

# A NEW LEADING MECHANISM FOR NEUTRINOLESS DOUBLE-BETA DECAY

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with

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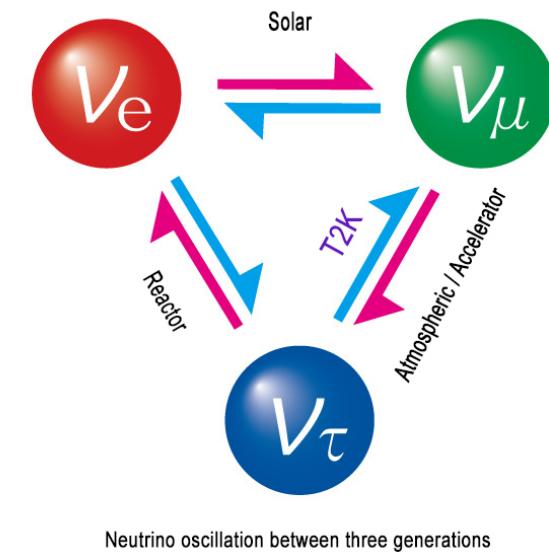
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# Outline

- Introduction
- Neutrinoless Double-Beta Decay
- The Way of Effective Field Theory
- Renormalization
- Estimate of Low-Energy Constant
- "*Ab Initio*" Example
- Discussion
- Conclusion

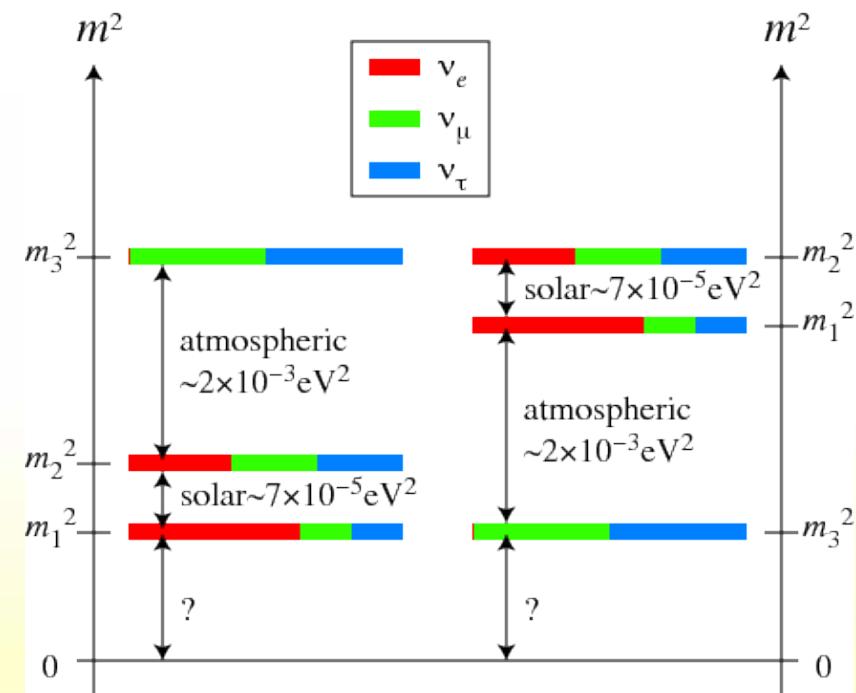
# Introduction

one of the  
most important discoveries  
after Standard Model



$$P_{i \rightarrow j} \approx \sin^2(2\theta_{ij}) \sin^2\left(\frac{L}{4E} \Delta m_{ij}^2\right)$$

(two flavors)



King '15

neutrinos mix  
and have mass

SM  
not complete

$m_i \lesssim 2 \text{ eV}$  PDG '18

## Two mechanisms

1) (light) right-handed neutrinos  $\nu_R \neq \nu_R^c \equiv C\gamma^{0T}(\nu_L)^\dagger$   $C = i\gamma_2\gamma_0$

$$\mathcal{L} = \mathcal{L}_{SM} + \mathcal{L}_{\nu_R} + \dots \quad \mathcal{L}_{\nu_R} = -y_\nu \underbrace{\left( \bar{\ell}_L \tilde{\varphi} \nu_R + \text{H.c.} \right)}_{}$$

$\langle \varphi \rangle \sim v/\sqrt{2}$   $\times \frac{\varphi}{v} \nu_R$   $= -\frac{y_\nu v}{\sqrt{2}} (\bar{\nu}_L \nu_R + \text{H.c.}) + \dots$

Dirac mass

$$\nu_D \equiv \nu_L + \nu_R \quad m_\nu \sim 0.1 \text{ eV} \quad \rightarrow \quad y_\nu \sim 10^{-12} \quad \text{possible but why?}$$

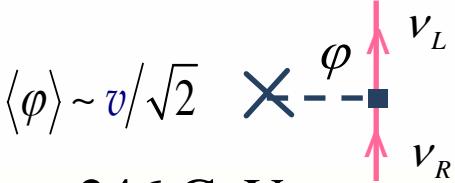
cf.  $\begin{cases} y_e \sim 3 \cdot 10^{-6} \\ \text{different from quark mixing pattern} \end{cases}$

## Two mechanisms

1) (light) right-handed neutrinos  $\nu_R \neq \nu_R^c \equiv C\gamma^{0T}(\nu_L)^\dagger$  Majorana '37

...

$$\mathcal{L} = \mathcal{L}_{SM} + \mathcal{L}_{\nu_R} + \dots \quad \mathcal{L}_{\nu_R} = -y_\nu \underbrace{\left( \bar{\ell}_L \tilde{\varphi} \nu_R + \text{H.c.} \right)}_{= -\frac{y_\nu v}{\sqrt{2}} (\bar{\nu}_L \nu_R + \text{H.c.}) + \dots} - \frac{M_R}{2} \left( \bar{\nu}_L^c \nu_R + \text{H.c.} \right)$$



$\langle \varphi \rangle \sim v/\sqrt{2}$

$v \simeq 246 \text{ GeV}$

Dirac mass

Majorana mass

$M_R$

new mass scale!

$|\Delta L| = 2$

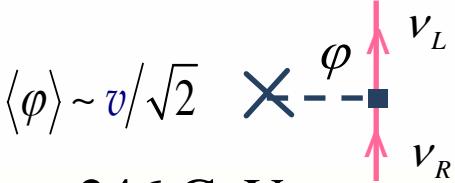
$M_R \lesssim y_\nu v$  can explain some of the experimental anomalies  
possible but why?

# Two mechanisms

1) (light) right-handed neutrinos  $\nu_R \neq \nu_R^c \equiv C\gamma^{0T}(\nu_L)^\dagger$  Majorana '37

...

$$\mathcal{L} = \mathcal{L}_{SM} + \mathcal{L}_{\nu_R} + \dots \quad \mathcal{L}_{\nu_R} = -y_\nu \underbrace{\left( \bar{\ell}_L \tilde{\varphi} \nu_R + \text{H.c.} \right)}_{= -\frac{y_\nu v}{\sqrt{2}} (\bar{\nu}_L \nu_R + \text{H.c.}) + \dots} - \frac{M_R}{2} (\bar{\nu}_L^c \nu_R + \text{H.c.})$$

$\langle \varphi \rangle \sim v/\sqrt{2}$    $v \simeq 246 \text{ GeV}$

Dirac mass      Majorana mass      new mass scale!  $|\Delta L| = 2$

$$M_R \gtrsim y_\nu v$$

$$\nu_M = \nu_L + \nu_R^c + \dots$$

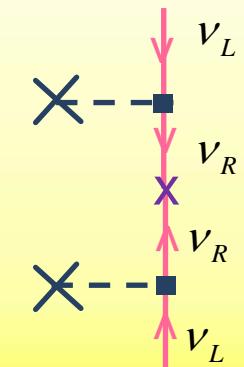
$$M \rightarrow U^\dagger M U \approx \begin{pmatrix} (y_\nu v)^2 / M_R & 0 \\ 0 & M_R \end{pmatrix}$$

$$m_\nu \sim 0.1 \text{ eV} \implies y_\nu \sim y_e \sqrt{M_R/v}$$

alleviates fine-tuning

$$N = \nu_R + \nu_L^c + \dots$$

decouples at low energies



Natural possibility:  $M_R \sim M_L \gg v \rightarrow (y_\nu v)^2 / M_R \ll v$

makes  
leptogenesis  
possible

Minkowski '77

(type I) see-saw mechanism



Fukugita + Yanagida '86

More generally, independent on details of high-energy physics:

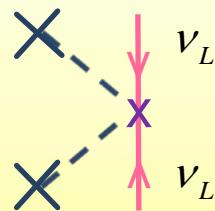
2) dimension-five operator

Weinberg '79

Weldon + Zee '80

$$\mathcal{L} = \mathcal{L}_{SM} + \mathcal{L}_{\text{dim}=5} + \dots$$

$$\mathcal{L}_{\text{dim}=5} = \frac{c_5}{M_L} \left[ (\ell^T C \tilde{\phi}) (\tilde{\phi}^T \ell) + \text{H.c.} \right]$$



$$= \frac{c_5 v^2}{2 M_L} (\bar{\nu}_L \nu_R^c + \text{H.c.}) + \dots$$

Majorana mass

$$|\Delta L| = 2$$

$$m_\nu \sim 0.1 \text{ eV} \rightarrow M_L \sim c_5 \cdot 10^{15} \text{ GeV}$$

comparable to GUT scale!

$$\text{NDA: } c_5 = \mathcal{O}(4\pi\alpha)$$

coincidence?

## Not exclusive mechanisms!

- B, L accidental symmetries at classical level
- non-perturbative effects break B+L, but conserve B-L
- unless B-L is exact, dim-5 op is allowed and will be there;  
it should be the most important effect of new physics  
→ coincidence that it can explain shortcoming of the SM?

N.B. In some models,  $c_5 \sim y_e^2 \sim 10^{-11}$

→ higher-dim ops could be important

Talk by Dekens  
next week

Prézeau, Ramsey-Musolf  
+ Vogel '09

Graesser '17

Cirigliano *et al.* '17'18

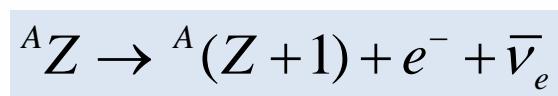
Here: only light neutrinos and dim-5 op

neutrino oscillations:  $U(1)_{L_e} \times U(1)_{L_\mu} \times U(1)_{L_\tau}$  not a symmetry  
is  $U(1)_{B-L}$  ?

# $0\nu2\beta$ decay

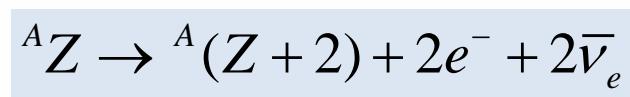
lots of nucleons for lots of time  $\rightarrow$  most sensitive probe of B-L violation

single-beta decay



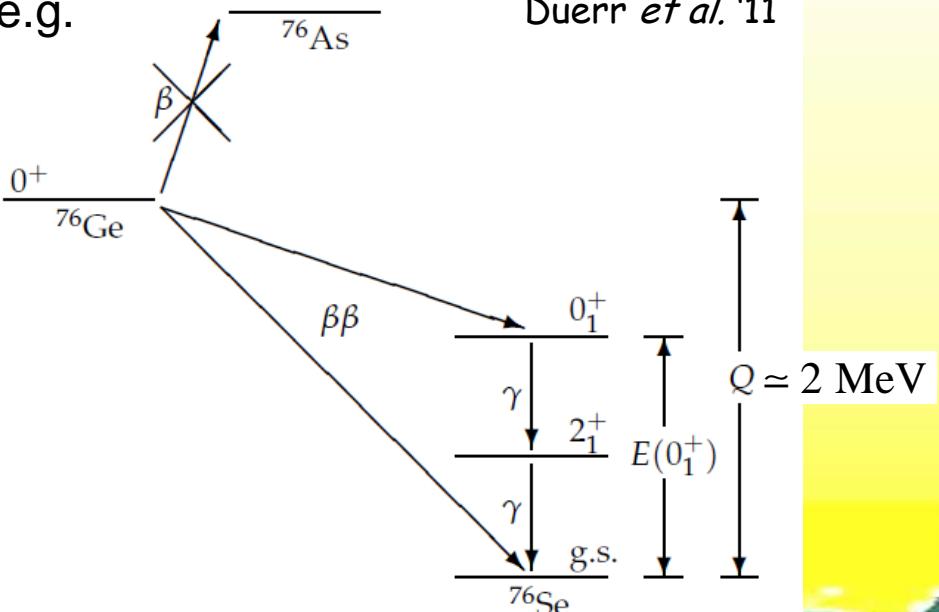
$$(T_{1/2}^{(\beta)})^{-1} \propto (G_F f_\pi^2)^2$$

two-neutrino  
double-beta decay



$$(T_{1/2}^{(2\nu2\beta)})^{-1} \propto (G_F f_\pi^2)^4$$

e.g.



Duerr *et al.* '11

too small to measure except when single-beta decay kinematically forbidden

$$T_{1/2}^{(2\nu2\beta)}({}^{76}\text{Ge} \rightarrow {}^{76}\text{Se}) = 1.84_{-0.10}^{+0.14} \cdot 10^{21} \text{ y}$$

GERDA Collab. '15

Table 1  $\beta^- \beta^-$  decay transitions for naturally occurring parent isotopes\*

Transition	$T_0$ (keV)	Abundance (%)	Excitation energy of first $2^+$ state (keV)**
$^{46}\text{Ca} \rightarrow ^{46}\text{Ti}$	985	0.0035	889
$^{48}\text{Ca} \rightarrow ^{48}\text{Ti}\dagger$	4272	0.187	984
$^{70}\text{Zn} \rightarrow ^{70}\text{Ge}$	1001	0.62	—
$^{76}\text{Ge} \rightarrow ^{76}\text{Se}$	2045	7.8	559
$^{80}\text{Se} \rightarrow ^{80}\text{Kr}$	136	49.8	—
$^{82}\text{Se} \rightarrow ^{82}\text{Kr}$	3005	9.2	776
$^{86}\text{Kr} \rightarrow ^{86}\text{Sr}$	1249	17.3	1077
$^{94}\text{Zr} \rightarrow ^{94}\text{Mo}$	1148	17.4	871
$^{96}\text{Zr} \rightarrow ^{96}\text{Mo}\dagger$	3350	2.8	778
$^{98}\text{Ru} \rightarrow ^{98}\text{Ru}$	111	24.1	—
$^{100}\text{Mo} \rightarrow ^{100}\text{Ru}$	3033	9.6	540
$^{104}\text{Ru} \rightarrow ^{104}\text{Pd}$	1301	18.7	556
$^{110}\text{Pd} \rightarrow ^{110}\text{Cd}$	2014	11.8	658
$^{114}\text{Cd} \rightarrow ^{114}\text{Sn}$	540	28.7	—
$^{116}\text{Cd} \rightarrow ^{116}\text{Sn}$	2808	7.5	1294
$^{122}\text{Sn} \rightarrow ^{122}\text{Te}$	358	4.56	—
$^{124}\text{Sn} \rightarrow ^{124}\text{Te}$	2278	5.64	603
$^{128}\text{Te} \rightarrow ^{128}\text{Xe}$	869	31.7	443
$^{130}\text{Te} \rightarrow ^{130}\text{Xe}$	2533	34.5	536
$^{134}\text{Xe} \rightarrow ^{134}\text{Ba}$	843	10.4	605
$^{136}\text{Xe} \rightarrow ^{136}\text{Ba}$	2481	8.9	819
$^{142}\text{Ce} \rightarrow ^{142}\text{Nd}$	1414	11.1	—
$^{146}\text{Nd} \rightarrow ^{146}\text{Sm}\dagger$	61	17.2	—
$^{148}\text{Nd} \rightarrow ^{148}\text{Sm}$	1928	5.7	550
$^{150}\text{Nd} \rightarrow ^{150}\text{Sm}$	3367	5.6	334
$^{154}\text{Sm} \rightarrow ^{154}\text{Gd}$	1250	22.6	123
$^{160}\text{Gd} \rightarrow ^{160}\text{Dy}$	1731	21.8	87
$^{170}\text{Er} \rightarrow ^{170}\text{Yb}$	655	14.9	84
$^{176}\text{Yb} \rightarrow ^{176}\text{Hf}$	1077	12.6	88
$^{186}\text{W} \rightarrow ^{186}\text{Os}$	489	28.6	137
$^{192}\text{Os} \rightarrow ^{192}\text{Pt}$	408	41.0	317
$^{198}\text{Pt} \rightarrow ^{198}\text{Hg}$	1043	7.2	412
$^{204}\text{Hg} \rightarrow ^{204}\text{Pb}$	414	6.9	—
$^{232}\text{Th} \rightarrow ^{232}\text{U}\S$	850	100	48
$^{238}\text{U} \rightarrow ^{238}\text{Pu}\ \$	1146	99.275	44

$$Q \geq 2m_e$$

pairing

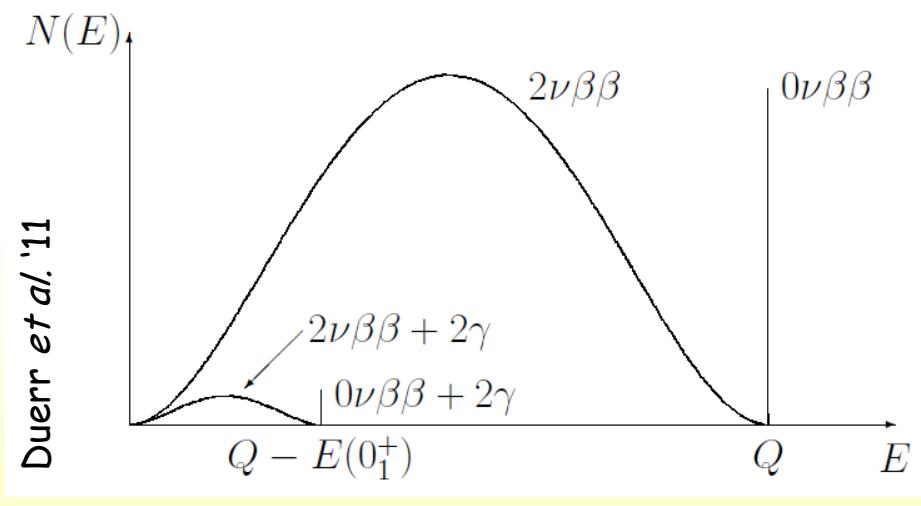
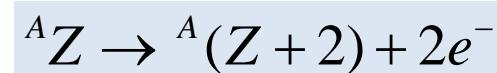


parent : even-even,  $J^P = 0^+$   
 daughter: even-even,  
 typically  $J^P = 0^+$  (g.s.)

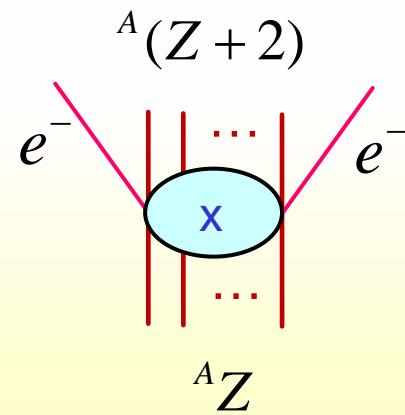
$$\Delta I = 2$$

Haxton + Stephenson '84

neutrinoless  
double-beta decay



$$\Delta L = 2$$

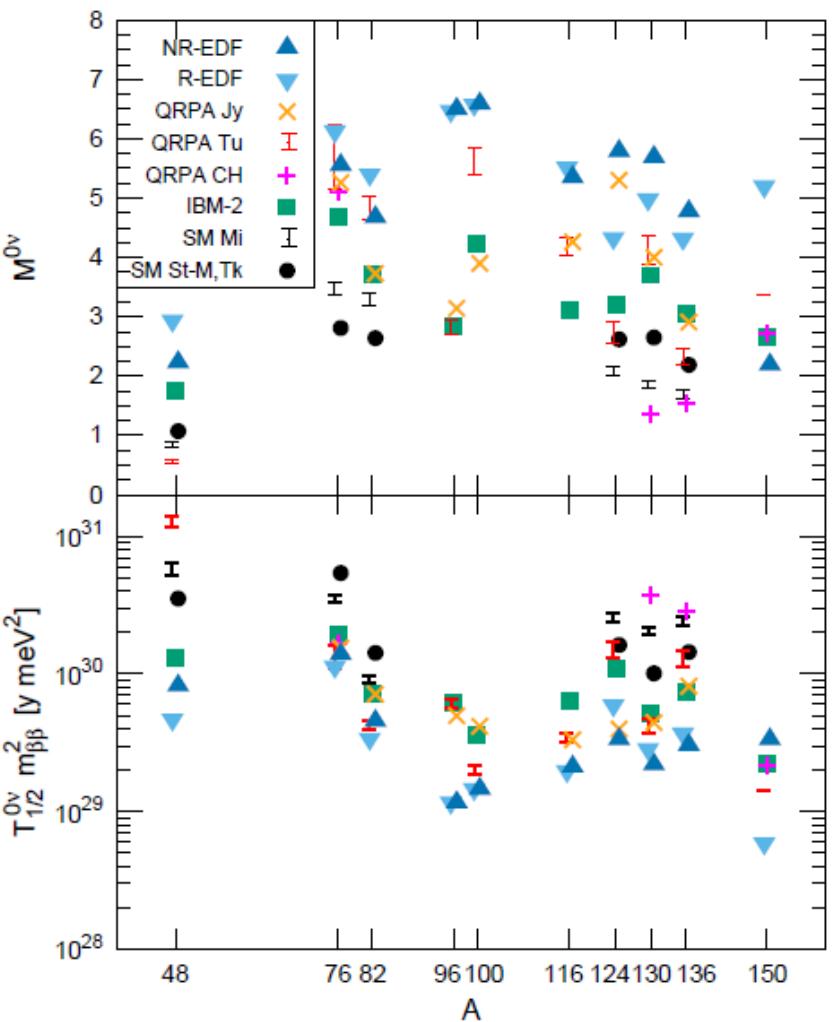


even rarer: e.g.,  $T_{1/2}^{(0\nu 2\beta)}({}^{76}\text{Ge} \rightarrow {}^{76}\text{Se}) > 8.0 \cdot 10^{25} \text{ y}$

GERDA-II Collab. '18

$$m_{\nu i} \lesssim M_{nuc} \implies \left( T_{1/2}^{(0\nu 2\beta)} \right)^{-1} \propto |M^{(0\nu)}|^2 |m_{\beta\beta}|^2$$

nuclear matrix element



effective  
Majorana mass

$$m_{\beta\beta} = \sum_{i=1}^n U_{ei}^2 m_{\nu i}$$

neutrino  
masses

PMNS matrix elements

$$\begin{cases} c_{ij} \equiv \cos \theta_{ij} \\ s_{ij} \equiv \sin \theta_{ij} \end{cases}$$

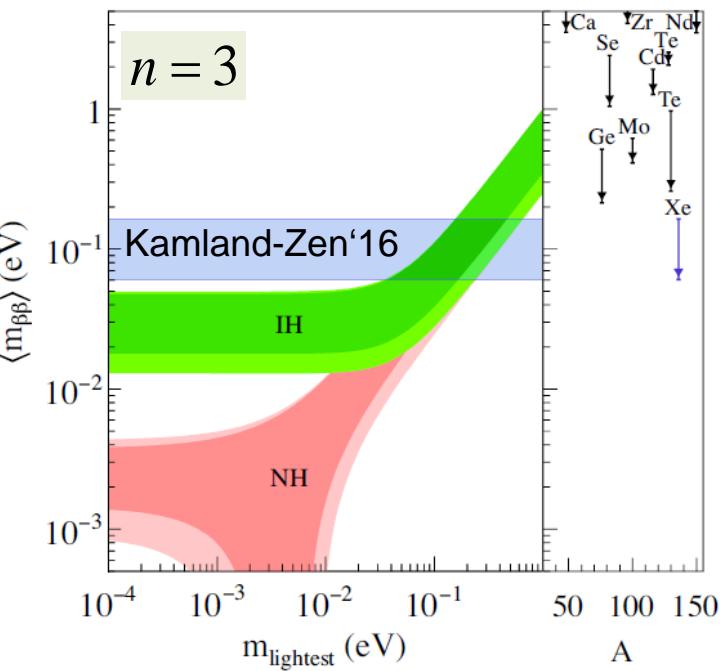
Majorana phases

Dirac phase

$$m_{\beta\beta} = m_{\nu 1} c_{12}^2 c_{13}^2 + m_{\nu 2} s_{12}^2 c_{13}^2 e^{i\alpha_{21}} + m_{\nu 3} s_{13}^2 e^{i(\alpha_{31}-2\delta)}$$

next-gen  
expts

Engel +  
Menéndez '17



major uncertainty: nuclear matrix element



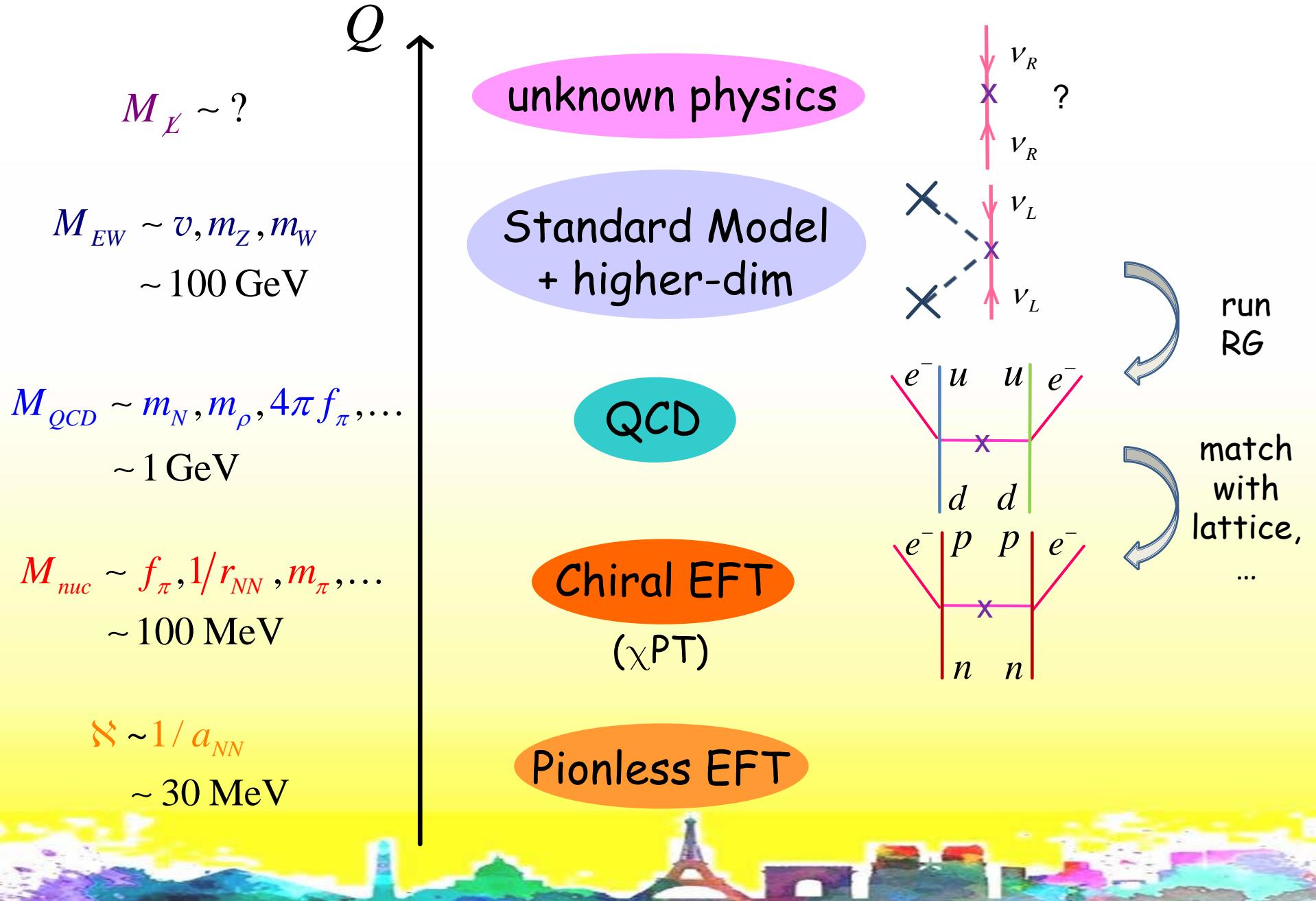
uncontrolled many-body approximations

enormous progress in *ab initio* calculations:  
 $^{48}\text{Ca}$  in horizon

input?

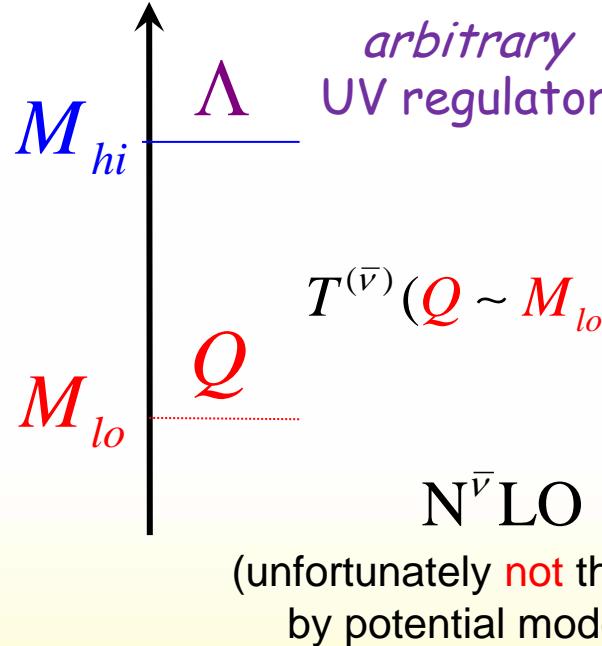
Chiral or Pionless EFT

# The Way of EFT



# Effective Field Theory <sup>C</sup>

momentum scales



non-analytic functions,  
from solution of dynamical eq.  
(e.g. Lippmann-Schwinger)

$$T^{(\bar{v})}(Q \sim M_{lo} \ll M_{hi}) \propto \sum_{\nu=0}^{\bar{v}} \left[ \frac{Q}{M_{hi}} \right]^{\nu} F^{(\nu)} \left( \frac{Q}{M_{lo}}, \frac{Q}{\Lambda}; \gamma_i^{(\nu)} \left( \frac{\Lambda}{M_{lo}}, \frac{M_{lo}}{M_{hi}} \right) \right) + \mathcal{O} \left( \frac{Q^{\bar{v}+1}}{M_{hi}^{\bar{v}+1}}, \frac{Q^{\bar{v}+1}}{M_{hi}^{\bar{v}} \Lambda} \right)$$

controlled

"low-energy constants"

RG invariance  
(absent for "chiral potentials")

(**OTHERWISE**, CUTOFF DEP NOT ERROR ESTIMATE)

$$\frac{\Lambda}{T^{(\bar{v})}} \frac{\partial T^{(\bar{v})}}{\partial \Lambda} = \mathcal{O} \left( \frac{Q^{\bar{v}+1}}{M_{hi}^{\bar{v}} \Lambda} \right)$$

model independent

(**OTHERWISE**, SENSITIVE TO HIGH-MOM DETAILS)



to minimize cutoff errors,  $\Lambda \gtrsim M_{hi}$   
for realistic error estimate,  $\Lambda \in [M_{hi}, \infty)$

# QCD (-LITE)

$$Q \ll M_{EW}$$

d.o.f.s

quarks:  $q = \begin{pmatrix} u \\ d \end{pmatrix}$       gluons:  $G_\mu^a$       (+ photon:  $A_\mu$ )

symmetries

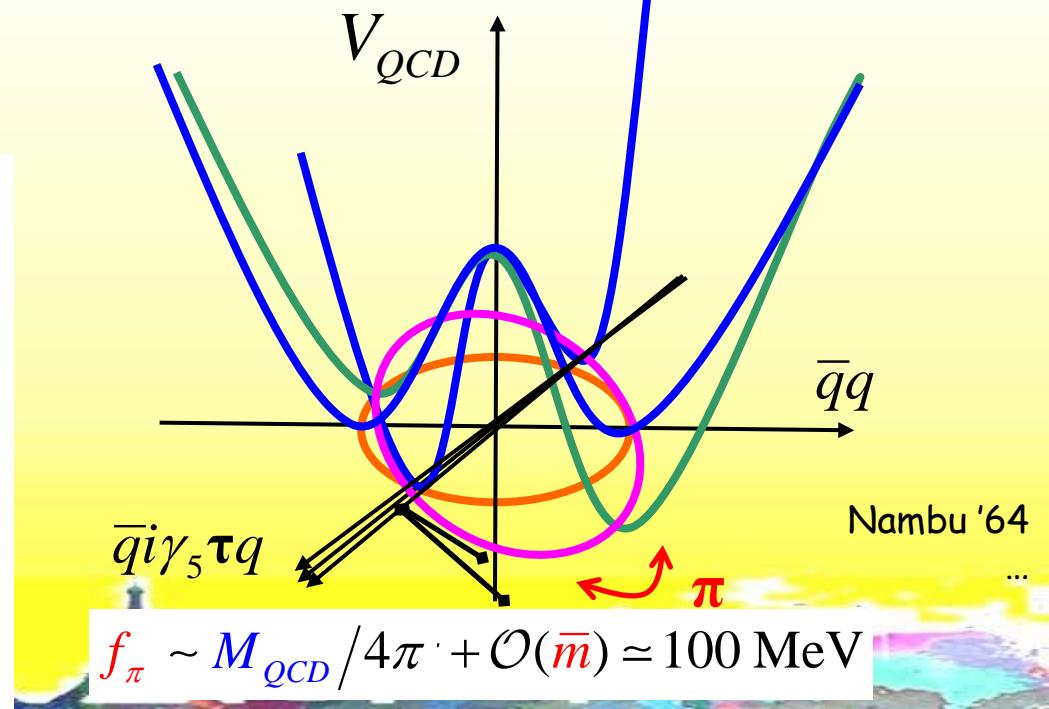
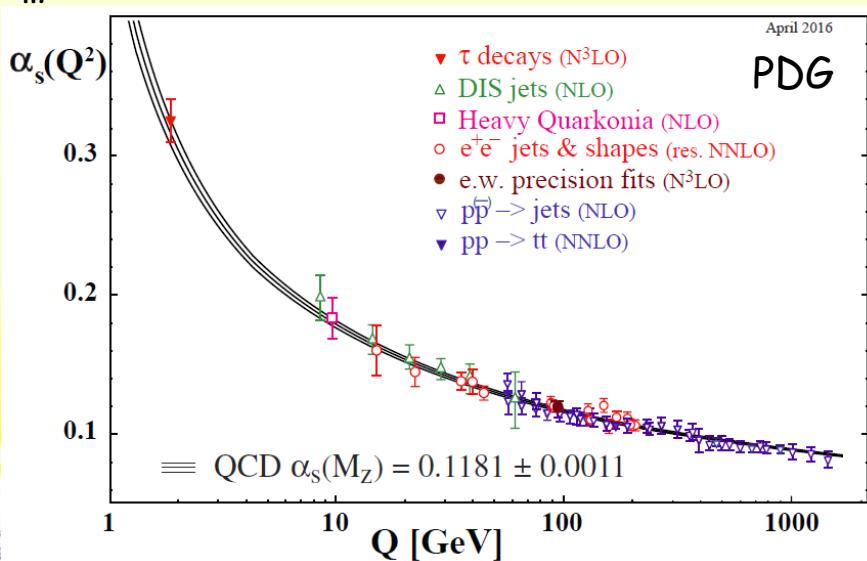
SO(3,1) global, SU(3)<sub>c</sub> (+U(1)<sub>em</sub>) gauge

$$\mathcal{L}_{QCD} = \underbrace{\bar{q}(i\partial + g_s G)}_{\text{Basic}} q - \frac{1}{2} \text{Tr } G^{\mu\nu} G_{\mu\nu} + \underbrace{\bar{m} \bar{q}(1 - \varepsilon \tau_3)}_{\text{Basic}} q + \dots$$

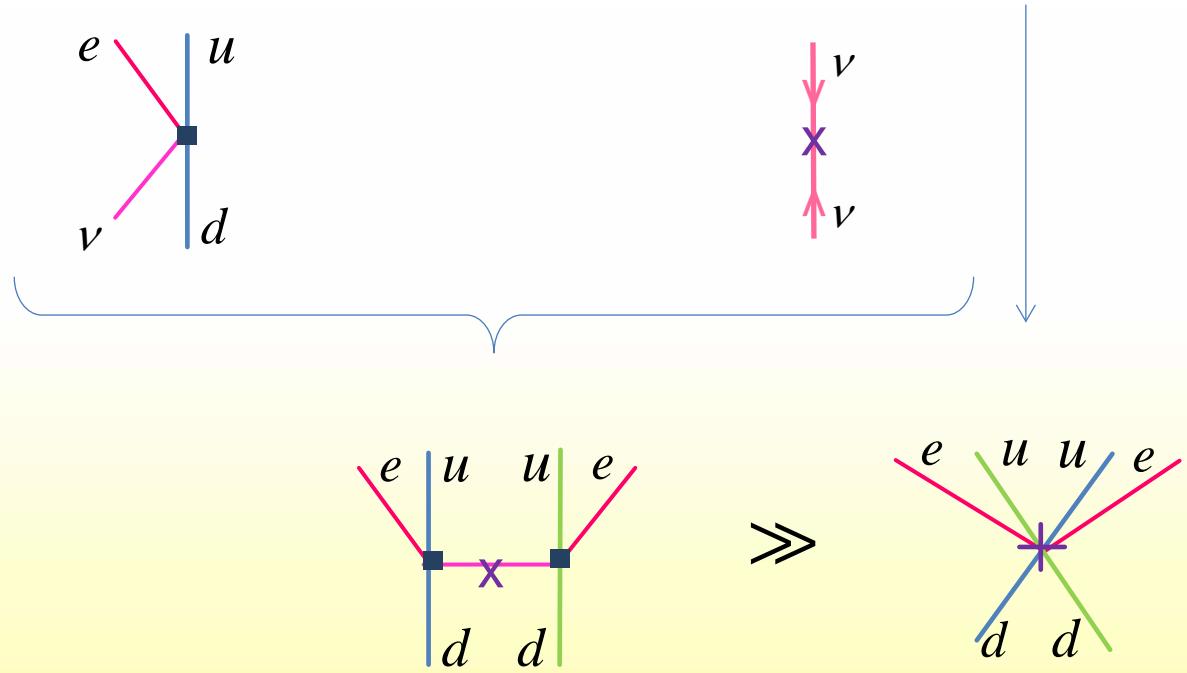
mass scales

$$M_{QCD} \sim m_N, m_\rho, 4\pi f_\pi, \dots \sim 1 \text{ GeV} \quad m_\pi \sim \sqrt{\bar{m} M_{QCD}} \simeq 140 \text{ MeV}$$

Gross + Wilczek '73  
Politzer '73



$$\mathcal{L}_{QCD} = \dots + \frac{G_F}{\sqrt{2}} V_{ud} \left( \bar{e}_L \gamma_\mu v_{eL} \bar{u}_L \gamma^\mu d_L + \text{H.c.} \right) - \frac{m_{\beta\beta}}{2} v_{eL}^T C v_{eL} + \dots$$

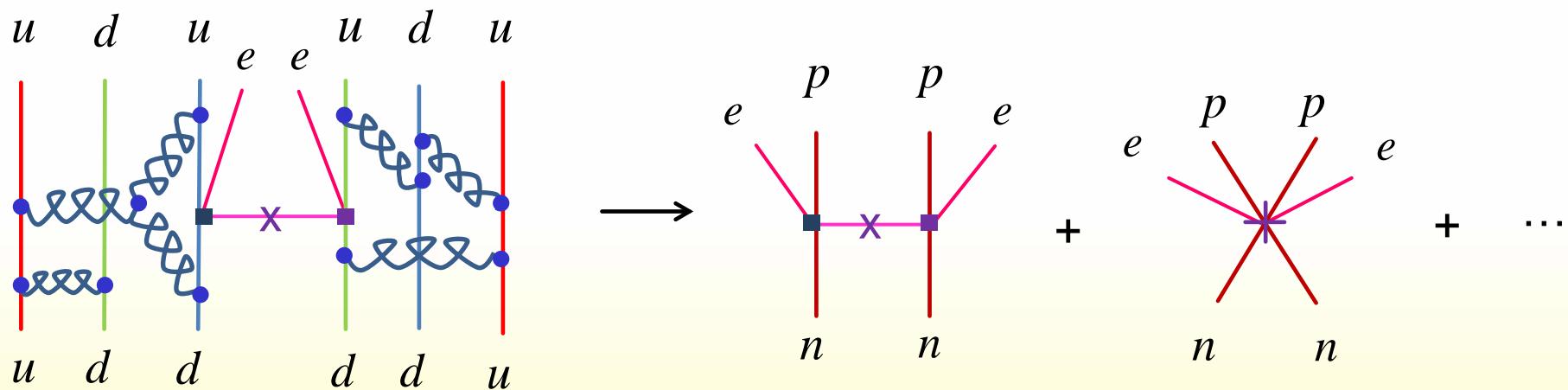


$$\propto G_F^2 \frac{m_{\beta\beta}}{Q^2}$$

$$\propto G_F^2 \frac{m_{\beta\beta}}{M_{EW}^2}$$

$Q \sim M_{QCD}$

$Q \ll M_{QCD}$



$$\propto G_F^2 \frac{m_{\beta\beta}}{Q^2}$$

$$\propto G_F^2 \frac{m_{\beta\beta}}{?^2}$$

$Q \sim m_\pi \ll M_{QCD}$

## Chiral EFT

d.o.f.s

nucleons:  $N = \begin{pmatrix} p \\ n \end{pmatrix}$

pions:  $\pi = \begin{pmatrix} (\pi^+ + \pi^-)/\sqrt{2} \\ i(\pi^+ - \pi^-)/\sqrt{2} \\ \pi^0 \end{pmatrix}$

(+ photon:  $A_\mu$ )

+ Deltas + Roper + ...?

symmetries

SO(3,1) global, SU(3)<sub>c</sub> (+U(1)<sub>em</sub>) gauge, ~~SU(2) × SU(2)~~ global  
(trivial)

$$\mathcal{L}_{\chi EFT} = \frac{1}{2} \left( \partial_\mu \pi \cdot \partial^\mu \pi - m_\pi^2 \pi^2 \right) + N^\dagger \left( i \partial_0 + \frac{\vec{\nabla}^2}{2m_N} \right) N + \frac{g_A}{2f_\pi} N^\dagger \vec{\sigma} \cdot \vec{\tau} N \cdot \vec{\nabla} \pi$$

$$+ C_0 N^\dagger N N^\dagger N + \dots$$

other spin/isospin,  
chiral partners,  
more derivatives and fields,  
powers of pion mass

expansion in:

$$\frac{Q}{M_{QCD}} \sim \begin{cases} Q/m_N & \text{non-relativistic} \\ Q/m_\rho, \dots & \text{multipole} \\ Q/4\pi f_\pi & \text{pion loop} \end{cases}$$

$Q \ll m_\pi$

## Pionless EFT

d.o.f.s

nucleons:  $N = \binom{p}{n}$  (+ photon:  $A_\mu$ )

symmetries

$SO(3,1)$  global,  $SU_c(3)$  (+ $U_{em}(1)$ ) gauge  
(trivial)

$$\mathcal{L}_{\pi EFT} = N^+ \left( i\partial_0 + \frac{\vec{\nabla}^2}{2m_N} \right) N + C_0 N^+ N N^+ N + D_0 N^+ N N^+ N N^+ N + \dots$$

more derivatives  
and fields,  
isospin violation

Classically the same as Chiral EFT minus pions,  
but renormalization different in general

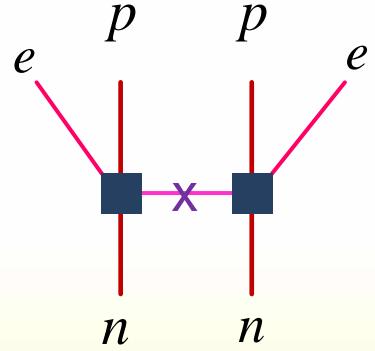
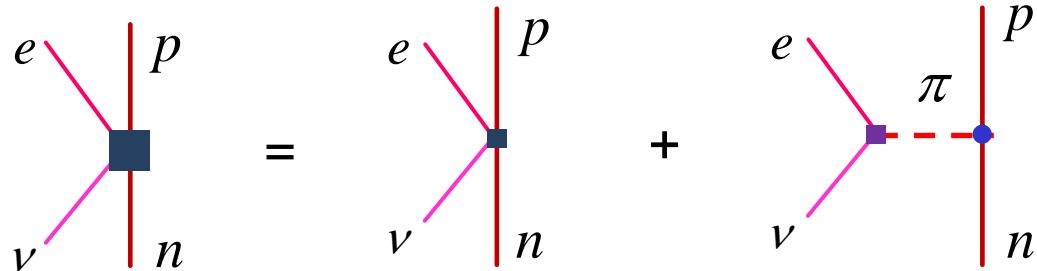
# Chiral EFT for definiteness:

$$\mathcal{L}_{\chi EFT} = \dots + \sqrt{2} \mathbf{G}_F V_{ud} \left\{ \bar{e}_L \gamma_\mu \nu_{eL} \left[ f_\pi \partial^\mu \pi^- - N^\dagger (\delta_0^\mu - g_A \delta_i^\mu \sigma^i) \tau^+ N \right] + \text{H.c.} \right\} + \dots$$



$$\mathcal{L}_{\chi EFT} = \dots - \frac{m_{\beta\beta}}{2} \nu_{eL}^T C \nu_{eL} + g_\nu G_F^2 V_{ud}^2 m_{\beta\beta} \left\{ \bar{e}_L C \bar{e}_L^T N^\dagger \tau^+ N N^\dagger \tau^+ N + \text{H.c.} \right\} + \dots$$





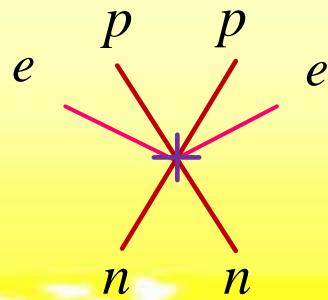
$$\propto 2 G_F^2 V_{ud}^2 m_{\beta\beta} V_\nu^{(0)}(\vec{q})$$

$$G_F V_{ud} \quad G_F V_{ud} f_\pi Q \frac{1}{Q^2} \frac{Q}{f_\pi}$$

$$S_{12}(\hat{q}) \equiv \vec{\sigma}_1 \cdot \hat{q} \vec{\sigma}_2 \cdot \hat{q} - \frac{1}{3} \vec{\sigma}_1 \cdot \vec{\sigma}_2$$

$$V_\nu^{(0)}(\vec{q}) = \frac{\tau_1^+ \tau_2^+}{\vec{q}^2} \left\{ 1 + g_A^2 \left[ S_{12}(\hat{q}) - \frac{2}{3} \vec{\sigma}_1 \cdot \vec{\sigma}_2 \right] - \frac{g_A^2 m_\pi^4}{(\vec{q}^2 + m_\pi^2)^2} \left[ S_{12}(\hat{q}) + \frac{1}{3} \vec{\sigma}_1 \cdot \vec{\sigma}_2 \right] \right\}$$

Cirigliano *et al.* '17

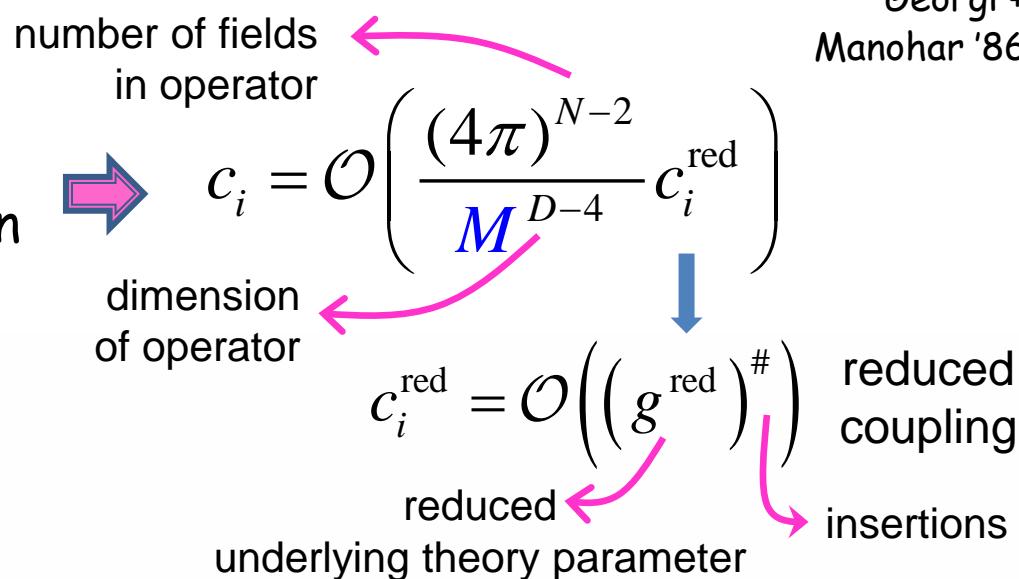


$$\propto 2 G_F^2 V_{ud}^2 m_{\beta\beta} V_{ct}^{(?)}(\vec{q})$$

$$V_{ct}^{(?)} = -g_\nu \tau_1^+ \tau_2^+$$

# naïve dimensional analysis (NDA)

## perturbative renormalization



e.g.

$$g_\nu G_F^2 V_{ud}^2 m_{\beta\beta} = \mathcal{O}\left(\frac{(4\pi)^4}{M_{QCD}^5} \left(g_\nu G_F^2 V_{ud}^2 m_{\beta\beta}\right)^{\text{red}}\right)$$

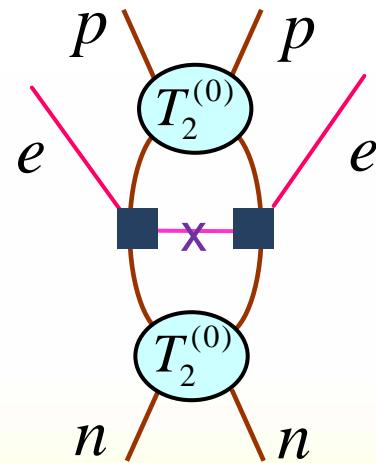
$$\left(g_\nu G_F^2 V_{ud}^2 m_{\beta\beta}\right)^{\text{red}} = \mathcal{O}\left(\left(G_F^2 V_{ud}^2\right)^{\text{red}} \left(m_{\beta\beta}\right)^{\text{red}}\right)$$

$$\left(G_F V_{ud}\right)^{\text{red}} = \mathcal{O}\left(\frac{M_{QCD}^2}{(4\pi)^2} G_F V_{ud}\right) \quad \left(m_{\beta\beta}\right)^{\text{red}} = \mathcal{O}\left(\frac{m_{\beta\beta}}{M_{QCD}}\right)$$

BUT... NUCLEAR AMPLITUDES NONPERTURBATIVE!

# Renormalization

LO



$$T_2^{(0)} = V_2^{(0)} + T_2^{(0)} V_2^{(0)}$$

The diagram illustrates the renormalization of the  $T_2^{(0)}$  vertex. It is shown as a sum of two terms: a bare vertex  $V_2^{(0)}$  and a correction term involving a loop of  $T_2^{(0)}$  and  $V_2^{(0)}$  vertices.

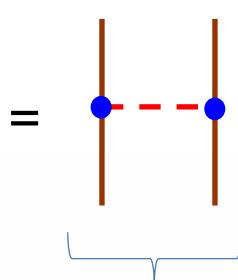
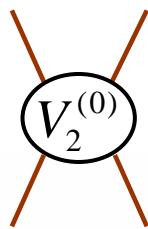
LO

Weinberg '91

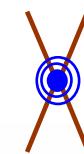
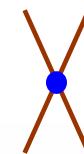
$S = 0, 1$   
 $l = 0$

$S = 0$   
 $l = 0$

Kaplan, Savage  
+ Wise '96



+



+

$S = 1$   
 $l \lesssim 2$

Nogga, Timmermans + vK '05  
Birse '06

$$= \frac{4\pi}{m_N M_{NN}} \boldsymbol{\tau}_1 \cdot \boldsymbol{\tau}_2 \left[ S_{12}(\hat{q}) + \frac{1}{3} \vec{\sigma}_1 \cdot \vec{\sigma}_2 \right] \left[ 1 - \frac{m_\pi^2}{\vec{q}^2 + m_\pi^2} \right]$$

singular, requires counterterms  
in waves where it is iterated

$$= \frac{4\pi}{m_N M_{NN}} \left\{ C_0(^3S_1) + C_0(^1S_0) + \frac{m_\pi^2}{M_{NN}^2} D_2(^1S_0) \right.$$

$$\left. + \frac{p'p}{M_{NN}^2} [C_2(^3P_0) + C_2(^3P_2)] + ? \right\}$$

larger than NDA!

$$M_{NN} \equiv \frac{4\pi f_\pi}{g_A^2 m_N} f_\pi \sim f_\pi$$

Kaplan, Savage + Wise '98

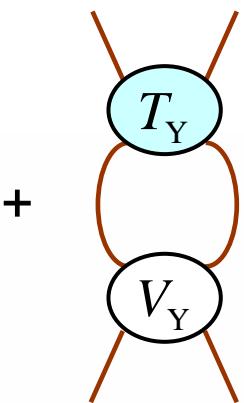
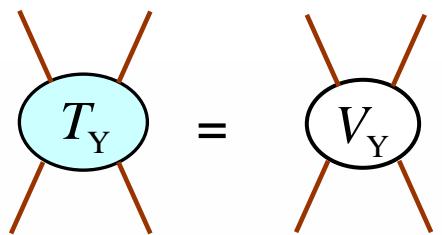
subLOs

NDA relative to LO (except spin-singlet  $S$  wave)

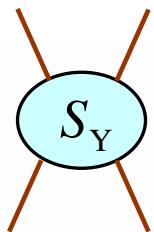
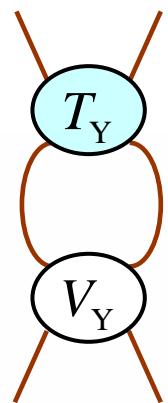
Long + vK '07  
Long + Yang '12

$$^1S_0 \quad V_2^{(0)}(\vec{q}) = \frac{4\pi}{m_N M_{NN}} \left[ C_0(^1S_0) + \frac{m_\pi^2}{M_{NN}^2} D_2(^1S_0) + 1 - \frac{m_\pi^2}{\vec{q}^2 + m_\pi^2} \right] \equiv \frac{4\pi}{m_N M_{NN}} \tilde{C} + V_Y(\vec{q})$$

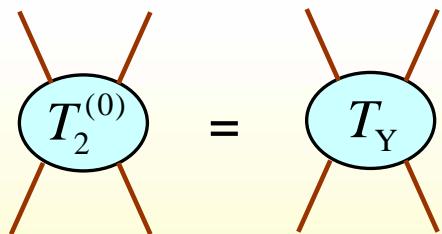
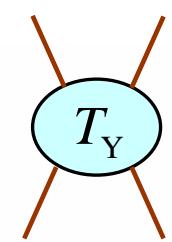
singular regular



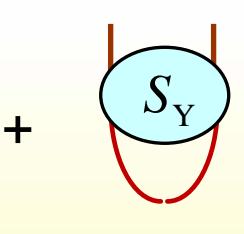
+



+

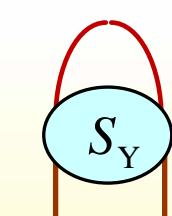


well-defined



well-defined

$$\times (\bullet^{-1} - \underbrace{\quad}_{S_Y})^{-1} \times S_Y$$



Kaplan, Savage  
+ Wise '96  
Long + Yang '13

$$\propto \Lambda + \# \frac{m_\pi^2}{M_{NN}} \ln \left( \frac{\Lambda}{M_{NN}} \right) + \# \frac{k^2}{\Lambda} + \dots$$

need for counterterms:

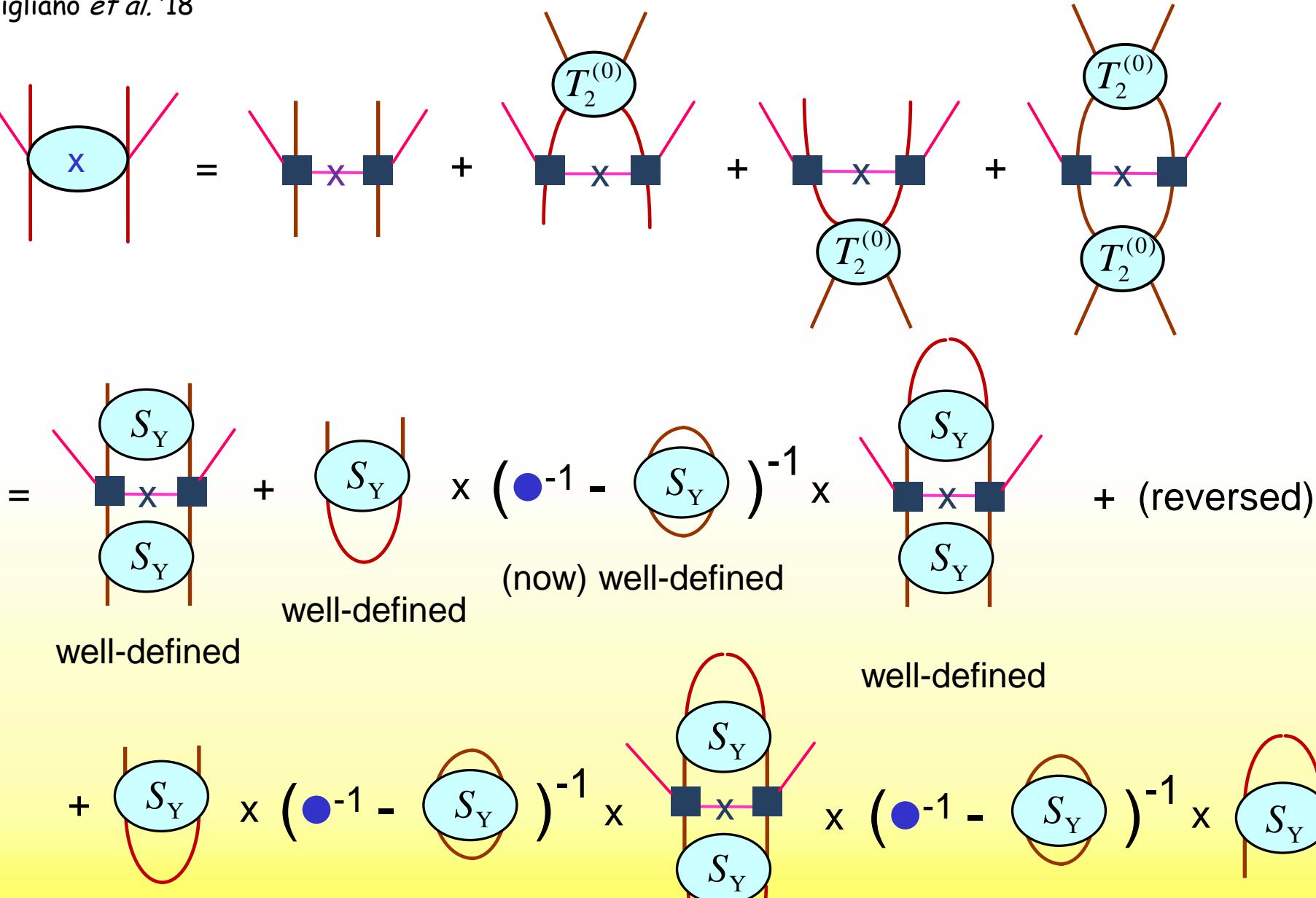
two at LO

one at NLO

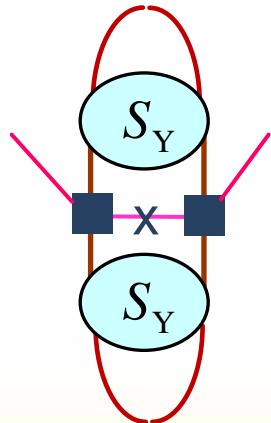
LO

dim reg with min sub:  $\tilde{C}^{-1}(\mu) = -\# \frac{m_\pi^2}{M_{NN}} \ln \left( \frac{\mu}{\mu_*} \right) + \dots$

determined from  
scattering length  
at physical pion mass



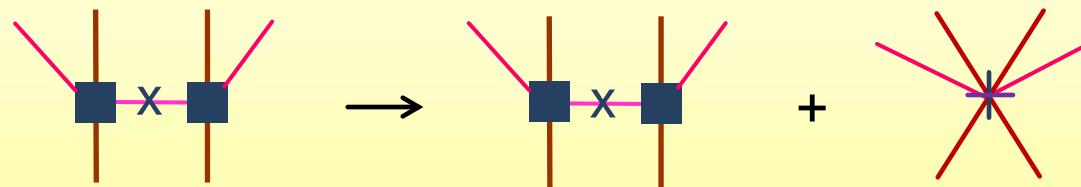
$$V_\nu^{(0)}(\vec{q}) = \frac{\tau_1^+ \tau_2^+}{\vec{q}^2} \left\{ 1 + 2g_A^2 + \frac{g_A^2 m_\pi^4}{(\vec{q}^2 + m_\pi^2)^2} \right\}$$



$$= - \left( \frac{m_N}{4\pi} \right)^2 \frac{1 + 2g_A^2}{2} \left[ \Delta + \ln \frac{\mu^2}{-(|\vec{p}| + |\vec{p}'|)^2 + i0^+} \right] + \dots$$

$$\Delta = \frac{1}{d-4} - C_E + \ln(4\pi) + 1$$

counterterm needed!



$$V_{\text{ct}}^{(0)} = -g_\nu \tau_1^+ \tau_2^+$$

$$= \dots + S_Y \times (\bullet^{-1} - S_Y)^{-1} \times \bullet^{-1} \times + \times \bullet^{-1} \times (\bullet^{-1} - S_Y)^{-1} \times S_Y$$

$$\rightarrow + \bullet^{-1} \times + \times \bullet^{-1}$$

dim reg with  
min sub

$$= \left( \frac{m_N}{4\pi} \right)^2 \left[ \frac{M_{NN}^2 g_\nu(\mu)}{\tilde{C}^2(\mu)} - \frac{1+2g_A^2}{2} \ln \frac{\mu^2}{-(|\vec{p}|+|\vec{p}'|)^2 + i0^+} \right] + \dots$$

$$\Rightarrow \mu \frac{d}{d\mu} \frac{M_{NN}^2 g_\nu(\mu)}{\tilde{C}^2(\mu)} = 1 + 2g_A^2 \Rightarrow g_\nu = \mathcal{O}\left(\frac{1}{M_{NN}^2}\right) \gg \mathcal{O}\left(\frac{1}{M_{QCD}^2}\right)$$

# Alternative: numerical solution of Schrödinger equation in coordinate space

$$\tilde{C} \delta^{(3)}(\vec{r}) \rightarrow \tilde{C}(R) \delta_R^{(3)}(\vec{r}) \quad \Rightarrow \quad \tilde{C}(R) = \# R + \# \frac{m_\pi^2}{M_{NN}} R^2 \ln\left(\frac{R}{R_*}\right) + \dots \quad \text{Beane, Bedaque, Savage + vK '02}$$

here  $\delta_R^{(3)}(\vec{r}) = \frac{e^{-r^2/R^2}}{\pi^{3/2} R^3}$

$$g_\nu \delta^{(3)}(\vec{r}) \rightarrow g_\nu(R) \delta_R^{(3)}(\vec{r})$$

determined from scattering length

$$A_{\Delta L=2}^{(\nu)} = - \int d^3 r \psi_{\vec{p}'}^-(\vec{r}) V_\nu^{(0)}(\vec{r}) \psi_{\vec{p}}^+(\vec{r})$$

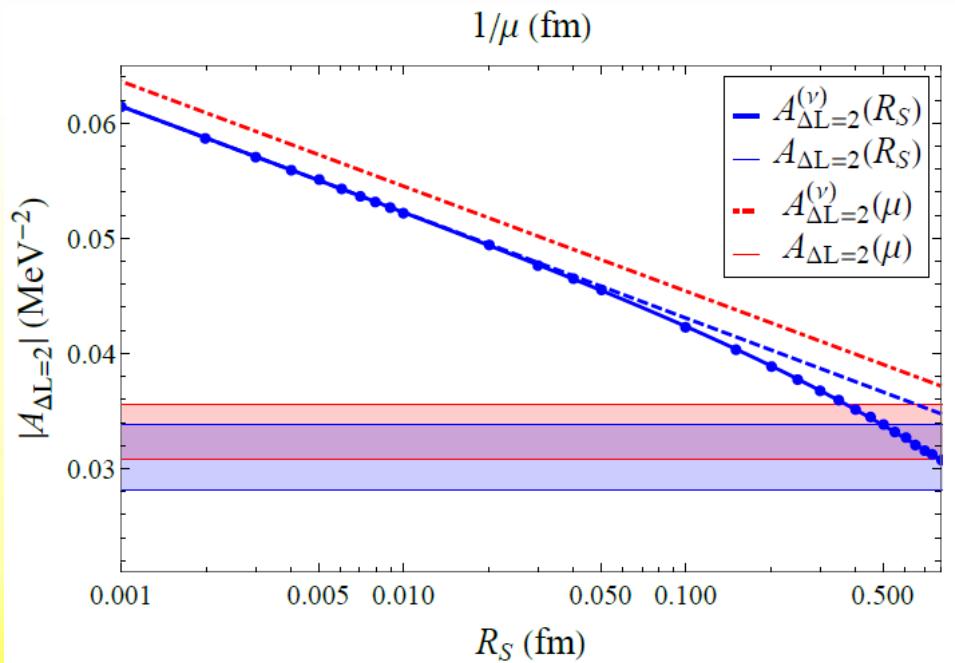
$$A_{\Delta L=2}^{(NN)} = - \int d^3 r \psi_{\vec{p}'}^-(\vec{r}) V_{\text{ct}}^{(0)}(\vec{r}) \psi_{\vec{p}}^+(\vec{r})$$

$$A_{\Delta L=2} = A_{\Delta L=2}^{(\nu)} + A_{\Delta L=2}^{(NN)}$$



$$\frac{M_{NN}^2 g_\nu(\mu)}{\tilde{C}^2(\mu)} \simeq - \left(1 + 2g_A^2\right) \ln\left(\frac{R}{R_\nu}\right) + \# R + \dots$$

determined how?



$$|\vec{p}| = 1 \text{ MeV} \quad |\vec{p}'| = 38 \text{ MeV} \quad \vec{p}_{e1} = \vec{p}_{e2} = 0$$

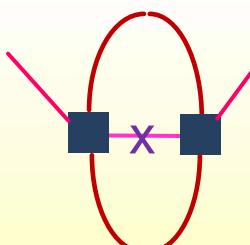
higher waves

well defined without enhanced counterterms

Perturbative pions? LO same as Pionless EFT

## Renormalization in Pionless EFT

Cirigliano *et al.* '18

$$\left. \begin{aligned} V_2^{(0)} &= \frac{4\pi}{m_N M_{lo}} C_0 \\ V_\nu^{(0)}(\vec{q}) &= \frac{\tau_1^+ \tau_2^+}{\vec{q}^2} \left(1 + 3g_A^2\right) \end{aligned} \right\} = - \left( \frac{m_N}{4\pi} \right)^2 \frac{1 + 3g_A^2}{2} \left[ \Delta + \ln \frac{\mu^2}{-(|\vec{p}| + |\vec{p}'|)^2 + i0^+} \right] + \dots$$


$$V_{ct}^{(0)} = -g_\nu \tau_1^+ \tau_2^+ \rightarrow \mu \frac{d}{d\mu} \frac{M_{lo}^2 g_\nu(\mu)}{C_0^2(\mu)} = 1 + 3g_A^2 \rightarrow g_\nu = \mathcal{O}\left(\frac{1}{M_{lo}^2}\right) \gg \mathcal{O}\left(\frac{1}{M_{hi}^2}\right)$$

# LEC Estimate

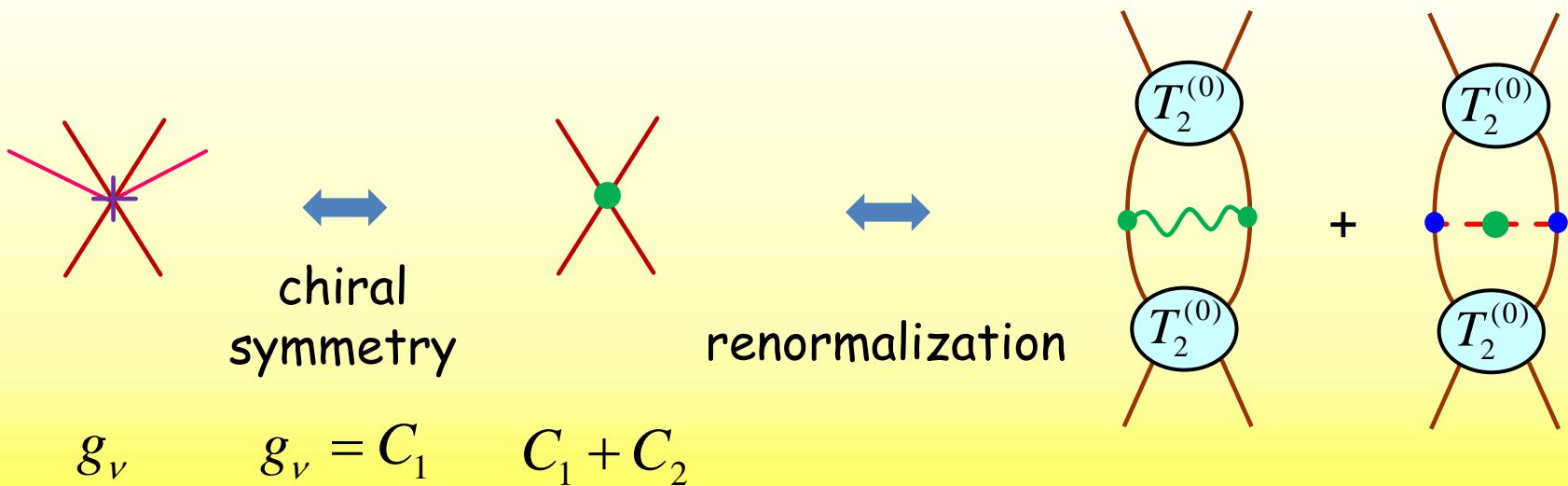
cf. Nicholson *et al.* '16'18  
Shanahan *et al.* '17

- eventually, match to lattice QCD L-violating amplitude as done in strong-interacting sector

cf. Barnea *et al.* '15

...

- for now, estimate from connection with isospin violation



$$g_\nu \propto \left\langle pp \left| \frac{1}{\vec{q}^2} \right| nn \right\rangle \quad \text{same as electromagnetism for } I=2$$

$$\left\{ \begin{array}{l} O_1 = N^\dagger u^\dagger Q_L u N N^\dagger u^\dagger Q_L u N - \frac{1}{6} \text{Tr} \left( u^{\dagger 2} Q_L u^2 Q_L \right) N^\dagger \boldsymbol{\tau} N \cdot N^\dagger \boldsymbol{\tau} N + (L \leftrightarrow R) \\ O_2 = 2 \left[ N^\dagger u^\dagger Q_L u N N^\dagger u Q_R u^\dagger N - \frac{1}{6} \text{Tr} \left( u^{\dagger 2} Q_L u^2 Q_R \right) N^\dagger \boldsymbol{\tau} N \cdot N^\dagger \boldsymbol{\tau} N \right] \end{array} \right.$$

$$u = \exp(i\boldsymbol{\tau} \cdot \boldsymbol{\pi}/2f_\pi) \quad \left\{ \begin{array}{ll} \text{E\&M} & Q_L = Q_R = \frac{\tau_3}{2} \\ \text{L violation} & Q_L = \tau^+ \quad Q_R = 0 \end{array} \right.$$

$$\rightarrow \mathcal{L}_{\chi EFT} = \dots + \frac{\pi}{4} \alpha (C_1 + C_2) \left[ N^\dagger \tau_3 N N^\dagger \tau_3 N - \frac{1}{3} N^\dagger \boldsymbol{\tau} N \cdot N^\dagger \boldsymbol{\tau} N \right]$$

$$+ G_F^2 V_{ud}^2 m_{\beta\beta} (C_1) \bar{e}_L C \bar{e}_L^T N^\dagger \tau^+ N N^\dagger \tau^+ N + \dots$$

$$= g_\nu$$

multi-pion E&M interactions  
can separate  $C_1$  and  $C_2$

... but difficult.  
for now:

estimate  $C_1 + C_2$  from  $a_{\text{CIB}} = \frac{a_{pp} + a_{nn}}{2} - a_{np} \simeq 10.3 \text{ fm}$

assume  $C_1 \sim C_2$

uncontrolled error

$V_2^{(0)}$  →  $V_2^{(0)}$  + +

$$\frac{4\pi}{m_N M_{NN}} + \frac{4\pi}{m_N M_{NN}} \frac{\alpha m_N M_{NN}}{Q^2} + \left( \frac{Q}{f_\pi} \right)^2 \frac{1}{Q^4} \frac{\alpha M_{QCD}^2}{4\pi} \sim \frac{4\pi}{m_N M_{NN}} \frac{\alpha m_N M_{NN}}{Q^2}$$

vK '93

Friar, Goldman + vK '96

...

LO for  $Q \lesssim \sqrt{\alpha m_N M_{NN}} \sim 30 \text{ MeV}$

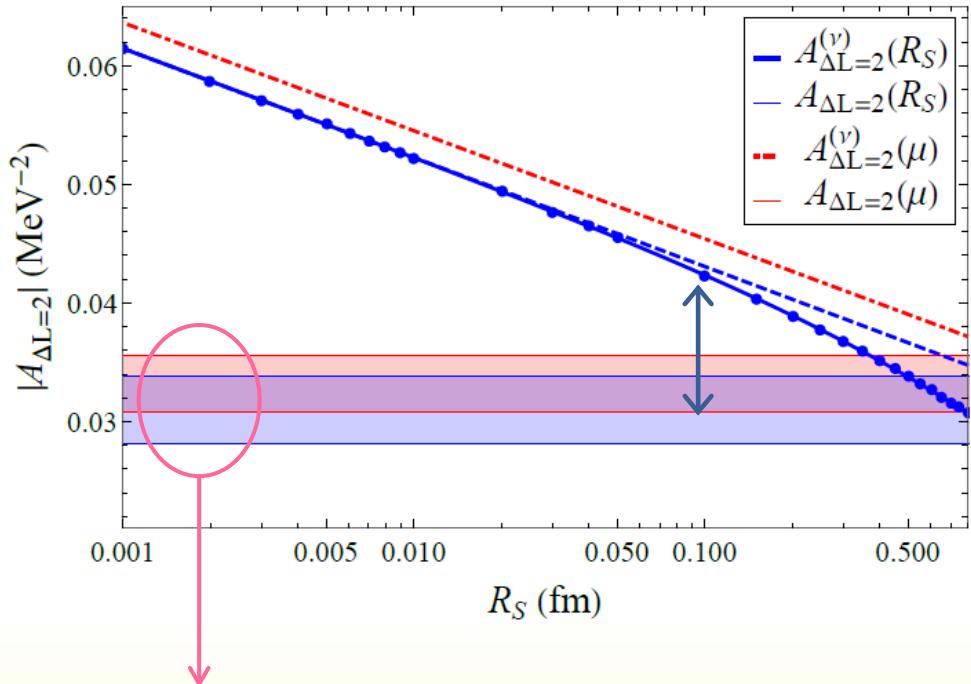
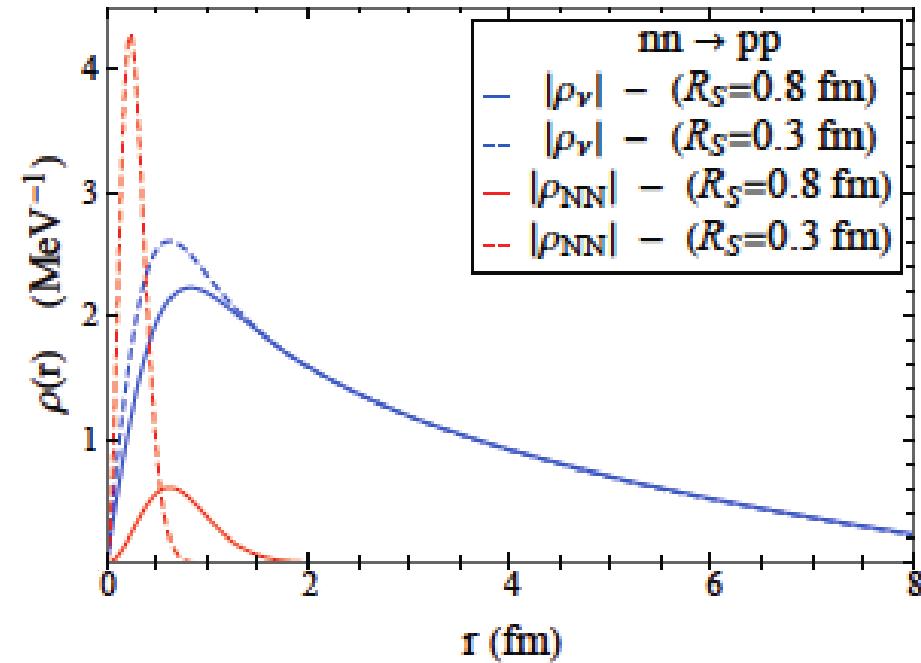
$$\mu \frac{d}{d\mu} \left[ \frac{M_{NN}^2}{\tilde{C}^2(\mu)} \frac{C_1(\mu) + C_2(\mu)}{2} \right] = 1 + g_A^2 \frac{m_{\pi^\pm}^2 - m_{\pi^0}^2}{e^2 f_\pi^2}$$

e.g.  $\left. \frac{M_{NN}^2}{\tilde{C}^2(\mu)} \frac{C_1(\mu) + C_2(\mu)}{2} \right|_{\mu=m_\pi} \approx 5$  or  $\left. \frac{M_{NN}^2}{\tilde{C}^2(\mu)} \frac{C_1(\mu) + C_2(\mu)}{2} \right|_{R=0.5 \text{ fm}} \approx 4$

$1/\mu \text{ (fm)}$ 

- $A_{\Delta L=2}^{(\nu)} = -\int d^3r \psi_{\vec{p}'}^- (\vec{r}) V_\nu^{(0)} (\vec{r}) \psi_{\vec{p}}^+ (\vec{r})$
- $A_{\Delta L=2}^{(NN)} = -\int d^3r \psi_{\vec{p}'}^- (\vec{r}) V_{\text{ct}}^{(0)} (\vec{r}) \psi_{\vec{p}}^+ (\vec{r})$
- $A_{\Delta L=2} = A_{\Delta L=2}^{(\nu)} + A_{\Delta L=2}^{(NN)}$

$$A_{\Delta L=2} = \int dr \rho(r)$$



$$C_1(\mu) = C_2(\mu) \text{ for } \mu \in [0.002, 0.8] \text{ fm}$$

$$\left. \frac{A_{\Delta L=2}^{(NN)}}{A_{\Delta L=2}^{(\nu)}} \right|_{R=0.1 \text{ fm}} \simeq 0.3$$

# *Ab Initio Example*

cf. Pastore *et al.* '18

Variational Monte Carlo

AV18+UIX

Wiringa, Stoks + Schiavilla '95  
Pieper '08

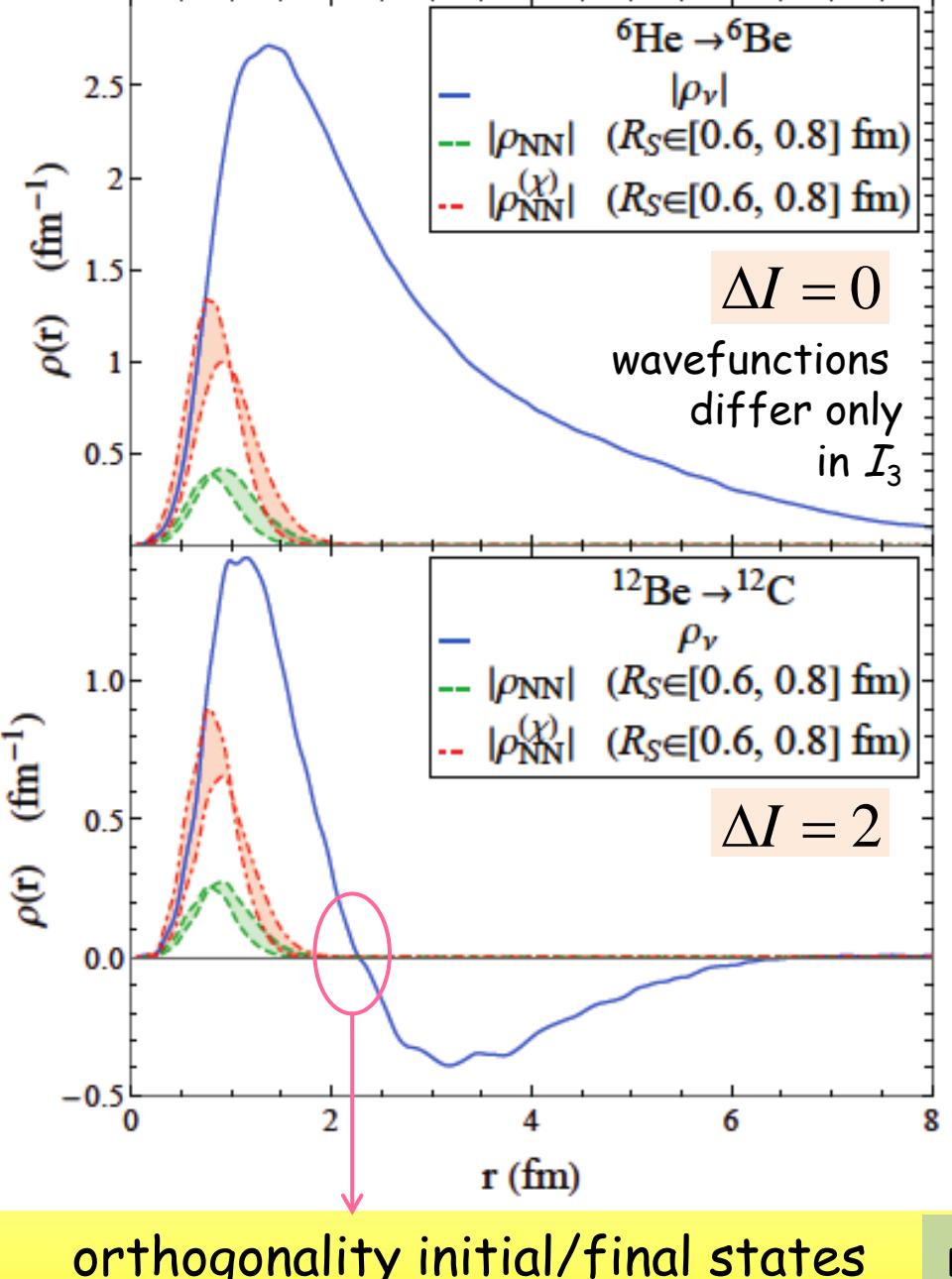
single-beta decay:  
agrees with experiment  $\leq 10\%$   
for  $A \leq 10$   
Pastore *et al.* '17

uncontrolled  
error

three  
strategies  
for  
short-range  
contribution

- our extraction
- fit to phase shifts from a chiral potential  
Piarulli *et al.* '14'16
- replacement with AV18's short-range CIB

similar  
results



$$\frac{A_{\Delta L=2}^{(NN)}}{A_{\Delta L=2}^{(\nu)}} \approx 0.1$$

$$\frac{A_{\Delta L=2}^{(NN)}}{A_{\Delta L=2}^{(\nu)}} \approx 0.3 - 0.6$$

Šimkovic *et al.* '08  
Menéndez *et al.* '09

robust feature of realistic transitions

# Discussion

## ❖ why "new"?

{ correlations at distances  $\lesssim 1/M_{QCD}$   
not accounted for internucleon potential

→ not the same as correlations missed in single-particle basis

cf. Miller + Spencer '76

Haxton + Stephenson '84

...

## ❖ why "leading"?

needed for the model-independent definition  
of light-neutrino exchange

→ not the same as a model for a form-factor refinement

Vergados '81

(e.g. a  $\sim 10\%$  in ab initio calculations)

Pastore *et al.* '18

...

...

**However,**  
exactly how important depends on  
effective scale in (consistently derived)  
strong-interaction potential  
in many-body environment

*N.B.*  
Range of effect **NOT** smaller than  
that of the internucleon interaction

perspectives for implementation  
in realistic nuclei?



# Conclusion

Effective field theory allows us to connect  
B - L-violating physics beyond the Standard Model  
and nuclear physics in a controlled and systematic way

A leading QCD-range contribution to  
neutrinoless double-beta decay can be identified  
from renormalization

Proper determination requires matching with lattice QCD,  
but an estimate can be obtained  
from electromagnetic nuclear processes

*Ab initio* calculations in light nuclei are consistent with  
power-counting expectations