

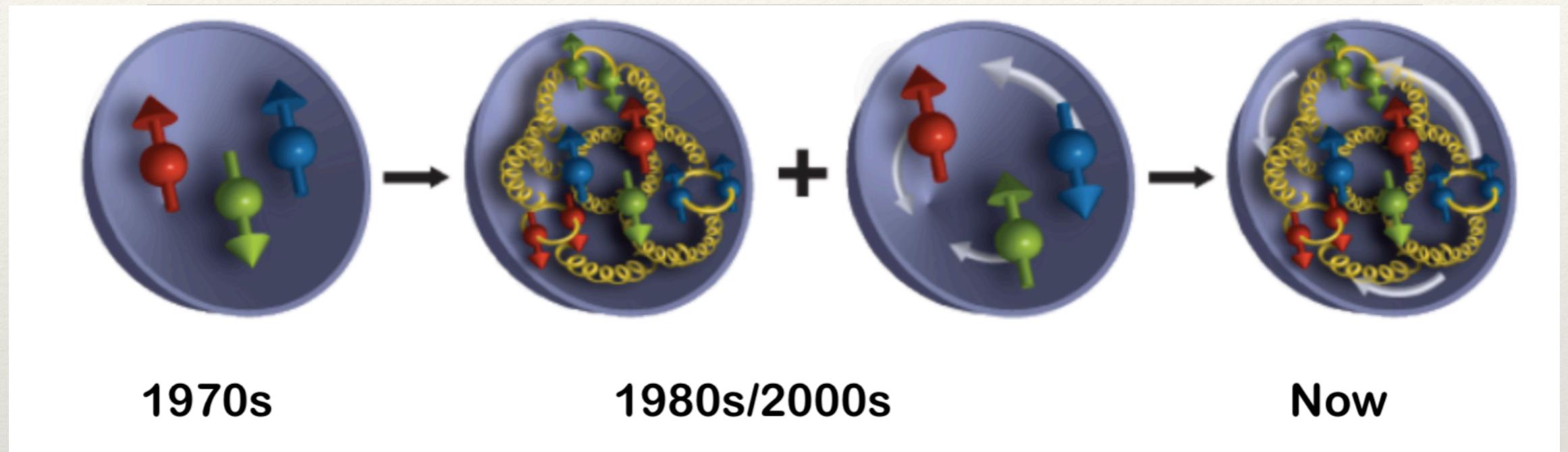


*Ignazio Scimemi (UCM)*

TMD extraction including  
higher order corrections: path  
dependence and precision

Results in collaboration with  
**Alexey Vladimirov (Regensburg)**  
(arXiv:1706.01473,...)  
and ongoing related work with  
**Valerio Bertone (Pavia),**

# Outline



- ❖ Overview of hadron structure concepts
- ❖ Factorization for TMDs
- ❖ 2-D Evolution
- ❖ Phenomenology



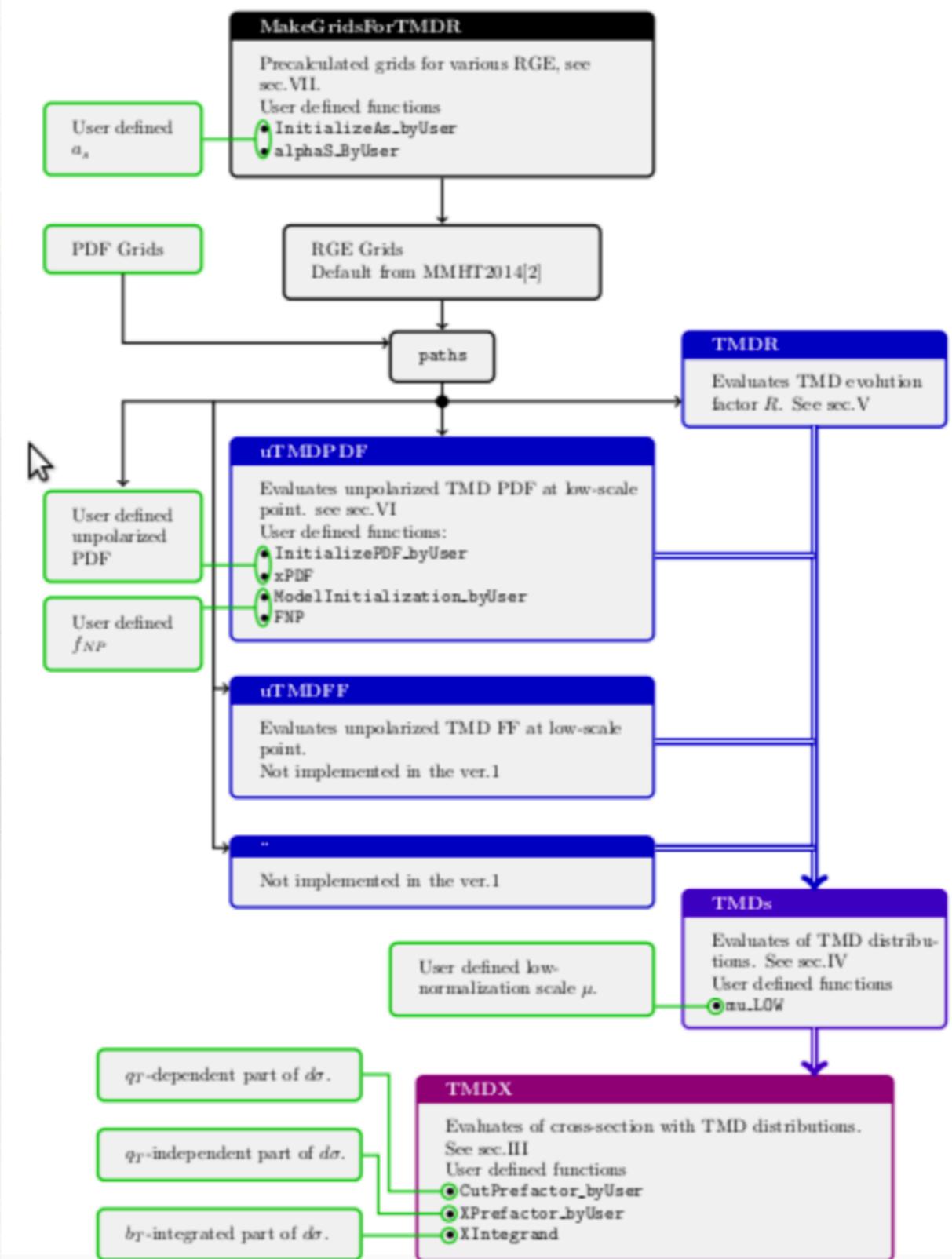
# arTeM[ide]

- FORTRAN 90 code
- Module structure
- Convolutions, evolution (LO,NLO,NNLO)
- Fourier to  $q_T$ -space, integrations over phase space
- Scale-variation ( $\zeta$ -prescription)
- User defined PDFs, scales,  $f_{NP}$
- Efficient code ( $\sim 10^9$  TMDs  $\sim 6.$  min at NNLO)

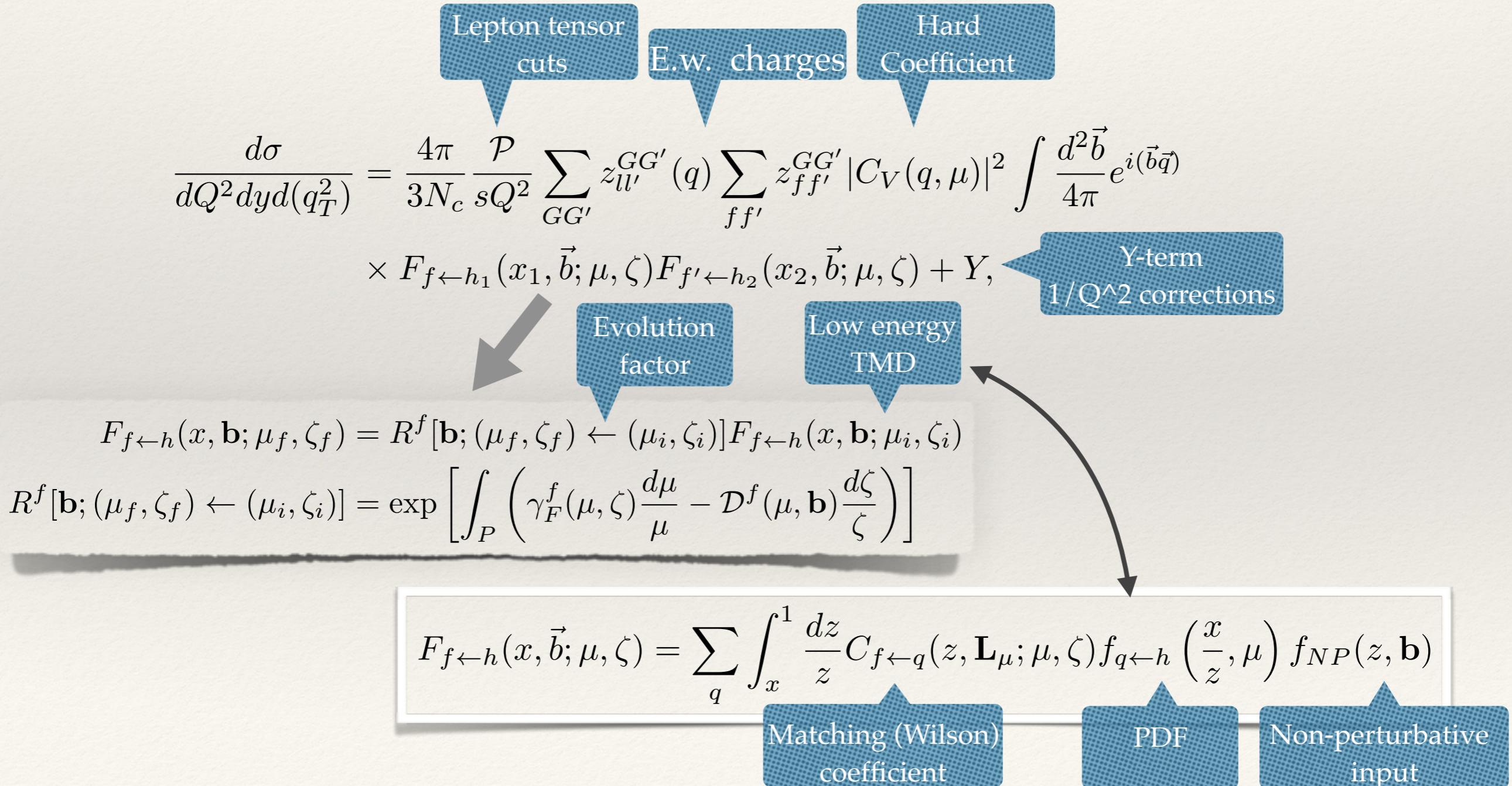
Currently ver 1.3

Available at: <https://teorica.fis.ucm.es/artemide>

Future plans: add modules for fragmentations, and polarized TMDs



# Cross section and TMD structure



# Cross section and TMD structure

$$\frac{d\sigma}{dQ^2 dy d(q_T^2)} = \frac{4\pi}{3N_c} \frac{\mathcal{P}}{sQ^2} \sum_{GG'} z_{ll'}^{GG'}(q) \sum_{ff'} z_{ff'}^{GG'} |C_V(q, \mu)|^2 \int \frac{d^2 \vec{b}}{4\pi} e^{i(\vec{b}\vec{q})}$$

$$\times F_{f \leftarrow h_1}(x_1, \vec{b}; \mu, \zeta) F_{f' \leftarrow h_2}(x_2, \vec{b}; \mu, \zeta) + \cancel{X}$$

Only small qT data

$$F_{f \leftarrow h}(x, \mathbf{b}; \mu_f, \zeta_f) = R^f[\mathbf{b}; (\mu_f, \zeta_f) \leftarrow (\mu_i, \zeta_i)] F_{f \leftarrow h}(x, \mathbf{b}; \mu_i, \zeta_i)$$

$$R^f[\mathbf{b}; (\mu_f, \zeta_f) \leftarrow (\mu_i, \zeta_i)] = \exp \left[ \int_P \left( \gamma_F^f(\mu, \zeta) \frac{d\mu}{\mu} - \mathcal{D}^f(\mu, \mathbf{b}) \frac{d\zeta}{\zeta} \right) \right]$$

$$F_{f \leftarrow h}(x, \vec{b}; \mu, \zeta) = \sum_q \int_x^1 \frac{dz}{z} C_{f \leftarrow q}(z, \mathbf{L}_\mu; \mu, \zeta) f_{q \leftarrow h} \left( \frac{x}{z}, \mu \right) f_{NP}(z, \mathbf{b})$$

$\zeta$ -prescription      Matching (Wilson) coefficient      PDF      Gaussian? Exponential?

# 2-D TMD evolution

COUPLED EVOLUTION OF TMD ...

TMD (standard) anomalous dimension

$$\mu^2 \frac{d}{d\mu^2} F_{f \leftarrow h}(x, b; \mu, \zeta) = \frac{\gamma_F(\mu, \zeta)}{2} F_{f \leftarrow h}(x, b; \mu, \zeta)$$

$$\zeta \frac{d}{d\zeta} F_{f \leftarrow h}(x, b; \mu, \zeta) = -\mathcal{D}(\mu, b) F_{f \leftarrow h}(x, b; \mu, \zeta)$$

TMD rapidity anomalous dimension

Collinear overlap

$$\zeta \frac{d}{d\zeta} \gamma_F(\mu, \zeta) = -\Gamma(\mu)$$

$$\mu \frac{d}{d\mu} \mathcal{D}(\mu, b) = \Gamma(\mu)$$



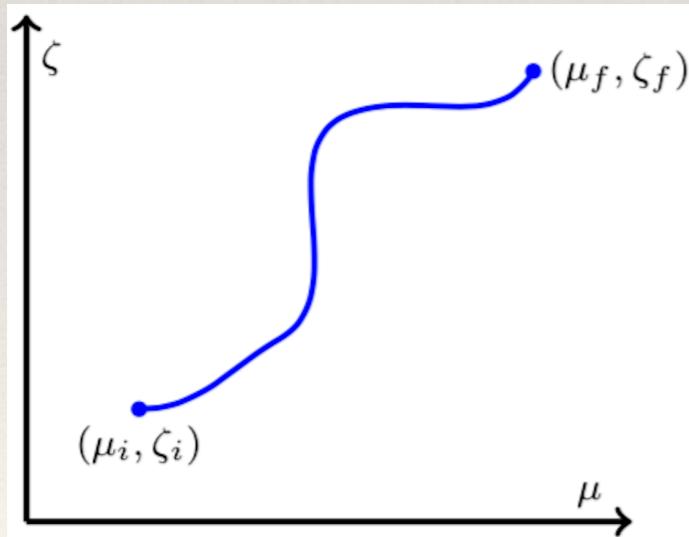
# Ambiguity in the TMD evolution

## COUPLED EVOLUTION OF TMD AND TRUNCATION OF THE PERTURBATIVE SERIES

Integrability Condition...

$$\zeta \frac{d}{d\zeta} \gamma_F(\mu, \zeta) = -\mu \frac{d}{d\mu} \mathcal{D}(\mu, b)$$

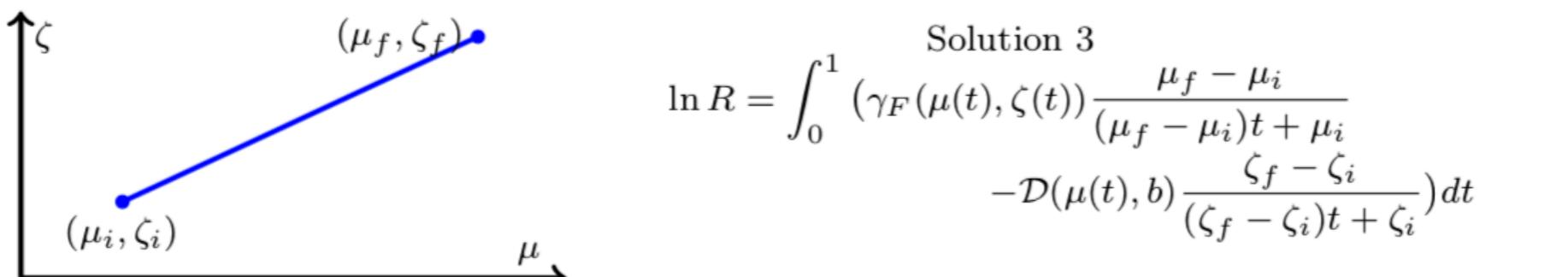
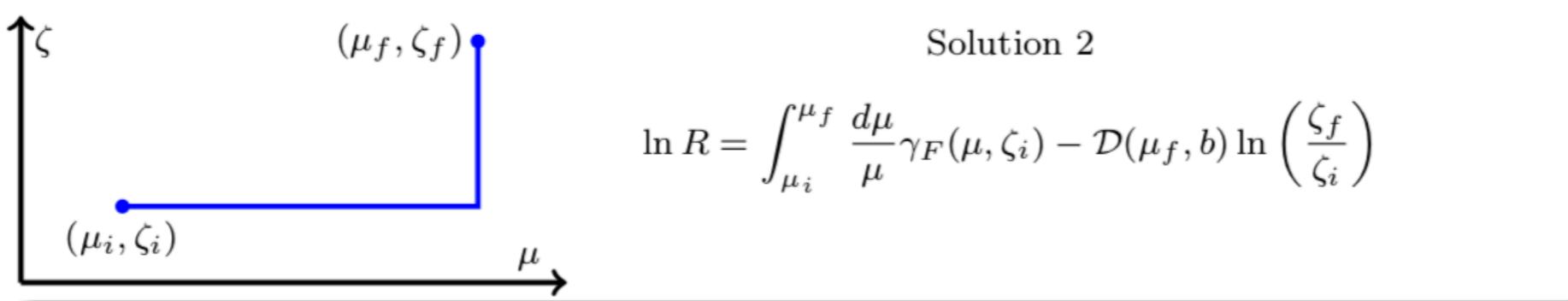
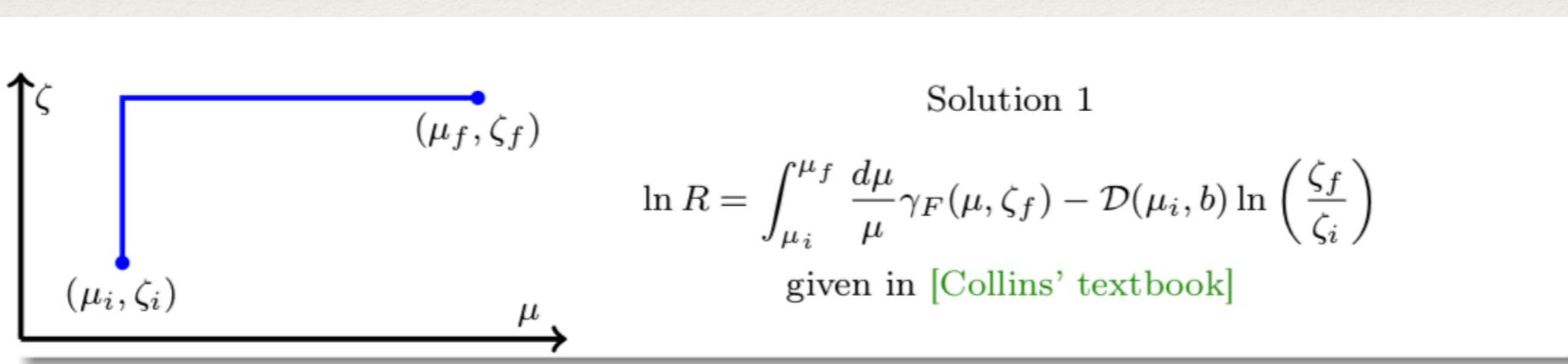
...ensures the path independence of the evolution factor...



$$R[b; (\mu_f, \zeta_f) \rightarrow (\mu_i, \zeta_i)] = \exp \left[ \int_P \left( \gamma_F(\mu, \zeta) \frac{d\mu}{\mu} - \mathcal{D}(\mu, b) \frac{d\zeta}{\zeta} \right) \right]$$

# Ambiguity in the TMD evolution

## COUPLED EVOLUTION OF TMD AND TRUNCATION OF THE PERTURBATIVE SERIES



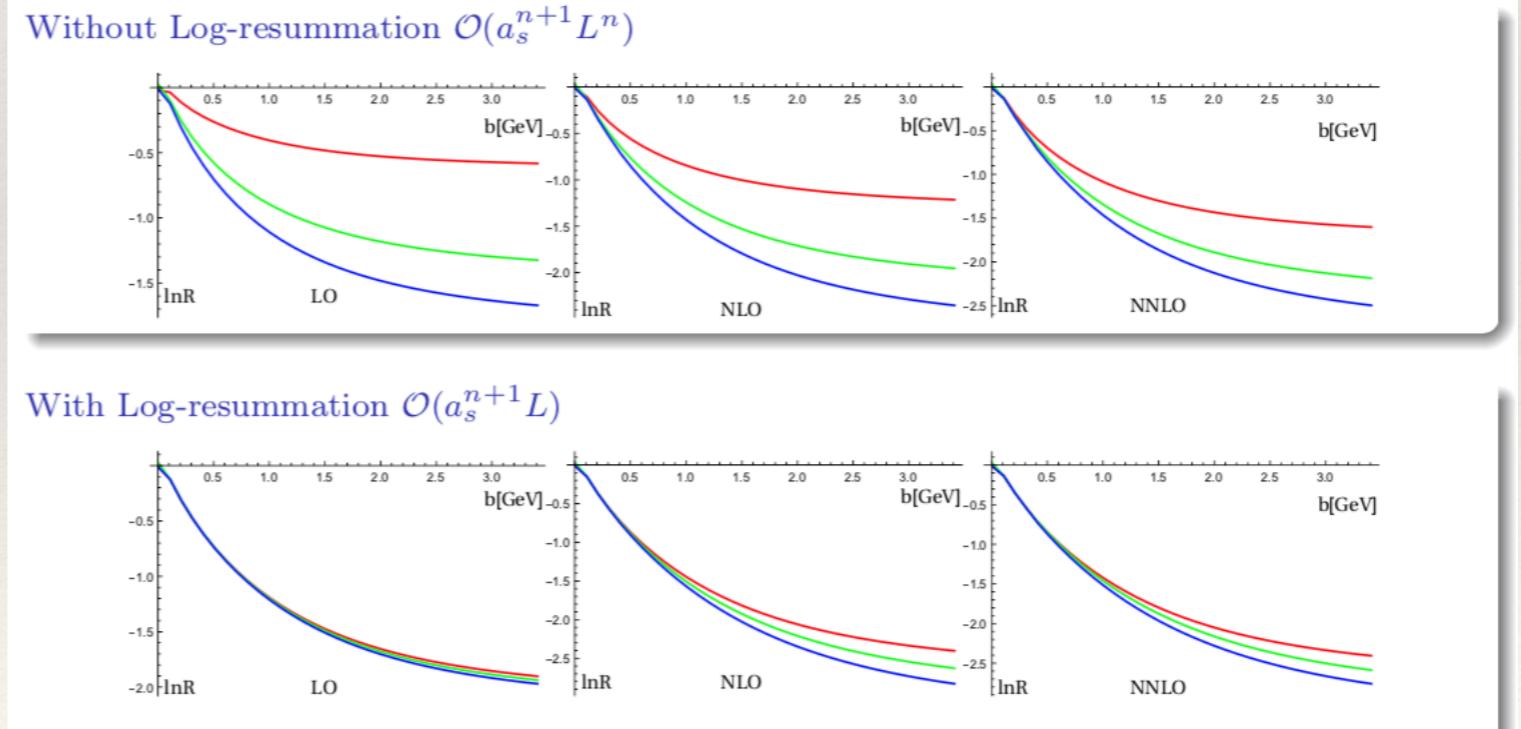
# Ambiguity in the TMD evolution

## COUPLED EVOLUTION OF TMD AND TRUNCATION OF THE PERTURBATIVE SERIES

In practice due to the truncation of the perturbative series:  
Transitivity and reversibility of evolution is lost

$$\zeta \frac{d}{d\zeta} \gamma_F(\mu, \zeta) \neq -\mu \frac{d}{d\mu} \mathcal{D}(\mu, b)$$

**For  $Q=M_z$  the solution path dependence enormous:  
at  $b=0.5$  an error of about 18%  
at N3LO on the un-resummed evolution factor R**



## 2D Evolution field: Notation and ideal case

The evolution scales  
are treated equally

$$\vec{\nu} = \left( \ln \frac{\mu^2}{1 \text{ GeV}^2}, \ln \frac{\zeta}{1 \text{ GeV}^2} \right)$$

Differentiation

$$\vec{\nabla} = \frac{d}{d\vec{\nu}} = (\mu^2 \frac{d}{d\mu^2}, \zeta \frac{d}{d\zeta}), \quad \mathbf{curl} = (-\zeta \frac{d}{d\zeta}, \mu^2 \frac{d}{d\mu^2})$$

Evolution field

$$\mathbf{E}(\vec{\nu}, b) = \left( \frac{\gamma_F(\vec{\nu})}{2}, -\mathcal{D}(\vec{\nu}, b) \right)$$

TMD Evolution

$$\vec{\nabla} F(x, b; \vec{\nu}) = \mathbf{E}(\vec{\nu}, b) F(x, b; \vec{\nu})$$

Integrability Condition  
and Scalar Potential

$$\vec{\nabla} \times \mathbf{E} = 0 \Rightarrow \mathbf{E}(\vec{\nu}, b) = \vec{\nabla} U(\vec{\nu}, b)$$

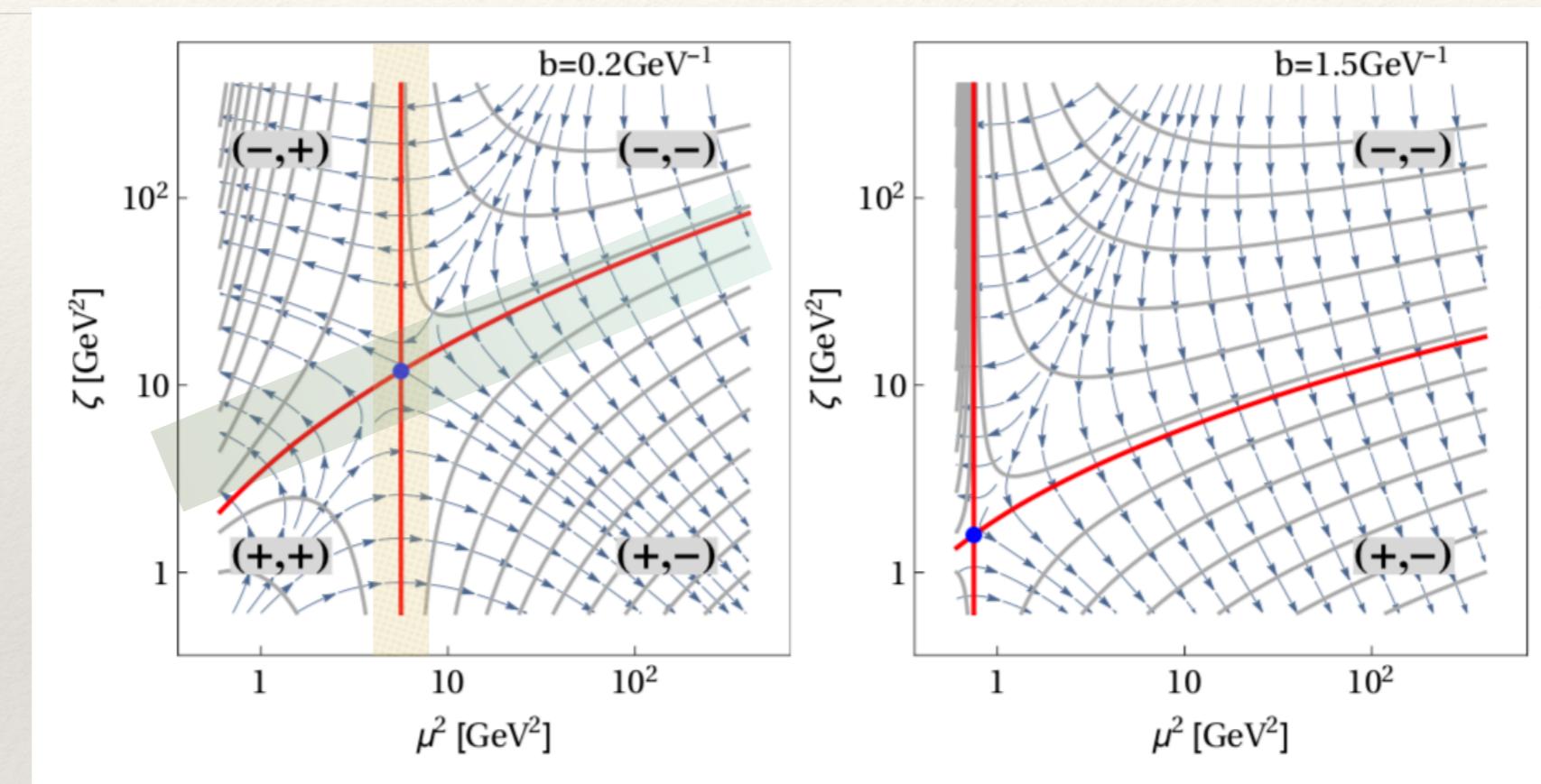
$$\ln R[b; \vec{\nu}_f \rightarrow \vec{\nu}_i] = U(\vec{\nu}_f, b) - U(\vec{\nu}_i, b)$$

with

Evolution kernel

$$U(\vec{\nu}, b) = \int^{\nu_1} \frac{\Gamma(s)s - \gamma_V(s)}{2} ds - \mathcal{D}(\vec{\nu}, b)\nu_2 + \text{const}(b)$$

## 2D Evolution field: Notation and ideal case



= saddle point

Singularities: Landau pole (on the left, not shown) and saddle point  $\mathbf{E}(\vec{\nu}_{\text{saddle}}, b) = \vec{0}$

Equipotential/null-evolution curves:  $\vec{\omega}(t, \vec{\nu}_B, b) = (t, \omega(t, \vec{\nu}_B, b)) \rightarrow \frac{d\vec{\omega}}{dt} \cdot \vec{\nabla}U(\vec{\omega}, b) = 0$

Special null-evolution curves:  $\mu = \mu_{\text{saddle}}$  and  $\vec{\nu}_B = \vec{\nu}_{\text{saddle}}$

# Truncation of the perturbative series

The truncation introduces a path difference

$$\delta\Gamma(\mu, b) = \Gamma(\mu) - \mu \frac{d\mathcal{D}(\mu, b)}{d\mu},$$

$$\delta\Gamma^{(N)} = 2 \sum_{n=1}^N \sum_{k=0}^n n \bar{\beta}_{n-1}(a_s) a_s^{n-1} d^{(n,k)} \mathbf{L}_\mu^k$$

$$\text{with } \bar{\beta}_n(a_s) = \beta(a_s) - \sum_{k=0}^{n-1} \beta_k a_s^{k+2}$$

$$\mathbf{L}_\mu = \ln \left( \frac{X^2 b^2}{4e^{-2\gamma_E}} \right)$$

$\delta\Gamma^{(N)} \sim \mathcal{O}(a_s^{N+1} \mathbf{L}_\mu^N)$  with perturbative  $D$

$\delta\Gamma^{(N)} \sim \mathcal{O}(a_s^{N+1} \mathbf{L}_\mu)$  with resummed  $D$

$$\ln \frac{R[b; \{\mu_1, \zeta_1\} \xrightarrow{P_1} \{\mu_2, \zeta_2\}]}{R[b; \{\mu_1, \zeta_1\} \xrightarrow{P_2} \{\mu_2, \zeta_2\}]} = \frac{1}{2} \int_{\Omega(P_1 \cup P_2)} d^2\nu \delta\Gamma(\vec{\nu}, b) = \int_{\mu_2}^{\mu_1} \frac{d\mu}{\mu} \delta\Gamma(\mu, b) \ln \left( \frac{\zeta_1(\mu)}{\zeta_2(\mu)} \right)$$

The path dependence is enhanced by the difference in rapidity scale

At large value of impact parameter the breaking of integrability condition becomes crucial

# Recovering path independence

Helmholtz decomposition  
of evolution fields

Basic properties  
of evolution fields

Scalar potentials

$$\mathbf{E}(\vec{\nu}, b) = \tilde{\mathbf{E}}(\vec{\nu}, b) + \Theta(\vec{\nu}, b)$$

$$\operatorname{curl} \tilde{\mathbf{E}} = 0, \quad \vec{\nabla} \cdot \vec{\Theta} = 0, \quad \tilde{\mathbf{E}} \cdot \Theta = 0.$$

$$\tilde{\mathbf{E}}(\vec{\nu}, b) = \vec{\nabla} \tilde{U}(\vec{\nu}, b) \quad \Theta(\vec{\nu}, b) = \operatorname{curl} V(\vec{\nu}, b)$$

$$\operatorname{curl} \mathbf{E} = \operatorname{curl} \Theta = \frac{\delta \Gamma(\vec{\nu}, b)}{2} \neq 0$$

Ideally one could repair the truncation using decomposition of the evolution field

THE INTEGRABILITY CONDITION IS RE-ESTABLISHED DEFINING THE EVOLUTION KERNEL AS

$$\ln R[b; \vec{\nu}_f \rightarrow \vec{\nu}_i] = \tilde{U}(\vec{\nu}_f, b) - \tilde{U}(\vec{\nu}_i, b)$$

$$\nabla^2 \tilde{U}(\vec{\nu}, b) = \frac{1}{2} \frac{d\gamma_F(\vec{\nu})}{d\nu_1}$$

However in order to fix completely the evolution potential one needs boundary condition for the evolution field:  
at the moment no theoretically solid non-perturbative input is known

# Recovering path independence

We modify anomalous dimensions such that integrability restored

$$\mu \frac{d\mathcal{D}(\mu, b)}{d\mu} = -\zeta \frac{d\gamma_F(\mu, \zeta)}{d\zeta}$$

It can be done from both sides of the equation.

Improved  $\mathcal{D}$

Facilitate

$$\mu \frac{d\mathcal{D}}{d\mu} = \Gamma.$$

by

$$\mathcal{D}(\mu, b) = \int_{\mu_0}^{\mu} \frac{d\mu}{\mu} \Gamma(\mu) + \mathcal{D}(\mu_0, b)$$

- In the spirit of [Collins' text book].
- Already used in many studies
- However, it is not the best way

Improved  $\gamma$

We set

$$\zeta \frac{d\gamma_F}{d\zeta} \equiv -\mu \frac{d\mathcal{D}}{d\mu} = \delta\Gamma - \Gamma$$

Or

$$\gamma_F(\mu, \zeta) \rightarrow \gamma_M(\mu, \zeta, b)$$

$$\gamma_M = (\Gamma - \delta\Gamma) \ln \left( \frac{\mu^2}{\zeta} \right) - \gamma_V$$

- Completely self consistent
- Very natural



# Improved D scenario

$$\mathcal{D}(\mu, b) = \int_{\mu_0}^{\mu} \frac{d\mu'}{\mu'} \Gamma(\mu') + \mathcal{D}(\mu_0, b) \longrightarrow \tilde{U}(\vec{\nu}, b; \mu_0) = \int_{\ln \mu_0^2}^{\nu_1} \frac{\Gamma(s)(s - \nu_2) - \gamma_V(s)}{2} ds - \mathcal{D}(\mu_0, b)\nu_2 + \text{const}(b)$$

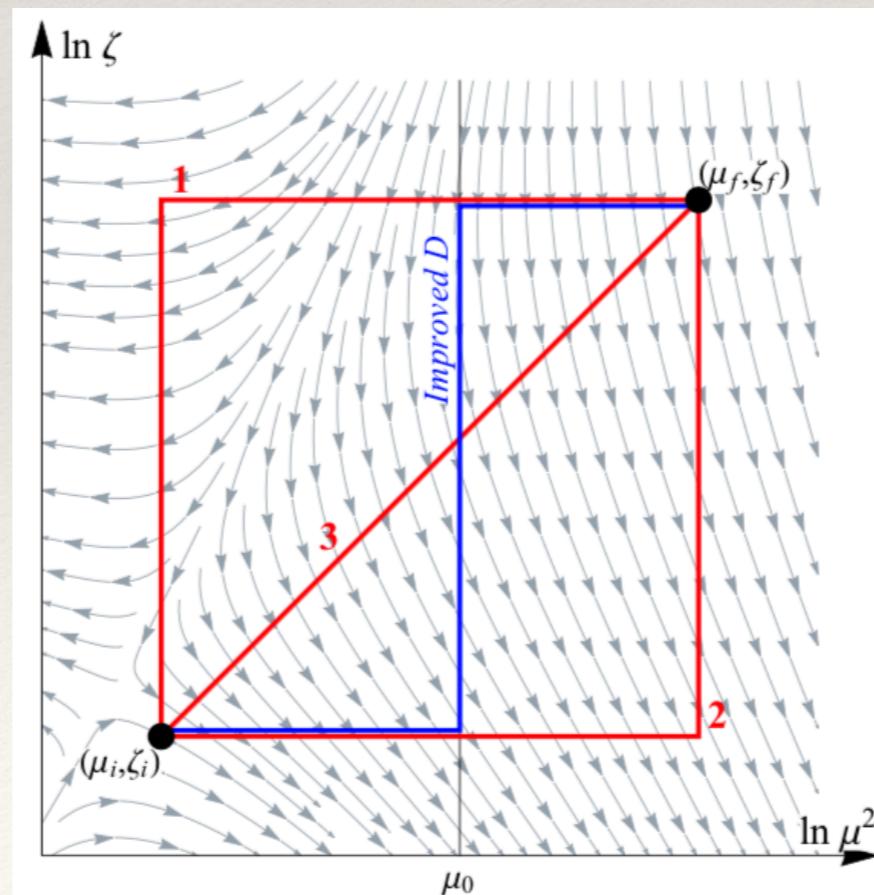
The truncation effects should be minimized by the choice of  $\mu_0$

$$\ln R[b; (\mu_f, \zeta_f) \rightarrow (\mu_i, \zeta_i); \mu_0] = \int_{\mu_i}^{\mu_f} \frac{d\mu}{\mu} \left( \Gamma(\mu) \ln \left( \frac{\mu^2}{\zeta_f} \right) - \gamma_V(\mu) \right) - \int_{\mu_0}^{\mu_i} \frac{d\mu}{\mu} \Gamma(\mu) \ln \left( \frac{\zeta_f}{\zeta_i} \right) - \mathcal{D}(\mu_0, b) \ln \left( \frac{\zeta_f}{\zeta_i} \right).$$

This is a mixture of solution 1 and 2.

The **solution dependence** is parameterized by  $\mu_0$

In order to compare fits one should agree on a conventional  $\mu_0$  scale



The minimization occurs only when one finds a  $\mu_0$  such that  
 $\delta \Gamma(\mu_0, b) = 0$

# Improved $\gamma$ scenario

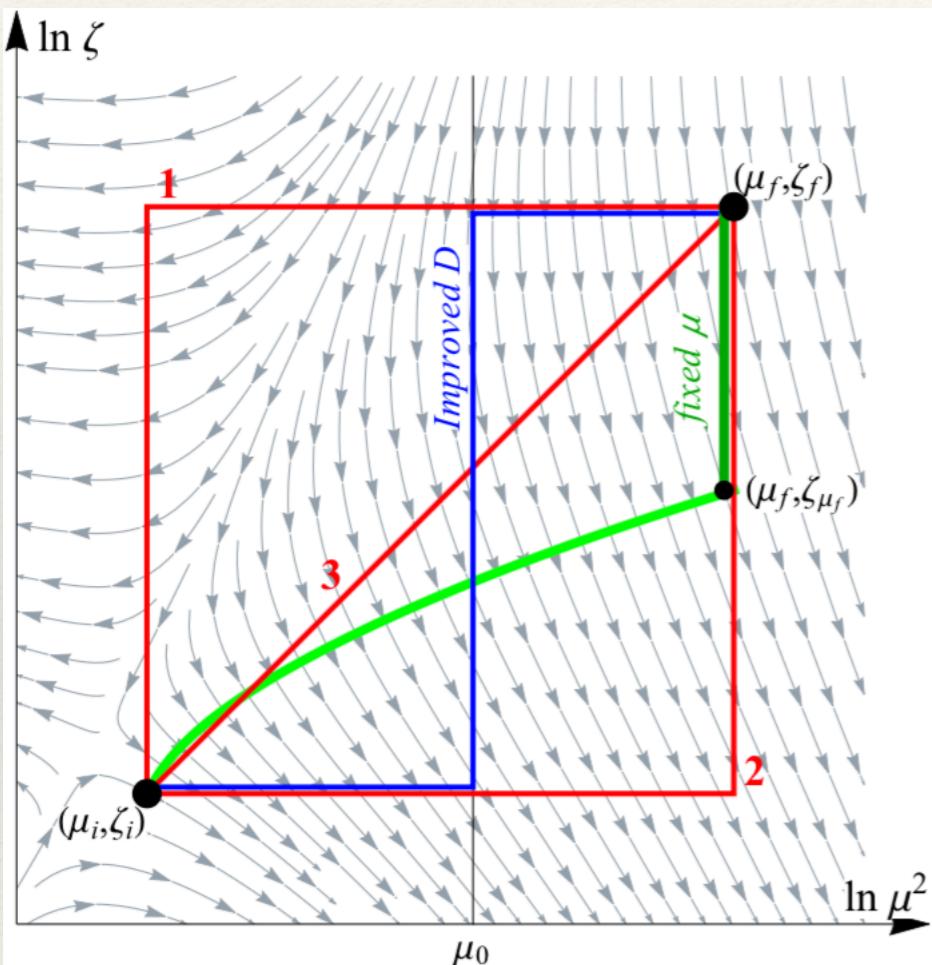
$$\gamma_M(\mu, \zeta, b) = (\Gamma(\mu) - \delta\Gamma(\mu, b))\mathbf{l}_\zeta - \gamma_V(\mu) \longrightarrow \tilde{U}(\vec{\nu}, b) = \int^{\nu_1} \frac{(\Gamma(s) - \delta\Gamma(s, b))s - \gamma_V(s)}{2} ds - \mathcal{D}(\vec{\nu}, b)\nu_2 + const(b)$$

$$\ln R[b; (\mu_f, \zeta_f) \rightarrow (\mu_i, \zeta_i)] = - \int_{\mu_i}^{\mu_f} \frac{d\mu}{\mu} (2\mathcal{D}(\mu, b) + \gamma_V(\mu)) + \mathcal{D}(\mu_f, b) \ln \left( \frac{\mu_f^2}{\zeta_f} \right) - \mathcal{D}(\mu_i, b) \ln \left( \frac{\mu_i^2}{\zeta_i} \right)$$

## CLEAR ADVANTAGES:

- NO MORE THE INTERMEDIATE SCALE  $\mu_0$
- PATH INDEPENDENCE
- SIMPLICITY
- WE ACHIEVE A CLEAR SEPARATION OF EVOLUTION AND NON-PERTURBATIVE PART OF THE TMD

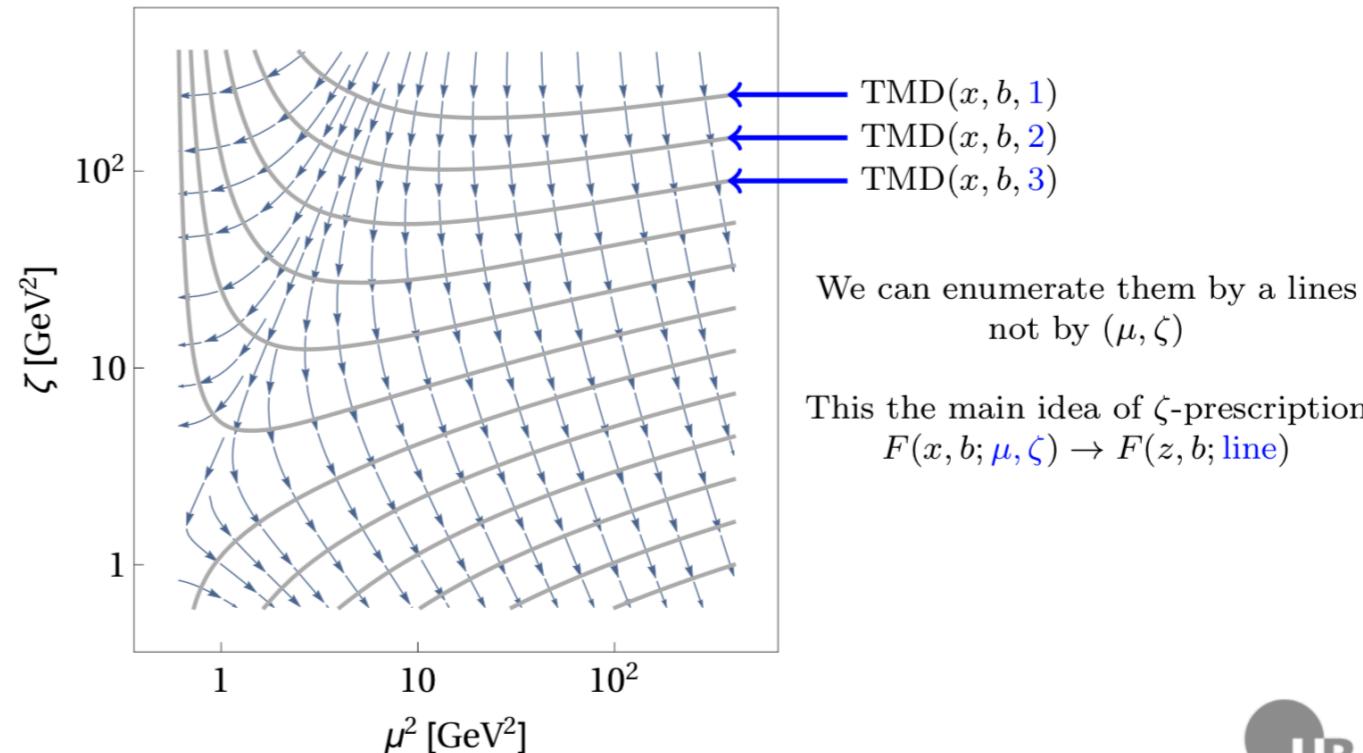
# Equivalent TMDs: equipotential lines



We can provide evolution first on an *equipotential line* and then on a vertical line.

The 2-D evolution just connects TMDs on different equipotential lines

TMD distributions on the same equipotential line are equivalent.





# TMD on equipotential lines

The TMDs one equipotential lines are not evolved so one can define a TMD by a single parameter line

$$F(x, b; \vec{\nu}_B) = F(x, b; \vec{\nu}'_B), \quad \vec{\nu}'_B \in \vec{\omega}(\vec{\nu}_B, b).$$

ONE CAN HAVE AN EVOLUTION ONLY WHEN MOVING BETWEEN DIFFERENT LINES

$$F(x, b; \vec{\nu}_B) = R[b; \vec{\nu}_B \rightarrow \vec{\nu}'_B] F(x, b; \vec{\nu}'_B)$$

Outcome: the modeling of the non-perturbative part of the TMD does not depend anymore on the relation between renormalization scale and impact parameter.

Question: Is there a preferred line?

Left for Technical discussion

# The optimal TMD distribution

There is a consistency constraint in the TMD matching to PDFs

$$F_{f \rightarrow k}(x, b; \vec{\nu}_B) = \sum_n \sum_{f'} C_{f \rightarrow f'}^{(n)}(x, b, \vec{\nu}_B, \mu_{\text{OPE}}) \otimes f_{f' \rightarrow h}^{(n)}(x, \mu_{\text{OPE}})$$

The values of  $\mu_{\text{OPE}}$  are restricted to the values of  $\mu$  taken along the null-evolution curve

if  $\nu_{B,1} < \ln \mu_{\text{saddle}}^2 \Rightarrow \mu_{\text{OPE}} < \mu_{\text{saddle}},$

if  $\nu_{B,1} > \ln \mu_{\text{saddle}}^2 \Rightarrow \mu_{\text{OPE}} > \mu_{\text{saddle}},$

if  $\vec{\nu}_B = (\ln \mu_{\text{saddle}}^2, \ln \zeta_{\text{saddle}}) \Rightarrow \mu_{\text{OPE}} \text{ unrestricted}$



# $\zeta$ -prescription

We have just to evolve between different equipotential/null-evolution line

$$F(x, b; \mu_f, \zeta_f) = R[b; (\mu_f, \zeta_f) \rightarrow (\mu_f, \zeta_{\mu_f}(\vec{\nu}_B, b))] F(x, b; \vec{\nu}_B)$$

This is realized choosing  $\zeta_\mu(b)$  such that

$$\frac{\gamma_F(\mu, \zeta_\mu(b))}{2\mathcal{D}(\mu, b)} = \frac{\mu^2}{\zeta_\mu(b)}$$

$$\mu^2 \frac{dF(x, \mathbf{b}; \mu, \zeta_\mu)}{d\mu^2} = 0.$$

# Perturbative orders...

name	$\mathcal{D}$	$\gamma_V$	$H$	$C_{f \leftarrow f'}$	$a_s(\text{run})$	PDF (evolution)
LO	$a_s^1$	$a_s^1$	$a_s^0$	$a_s^0$	lo	lo
NLO	$a_s^2$	$a_s^2$	$a_s^1$	$a_s^1$	nlo	nlo
NNLO	$a_s^3$	$a_s^3$	$a_s^2$	$a_s^2$	nnlo	nnlo

...Theoretical uncertainties  
in QCD analysis...

MATCHING  
SCALES

$$\frac{d\sigma}{dQ^2 dy d(q_T^2)} = \frac{4\pi}{3N_c} \frac{\mathcal{P}}{sQ^2} \sum_{GG'} z_{ll'}^{GG'}(q) \sum_{ff'} z_{ff'}^{GG'} \int \frac{d^2 \vec{b}}{4\pi} e^{i(\vec{b}\vec{q})} |C_V(Q, \textcolor{red}{c}_2 Q)|^2 \left\{ R^f[\vec{b}; (\textcolor{red}{c}_2 Q, Q^2) \rightarrow (\textcolor{red}{c}_3 \mu_i, \zeta_{c_3 \mu_i}); \textcolor{red}{c}_1 \mu_i] \right\} \\ \times F_{f \leftarrow h_1}(x, \vec{b}; \textcolor{red}{c}_4 \mu_{\text{OPE}}, \zeta_{c_4 \mu_{\text{OPE}}}) F_{f' \leftarrow h_2}(x, \vec{b}; \textcolor{red}{c}_4 \mu_{\text{OPE}}, \zeta_{c_4 \mu_{\text{OPE}}})$$

Small b  
Scale

In the implementation we must choose matching prescriptions such that the perturbative series is as convergent as possible, undesired power corrections are not introduced

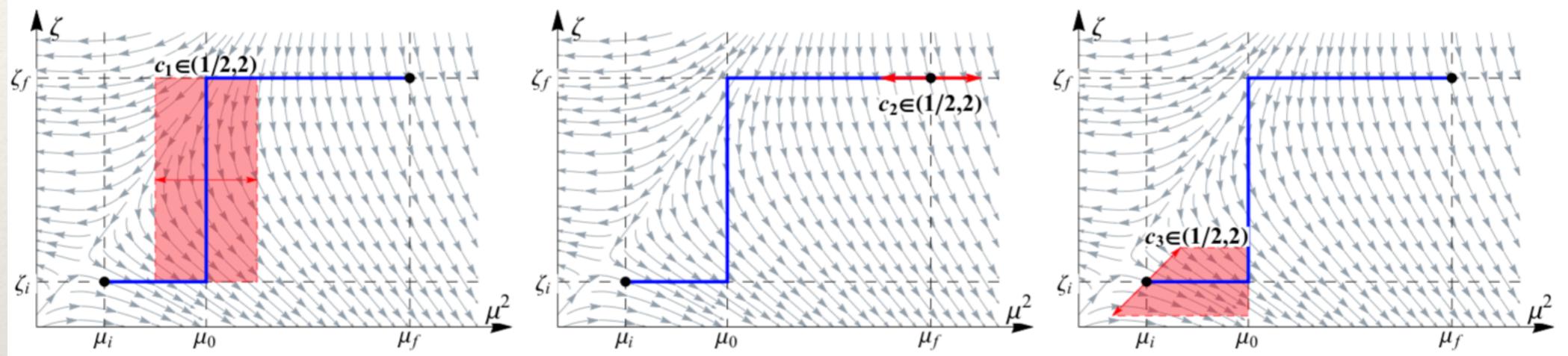
Hard  
Scale

Low  
Scale

Rapidity  
Evolution

Parameters and quality of the fits depend strongly on the choices made for the implementation

# Details of scale variations

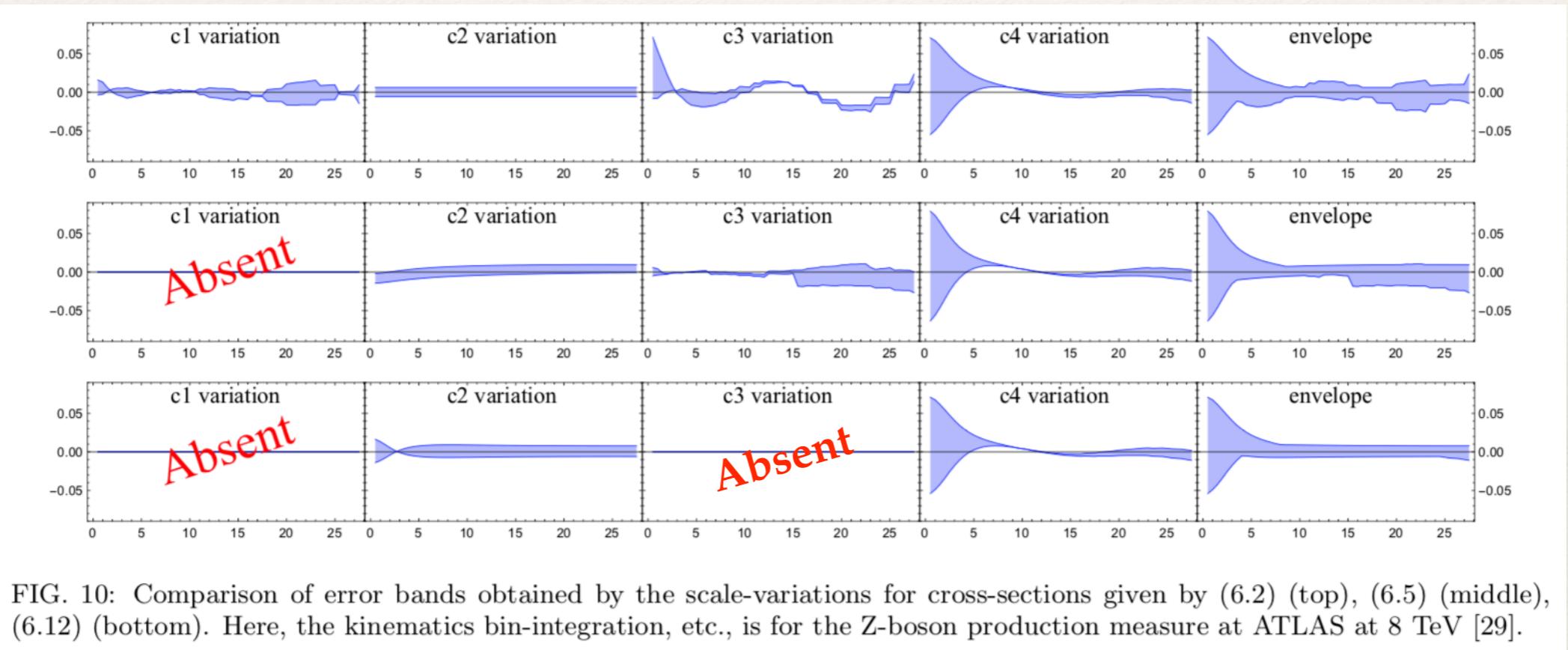


- $c_1$  measure only solution dependence
- $c_2$  measure mismatch between  $H$  and  $R$  + solution dependence
- $c_3$  measure mismatch between  $F$  and  $R$  + solution dependence
- $c_4$  measure mismatch between  $C$  and  $f$

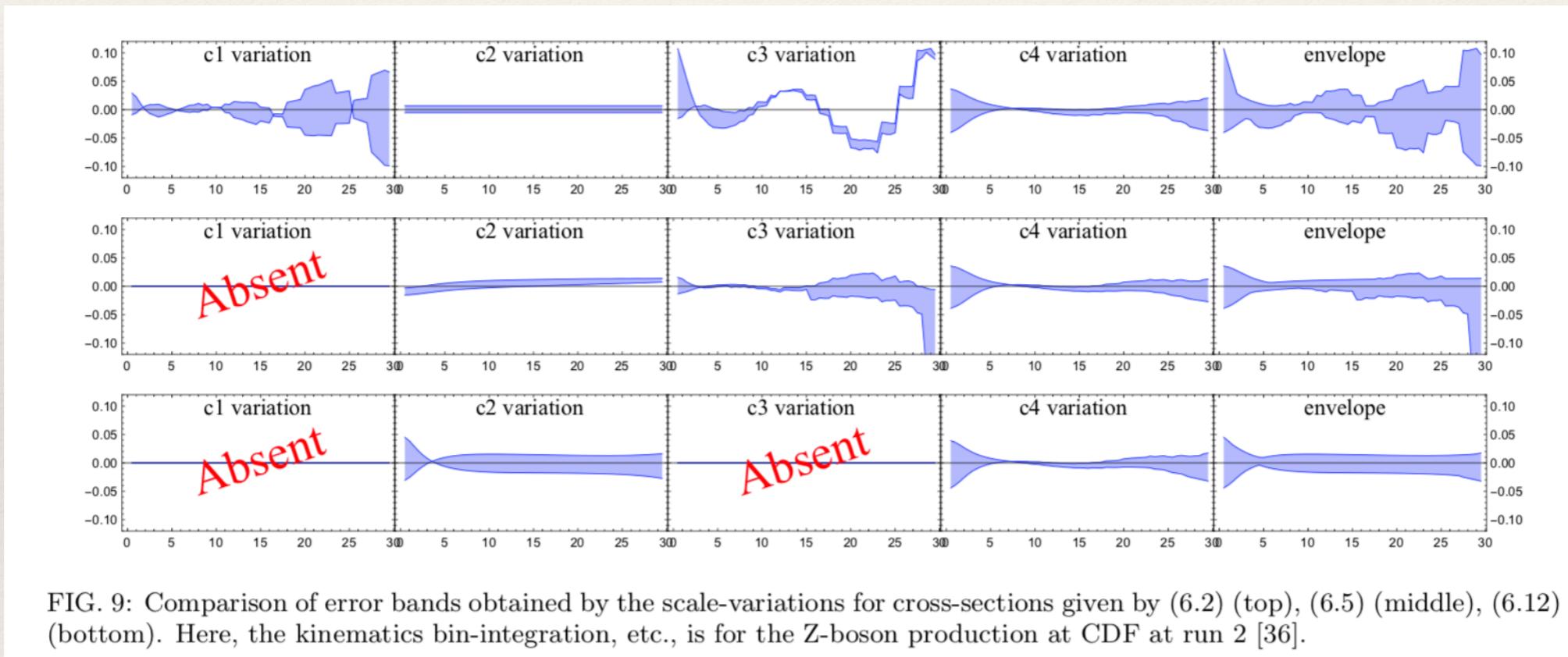
Eliminated by gamma-scenario

Included in  $c_2$  by optimal TMD definition

# A new error analysis: LHC



# A new error analysis: CDF



# A new error analysis: E288

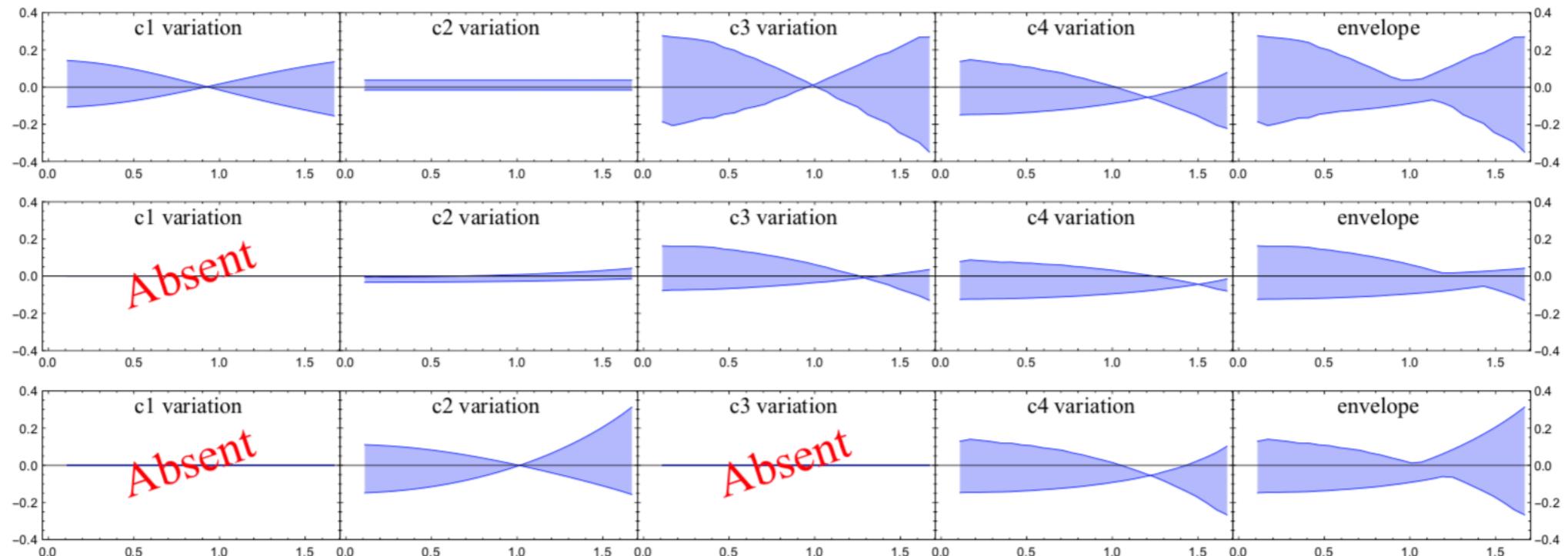


FIG. 11: Comparison of error bands obtained by the scale-variations for cross-sections given by (6.2) (top), (6.5) (middle), (6.12) (bottom). Here, the kinematics bin-integration, etc., is for Drell-Yan process measured at E288 experiment at  $E_{\text{beam}} = 200\text{GeV}$  and  $Q = 6 - 7\text{GeV}$  [38].

# Modeling non-perturbative inputs for TMD extraction

The TMD modeling is not very constrained

$$F_{q \leftarrow h}(x, \mathbf{b}) = \int_x^1 \frac{dz}{z} \sum_f C_{q \leftarrow f}(z, \mathbf{b}; \mu, \zeta_\mu) f_{f \leftarrow h}\left(\frac{x}{z}, \mu\right) f_{NP}(z, \mathbf{b})$$

Perturbative Wilson coefficient matching

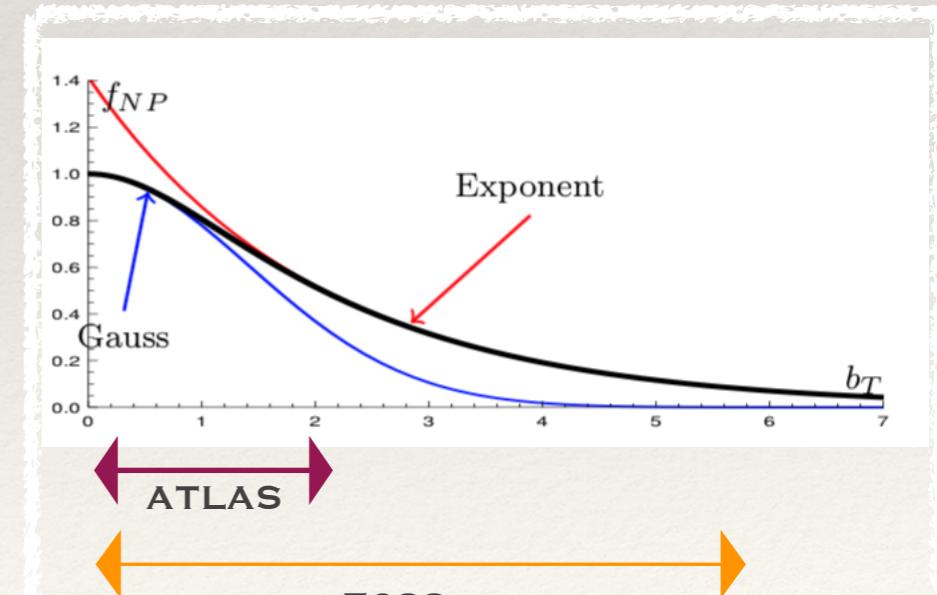
PDF

Non-perturbative non-asymptotic part

Asymptotic limit of TMD  
for large transverse momentum

+ a nonperturbative contribution to evolution factor

$$D^{NP} \sim g_K b b^*$$



# Data and limit of TMD analysis

The limits of the TMD analysis are defined by the limit of factorization and are independent of the non-perturbative parametrization of TMDs or perturbative order

$$\delta_t = q_t/M$$

For high energy data we find  $\delta_t \lesssim 0.2$

ATLAS experiment has an extraordinary precision:  
is this criterium sufficient?

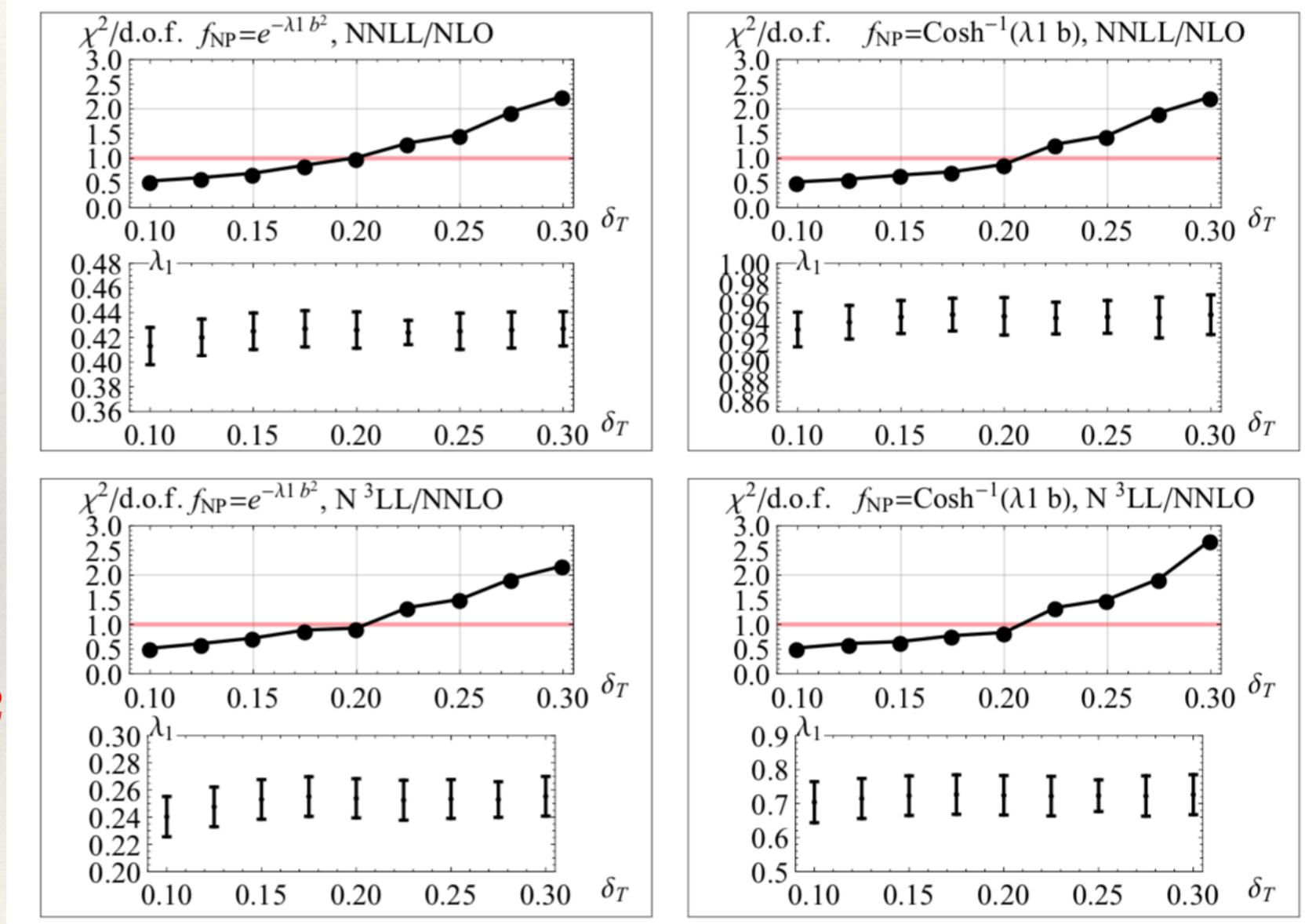


Table from arXiv:1706:01473

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# Statistics

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$\chi^2$

minimization requires the analysis of experimental correlations

$$\text{Experimental result (i)} \simeq m_i \pm \sigma_{i,\text{stat}} \pm \sigma_{i,\text{unc}} \pm \sum_{k=1}^N \sigma_{i,\text{corr}}^{(k)}$$

$m_i$  = central value of measurement i

$\sigma_{i,\text{stat}}$  = uncorrelated statistical error

$\sigma_{i,\text{unc}}$  = uncorrelated systematic error

$\sigma_{i,\text{corr}}$  = correlated error

All this information is provided by experiments and should be used to make the correlation matrix

# Statistics

$\chi^2$

minimization requires the analysis of experimental correlations

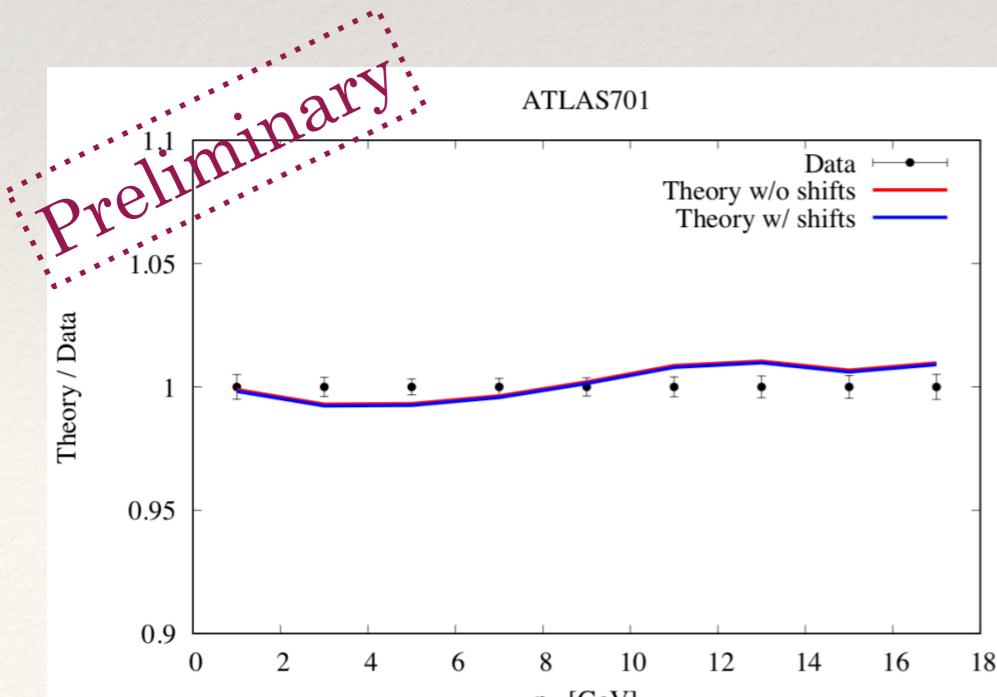
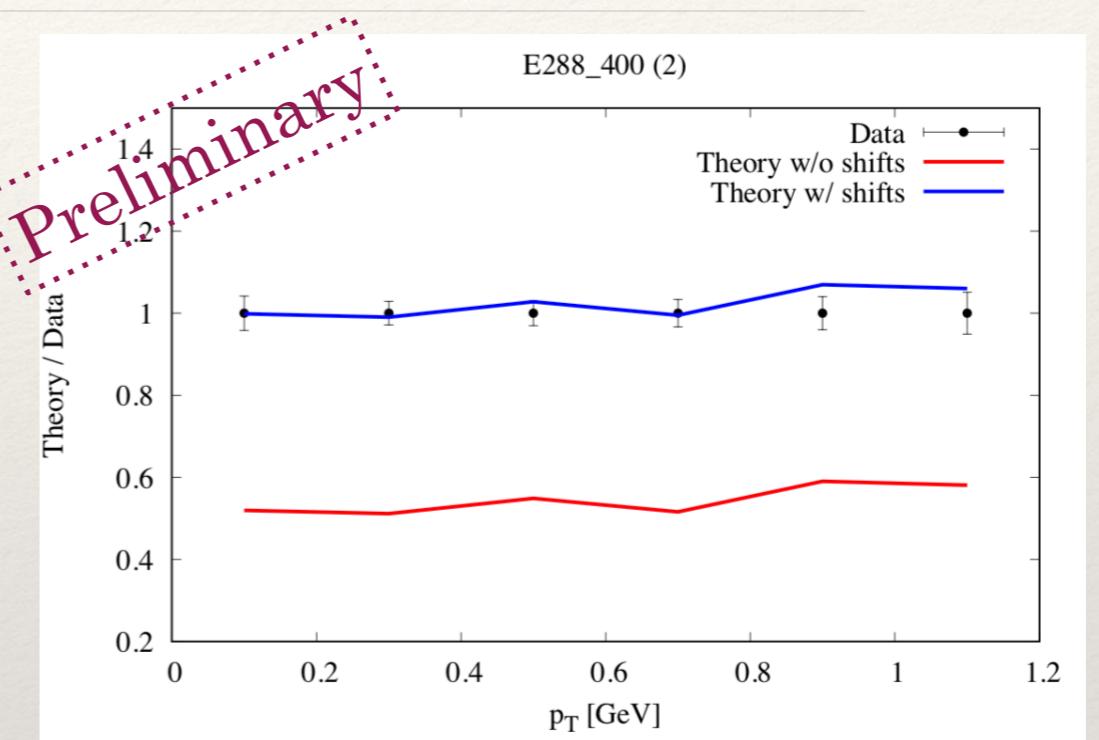
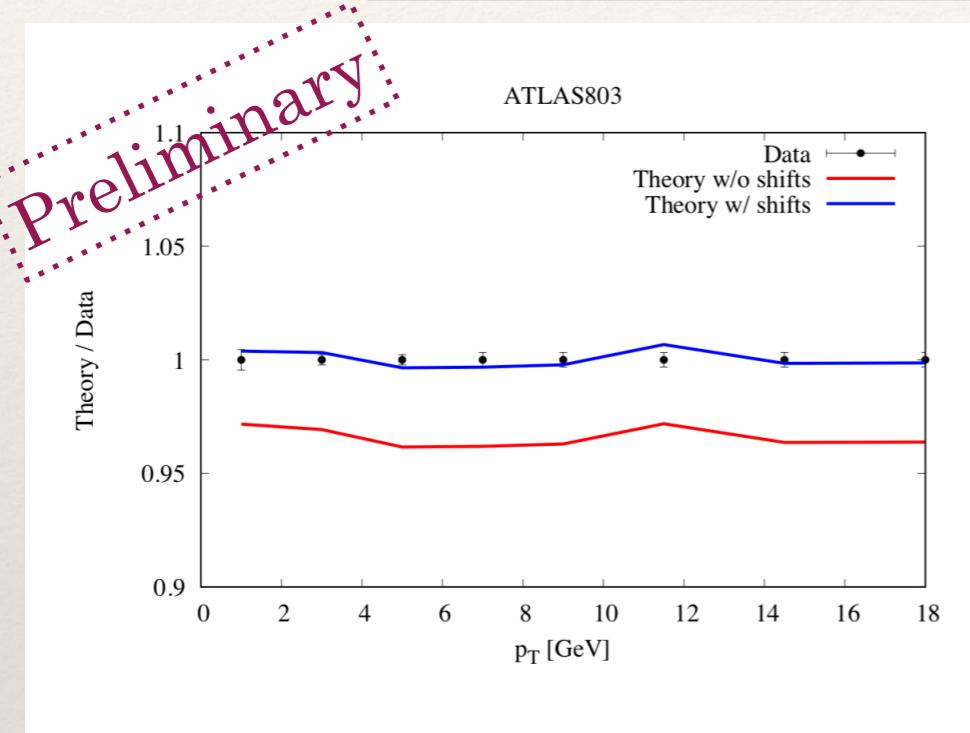
$$V_{ij} = (\sigma_{i,stat}^2 + \sigma_{i,unc}^2)\delta_{ij} + \sum_{i=1}^N \sigma_{i,corr}^{(k)} \sigma_{j,corr}^{(k)}$$

$$\chi^2 = \sum_{i,j=1}^N (m_i - t_i) V_{ij}^{-1} (m_j - t_j)$$

The effects of correlation in systematics can buy visualized calculating  
the systematic **SHIFTS**

We reformulate this in terms of  
nuisance parameters,  
uncorrelated uncertainties,  
shifted theoretical predictions

# Comparison shifted/unshifted results



The amount of shifts depends on sets..  
but it is generally significative.

# Resume fo main uncertainties

- 1. THE FACTORIZATION ESTABLISHES SOME LIMITS FOR ITS VALIDITY.**
- 2. SOME DATA SETS (ATLAS) CAN BE MORE SENSITIVE TO Y-TERMS AND UN-FACTORIZABLE CONTRIBUTIONS DUE TO THEIR PRECISION**
- 3. SCALE VARIATIONS**
- 4. PDFs: DIFFERENT SETS AND REPLICAS CAN PROVIDE DIFFERENT RESULTS**
- 5. MODEL BUILDING: STILL IN A GUESS AND TRY PROCESS ...**

QED corrections .  
See talk of Miguel

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# Conclusions

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- ❖ A NNLO ANALYSIS IS NECESSARY FOR FITTING DATA AND EXTRACTING UNPOLARIZED TMDs.
- ❖ LHC PROVIDES VERY PRECISE DATA THAT SHOULD BE INCLUDED IN FITS (ESPECIALLY DATA OFF THE Z-BOSON PEAK). ATLAS AND CMS COULD DO BETTER AT 13 TEV!!
- ❖ THE DATA ANALYSIS SHOULD COMBINE HIGH ENERGY AND LOW ENERGY DATA, BECAUSE THEY ARE SENSITIVE TO DIFFERENT NON-PERTURBATIVE REGIONS, BOTH COMPATIBLE WITH TMD FACTORIZATION
- ❖ SCALE CHOICES AND PRESCRIPTION SHOULD BE CRITICALLY ANALYZED (2D-EVOLUTION AND ZETA-PRESCRIPTION, OPTIMAL TMDs PROVIDE A BETTER DESCRIPTION OF ERRORS AND SEPARATION OF PERTURBATIVE/NON-PERTURBATIVE EFFECTS)
- ❖ ALL THIS IS/WILL BE INCLUDED IN arTeMiDe (already new 1.3 release)

MORE TO BE DONE

IMPROVE THE STATISTICAL ANALYSIS, ESPECIALLY FOR LHC DATA

COMPASS DATA FOR DY AND SIDIS

EXTEND THE CODE TO POLARIZED PROCESSES AND JETS

PREPARE FOR THE ADVENT OF EIC