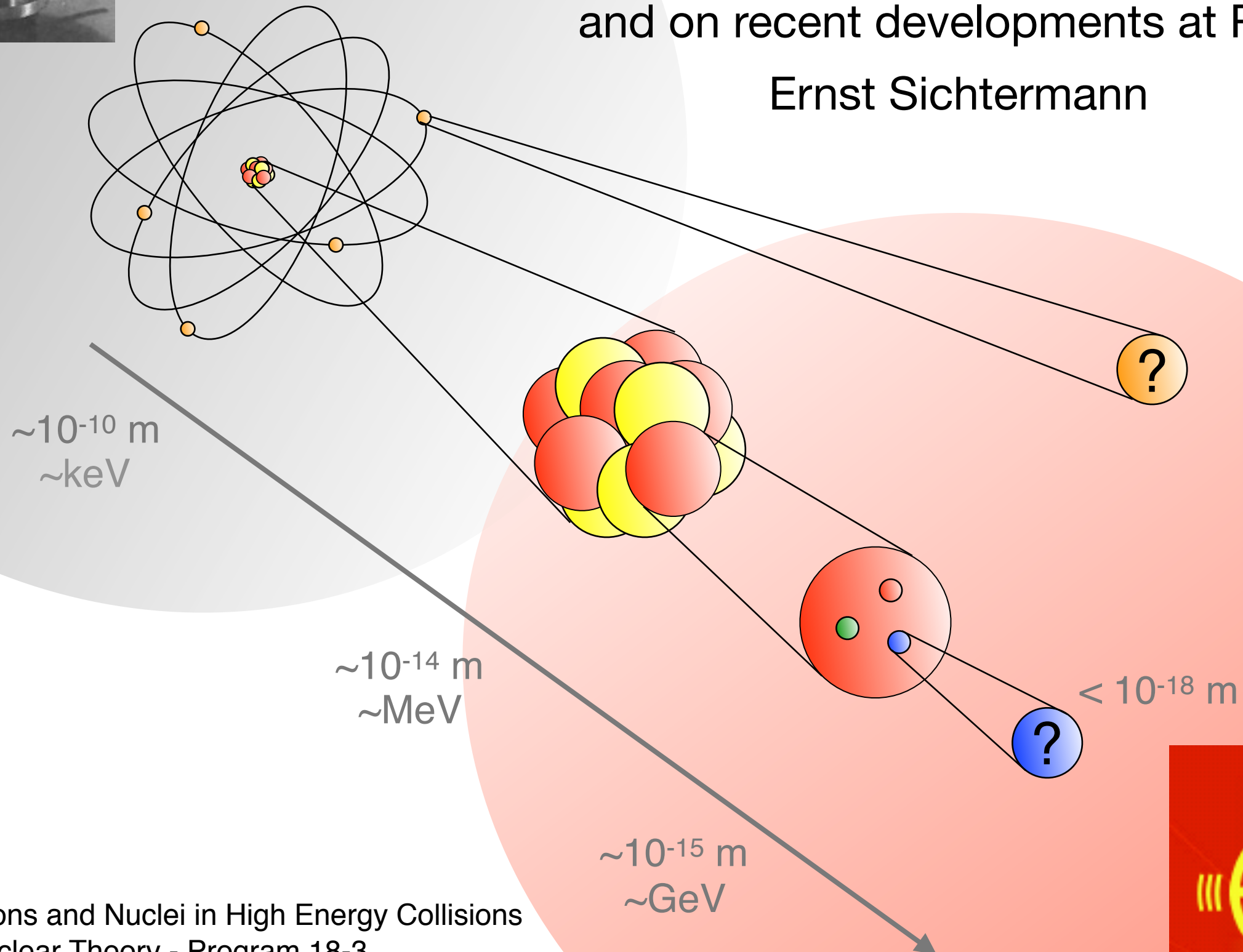


A few comments on the spin decomposition, and on recent developments at RHIC

Ernst Sichteremann



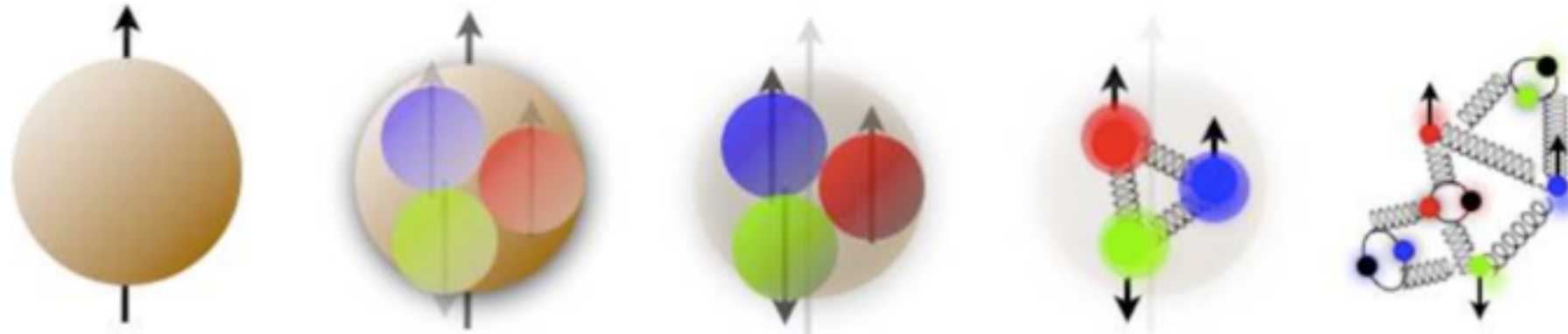
What *is* a proton, neutron, nucleus anyway?

mass →	$\approx 2.3 \text{ MeV}/c^2$	$\approx 1.275 \text{ GeV}/c^2$	$\approx 173.07 \text{ GeV}/c^2$	0	$\approx 126 \text{ GeV}/c^2$
charge →	$2/3$	$2/3$	$2/3$	0	0
spin →	$1/2$	$1/2$	$1/2$	1	0
	u up	c charm	t top	g gluon	H Higgs boson
QUARKS	$\approx 4.8 \text{ MeV}/c^2$	$\approx 95 \text{ MeV}/c^2$	$\approx 4.18 \text{ GeV}/c^2$	0	
	$-1/3$	$-1/3$	$-1/3$	0	
	$1/2$	$1/2$	$1/2$	1	
	d down	s strange	b bottom	γ photon	
	$0.511 \text{ MeV}/c^2$	$105.7 \text{ MeV}/c^2$	$1.777 \text{ GeV}/c^2$	$91.2 \text{ GeV}/c^2$	
	-1	-1	-1	0	
	$1/2$	$1/2$	$1/2$	1	
	e electron	μ muon	τ tau	Z Z boson	
LEPTONS	$< 2.2 \text{ eV}/c^2$	$< 0.17 \text{ MeV}/c^2$	$< 15.5 \text{ MeV}/c^2$	$80.4 \text{ GeV}/c^2$	
	0	0	0	± 1	
	$1/2$	$1/2$	$1/2$	1	
	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	W W boson	
				GAUGE BOSONS	

The proton is 2 up quarks and 1 down quark, ...

Really? “Just open many textbooks...”

What *is* a proton, neutron, nucleus?



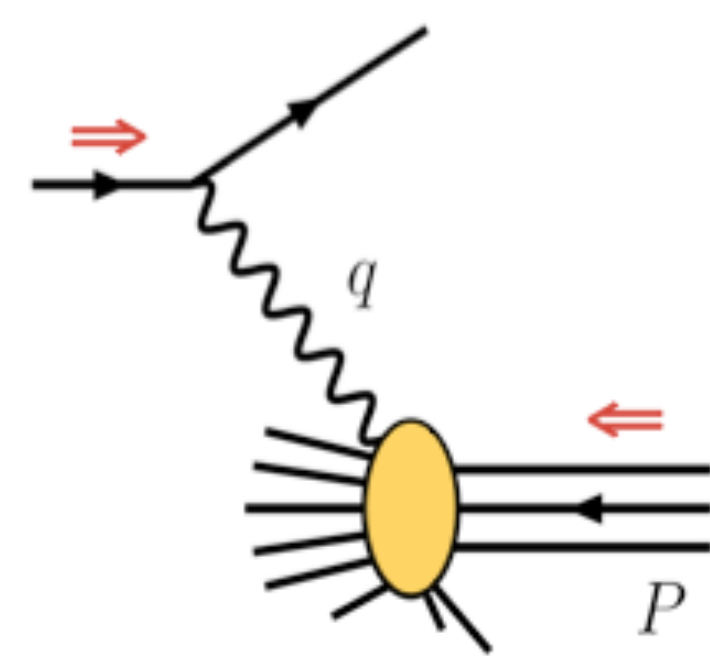
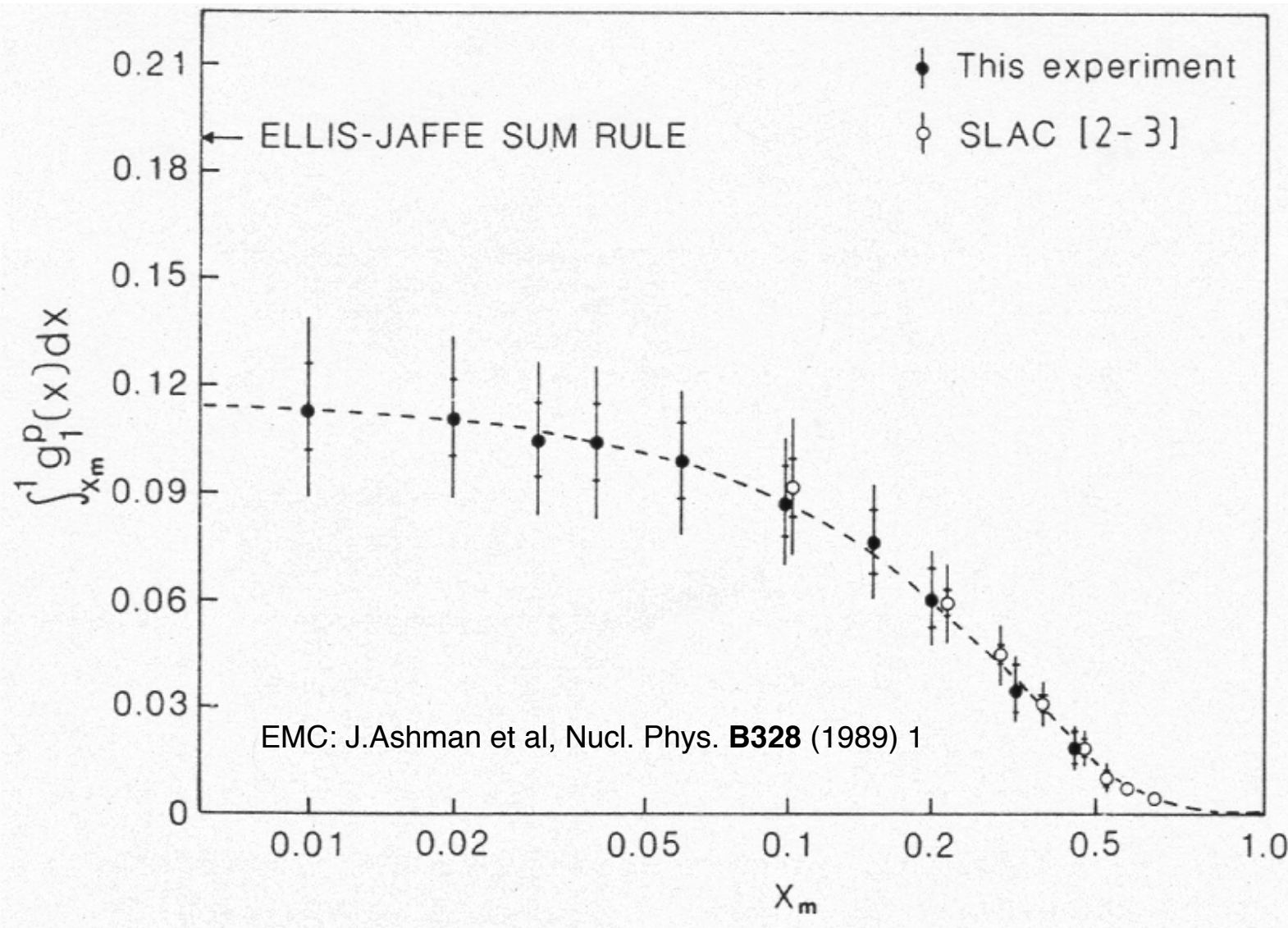
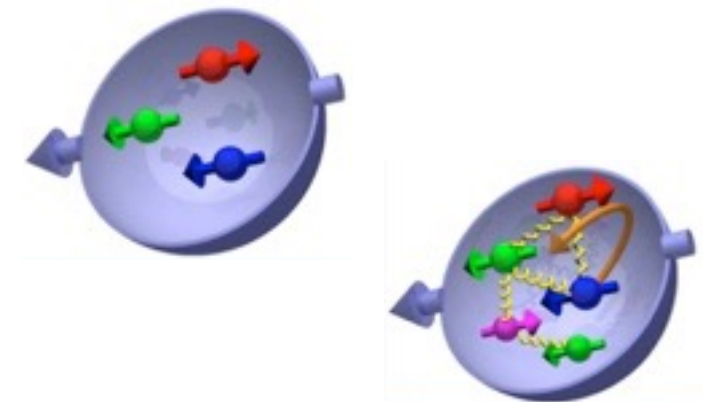
A high-energy view: an unseparated, broadband beam of quarks, anti-quarks, and gauge bosons (primarily gluons), and perhaps other constituents, yet unknown.

*40 years of an amazingly robust idealization:
Renormalization group-improved Parton Model*

*Factorization theorem(s) + one-dimensional parton distributions,
no correlations among the partons*

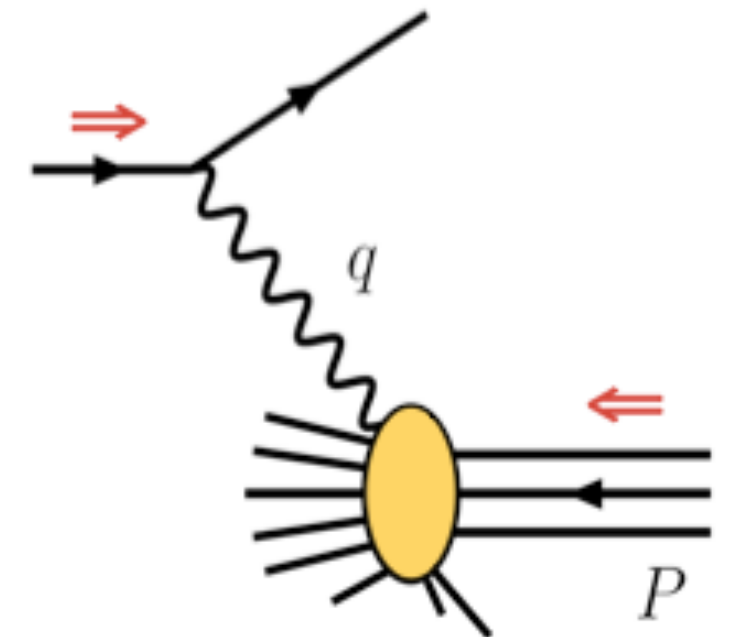
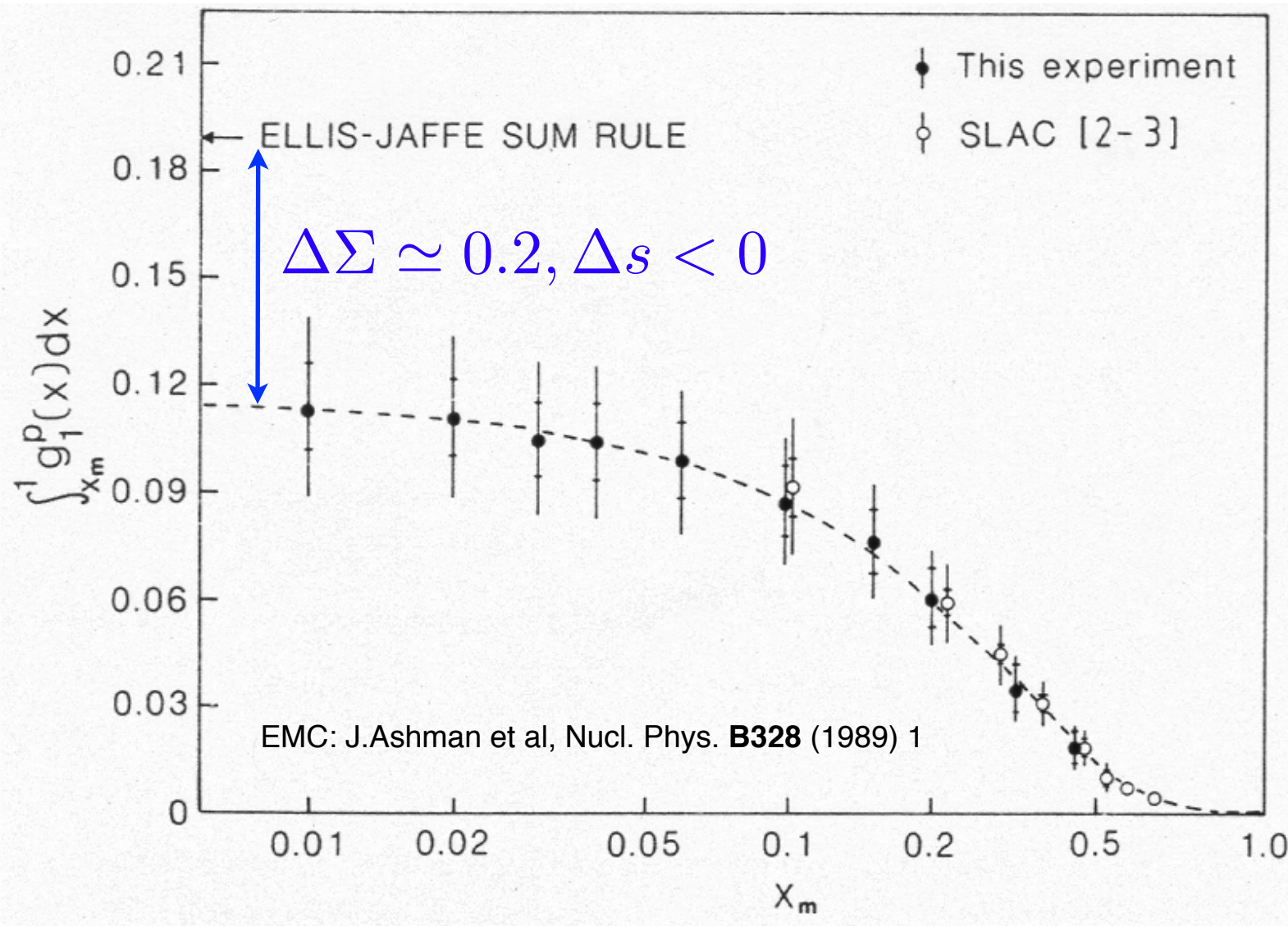
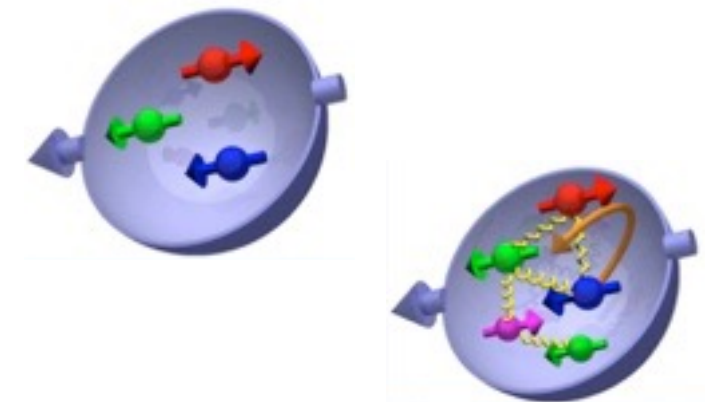
***Really? More than a few of our high-energy observations are actually different
Essential to separate intrinsic structure from interaction dynamics,
push the envelope beyond the theoretically established,
obtain meaningful accuracy.***

Really? - Proton spin



$$\sigma(\Rightarrow, \Leftarrow) - \sigma(\Rightarrow, \Rightarrow) \sim g_1(x, Q^2)$$

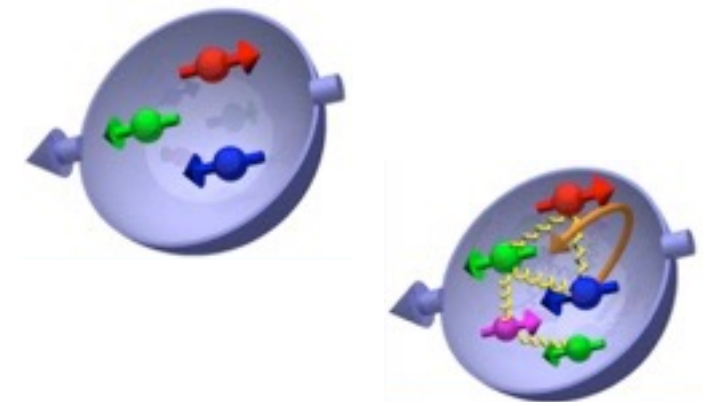
Really? - Proton spin



$$\sigma(\Rightarrow, \Leftarrow) - \sigma(\Rightarrow, \Rightarrow) \sim g_1(x, Q^2)$$

The sum of quark and anti-quark spins contribute little to the proton spin, and strange quarks are negatively polarized.

Really? - Proton spin



For the proton,

$$\Gamma_1 = \int_0^1 g_1(x) dx = \int_0^1 \left(\frac{1}{2} \sum e_q^2 \Delta q(x) \right) dx = \frac{1}{2} \left(\frac{4}{9} \Delta_1 u + \frac{1}{9} \Delta_1 d + \frac{1}{9} \Delta_1 s \right)$$

$$= \frac{1}{12} (\Delta_1 u - \Delta_1 d) + \frac{1}{36} (\Delta_1 u + \Delta_1 d - 2\Delta_1 s) + \frac{1}{9} (\Delta_1 u + \Delta_1 d + \Delta_1 s)$$

Known from weak neutron to proton decay

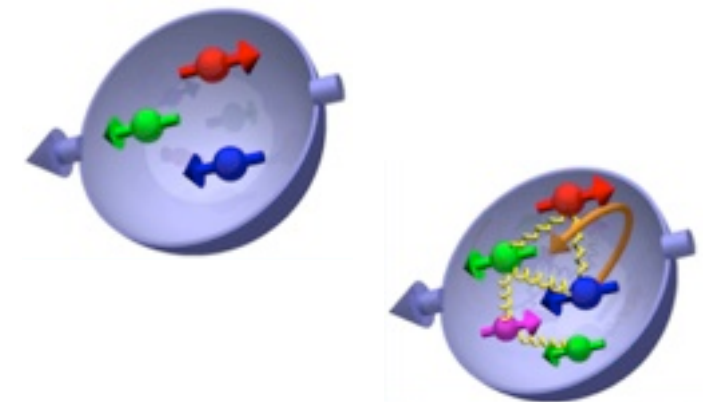
Known from weak neutron to proton decay,
combined with weak Σ to neutron decay

Unique to DIS, $\Delta\Sigma$

which becomes a prediction if $\Delta_1 s = 0$

No (reliable) substitute for energy; $x \propto 1/\sqrt{s}$


Really? - Proton spin




For the proton,

$$\Gamma_1 = \int_0^1 g_1(x) dx = \int_0^1 \left(\frac{1}{2} \sum e_q^2 \Delta q(x) \right) dx = \frac{1}{2} \left(\frac{4}{9} \Delta_1 u + \frac{1}{9} \Delta_1 d + \frac{1}{9} \Delta_1 s \right)$$

$$= \frac{1}{12} (\Delta_1 u - \Delta_1 d) + \frac{1}{36} \underbrace{(\Delta_1 u + \Delta_1 d - 2\Delta_1 s)}_{a_8 = 3F - D = 0.59 \pm 0.03} + \frac{1}{9} (\Delta_1 u + \Delta_1 d + \Delta_1 s)$$



 $< 10\%$



 Known from weak neutron to proton decay,
 combined with weak Σ to neutron decay

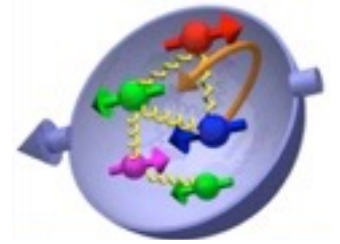
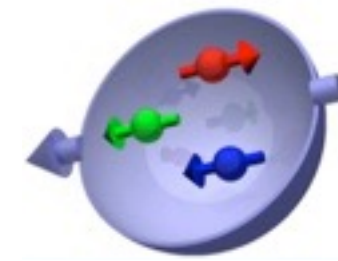


 Unique to DIS, $\Delta\Sigma$

Since,

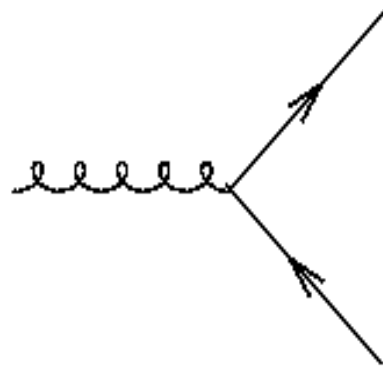
$$\left. \begin{array}{l} \frac{\partial \Gamma_1}{\partial a_8} \Big|_{\text{Ellis-Jaffe}} \simeq \frac{5}{36} \\ \frac{\partial \Gamma_1}{\partial a_8} \Big|_{\text{experiment}} \simeq 0 \end{array} \right\} \text{one can recover the E-J expectation with a} \\ \text{sizeable shift of } a_8 = 3F - D, \quad a_8 \simeq 0.2 \pm 0.1$$

Really? - Proton spin



Numerous follow-up questions and experiment programs,

Among the early attempts at a resolution,



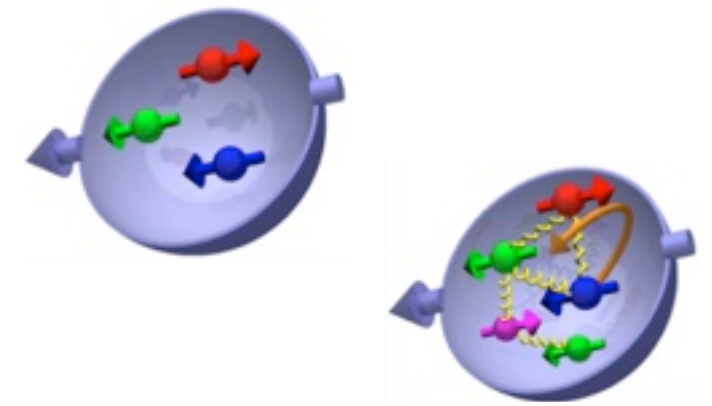
with the gluons *polarized*.

G. Altarelli and G.G. Ross Phys. Lett. **B212** (1998) 391

Note: this attempt requires *very* large polarization, *factors* larger than the nucleon spin itself, and by inference, *huge* compensating *orbital momenta*. Quite the proton, a ground-state object and all.

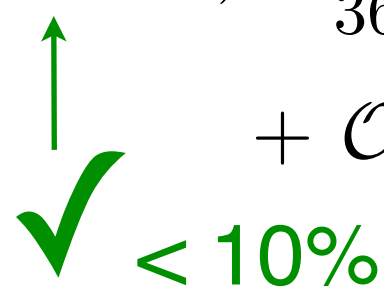
Other attempts include e.g extrapolation over unmeasured low-x.

DIS - Proton spin



For the proton,

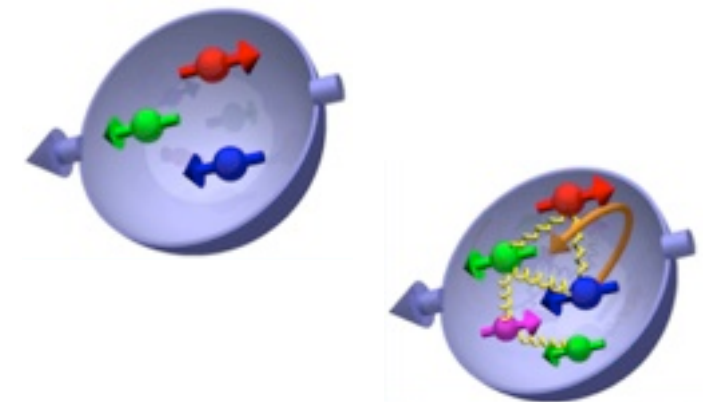
$$\begin{aligned}\Gamma_1 &= \int_0^1 g_1(x) dx = \int_0^1 \left(\frac{1}{2} \sum e_q^2 \Delta q(x) \right) dx = \frac{1}{2} \left(\frac{4}{9} \Delta_1 u + \frac{1}{9} \Delta_1 d + \frac{1}{9} \Delta_1 s \right) \\ &= \frac{1}{12} (\Delta_1 u - \Delta_1 d) + \frac{1}{36} (\Delta_1 u + \Delta_1 d - 2\Delta_1 s) + \frac{1}{9} (\Delta_1 u + \Delta_1 d + \Delta_1 s) \\ &\quad + \mathcal{O}(\alpha_s) \text{ now well known} + \mathcal{O}(1/Q^2)\end{aligned}$$



Similar can be done for the neutron,

experimentally via the deuteron or ^3He ,

DIS - Proton spin



For the proton,

$$\begin{aligned}\Gamma_1 &= \int_0^1 g_1(x) dx = \int_0^1 \left(\frac{1}{2} \sum e_q^2 \Delta q(x) \right) dx = \frac{1}{2} \left(\frac{4}{9} \Delta_1 u + \frac{1}{9} \Delta_1 d + \frac{1}{9} \Delta_1 s \right) \\ &= \frac{1}{12} (\Delta_1 u - \Delta_1 d) + \frac{1}{36} (\Delta_1 u + \Delta_1 d - 2\Delta_1 s) + \frac{1}{9} (\Delta_1 u + \Delta_1 d + \Delta_1 s) \\ &\quad + \mathcal{O}(\alpha_s) \text{ now well known} + \mathcal{O}(1/Q^2)\end{aligned}$$

↑
✓

Similar can be done for the neutron,

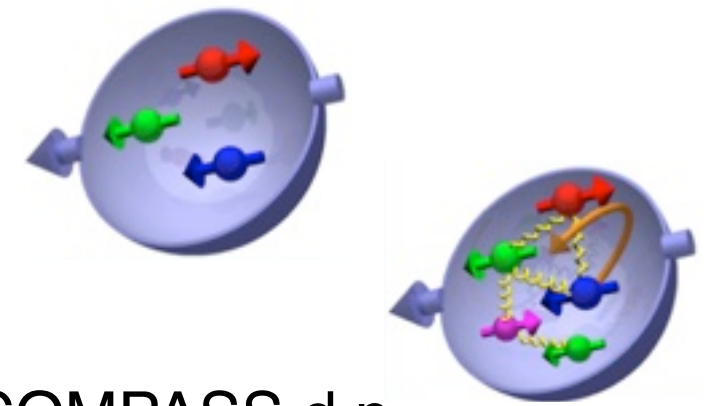
experimentally via the deuteron or ^3He ,

Note, experimental precisions can straightforwardly be matched as can the (low) energies in fixed-target experiments.

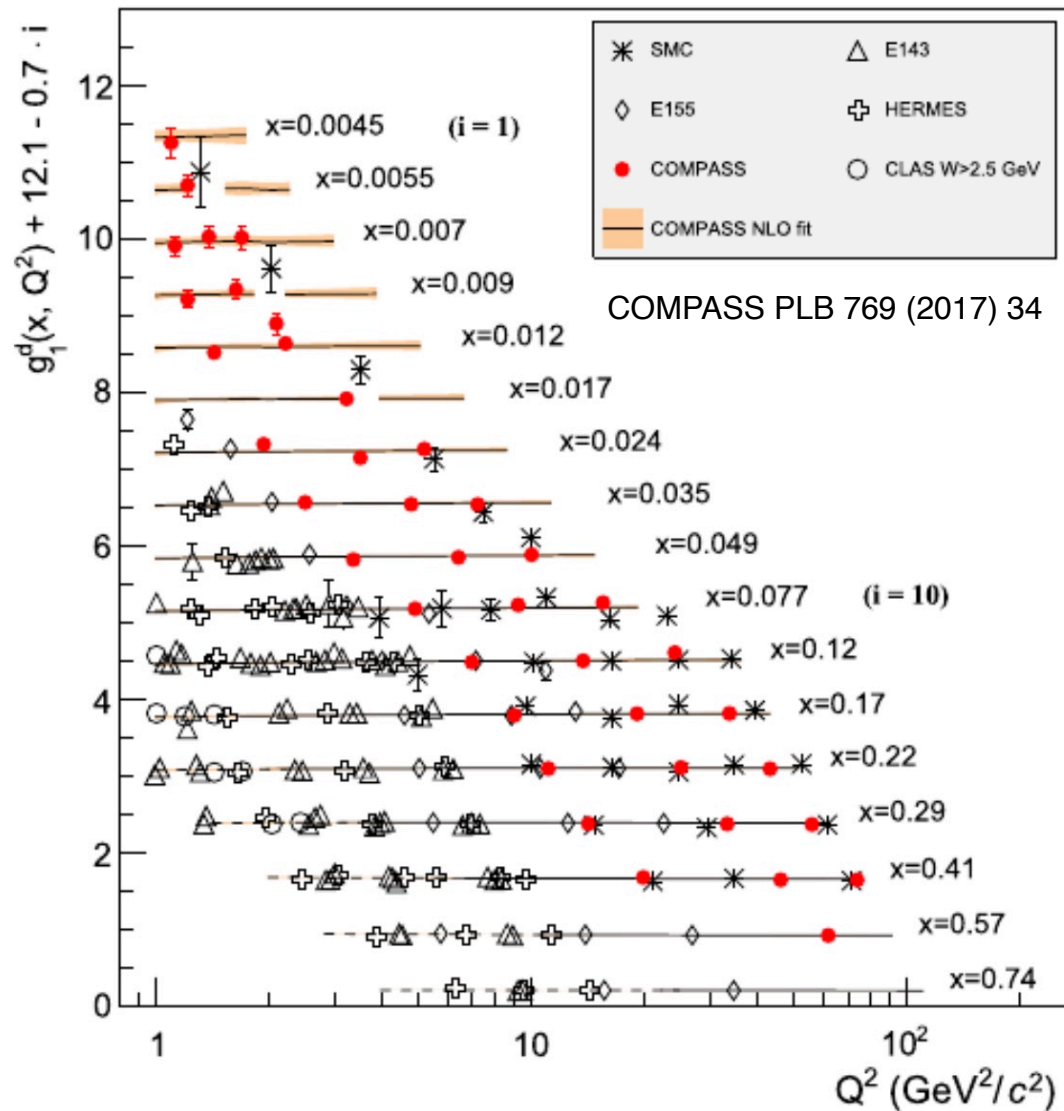
Not so at a collider and looking ahead to EIC we should revisit the handling of nuclear effects.



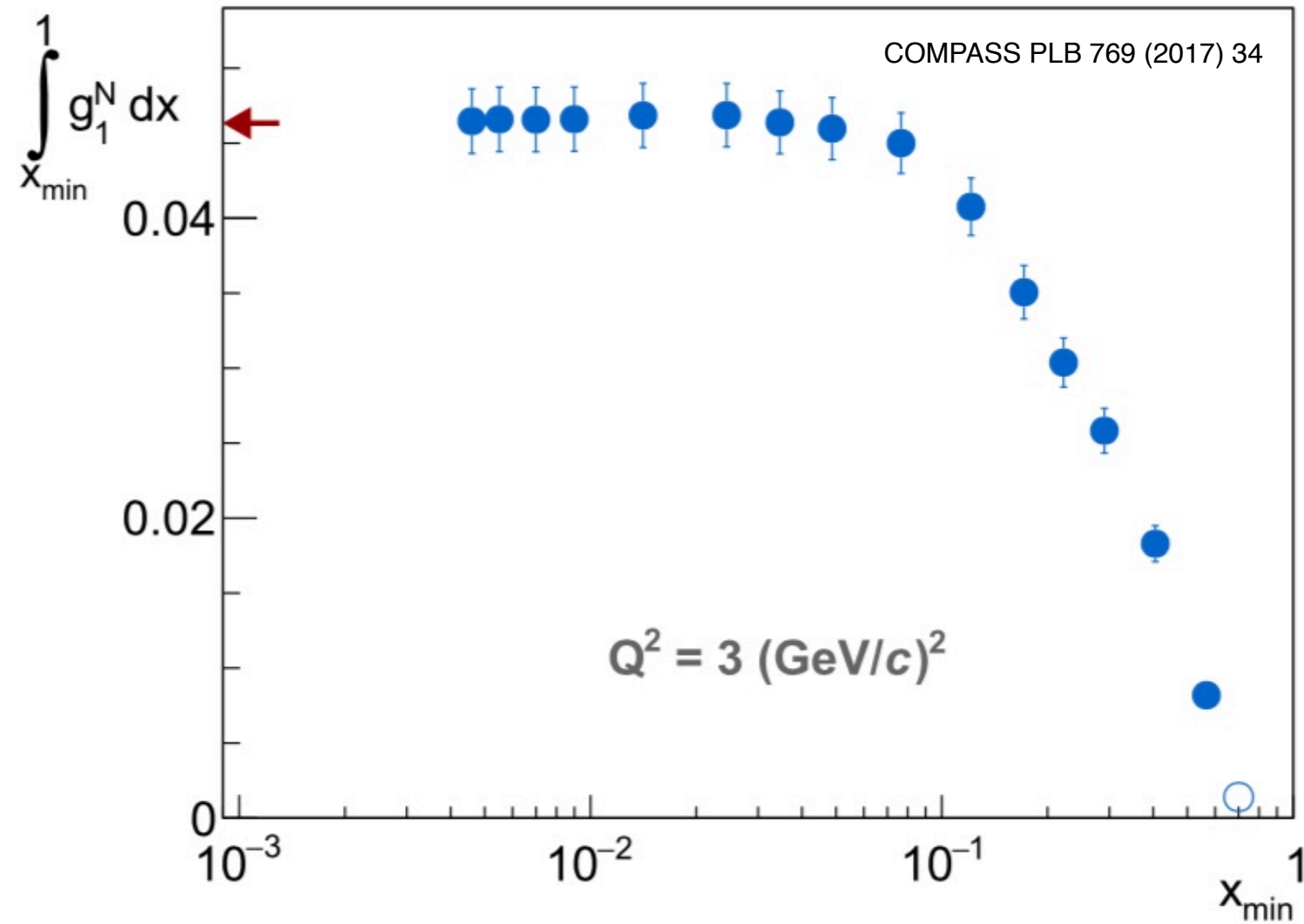
DIS - Neutron spin



World deuteron data, $+\mathcal{O}(\alpha_s)$



Neutron, from COMPASS d,p

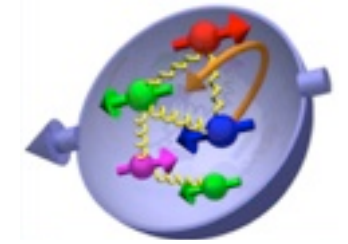
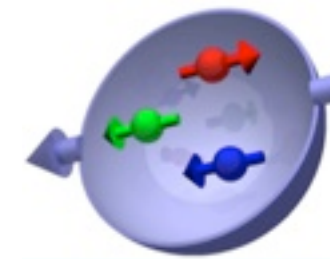


$$\Gamma_1^{NS} = 0.192 \pm 0.007_{\text{stat}} \pm 0.015_{\text{syst}}$$

$$|g_A/g_V| = 1.29 \pm 0.05_{\text{stat}} \pm 0.10_{\text{syst}}$$

✓ < 10%

DIS - spin decomposition



$$a_8 = \underbrace{\Delta_1 u + \Delta_1 d - 2\Delta_1 s}_{3F - D} = 0.59 \pm 0.03$$

Known from weak neutron to proton decay,
combined with weak Σ to neutron decay

Channel	$f_1^{SU(3)}$	$ f_1 V_{us} $	$(g_1/f_1)^{SU(3)}$	$(g_1/f_1)^{\text{exp}}$
→ $n \rightarrow p$	1	n/a	$F + D$	1.2670(30)
$\Lambda \rightarrow p$	$-\sqrt{3}/2$	0.2221(33)	$F + D/3$	0.718(15)
→ $\Sigma^- \rightarrow n$	-1	0.2274(49)	$F - D$	-0.340(17)
$\Xi^- \rightarrow \Lambda$	$\sqrt{3}/2$	0.2367(97)	$F - D/3$	0.25(5)
$\Xi^- \rightarrow \Sigma^0$	$\sqrt{1/2}$	n/a	$F + D$	n/a
$\Xi^0 \rightarrow \Sigma^+$	1	0.216(33)	$F + D$	1.32(22)

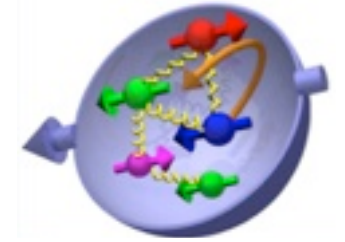
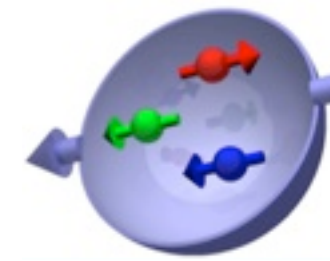
A 1+1-experiment determination, more or less, with little hope of materially better data,

SU(3) breaking often largely ignored so far,

Renewed opportunity for lattice-QCD?

$\Delta\Sigma$

DIS - spin decomposition



Channel	$f_1^{SU(3)}$	$ f_1 V_{us} $	$(g_1/f_1)^{SU(3)}$	$(g_1/f_1)^{\text{exp}}$
$n \rightarrow p$	1	n/a	$F + D$	1.2670(30)
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$\Xi^- \rightarrow \Sigma^0$	$\sqrt{1/2}$	n/a	$F + D$	n/a
$\Xi^0 \rightarrow \Sigma^+$	1	0.216(33)	$F + D$	1.32(22)



$$\longrightarrow a_0(Q^2 = 3 \text{ (GeV/c)}^2) = 0.32 \pm 0.02_{\text{stat}} \pm 0.04_{\text{syst}} \pm 0.05_{\text{evol}} .$$

COMPASS PLB 769 (2017) 34

Note, *semi*-inclusive DIS data truly drive the DIS flavor decomposition. 11

RHIC - Polarized Proton-Proton Collider

Unique opportunities to study nucleon spin properties and spin in QCD,

Longitudinal data

STAR

$\sqrt{s} = 200 \text{ GeV}$

2005

2006

2009

2015

35 pb⁻¹

50 pb⁻¹

$\sqrt{s} = 500 \text{ GeV}$

2009

2011

2012

2013

350 pb⁻¹

Transverse data

$\sqrt{s} = 200 \text{ GeV}$

2006

2008

2012

2015

38 pb⁻¹

50 pb⁻¹

$\sqrt{s} = 500 \text{ GeV}$

2011

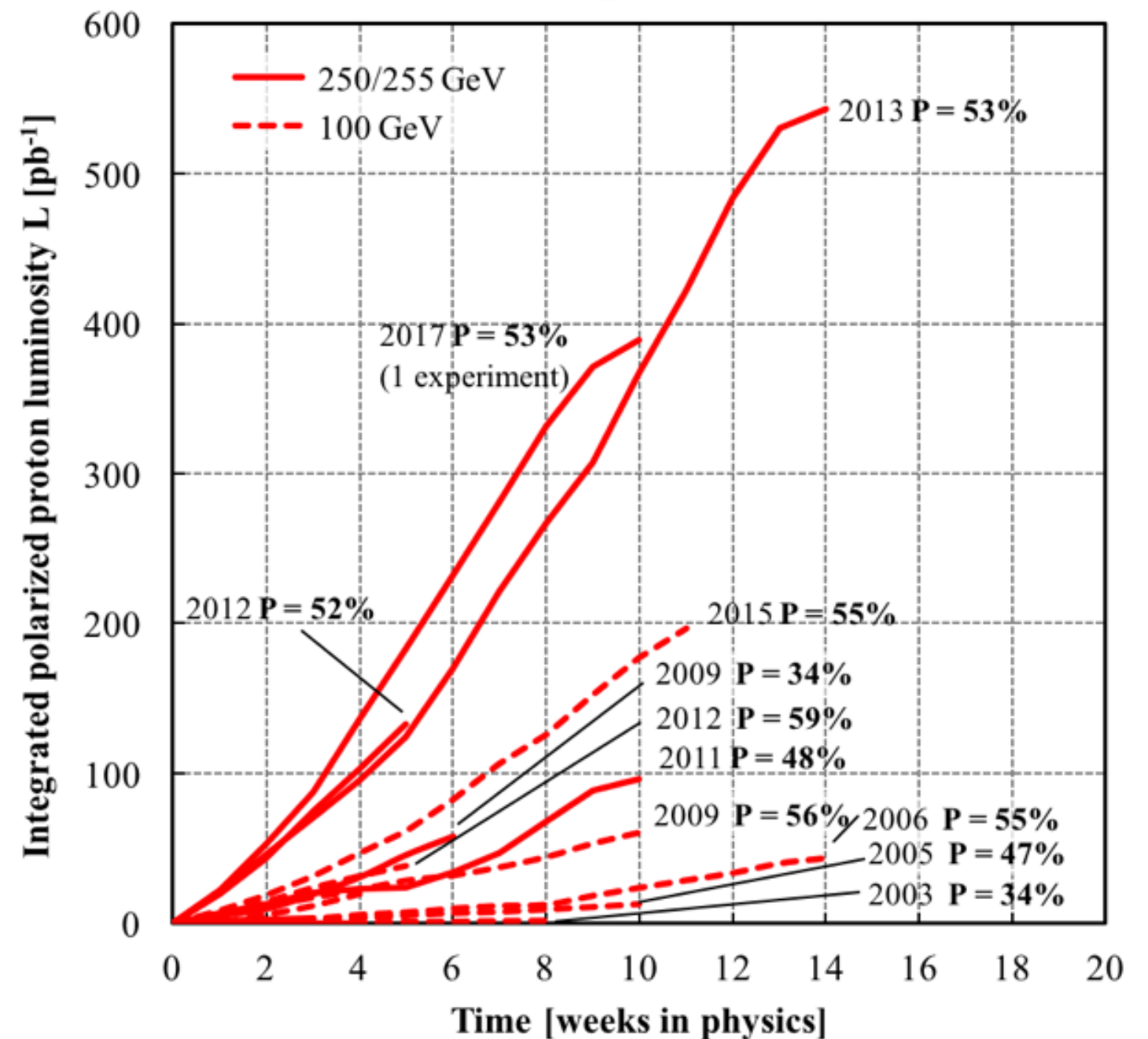
2017

25 pb⁻¹

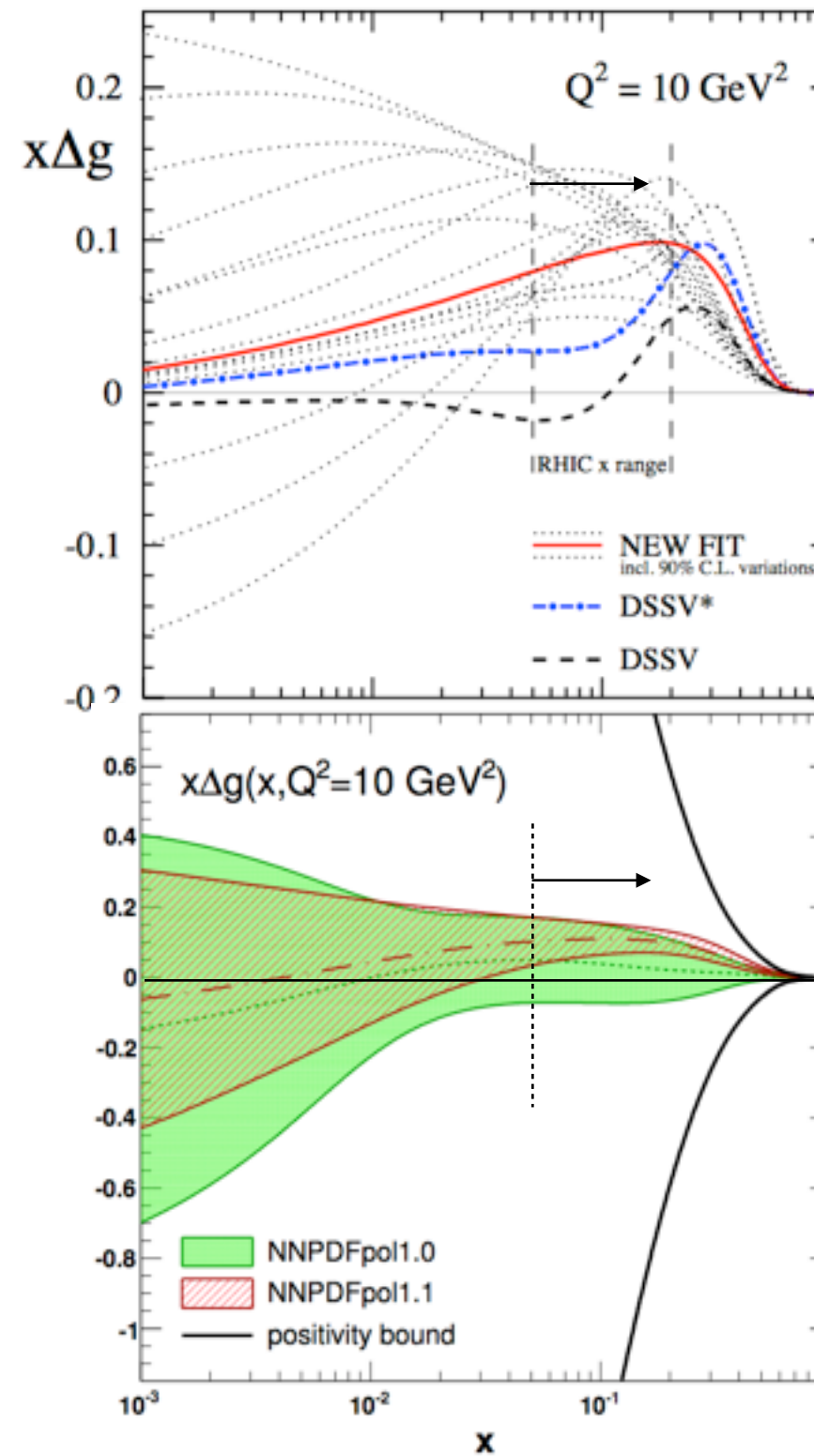
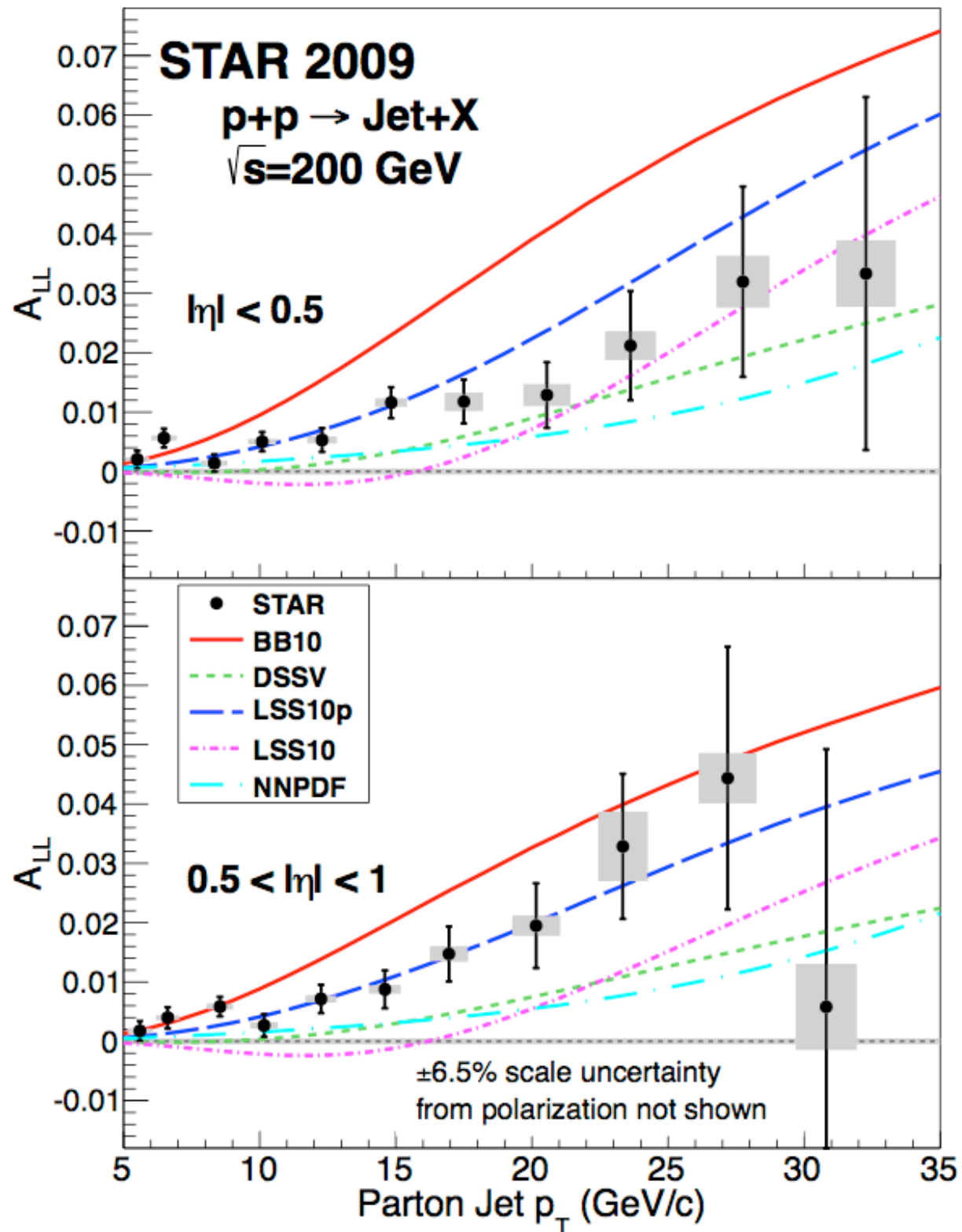
350 pb⁻¹

50-60% polarization

Polarized protons



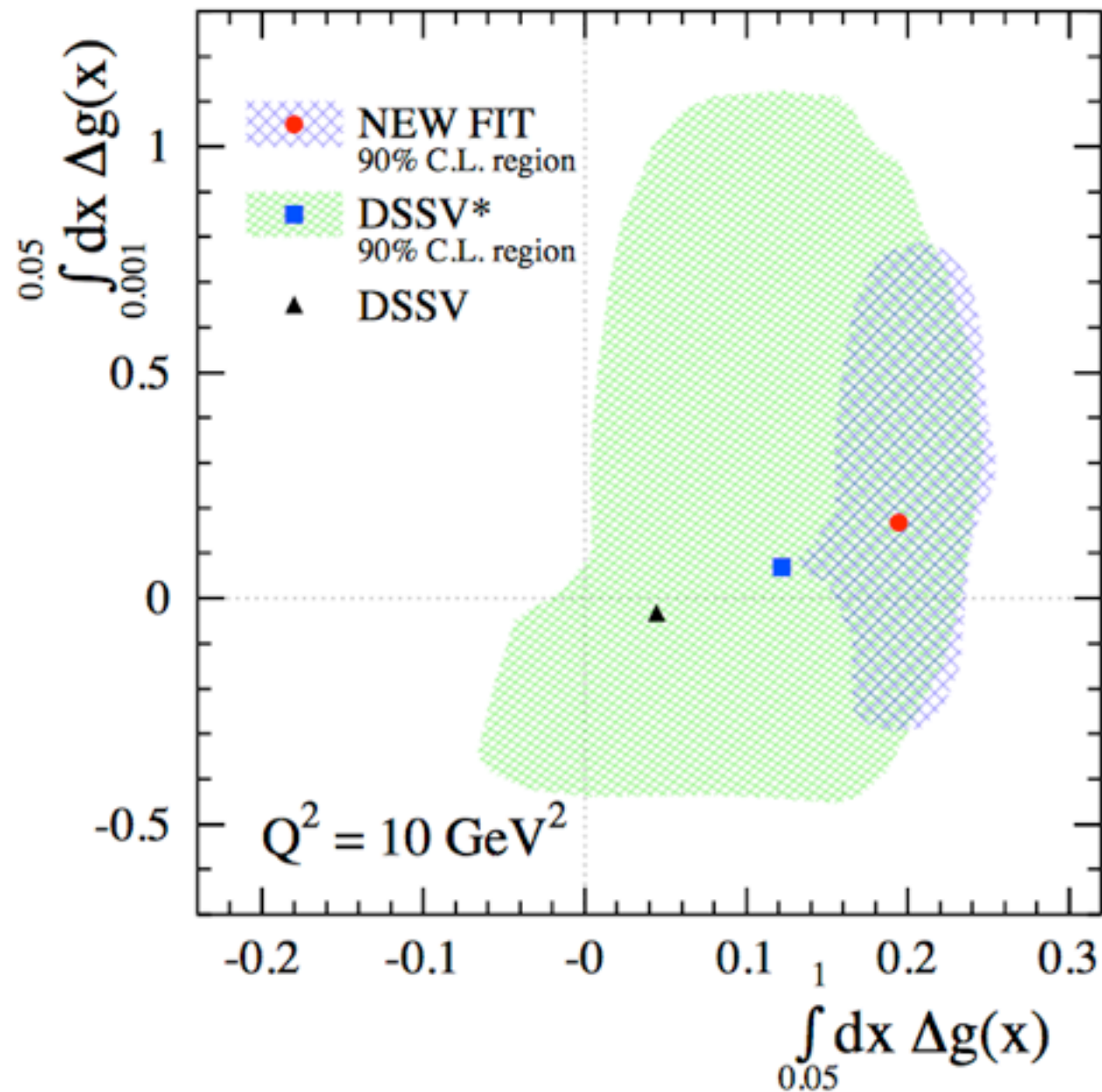
Phys.Rev.Lett 115 (2015) 092002

 0.20 ± 0.07 DSSV, PRL 113,
012001(2014) 0.21 ± 0.10 NNPDF, Nucl. Phys. B
887, 276 (2014)Gluon polarization is positive in the region of the data; ~ 0.2

Gluon Polarization

Some properties of the DSSV polarized gluon:

DSSV, PRL 113, 012001(2014)

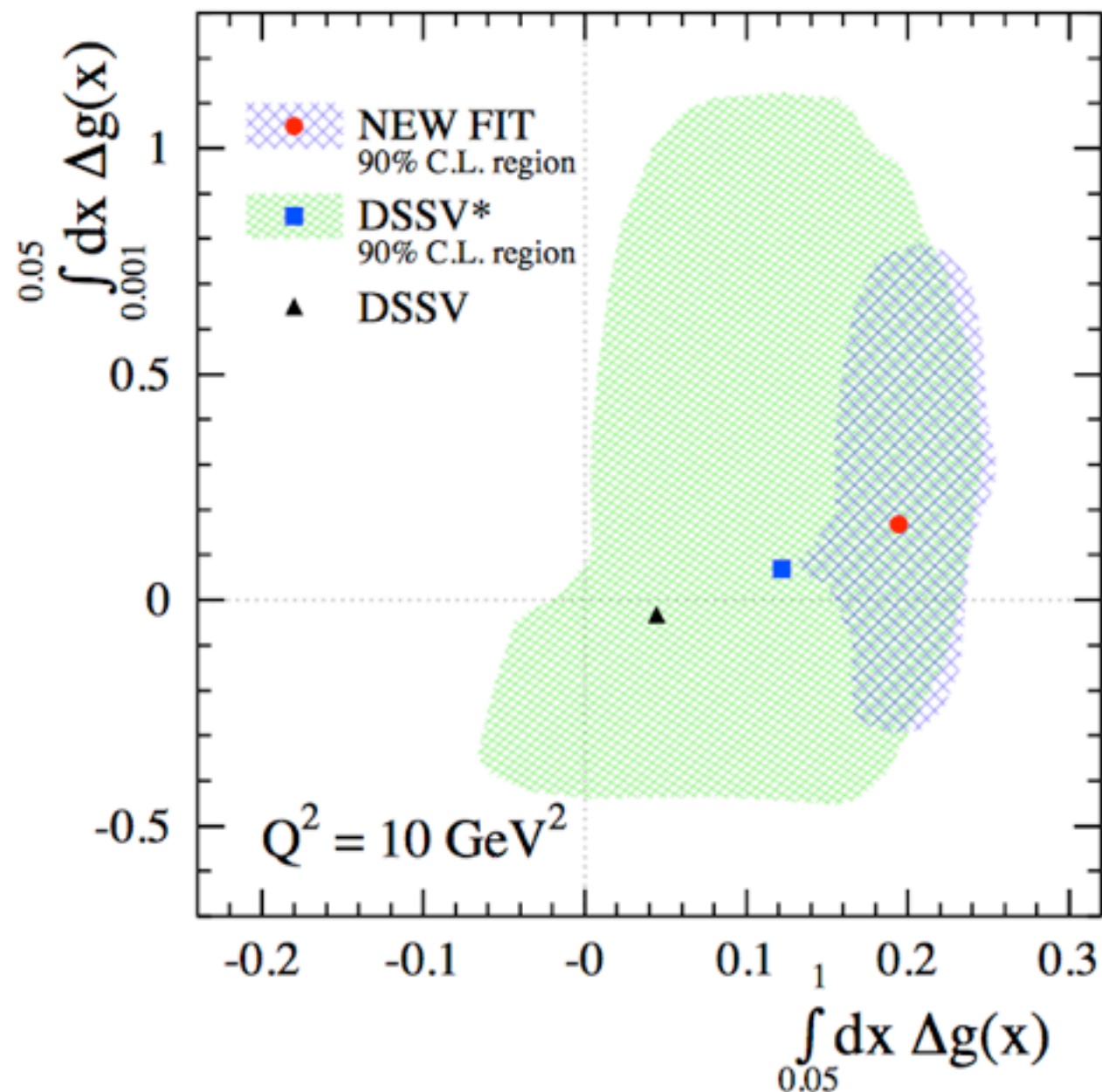


Easy to "hide" $1 \hbar$ in the unmeasured region

Gluon Polarization

Some properties of the DSSV polarized gluon:

DSSV, PRL 113, 012001(2014)



Strong impetus for

better precision, via renewed measurement

sensitivity to underlying kinematics, via correlation (di-jet) measurement

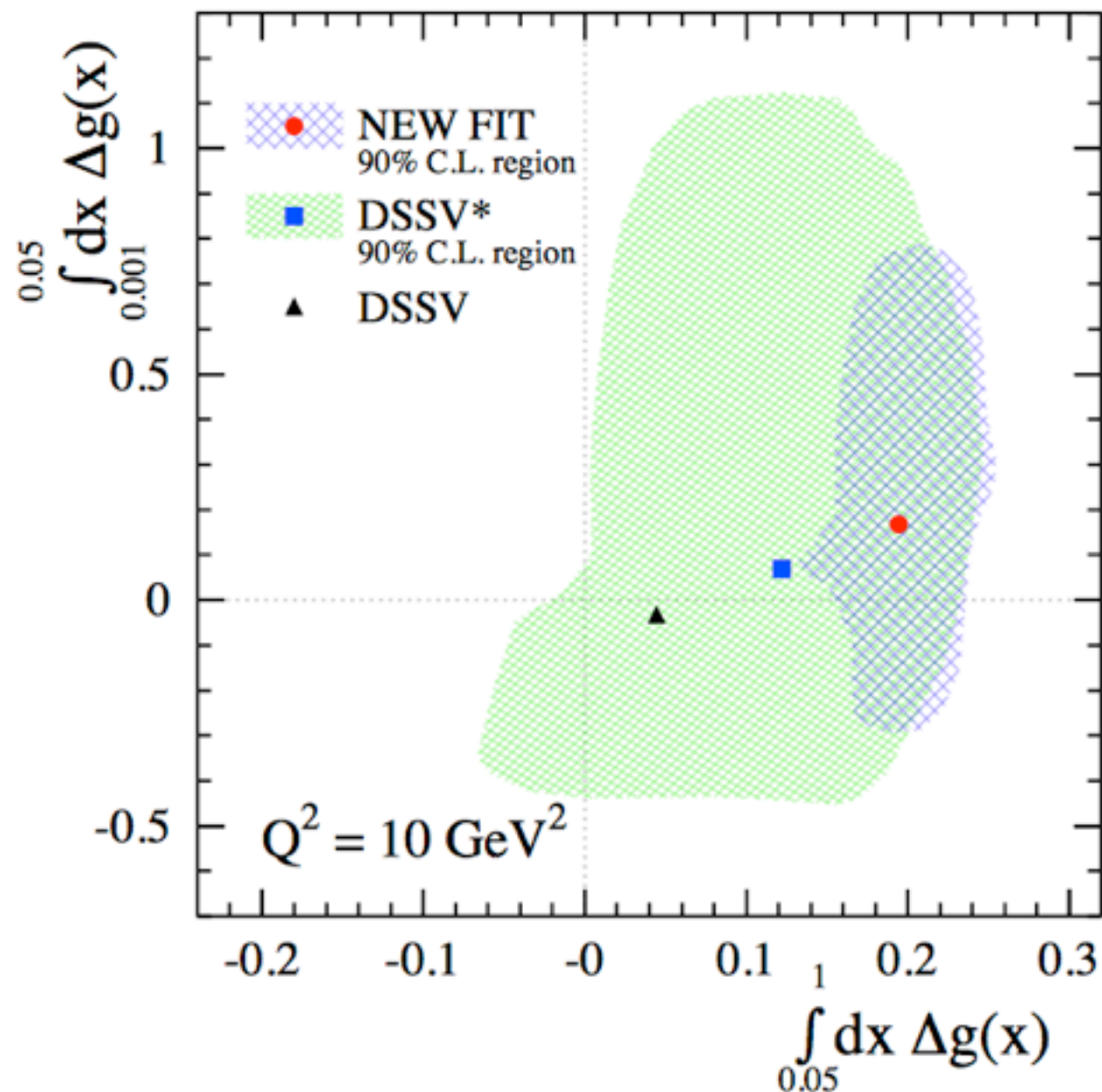
sensitivity to smaller x , via 500 GeV data, forward acceptance

Easy to “hide” $1 \hbar$ in the unmeasured region

Glauon Polarization

Some properties of the DSSV polarized gluon:

DSSV, PRL 113, 012001(2014)



The good news,

STAR is releasing (has released) a *wealth* of data addressing each of these aspects,

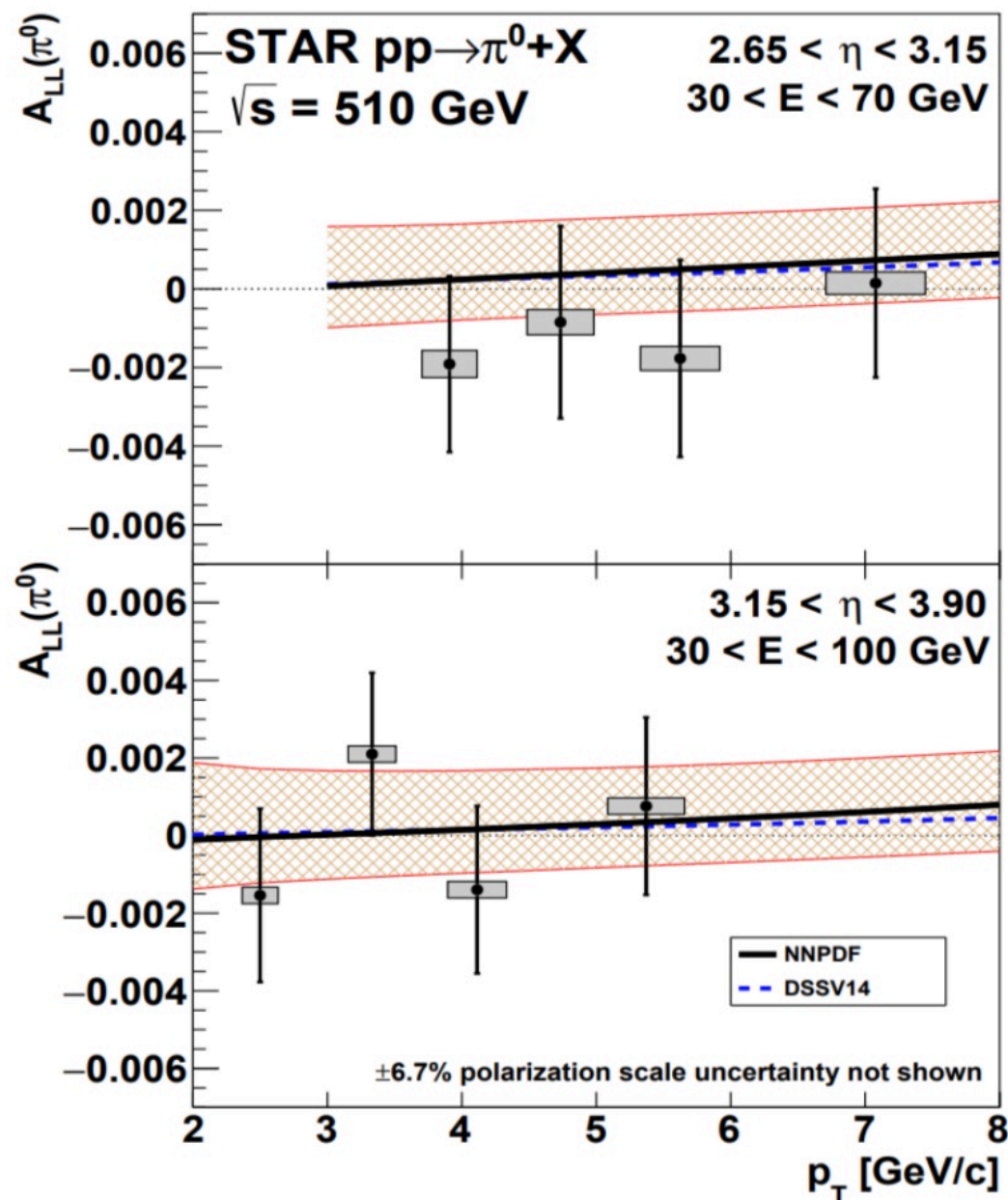
has a science-driven plan for forward instrument upgrades (a talk in itself; truth in advertisement plan \neq approval, at least not as of today).

Easy to “hide” $1 \hbar$ in the unmeasured region

Gluon Polarization

An early glimpse in the forward acceptance region:

arXiv: 1805.09745, PRD 98, 032013 (2018)



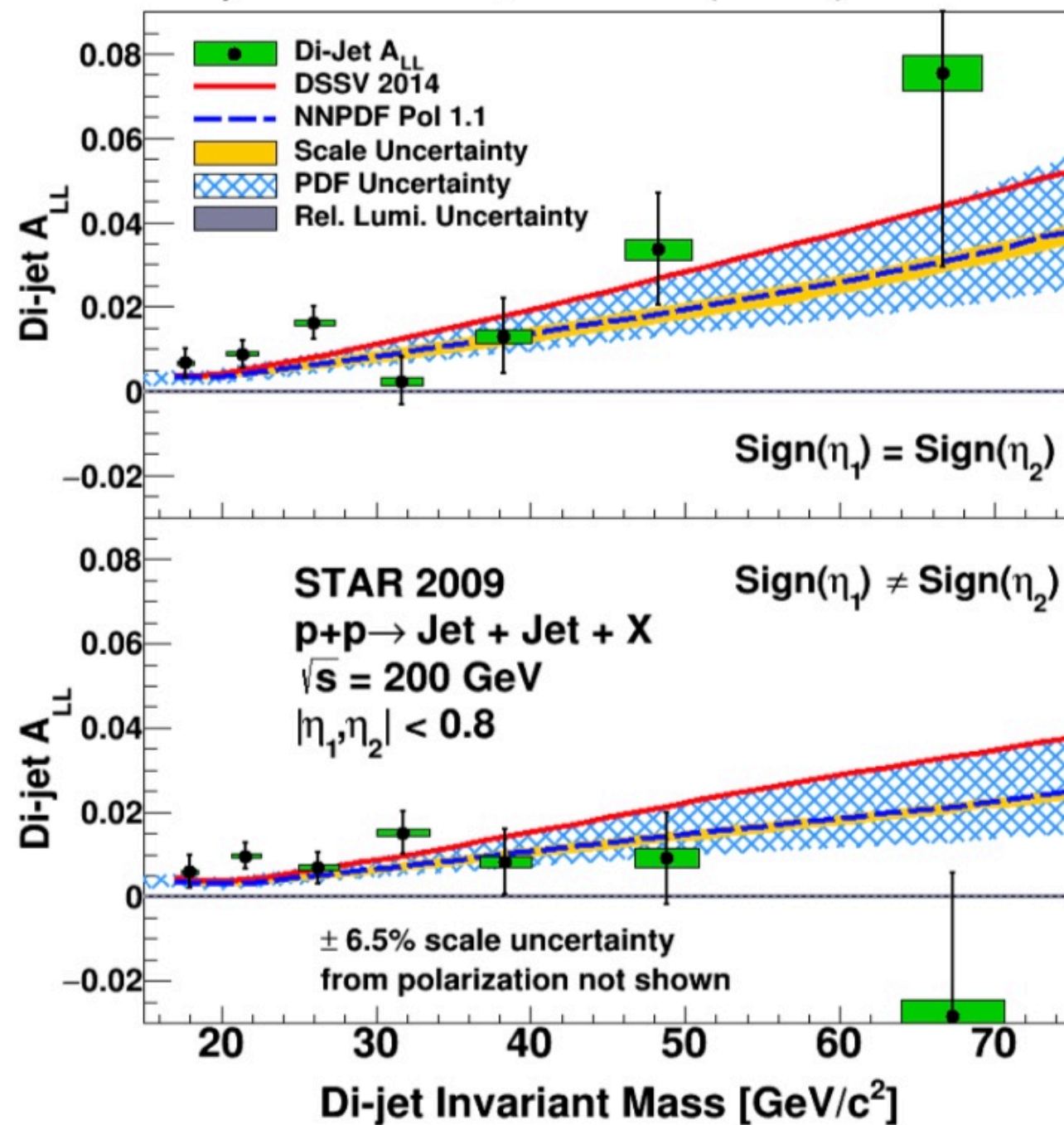
- Results are given for transverse momenta in the range $2 < p_T < 10 \text{ GeV/c}$ within two regions of pseudorapidity that span $2.65 < \eta < 3.9$
- These results are sensitive to the polarized gluon parton distribution function, $\Delta g(x)$, down to the region of parton momentum fraction $x \sim 0.001$
- These results will provide the first direct experimental constraints in $x \ll 0.01$

Correlation measurements will access larger (average) partonic asymmetries.

Gluon Polarization

Mid-central *di-jet* asymmetries:

Phys. Rev. D 95, 071103 (2017)

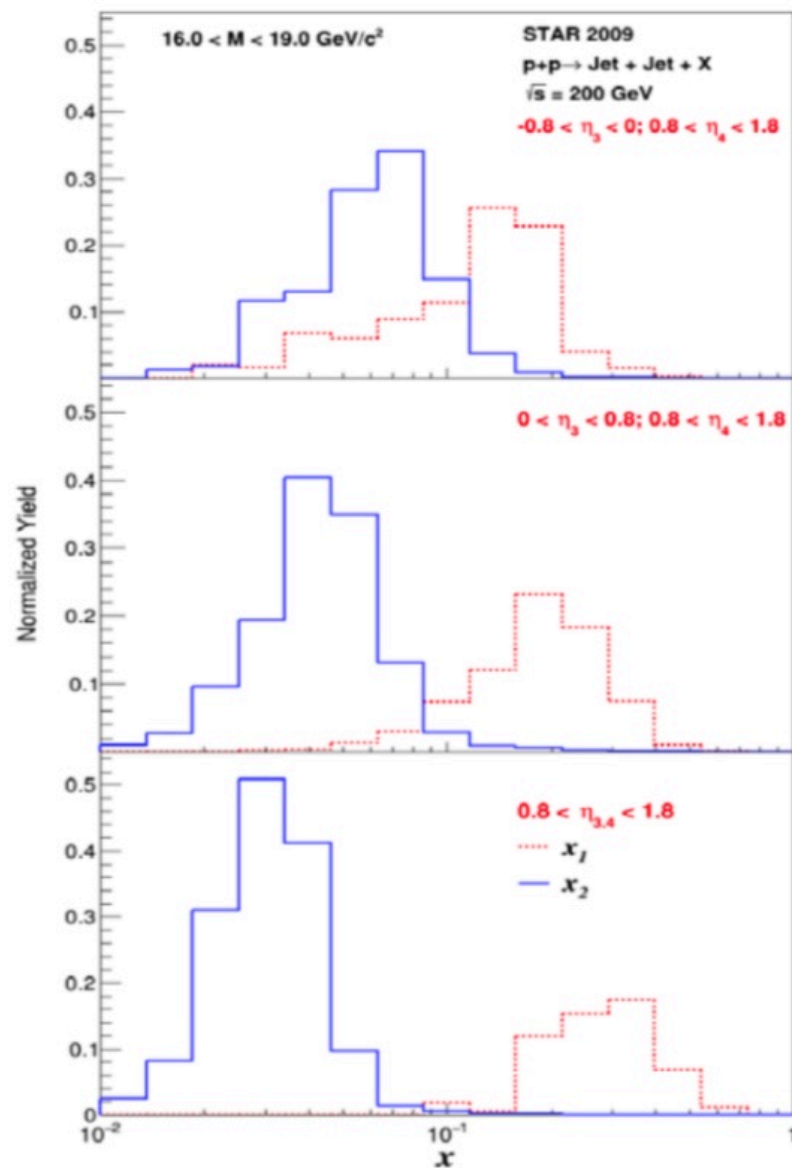
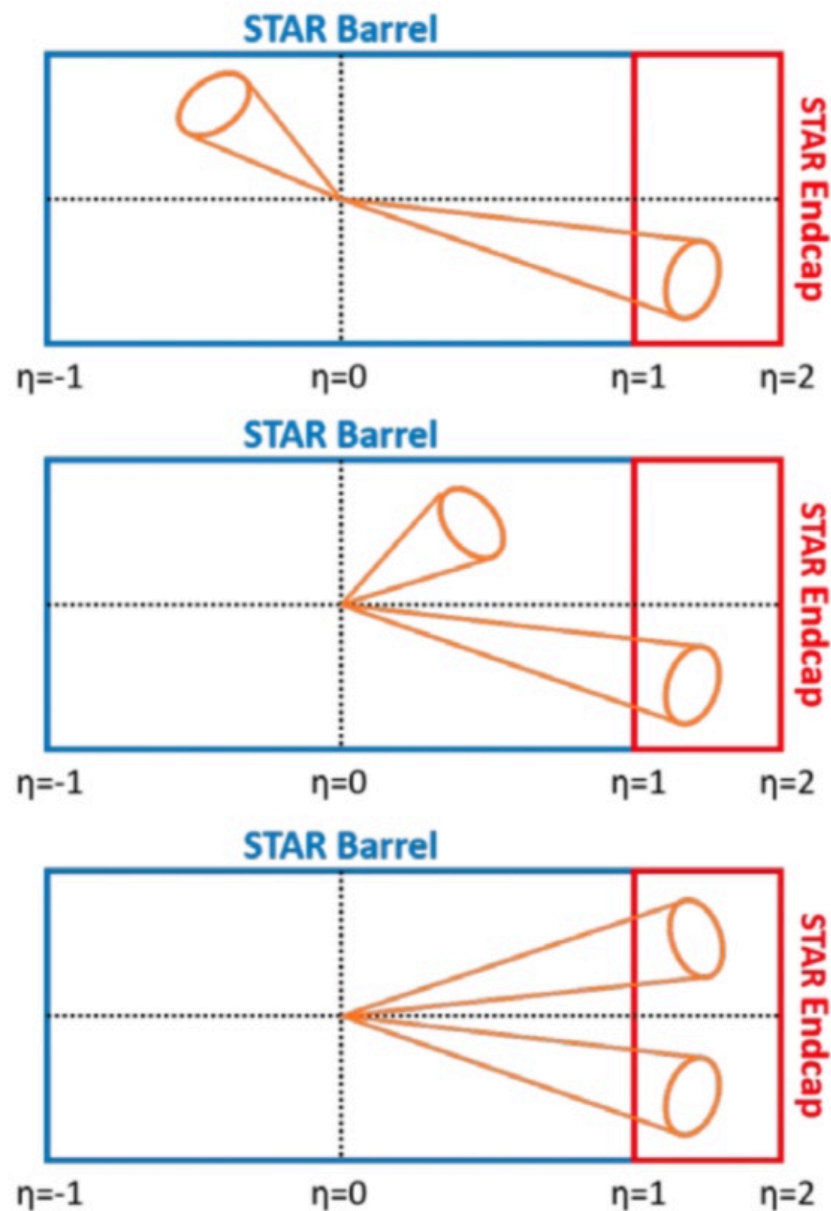


Towards sensitivity to Bjorken- x .

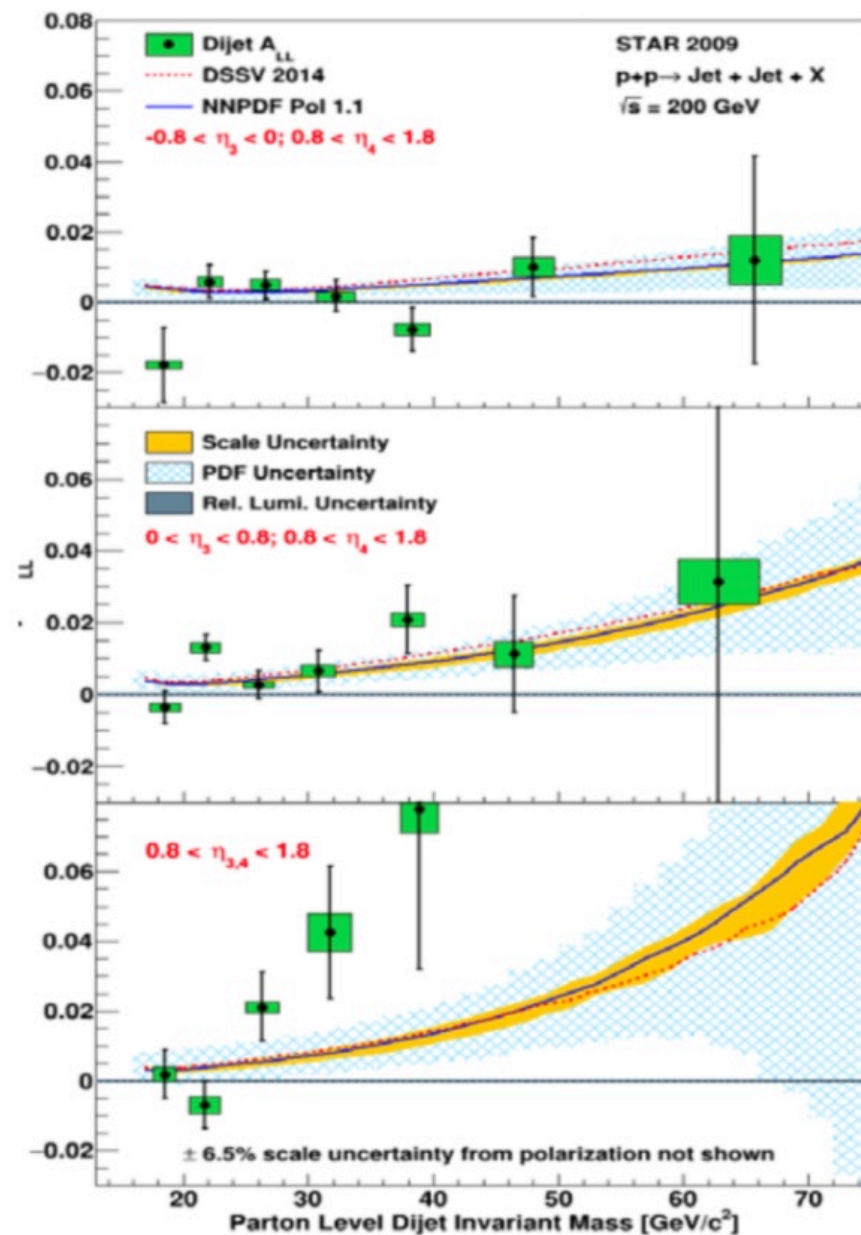
Preliminary results at 500 GeV have come out as well, paper in preparation

Gluon Polarization

di-jet asymmetries in a more forward region:



PRD 98 (2018) 032011



Impact clearly exists; quantifying it will require renewed global analysis (and/or reweighting)

Quark Polarization at RHIC

$\sqrt{s} = 500$ GeV above W production threshold,

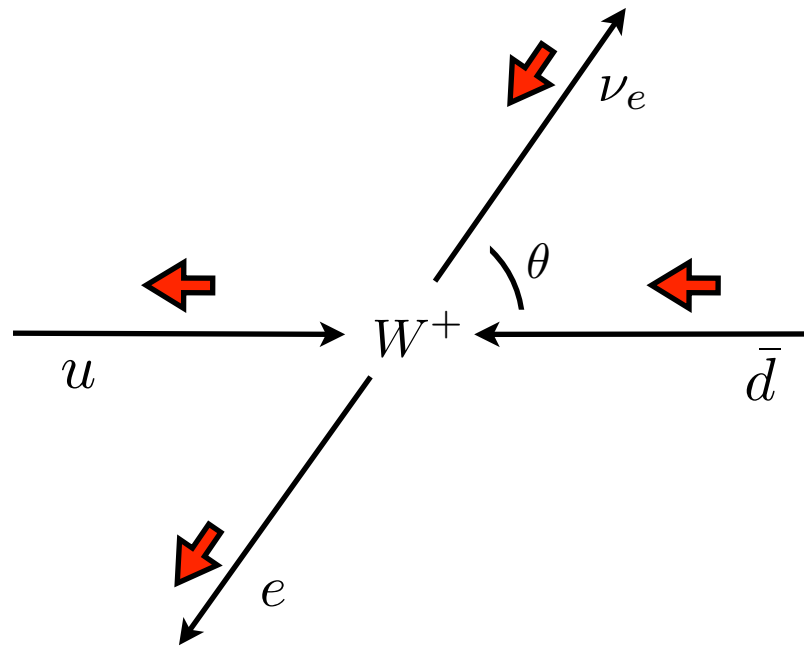
Experiment Signature:

large p_T lepton, missing E_T

Experiment Challenges:

charge-ID at large $|\text{rapidity}|$
electron/hadron discrimination
luminosity hungry

Free of fragmentation (!)



$$\Delta\sigma^{\text{Born}}(\vec{p}p \rightarrow W^+ \rightarrow e^+ \nu_e) \propto -\Delta u(x_a)\bar{d}(x_b)(1+\cos\theta)^2 + \Delta\bar{d}(x_a)u(x_b)(1-\cos\theta)^2$$

Spin Measurements:

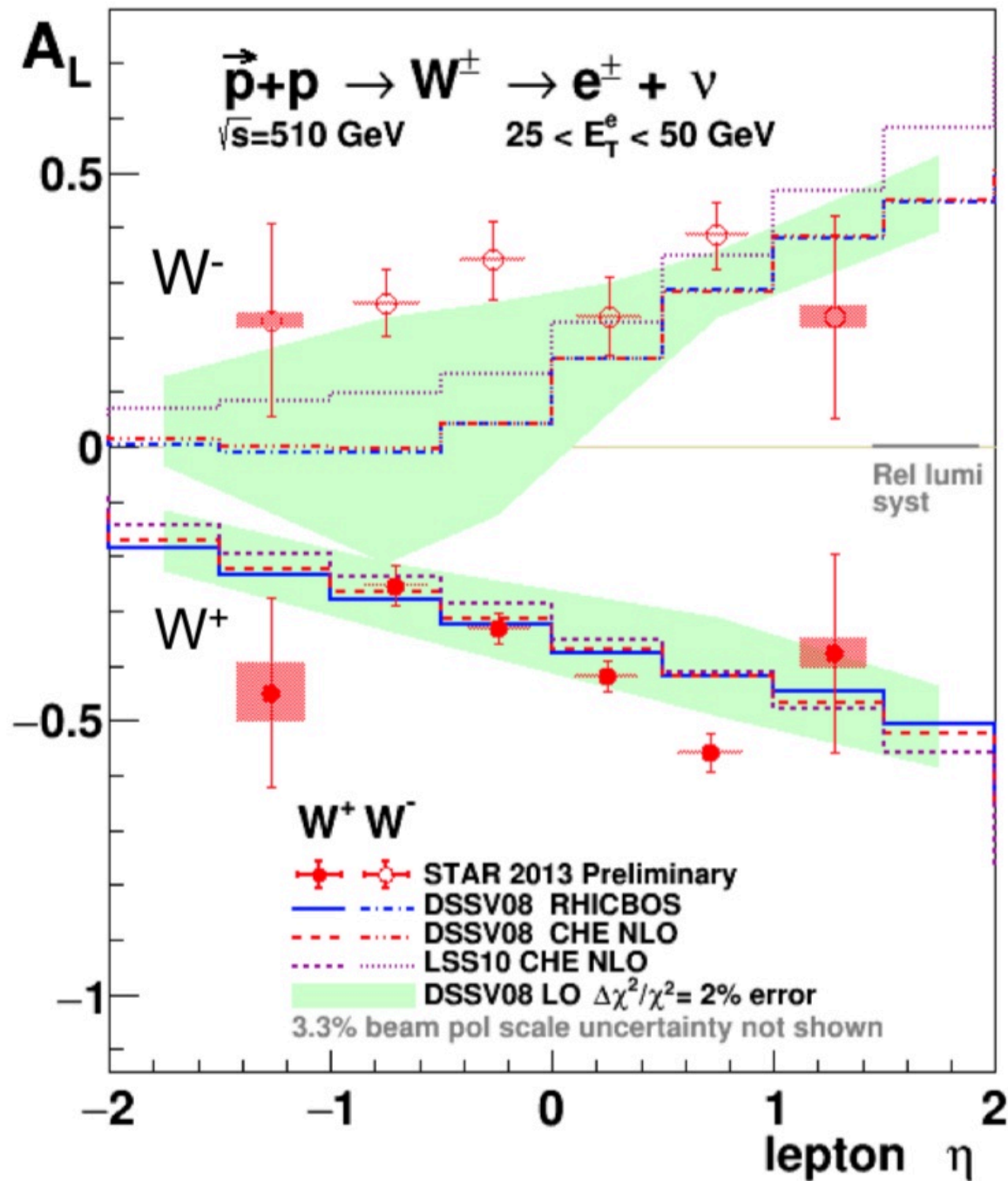
$$A_L(W^+) = \frac{-\Delta u(x_a)\bar{d}(x_b) + \Delta\bar{d}(x_a)u(x_b)}{u(x_a)\bar{d}(x_b) + \bar{d}(x_a)u(x_b)} = \begin{cases} -\frac{\Delta u(x_a)}{u(x_a)}, & x_a \rightarrow 1 \\ \frac{\Delta\bar{d}(x_a)}{\bar{d}(x_a)}, & x_b \rightarrow 1 \end{cases}$$

LO expressions to illustrate overall behavior,

$$A_L(W^-) = \begin{cases} -\frac{\Delta d(x_a)}{d(x_a)}, & x_a \rightarrow 1 \\ \frac{\Delta\bar{u}(x_a)}{\bar{u}(x_a)}, & x_b \rightarrow 1 \end{cases}$$

NLO known and used in extracting pPDFs.

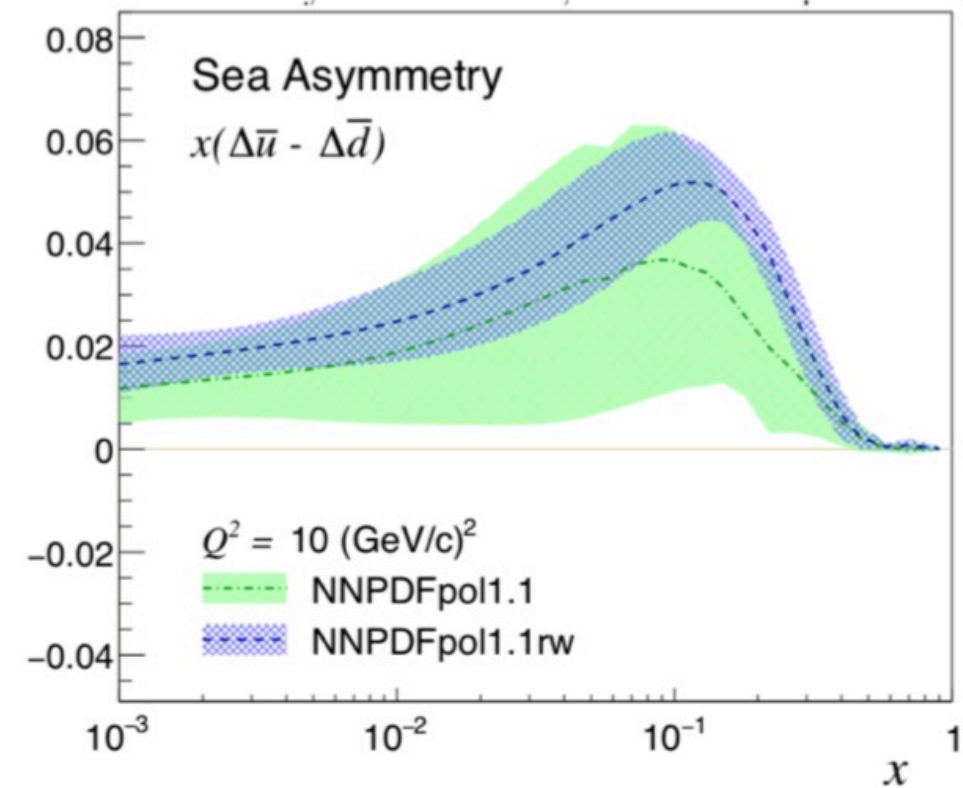
Quark Polarization at RHIC



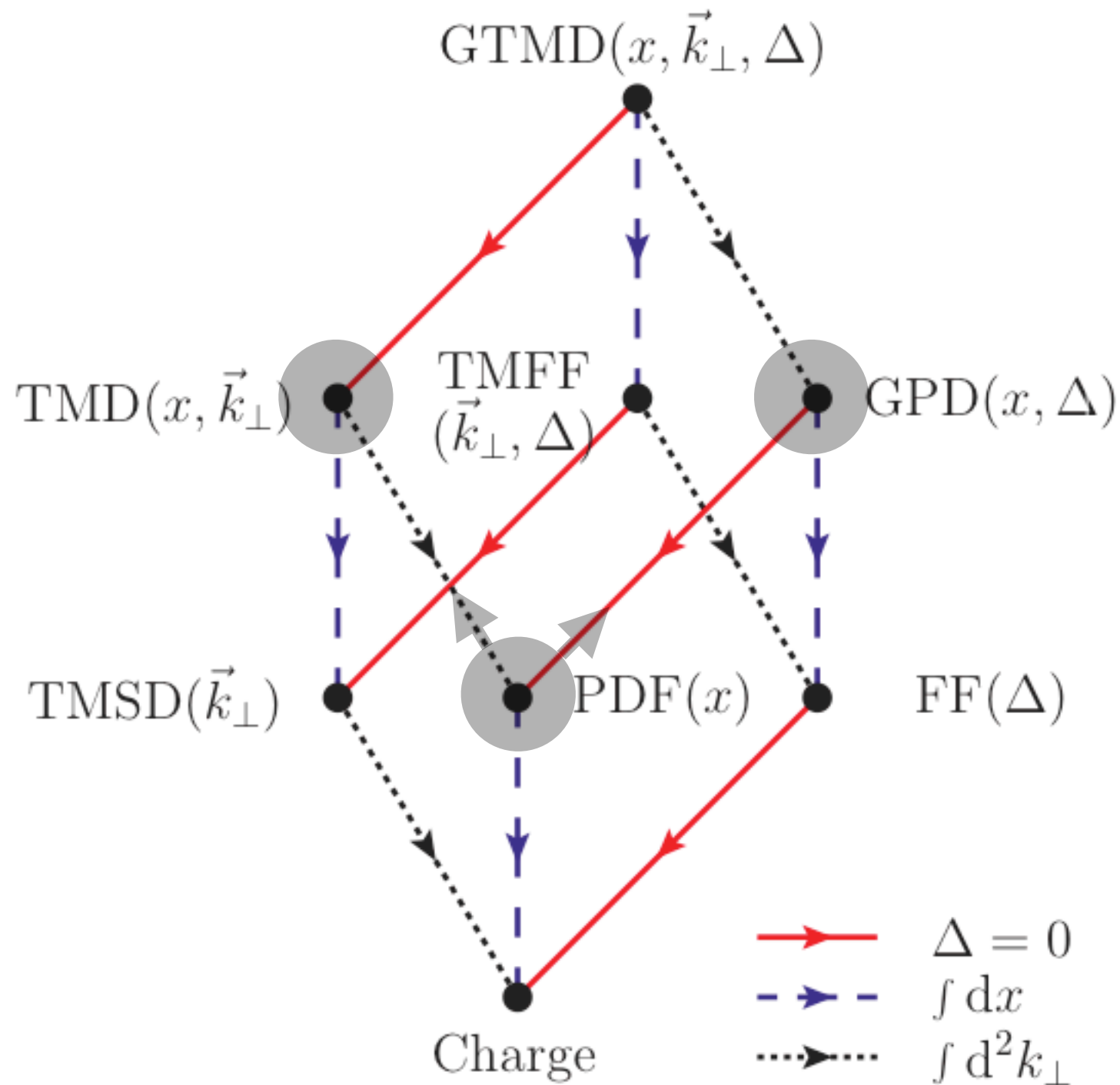
See e.g. J. Zhang, INPC
Q.H. Xu, DIS

- Further confirmed the polarized sea asymmetry:

$$\Delta\bar{u} > \Delta\bar{d}$$



Beyond Quark and Gluon Spins



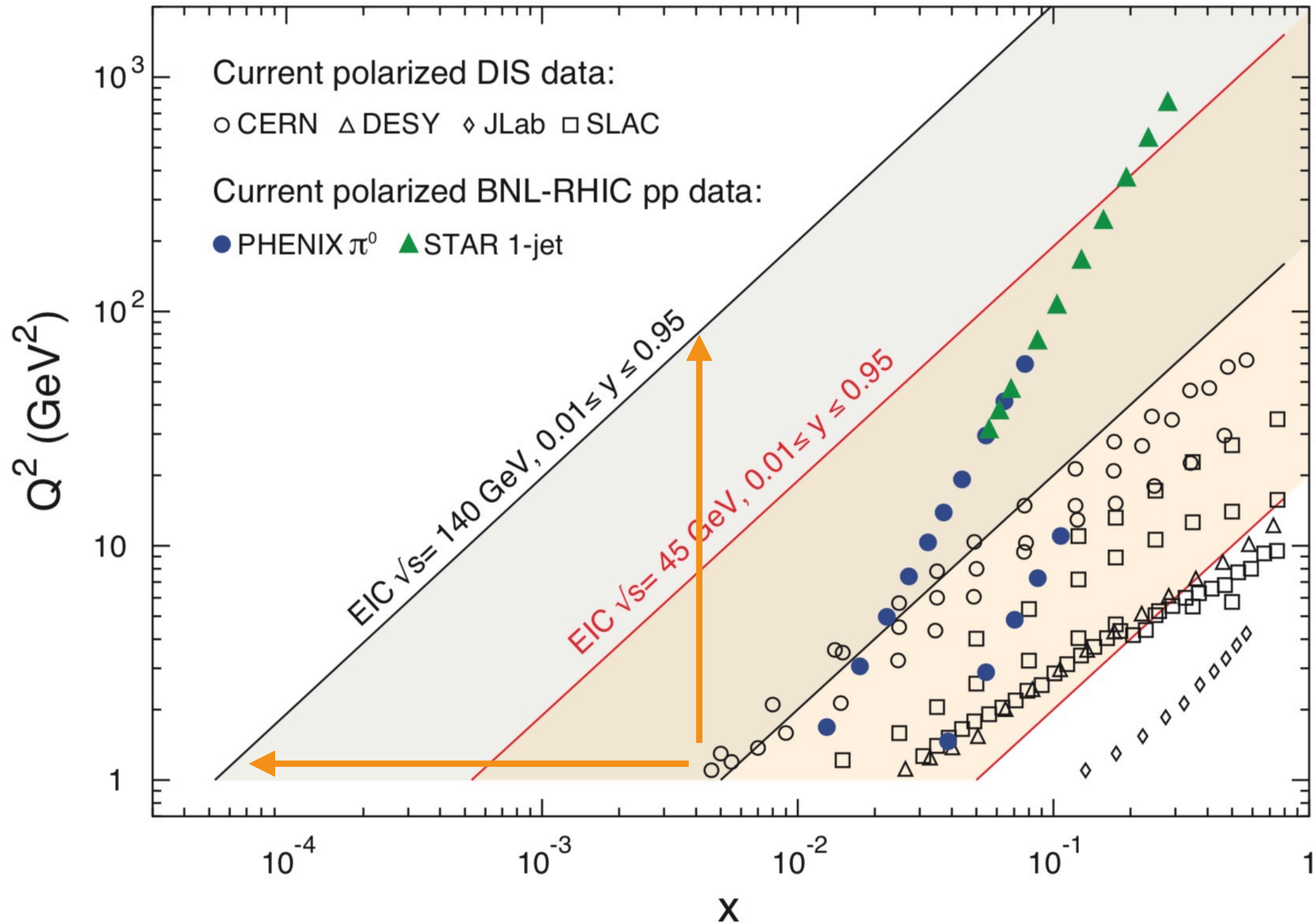
Theory may be ahead of experiment, although many questions remain,

Beautiful initial (DVCS) measurements from HERMES and JLab,

IMHO, very far from reliable insights on angular momentum parts in the (Ji) spin-decomposition,

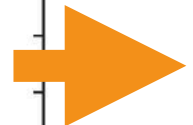
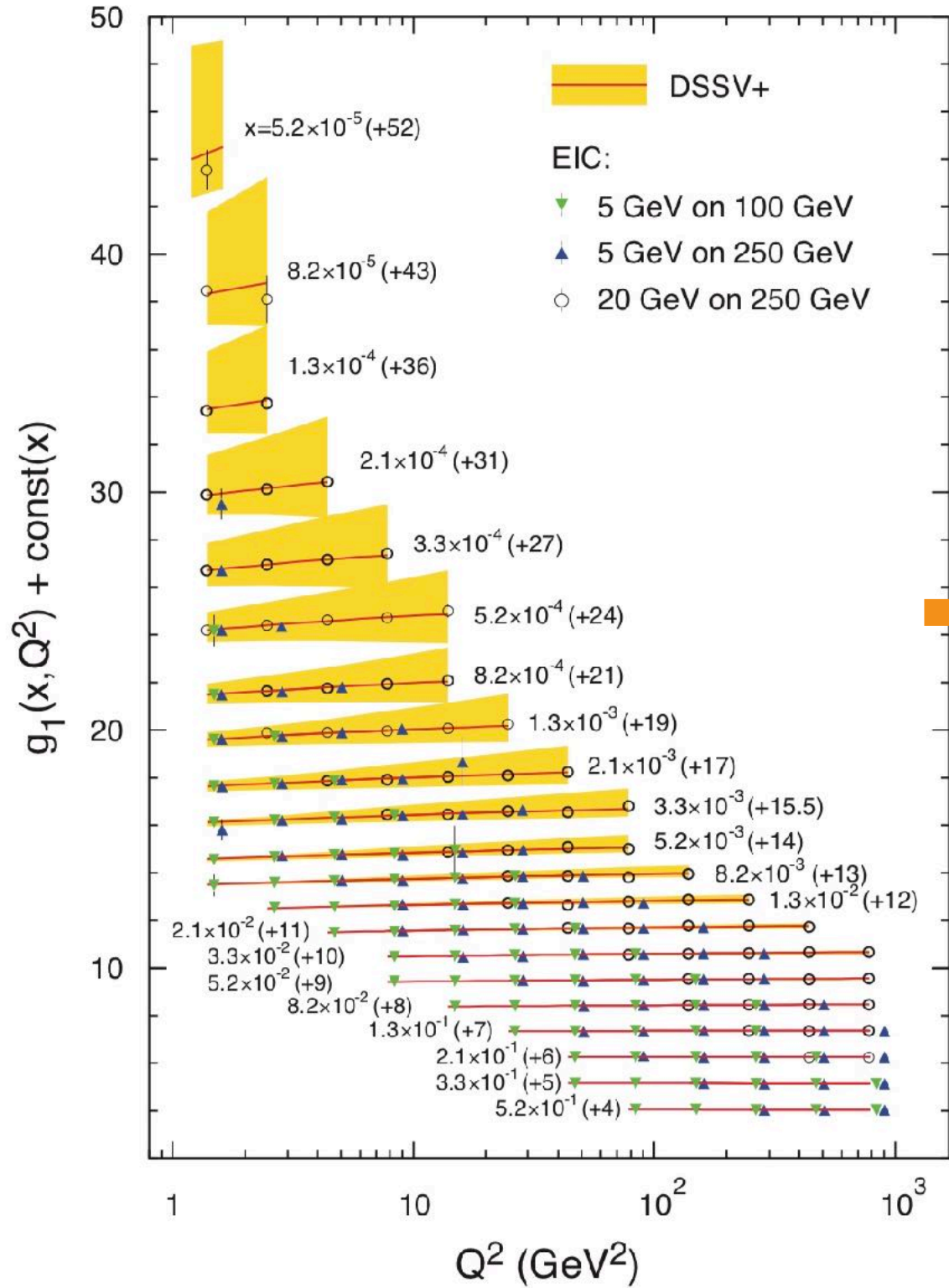
Looking Ahead

U.S.-based EIC - Proton Spin

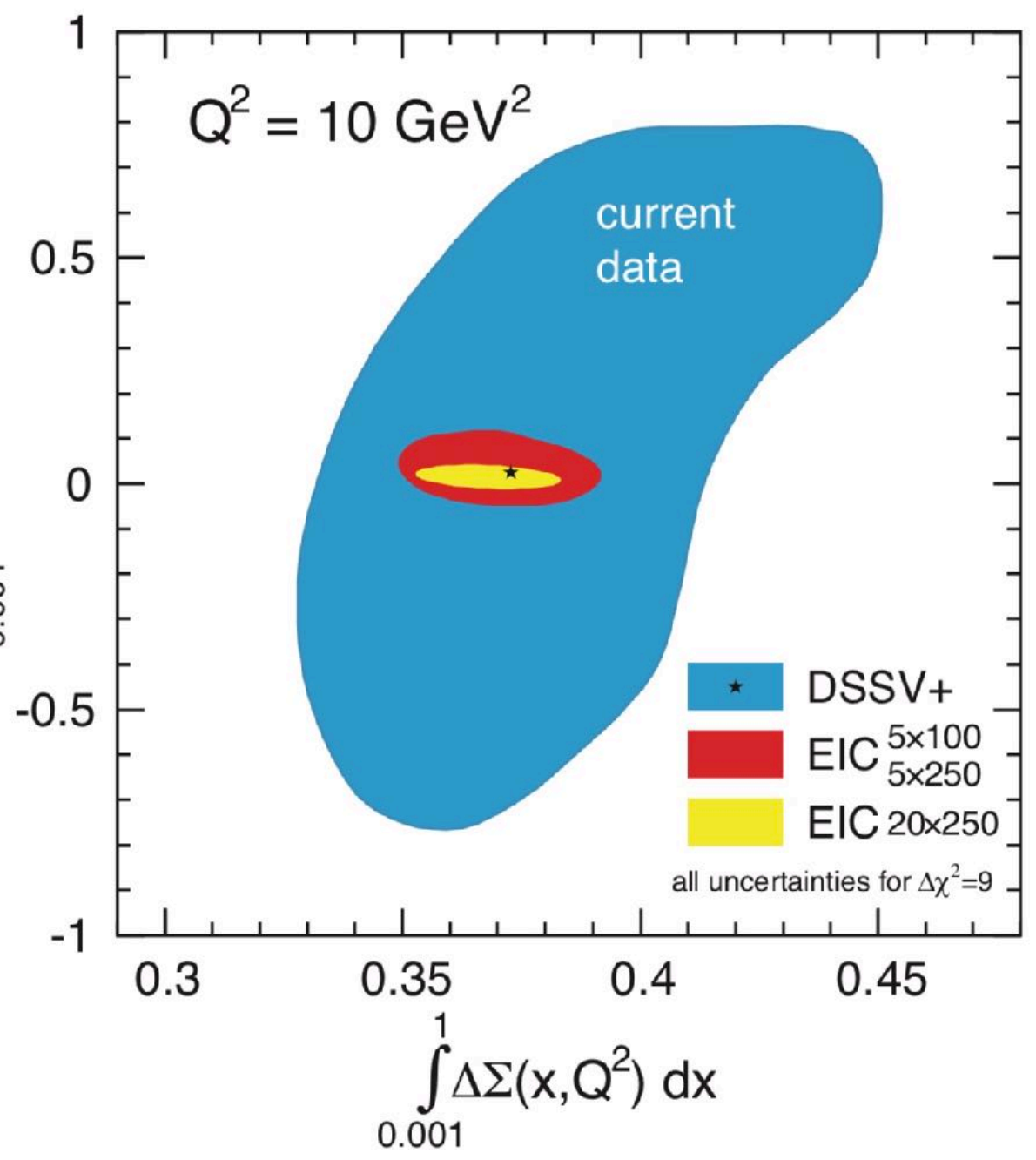


Two orders in x and Q^2 compared to existing data; few, if any, alternatives.

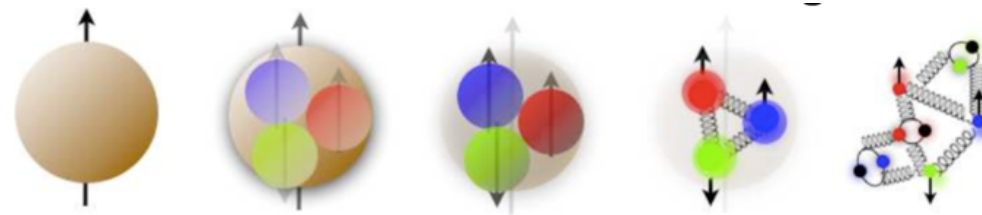
U.S.-based EIC - Proton Spin



$$\int_{0.001}^1 \Delta g(x, Q^2) dx$$



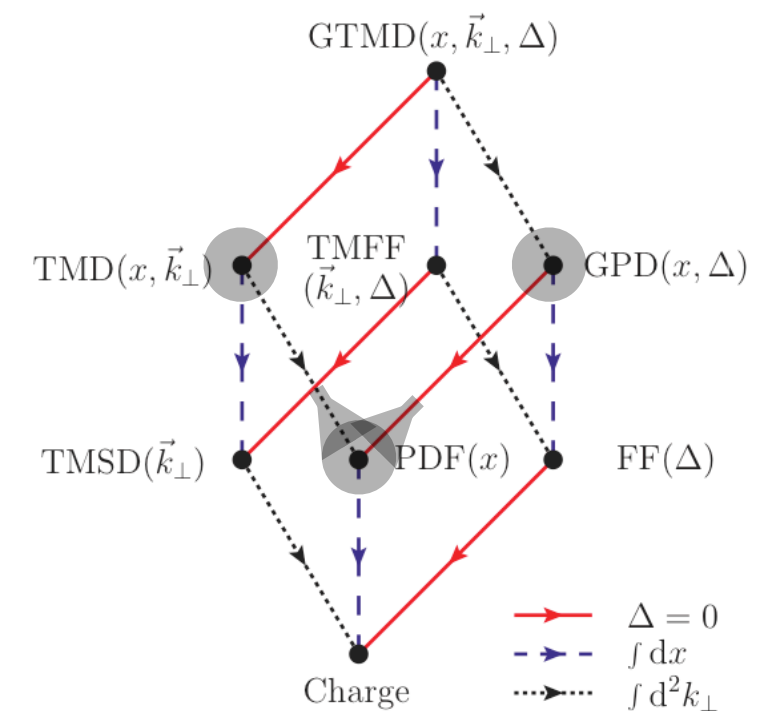
Conclusive insights in quark and gluon helicity from inclusive measurements, and orbital momentum by subtraction (!)



Also experimentally, we are still very far from a reliable decomposition of the proton spin

DIS data:

- small- x measurements provided the impetus for renewed study of the proton spin,
- data on proton and neutron targets over a wide x -range, confirming the Bjorken Sum rule, decent insight in the sum of quark and anti-quark spins,
- initial sensitivities to scale dependence,
- best (lack of?) insight in strangeness,
- start of DVCS measurements with sensitivity to orbital momentum



RHIC spin program:

- has achieved the most sensitive insights in **gluon polarization** in the nucleon, *gluons are positively polarized for momentum fractions $x > 0.05$, at the level of $0.2 h$ for $Q^2 = 10 \text{ GeV}^2$*
- has provided evidence, with measurements at the W -mass scale that are free of fragmentation uncertainties, of non-perturbative **sea-quark polarization**,
- (quite promising TMD measurements; again a talk by itself)

EIC + theory will be essential to arrive the spin decomposition (or at least a partial one).