Electroweak processes in nuclei

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"From nucleons to nuclei: enabling discovery for neutrinos, dark matter and more", INT workshop, Seattle, WA, June 2018

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Outline

- Low-energy nuclear physics for solar neutrino generation: radiative capture reactions
- GeV-neutrino—nucleus reactions for base-line neutrino experiment: neutral-current induced photon production
- Hadronic physics for base-line neutrino experiment: weak-Compton scattering and nucleon form factors
- Dark-photon explanation in Be-8 anomaly
- Summary

Solar neutrinos: radiative capture reactions

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${}^{7}_{4}Be + p \rightarrow {}^{8}_{5}B + \gamma$: basics

- B8: a p-wave **shallow** bound state
- Proton-Be s-wave has large scattering lengths
- Strong Coulomb effect

$$
\frac{7}{4}Be + p \rightarrow \frac{8}{5}B + \gamma: \text{picture}
$$
\n
$$
\boxed{AMP \sim \int_{>A^{-1}}^{+\infty} dr \psi_f(r)r\psi_i(r) + \int_0^{A^{-1}} dr \psi_f(r)r\psi_i(r)}
$$
\nS,D

$$
{}_{4}^{7}Be + p \rightarrow {}_{5}^{8}B + \gamma:picture
$$
\n
$$
{}_{AMP\sim} \int_{\rho}^{+\infty} dr \psi_{f}(r) r \psi_{i}(r) + \int_{0}^{\Lambda^{-1}} dr \psi_{f}(r) r \psi_{i}(r)
$$

9 parameters: scattering lengths, effective ranges, ANCs, and short-distance contact terms

$$
\int_{0}^{1} \frac{1}{\sqrt{1-\frac{1}{2}}}\int_{0}^{\frac{1}{2}} \frac{1}{\sqrt{1-\frac{1}{2}}}\int_{0}^{\frac{1}{
$$

S,D

$$
{}_{4}^{7}Be + p \rightarrow {}_{5}^{8}B + \gamma:picture
$$
\n
$$
{}_{AMP\sim} \int_{\rho}^{+\infty} dr \psi_{f}(r) r \psi_{i}(r) + \int_{0}^{\Lambda^{-1}} dr \psi_{f}(r) r \psi_{i}(r)
$$

9 parameters: scattering lengths, effective ranges, ANCs, and short-distance contact terms

Initial state interaction is similar to the final state interaction in neutrino—nucleus reaction

S,D

$$
\frac{7}{4}Be + p \rightarrow \frac{8}{5}B + \gamma: \text{picture}
$$
\n
$$
\lim_{\Delta M^{p} \to \int_{\Delta \Lambda^{-1}}^{\infty} dr \psi_{f}(r)r\psi_{i}(r) + \int_{0}^{\Lambda^{-1}} dr \psi_{f}(r)r\psi_{i}(r) \rangle
$$
\n9 parameters: scattering lengths, effective ranges,
\nANCs, and short-distance contact terms
\n<sup>Initial state interaction is similar to the final state
\ninteraction in neutron–nucleus reaction
\ninteraction in neutron–nucleus reaction
\n
$$
\sum_{\text{on}} \sum_{\text{on}} \sum_{\text{off}} \sum_{\text{off
$$</sup>

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 $\left($

 $\rm (II)$

${}^{7}_{4}Be + p \rightarrow {}^{8}_{5}B + \gamma$: comparisons

The EFT at NLO reproduces other models by 1% below 1 MeV • **Other models can be "projected" into EFT parameter space.**

X.Z., K. Nollett, and D. Phillips, 2018

Bayesian inference:

$$
\mathrm{pr}(\boldsymbol{g},\{\xi_i\}|D;T;I) = \mathrm{pr}(D|\boldsymbol{g},\{\xi_i\};T;I)\,\mathrm{pr}(\boldsymbol{g},\{\xi_i\}|I)
$$

Bayesian inference:

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X.Z., K. Nollett, and D. Phillips, PLB (2015)

Bayesian inference:

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X.Z., K. Nollett, and D. Phillips, PLB (2015)

Bayesian inference:

X.Z., K. Nollett, and D. Phillips, PLB (2015)

X.Z., K. Nollett, and D. Phillips (in preparation)

$$
{}^{3}_{2}\text{He} + {}^{4}_{2}\text{He} \rightarrow {}^{7}_{4}\text{Be} + \gamma
$$

$$
\frac{Q_{low}}{\Lambda} \approx 0.4
$$

$$
\eta = \frac{Z_3 Z_4 \alpha_{EM} M_R}{Q_{low}} \approx 0.7
$$

X.Z., K. Nollett, and D. Phillips (in preparation)

${}_{2}^{3}$ He + ${}_{2}^{4}$ He → ${}_{4}^{7}$ Be + γ: new avenue to constrain S(0)

 $d\sigma$ $d\Omega$ $\propto 1 + A_2 \cos^2 \theta$

${}_{2}^{3}$ He + ${}_{2}^{4}$ He → ${}_{4}^{7}$ Be + γ: new avenue to constrain S(0)

$$
\frac{d\sigma}{d\Omega} \propto 1 + A_2 \cos^2 \theta
$$

Halo-EFT+Bayesian inference can find valuable correlations to guide experiments

${}_{2}^{3}$ He + ${}_{2}^{4}$ He → ${}_{4}^{7}$ Be + γ: unexpected

Capture data constrains scattering parameters

Base-line neutrino experiment: neutral-current induced photon production

MiniBooNE event excess

MiniBooNE Collaboration (2009, 2018)

MiniBooNE event excess

MiniBooNE event excess

MiniBooNE Collaboration (2009, 2018)

NC photon production?

NC photon production?

J.A. Harvey, C.T. Hill, R.J. Hill, 2007, 2008 R.J. Hill, 2010, 2011 J. L. Rosner, 2015

NC photon production?

Form factors are poorly known

J.A. Harvey, C.T. Hill, R.J. Hill, 2007, 2008 R.J. Hill, 2010, 2011 J. L. Rosner, 2015

Production of single photons in the exclusive neutrino process $vN \rightarrow v\gamma N$

S. S. Gershtein, Yu. Ya. Komachenko, and M. Yu. Khlopov

Institute of High Energy Physics, Serpukhov (Submitted 16 January 1981) Yad. Fiz. 33, 1597-1604 (June 1981)

It is shown that the experimentally observed production of single photons in neutrino interactions involving neutral currents without visible accompaniment of other particles can be explained by the scattering of the neutrino by a virtual ω meson with small momentum transfer to a nucleon and subsequent coherent enhancement of the process in the nucleus.

PACS numbers: $13.15. + g$, 14.80.Kx

1. INTRODUCTION

In neutrino experiments performed at CERN using the chamber Gargamelle, more than ten events were detected in which it was observed that single photons with energy $1-10$ GeV were produced without visible tracks of any other particles.¹ It can be assumed that the observed events correspond to the weak-electromagnetic process of single-photon production in the reaction

$$
\mathsf{v} N \to \mathsf{v} \gamma N, \tag{1}
$$

$$
{\mu\nu} = \sum{\nu} T^{(M)} P^{(M)} J^{(M)}_{\mu\nu} ,
$$

 \boldsymbol{H}

in which $T^{(M)}$ is the vertex for emission of a virtual meson (M) by the target nucleon, $P^{(M)}$ is the meson propagator, and $J_{\mu\nu}^{(M)} = \int \langle 0| T(J_{\mu}^{\mu\prime}(x), J_{\nu}^{EM}(y))|M \rangle e^{i\alpha x + i\rho y} d^4x d^4y$ is the weak-electromagnetic $Z^0M\gamma$ vertex. The notation for the particle momenta is given in Fig. 2.

In accordance with the estimates of Ref. 3, we shall take into account the contributions to the diagram of Fig.

 (3)

A systematic calculation

- The nucleon level physics (form factors)
- Benchmarked against electron-nucleus quasi-elastic and (in)coherent pion production reactions
- Many body effects: Fermi motion, resonance modification, final state interaction…
- A relativistic many body theory (quantum hadrondynamics, QHD) for studying GeV-lepton-nucleus reactions
	- Dirac spinor
	- Mean field approximation

A systematic calculation

X.Z. and B.D.Serot (2012, 2013)

Cross section needs to be at least doubled
Report for INT neutrino-nucleus cross section workshop (2013) G. T. Garvey, D. A. Harris, H. A. Tanaka, R. Tayloe, G. P. Zeller, arXiv: 1412.4294

R.J. Hill, 2010, 2011 X.Z. and B. Serot, 2012,2013, E. Wang, L. Alvarez 6/27/2018 *-Ruso , J. Nieves, 2015*

Base-line neutrino experiment: hadronic physics

Qweak experiment at Jlab

$$
A_{ep} \equiv \frac{\sigma_+ - \sigma_-}{\sigma_+ + \sigma_-} = A_0 \Big[1 - 4 \sin^2 \theta_W + Q^2 B(Q^2, \theta) \Big]
$$

It probes high energy scale physics

Radiative correction (gamma Z box)

M. Gorchtein and C.J. Horowitz, (2009); M. Gorchtein, C.J. Horowitz, and M.J. Ramsey-Musolf, (2011); B.C. Rislow and C.E. Carlson, (2013); N.L. Hall, P.G. Blunden, W. Melnitchouk, A.W. Thomas and R.D. Young, (2013)

Dispersion analysis on weak-Compton scattering

Again form factors are poorly known

•The Z vertex is poorly known. Need neutrino measurement • Our first work reduces the uncertainty in extracting Q_{W}^{p} M. Gorchtein and X.Z. (2015)

Partially supported by Fermilab

Axial current form factors are important

- They are an important part of the systematic uncertainty in base-line neutrino oscillation experiments
- They impact calculations of neutrino-nucleus reactions and radiative corrections

$$
\langle N\lambda'|J_{EM}^{\mu}|N\lambda\rangle = \overline{u}_{\lambda'} \left[F_1\gamma^{\mu} + F_2 \frac{i\sigma^{\mu\nu}q_{\nu}}{2M_N}\right]u_{\lambda}
$$

$$
\langle N\lambda'|J_A^{\mu}|N\lambda\rangle = \overline{u}_{\lambda'} \left[G_A\gamma^{\mu}\gamma_5 + G_P \frac{q^{\mu}\gamma_5}{2M_N}\right] \frac{\tau}{2}u_{\lambda}
$$

Axial current form factors are important

- They are an important part of the systematic uncertainty in base-line neutrino oscillation experiments
- They impact calculations of neutrino-nucleus reactions and radiative corrections

- Lattice QCD won't be the full answer: high Q^2 behavior, N \rightarrow Resonance transition (inelastic) form factors
- We need a model/framework to cover elastic and inelastic form factors at $Q^{\wedge}2$ from zero to a few GeV^2.
- Other approaches: "meson-dominance" model (see Emilie Passemar's talk), Z-expansion (by $R_{\rm 6/2}$, $R_{\rm 20}$, and Bayesian analysis on data (Luis Alveriz-Ruso et.al.,) $_{\rm 23}$

S. J. Brodsky et.al., Phys. Rept., 301, 299 (1998)

S. J. Brodsky et.al., Phys. Rept., 301, 299 (1998)

$$
\begin{array}{lcl} |N,\lambda,P^+,\mathbf{0}\rangle &= \sqrt{Z}|N,\lambda\rangle_{Bare} + \sum_{N'=N}^{\Delta}\sum_{x,\mathbf{k}^\perp}\sum_{\lambda'}\Phi_{N',\lambda'}^\lambda(x,\mathbf{k}^\perp)|N',\lambda',xP^+,\mathbf{k}^\perp\rangle\otimes|\pi,(1-x)P^+,-\mathbf{k}^\perp\rangle\\ |N,\lambda\rangle_{Bare} &= |qqq\rangle \\ &= \sum_{D=S}^A\sum_{x,\mathbf{k}^\perp}\sum_{\lambda_D\lambda_q}\Psi_{D,\lambda_D,\lambda_q}^\lambda(x,\mathbf{k}^\perp)|q,\lambda_q,xP^+,\mathbf{k}^\perp\rangle\otimes|D,\lambda_D,(1-x)P^+,-\mathbf{k}^\perp\rangle \end{array}
$$

R.L. Jaffe, Phys. Rept., 409, 1 (2005) S. J. Brodsky et.al., Phys. Rept., 301, 299 (1998)

$$
|N, \lambda, P^{+}, \mathbf{0}\rangle = \sqrt{Z}|N, \lambda\rangle_{Bare} + \sum_{N'=N}^{\Delta} \sum_{x, \mathbf{k}^{\perp}} \sum_{\lambda'} \Phi_{N', \lambda'}^{\lambda}(x, \mathbf{k}^{\perp})|N', \lambda', xP^{+}, \mathbf{k}^{\perp}\rangle \otimes |\pi, (1-x)P^{+}, -\mathbf{k}^{\perp}\rangle
$$

\n
$$
|N, \lambda\rangle_{Bare} = |qq\rangle
$$

\n
$$
= \sum_{D=S}^{A} \sum_{x, \mathbf{k}^{\perp}} \sum_{\lambda_D \lambda_q} \Psi_{D, \lambda_D, \lambda_q}^{\lambda}(x, \mathbf{k}^{\perp})|q, \lambda_q, xP^{+}, \mathbf{k}^{\perp}\rangle \otimes |D, \lambda_D, (1-x)P^{+}, -\mathbf{k}^{\perp}\rangle
$$

Scalar & axial-vector **diquarks** 6/27/2018

R.L. Jaffe, Phys. Rept., 409, 1 (2005) S. J. Brodsky et.al., Phys. Rept., 301, 299 (1998) I. Cloet and G. Miller, Phys.Rev.C, 86, 015208 (2012)

$$
|N, \lambda, P^{+}, \mathbf{0}\rangle = \sqrt{Z}|N, \lambda\rangle_{Bare} + \sum_{N'=N}^{\Delta} \sum_{x, \mathbf{k}^{\perp}} \sum_{\lambda'} \Phi^{\lambda}_{N', \lambda'}(x, \mathbf{k}^{\perp})|N', \lambda', xP^{+}, \mathbf{k}^{\perp}\rangle \otimes |\pi, (1-x)P^{+}, -\mathbf{k}^{\perp}
$$

\n
$$
|N, \lambda\rangle_{Bare} = |qq\rangle
$$

\n
$$
= \sum_{D=S}^{\Delta} \sum_{x, \mathbf{k}^{\perp}} \sum_{\lambda_D \lambda_q} \Psi^{\lambda}_{D, \lambda_D, \lambda_q}(x, \mathbf{k}^{\perp})|q, \lambda_q, xP^{+}, \mathbf{k}^{\perp}\rangle \otimes |D, \lambda_D, (1-x)P^{+}, -\mathbf{k}^{\perp}\rangle
$$

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$$
|N, \lambda, P^+, \mathbf{0}\rangle = \sqrt{Z}|N, \lambda\rangle_{Bare} + \sum_{N'=N}^{\infty} \sum_{x, \mathbf{k}^{\perp}} \sum_{\lambda'} \Phi_{N', \lambda'}^{\lambda}(x, \mathbf{k}^{\perp})|N', \lambda', xP^+, \mathbf{k}^{\perp}\rangle \otimes |\pi, (1-x)P^+, -\mathbf{k}^{\perp}\rangle
$$

\n $|N, \lambda\rangle_{Bare} = |qq\rangle$
\nDelta
\nDelta resonance included in our work
\n $= \sum_{D=S}^{A} \sum_{x, \mathbf{k}^{\perp}} \sum_{\lambda_D \lambda_q} \Psi_{D, \lambda_D, \lambda_q}^{\lambda}(x, \mathbf{k}^{\perp})|q, \lambda_q, xP^+, \mathbf{k}^{\perp}\rangle \otimes |D, \lambda_D, (1-x)P^+, -\mathbf{k}^{\perp}\rangle$

Scalar & axial-vector **diquarks** 6/27/2018

R.L. Jaffe, Phys. Rept., 409, 1 (2005) S. J. Brodsky et.al., Phys. Rept., 301, 299 (1998) I. Cloet and G. Miller, Phys.Rev.C, 86, 015208 (2012)

24 Scalar & axial-vector diquarks Delta resonance included in our work Δ Δ , Δ 6/27/2018

LFQM: EM and Axial form factors

• The bare-quark contribution to $F_{1,2}$ is directly related to the overlap of quark wave functions:

$$
F_1^{Bare}(Q^2) = \sum_{D=S}^{A} \sum_{x,\boldsymbol{k}^{\perp}} \sum_{\lambda_D \lambda_q} \left[\Psi_{D,\lambda_D,\lambda_q}^{\lambda=+1/2}(x,\boldsymbol{k}^{\perp}) \right]^* \Psi_{D,\lambda_D,\lambda_q}^{\lambda=+1/2}(x,\boldsymbol{k}^{\perp})
$$

• The bare-quark contribution to G_A , is also related to the wave function overlap, but has different component-weights from $F_{1,2}$:

$$
G_A^{Bare}(Q^2) = \sum_{D=S}^{A} \sum_{x,\boldsymbol{k}^{\perp}} \sum_{\lambda_D \lambda_q} \left[\Psi_{D,\lambda_D,\lambda_q}^{\lambda=+1/2}(x,\boldsymbol{k}^{\perp'}) \right]^* \Psi_{D,\lambda_D,\lambda_q}^{\lambda=+1/2}(x,\boldsymbol{k}^{\perp}) (-1)^{\lambda_q - \frac{1}{2}}
$$

 $N: \longrightarrow N$

 \overline{N}

ЛÍ

 N N

Δ

 N_{\cdot}

Δ

• The pion cloud couples elastic form factor to the inelastic form factors 6/27/2018 $\overline{\mathsf{L}}$ 25

Fit EM FFs: preliminary results

$$
G_E \equiv F_1 + \frac{Q^2}{4M_N} F_2
$$

\n
$$
G_M \equiv F_1 + F_2
$$

\n
$$
G_D \equiv \left(1 + \frac{Q^2}{0.71 \text{GeV}^2}\right)^{-2}
$$

Fit EM FFs: preliminary results

Fit EM FFs: preliminary results

Dark photon: Be-8 anomaly

Observation of Anomalous Internal Pair Creation in ⁸Be: A Possible Indication of a Light, **Neutral Boson**

A. J. Krasznahorkay, M. Csatlós, L. Csige, Z. Gácsi, J. Gulyás, M. Hunyadi, I. Kuti, B. M. Nyakó, L. Stuhl, J. Timár, T. G. Tornyi, and Zs. Vajta

Institute for Nuclear Research, Hungarian Academy of Sciences (MTA Atomki), P.O. Box 51, H-4001 Debrecen, Hungary

T. J. Ketel

Nikhef National Institute for Subatomic Physics, Science Park 105, 1098 XG Amsterdam, Netherlands

A. Krasznahorkay

CERN, CH-1211 Geneva 23, Switzerland and Institute for Nuclear Research, Hungarian Academy of Sciences (MTA Atomki), P.O. Box 51, H-4001 Debrecen, Hungary (Received 7 April 2015; published 26 January 2016)

Electron-positron angular correlations were measured for the isovector magnetic dipole 17.6 MeV $(J^{\pi} = 1^+, T = 1)$ state \rightarrow ground state $(J^{\pi} = 0^+, T = 0)$ and the isoscalar magnetic dipole 18.15 MeV $(J^{\pi} = 1^{+}, T = 0)$ state \rightarrow ground state transitions in ⁸Be. Significant enhancement relative to the internal pair creation was observed at large angles in the angular correlation for the isoscalar transition with a confidence level of $> 5\sigma$. This observation could possibly be due to nuclear reaction interference effects or might indicate that, in an intermediate step, a neutral isoscalar particle with a mass of 16.70 ± 0.35 (stat) ± 0.5 (syst) MeV/ c^2 and $J^{\pi} = 1^{+}$ was created.

The theoretical model used is from M. E. Rose [PR 76, 678 (1949)]; No interference was studied.

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 $\overline{\mathsf{X}.\mathsf{Z}.\mathsf{and} \mathsf{G}.\mathsf{Miller}, 2017:\mathsf{they}\;interferel.}$

Photon production data D. Zahnow et.al., *Z. Phys. A* **D. Zahnow et.al.,** *Z. Phys. A* **D. Zahnow et.al.,** *Z. Phys. A*

351, 229 (1995); B. MainsBridge, *Nucl.Phys.* **21**, 1(1960); D.J. Schlueter, et.al., *Nucl.Phys.* **58**, 254 (1964)

Photon production data

D. Zahnow et.al., *Z. Phys. A* **351**, 229 (1995); B. MainsBridge, *Nucl.Phys.* **21**, 1(1960); D.J. Schlueter, et.al., *Nucl.Phys.* **58**, 254 (1964)

$$
\sum |\mathsf{M}|^2 \equiv T_0 \Big[1 + a_1 P_1(\cos \theta) + a_2 P_2(\cos \theta) \Big] \, \stackrel{\scriptscriptstyle{\mathsf{I}(1960); \, \mathsf{D}(1064)}}{\scriptscriptstyle{\mathsf{[1964]}}}
$$

Photon production data

D. Zahnow et.al., *Z. Phys. A* **351**, 229 (1995); B. MainsBridge, *Nucl.Phys.* **21**, 1(1960); D.J. Schlueter, et.al., *Nucl.Phys.* **58**, 254 (1964)

Photon production data

D. Zahnow et.al., *Z. Phys. A* **351**, 229 (1995); B. MainsBridge, *Nucl.Phys.* **21**, 1(1960); D.J. Schlueter, et.al., *Nucl.Phys.* **58**, 254 (1964)

On dark-photon explanation

On dark-photon explanation

- A dark-photon with 17-MeV mass might be the cause (e.g. J. L. Feng et.al., 2017)
- 6/27/2018 **broduction of dark photon (not seen experimentally)** and the set of • \rightarrow $J_{dark\gamma} = J_{EM,vec} \rightarrow$ E1 and M1 have similar size for photon \rightarrow smooth background

Summary

- A theoretical calculation with well-understood systematical uncertainty is really useful for predictions and guiding experiments (lesson from the EFT application in radiative capture reactions)
- The NC photon production couldn't fully explain the MiniBooNE low energy event excess (not then and not now)
- Weak-Compton scattering amplitude is relevant for the NC photon production, and radiative correction to weak processes (parity-violating electron-nucleon scattering, neutrino-nucleon scattering, and neutron beta decay)
- Nucleon axial current form factors are being studied in a light-front quark model as well as other approaches. Stay tuned
- Be-8 anomaly: the dark-photon explanation seems inconsistent with the experiment

 $J \equiv \big\langle \textsf{Be}\big|\widehat{J}\big|\textsf{Li}\!+\!\textsf{p} \big\rangle$ \hat{I} Li+

$$
J' = (CG) q U_{E1} + q^2 \frac{p}{M} [(CG) U_{E2,1} + (CG) U_{E2,2}]
$$

$$
J' = (CG) \omega U_{E1} + q \frac{p}{M} \left[(CG) U_{M1,1} + (CG) U_{M1,2} \right]
$$

$$
J' = (CG) \omega U_{E1} + q \frac{p}{M} \left[+(CG) \omega U_{E2,1} + (CG) \omega U_{E2,2} \right]
$$

$$
J \equiv \left< \textsf{Be} \big| \hat{J} \big| \textsf{Li} + \textsf{p} \right>
$$

$$
J' = (CG) q U_{E1} + q^2 \frac{p}{M} [(CG) U_{E2,1} + (CG) U_{E2,2}]
$$
\n
$$
J' = (CG) \omega U_{E1} + q \frac{p}{M} \left[(CG) U_{M1,1} + (CG) U_{M1,2} \right]
$$
\n
$$
U_{M1,1} \sim -\frac{\sqrt{\Gamma_{Y(0)}\Gamma_{(0)}X_{(0)}}}{E - E_{(0)} + i\frac{\Gamma_{(0)}}{2}} + \frac{\sqrt{\Gamma_{Y(1)}\Gamma_{(1)}X_{(1)}}}{E - E_{(1)} + i\frac{\Gamma_{(1)}}{2}}
$$
\n
$$
U_{M1,2} \sim \frac{\sqrt{\Gamma_{Y(0)}\Gamma_{(0)}(1 - X_{(0)})}}{E - E_{(0)} + i\frac{\Gamma_{(0)}}{2}} + \frac{\sqrt{\Gamma_{Y(1)}\Gamma_{(1)}X_{(1)}}}{E - E_{(1)} + i\frac{\Gamma_{(1)}}{2}}
$$
\n
$$
E - E_{(2)} + i\frac{\Gamma_{(1)}}{2}
$$
\n
$$
U_{E1} \sim d_{E1}(1 - d_{E1}^2 \frac{p^2}{\Lambda^2}); \quad U_{E2,1} \sim d_{E2,1}; \quad U_{E2,2} \sim d_{E2,2} \quad \text{as}
$$

 Ψ

M1

 ϕ