

# Unpolarised quark TMDs: extraction, problems and prospects

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in collaboration with  
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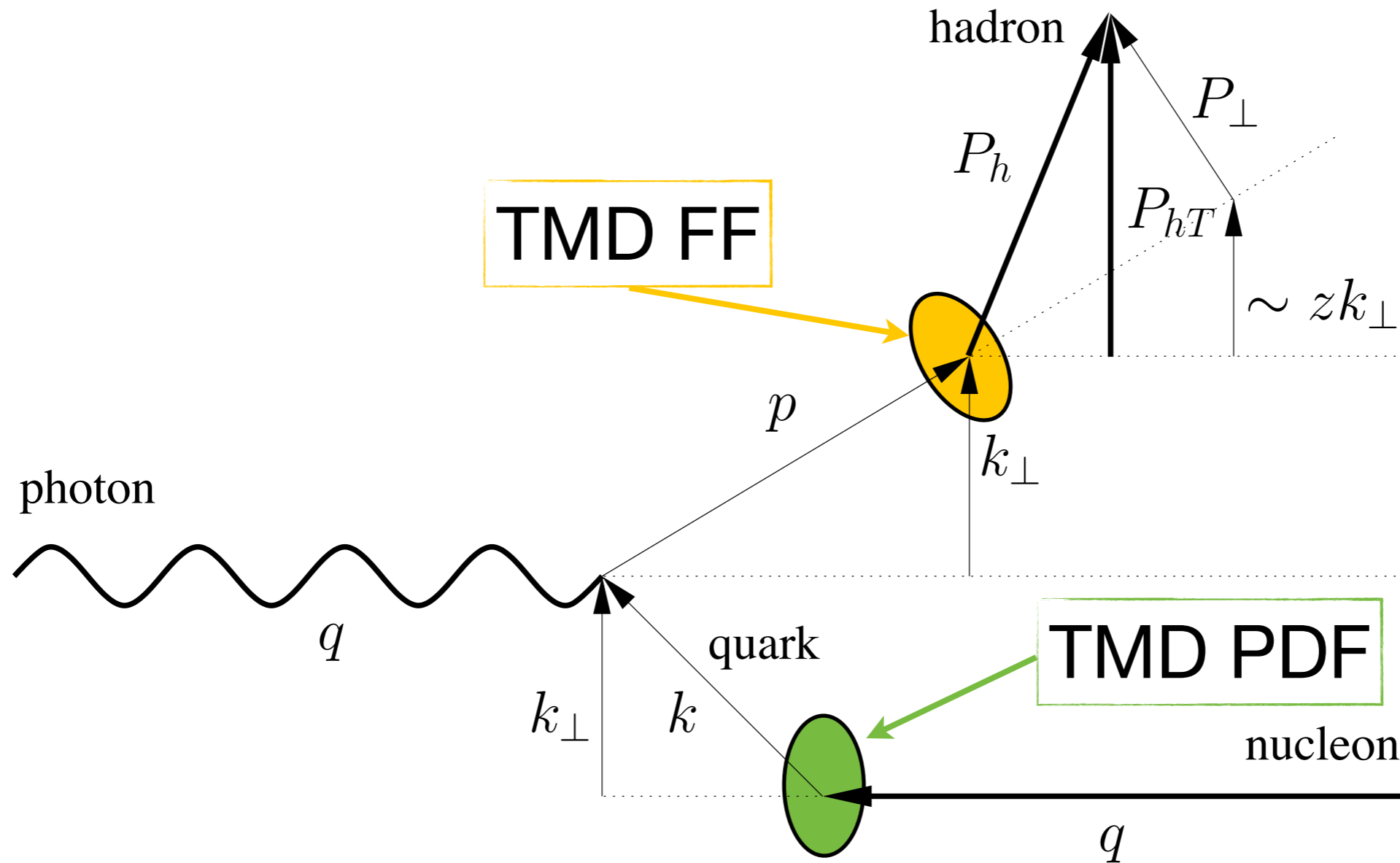
## Part 1

Unpolarised quark TMD:

past, present and future of an almost-global fit

# Semi-inclusive Deep Inelastic Scattering

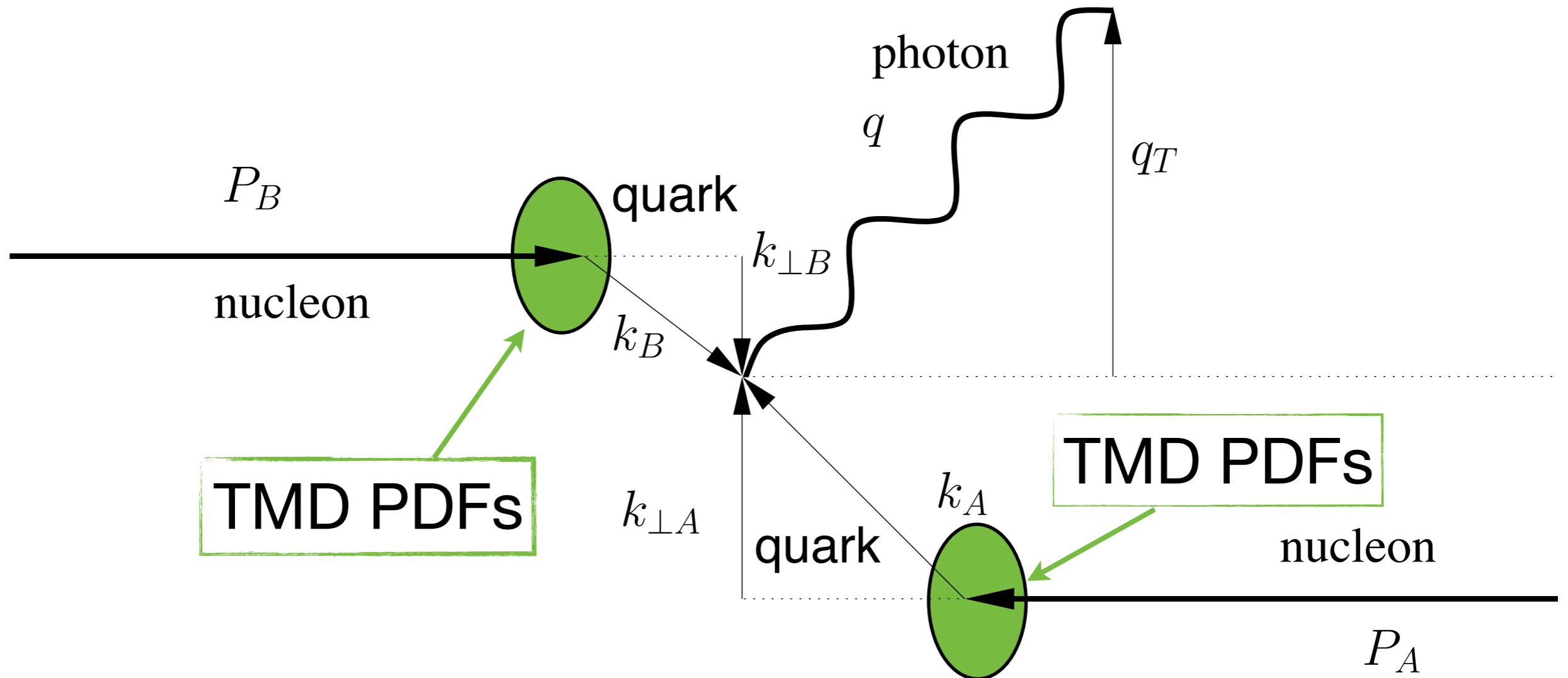
$$l(\ell) + N(\mathcal{P}) \rightarrow l(\ell') + h(\mathcal{P}_h) + X$$



# Drell-Yan processes and Z production

$$A + B \rightarrow \gamma^* \rightarrow l^+ l^-$$

$$A + B \rightarrow Z \rightarrow l^+ l^-$$



# A selection of results

	Framework	HERMES	COMPASS	DY	Z production	N of points
KN 2006 <a href="#">hep-ph/0506225</a>	LO-NLL	✗	✗	✓	✓	98
Pavia 2013 (+Amsterdam, Bilbao) <a href="#">arXiv:1309.3507</a>	No evolution	✓	✗	✗	✗	1538
Torino 2014 (+JLab) <a href="#">arXiv:1312.6261</a>	No evolution	✓ (separately)	✓ (separately)	✗	✗	576 (H) 6284 (C)
DEMS 2014 <a href="#">arXiv:1407.3311</a>	NLO-NNLL	✗	✗	✓	✓	223
EIKV 2014 <a href="#">arXiv:1401.5078</a>	LO-NLL	1 (x, Q <sup>2</sup> ) bin	1 (x, Q <sup>2</sup> ) bin	✓	✓	500 (?)
Pavia 2017 <a href="#">arXiv:1703.10157</a>	LO-NLL	✓	✓	✓	✓	8059
SV 2017 <a href="#">arXiv:1706.01473</a>	NNLO-NNLL	✗	✗	✓	✓	309

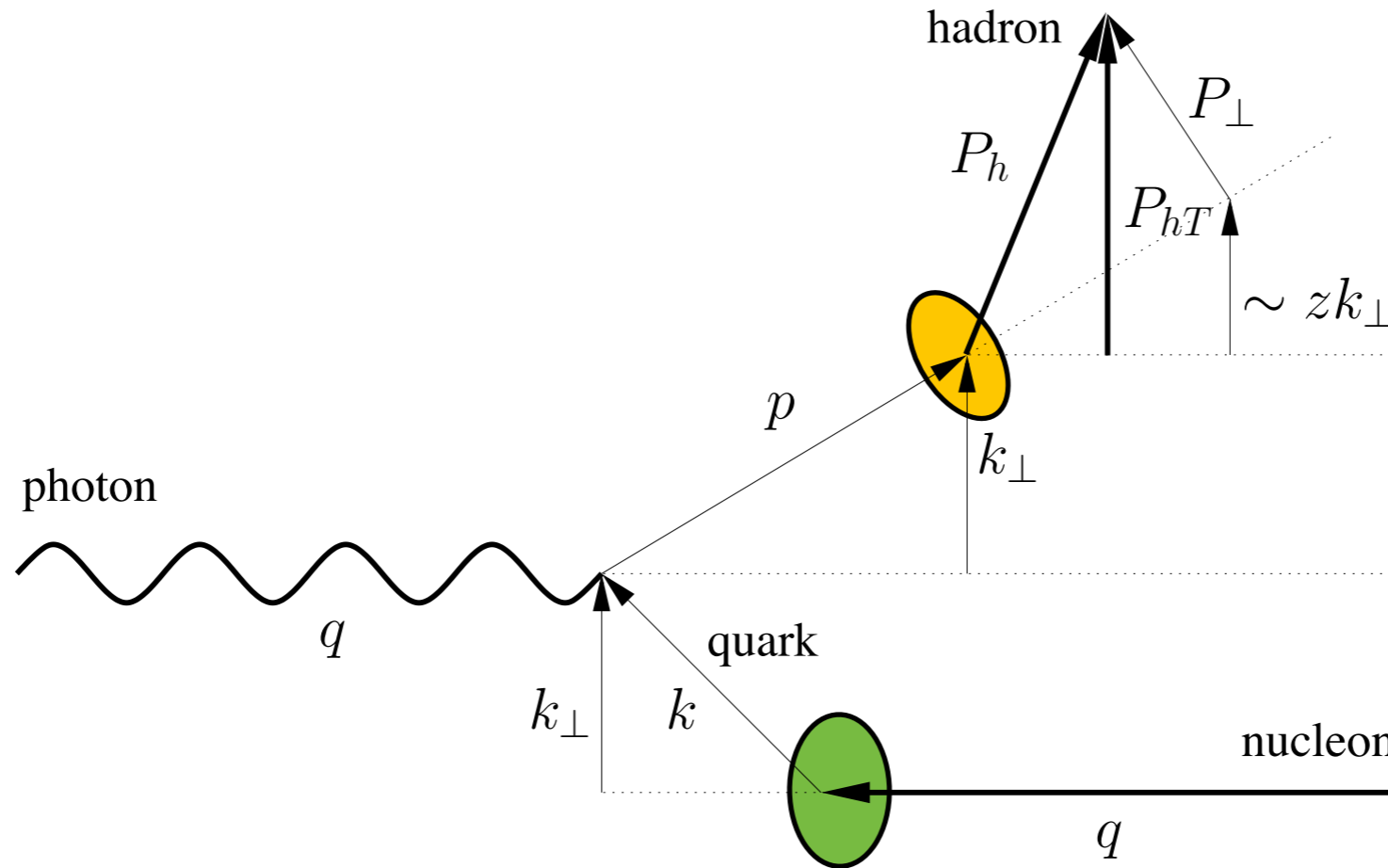
**Pavia (realistically) 2019: NLO-NLL + LHC data!**

# SIDIS: fitting the hadron multiplicities

$$m_N^h(x, z, |\mathbf{P}_{hT}|, Q^2) = \frac{d\sigma_N^h / (dx dz d|\mathbf{P}_{hT}| dQ^2)}{d\sigma_{\text{DIS}} / (dx dQ^2)} = \frac{2\pi |\mathbf{P}_{hT}| F_{UU,T}(x, z, \mathbf{P}_{hT}^2, Q^2) + 2\pi\epsilon |\mathbf{P}_{hT}| F_{UU,L}(x, z, \mathbf{P}_{hT}^2, Q^2)}{F_T(x, Q^2) + \epsilon F_L(x, Q^2)}$$

higher in  $\alpha_s$

$$M^2 \ll Q^2, P_{hT}^2 \ll Q^2$$



At present accuracy  
(LO-NLL)

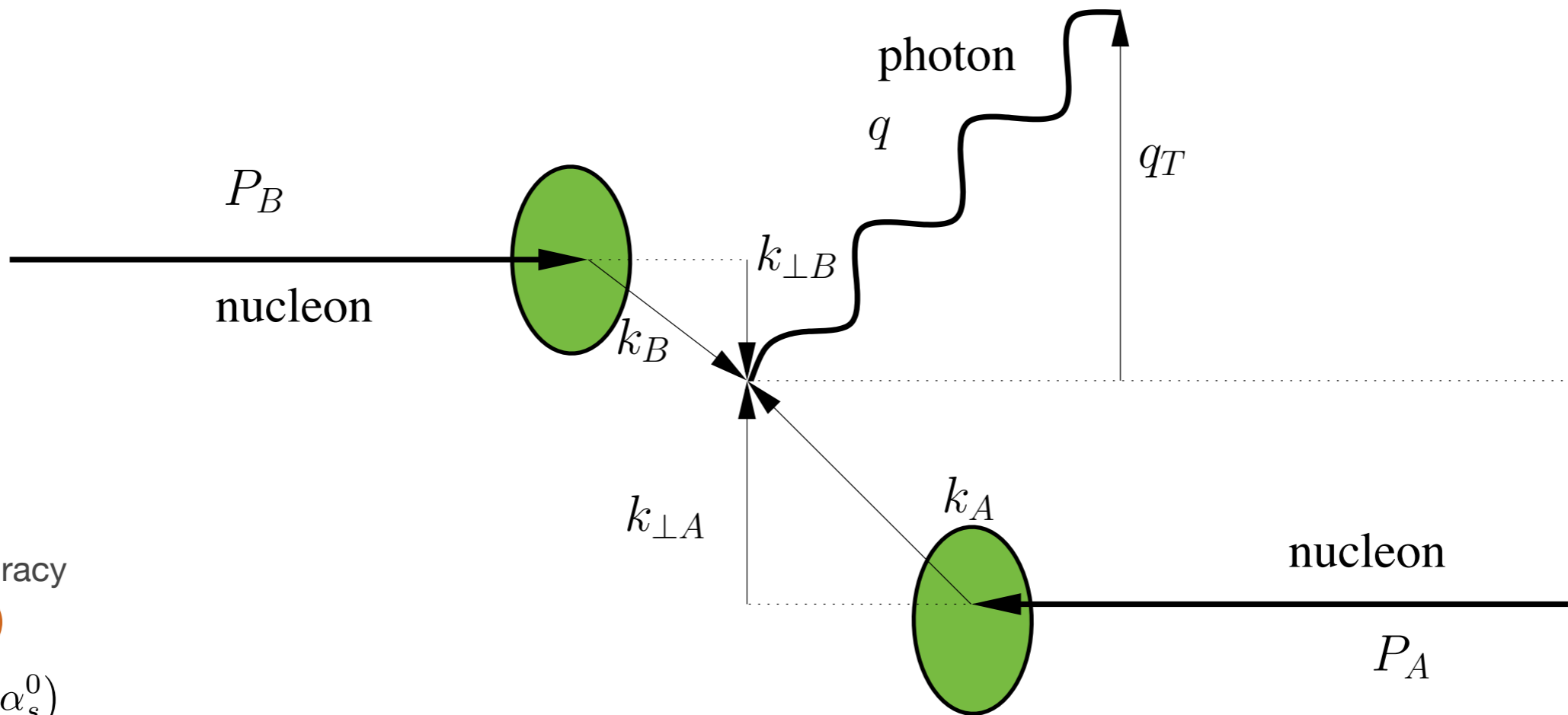
$$\mathcal{H}_{UU,T} \simeq \mathcal{O}(\alpha_s^0)$$

$$Y_{UU,T}(Q^2, P_{hT}^2) \simeq 0$$

$$F_{UU,T}(x, z, P_{hT}^2, Q^2) = \sum_a \mathcal{H}_{UU,T}^a(Q^2; \mu^2) \int d^2 k_T d^2 P_T f_1^a(x, k_T^2; \mu^2) D_1^{h/a}(z, P_T^2; \mu^2) \cdot \delta^2(zk_T - P_{hT} + P_T) + Y_{UU,T}(Q^2, P_{hT}^2) + \mathcal{O}(M^2/Q^2)$$

# DY: fitting the $q_T$ distributions

$$\frac{d\sigma}{dQ^2 dq_T^2 d\eta} = \sigma_0^{\gamma,Z} \left( F_{UU}^1 + \frac{1}{2} F_{UU}^2 \right) \rightarrow q_T^2 \ll Q^2$$



At present accuracy  
(LO-NLL)

$$\mathcal{H}_{UU,T} \simeq \mathcal{O}(\alpha_s^0)$$

$$Y_{UU,T}(Q^2, P_h^2 T) \simeq 0$$

$$F_{UU}^1(x_A, x_B, q_T^2, Q^2) = \sum_a \mathcal{H}_{UU}^{1a}(Q^2) \times \int d^2\mathbf{k}_{\perp A} d^2\mathbf{k}_{\perp B} f_1^a(x_A, \mathbf{k}_{\perp A}^2; Q^2) f_1^{\bar{a}}(x_B, \mathbf{k}_{\perp B}^2; Q^2) \delta^{(2)}(\mathbf{k}_{\perp A} - \mathbf{q}_T + \mathbf{k}_{\perp B}) + Y_{UU}^1(Q^2, q_T^2) + \mathcal{O}(M^2/Q^2).$$

# Evolution of TMDs

analogous formula for FF

## Fourier transform: $\xi_T(b_T)$ space

$$f_1^a(x, k_\perp; \mu^2) = \frac{1}{2\pi} \int d^2\xi_T e^{-i\xi_T \cdot k_\perp} \tilde{f}_1^a(x, \xi_T; \mu^2)$$

$$\tilde{f}_1^a(x, \xi_T; \mu^2) =$$

$$= \sum_i \left( \tilde{C}_{a/i} \otimes f_1^i \right) (x, \bar{\xi}_*; \mu_b) e^{\tilde{S}(\bar{\xi}_*; \mu_b, \mu)} e^{g_K(\xi_T) \ln(\mu/\mu_0)} \hat{f}_{NP}^a(x, \xi_T)$$

collinear PDF  
(extracted from data)

NP part of evolution  
(extracted from data)

NP part of TMD  
(extracted from data)

perturbative QCD



# Model: non perturbative elements

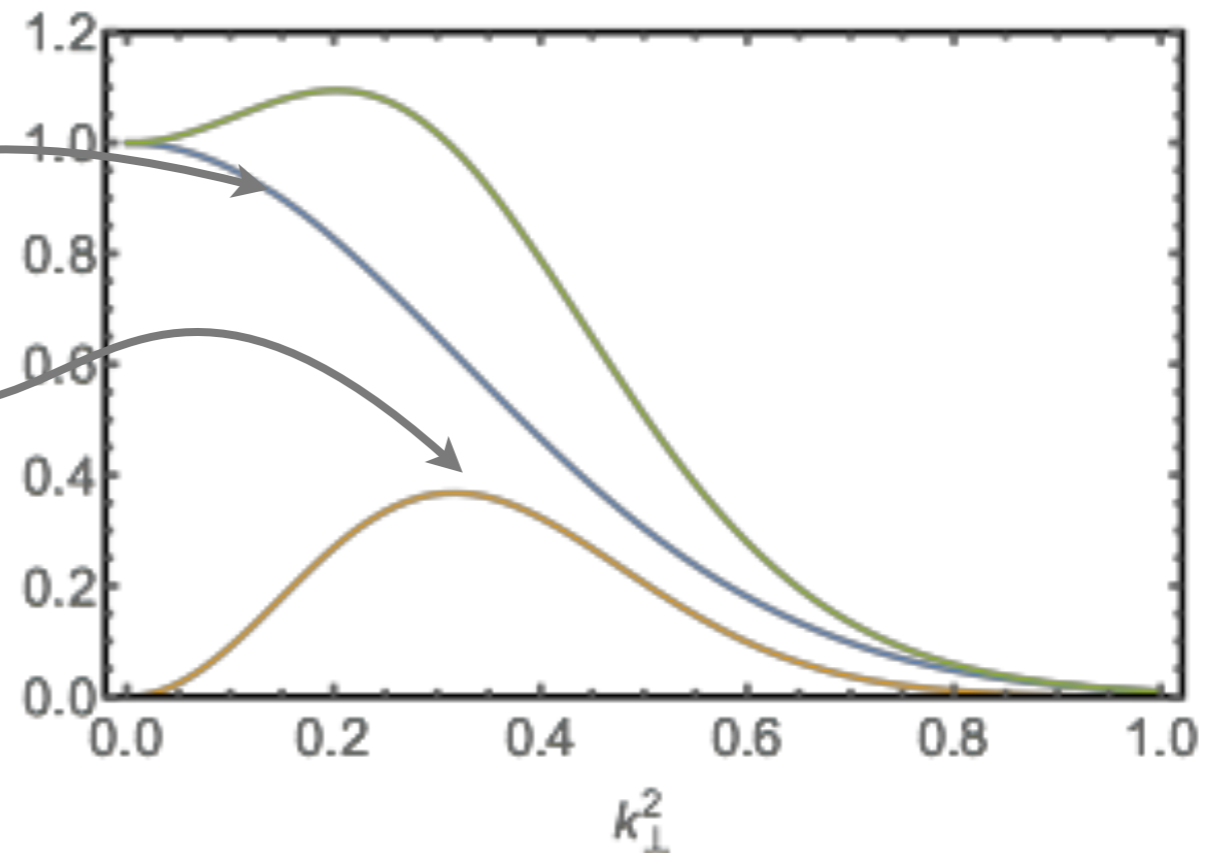
$$f_{1NP}^a(x, k_{\perp}^2) = \frac{1}{\pi} \frac{(1 + \lambda k_{\perp}^2)}{g_{1a} + \lambda g_{1a}^2} e^{-\frac{k_{\perp}^2}{g_{1a}}}$$

$$N_1 \equiv g_1(\hat{x}) \quad \hat{x} = 0.1$$

$$g_1(x) = N_1 \frac{(1-x)^{\alpha} x^{\sigma}}{(1-\hat{x})^{\alpha} \hat{x}^{\sigma}}$$

**weighted sum of two Gaussian distributions:**

**same widths** for TMD PDFs  
**different widths** for TMD FFs



$$D_{1NP}^{a \rightarrow h}(z, P_{\perp}^2) = \frac{1}{\pi} \frac{1}{g_{3a \rightarrow h} + (\lambda_F / z^2) g_{4a \rightarrow h}^2} \left( e^{-\frac{P_{\perp}^2}{g_{3a \rightarrow h}}} + \lambda_F \frac{P_{\perp}^2}{z^2} e^{-\frac{P_{\perp}^2}{g_{4a \rightarrow h}}} \right)$$

$$\hat{z} = 0.5$$

$$g_{3,4}(z) = N_{3,4} \frac{(z^{\beta} + \delta)(1-z)^{\gamma}}{(\hat{z}^{\beta} + \delta)(1-\hat{z})^{\gamma}}$$

Inspired by **model calculations:**

Matevosyan et al.

Phys. Rev. D85, 014021 (2012), 1111.1740

Bacchetta et al.

Phys. Lett. B659, 234 (2008), 0707.3372

Bacchetta et al.

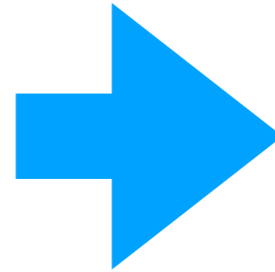
Phys. Rev. D65, 094021 (2002),

hep-ph/0201091

# Model: non-perturbative evolution

$$g_K(b_T; g_2) = -g_2 \frac{b_T^2}{2}$$

Large  $b_T$  correction to evolution  
(other functional forms to be explored)



There are **11 free parameters**  
in a flavor independent  
scenario

## Model: $b_T$ -integration

$$\hat{b}(b_T; b_{\min}, b_{\max}) = b_{\max} \left( \frac{1 - e^{-b_T^4/b_{\max}^4}}{1 - e^{-b_T^4/b_{\min}^4}} \right)$$

$\nearrow b_{\max}, \quad b_T \rightarrow +\infty$

avoid Landau pole

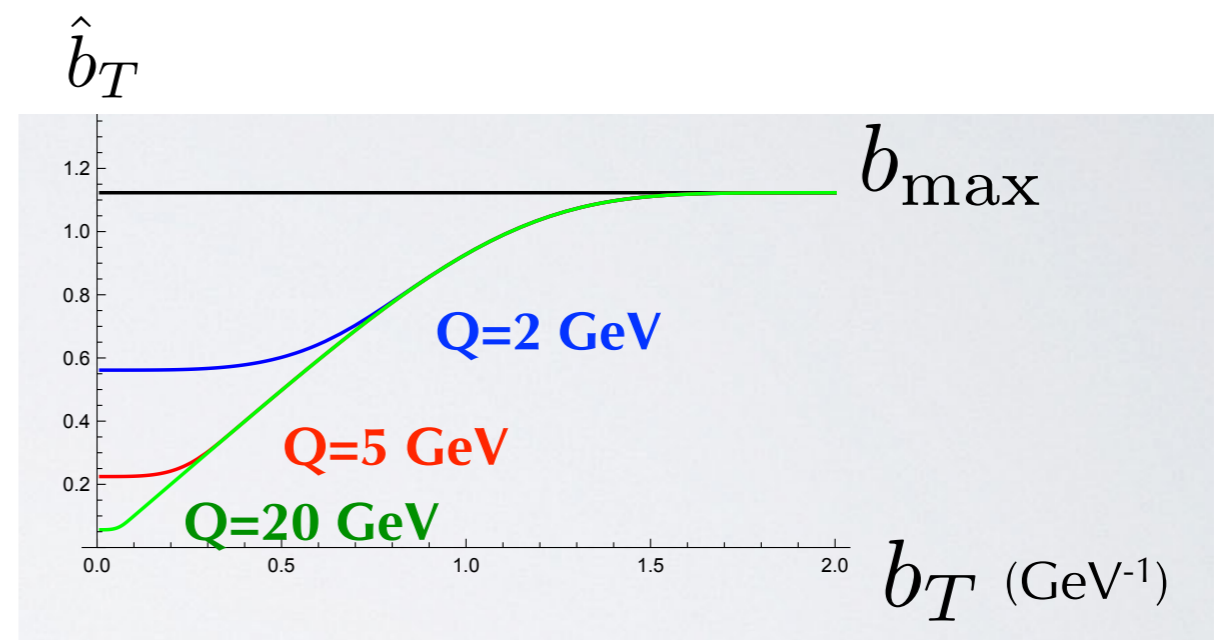
$\searrow b_{\min}, \quad b_T \rightarrow 0$

recover collinear fact.

$$b_{\min} = 2e^{-\gamma E}, \quad b_{\max} = 2e^{-\gamma E}/Q$$

Regularization needed to **recover the cross section integrated over  $q_T$**  in collinear factorization.

**Crucial** from the **theory** point of view and for the **phenomenology of SIDIS (low Q)**



# Experimental data



SIDIS  $\mu\text{N}$   
**6252**  
data points



SIDIS eN  
**1514**  
data points

March 2018: 2124 new data points —> fit in progress!

# Total: **8059** data points



Drell-Yan  
**203**  
data points

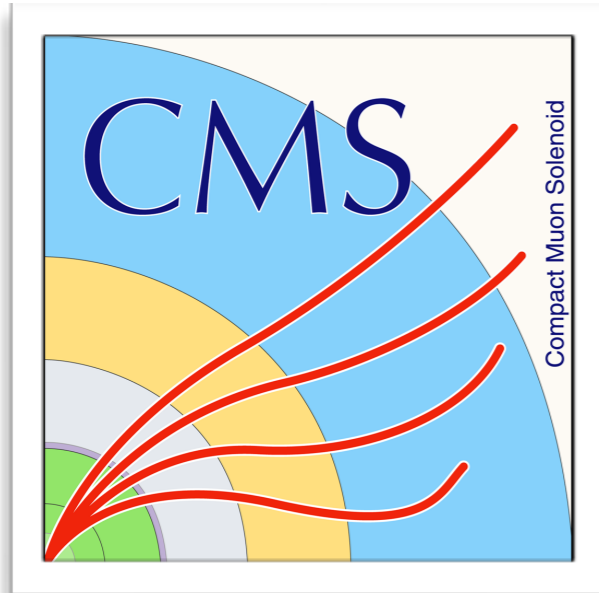


Z Production



**90**  
data points

# Work in progress!



7 TeV  
8 TeV

$$q\bar{q} \rightarrow Z_0/\gamma^* + X$$

7 TeV  
8 TeV

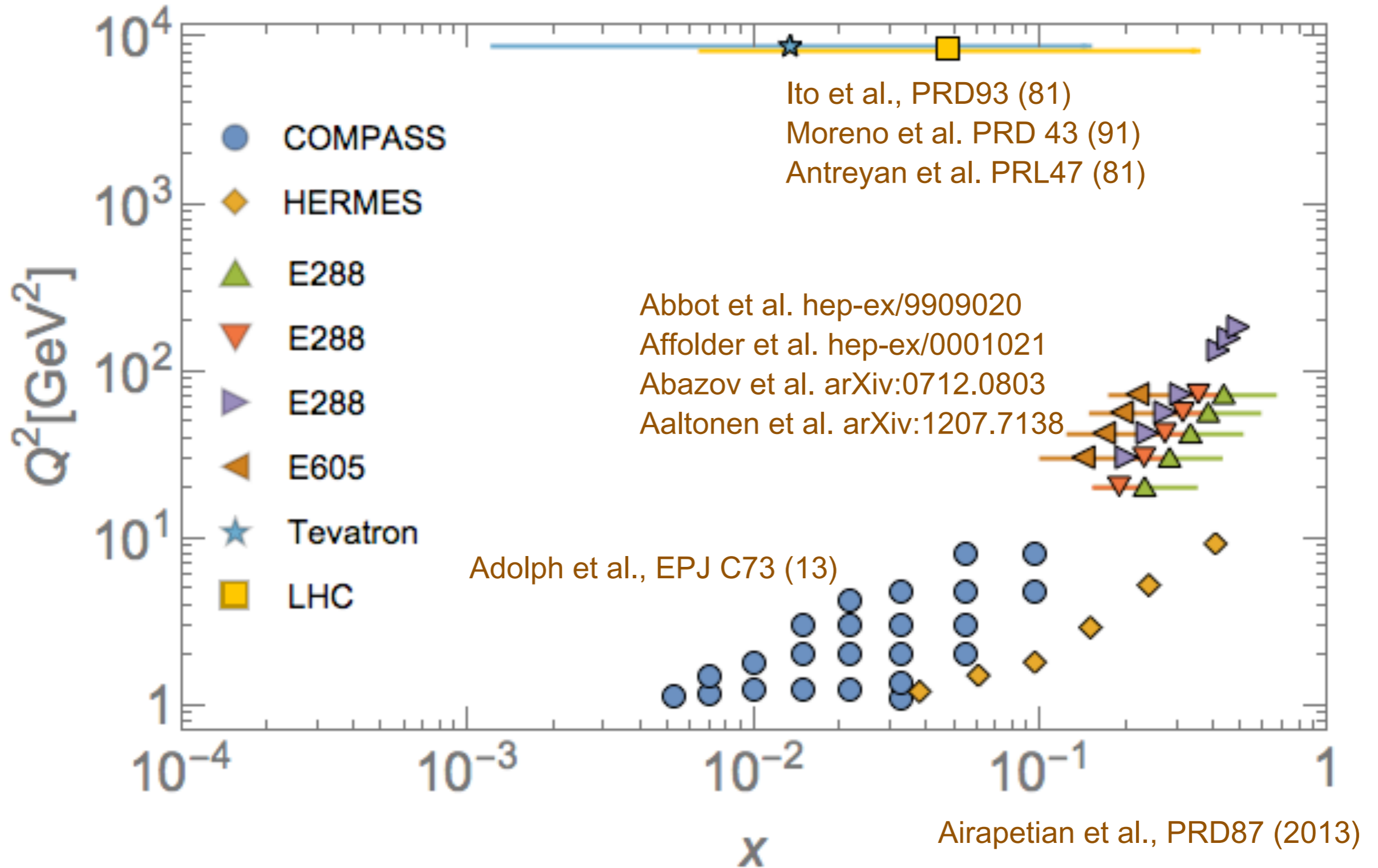
$$pp \rightarrow Z_0/\gamma^* \rightarrow (\mu^+ + \mu^- / e^+ + e^-)$$



7 TeV  
8 TeV  
13 TeV

$$pp \rightarrow Z_0 \rightarrow \mu^+ + \mu^-$$

# Distribution of data



# Data selection: SIDIS

	HERMES $p \rightarrow \pi^+$	HERMES $p \rightarrow \pi^-$	HERMES $p \rightarrow K^+$	HERMES $p \rightarrow K^-$
Reference	[61]			
Cuts	$Q^2 > 1.4 \text{ GeV}^2$ $0.2 < z < 0.7$ $P_{hT} < \text{Min}[0.2 Q, 0.7 Qz] + 0.5 \text{ GeV}$			
Points	190	190	189	187
Max. $Q^2$	9.2 $\text{GeV}^2$			
$x$ range	$0.06 < x < 0.4$			

TMD factorization  
( $P_{hT}^2/z^2 \ll Q^2$ )

avoid target fragmentation  
(low  $z$ )  
and exclusive contributions  
(high  $z$ )

Problem with normalization  
in the previous release

	HERMES $D \rightarrow \pi^+$	HERMES $D \rightarrow \pi^-$	HERMES $D \rightarrow K^+$	HERMES $D \rightarrow K^-$	COMPASS $D \rightarrow h^+$	COMPASS $D \rightarrow h^-$
Reference						
Cuts	$Q^2 > 1.4 \text{ GeV}^2$ $0.2 < z < 0.7$ $P_{hT} < \text{Min}[0.2 Q, 0.6 Qz] + 0.5 \text{ GeV}$					
Points	188	188	186	187	3024	3021
Max. $Q^2$	9.2 $\text{GeV}^2$				10 $\text{GeV}^2$	
$x$ range	$0.06 < x < 0.4$				$0.006 < x < 0.12$	
					Observable: $\frac{m_N^h(x, z, \mathbf{P}_{hT}^2, Q^2)}{m_N^h(x, z, \text{Min}[\mathbf{P}_{hT}^2], Q^2)}$	

# Data selection: Drell-Yan & Z

	E288 200	E288 300	E288 400	E605
Cuts	$q_T < 0.2 Q + 0.5 \text{ GeV}$			
Points	45	45	78	35
$\sqrt{s}$	19.4 GeV	23.8 GeV	27.4 GeV	38.8 GeV
$Q$ range	4-9 GeV	4-9 GeV	5-9, 11-14 GeV	7-9, 10.5-18 GeV
Kin. var.	$y=0.4$	$y=0.21$	$y=0.03$	$-0.1 < x_F < 0.2$

Drell-Yan  
data

Z production  
data

	CDF Run I	D0 Run I	CDF Run II	D0 Run II
Cuts	$q_T < 0.2 Q + 0.5 \text{ GeV} = 18.7 \text{ GeV}$			
Points	31	14	37	8
$\sqrt{s}$	1.8 TeV	1.8 TeV	1.96 TeV	1.96 TeV

# An almost-global fit

	Framework	HERMES	COMPASS	DY	Z production	N of points
Pavia 2017 arXiv:1703.10157	LO-NLL	✓	✓	✓	✓	8059

## PROs

almost a **global fit** of quark unpolarized TMDs

includes **TMD evolution**

**replica (bootstrap)** fitting methodology

**kinematic dependence** for intrinsic  $k_T$

**beyond Gaussian** assumption for intrinsic  $k_T$

## CONs

no “pure” info on TMD FFs (would need  $e^+ e^-$  data)

accuracy of TMD evolution: not the state of the art\*

only “low”  $q_T$  (no fixed order and Y-term)\*

no flavor dependence\*\*

\* **working on it!**

\*\* **thinking about working on it!**



# Agreement data-theory

Flavor independent configuration  
11 parameters

Points	Parameters	$\chi^2$	$\chi^2/\text{d.o.f.}$
8059	11	$12629 \pm 363$	$1.55 \pm 0.05$

	HERMES $p \rightarrow \pi^+$	HERMES $p \rightarrow \pi^-$	HERMES $p \rightarrow K^+$	HERMES $p \rightarrow K^-$
Points	190	190	189	187
$\chi^2/\text{points}$	4.83	2.47	0.91	0.82

	HERMES $D \rightarrow \pi^+$	HERMES $D \rightarrow \pi^-$	HERMES $D \rightarrow K^+$	HERMES $D \rightarrow K^-$	COMPASS $D \rightarrow h^+$	COMPASS $D \rightarrow h^-$
Points	190	190	189	189	3125	3127
$\chi^2/\text{points}$	3.46	2.00	1.31	2.54	1.11	1.61

	E288 [200]	E288 [300]	E288 [400]	E605
Points	45	45	78	35
$\chi^2/\text{points}$	0.99	0.84	0.32	1.12

	CDF Run I	D0 Run I	CDF Run II	D0 Run II
Points	31	14	37	8
$\chi^2/\text{points}$	1.36	1.11	2.00	1.73

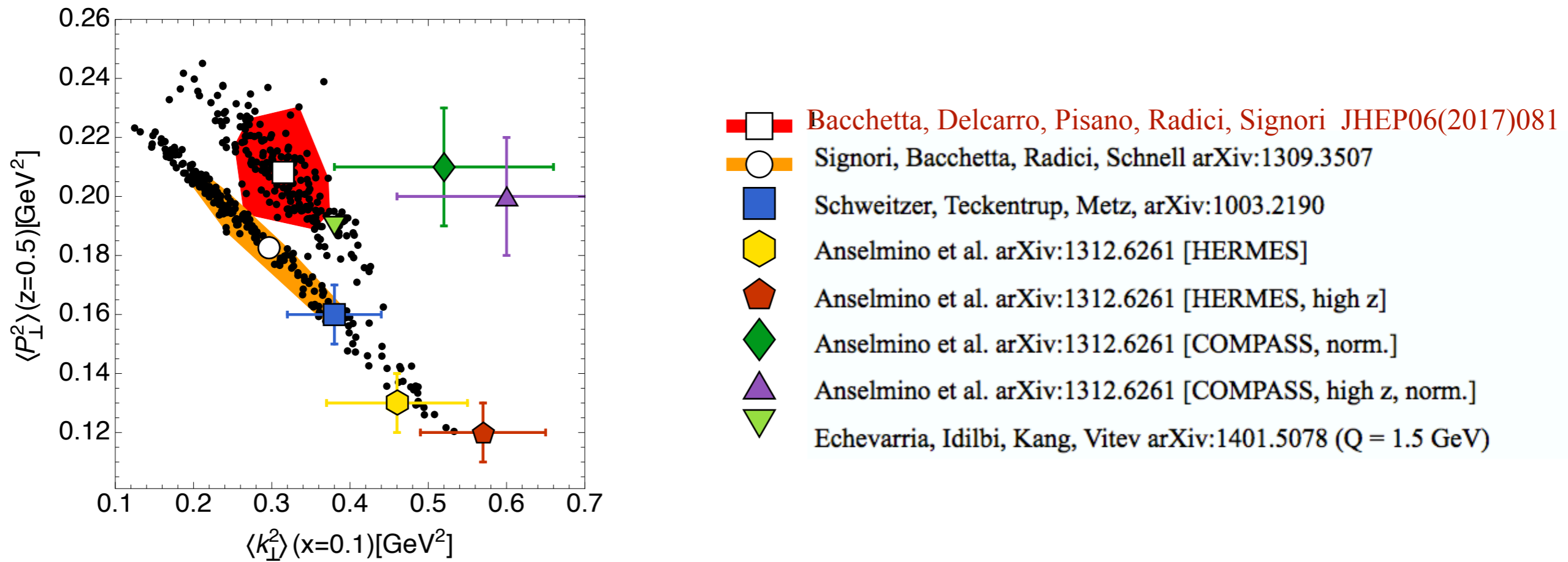
**Hermes** P/D into  $\pi^+$ :  
problems at low z

**Hermes** kaons better than pions:  
larger uncertainties from FFs

**Compass** : better agreement due to  
#points and normalization

**Stay tuned for LHC data and NLO-NLL** 17

# Average transverse momenta



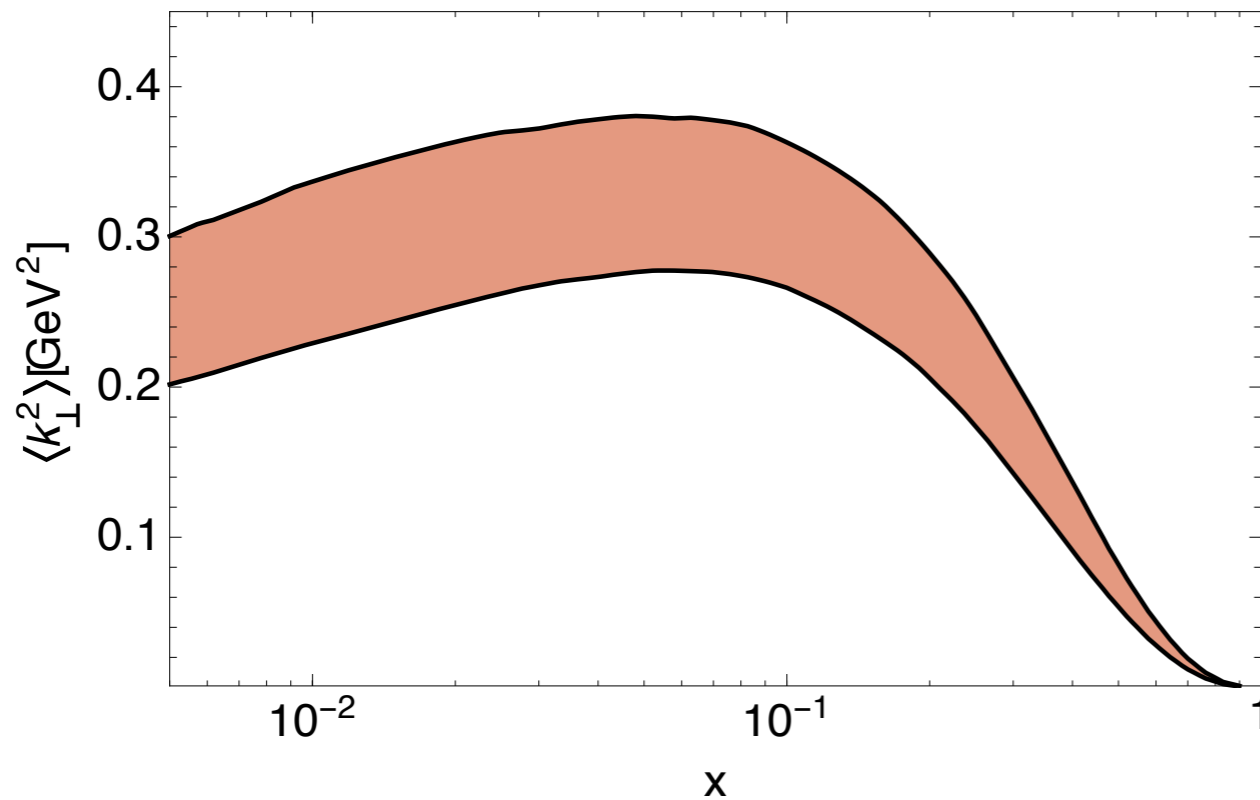
Red/orange regions: **68% CL** from replica method

Inclusion of **DY/Z** diminishes the correlation

Inclusion of **Compass** increases the  $\langle P_{\perp}^2 \rangle$  and reduces its spread

**e+e-** would further reduce the correlation

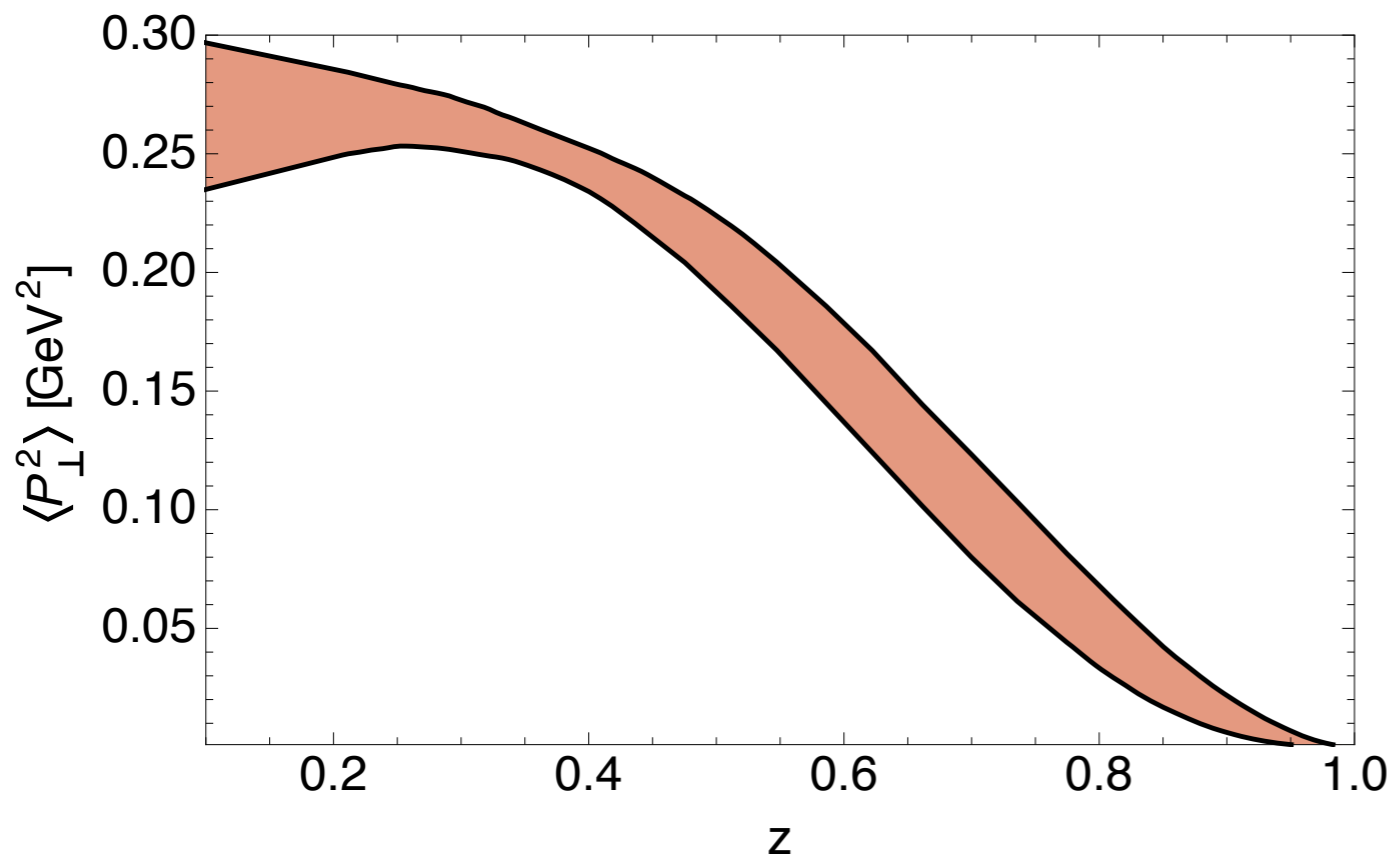
# Average transverse momentum



x-dependence width  
( $Q^2=1 \text{ GeV}^2$ )

**TMD PDF**

$$\langle k_{\perp}^2 \rangle(x) = \frac{\int d^2 k_{\perp} k_{\perp}^2 f_1^a(x, k_{\perp}^2, Q = 1 \text{ GeV})}{\int d^2 k_{\perp} f_1^a(x, k_{\perp}^2, Q = 1 \text{ GeV})}$$



**TMD FF**

$$\langle P_{\perp}^2 \rangle(z) = \frac{\int d^2 P_{\perp} P_{\perp}^2 D_1^{a \rightarrow h}(z, P_{\perp}^2, Q = 1 \text{ GeV})}{\int d^2 P_{\perp} D_1^{a \rightarrow h}(z, P_{\perp}^2, Q = 1 \text{ GeV})}$$

# Stability of the results

Best  $\chi^2/\text{dof} = \mathbf{1.55}$

**If we**

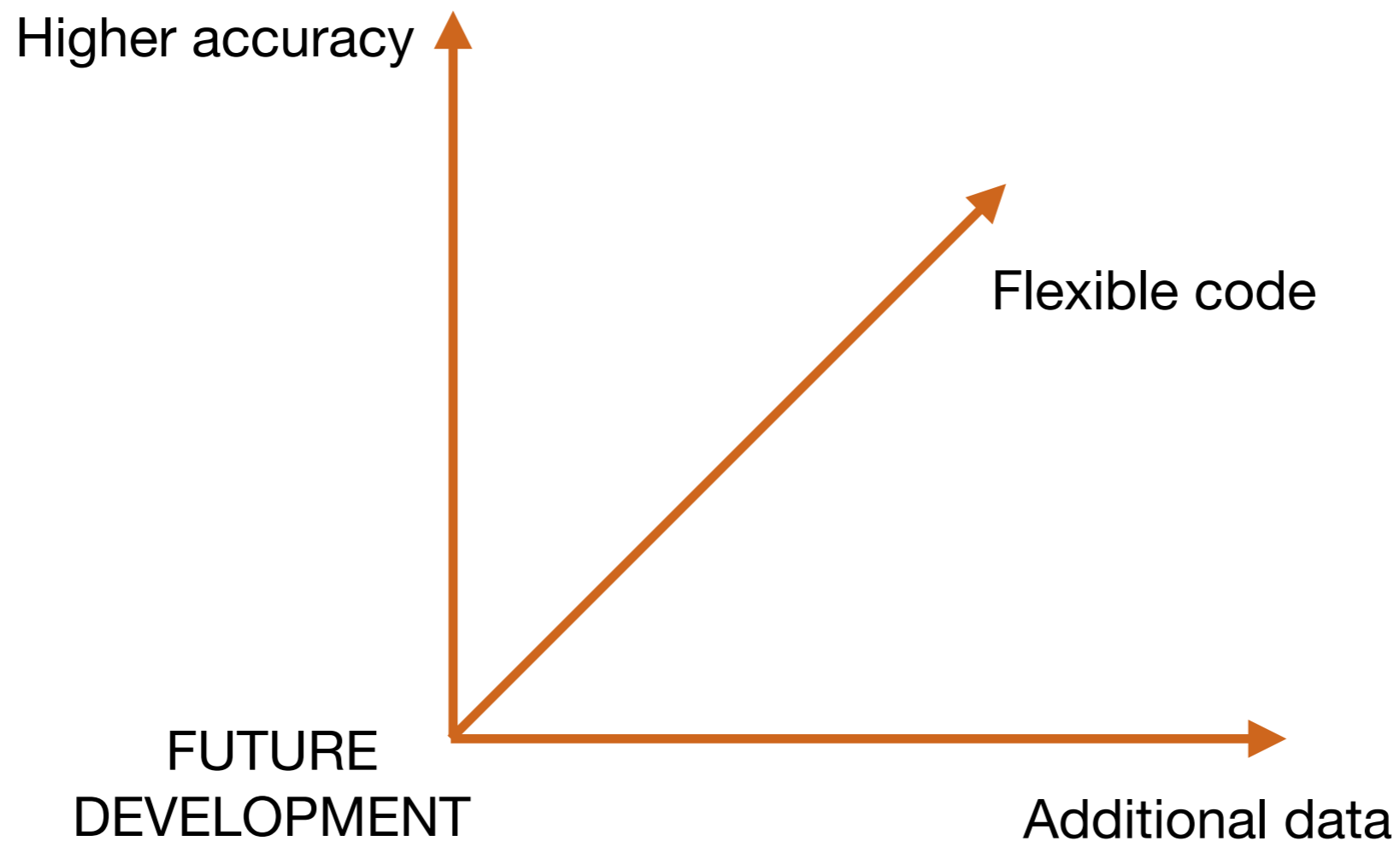
- **normalize** HERMES data as we did for COMPASS:  $\chi^2/\text{dof} = \mathbf{1.27}$
- **change collinear PDFs**: w.r.t to NLO GJR 2008 default choice:  
NLO MSTW 2008 ( $\chi^2/\text{dof} = \mathbf{1.84}$ ), NLO CJ12 ( $\chi^2/\text{dof} = \mathbf{1.85}$ )
- **choose more stringent cuts** (deeper into TMD factorization region):  
 $Q^2 > 1.5 \text{ GeV}^2$ ;  $0.25 < z < 0.6$ ;  $P_{hT} < 0.2Qz \Rightarrow \chi^2/\text{dof} = \mathbf{1.02}$  (477 bins)

# Conclusions and open issues

First global extraction of TMDs from SIDIS, DY and Z boson

Test of the universality and evolution formalism of partonic TMDs

Definition of a parametrization of TMDs from 8000 data points



## Part 2

Stumbling into unexpected problems:

Drell-Yan at low  $Q^2$  and high  $q_T$

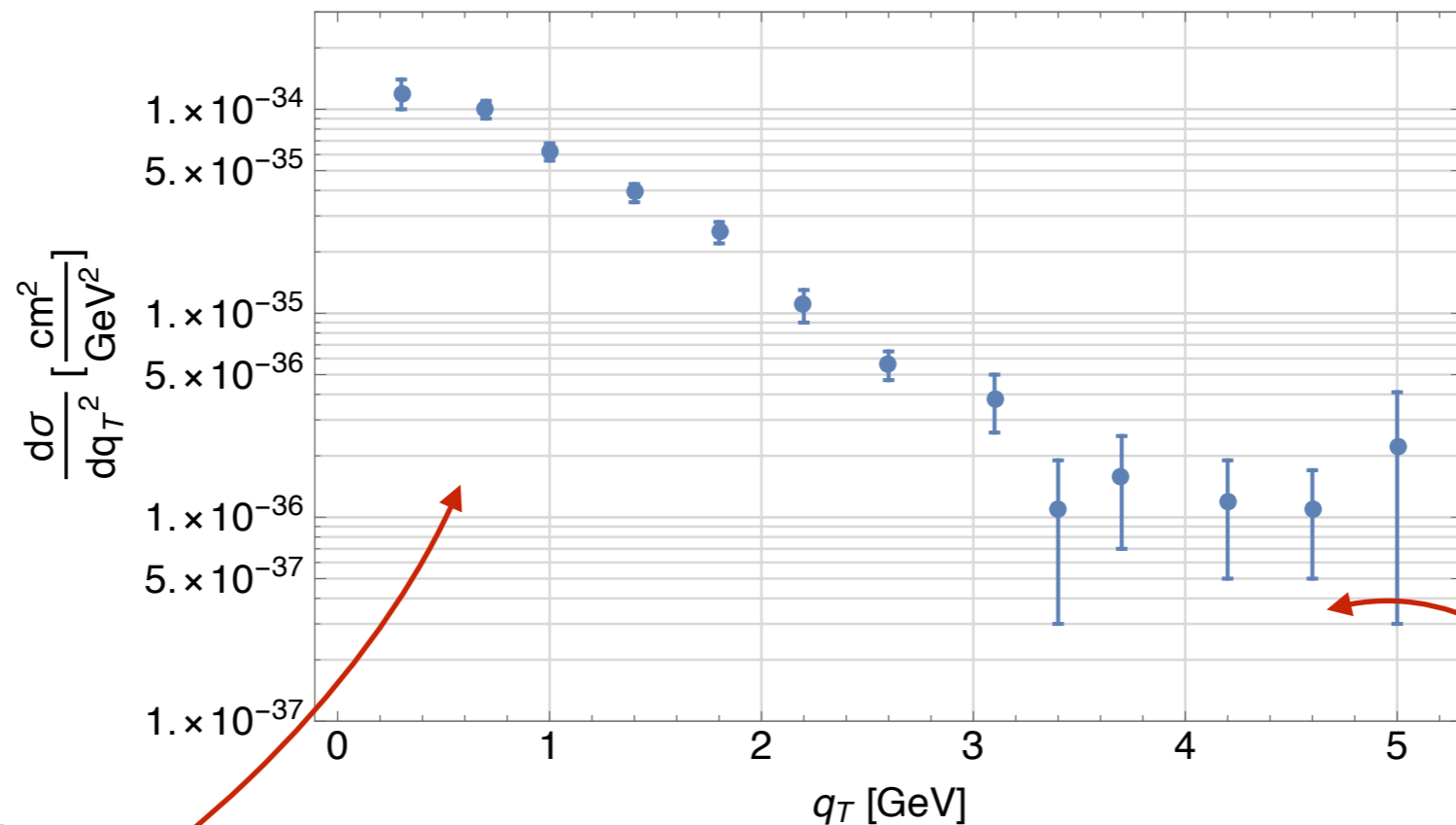
# Low-energy Drell-Yan data

Experiment	Reaction	Year	TMD fits	PDF fits
R209	p-p	1981	✓	✗
E288	p-Cu(Pt)	1981	✓	✗
E605	p-Cu	1991	✓	✓
E866	p-p(d)	2003	✗	✓
E615	pi-W	1989	✗	✓

$$20 \text{ GeV} \lesssim \sqrt{s} \lesssim 60 \text{ GeV}$$

# Transverse momentum of Drell-Yan pairs

R209 @CERN (1981)  
 $\sqrt{s} = 62 \text{ GeV}, 5 \text{ GeV} < Q < 8 \text{ GeV}$



Transverse momentum  
 resummation  
 $(q_T\text{-logs}) \alpha_s^n \ln^m \frac{q_T^2}{Q^2}$   
 + non-perturbative

Fixed order  
 collinear factorization

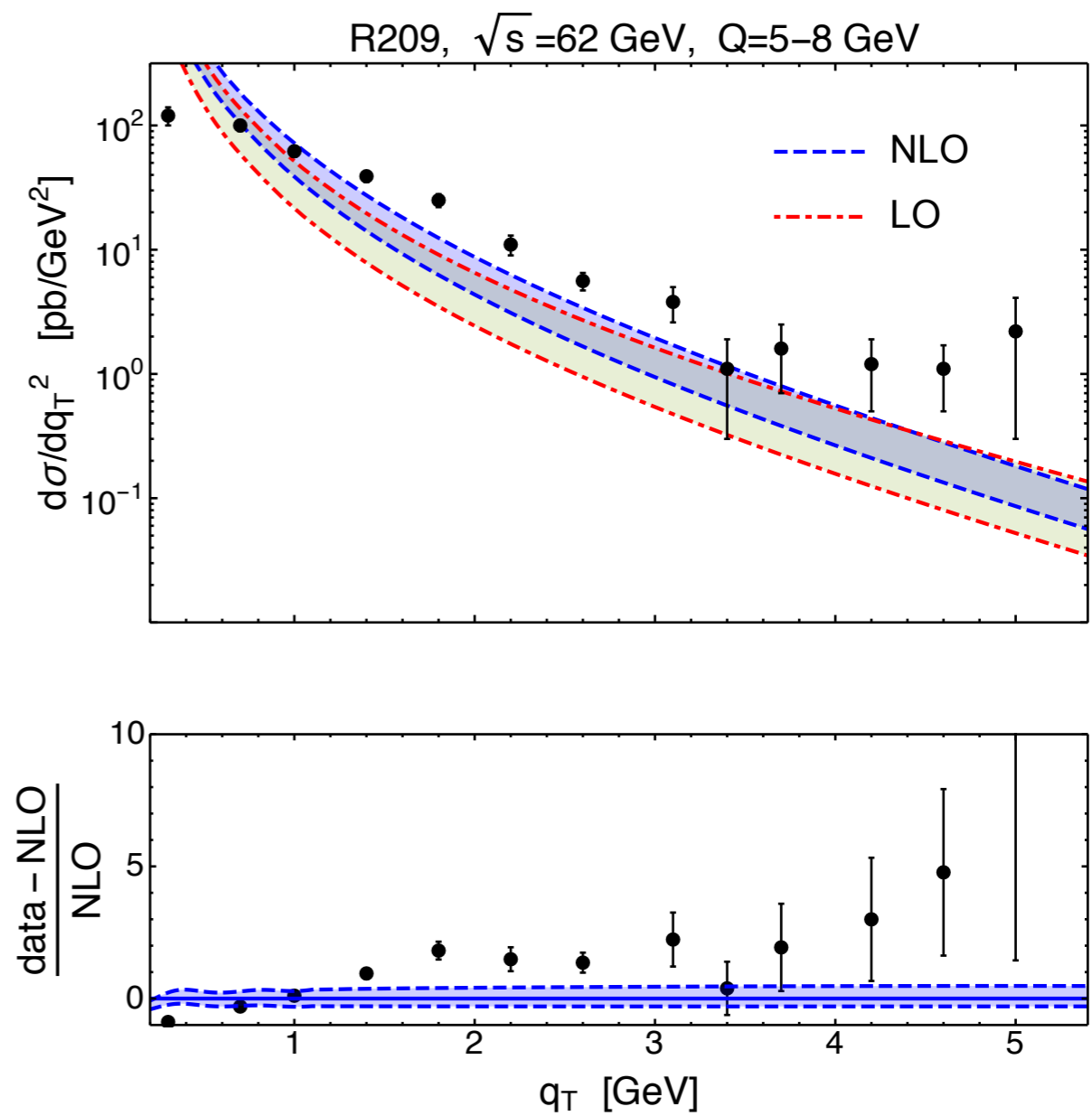
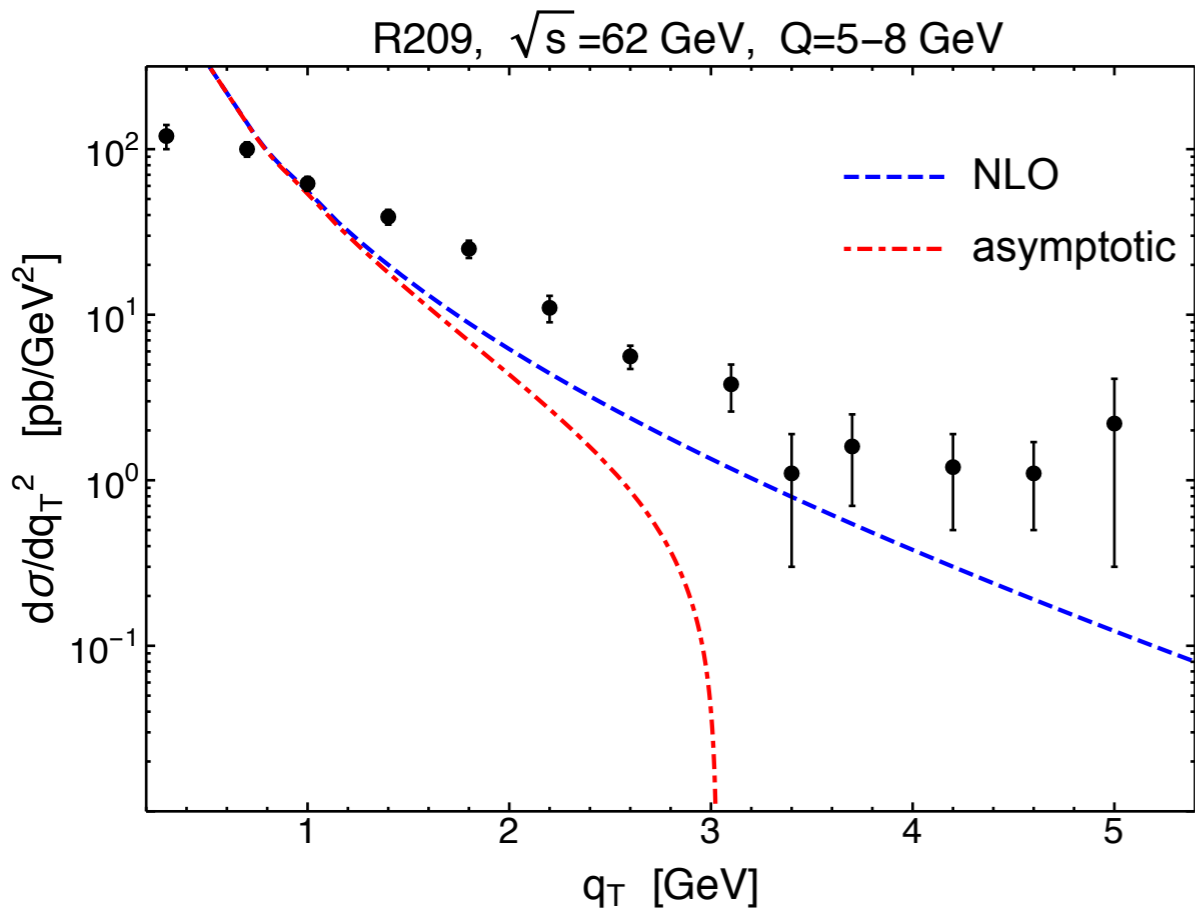
$$\frac{d\sigma}{dq_T^2}(\text{matched}) = \underbrace{\frac{d\sigma}{dq_T^2}(\text{resum})_{NLL}}_W - \underbrace{\frac{d\sigma}{dq_T^2}(\text{expanded})}_{O(\alpha_s^3)} + \frac{d\sigma}{dq_T^2}(\text{LO})$$

Asymptotic term

W
Y



## scale uncertainty

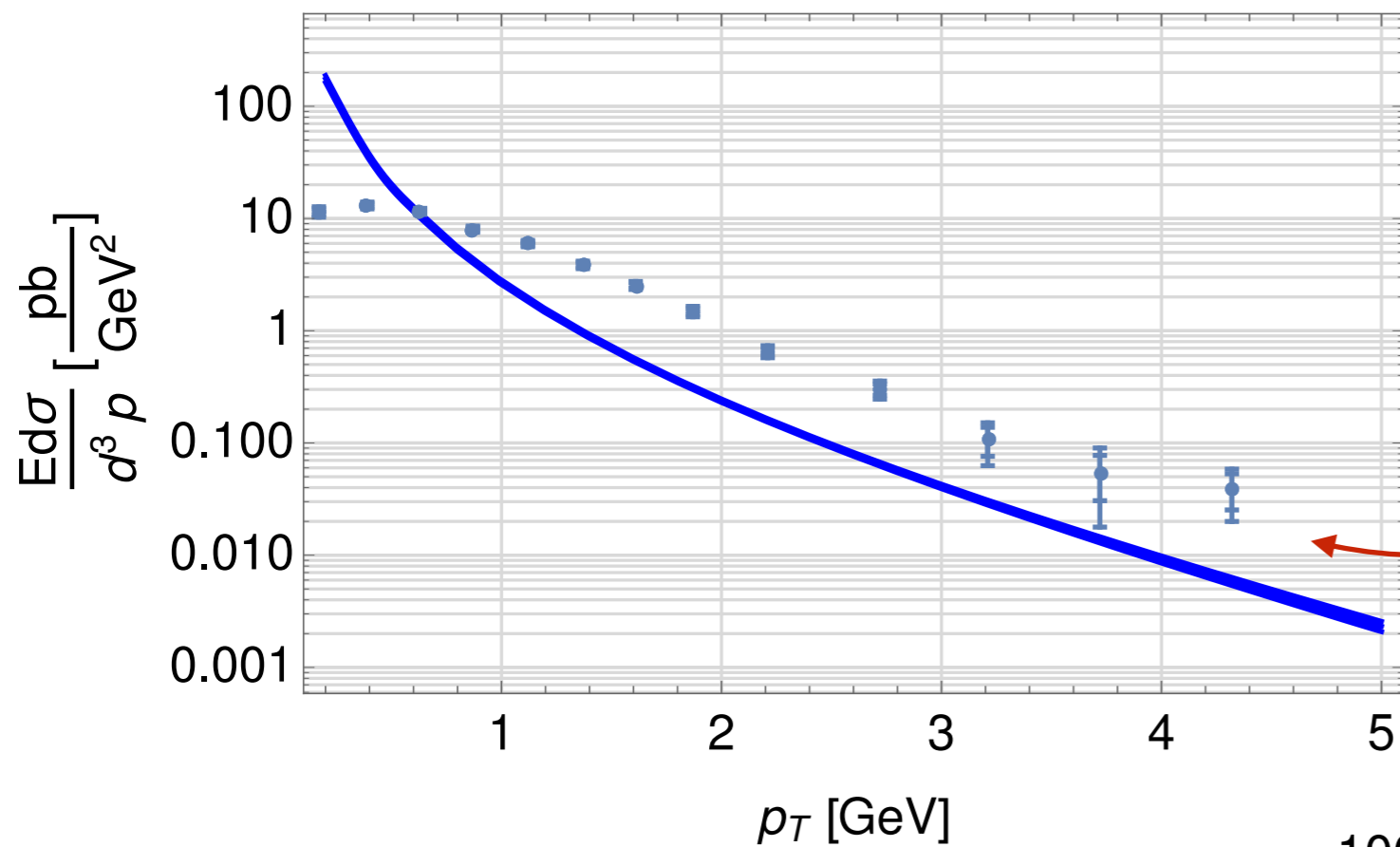


E866/NuSea

$$pp \rightarrow \mu^+ \mu^- X$$

$$\sqrt{s} = 38.8 \text{ GeV}$$

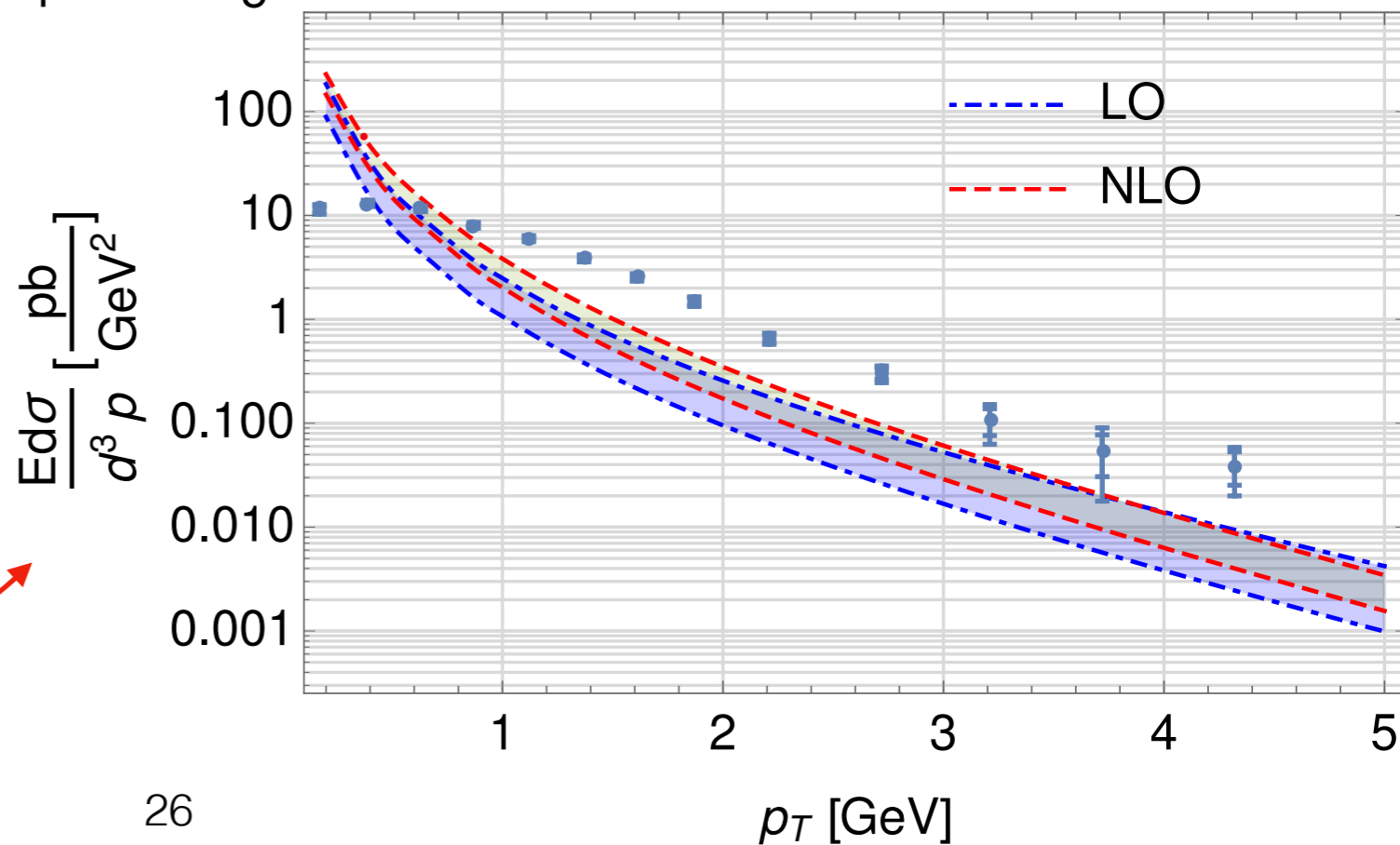
$Q=4.2-5.2 \text{ GeV}, x_F=0.15-0.35$

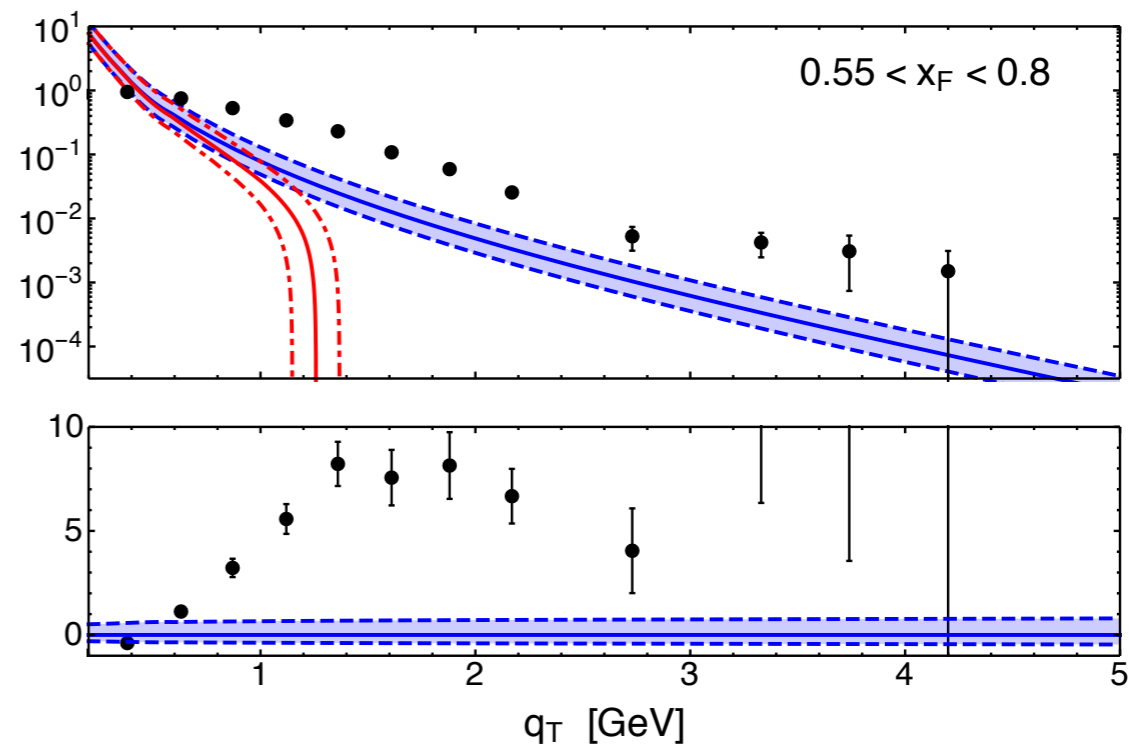
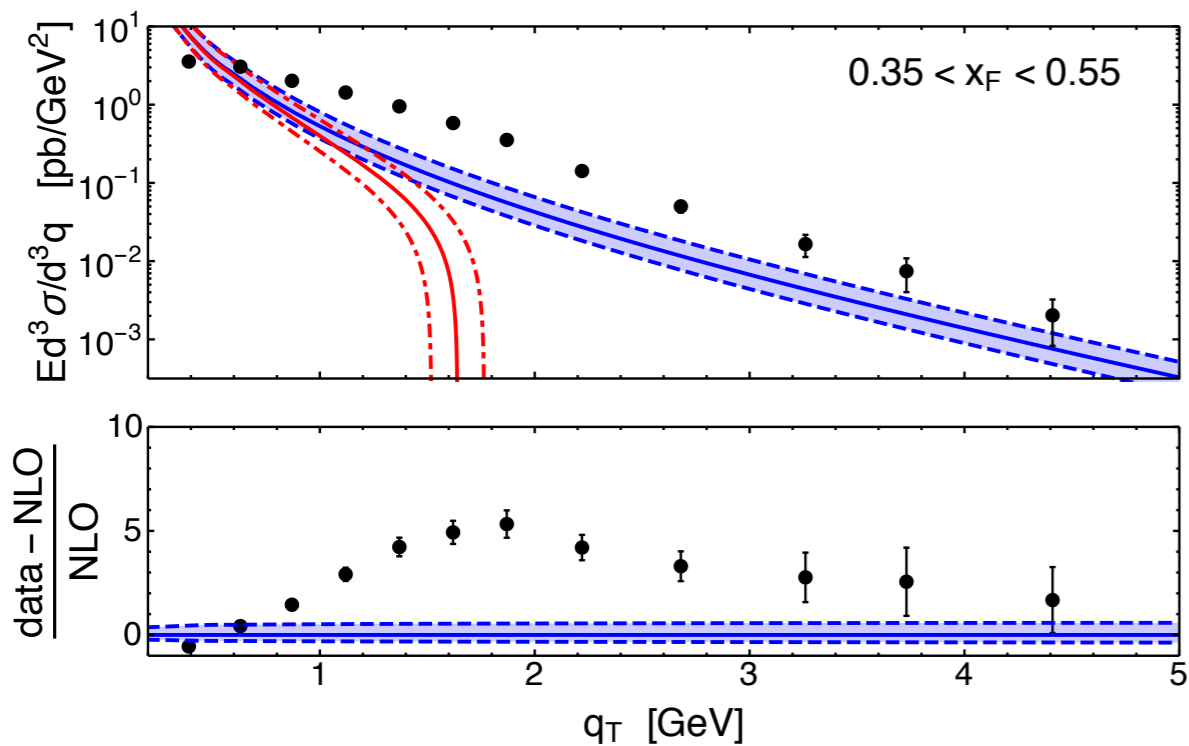
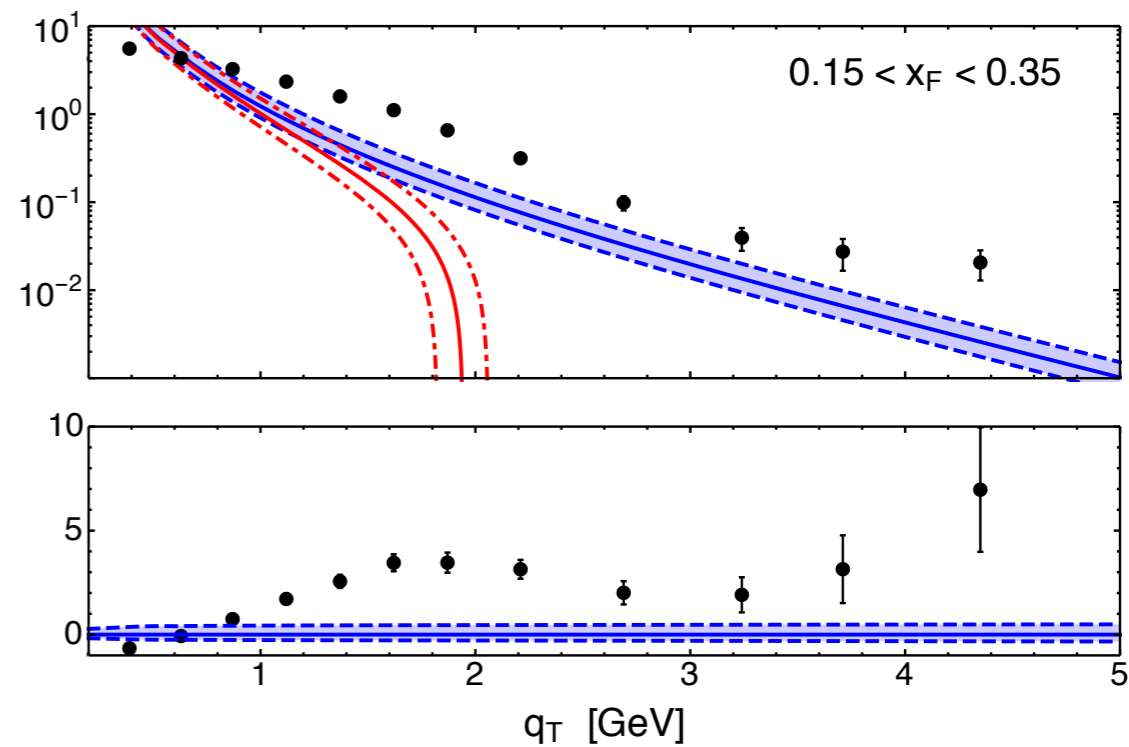
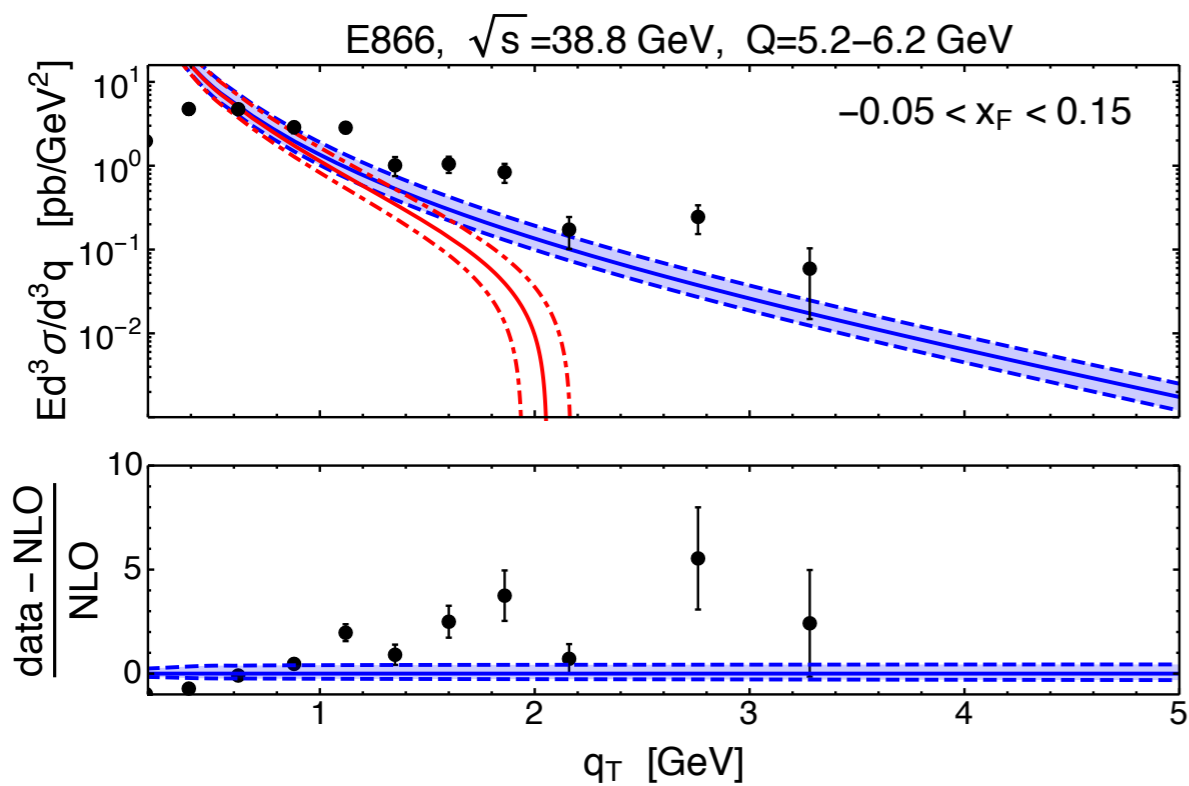


NLO  $\mathcal{O}(\alpha_s^2)$   
+PDF uncertainty

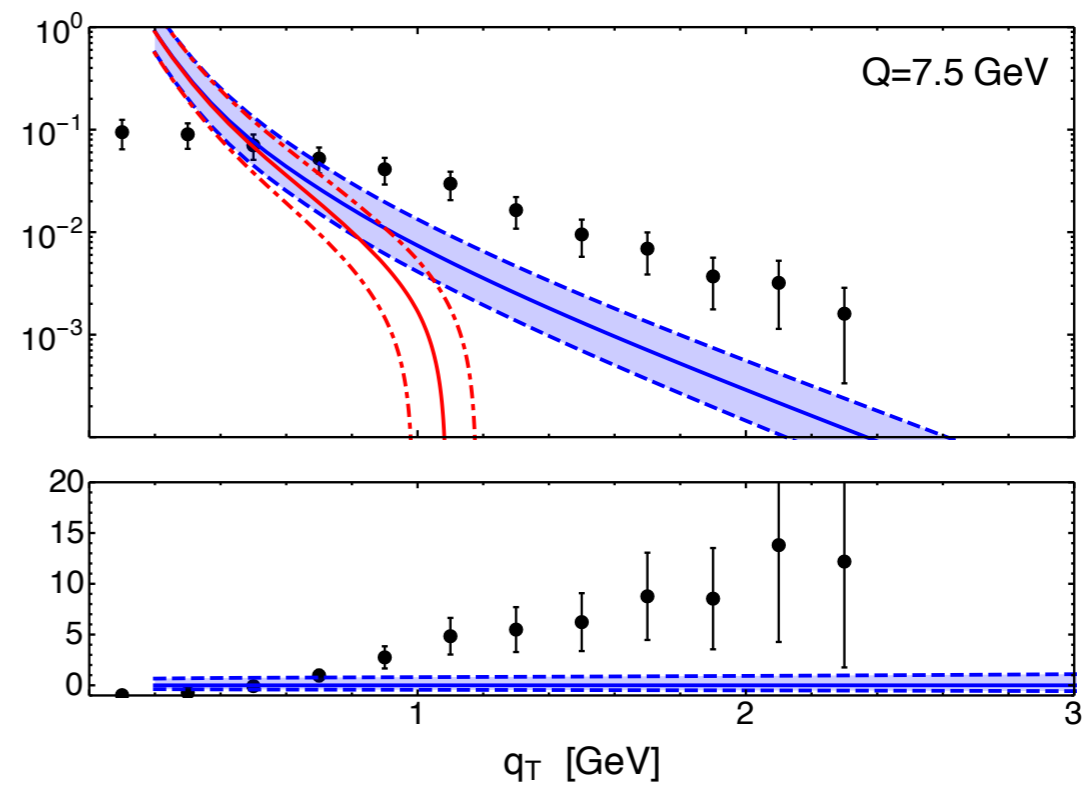
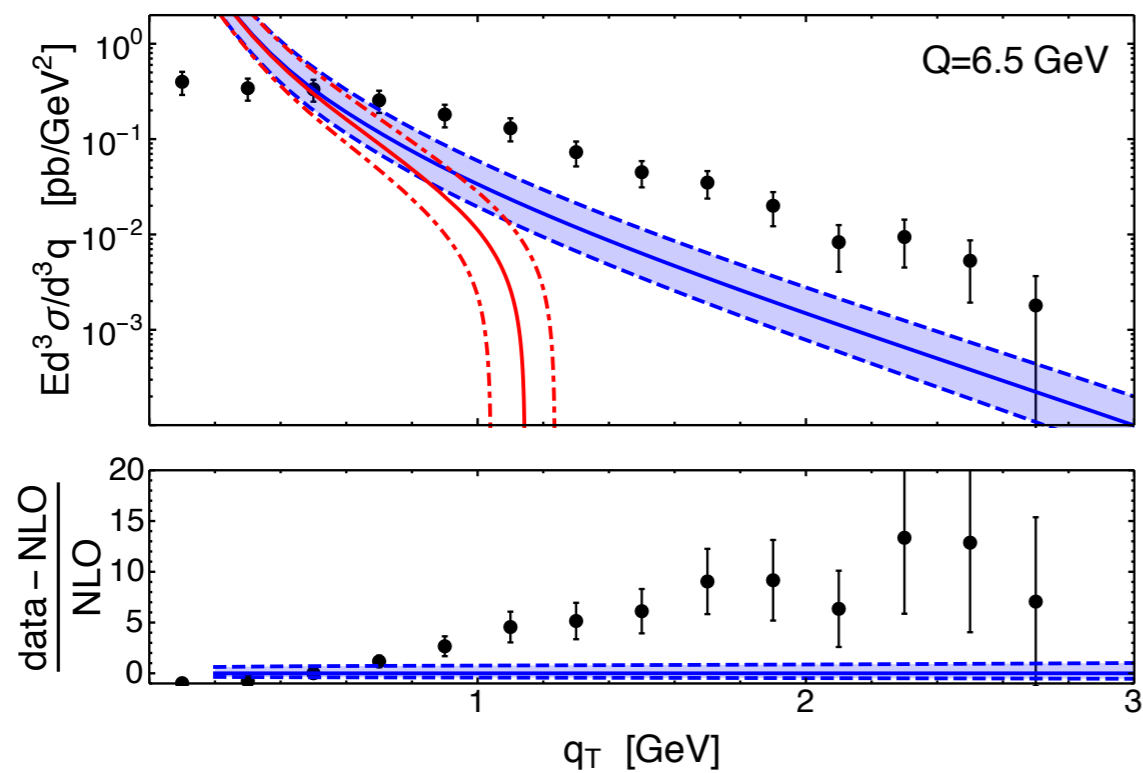
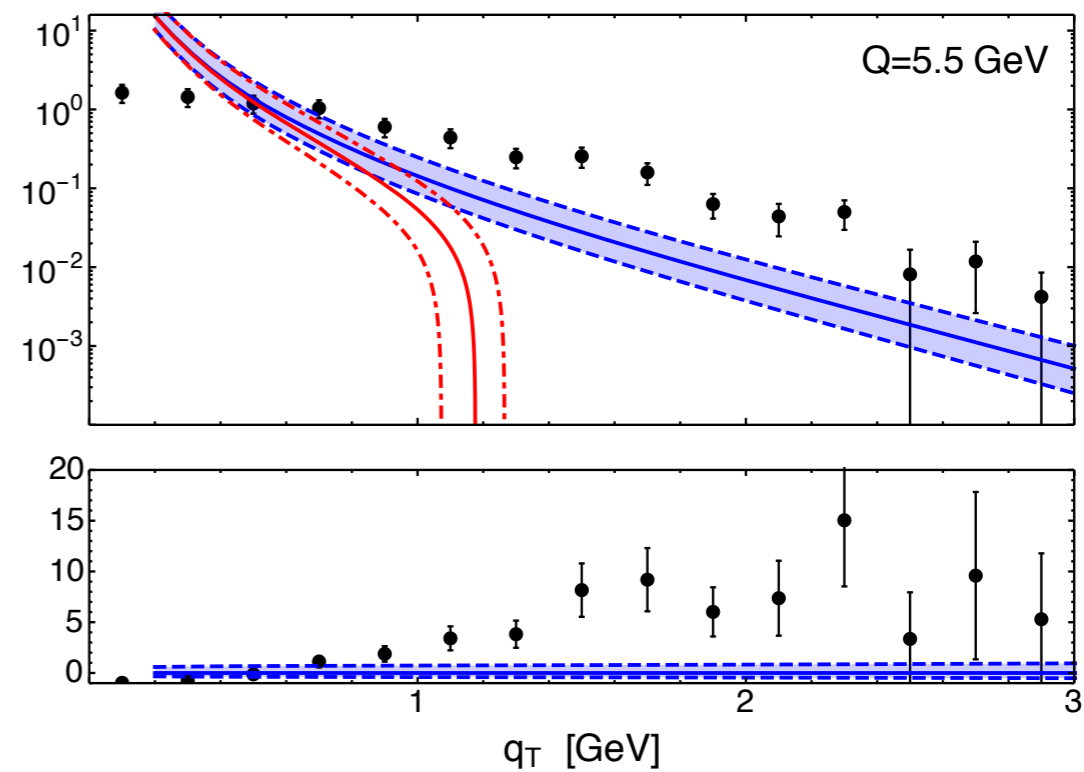
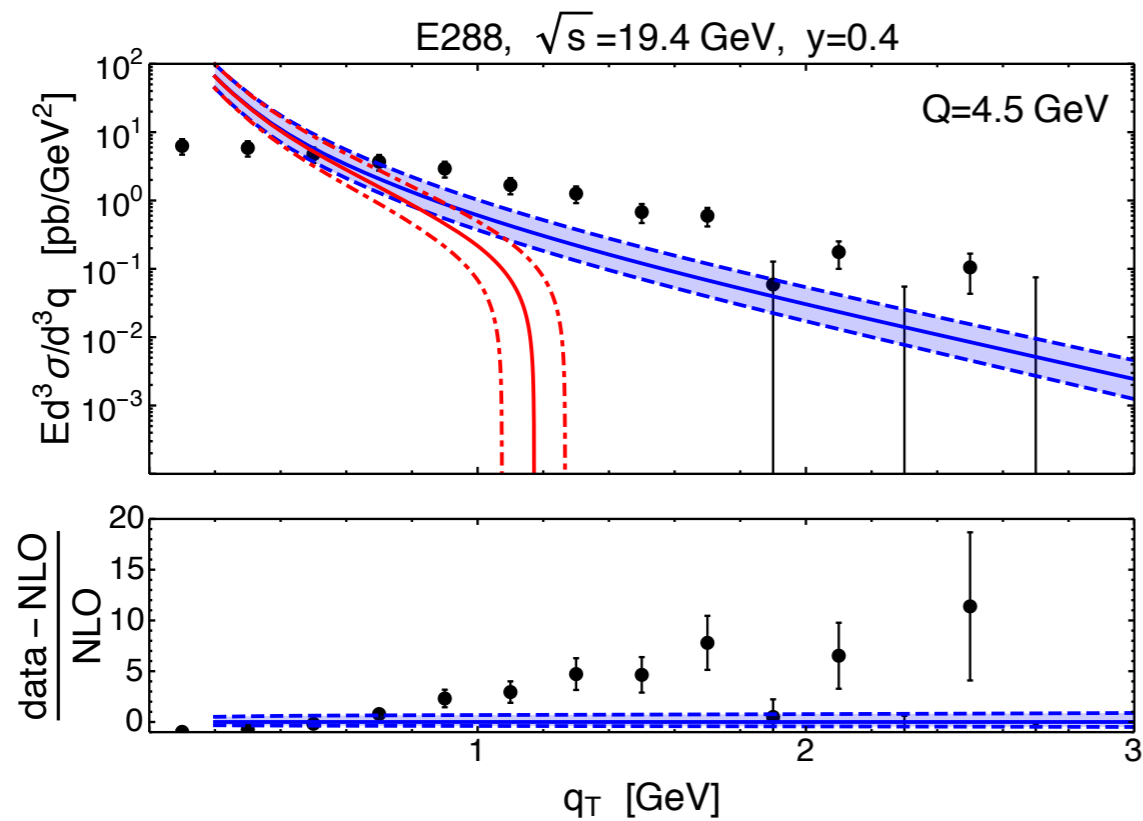
$Q=4.7 \text{ GeV}, x_F=\{0.15,0.35\}, \text{target}=p$

scale uncertainty



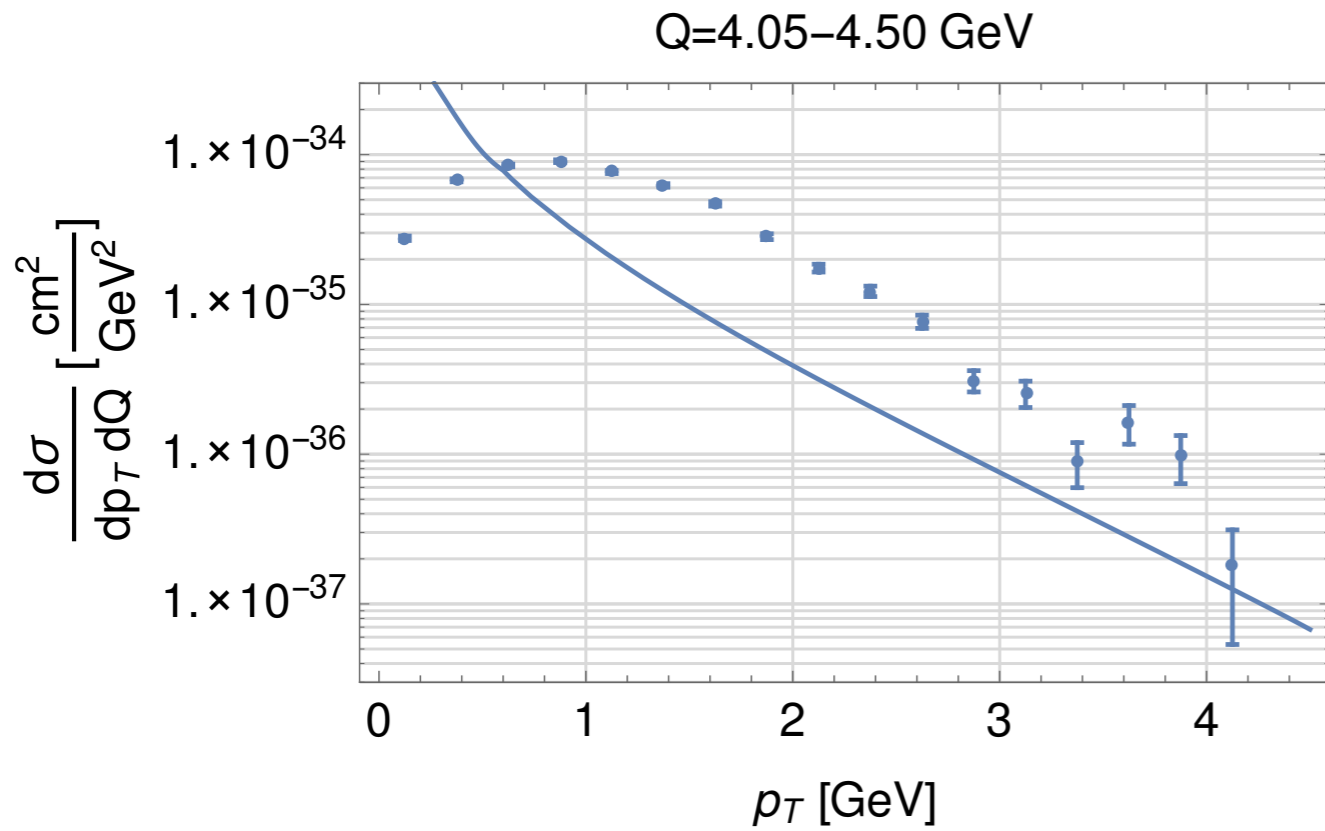


--- NLO  
 --- asymptotic

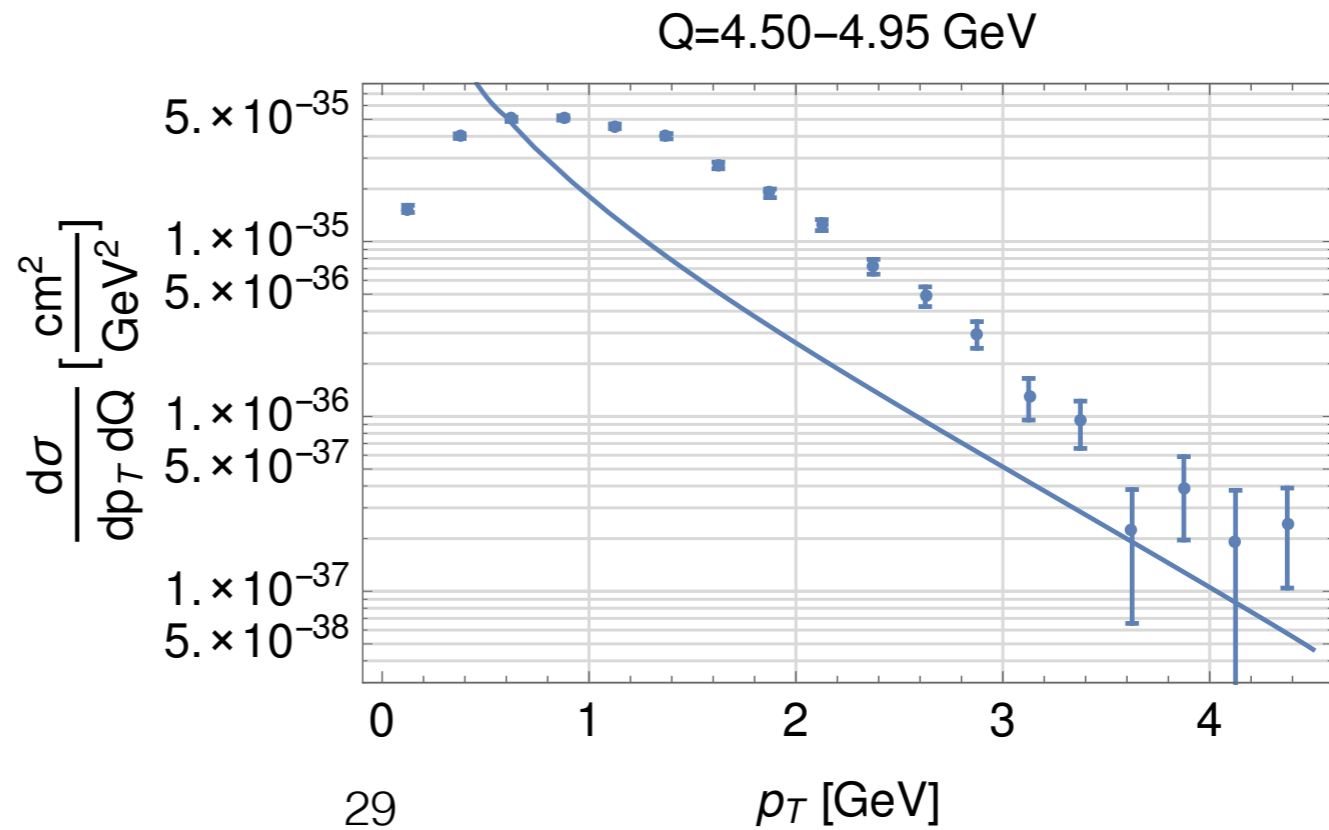
**E288** $p \text{ Cu}(Pt) \rightarrow \mu^+ \mu^- X$ 

**E615**

$$\pi W \rightarrow \mu^+ \mu^- X$$
$$\sqrt{s} = 21.8 \text{ GeV}$$

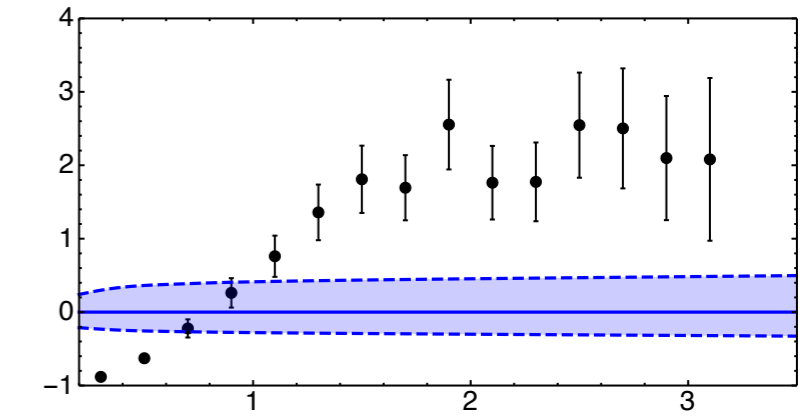
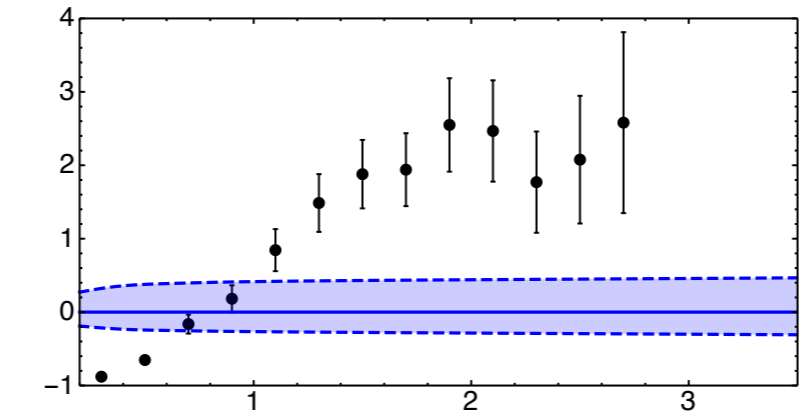
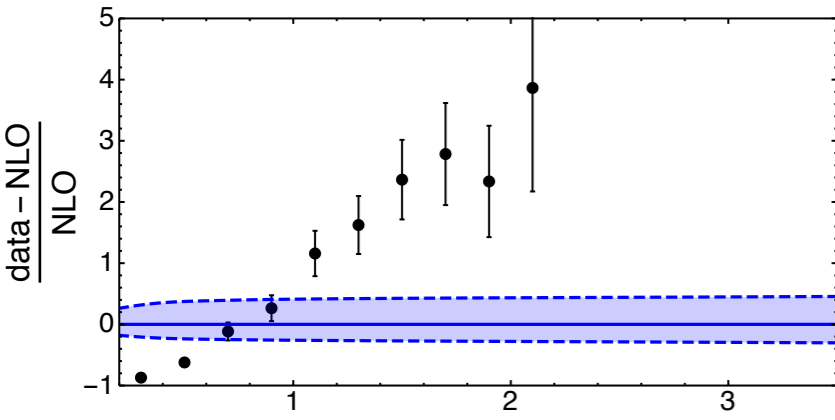
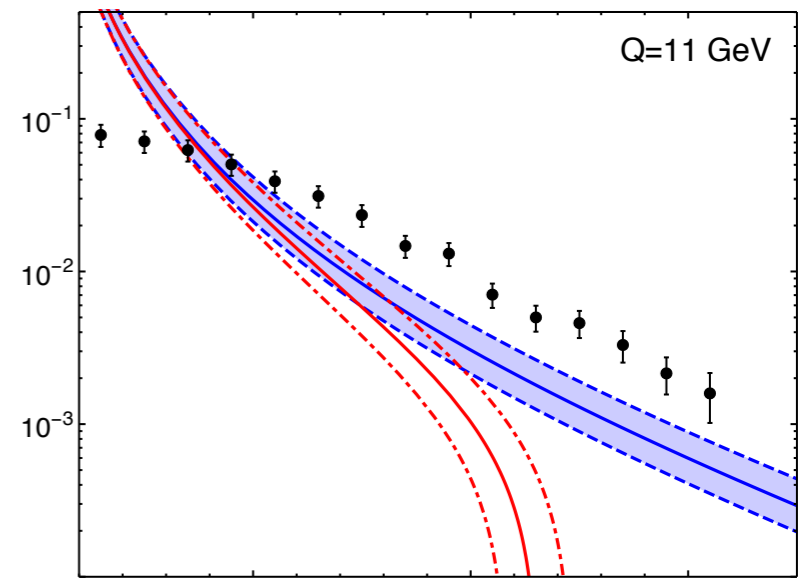
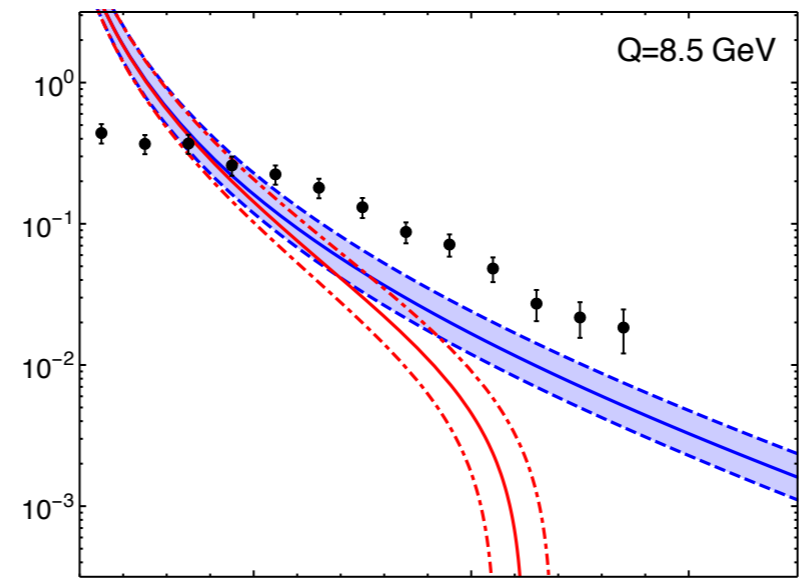
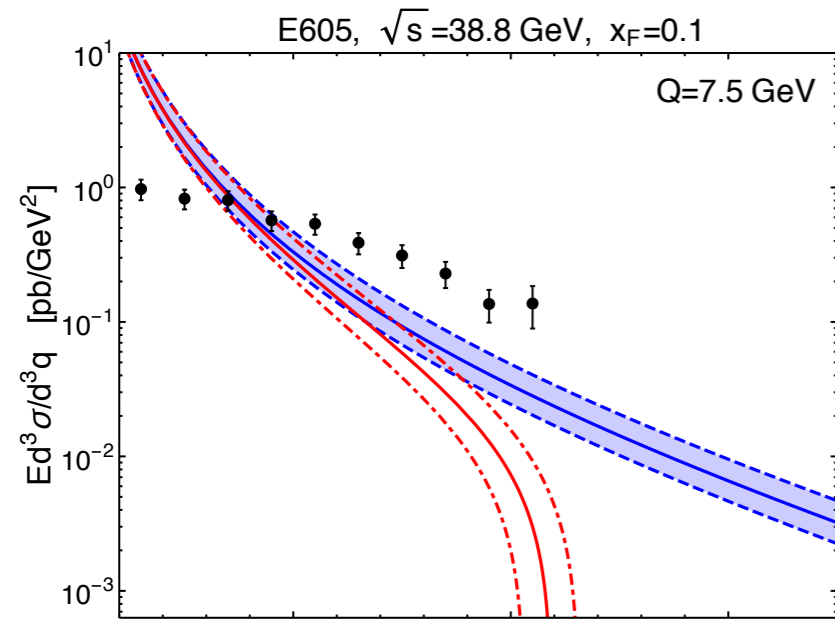


**NLO**  $\mathcal{O}(\alpha_s^2)$



E605

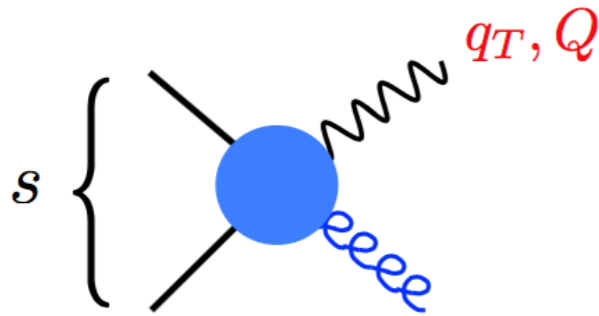
$p \text{ Cu(Pt)} \rightarrow \mu^+ \mu^- X$   
 $\sqrt{s} = 38.8 \text{ GeV}$



--- NLO  
- - - asymptotic

# threshold resummation

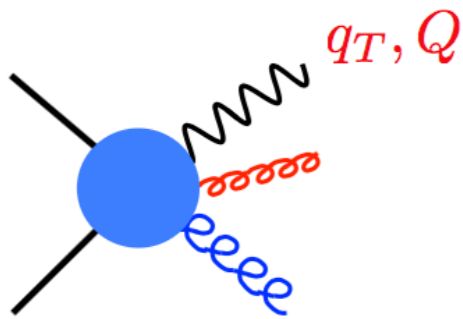
• LO :



$$\sqrt{s} \geq q_T + \sqrt{Q^2 + q_T^2}$$

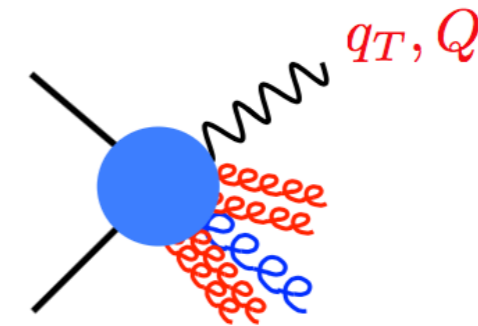
$$y_T \equiv \frac{q_T + \sqrt{q_T^2 + Q^2}}{\sqrt{s}} \leq 1$$

• NLO :



$$\frac{d\hat{\sigma}^{\text{NLO}}}{dq_T} \propto \alpha_s [\mathcal{A} \log^2(1 - y_T^2) + \mathcal{B} \log(1 - y_T^2) + \mathcal{C}]$$

• N<sup>k</sup>LO :

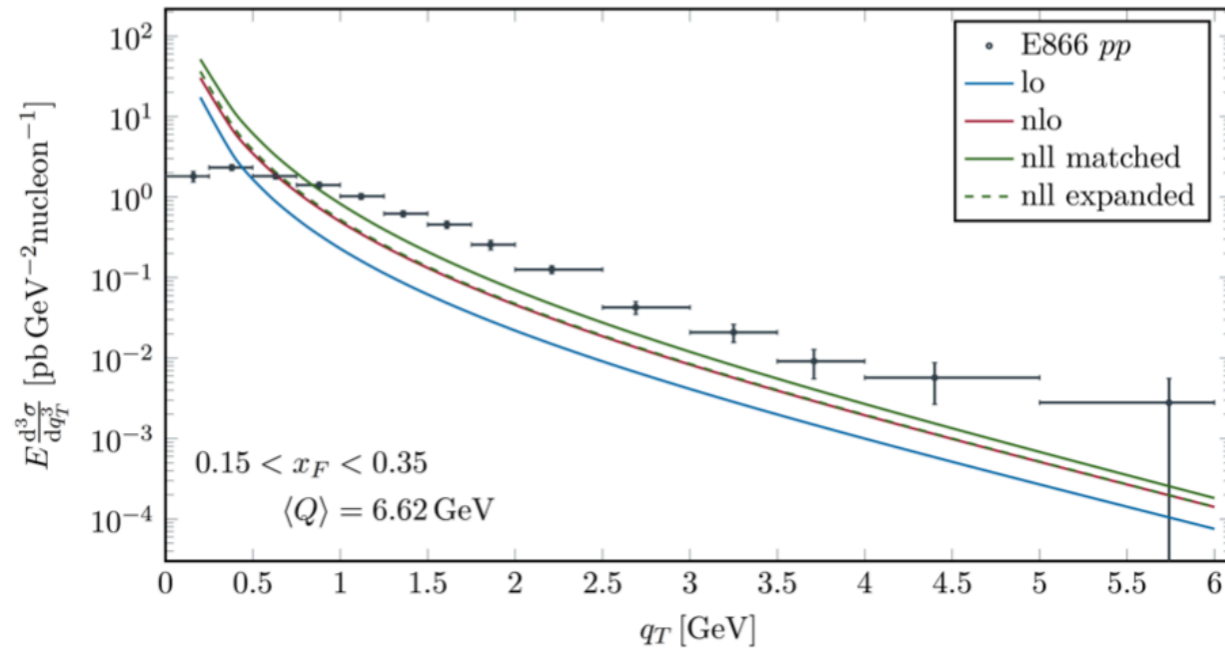


$$\frac{d\hat{\sigma}^{\text{N}^k\text{LO}}}{dq_T} \propto \alpha_s^k \log^{2k}(1 - y_T^2) + \dots$$

• threshold logarithms

W. Vogelsang @Transversity 2017

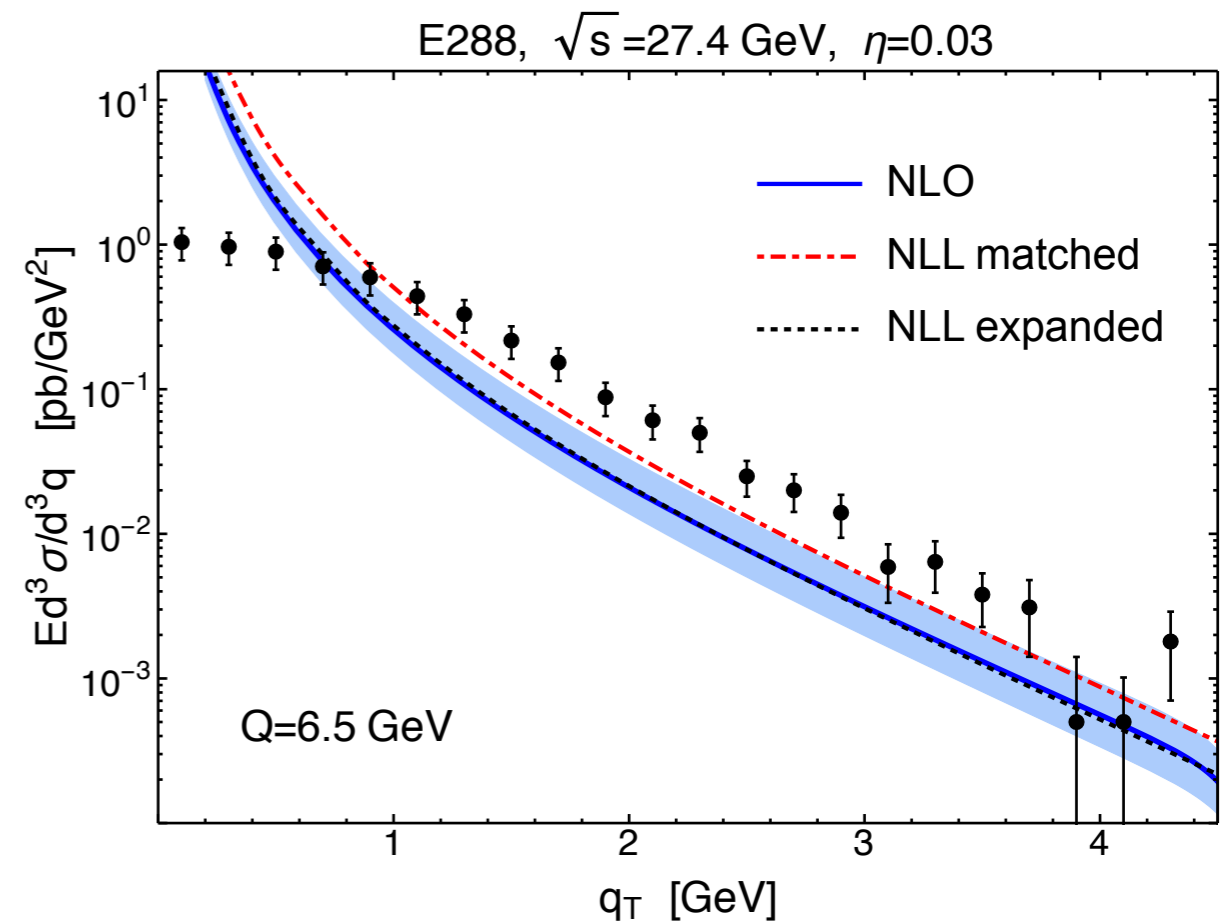
# threshold resummation



E288

E866/NuSea

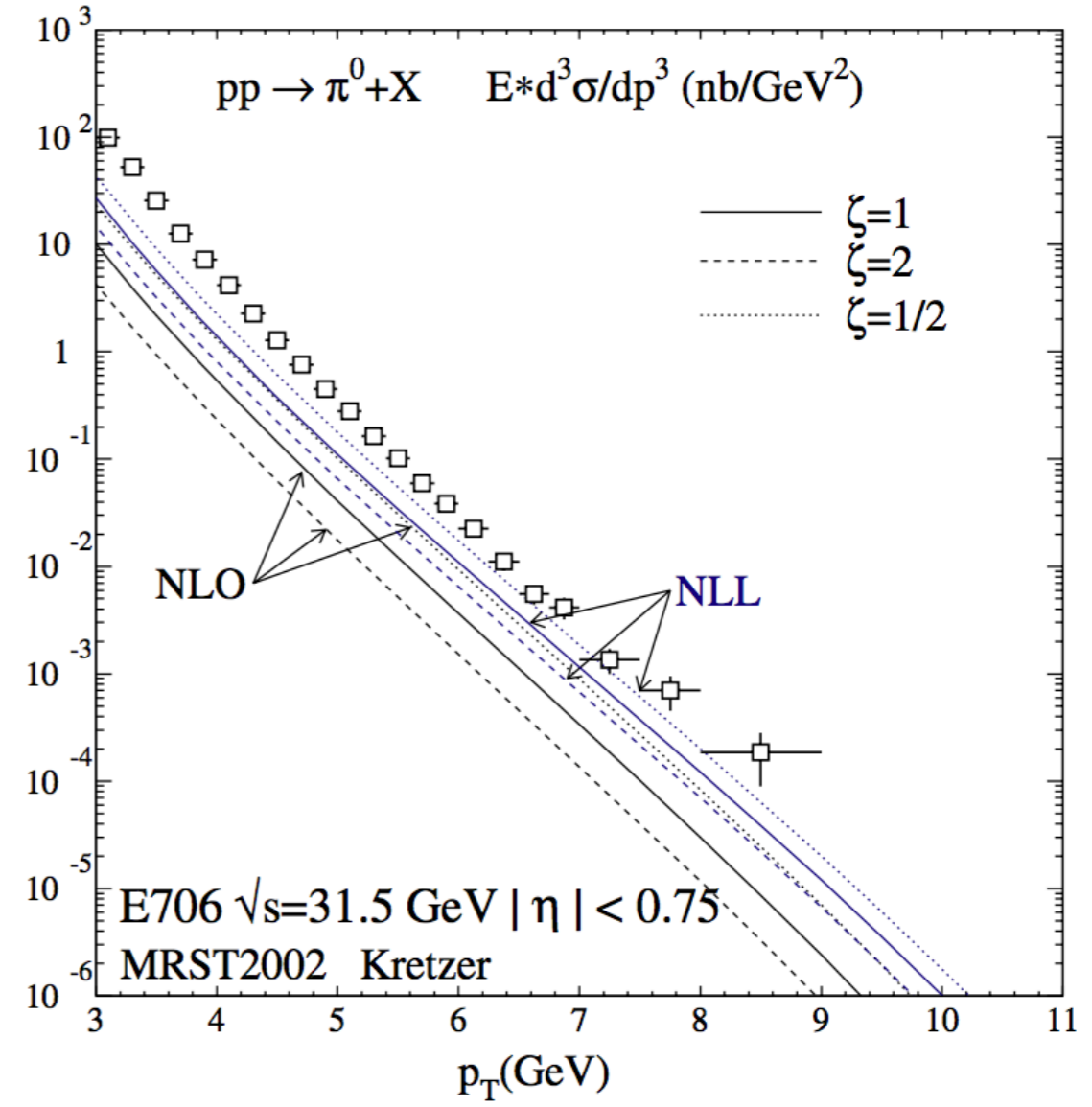
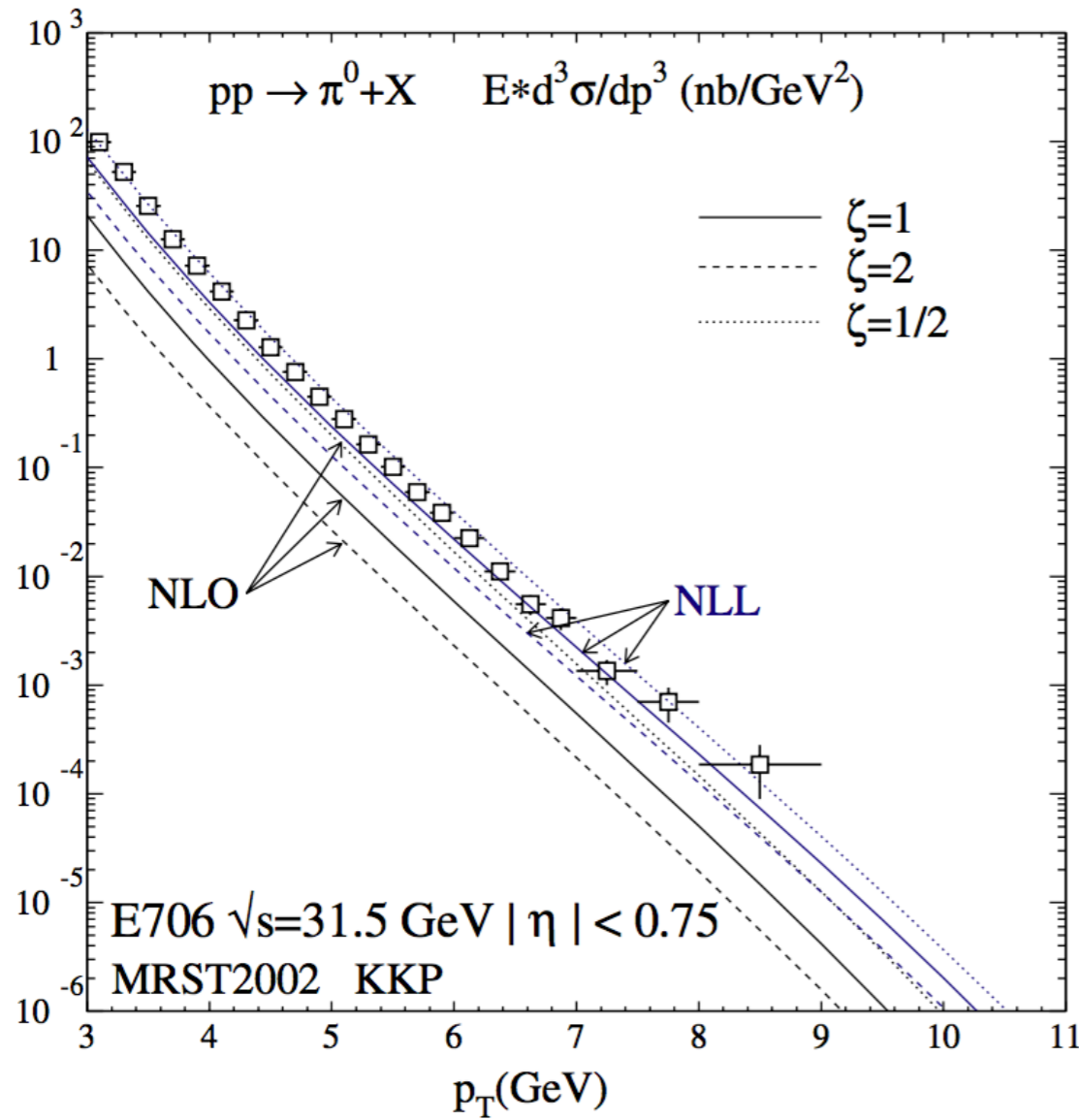
W. Vogelsang @Transversity 2017





# known similar cases

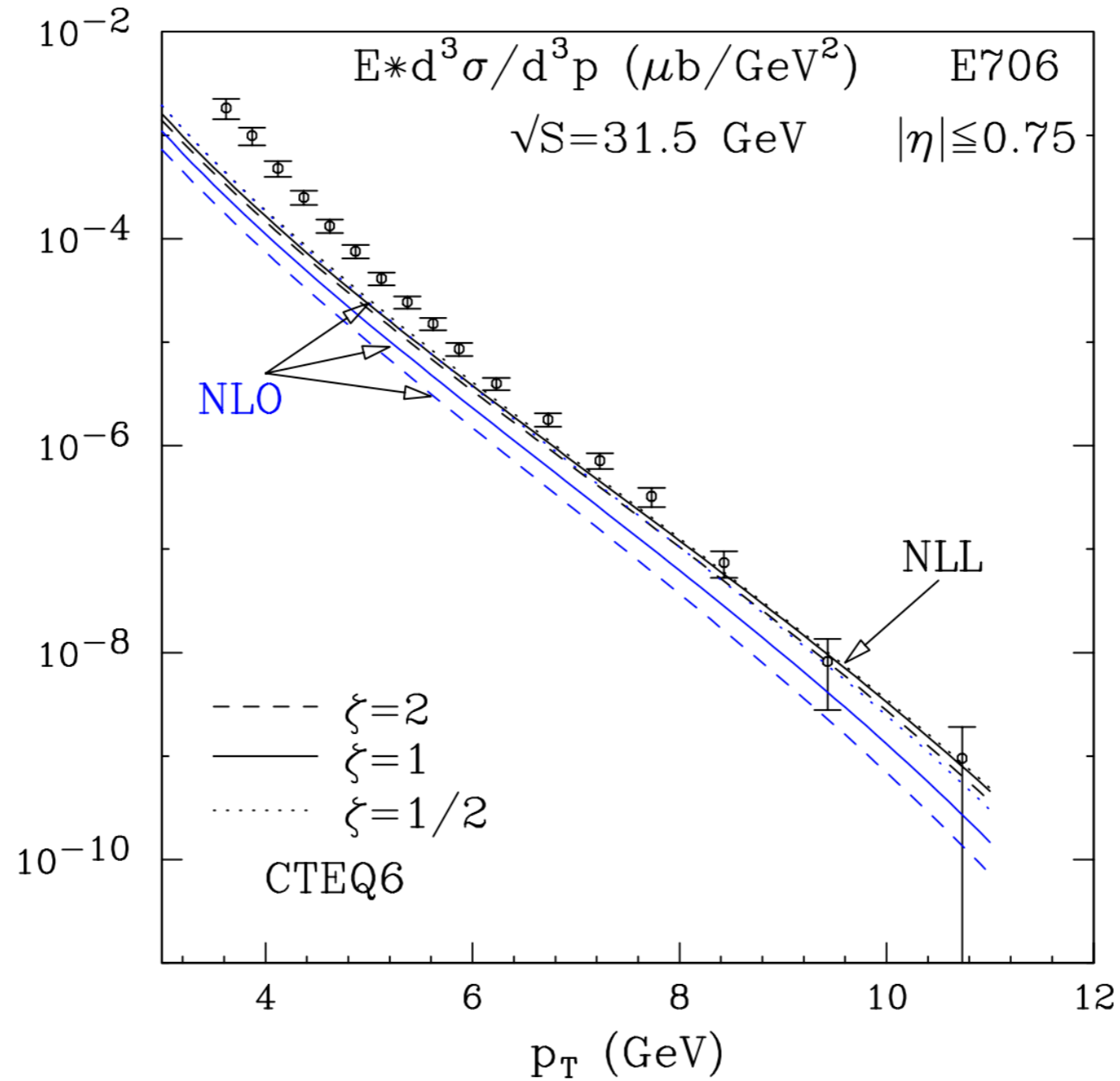
## pion production



de Florian Vogelsang PRD 71 114004 (2005)

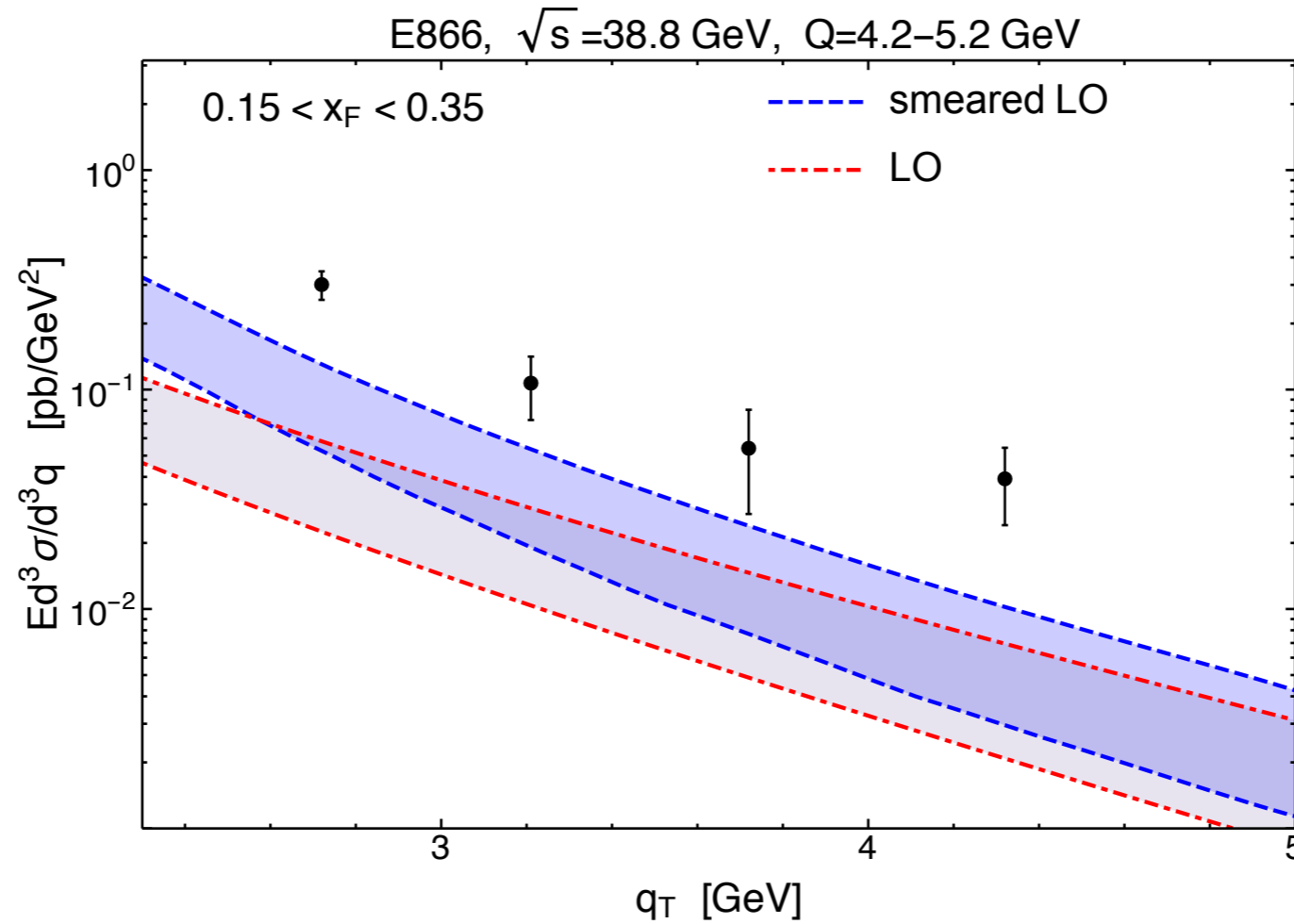
# known similar cases

prompt photon



de Florian Vogelsang PRD 72 014014 (2005)

# intrinsic $k_T$ smearing



$$f_q(x, \mathbf{k}_T) = f(x) \frac{1}{\pi \langle k_T^2 \rangle} e^{-\frac{k_T^2}{\langle k_T^2 \rangle}}$$

$$\langle k_T^2 \rangle = 0.81 \text{ GeV}^2$$

taken from TMD fit  
 flavour-blind and kinematical-independent  
 (gluons as well!)

# Conclusions (?)

- fixed-order pQCD largely underestimates low-energy Drell-Yan data at high  $q_T$
- neither threshold resummation nor intrinsic- $k_T$  models seem to help
- more high  $q_T$  data needed
- important to see effects of E866 data in TMD fits
- any help/hint/comment/suggestion is welcome!

## Part 3

Impact on precision measurements at the LHC:  
the  $W$  mass case

# The extraction of physical quantities

## Observables

- accessible via **counting experiments**: cross sections and asymmetries

## Pseudo-Observables

- functions of cross sections and symmetries
- **require a model** to be properly defined
  - $M_Z$  at LEP as pole of the Breit-Wigner resonance factor
  - $M_W$  at hadron colliders as fitting parameter of a *template fit* procedure

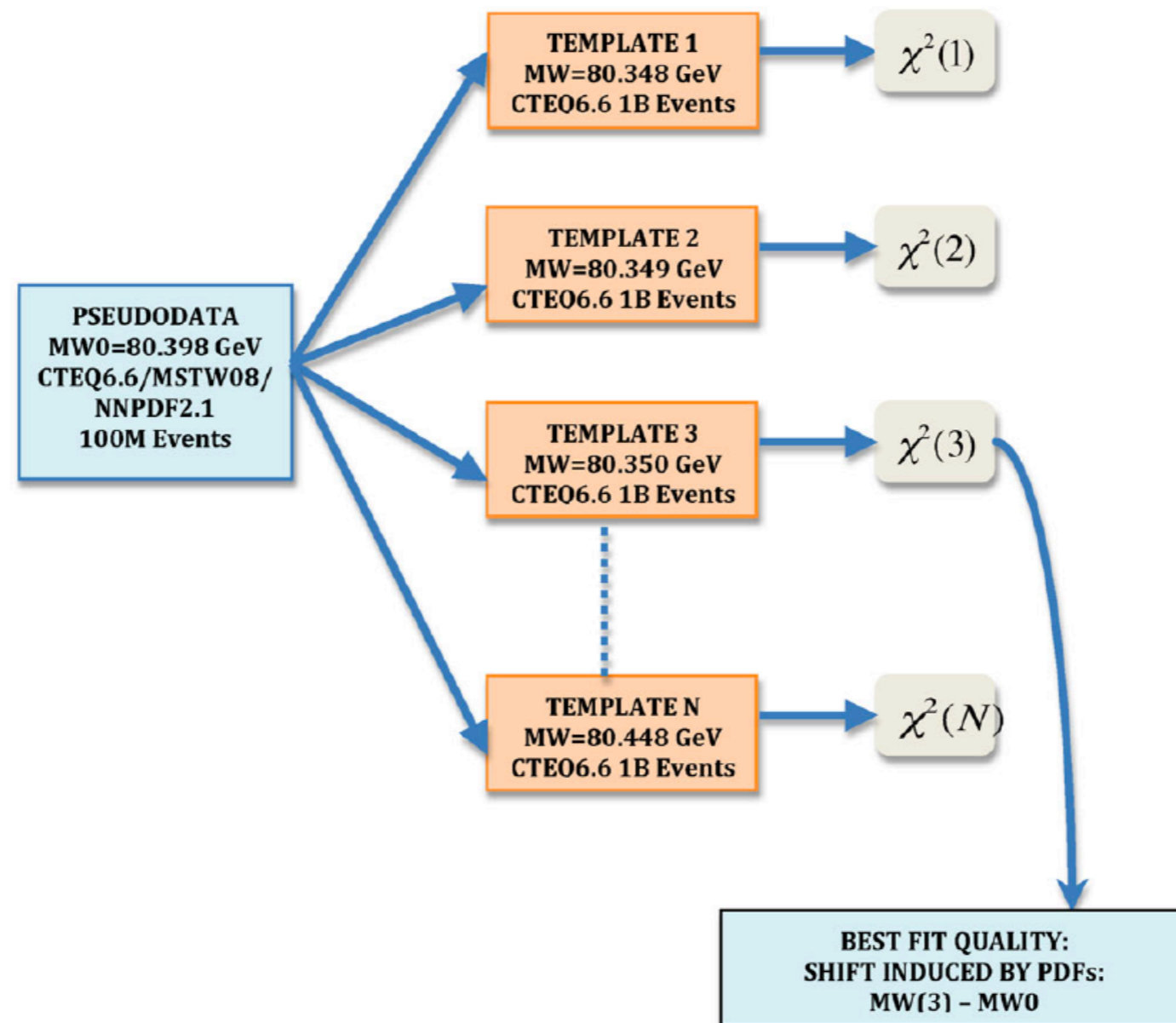
## Template fit

1. generate several histograms with the highest available theoretical accuracy and degree of realism in the detector simulation, and let the fit parameter (e.g.  $M_W$ ) vary in a range
  2. the histogram that best describes data selects the preferred (*i.e.* measured)  $M_W$
- the result of the fit depends on the **hypotheses used to compute the templates** (PDFs, scales, non-perturbative, different prescriptions, ...)
- these hypotheses **should be treated as theoretical systematic errors**

# General template-fit strategy (example: PDF uncertainty)

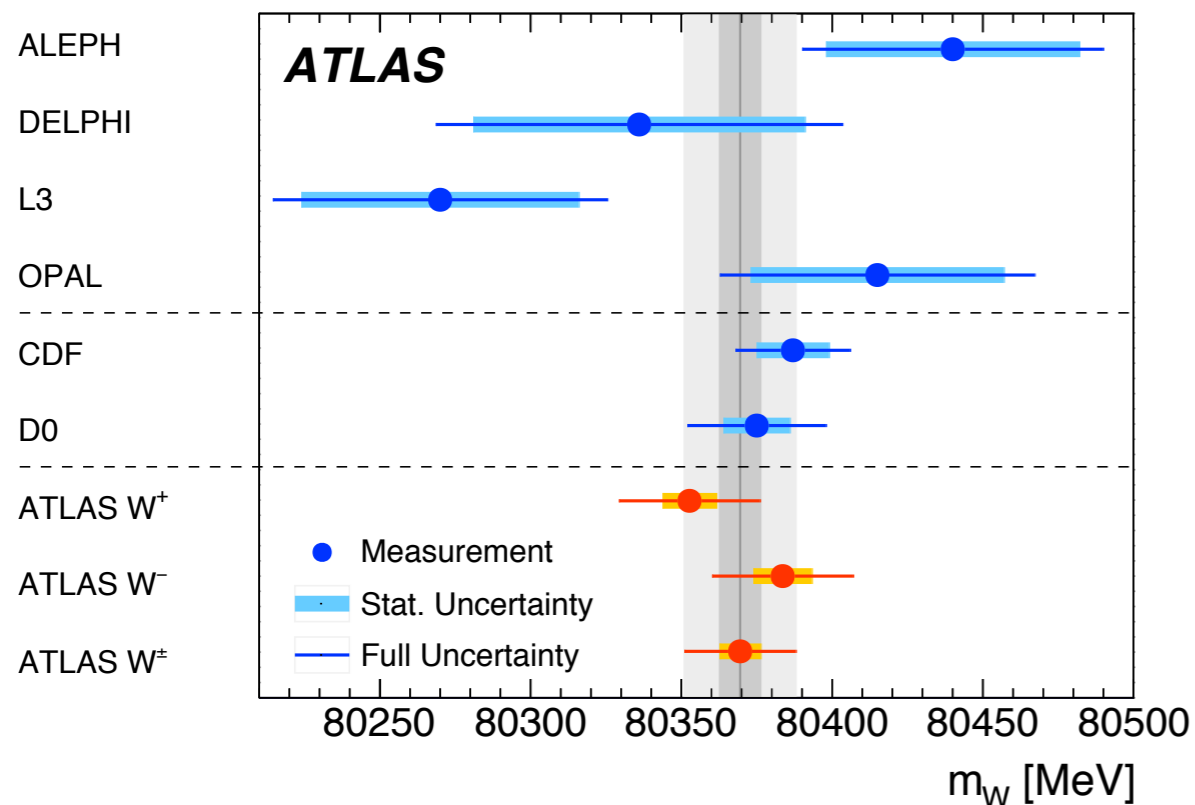
Bozzi, Rojo, Vicini PRD 83, 113008 (2011)

- **pseudodata** with different PDF sets: low-statistics (100M) and fixed  $M_{W0}$
- **templates** with a reference PDF set (CTEQ6.6): high-statistics (1B) and different  $M_W$
- same code used to generate both pseudodata and templates → **only effect probed is the PDF one**



# The $W$ mass

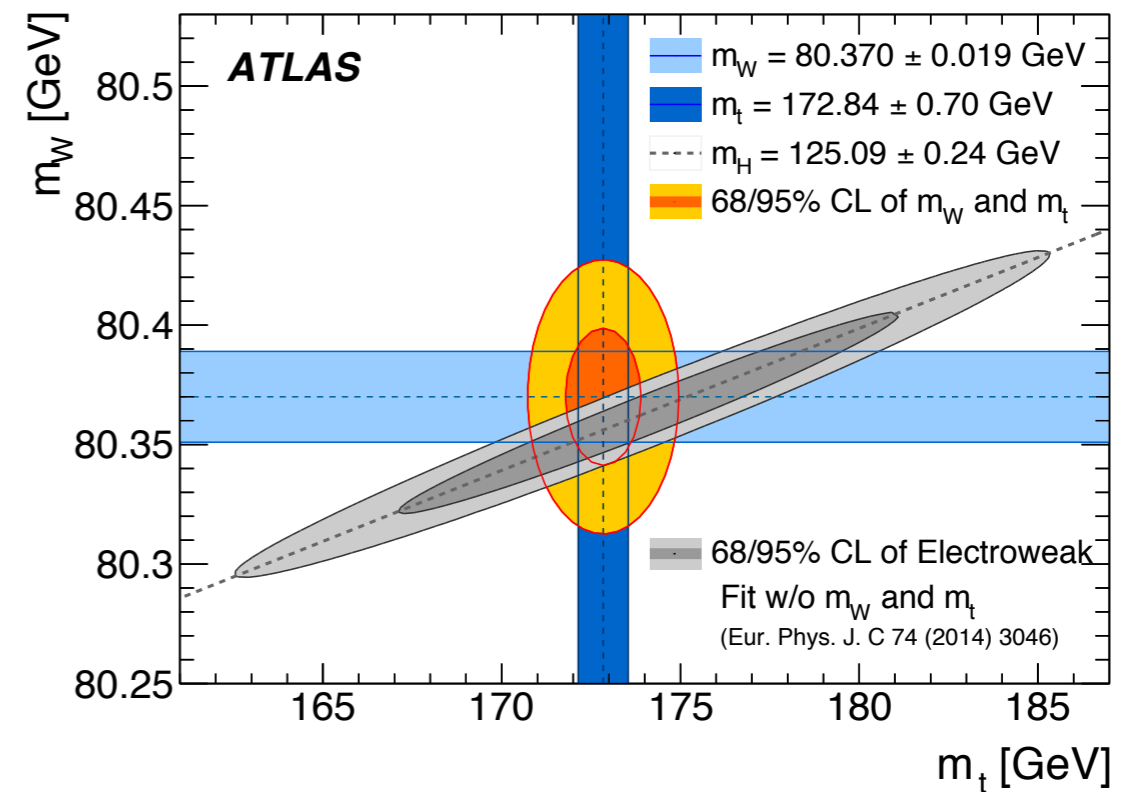
ATLAS, EPJC 78, 110 (2018)



## Experimental measurements

$$M_W = 80.379 \pm 12 \text{ MeV}$$

(7 stat, 11 exp, 14 th)



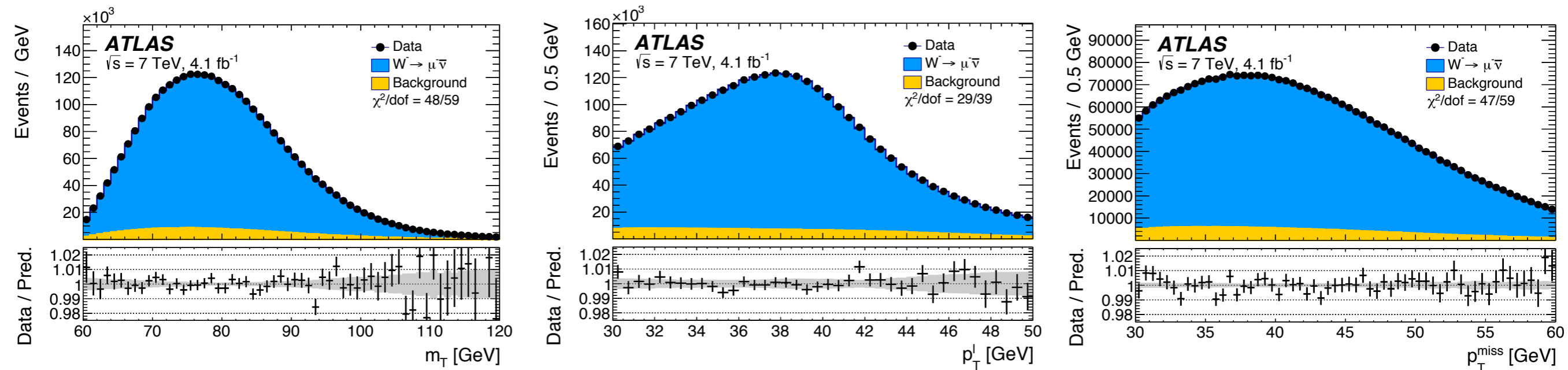
## Global EW fit

$$M_W = 80.356 \pm 8 \text{ MeV}$$

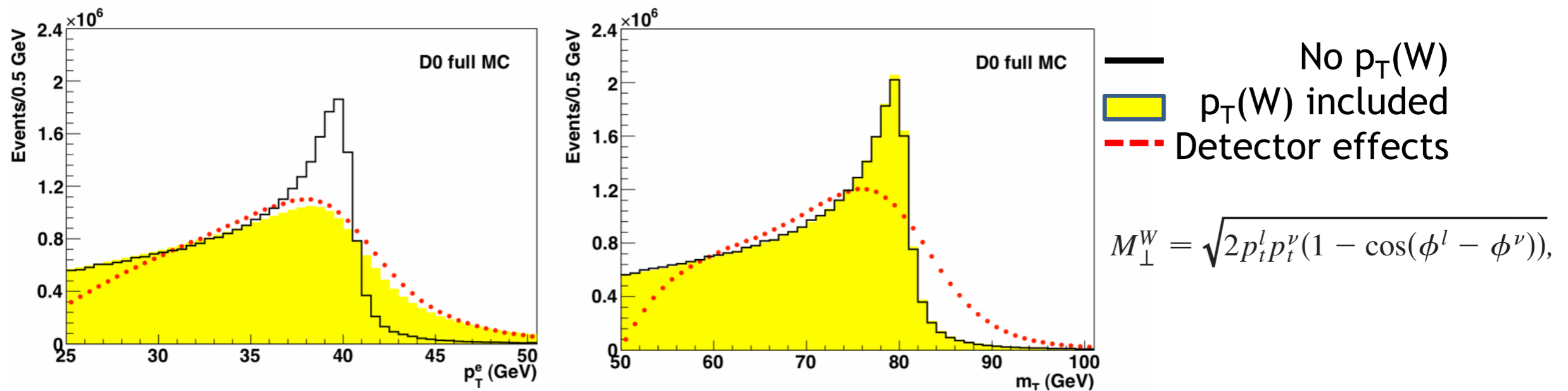
The determination of the  $W$ -boson mass from the global fit of the electroweak parameters has an uncertainty of 8 MeV, which sets a natural target for the precision of the experimental measurement of the mass of the  $W$  boson. The modelling uncertainties, which currently dominate the overall uncertainty on the  $m_W$  measurement presented in this note, need to be reduced in order to fully exploit the larger data samples available at centre-of-mass energies of 8 and 13 TeV. A better knowledge of the PDFs, as achievable with the inclusion in PDF fits of recent precise measurements of  $W$ - and  $Z$ -boson rapidity cross sections with the ATLAS detector [41], and improved QCD and electroweak predictions for Drell-Yan production, are therefore crucial for future measurements of the  $W$ -boson mass at the LHC.



# Observables and techniques



$M_W$  extracted from the study of the **shape** of  $m_T$ ,  $p_{Tl}$ ,  $p_{Tmiss}$   
**Jacobian peak** enhances sensitivity to  $M_W$

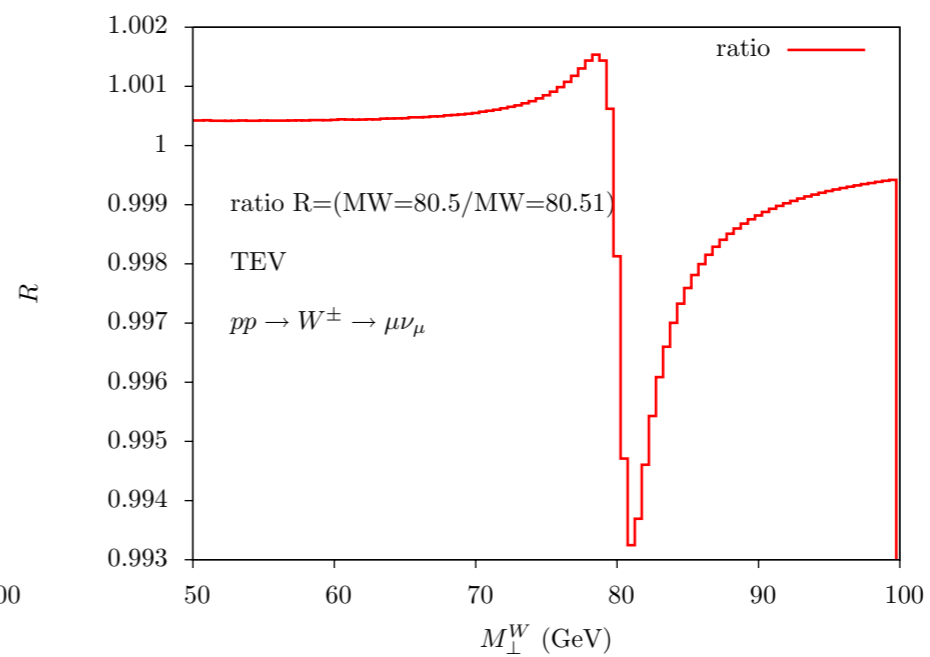
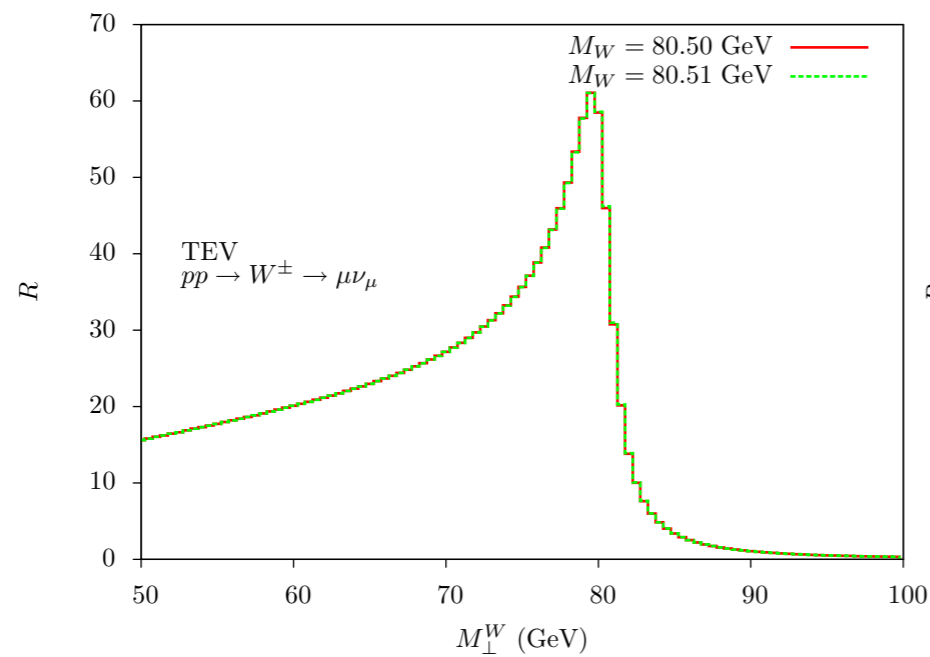


Transverse mass: **important** detector smearing effects, **weakly** sensitive to  $p_{TW}$  modelling  
 Lepton  $p_T$ : **moderate** detector smearing effects, **extremely** sensitive to  $p_{TW}$  modelling  
 $p_{TW}$  modelling depends on flavour and all-order treatment of QCD corrections

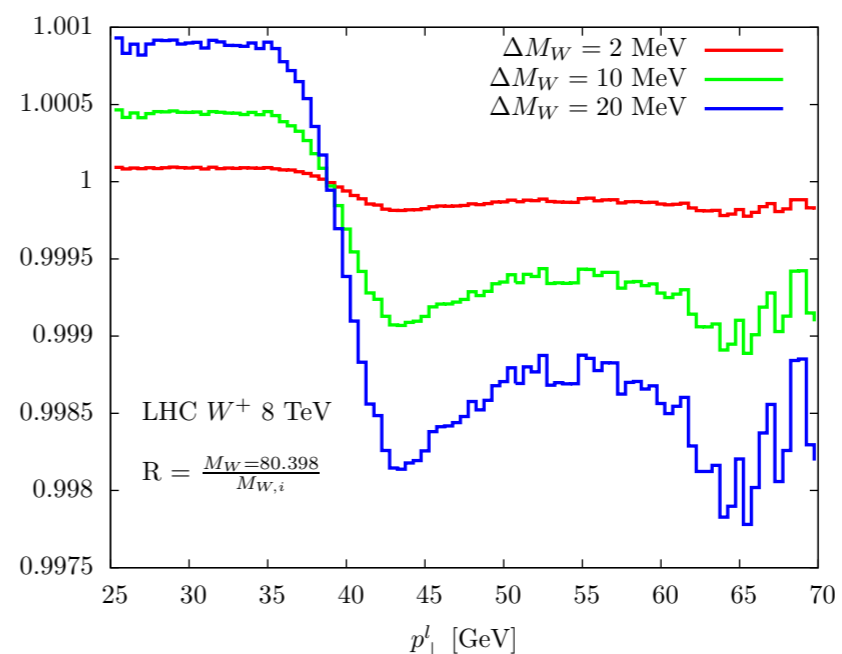
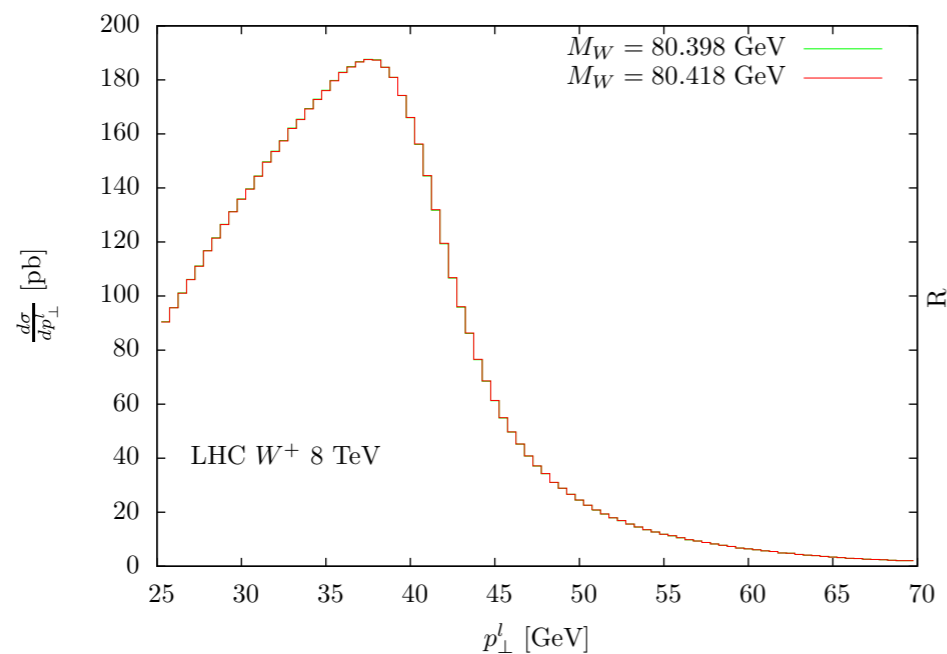
# Observables and techniques

Challenging shape measurement: a distortion at the **few per mille** level of the distributions yields a shift of **O(10 MeV)** of the  $M_W$  value

$m_T$



$p_{Tl}$



# Uncertainties on $M_W$ due to $p_{TW}$

## CDF

$m_T$ fit uncertainties				$p_T^\ell$ fit uncertainties			
Source	$W \rightarrow \mu\nu$	$W \rightarrow e\nu$	Common	Source	$W \rightarrow \mu\nu$	$W \rightarrow e\nu$	Common
Lepton energy scale	7	10	5	Lepton energy scale	7	10	5
Lepton energy resolution	1	4	0	Lepton energy resolution	1	4	0
Lepton efficiency	0	0	0	Lepton efficiency	1	2	0
Lepton tower removal	2	3	2	Lepton tower removal	0	0	0
Recoil scale	5	5	5	Recoil scale	6	6	6
Recoil resolution	7	7	7	Recoil resolution	5	5	5
Backgrounds	3	4	0	Backgrounds	5	3	0
PDFs	10	10	10	PDFs	9	9	9
$W$ boson $p_T$	3	3	3	$W$ boson $p_T$	9	9	9
Photon radiation	4	4	4	Photon radiation	4	4	4
Statistical	16	19	0	Statistical	18	21	0
Total	23	26	15	Total	25	28	16

## D0

Source	Section	$m_T$	$p_T^\ell$	$E_T$
Experimental				
Electron Energy Scale	VII C4	16	17	16
Electron Energy Resolution	VII C5	2	2	3
Electron Shower Model	V C	4	6	7
Electron Energy Loss	VD	4	4	4
Recoil Model	VII D3	5	6	14
Electron Efficiencies	VII B10	1	3	5
Backgrounds	VIII	2	2	2
$\Sigma(\text{Experimental})$		18	20	24
$W$ Production and Decay Model				
PDF	VIC	11	11	14
QED	VIB	7	7	9
Boson $p_T$	VIA	2	5	2
$\Sigma(\text{Model})$		13	14	17
Systematic Uncertainty (Experimental and Model)		22	24	29
$W$ Boson Statistics	IX	13	14	15
Total Uncertainty		26	28	33

## ATLAS

$W$ -boson charge Kinematic distribution	$W^+$		$W^-$		Combined	
	$p_T^\ell$	$m_T$	$p_T^\ell$	$m_T$	$p_T^\ell$	$m_T$
$\delta m_W$ [MeV]						
Fixed-order PDF uncertainty	13.1	14.9	12.0	14.2	8.0	8.7
AZ tune	3.0	3.4	3.0	3.4	3.0	3.4
Charm-quark mass	1.2	1.5	1.2	1.5	1.2	1.5
Parton shower $\mu_F$ with heavy-flavour decorrelation	5.0	6.9	5.0	6.9	5.0	6.9
Parton shower PDF uncertainty	3.6	4.0	2.6	2.4	1.0	1.6
Angular coefficients	5.8	5.3	5.8	5.3	5.8	5.3
Total	15.9	18.1	14.8	17.2	11.6	12.9

# $\rho_{TW}$ and the modelling of intrinsic $k_T$

- $\rho_{TI} \Leftrightarrow \rho_{TW} \Leftrightarrow$  QCD initial state radiation + intrinsic  $k_T$  (usually, a Gaussian in  $k_T$ )
- Intrinsic  $k_T$  effects measured on  $Z$  data and used to predict  $W$  distributions, *assuming universality*

but

*different flavour structure*

*different phase space available*

—> *different Gaussian factors for different flavours*

$$f_1^{aNP}(x, k_{\perp}^2; Q^2) = \frac{f_1^a(x, Q^2)}{\pi \langle k_{\perp}^2 \rangle_a} e^{-k_{\perp}^2 / \langle k_{\perp}^2 \rangle_a}$$

$$\langle k_{\perp}^2, u_v \rangle \neq \langle k_{\perp}^2, d_v \rangle \neq \langle k_{\perp}^2, u_s \rangle \neq \langle k_{\perp}^2, d_s \rangle \neq \langle k_{\perp}^2, sea \rangle$$

~~Flavor and kinematic dependent widths~~

# Choice of NP parameters

$$\frac{d\sigma}{dq_T} \sim \text{FT} \exp\{-g_{NP} b_T^2\} \longrightarrow \text{Fit to } Z/\gamma^* \text{ Tevatron data: } g_{NP} \sim 0.8 \text{ GeV}^2$$

[Guzzi, Nadolsky, Wang (2014)]

For each TMD:  $0.4 \text{ GeV}^2 \sim g_{NP}^a \longrightarrow g_{evo} \ln\left(\frac{Q^2}{Q_0^2}\right) + g_a \longrightarrow \text{variation range for } g_a$

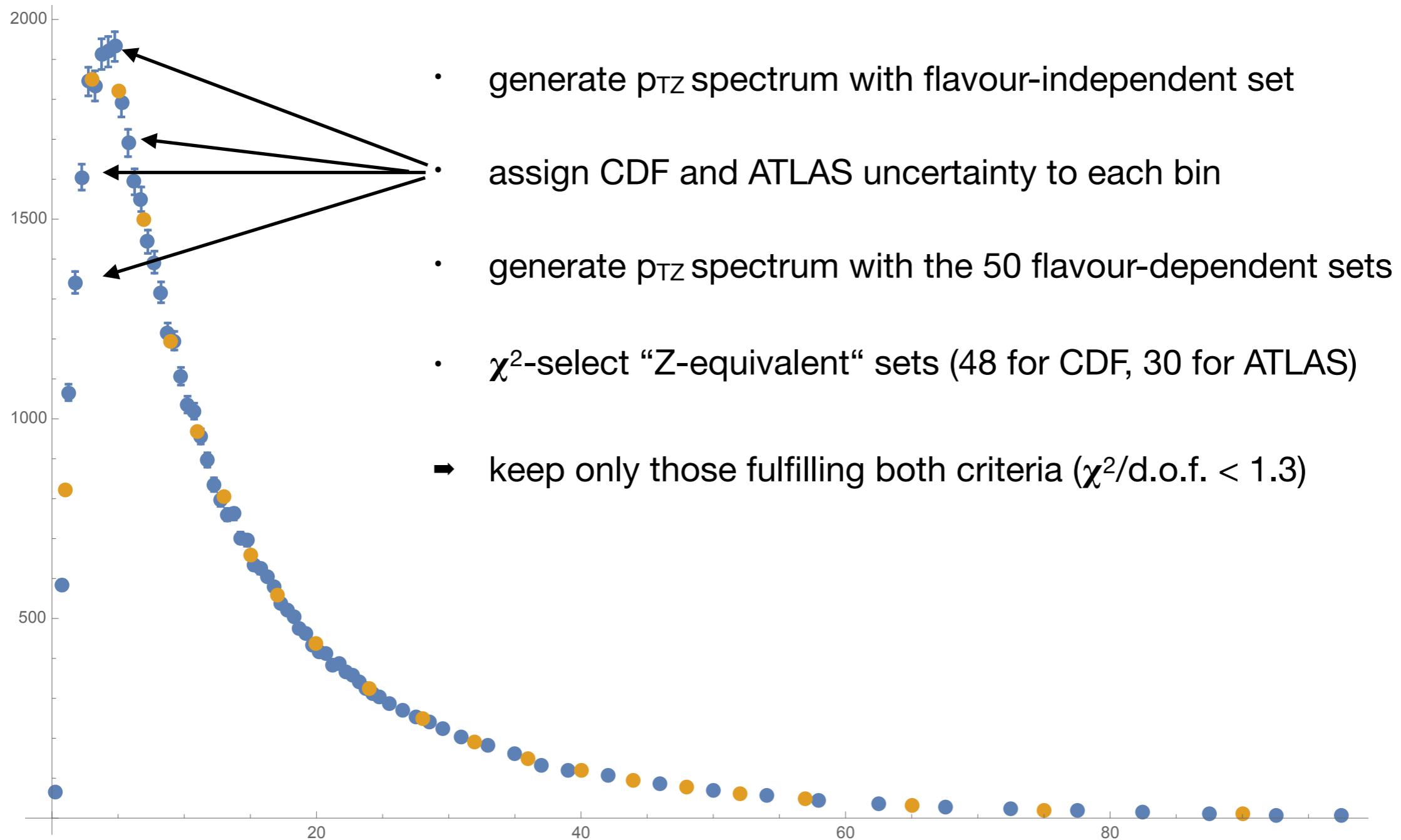
Fit to SIDIS/DY/Z data:  $g_{evo} \ln\left(\frac{Q^2}{Q_0^2}\right) \in [0.17, 0.39] \text{ GeV}^2$

[Bacchetta, Delcarro, Pisano, Radici, Signori (2017)]

We consider :

- **50 flavour-dependent sets**  $\{g_{NP}^{u_v}, g_{NP}^{d_v}, g_{NP}^{u_s}, g_{NP}^{d_s}, g_{NP}^s\}$  with  $g_{NP}^a \in [0.2, 0.6] \text{ GeV}^2$
- **1 flavour-independent set** with  $g_{NP}^a = 0.4 \text{ GeV}^2$

# “Z-equivalent” sets



NLL+LO QCD curves obtained through a modified version of the **DYqT** code [Bozzi, Catani, deFlorian, Ferrera, Grazzini (2009,2011)]  
(Tevatron 1.96 TeV & LHC 7 TeV)

# Impact on the determination of $M_W$

- Take the “Z-equivalent” *flavour-dependent* parameter sets and compute *low-statistics* (135M)  $m_T$  and  $p_{T\ell}$  distributions

➔ these are our **pseudodata**

- Take the *flavour-independent* parameter set and compute *high-statistics* (750M)  $m_T$  and  $p_{T\ell}$  distributions for 30 different values of  $M_W$

➔ these are our **templates**

- **perform the template fit procedure and compute the shifts induced by flavour effects**
- transverse mass: zero or few MeV shifts, generally favouring lower values for  $W^-$  (**preferred by EW fit**)
- lepton  $p_T$ : quite important shifts ( $W^+$  set 3: **9 MeV**, envelope: **up to 15 MeV**)

Set	$u_v$	$d_v$	$u_s$	$d_s$	$s$
1	0.34	0.26	0.46	0.59	0.32
2	0.34	0.46	0.56	0.32	0.51
3	0.55	0.34	0.33	0.55	0.30
4	0.53	0.49	0.37	0.22	0.52
5	0.42	0.38	0.29	0.57	0.27

	$\Delta M_{W^+}$		$\Delta M_{W^-}$	
Set	$m_T$	$p_{T\ell}$	$m_T$	$p_{T\ell}$
1	0	-1	-2	3
2	0	-6	-2	0
3	-1	9	-2	-4
4	0	0	-2	-4
5	0	4	-1	-3

NLL+LO QCD analysis obtained through a modified version of the **DYRes** code [Catani, deFlorian, Ferrera, Grazzini (2015)]  
(LHC 7 TeV, ATLAS acceptance cuts)

**Statistical uncertainty: 2.5 MeV**

Bacchetta, Bozzi, Radici, Ritzmann, Signori (arXiv:1807.02101)

# Outlook

- First flavour-dependent study of the impact of intrinsic transverse momentum on the determination of the  $W$  mass
- Flavour effects are both important and detectable: no “flavour-blind” analysis allowed
- Future: possible flavour effects on  $W$  mass at LHCb, on CC/NC ratios (i.e.,  $pt_W/pt_Z$ ), ...