



WAYNE STATE  
UNIVERSITY



U.S. DEPARTMENT OF  
**ENERGY**

Office of Science



# Jets and event generation in AA and at an EIC

Abhijit Majumder

# Outline

- Some theory background
- Phenomenology
- Results from JETSCAPE for A-A
- What is needed for an eA generator.

# Basic Setup (Vacuum)

- Factorization, Single log resummation:

$$D(z) = \delta(1 - z) + \frac{\alpha_S}{2\pi} P(y) \left[ \frac{1}{\epsilon} + \gamma - \log(4\pi) + \log\left(\frac{Q^2}{\mu^2}\right) \right]$$

- Evolution equation for fragmentation function

$$\frac{dD(z, Q^2)}{dQ^2} = \frac{\alpha_S}{2\pi Q^2} \int_z^1 \frac{dy}{y} P(y) D\left(\frac{z}{y}, Q^2\right)$$

- Or simulate shower by deriving a Sudakov form factor.

$$S(Q^2, \mu_0^2) = e^{-\int_{\mu_0^2}^{Q^2} \frac{d\mu^2}{\mu^2} \frac{\alpha_S(\mu^2)}{2\pi} \int_{\mu_0^2/\mu^2}^{1-\mu_0^2/\mu^2} dy \hat{P}(y)}$$

# Basic setup: concept of distance

- In a pure vacuum calculation, knowing the location of a split is not important
- Becomes very important in a medium
- Need a mechanism of generating locations of splits even in a vacuum simulation.
- Simulated: MATTER simulator

# Uncertainty analysis

In light-cone components, the wavefunction is

$$\psi(q) e^{iq^- y^+} e^{iq^+ y^-} e^{-iq_\perp y_\perp}$$

one needs to keep track of  $y^-$

in probability of parton, phase from amplitude and c.c.

$$\left[ e^{iq^- y^+} e^{iq^+ y^-} e^{-iq_\perp y_\perp} \right] \left[ e^{-iq'^- y'^+} e^{-iq'^+ y'^-} e^{ik'_\perp y'_\perp} \right]$$

focussing only on  $q^+$

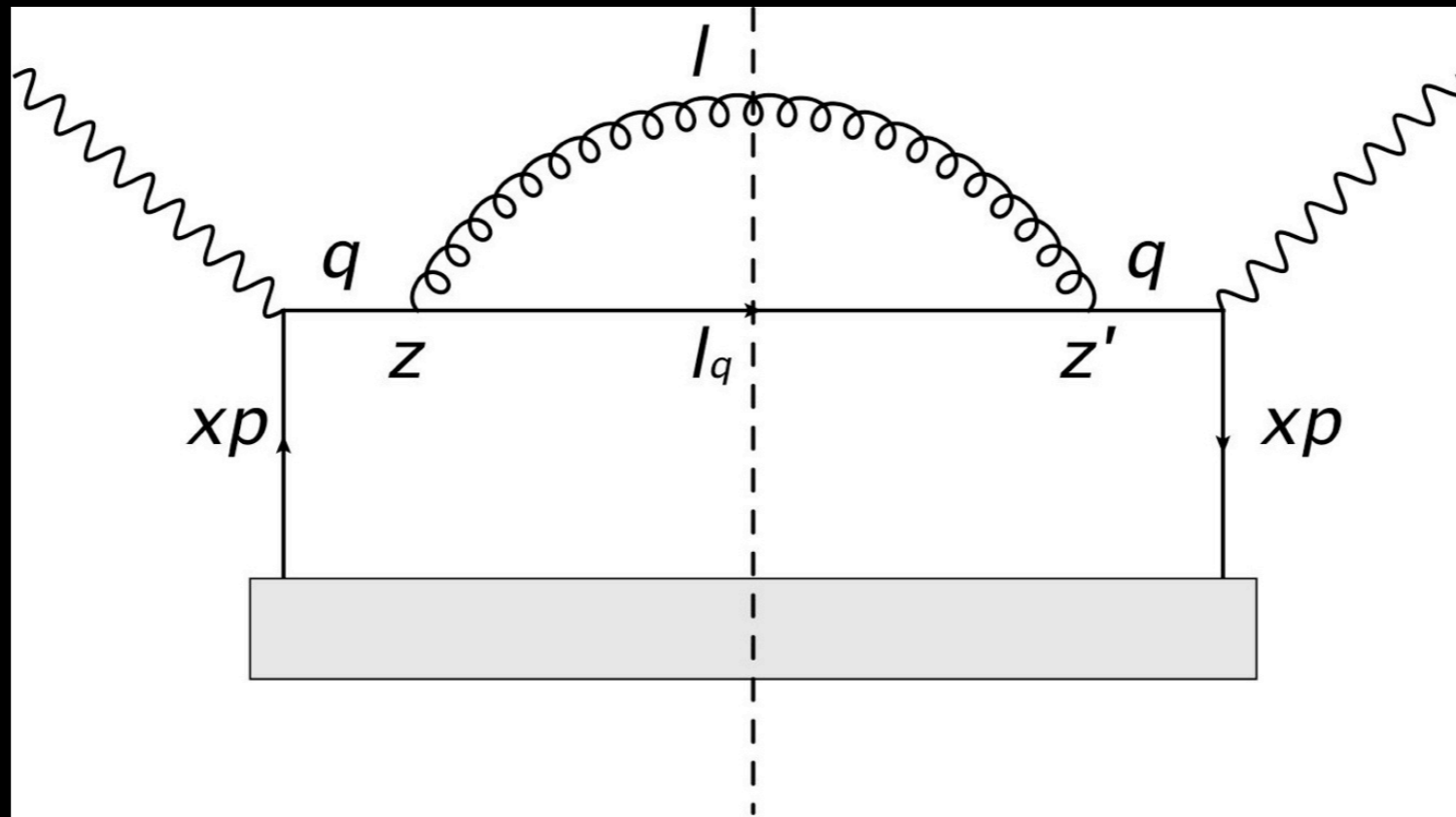
$$e^{i\bar{q}^+ \delta y^-} e^{i\delta q^+ \bar{y}^-}$$

(-) direction



Use hard emissions to denote the parton's length travelled

# Consider one emission and $q^+$



$$\bar{z} = \frac{z + z'}{2}$$

$$\delta z = z - z'$$

what is the role of  $z$  and  $z'$  ?

$$\int_0^\infty d^4 \bar{z} \exp [i(\delta q) \bar{z}] \int d^4 \delta z \exp [i\delta z (l + l_q - q)]$$

$\delta q$  is the uncertainty in  $q$ ,

# How much uncertainty can there be ?

To be sensible:  $\delta q \ll q$

we assume a Gaussian distribution around  $q^+$

And try different functional forms of the width

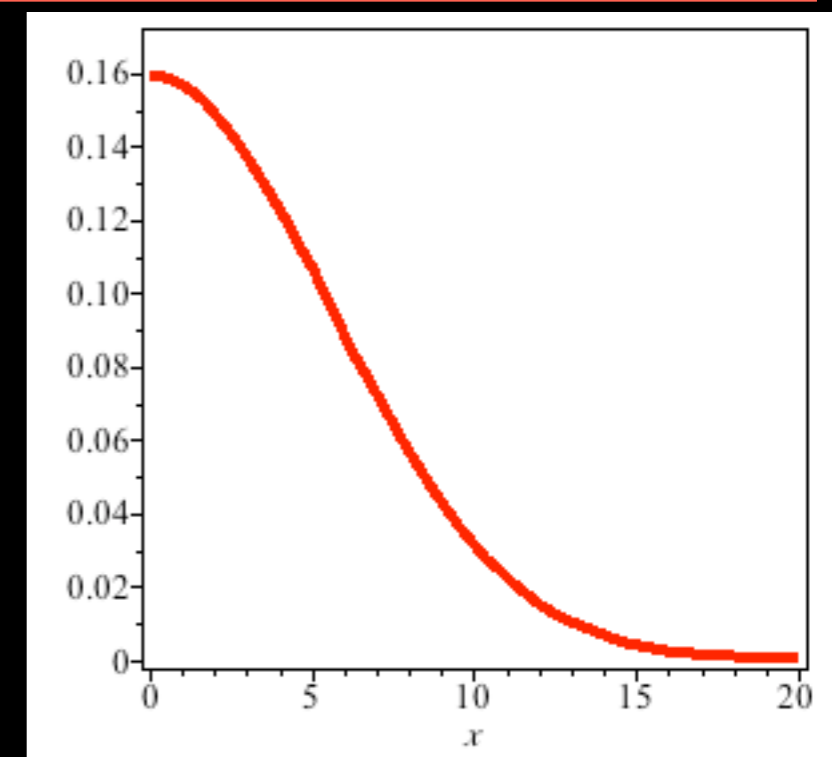
We set the form by insisting  $\langle \tau \rangle = 2q^+ / (Q^2)$

to obtain the  $z^-$  distribution only need to assume a  $\delta q^+$  distribution

$$\rho(\delta q^+) = \frac{e^{-\frac{(\delta q^+)^2}{2[2(q^+)^2/\pi]}}}{\sqrt{2\pi[2(q^+)^2/\pi]}}$$

A normalized Gaussian with  
a variance  $2q^+/\pi$

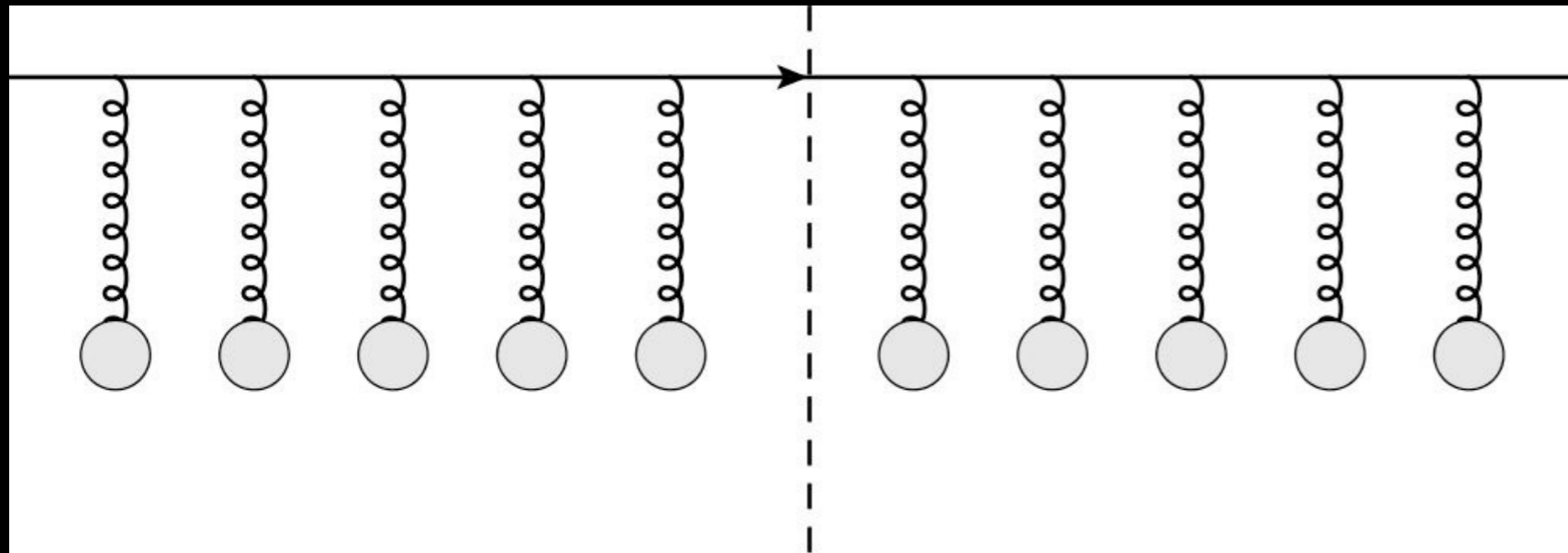
FT gives  
the following  
distribution in  
distance



# Scales of a hard parton in a medium

A parton in a jet shower, has momentum components

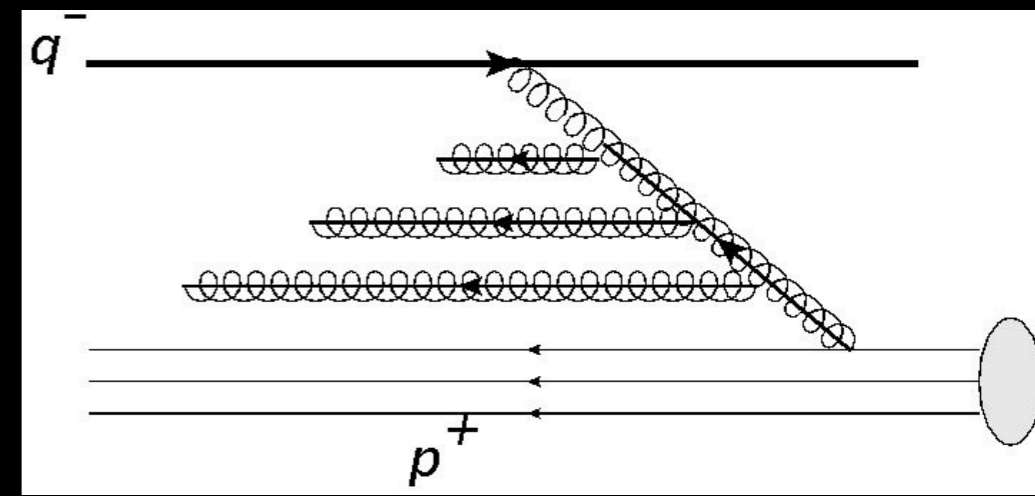
$$q = (q^-, q^+, q_T) = (1, \lambda^2, \lambda)Q, \quad Q: \text{Hard scale}, \quad \lambda \ll 1, \quad \lambda Q \gg \Lambda_{\text{QCD}}$$



hence, gluons have

$$k_{\perp} \sim \lambda Q, \quad k^+ \sim \lambda^2 Q$$

Called Glauber gluons



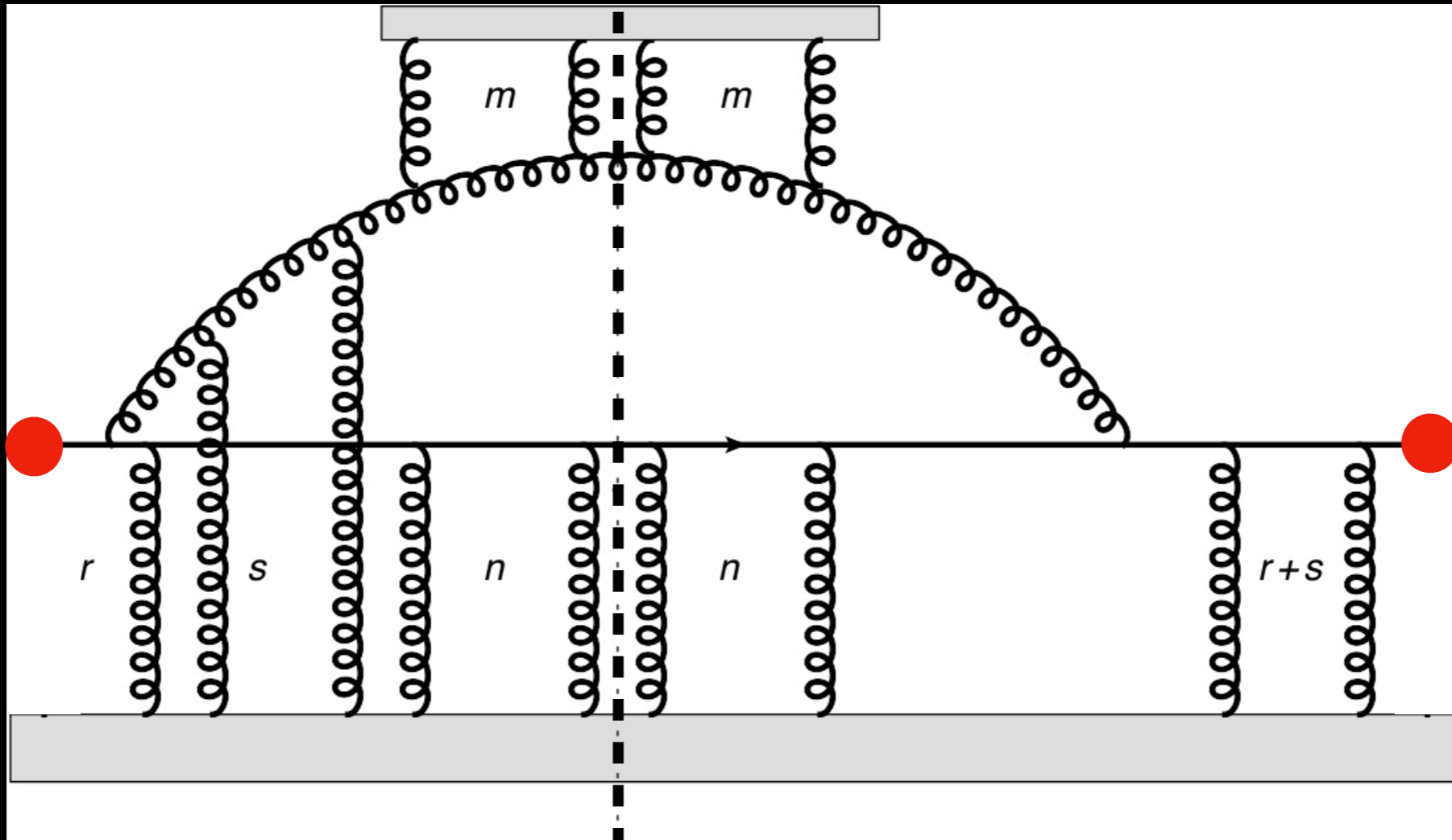


# At large virtuality

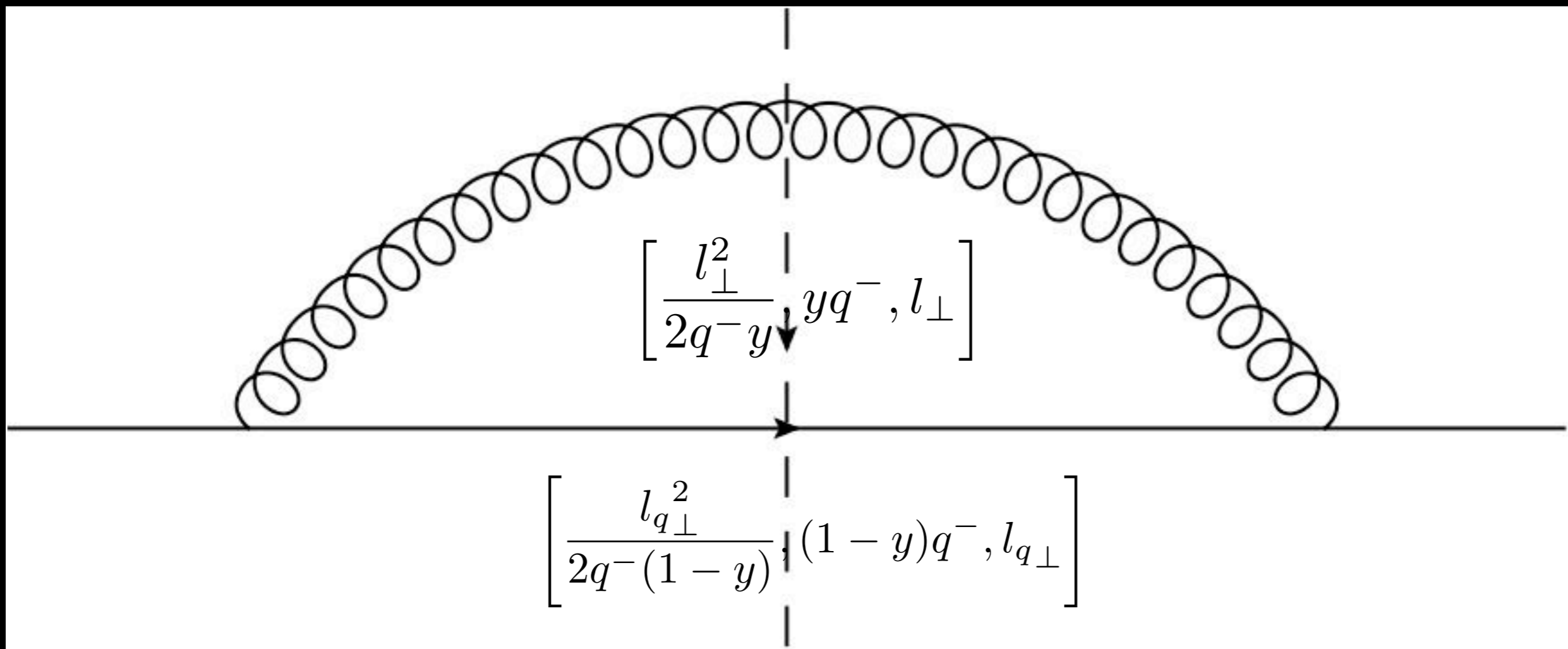
The transverse momentum is resolved  $Q^2 \sim l_{\perp}^2 \sim k_{\perp}^2$   
 at the scale  $Q^2 \gg \hat{q} \tau$

Rare hard scatterings.

$$l_{\perp}^2 \gg \langle k_{\perp}^2 \rangle \sim \hat{q} \tau$$

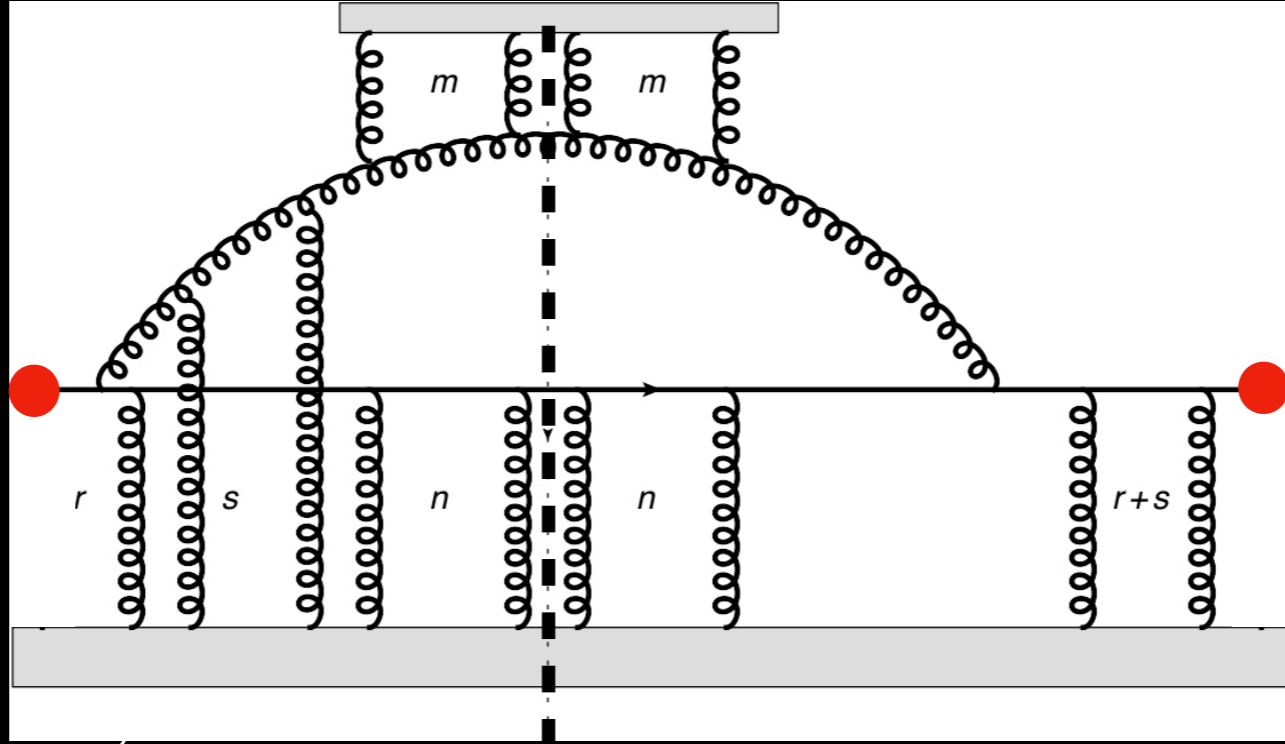


# Case of no scattering



$$\sim \frac{\alpha_s C_F}{2\pi} \int dy d^2 l_{\perp} d^2 l_{q\perp} P(y) \frac{l_{\perp} \cdot l_{\perp}}{l_{\perp}^2 l_{\perp}^2} \delta^2(l_{\perp} + l_{q\perp})$$

# One emission from multiple scattering



$$\int dl_{\perp} dl_{q_{\perp}} dy \text{ C.F. } \delta^2 \left( q_{\perp} + l_{\perp} - \sum_{i=1}^s k_{\perp}^i - \sum_{j=1}^r p_{\perp}^j - \sum_{l=1}^m k_{\perp}^l - \sum_{k=1}^n p_{\perp}^k \right)$$

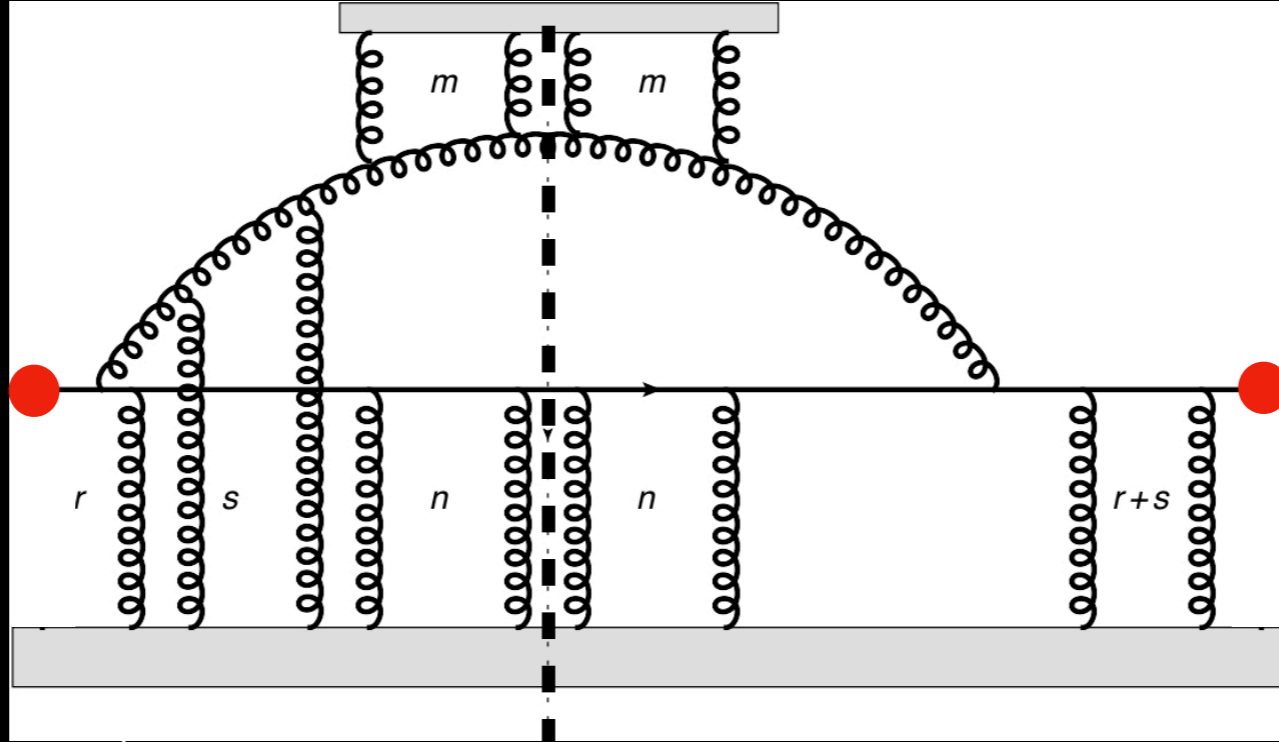
$$\frac{l_{\perp} - \sum_{i=1}^s k_{\perp}^i - \sum_{l=1}^m k_{\perp}^l}{(l_{\perp} - \sum_{i=1}^s k_{\perp}^i - \sum_{l=1}^m k_{\perp}^l)^2} \cdot \frac{l_{\perp} - y \sum_{i=1}^{r+s} k_{\perp}^i - \sum_{l=1}^m k_{\perp}^l}{(l_{\perp} - y \sum_{i=1}^s k_{\perp}^i - \sum_{l=1}^m k_{\perp}^l)^2}$$

$$\prod_{i=1}^N \int dy_i^- \frac{\int d^3 \delta y_i \rho \langle p | A^+(y_i^- + \delta y_i^-, 0) A^+(y_i^-, -\delta y_i^{\perp}) | p \rangle e^{ik_{\perp}^i \delta y_i^{\perp}}}{2p^+(N_c^2 - 1)}$$

$$\left[ \theta(\zeta_I^- - y_E^-) \left\{ e^{-ip^+ x_L y_E^-} - e^{-ip^+ x_L \zeta_I^-} \right\} - \theta(\zeta_I^- - y_I^-) e^{-ip^+ x_L y_I^-} - \theta(y_I^- - \zeta_I^-) e^{-ip^+ x_L \zeta_I^-} \right]$$

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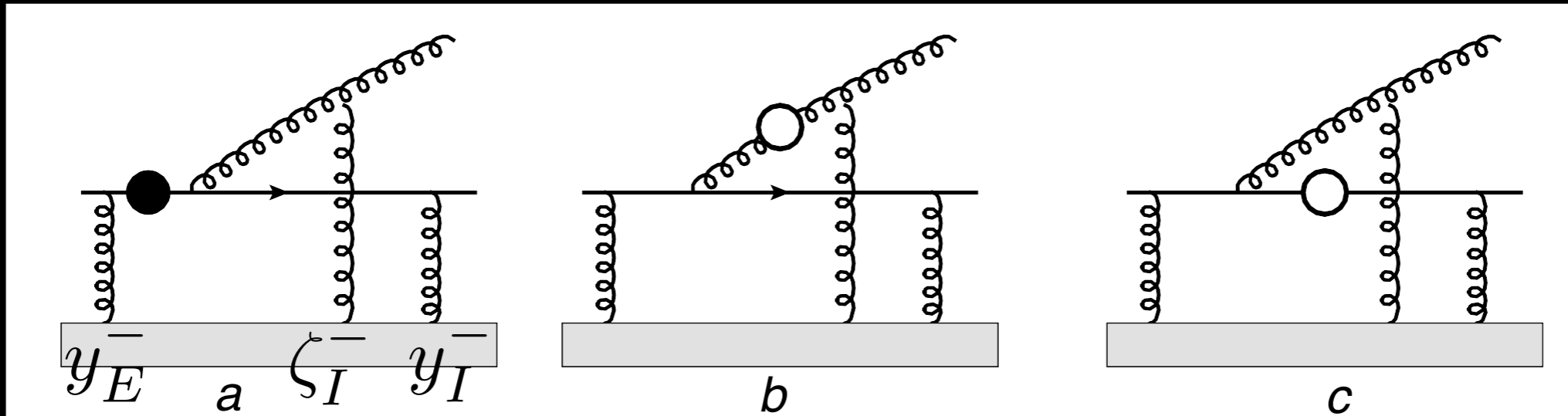
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if  $l_T \gg \langle k_T \rangle$ , can expand in ratio

$$\frac{1}{l_{\perp}^2} - \frac{(1-y+y^2) \left( \sum_{i=1}^s k_{\perp}^i \right)^2}{l_{\perp}^4} - \frac{\left( \sum_{i=1}^m k_{\perp}^i \right)^2}{l_{\perp}^4} + 2(1+y^2) \frac{\left( l_{\perp} \cdot \sum_{i=1}^s k_{\perp}^i \right)^2}{l_{\perp}^6} + 4 \frac{\left( l_{\perp} \cdot \sum_{i=1}^m k_{\perp}^i \right)^2}{l_{\perp}^6}.$$

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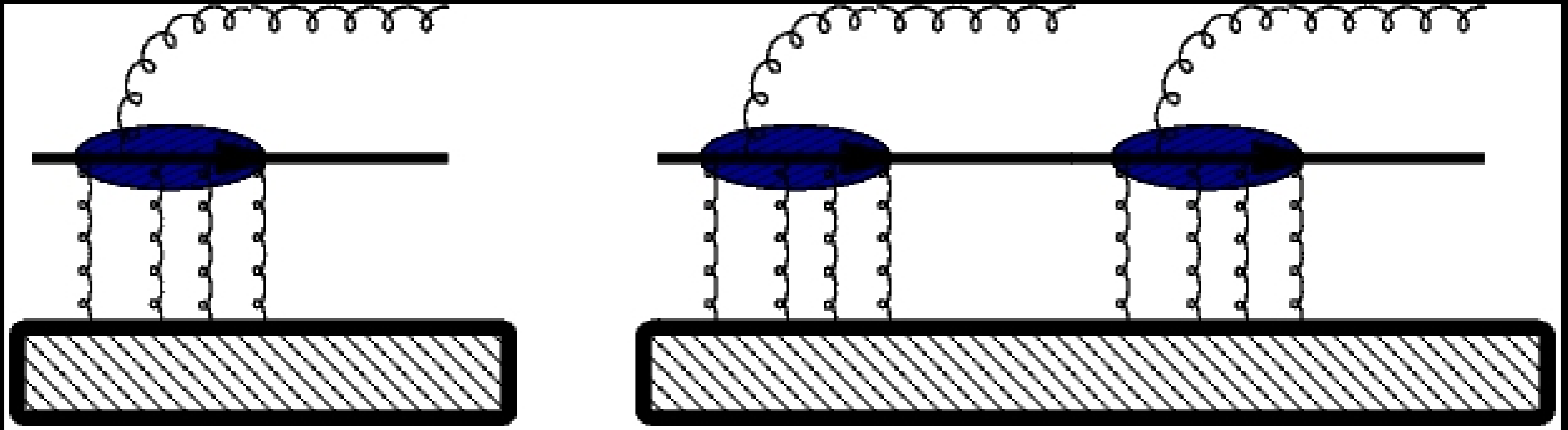
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This is what we mean by vacuum medium interference

Can show that this reduces to the case of single scattering induced single emission as in Wang and Guo Nucl.Phys. A696 (2001) 788-832.

This needs to be repeated as long as  $Q \gg \hat{q}L$



- Usual assumption, multiple emissions are independent!
- The reason for this depends on your approximation scheme
- At next to leading twist, vacuum ordering prevails.

# Resum with DGLAP

Per radiation, with or without scattering

$$\frac{\alpha_S}{2\pi} \int \frac{dl_{\perp}^2}{l_{\perp}^2} \int dy P(y) \left[ 1 + \underbrace{\int_0^{\tau_f} d\zeta \frac{\hat{q}}{l_{\perp}^2}}_{\text{Phase Factors}} \right]$$

No divergence, yields finite term

$$\tau_f = \frac{2Ey(1-y)}{l_{\perp}^2}$$

Resum into Fragmentation function

$$\frac{\alpha_S}{2\pi} \int dy P(y) \left[ \frac{1}{\epsilon} + \gamma - \log(4\pi) + \log\left(\frac{Q^2}{\mu^2}\right) + \hat{q}\# \right]$$

Or, simulate with Sudakov.

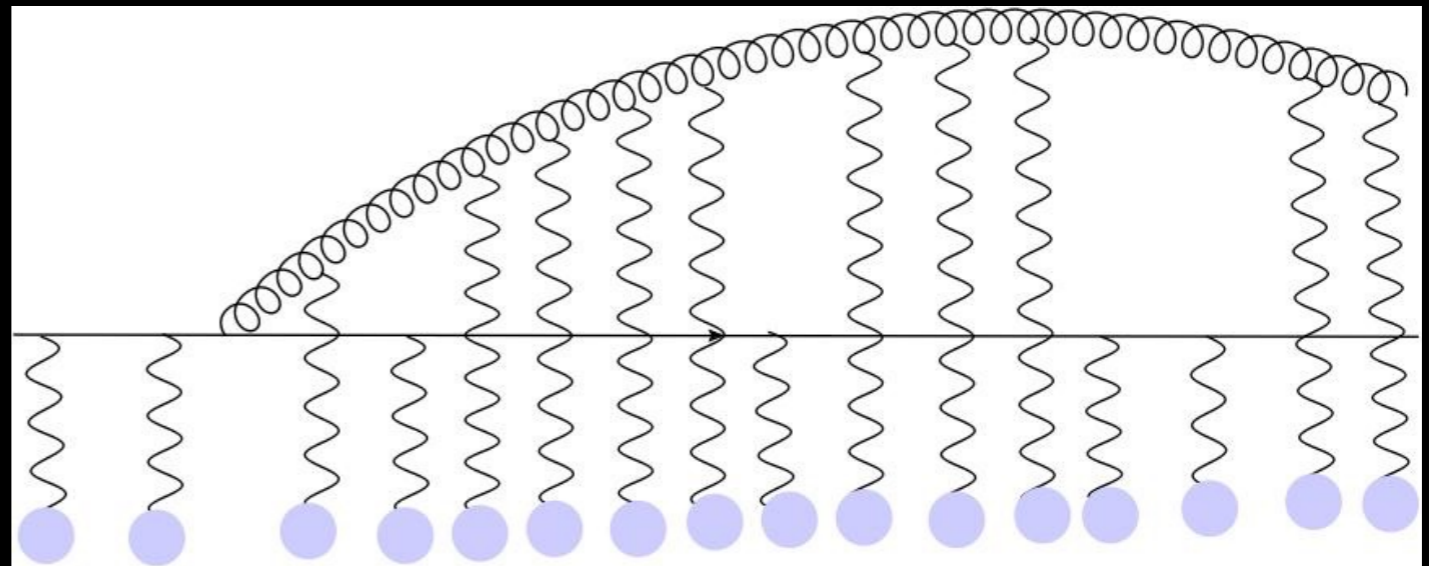
# As virtuality comes down

- High energy partons with virtuality  $Q = \hat{q} \tau$
- Partons with virtuality  $\mu^2 = \lambda^2 Q^2$  have lifetime  $1/(\lambda^2 Q)$
- Over this long lifetime, the parton “can” endure several scatterings
- BDMPS regime
- need a rate equation for multiple emission
- Modeled: LBT, MARTINI



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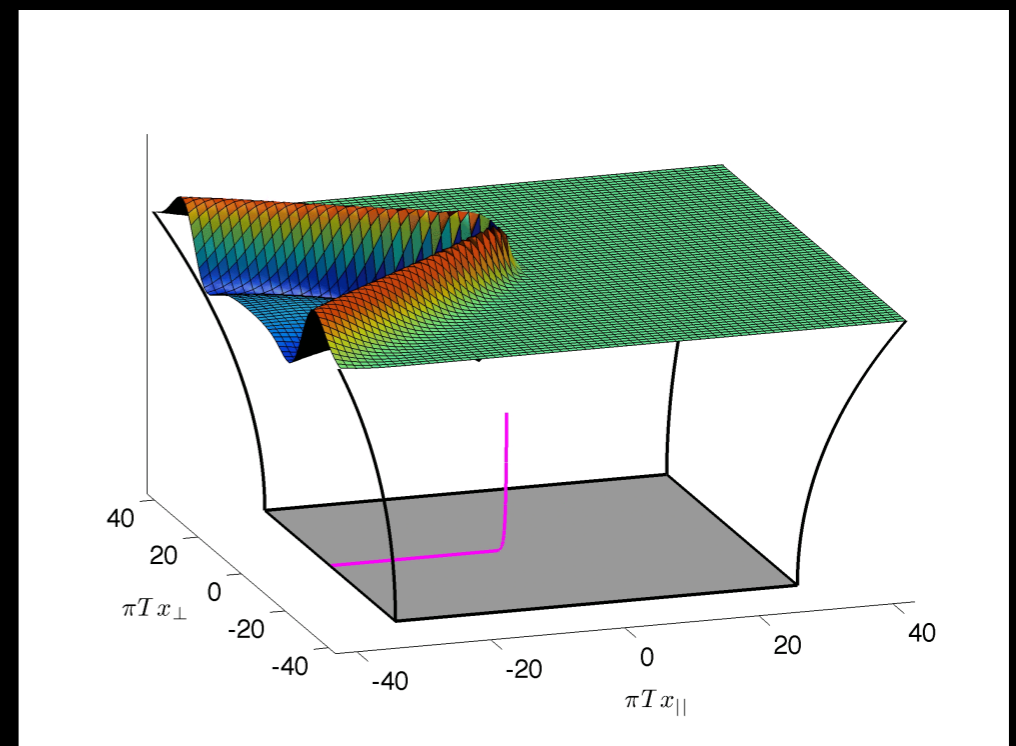
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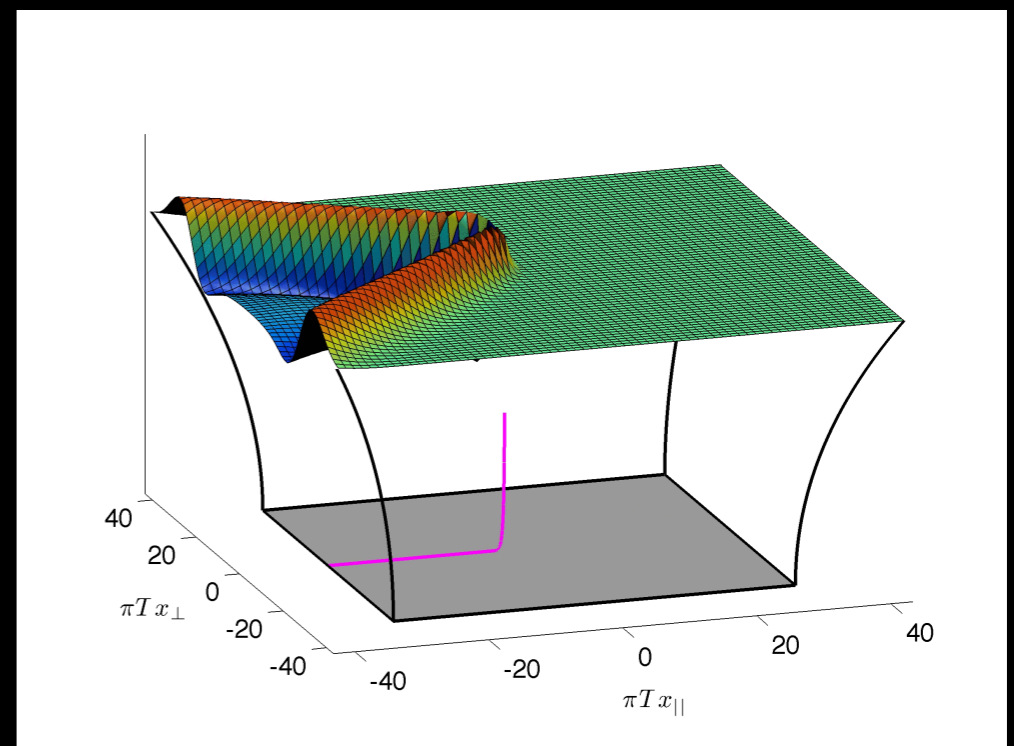




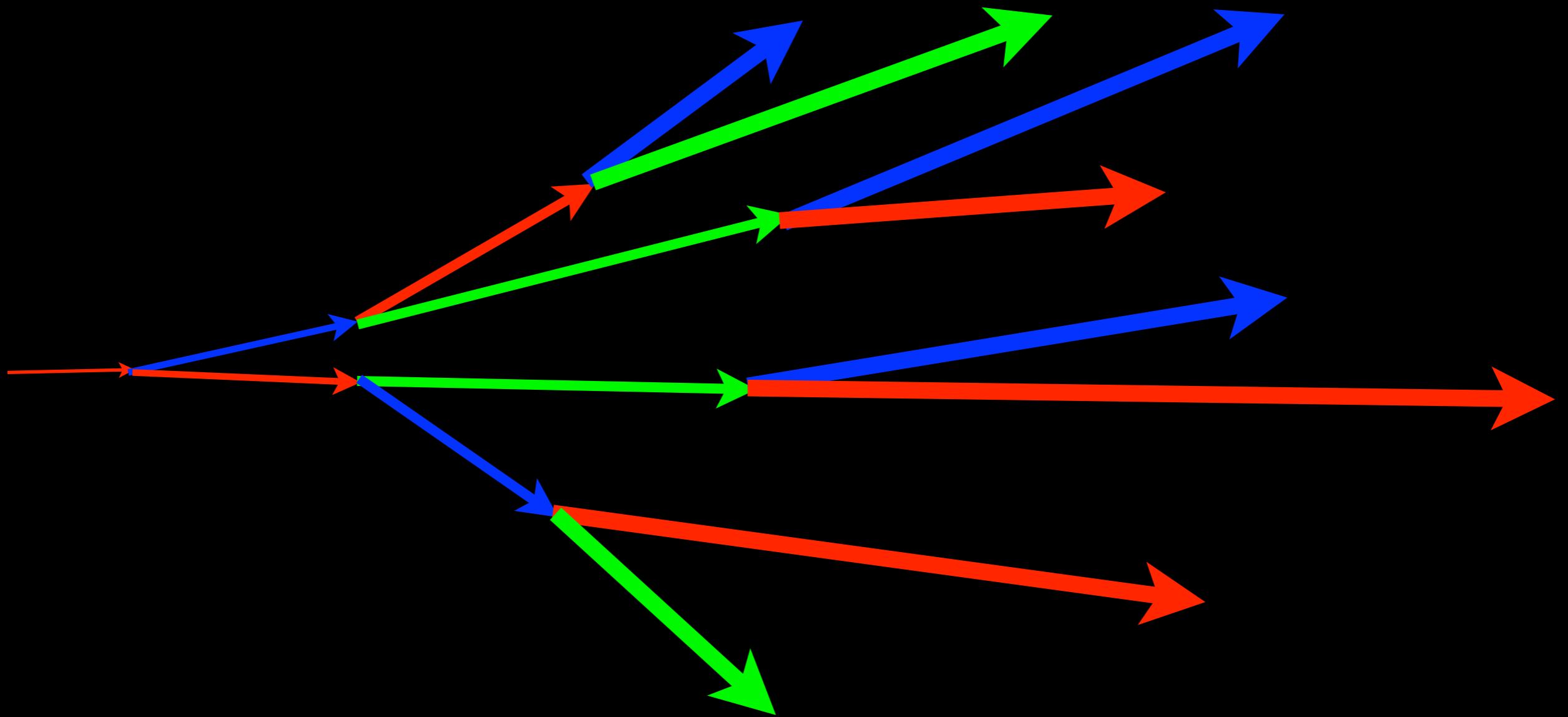
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*P. Chesler, L. Yaffe, W. Horowitz, A. Mueller, E. Iancu,  
J. Casalderrey-Solana, G. Milhano, D. Pablos, K. Rajagopal*

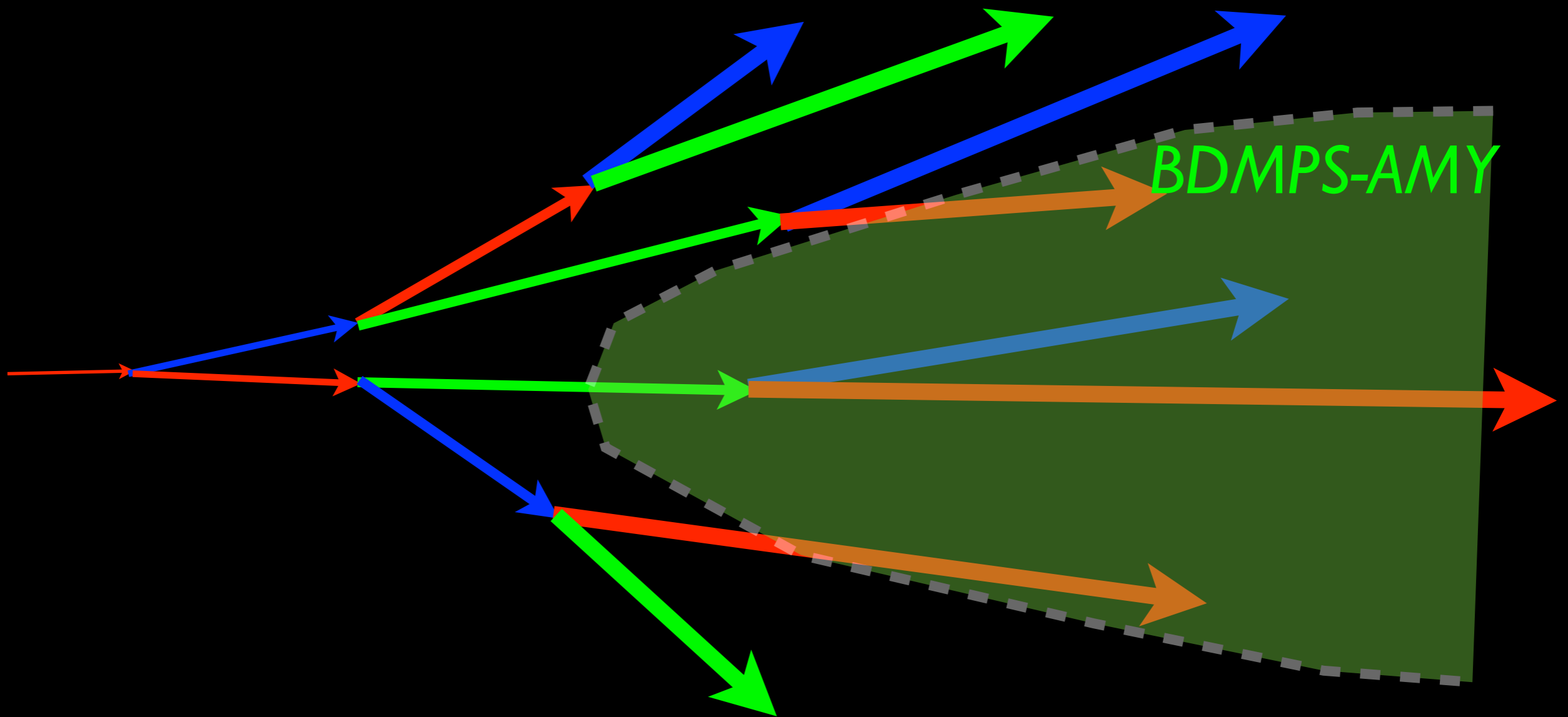


# Grand picture (leading hadrons)



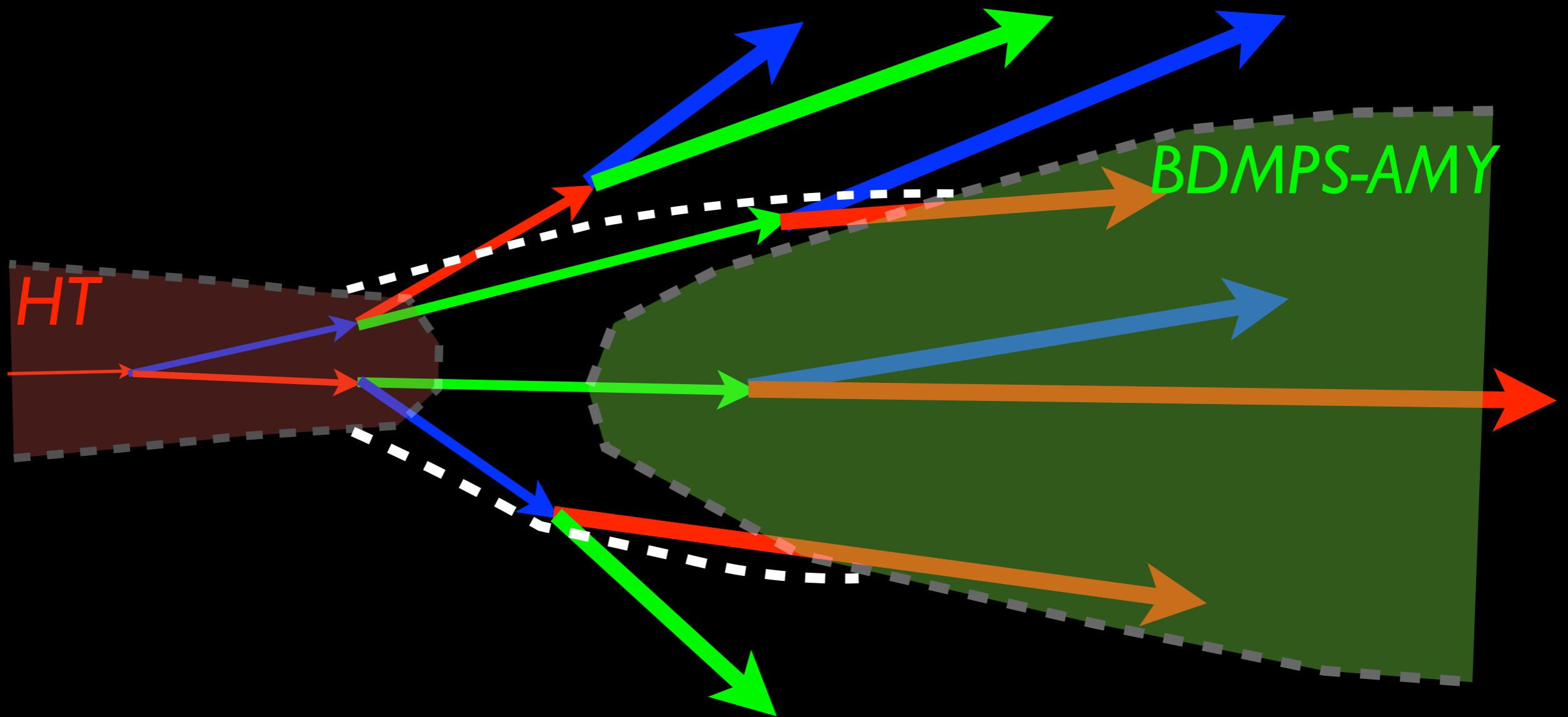
*In a static brick*

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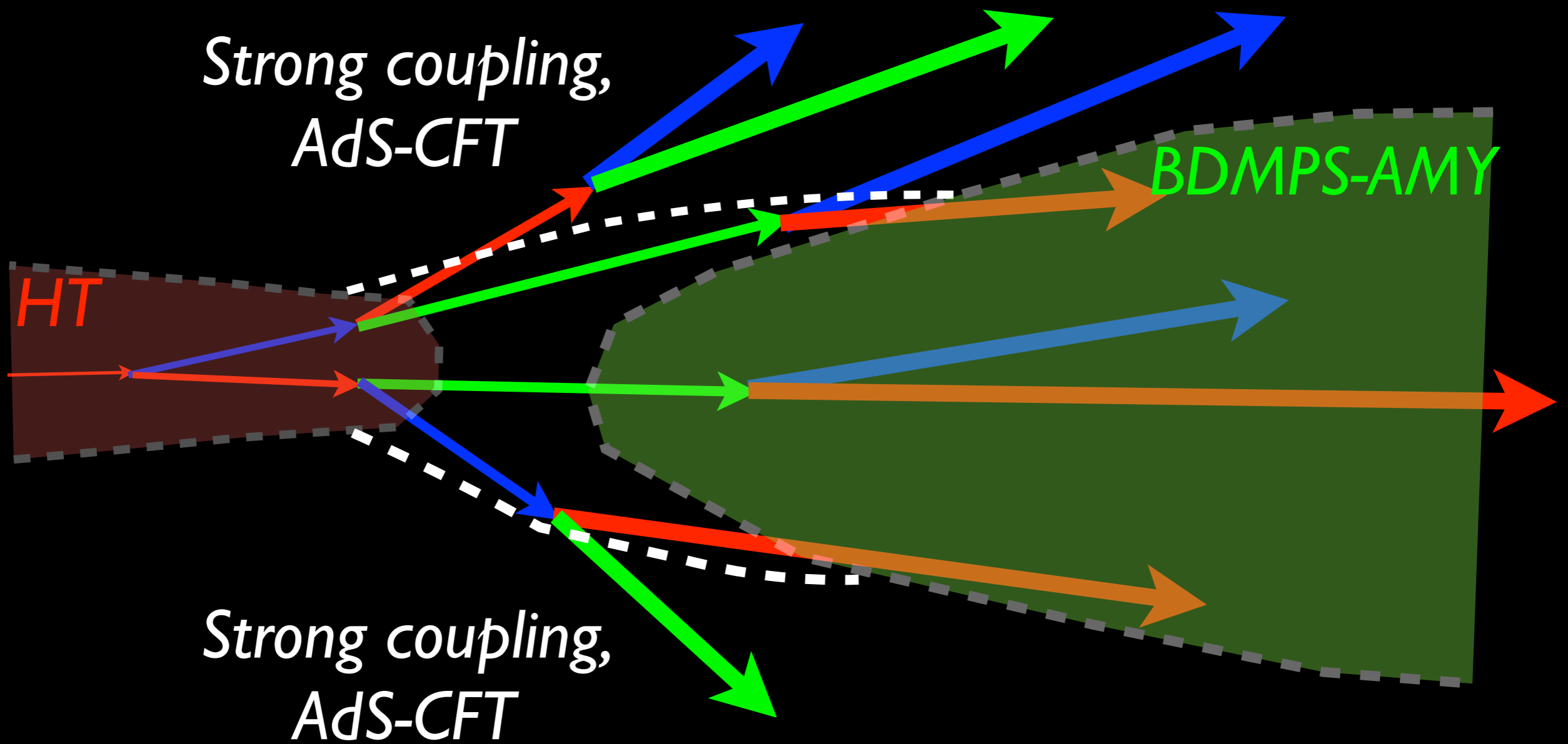
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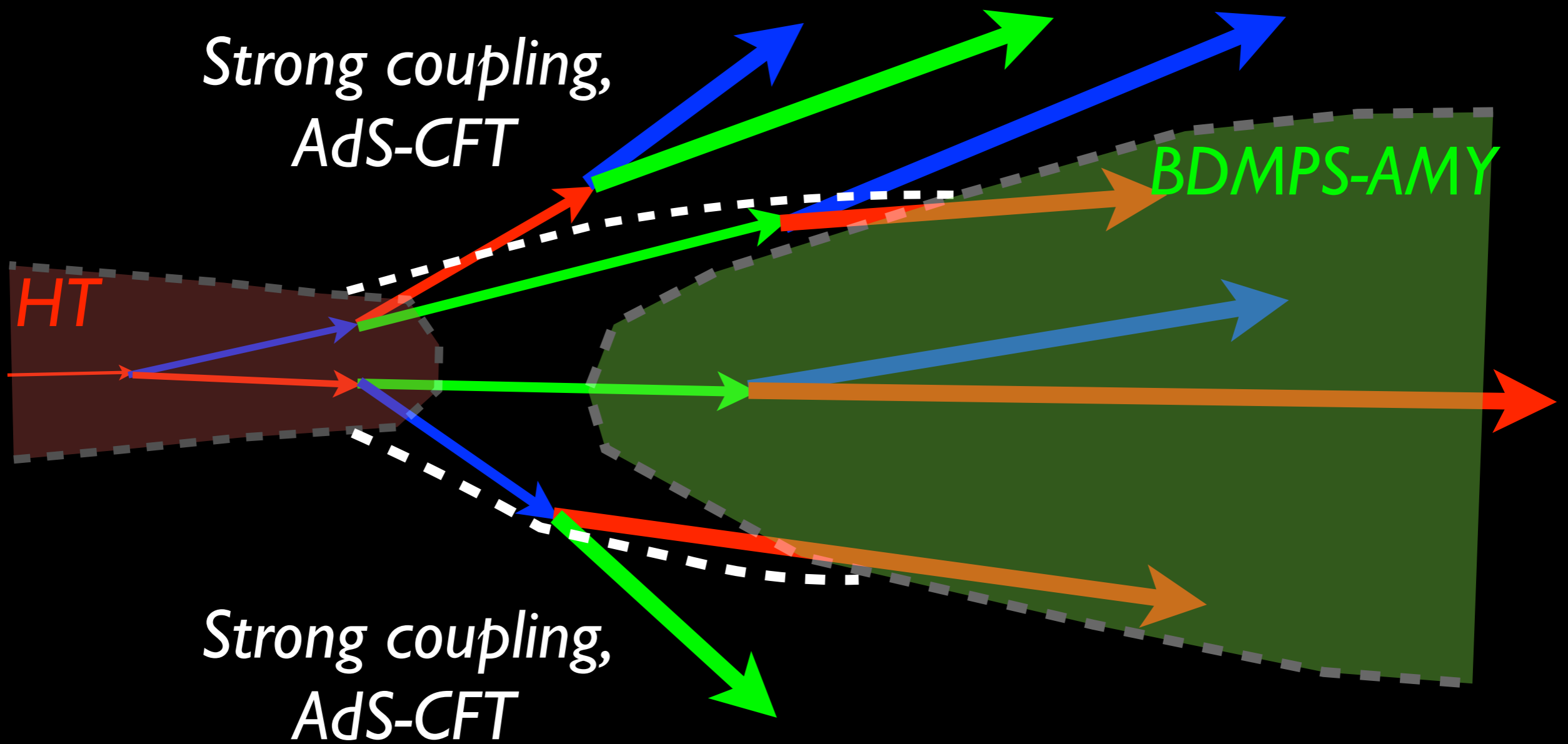
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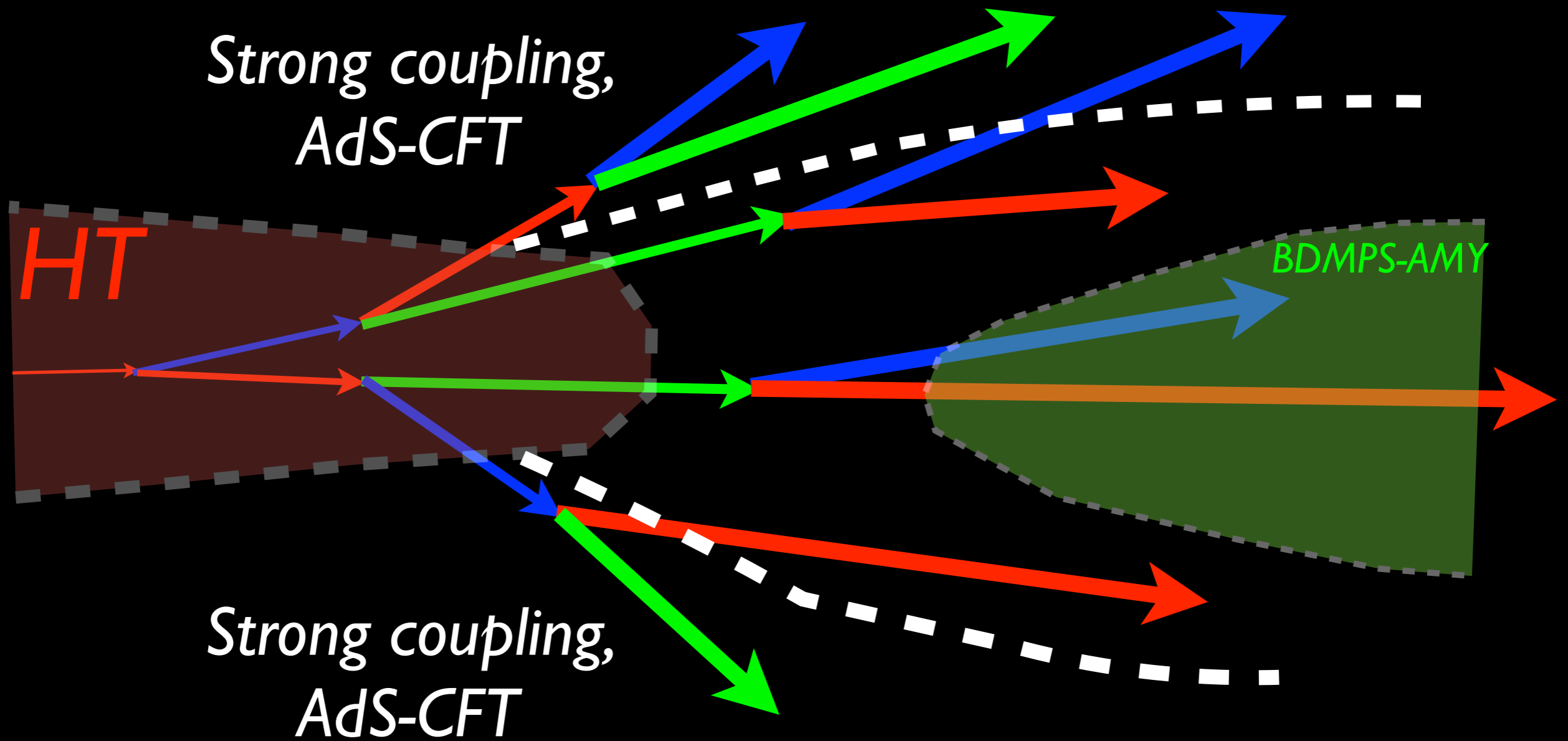
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*In an expanding QGP*

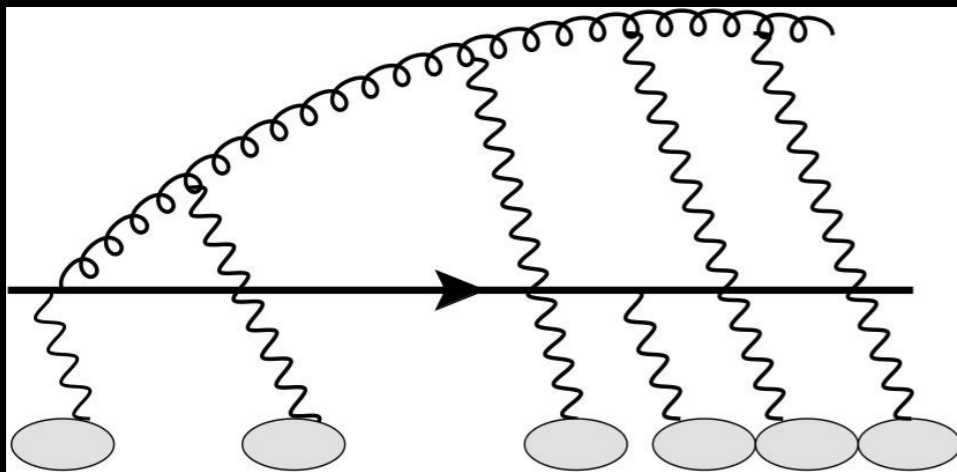
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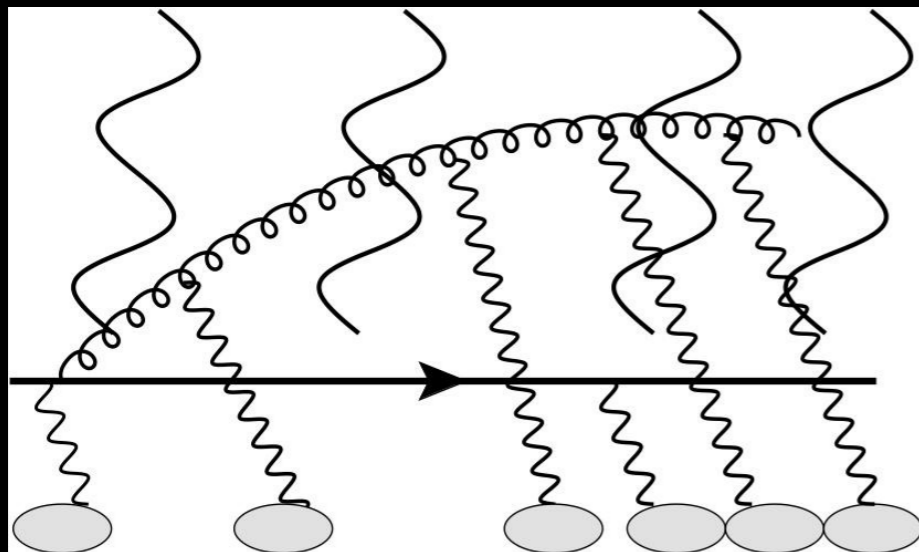
# Energy deposition-thermalization

Drag on a jet is energy dump in a medium  $\hat{e} = \frac{dE}{dx}$



← space-like gluons

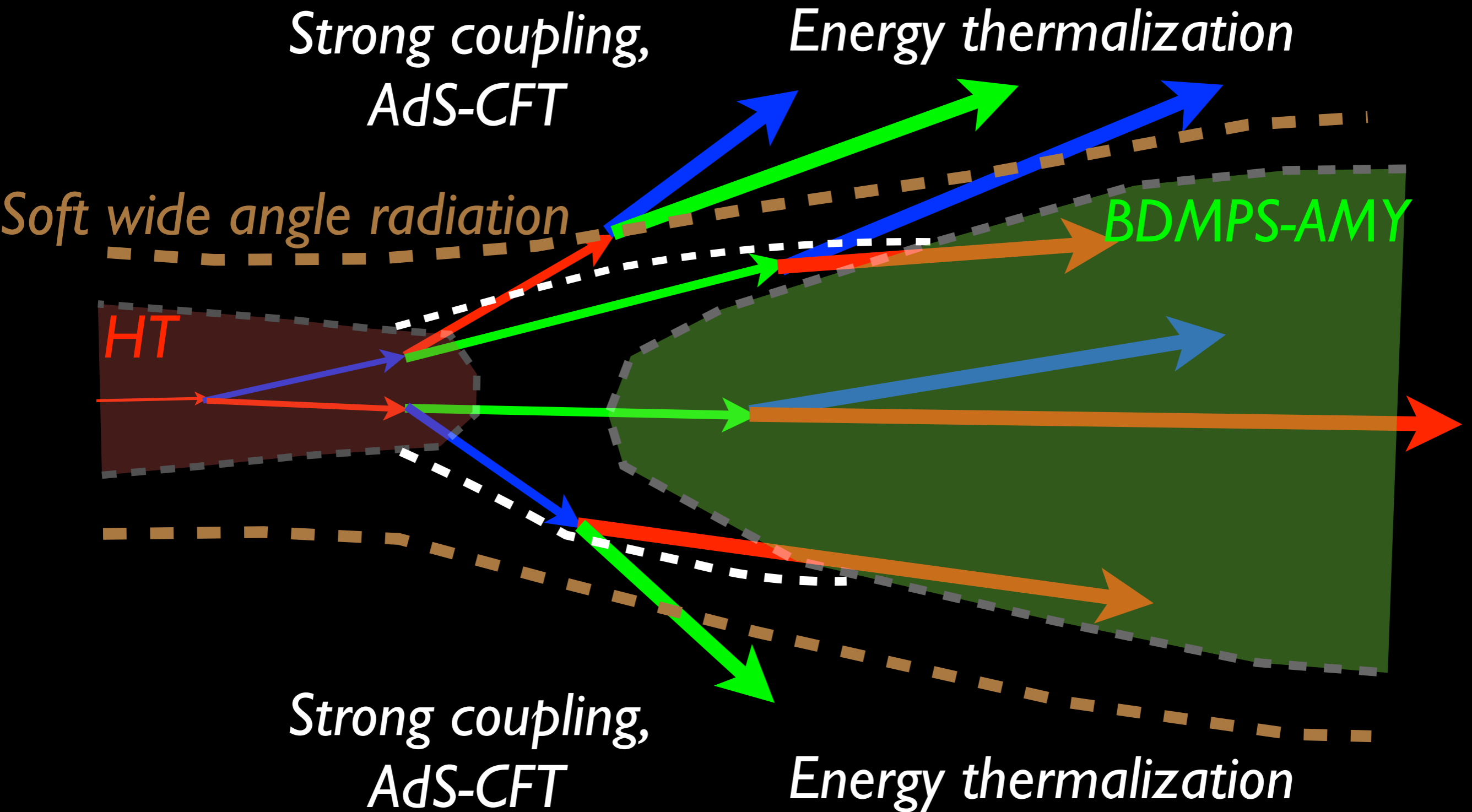
Could also have another component from very soft large angle radiation



← time-like gluons

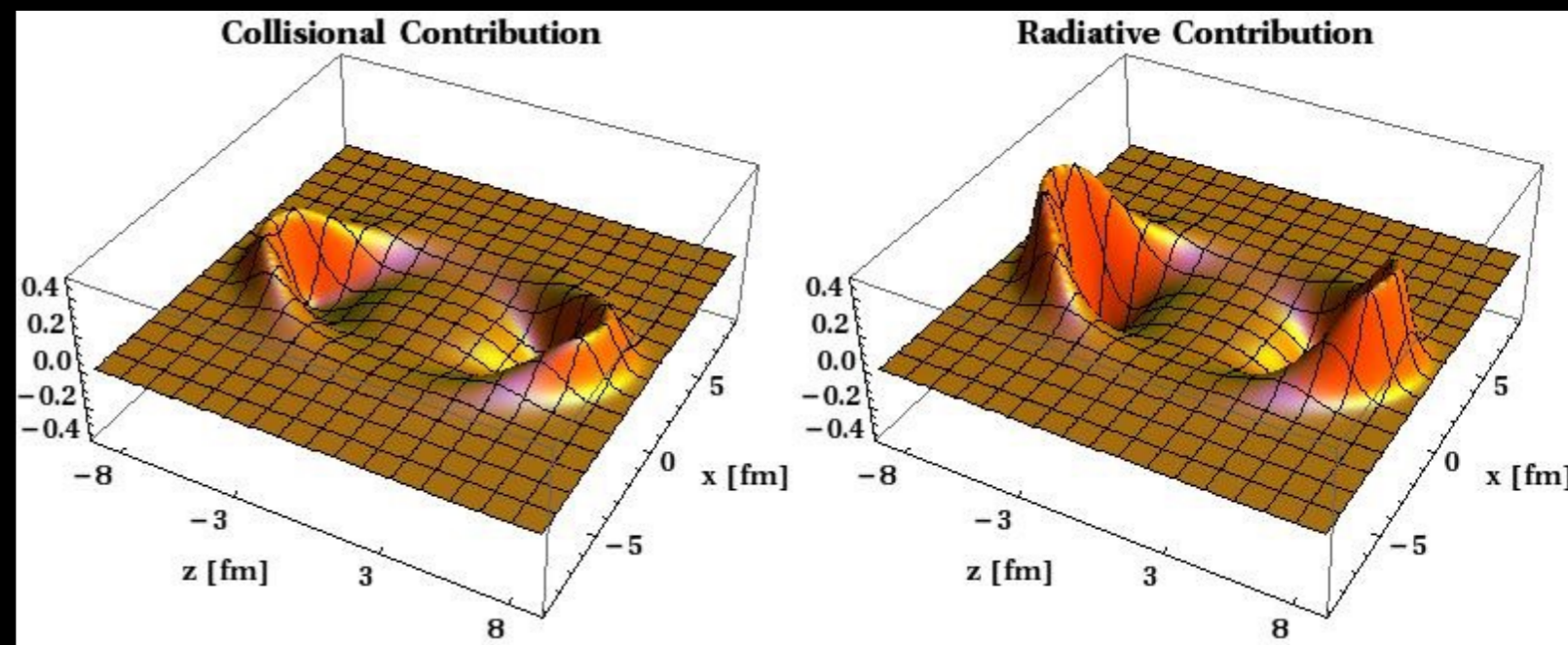
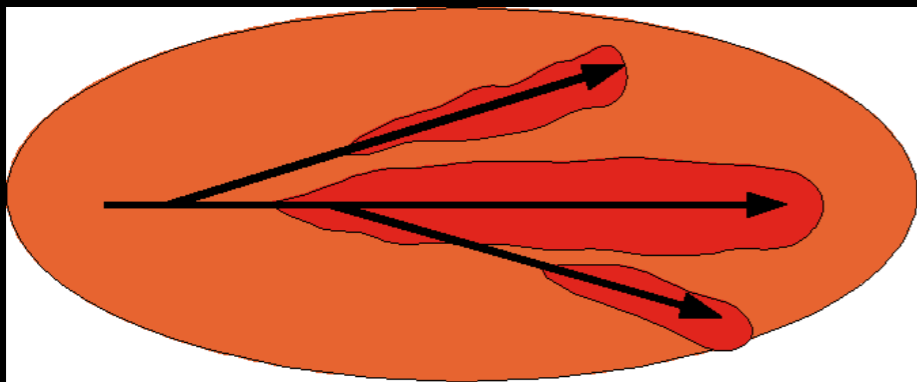


# Energy deposition-thermalization



# Type II transport coefficients

- Should be calculable directly in AdS/CFT.
- or any phenomenological model of the medium e.g., MARTINI, CCNU-LBNL, JEWEL
- Will be greatly enhanced by perturbative splits
- Need a way to formalize these for any model



*B. Neufeld & B. Muller,  
G-Y.Qin, AM, H. Song and U. Heinz*

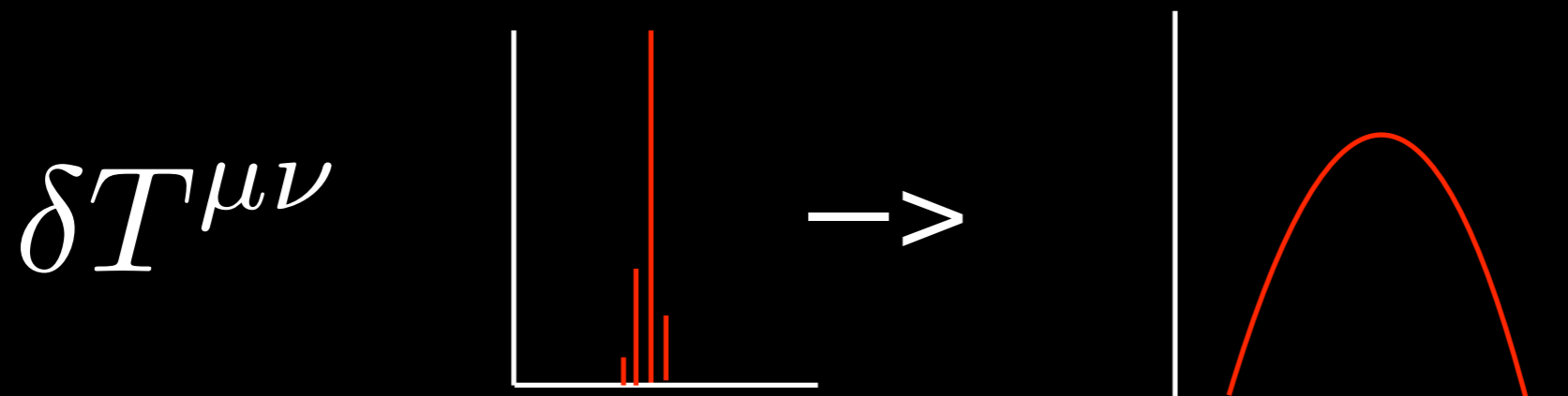
In general, 2 kinds of transport coefficients

*Type 1: which quantify how the medium changes the jet*

$$\hat{q}(E, Q^2) \quad \hat{q}_4(E, Q^2) = \frac{\langle p_T^4 \rangle - \langle p_T^2 \rangle^2}{L} \dots$$

$$\hat{e}(E, Q^2) \quad \hat{e}_2(E, Q^2) = \frac{\langle \delta E^2 \rangle}{L} \quad \hat{e}_4(E, Q^2) = \frac{\langle \delta E^4 \rangle - \langle \delta E^2 \rangle^2}{L} \dots$$

*Type 2: which quantify the space-time structure of the deposited energy momentum at the hydro scale*



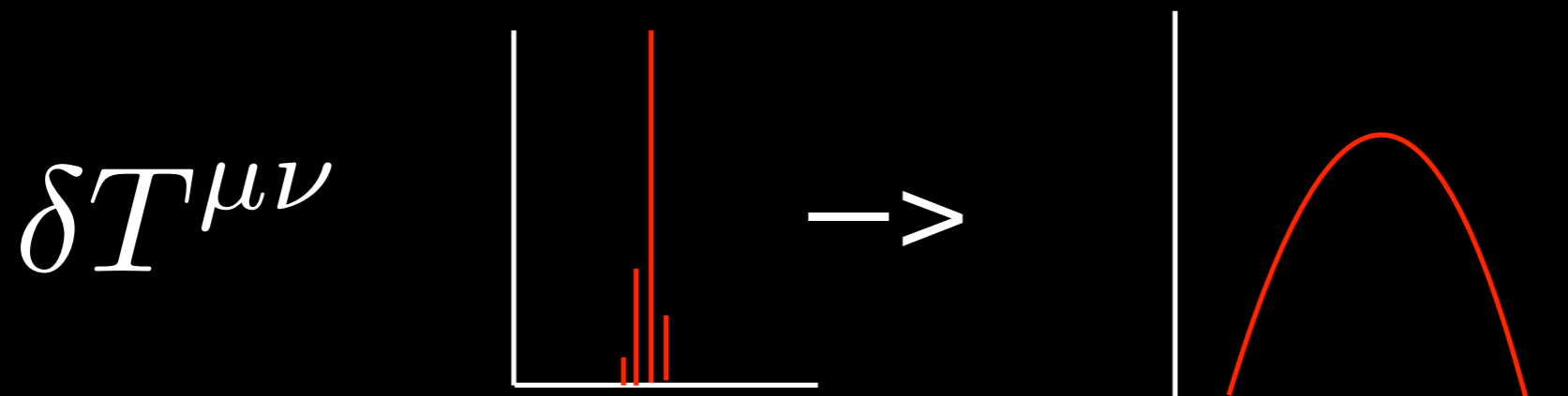
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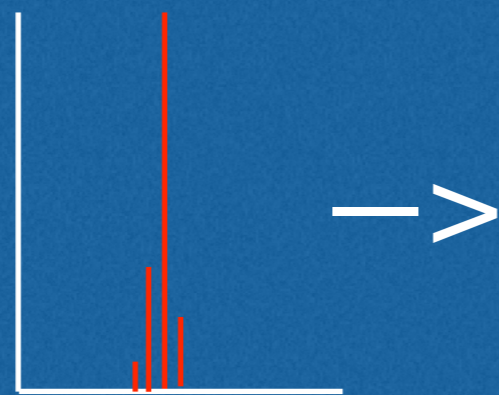
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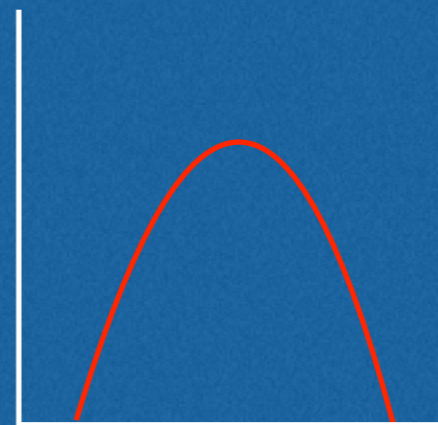
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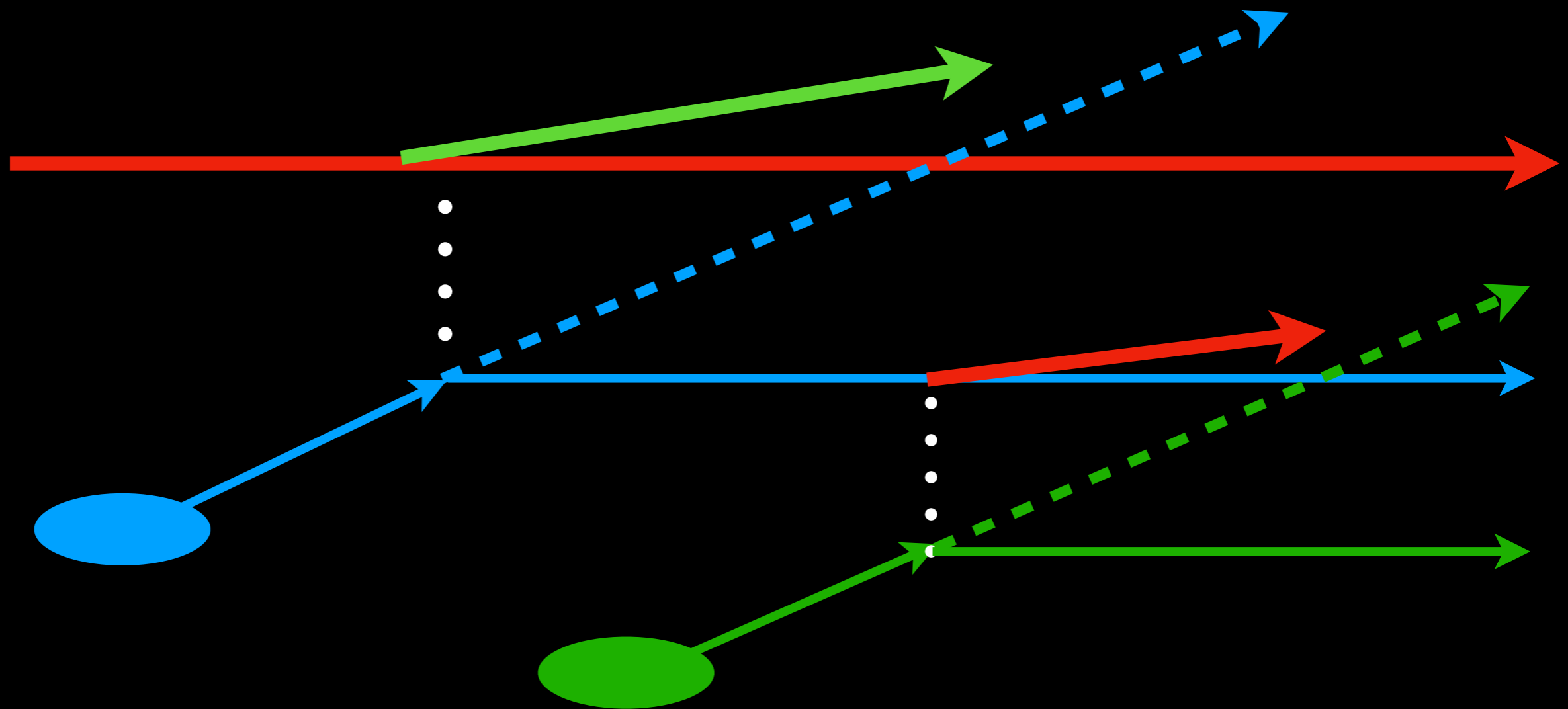
$\delta T^{\mu\nu}$



$\rightarrow$



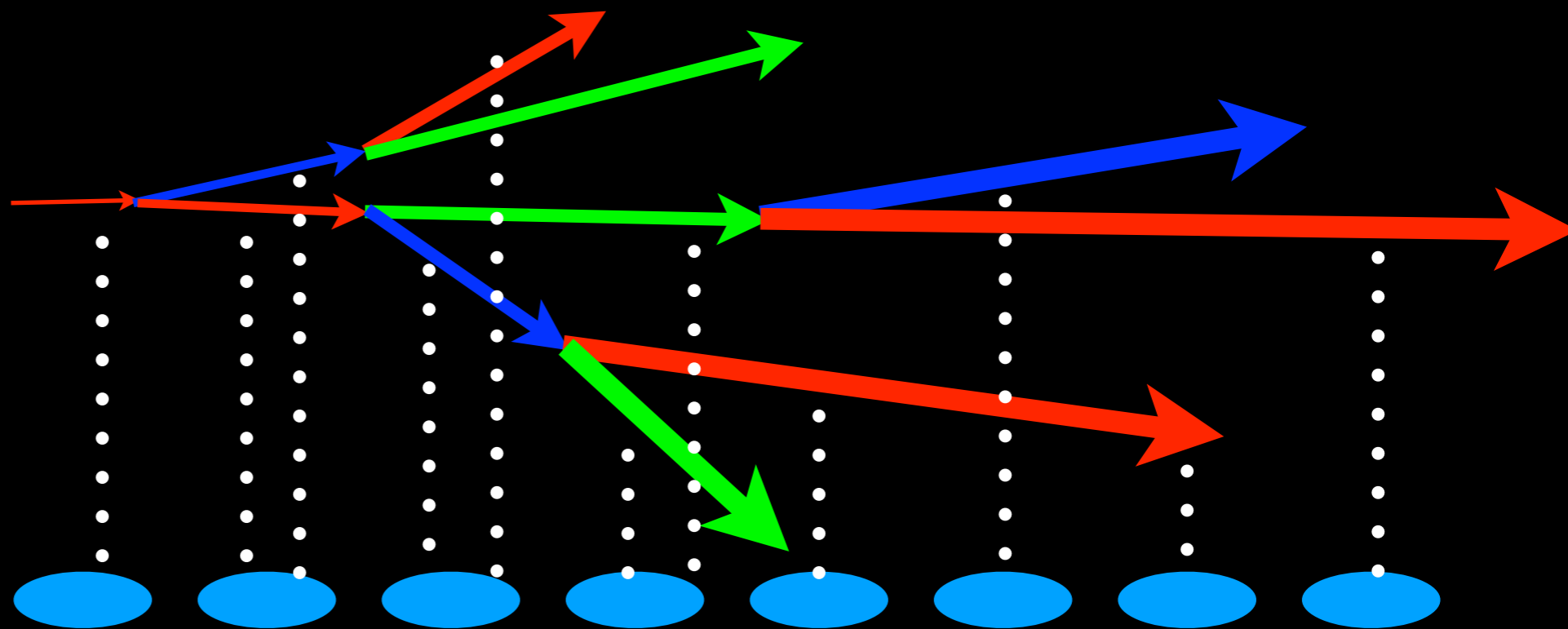
# How this done currently



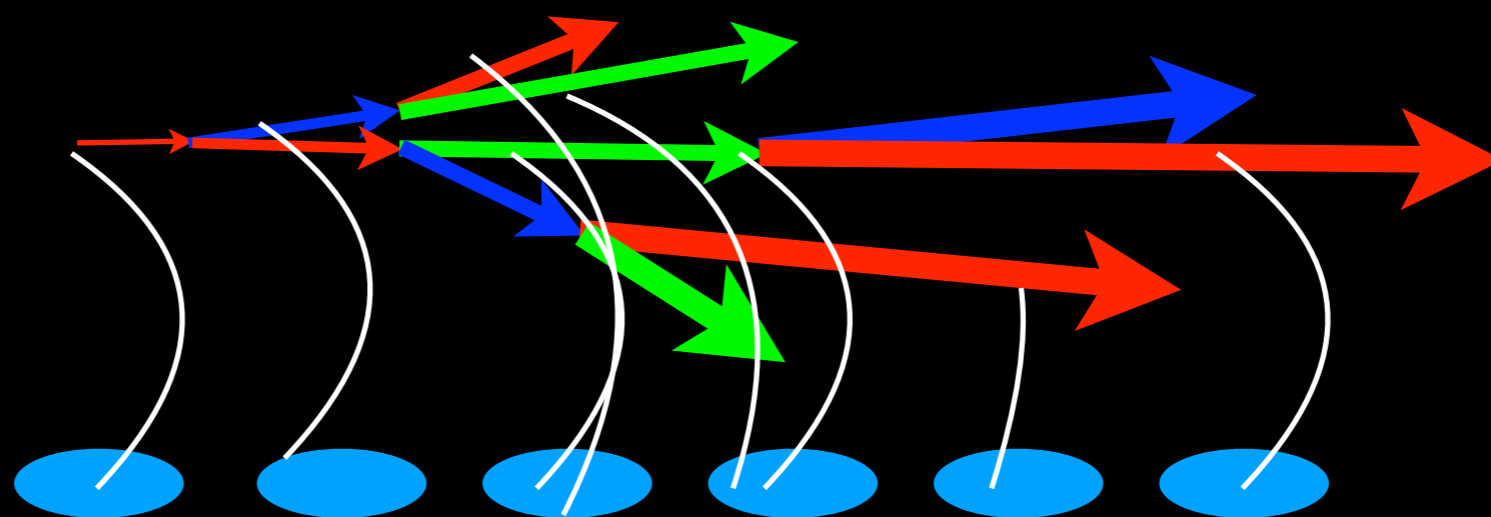
Full jet carries recoil particles  
sampled from a Boltzmann distribution.  
as regular jet partons, and negative partons or holes

# Other methods

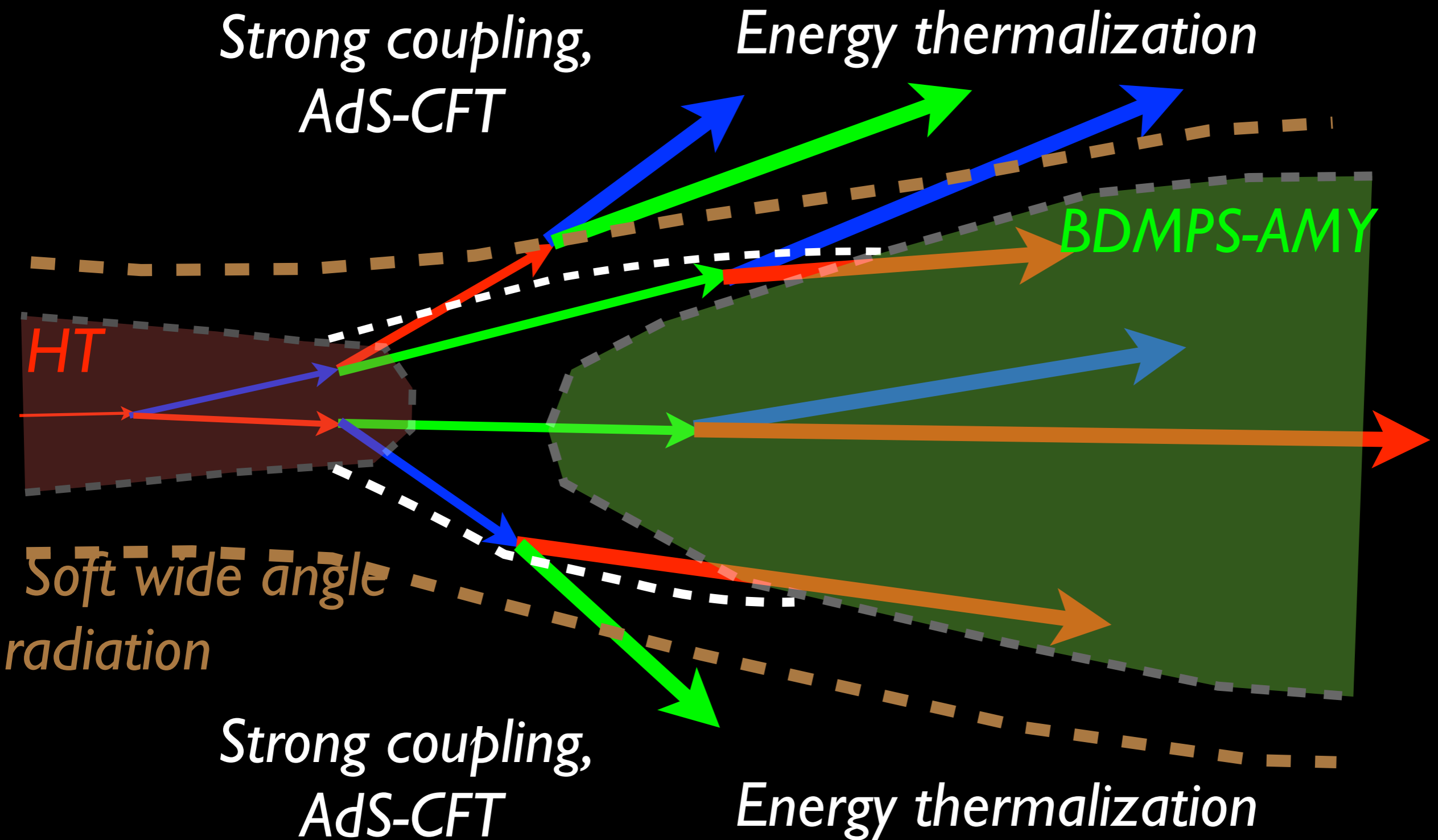
Constant  
Broadening



AdS/CFT drag

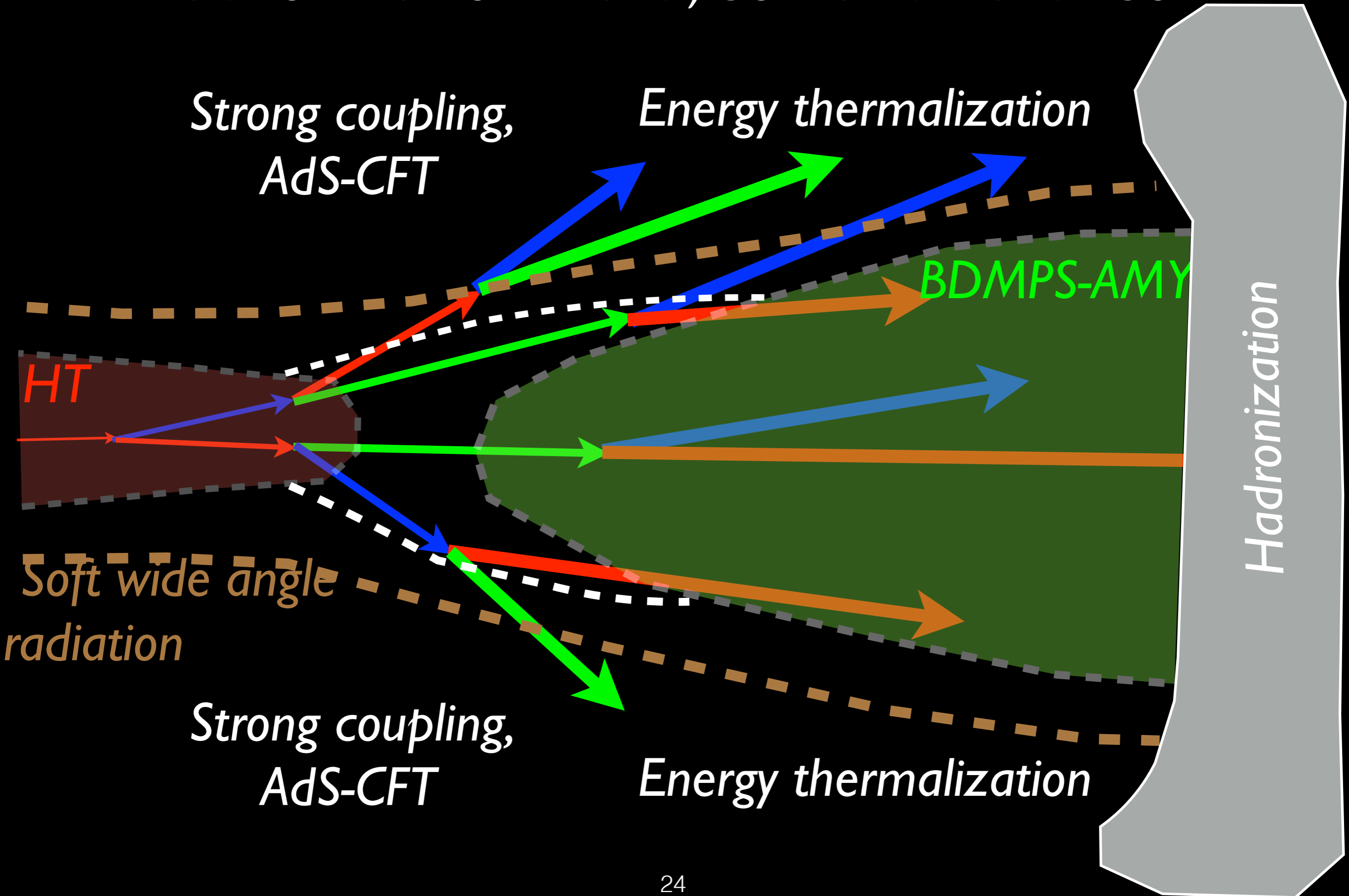


# Hadronization: hard, soft and hard -soft

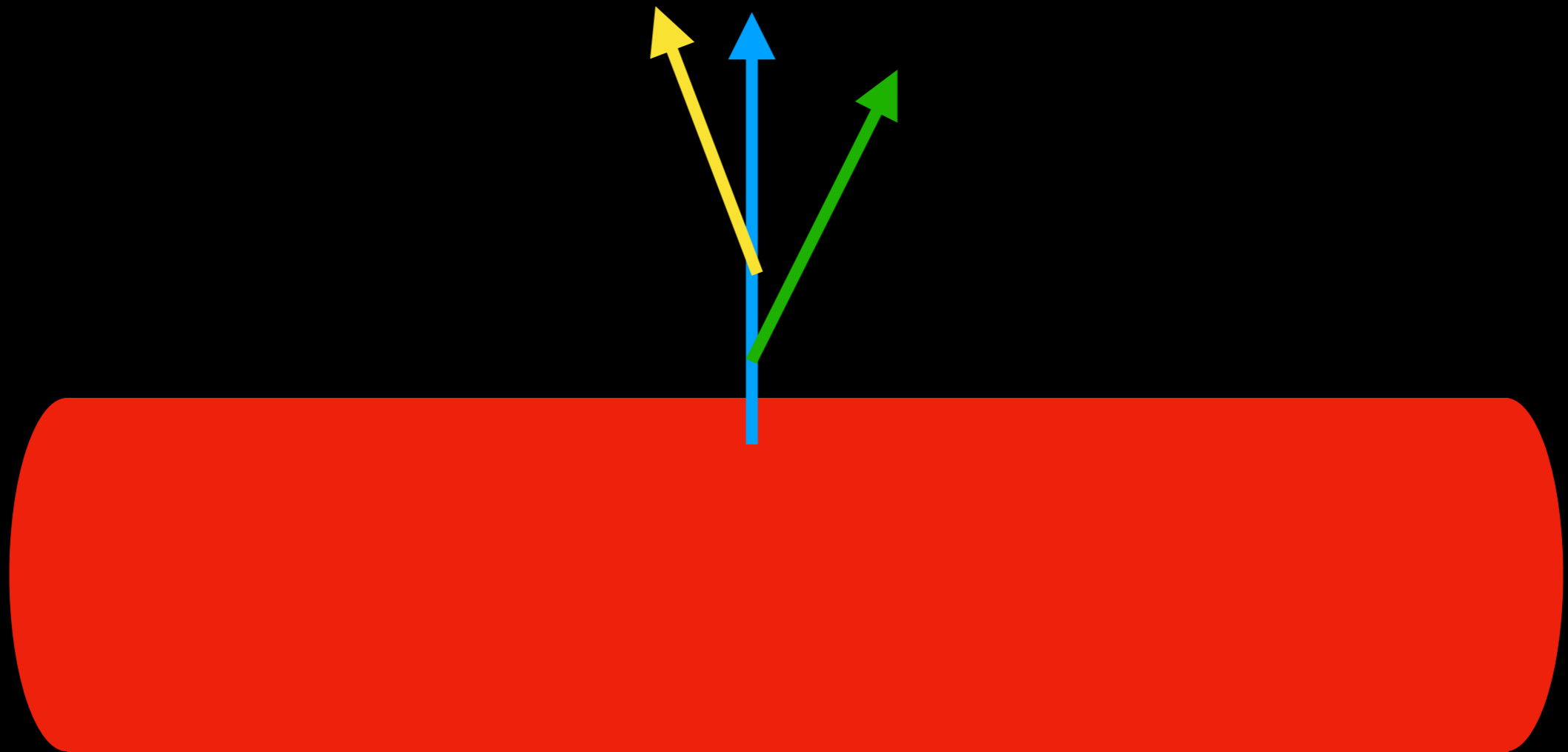




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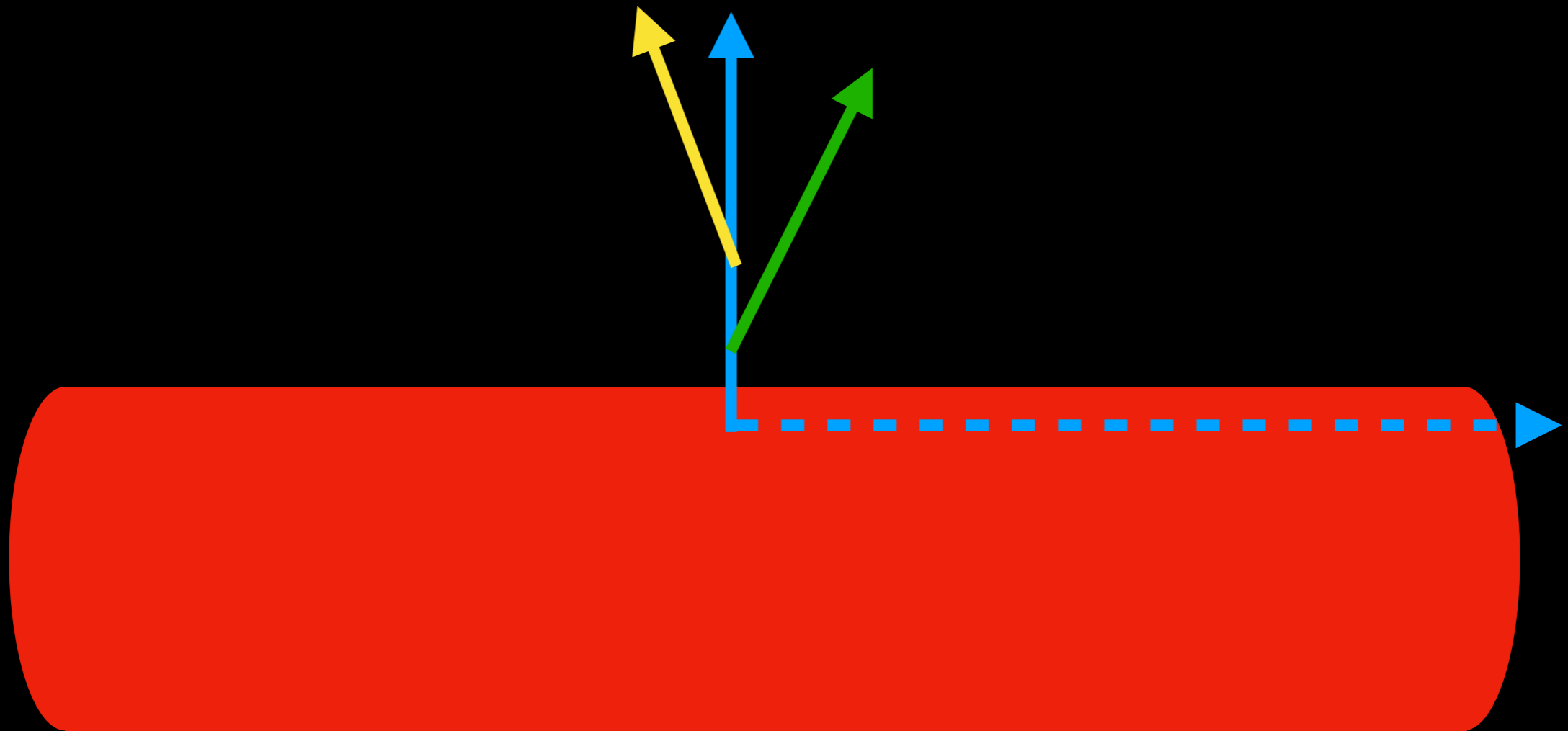


# A jet hadronization mechanism that generalizes from p-p to A-A



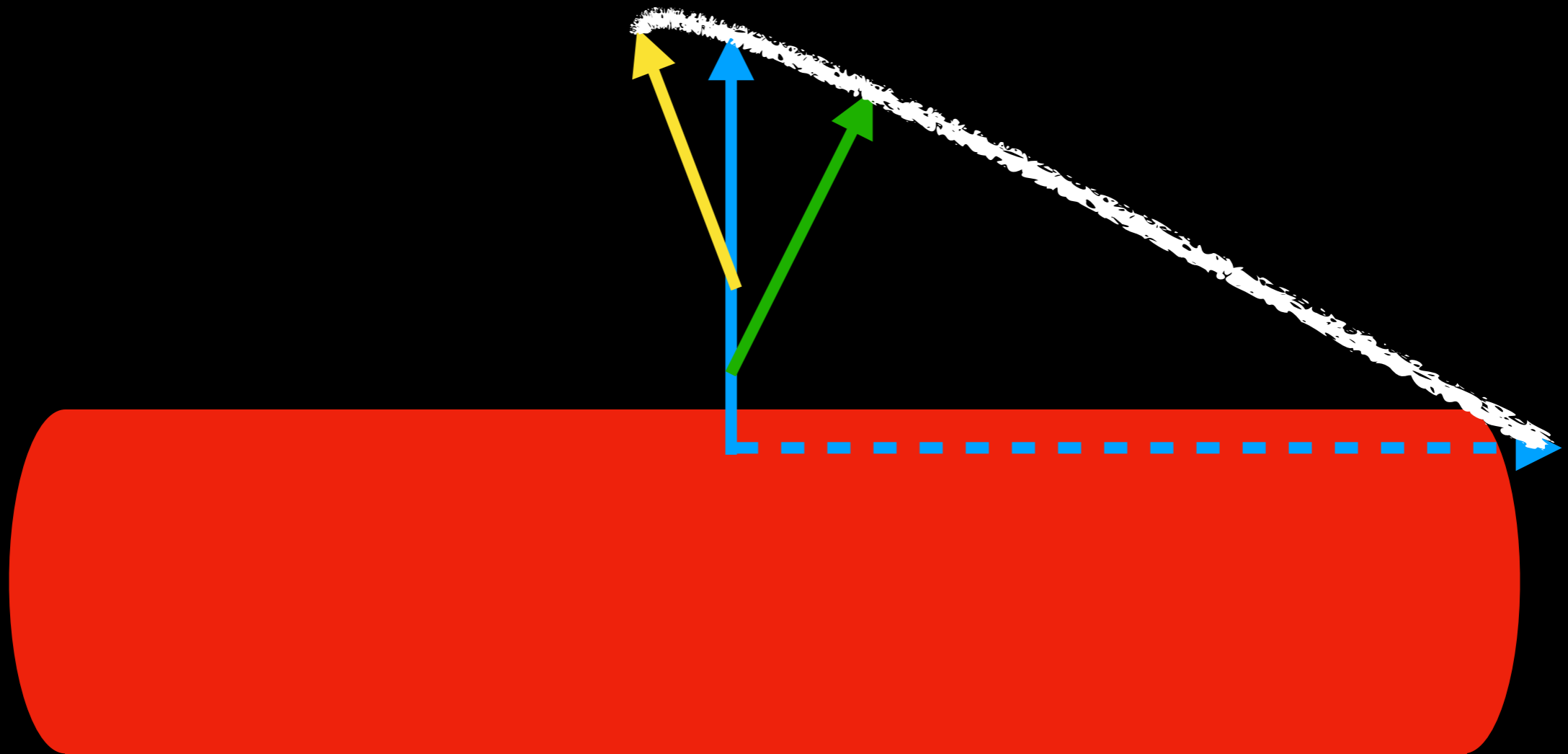
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1. Observables that only depend on type 1
  1. Strong dependence on hard  $\sigma$  :
    1. Hadron  $R_{AA}$ , high  $p_T$   $v_2$ !
    2. Dihadron,  $I_{AA}$ ,  $\gamma$ -Hadron

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2. Dihadron,  $I_{AA}$ ,  $\gamma$ -Hadron

*(clear dependence on  $q$ , but also require fragmentation functions)*

### 2. Weaker dependence on hard $\sigma$ :

1. Near side  $I_{AA}$  ! *(badly surface biased)*

# Observables: more type 2, more MC

1. Observables that only depend on type 1
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Jet medium correlations

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# Need a Monte-Carlo event generator based approach

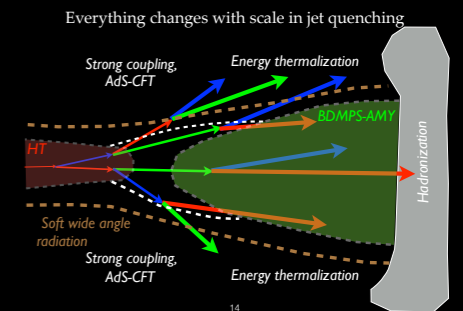
Need to have a framework

- That can modularly incorporate a variety of theoretical approaches
- Which can allow you to model medium response, and entire range of transport coefficients
- Can address all observables simultaneously

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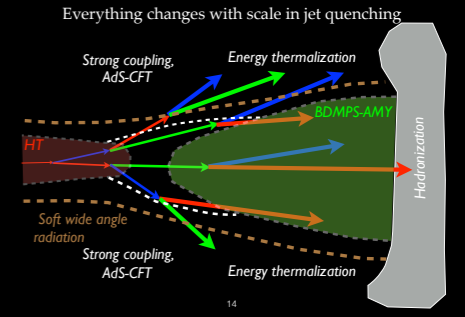
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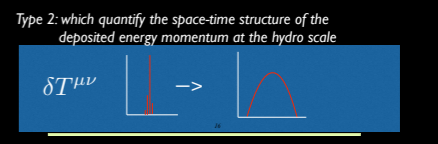


In general, 2 kinds of transport coefficients

Type 1: which quantify how the medium changes the jet

$$\hat{q}(E, Q^2) \quad \hat{q}_s(E, Q^2) = \frac{\langle p_T^4 \rangle - \langle p_T^2 \rangle^2}{L} \dots$$

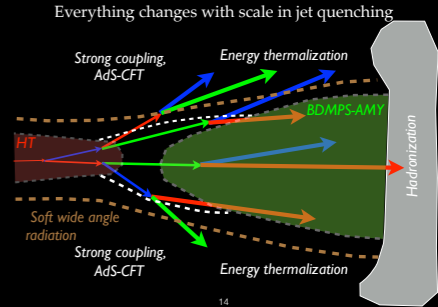
$$\hat{\epsilon}(E, Q^2) \quad \hat{\epsilon}_2(E, Q^2) = \frac{\langle \delta E^2 \rangle}{L} \quad \hat{\epsilon}_4(E, Q^2) = \frac{\langle \delta E^4 \rangle - \langle \delta E^2 \rangle^2}{L} \dots$$



# Need a Monte-Carlo event generator based approach

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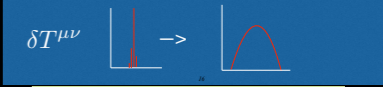
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Type 2: which quantify the space-time structure of the deposited energy momentum at the hydro scale



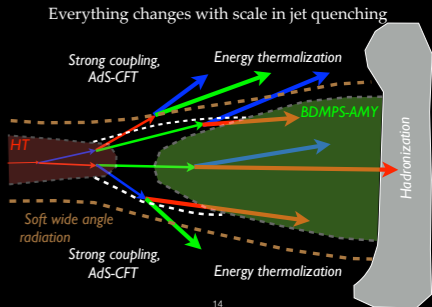
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  3. Observables that depend strongly on type 2
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# Need a Monte-Carlo event generator based approach

Need to have a framework

- That can modularly incorporate a variety of theoretical approaches
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In general, 2 kinds of transport coefficients

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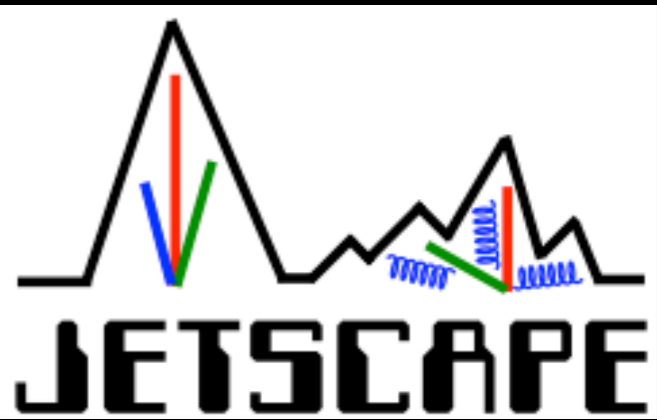
$$\hat{q}(E, Q^2) \quad \hat{q}_s(E, Q^2) = \frac{\langle p_T^4 \rangle - \langle p_T^2 \rangle^2}{L} \dots$$

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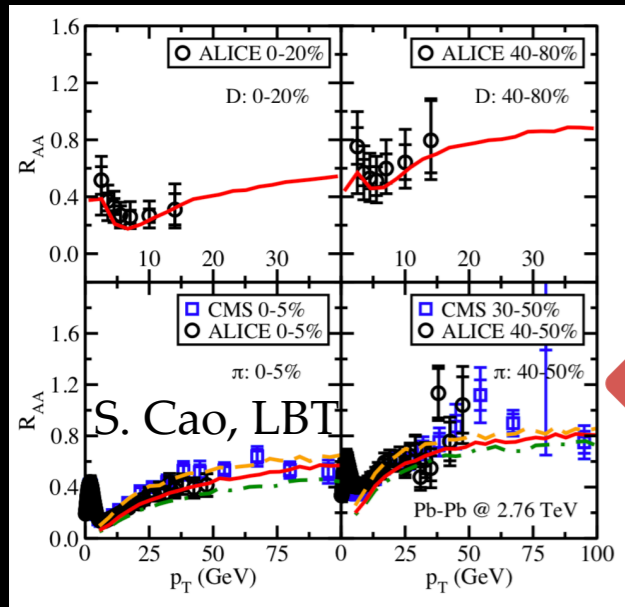
Such a framework now exists: JETSCAPE  
<https://github.com/JETSCAPE>



# Applying Multi-scale models

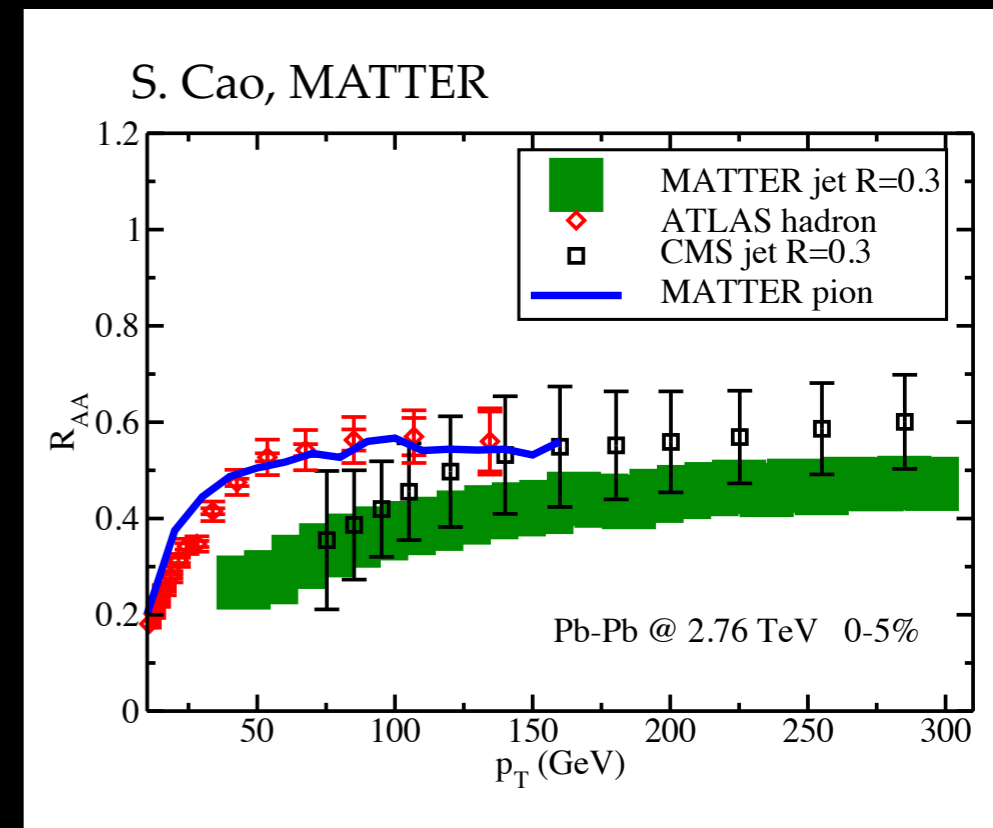
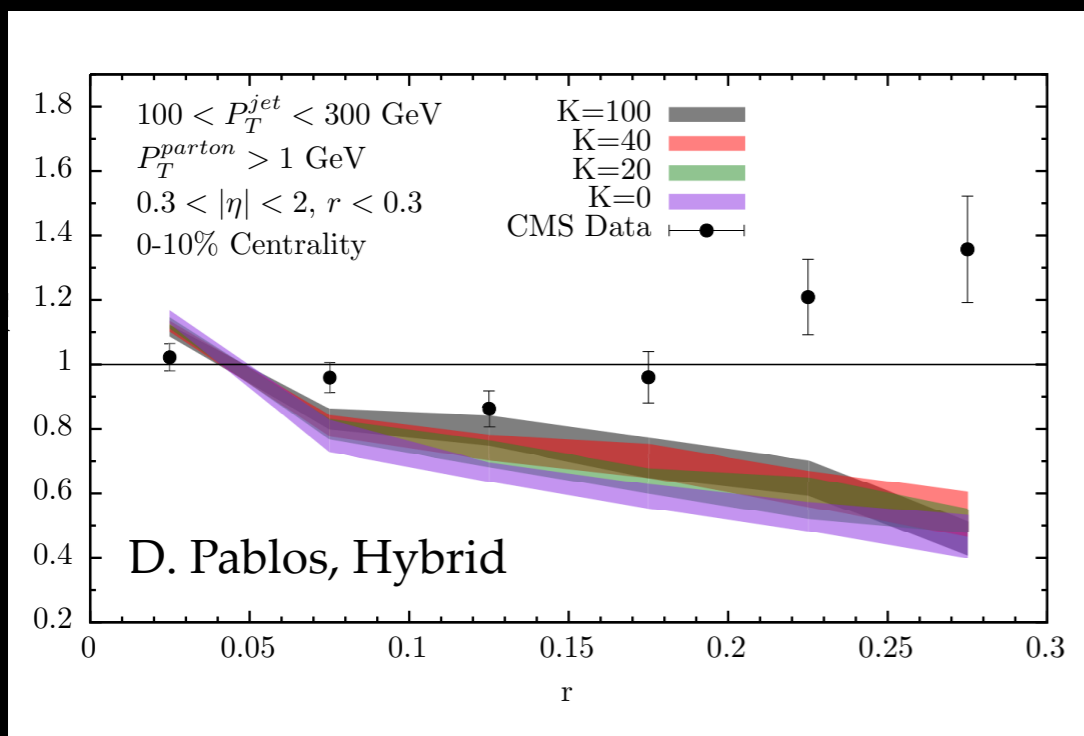
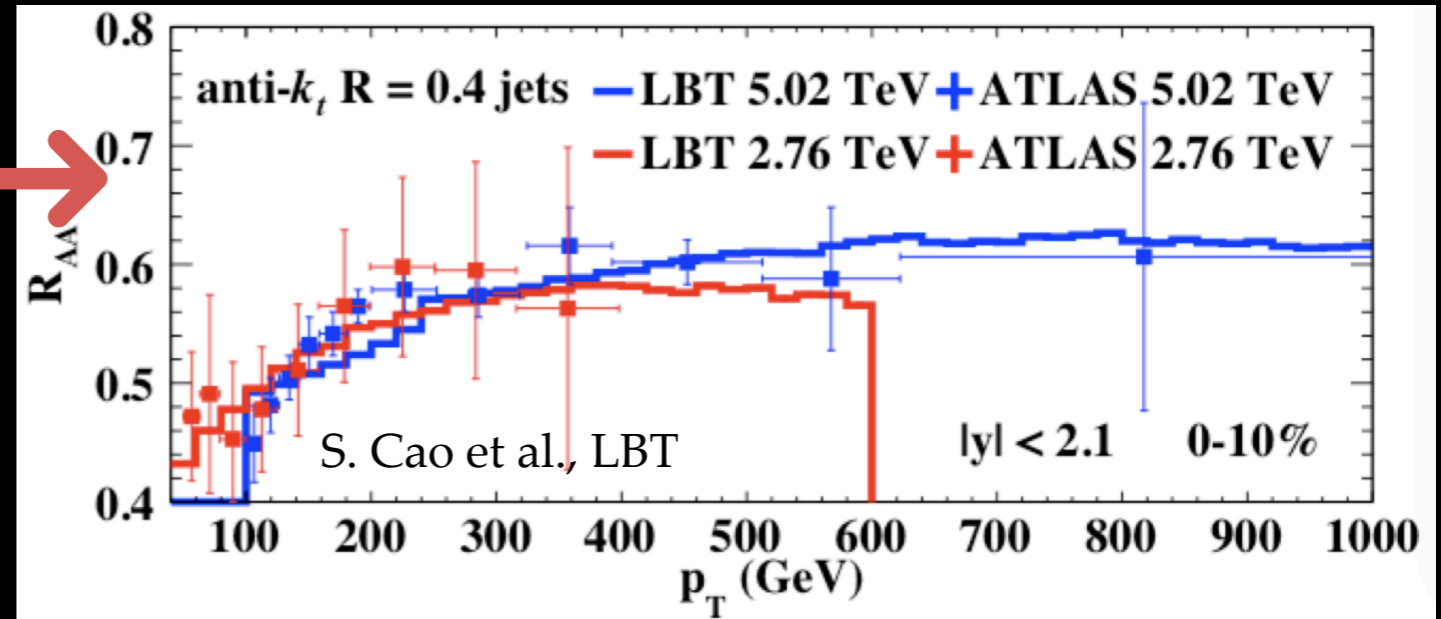
Its the right thing to do.

Pushing limited approaches past limits creates tension!

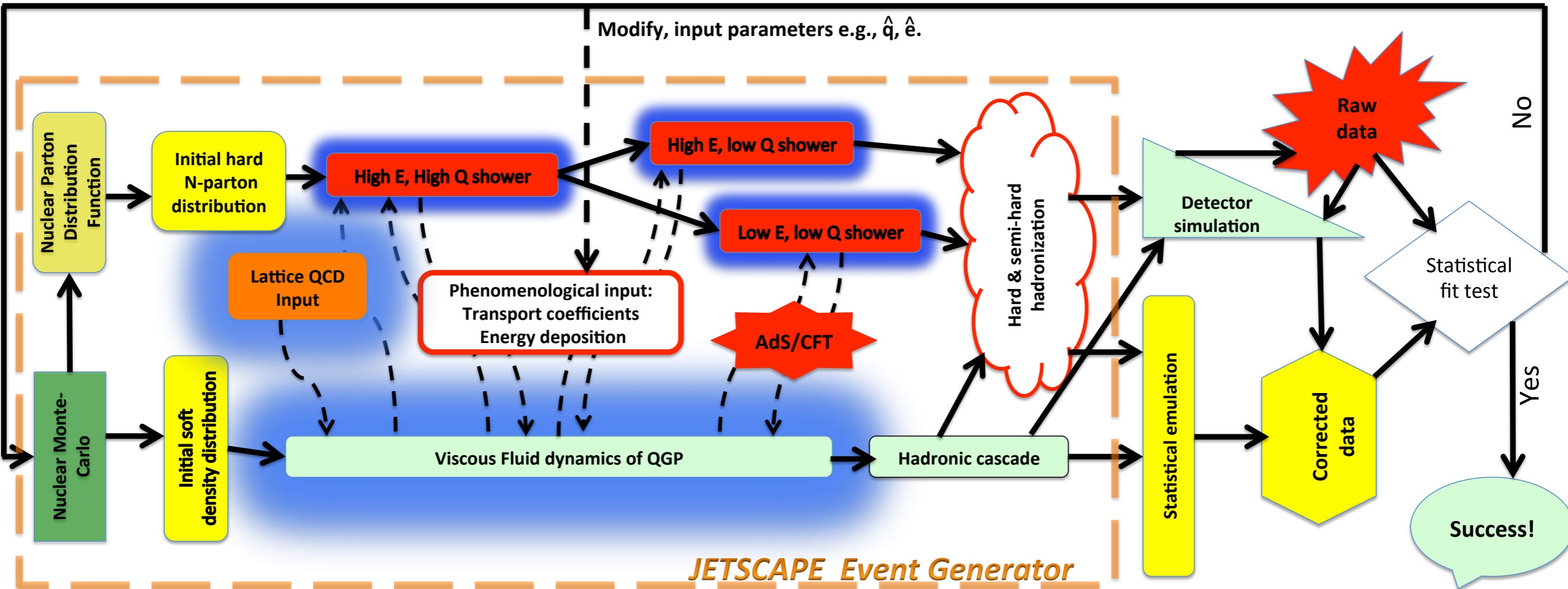


LBT  
fixed  $\alpha_s=0.15$

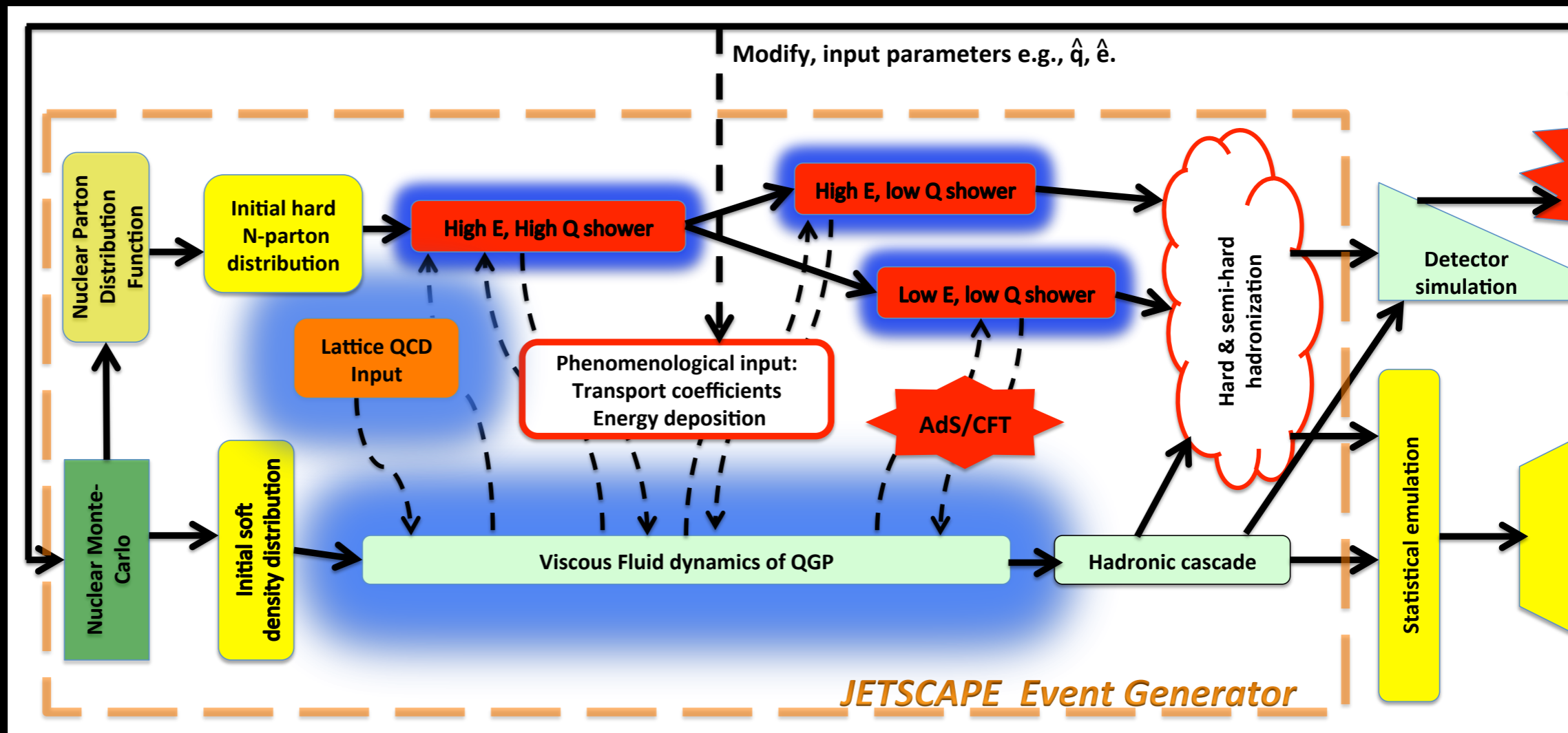
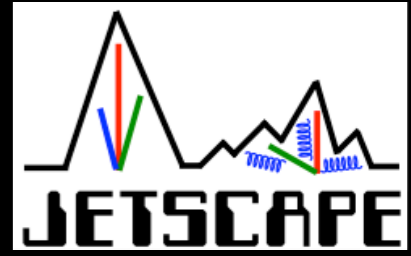
mean  $\alpha_s=0.2$



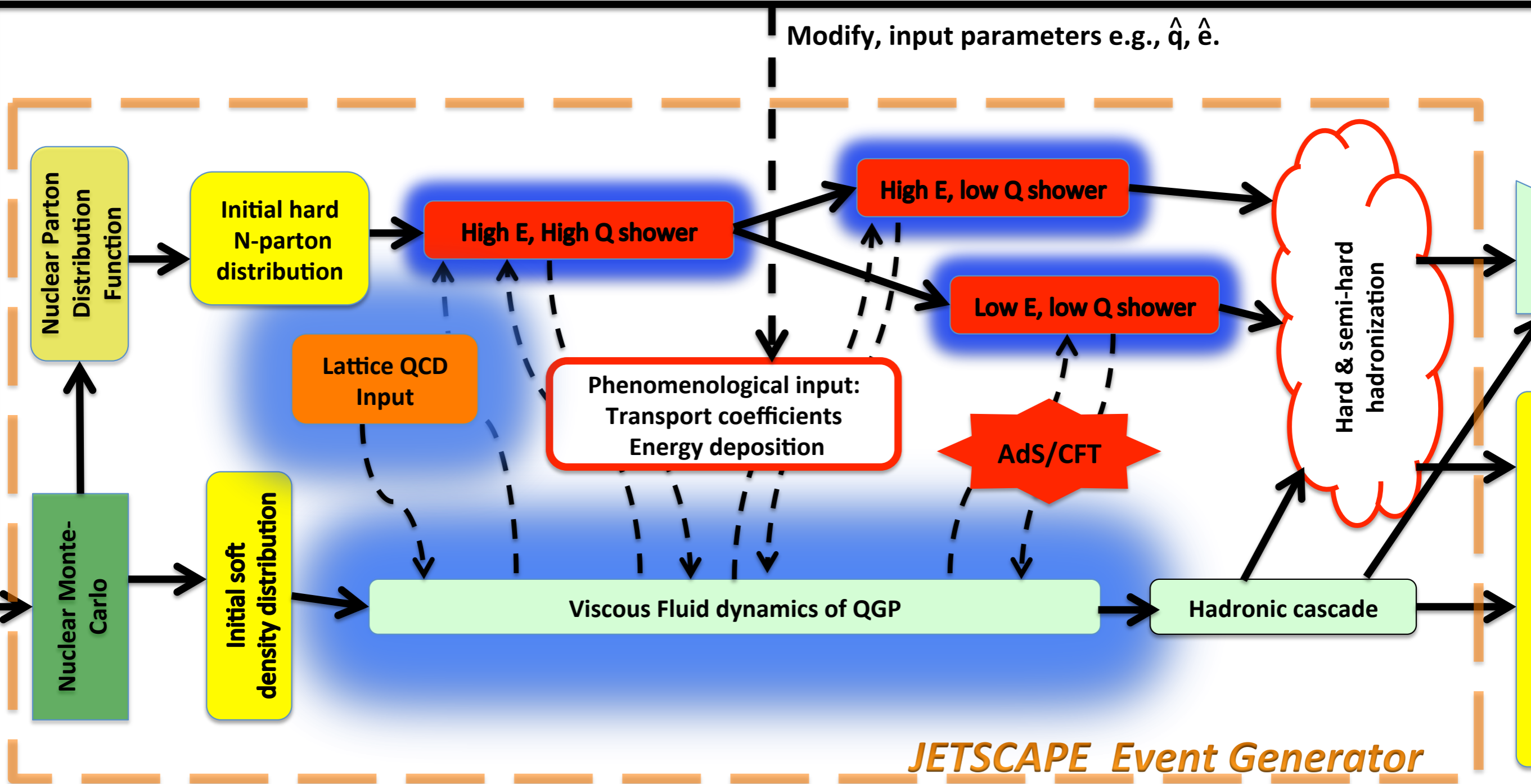
# How would this work?



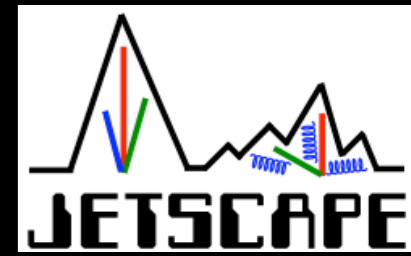
# How would this work?



# How would this work?



# Using the full event generator

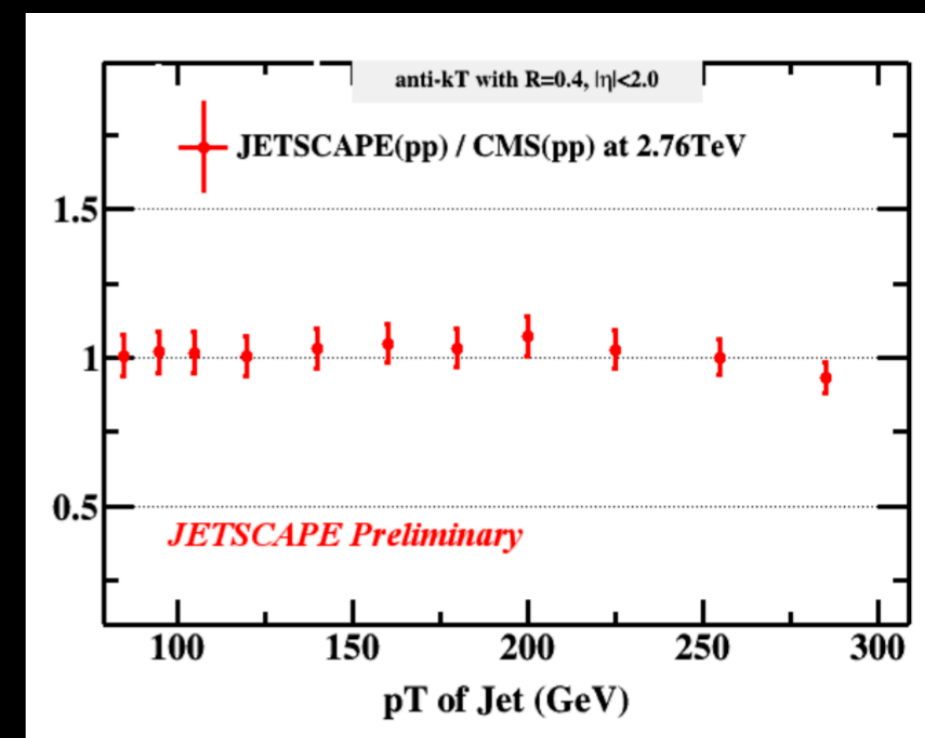
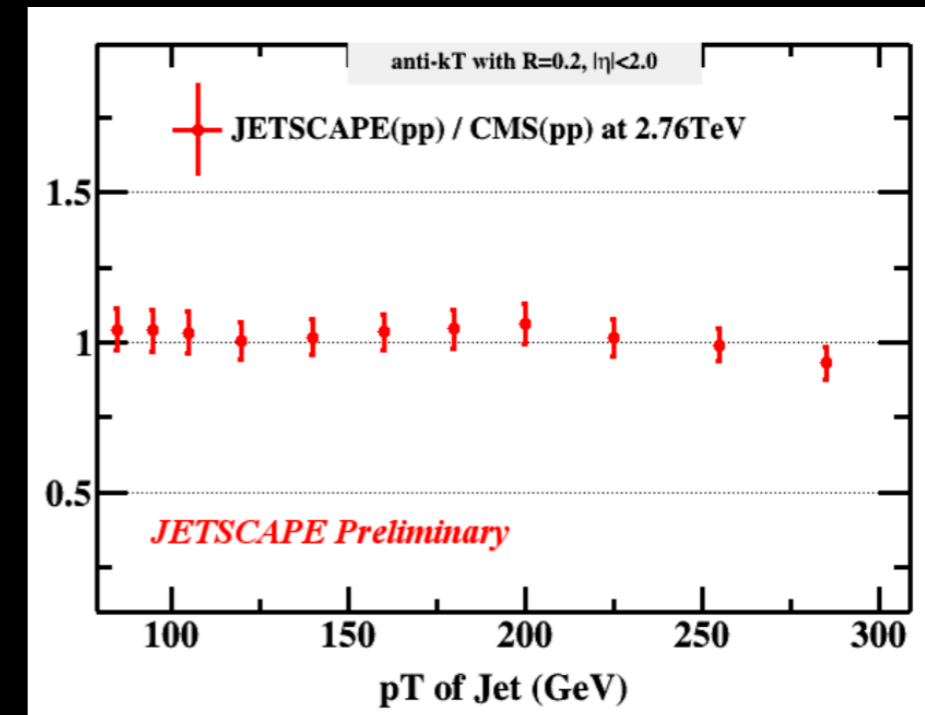
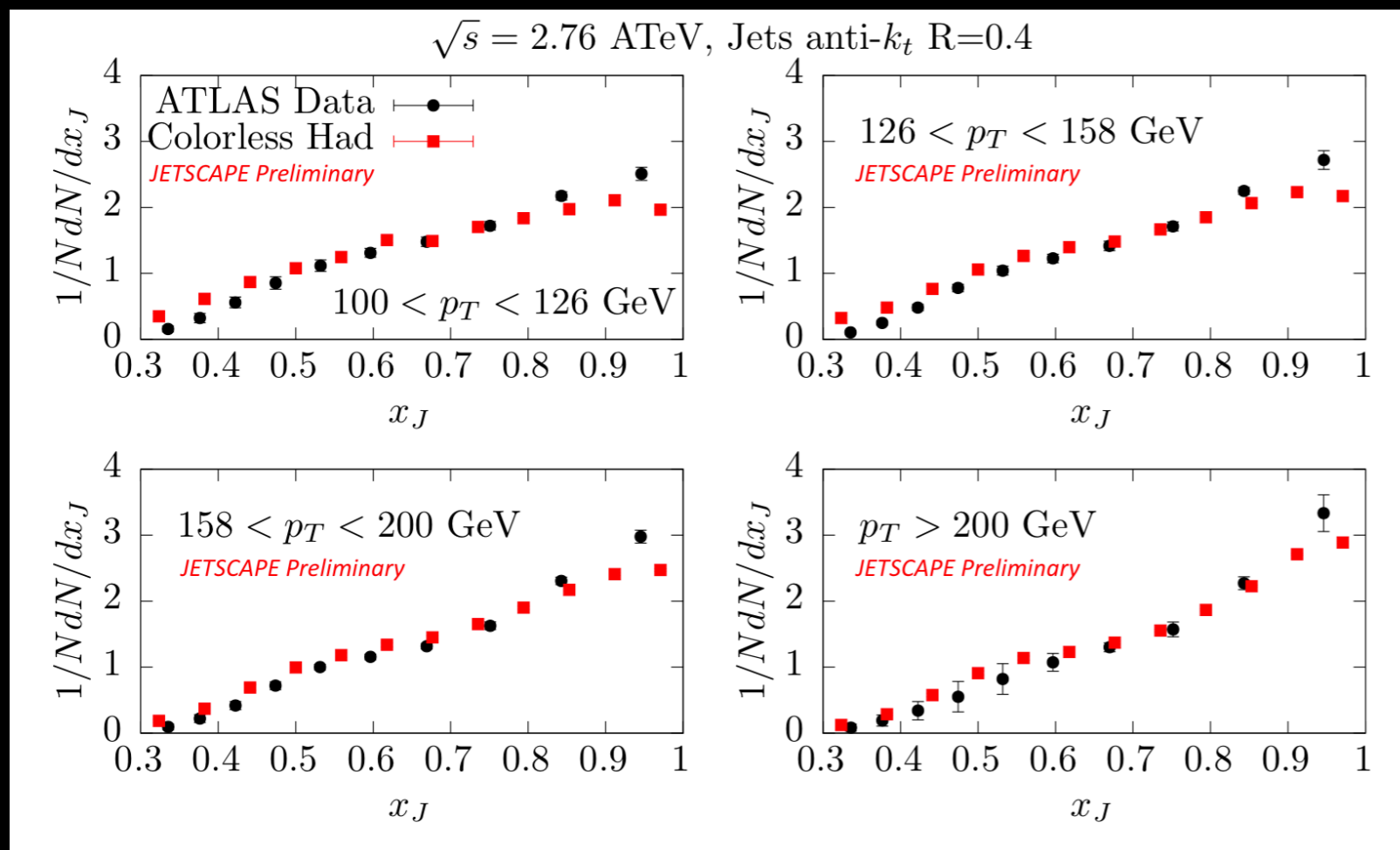


- Any good event generator needs a good p-p baseline

PYTHIA for initial state

MATTER for all final state partons  $> 1\text{GeV}$

PYTHIA based hadronization of final partons



# Preliminary results from JETSCAPE



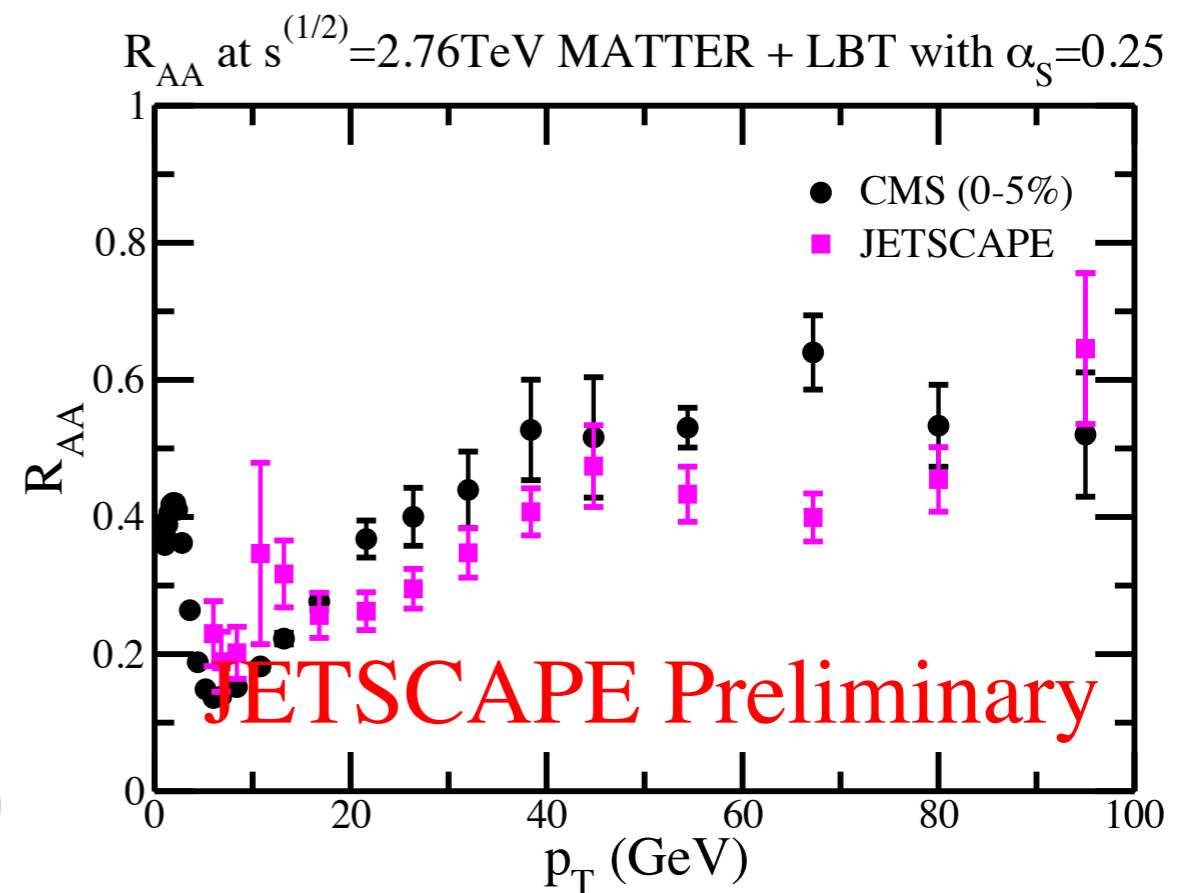
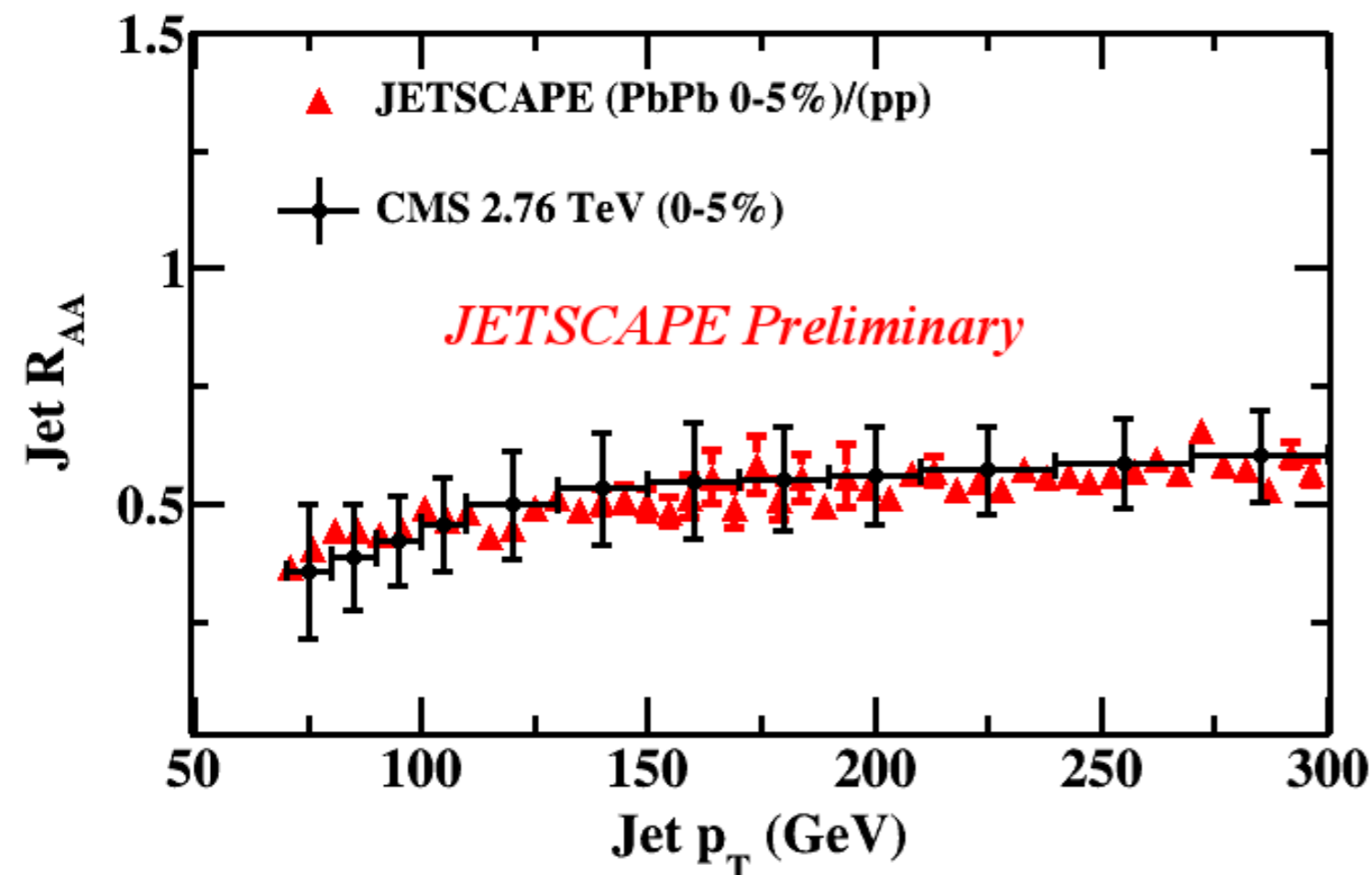
Initial state with TRENTO for both hydro and jets

TRENTO  $\rightarrow$  PreEquib  $\rightarrow$  MUSIC  $\rightarrow$  Soft Hadronization

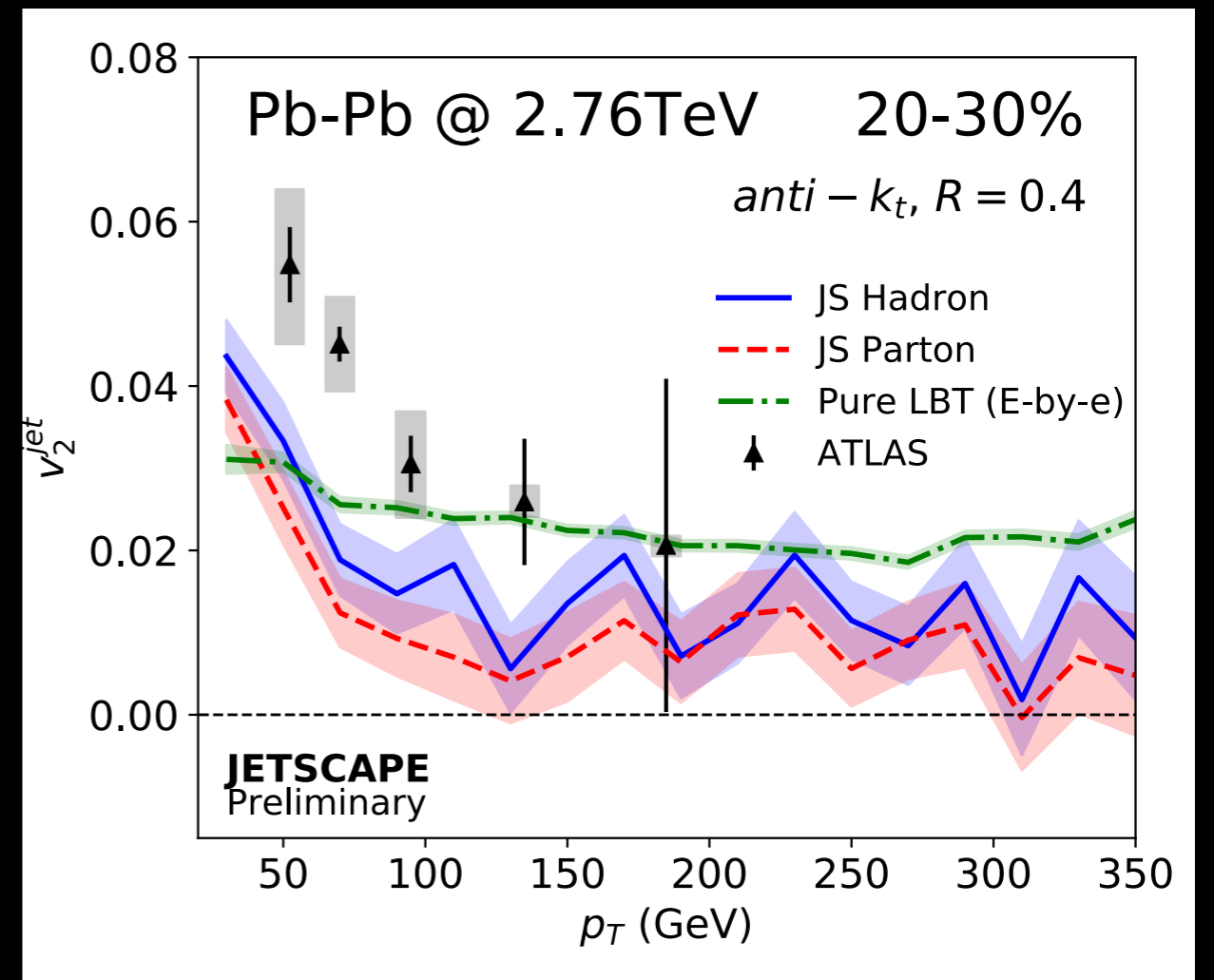
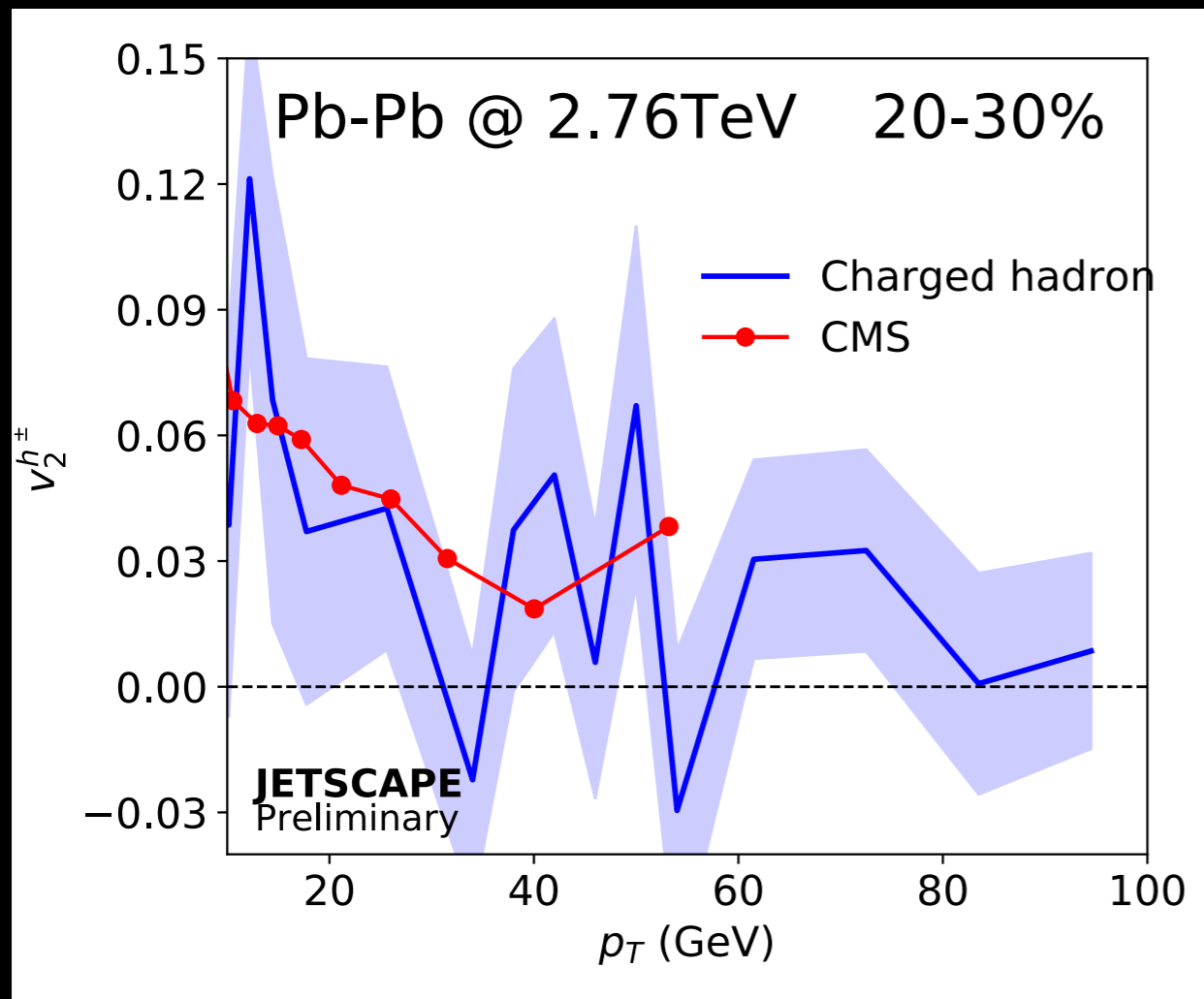
TRENTO  $\rightarrow$  PYTHIA init

$\rightarrow$  (MATTER/LBT/MARTINI/AdS) + MUSIC profile

$\rightarrow$  PYTHIA based hadronization



# Jet and leading hadron $v_2$

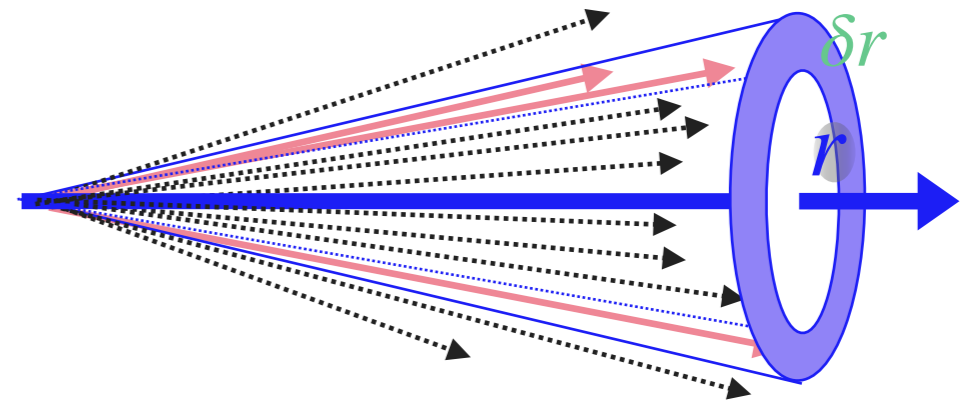


Need event-by-event hydro and initial state to hydro adjustments

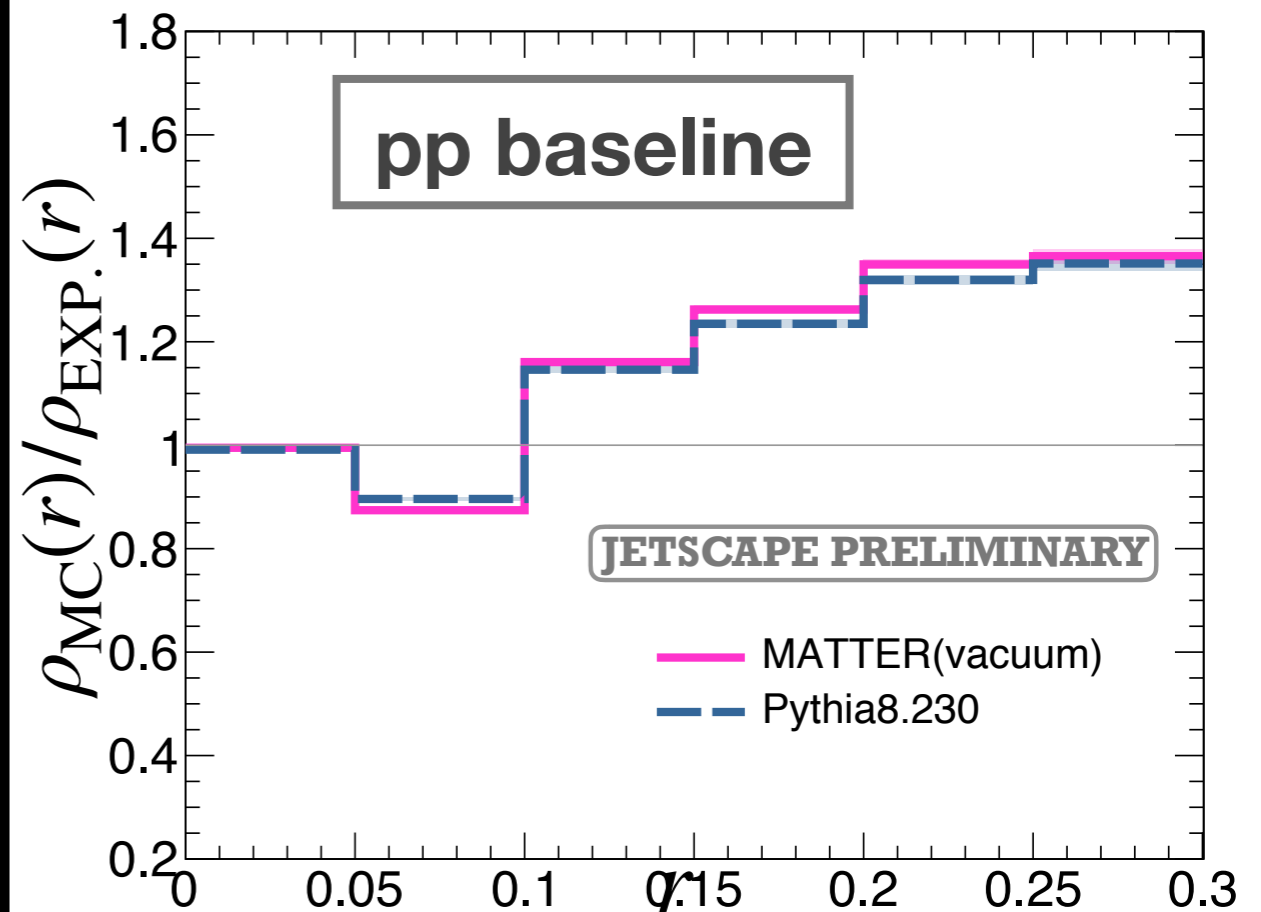
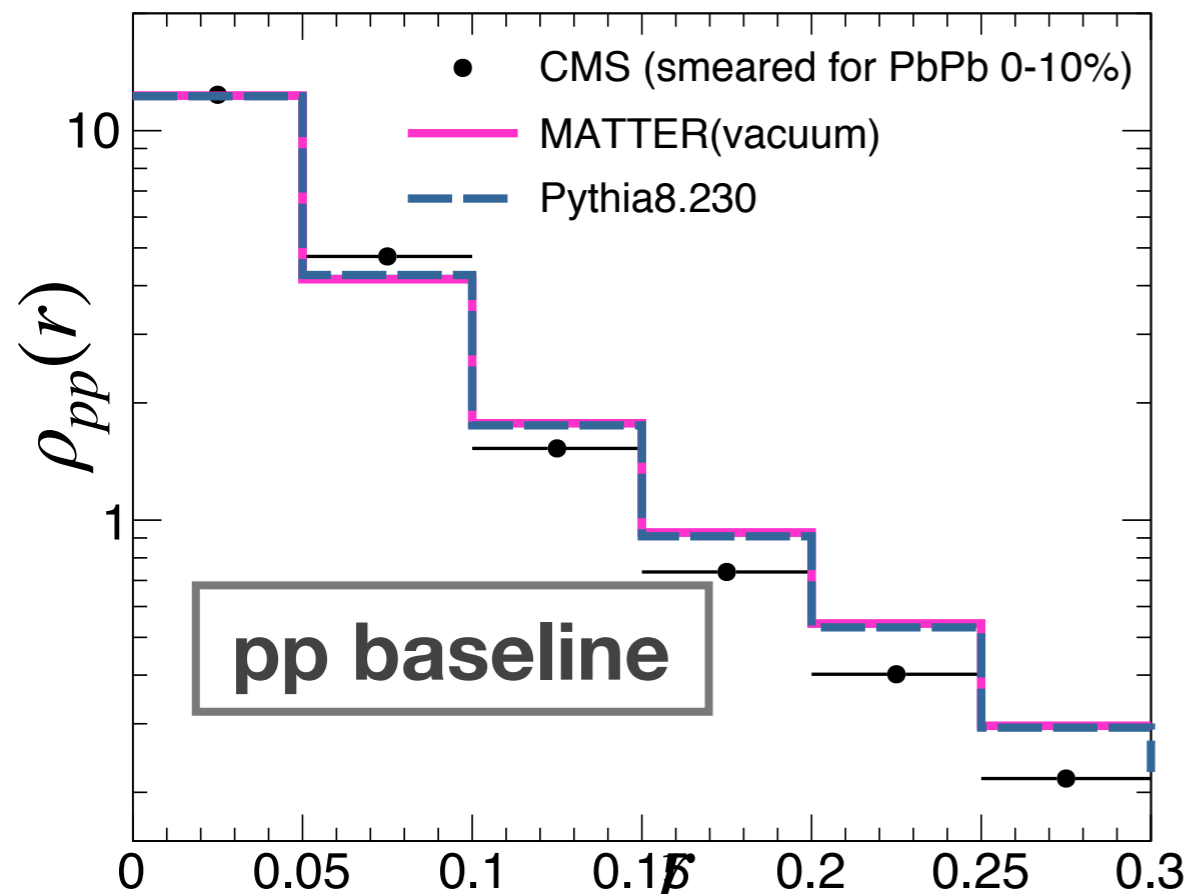


# Jet shape

$$\rho(r) = \frac{1}{N_{\text{jet}}} \sum_{\text{jet}} \left[ \frac{1}{p_{\text{T}}^{\text{jet}}} \frac{\sum_{\text{trk} \in (r-\delta r/2, r+\delta r/2)} p_{\text{T}}^{\text{trk}}}{\delta r} \right]$$



JETSCAPE,  $pp$  2.76 TeV, anti- $k_{\text{T}}$   $R = 0.3$ ,  $p_{\text{T}}^{\text{jet}} > 100$  GeV,  $0.3 < |\eta_{\text{jet}}| < 2.0$ ,  $p_{\text{T}}^{\text{trk}} > 1$  GeV

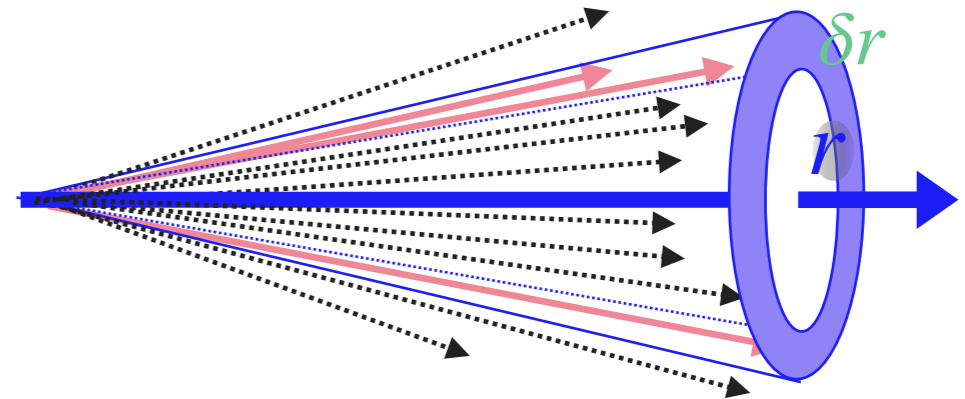


$p_{\text{T}}$  in angular bins from jet axis

# Jet Shape

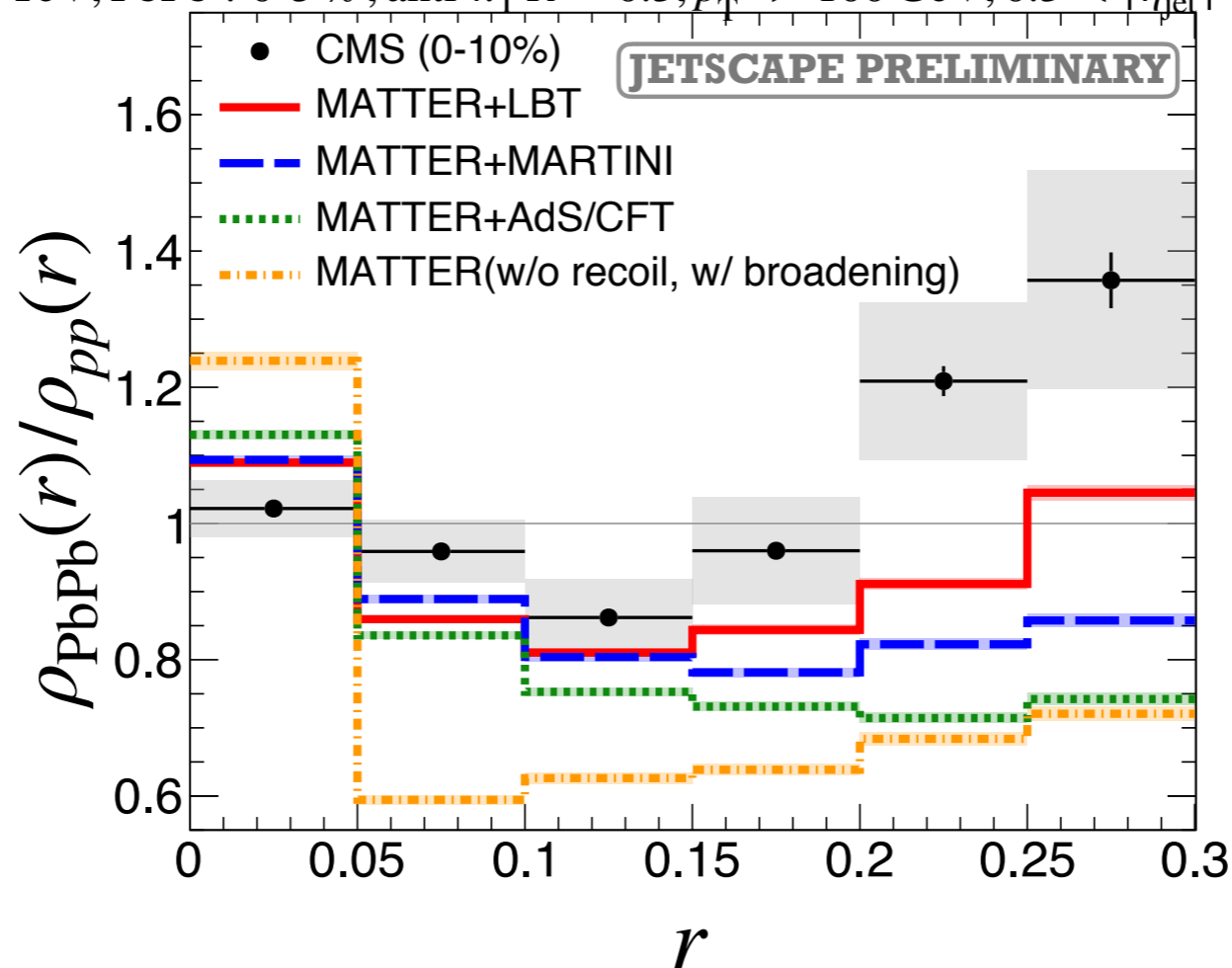
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**note: self-normalized observable**



JETSCAPE, 2.76 TeV, PbPb : 0-5 % , anti- $k_{\text{T}}$   $R = 0.3$ ,  $p_{\text{T}}^{\text{jet}} > 100$  GeV,  $0.3 < |\eta_{\text{jet}}| < 2.0$ ,  $p_{\text{T}}^{\text{trk}} > 1$  GeV

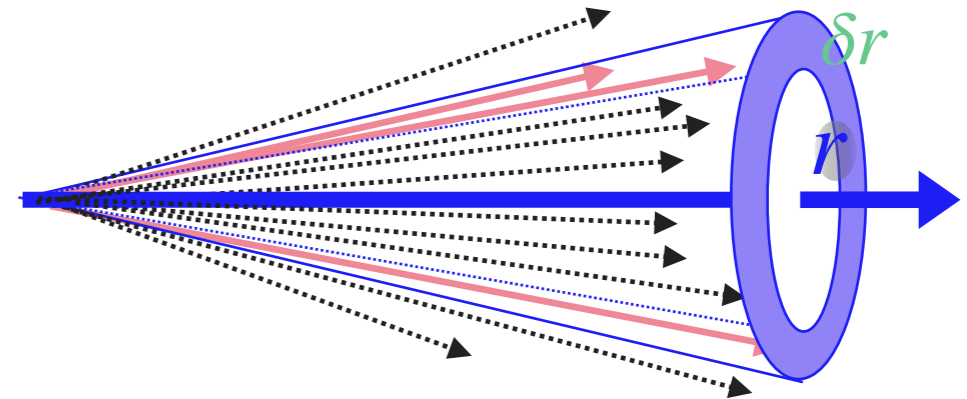
**PbPb/pp**



# Jet Shape

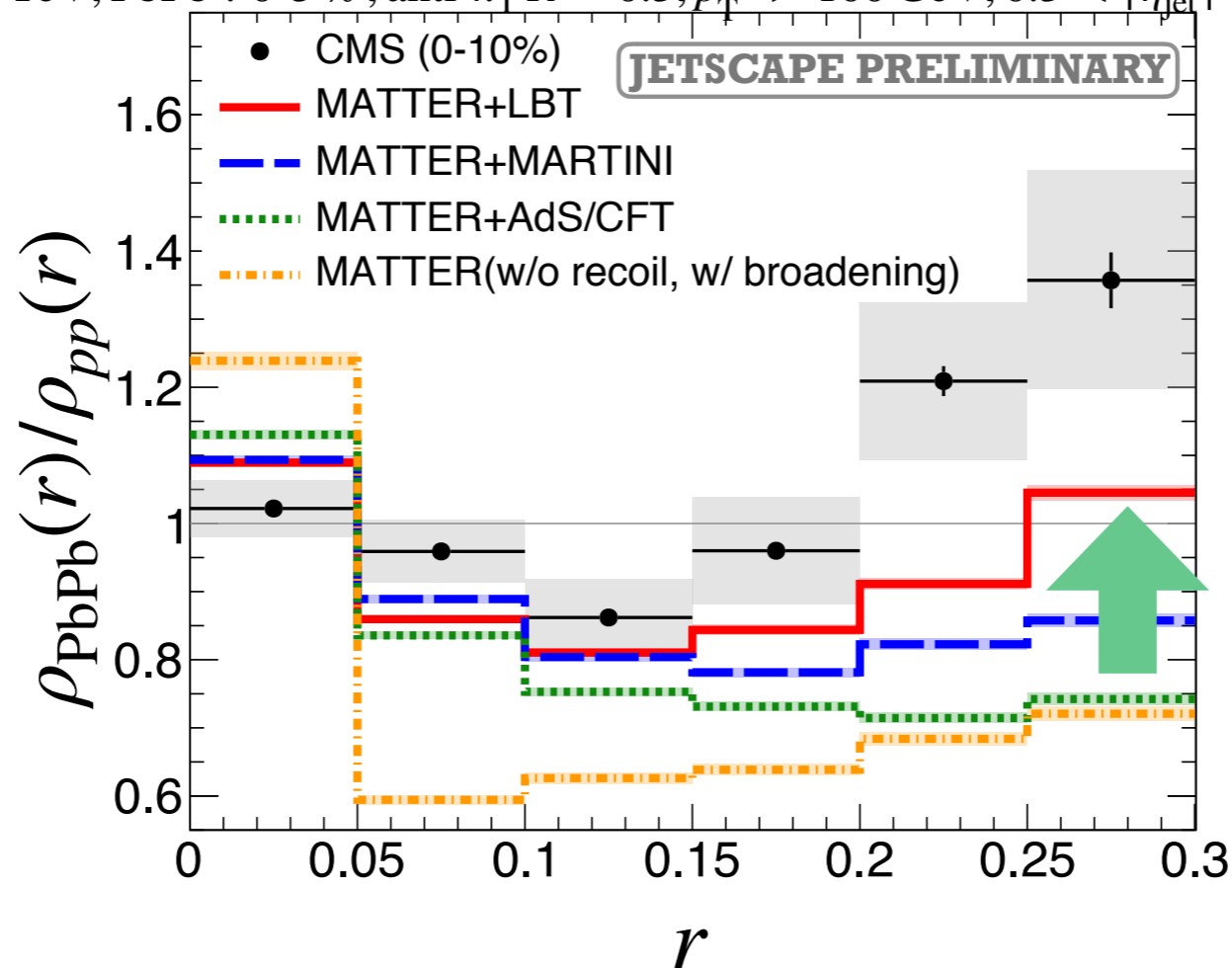
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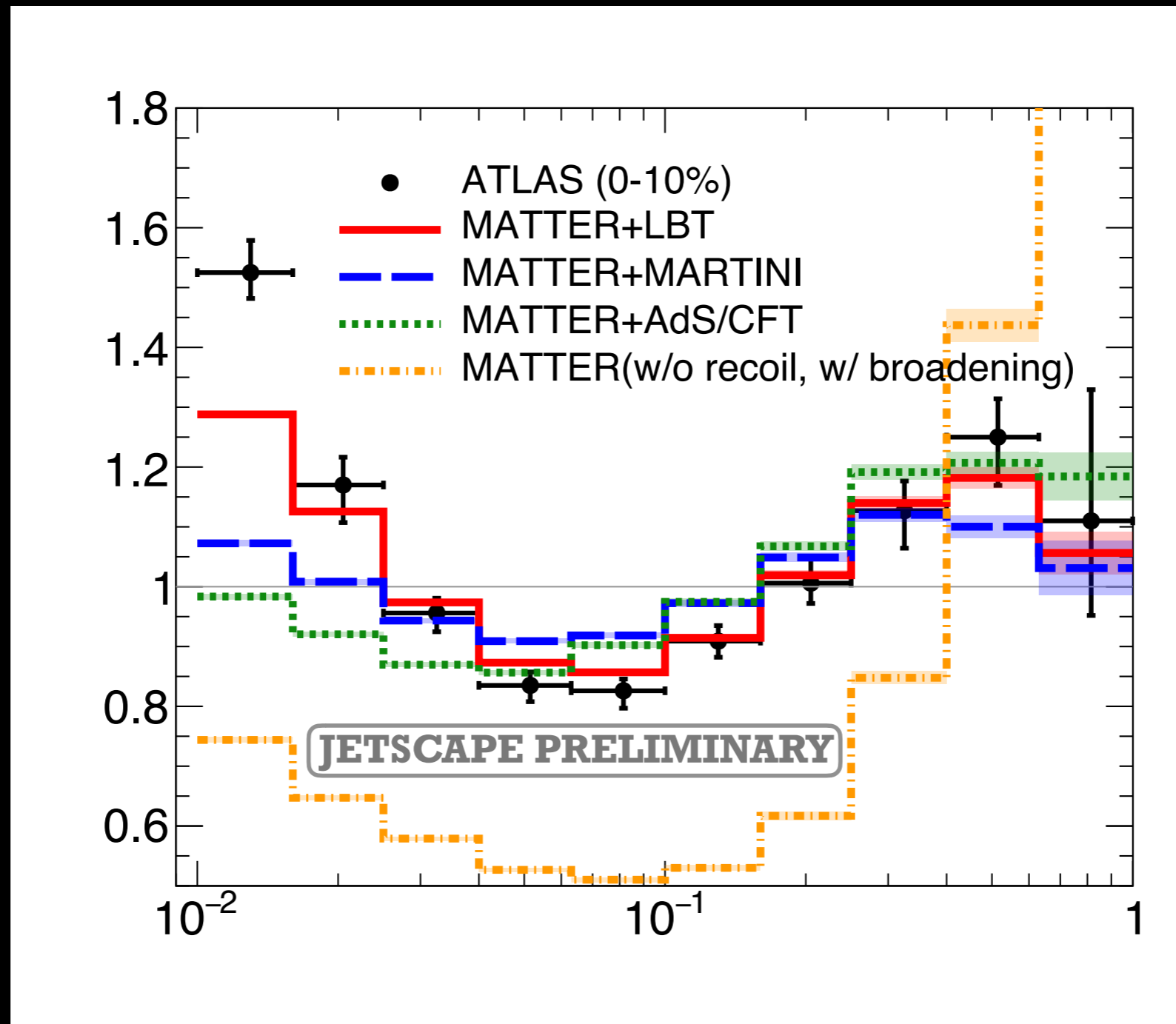


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**PbPb/pp**



# Fragmentation function



fraction of energy carried by hadrons in jet

# Outcome from JETSCAPE

- 1) Very good description of most of the data
- 2) Minor discrepancies in p-p: need better tuning
- 3) Minor discrepancies in A-A: better phenomenology (modeling medium response)
- 4) Plain broadening or drag does not seem to work
- 5) Partonic recoil has a lot of success (Sensitivity to recoil kernel?)

# Going from AA to eA

- 1) No hadronic energy loss
- 2) Minimal hadronic response
- 3) Hadronization in a hadronic medium?
- 4) Simulation of event activity
- 5) Simulation of TMDPDFs/GPDs/spin dependent objects

# Modeling differences in leading hadrons

Assuming nuclear PDF =  
 $A \times$  nucleon p. d. f.

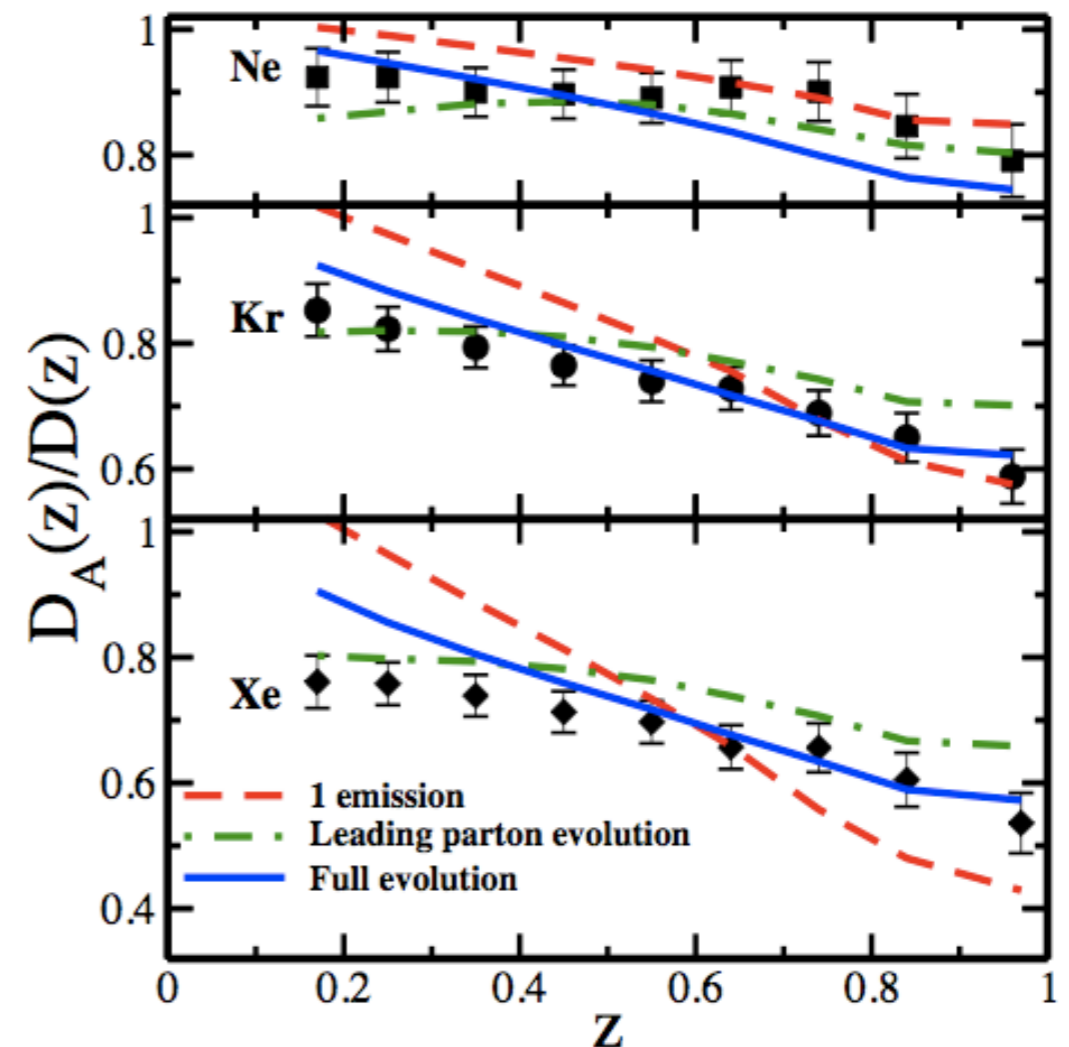
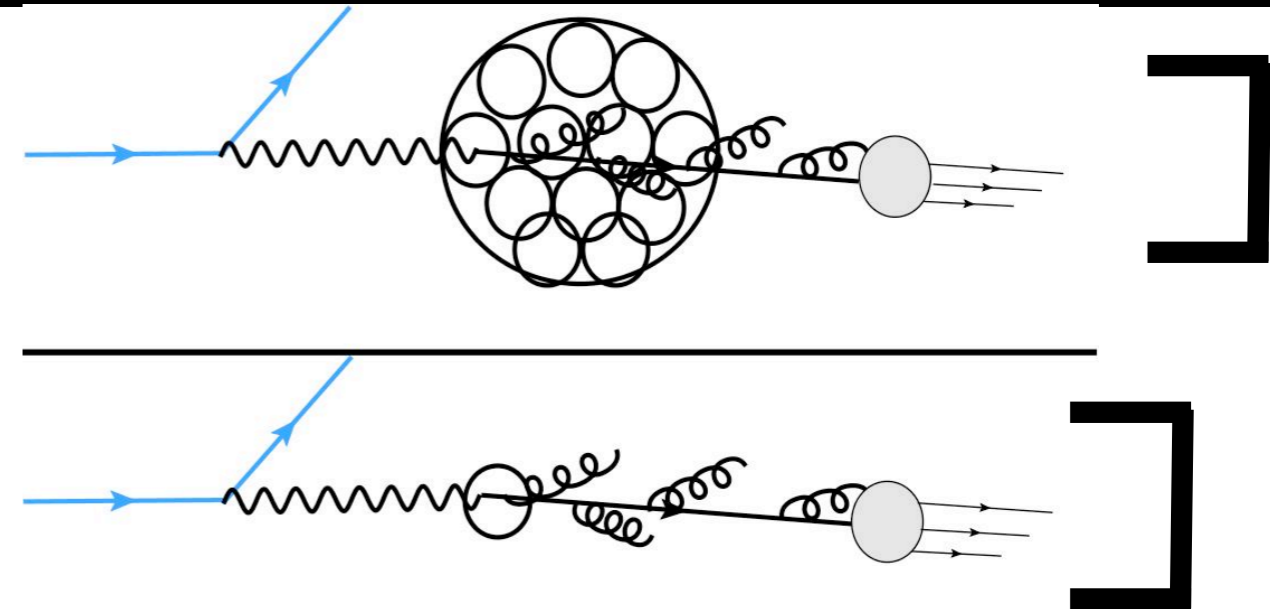
Data from HERMES at DESY

Three different nuclei

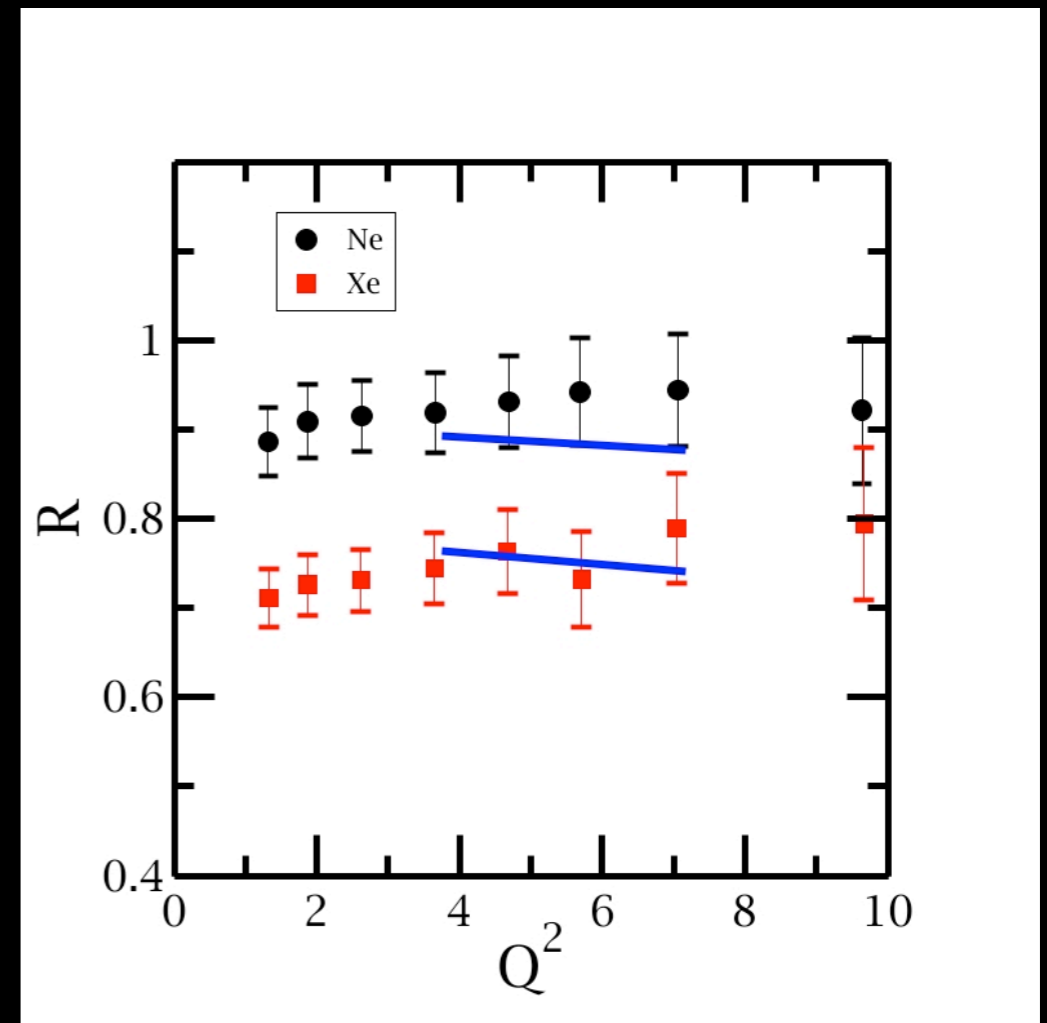
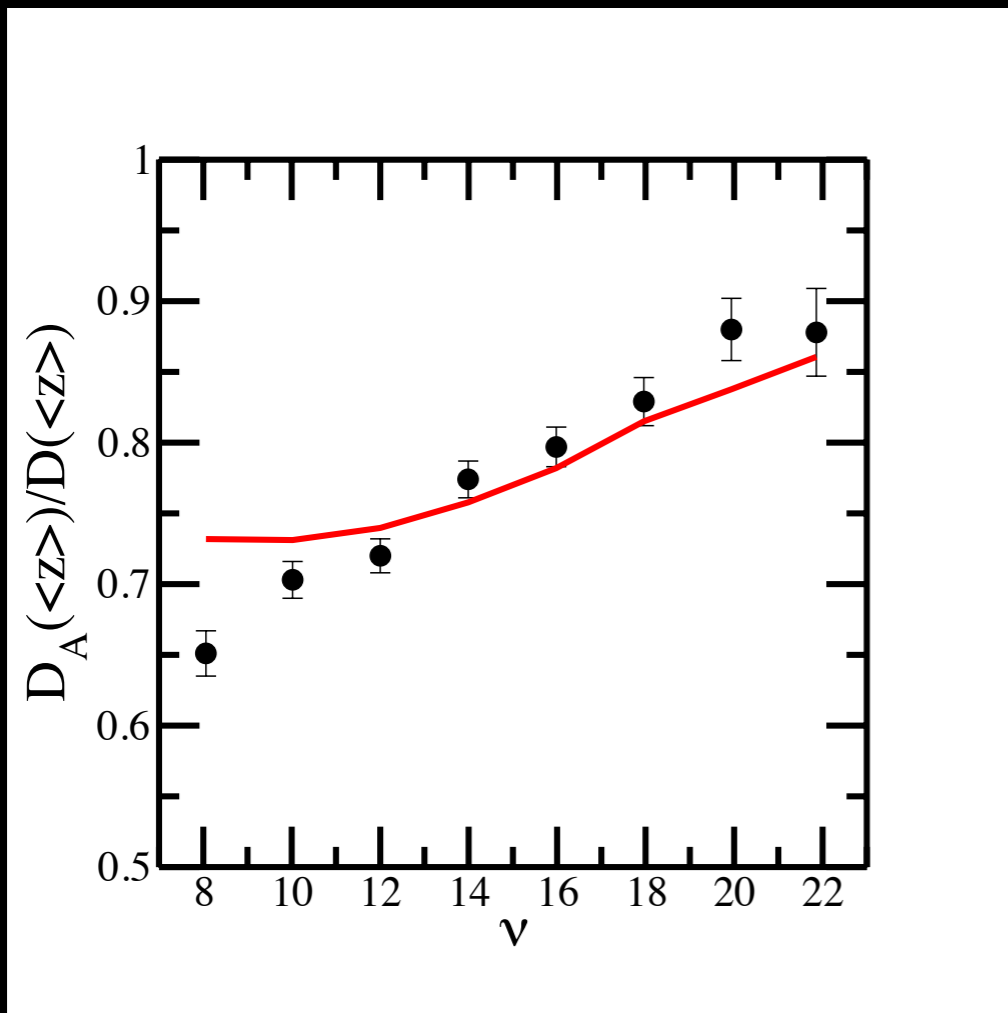
one  $\hat{q} = 0.08 \text{ GeV}^2/\text{fm}$

Fit one data point in Ne  
 everything else is prediction

$Q^2 = 3-4 \text{ GeV}^2$ ,  $\nu = 16-20 \text{ GeV}$



# The $\nu$ and $Q^2$ dependence



Modeling approximations made!

$$\tilde{D}(z, Q^2, \nu) \Big|_{\zeta}^{\zeta_f} \longrightarrow \tilde{D}(z, Q^2, \nu) \Big|_{\zeta_i}^{\zeta_f}$$



# Xin-Nian's version

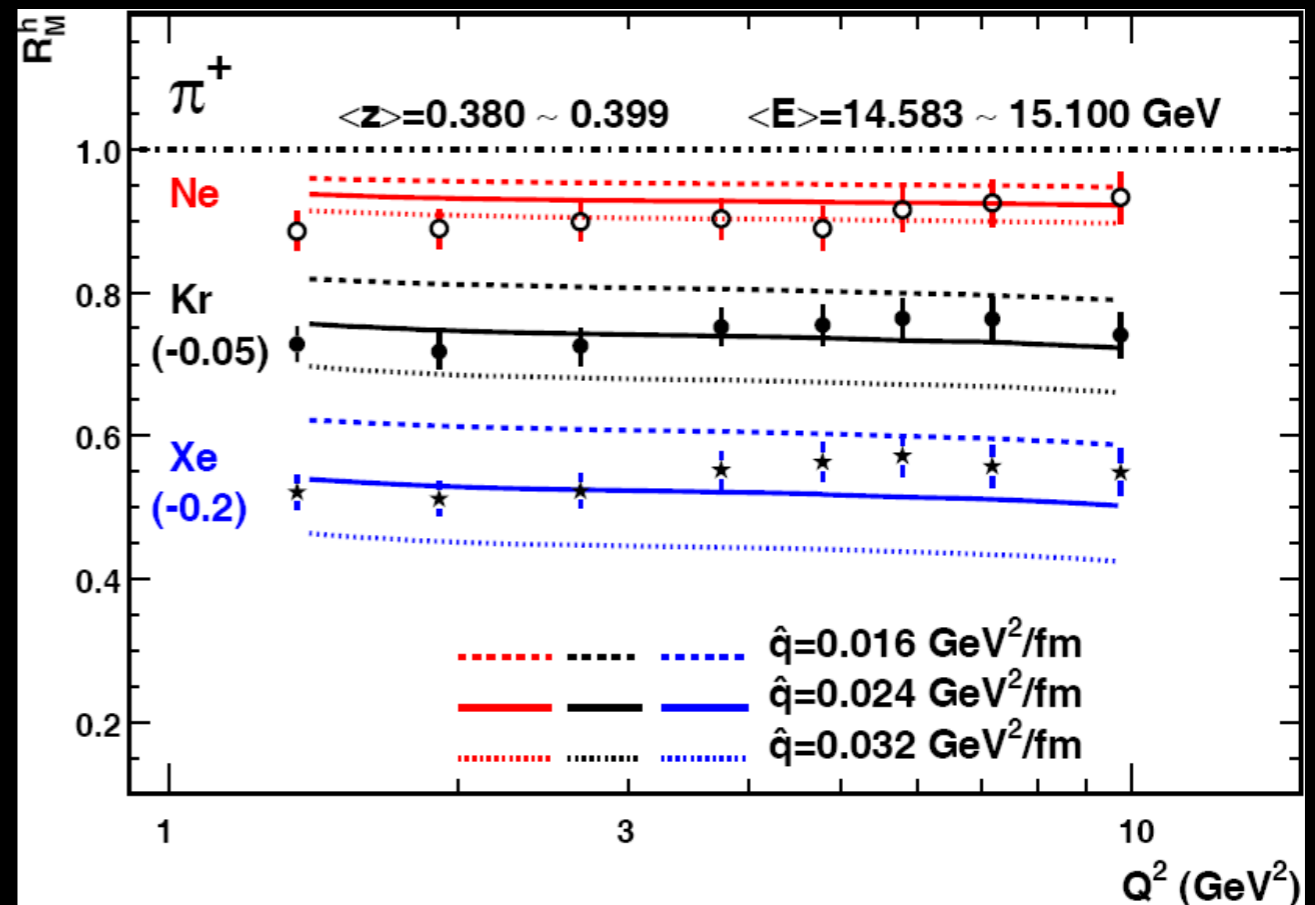
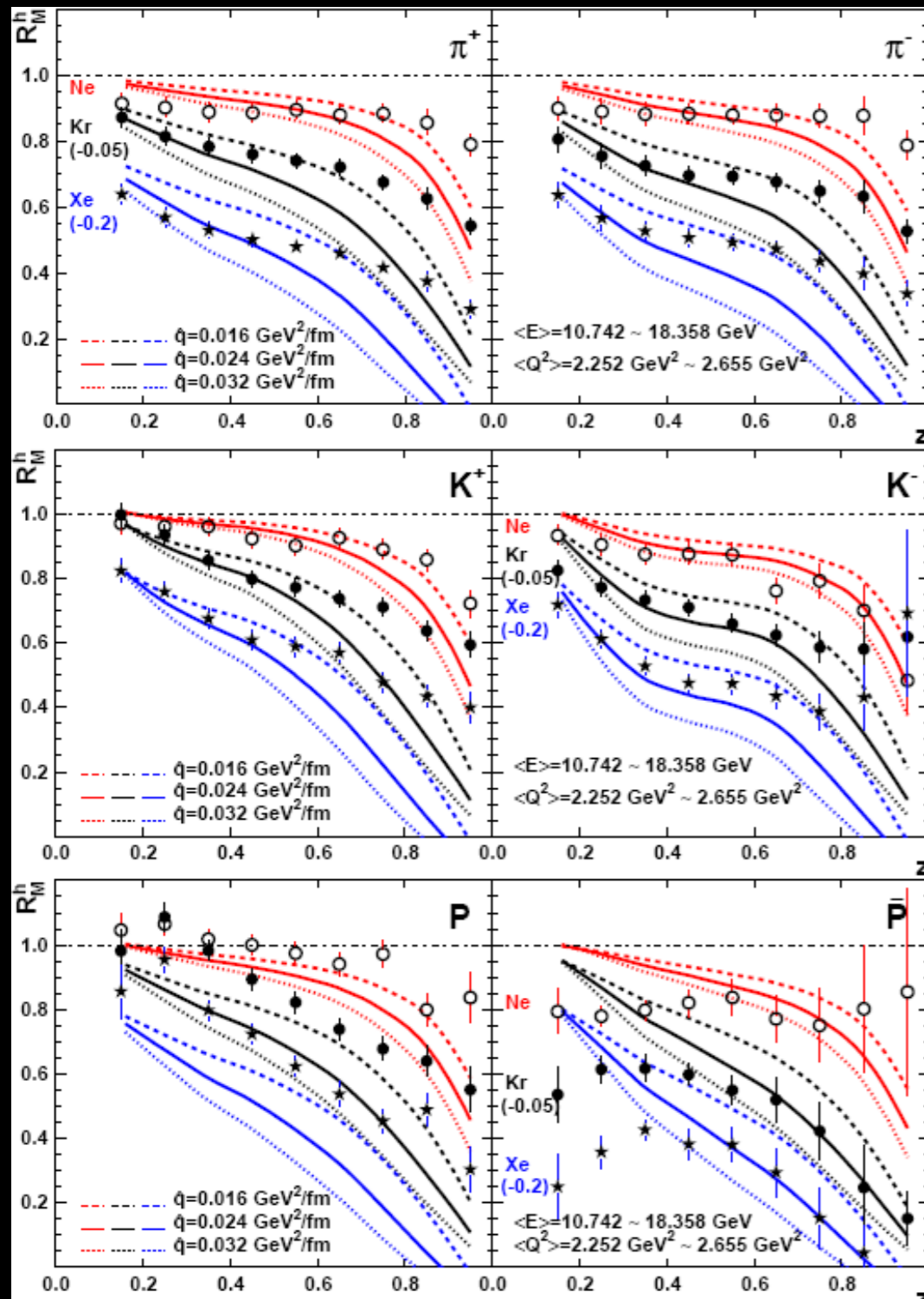
instead of vacuum FF as input

use a real **Medium modified FF**

Idea: Jet never drops below

$\mu = 1 \text{ GeV}$

in principle the MMFF input has to be measured in expt.



Thank you for your attention!