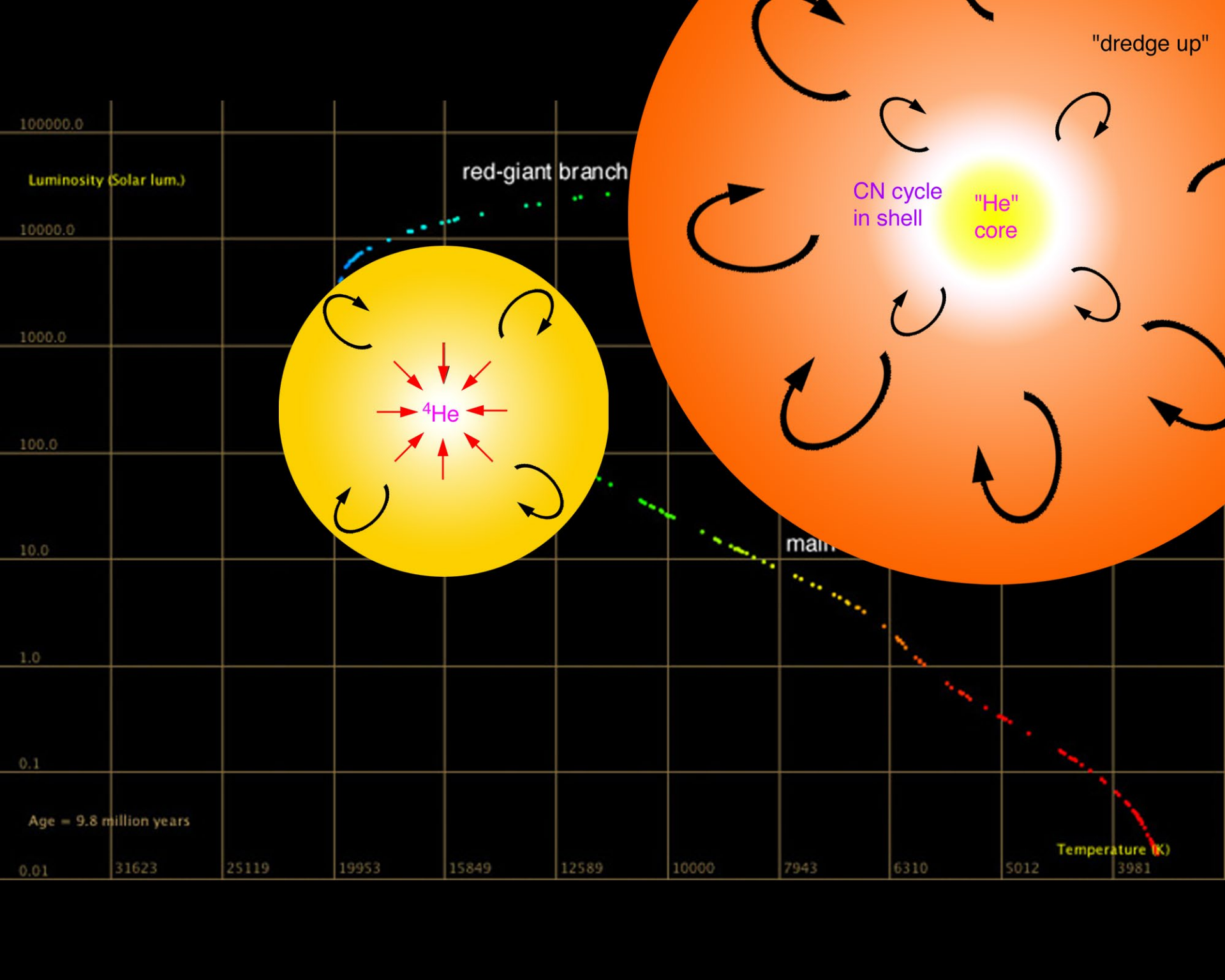
CNO4

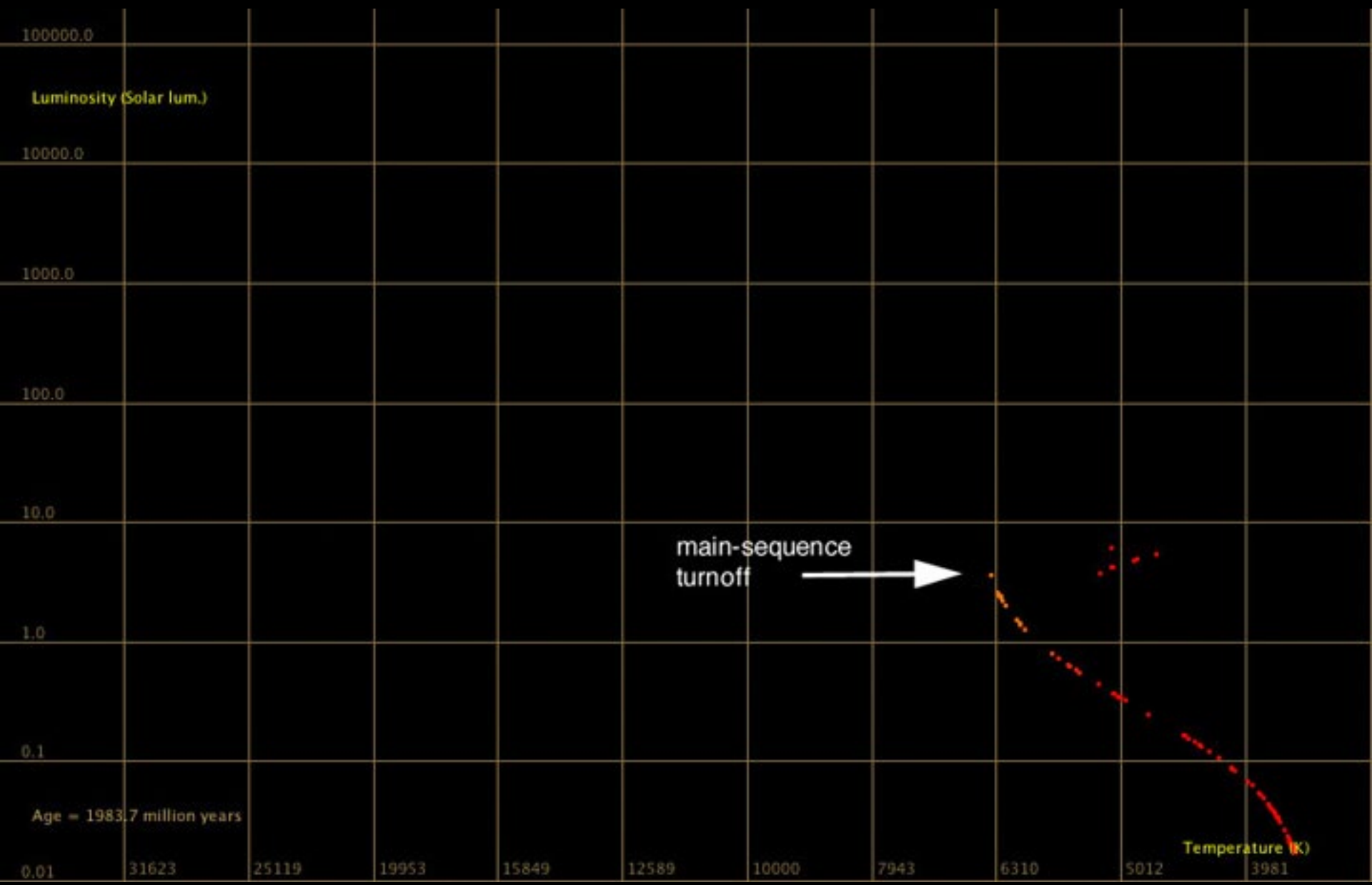


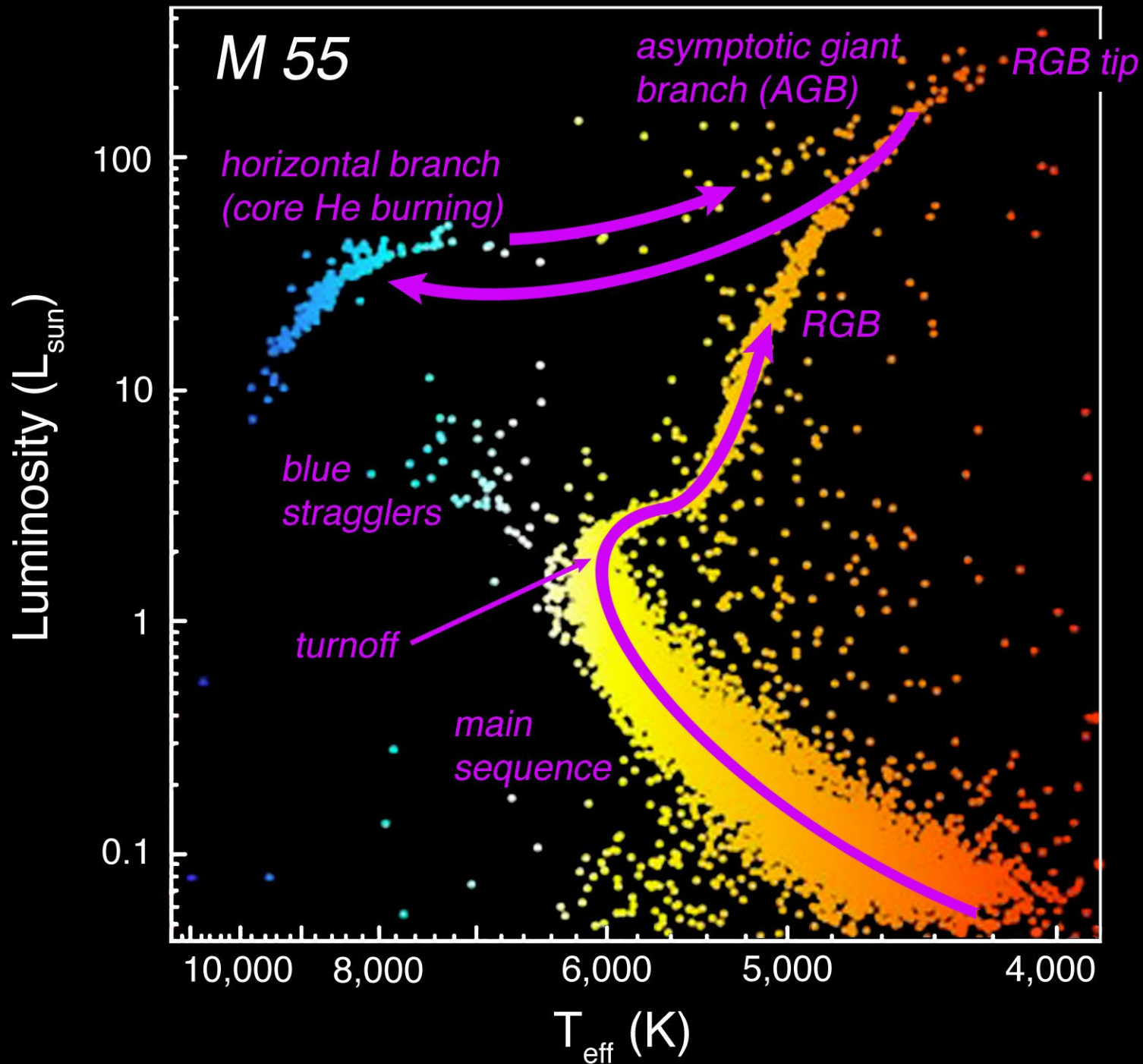


later:







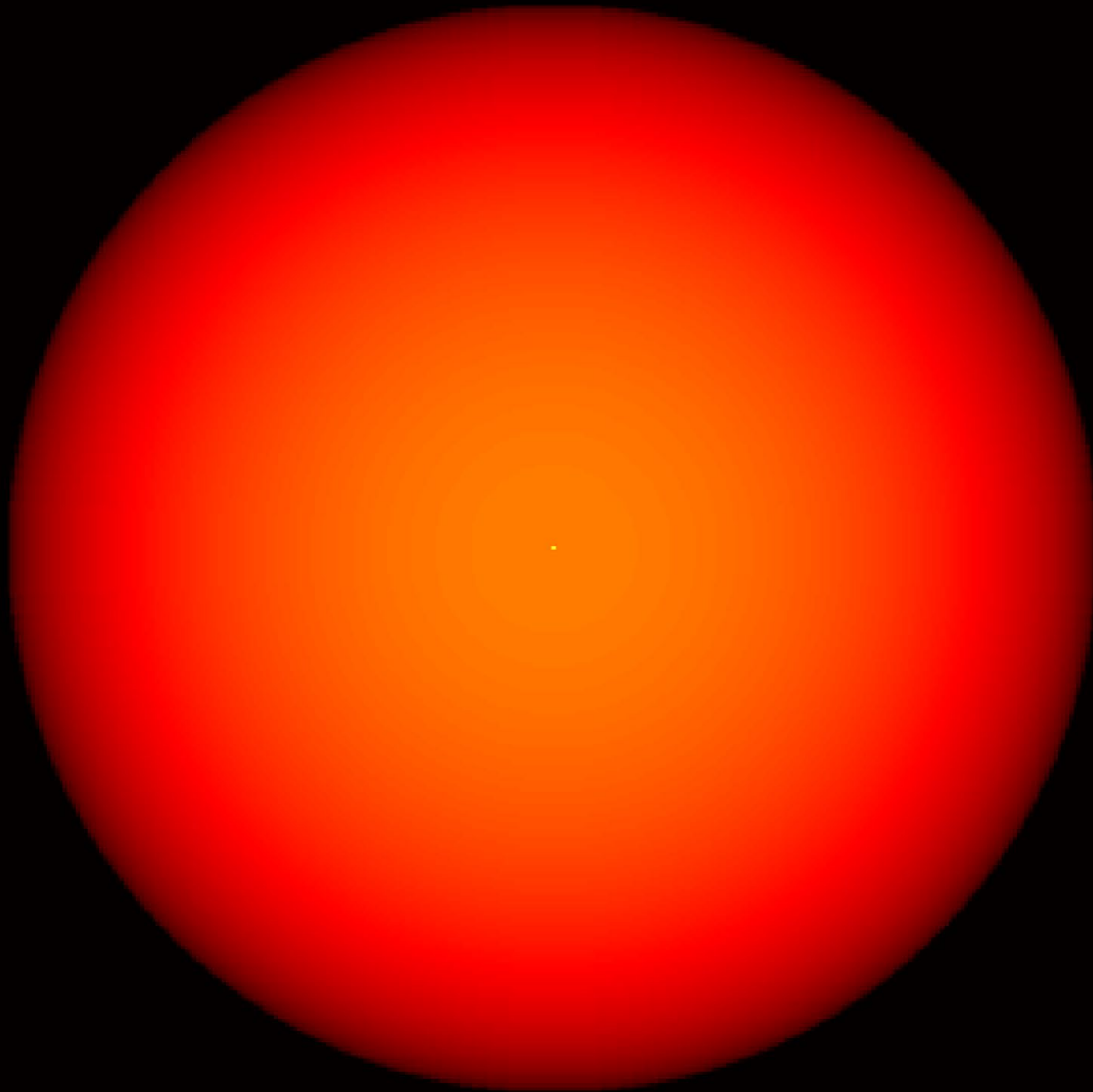


. the sun

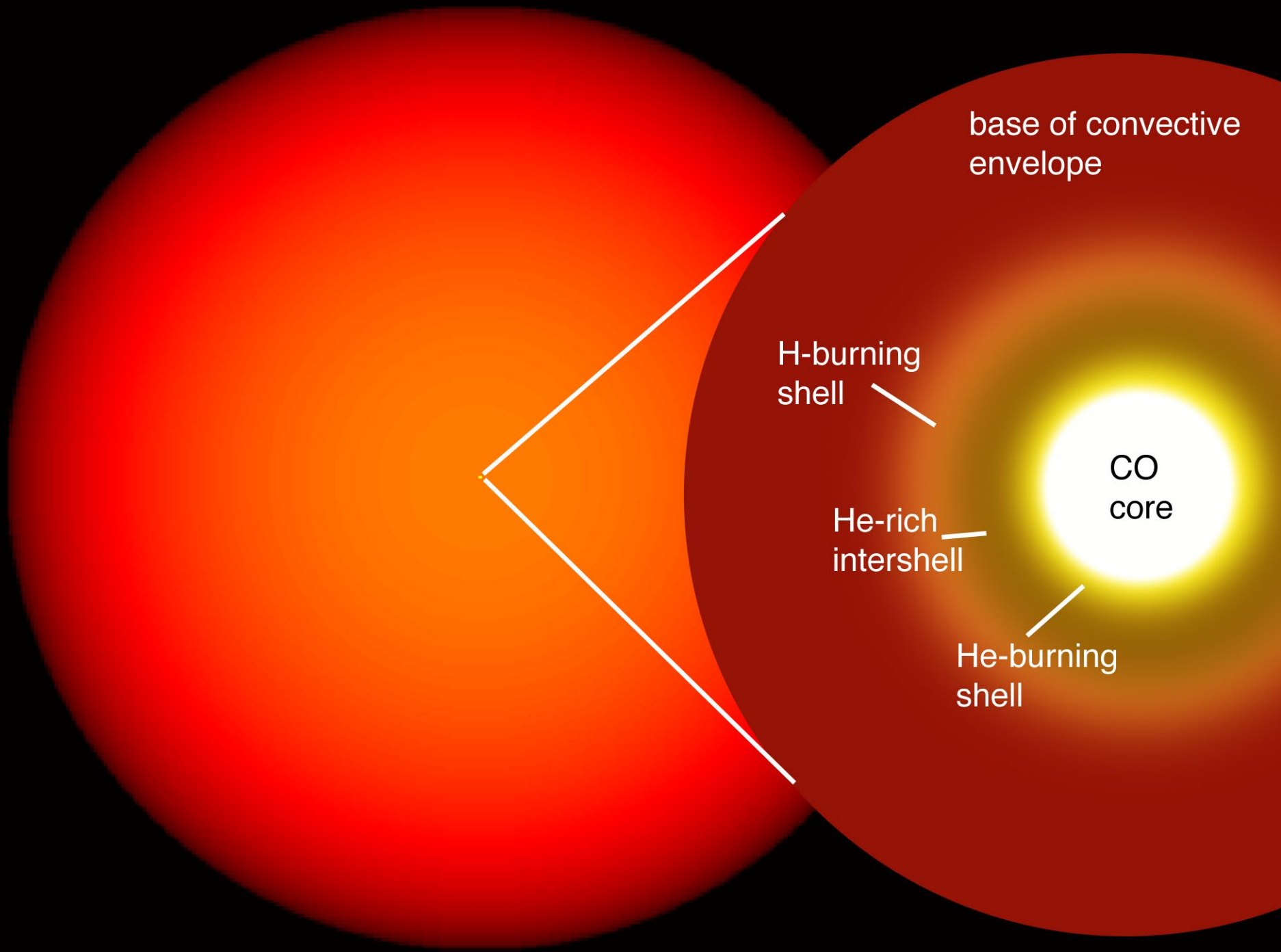


red-giant
phase

 horizontal branch



AGB



base of convective envelope

H-burning shell

He-rich intershell

He-burning shell

CO core

Planetary Nebula Mz 3



Hubble
Heritage

ages of globular clusters



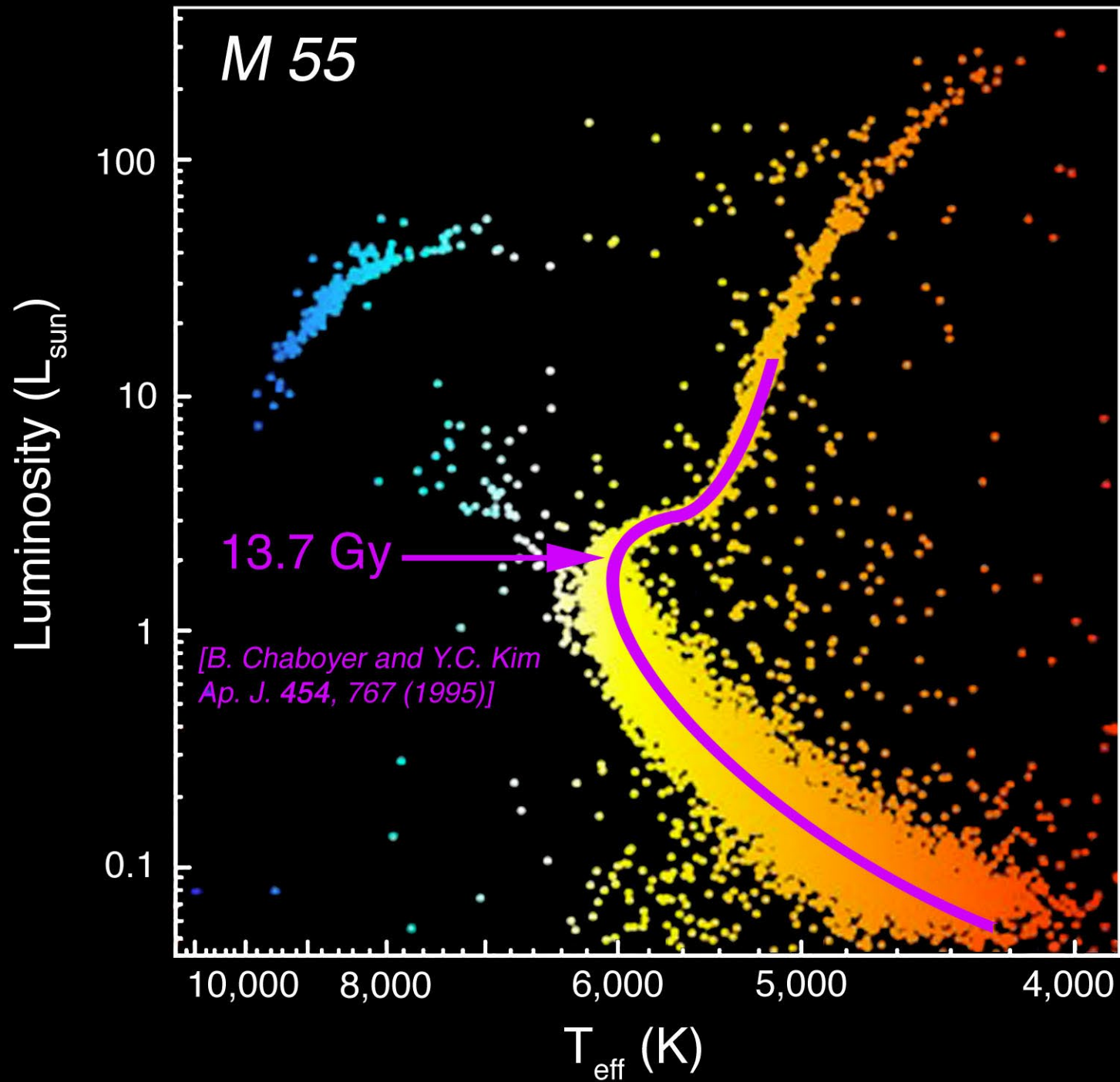
(this is M53)



Globular clusters are coeval, chemically homogeneous groups of 10^3 - 10^6 stars

They provide an integrated sequence of stellar evolution

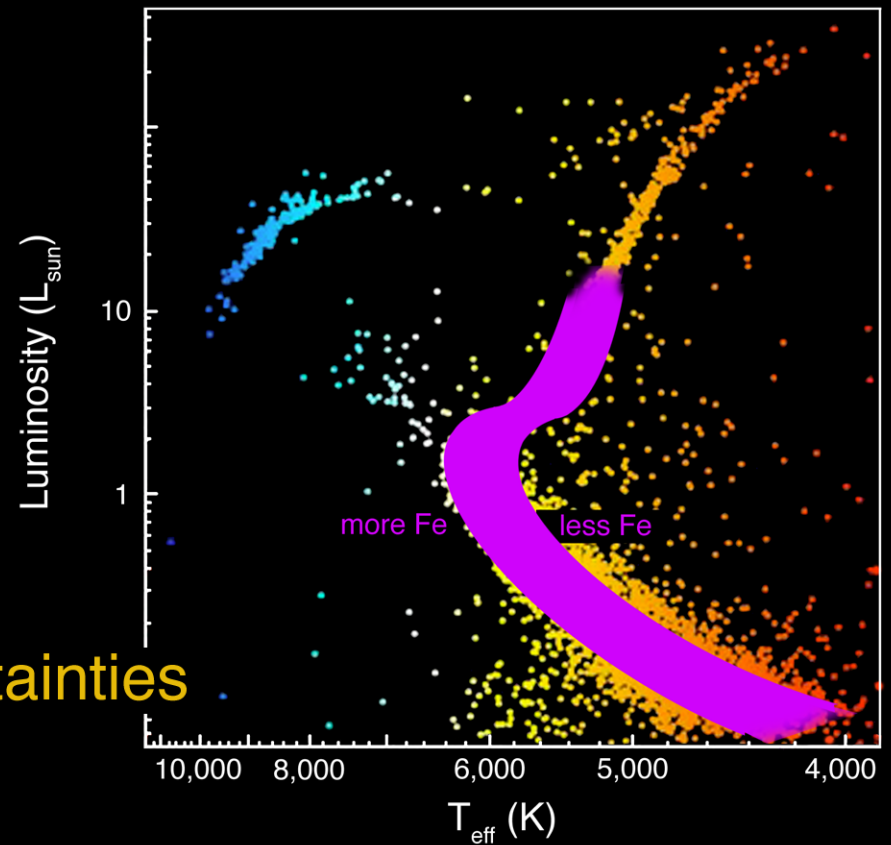
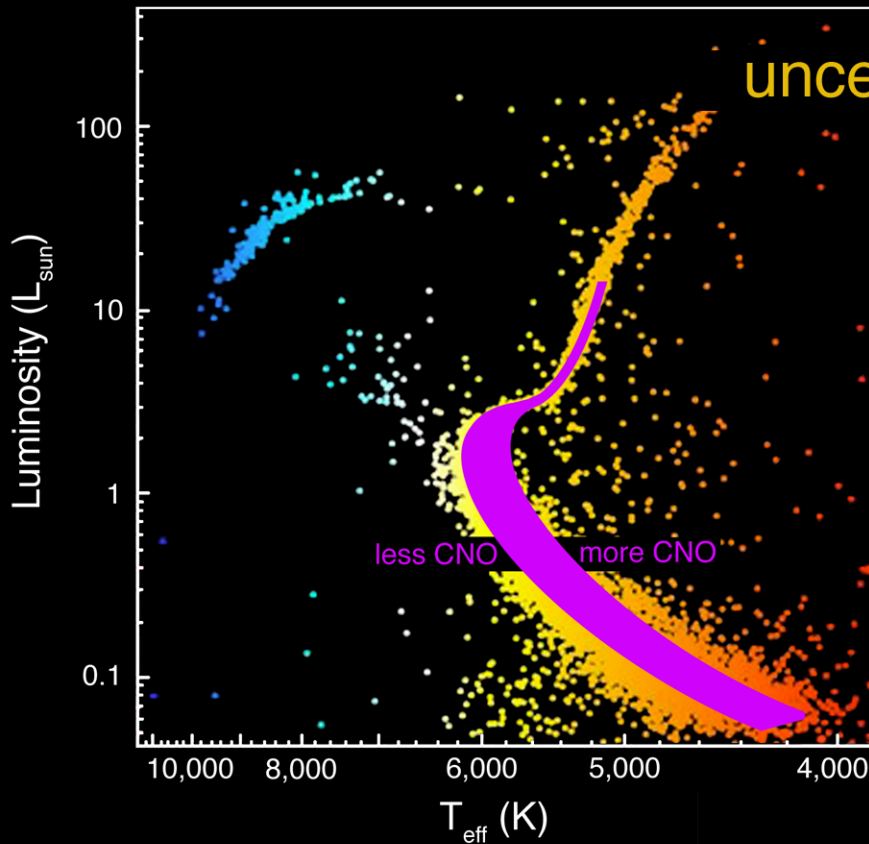
Their kinematics and ages trace out the evolution of structure in the galaxy



distance scale: affects absolute luminosity - only a few parallax measurements, t/L relationship for RR-Lyraes...

He abundance: more He, less H;
when does CN cycle take over?

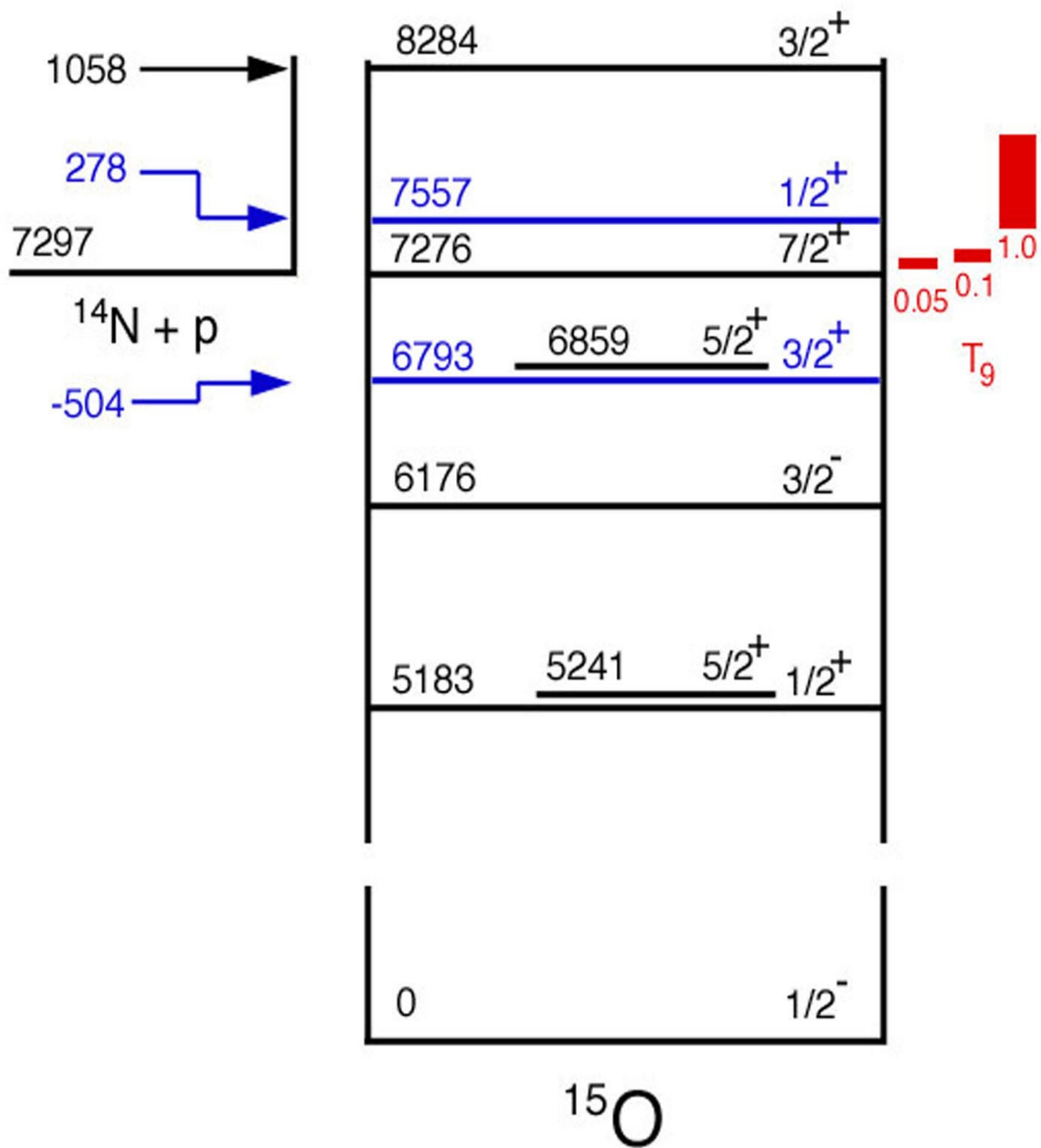
convection: use mixing-length theory;
if dT/dr increases, then radius decreases and T_{eff} goes up

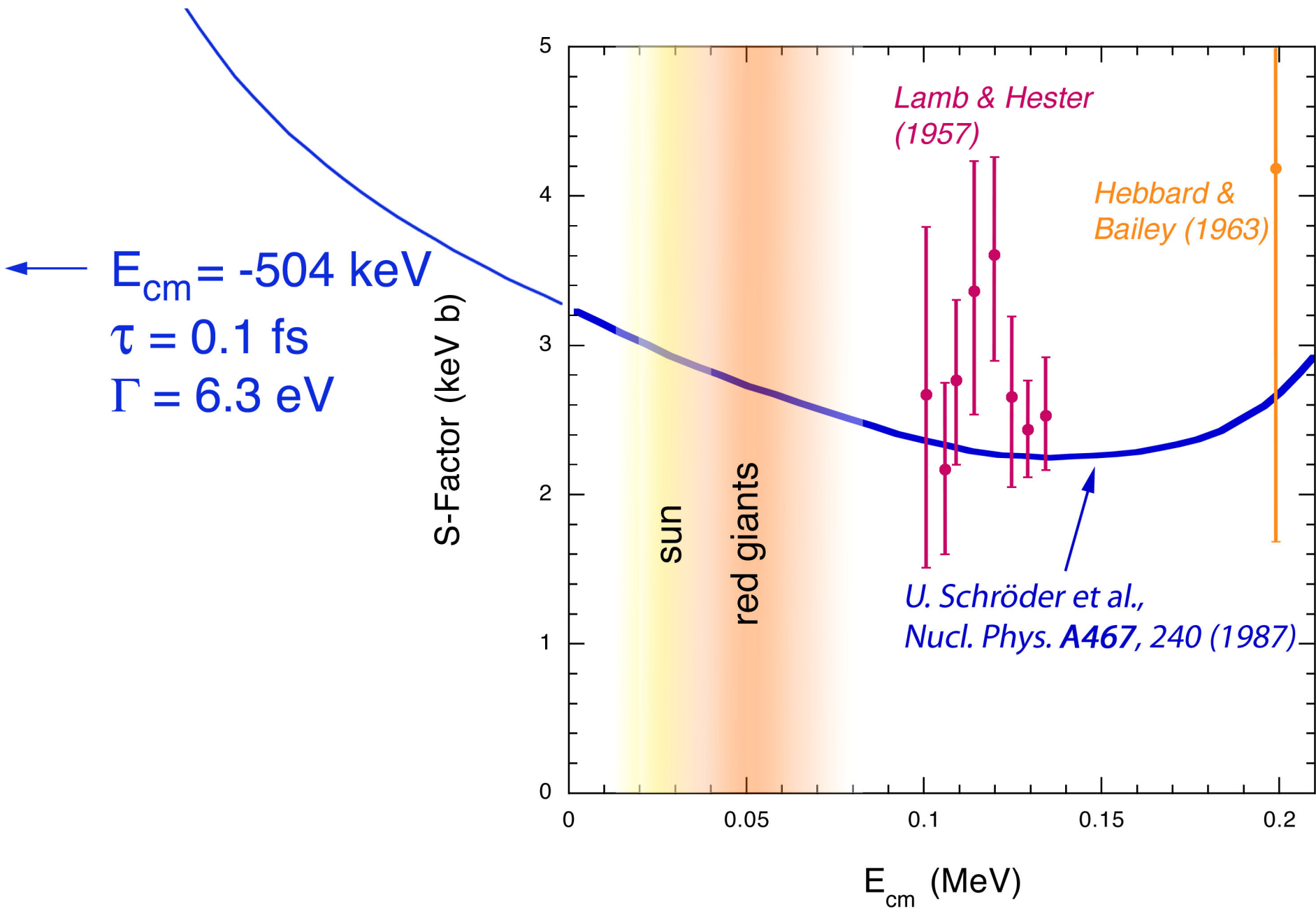


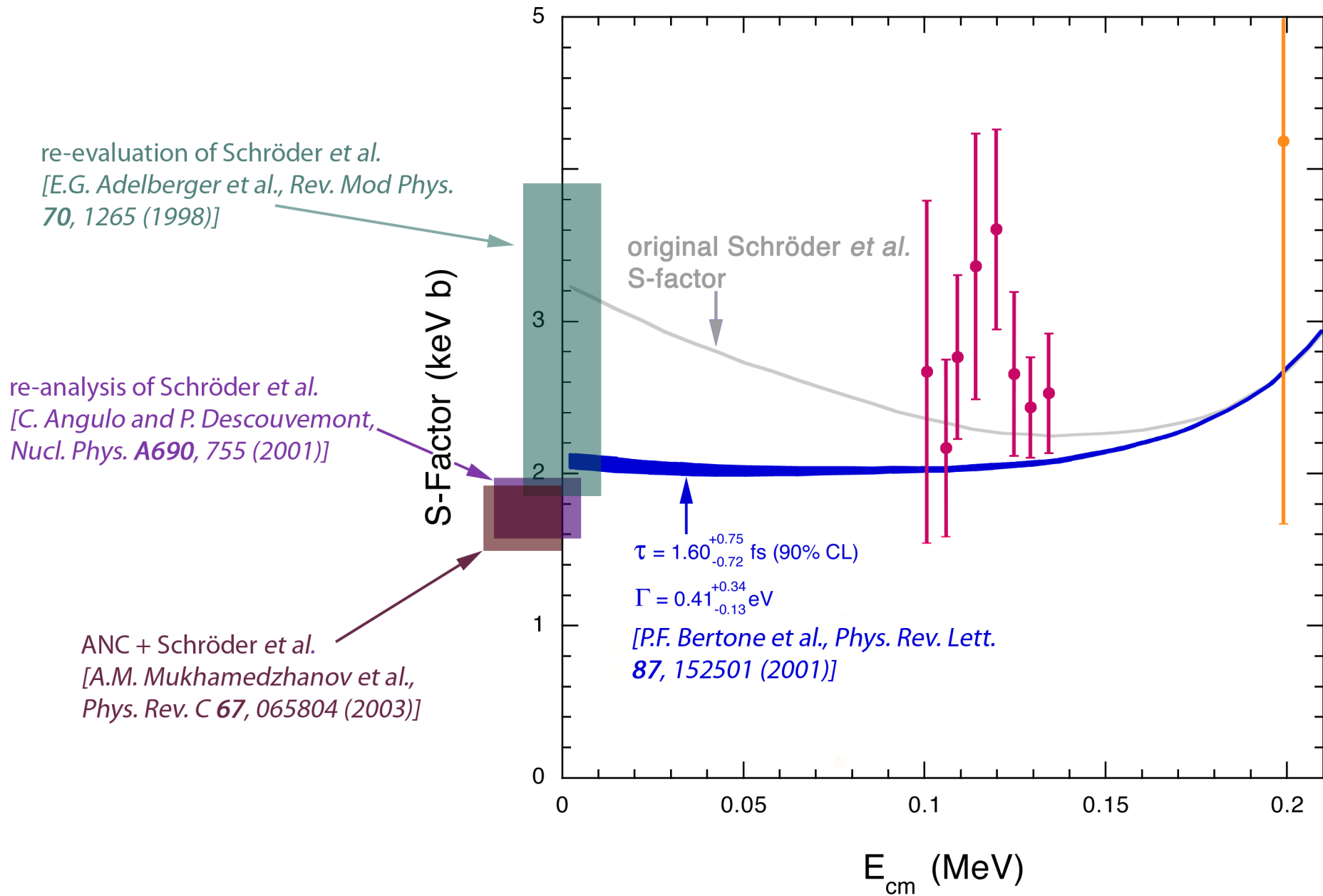
opacity: affects size of envelope, T_{eff}

diffusion: decreases H abundance,
reduces τ_{ms}

$^{14}\text{N}(p,\gamma)^{15}\text{O}$: regulates power in CN
cycle, affects L_{TO}







LUNA2 (400 kV)

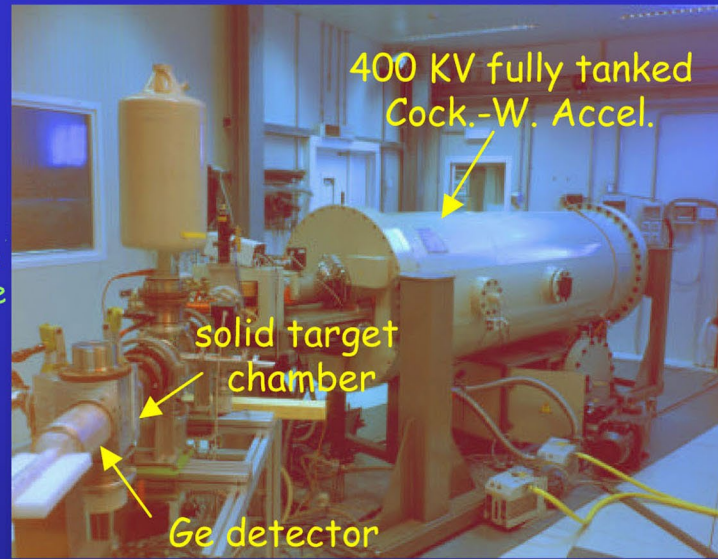
Voltage Range :
50 - 400 kV

Output Current: 1 mA 75% H
(@ 400 kV) 25% H₂
: 500 μA ⁴He

Beam energy spread:
76 eV

Long term stability (1 h) :
10 eV

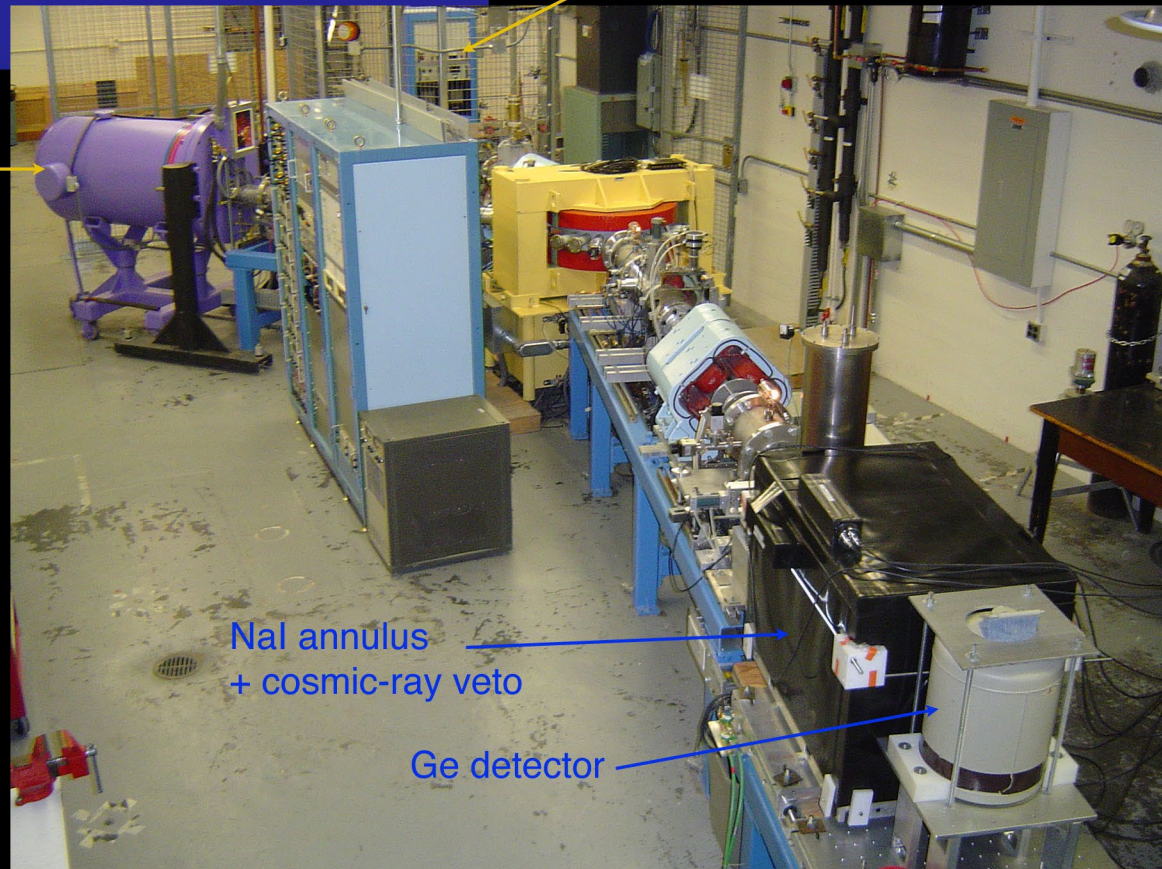
Terminal Voltage ripple:
10 Vpp



200-kV ECR

1-MV van de Graaff

LENA



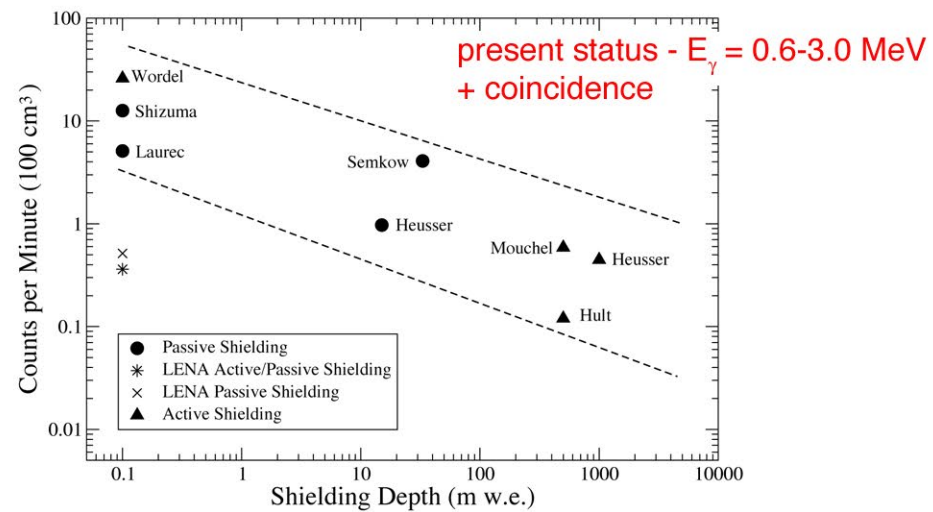
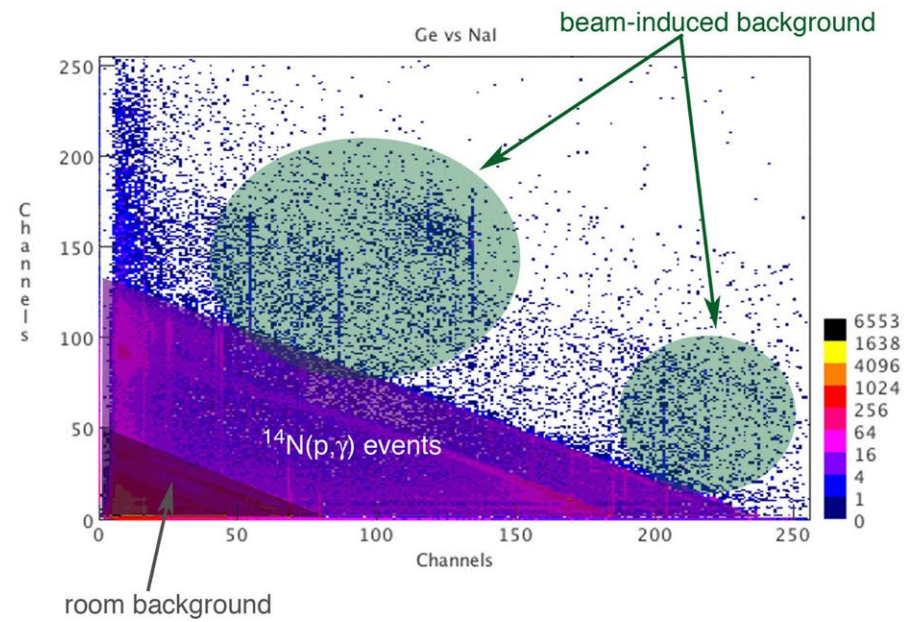
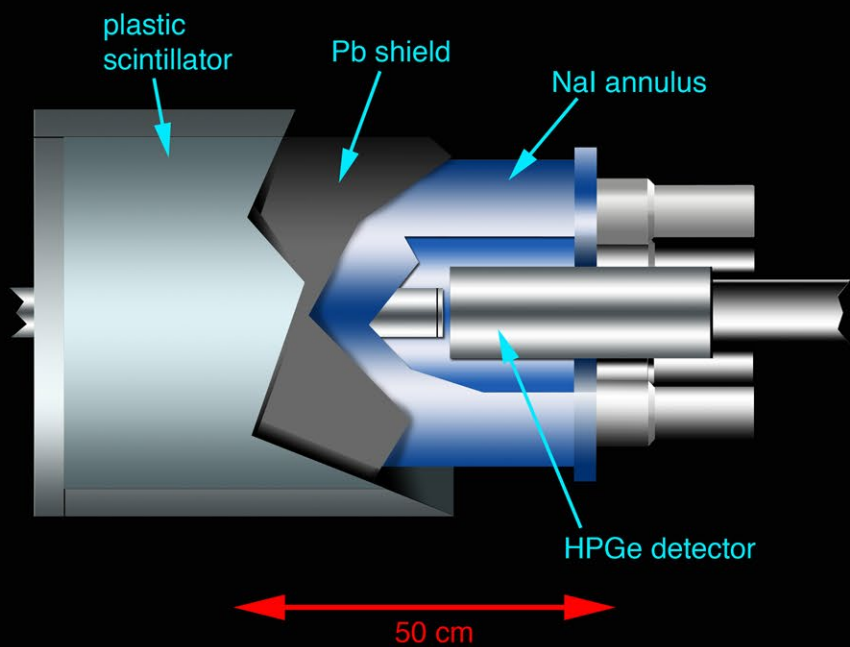
classical approach:



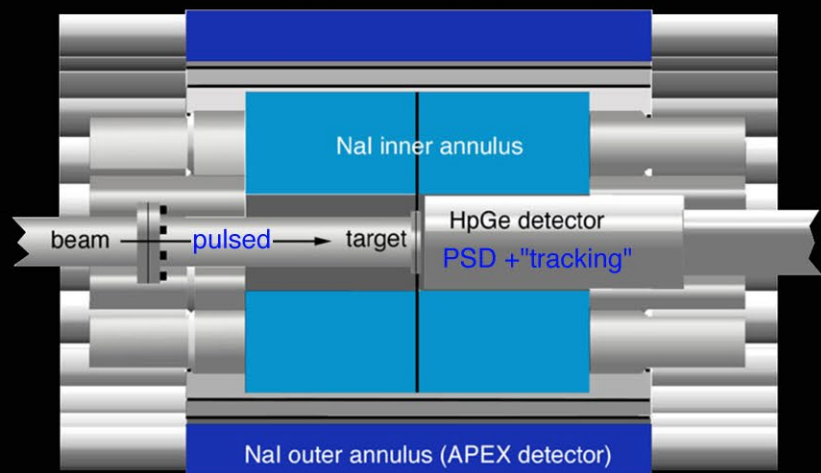
$$\text{figure of merit} = \frac{\text{signal rate}}{\sqrt{\text{background rate}}}$$

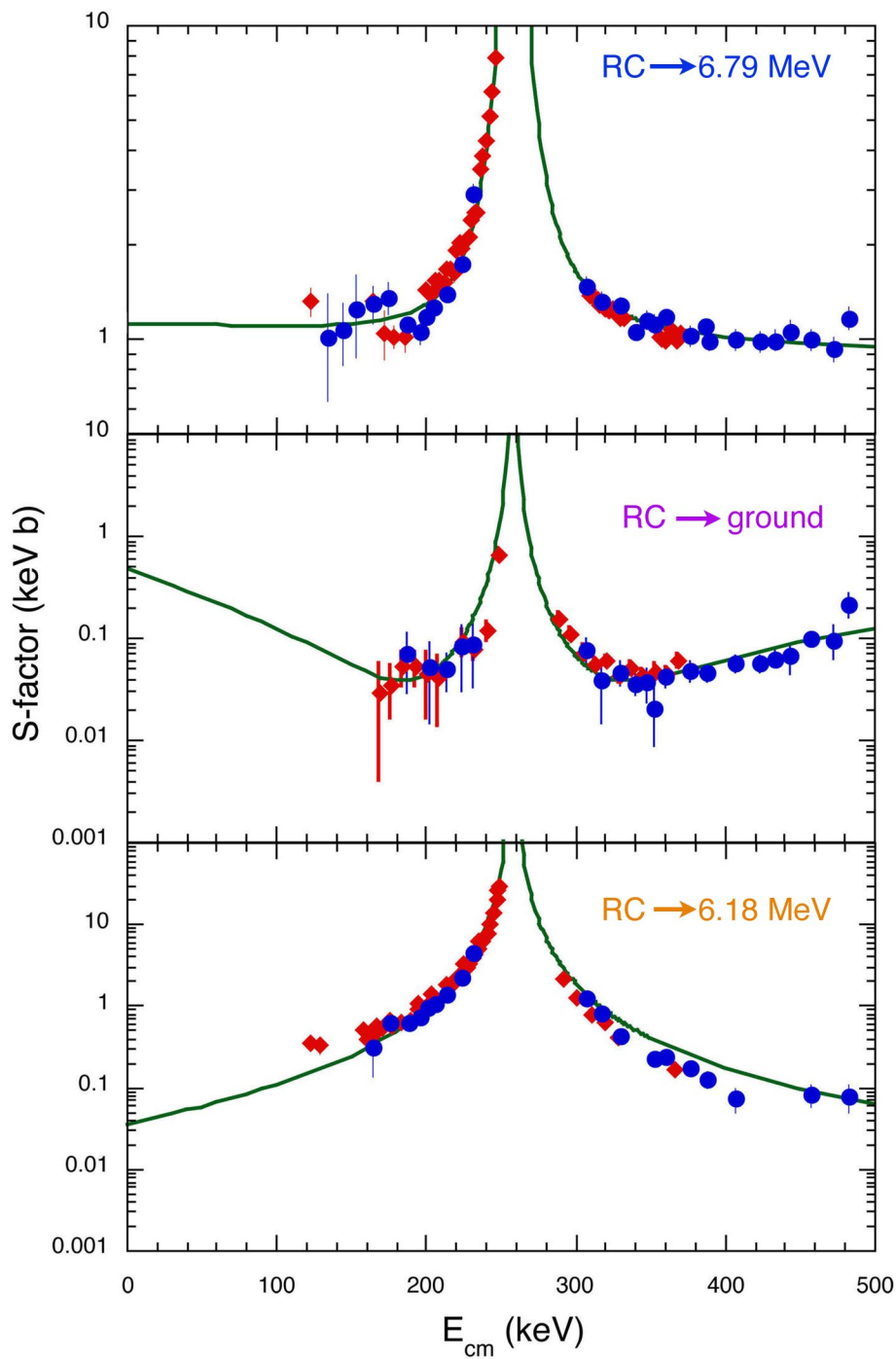
sources of background:

1. beam (always present at some level)
2. natural radioactivity (up to ~ 3 MeV; suppress with passive shielding)
3. cosmic rays (direct interactions of muons, neutrons, muon-induced bremsstrahlung, etc. ; suppress with active shield or move underground)



future improvements:

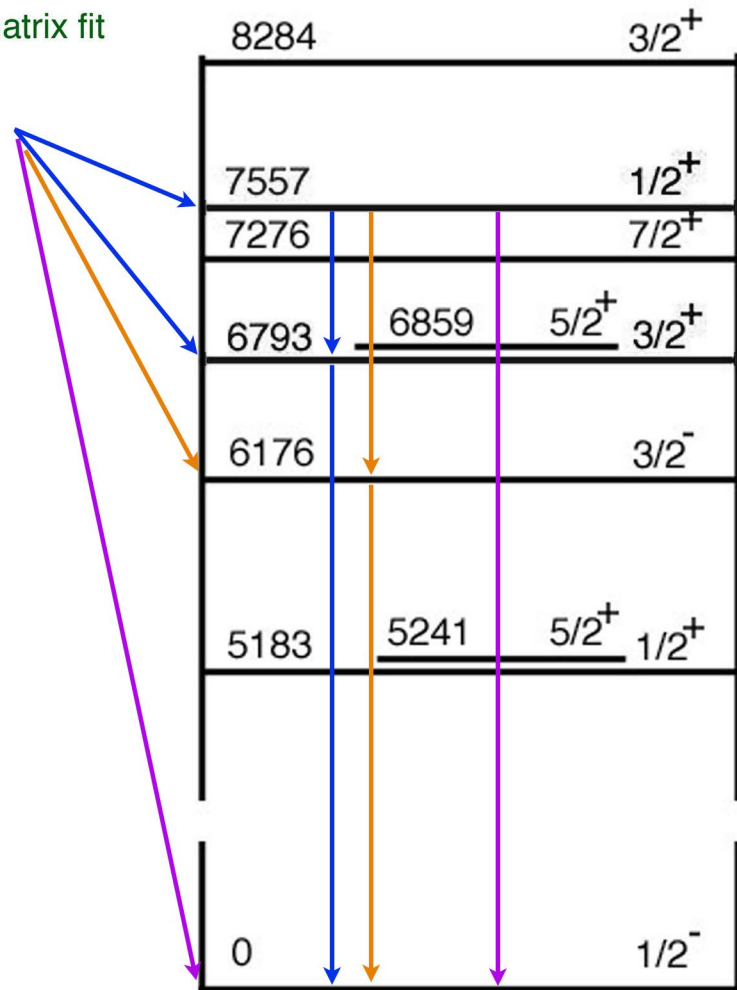




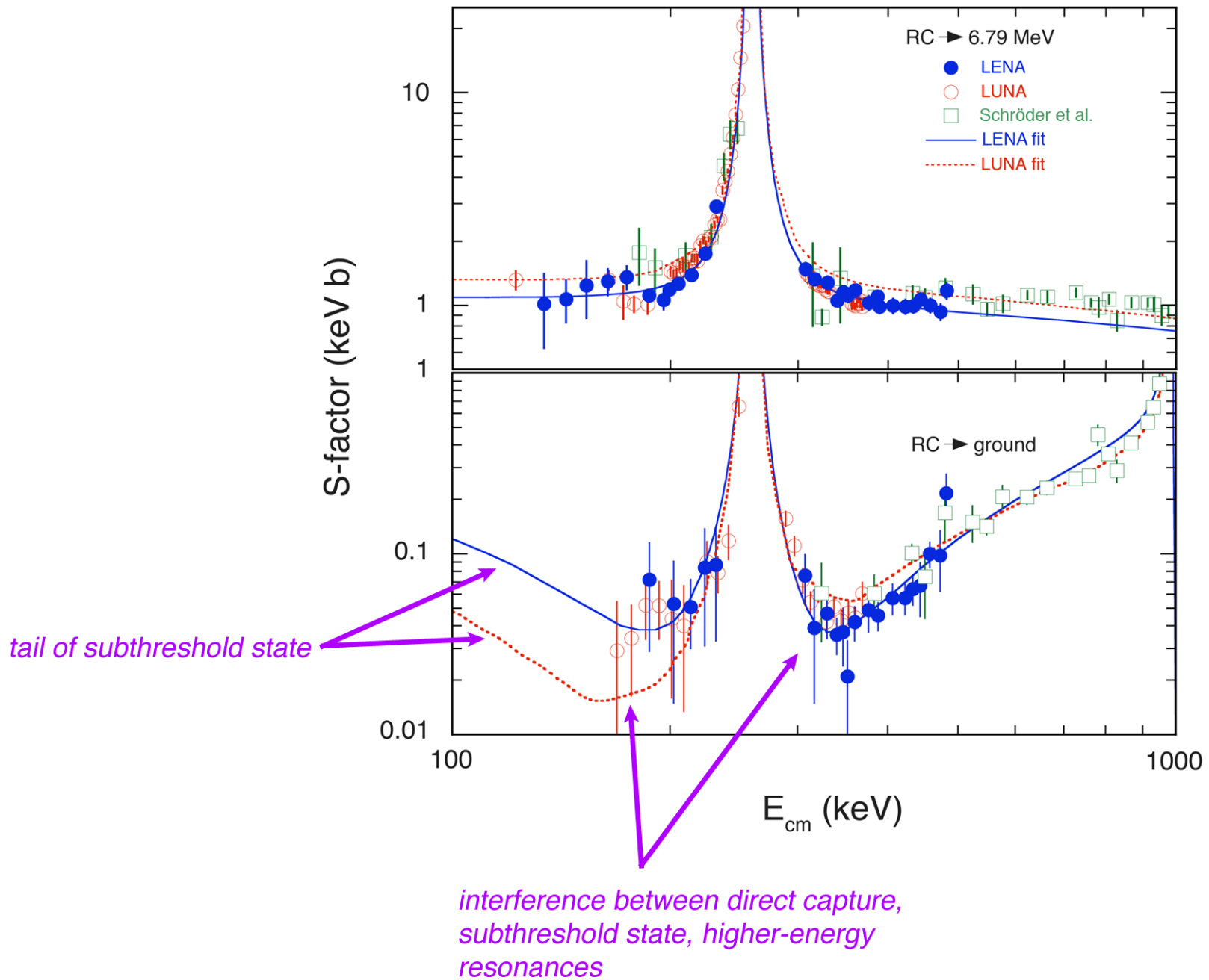
● LENA - R.C. Runkle *et al.*, Phys. Rev. Lett. **94**, 082503 (2005)

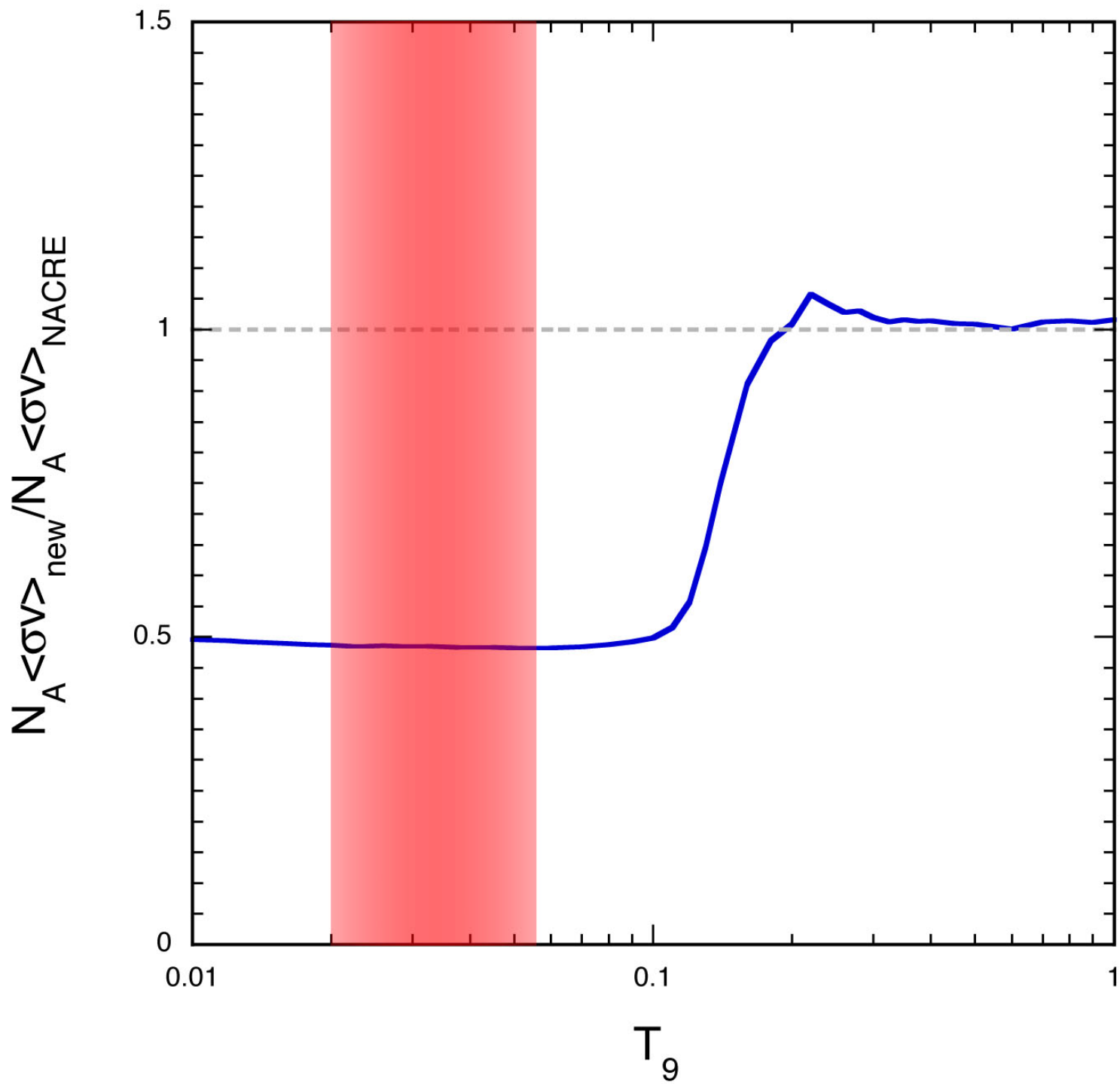
◆ LUNA - A. Formicola *et al.*, Phys. Lett. B **591**, 61 (2004)

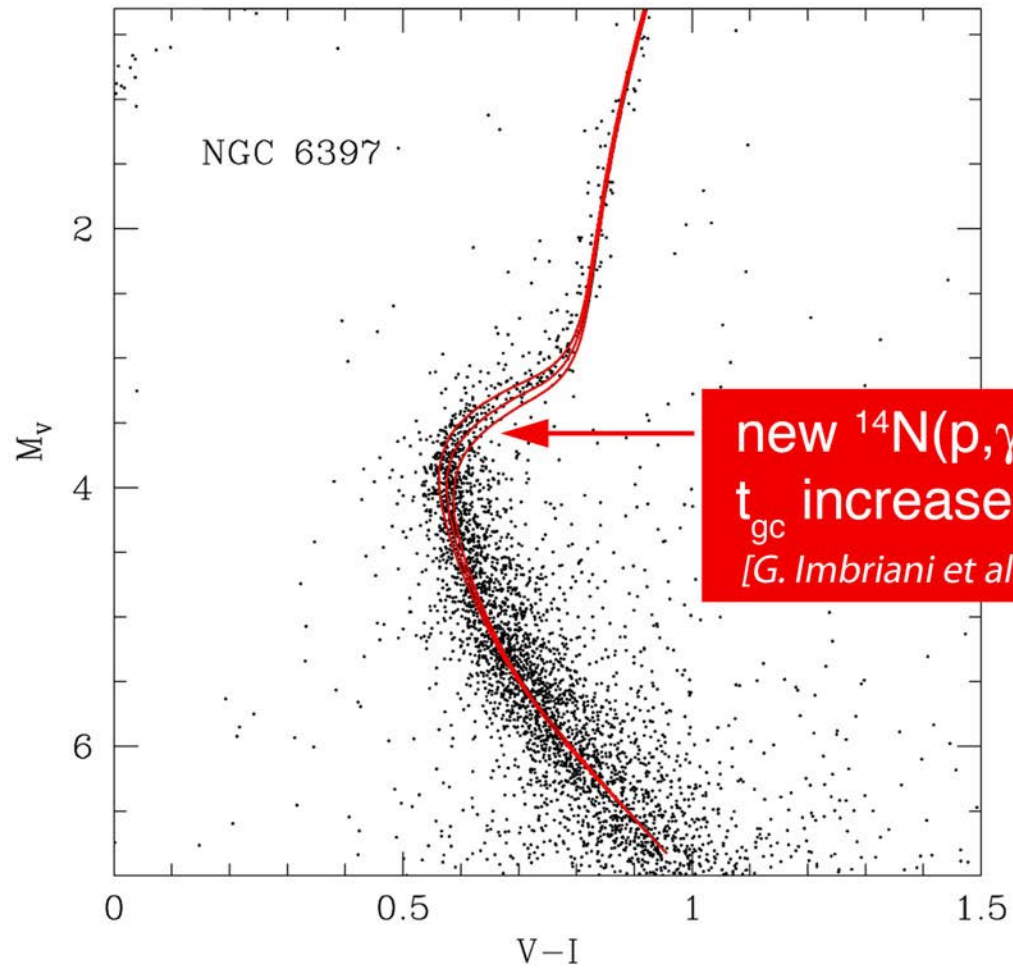
— R-matrix fit



^{15}O

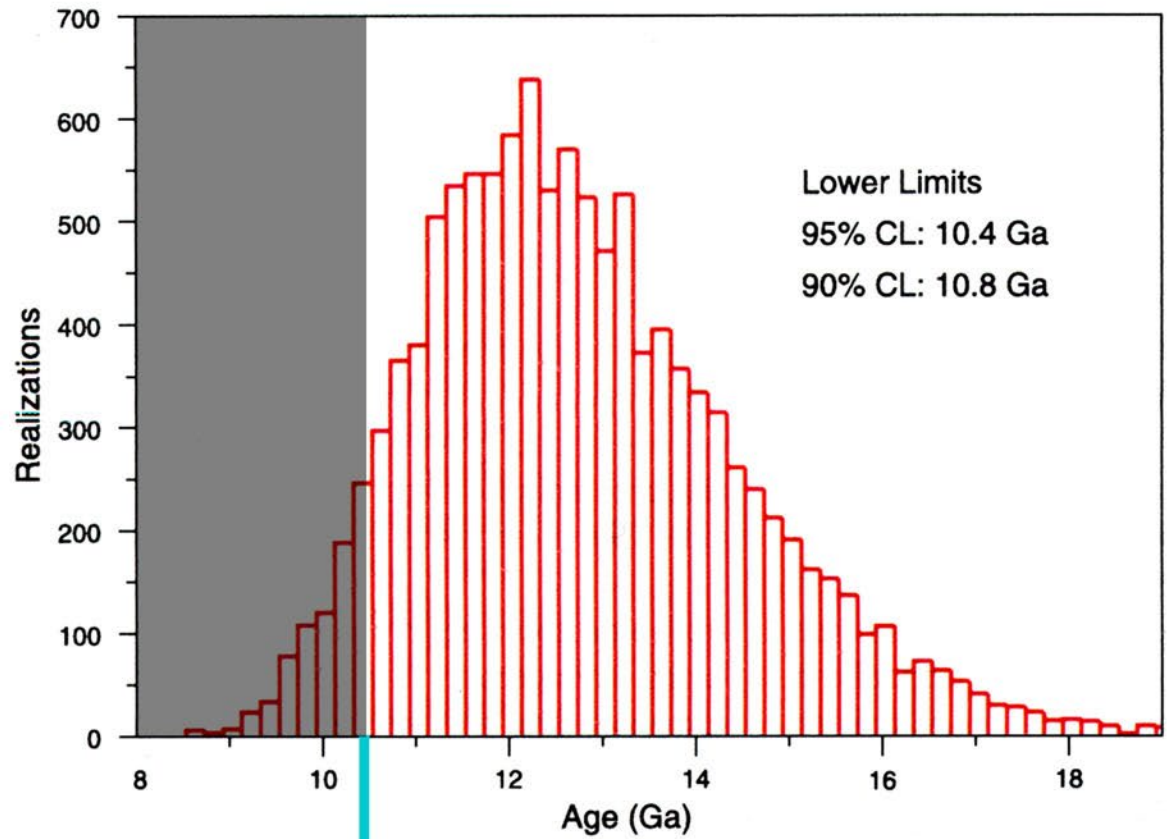






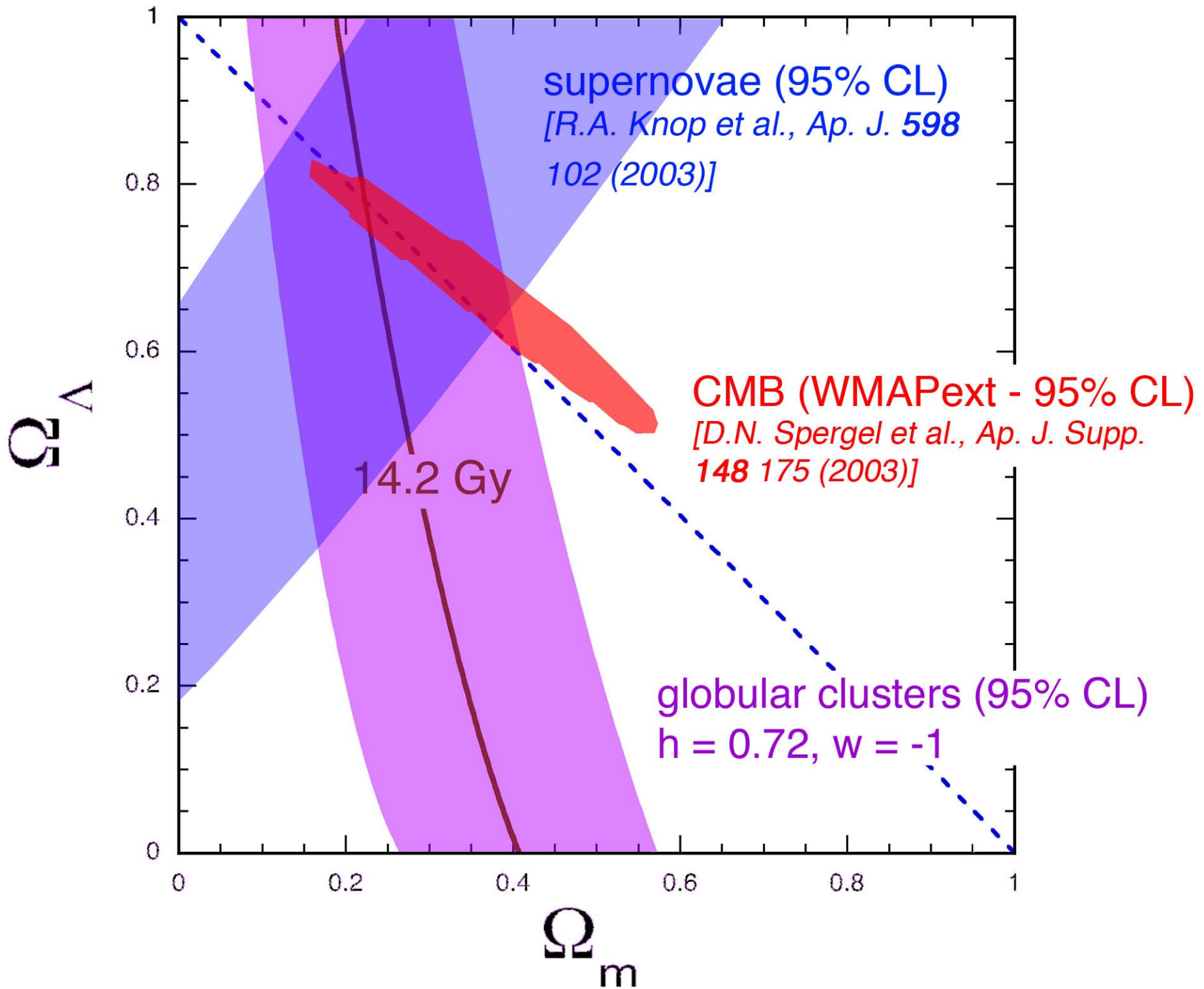
new $^{14}\text{N}(p,\gamma)$ rate:
 t_{gc} increases by 0.7 - 1 Gy
[G. Imbriani et al. A & A 420, 625 (2004)]

L.M. Krauss & B. Chaboyer, *Science* **299**, 65 (2003)



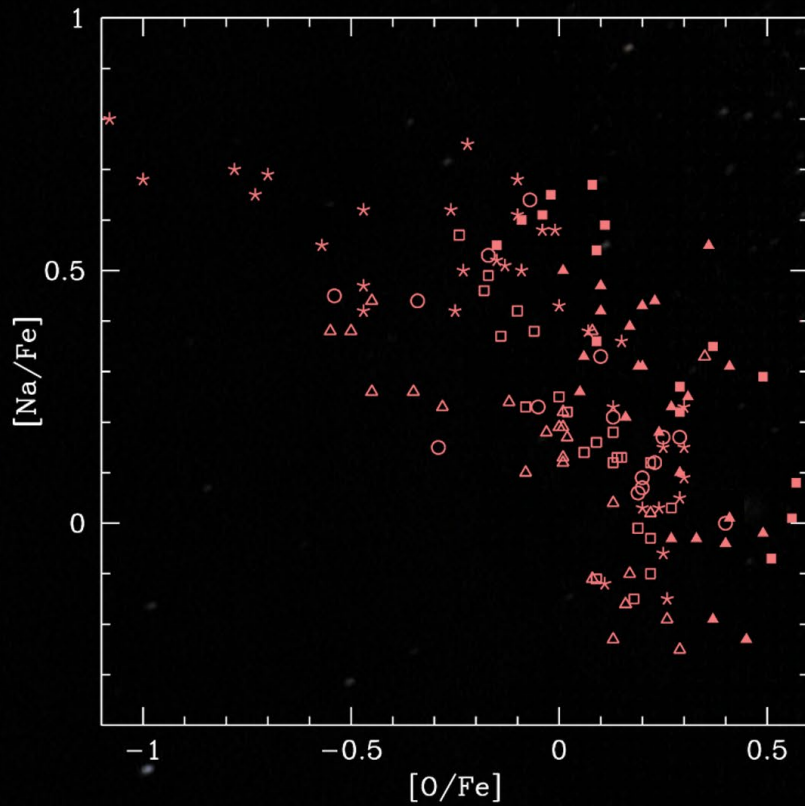
$t_{gc} \gtrsim 11.2 \text{ Gy}$

best-fit age $\approx 13.4 \text{ Gy}$



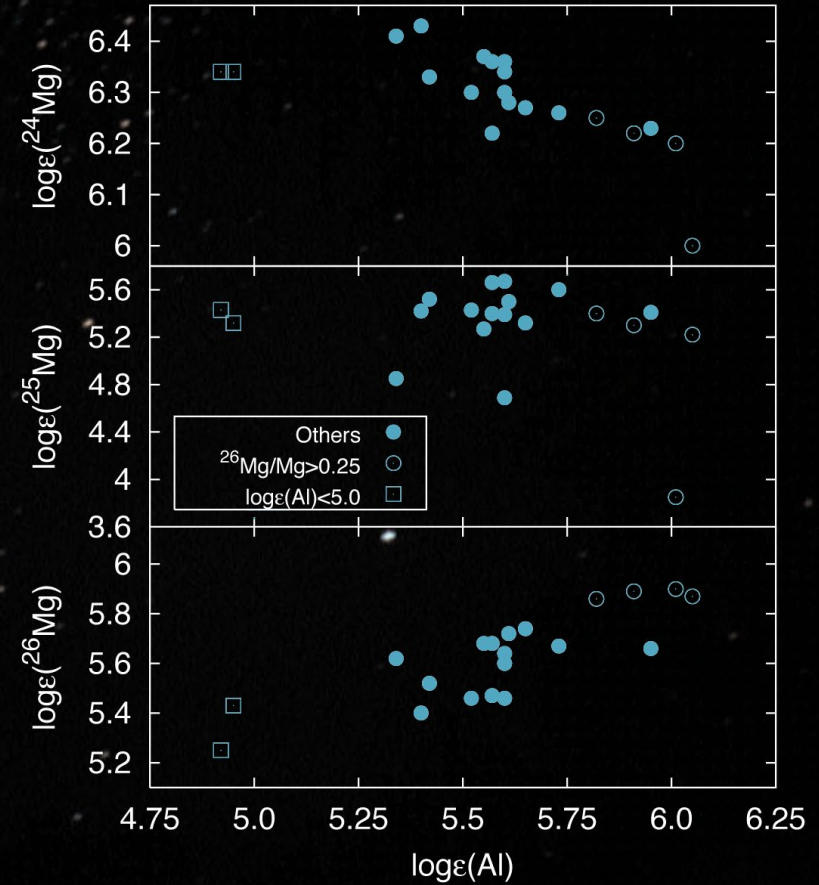
Abundance anomalies in globular clusters

Na vs. O



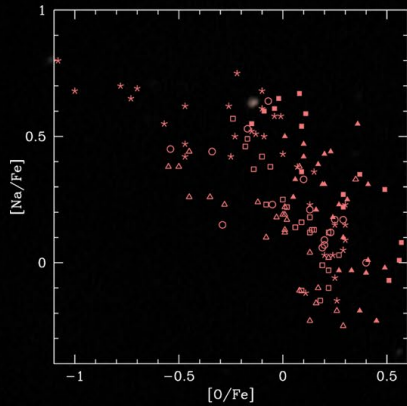
various clusters; see: P. Ventura and F. D'Antona, *A&A* 457, 995 (2006)

Mg vs. Al



NGC 6752: D. Yong et al., *A&A* 402, 985 (2003)

Abundance anomalies in globular clusters

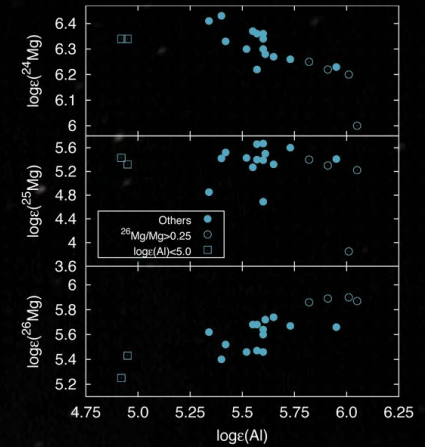


Note range and overall enhancement of Na, Mg and anticorrelation with O, Al

This is observed in clusters, but not in field stars

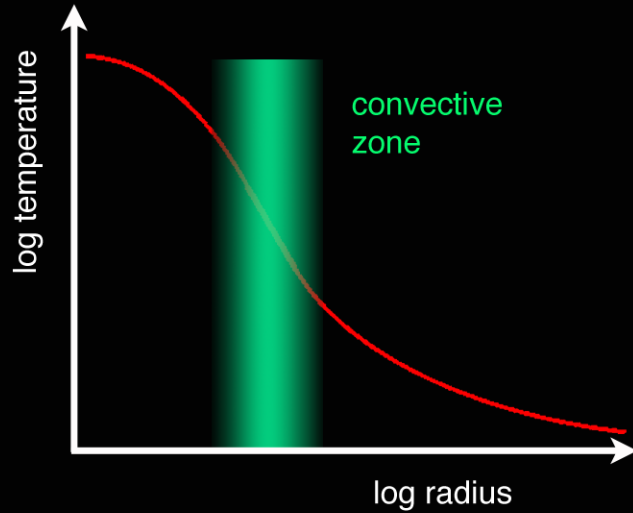
Neither Na nor Al should be on the surfaces of these stars because the surface radiative zone stops convection

Is this the signature of some “extra” mixing process? If so, what does this imply for evolution and cluster ages?

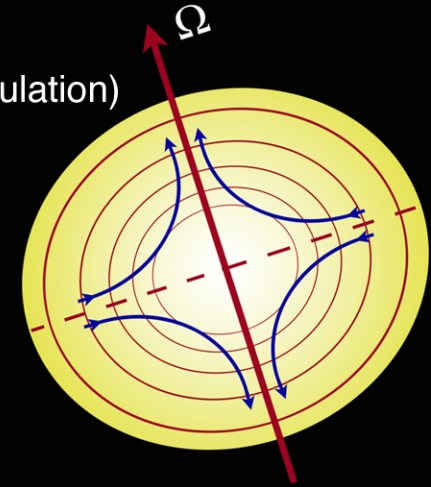


mixing mechanisms

1. convection



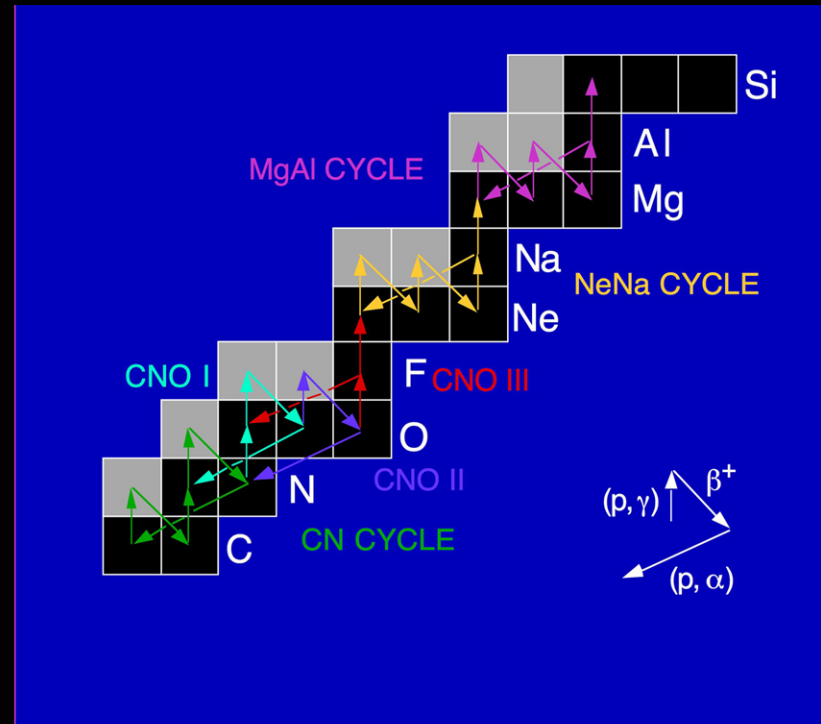
2. rotation (meridional circulation)



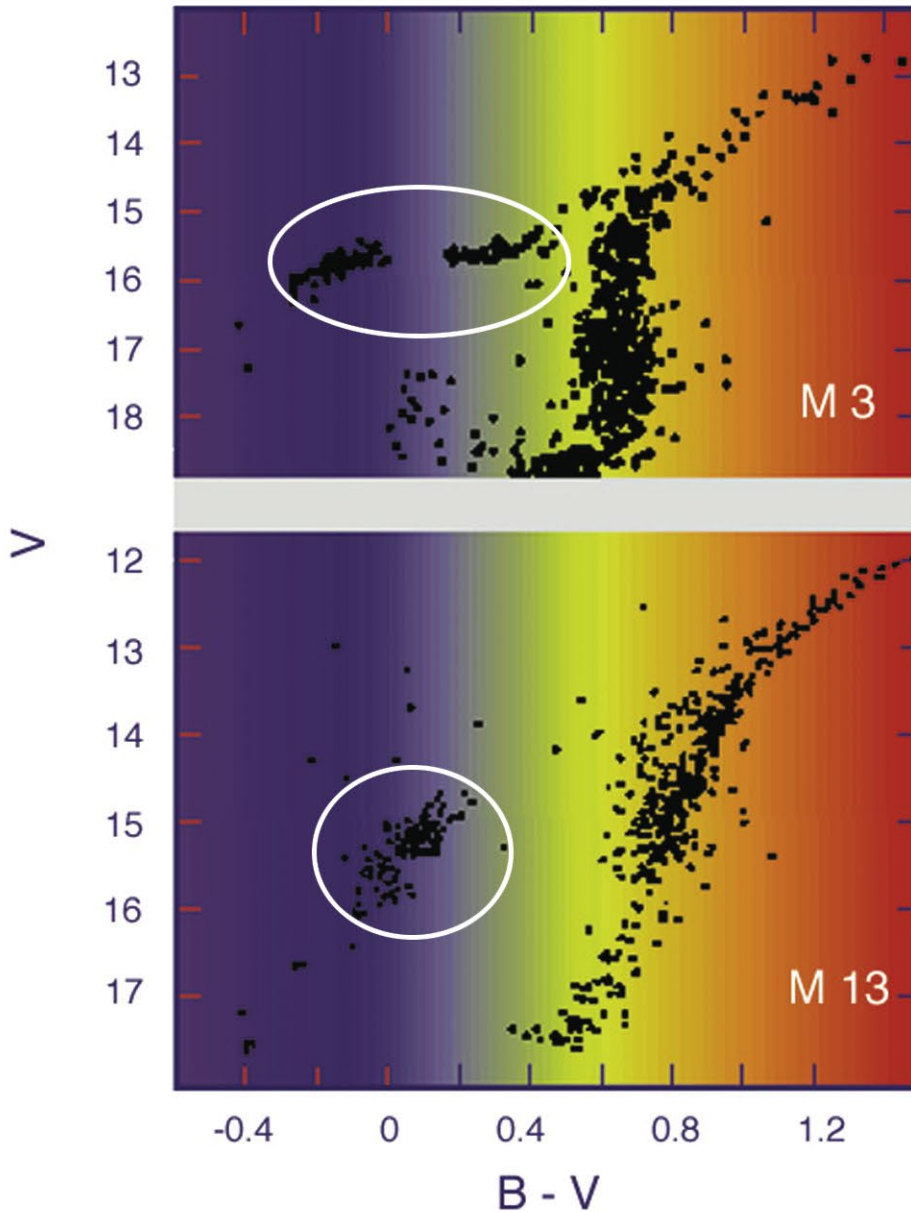
3. gravitational settling

4. diffusion

5. MHD, etc.



2 clusters with similar $[Fe/H]$ (~ -1.6), but note differences in “horizontal branch” (core He burning)

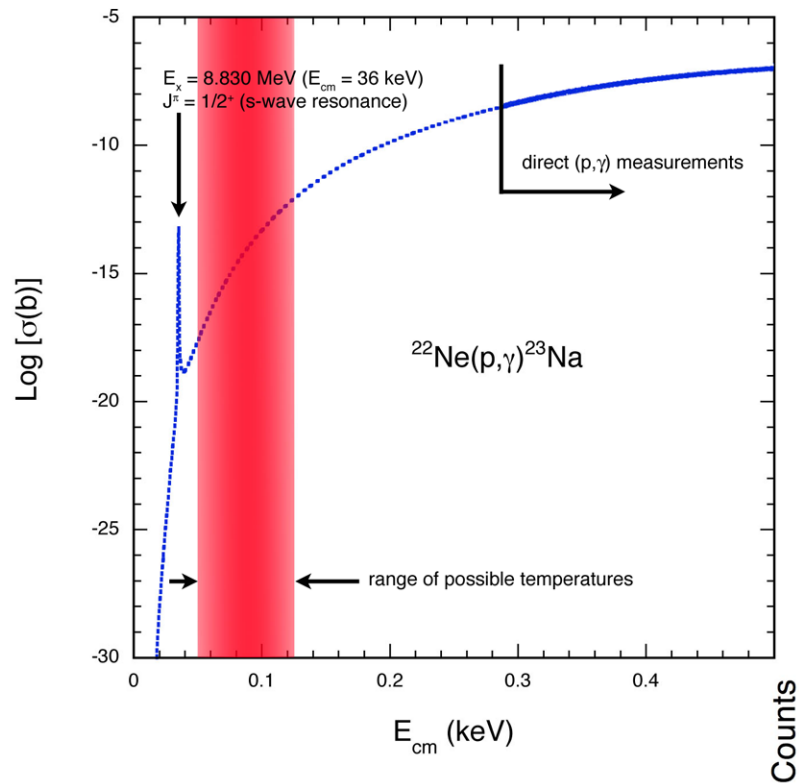


no Al vs. Mg

Al vs. Mg

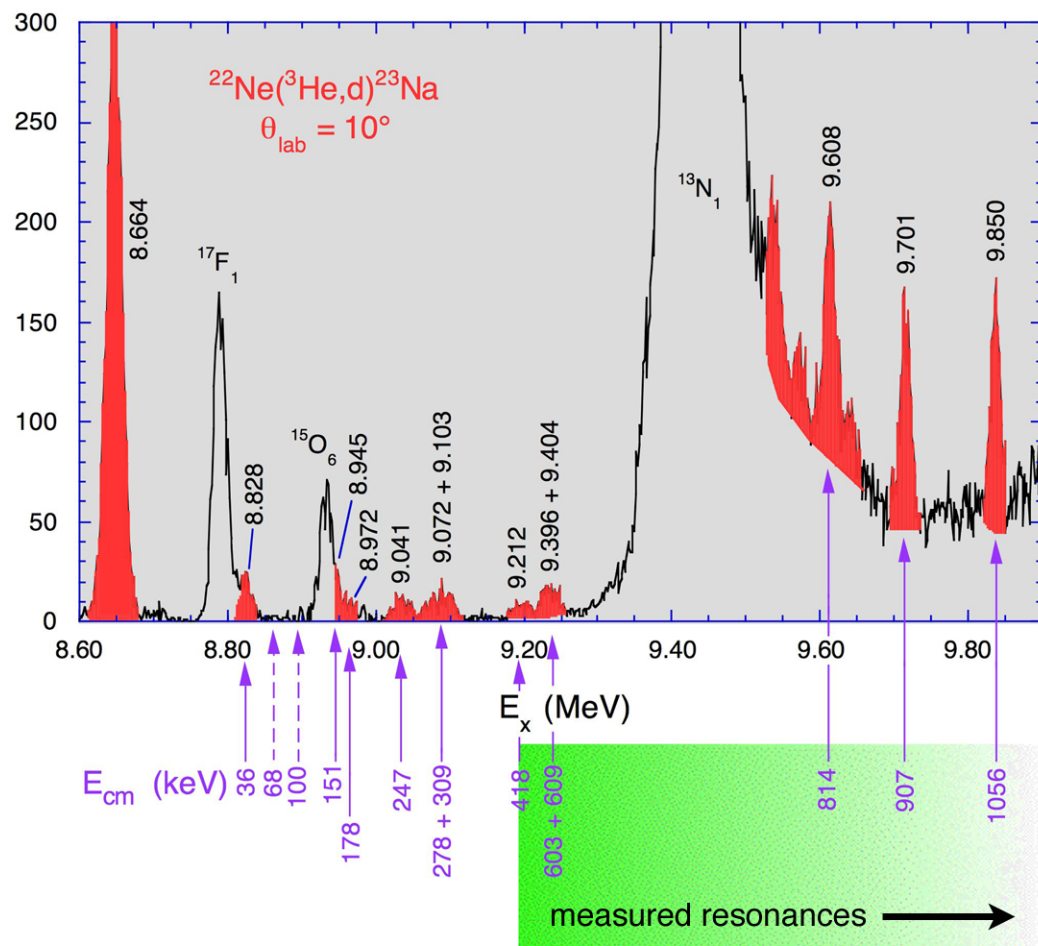
if mixing brings Al to the surface, it also brings He; He displaces H^- and opacity drops \rightarrow envelope shrinks and gets bluer, brighter

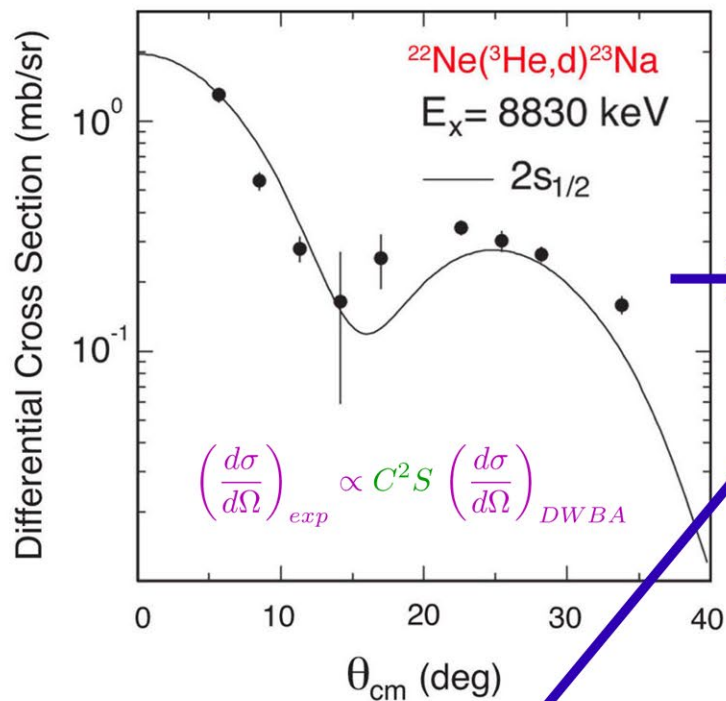
overestimate age by 2 Gy?



← this is a common situation - a direct measurement of the 36-keV resonance would take several million years of beam time

indirect approach →





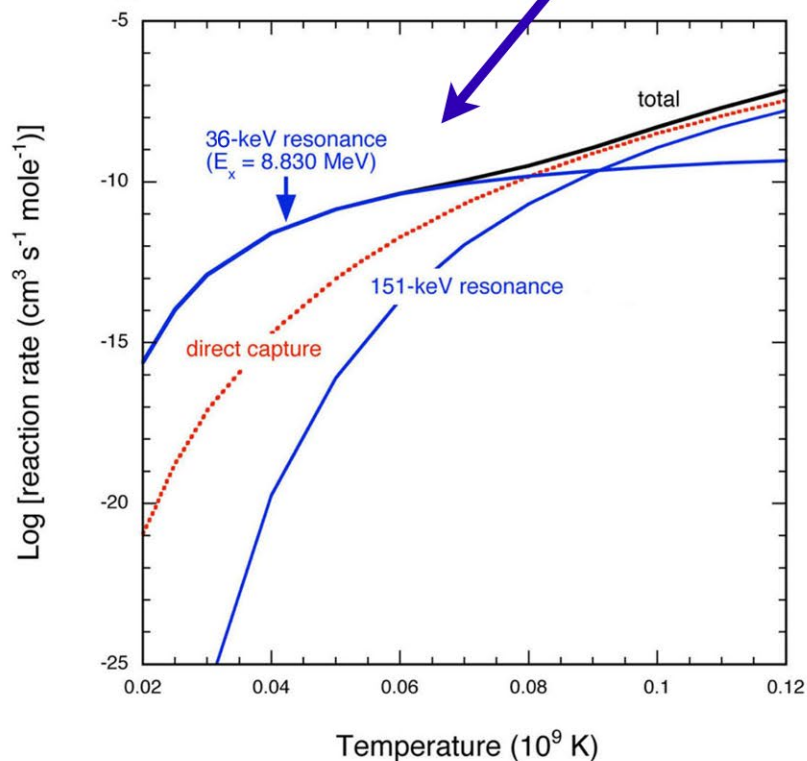
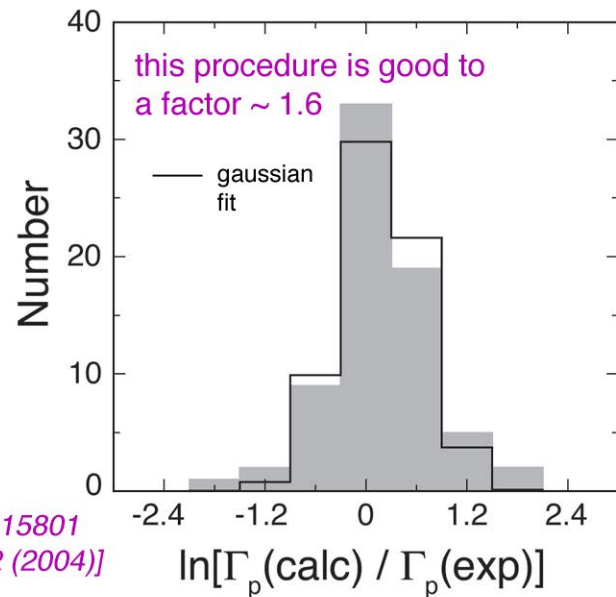
$$\omega\gamma = \omega \frac{\Gamma_p \Gamma_\gamma}{\Gamma} \approx \omega \Gamma_p$$

$$\Gamma_p = 2 C^2 S \gamma_{sp}^2 P_\ell(E_r)$$

$$C^2 S = 0.02$$

$$\rightarrow \Gamma_p = 3.6 \times 10^{-15} \text{ eV}$$

[S.E. Hale et al., Phys. Rev. **C65**, 015801 (2001) and Phys. Rev. **C70**, 045802 (2004)]



alternately, overlap integral for $B \rightarrow A + p$ can be approximated:

$$I_A^B(r) \approx C_B \frac{W_{-\eta, l+1/2}(2kr)}{r}$$

↑
asymptotic normalization coefficient

(by the way, $C_B = (C^2 S)^{1/2} b_B$; single-particle radial wavefn

$$R(r) \approx b_B \frac{W_{-\eta, l+1/2}(2kr)}{r}$$

the procedure for extracting ANCs is less model dependant than for spectroscopic factors, but this largely goes away in the calculation of Γ_p

[see e.g. A.M. Mukhamedzhanov & R. Tribble, Phys. Rev. **C59**, 3418 (1999) and P.F. Bertone et al., Phys. Rev. **C66**, 055804 (2002) for a comparison of the 2 techniques]

The current picture:

1. Na vs. O can arise from $O \rightarrow N$ in the CN cycle and $Ne \rightarrow Na$ in the NeNa cycle IF the rate for the $^{23}\text{Na}(p,\alpha)^{20}\text{Ne}$ reaction is reduced by a factor of ~ 4 [see P. Ventura and F. D'Antona, A&A 457, 995 (2006)].

2. H-burning in low-mass stars can not produce Mg vs. Al unless our current stellar models are wrong (predicted temperatures are too low).

3. Both effects can arise from environmental pollution - winds from AGB stars.



AGB stars

false-color image of NGC 2371:

hydrogen

oxygen

sulfer, nitrogen

C-O core (white dwarf)

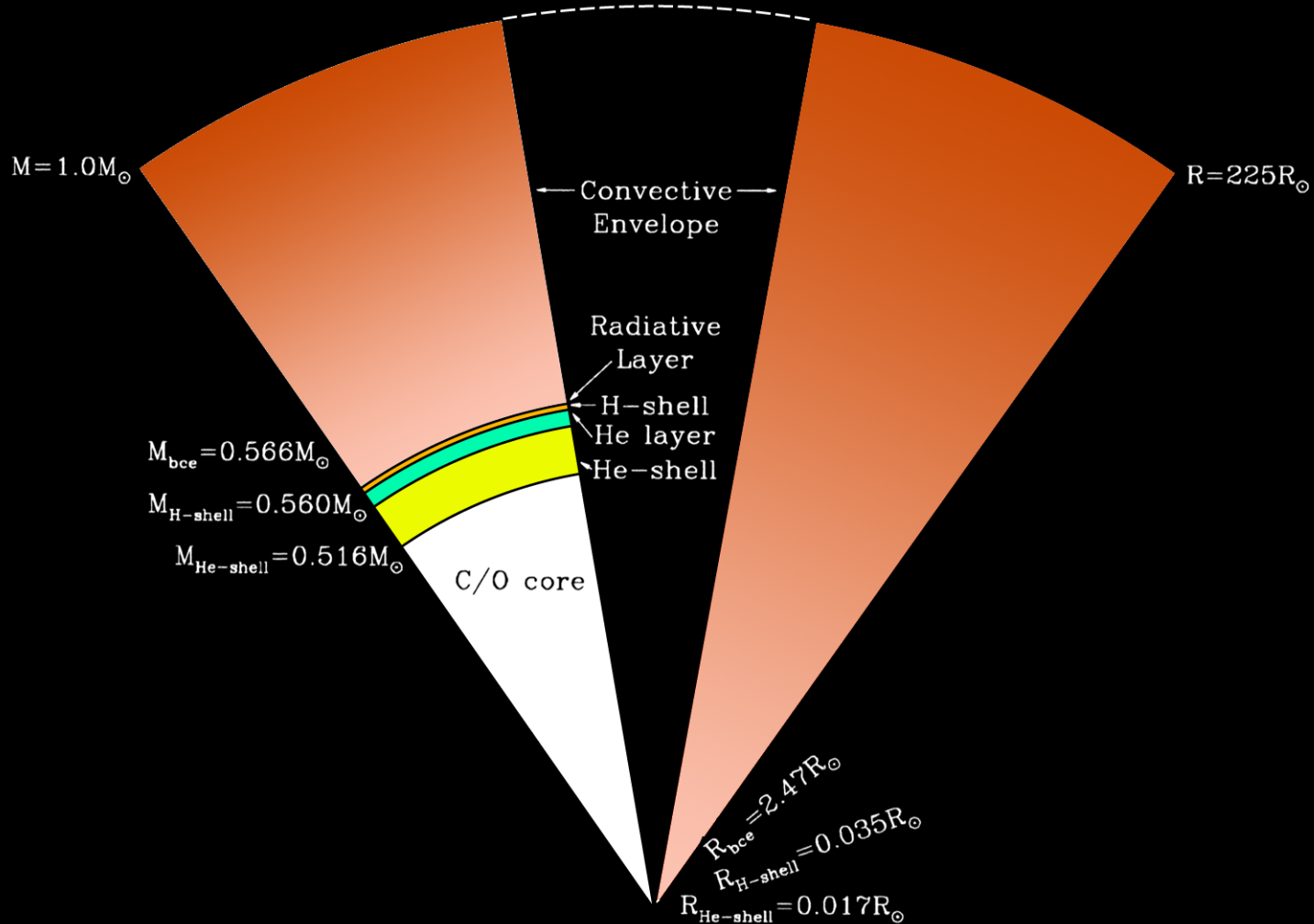


Fig. 2.6. A schematic view of a $1 M_{\odot}$ AGB star interior. On the **left**, various regions in the star are plotted against mass fraction, while on the **right** the regions are plotted against radius. M_{bce} is the mass at the base of the convective envelope, while $M_{\text{H-shell}}$ and $M_{\text{He-shell}}$ are the masses at the middle of the hydrogen- and helium-burning shells, respectively

[adapted from J.C. Lattanzio and P.R. Wood in "Asymptotic Giant Branch Stars", H. J. Habing, Hans Olofsson, ed., Springer (2003)]

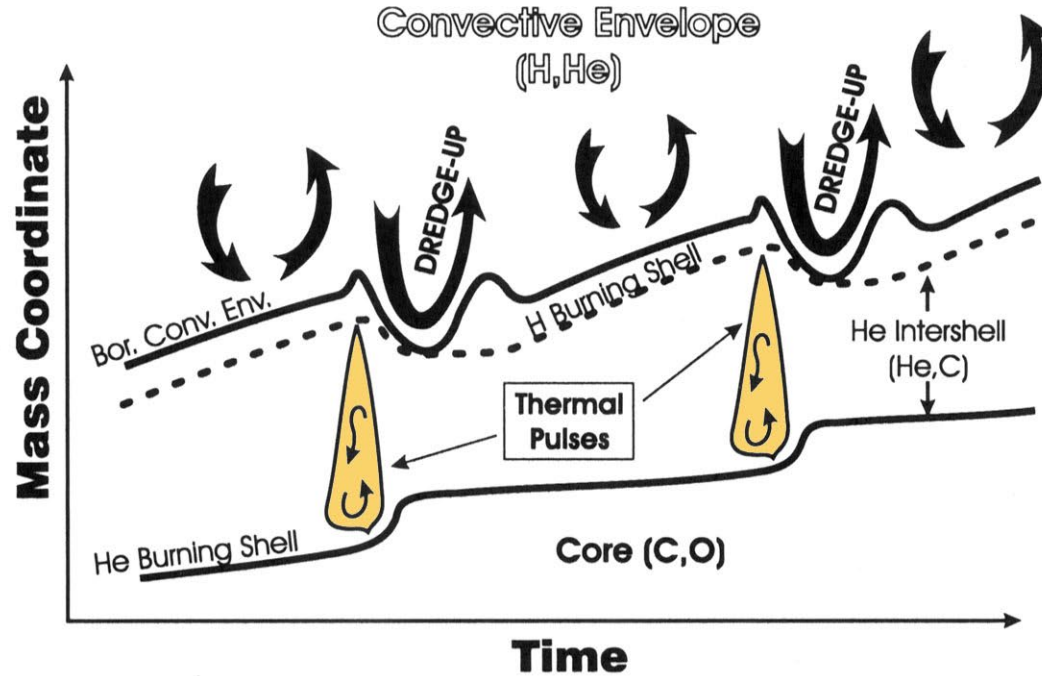


Fig. 1. This sketch illustrates the evolution of the positions of the inner border of the convective envelope, the H-burning shell and the He-burning shell, during the thermally pulsing AGB phase. The convective regions generated by two subsequent thermal pulses are also shown. Note that the temporal developments of thermal pulses and of following TDU episodes are off scale with respect to the interpulse period.

AGB nucleosynthesis ($\sim 1-3 M_{\odot}$)

1. Interpulse phase, H-burning shell is main source of luminosity:

H \rightarrow He in CNO cycles; $^{12}\text{C} \downarrow$, $^{18}\text{O} \downarrow$, $^{13}\text{C} \uparrow$, $^{14}\text{N} \uparrow$, $^{17}\text{O} \uparrow$
if base of convective envelope reaches H-burning shell,
then ^7Li , ^{19}F , NeNa and MgAl cycles in “hot-bottom
burning”

Mixing of protons from envelope into intershell;
 $^{12}\text{C}(p,\gamma)^{13}\text{N}(\beta^+)^{13}\text{C}(\alpha,n)^{16}\text{O}$,
n + “Fe” \rightarrow “s-process” (main component)

2. Thermal pulse, He-burning shell is main source of luminosity:

$3\alpha \rightarrow ^{12}\text{C}$, $^{12}\text{C}(\alpha,\gamma)^{16}\text{O}$
 $^{14}\text{N}(\alpha,\gamma)^{18}\text{F}(\beta^+)^{18}\text{O}(\alpha,\gamma)^{22}\text{Ne}(\alpha,n)^{25}\text{Mg}$
n + “Fe” \rightarrow s-process

3. Power down: convective envelope reaches into intershell
“dredge up”

How do we know that this is happening?

SPECTROSCOPIC OBSERVATIONS OF STARS OF CLASS S

PAUL W. MERRILL

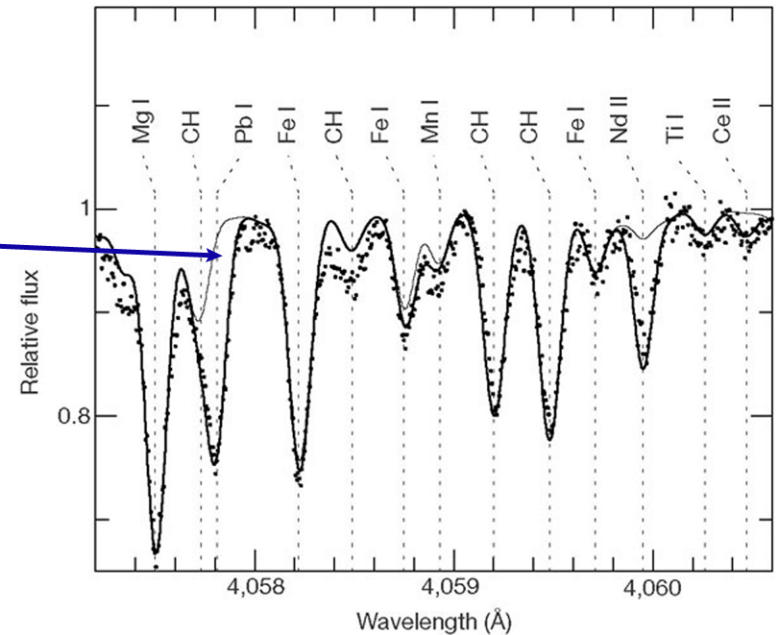
MOUNT WILSON AND PALOMAR OBSERVATORIES
CARNEGIE INSTITUTION OF WASHINGTON
CALIFORNIA INSTITUTE OF TECHNOLOGY

Received February 27, 1952

Lines of $Tc\ I$, an element believed to have no completely stable isotope, appear to be stronger in the stars with the more dominant S-type characteristics. This fact, together with others, might suggest that S-type stars represent a comparatively transient phase of stellar existence.

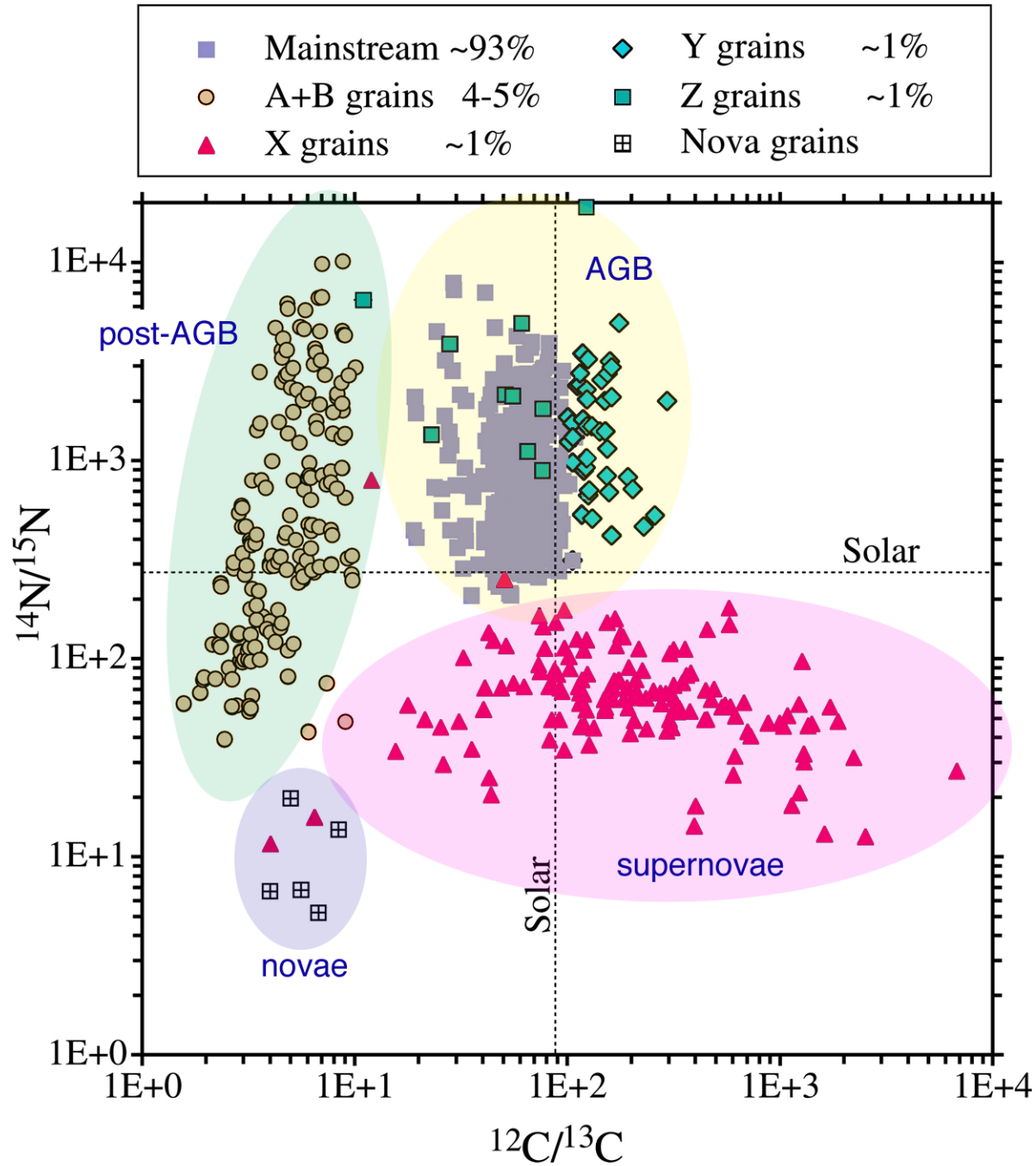
ApJ 116, 21 (1952)

enhanced Pb in AGB stars



S. Van Eck, S. Goriely, A. Jorissen and B. Plez, Nature 412, 793 (2001)

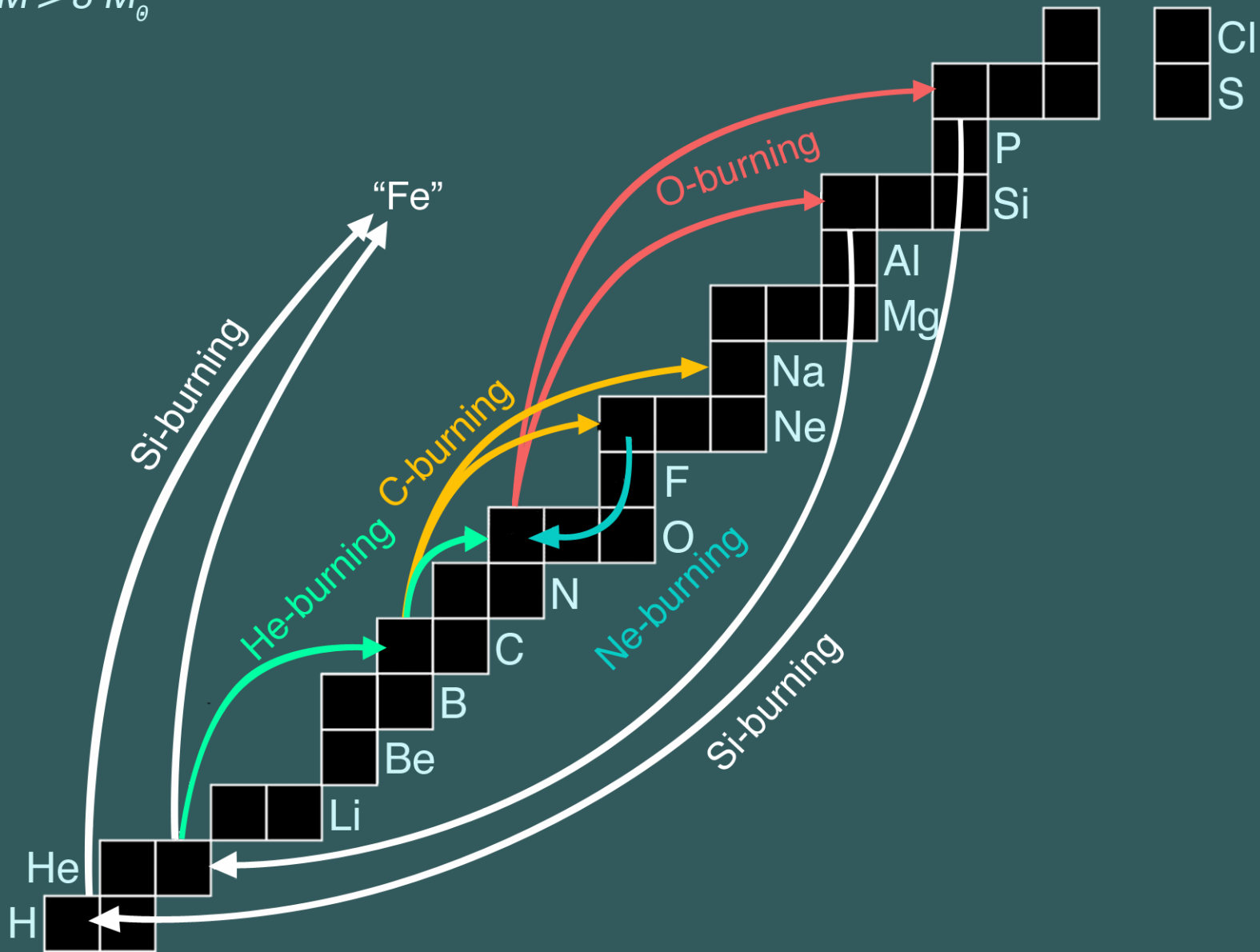
SiC meteoritic grains



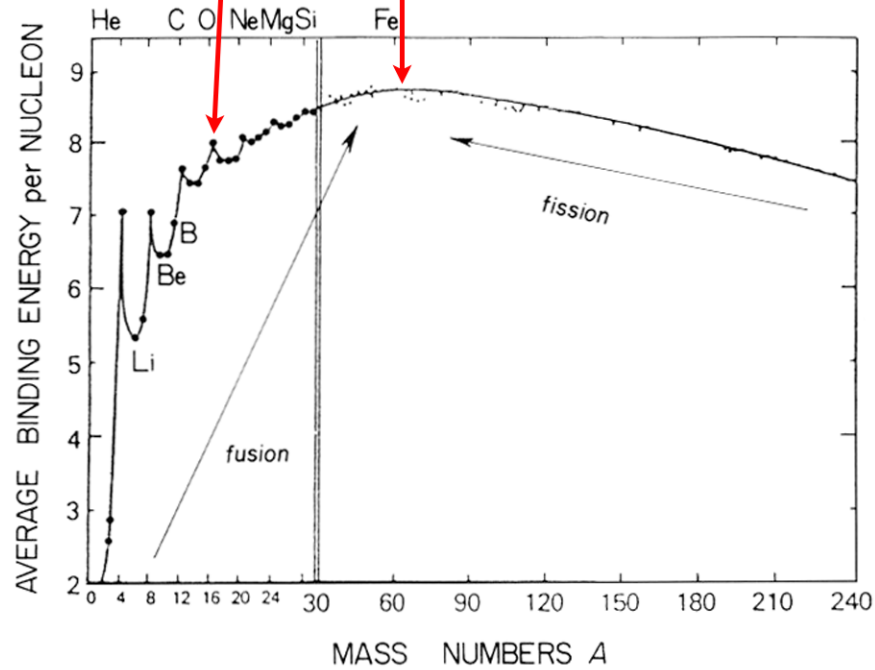
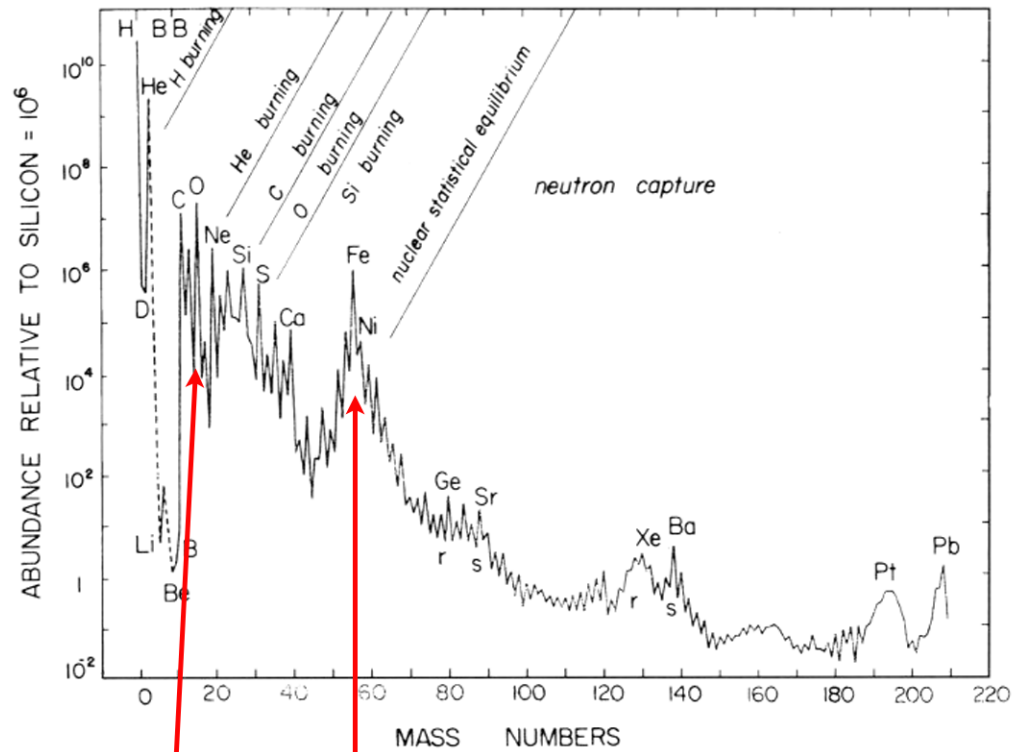
adapted from E. Zinner et al., *Ap J* 650, 350 (2006)

Advanced burning stages

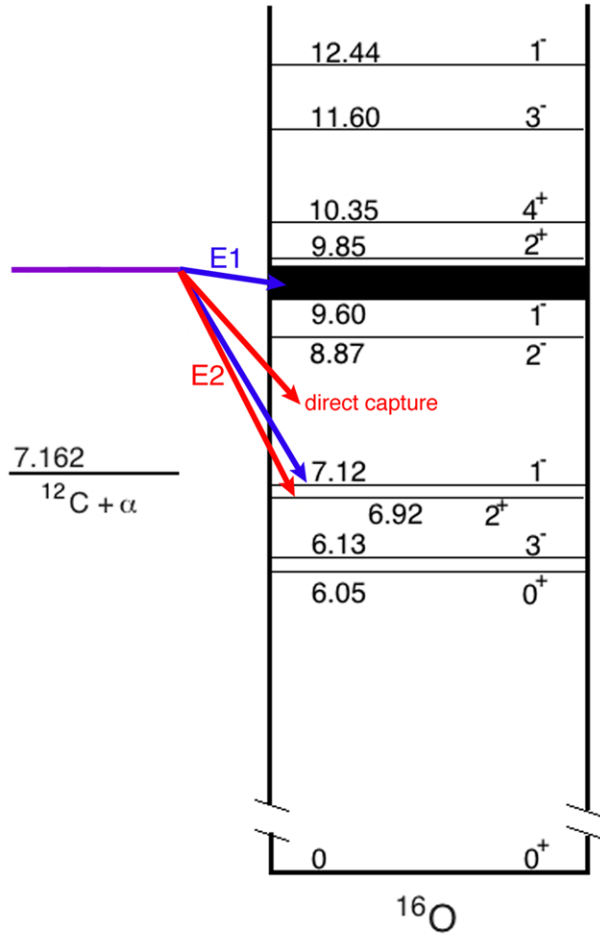
$M > 8 M_{\odot}$



elemental distribution
reflects some basic
nuclear properties



$^{12}\text{C}(\alpha, \gamma)^{16}\text{O}$



must also include interference with tails of distant 1⁻ and 2⁺ states

recent capture data and R-matrix fits

J. Phys. G: Nucl. Part. Phys. **35** (2008) 014009

F Strieder

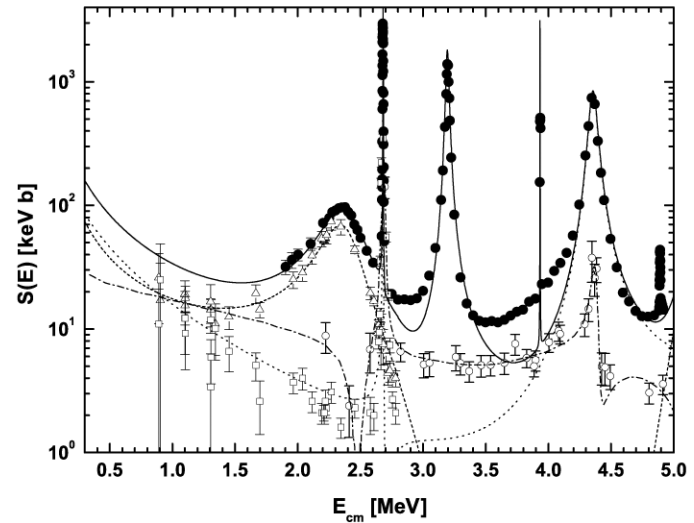


Figure 1. ERNA total S factor data (filled-in circles) [20] for $^{12}\text{C}(\alpha, \gamma)^{16}\text{O}$ compared with the recent E1 (open triangles) and E2 (open squares) γ -measurements [19] and the $E_x = 6.05$ MeV cascade data (open circles) [21]. The solid line represents the sum of the single amplitudes of an R matrix fit [26] (the dotted and dashed lines are the E1 and E2 amplitudes, respectively). In addition, the R matrix fit of [21] to their cascade data (dotted-dashed line) is shown. The latter component is not included in the sum and might explain the high yield in the ERNA data between the resonances.

[19] Assunção M *et al* 2006 *Phys. Rev. C* **73** 055801

Fey M 2004 *PhD Thesis* Universität Stuttgart, Germany

[20] Schürmann D *et al* 2005 *Eur. Phys. J. A* **26** 301

[21] Matei C *et al* 2006 *Phys. Rev. Lett.* **97** 242503

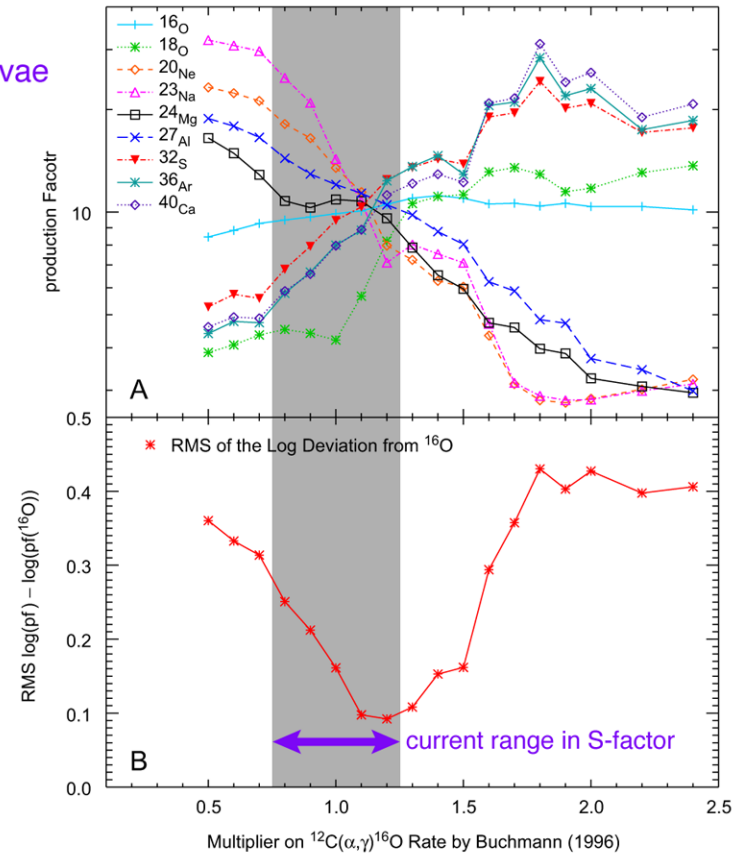
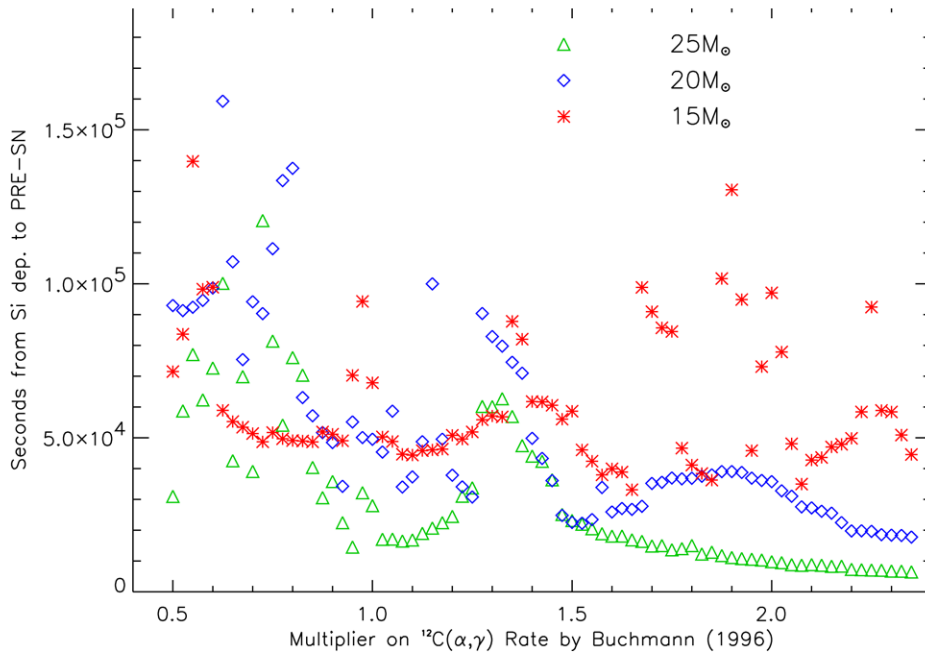
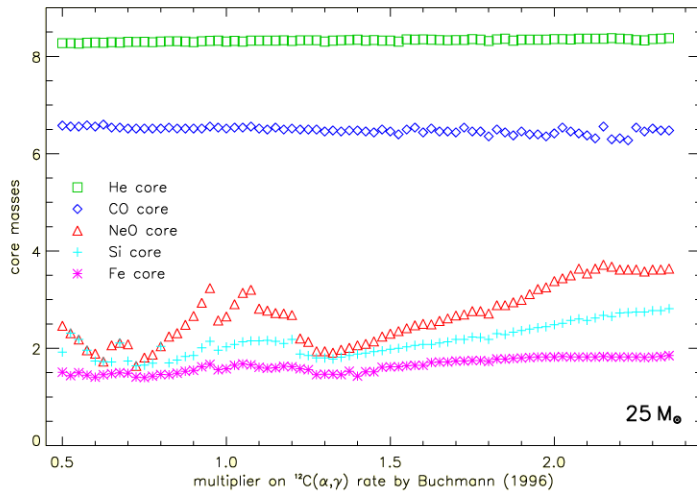
[26] Kunz R *et al* 2002 *Astrophys. J.* **567** 643

$S(300) = 145 \text{ keV b} \pm \sim 25\%$

[L.R. Buchmann and C.A. Barnes, *Nucl. Phys. A* **777**, 256 (2006)]

effect of $^{12}\text{C}(\alpha,\gamma)$ in massive stars (some examples)

supernovae



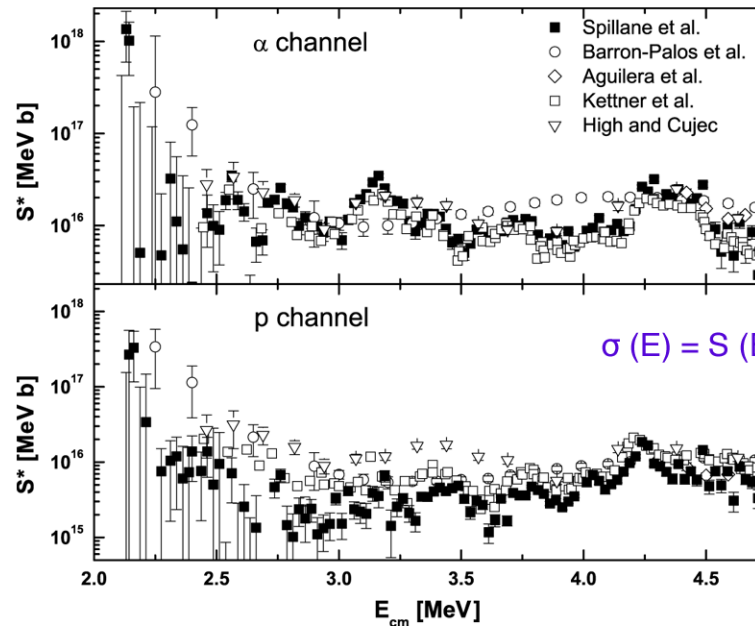
S.E. Woosley and A. Heeger, Phys. Rep. 442, 269 (2007)
 and *M. Boyse, senior thesis, U.C. Santa Cruz (2002)*
 (<http://www.supersci.org/data/nucleo/12cag/index.html>)

also: chemical composition of white dwarfs,
 propagation of deflagration front in SNIa, etc.

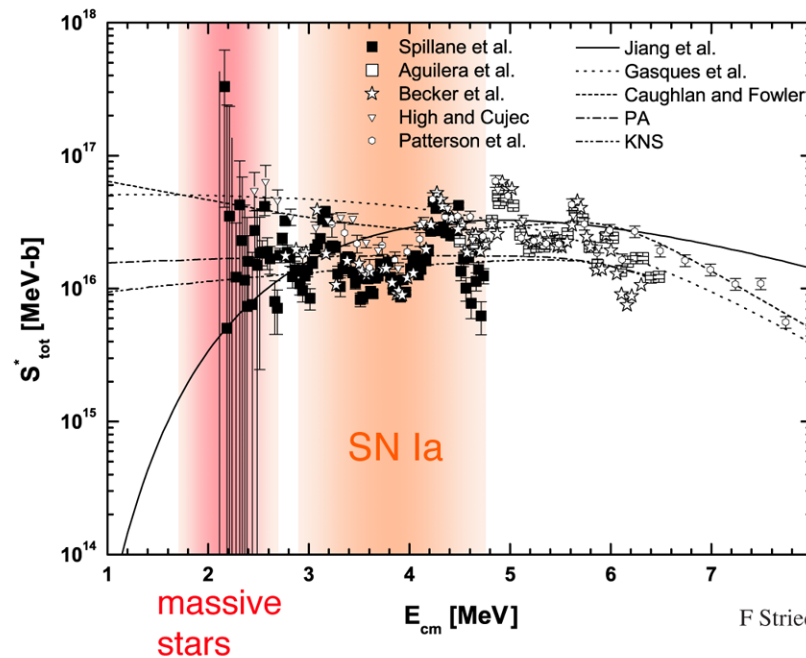
Carbon burning: $^{12}\text{C} + ^{12}\text{C}$
 $^{12}\text{C} + ^{16}\text{O}$

$M > 8 M_{\odot}$, $T_9 \sim 0.85$ or SN Ia, CO white dwarf, $T_9 \sim 2.0$

2 dominant channels



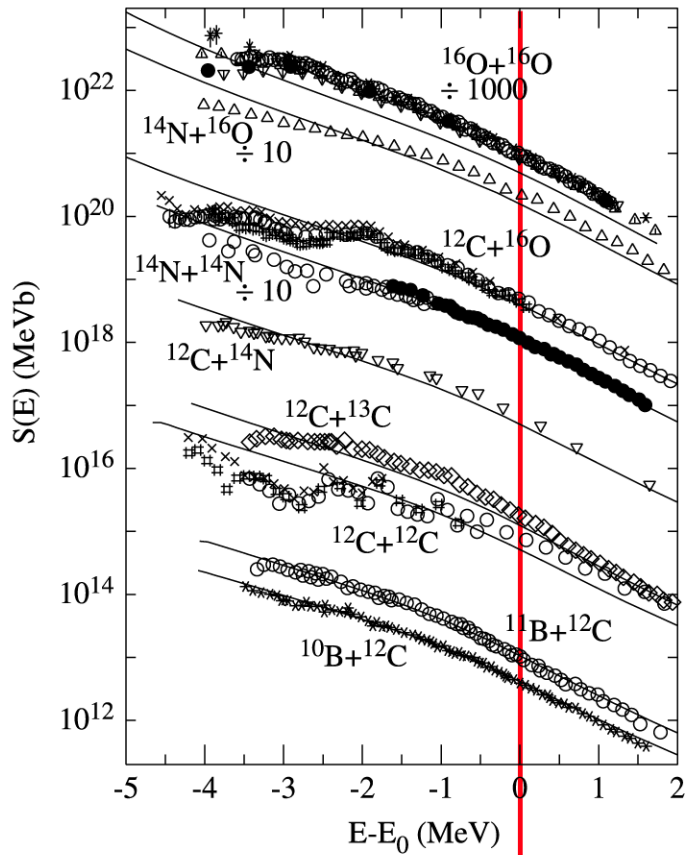
$$\sigma(E) = S(E) \cdot E^{-1} \exp(-87.21E^{-1/2} - 0.46E)$$



origin of resonant structures
 is not well understood -
 quasi-molecular states?

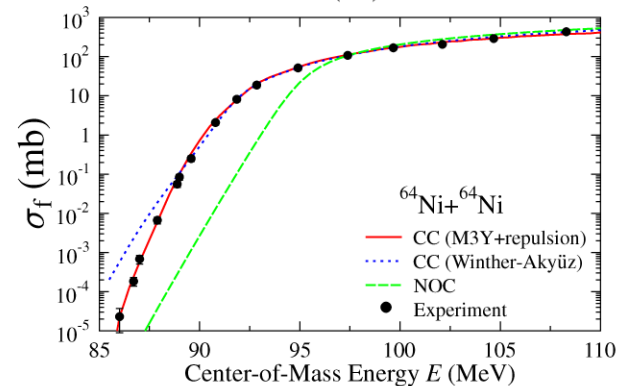
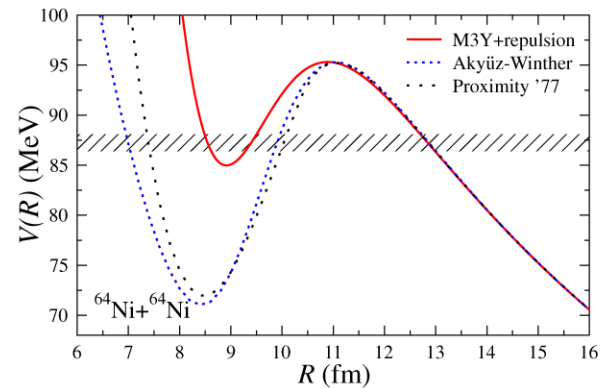
Do we understand the fusion process at low energies?

[see C.L. Jiang et al., *Phys Rev. C* 75, 015803 (2007)]

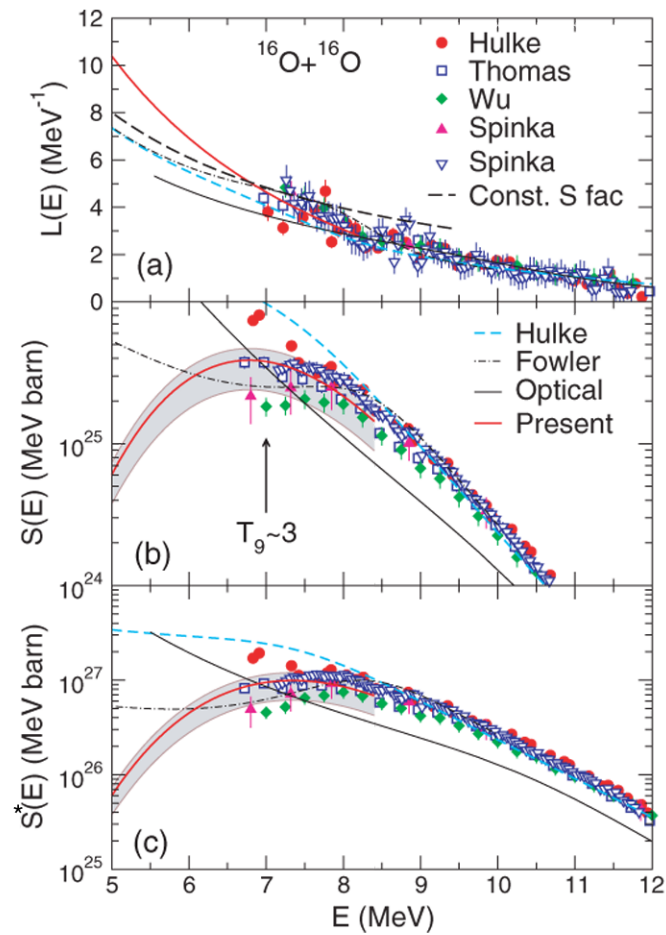


Coulomb barrier

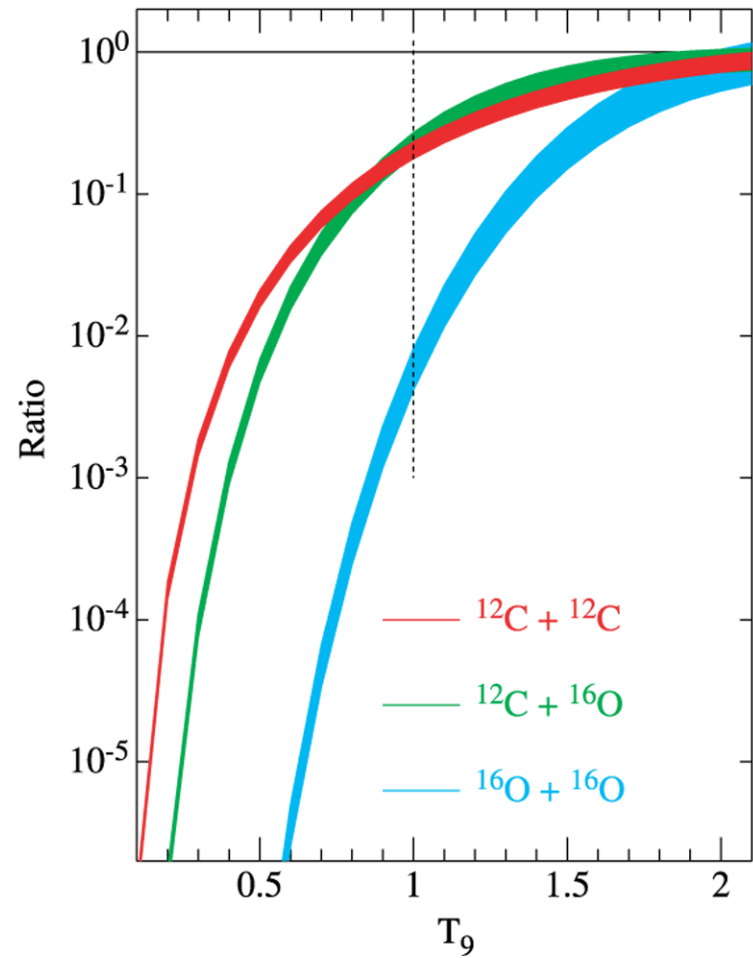
Notice that (optical-model) calculations over-predict the low-energy S-factor. Short-range repulsive part of N-N interaction gives rise to minimum in energy vs. density at about 0.16 nucleons/fm³ ("saturation density"). This reduces the tunneling probability at low energies. In terms of potentials [see S. Mescu and H. Esbensen, (*PRL* 96, 112701 (2006))]:



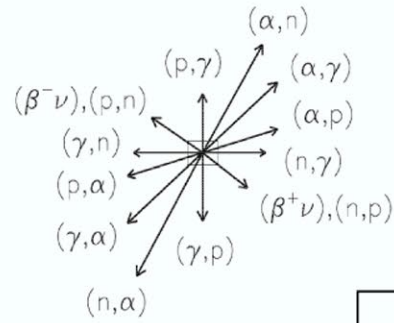
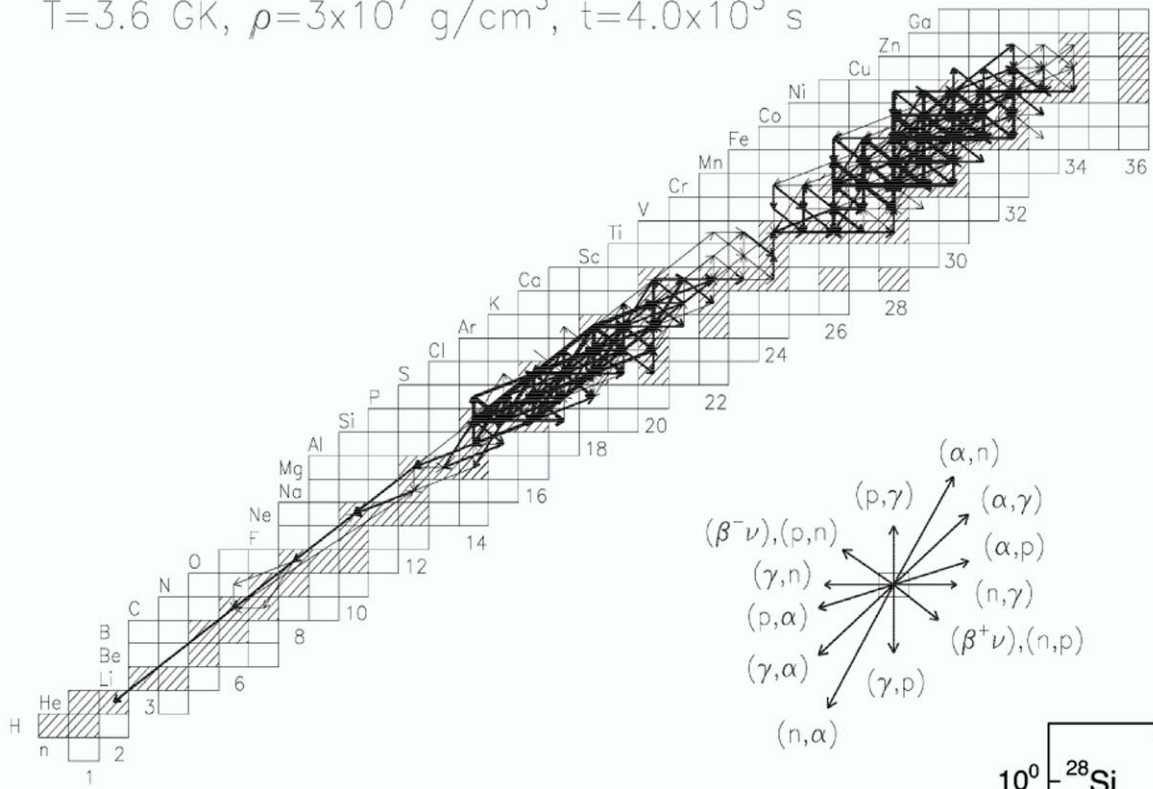
from C.L. Jiang, *Phys. Rev. C* **75**, 015803 (2007)



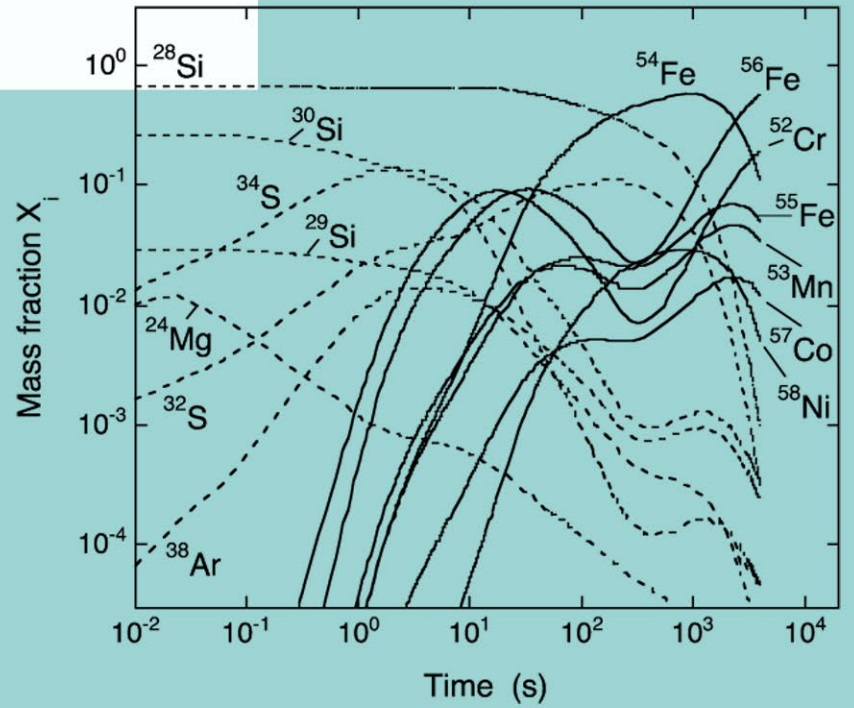
ratio vs. Fowler, Caughlam, Zimmerman compilation (1975)



$T=3.6 \text{ GK}$, $\rho=3 \times 10^7 \text{ g/cm}^3$, $t=4.0 \times 10^3 \text{ s}$



Core Si-burning
25 M_{\odot}



(courtesy of C. Iliadis)

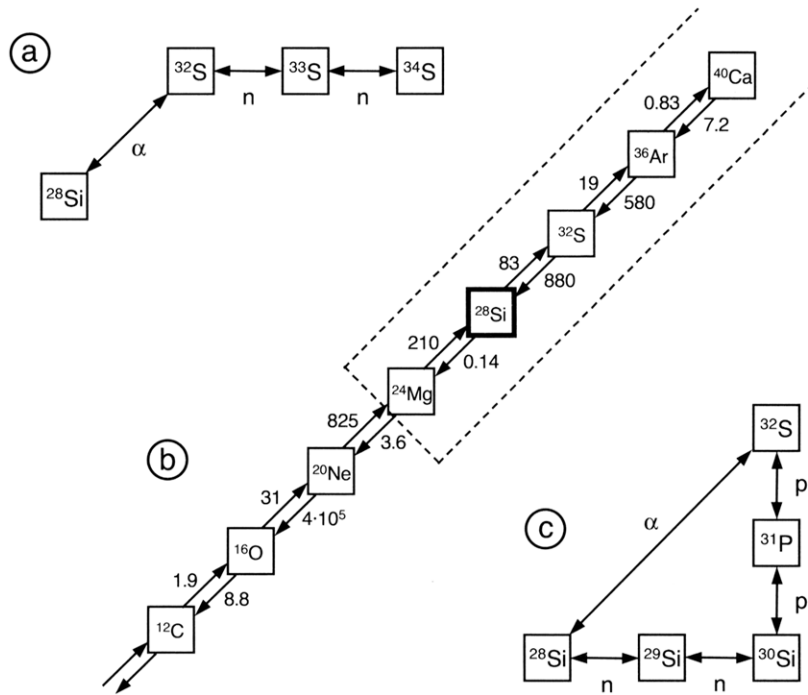
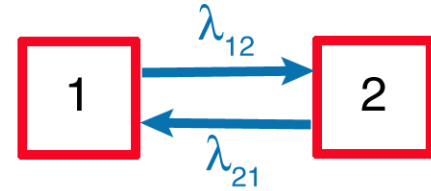


Fig. 5.54 Reaction chains in silicon burning. (a) The reaction chain $^{28}\text{Si} \leftrightarrow ^{32}\text{S} \leftrightarrow ^{33}\text{S} \leftrightarrow ^{34}\text{S}$ in equilibrium. (b) $(\alpha, \gamma) \leftrightarrow (\gamma, \alpha)$ reaction links between ^{12}C and ^{40}Ca . The numbers next to the arrows indicate values of the decay constants λ_α and λ_γ (in units of s^{-1}) for (α, γ) and (γ, α) reactions, respectively, assuming a temperature of $T = 3.6$ GK. The quantity

λ_α is calculated by using $\rho = 3 \times 10^7 \text{ g/cm}^3$ and $X_\alpha = 10^{-6}$. The latter value is adopted from the network calculation displayed in Fig. 5.52. Nuclides located within the region demarked by the dashed lines are in quasiequilibrium. (c) The closed reaction chain $^{28}\text{Si} \leftrightarrow ^{32}\text{S} \leftrightarrow ^{31}\text{P} \leftrightarrow ^{30}\text{Si} \leftrightarrow ^{29}\text{Si} \leftrightarrow ^{28}\text{Si}$ in equilibrium.

photodisintegration leads to equilibrium



$$\frac{dN_1}{dt} = -N_1\lambda_{12} + N_2\lambda_{21}$$

$$\frac{dN_2}{dt} = -N_2\lambda_{21} + N_1\lambda_{12}$$

$$\frac{d}{dt} \begin{pmatrix} N_1 \\ N_2 \end{pmatrix} = \begin{bmatrix} -\lambda_{12} & \lambda_{21} \\ \lambda_{12} & -\lambda_{21} \end{bmatrix} \begin{pmatrix} N_1 \\ N_2 \end{pmatrix}$$

$$\frac{d}{dt} \begin{pmatrix} N_1 \\ N_2 \end{pmatrix} = \begin{bmatrix} -\lambda_{12} & \lambda_{21} \\ \lambda_{12} & -\lambda_{21} \end{bmatrix} \begin{pmatrix} N_1 \\ N_2 \end{pmatrix}$$

suppose at $t = 0$, $\begin{pmatrix} N_1 \\ N_2 \end{pmatrix} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$, then

$$\begin{pmatrix} N_1(t) \\ N_2(t) \end{pmatrix} = \frac{1}{\lambda_{12} + \lambda_{21}} \begin{pmatrix} \lambda_{21} \\ \lambda_{12} \end{pmatrix} + \frac{1}{\lambda_{12} + \lambda_{21}} \begin{pmatrix} \lambda_{12} \\ -\lambda_{12} \end{pmatrix} e^{-(\lambda_{12} + \lambda_{21})t}$$

$$\begin{aligned} \text{after a sufficiently long time: } N_1 &\longrightarrow \frac{\lambda_{21}}{\lambda_{12} + \lambda_{21}} & N_1 \text{ and } N_2 \text{ form a} \\ N_2 &\longrightarrow \frac{\lambda_{12}}{\lambda_{12} + \lambda_{21}} & \text{quasi-equilibrium cluster} \end{aligned}$$

However, note that $N_1/N_2 (= \lambda_{21}/\lambda_{12})$ does not depend on reaction rates! Recall that we already derived

$$\frac{\lambda_{21}}{\lambda_{12}} \propto e^{-Q/kT}$$

When we calculate $\langle \sigma v \rangle$ for a photon-induced reaction, we have to include $E_\gamma = pc$ and photon statistics. At a given temperature,

$$\begin{aligned} \lambda_{21} &= \frac{8\pi}{h^3 c^2} \int_0^\infty \frac{E_\gamma^2}{e^{E_\gamma/kT} - 1} \sigma(E_\gamma) dE_\gamma \quad \text{and} \\ \frac{\lambda_{21}}{\lambda_{12}} &= \left(\frac{2\pi}{h^2} \right)^{3/2} \frac{(\mu kT)^{3/2}}{N_A} \frac{(2j+1)(2J_1+1)}{2J_2+1} e^{-Q_{12}/kT}, \end{aligned}$$

where J_1 and J_2 are the spins of nuclei 1 and 2; j is the spin of whatever is interacting with nucleus 1. Note that this depends on the Q -value, not on the cross section. One complication is that we now have to consider the roles of excited states in the transition rates, each of which makes its own contribution to λ_{12} and λ_{21} .

Excited states:

As long as the forward and backward reactions maintain equilibrium, the transition rate has the same form as before, but is weighted by the probability that the state in question is occupied. In other words, the transition rate is multiplied by a *normalized partition function*:

$$G^{norm} = \frac{\sum_i g_i e^{-E_{xi}/kT}}{g_{ground}}, \text{ where } g = 2J + 1$$

Also, to do this properly, we need to keep track of the number of reacting nuclei, which I'll call N_0 . The net result is that the abundance ratio N_2/N_1 is replaced by N_2/N_0N_1 :

$$0+1 \leftrightarrow 2+\gamma : \frac{N_2}{N_0N_1} = \left(\frac{h^2}{2\pi}\right)^{3/2} \frac{1}{(\mu_{01}kT)^{3/2}} \frac{G_3^{norm}}{G_0^{norm}G_1^{norm}} e^{-Q_{0+1}/kT} \text{ (Saha equation)}$$

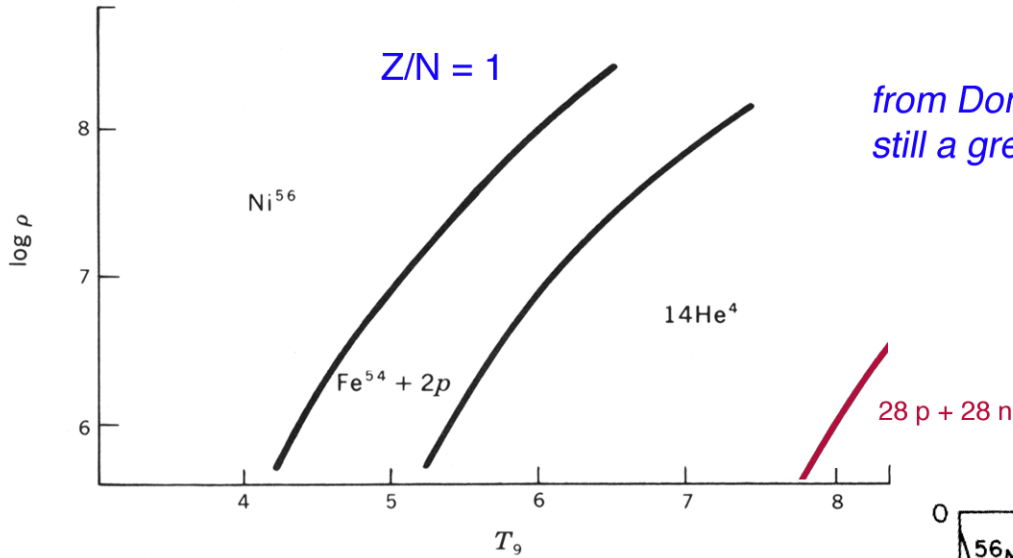
Here's an example. Suppose that the initial Si is dissociated into a gas of protons and neutrons, which are re-assembled into heavier nuclei, which are photodisintegrated, etc. so that all forward and backward reactions are in equilibrium. Nucleus Y is made of π protons and ν neutrons, and

$$N_Y = N_p^\pi N_n^\nu \frac{1}{\theta^{A-1}} \left(\frac{m_Y}{m_p^\pi m_n^\nu}\right) \frac{g_Y}{2^A} G_Y^{norm} e^{B_Y/kT}$$

$$\text{where } A = \pi + \nu \text{ and } \theta = (\mu_{01}kT)^{3/2}.$$

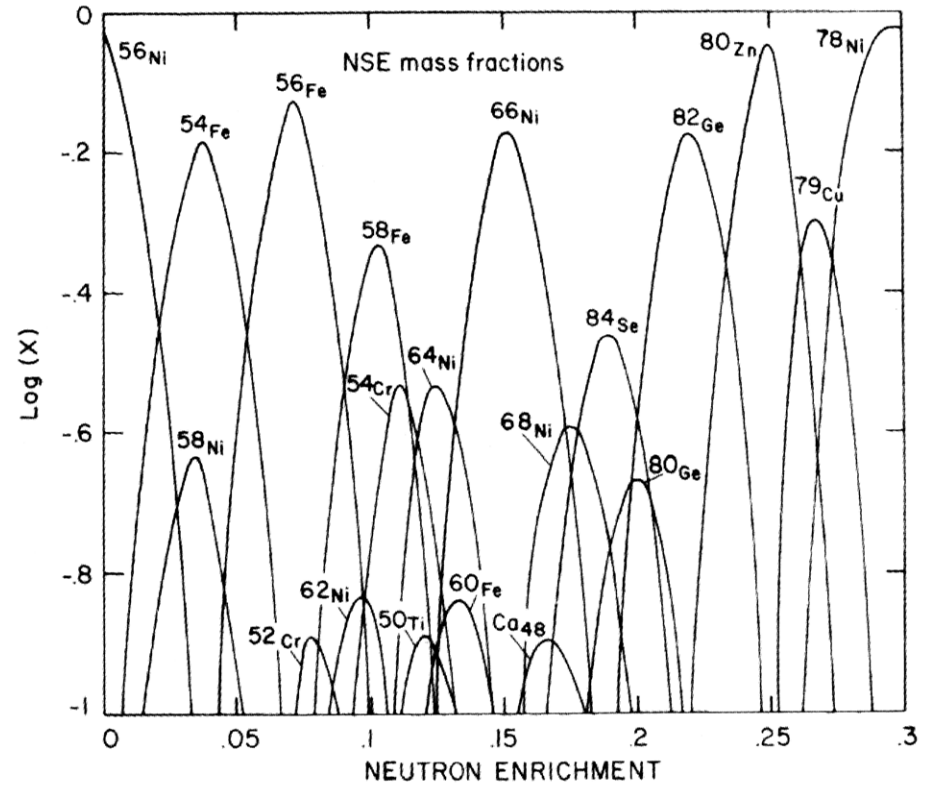
This requires multiple applications of the Saha equation - one for each step up to nucleus Y. Notice that the Q-value is replaced by the binding energy of Y (B_Y), which is just the Q-value for assembling π protons and ν neutrons.

During Si-burning, nucleons and nuclei are re-arranged in favor of maximum binding energy, which depends on T , ρ and Z/N :

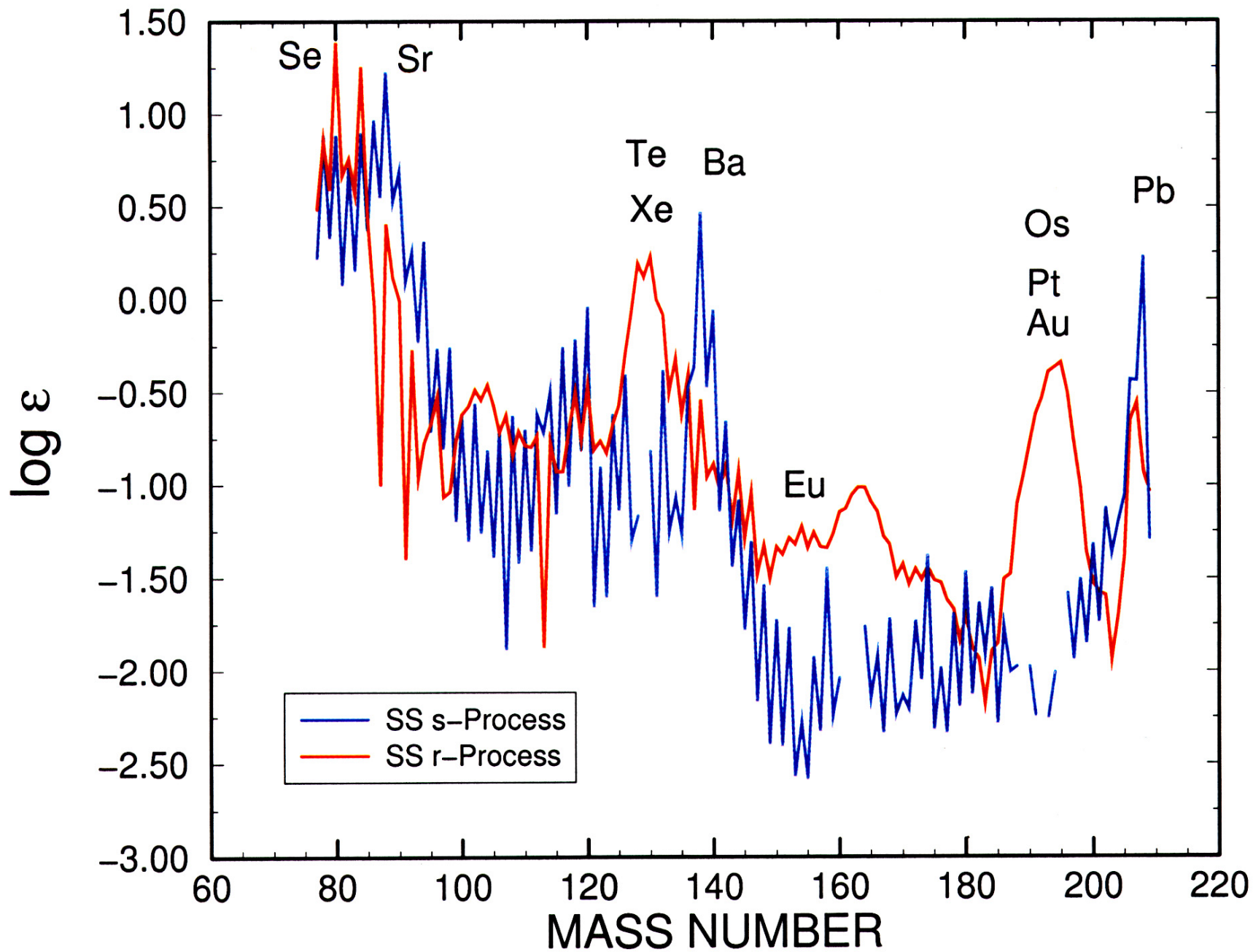


from Don Clayton's book (with modification - still a great resource)

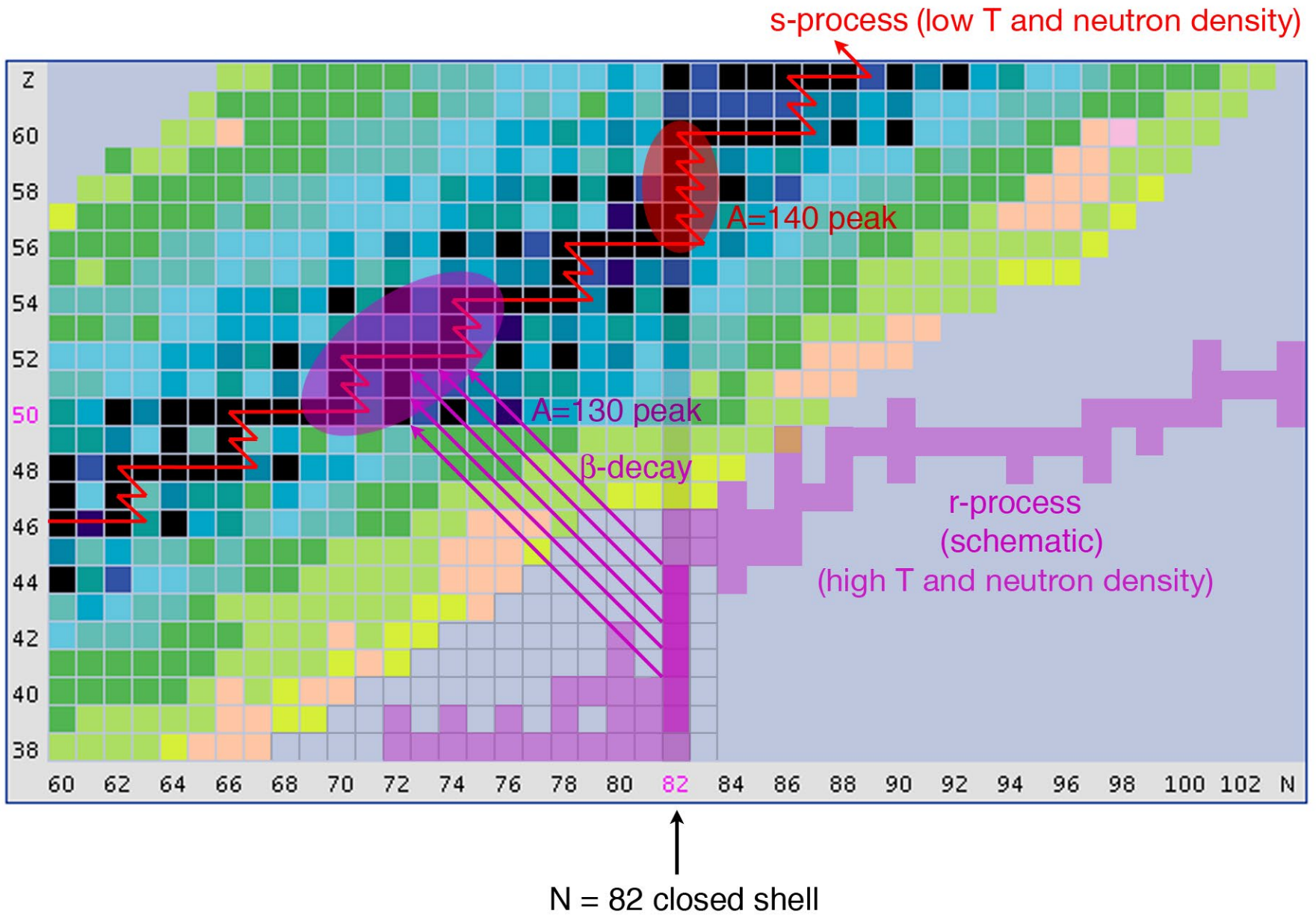
for $T_9 = 3.5$, $\rho = 10^7 \text{ g/cm}^3$ (from Iliadis)



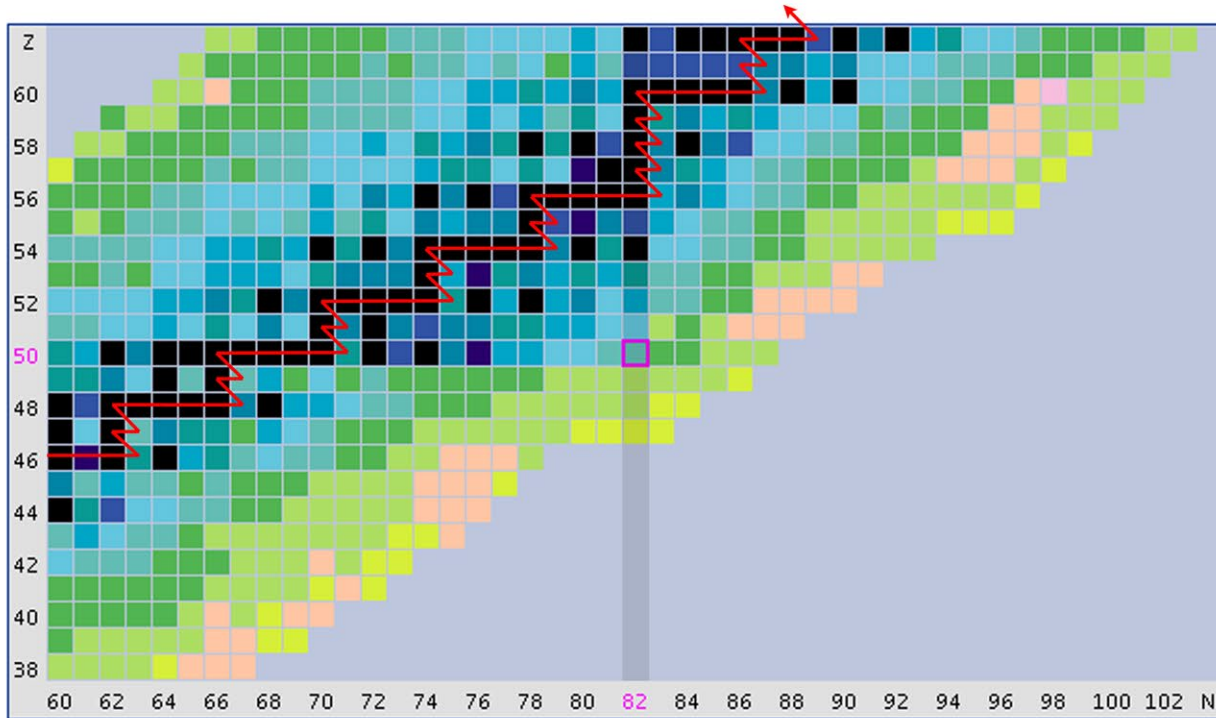
nuclei heavier than Fe



origin of the abundance peaks



The s-process: $T_9 \sim 0.08$ ($kT \sim 8$ keV), $\rho_n \sim 10^7/\text{cm}^3$, duration $\sim 2 \times 10^4$ y



some equations:
$$\frac{dN(A)}{dt} = -N_n N(A) \langle \sigma v \rangle_A + N_n N(A-1) \langle \sigma v \rangle_{A-1}$$

$$\begin{aligned} N_A \langle \sigma \rangle &\equiv \frac{N_A \langle \sigma v \rangle}{v_T} = \frac{1}{v_T} N_A \int_0^\infty v \phi(v) \sigma_n(v) dv \\ &= \frac{4}{\sqrt{\pi}} \frac{N_A}{v_T^2} \int_0^\infty v \sigma_n(v) \left(\frac{v}{v_T} \right)^2 e^{-(v/v_T)^2} dv \end{aligned}$$

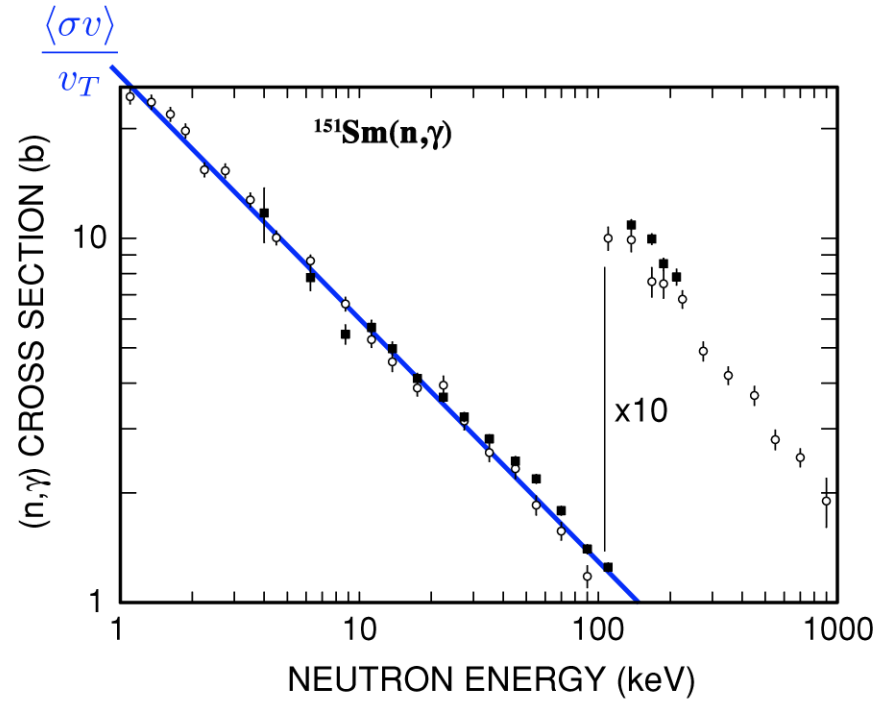
$$v_T = \sqrt{\frac{2kT}{\mu}}, \quad \mu \approx m_n$$

why do this?

low-energy, s-wave capture : $\sigma \propto P_\ell(E) = kR$ so $\sigma \propto \frac{1}{v}$

higher energies : $\sigma \propto \frac{1}{v^2}$ (s-waves); $\propto v$ (p-waves)

so $\langle \sigma v \rangle \approx \text{const.} \approx \langle \sigma \rangle v_T$



**K. Wisshak et al.,
Phys. Rev. C 73, 015802 (2006)**

$$\frac{dN(A)}{dt} = v_T N_n(t) [-N(A) \langle \sigma \rangle_A + N(A-1) \langle \sigma \rangle_{A-1}]$$

$$\text{neutron exposure } \tau = v_T \int N_n(t) dt \implies dt = \frac{d\tau}{v_T N_n(t)}$$

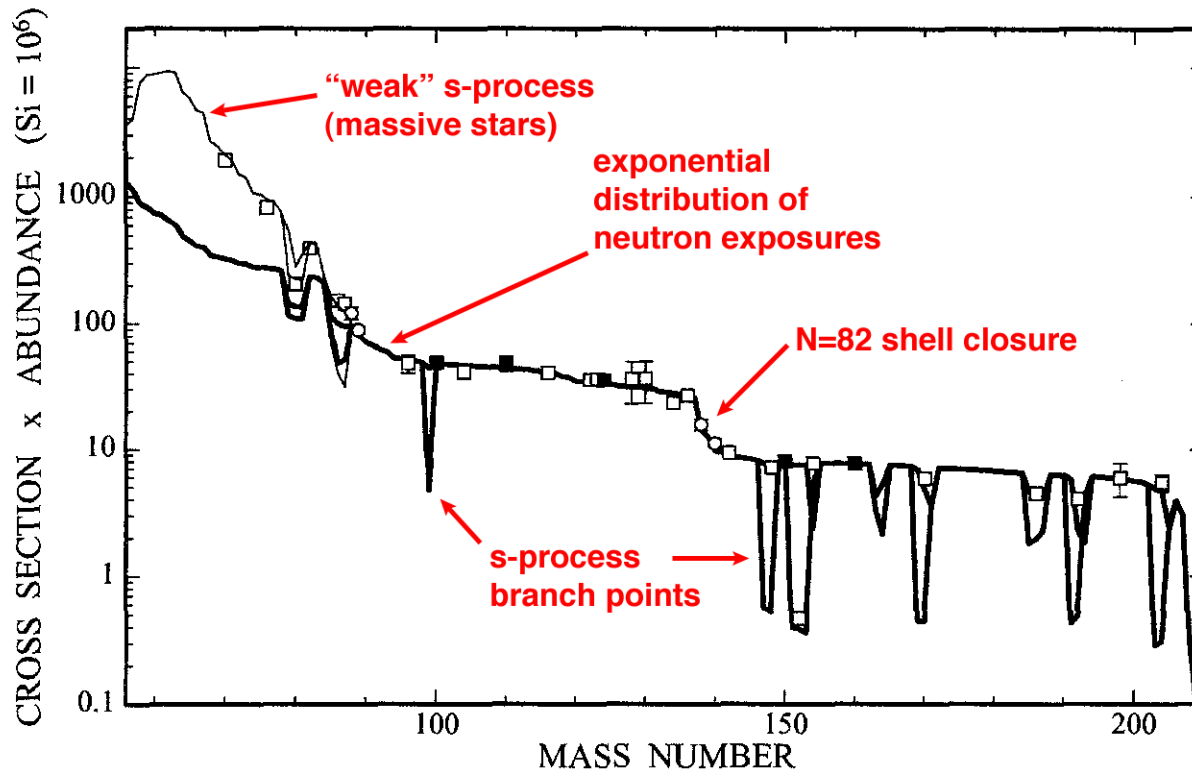
$$\text{so } \frac{dN(A, \tau)}{d\tau} = -N(A) \langle \sigma \rangle_A + N(A-1) \langle \sigma \rangle_{A-1}$$

$$\frac{dN(A, \tau)}{d\tau} = -N(A)\langle\sigma\rangle_A + N(A-1)\langle\sigma\rangle_{A-1}$$

this is a self-regulating system, i.e. for sufficiently long times:

$$\frac{dN(A, \tau)}{d\tau} \longrightarrow 0 \text{ or } N(A)\langle\sigma\rangle_A = N(A-1)\langle\sigma\rangle_{A-1}$$

”local approximation”, $N\langle\sigma\rangle \approx \text{const.}$

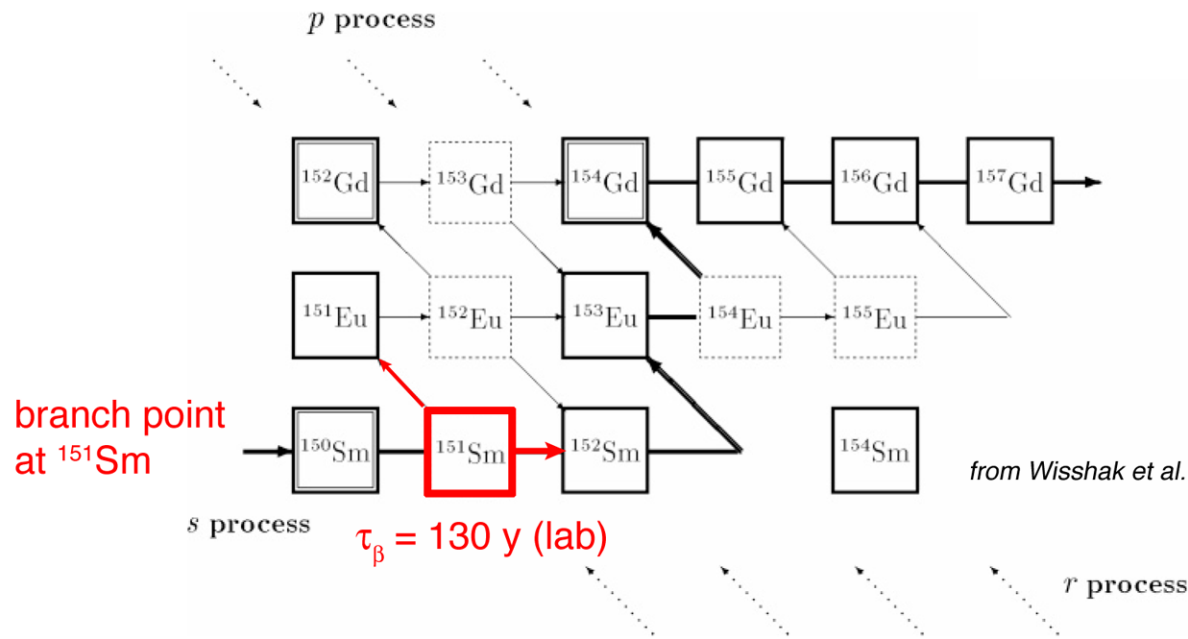


“s” implies $\tau_n < \tau_\beta$

e.g. $A = 150$,
 $kT = 8 \text{ keV}$,
 $v_T = 10^7 \text{ cm/s}$
 $\langle \sigma \rangle \sim 1 \text{ b}$

$$\langle \sigma \rangle v_T = 10^{-18} \text{ cm}^3/\text{s}$$

$$\tau_n = (N_n \langle \sigma \rangle v_T)^{-1} = 300 \text{ y}$$



β -decay (temperature dependent)
 vs.
 n-capture (depends mostly on N_n)

branch points show evidence for activation of the ^{22}Ne n-source during thermal pulses: $T_9 \sim 0.25\text{-}0.3$, $\rho_n \sim 10^{10}/\text{cm}^3$, duration of $\sim 10\text{-}20 \text{ y}$

Another reason why the s-process is interesting:

D.L. Lambert and C.A. Prieto, *Mon. Not. R. Astron. Soc.* **335**, 325 (2002)

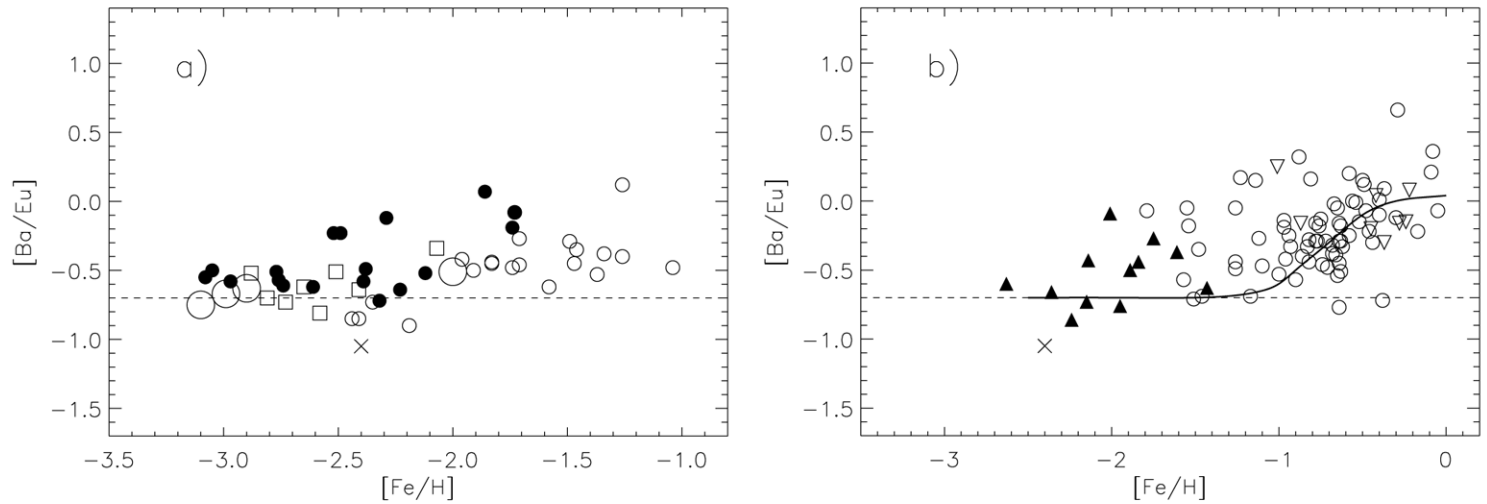
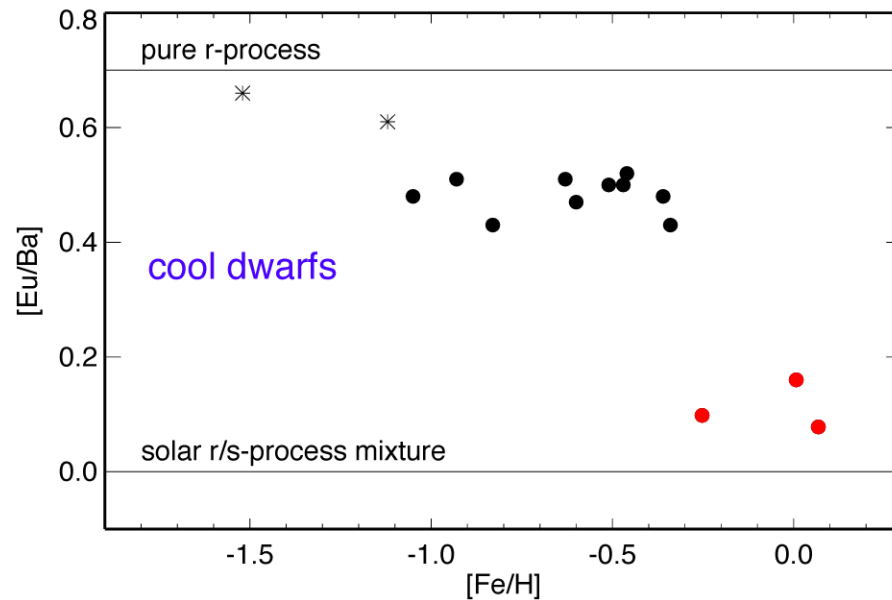
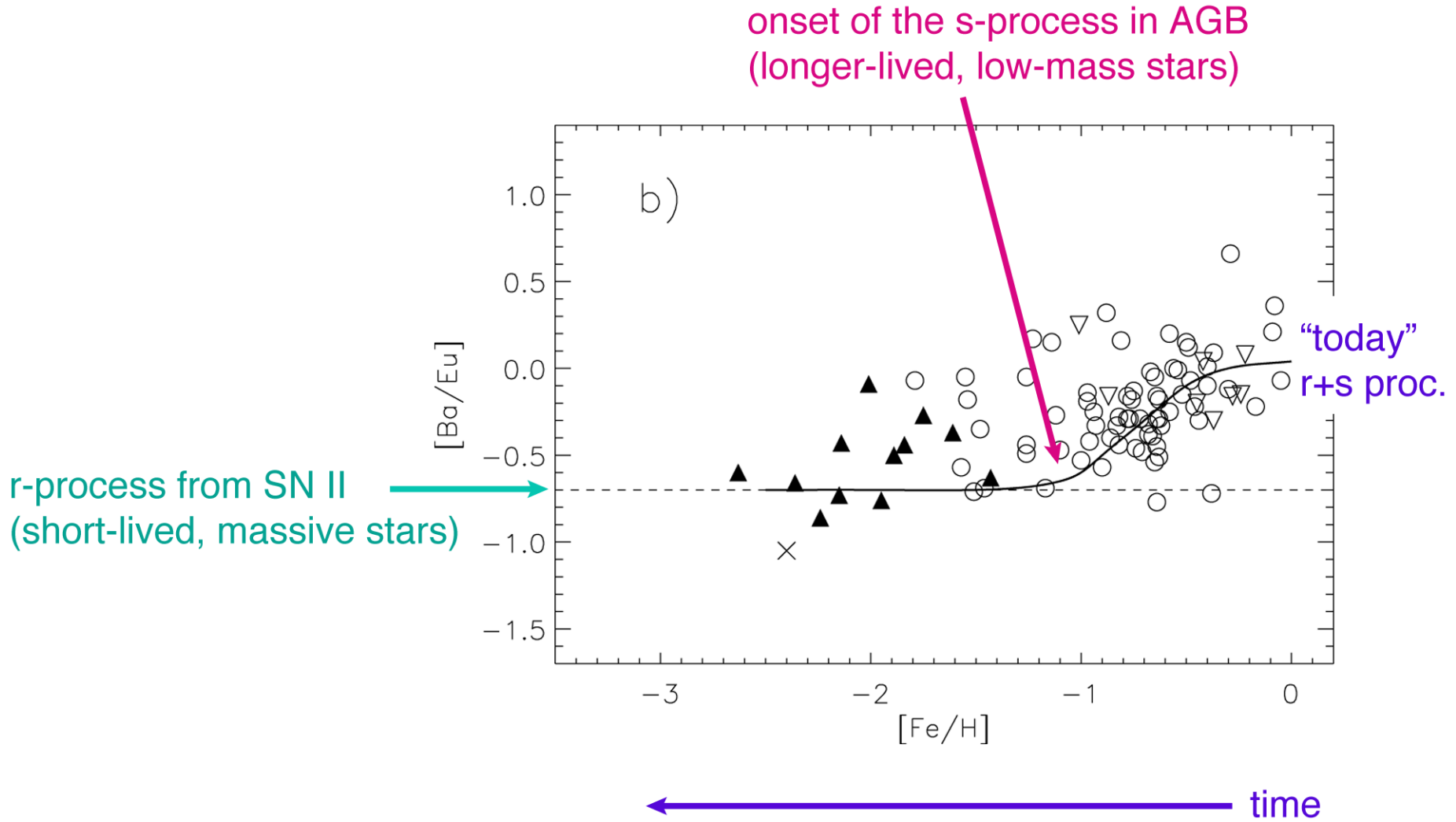


Figure 4. The abundance ratio $[Ba/Eu]$ versus $[Fe/H]$ for a representative sample of metal-poor giants (a) and dwarf/sub-giants (b). HD 140283 is identified by a cross. Symbols are as in Fig. 3 where the four severely r-process enriched giants are shown by large open circles.

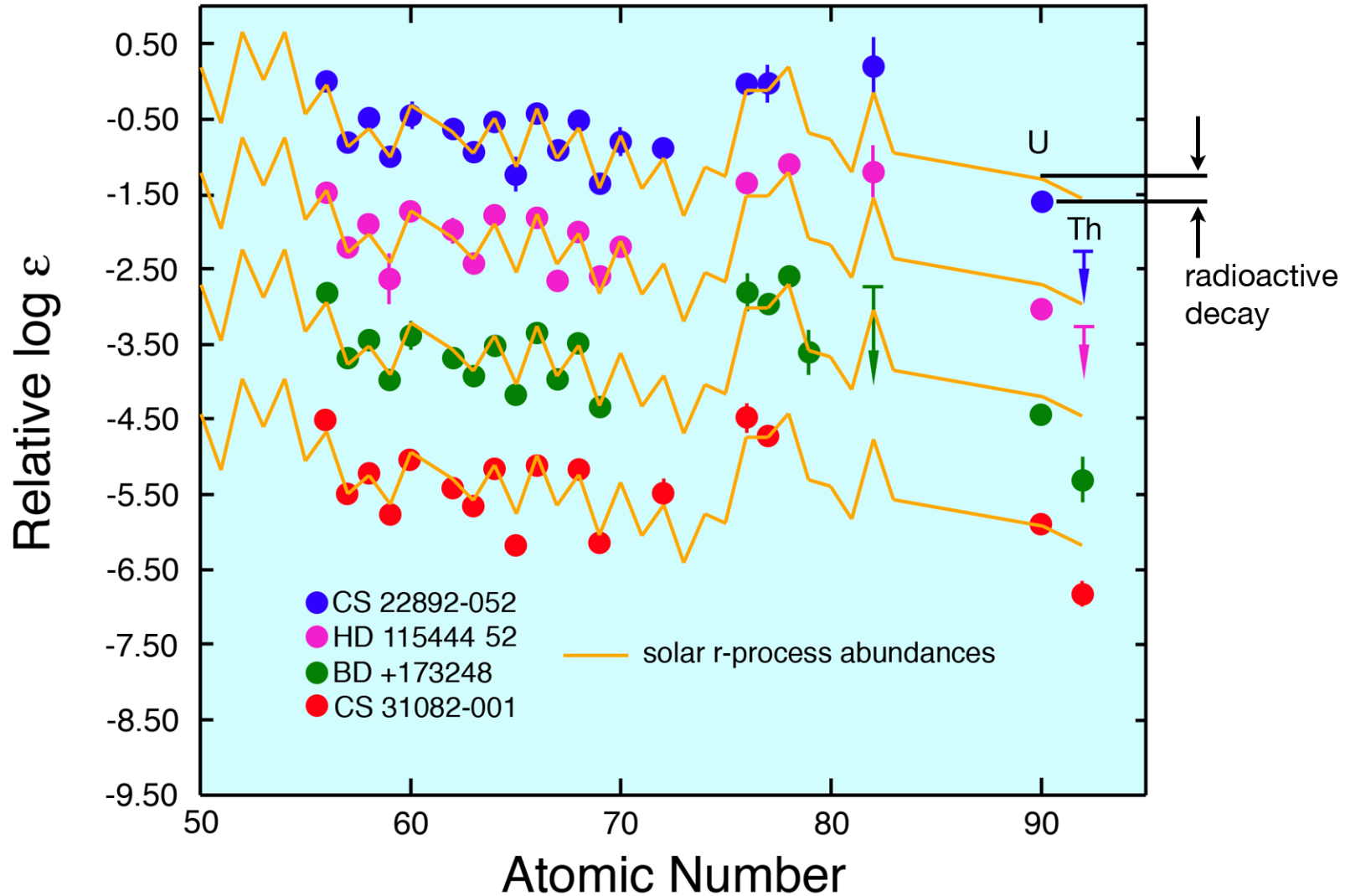


L. Mashonkina and T. Gehren,
A&A **364**, 249 (2000)

a rough interpretation



Observations of very metal-poor halo stars

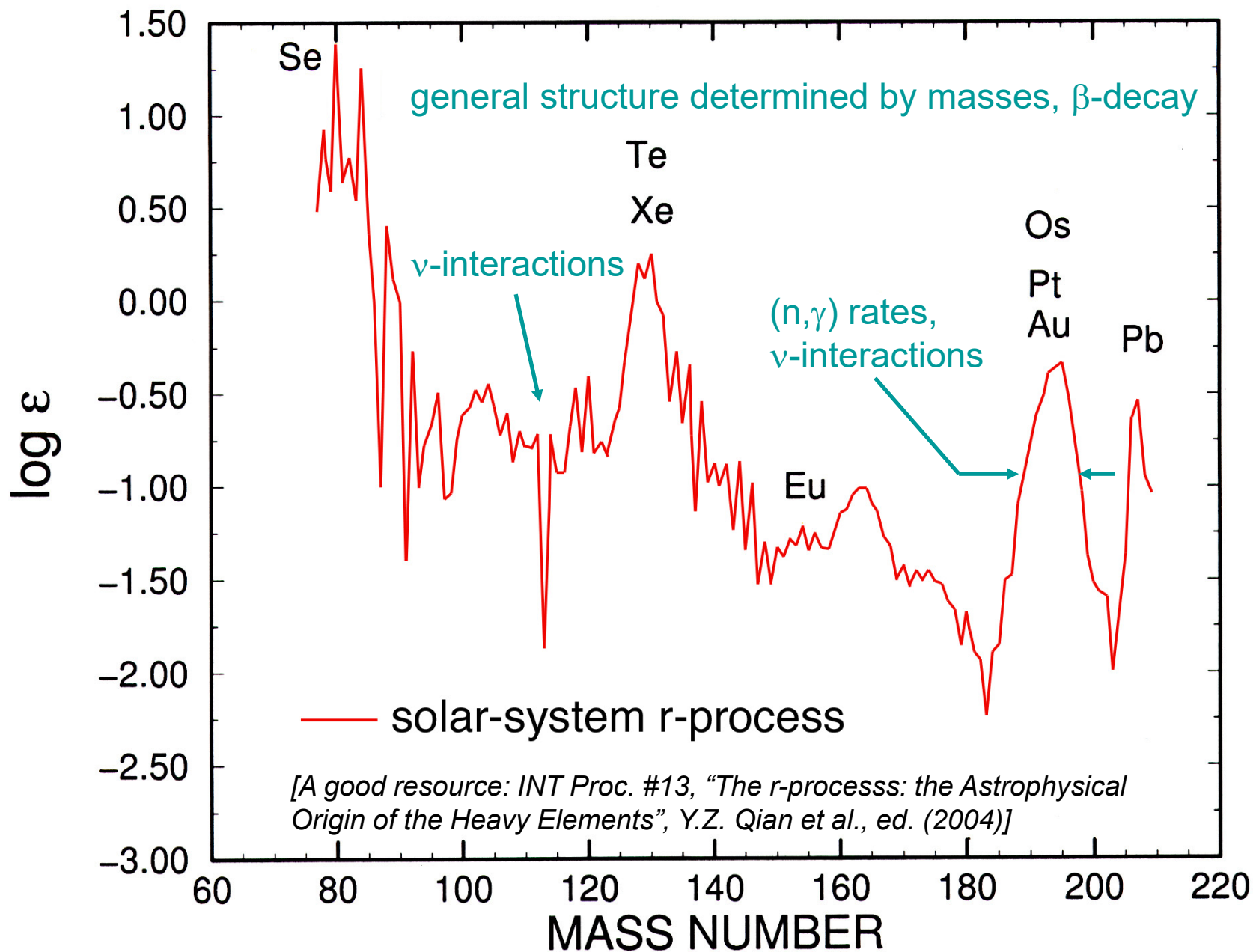


adapted from J.J. Cowan and C. Sneden

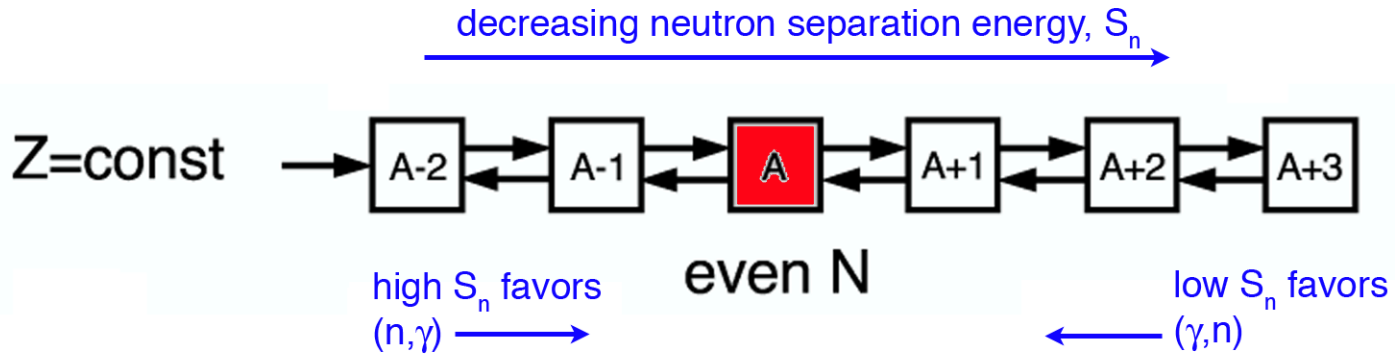
Eu-Th ages $\sim 12 - 15$ Gy

U-Th age = 14.1 ± 2.4 Gy [CS 31082-001, S. Wanajo *et al.*,
Ap. J. 593, 968 (2003)]

r-process: we need an environment with $T_9 > 1$ and $\rho_n \sim 10^{22}/\text{cm}^3$ (so $\tau_{(n,\gamma)} \sim 100$ ns)



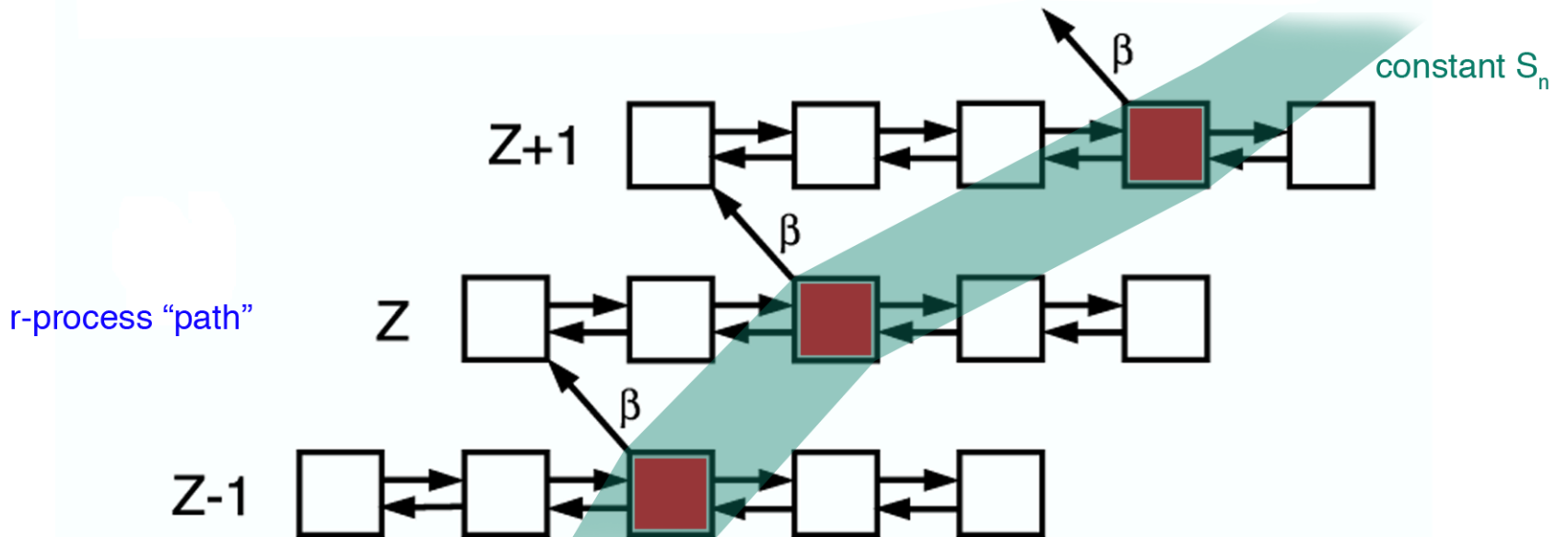
building blocks of the r-process



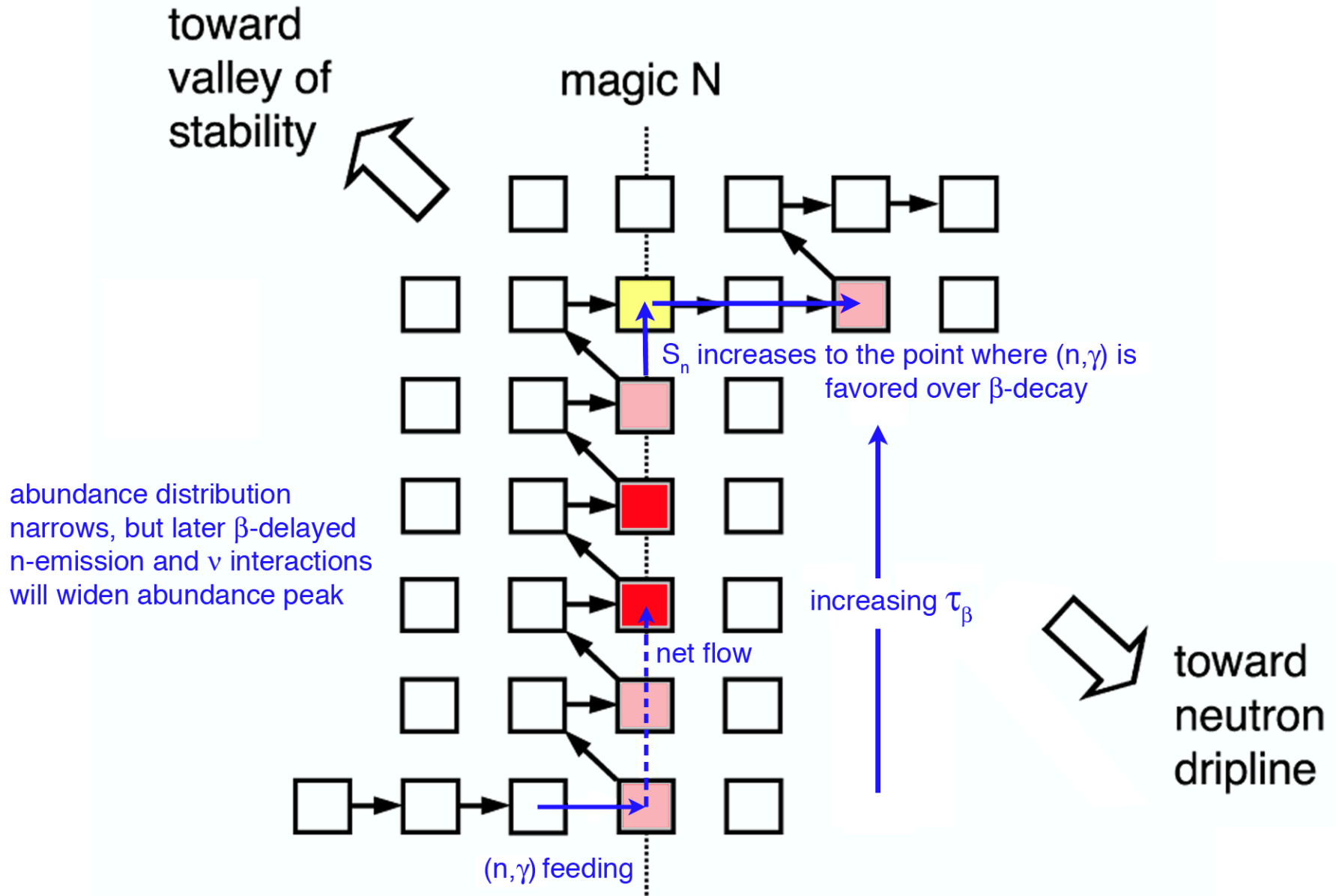
for $(n, \gamma) - (\gamma, n)$ equilibrium:

$$\frac{N(Z, A+1)}{N(Z, A)} = n_n \left(\frac{2\pi\hbar^2}{\mu_A kT} \right)^{3/2} \frac{2J_{A+1} + 1}{(2J_A + 1)(2J_n + 1)} \frac{G_{A+1}^{\text{norm}}}{G_A^{\text{norm}}} e^{S_n/kT} \quad (\text{Saha equation})$$

for $\frac{N(Z, A+1)}{N(Z, A)} = 1$: $S_n(\text{MeV}) = \frac{T_9}{11.605} [77.8 + 1.5 \ln T_9 - \ln n_n(\text{cm}^{-3})] \simeq 3 \text{ MeV}$



at the closed neutron shells:

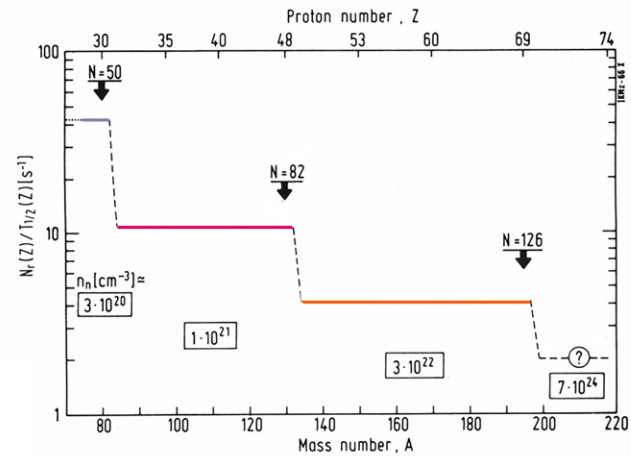


mass flow between isotopic chains: $\frac{dN_Z}{dt} = -\lambda_{\beta(Z)}N_Z + \lambda_{\beta(Z-1)}N_{Z-1}$

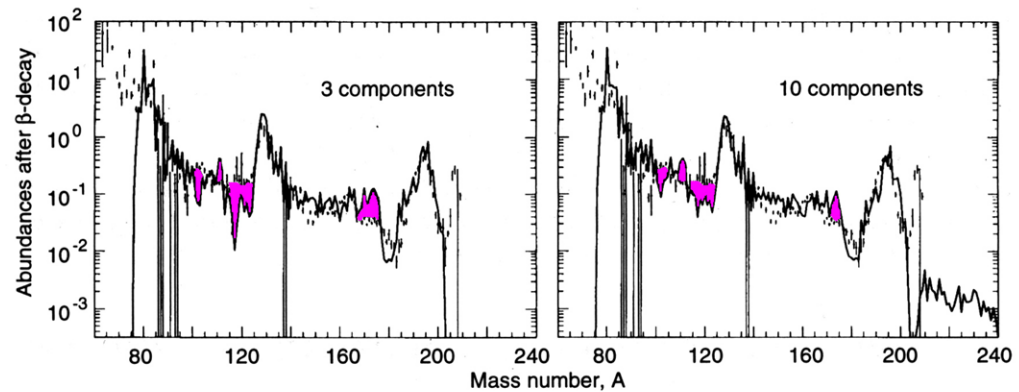
which evolves to $\frac{dN_Z}{dt} = 0 \rightarrow \lambda_{\beta(Z)}N_Z \approx \lambda_{\beta(Z-1)}N_{Z-1}$ or $\lambda_{\beta(Z)}N_Z = \text{const.}$

(“steady flow approx.”)

best-fit parameters for steady flow
[K.L. Kratz et al.]

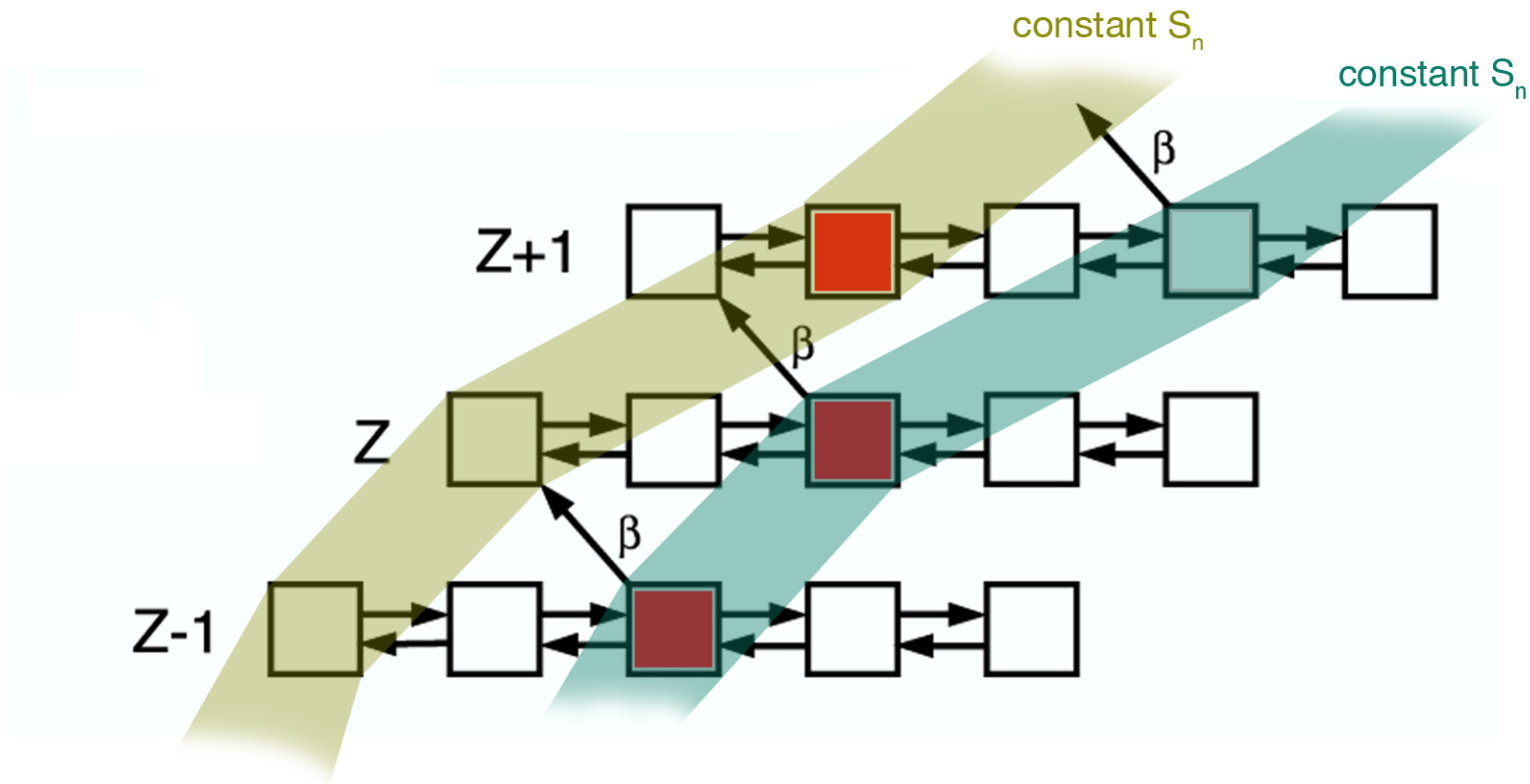


but note mid-shell problems -
nuclear physics or astrophysics?



freezeout:

as T, n_n go down, equilibrium shifts to higher S_n , i.e. β -decay goes to higher S_n and (n, γ) cannot push out to lower S_n so a new equilibrium is established at higher S_n and the flow moves closer to stability



finally, equilibrium breaks down and $\tau_n > \tau_\beta \longrightarrow \beta$ -decay to stability

recap:

Nucleosynthesis in the r-process

JINA

Joint Institute for Nuclear Astrophysics 2002

Movie : H. Schatz, T. Elliot
NSCL, Michigan State University

Calculation : K. Vaughan, J.L. Galache,
and A. Aprahamian, University of Notre Dame

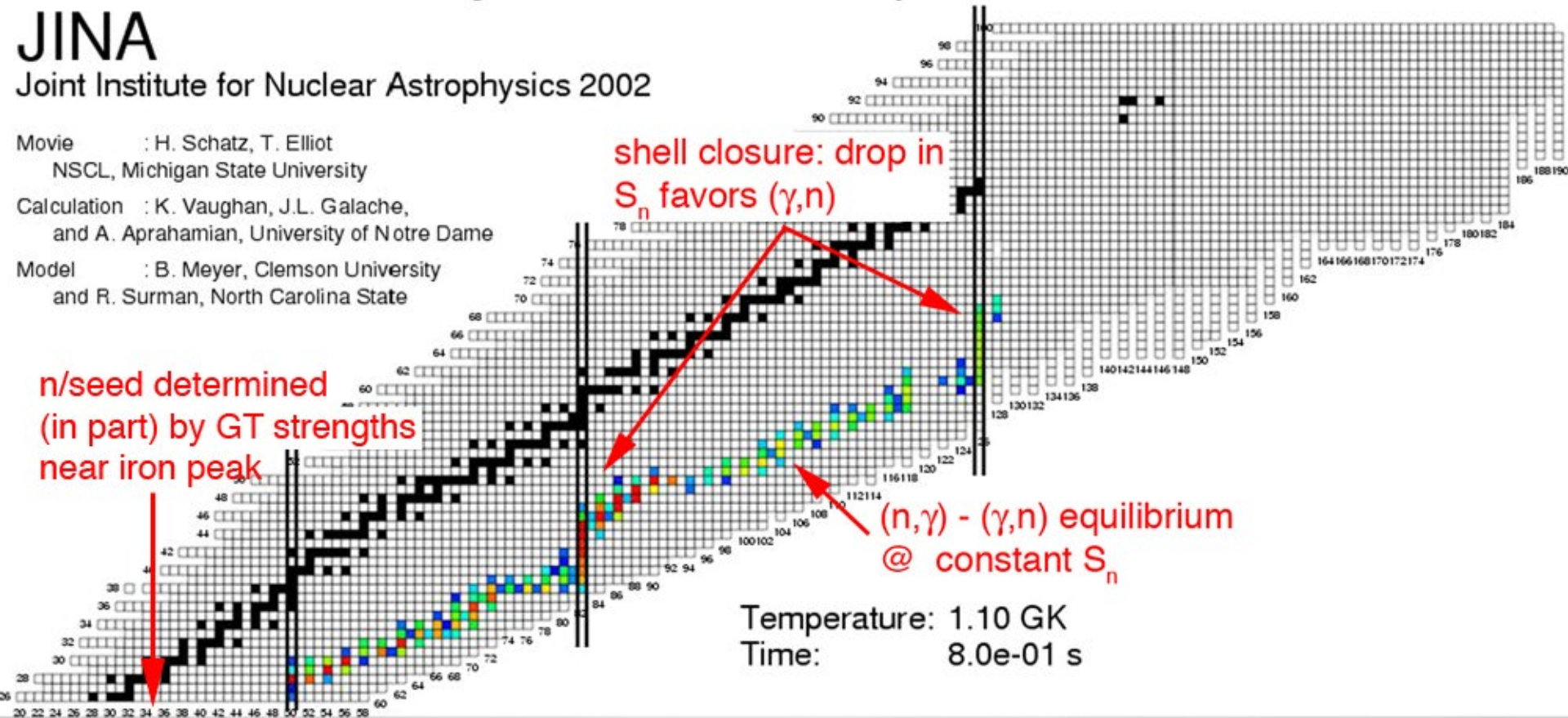
Model : B. Meyer, Clemson University
and R. Surman, North Carolina State

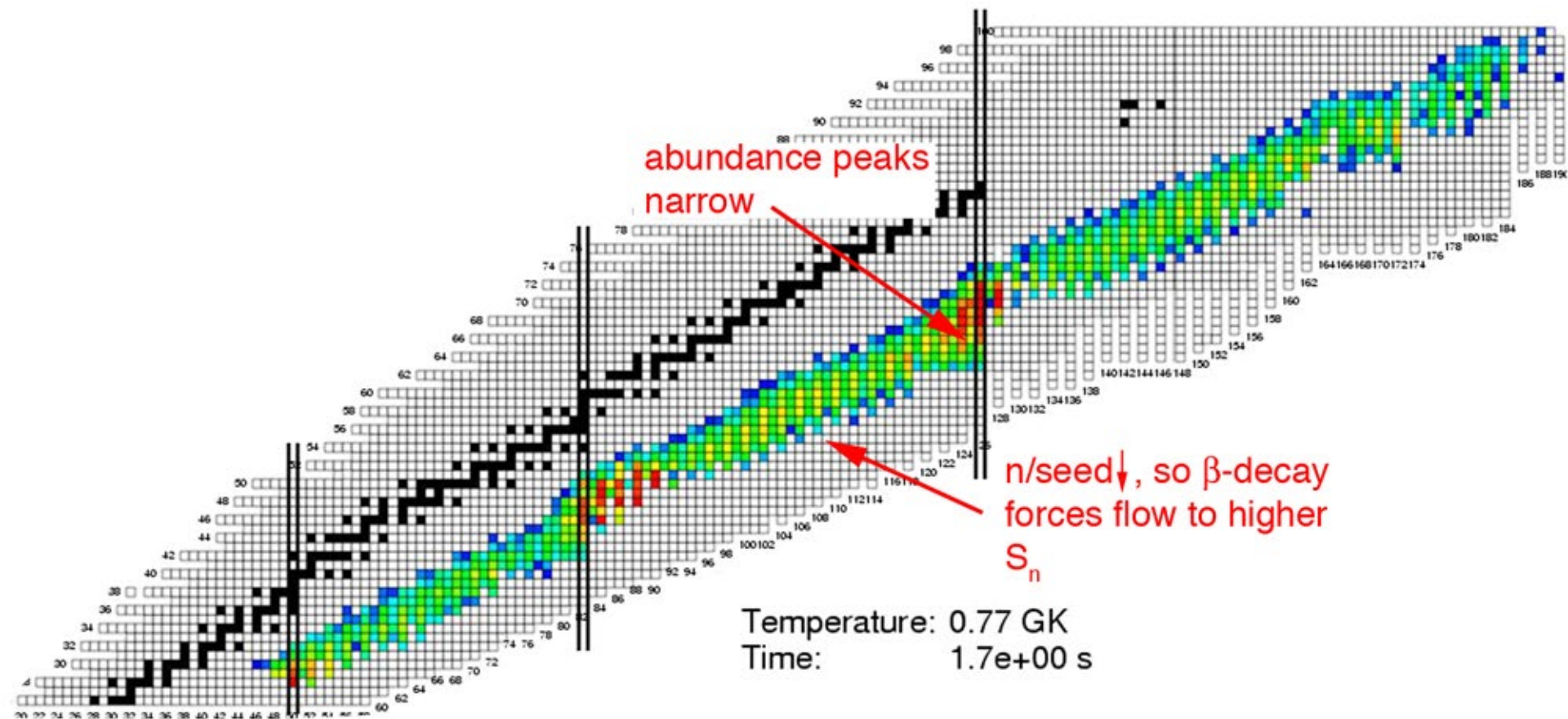
n/seed determined
(in part) by GT strengths
near iron peak

shell closure: drop in
 S_n favors (γ, n)

$(n, \gamma) - (\gamma, n)$ equilibrium
@ constant S_n

Temperature: 1.10 GK
Time: 8.0e-01 s

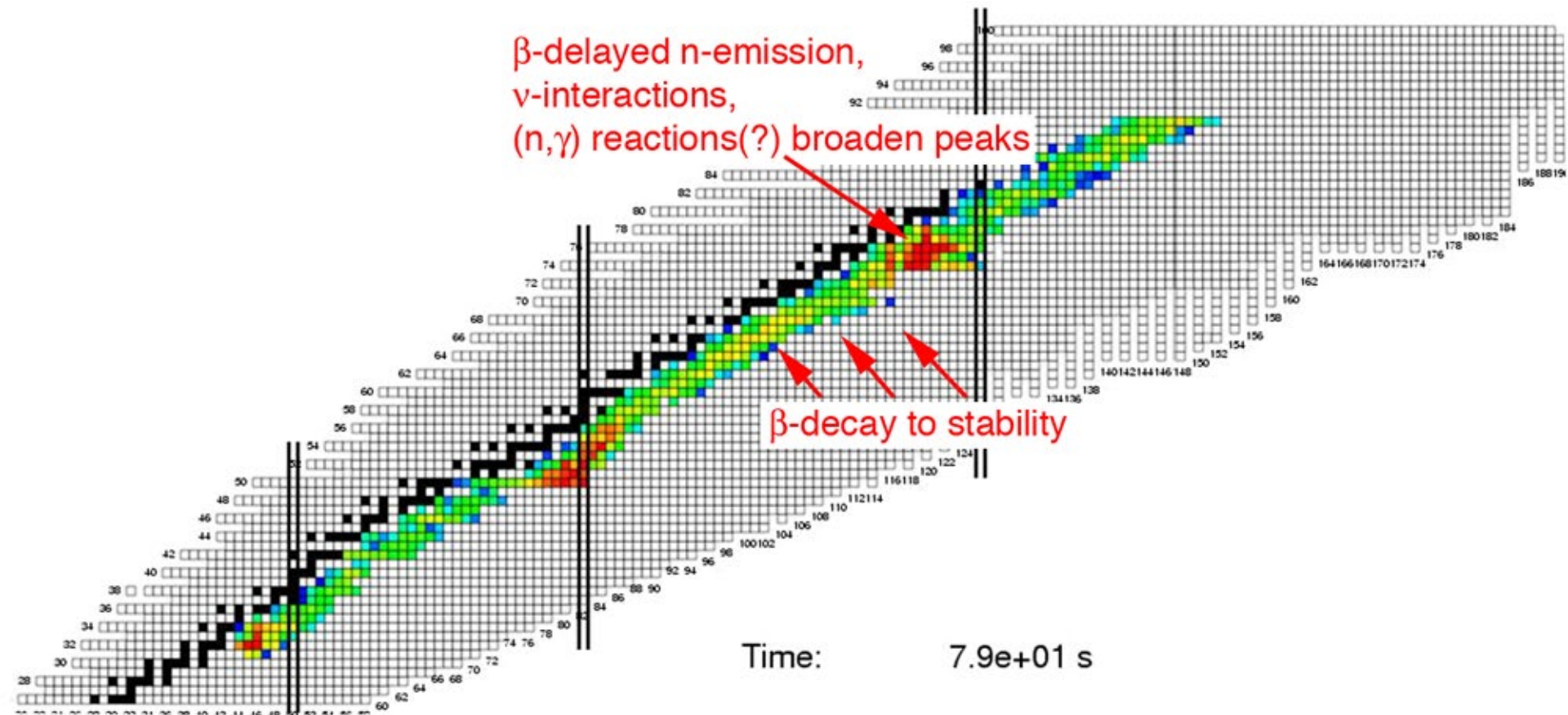




β -delayed n-emission,
 ν -interactions,
(n, γ) reactions(?) broaden peaks

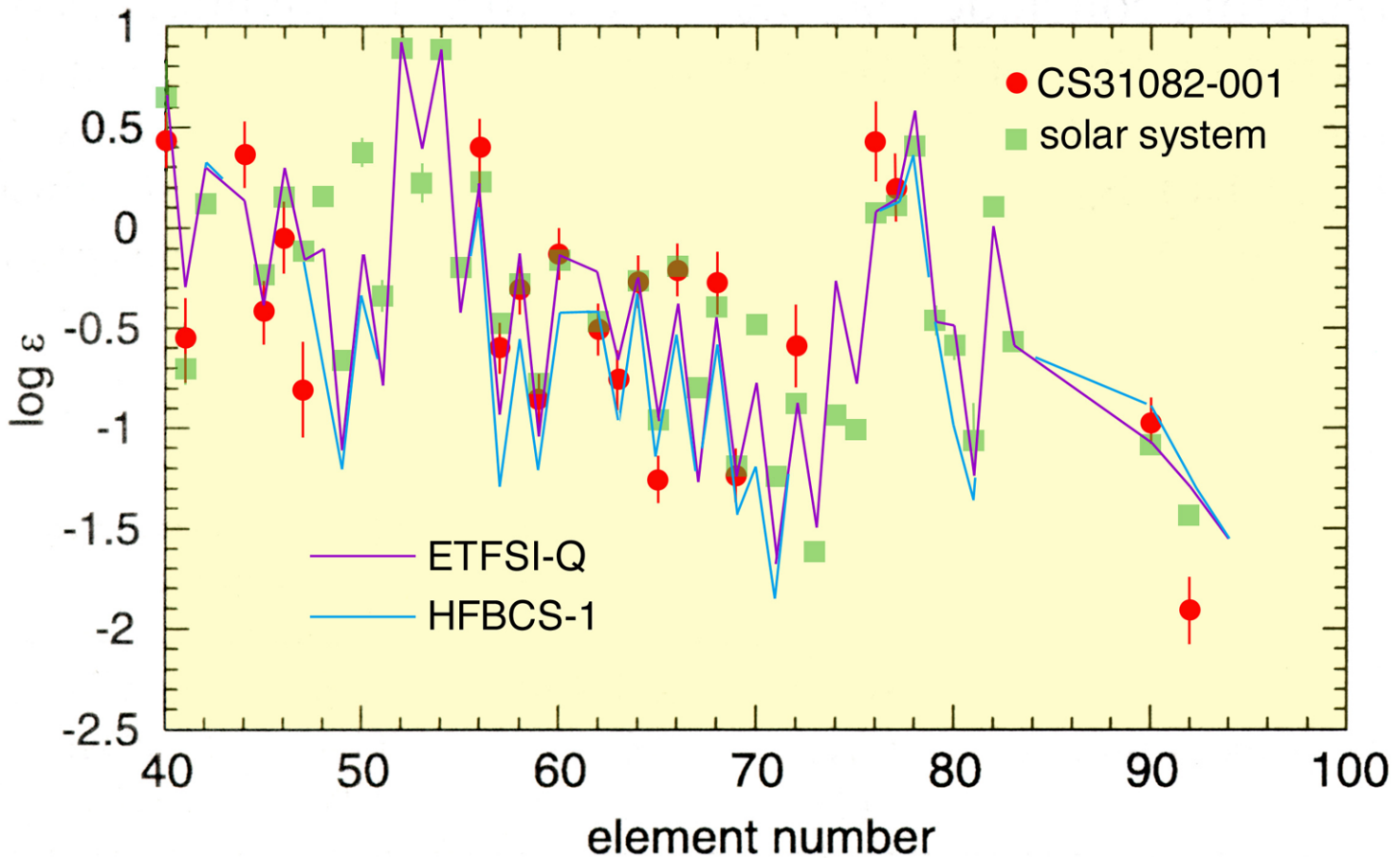
β -decay to stability

Time: 7.9e+01 s



So far, this is entirely schematic *and* there's been no mention of where this might occur. However, if we want to say something about ages or astrophysics from the abundances, then the nuclear input has to be correct:

For example, calculations with 2 different mass models (which predict S_n and τ_β):



H. Schatz et al. Ap. J. 579, 626 (2002)

mass models

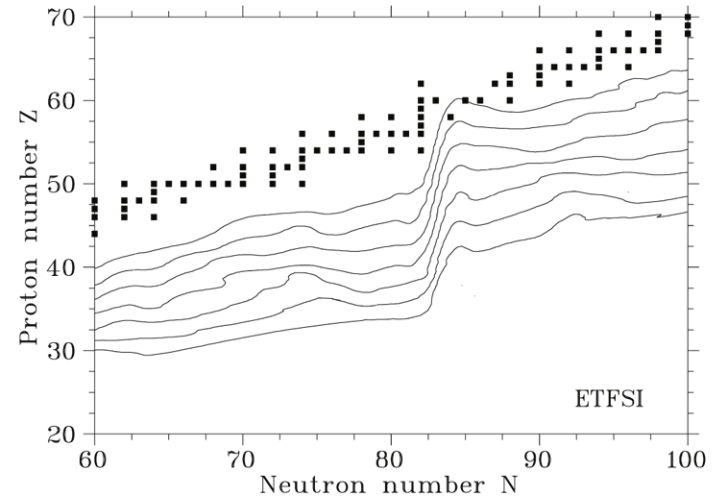
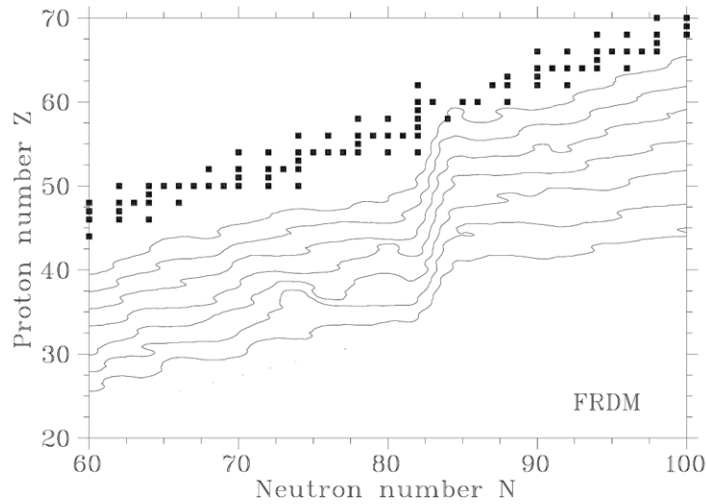
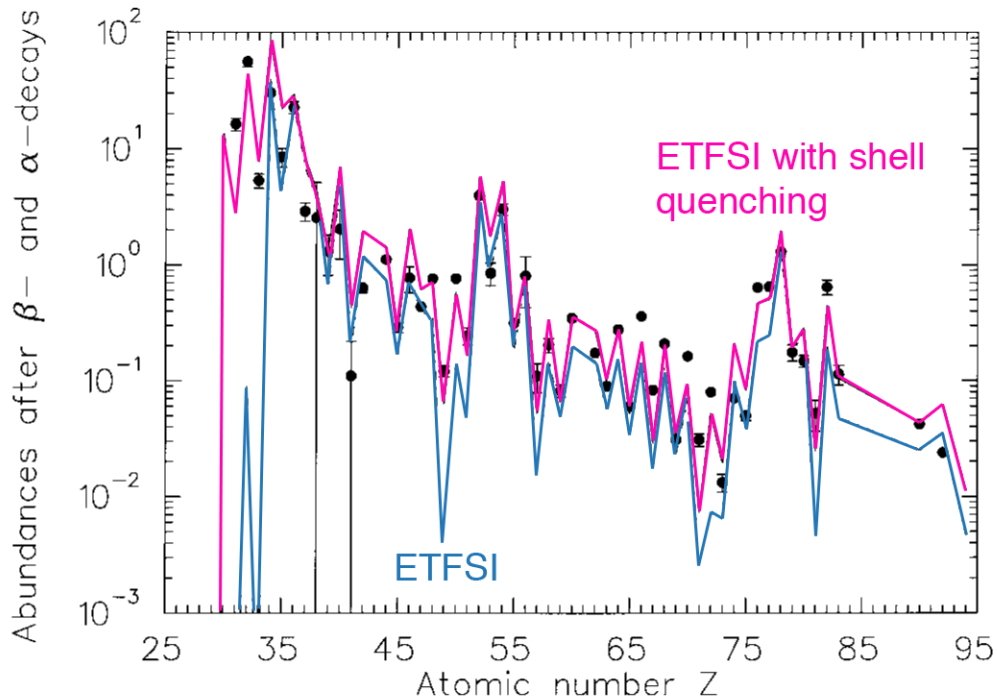


FIG. 1.—Contour plots of constant neutron separation energies in the $80 \leq A \leq 140$ mass region for the FRDM mass model (Möller et al. 1995) and the ETFSI mass model (Aboussir et al. 1995) at $S_n = 1, 2, 3, \dots, 7$ MeV for even- N isotopes. The saddle point behavior before the shell closure at $N = 82$, causes the deep trough before the peak at $A = 130$ (see upper part of Fig. 3) as the step from the abundance maximum of an isotopic chain Z to $Z + 1$ can cause a large jump in N or equivalently A , leading to a large number of unpopulated mass numbers A .

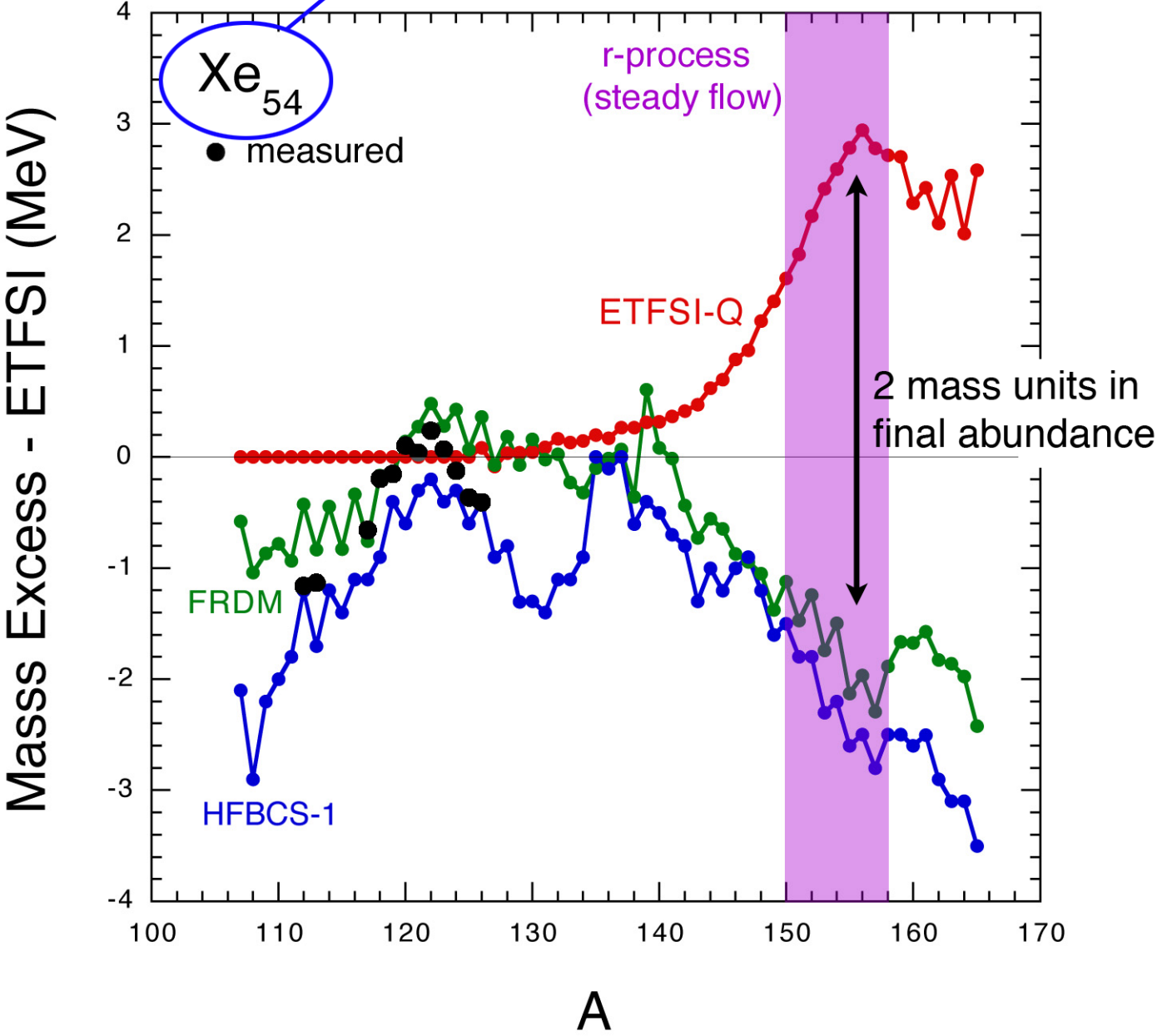


[reducing the shell gap slows (n, γ) vs. (γ, n) and increases τ_{β} , both of which impede flow out of mid-shell region]

[C. Freiburghaus et al. *Ap. J.* **516**, 381 (1999)]

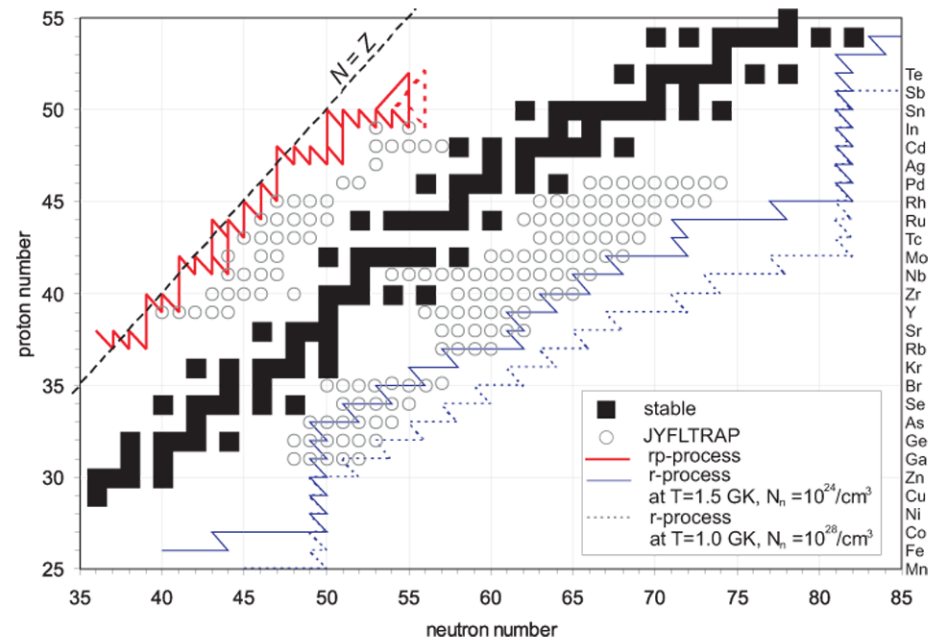
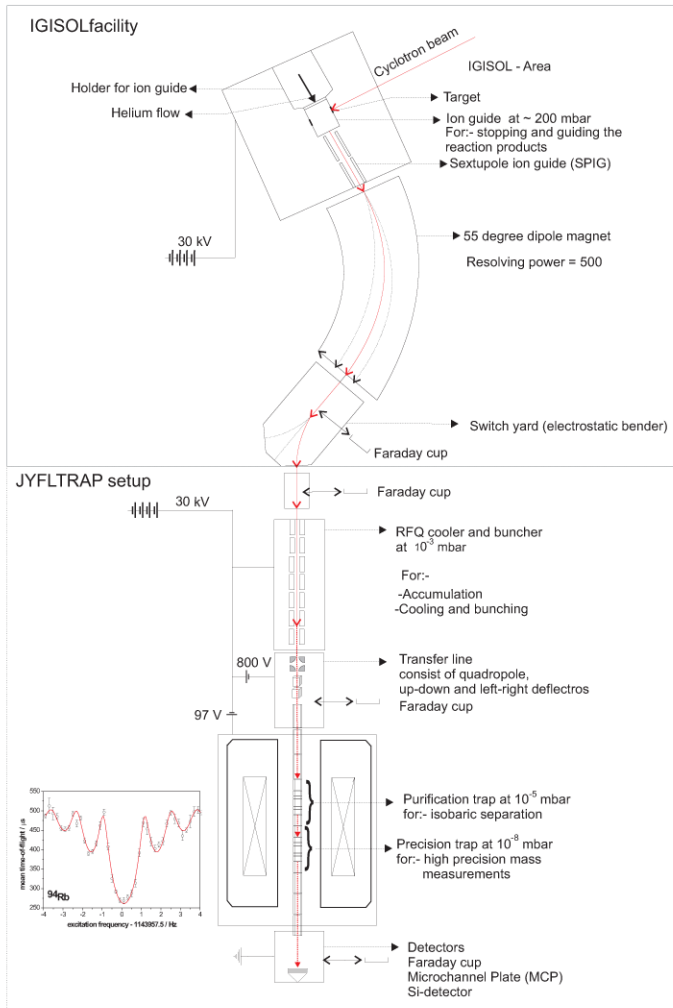
a fairly typical situation:

leads to Eu

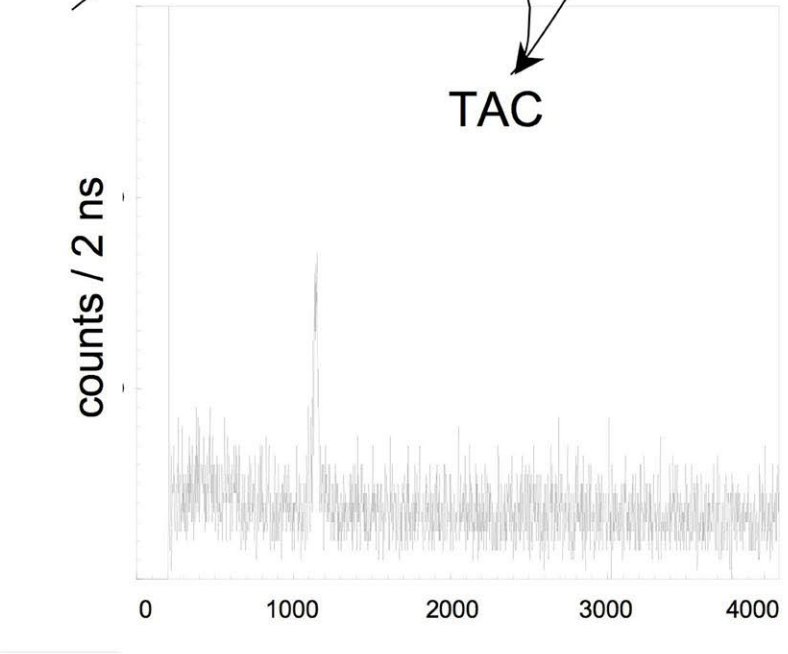
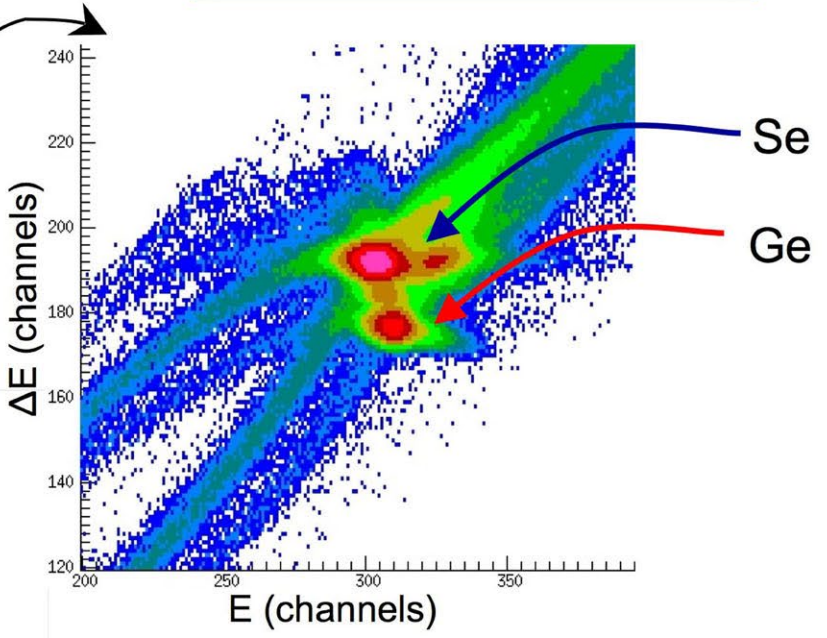
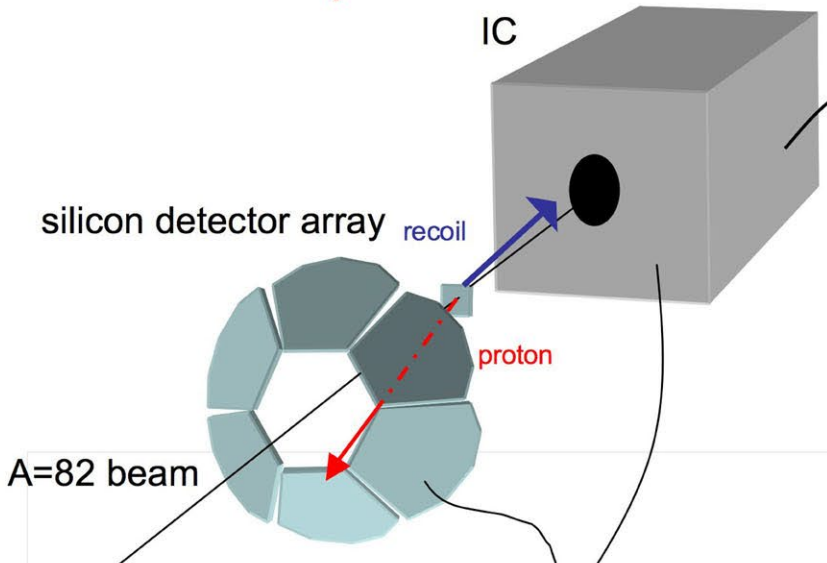


mass measurements of neutron-rich nuclei

[this example from S. Rahaman *et al.*, EPJ Special Topics, 150, 349 (2007)]

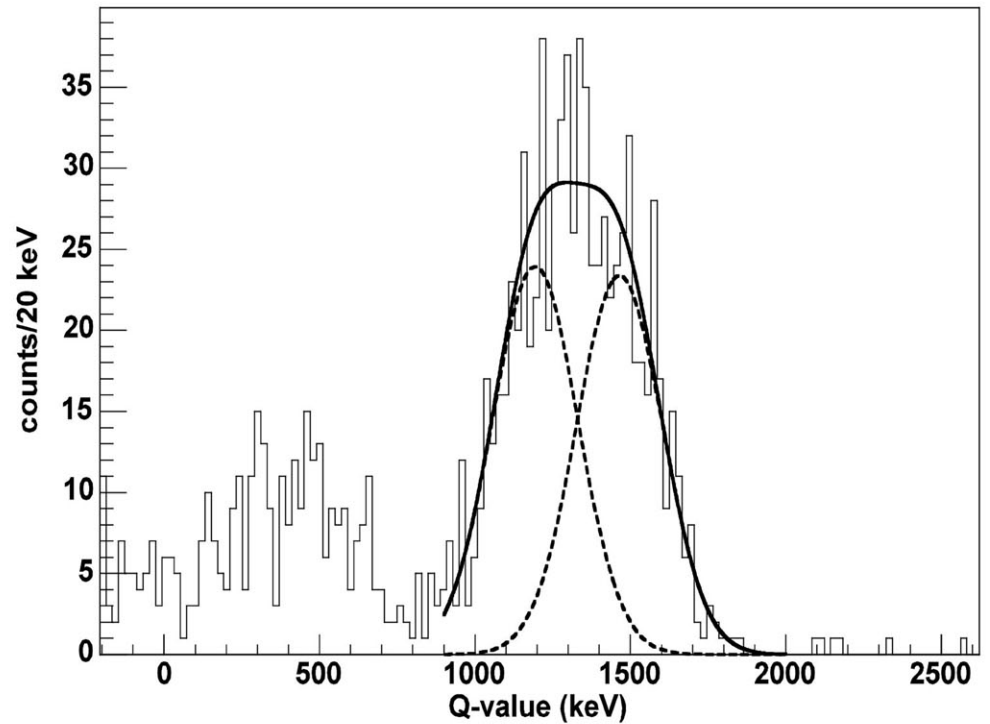
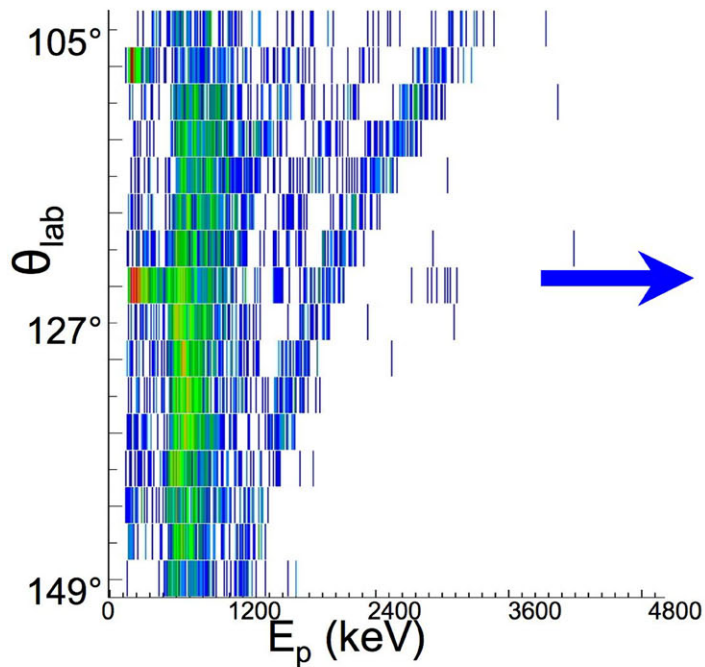


into the N = 50 peak



TAC

$E_{\text{beam}} = 330 \text{ MeV (4 MeV/u)}$
 $430 \mu\text{g/cm}^2 \text{ CD}_2 \text{ target}$
 Ionization chamber at $\theta_{\text{lab}} = 0^\circ$ filled with CF_4
 SIDAR in lampshade configuration covering $\theta_{\text{lab}} = 105^\circ\text{-}150^\circ$
 coincidence timing between IC and SIDAR

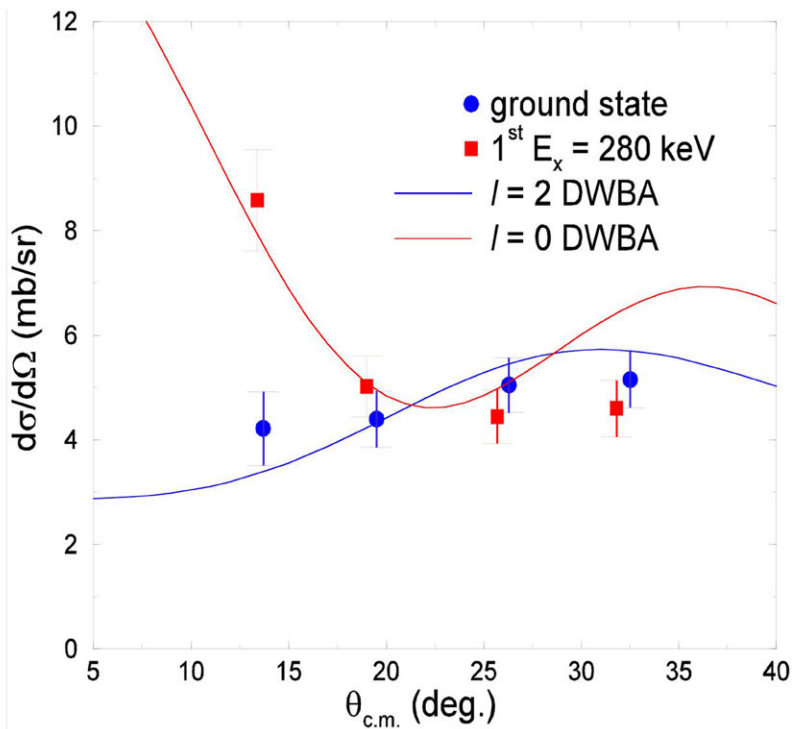


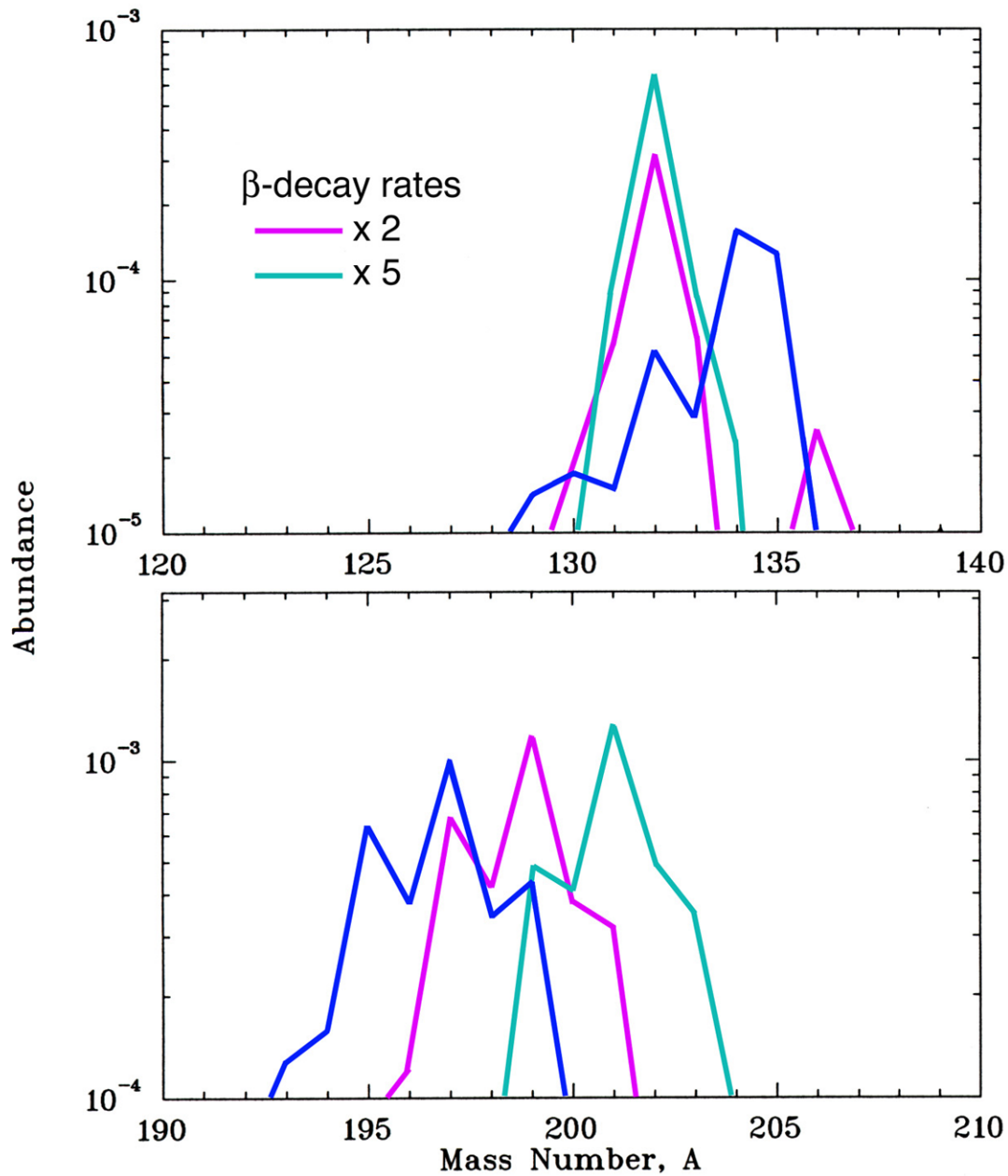
$Q = 1.47 (\pm 0.02 \text{ stat.}, \pm 0.07 \text{ sys.}) \text{ MeV}$

$1^{\text{st}} E_x = 280 (\pm 20 \text{ stat.}) \text{ keV}$

$S_n(^{83}\text{Ge}) = 3.69 \pm 0.07 \text{ MeV}$

$\Delta(^{83}\text{Ge}) = -61.25 \pm 0.26 \text{ MeV}$

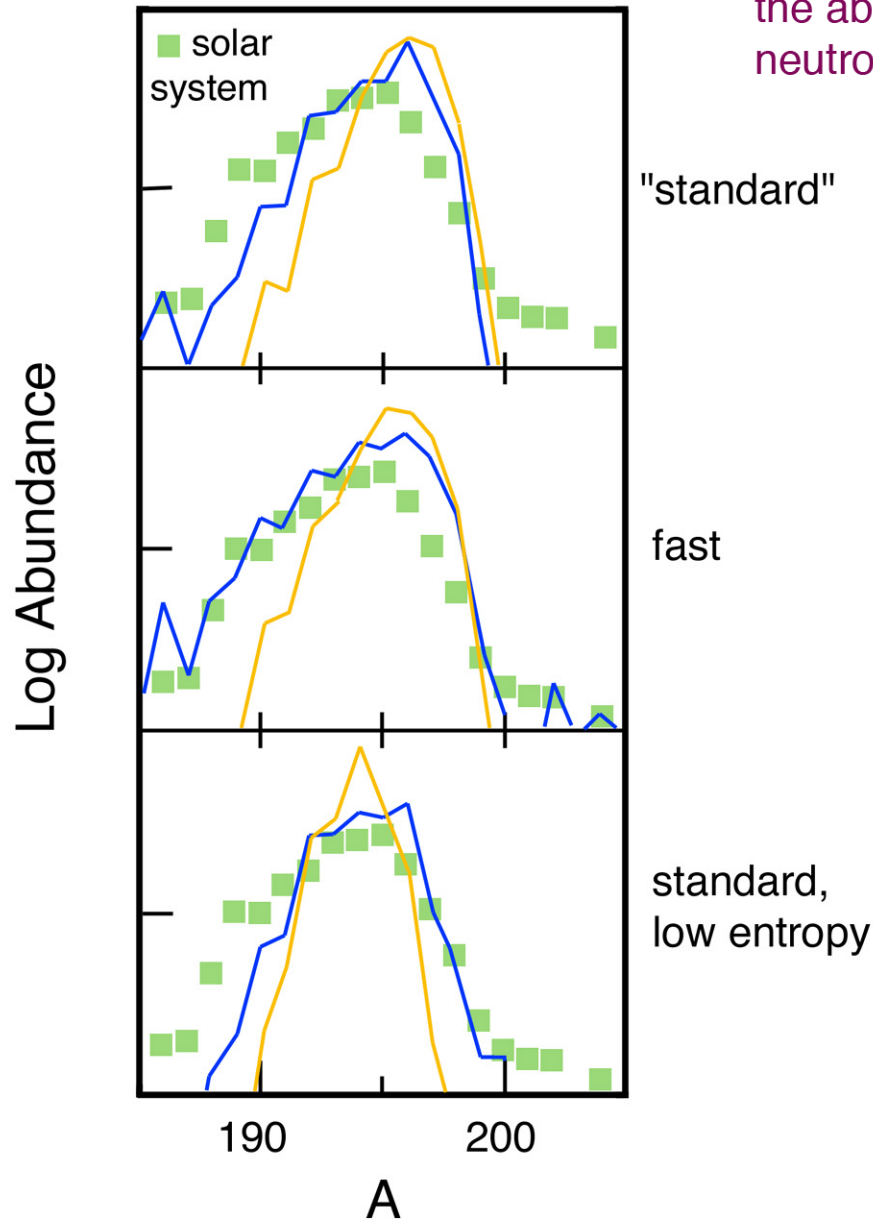




here material moves into N=82 region faster and abundances shift to lower Z

(later on)
 β -decay removes neutrons so freezeout occurs at higher T (lower S_n)

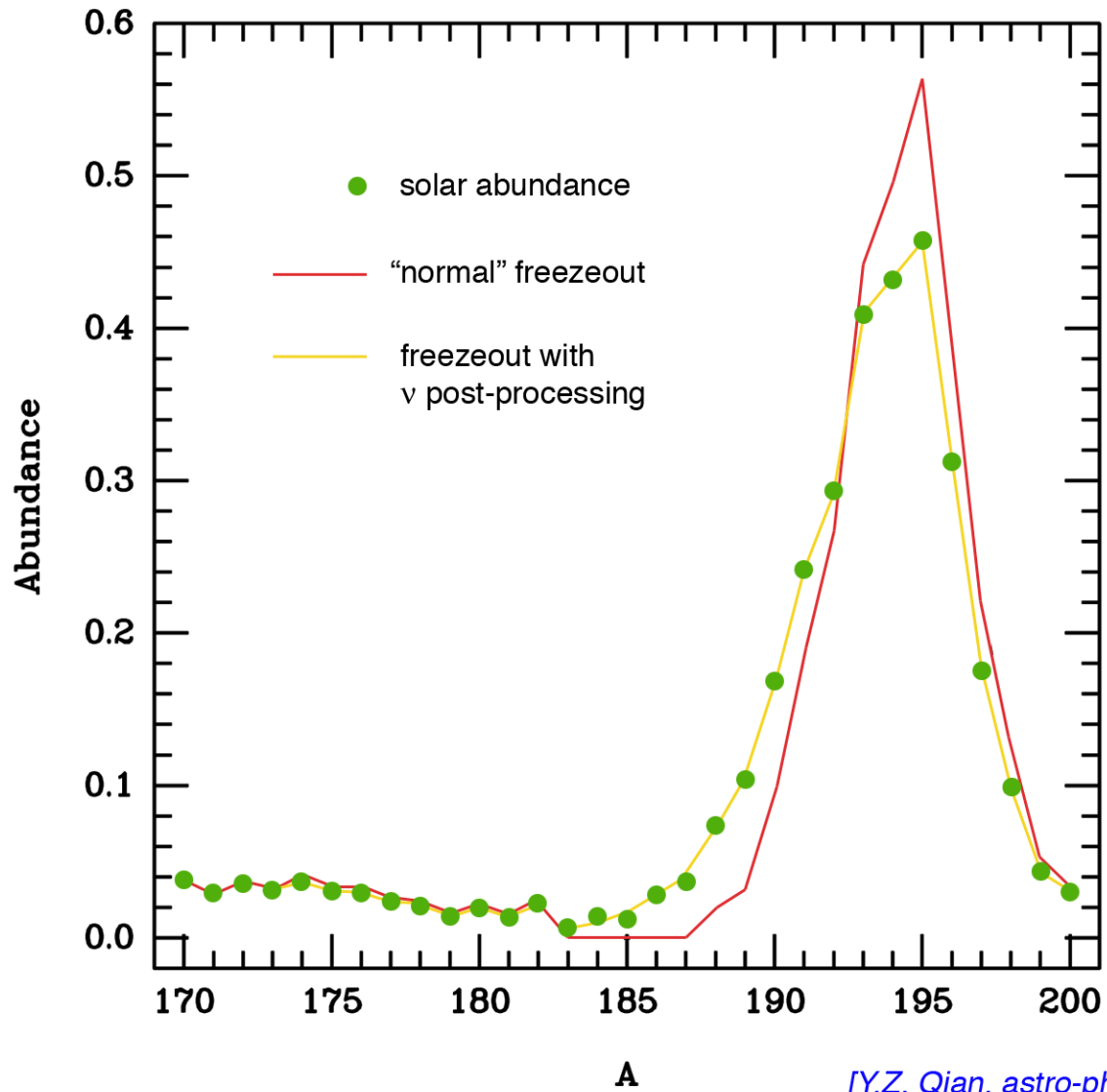
Effect of n-capture rates



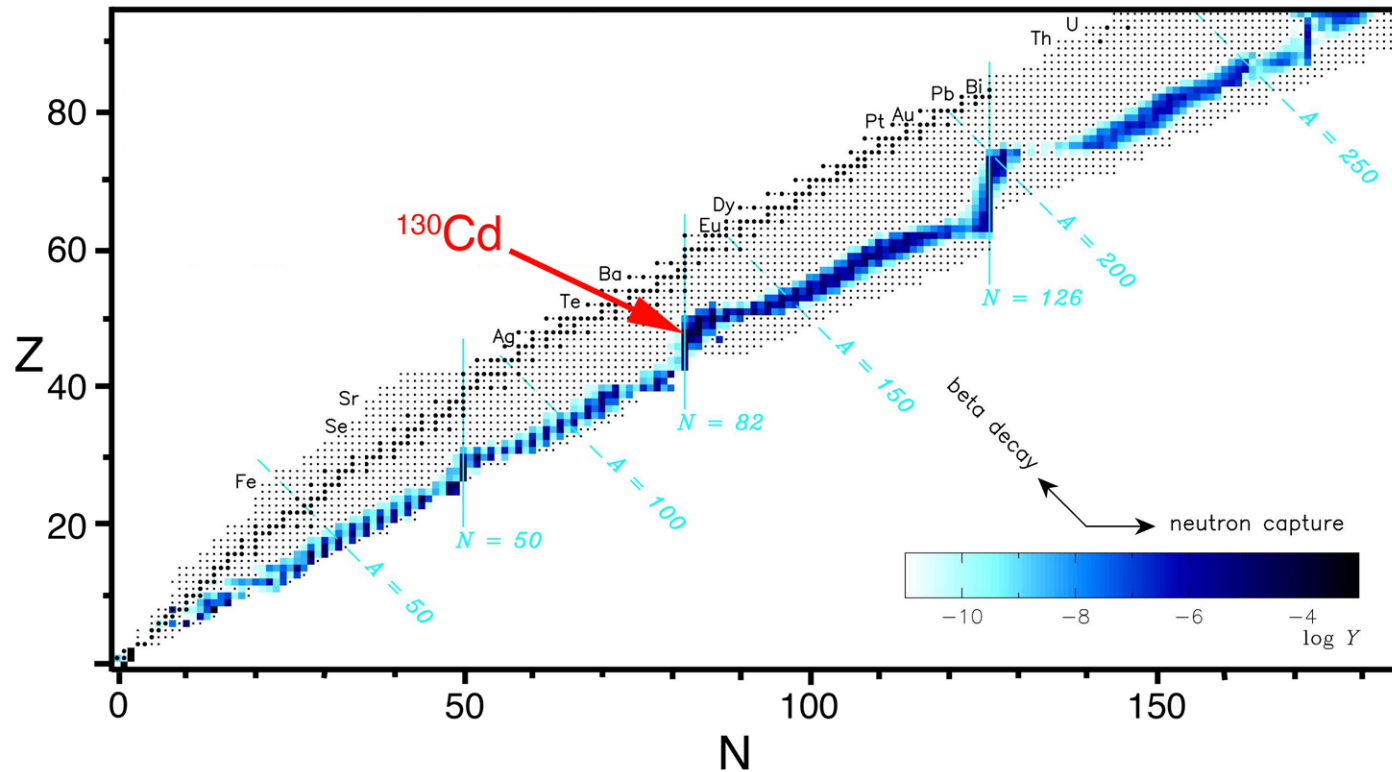
neutron capture can influence the morphology of the abundance peaks, particularly if there are free neutrons at freezeout

(note that this looks similar to what we saw for β -decay rates - it's very difficult to isolate a single "critical" effect!)

other effects, e.g. late-time (ν, n) reactions



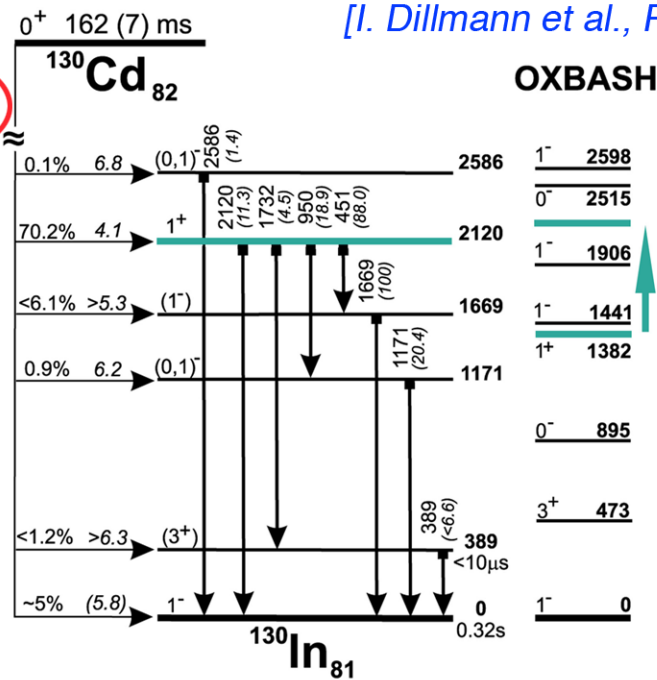
But...



[I. Dillmann et al., Phys. Rev. Lett. 91, 162503 (2003)]

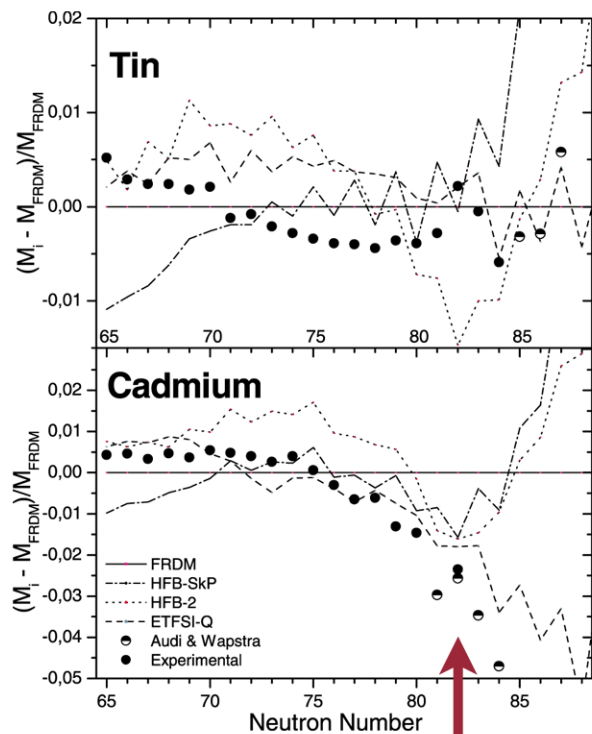
$Q_\beta = 8.34 \text{ MeV}$

higher than expected,
(consistent with shell
quenching)

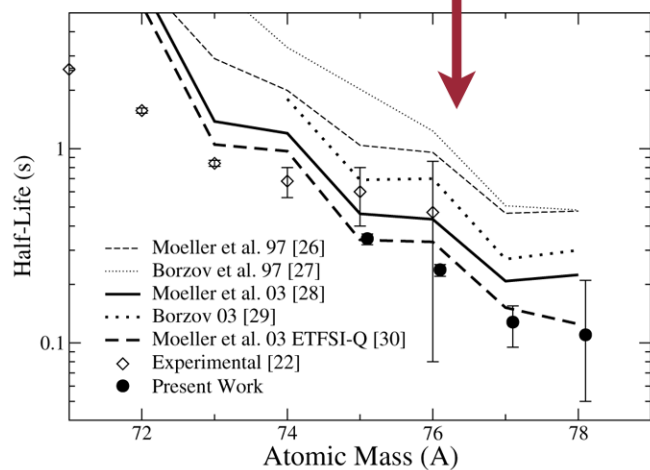


reduce two-body
matrix element
(B.A. Brown)

$\pi g_{9/2} \times \nu g_{7/2}$ GT resonance
 must reduce p-n
 $g_{9/2} g_{7/2} \longleftrightarrow g_{9/2} h_{11/2}$
 interaction

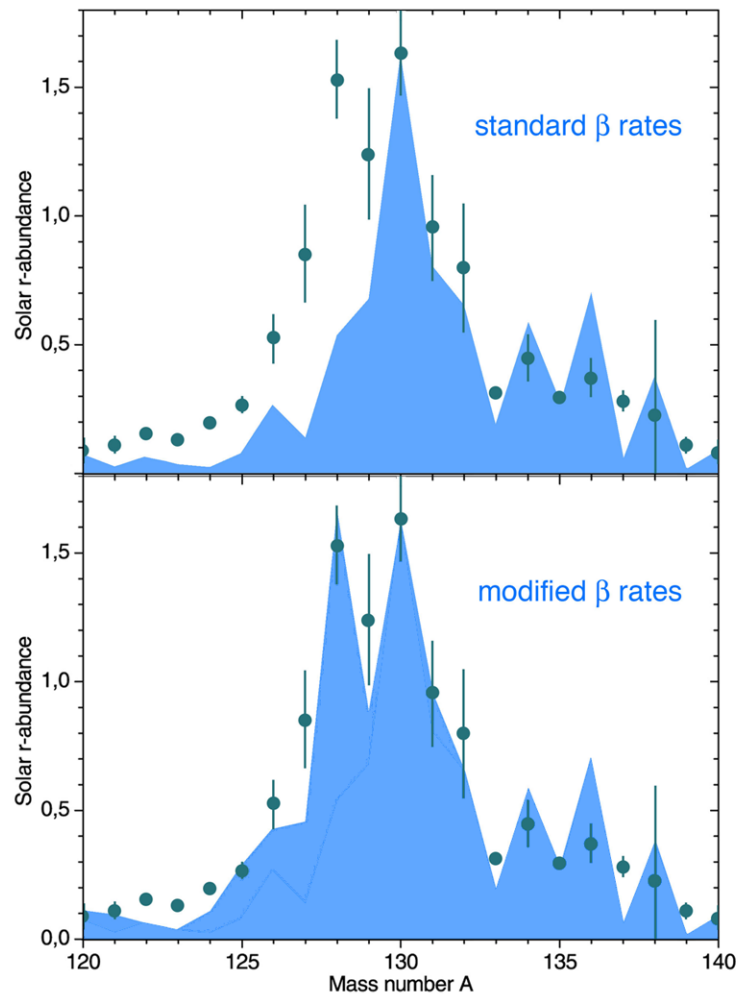


evidence for shell quenching



half-life of ^{78}Ni

[P.T. Hosmer et al.,
Phys. Rev. Lett **94**, 112501 (2005)]



improved nuclear structure
 no ν -interactions required

what is the site of the r-process?

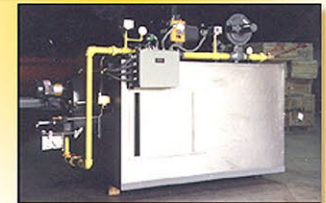


In 1995, WalkerGroup/CNI developed an The Envirobranding(r) process for IKEA. The 7200-square-foot space transformed itself every six weeks - from IKEA Sleeps to IKEA Cooks to IKEA Plays, etc. - and all the signage, graphics, merchandise presentations, cabinets, audio, in-store promotions and printed media changed in tandem with product change-outs.

Series R Process Air Heaters

- Meets FM, NFPA and IRI Standards
- Fuels Natural or Propane Gas
- Single Pass or Recirculating
- Standard Units Available with the following Specifications
- Static Pressures from $-5''$ WC to $2''$ WC
- Maximum Outlet Temperatures to 1000°F
- Capacities of 500,000 thru 4,500,000 BTUH

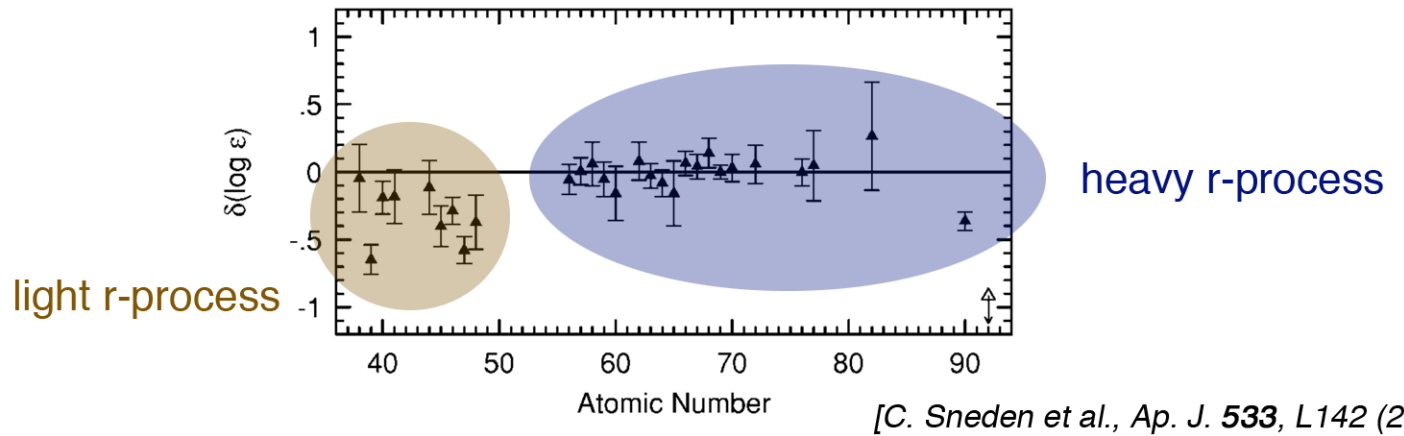
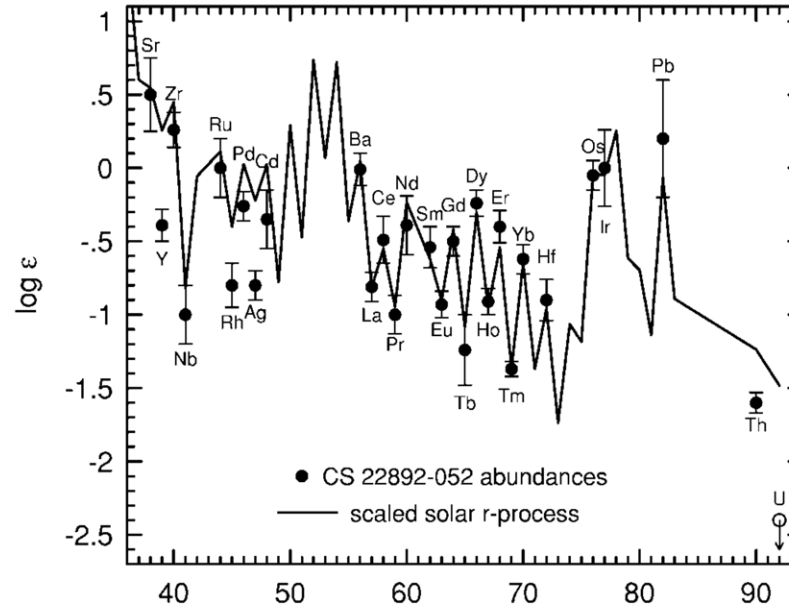
RECIRCULATING AIR HEATERS



Top: 2.5 MILLION BTUH RECIRCULATING SERIES R PROCESS AIR HEATERS FOR A 5 ZONE PRINTING PRESS.

Bottom: 800,000 BTUH SERIES R PROCESS AIR HEATER WITH CONTROL PANEL SUPPLIED FOR REMOTE MOUNTING.

What is the site of the r-process (where do we find lots of neutrons and high temperatures)?
 First of all, is it correct to say *the* r-process?



[C. Sneden et al., *Ap. J.* **533**, L142 (2000)]

there is also evidence in meteorite data



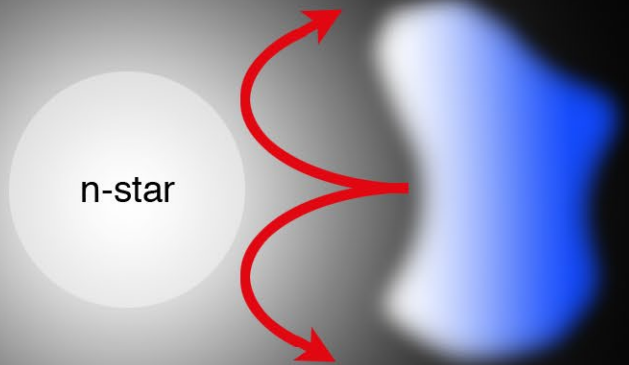
full r-process requires ~ 150 neutrons/seed

relevant quantities are entropy, S ; electron fraction, Y_e (or proton/nucleon) and expansion timescale

e.g. low $S \longrightarrow$ low Y_e , which may be found in neutron-star material

higher entropies can have $Y_e \sim 0.4 - 0.5$, which can be characteristic of supernovae

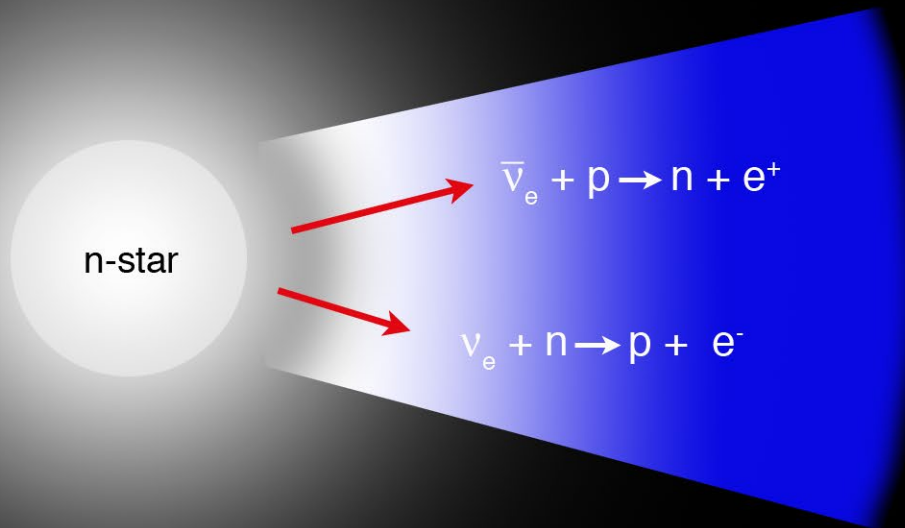
current thinking: type II supernovae or neutron-star mergers (or both)



low-entropy, prompt explosion

8 - 10 M_{\odot} progenitor

*the r-process in supernovae
(cartoon view)*



high entropy, ν -heated wind

$\geq 10 M_{\odot}$ progenitor

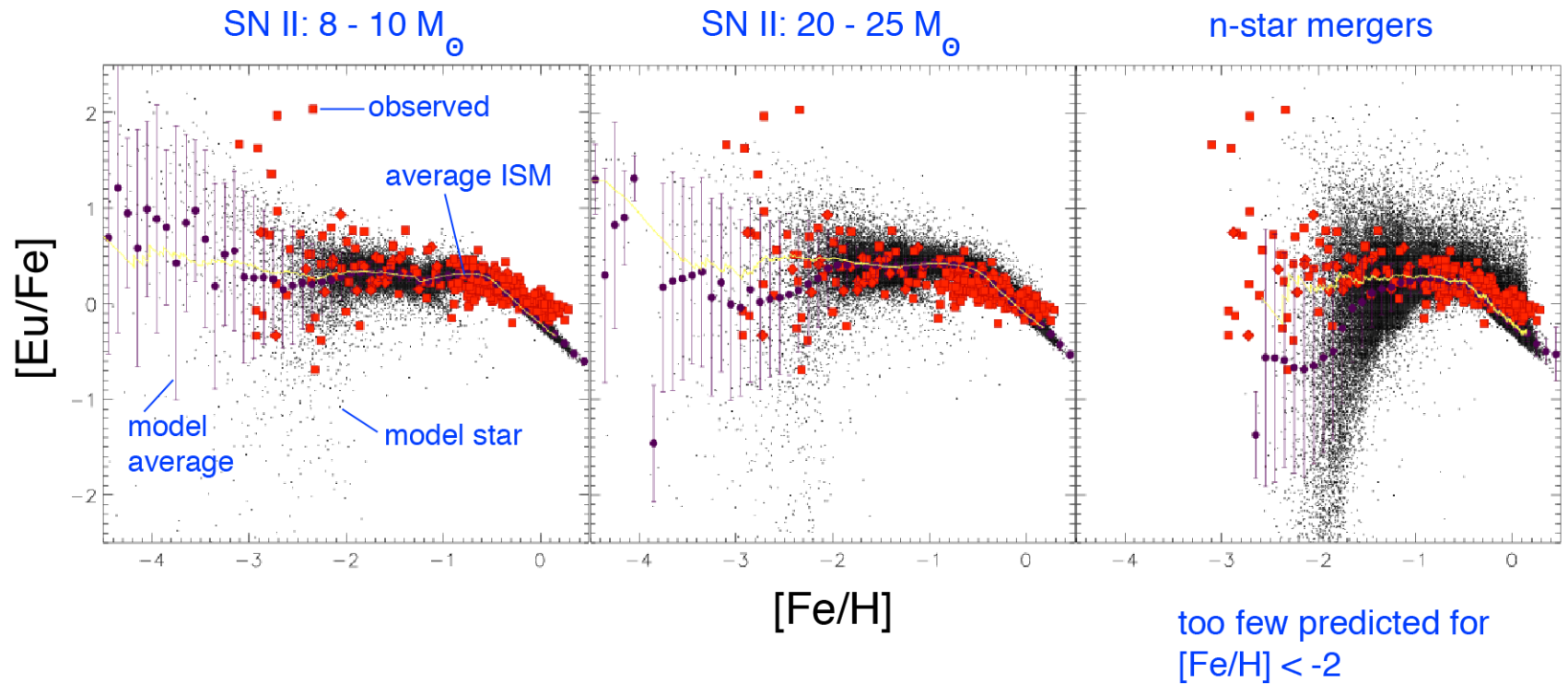
$\bar{\nu}_e + p$ is faster since $\bar{\nu}_e$ are hotter \longrightarrow matter becomes n-rich

neutron-star merger:

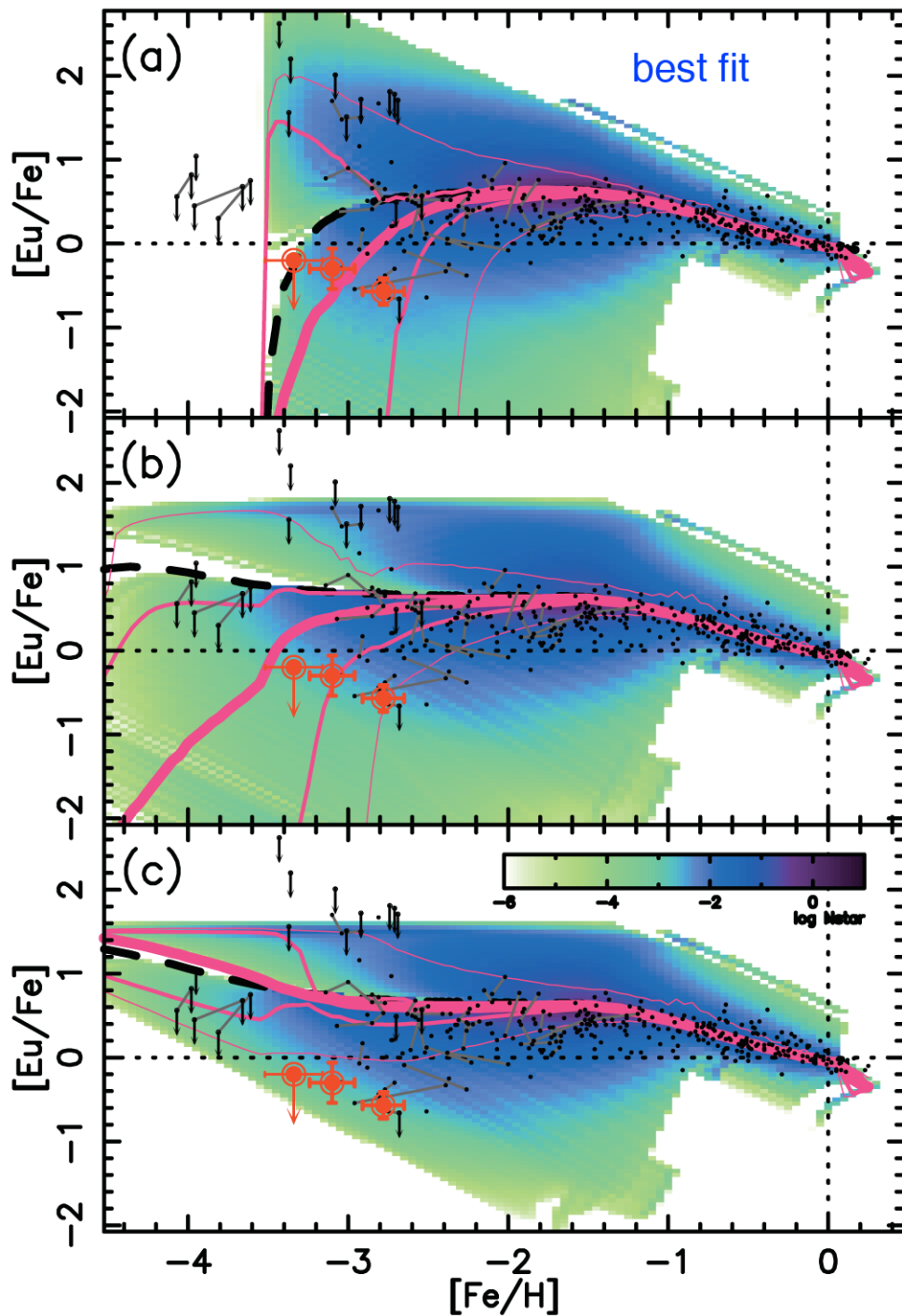
.

by Roland Oeschlin (Univ. of Basel, quasar.physik.unibas.ch/~oeschlin/pict.html)

observational constraint:



chemical evolution calculation by D. Argast et al., Astron. Astrophys. 416, 997 (2004)



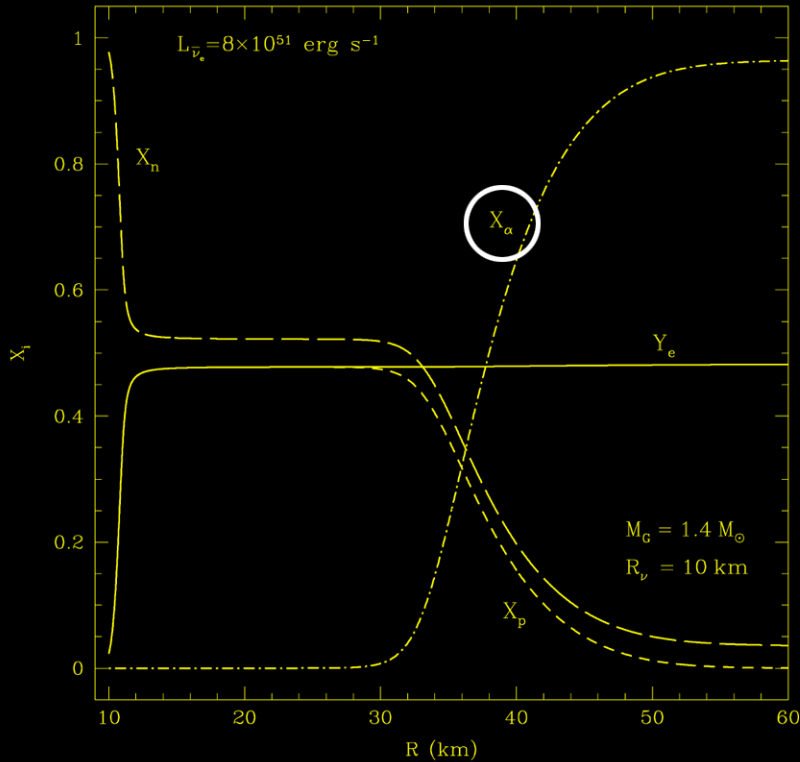
*new observations by
Y. Ishimaru et al., Ap. J 600, L47 (2004)*

lower masses seem favored

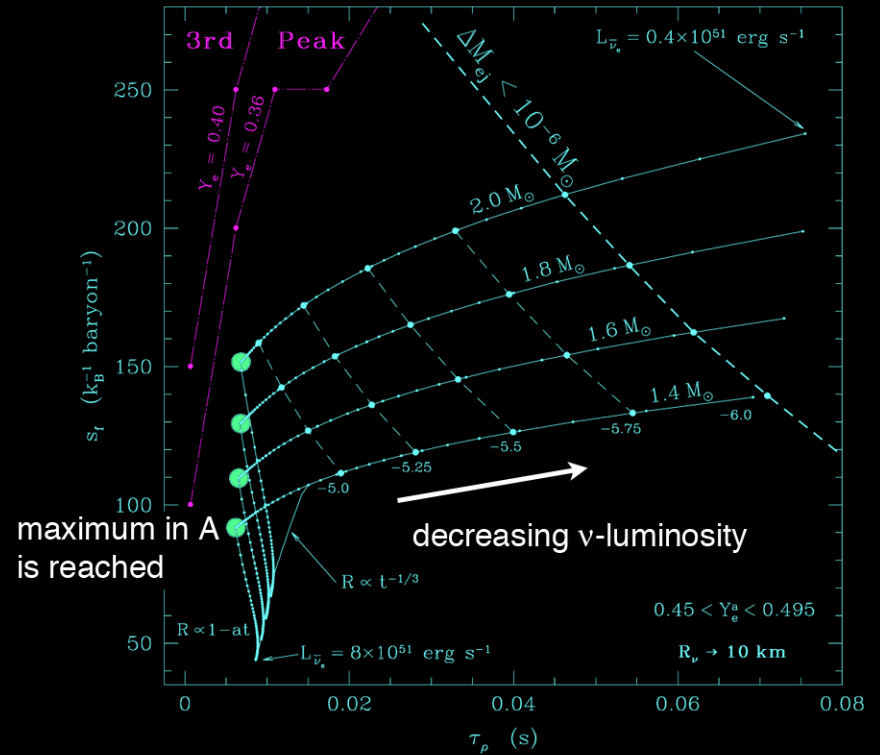
FIG. 2.—Comparison of the observed data with the model predictions. The r -process site is assumed to be SNe of (a) $8-10 M_{\odot}$, (b) $20-25 M_{\odot}$, and (c) greater than $30 M_{\odot}$ stars. The predicted number density of stars per unit area is color coded. The average stellar abundance distributions are indicated by heavy lines, with 50% and 90% confidence intervals (*medium and light lines, respectively*). The average abundances of the ISM are denoted by the heavy dashed lines. The current observational data are given by open circles, with others (*filled circles*) taken from Gratton & Sneden (1994), McWilliam et al. (1995), McWilliam (1998), Woolf, Tomkin, & Lambert (1995), Ryan et al. (1996), Shetrone (1996), Sneden et al. (1996), Westin et al. (1998), Burris et al. (2000), Fulbright (2000), Norris, Ryan, & Beers (2001), Johnson (2002), Johnson & Bolte (2002), François et al. (2003), and Honda et al. (2003).

the r-process in a ν -driven wind

[T.A. Thompson et al., *Ap. J.* 562, 887 (2001)]



note production of α -particles
(generally thought to be bad since
the ν -opacity drops and thus n /seed
drops)



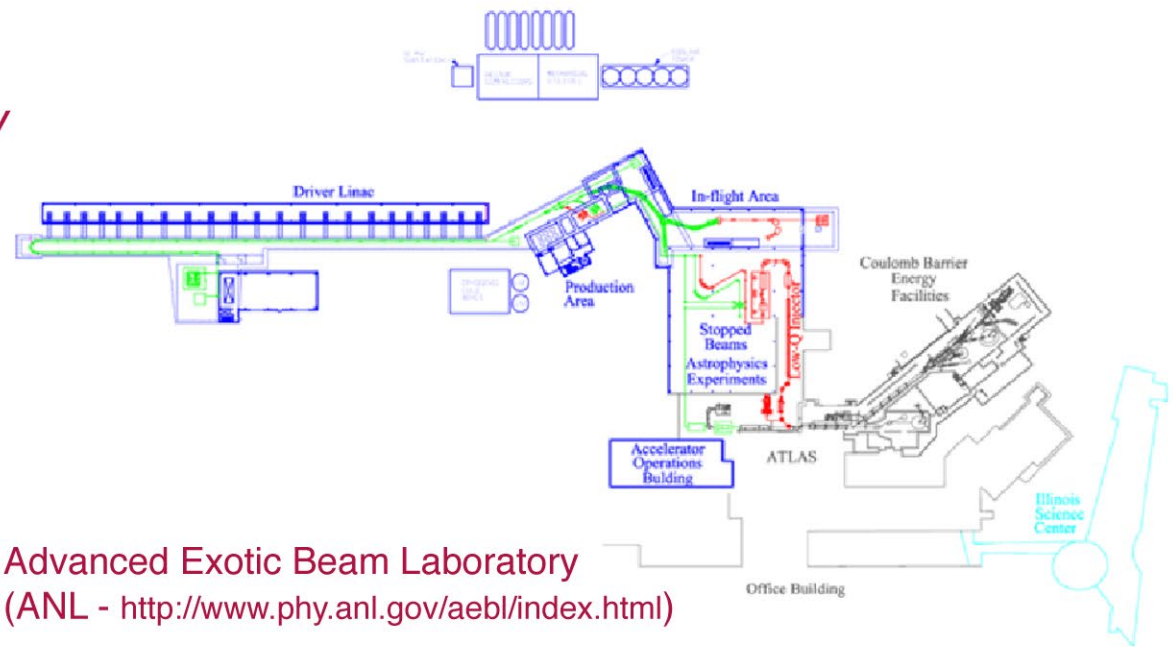
(e-folding time of density at $T = 0.5$ MeV)

in these calculations, r-process doesn't reach
the $A = 195$ peak (doesn't get beyond $A \sim 90$
for $1.4 M_{\odot}$ model)



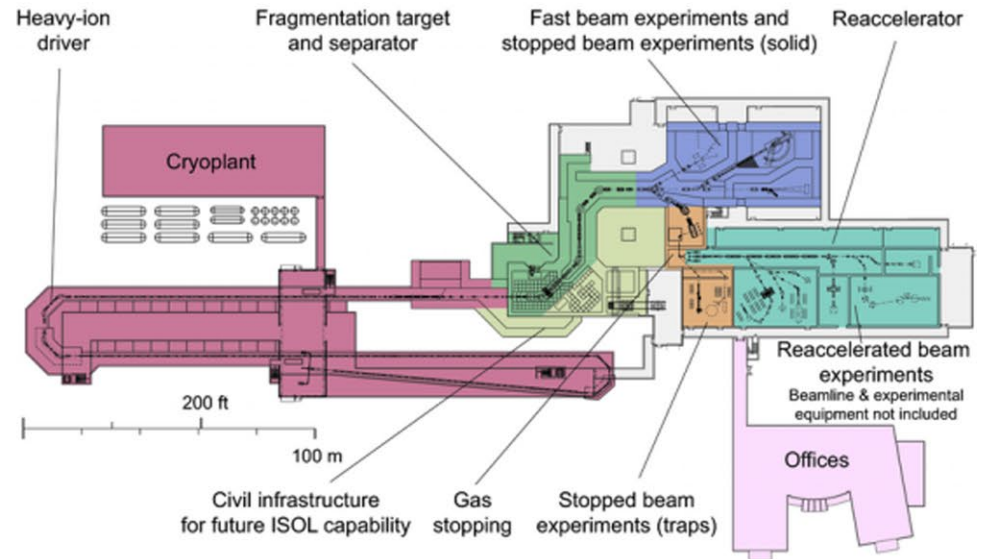
Initiatives in
nuclear astrophysics

*Experimental initiatives:
a next-generation RIB facility*

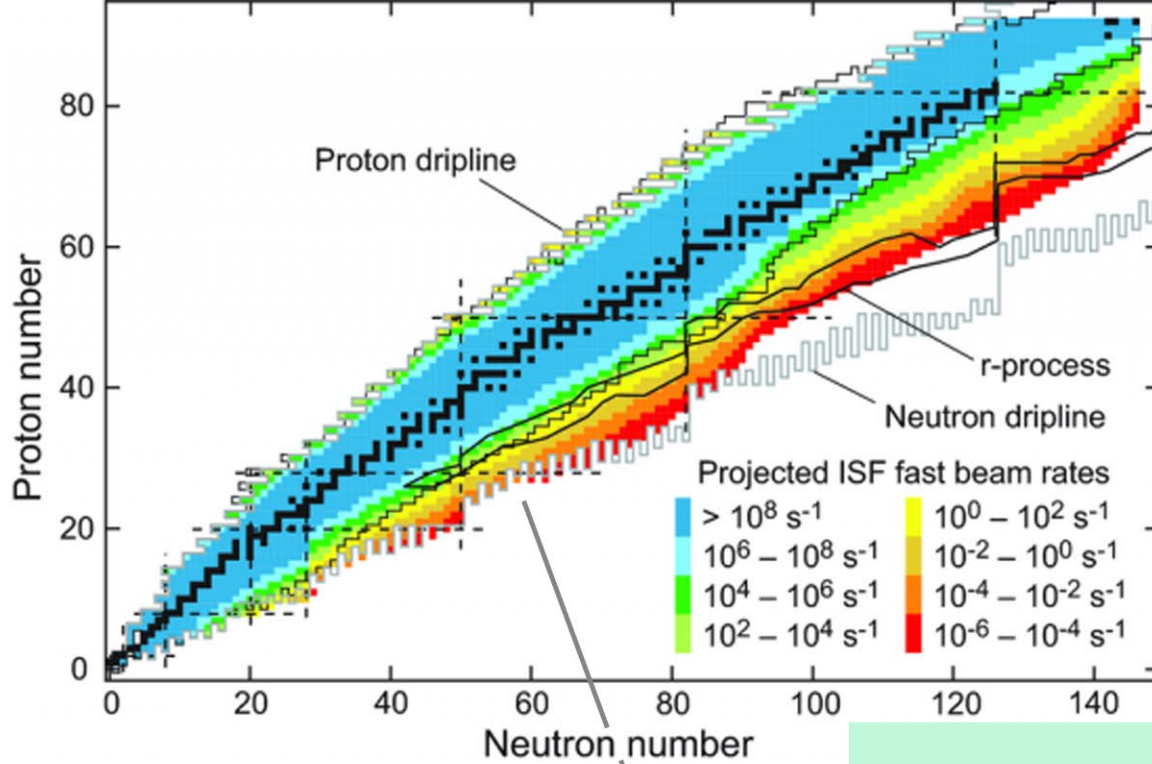


Advanced Exotic Beam Laboratory
(ANL - <http://www.phy.anl.gov/aeb/index.html>)

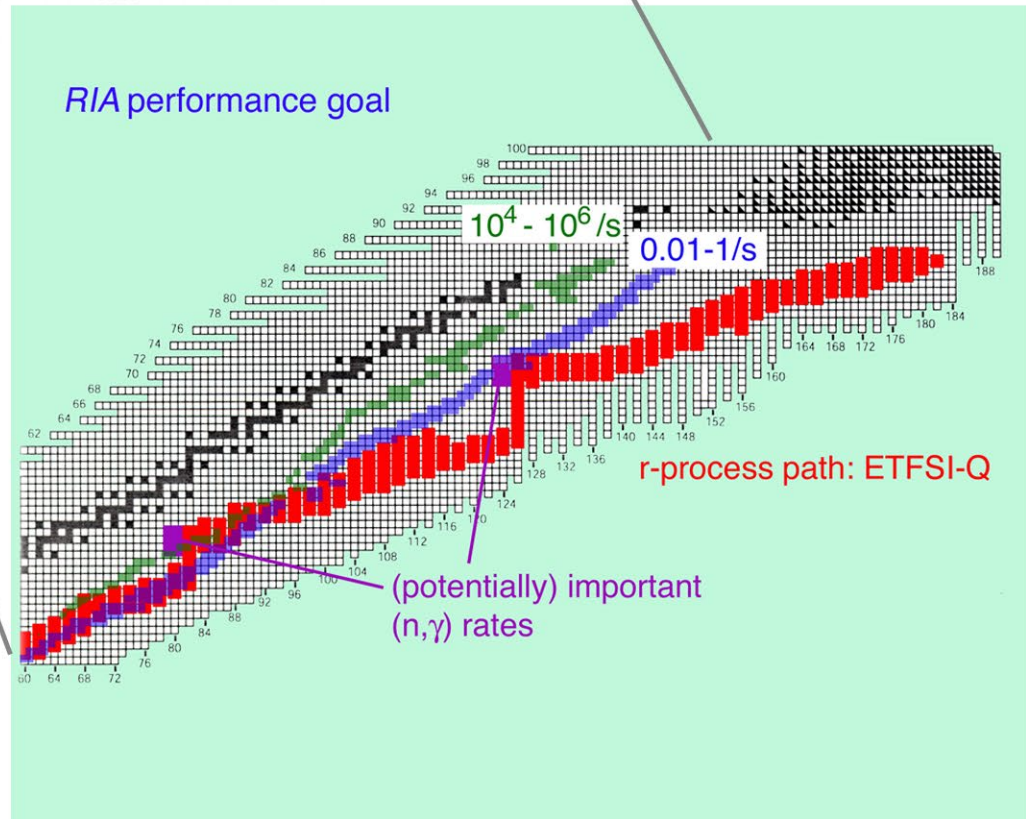
both designs feature a 200-MeV, 400 kW driver, stopped, re-accelerated and fast beams



Isotope Science facility
(MSU - <http://www.nsl.mscl.edu/future/isf/>)



projected beam intensities:
ISF vs. original RIA

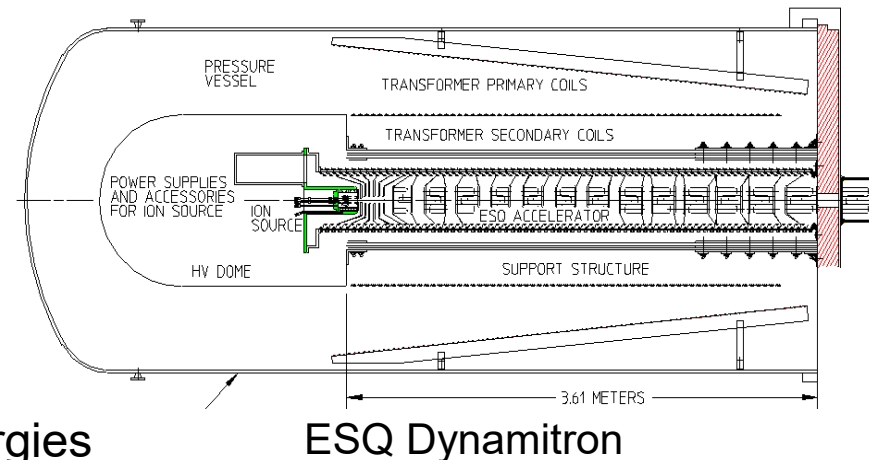
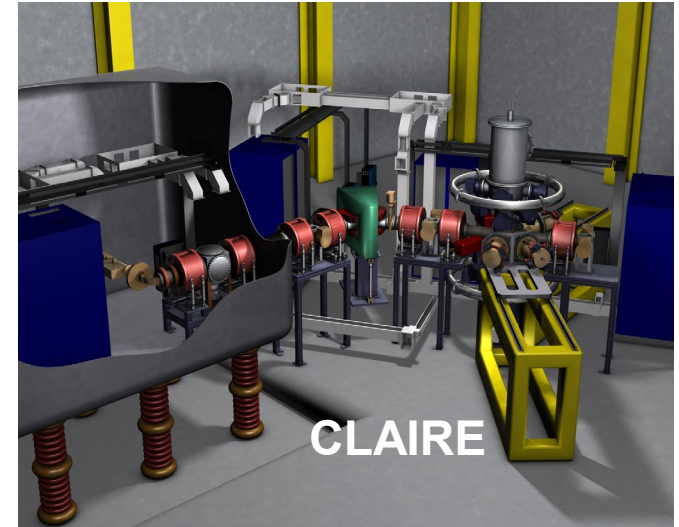


ALNA - Accelerator Laboratory for Nuclear Astrophysics Underground

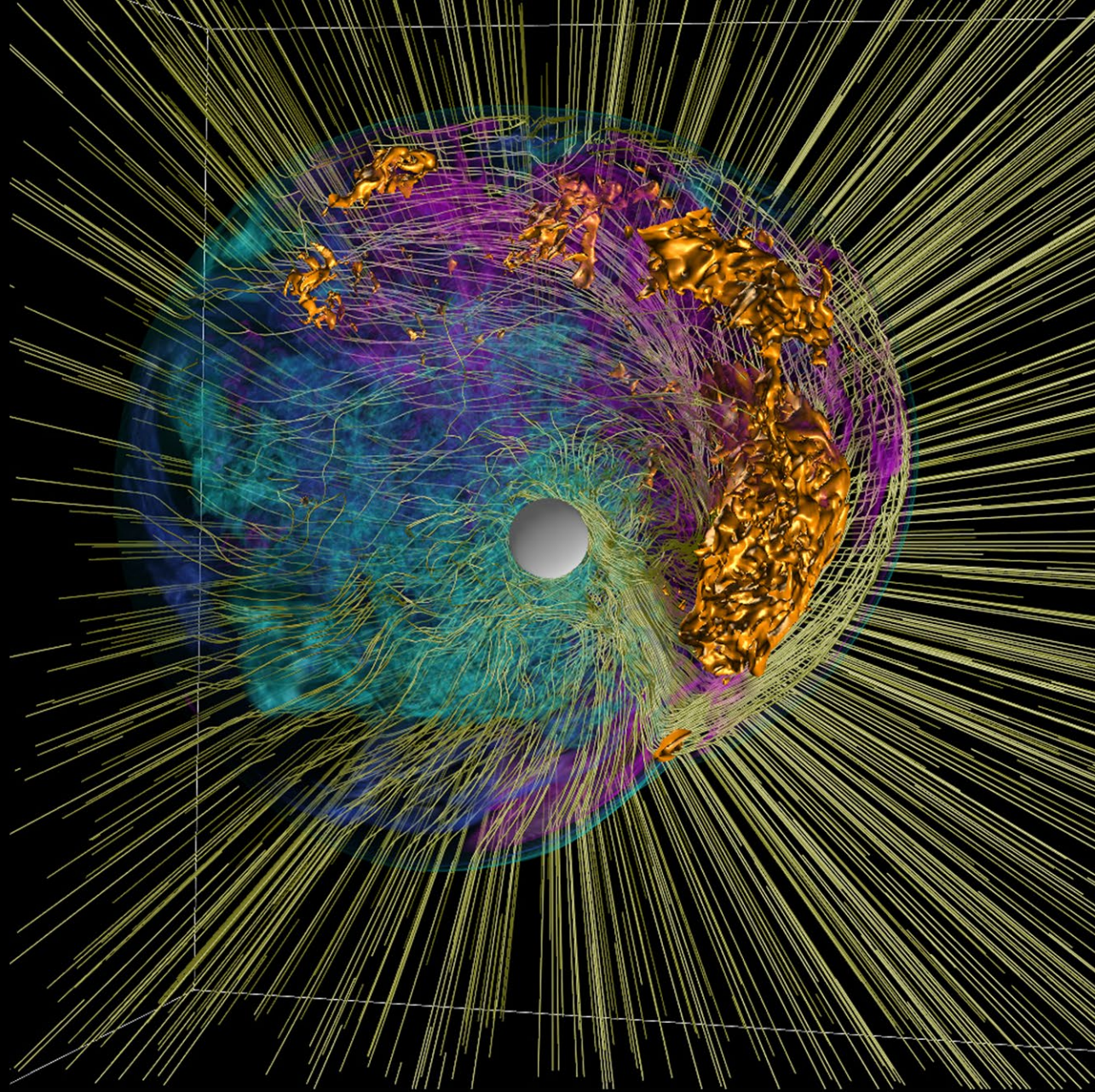
(from DUSEL science meeting)

Two accelerator based experimental areas

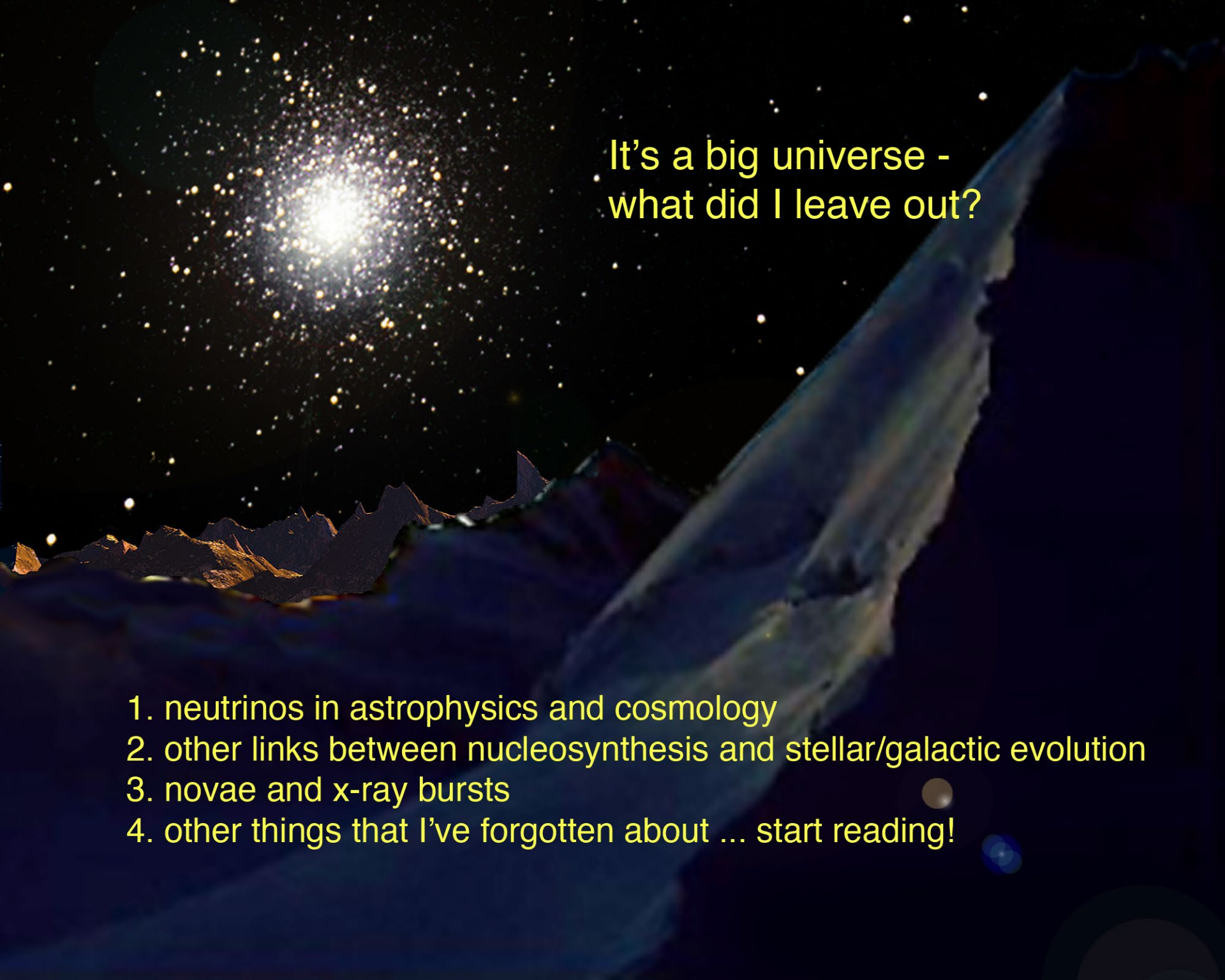
- High current DC accelerator (CLAIRE)
 - A compact, high intensity low energy accelerator for forward kinematics reactions (complementary or expanding on LUNA activities)
- A high intensity heavy ion accelerator
 - for inverse kinematic reaction and low energy fusion reactions
- Ion sources for both accelerators
 - high intensity 1+ ECR (up to 100mA)
 - Medium intensity n+ ECR (.5mA)
- The energy range of both accelerators combined should ideally cover beam energies from as low as 50keV up to 1 MeV/u
- The two accelerators should have an overlap in energy range for comparison between experiments over a common energy.



Large-scale simulations
e.g. Jaguar @ ORNL:
31,000 cores,
263 teraflops



The stream lines in this image show the two counter rotating flows that may be established below the supernova shock wave (the surface in the image) by the instability of the shock in a core collapse supernova explosion. The innermost flow accretes onto the central object, known as the proto-neutron star, spinning it up. This may be the mechanism whereby pulsars (spinning neutron stars) are born. [Blondin and Mezzacappa, Nature 445, 58 (2007)]



It's a big universe -
what did I leave out?

1. neutrinos in astrophysics and cosmology
2. other links between nucleosynthesis and stellar/galactic evolution
3. novae and x-ray bursts
4. other things that I've forgotten about ... start reading!