

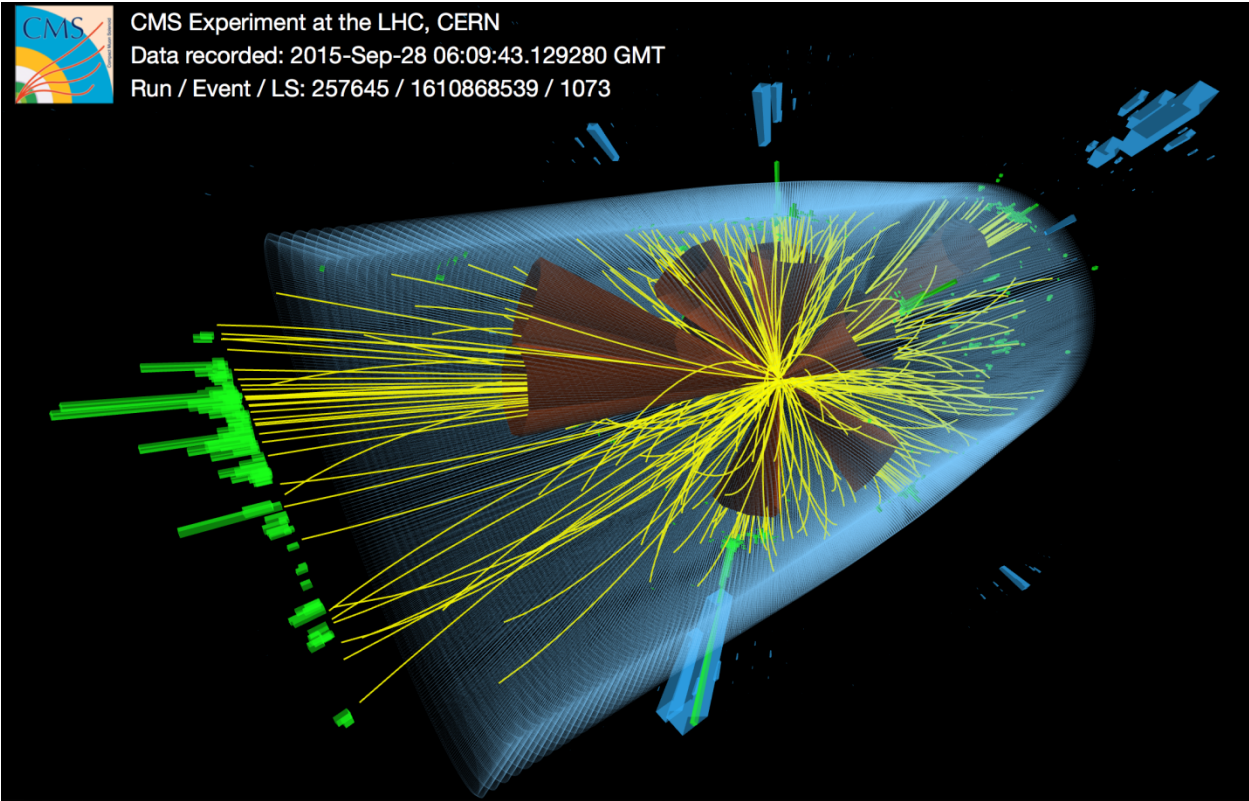
Theory review of jets at the EIC

Felix Ringer

Lawrence Berkeley National Laboratory

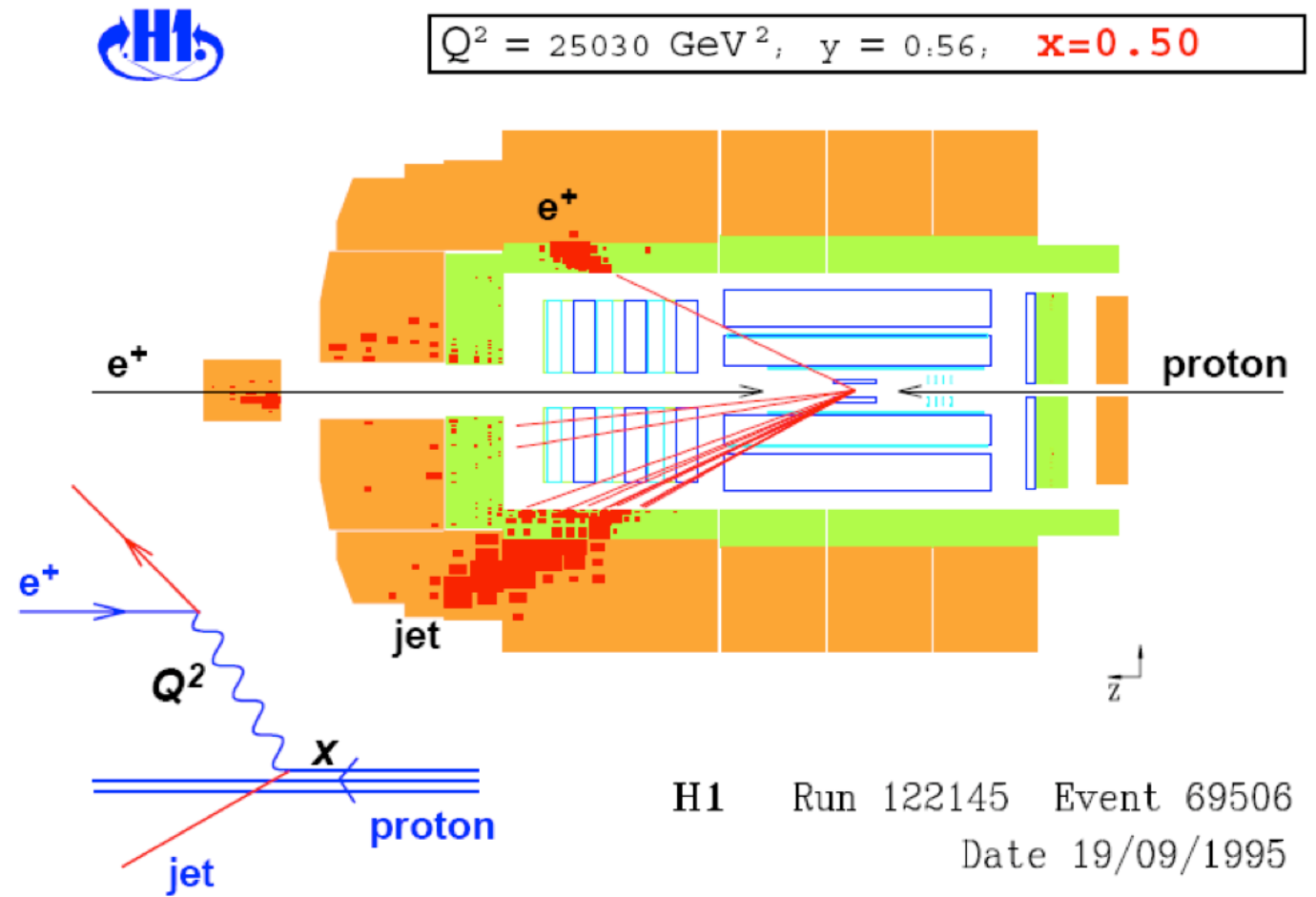
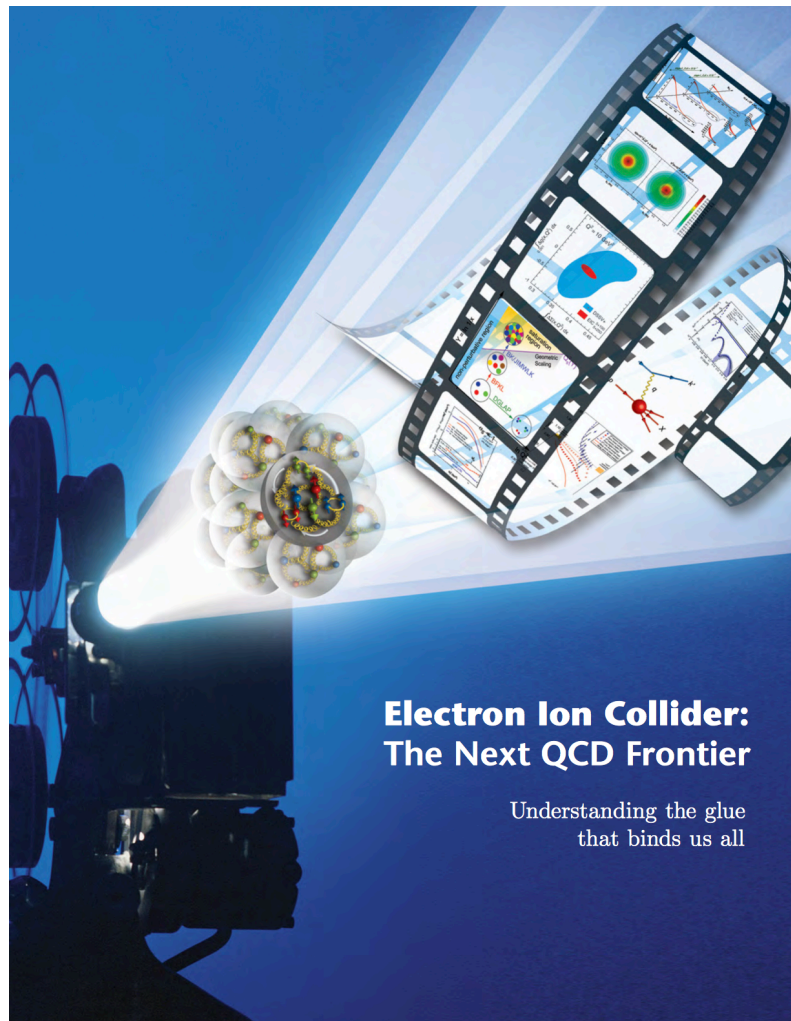
INT, Seattle, 10/17/18





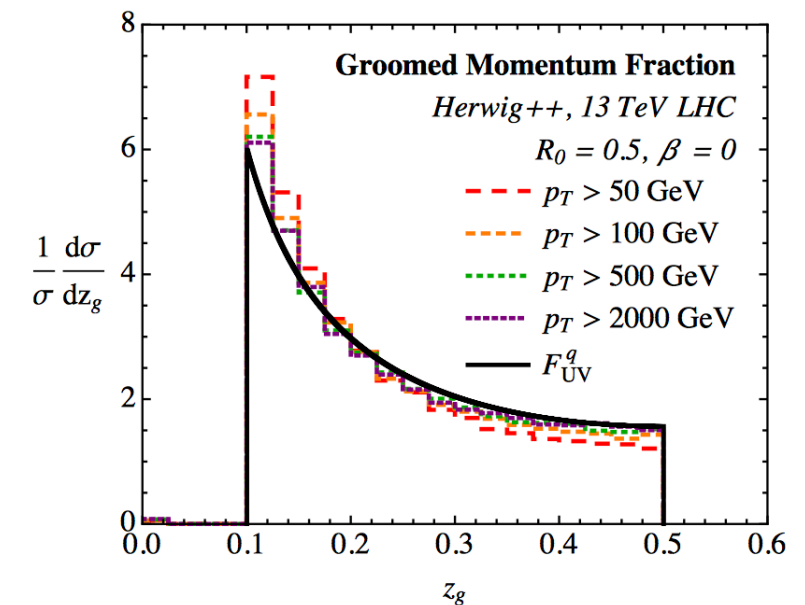
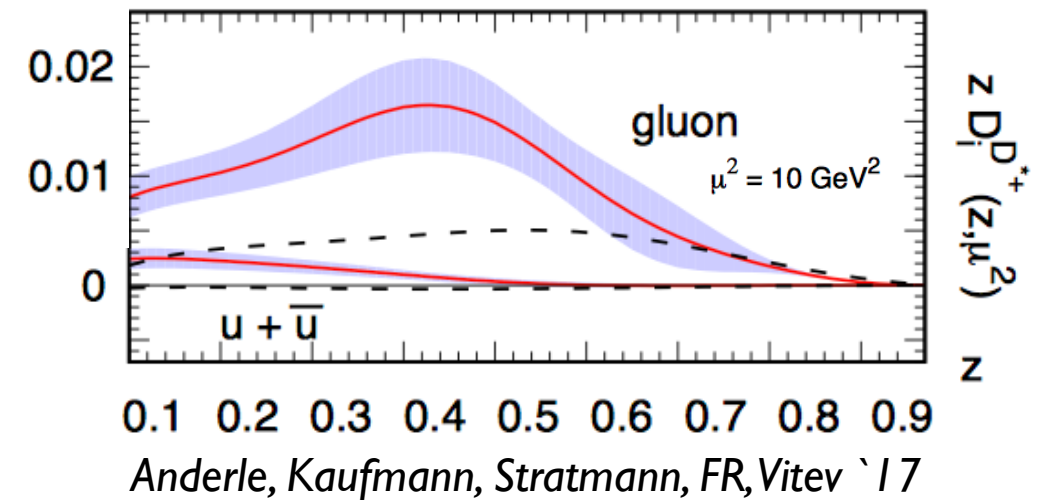
Jets and jet substructure at

- LEP, HERA
- Tevatron, RHIC, LHC
- EIC

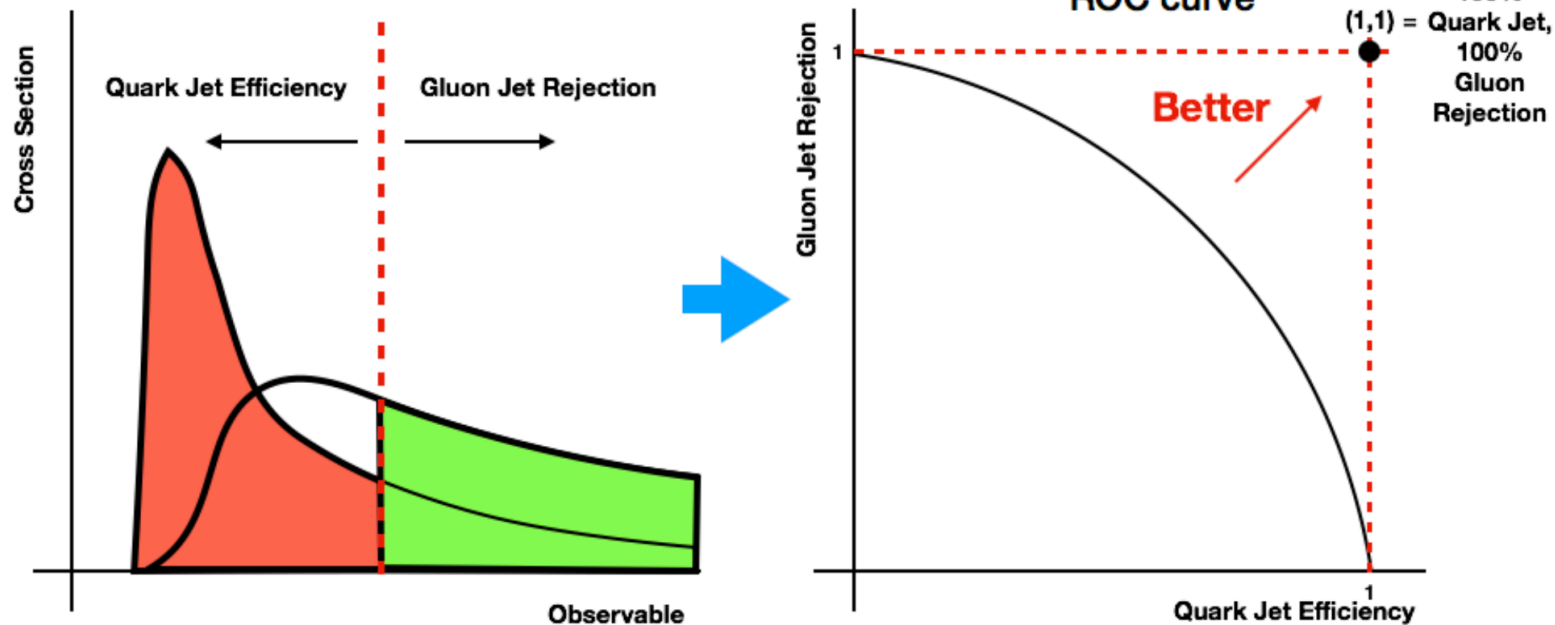


A few of recent examples:

- Quark/ gluon tagging using for example jet angularities
- Jet charge
- Hadron-in-jet distributions
- Possible extraction of α_s Les Houches '17
- Measurement of the QCD splitting function using Soft drop or subjets

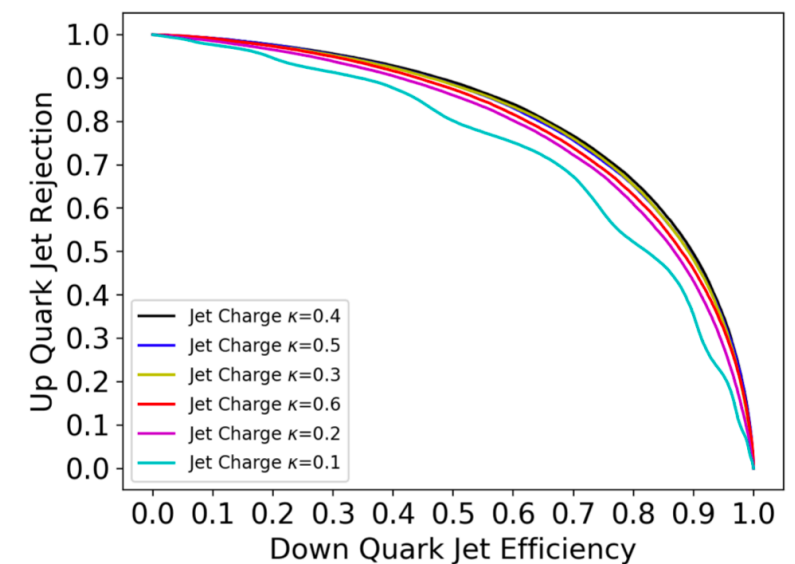


Larkoski, Marzani, Thaler '15



Kang, Lee, FR '18

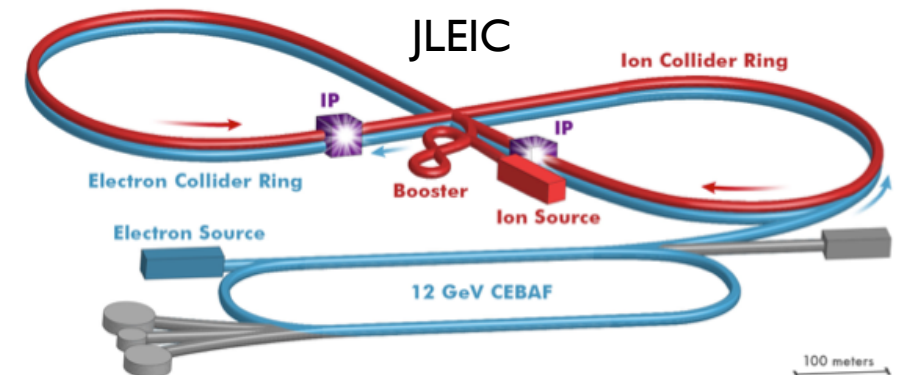
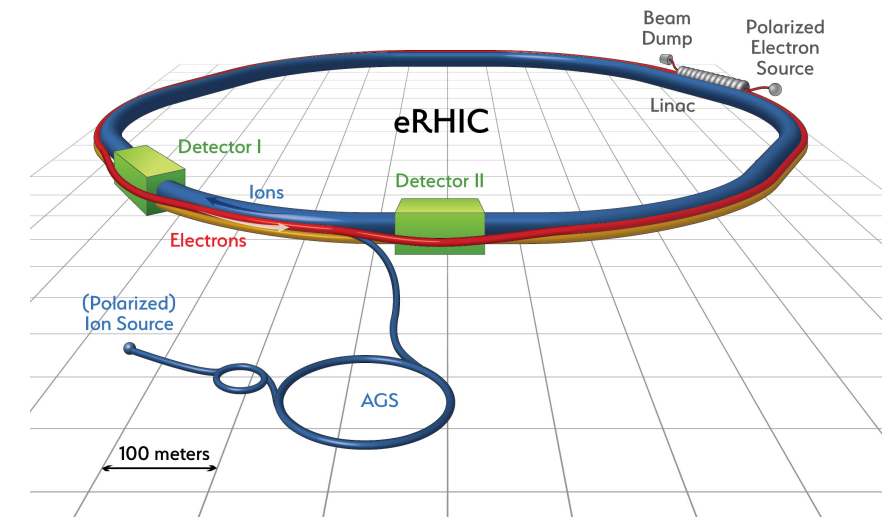
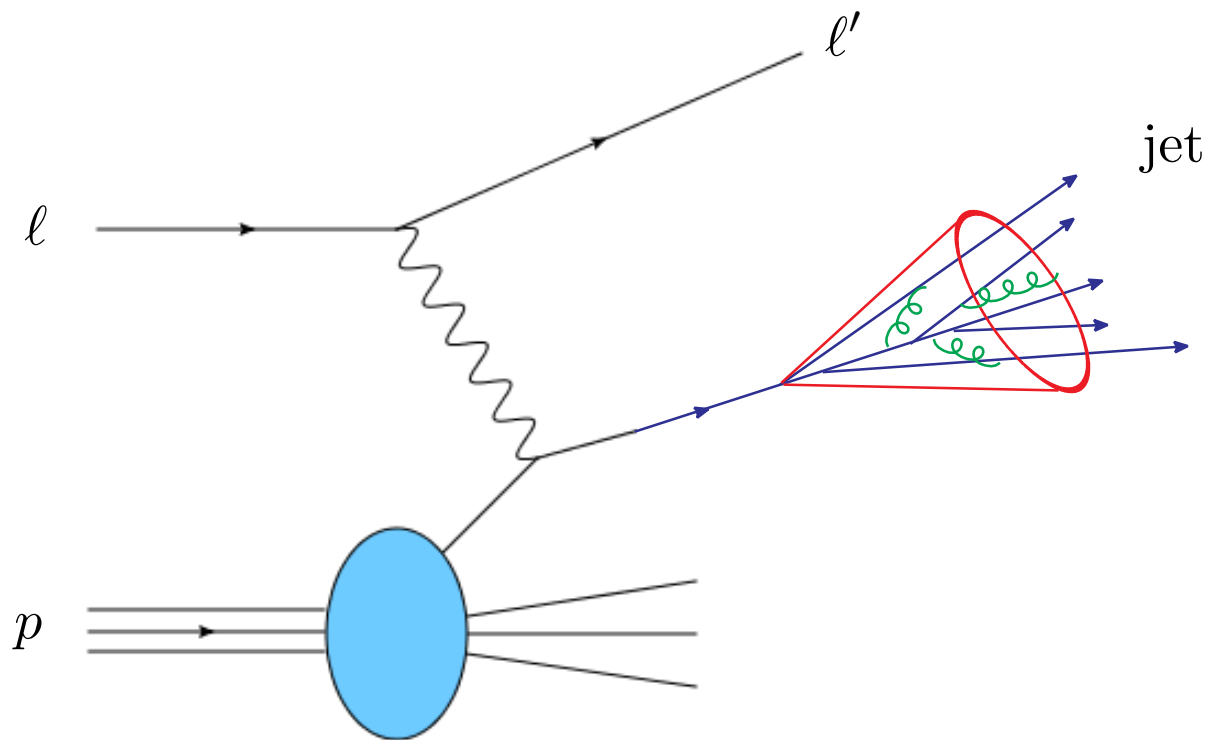
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Fraser, Schwartz '18

Jets at an EIC

- Jets are inherently interesting
- Constrain non-perturbative quantities
e.g. collinear and TMD (un)polarized PDFs



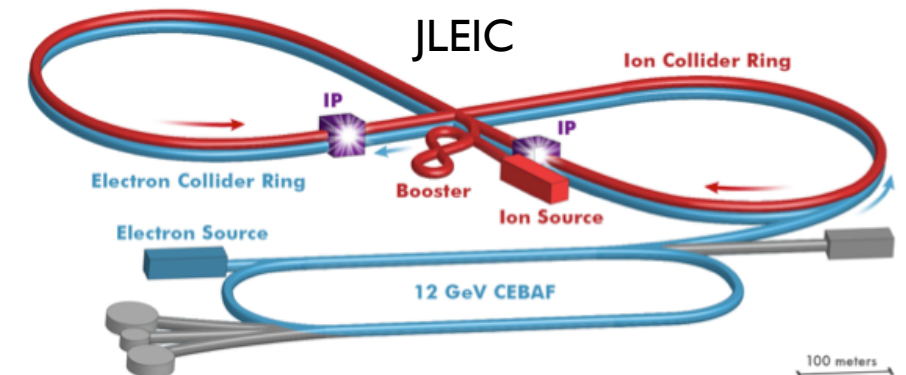
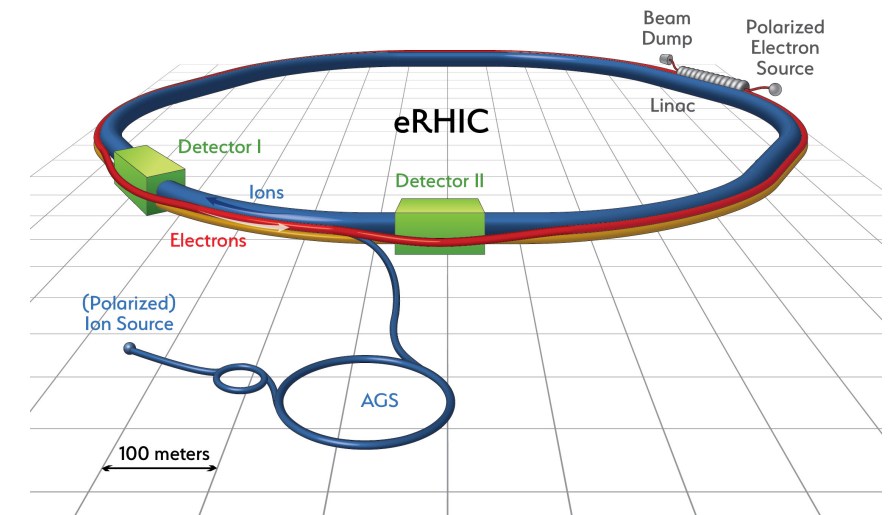
For recent work see for example: Schlegel, Hinderer, Vogelsang `15, Ablov, Boughezal, Liu, Petriello `16, Klasen, Kovarik `18, Currie, Gehrmann, Glover, Huss, Niehus, Vogt `18, Chu, Aschenauer, Lee, Zhang `17 ...

Jets at an EIC

- Jets are inherently interesting
- Constrain non-perturbative quantities
e.g. collinear and TMD (un)polarized PDFs
- No fragmentation functions required
- Complimentary to observables with identified hadrons
- Probe of nuclear matter effects in eA
- Can make use of new methods developed for the LHC and RHIC like jet substructure and tagging

Challenge: We have to understand the NP physics of jets

1. Validate with RHIC, HERA measurements or
2. Compare to MC simulations



Outline

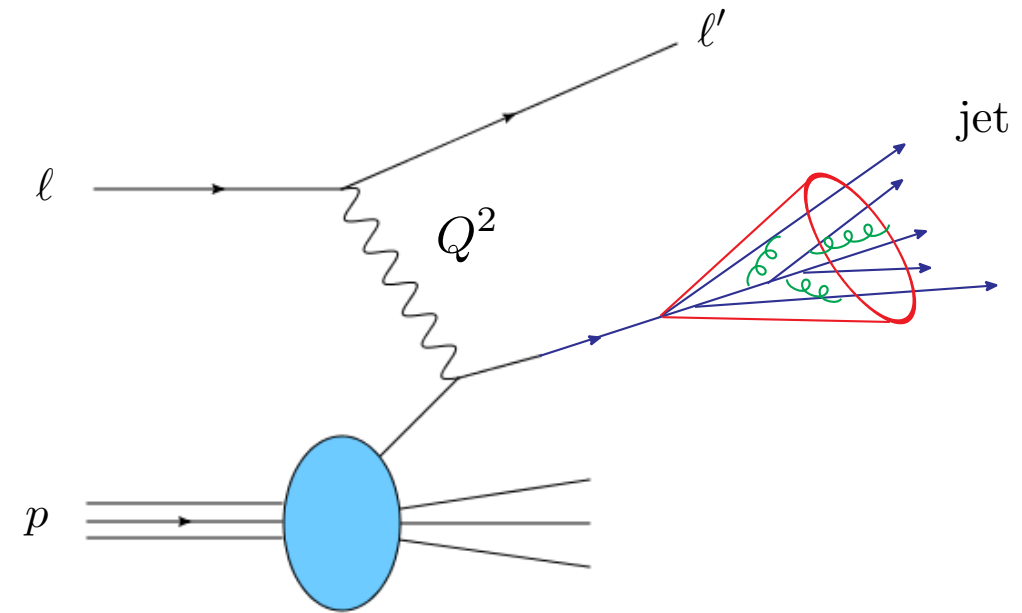
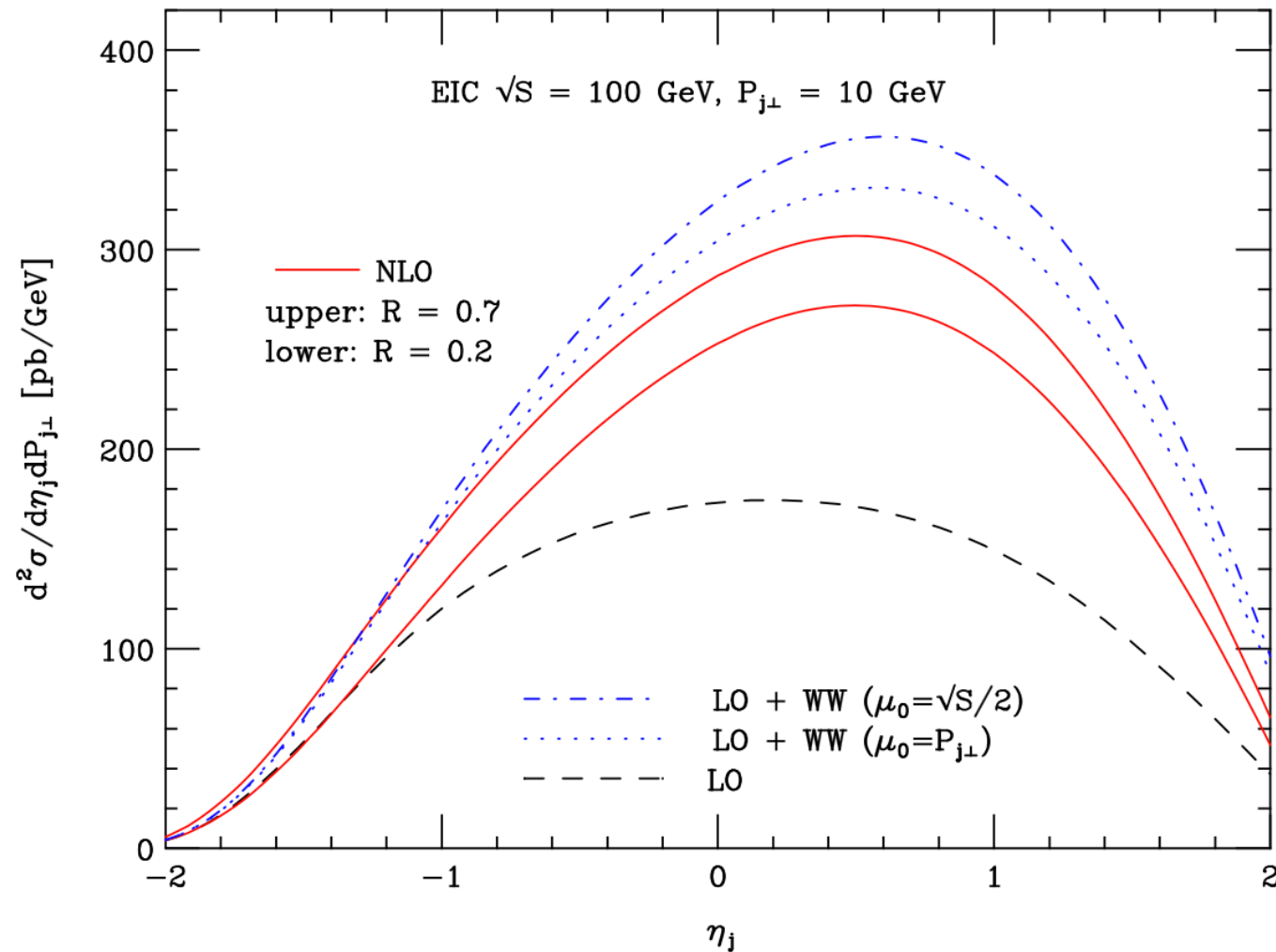
- Introduction
- Inclusive jets at the EIC
- Jet substructure
- Jet correlations
- Conclusions

Single inclusive jets at the EIC

- $pp \rightarrow \text{jet} + X$

Lepton unobserved, high p_T

$$\frac{d\sigma}{dp_T d\eta}$$



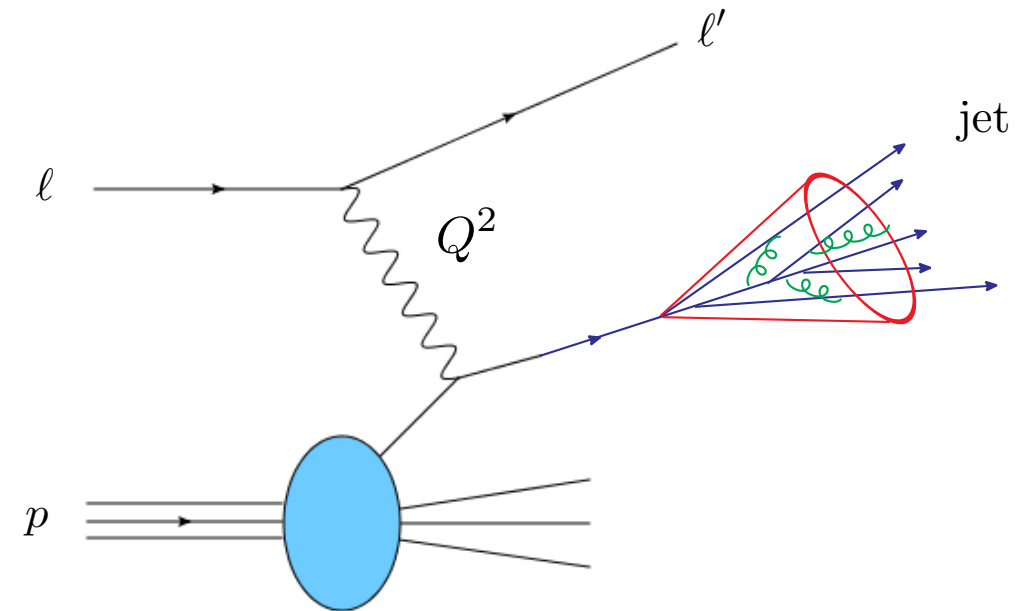
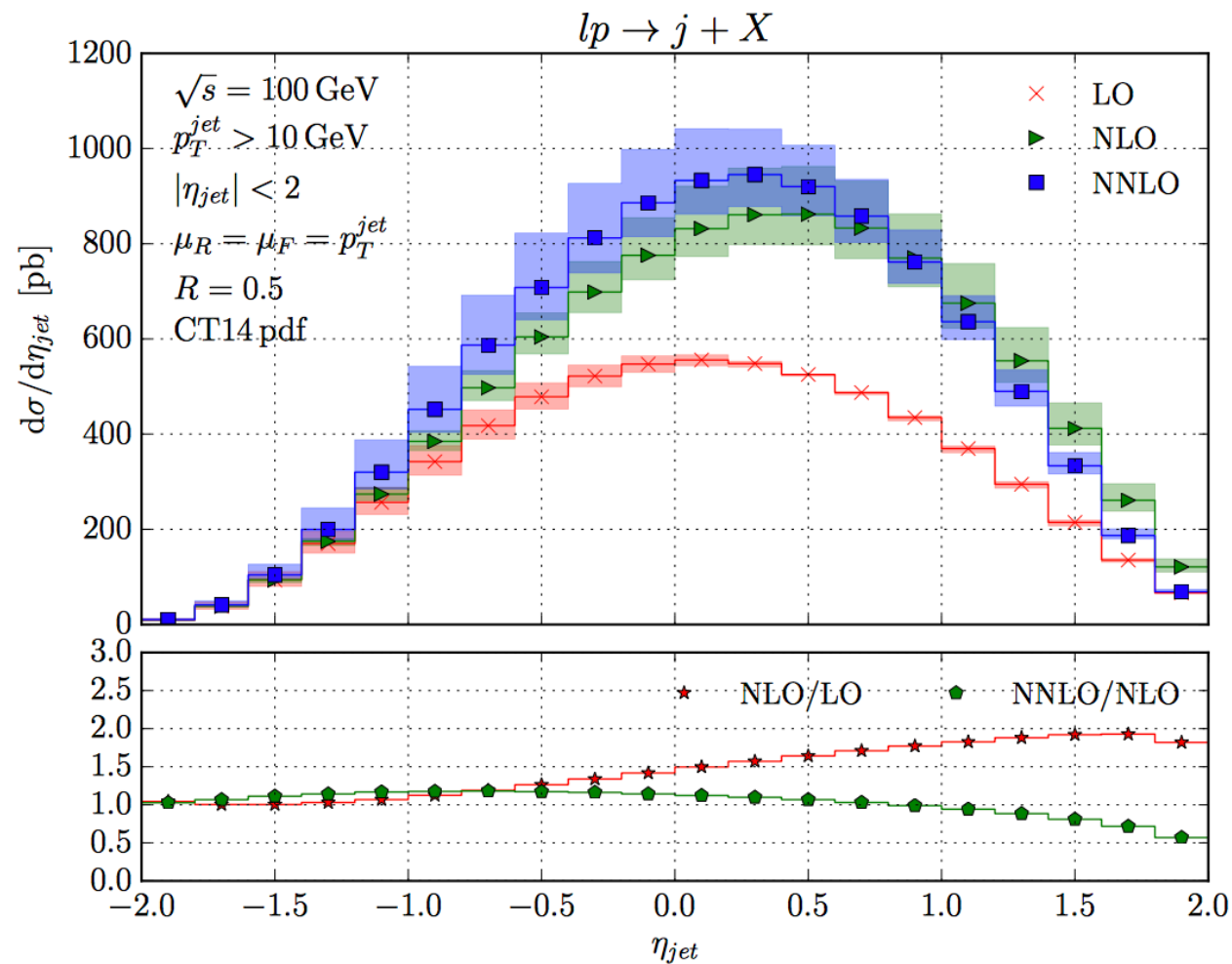
Schlegel, Hinderer, Vogelsang '15, '17,
Abelov, Boughezal, Liu, Petriello '16,
Boughezal, Petriello, Xing '18

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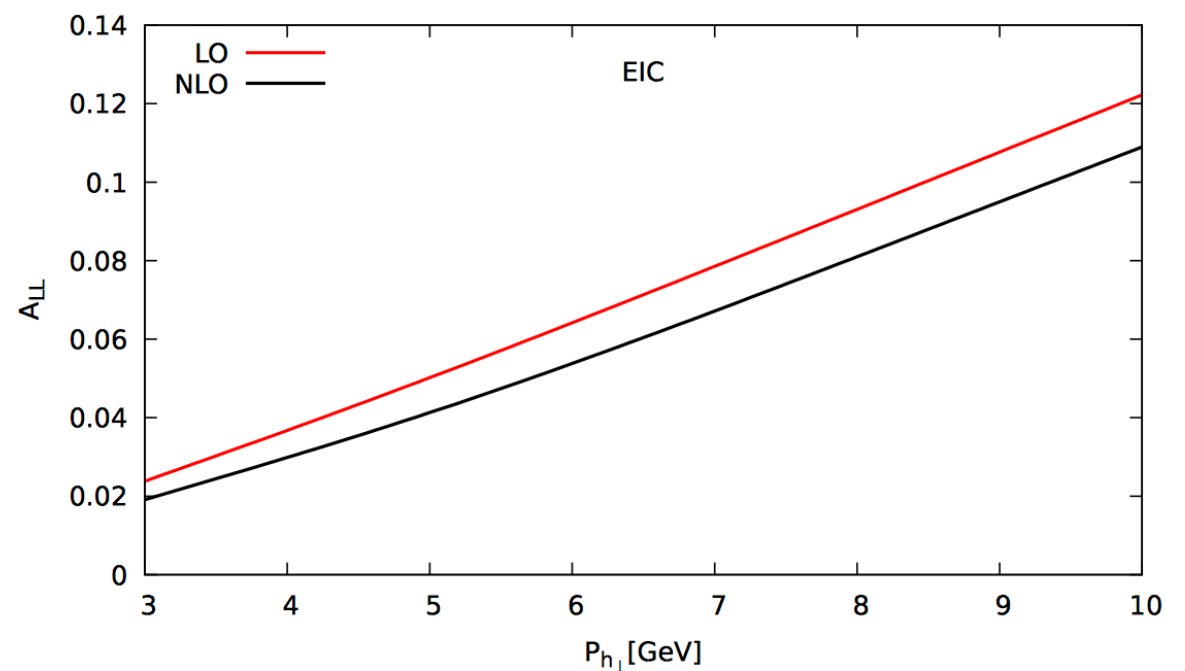
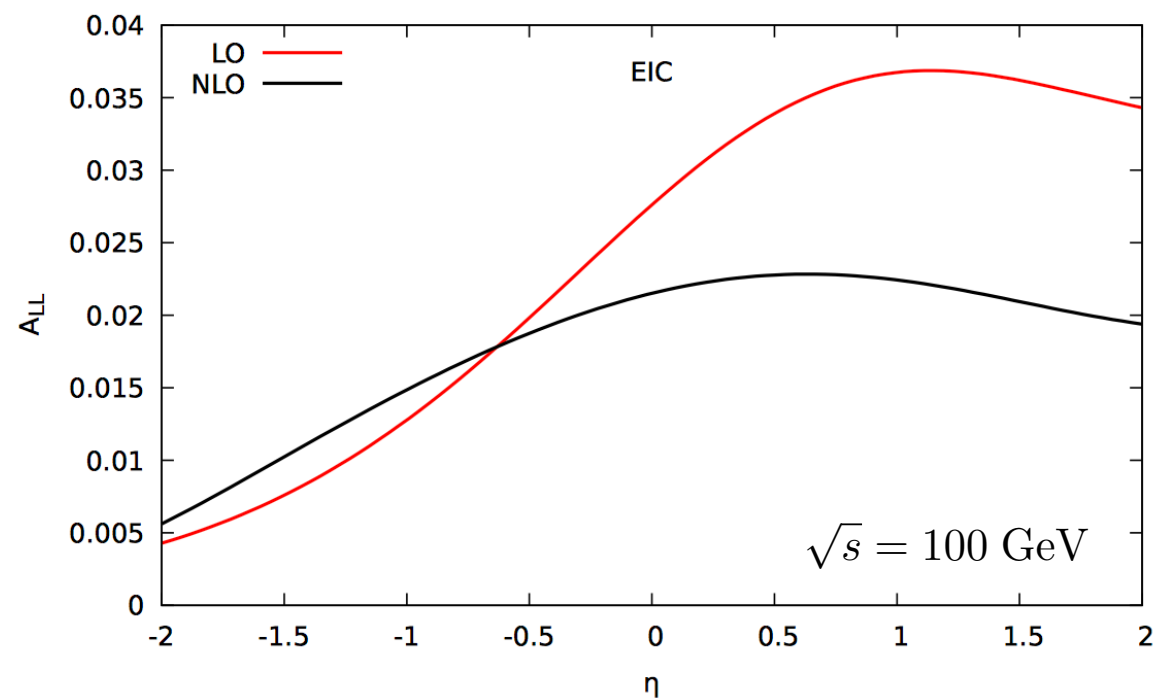
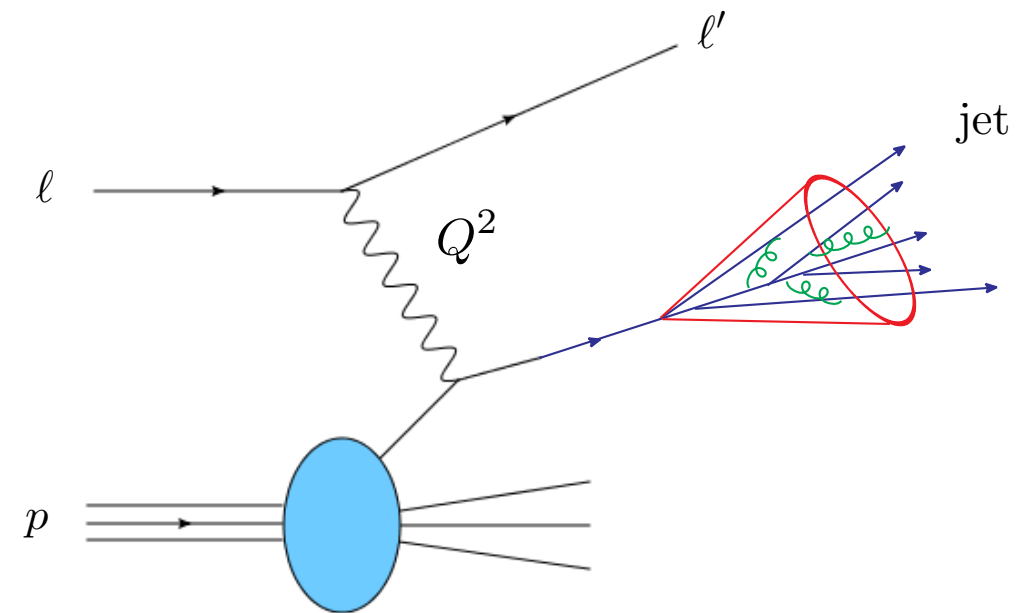
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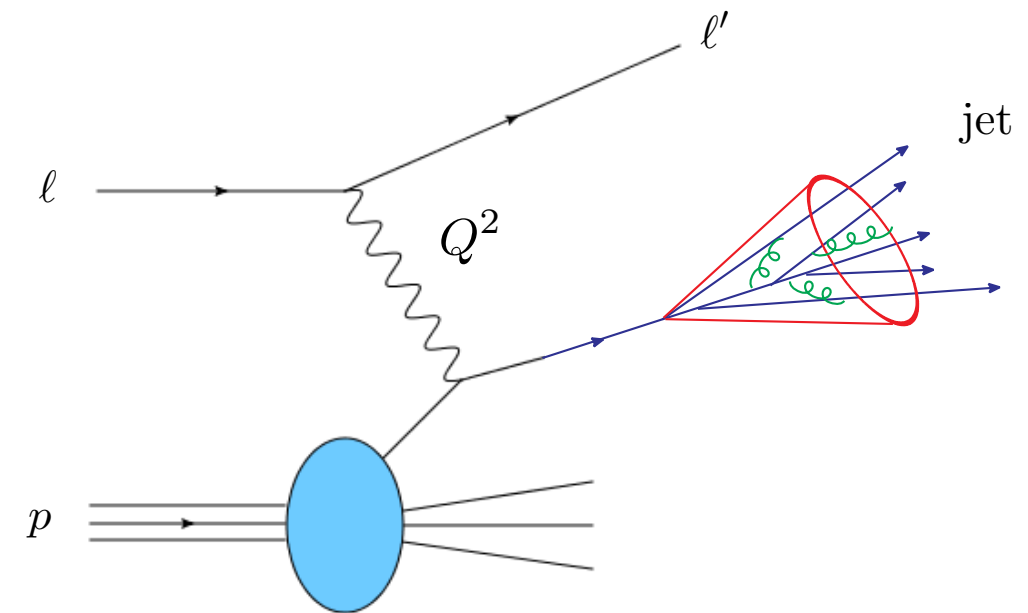
$$\frac{d\sigma}{dp_T d\eta}$$

- $pp \rightarrow \ell + \text{jet} + X$ DIS, high p_T, Q^2

$$\frac{d\sigma}{dp_T d\eta dQ^2}$$

- $pp \rightarrow \ell + \text{jet} + X$ Photoproduction, high $p_T, Q^2 < 0.1 \text{ GeV}^2$


$$\frac{d\sigma}{dp_T d\eta dQ^2}$$



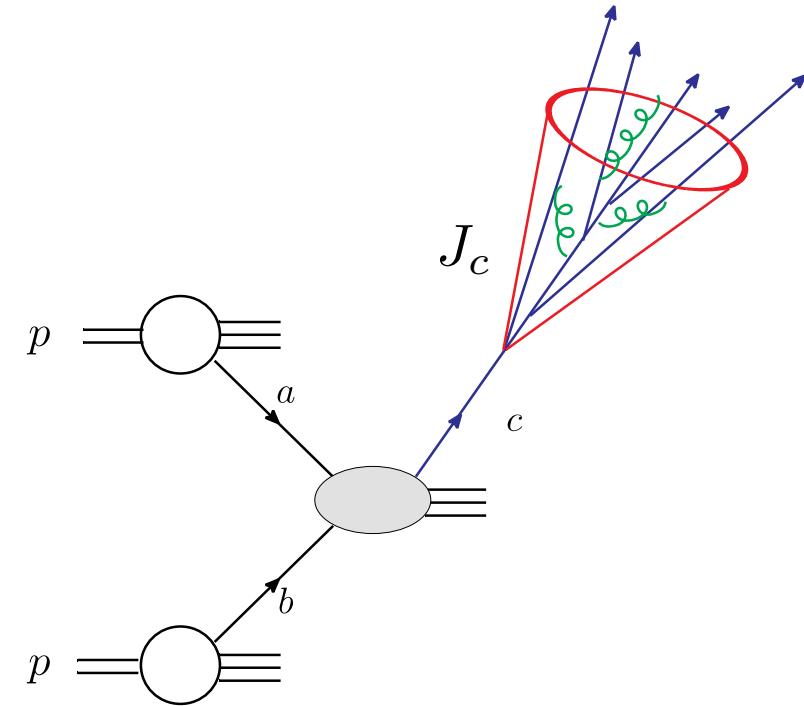
QCD factorization

- Inclusive jet production $pp \rightarrow \text{jet} + X$

$$\frac{d\sigma^{pp \rightarrow \text{jet} X}}{dp_T d\eta} = \sum_{a,b,c} f_a \otimes f_b \otimes H_{ab}^c \otimes J_c + \mathcal{O}(R^2)$$

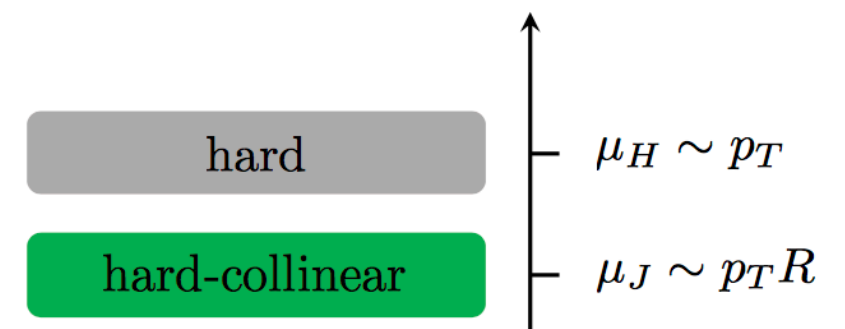


 perturbatively calculable



RG evolution of jet functions

$$\mu \frac{d}{d\mu} J_i = \sum_j P_{ji} \otimes J_j$$



Dasgupta, Dreyer, Salam, Soyez `15
 Kaufmann, Mukherjee, Vogelsang `15
 Kang, FR, Vitev `16
 Dai, Kim, Leibovich `16

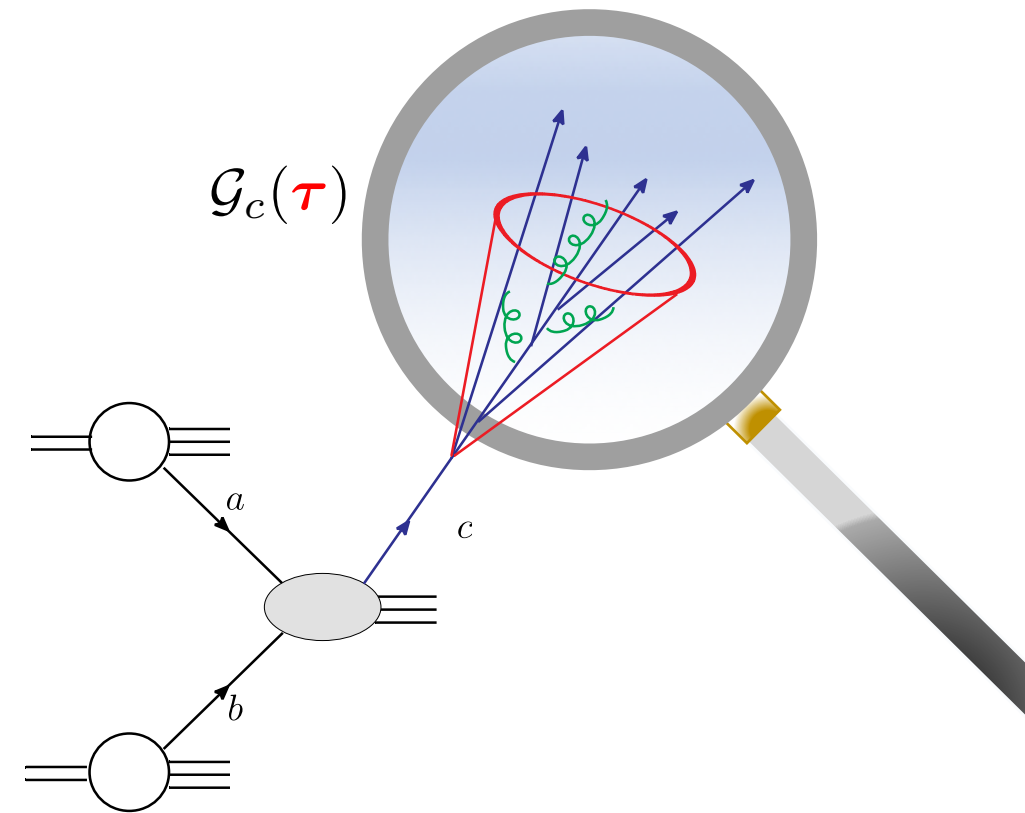
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- Jet substructure τ

$$\frac{d\sigma^{pp \rightarrow (\text{jet } \tau) X}}{dp_T d\eta d\tau} = \sum_{abc} f_a \otimes f_b \otimes H_{ab}^c \otimes \mathcal{G}_c(\tau) + \mathcal{O}(R^2)$$



Dasgupta, Dreyer, Salam, Soyez `15
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- Hard functions for lepton-proton scattering, e.g.

$$\frac{d\sigma^{\ell p \rightarrow \ell' \text{ jet} + X}}{dp_T d\eta dQ^2 d\tau}$$

- Photoproduction

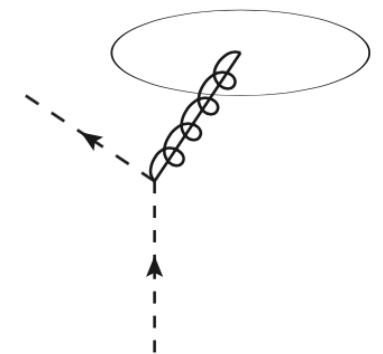
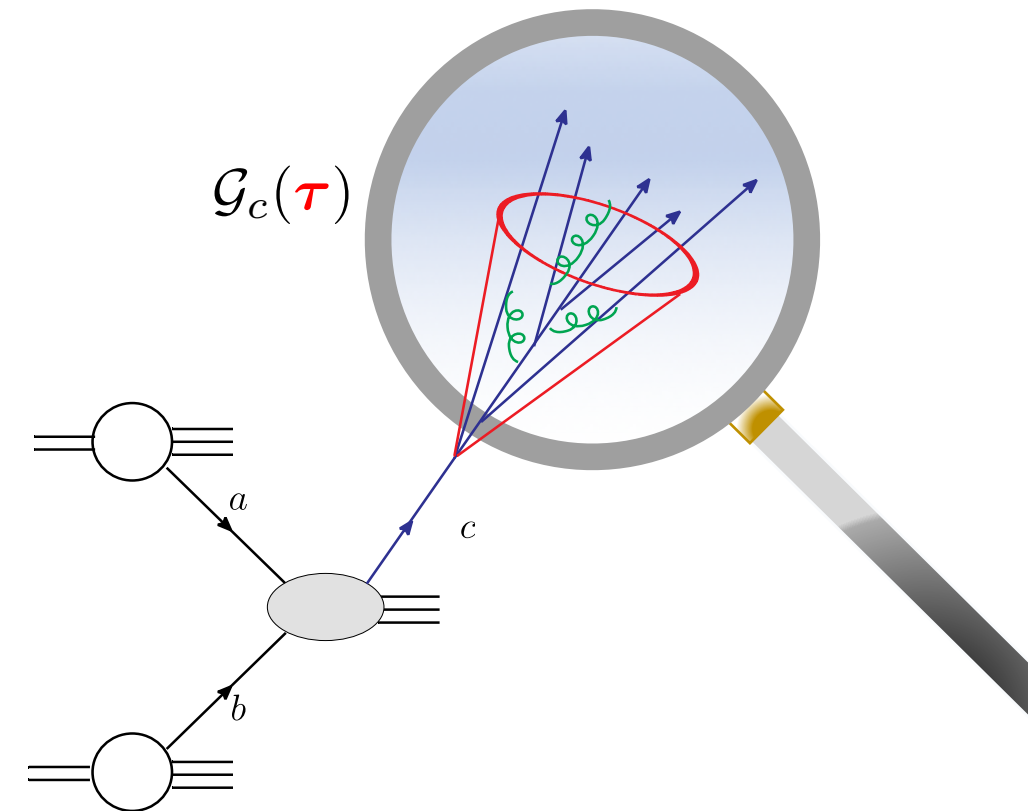
Jäger, Stratmann, Vogelsang '03

(unpolarized and polarized)

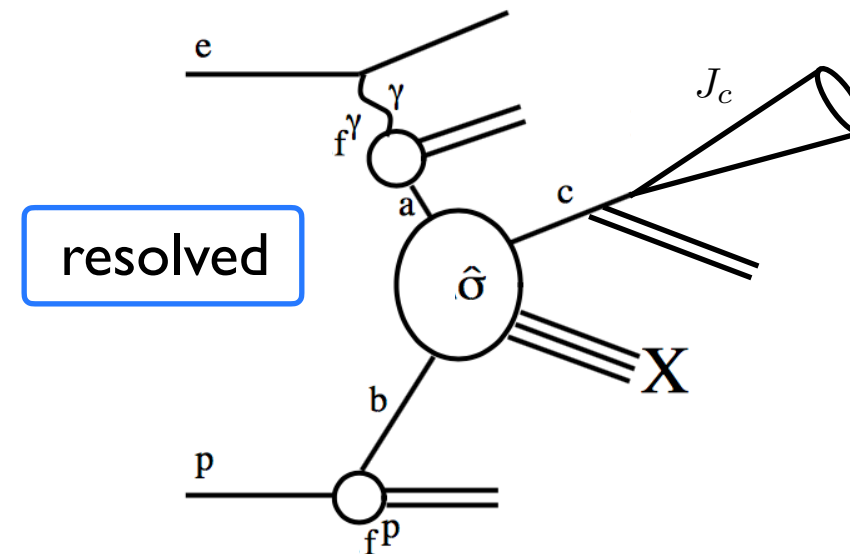
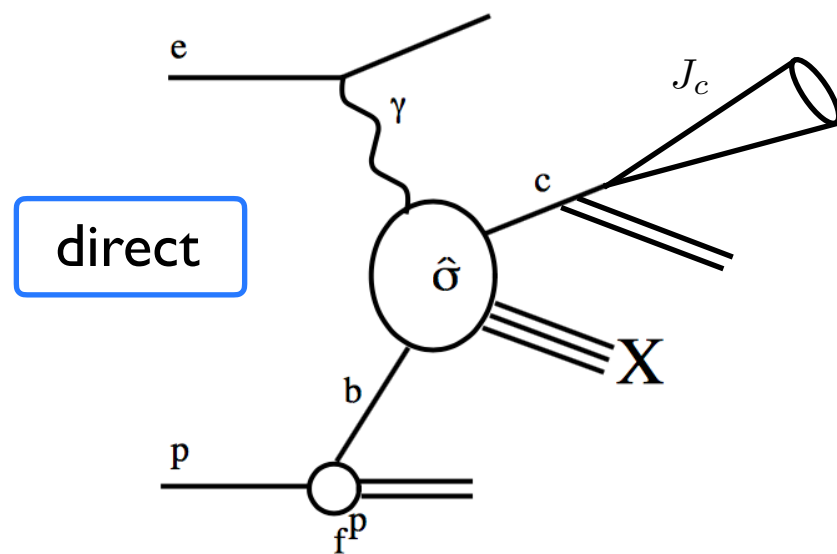
- DIS

Daleo, de Florian, Sassot '04,

Gonzalez-Hernandez, Rogers, Sato, Wang '18



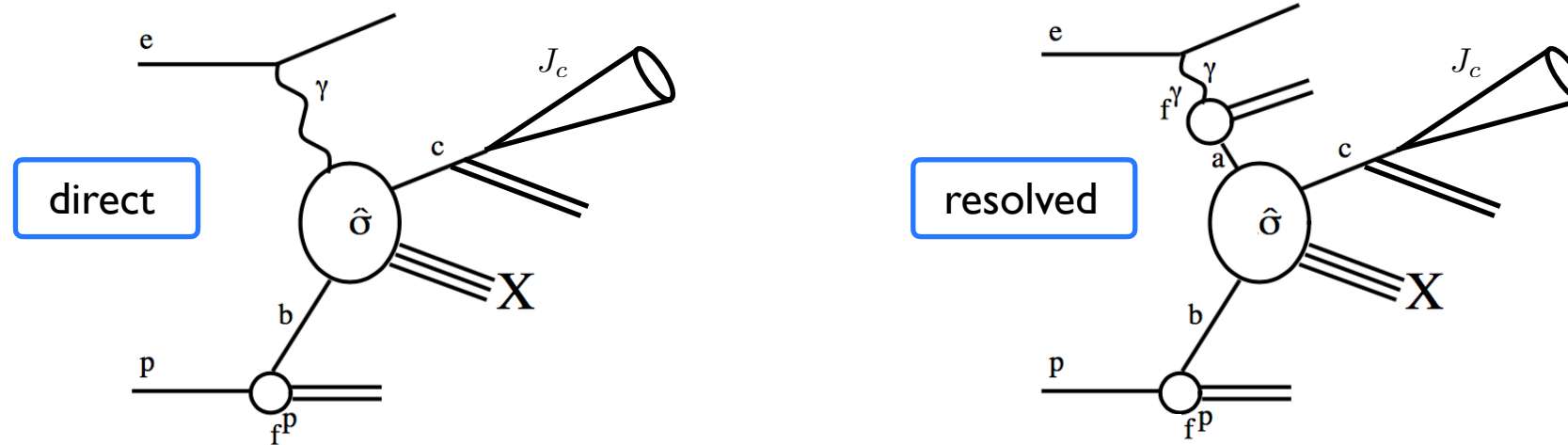
Photoproduction at the EIC



- Require high p_T and $Q^2 < 0.1 \text{ GeV}^2$
- Access the parton content of (polarized) photons

Jäger, Stratmann, Vogelsang `03
 de Florian, Pфеuffer, Schäfer, Vogelsang `13
 Chu, Aschenauer, Lee, Zhang `17

Photoproduction at the EIC



- Inclusive jets

$$\frac{d\sigma}{dp_T d\eta dQ^2} = \sum_{a,b,c} f_{a/l} \otimes f_{b/p} \otimes H_{ab}^c \otimes J_c$$

Weizsäcker-Williams spectrum
resolved: $\otimes f_{a/\gamma}$

- Jet mass

$$\frac{d\sigma}{dp_T d\eta dQ^2 dm_J} = \sum_{a,b,c} f_{a/l} \otimes f_{b/p} \otimes H_{ab}^c \otimes \mathcal{G}_c(m_J)$$

hard

$$\mu_H \sim p_T$$

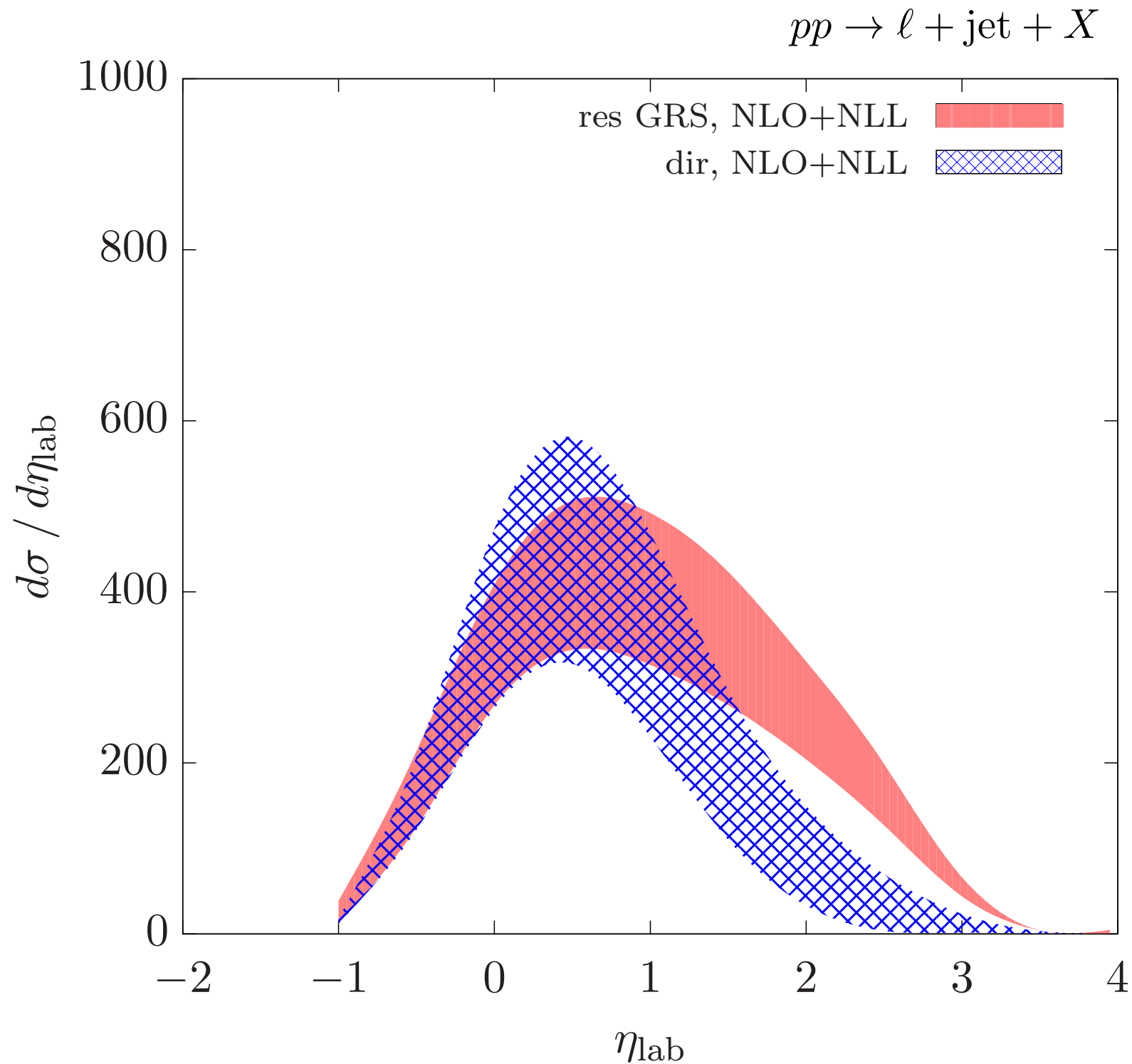
hard-collinear

$$\mu_J \sim p_T R$$

Jäger, Stratmann, Vogelsang '03
Chu, Aschenauer, Lee, Zhang '17

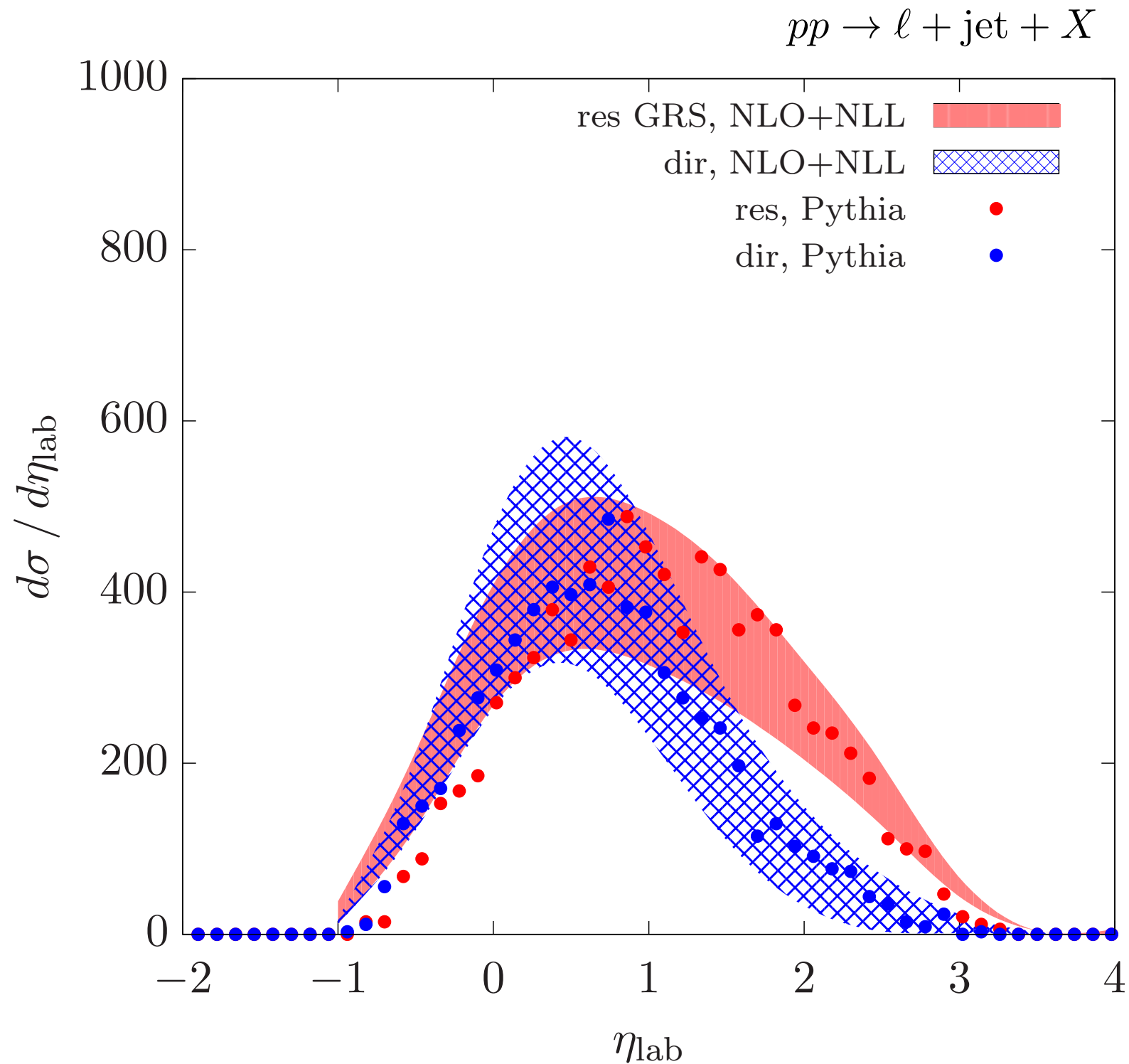
Phenomenology

$\sqrt{s} = 141 \text{ GeV}$
 $R = 0.8$
 $p_T > 10 \text{ GeV}$
 $Q^2 < 0.1 \text{ GeV}^2$
 $E_e = 20 \text{ GeV}$
 $E_p = 250 \text{ GeV}$



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Cold nuclear matter effects in eA

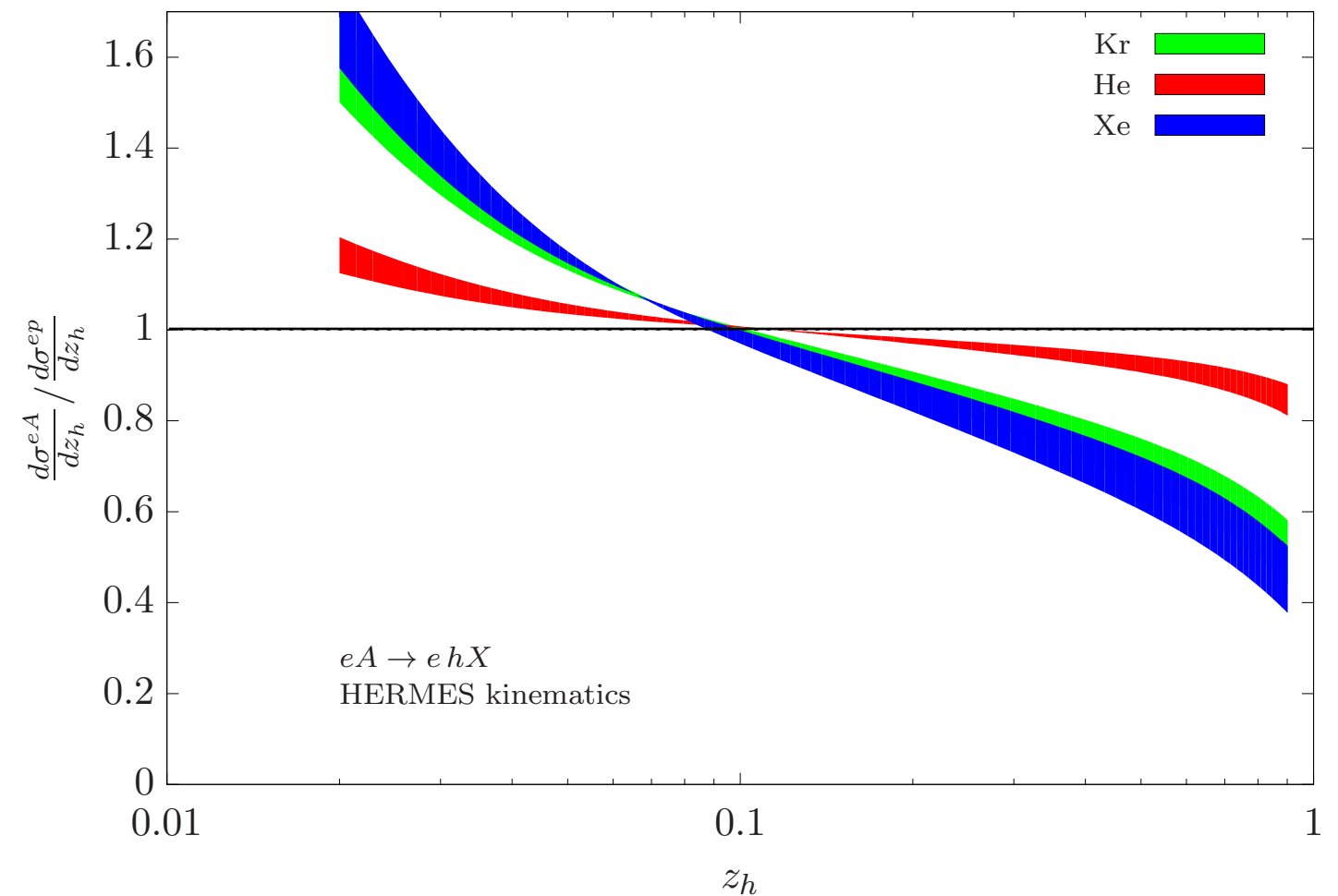
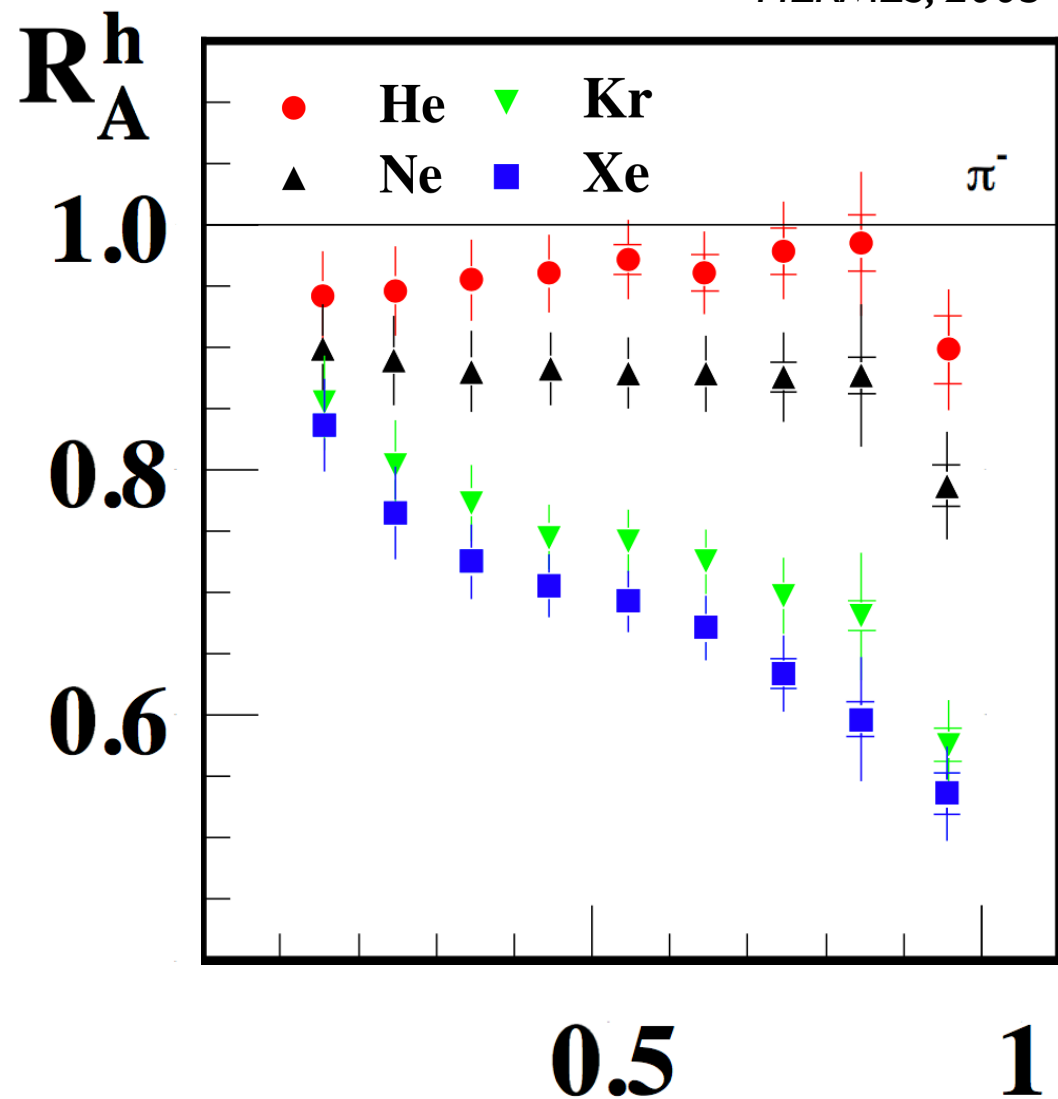
FR, Sato, Vitev - in preparation

- Hadron multiplicity ratios $d\sigma/dz_h$
- SIDIS

$$Q^2 > 1 \text{ GeV}^2 \quad \nu < 23 \text{ GeV}$$

$$W^2 > 10 \text{ GeV}^2$$

HERMES, 2003



Constrain medium input and extrapolate
to jets at the EIC

$$D_i^h(z_h) \rightarrow D_i^{\text{med},h}(z_h)$$

Z

Outline

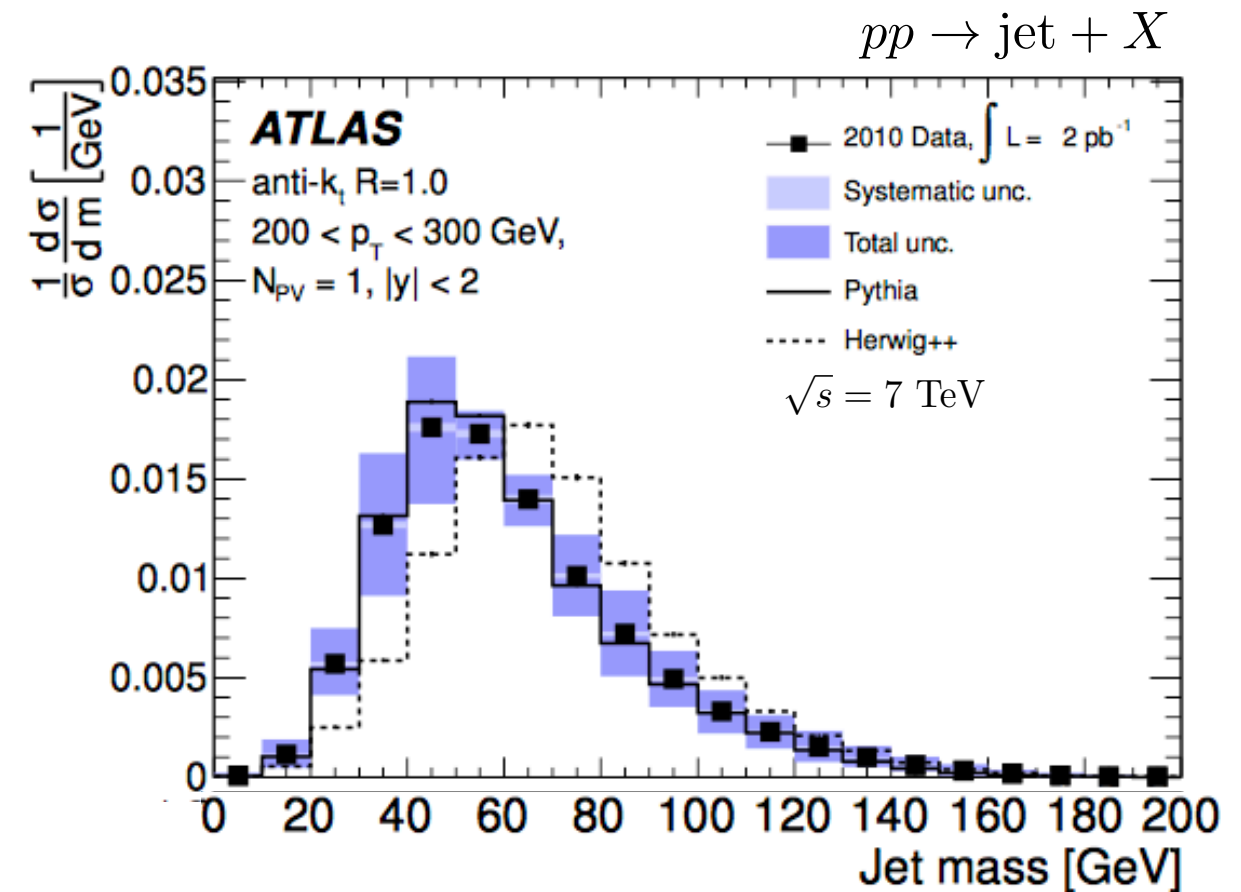
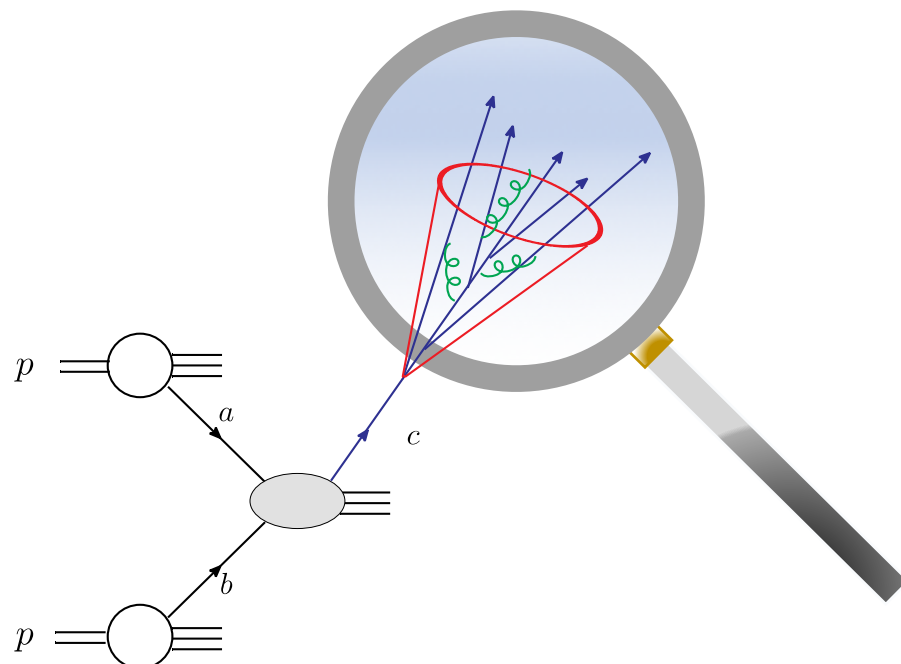
- Introduction
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- Jet substructure
- Jet correlations
- Conclusions

The jet mass at the LHC

Kang, Lee, FR '18,
Kang, Lee, Liu, FR '18

- Jet mass $m_J^2 = \left(\sum_{i \in J} p_i \right)^2$ for inclusive jet production $pp \rightarrow (\text{jet } m_J^2) X$
- Quark-gluon discrimination
- NP contribution:
 - Multi parton interactions (MPI)
 - Hadronization
 - Pileup
- Including soft drop: α_s extraction possible

Les Houches '17



ATLAS, JHEP 1205 (2012) 128

see also: Li, Li, Yuan '11,
Dasgupta, Khelifa-Kerfa, Marzani, Spannowsky '12, ...

Factorization

- Hard-collinear factorization $R \ll 1$

$$\frac{d\sigma}{d\eta dp_T d\tau} = \sum_{abc} f_a(x_a, \mu) \otimes f_b(x_b, \mu) \otimes H_{ab}^c(x_a, x_b, \eta, p_T/z, \mu) \otimes \mathcal{G}_c(z, p_T, R, \tau, \mu)$$

Kang, Lee, FR '18,
Kang, Lee, Liu, FR '18

$$\tau = \frac{m_J^2}{p_T^2}$$

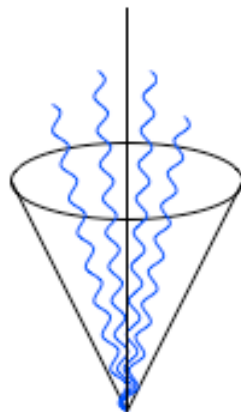
- Hard-collinear-soft factorization $\tau \ll R^2$

$$\mathcal{G}_c(z, p_T, R, \tau, \mu) = \sum_i \mathcal{H}_{c \rightarrow i}(z, p_T R, \mu) C_i(\tau, p_T, \mu) \otimes S_i(\tau, p_T, R, \mu)$$

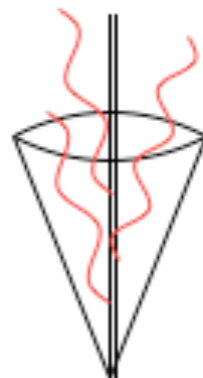
$pp \rightarrow (\text{jet } m_J^2) X$

hard-matching

collinear



soft



1st step
hard-collinear

2nd step
soft-collinear

$H_{ab}^c(p_T)$

$\mathcal{G}_c(p_T, R, \tau)$

$\mathcal{H}_{c \rightarrow i}(p_T R)$

$C_i(\tau)$

$S_i(\tau)$

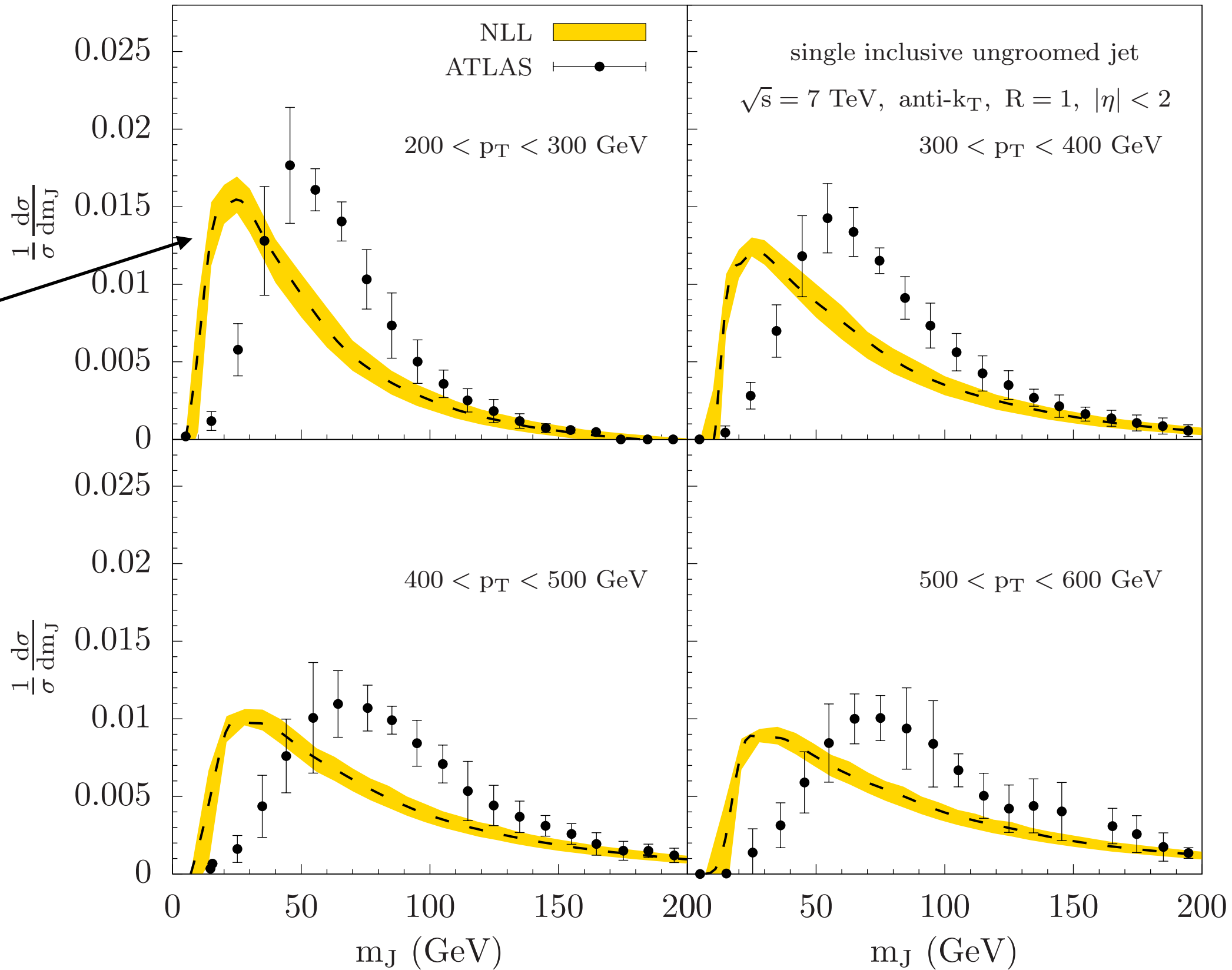
$\mu_H \sim p_T$

$\mu_J \sim p_T R$

$\mu_C \sim p_T \tau^{\frac{1}{2}}$

$\mu_S \sim \frac{p_T \tau}{R}$

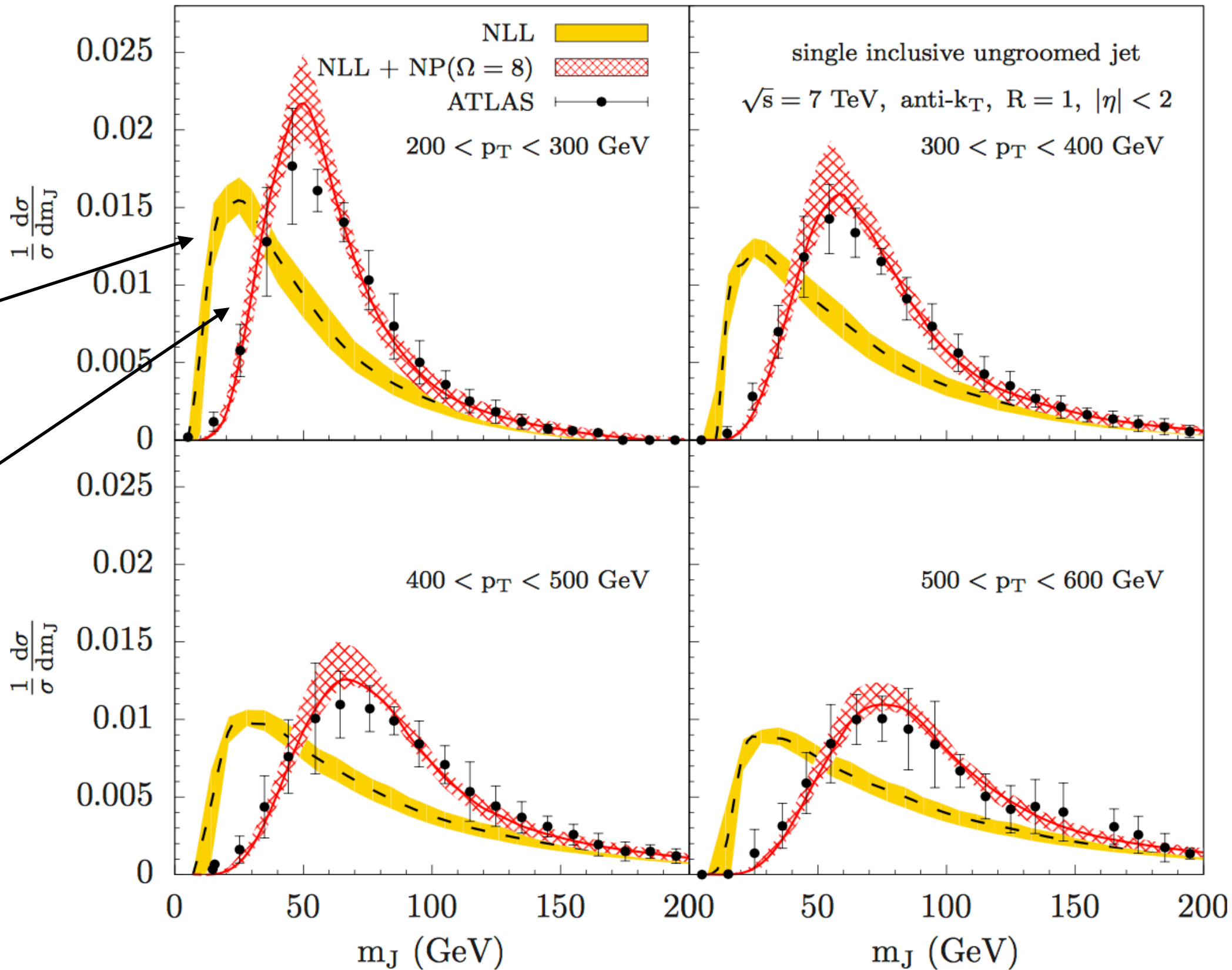
$pp \rightarrow (\text{jet } m_J^2) X$

 Perturbative result
 


$$pp \rightarrow (\text{jet } m_J^2) X$$

Perturbative result

Including $d\sigma^{\text{pert}} \otimes F$
NP shape function



$$F_i(k) = \frac{4k}{\Omega^2} \exp(-2k/\Omega)$$

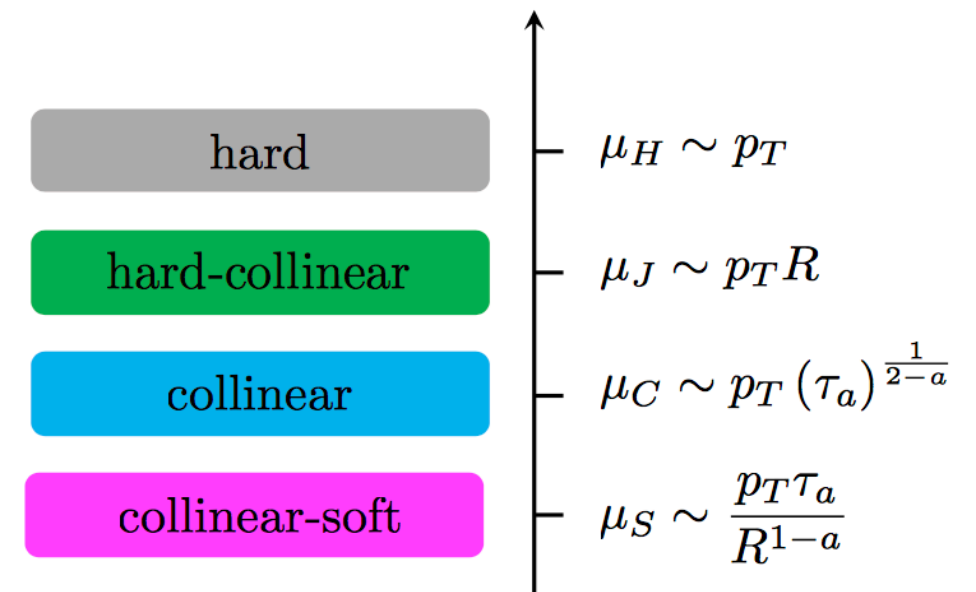
Stewart, Tackmann, Waalewijn '15

Jet angularities

Berger, Kucs, Sterman '03,
Ellis, Vermilion, Walsh, Hornig, Lee '10,
Hornig, Makris, Mehen '16,
Kang, Lee, FR '18

- Family of observables with a continuous parameter a
- Jet mass ($a = 0$), jet broadening ($a = 1$)
- Dependence on jet axis: standard, recoil free
- Event shape type of observables

$$\tau_a = \frac{1}{p_T} \sum_{i \in J} p_{Ti} \Delta R_{iJ}^{2-a}$$

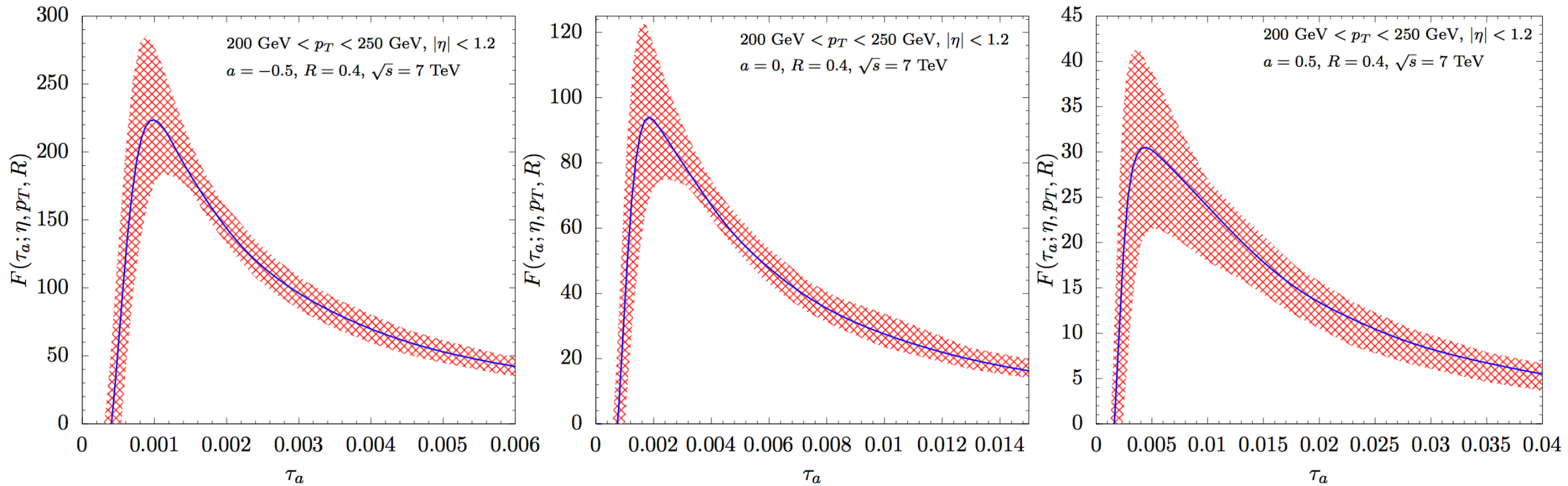


- Factorization $\tau_a^{1/(2-a)} \ll R$

$$\mathcal{G}_c(z, p_T, R, \tau_a, \mu) = \sum_i \mathcal{H}_{c \rightarrow i}(z, p_T R, \mu) C_i(\tau_a, p_T, \mu) \otimes S_i(\tau_a, p_T, R, \mu)$$

Jet angularities

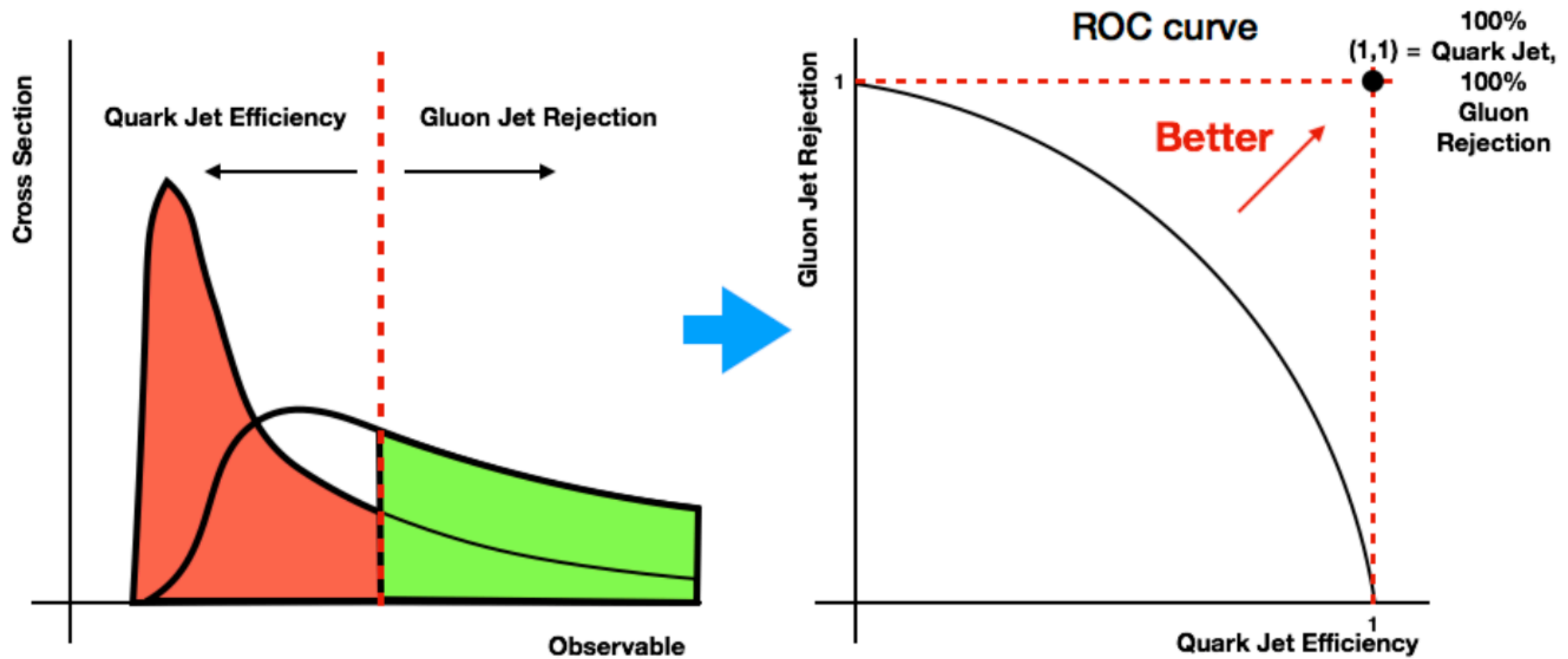
Kang, Lee, FR '18



$$F(\tau_a; \eta, p_T, R) = \frac{d\sigma^{pp \rightarrow (\text{jet } \tau_a) X}}{d\eta dp_T d\tau_a} \bigg/ \frac{d\sigma^{pp \rightarrow \text{jet} X}}{d\eta dp_T}$$

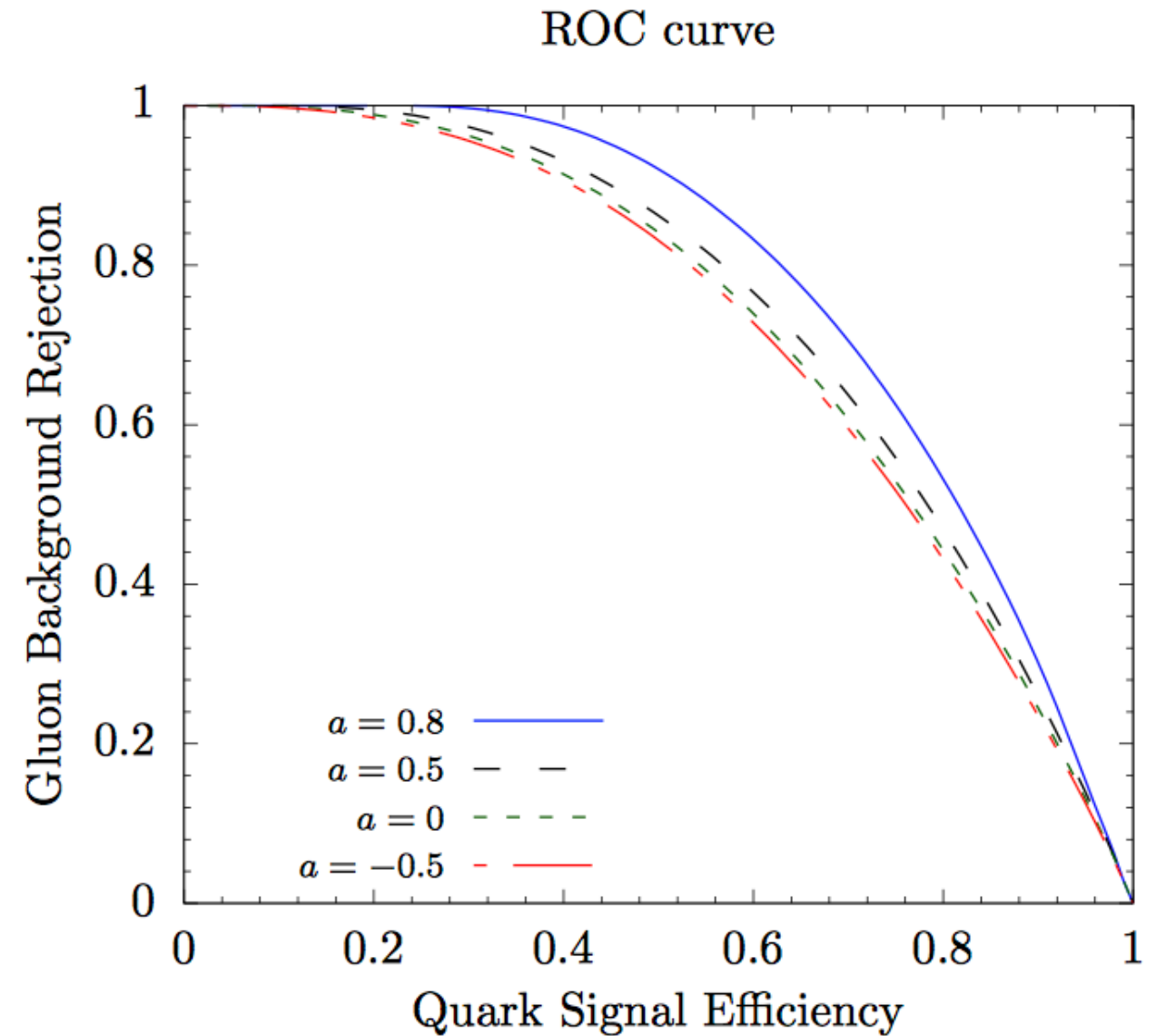
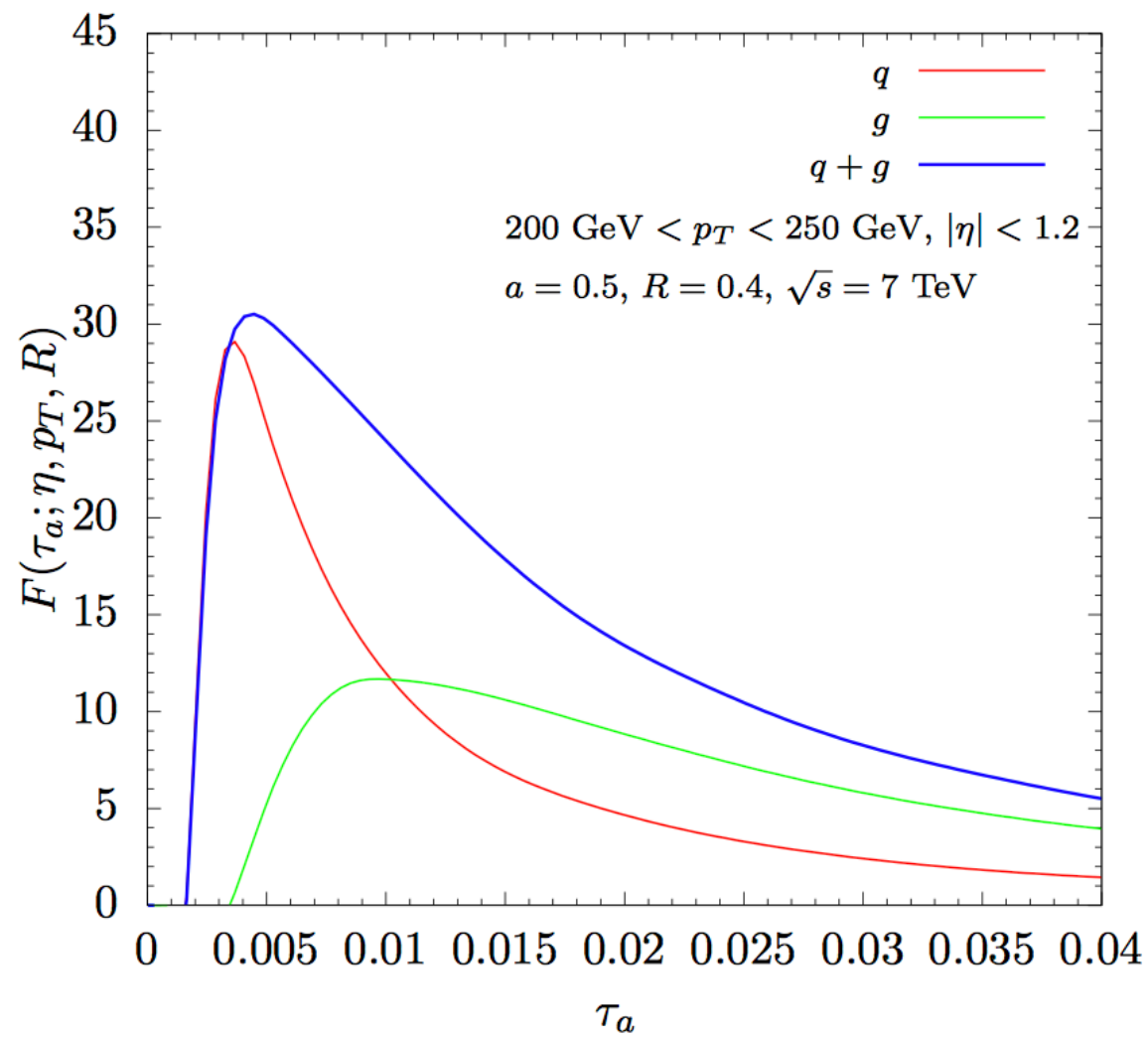
Quark-gluon discrimination

Kang, Lee, FR '18

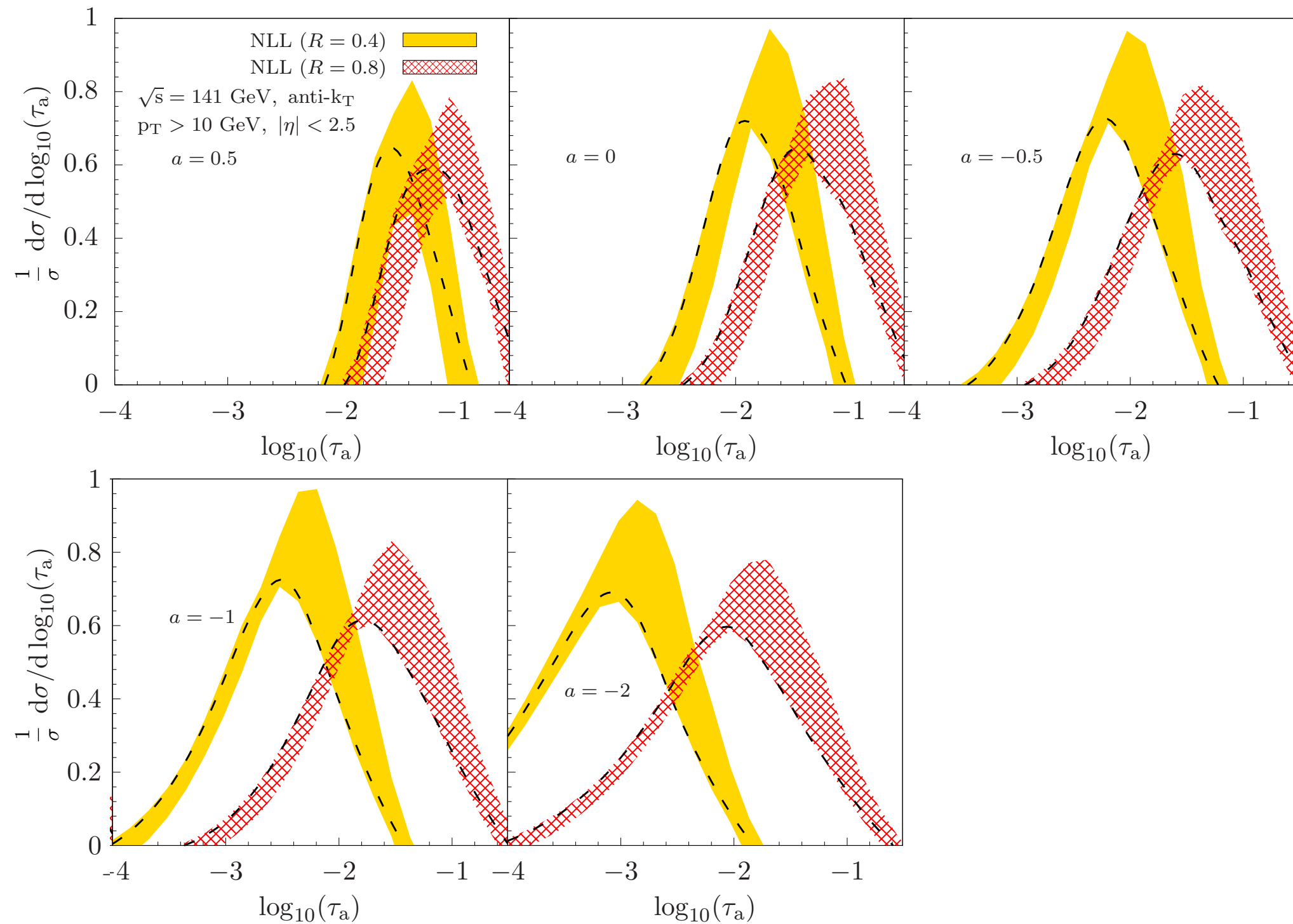


Quark-gluon discrimination

Kang, Lee, FR '18

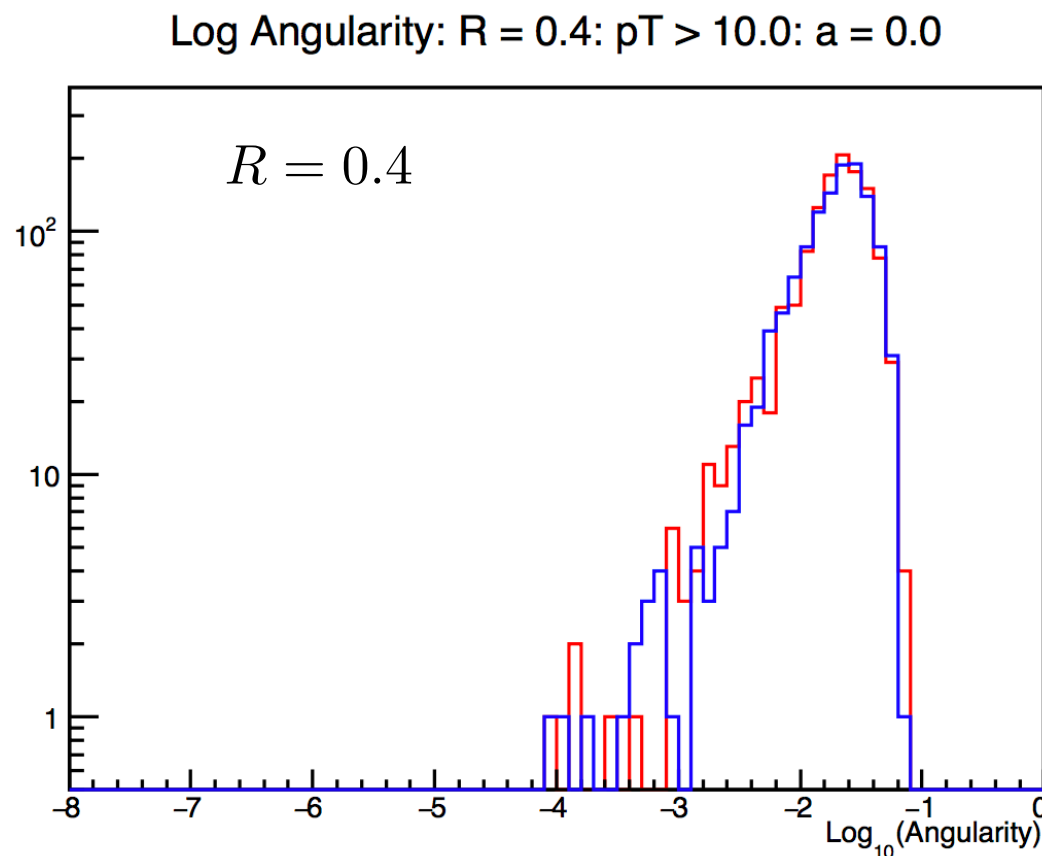
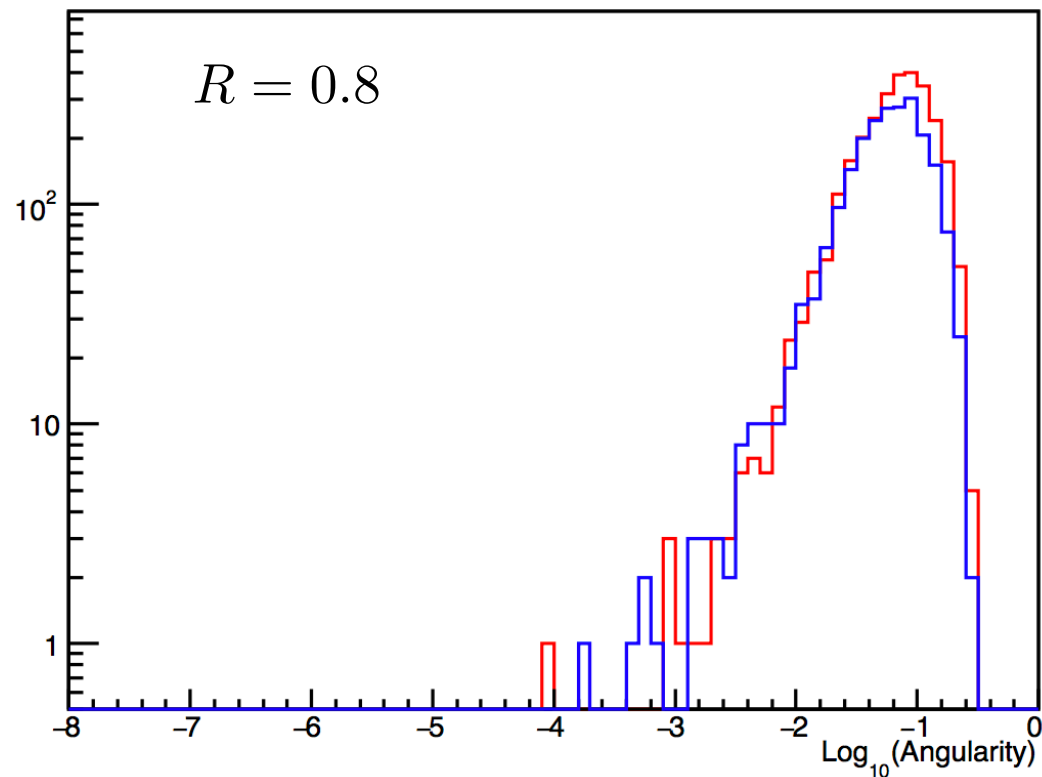



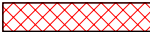
Photoproduction at the EIC

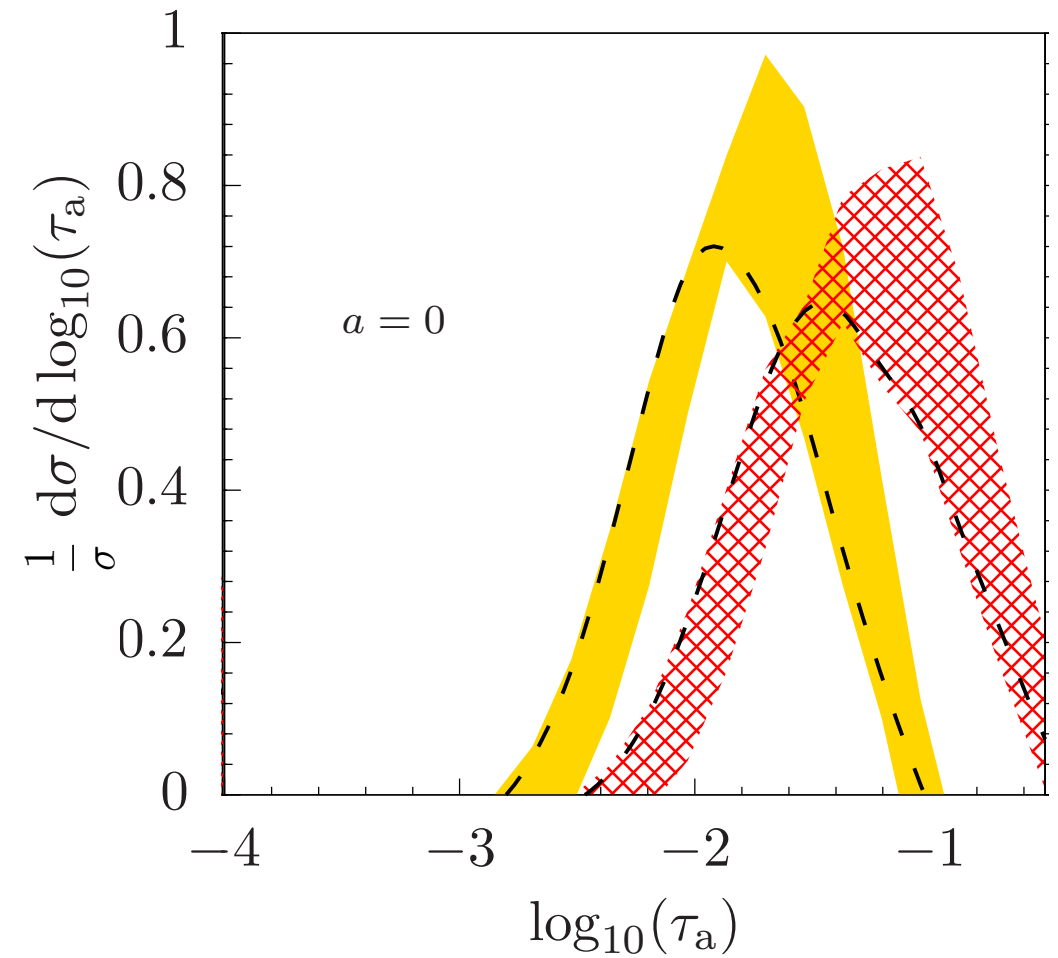


Photoproduction at the EIC

Log Angularity: $R = 0.8$: $p_T > 10.0$: $a = 0.0$



NLL ($R = 0.4$) 
 NLL ($R = 0.8$) 
 $\sqrt{s} = 141$ GeV, anti- k_T
 $p_T > 10$ GeV, $|\eta| < 2.5$



Power corrections

• e.g. $m_J^2 = \left(\sum_{i \in J} p_i \right)^2$ vs. $\tau_0 = \frac{1}{p_T} \sum_{i \in J} p_{Ti} \Delta R_{iJ}^2$

hard

hard-collinear

collinear

collinear-soft

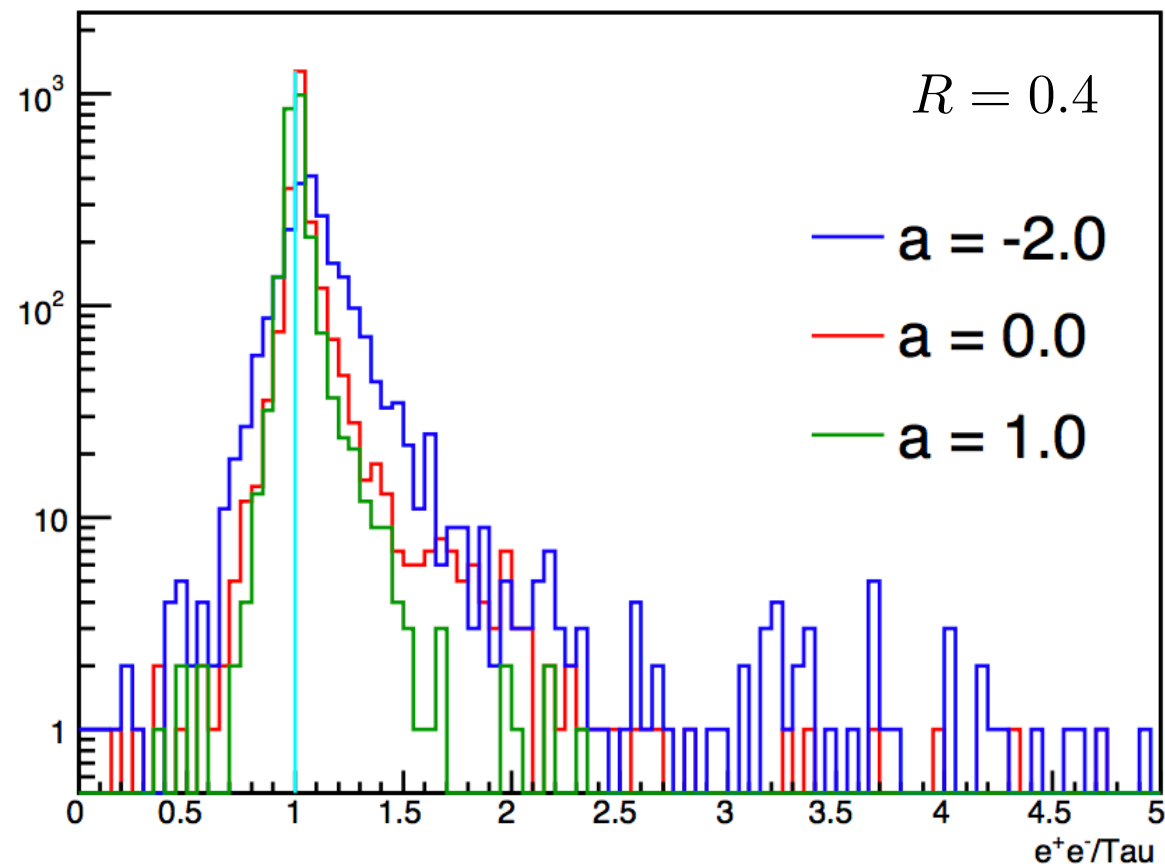
$$\mu_H \sim p_T$$

$$\mu_J \sim p_T R$$

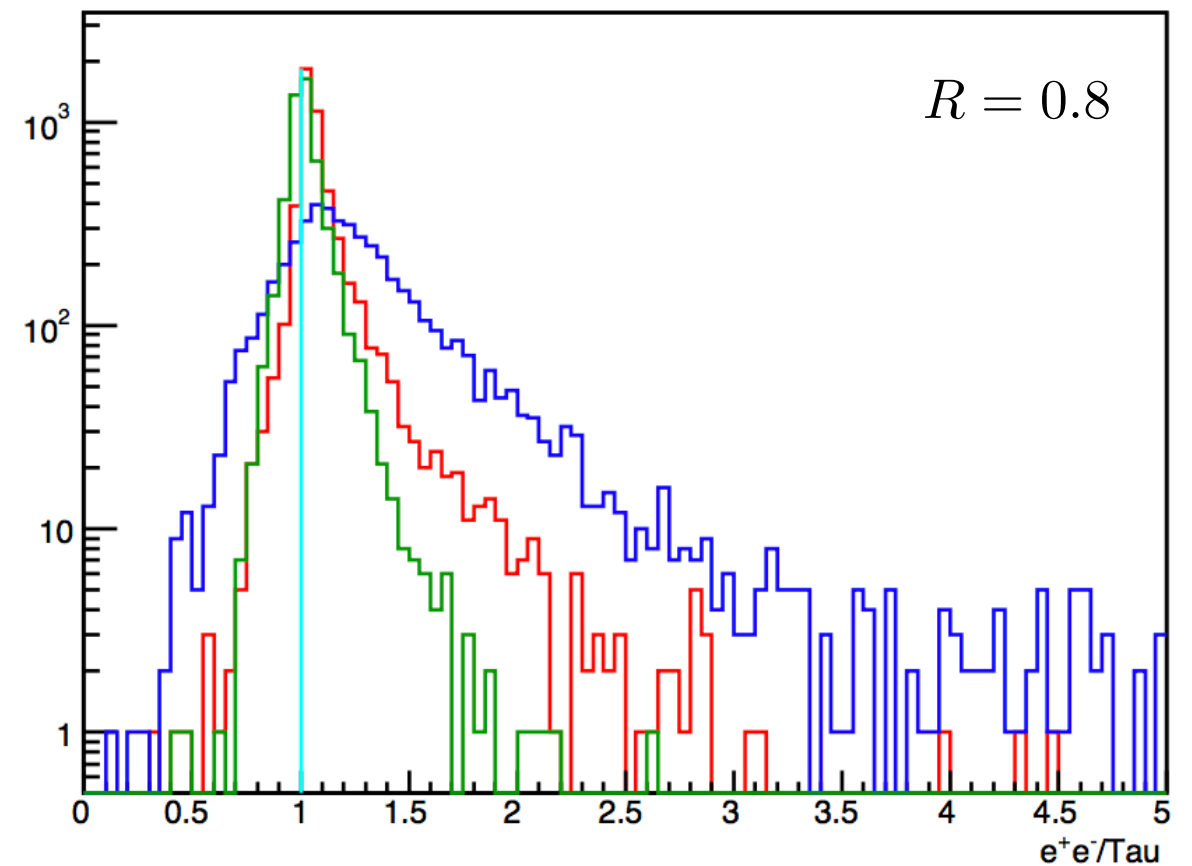
$$\mu_C \sim p_T (\tau_a)^{\frac{1}{2-a}}$$

$$\mu_S \sim \frac{p_T \tau_a}{R^{1-a}}$$

Angularity e^+e^- Over Tau (Massive Particles): $R=0.4$ $p_T > 10.0$



Angularity e^+e^- Over Tau (Massive Particles): $R=0.8$ $p_T > 10.0$

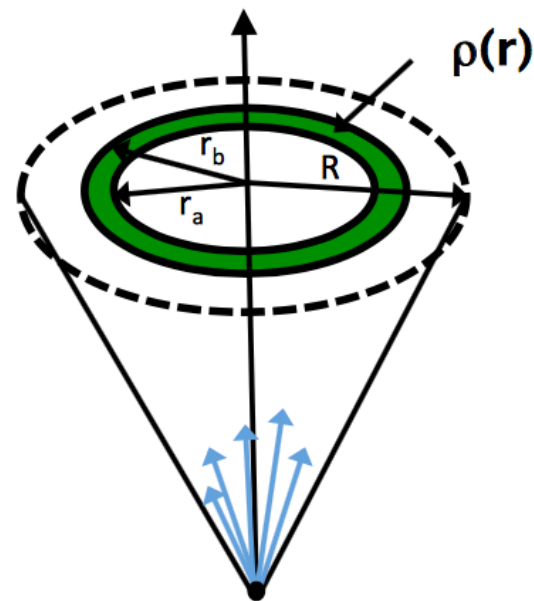
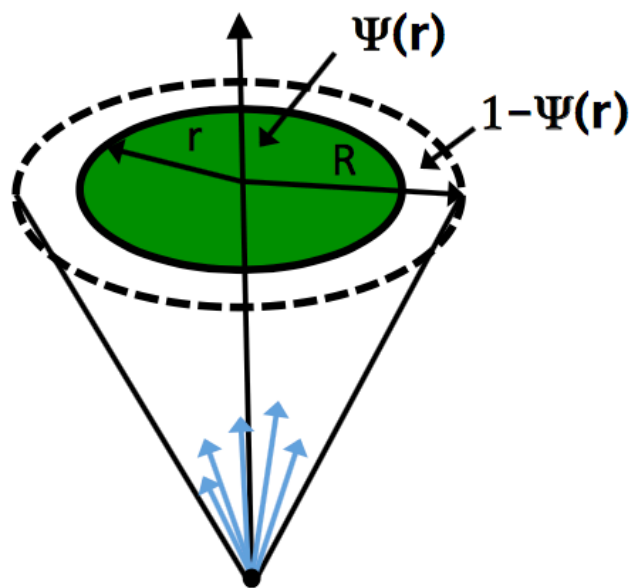


in collaboration with Aschenauer, Page

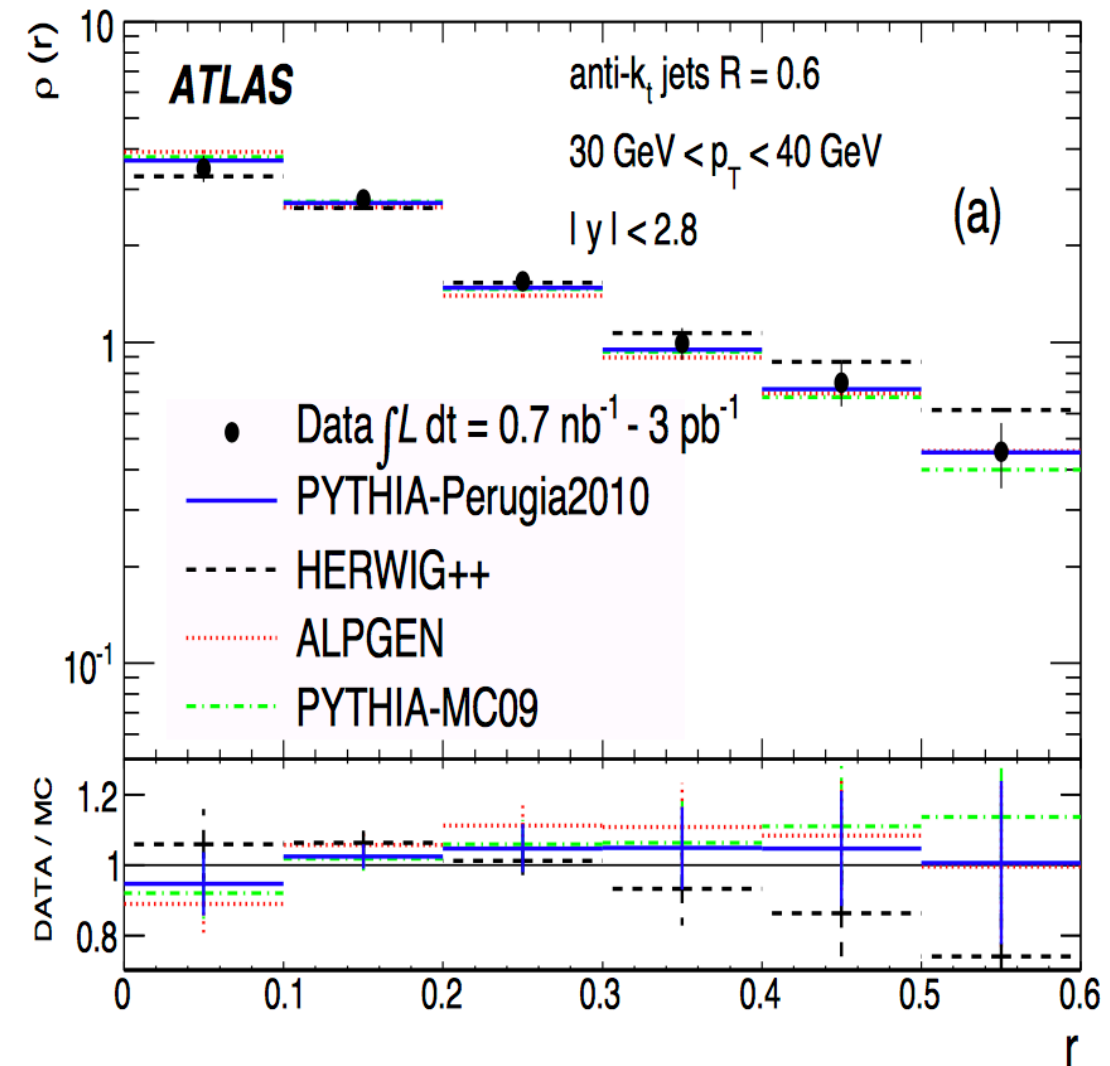
The jet energy profile

$$\psi(r) = \frac{\sum_{\Delta R_{iJ} < r} p_{Ti}}{\sum_{\Delta R_{iJ} < R} p_{Ti}}$$

$$\rho(r) = \frac{d\psi(r)}{dr}$$



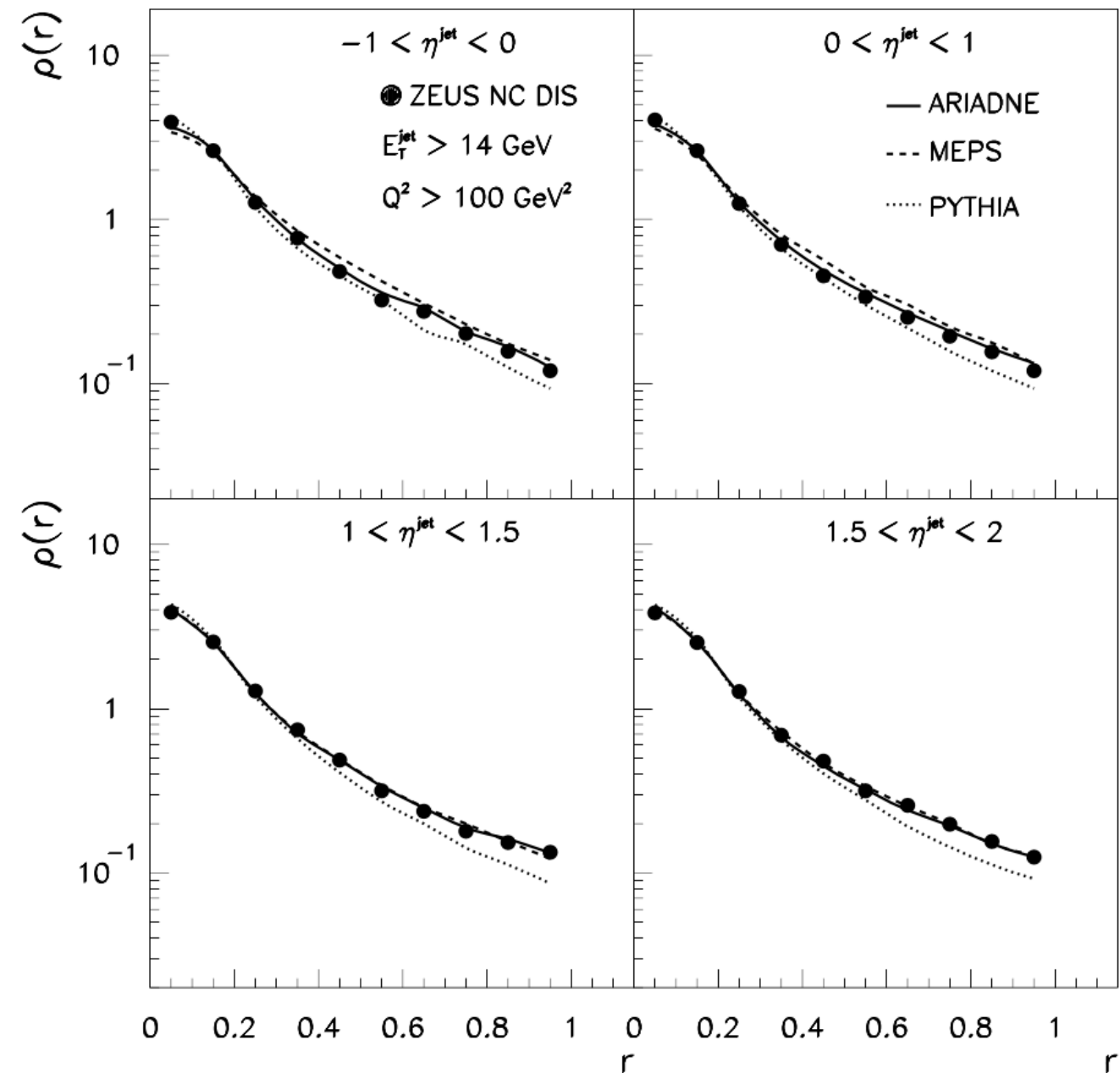
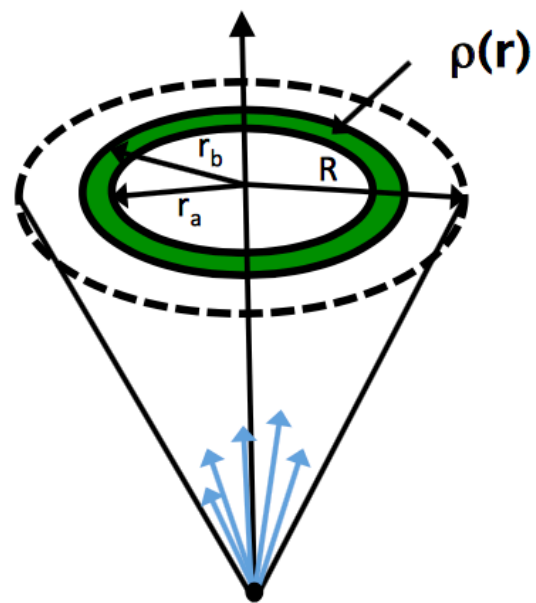
CMS, PLB 730 (2014) 243



ATLAS, PRD 83 (2011) 052003

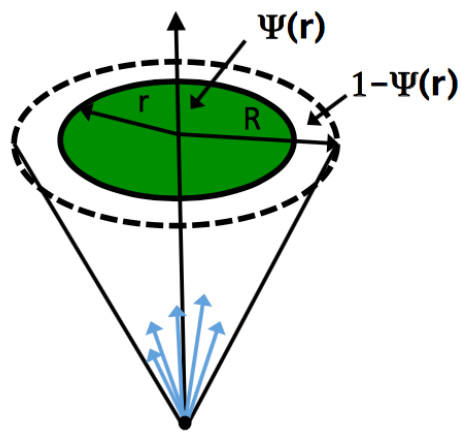
- Most frequently studied jet substructure observable
- LEP, HERA, Tevatron, LHC, ...
- Inclusive jets, Z+jet, Higgs+jet, ...

The jet energy profile



ZEUS, *Eur. Phys. J C8* (1999) 367

The jet energy profile



$$\psi(r) = \frac{\sum_{\Delta R_{iJ} < r} p_{Ti}}{\sum_{\Delta R_{iJ} < R} p_{Ti}}$$

$$\rho(r) = \frac{d\psi(r)}{dr}$$

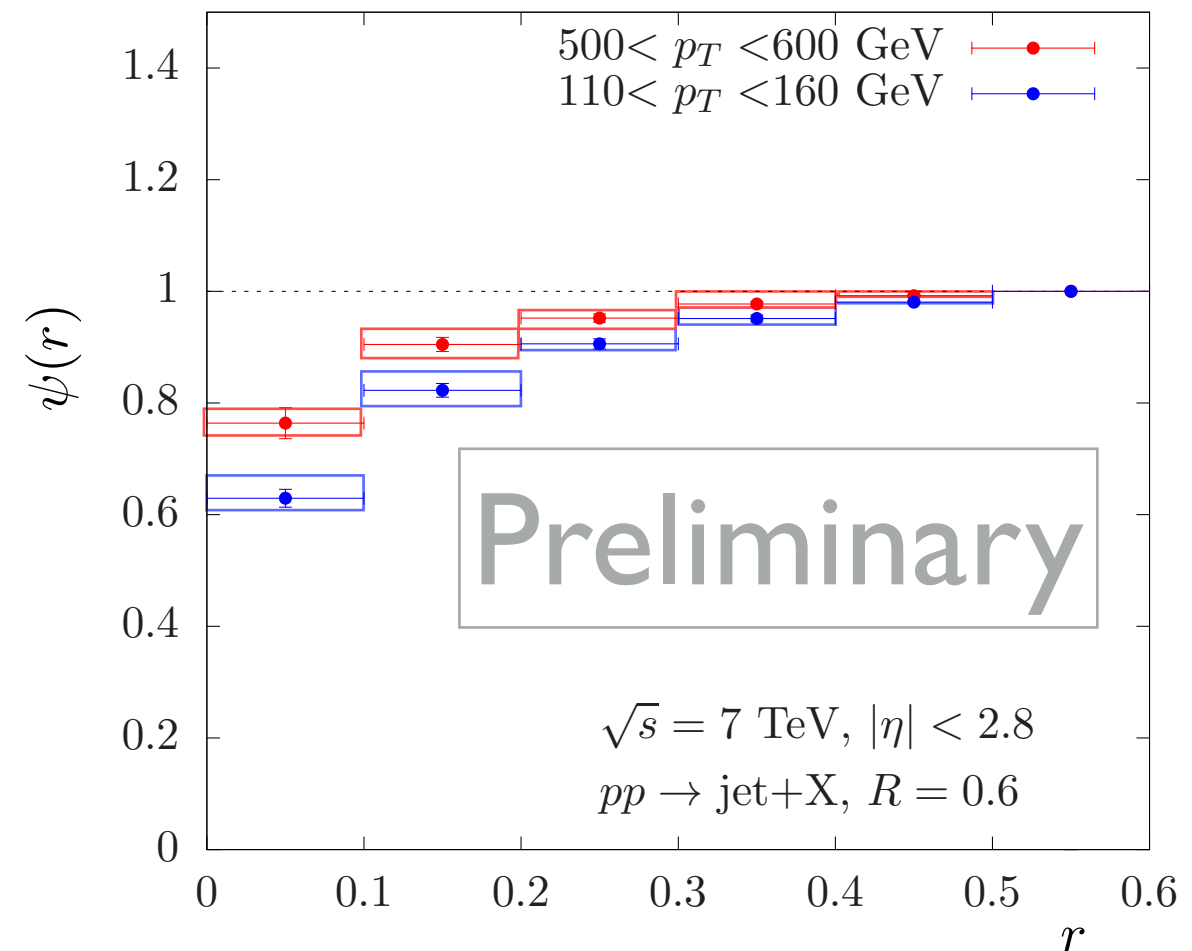
Kang, FR, Waalewijn '16
Cal, FR, Waalewijn - in preparation

- Factorization beyond leading-log

$$\mathcal{G}_i(z, p_T R, r/R, \mu) = \sum_j \mathcal{H}_{i \rightarrow j}(z, p_T R, \mu) \times \int d^2 k_{\perp} C_j(p_T r, k_{\perp}, \mu, \nu) S_j^G(k_{\perp}, \mu, \nu R) S_j^{\text{NG}}(r/R)$$

- NLL' resummation of $\ln(r/R)$
- Rapidity RG evolution, SCET_{II}
- Soft recoil
- Non-global logarithms

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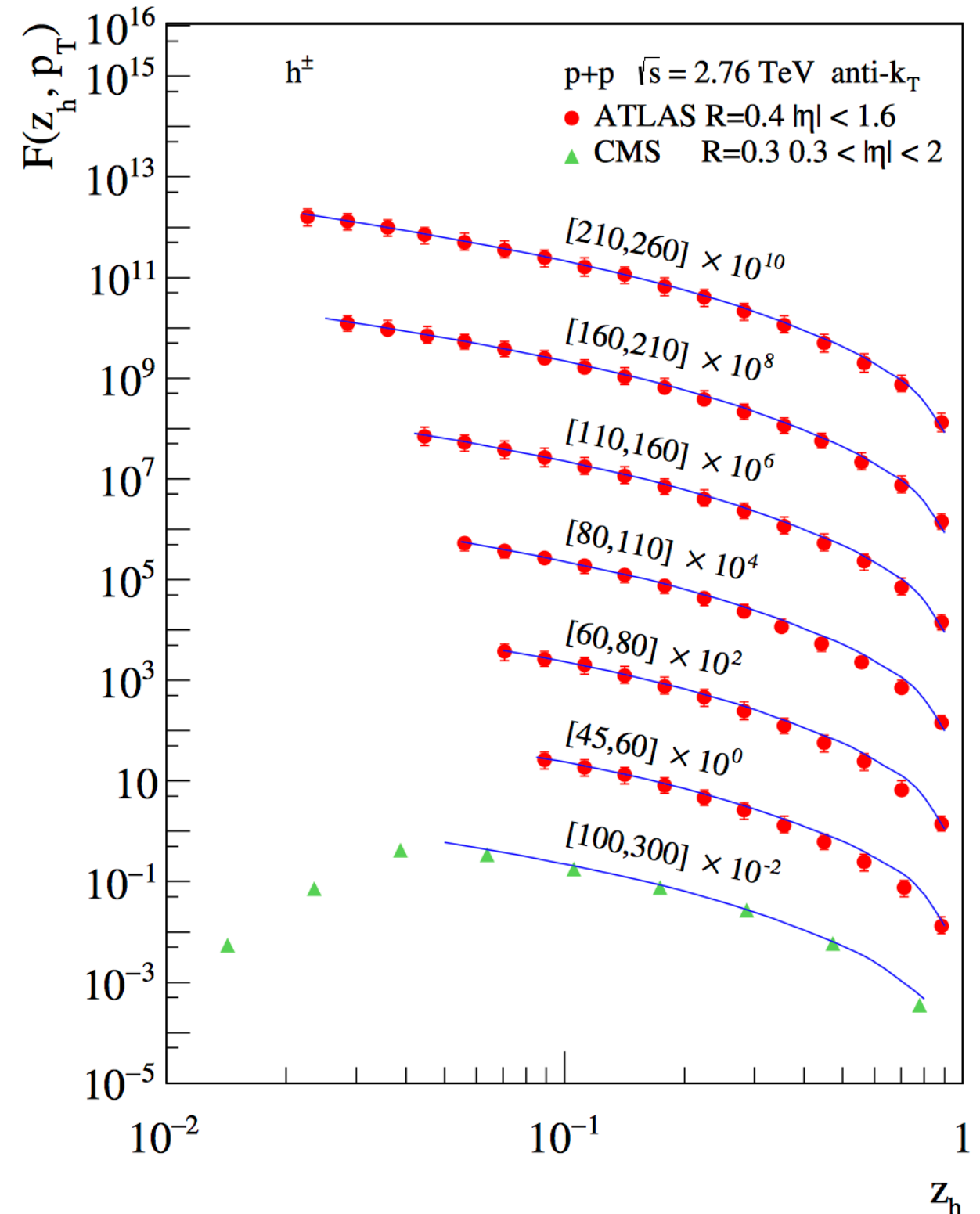
Earlier work see: Ellis, Kunszt, Soper '92
Seymour '98
Li, Li, Yuan '11
Chien, Vitev '14

Identified hadrons inside jets

- Constrain fragmentation functions
- Tagging

$$\frac{d\sigma_{pp \rightarrow (\text{jet } h) X}}{dp_T d\eta dz_h} = \sum_{abc} f_a \otimes f_b \otimes H_{ab}^c \otimes \mathcal{G}_c(z_h)$$

Arleo, Fontannaz, Guillet, Nguyen `14
 Kaufmann, Mukherjee, Vogelsang `15
 Kang, FR, Vitev `16



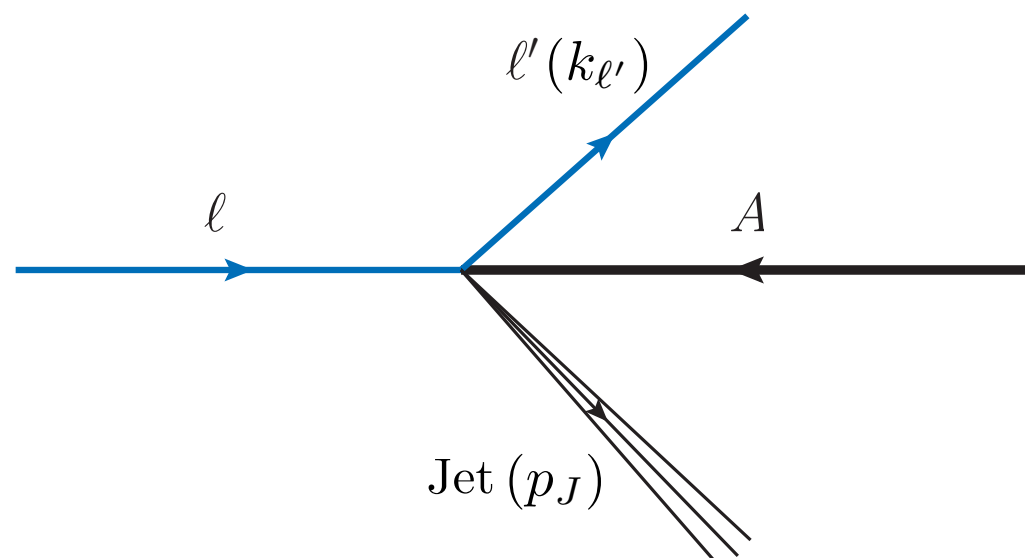
Outline

- Introduction
- Inclusive jets at the EIC
- Jet substructure
- Jet correlations
- Conclusions

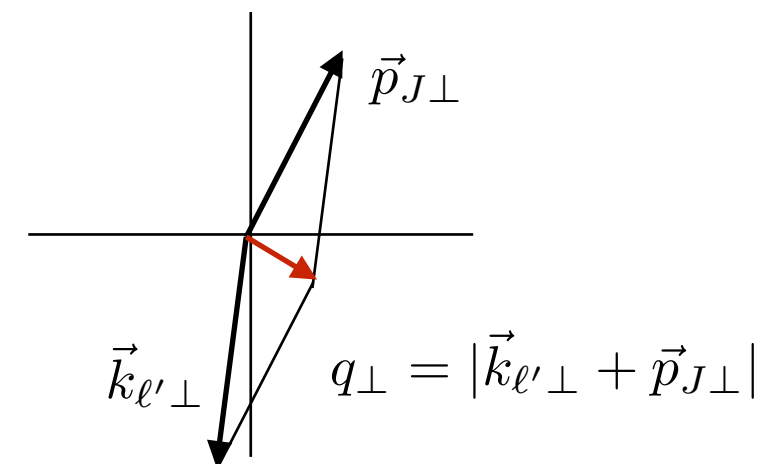
Lepton-jet correlations

Liu, FR, Vogelsang, Yuan
- in preparation

- Measure imbalance between lepton and jet
- Spin asymmetries and eA collisions
- Analogous to e.g. $pp \rightarrow \text{di-jets} + X$ Sun, Yuan, Yuan '15
- cms or laboratory frame; close analogy to pp collisions



Transverse plane



- Consider $\frac{d\sigma}{dy_{l'} d^2 k_{\perp l'} d^2 q_{\perp}}$

Requires TMD resummation for $q_{\perp} \ll k_{l' \perp}$
for the back-to-back configuration,
and jet radius resummation for $R \ll 1$

Factorization

- Joint q_{\perp} and jet radius resummation

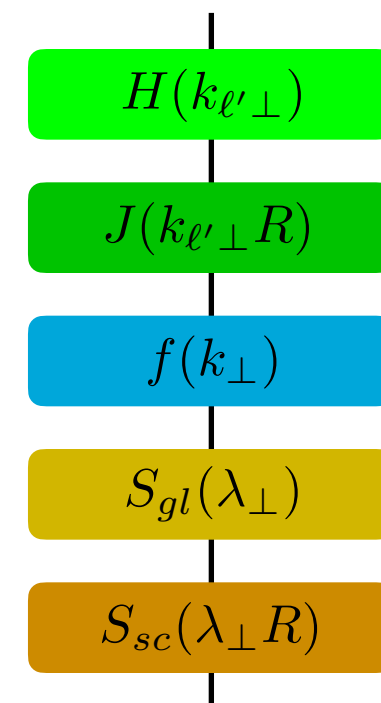
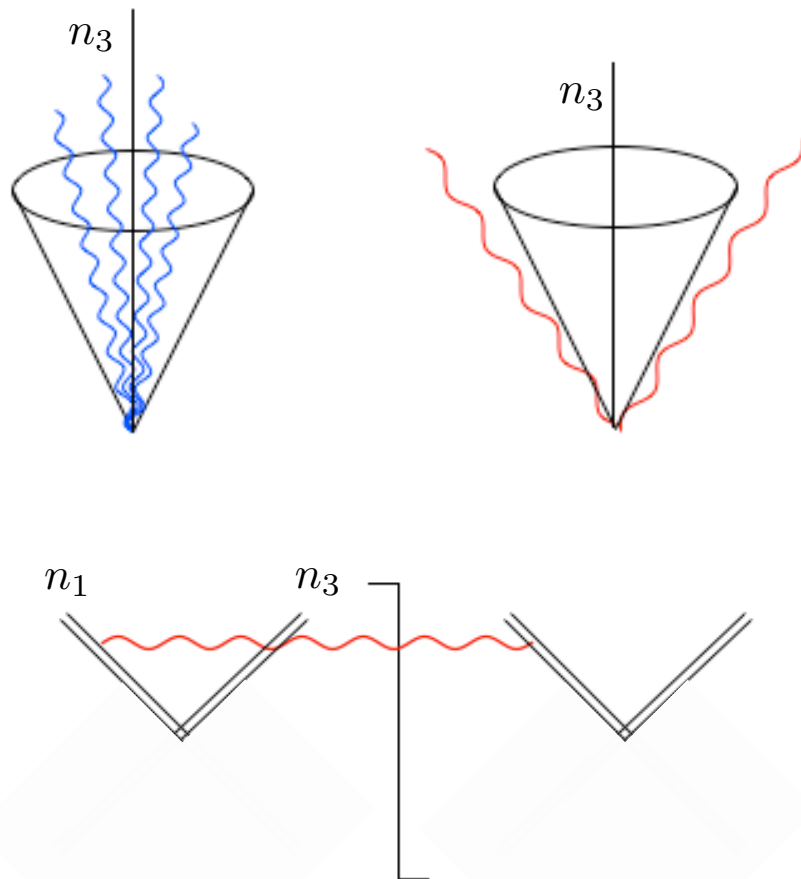
Liu, FR, Vogelsang, Yuan
- in preparation

Hard (virtual) Jet function

$$\frac{d\sigma}{dy_{e'} d^2 k_{\perp e'} d^2 q_{\perp}} = H_q(k_{e'\perp}, \mu) J_q(k_{e'\perp} R, \mu)$$

$$\int d^2 k_{\perp} d^2 \lambda_{1\perp} d^2 \lambda_{2\perp} x f_q(x, k_{\perp}, \mu, \nu) S_{gl}(\lambda_{1\perp}, \mu, \nu) S_{sc}(\lambda_{2\perp} R, \mu) \delta^{(2)}(q_{\perp} - k_{\perp} - \lambda_{1\perp} - \lambda_{2\perp})$$

Global soft Soft-collinear (in the jet direction)



Azimuthal lepton-jet correlation

Liu, FR, Vogelsang, Yuan
- in preparation

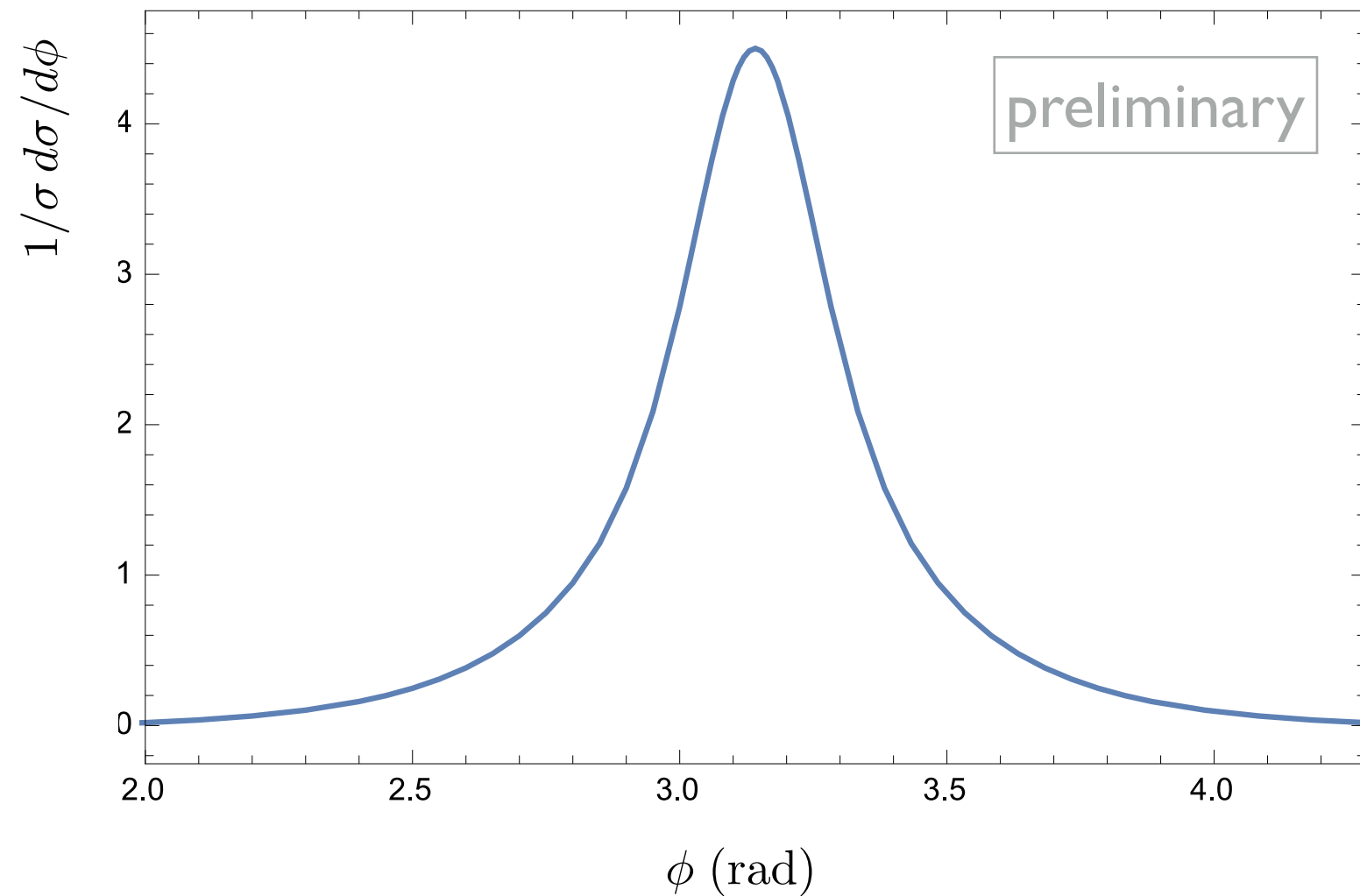
- Sample EIC kinematics

$$\sqrt{s} = 80 \text{ GeV}$$

$$k_{e' \perp} = 5 \text{ GeV}$$

$$5 < p_{\perp} < 10 \text{ GeV}$$

- currently $\ln R$ not yet resummed



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Conclusions

- Jets can be a unique tool at the future EIC
- Requires further theoretical efforts
- Extract collinear and TMD PDFs
- Jet substructure
- NP effects important
- Probe of nuclear matter

