



# SEARCHING FOR AND MEASURING GRAVITATIONAL WAVES OPPORTUNITIES AND CHALLENGES

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on behalf of the LIGO Scientific Collaboration and Virgo Collaboration

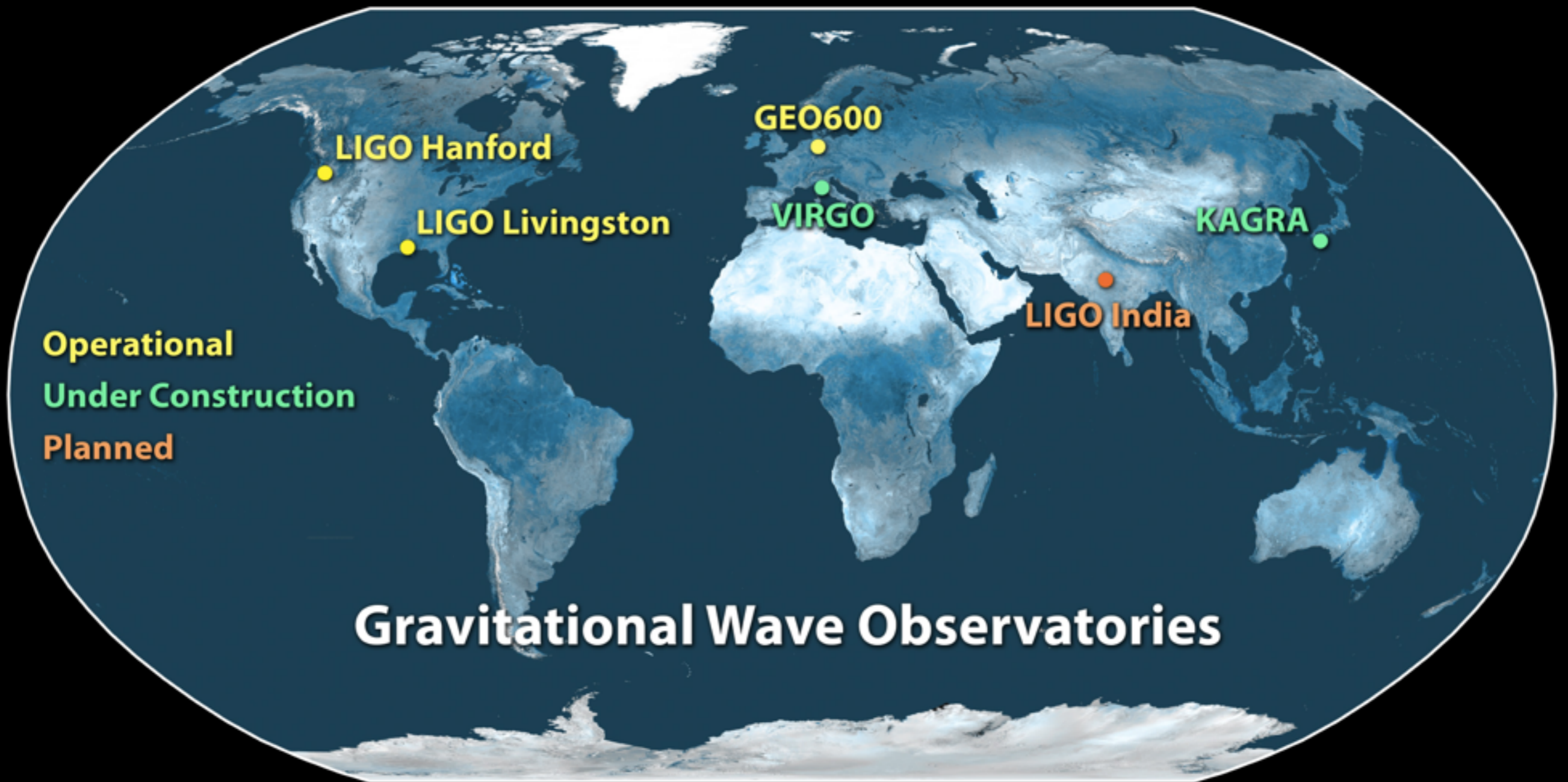


# OVERVIEW

- LIGO has taken about 165 days worth of data over two observing runs
  - made five discoveries of
- LIGO and Virgo jointly took data during 1-25 August 2017
  - a network of three (or more ) detectors is essential for full reconstruction of the incident gravitational wave
    - LIGO and Virgo have data sharing agreements
    - they make each others data available within seconds of data taking
  - LIGO and Virgo jointly detected GW170814 and GW170817
- ~~GW170814 another binary black hole merger~~
  - ~~detected in triple coincidence, localized to a factor of 30 better than LIGO alone, 3 detectors give polarization~~
- GW170817 - first observation of a binary neutron star merger
  - beginning of multi-messenger astronomy with gravitational waves

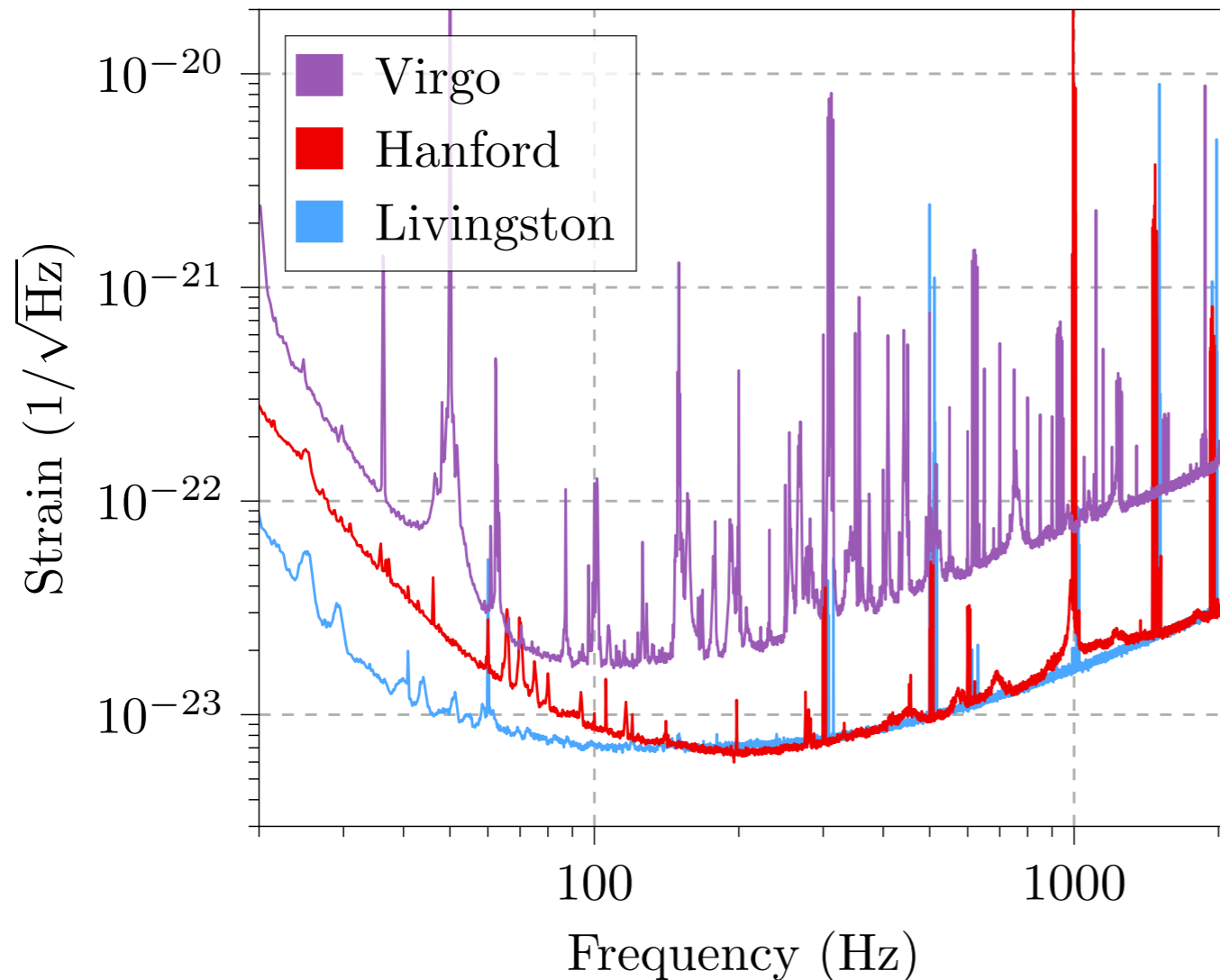
AND THEN THERE WERE THREE ...

# GW INTERFEROMETER NETWORK





# SENSITIVITY AND DISTANCE REACH TO BINARY NEUTRON STARS



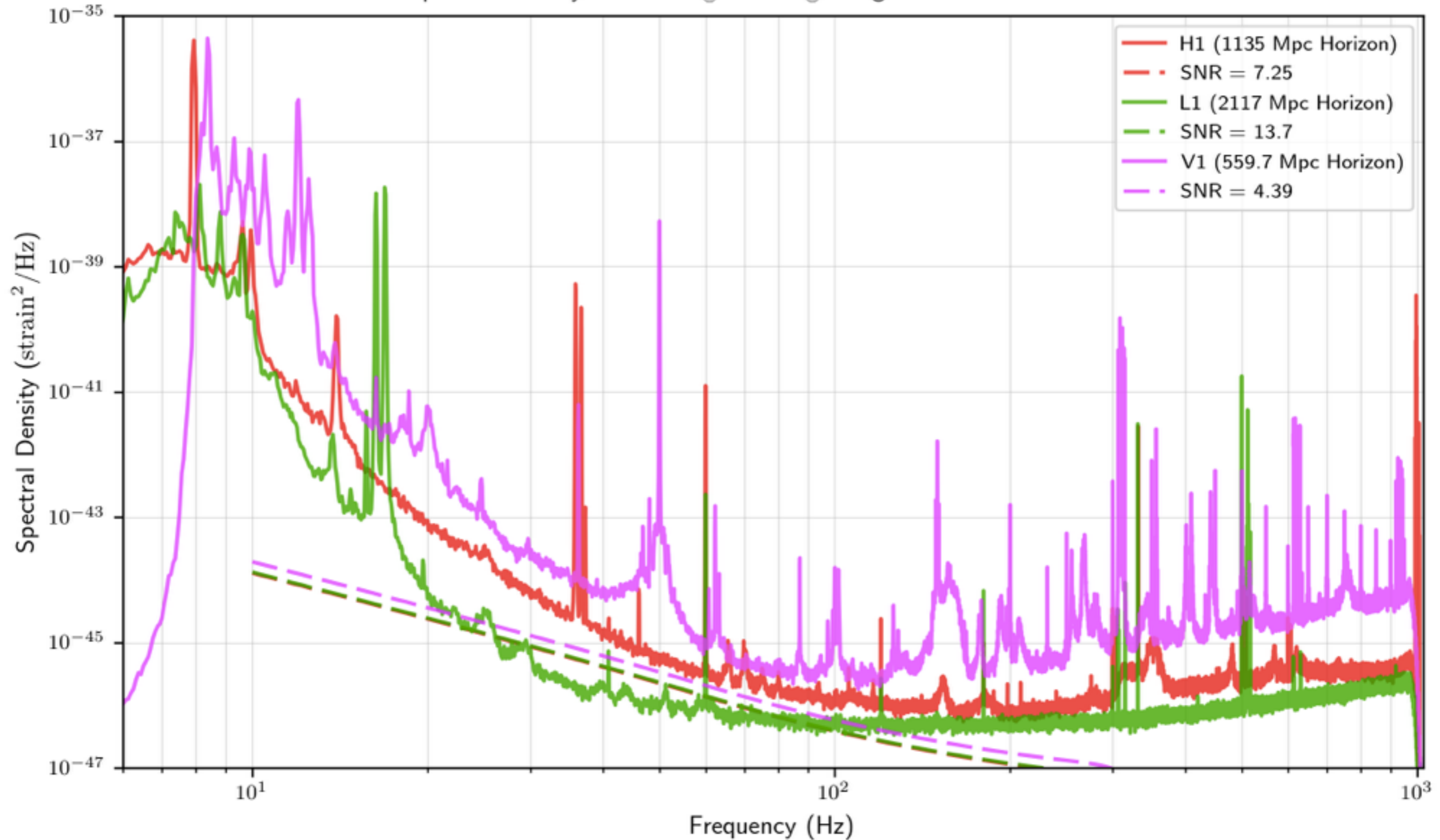
- horizon distance of a detector: distance at which a face-on, overhead binary would produce a signal to noise ratio of 8
- distance reach of a detector: a factor 2.33 smaller than horizon distance

Detector	Range	Horizon
LIGO Livingston	100 Mpc	230 Mpc
LIGO Hanford	50 Mpc	115 Mpc
Virgo	27 Mpc	63 Mpc

TWO WEEKS INTO THE RUN ...

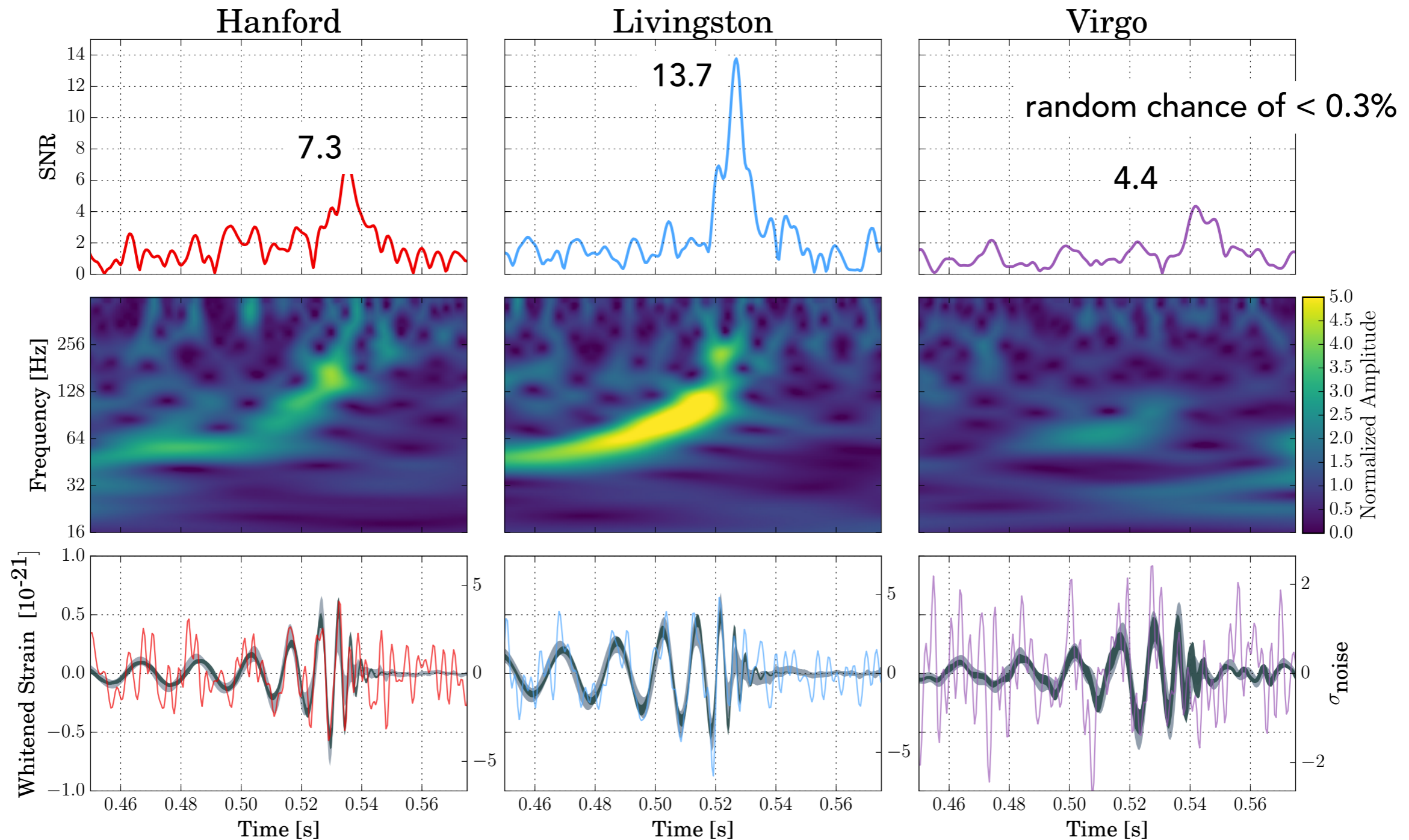
# GSTLAL REPORTS A CANDIDATE

Strain Noise Spectral Density for  $29.5 M_{\odot}-24.9 M_{\odot}$  Merger Candidate at 1186741861.53 GPS



# GW170814: DETECTION

THREE DETECTOR SIGNAL MODEL IS PREFERRED WITH BAYES FACTOR OF 1600  
Signal arrived on August 14, 2017 10:30:43 UTC at Livingston, 8 ms later at Hanford,  
14 ms later at Virgo; false alarm rate < 1 in 140,000 years

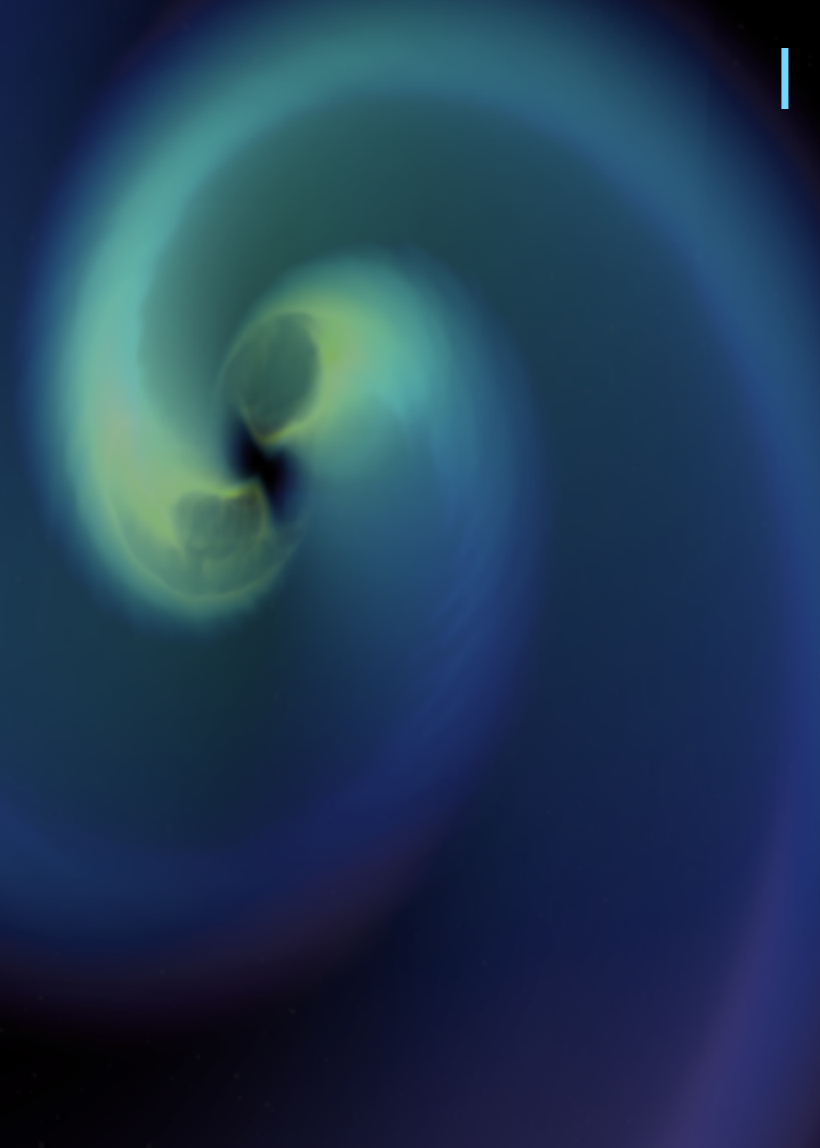


THREE DAYS AFTER GW170814 ...



FIRST COSMIC EVENT OBSERVED IN  
GRAVITATIONAL WAVES AND LIGHT

GW170817: AUGUST 17, 2017, 12:41:04 UTC  
FIRST OBSERVATION OF A NEUTRON STAR  
INSPIRAL





## GW170817: Observation of Gravitational Waves from a Binary Neutron Star Inspiral

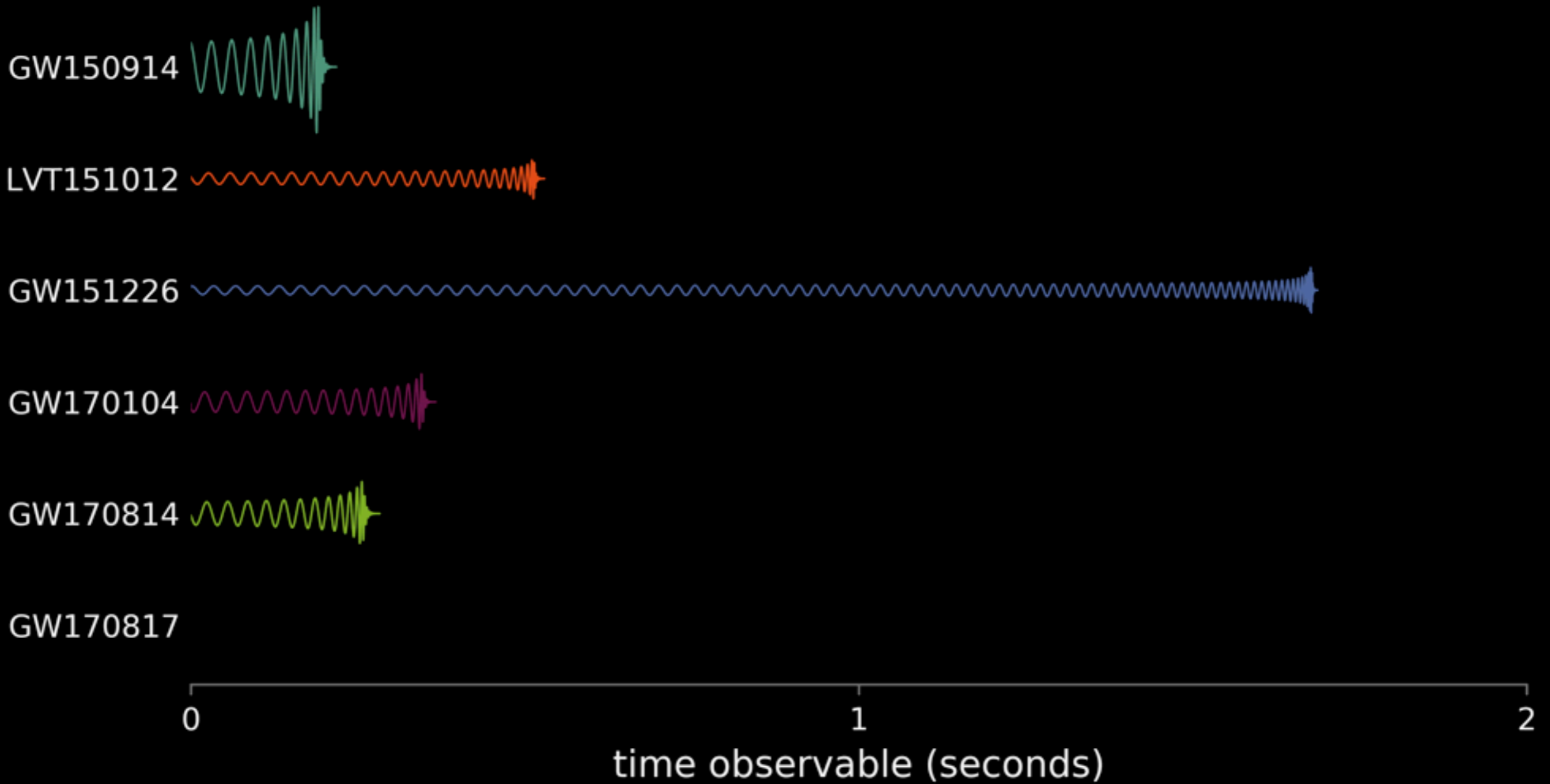
B. P. Abbott *et al.*\*

(LIGO Scientific Collaboration and Virgo Collaboration)

(Received 26 September 2017; revised manuscript received 2 October 2017; published 16 October 2017)

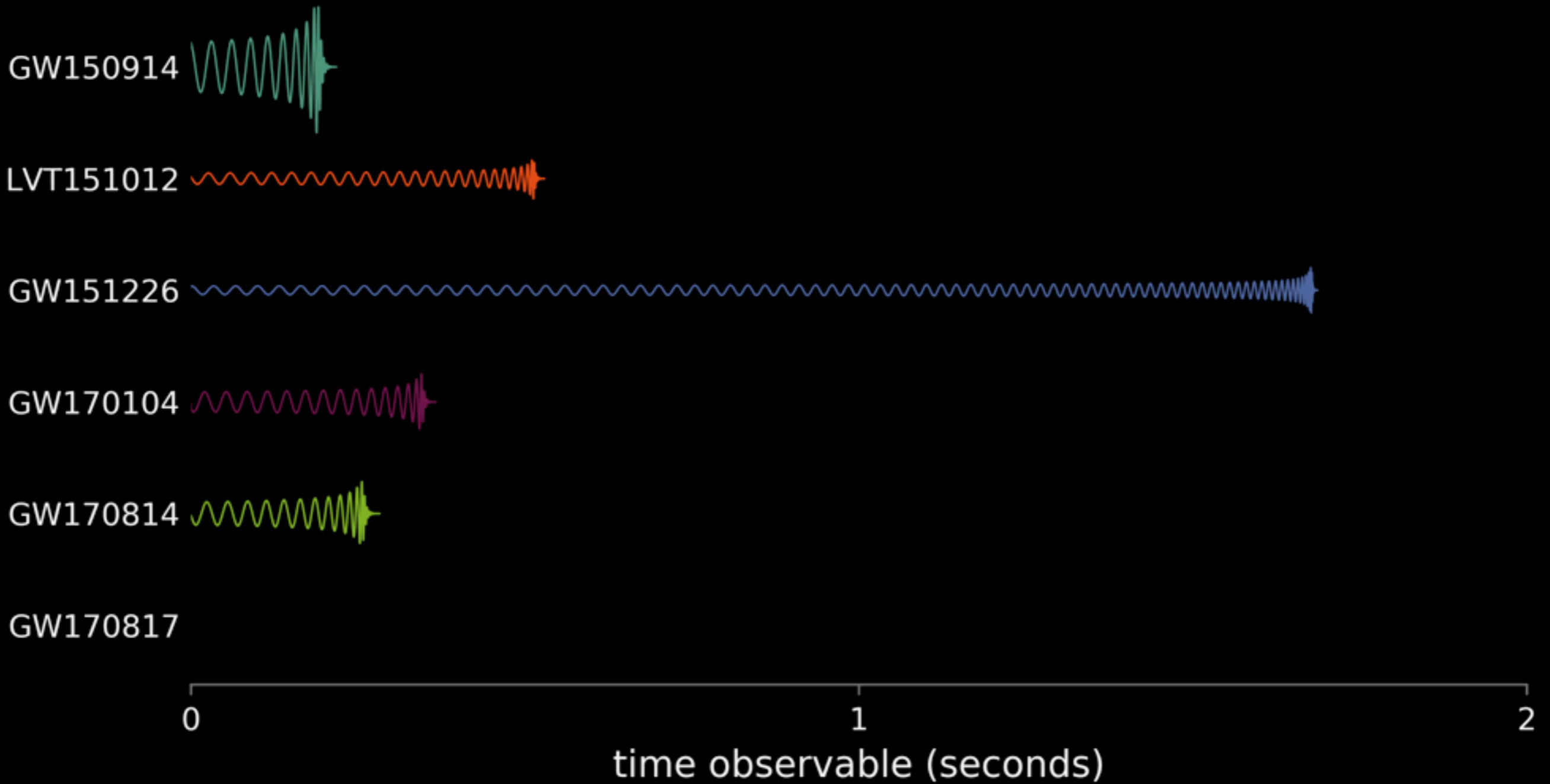
On August 17, 2017 at 12:41:04 UTC the Advanced LIGO and Advanced Virgo gravitational-wave detectors made their first observation of a binary neutron star inspiral. The signal, GW170817, was detected with a combined signal-to-noise ratio of 32.4 and a false-alarm-rate estimate of less than one per  $8.0 \times 10^4$  years. We infer the component masses of the binary to be between 0.86 and  $2.26 M_{\odot}$ , in agreement with masses of known neutron stars. Restricting the component spins to the range inferred in binary neutron stars, we find the component masses to be in the range  $1.17\text{--}1.60 M_{\odot}$ , with the total mass of the system  $2.74^{+0.04}_{-0.01} M_{\odot}$ . The source was localized within a sky region of  $28 \text{ deg}^2$  (90% probability) and had a luminosity distance of  $40^{+8}_{-14}$  Mpc, the closest and most precisely localized gravitational-wave signal yet. The association with the  $\gamma$ -ray burst GRB 170817A, detected by Fermi-GBM 1.7 s after the coalescence, corroborates the hypothesis of a neutron star merger and provides the first direct evidence of a link between these mergers and short  $\gamma$ -ray bursts. Subsequent identification of transient counterparts across the electromagnetic spectrum in the same location further supports the interpretation of this event as a neutron star merger. This unprecedented joint gravitational and electromagnetic observation provides insight into astrophysics, dense matter, gravitation, and cosmology.

# SIGNAL LASTED FOR SEVERAL MINUTES IN BAND



LIGO/University of Oregon/Ben Farr

# SIGNAL LASTED FOR SEVERAL MINUTES IN BAND

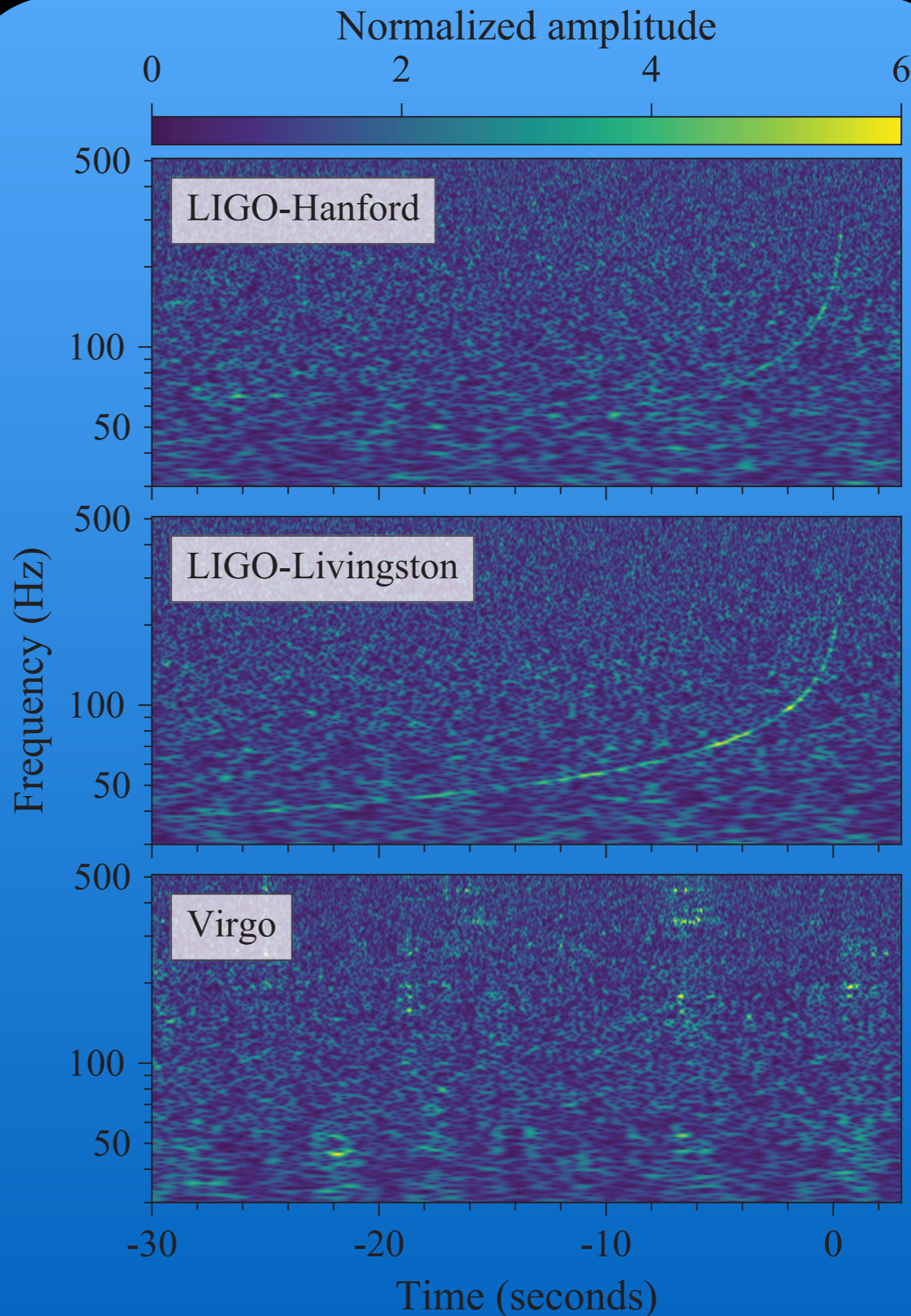


LIGO/University of Oregon/Ben Farr



TIME  
FREQUENCY  
PLOT OF  
GW170817

- ❖ Signal-to-noise ratio of 32.4
- ❖ loudest yet
- ❖ False alarm rate of 1 in  $10^6$  yrs
- ❖ most significant of all





# DETECTION: STATEMENT OF THE PROBLEM

- detector output consists of:
  - only background noise:  $x(t) = n(t)$
  - noise + some interesting signal:  $x(t) = h(t) + n(t)$
  - given a detector output which of the two possibilities is more likely given that the noise background is Gaussian and stationary
- formulate the problem as Bayes' theorem:

$$P(h|x) = \frac{P(x|h)P(h)}{P(x)}$$

- posterior prob. = likelihood x prior / evidence

• denominator is:  $P(x) = P(x|h)P(h) + P(x|\bar{h})P(\bar{h})$

• define likelihood ratio:

$$\Lambda = \frac{P(x|h)}{P(x|\bar{h})}$$

• if signals are rare then

$$P(h) \ll 1 \text{ and } P(\bar{h}) = 1 - P(h) \simeq 1$$

• in that case the posterior prob. of a signal given data is:

$$P(h|x) = \frac{\Lambda P(h)}{1 + \Lambda P(h)}$$

• for confident detection

$$\Lambda \gg 1/P(h)$$

• rarer the signal larger should be the likelihood for a given confidence: for 5-sigma detection  $P(h|x) \simeq 0.999\ 999$

**one in a million**

# COMPUTING THE LIKELIHOOD RATIO

- noise is a Gaussian random process, so at any instant  $t_k$

$$P(n_k) = \frac{1}{\sqrt{2\pi}\sigma_k} e^{-n_k^2/2\sigma_k^2}$$

- it is more convenient to deal with Fourier domain quantities  $N_k$  (similarly,  $X_k$  and  $H_k$ ):

$$P(N_k) = \frac{1}{\sqrt{2\pi}S_k} e^{-N_k^2/2S_k^2}$$

- so the probability of getting a sequence  $P(\{N_k\})$

$$P(\{N_k\}) = \prod_k \frac{1}{\sqrt{2\pi}S_k} e^{-N_k^2/2S_k^2} \propto e^{-\frac{1}{2}\langle n, n \rangle}$$

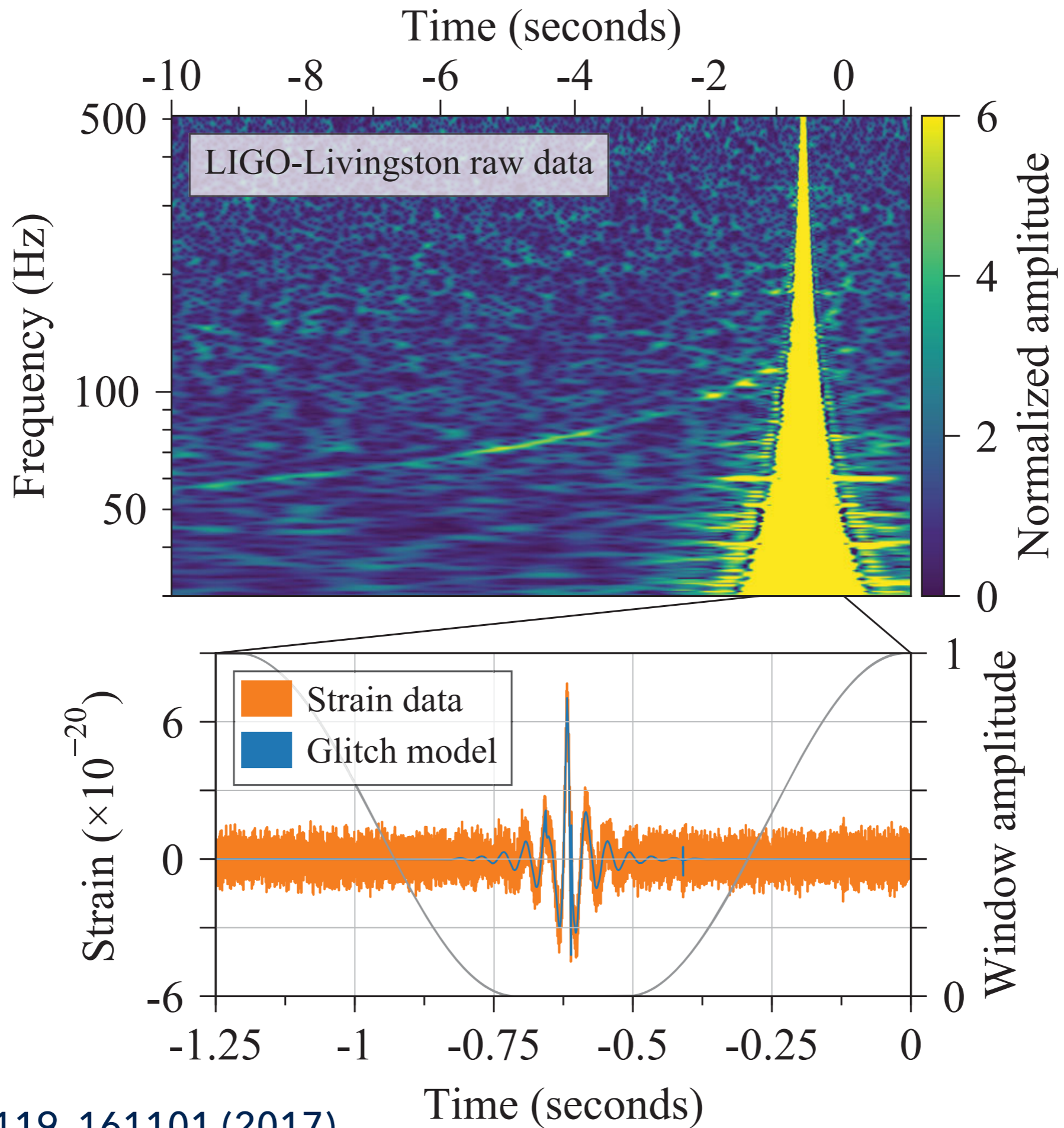
$\langle a, b \rangle = \sum |N_k|^2/S_k^2$

- if signal is absent  $n=x$ , if signal is present  $n=x-h$ :

$$\Lambda = \frac{P(x|h)}{P(x|n)} = \frac{e^{-\frac{1}{2}\langle x-h, x-h \rangle}}{e^{-\frac{1}{2}\langle x, x \rangle}} = e^{\langle x, h \rangle - \frac{1}{2}\langle h, h \rangle}$$

# DIFFICULTIES ...

- the likelihood ratio is computationally very expensive:
  - $\langle x, h \rangle$  would need to be computed at 10's of millions of points in the parameter space (parameters  $\mu$ ) before giving up - **signal**
  - a scheme would be needed to compute  $P(x|h)$  - **background**
- noise is not Gaussian or stationary
  - nothing much can be done about non-stationarity: detector behavior is assumed to be stable over periods  $\sim$  days
  - non-Gaussian and non-stationary data is rejected
    - glitch rejection, signal consistency checks, coincidence and coherent analysis, etc.





# A GEOMETRICAL FORMULATION OF DATA ANALYSIS: SIGNAL MANIFOLD

- detector outputs can be thought of as vectors
- the set of all detector outputs forms a vector space
- signals are also vectors that live in this vector space
- space of signals forms a manifold: signal parameters (e.g. masses and spins of black holes) are coordinates that determine the dimension of the manifold
- the scalar product  $\langle a, b \rangle$  can be used to induce a metric on the manifold:  $g_{\alpha\beta} = \langle h_{\alpha}, h_{\beta} \rangle$ , where  $h_{\alpha} = \delta h / \delta \mu_{\alpha}$
- the signal space now acquires a shape

# TEMPLATE BANKS FOR COMPUTING

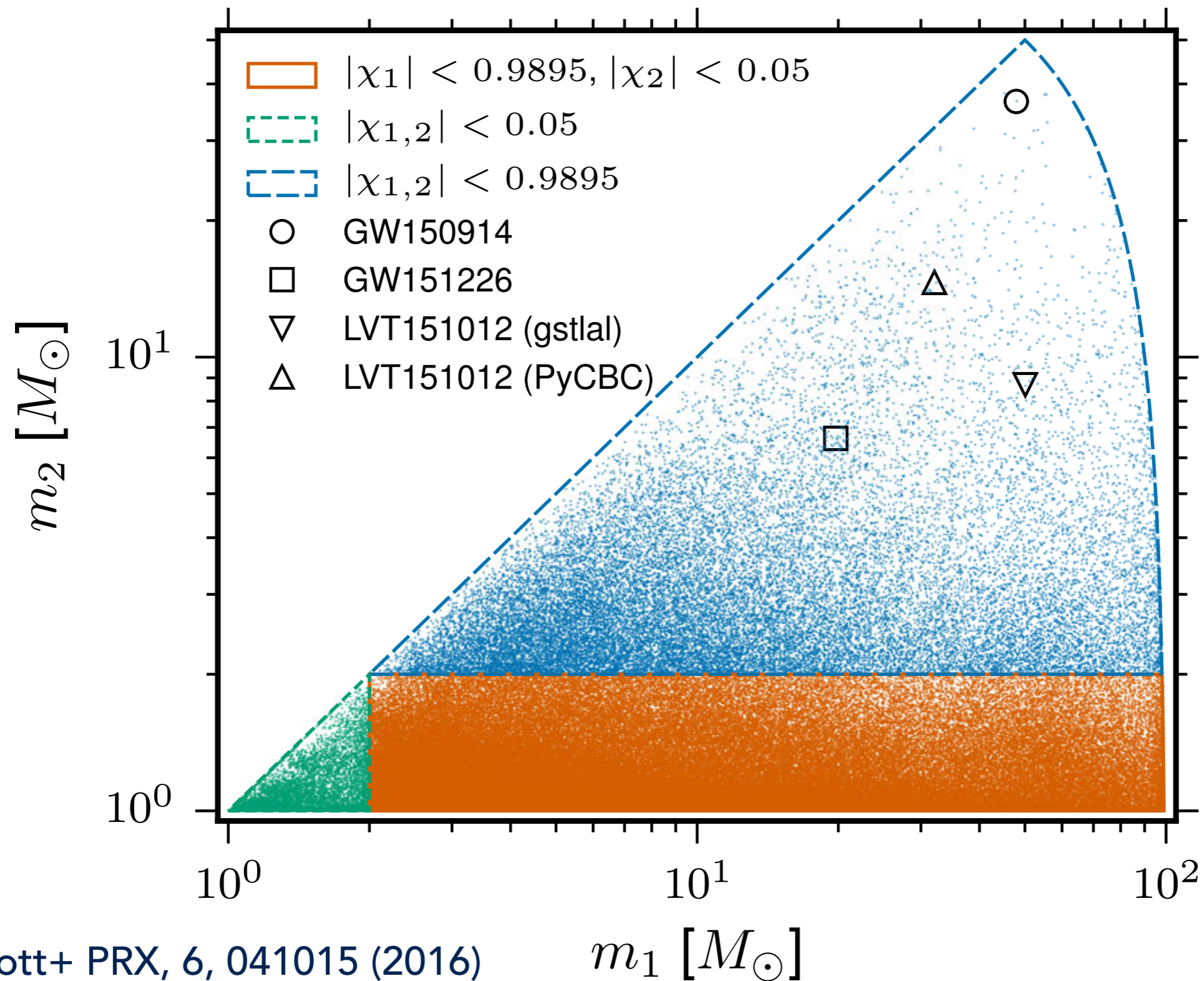
$$\langle x, h(\mu) \rangle$$

- volume of the parameter space is:  $V = \int \sqrt{g} d^n \mu$
- if each template covers a volume  $V$  then the number of templates is:

$$N = \frac{1}{\Delta V} \int \sqrt{g} d^n \mu$$

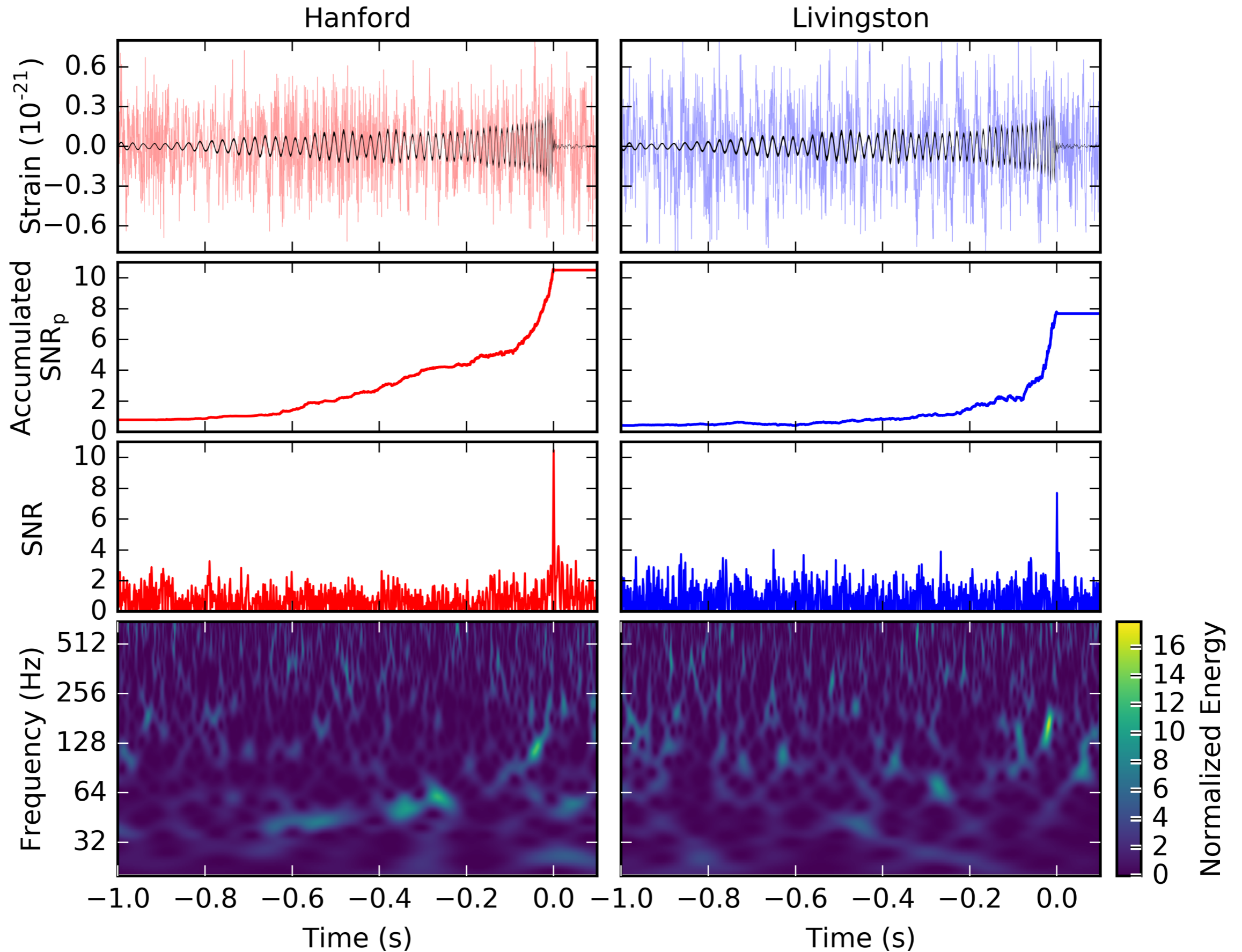
- but how to choose templates ... **template placement problem**, a hard problem with only sub-optimal solutions
- a uniform grid, say, in the space of masses and spins, or something more fancy?
- a hexagonal lattice, stochastic method, ...
- O1 search deployed 250,000 templates for compact binary coalescence searches, O2 about 500,000 templates

# MATCHED FILTER SEARCH FOR SIGNALS OF KNOWN SHAPE



Matched filtering and waveform models were critical for detection and signal reconstruction

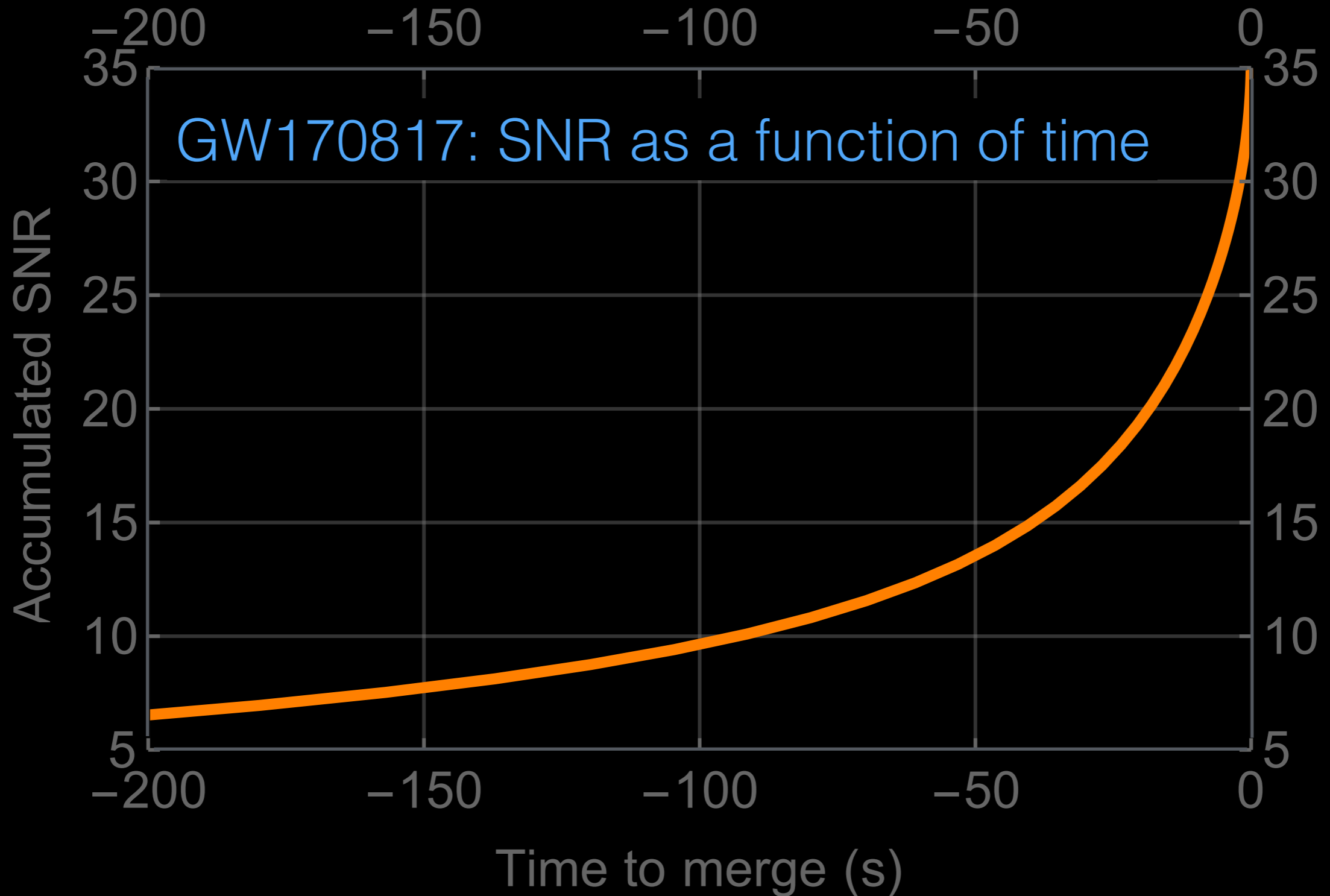
GW151226



A Gravitational-Wave  
Early-Warning  
System

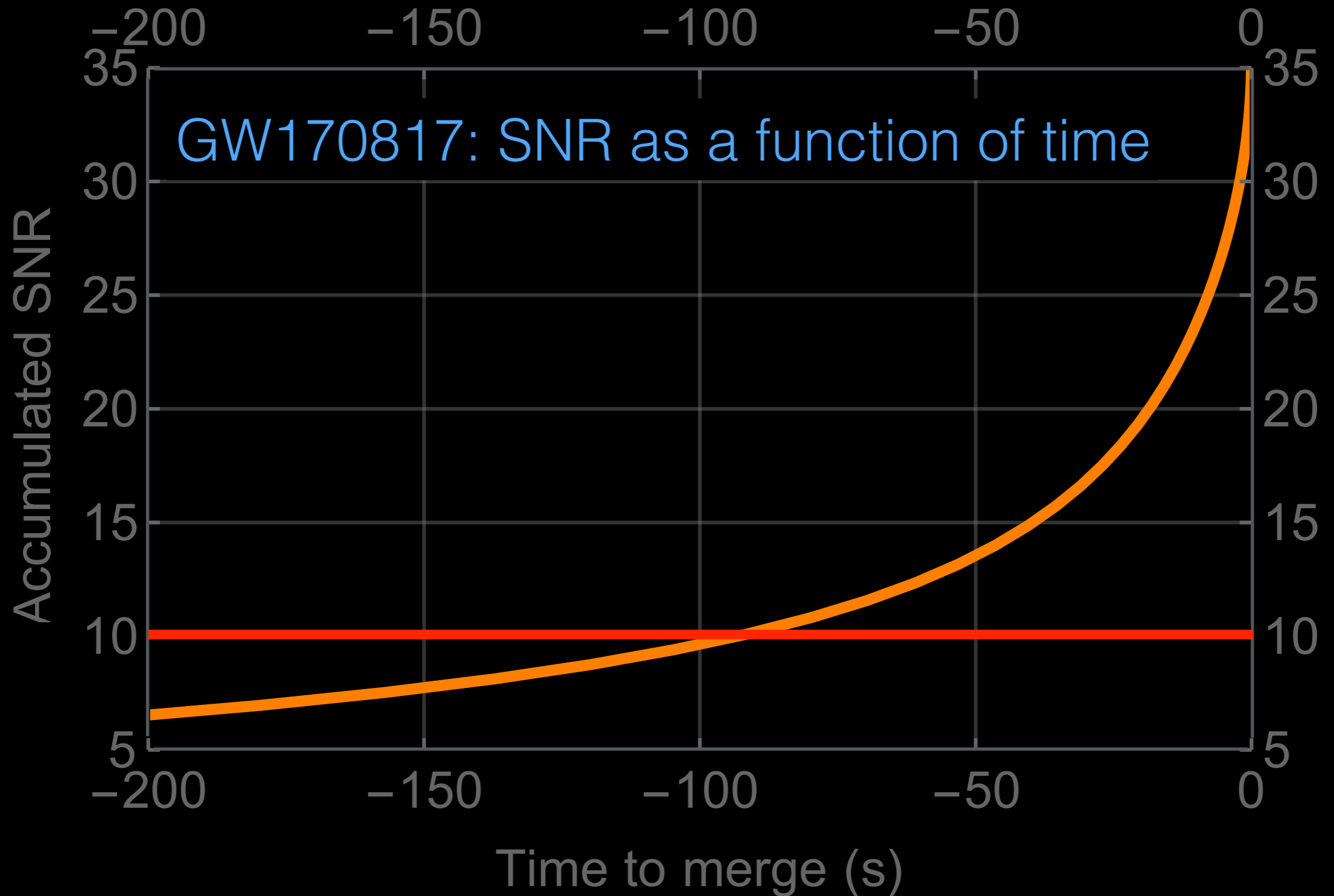


# HOW QUICKLY CAN WE ISSUE AN ALERT FOR A GW170817-LIKE EVENT



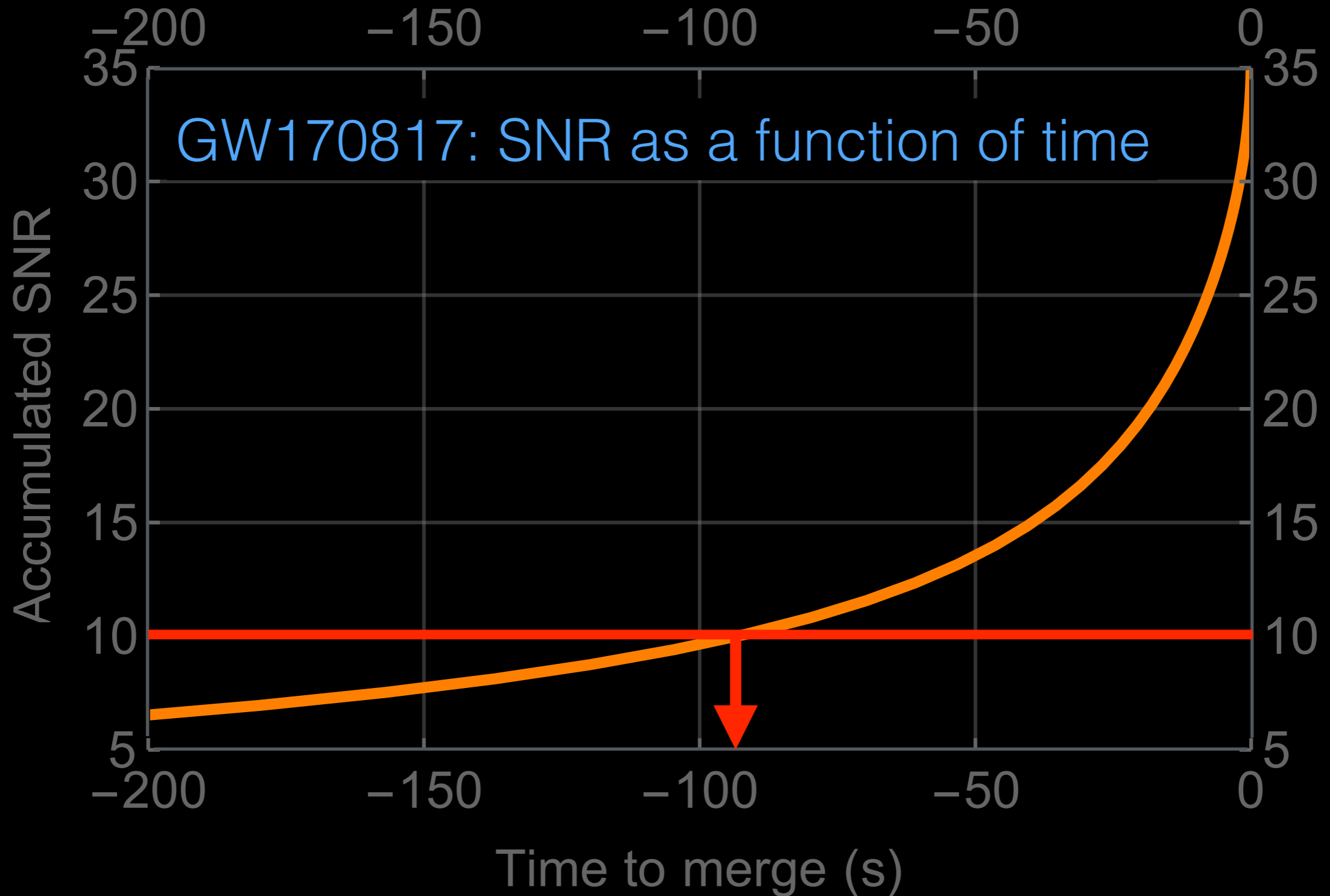
Single detector SNR

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Single detector SNR

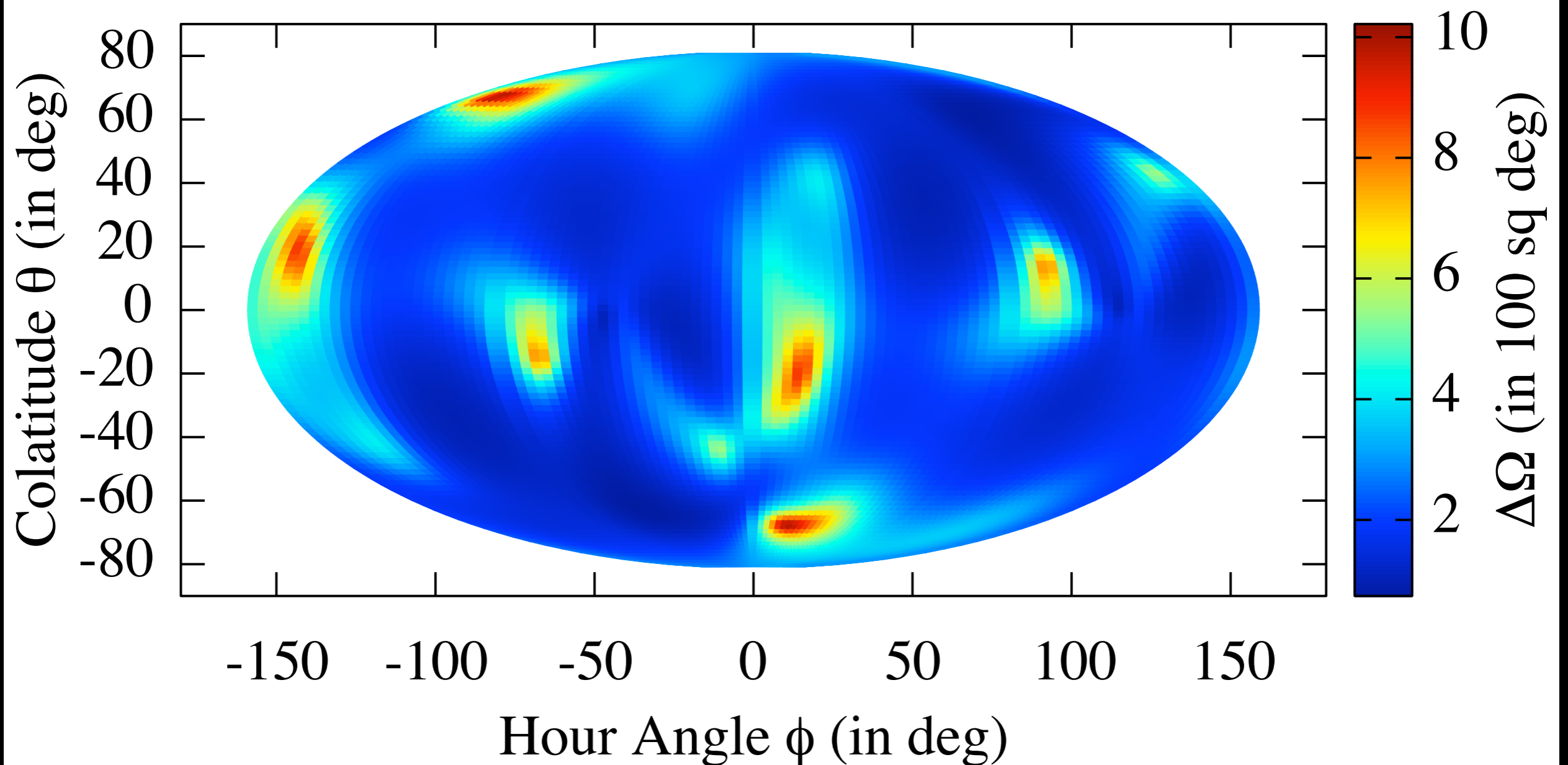
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Single detector SNR

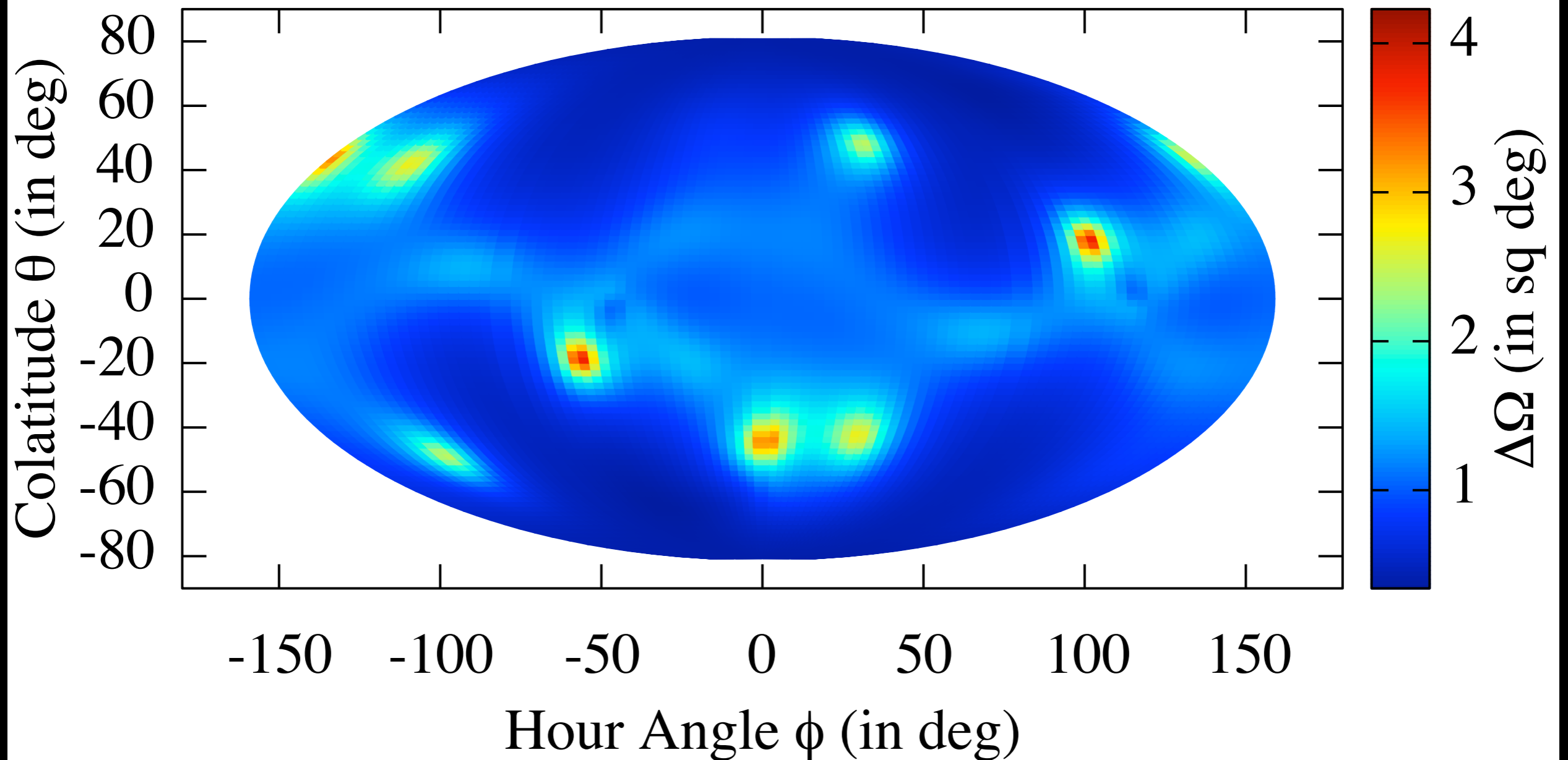
# SKY RESOLUTION BEFORE MERGER OF A GW170817-LIKE EVENT

$\Delta\Omega$  at ( $f=30\text{Hz}$ ,  $t_C=-60\text{s}$ ,  $\iota=30\text{ deg}$ ) for HILV



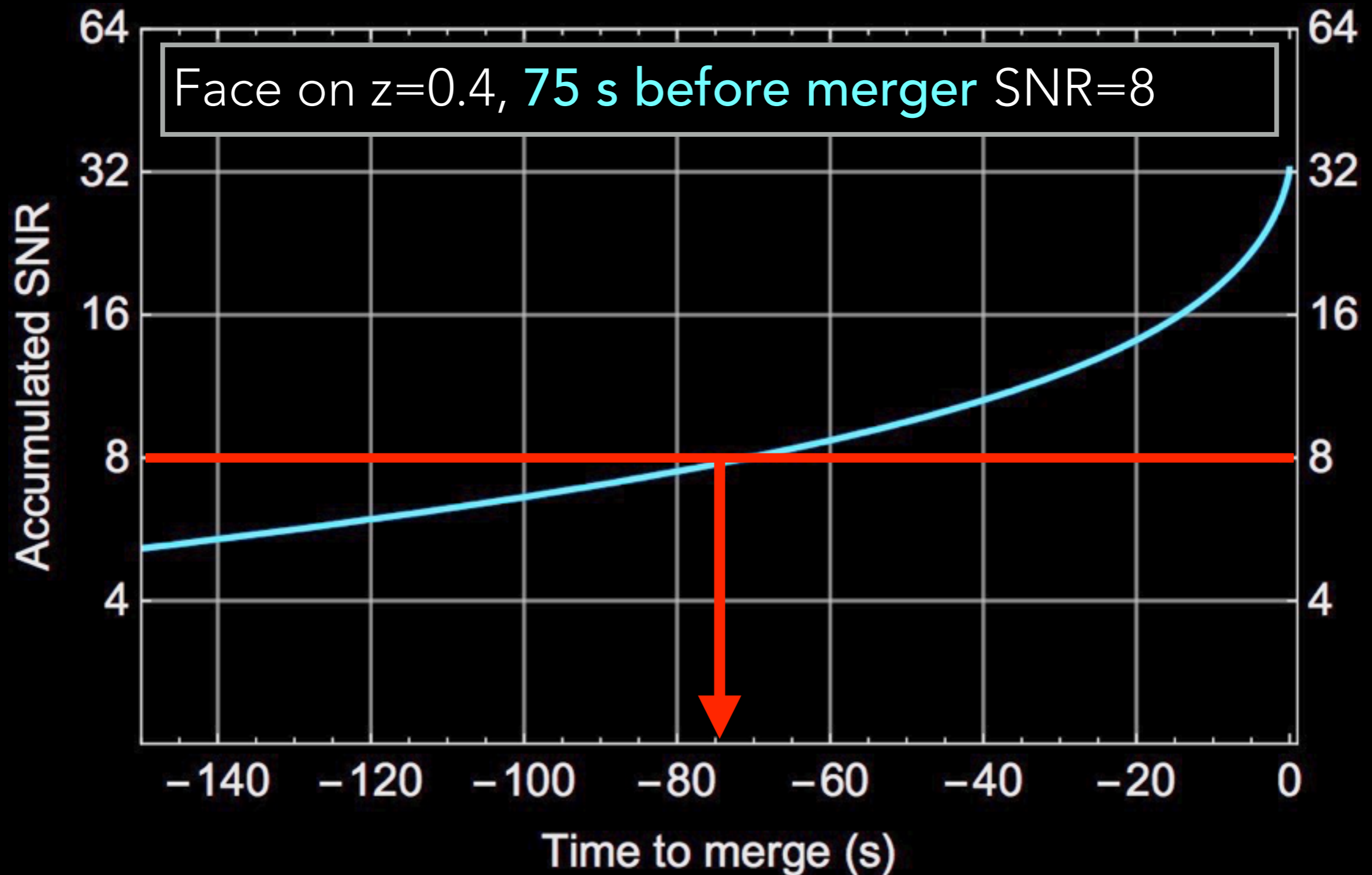
# SKY RESOLUTION AFTER MERGER OF A GW170817-LIKE EVENT

$\Delta\Omega$  at ( $f$ =LSO,  $t_C$ =0s,  $\iota$ =30 deg) for HILV





# EARLY WARNING IN THE ERA OF NEXT GENERATION OF DETECTORS



Single detector SNR

measuring source  
parameters

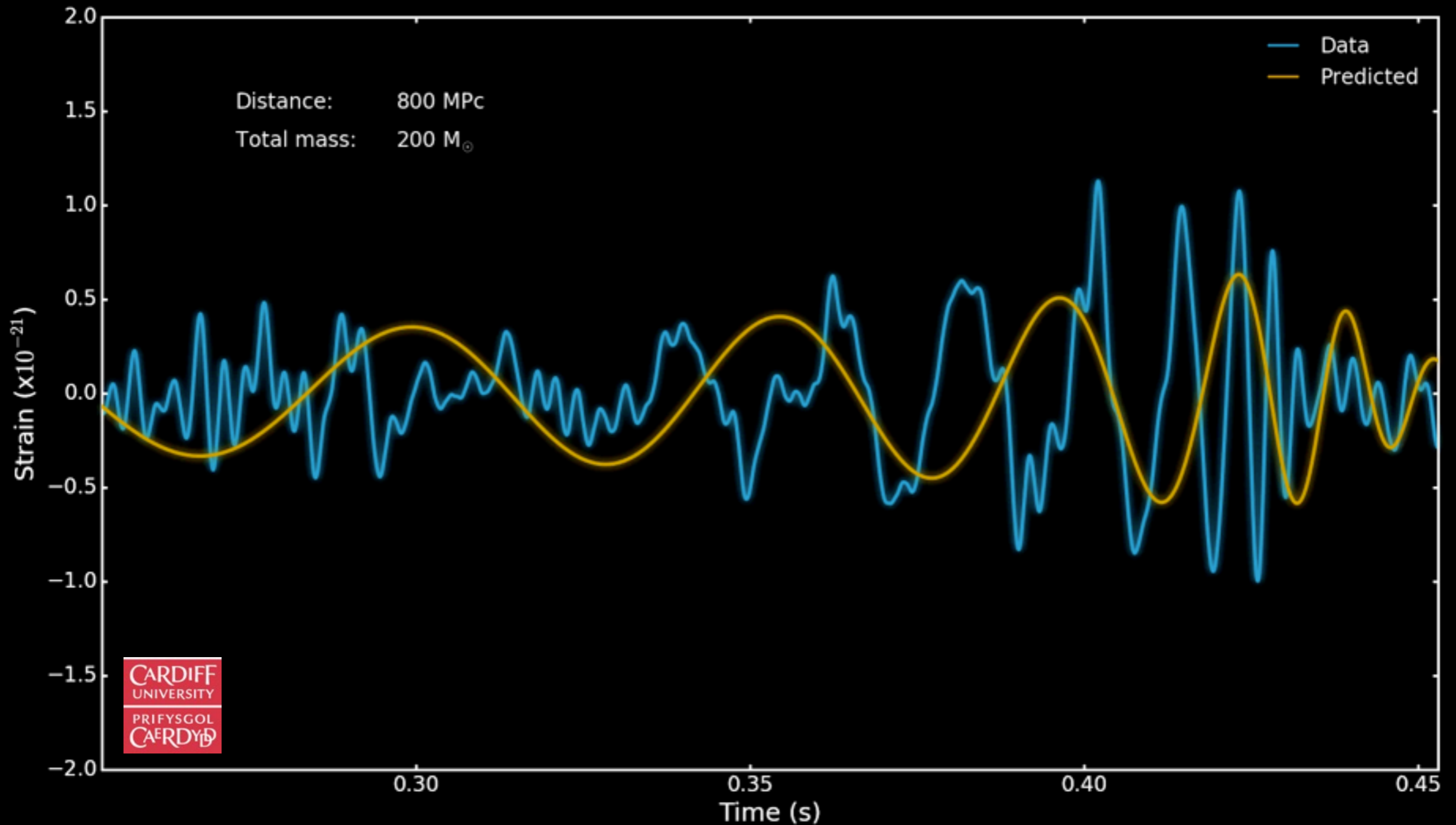
# MEASURING SOURCE PARAMETERS

- Bayesian analysis is used to infer the posterior probability density of parameters  $\mu = \{\mu_1, \mu_2, \dots, \mu_n\}$  given the data  $x$ :

$$P(h(\mu)|x) = \frac{P(x|h(\mu))P(h)}{P(x)}$$

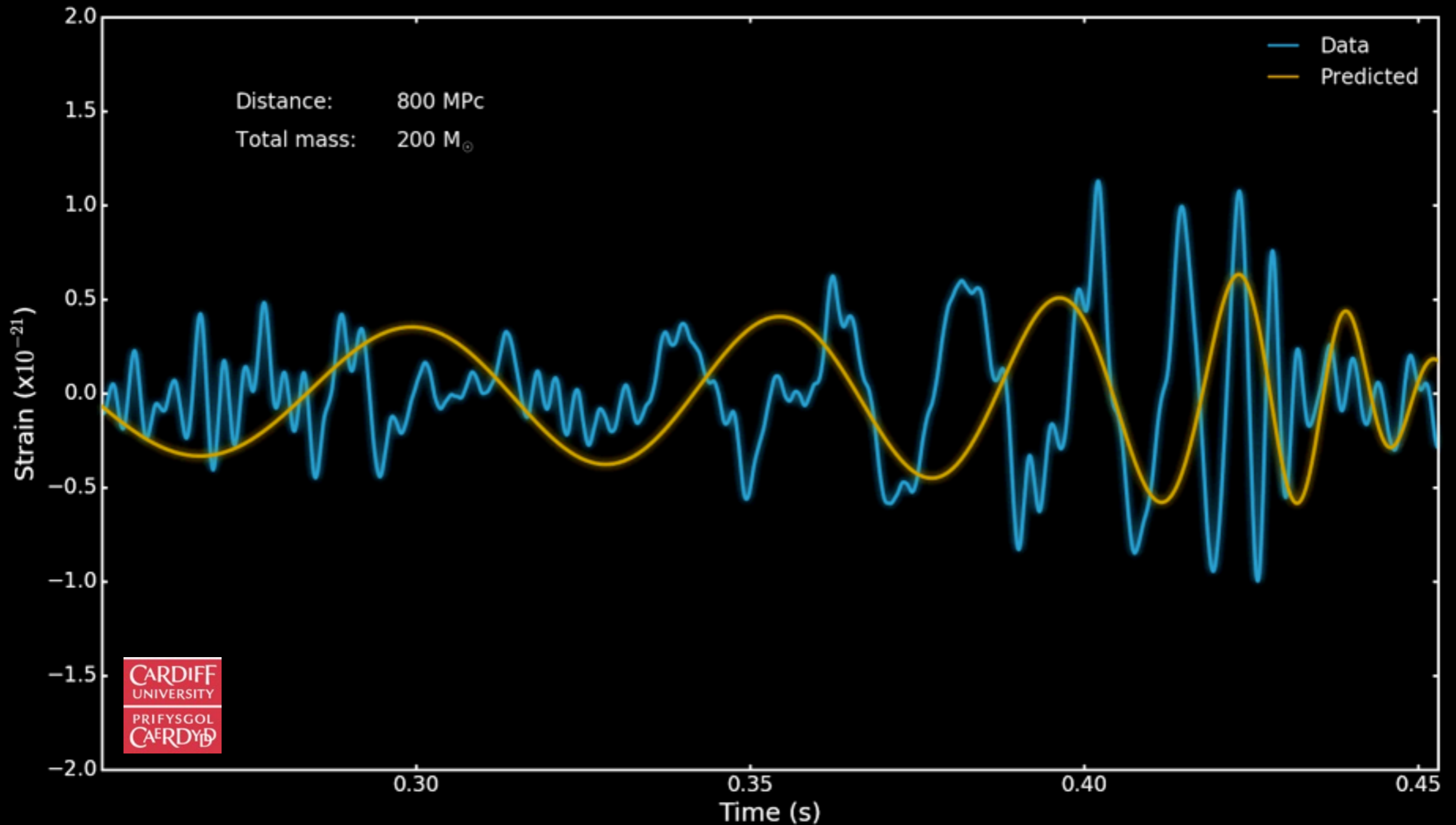
- in the case of binary black holes signal parameters are component masses  $(m_1, m_2)$  and spins  $(\mathbf{S}_1, \mathbf{S}_2)$ , ~~eccentricity  $e$~~ , sky position  $(\theta, \phi)$ , distance  $D$ , binary orientation angles  $(\iota, \delta)$ , time of and phase at coalescence  $(t_c, \phi_c)$ ; PSD, calibration, etc.
- likelihood  $P(x|h(\mu))$  is very expensive as it requires computing the overlap of millions of waveforms with the data and **different signal models**
- impossible to compute without fast, analytic waveform models

# PARAMETER ESTIMATION USING WAVEFORMS PREDICTED BY GR



Data & Best-fit Waveform: LIGO Open Science Center ([losc.ligo.org](https://losc.ligo.org)); Prediction & Animation: C.North/M.Hannam (Cardiff University)

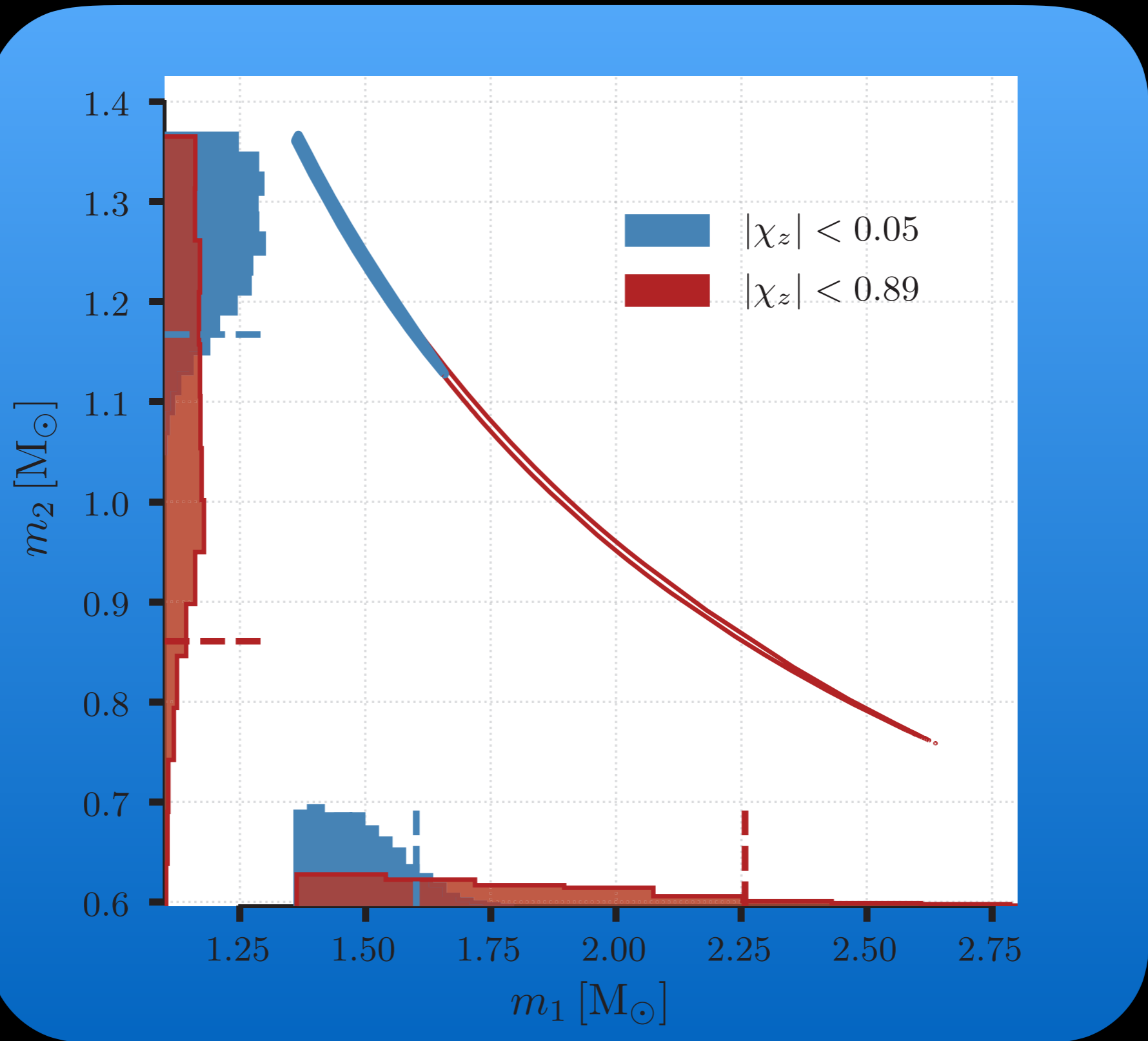
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# COMPONENT MASSES



# PROPERTIES OF GW170817: LOW NEUTRON STAR SPIN

	Low-spin priors ( $ \chi  \leq 0.05$ )
Primary mass $m_1$	1.36–1.60 $M_\odot$
Secondary mass $m_2$	1.17–1.36 $M_\odot$
Chirp mass $\mathcal{M}$	$1.188^{+0.004}_{-0.002} M_\odot$
Mass ratio $m_2/m_1$	0.7–1.0
Total mass $m_{\text{tot}}$	$2.74^{+0.04}_{-0.01} M_\odot$
Radiated energy $E_{\text{rad}}$	$> 0.025 M_\odot c^2$
Luminosity distance $D_L$	$40^{+8}_{-14}$ Mpc
Viewing angle $\Theta$	$\leq 55^\circ$
Using NGC 4993 location	$\leq 28^\circ$
Combined dimensionless tidal deformability $\tilde{\Lambda}$	$\leq 800$
Dimensionless tidal deformability $\Lambda(1.4M_\odot)$	$\leq 800$

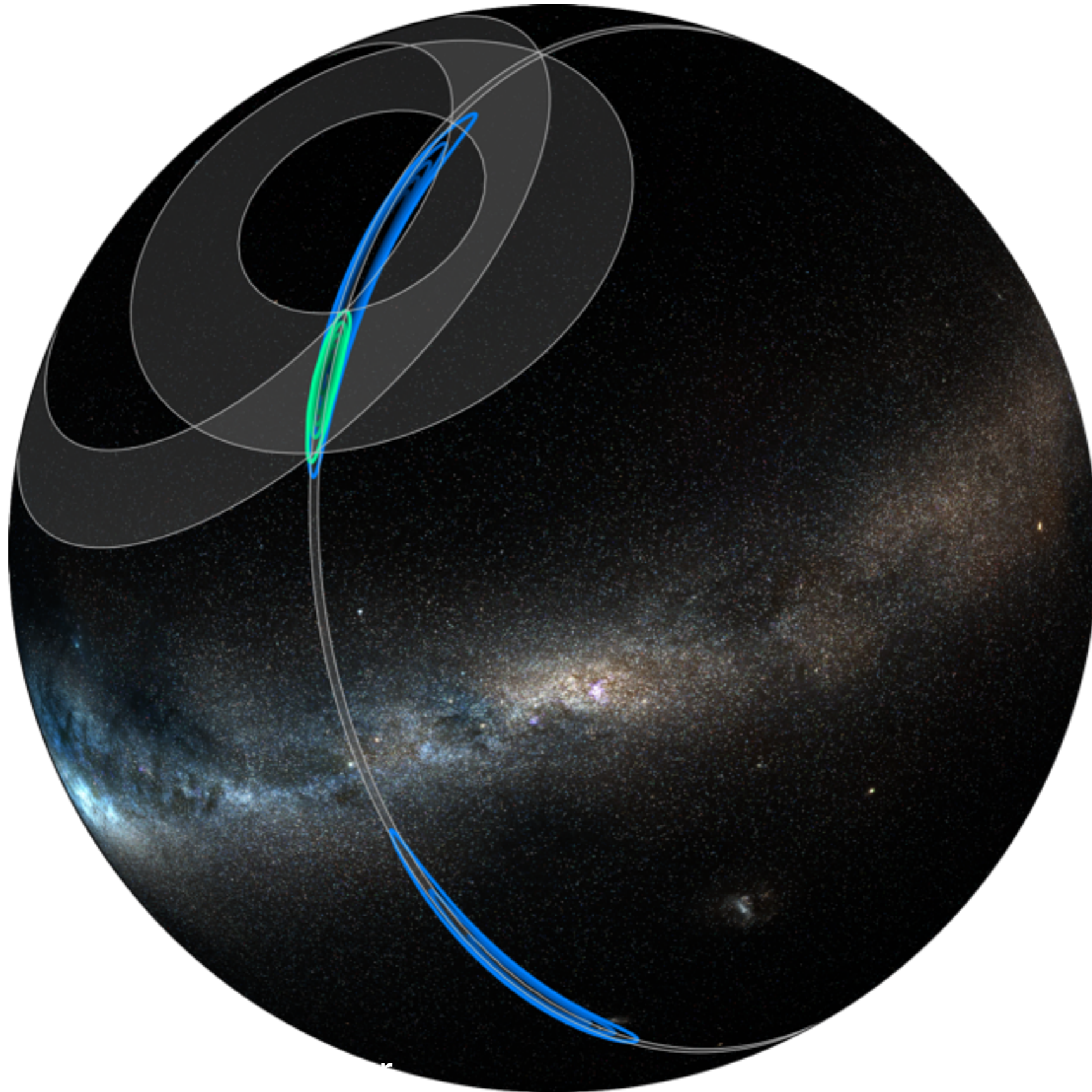
# PROPERTIES OF GW170817: HIGH NEUTRON STAR SPIN

	High-spin priors ( $ \chi  \leq 0.89$ )
Primary mass $m_1$	1.36–2.26 $M_\odot$
Secondary mass $m_2$	0.86–1.36 $M_\odot$
Chirp mass $\mathcal{M}$	$1.188^{+0.004}_{-0.002} M_\odot$
Mass ratio $m_2/m_1$	0.4–1.0
Total mass $m_{\text{tot}}$	$2.82^{+0.47}_{-0.09} M_\odot$
Radiated energy $E_{\text{rad}}$	$> 0.025 M_\odot c^2$
Luminosity distance $D_L$	$40^{+8}_{-14}$ Mpc
Viewing angle $\Theta$	$\leq 56^\circ$
Using NGC 4993 location	$\leq 28^\circ$
Combined dimensionless tidal deformability $\tilde{\Lambda}$	$\leq 700$
Dimensionless tidal deformability $\Lambda(1.4M_\odot)$	$\leq 1400$





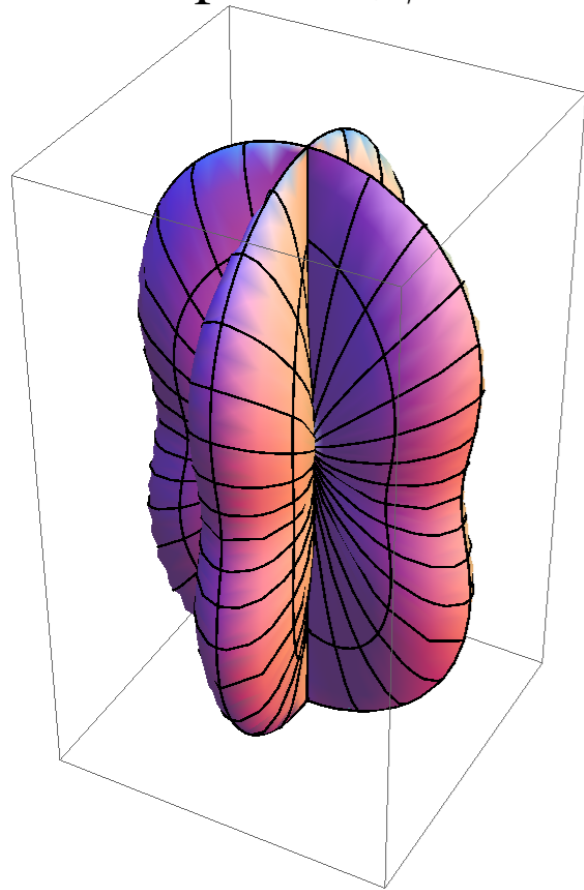
# HOW DO WE LOCALIZE A SOURCE?



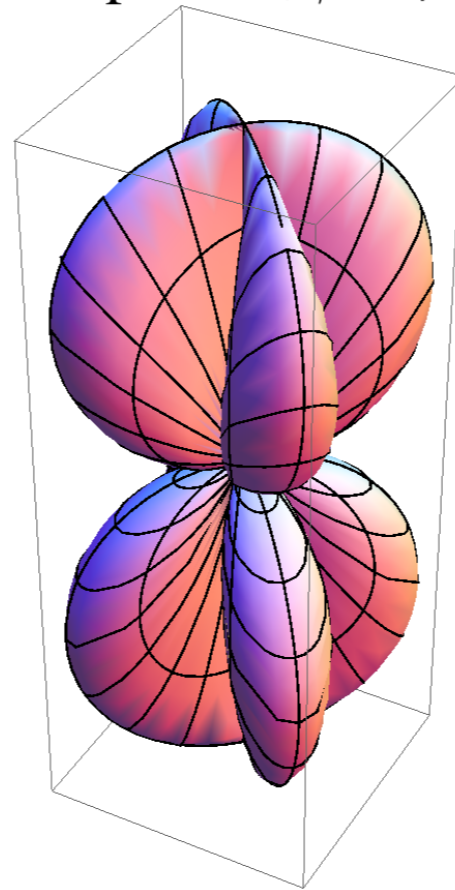


# ANTENNA PATTERN FUNCTIONS

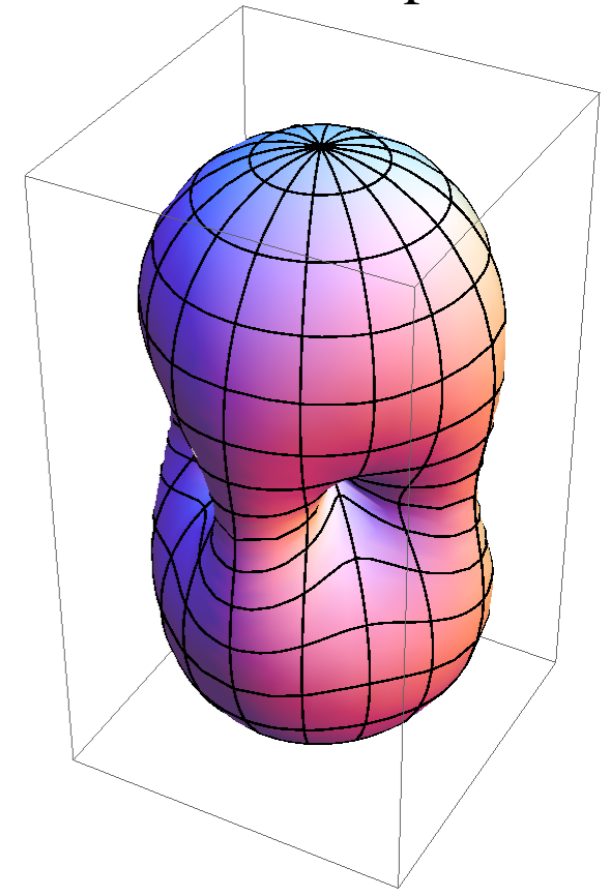
"+" pattern,  $\psi=0$



"x" pattern,  $\psi=\pi/4$

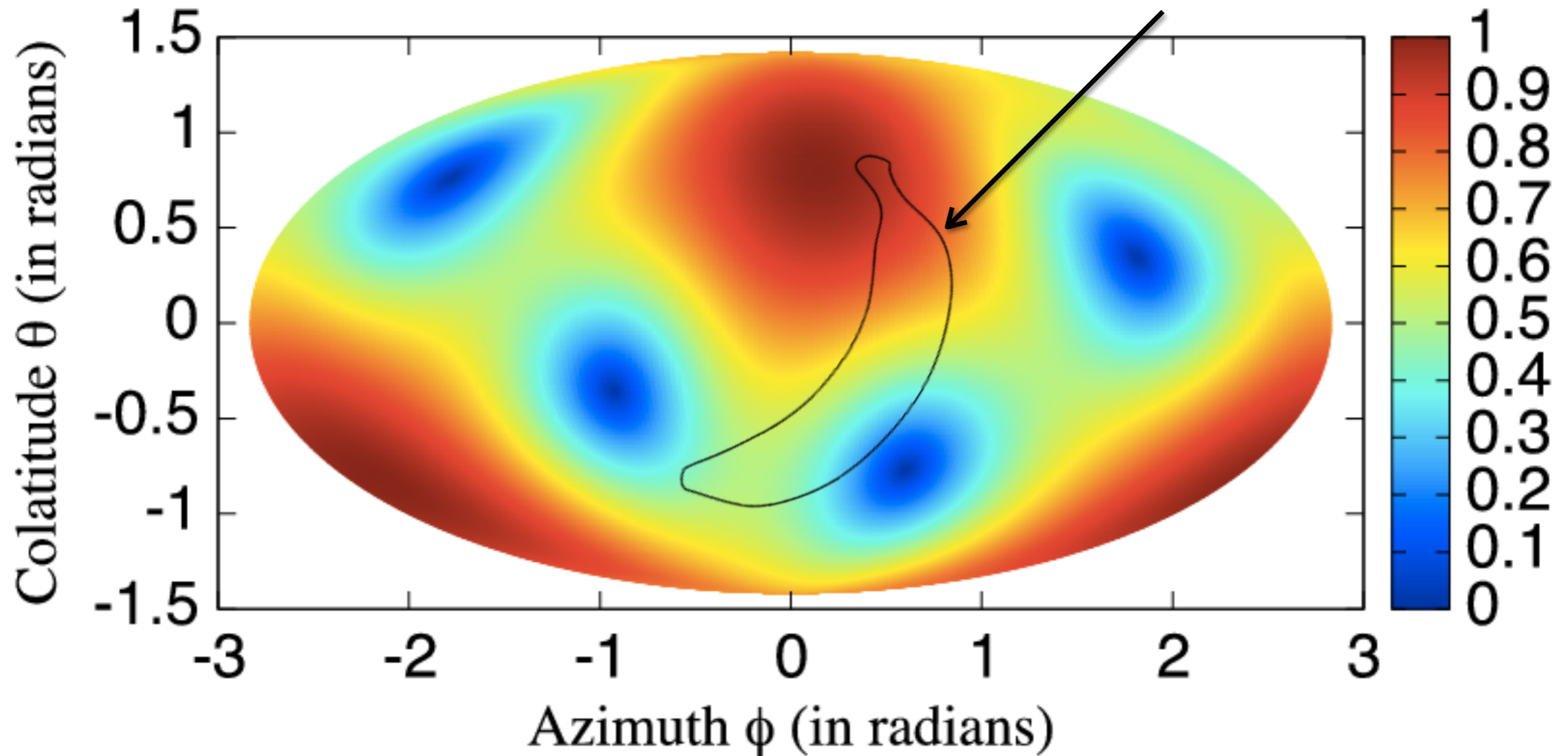


RMS antenna pattern



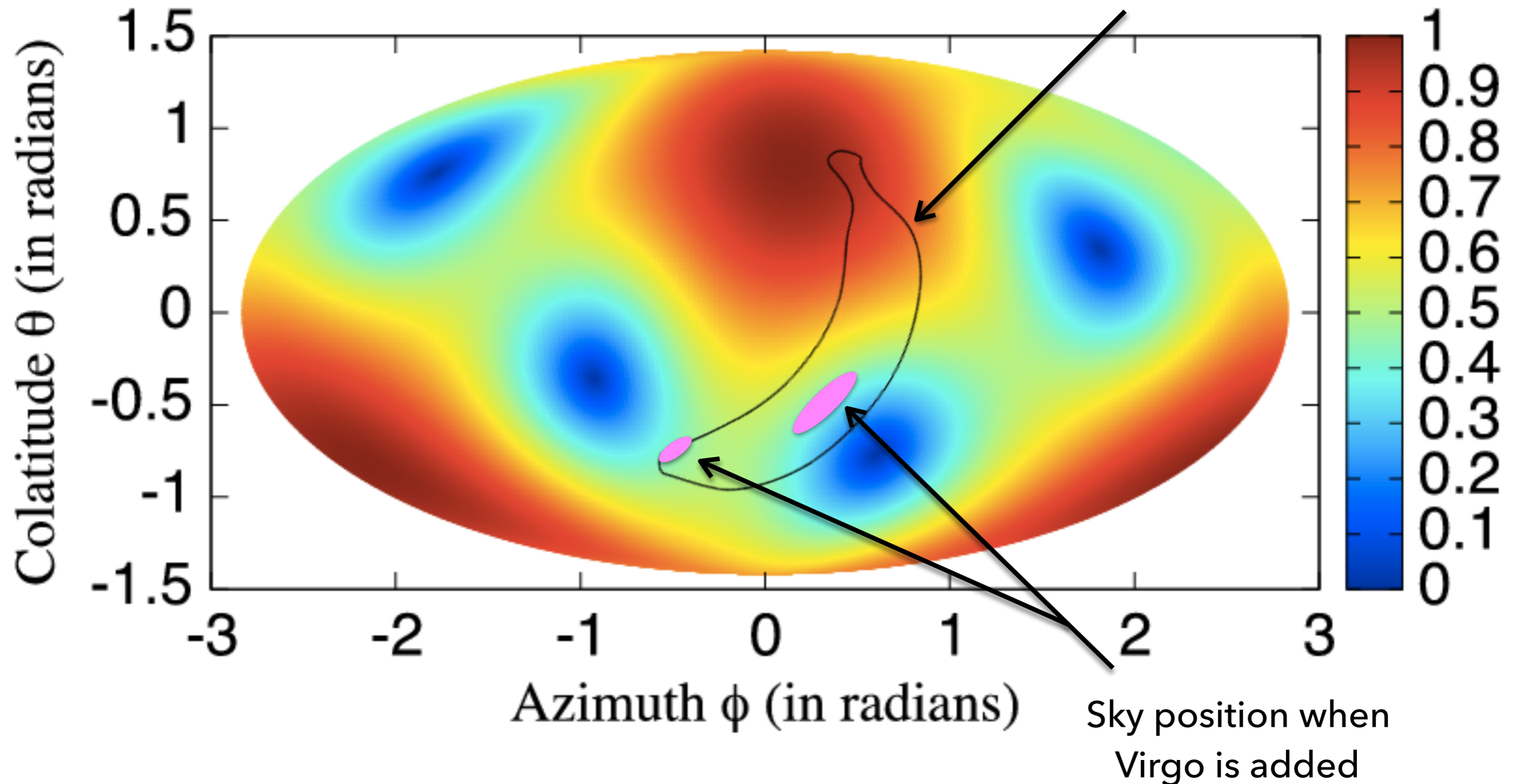
# SKY LOCALIZATION EVEN WHEN A DETECTOR DOESN'T "SEE" THE SIGNAL

Sky position uncertainty due to LIGO Hanford and Livingston



# SKY LOCALIZATION EVEN WHEN A DETECTOR DOESN'T "SEE" THE SIGNAL

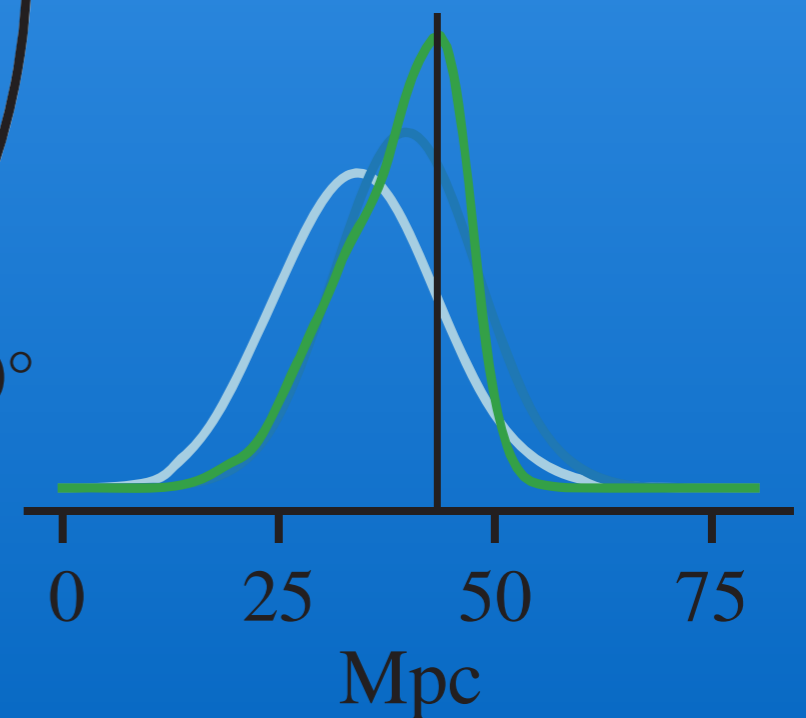
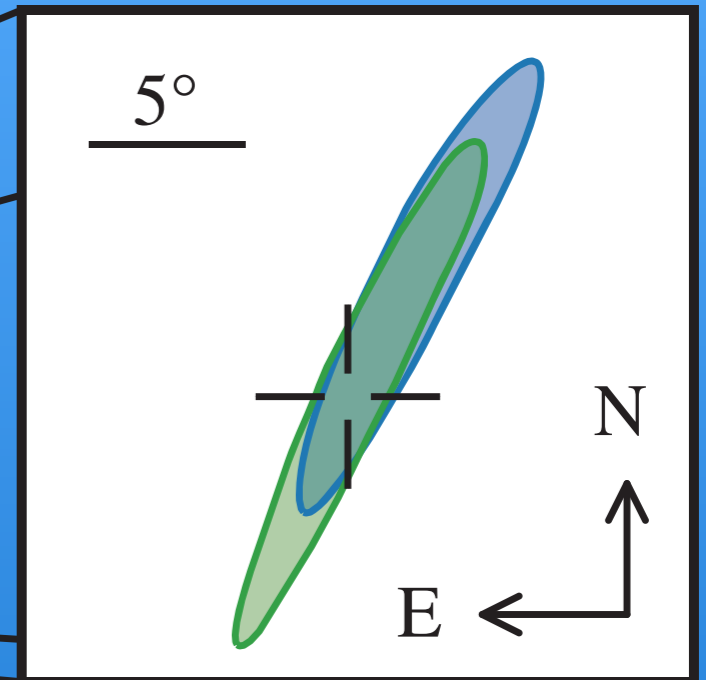
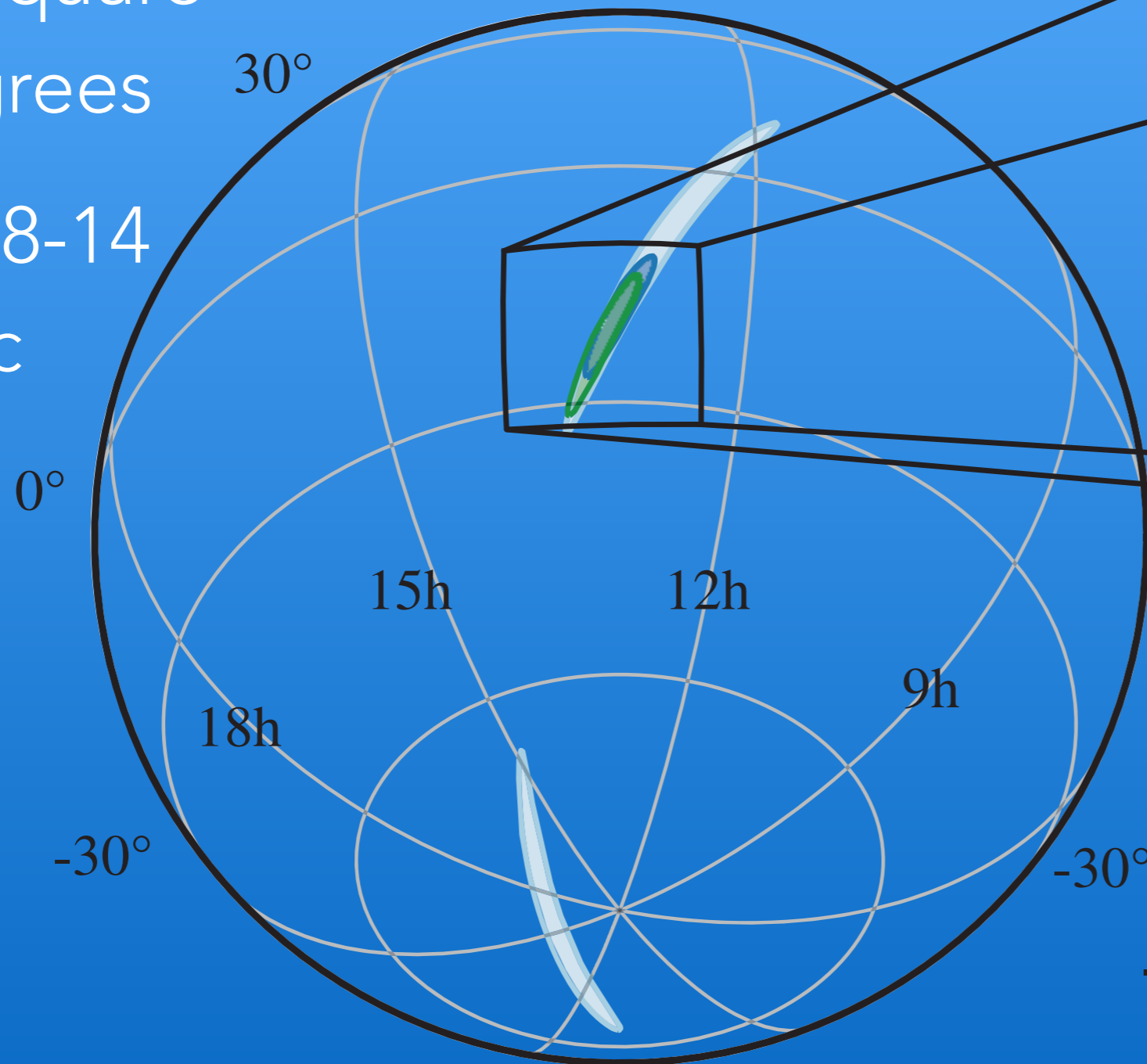
Sky position uncertainty due to LIGO Hanford and Livingston



# SKY POSITION AND DISTANCE

❖ 28 square degrees

❖ 40+8-14 Mpc



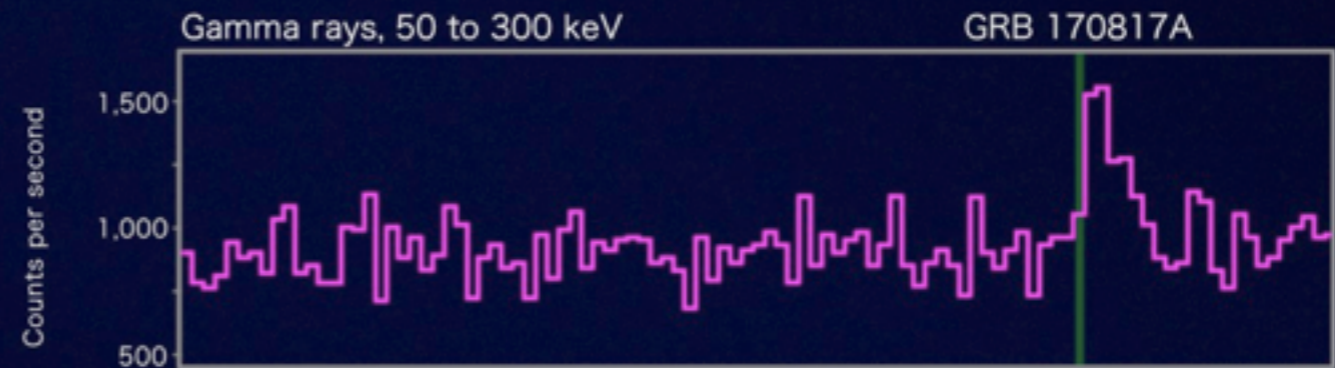
❖ most precisely localized yet



# GRB IN FERMI AND INTEGRAL 1.7 S AFTER COALESCENCE

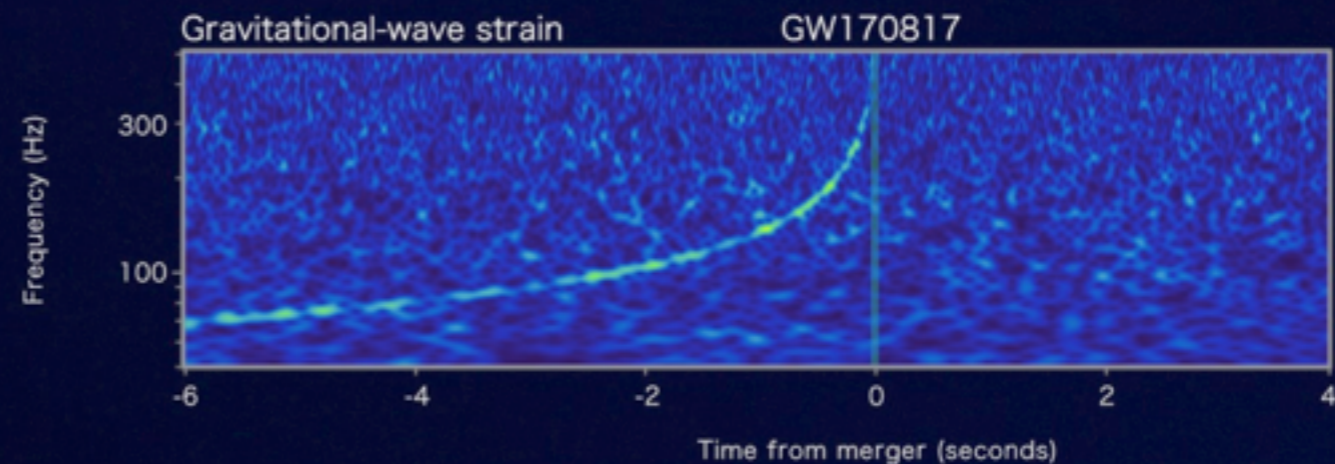
## Fermi

Reported 16 seconds  
after detection



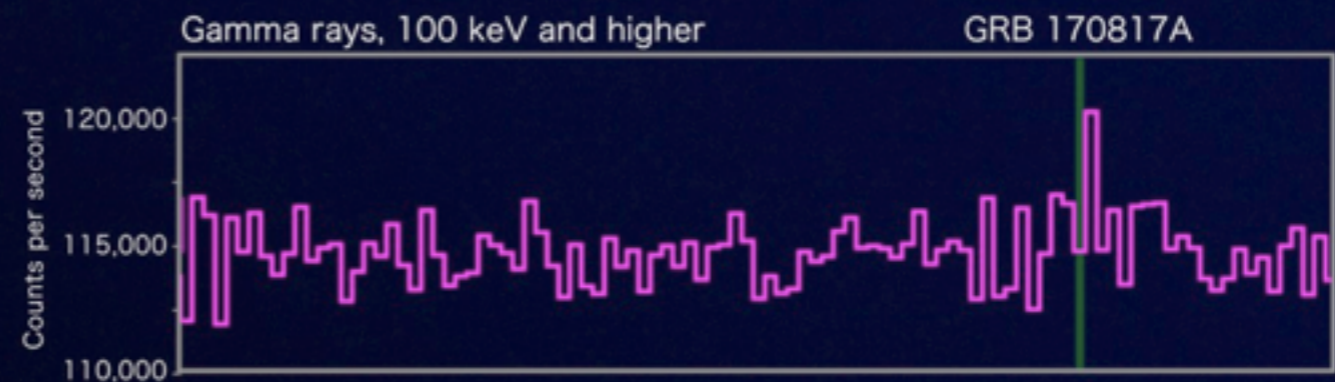
## LIGO-Virgo

Reported 27 minutes  
after detection

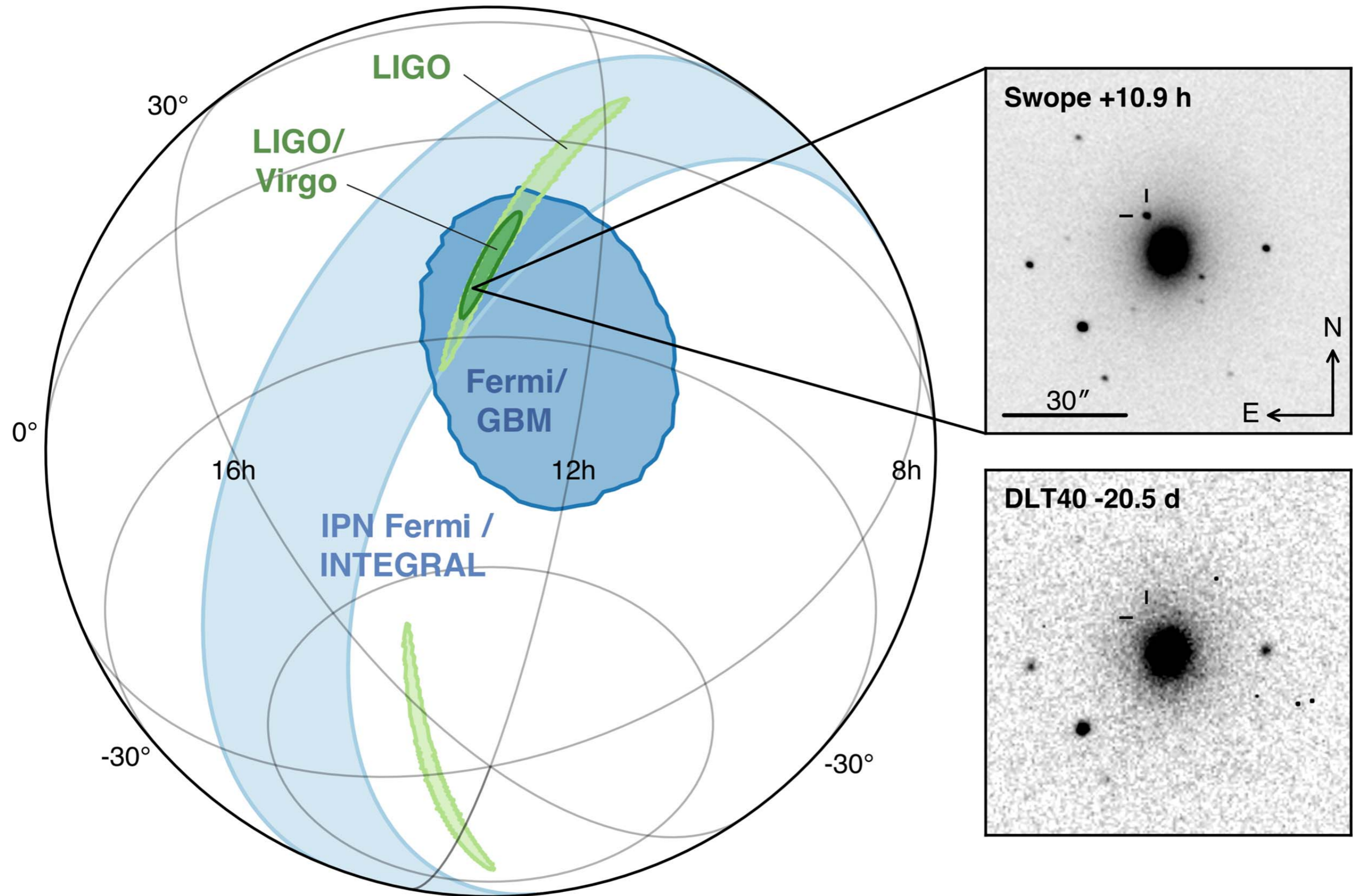


## INTEGRAL

Reported 66 minutes  
after detection

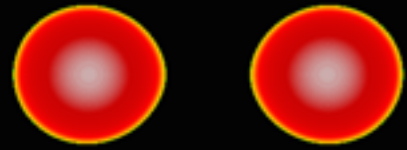




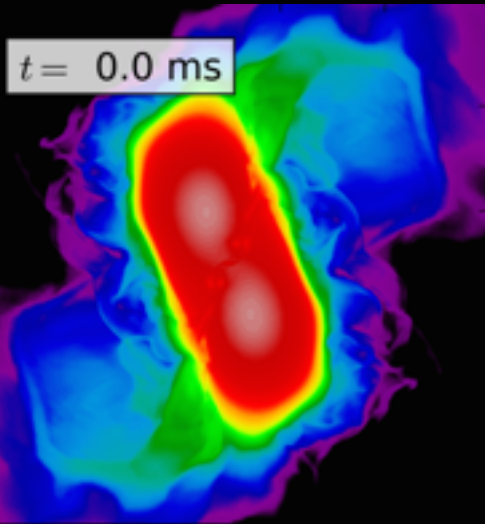




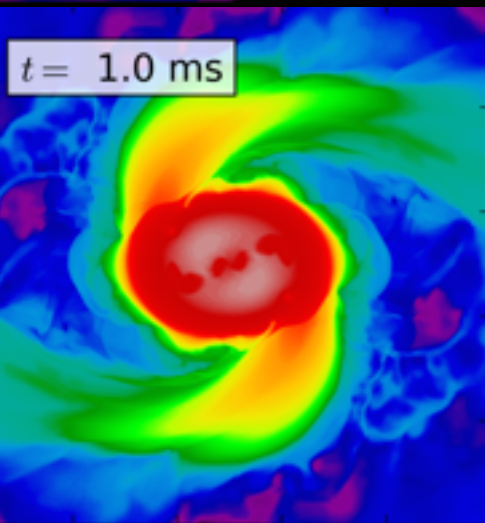
$t = -8.1 \text{ ms}$



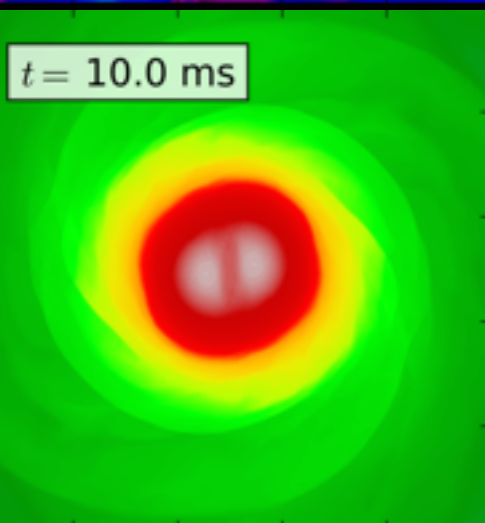
$t = 0.0 \text{ ms}$



$t = 1.0 \text{ ms}$



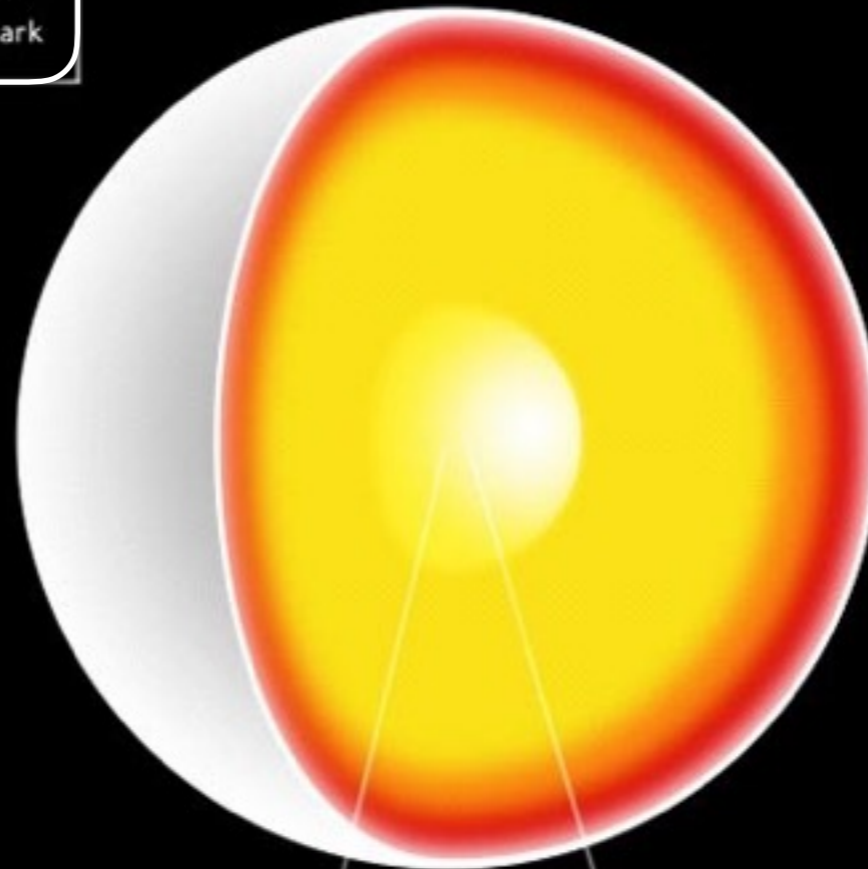
$t = 10.0 \text{ ms}$



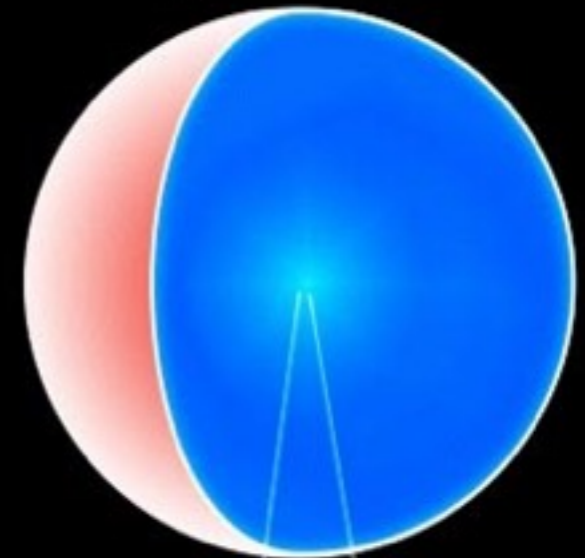
# EQUATION OF STATE OF DENSE NUCLEAR AND OTHER EXTREME MATTER



Neutron Star



Strange Quark Star



Densities  $\sim 4 \times 10^{17} \text{ kg/m}^3$



# SIGNATURE OF EQUATION OF STATE IN BINARY NEUTRON STAR WAVEFORMS

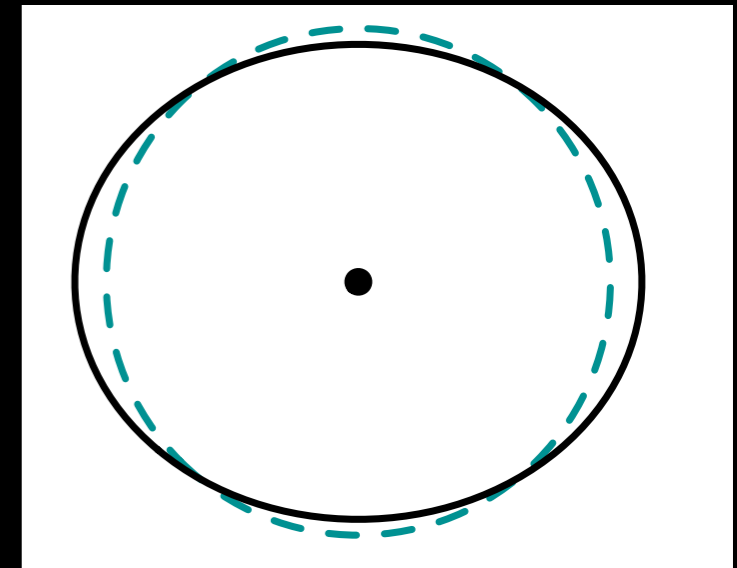
- ❖ tidal field  $\mathcal{E}$  of one companion induces a quadrupole moment  $Q$  in the other
- ❖ in the adiabatic approximation

$$Q_{ij} = -\lambda(m) \mathcal{E}_{ij}, \quad \lambda(m) = (2/3) k_2(m) R^5(m)$$

- ❖  $\lambda(m)$  is tidal deformability,  $k_2(m)$  is the Love number and  $R$  is the NS radius

$$\Lambda \equiv G\lambda(Gm_{\text{NS}}/c^2)^{-5}$$

$$\Lambda \in [300, 600]$$

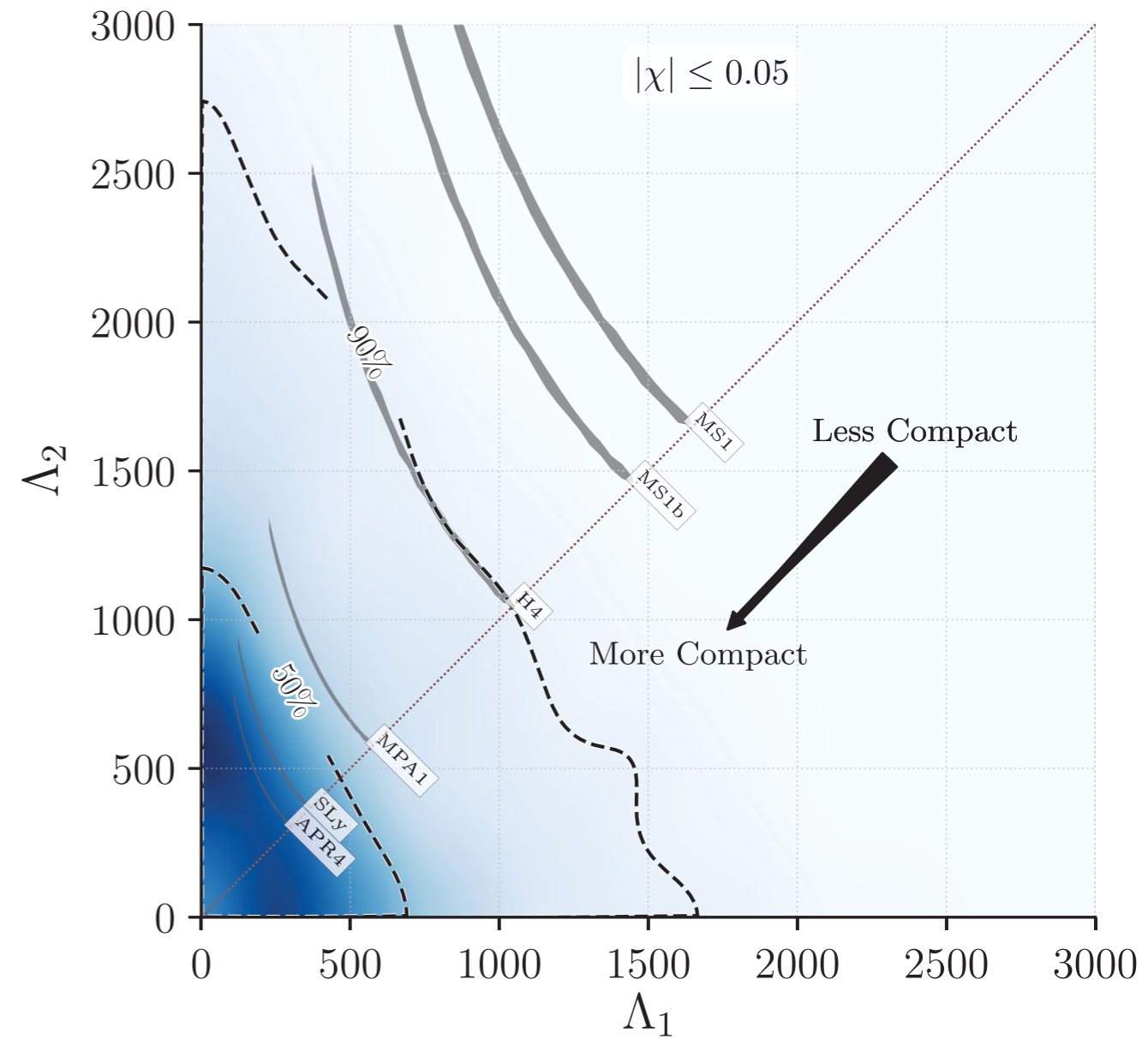
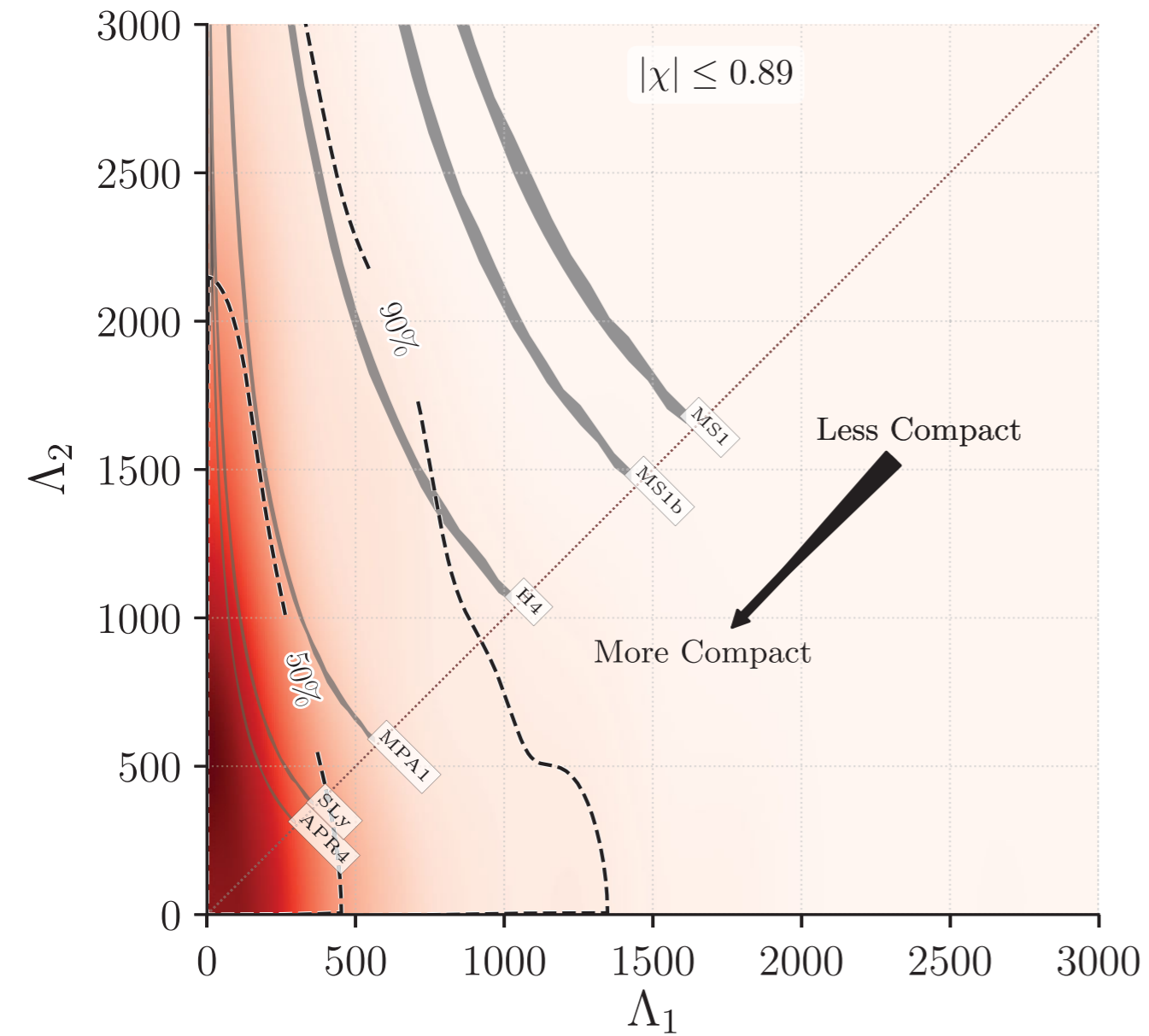


sketch: J. Read



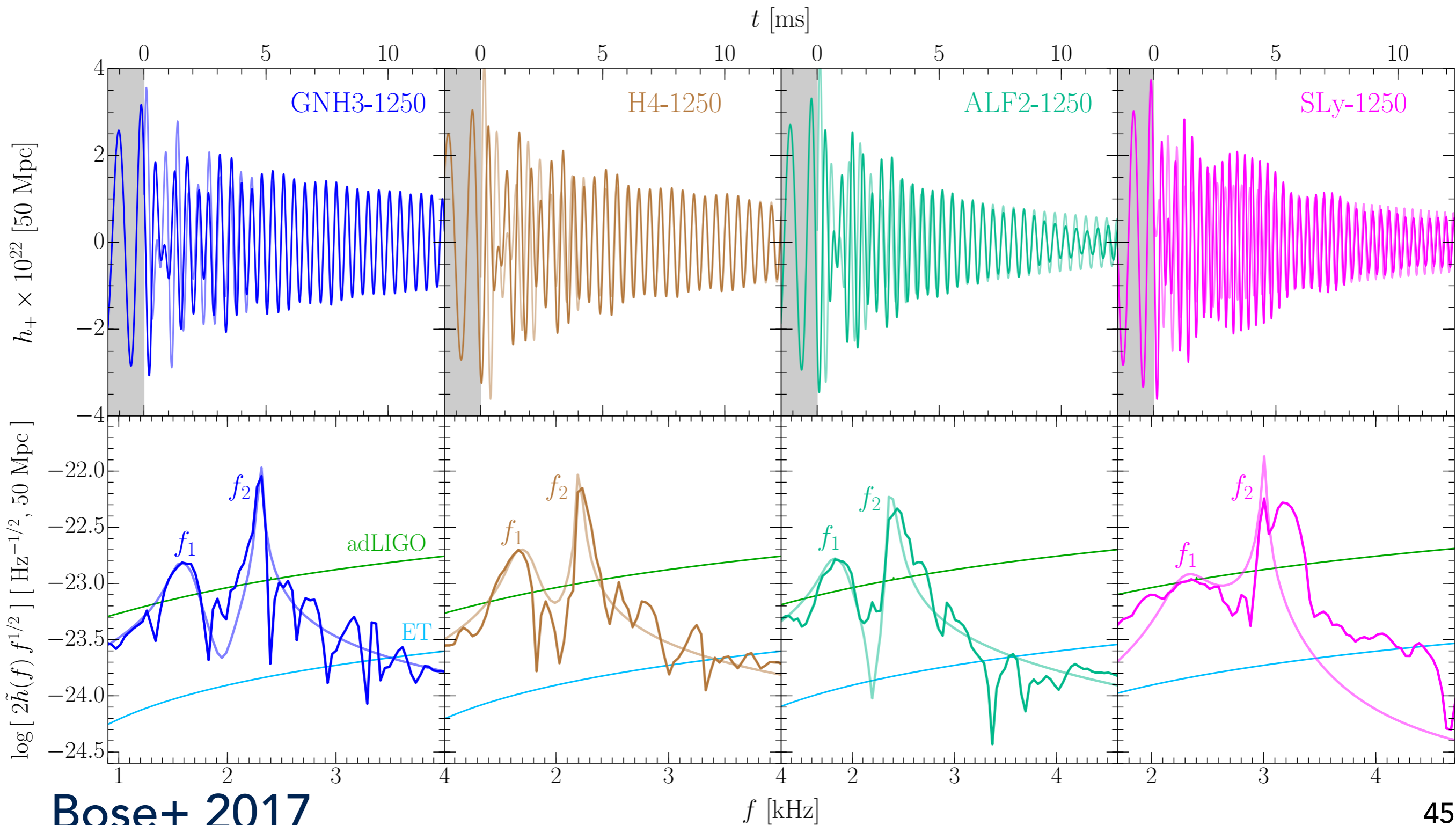


# TIDAL DEFORMABILITY OF NEUTRON STARS



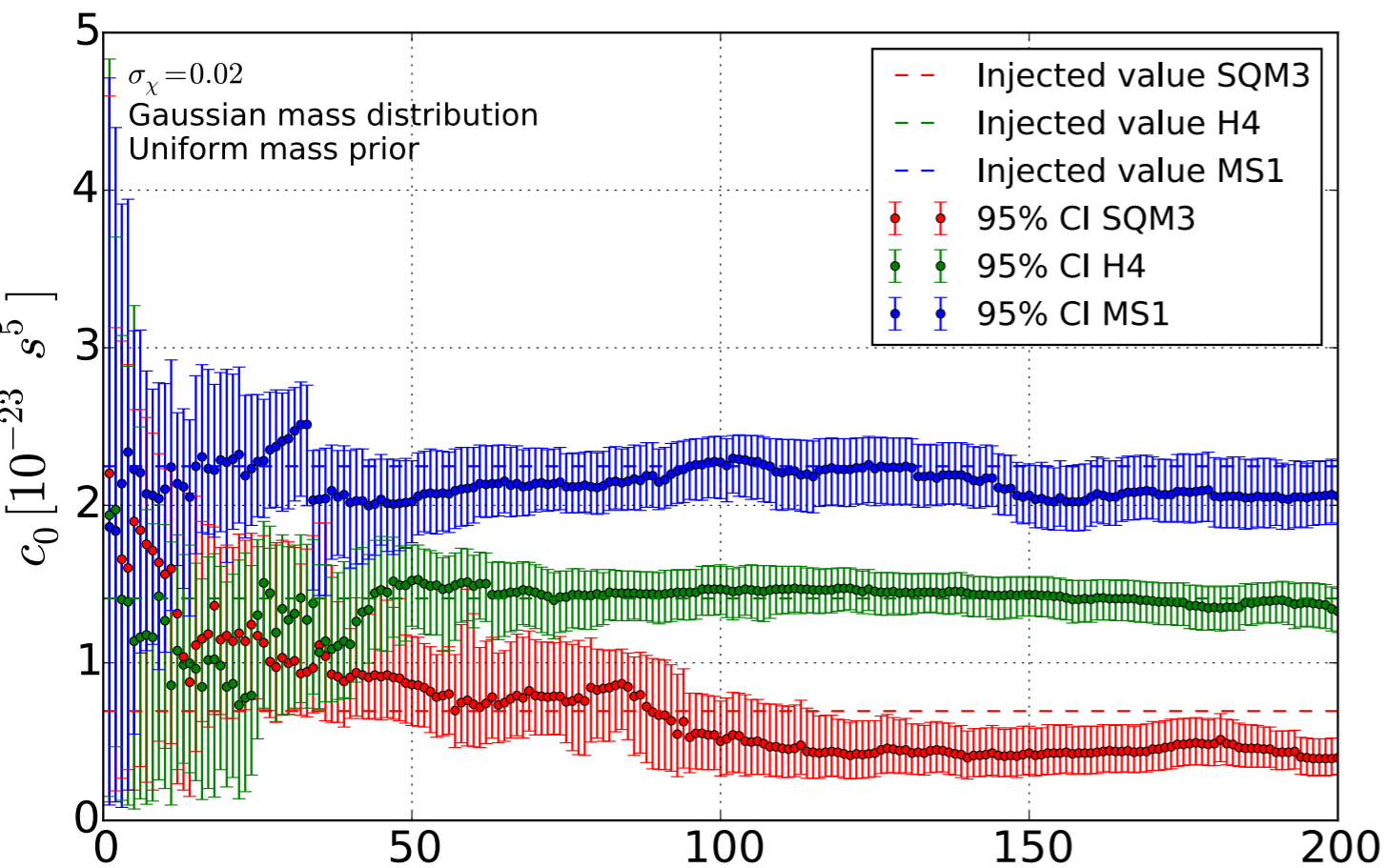
# BINARY NEUTRON STAR WAVEFORMS

$$h(t) = \alpha \exp(-t/\tau_1) [\sin(2\pi f_1 t) + \sin(2\pi(f_1 - f_{1\epsilon})t) + \sin(2\pi(f_1 + f_{1\epsilon})t)] + \exp(-t/\tau_2) \sin(2\pi f_2 t + 2\pi\gamma_2 t^2 + \pi\beta_2).$$

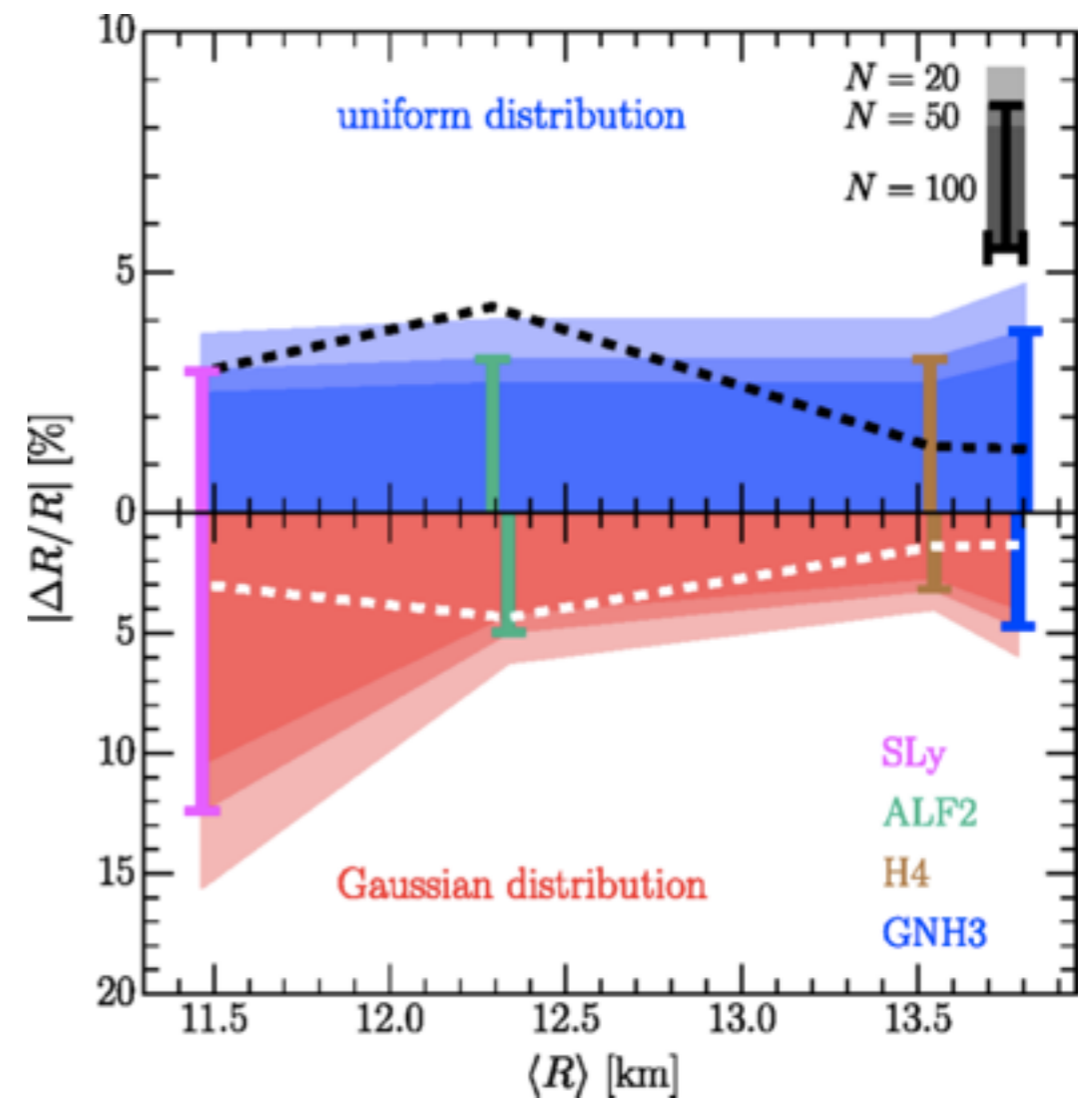


Equation of state from inspiral part of the waveform

radius and tidal deformability from the post-merger signal

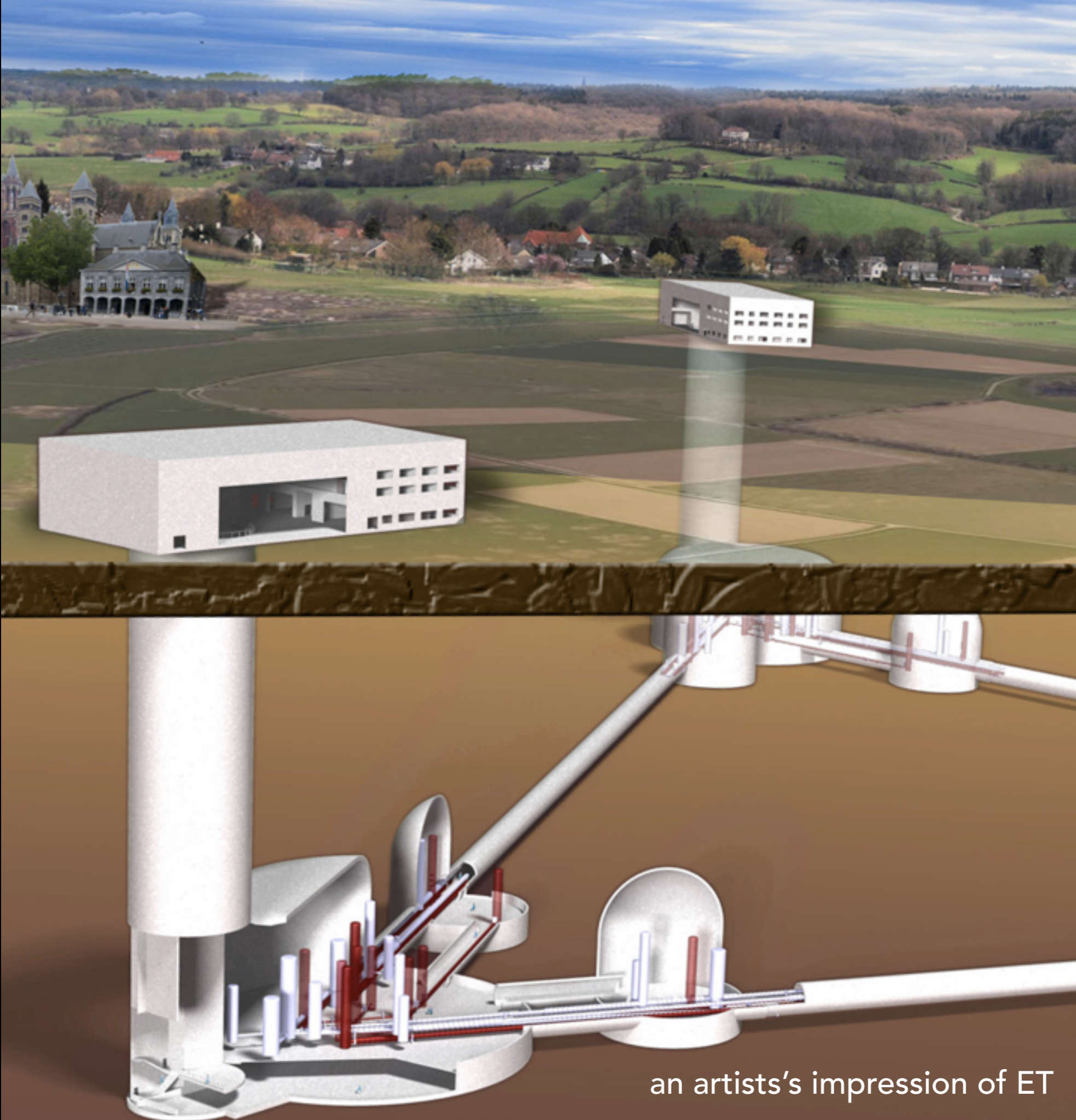


Agathos+, 2015



Bose+, 2017





**VOYAGER:**  
x 3 improvement  
in aLIGO strain  
sensitivity

**EINSTEIN  
TELESCOPE:**  
Triangular, 10 km  
arm length,  
underground,  
cryogenic  
detectors

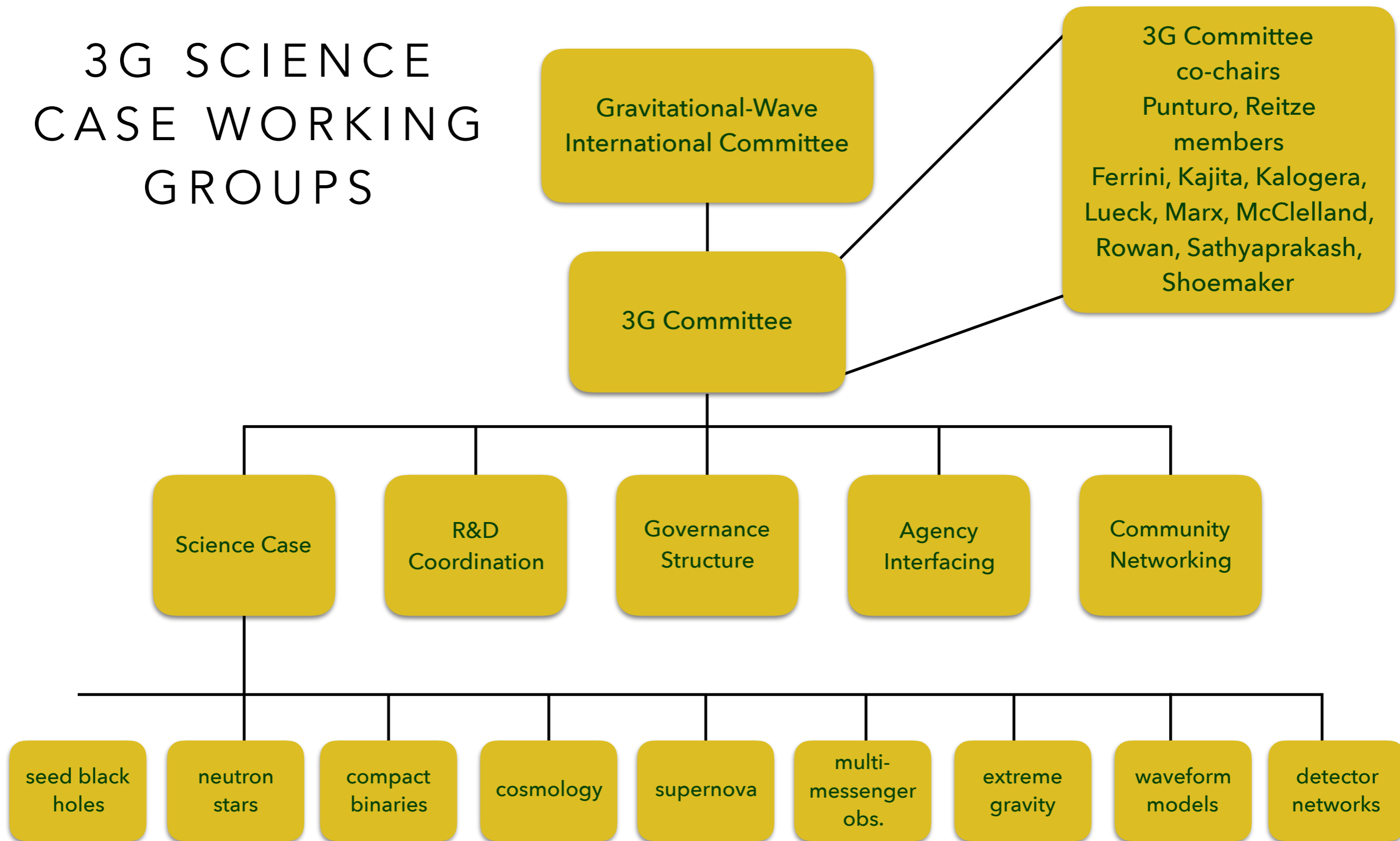
**COSMIC  
EXPLORER:**  
40 km arm length,  
cryogenic,  
overground  
interferometer

an artist's impression of ET

# NEXT GENERATION OF GW DETECTORS

- to fully exploit the GW window we will need new facilities
- GWIC formed a subcommittee to develop a vision for the next generation of ground-based detectors
- one of the charges to the GWIC subcommittee is:
  - *“commission a study of ground-based gravitational wave science from the global scientific community, investigating potential science vs. architecture vs. network configuration vs. cost trade-offs, ...”*
- GWIC subcommittee has constituted five 3G subcommittees:
  - (1) Science Case Team (3G-SCT), (2) R&D Coordination, (3) Governance, (4) Agency Interfacing, (5) Community Networking
- the Science Case will be developed by an international consortium of scientists under the leadership of the 3G-SCT (18 members)

# 3G SCIENCE CASE WORKING GROUPS



for membership of committees see:  
<https://gwic.ligo.org/3Gsubcomm/>

# WHAT CAN GW ASTRONOMY TELL US?

## ❖ fundamental physics

- ❖ equation of state of ultra dense matter, dark energy EoS
- ❖ gravastars, wormholes, ..., testing non-BH paradigms?

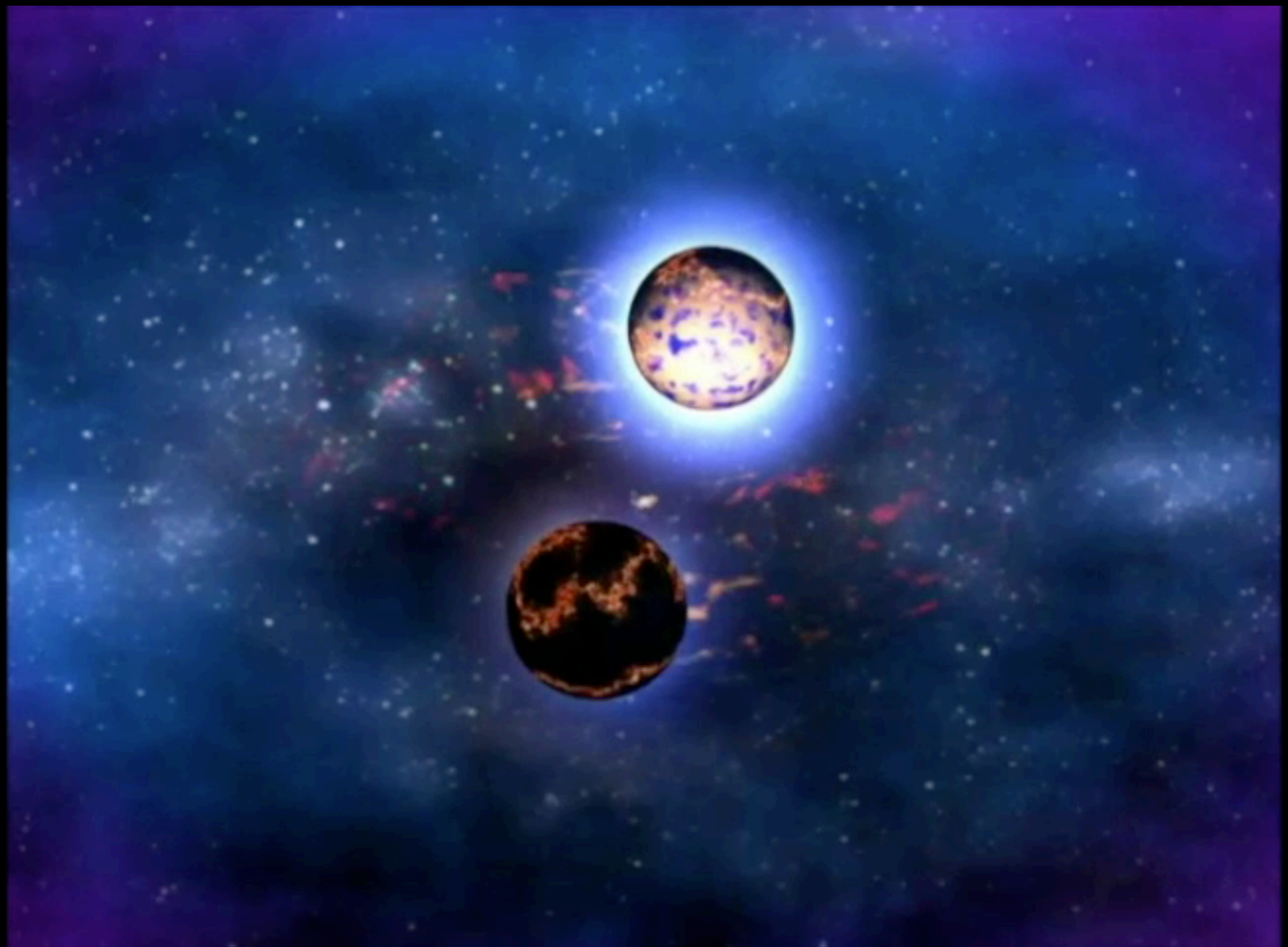
## ❖ astrophysics

- ❖ formation and evolution of compact binaries, GRB engines, supernovae

## ❖ cosmology

- ❖ primordial and astronomical GW backgrounds
- ❖ primordial origin of black hole binaries
- ❖ standard siren cosmography









# LIGO-LIVINGSTON OBSERVATORY





# LIGO-HANFORD OBSERVATORY





# VIRGO AT CASCINA, ITALY



Credit: Virgo

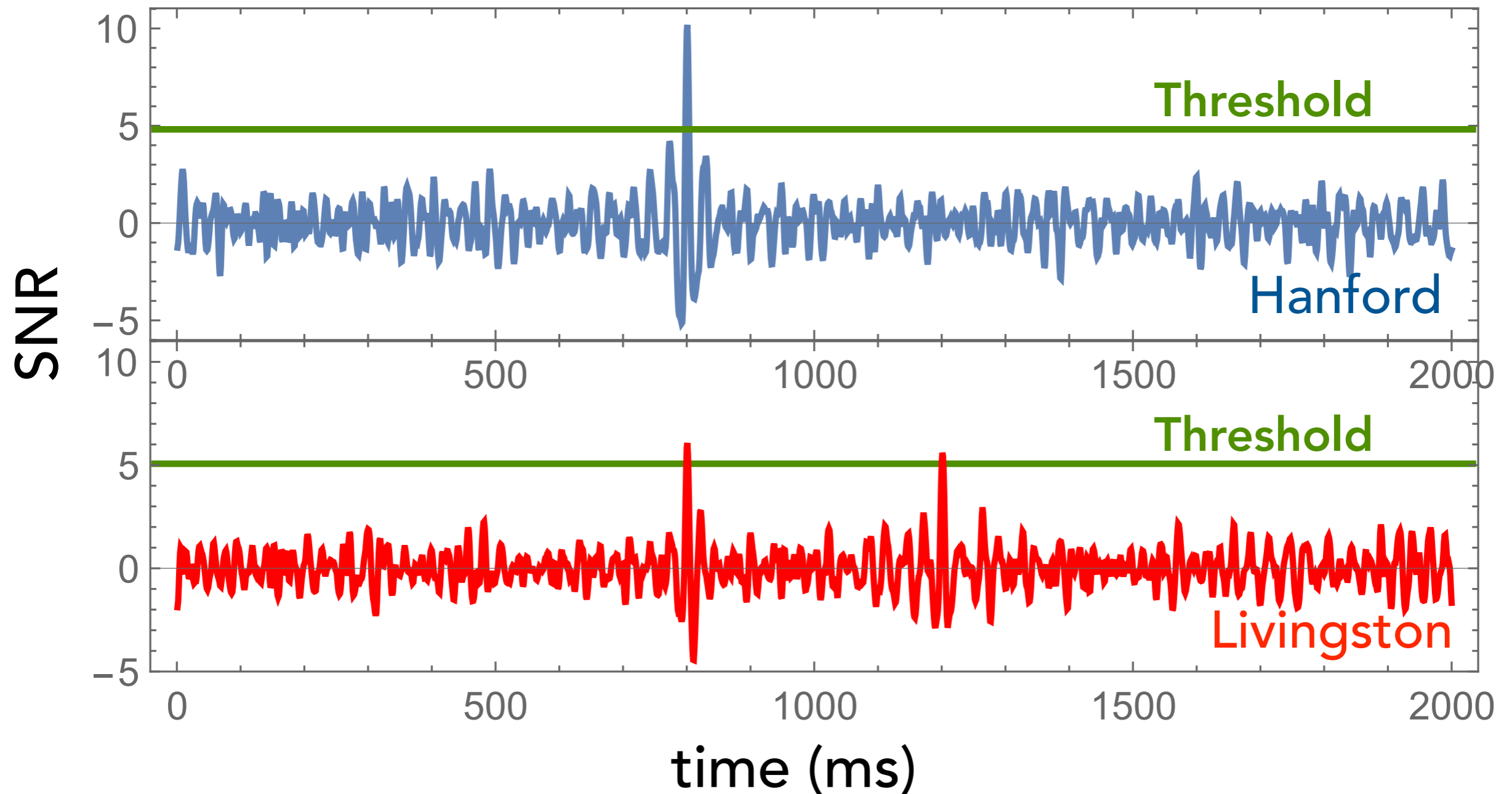
# HOW DO WE MEASURE THE BACKGROUND?

- two independent methods are used to measure the background
  - method of **time-shifts** with coincident triggers
  - method of **likelihood** with single detector triggers
- **time-shift** method
  - change the time stamp of triggers from one detector relative to the other by more than the light travel time between the detectors and then look for coincidence
- likelihood method
  - compute the probability density function of non-coincident triggers as a function of their likelihood for each detector; deduce the likelihood of chance coincidence from the distributions



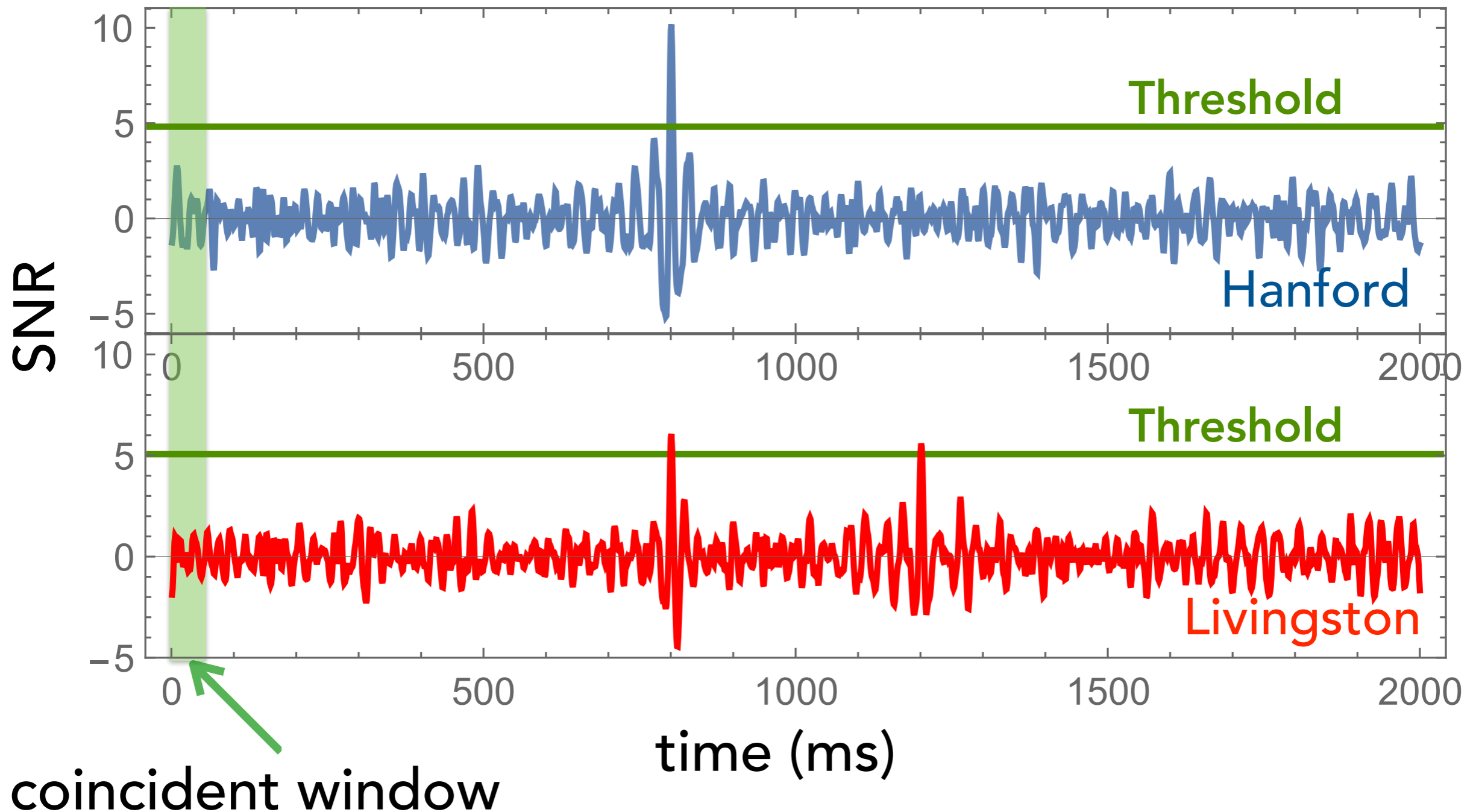
# COINCIDENT DETECTION

- coincidence detection: look for triggers coincident within light-travel time in a network of detectors



# COINCIDENT DETECTION

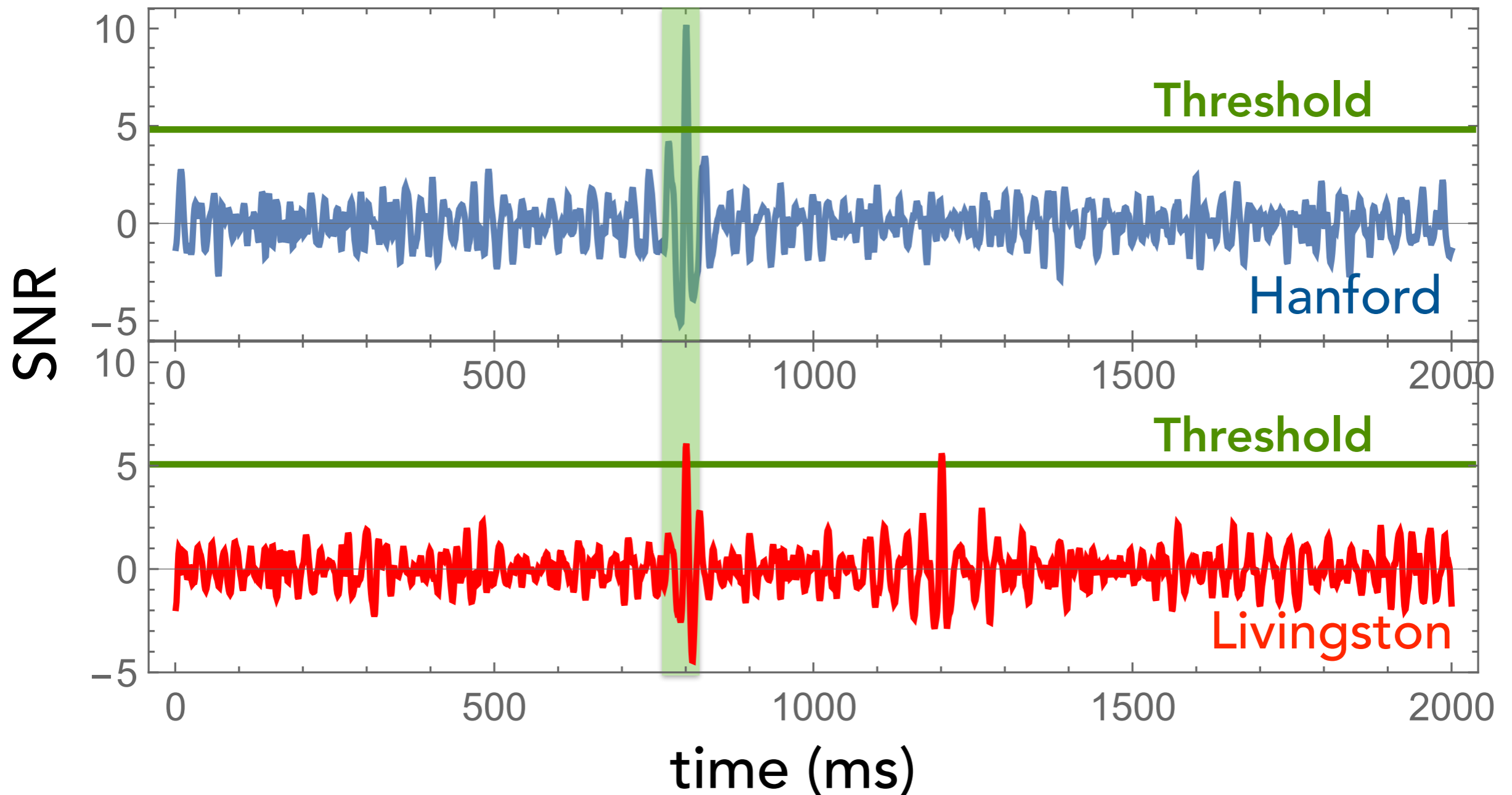
- coincidence detection: look for triggers coincident within light-travel time in a network of detectors





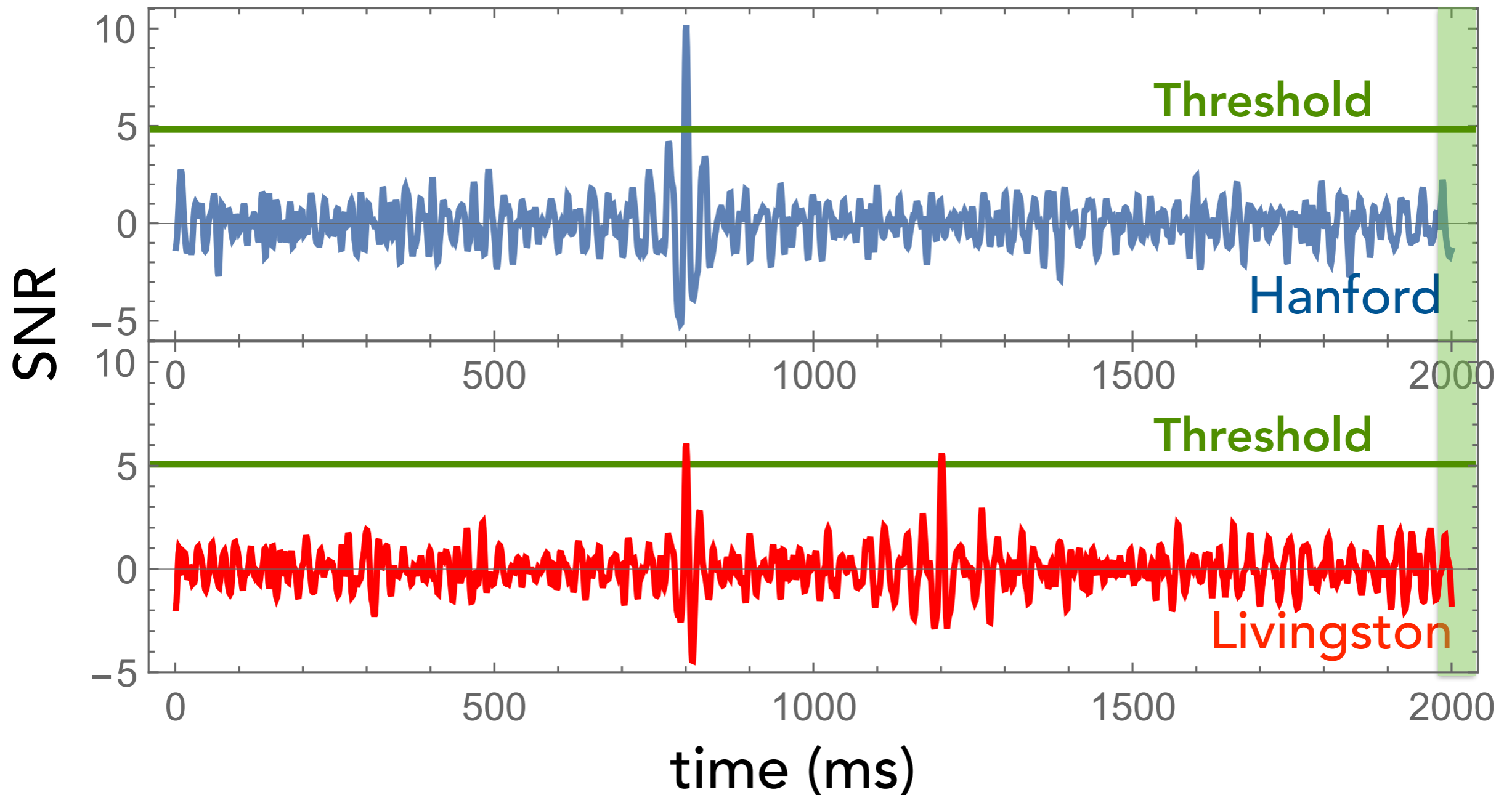
# COINCIDENT DETECTION

- coincidence detection: look for triggers coincident within light-travel time in a network of detectors



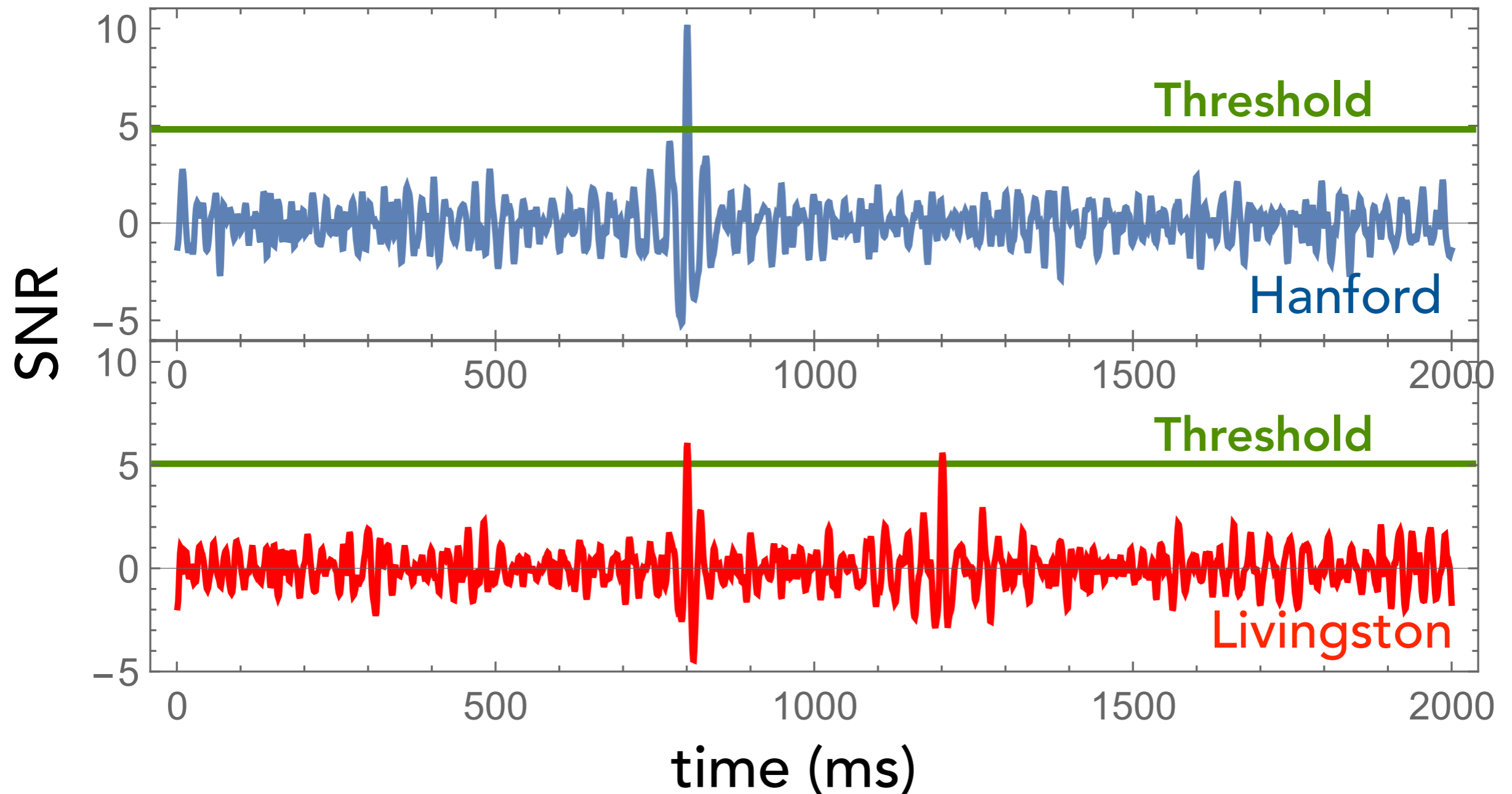
# COINCIDENT DETECTION

- coincidence detection: look for triggers coincident within light-travel time in a network of detectors



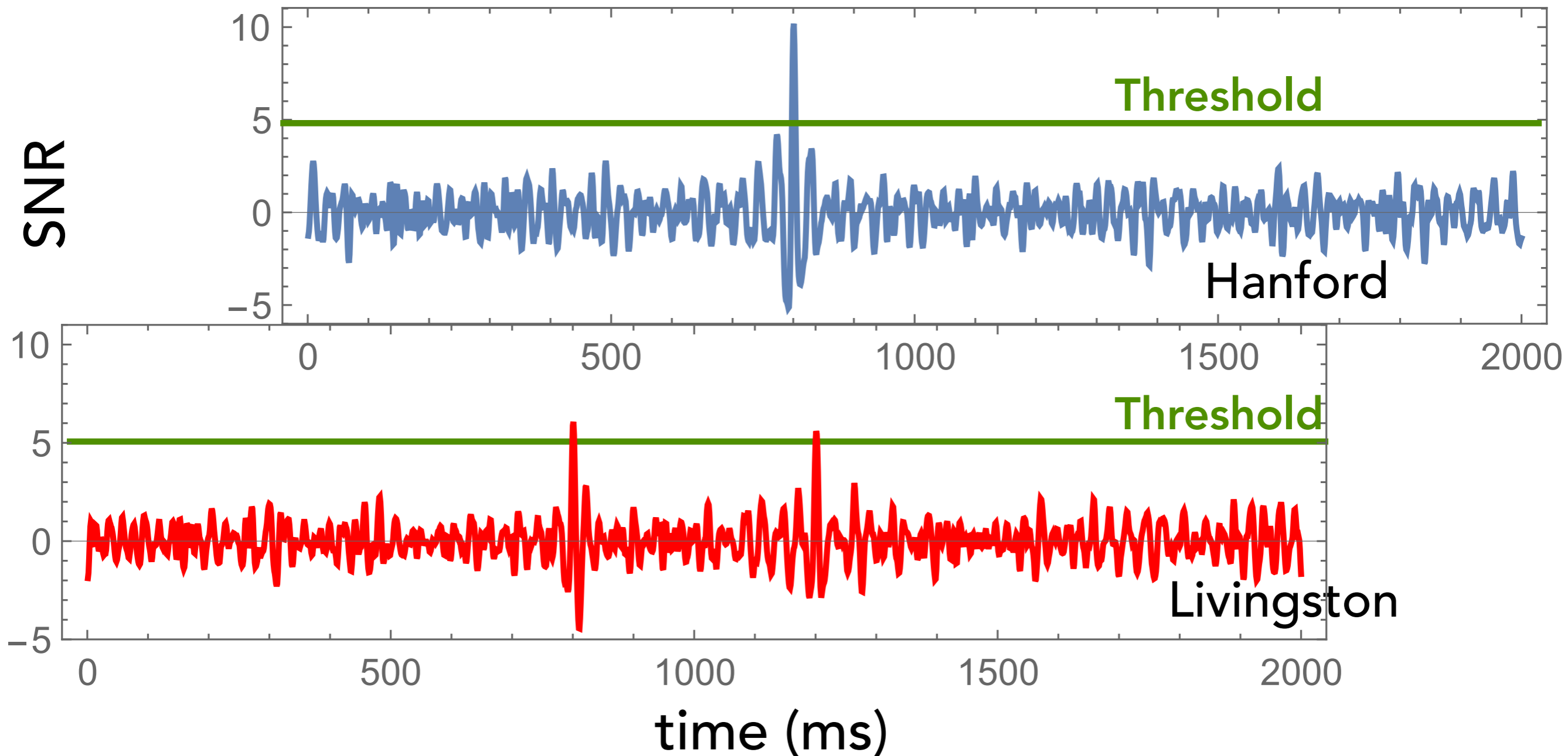
# COINCIDENT DETECTION

- coincidence detection: look for triggers coincident within light-travel time in a network of detectors



# TIME-SHIFT METHOD FOR BACKGROUND ESTIMATION

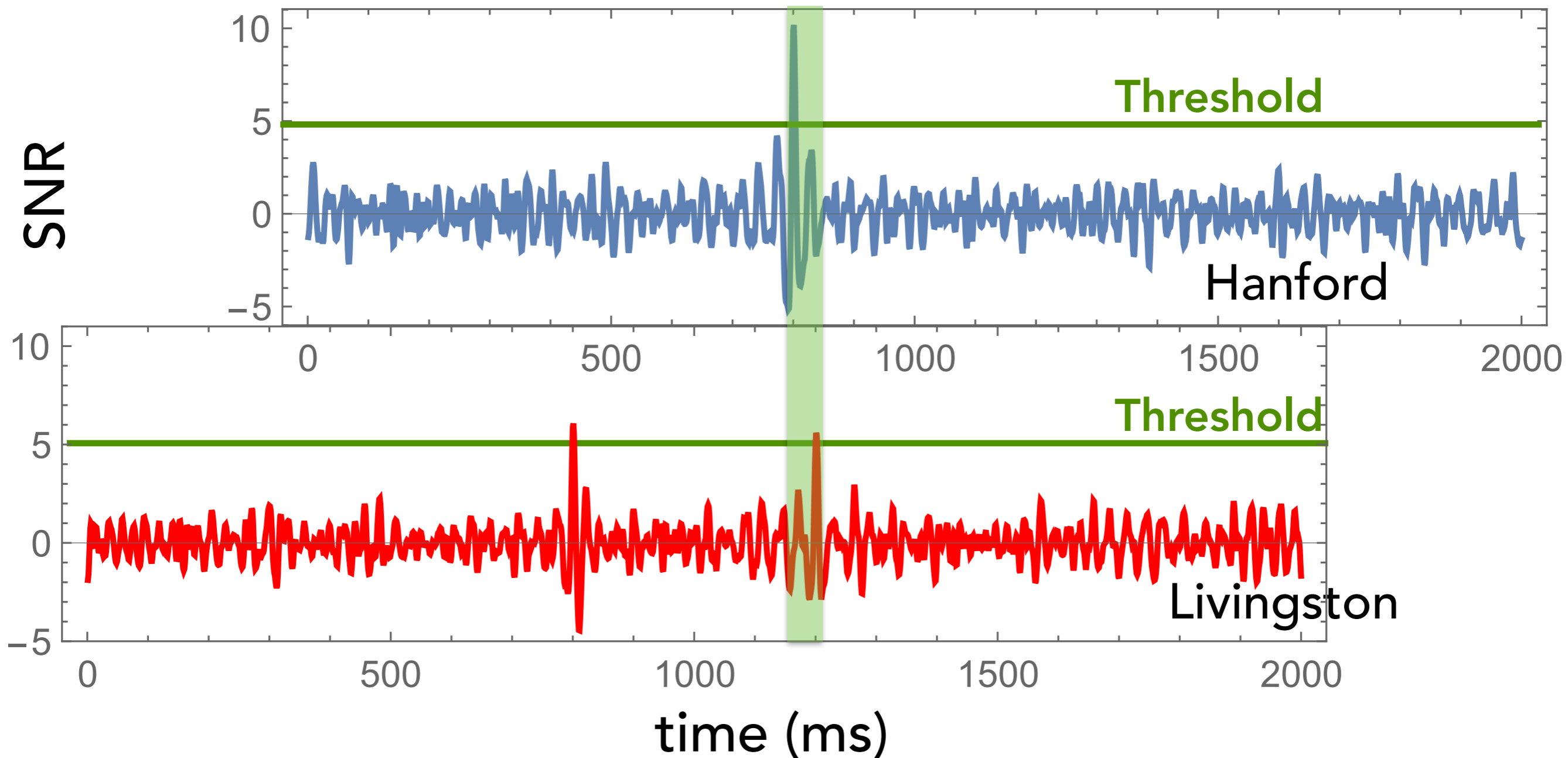
- shift one of the data sets with respect to the other and then look for coincidence - any coincidence now is a false alarm



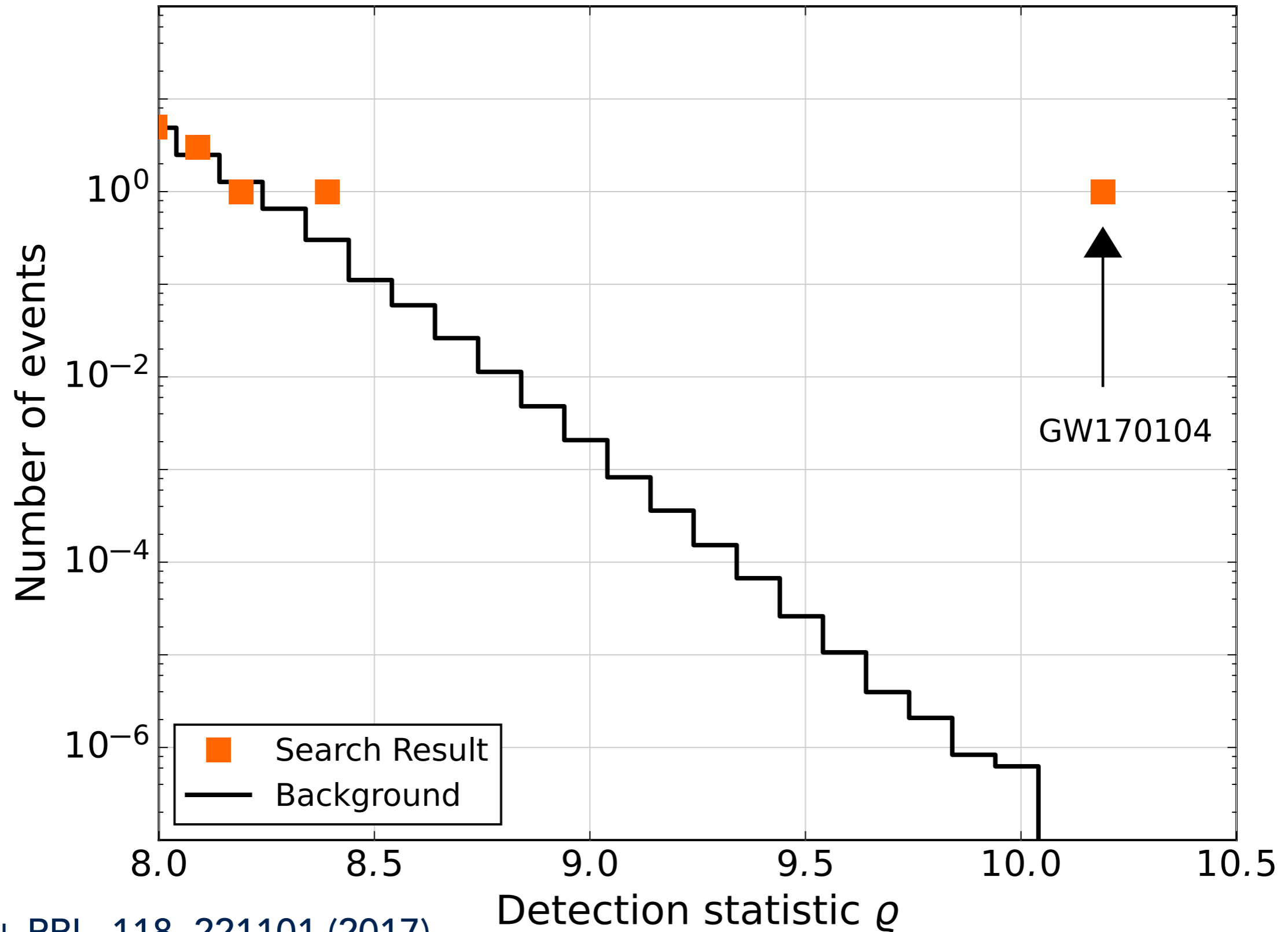


# TIME-SHIFT METHOD FOR BACKGROUND ESTIMATION

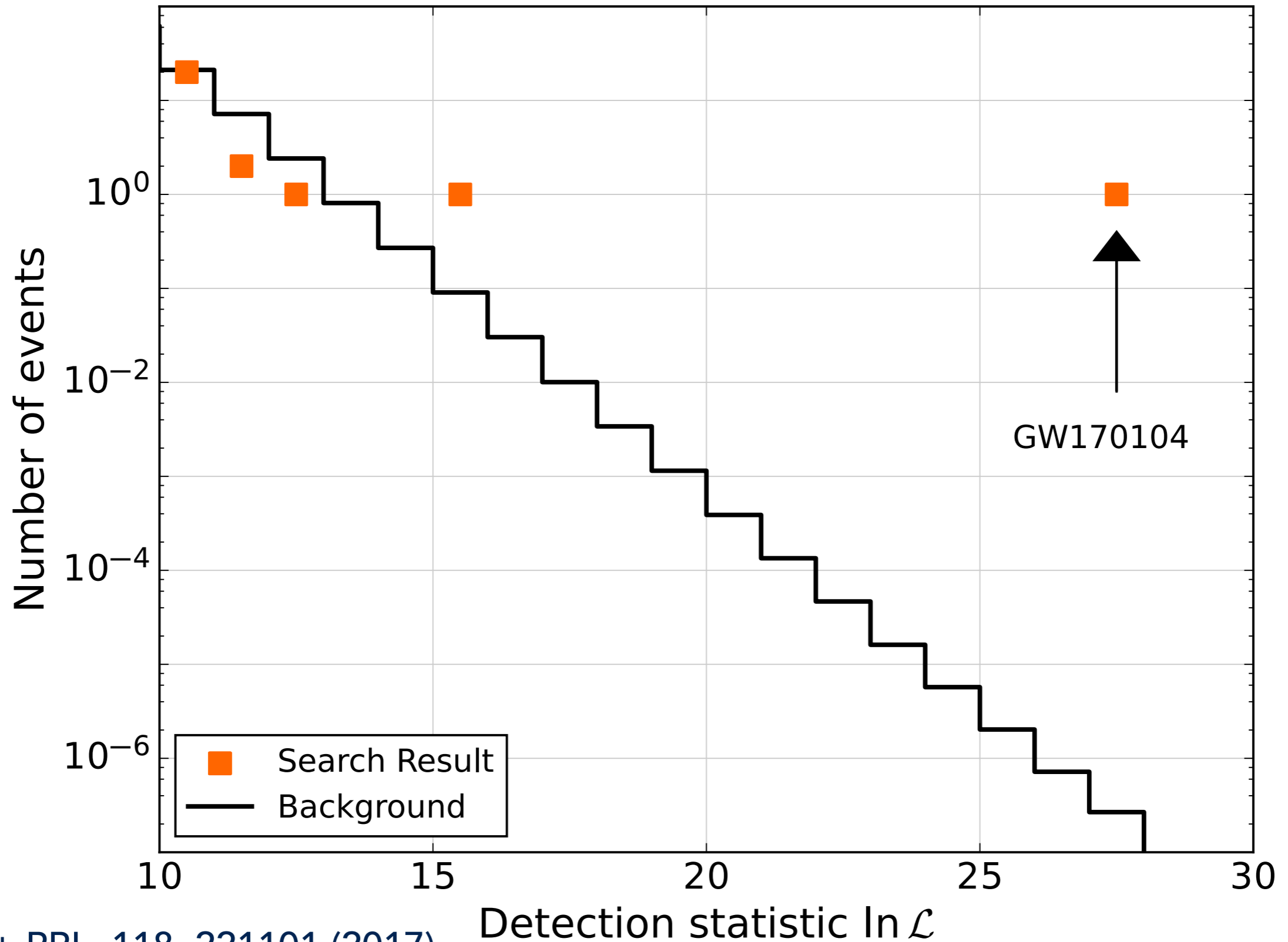
- shift one of the data sets with respect to the other and then look for coincidence - any coincidence now is a false alarm



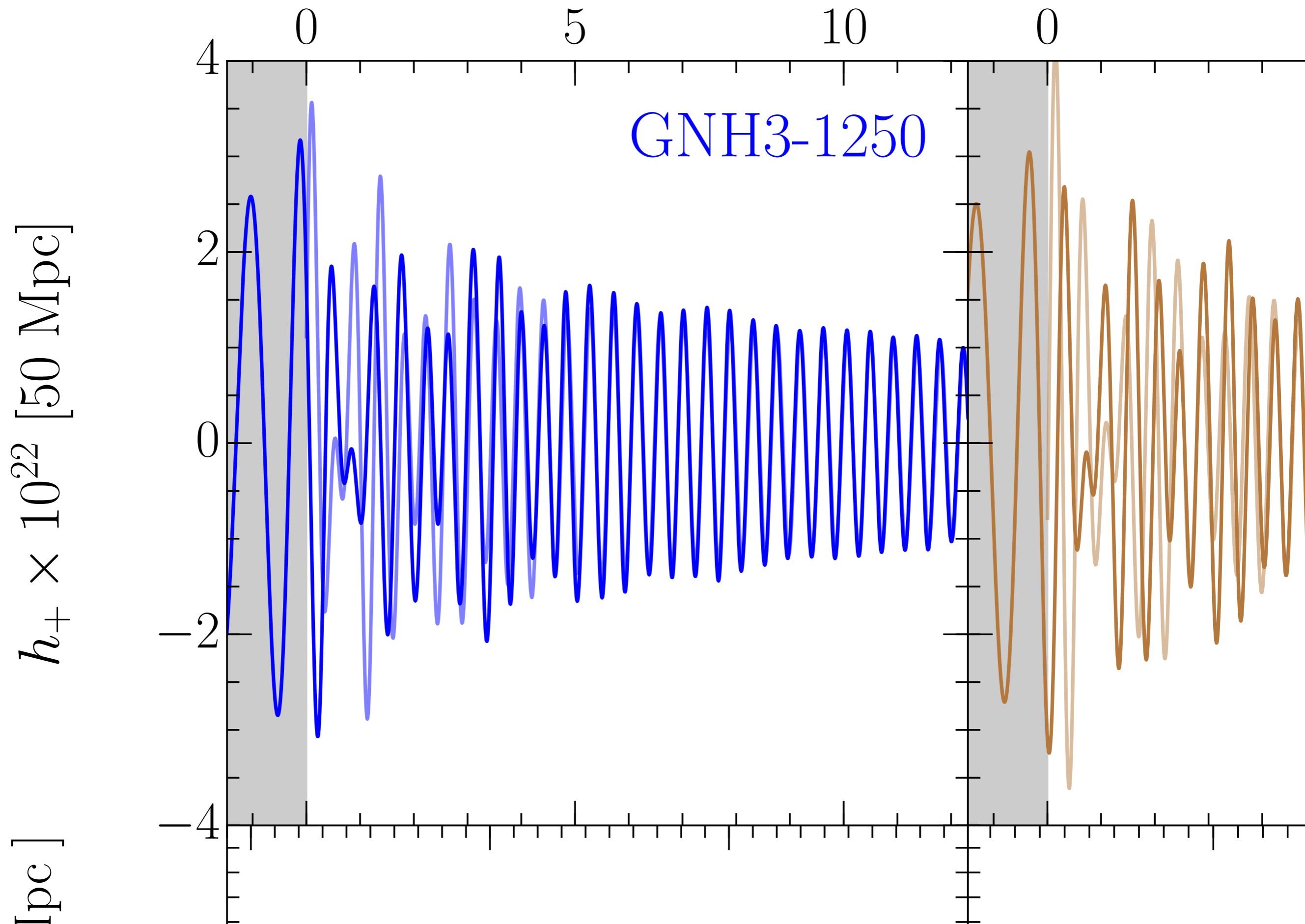
# SIGNIFICANCE OF GW170104: TIME-SHIFT METHOD



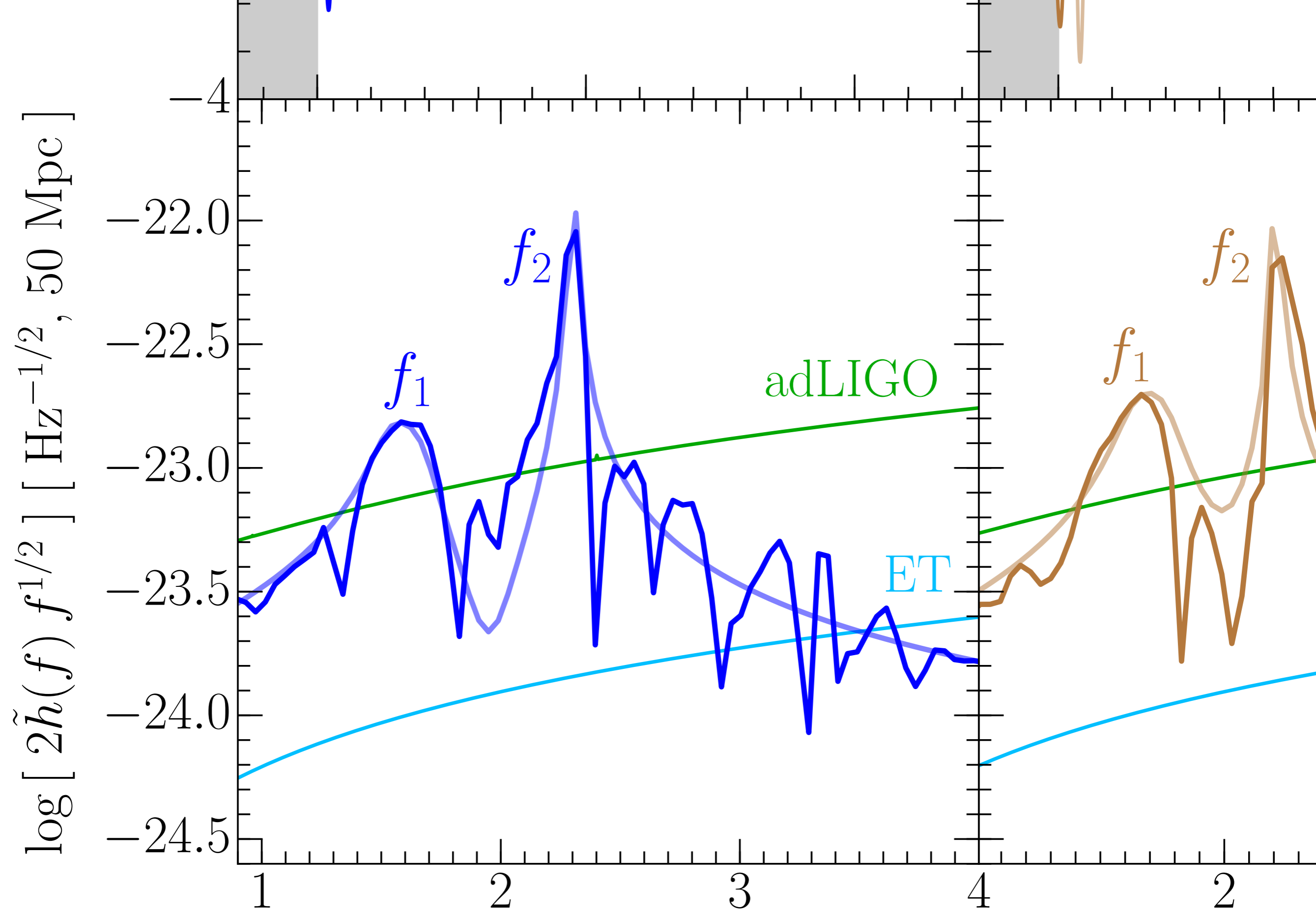
# SIGNIFICANCE OF GW170104: LIKELIHOOD METHOD



Bose+ 2017







Bose+ 2017

$t$  [ms]

10

0

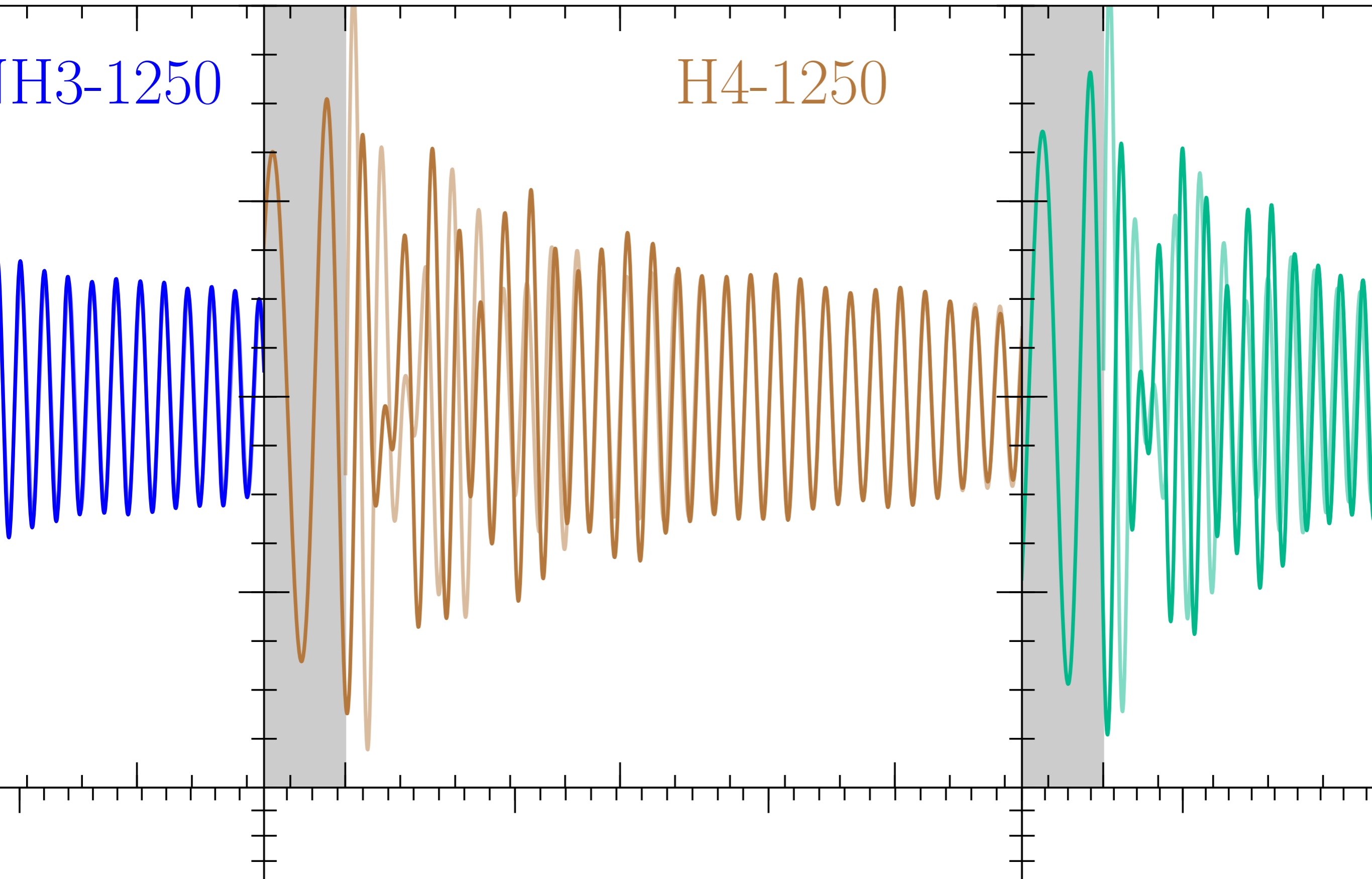
5

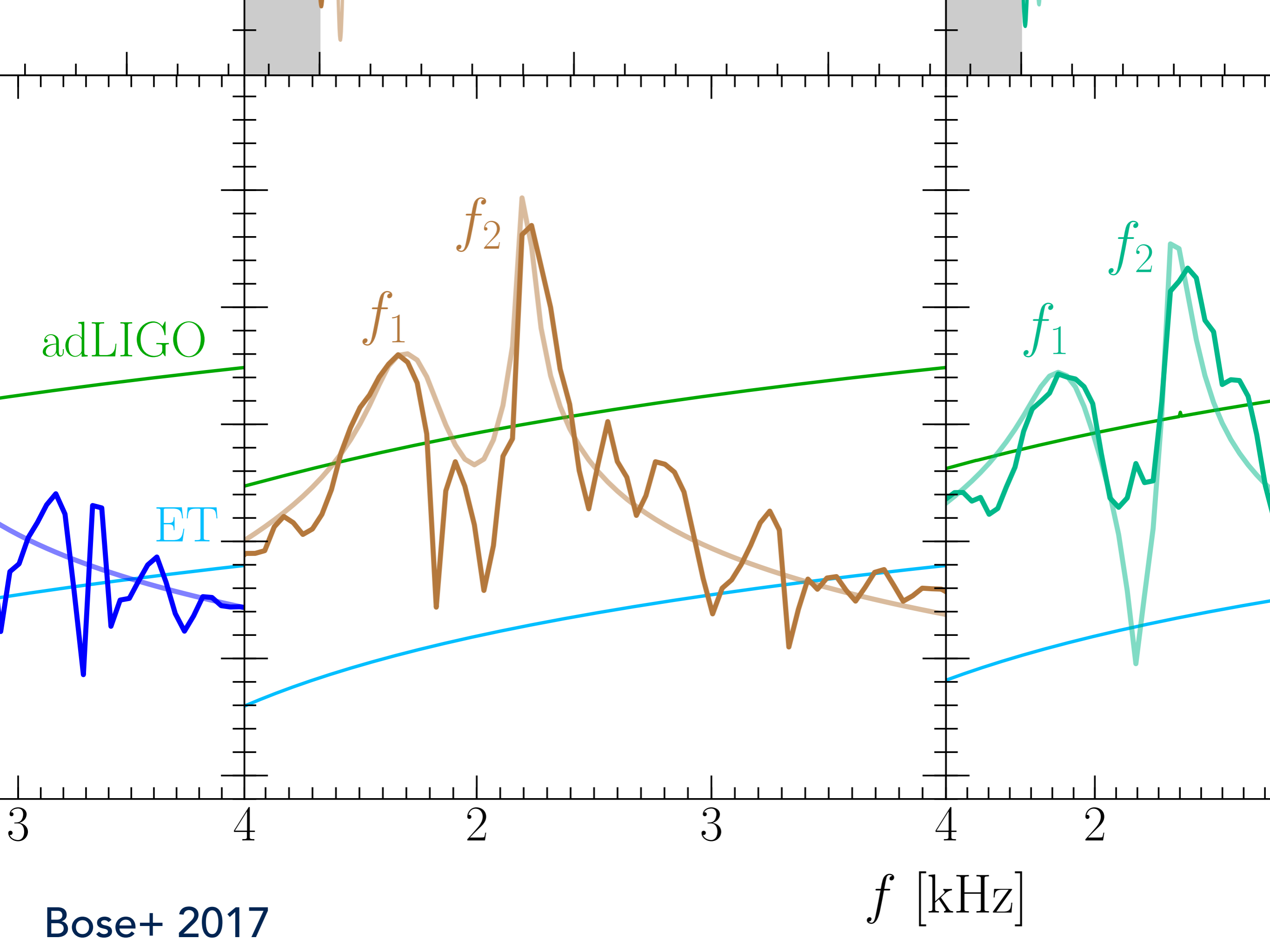
10

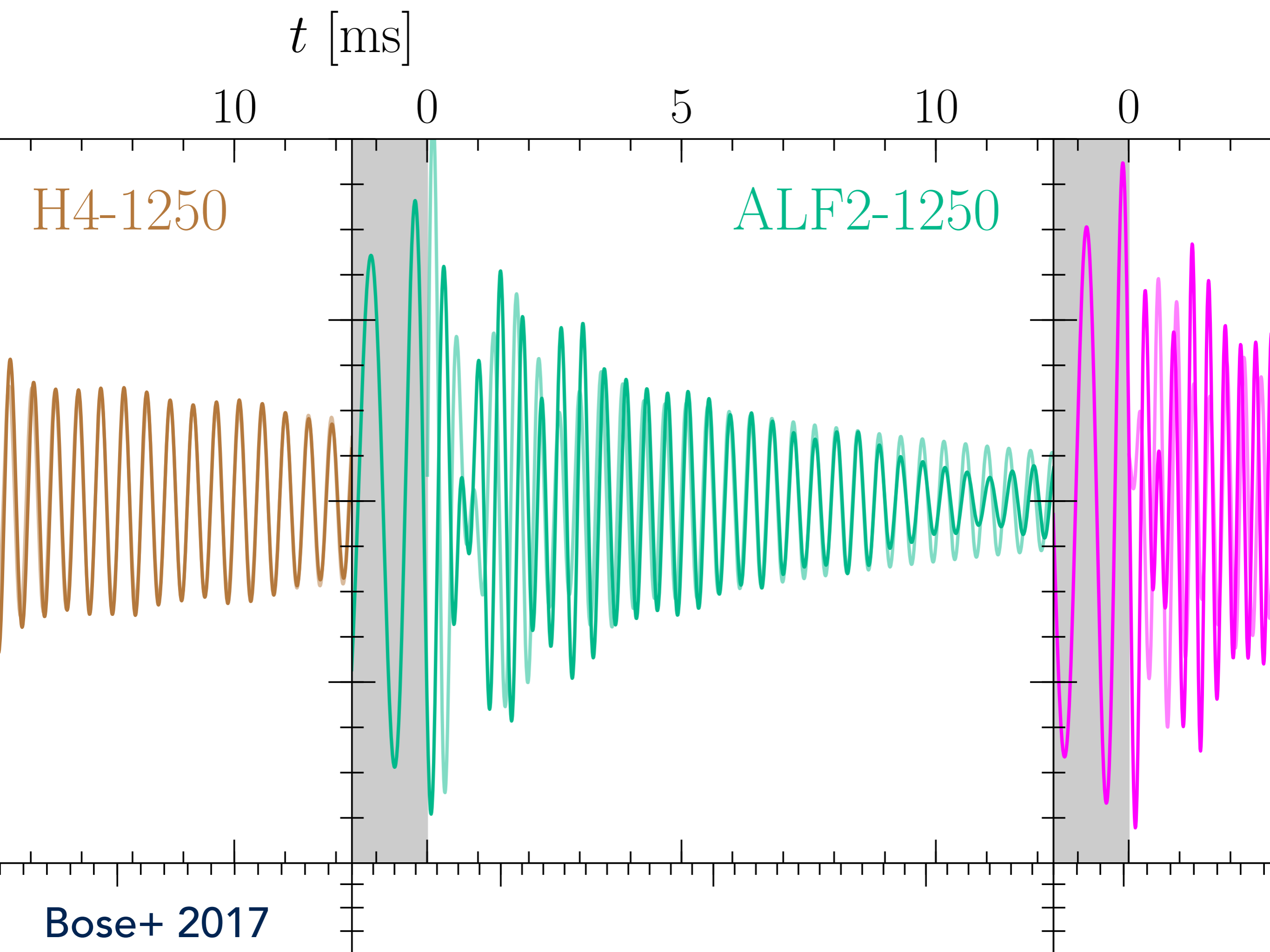
0

H3-1250

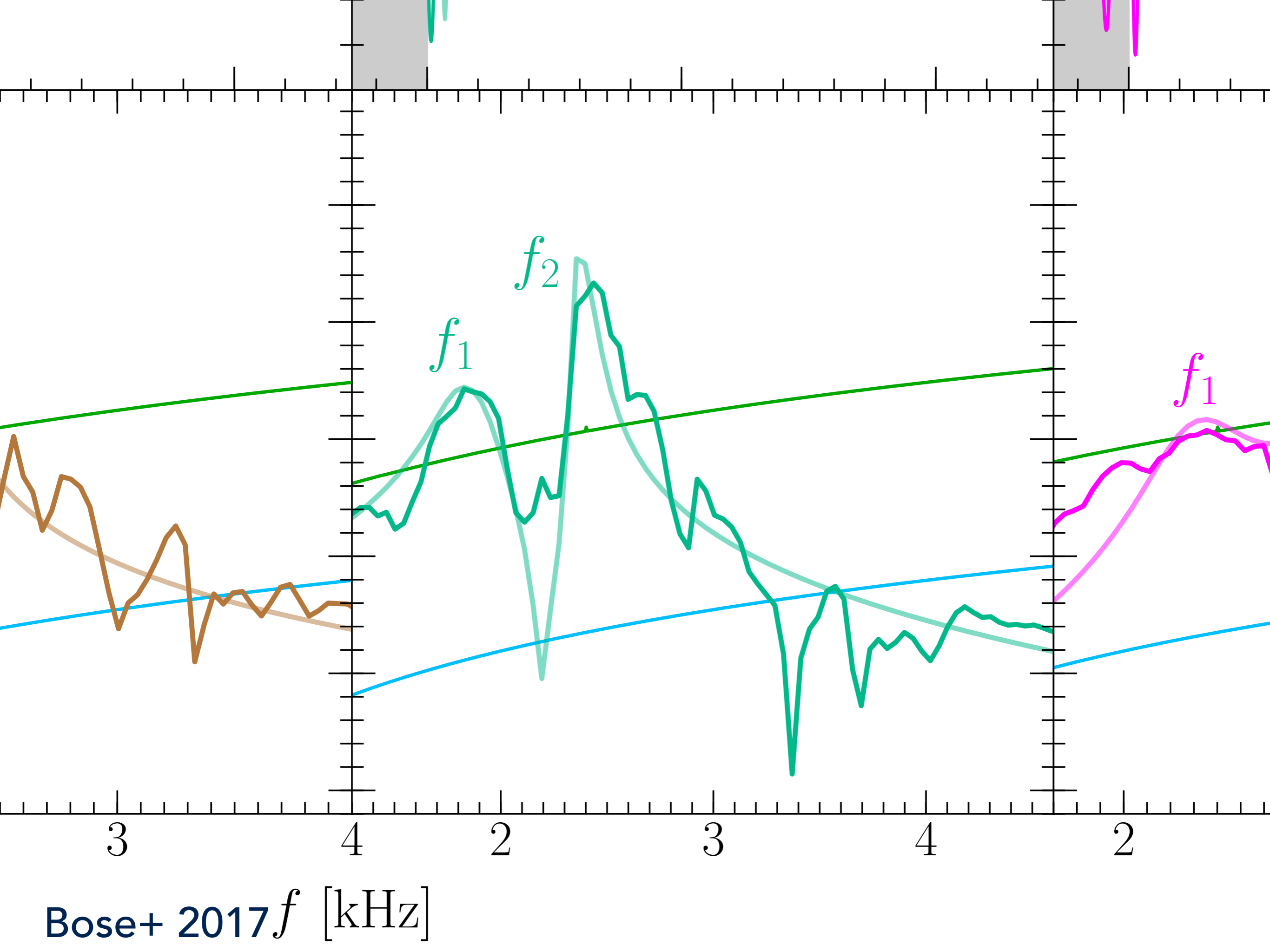
H4-1250

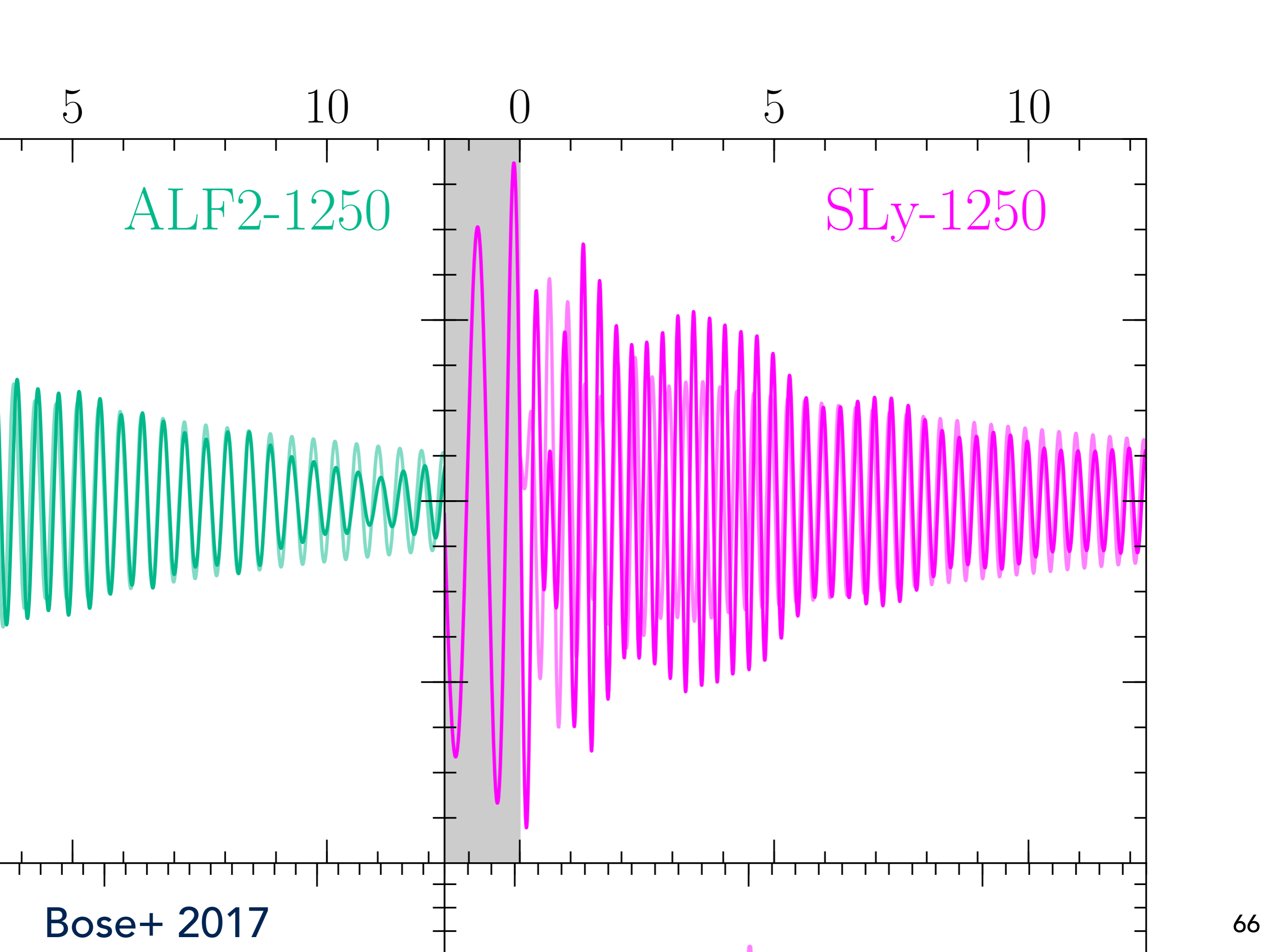












5

10

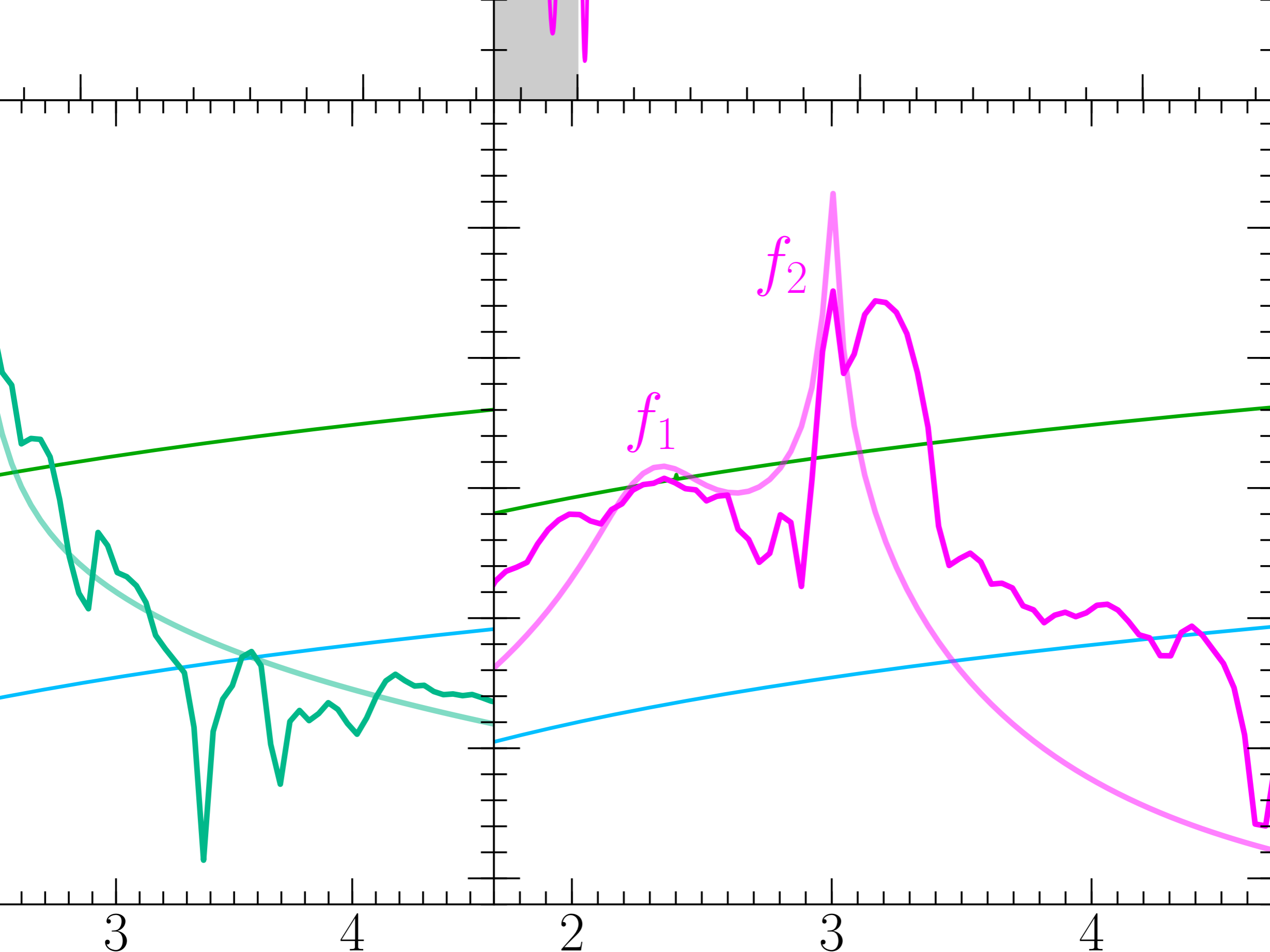
0

5

10

ALF2-1250

SLy-1250



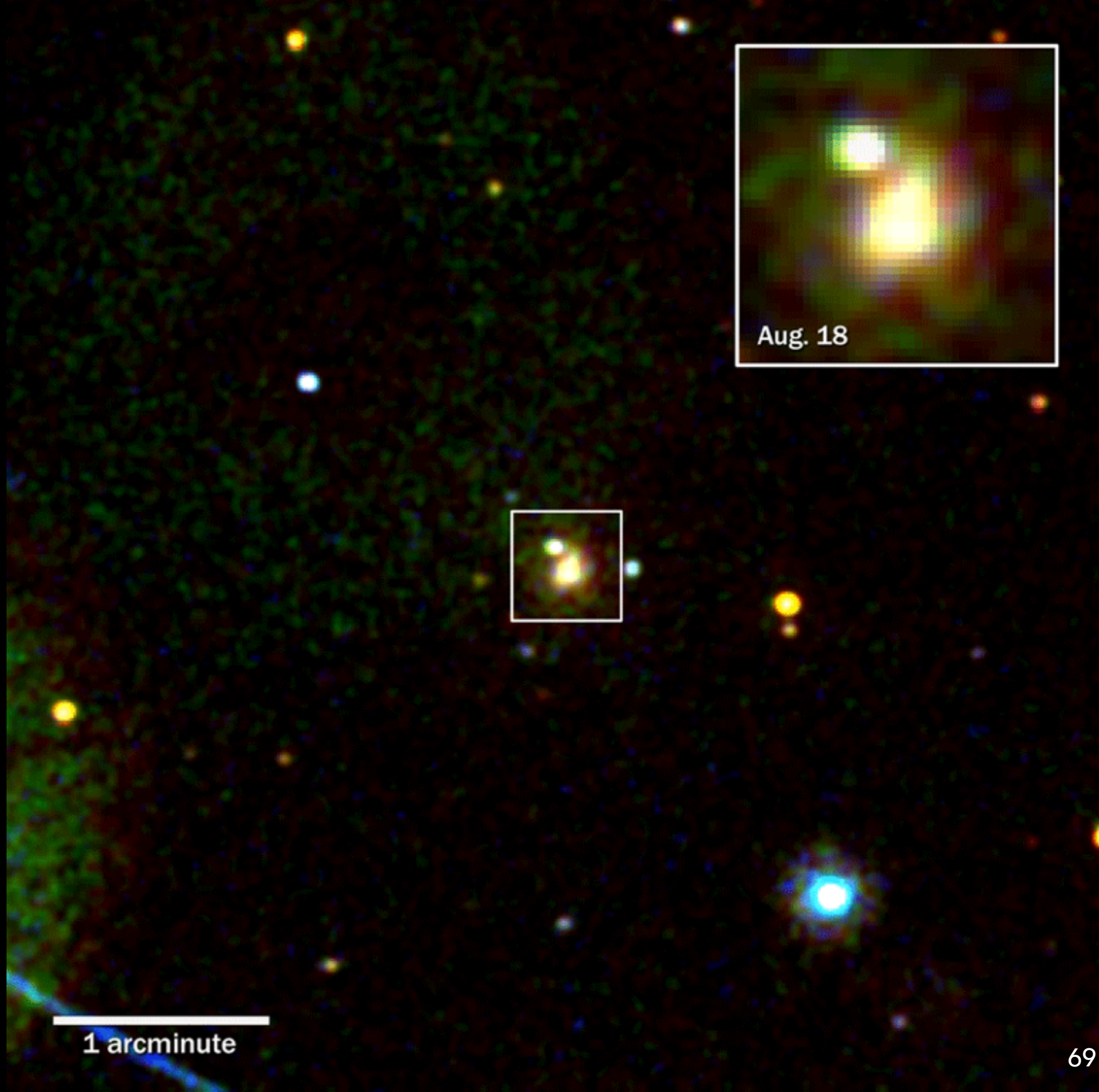
# HOST LOCATED IN NGC 4993



NGC 4993  
[NGC 4994]

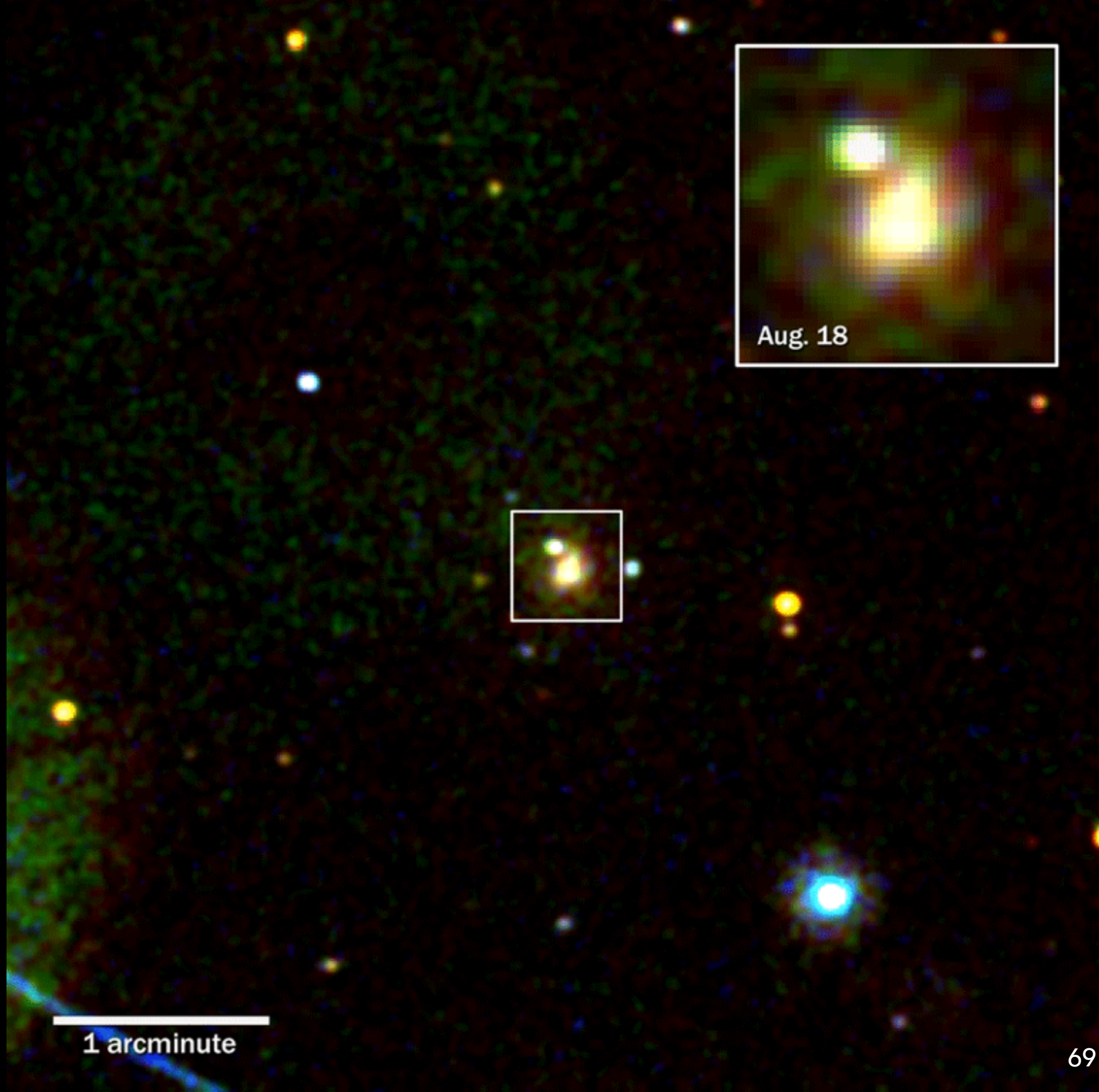


UV:  
CREDIT  
NASA  
AND  
SWIFT

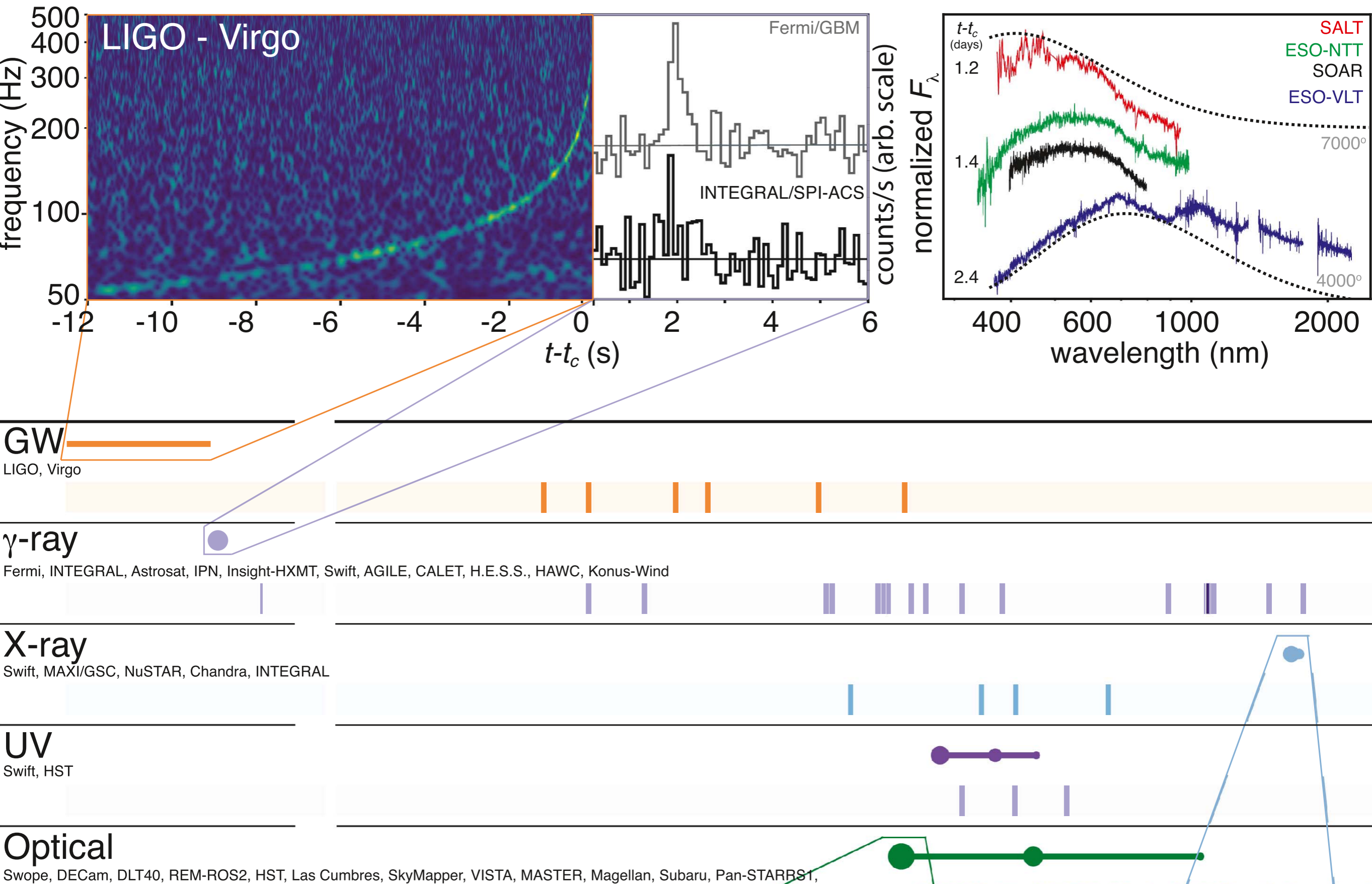


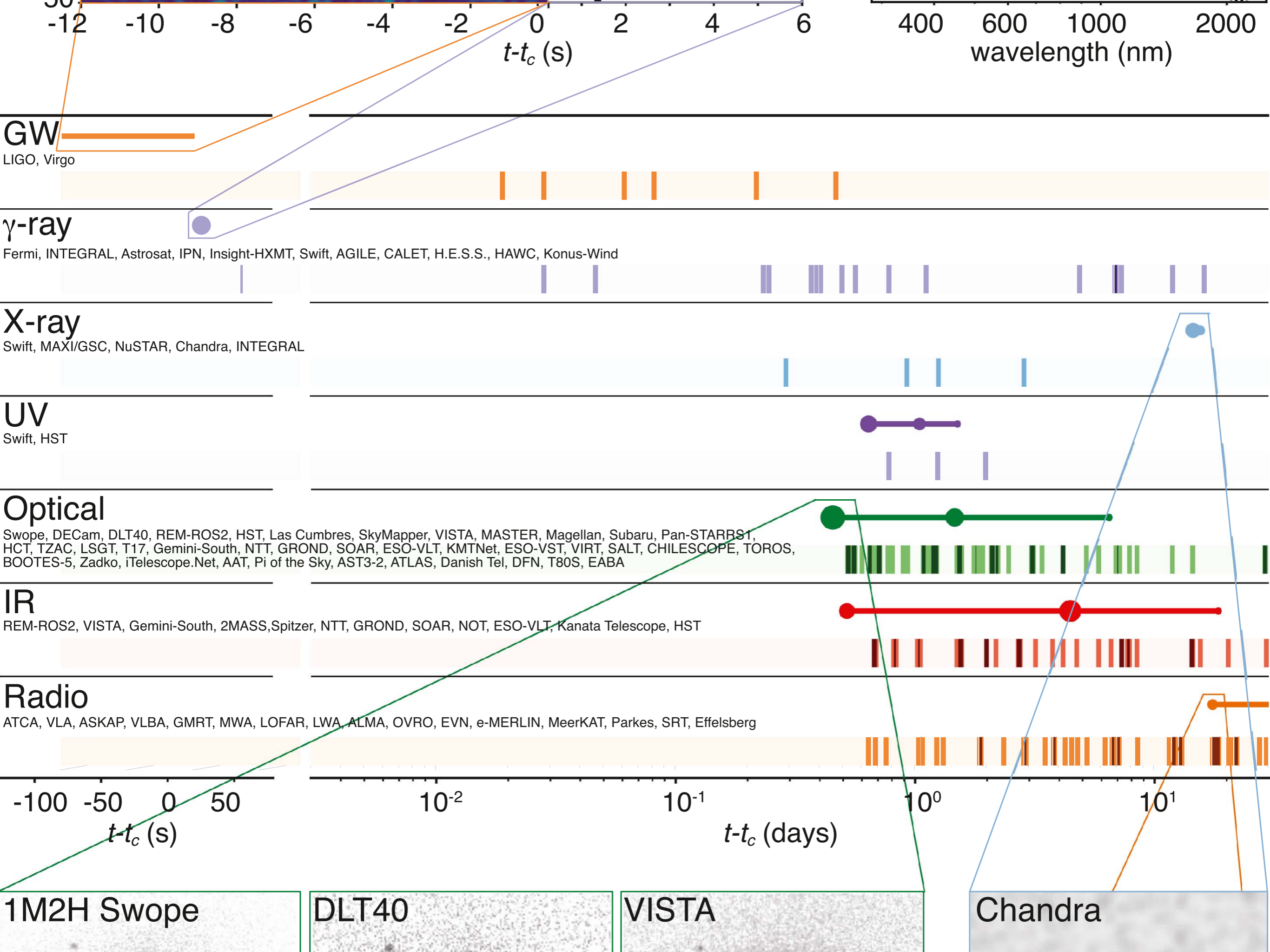


UV:  
CREDIT  
NASA  
AND  
SWIFT











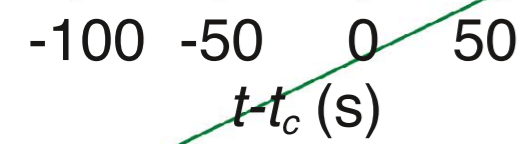
HCT, TZAC, LSGT, T17, Gemini-South, NTT, GROND, SOAR, ESO-VLT, KMTNet, ESO-VST, VIRT, SALT, CHILESCOPE, TOROS, BOOTES-5, Zadko, iTelescope.Net, AAT, Pi of the Sky, AST3-2, ATLAS, Danish Tel, DFN, T80S, EABA

## IR

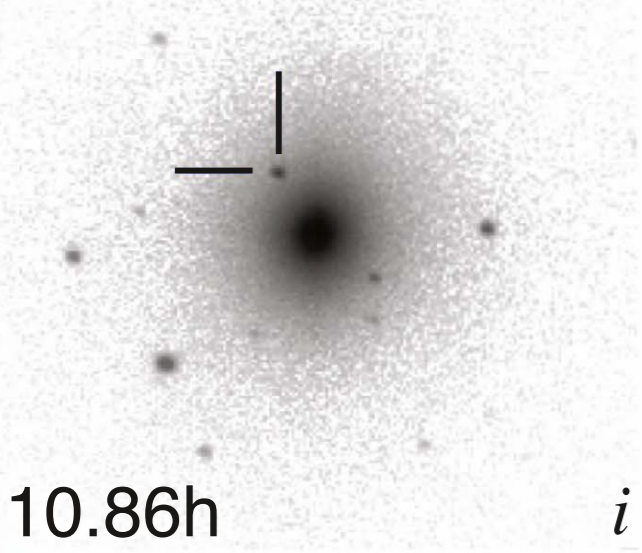
REM-ROS2, VISTA, Gemini-South, 2MASS, Spitzer, NTT, GROND, SOAR, NOT, ESO-VLT, Kanata Telescope, HST

## Radio

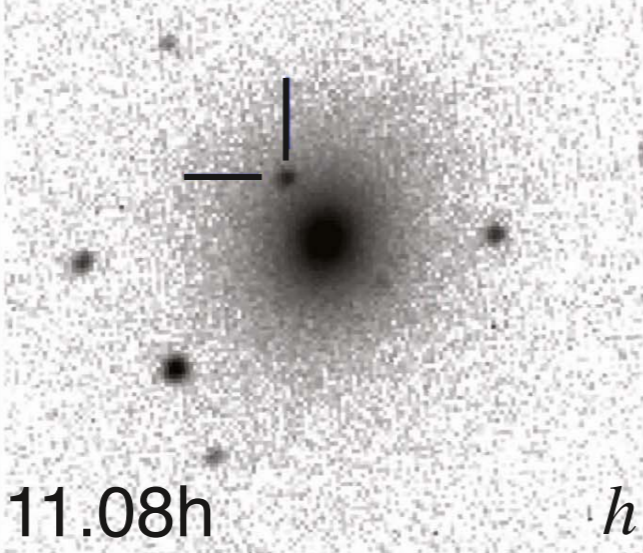
ATCA, VLA, ASKAP, VLBA, GMRT, MWA, LOFAR, LWA, ALMA, OVRO, EVN, e-MERLIN, MeerKAT, Parkes, SRT, Effelsberg



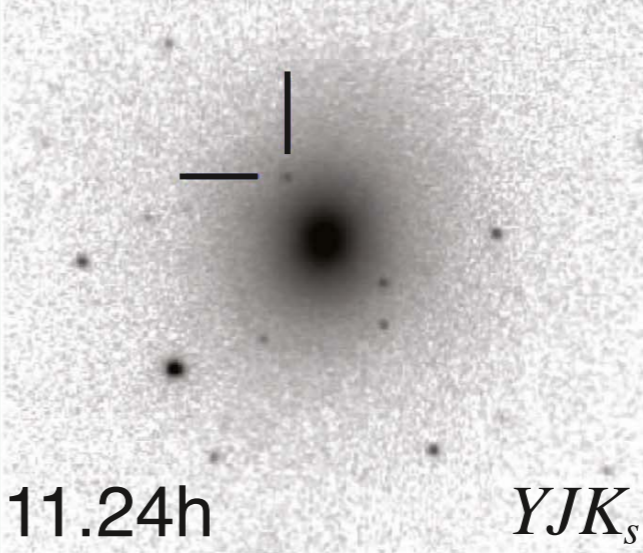
1M2H Swope



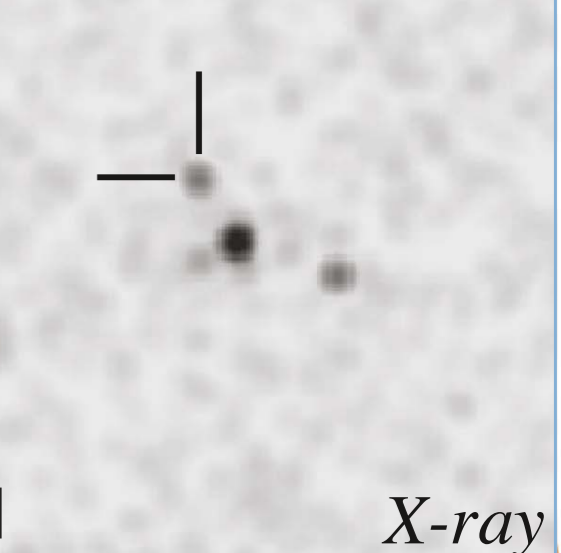
DLT40



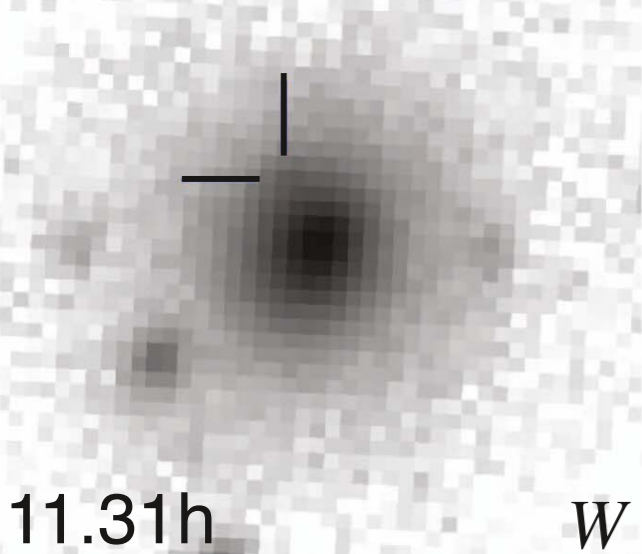
VISTA



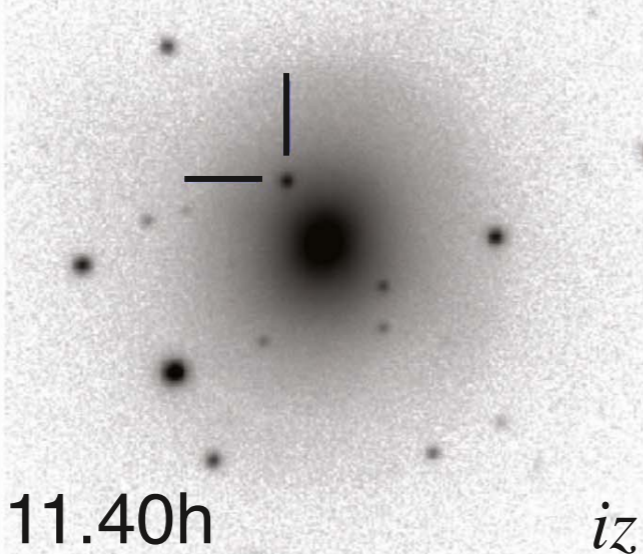
Chandra



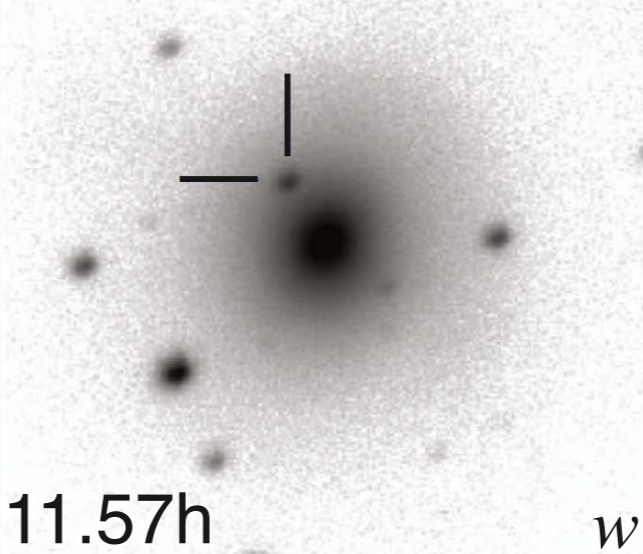
MASTER



DECam



Las Cumbres



J VLA

