Experimental motivations for studying few-hadron systems on the lattice

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Multi-Hadron Systems from Lattice QCD INT, Seattle, February 5th, 2018

Outline

- **Introduction**
- The light sector: the 3π system
	- \bullet \rightarrow \rightarrow \rightarrow \rightarrow \rightarrow \rightarrow
	- The $a_1(1260)$
	- The hybrid π_1
	- The $a_1(1420)$
- The heavy sector: XYZ
	- The $X(3872)$ and the Y states
	- Two-body subchannels: Z_c s and Z_b s
	- Complicated Dalitz plots

Experiment vs. Lattice QCD

- Higher and higher statistics $\sqrt{\mathbf{x}}$
- Lots of multiparticles decay channels available \checkmark
- Scattering information entangled to production mechanisms \boldsymbol{x}
- Experiments happen at the physical point only x
	- Orthogonal systematics \checkmark
	- Scattering information separated from production; unaccessible channels
	- Although QCD is rigid, one can vary the input parameters (quark masses, N_c and n_f) and study the effect on amplitudes \checkmark

Experiment vs. Lattice QCD

Intermediate step through a 2-body isobar (partial wave truncation)

Experiment vs. Lattice QCD

Intermediate step through a 2-body isobar (partial wave truncation)

Light spectrum (1-particle correlators)

The $a_1(1260)$

Despite it has been known since forever, the resonance parameters of the a_1 (1260) are poorly determined The production (and model) dependence is affecting their extraction

The $a_1(1260)$

$a_1(1260)$ WIDTH

INSPIRE search

The extraction of the resonance in the τ decay should be the cleanest, but the determination of the pole is still unstable **→ See A. Jackura's talk tomorrow**

(Lattice simulations with stable ρ , Lang, Leskovec, Mohler, Prelovsek, JHEP 1404, 162)

$\pi p \rightarrow 3\pi p$ diffractive production

Deck amplitude

This production mechanism allows for a nonresonant contribution (Deck effect) Because of the light mass of the pion, the singularity is close to the physical region and generates a peaking background

$\pi_1(1600) \rightarrow \rho \pi \rightarrow \pi \pi \pi$

The strength of the Deck effect depends on the momentum transferred t , but the precise estimates rely on the model for the Deck amplitude

A strong signal is also observed in $\eta^{(\prime)}\pi$, consistent with the naive expectation for a hybrid meson

Having the $3\pi \rightarrow 3\pi$ scattering data from Lattice will allow for a coupled channel analysis unaffected by the Deck effect

$a_1(1420) \to f_0(980) \pi \to \pi \pi \pi$

COMPASS claimed the observation of another a_1 at a slightly higher mass

- Narrower than the $a_1(1260)$
- Unexpected in quark model or lattice spectra
- Only seen in $f_0(980)\pi$

$a_1(1420) \to f_0(980)\pi \to \pi\pi\pi$

It has been proposed that the peak is due to a triangle singularity i.e. a dynamical enhancement generated by rescattering

Mikhasenko, Ketzer, Sarantsev, PRD91, 094015

Triangle **Breit-Wigner**

If that is the case, the strength of the signal would dramatically depend on the mass of the exchanges: studying the amplitude at different pion/kaon masses will confirm whether this is true

The heavy sector: XYZ states

Esposito, AP, Polosa, Phys.Rept. 668

(3872)

- Discovered in $B \to K X \to K J/\psi \pi \pi$
- Quantum numbers 1^{++}
- Very close to DD^* threshold
- Too narrow for an abovetreshold charmonium
- **Isospin violation too big** $\Gamma(X \rightarrow J/\psi \omega)$ $\Gamma(X \rightarrow J/\psi \rho)$ $~ 0.8 \pm 0.3$
- **Mass prediction not** compatible with $\chi_{c1}(2P)$

 $M = 3871.68 \pm 0.17$ MeV $M_X - M_{DD^*} = -3 \pm 192 \text{ keV}$ $Γ < 1.2$ MeV @90%

(3872)

Large prompt production at hadron colliders $\sigma_B/\sigma_{TOT} = (26.3 \pm 2.3 \pm 1.6)\%$

 $\sigma_{PR} \times B(X \rightarrow J/\psi \pi \pi)$ $=$ (1.06 \pm 0.11 \pm 0.15) nb

CMS, JHEP 1304, 154

$X(3872)$ on the lattice

Prelovsek, Leskovec, PRL111, 192001

Three body dynamics $D\overline{D}\pi$ may play a role. Playing with lighter charm mass? • A full amplitude analysis is missing, and is now mandatory

Vector Y states

(4260)

BESIII, PRL118, 092002 (2017)

BESII

New BESIII data show a peculiar lineshape for the $Y(4260)$, and suggest a state narrower and lighter than in the past

The state is mature for a coupled channel analysis (on the lattice?)

 $^+e^- \rightarrow h_c \pi \pi$

- Fit curve: Total

Fit curve: Y(4220)

Fit curve: Y(4390)

+ BESIII: R-scan data sample

 \bullet BESIII: XYZ data sample

 250

 $200F$

150

100

50

 -50

Dressed Cross section (pb)

Charged Z states: $Z_c(3900)$, $Z'_c(4020)$

In the Dalitz plot projections, two states appear slightly above $D^{(*)}D^{*}$ thresholds

$$
e^{+}e^{-} \rightarrow Z_{c}(3900)^{+}\pi^{-} \rightarrow J/\psi \pi^{+}\pi^{-} \text{ and } \rightarrow (DD^{*})^{+}\pi^{-}
$$

\n
$$
M = 3888.7 \pm 3.4 \text{ MeV}, \Gamma = 35 \pm 7 \text{ MeV}
$$

\n
$$
e^{+}e^{-} \rightarrow Z_{c}'(4020)^{+}\pi^{-} \rightarrow h_{c} \pi^{+}\pi^{-} \text{ and } \rightarrow \overline{D}^{*0}D^{*+}\pi^{-}
$$

\n
$$
M = 4023.9 \pm 2.4 \text{ MeV}, \Gamma = 10 \pm 6 \text{ MeV}
$$

Charged Z states: $Z_b(10610)$, $Z'_b(10650)$

Z_c s on the lattice

- \blacktriangleright The number of energy levels we find is equal to the number of expected non-interacting meson-mesons.
- Finite-volume spectrum lies close to non-interacting meson-meson levels suggesting there are weak meson-meson interactions.
- \blacktriangleright There is no strong indication for a bound state or narrow resonance in this channel. $Z_C(3900)$?
- Tetraquark operators do not have a significant effect on calculating the spectrum.

No calculations have found evidence for a resonance Prelovsek, Leskovec, PLB727, 172-176 HALQCD, PRL117, 242001 HadSpec, JHEP 1711, 033

Amplitude analysis for $Z_c(3900)$

One can test different parametrizations of the amplitude, which correspond to different singularities \rightarrow different natures AP *et al.* (JPAC), PLB772, 200

$$
f_i(s, t, u) = 16\pi \sum_{l=0}^{L_{\text{max}}} (2l+1) \left(a_{l,i}^{(s)}(s) P_l(z_s) + a_{l,i}^{(t)}(t) P_l(z_t) + a_{l,i}^{(u)}(u) P_l(z_u) \right) \quad \text{Khuri-Treiman}
$$
\n
$$
f_{0,i}(s) = \frac{1}{32\pi} \int_{-1}^{1} dz_s f_i(s, t(s, z_s), u(s, z_s)) = a_{0,i}^{(s)} + \frac{1}{32\pi} \int_{-1}^{1} dz_s \left(a_{0,i}^{(t)}(t) + a_{0,i}^{(u)}(u) \right) \equiv a_{0,i}^{(s)} + b_{0,i}(s)
$$
\n
$$
f_{l,i}(s) = \frac{1}{32\pi} \int_{-1}^{1} dz_s P_l(z_s) \left(a_{0,i}^{(t)}(t) + a_{0,i}^{(u)}(u) \right) \equiv b_{l,i}(s) \quad \text{for } l > 0. \quad f_{0,i}(s) = b_{0,i}(s) + \sum_j t_{ij}(s) \frac{1}{\pi} \int_{s_j}^{\infty} ds' \frac{\rho_j(s')b_{0,j}(s')}{s'-s},
$$
\n
$$
f_i(s, t, u) = 16\pi \left[a_{0,i}^{(t)}(t) + a_{0,i}^{(u)}(u) + \sum_j t_{ij}(s) \left(c_j + \frac{s}{\pi} \int_{s_j}^{\infty} ds' \frac{\rho_j(s')b_{0,j}(s')}{s'(s'-s)} \right) \right],
$$

Fit: III

Fit: III+tr.

Fit: IV+tr.

Fit: tr.

Fit summary

Data can hardly distinguish these scenarios.

Lattice QCD can actually provide the scattering matrix as an input to this analysis

More complicated Dalitz plots

BESIII, PRD96, 032004

In the reaction $e^+e^- \rightarrow \psi^{\prime}\pi^+\pi^-$, the situation looks even more obscure

Data refused to be fitted with any simple model

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More complicated Dalitz plots

Outlook

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Lattice can disentangle the scattering from the production mechanism Three body dynamics AND coupled channels

Lattice can provide the $2 \rightarrow 2$ scattering amplitude that can be used as input in the phenomenological models

BACKUP

Pole extraction

Pentaquarks!

LHCb, PRL 115, 072001 LHCb, PRL 117, 082003

Two states seen in $\Lambda_b \to (J/\psi p) K^-$, evidence in $\Lambda_b \to (J/\psi p) \pi^ M_1 = 4380 \pm 8 \pm 29$ MeV $Γ_1 = 205 ± 18 ± 86$ MeV $M_2 = 4449.8 \pm 1.7 \pm 2.5$ MeV $\Gamma_2 = 39 \pm 5 \pm 19$ MeV

Quantum numbers $J^P =$ 3 2 − , 5 2 + or 3 2 + , 5 2 − or 5 2 + , 3 2 − Opposite parities needed for the

interference to correctly describe angular distributions, low mass region contaminated by Λ^* (model dependence?)

No obvious threshold nearby

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Other beasts

One/two peaks seen in $B \to XK \to J/\psi \phi K$, close to threshold

 $X(3915)$, seen in $B \to X K \to J/\psi \omega$ and $\gamma \gamma \rightarrow X \rightarrow J/\psi \omega$ $J^{PC} = 0^{++}$, candidate for $\chi_{c0}(2P)$ But $X(3915) \nrightarrow D\overline{D}$ as expected, and the hyperfine splitting $M(2^{++}) - M(0^{++})$ too small

P_c photoproduction

To exclude any rescattering mechanism, we propose to search the $P_c(4450)$ state in photoproduction.

$$
\langle \lambda_{\psi} \lambda_{p'} | T_r | \lambda_{\gamma} \lambda_p \rangle = \frac{\langle \lambda_{\psi} \lambda_{p'} | T_{\text{dec}} | \lambda_R \rangle}{M_r^2 - W^2} \frac{\langle \lambda_R | T_{\text{em}}^\dagger | \lambda_{\gamma} \lambda_p \rangle}{\text{in} \Gamma_r M_r}
$$

Hadronic part

- 3 independent helicity couplings,
	- \rightarrow approx. equal, $g_{\lambda_{\psi},\lambda_{p'}} \sim g$
- g extracted from total width and (unknown) branching ratio

Vector meson dominance relates the radiative width to the hadronic width

$$
\Gamma_{\gamma} = 4\pi\alpha \,\Gamma_{\psi p} \left(\frac{f_{\psi}}{M_{\psi}}\right)^2 \left(\frac{\bar{p}_i}{\bar{p}_f}\right)^{2\ell+1} \times \frac{4}{6}
$$

Hiller Blin, AP *et al.* (JPAC), PRD94, 034002

Dictionary – Quark model

 $L =$ orbital angular momentum

 \overline{q}

 $\overline{\overline{q}}$

 $I =$ total angular momentum = exp. measured spin

 $I =$ isospin = 0 for quarkonia

 $L-S\leq J\leq L+S$ $P = (-1)^{L+1}, C = (-1)^{L+S}$ $G = (-1)^{L+S+I}$

But
$$
J/\psi = \psi(1S), \ \psi' = \psi(2S)
$$

Charged Z states: $Z(4430)$ Candidates / (0.2 GeV^2)
 $\frac{8}{5}$ Candidates / (0.02 GeV^2)
10
10
1 $\frac{22}{m_{\psi^\prime\pi^{\scriptscriptstyle -}}^2\,[\text{GeV}^2]}$ 18 20 $\frac{2}{m_{K^+\pi^-}^2}$ [GeV²] 16 1.5 0.5 **LHCD**
NHC $Z(4430)^+ \rightarrow \psi(2S) \pi^+$ $\mathbf{E}^{0.2}$ $I^G J^{PC} = 1^+ 1^{+-}$ If the amplitude is a free complex number, in each $\frac{2}{10}$ / $\frac{\pi}{7}$ $M = 4475 \pm 7^{+15}_{-25}$ MeV bin of $m_{\psi^{\prime}\pi^+}^2$ -0.2 $\Gamma = 172 \pm 13^{+37}_{-34}$ MeV the resonant behaviour -0.4 appears as well Far from open charm thresholds -0.6

 $\frac{0.2}{\text{Re }A^Z}$

 -0.2

 θ

 -0.4

$Y(4260) \to DD_1?$

e⁺e⁻ \to Y(4260) $\to \pi$ ⁻ \bar{D}^0D^{*+}

Flavored $X(5568)$

- A flavored state seen in $B_s^0 \pi$ invariant mass by D0 (both $B_s^0 \rightarrow J/\psi \phi$ and \rightarrow $D_s \mu \nu$),
- not confermed by LHCb or CMS
- (different kinematics? Compare differential distributions)

Controversy to be solved

S-Matrix principles

$$
A(s,t) = \sum_{l} A_{l}(s) P_{l}(z_{s})
$$

Analyticity

$$
A_{l}(s) = \lim_{\epsilon \to 0} A_{l}(s + i\epsilon)
$$

$$
s\text{-plane}
$$
\n
$$
A_l(s + i\epsilon) \neq A_l(s - i\epsilon)
$$
\n
$$
A_l(s + i\epsilon) \neq A_l(s - i\epsilon)
$$
\nUnitarity

These are constraints the amplitudes have to satisfy, but do not fix the dynamics

Resonances (QCD states) are poles in the unphysical Riemann sheets

Bound states on the real axis 1st sheet Not-so-bound (virtual) states on the real axis 2nd sheet

Example: The charged $Z_c(3900)$

A charged charmonium-like resonance has been claimed by BESIII in 2013.

 $e^+e^- \to Z_c(3900)^+\pi^- \to J/\psi \pi^+\pi^-$ and $\to (DD^*)^+\pi^ M = 3888.7 \pm 3.4$ MeV, $\Gamma = 35 \pm 7$ MeV 5.8 5 $M^2(D^*\pi^+)$ 4.8 4.6 15 15.5 16 16.5 $M^2(D^0D^*)$

Such a state would require a minimal 4q content and would be manifestly exotic

$$
f_i(s, t, u) = 16\pi \sum_{l=0}^{L_{\text{max}}} (2l+1) \left(a_{l,i}^{(s)}(s) P_l(z_s) + a_{l,i}^{(t)}(t) P_l(z_t) + a_{l,i}^{(u)}(u) P_l(z_u) \right) \quad \text{Khuri-Treiman}
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\n
$$
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$$
\n
$$
f_i(s, t, u) = 16\pi \left[a_{0,i}^{(t)}(t) + a_{0,i}^{(u)}(u) + \sum_j t_{ij}(s) \left(c_j + \frac{s}{\pi} \int_{s_j}^{\infty} ds' \frac{\rho_j(s')b_{0,j}(s')}{s'(s'-s)} \right) \right],
$$

Triangle singularity

Logarithmic branch points due to exchanges in the cross channels can simulate a resonant behavior, only in very special kinematical conditions (Coleman and Norton, Nuovo Cim. 38, 438), However, this effects cancels in Dalitz projections, no peaks (Schmid, Phys.Rev. 154, 1363)

$$
f_{0,i}(s) = b_{0,i}(s) + \frac{t_{ij}}{\pi} \int_{s_i}^{\infty} ds' \frac{\rho_j(s')b_{0,j}(s')}{s'-s}
$$

...but the cancellation can be spread in different channels, you might still see peaks in other channels only!

Szczepaniak, PLB747, 410-416 Szczepaniak, PLB757, 61-64 Guo, Meissner, Wang, Yang PRD92, 071502

Testing scenarios

We approximate all the particles to be scalar $-$ this affects the value of couplings, which are not normalized anyway – but not the position of singularities. This also limits the number of free parameters

$$
f_i(s,t,u) = 16\pi \left[a_{0,i}^{(t)}(t) + a_{0,i}^{(u)}(u) + \sum_j t_{ij}(s) \left(c_j + \frac{s}{\pi} \int_{s_j}^{\infty} ds' \frac{\rho_j(s')b_{0,j}(s')}{s'(s'-s)} \right) \right],
$$

The scattering matrix is parametrized as $(t^{-1})_{ij} = K_{ij} - i \rho_i \, \delta_{ij}$ Four different scenarios considered:

- «III»: the K matrix is $\frac{g_i g_j}{M^2-S}$, this generates a pole in the closest unphysical sheet the rescattering integral is set to zero
- «III+tr.»: same, but with the correct value of the rescattering integral
- «IV+tr.»: the K matrix is constant, this generates a pole in the IV sheet
- «tr.»: same, but the pole is pushed far away by adding a penalty in the χ^2

Singularities and lineshapes

Different lineshapes according to different singularities

Guerrieri, AP, Piccinini, Polosa, IJMPA 30, 1530002

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 $\bar{B}^0 \to K^-(\pi^+ J\!/\psi)$

 1^{+-}

 $Z(4200)^+$

 $Belle^{62}(7.2)$