



# AZIMUTHAL ANISOTROPIES FROM COMBINED INITIAL+FINAL STATE FRAMEWORKS

WORK WITH CHUN SHEN AND PRITHWISH TRIBEDY

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BROOKHAVEN NATIONAL LABORATORY



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U.S. DEPARTMENT OF  
**ENERGY**

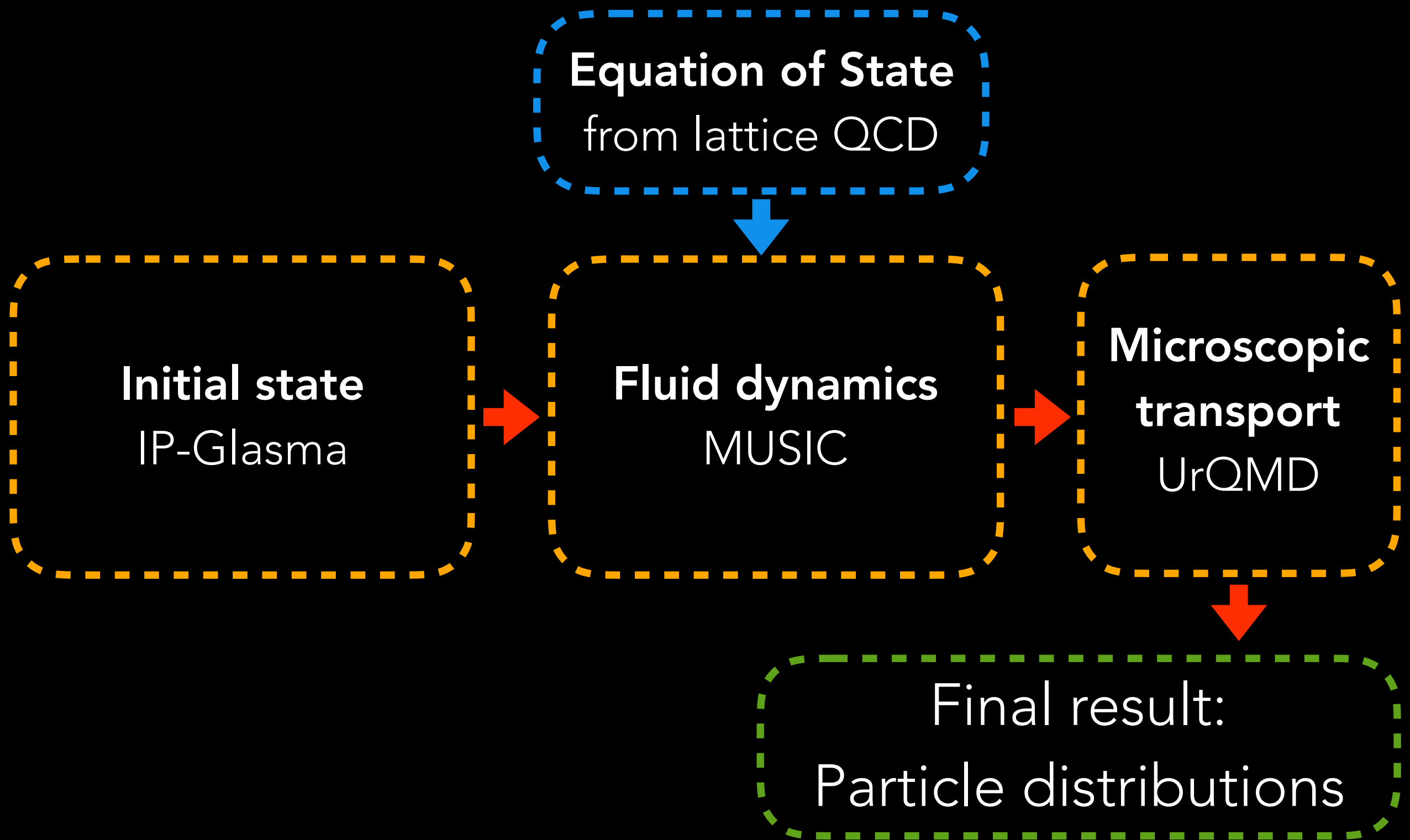
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# What is the dominant origin of azimuthal anisotropies in small systems?

- Initial momentum anisotropy from CGC (in IP-Glasma)
- Hydrodynamics with shear and bulk viscosities
- Include microscopic hadronic transport (UrQMD) at low  $T$
- Fix parameters (e.g. transport parameters) in collisions of Pb+Pb, predict Xe+Xe and smaller systems
- Do the same for RHIC: fix parameters using AA (and HERA) and predict  $v_n$  in p+Au and d+Au collisions
- Determine origin of azimuthal anisotropy in small systems
- Lay out problems with viscous hydro in small systems

# SIMULATION FRAMEWORK



# Initial state and pre-equilibrium: IP-Glasma

B.Schenke, P.Tribedy, R.Venugopalan, PRL108, 252301 (2012), PRC86, 034908 (2012)

Solve Yang-Mills equations with incoming color currents  
constrained with IPSat model fit to HERA data

Kowalski, Teaney, Phys.Rev. D68 (2003) 114005

Kovner, McLerran, Weigert, Phys. Rev. D52, 6231 (1995)

Krasnitz, Venugopalan, Nucl.Phys. B557 (1999) 237

Color charge density constructed from nucleons with three  
quark substructure (needed for p+A but also diffractive HERA data)

H. Mäntysaari, B. Schenke, Phys. Rev. Lett. 117 (2016) 052301 and Phys.Rev. D94 (2016) 034042

this is a place where EIC could help further constrain initial state

Includes fluctuations of:

impact parameter, nucleon positions, quark positions,  
color charge normalization, color charges



# Matching to fluid dynamics

Extract energy density and flow velocity from fields'  $T_{\text{QCD}}^{\mu\nu}$

$$\varepsilon u^\nu = u_\mu T^{\mu\nu}$$

Initial shear viscous tensor is given by (here used  $P=\varepsilon/3$ )

$$\pi^{\mu\nu} = T_{\text{QCD}}^{\mu\nu} - \underbrace{\frac{4}{3}\varepsilon u^\mu u^\nu + \frac{\varepsilon}{3}g^{\mu\nu}}_{\text{ideal part}}$$

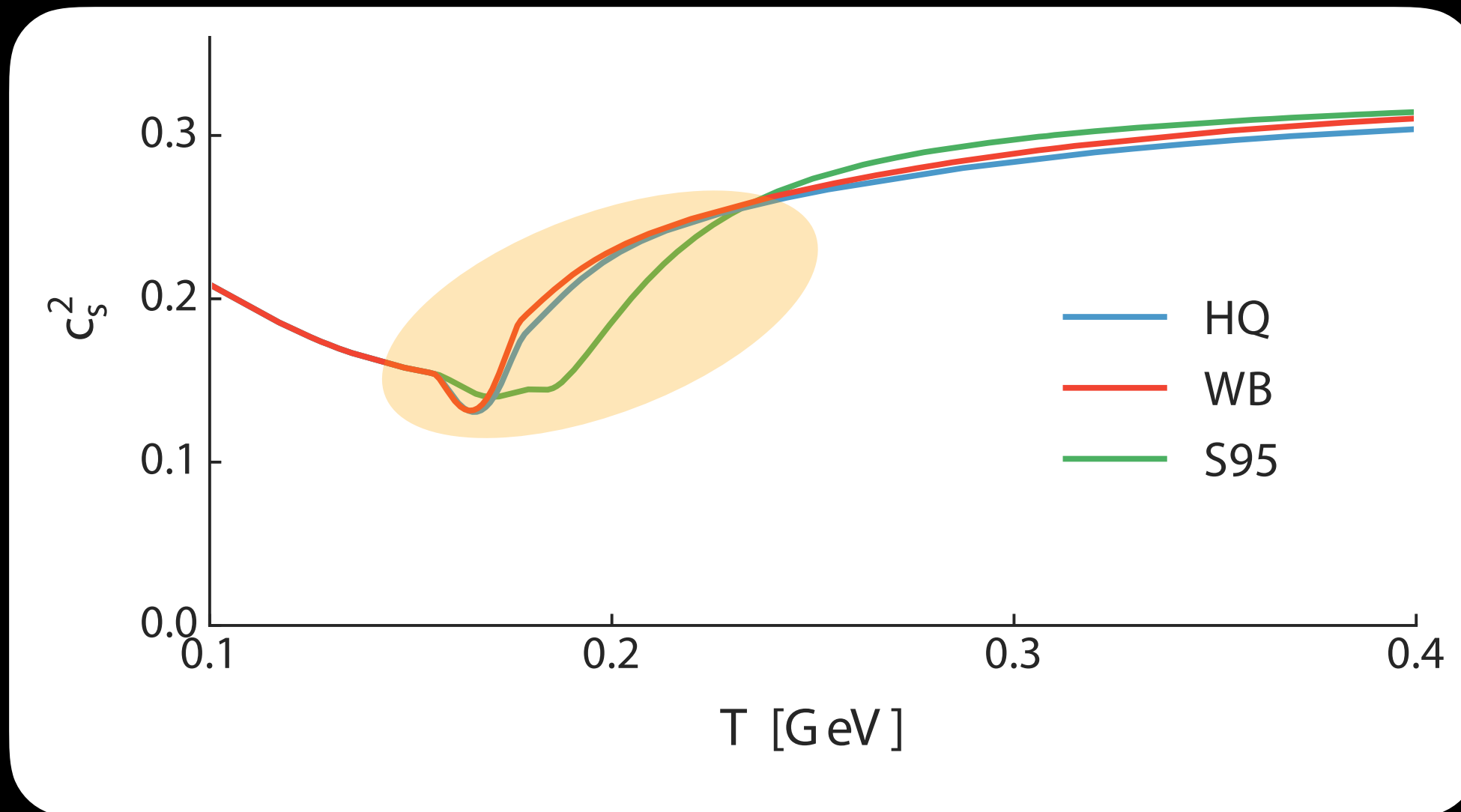
Absorb the difference to the lattice EoS in a 'bulk' stress term (here,  $P$  from the lattice EoS)

$$\Pi = \frac{\varepsilon}{3} - P$$

# Equation of State

Use a new EoS constructed from (WB) LQCD data

Larger speed of sound compared to s95p leads to more flow



Affects  
extraction  
of viscosities:  
 $v_n$  change  
by 10%  
 $\eta/s$  needs to  
change by  
~50%

Figure from J.S. Moreland, R.A. Soltz, *Phys.Rev. C93*, 044913 (2016), also see P. Alba et al. arXiv:1711.05207

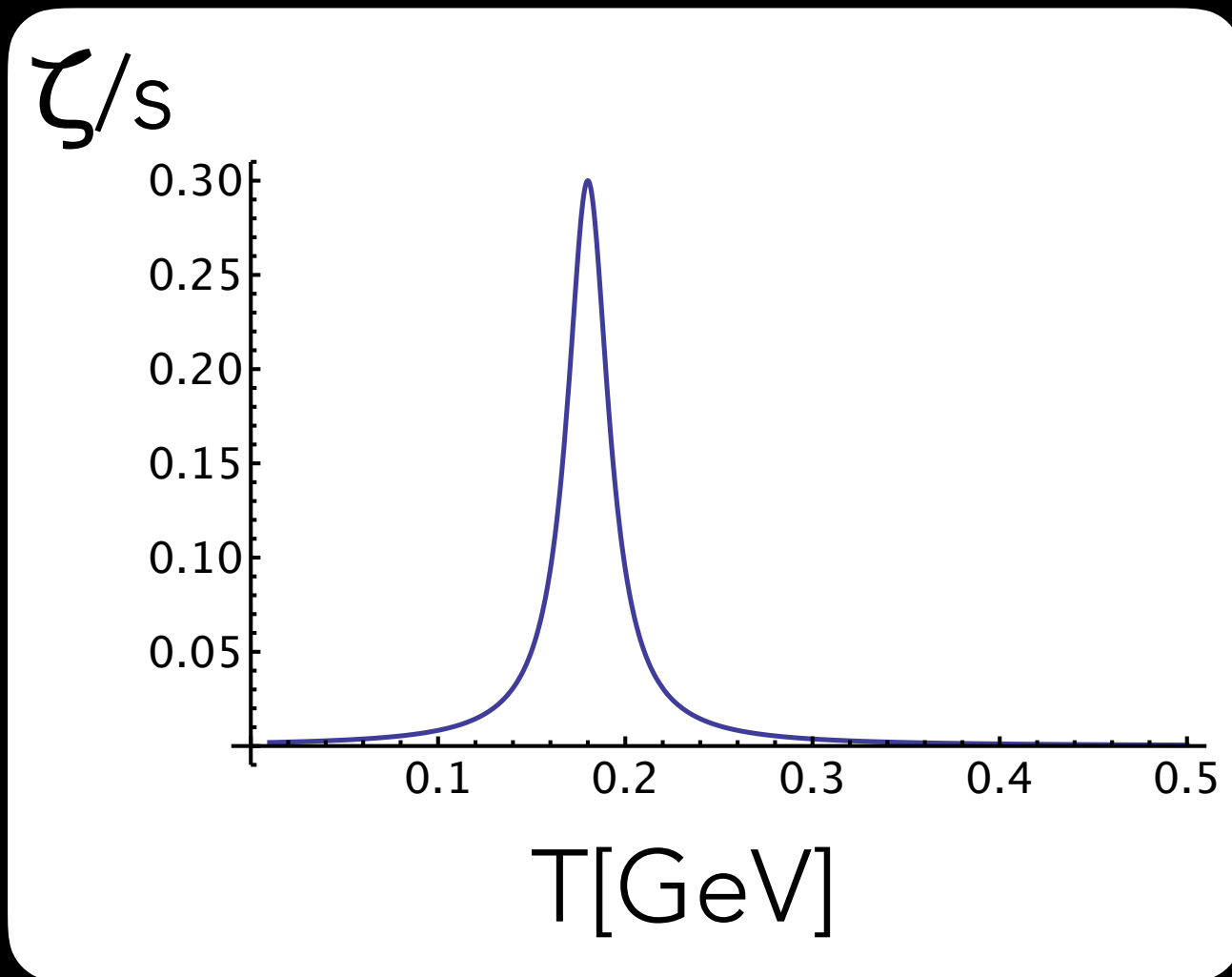
s95: P. Huovinen and P. Petreczky, *Nucl. Phys. A837*, 26–53 (2010)

HQ: A. Bazavov et al. (HotQCD), *Phys. Rev. D90*, 094503 (2014)

WB: S. Borsanyi, Z. Fodor, C. Hoelbling, S. D. Katz, S. Krieg, K. K. Szabo, *Phys. Lett. B730*, 99–104 (2014)

# Viscosities - all parameters fit in AA

Constant  $\eta/s$



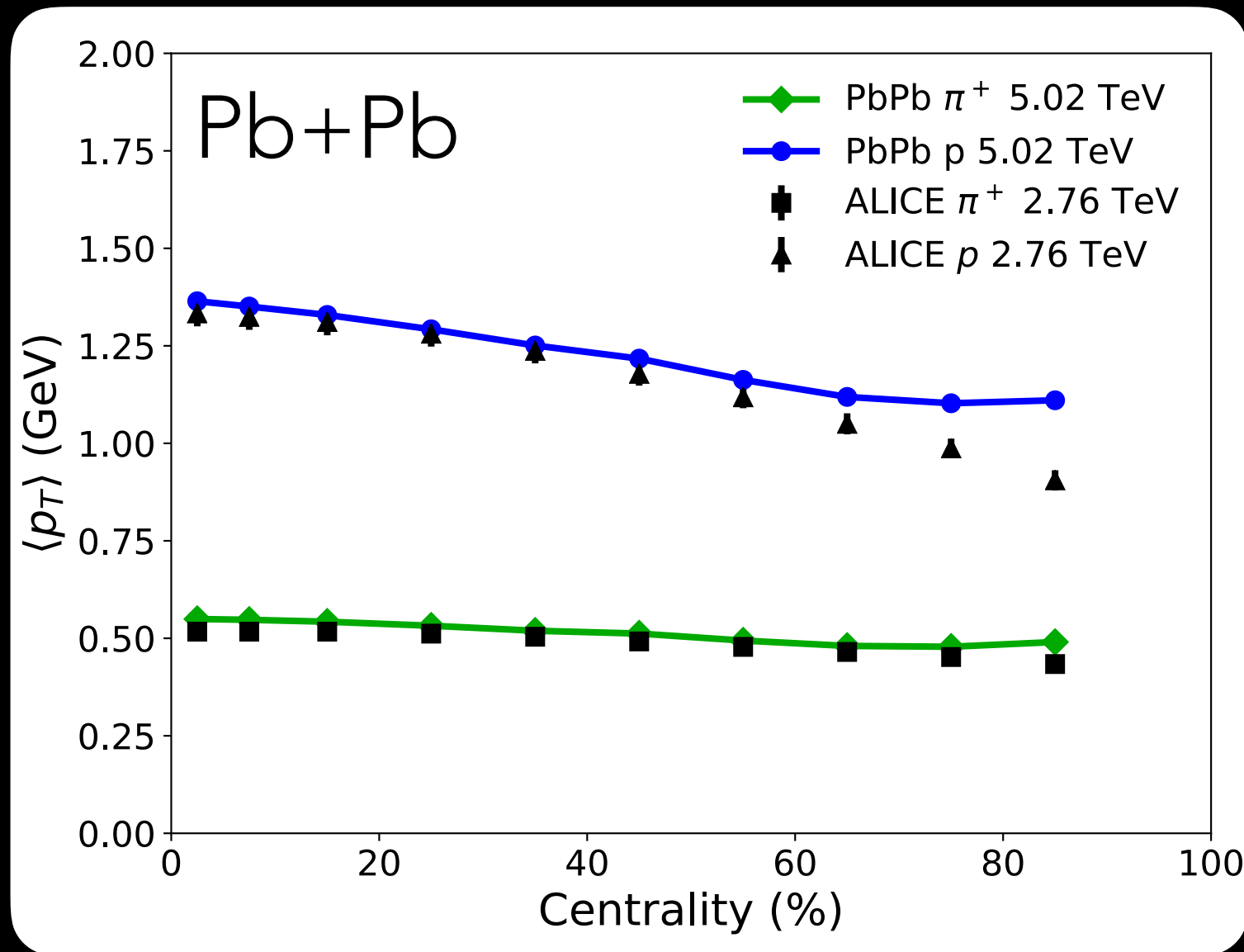
Bulk viscosity  
peaks at 180 MeV

Width, height,  
and position  
are free parameters

S. Ryu, J.-F. Paquet, C. Shen, G. Denicol, B. Schenke, S. Jeon, C. Gale, *Phys. Rev. C* **97**, 034910, (2018)

# Mean transverse momentum

B. Schenke, C. Shen, P. Tribedy, in preparation

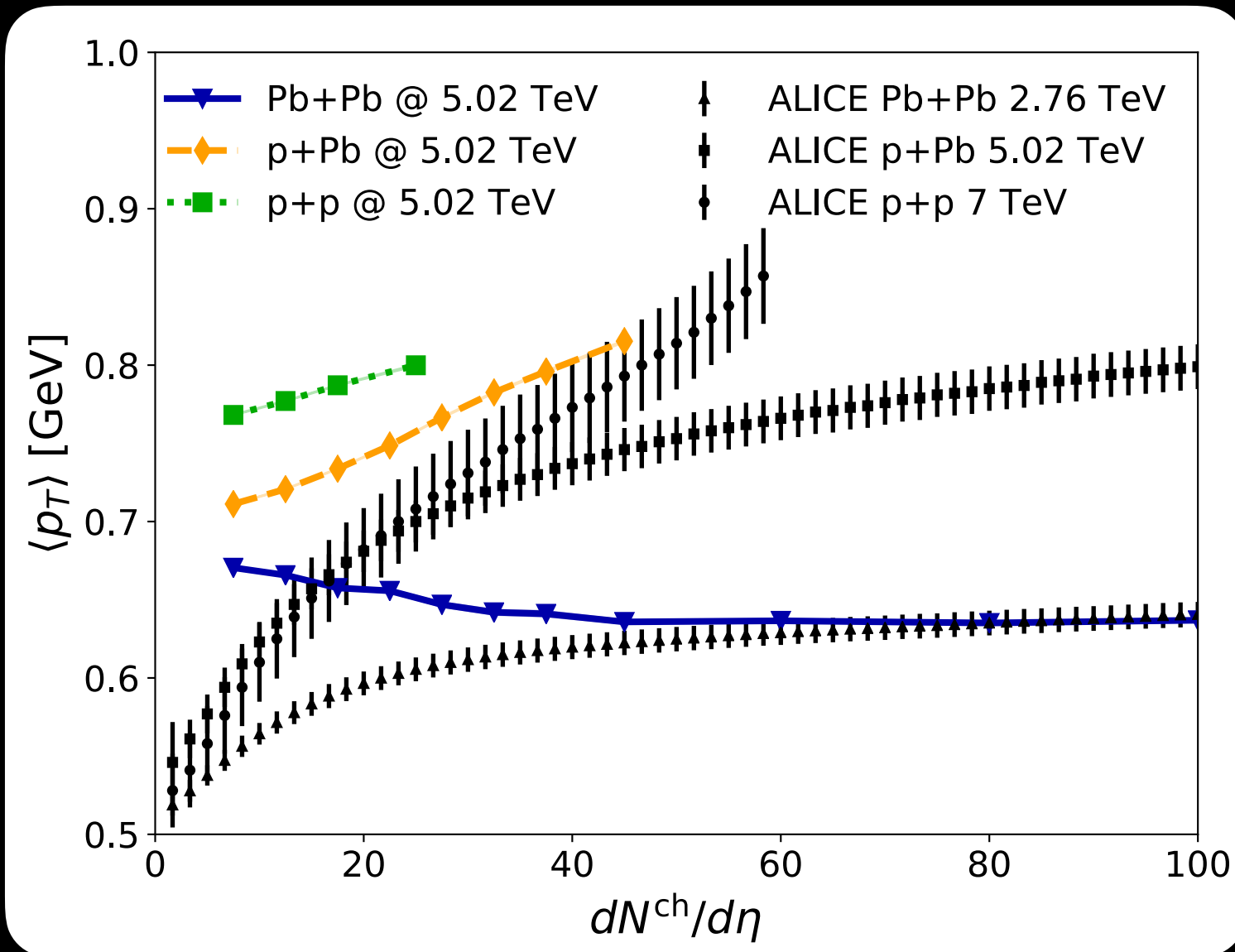


Bulk viscosity smaller at low T (low multiplicity)

UrQMD also may have too little bulk viscosity

# Mean transverse momentum

B. Schenke, C. Shen, P. Tribedy, in preparation



p+Pb  $\langle p_T \rangle$

~8% > than data

p+p  $\langle p_T \rangle$  ~12% > data

Pb+Pb  $\langle p_T \rangle$  over-estimated at  $N_{ch} < 60$

Bulk viscosity smaller at low T (low multiplicity)

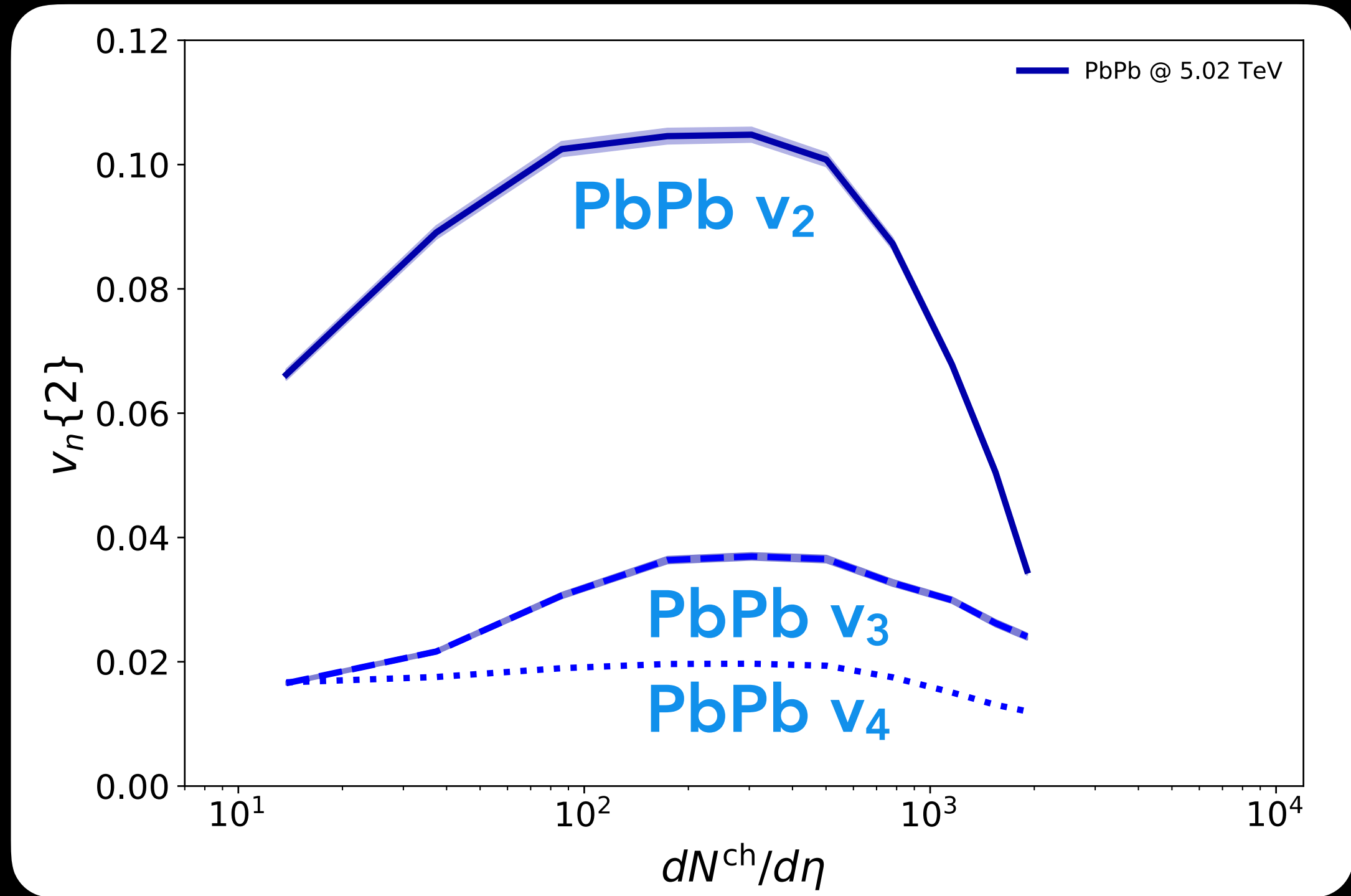
UrQMD also may have too little bulk viscosity



# Anisotropy vs. multiplicity

B. Schenke, C. Shen, P. Tribedy, in preparation

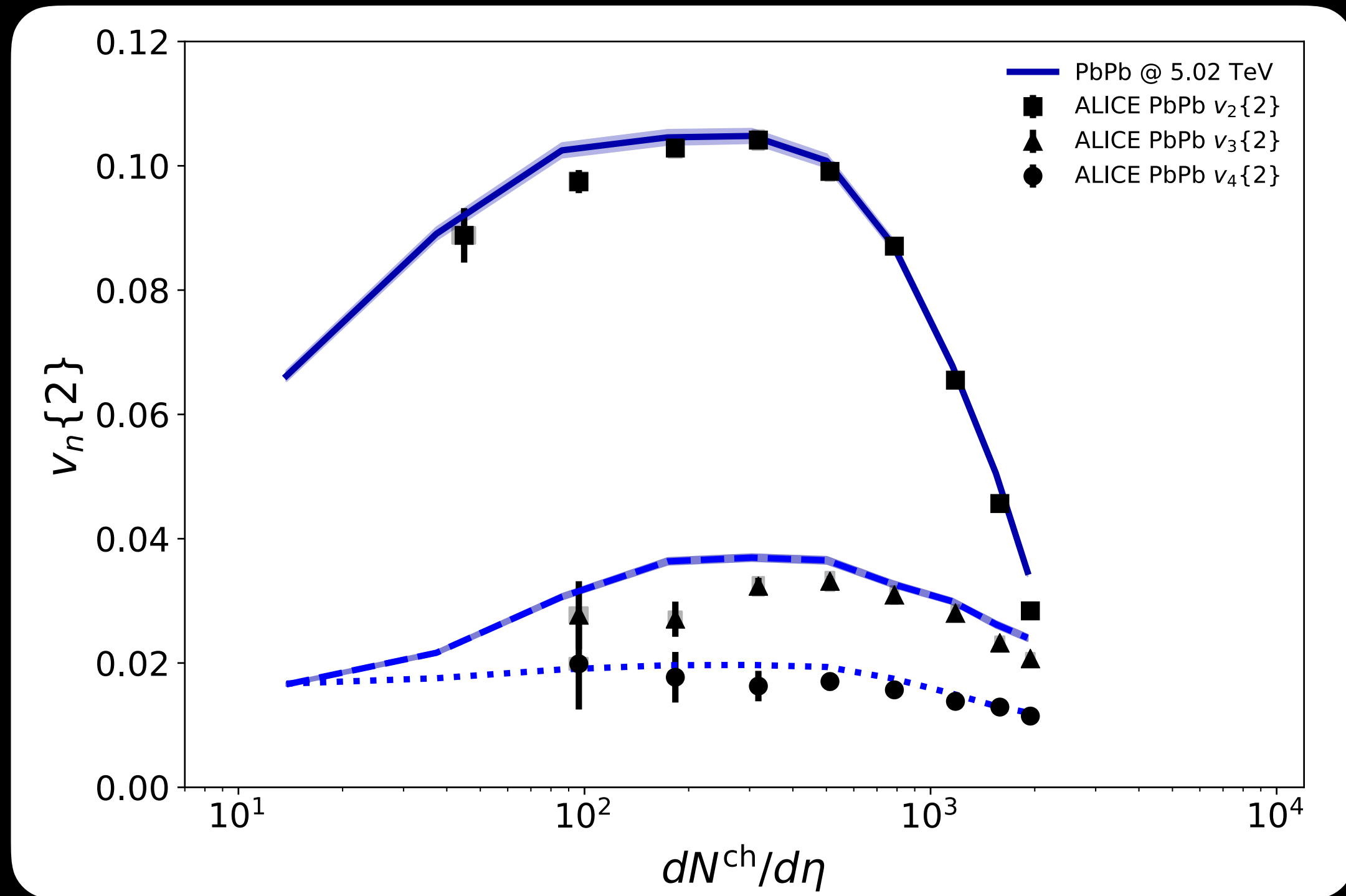
$\eta/s=0.13$



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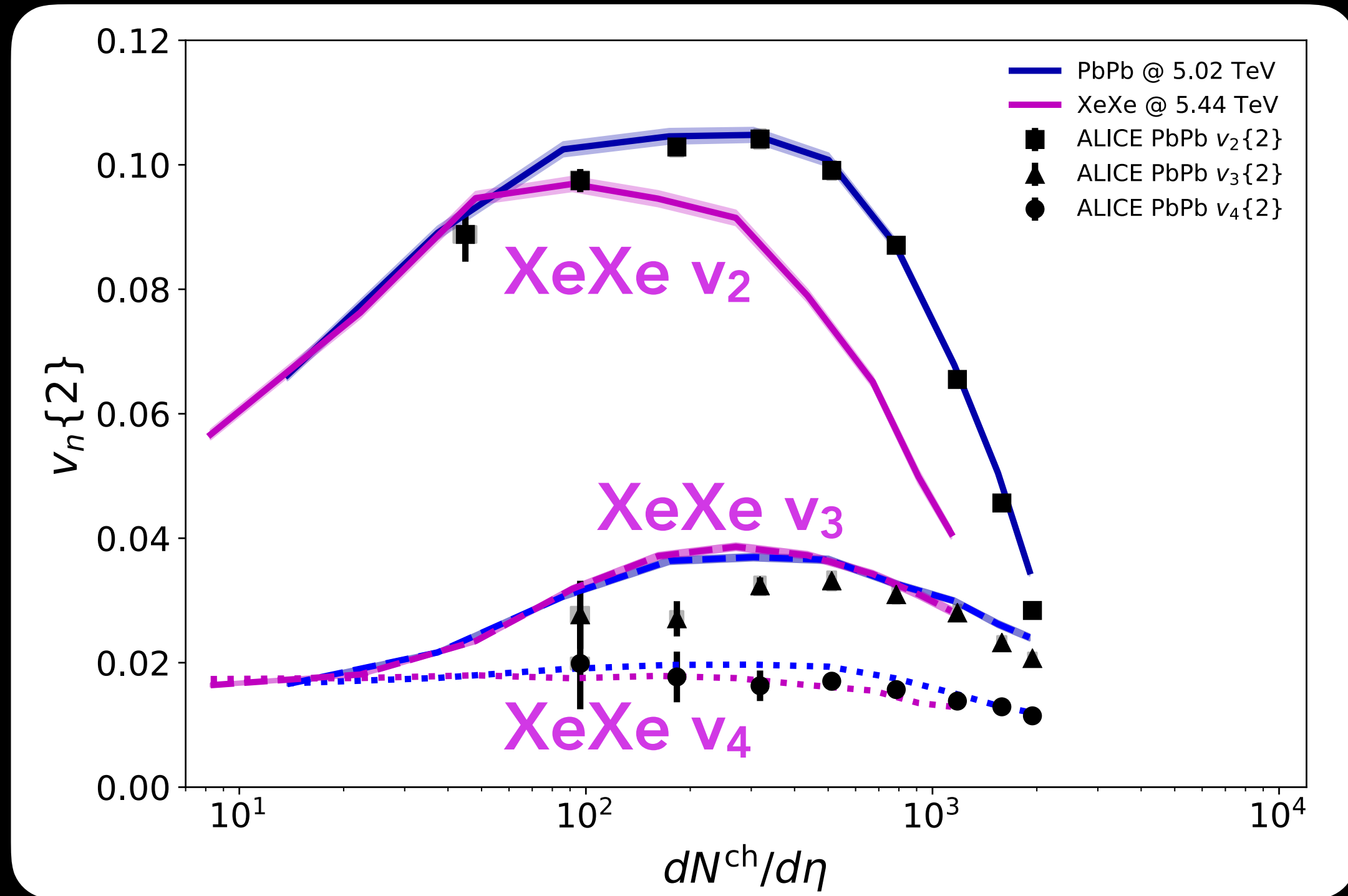
Experimental data: J. Adam et al. (ALICE), Phys. Rev. Lett. 116, 132302 (2016)

B. B. Abelev et al. (ALICE), Phys. Rev. C90, 054901 (2014)

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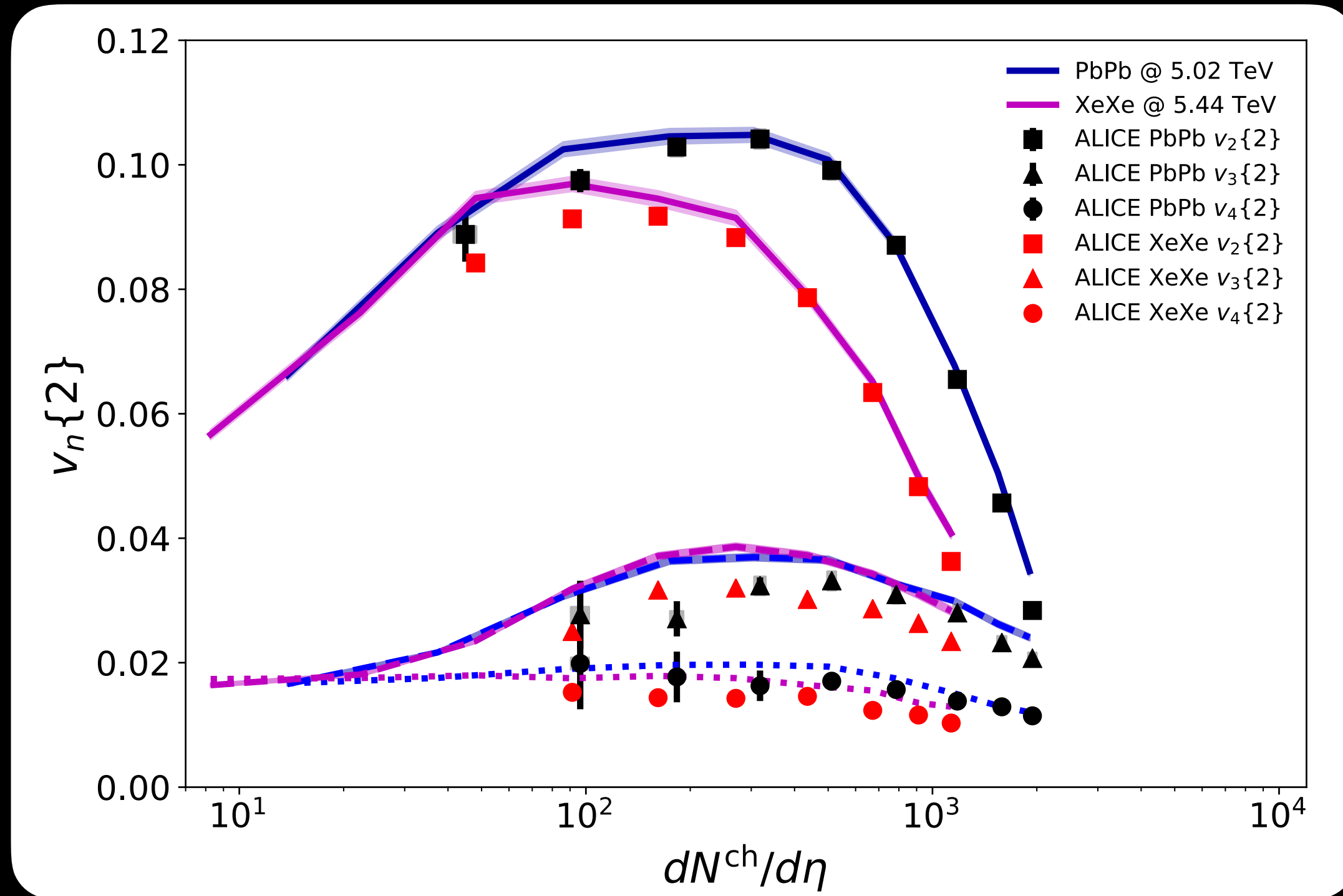
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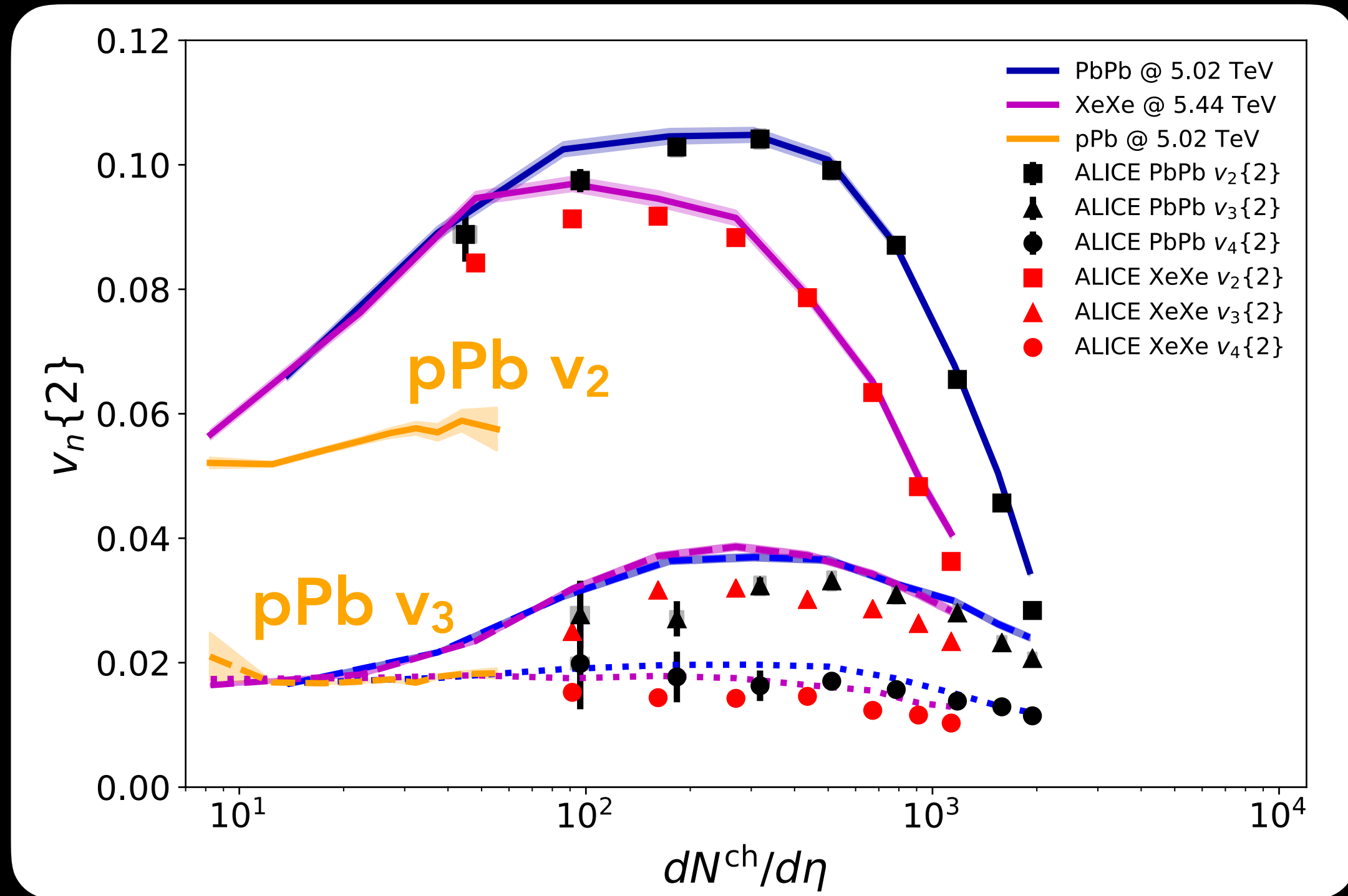
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B. B. Abelev et al. (ALICE), Phys. Rev. C90, 054901 (2014), ALICE Collaboration, arXiv:1805.01832

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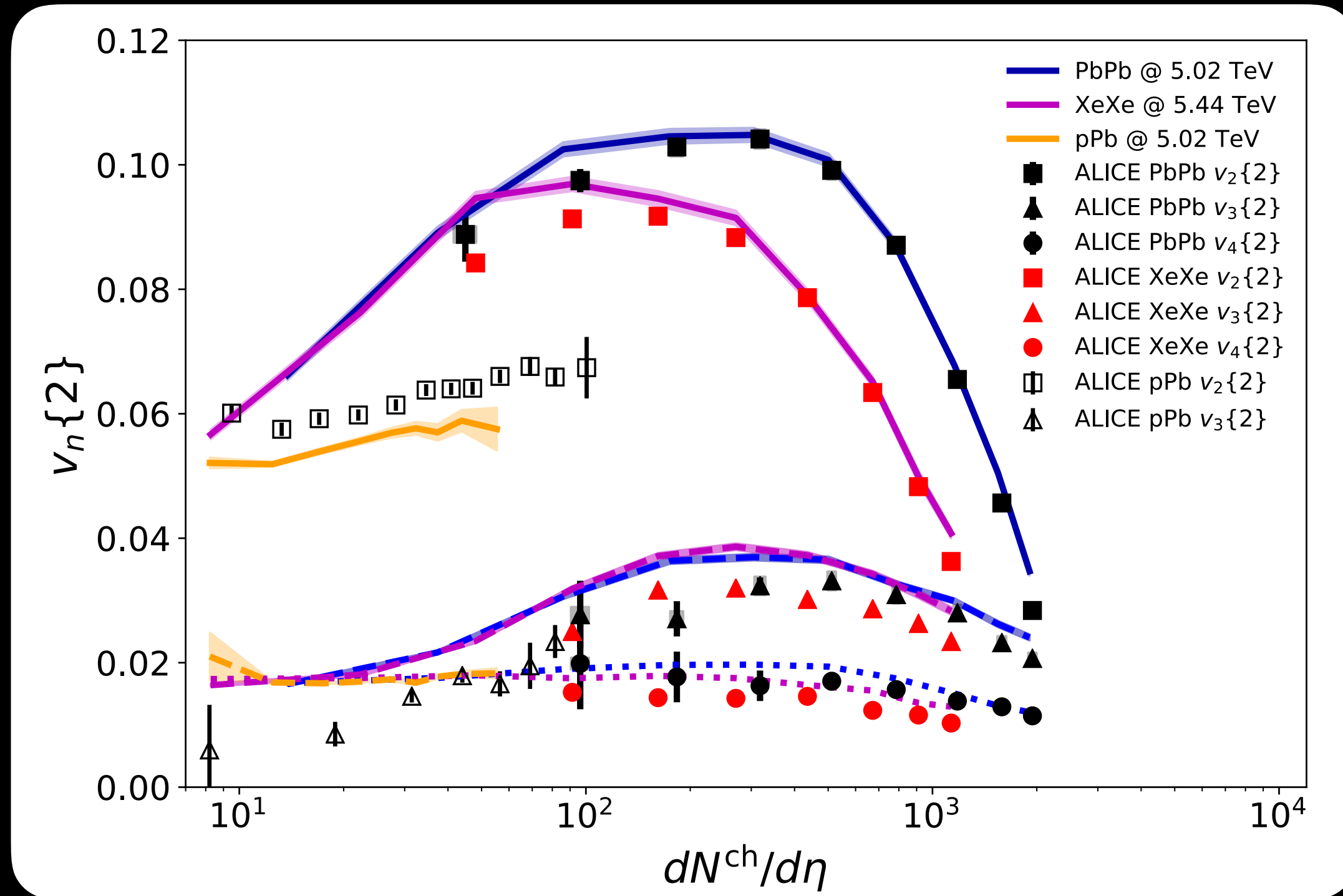
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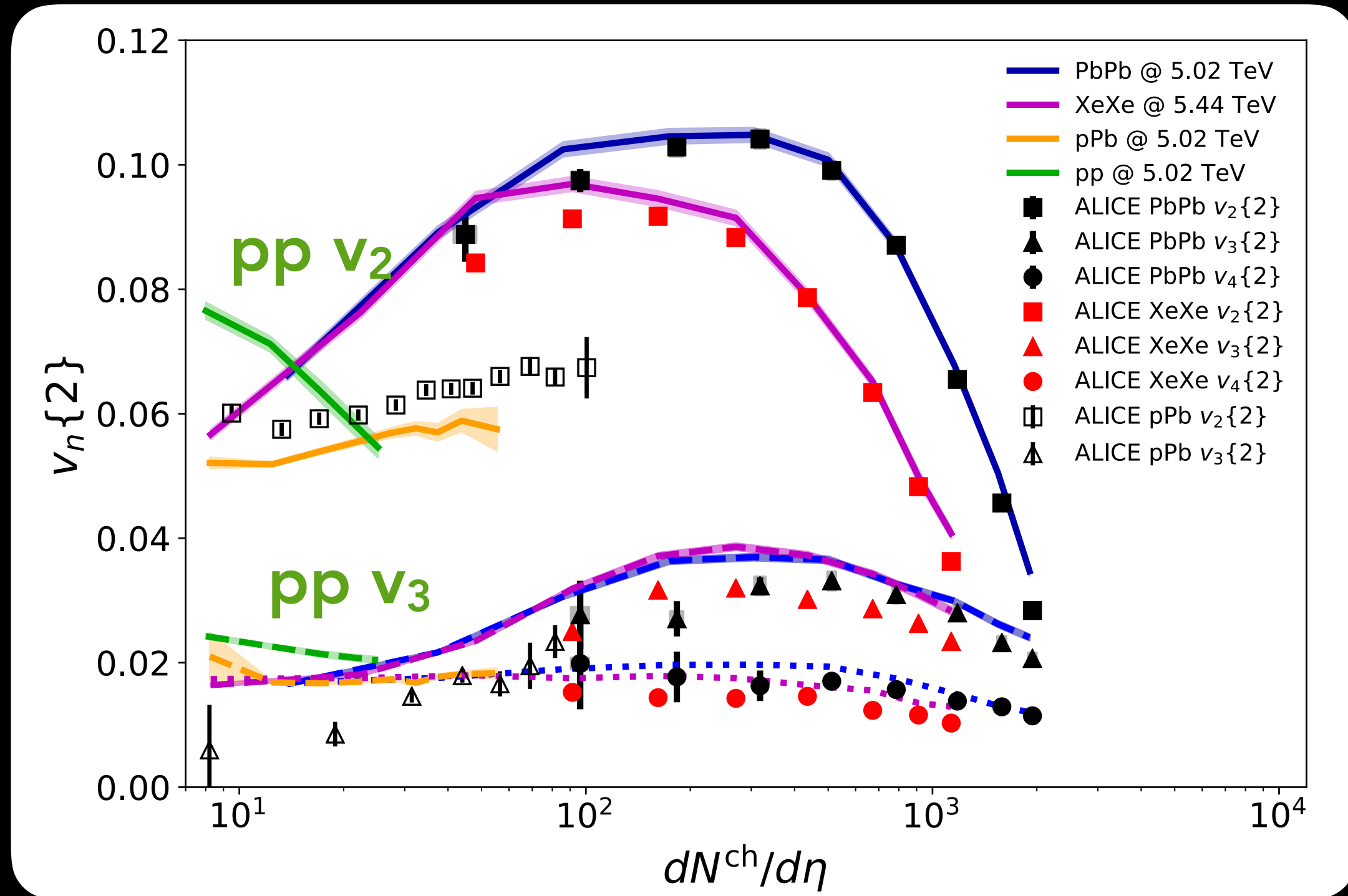
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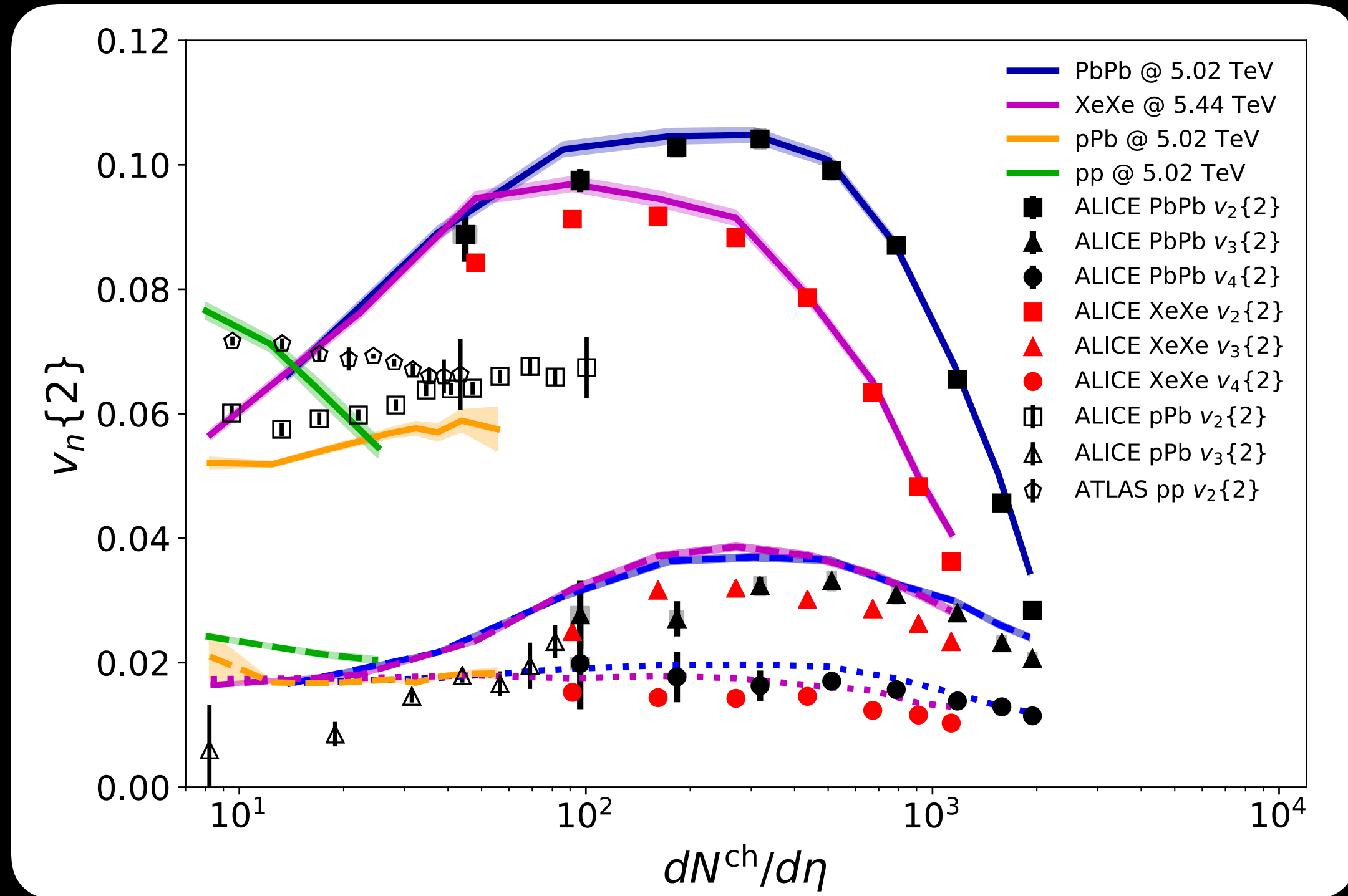
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ATLAS Collaboration, Eur. Phys. J. C (2017) 77:428

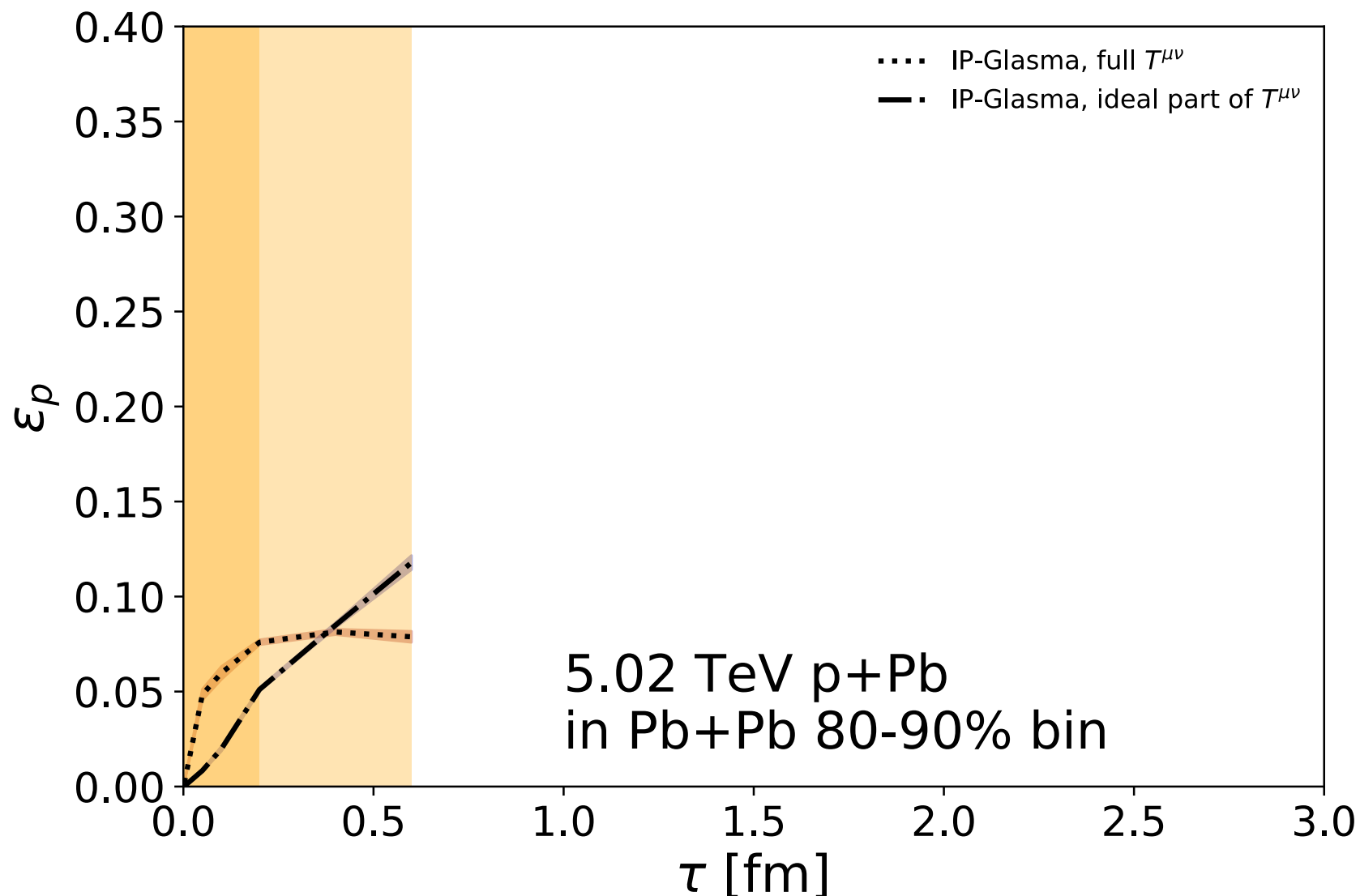
# When is momentum anisotropy generated in p+Pb?

p+Pb events in 80-90% Pb+Pb class

IP-Glasma

$$\epsilon_p = \sqrt{\frac{\langle T^{xx} - T^{yy} \rangle^2 + \langle 2T^{xy} \rangle^2}{\langle T^{xx} + T^{yy} \rangle^2}}$$

averages over space  
(weighted with energy density)



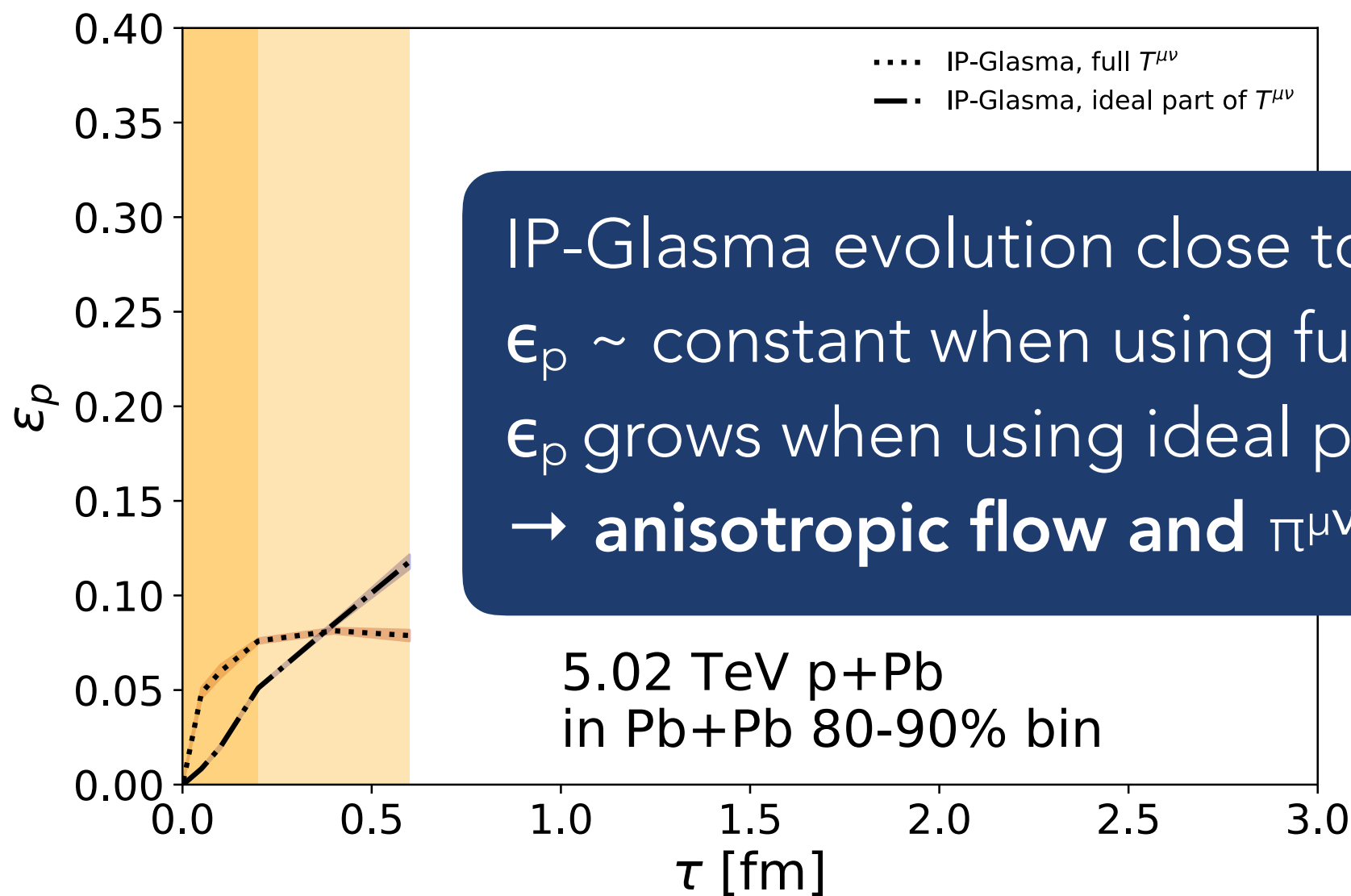
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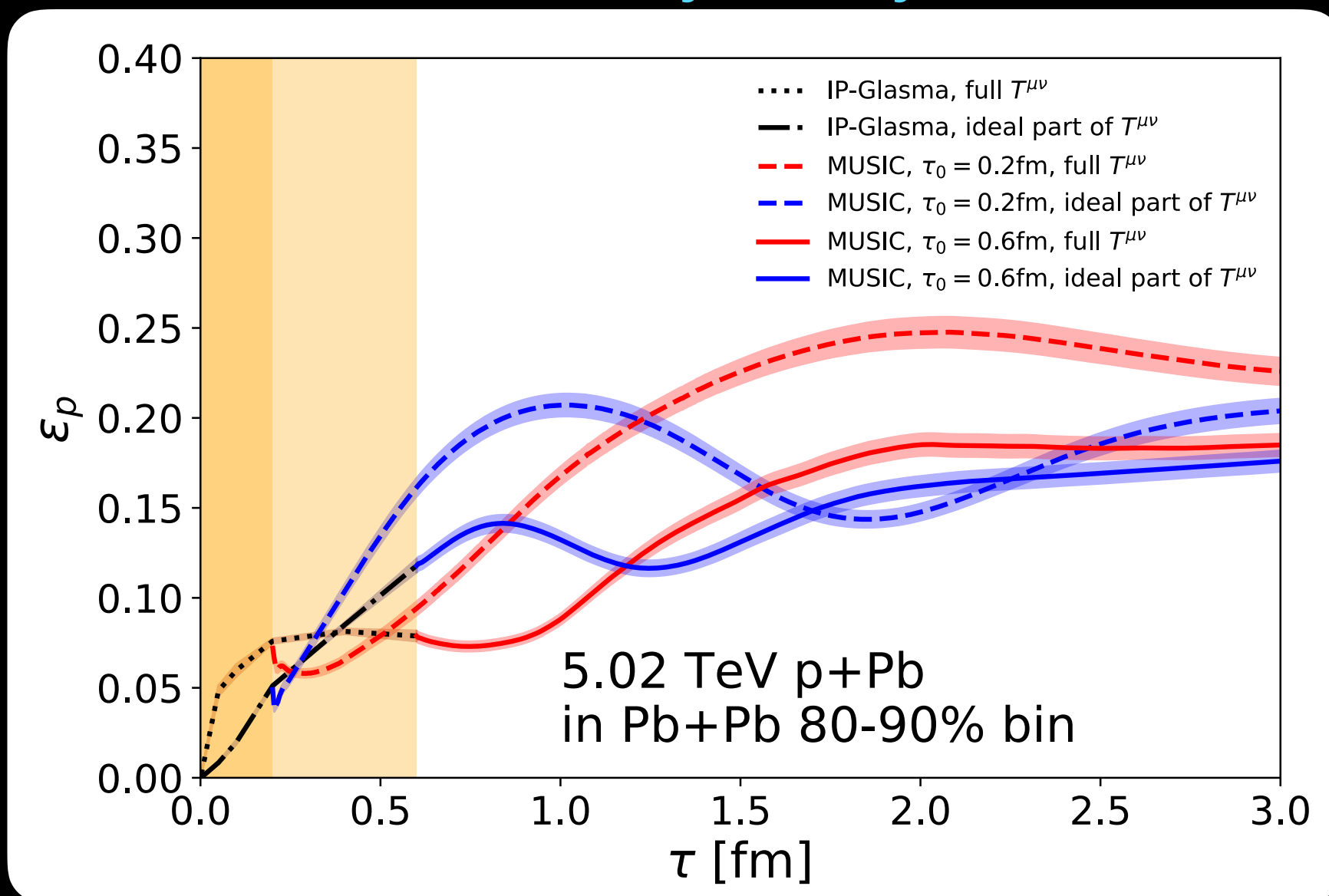
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IP-Glasma

Hydrodynamics



Switching at  $\tau=0.6\text{fm}$ :  
(full lines)

initial  $\epsilon_p$  with full  $T^{\mu\nu}$   
~45% of final value

Switching at  $\tau=0.2\text{fm}$ :  
(dashed lines)

initial  $\epsilon_p$  with full  $T^{\mu\nu}$   
~35% of final value

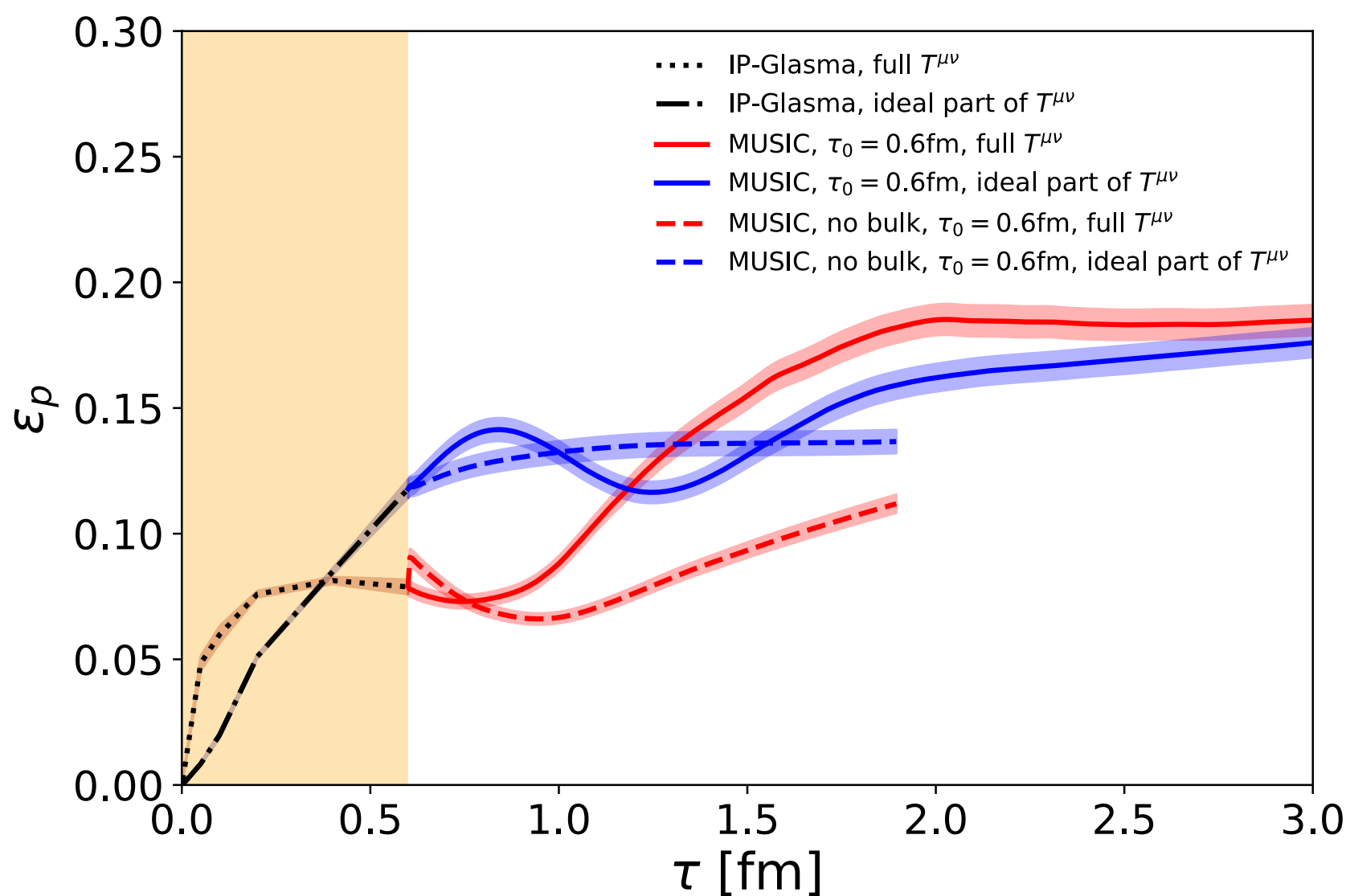
# When is momentum anisotropy generated in p+Pb?

## Effect of bulk viscosity

$$\epsilon_p = \sqrt{\frac{\langle T^{xx} - T^{yy} \rangle^2 + \langle 2T^{xy} \rangle^2}{\langle T^{xx} + T^{yy} \rangle^2}}$$

IP-Glasma

Hydrodynamics



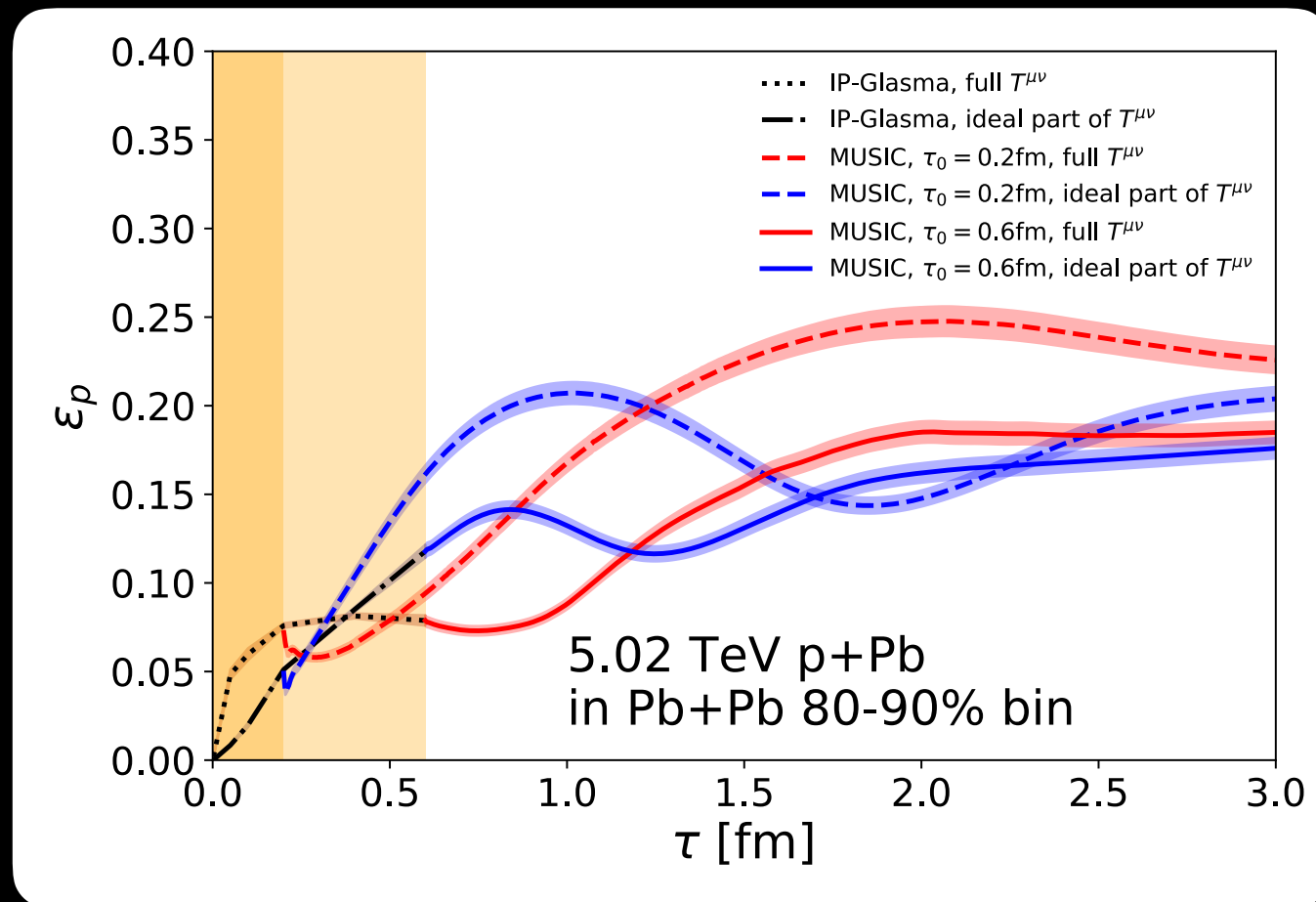
With bulk viscosity  
(full lines)

initial  $\epsilon_p$  with full  $T^{\mu\nu}$   
~45% of final value

w/o bulk viscosity  
(dashed lines)

initial  $\epsilon_p$  with full  $T^{\mu\nu}$   
~70% of final value

# When is momentum anisotropy generated in p+Pb?



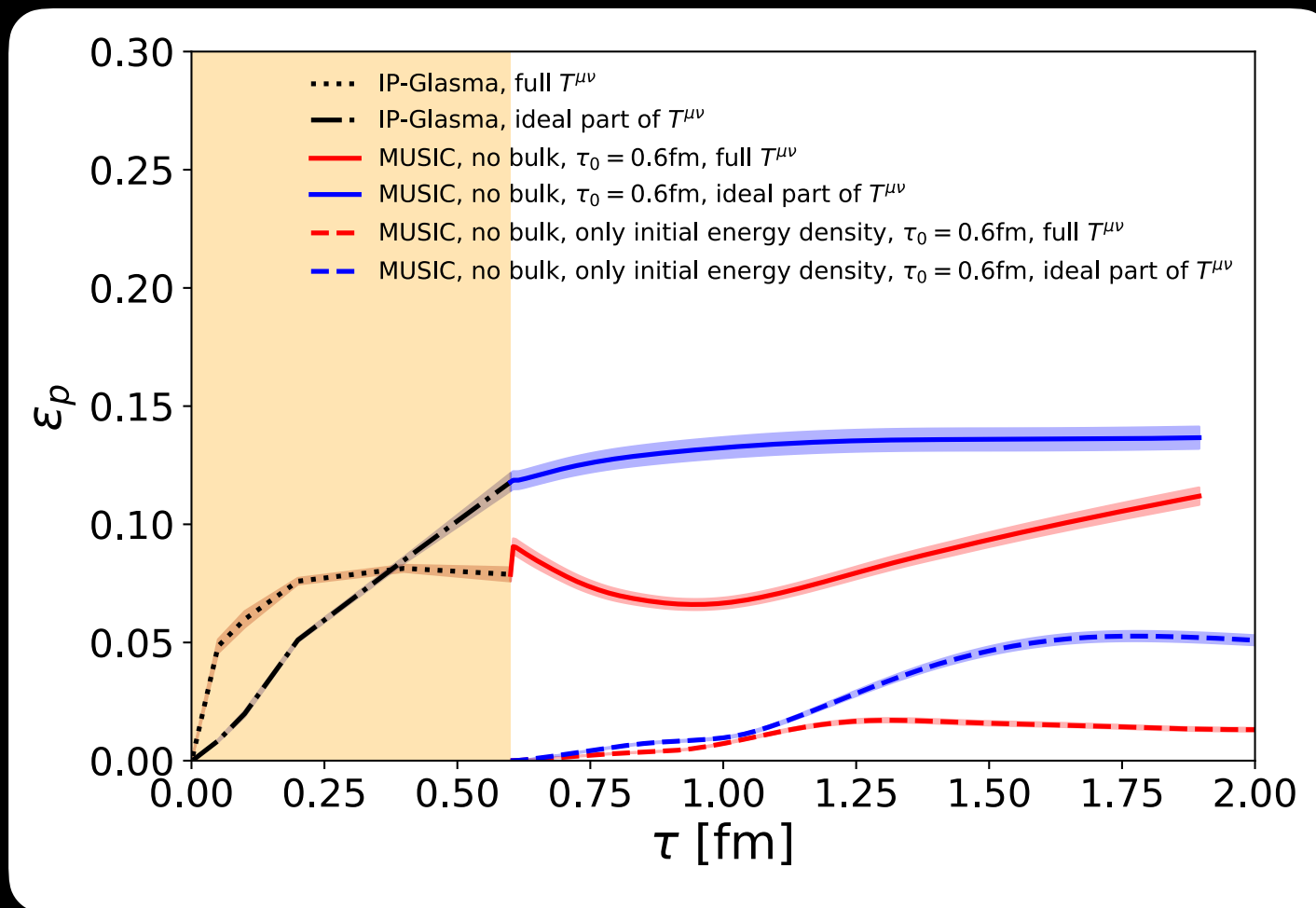
$$\epsilon_p = \sqrt{\frac{\langle T^{xx} - T^{yy} \rangle^2 + \langle 2T^{xy} \rangle^2}{\langle T^{xx} + T^{yy} \rangle^2}}$$

- Initial state color glass  $v_2$  encoded in initial  $T^{\mu\nu}$
- Free streaming makes (ideal) flow anisotropy and  $\pi^{\mu\nu}$  grow
- Role of hydrodynamics is to dynamically reduce the initial  $\pi^{\mu\nu}$  and possibly generate more anisotropy
- Tricky questions about artifacts of matching arise...

Possible improvement: [A. Kurkela, A. Mazeliauskas, J.-F. Paquet, S. Schlichting, D. Teaney, arXiv:1805.01604](#)

# When is momentum anisotropy generated in p+Pb?

## No bulk, with and w/o initial flow

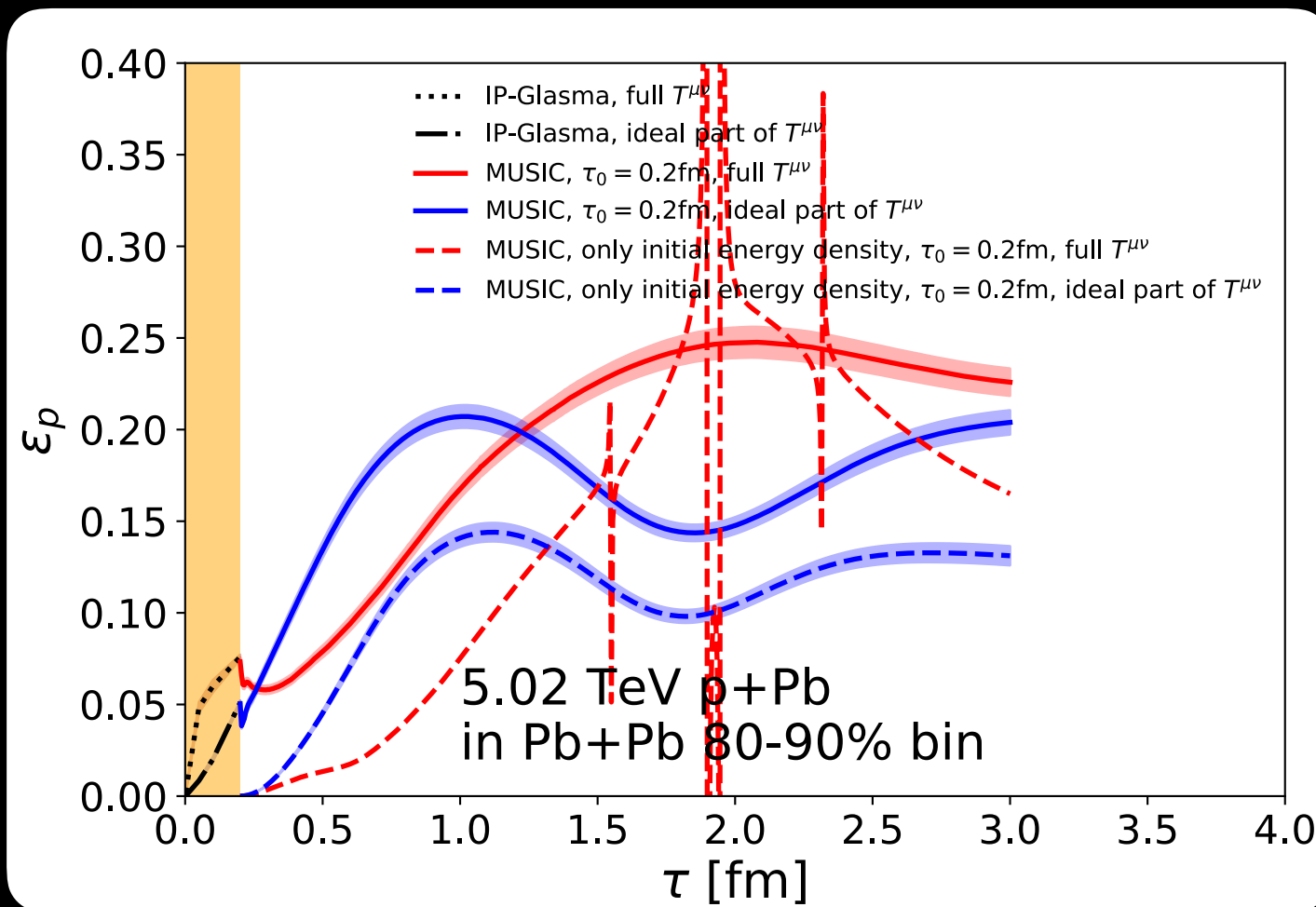


$$\epsilon_p = \sqrt{\frac{\langle T^{xx} - T^{yy} \rangle^2 + \langle 2T^{xy} \rangle^2}{\langle T^{xx} + T^{yy} \rangle^2}}$$

Turning off initial flow when switching at  $\tau=0.6\text{fm}$   
 almost no anisotropic flow is built up  
 This is also reflected in  $v_n$  values

# When is momentum anisotropy generated in p+Pb?

With bulk, with and w/o initial flow

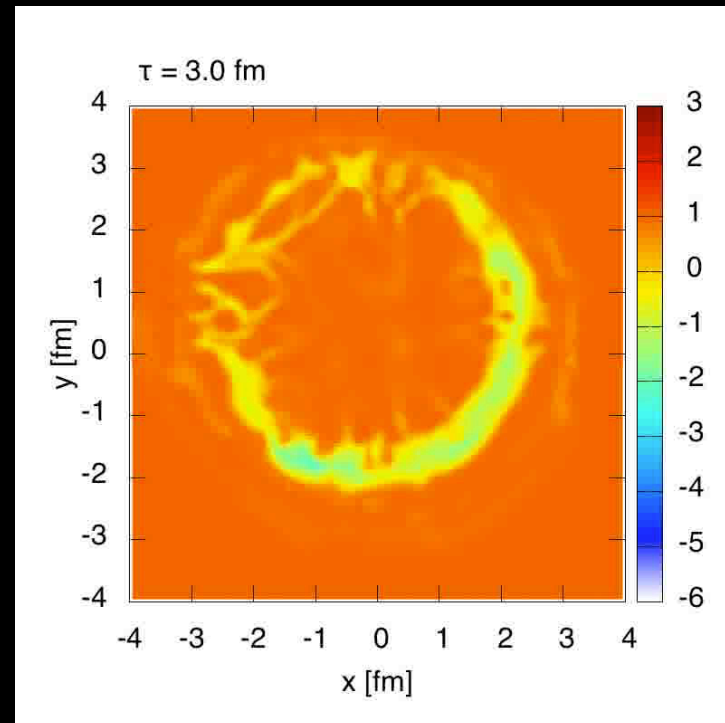
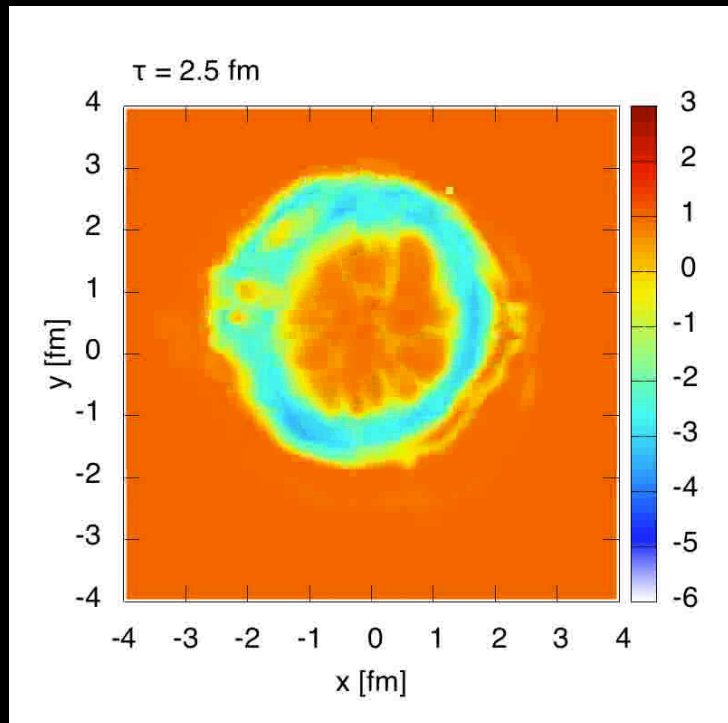
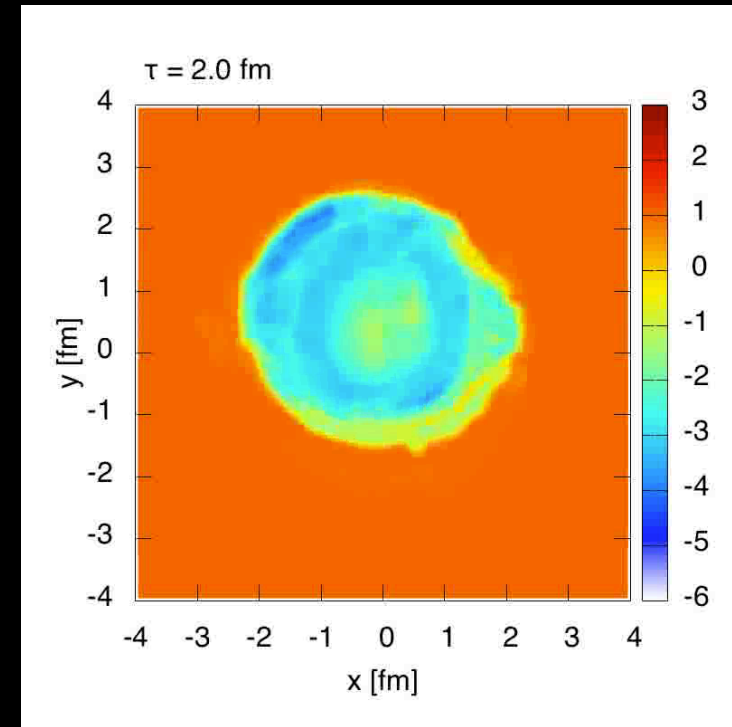
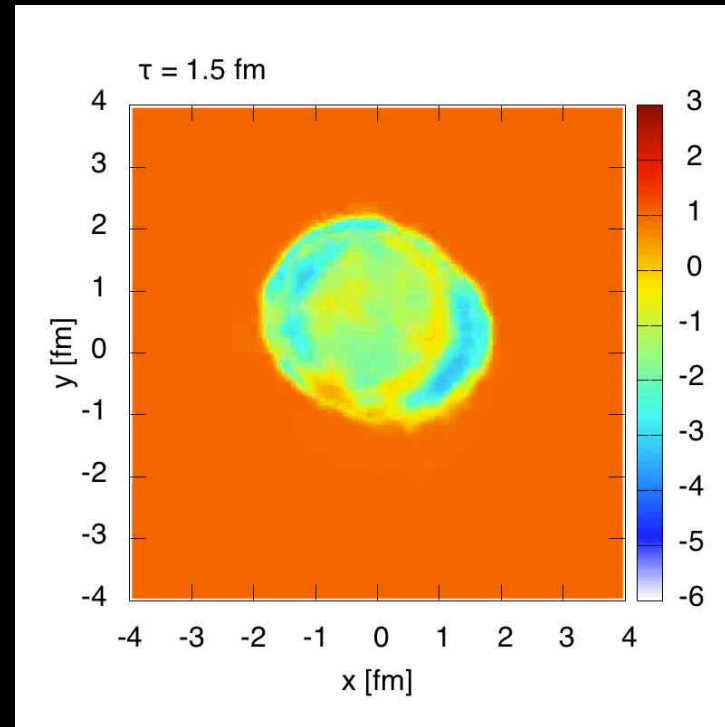
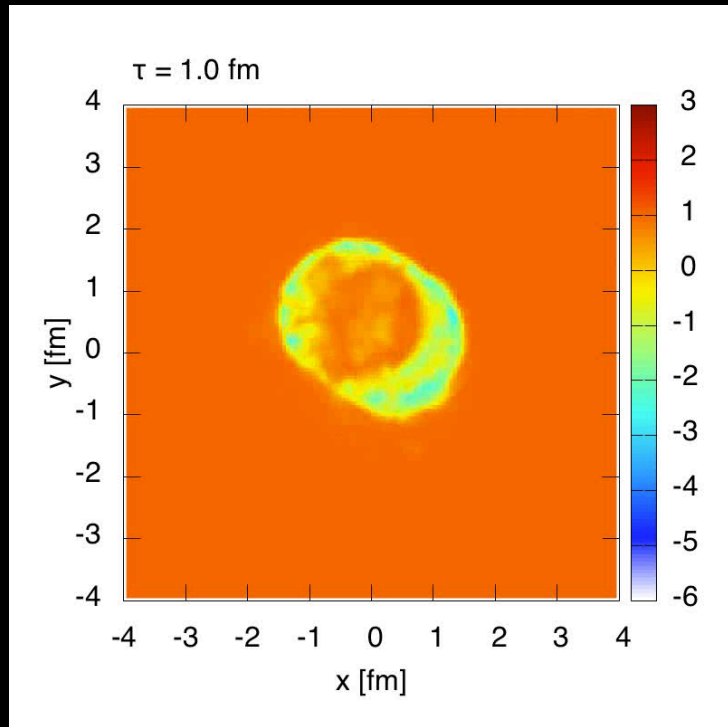


$$\epsilon_p = \sqrt{\frac{\langle T_{xx} - T_{yy} \rangle^2 + \langle 2T_{xy} \rangle^2}{\langle T_{xx} + T_{yy} \rangle^2}}$$

Things go crazy when denominator goes through zero  
Happens because of bulk correction  $\sim -$  ideal pressure



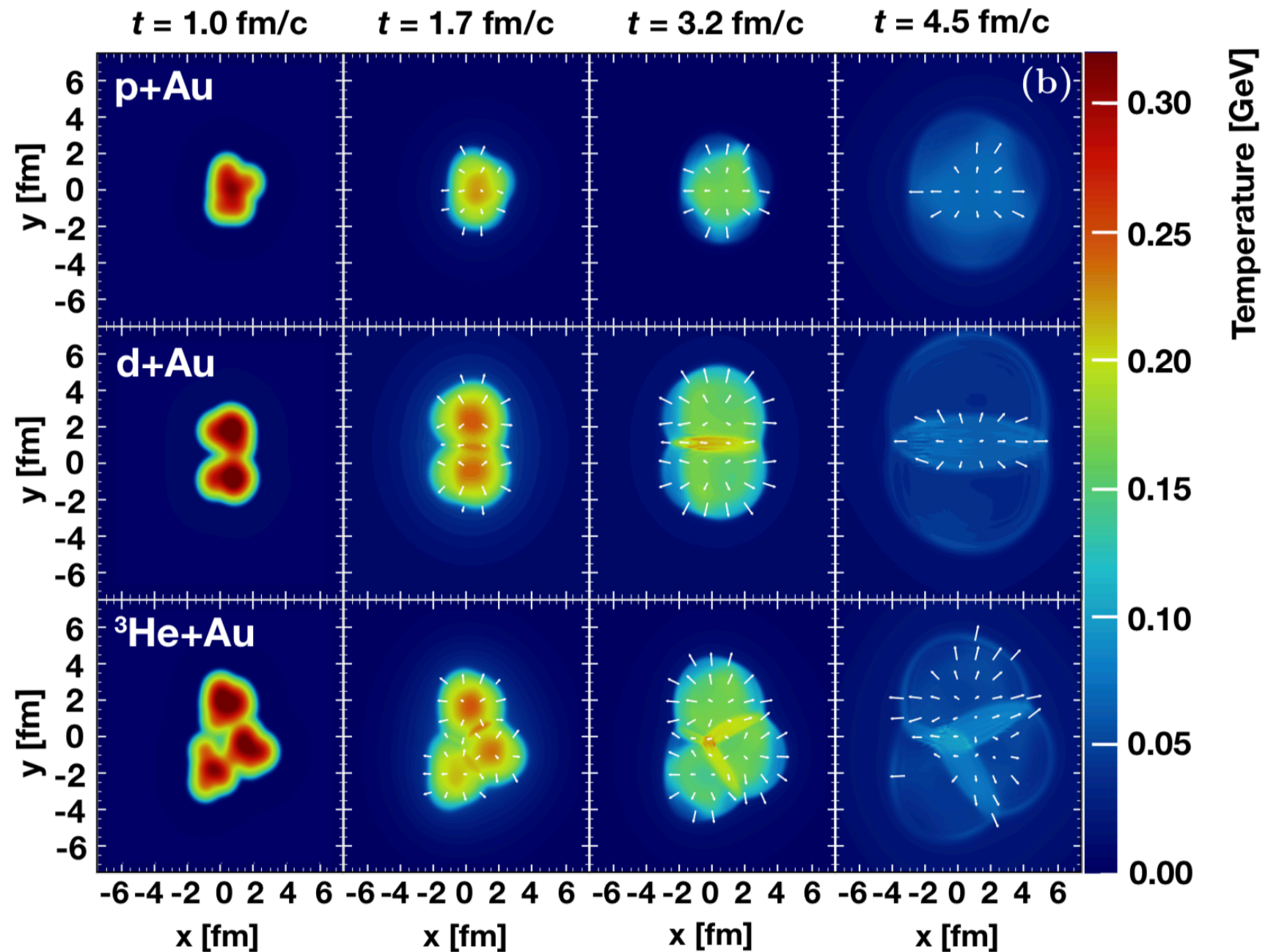
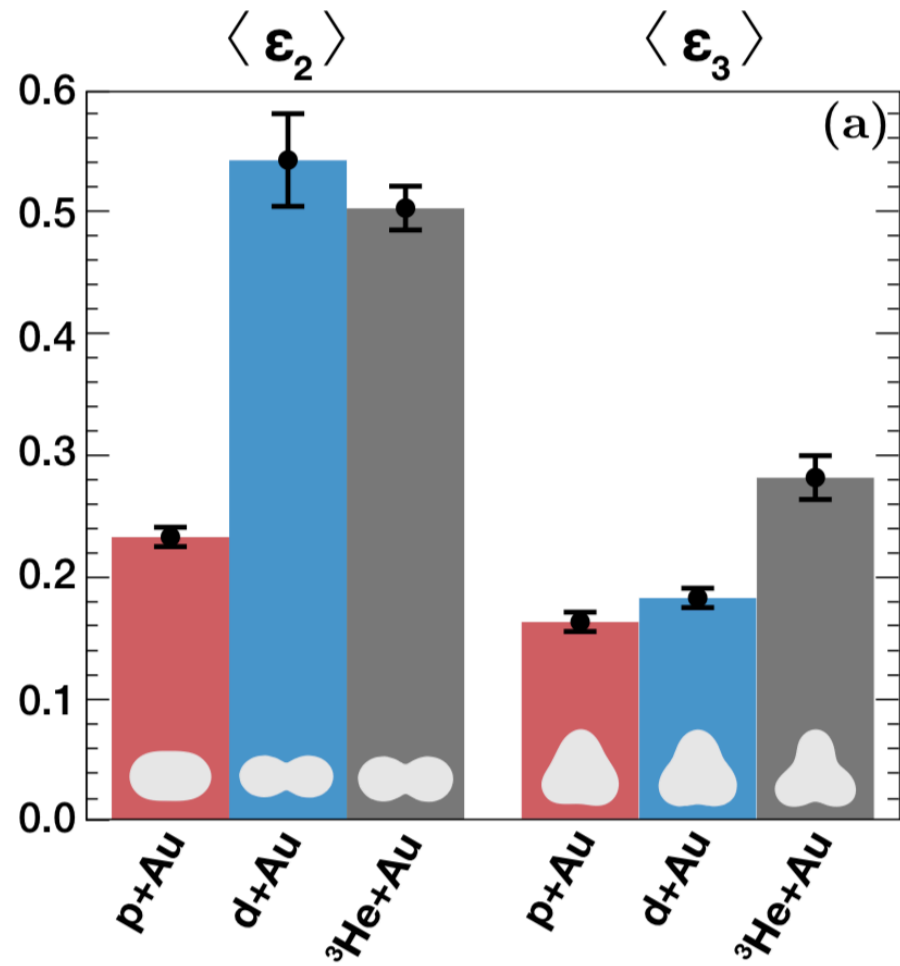
# Large bulk viscosity $\rightarrow$ negative pressure



$1 + \Pi/P$   
in a p+Pb collision

# RHIC system scan: pAu, dAu, $^3\text{HeAu}$

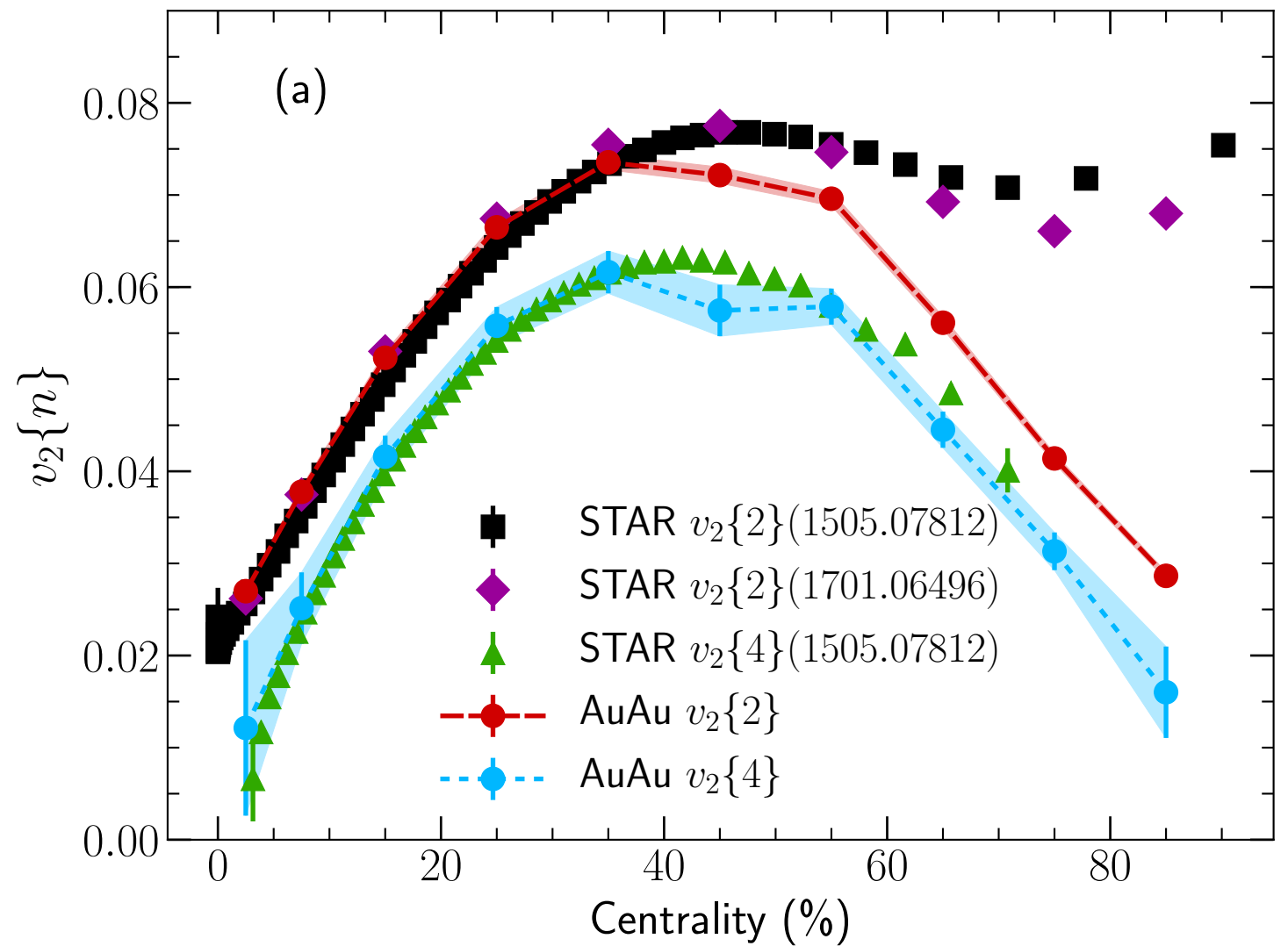
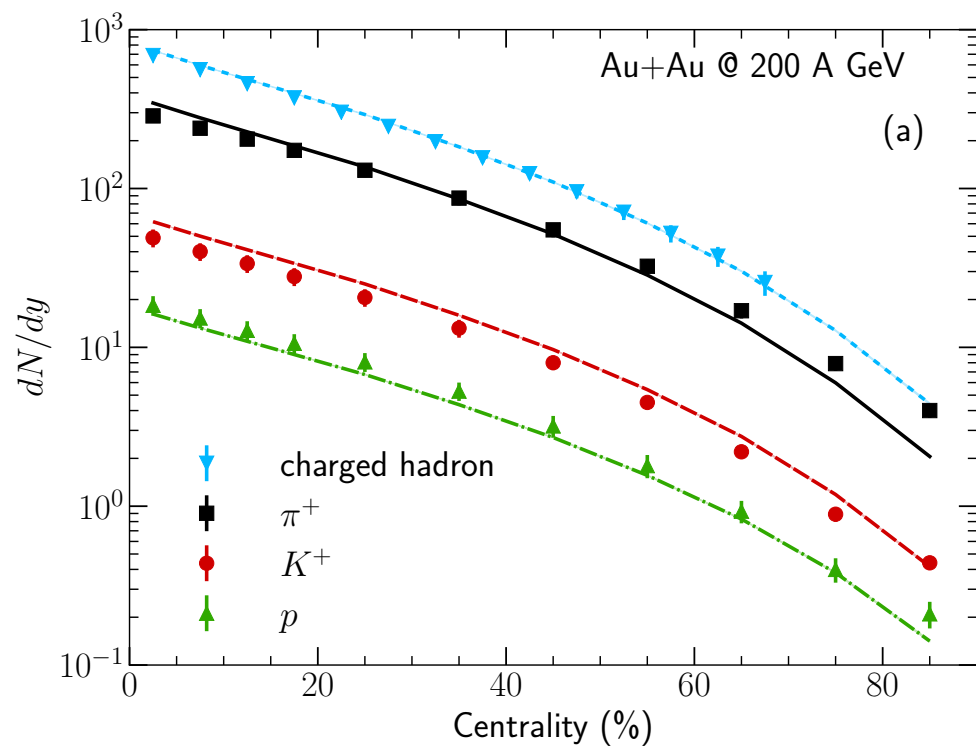
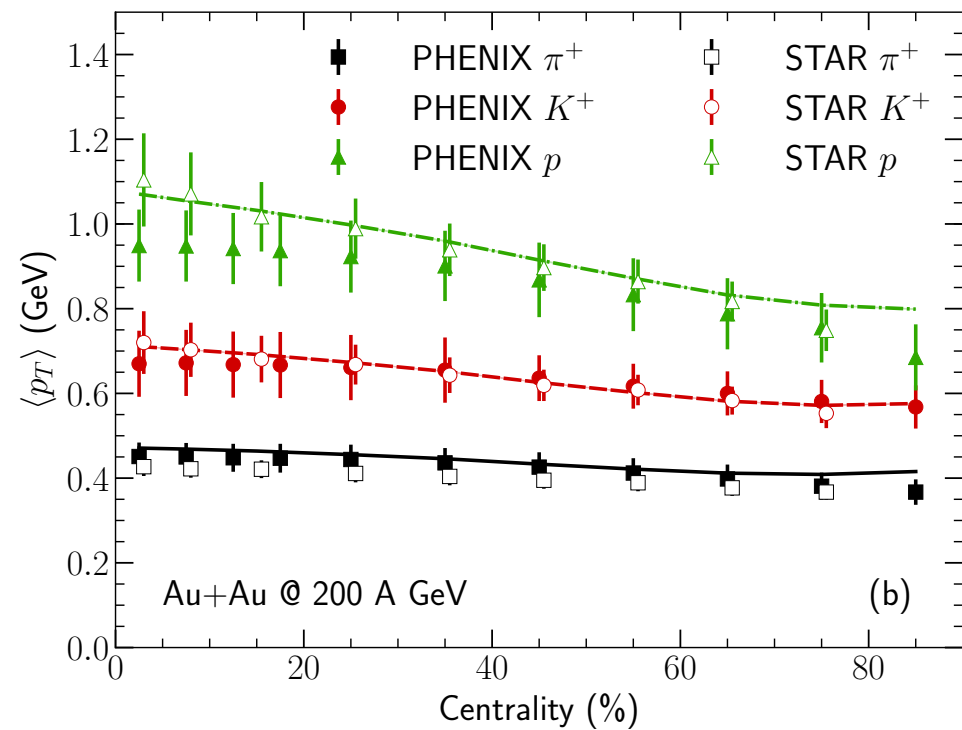
PHENIX Collaboration, arXiv:1805.02973v2



# Fix parameters in Au+Au

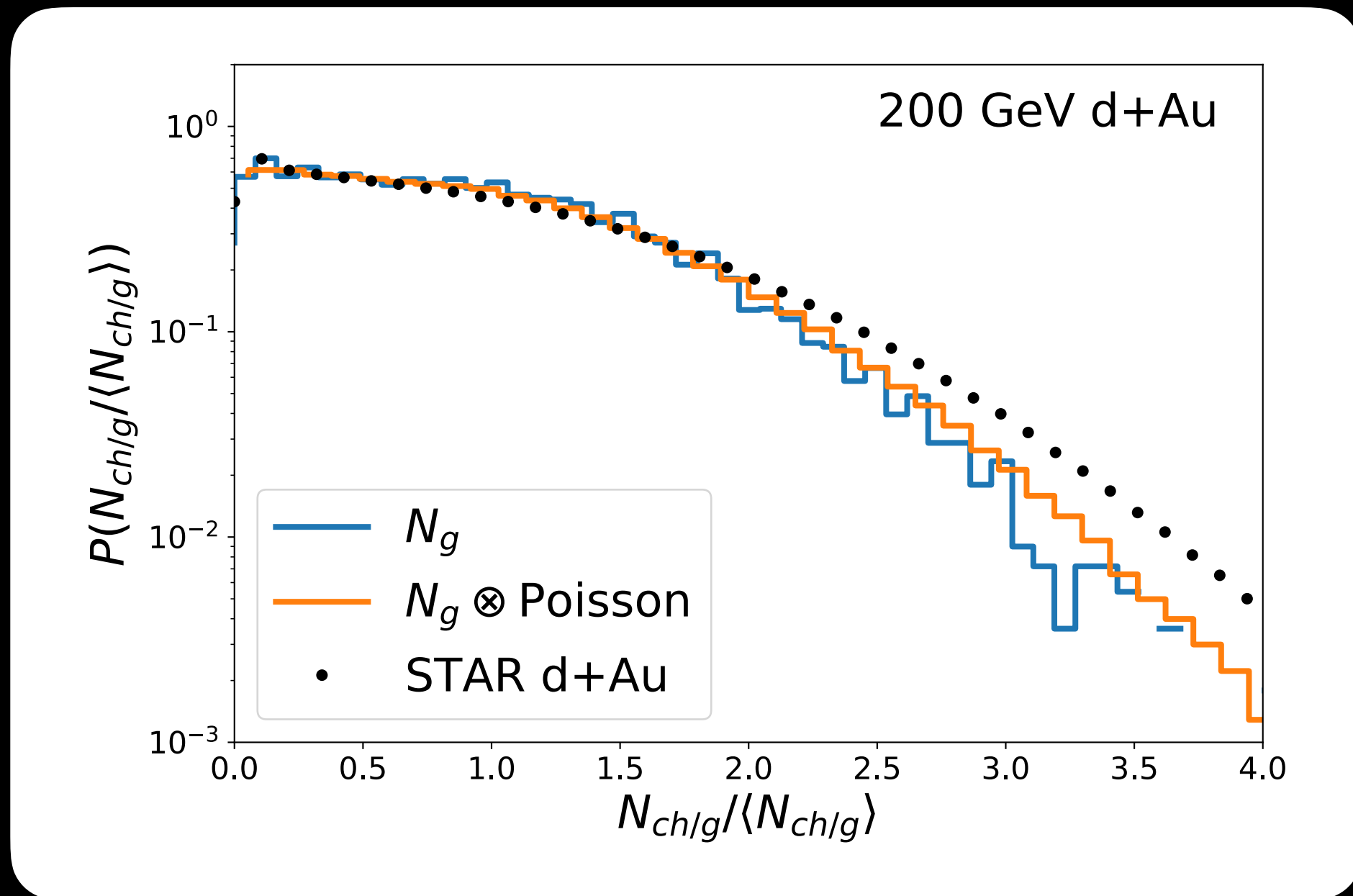
B. Schenke, C. Shen, P. Tribedy, in preparation

$\eta/s=0.12$



# RHIC system scan

B. Schenke, C. Shen, P. Tribedy, in preparation

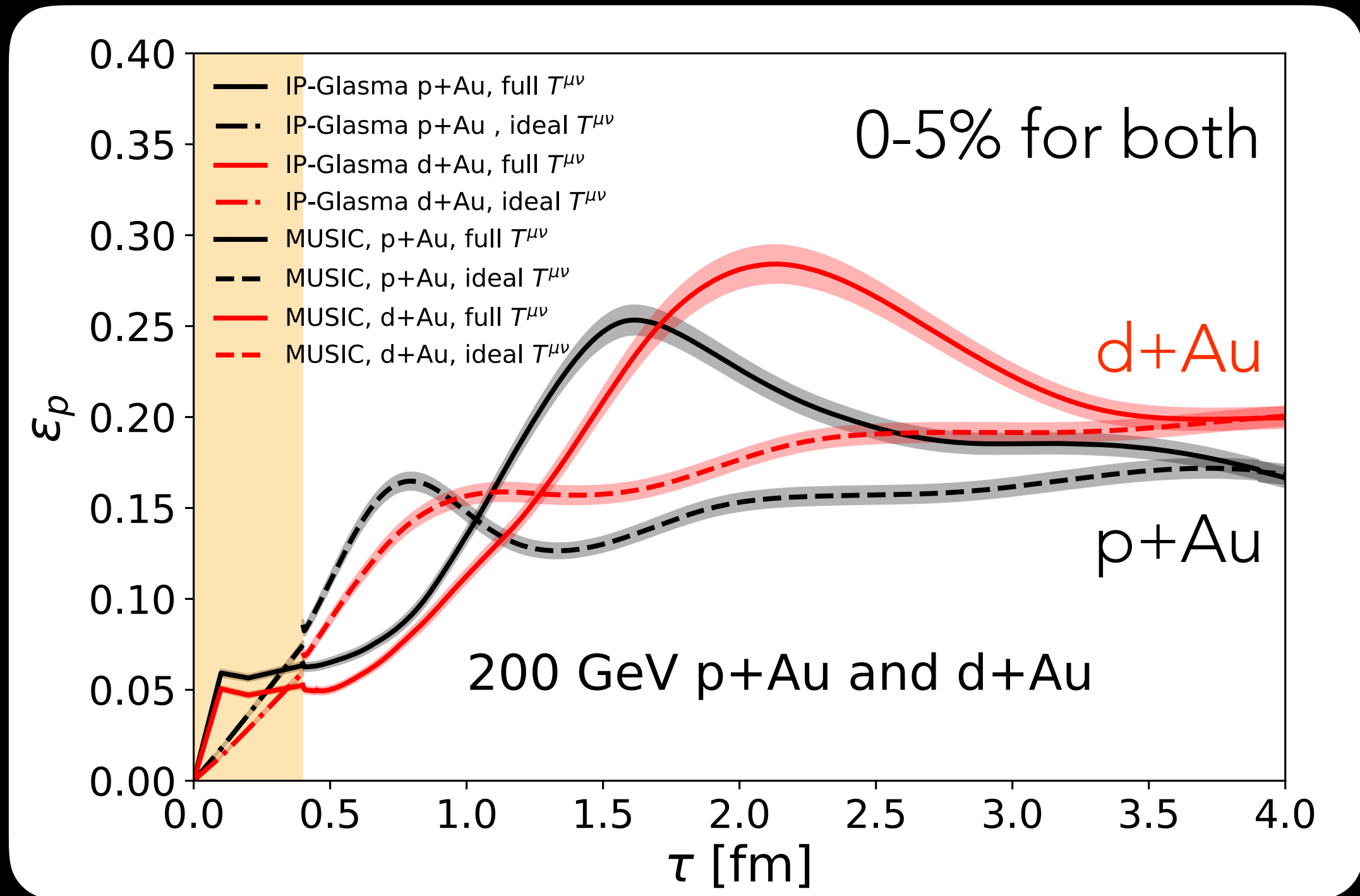


Multiplicity distribution: d+Au 200 GeV

# RHIC system scan

$$\epsilon_p = \sqrt{\frac{\langle T^{xx} - T^{yy} \rangle^2 + \langle 2T^{xy} \rangle^2}{\langle T^{xx} + T^{yy} \rangle^2}}$$

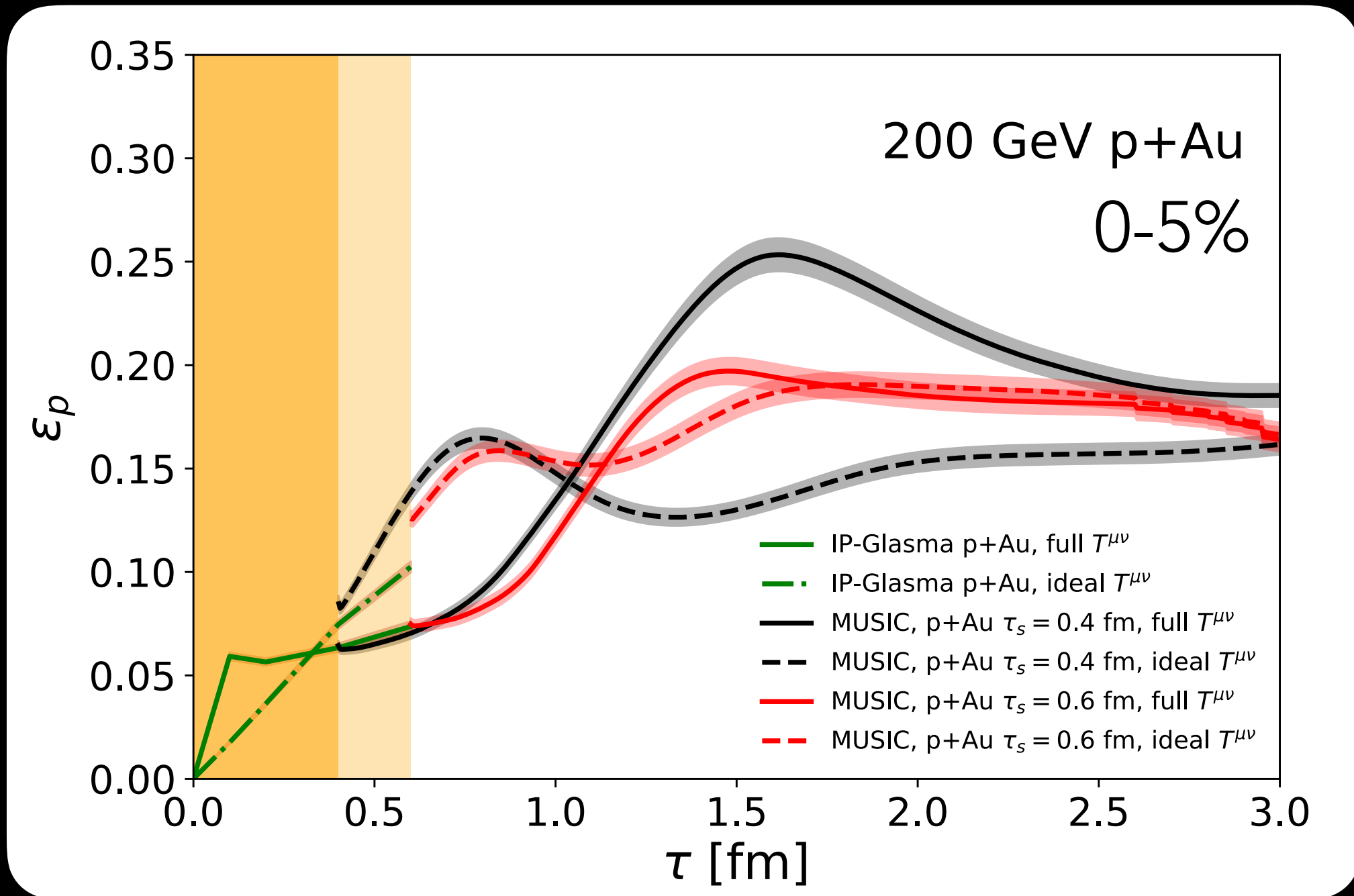
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# RHIC system scan

$$\epsilon_p = \sqrt{\frac{\langle T^{xx} - T^{yy} \rangle^2 + \langle 2T^{xy} \rangle^2}{\langle T^{xx} + T^{yy} \rangle^2}}$$

B. Schenke, C. Shen, P. Tribedy, in preparation

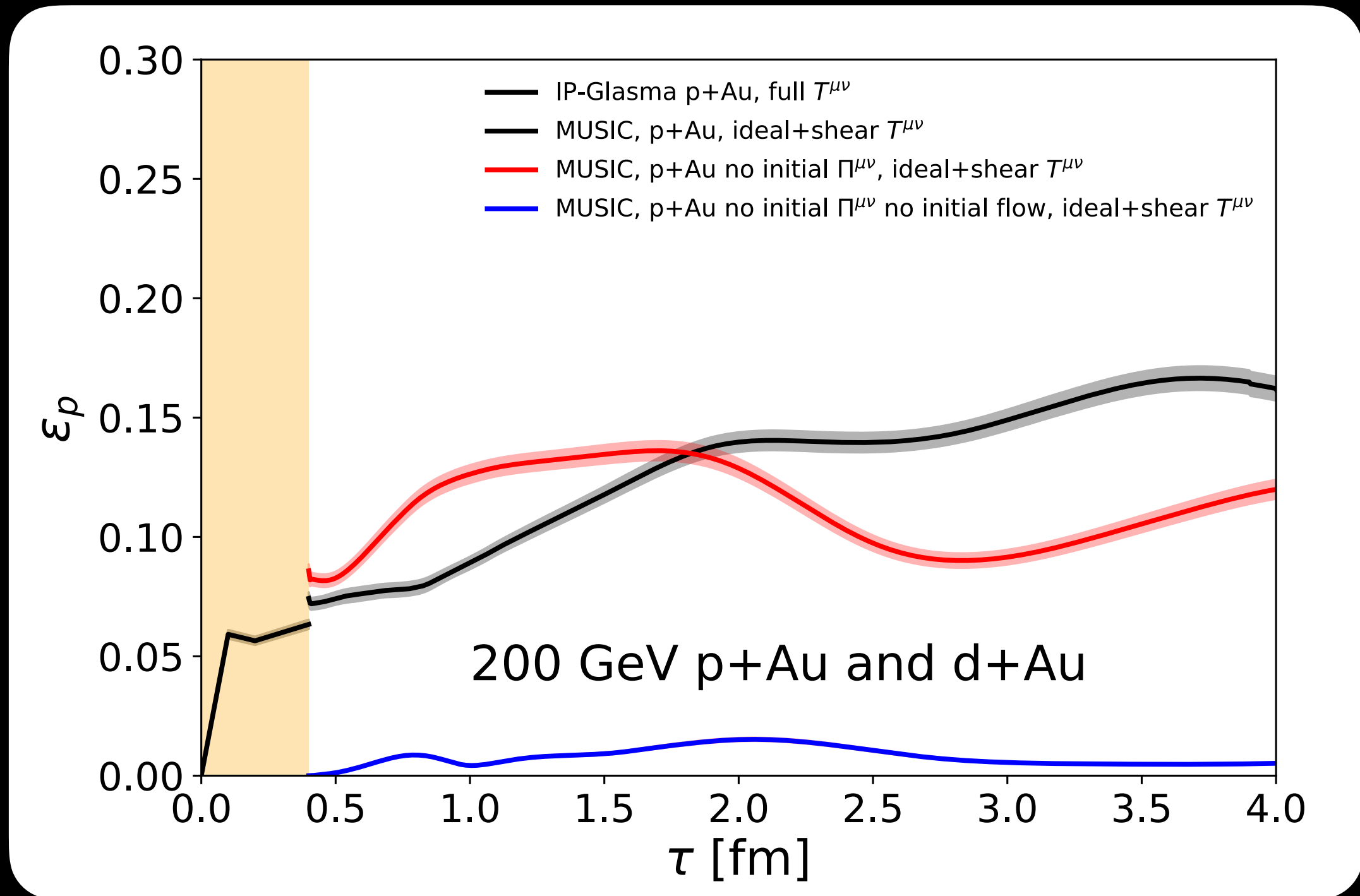


jump in ideal part from difference in P (EoS)

# RHIC system scan

$$\epsilon_p = \sqrt{\frac{\langle T^{xx} - T^{yy} \rangle^2 + \langle 2T^{xy} \rangle^2}{\langle T^{xx} + T^{yy} \rangle^2}}$$

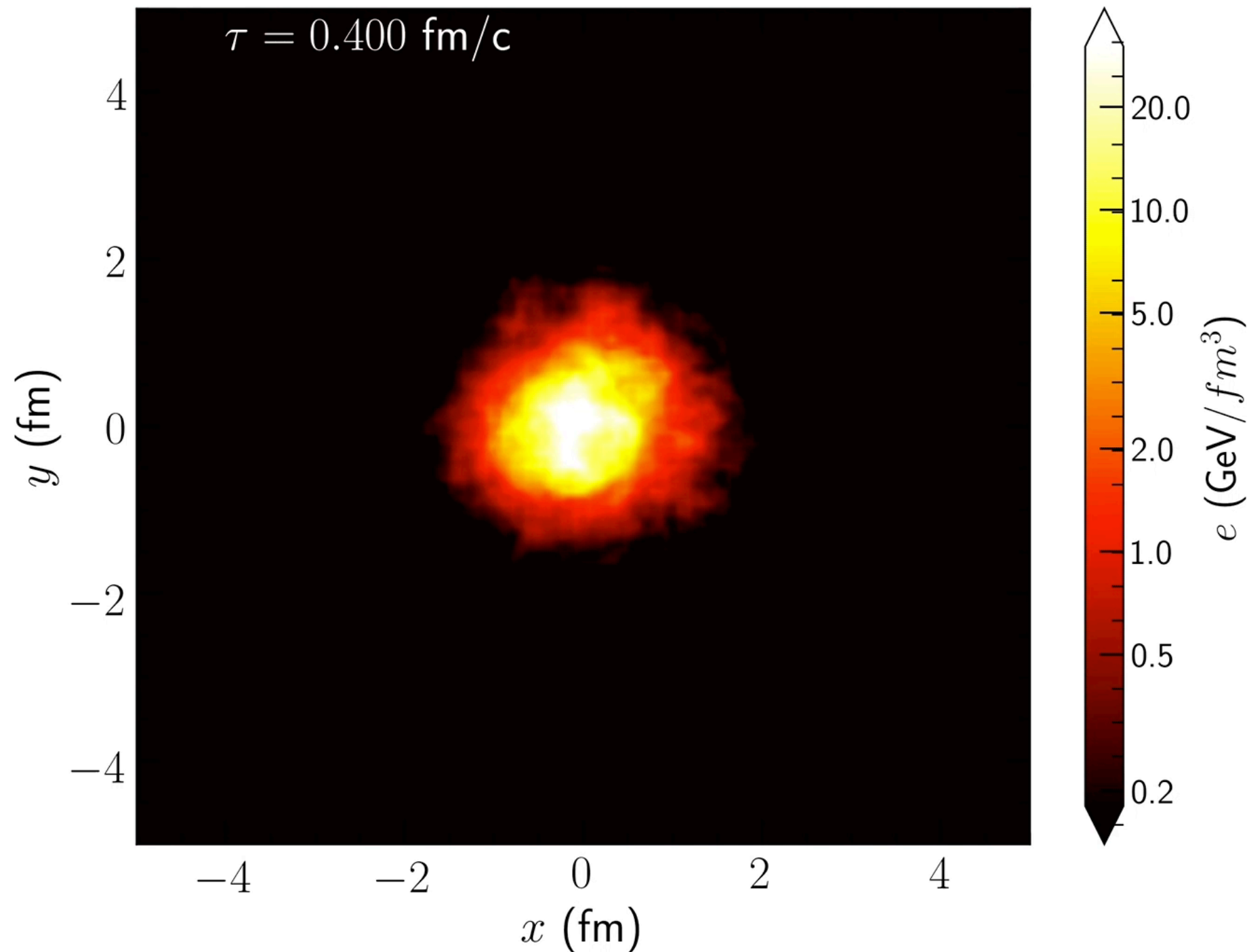
B. Schenke, C. Shen, P. Tribedy, in preparation





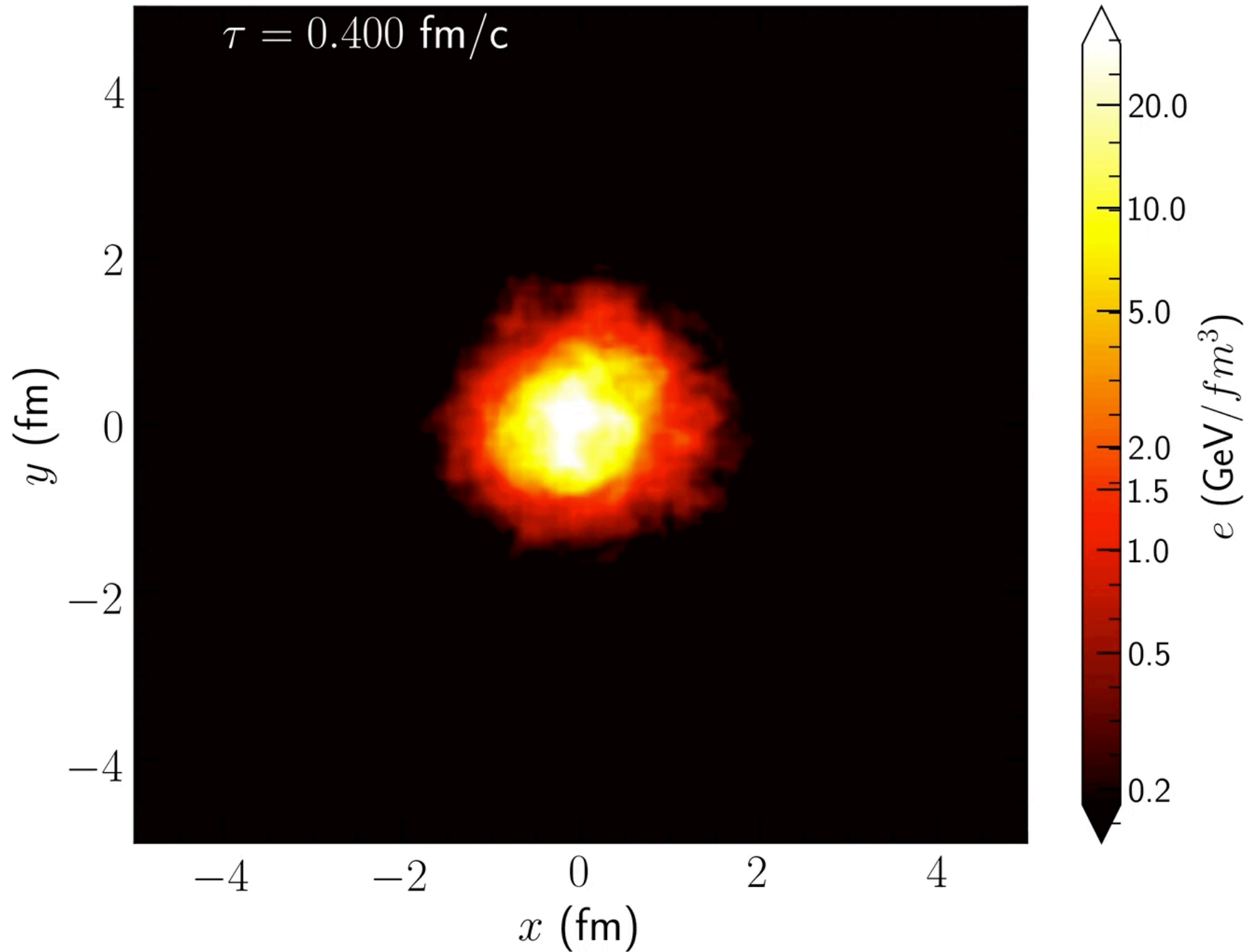
# RHIC system scan

B. Schenke, C. Shen, P. Tribedy, in preparation



# RHIC system scan

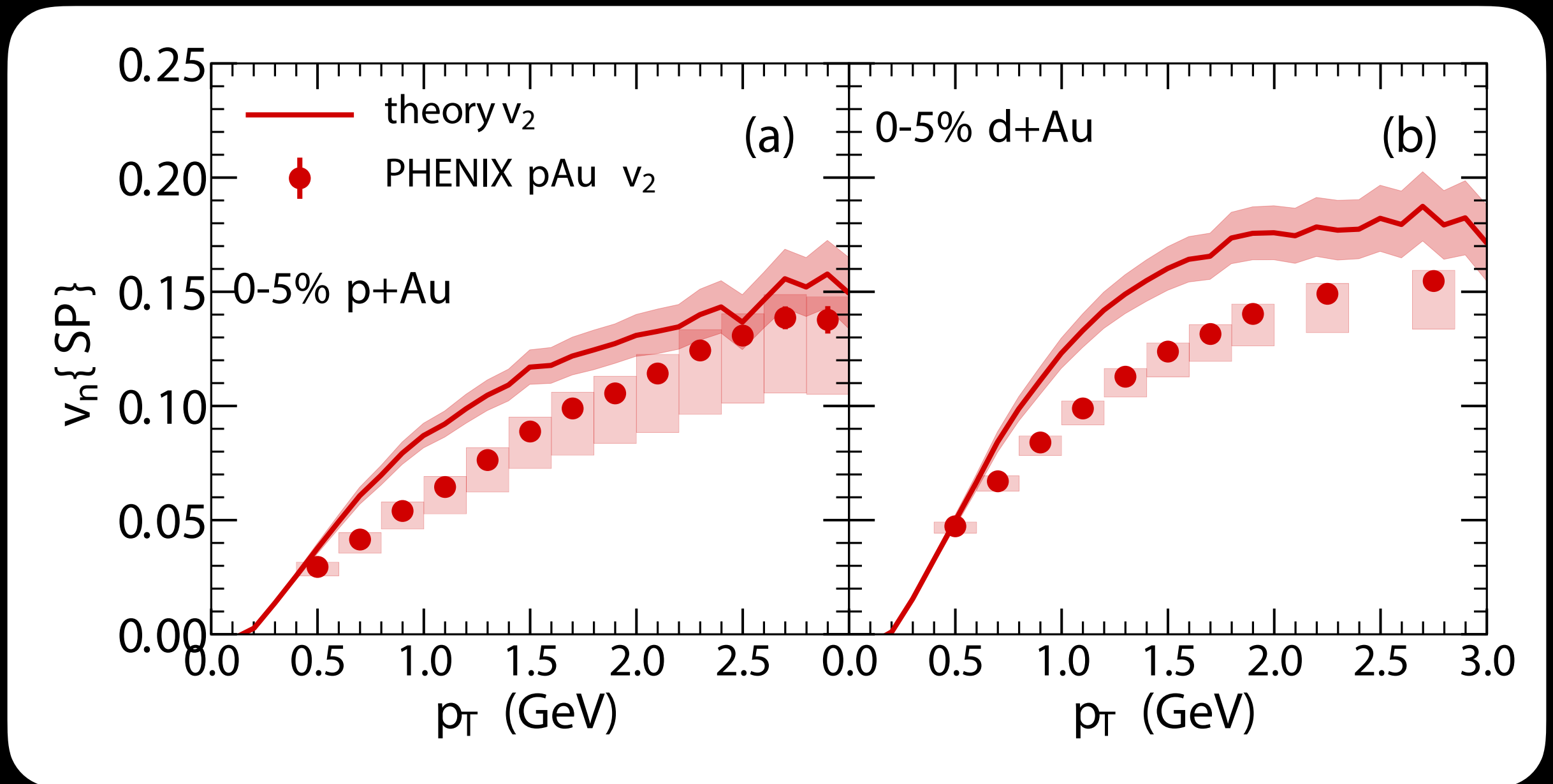
B. Schenke, C. Shen, P. Tribedy, in preparation



# $v_2$ in pAu and dAu at 0-5%

B. Schenke, C. Shen, P. Tribedy, in preparation

$\eta/s=0.12$

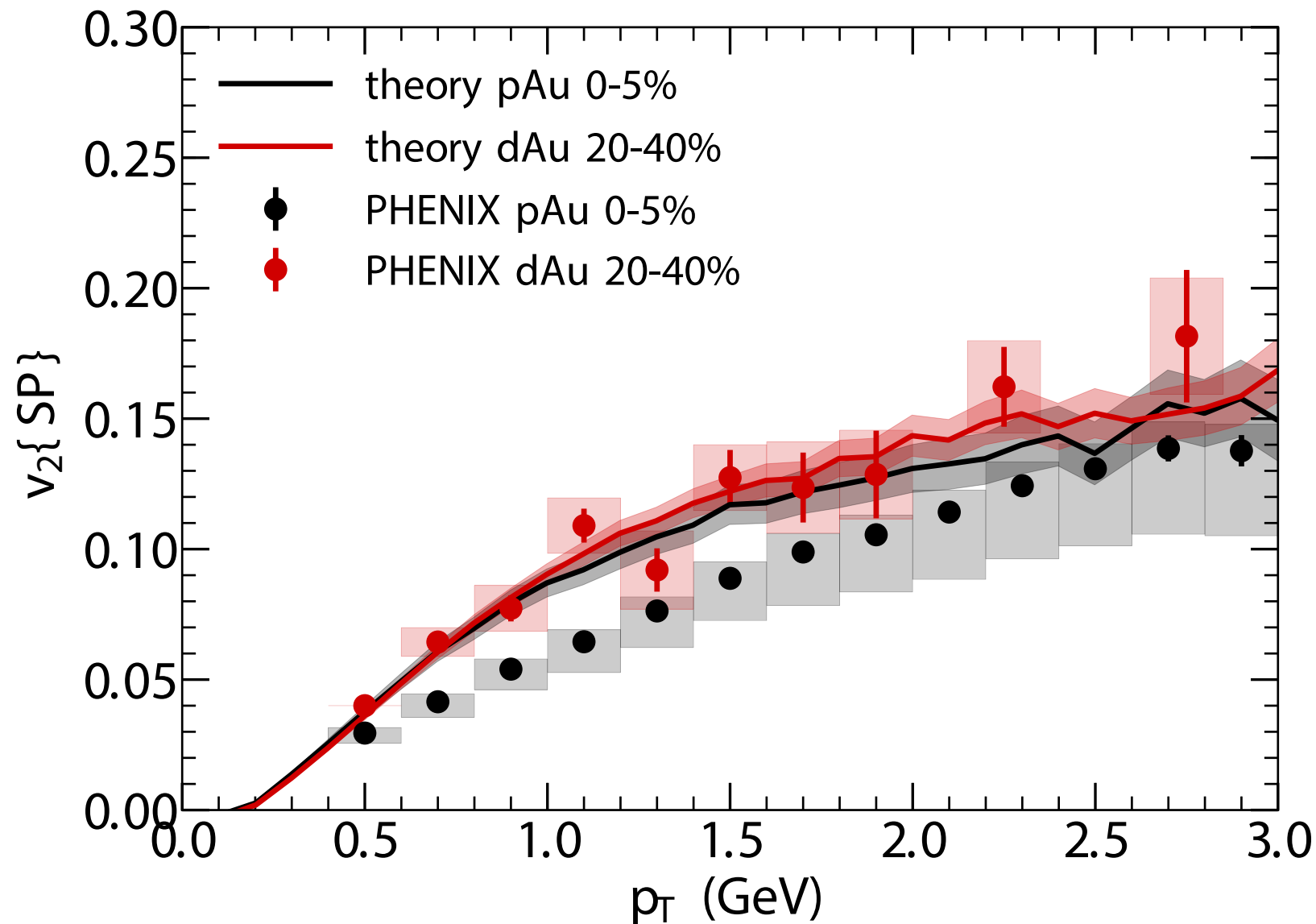


PHENIX Collaboration, e-Print: [arXiv:1805.02973](https://arxiv.org/abs/1805.02973)

Calculation:  $dN/d\eta = 19.6$  for dAu, 11.3 for pAu

# $v_2$ in pAu and dAu at $\sim$ same $N_{ch}$

B. Schenke, C. Shen, P. Tribedy, in preparation



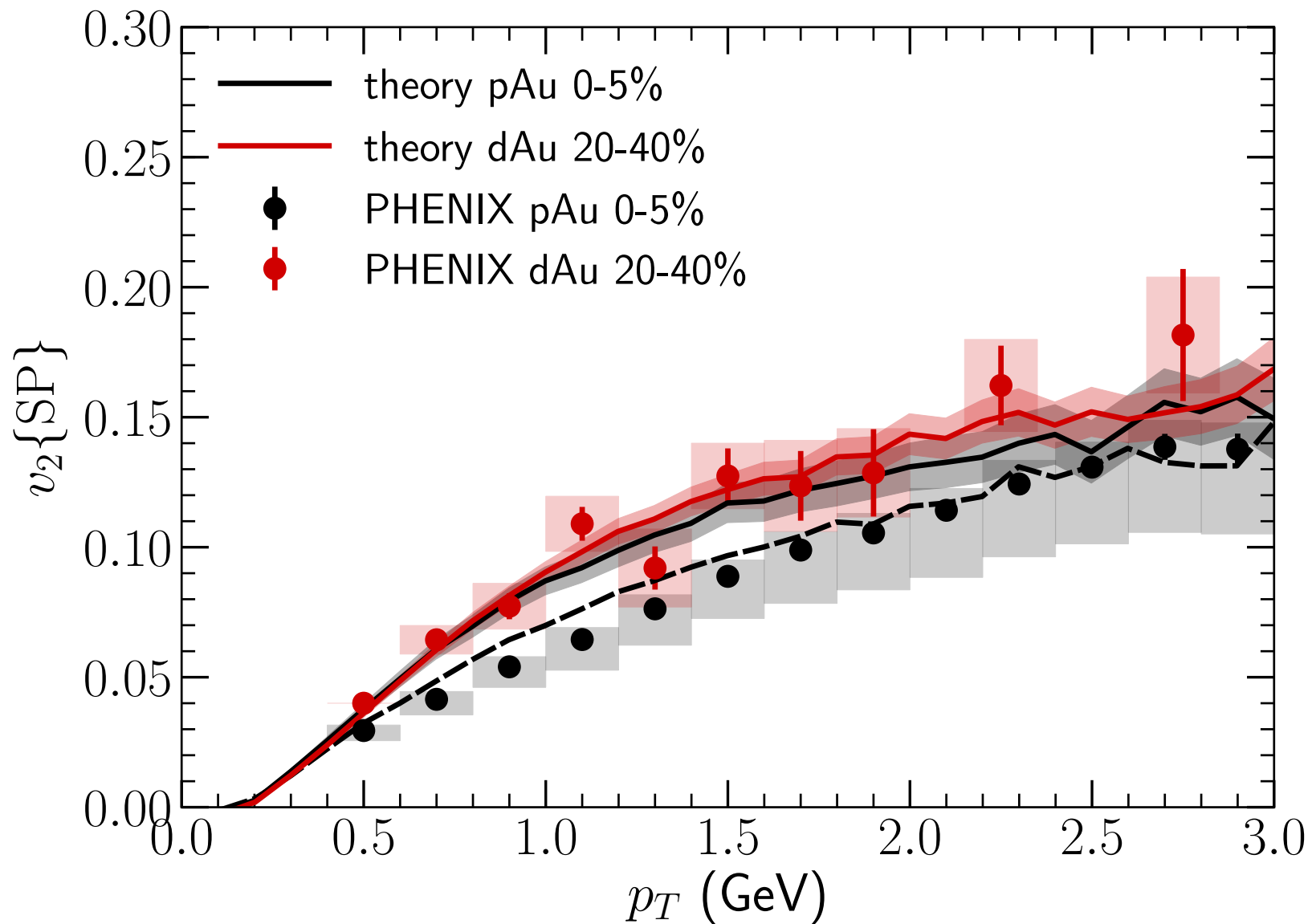
$\eta/s=0.12$

PHENIX Collaboration, e-Print: [arXiv:1805.02973](https://arxiv.org/abs/1805.02973)

Calculation:  $dN/d\eta = 9.8$  for dAu, 11.3 for pAu

# $v_2$ in pAu and dAu at $\sim$ same $N_{ch}$

B. Schenke, C. Shen, P. Tribedy, in preparation



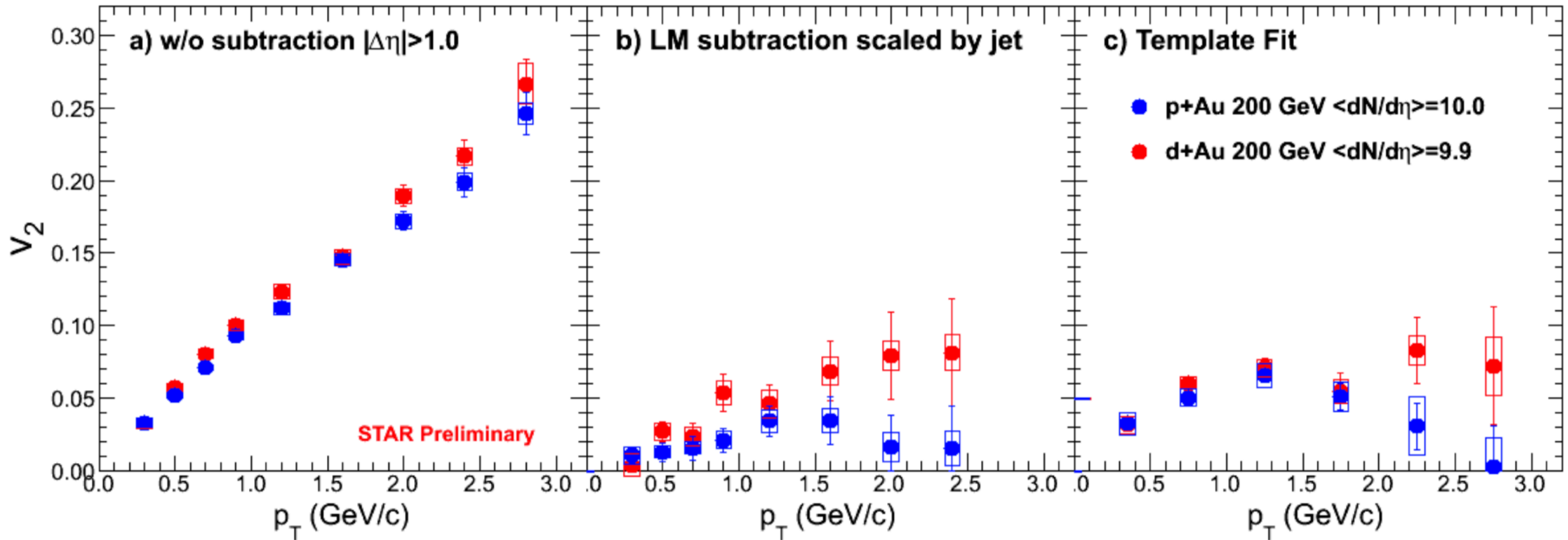
dashed line:  
different  
parameters for  
fluctuating  
proton

dAu  
little affected

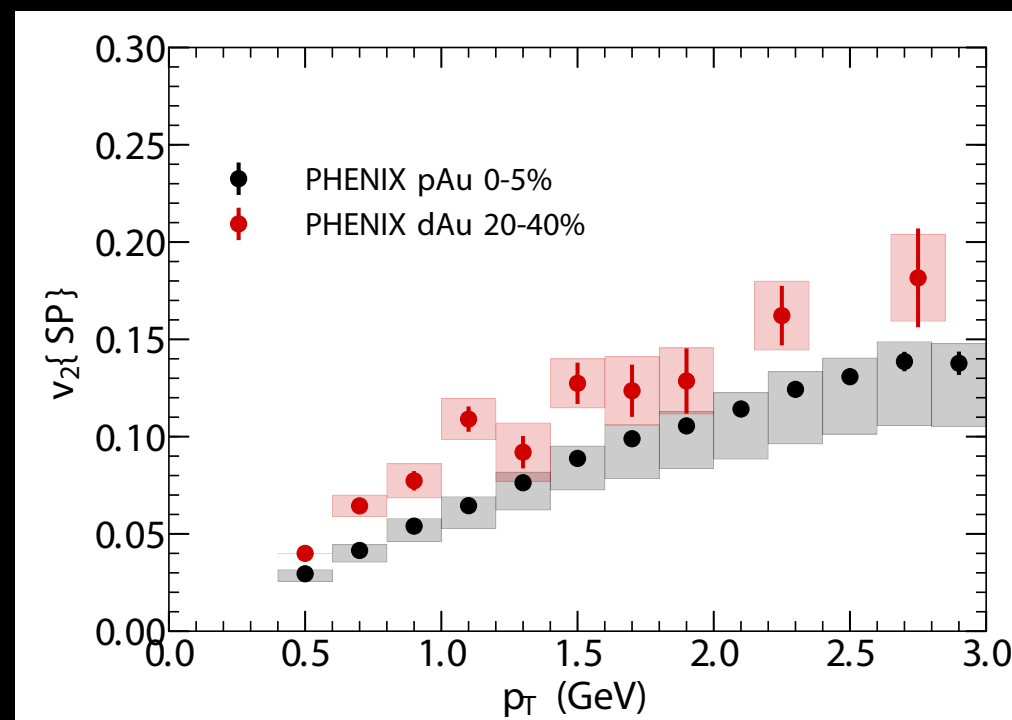
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# Data: $v_2$ in pAu and dAu at $\sim$ same $N_{ch}$

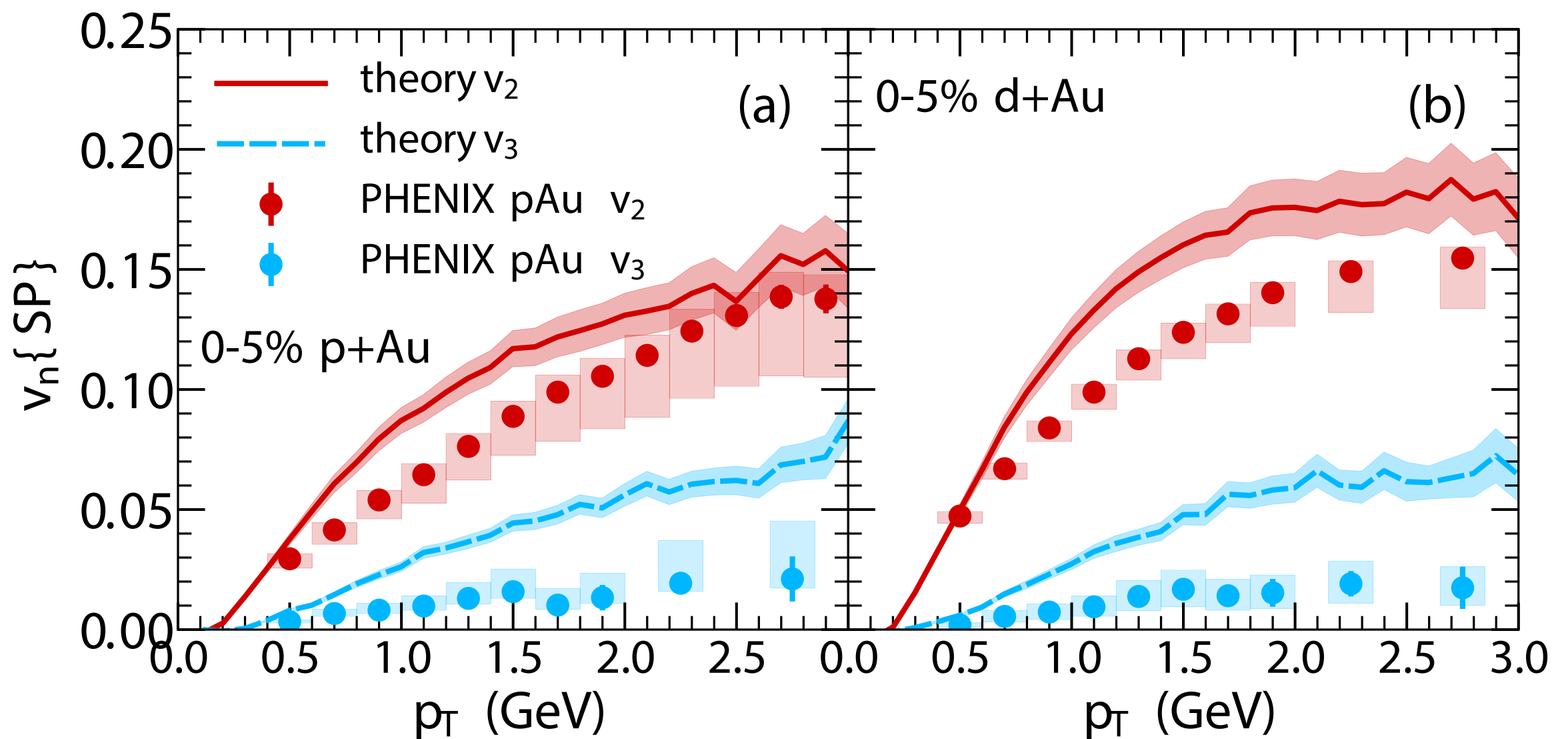


STAR Collaboration, talk by Shengli Huang, QM2018  
PHENIX Collaboration, e-Print: arXiv:1805.02973



# $v_3$ in pAu and dAu - too large...

B. Schenke, C. Shen, P. Tribedy, in preparation

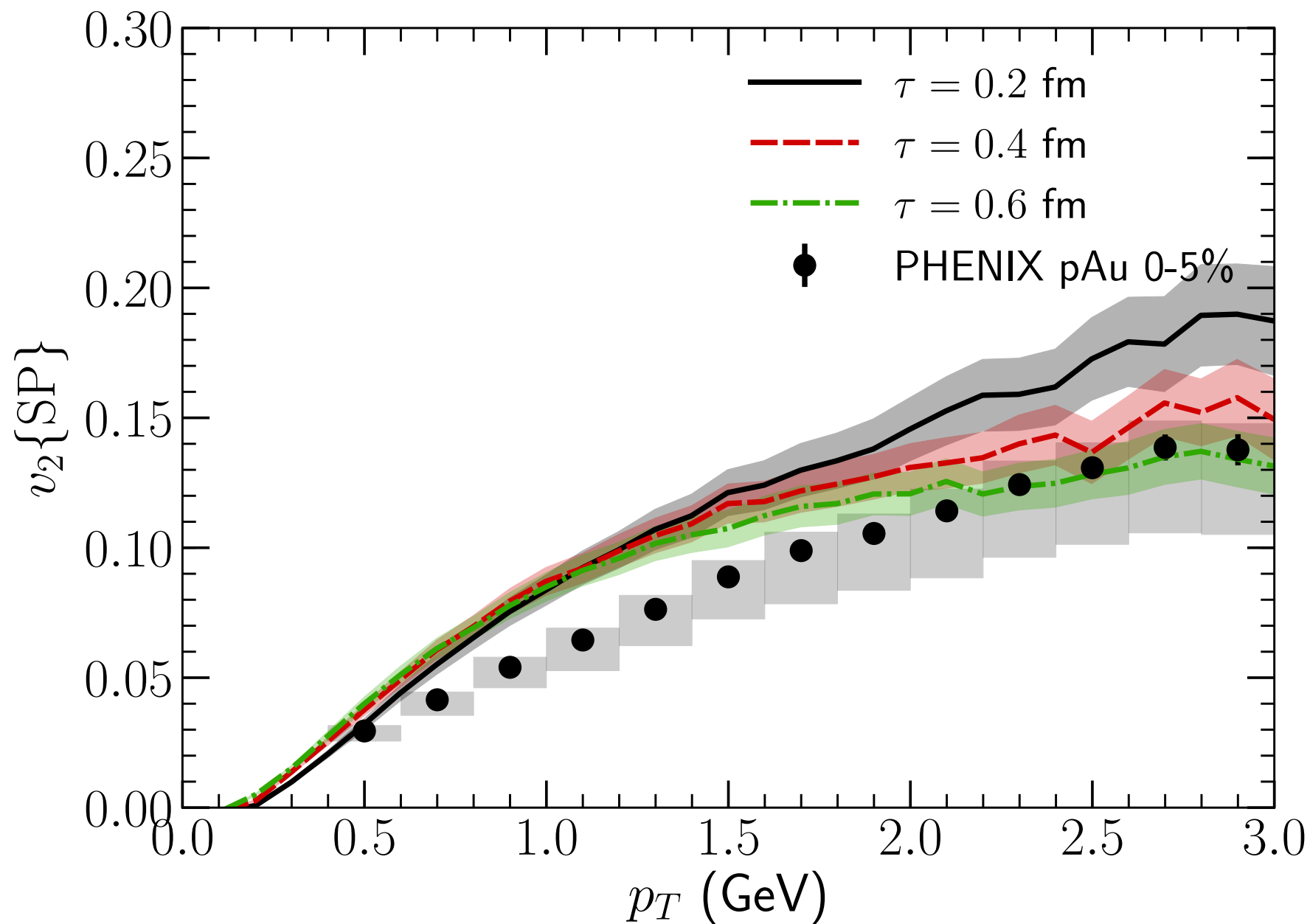


PHENIX Collaboration, e-Print: [arXiv:1805.02973](https://arxiv.org/abs/1805.02973)

Calculation:  $dN/d\eta = 19.6$  for dAu, 11.3 for pAu

# Effect of switching time on $v_2$

B. Schenke, C. Shen, P. Tribedy, in preparation



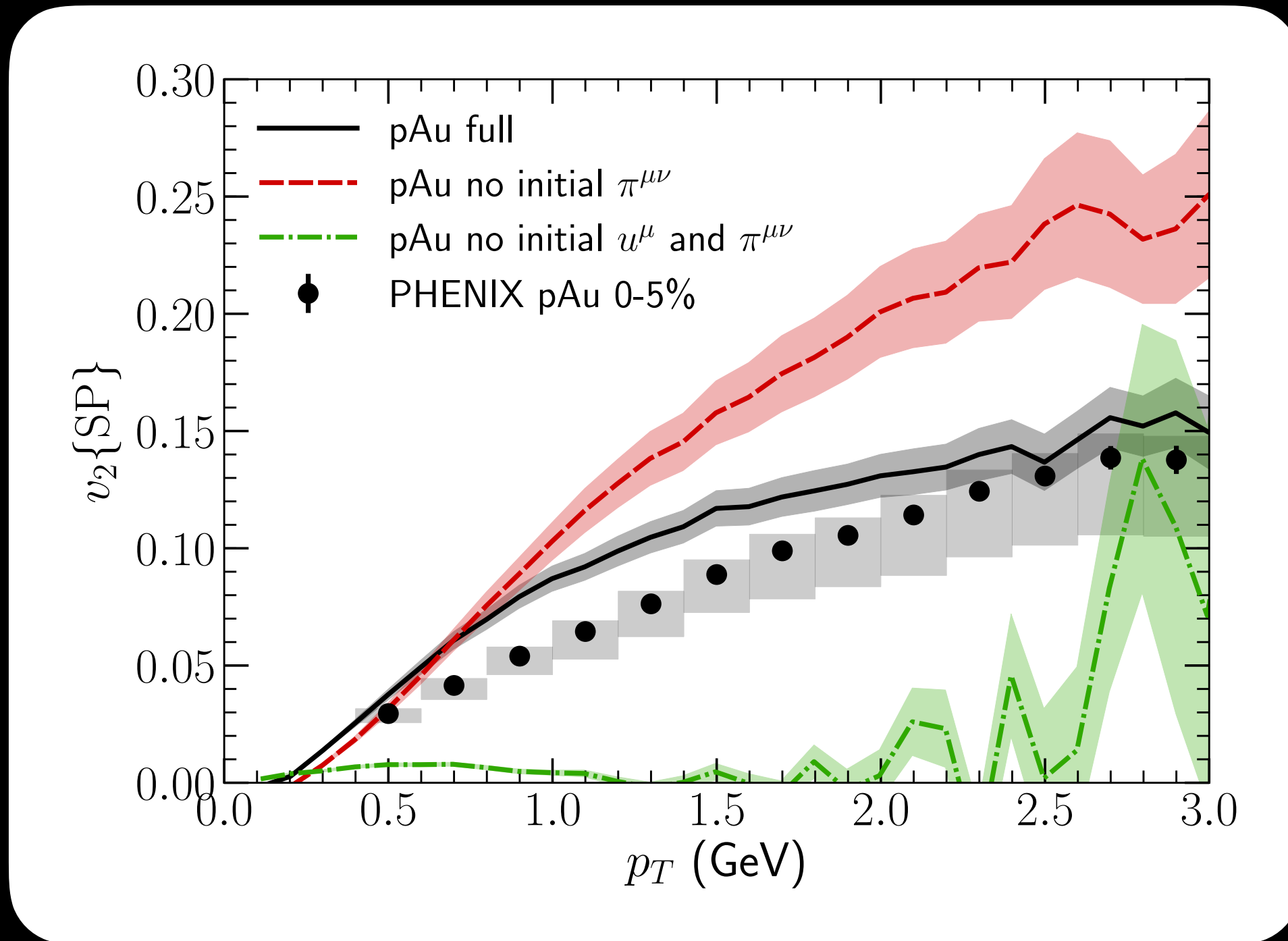
larger  
initial  $\pi^{\mu\nu}$  for  
later  
switching  
time:  
reduction of  
 $v_2$  at high  $p_T$



# Effect of initial flow and viscous tensor

B. Schenke, C. Shen, P. Tribedy, in preparation

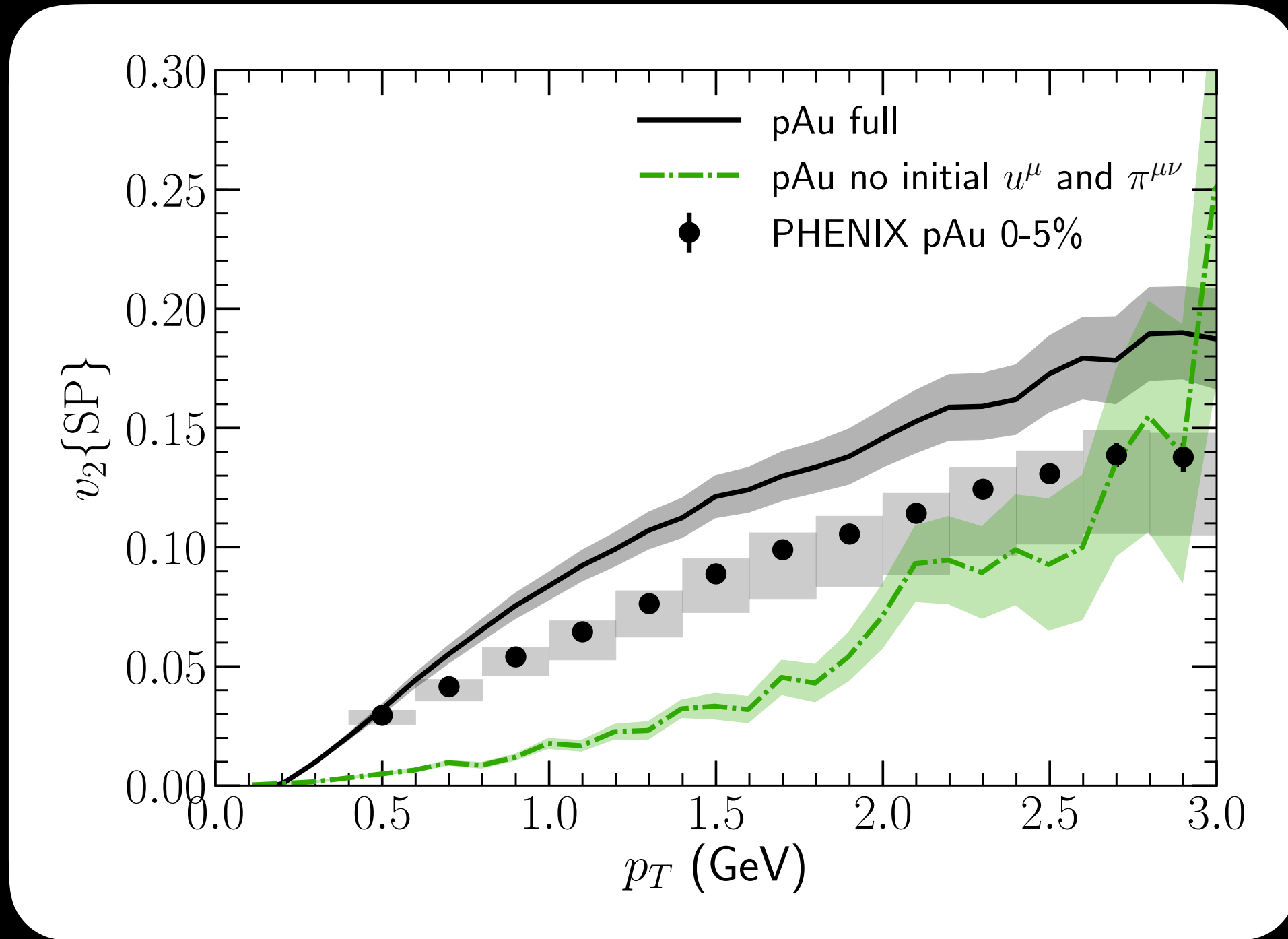
$\tau_0=0.4\text{fm}$



# Effect of initial flow

B. Schenke, C. Shen, P. Tribedy, in preparation

$\tau_0=0.2\text{fm}$



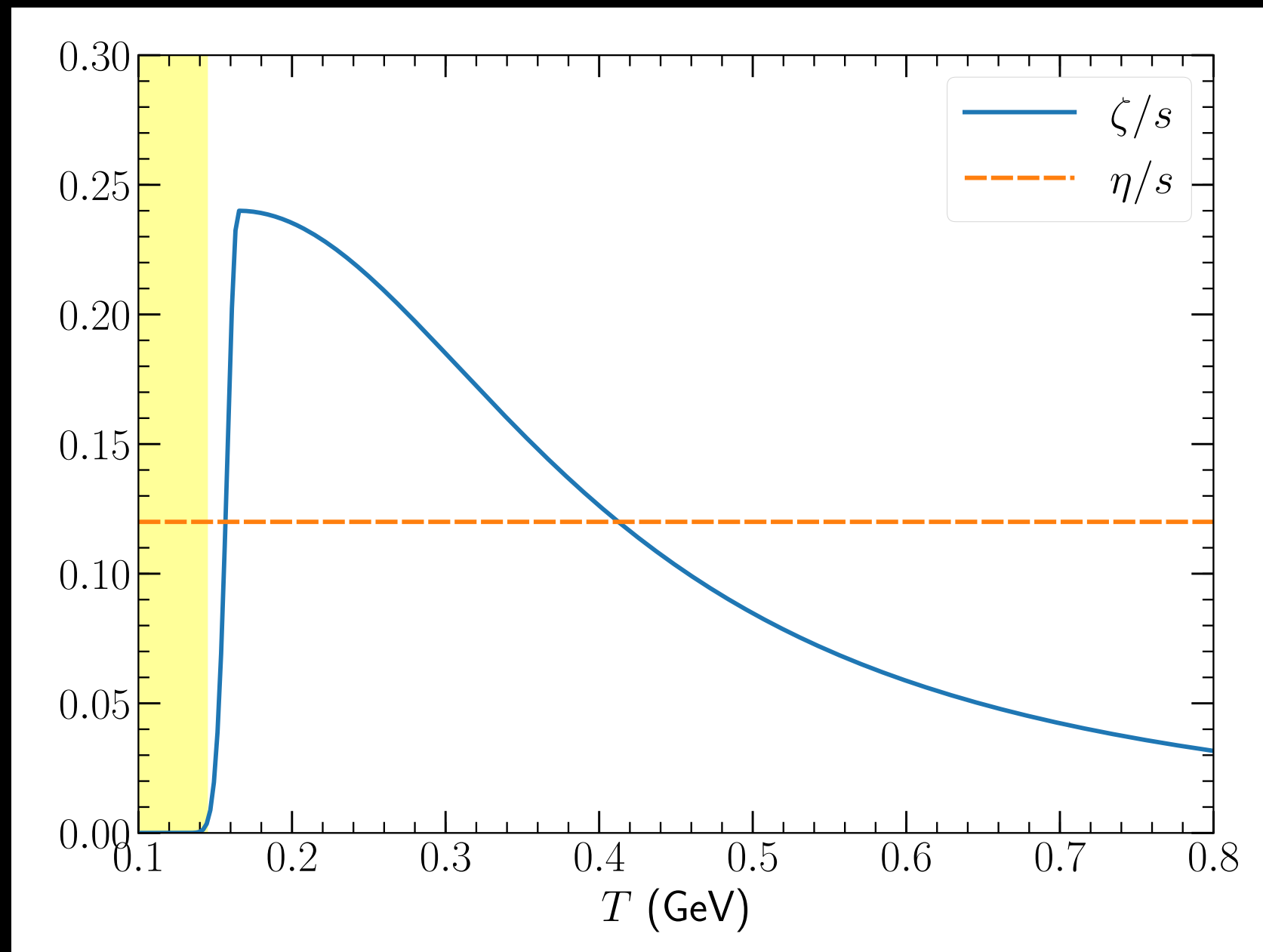
A photograph of the Seattle skyline at sunset, viewed from a distance across a body of water. The sky is a mix of orange, yellow, and blue, and the city lights are visible against the horizon. The Space Needle is prominent on the right side of the skyline.

# Conclusions

- Heavy ions well described by hydrodynamics for range of  $>2$  orders of magnitude in multiplicity
- **Initial state contributes** to the final anisotropy in p+A depending on switching time and transport params.
- Large bulk viscosity is a problem: causes negative pressures and large  $\delta f$ -corrections - seems to dominate evolution in small systems
- High sensitivity to initial flow, viscous tensor, in small systems at RHIC - can we trust hydro there?

# Backup

# MODIFIED BULK VISCOSITY



For RHIC we used broader bulk viscosity with lower peak and more extreme drop above the switching temperature

Will redo LHC calculations with this too

# PROTON SHAPE FLUCTUATIONS

Do not only sample nucleon positions  
but also gluonic hot spots inside a nucleon  
(e.g. around 3 valence quarks)

Will mostly make a difference for the geometry in  $p+A$   
and  $p+p$  collisions

Next:

Constrain the size and distribution of these hot spots  
using data from  $e+p$  collisions

# Diffractive $J/\Psi$ production

H. Mäntysaari, B. Schenke, Phys. Rev. Lett. 117 (2016) 052301; Phys.Rev. D94 (2016) 034042

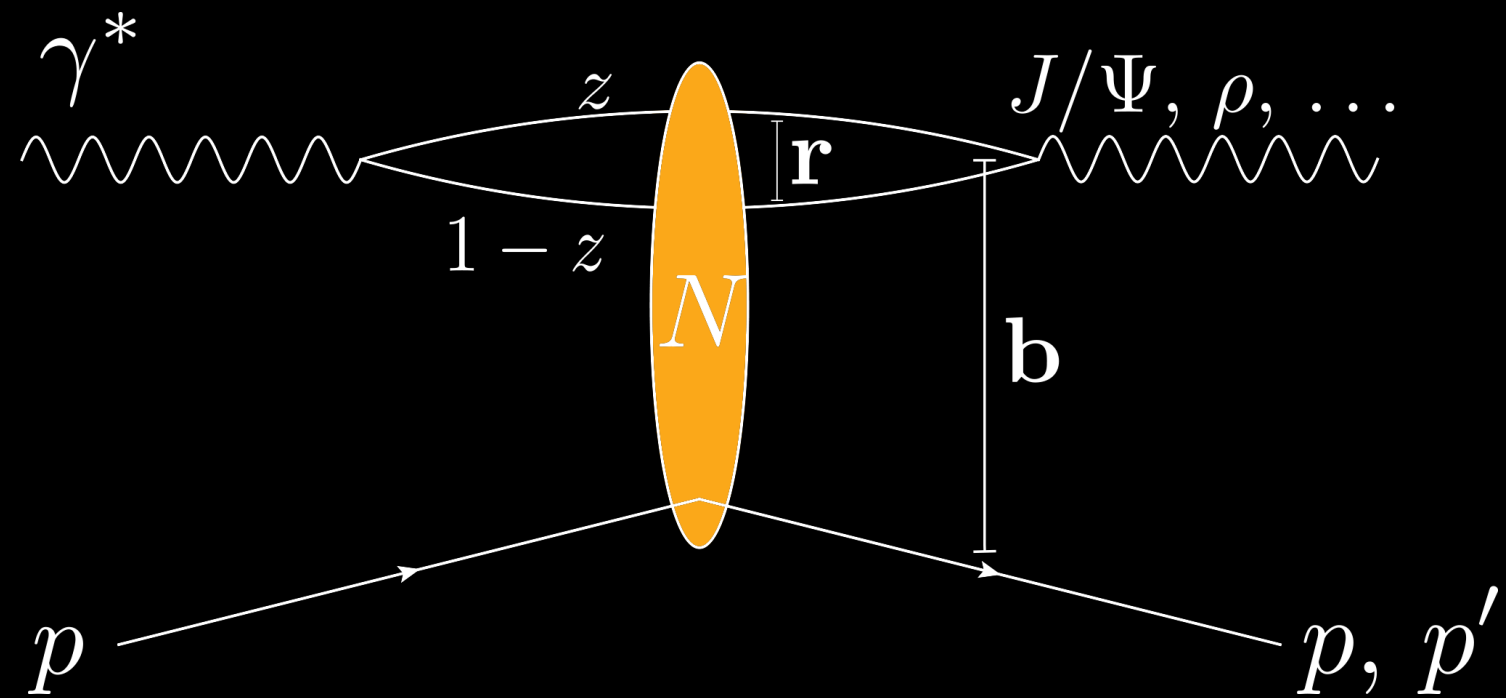
No exchange of color charge  
→ Large rapidity gap

Coherent diffraction:

Proton remains intact, Sensitive to average gluon distribution in the proton

Incoherent diffraction:

Proton breaks up, Sensitive to shape fluctuations



# CGC Framework $J/\Psi$ production

H. Mäntysaari, B. Schenke, *Phys. Rev. Lett.* 117 (2016) 052301; *Phys.Rev.* D94 (2016) 034042

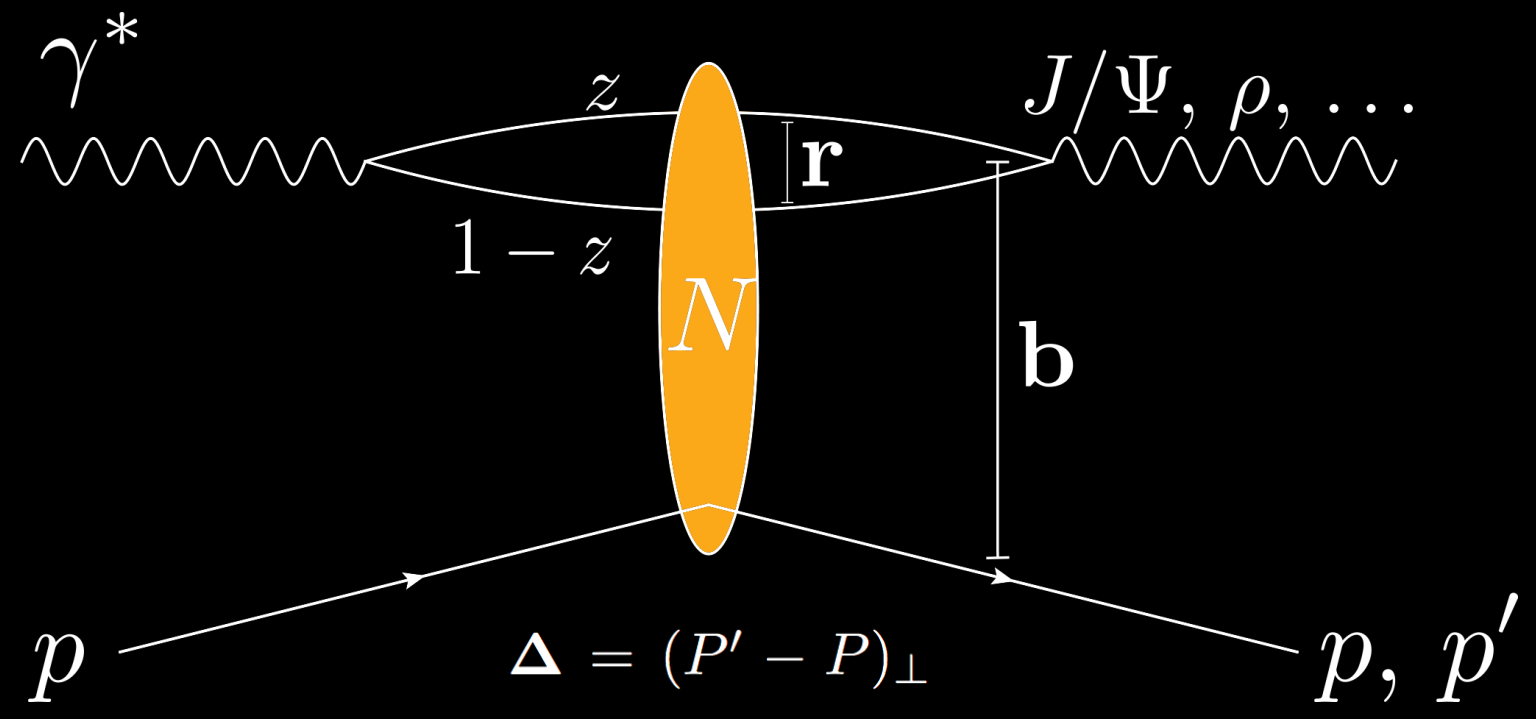
Diffractive eigenstates are color dipoles

at fixed  $r_T$  and  $b_T$

see

M. L. Good and W. D. Walker

*Phys. Rev.* 120 (1960) 1857.



Scattering amplitude

$$A \sim \int d^2 b dz d^2 r \psi^* \psi^V(r, z, Q^2) e^{-ib \cdot \Delta} N(r, x, b)$$

Dipole amplitude  $N$  determined in IPsat or IP-Glasma



# Averaging over the target

H. Mäntysaari, B. Schenke, Phys. Rev. Lett. 117 (2016) 052301; Phys.Rev. D94 (2016) 034042

COHERENT DIFFRACTION:  
TARGET STAYS INTACT

$$\frac{d\sigma^{\gamma^* p \rightarrow Vp}}{dt} = \frac{1}{16\pi} \left| \langle \mathcal{A}^{\gamma^* p \rightarrow Vp}(x_{\mathbb{P}}, Q^2, \Delta) \rangle \right|^2$$

INCOHERENT DIFFRACTION:  
TARGET BREAKS UP

$$\frac{d\sigma^{\gamma^* p \rightarrow Vp^*}}{dt} = \frac{1}{16\pi} \left( \left\langle \left| \mathcal{A}^{\gamma^* p \rightarrow Vp}(x_{\mathbb{P}}, Q^2, \Delta) \right|^2 \right\rangle - \left| \langle \mathcal{A}^{\gamma^* p \rightarrow Vp}(x_{\mathbb{P}}, Q^2, \Delta) \rangle \right|^2 \right)$$

SENSITIVE TO FLUCTUATIONS!

SEE

H. I. MIETTINEN  
AND J. PUMPLIN  
PHYS. REV. D18 (1978) 1696

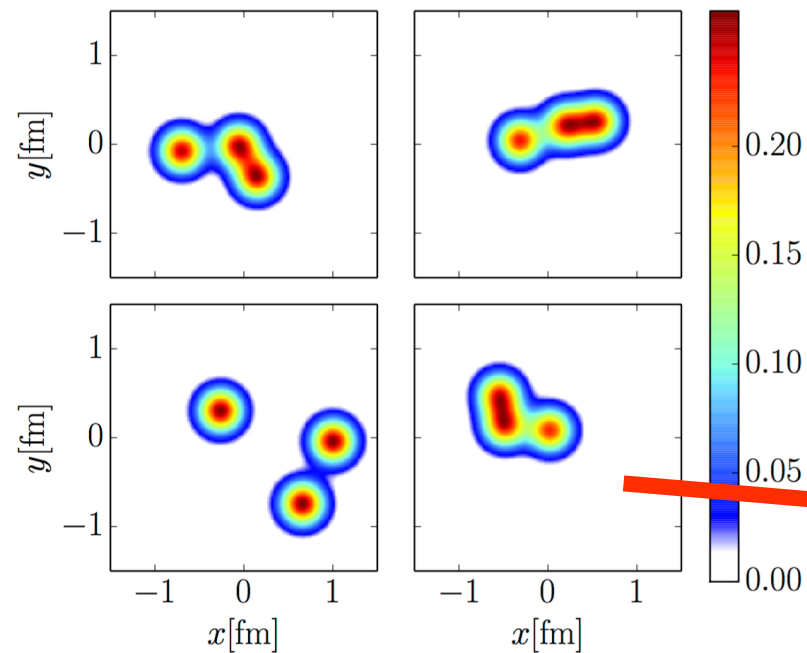
Y. V. KOVCHEGOV  
AND L. D. MCLERRAN  
PHYS. REV. D60 (1999) 054025

A. KOVNER AND  
U. A. WIEDEMANN  
PHYS. REV. D64 (2001) 114002

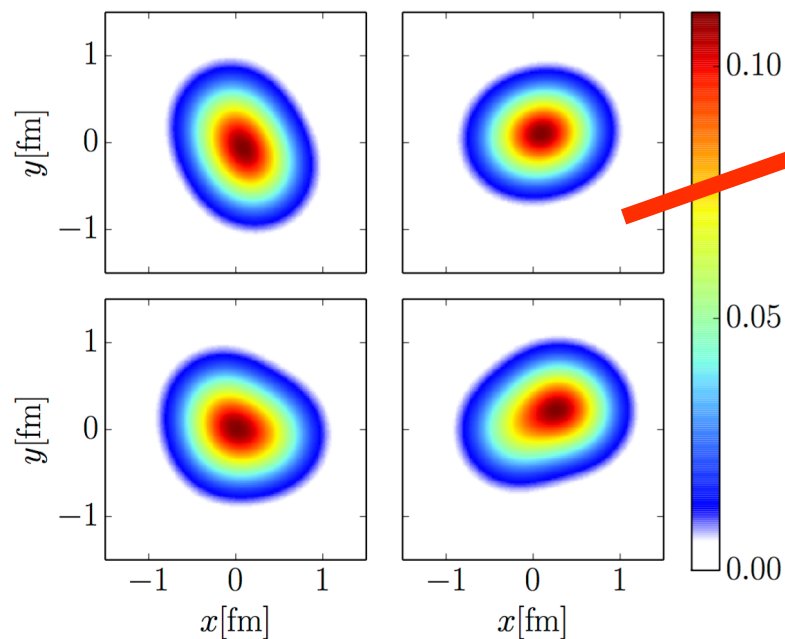
# Introduce geometric fluctuations

Assume 3 valence quark-like hot spots

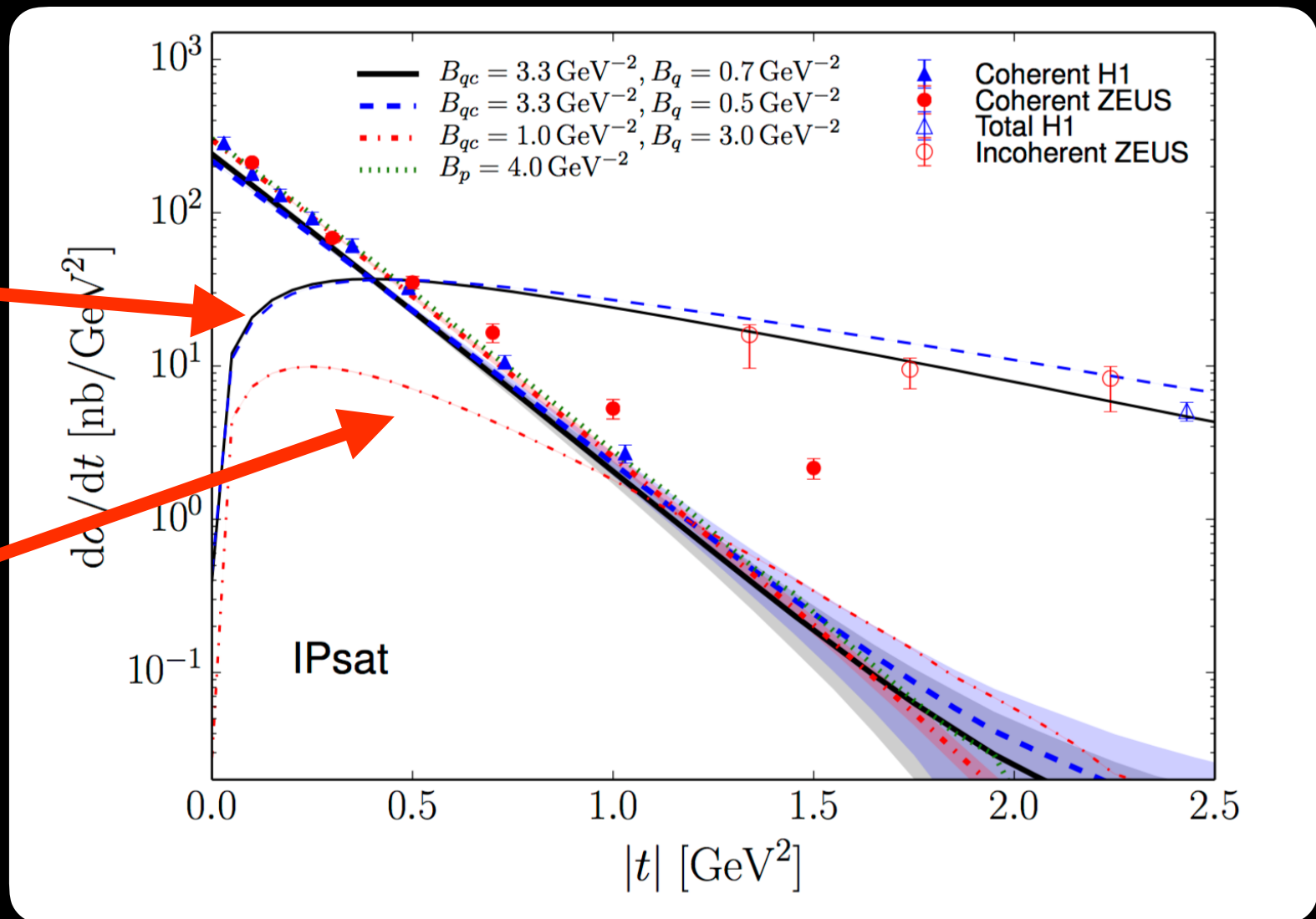
H. Mäntysaari, B. Schenke, *Phys. Rev. Lett.* 117 (2016) 052301  
*Phys.Rev. D*94 (2016) 034042



(a)  $B_{qc} = 3.3 \text{ GeV}^{-2}, B_q = 0.7 \text{ GeV}^{-2}$



(b)  $B_{qc} = 1.0 \text{ GeV}^{-2}, B_q = 3.0 \text{ GeV}^{-2}$



H1 collaboration, *Eur. Phys. J. C*46 (2006) 585,

*Phys. Lett. B*568 (2003) 205

ZEUS collaboration, *Eur. Phys. J. C*24 (2002) 345

*Eur. Phys. J. C*26 (2003) 389

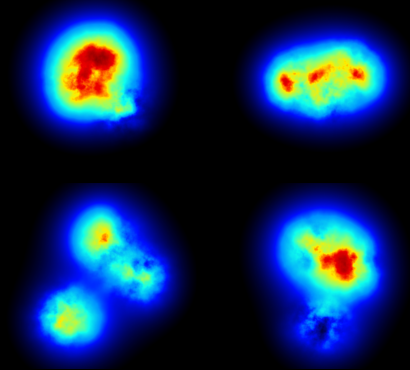
# IP-Glasma calculation

H. Mäntysaari, B. Schenke, *Phys. Rev. Lett.* 117 (2016) 052301; *Phys.Rev. D*94 (2016) 034042

Geometric + color charge fluctuations

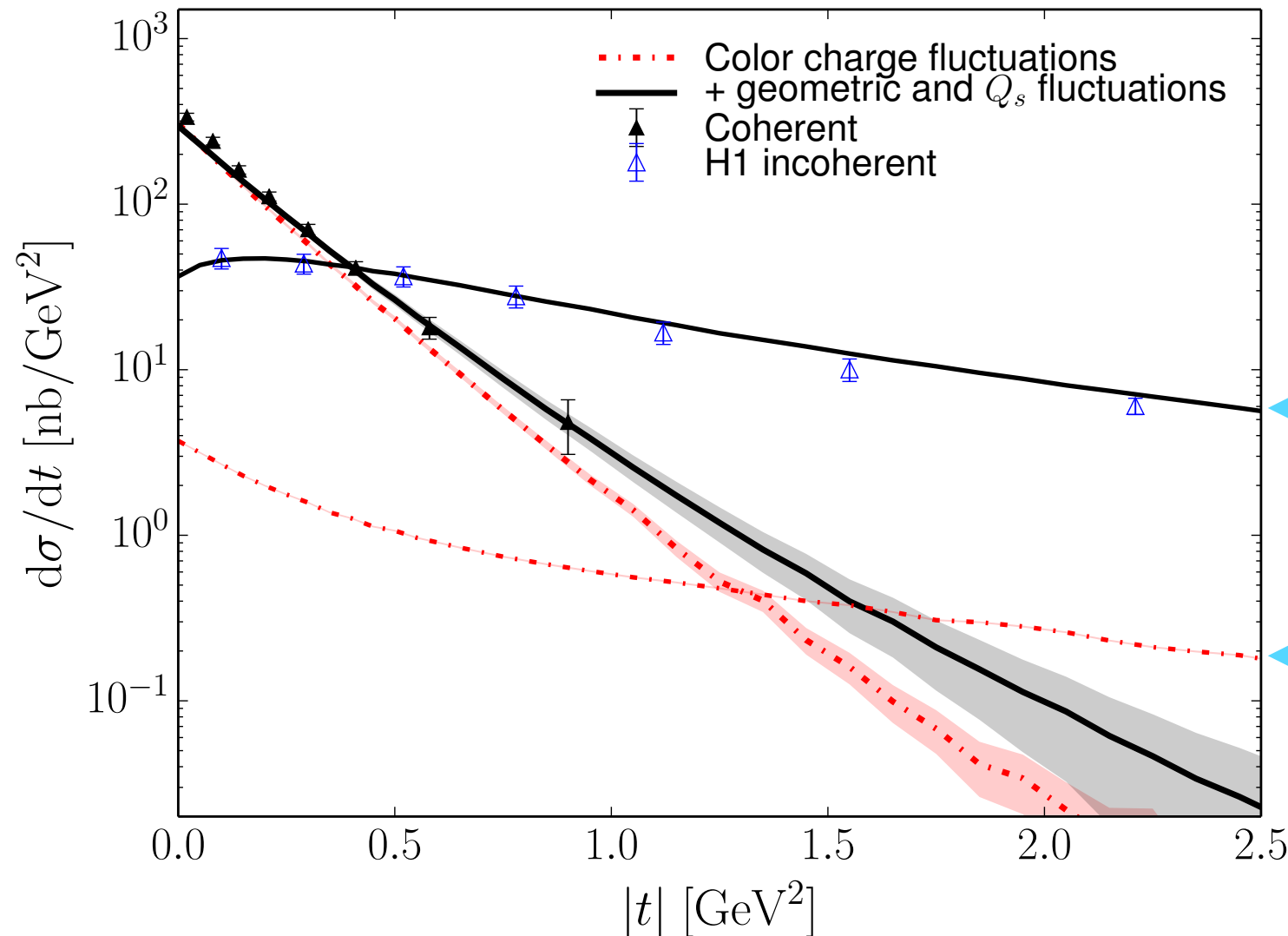
Dipole amp.:  $N(\vec{r}, x_{\mathbb{P}}, \vec{b}) = N(\vec{x} - \vec{y}, x_{\mathbb{P}}, (\vec{x} + \vec{y})/2) = 1 - \text{Tr} V(\vec{x}) V^\dagger(\vec{y}) / N_c$

Wilson lines



tuned shape fluctuations

round proton



H1 Collaboration, *Eur. Phys. J. C*73 (2013) no. 6 2466

# IP-Glasma + parton cascade

M. Greif, C. Greiner, B. Schenke, S. Schlichting, Z. Xu, arXiv:1708.02076, Phys. Rev. D96, 091509(R)

To study how final state interactions affect the initial state correlations, we use a microscopic final state model, the parton cascade BAMPS

Z.Xu, C. Greiner, PRC71, 064901 (2005)



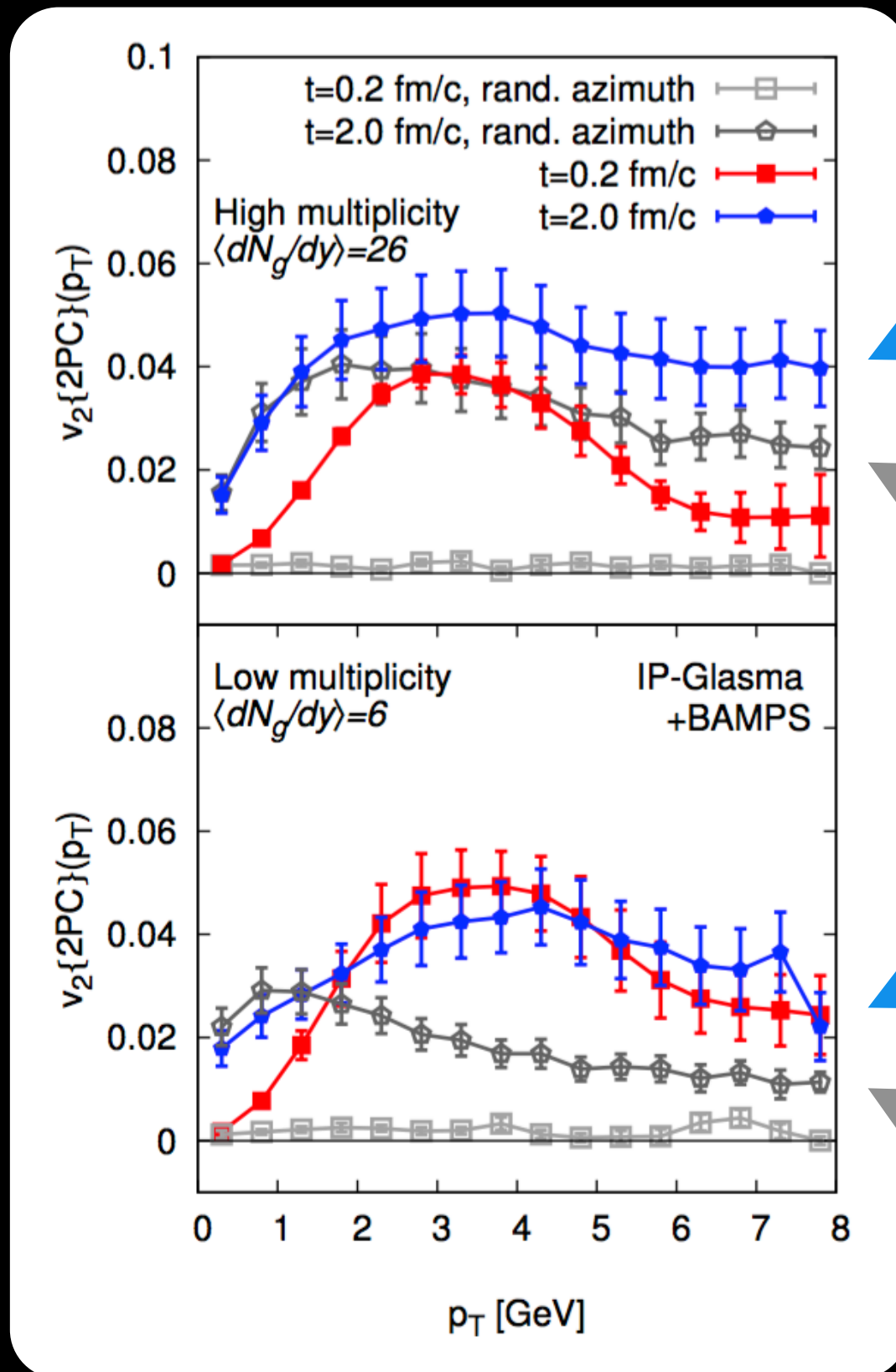
smear  $\rightarrow$  Husimi Distribution

$\rightarrow$  study momentum anisotropy as function of time

# Effect of initial correlations on final $v_2$

M. Greif, C. Greiner, B. Schenke, S. Schlichting, Z. Xu, arXiv:1708.02076, Phys. Rev. D96, 091509(R)

high  
multiplicity  
low  
multiplicity



with initial corr.

without initial corr.

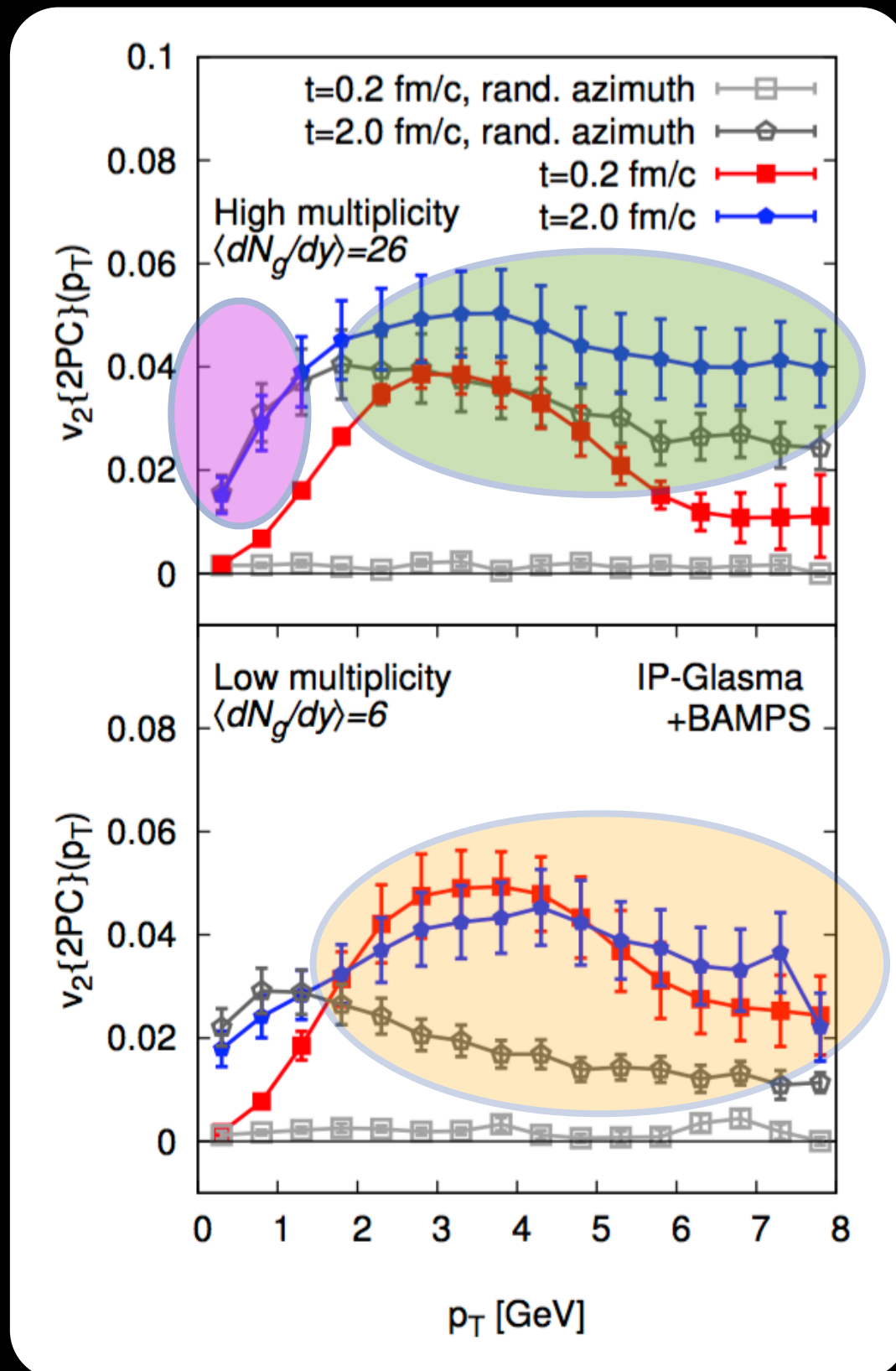
with initial corr.

without initial corr.

# Effect of initial correlations on final $v_2$

M. Greif, C. Greiner, B. Schenke, S. Schlichting, Z. Xu, arXiv:1708.02076, Phys. Rev. D96, 091509(R)

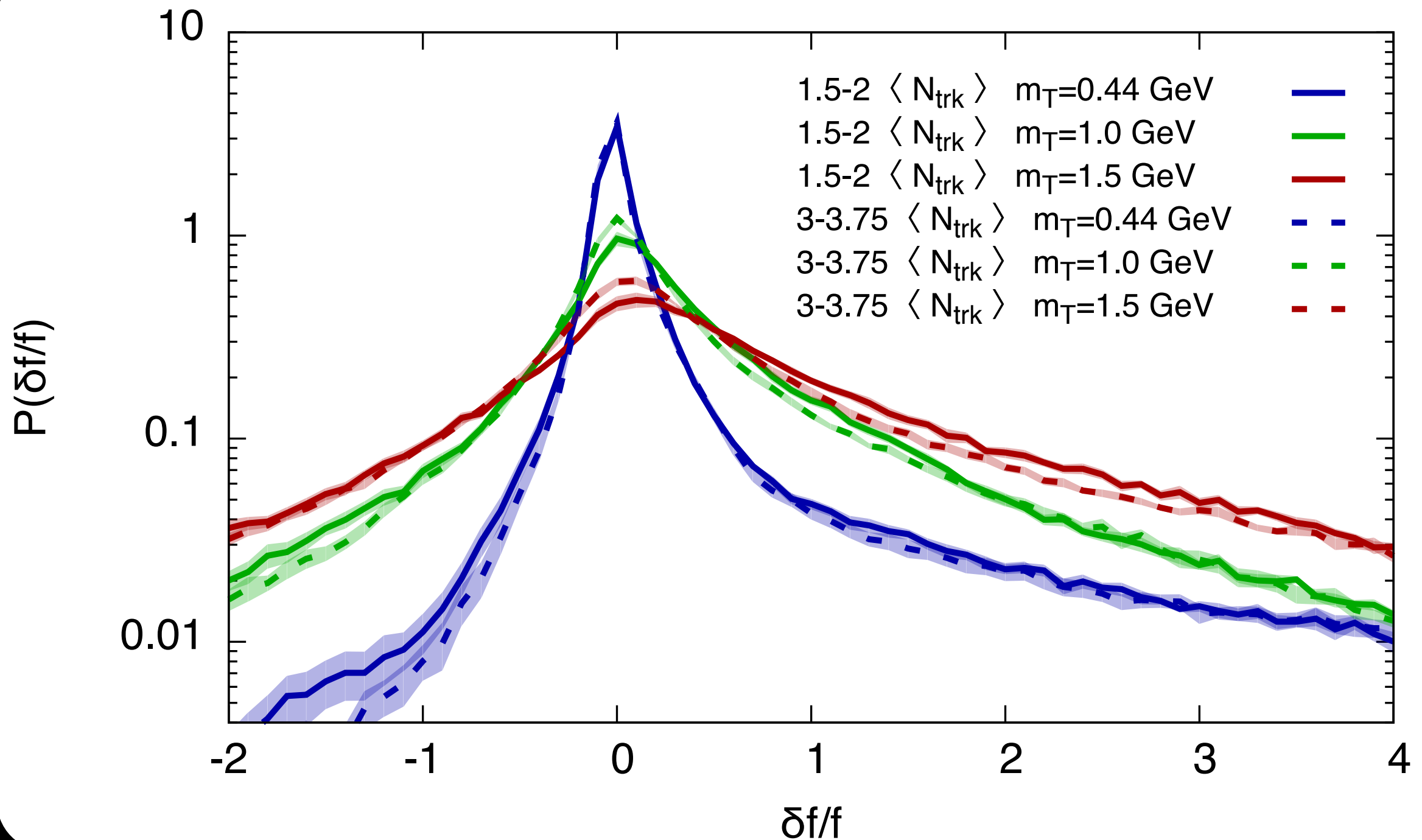
high  
multiplicity  
low  
multiplicity



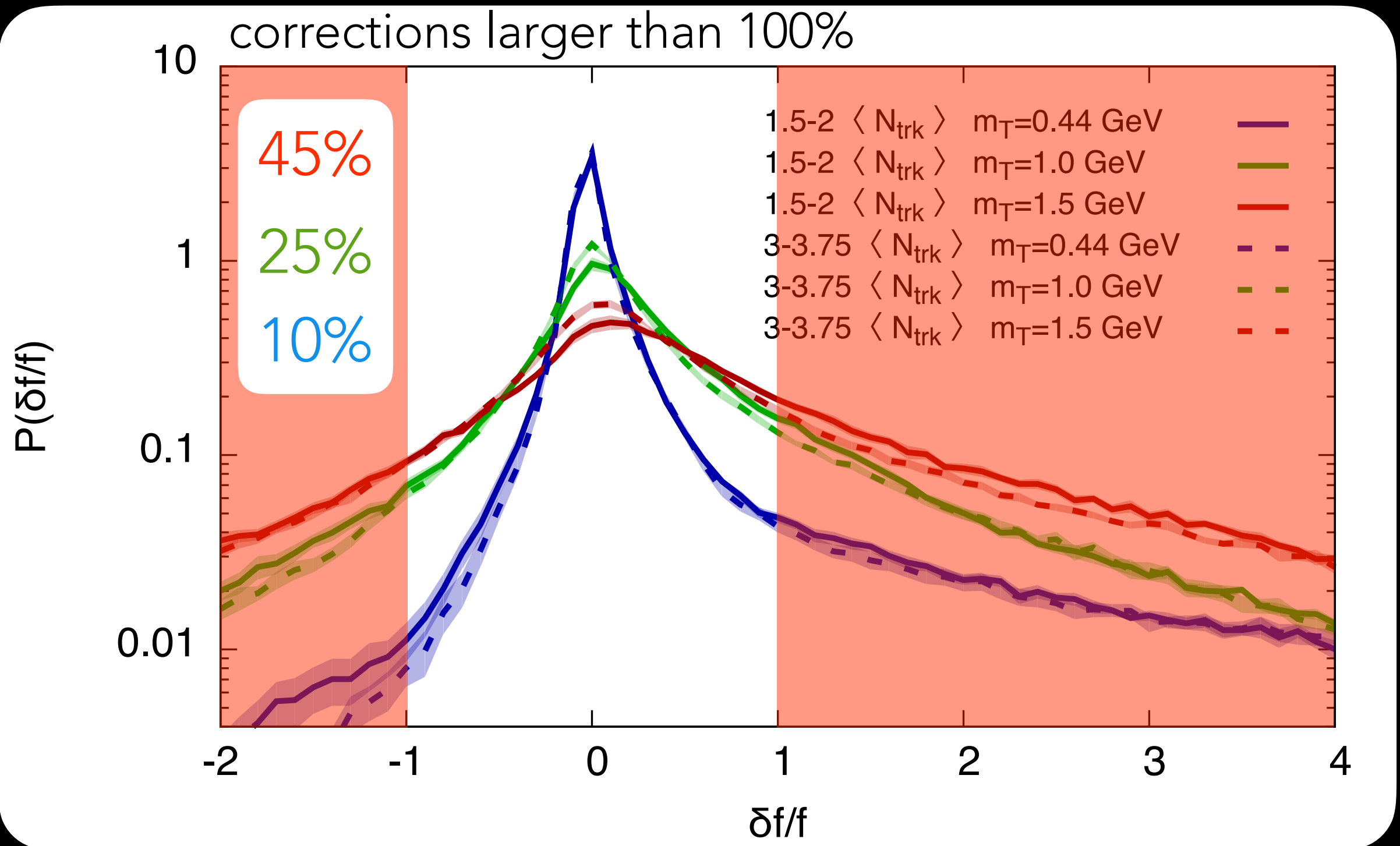
- negligible effect at small  $p_T$  and high multiplicity
- significant effect at  $p_T > 2$  GeV and low multiplicity
- visible effect at  $p_T > 3$  GeV and high multiplicity



# Histogram of $\delta f/f$ on the switching surface



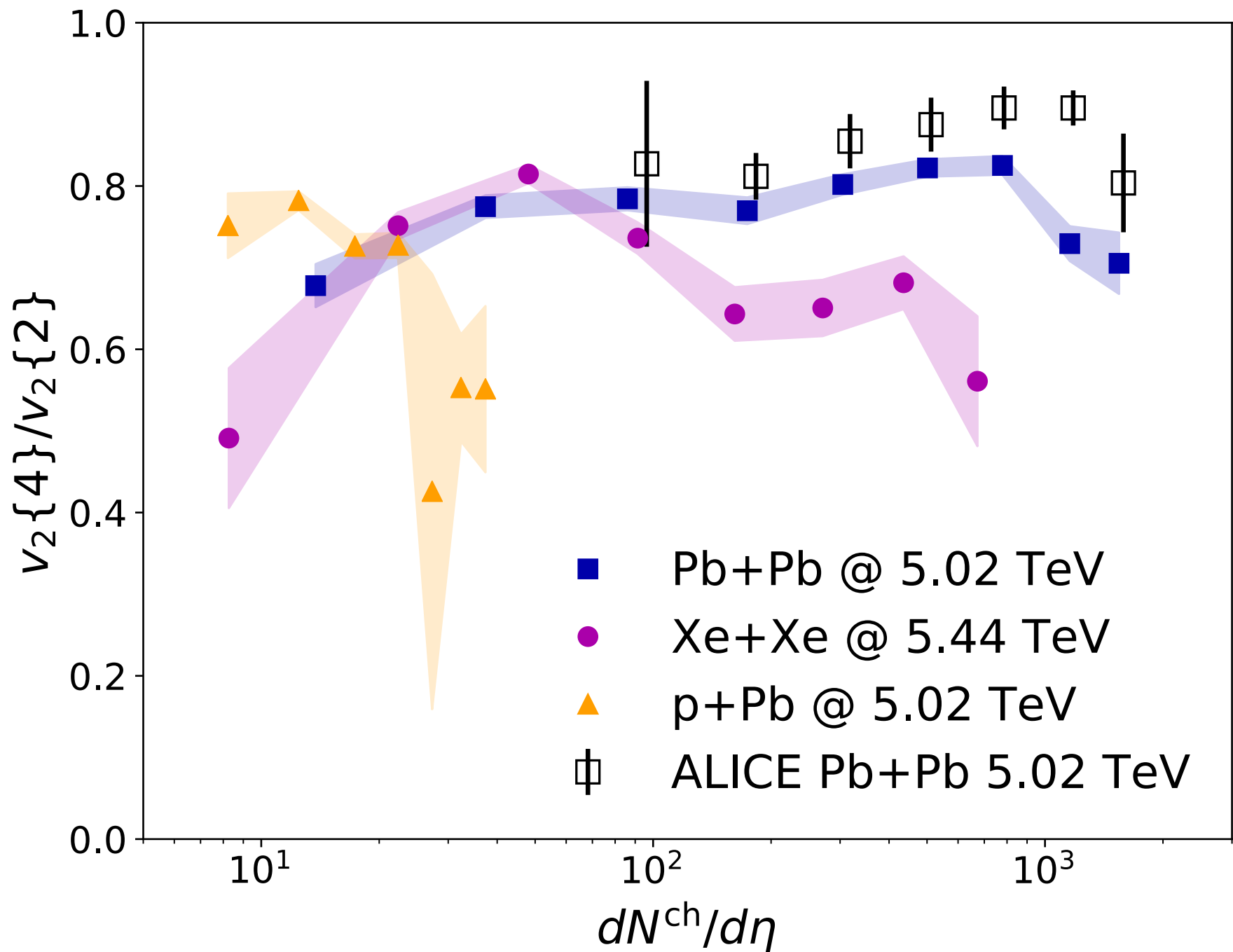
# Histogram of $\delta f/f$ on the switching surface





# Cumulant ratios

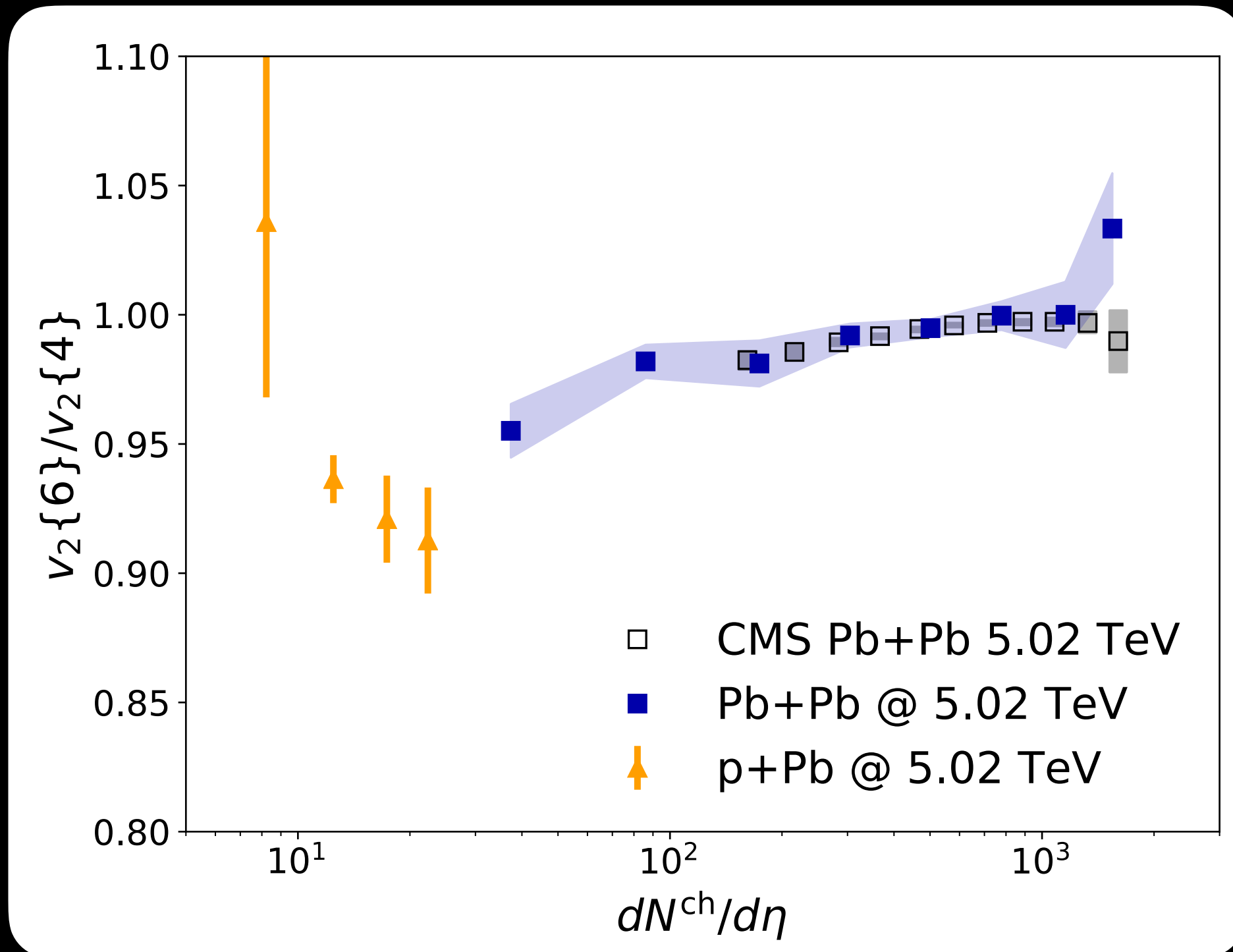
B. Schenke, C. Shen, P. Tribedy, in preparation



Experimental data: J. Adam et al. (ALICE), Phys. Rev. Lett. 116, 132302 (2016)

# Cumulant ratios

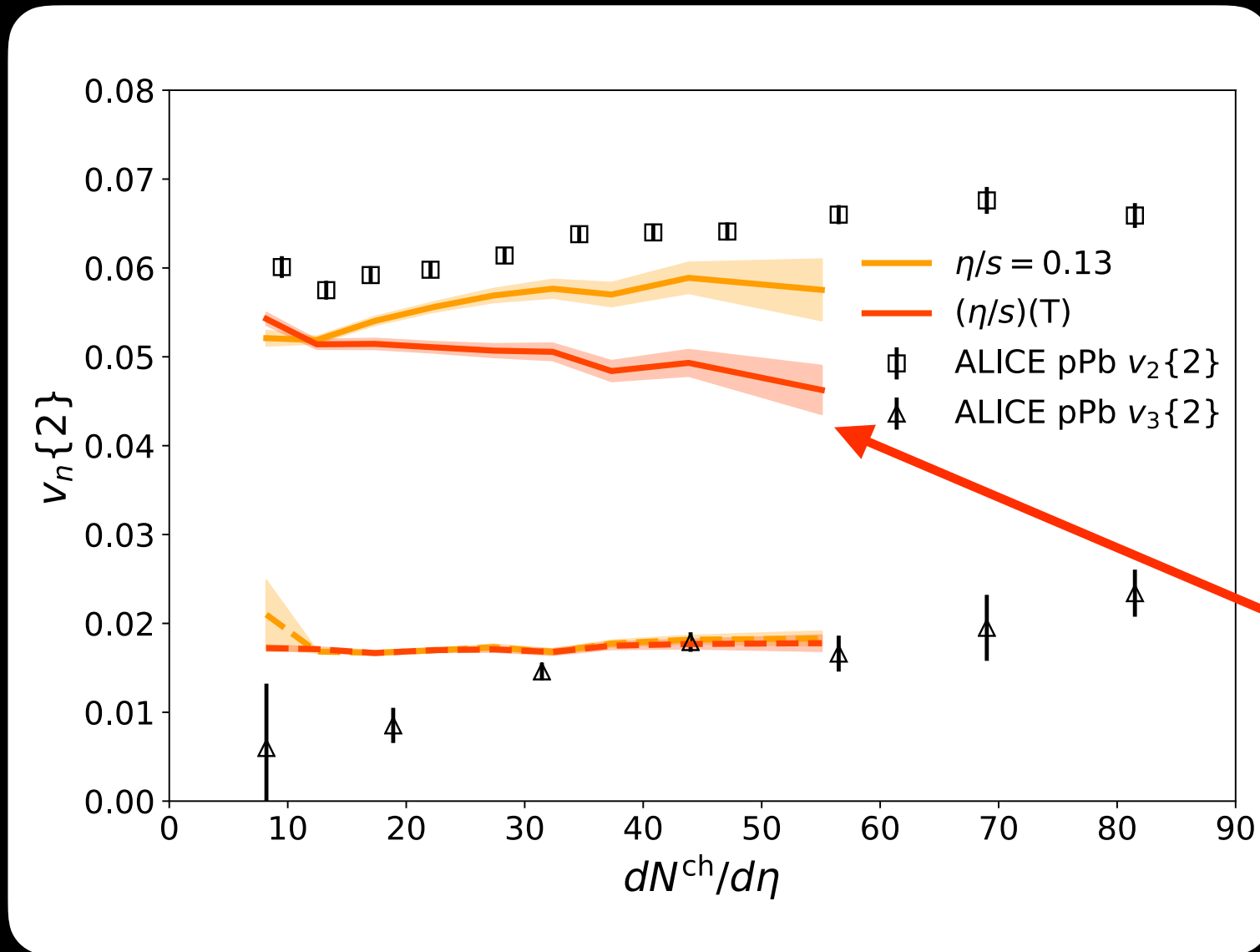
B. Schenke, C. Shen, P. Tribedy, in preparation



Experimental data: A. M. Sirunyan et al. (CMS), (2017), arXiv:1711.05594

# Not much room for T-dependent $\eta/s$

B. Schenke, C. Shen, P. Tribedy, in preparation

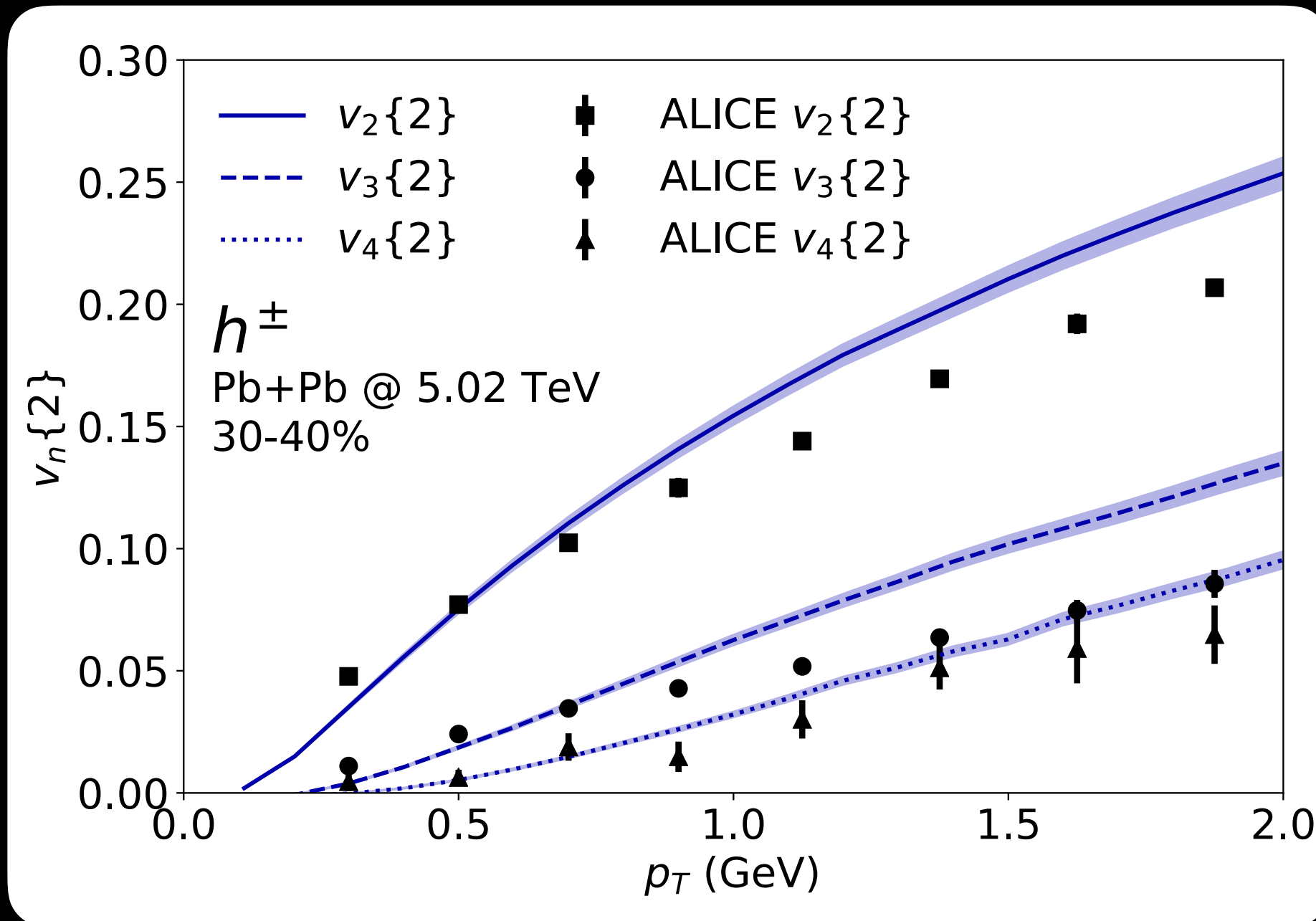


Rising  $\eta/s$  with increasing  $T$  leads to dropping  $v_2$  for p+Pb

Experimental data: B. B. Abelev et al. (ALICE), Phys. Rev. C90, 054901 (2014)

# Differential $v_n$

B. Schenke, C. Shen, P. Tribedy, in preparation

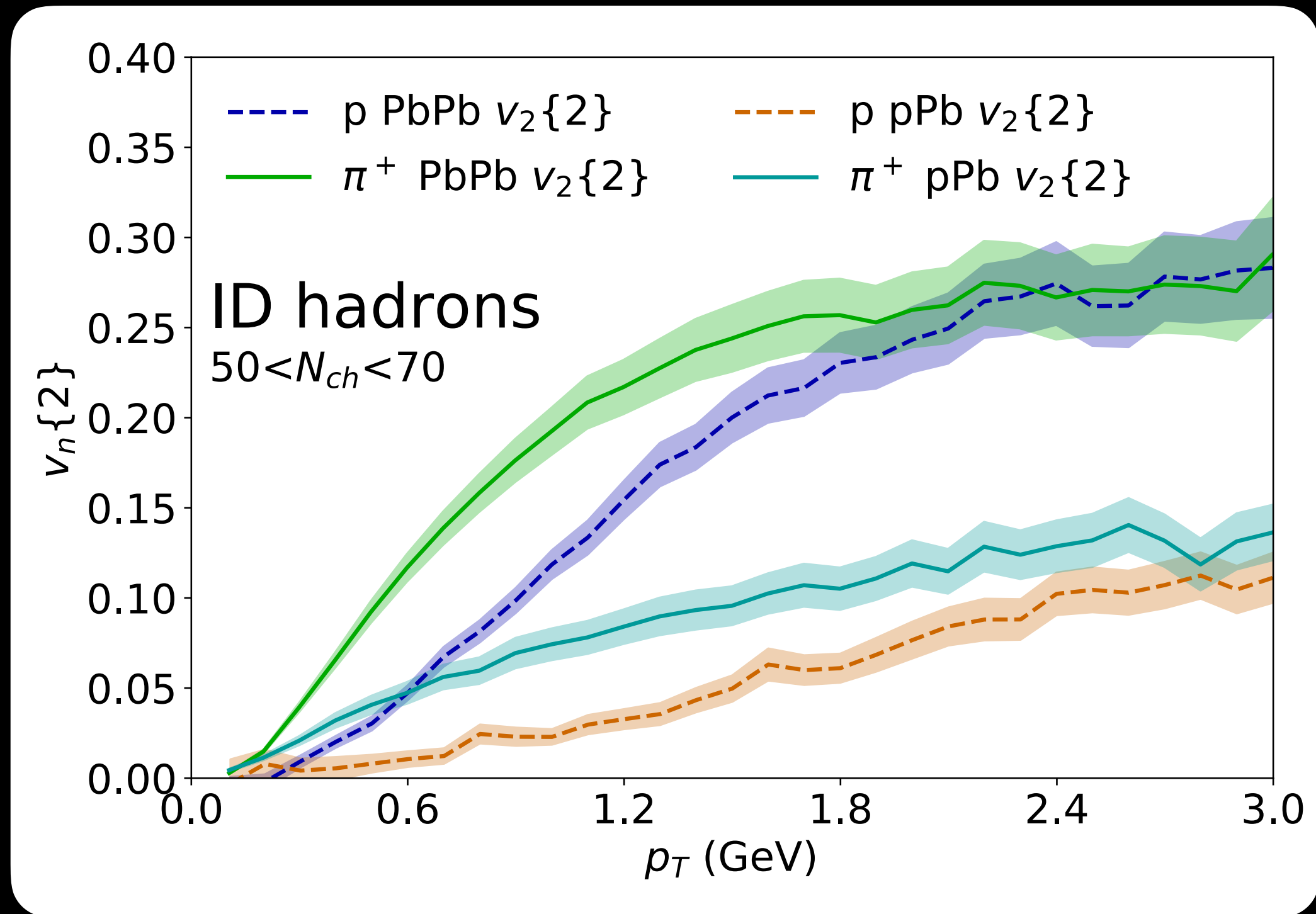


New EoS and inclusion of bulk viscosity makes agreement worse

Experimental data: ALICE Collaboration, Phys.Rev.Lett. 116, 132302 (2016)

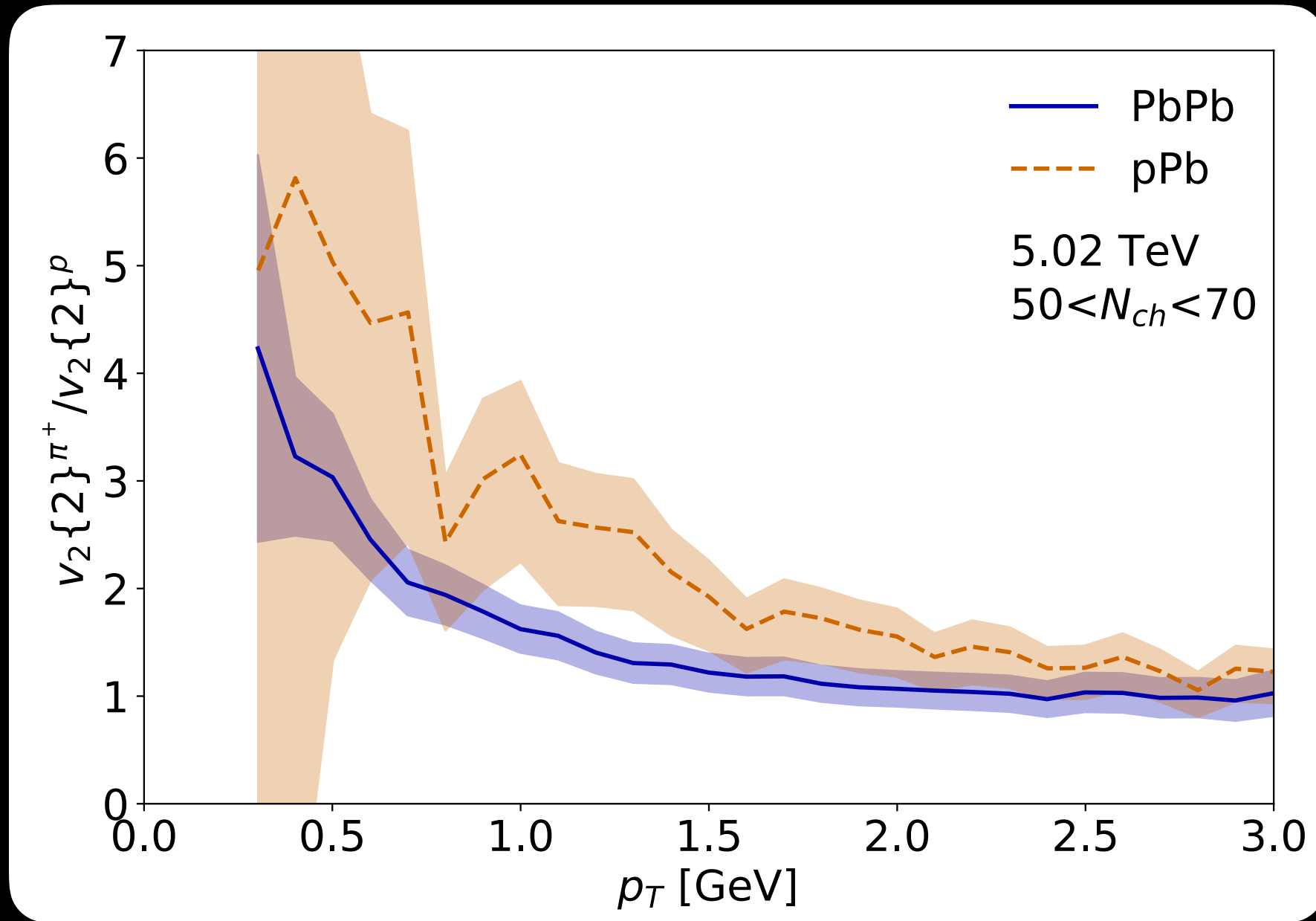
# Mass splitting

B. Schenke, C. Shen, P. Tribedy, in preparation



# More mass splitting in p+Pb

B. Schenke, C. Shen, P. Tribedy, in preparation



as expected from larger mean transverse momentum

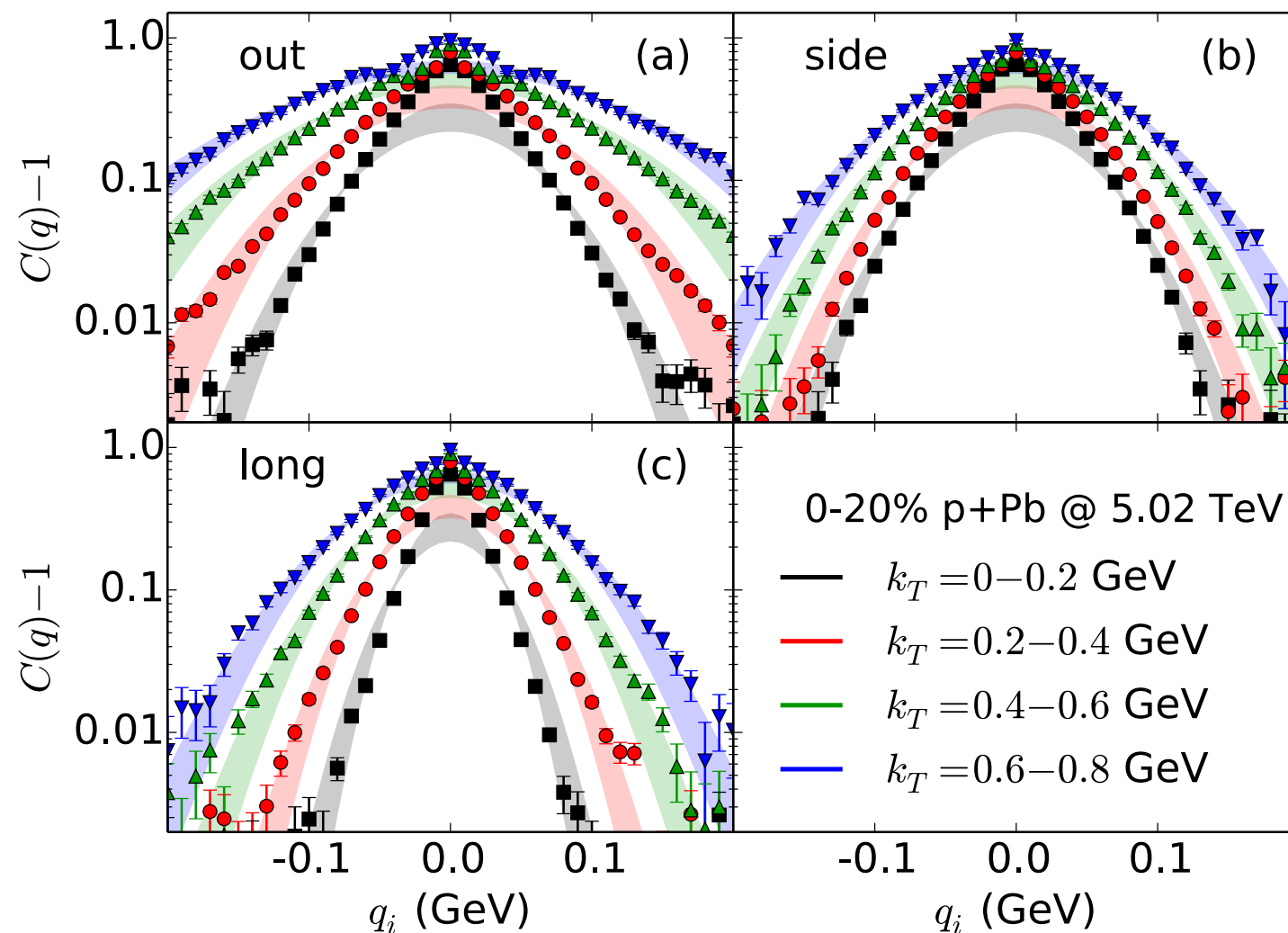
# HBT radii

H. Mäntysaari, B. Schenke, C. Shen, P. Tribedy, arXiv:1705.03177

$$C(\mathbf{q}) = 1 + \frac{\frac{1}{\langle N_{\text{pair}} \rangle} \langle \sum_{ij} \cos(\mathbf{q}_{ij} \cdot \mathbf{x}_{ij}) \rangle}{\frac{1}{\langle N_{\text{mix pair}} \rangle} \langle N_{\text{mix pair}}(\mathbf{q}) \rangle}$$

M. A. Lisa, S. Pratt, R. Soltz, and U. Wiedemann,  
Ann. Rev. Nucl. Part. Sci. 55, 357 (2005)

R. Hanbury Brown and R. Q. Twiss  
Nature 178, 1046 (1956)



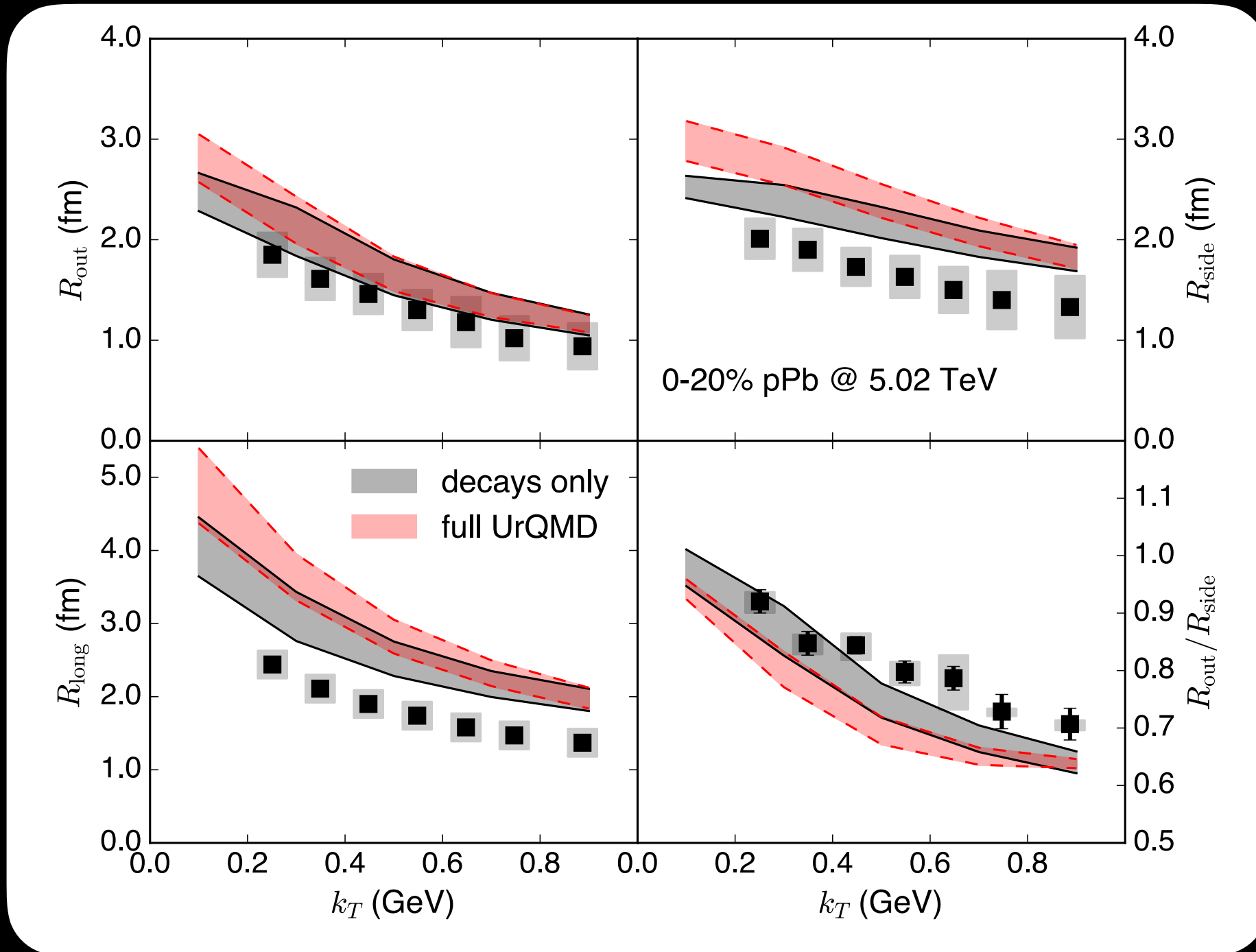
Fit to the Pratt-Bertsch parameterization in the longitudinally co-moving system

S. Pratt, Phys. Rev. D33, 1314 (1986)  
G. Bertsch, M. Gong, and M. Tohyama  
Phys. Rev. C37, 1896 (1988).

# HBT radii

H. Mäntysaari, B. Schenke, C. Shen, P. Tribedy, arXiv:1705.03177

Data: ALICE Collaboration, J. Adam et al. (ALICE), Phys. Rev. C91, 034906 (2015)

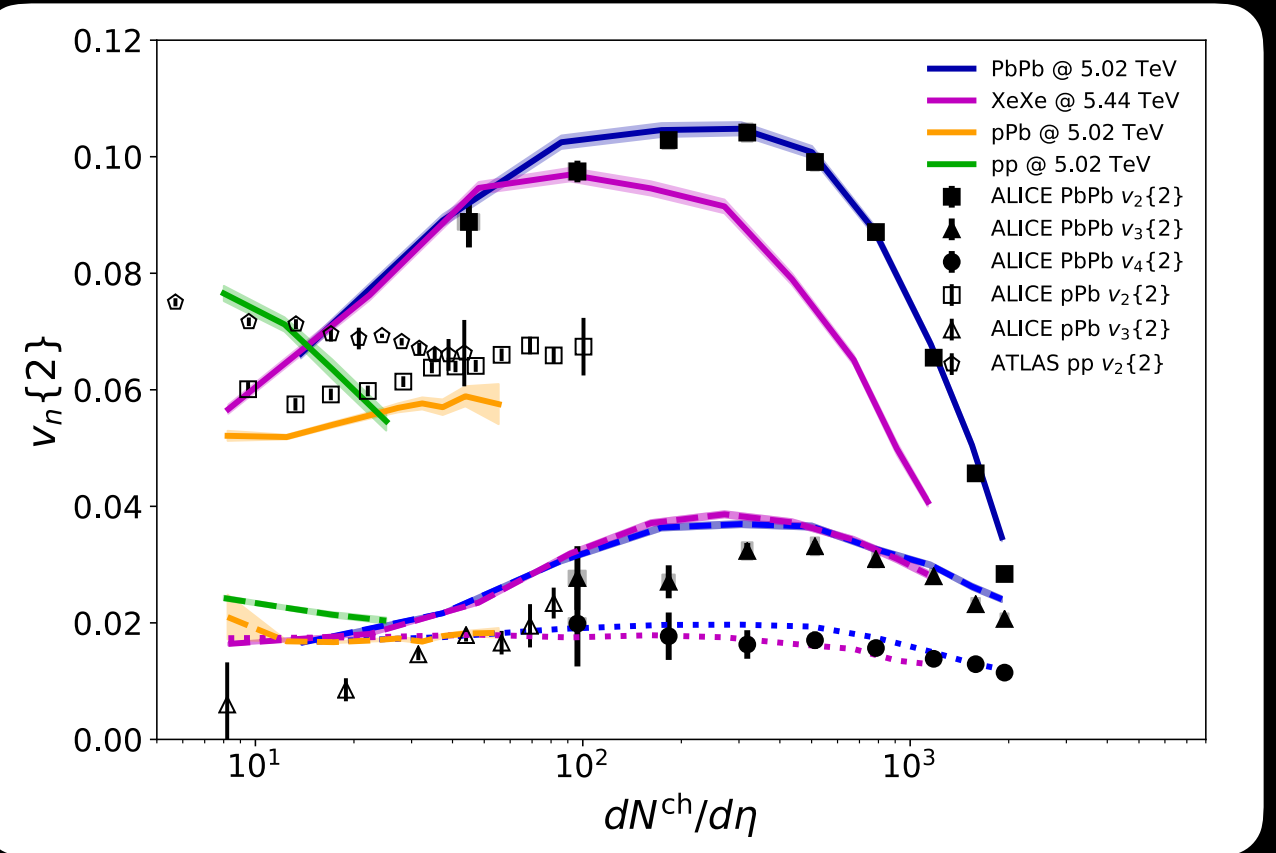
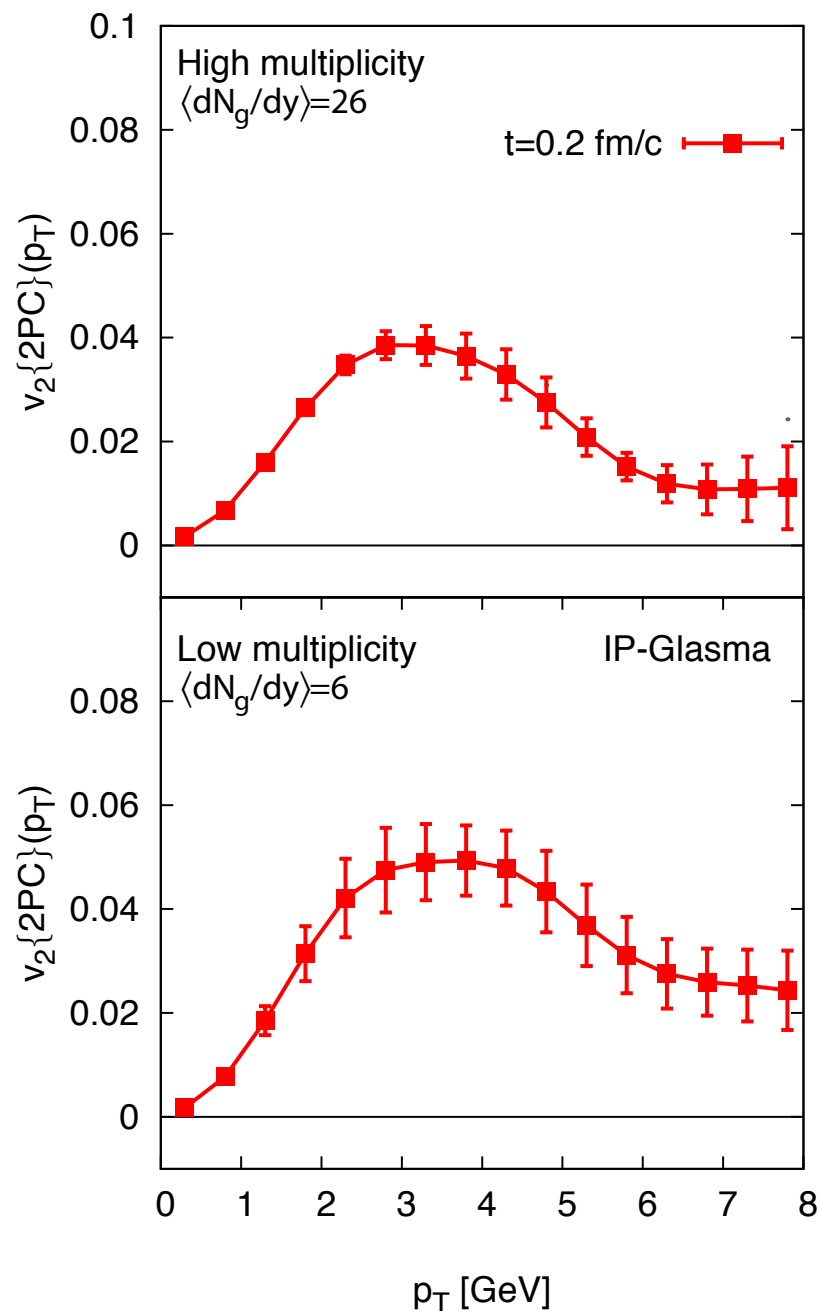


$\tau_0 = 0.4 \text{ fm} \quad (\eta/s)(T)$



# p+p $v_n$ drop with multiplicity

...so do the initial state anisotropies (shown for pPb):

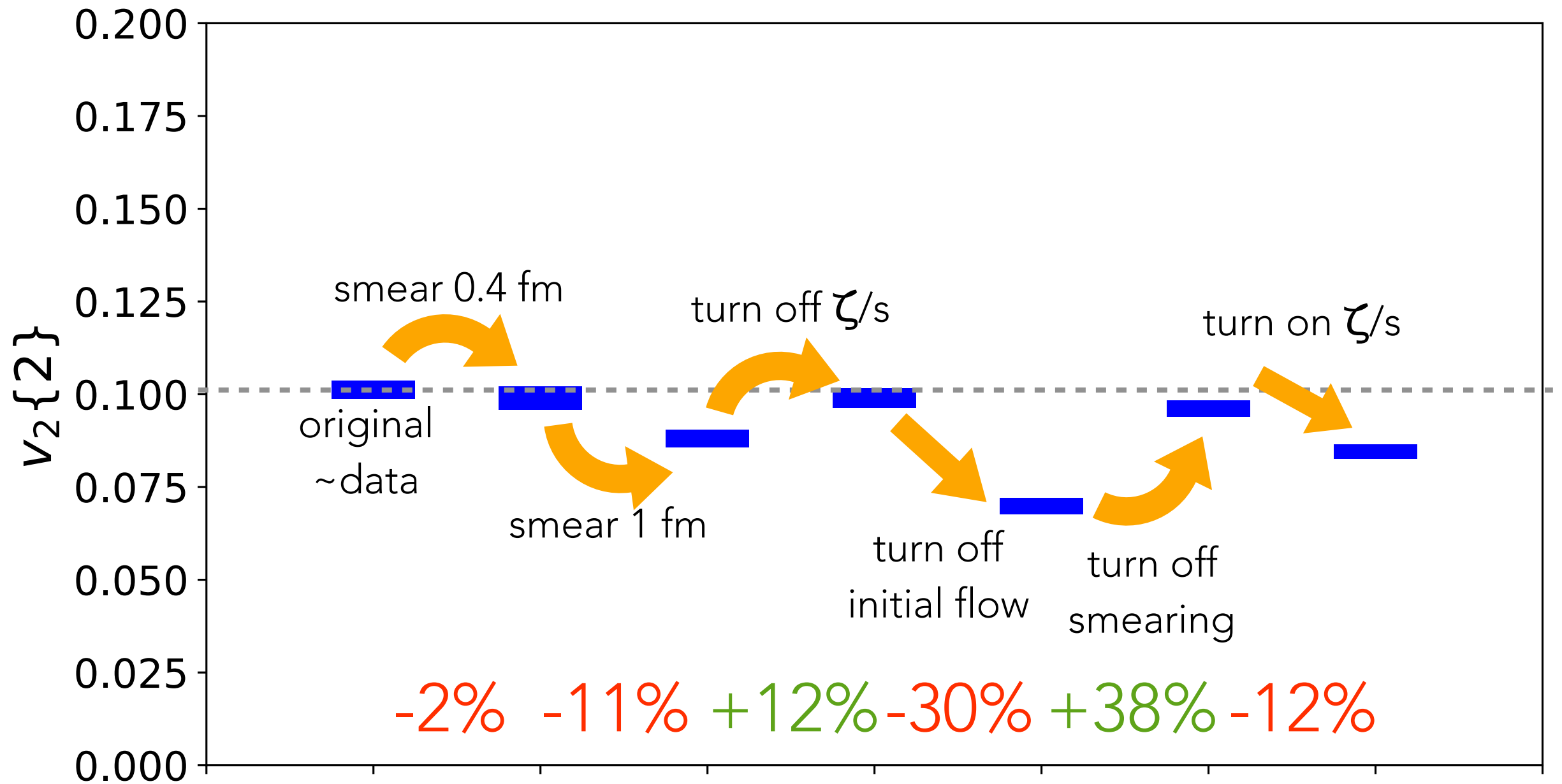


When switching at  $\tau = 0.6 \text{ fm}$ , a large part of the anisotropy is from the initial state

**Warning:** Removing dijet contribution by subtracting peripheral events may remove some real long range physics ...

# Effects of initial flow and smearing on $v_2$

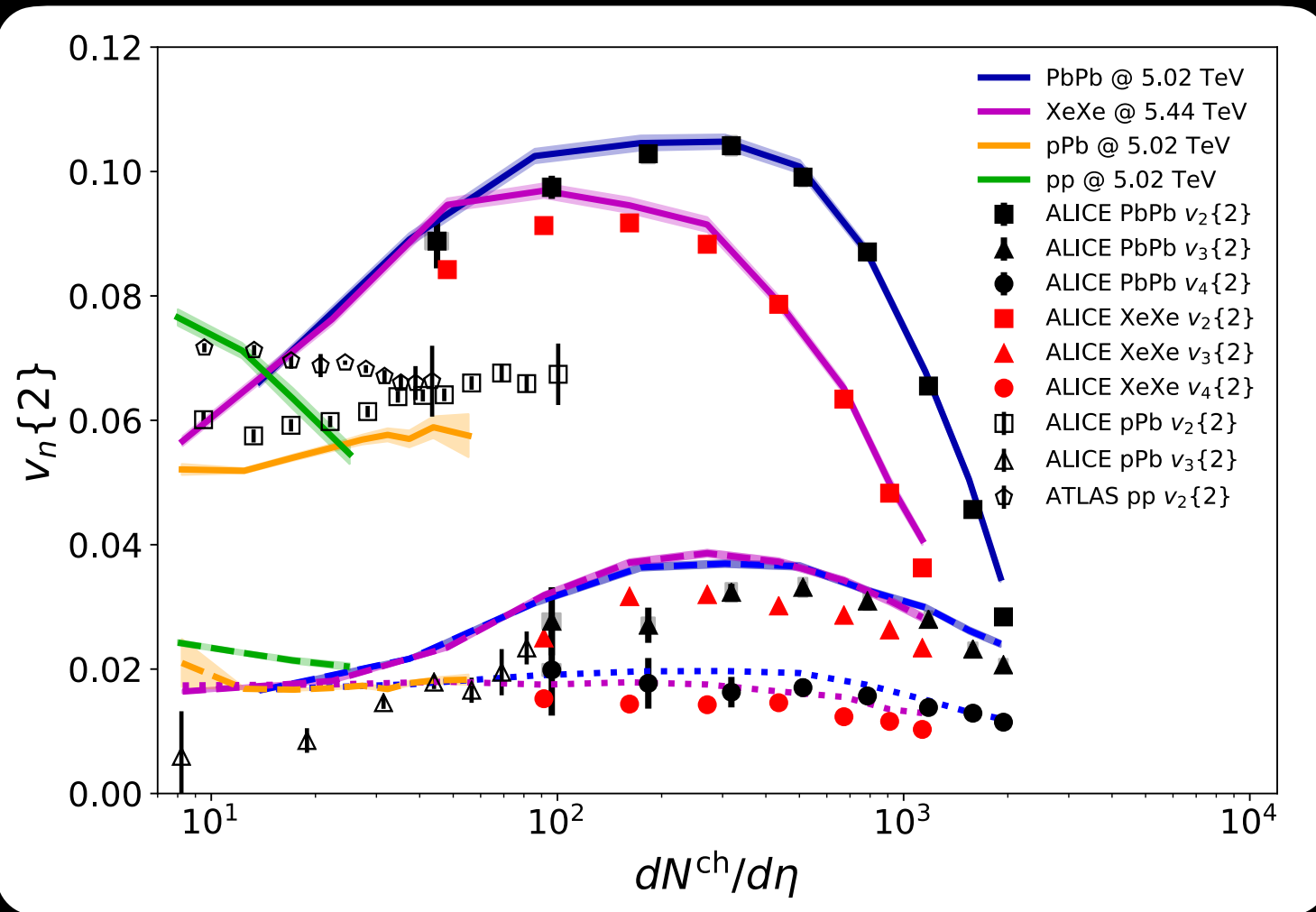
B. Schenke, C. Shen, P. Tribedy, in preparation



Also differences in bulk  $\delta f$  between calculations

# Anisotropy vs. multiplicity

B. Schenke, C. Shen, P. Tribedy, in preparation



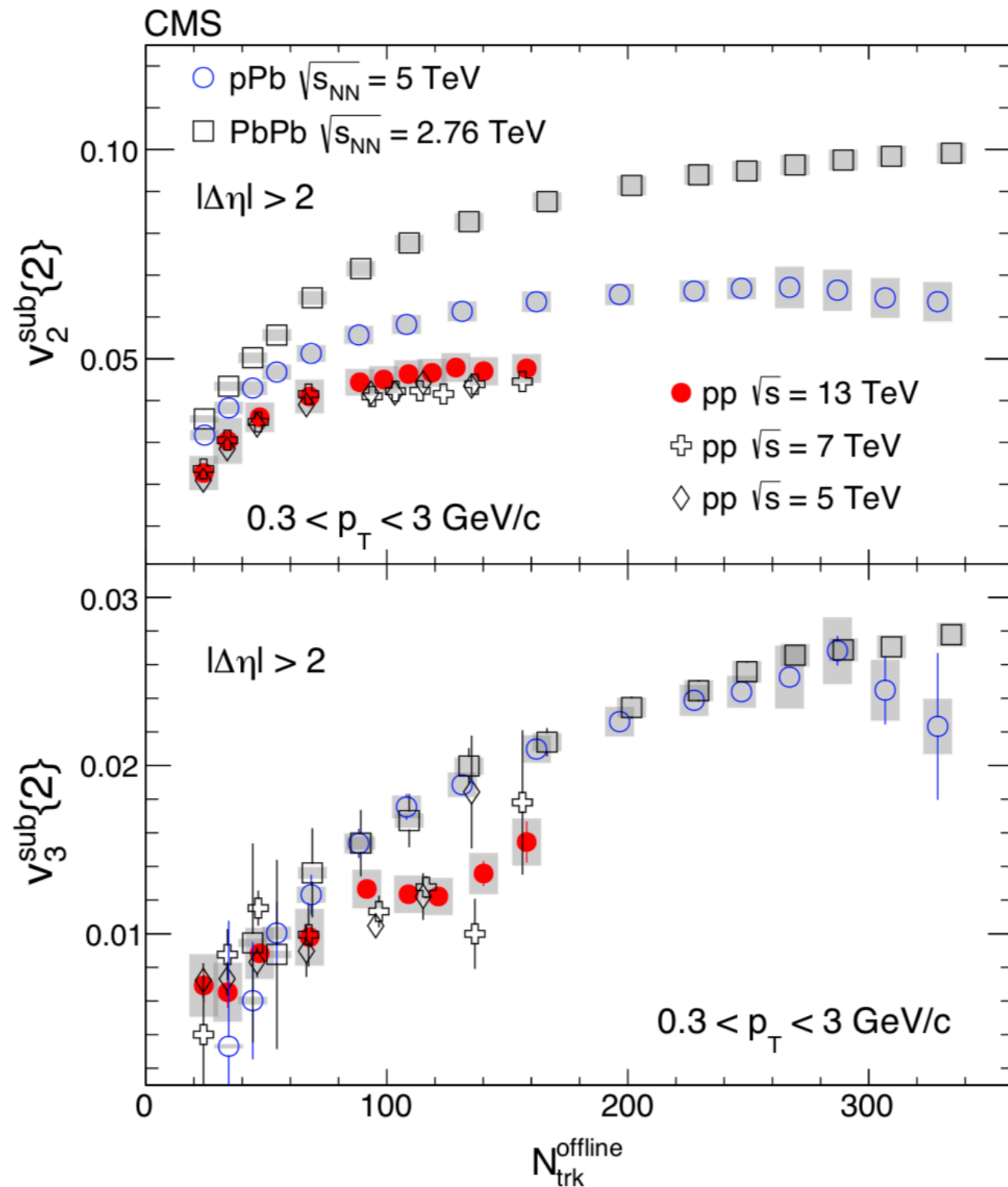
$|\eta| < 0.8$  for ALICE

Results are boost invariant - comparison to ATLAS (CMS) difficult because there  $|\eta| < 2.5$  (2.4)

Experimental data: J. Adam et al. (ALICE), Phys. Rev. Lett. 116, 132302 (2016)

B. B. Abelev et al. (ALICE), Phys. Rev. C90, 054901 (2014), CMS Collaboration, Phys.Lett. B765 (2017) 193-220

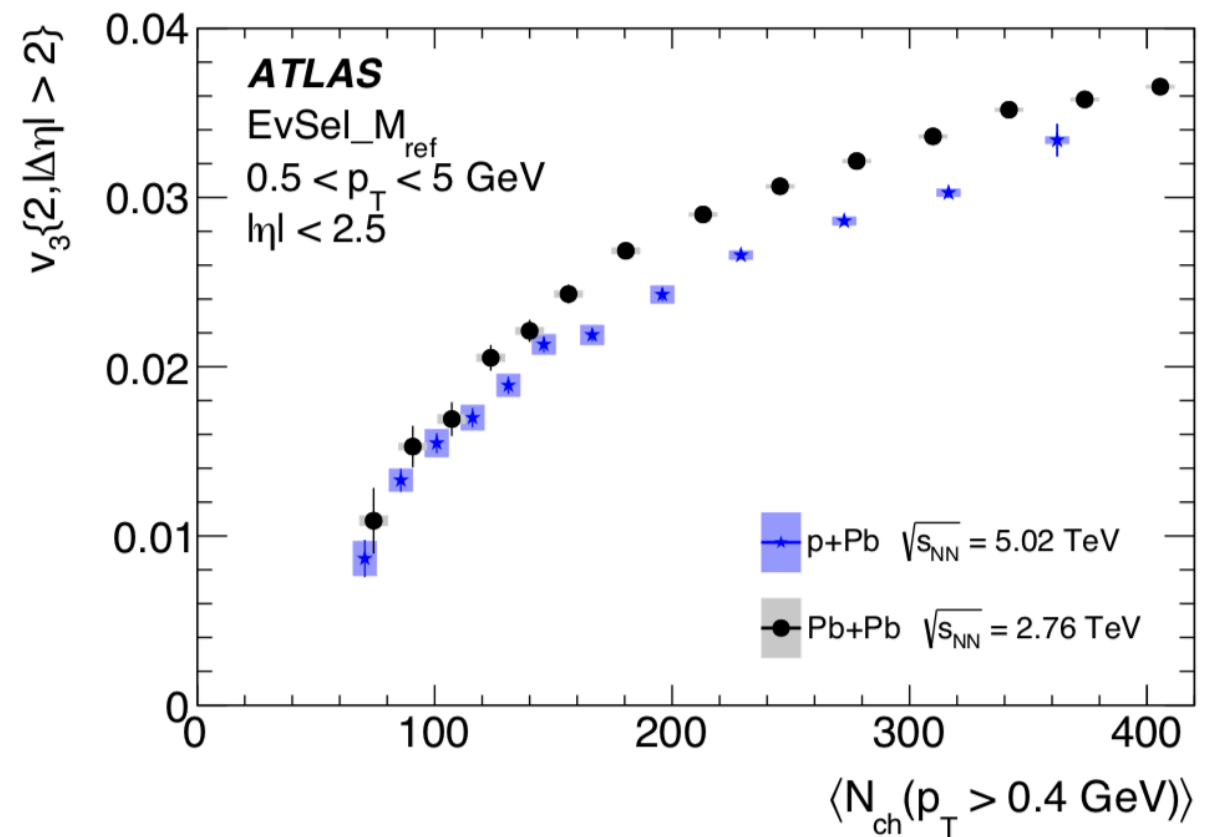
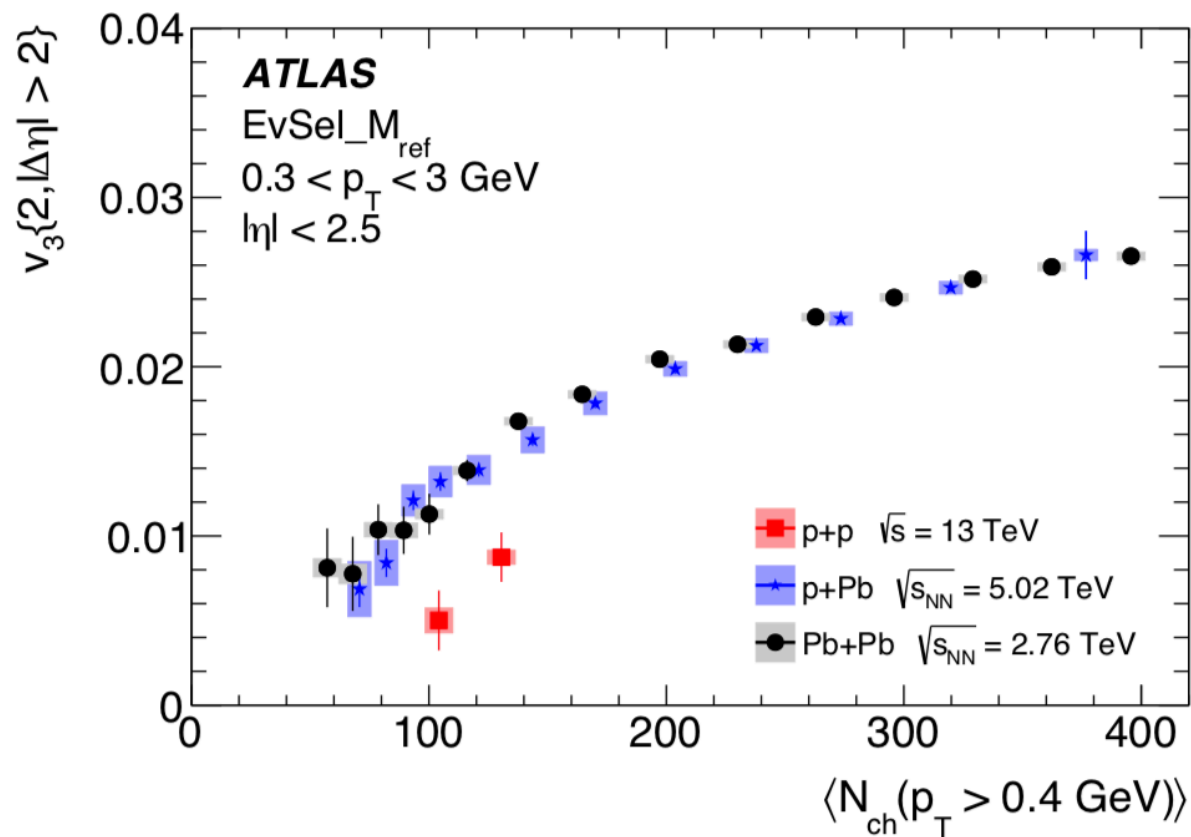
# Why is $v_3$ same in p+Pb and Pb+Pb?



We expect vastly different eccentricity distributions for the two systems

Why is  $v_3^{\text{pPb}} \approx v_3^{\text{PbPb}}$ ?

# Equality depends on $p_T$ cut



ATLAS Collaboration, Eur.Phys.J. C77 (2017) no.6, 428

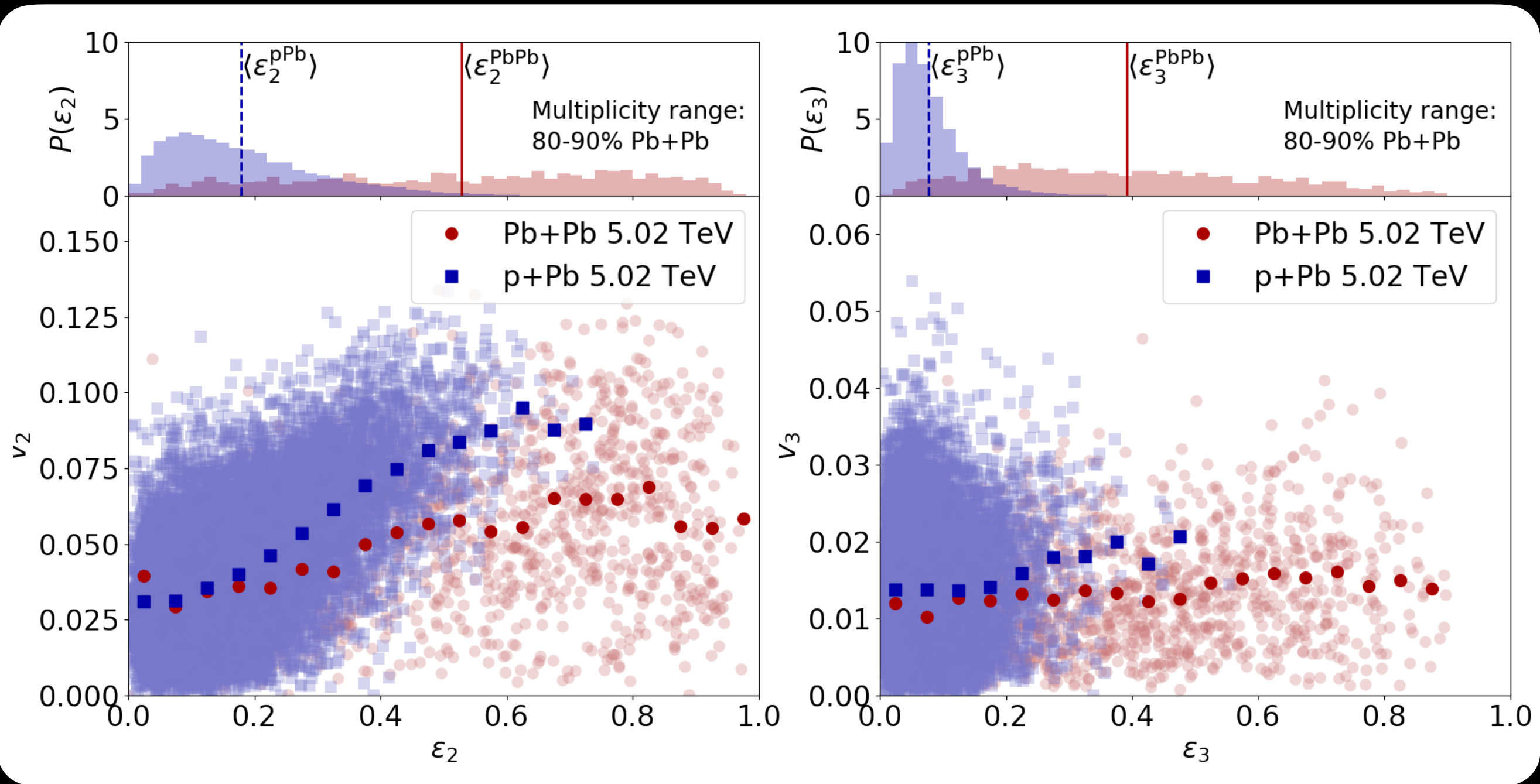
Energies different, but  $v_3^{\text{PbPb}}$  only  $\sim 5\%$  larger at 5.02 TeV

ALICE, Phys. Rev. Lett. 116 (2016) 132302

Some level of coincidence, but there is some physics...

# Geometry - flow correlations

First: Eccentricity distributions are indeed different

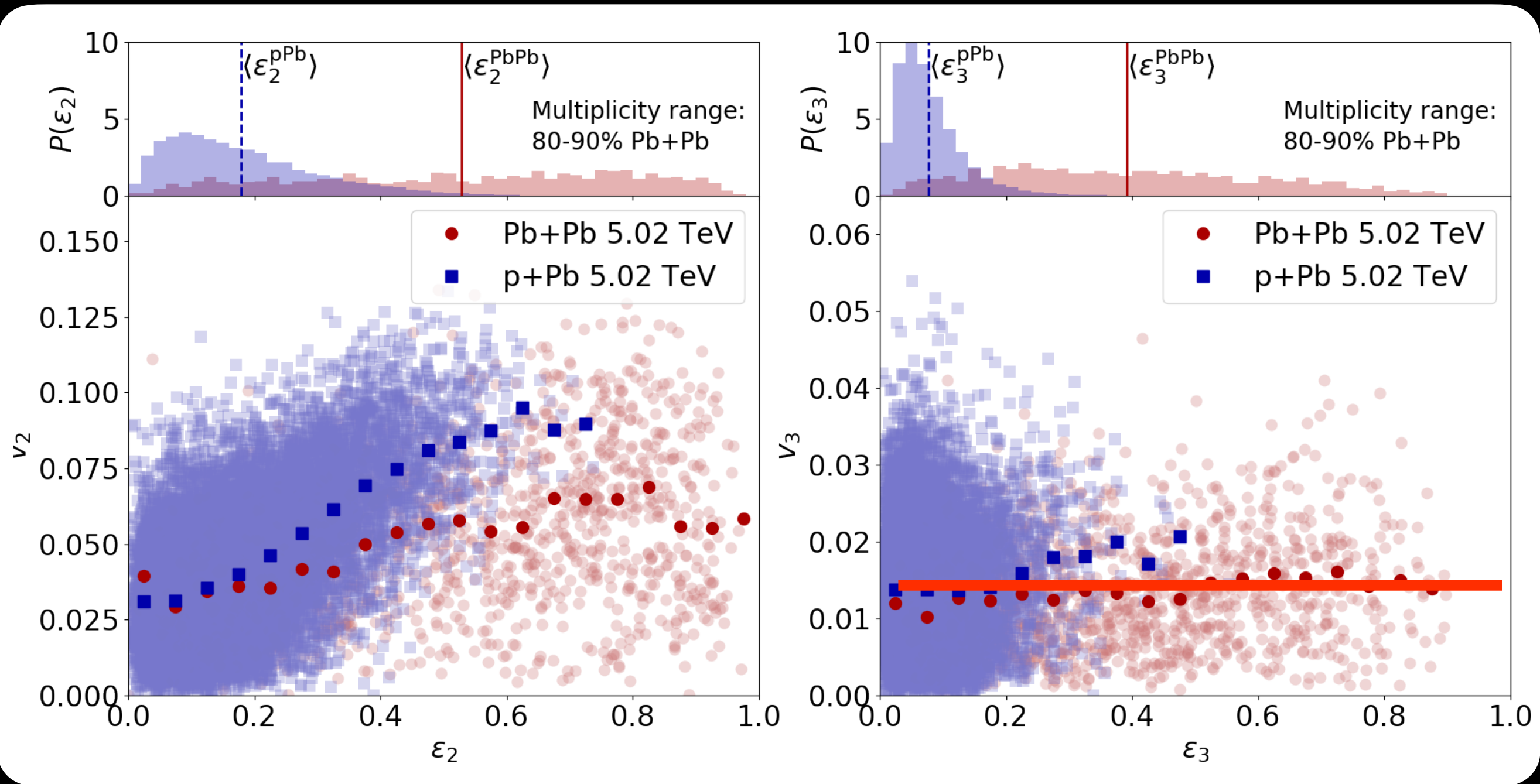


B. Schenke, C. Shen, P. Tribedy, in preparation



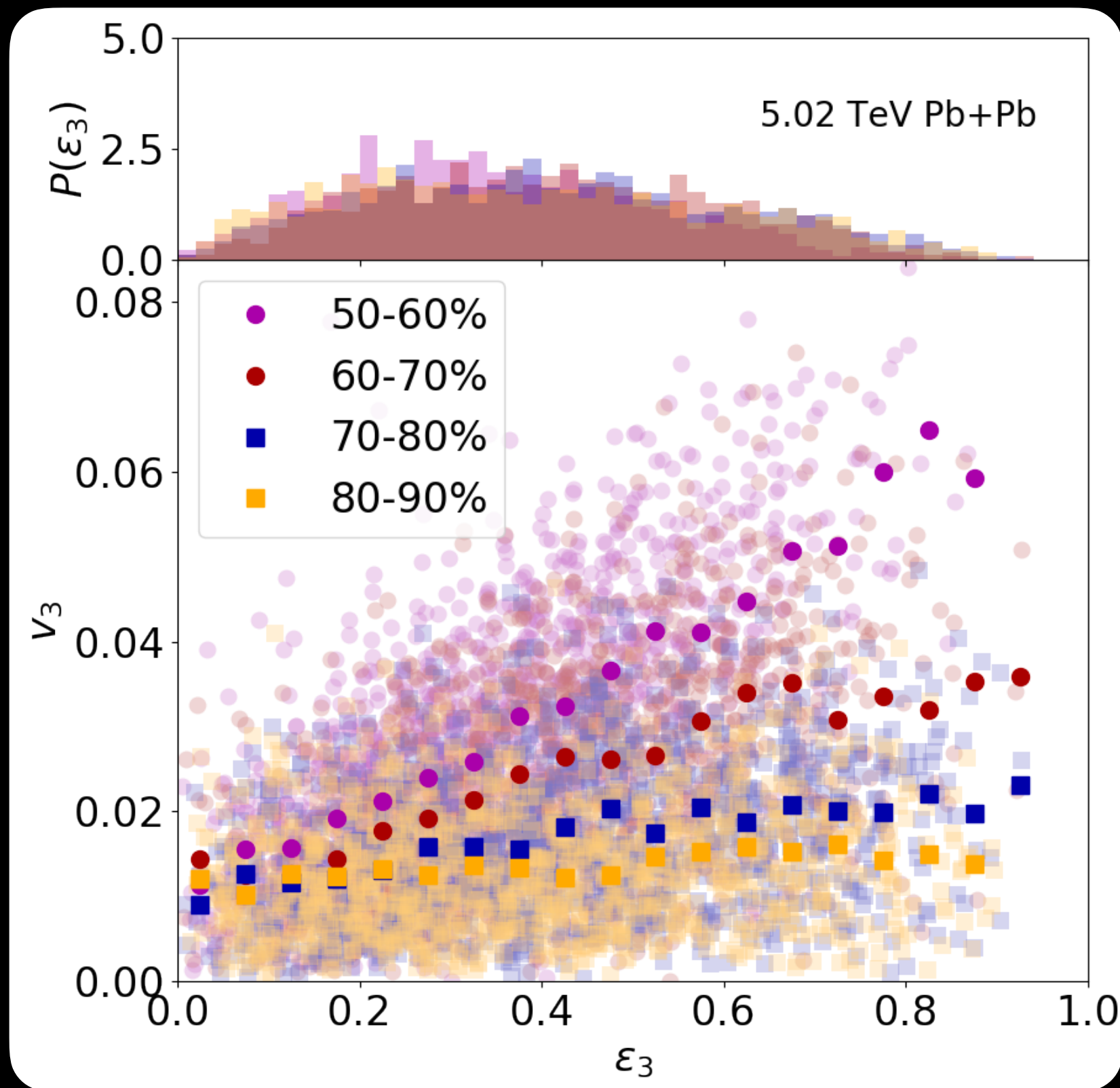
# Geometry - flow correlations

First: Eccentricity distributions are indeed different



But: In very peripheral Pb+Pb no correlation with  $v_3$

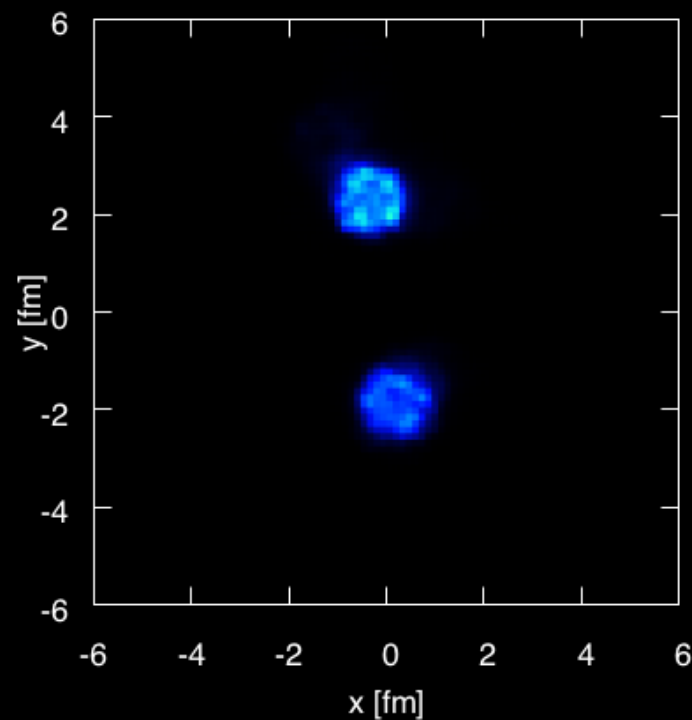
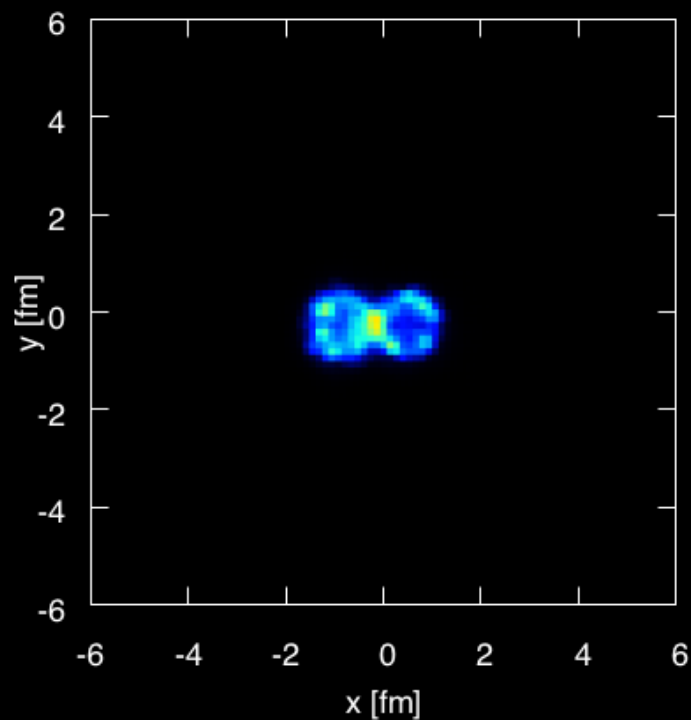
# Correlation gradually vanishes



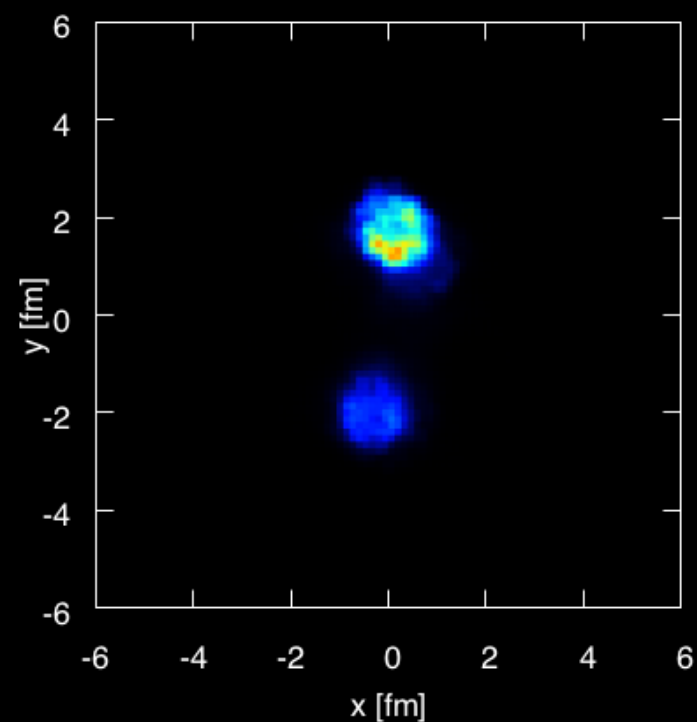
the more  
peripheral we go



# Correlation vanishes in peripheral PbPb



Initial energy densities



Many peripheral PbPb events consist of separated blobs that barely interact with one another  $v_n$  driven by geometry of single blob  
**Like separate p+Pb collisions**

# Situation in IP-Glasma

This leads to smaller  $v_n$  compared to pPb at the same multiplicity, because

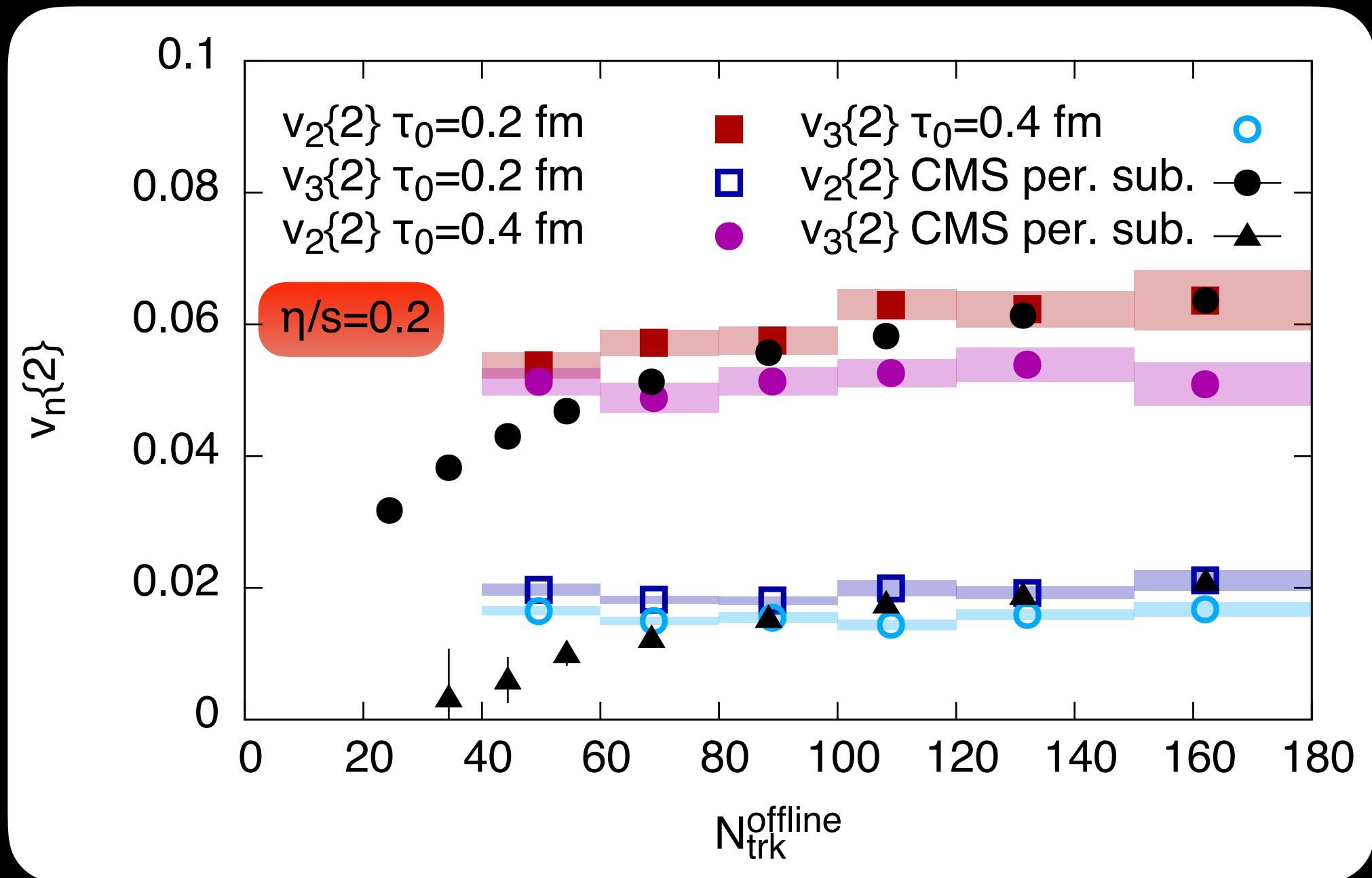
- 1) geometry of separate blobs not aligned
- 2) energy density in blobs lower than in 1 pPb blob

Finite interaction between blobs must compensate for that

But in fact in the calculation  $v_3$  are only same at very low multiplicity (data shows same value to higher multiplicity)

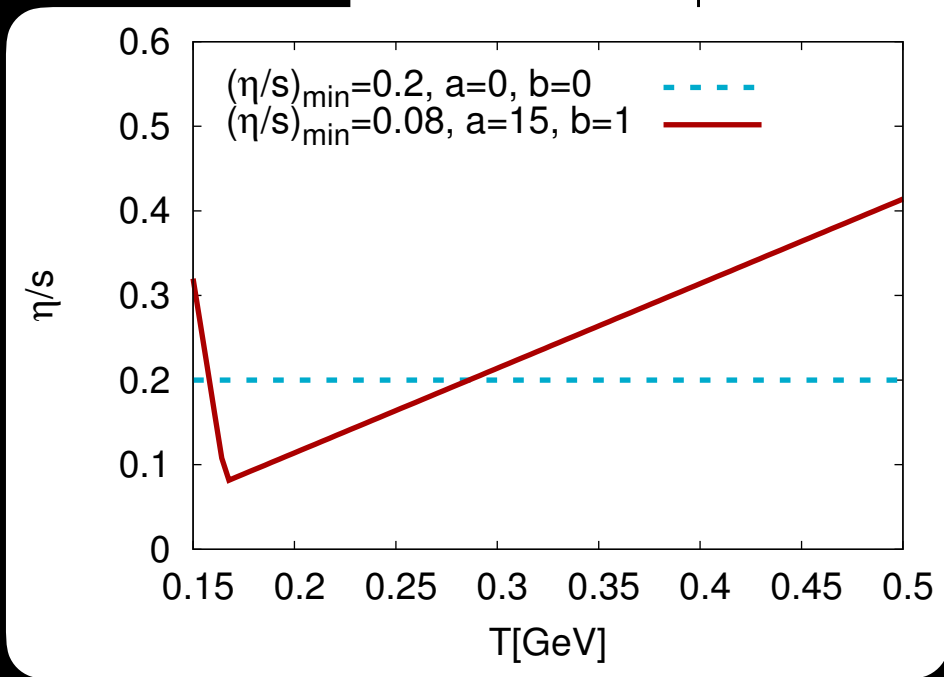
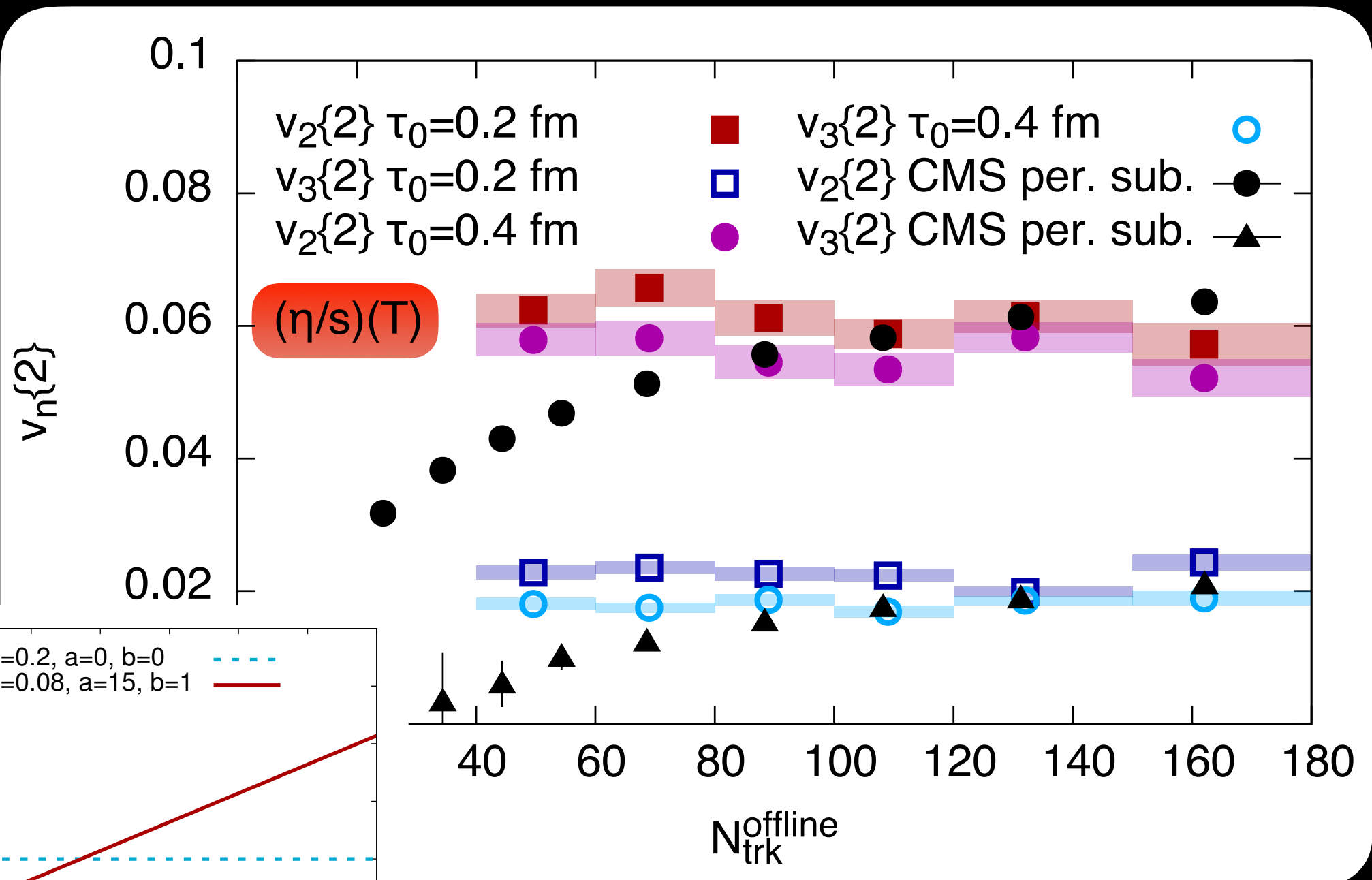
# Integrated anisotropic flow

H. Mäntysaari, B. Schenke, C. Shen, P. Tribedy, arXiv:1705.03177

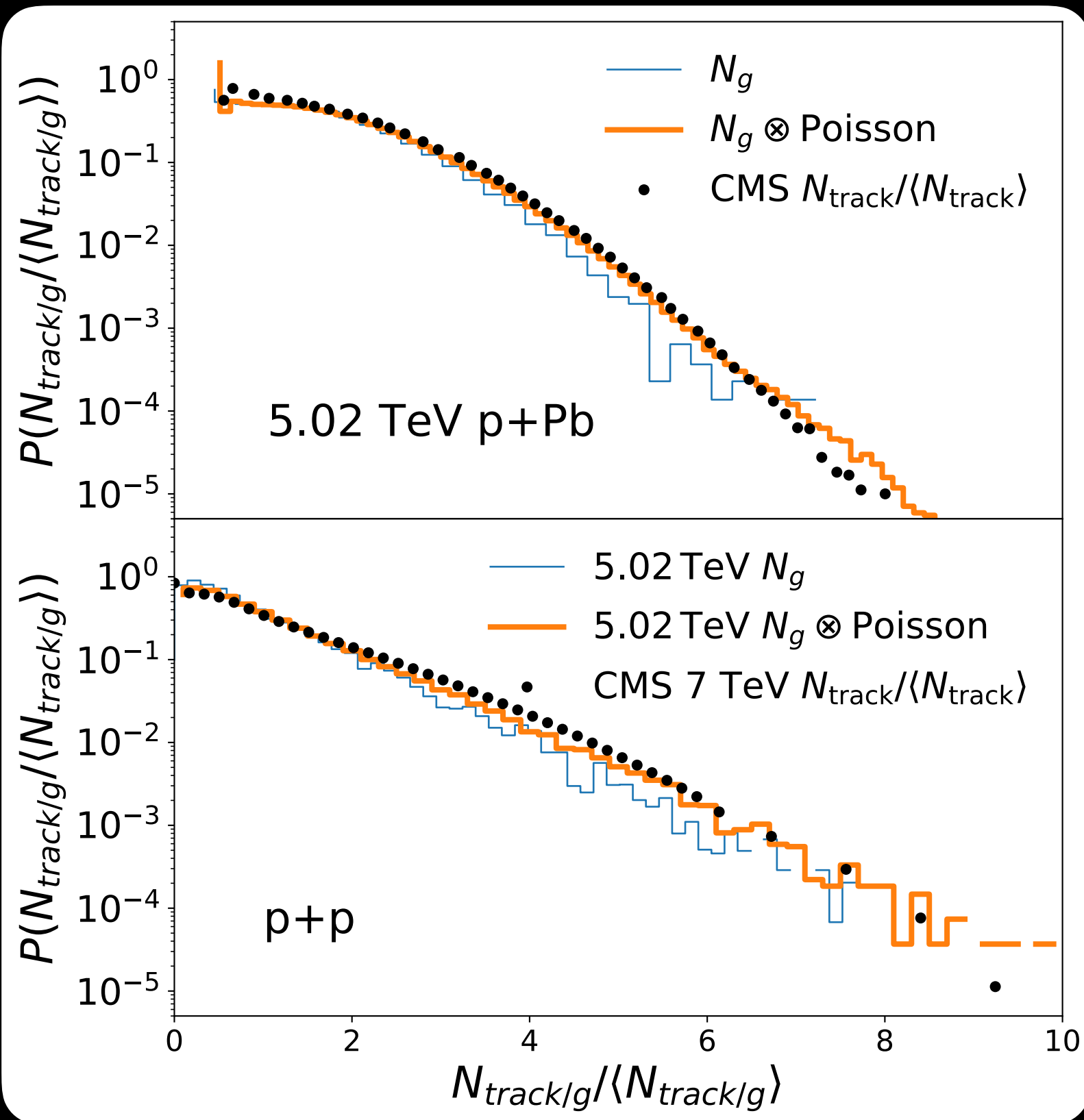


# Integrated anisotropic flow

H. Mäntysaari, B. Schenke, C. Shen, P. Tribedy, arXiv:1705.03177



# MULTIPLICITY DISTRIBUTIONS



- Includes fluctuations of
- nucleon positions in Pb
  - hot spot positions
  - saturation scale normalization
  - color charges
  - Poisson fluctuations to estimate effect from hadronization

# VISCOUS FLUID DYNAMICS

Energy momentum conservation:  $\partial_\mu T^{\mu\nu} = 0$

with  $T^{\mu\nu} = \varepsilon u^\mu u^\nu - (P + \Pi)\Delta^{\mu\nu} + \pi^{\mu\nu}$

Navier-Stokes limit:

$\Pi = -\zeta \nabla_\alpha u^\alpha$  (bulk viscous pressure)

$\pi^{\mu\nu} = \eta \nabla^{\langle\mu} u^{\nu\rangle} = \eta[\nabla^\mu u^\nu + \nabla^\nu u^\mu - \frac{2}{3}\Delta^{\mu\nu}(\nabla_\alpha u^\alpha)]$  (shear)

Implementing this is numerically unstable. Need to go to higher order in gradients  $\rightarrow$  evolution equations for  $\Pi$  and  $\pi^{\mu\nu}$  involving relaxation times  $\tau_\Pi$  and  $\tau_\pi$

# VISCOUS FLUID DYNAMICS

Second order equations derived by Israel and Stewart

W. Israel and J. M. Stewart, *Phys. Lett.* 58A, 213 (1976); *Ann. Phys. (N.Y.)* 118, 341 (1979)

New method involving systematic power-counting in Knudsen and inverse Reynolds number

G. S. Denicol, H. Niemi, E. Molnar, D. H. Rischke, *Phys.Rev.* D85, 114047 (2012)

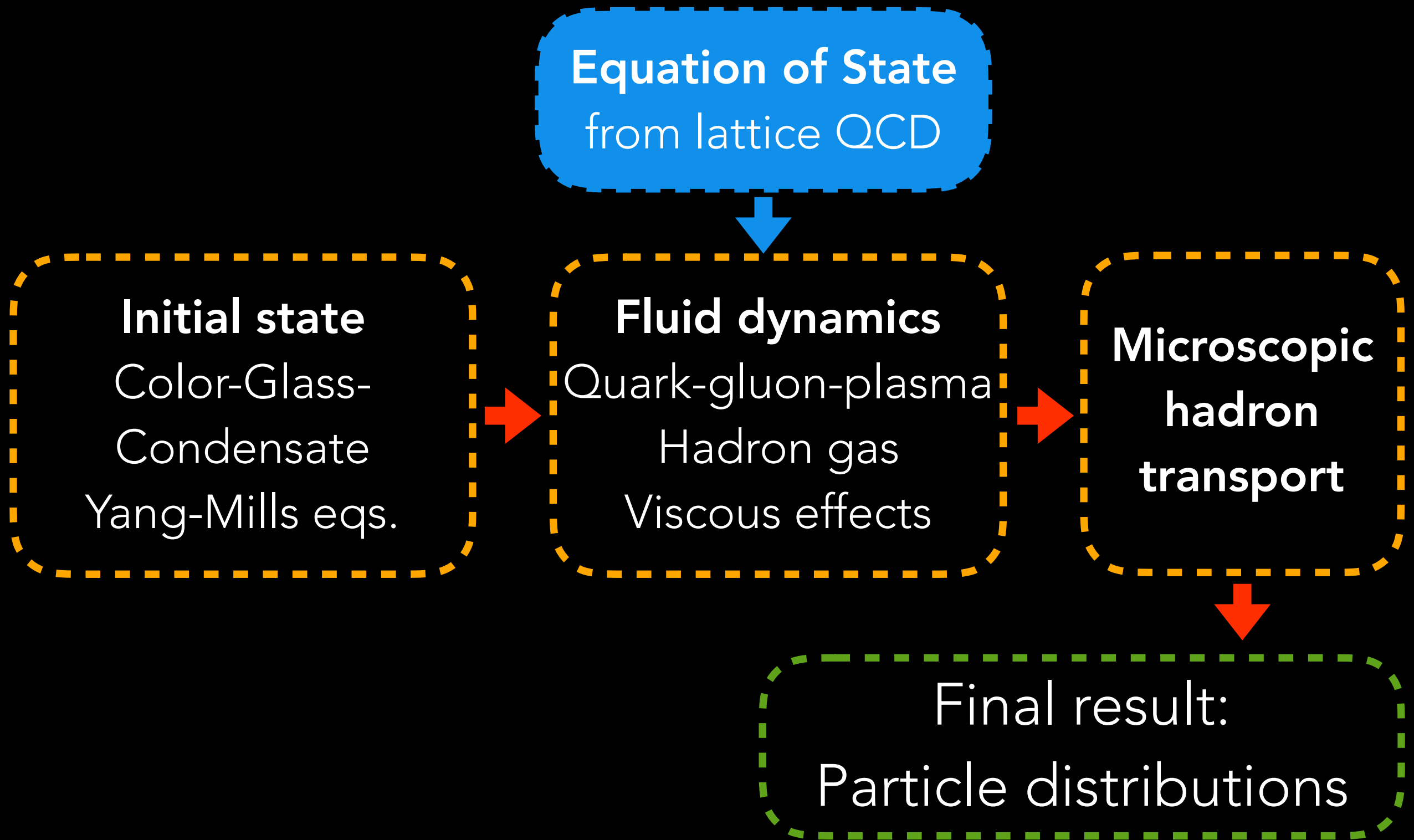
All transport coefficients are determined within this scheme once values for  $\eta$  and  $\zeta$  are chosen

G. S. Denicol, H. Niemi, E. Molnar, D. H. Rischke, *Phys.Rev.* D85, 114047 (2012)

G. S. Denicol, S. Jeon, and C. Gale, *Phys.Rev.* C90, 024912 (2014)

$$\tau_{\Pi} = 5 \frac{\eta}{\varepsilon + P} \quad \tau_{\Pi} = \frac{1}{15 \left(\frac{1}{3} - c_s^2\right)^2} \frac{\zeta}{\varepsilon + P}$$

# SIMULATION FRAMEWORK





# EQUATION OF STATE

Equation of  
State

To close the equations we need  $P(\epsilon)$

We use an EoS constructed from lattice QCD data

S. Borsanyi, Z. Fodor, C. Hoelbling, S. D. Katz, S. Krieg, K. K. Szabo, *Phys. Lett. B* 730, 99–104 (2014)

S. Borsanyi, Z. Fodor, S. D. Katz, S. Krieg, C. Ratti, and K. Szabo, *JHEP* 01, 138 (2012)

$$\frac{P(T)}{T^4} = \frac{P(T_{\text{low}})}{T_{\text{low}}^4} + \int_{T_{\text{low}}}^T \frac{dT'}{T'} \frac{\epsilon - 3P}{T'^4} \quad \text{measured trace anomaly}$$

smoothly matched to a hadron resonance gas

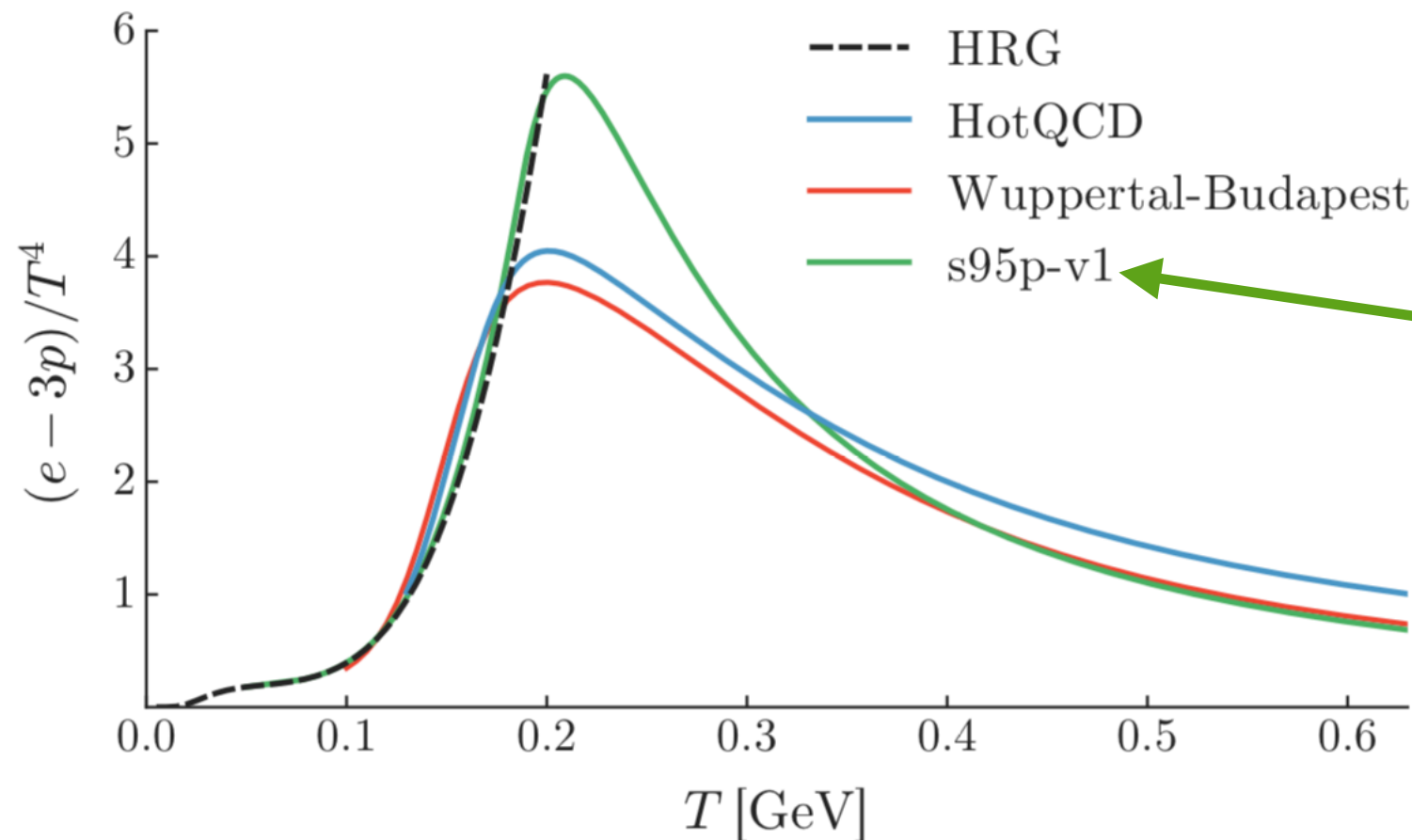
around  $T_{\text{match}} \approx 165$  MeV

The EoS is also constructed at non-zero  $\mu_B$  which we do not need in this talk

# EQUATION OF STATE

Equation of State

Different lattice results and constructions



what we use now

previously used

Figure from J.S. Moreland, R.A. Soltz, Phys.Rev. C93, 044913 (2016)

s95p-v1: P. Huovinen and P. Petreczky, Nucl. Phys. A837, 26–53 (2010)

HotQCD: A. Bazavov et al. (HotQCD), Phys. Rev. D90, 094503 (2014)

WB: S. Borsanyi, Z. Fodor, C. Hoelbling, S. D. Katz, S. Krieg, K. K. Szabo, Phys. Lett. B730, 99–104 (2014)

# MICROSCOPIC HADRON CASCADE

Microscopic  
hadron transport

Sample particles on the freeze-out surface  
(surface of constant energy density)  
according to

$$E \frac{dN_i}{d^3p} = \frac{g_i}{(2\pi)^3} \Delta^3 \Sigma_{\mu} p^{\mu} (f_i^{(0)} + \delta f_i)$$

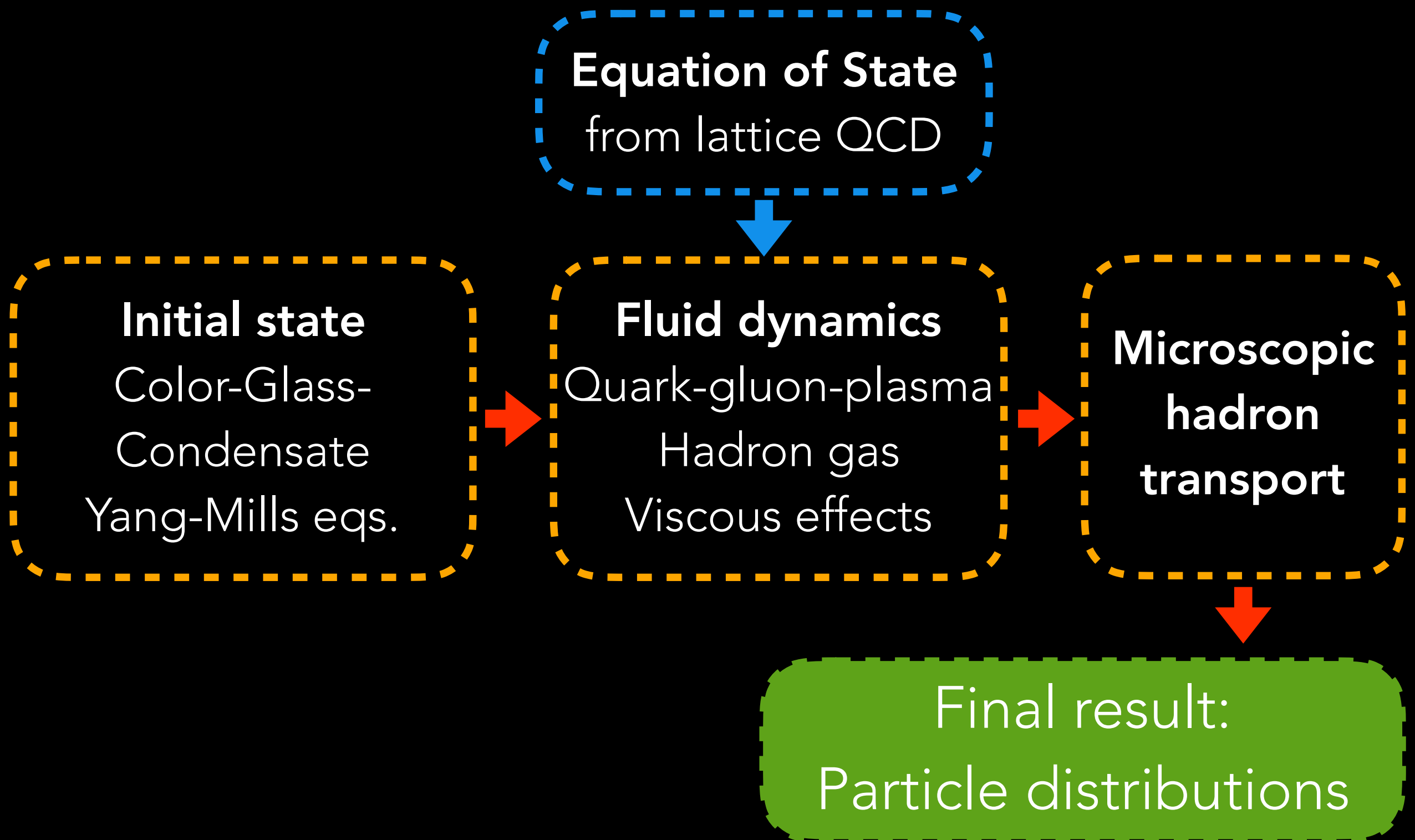
then feed particles into UrQMD

S. A. Bass et al., *Prog. Part. Nucl. Phys.* 41, 255–369 (1998)

M. Bleicher et al., *J. Phys. G* 25, 1859–1896 (1999)

which performs resonance decays and scattering  
according to hadronic cross sections

# SIMULATION FRAMEWORK

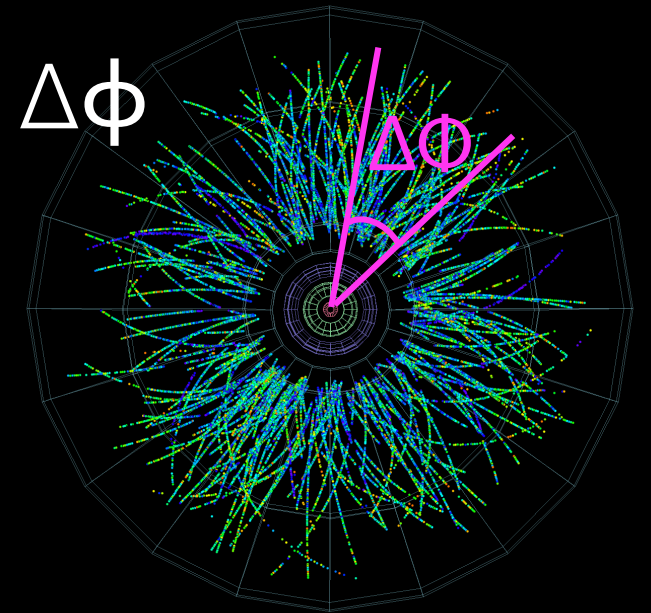


# Introduction: Multi-particle correlations

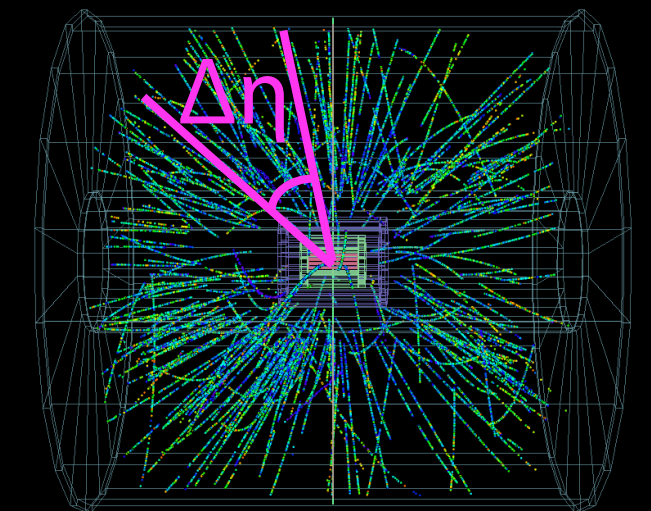
2-particle correlation as a function of  $\Delta\eta$  and  $\Delta\phi$

$\Delta\eta$ : DIFFERENCE IN PSEUDO-RAPIDITY

$\Delta\phi$ : DIFFERENCE IN AZIMUTHAL ANGLE



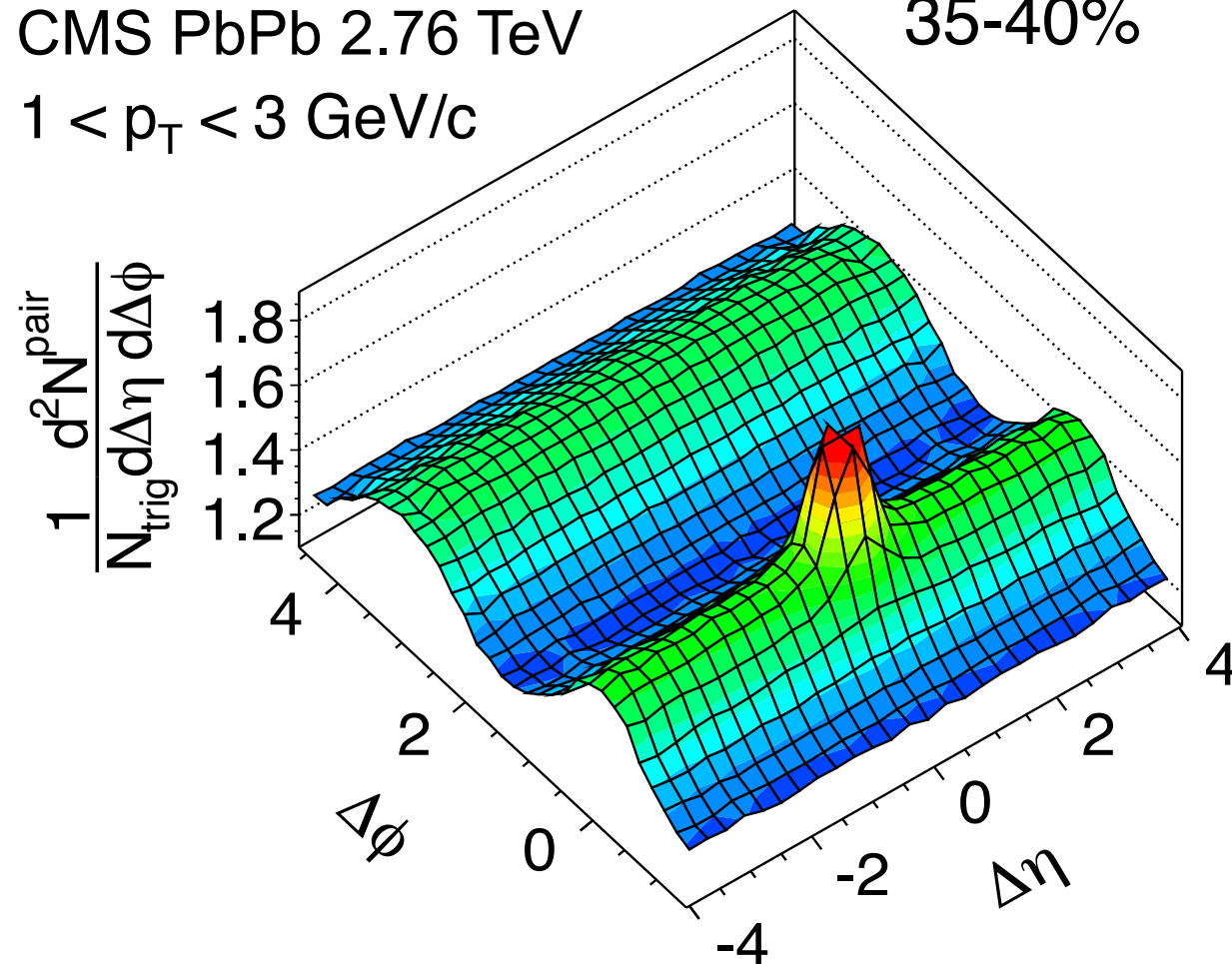
$\Delta\phi$ : DIFFERENCE  
IN AZIMUTHAL ANGLE



$\Delta\eta$ : DIFFERENCE  
IN PSEUDO-RAPIDITY

CMS PbPb 2.76 TeV  
 $1 < p_T < 3$  GeV/c

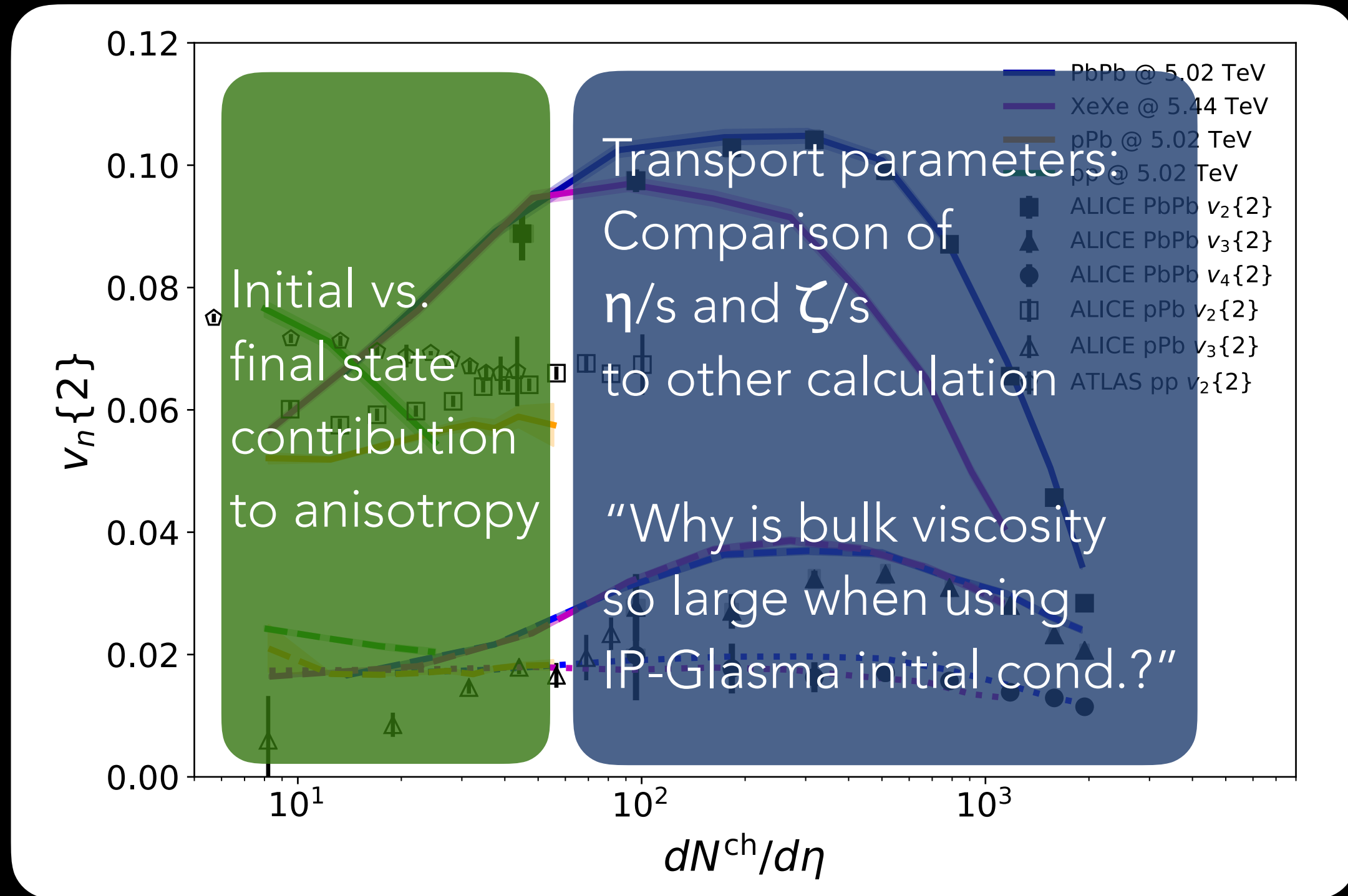
35-40%



CMS COLL., EUR. PHYS. J. C72 (2012)

# Important questions

B. Schenke, C. Shen, P. Tribedy, in preparation



Experimental data: J. Adam et al. (ALICE), Phys. Rev. Lett. 116, 132302 (2016)

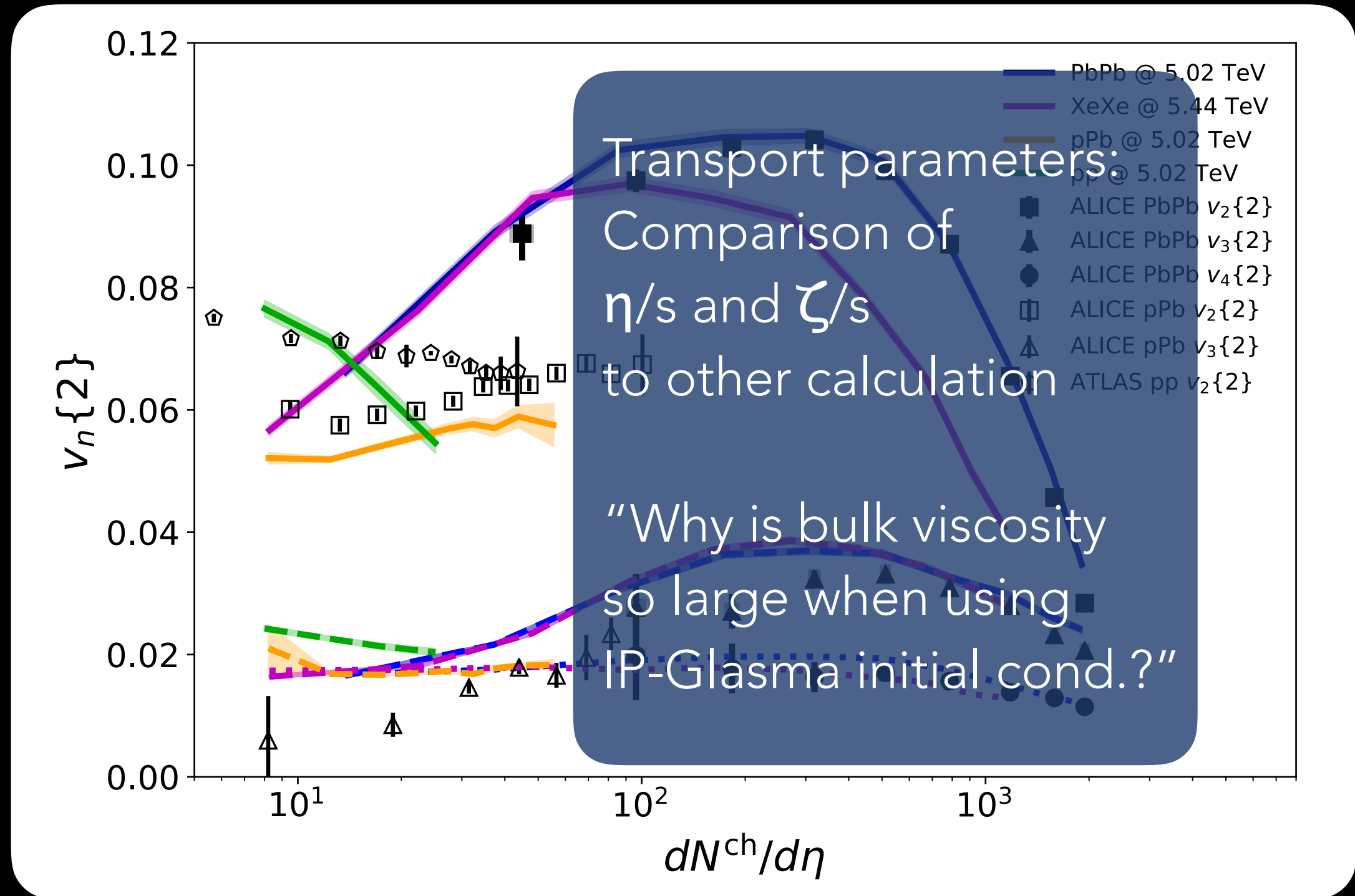
B. B. Abelev et al. (ALICE), Phys. Rev. C90, 054901 (2014), ALICE Collaboration, arXiv:1805.01832

ATLAS Collaboration, Eur. Phys. J. C (2017) 77:428 85

Björn Schenke, BNL

# Why do we need a large $\zeta/s$ ?

B. Schenke, C. Shen, P. Tribedy, in preparation



Experimental data: J. Adam et al. (ALICE), Phys. Rev. Lett. 116, 132302 (2016)

B. B. Abelev et al. (ALICE), Phys. Rev. C90, 054901 (2014), ALICE Collaboration, arXiv:1805.01832

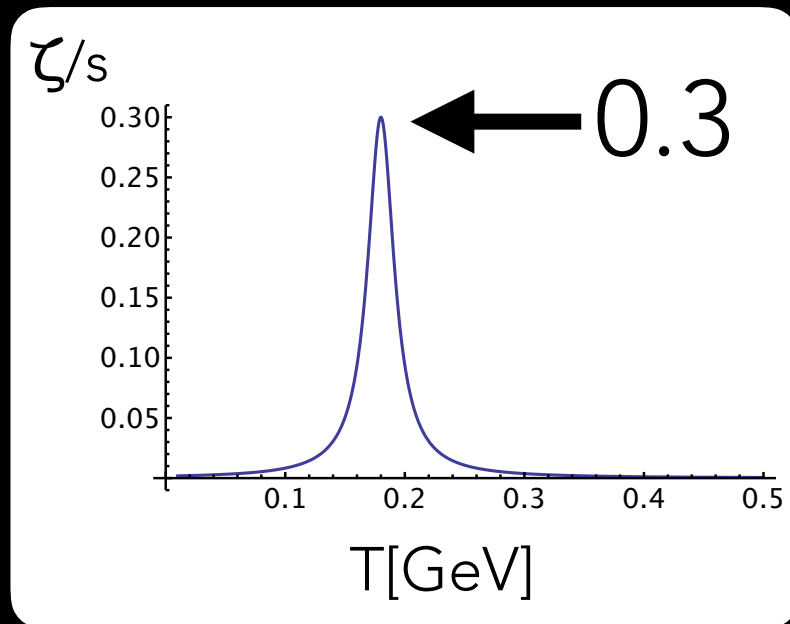
ATLAS Collaboration, Eur. Phys. J. C (2017) 77:428 86

Björn Schenke, BNL

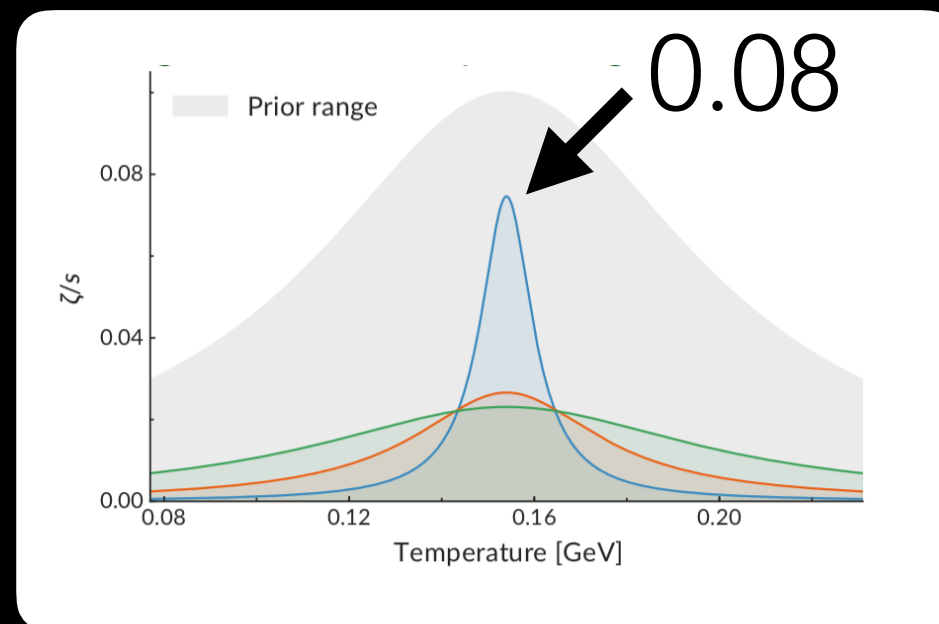


# Why do we need large bulk viscosity?

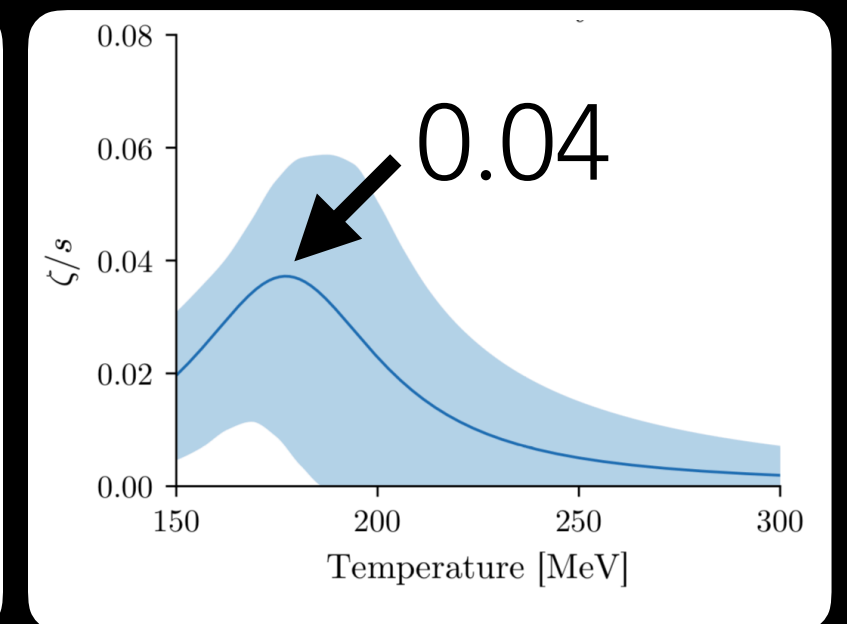
B. Schenke, C. Shen, P. Tribedy, in preparation



this work



S.A. Bass @ QM2017



J. E. Bernhard, arXiv:1804.06469

Also:  $\zeta/s = 0.01$  in R.D. Weller, P. Romatschke, Phys.Lett. B774 (2017) 351-356

$\zeta/s = 0.04$  in P. Bozek, Phys. Lett. B 699 (2011) 283

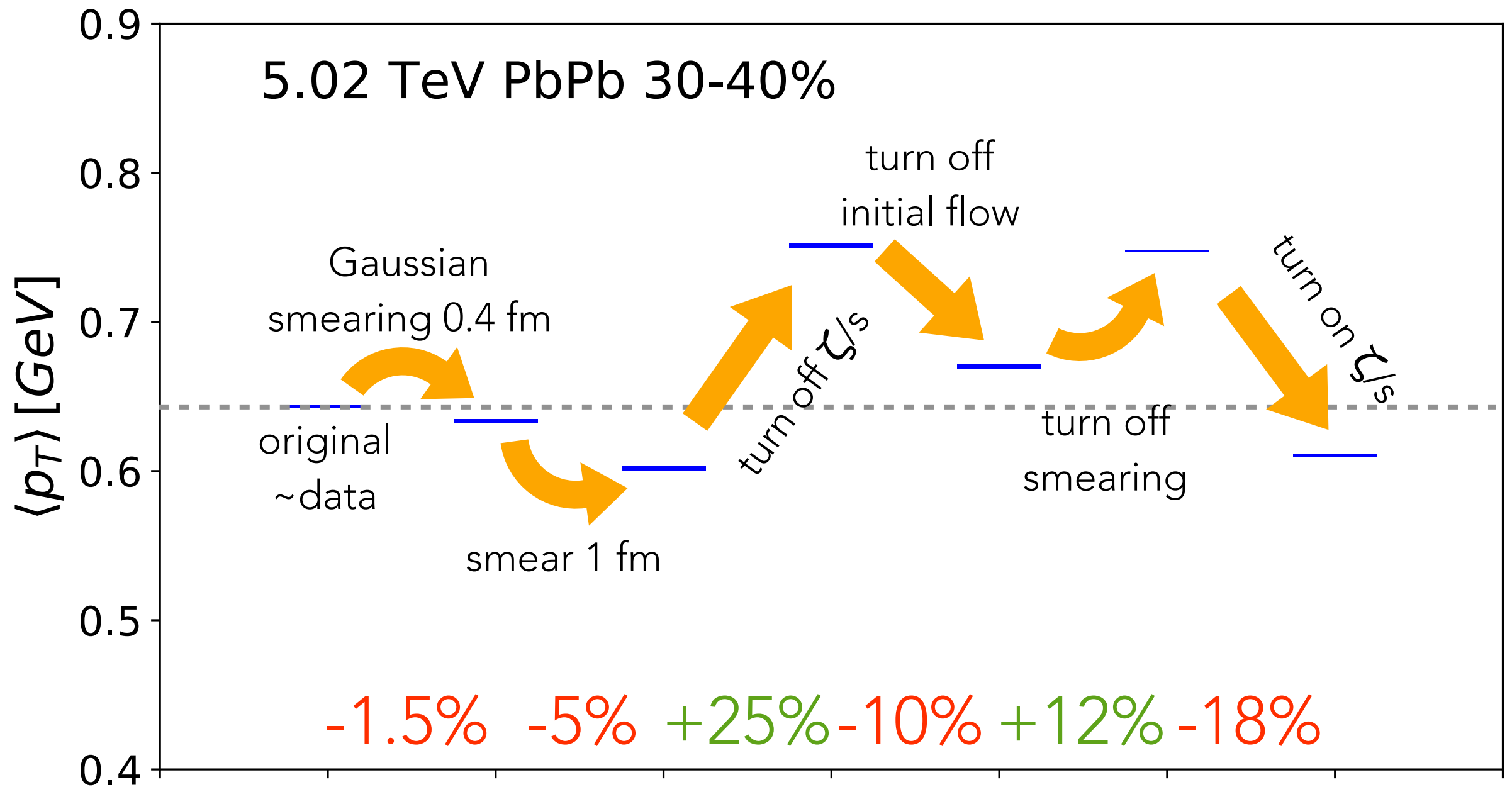
IP-Glasma initial condition requires large bulk viscosity because it generates large  $\langle p_T \rangle$ . But why?

**Possible answers: 1. Strong initial flow 2. Spiky/compact geometry**



# Effects of initial flow and smearing on $\langle p_T \rangle$

B. Schenke, C. Shen, P. Tribedy, in preparation



Also differences in bulk  $\delta f$  between calculations

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# Answer: ~50% initial flow, ~50% size

B. Schenke, C. Shen, P. Tribedy, in preparation

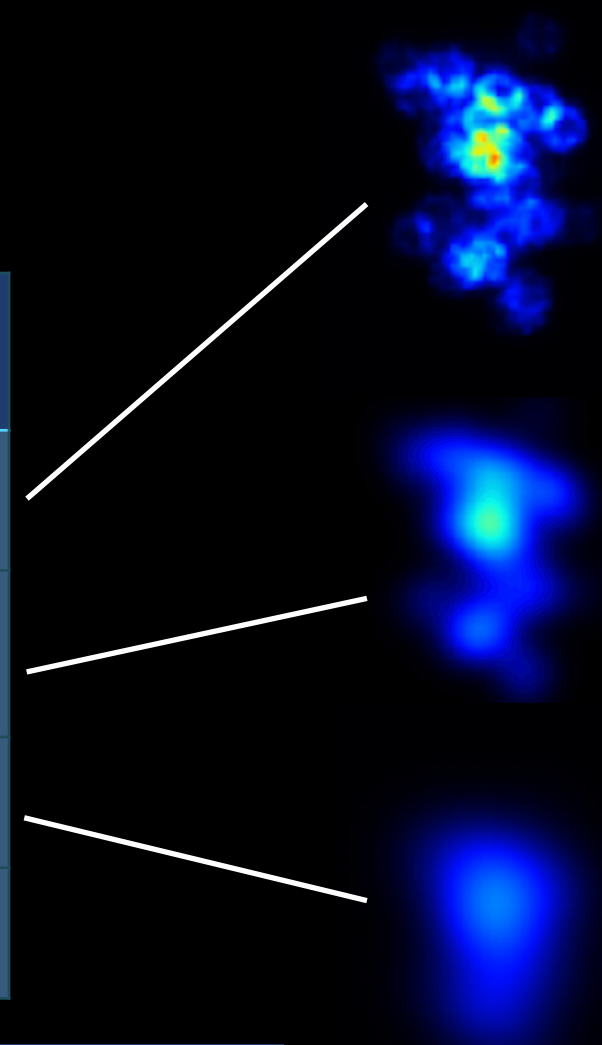
Substructure has little effect on  $v_n$  and  $\langle p_T \rangle$

F. G. Gardim, F. Grassi, P. Ishida, M. Luzum, P. S. Magalhães, J. Noronha-Hostler, arXiv:1712.03912 [nucl-th]

Main effect of Gaussian smearing results from distributing energy over a larger area:

Average rms radii for 30-40% Pb+Pb:

	$\langle r^2 \rangle^{1/2}$ [fm]
IP-GLASMA	2.6
0.4fm SMEARED IP-GLASMA	2.69
1fm SMEARED IP-GLASMA	2.98
MC-GLAUBER $\sigma=0.4$ fm	2.94



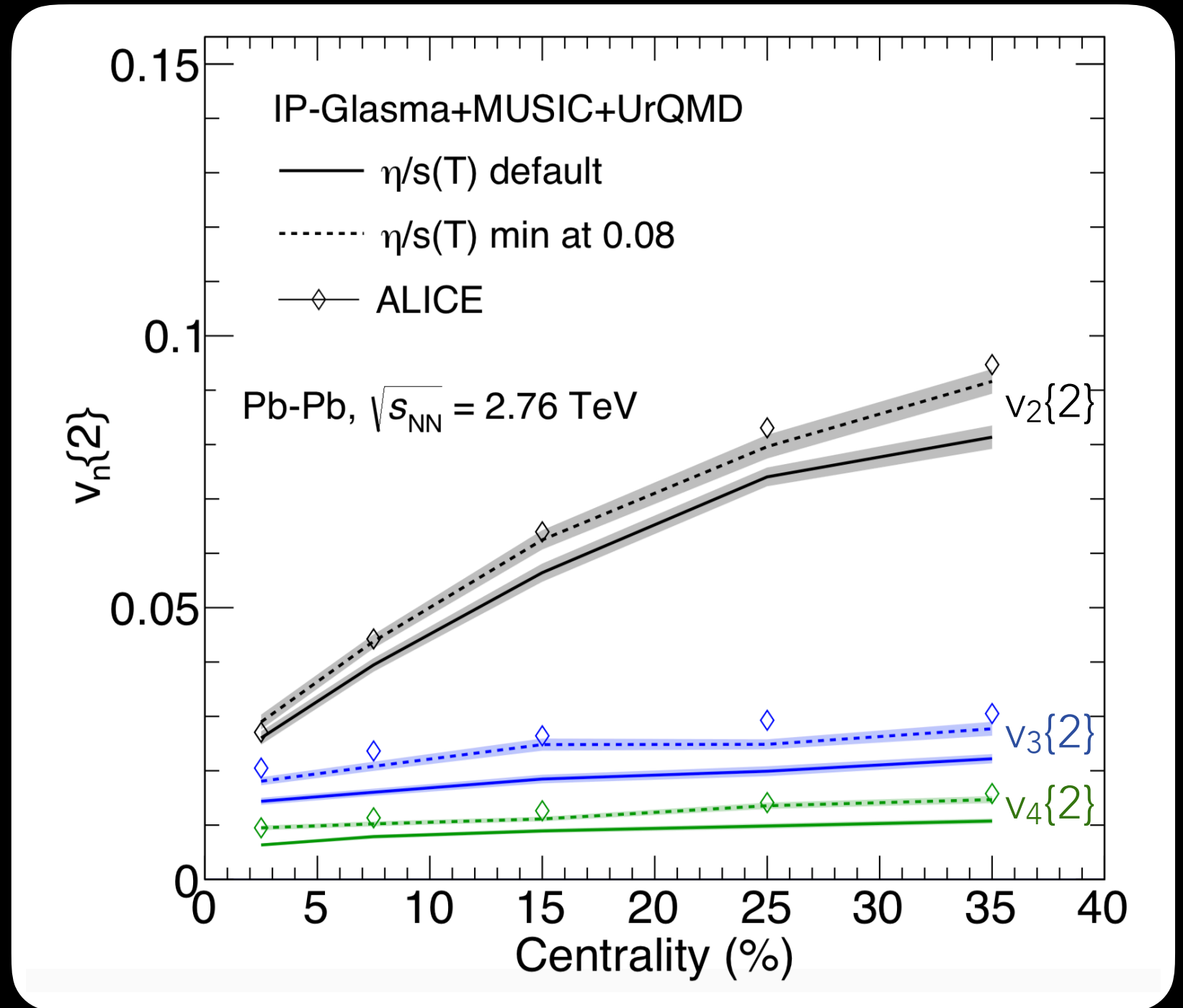
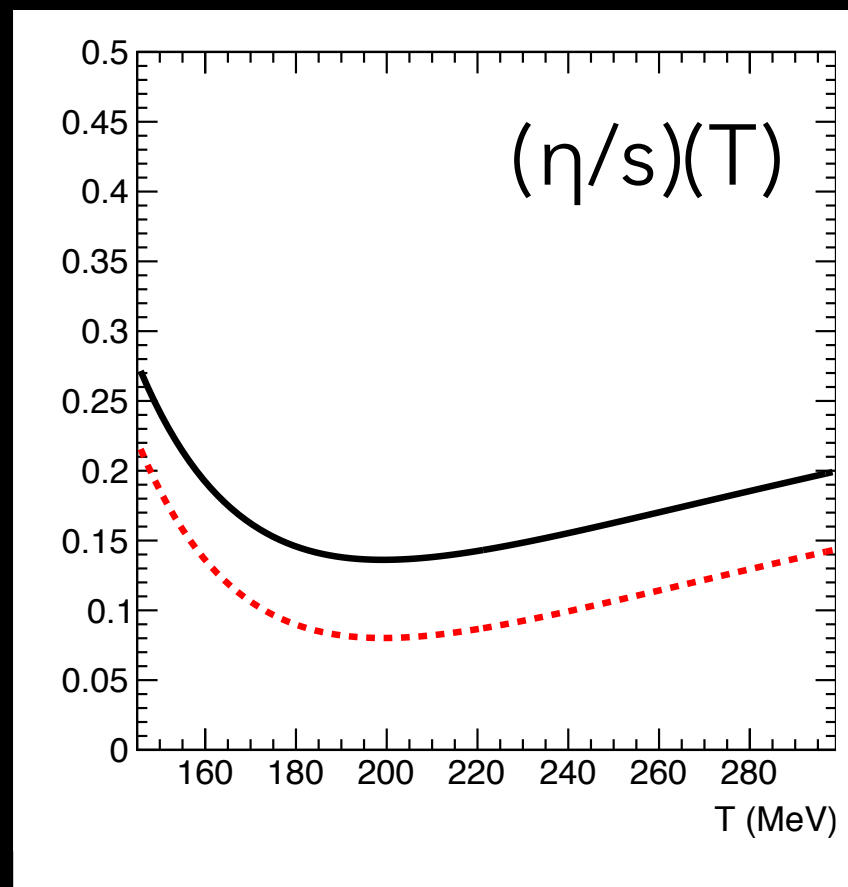
NOTE: JUST  $p=0$  TRENTO DOES NOT MEAN IP-GLASMA

# QCD based $(\eta/s)(T)$

SEE POSTER BY A. DUBLA

A. Dubla, S. Masciocchi, J. M. Pawlowski, B. Schenke, C. Shen, J. Stachel, arXiv:1805.02985

$(\eta/s)(T)$  from a functional diagrammatical approach to QCD  
transport coefficients



M. Haas, L. Fister, and J. M. Pawlowski  
Phys.Rev. D90, 091501 (2014)

N. Christiansen, M. Haas

J. M. Pawlowski, and N. Strodthoff  
Phys. Rev. Lett. 115, 112002 (2015)