

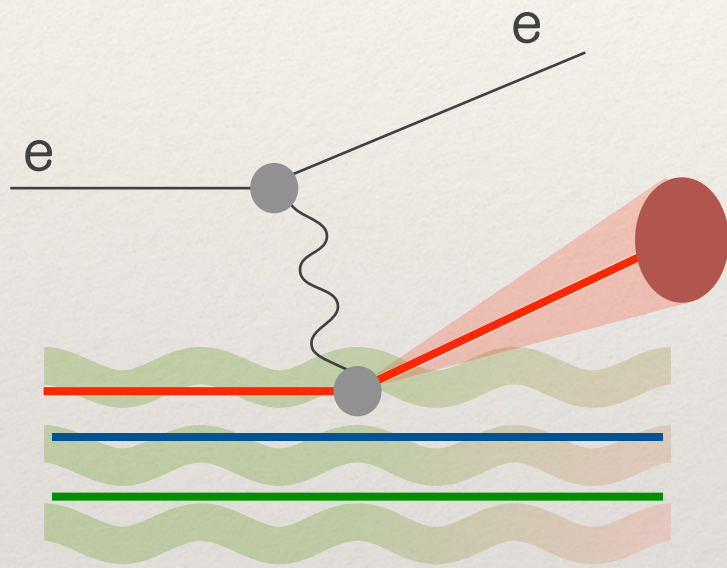


Ignazio Scimemi (UCM)

Exploring transverse
momentum distribution
with *Jets*

Most recent results in collaboration with
Duff Neill,
Wouter Waalewijn
JHEP 1704 (2017) 020
and Daniel Gutierrez-Reyes,
W. Waalewijn, Lorenzo Zoppi
arXiv:1807.07573, PRL...

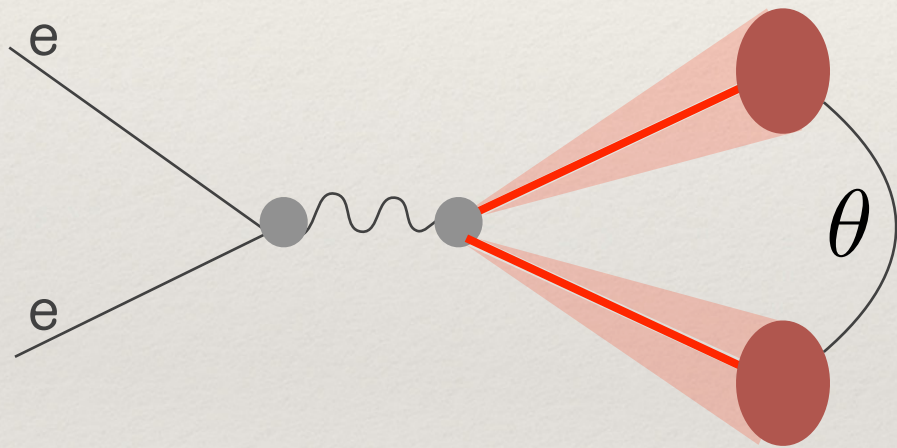
Di-jet interactions



JETS CAN BE USED ALSO IN A DIFFERENT WAY:
SIDIS WITH A FINAL JET

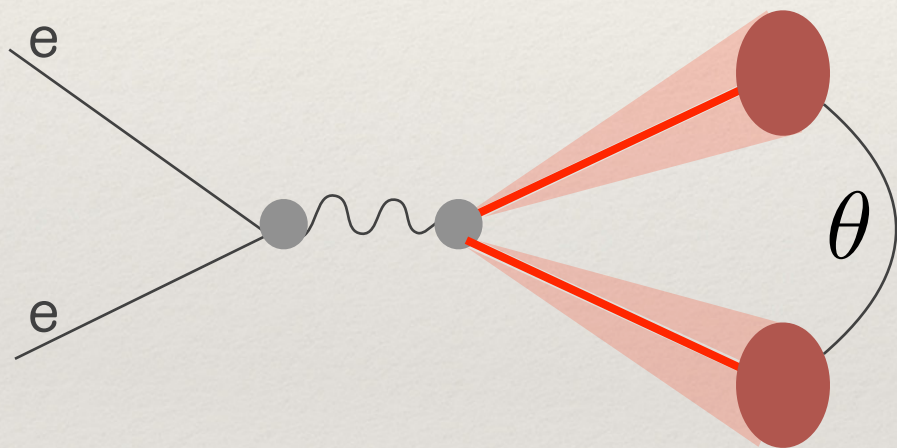
$$e + p \rightarrow e + jet + X$$

Di-jet interactions



HOW SHOULD WE DEFINE JET PARAMETERS TO STUDY TMDs?

Di-jet interactions



$$z_j = E_j / Q$$

Energy fraction of the
initiating quark

$$\mathbf{q} = \frac{\mathbf{p}_1}{z_1} + \frac{\mathbf{p}_2}{z_2}$$

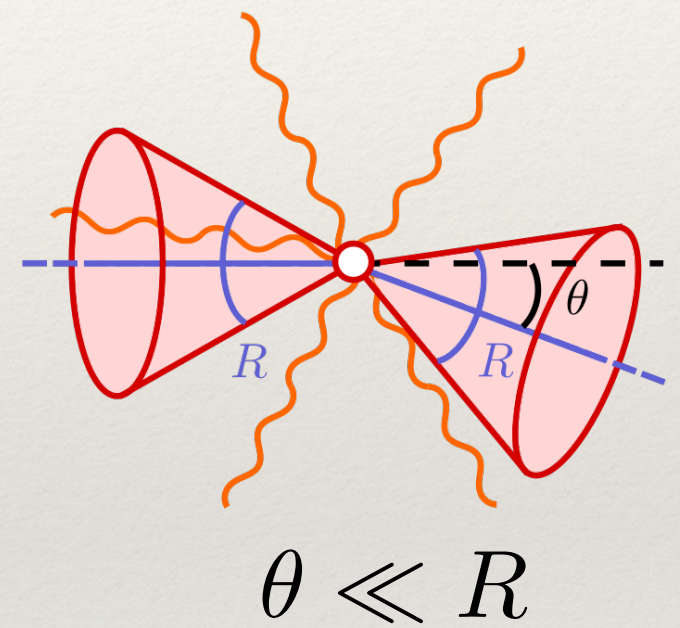
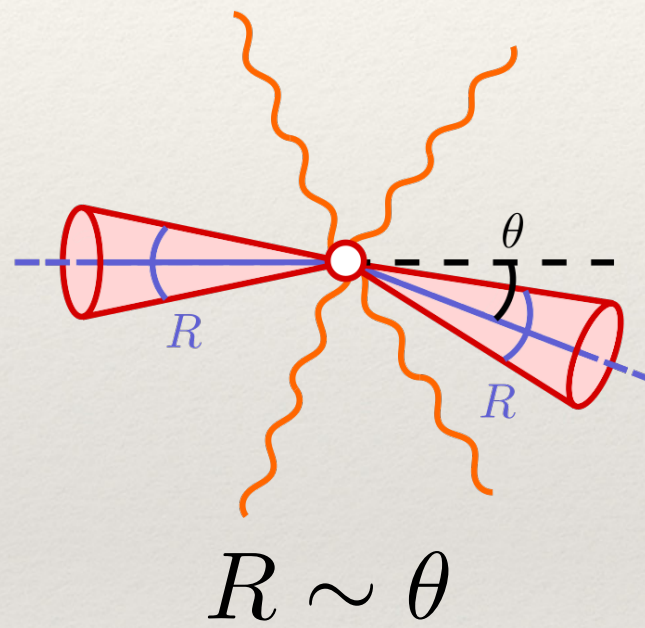
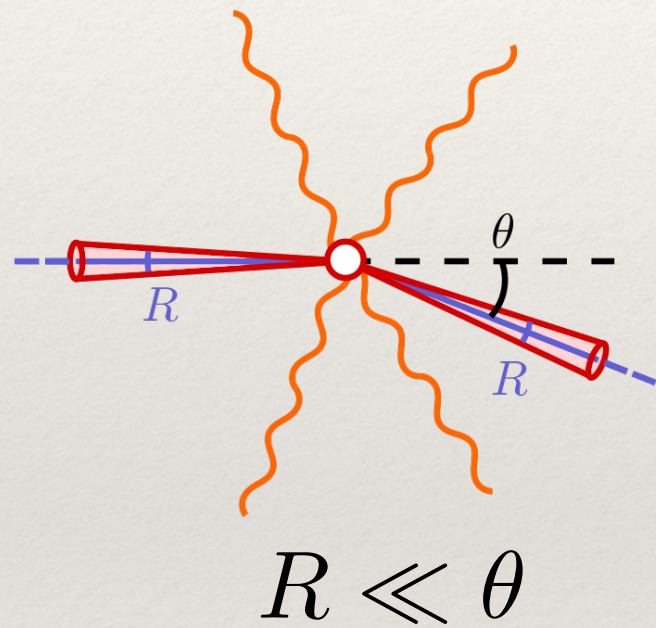
Momentum de-correlation
of the 2 jets

$$\theta = 2 \frac{|\mathbf{q}|}{Q}$$

Angular de-correlation of
the 2 jets

Di-jet interactions

WE EXPECT TO RECOVER A TMD LIKE LIMIT FOR $\theta \ll 1$



...BUT THE FINAL RESULT CRUCIALLY DEPENDS ON THE ANGULAR VS RADIUS INTERPLAY

Factorization for small radius jets

$$\frac{d\sigma}{dz_1 dz_2 dQ^2 d\mathbf{q}} = H(Q^2, \mu) \int \frac{d\mathbf{b}}{(2\pi)^2} e^{-i\mathbf{b}\cdot\mathbf{q}} J_q^{\text{axis}}(z_1, \mathbf{b}, QR, \mu, \zeta_1) J_{\bar{q}}^{\text{axis}}(z_2, \mathbf{b}, QR, \mu, \zeta_2) \left[1 + \mathcal{O}\left(\frac{\mathbf{q}^2}{Q^2}\right) \right]$$

The factorization works like for hadron TMD, with the same soft factor reabsorbed into each jet

$$\mu^2 \frac{d}{d\mu^2} J_i^{\text{axis}}(z, \mathbf{b}, QR, \mu, \zeta) = \frac{1}{2} \gamma_F^i(\mu, \zeta) J_i^{\text{axis}}(z, \mathbf{b}, QR, \mu, \zeta),$$
$$\zeta \frac{d}{d\zeta} J_i^{\text{axis}}(z, \mathbf{b}, QR, \mu, \zeta) = -\mathcal{D}^i(\mu, \mathbf{b}) J_i^{\text{axis}}(z, \mathbf{b}, QR, \mu, \zeta).$$

SAME EVOLUTION AS IN THE CASE OF HADRONS!

how small?

Factorization for small radius jets

$R \lesssim \theta$ We can evaluate the usual OPE on transverse momentum integrated objects

$$J_i^{\text{axis}} \rightarrow \sum_j \int \frac{df z'}{z'} \mathbb{C}_{i \rightarrow j} \left(\frac{z}{z'}, \mathbf{b}, \mu, \zeta \right) \mathcal{J}_j(z', z' Q R, \mu) [1 + \mathcal{O}(\mathbf{b}^2 Q^2 R^2)]$$

THE SAME AS FOR FRAGMENTATION FUNCTIONS!!
M.G. ECHEVARRIA, I.S., A.VLADIMIROV 1604.07869

THE SAME AS FOR HADRONS
INSIDE JETS WITH SJA!!
Z.KANG, F.RINGER 1705.08443...

how small?

Factorization for small radius jets

$R \ll \theta$ We recover the hadrons.. and the fragmentation functions..

$$\mathcal{J}_j(z, QR, \mu) \rightarrow \sum_h d_{j \rightarrow h}(z, \mu) \left[1 + \mathcal{O}\left(\frac{Q^2 R^2}{\Lambda_{\text{QCD}}^2}\right) \right]$$

...UP TO NOW NOTHING DEPENDS ON THE JET RADIUS....

Factorization for big radius jets: only WTA

$$\theta < R$$

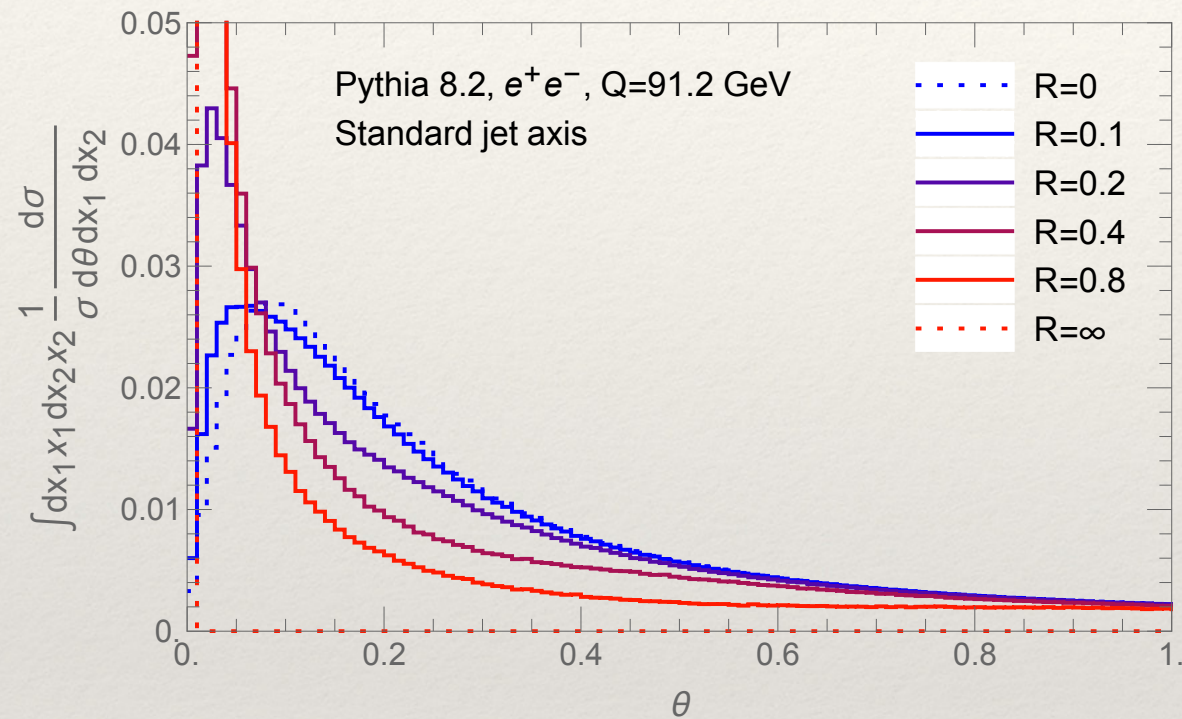
The **standard jet axis** does not allow the factorization of the cross-section! This axis is sensitive to the radiation inside the jet (which can be hard), but the momentum de-correlation is sensitive only to radiation outside the jet... which can have multiple origin.

The **WTA axis** is not affected by the origin of soft radiation, which can be inside or outside of the jet ...so the soft radiation is independent on the radius of the jet!

1-loop

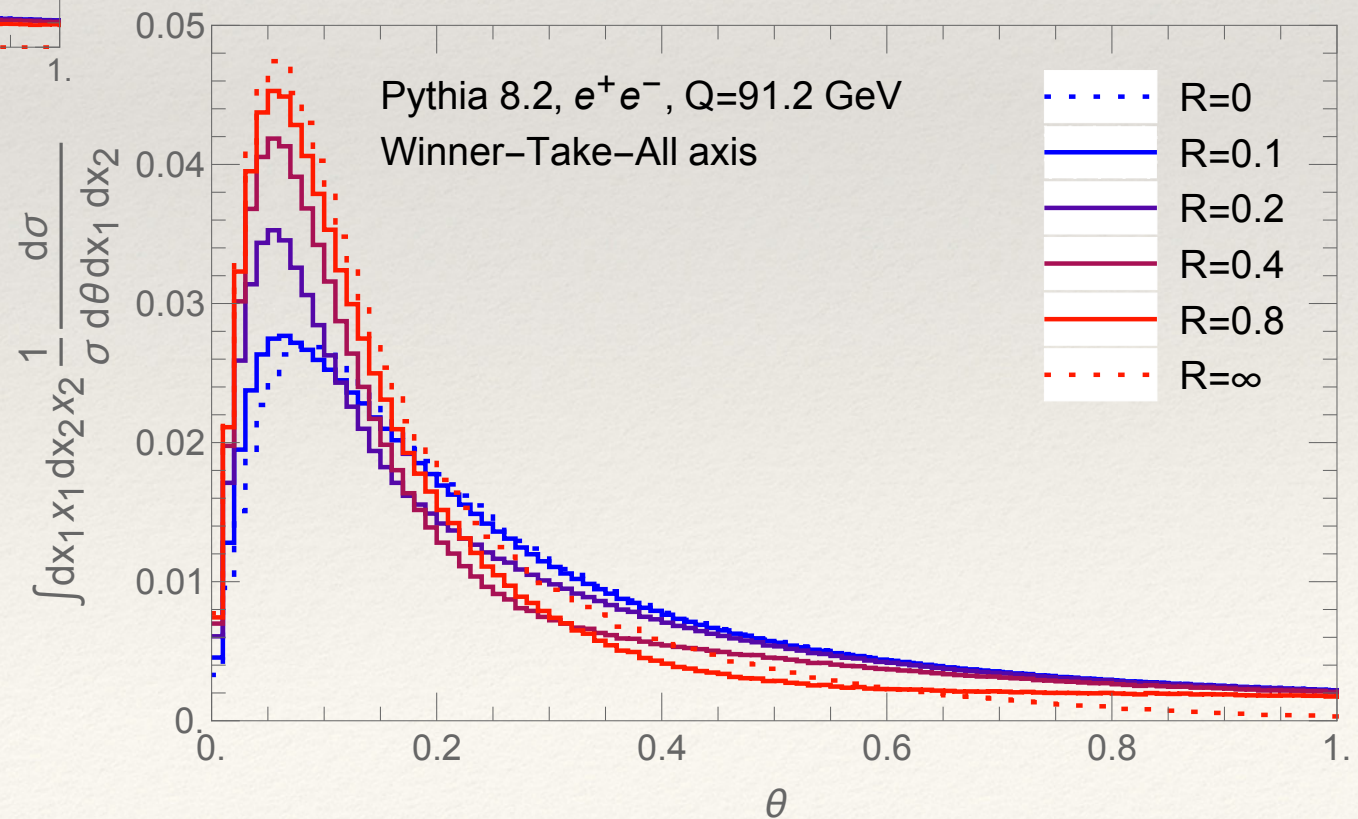
$$J_i^{[1] \text{WTA}} = 2\delta(1-z) \left\{ N_i + L_\mu \left[C'_i + C_i(\mathbf{1}_\zeta - L_\mu) \right] \right\}$$

A check from Pythia

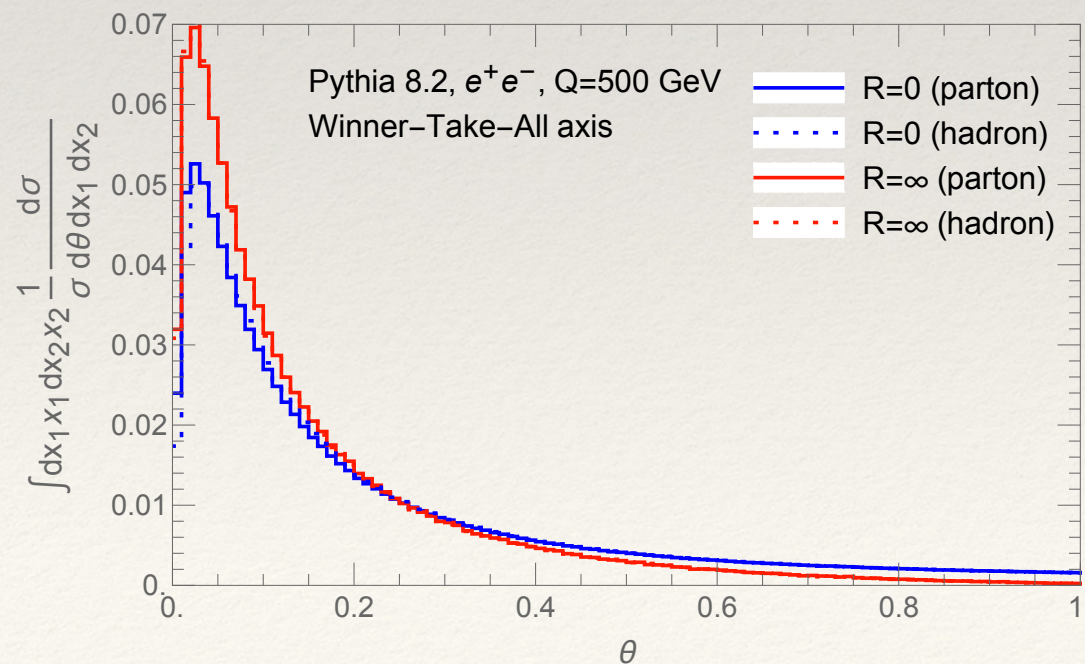
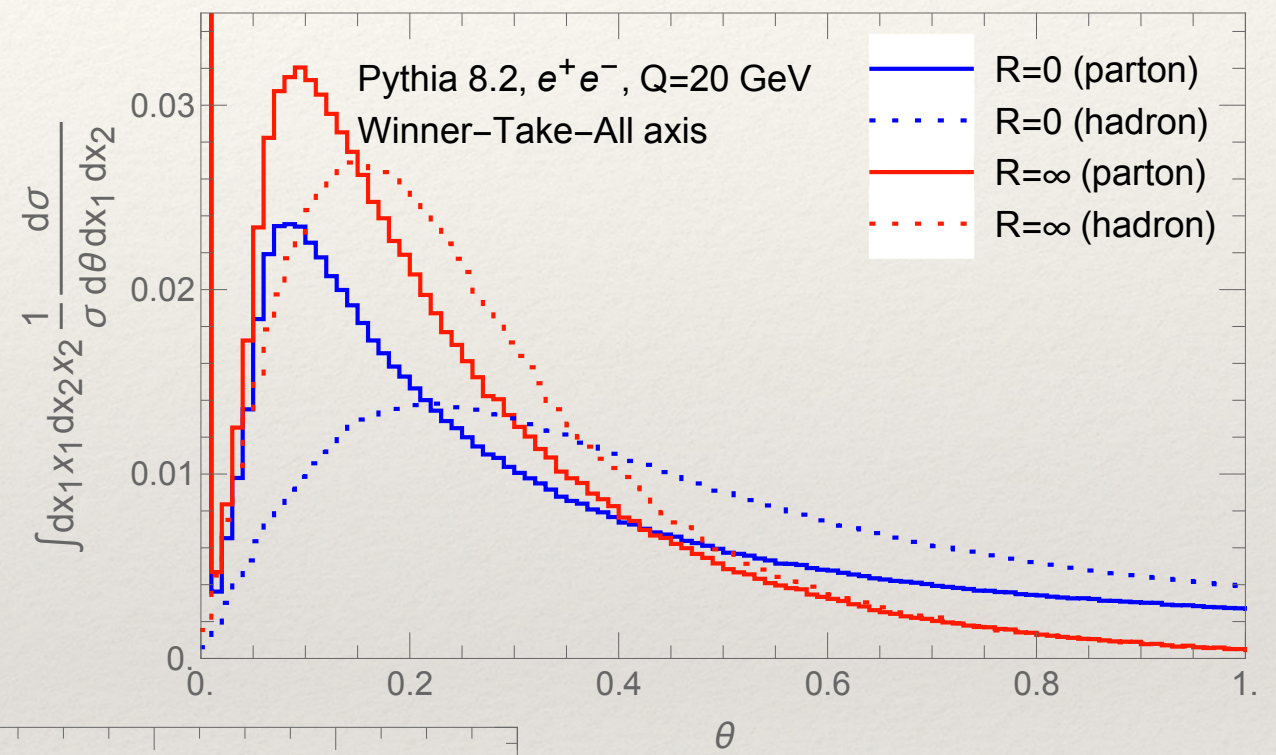
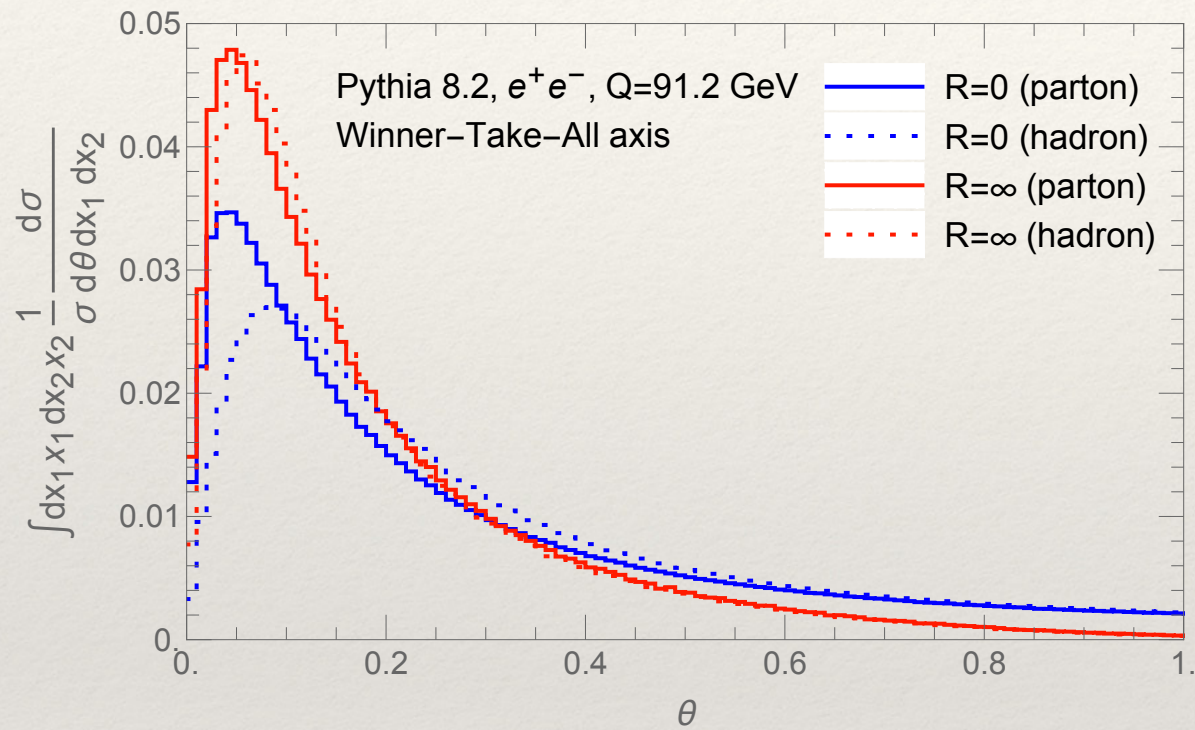


THE STANDARD JET AXIS GETS UNSTABLE FOR $R > 0.2$ AND SMALL ANGLES

THE WTA AXIS IS STABLE FOR ALL R



A check from Pythia: hadronization effects



Conclusions

We have observables and Jet TMDs whose (double-scale) evolution is dictated by the same soft factors as for hadrons

| Process / Axis | Standard Jet Axis | WTA |
|-----------------------------------|--|---|
| Hadron inside jet | Standard Hadron TMD, semi-inclusive TMD fragmenting jet function | DGLAP Hadron TMD, semi-inclusive TMD fragmenting jet function with WTA |
| 2-jet momentum de- correlation | Double-scale evolution for Jet TMDs; it works only for $R < 0.2$ | Double-scale evolution for Jet TMDs; it works only all R |