

A visualization of gravitational waves, showing two bright, glowing spheres (representing black holes or neutron stars) in the process of merging. The spheres are surrounded by concentric, glowing rings of light that ripple outwards, illustrating the propagation of gravitational waves through spacetime. The background is a dark, starry field.

# Gravitational wave probes of dense matter

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# Exciting times ...

PRL **116**, 061102 (2016) week ending  
12 FEBRUARY 2016

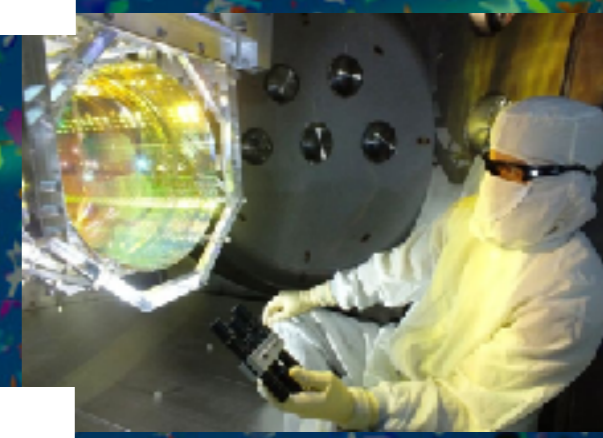
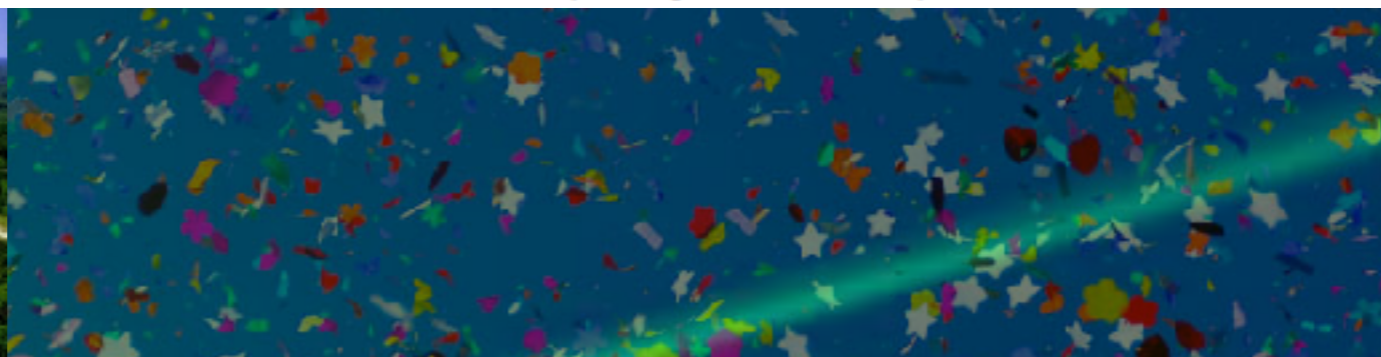
Selected for a Viewpoint in *Physics*  
PHYSICAL REVIEW LETTERS

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**Observation of Gravitational Waves from a Binary Black Hole Merger**


B. P. Abbott *et al.*<sup>\*</sup>  
(LIGO Scientific Collaboration and Virgo Collaboration)  
(Received 21 January 2016; published 11 February 2016)



PRL **119**, 161101 (2017) week ending  
20 OCTOBER 2017

Selected for a Viewpoint in *Physics*  
PHYSICAL REVIEW LETTERS

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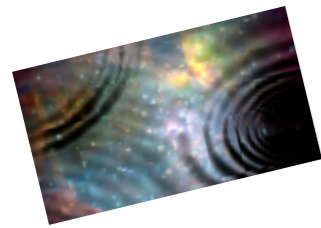


**GW170817: Observation of Gravitational Waves from a Binary Neutron Star Inspiral**

B. P. Abbott *et al.*<sup>\*</sup>  
(LIGO Scientific Collaboration and Virgo Collaboration)  
(Received 26 September 2017; revised manuscript received 2 October 2017; published 16 October 2017)

... the era of GW astronomy has started!

# Present & future windows to the cosmos



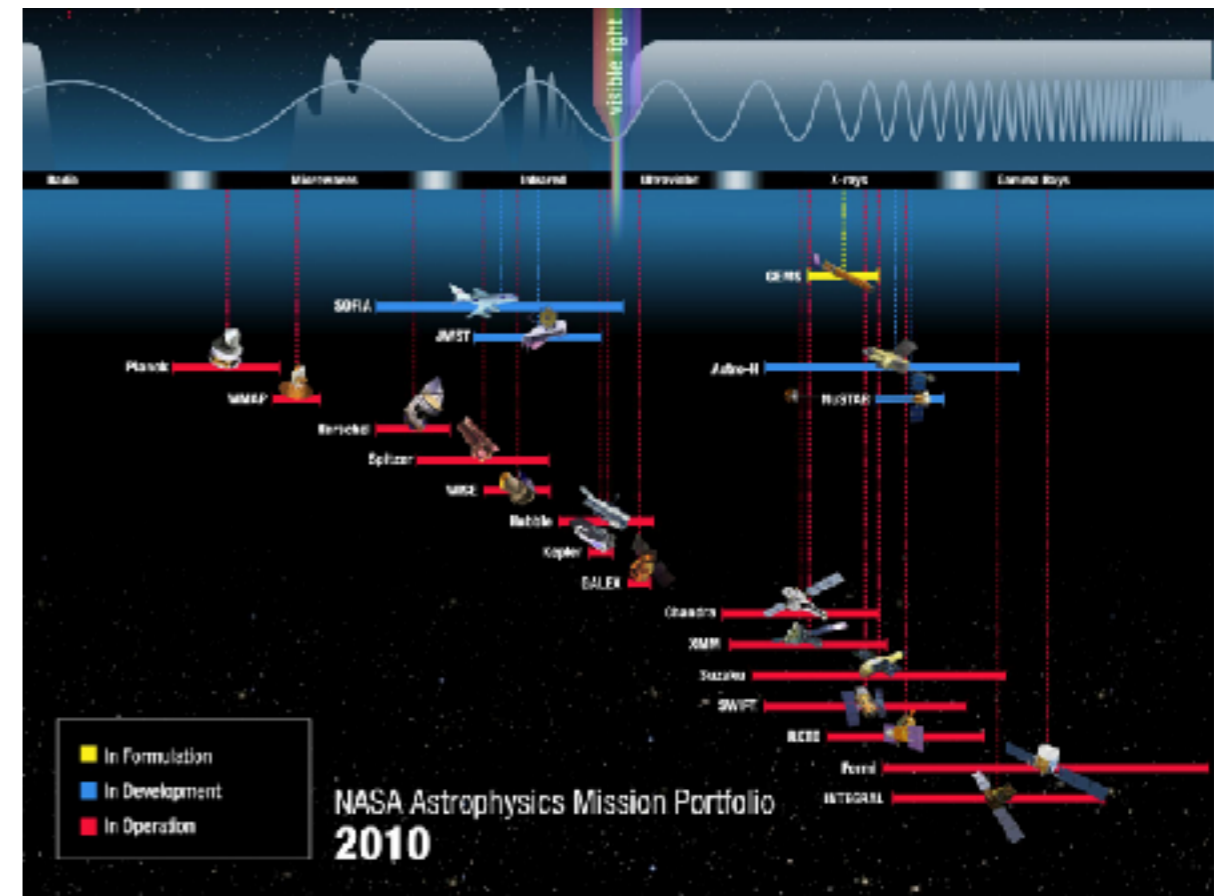
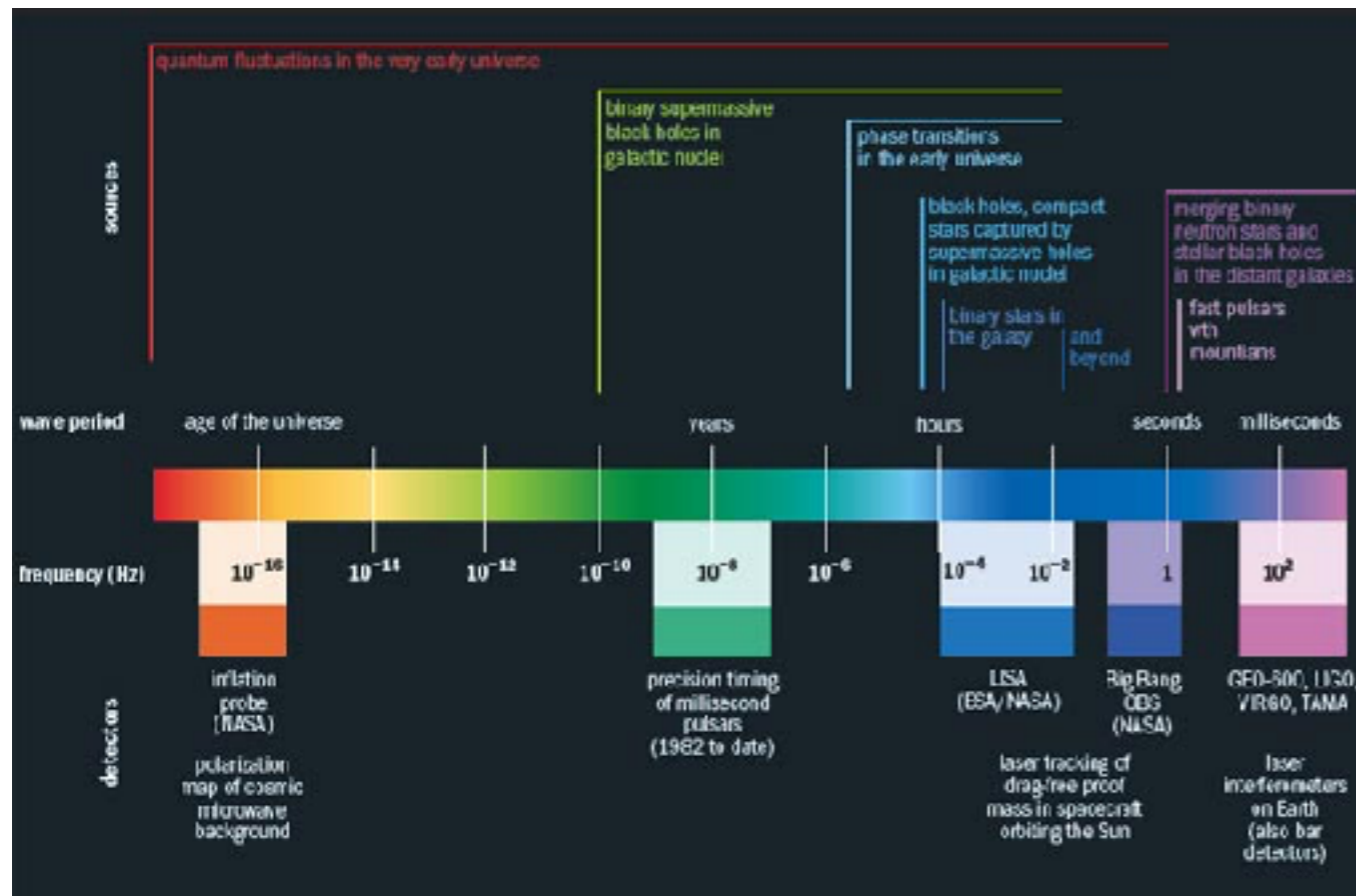
gravitational waves

- Emitted by huge and quickly moving masses
- Hardly absorbed by matter
- Probe the interior of dense objects



electromagnetic radiation

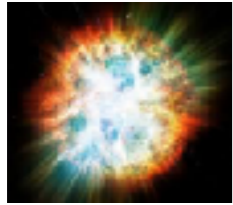
- Emitted by (thermally) moving charges
- Generally easily absorbed by matter
- Probe the surface of dense objects



frequency

(particle rays >>)

# Generic evolution of pulsars



Newborn compact stars

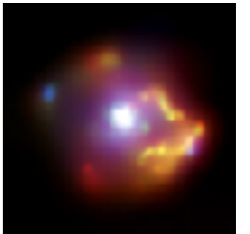
... some could spin about as fast as allowed by stability ( $>1\text{kHz}$ )

C. D. Ott, et. al., APJS, 164 (2006) 130



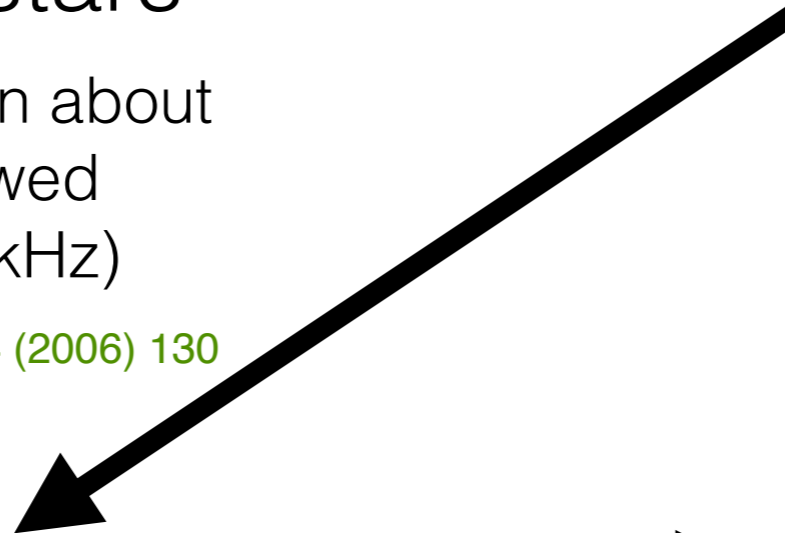
Young compact objects

(e.g. CasA, SN1987A)  
no pulsation,  
most even undetected



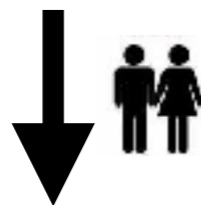
Observed young pulsars

ages  $>1000$  years & spin with surprisingly low frequencies



Non-pulsating compact stars

... become invisible



Why?



Low mass X-ray binaries

spinup by accretion from a companion over many millions of years



“recycling”



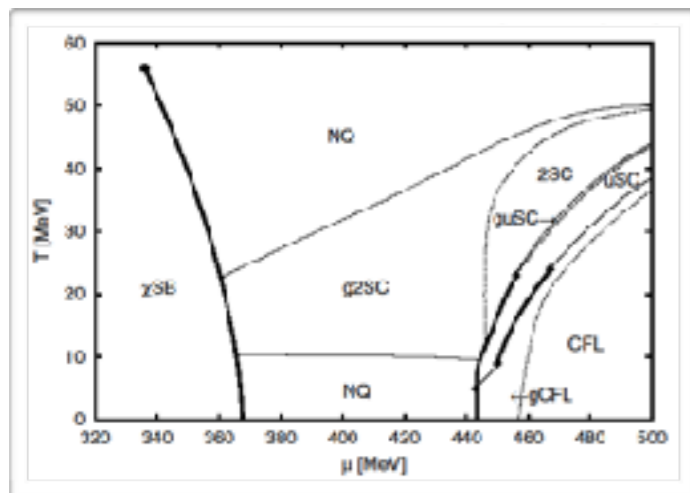
Millisecond pulsars

can be billions of years old and are extremely stable



# Forms of dense matter

- In hadronic matter there are simply many different particles: (non-relativistic) nucleons, hyperons, leptons, ... and maybe mesons
- There are few quarks, but a wealth of possible condensation patterns:



- ▶ fully gapped phases (color-flavor locking at asymptotic  $\mu$ )
- ▶ partially gapped color superconducting phases (e.g. 2SC)
- ▶ inhomogeneous and anisotropic condensates (e.g. LOFF)
- ▶ ungapped quark matter

$m_s$

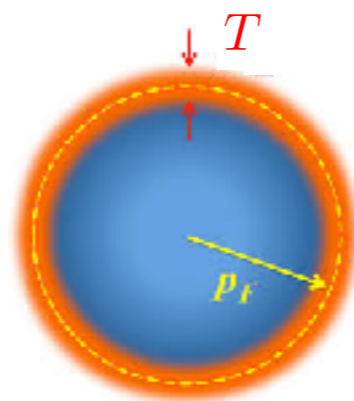


S. Ruster, et. al., PRD 73 (2006) 034025

◆ Many dozens of studied phases - uncountably many potential ones!

Equation of state is rather similar for different forms of matter ...

Material properties, determined by low energy degrees of freedom, can be drastically different



# Dissipation in dense matter

- Shear viscosity from particle scattering (strong/EM interaction)

candidate phase	dominant processes	shear viscosity	reference
(ungapped) nuclear matter	$e + e \rightarrow e + e$ $n + n \rightarrow n + n$	$\eta \sim (T/\mu)^{-5/3} \& (T/\mu)^{-2}$	Shternin, <i>et.al.</i> , PRD 78 (2008) 063006
hyperonic matter	$e + e \rightarrow e + e$ $n + n \rightarrow n + n$	$\eta \sim (T/\mu)^{-5/3} \& (T/\mu)^{-2}$	“
superfluid nuclear matter	$e + e \rightarrow e + e$	$\eta \sim (T/\mu)^{-3}$	Manuel, <i>et.al.</i> , PRD 84 (2011) 123007
ungapped quark matter	$q + q \rightarrow q + q$	$\eta \sim (T/\mu)^{-5/3}$	Heiselberg, <i>et.al.</i> , PRD 48 (1993) 2916
CFL quark matter	$H \rightarrow H + H$	$\eta \sim (T/\mu)^4$	Manuel, <i>et. al.</i> , JHEP 09 (2005) 76; Andersson, <i>et. al.</i> , PRD 82 (2010) 023007

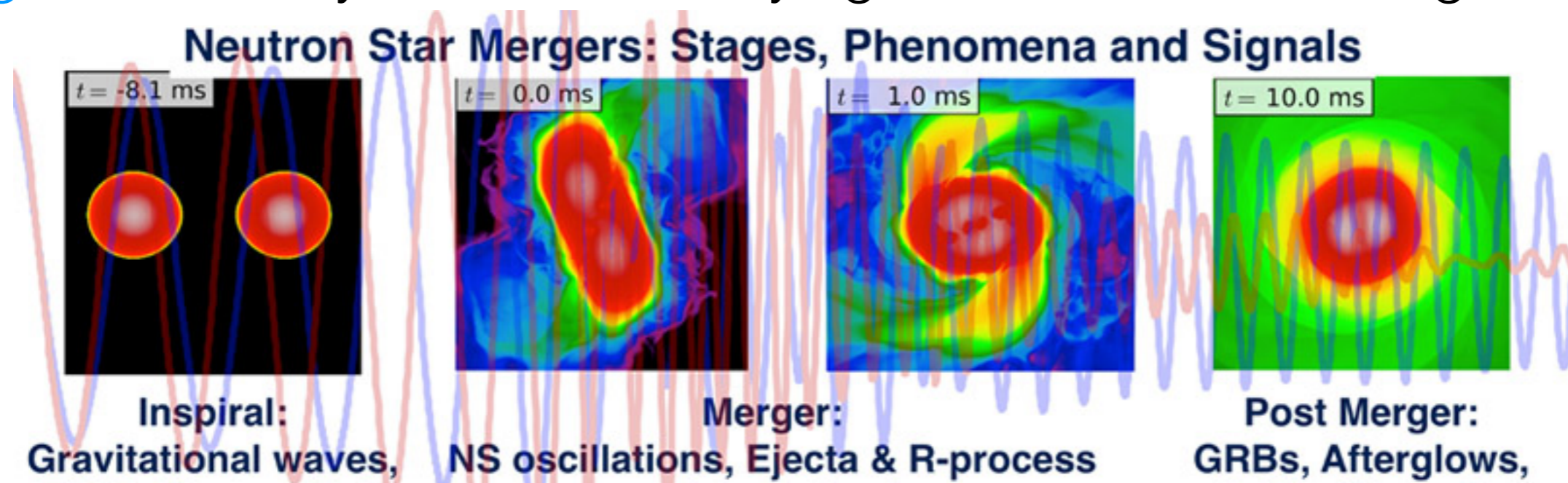
- Bulk viscosity from particle transformation (weak interaction)

candidate phase	dominant processes	bulk viscosity: low T	reference
(ungapped) nuclear matter	$n(+n) \rightarrow p(+n) + e + \bar{\nu}$ $p(+n) \rightarrow n(+n) + e + \nu$	$\zeta \sim (T/\mu)^6$ or $(T/\mu)^4$	Sawyer, PLB 233 (1989) 412; Haensel, <i>et.al.</i> , PRD 45 (1992) 4708
hyperonic matter	$n + n \rightarrow p + \Sigma^-, \dots$	$\zeta \sim (T/\mu)^2$	Haensel, <i>et. al.</i> , A&A 381 (2002) 1080
superfluid nuclear matter	$e + l \leftrightarrow \mu + l + \nu + \bar{\nu}$	$\zeta \sim (T/\mu)^7$	Alford, <i>et.al.</i> , PRC 82 (2010) 055805
ungapped quark matter	$d + u \leftrightarrow s + u$	$\zeta \sim (T/\mu)^2$	Madsen, PRD 46 (1992) 3290
CFL quark matter	$K_0 \rightarrow H + H$	$\zeta \sim e^{-c(\mu/T)}$	Alford, <i>et.al.</i> , PRC 75 (2007) 055209

Alternative forms of matter show dramatically different damping, since  $T/\mu \sim O(10^{-4})$

# Neutron star merger phases

- *Inspiral*: Neutron stars in a binary emit gravitational radiation whereby they lose energy and approach each other
  - ▶ this process speeds up and gives a characteristic “chirp” signal
- *Merger*: Once they merge, the evolution depends on the total mass:
  - ▶ if it is very low a stable massive neutron star might form
  - ▶ if it is high it will collapse immediately to a black hole
  - ▶ at intermediate masses a metastable state forms, that is stabilized by its angular momentum (or thermal pressure), before it collapses
- *Ringdown*: Finally there is a decaying oscillation of the merged object



# Merger dynamics

- A compact star merger produces a highly excited system with huge kinetic energy

- ▶ can be dissipated in two different ways:

- ✓ gravitational wave emission

- ➔ internal dissipation?

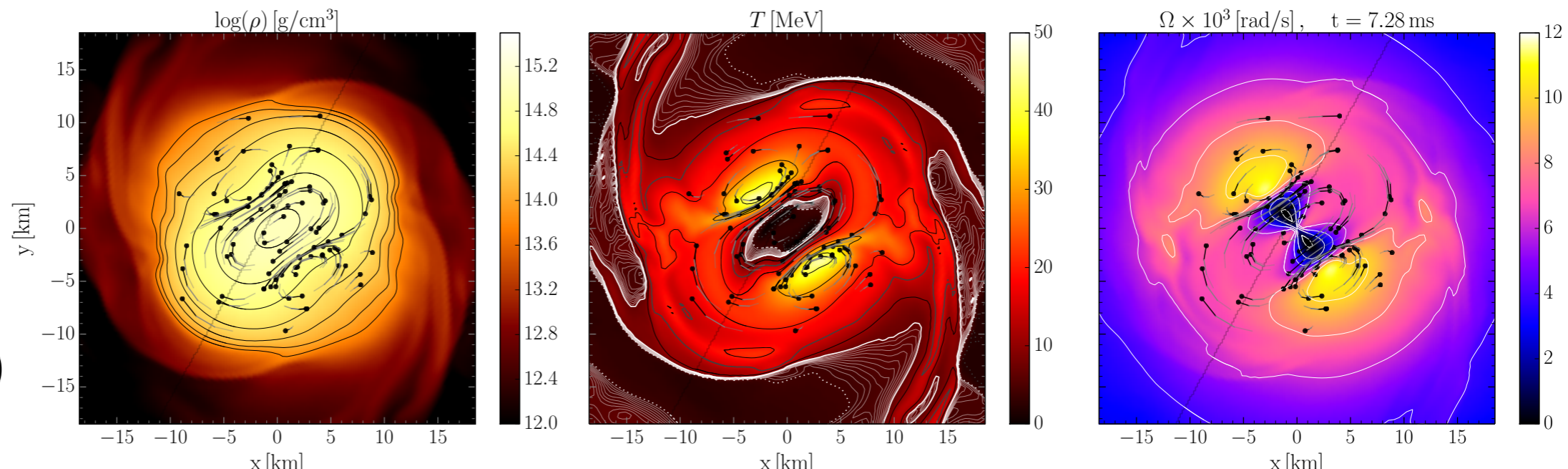
M. Alford, L. Bovard, M. Hanauske, L. Rezzolla, K. Schwenzer, PRL 120, 041101 (2018)

- Simulations are presently treated in ideal hydrodynamics

- gravitational wave emission for dozens of milliseconds

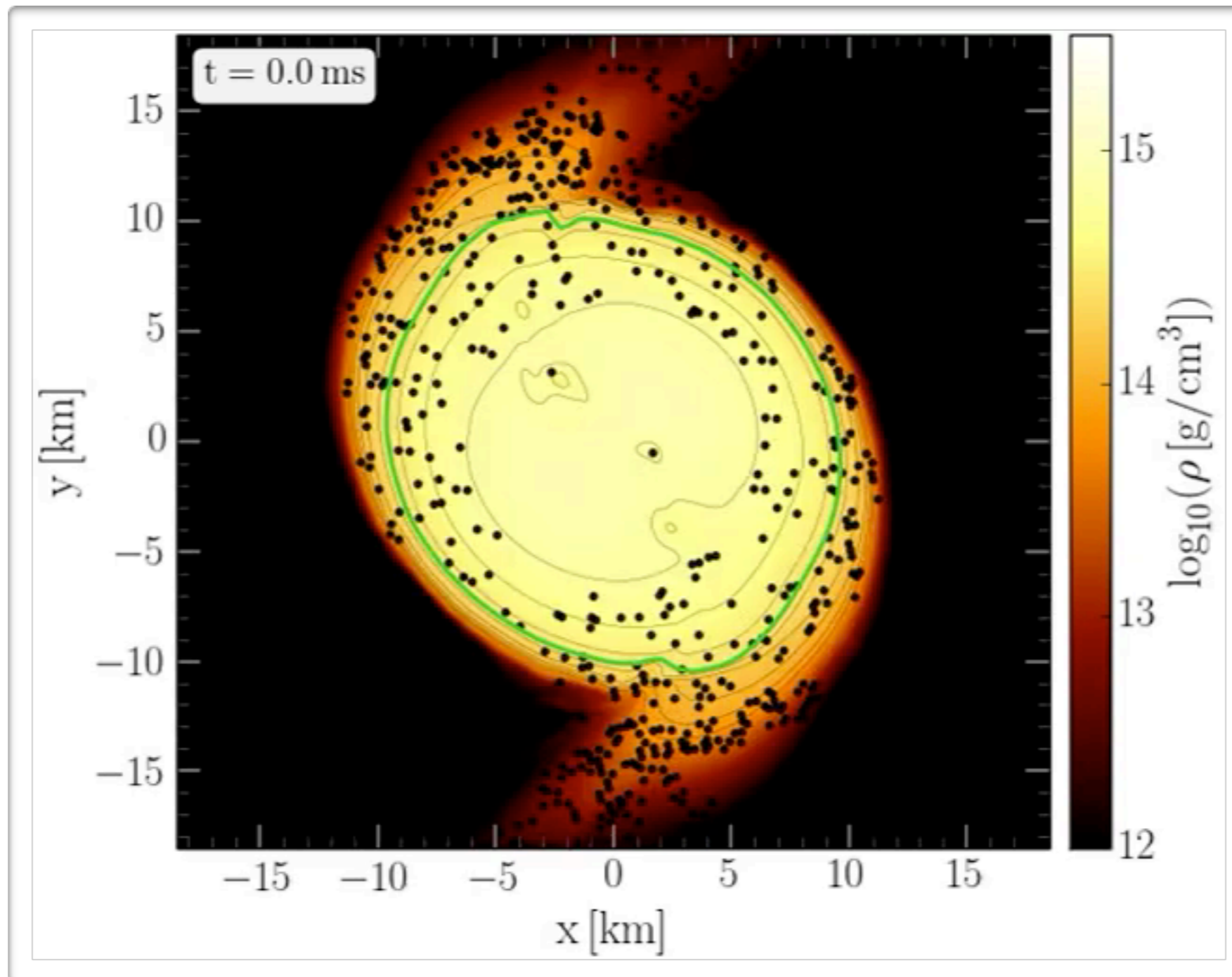
- Dissipation could affect both form and duration of the signal

as well as the final state (compact star / black hole)



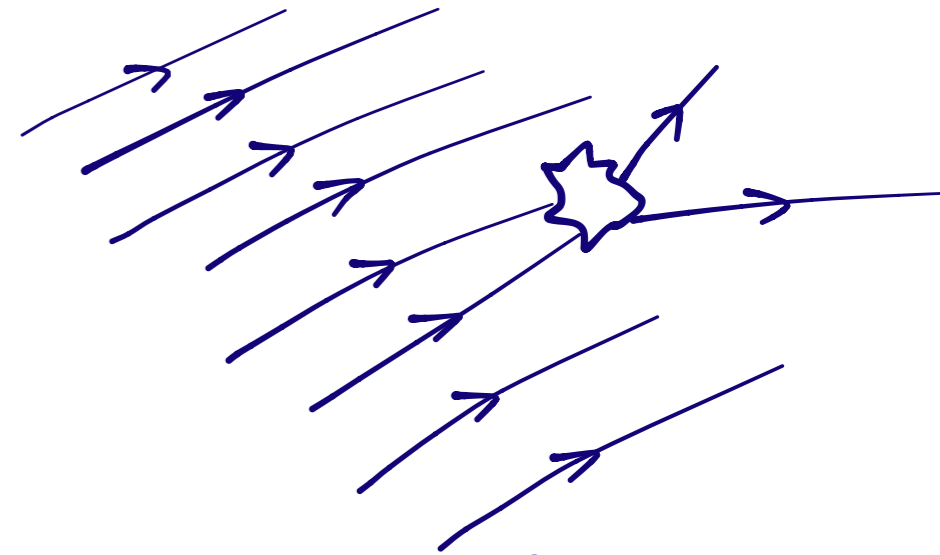


# Exemplary merger simulation (density)



simulation by L. Rezzolla and collaborators

# Shear dissipation timescale



- The kinetic energy density of a (Newtonian) fluid flowing in x-direction is  $e_{\text{kin}} = \frac{1}{2}\rho v_x^2$
- The dissipated power density due to shear is  $w_{\text{shear}} \approx \eta (dv_x/dz)^2$
- If the velocity changes direction on a distance scale  $z_{\text{typ}}$ , this provides a characteristic time scale on which shear dissipation becomes relevant:  $\tau_\eta \equiv e_{\text{kin}}/w_{\text{shear}} \approx \rho z_{\text{typ}}^2/(2\eta)$
- At low  $T$  **electrons** dominate the shear viscosity  $\eta^{(e)} \approx 0.2 n_e^{14/9} / (\alpha^{5/3} T^{5/3})$  which gives  
Shternin & Yakovlev, PRD 78 (2008) 063006

$$\tau_\eta^{(e)} \approx 1.6 \times 10^8 \text{ s} \left( \frac{z_{\text{typ}}}{1 \text{ km}} \right)^2 \left( \frac{T}{1 \text{ MeV}} \right)^{5/3} \left( \frac{n_0}{n_B} \right)^{5/9} \left( \frac{0.1}{x_p} \right)^{14/9},$$
- However at high  $T$  **neutrinos** dominate  $\eta^{(\nu)} \approx 0.46 n_\nu^{4/3} / (G_F^2 (m_n^*)^2 n_e^{1/3} T^2)$  since their mean free path becomes short enough that they are trapped inside the star  
Goodwin & Pethick, APJ 253 (1982) 816

$$\tau_\eta^{(\nu)} \approx 54 \text{ s} \left( \frac{0.1}{x_p} \right) \left( \frac{m_n^*}{0.8 m_n} \right)^2 \left( \frac{\mu_e}{2 \mu_\nu} \right)^4 \left( \frac{z_{\text{typ}}}{1 \text{ km}} \right)^2 \left( \frac{T}{10 \text{ MeV}} \right)^2$$

# Thermal conduction timescale

- The thermal equilibration timescale can be estimated in terms of the distance  $z_{\text{typ}}$  of thermal gradients:  $\tau_{\kappa} \approx c_V z_{\text{typ}}^2 / (6\kappa)$
- Thermal transport results from the movement of microscopic particles and the thermal conductivity is in kinetic theory given by

$$\kappa \propto \sum_i \kappa_i \propto \sum_i n_i v_i \lambda_i$$

↑ particle density    ↑ mean free path

- At low  $T$  **electrons** dominate  $\kappa_e \approx 1.5 n_e^{2/3} / \alpha$  Shternin & Yakovlev, PRD 75 (2007) 103004

$$\tau_{\kappa}^{(e)} \approx 5 \times 10^8 \text{ s} \left( \frac{0.1}{x_p} \right)^{\frac{2}{3}} \left( \frac{m_n^*}{0.8 m_n} \right) \left( \frac{n_0}{n_B} \right)^{\frac{1}{3}} \left( \frac{z_{\text{typ}}}{1 \text{ km}} \right)^2 \left( \frac{T}{1 \text{ MeV}} \right)$$

- However at high  $T$  **neutrinos** dominate  $\kappa_{\nu} \approx 0.33 n_{\nu}^{2/3} / (G_F^2 (m_n^*)^2 n_e^{1/3} T)$  since they become degenerate Goodwin & Pethick, APJ 253 (1982) 816

$$\tau_{\kappa}^{(\nu)} \approx 0.7 \text{ s} \left( \frac{0.1}{x_p} \right)^{\frac{1}{3}} \left( \frac{m_n^*}{0.8 m_n} \right)^3 \left( \frac{\mu_e}{2 \mu_{\nu}} \right)^2 \left( \frac{z_{\text{typ}}}{1 \text{ km}} \right)^2 \left( \frac{T}{10 \text{ MeV}} \right)^2$$

# Bulk viscosity

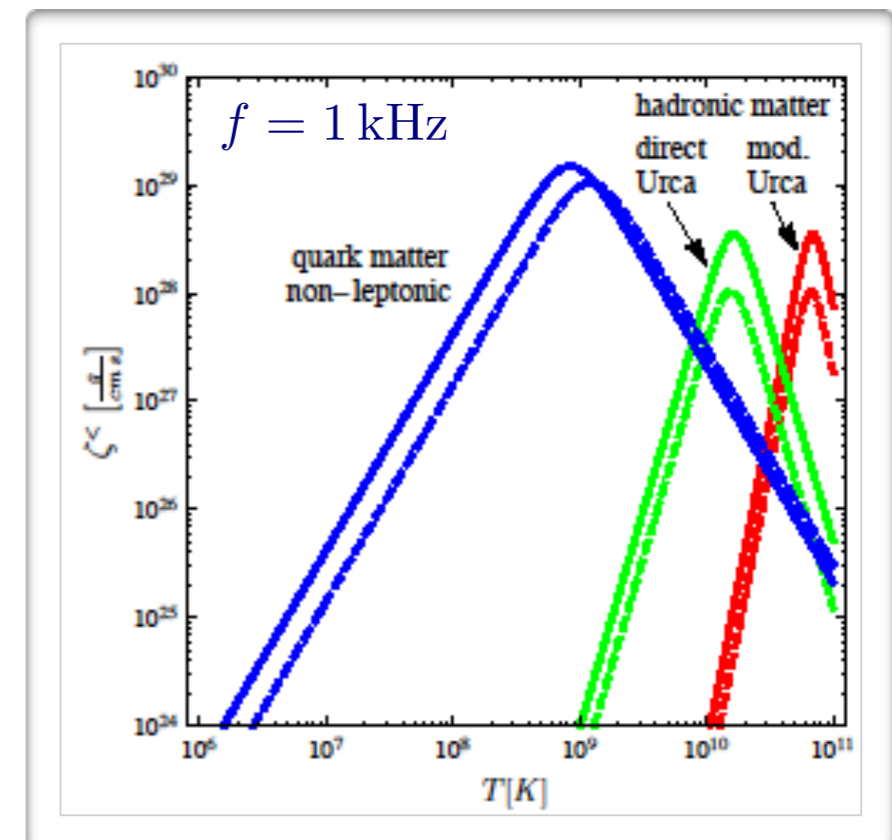
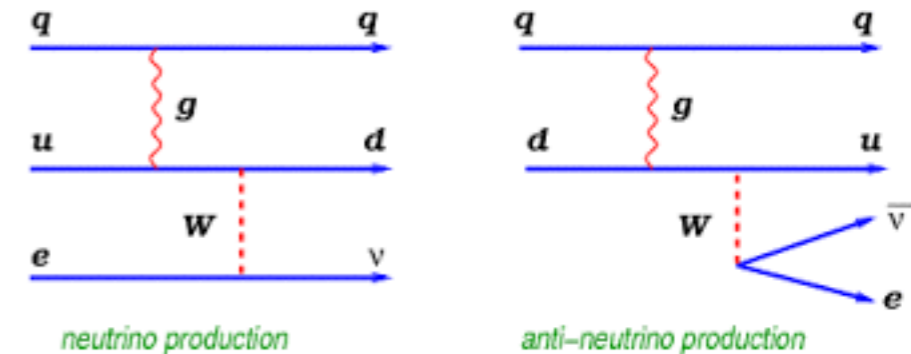
- The bulk viscosity describes the dissipation, due to a non-adiabatic density change - resulting in a new statistical equilibrium
- In particular for a density oscillation, changing the chemical composition works by slow weak interactions and therefore lags behind a driving density oscillation
- The average bulk viscosity is maximal if the equilibration time scale matches the external oscillation time which results in a resonant behavior

$$\zeta = \frac{C^2 \tilde{\Gamma} T^\delta}{\omega^2 + \tilde{\Gamma}^2 B^2 T^{2\delta}}$$

- The maximum is given by

$$\bar{\zeta}_{\max} = Y_\zeta \bar{n} t_{\text{dens}} \quad , \quad Y_\zeta \equiv C^2 / (4\pi B \bar{n})$$

Modified Urca interactions:  
(quarks bound in baryons)

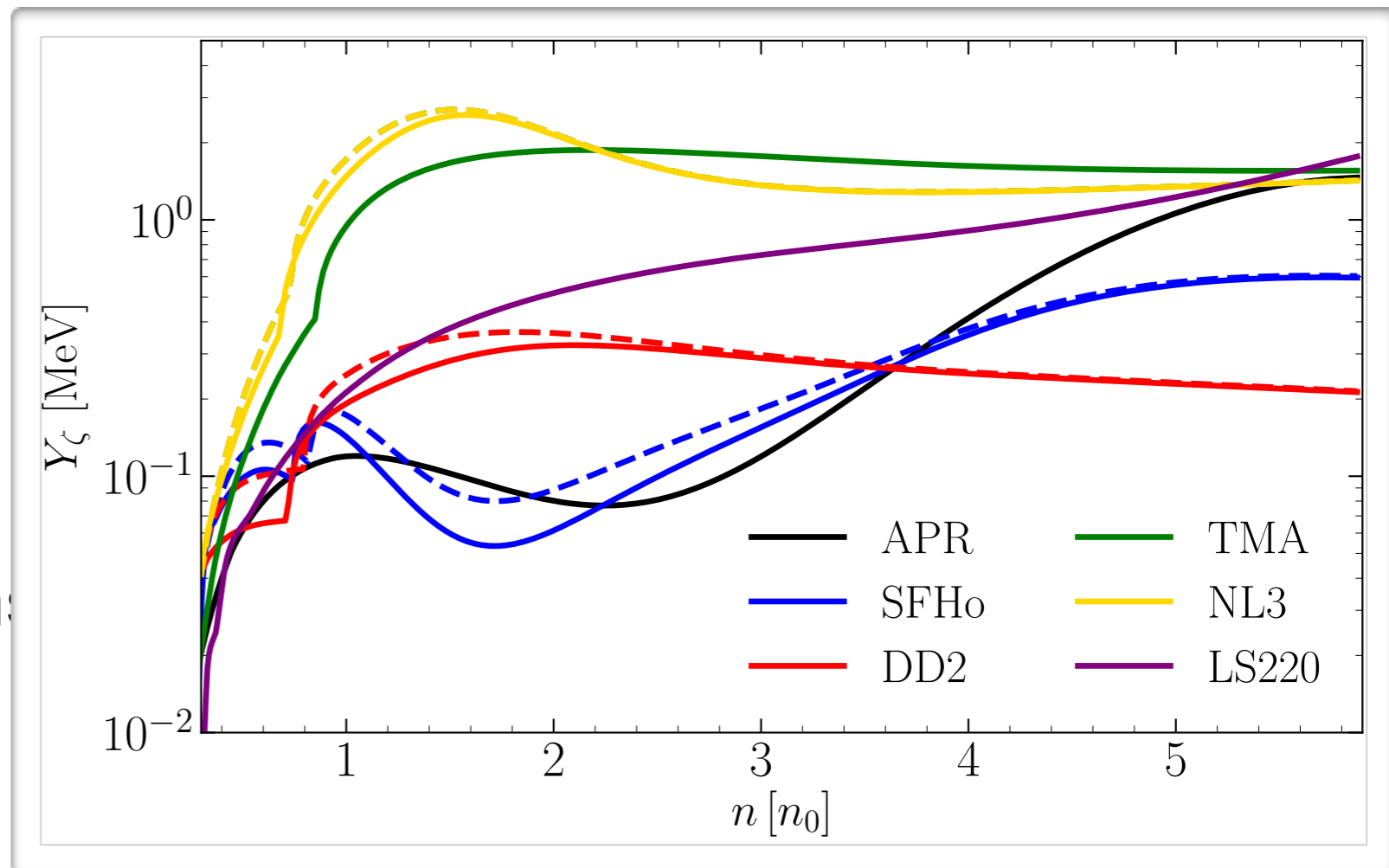


# Bulk dissipation time scale

- The energy density due to compression is  $\mathcal{E}_{\text{comp}} \approx K\bar{n}(\Delta n/\bar{n})^2/18$
- The dissipated power density due to bulk viscosity is for a harmonic oscillation  $(d\mathcal{E}/dt)_{\text{bulk}} \approx 2\pi^2\bar{\zeta}(\Delta n/\bar{n})^2/t_{\text{dens}}^2$
- This gives the bulk timescale  $\tau_{\zeta} \equiv \mathcal{E}_{\text{comp}}/(d\mathcal{E}/dt)_{\text{bulk}} \approx K\bar{n}t_{\text{dens}}^2/(36\pi^2\bar{\zeta})$
- This gives a time scale  $\tau_{\zeta}^{\text{min}} \approx 3 \text{ ms} \left(\frac{t_{\text{dens}}}{1 \text{ ms}}\right) \left(\frac{K}{250 \text{ MeV}}\right) \left(\frac{0.25 \text{ MeV}}{Y_{\zeta}}\right)$
- The maximum is reached for all relevant densities and frequencies at

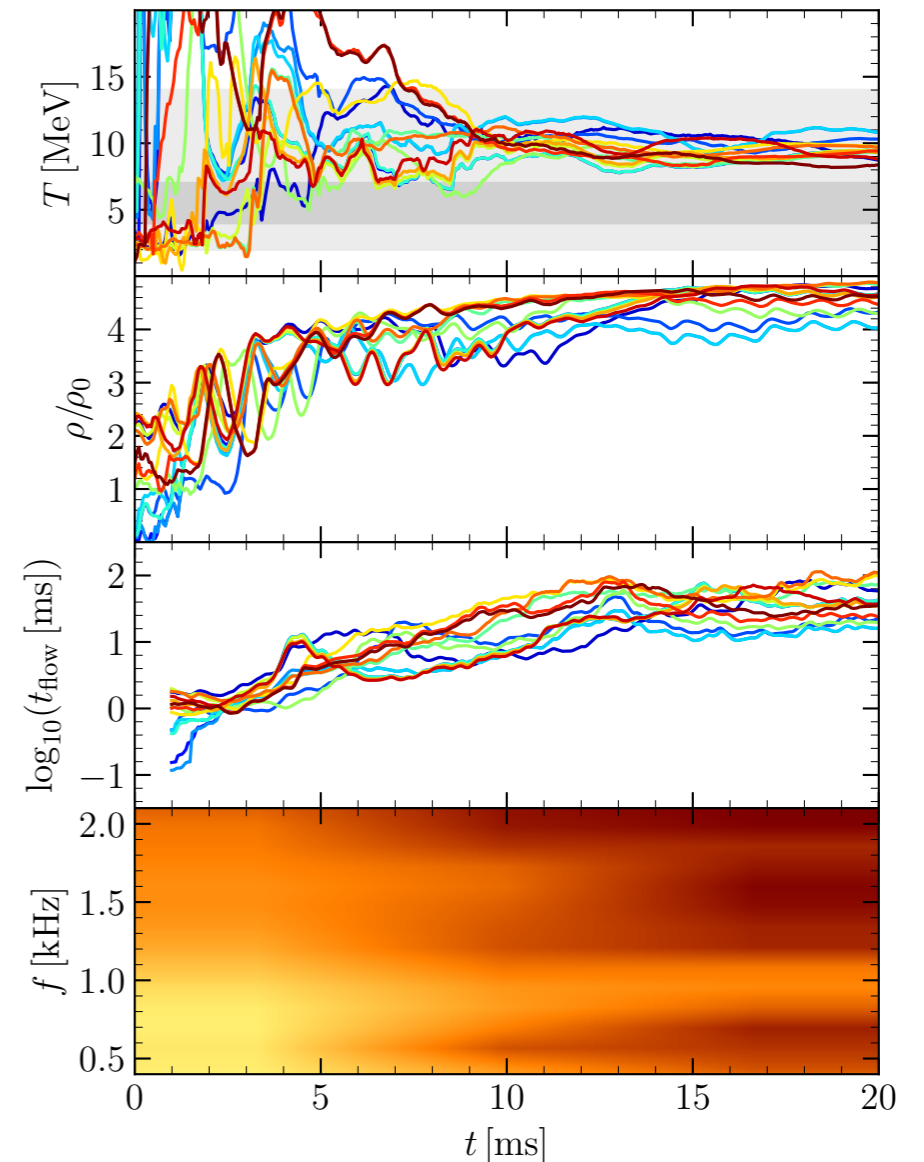
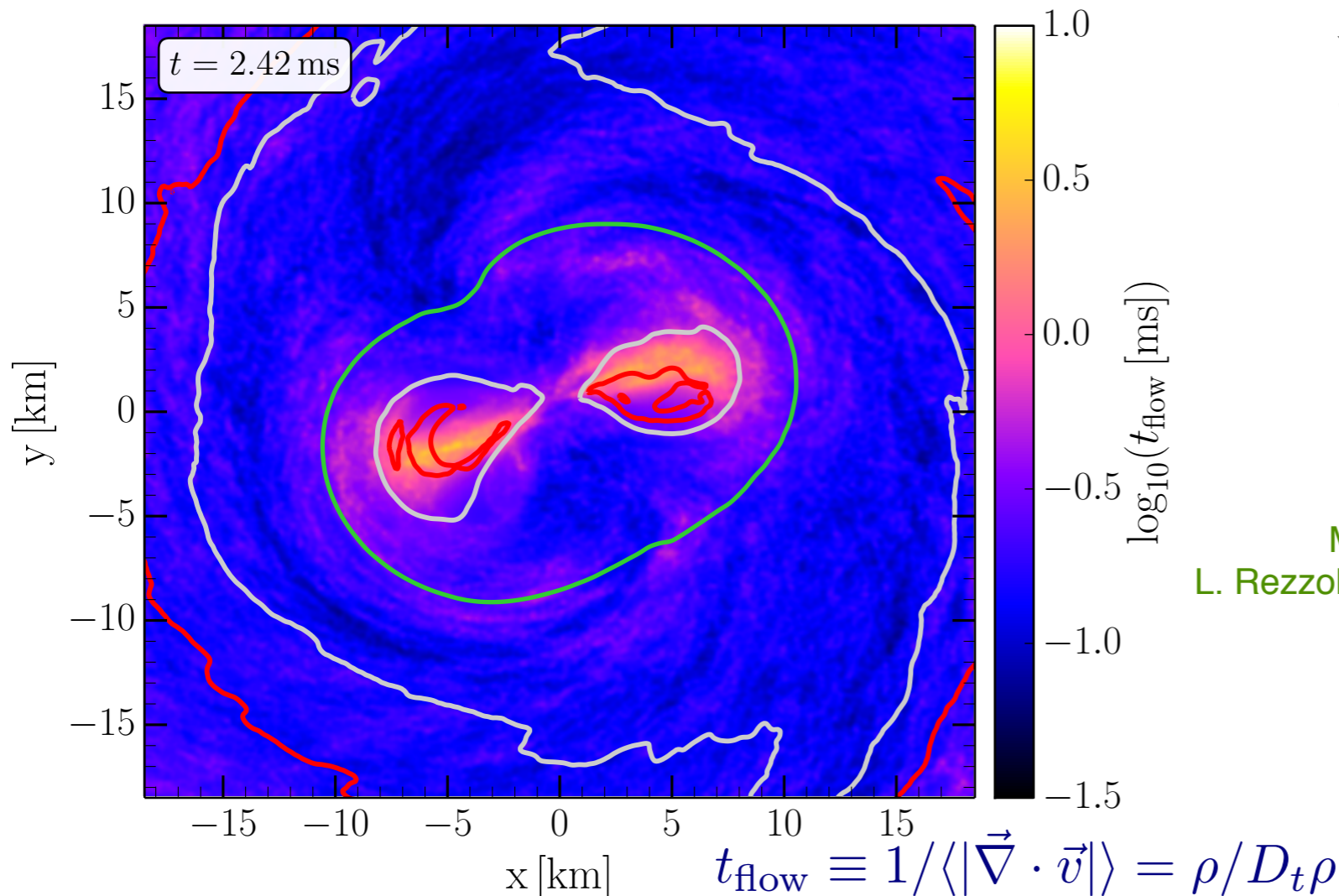
$$T_{\zeta_{\text{max}}}^{\text{nmU}} \approx 4 - 7 \text{ MeV}$$

- If parts of the star are at such temperatures and undergo density oscillations on ms-timescales the damping will be huge!



# Damping of density oscillations

- Very strong damping in sizable regions within the dense merger product
- Dissipation needs to be included in relativistic hydro simulations
- Could be strong enough to significantly change the evolution ...



$$t_{\text{dens}} \approx (4\Delta n/\bar{n})t_{\text{flow}} \sim t_{\text{flow}}$$

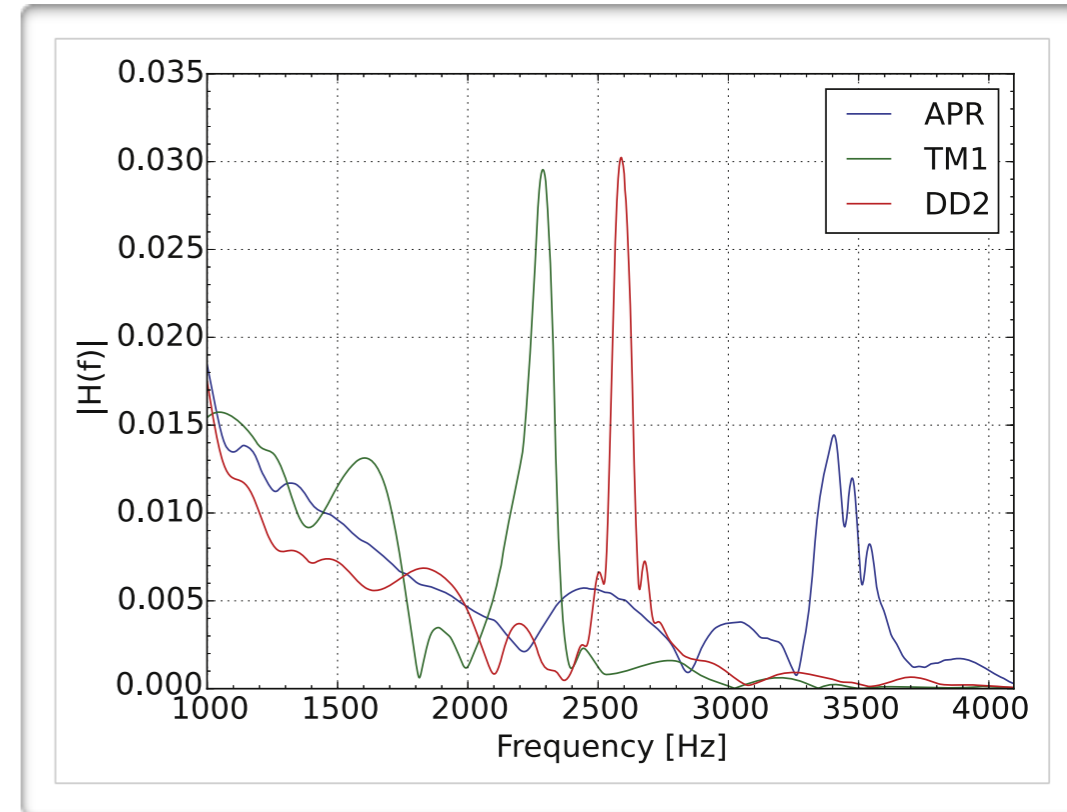
M. Alford, L. Bovard, M. Hanauske,  
L. Rezzolla, K. Schwenzer, PRL 120, 041101 (2018)

thermal dUrca  
opening?

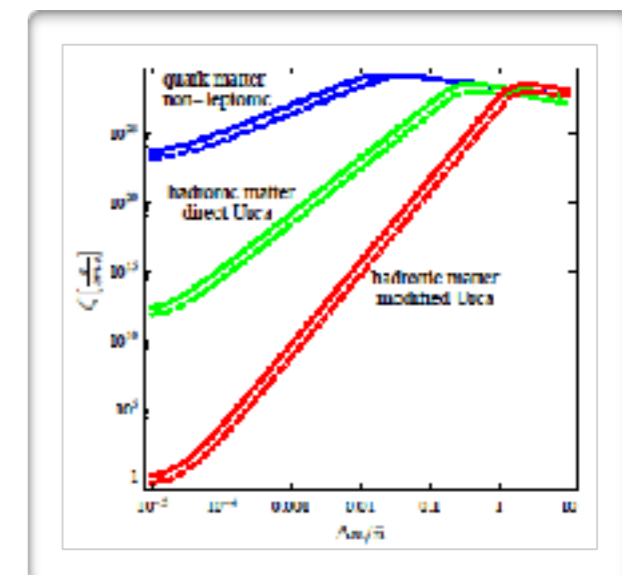
Alford, Harris, arXiv:1803.00662

# Expected impact on the GW signal

- A significant damping on ms-timescales will drain energy and thereby shorten the gravitational wave signal
  - ✓ should be observable due to characteristic oscillations
- If the dissipated heat will not be efficiently distributed, the additional pressure could stabilize the remnant and will change the large scale flow as well as the GW signal
- To compare to future GW data requires realistic simulations that include dissipative effects
  - hard to implement (non-linearities)
- Bulk viscosity is even enhanced at large amplitudes and methods to include bulk viscosity are currently developed ...



J. Clark, et. al. *Class. Quantum Grav.* 33 (2016) 085003



Mergers are like falling stars ...



... but there could be literally billions of continuous compact gravitational wave sources!



# R-mode oscillations

- **R-mode**: Global oscillation eigenmode of a rotating star which emits gravitational waves

N. Andersson, *Astrophys. J.* 502 (1998) 708,

K. Kokkotas, *LRR* 2 (1999) 2,

N. Andersson, K. Kokkotas, *IJMP D10* (2001) 384

- Mainly an incompressible flow in individual shells, but involves density fluctuations at large frequency

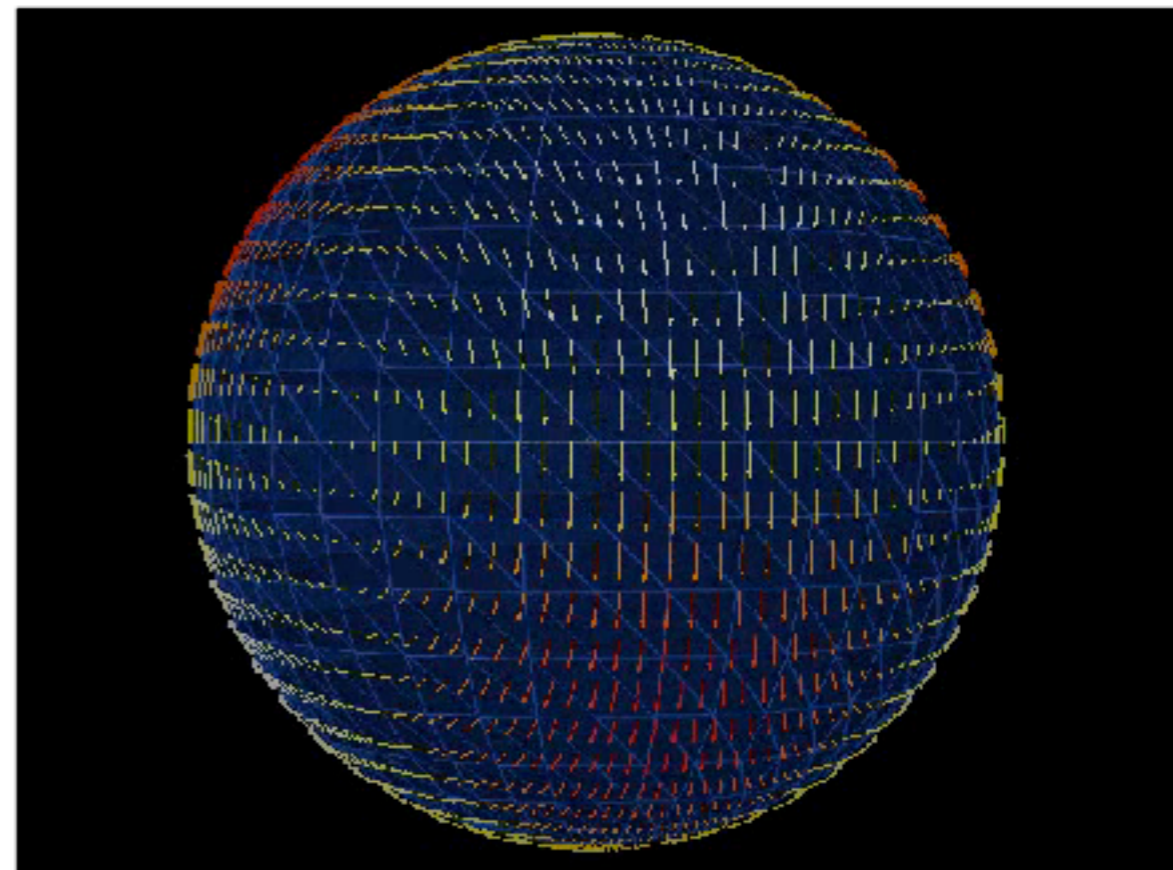
L. Lindblom, et. al., *PRL* 80 (1998) 4843,

B. J. Owen, et. al., *Phys. Rev. D* 58 (1998) 084020



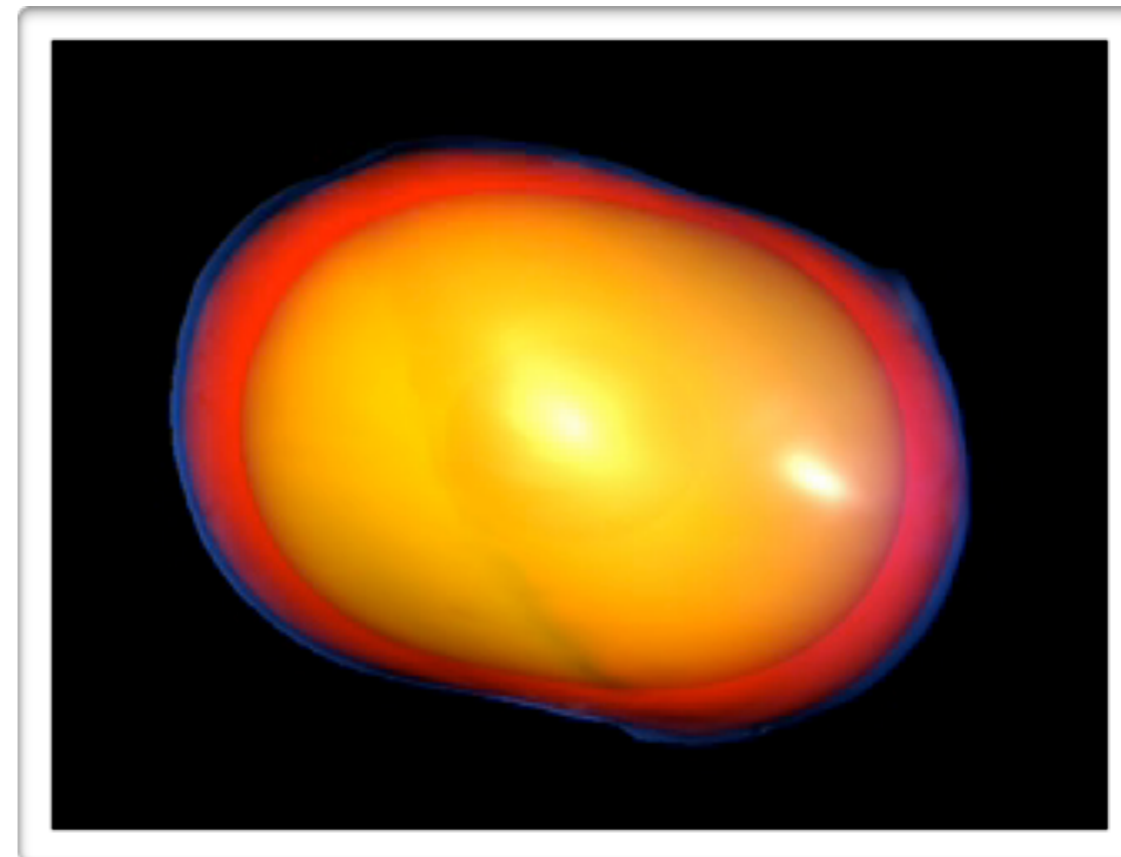
- Large amplitude r-modes could cause a quick spindown

- Yet we see very fast spinning (and slowly decelerating) sources: limits the amplitude



Visualization by M. Beilicke

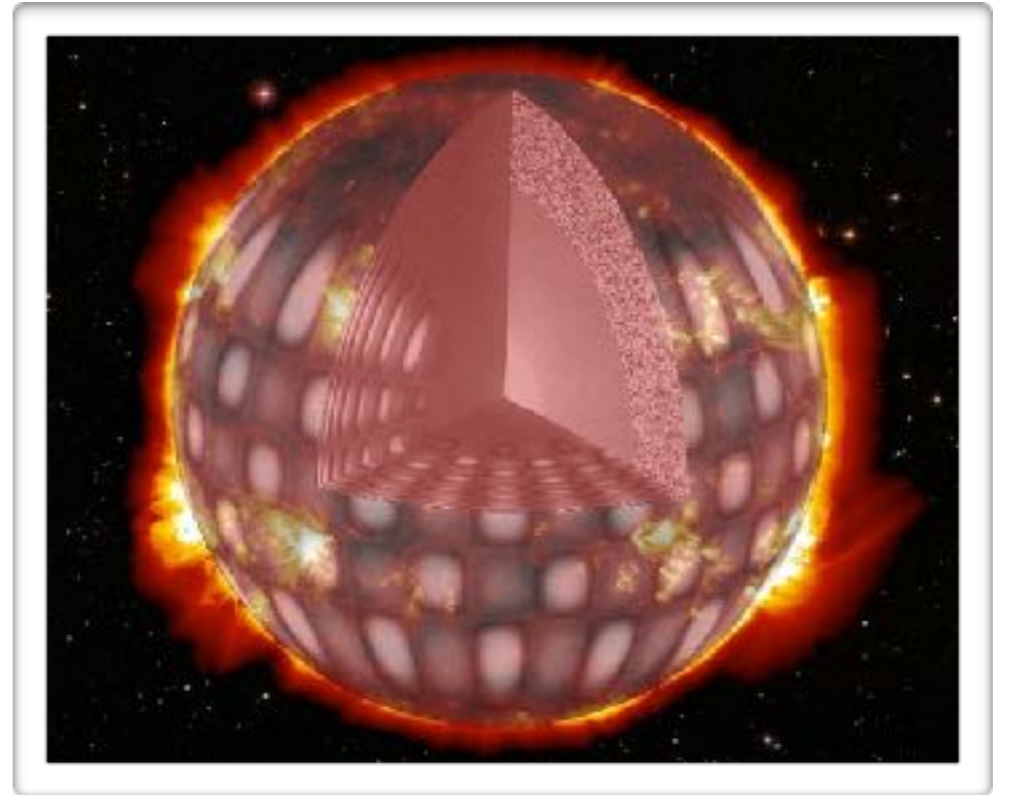
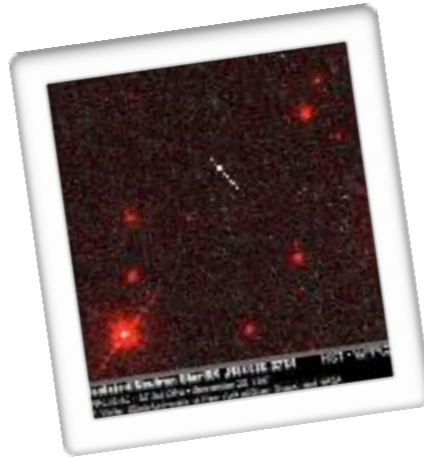
r-mode spectrum:  $\omega = -4/3\chi\Omega$





Simulation by L. Lindblom



# “Seeing into ... ... a compact star”



- Electromagnetic radiation originates from the surface - connection to the interior very indirect
- Yet, one can use similar methods we use to learn about the interior of the earth or the sun: **“Seismology”**
- When non-axisymmetric **oscillations** are not damped away they **emit gravitational waves**, spinning a star down ...
  - ✓ **direct** detection via gravitational wave detectors  advanced LIGO
  - ✓ **indirect** detection via spin data of pulsar: many fast spinning sources observed! 
- Star **oscillations are damped by viscosity**, which is induced by microscopic particle interactions

... links macroscopic observables to microphysics of dense matter

# R-mode instability

- General relativity and ideal hydrodynamics predict that r-modes are unstable to gravitational wave emission

→ mode amplitude (fluid velocity) grows exponentially

J. Friedman, B. Schutz, APJ 221 (1978) 937

- Yet realistic cold dense matter is not (even close to) an ideal fluid ...

there are two possibilities:



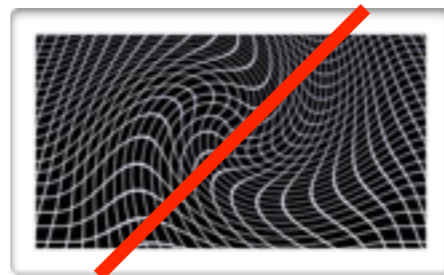
**Damping**

**Saturation**



- If the viscous damping is strong enough even at low amplitude, the mode is completely damped away (does not even arise)

→ no gravitational waves



- But even if the mode is initially unstable, the growth eventually stops due to some non-linear damping mechanism, e.g.:

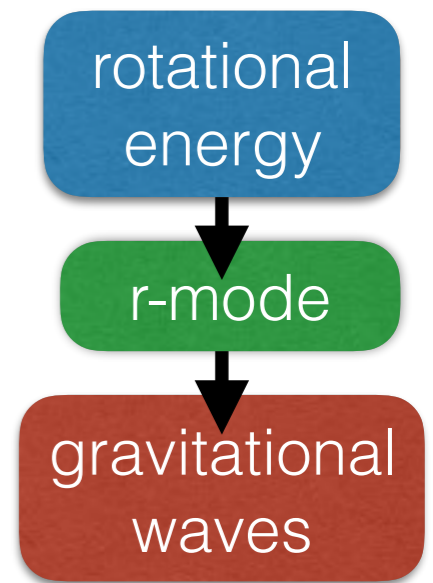
- ▶ **non-linear hydro or viscous damping - large**  $\alpha_{\text{sat}} = O(1)$

L. Lindblom, et. al., PRL 86 (2001) 1152,

M. Alford, S. Mahmoodifar and K.S., PRD 85 (2012) 044051

- ▶ **mode-coupling - moderate**

P. Arras, et. al., Astrophys. J. 591 (2003) 1129  $\alpha_{\text{sat}} = O(10^{-5})$



# “Effective Theory of pulsars”

- Observable macroscopic properties depend only on quantities that are integrated over the entire star:

$$I = \tilde{I} M R^2 \quad (\text{MOMENT OF INERTIA})$$

$$P_G = \frac{32\pi(m-1)^{2m}(m+2)^{2m+2}}{((2m+1)!!)^2(m+1)^{2m+2}} \tilde{J}_m^2 G M^2 R^{2m+2} \alpha^2 \Omega^{2m+4} \quad (\text{POWER DRIVING THE R-MODE})$$

$$P_S = -\frac{(m-1)(2m+1)\tilde{S}_m \Lambda_{\text{QCD}}^{3+\sigma} R^3 \alpha^2 \Omega^2}{T^\sigma} \quad (\text{DISSIPATED POWER DUE TO SHEAR / BULK VISCOSITY})$$

$$P_B = -\frac{16m}{(2m+3)(m+1)^5 \kappa^2} \frac{\Lambda_{\text{QCD}}^{9-\delta} \tilde{V}_m R^8 \alpha^2 \Omega^4 T^\delta}{\Lambda_{\text{EW}}^4 \tilde{J}_m}$$

$$L_\nu = 4\pi R^3 \Lambda_{\text{EW}}^4 \Lambda_{\text{QCD}}^{1-\theta} \tilde{L} T^\theta \quad (\text{NEUTRINO LUMINOSITY})$$

# “Effective Theory of pulsars”

- Observable macroscopic properties depend only on quantities that are integrated over the entire star:

$$I = \tilde{I} M R^2$$

$$\tilde{I} \equiv \frac{8\pi}{3MR^2} \int_0^R dr r^4 \rho$$

$$P_G = \frac{32\pi(m-1)^{2m}(m+2)^{2m+2}}{((2m+1)!!)^2(m+1)^{2m+2}} \tilde{J}_m^2 G M^2 R^{2m+2} \alpha^2 \Omega^{2m+4}$$

$$\tilde{J}_m \equiv \frac{1}{MR^{2m}} \int_0^R dr r^{2m+2} \rho$$

$$P_S = -(m-1)(2m+1) \tilde{S}_m \frac{\Lambda_{\text{QCD}}^{3+\sigma} R^3 \alpha^2 \Omega^2}{T^\sigma} \quad \text{with}$$

$$\tilde{S}_m \equiv \frac{1}{R^{2m+1} \Lambda_{\text{QCD}}^{3+\sigma}} \int_{R_i}^{R_o} dr r^{2m} \tilde{\eta}$$

$$P_B = -\frac{16m}{(2m+3)(m+1)^5 \kappa^2} \tilde{V}_m \frac{\Lambda_{\text{QCD}}^{9-\delta} R^8 \alpha^2 \Omega^4 T^\delta}{\Lambda_{\text{EW}}^4 \tilde{J}_m}$$

$$\tilde{V}_m \equiv \frac{\Lambda_{\text{EW}}^4}{R^3 \Lambda_{\text{QCD}}^{9-\delta}} \int_{R_i}^{R_o} dr r^2 A^2 C^2 \tilde{\Gamma} (\delta \Sigma_m)^2$$

$$L_\nu = 4\pi R^3 \Lambda_{\text{EW}}^4 \Lambda_{\text{QCD}}^{1-\theta} \tilde{L} T^\theta$$

$$\tilde{L} \equiv \frac{1}{R^3 \Lambda_{\text{EW}}^4 \Lambda_{\text{QCD}}^{1-\theta}} \int_{R_i}^{R_o} dr r^2 \tilde{\epsilon}$$

- Damping is strongly temperature dependent and r-modes strongly heat a source, which requires to consider the thermal evolution
- Pulsar evolution for r-mode amplitude  $\alpha$ , angular velocity  $\Omega$  and temperature  $T$  are obtained from global conservation laws

B. J. Owen, et. al., Phys. Rev. D 58 (1998) 084020

- \* Universal hierarchy of evolution time scales:  $\tau_\alpha \ll \tau_T \ll \tau_\Omega$

M. Alford & K. S., APJ 781 (2014) 26

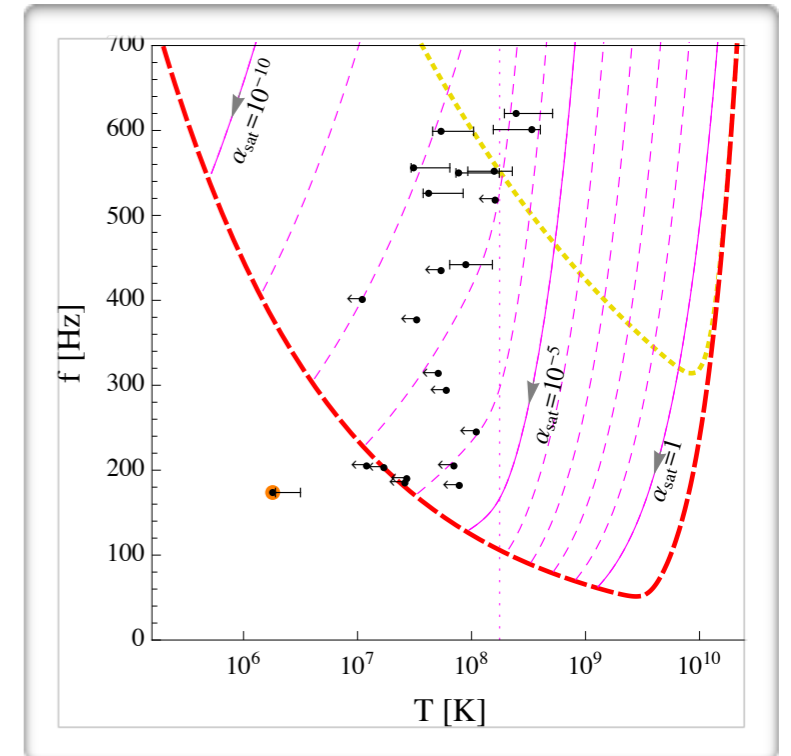
- ◆ Pulsar evolution decouples and allows semi analytic results

# Effective r-mode spindown

- The r-mode saturation mechanism is unknown and the amplitude generally depends in on powers of temperature and frequency

$$\alpha_{\text{sat}} = \hat{\alpha} T^{\beta} \Omega^{\gamma}$$

- Due to the scale hierarchy, the r-mode spindown proceeds along thermal steady state trajectories with an altered spindown law



$$\frac{d\Omega}{dt} = -\frac{3}{I} \left( \frac{\chi^{5\theta} (3 - 2\chi)^{2\beta} \hat{G}^{\theta} \hat{\alpha}_{\text{sat}}^{2\theta}}{\hat{L}^{2\beta}} \right)^{\frac{1}{\theta - 2\beta}} \Omega^{n_{\text{rm}}} \quad n_{\text{rm}} \equiv \frac{(7 + 2\gamma)\theta + 2\beta}{\theta - 2\beta}$$

➔ in terms of an **effective r-mode braking index**

- e.g. mode coupling:  $n_{\text{rm}}^{(\text{mc})} = 4$ , vortex-fluxtube-cutting:  $n_{\text{rm}}^{(\text{vfc})} = 1$

P. Arras, et. al., *Astrophys. J.* 591 (2003) 1129

B. Haskell, K. Glampedakis, N. Andersson, *MNRAS* 441 (2014) 1662

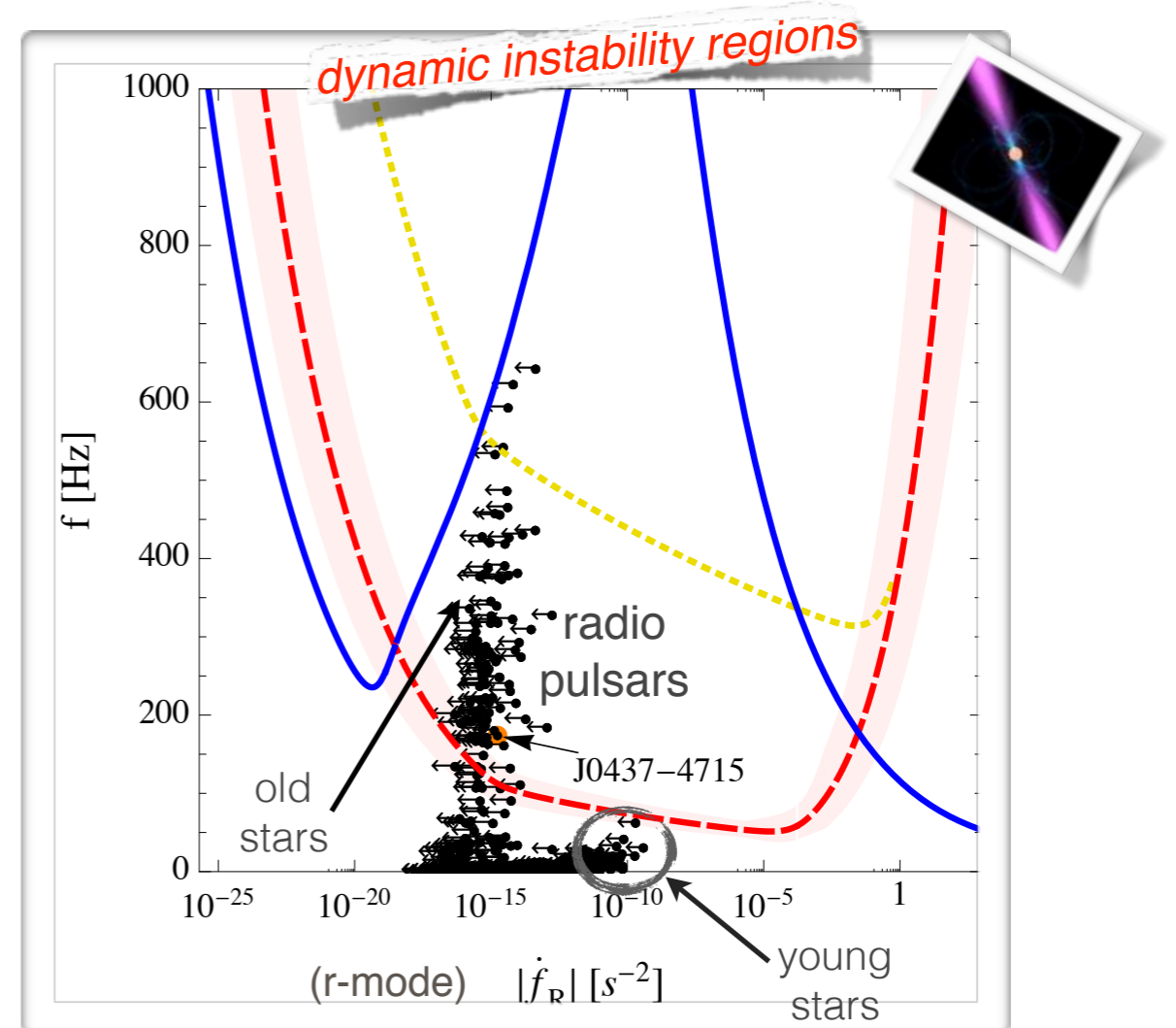
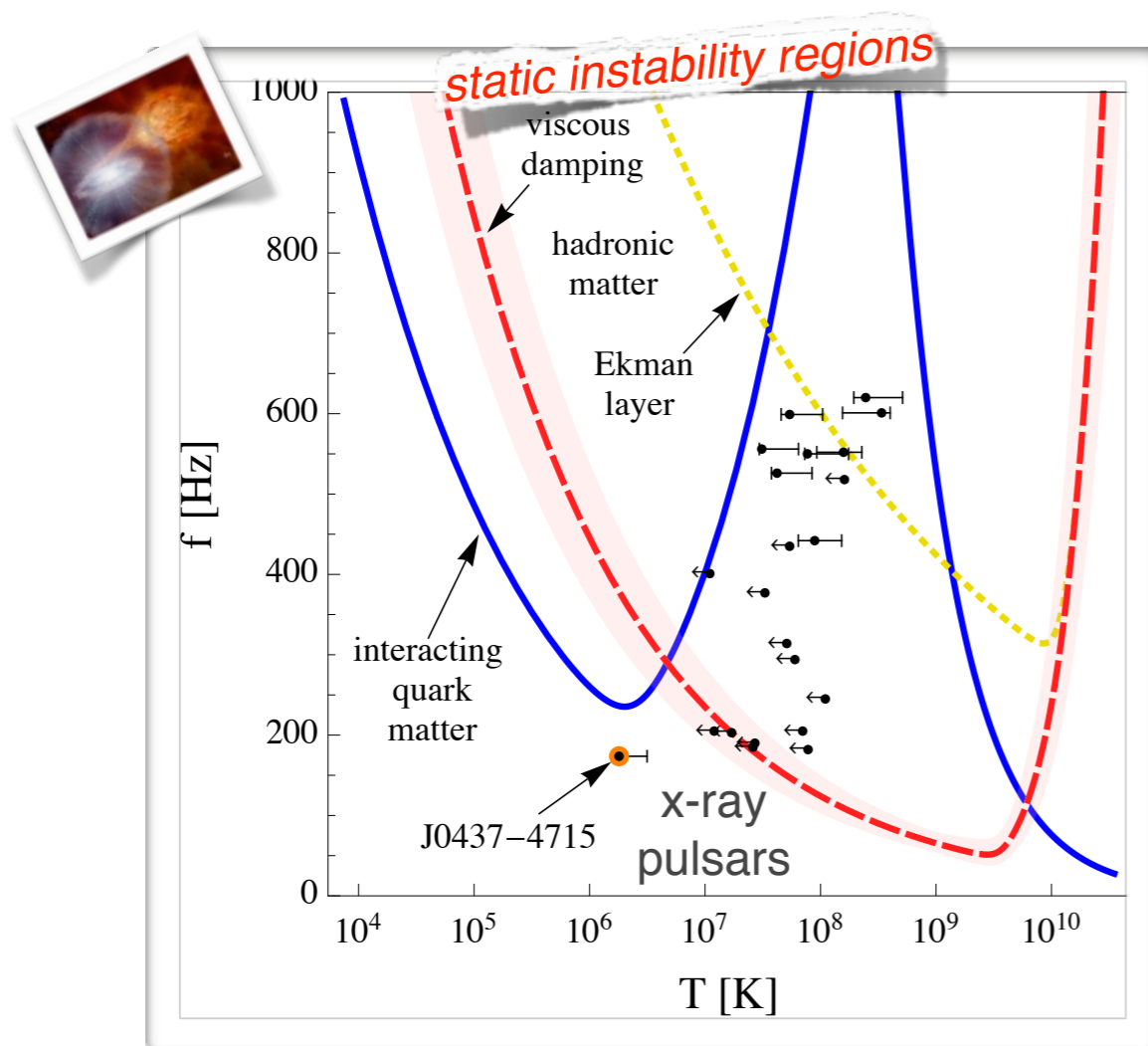
- Semi-analytic results** for the entire r-mode evolution ...

e.g. final frequency for a neutron star:

$$f_f^{(NS)} \approx 61.4 \text{ Hz} \frac{\tilde{S}_{\frac{3}{23}} \tilde{L}_{\frac{5}{184}}}{\tilde{J}_{\frac{29}{92}} \alpha_{\text{sat}}^{\frac{5}{92}}} \left( \frac{1.4 M_{\odot}}{M} \right)^{\frac{29}{92}} \left( \frac{11.5 \text{ km}}{R} \right)^{\frac{87}{184}}$$

Extremely insensitive to microscopic details ... but not to the form of dense matter!

# R-mode instability regions vs. thermal x-ray & radio timing data



M. Alford & K. S., PRL 113 (2014) 251102 & NPA 931 (2014) 740

Instability boundaries in temperature & timing space:

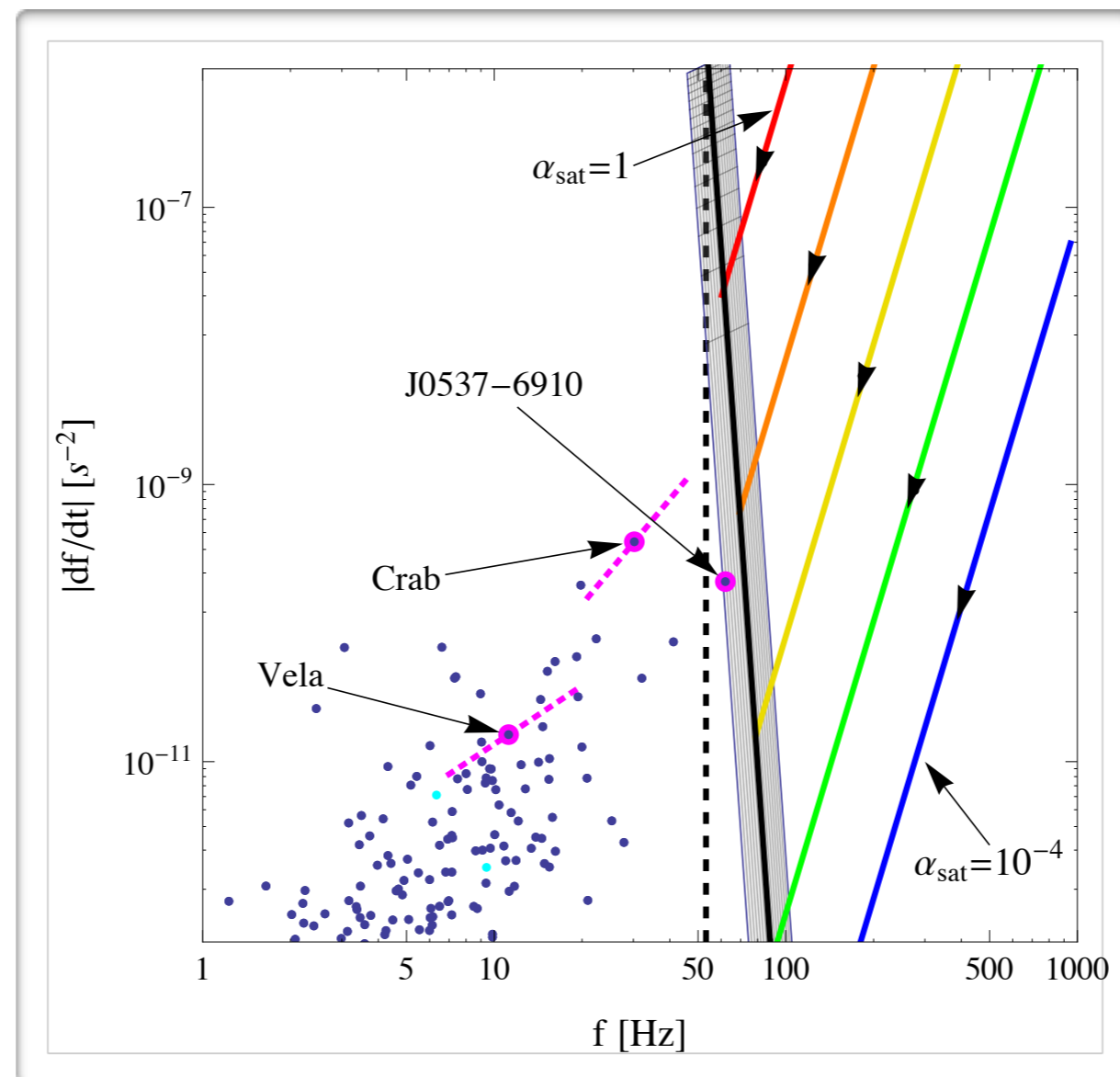
$$\Omega_{ib}(\dot{\Omega}) = \left( \hat{D}^\theta I^\delta |\dot{\Omega}|^\delta / \left( 3^\delta \hat{G}^\theta \hat{L}^\delta \right) \right)^{1/((8-\psi)\theta-\delta)}$$

*independent of saturation physics!*

Standard neutron matter cannot damp r-modes in these sources!

# Quantitative explanation of low pulsar frequencies

- r-mode emission can *quantitatively* explain the low rotation frequencies of young pulsars (which already spin too slow to emit GWs),
  - ➔ Even younger sources are promising GW targets!





# Temperature bounds on ms-pulsars

- r-modes strongly heat a source
  - ◆ temperature bounds impose r-mode amplitude bounds

S. Mahmoodifar and T. Strohmayer, APJ 773 (2013) 140;

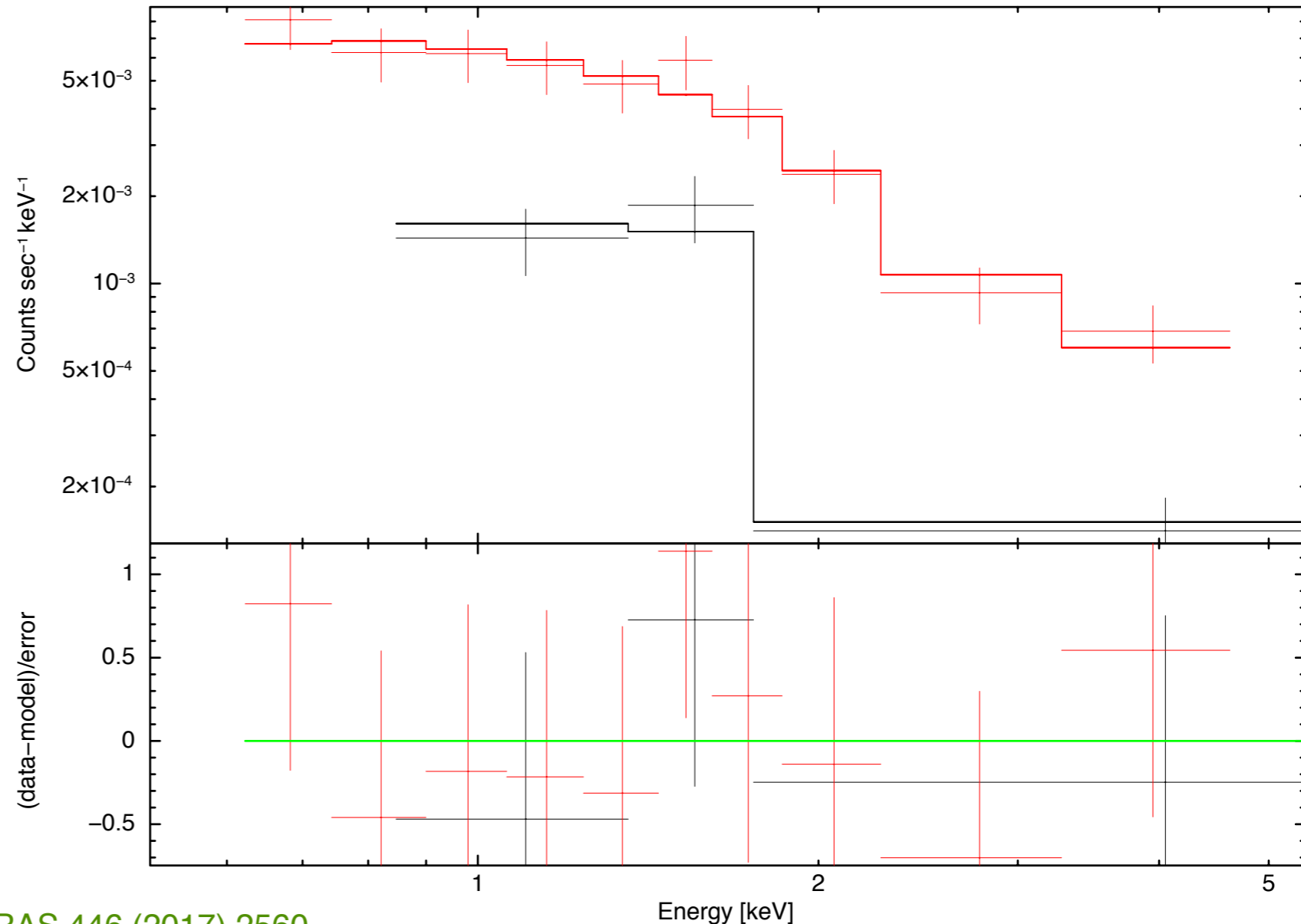
K. S., T. Boztepe, T. Güver, E. Vurgun, MNRAS 446 (2017) 2560  
S. Bhattacharya, C. Heinke, A. Chugunov;  
P. Freire, A. Ridolfi, S. Bogdanov, arXiv:1709.01807

- Although most millisecond pulsars are too faint to measure their temperature, X-ray luminosity measurements impose upper bounds on the temperature ...

- New dedicated XMM-Newton observation of J1810+1744 ( $f=602\text{Hz}$ )

- Spectral fit does not require surface comp. (hotspot + power law)

- Bound from checking at which temperature, a surface component would invalidate the fit



K. S., T. Boztepe, T. Güver, E. Vurgun, MNRAS 446 (2017) 2560

T. Boztepe, T. Güver & K. S. in preparation

# r-mode amplitude bounds

- Temperature bounds impose tight bounds on the r-mode amplitude

$$\alpha_{\text{sat}} \leq \sqrt{\frac{375}{2^{25} \pi^6 (3 - 2\chi) \chi^5 G \tilde{J} M R^2} \left(1 - \frac{2GM}{R}\right)^{-1} \frac{T_\infty^2}{f^4}}$$

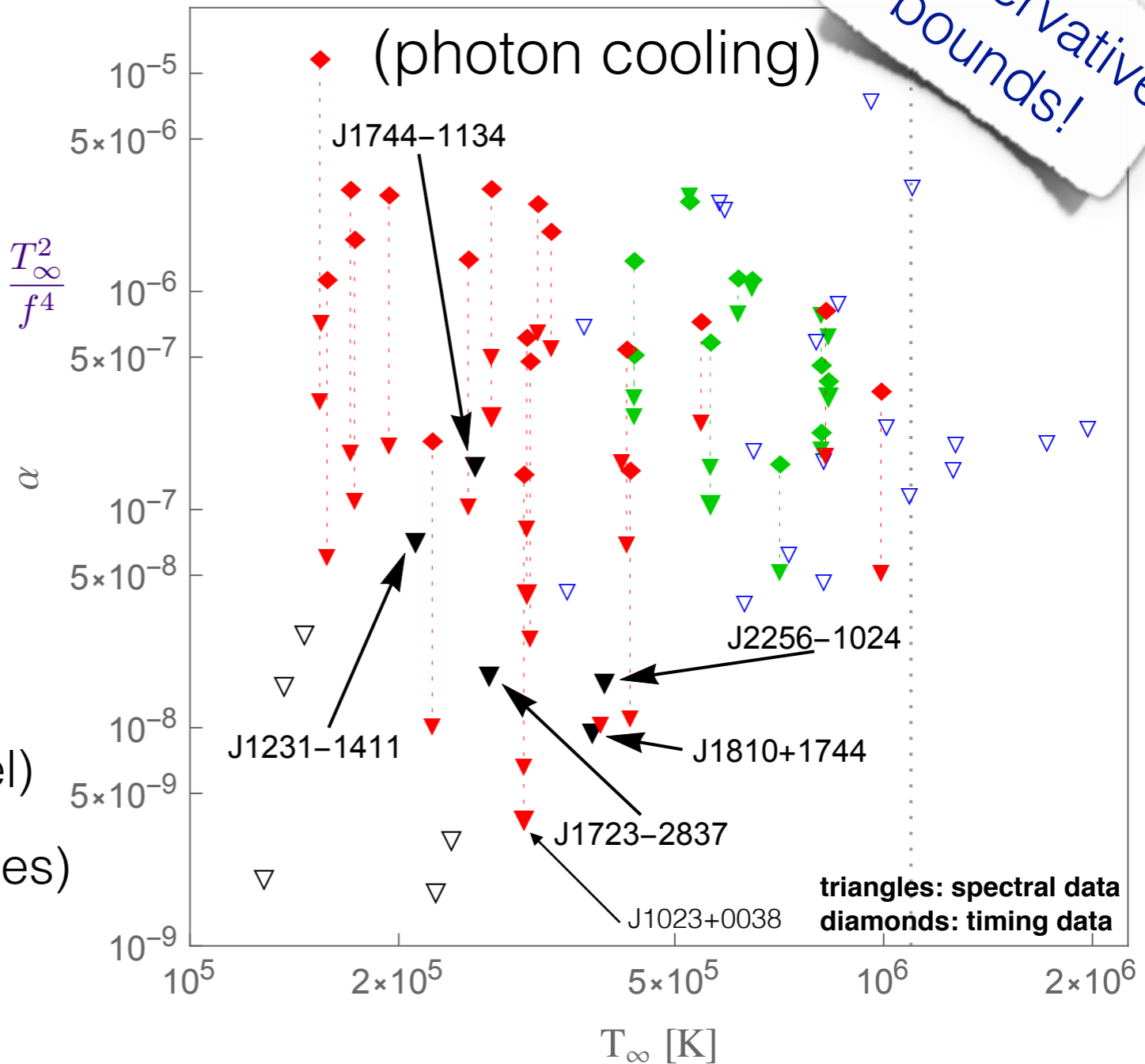
T. Boztepe, T. Güver & K. S. in preparation

- New bound on J1810+1744 (f = 602 Hz), sets the lowest bound, yet:

$$\alpha_{\text{sat}} \lesssim 2 \times 10^{-9} \quad (\text{standard NS model})$$

$$\alpha_{\text{sat}} \lesssim 10^{-8} \quad (\text{including uncertainties})$$

- Close to completely ruling out r-modes in these sources!



K. S., T. Boztepe, T. Güver, E. Vurgun, MNRAS 446 (2017) 2560,  
T. Boztepe, T. Güver & K.S., in preparation

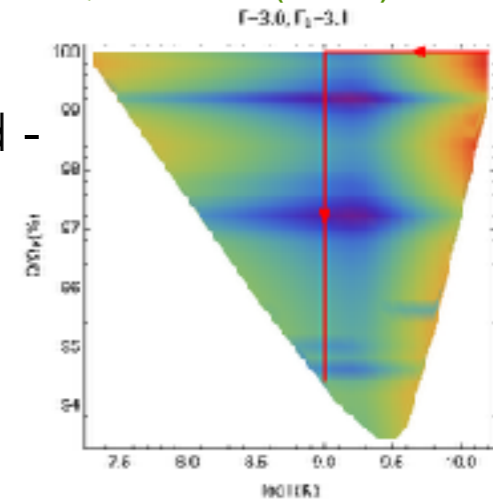
r-modes have a strong impact on the thermal evolution, even when they are irrelevant for the spindown!

$$\alpha_{\text{sat}} < 1.4 \times 10^{-9} \left(\frac{T_\infty}{10^5 \text{ K}}\right)^2 \left(\frac{500 \text{ Hz}}{f}\right)^4$$

# Standard damping mechanisms

What could saturate r-modes at such low amplitudes  $\alpha \lesssim 10^{-9} - 10^{-8}$  ?

- ~~Ekman damping~~  $\rightarrow$  “pasta”
  - L. Bildsten, G. Ushomirsky, APJ 529 (2000) 33,
  - L. Lindblom, B. Owen, G. Ushomirsky, PRD 62 (2000) 084030
- ~~Non-linear hydro~~  $\alpha_{\text{sat}} = O(1)$ 
  - L. Lindblom, et. al., PRL 86 (2001) 1152,
  - W. Kastaun, Phys.Rev. D84 (2011) 124036
- ~~Non-linear viscosity~~  $\alpha_{\text{sat}} = O(1)$ 
  - M. Alford, S. Mahmoodifar and K.S., PRD 85 (2012) 044051
- ~~Mode coupling~~  $\alpha_{\text{sat}} > 10^{-6}$  (1. parametric instability threshold - best estimate!)
  - P. Arras, et. al., Astrophys. J. 591 (2003) 1129,
  - R. Bondarescu, et. al., Astrophys. J. 778 (2013) 9
  - ▶ complicated since there are many modes ...
- Magnetic fields generated by ~~Differential rotation~~ (f-mode)
  - L. Rezzolla, F. Lamb, S. Shapiro, APJ 531 (1999) 139; A. Chugunov, J. Friedman, L. Lindblom, L. Rezzolla, arXiv:1712.09224
  - ▶ not relevant since the mechanism is weaker than estimated
- ~~Mutual friction~~ B. Haskell, N. Andersson, A. Passamonti, MNRAS 397 (2009) 1464



P. Pnigouras,  
K. Kokkotas,  
1607.03059

$\rightarrow$  All “standard mechanisms”, that are independent of the composition and could be present in minimal neutron stars, face big challenges!

# This is getting interesting ...

There are several composition-dependent mechanisms in more interesting forms of matter (random selection):

- Completely **ungapped quark matter** (non-Fermi liquid interactions)
  - spindown along a stability window (dynamic saturation)

N. Andersson, I. Jones, K. D. Kokkotas, MNRAS 337 (2002) 1224,  
M. Alford & K. S., PRL 113 (2014) 251102 & NPA 931 (2014) 740

- **Hyperonic matter**

L. Lindblom, B. Owen, PRD 65 (2002) 063006

- **Resonance coupling** in superfluids

M. Gusakov, A. Chugunov, E. Kantor, PRL 112 (2014) 151101

- **Vortex / fluxtube cutting?**  $\alpha_{\text{sat}} \approx 10^{-7} - 10^{-6}$

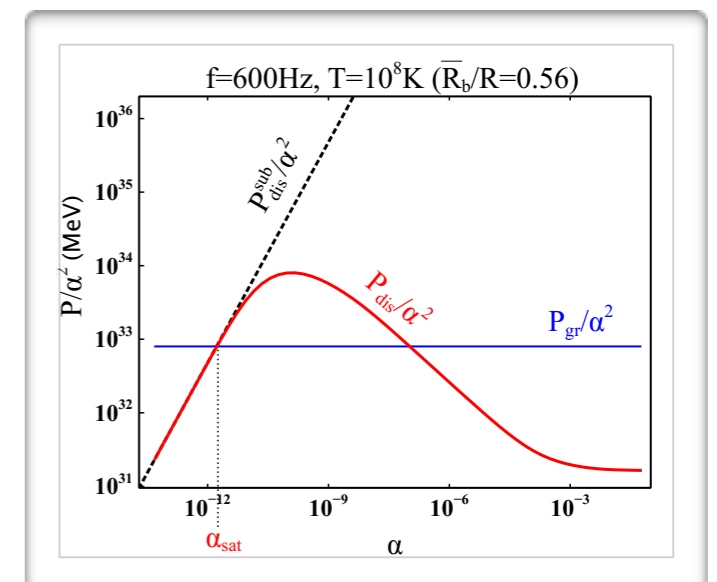
B. Haskell, K. Glampedakis, N. Andersson, MNRAS 441 (2014) 1662

- **Phase conversion** in hybrid stars

M. Alford, S. Han & K. S., PRC 91 (2015) 055804

★ Strongest saturation mechanism  $\alpha_{\text{sat}} < 10^{-10}$

- Pasta phases?? ... or something we haven't even thought about ...



# aLIGO search for continuous waves

- First aLIGO all-sky search for continuous gravitational waves: O1 data (2015)
  - (semi-coherent) all-band: 10-2000 Hz
    - very promising for r-modes
  - ➔ NO signal detected!
- Search not specifically tailored towards r-mode gravitational waves, but should be applicable ...
  - un-targeted search (frequencies unknown)
  - linear spindown model (braking index enters only at quadratic order)
  - wide range of spindown rates:

$$-10^{-8} \text{ Hz/s} \leq \dot{\nu} \leq +10^{-9} \text{ Hz/s}$$



# Gravitational strain of young sources

- r-mode evolution has three stages
  - ▶ mode growth
  - ▶ early stage (frequency constant)
  - ▶ late time stage (independent of initial conditions)

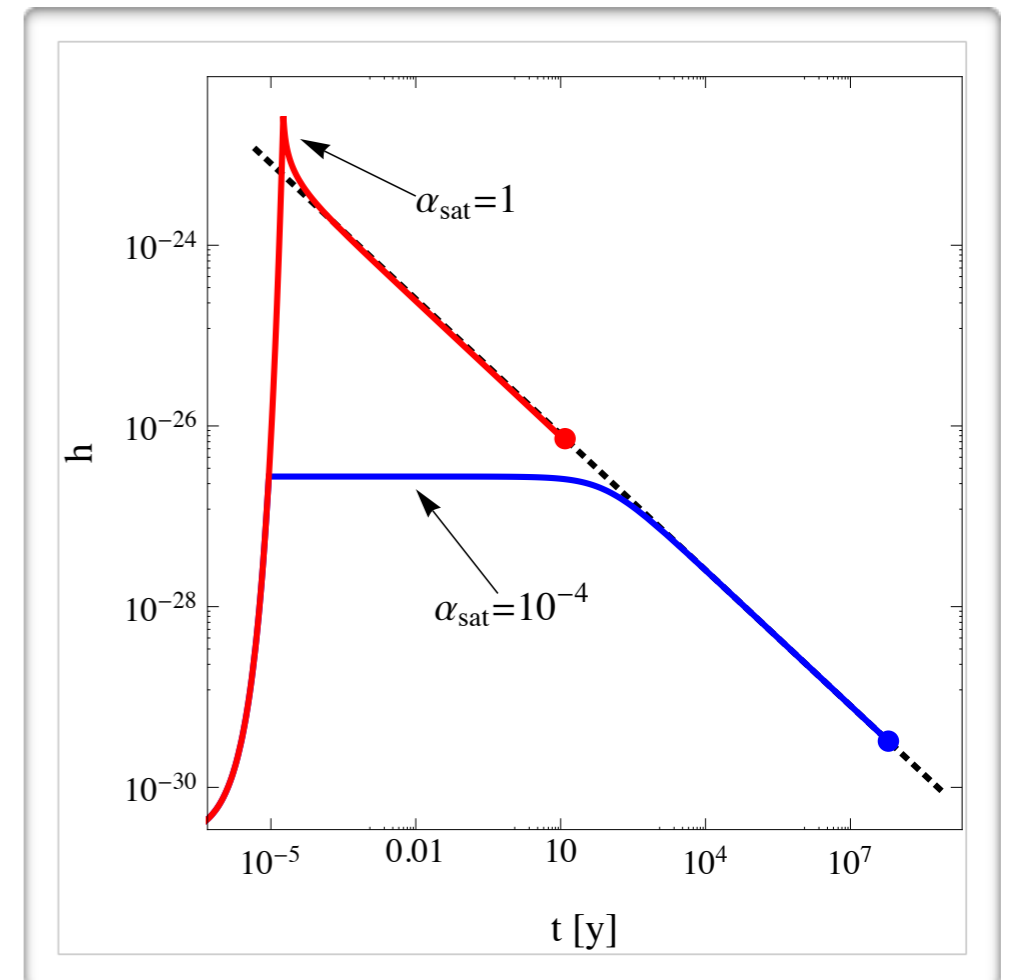
- Intrinsic strain in the late-time stage:

B. Owen, PRD 82 (2010) 104002

$$h_0 \xrightarrow{\Omega \ll \Omega_i} \sqrt{\frac{5CGI}{8\chi D^2 t}}$$

saturation mechanism  
 $c \equiv \frac{1 - 2\beta/\theta}{1 + \gamma/3 + 2\beta/(3\theta)}$   
( $\alpha_{\text{sat}} = \hat{\alpha} T^\beta \Omega^\gamma, L = \hat{L} T^\theta$ )  
M. Alford & K. S., Astrophys. J. 781 (2014) 26

K. S. in preparation  
r-mode spectrum  $\omega = -4/3\chi\Omega$



- Allows to take into account the uncertainties in the analysis, which is important to abstract information from gravitational wave data

# GW emission from young, nearby sources

- A handful of “recent” historic SN remnants are known in our local group LIGO Col., arXiv:1412.5942

- ▶ Cas A (~335 years, Milky way)

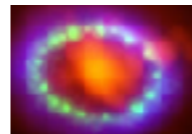
LIGO Col., APJ 722 (2010) 1504



- ▶ G1.9+0.3 (~145 years, Milky way)



- ▶ SN 1987A (Large Mag. Cloud)



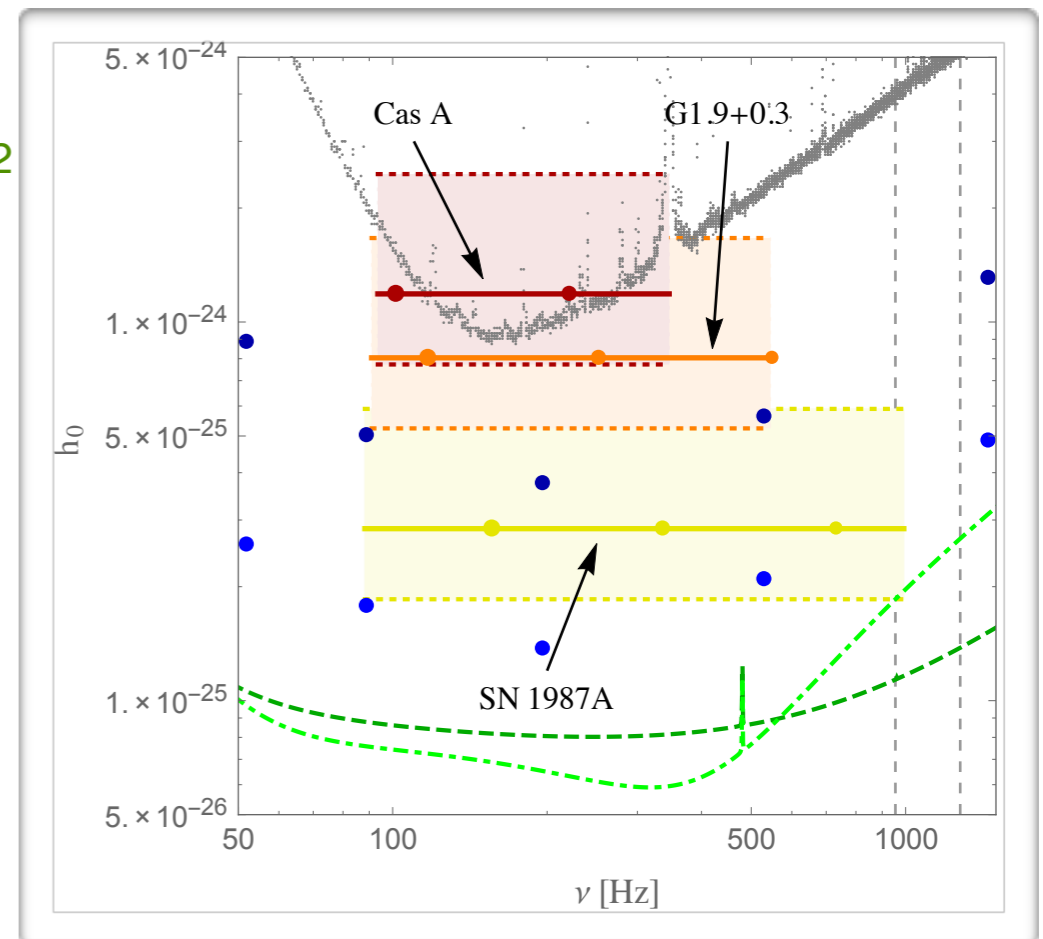
- Including uncertainties Cas A & G1.9+0.3 should have been above the background!

★ No sizable r-modes in these sources

- dissipation could either be strong, so that  $\alpha \lesssim 10^{-3}$

- or the amplitude is large,  $\alpha^{(\text{Cas A})} \gtrsim 0.1$  and  $\alpha^{(\text{G1.9+0.3})} \gtrsim 0.2$ , so that the r-mode spindown phase is already over

- Should exclude r-mode amplitudes  $10^{-3} \lesssim \alpha \lesssim 0.1$ , if these sources were born quickly rotating



K. S. in preparation

**work in progress**

So far we are at the beginning ...





... but it could be only a matter of sensitivity

