

theory of pion production for nu-d
- Neutrino induced pion production reaction on
deuteron -

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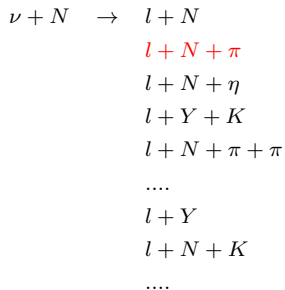
Collaborators:

$\nu d, \gamma d$: S.X. Nakamura, H. Kamano, T. -S. H. Lee

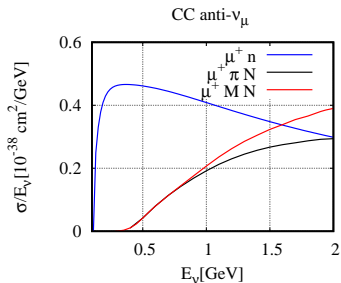
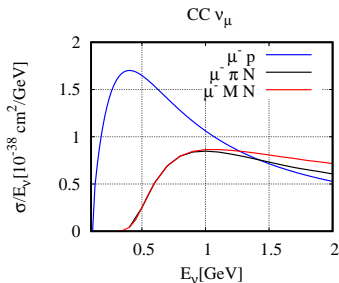
pion angular distribution: J. E. Sobczyk, E. Hernandez, S. X. Nakamura, J. Nieves

- Motivation
- Models of neutrino induced pion production reactions
- Neutrino deuteron reaction and extraction of elementary cross section
- Summary

CC Neutrino-nucleon reaction (building block to describe neutrino-nucleus reaction)



Neutrino-nucleon cross section



- cross section of single pion production is as large as non-meson production (DCC model, S. X. Nakamura et al.)
- non negligible contribution of $2\pi, K, \eta$ production channels($\bar{\nu}$).

Single pion production

$$\begin{aligned}\nu_\mu + p &\rightarrow \mu^- + \pi^+ + p, & \bar{\nu}_\mu + n &\rightarrow \mu^+ + \pi^- + n \\ \nu_\mu + n &\rightarrow \mu^- + \pi^+ + n, & \bar{\nu}_\mu + p &\rightarrow \mu^+ + \pi^- + p \\ \nu_\mu + n &\rightarrow \mu^- + \pi^0 + p, & \bar{\nu}_\mu + p &\rightarrow \mu^+ + \pi^0 + n\end{aligned}$$

Cross sections

$$\sigma(E_\nu), \quad \frac{d\sigma}{dQ^2}, \quad \frac{d\sigma}{dW_{\pi N}}, \quad \frac{d\sigma}{dW_{\pi N} dQ^2 d\Omega_\pi}$$

Data on single pion production

Data on Neutrino induced Single pion production

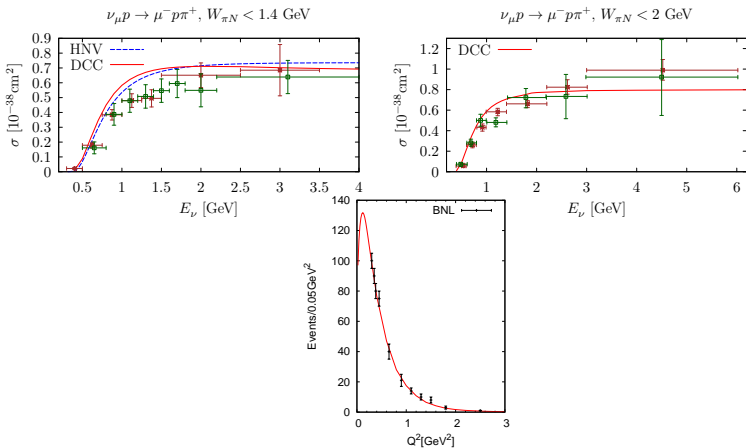
(<http://hepdata.cedar.ac.uk/review/neutrino/>)

				1 π	2 π
GGM	Lerche 1978	ν	Propane	1-10	
	Bolognese 1979	$\bar{\nu}$	Propane-Freon	1-7.5	
BEBC	Allen 1986	ν	p	10-80	
	Allasia 1990	$\nu, \bar{\nu}$	d	5-150	
BNL	Kitagaki 1986	ν	d	0.5 - 3	0.5 - 3
ANL	Barish 1979	ν	p,d	0.4 - 6	
	Radecky 1982	ν	d	0.5 - 1.5	
	Day 1983	ν	d		0.75-5.55
FNAL	Bell 1978	ν	p	15-40	
SKAT	Ammosov 1988	ν	Freon(CF ₃ Br)	4-18	
	Grabosch 1989	$\nu, \bar{\nu}$	Freon(CF ₃ Br)	3.5-6	

- Reanalysis of ANL/BNL data

(C. Wilkinson et al. PRD90 (2014), P. Rodrigues, C. Wilkinson, K. McFarland, EPJC76 (2016))

models of pion production are 'tested' against ANL/BNL data.



$\sigma(\nu N)_{exp}$ are extracted from νd data without taking into account FSI.

$$\langle F | j_{CC}^{\mu} | I \rangle \sim \langle (\pi NN)_{PLW} | j_{CC}^{\mu} | d \rangle$$

- It is well known FSI is important for $\gamma d \rightarrow \pi^0 pn$ and not so important for $\gamma d \rightarrow \pi^- pp$. (channel dependent role of FSI)
- more than 30% effects of FSI on pion angular distribution $\frac{d\sigma}{dE_\mu d\Omega_\mu d\Omega_\pi}$ around 'QE' Δ production kinematics have been pointed out. Jia-jun Wu, T. -S. H. Lee, T. Sato PRC91 (2015)

in this talk

- Extend our previous analysis to cover whole phase space of $\mu^- \pi NN$ to examine how important final state interaction in $\nu + d \rightarrow l + \pi + N + N$.
Try to extract $\sigma(\nu N)$ from νd data without full microscopic calculation.

Model of meson production

$$\langle MB | J_\alpha^\mu | N \rangle$$

$$J_{em}^\mu = V_3^\mu + V_{IS}^\mu$$

$$J_{CC}^\mu = V_{1+i2}^\mu - A_{1+i2}^\mu \quad (\Delta S = 0 \text{ current without CKM})$$

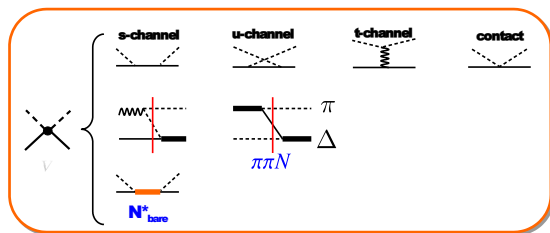
$$J_{NC}^\mu = V_3^\mu - A_3^\mu - 2 \sin^2 \theta_W J_{em}^\mu - \frac{1}{2} \bar{s} \gamma^\mu (1 - \gamma_5) s$$

- meson production through resonance excitation and non-resonant mechanisms.
- model should be constrained as much as possible by existing data on pion, photon and electron induced reactions.

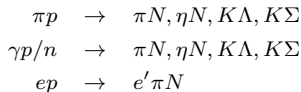
ANL-Osaka DCC model

Model developed for N^* physics: spectrum of N^* , Δ ($W < 2GeV$), transition form factors

- Fock-Space: isobar (N^* , Δ), Meson-Baryon (πN , ηN , $K\Lambda$, $K\Sigma$, $\pi\pi N$ ($\pi\Delta$, ρN , σN))
- Coupled-channel (Lippmann-Schwinger) equation is solved numerically.

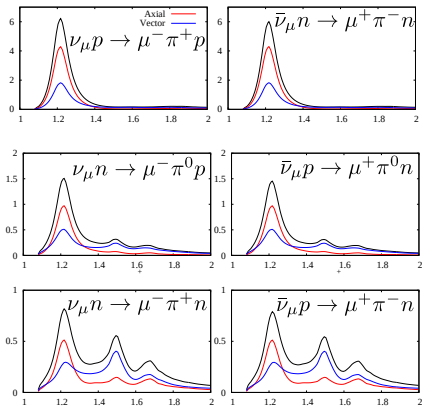


- analyze available data on pion, photon, electron induced meson production



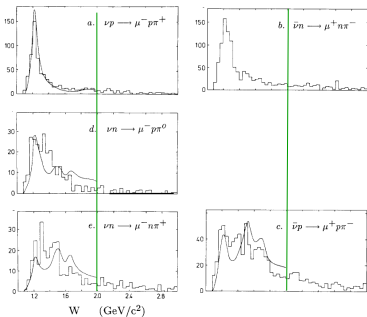
- resonance spectrum and coupling constants, form factors at resonance pole are extracted from the analytic continuation of the amplitude.
- neutrino reaction: Axial vector current : $g_A^{NN^*}$ from $g_\pi^{NN^*}$ assuming PCAC and dipole form factor, except $\Delta(1232)$.

$d\sigma/dW_{\pi N}$ of single pion production $E_\nu = 40\text{GeV}$



Neutrino

anti-neutrino



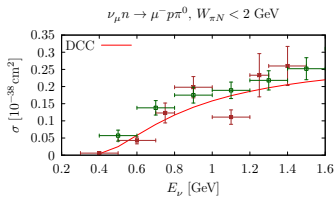
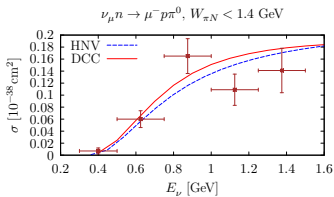
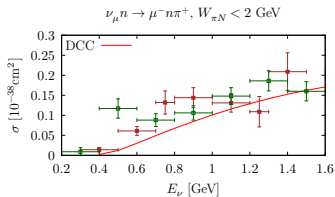
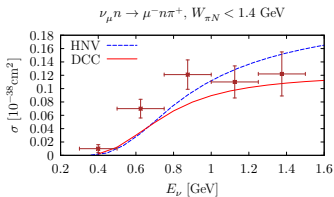
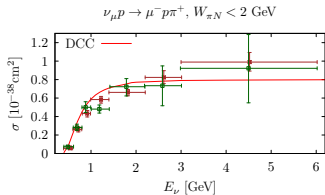
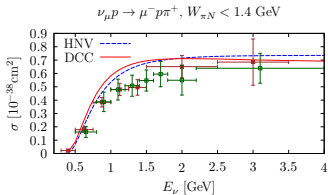
BECB NP343,285(1990)

- $\Delta(1232)$ gives most important contribution for all channels.
- One can make only qualitative test of model for W dependence.

comparison of models I : total cross section of single pion production

J. E. Sobczyk, E. Hernandez, S. X. Nakamura, J. Nieves, T. Sato

- DCC: ANL-Osaka
- HNV: E. Hernandez, J. Nieves, M. Valverde
 - single pion production in Δ region
 - non-resonant interaction from chiral Lagrangian
 - Unitarity (Satisfy Watson theorem for P_{33})

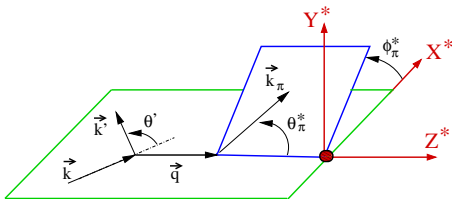


comparison of models II : Angular distribution of pion production off nucleons

$$\frac{d\sigma^{CC}}{dW_{\pi N} dQ^2 d\Omega_{\pi}^*} = \frac{G_F^2 W_{\pi N}}{4\pi M k^2} [A + B \cos \phi_{\pi} + C \cos 2\phi_{\pi} + D \sin \phi_{\pi} + E \sin 2\phi_{\pi}]$$

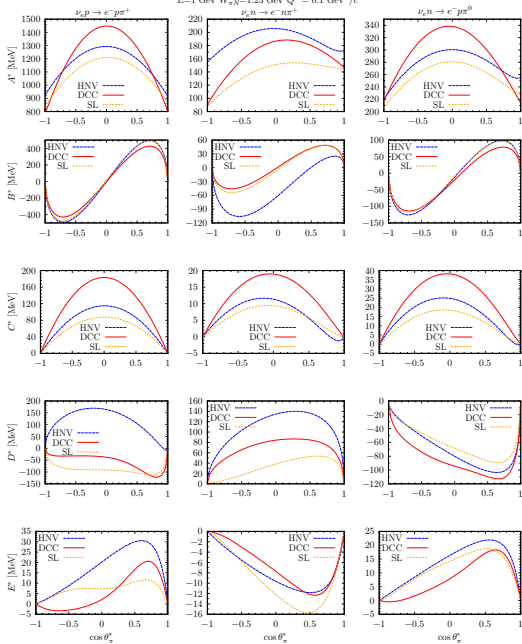
T.Sato, D. Uno, T. -S. H. Lee (2003), E. Hernandez, J.Nieves, M. Valverde, PRD76, 033005 (2007)

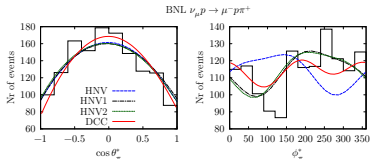
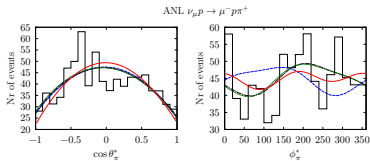
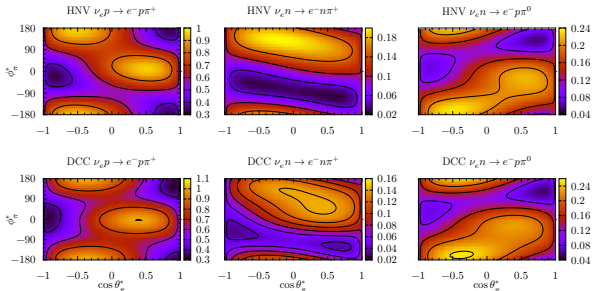
- **parity violating T-odd** angular distributions are generated.
- angular distribution pion may reveal differences among models that are not seen well in integrated cross sections.



$$\text{PV: } \sin \phi_{\pi} \sim \mathbf{k} \times \mathbf{k}' \cdot \mathbf{k}_{\pi}$$

$E=1\text{ GeV}$ $W_{\pi N}=1.23\text{ GeV}$ $Q^2=0.1\text{ GeV}^2/c^2$



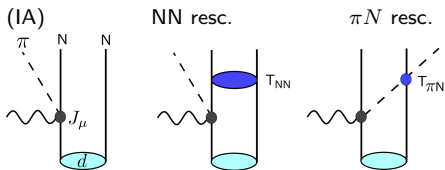


Neutrino induced pion production on deuteron

- how important final state interaction in $\nu + d \rightarrow l + \pi + N + N$?
simple recipe to extract $\sigma(\nu N)$ from νd data?

leading order terms of FSI

$$|[\pi NN]_{PLW} \rangle \rightarrow (1 + G_0 T_{NN} + G_0 T_{\pi N}) |[\pi NN]_{PLW} \rangle$$



note:

- Above rescattering terms are the leading order of multiple scattering theory (Faddeev Eq.). More elaborate description of three-body (πNN) dynamics may be possible (A. Matsuyama T.-S.H. Lee PRC34(1986), M. Schwamb Phys. Rep. 485(2010))
- 'Meson exchange current' is not considered.

T. Sato et al.: Electron Scattering and Charged Pion Photoproduction on ^{12}C and ^{13}C

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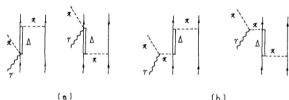


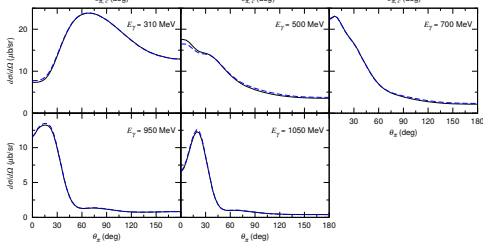
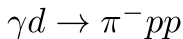
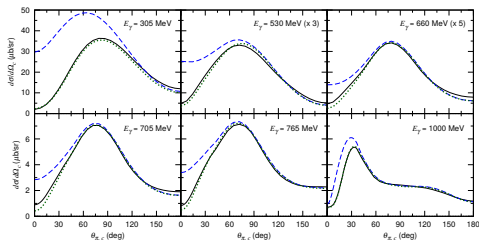
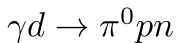
Fig.4a and b. Two-body operators due to the virtual isobar. Diagrams a and b are corrections to the Kroell-Ruderman and the pion pole terms, respectively.

TS, K. Koshigiri, H. Ohtsubo, Z. Phys. A320(1985)

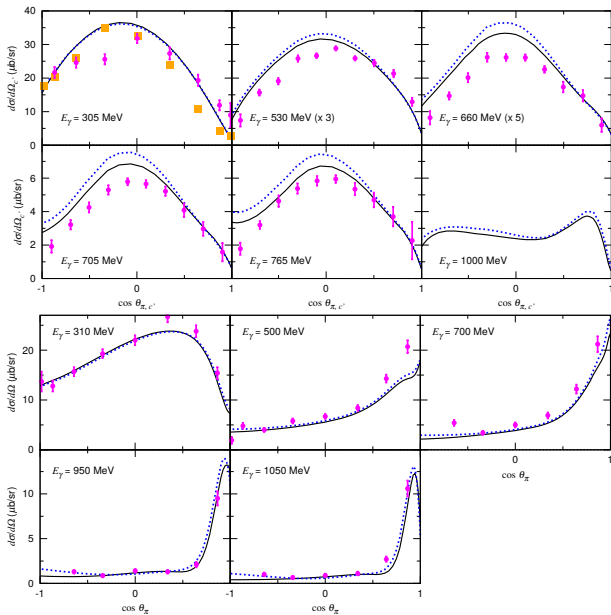
Example of NN rescattering amplitude

$$\begin{aligned}
 J_{\mu}^{NN-resc} &= \langle [\pi NN]_{PLW} | t_{NN} G_0 J_{\mu}^{CC} | d \rangle = \sum_{spin, isospin} \int d\mathbf{l} \\
 &\times \langle N_1(\mathbf{p}_1) N_2(\mathbf{p}_2) | t_{NN}(M_{N_1 N_2}) | \tilde{N}'_1(\mathbf{q} - \mathbf{k} + \mathbf{l}) N'_2(-\mathbf{l}) \rangle \\
 &\times \frac{\langle \pi(\mathbf{k}) \tilde{N}'_1(\mathbf{q} - \mathbf{k} + \mathbf{l}) | J_{\mu}(W, \mathbf{q}) | N'_1(\mathbf{l}) \rangle}{E - E_N(\mathbf{q} - \mathbf{k} + \mathbf{l}) - E_N(-\mathbf{l}) - E_{\pi}(\mathbf{k}) + i\epsilon} \langle N'_1(\mathbf{l}) N'_2(-\mathbf{l}) | \Psi_d(s_d) \rangle
 \end{aligned}$$

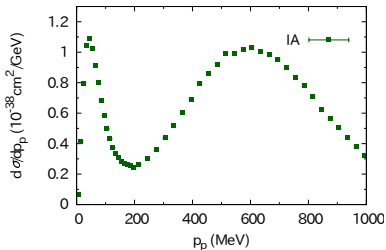
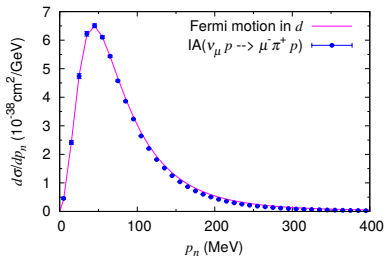
- ANL-Osaka model: $J_{CC}^{\mu}, t_{\pi N}$
Bonn-NN-potential: t_{NN}
- 3dim loop integration + 7-dim phase space(Monte-Carlo)



- Large FSI for π^0 production. 3S_1 scattering state is orthogonal to deuteron bound state. (in DW, deuteron component is eliminated from NN PLW.)



momentum distribution of spectator nucleon ($\nu + d \rightarrow \mu^- + \pi^+ + p + n$)
 – separate proton and neutron π^+ production reaction –



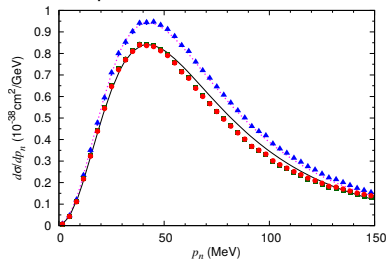
neutron spectator ($p \rightarrow \pi^+ p$)

proton spectator ($n \rightarrow \pi^+ n$)

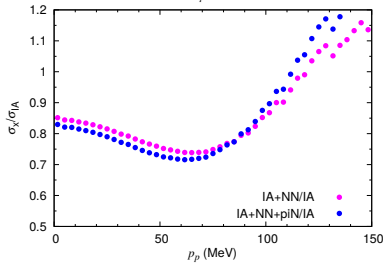
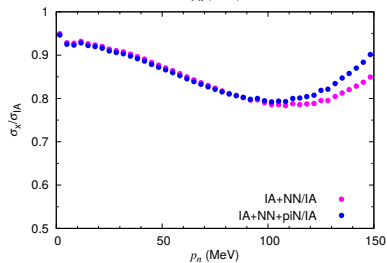
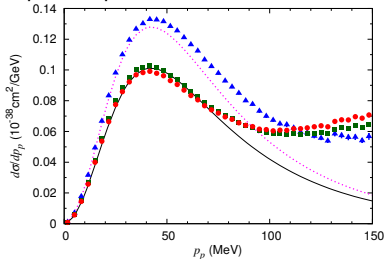
- $p \rightarrow \pi^+ p$ ($n \rightarrow \pi^+ n$) mechanism is dominated in $p_n < 150 \text{ MeV}$ ($p_p < 150 \text{ MeV}$).
- (momentum of muon and pion are integrated)

Effects of FSI $\nu_\mu + d \rightarrow \mu^- + \pi^+ + p + n$ ($E_\nu = 0.5\text{GeV}$)

neutron spectator

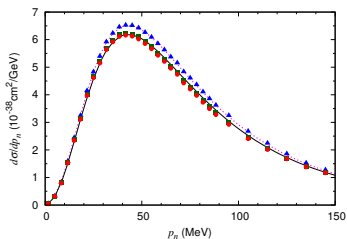


proton spectator

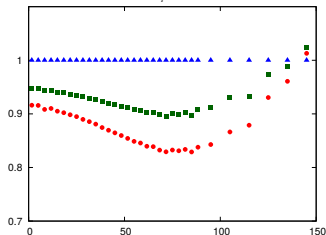
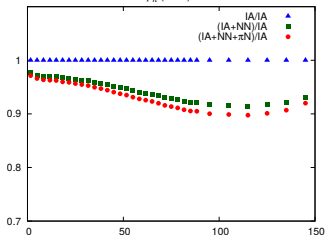
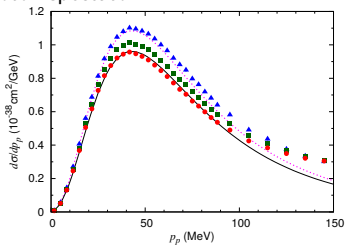


Effects of FSI $\nu_\mu + d \rightarrow \mu^- + \pi^+ + p + n$ ($E_\nu = 1\text{GeV}$)

neutron spectator



proton spectator

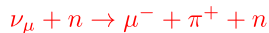
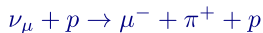
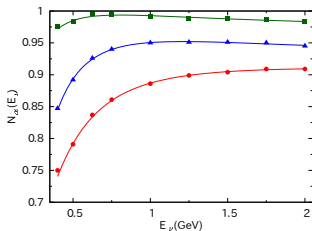


- about (5 ~ 30) % FSI effects depending on E_ν , p_s and channel.

$N_\alpha(E_\nu)$ parametrization of FSI

$$\frac{d\sigma_{\nu d}(E_\nu)}{dp_s} \sim N_\alpha(E_\nu) \frac{d\sigma_{\nu N}}{dp_s}$$

$$\frac{d\sigma_{\nu N}}{dp_s} = p_s^2 \int d\Omega_{p_s} \sigma_\alpha(\tilde{E}_\nu) |\psi_d(\vec{p}_s)|^2$$



- Ideally, one fit data using amplitude with FSI calculated by 'model of elementary amplitude'.
- N_α : fitting 'our' spectator distribution with FSI for $p_s < 50 MeV$ by using 'our' 'convoluted' cross section.

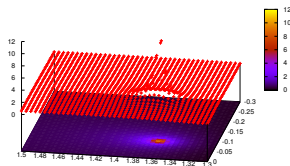
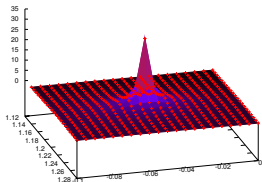
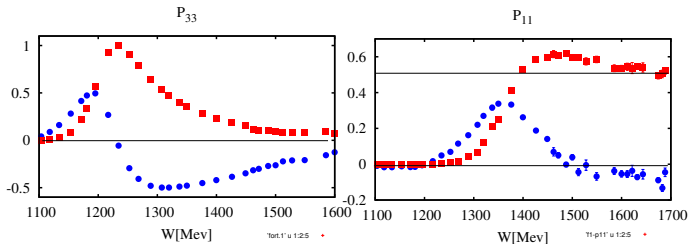
- Pion angular distribution in Δ region is discussed in ANL-Osaka model and HNV model.
 - angular distribution is sensitive to interference among partial wave amplitudes, phase of amplitudes, non-resonant mechanism.
 - parity violating T-odd correlation shows up with non-negligible strength.
- Role of FSI is examined within the first order rescattering correction.
 - pion photoproduction on deuteron is reasonably well described in DCC model+FSI.
 - FSI for the spectator momentum distribution of νd : FSI can be as large as 30% effect depending on E_ν, p_s , channel.
 - Main mechanism of FSI: NN rescattering($p\pi^+, n\pi^+$) πN rescattering ($n\pi^+$) FSI is small for π^0 production.

Acknowledgments KAKENHI JP25105010,JP16K053454.

Backup

Full amplitude is needed, not res-only

$$\pi N \text{ amplitude} \quad \mathcal{F} = \frac{S - 1}{2i}$$



Approximate relation between structure functions

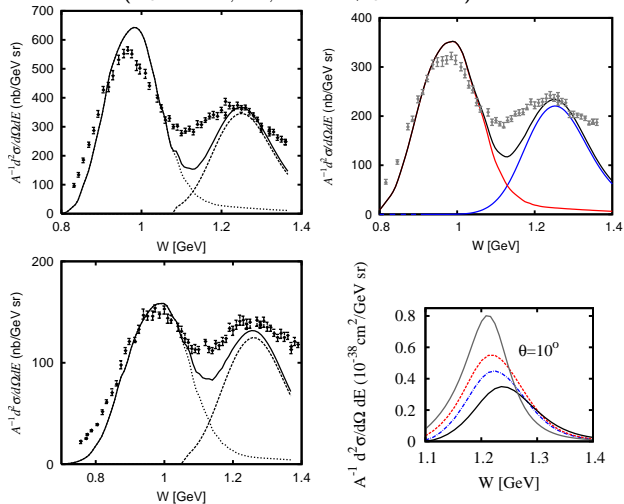
$$F_3^{CC} \text{ and } F_3^{\gamma Z} \quad (F_i^\alpha = (F_{ip}^\alpha + F_{in}^\alpha)/2)$$

$$2F_3^{\gamma Z} = F_3^{CC} \propto V_{IV}(A_{IV})^* \quad \text{DCC}$$

$$2F_3^{\gamma Z} \approx F_3^{CC} \sim u - \bar{u} + d - \bar{d} \quad \text{PDF}$$

* $W_3^{\gamma N}$ can be used to test F_3^{CC} for neutrino reaction.

$e^{12}C \rightarrow eX (E_e = 0.96, 1.1, 1.3 \text{ GeV}, \theta_e = 37.5^\circ)$



B. Szczerbinska, T. Sato, K. Kubodera, T.-S. H. Lee, PLB649(2007) 132

$$L^{\mu\nu}W_{\mu\nu} = \frac{Q^2}{1-\epsilon} \frac{1}{2} \sum_{s'_N, s_N} [R_T + \epsilon R_L + \sqrt{2\epsilon(1+\epsilon)} R_{LT} \cos \phi_\pi + \epsilon R_{TT} \cos 2\phi_\pi \\ + \sqrt{2\epsilon(1+\epsilon)} R_{LT'} \sin \phi_\pi + \epsilon R_{TT'} \sin 2\phi_\pi]$$

$$R_T = \frac{|j_c^x|^2 + |j_c^y|^2}{2} \mp \sqrt{1-\epsilon^2} \text{Im}(j_c^x j_c^{y*}),$$

$$R_L = \frac{Q^2}{q_c^2} |\bar{j}_c^0|^2,$$

$$R_{LT} = \sqrt{\frac{Q^2}{q_c^2}} [-\text{Re}(\bar{j}_c^0 j_c^{x*}) \pm \sqrt{\frac{1-\epsilon}{1+\epsilon}} \text{Im}(\bar{j}_c^0 j_c^{y*})],$$

$$R_{TT} = \frac{(|j_c^x|^2 - |j_c^y|^2)}{2},$$

$$R_{LT'} = \sqrt{\frac{Q^2}{q_c^2}} [\text{Re}(\bar{j}_c^0 j_c^{y*}) \pm \sqrt{\frac{1-\epsilon}{1+\epsilon}} \text{Im}(\bar{j}_c^0 j_c^{x*})],$$

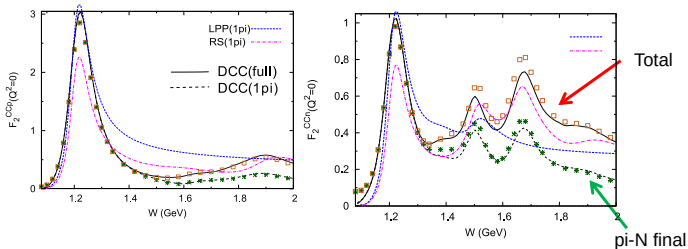
$$R_{TT'} = -\text{Re}(j_c^x j_c^{y*}),$$

where

$$\epsilon = \frac{1}{1 + \frac{2|q|^2}{Q^2} \tan^2 \frac{\theta_l}{2}}$$

Axial vector current at $Q^2 = 0$

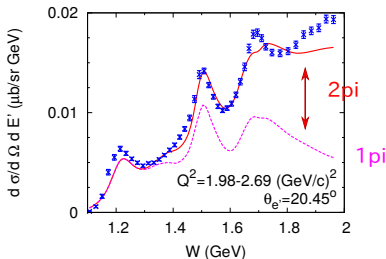
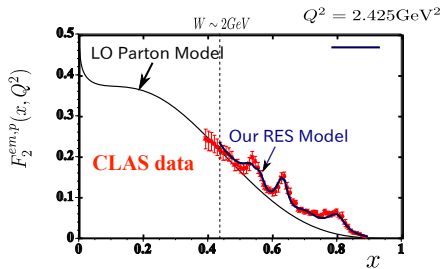
Axial Vector current F_2^{CC} at $Q^2 = 0$



$$\text{Using PCAC, } F_2^{CC}(Q^2 = 0) = \frac{2f_\pi^2}{\pi} \sigma(\text{virtual}\pi + N)$$

open box, green cross are data.

Vector current at large Q^2



description of ep in RES, smoothly connected to DIS