

# Searches for signals from unknown or poorly known sources

**Alicia M Sintes**

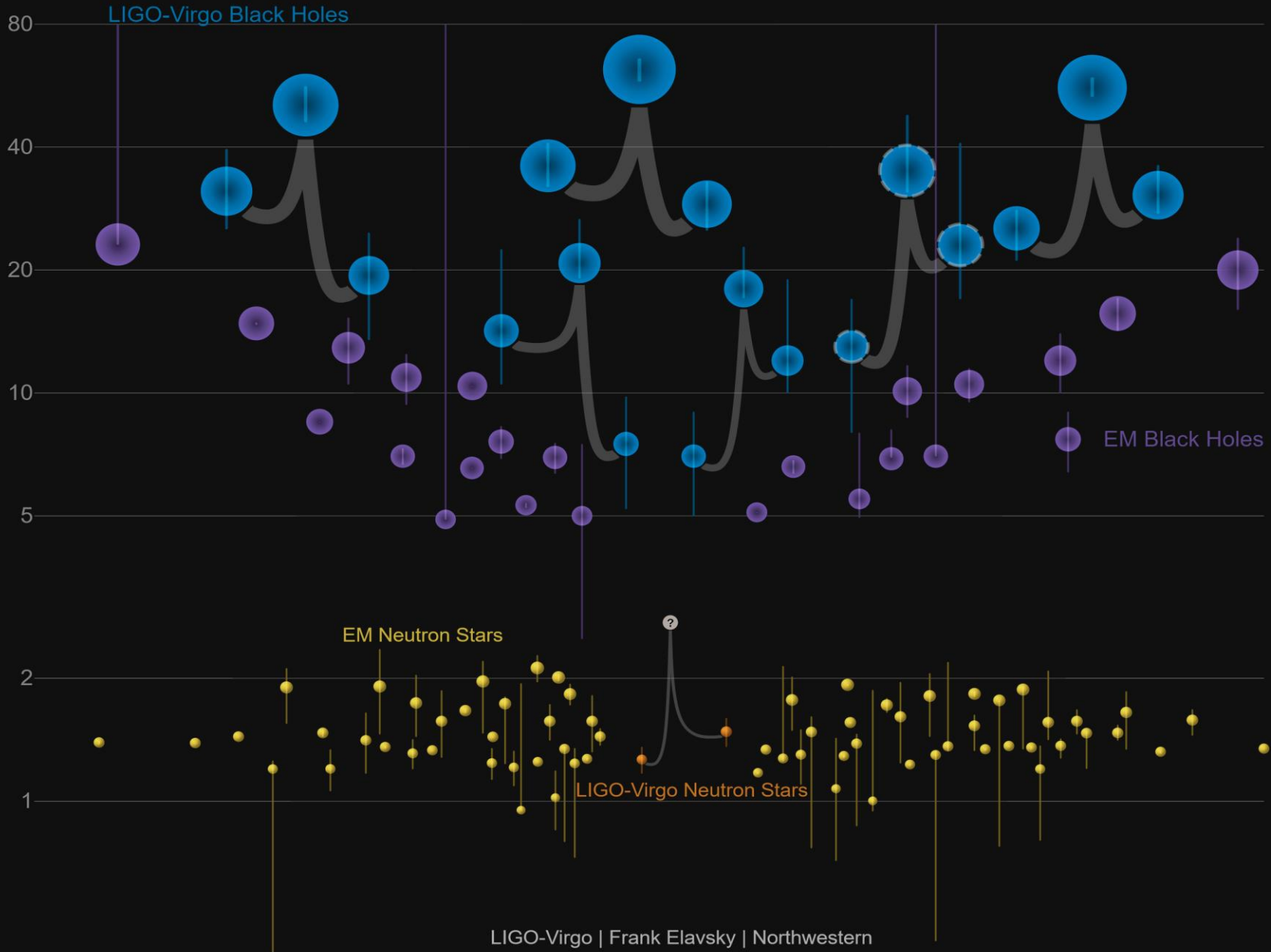
Dept. Física & IAC3 - Universitat de les Illes Balears &  
Institut d'Estudis Espacials de Catalunya (IEEC).

**For the LIGO Scientific Collaboration and Virgo Collaboration**



# Masses in the Stellar Graveyard

*in Solar Masses*



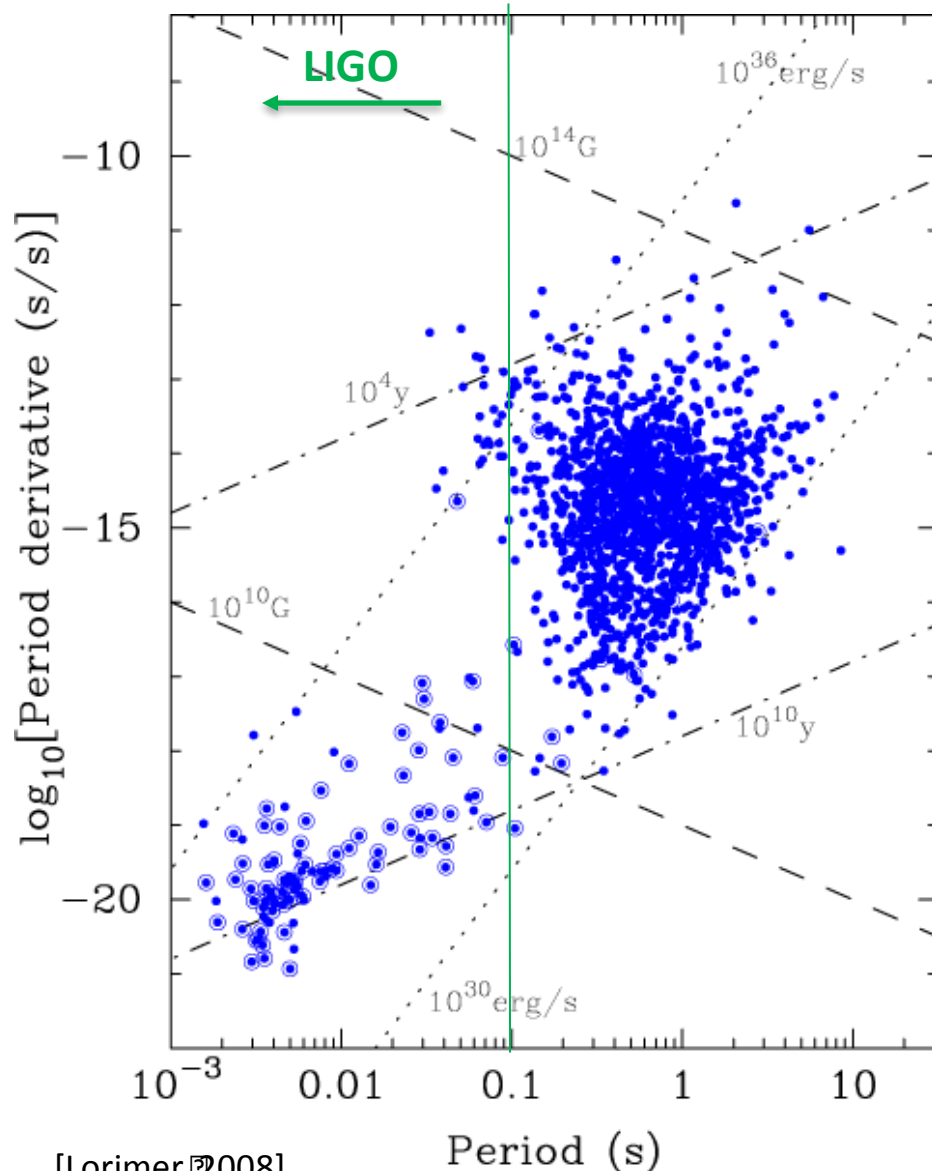
## No continuous gravitational waves (CW) detected... yet!

- Source emitting nearly monochromatic sinusoidal waves
- Signal is weak, but persistent over years of data taking
- Most searches begin *after* an observing run has ended, and all the data is in
- Still analysing LIGO O1 & O2 data
- Strict emission limits have already been set from initial detector era data on signals from known and unknown **neutron star** sources.

## Content

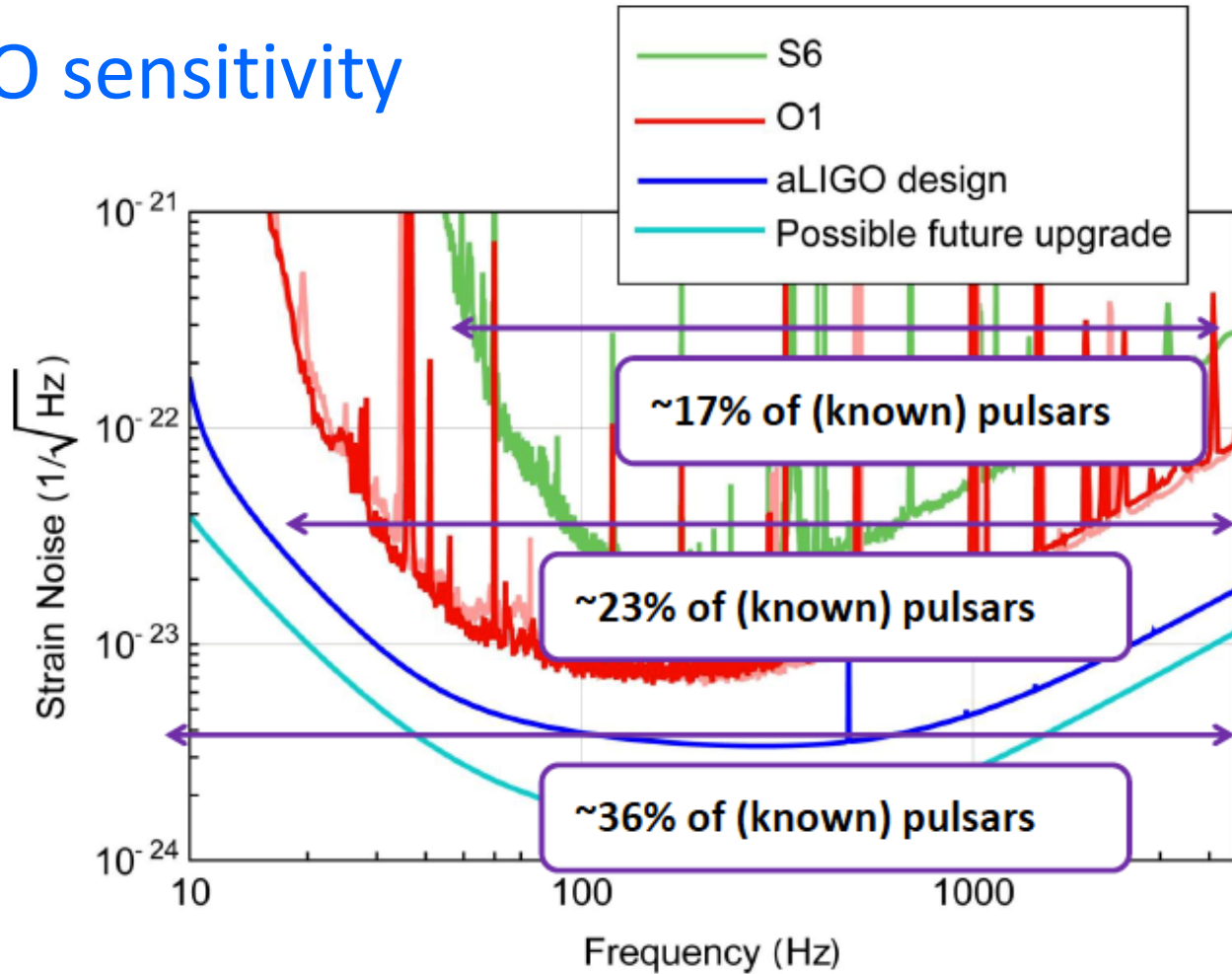
- ❖ **Blind all-sky Searches**
- ❖ **Search for signal of post-merger remnant from GW170817**

## Searching CW signals



- There are a few thousand known pulsars
- 40,000 millisecond pulsars in our galaxy [Lorimer, Living Rev. Relativity, 11 2008]
- $O(10^6 - 10^7)$  undiscovered EM quiet NS within 5kpc [Narayan. *ApJ*, 1987]
- Potential to discover off-axis pulsars or gravitars

# aLIGO sensitivity

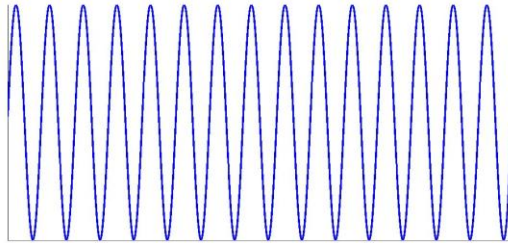


B.P. Abbott et al., *PRL* 116:131103 (2016)

We have no idea how many signal detections to expect in first years of aLIGO/Adv.  
*Advocate for better modeling of neutron star deformation to enhance science case?*

# The Signal from a NS

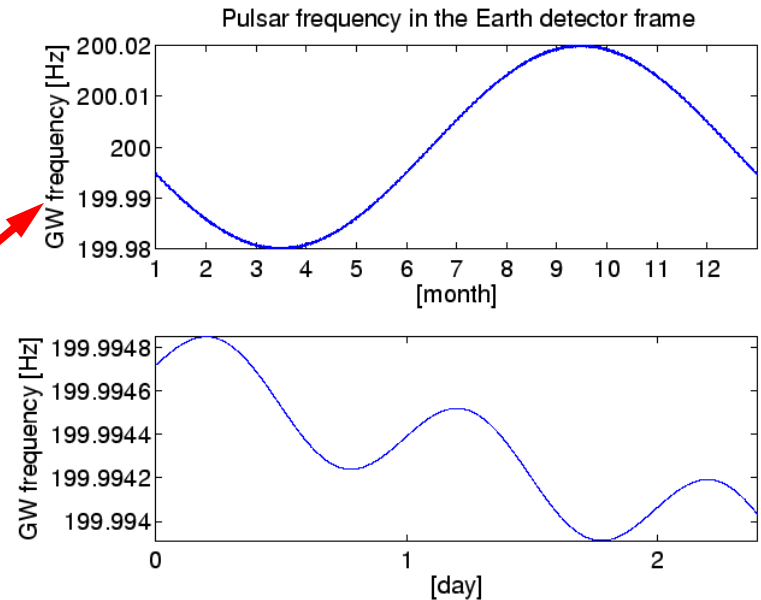
## At the source



Spin-down  $\Rightarrow$  phase evolution

- Annual variation: up to  $\sim 10^{-4}$
- Daily variation: up to  $\sim 10^{-6}$

## At the detector



Frequency modulation + amplitude modulation

... more complications for GW signals from pulsars in binary systems

Additional Doppler shift due to orbital motion of neutron star

Varying gravitational red-shift if orbit is elliptical

Shapiro time delay if GW passes near companion

## Continuous Waves Searches (1)

These searches have several parameters:

*May be known, used in the  
search:*

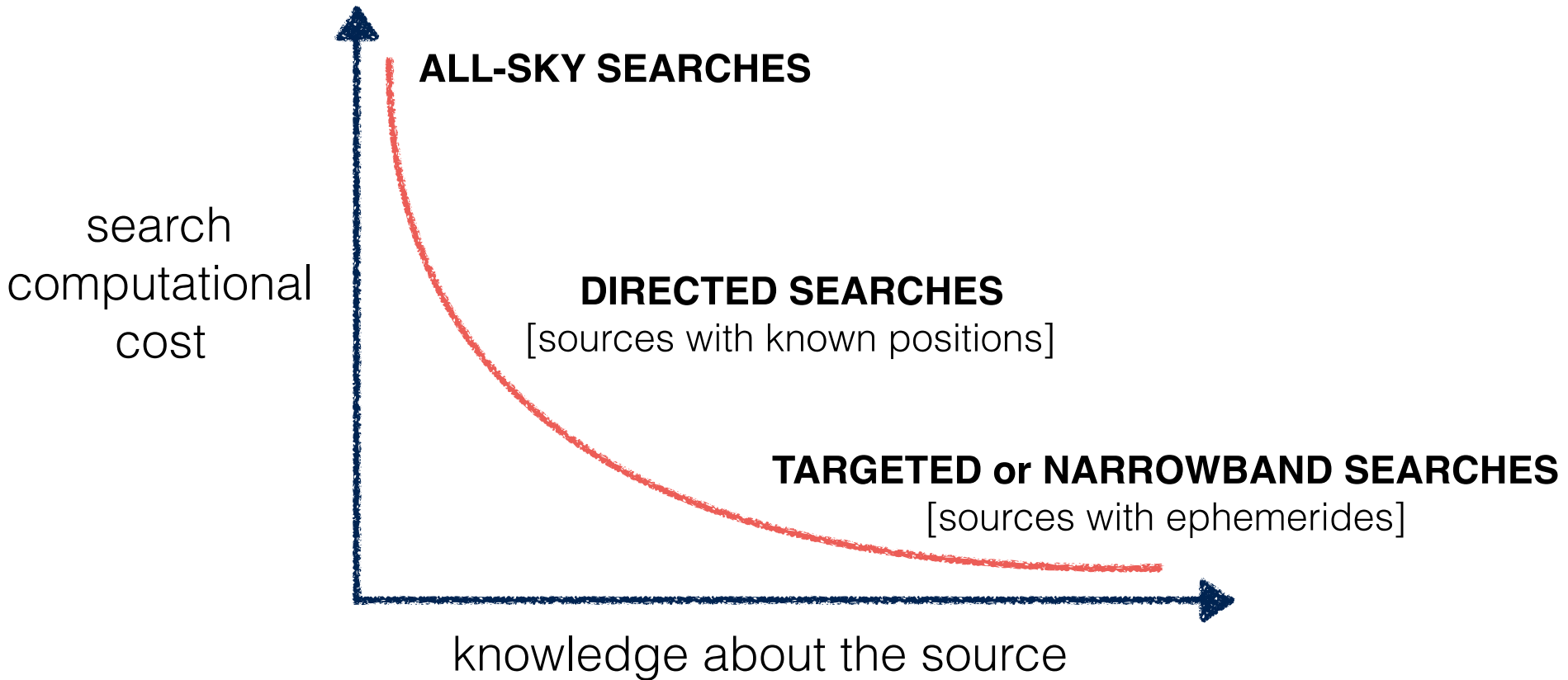
position  
frequency,  
frequency derivatives  
orbital parameters

*Not explicitly searched for:*

initial phase  
inclination angle  
polarization  
amplitude

Different algorithms have been developed, depending on what we know about the source: source parameters knowledge, waveform knowledge, isolated or binary system sources etc.

## Types of CW searches



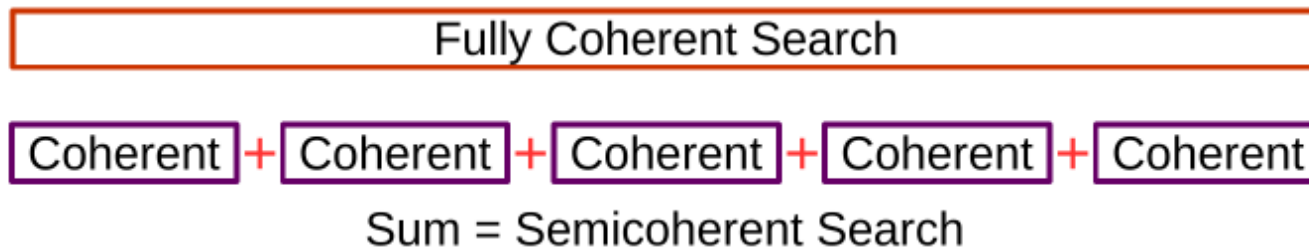


## Continuous Waves Searches (2)

- Detection of signals from a single target :
  - Compute correlation with known waveform. Analyze significance.  
This procedure is not computationally limited
- Blind search of large datasets:
  - *Sweep large area of parameter space*
  - Use *carefully chosen algorithm* for signal detection
    - Number of distinct sky location scales like  $f^2 T_{\text{coh}}^2$
    - For isolated NS computing cost scales as  $T_{\text{coh}}^{6+}$  without 2nd frequency derivative!
    - Limits Coherent *F-Statistic* ( $T_{\text{coh}} \sim 1\text{-few days}$ )
  - Pure Gaussian noise triggers events at  $6\sigma$  level. Real data produces  $>7\sigma$  artifacts
  - Computation efficiency becomes as important as statistical efficiency.
  - **All-sky survey at full sensitivity not possible**
- The cornerstones of CW searches are:
  - sensitivity
  - robustness with respect to signal uncertainties and instrumental noise
  - computational load

## Semi-Coherent Methods

split data of length  $T$  into  $N_{\text{seg}}$  segments of length  $T_{\text{seg}}$   
+ combine coherent results by summing:



less sensitive for same amount of data, but much faster!

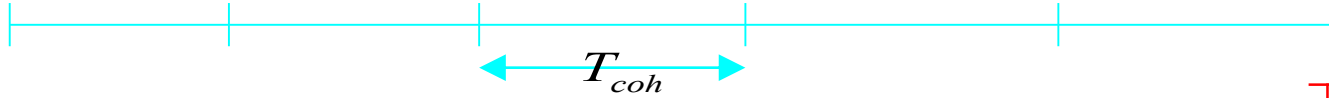
☞ allows analysing all the data

☞ more sensitive at fixed computing cost if  $\Delta(\text{sky}, f, \dot{f}, \dots) > 0$

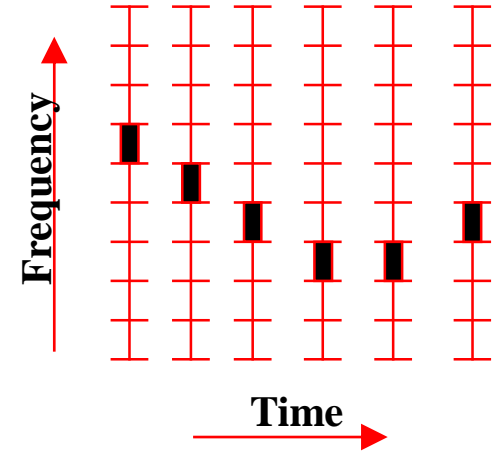
[+] maximize sensitivity (template banks,  $N_{\text{seg}}$ ,  $T_{\text{seg}}$ ) at fixed cost

[+] maximize computing power: clusters, GPUs, Einstein@Home

# Semi-coherent power-sum methods



- The idea is to perform a search over the total observation time using a *semi-coherent* (sub-optimal) method.
- Several methods have been developed to search for cumulative excess power from a hypothetical periodic gravitational wave signal:



## Stacked power spectra

- Based on FT each segment ( $T_{coh} \sim 0.5-2.0$  hours) from  $h(t)$ ,
- Examining successive spectral estimates, tracking the frequency drifts due to Doppler modulations and  $df/dt$  as the incoherent step.

- **Raw spectral powers:**

Stack-slide (Radon transform),  
Power-flux, Loose coherence

- **Thresholded powers (Robust pattern detection technique)**

Frequency Hough transform,  
Sky Hough transform

$$SNR \propto \frac{h_o}{\sqrt{S_n}} T_{coh}^{\frac{1}{2}} N_{seg}^{\frac{1}{4w}},$$

$w(N_{seg}, pFA)$  range  $[1, \uparrow 3.5]$

[Prix & Shaltev, PRD85, 2012]

## Multi-segment Demodulated spectra – F-Statistic

( $T_{coh} \sim 1$ -few days)

- Coincident *F*-Statistic
- Stacked *F*-Statistic (Einstein@Home)

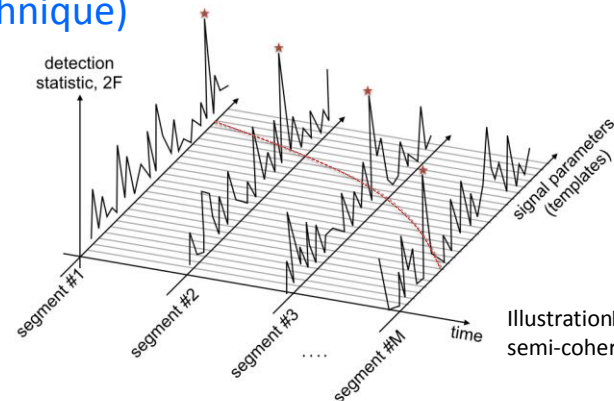
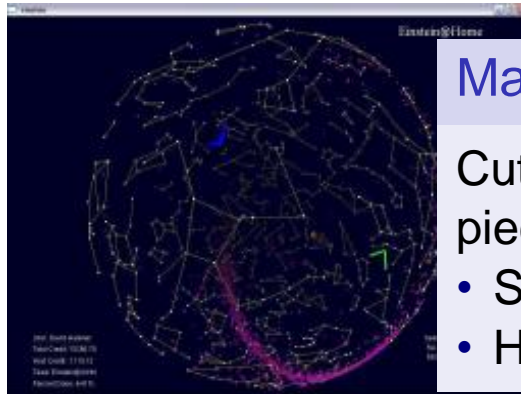


Illustration of stack-slide semi-coherent method



## Maximize available computing power

Cut parameter-space  $\Delta$  ( $\text{sky}, f, \dot{f}, \dots$ ) into small pieces

- Send these “workunits” to participating hosts
- Hosts return finished work and request next

- Public distributed computing project, launched Feb. 2005
  - $\leftarrow$  100,000 participants,  $\leftarrow$  5 PFlop/s (24x7)
  - All-sky and directed CW searches
  - Workunits run  $\leftarrow$  6 – 12 h on hosts
  - Typical search runs  $\leftarrow$  3 – 12 months on E@H
- + You can sign up and help! <https://einsteinathome.org>

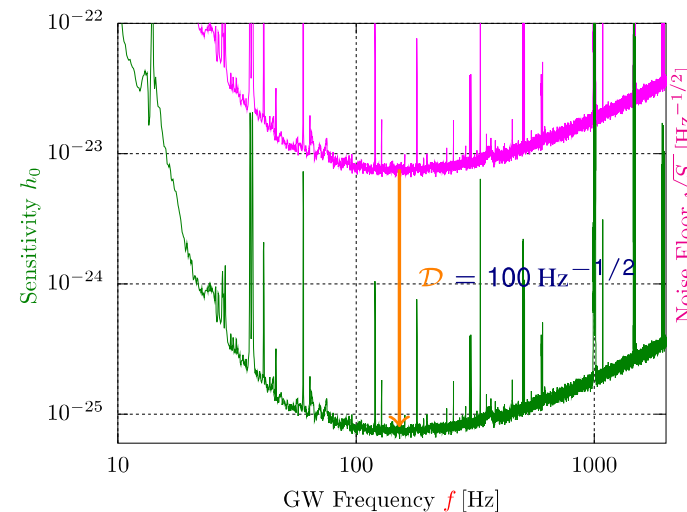
# Sensitivity Depth $\mathcal{D}$ of a CW search

Sensitivity / Upper Limit  $\equiv$  Smallest detectable  $h_0$  | confidence=90%  
p-value=1%

Depends on

- data quality: PSD  $S_n(f)$
- search method  $\Rightarrow$  constant sensitivity depth  $\mathcal{D}$

$$h_0(f) = \frac{\sqrt{S_n(f)}}{\mathcal{D}}$$



Examples:

- Fully-coherent search, 2 years of data from 2 detectors:  
 $\Rightarrow \mathcal{D} \sim 1000 \text{ Hz}^{-1/2}$
- Semi-coherent **all-sky** search over  $f, \dot{f}$ :  
 $\Rightarrow \mathcal{D} \sim 20 - 50 \text{ Hz}^{-1/2}$

## O1 all-sky searches

### Fast turnaround, broad, robust

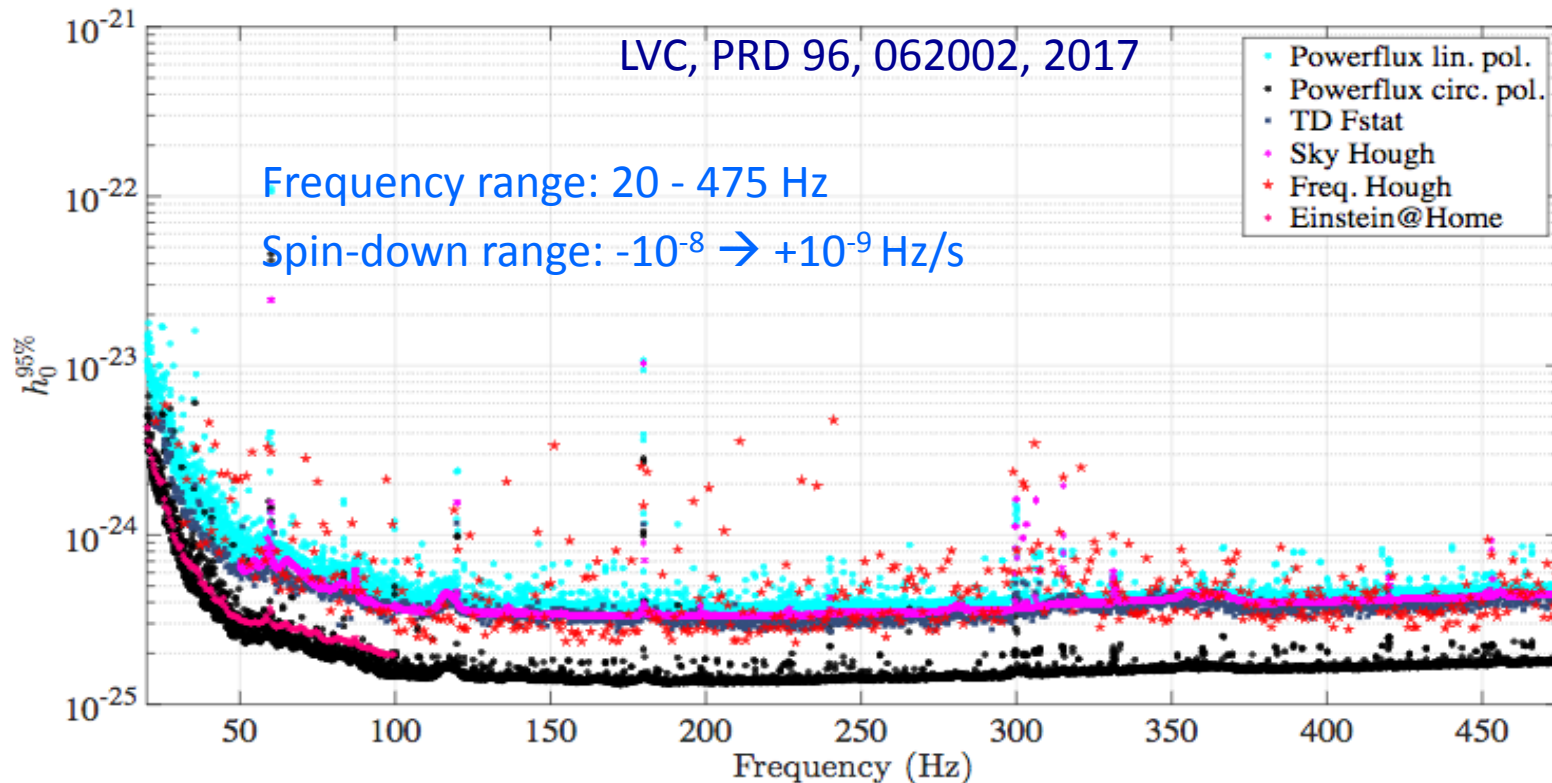
- Two searches: 20 – 475 Hz , 475 – 2000 Hz  
[-10,+1] x 10<sup>-9</sup> Hz/s
- Four pipelines: PowerFlux, time- domain F-statistic, Sky Hough and Frequency Hough

### Computational intensive, more sensitive

- 20 – 100 Hz  
[-2.6, 0.3] x 10<sup>-9</sup> Hz/s
- Einstein@Home

Spindown range implies limit on ages searched

# O1 all-sky fast turnaround searches



Four pipelines: PowerFlux, time-domain F-statistic, Sky Hough and Frequency Hough

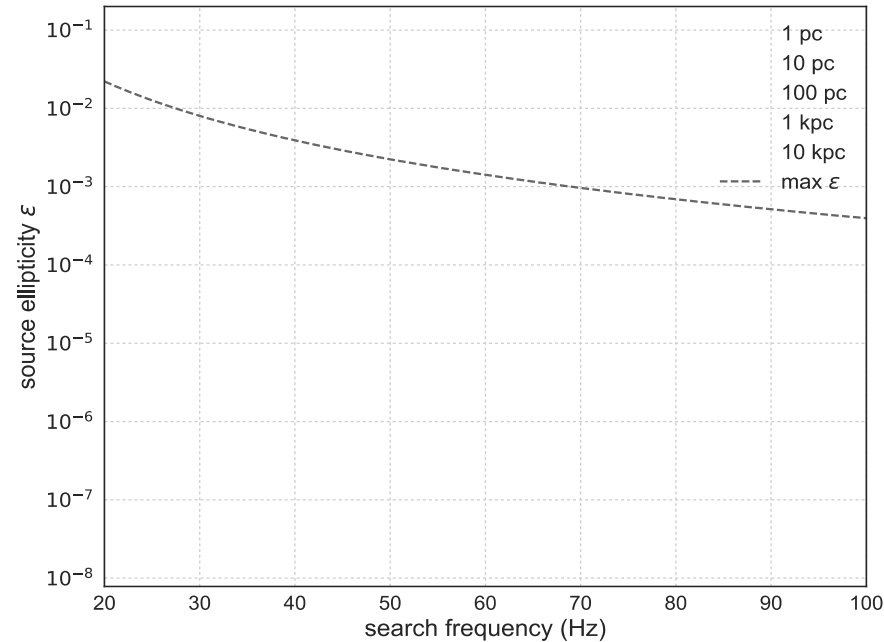
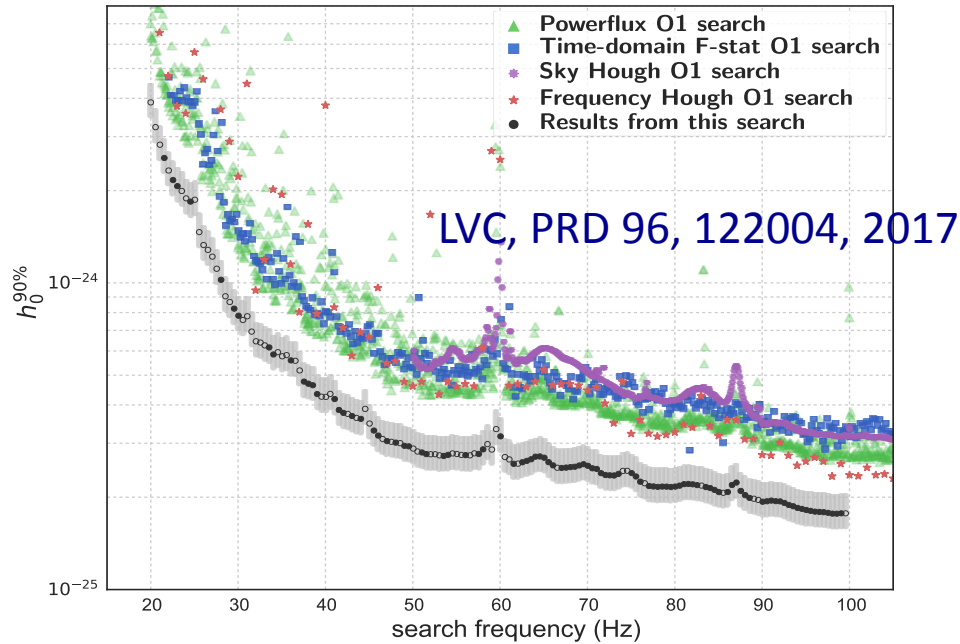
No candidate survived the follow-up.

Significant improvement in the ULs with respect to past analyses ( $> 3x$ )

Best limits on  $h_0$  of  $1.5 \times 10^{-25}$  (optimal source spin orientation) near 170 Hz

At 475 Hz sensitive to NS with ellipticity  $\epsilon > 8 \times 10^{-7}$  as far as 1kpc, for optimal spin orientation

# O1 all-sky Einstein@Home search



Search ranges:  $f : [20, 100]$  Hz, spin-down:  $[-2.6, 0.3] \times 10^{-9}$  Hz/s

$N_{\text{seg}}=12$ ,  $T_{\text{coh}}=210\text{h}=8.8\text{d}$   $3 \times 10^{17}$  templates

Best limits on  $h_0$  of  $1.8 \times 10^{-25}$  (marginalised) near 100 Hz

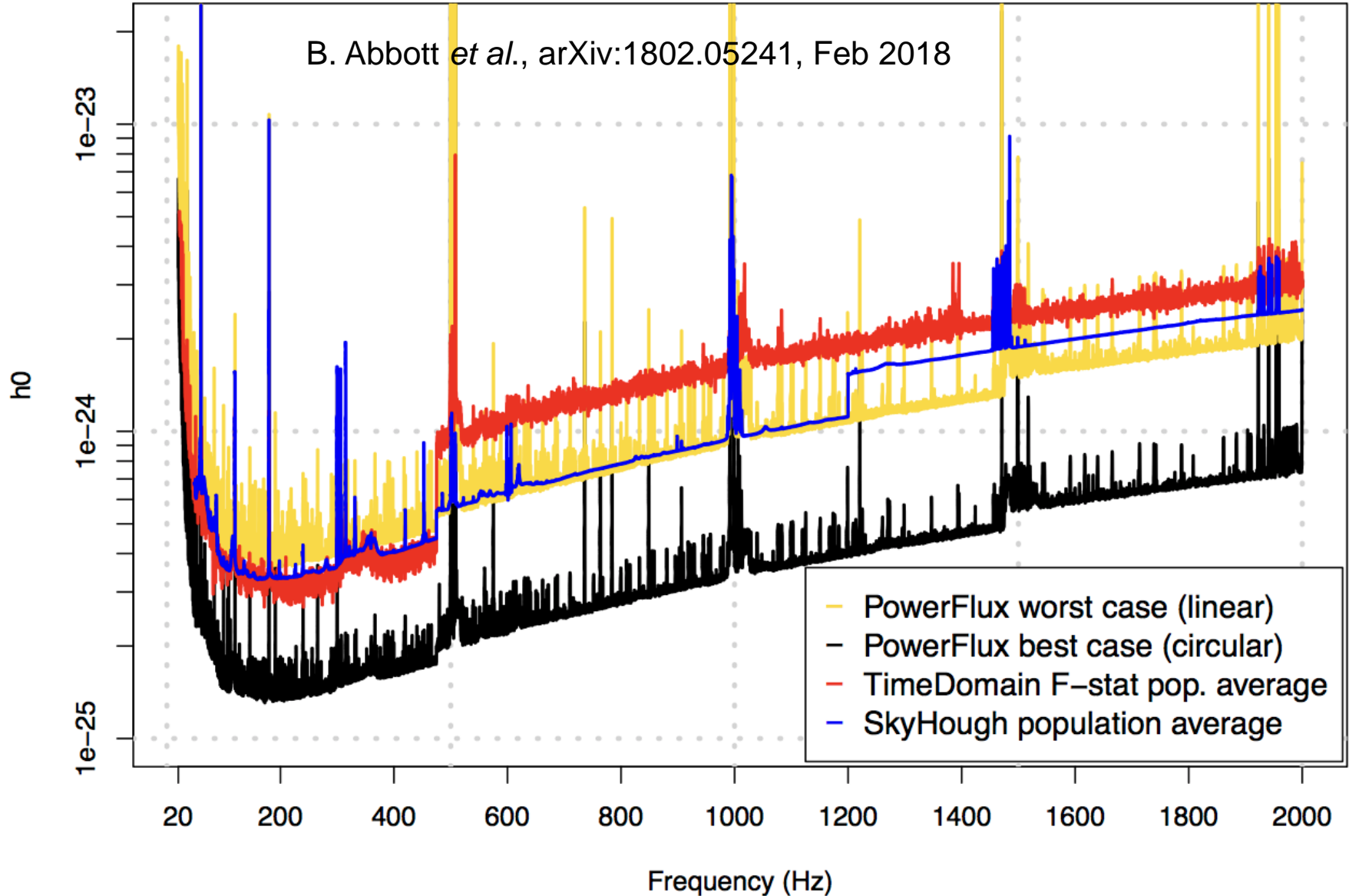
Sensitivity Depth  $D \sim 49 \text{ Hz}^{-1}$

At 55Hz, exclude sources with ellipticity above  $10^{-5}$  within 100pc

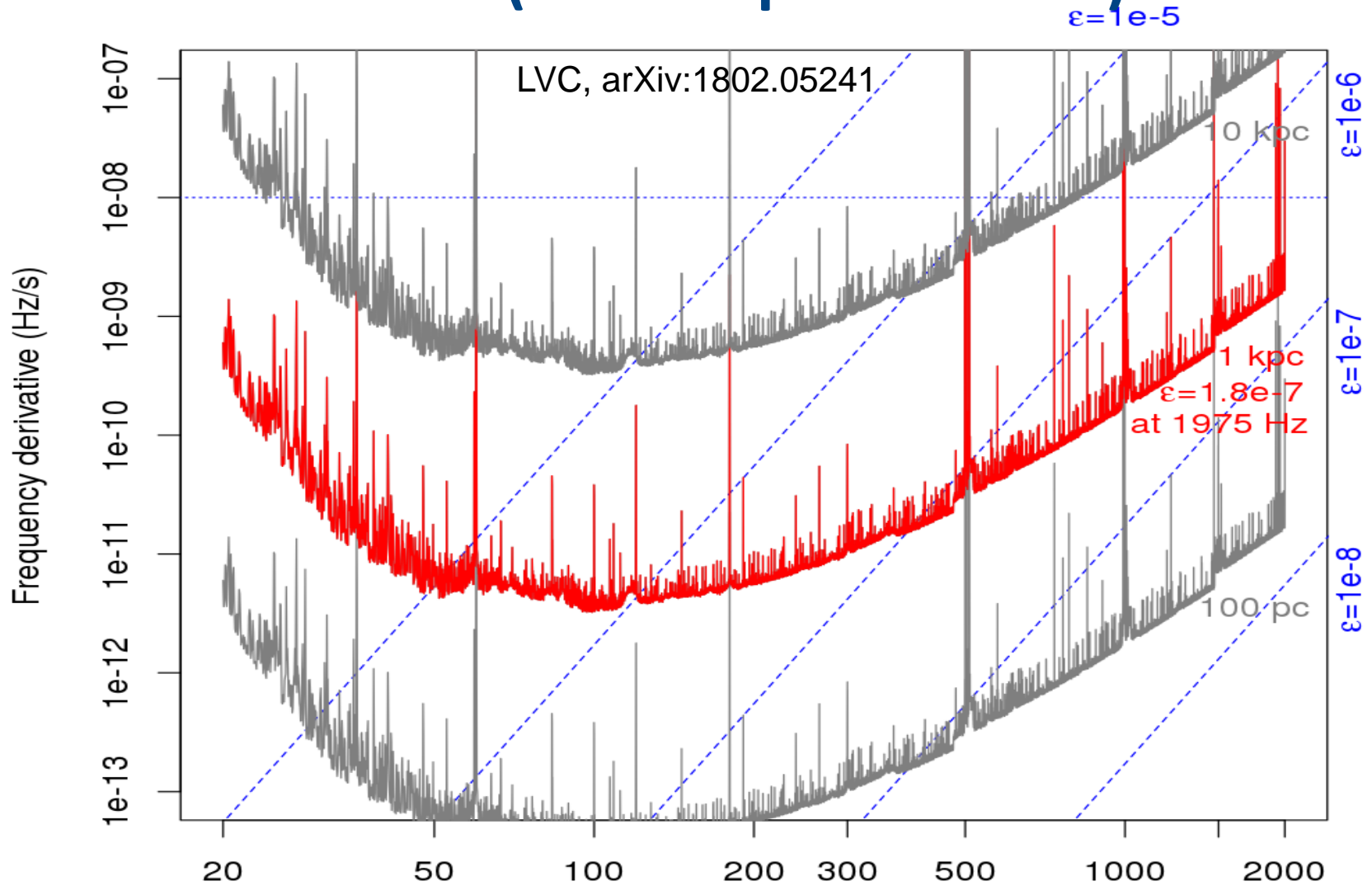


# O1 full band all-sky search

B. Abbott *et al.*, arXiv:1802.05241, Feb 2018



# Search reach (circular polarization)



Sensitive to NS with ellipticity  $> 1.8 \times 10^{-7}$   
as far as 1kpc, for optimal spin orientation

Frequency (Hz)

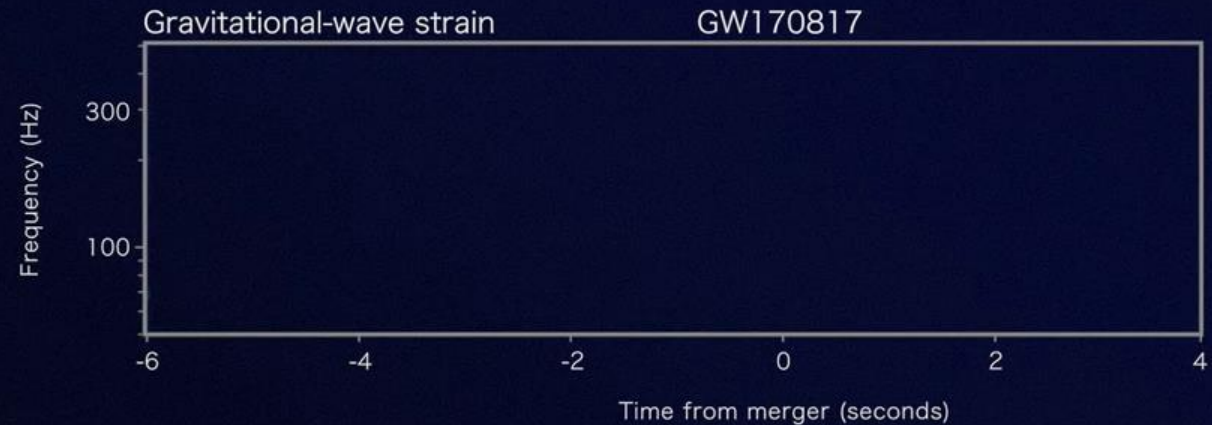
# GRB 170817A - GW170817:

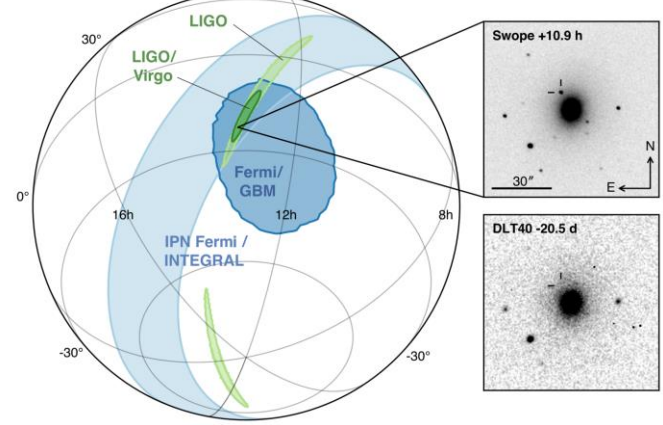
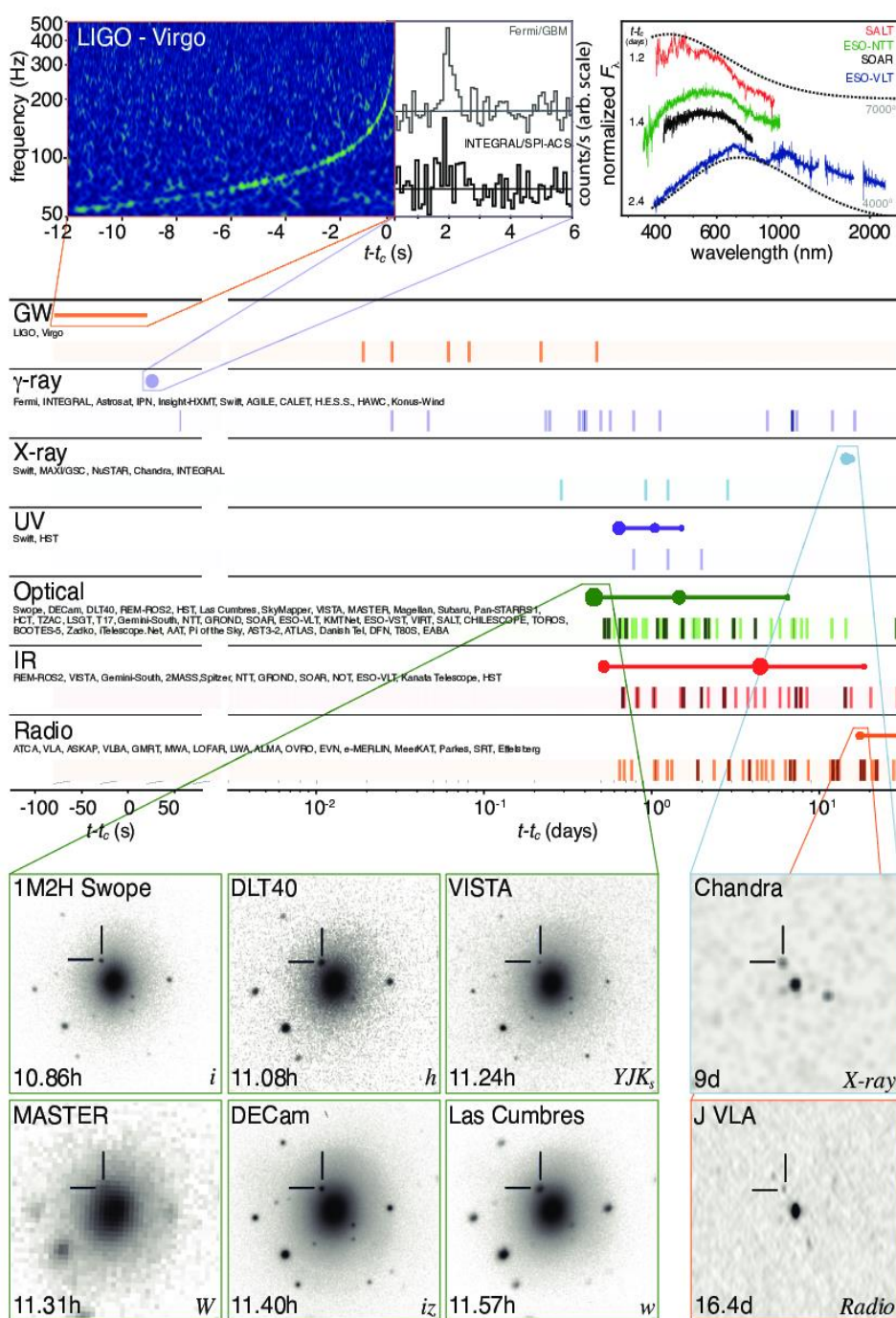
Coincident Detection with Gravitational Waves and Gamma Rays.

LIGO and Virgo and partners make first detection of gravitational waves and light produced by colliding neutron stars



LIGO





## Post-merger remnant from GW170817

Challenges for longer-duration search:

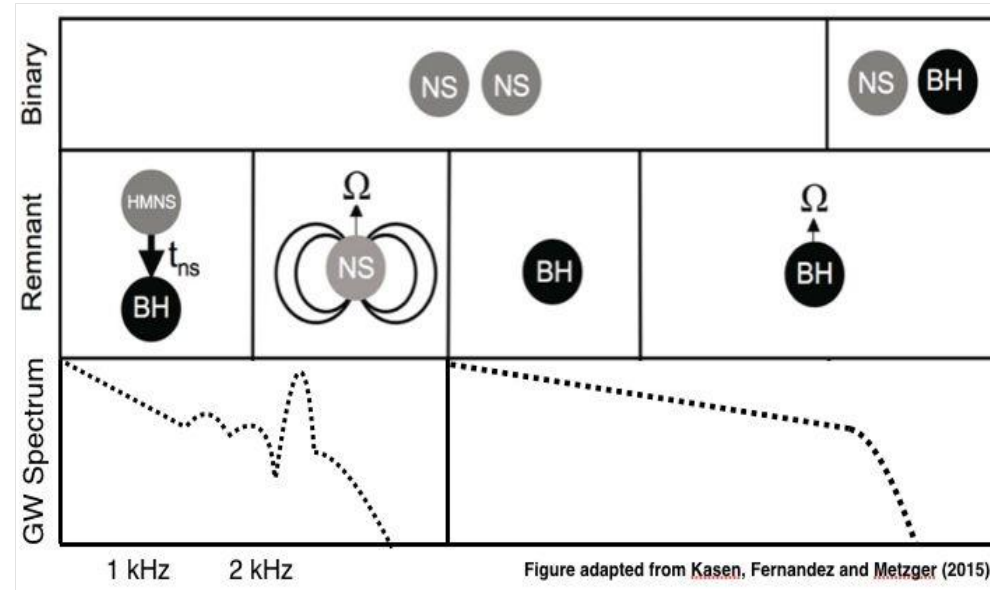
- Unknown GW emission frequency and (rapid) signal evolution
- Distance is far for traditional CW searches

$$d = 40_{-14}^{+8} \text{ Mpc}$$

Detection unlikely, but worth developing the searches, verify expectations & determine future prospects.

# Post-merger Scenarios

Theoretically, the end-product of a BNS merger can be (depending on the remnant mass and EOS):



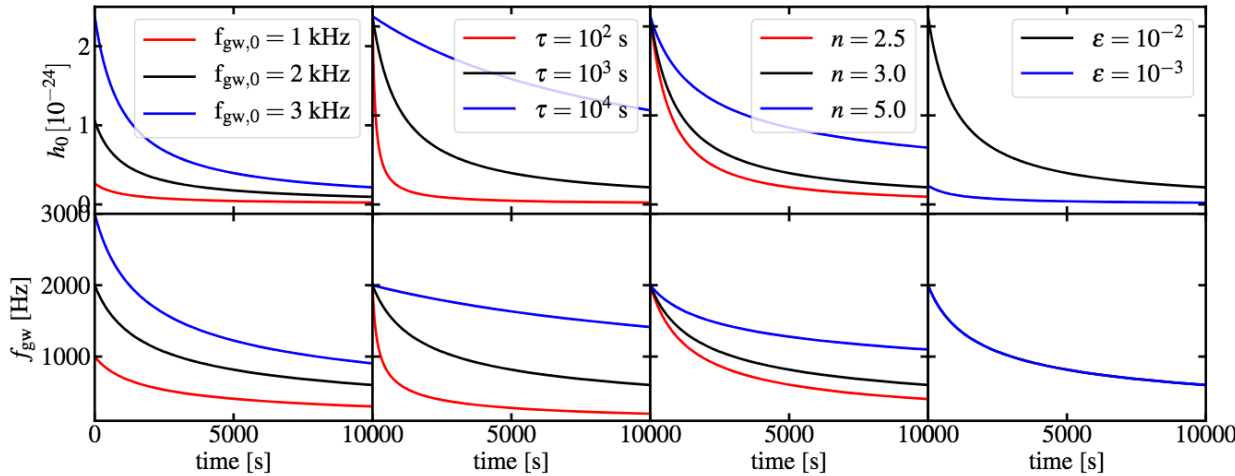
- Prompt collapse to a BH (BH ringing  $>6$  kHz)
- Unstable hypermassive NS, supported by differential rotation and thermal pressure  
→ Collapse after 10-100 ms
- Supramassive, metastable NS, supported by centrifugal force  
→ Collapse after  $O(10-10000$  s)
- **Stable remnant NS** ( $t_{\text{GW}} \sim 100$  ms, minutes-weeks+)

## GW emission from the remnant

The newborn NS may emit a “transient” GW signals due to:

- the formation of a millisecond magnetar  
(e.g. Giacomazzo+, 2013, 2014; Dall’Osso+, 2012; Lü+, 2015; Rowlinson+, 2013; Gompertz+, 2013, 2014)
- the development of dynamical or secular instabilities, like r-modes or bar-modes  
(e.g. Andersson, 1998; Lindblom, 1998; Corsi+, 2009; Passamonti+, 2013; Doneva+, 2015)
- ?

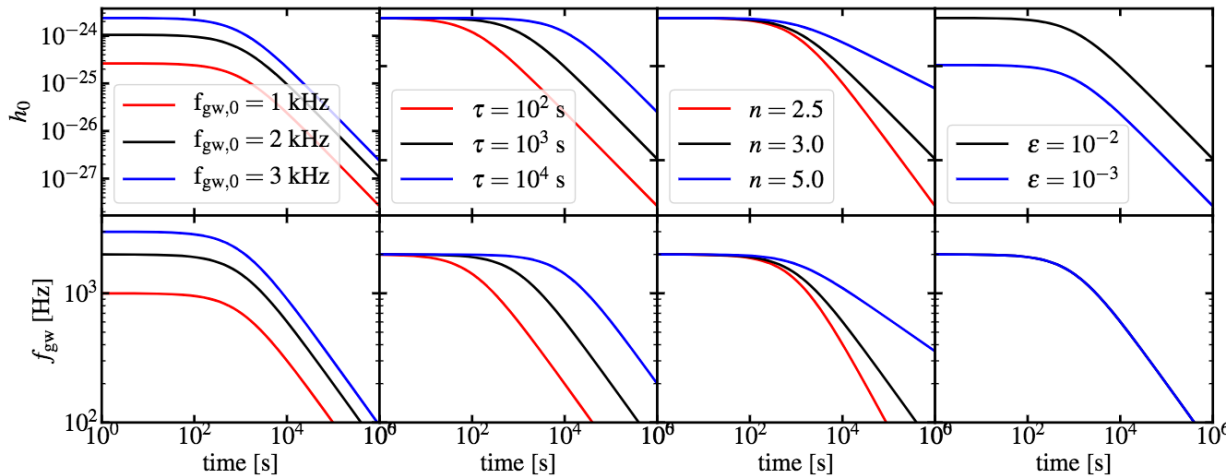
# Magnetar-like emission waveform examples



Periodic signal with power law frequency evolution

$$\dot{\Omega} = -k\Omega^n$$

depending on the braking mechanisms



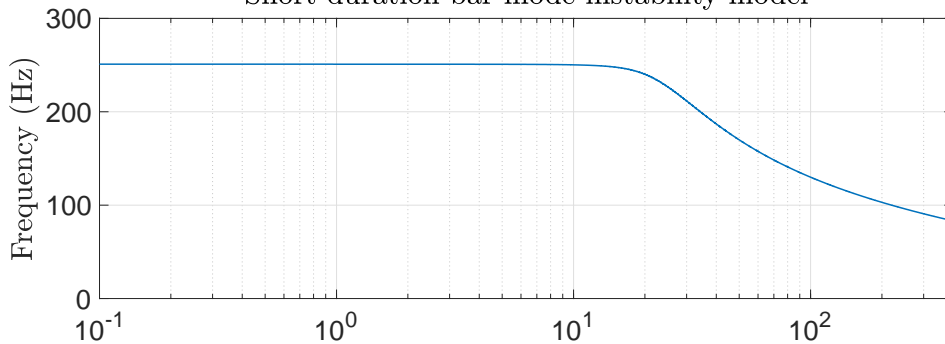
GW contribution to the spin-down cannot be excluded

Due to fast spin-down the GW signal frequency may become too small after hours-days

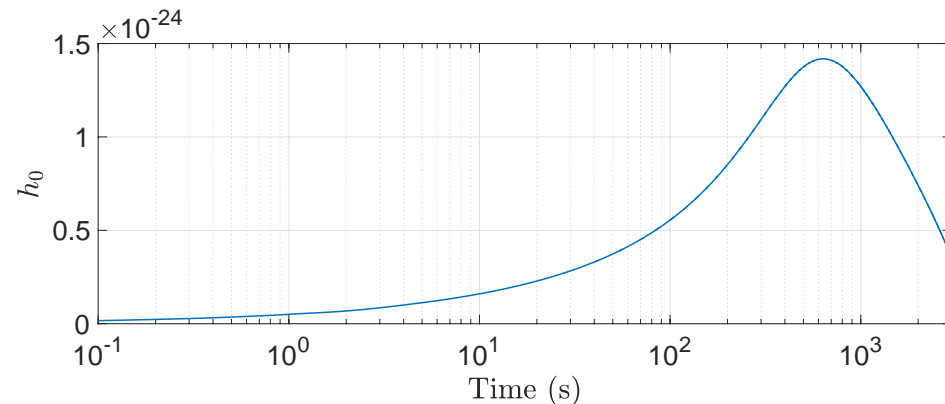
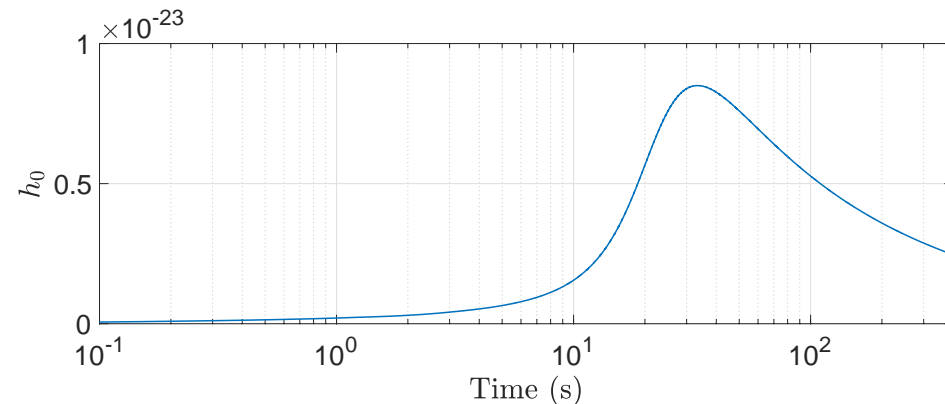
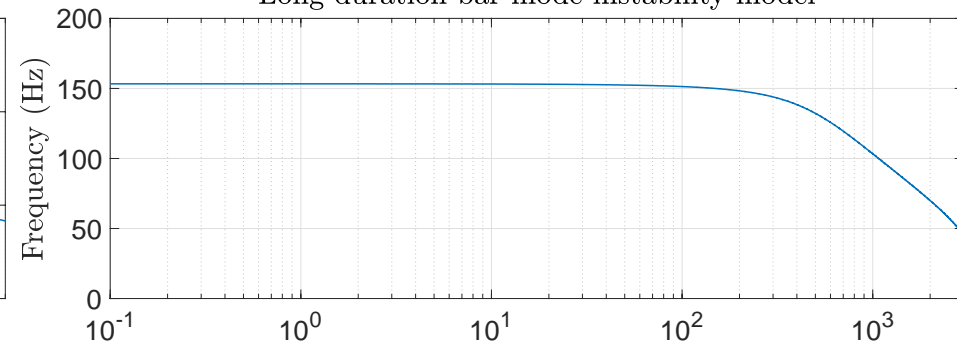
# Bar-mode instability model waveform examples

Dynamical and secular, with different time scales, depending on the ratio between kinetic and gravitational binding energy

Short duration bar-mode instability model



Long duration bar-mode instability model

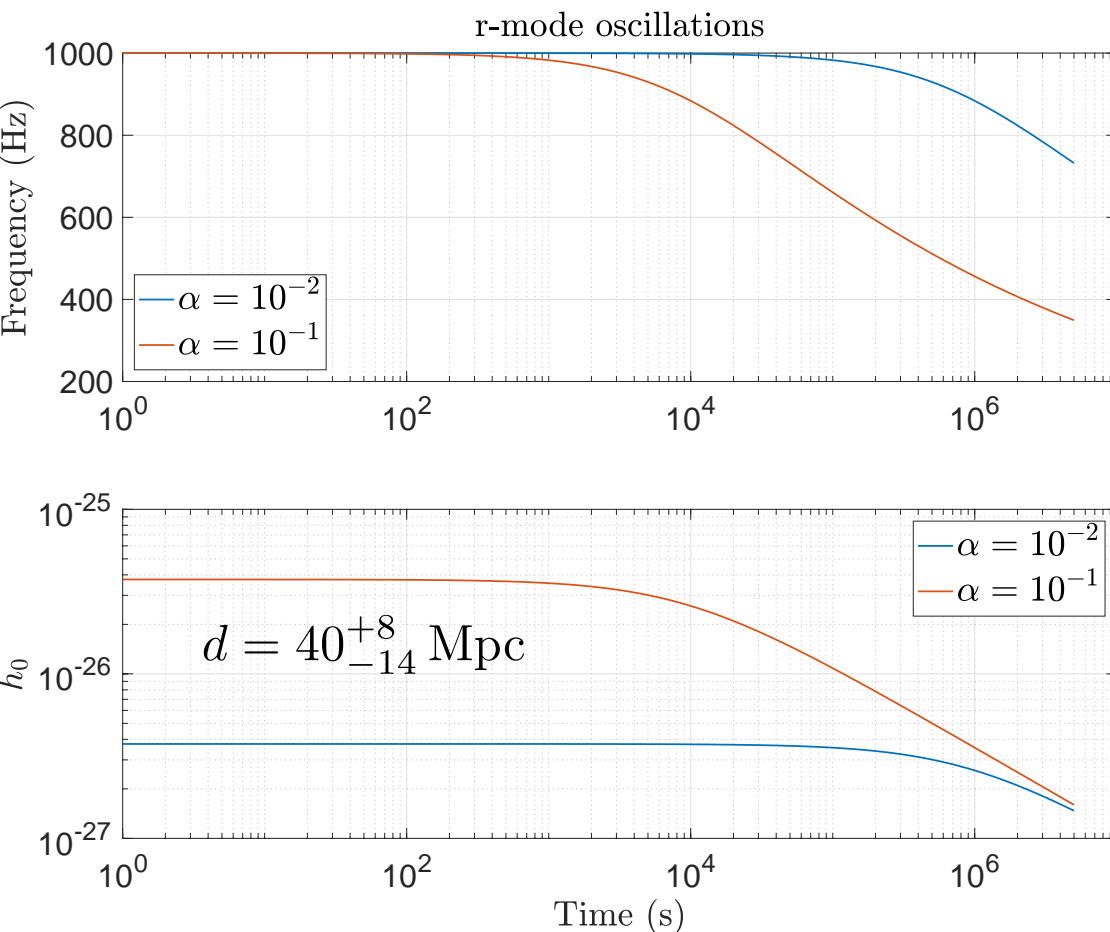


“Typical” GRB magnetar: 1.4 Msun, 20 km radius,  $1e14$  G,  $n = 1$



# R-mode instability

(e.g. Haskell, 2016 for a review)

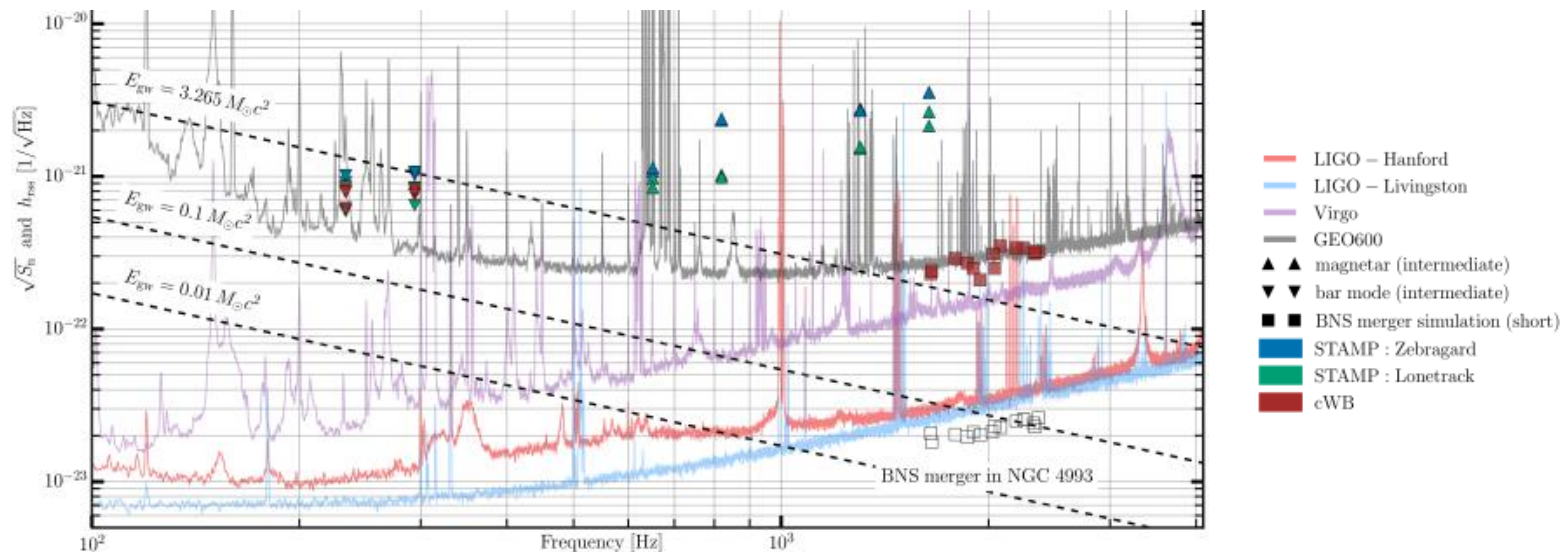


- GW frequency  $\sim 4/3 f_{\text{rot}}$
- Frequency evolution described by a power law with braking index  $n=7$ ;
- r-mode saturation amplitude depends on NS EOS
- GW signal time scale O(hours-days)

## Short-duration remnant searches

LVC, ApJL 851 (2017) sets upper limit for short (<1 s) and intermediate (<500 s) duration post-merger signals for GW170817

- Two pipelines (cWB, STAMP), based on excess power in time-frequency:
  - cWB burst analysis (. 1s 1–4 kHz HL and . 1000s 24–2048 Hz HLV)
  - STAMP directional stochastic analysis (500 s maps, 24–4000 Hz HL)



- CW pipelines not involved
- At least a factor of 10 above model predictions

## Long-duration remnant searches

- Predictions rule of thumb: “Signals detectable up to  $\sim 20\text{-}25$  Mpc in Advanced LIGO-Virgo detectors, **assuming matched filtering**”.
- In general, of course, we cannot use matched filtering as we do not know signal parameters in advance.
- We must rely on semi-coherent or un-modeled methods, which are less sensitive.
- **EM observations crucial to reduce parameter space and to improve detection significance**
- $t \gg 500$  s fall within CW + stochastic groups’ remit
- Available data: from GW170817 coalescence to end of O2: 8.5 days
- Main physical model: power law spindown (‘ms magnetar’)

$$\dot{\Omega} = -k\Omega^n$$

$$f_{\text{gw}}(t) = f_{\text{gw},0} \left( 1 + \frac{t}{\tau} \right)^{\frac{1}{1-n}} \quad \tau = \frac{-\Omega_0^{1-n}}{k(1-n)}$$

# Long-duration remnant searches

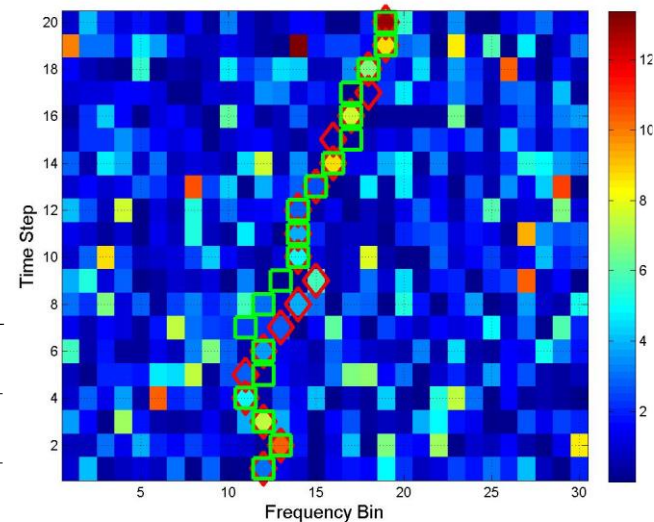
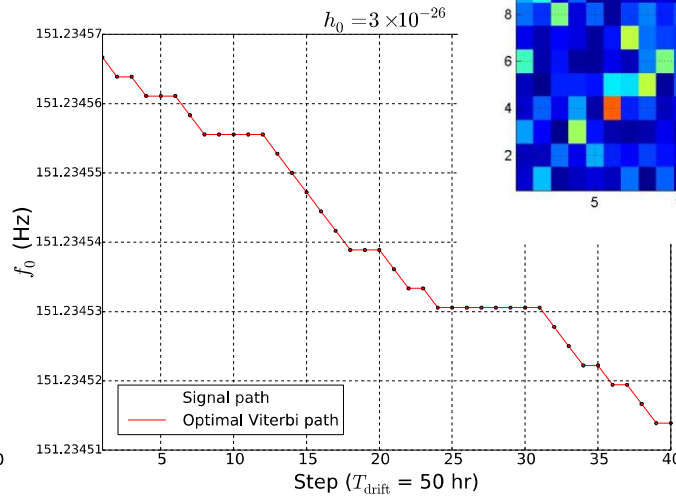
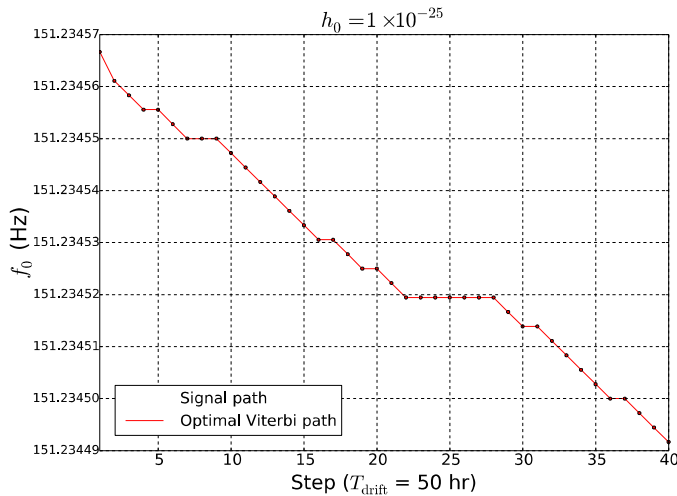
Broadly speaking, two kinds of searches are being considered for the search of very long transient signals from the remnant of GW170817:

- **Unmodelled search ( $10^2$  to  $10^4$ s intermediate duration)**
  - **STAMP-VLT** (stochastic search) based on excess power in spectrograms (Thrane+, 2013)
  - hidden-Markov **Viterbi** tracking , previously used for Sco X-1, young SNRs [Suvorova et al PRD 96 (2016) 102006, Sun et al, PRD 97 (2018) 043013]
    - → More robust against fluctuations and transient instrumental glitches  
Require short tracking step size (1 s)  
Optimal observing time  $\sim$  spin-down time-scale
- **Model-based searches (hours/days duration)**
  - based on variations of methods used for standard continuous wave searches: **SkyHough** and **FrequencyHough**: previously used for all-sky searches [LVC, PRD 96 (2017) 062002]
    - → Allow to estimate signal parameters (in case of detection)
- 4 pipelines: 2 'unmodelled', 2 semi-coherent with grid over parameter space

# Hidden Markov model and Viterbi

## Tracking rapidly spin-down CW signals with timing noise

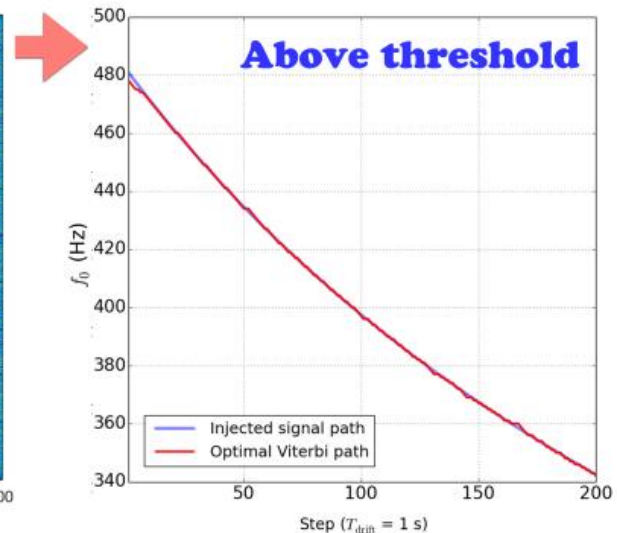
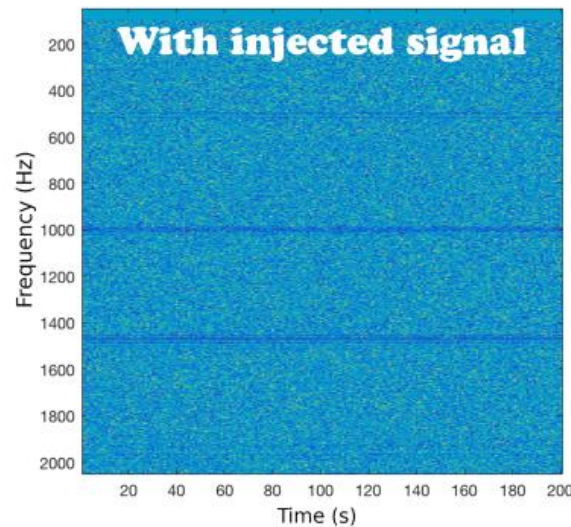
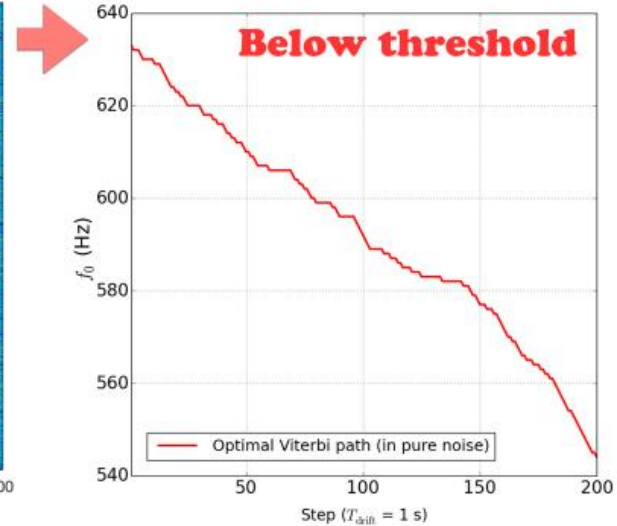
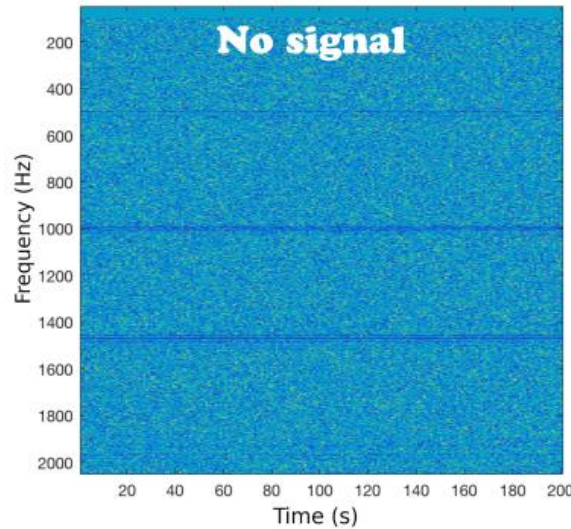
- $\dot{f}_{0inj} \leftarrow 10^{-11} \text{ Hz s}^{-1}$ ,  $\overline{\Delta t}_{\text{spin-down}} \leftarrow \overline{\Delta t}_{\text{timing-noise}}$
- $\cos \diamond \leftarrow 0.7$ ,  $\rho \overline{S}_h = 4 \rightarrow 10^{-24} \text{ Hz}^{-1/2}$
- $h_0 = 1 \rightarrow 10^{-25}$  (left) and  $h_0 = 3 \rightarrow 10^{-26}$  (right)



Sun et al., PRD 97, 043013 (2018)

# Example: Tracking a millisecond magnetar signal

Viterbi



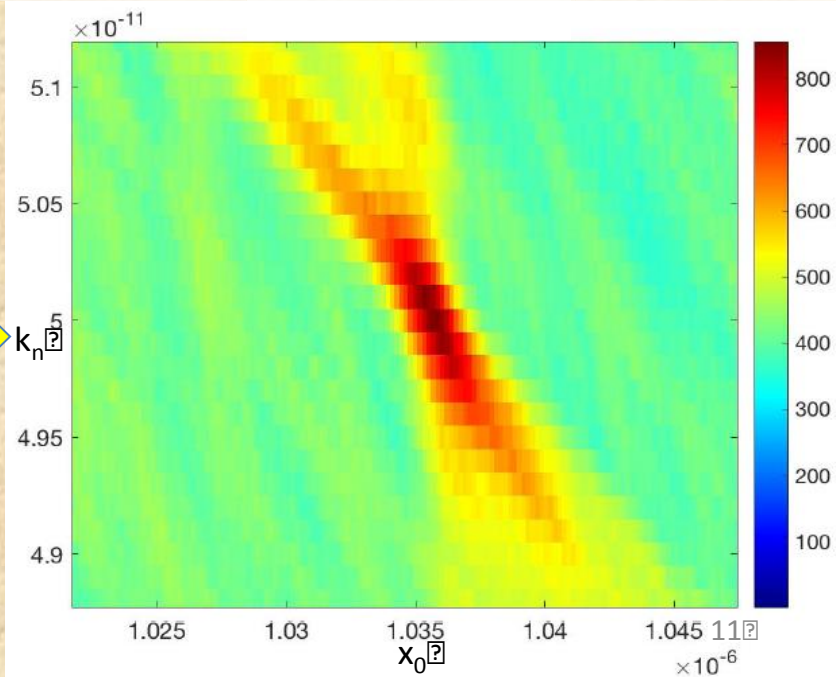
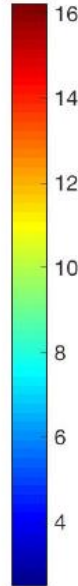
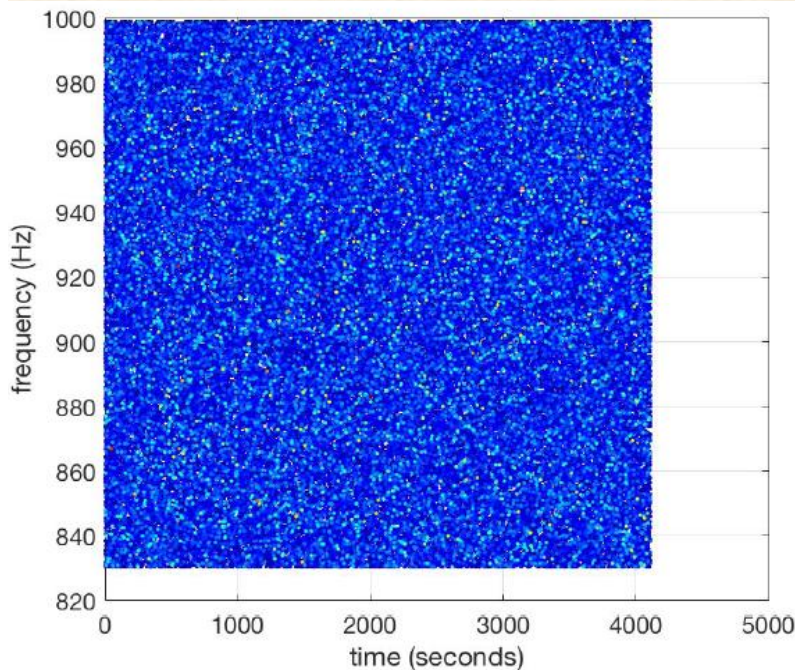
# Generalizing the FrequencyHough

- Assumes a power law for the frequency evolution:
- Peaks in time-frequency plane are mapped into straight lines in the transformed  $x_0/k_n$  plane

$$f(t) = f_0 \left( 1 + (n-1) \frac{f_0}{f_0} (t-t_0) \right)^{-1/(n-1)}$$

$$(x_0 = f_0^n, k_n = f_0/n)$$

- The search is done over a grid built on the parameter space:  $f_0, k_n, n$



Magnetar case ( $n = 3$ )

## Search plan

- Grid over braking index  $n \rightarrow$  we search over all possibilities of emission mechanisms (and combinations)
  - 1 Hough per braking index
  - $f_0$ : [500, 2000] Hz
  - $n$ : [2.5, 7]
  - $\dot{f}$ :  $[-\frac{1}{2^2}, -\frac{1}{16^2}]$  Hz/s
  - Looking for sources lasting at most 1 day
  - Beginning the search about 1 hour after the merger
    - Signal immediately after merger is very complicated
    - Less frequency variation later because spindown is smaller
    - Improve sensitivity because we use longer FFTs
  - Search with varying  $T_{FFT}$  (2,4,8 s) in different portions of the parameter space to maximize sensitivity
  - Computation cost:  $O(\text{days})$
- Detection of long-transient signals from GW170817 is unlikely, but it is important to setup analysis methods.
  - Detection of GWs from the post-merger would provide a wealth of information on the remnant.



## Conclusions

- LIGO and Virgo Collaborations have set forth a robust program to detect continuous gravitational waves
- Detecting one source would provide rich laboratory – including post-merger remnant searches!
- Critically important: improved detectors, sensitive, robust and faster algorithms, and continued collaboration with EM partners
- No guaranteed future CW detections, but . . .  
. . . we are entering very interesting territory!