

Towards generalization of low x evolution equations

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Based on papers:

M. Hentschinski, A. Kusina, K.K, M. Serino; Eur.Phys.J. C78 (2018) no.3, 174

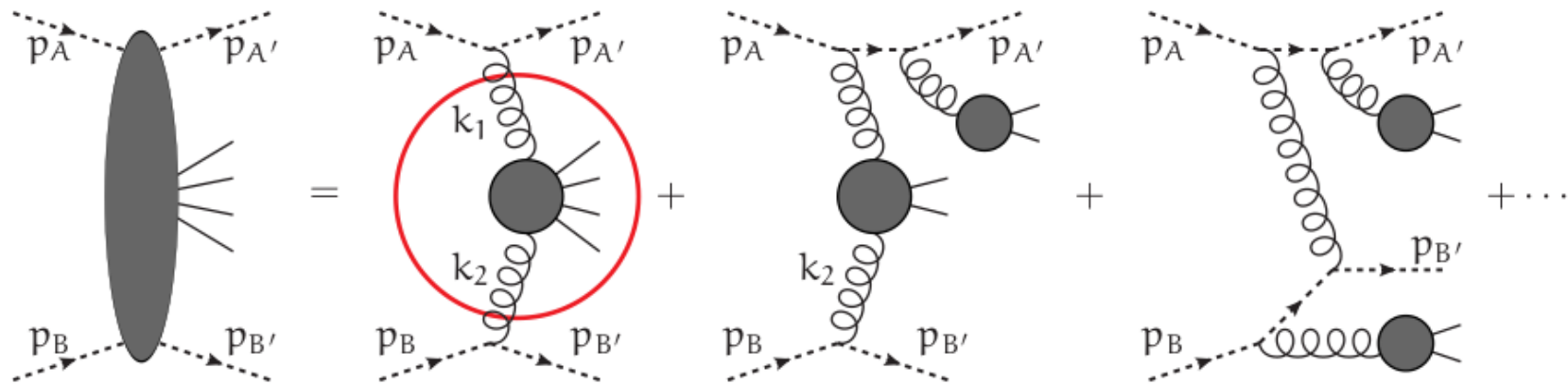
M. Hentschinski, A. Kusina, K.K; Phys. Rev. D 94, 114013 (2016)

O. Gituliar, M. Hentschinski, K.K; JHEP 1601 (2016) 181

Hard coefficient functions in kt factorization:

One consider embedding off-shell amplitude in on-shell and introduces eikonal lines

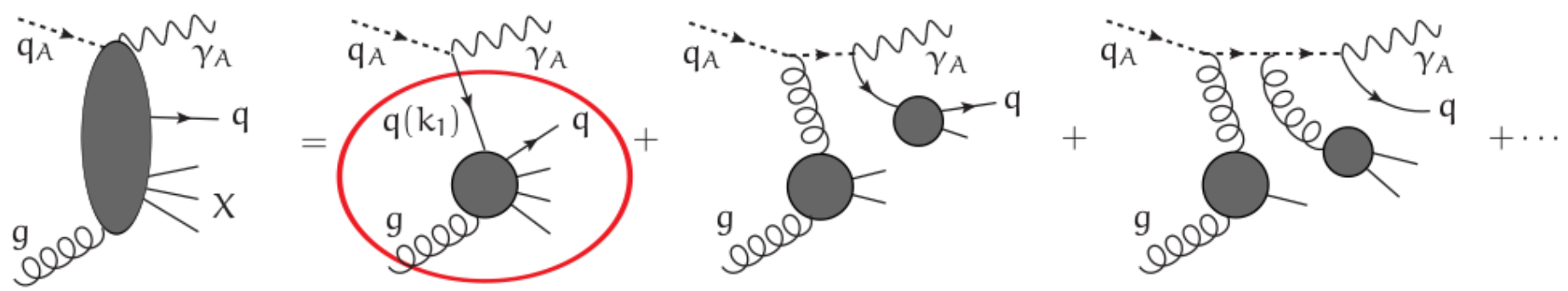
Kotko, KK, van Hameren 2013,
KK, Salwa, van Hameren 2013



$$j \xrightarrow{\text{wavy}} i = -i \delta_{i,j} u(p_1)$$

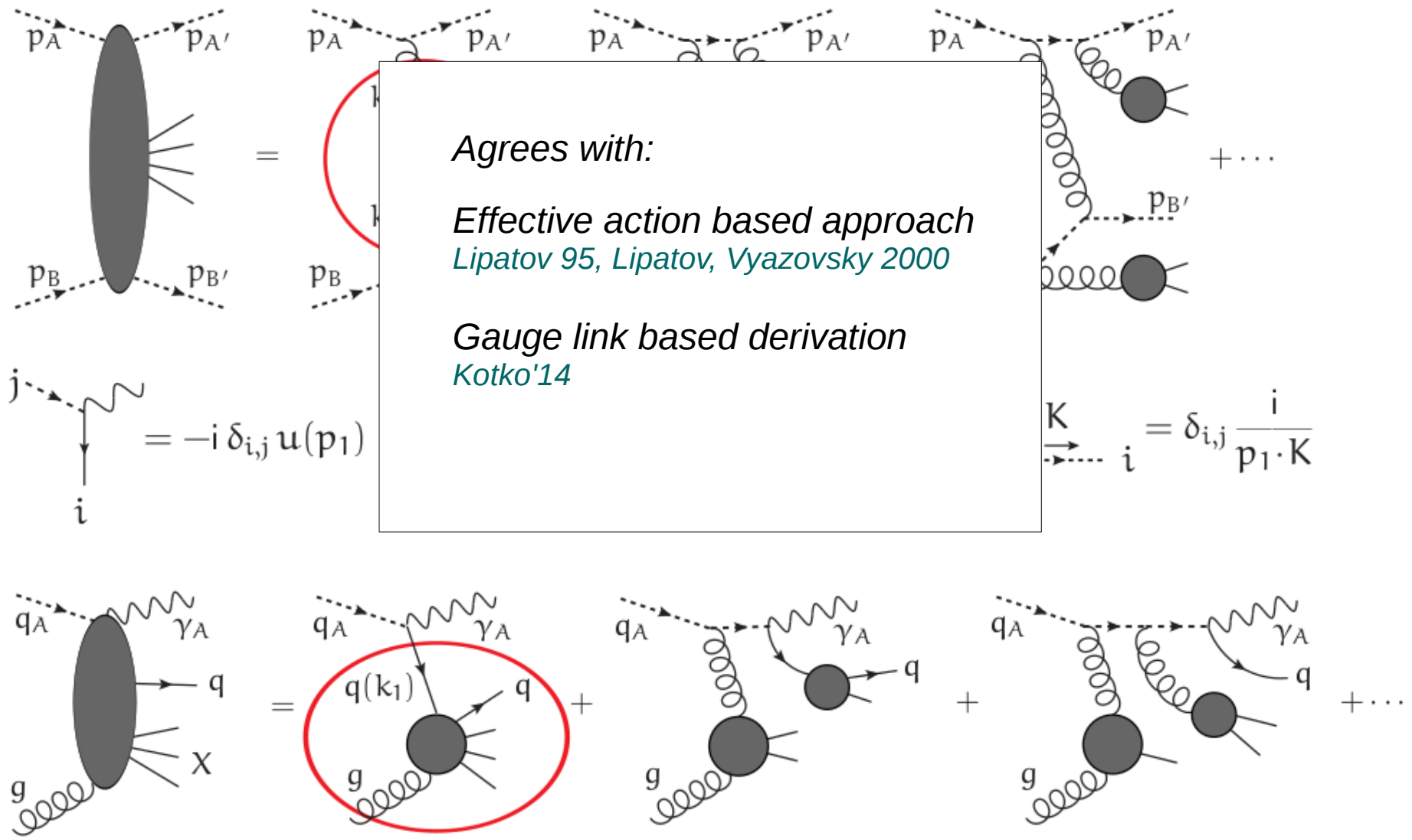
$$j \xrightarrow{\text{wavy}} i = -i T_{i,j}^a p_i^\mu$$

$$j \xrightarrow{K} i = \delta_{i,j} \frac{i}{p_1 \cdot K}$$



Hard coefficient functions in HEF:

Kotko, KK, van Hameren 2013,
 KK, Salwa, van Hameren 2013



Evolution- in HEF, CGC

USE higher order corrections to BFKL/BK/JIMWLK

but:

What about evolution of quarks? Can one get in some limit complete DGLAP at least an LO?

Use CCFM includes “1/z” and “1/(1-z)” terms of splitting function, depends on hard scale

but:

does not allow to account for finite terms like “z(1-z)”. Jumps from low z to large z.

Framework limited only to gluons. Limited description of data.

Framework by Balitsky and Tarasov: large “z”, small “z”, moderate “z”, Sudakov, nonlinearity, spin dependence. The same kinematics in the kernel as in our approach.

but:

limited so far to gluons only. Not clear how to deal with it numerically

Kimber, Martin, Ryskin, Watt or “Parton Branching” Jung et al [1804.11152](#) provides full set of TMD pdfs.

but:

DGLAP based only integral version fully consistent. They should be at least refitted.

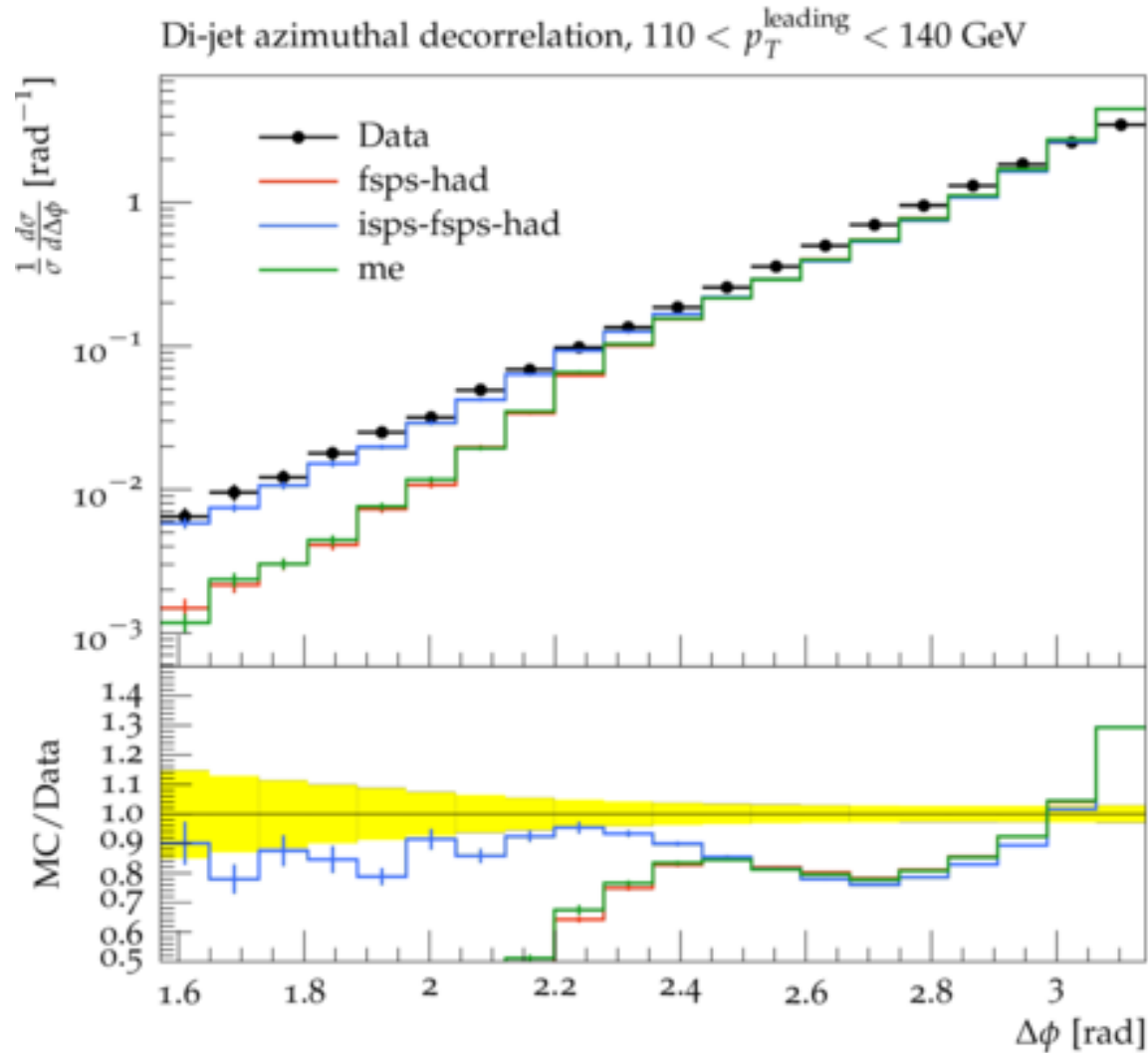
Ciafaloni, Colferai, Staśto, Salam [JHEP 0708:046,2007](#) → ansatz for system of equations unifying DGLAP and BFKL.

but

quark splitting functions are k_t independent.

Example- dijets- azimuthal angle correlations – central region

M. Bury, A. van Hameren, H. Jung, KK, S. Sapeta, M. Serino '17



Simulation in
KaTie+ CASCADE

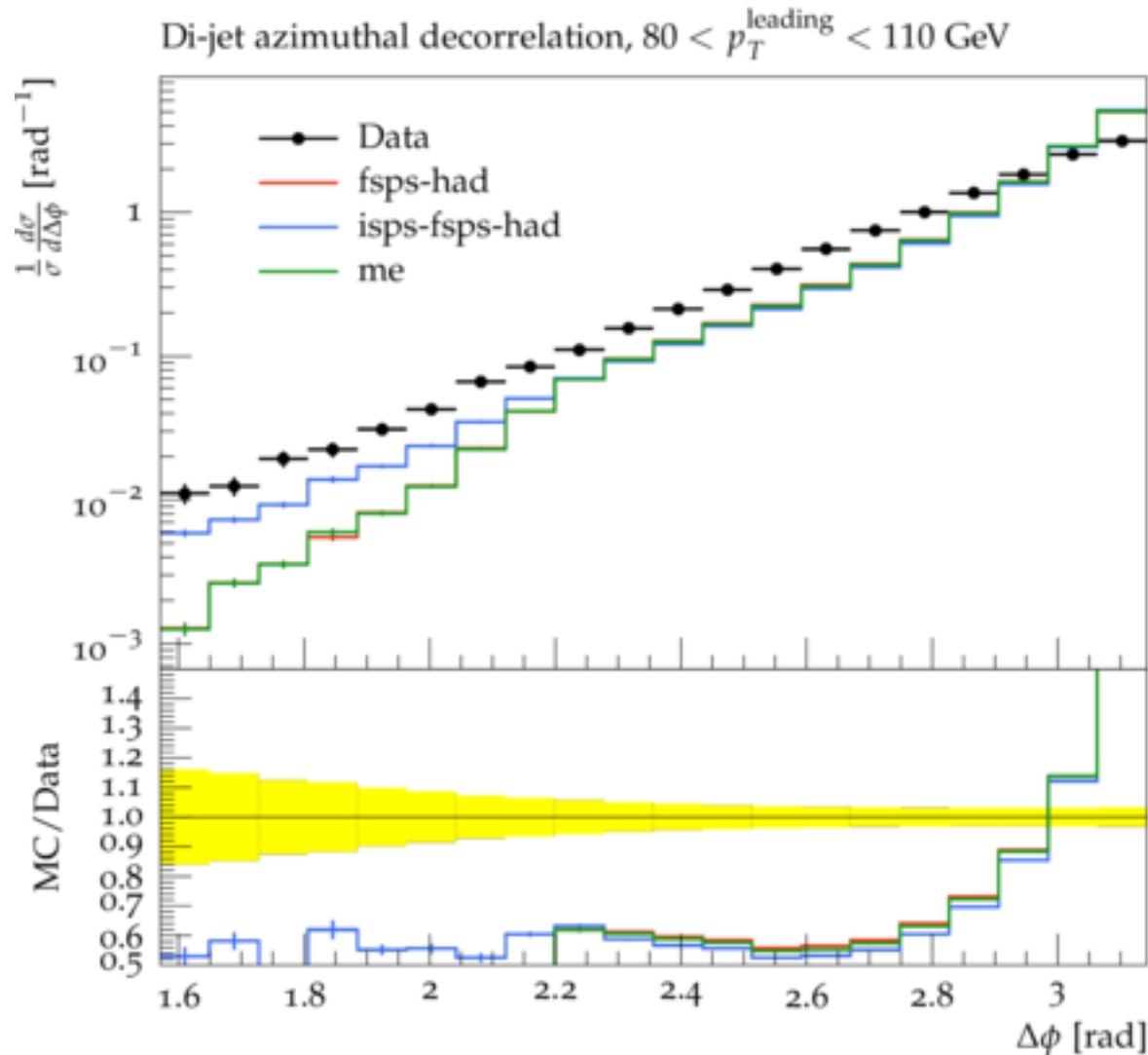
KMR
pdfs used
unintegrated
DGLAP based

Together with
off-shell ME

as obtained
from KaTie
ME generator

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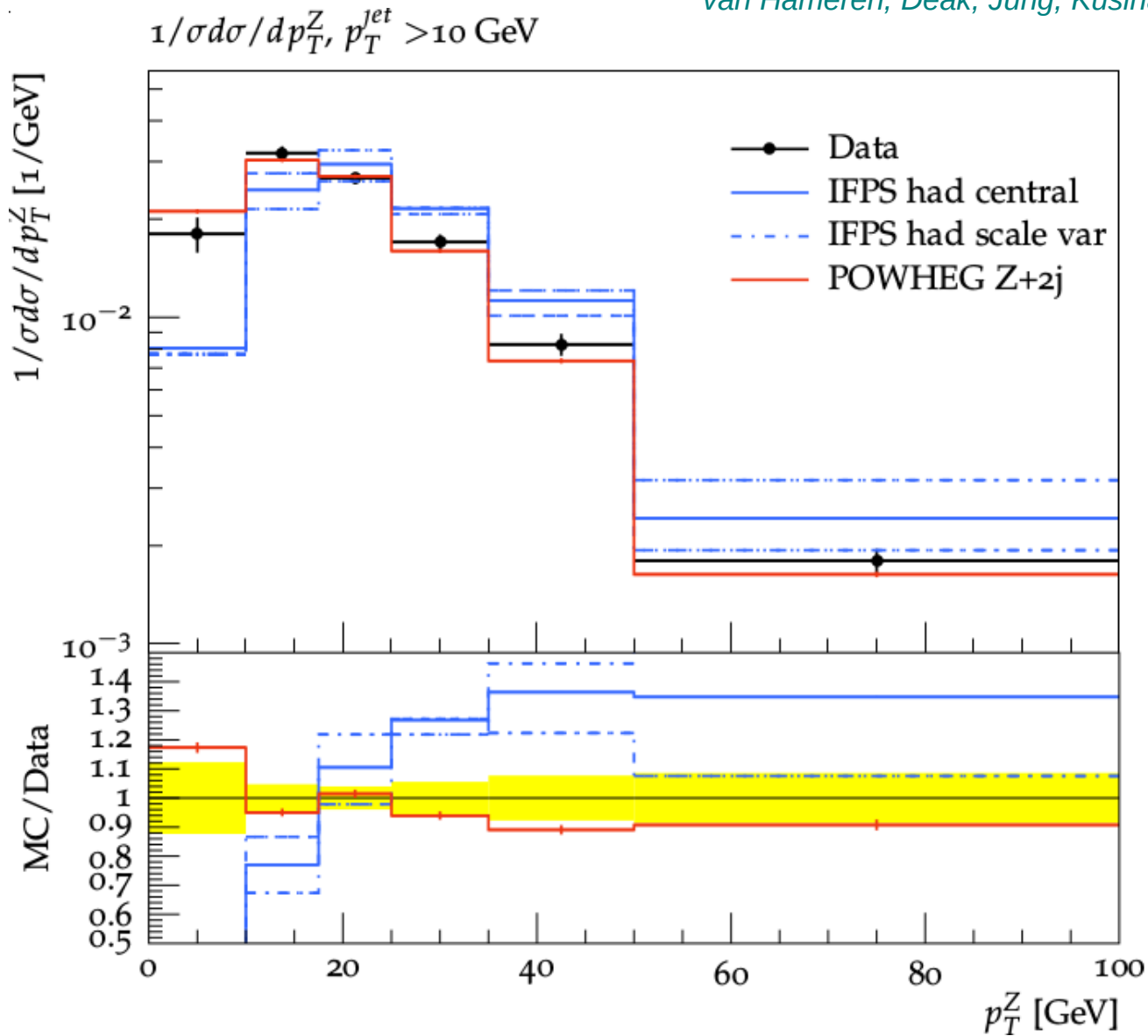
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Example- Z+jet- p_T of Z

van Hameren, Deak, Jung, Kusina, Kutak, M. Serino '18



*Simulation in
KaTie+ CASCADE*

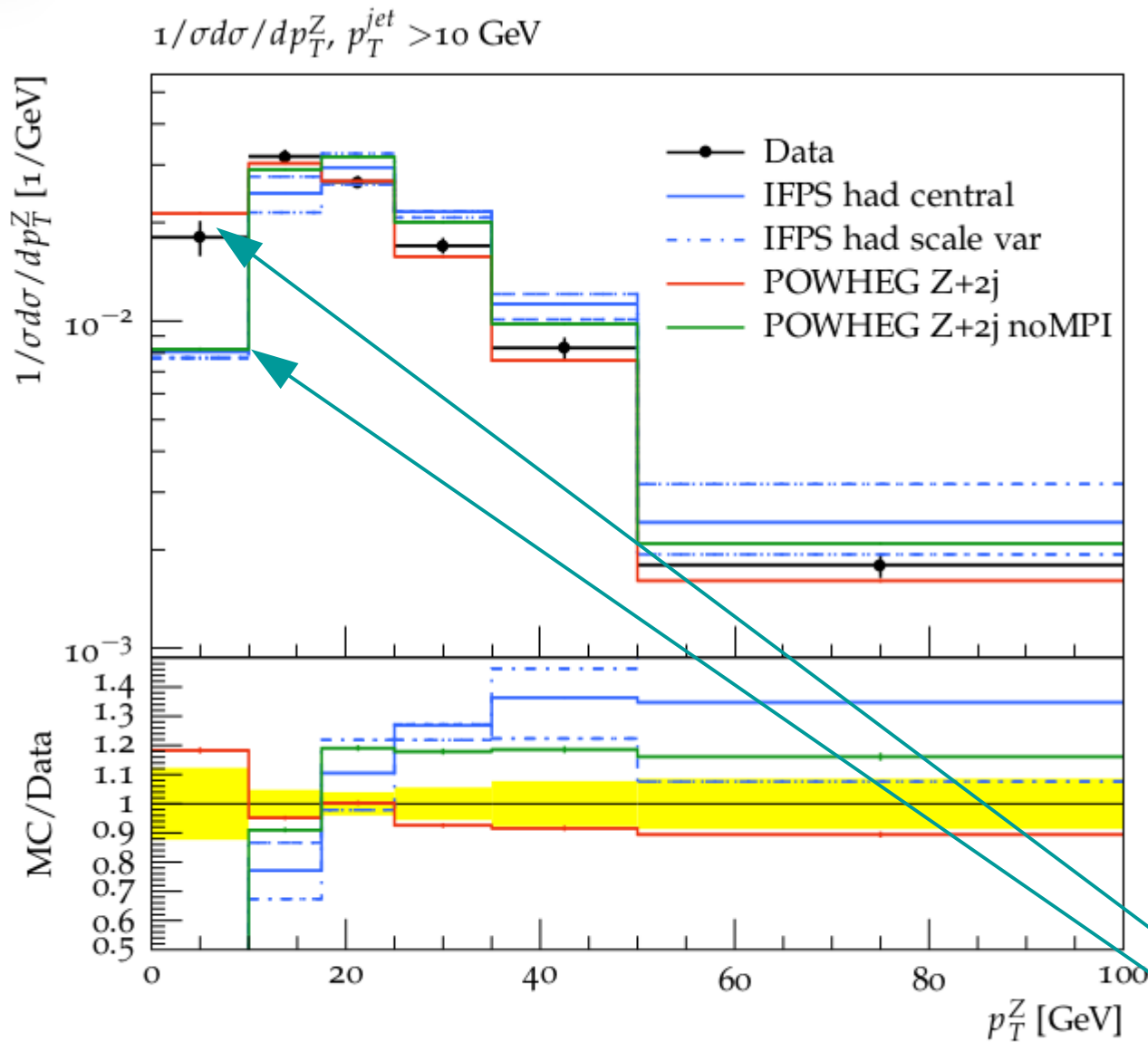
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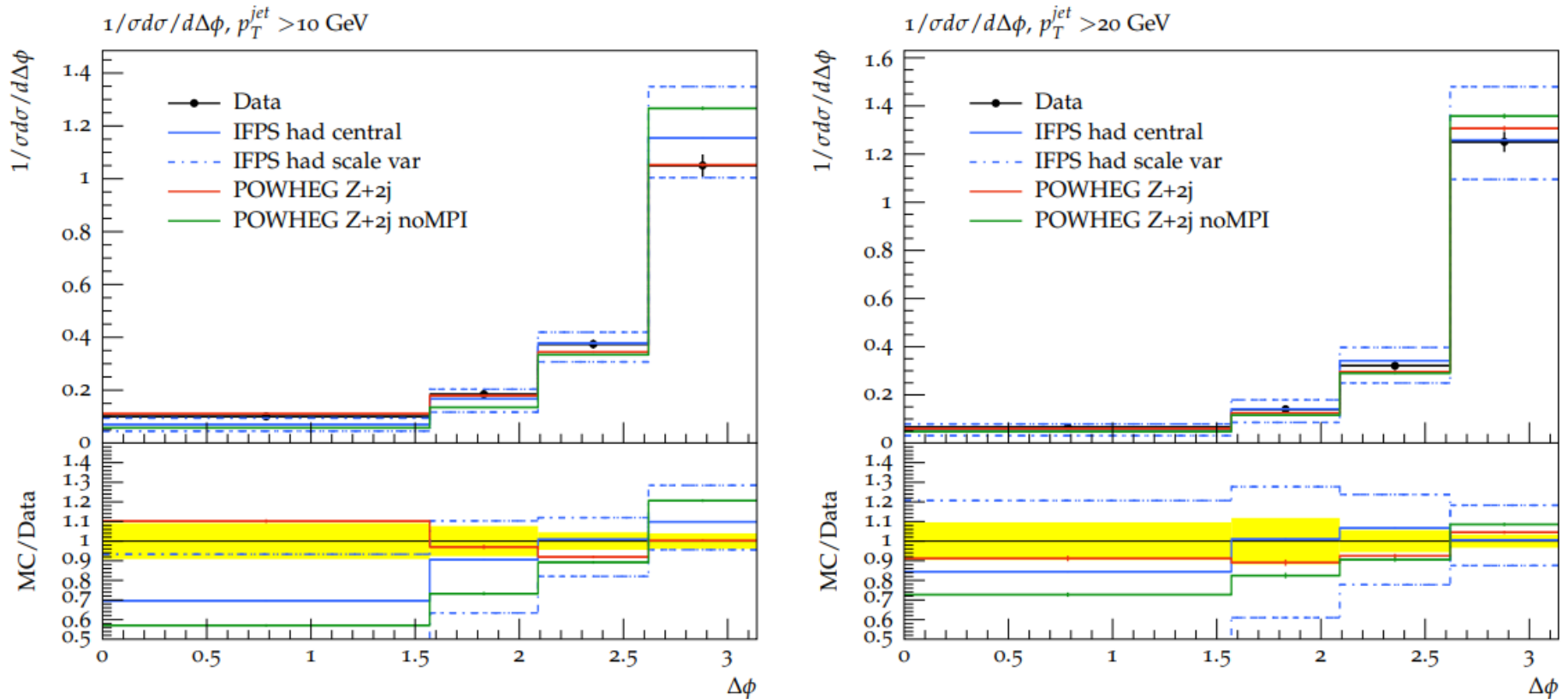
*Together with
off-shell ME
as obtained
from*

*KaTie
ME generator*

*Large contribution
from MPI in
POWHEG*

Example- Z+jet- decorelations

van Hameren, Deak, Jung, Kusina, Kutak, M. Serino '18



Simulation in KaTie+ CASCADE + Parton Branching pdfs used unintegrated DGLAP based Together with off-shell ME as obtained from KaTie ME generator

The goal

- *go beyond DGLAP and BFKL by generalized splitting kernel*
- *coverage of all “z” regions*
- *extend evolution towards large x*
- *reproduce collinear limit (DGLAP)*
- *reproduce BFKL in low “z” limit*
- *k_T -dependent splitting functions*
- *in longer term goal: to describe large class of exclusive processes*

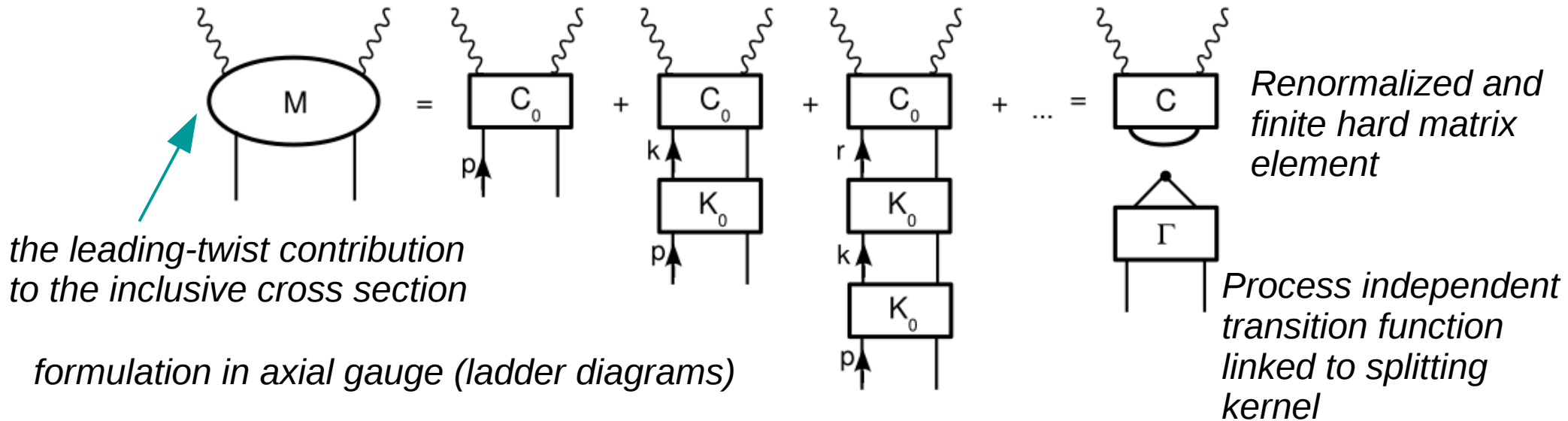
We aim at will achieving this goals by using Curci-Furmanski-Petronzio (CFP) and Catani-Hautmann (CH) formalisms.

Curci, Furmanski, Petronzio Nucl. Phys. B175 (1980) 27

Catani, Hautmann NPB427 (1994) 475524

Curci-Furmanski-Petronzio method

Factorization based on generalized ladder expansion (in terms of Two Particle Irreducible (2PI) kernels)



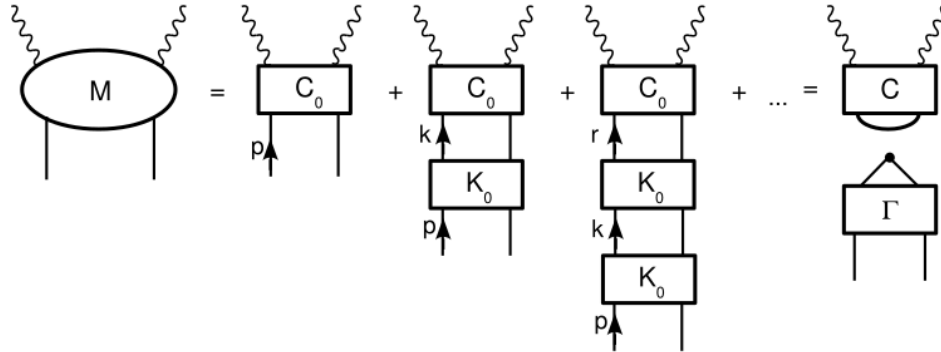
C_0 hard scattering coefficient function

K_0 2PI kernels connected only by convolution in x this is achieved by introducing appropriate projector operators

How does it work....

Curci-Furmanski-Petronzio

- factorization



*notation from CFP paper
they studied Pqq*

$$k_\mu = x_\mu + \alpha n_\mu + k_\perp \mu$$

*finite (M – pole part is
finite)*

$$M = \frac{1}{2} C_0 K_0 \not{p} = \frac{1}{2} C_0 \mathbb{P} K_0 \not{p} + \frac{1}{2} C_0 (1 - \mathbb{P}) K_0 \not{p}$$

$$\frac{1}{2} C_0 \mathbb{P} K_0 \not{p} = \frac{1}{2} C_0 \mathbb{P}_\epsilon \mathbb{P}_s K_0 \not{p}$$

*the projector performs
integral over phase
space of “k” and
extracts poles*

*C₀ hard scattering
coefficient function*

K₀ 2PI kernels

$$= \frac{1}{2} C_0 \mathbb{P}_\epsilon \mathbb{P}_{out} K_0 \mathbb{P}_{in}$$

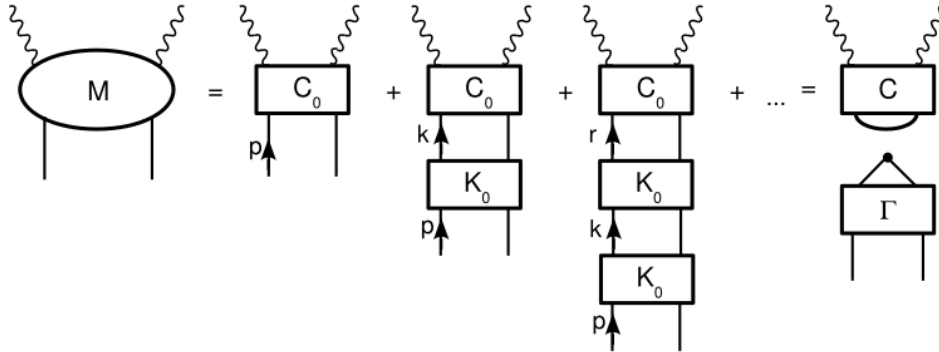
$$= \int \frac{dx}{x} \frac{1}{2} C_0 \mathbb{P}_{out} |_{k^2=0} \Gamma\left(\frac{Q^2}{\mu_F^2}, x, \frac{1}{\epsilon}\right)$$

*factorization
convolution only
in “x”*

*pole part
spin part*

Curci-Furmanski-Petronzio

- factorization



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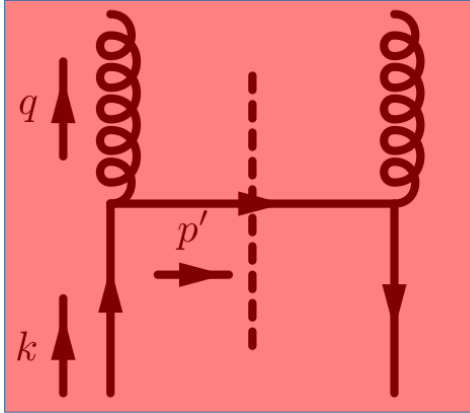
C_0 hard scattering
coefficient function

K_0 2PI kernels

pole part
spin part

Curci-Furmanski-Petronzio

- splitting function



- incoming propagators amputated
- contains propagator of outgoing parton + incoming on-shell

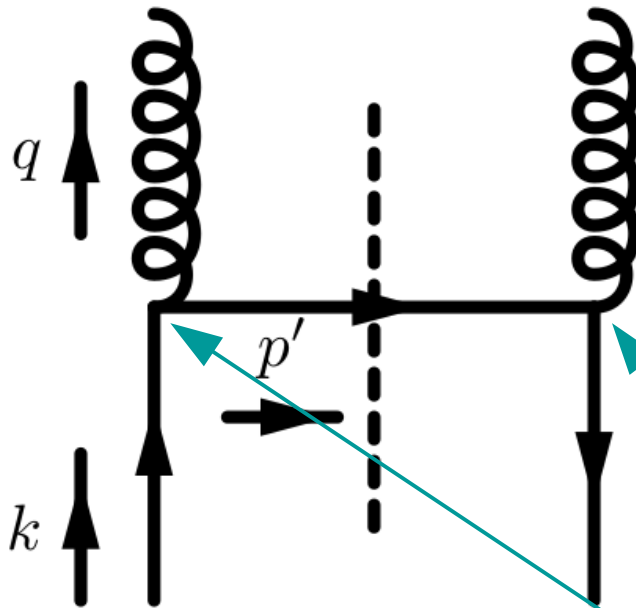
The CFP method applied to construct splitting functions

$$\Gamma \sim \hat{K}_{ij} \left(z, \frac{\mathbf{k}^2}{\mu^2}, \epsilon, \alpha_s \right) = z \int \frac{dq^2 d^{2+2\epsilon} \mathbf{q}}{2(2\pi)^{4+2\epsilon}} \Theta(\mu_F^2 + q^2) \mathbb{P}_{j, \text{in}} \otimes \hat{K}_{ij}^{(0)}(q, k) \otimes \mathbb{P}_{i, \text{out}}$$

$$= \frac{\alpha_s}{2\pi\Gamma(1+\epsilon)} z \int_0^{\mu_F^2} \frac{dq^2}{q^2} \left(\frac{e^{-\gamma_E q^2}}{\mu^2} \right)^\epsilon P_{ij}^{(0)}(z; \epsilon)$$

The method can be used to prove factorization and to derive evolution equations

Generalization to HEF kinematics



$$q^\mu = xp^\mu + q_\perp^\mu + \frac{q^2 + \mathbf{q}^2}{2x p \cdot n} n^\mu$$

$$k^\mu = yp^\mu + k_\perp^\mu \quad \text{ordering in "-" components}$$

Catani, Hautmann NPB427 (1994) 475524

F. Hautmann, M. Hentschinski, H. Jung
Nucl.Phys. B865 (2012) 54-66

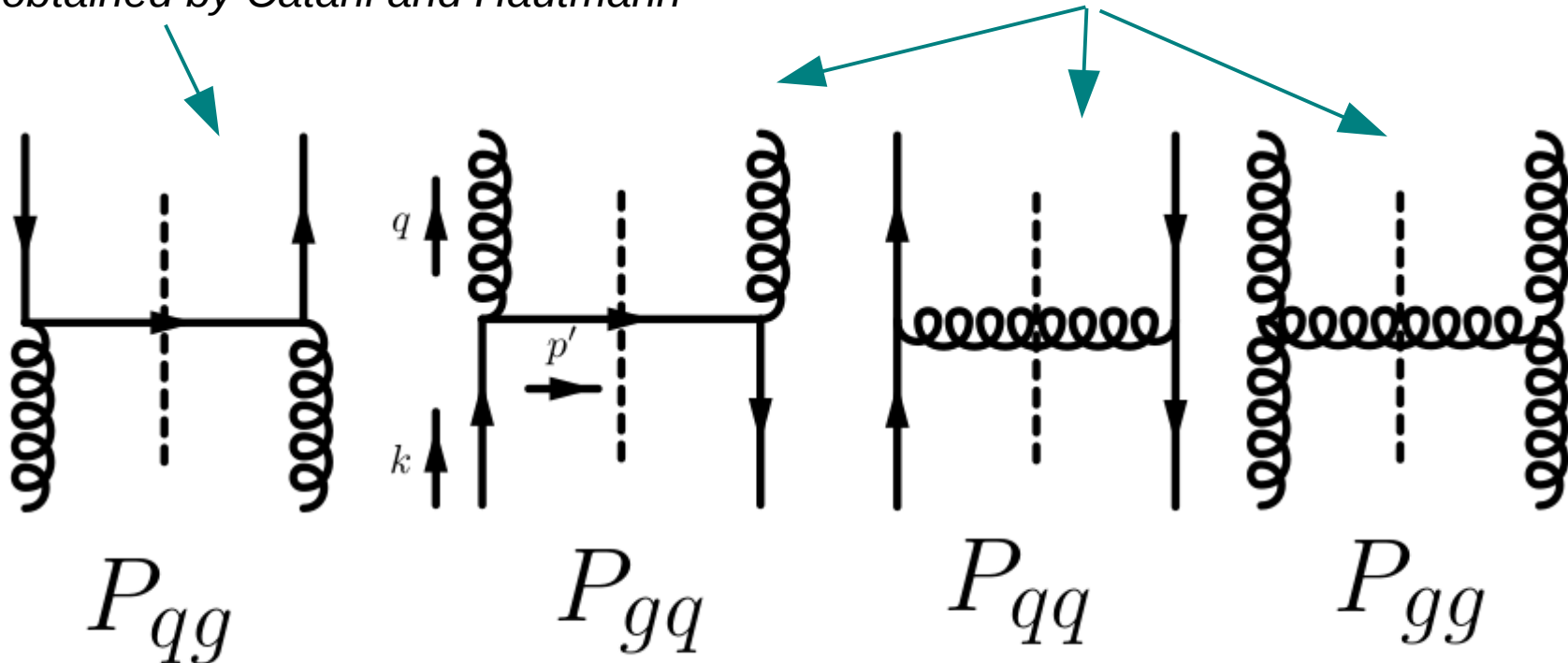
We will define and constrain splitting functions by requiring:

- gauge invariance/current conservation of vertices
- appropriate projector operators (can be obtained from Lipatov effective action or equivalently by spin helicity method)
- HEF limit, collinear limit

Generalization to HEF kinematics

O. Gituliar, M. Hentschinski, K.K; JHEP 1601 (2016) 181
Hentschinski, Kusina, KK, Serino '17

Kernel obtained by Catani and Hautmann



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- HEF limit, collinear limit

CH kernel

Application of the method to P_{qg}

Usage of axial gauge. The outgoing projector is the same for quark as in the original CFP

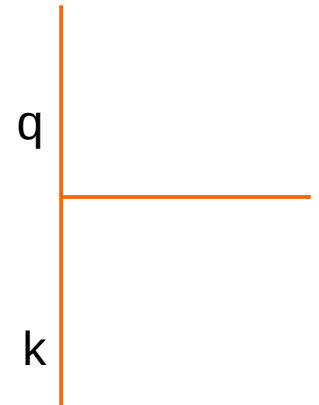
The projector for incoming gluons obtained from

$$\mathcal{M}^{g^* g^* \rightarrow q\bar{q}}(k_1, k_2; p_3, p_4) = \frac{2 y_1 y_2 p_1^{\mu_1} p_2^{\mu_2}}{\sqrt{k_{1\perp}^2 k_{2\perp}^2}} d_{\mu_1 \nu_1}(k_1) d_{\mu_2 \nu_2}(k_2) \hat{\mathcal{M}}_{\mu_1, \mu_2}^{g^* g^* \rightarrow q\bar{q}}(k_1, k_2; p_3, p_4)$$

$$y_1 p_1^{\mu_1} d_{\mu_1 \nu_1}(k_1) = k_{1\perp \nu_1} \quad y_2 p_2^{\mu_2} d_{\mu_2 \nu_2}(k_2) = k_{2\perp \nu_2}$$

$$\mathbb{P}_{g,in}^{S \mu\nu} = -\frac{k_{\perp}^{\mu} k_{\perp}^{\nu}}{k_{\perp}^2} \quad \mathbb{P}_{q,out}^S = \frac{\not{n}}{2q \cdot n}$$

$$\tilde{\mathbf{q}} = \mathbf{q} - z\mathbf{k}$$

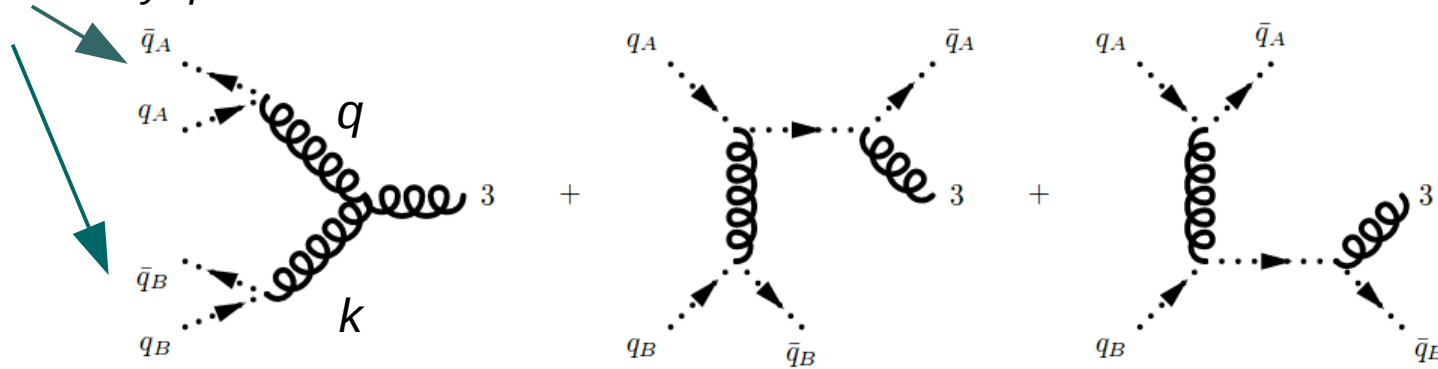


$$\bar{P}_{qg}^{(0)} = T_R \left(\frac{\tilde{\mathbf{q}}^2}{\tilde{\mathbf{q}}^2 + z(1-z)\mathbf{k}^2} \right)^2 \left[z^2 + (1-z)^2 + 4z^2(1-z)^2 \frac{\mathbf{k}^2}{\tilde{\mathbf{q}}^2} \right]$$

Vertices – example derivation

M. Hentschinski, A. Kusina, K.K, M. Serino; Eur.Phys.J. C78 (2018) no.3, 174

auxiliary quarks



$$\mathcal{A}(q, k, p') = (\sqrt{2}) \frac{p_{\mu_1} n_{\mu_2} \epsilon_{\mu_3}(p')}{q^2 k^2} \left\{ \mathcal{V}^{\lambda\kappa\mu_3}(q, k, p') d^{\mu_1}_{\lambda}(q) d^{\mu_2}_{\kappa}(k) \right. \\ \left. + d^{\mu_1\mu_2}(k) \frac{q^2 n^{\mu_3}}{n \cdot p'} - d^{\mu_1\mu_2}(q) \frac{k^2 p^{\mu_3}}{p \cdot p'} \right\} \\ \equiv (\sqrt{2}) \frac{p_{\mu_1} n_{\mu_2} \epsilon_{\mu_3}(p')}{q^2 k^2} \Gamma^{\mu_1\mu_2\mu_3}(q, k, p')$$

current conservation w.r.t outgoing gluon

$q \rightarrow$ general kinematics

$k \rightarrow$ HEF

Full set of projectors

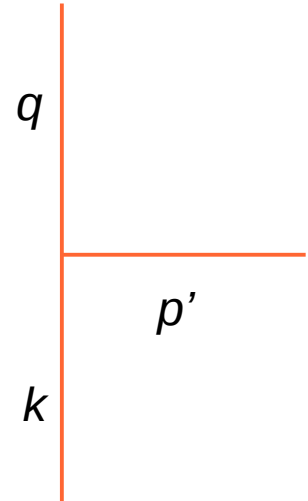
Constrained by Ward identities and appropriate limits the splitting functions should have correct DGLAP and BFKL limits we have the following projectors

$$\mathbb{P}_{g, \text{in}}^{s \mu\nu} = -y^2 \frac{p^\mu p^\nu}{k_\perp^2}$$

$$\mathbb{P}_{g, \text{out}}^{s \mu\nu} = -g^{\mu\nu} + \frac{k^\mu n^\nu + k^\nu n^\mu}{k \cdot n} - k^2 \frac{n_\mu n_\nu}{(k \cdot n)^2}$$

$$\mathbb{P}_{q, \text{in}}^s = \frac{y \not{p}}{2}$$

$$\mathbb{P}_{q, \text{out}}^s = \frac{\not{n}}{2 n \cdot l}$$



$$q^\mu = x p^\mu + q_\perp^\mu + \frac{q^2 + \mathbf{q}^2}{2x p \cdot n} n^\mu$$

$$k^\mu = y p^\mu + k_\perp^\mu$$

Full set of vertices

M. Hentschinski, A. Kusina, K.K, M. Serino; Eur.Phys.J. C78 (2018) no.3, 174

$$\Gamma_{q^* g^* q}^\mu(q, k, p') = igt^a d^\mu{}_\nu(k) \left(\gamma^\nu - \frac{n^\nu}{k \cdot n} \not{n} \right)$$

$$\Gamma_{g^* q^* q}^\mu(q, k, p') = igt^a d^\mu{}_\nu(q) \left(\gamma^\nu - \frac{p^\nu}{p \cdot q} \not{k} \right)$$

$$\Gamma_{q^* q^* g}^\mu(q, k, p') = igt^a \left(\gamma^\mu - \frac{p^\mu}{p \cdot p'} \not{k} + \frac{n^\mu}{n \cdot p'} \not{n} \right)$$

$$\Gamma_{g^* g^* g}^{\mu_1 \mu_2 \mu_3}(q, k, p') = i g f^{abc} \left\{ \mathcal{V}^{\lambda \kappa \mu_3}(q, k, p') d^{\mu_1}{}_\lambda(q) d^{\mu_2}{}_\kappa(k) \right. \\ \left. + d^{\mu_1 \mu_2}(k) \frac{q^2 n^{\mu_3}}{n \cdot p'} - d^{\mu_1 \mu_2}(q) \frac{k^2 p^{\mu_3}}{p \cdot p'} \right\}$$

Obtained using spinor helicity methods

Van Hameren, Kotko, Kutak, JHEP 1301 (2013) 078

remark: can be obtained
from Lipatov effective action

Example calculation of splitting function: P_{gg} case

M. Hentschinski, A. Kusina, K.K, M. Serino; Eur.Phys.J. C78 (2018) no.3, 174

$$\mathbb{P}_{g, \text{in}} \otimes \hat{K}_{gg}^{(0)}(q, k) \otimes \mathbb{P}_{g, \text{out}} =$$

$$\mathbb{P}_{g, \text{in}}^{\beta\beta'}(k) \mathbb{P}_{g, \text{out}}^{\mu'\nu'}(q) (\Gamma_{g^*g^*g}^{\beta\mu\alpha})^\dagger \Gamma_{g^*g^*g}^{\nu\beta'\alpha'} \frac{-id^{\mu\mu'}(q)}{q^2 - i\epsilon} \frac{id^{\nu\nu'}(q)}{q^2 + i\epsilon} d^{\alpha\alpha'}(k - q)$$

$$\tilde{P}_{gg}^{(0)}(z, \tilde{\mathbf{q}}, \mathbf{k}) = 2C_A \left\{ \frac{\tilde{\mathbf{q}}^4}{(\tilde{\mathbf{q}} - (1-z)\mathbf{k})^2 [\tilde{\mathbf{q}}^2 + z(1-z)\mathbf{k}^2]} \left[\frac{z}{1-z} + \frac{1-z}{z} + \right. \right. \\ \left. \left. + (3-4z) \frac{\tilde{\mathbf{q}} \cdot \mathbf{k}}{\tilde{\mathbf{q}}^2} + z(3-2z) \frac{\mathbf{k}^2}{\tilde{\mathbf{q}}^2} \right] + \frac{(1+\epsilon)\tilde{\mathbf{q}}^2 z(1-z)[2\tilde{\mathbf{q}} \cdot \mathbf{k} + (2z-1)\mathbf{k}^2]^2}{2\mathbf{k}^2[\tilde{\mathbf{q}}^2 + z(1-z)\mathbf{k}^2]^2} \right\}$$

$$\tilde{\mathbf{q}} = \mathbf{q} - z\mathbf{k}$$

Results

M. Hentschinski, A. Kusina, K.K, M. Serino; Eur.Phys.J. C78 (2018) no.3, 174

For sake of presentation: only angular averaged kernels

$$\begin{aligned}
 \bar{P}_{qg}^{(0)} &= T_R \left(\frac{\tilde{q}^2}{\tilde{q}^2 + z(1-z)\mathbf{k}^2} \right)^2 \left[z^2 + (1-z)^2 + 4z^2(1-z)^2 \frac{\mathbf{k}^2}{\tilde{q}^2} \right] \\
 \bar{P}_{gq}^{(0)} &= C_F \left[\frac{2\tilde{q}^2}{z|\tilde{q}^2 - (1-z)^2\mathbf{k}^2|} - \frac{(2-z)\tilde{q}^4 + z(1-z^2)\mathbf{k}^2\tilde{q}^2}{(\tilde{q}^2 + z(1-z)\mathbf{k}^2)^2} \right] \\
 \bar{P}_{qq}^{(0)} &= C_F \frac{\tilde{q}^2}{\tilde{q}^2 + z(1-z)\mathbf{k}^2} \\
 &\quad \left[\frac{\tilde{q}^2 + (1-z^2)\mathbf{k}^2}{(1-z)|\tilde{q}^2 - (1-z)^2\mathbf{k}^2|} + \frac{z^2\tilde{q}^2 - z(1-z)(1-3z+z^2)\mathbf{k}^2}{(1-z)(\tilde{q}^2 + z(1-z)\mathbf{k}^2)} \right] \\
 \bar{P}_{gg}^{(0)} &= C_A \frac{\tilde{q}^2}{\tilde{q}^2 + z(1-z)\mathbf{k}^2} \left[\frac{(2-z)\tilde{q}^2 + (z^3 - 4z^2 + 3z)\mathbf{k}^2}{z(1-z)|\tilde{q}^2 - (1-z)^2\mathbf{k}^2|} \right. \\
 &\quad \left. + \frac{(2z^3 - 4z^2 + 6z - 3)\tilde{q}^2 + z(4z^4 - 12z^3 + 9z^2 + z - 2)\mathbf{k}^2}{(1-z)(\tilde{q}^2 + z(1-z)\mathbf{k}^2)} \right]
 \end{aligned}$$

Kinematic limits P_{gg} – DGLAP BFKL

with this variable one can disentangle singularities

$$\tilde{\mathbf{p}} = \frac{\mathbf{k} - \mathbf{q}}{1 - z}$$

DGLAP limit:

$$\lim_{\mathbf{k}^2 \rightarrow 0} \int_0^{2\pi} d\phi P(z, \mathbf{k}^2, \tilde{\mathbf{p}}^2) = 2C_A \left[\frac{z}{1-z} + \frac{1-z}{z} + z(1-z) \right]$$

BFKL limit:

$$\begin{aligned} \lim_{z \rightarrow 0} \hat{K}_{gg} \left(z, \frac{\mathbf{k}^2}{\mu^2}, \epsilon, \alpha_s \right) &= \frac{\alpha_s C_A}{\pi (e^{\gamma_E} \mu^2)^\epsilon} \int \frac{d^{2+2\epsilon} \tilde{\mathbf{p}}}{\pi^{1+\epsilon}} \Theta(\mu_F^2 - (\mathbf{k} - \tilde{\mathbf{p}})^2) \frac{1}{\tilde{\mathbf{p}}^2} \\ &= \int \frac{d^{2+2\epsilon} \mathbf{q}}{\pi^{1+\epsilon}} \Theta(\mu_F^2 - \mathbf{q}^2) \frac{\alpha_s C_A}{\pi (e^{\gamma_E} \mu^2)^\epsilon} \frac{1}{(\mathbf{q} - \mathbf{k})^2}, \end{aligned}$$

q

k

$p' = k - q$

Kinematic limits P_{gg} - CCFM

$$p' \equiv k - q = yp(1-z) + \mathbf{k} - \mathbf{q} + \frac{q^2 + \mathbf{q}^2}{2xp \cdot n}n$$

$$\frac{p'}{1-z} = yp + \frac{\mathbf{k} - \mathbf{q}}{1-z} + \frac{q^2 + \mathbf{q}^2}{2(1-z)xp \cdot n}n$$

$$\tilde{\mathbf{p}} = \frac{\mathbf{k} - \mathbf{q}}{1-z}$$

related to angle

q

$p'=k-q$

k

CCFM limit:

$$\lim_{\tilde{\mathbf{p}} \rightarrow 0} \hat{K}_{gg} \left(z, \frac{\mathbf{k}^2}{\mu^2}, 0, \alpha_s \right) = z \int_{\tilde{\mathbf{p}}_{min}^2}^{\tilde{\mathbf{p}}_{max}^2} \frac{d\tilde{\mathbf{p}}^2}{\tilde{\mathbf{p}}^2} \frac{\alpha_s C_a}{\pi} \left[\frac{1}{z} + \frac{1}{1-z} + \mathcal{O} \left(\frac{\tilde{\mathbf{p}}^2}{\mathbf{k}^2} \right) \right]$$

Towards evolution equation

- *For now we have real part emissions of the splitting functions.*
- *The non diagonal splitting functions do not have virtual contribution at the LO.*
- *They are divergent when $p' \rightarrow 0$. The diagonal once have virtual contributions.*
- *However, the distribution of gluons gets contribution from quarks....*
- *We can consider the following model*

Towards evolution equation

Real part of P_{qq} to be complemented by virtual corrections \rightarrow can expect cancellations of singularities but P_{gq} is divergent

For gluonic part we use low z limit part of P_{gg} i.e. LO BFKL equation

$$\mathcal{F}(x, \mathbf{q}^2) = \mathcal{F}^0(x, \mathbf{q}^2) + \bar{\alpha}_s \int_x^1 \frac{dz}{z} \int \frac{d^2\mathbf{p}}{\pi\mathbf{p}^2} \left[\mathcal{F}\left(\frac{x}{z}, |\mathbf{q} + \mathbf{p}|^2\right) - \theta(\mathbf{q}^2 - \mathbf{p}^2) \mathcal{F}\left(\frac{x}{z}, \mathbf{q}^2\right) \right]$$

add quark induced contribution

$$+ \frac{\alpha_s}{2\pi} \int_x^1 \frac{dz}{z} \int \frac{d^2\mathbf{p}}{\pi\mathbf{p}^2} P_{gq}(z, \mathbf{p}, \mathbf{q}) \mathcal{Q}\left(\frac{x}{z}, |\mathbf{p} + \mathbf{q}|^2\right)$$

Towards evolution equation- BFKL with Regge form factor

Use simplified P_{gg} kernel i.e. BFKL limit. Introduce phase space slicing parameter to separate resolved and unresolved emissions

$$\mathcal{F}(x, \mathbf{q}^2) = \mathcal{F}^0(x, \mathbf{q}^2) + \bar{\alpha}_s \int_x^1 \frac{dz}{z} \left[\int_{\mu^2} \frac{d^2 \mathbf{p}}{\pi \mathbf{p}^2} \mathcal{F} \left(\frac{x}{z}, |\mathbf{q} + \mathbf{p}|^2 \right) - \ln \frac{\mathbf{q}^2}{\mu^2} \mathcal{F} \left(\frac{x}{z}, \mathbf{q}^2 \right) \right]$$

Using Mellin transforms and some algebra we get

$$\mathcal{F}(x, \mathbf{q}^2) = \underbrace{\tilde{\mathcal{F}}^0(x, \mathbf{q}^2)}_{\text{modified}} + \bar{\alpha}_s \int_x^1 \frac{dz}{z} \underbrace{\Delta_R(z, \mathbf{q}^2, \mu^2)}_{\exp(-\bar{\alpha}_s \ln 1/z \ln \mathbf{q}^2/\mu^2)} \int_{\mu^2} \frac{d^2 \mathbf{p}}{\pi \mathbf{p}^2} \mathcal{F} \left(\frac{x}{z}, |\mathbf{q} + \mathbf{p}|^2 \right)$$

Stable in $\mu \rightarrow 0$

Towards evolution equation

M. Hentschinski, A. Kusina, K.K; Phys. Rev. D 94, 114013 (2016)

For quark part the crucial difference: no virtual corrections $\int \frac{d\mathbf{p}^2}{\mathbf{p}^2} \rightarrow \int_{\mu^2} \frac{d\mathbf{p}^2}{\mathbf{p}^2}$

$$\text{'BFKL'} + \frac{\alpha_s}{2\pi} \int_x^1 \frac{dz}{z} \int_{\mu^2} \frac{d^2\mathbf{p}}{\pi\mathbf{p}^2} P_{gq}(z, \mathbf{p}, \mathbf{q}) \mathcal{Q}\left(\frac{x}{z}, |\mathbf{p} + \mathbf{q}|^2\right)$$

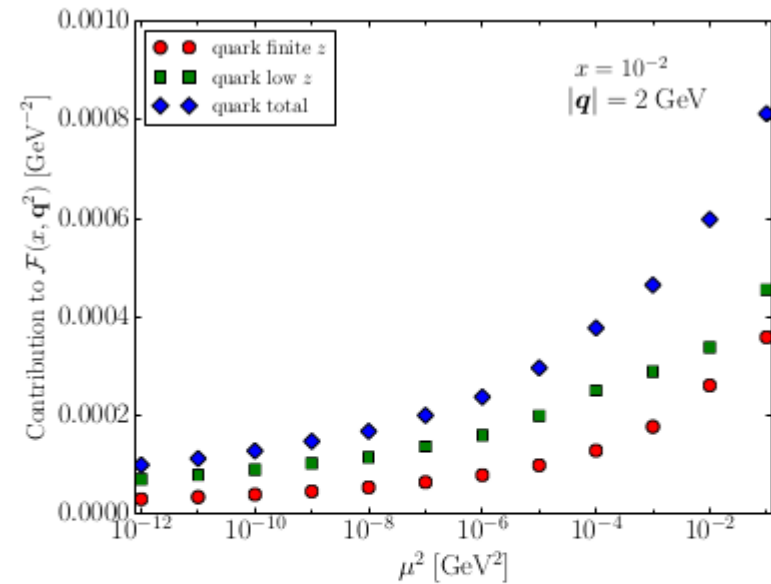
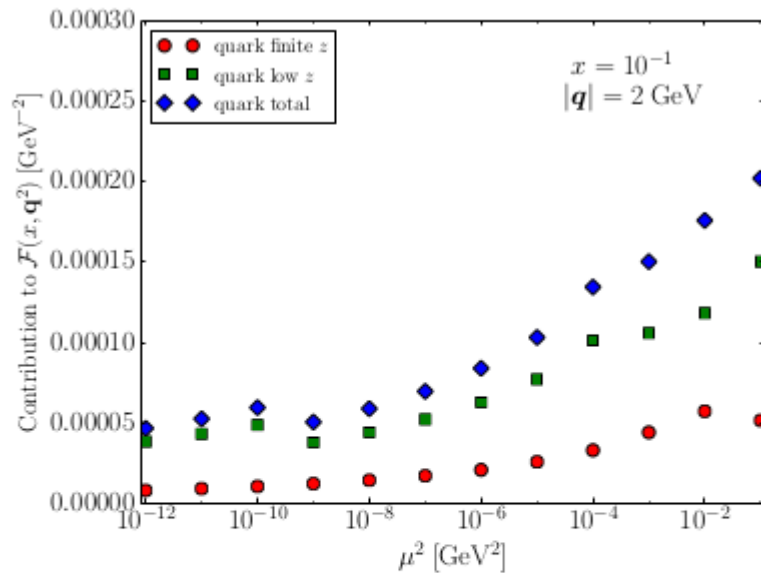
The equation for gluon reads:

$$\begin{aligned} \mathcal{F}(x, \mathbf{q}^2) = & \tilde{\mathcal{F}}^0(x, \mathbf{q}^2) + \frac{\alpha_s}{2\pi} \int_x^1 \frac{dz}{z} \int \frac{d^2\mathbf{p}}{\pi\mathbf{p}^2} \theta(\mathbf{p}^2 - \mu^2) \left[\Delta_R(z, \mathbf{q}^2, \mu^2) \right. \\ & \left. \left(2C_A \mathcal{F}\left(\frac{x}{z}, |\mathbf{q} + \mathbf{p}|^2\right) + C_F \mathcal{Q}\left(\frac{x}{z}, |\mathbf{q} + \mathbf{p}|^2\right) \right) \right. \\ & \left. - \int_z^1 \frac{dz_1}{z_1} \Delta_R(z_1, \mathbf{q}^2, \mu^2) \left[\tilde{P}'_{gq}\left(\frac{z}{z_1}, \mathbf{p}, \mathbf{q}\right) \frac{z}{z_1} \right] \mathcal{Q}\left(\frac{x}{z}, |\mathbf{q} + \mathbf{p}|^2\right) \right] \end{aligned}$$

where

$$P_{gq} = \tilde{P}_{gq}/z$$

Towards evolution equation - stability



Resummation of $\ln \mathbf{q}^2 / \mu^2$ in $\Delta_R = \left(\frac{\mu^2}{\mathbf{q}^2} \right)^{\bar{\alpha}_s \ln 1/z}$ cuts of $\mu \rightarrow$ region

Conclusions and outlook

- *We have applied CFP and CH technique to calculate real emissions splitting functions*
- *We used the splitting functions to construct model equation for gluon density receiving contributions from quarks*
- *We found that found that resummation of virtual contributions to P_{gg} at low x helps with treatment of singularity of P_{gq} splitting function*
- *Virtual contributions to P_{gg} and P_{qq} should be computed using the same formalism*
- *Evolution variable: will come after getting full kernels*
- *The full set of evolution equations*
- *Relation to operator definition of TMD, address nonlinearities*
- *Solution*
- *Monte Carlo implementation*

REF 2018



Workshop on Resummation, Evolution, Factorization 2018

19-23 November 2018
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REF 2018 is the 5th workshop in the series of workshops on Resummation, Evolution, Factorization. The workshop wishes to bring together experts of different communities specialized in: nuclear structure; transverse momentum dependent distributions; small-x physics; effective field theories.

On Friday the 23rd of November there will be a tutorial on the use of existing software for the calculation of hadron scattering processes. The emphasis will be on programs that employ TMDs, for example those provided by TMDlib. The fixed-order program KaTie, and the parton shower program CASCADE will be addressed, as well as their merging.

Previous meetings

- 13-16 November 2017 Madrid (Spain)
- 7-10 November 2016 Antwerp (Belgium)
- 2-5 November 2015 DESY Hamburg (Germany)
- 8-11 December 2014 Antwerp (Belgium)

Scientific committee:

Elke Aschenauer	Daniel Boer
Igor Cherednikov	Markus Diehl
Didar Dobur	David Dudal
Miguel García Echevarría	
Laurent Favart	Francesco Hautmann
Hannes Jung	Fabio Maltoni
Piet Mulders	Gunar Schnell
Andrea Signori	Pierre Van Mechelen



Starts 19 Nov 2018, 13:00
Ends 23 Nov 2018, 15:00
Europe/Warsaw



Krzysztof Kutak (chairman)
Andreas van Hameren
Sebastian Piotr Sapeta
Piotr Kotko



Other Institutes

Institute of Nuclear Physics
Polish Academy of Sciences
Kraków, Poland



There are no materials yet.

