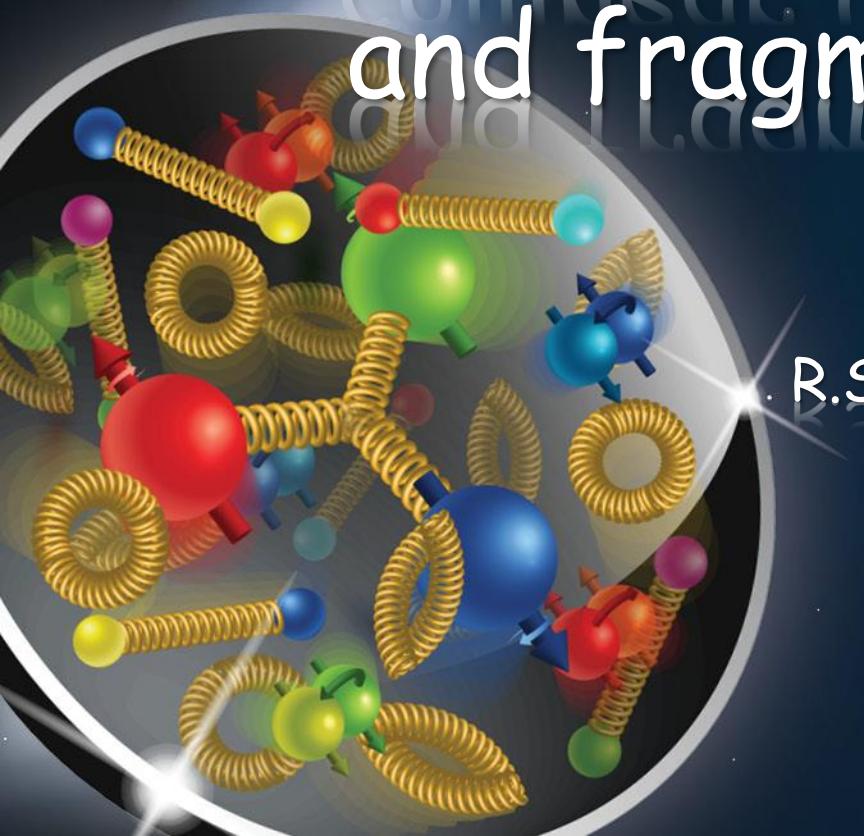


EIC

collinear (un)-polarized PDFs and fragmentation functions



I. Borsa, X. Chu, Ch. van Hulse,
R. Sassot, H. Spiesberger, M. Stratmann,
K. Wichmann, E.C. Aschenauer

Electron Ion Collider

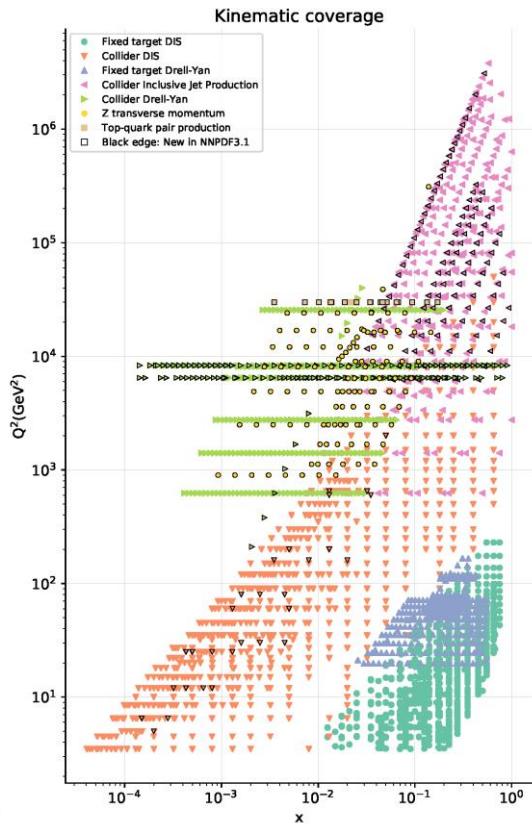
The inner life of hadrons

Parton distribution functions

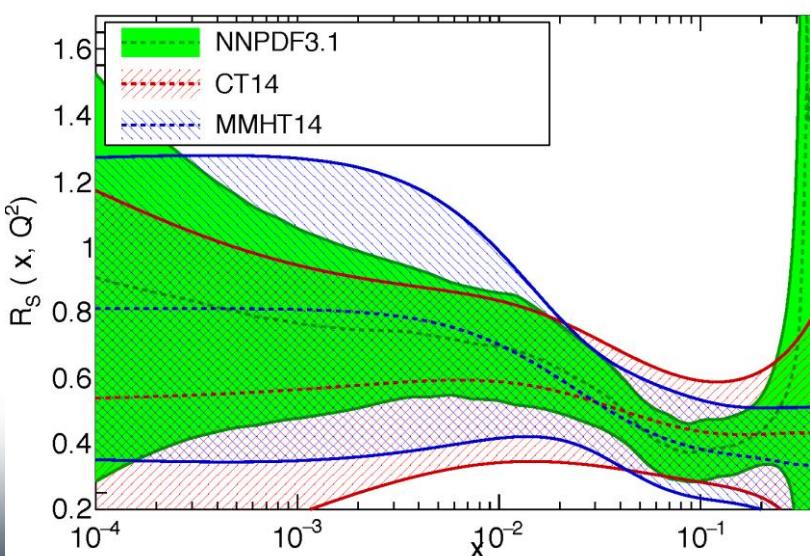
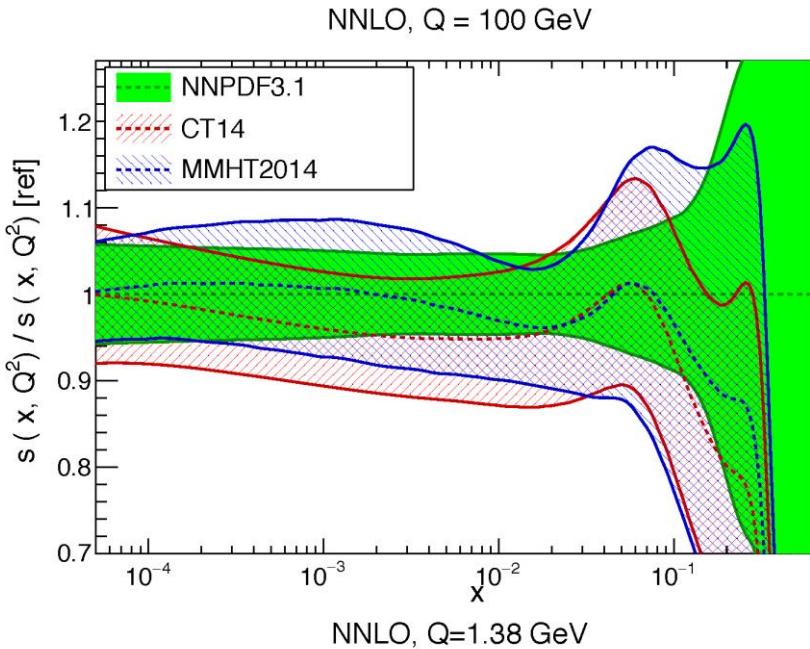
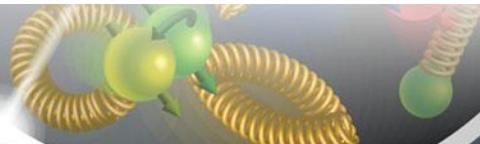


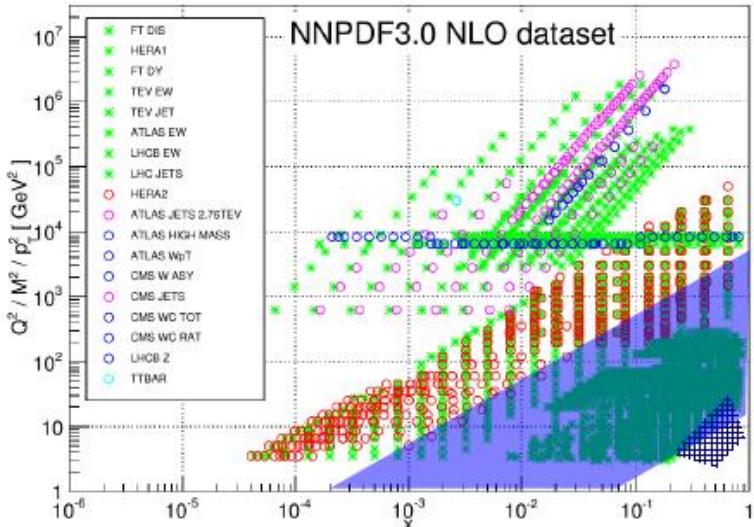
s(x) and sbar(x) where do we stand?

NNPDF 3.1 arXiv:1706.00428

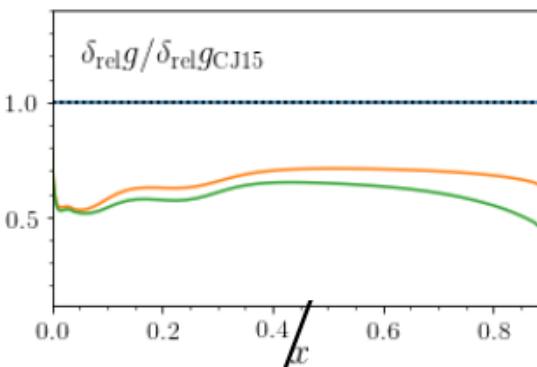
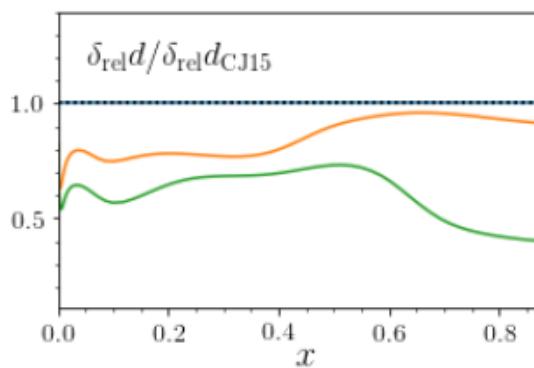
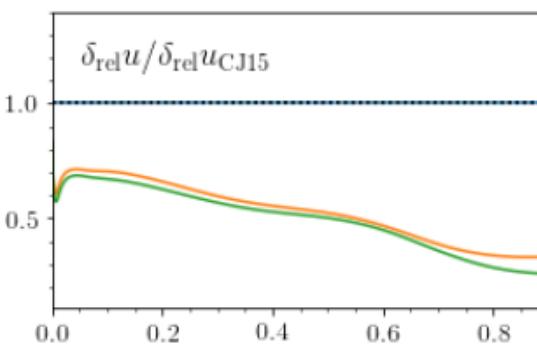
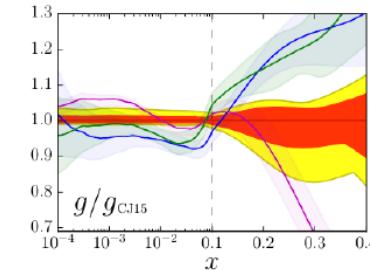
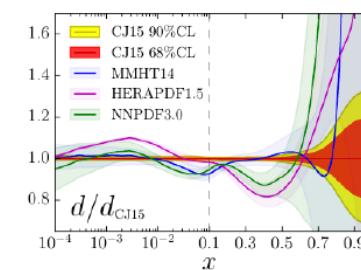
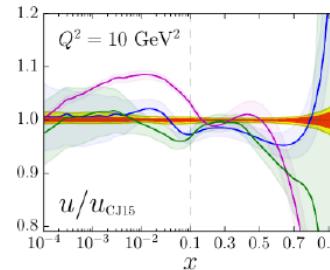


$$r_s(x, Q^2) = \frac{s(x, Q^2) + \bar{s}(x, Q^2)}{\bar{d}(x, Q^2) + \bar{u}(x, Q^2)}.$$





Baseline: CJ-15



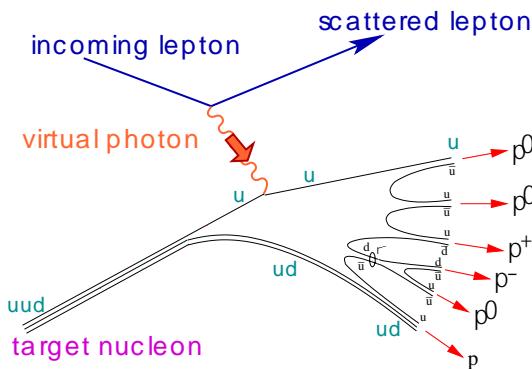
Relative error improvement:

- pseudo-data for $0.01 < x < 0.9$
- NC Cross sections on proton target
- F_2^n from deuterium with tagged proton spectator
- $10 \times 100 \text{ GeV}^2$ at 100 fb^{-1} ,
- energy scan $\sqrt{s} = 57, 49, 28 \text{ GeV}$ at 10 fb^{-1}

→ more studies in progress

HOW TO ACCESS SEA QUARKS IN DIS

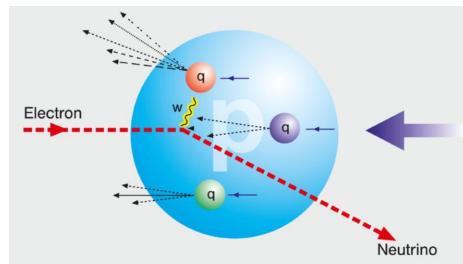
SIDIS:



Detect identified hadrons in coincidence to scattered lepton

- needs fragmentation functions to correlate hadron type with parton
- Detector: PID over a wide range of η

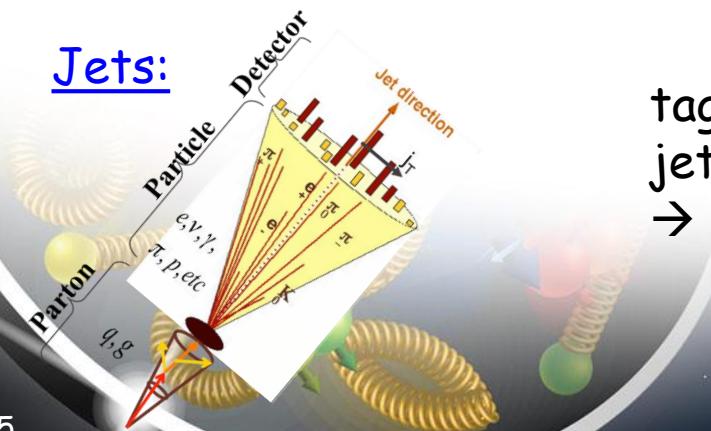
Charge Current:



W-exchange: direct access to the quark flavor
no FF - complementary to SIDIS

- Detector: large rapidity coverage and large \sqrt{s}

Jets:



tag sea-quarks through the sub-processes and jet substructure

- Detector: large rapidity coverage and PID

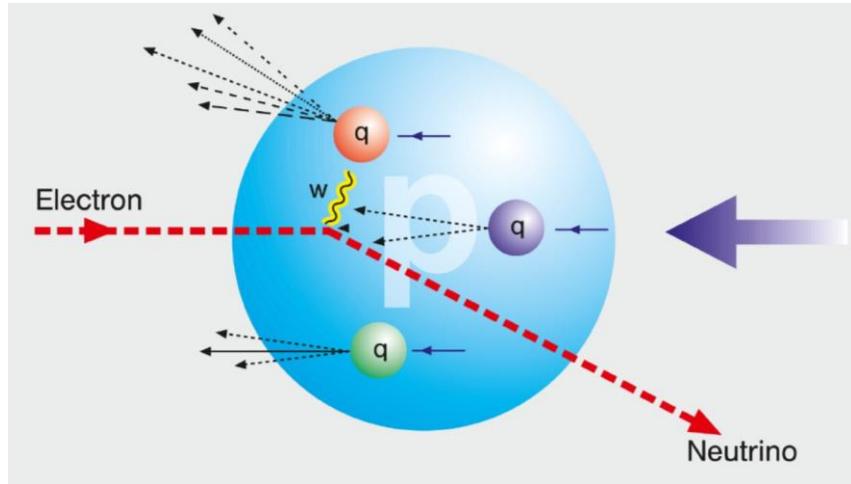
Observables: Charge Current in ep and eA

W-exchange:
direct access to the quark flavor

Ws are maximally parity violating
→ Ws couple only to one parton helicity

$$W^- + p \rightarrow u\bar{d}$$

$$W^- + n \rightarrow d\bar{u}$$



Complementary to SIDIS:

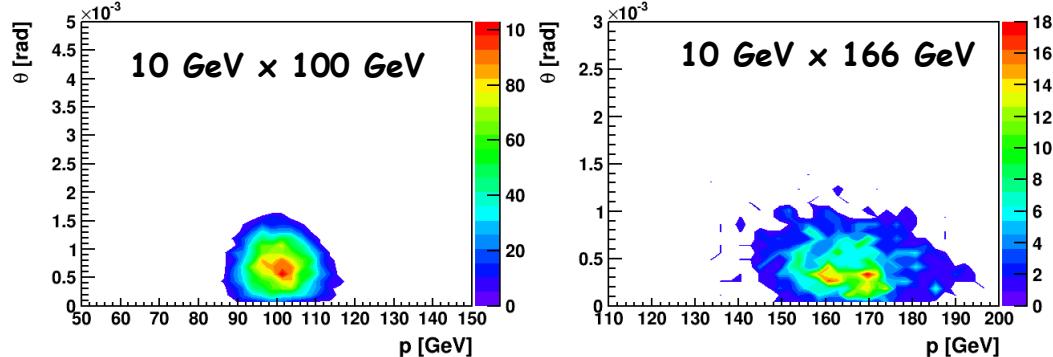
- high Q²-scale: > 100 GeV²
 - best way to measure at very high x
 - extremely clean theoretically
 - No Fragmentation function
- stringent test on theory approach for SIDIS

UNIVERSALITY of PDFs

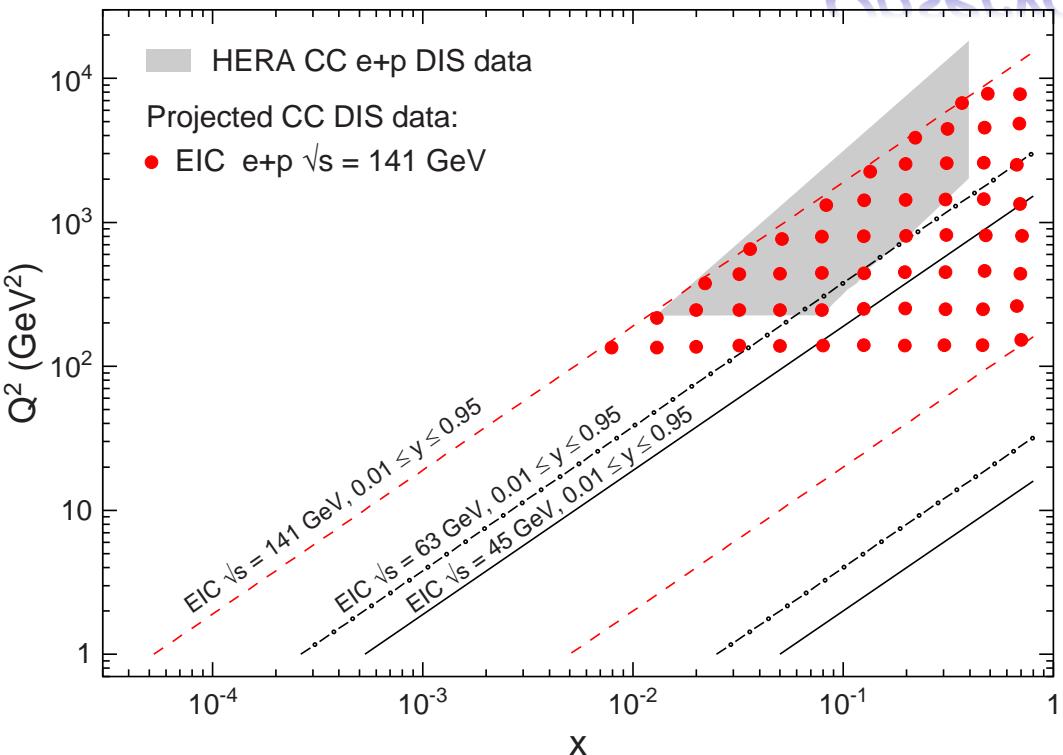
EIC:
first time charge current physics
in polarized ep and eA collisions

effective neutron target:
(un)polarized Deuterium or /and He-3
through tagging the spectator proton(s)

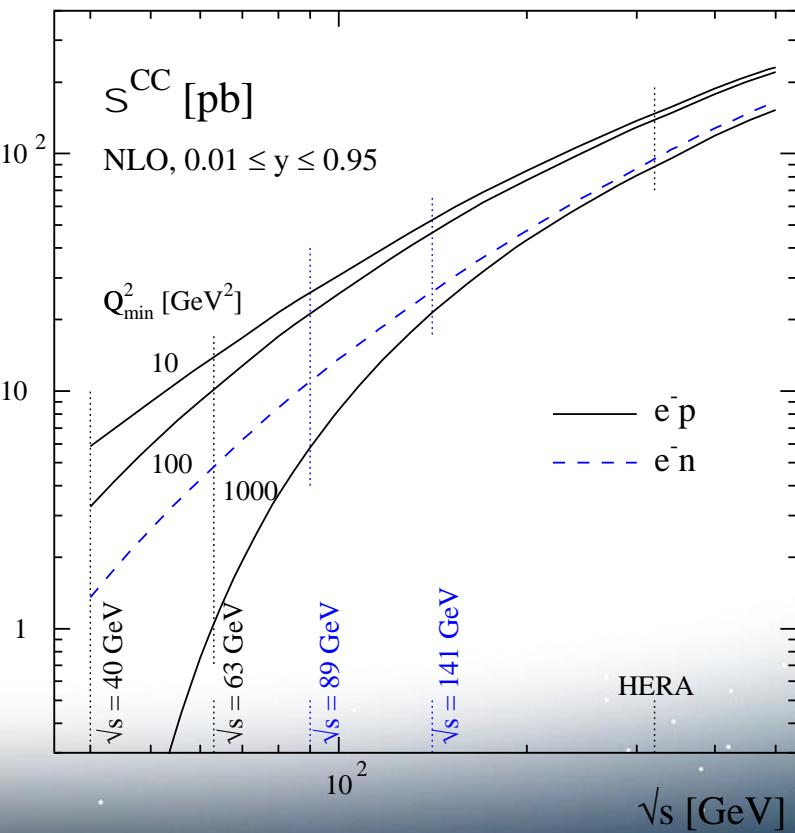
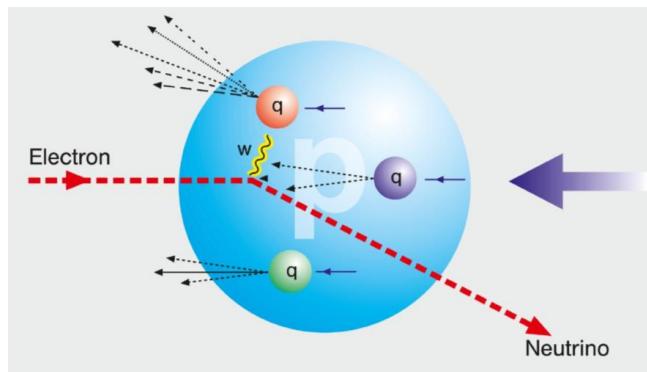
Deuterium spectator protons: He-3 spectator protons:



Observables: Charge Current in ep



EIC has a large kinematic coverage for charge current events (○)



Observables: Charge Current in ep and eA

Just some of the physics opportunities:

polarized ep/en:

- test models based on helicity retention $\Delta d/d \rightarrow 1$
(Phys.Rev.Lett. 99 (2007) 082001)
- precision test models assuming charge symmetry violation
- precision test hardness of W_s
- tag charm in coincidence with CC event $\rightarrow \Delta s$

unpolarized ep/en:

- impact on PDFs \rightarrow high x quark PDFs
 - tag charm in coincidence ot CC event $\rightarrow s$
- precision constrain on light quark weak neutral current couplings a_u, v_u, a_d, v_d

unpolarized eA:

- Test Models for the EMC-effect
 - charge symmetry violation
 - Isovector EMC effect

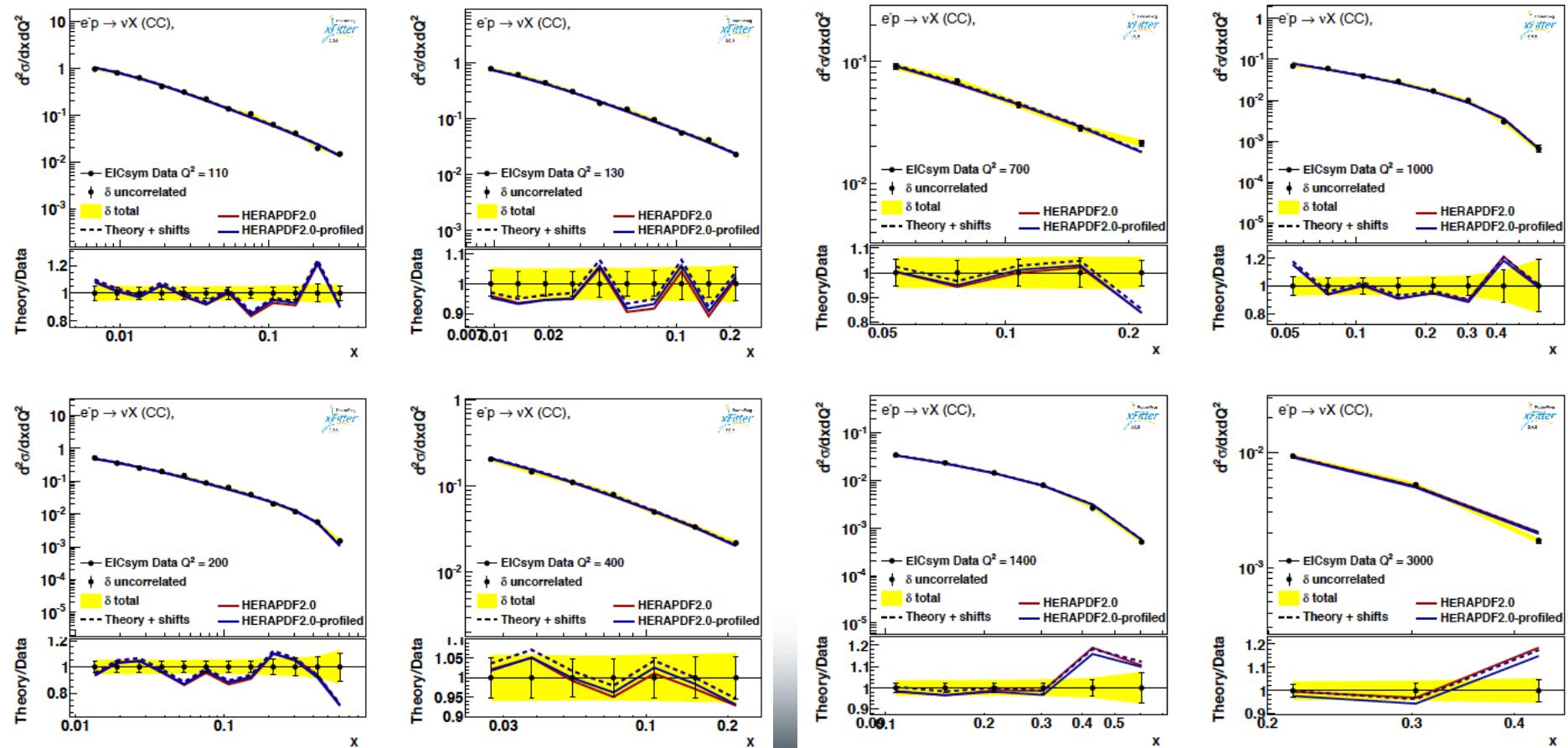
(Cloet, Bentz, Thomas et. al., PRL 102 252301)

CC@EIC: Impact on PDFs

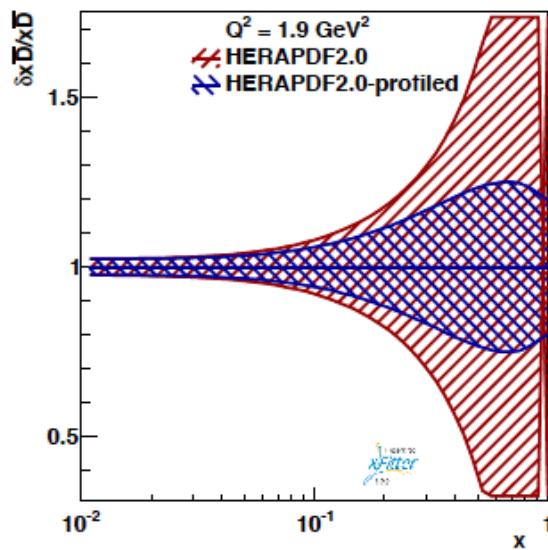
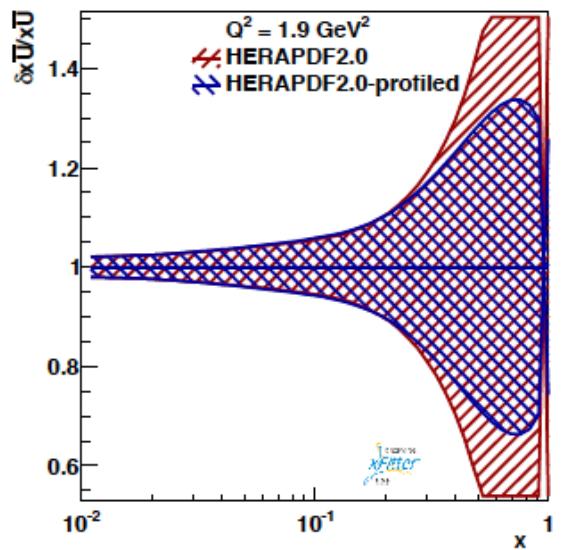
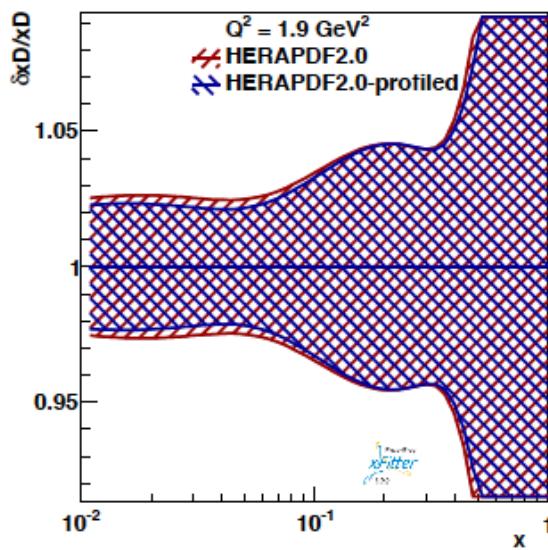
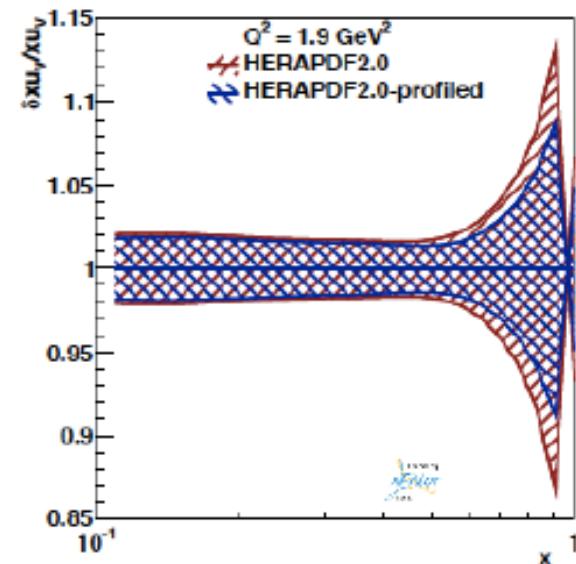
Generated 10 fb^{-1} worth of ep CC events with DJANGOH for 20 GeV \times 250 GeV



is used to get the impact on PDFs
good agreement between pseudo-data and prediction



Impact of CC@EIC to PDFs



$$xU = xu + xc$$

$$xD = xd + xs$$

$$x\bar{U} = x\bar{u} + x\bar{c}$$

$$x\bar{D} = x\bar{d} + x\bar{s}$$

$$xu_v = xU - x\bar{U}$$

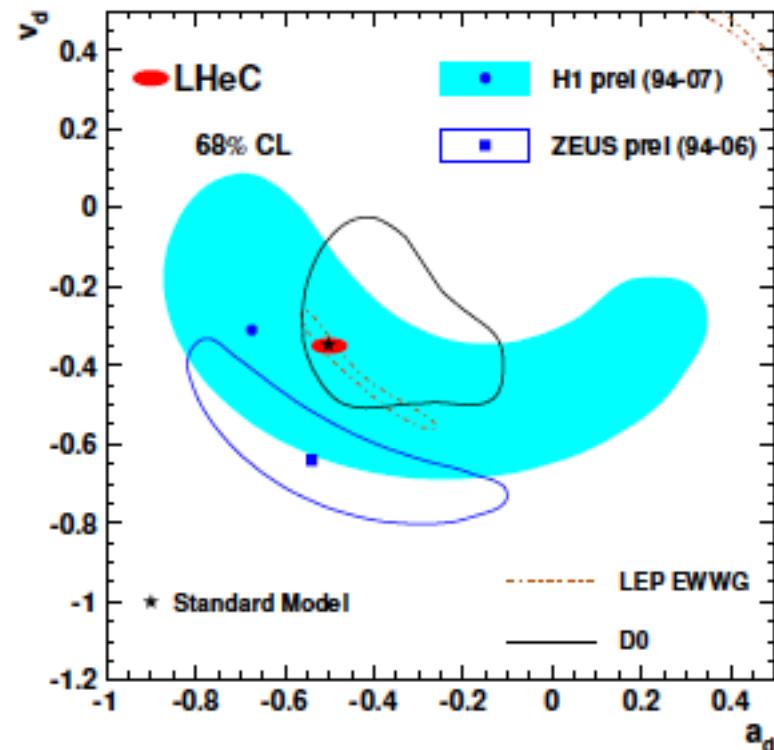
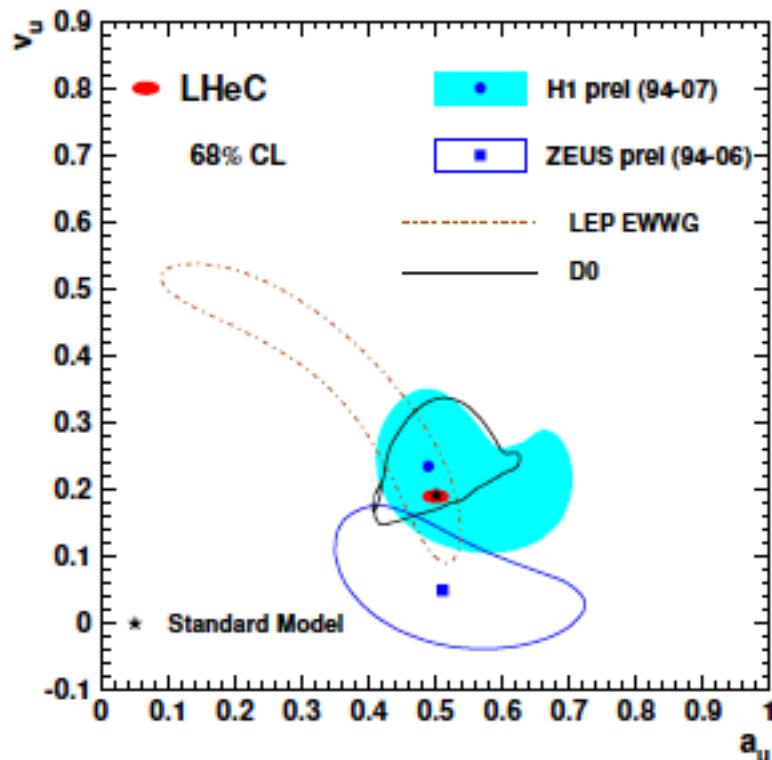
$$xd_v = xD - x\bar{D}$$

Very strong impact on $x\bar{D}$
significant impact on xu_v ,
Need to still understand in
detail why there is impact on
 $x\bar{U}$

→ very promising first results

What can an EIC Do?

Should study what NC and CC cross sections at EIC can tell us on the vector and axial-vector weak neutral current couplings



What can SIDIS@EIC Teach us

Cuts:

$Q^2 > 1 \text{ GeV}^2$ $0.1 < y < 0.95$ $W^2 > 10 \text{ GeV}^2$ $p_T > 0.2 \text{ GeV}$

PID:

-3.5 < rapidity < -1 RICH:
-1.5 < rapidity < -1 dE/dx

pi:
 $0.5 < p < 5 \text{ GeV}$
 $0.2 < p < 0.6 \text{ GeV}$

K:
 $1.6 < p < 5 \text{ GeV}$
 $0.2 < p < 0.6 \text{ GeV}$

p:
 $3 < p < 8 \text{ GeV}$
 $0.2 < p < 1.0 \text{ GeV}$

-1 < rapidity < 1 : dE/dx & DIRC:

$0.2 < p < 4 \text{ GeV}$

$0.2 < p < 0.7 \text{ & } 0.8 < p < 4 \text{ GeV}$

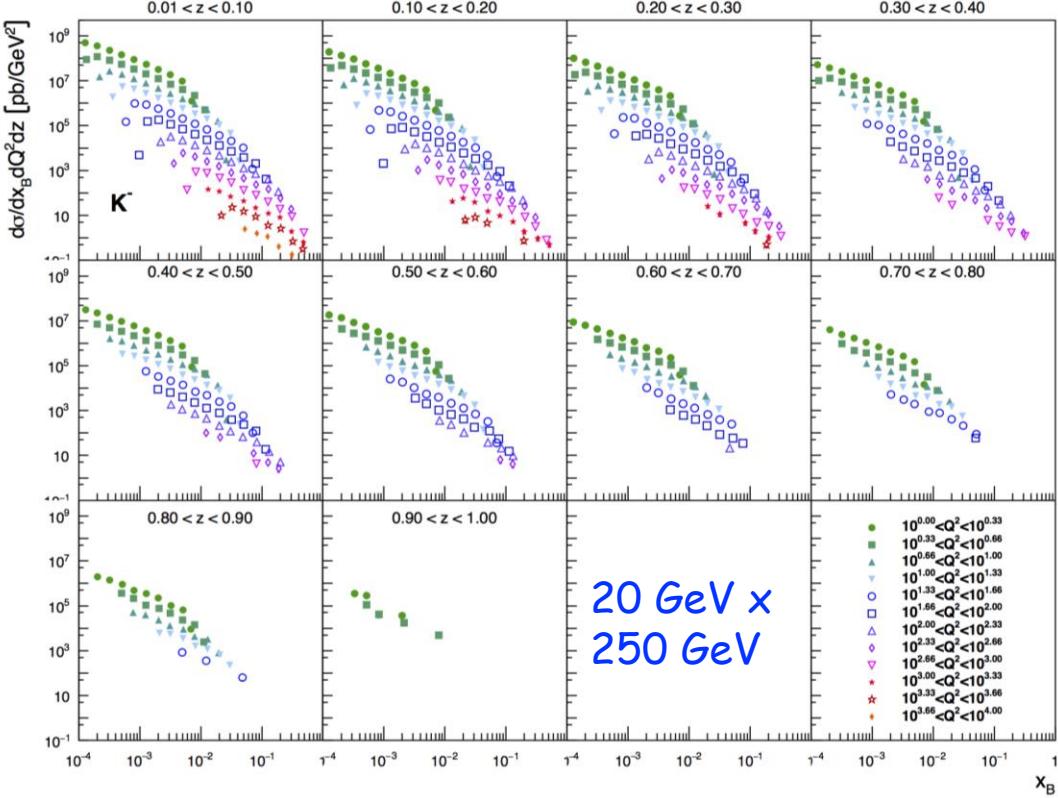
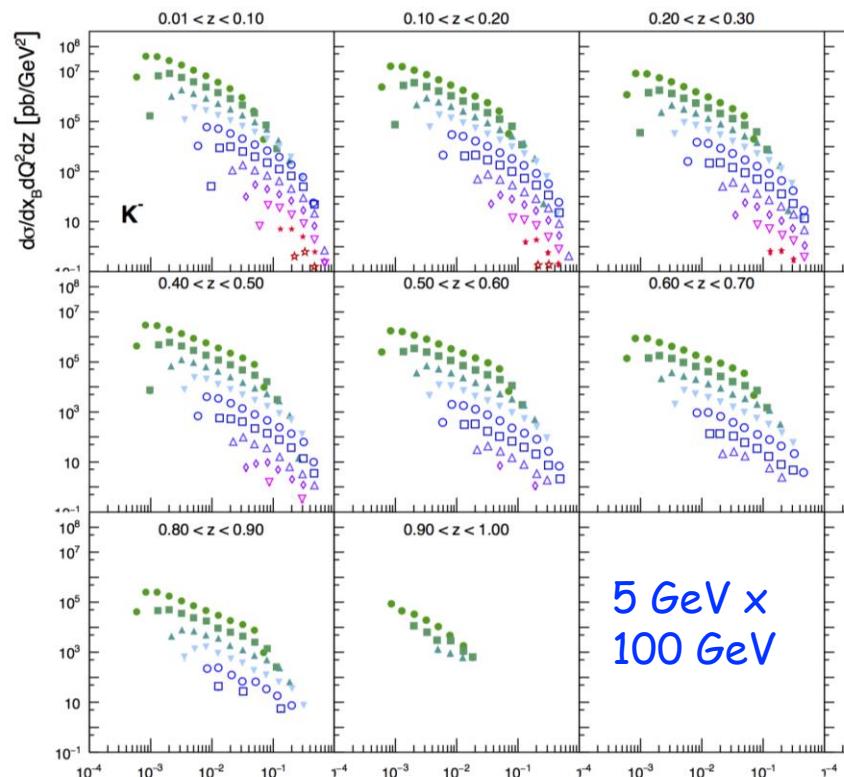
$0.2 < p < 1.1 \text{ & } 1.5 < p < 4 \text{ GeV}$

1 < rapidity < 3.5 RICH
1 < rapidity < 1.5 dE/dx

$0.5 < p < 50 \text{ GeV}$
 $0.2 < p < 0.6 \text{ GeV}$

$1.6 < p < 50 \text{ GeV}$
 $0.2 < p < 0.6 \text{ GeV}$

$3 < p < 50 \text{ GeV}$
 $0.2 < p < 1.0 \text{ GeV}$



PDFs: flavor separation from SIDIS@EIC

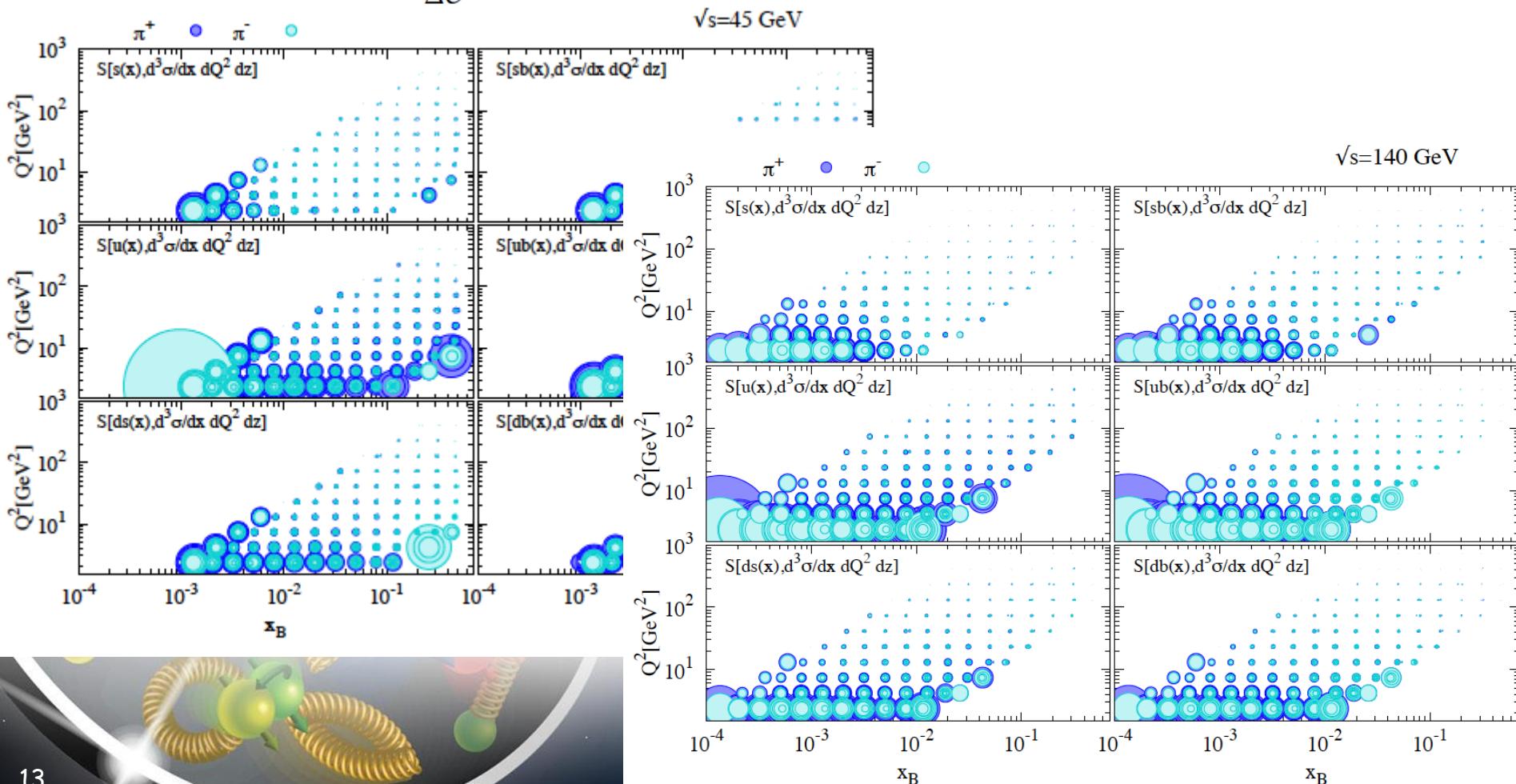
Use reweighting method to define EIC SIDIS data impact on collinear unpolarized PDFs and Fragmentation functions

Correlation factor of observable \mathcal{O} to a flavor i

$$\rho[f_i, \mathcal{O}] = \frac{\langle \mathcal{O} \cdot f_i \rangle - \langle \mathcal{O} \rangle \langle f_i \rangle}{\Delta \mathcal{O} \Delta f_i}, \xrightarrow[\xi \equiv \frac{\delta \mathcal{O}}{\Delta \mathcal{O}}]{\text{account for uncertainties}} S[f_i, \mathcal{O}] = \frac{\langle \mathcal{O} \cdot f_i \rangle - \langle \mathcal{O} \rangle \langle f_i \rangle}{\xi \Delta \mathcal{O} \Delta f_i},$$

$\delta \mathcal{O}$: exp. uncertainty
Observable

Δ PDF in Observable



PDFs: flavor separation from SIDIS@EIC

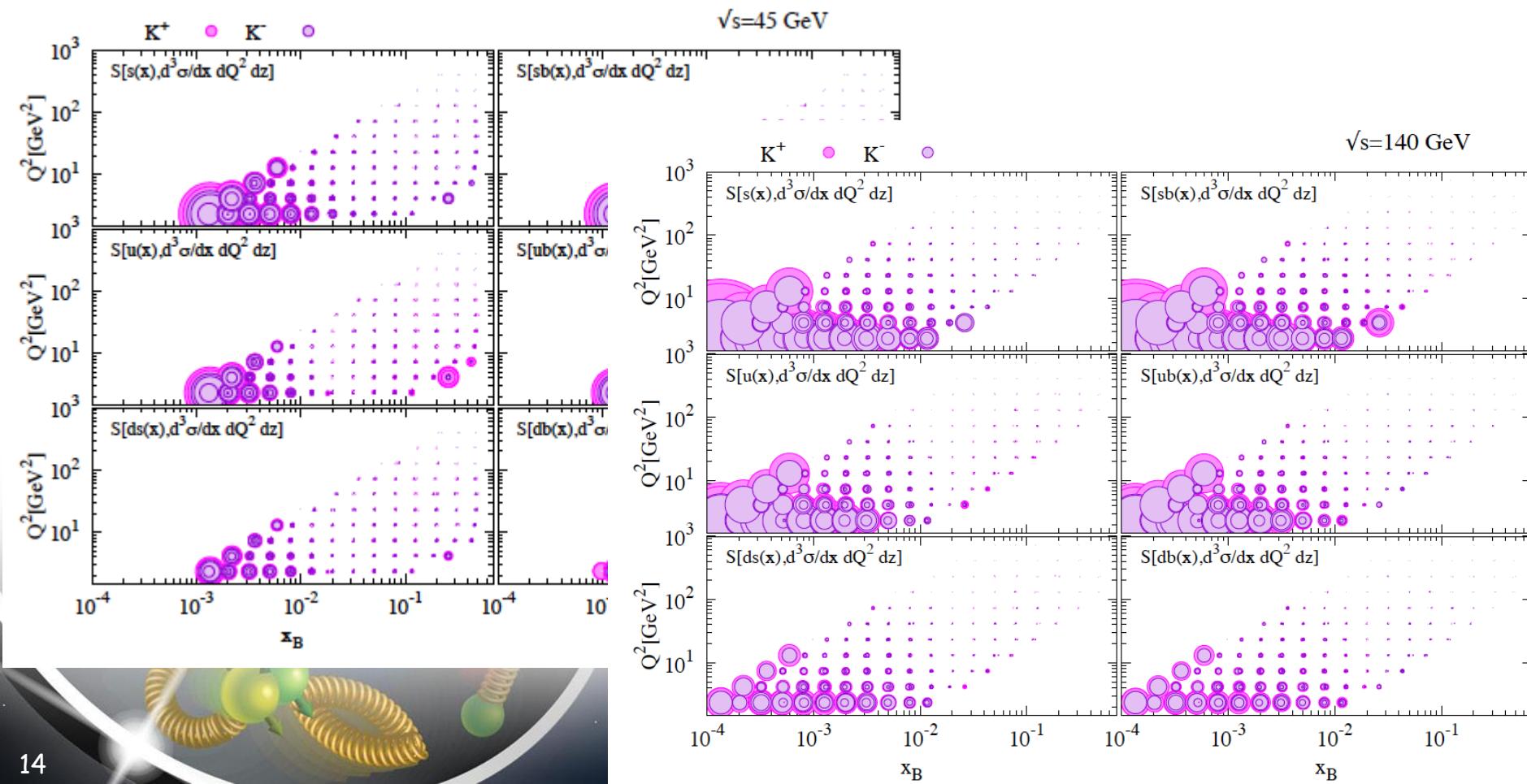
Use reweighting method to define EIC SIDIS data impact on collinear unpolarized PDFs and Fragmentation functions

Correlation factor of observable \mathcal{O} to a flavor i

$$\rho[f_i, \mathcal{O}] = \frac{\langle \mathcal{O} \cdot f_i \rangle - \langle \mathcal{O} \rangle \langle f_i \rangle}{\Delta \mathcal{O} \Delta f_i}, \xrightarrow[\xi \equiv \frac{\delta \mathcal{O}}{\Delta \mathcal{O}}]{\text{account for uncertainties}} S[f_i, \mathcal{O}] = \frac{\langle \mathcal{O} \cdot f_i \rangle - \langle \mathcal{O} \rangle \langle f_i \rangle}{\xi \Delta \mathcal{O} \Delta f_i},$$

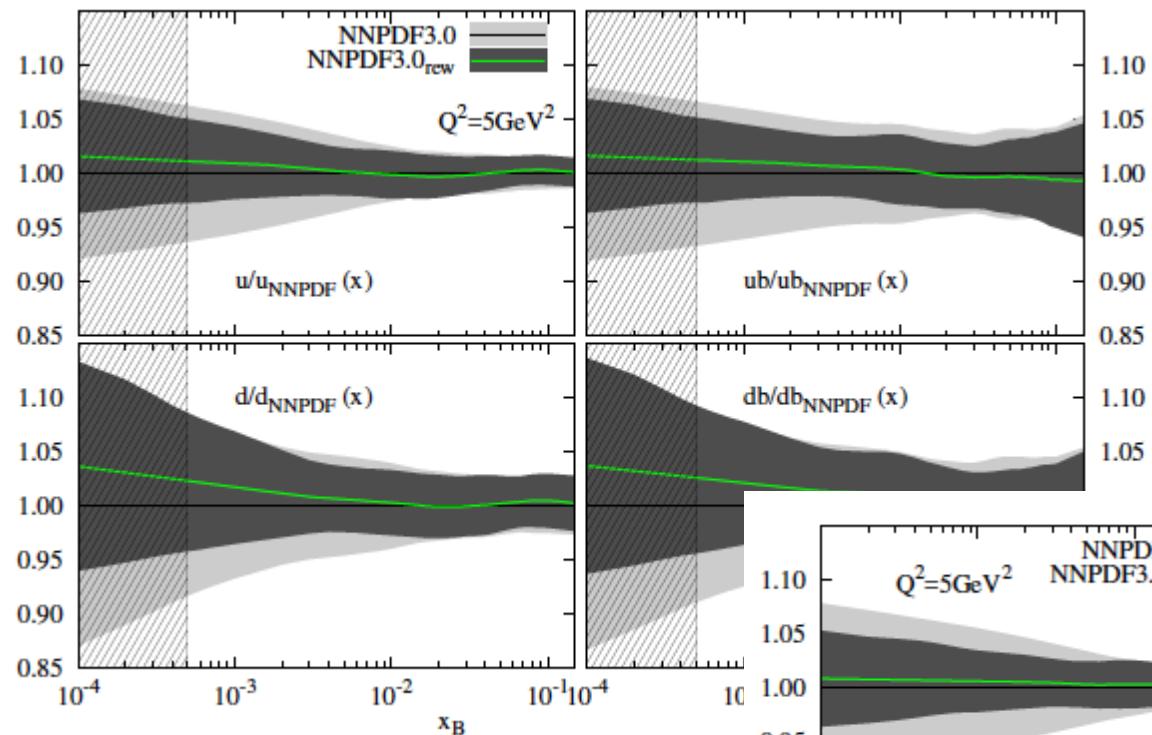
$\delta \mathcal{O}$: exp. uncertainty
Observable

Δ PDF in Observable

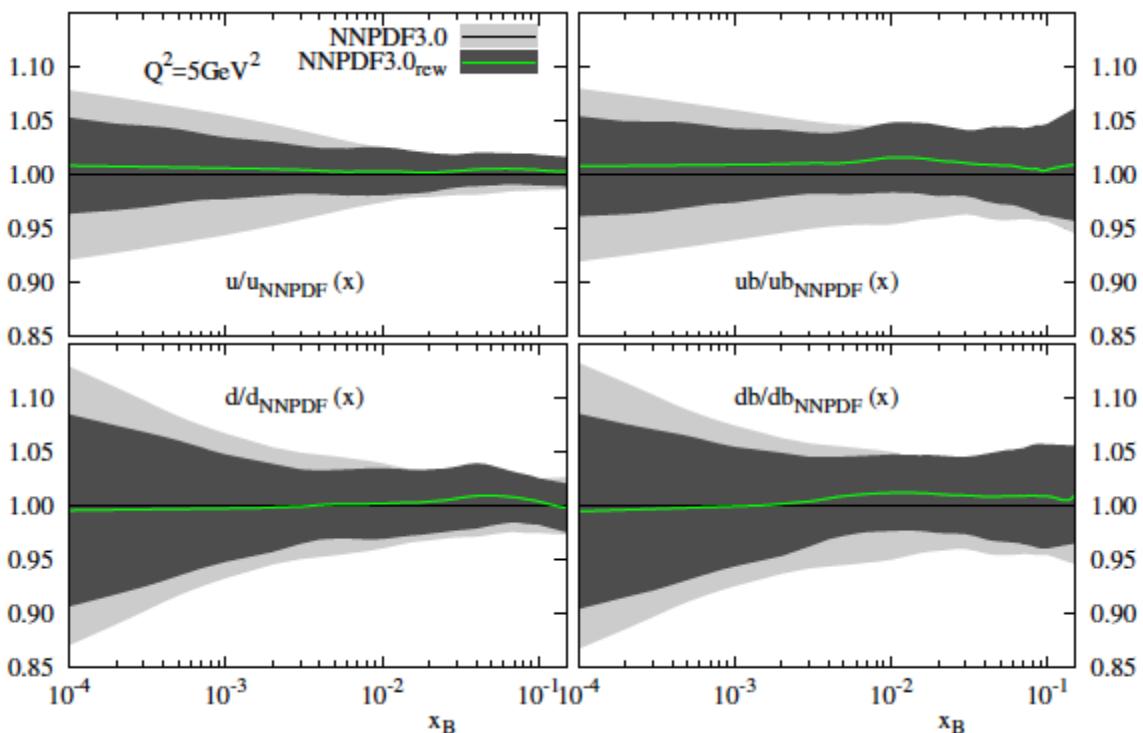


PDF Constrain from SIDIS@EIC

$\sqrt{s}=45 \text{ GeV}$



$\sqrt{s}=145 \text{ GeV}$

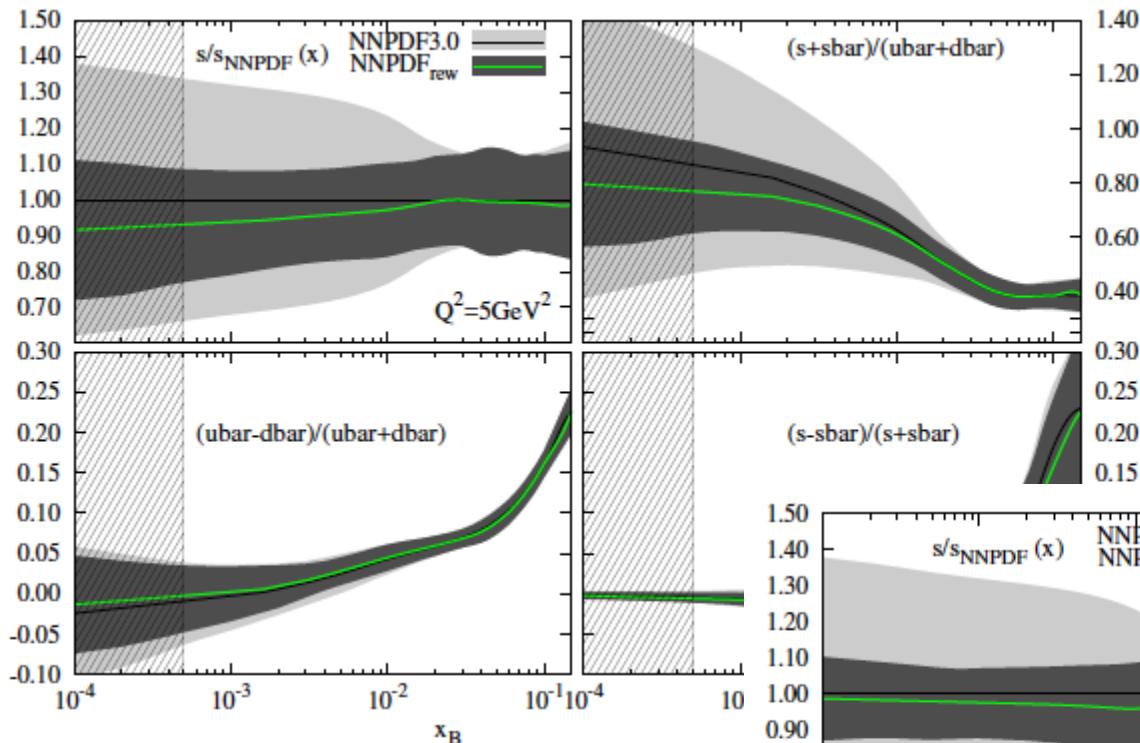


Impressive constrain of
light quarks for $x < 0.1$
need to investigate $x > 0.1$ more
→ impact grows with \sqrt{s}

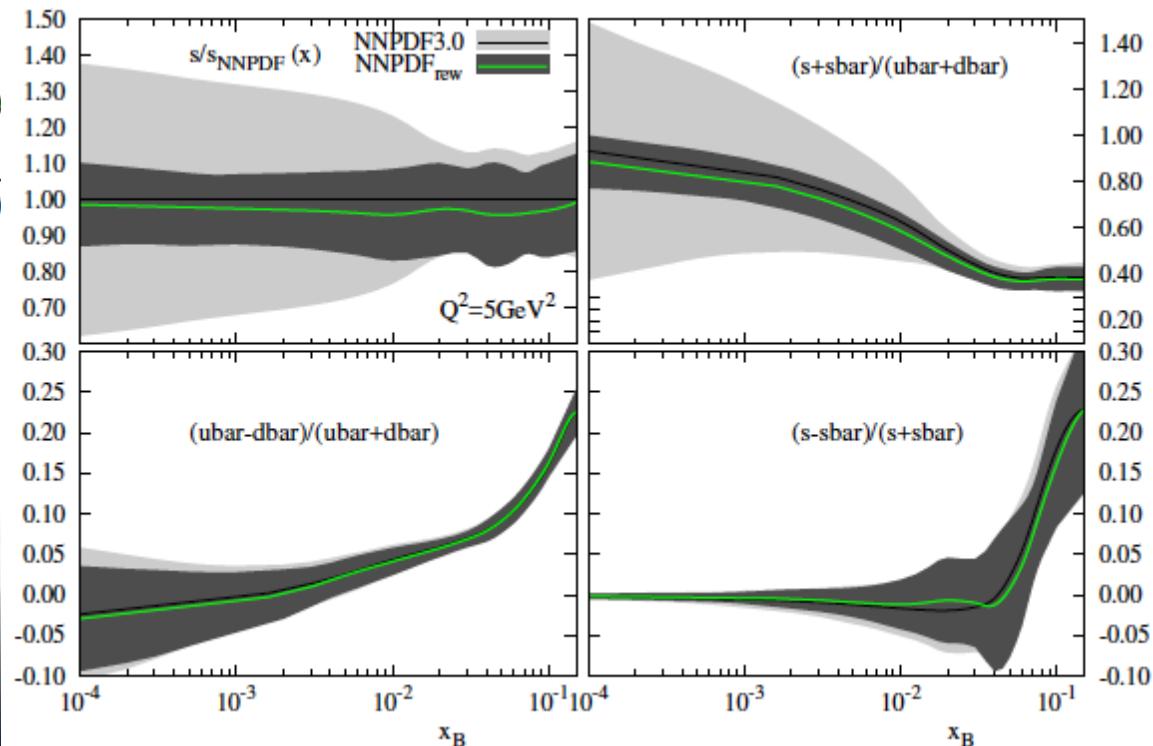


PDF Constrain from SIDIS@EIC

$\sqrt{s}=45 \text{ GeV}$



$\sqrt{s}=145 \text{ GeV}$

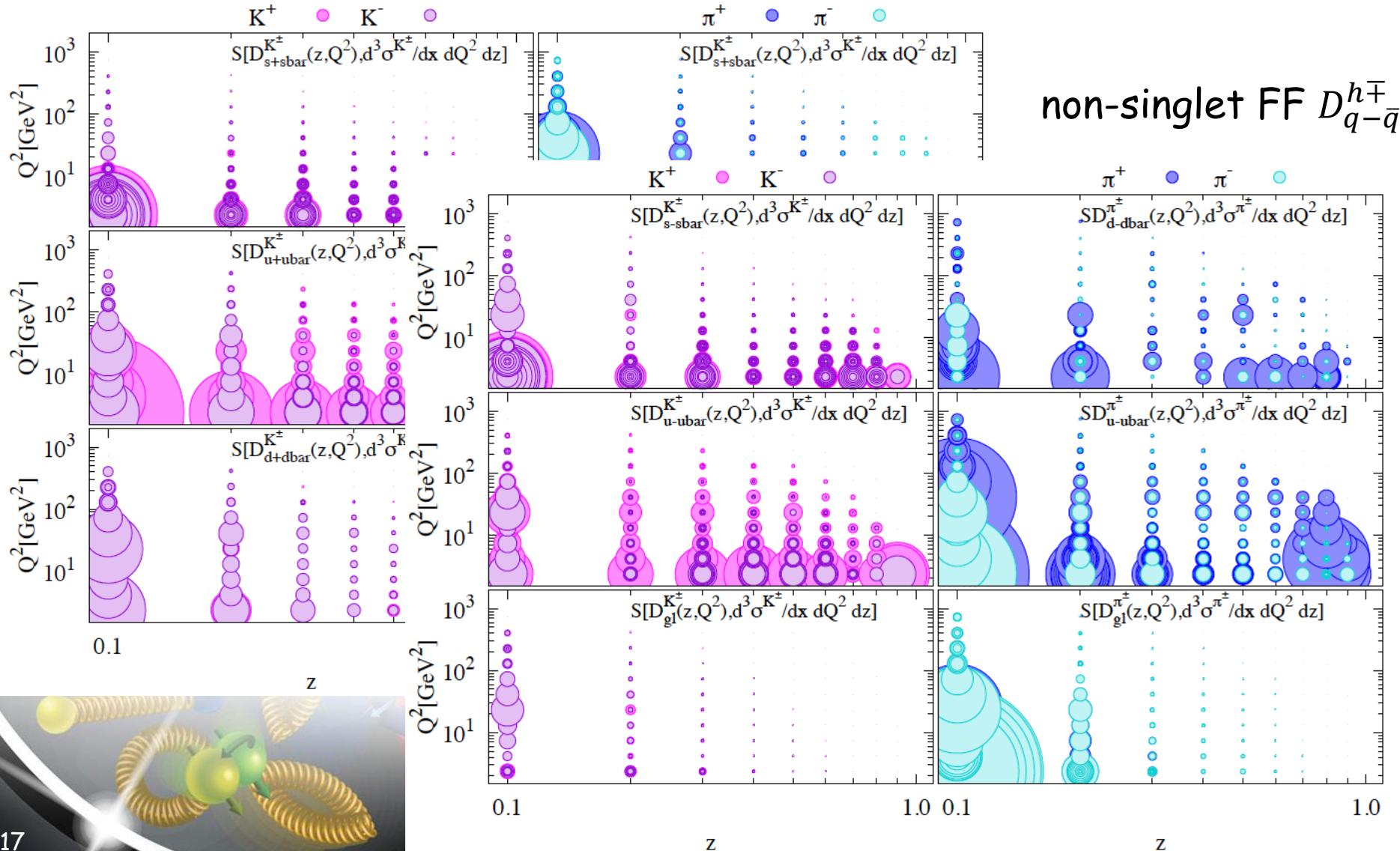


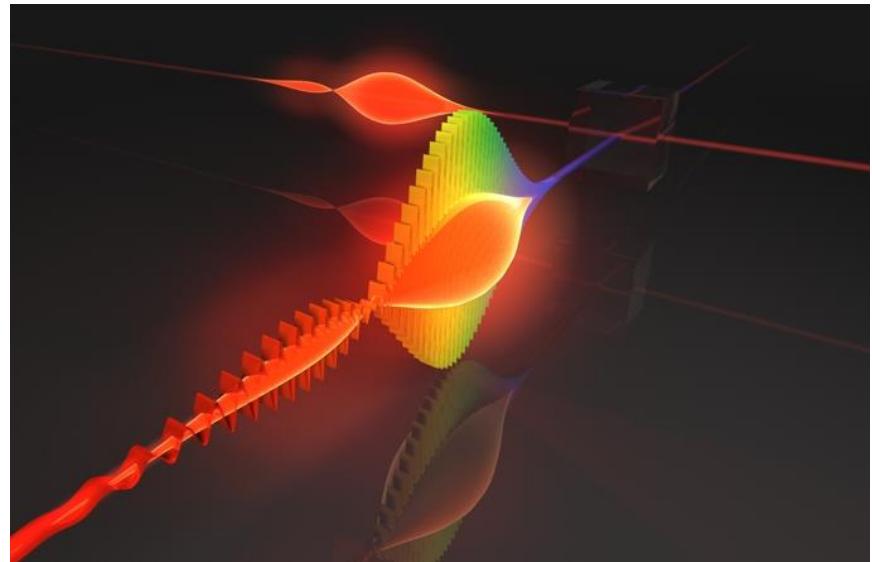
If you want to know
s-PDF ask the EIC
→ impact grows with \sqrt{s}

FF Constrain from SIDIS@EIC

Utilize the same method as for PDFs

singlet FF $D_{q+\bar{q}}^{h\mp}$



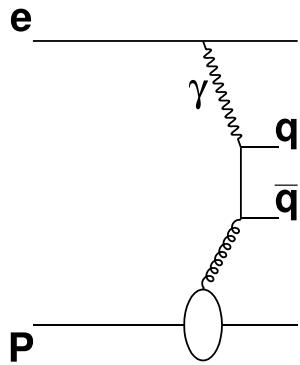


Example for Jet Physics at an EIC: Unpolarized and polarized photon structure

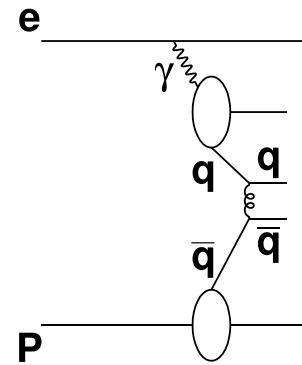
Details: X. Chu, ECA arXiv:1705.08831

Photon Parton Structure

In high energy $e\gamma$ collision, two types of processes lead to the production of di-jets:



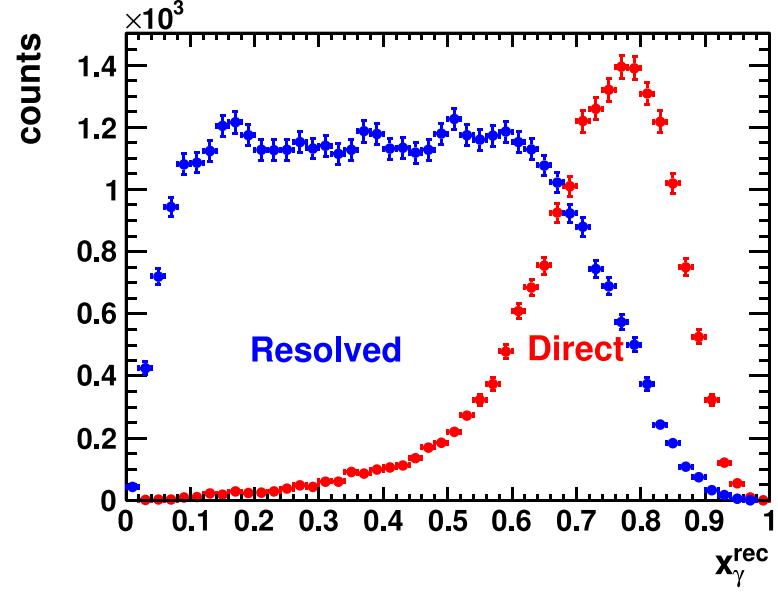
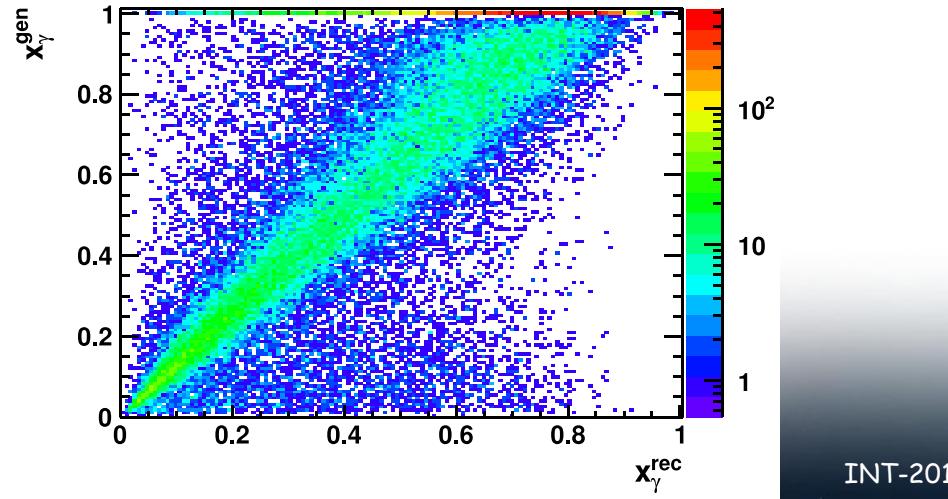
direct: point-like photon



resolved: hadronic photon

- Di-jets@EIC ideal probe to constrain (un)polarised Photon-PDFs
 - Direct/resolved contributions can be separated reconstructing x_γ

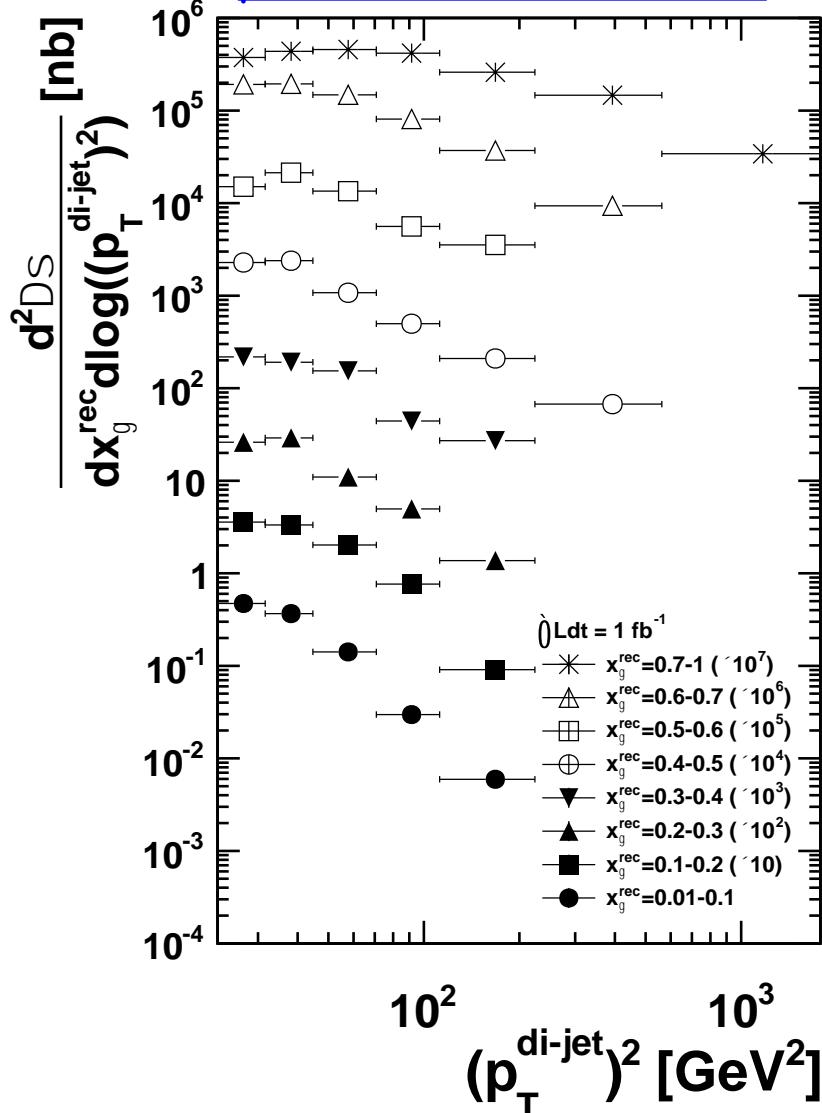
$$x_\gamma^{rec} = \frac{1}{2E_e y} (p_{T1} e^{-\eta_1} + p_{T2} e^{-\eta_2})$$



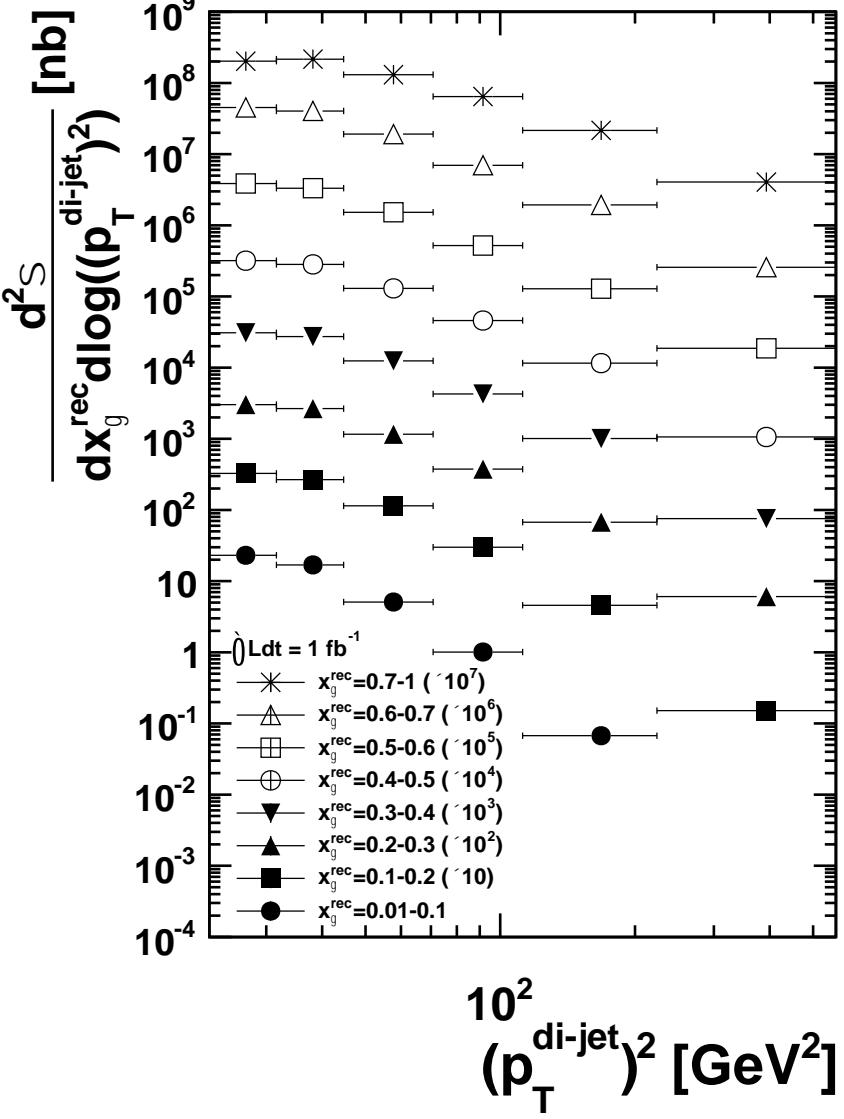
Aschenauer

Photon Parton Structure

polarized cross section:



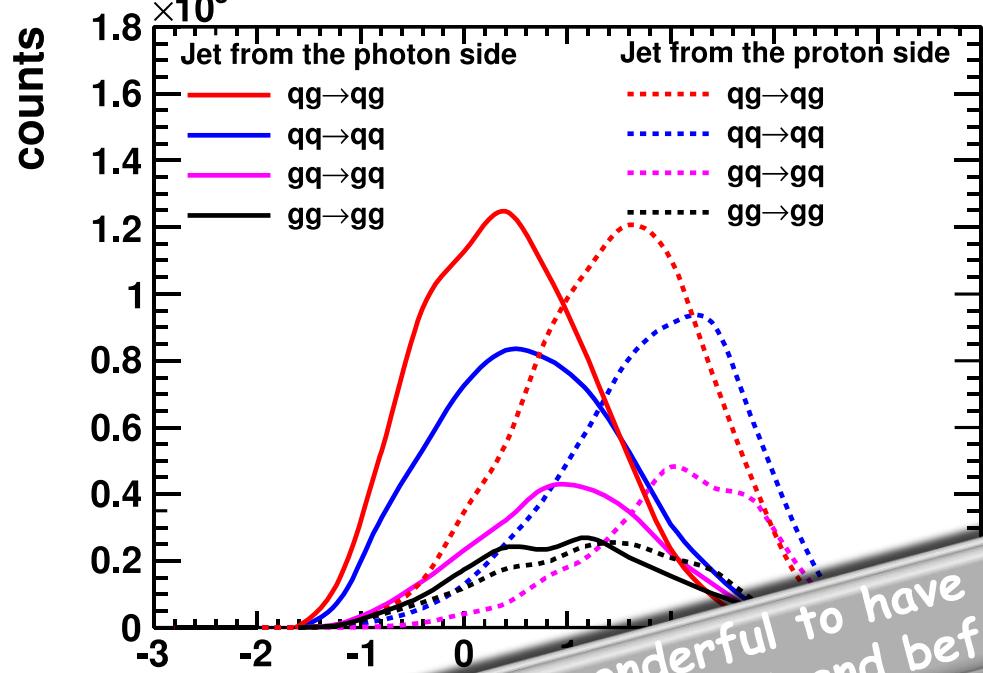
unpolarized cross section:



Input: proton-CTEQ-5 & g : SAS

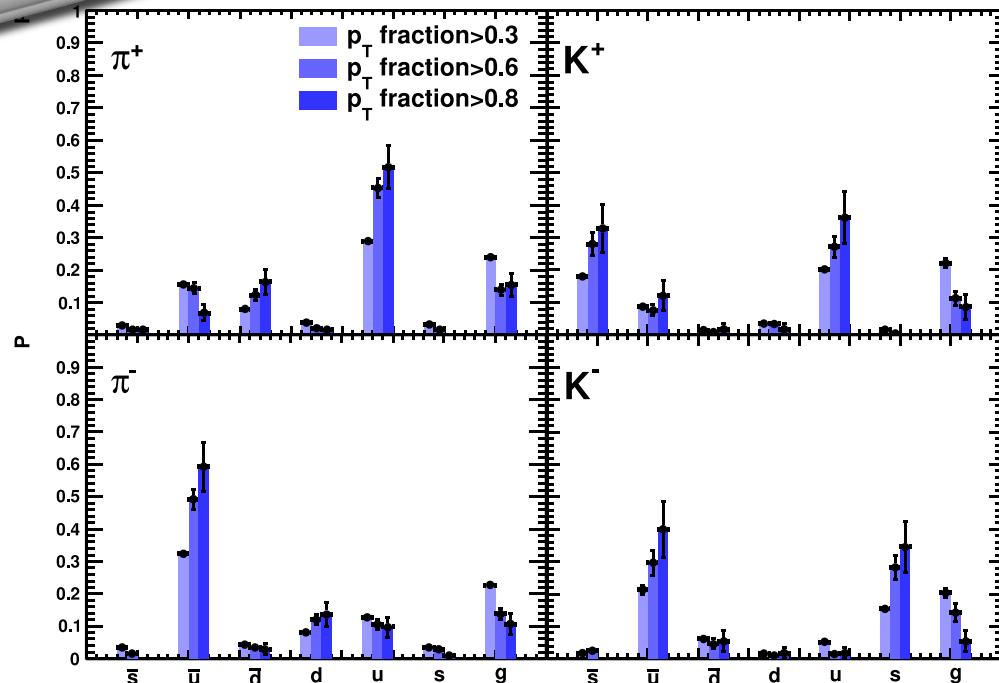
Input: proton-DSSV &
 γ : PLB 337 373 (1994)

Photon Parton Structure

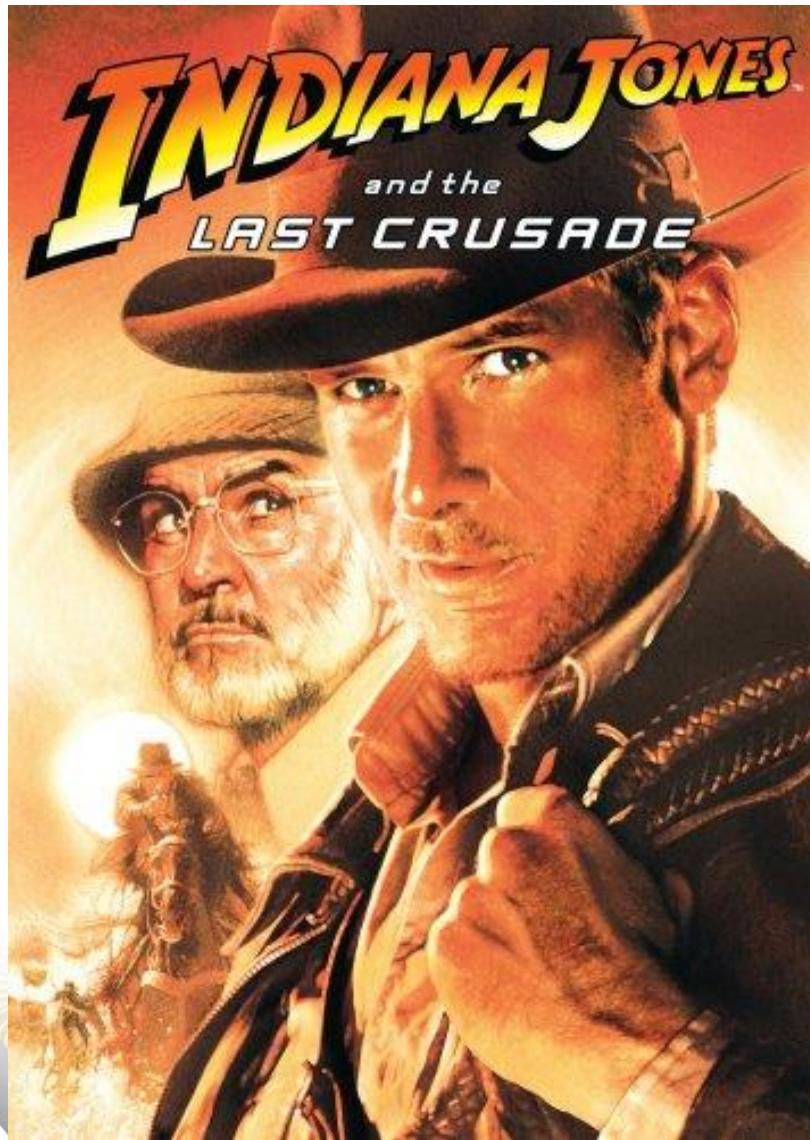


It would be wonderful to have unpolarised photon PDFs with all data (LEP & HERA and before) fitted with uncertainties

identified hadron tagging in jet enhances flavor sensitivity



What else can be done



The Holy Grail

Why should we care?

Spin ideal tool to understand the dynamics of sea quarks and gluons inside the hadron

Despite decades of QCD - Spin one of the least understood quantities

→ Consequence very few models, but several physics pictures, which can be tested with high precision data

□ the pion/kaon cloud model

- rooted in deeper concepts → chiral symmetry
- generated q-qbar pairs (sea quarks) at small(ish)-x are predicted to be unpolarized
- gluons if generated from sea quarks unpolarised → spatial imaging
- a high precision measurement of the flavor separated polarized quark and gluon distributions as fct. of x is a stringent way to test.

□ the chiral quark-soliton model

- sea quarks are generated from a "Dirac sea" with a rich dynamical structure but excludes gluons at its starting scale
- sea quarks are polarized → asymmetry $\Delta\bar{u} \neq \Delta\bar{d}$
- a high precision measurement of the flavor separated polarized quark as fct. of x is a stringent way to test

□ stringent test of lattice calculations

- the relative importance of lattice graphs
- probe quark is connected to the proton wave function or is created from the 'gluon soup' inside the proton

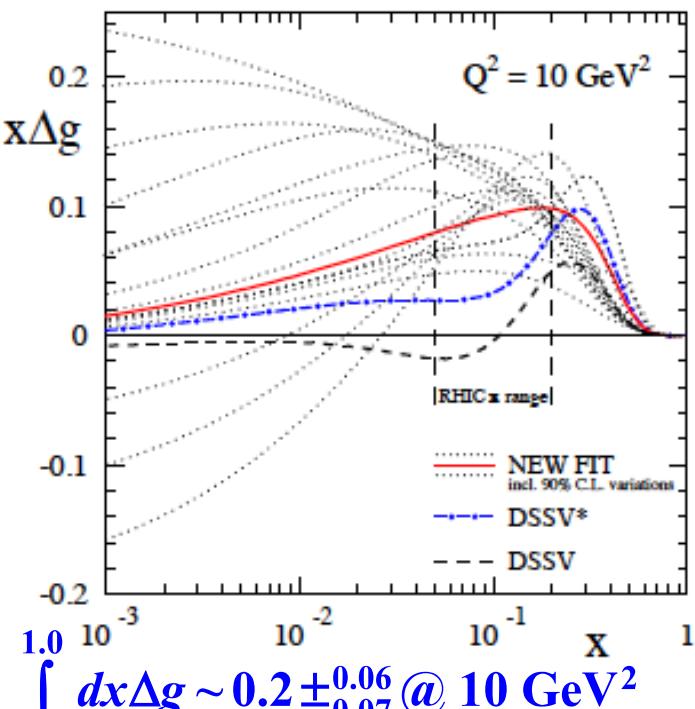
What we have now: $\int \Delta g(x)$

DSSV: arXiv: 1404.4293, PRL 113, 012001

DSSV: arXiv:0904.3821

DSSV*: DSSV + all new (SI)DIS

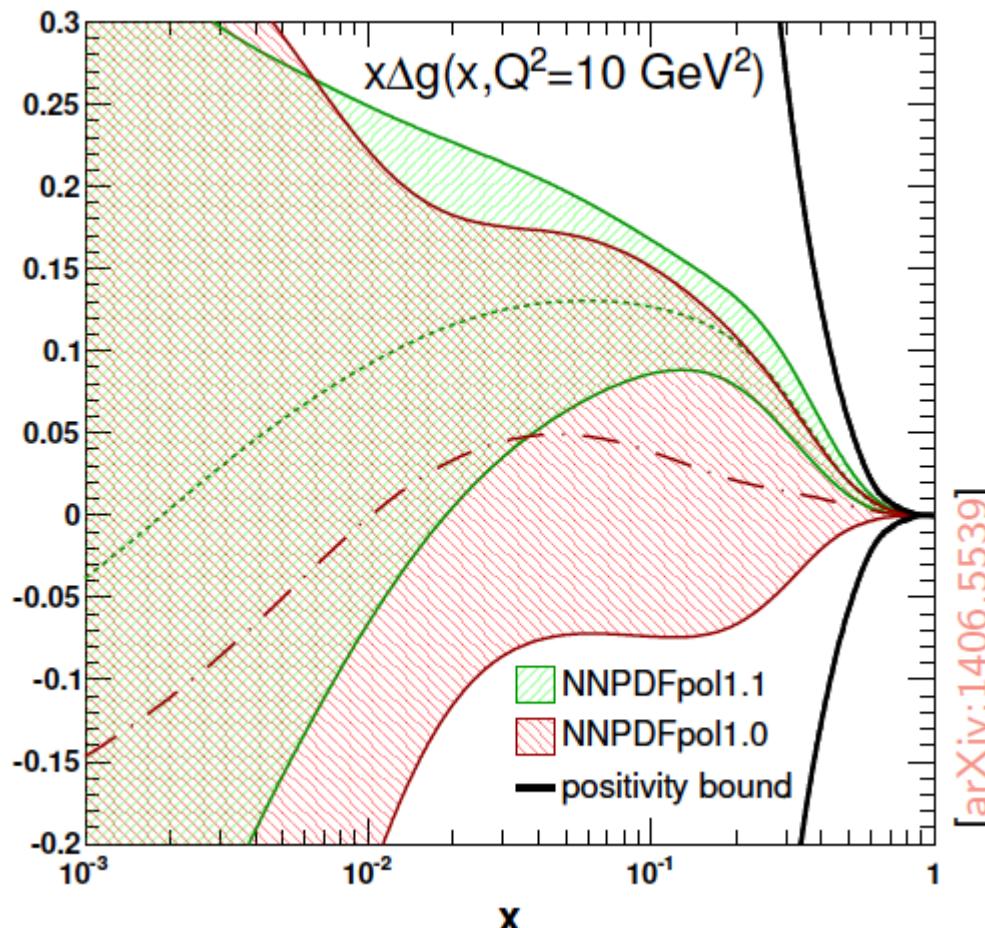
DSSV: DSSV* & RHIC 2009



First time a significant non-zero $Dg(x)$

- strong constrain on $\int \Delta g(x)$
- first $\int \Delta g(x) > 0$
- completely consistent with DSSV* in 90% C.L.

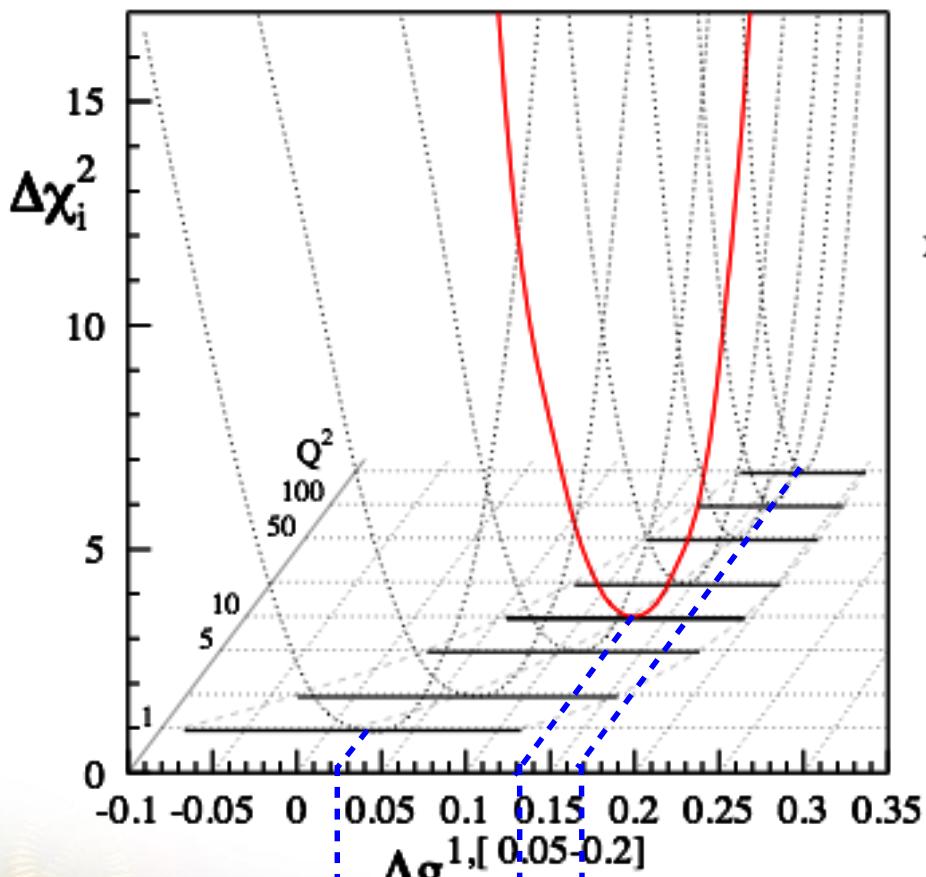
Impact in NNPDF



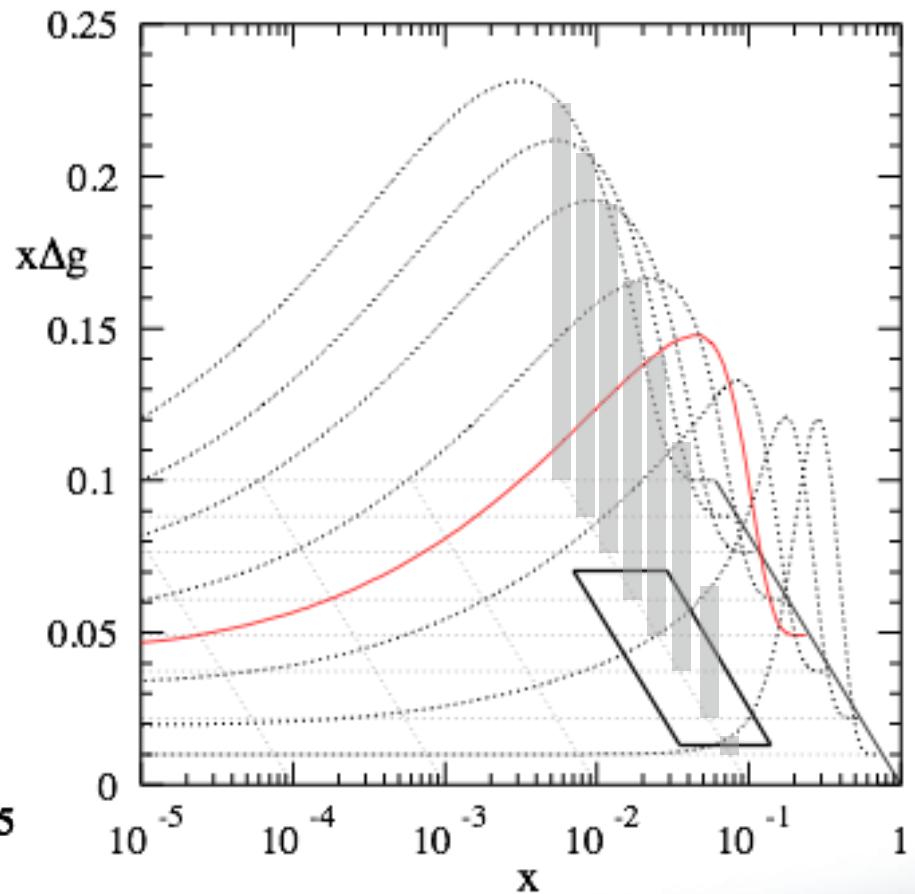
only STAR jets included

Q^2 -Dependence

$$\Delta g^{1,[0.05-0.2]}(Q^2) \equiv \int_{0.05}^{0.2} \Delta g(x, Q^2) dx$$



Δg_{1,[0.05-0.2]}
high Q^2
medium Q^2
low Q^2

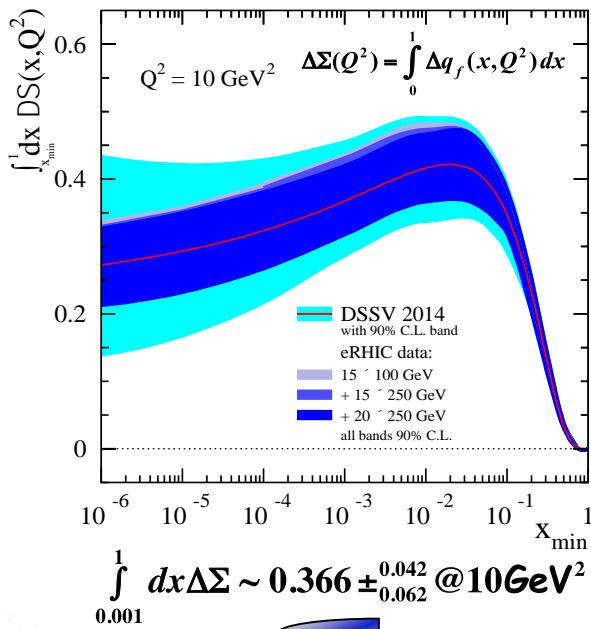


very fast evolution
in RHIC kinematics

Why is separating quark flavors important?

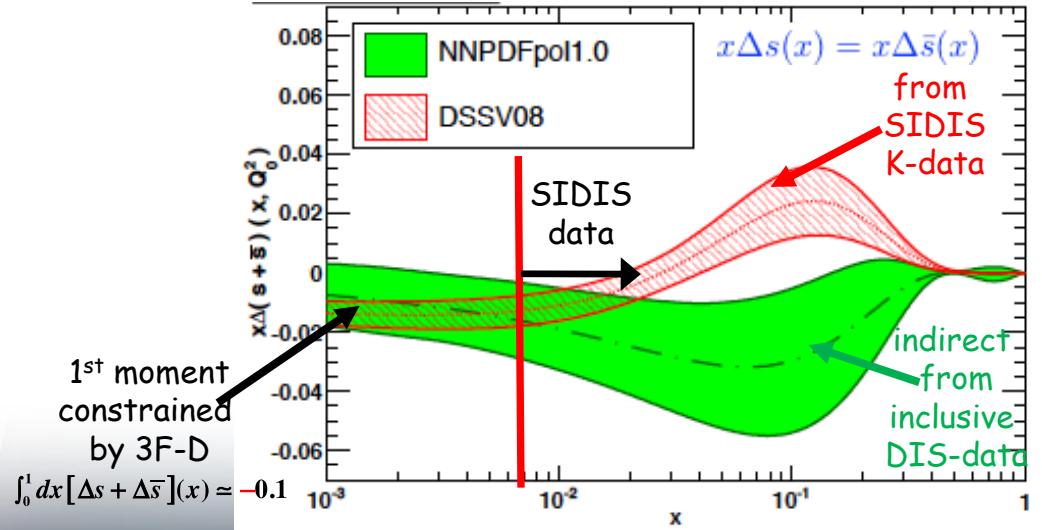
Why is separating quark flavors important?

- nuclear structure is encoded in parton distribution functions
- understand dynamics of the quark-antiquark fluctuations
- flavor asymmetry in the light quark sea in the proton
unpolarized: \bar{u} < \bar{d} Helicity: $\Delta\bar{u} > \Delta\bar{d}$ TMDs: ?????
- shape of polarized sea-quark PDFs critical for quark contribution to spin

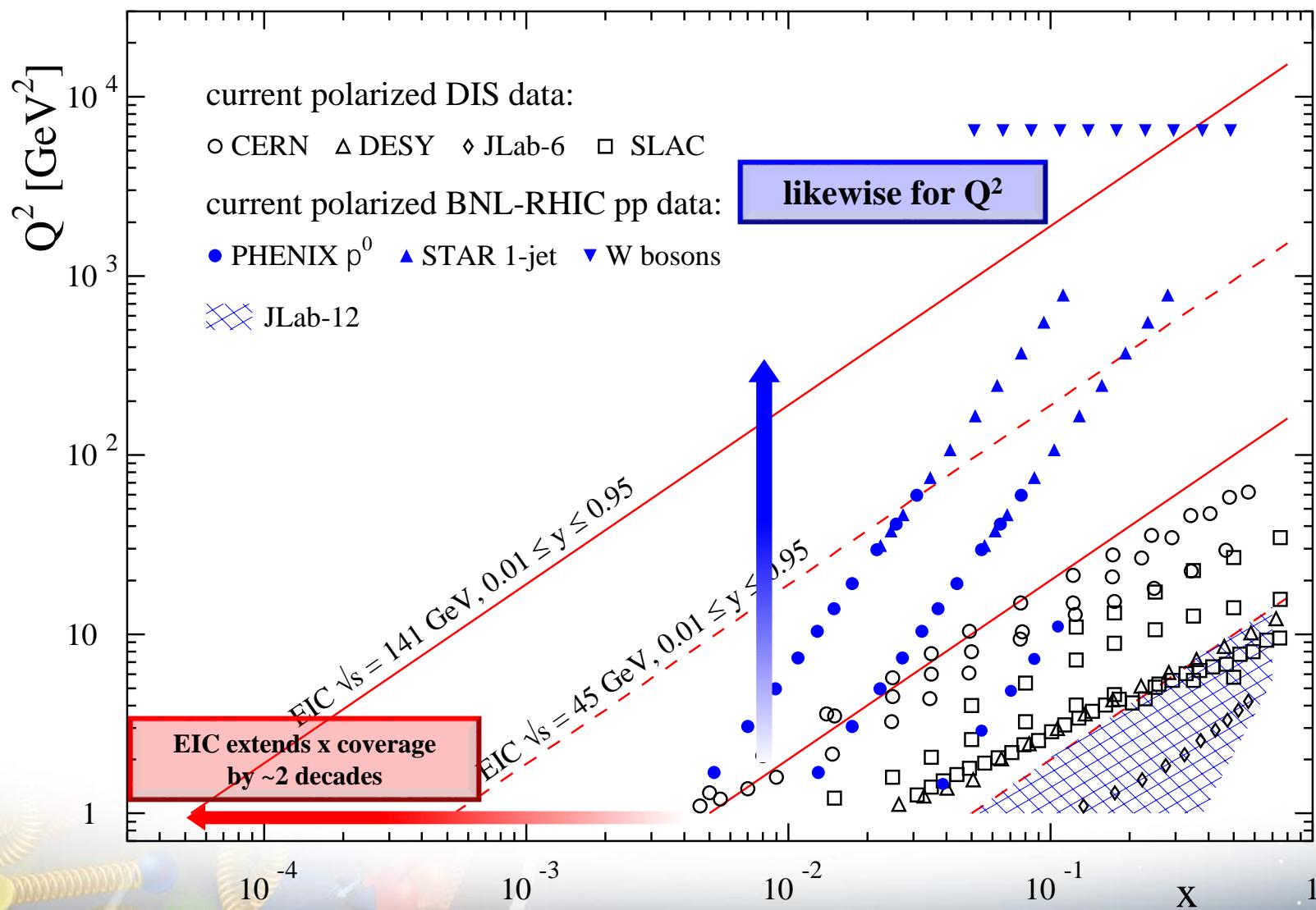


$\Delta\Sigma$ does not converge at low x

- due to current constraints put in the fits
- strangeness was identified to be one of the least known quantities
 - both unpolarized and polarized



present vs EIC kinematic coverage



Details: R.Sassot, M. Stratmann, ECA, [arXiv:1206.6014](https://arxiv.org/abs/1206.6014), [arXiv:1509.06489](https://arxiv.org/abs/1509.06489)

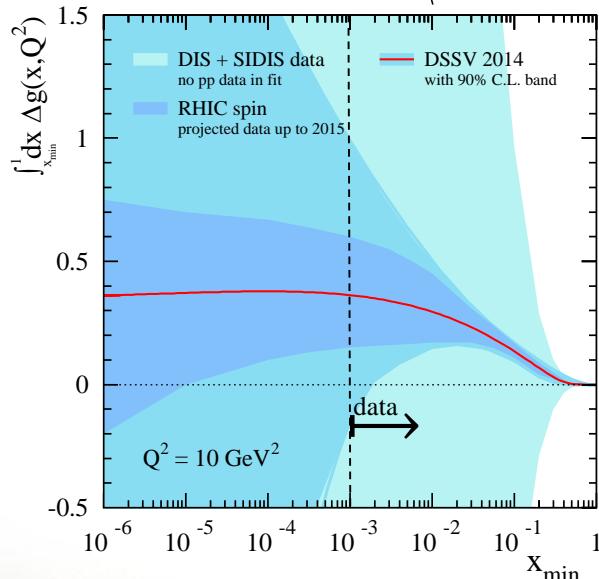
What forms the Spin of the Proton



Spin is more than the number $\frac{1}{2}$! It is the interplay between the intrinsic properties and interactions of quarks and gluons

What do we know:

$$\frac{1}{2}\hbar = \left\langle P, \frac{1}{2} | J_{QCD}^z | P, \frac{1}{2} \right\rangle$$

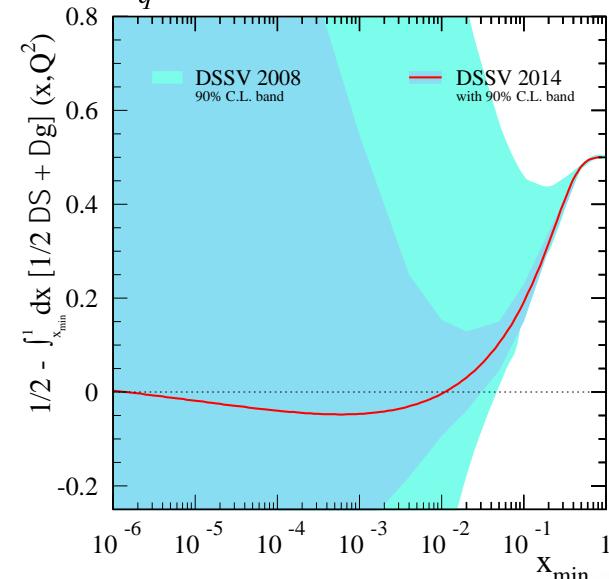
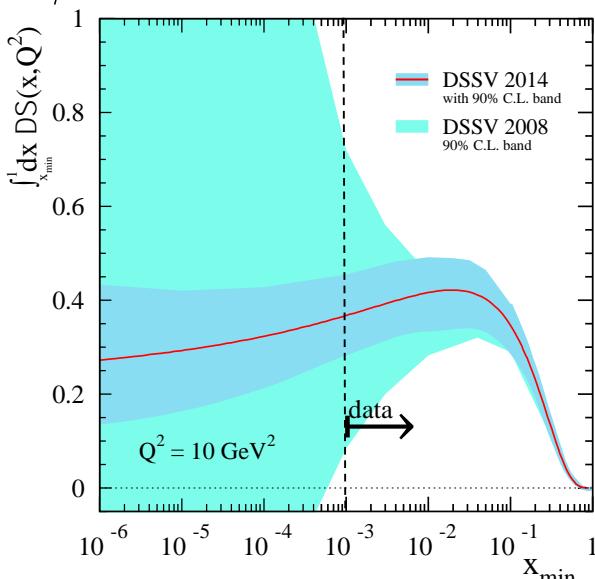


total
quark spin

gluon
spin

angular
momentum

$$\frac{1}{2} \int_0^1 dx \Delta \Sigma(x, Q^2) + \int_0^1 dx \Delta G(x, Q^2) + \int_0^1 dx \left(\sum_q L_q^z + L_g^z \right)$$



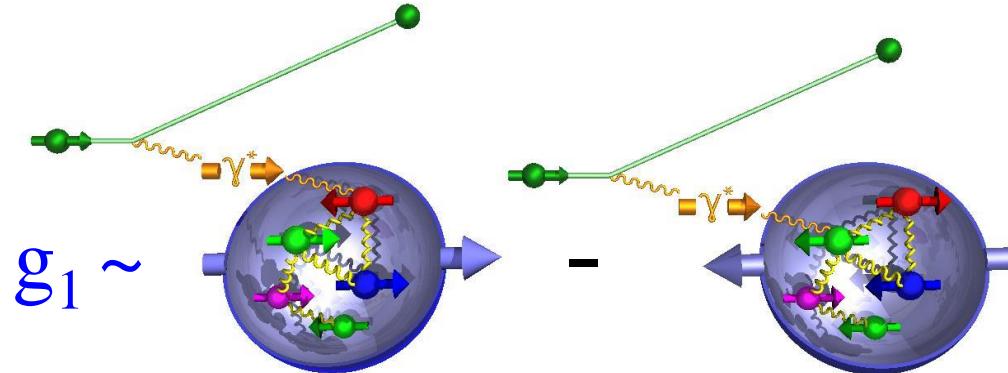
$1/2 -$ Gluon 40%

-- Quarks 30%

= orbital angular momentum

How to decompose the Spin of the Proton

To determine the contribution of quarks and gluons to the spin of the proton, one needs to measure the cross section difference g_1 as function of x and Q^2



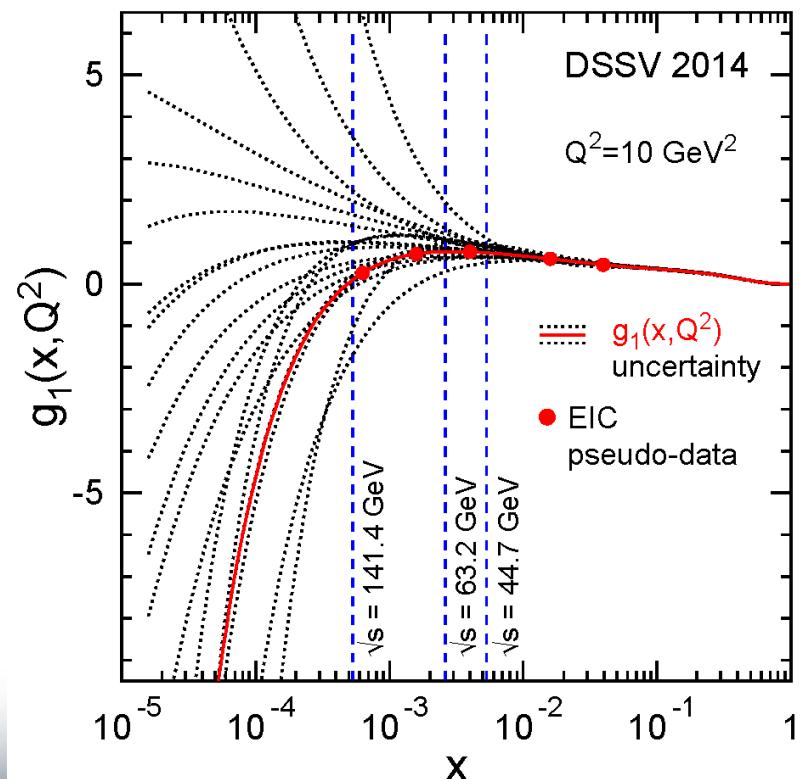
quark contribution:

The integral of Δq over x from 0 to 1

gluon contribution:

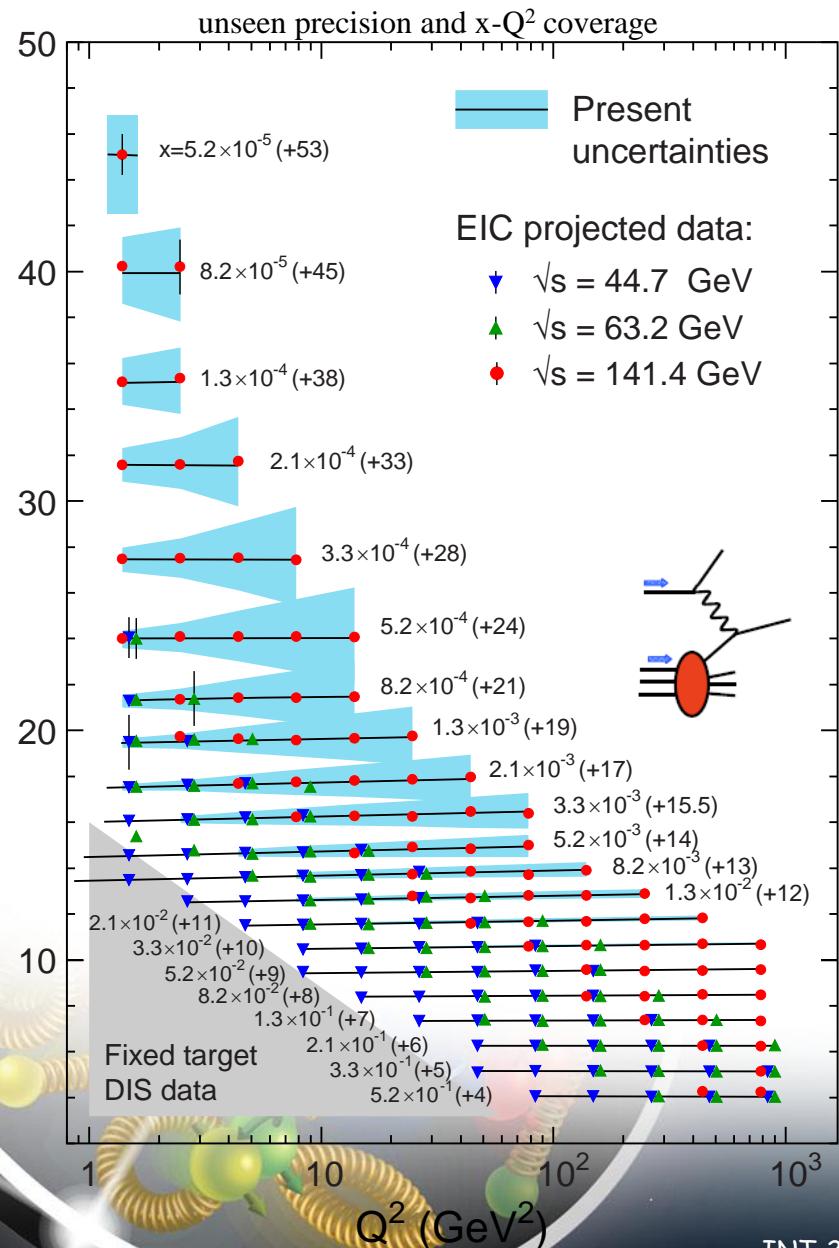
$$dg_1(x, Q^2) / d\ln Q^2 \rightarrow \Delta g(x, Q^2)$$

The current knowledge about g_1 as function of x at $Q^2 = 10 \text{ GeV}^2$



g^P the way to find the Spin

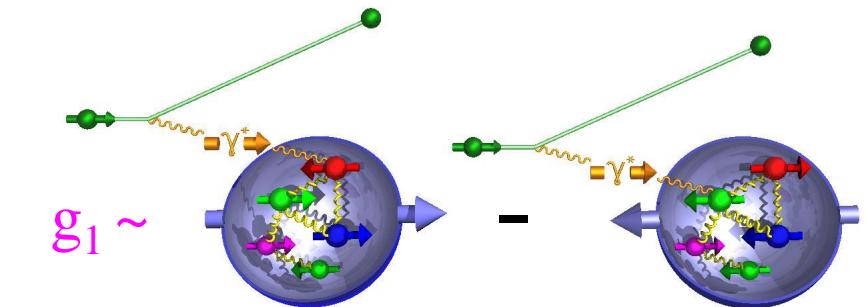
M.Stratmann, R. Sassot, ECA: arXiv:1206.6014 & 1509.06489



cross section: $\frac{d^2\sigma}{d\Omega dE} \sim L_{\mu\nu} W^{\mu\nu}$

$$W^{\mu\nu} = -g^{\mu\nu} F_1 - \frac{p^\mu p^\nu}{v} F_2 + \frac{i}{v} \epsilon^{\mu\nu\lambda\sigma} q^\lambda s^\sigma g_1$$

$$+ \frac{i}{v^2} \epsilon^{\mu\nu\lambda\sigma} q^\lambda (p \cdot q s^\sigma - s \cdot q p \sigma) g_2$$



pQCD scaling violations

$$\frac{dg_1}{d \log(Q^2)} \sim -\Delta g(x, Q^2)$$

$$\Delta \Sigma(Q^2) = \int_0^1 g_1(x, Q^2) dx = \int_0^1 \Delta q_f(x, Q^2) dx$$

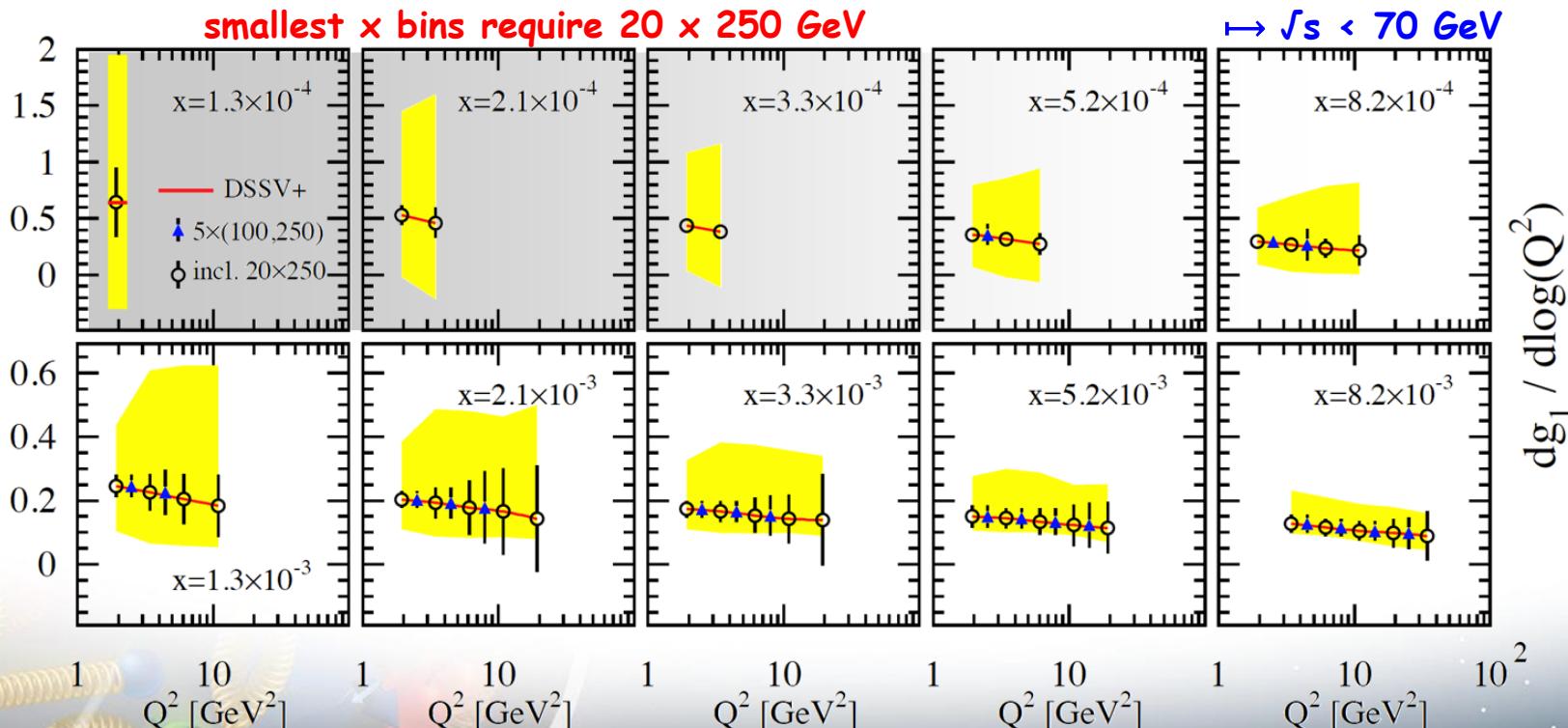
scaling violations at small x

rough small- x approximation to Q^2 -evolution:

$$\frac{dg_1}{d\log(Q^2)} \propto -\Delta g(x, Q^2)$$

spread in $\Delta g(x, Q^2)$ translates into spread of scaling violations for $g_1(x, Q^2)$

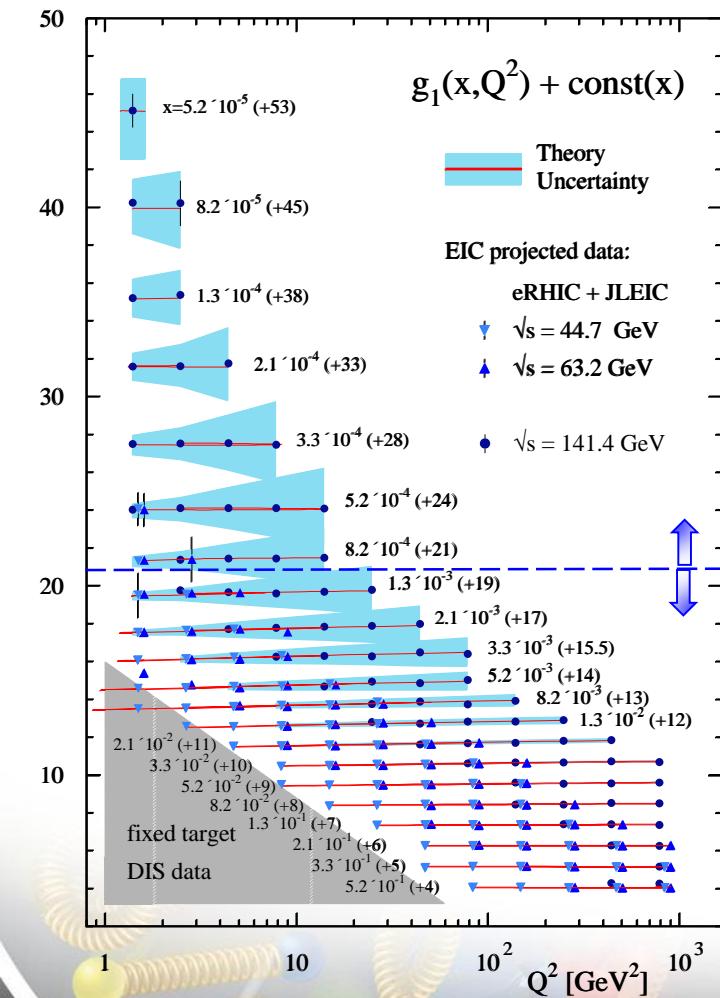
- ❑ need x-bins with at least two Q^2 values to compute derivative (limits x reach somewhat)



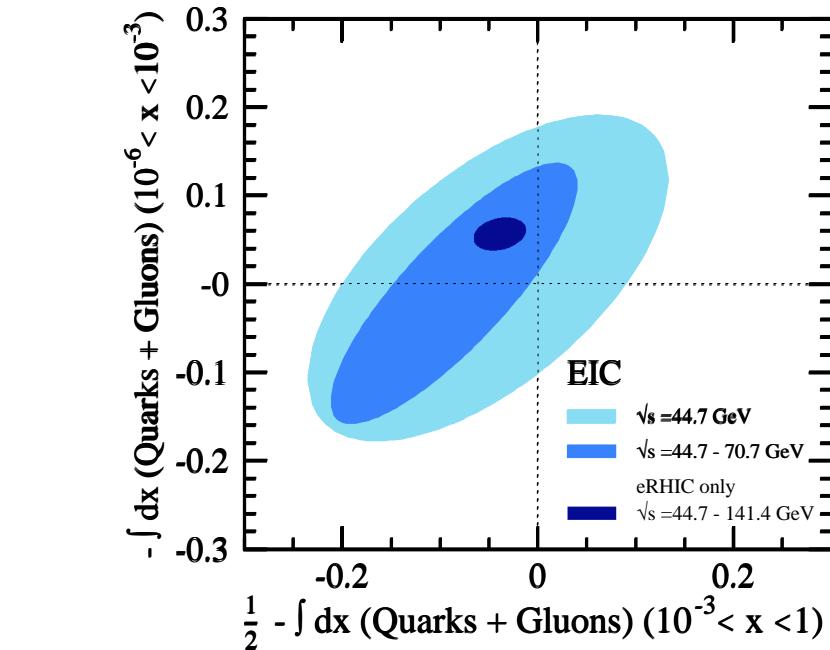
- error bars for moderate 10fb^{-1} per c.m.s. energy; bands parameterize current DSSV+ uncertainties

What forms the Spin of the Proton

The polarized SF $g_1(x, Q^2)$ as measured by EIC for low \sqrt{s}



arXiv:1509.06489
PRD 92, 094030



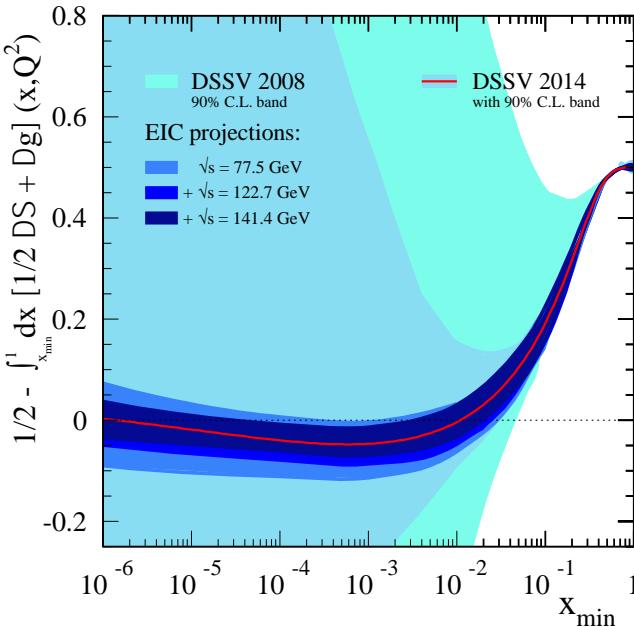
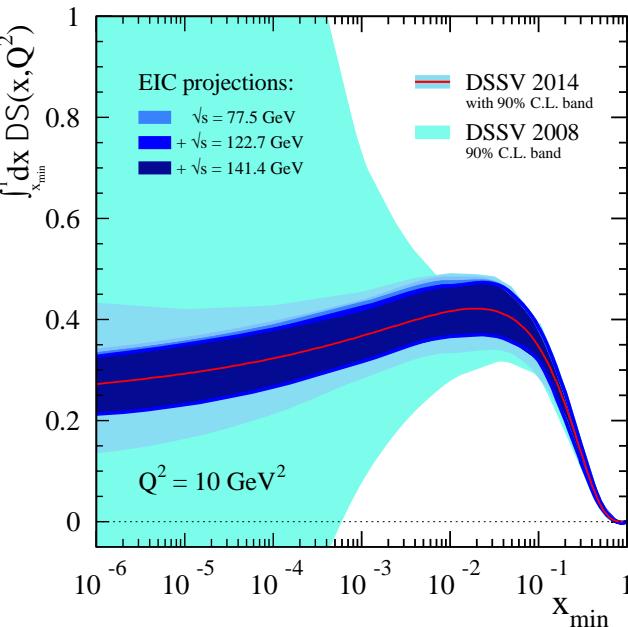
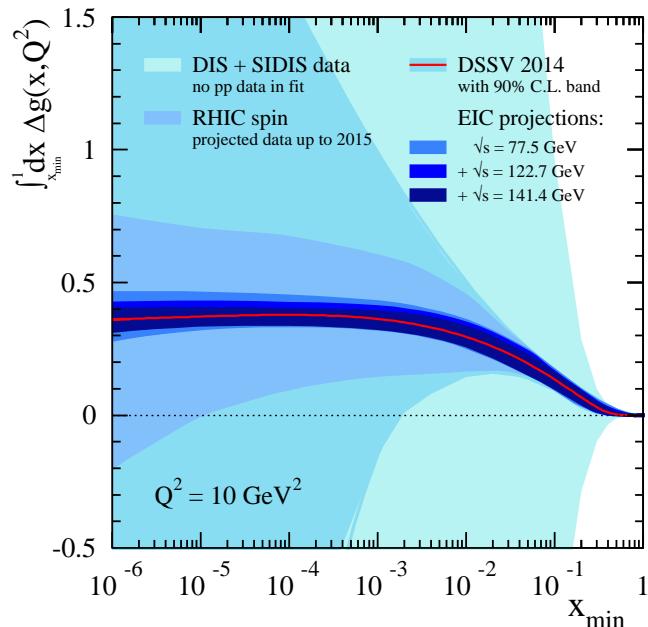
Only with the center-of-mass energies available at EIC the different contributions to the spin of the proton can be disentangled

Where does the Spin of the proton hide

“Helicity sum rule:”

$$\frac{1}{2}\hbar = \left\langle P, \frac{1}{2} | J_{QCD}^z | P, \frac{1}{2} \right\rangle = \sum_q \frac{1}{2} S_q^z + S_g^z + \sum_q L_q^z + L_g^z$$

total
quark spin gluon spin angular momentum



$1/2 \cdot$

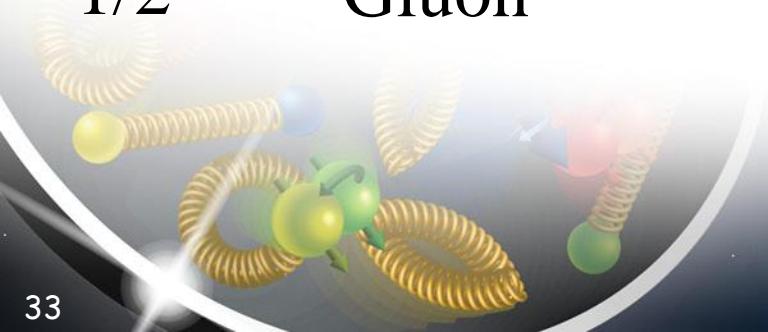
Gluon

-

Quarks

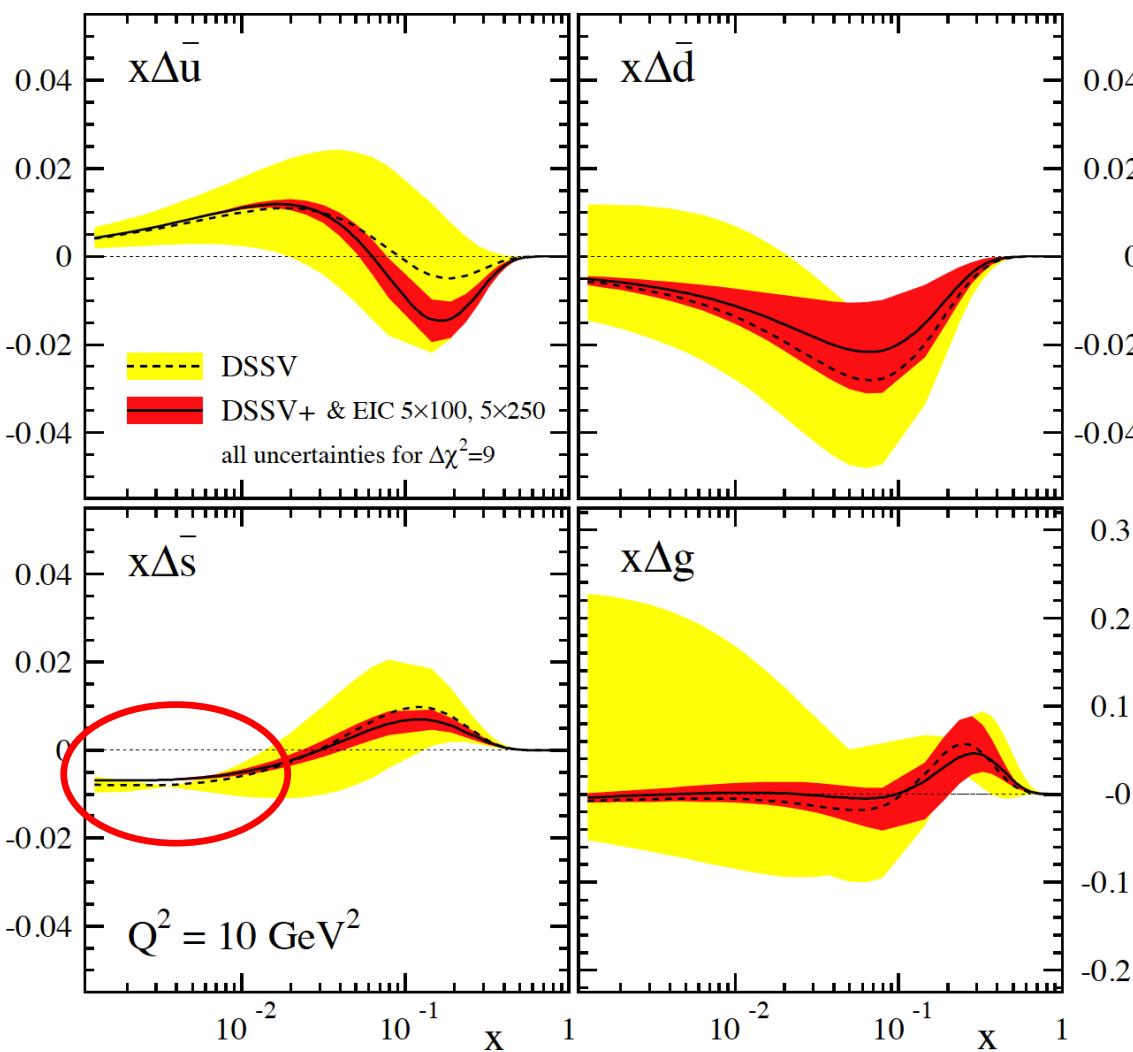
=

orbital angular momentum



SIDIS@EIC: HELICITY PDFs

Can cover the same kinematics for $g_1^{\pi, K}$ as for g_1
 → will constrain Δq



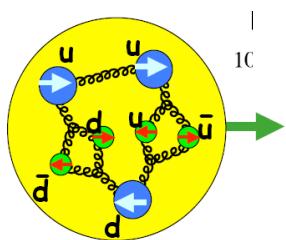
yet, small x behavior completely unconstrained
 → determines x -integral,
 which enters proton spin sum

- includes data for $\sqrt{s}=45 \text{ GeV} \& 70 \text{ GeV}$
 - can be pushed to $x=10^{-4}$ with $\sqrt{s}=140 \text{ GeV}$ data
 - Low x -behavior for Δs is artificial due to constraints put in the fits 3F-D
 → EIC can remove all constraints
- "issues":**
- (SI)DIS @ EIC limited by **systematic uncertainties**
 need to control rel. lumi, polarimetry, PID performance, ... very well

probing a possible asymmetry in the polarized sea

- current SIDIS data not sensitive to $\Delta\bar{u}(x) - \Delta\bar{d}(x)$ (known to be sizable for unpol. PDFs)
- many models predict sizable asymmetry [large N_c , chiral quark soliton, meson cloud, Pauli blocking]

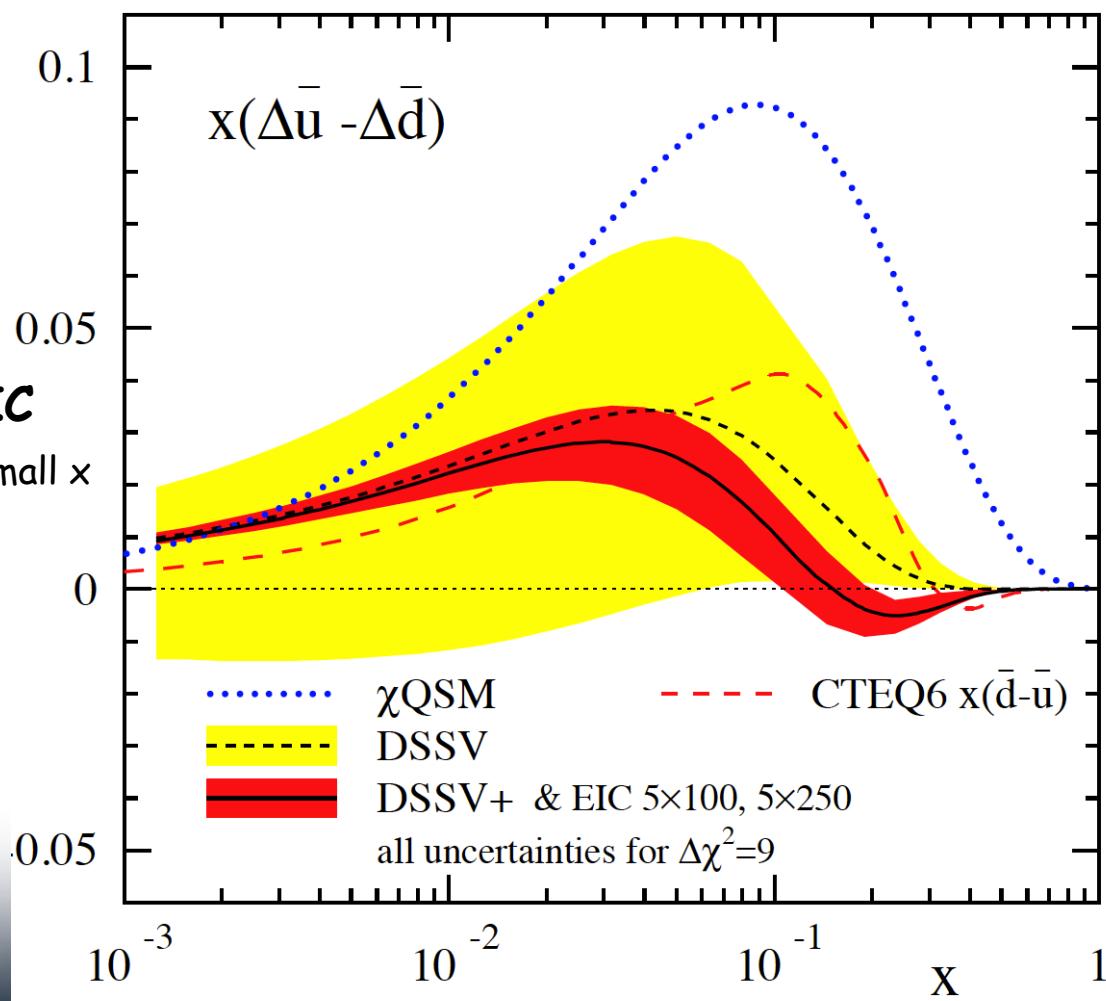
Thomas, Signal, Cao; Holtmann, Speth, Fassler;
Diakonov, Polyakov, Weiss; Schafer, Fries; Kumano;
Wakamatsu; Gluck, Reya; Bourrely, Soffer, ...



- can be easily studied at an EIC

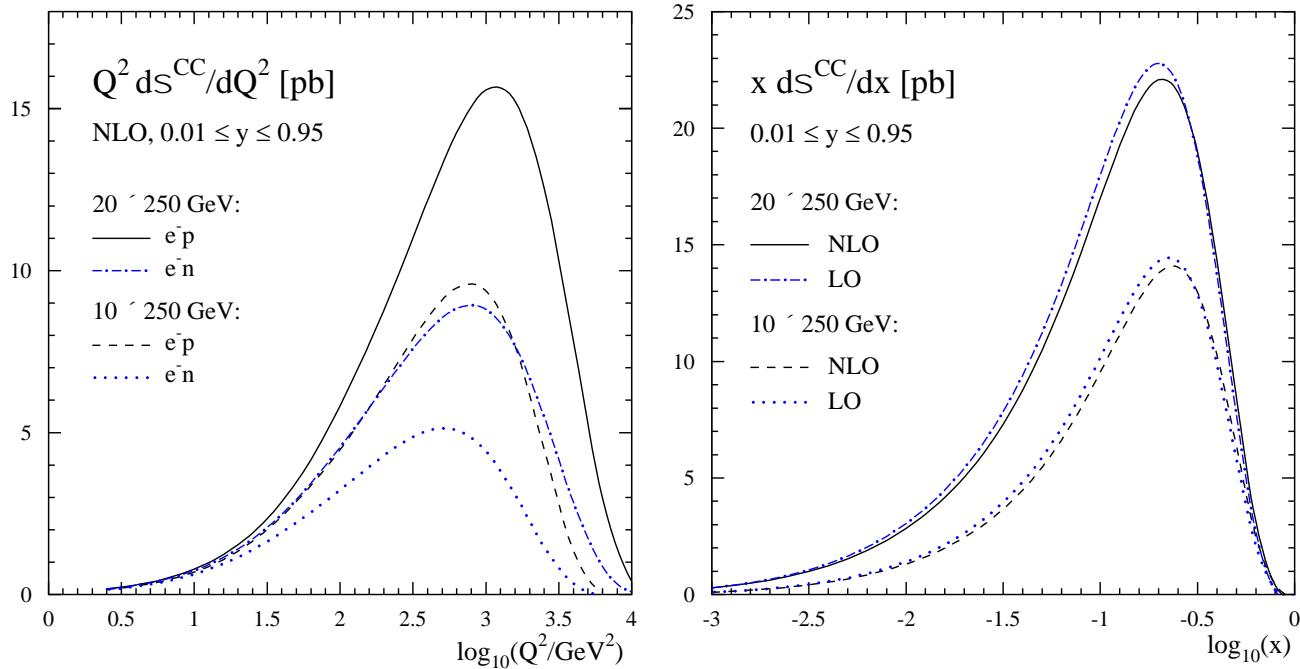
main effect expected to be at not too small x
→ can test x dependence

- can try to look into a possible
 $\Delta s(x) - \Delta \bar{s}(x)$
with $K^{+/-}$ SIDIS data



Observables: Charge Current in polarized ep

Polarized CC cross section



Approximate behavior of the LO single spin asymmetry

$$y \rightarrow 0$$

$$A_L^{W^-, p} \frac{\Delta u(x) - \Delta \bar{d}(x)}{u(x) + \bar{d}(x)}$$

$$y = 1/2$$

$$\frac{4\Delta u(x) - \Delta \bar{d}(x)}{4u(x) + \bar{d}(x)}$$

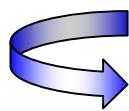
$$y \rightarrow 1$$

$$\frac{\Delta u(x)}{u(x)}$$

$$A_L^{W^-, n} \frac{\Delta d(x) - \Delta \bar{u}(x)}{d(x) + \bar{u}(x)}$$

$$\frac{4\Delta d(x) - \Delta \bar{u}(x)}{4d(x) + \bar{u}(x)}$$

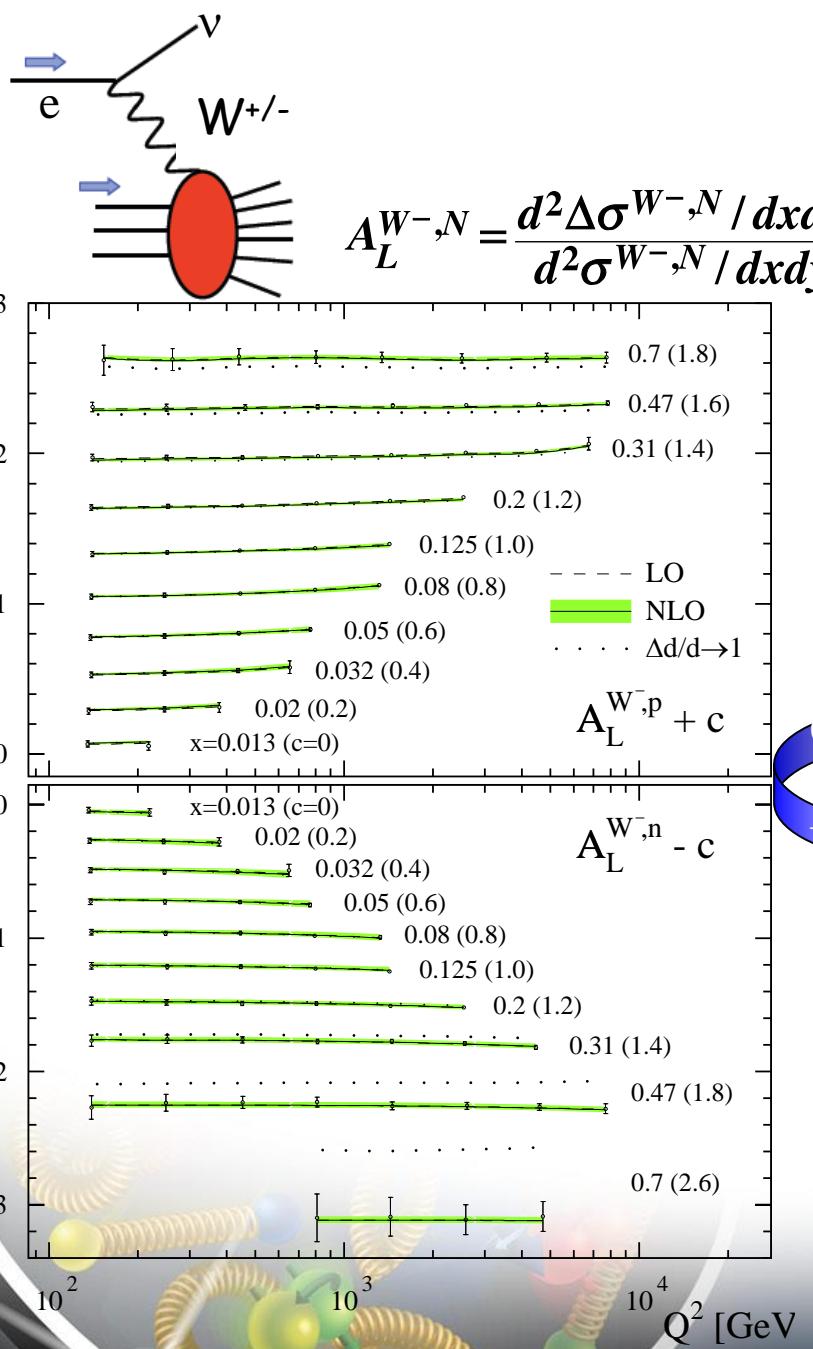
$$\frac{\Delta d(x)}{d(x)}$$



similar to what is seen in
W production in polarized pp

Details: Th. Burton, T. Martini, H. Spiesberger, M. Stratmann, ECA, arXiv:13095327 PRD 88 (2013) 114025

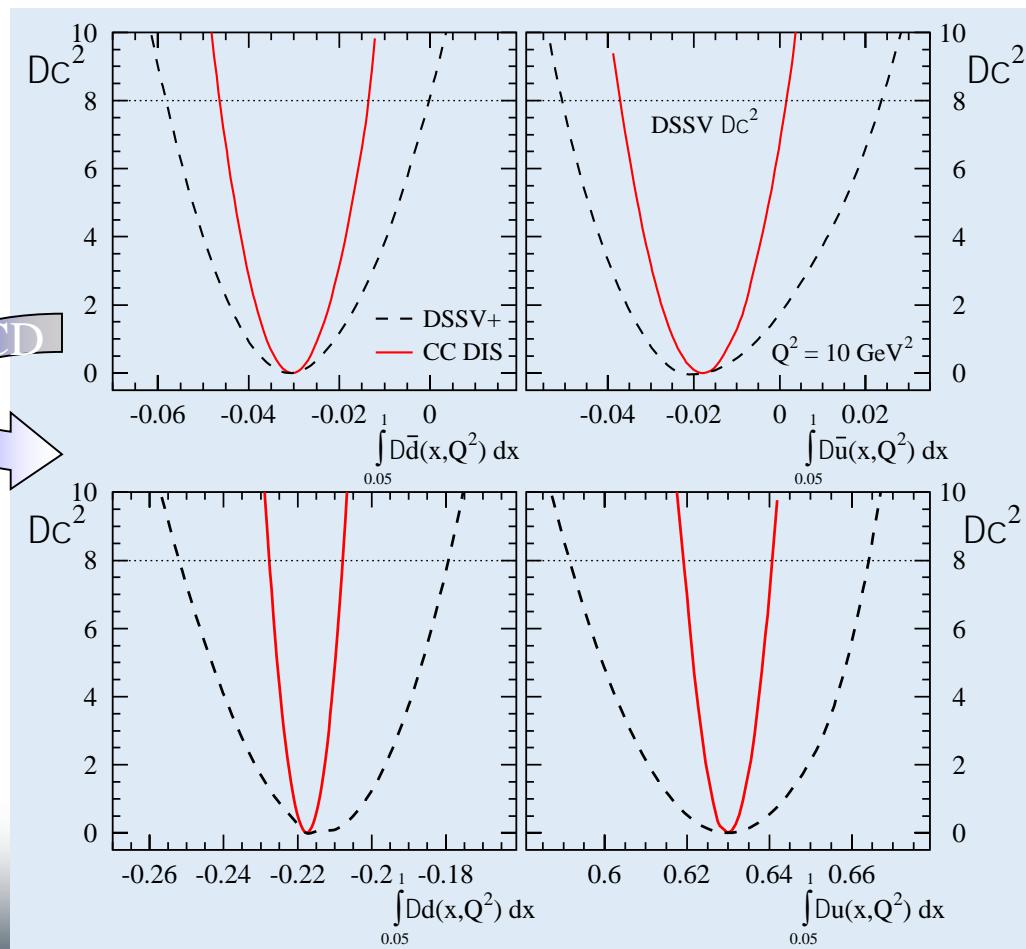
Polarized EW PHYSICS



$$g_1^{W^-,p}(x) = \Delta u(x) + \Delta \bar{d}(x) + \Delta c(x) + \Delta \bar{s}(x)$$

$$g_1^{W^-,n}(x) = \Delta d(x) + \Delta \bar{u}(x) + \Delta c(x) + \Delta \bar{s}(x)$$

More Details: arXiv: [1309.5327](https://arxiv.org/abs/1309.5327)



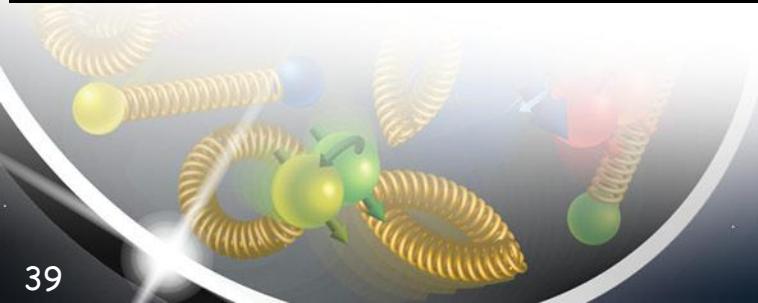
- ❑ More work to be done on unpolarized PDF and FF constrains
 - but EIC will be critical for PDF and FF constrains
 - did not discuss inclusive DIS and $F_2^C \rightarrow$ but coverage better than for eA
arXiv:1708.05654
- ❑ EIC at high \sqrt{s} is the only machine to unravel the different components to the spin of the proton
 - critical for low-x behaviour
- ❑ CC important observable for flavor separation and testing limitations of SIDIS

Questions to be answered before an EIC

- ❑ effective neutron target: \sqrt{s} Deuterium: 100 GeV Helium-3: 166 GeV
 - He-3 larger x coverage proton equivalent \sqrt{s} : 250 GeV
 - what is the better choice with respect to nuclear effects
- ❑ What are the limiting theoretical factors to determine high-x PDFs?
 - what is the golden observable to constrain $g(x, Q^2)$ at high x
- ❑ How can we measure Lq and Lg from Jaffe-Manohar
- ❑ What are the golden observables to learn about hadronization
 - Correlations between different rapidity ranges and distributions inside jets?

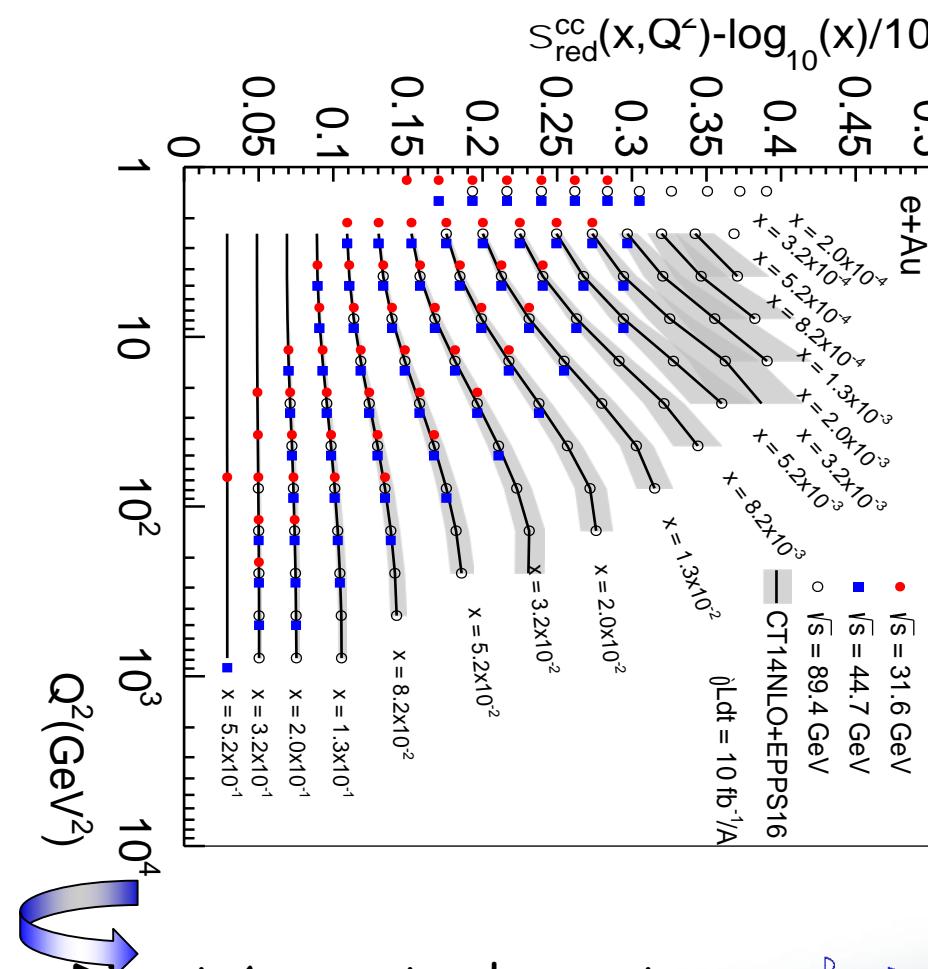
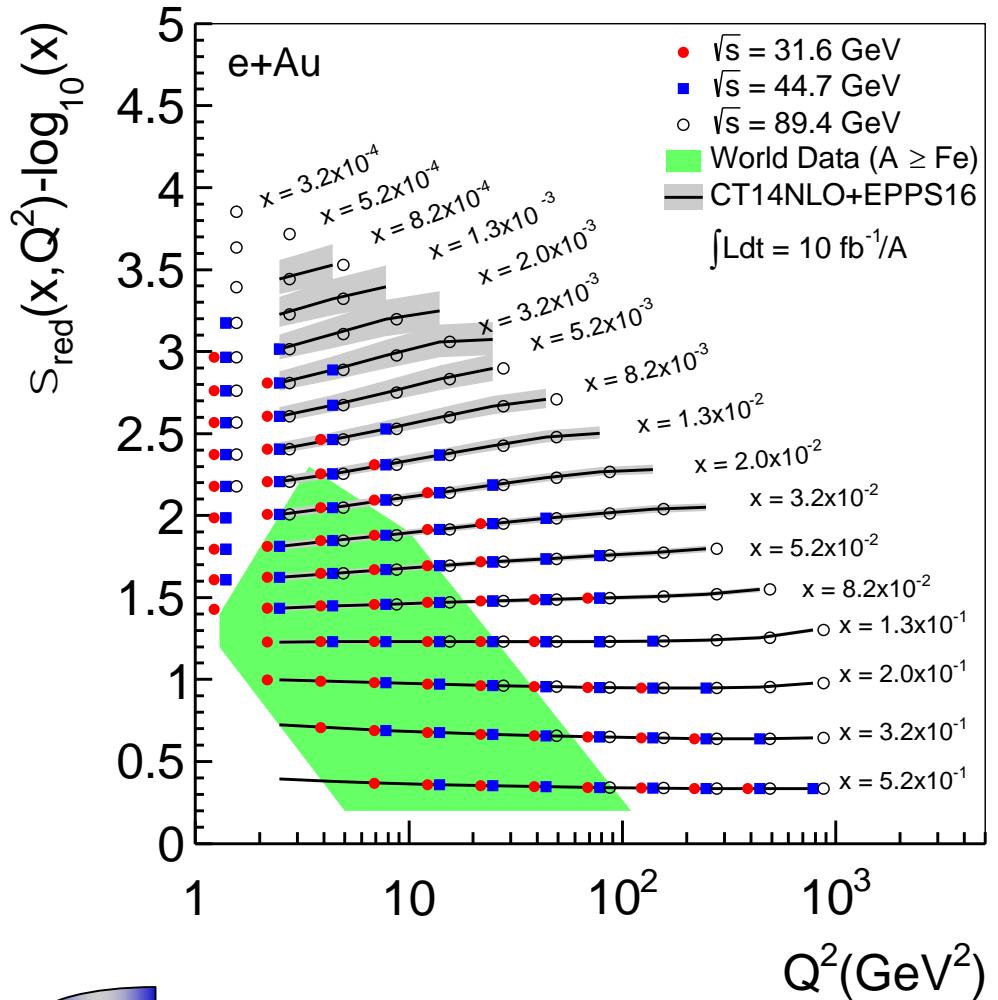


BACK UP



Inclusive Cross-Sections in eA

arXiv:1708.05654

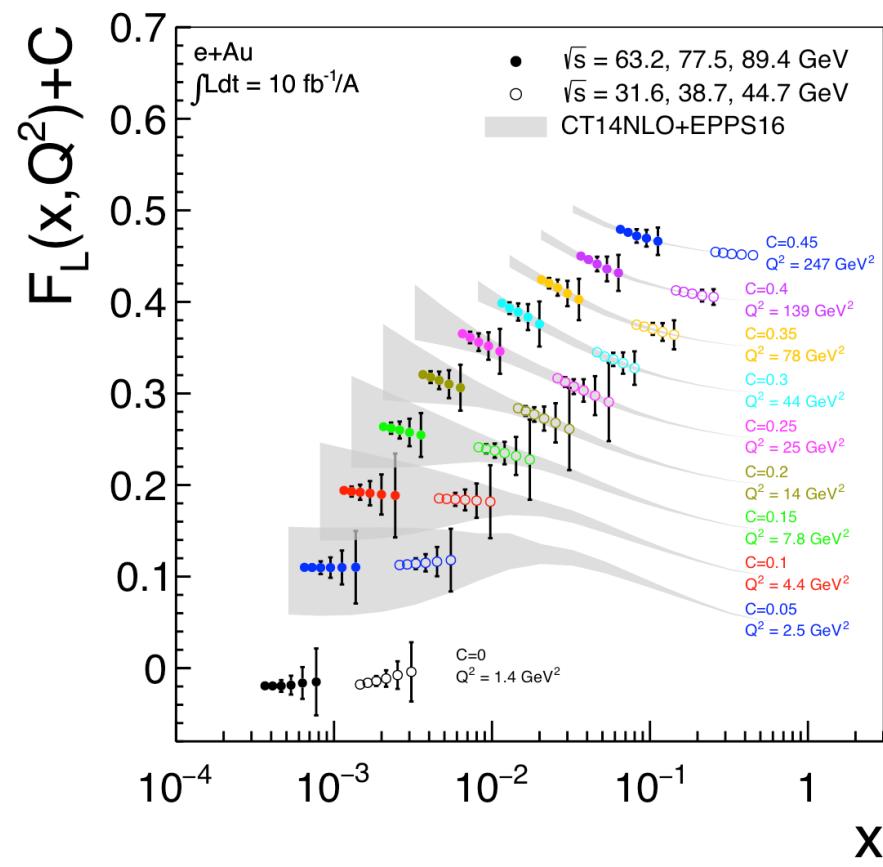
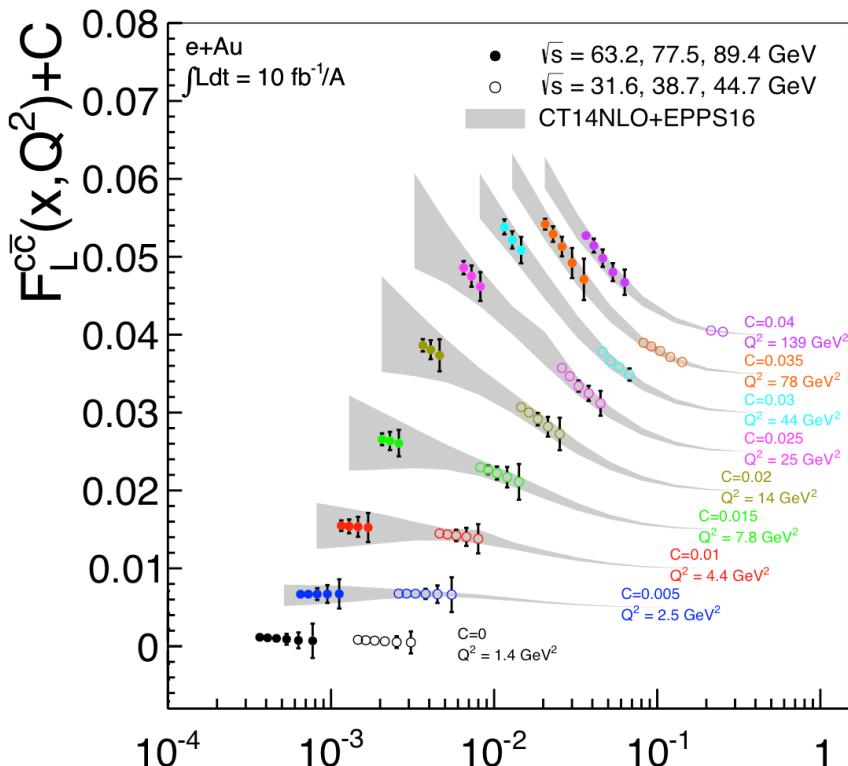


Direct Access to gluons at medium to high x by tagging photon-gluon fusion through charm events

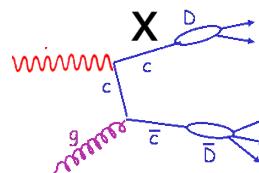


Direct Access to Gluons in eA

For Details: arXiv:1708.05654



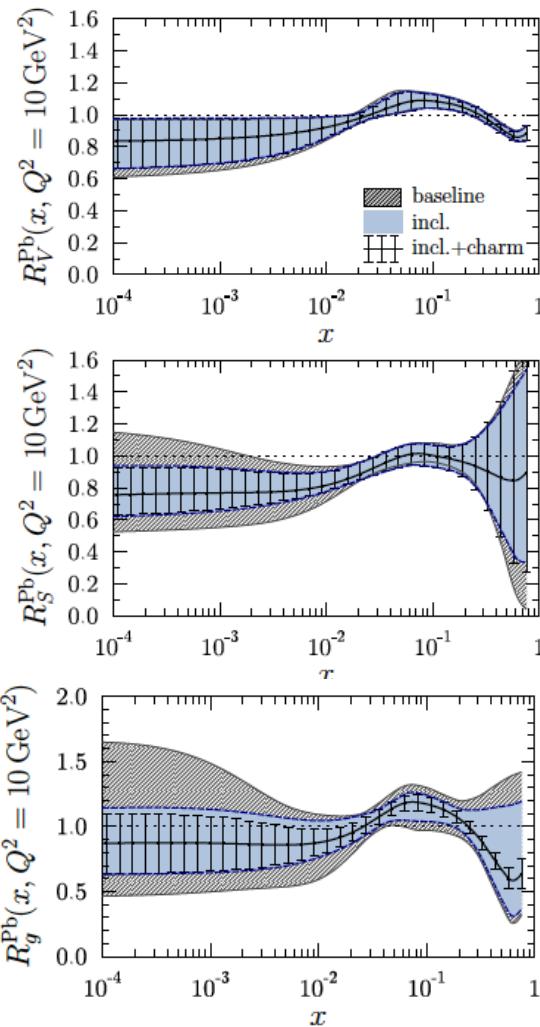
Direct Access to gluons at medium to high x by tagging photon-gluon fusion through charm events



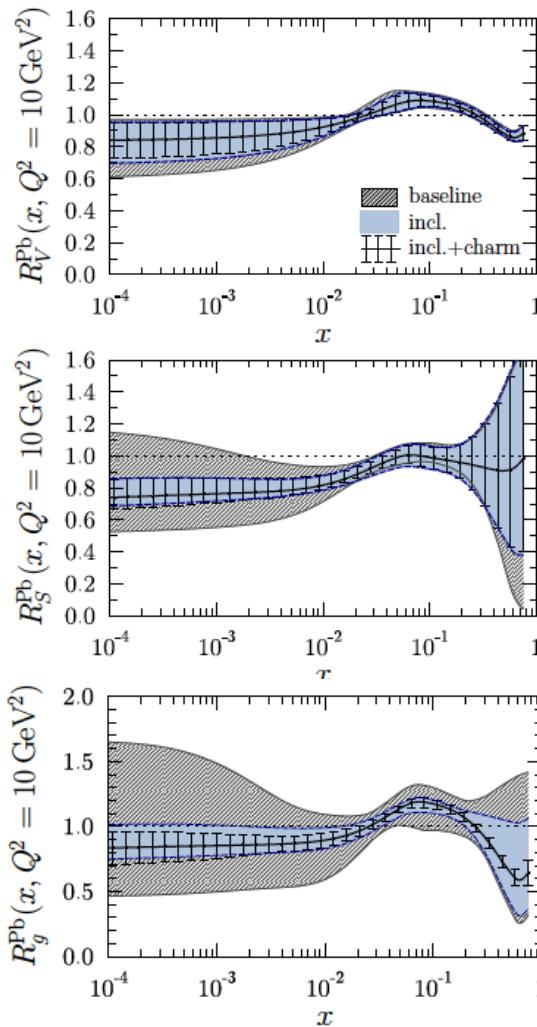
high precision F_L^{charm} will offer an opportunity to benchmark different GM-VFNS schemes with an unprecedented precision.

EIC: Impact on the Knowledge of 1D Nuclear PDFs

$\sqrt{s} < 45 \text{ GeV}$



$\sqrt{s} < 90 \text{ GeV}$

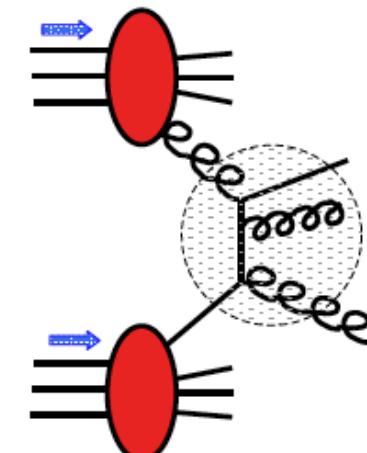
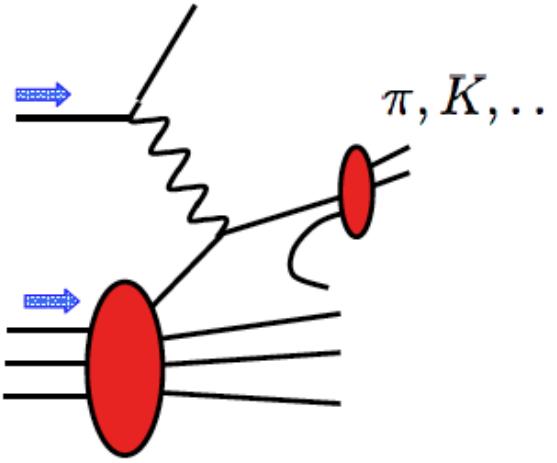
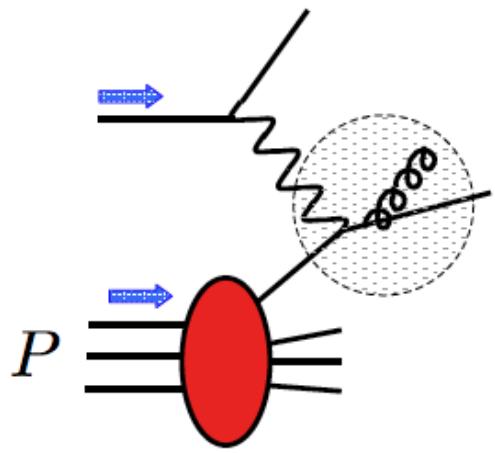


Ratio of PDF of Pb over Proton

- Without EIC, large uncertainties
→ With EIC significantly reduced uncertainties
- Complementary to RHIC and LHC pA data.
Provides information on initial state for heavy ion collisions.
- Does the nucleus behave like a proton at low-x?
→ relevant to very high-energy cosmic ray studies
→ critical input to AA
- submitted to PRD
arXiv:1708.05654

probes of nucleon helicity structure

$$\Delta f(x) = f_{\rightarrow}(x) - f_{\leftarrow}(x)$$



$\Delta q + \Delta \bar{q}$

$\Delta q, \Delta \bar{q}$ pions, kaons

Δg 1-jet, 1-hadron

Δg charm, 2-hadrons

$\Delta q, \Delta \bar{q}$ $W^{+/-}$ bosons

guiding principle: **factorization**

e.g. **DIS** $d\Delta\sigma = \sum_{f=q,\bar{q},g} \int dx \Delta f(x, Q^2) d\hat{\Delta\sigma}_{\gamma^* f}(xP, \alpha_s(Q^2))$

essential: QCD corrections $d\hat{\Delta\sigma} = d\hat{\Delta\sigma}^{\text{LO}} + \alpha_s d\hat{\Delta\sigma}^{\text{NLO}} + \dots$

need DIS + SIDIS + pp to constrain all aspects of PDFs (a way to test factorization)