

Gluon Sivers Function in J/ψ Production at EIC

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Gluon Sivers Function

Very little is known about GSF apart from a positivity bound

Burkardt's sum rule still leaves some room for GSF, moreover not all GSF are constrained by it

GSF : two gauge links ; process dependence more involved

Simplest possibilities : ++ (Weizsacker-Williams (WW) gluon distributions)
and +- (Dipole distributions)

more complicated combinations are possible ; see for example Buffing, AM, Mulders, PRD 88, 054027 (2013)

J/ψ production at EIC is an effective way to study WW type GSF as it probes at LO through
 $\gamma^* g \rightarrow c\bar{c}$

Recent results from COMASS on GSF

COMPASS Collaboration, J. Phys. Conf. Ser 678, 012050 (2016)

Sivers Asymmetry in J/ψ Production

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Due to final state interactions, in ep collision, SSA in heavy quarkonium production is non-zero when the heavy quark pair is produced in color octet state

F. Yuan, PRD 78, 014024 (2008)

Consider the process $e(l) + p^\uparrow(P) \rightarrow e(l') + J/\psi(P_h) + X$,

Differential cross section for unpol process

$$d\sigma = \frac{1}{2s} \frac{d^3l'}{(2\pi)^3 2E_{l'}} \frac{d^3P_h}{(2\pi)^3 2E_h} \int dx d^2k_\perp (2\pi)^4 \delta^4(q + k - P_h) \\ \times \frac{1}{Q^4} L^{\nu\nu'}(l, q) \Phi_g^{\mu\mu'}(x, k_\perp) \mathcal{M}_{\mu\nu}^{\gamma^* g \rightarrow J/\psi} \mathcal{M}_{\mu'\nu'}^{* \gamma^* g \rightarrow J/\psi}$$

$$\Phi_g^{\mu\mu'}(x, k_\perp) = \frac{1}{2x} \left\{ -g_T^{\mu\mu'} f_1^g(x, k_\perp^2) + \left(\frac{k_\perp^\mu k_\perp^{\mu'}}{M_p^2} + g_T^{\mu\mu'} \frac{k_\perp^2}{2M_p^2} \right) h_1^{\perp g}(x, k_\perp^2) \right\}, \quad \begin{aligned} q &= l - l' \\ Q^2 &= -q^2 \end{aligned}$$

Transversely polarized target

$$\Phi_g^{T\mu\mu'}(x, k_\perp) = -\frac{1}{2x} g_T^{\mu\mu'} \frac{\epsilon_T^{\rho\sigma} k_{\perp\rho} S_{T\sigma}}{M_p} f_{1T}^{\perp g}(x, k_\perp^2)$$

Sivers Asymmetry in J/ψ Production

Numerator and denominator of the SSA

$$\frac{d\sigma^\uparrow}{dydx_Bd^2P_{hT}} - \frac{d\sigma^\downarrow}{dydx_Bd^2P_{hT}} = \frac{\alpha}{8sxQ^4} [A_0 + A_1 \cos \phi_h] \Delta^N f_{g/p^\uparrow}(x, P_{hT}).$$

$$\frac{d\sigma^\uparrow}{dydx_Bd^2P_{hT}} + \frac{d\sigma^\downarrow}{dydx_Bd^2P_{hT}} = \frac{2\alpha}{8sxQ^4} [A_0 + A_1 \cos \phi_h] f_{g/p}(x, P_{hT}^2),$$

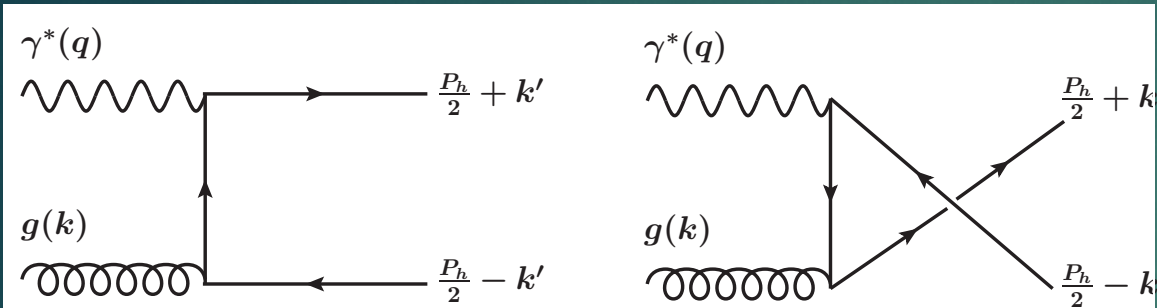
$$\Delta^N f_{g/p^\uparrow}(x, P_{hT}, Q_f) = -2f_{1T}^{\perp g}(x, P_{hT}, Q_f) \frac{(\hat{P} \times P_{hT}) \cdot S}{M_p}.$$

Trento convention

A_0 and A_1 : calculated in color octet model

$$z = P \cdot P_h / P \cdot q; \quad x_B = \frac{Q^2}{2P \cdot q}, \quad y = \frac{P \cdot q}{P \cdot l}$$

LO Amplitude of $\gamma^* g \rightarrow J/\Psi$



Approach of Boer, Pisano, PRD 86, 094007 (2012); Baier, Ruckl, Z. Phys. C 19, 251 (1983)

Factorized form of the cross section. : initial state partons form a heavy quark pair with definite color and angular momentum quantum numbers, and a non-perturbative matrix element through which the pair forms J/Ψ

$$M^{\mu\nu} \left(\gamma^* g \rightarrow Q\bar{Q} [{}^{2S+1}L_J^{(1,8a)}] \right) = \sum_{L_z S_z} \int \frac{d^3 k'}{(2\pi)^3} \Psi_{LL_z}(k') \langle LL_z; SS_z | JJ_z \rangle \text{Tr} [O^{\mu\nu}(q, k, P_h, k') P_{SS_z}(P_h, k')]$$



Eigenfunction of OAM L



Spin projection operator

k' : relative momentum of the heavy quark pair. Taylor expansion about $k'=0$ gives S wave and P wave amplitudes

Small x TMDs : Bacchetta, Boer, Pisano, Taelis, arXiv: 1809.02056 [hep-ph]

LO Amplitude of $\gamma^* g \rightarrow J/\Psi$

$$O^{\mu\nu}(q, k, P_h, k') = \sum_{ij} \langle 3i; 3j | 8a \rangle g_s (ee_c) \left\{ \gamma^\nu \frac{P_h/2 + \not{k}' - \not{q} + m_c}{(P_h/2 + k' - q)^2 - m_c^2} \gamma^\mu (T^b)^{ji} \right. \\ \left. + \gamma^\mu (T^b)^{ji} \frac{P_h/2 + \not{k}' - \not{k} + m_c}{(P_h/2 + k' - k)^2 - m_c^2} \gamma^\nu \right\}$$

SU(3) CG coeff : projects out the color state of heavy quark pair, color singlet or color octet

Spin projection operator : projects out spin singlet and triplet

Example : S wave amplitude :

$$\mathcal{M}^{\mu\nu}[^1S_0^{(8a)}] = 2i \frac{\sqrt{2} g_s (ee_c) \delta^{ab}}{\sqrt{\pi M} (Q^2 + M^2)} R_0(0) \epsilon^{\mu\nu\rho\sigma} k_\rho P_{h\sigma}$$

Radial wave function at the origin is related to long distance matrix elements (LDME)

$$\langle 0 | \mathcal{O}_8^{J/\psi} (^1S_J) | 0 \rangle = \frac{2}{\pi} (2J + 1) |R_0(0)|^2$$

Ko, Lee, Song, PRD 54, 4312 (1996)

SSA in color octet model

Contribution to the Sivers asymmetry comes from

$$A_0 = [1 + (1 - y)^2] \frac{N Q^2}{y^2 M} \left\{ \langle 0 | O_8^{J/\psi}({}^1S_0) | 0 \rangle + \frac{4}{3M^2} \frac{(3M^2 + Q^2)^2}{(M^2 + Q^2)^2} \langle 0 | O_8^{J/\psi}({}^3P_0) | 0 \rangle \right. \\ \left. + \frac{8Q^2}{3M^2(M^2 + Q^2)^2} \left(\frac{4M^2(1 - y)}{1 + (1 - y)^2} + Q^2 \right) \langle 0 | O_8^{J/\psi}({}^3P_1) | 0 \rangle \right. \\ \left. + \frac{8}{15M^2(M^2 + Q^2)^2} \left(6M^4 + Q^4 + 12M^2Q^2 \frac{1 - y}{1 + (1 - y)^2} \right) \langle 0 | O_8^{J/\psi}({}^3P_2) | 0 \rangle \right\}$$

M : mass of J/ψ

$$Q^2 = x_B y s$$

LDMEs : Ma and Venugopalan , PRL 113, 192301 (2014); Chao et al, PRL 108, 242004 (2012); Sharma and Vitev, PRC 87, 044905 (2013).

Contribution from unpolarized gluons only considered in the denominator

AM, S. Rajesh, EPJC 77, 854 (2017)

Gluon Sivers Function

$$\Delta^N f_{g/p^\uparrow}(x, k_\perp) = 2\mathcal{N}_g(x) f_{g/p}(x, \mu) h(k_\perp) \frac{e^{-k_\perp^2/\langle k_\perp^2 \rangle}}{\pi \langle k_\perp^2 \rangle}$$

D'Alesio, Murgia, Pisano, JHEP 09, 119 (2015)

$$\mathcal{N}_g(x) = N_g x^\alpha (1-x)^\beta \frac{(\alpha + \beta)^{(\alpha + \beta)}}{\alpha^\alpha \beta^\beta}$$

$$h(k_\perp) = \sqrt{2} e \frac{k_\perp}{M_1} e^{-k_\perp^2/M_1^2}$$

Best fit parameter sets : SIDIS1 And SIDIS2

$$(a) \quad \mathcal{N}_g(x) = (\mathcal{N}_u(x) + \mathcal{N}_d(x))/2$$

BV-a

Best fit parameters for u and d quark Sivers function from

$$(b) \quad \mathcal{N}_g(x) = \mathcal{N}_d(x)$$

BV-b

Anselmino et al, JHEP 04, 046 (2017)

Boer and Vogelsang, PRD 69, 094025 (2004)

Non-universality :

$$\Delta_{DY}^N f_{g/p^\uparrow}(x, k_\perp) = -\Delta_{SIDIS}^N f_{g/p^\uparrow}(x, k_\perp)$$

TMD Evolution

$$f_{1T}^{\perp g}(x, P_{kT}, Q_f) = -\frac{1}{2\pi P_{kT}} \int_0^\infty db_\perp b_\perp J_1(P_{kT} b_\perp) f'_{1T}{}^{\perp g}(x, b_\perp, Q_f)$$

$$f_{g/p}(x, P_{kT}, Q_f) = \frac{1}{2\pi} \int_0^\infty db_\perp b_\perp J_0(P_{kT} b_\perp) f_{g/p}(x, b_\perp, Q_f)$$

Aybat, Rogers, PRD 83, 114042 (2011); Aybat, Collins, Qiu, Rogers, PRD 85, 034043 (2012)

Derivative of Sivers function obeys same evolution equation as unpol TMD

$$f'_{1T}{}^{\perp g}(x, b_\perp, Q_f) = f'_{1T}{}^{\perp g}(x, b_\perp, Q_i) \exp\left\{-\int_{c/b_*}^{Q_f} \frac{d\mu}{\mu} \left(A \log\left(\frac{Q_f^2}{\mu^2}\right) + B\right)\right\} \\ \times \exp\left\{-\left[g_1^{\text{sivers}} + \frac{g_2}{2} \log \frac{Q_f}{Q_0}\right] b_\perp^2\right\}$$

Perturbative expansion for A and B

Initial scale of TMDs $Q_i = c/b_*(b_\perp)$ $c = 2e^{-\gamma_E}$ Final scale $Q_f = M$

$$b_*(b_\perp) = \frac{b_\perp}{\sqrt{1 + \left(\frac{b_\perp}{b_{max}}\right)^2}} \approx b_{max}; \quad (b_\perp \rightarrow \infty)$$

$$b_*(b_\perp) \approx b_\perp; \quad (b_\perp \rightarrow 0)$$

Best fit parameters from Echevarria et al, PRD 89, 074013 (2014)

TMD Evolution

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$$f_1^g(x, b_\perp, Q_i) = \sum_{i=g,q} \int_x^1 \frac{d\hat{x}}{\hat{x}} C_{i/g}(x/\hat{x}, b_\perp, \alpha_s, Q_i) f_{i/p}(\hat{x}, c/b_\star) + \mathcal{O}(b_\perp \Lambda_{QCD}),$$

TMDs at initial scale : Coefficient function is calculated perturbatively for each TMD

At leading order

$$f_1^g(x, b_\perp, Q_i) = f_{g/p}(x, c/b_\star) + \mathcal{O}(\alpha_s),$$

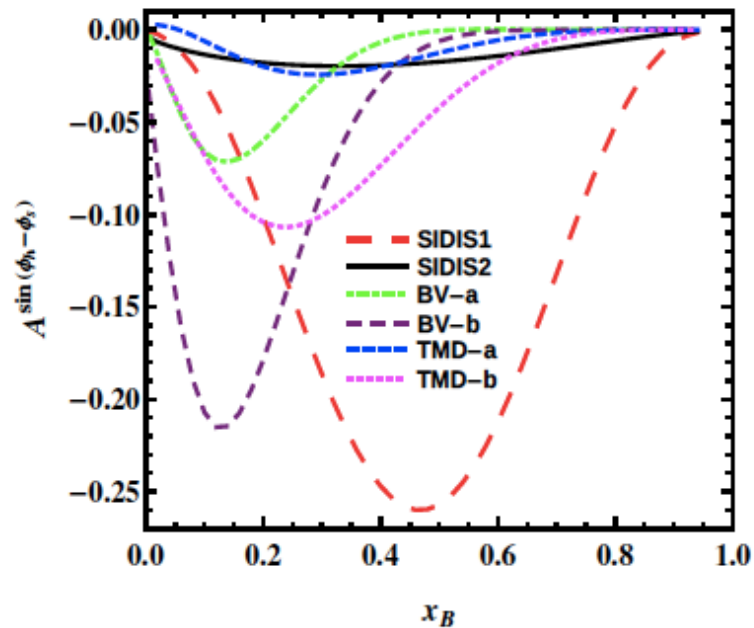
$$f_{1T}^{\perp g}(x, b_\perp, Q_i) \simeq \frac{M_p b_\perp}{2} T_{g,F}(x, x, Q_i)$$

Qiu-Sterman function

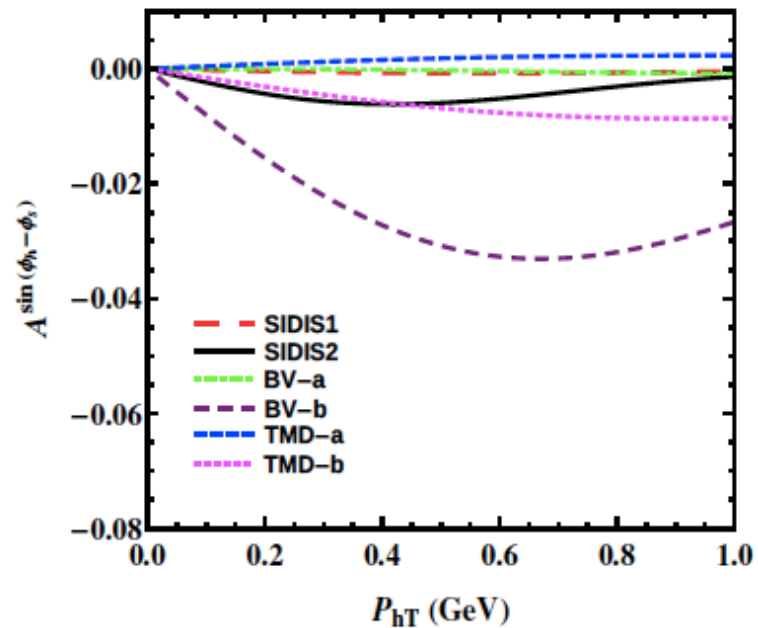
$$T_{g,F}(x, x, Q_i) = \mathcal{N}_g(x) f_{g/p}(x, Q_i)$$

Two choices of \mathcal{N}_g (Same as before): TMD –a and TMD –b parametrizations

Numerical results



(a)

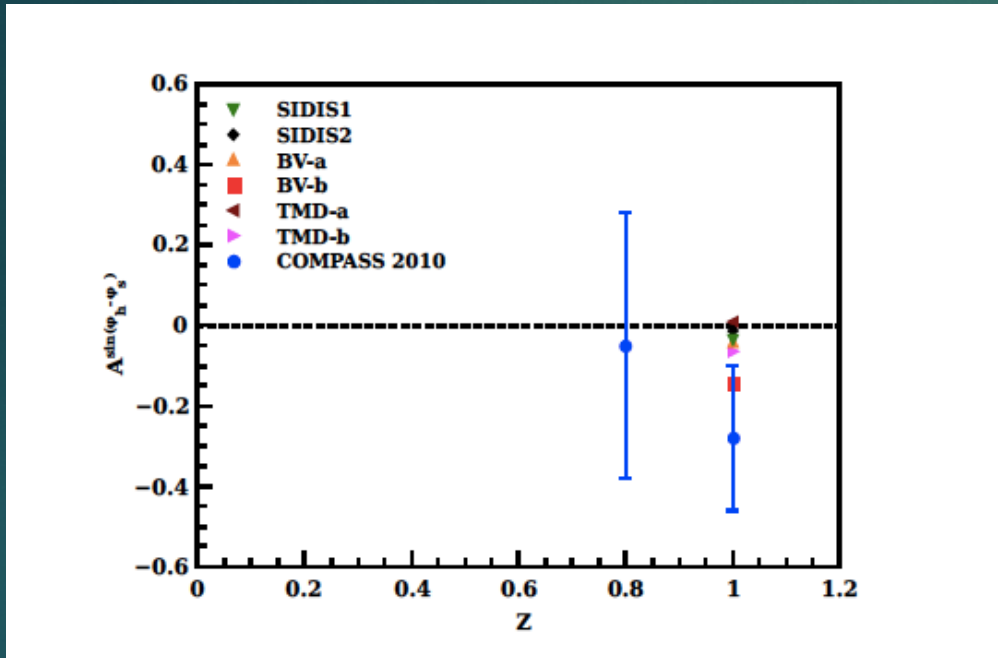


(b)

Sivers asymmetry for EIC $\sqrt{s} = 45$ GeV using different parametrizations

Integration ranges are $0 < P_{hT} < 1$ GeV; $0.1 < y < 0.9$; $0.001 < x_B < 0.9$

Numerical Results



Sivers asymmetry compared with COMPASS data

Data from

J. Phys. Conf. Ser. 678, 012050 (2016) (COMPASS)

$$\sqrt{s} = 17.2 \text{ GeV}; 0 < P_{hT} < 1 \text{ GeV};$$
$$0.1 < y < 0.9; 0.0001 < x_B < 0.65$$

All parametrizations give negative asymmetry

AM, S. Rajesh, EPJC 77, 854 (2017)

BV-b gives results within the error bar of the experiment

Gluon Sivers function in Inclusive Photoproduction of J/ψ

Consider inclusive process $e(l) + p^\uparrow(P) \rightarrow J/\psi(P_h) + X$

In the kinematical limit when the photon is almost real (forward scattering)

Dominating subprocess is photon-gluon fusion $\gamma(q) + g(k) \rightarrow J/\psi(P_h) + g(p_g)$

Two types of contributions (1) Direct : photon interacts electromagnetically with partons in the proton (2) Resolved : photon acts as a source of partons and they interact strongly with the partons in the proton

We consider only direct photoproduction , resolved photo production mainly contributes in low z region

$$z = \frac{P \cdot P_h}{P \cdot q}$$

Can be determined using Jacquet-Blondel Method without detecting final lepton

LO photon-gluon fusion $\gamma + g \rightarrow J/\psi$ Contributes at $z=1$: removed using cut on z

Gluon Sivers function in inclusive photoproduction of J/ψ

Diffractive process contributes at $z \approx 1$; $P_{hT} \approx 0$ Ryskin, Z. Phys. C 57, 89 (1993)

Gluon and heavy quark fragmentation for larger values of P_{hT}

To choose inelastic process we have used the kinematical cut $0.3 < z < 0.9$

Contribution from photon-quark fusion negligible compared to photon-gluon fusion

$$A_N = \frac{d\sigma^\uparrow - d\sigma^\downarrow}{d\sigma^\uparrow + d\sigma^\downarrow}$$

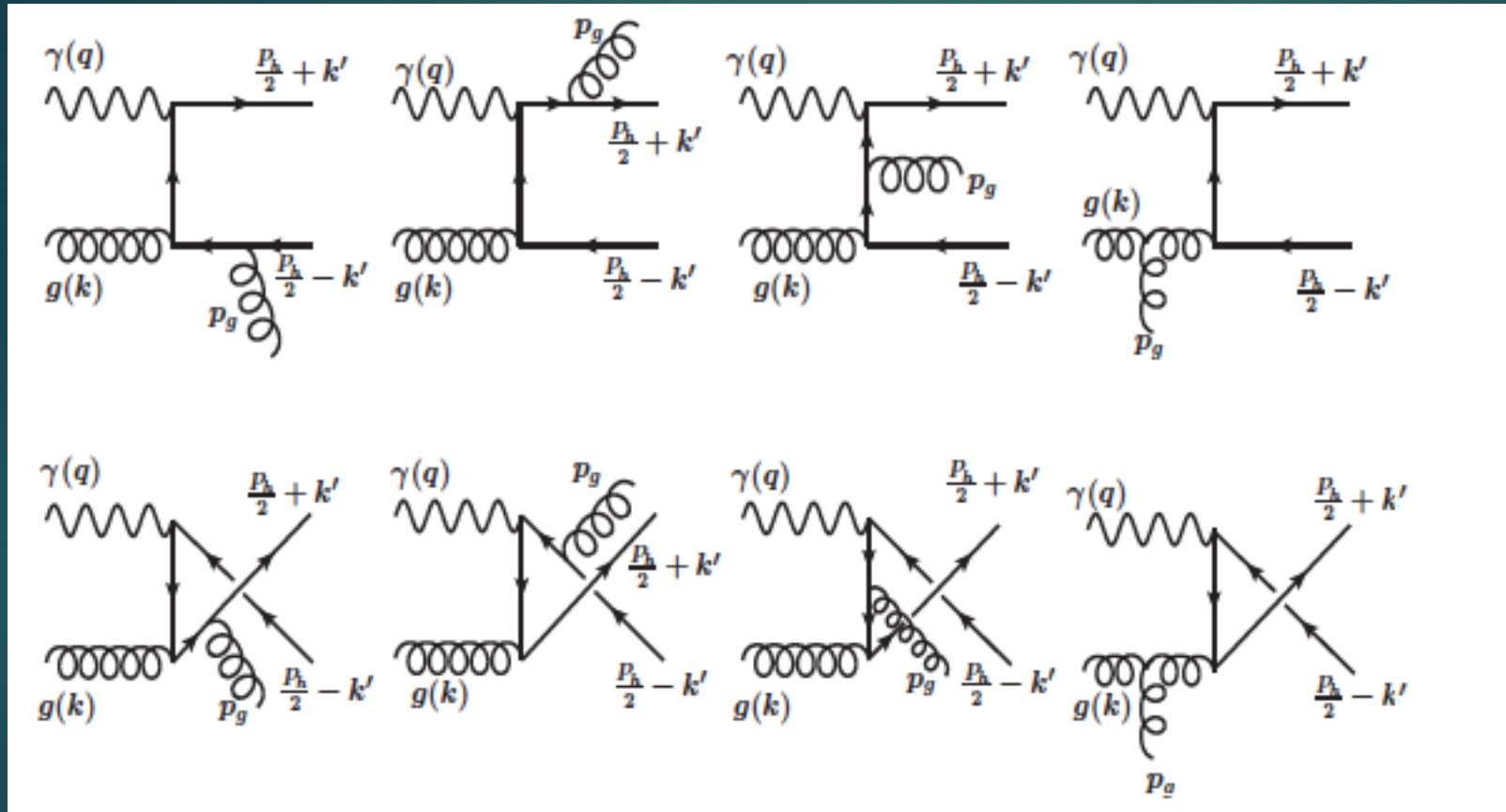
Final state heavy quark pair is produced unpolarized in photon-gluon fusion ; contribution to the numerator of the asymmetry comes mainly from gluon Sivers function

Linearly polarized gluons do not contribute to the denominator as long as the lepton is unpolarized

D'Alesio, Flore, Murgia, PRD 95, 094002 (2017); Anselmino et al, PRD 70, 074025 (2004)

Inclusive photoproduction of J/ψ

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We follow the same approach as before to calculate the amplitude for heavy quarkonium production in color octet model

Virtual diagrams contribute at $z=1$

Inclusive photoproduction of J/ψ

Numerator of the asymmetry

Amplitude calculated in NRQCD

$$\begin{aligned}
 d\sigma^\uparrow - d\sigma^\downarrow &= \frac{d\sigma^{ep^\uparrow \rightarrow J/\psi X}}{dzd^2\mathbf{P}_T} - \frac{d\sigma^{ep^\downarrow \rightarrow J/\psi X}}{dzd^2\mathbf{P}_T} \\
 &= \frac{1}{2z(2\pi)^2} \int dx_\gamma dx_g d^2\mathbf{k}_{\perp g} f_{\gamma/e}(x_\gamma) \Delta^N f_{g/p^\uparrow}(x_g, \mathbf{k}_{\perp g}) \\
 &\quad \times \delta(\hat{s} + \hat{t} + \hat{u} - M^2) \frac{1}{2\hat{s}} |\mathcal{M}_{\gamma+g \rightarrow J/\psi+g}|^2,
 \end{aligned}$$

Weizsacker-Williams distribution for photons inside an electron

Frixione et al, PLB, 319, 339 (1993)

$$f_{\gamma/e}(x_\gamma) = \frac{\alpha}{2\pi} \left[2m_e^2 x_\gamma \left(\frac{1}{Q_{min}^2} - \frac{1}{Q_{max}^2} \right) + \frac{1 + (1 - x_\gamma)^2}{x_\gamma} \ln \frac{Q_{max}^2}{Q_{min}^2} \right]$$

$$Q_{min}^2 = m_e^2 \frac{x_\gamma^2}{1 - x_\gamma}$$

Same parametrizations for Sivers function and unpolarized TMD as before

Inclusive photoproduction of J/ψ

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Amplitude can be written as

$$\mathcal{M}(\gamma g \rightarrow Q\bar{Q}[{}^{2S+1}L_J^{(1,8)}](P_h) + g) = \sum_{L_z S_z} \int \frac{d^3 \mathbf{k}'}{(2\pi)^3} \Psi_{LL_z}(k') \langle LL_z; SS_z | JJ_z \rangle \\ \times \text{Tr}[O(q, k, P_h, k') \mathcal{P}_{SS_z}(P_h, k')],$$

$$O(q, k, P_h, k') = \sum_{m=1}^8 C_m O_m(q, k, P_h, k').$$

Each operator O_m is calculated from individual Feynman diagram, as well as the color factor C_m

$$\mathcal{M}[{}^{2S+1}S_J^{(8)}](P_h, k) = \frac{1}{\sqrt{4\pi}} R_0(0) \text{Tr}[O(q, k, P_h, k') \mathcal{P}_{SS_z}(P_h, k')] \Big|_{k'=0} \\ = \frac{1}{\sqrt{4\pi}} R_0(0) \text{Tr}[O(0) \mathcal{P}_{SS_z}(0)],$$

Approach of Boer, Pisano, PRD 86, 094007 (2012); Baier, Ruckl, Z. Phys. C 19, 251 (1983)

$$\mathcal{M}[{}^{2S+1}P_J^{(8)}] = -i \sqrt{\frac{3}{4\pi}} R'_1(0) \sum_{L_z S_z} \varepsilon_{L_z}^\alpha(P_h) \langle LL_z; SS_z | JJ_z \rangle \frac{\partial}{\partial k'^\alpha} \text{Tr}[O(q, k, P_h, k') \mathcal{P}_{SS_z}(P_h, k')] \Big|_{k'=0} \\ = -i \sqrt{\frac{3}{4\pi}} R'_1(0) \sum_{L_z S_z} \varepsilon_{L_z}^\alpha(P_h) \langle LL_z; SS_z | JJ_z \rangle \text{Tr}[O_\alpha(0) \mathcal{P}_{SS_z}(0) + O(0) \mathcal{P}_{SS_z \alpha}(0)]$$

S. Rajesh, Raj Kishore, AM PRD 98, 014007 (2018)

Amplitude in color octet model

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$$s_1 = \hat{s} - M^2, \quad t_1 = \hat{t} - M^2, \quad u_1 = \hat{u} - M^2.$$

$$|\mathcal{M}[{}^3S_1^{(8)}]|^2 = \frac{5\pi^3 e_c^2 \alpha_s^2 \alpha}{36M} \langle 0 | \mathcal{O}_8^{J/\psi} ({}^3S_1) | 0 \rangle \frac{512M^2}{s_1^2 t_1^2 u_1^2} \\ \times \{s_1^2 (s_1 + M^2)^2 + u_1^2 (u_1 + M^2)^2 + t_1^2 (t_1 + M^2)^2\}$$

S. Rajesh, Raj Kishore, AM
PRD 98, 014007 (2018)

There are contributions from ${}^3S_1, {}^1S_0, {}^3P_J$ in color octet model

Both color singlet and color octet contributions are included in the denominator

Amplitude squared are calculated using FORM

LDMEs taken from

Chao et al, PRL 108, 242004 (2012); Butenschoen and Kniehl, PRD 84, 051501 (2011); Zhang et al, PRL 114, 092006 (2015).

Amplitude squared in color octet model

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$$\begin{aligned}
 |\mathcal{M}[^3P_1^{(8)}]|^2 = & \frac{\pi^3 e_c^2 \alpha_s^2 \alpha}{8M} \langle 0 | \mathcal{O}_8^{J/\psi} (^3P_1) | 0 \rangle \frac{2048}{m^2 s_1^4 t_1^4 u_1^4 (m^2 + u_1)^2} \left\{ 8s_1 t_1 u_1 m^{20} + 4(5s_1^2 t_1^2 \right. \\
 & + (s_1 + t_1)^2 u_1^2) m^{18} + 4u_1 (2(s_1^2 - 4t_1 s_1 + t_1^2) u_1^2 + s_1 t_1 (5s_1^2 + 8t_1 s_1 + 5t_1^2)) \\
 & \times m^{16} + 2(-2(s_1^2 + 16t_1 s_1 + t_1^2) u_1^4 + s_1 t_1 (12s_1^2 + 23t_1 s_1 + 12t_1^2) u_1^2 + 2s_1^2 t_1^2 \\
 & \times (3s_1^2 - 7t_1 s_1 + 3t_1^2)) m^{14} + 2u_1 (-10(s_1 + t_1)^2 u_1^4 + (2s_1^4 - 16t_1 s_1^3 + 71t_1^2 s_1^2 \\
 & - 16t_1^3 s_1 + 2t_1^4) u_1^2 + s_1 t_1 (-2s_1^4 + 3t_1 s_1^3 - 22t_1^2 s_1^2 + 3t_1^3 s_1 - 2t_1^4)) m^{12} \\
 & + (- (16s_1^2 + 7t_1 s_1 + 16t_1^2) u_1^6 + 2(6s_1^4 - 31t_1 s_1^3 + 109t_1^2 s_1^2 - 31t_1^3 s_1 + 6t_1^4) u_1^4 \\
 & - s_1 t_1 (3s_1^4 + 16t_1 s_1^3 + 20t_1^2 s_1^2 + 16t_1^3 s_1 + 3t_1^4) u_1^2 - 2s_1^2 t_1^2 (2s_1^4 + 7t_1 s_1^3 - 10t_1^2 s_1^2 \\
 & + 7t_1^3 s_1 + 2t_1^4)) m^{10} + u_1 ((-4s_1^2 + 3t_1 s_1 - 4t_1^2) u_1^6 + (12s_1^4 - 28t_1 s_1^3 + 159t_1^2 s_1^2 \\
 & - 28t_1^3 s_1 + 12t_1^4) u_1^4 + s_1 t_1 (5s_1^4 - 16t_1 s_1^3 - 45t_1^2 s_1^2 - 16t_1^3 s_1 + 5t_1^4) u_1^2 - s_1^2 t_1^2 \\
 & \times (3s_1^4 + 5t_1 s_1^3 - 12t_1^2 s_1^2 + 5t_1^3 s_1 + 3t_1^4)) m^8 + (3s_1 t_1 u_1^8 + (4s_1^4 + 55t_1^2 s_1^2 + 4t_1^4) \\
 & \times u_1^6 + s_1 t_1 (3s_1^4 - 16t_1 s_1^3 - 87t_1^2 s_1^2 - 16t_1^3 s_1 + 3t_1^4) u_1^4 + s_1 t_1 (2s_1^6 - t_1 s_1^5 + 21t_1^2 s_1^4 \\
 & - 15t_1^3 s_1^3 + 21t_1^4 s_1^2 - t_1^5 s_1 + 2t_1^6) u_1^2 + s_1^3 (s_1 - t_1)^2 t_1^3 (2s_1 + t_1) (s_1 + 2t_1)) m^6 \\
 & + s_1 t_1 u_1 (u_1^8 + (2s_1^2 + 3t_1 s_1 + 2t_1^2) u_1^6 - (s_1^4 + 12t_1 s_1^3 + 59t_1^2 s_1^2 + 12t_1^3 s_1 + t_1^4) u_1^4 \\
 & + (2s_1^6 - 7t_1 s_1^5 + 24t_1^2 s_1^4 - 7t_1^3 s_1^3 + 24t_1^4 s_1^2 - 7t_1^5 s_1 + 2t_1^6) u_1^2 - s_1^2 (s_1 - t_1)^2 \\
 & \times t_1^2 (s_1^2 + t_1 s_1 + t_1^2)) m^4 - s_1^2 t_1^2 u_1^2 (3u_1^6 + (2s_1^2 + 13t_1 s_1 + 2t_1^2) u_1^4 \\
 & + (5s_1^4 - 13t_1 s_1^3 - 7t_1^2 s_1^2 - 13t_1^3 s_1 + 5t_1^4) u_1^2 + s_1^2 (s_1 - t_1)^2 t_1^2) m^2 \\
 & \left. + s_1^3 t_1^3 (s_1^2 + t_1 s_1 + t_1^2) u_1^3 ((s_1 - t_1)^2 + 3u_1^2) \right\}
 \end{aligned}$$

$$\langle 0 | \mathcal{O}_1^{J/\psi} ({}^{2S+1}S_J) | 0 \rangle = \frac{N_c}{2\pi} (2J + 1) |R_0(0)|^2,$$

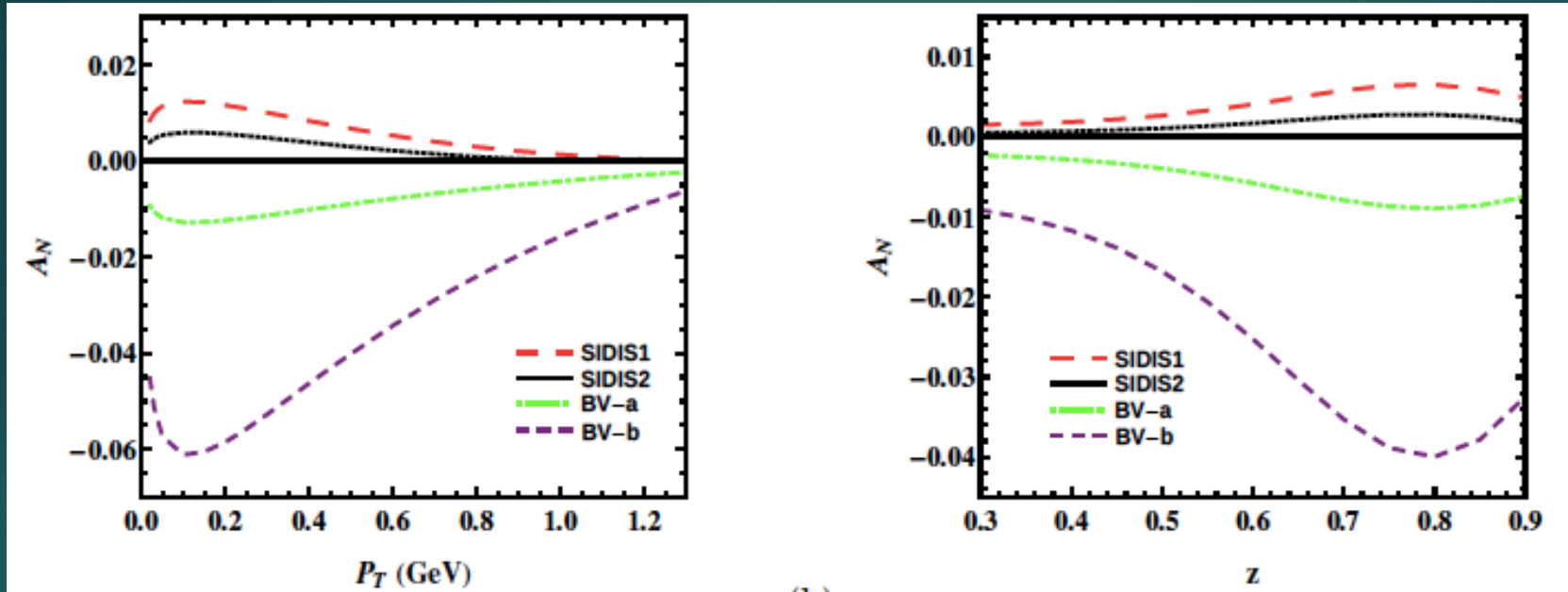
$$\langle 0 | \mathcal{O}_8^{J/\psi} ({}^{2S+1}S_J) | 0 \rangle = \frac{2}{\pi} (2J + 1) |R_0(0)|^2,$$

$$\langle 0 | \mathcal{O}_8^{J/\psi} ({}^3P_J) | 0 \rangle = \frac{2N_c}{\pi} (2J + 1) |R'_1(0)|^2.$$

S. Rajesh, Raj Kishore, AM
PRD 98, 014007 (2018)

Numerical Results

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SSA at EIC

$$\sqrt{s} = 45 \text{ GeV}$$

Integration ranges :

$$0 < P_T < 1 \text{ GeV}$$

$$0.3 < z < 0.9$$

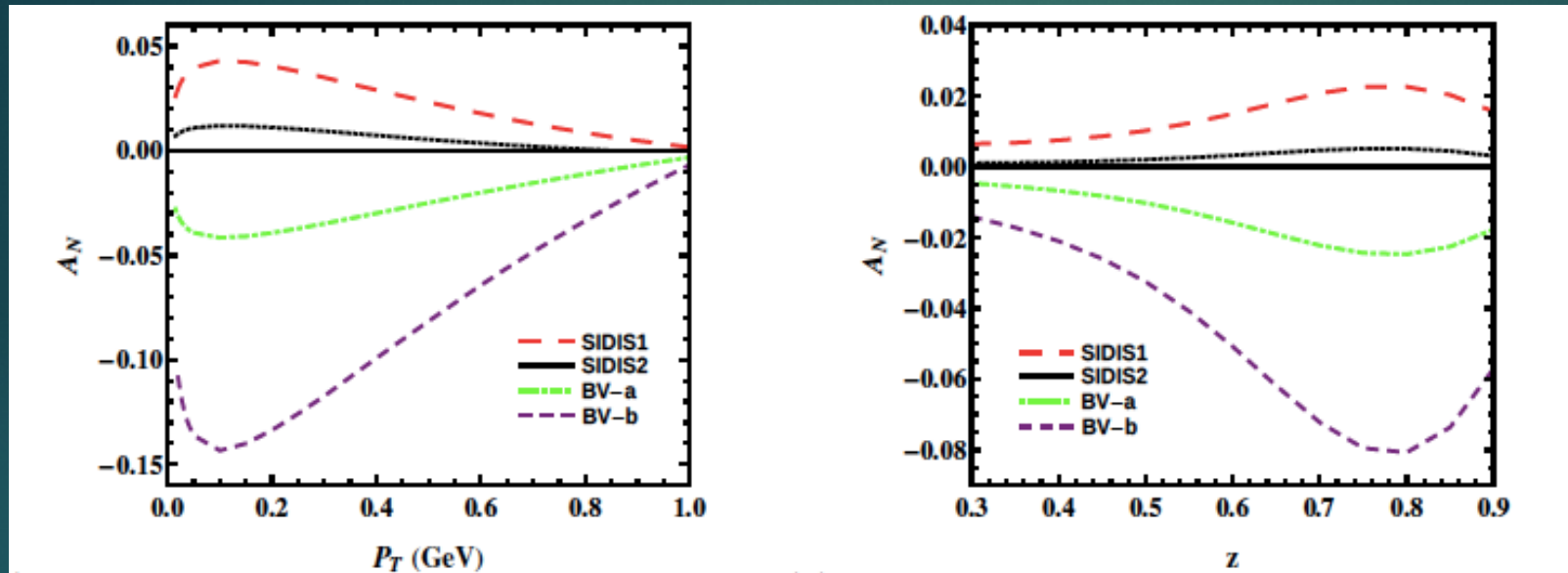
SSA increases by a maximum of 30 % if CS is not included in the denominator

SSA using LDMEs from Chao et al, PRL 108, 242004 (2012) and Zhang et al, PRL 114, 092006 (2015) are similar in magnitude

LDMEs of Butenschoen and Kniehl, PRD 84, 051501 (2011) give smaller asymmetry

Numerical Results

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SSA at COMPASS

$$\sqrt{s} = 17.2 \text{ GeV}$$

Integration ranges :

$$0 < P_T < 1 \text{ GeV}$$

$$0.3 < z < 0.9$$

Size and sign of the asymmetry depends on the parametrization of GSF used

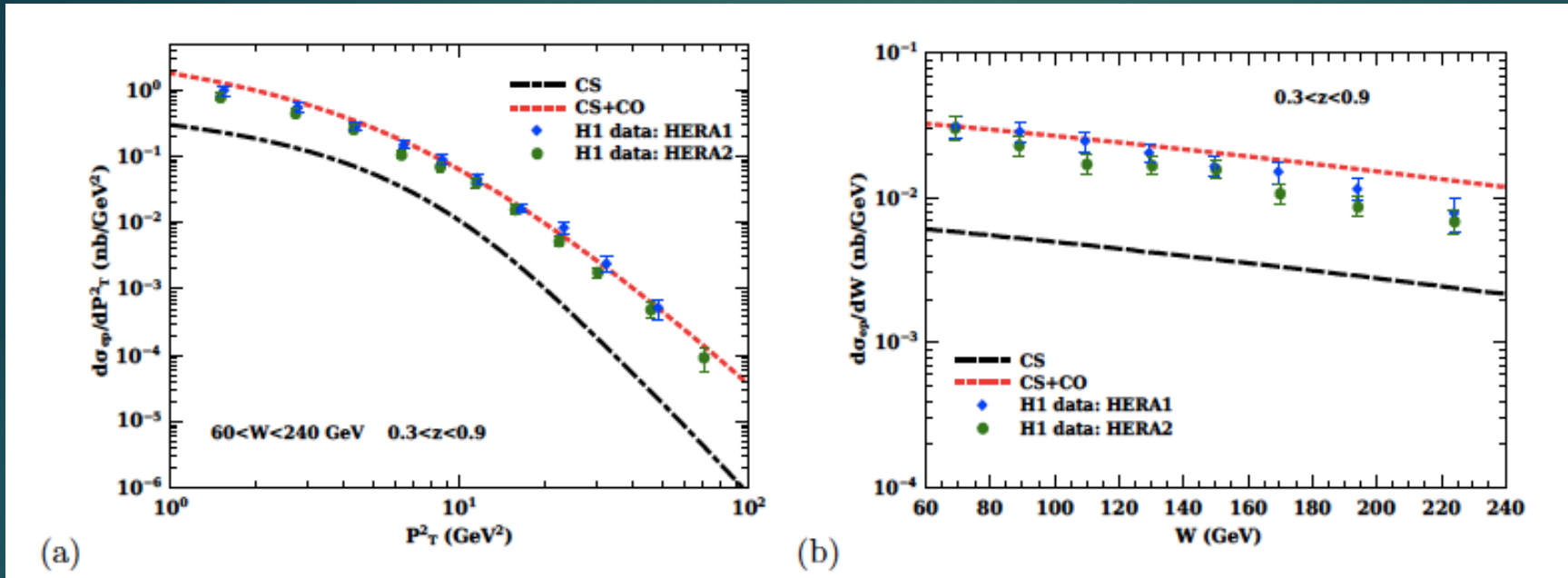
Asymmetry increases slightly for higher values of Gaussian widths of unpolarized TMD

SIDIS-2 gives very small asymmetry

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PRD 98, 014007 (2018)

Cross Section for Unpolarized Process

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Cross section for the process

$$e + p \rightarrow J/\psi + X$$

$$\sqrt{s} = 318 \text{ GeV (HERA)}$$

$$\langle k_{\perp g}^2 \rangle = 1 \text{ (GeV)}^2$$

W is the invariant mass of photon-proton system

$$1 < P_T < 10 \text{ GeV}, 60 < W < 240 \text{ GeV}, 0.3 < z < 0.9$$

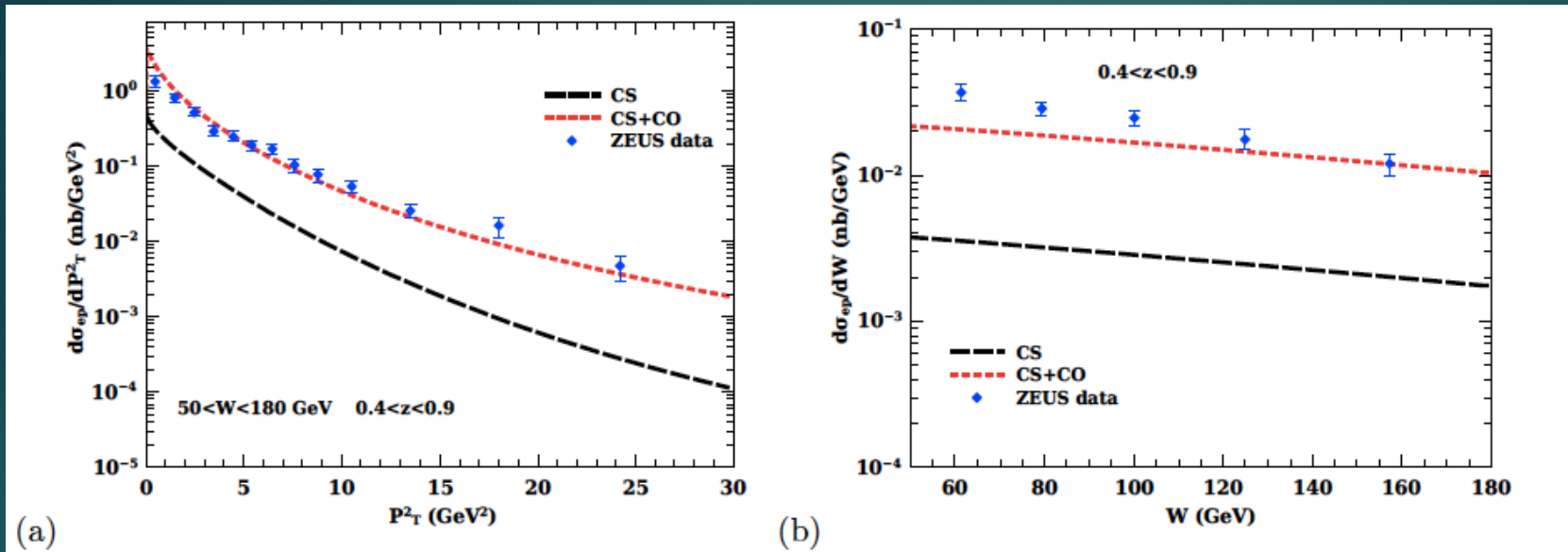
Data from H1 collaboration, EPJC 25, 25 (2002); EPJC 68, 401 (2010)

LDMEs from Zhang et al, PRL 114, 092006 (2015)

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Cross Section for Unpolarized Process

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Cross section for the process

$$e + p \rightarrow J/\psi + X$$

$$\sqrt{s} = 300 \text{ GeV}$$

$$\langle k_{\perp g}^2 \rangle = 1 \text{ (GeV)}^2$$

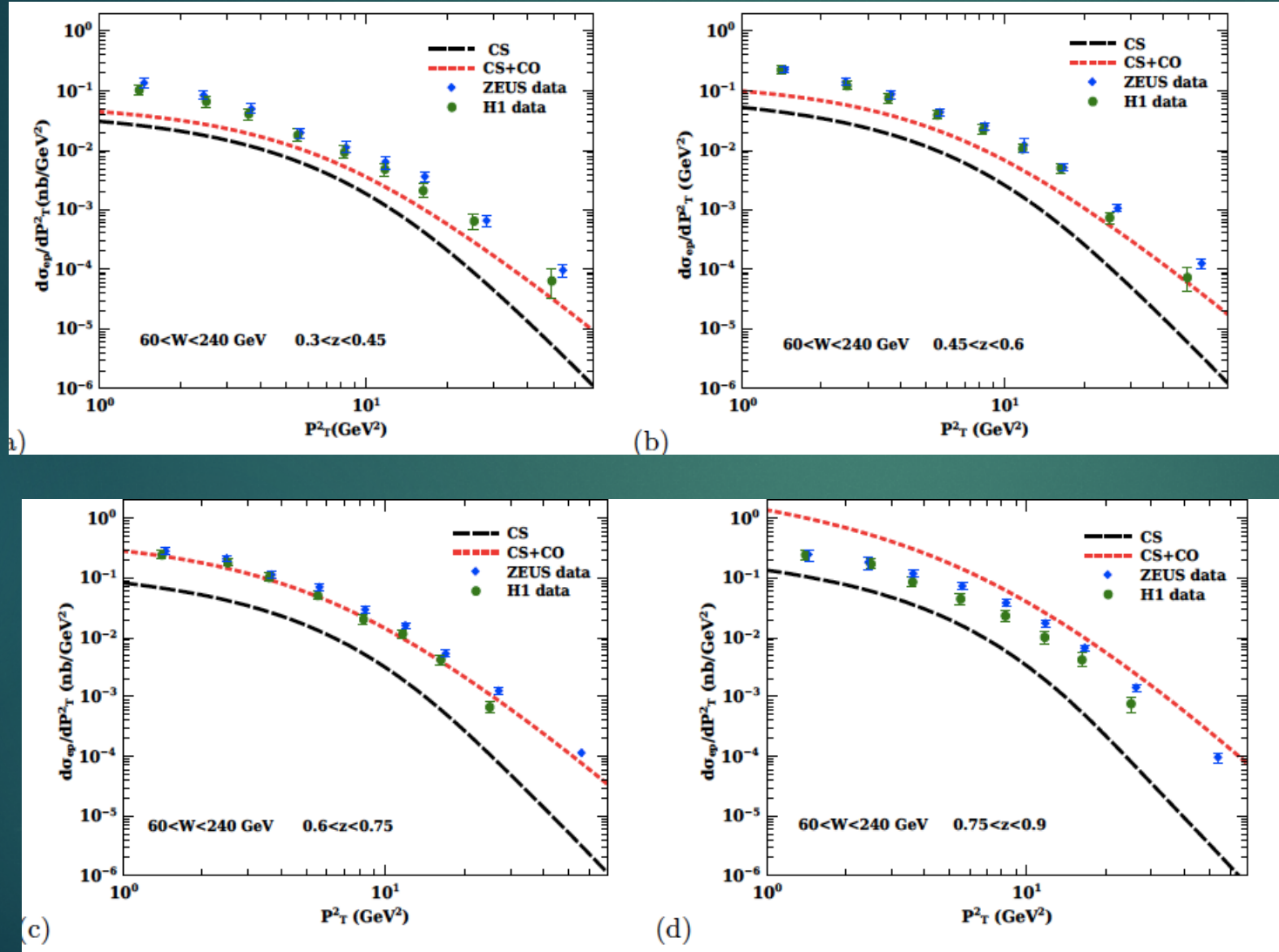
$$1 < P_T < 5 \text{ GeV}; 50 < W < 180 \text{ GeV}, 0.4 < z < 0.9$$

Data from ZEUS Collaboration, EPJC 27, 173 (2003)

LDMEs from Zhang et al, PRL 114, 092006 (2015)

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CS vs CO contribution



$$\sqrt{s} = 318 \text{ GeV}$$

$$\langle k_{\perp g}^2 \rangle = 1 \text{ (GeV)}^2$$

Data from

H1 collaboration,
EPJC 68, 401 (2010)

ZEUS Collaboration,
JHEP 02, 071 (2013)

LDMEs from

Zhang et al, PRL 114, 092006
(2015)

Conclusion

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Single spin asymmetry in J/ψ production in ep collision provides a direct way to access the GSF through the LO photon-gluon process

Sizable negative Sivers asymmetry in color octet model, agrees with COMPASS result

Inclusive photoproduction of J/ψ : wider kinematical region accessible to colliders like EIC

NRQCD based color octet model gives sizable SSA that can access GSF

Size and sign of the SSA depends strongly on the parametrization of the GSF

Theoretical calculation of the cross section using TMDs describe the HERA data well when both CS and CO contributions are taken into account