

# Three-particle Force from Lattice Simulations

Fernando Romero-López

In collaboration with: A. Rusetsky & C. Urbach  
*in preparation...*

University of Valencia, IFIC

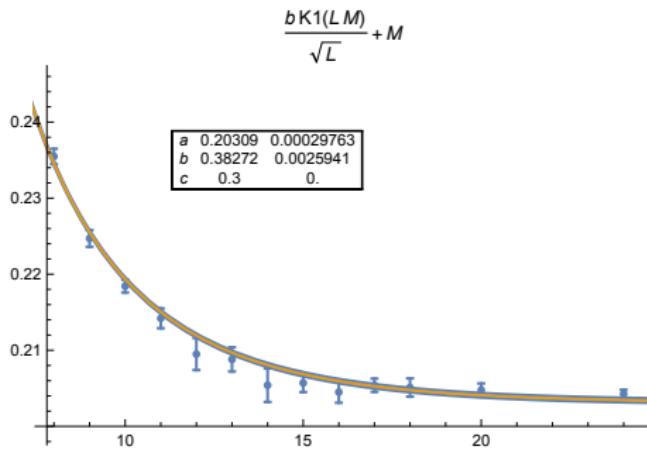
*[fernando.romero@ific.uv.es](mailto:fernando.romero@ific.uv.es)*

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# One-Particle Energy

Complex  $\varphi^4$  Theory:

$$S = \sum_x \left( -\kappa \sum_{\mu} (\varphi_x^* \varphi_{x+\mu} + c.c.) - \lambda(|\varphi_x|^2 - 1)^2 + |\varphi_x|^2 \right)$$



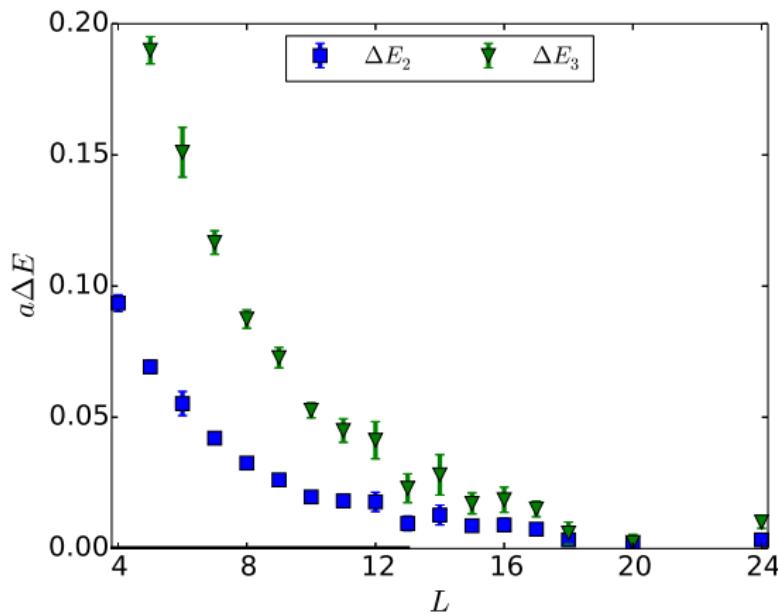
- $\chi^2/dof = 12.5/15$
- $aM = 0.20309(30)$
- Precise determination of  $M(L)$

# Two and Three-Particle Energies

→ Use volume-dependent mass:  $\Delta E_{2(3)} = E_{2(3)} - 2(3)M(L)$

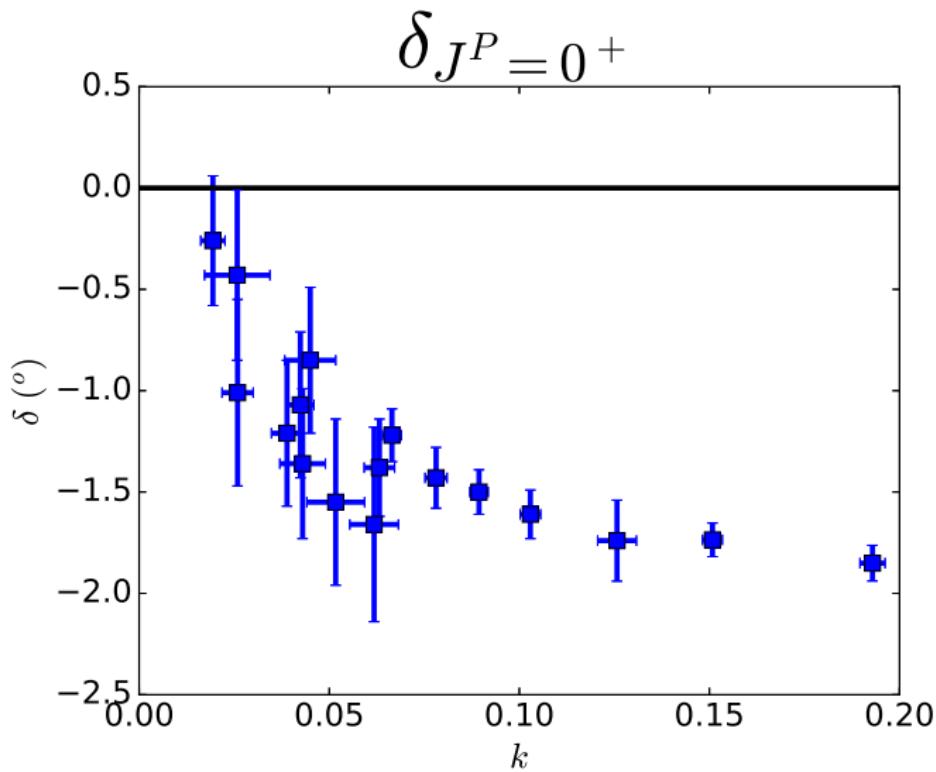
**Exponential terms further suppressed by  $L^2$ .**

(See A. Rusetsky's talk)



## Phase Shift: Checking Perturbability

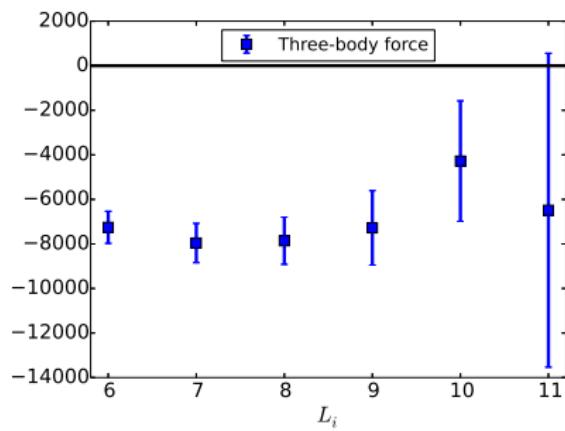
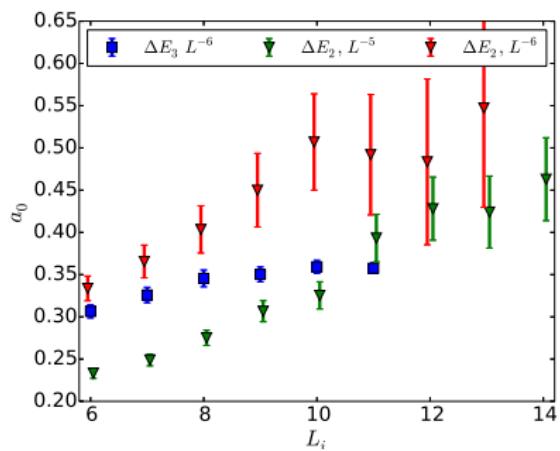
$$\rightarrow \text{Lüscher Method: } \cot \delta_0 = \frac{Z_{00}(1, q^2)}{\pi^{3/2} q}$$



# Three-Particle Force (Preliminary)

→ Fit  $\Delta E_{2/3}$  to order  $L^{-6}$

Obtain scattering length ( $a_0$ ) and three-body force  $\Delta E_3 \supset -\frac{c}{L^6}$



# Conclusion

- One needs small volumes to increase sensitivity, where  $ML \sim 2$ .
- Use volume-dependent mass,  $M(L)$ , for a better suppression of exponential terms.
- Three-body Force seems to be present and measurable.
- Still some fit instability → fitting strategy?