# Probing BFKL dynamics, saturation anddiffraction at hadronic colliders

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Contents:

- Proton structure (quarks and <sup>g</sup>luons)
- BFKL dynamics (Forward and Mueller Navelet jets, jet gap jet)
- Jet gap jet in diffraction at the LHC
- Diffractive events: Pomeron structure, jet gap jets
- Photon induced processes



### The HERA accelerator at DESY, Hamburg

HERA: ep collider who closed in 2007, about 1 fb<sup>-1</sup> accumulated



### **HERA kinematics**



Kinematic variables:

- Virtuality exchanged boson

$$
Q^2=-q^2=-(k-k^\prime)^2
$$

- Bjorken scaling variable

$$
x=\frac{Q^2}{2p\cdot q}
$$

- Measurement of the  $ep \rightarrow eX$  cross section: as a function of two independent variables  $x$  and  $O^2$ independent variables  $x$  and  $Q^2$
- $\bullet$  Many methods available to measure  $x$  (momentum fraction of the proton carried by the interacting quark), or  $Q^2$  (transfered energy squared) using scattered electron or hadron information

### The proton structure



- Study the proton structure as a function of  $x$  (Balitski Fadin Kuraev Lipatov evolution equation) or as a function of  $Q^2$  (Dokshitzer Gribov Lipatov Altarelli Parisi)
- $\bullet$   $Q^2$ : Resolution power (like a microscope):
- $\bullet \; x$ : momentum fraction of the proton carried away by the quark/gluon how does the gluon density increase at low  $x$ ?

### <sup>A</sup> picture of one electron-proton interaction

- One electron-proton interaction in the H1 detector: the electron is scattered and the proton is destroyed
- The electron probes the proton structure in terms of quarks and <sup>g</sup>luons



### Measurement of the proton structure function  $F_2$

• Measurement of the DIS cross section

$$
\frac{d\sigma}{dx dQ^2} = \frac{4\pi\alpha^2}{2xQ^4} \left[ (1 + (1 - y)^2) F_2(x, Q^2) - y^2 F_L(x, Q^2) \right]
$$

- Use these data to make QCD fits using NLO (or NNLO) Dokshitzer Gribov Lipatov Altarelli Parisi evolution equation and determine the proton structure in quarks and gluons → allows to predict cross section<br>at Tevatron /LHC at Tevatron/LHC
- At low x: evolution driven by  $g \to q\bar{q}$ , at high  $x, q \to qg$  becomes important important
- Take all data for  $Q^2 > \sim 4$  GeV $^2$ , to be in the perturbative QCD region

$$
\frac{dF_2}{d\log Q^2} \sim \frac{\alpha_S}{2\pi} \left[ P_{qg} \otimes g + P_{qq} \otimes \Sigma \right]
$$



### Kinematical domain at HERA



### <sup>15</sup> years of proton structure measurements at HERA

- $\bullet\,$  Low  $x$  and high gluon density: new field, main discovery at HERA
- <sup>15</sup> years of work: proton structure in terms of quarks and <sup>g</sup>luons: NLOQCD is working well!
- Missing transverse information (TMDs, GPDs...): to be performed at the EIC, also using Deeply Virtual Compton Scattering events



### Quark and Gluon extraction

- Using the DGLAP evolution equation, obtain the quark and <sup>g</sup>luondensities in the proton as a function of  $x$  and  $Q^2$
- Method: Assume quark and gluon distributions at  $Q_0^2 = 4$   $GeV^2$  with some parameters, compute cross section for different  $Q^2$  using DGLAP, and fit the parameters so that they describe the measured values
- $\bullet\,$  Proton is gluon dominated at small  $x$



### <sup>A</sup> better understanding of the heavy ion structure

- Kinematical domain at the EIC
- The heavy ion structure is poorly known at low  $x$  and also at high  $Q^2$ : similar situation as before HERA but for nuclei
- Similar gain in kinematical domain  $(x$  and  $Q^2)$  for nuclei compared to HERA for the proton
- See E.C. Aschenauer at al., ArXiv:1708.05654



### <sup>A</sup> better understanding of the heavy ion structure

- As an example: measure  $eA \rightarrow eX$  cross section
- $eAu$  cross section measurement
- Very good precision expected: can we see new effects in QCD such as saturation (higher <sup>g</sup>luon density in heavy ions)





### Forward jet measurement at HERA



- Full BFKL NLL calculation used for the BFKL kernel, available in S3 and S4 resummation schemes to remove the spurious singularities (modulo the impact factors taken at LL)
- Equation:

$$
\frac{d\sigma_{T,L}^{\gamma^* p \to JX}}{dx_J dk_T^2} = \frac{\alpha_s(k_T^2)\alpha_s(Q^2)}{k_T^2 Q^2} f_{eff}(x_J, k_T^2)
$$

$$
\int \frac{d\gamma}{2i\pi} \left(\frac{Q^2}{k_T^2}\right)^{\gamma} \phi_{T,L}^{\gamma}(\gamma) e^{\bar{\alpha}(k_T Q)\chi_{eff}[\gamma,\bar{\alpha}(k_T Q)]Y}
$$

• Implicit equation:  $\chi_{eff}(\gamma, \alpha) = \chi_{NLL}(\gamma, \alpha, \chi_{eff}(\gamma, \alpha))$  solved numerically (Nucl. Phys. <sup>B</sup> <sup>739</sup> (2006) 131; Phys. Lett. <sup>B</sup> <sup>655</sup> (2007) 236; Eur. Phys. J. C55 (2008) 259)

#### Comparison with H1 triple differential data



**<sup>d</sup>**σ**/dx dpT<sup>2</sup> d Q<sup>2</sup> - H1 DATA**

### Mueller Navelet jets

Same kind of processes at the Tevatron and the LHC



- Same kind of processes at the Tevatron and the LHC: Mueller Navelet jets
- $\bullet$  Study the  $\Delta \Phi$  between jets dependence of the cross section:
- See papers by Papa, Murdaca, Wallon, Szymanowski, Ducloue, Sabio-Vera, Chachamis...

# Mueller Navelet jets:  $\Delta\Phi$  dependence

- $\bullet$  Study the  $\Delta \Phi$  dependence of the relative cross section
- Relevant variables:

$$
\Delta \eta = y_1 - y_2
$$
  
\n
$$
y = (y_1 + y_2)/2
$$
  
\n
$$
Q = \sqrt{k_1 k_2}
$$
  
\n
$$
R = k_2/k_1
$$

• Azimuthal correlation of dijets:

$$
2\pi \frac{d\sigma}{d\Delta \eta dR d\Delta \Phi} / \frac{d\sigma}{d\Delta \eta dR} = 1 +
$$

$$
\frac{2}{\sigma_0(\Delta \eta, R)} \sum_{p=1}^{\infty} \sigma_p(\Delta \eta, R) \cos(p\Delta \Phi)
$$

where

$$
\sigma_p = \int_{E_T}^{\infty} \frac{dQ}{Q^3} \alpha_s (Q^2/R) \alpha_s (Q^2 R)
$$

$$
\left( \int_{y_<}^{y_>} dy x_1 f_{eff}(x_1, Q^2/R) x_2 f_{eff}(x_2, Q^2 R) \right)
$$

$$
\int_{1/2-\infty}^{1/2+\infty} \frac{d\gamma}{2i\pi} R^{-2\gamma} e^{\bar{\alpha}(Q^2)\chi_{eff}(p)\Delta\eta}
$$

# Mueller Navelet jets:  $\Delta\Phi$  dependence

•  $1/\sigma d\sigma/d\Delta\Phi$  spectrum for BFKL LL and BFKL NLL as a function of  $\Delta\Phi$  for different values of  $\Delta\eta$ , scale dependence:  $\sim$ 20%



- C. Marquet, C.R., Phys. Rev. D79 (2009) <sup>034028</sup>
- Mueller Navelet jets at NLL and saturation effects: Study in progress with F. Deganutti, T. Raben, S. Schlichtling

### Effect of energy conservation on BFKL equation

- BFKL cross section lacks energy-momentum conservation since these effects are higher order corrections
- $\bullet\,$  Following Del Duca-Schmidt, we substitute  $\Delta\eta$  by an effective rapidity interval  $y_{eff}$

$$
y_{eff} = \Delta \eta \left( \int d\phi \cos(p\phi) \frac{d\sigma^{O(\alpha_s^3)}}{d\Delta \eta dy dQ dR d\Delta \Phi} \right)
$$

$$
\left( \int d\phi \cos(p\phi) \frac{d\sigma^{LL-BFKL}}{d\Delta \eta dy dQ dR d\Delta \Phi} \right)^{-1}
$$

where  $d\sigma^{O(\alpha_s^3)}$  is the exact  $2\!\to\!3$  contribution to the  $hh\!\to\!JXJ$ cross-section at order  $\alpha_s^3$ , and  $d\sigma^{LL-BFKL}$  is the LL-BFKL result

• $\bullet$  To compute  $d\sigma^{O(\alpha_s^3)},$  we use the standard jet cone size  $R_{cut}\!=\!0.5$  when integrating over the third particle's momentum

#### Mueller Navelet cross sections: energy conservation effect in BFKL

- Effect of energy conservation on BFKL dynamics
- $\bullet$  Large effect if jet  $p_T$  ratios not close to 1: goes closer to DGLAP predictions, needs jet  $p_T$  ratio  $< 1.1$ - $1.15\,$



### Saturation effects at the LHC: Use pA data

- $\bullet$  Saturation effects: need to go to low  $x$ , jets as forward as possible on the same side
- Compare pp and pA runs in order to remove many systematics



### **Saturation effects at the LHC**

- $\bullet$  Suppression factor between pp and pA runs: estimated to be  $1/2$  in CASTOR acceptance
- Important to get CASTOR in pA and low lumi pp data
- Study performed by Cyrille Marquet et al.; in progress by F. Deganutti, M. Hentschinski, T. Raben, S. Schlichting, CR



### Jet gap jet cross sections



- $\bullet$  Test of BFKL evolution: jet gap jet events, large  $\Delta\eta$ , same  $p_T$  for both jets in BFKL calculation
- Principle: Implementation of BFKL NLL formalism in HERWIG Monte Carlo (Measurement sensitive to jet structure and size, gap size smaller than  $\Delta\eta$  between jets)

#### BFKL formalism

• BFKL jet gap jet cross section: integration over  $\xi,~p_T$  performed in Herwig event generation

$$
\frac{d\sigma^{pp \to XJJY}}{dx_1 dx_2 dp_T^2} = \mathcal{S} \frac{f_{eff}(x_1, p_T^2) f_{eff}(x_2, p_T^2)}{16\pi} \left| A(\Delta \eta, p_T^2) \right|^2
$$

where  $S$  is the survival probability (0.1 at Tevatron, 0.03 at LHC)

$$
A(\Delta \eta, p_T^2) = \frac{16N_c \pi \alpha_s^2}{C_F p_T^2} \sum_{p=-\infty}^{\infty} \int \frac{d\gamma}{2i\pi} \frac{[p^2 - (\gamma - 1/2)^2]}{[(\gamma - 1/2)^2 - (p - 1/2)^2]}
$$

$$
\frac{\exp\left\{\frac{\alpha_S N_C}{\pi} \chi_{eff} \Delta \eta\right\}}{[(\gamma - 1/2)^2 - (p + 1/2)^2]}
$$

- $\bullet$   $\alpha_S$ : 0.17 at LL (constant), running using RGE at NLL
- $\bullet\,$  BFKL effective kernel  $\chi_{eff}$ : determined numerically, solving the implicit equation:  $\chi_{eff} = \chi_{NLL}(\gamma, \bar{\alpha} \,\, \chi_{eff})$
- S4 resummation scheme used to remove spurious singularities in BFKLNLL kernel
- Implementation in Herwig Monte Carlo: needed to take into account jet size and at parton level the gap size is equal to  $\Delta\eta$  between jets
- Herwig MC: Parametrised distribution of  $d\sigma/dp_T^2$  fitted to BFKL NLL cross section (2200 points fitted between  $10 < p_T < 120$  GeV,  $0.1 < \Delta \eta < 10$  with a  $\chi^2 \sim 0.1$ )

### Comparison with D0 data

- D0 measurement: Jet gap jet cross section ratios as <sup>a</sup> function of second highest  $E_T$  jet, or  $\Delta \eta$  for the low and high  $E_T$  samples, the gap between jets being between -1 and <sup>1</sup> in rapidity
- •Comparison with BFKL formalism:

$$
Ratio = \frac{BFKL \ NLL \ Hervig}{Dijet \ Hervig} \times \frac{LO \ QCD \ NLOJet++}{NLO \ QCD \ NLOJet++}
$$

• Reasonable description using BFKL NLL formalism



### Full NLL calculation (in progress)

- Combine NLL kernel with NLO impact factors (Hentschinski, Madrigal, Murdaca, Sabio Vera 2014)
- At NLO, impact factors are much more complicated!



### NLL impact factors

- –Mix loop momenta (not factorized)
- Involve jet distributions with two final states
- Contain complicated non-analytic progress
- Work in progress by D. Colferai, F. Daganutti, T. Raben
- Will lead to an improved parametrisation to be omplemented in**HERWIG**

# Understanding saturation?  $F_{L}$  measurement at  $\sf HERA$

- Different impacts of saturation on longitudinal and transverse cross sections
- • $\bullet$  Important to measure  $F_2$  and  $F_L$  independently at HERA: unfortunately, the error bars were large

$$
\frac{d\sigma}{dx dQ^2} = \frac{4\pi\alpha^2}{2xQ^4} \left[ (1 + (1 - y)^2) F_2(x, Q^2) - y^2 F_L(x, Q^2) \right]
$$





# $F_{L}$  measurement at the EIC  $\,$

- $\bullet$   $F_L$  measurement in eA collisions
- High precision expected: important to probe saturation effects, and see different evolutions between  $F_2$  and  $F_L$
- This could be <sup>a</sup> clear indication of saturation!



### **Diffraction: DIS and Diffractive event at HERA**



eHI<sub>5</sub>

 $\frac{1}{Z}^{\text{R}}$ 

### Definition of diffraction: example of HERA

- Typical DIS event: part of proton remnants seen in detectors in forwardregion (calorimeter, forward muon...)
- HERA observation: in some events, no energy in forward region, or in other words no colour exchange between proton and jets produced inthe hard interaction
- Leads to the first experimental method to detect diffractive events: rapidity gap in calorimeter: difficult to be used at the LHC because of pile up events
- Second method to find diffractive events: Tag the proton in the final state, method to be used at the LHC (example of AFP project)



### Diffractive kinematical variables



- Momentum fraction of the proton carried by the colourless object (pomeron):  $x_p = \xi = \frac{Q^2 + M_X^2}{Q^2 + W^2}$
- Momentum fraction of the pomeron carried by the interacting parton if we assume the colourless object to be made of quarks and <sup>g</sup>luons:  $\beta = \frac{Q^2}{Q^2 + M_X^2} = \frac{x_{Bj}}{x_P}$
- 4-momentum squared transferred:  $t = (p p')^2$

### Parton densities in the pomeron (H1)

- Extraction of <sup>g</sup>luon and quark densities in pomeron: <sup>g</sup>luon dominated
- $\bullet$  Gluon density poorly constrained at high  $\beta$



## Factorization breaking between  $\emph{ep}$  and  $\emph{pp}$

- Comparison between Tevatron CDF data and extrapolations from HERA
- Discrepancy due to survival probability





### Factorization studies at HERA in Photoproduction

- $\bullet\,$  Factorization is not expected to hold for resolved  $\gamma$
- Observed by H1 but not by ZEUS; measurement to be done at the EIC?





### **Hard diffraction at the LHC**

- $\bullet\,$  Dijet production: dominated by  $gg$  exchanges;  $\gamma+$ jet production: dominated by  $qg$  exchanges
- Jet gap jet in diffraction: Probe BFKL
- Three aims
- $-$  Is it the same object which explains diffraction in  $pp$  and  $ep?$
- Further constraints on the structure of the Pomeron as was determined at HERA
- – Survival probability: difficult to compute theoretically, needs to be measured, inclusive diffraction is optimal place for measurement



### Inclusive diffraction at the LHC: sensitivity to <sup>g</sup>luon density

- Predict DPE dijet cross section at the LHC in AFP acceptance, jets with  $p_T >$ 20 GeV, reconstructed at particle level using anti-k $_T$  algorithm
- Sensitivity to <sup>g</sup>luon density in Pomeron especially the <sup>g</sup>luon density onPomeron at high  $\beta$ : multiply the gluon density by  $(1-\beta)^{\nu}$  with  $\nu = -1, ..., 1$
- Measurement possible with 10  $pb^{-1}$ , allows to test if gluon density is similar between HERA and LHC (universality of Pomeron model)
- Dijet mass fraction: dijet mass divided by total diffractive mass  $(\sqrt{\xi_1 \xi_2 S})$



### Inclusive diffraction at the LHC: sensitivity to quark densities

- Predict DPE  $\gamma+$ jet divided by dijet cross section at the LHC
- Sensitivity to universality of Pomeron model
- Sensitivity to quark density in Pomeron, and of assumption:  $u=d=s=\bar{u}=\bar{d}=\bar{s}$  used in QCD fits at HERA
- Measurement of  $W$  asymmetry also sensitive to quark densities
- $\bullet$  Perform the diffractive/ultra-peripheral studies at the EIC



### Jet gap jet events in diffraction

- Jet gap jet events in DPE processes: clean process, allows to go to larger  $\Delta \eta$  between jets
- See: Gaps between jets in double-Pomeron-exchange processes at the LHC, C. Marquet, C. Royon, M. Trzebinski, R. Zlebcik, Phys. Rev. <sup>D</sup><sup>87</sup> (2013) <sup>034010</sup>
- Can be studied at EIC: gaps between jets



### Exclusive diffraction at the LHC (and the EIC)



- Many exclusive channels can be studied at medium and high luminosity: jets,  $\chi_C$ , charmonium,  $J/\Psi....$
- Possibility to reconstruct the properties of the object produced exclusively (via photon and <sup>g</sup>luon exchanges) from the tagged proton: system completely constrained
- Central exclusive production is a potential channel for BSM physics: sensitivity to high masses up to  $1.8$  TeV (masses above 400 GeV, depending how close one can go to the beam)
- $\bullet\,$  Very interesting channel at high mass sensitive to  $\gamma\gamma\gamma\gamma$  anomalous couplings (via loops or resonane) (see S. Fichet, G. von Gersdorff, C. Royon, Phys. Rev.. D93 (2016) no.7, 075031; Phys. Rev. Lett. <sup>116</sup> (2016) no.23, <sup>231801</sup>
- $\bullet\,$  Exclusive production can be studied both in  $ep$  and  $eA$  at the EIC

Search for  $\gamma\gamma WW$ ,  $\gamma\gamma\gamma\gamma$  quartic anomalous coupling at the LHC



- Study of the process:  $pp \to ppWW$ ,  $pp \to ppZZ$ ,  $pp \to pp\gamma\gamma$
- Standard Model:  $\sigma_{WW} = 95.6$  fb,  $\sigma_{WW}(W = M_X > 1 TeV) = 5.9$  fb
- $\bullet\,$  Process sensitive to anomalous couplings:  $\gamma\gamma WW$ ,  $\gamma\gamma ZZ$ ,  $\gamma\gamma\gamma\gamma;$ motivated by studying in detail the mechanism of electroweak symmetry breaking, predicted by extradim. models
- $\bullet\,$  Rich  $\gamma\gamma$  physics at LHC: see papers by C. Baldenegro, E. Chapon, S. Fichet, G. von Gersdorff, O. Kepka, B. Lenzi, C. Royon, M. Saimpert: Phys. Rev. D78 (2008) 073005; Phys. Rev. D81 (2010) 074003; Phys.Rev. D89 (2014) <sup>114004</sup> ; JHEP <sup>1502</sup> (2015) 165; Phys. Rev. Lett. <sup>116</sup> (2016) no 23, 231801; Phys. Rev. D93 (2016) no 7, 075031; JHEP <sup>1706</sup> (2017) <sup>142</sup>

#### $\gamma\gamma$ exclusive production: SM contribution



- • $\bullet$  QCD production dominates at low  $m_{\gamma\gamma}$ , QED at high  $m_{\gamma\gamma}$
- Important to consider W loops at high  $m_{\gamma\gamma}$
- At high masses  $(> 200 \text{ GeV})$ , the photon induced processes are dominant
- Conclusion: Two photons and two tagged protons means photon-induced process

### Motivations to look for quartic  $\gamma\gamma$  anomalous couplings



• Two effective operators at low energies

$$
\mathcal{L}_{4\gamma} = \zeta_1^{\gamma} F_{\mu\nu} F^{\mu\nu} F_{\rho\sigma} F^{\rho\sigma} + \zeta_2^{\gamma} F_{\mu\nu} F^{\nu\rho} F_{\rho\lambda} F^{\lambda\mu}
$$

 $\bullet\;\gamma\gamma\gamma\gamma$  couplings can be modified in a model independent way by loops of heavy charge particles

$$
\zeta_1 = \alpha_{em}^2 Q^4 m^{-4} N c_{1,s}
$$

where the coupling depends only on  $Q^4m^{-4}$  (charge and mass of the charged particle) and on spin,  $c_{1,s}$  depends on the spin of the particle This leads to  $\zeta_1$  of the order of  $10^{-14}$ - $10^{-13}$ 

 $\bullet$   $\zeta_1$  can also be modified by neutral particles at tree level (extensions of the SM including scalar, pseudo-scalar, and spin-2 resonances that couple to the photon)  $\zeta_1 = (f_sm)^{-2}d_{1,s}$  where  $f_s$  is the  $\gamma\gamma X$  coupling of the new particle to the photon, and  $d_{1,s}$  depends on the spin of the particle; for instance, 2 TeV dilatons lead to  $\zeta_1\sim 10^{-13}$ 

One aside: what is pile up at LHC?



- The LHC machine collides packets of protons
- Due to high number of protons in one packet, there can be more thanone interaction between two protons when the two packets collide
- Typically up to <sup>50</sup> pile up events

### Search for quartic  $\gamma\gamma$  anomalous couplings



- $\bullet\,$  Search for  $\gamma\gamma\gamma\gamma$  quartic anomalous couplings
- Couplings predicted by extra-dim, composite Higgs models
- Analysis performed at hadron level including detector efficiencies, resolution effects, pile-up...



### Search for quartic  $\gamma\gamma$  anomalous couplings





- No background after cuts for 300 fb<sup>-1</sup>: sensitivity up to a few  $10^{-15}$ , better by <sup>2</sup> orders of magnitude with respect to "standard" methods
- Exclusivity cuts using proton tagging needed to suppress backgrounds
- $\bullet\,$  For  $Z\gamma$  production: gain of 3 orders of magnitude compared to usual LHC searches (looking for <sup>Z</sup> decaying leptonically and hadronically)

### Generalization - Looking for axion lile particles





### Search for axion like particles



- Production of axions via photon exchanges and tagging the intact protons in the final state complementary to the usual search at the LHC $(Z$  decays into 3 photons): sensitivity at high axion mass (spin 0 even) resonance, width <sup>45</sup> GeV)- C. Baldenegro, S. Fichet, G. von Gersdorff, C. Royon, ArXiv 1803.10835
- Complementarity with Pb Pb running: sensitivity to low mass diphoton, low luminosity but cross section increased by  $Z^4$

'

### Removing pile up: measuring proton time-of-flight



- Measure the proton time-of-flight in order to determine if they originate from the same interaction as our photon
- Typical precision: <sup>10</sup> ps means 2.1 mm

### **Conclusion**

- Inclusive structure function measurement: well described by perturbative  $\mathsf{QCD}_{\mathsf{r}}$  too inclusive to look for saturation/BFKL resummation effects
- EIC: ideal to understand better the ion structure
- Use dedicated observables for BFKL/saturation effects: very forward jets (HERA/EIC) and dijets (CASTOR in CMS for instance), Mueller Navelet jets (LHC), Jet gap jets (EIC/LHC)
- Full implementation of BFKL NLL kernel including impact factors (in progress) for many jet proceeses at HERA, Tevatron, LHC and thenEIC: to be implemented in MC
- Diffractive studies: Pomeron structure in terms of quarks and <sup>g</sup>luons (LHC/EIC)
- Photon exchange processes: Exploratory physics at the LHC

