

Nuclear astrophysics

A survey in 6 parts

Jeff Blackmon, Physics Division, ORNL

Nuclear physics plays an important role in astrophysics:

**Energy generation
Synthesis of elements**



astronomical observables

- 1. Introduction**
- 2. Big Bang**
- 3. Stellar structure & solar neutrinos**
- 4. Stellar evolution & s process**
- 5. Supernovae & r process**
- 6. Binary systems: Type Ia, novae, x-ray bursts**



National Nuclear Physics Summer School 2007
The Florida State University
July 8th - 21st

Interdisciplinary research

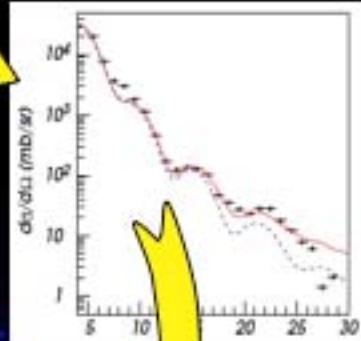
A variety of new tools in many areas are driving progress

Laboratory measurements

New beams & experimental techniques



Nuclear theory and data



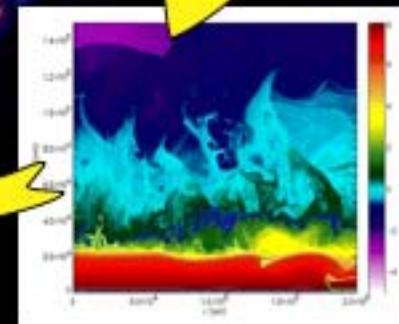
Observations

New orbiting instruments, increased optical power, presolar grains



Astrophysics

Improved shell model, reaction theory, rates, libraries & dissemination via the web



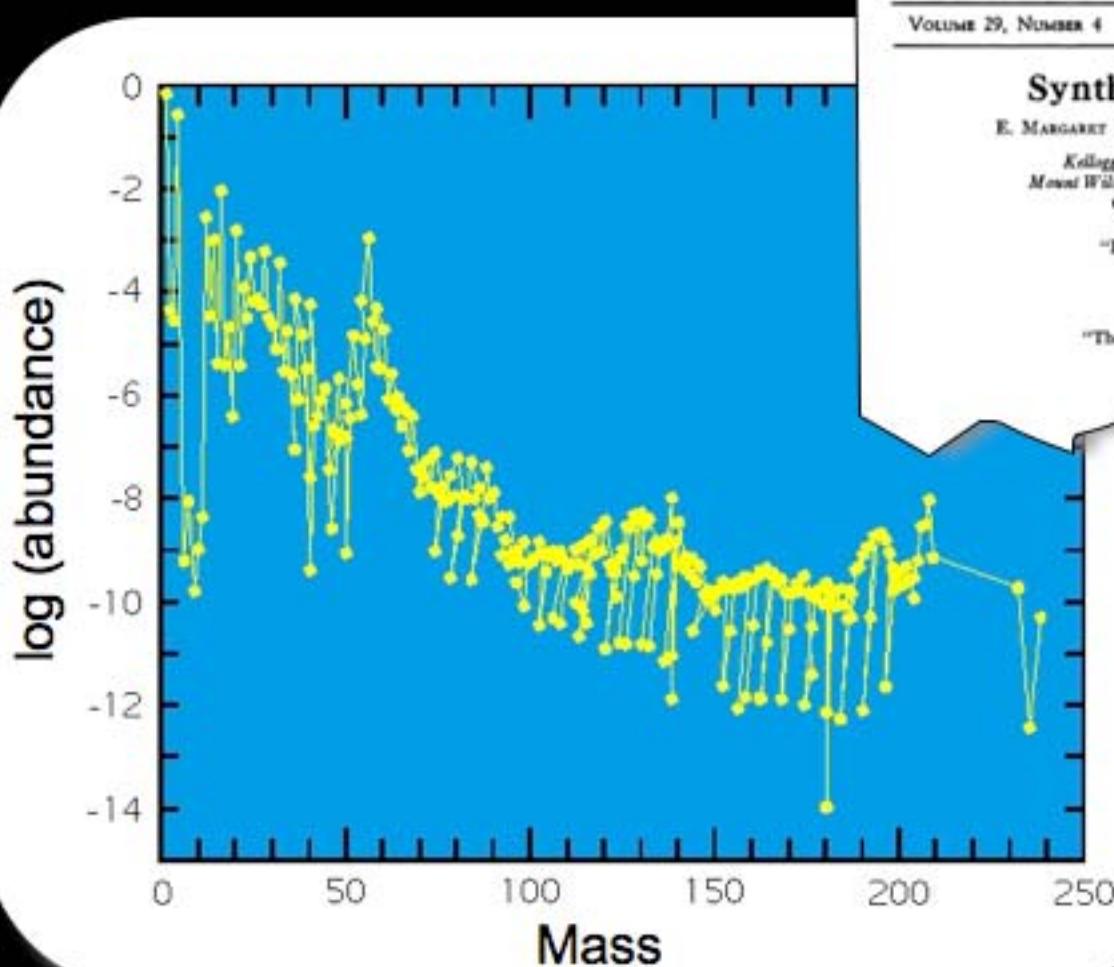
Advancing computing power → more realistic simulations



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Solar system abundances

**One of the most fundamental
and important observables**



REVIEWS OF MODERN PHYSICS

VOLUME 29, NUMBER 4

OCTOBER, 1957

Synthesis of the Elements in Stars*

E. MARGARET BURBIDGE, G. R. BURBIDGE, WILLIAM A. FOWLER, AND F. HOYLE

Kellogg Radiation Laboratory, California Institute of Technology, and
Mount Wilson and Palomar Observatories, Carnegie Institution of Washington,
California Institute of Technology, Pasadena, California

"It is the stars, The stars above us, govern our conditions";
(King Lear, Act IV, Scene 5)

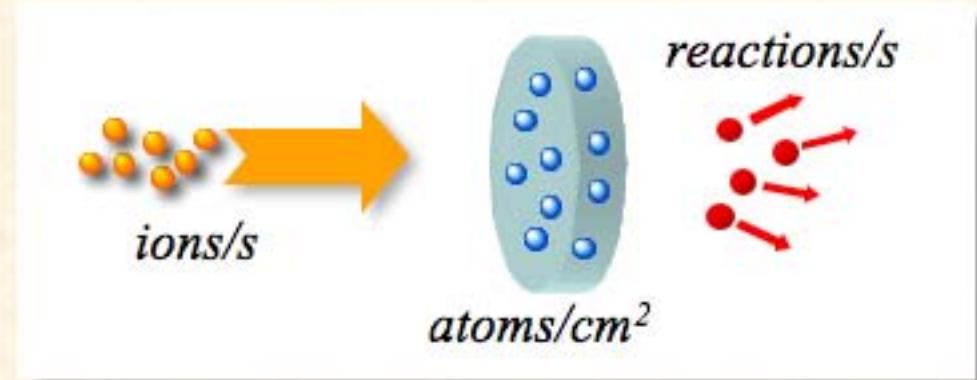
but perhaps

"The fault, dear Brutus, is not in our stars, But in ourselves,"
(Julius Caesar, Act I, Scene 2)

This year
marks the 50th
anniversary of
“B²FH”

Nuclear reactions in the lab & in space

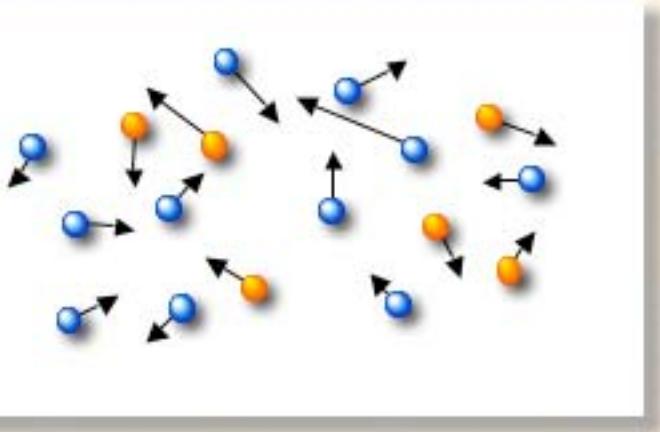
What you are used to in the lab:



cross section

$$\frac{\text{reactions}}{s} = \frac{\text{ions}}{s} \frac{\text{atoms}}{\text{cm}^2} \sigma$$

In astrophysical events:



reaction rate

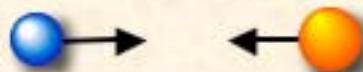
$$\frac{\text{reactions}}{\text{cm}^3 \text{s}} = \int \frac{n_x}{\text{cm}^3} \frac{n_y}{\text{cm}^3} v \sigma(v) \phi(v) dv$$

$$\phi(v) = 4\pi v^2 \left(\frac{\mu}{2\pi kT} \right)^{3/2} \exp\left(-\frac{\mu v^2}{2kT}\right)$$

$$\frac{\text{reactions}}{\text{cm}^3 \text{s}} = \frac{n_x}{\text{cm}^3} \frac{n_y}{\text{cm}^3} \langle \sigma v \rangle$$

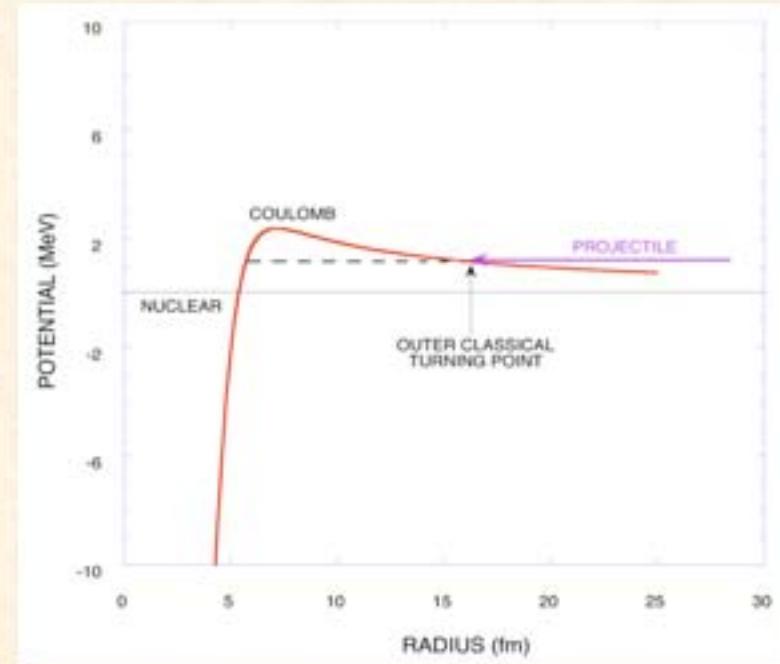
$$\langle \sigma v \rangle = \sqrt{\frac{8}{\pi\mu}} (kT)^{3/2} \int_0^\infty \sigma E e^{-E/(kT)} dE$$

The Coulomb barrier



Energy of particles in astrophysical environments is much lower than the Coulomb barrier

$$V_c = \frac{1.44 Z_a Z_b}{r} \text{ MeV}\cdot\text{fm}$$



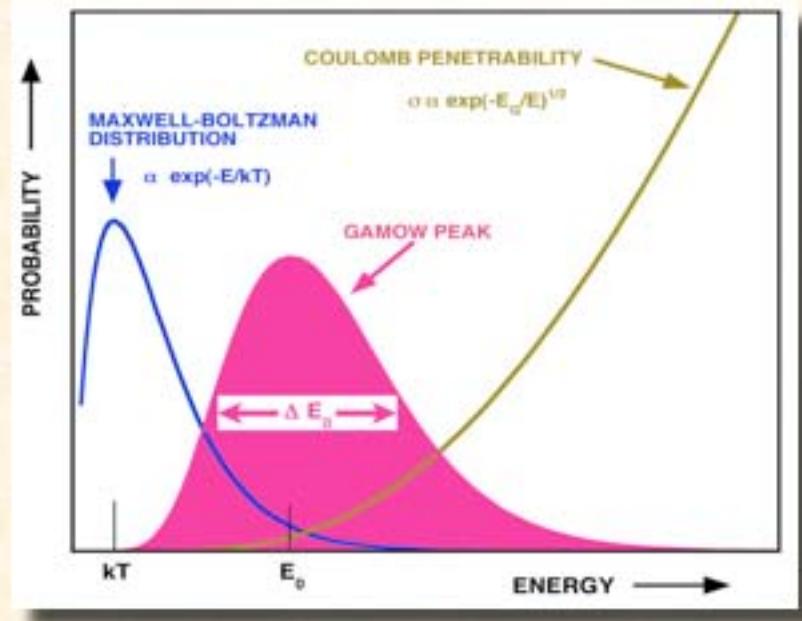
Reaction	site	$T (10^6 \text{ K})$	$kT (\text{keV})$	$r_{\text{tum}} (\text{fm})$	$r (\text{fm})$
p+p	sun	15	1.3	1100	2.5
p+ ¹⁴ N	CNO	30	2.6	3900	4.3
α + ¹² C	red giant	190	16	1060	4.8
p+ ¹⁷ F	nova	300	26	500	4.5
α + ³⁰ S	x-ray burst	1000	86	500	5.9
³ He+ ⁴ He	big bang	2000	170	33	3.8

The Gamow window

$$\langle \sigma v \rangle = \sqrt{\frac{8}{\pi \mu}} (kT)^{3/2} \int_0^{\infty} \sigma E e^{-E/(kT)} dE$$

$$\sigma \equiv \frac{S}{E} e^{-\sqrt{E_G/E}} \quad E_G \equiv \frac{2\mu}{\hbar^2} (\pi Z_1 Z_2 e^2)^2$$

$$\langle \sigma v \rangle = \sqrt{\frac{8}{\pi \mu}} (kT)^{3/2} \int_0^{\infty} S e^{-\sqrt{E_G/E}} e^{-E/(kT)} dE$$



Reaction	site	$T (10^6 \text{ K})$	$kT (\text{keV})$	$r_{tum} (\text{fm})$	$r (\text{fm})$	$E_0 (\text{keV})$
p+p	sun	15	1.3	1100	2.5	6
p+ ¹⁴ N	CNO	30	2.6	3900	4.3	42
α + ¹² C	red giant	190	16	1060	4.8	300
p+ ¹⁷ F	nova	300	26	500	4.5	230
α + ³⁰ S	x-ray burst	1000	86	500	5.9	1800
³ He+ ⁴ He	big bang	2000	170	33	3.8	580

Why the S-factor is useful

Example: ${}^3\text{He}(\alpha, \gamma) {}^7\text{Be}$

Important for:

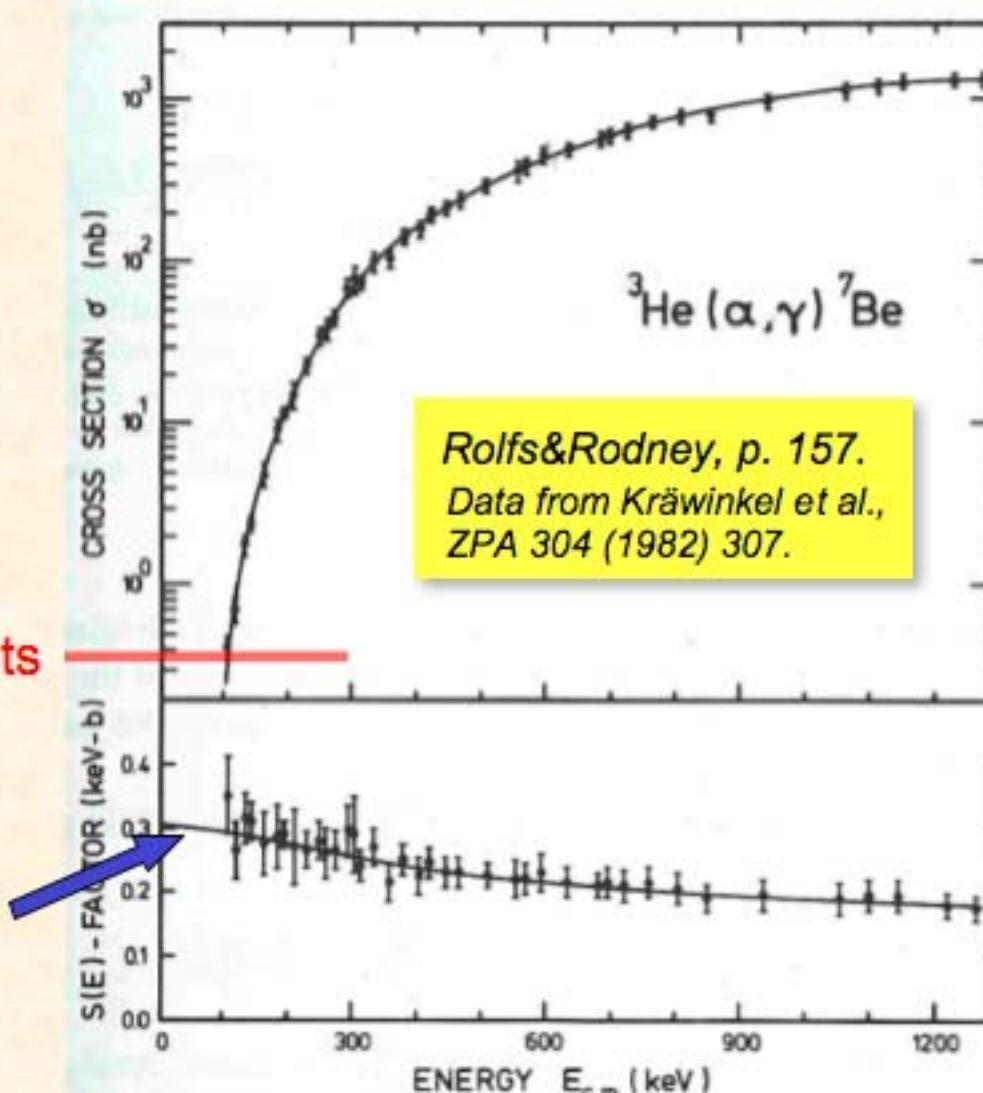
The sun (ν production)

Big Bang (Li production)

Limit of experiments

Need σ here for sun

But be careful...



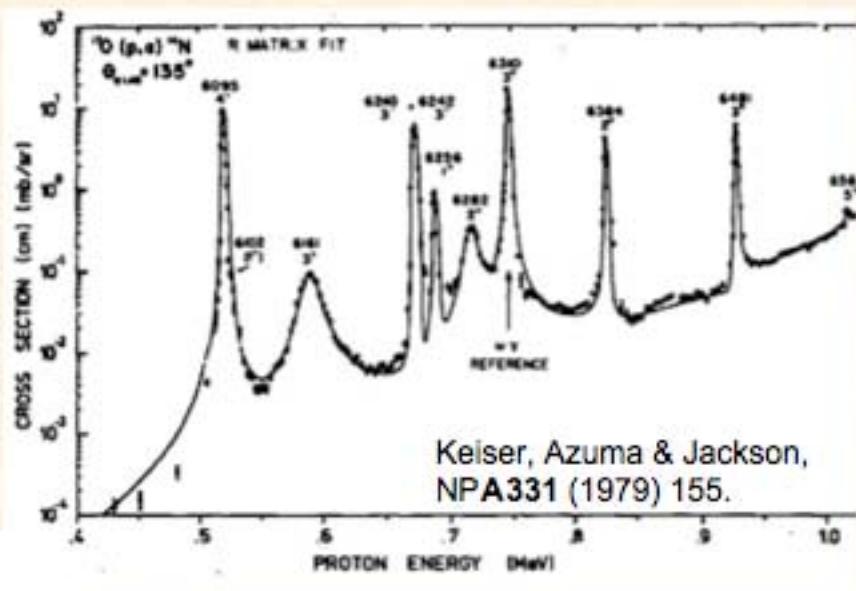
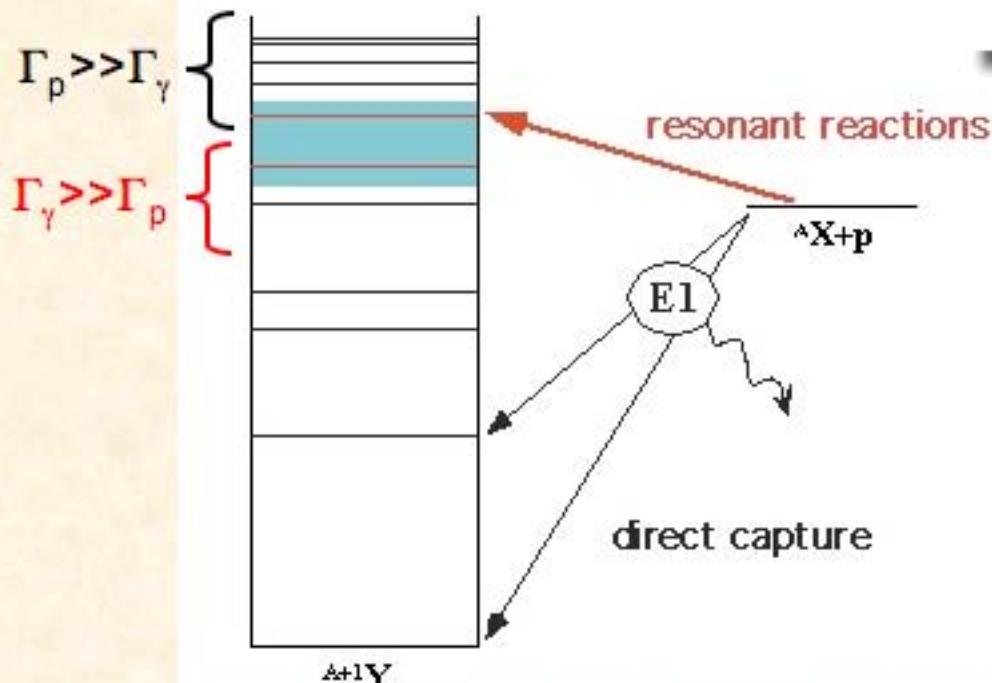
Identifying resonances is crucial

$$\langle \sigma v \rangle = \sqrt{\frac{8}{\pi \mu}} (kT)^{3/2} \int_0^{\infty} \sigma E e^{-E/(kT)} dE$$

$$\sigma(E) = \pi \lambda^2 \frac{2J+1}{(2J_x+1)(2J_y+1)} \frac{\Gamma_x \Gamma_y}{(E - E_r)^2 + (\Gamma/2)^2}$$

$$\Gamma_p = 2 \left(\frac{\hbar^2}{\lambda \mu R} \right) \left(\frac{\theta_p^2}{F_\ell^2 + G_\ell^2} \right)$$

→ Lecture 3



If resonance is narrow

$$\langle \sigma v \rangle = \left(\frac{2\pi}{\mu} kT \right)^{3/2} \hbar^2 (\omega \gamma) e^{-E_r/kT}$$

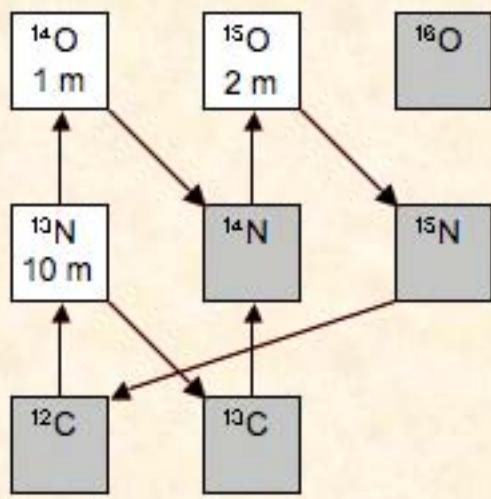
$$\omega \gamma = \frac{2J+1}{(2J_x+1)(2J_y+1)} \frac{\Gamma_x \Gamma_y}{\Gamma}$$

"resonance strength"

Solving a reaction rate network

The CN cycle: hydrogen burning

Identify important reactions



Nuclear physics → reaction rates

Astrophysical model to define the equations of state: ρ, T

Network of many coupled equations

$$\frac{dN_{^{12}\text{C}}}{dt} = N_{^{15}\text{N}} N_p \langle \sigma v \rangle_{^{15}\text{N}p} - N_{^{12}\text{C}} N_p \langle \sigma v \rangle_{^{12}\text{C}p}$$

$$\frac{dN_{^{13}\text{N}}}{dt} = N_{^{12}\text{C}} N_p \langle \sigma v \rangle_{^{12}\text{C}p} - N_{^{13}\text{N}} N_p \langle \sigma v \rangle_{^{13}\text{N}p} - \lambda_{^{13}\text{N}} N_{^{13}\text{N}}$$

$$\frac{dN_{^{13}\text{C}}}{dt} = \lambda_{^{13}\text{N}} N_{^{13}\text{N}} - N_{^{13}\text{C}} N_p \langle \sigma v \rangle_{^{13}\text{C}p}$$

$$\frac{dN_{^{14}\text{O}}}{dt} = N_{^{13}\text{N}} N_p \langle \sigma v \rangle_{^{13}\text{N}p} - \lambda_{^{14}\text{O}} N_{^{14}\text{O}}$$

$$\frac{dN_{^{14}\text{N}}}{dt} = N_{^{13}\text{C}} N_p \langle \sigma v \rangle_{^{13}\text{C}p} + \lambda_{^{14}\text{O}} N_{^{14}\text{O}} - N_{^{14}\text{N}} N_p \langle \sigma v \rangle_{^{14}\text{N}p}$$

$$\frac{dN_{^{15}\text{O}}}{dt} = N_{^{14}\text{N}} N_p \langle \sigma v \rangle_{^{14}\text{N}p} - \lambda_{^{15}\text{O}} N_{^{15}\text{O}}$$

$$\frac{dN_{^{15}\text{N}}}{dt} = \lambda_{^{15}\text{O}} N_{^{15}\text{O}} - N_{^{15}\text{N}} N_p \langle \sigma v \rangle_{^{15}\text{N}p}$$

→ Numerically solve for $N_x(t)$

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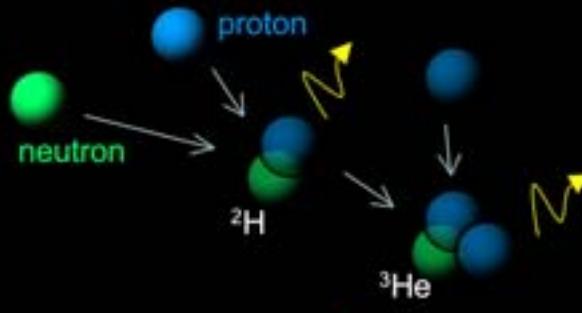
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The Early Universe

Space, time, matter, & energy began with the Big Bang

Independent observations tell us about different epochs

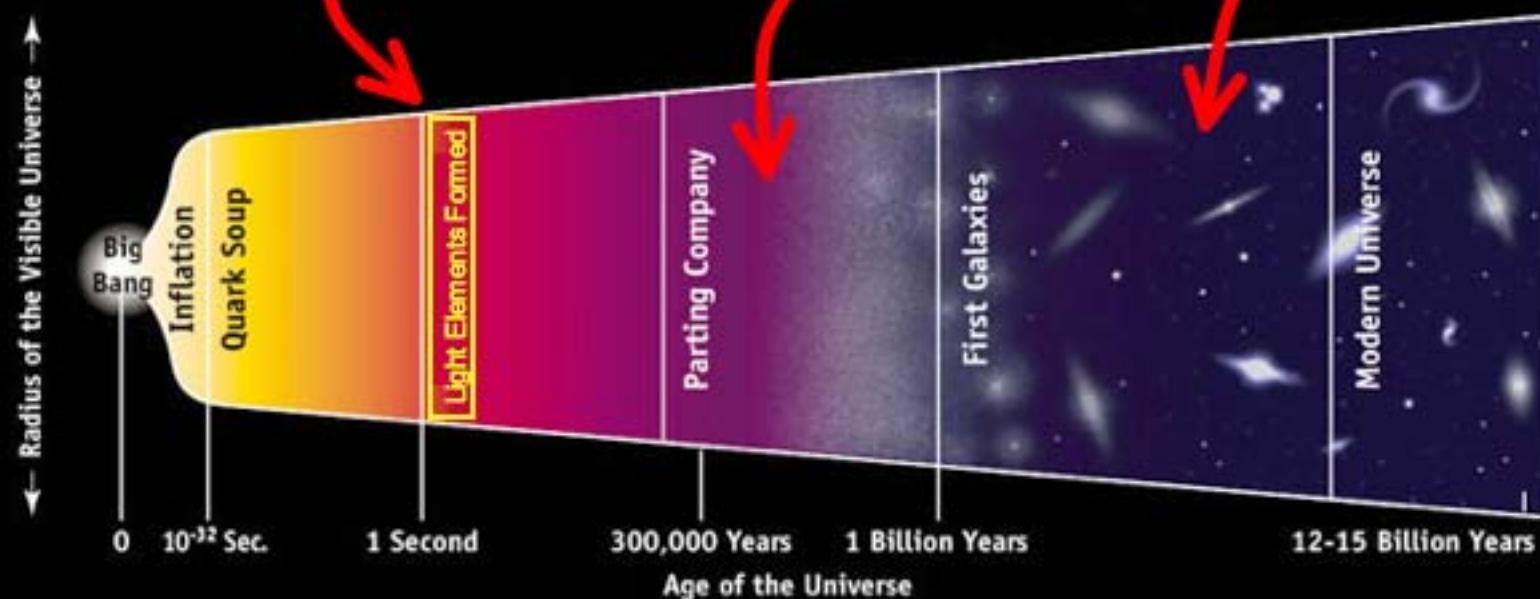
Nucleosynthesis



CMB -The afterglow



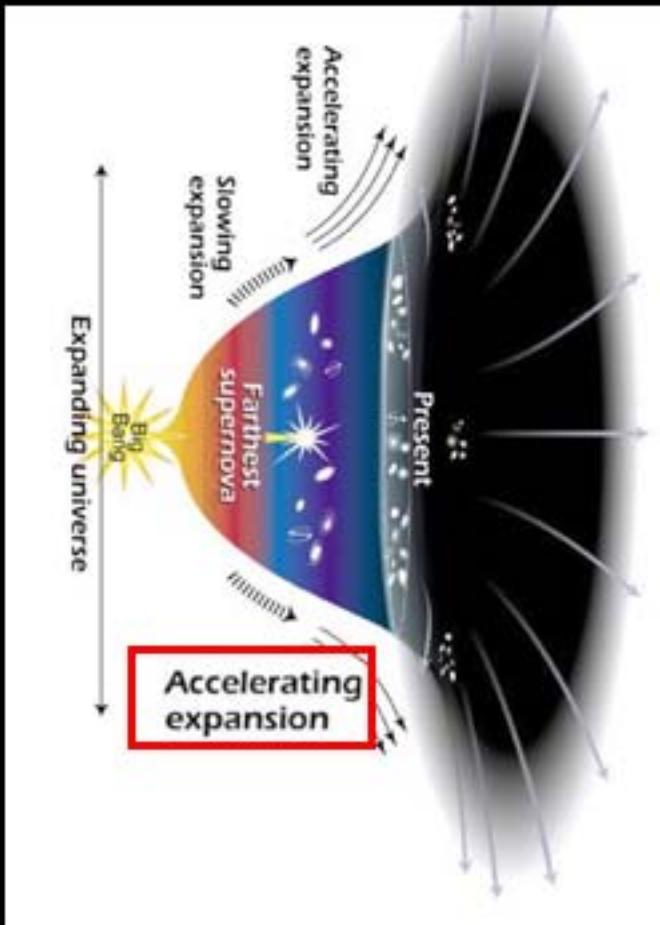
Stellar observations



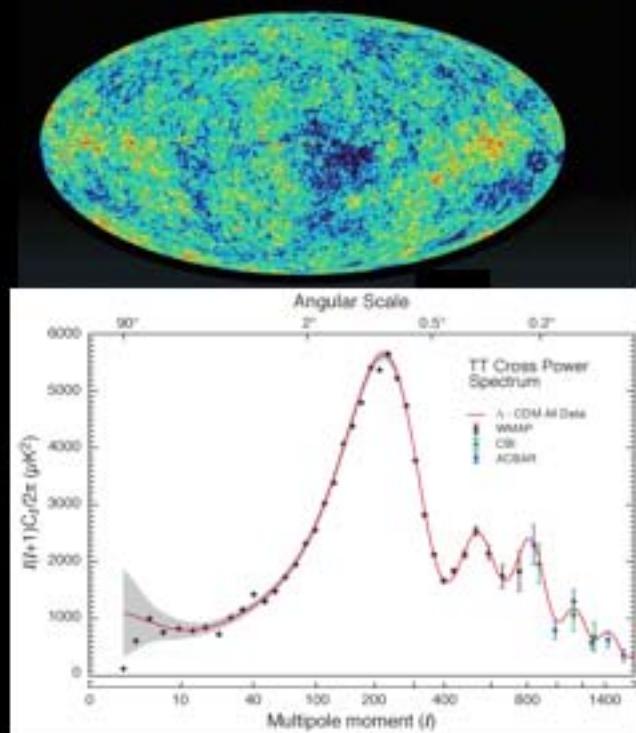
New Cosmological Paradigm

(Lecture 3)

Type 1a supernova
redshift vs.
distance indicates
the expansion
rate of the
universe is
accelerating

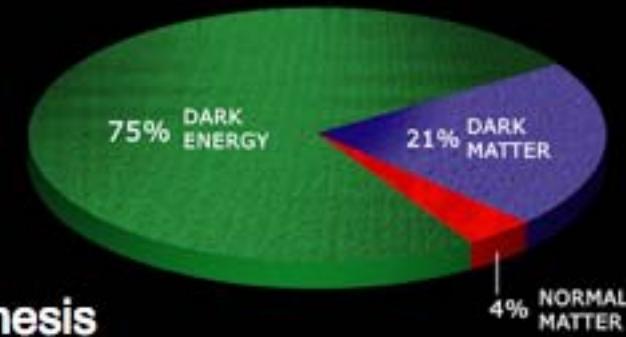


WMAP: CMB Observations

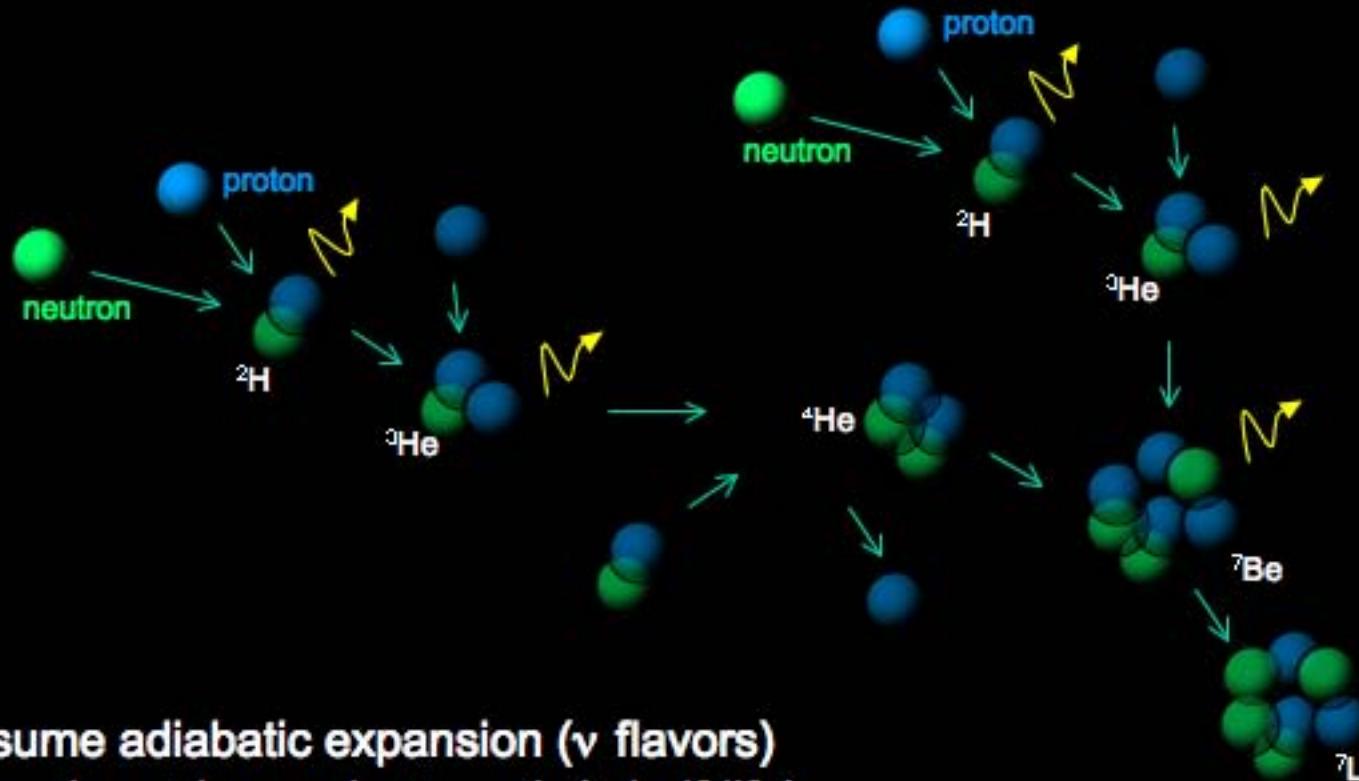


DARK ENERGY (e.g. cosmological constant) exerts a
“negative pressure” causing the acceleration

Only 4% of matter is baryonic → test with nucleosynthesis



The Homogeneous BBN Model



Assume adiabatic expansion (ν flavors)
n/p ratio set by weak strength (n half-life)
Only free parameter is baryon/photon ratio

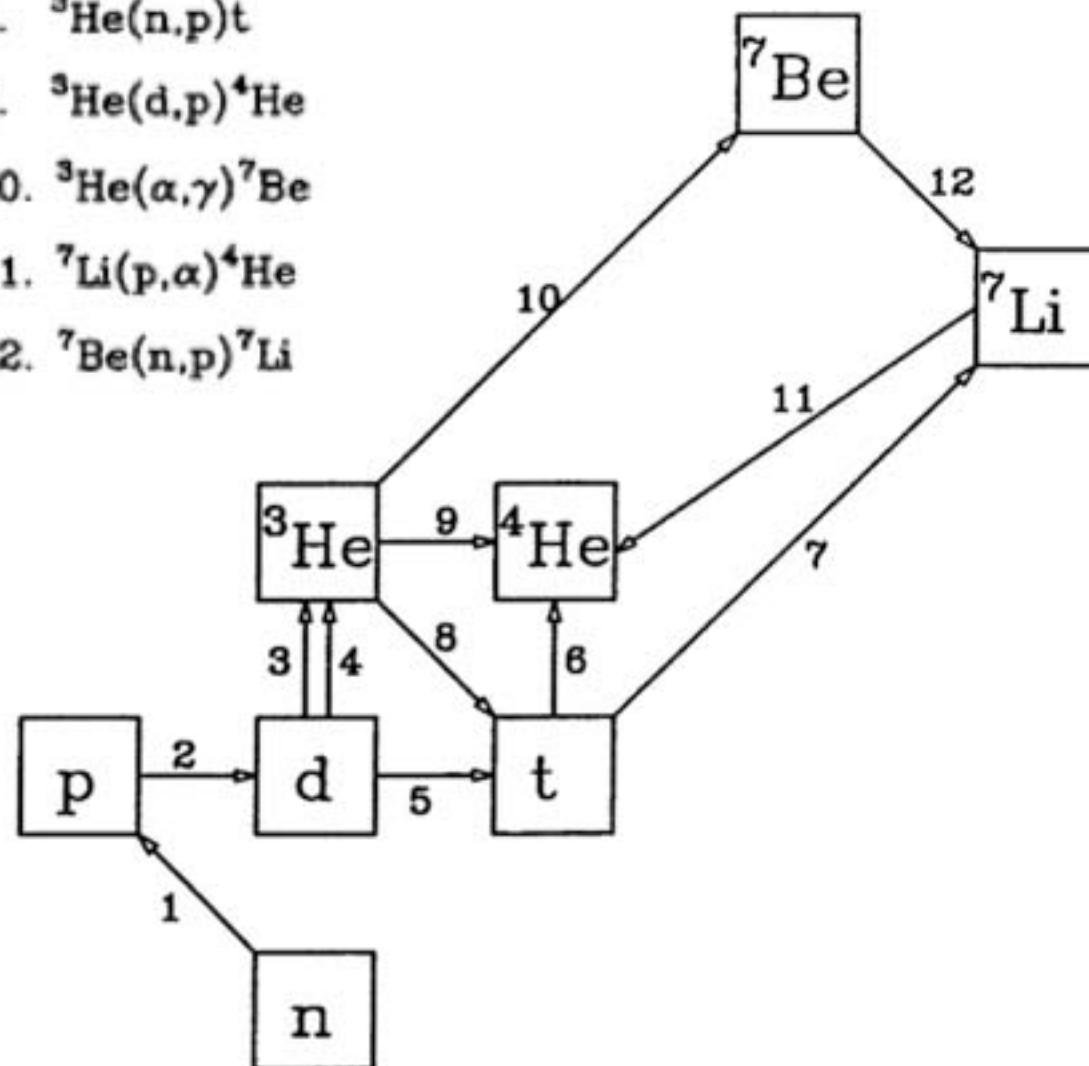
~All free neutrons into ^4He
Mass 5 & 8 gaps inhibit formation of heavy elements



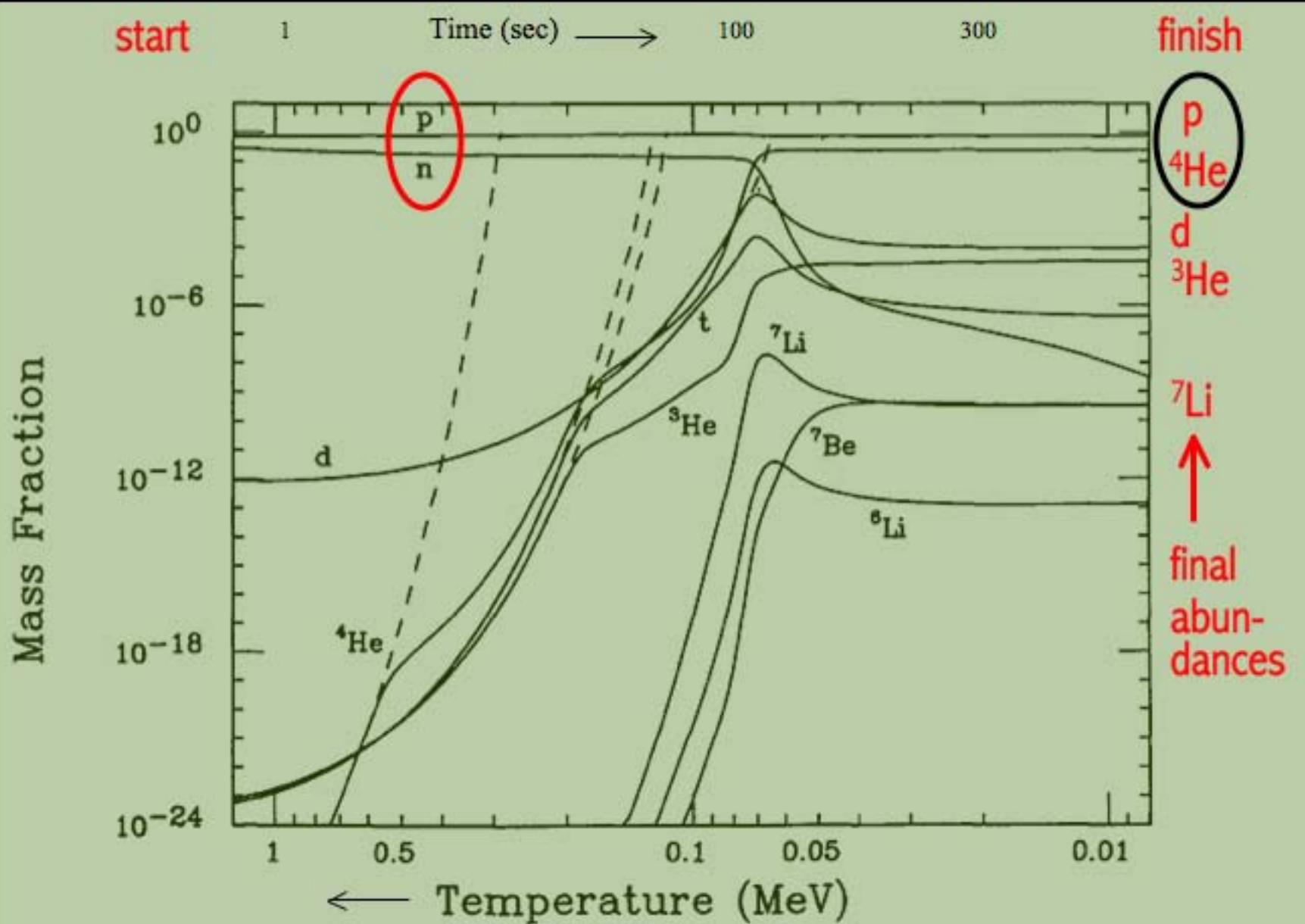
p ~75%
 ^4He ~25%
 $^2\text{H}, ^3\text{He}$ ~ 10^{-5}
 ^7Li ~ 10^{-10}

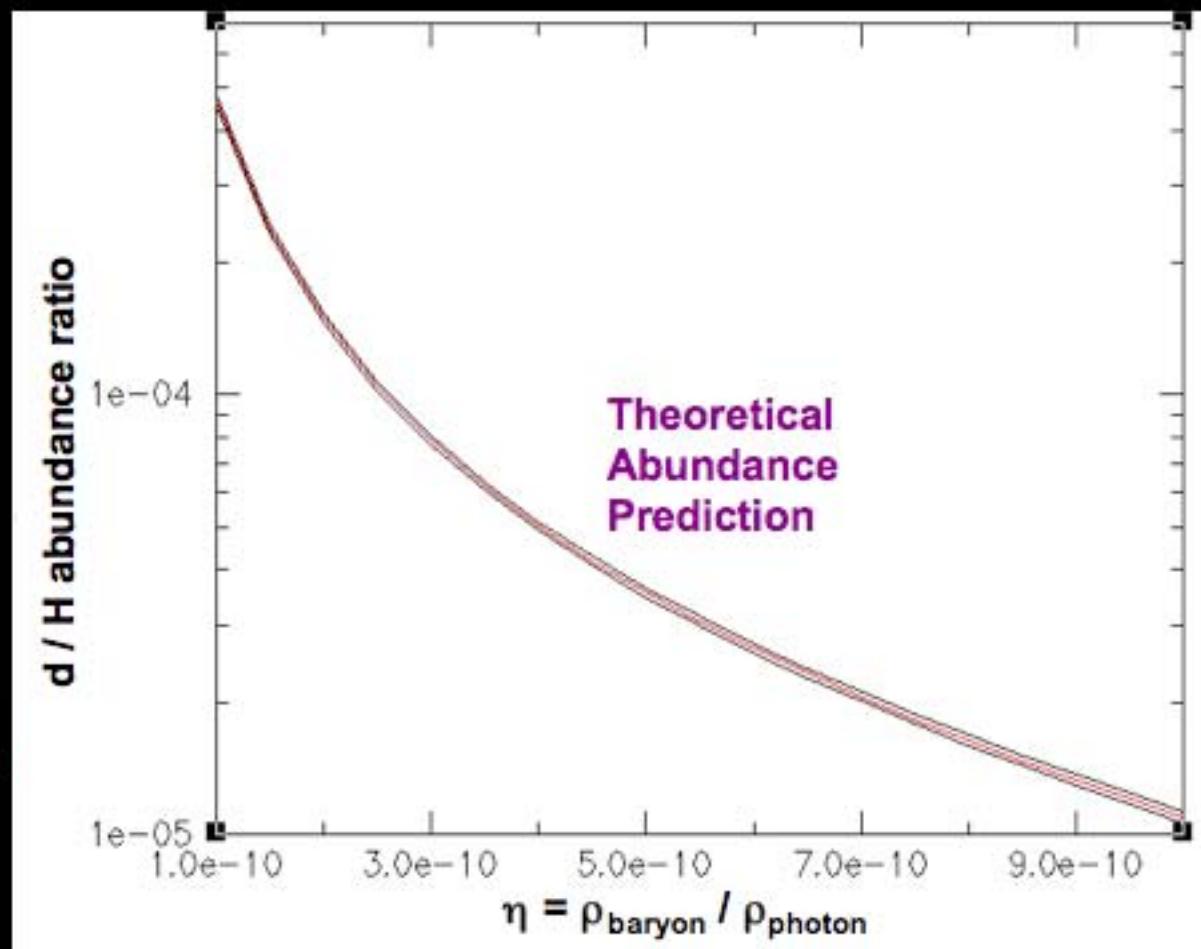
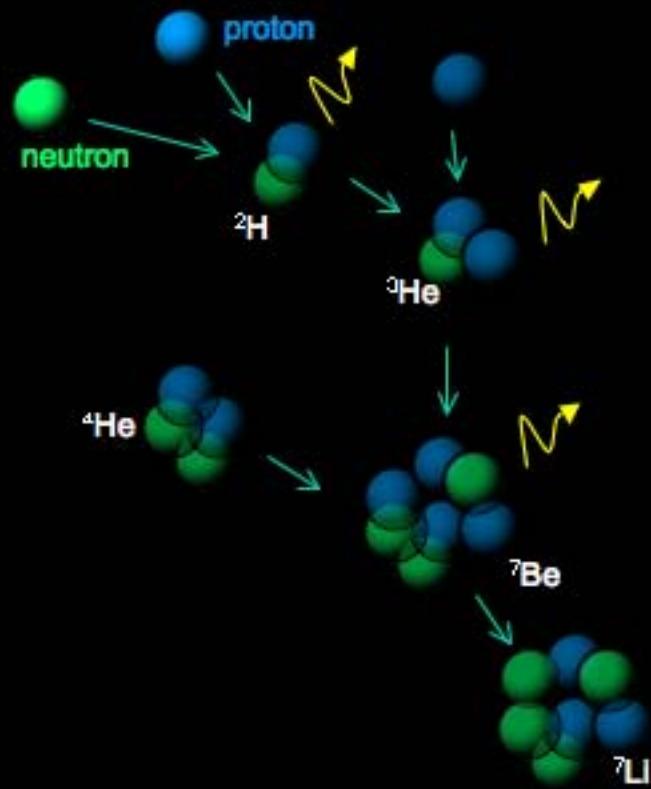
A Typical Big Bang Network

- | | |
|------------------------------|--|
| 1. $n \leftrightarrow p$ | 7. $t(\alpha, \gamma)^7\text{Li}$ |
| 2. $p(n, \gamma)d$ | 8. $^3\text{He}(n, p)t$ |
| 3. $d(p, \gamma)^3\text{He}$ | 9. $^3\text{He}(d, p)^4\text{He}$ |
| 4. $d(d, n)^3\text{He}$ | 10. $^3\text{He}(\alpha, \gamma)^7\text{Be}$ |
| 5. $d(d, p)t$ | 11. $^7\text{Li}(p, \alpha)^4\text{He}$ |
| 6. $t(d, n)^4\text{He}$ | 12. $^7\text{Be}(n, p)^7\text{Li}$ |



Solve the reaction rate network





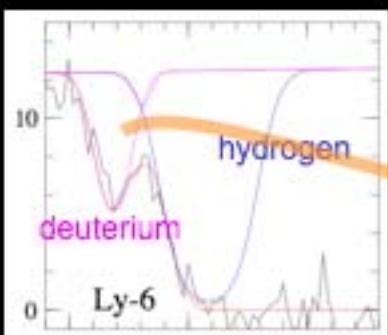
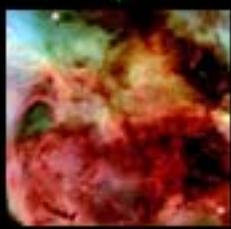
Abundance Observations can be used to constrain the “normal” matter density - *the free parameter in the theory* - independent of WMAP



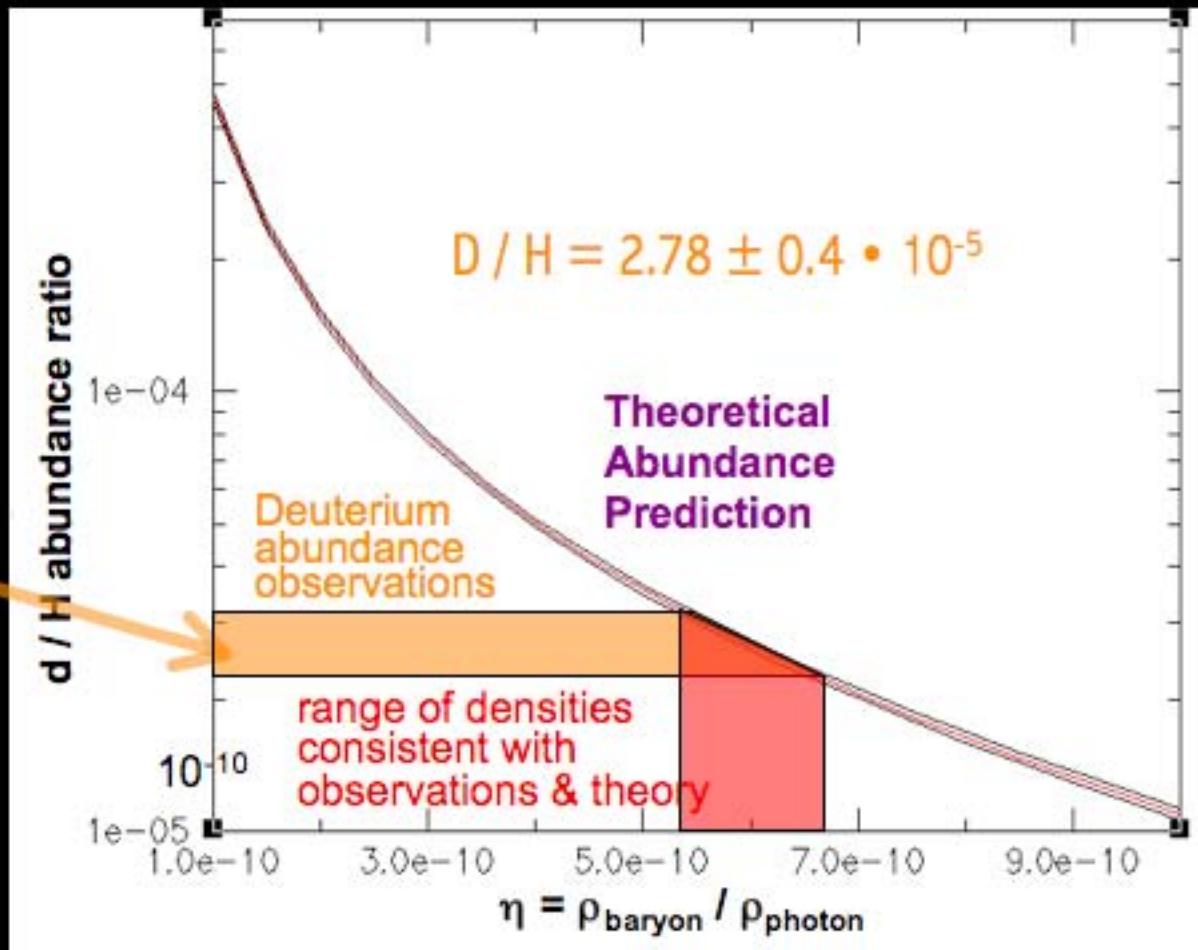
Quasi-Stellar Object (QSO)



"Primordial" Interstellar
Gas Cloud
(absorbs light)

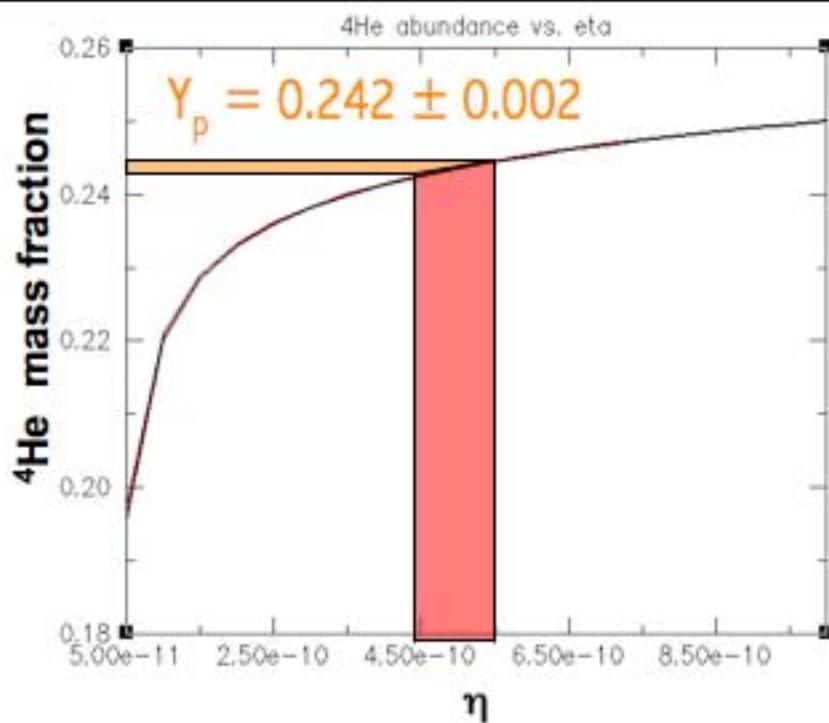


Keck Telescopes

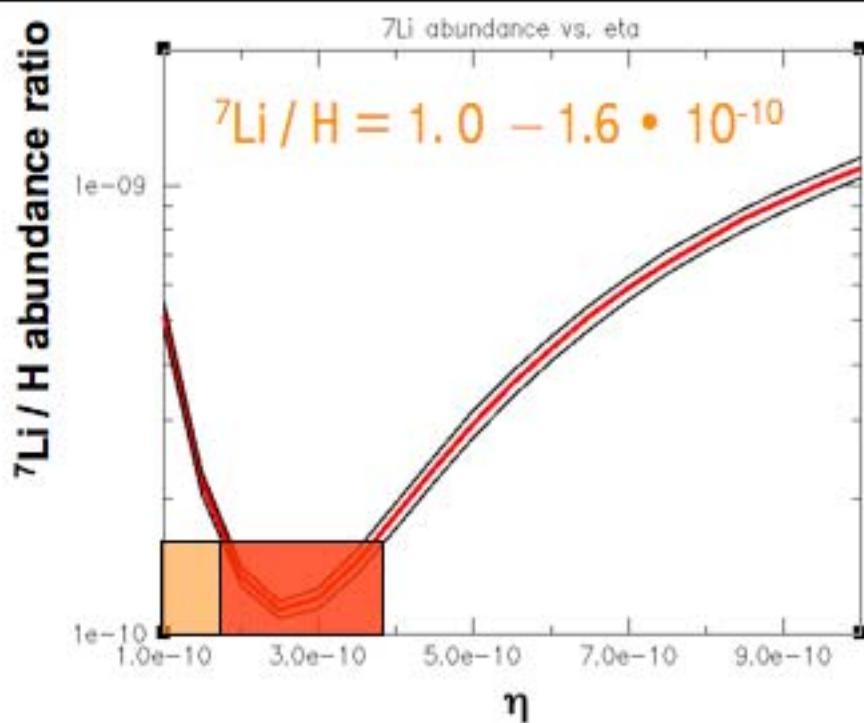


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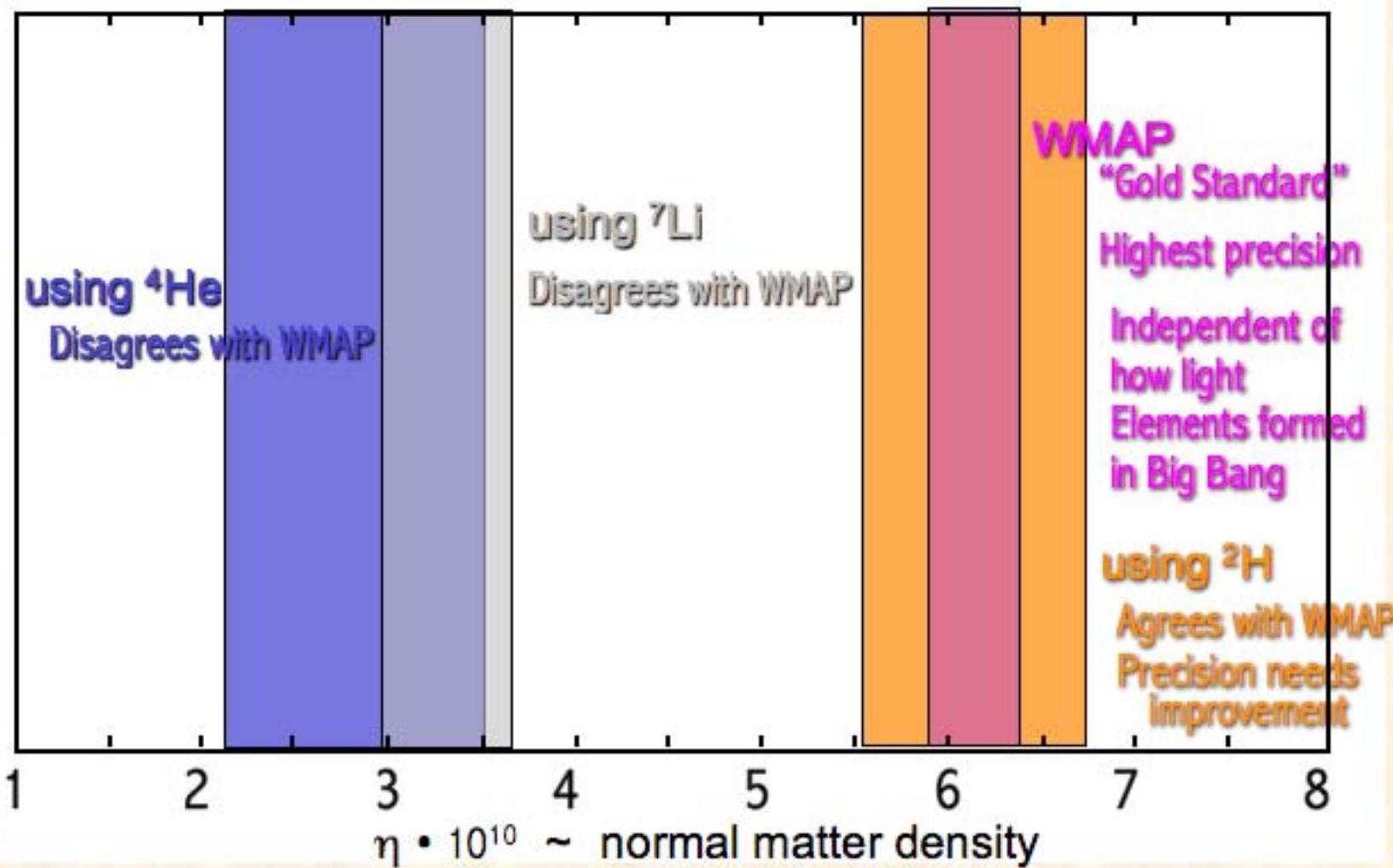
^4He : relatively weak constraint
but good observations?



^7Li : good constraint on
baryonic matter density



Comparing Matter Density Constraints



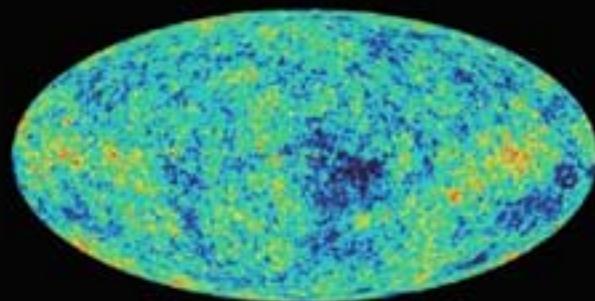
Is our understanding of dark energy / dark matter is wrong?

Are our observations / interpretations wrong?

Are there problems with our nuclear reaction network?

BIG BANG ONLINE

WELCOME ————— COMPUTE ————— RESOURCES



BIGBANGONLINE.ORG
where you use light element abundances
to constrain important Cosmological
parameters

C O M P U T E
Create, run, visualize, and share custom
Cosmology calculations using Big Bang
Nucleosynthesis theory

R E S O U R C E S
for Big Bang Nucleosynthesis
and related Cosmology studies

New online suite of cosmology codes under
development at **bigbangonline.org**

Enables users to **run** and **visualize** BBN calculations with
choice of reaction rates
choice of primordial abundance observations
choice of standard BBN or some non-standard variants

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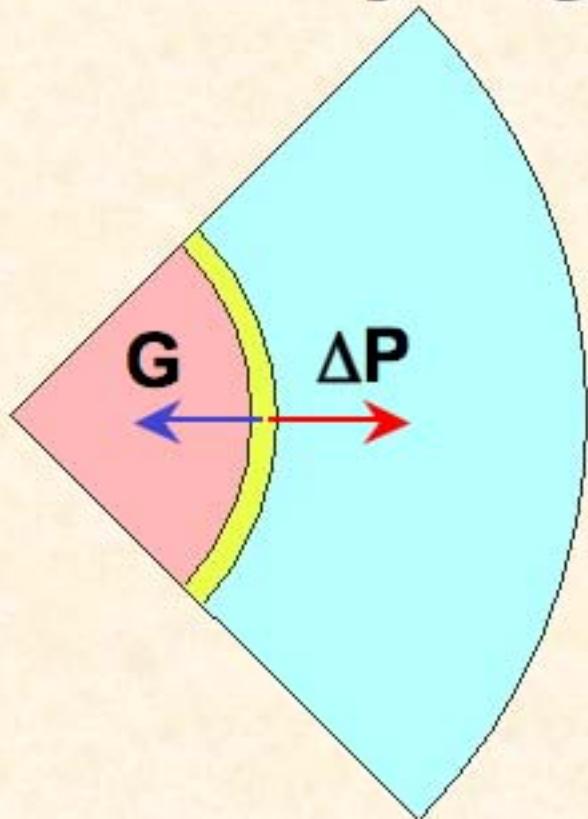
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Hydrogen burning in stars



Large T,P gradient

Opacity: photons absorbed and emitted at shorter λ

Luminosity-opacity/T relationship $\rightarrow L \propto M^4$

Hydrostatic equilibrium

$$\frac{dP(r)}{dr} = -\frac{GM_{in}(r)\rho(r)}{r^2}$$

Energy conservation

$$\frac{dL(r)}{dr} = \frac{\varepsilon(r)\rho(r)}{4\pi r^2}$$

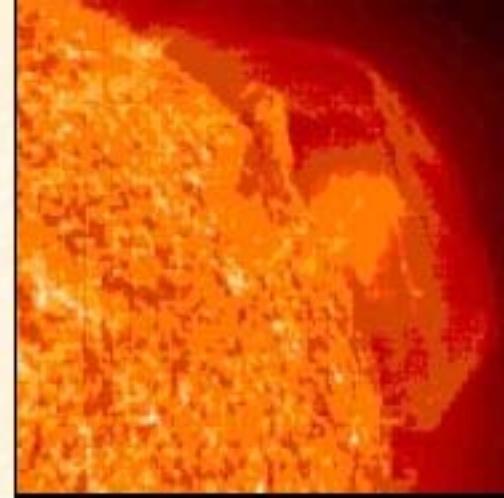
Pressure

$$P(r) = P_{gas}(r) + P_{rad}(r)$$

For sun (non-degenerate)

$$P_{gas}(r) = \frac{k}{\langle m \rangle} \rho(r)T(r)$$

$$P_{rad}(r) = \frac{1}{3}aT^4(r) \ll P_{gas}(r)$$



The sun

$M=2 \times 10^{30}$ kg

$\rho(0)=150$ g/cm³

$T(0)=1.5 \times 10^7$ K

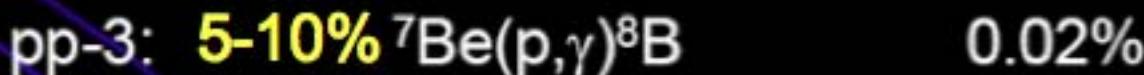
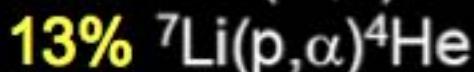
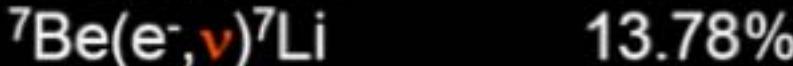
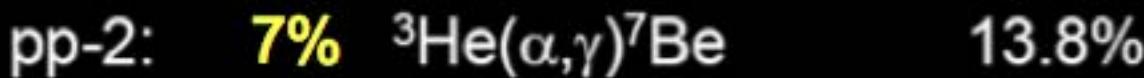
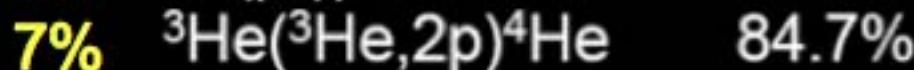
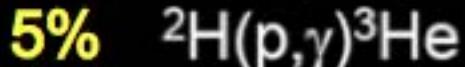
$T(\text{surf})=5800$ K

$L=3.8 \times 10^{26}$ W

5×10^4 yr for energy produced in sun's core to be radiated at surface

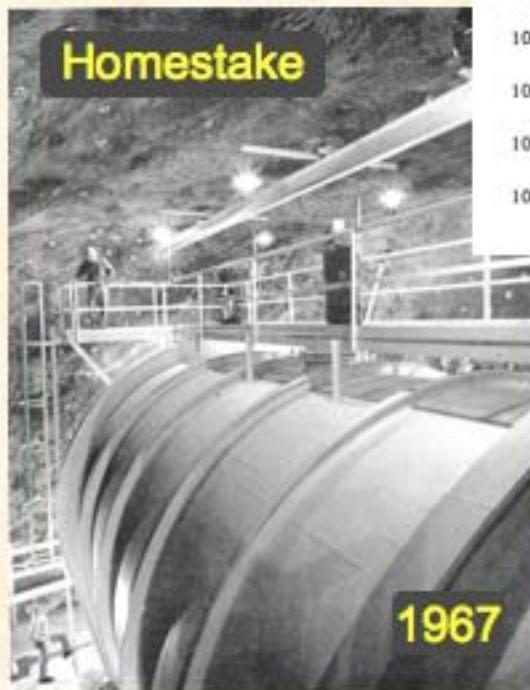
Solar power: The pp-chains

Thanks to substantial efforts in experiment, theory & evaluation

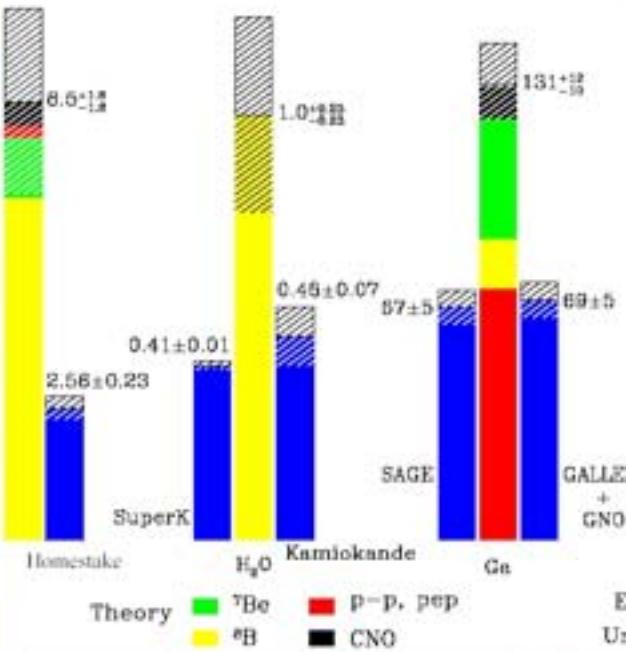
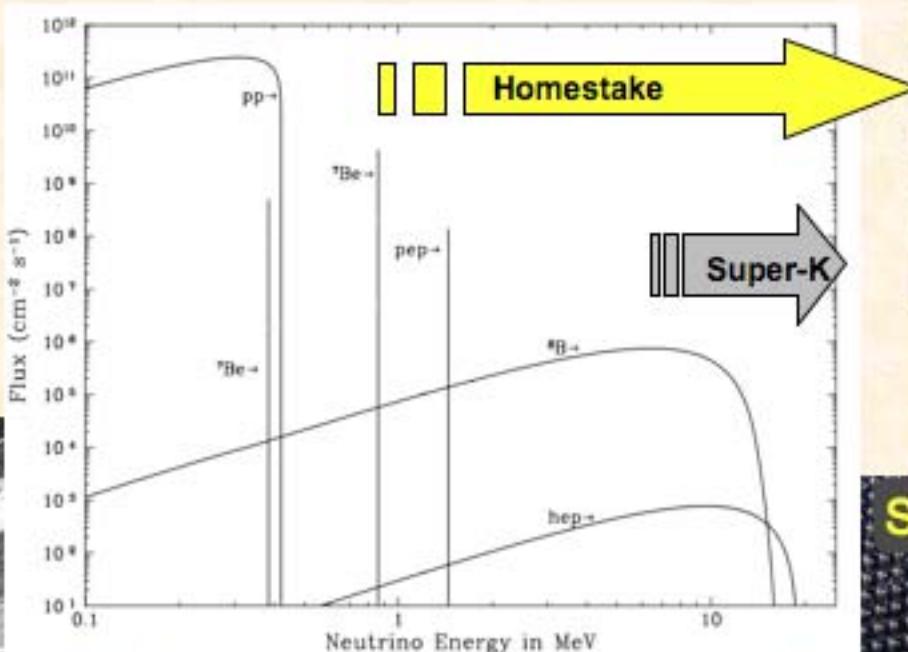


fusion of $4 \ ^1\text{H} \rightarrow 4\text{He} + 2\text{e}^+ + 2\nu\text{e} + 26.7 \text{ MeV}$ energy release

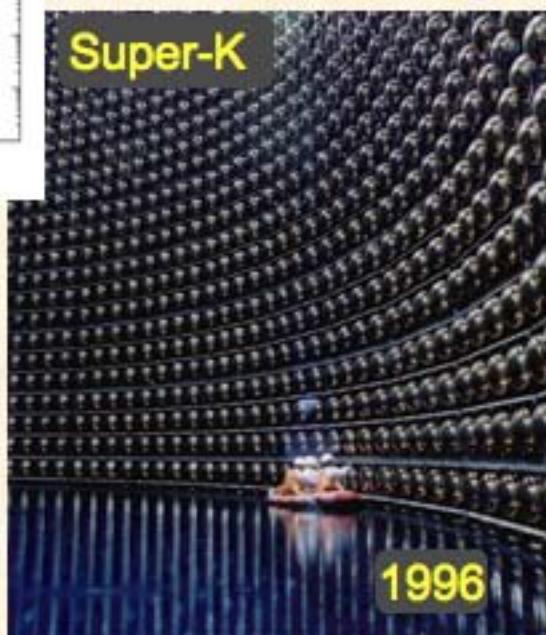
$6 \times 10^9 \nu_e / \text{cm}^2/\text{s}$
only direct probe
of solar core



Homestake Gold Mine
600kt perchloroethylene
100 events/yr
 $^{37}\text{Cl} + \nu_e \rightarrow ^{37}\text{Ar} + e^-$
~30% expectations

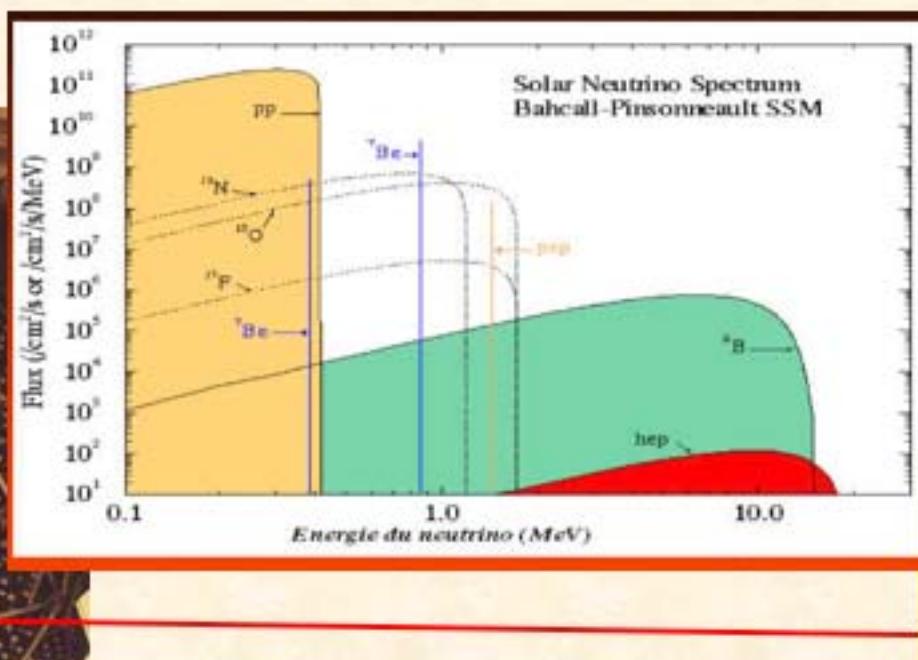
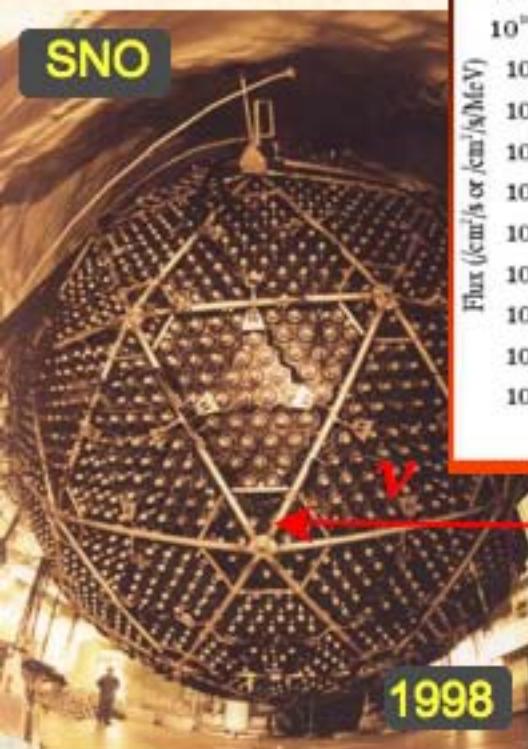


Real-time counting



Mozumi Mine
50,000 kt water
5,000 events/yr
 $\nu_e + e^-$ scattering
~40% expectations

SNO & SuperK measure only neutrinos from the decay of ${}^8\text{B}$



A accurate value for the predicted ${}^8\text{B}$ neutrino flux is need for comparison to the current generation of measurements

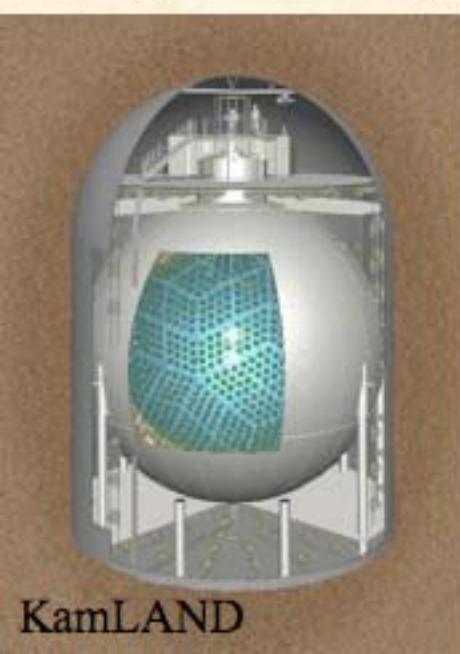
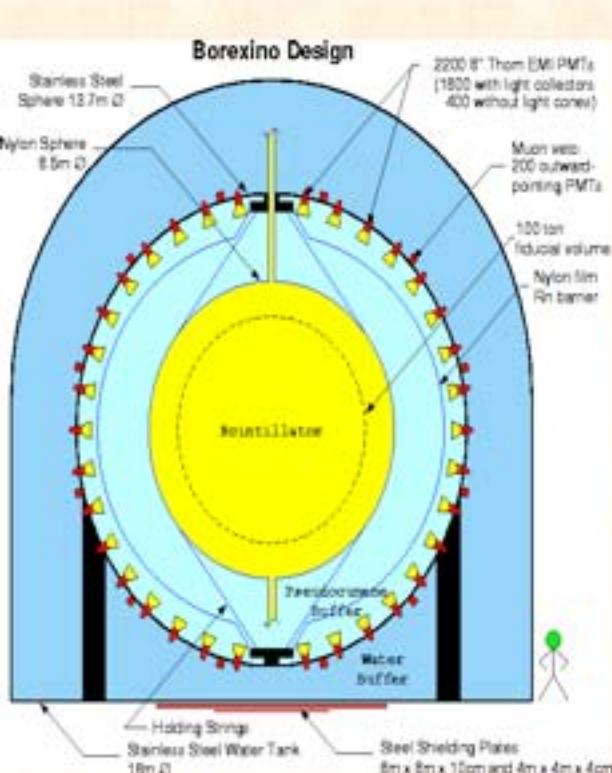
Creighton Nickel Mine
1 kt heavy water
 $\nu_x + d \rightarrow p + n$



$$\text{SuperK} \rightarrow \Phi_{\text{CC}} = (2.39 \pm 0.03_{\text{stat}} \pm 0.06_{\text{sys}}) \times 10^6 /(\text{cm}^2\text{s})$$

$$\text{SNO} \rightarrow \Phi_{\text{NC}} = (5.21 \pm 0.27_{\text{stat}} \pm 0.38_{\text{sys}}) \times 10^6 /(\text{cm}^2\text{s})$$

$$\Phi_{\text{SSM}} = 5.7 \times 10^6 /(\text{cm}^2\text{s}) \pm \sim 15\% \text{ metallicity reaction rates}$$



Flavor oscillation

- Neutrino mass eigenstates not the same as flavor eigenstates

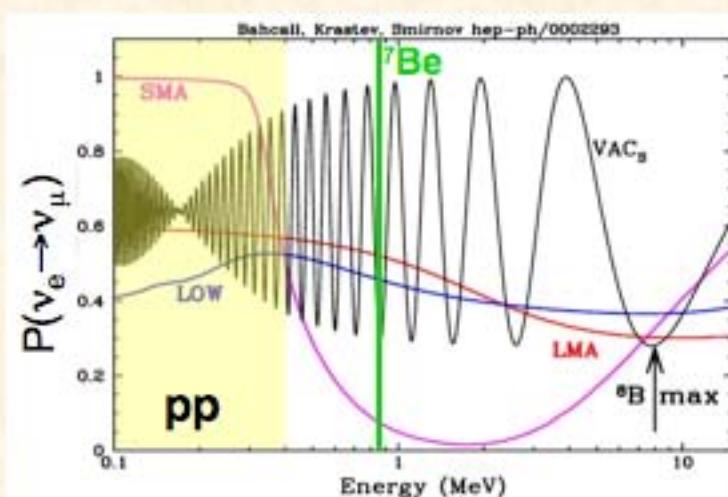
$$\text{In vacuum} \quad P(\nu_\alpha \rightarrow \nu_\beta) = \sin^2 2\theta \sin^2 \left(\frac{1.27 \Delta m^2 (eV^2) L(km)}{E_\nu (GeV)} \right)$$

- Strong evidence from observations of atmospheric neutrinos ($\nu_\mu \rightarrow \nu_\tau$)
- Observed in reactor experiments: KamLAND & Chooz
- Oscillations of solar (${}^8\text{B}$) neutrinos are enhanced by interactions with the high density of electrons in the solar core MSW: Mikheyev & Smirnov, SJNP 42 (85). Wolfenstein, PRD 17 (78).

${}^{7}\text{Be}$ = Focus of current experiments

KamLAND
Borexino

pp = Next-generation
CLEAN
LENS



"There are rare moments in science when a clear road to discovery lies ahead and there is broad consensus about the steps to take along that path. This is one such moment."

nation of parameters. The programs are complementary because only the U.S. program has sufficiently long baselines to provide good sensitivity to the mass hierarchy through matter enhancement. With both the U.S. and international programs, we may confidently anticipate a thorough understanding of neutrino mixing.

- We recommend the development of a spectroscopic solar neutrino experiment capable of measuring the energy spectrum of neutrinos from the primary pp fusion process in the sun.

adequate underground ta

A coordinated program has enormous discovery naturally upon the success of the U.S. program. It is circumstance that the question of science can be so clearly formulated and so directly addressed.



One of the 3 major recommendations

- The pp neutrino flux is accurately predicted by the solar luminosity.
- pp neutrinos oscillate (primarily) by vacuum oscillations not MSW oscillations.
- Would provide a clear test of solar physics, hydrostatic equilibrium, etc.
- Is the sun's energy output now the same as 50,000 years ago?

Measuring the pp flux: CLEAN

McKinsey & Coakley, Astroparticle Physics 22 (2005) 355.

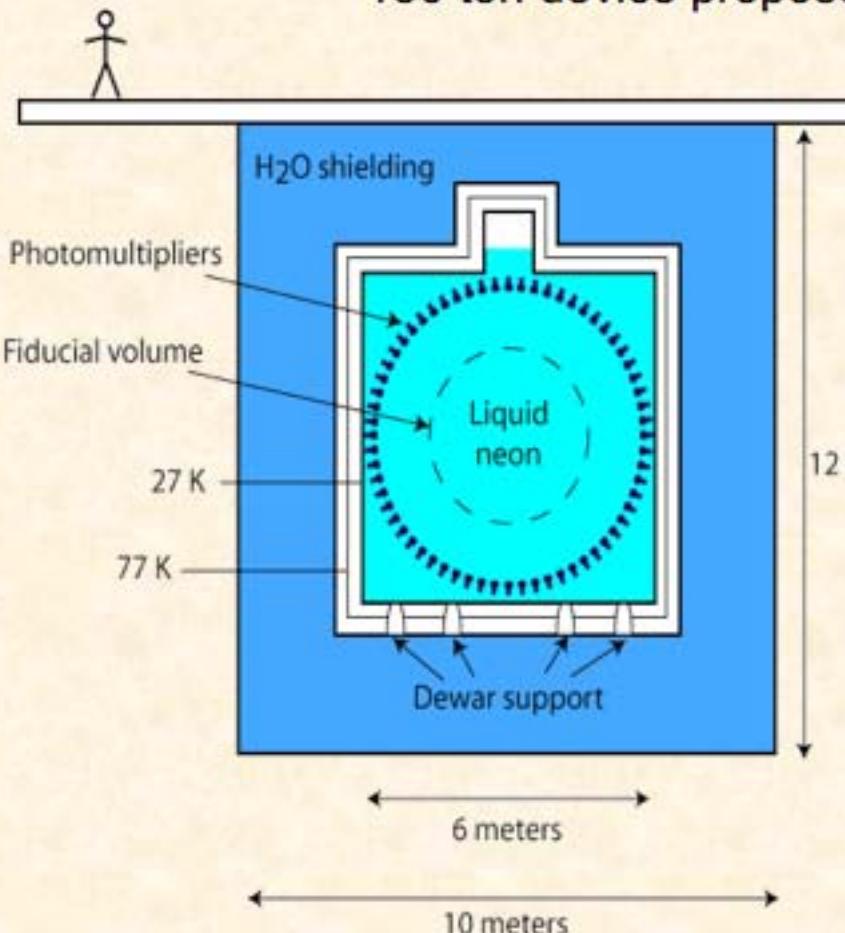
Very high purity liquid Ne or Ar

Thin film of shifting flour in front of PMTs

Good recoil/electron discrimination

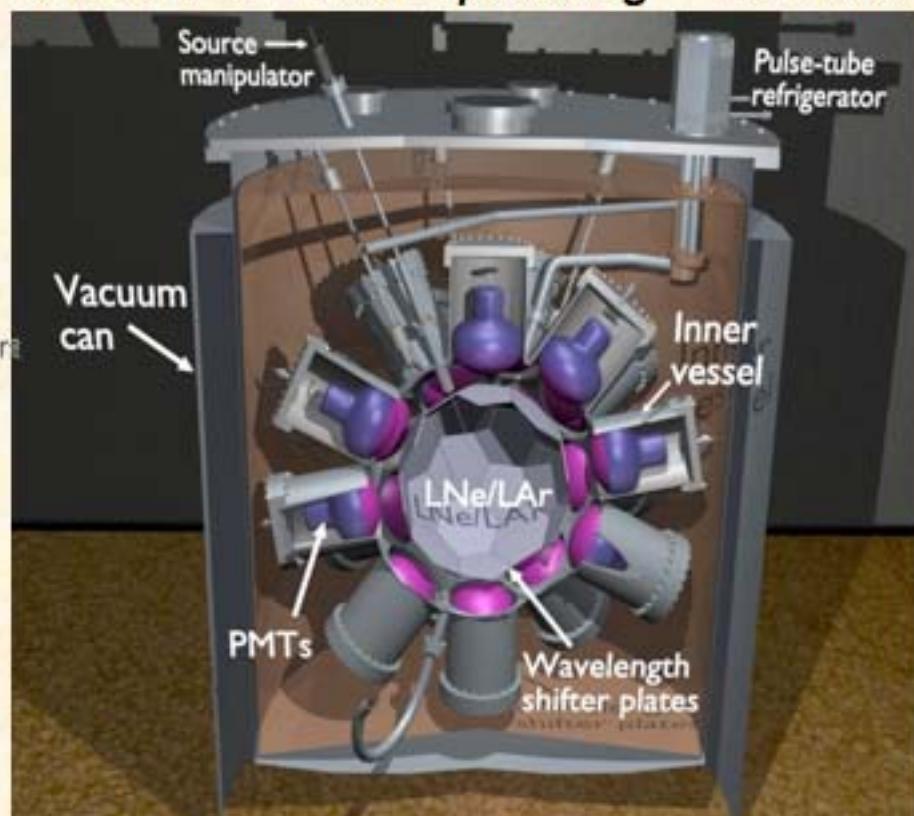
Very low threshold (few 10's keV)

130 ton device proposed (either SNO-Lab or DUSEL)



MiniCLEAN now operating

65 liters



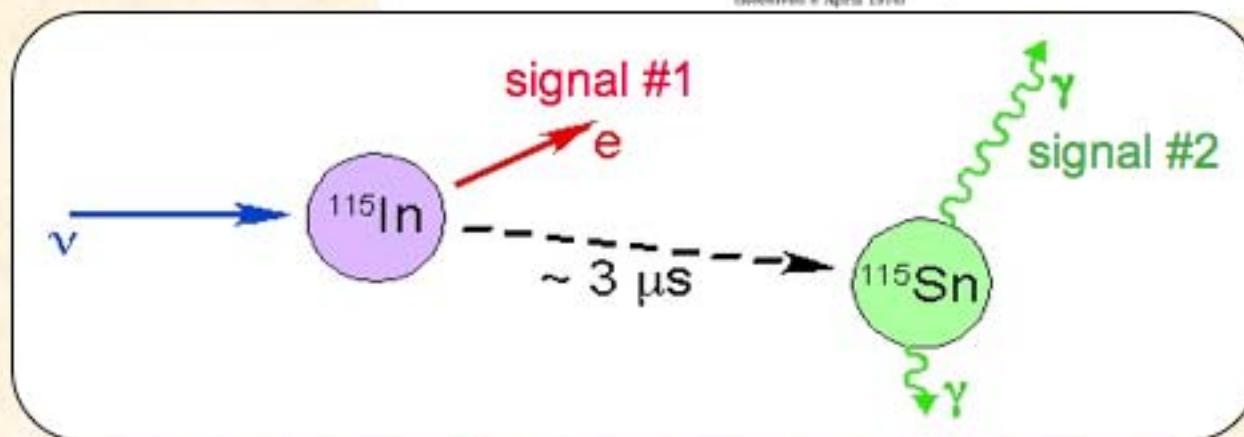
LENS: ν_e from pp fusion

#1 prompt electron
 $\rightarrow \nu_e$ energy (β -like)

Buffer up to $10\mu\text{s}$
 Shower

Time/space correlation

→ discrimination



Now: 8% In-loaded scintillator

Background

$2x^{115}\text{In}$ decays

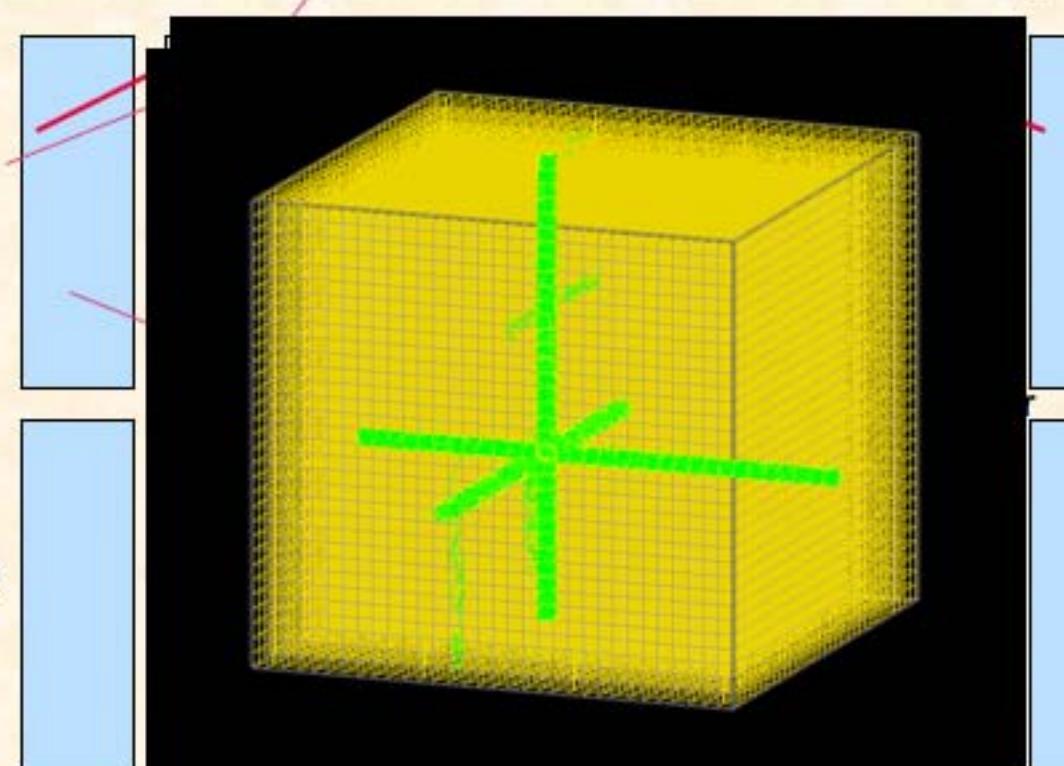
1 mimics prompt e

1 mimics γ cascade

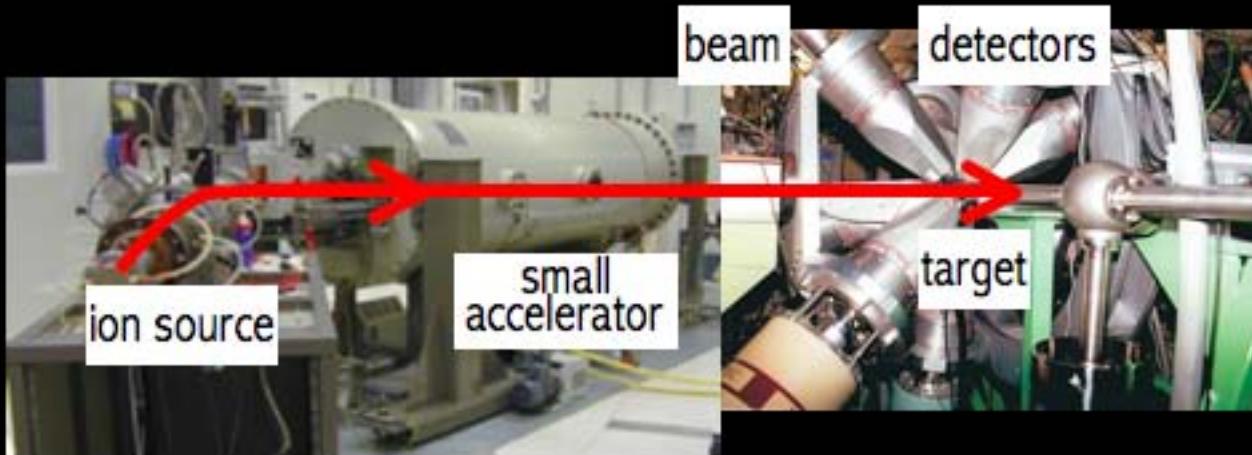
→ high segmentation

3D array of transparent cells

$(\sim 6 \text{ m})^3$ fiducial volume = ~ 15 tons In
 $\sim 500 \nu_{pp}$ events/yr



Nuclear Physics Laboratory Measurements



Directly measure cross sections in the lab at the lowest possible energies

Bombarding energy range $\sim 10 \text{ keV}$ to 3 MeV

High currents ($\sim \text{mA}$)

Long run times

Efficient detectors to obtain high statistics

Pure, stable targets

Absolute cross section measurements

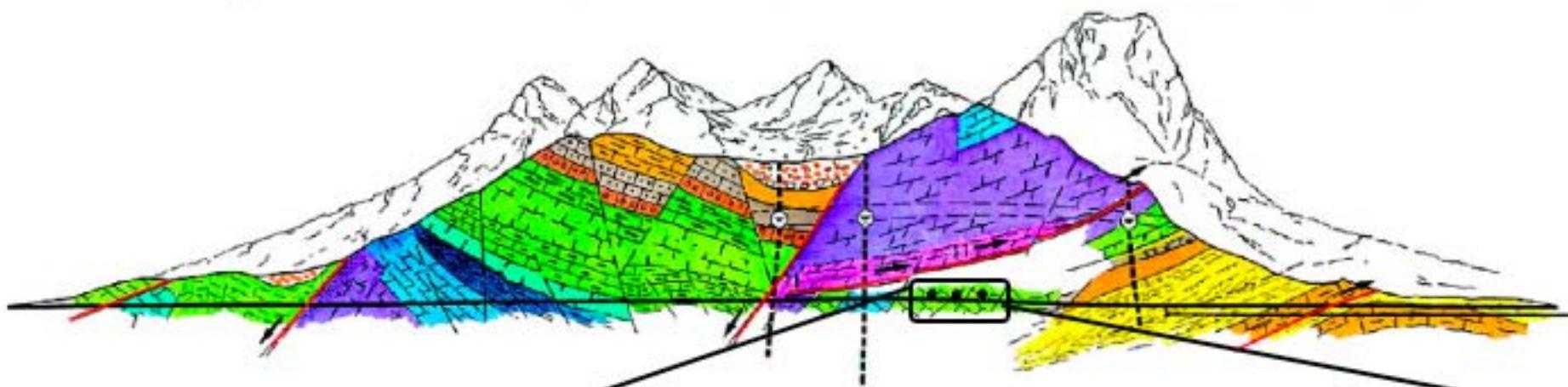
Good normalization & careful control of
systematic uncertainties

Background suppression crucial



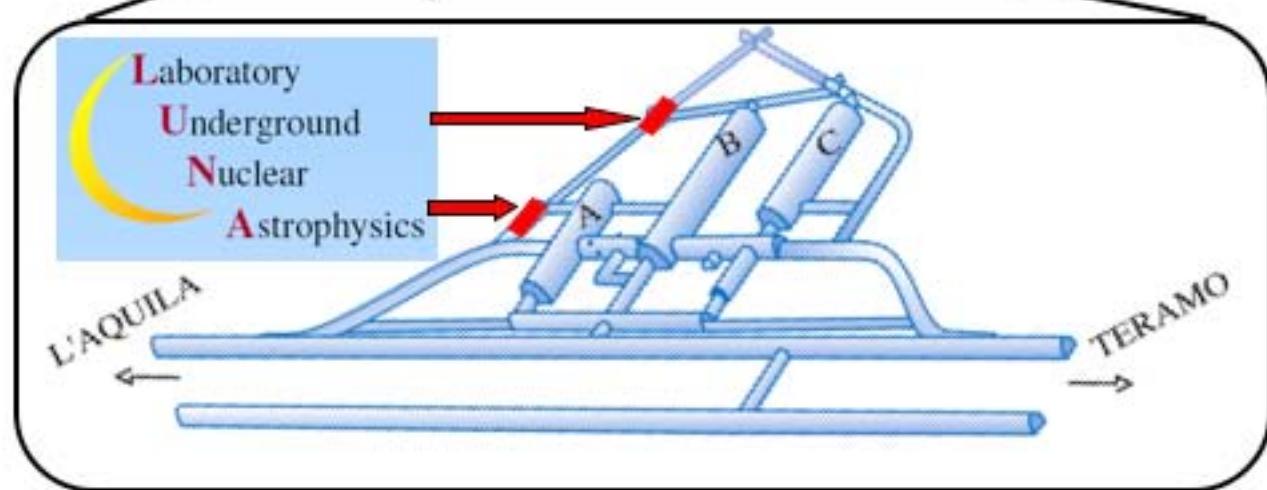


Laboratori Nazionali del Gran Sasso



Laboratory space adjacent
to highway tunnel

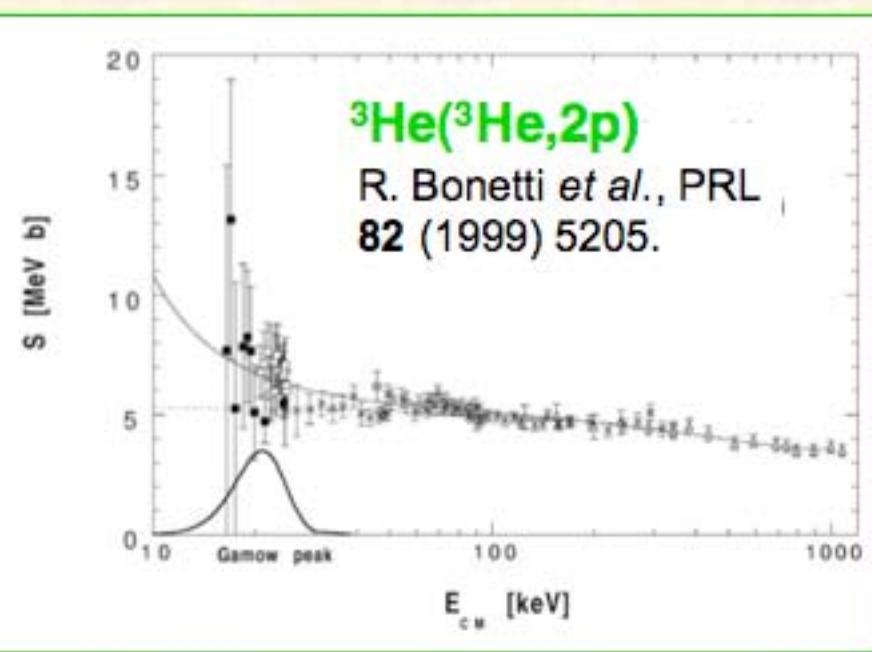
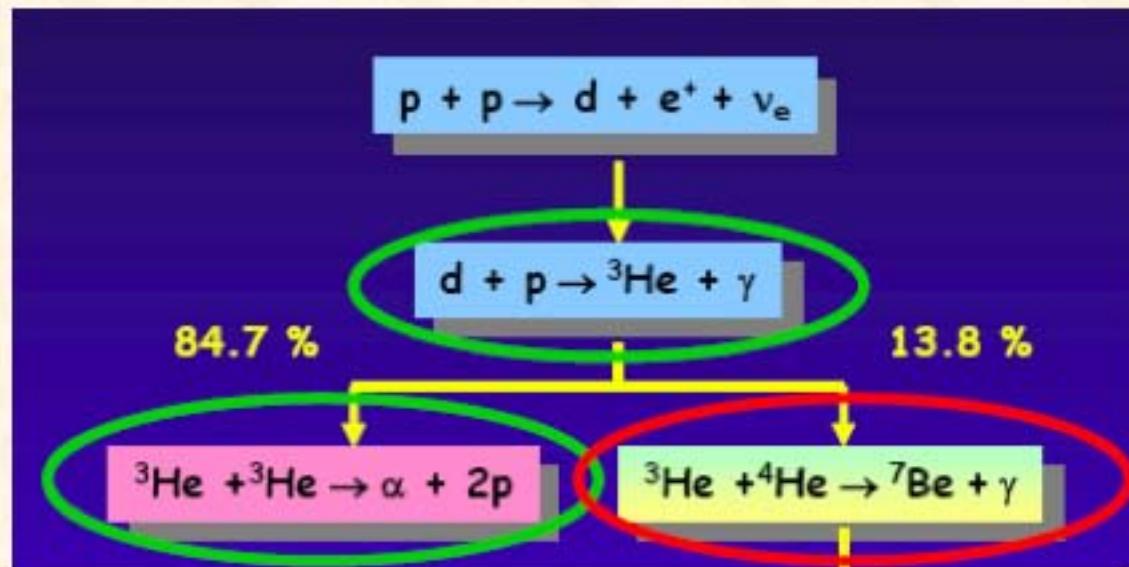
1400 m rock coverage
cosmic μ reduction = 10^{-6}
 μ rate ~ 1 (/m² h)



Low-energy accelerators at LNGS

50 keV accelerator

First σ
measurements
in solar
Gamow widow

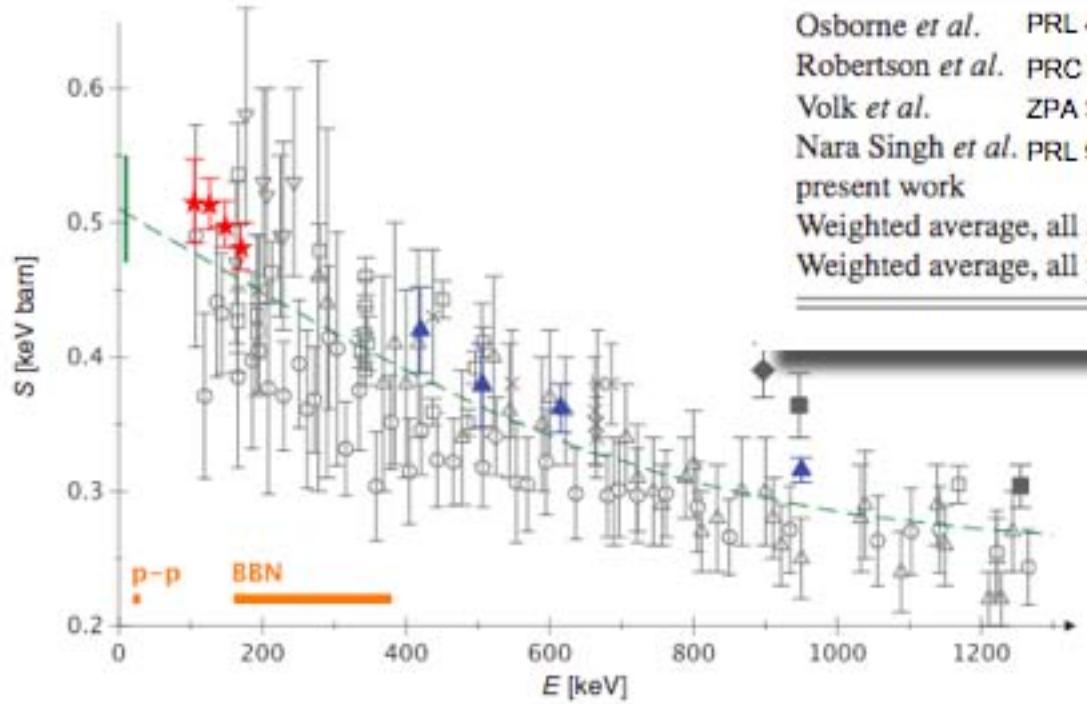
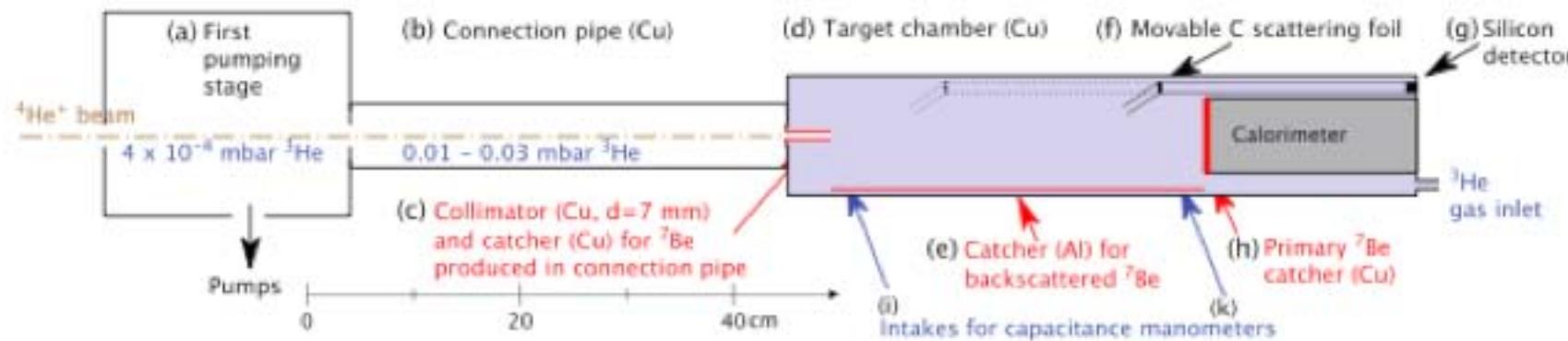


${}^3\text{He}(\alpha, \gamma){}^7\text{Be}$ with
400 keV accelerator



$^3\text{He}(\alpha, \gamma)^7\text{Be}$ @ LUNA

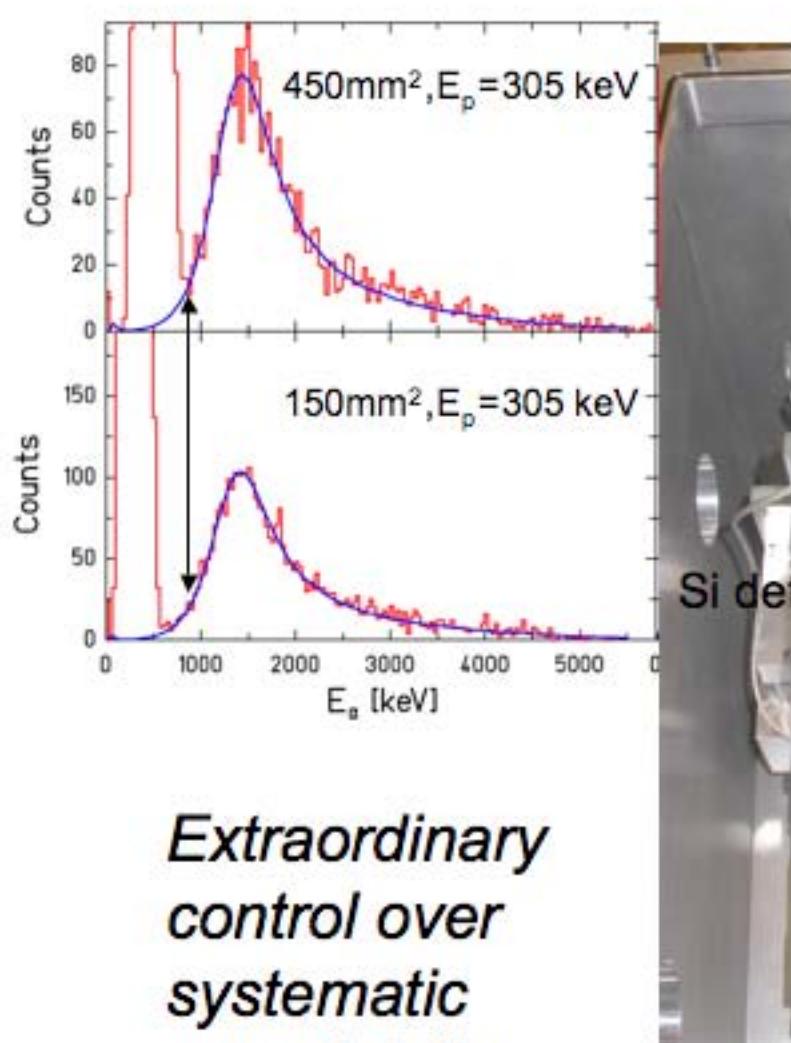
Gy. Gyürky, PRC 75 (2007) 035805.



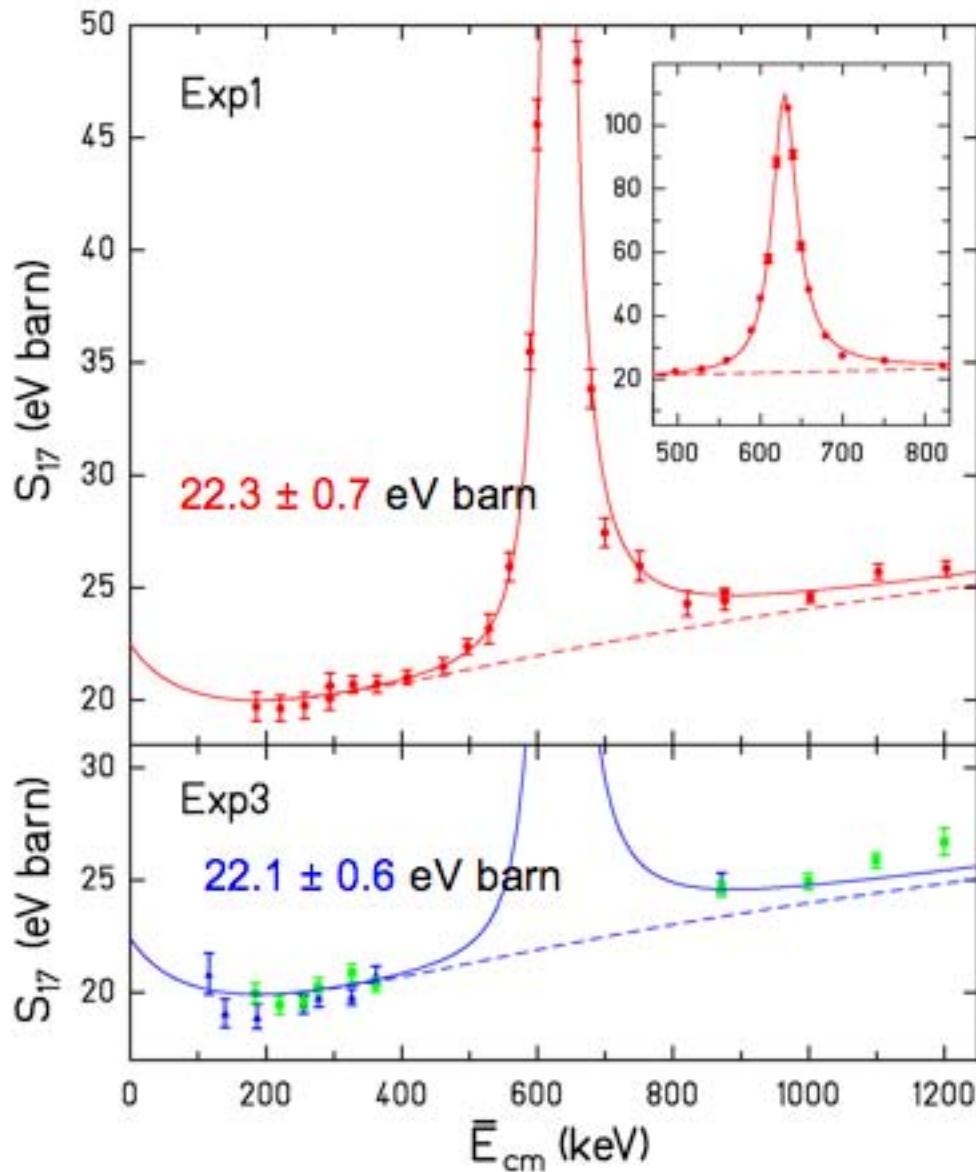
	Ref.	$S(0)$ (keV b)
Osborne <i>et al.</i> PRL 48 (1982)	[18]	0.535 ± 0.040
Robertson <i>et al.</i> PRC 27 (1983)	[19]	0.63 ± 0.04
Volk <i>et al.</i> ZPA 310 (1983)	[20]	0.56 ± 0.03
Nara Singh <i>et al.</i> PRL 93 (2004)	[21]	0.53 ± 0.02
present work		0.547 ± 0.017
Weighted average, all activation studies		0.553 ± 0.012
Weighted average, all prompt- γ studies	[3]	0.507 ± 0.016

$^{7}\text{Be}(p,\gamma)^{8}\text{B}$ at Seattle

Junghans et al., PRC
68 (2003) 065803.

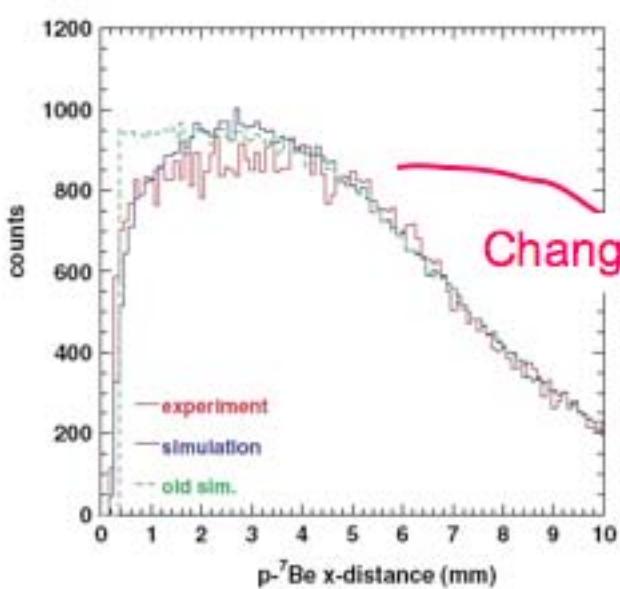
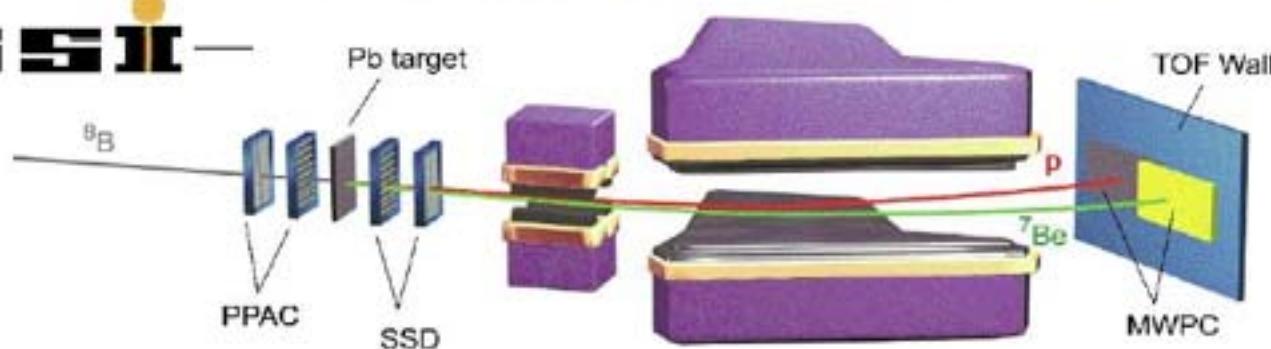


*Extraordinary
control over
systematic
uncertainties.*

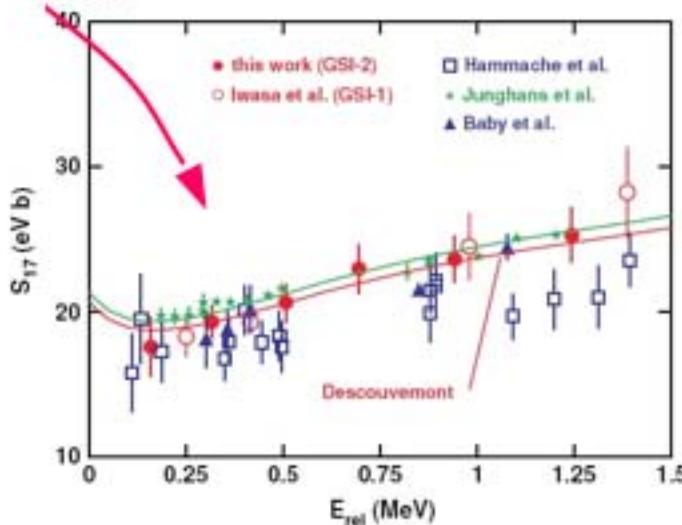
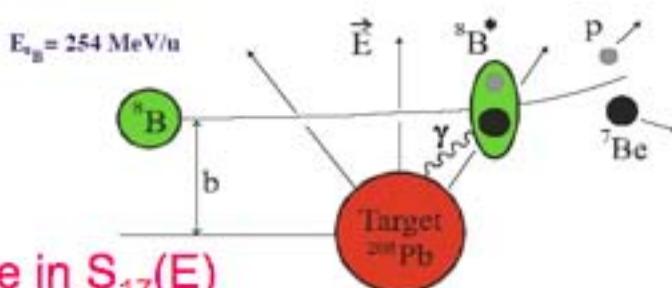


New Coulomb dissociation result

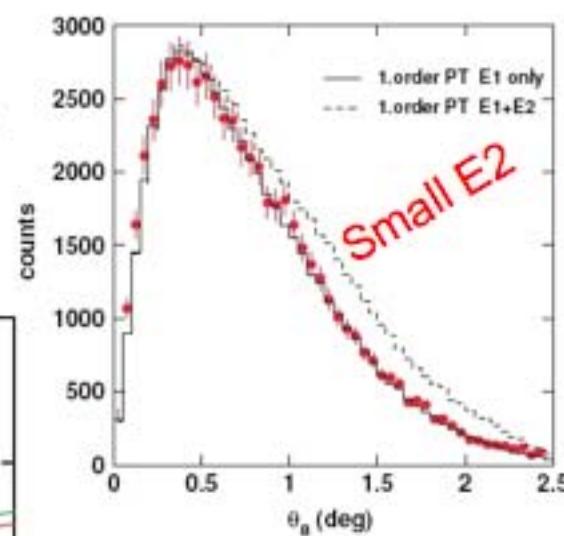
Schumann et al., PRC 73 (2006) 015806.



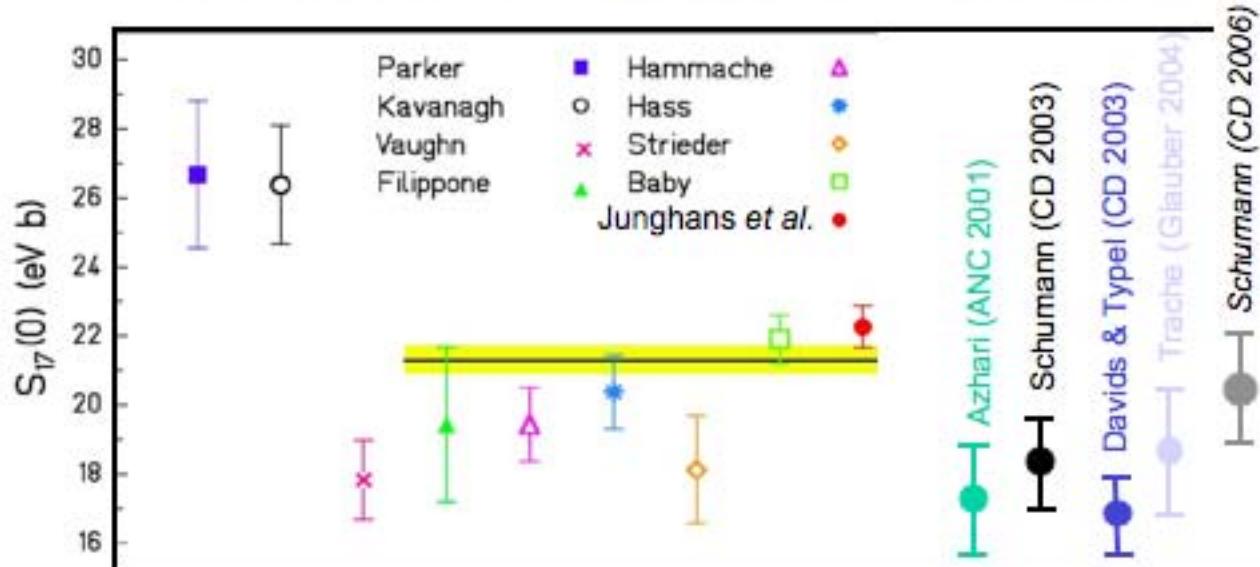
Change in $S_{17}(E)$



$20.6 \pm 0.8 \pm 1.2$ eV b



Recent ${}^7\text{Be}(p,\gamma){}^8\text{B}$ results



Evaluated S_{17} (eV b)

Junghans PRC 68 (2003) 065803. $21.4 \pm 0.5 \pm 0.6$

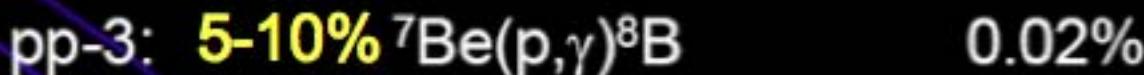
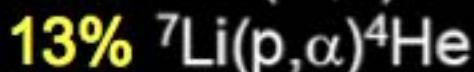
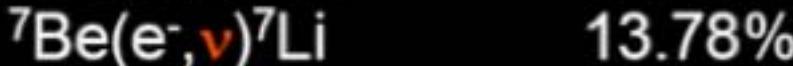
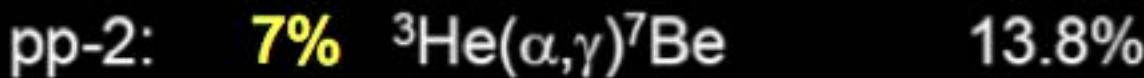
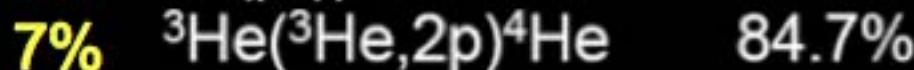
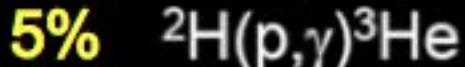
Davids & Typel PRC 68 (2003) 045802. $18.6 \pm 0.4 \pm 1.1$

Cyburt et al., PRC 70 (2004) 045801. $19.3 \rightarrow 21.4$
with $\sim 6\text{-}7\% \sigma$

- Precision has been significantly improved.
- Some questions remain.
- Additional high-precision measurement(s) are desired.

Solar power: The pp-chains

Thanks to substantial efforts in experiment, theory & evaluation



fusion of $4 \ ^1\text{H} \rightarrow 4\text{He} + 2\text{e}^+ + 2\nu\text{e} + 26.7 \text{ MeV}$ energy release

