

Neutrinoless double beta decay in effective field theory

with V. Cirigliano, J. de Vries, M.L. Graesser, E. Mereghetti, S. Pastore,
B. van Kolck, A. Walker-Loud

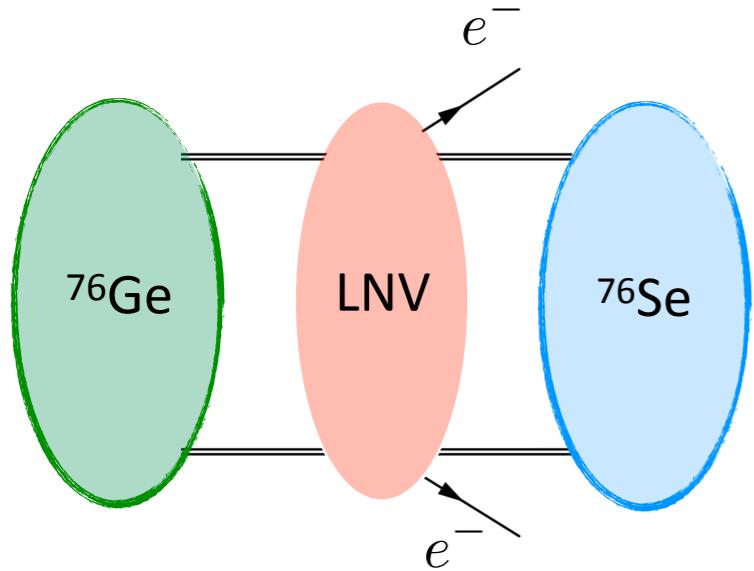
Based on:

arXiv:1806.02780, 1710.01729, 1802.10097,
1710.05026, 1708.09390



Introduction

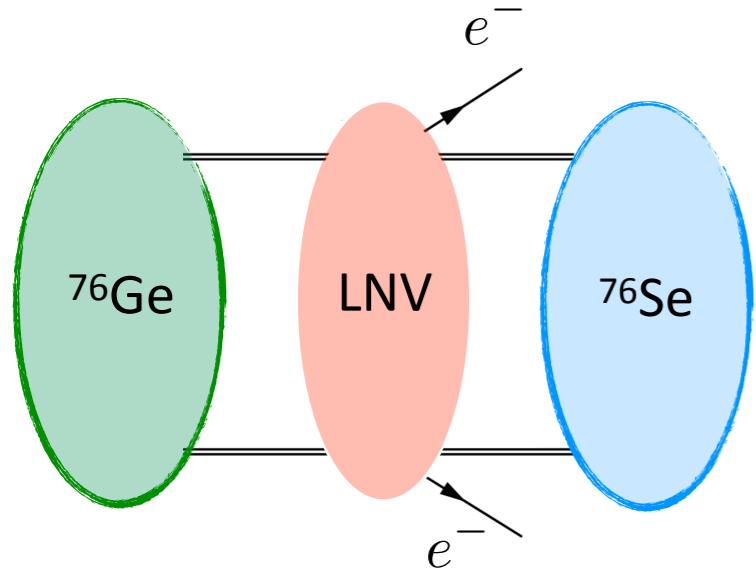
$0\nu\beta\beta$



- Violates lepton number, $\Delta L=2$

Introduction

$0\nu\beta\beta$

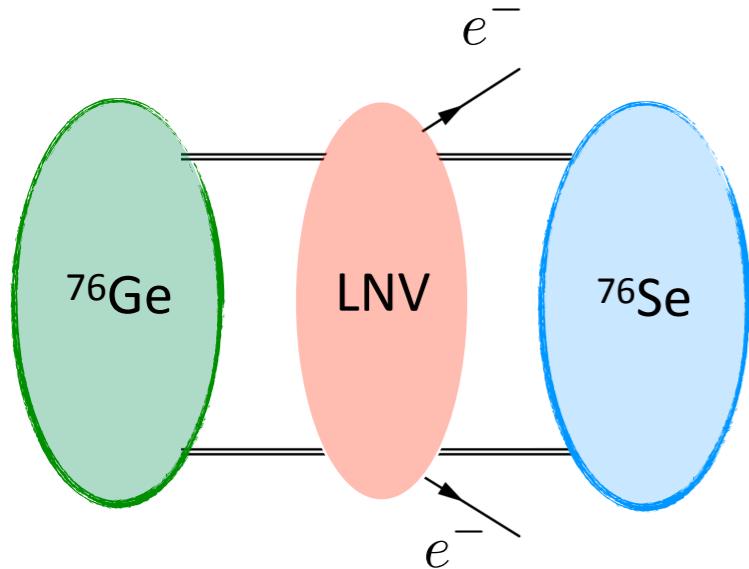


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- Stringently constrained experimentally
 - To be improved by 1-2 orders

	^{76}Ge	^{130}Te	^{136}Xe
$T_{1/2}^{0\nu}$	$> 5.3 \cdot 10^{25}$ [61]	$4.0 \cdot 10^{24}$ [63]	$1.07 \cdot 10^{26}$ [64]

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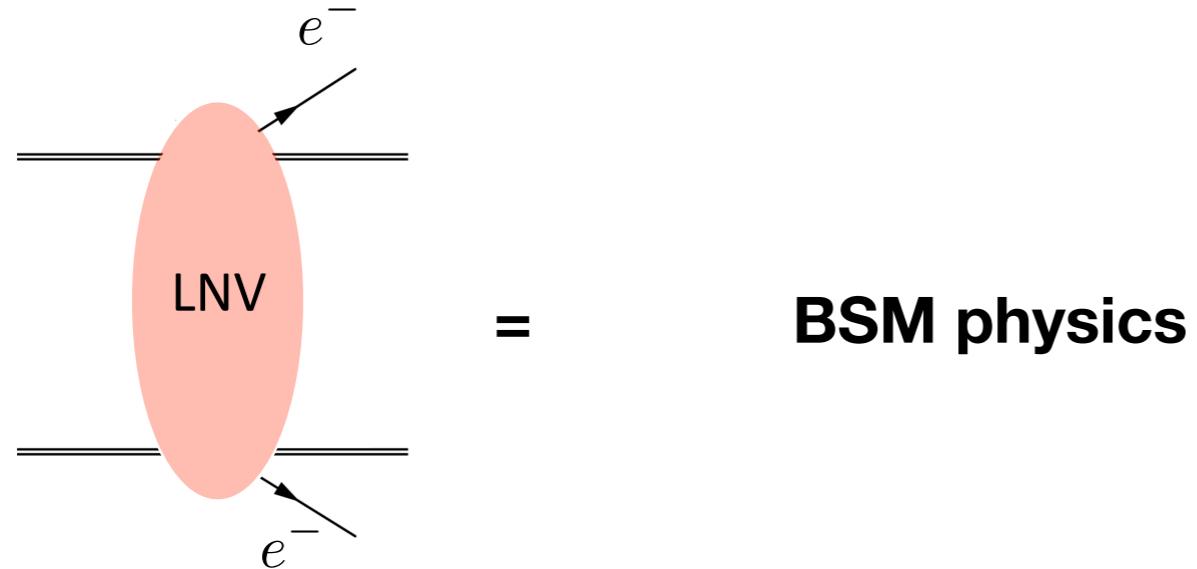


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- Would imply that
 - Neutrino's are Majorana particles
 - Physics beyond the SM

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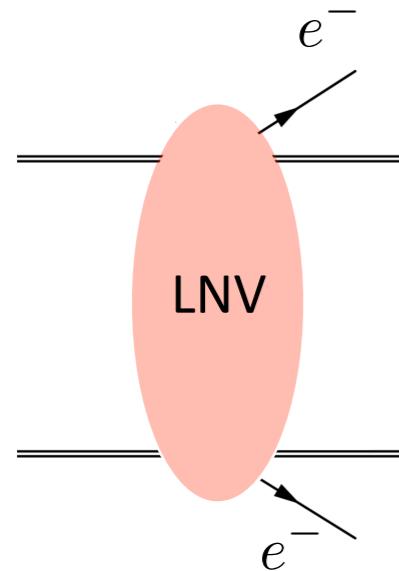
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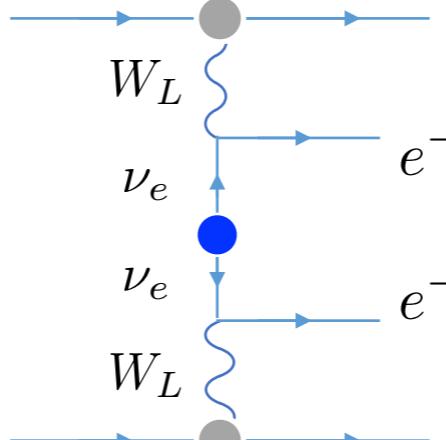
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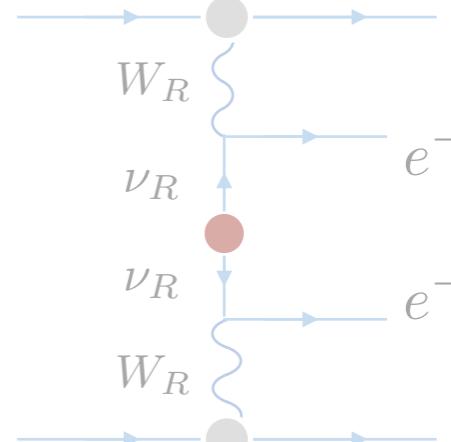
$0\nu\beta\beta$



Light Majorana mass?

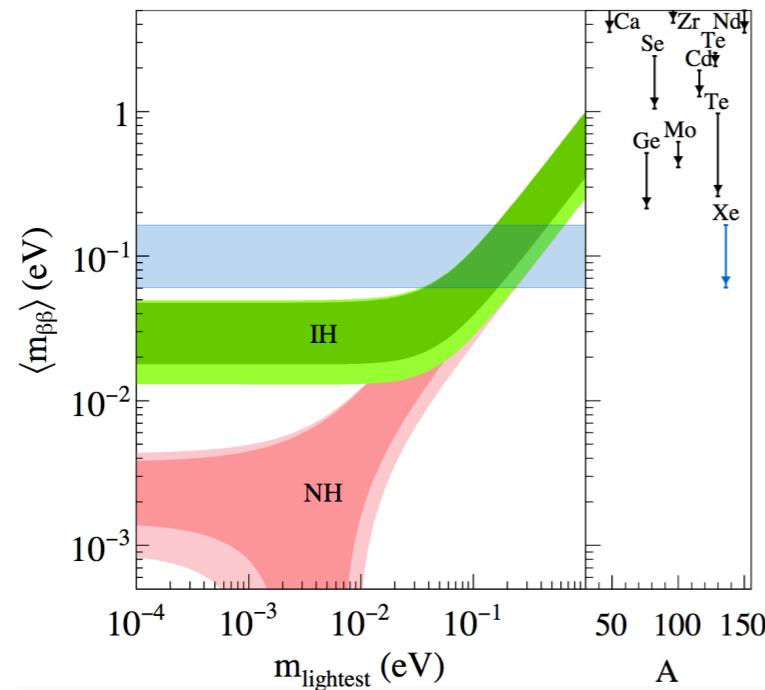


Left-right model?



+ ??

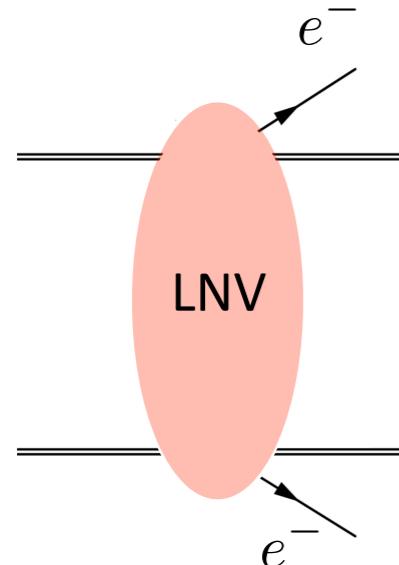
Well-known Majorana mass mechanism



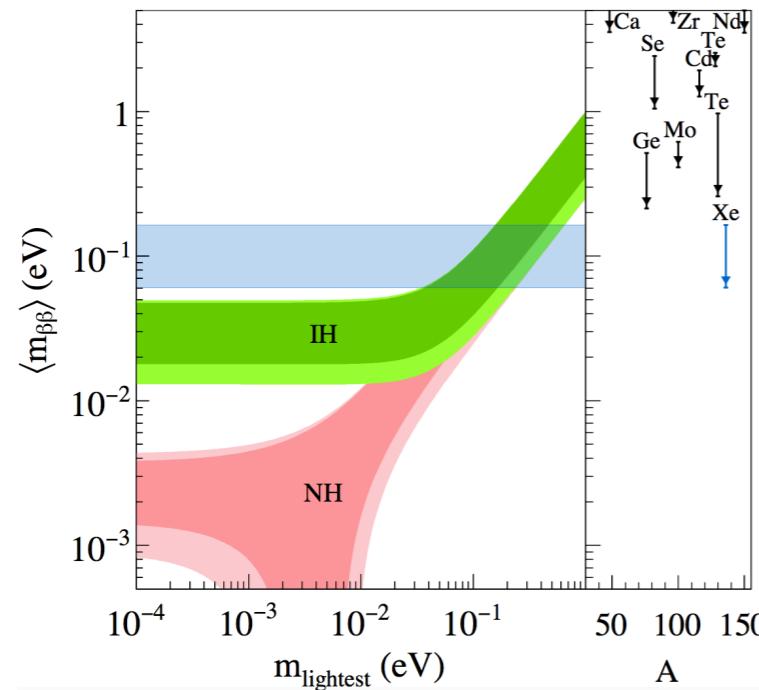
- Implications for the mass hierarchy

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$0\nu\beta\beta$



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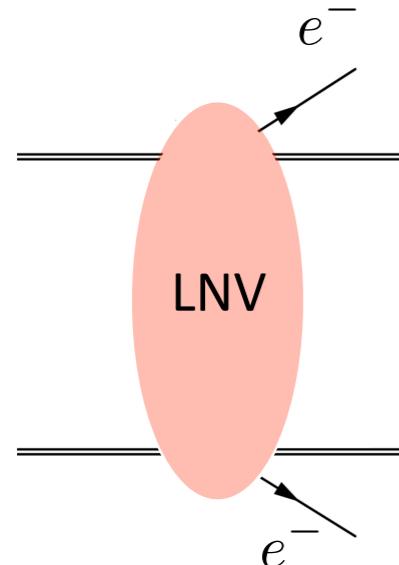
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Heavy BSM mechanisms

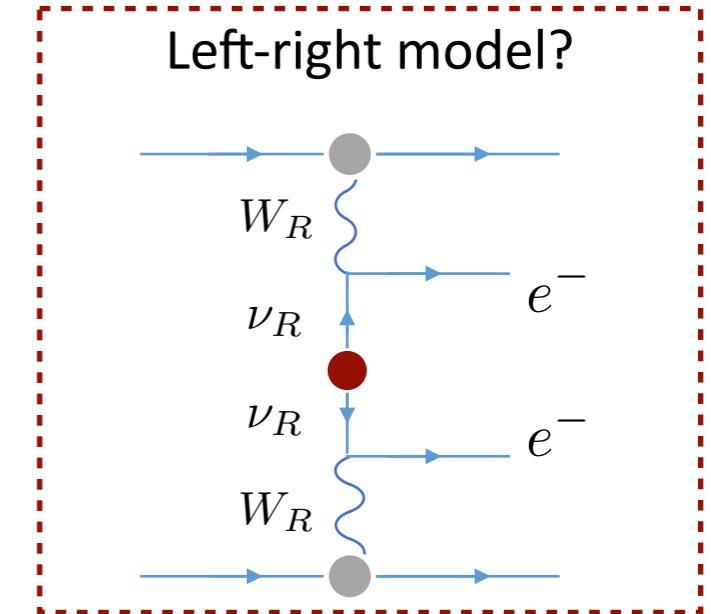
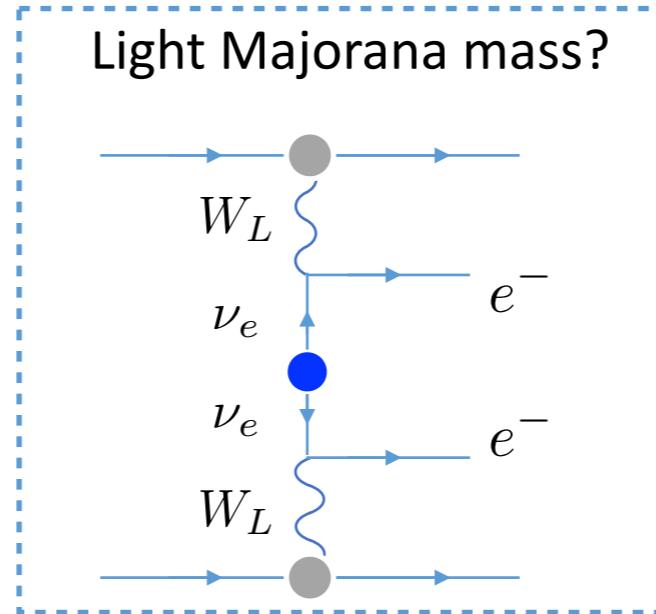
- Many possible scenarios
 - Left-right model,
 - R-parity violating SUSY
 - Leptoquarks...

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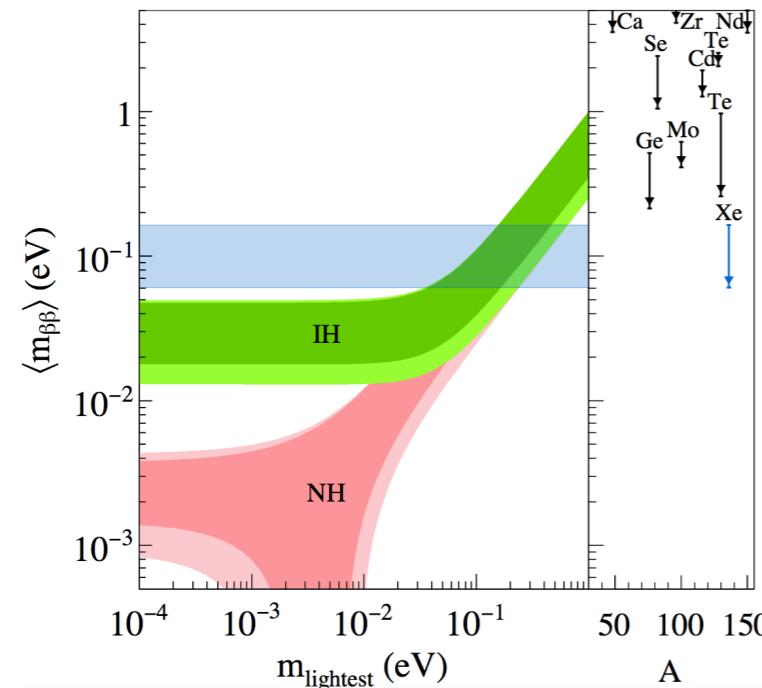


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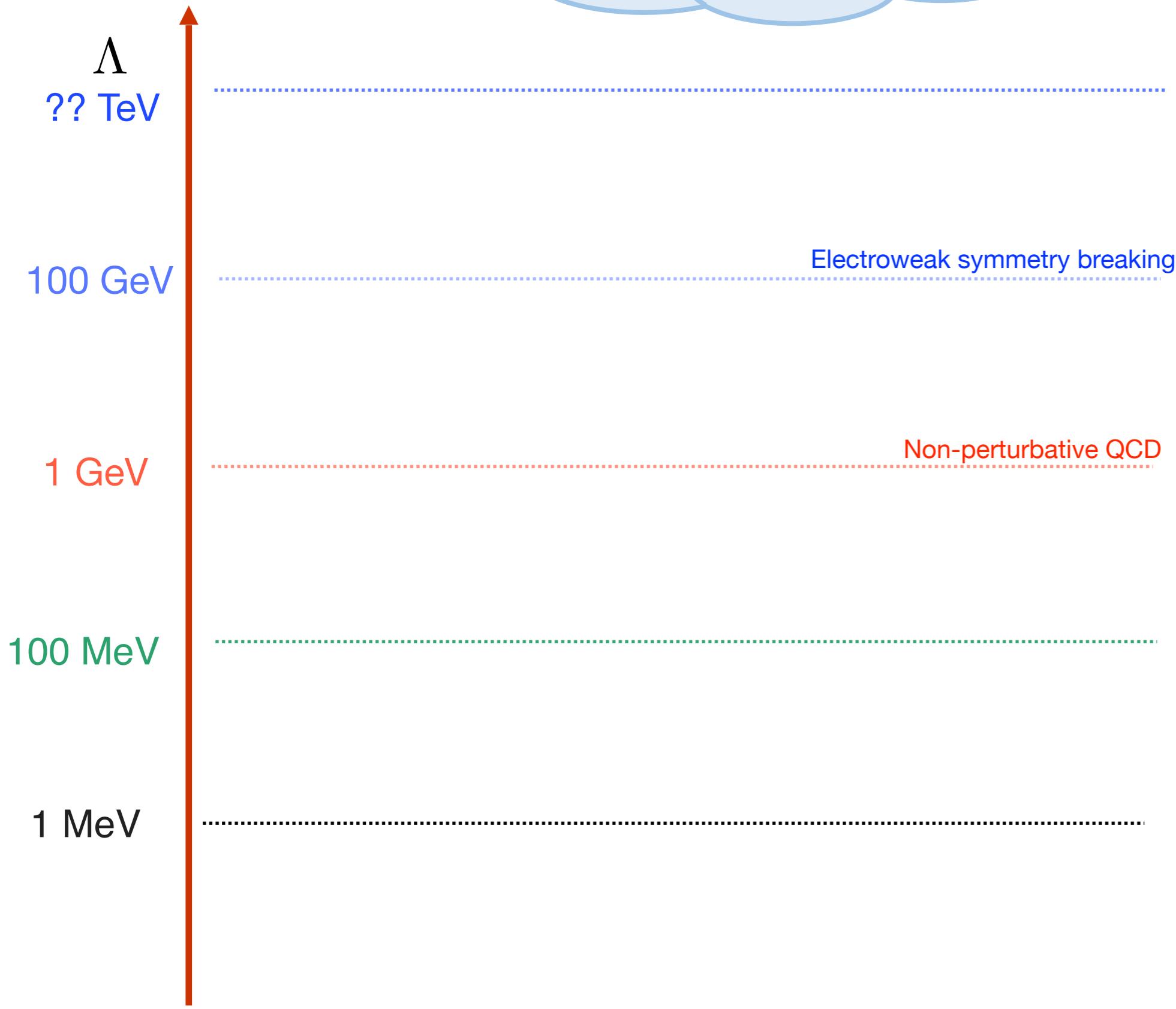
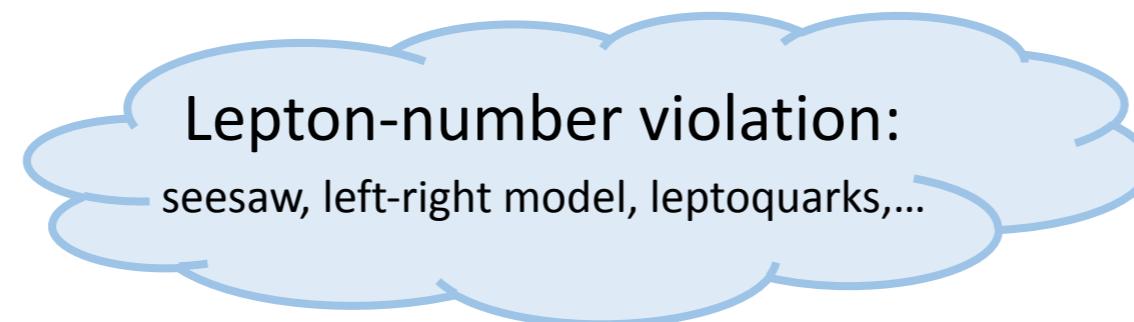


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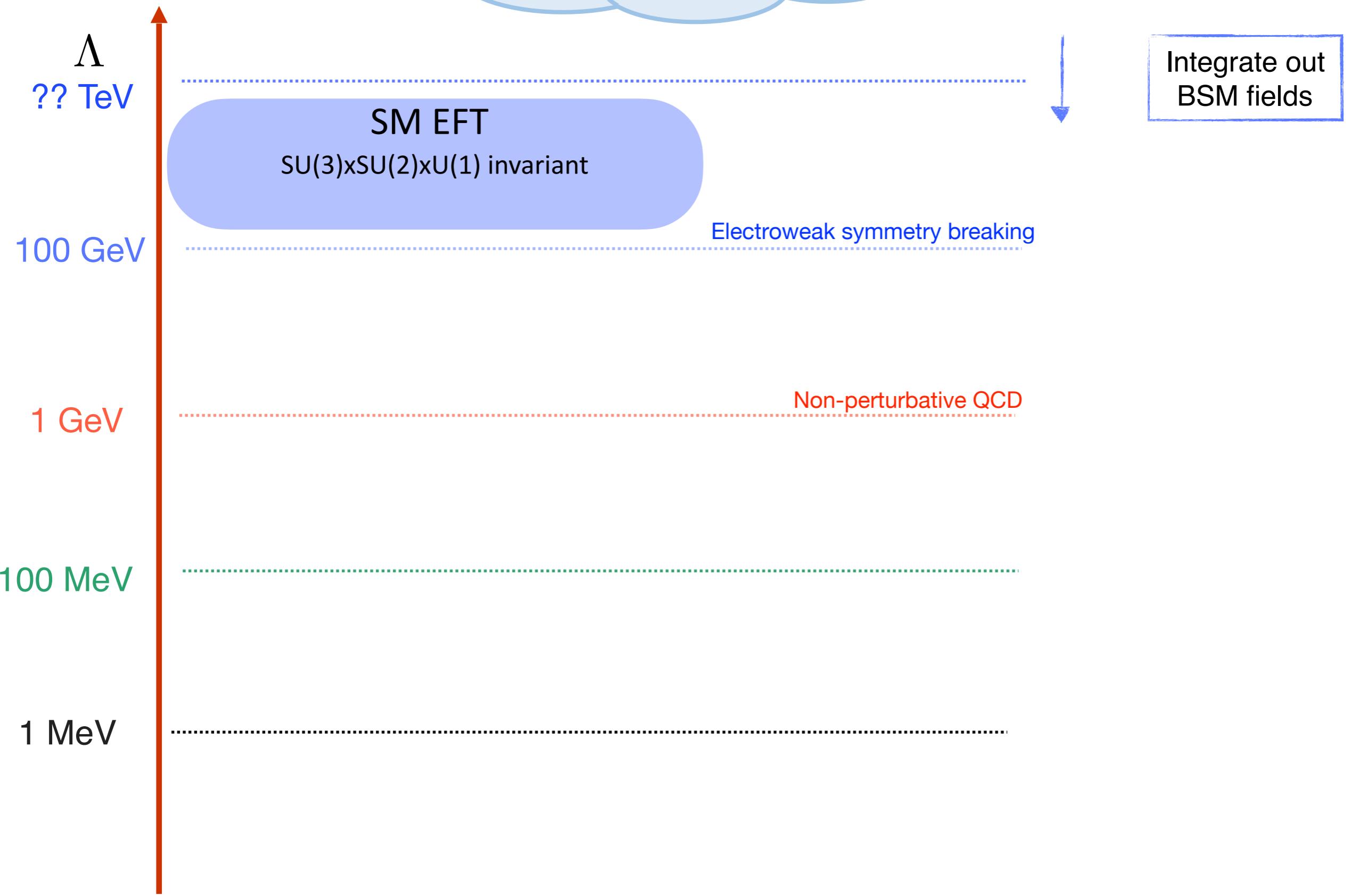
Heavy BSM mechanisms

- Many possible scenarios
 - Left-right model,
 - R-parity violating SUSY
 - Leptoquarks...
- How to describe all LNV sources systematically?

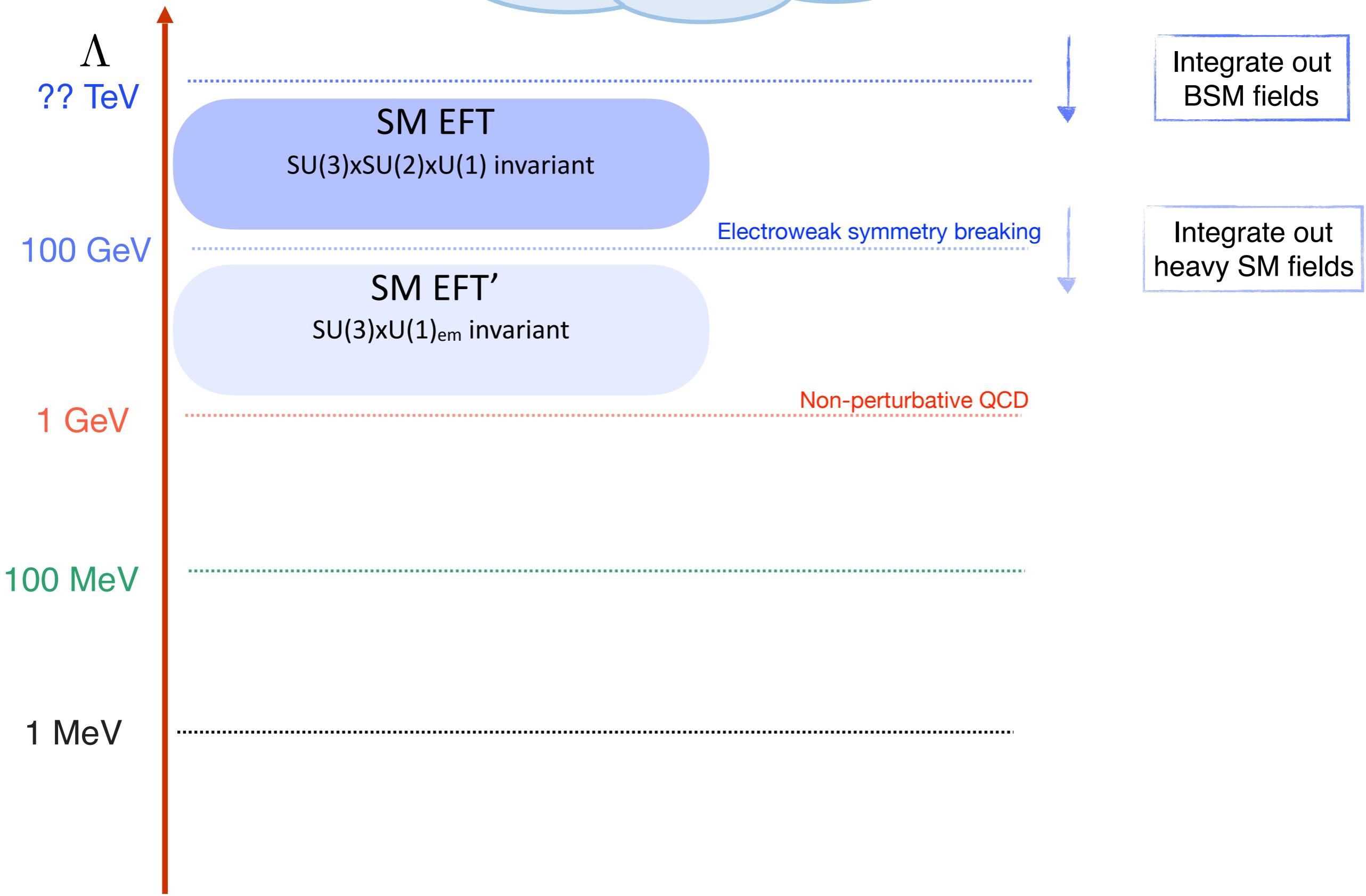
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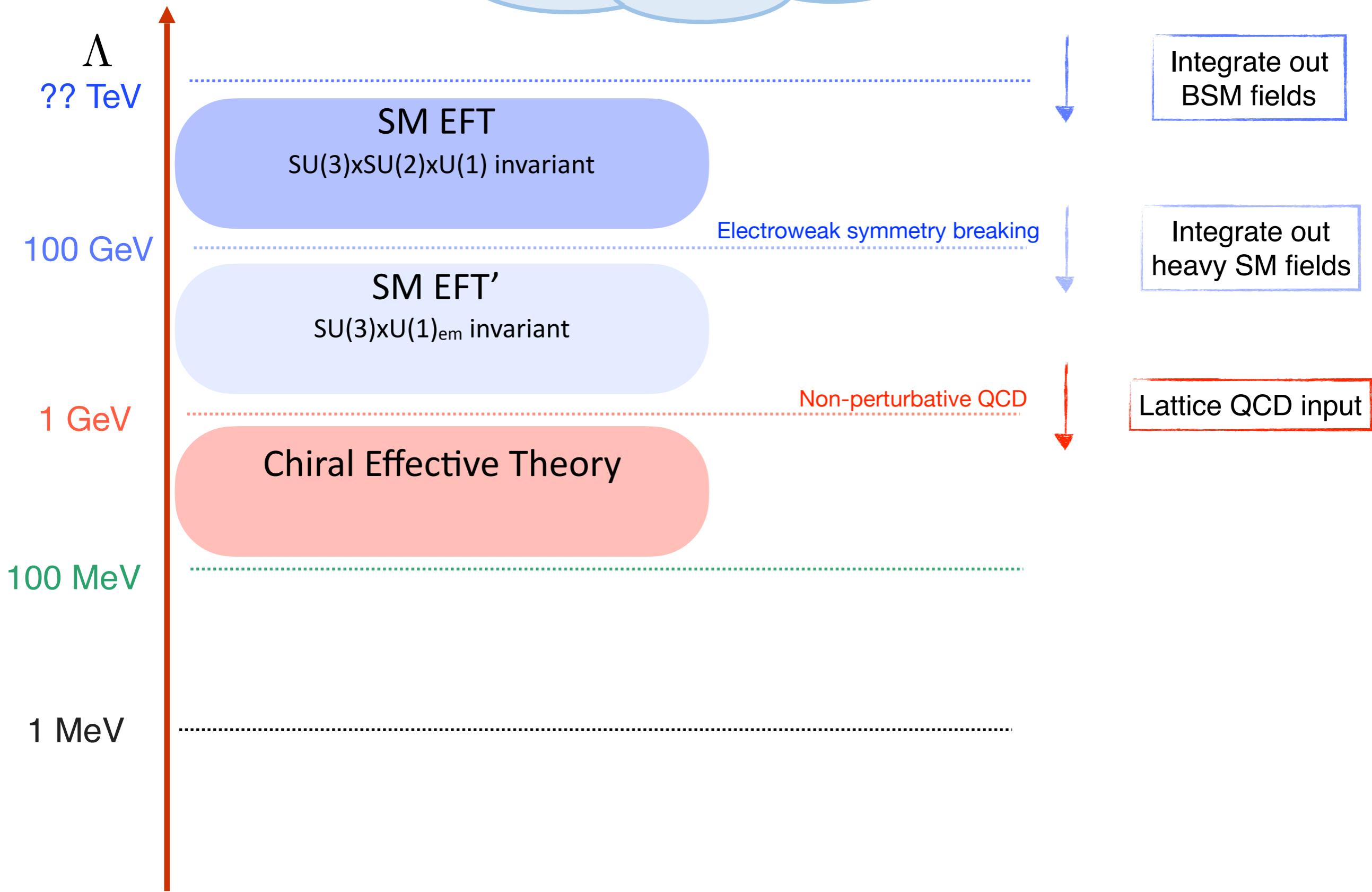
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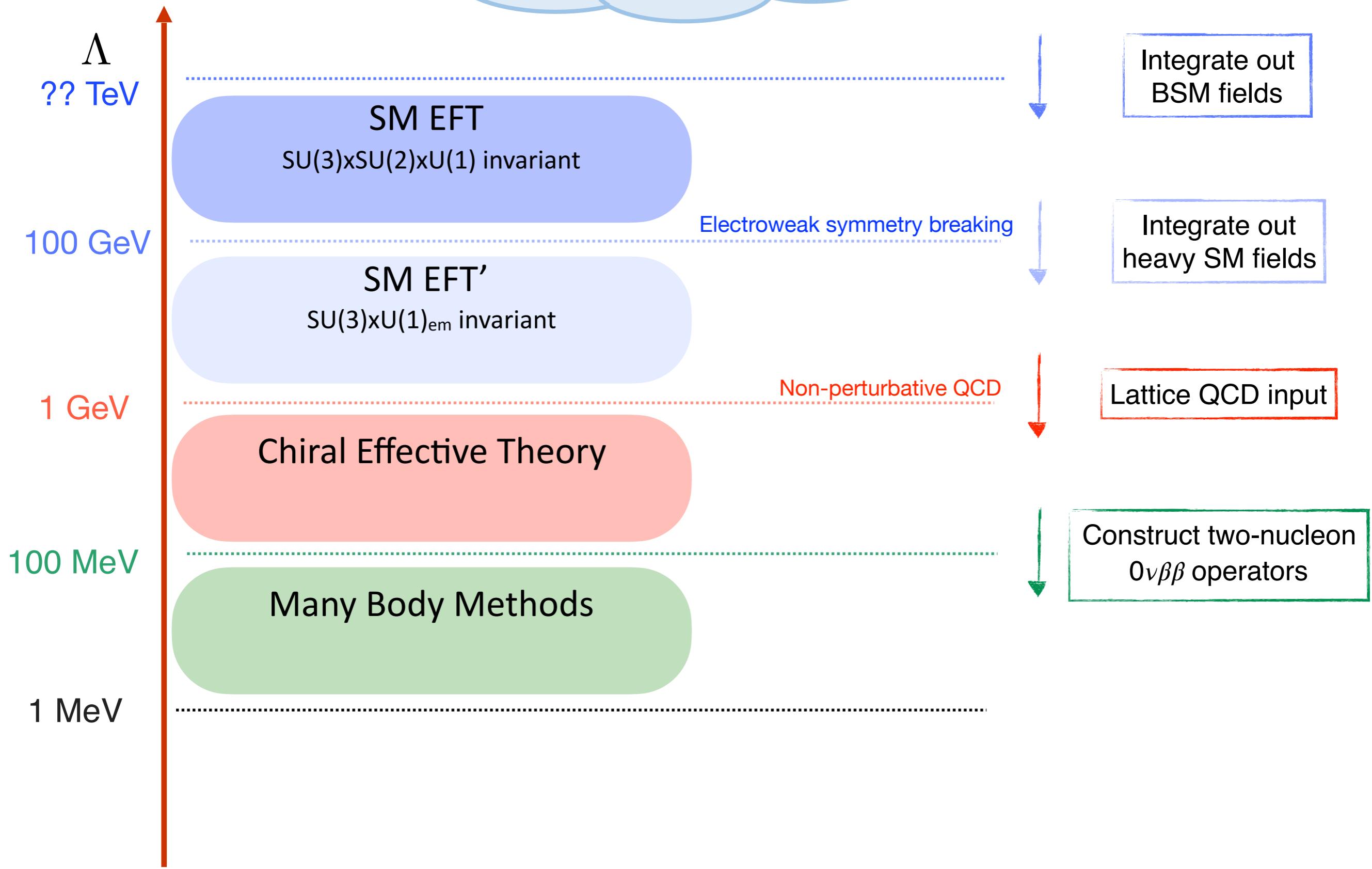
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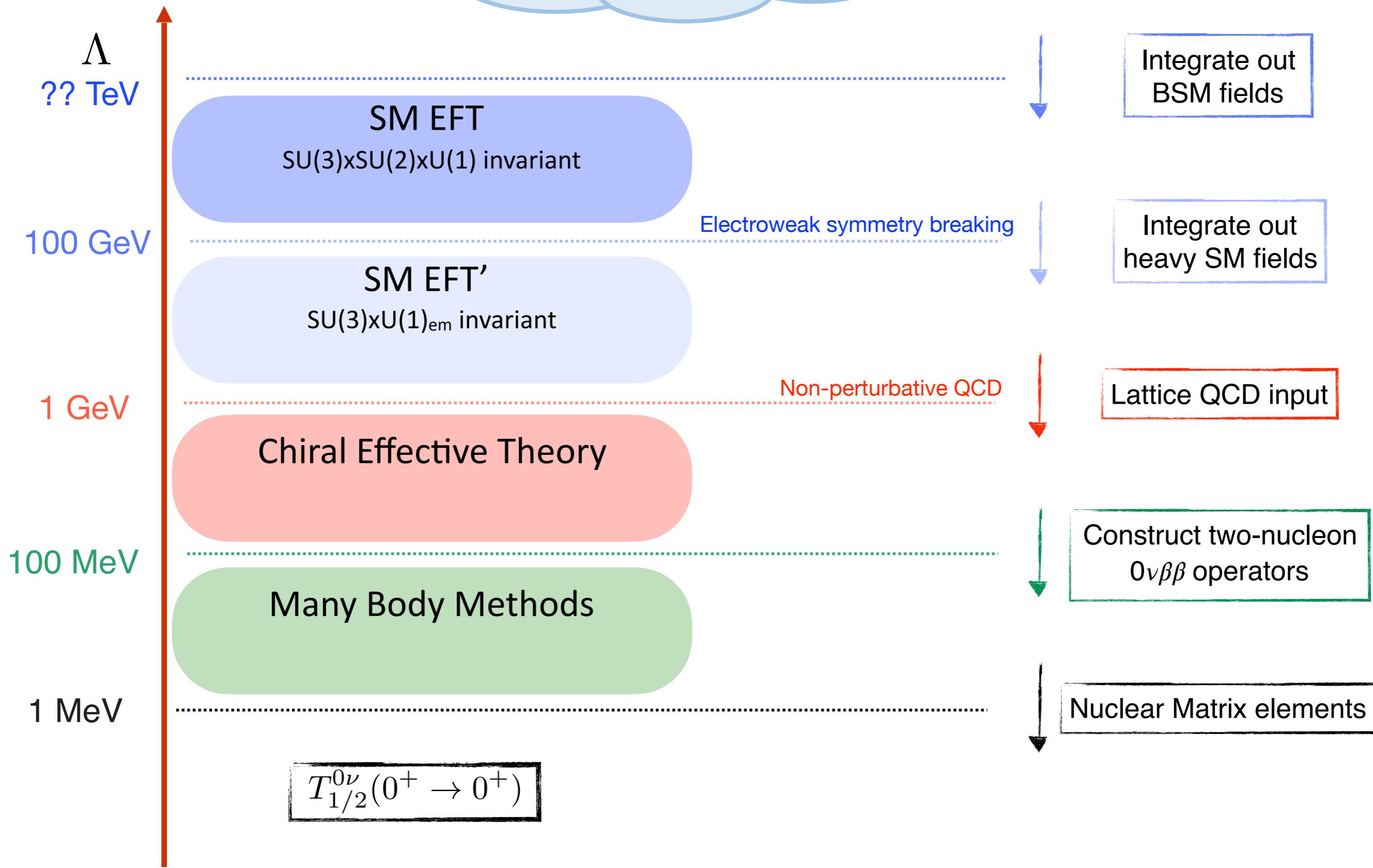
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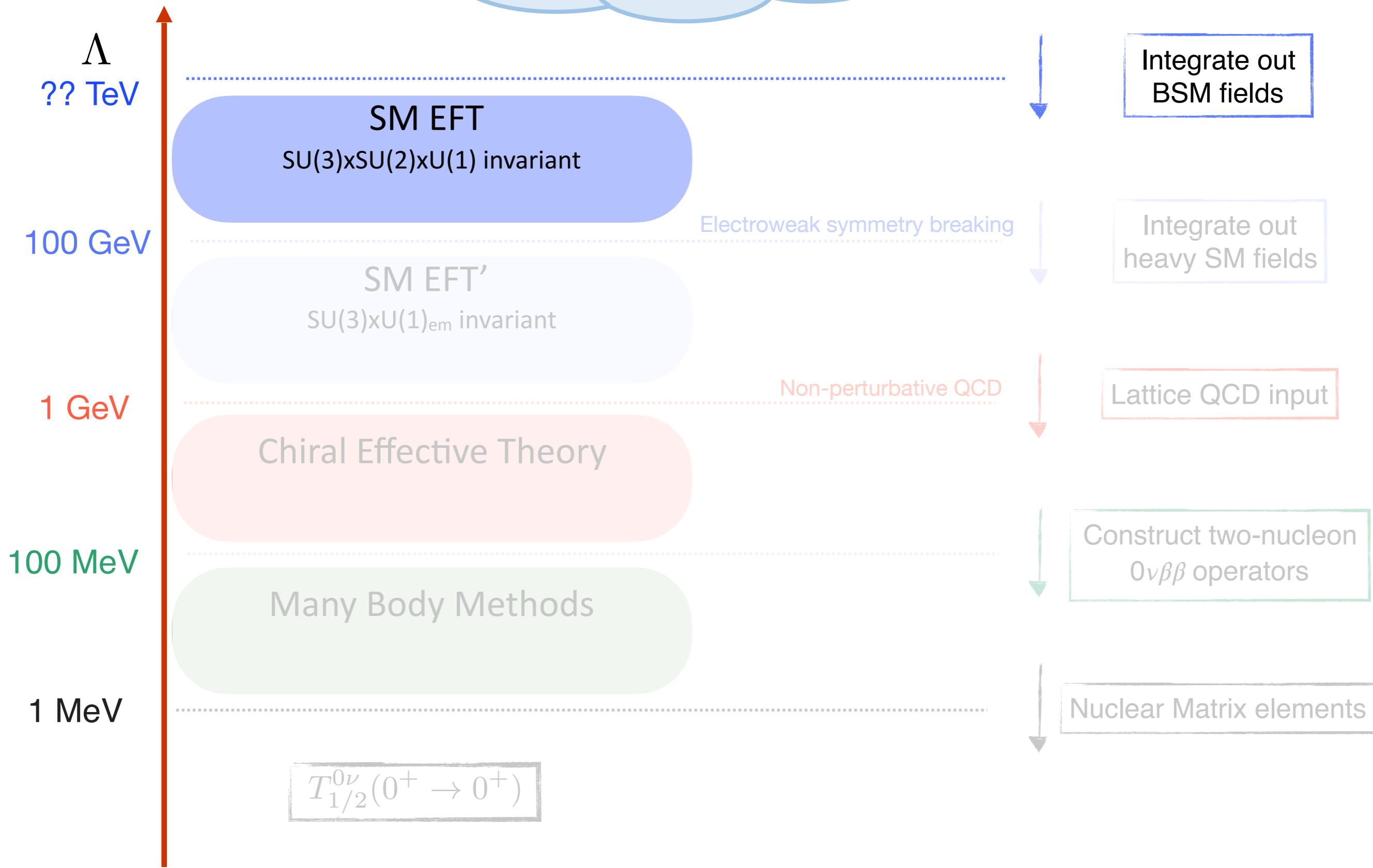
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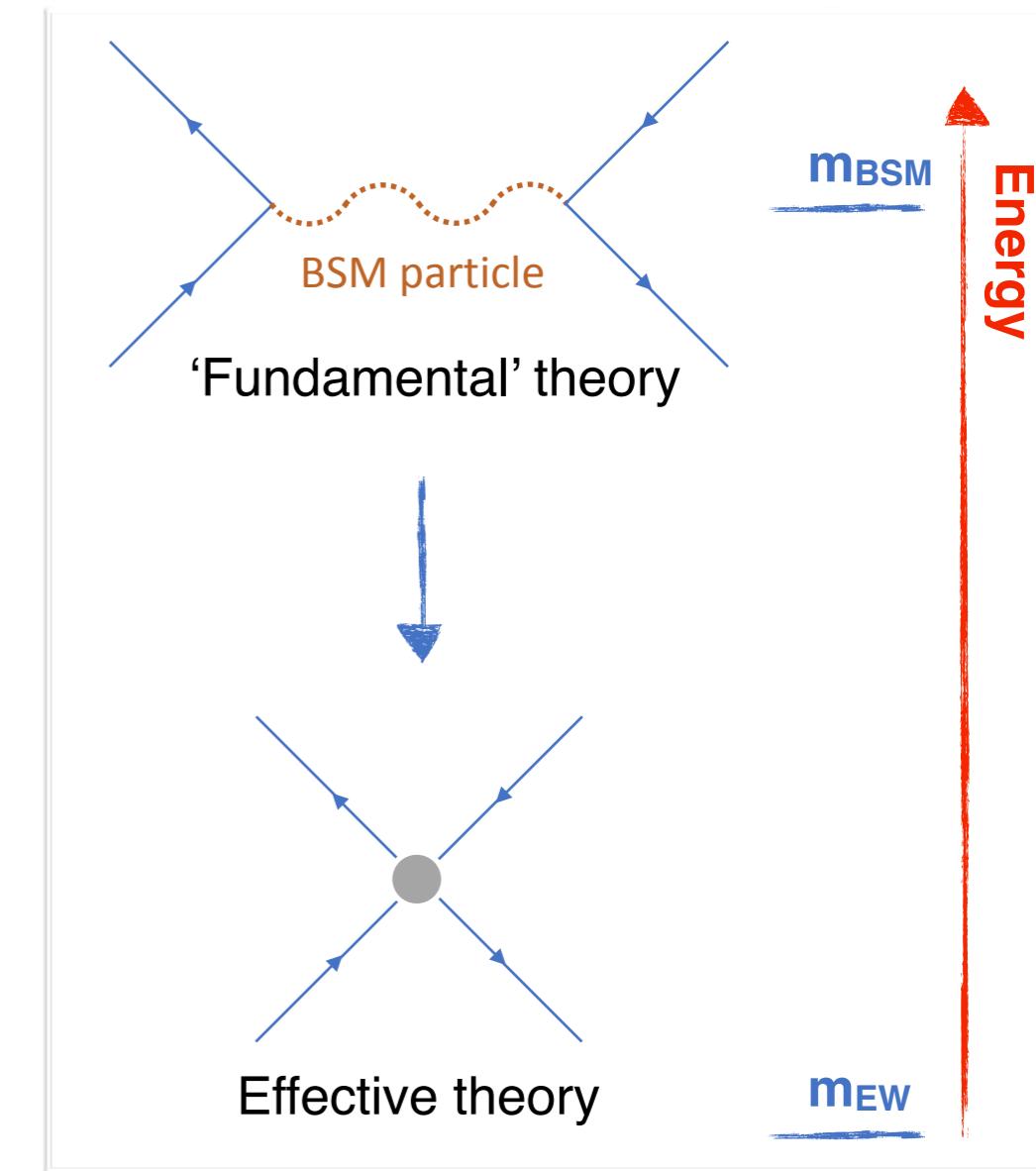


Effective Field Theory

Assumptions

- No new light degrees of freedom
- BSM physics appears above the electroweak scale, $m_{EW} \ll m_{BSM}$
- SM gauge group $SU(3) \times SU(2) \times U(1)$ is linearly realized
(elementary scalar $SU(2)$ doublet)

$$\mathcal{L} = ??$$



$$\mathcal{L}_{eff} = \mathcal{L}_{SM} + \frac{c_i^{(5)}}{\Lambda} O_i^{(5)} + \frac{c_i^{(7)}}{\Lambda^3} O_i^{(7)} + \dots$$

Effective Field Theory

$\Delta L=2$ operators only appear at odd dimensions, 5, 7, 9...

Dimension-five

- Just one operator
- Induces Majorana mass

$$\mathcal{L}_5 = \frac{c_5}{\Lambda} (L^T C \tilde{H})(\tilde{H}^T L)$$

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Dimension-seven

- All operators have been derived
- 12 $\Delta L=2$ operators

$$\mathcal{O}_{LH} \mid \begin{array}{c} 1 : \psi^2 H^4 + \text{h.c.} \\ \hline \epsilon_{ij} \epsilon_{mn} (L^i C L^m) H^j H^n (H^\dagger H) \end{array}$$

$$\mathcal{O}_{LHDe} \mid \begin{array}{c} 3 : \psi^2 H^3 D + \text{h.c.} \\ \hline \epsilon_{ij} \epsilon_{mn} (L^i C \gamma_\mu e) H^j H^m D^\mu H^n \end{array}$$

5 : $\psi^4 D + \text{h.c.}$	
$\mathcal{O}_{LL\bar{d}uD}^{(1)}$	$\epsilon_{ij} (\bar{d} \gamma_\mu u) (L^i C D^\mu L^j)$
$\mathcal{O}_{LL\bar{d}uD}^{(2)}$	$\epsilon_{ij} (\bar{d} \gamma_\mu u) (L^i C \sigma^{\mu\nu} D_\nu L^j)$
$\mathcal{O}_{\bar{L}QddD}^{(1)}$	$(QC \gamma_\mu d) (\bar{L} D^\mu d)$
$\mathcal{O}_{\bar{L}QddD}^{(2)}$	$(\bar{L} \gamma_\mu Q) (d C D^\mu d)$
$\mathcal{O}_{ddde\bar{D}}$	$(\bar{e} \gamma_\mu d) (d C D^\mu d)$

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$$\begin{array}{c} 5 : \psi^4 D + \text{h.c.} \\ \hline \begin{array}{ll} \mathcal{O}_{LL\bar{d}uD}^{(1)} & \epsilon_{ij} (\bar{d} \gamma_\mu u) (L^i C D^\mu L^j) \\ \mathcal{O}_{LL\bar{d}uD}^{(2)} & \epsilon_{ij} (\bar{d} \gamma_\mu u) (L^i C \sigma^{\mu\nu} D_\nu L^j) \\ \mathcal{O}_{\bar{L}QddD}^{(1)} & (Q C \gamma_\mu d) (\bar{L} D^\mu d) \\ \mathcal{O}_{\bar{L}QddD}^{(2)} & (\bar{L} \gamma_\mu Q) (d C D^\mu d) \\ \mathcal{O}_{ddde\bar{D}} & (\bar{e} \gamma_\mu d) (d C D^\mu d) \end{array} \end{array}$$

Dimension-nine

- Subset of operators constructed

$$\begin{aligned} \text{LM1} &= i\sigma_{ab}^{(2)} (\bar{Q}_a \gamma^\mu Q_c) (\bar{u}_R \gamma_\mu d_R) (\bar{\ell}_b \ell_c^C) \\ \text{LM2} &= i\sigma_{ab}^{(2)} (\bar{Q}_a \gamma^\mu \lambda^A Q_c) (\bar{u}_R \gamma_\mu \lambda^A d_R) (\bar{\ell}_b \ell_c^C) \\ \text{LM3} &= (\bar{u}_R Q_a) (\bar{u}_R Q_b) (\bar{\ell}_a \ell_b^C) \\ \text{LM4} &= (\bar{u}_R \lambda^A Q_a) (\bar{u}_R \lambda^A Q_b) (\bar{\ell}_a \ell_b^C) \\ \text{LM5} &= i\sigma_{ab}^{(2)} i\sigma_{cd}^{(2)} (\bar{Q}_a d_R) (\bar{Q}_c d_R) (\bar{\ell}_b \ell_d^C) \\ \text{LM6} &= i\sigma_{ab}^{(2)} i\sigma_{cd}^{(2)} (\bar{Q}_a \lambda^A d_R) (\bar{Q}_c \lambda^A d_R) (\bar{\ell}_b \ell_d^C) \\ \text{LM7} &= (\bar{u}_R \gamma^\mu d_R) (\bar{u}_R \gamma_\mu d_R) (\bar{e}_R e_R^C) \\ \text{LM8} &= (\bar{u}_R \gamma^\mu d_R) i\sigma_{ab}^{(2)} (\bar{Q}_a d_R) (\bar{\ell}_b \gamma_\mu e_R^C) \\ \text{LM9} &= (\bar{u}_R \gamma^\mu \lambda^A d_R) i\sigma_{ab}^{(2)} (\bar{Q}_a \lambda^A d_R) (\bar{\ell}_b \gamma_\mu e_R^C) \\ \text{LM10} &= (\bar{u}_R \gamma^\mu d_R) (\bar{u}_R Q_a) (\bar{\ell}_a \gamma_\mu e_R^C) \\ \text{LM11} &= (\bar{u}_R \gamma^\mu \lambda^A d_R) (\bar{u}_R \lambda^A Q_a) (\bar{\ell}_a \gamma_\mu e_R^C) \end{aligned}$$

- But no complete basis

Effective Field Theory

Naive scaling of Dimension 5, 7, 9 operators

$$\mathcal{A}_{0\nu\beta\beta} \sim \frac{c_5}{\Lambda} \left[1 + \left(\frac{v}{\Lambda}\right)^2 \frac{c_7}{c_5} + \left(\frac{v}{\Lambda}\right)^4 \frac{c_9}{c_5} \right]$$

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$m_\nu \sim c_5 v^2 / \Lambda$ implies two possible extremes:

- $c_5 = \mathcal{O}(1), \quad \Lambda = 10^{15} \text{ GeV}$ dimension-7, -9 irrelevant in this case (no signal at colliders)

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- This happens in well-known BSM models
 - For example the Left right model gives

$$c_9 = \mathcal{O}(1), \quad c_7 = \mathcal{O}(y_e), \quad c_5 = \mathcal{O}(y_e^2)$$

$$y_e = m_e/v \sim 10^{-6}$$

- The dimension-5, -7 and -9 operators can all be relevant for $\Lambda = \mathcal{O}(1 - 100) \text{ TeV}$

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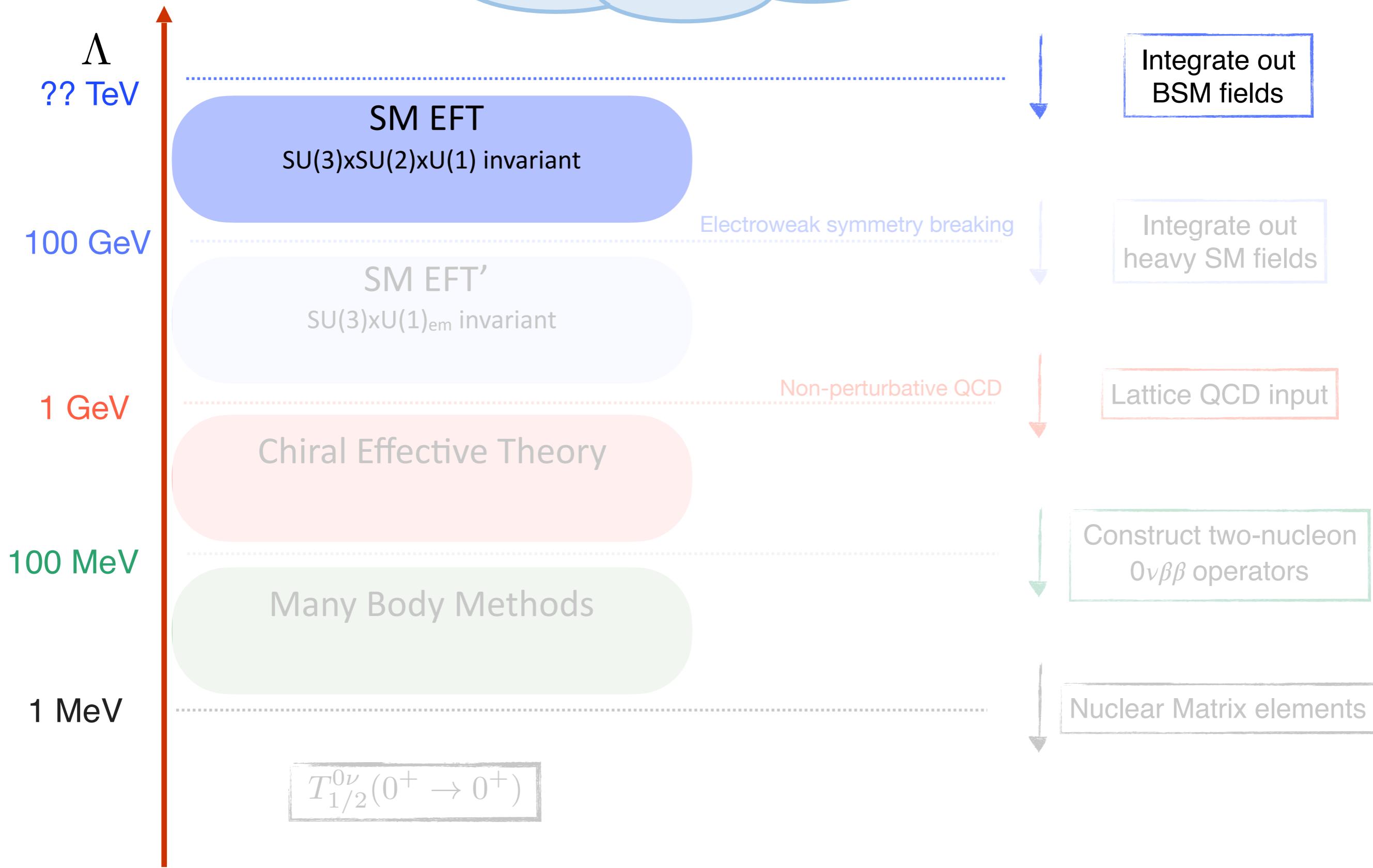
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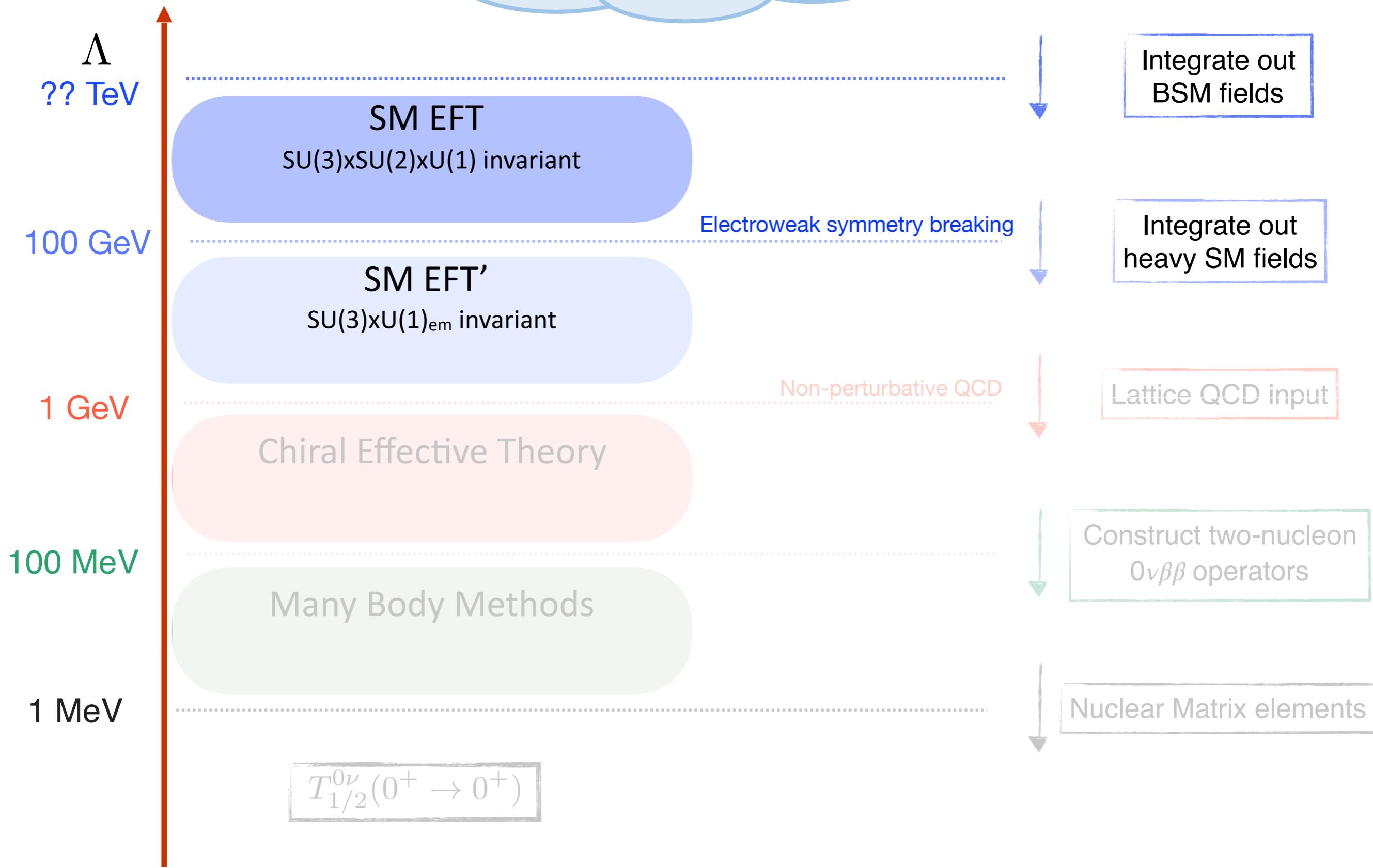
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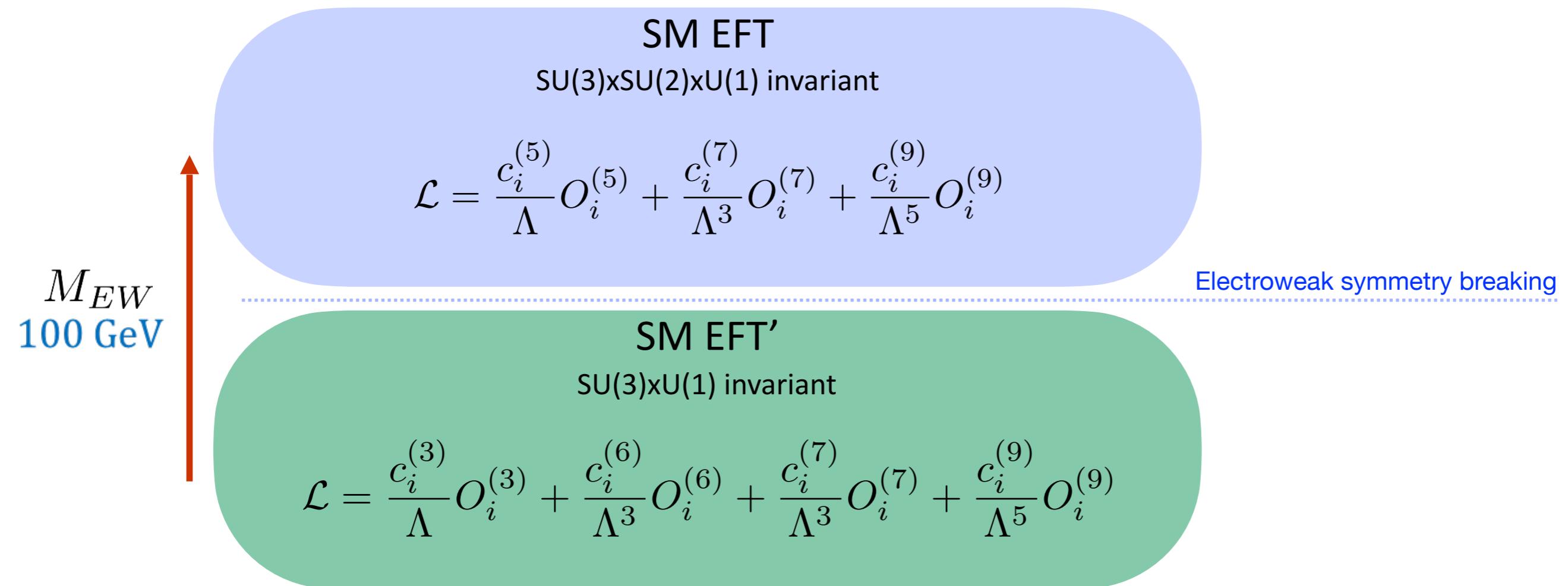
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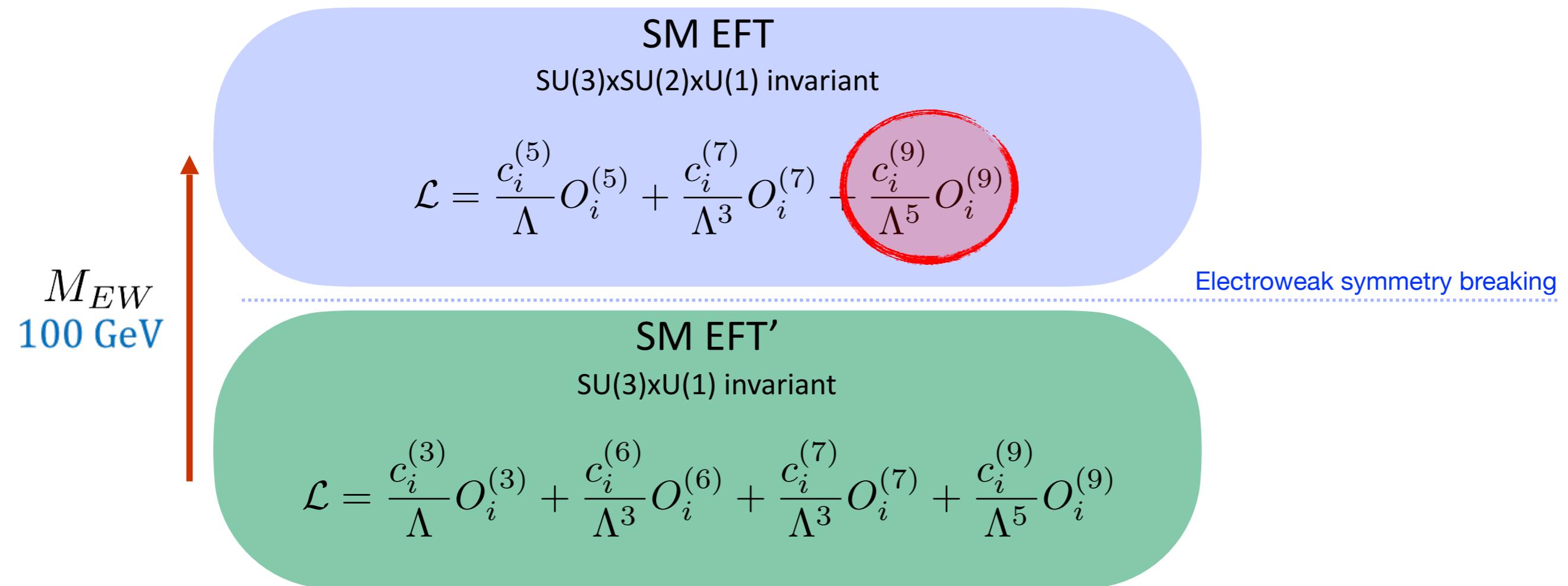


Matching at the electroweak scale



- Mismatch in dimensions due to insertions of the Higgs vacuum expectation value

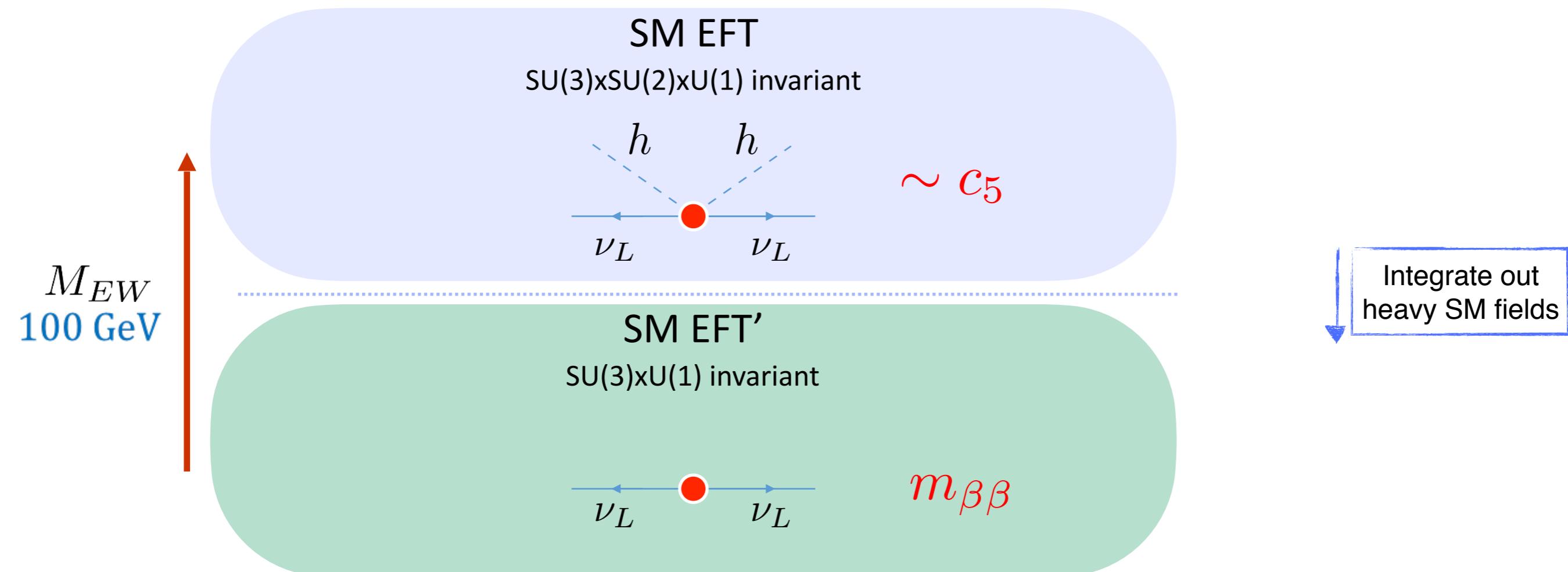
Matching at the electroweak scale



- Mismatch in dimensions due to insertions of the Higgs vacuum expectation value
- Complete basis unknown
- Take into account the known dimension-9 terms

Low-energy operators

Dimension-3

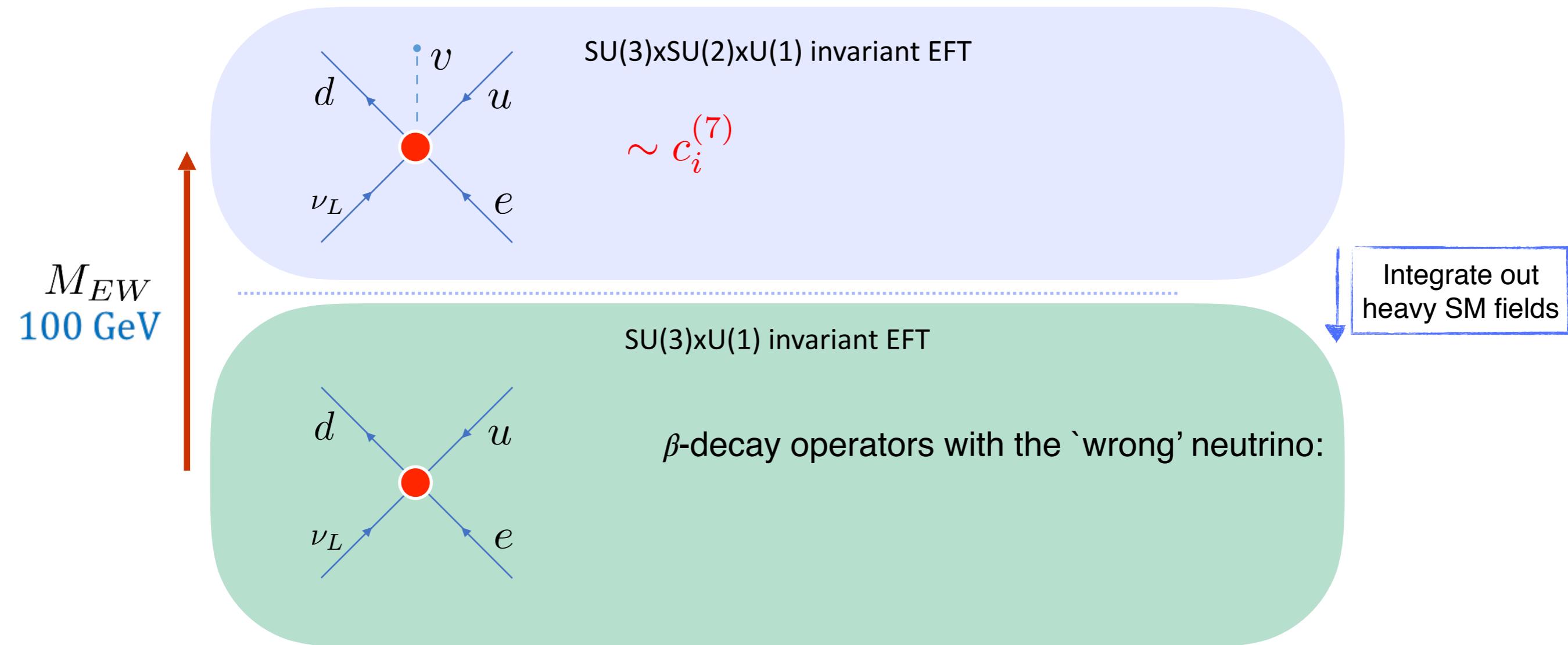


Induced by dimension-5 $SU(2)$ -invariant operator

$$m_{\beta\beta} \sim v^2 / \Lambda$$

Low-energy operators

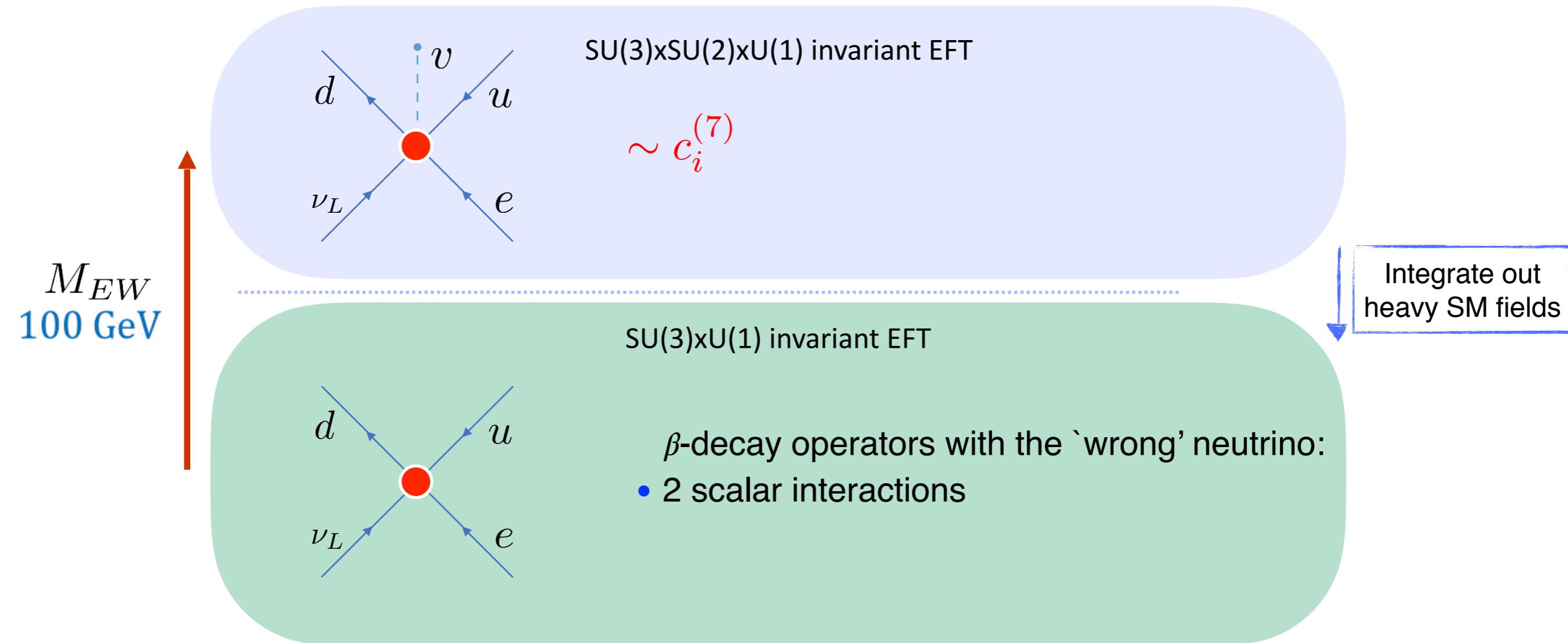
Dimension-6



$$\begin{aligned} \mathcal{L}_{\Delta L=2}^{(6)} = & \frac{2G_F}{\sqrt{2}} \left\{ C_{\text{VL},ij}^{(6)} \bar{u}_L \gamma^\mu d_L \bar{e}_{R,i} \gamma_\mu C \bar{\nu}_{L,j}^T + C_{\text{VR},ij}^{(6)} \bar{u}_R \gamma^\mu d_R \bar{e}_{R,i} \gamma_\mu C \bar{\nu}_{L,j}^T \right. \\ & \left. + C_{\text{SR},ij}^{(6)} \bar{u}_L d_R \bar{e}_{L,i} C \bar{\nu}_{L,j}^T + C_{\text{SL},ij}^{(6)} \bar{u}_R d_L \bar{e}_{L,i} C \bar{\nu}_{L,j}^T + C_{\text{T},ij}^{(6)} \bar{u}_L \sigma^{\mu\nu} d_R \bar{e}_{L,i} \sigma_{\mu\nu} C \bar{\nu}_{L,j}^T \right\} \end{aligned}$$

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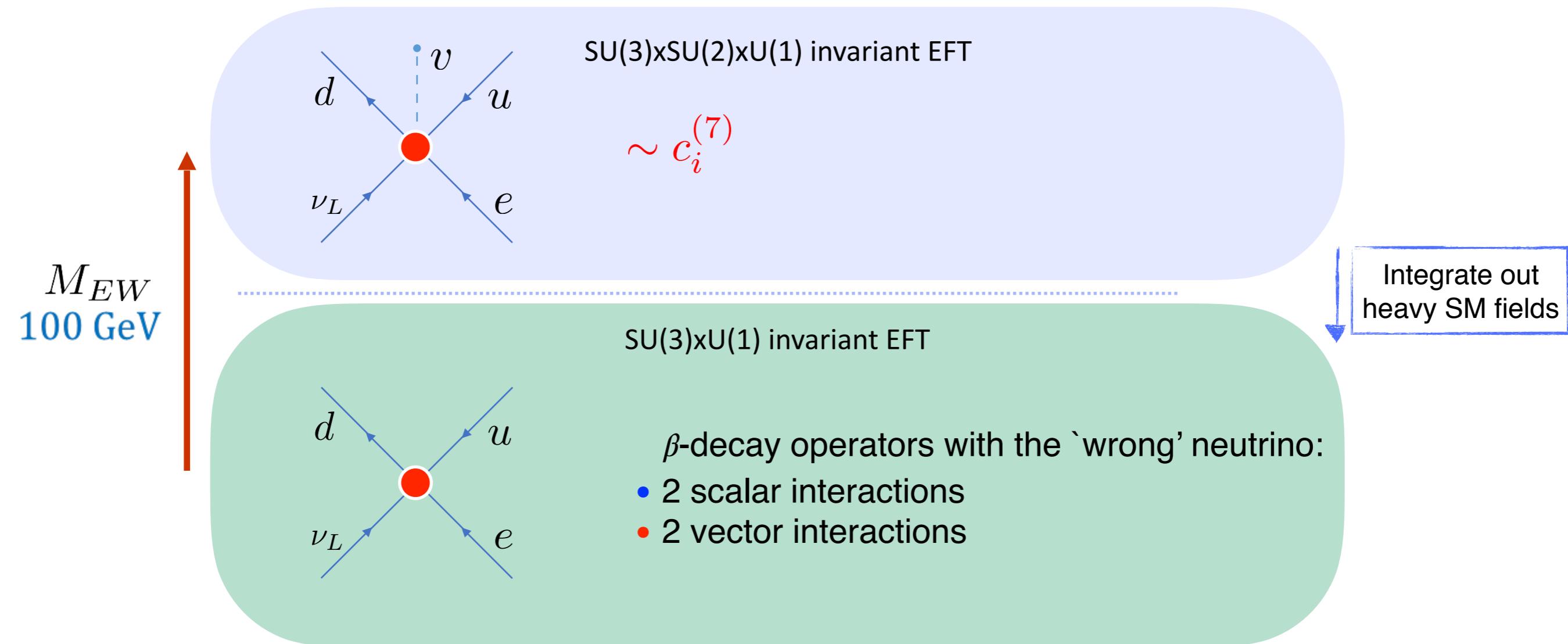
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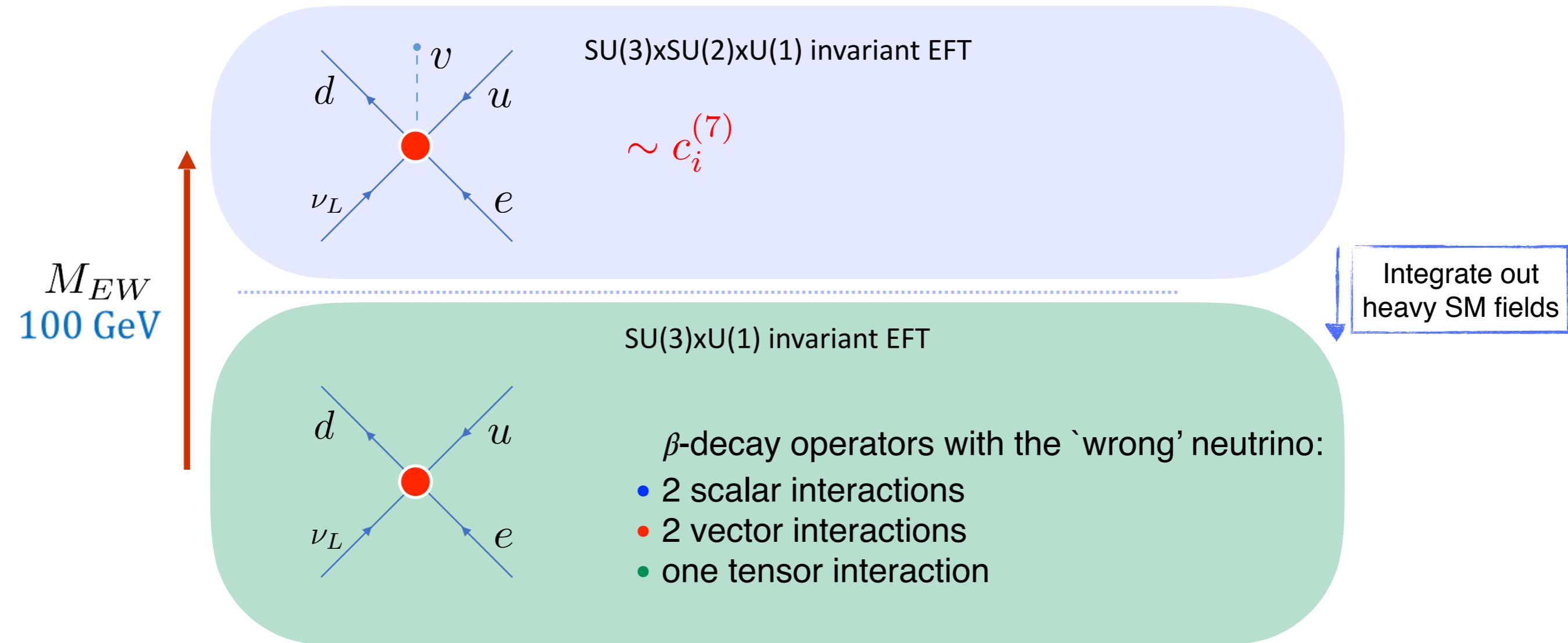
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Low-energy operators

Dimension-6

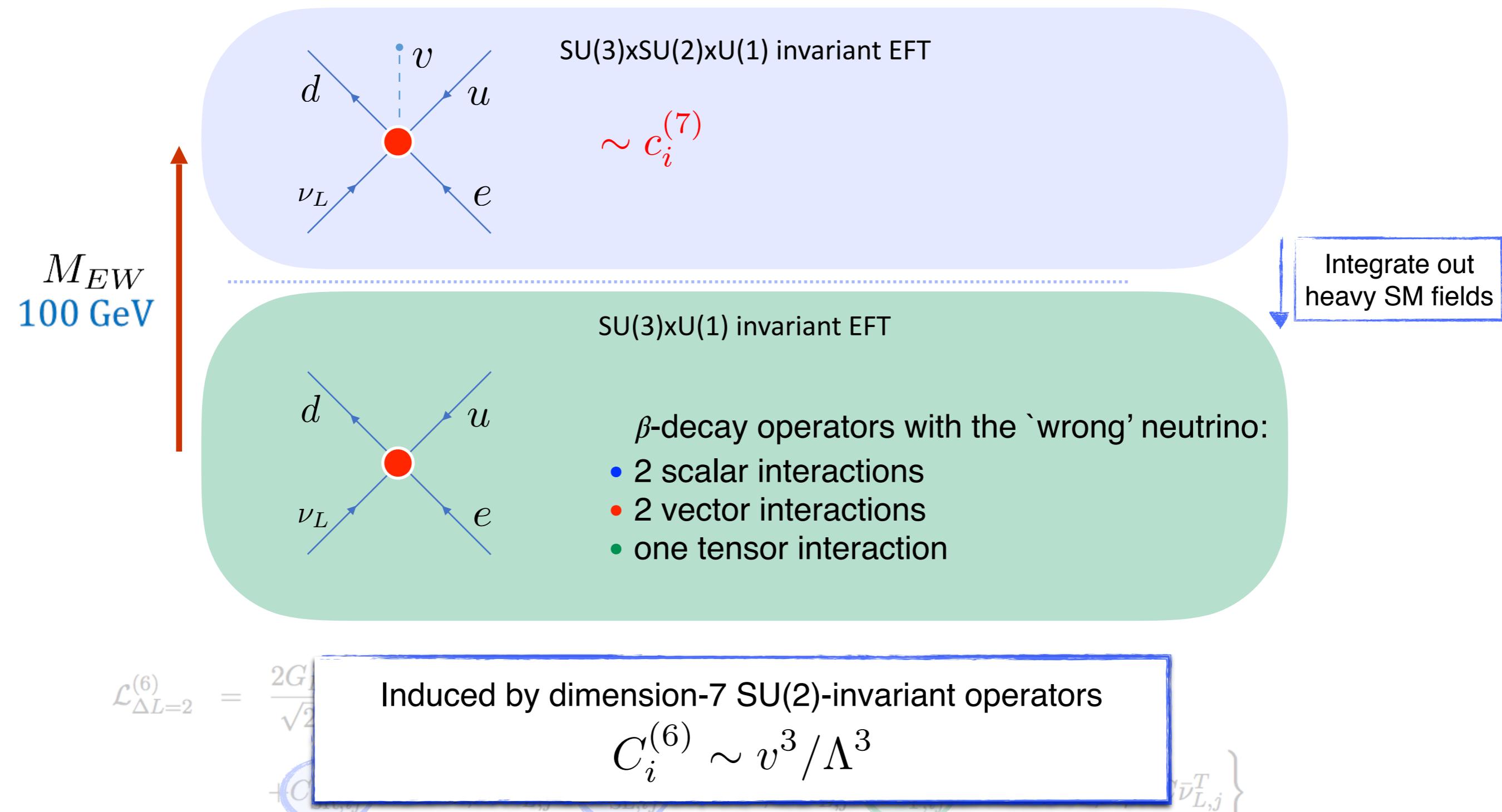


$$\mathcal{L}_{\Delta L=2}^{(6)} = \frac{2G_F}{\sqrt{2}} \left\{ C_{VL,ij}^{(6)} \bar{\nu}_L \gamma^\mu d_L \bar{e}_{R,i} \gamma_\mu C \bar{\nu}_{L,j}^T + C_{VR,ij}^{(6)} \bar{u}_R \gamma^\mu d_R \bar{e}_{R,i} \gamma_\mu C \bar{\nu}_{L,j}^T \right.$$

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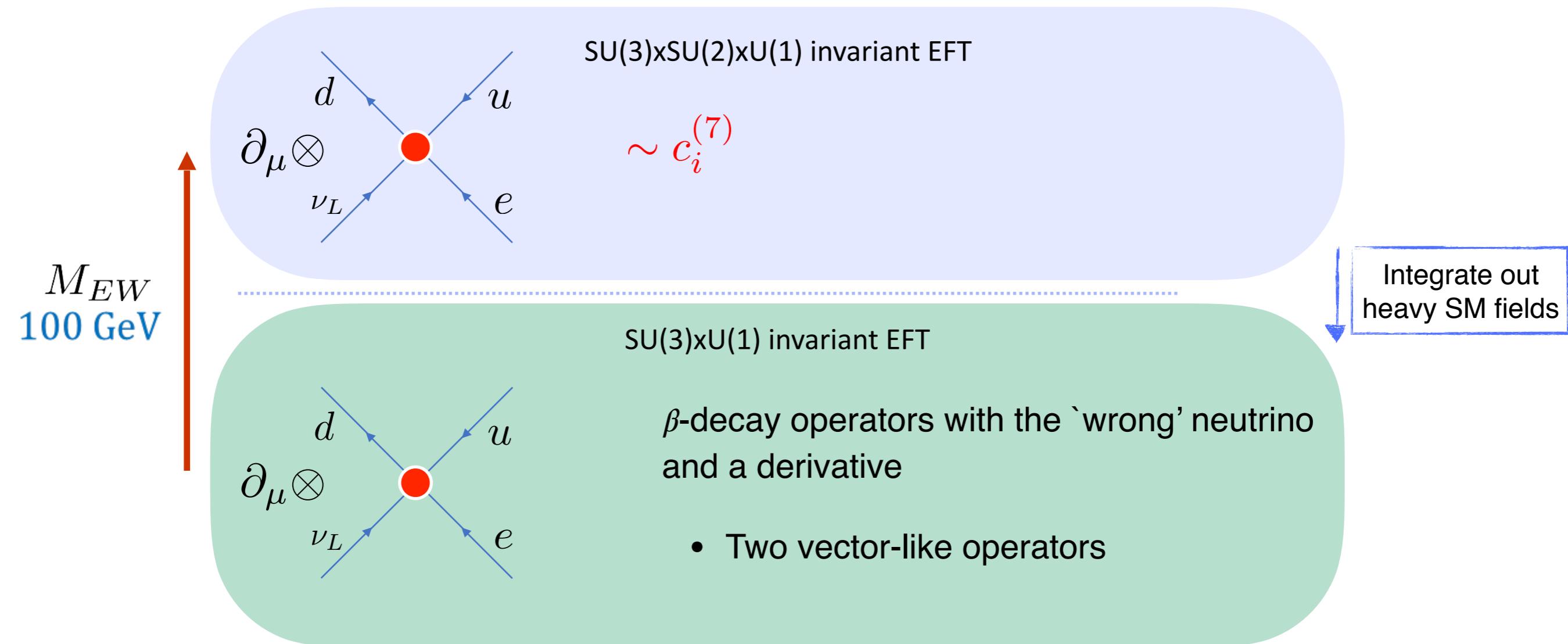
Low-energy operators

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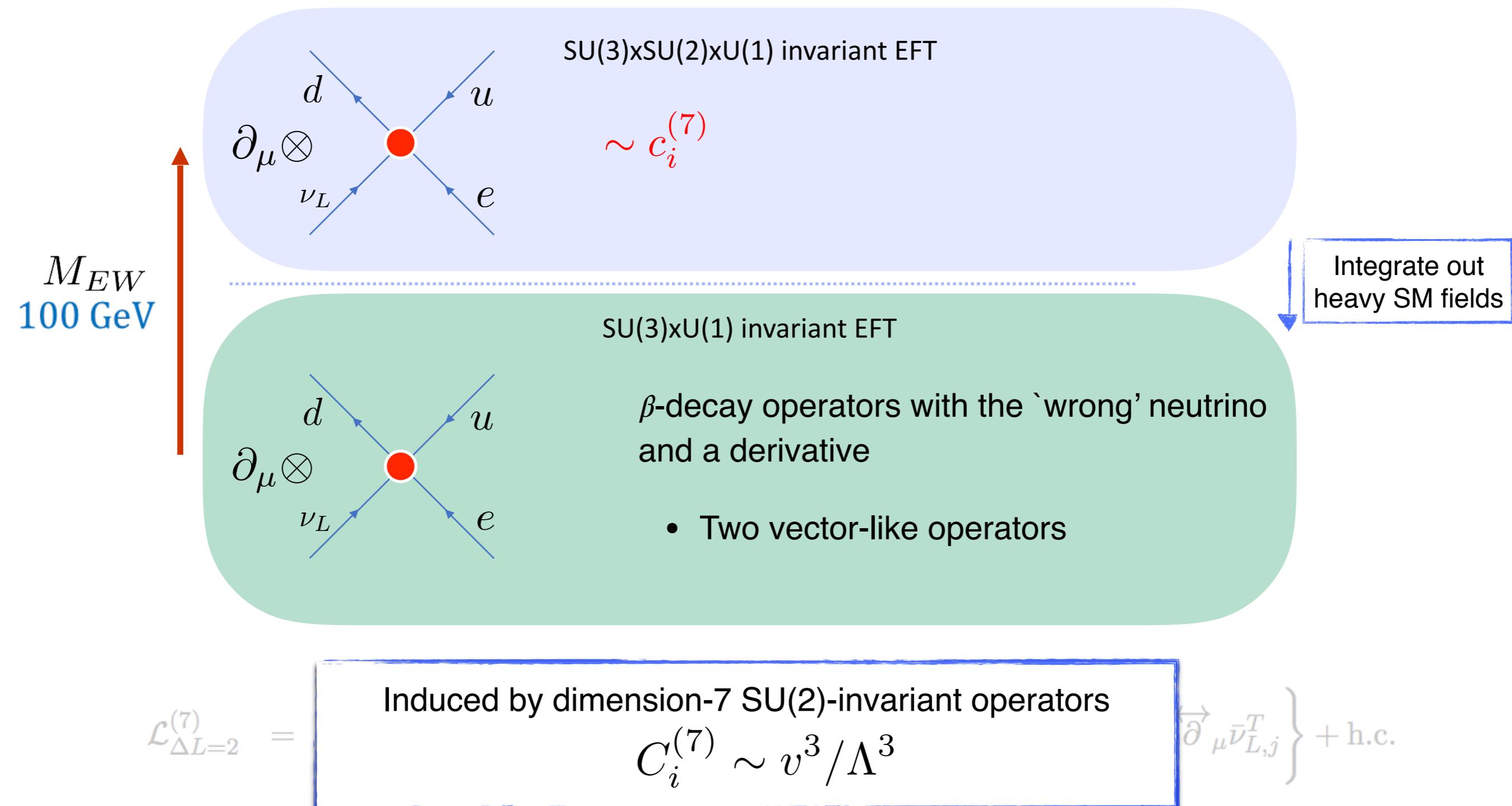
Dimension-7



$$\mathcal{L}_{\Delta L=2}^{(7)} = \frac{2G_F}{\sqrt{2}v} \left\{ C_{\text{VL},ij}^{(7)} \bar{u}_L \gamma^\mu d_L \bar{e}_{L,i} C i \overleftrightarrow{\partial}_\mu \bar{\nu}_{L,j}^T + C_{\text{VR},ij}^{(7)} \bar{u}_R \gamma^\mu d_R \bar{e}_{L,i} C i \overleftrightarrow{\partial}_\mu \bar{\nu}_{L,j}^T \right\} + \text{h.c.}$$

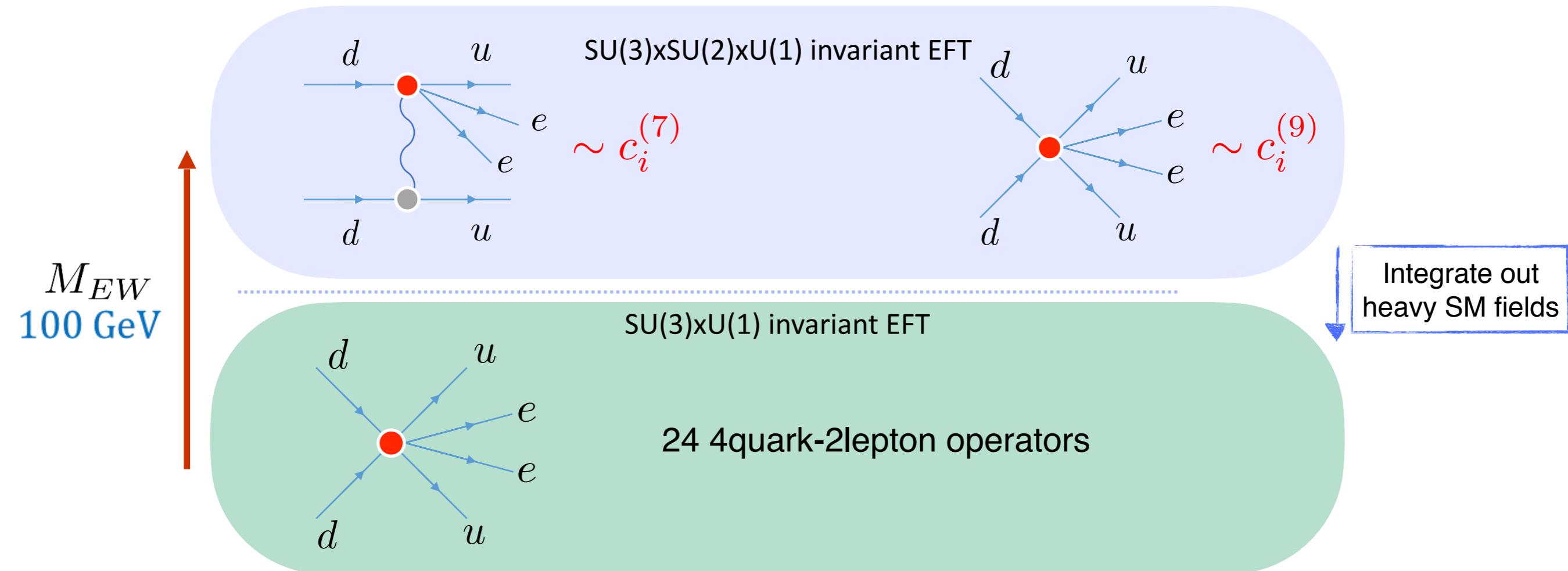
Low-energy operators

Dimension-7



Low-energy operators

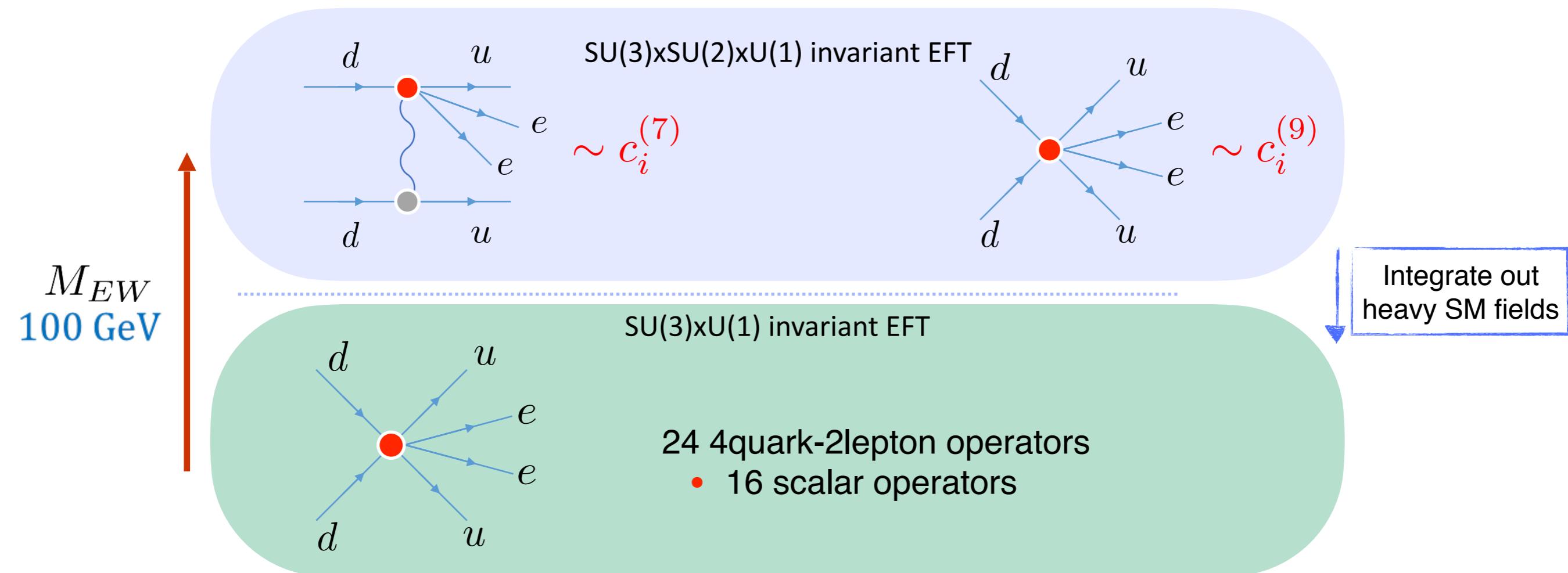
Dimension-9



$$\mathcal{L}_{\Delta L=2}^{(9)} = \frac{1}{v^5} \sum_i \left[\left(C_{iR}^{(9)} \bar{e}_R C \bar{e}_R^T + C_{iL}^{(9)} \bar{e}_L C \bar{e}_L^T \right) O_i + C_i^{(9)} \bar{e} \gamma_\mu \gamma_5 C \bar{e}^T O_i^\mu \right],$$

Low-energy operators

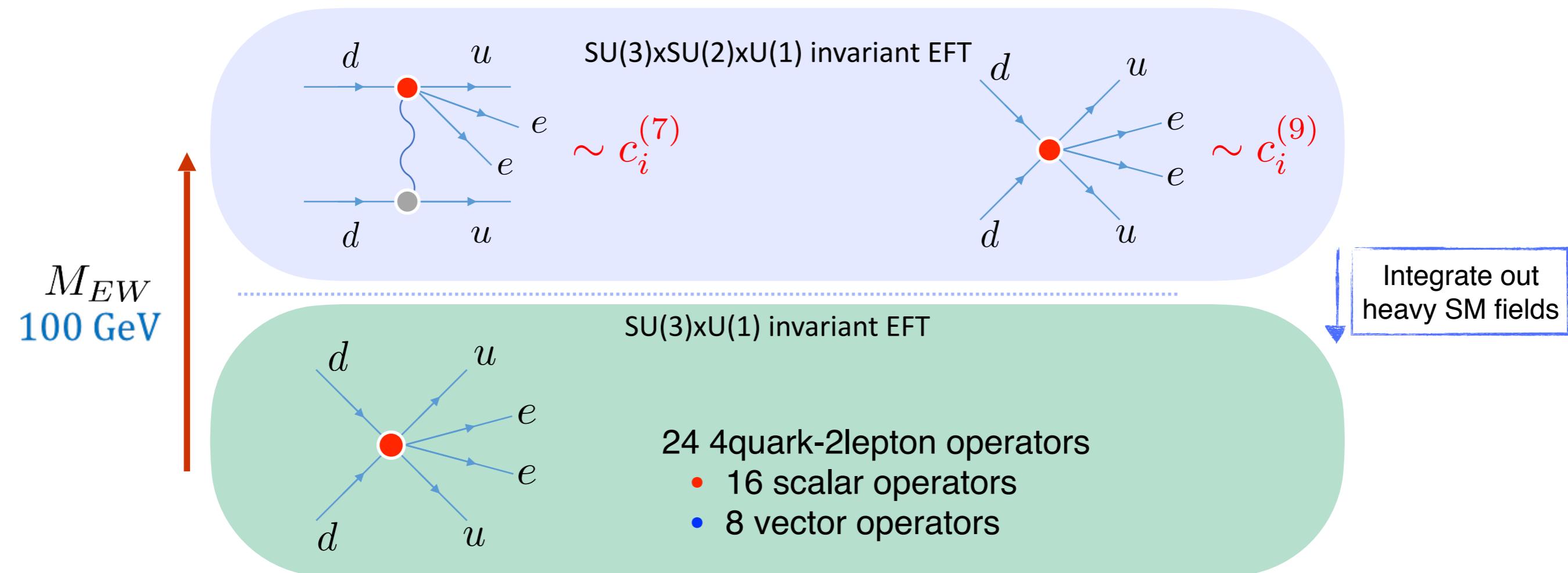
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Low-energy operators

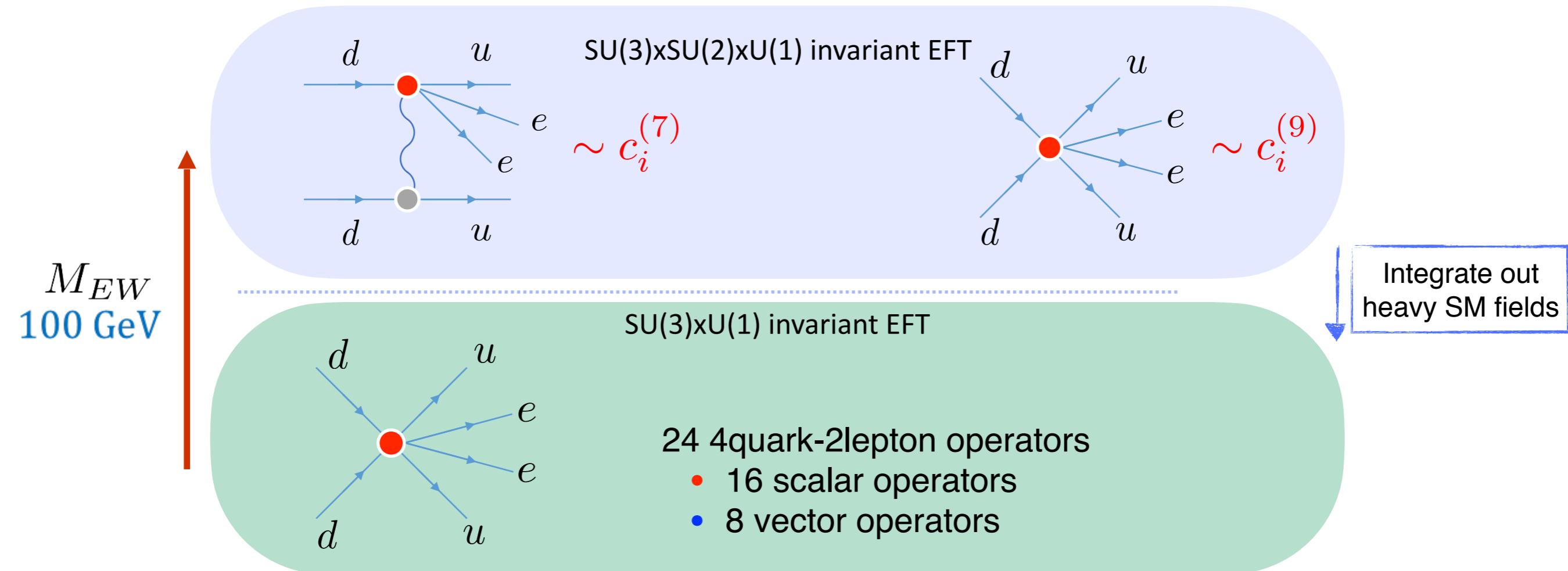
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Low-energy operators

Dimension-9



- 24 4quark-2lepton operators
 - 16 scalar operators
 - 8 vector operators

$$\mathcal{L}_{\Delta L=2}^{(9)}$$

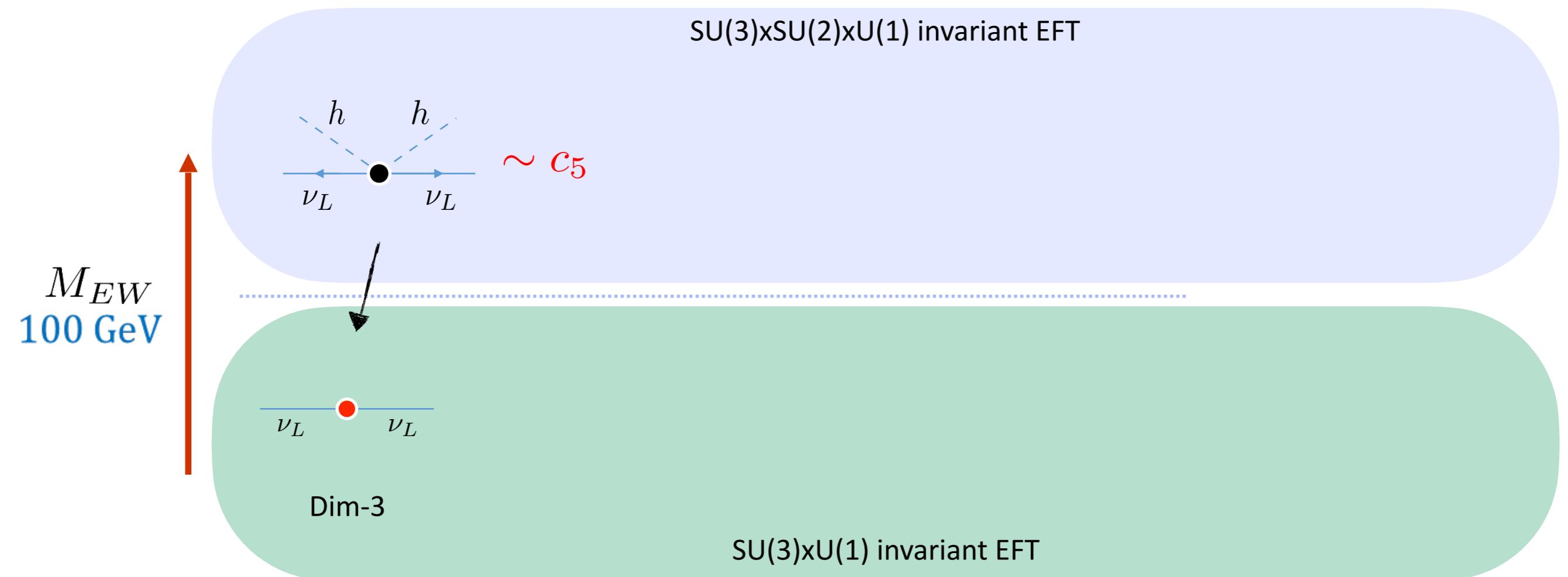
- 3 can be induced by dimension-7 operators
- 19 can be induced by dimension-9 operators

$$C_i^{(9)} \sim v^3/\Lambda^3$$

$$C_i^{(9)} \sim v^5/\Lambda^5$$

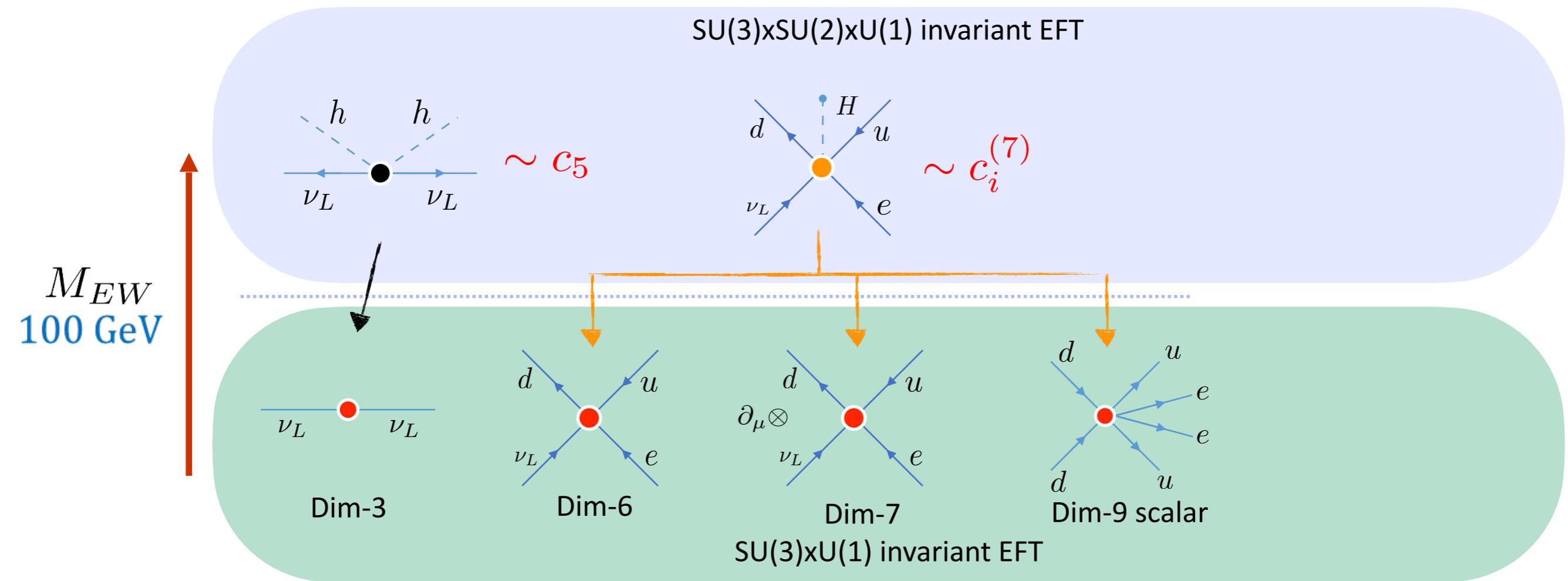
Low-energy operators

Summary



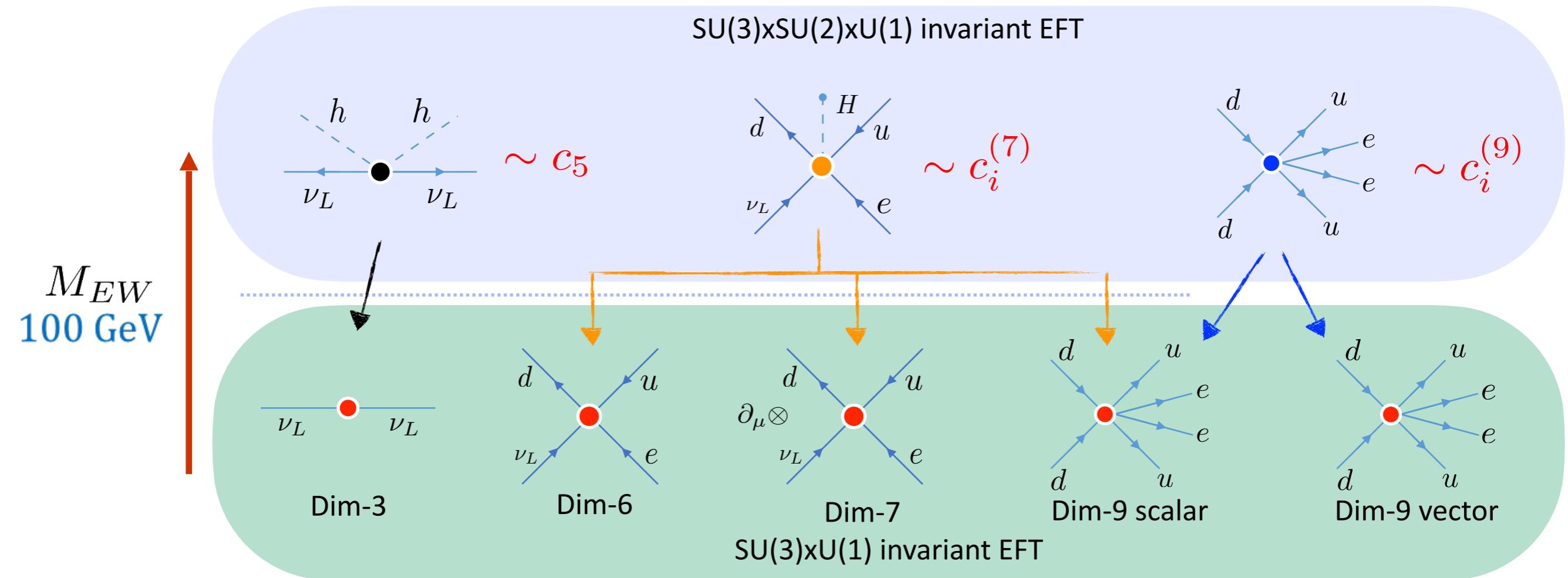
Low-energy operators

Summary

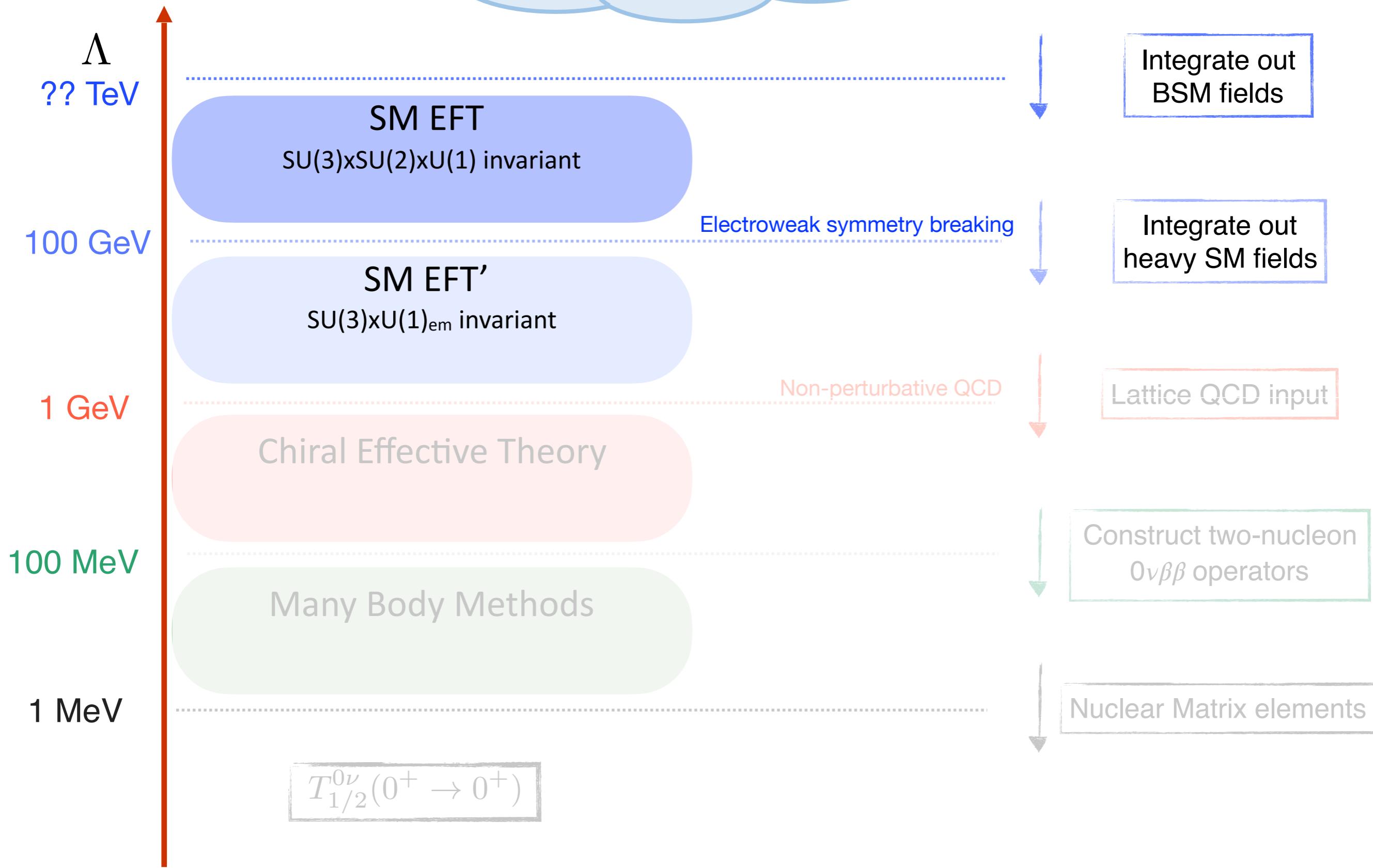


Low-energy operators

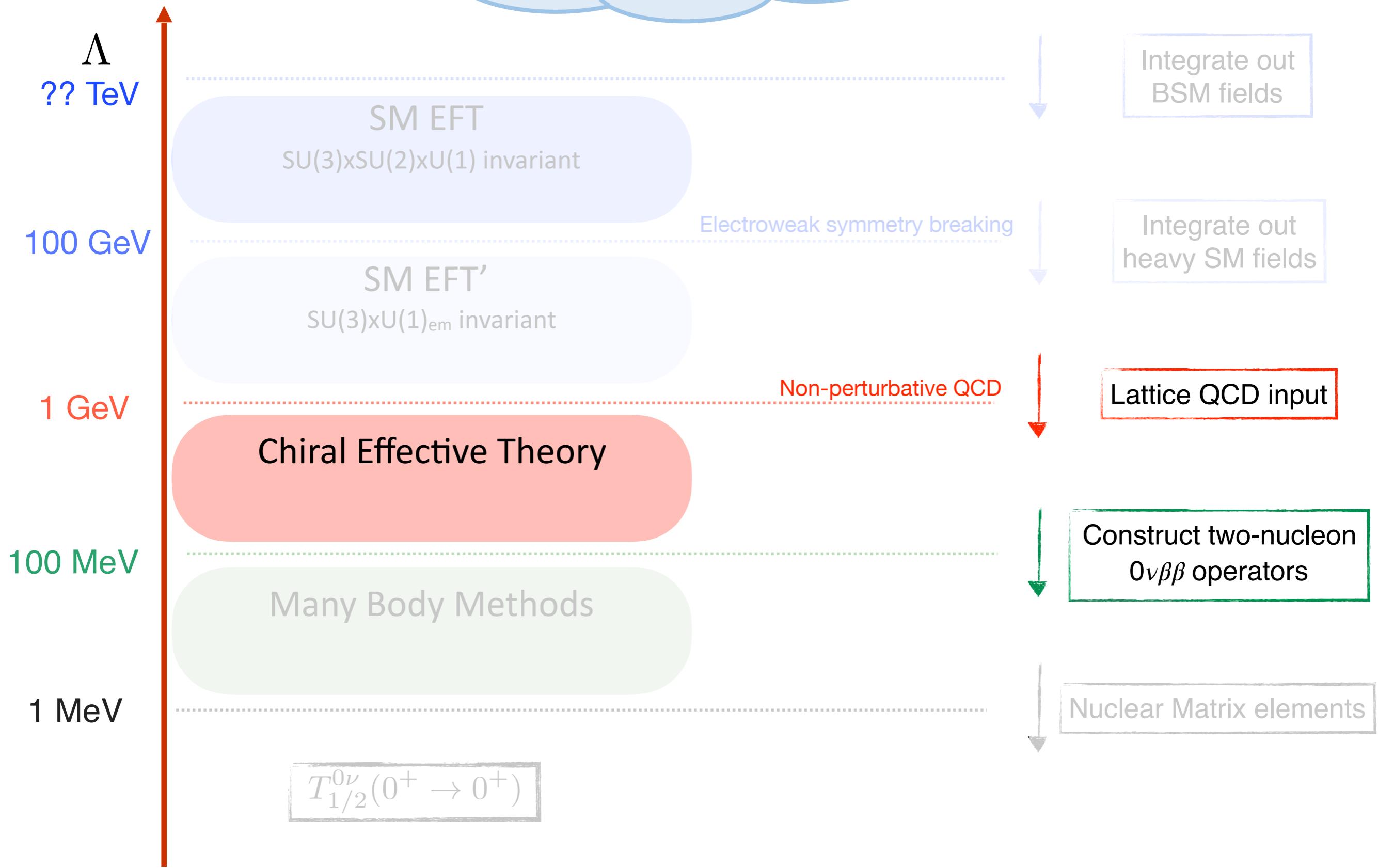
Summary



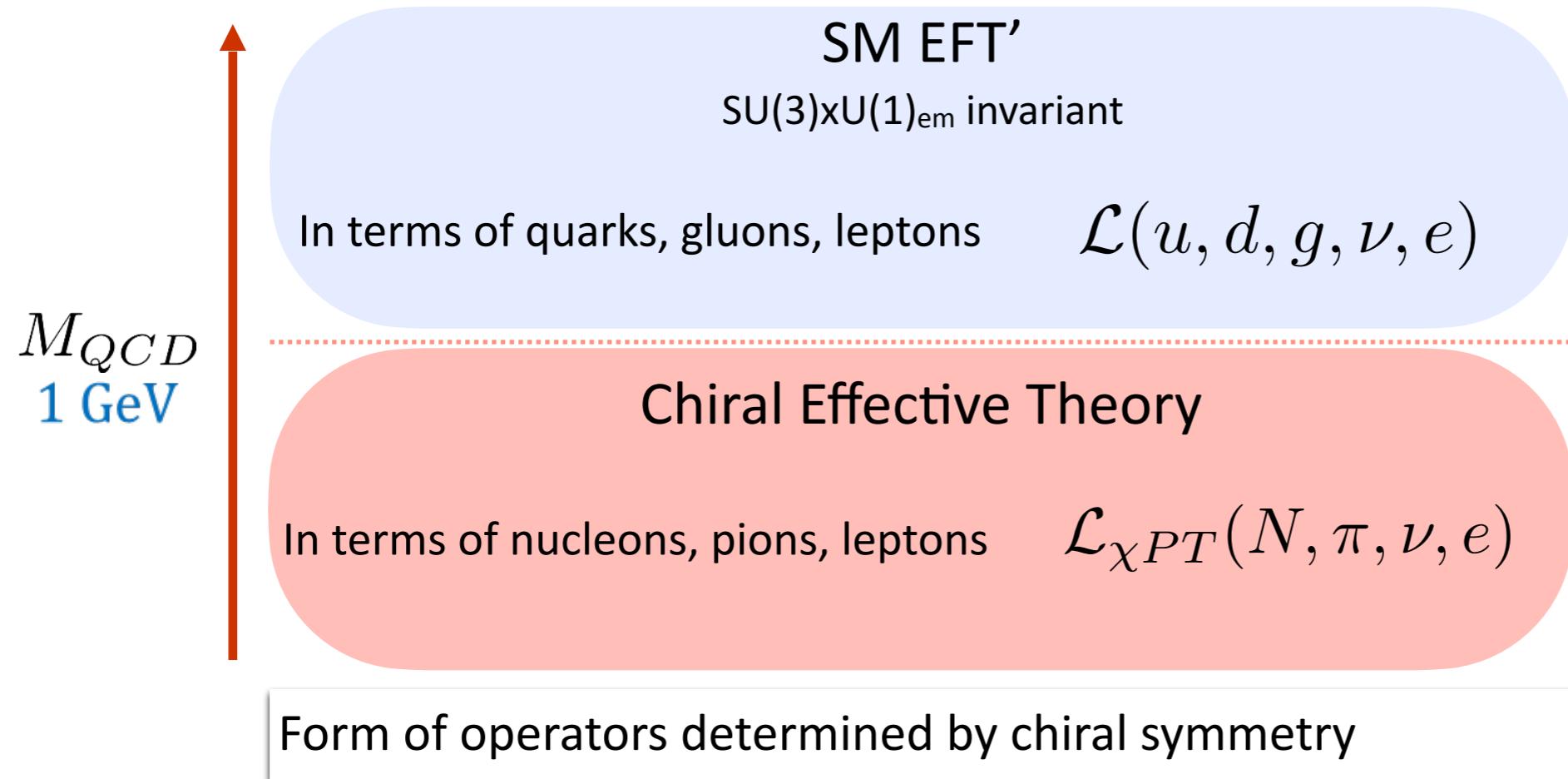
Outline



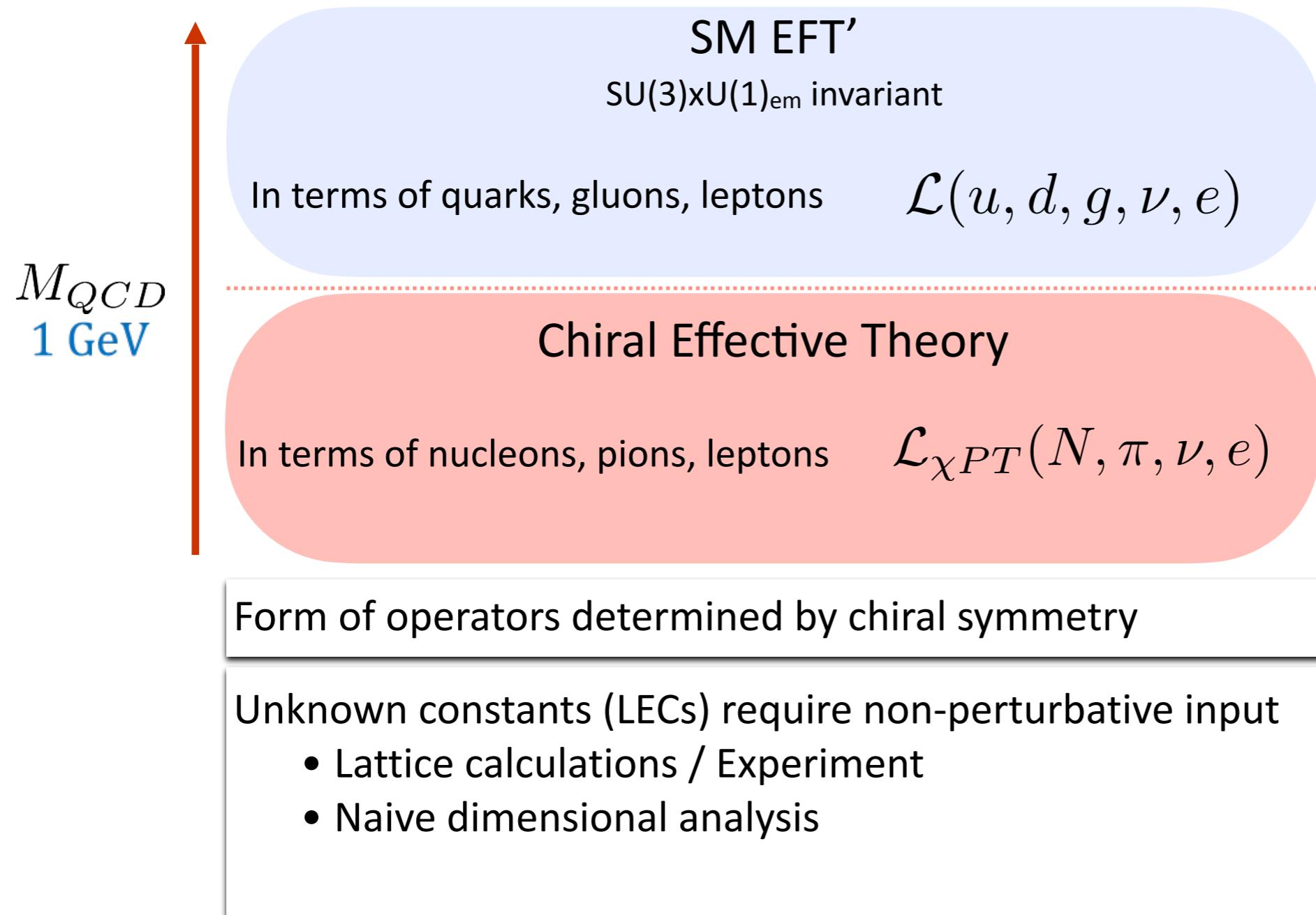
Outline



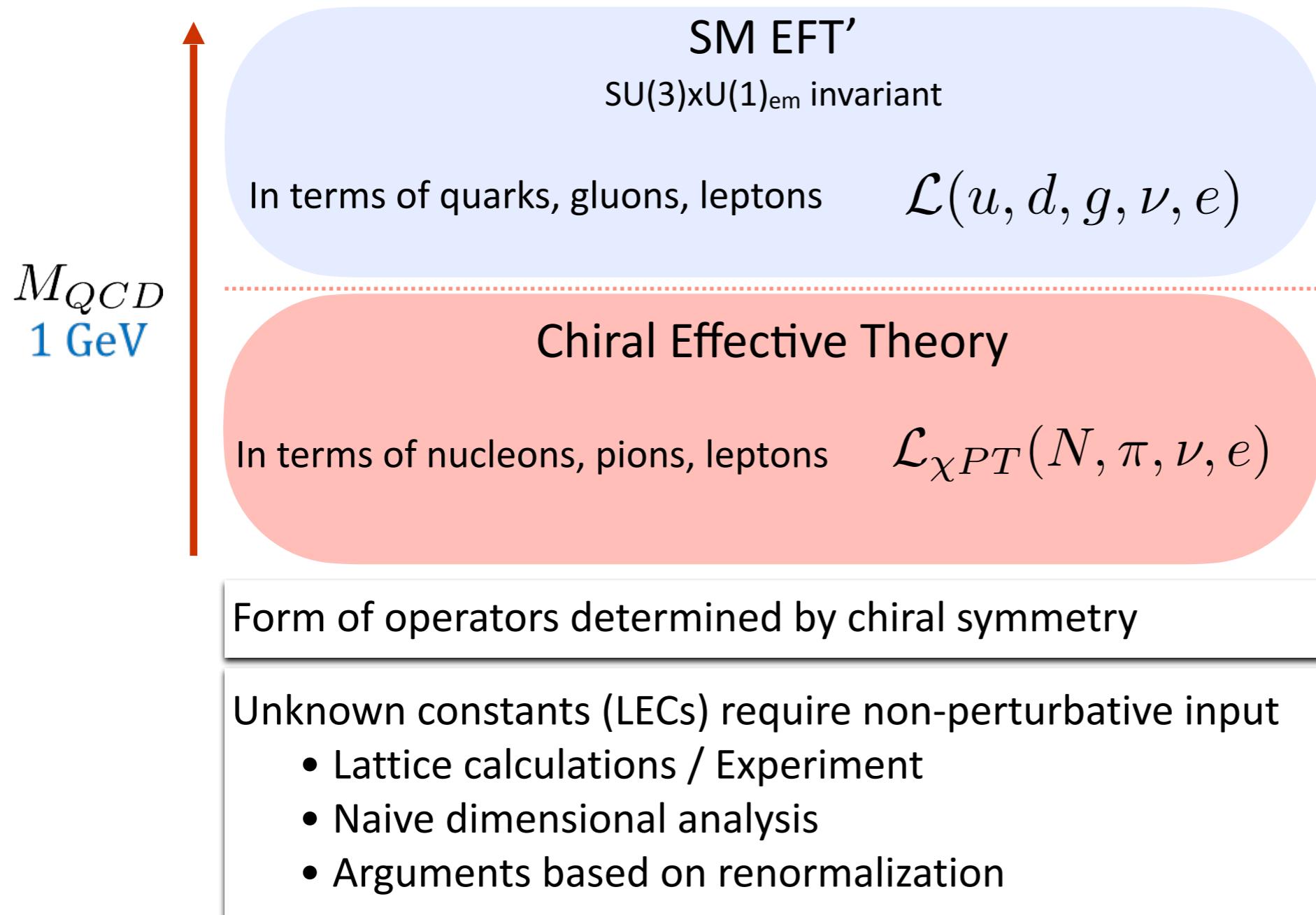
Matching to Chiral EFT



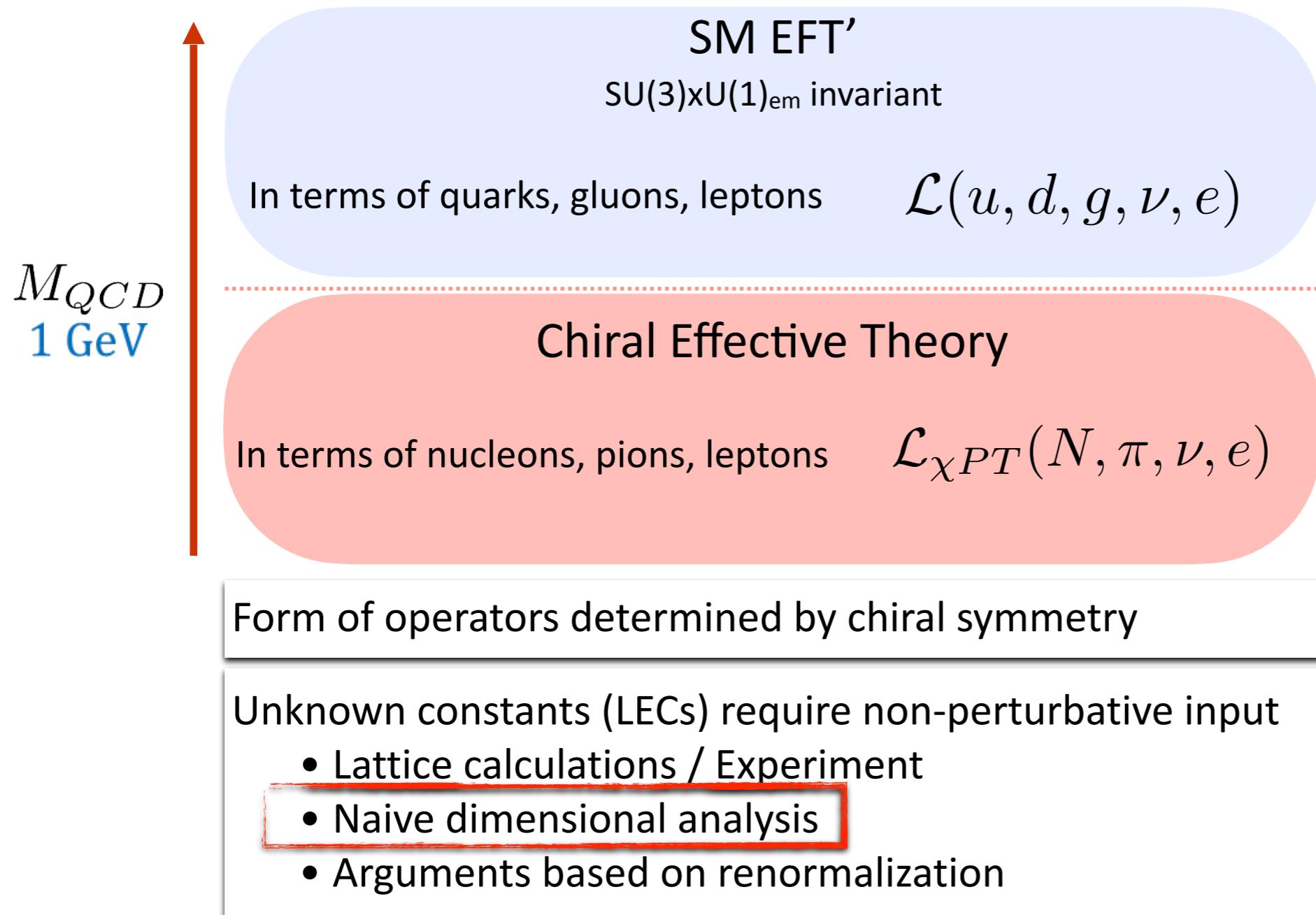
Matching to Chiral EFT



Matching to Chiral EFT



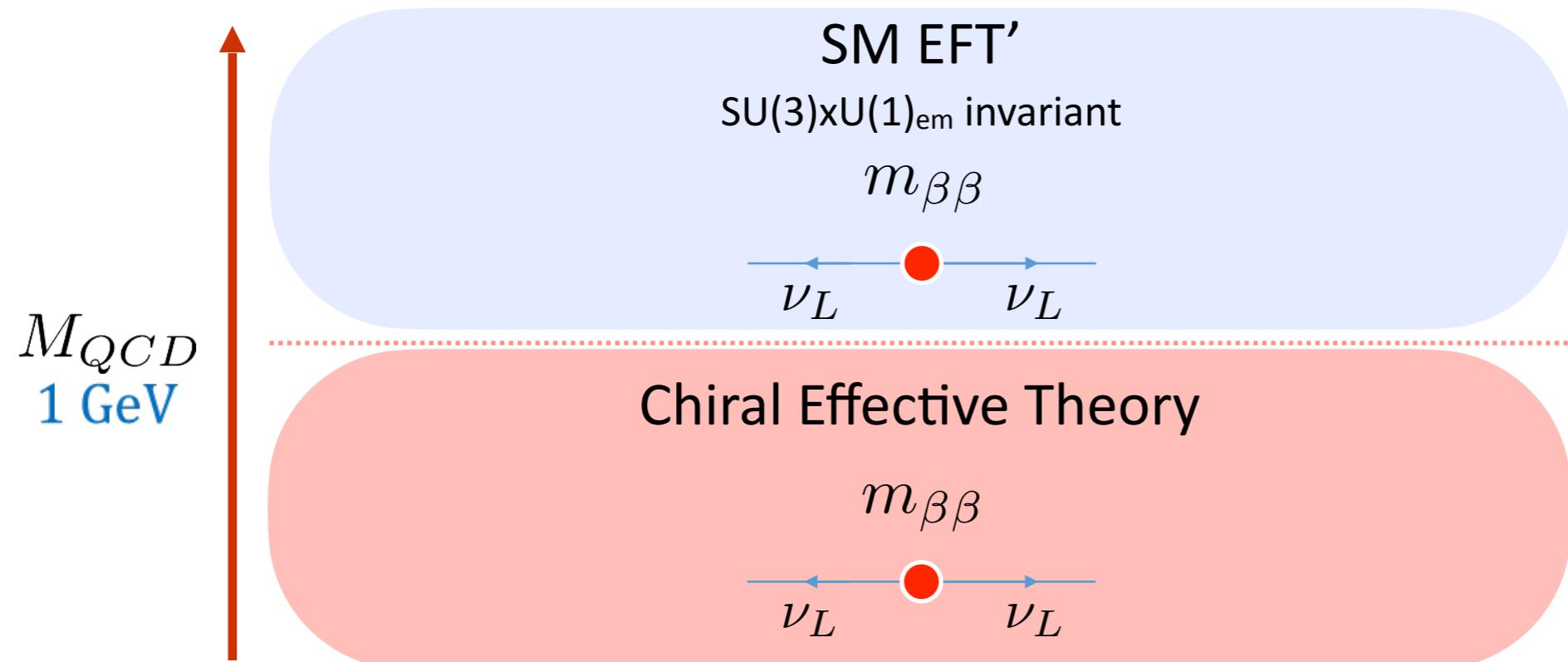
Matching to Chiral EFT



Matching to Chiral EFT

Majorana mass (dimension-3)

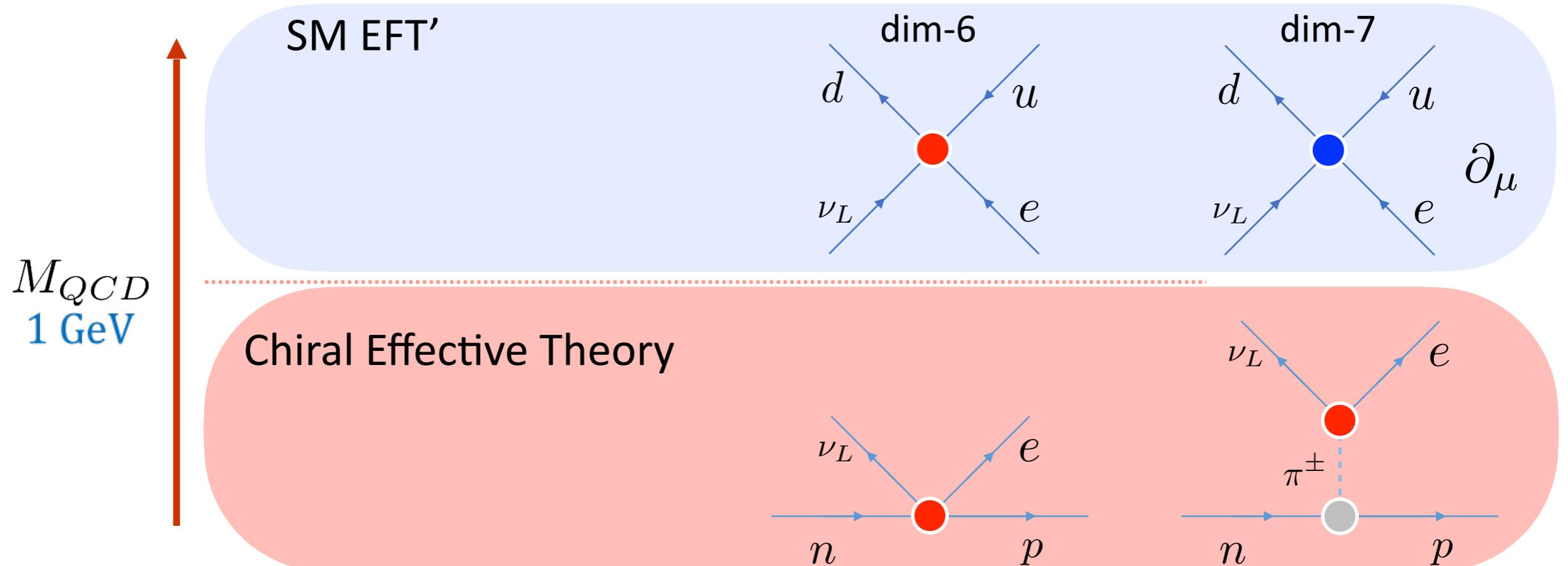
Warning: Based on NDA



Matching to Chiral EFT

Dimension-6 and -7

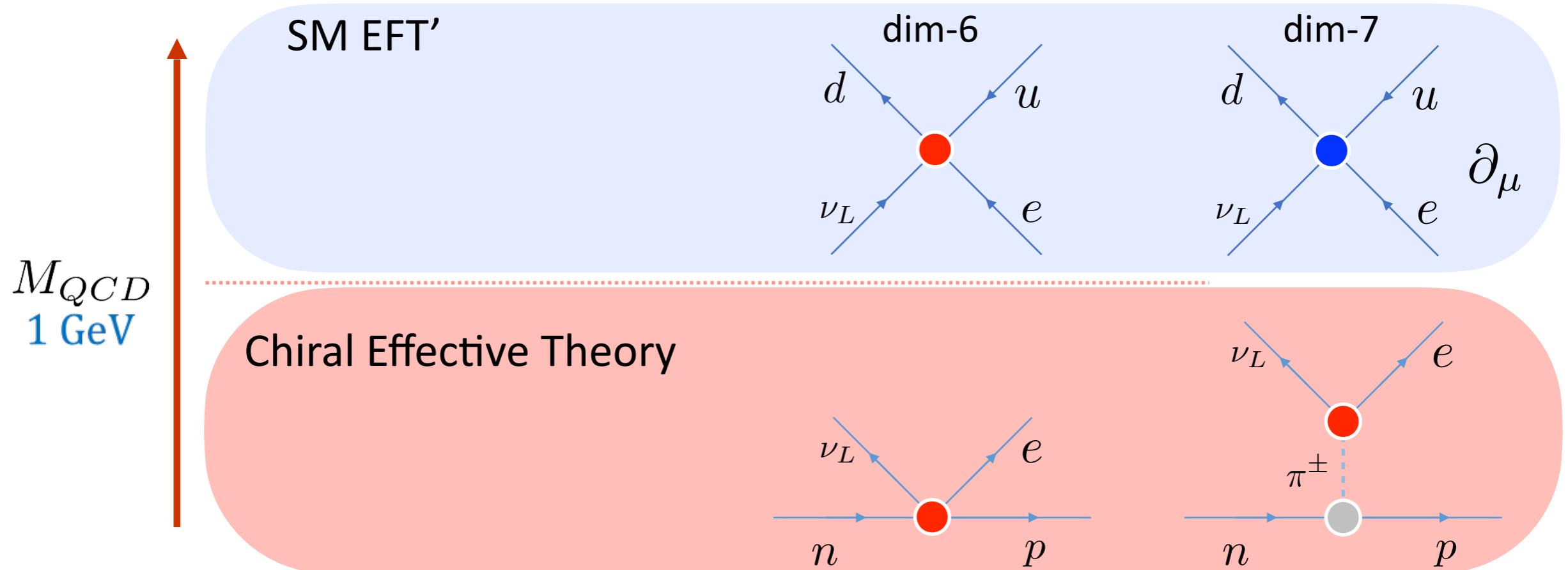
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Matching to Chiral EFT

Dimension-6 and -7

Warning: Based on NDA

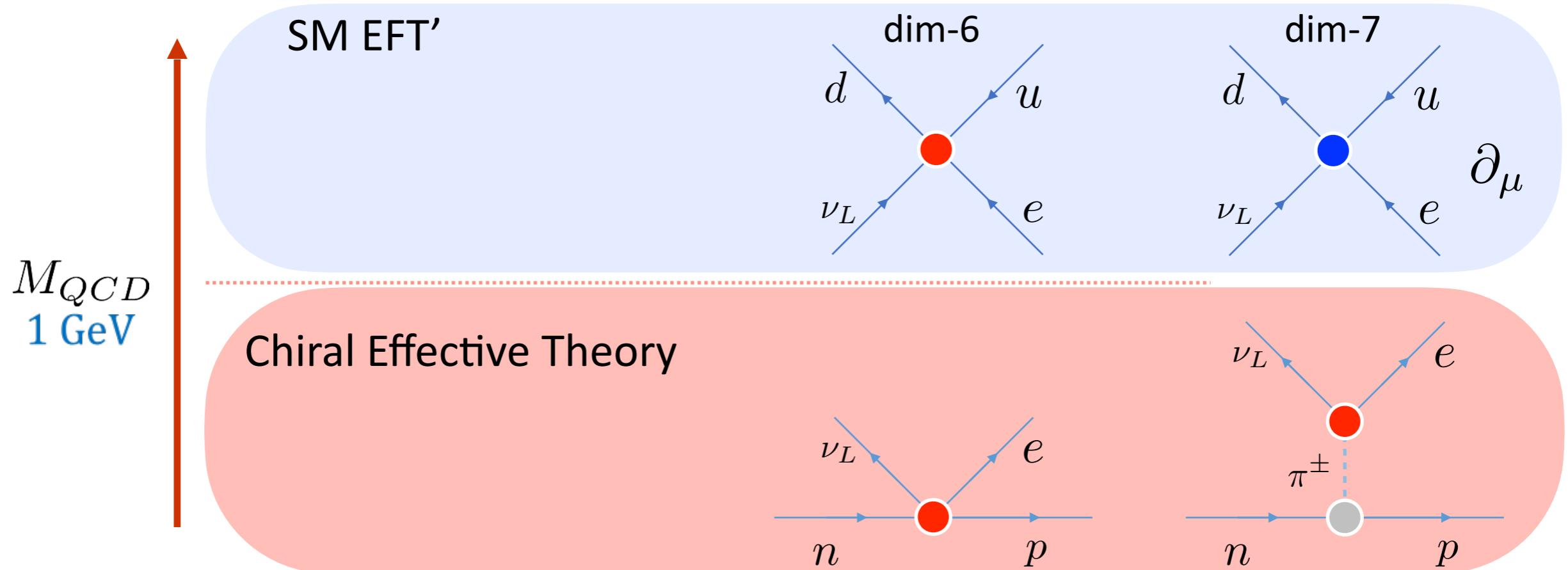


- Needed low-energy constants are the (scalar, vector, tensor) nucleon charges
 - $g_V, g_A, g_S, g_M, g_T, g'^T$

Matching to Chiral EFT

Dimension-6 and -7

Warning: Based on NDA



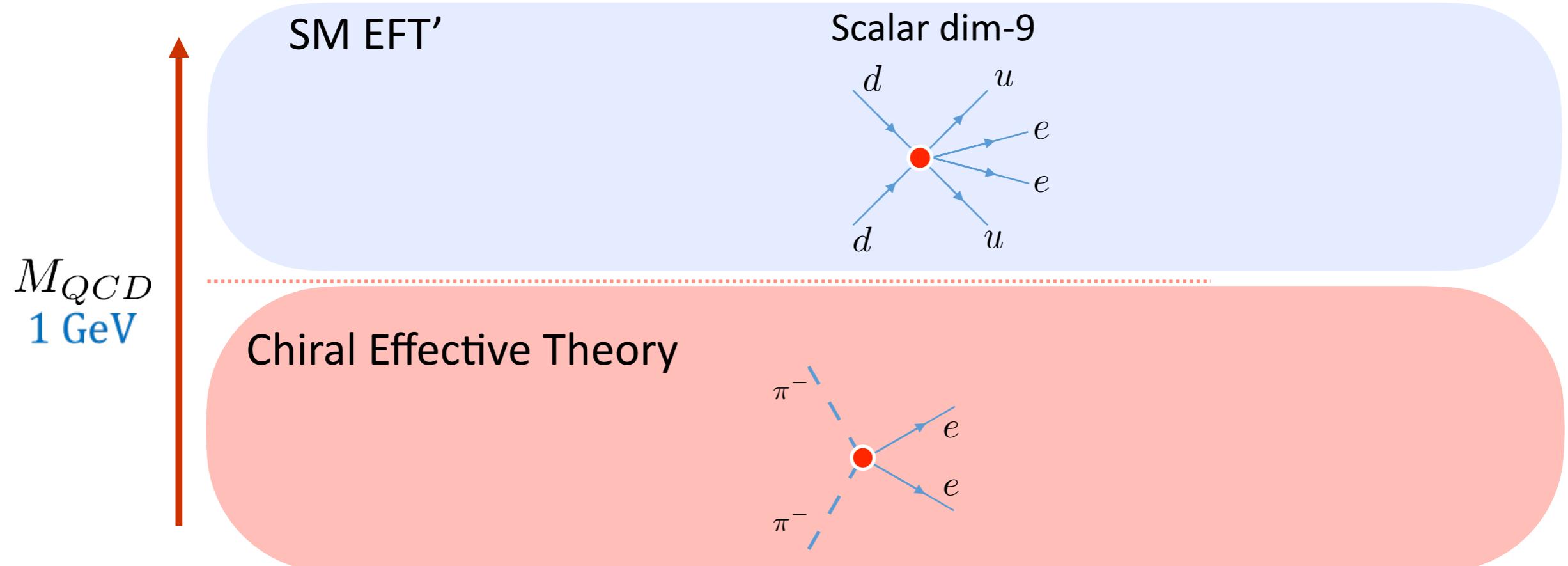
- Needed low-energy constants are the (scalar, vector, tensor) nucleon charges
 - $g_V, g_A, g_S, g_M, g_T, g^{\prime T}$
- Known from experiment and/or Lattice QCD
- Only estimates available, $O(1)$ by NDA

Matching to Chiral EFT

Dimension-9

Warning: Based on NDA

$$\mathcal{L}_{\Delta L=2}^{(9)} = \frac{1}{v^5} \sum_i \left[\left(C_{iR}^{(9)} \bar{e}_R C \bar{e}_R^T + C_{iL}^{(9)} \bar{e}_L C \bar{e}_L^T \right) O_i + C_i^{(9)} \bar{e} \gamma_\mu \gamma_5 C \bar{e}^T O_i^\mu \right],$$

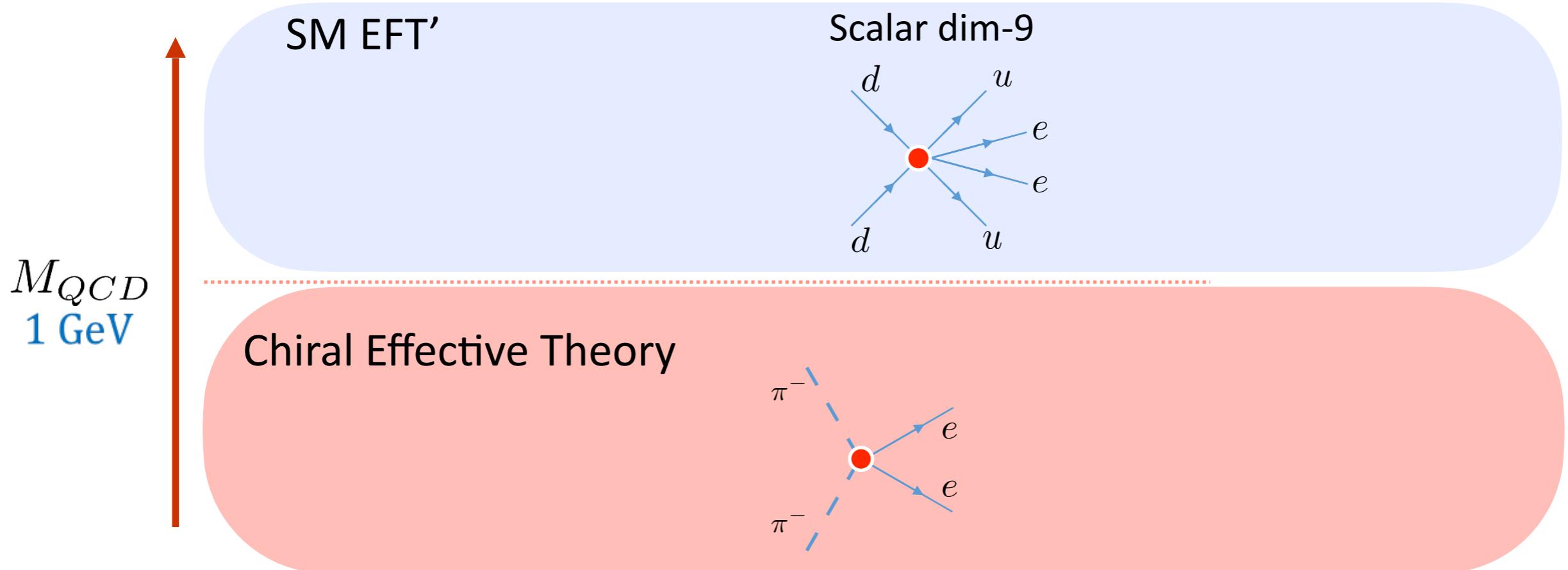


Matching to Chiral EFT

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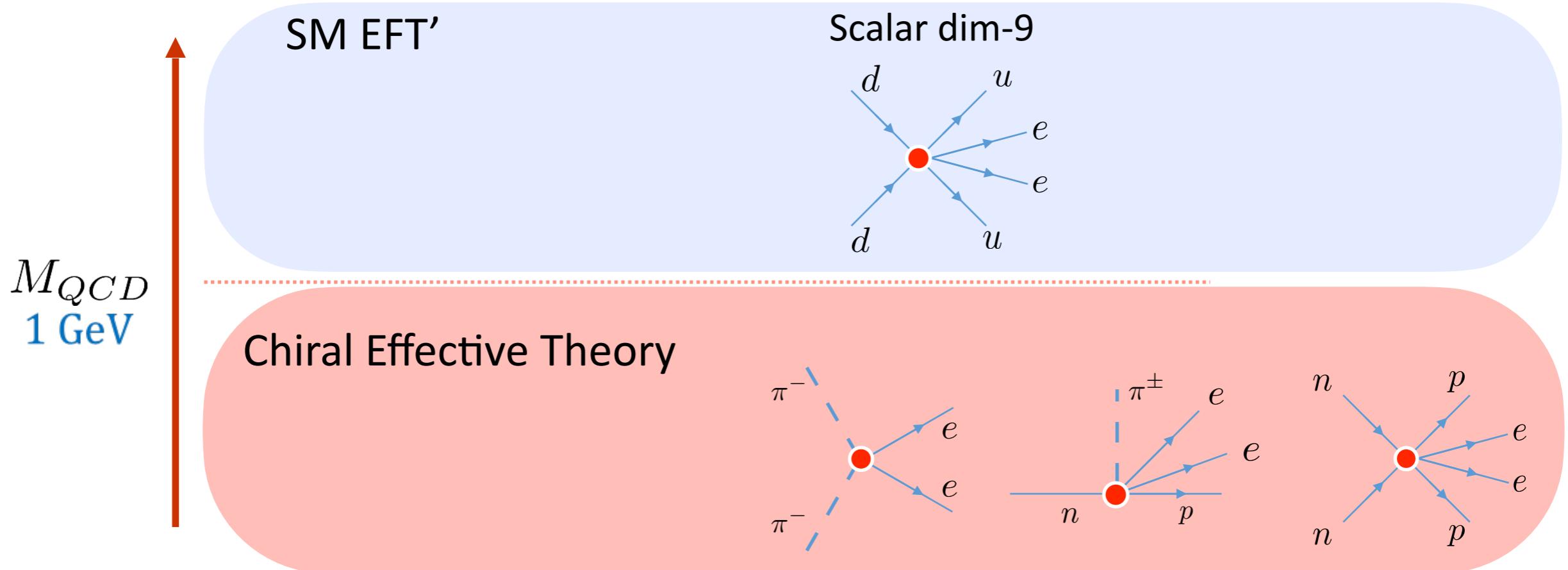
- Most scalar operators only induce $\pi\pi$ interactions

Matching to Chiral EFT

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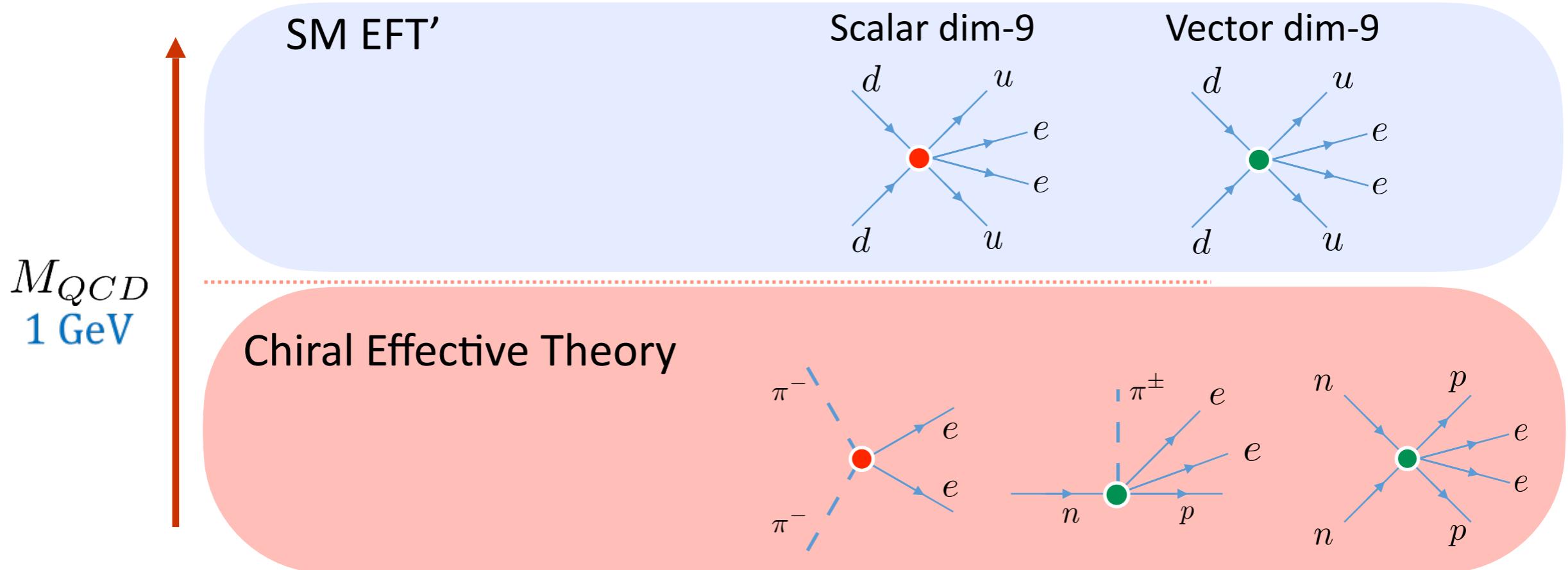
- Most scalar operators only induce $\pi\pi$ interactions
 - One hadronic structure for which πN & NN terms are important

Matching to Chiral EFT

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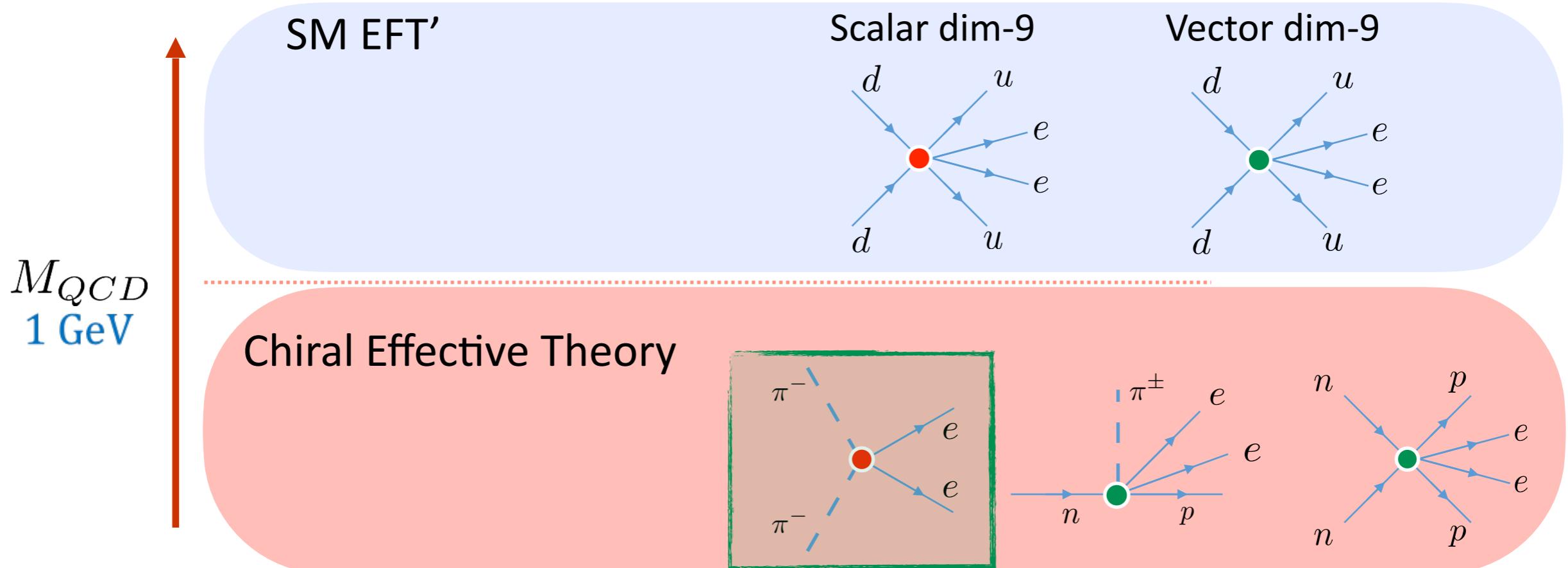
- Most scalar operators only induce $\pi\pi$ interactions
 - One hadronic structure for which πN & NN terms are important
- Vector operators induce πN & NN interactions

Matching to Chiral EFT

Dimension-9

Warning: Based on NDA

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- The LECs for the $\pi\pi$ terms are known
 - Direct lattice calculation
 - K-Kbar mixing + SU(3) chiral symmetry
- Vector operators induce πN & NN interactions

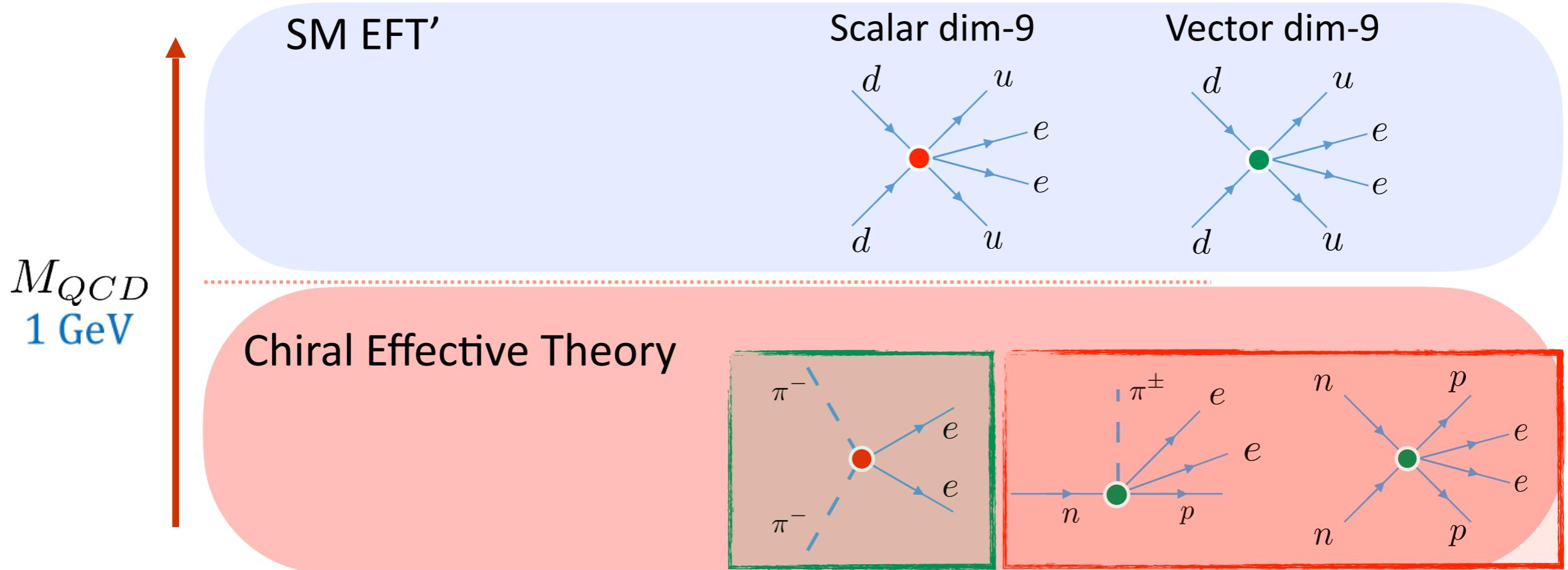
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Matching to Chiral EFT

Dimension-9

Warning: Based on NDA

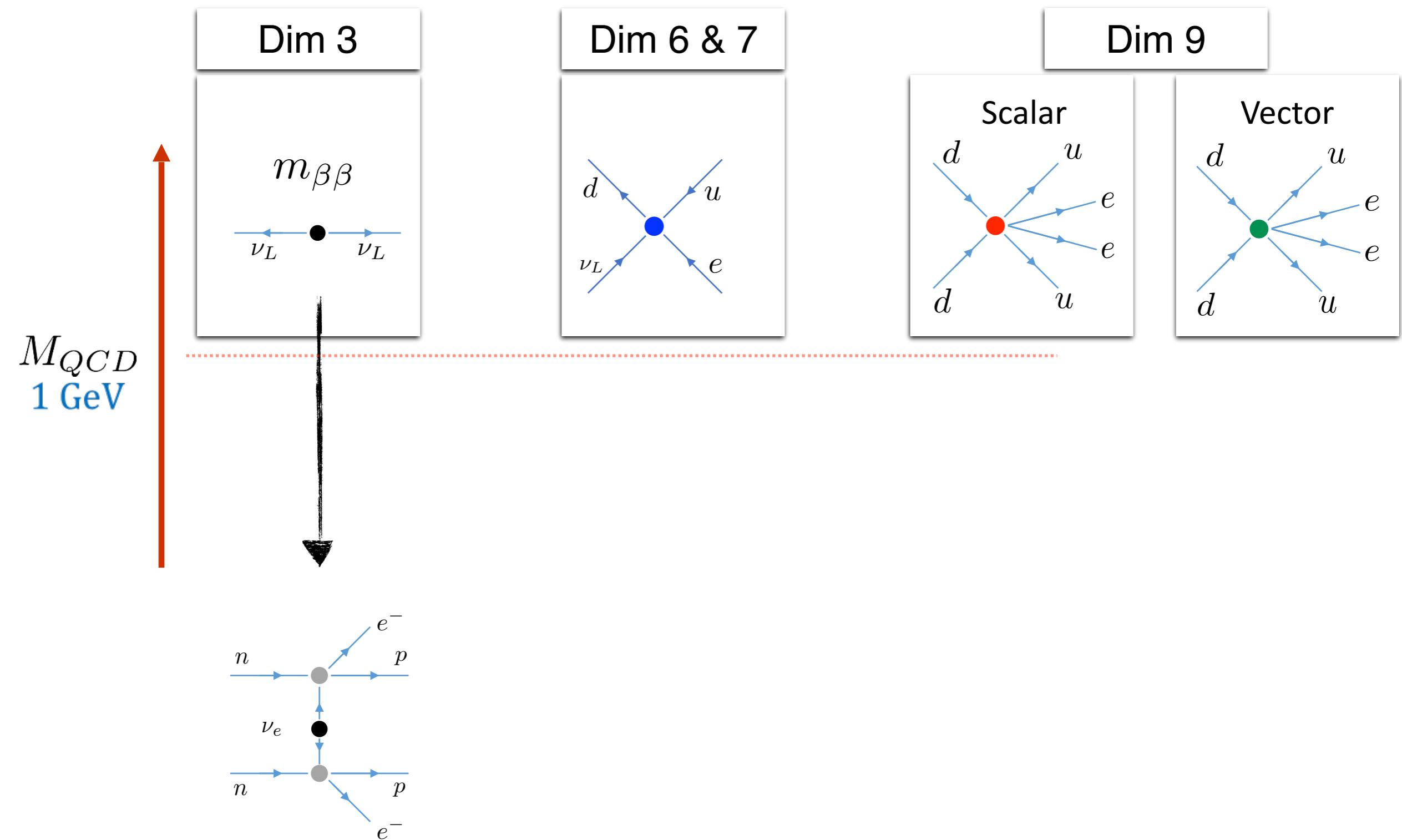
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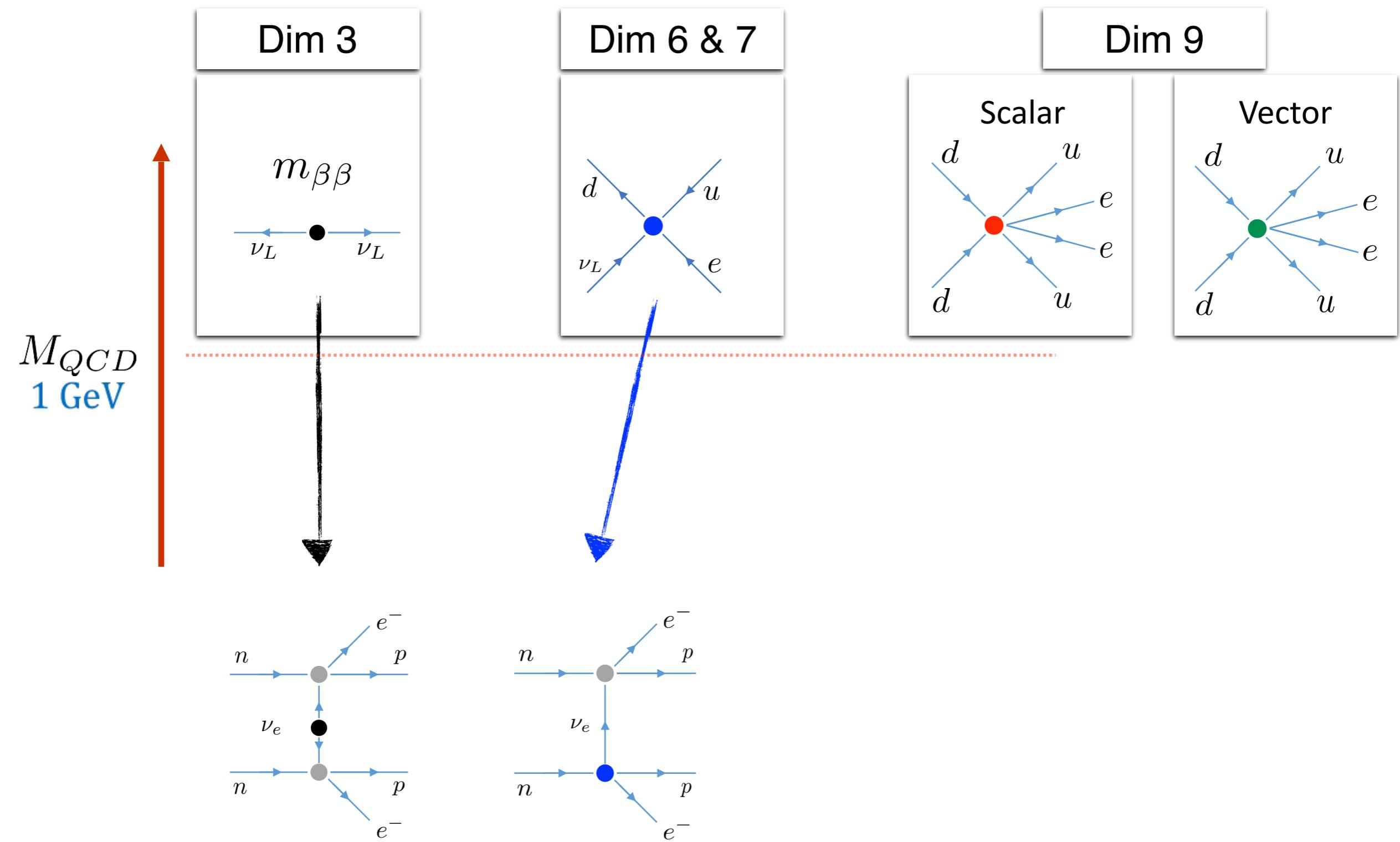
Chiral EFT

Summary



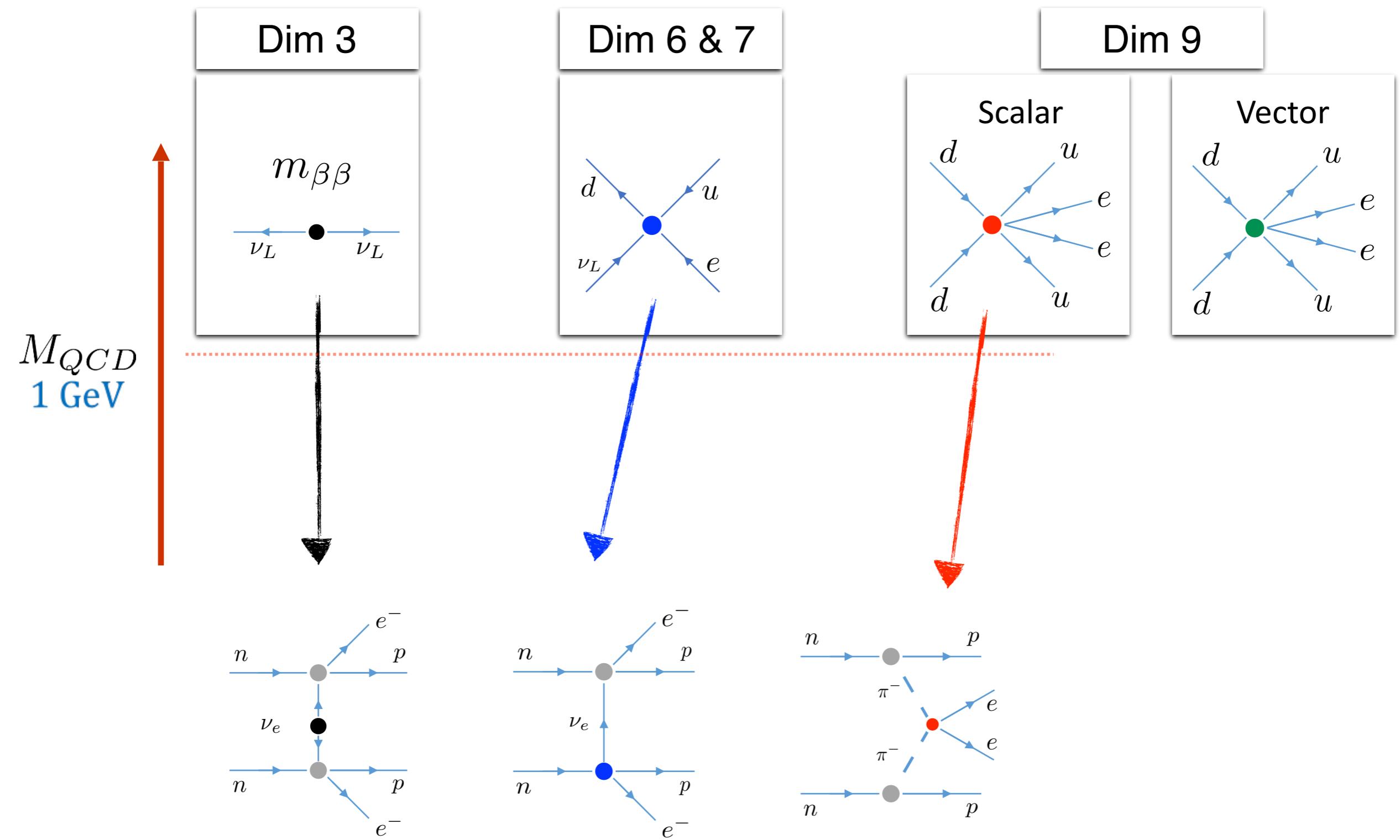
Chiral EFT

Summary



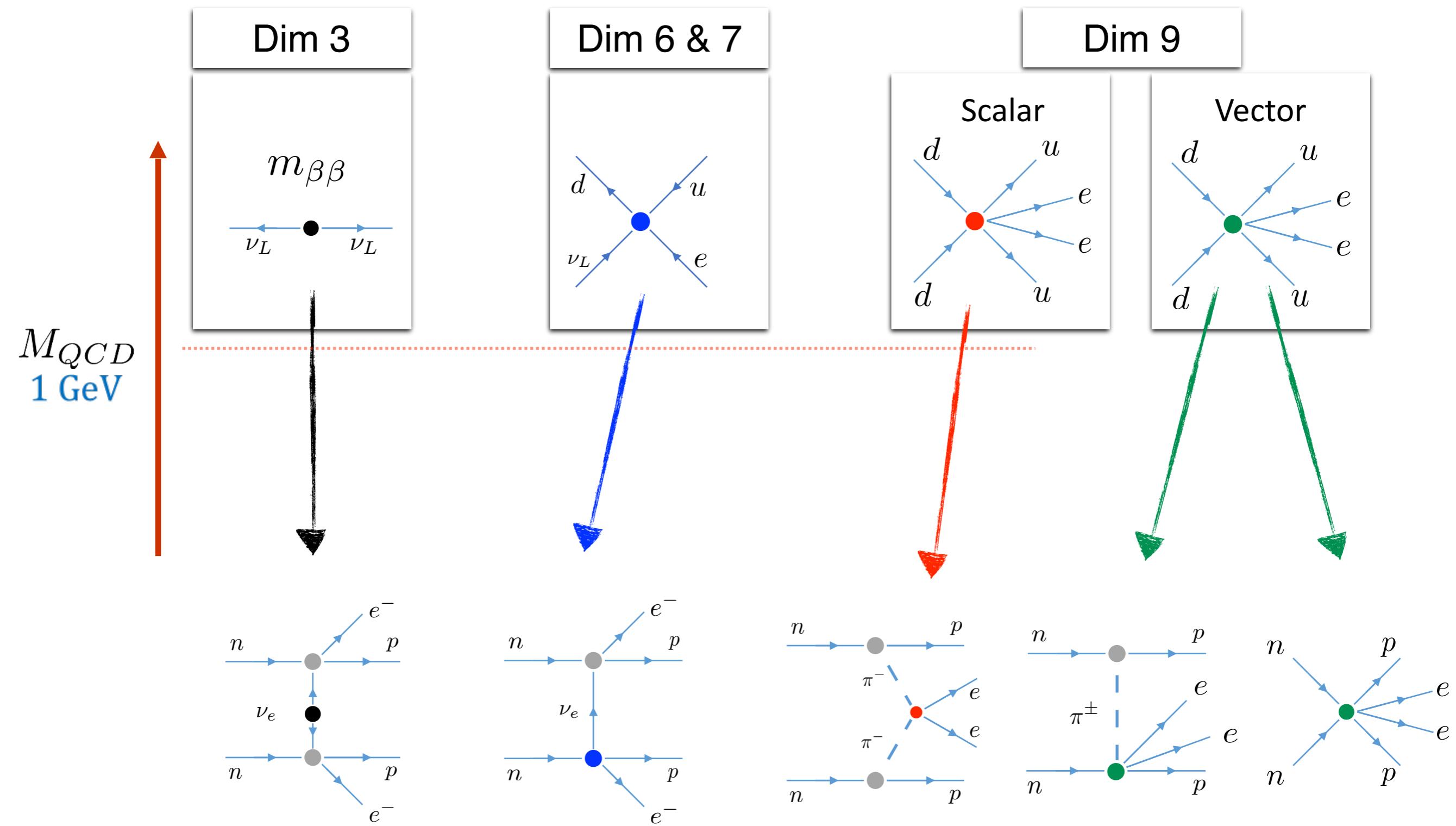
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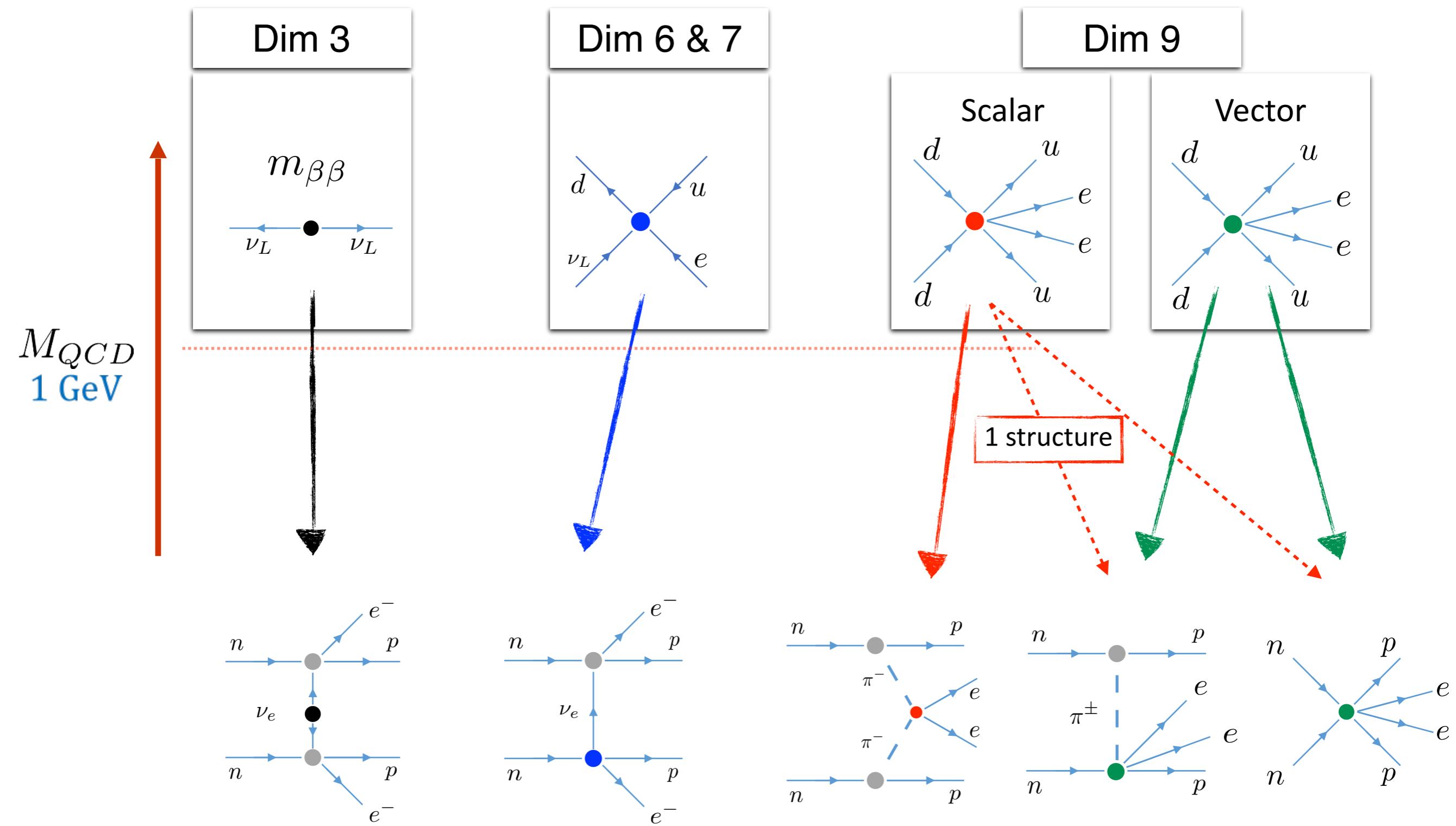
Chiral EFT

Summary



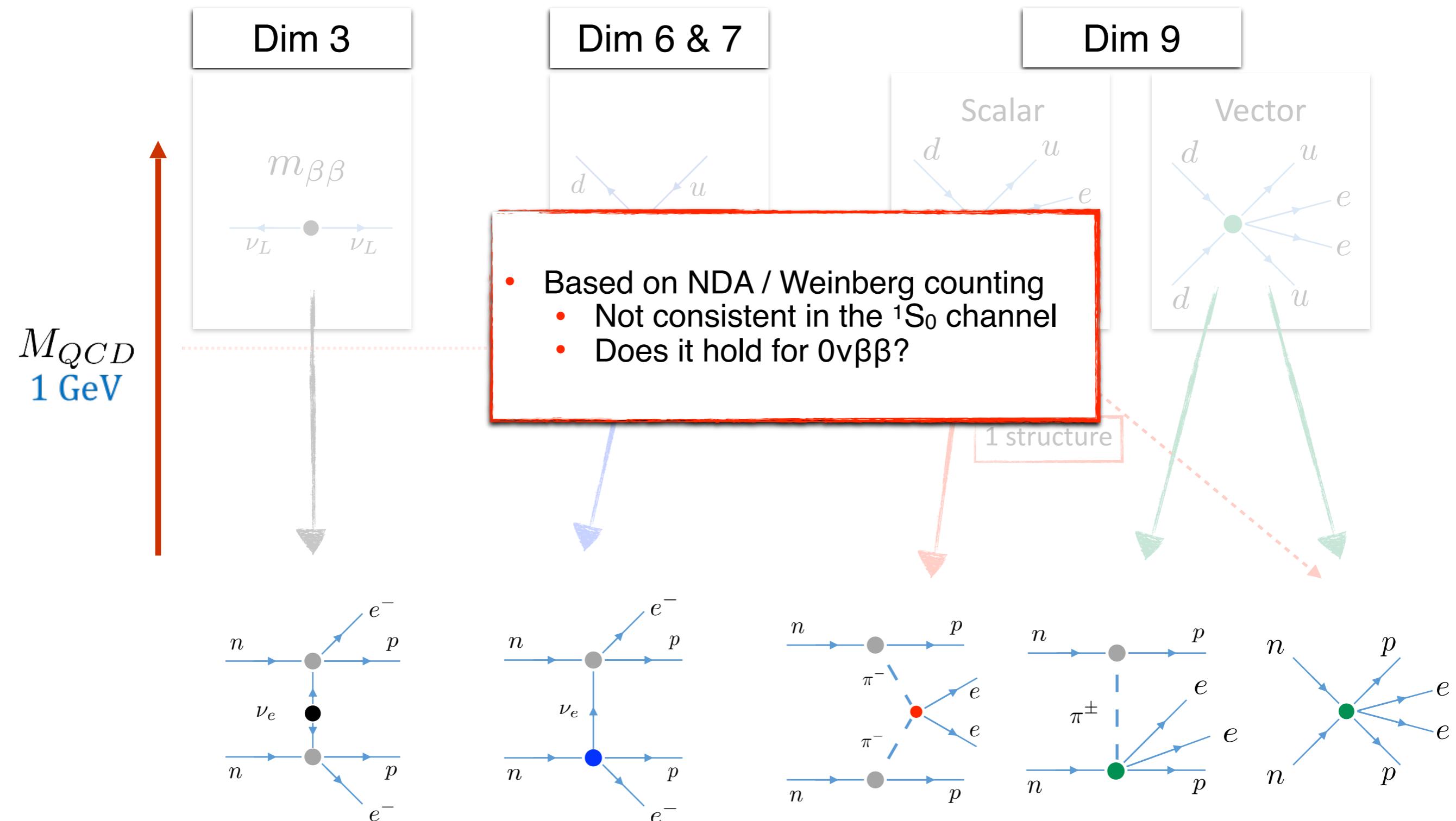
Chiral EFT

Summary



Chiral EFT

Summary



Checking the Weinberg counting

Majorana mass (dim 3)

- Use LO strong potential

$$V_0(\mathbf{q}) = \tilde{C} - \frac{g_A^2}{4F_\pi^2} \frac{m_\pi^2}{\mathbf{q}^2 + m_\pi^2}$$

- Renormalize using Dim. reg. (MS-bar)

Checking the Weinberg counting

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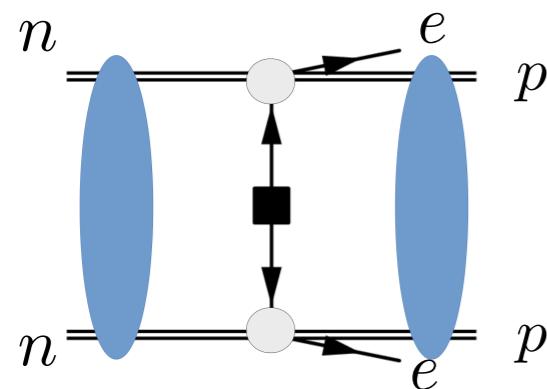
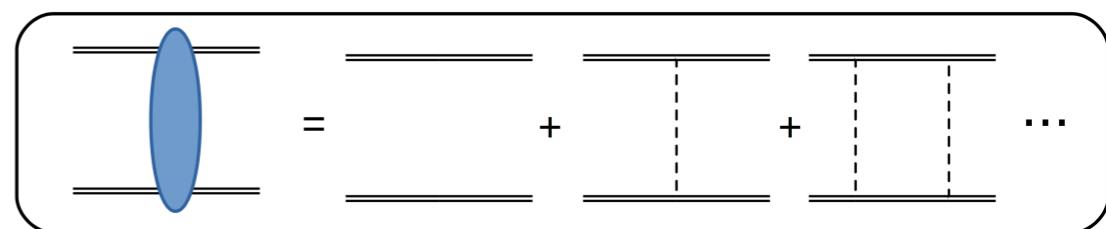
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Check if LO $\mathcal{A}(nn \rightarrow ppee)$ is finite

Dress the $\Delta L=2$ potential with strong interactions:



Checking the Weinberg counting

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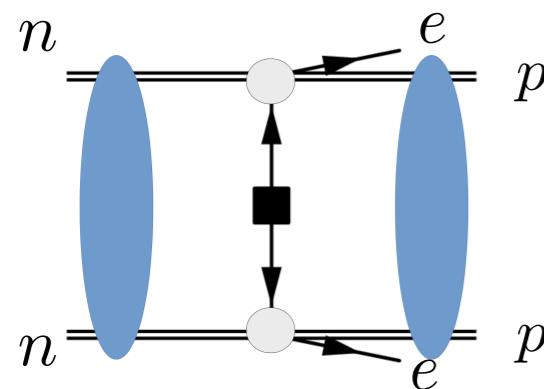
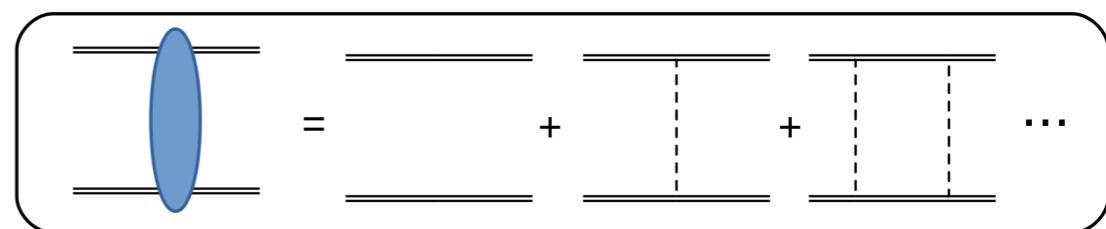
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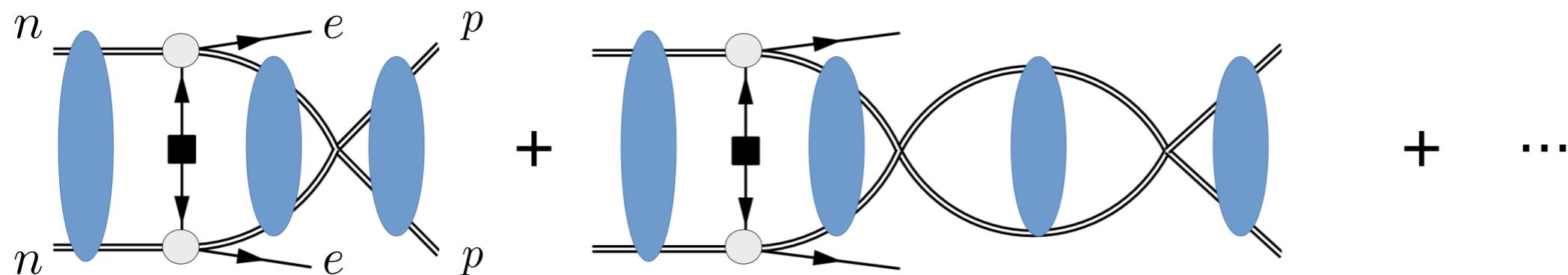
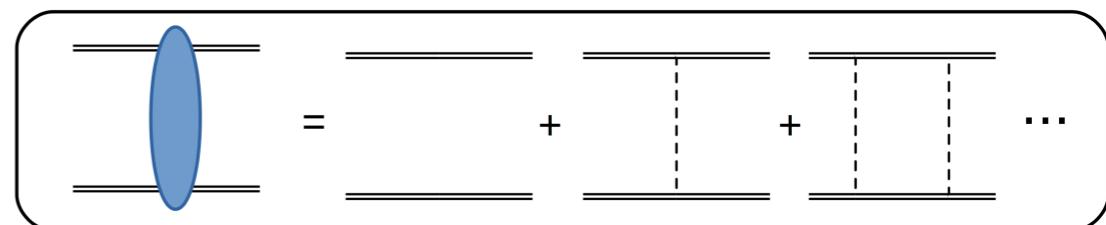
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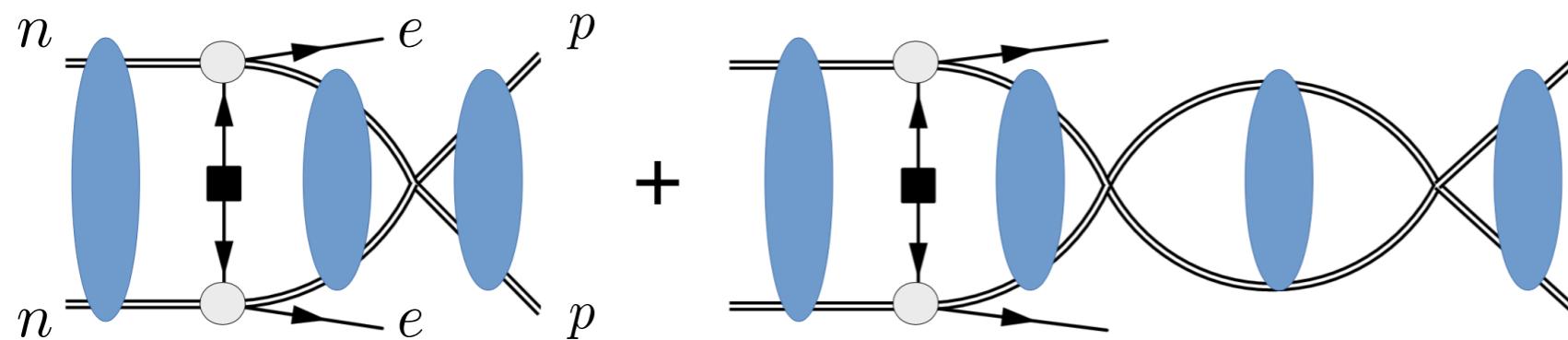
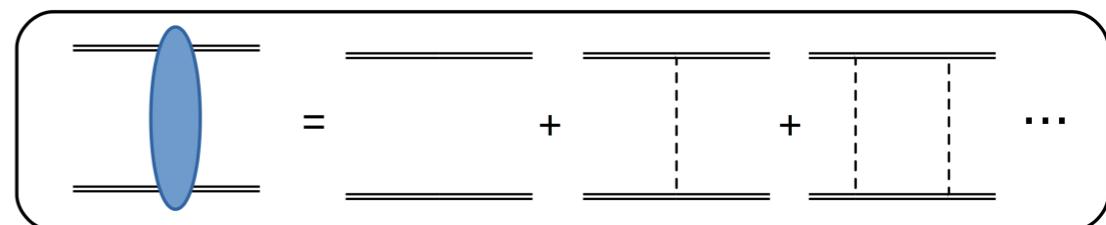
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+

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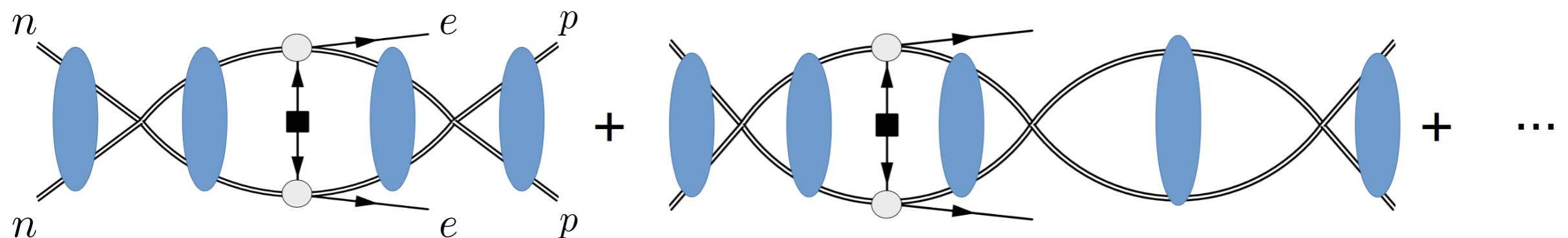
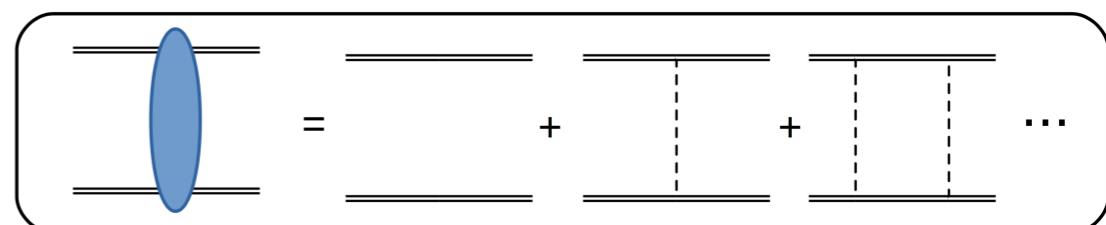
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Checking the Weinberg counting

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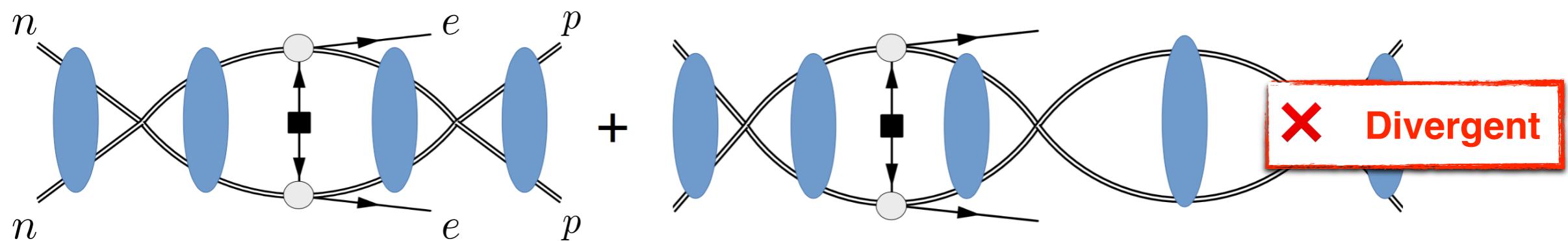
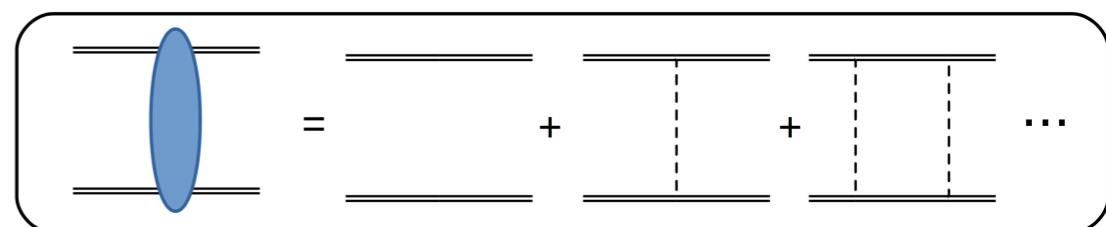
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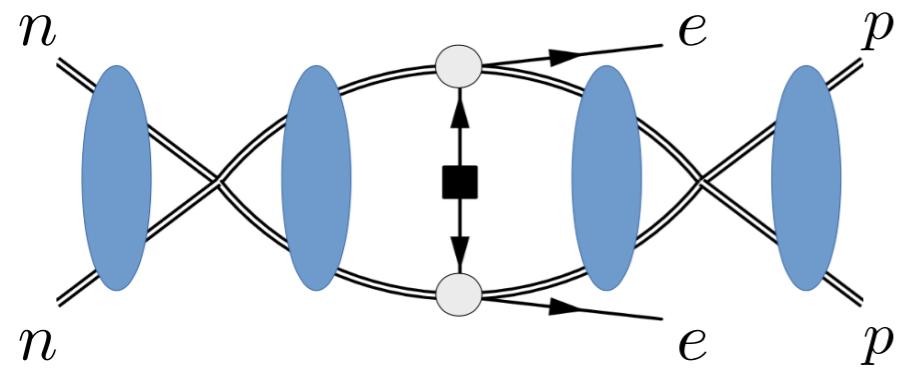
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Checking the Weinberg counting

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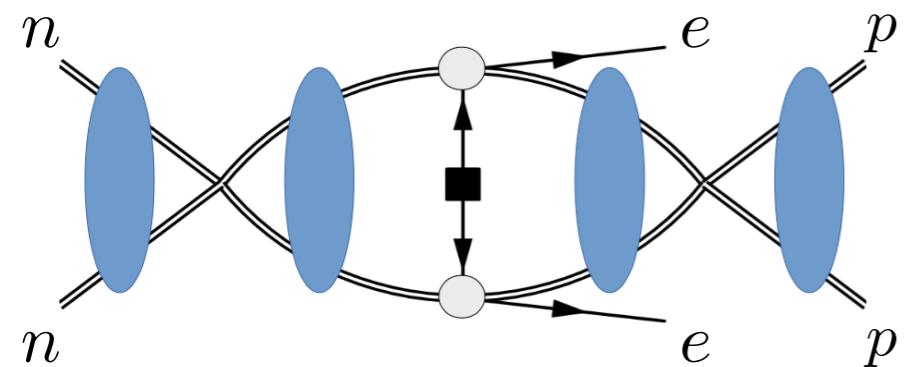


$$\sim m_N^2 \int d^3 q d^3 k \frac{1}{m_N E - \vec{q}^2} \frac{1}{(\vec{q} - \vec{k})^2} \frac{1}{m_N E' - \vec{k}^2}$$

+finite

Checking the Weinberg counting

Majorana mass (dim 3)



$$\begin{aligned}
 &= - \left(\frac{m_N}{4\pi} \right)^2 (1 + 2g_A^2) \frac{1}{2} \left(\log \frac{\mu^2}{-(|\mathbf{p}| + |\mathbf{p}'|)^2 + i0^+} + 1 \right) \\
 &\quad + \text{finite}
 \end{aligned}$$

Regulator dependent

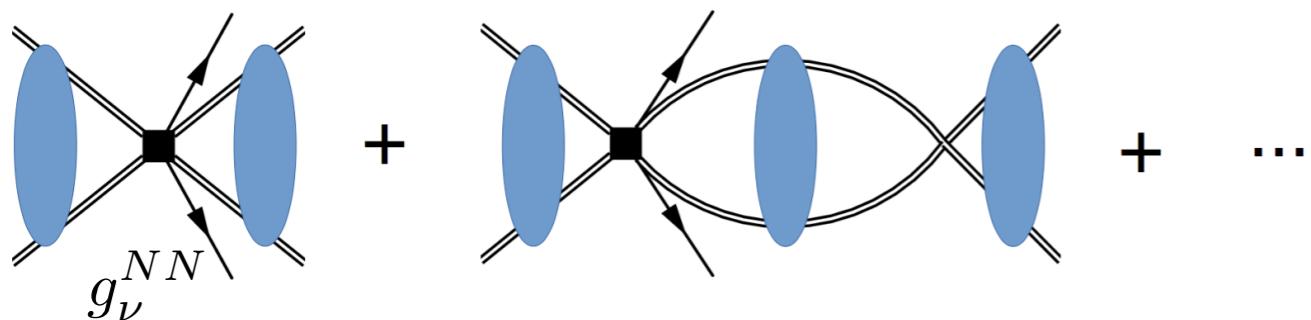
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Regulator dependent

Regulator dependence can be absorbed by a counterterm

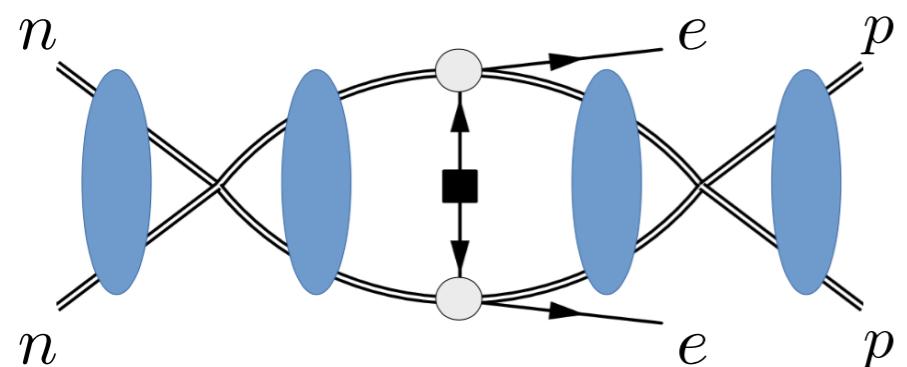


$$H_{\text{eff}} = 2G_F^2 V_{ud}^2 m_{\beta\beta} \bar{e}_L C \bar{e}_L^T V_\nu$$

$$V_{\nu,CT} = -2g_\nu^{NN} \tau^{(1)+} \tau^{(2)+}$$

Checking the Weinberg counting

Majorana mass (dim 3)

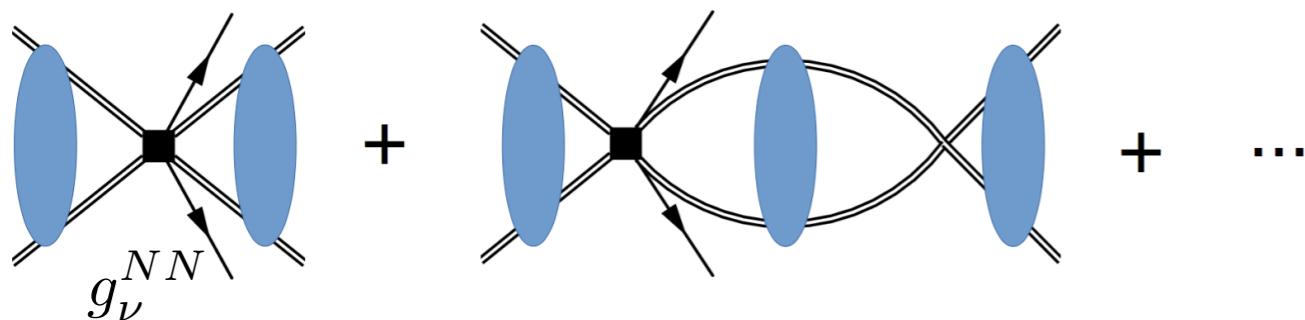


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$$V_{\nu,CT} = -2g_\nu^{NN} \tau^{(1)} + \tau^{(2)} + \dots$$



$$\frac{d}{d \ln \mu} \frac{g_\nu^{NN}}{(m_N \tilde{C}/4\pi)^2} = \frac{1}{2} + g_A^2$$

$$g_\nu^{NN} = \mathcal{O}(1/F_\pi^2)$$

Checking the Weinberg counting

Majorana mass (dim 3)

Similar for r-space regulator:

$$\tilde{C} \delta^{(3)}(\mathbf{r}) \rightarrow \frac{\tilde{C}(R_S)}{(\sqrt{\pi} R_S)^3} \exp\left(-\frac{r^2}{R_S^2}\right) \equiv \tilde{C}(R_S) \delta_{R_S}^{(3)}(\mathbf{r})$$

Checking the Weinberg counting

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$$\mathcal{A}_{\Delta L=2}^{(\nu)} = - \int d^3\mathbf{r} \psi_{\mathbf{p}'}^-(\mathbf{r})^* V_{\nu,0}(\mathbf{r}) \psi_{\mathbf{p}}^+(\mathbf{r}) \sim \tilde{C}(R_S)^2 [\ln(R_S) + \dots]$$

Regulator dependent

Checking the Weinberg counting

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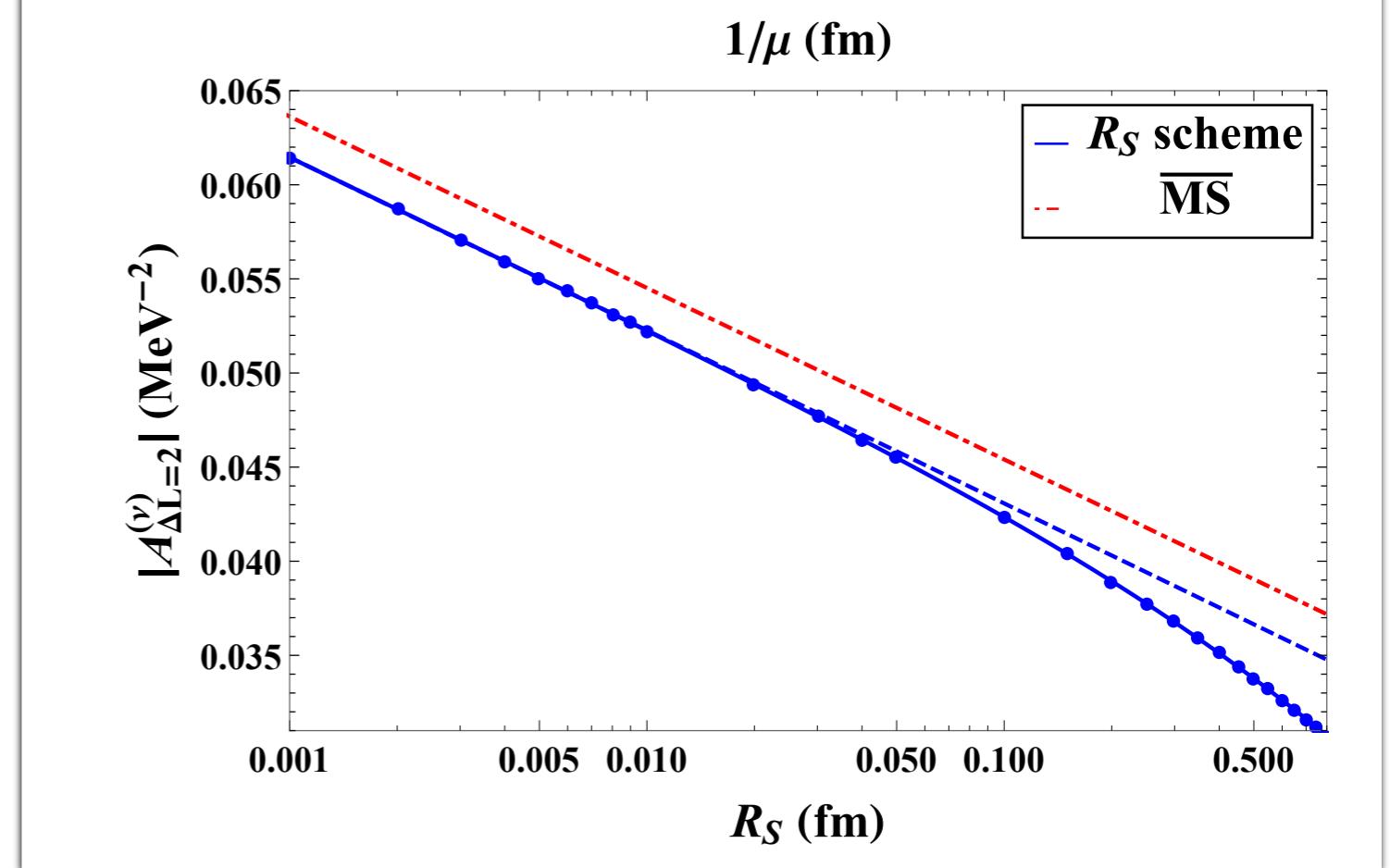
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Checking the Weinberg counting

Majorana mass (dim 3)

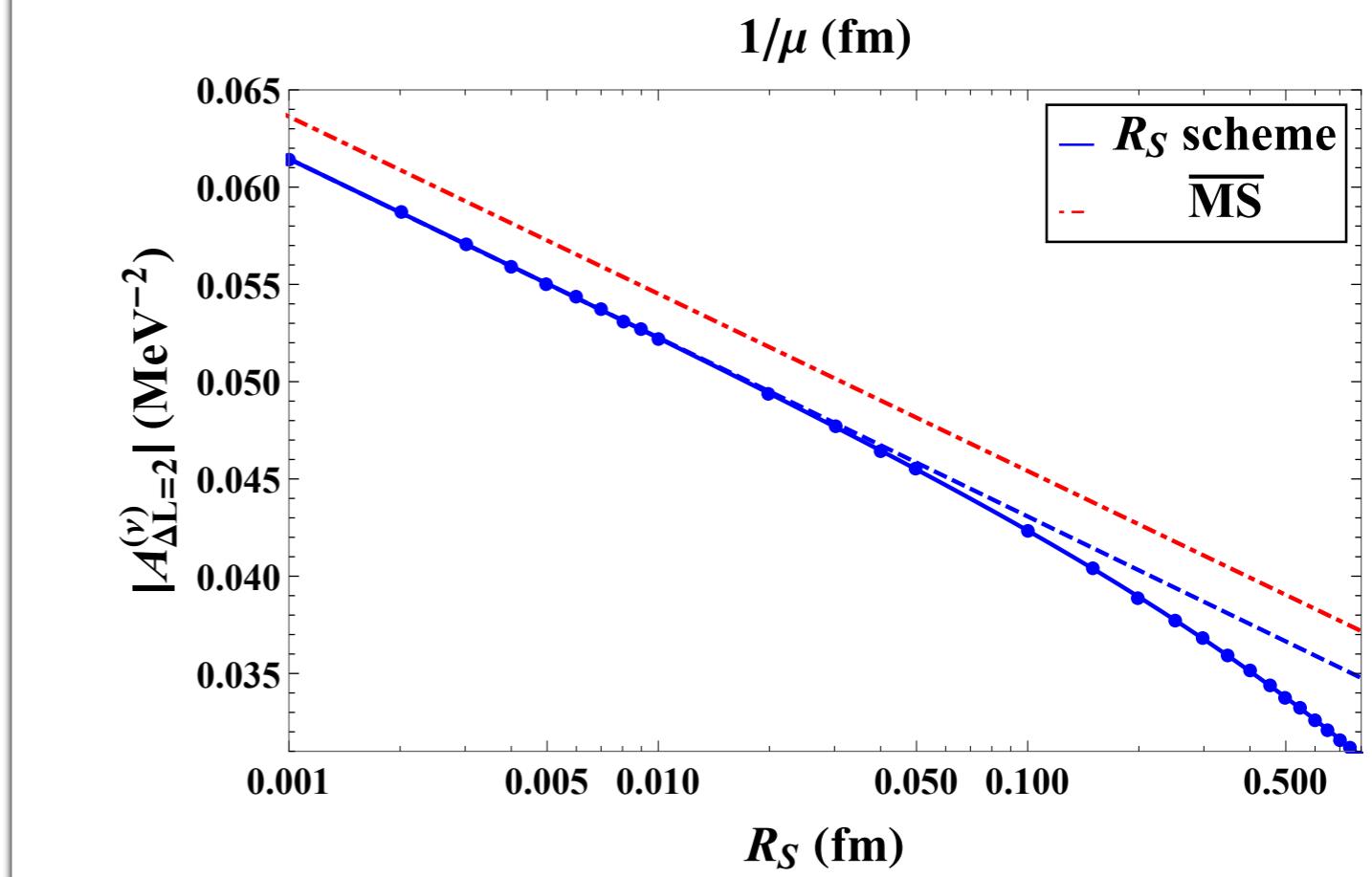
- Amplitudes obtained using
 - MSbar
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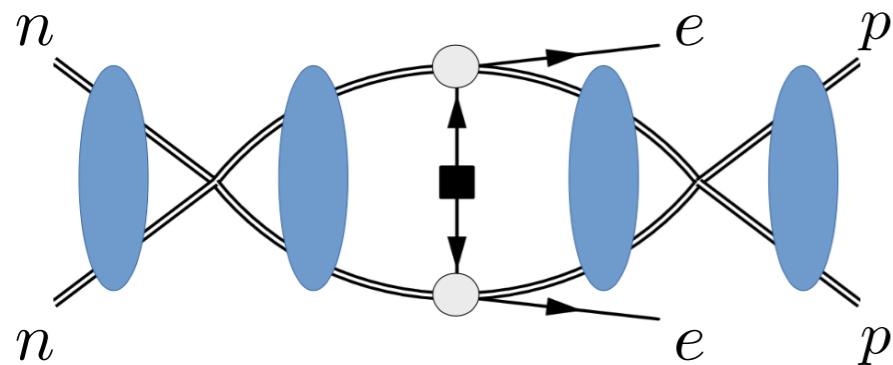
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- Need a LO contact interaction to cancel this dependence, g_ν^{NN}
 - At present unknown, unable to reliably estimate the impact
 - Could be determined from lattice calculation of nn->ppee
 - Estimate from relation to EM suggests a 25-60% contribution (backup slides)
 - Assumptions with uncontrolled error

Checking the Weinberg counting

Any effect for the dim-6,7,9 terms?

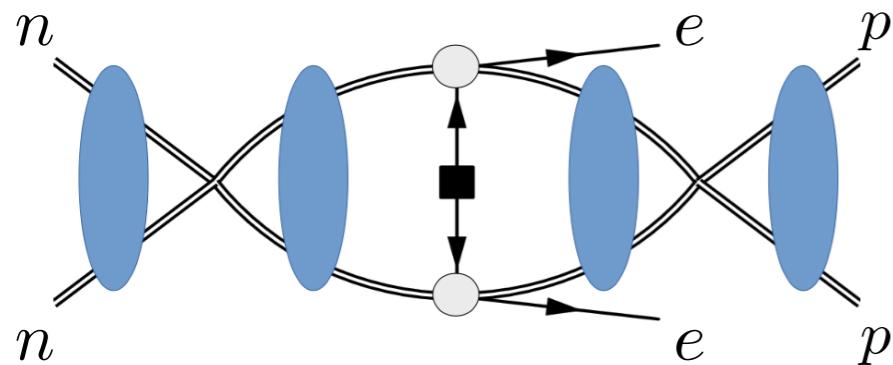


$$\sim m_N^2 \int d^3 q d^3 k \frac{1}{m_N E - \vec{q}^2} \frac{1}{(\vec{q} - \vec{k})^2} \frac{1}{m_N E' - \vec{k}^2}$$

- In the Majorana-mass case, the divergence is due to the LNV potential at large q (small r)
- Behaves like $V_{\Delta L=2} \sim 1/\vec{q}^2$

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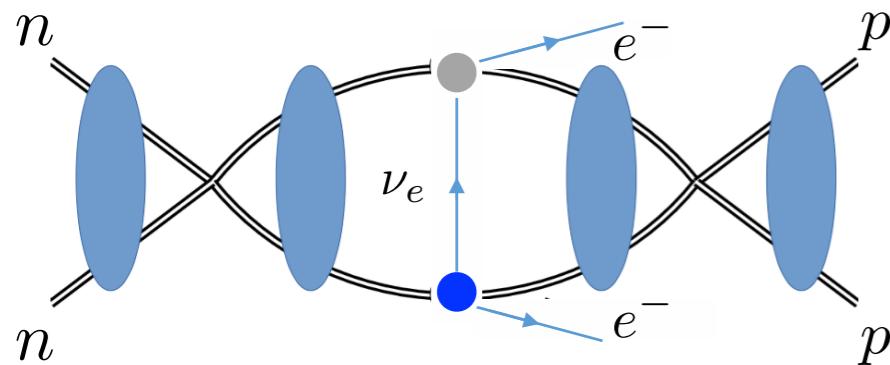
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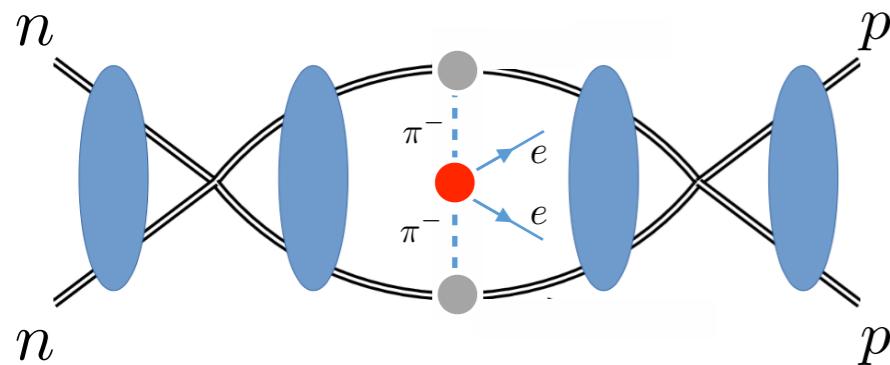
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Dimension-6,7,9

- Several potentials have the same behavior
 - The case for the vector operators $C_{VL,VB}^{(6)}$: $V_{\Delta L=2} \sim 1/\vec{q}^2$

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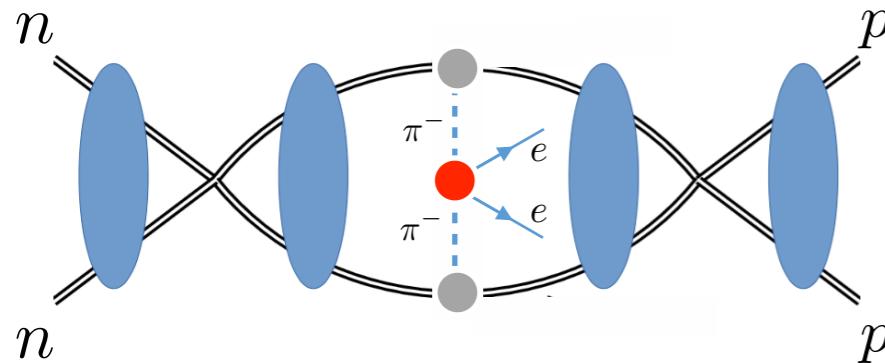
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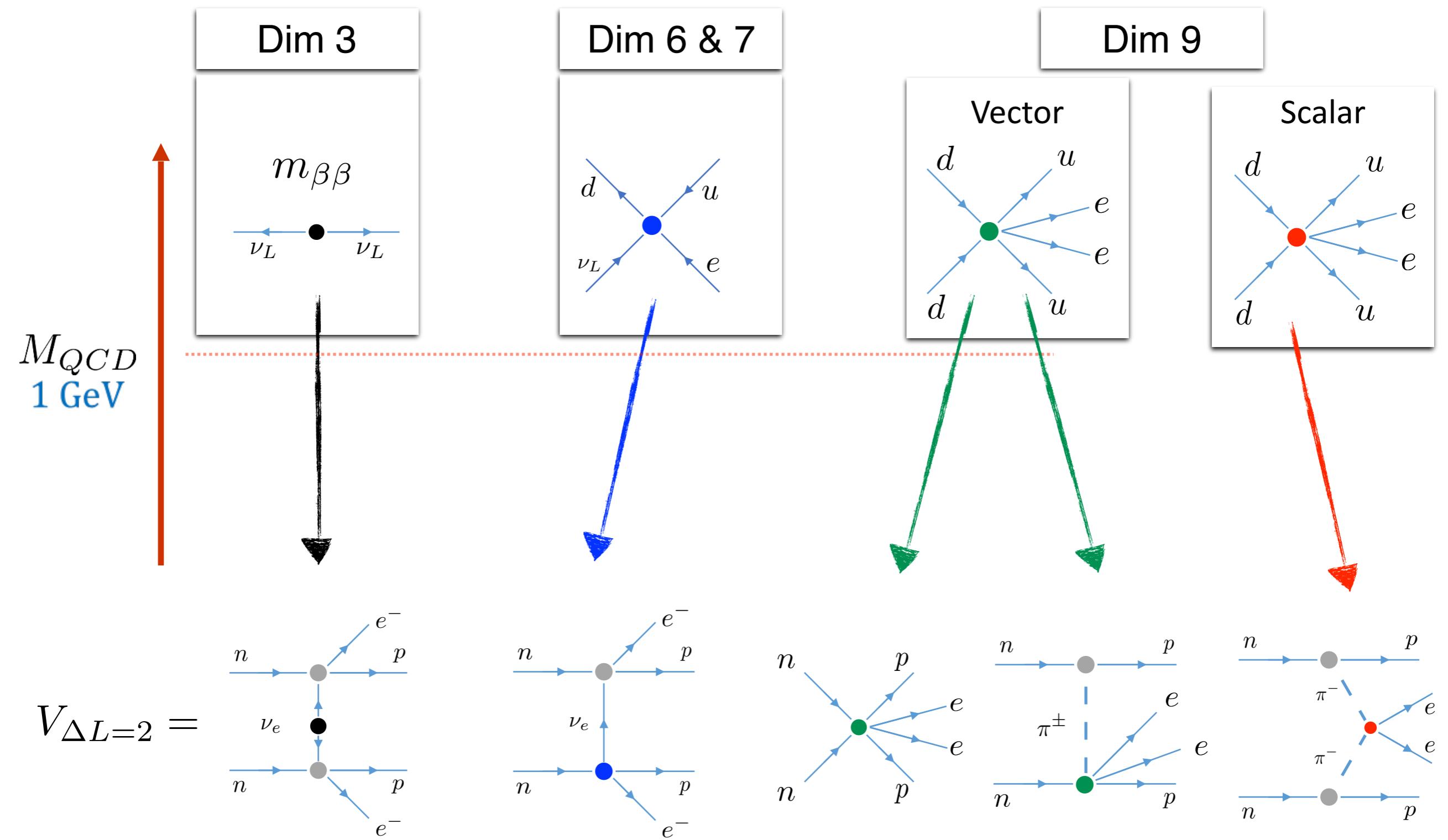
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- Need to include contact interactions at LO in these cases
 - Often disagrees with the Weinberg / NDA counting

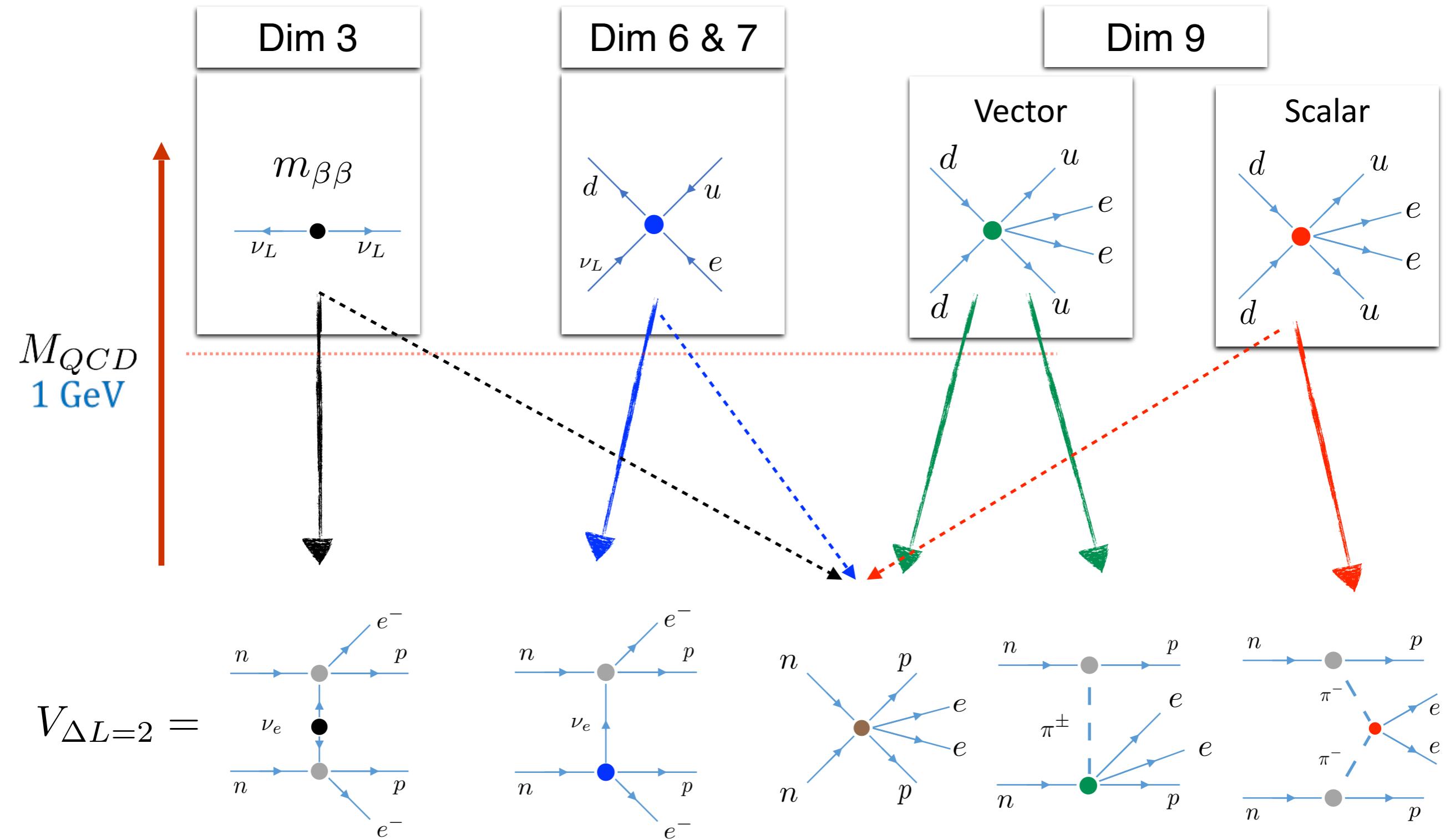
Chiral EFT

NDA / Weinberg



Chiral EFT

Beyond NDA / Weinberg



Chiral EFT

Power counting

Contributions to the amplitude scale as

	$d=3$	$C_{\text{SL, SR}}^{(6)}$	$C_{\text{T}}^{(6)}$	$C_{\text{VL}}^{(6)}$	$C_{\text{VR}}^{(6)}$	$C_{\text{VL, VR}}^{(7)}$	$C_{1\text{R}}^{(9)(\prime)}$	$C_{1\text{L}}^{(9)(\prime)}$	$C_{2\text{R}-5\text{R}}^{(9)(\prime)}$	$C_{2\text{L}-5\text{L}}^{(9)(\prime)}$	$C_{\text{vector}}^{(9)}$
$m_e \mathcal{A}$	$m_{\beta\beta}$	Λ_χ	$\Lambda_\chi \epsilon_\chi^2$	$\Lambda_\chi \epsilon_\chi^2$	$\Lambda_\chi \epsilon_\chi^3$	$\frac{\Lambda_\chi^2}{v} \epsilon_\chi^2$	$\frac{\Lambda_\chi^2}{v} \epsilon_\chi^2$	$\frac{\Lambda_\chi^2}{v} \epsilon_\chi^2$	$\frac{\Lambda_\chi^2}{v}$	$\frac{\Lambda_\chi^2}{v}$	$\frac{\Lambda_\chi^2}{v} \epsilon_\chi^2$

$$\Lambda_\chi = 1 \text{ GeV}, \quad \epsilon_\chi = m_\pi / \Lambda_\chi$$

Chiral EFT

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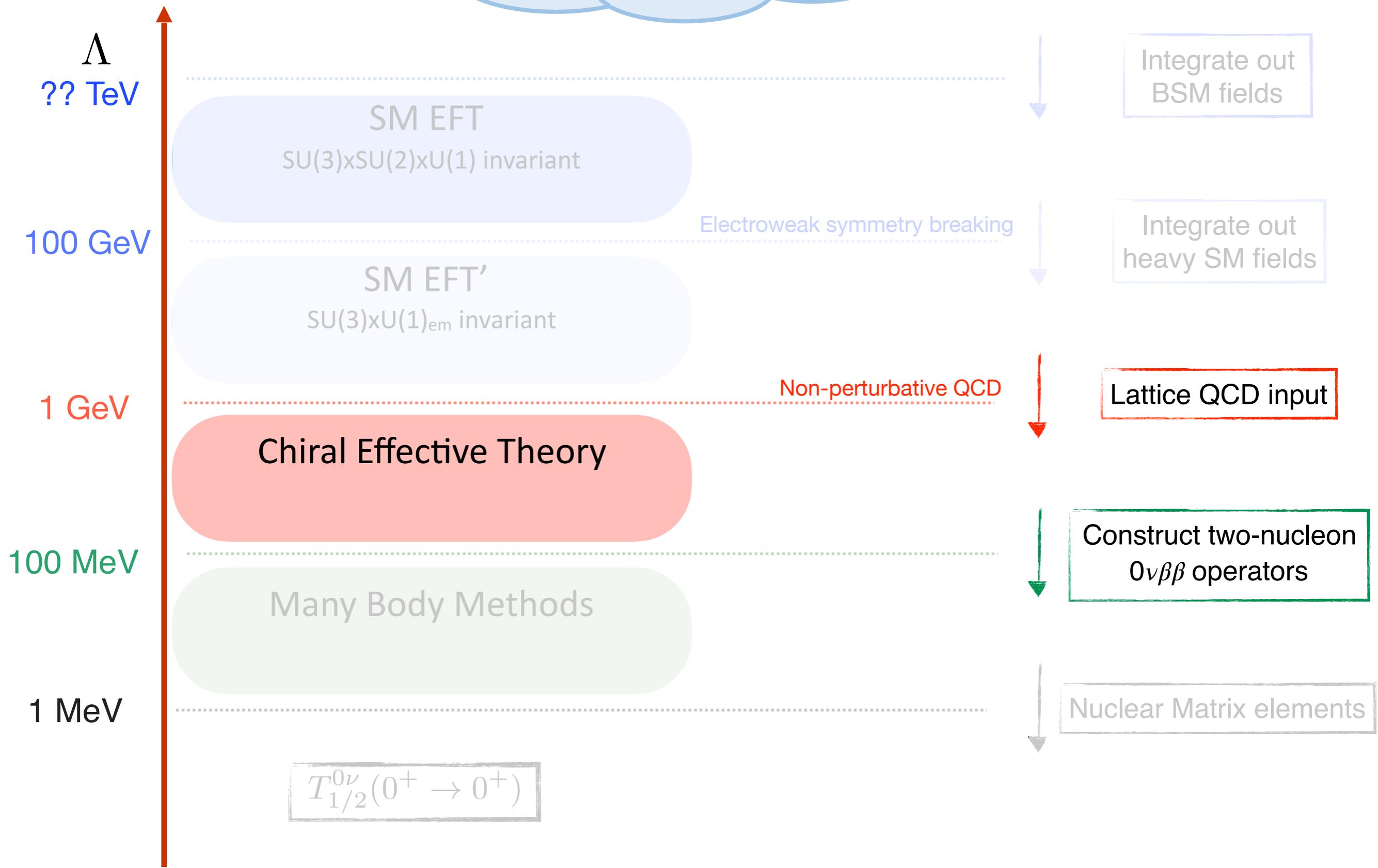
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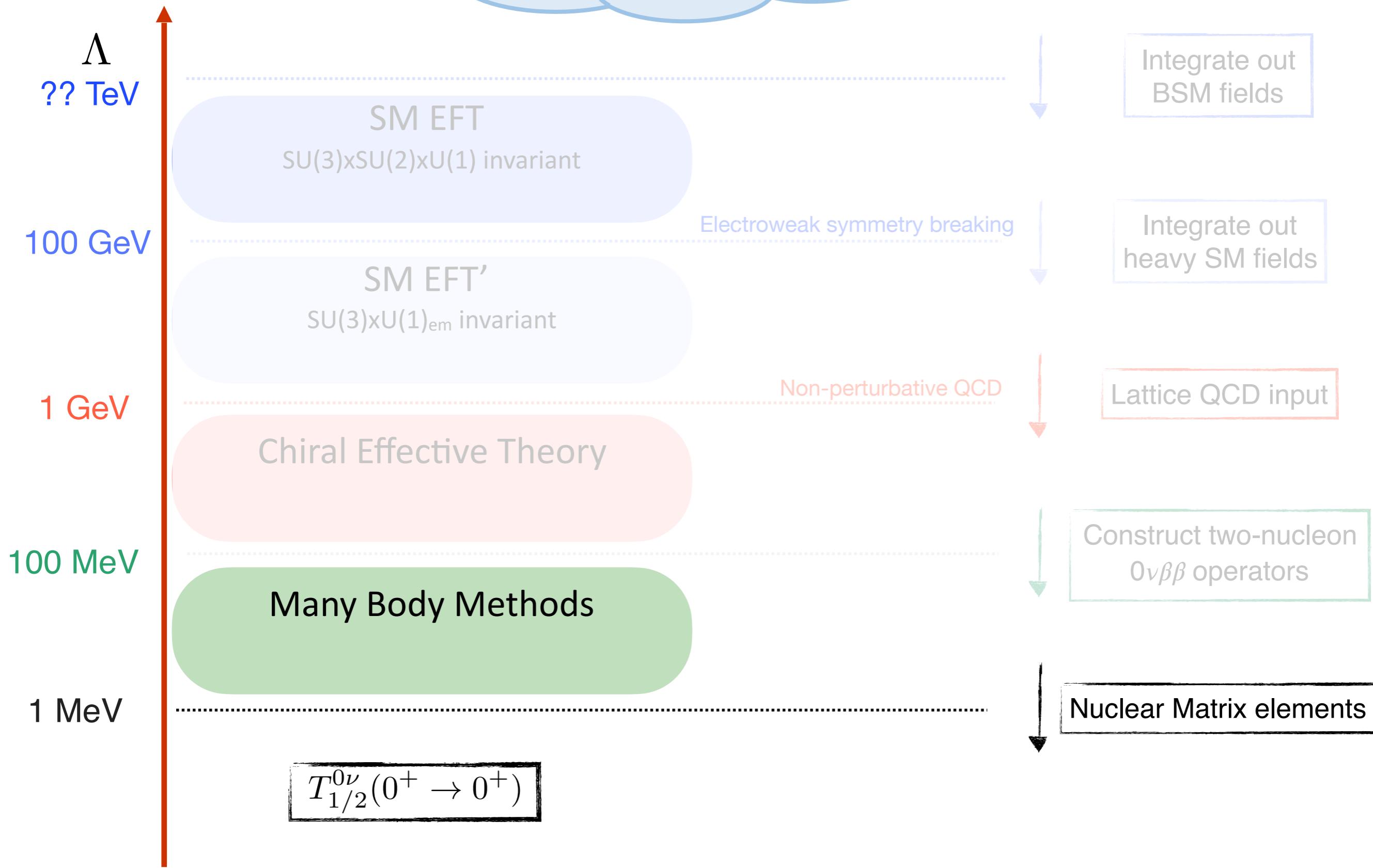
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- The dimension-seven and -nine operators are suppressed by Λ_χ/v
- Most operators are suppressed by two or three powers of $\epsilon_\chi = m_\pi/\Lambda_\chi$
- Should be combined with the scaling of the Wilson coefficients to see which are important
 - To be determined in explicit models of new physics

Outline



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The $0\nu\beta\beta$ half-life

$$\Gamma^{0\nu}(0^+ \rightarrow 0^+) \sim \left| \langle 0^+ | \sum_{\text{nucleons}} \int \frac{d^3\mathbf{q}}{(2\pi)^3} e^{i\mathbf{q}\cdot\mathbf{r}} V(\mathbf{q}^2) | 0^+ \rangle \right|^2 = \sum_{i,j} G_{i,j} M_i M_j g_i g_j C_i C_j^*$$

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 - Perturbative, determined by BSM physics

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Nuclear matrix elements

- All NMEs can be obtained from those of light/heavy neutrino exchange
 - 9 long-distance & 6 short-distance
 - Have been determined in literature
- Follow ChPT expectations fairly well
 - E.g. all $O(1)$

NMEs	^{76}Ge			
	[74]	[31]	[81]	[82, 83]
M_F	-1.74	-0.67	-0.59	-0.68
M_{GT}^{AA}	5.48	3.50	3.15	5.06
M_{GT}^{AP}	-2.02	-0.25	-0.94	
M_{GT}^{PP}	0.66	0.33	0.30	
M_{GT}^{MM}	0.51	0.25	0.22	
M_T^{AA}	—	—	—	
M_T^{AP}	-0.35	0.01	-0.01	
M_T^{PP}	0.10	0.00	0.00	
M_T^{MM}	-0.04	0.00	0.00	

NMEs	^{76}Ge			
	$M_{F, sd}$	$M_{GT, sd}^{AA}$	$M_{GT, sd}^{AP}$	$M_{GT, sd}^{PP}$
$M_{F, sd}$	-3.46	-1.55	-1.46	-1.1
$M_{GT, sd}^{AA}$	11.1	4.03	4.87	3.62
$M_{GT, sd}^{AP}$	-5.35	-2.37	-2.26	-1.37
$M_{GT, sd}^{PP}$	1.99	0.85	0.82	0.42
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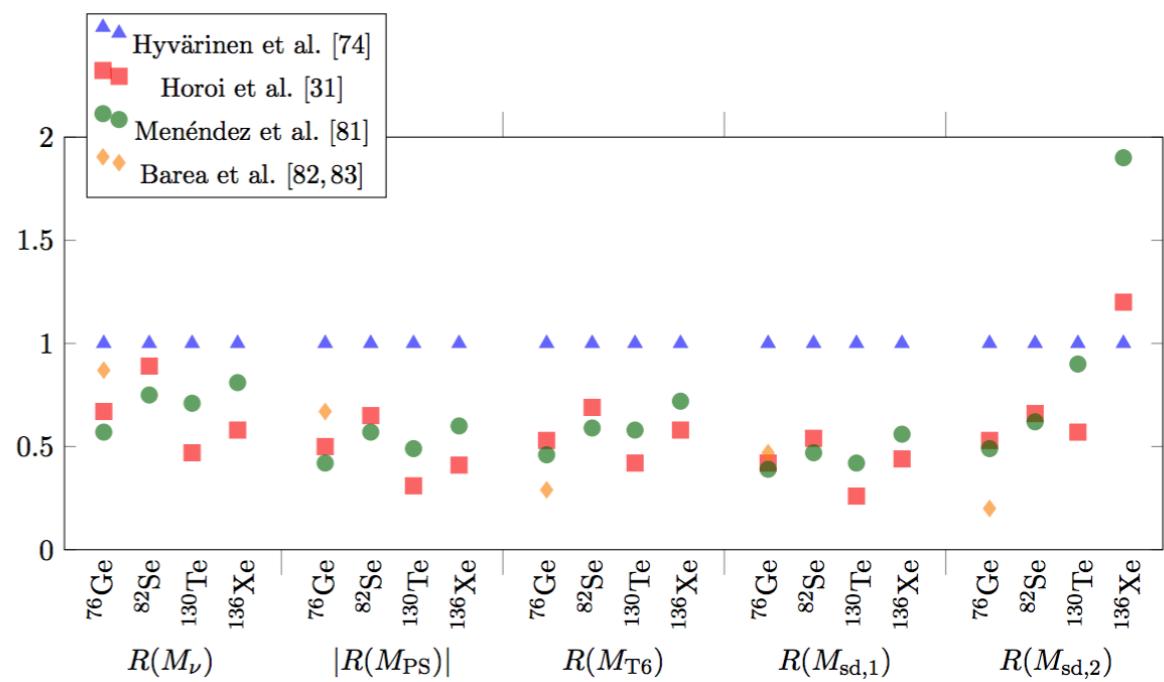
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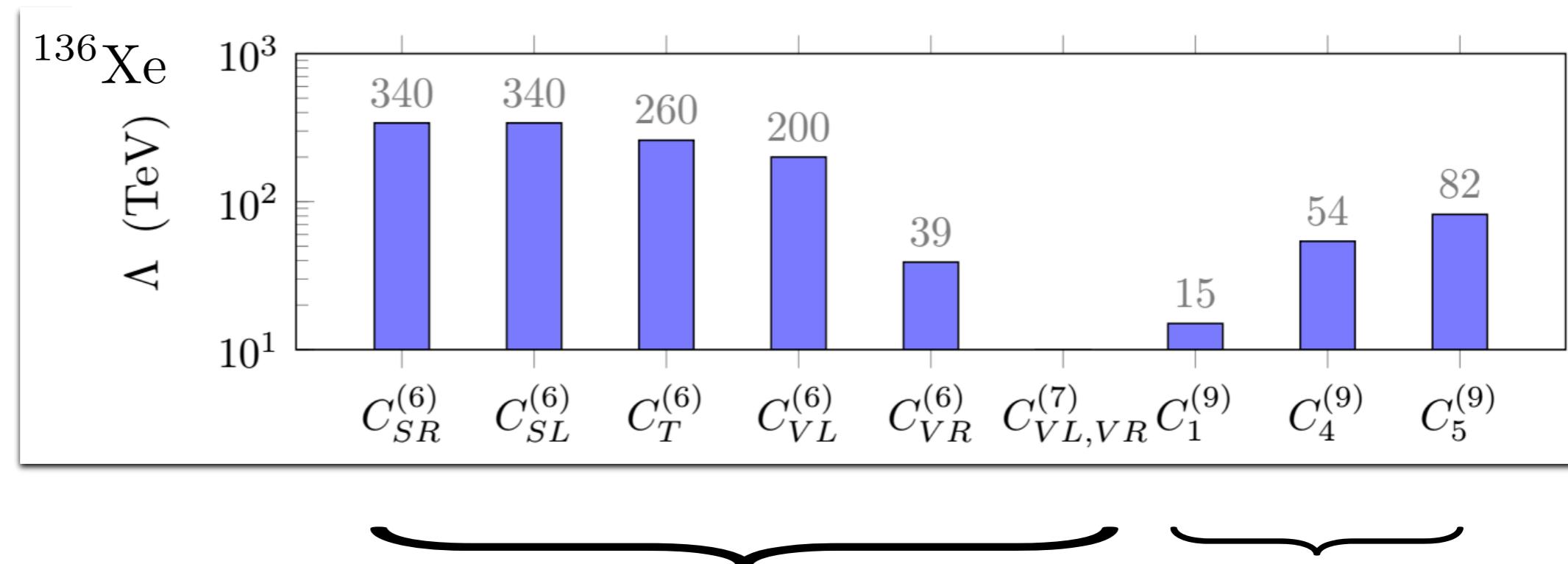
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- The NMEs differ by a factor 2-3 between methods
 - For Majorana-mass term & other LNV sources

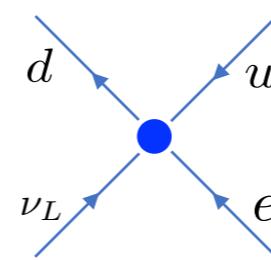


Current limits

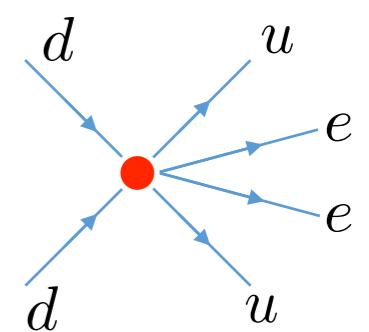
- Assumes $C_i = v^3/\Lambda^3$



- Uncertainties:
 - Unknown LECs
 - Nuclear Matrix elements



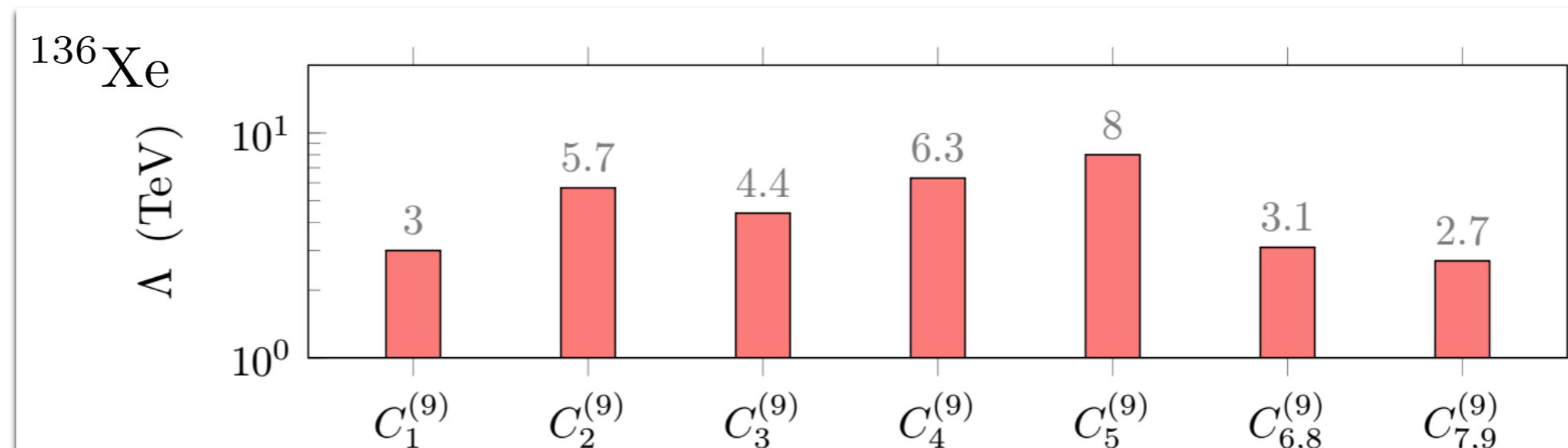
Dim 6 & 7



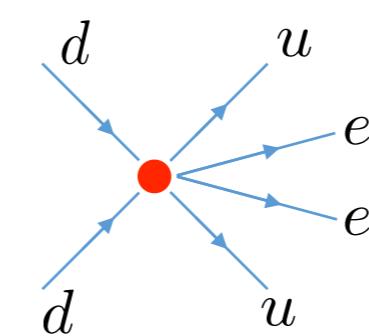
Dim 9

Current limits

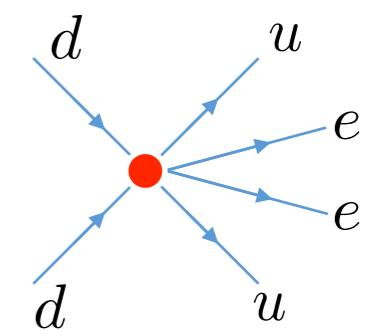
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Dim 9
Scalar



Dim 9
Vector

An example: LR model

In Left-Right models:

- SM gauge symmetry is extended to $SU(2)_R \times SU(2)_L \times U(1)_{B-L}$
- Allows for parity or charge-conjugation to be restored at high energies
- Explains neutrino masses through the see-saw mechanism (Type-I & Type-II)

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- New Fields:
 - Right-handed bosons W_R, Z_R
 - Right-handed neutrinos ν_R
 - Heavy new scalars δ_R^{++}

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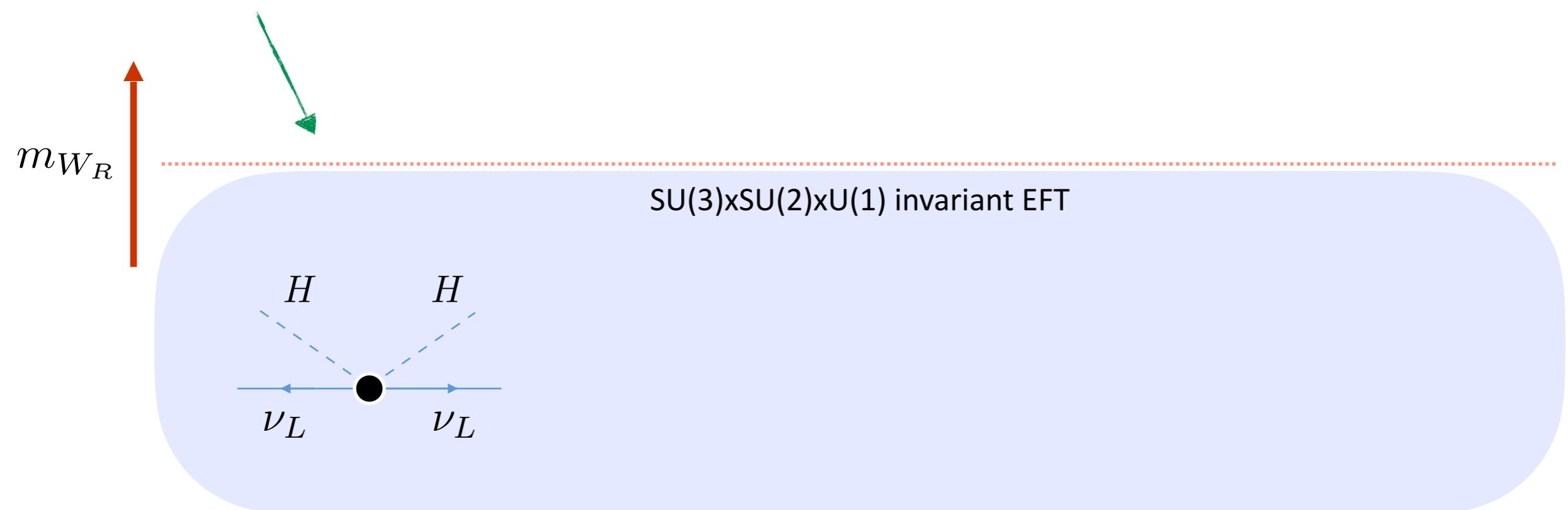
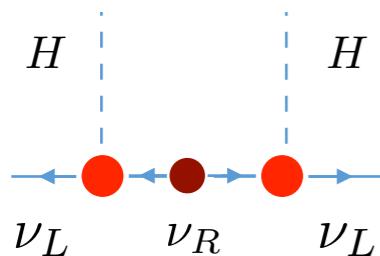
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Violates lepton number

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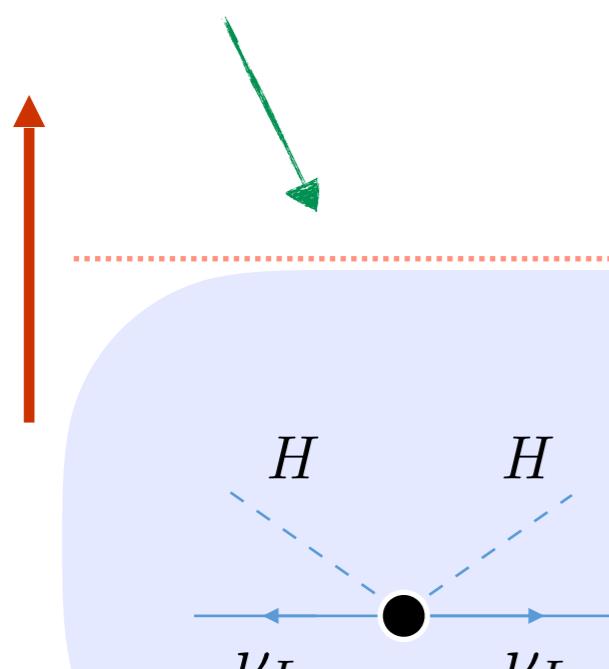
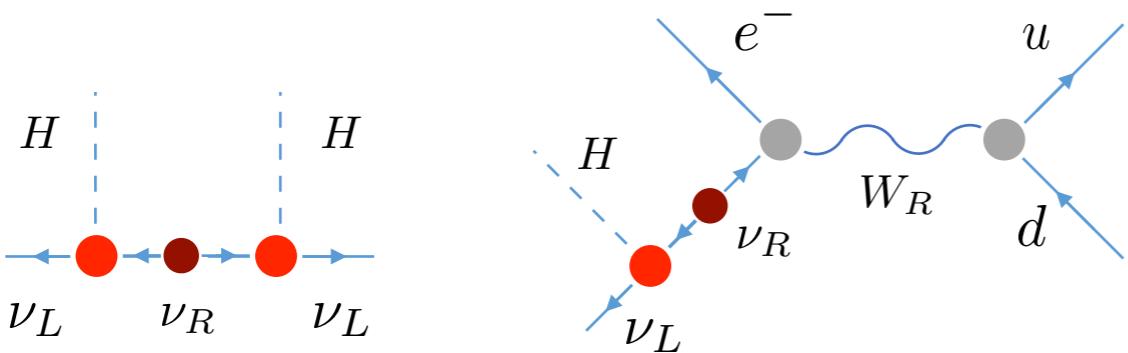
An example: LR model

- $\sim y_e = m_e/v$
- $\Delta L = 2$



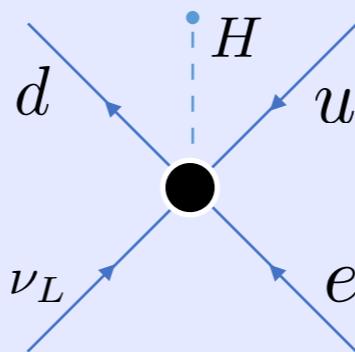
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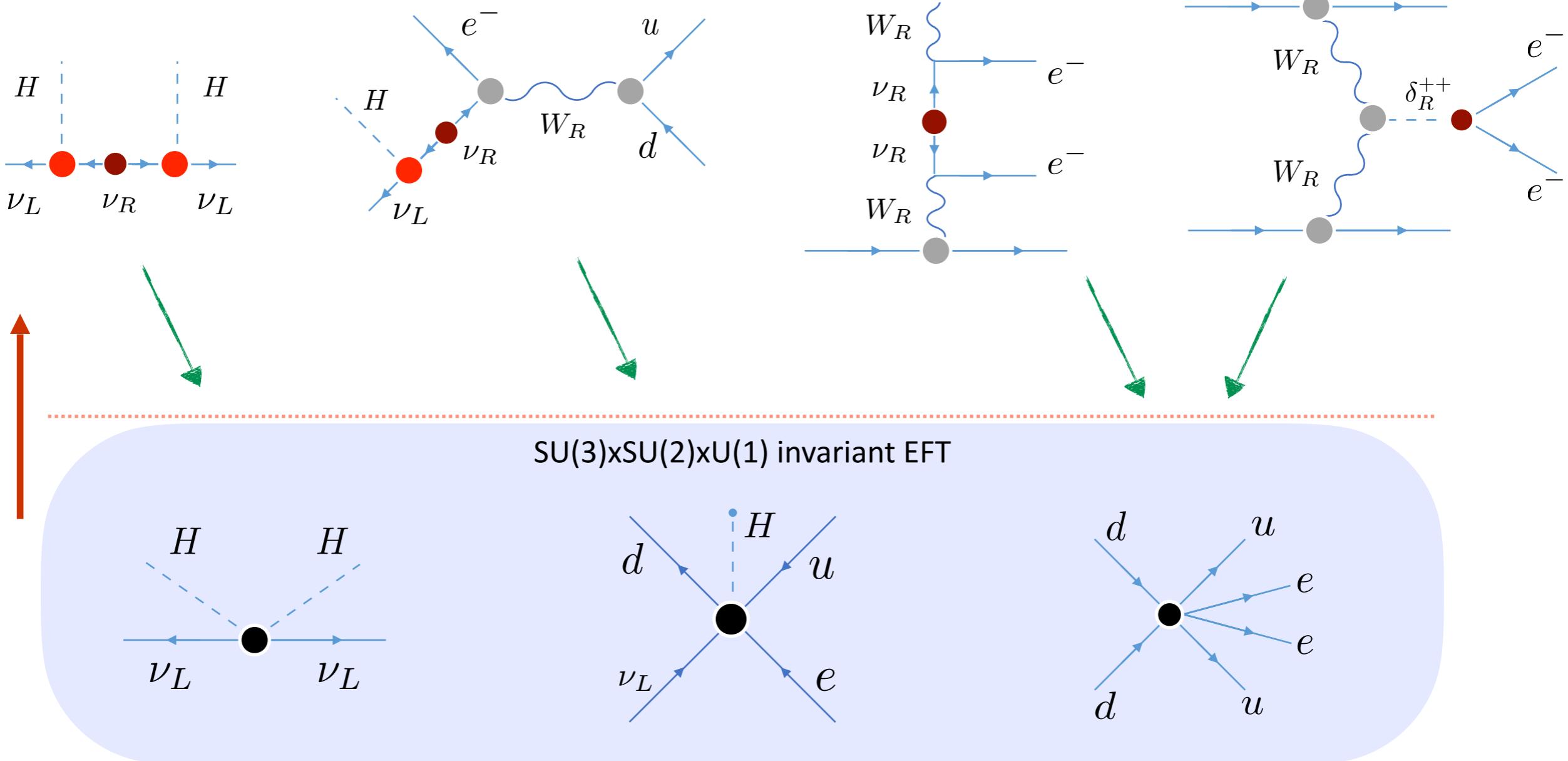
m_{W_R}

SU(3)xSU(2)xU(1) invariant EFT



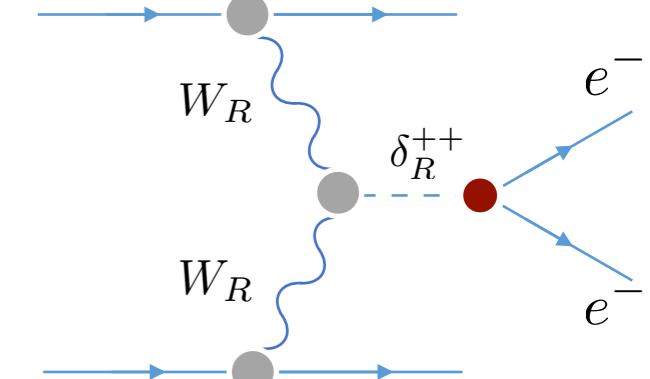
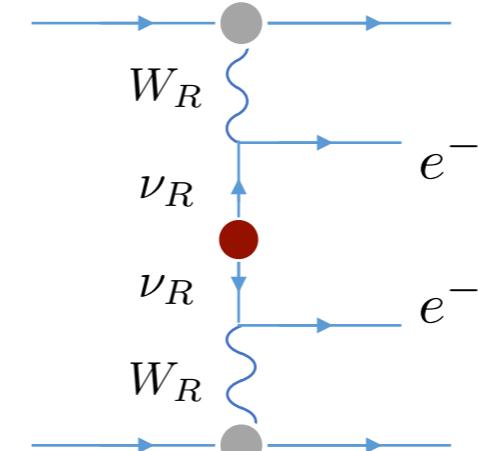
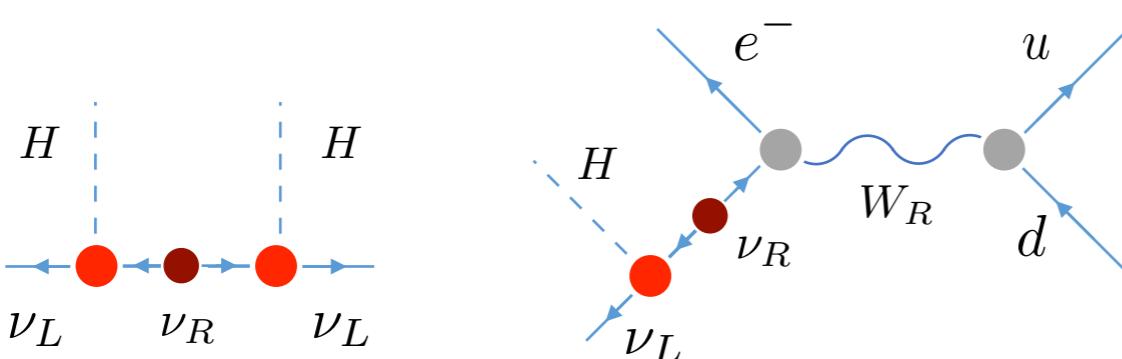
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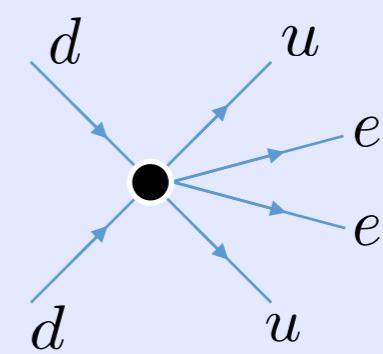
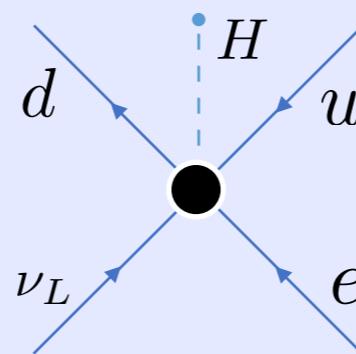
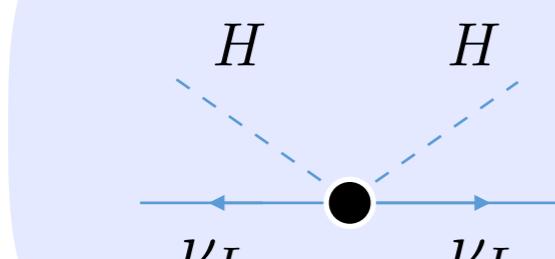
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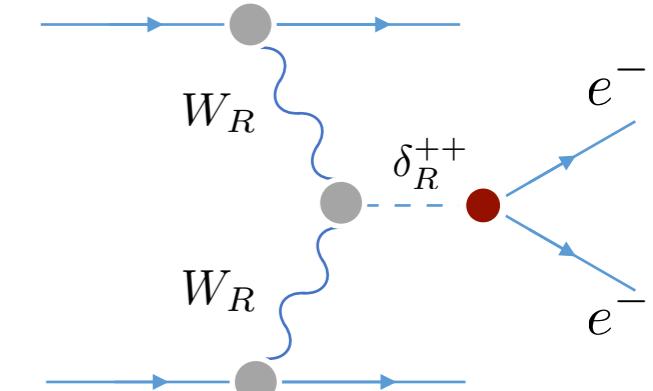
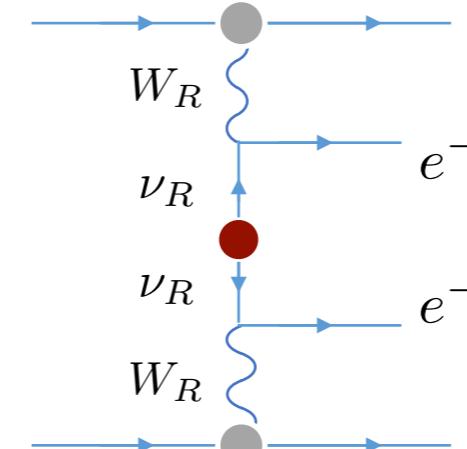
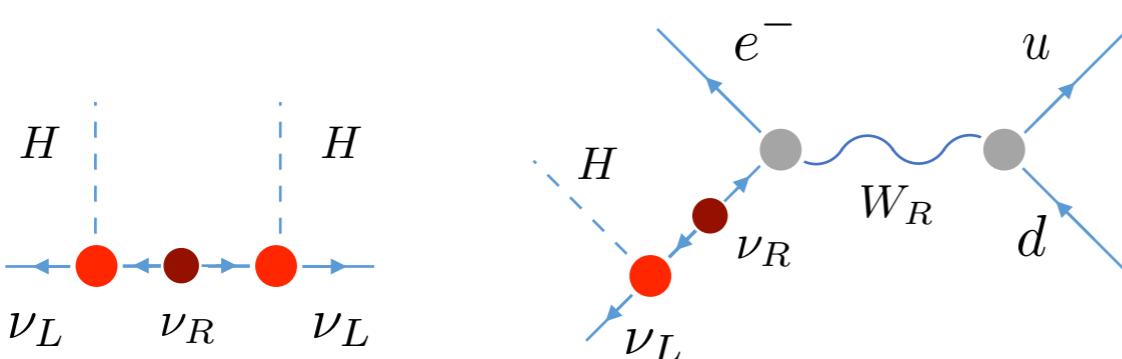
$$\text{dim-5} \sim y_e^2 \left(\frac{v}{\Lambda}\right)$$

$$\text{dim-7} \sim y_e \left(\frac{v}{\Lambda}\right)^3$$

$$\text{Dim-9} \sim \left(\frac{v}{\Lambda}\right)^5$$

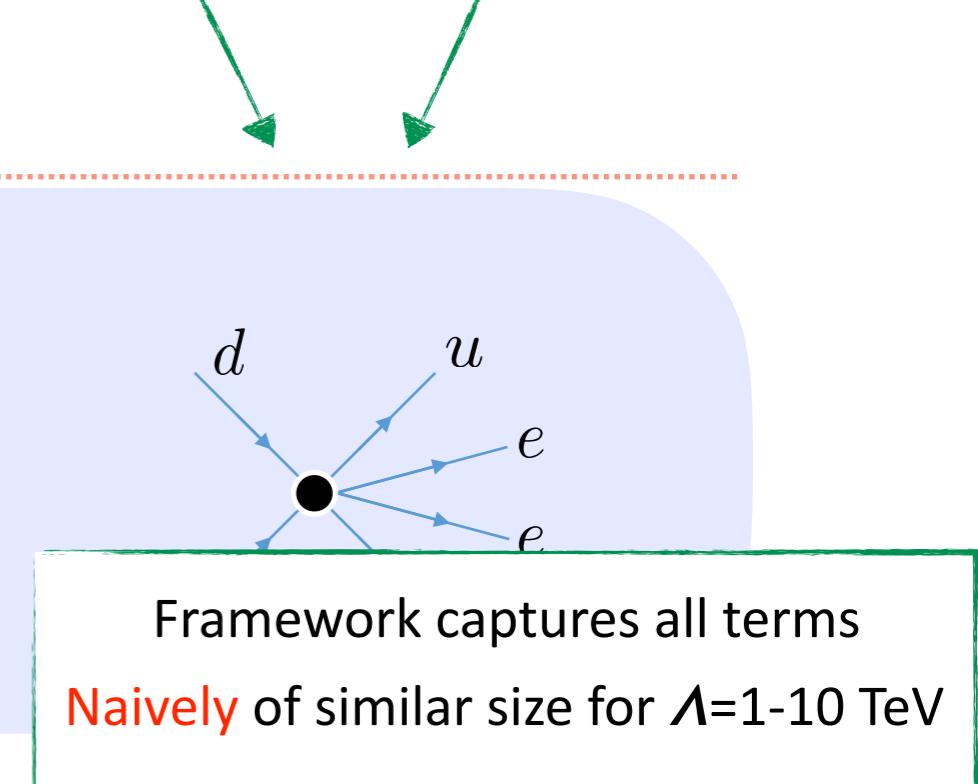
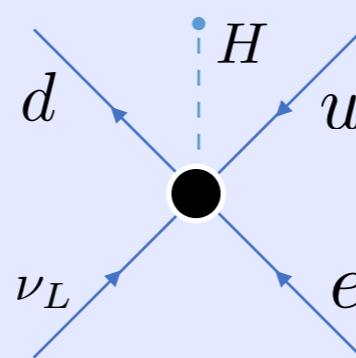
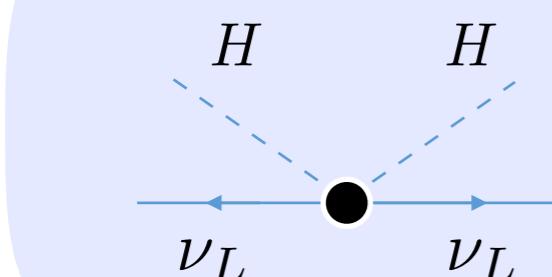
An example: LR model

- $\sim y_e = m_e/v$
- $\Delta L = 2$



m_{W_R}

SU(3)xSU(2)xU(1) invariant EFT



$$\text{dim-5} \sim y_e^2 \left(\frac{v}{\Lambda}\right)$$

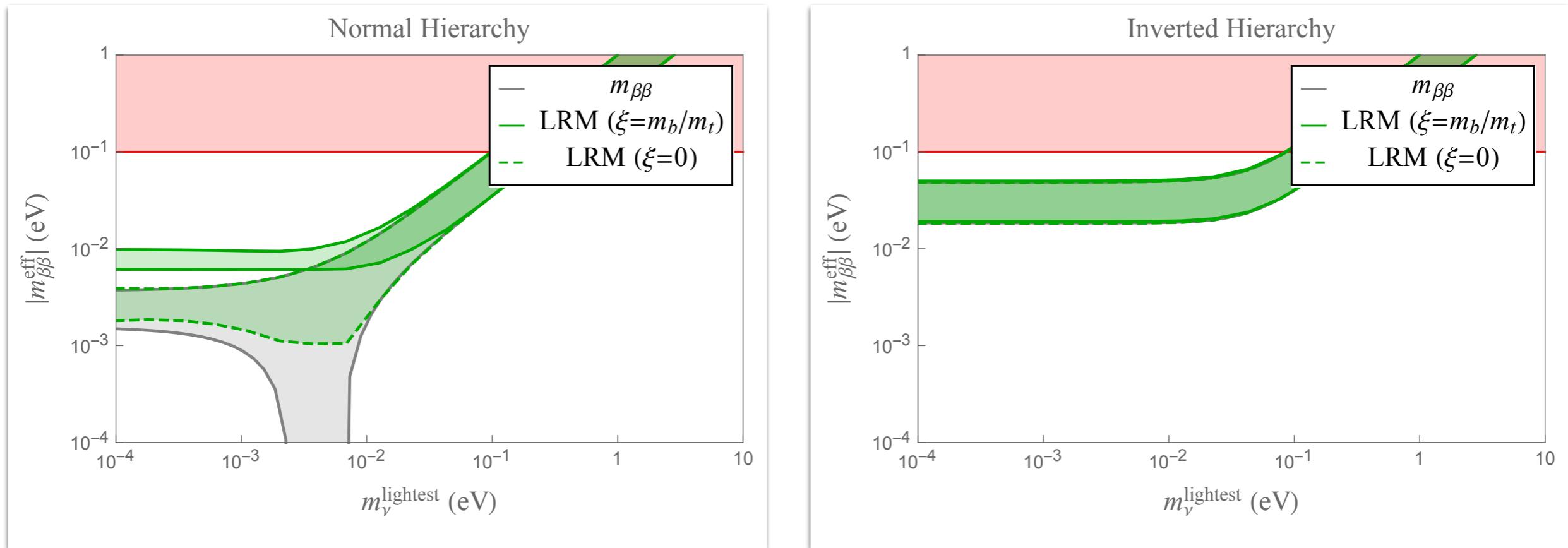
$$\text{dim-7} \sim y_e \left(\frac{v}{\Lambda}\right)^3$$

$$\text{Dim-9} \sim \left(\frac{v}{\Lambda}\right)^5$$

An example: LR model

$$m_{W_R} = 4.5 \text{ TeV}, \quad m_{\nu_R} = 10 \text{ TeV}, \quad m_{\delta_R^{++}} = 4 \text{ TeV}$$

- Assume right-handed neutrino mixing follows the PMNS matrix



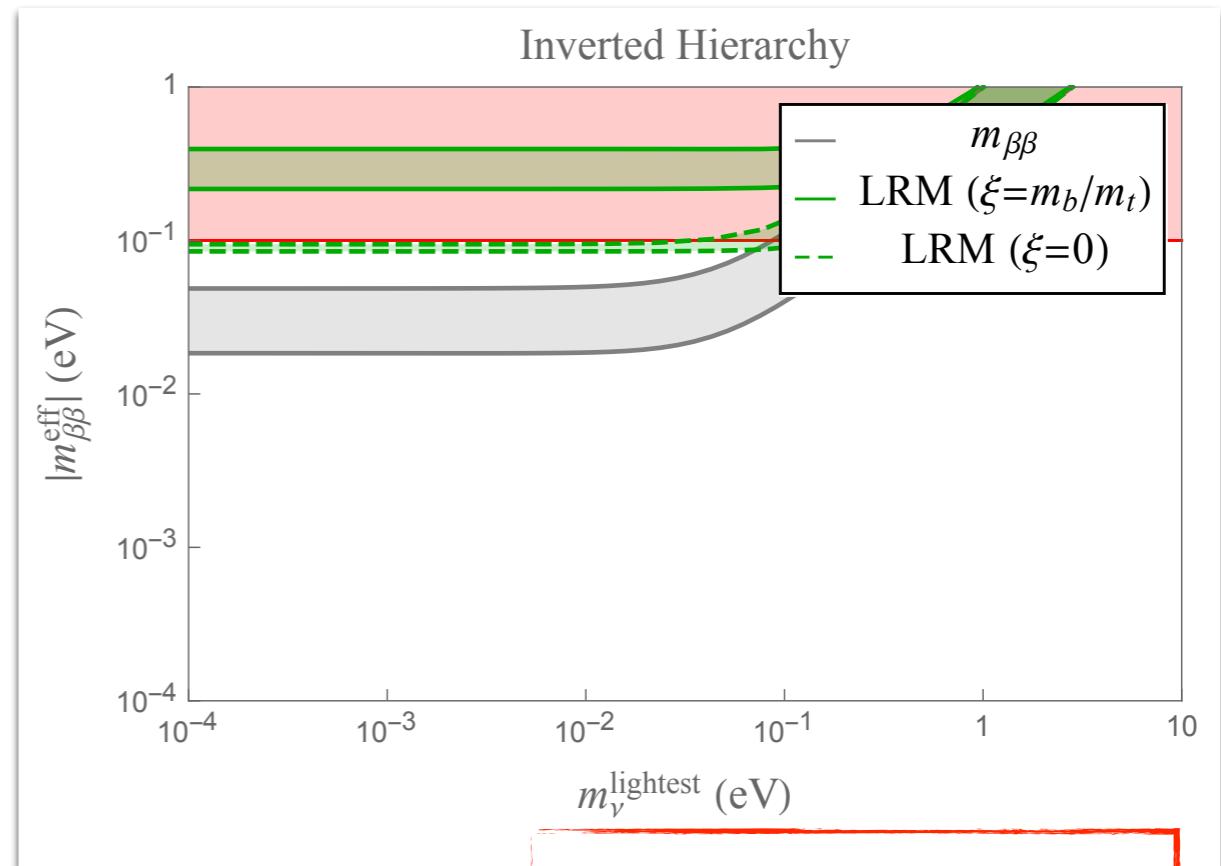
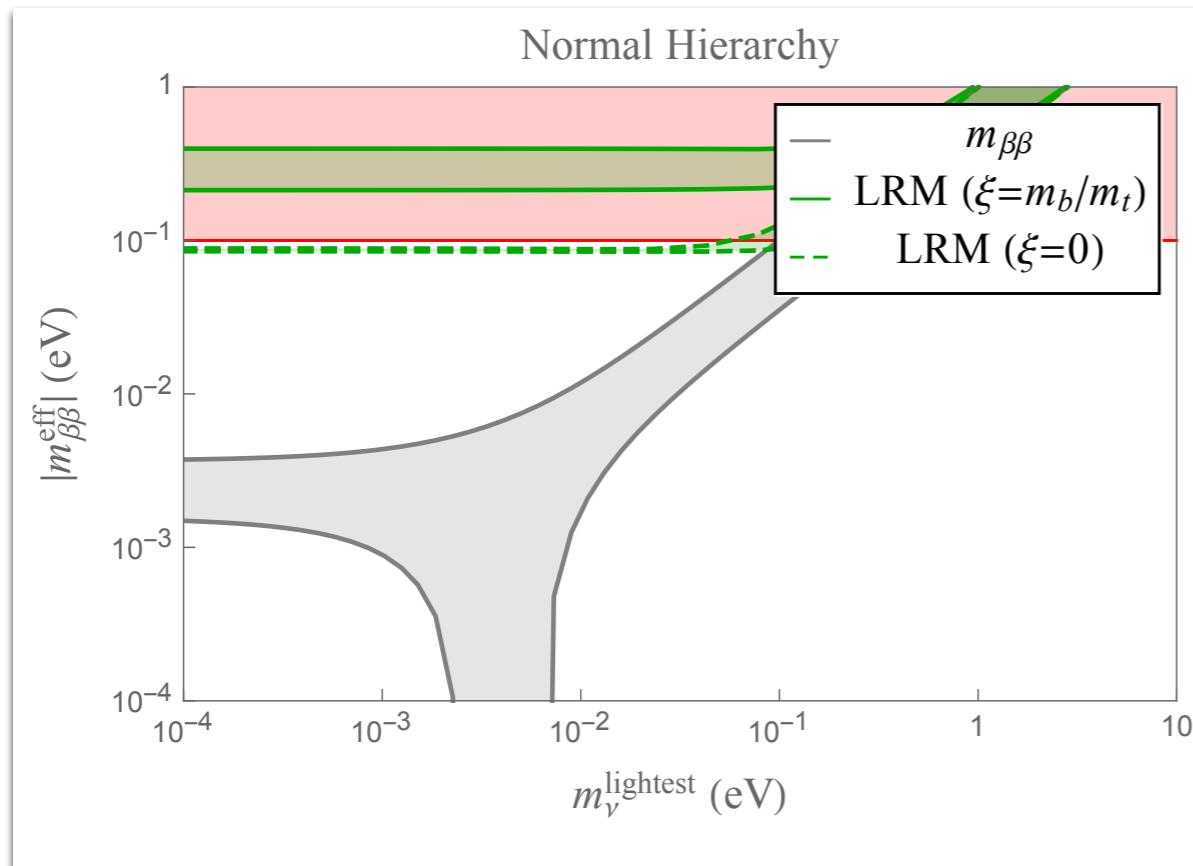
- Mild effect on NH (due to dim-9)
- Negligible effect in IH case, dim-5 terms dominate
 - Due to chiral suppression of the induced dim-6,7,9 operators

An example: LR model

$$m_{W_R} = 4.5 \text{ TeV}, \quad m_{\nu_R} = 10 \text{ GeV}, \quad m_{\delta_R^{++}} = 4 \text{ TeV}$$

- Assume right-handed neutrino mixing follows the PMNS matrix

Not excluded by collider searches

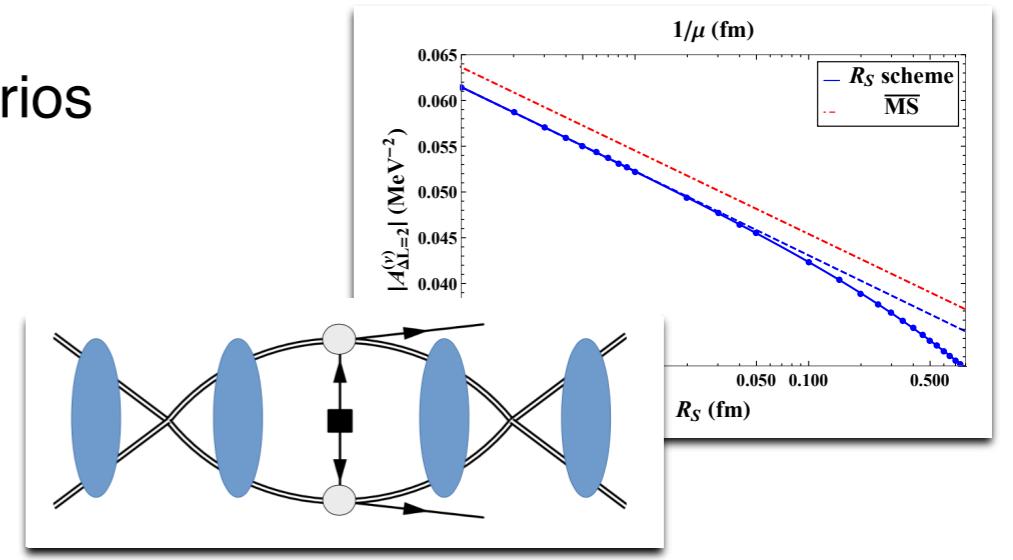


- Large effect in both NH & IH
- Now dominated by dim-9 terms

Subject to
NME / LEC uncertainties

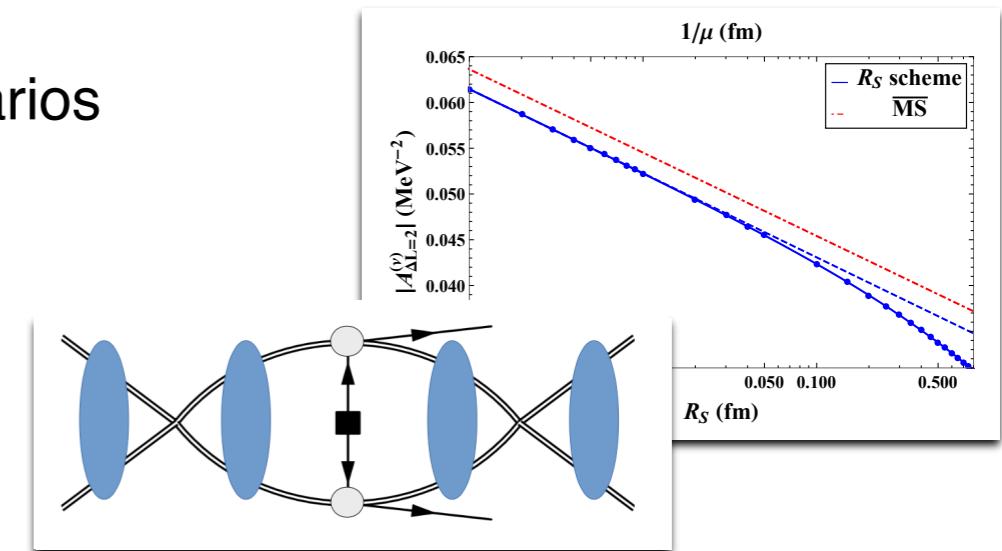
Summary

- EFTs allow a model-independent description of $\Delta L=2$ scenarios
- Renormalization requires counterterms beyond NDA

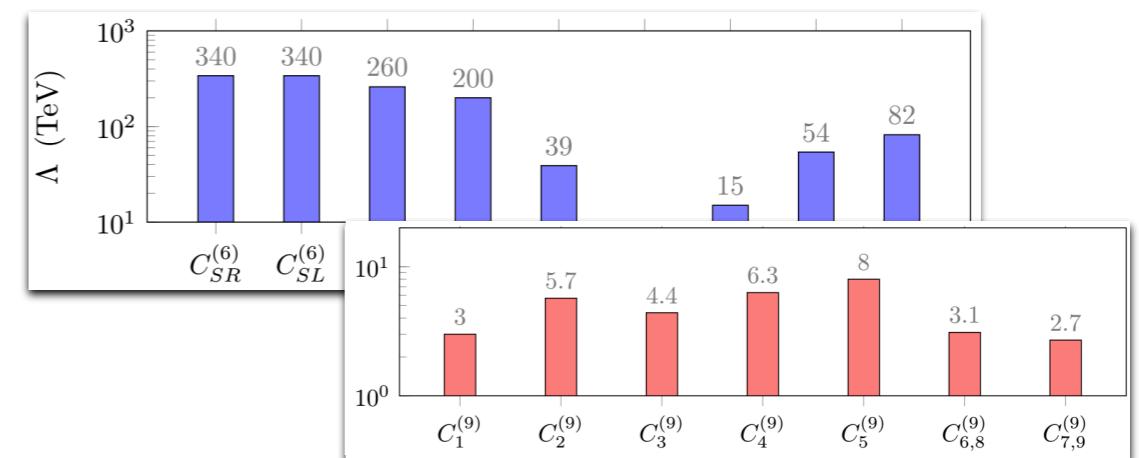


Summary

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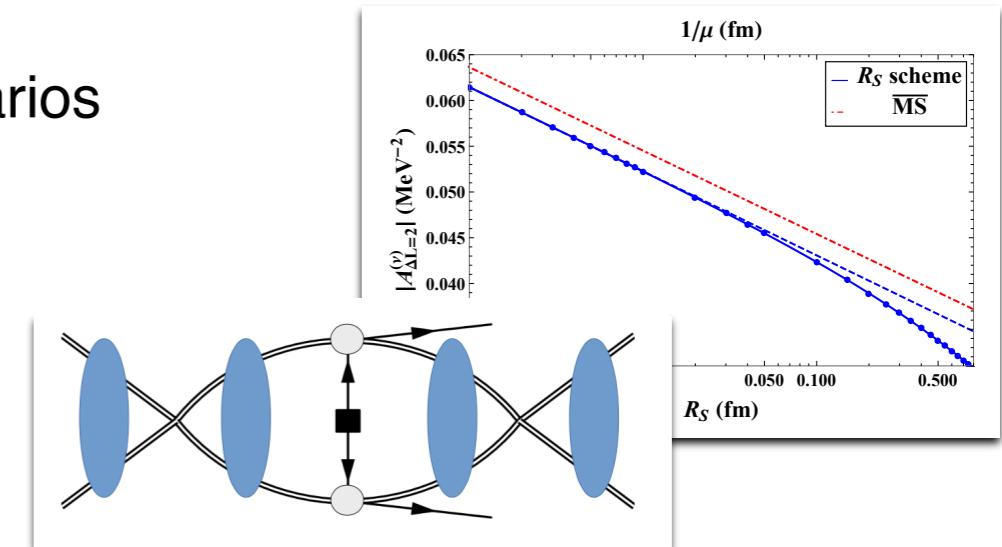


- Limits on higher-dimensional operators probe
 - O(1-10) TeV scales for dim-9
 - O(100) TeV scales for dim-7
- Order 1 uncertainties
 - Unknown LECs + NMEs

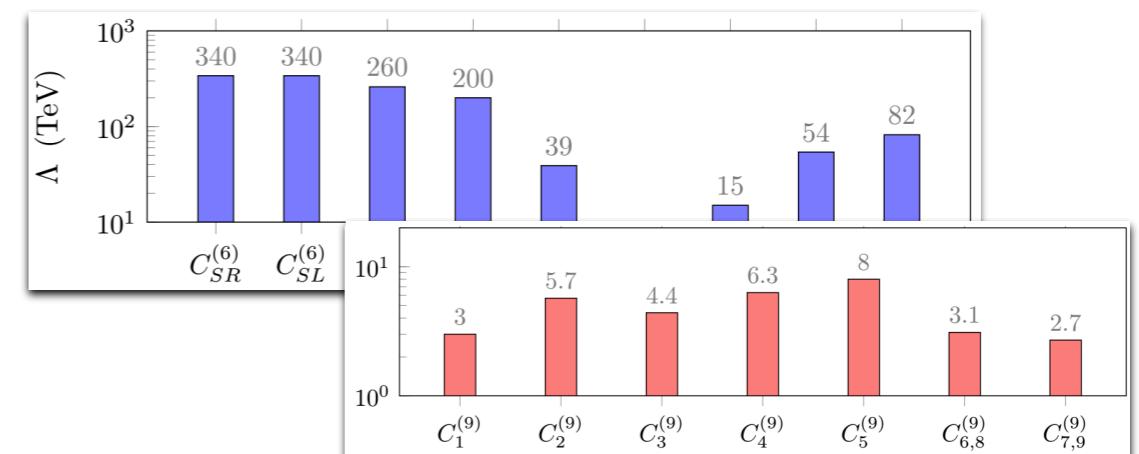


Summary

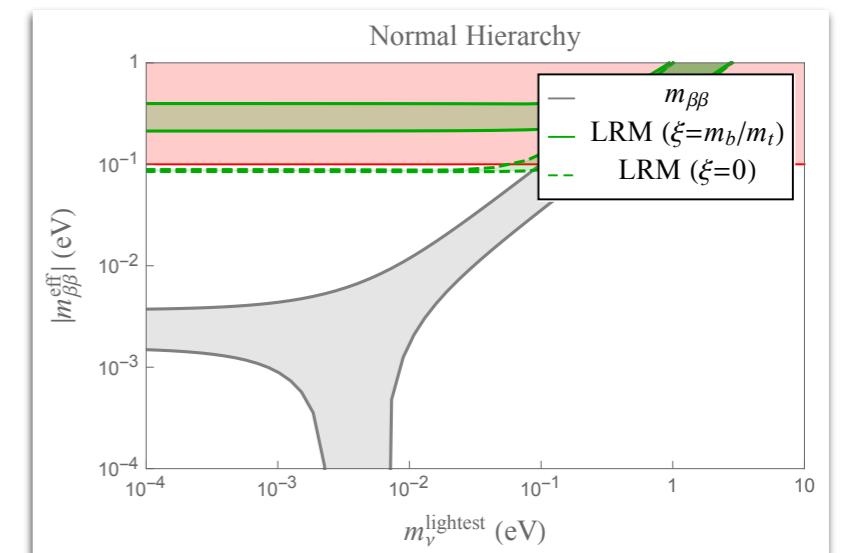
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- Limits on higher-dimensional operators probe
 - $O(1-10)$ TeV scales for dim-9
 - $O(100)$ TeV scales for dim-7
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- Explicit example: Left-right model
- Dimension-5, -7, and -9 induced
 - Captured by the EFT
 - Higher-dim. Operators can be important



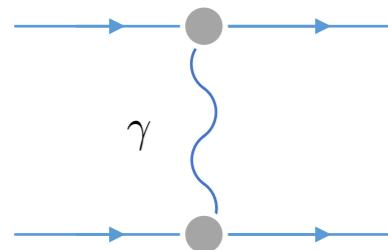
Back up slides

Relation to electromagnetism

Relation to electromagnetism

Majorana mass

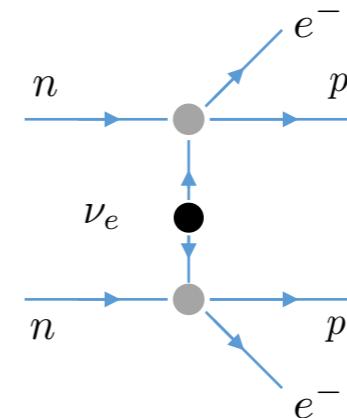
EM



$$\sim e^2/q^2$$



LNV



$$\sim G_F^2 m_{\beta\beta} / q^2$$

- Relation to Coulomb exchange?
 - $\Delta l=2$ piece of EM has similar chiral properties
 - Leptonic LNV part combines to a photon propagator

Relation to electromagnetism

Majorana mass

- Only two $\Delta l=2$ operators can be induced

$$O_1 = \bar{N} Q_L N \bar{N} Q_L N - \frac{\text{Tr } Q_L^2}{6} \bar{N} \vec{\tau} N \bar{N} \vec{\tau} N + (L \rightarrow R)$$

$$O_2 = \bar{N} Q_L N \bar{N} Q_R N - \frac{\text{Tr } Q_L Q_R}{6} \bar{N} \vec{\tau} N \bar{N} \vec{\tau} N + (L \leftrightarrow R)$$

with spurions

$$Q_L = u^\dagger Q_L u, \quad Q_R = u Q_R u^\dagger, \\ u = \exp(i\pi \cdot \tau / 2F_\pi)$$

Relation to electromagnetism

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EM

$$\mathcal{L}_{em} = e^2/4 (C_1 O_1 + C_2 O_2)$$

$$Q_L = Q_R = \tau^3/2$$

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LNV

$$\mathcal{L}_{LNV} = g_\nu^{NN} G_F^2 m_{\beta\beta} O_1 \bar{e} e^c$$

$$Q_L = \tau^+, \quad Q_R = 0$$

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Chiral symmetry

$$g_\nu^{NN} = C_1$$

Relation to electromagnetism

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EM

$$\mathcal{L}_{em} = e^2/4 (C_1 O_1 + C_2 O_2)$$

$$Q_L = Q_R = \tau^3/2$$

- EM induces an extra term

- Equivalent up to 2 pions
- Hard to disentangle



LNV

$$\mathcal{L}_{LNV} = g_\nu^{NN} G_F^2 m_{\beta\beta} O_1 \bar{e} e^c$$

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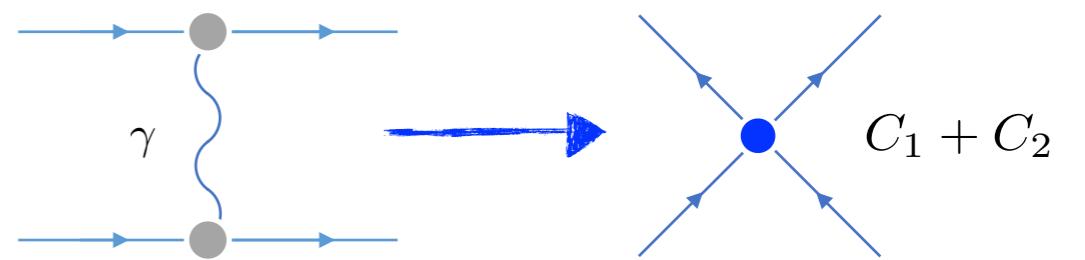
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$$g_\nu^{NN} = C_1$$

Relation to electromagnetism

Majorana mass

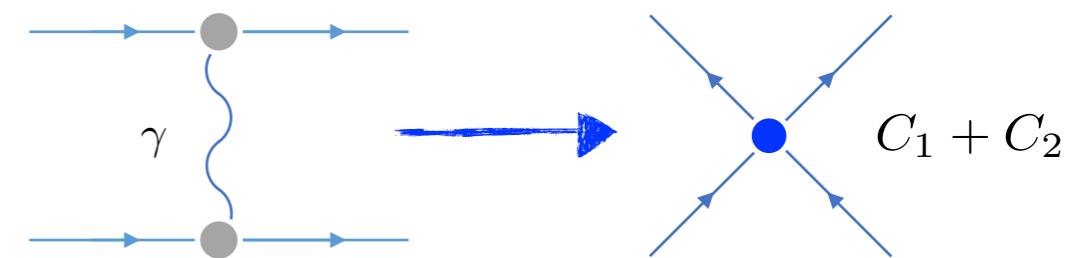
- $\Delta l=2$ in NN scattering
- Charge-independence breaking $(a_{nn} + a_{pp})/2 - a_{np}$
 - From photon exchange & the pion mass difference
 - $C_1 + C_2$ (needed at LO in isospin breaking)



Relation to electromagnetism

Majorana mass

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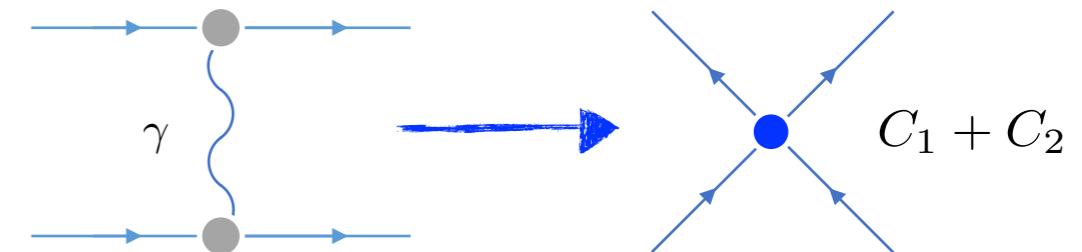


- Allows an estimate of g_ν^{NN}
 - Extract $C_1 + C_2$ from CIB
 - Assume $g_\nu^{NN}(\mu) = \frac{C_1(\mu) + C_2(\mu)}{2}$
 - Roughly 10% effect for $R_s = 0.6$ fm
 - Uncontrolled error

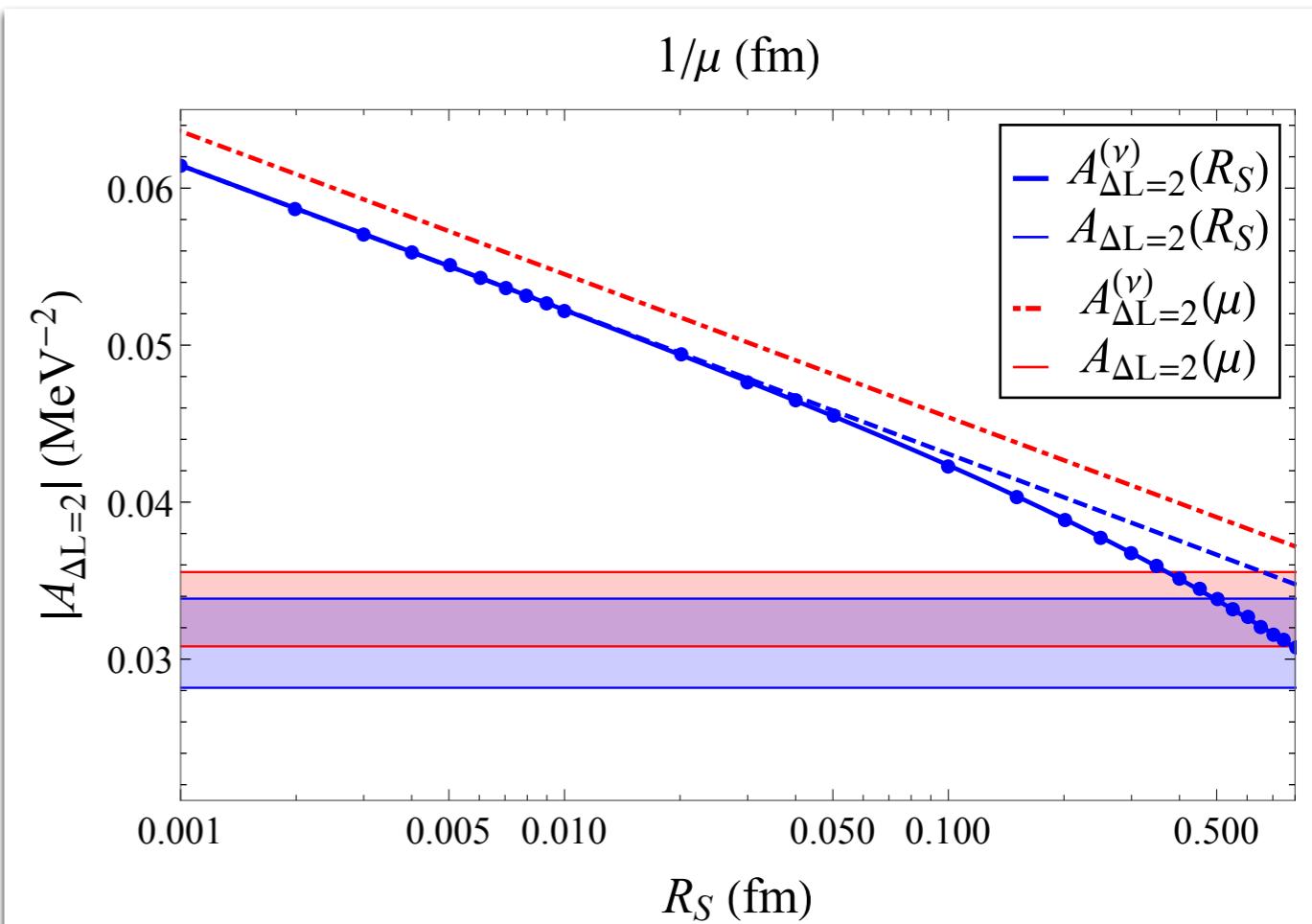
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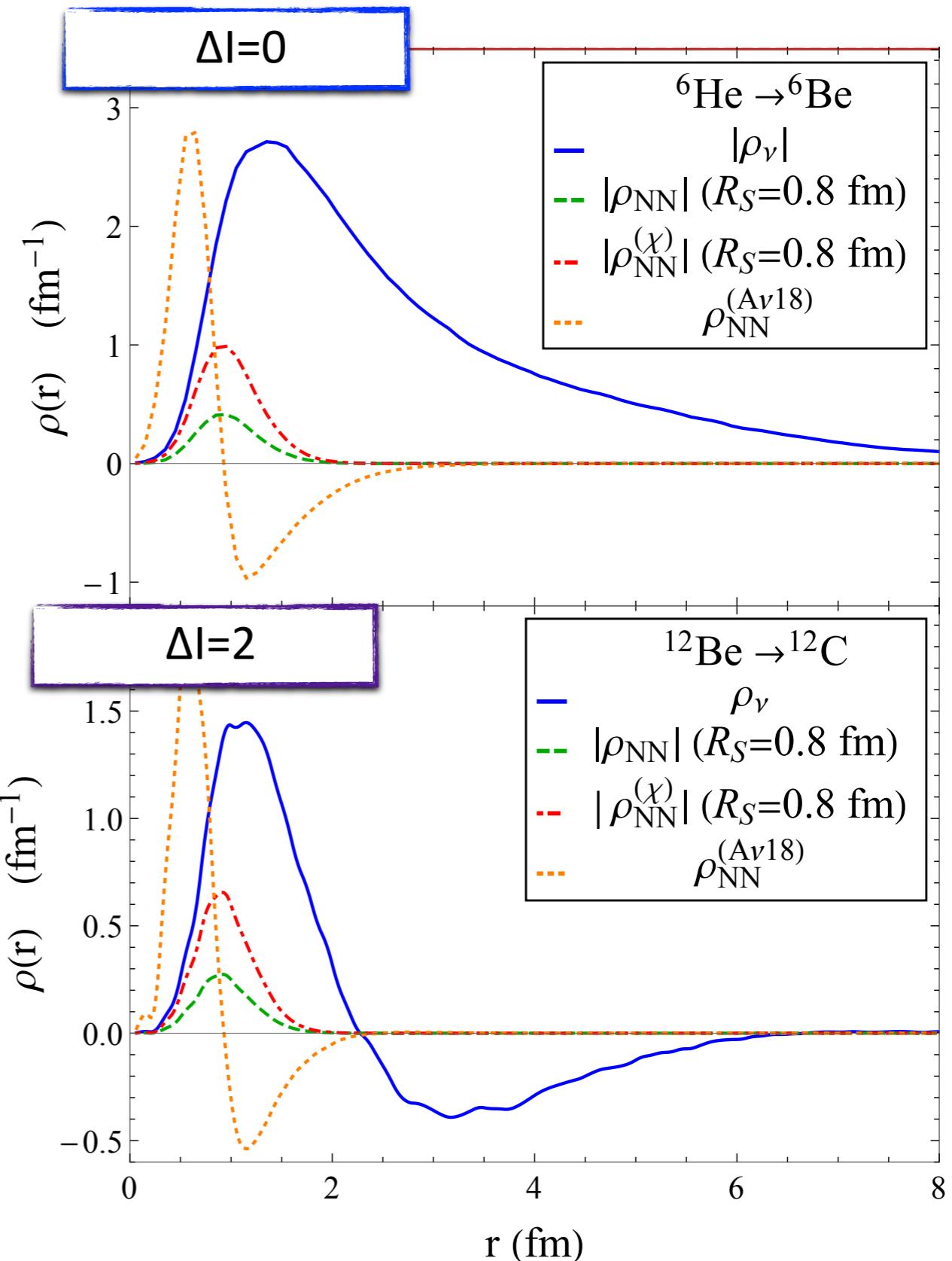
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Estimate of impact

Light nuclei

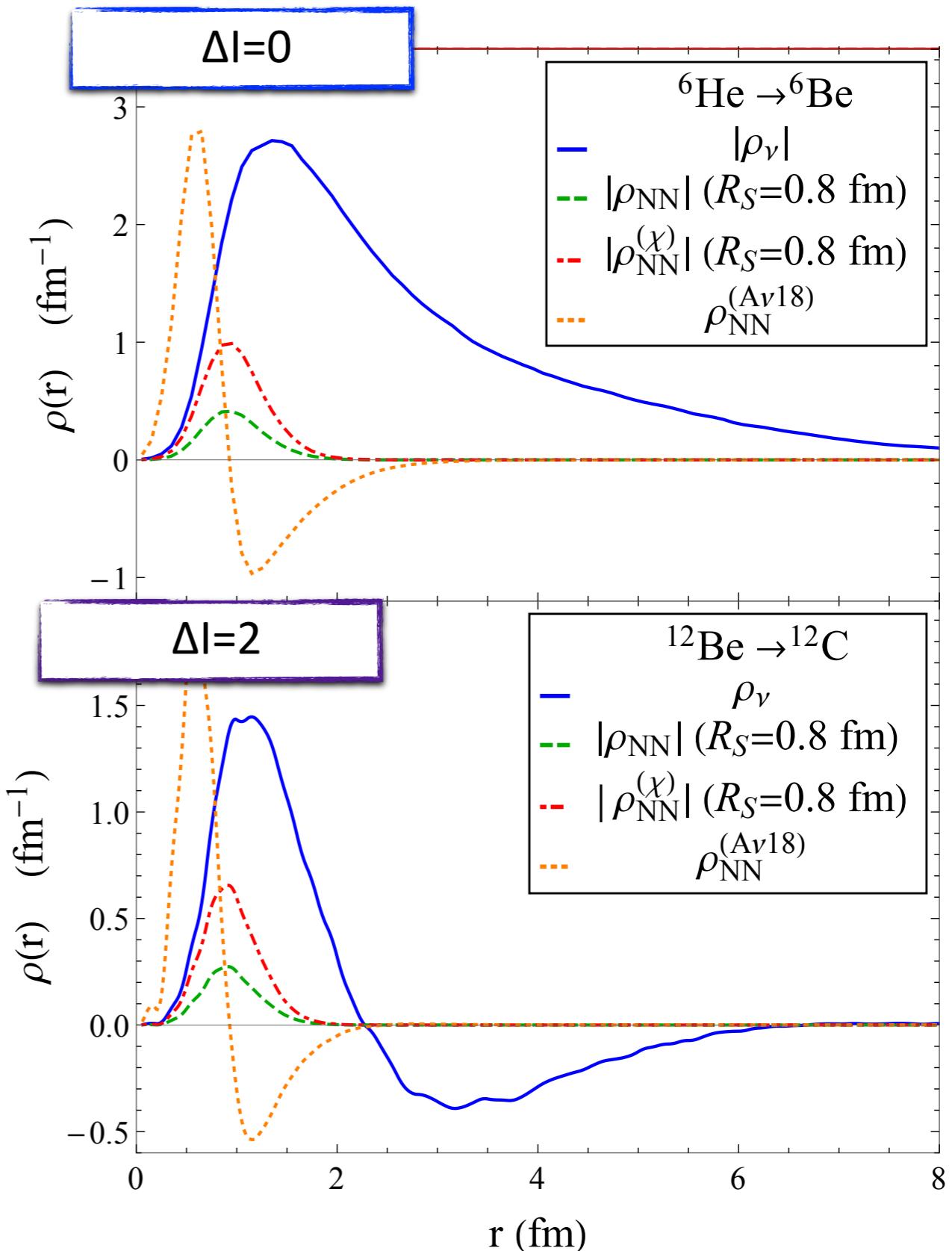
- Use ab initio wavefunctions
R. Wiringa, S. Pastore et. al.
- Estimate of $g_\nu^{NN}(R_S) = \frac{C_1(R_S) + C_2(R_S)}{2}$
 - Extract $C_1 + C_2$ from CIB in NN
 - From Chiral potential
M. Piarulli et. al. '16
- Use short-distance $\Delta l=2$ AV18 potential
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Estimate of impact

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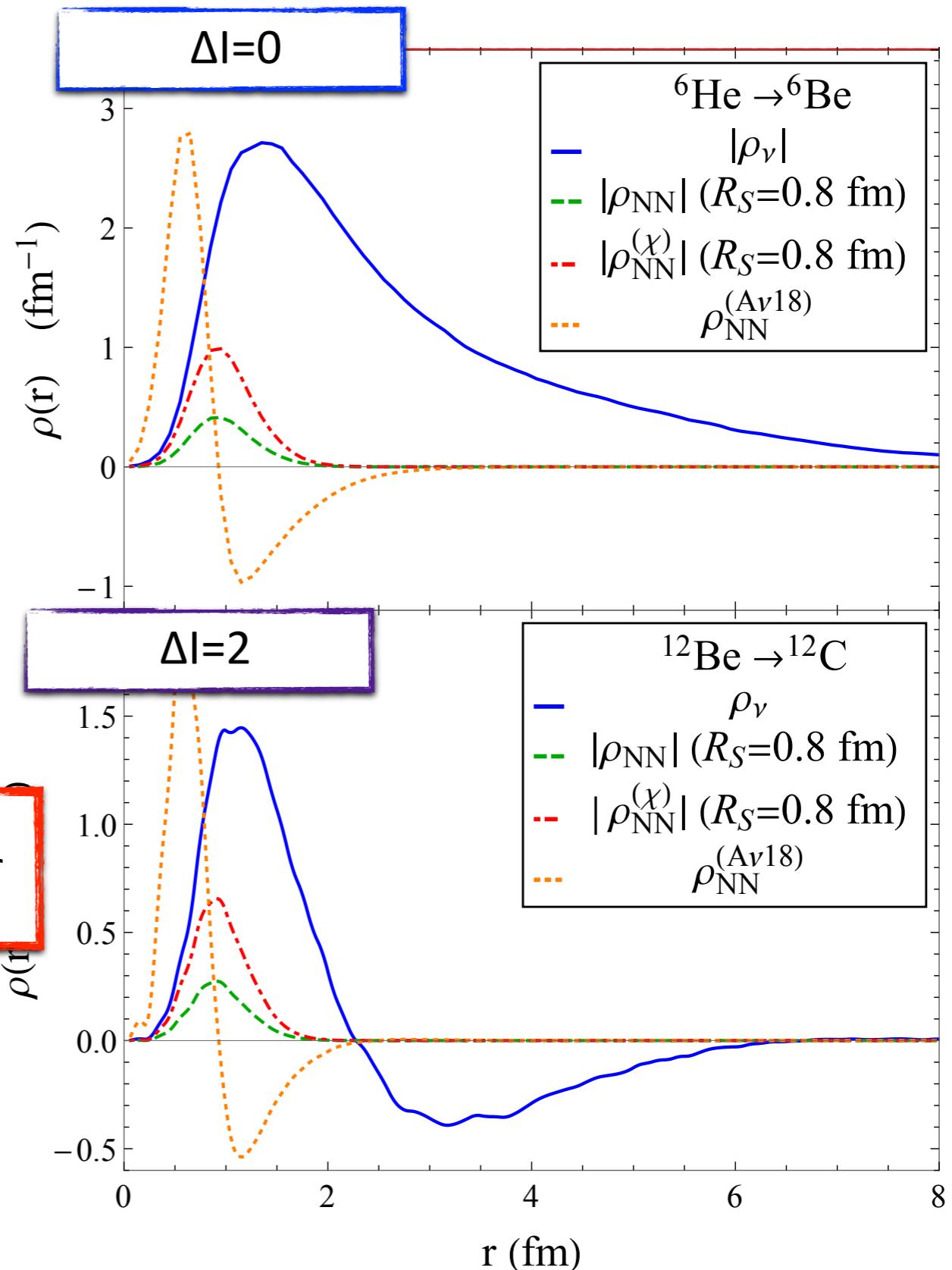
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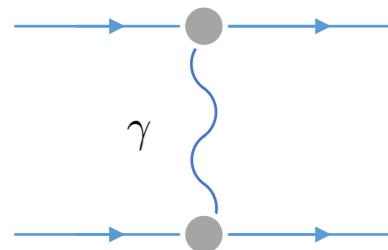
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 - Use short-distance $\Delta l=2$ AV18 potential
R. Wiringa, Stoks, Schiavilla, '95
- 10% effect in ${}^6\text{He} \rightarrow {}^6\text{Be}$
- 25-60% effect in ${}^{12}\text{Be} \rightarrow {}^{12}\text{C}$
 - Due to presence of a node
 - Feature in realistic $0\nu\beta\beta$ candidates



Relation to electromagnetism

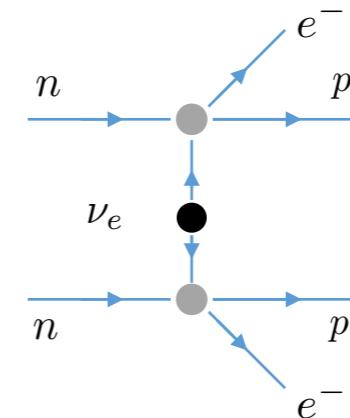
For non-standard cases?

EM



$$\sim e^2/q^2$$

LNV



$$\sim G_F^2 m_{\beta\beta}/q^2$$

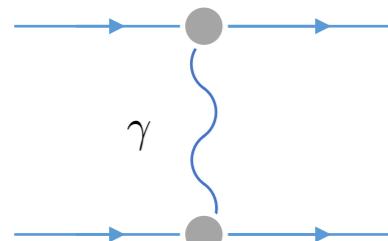


- Relation to Coulomb exchange relies on:
 - $\Delta l=2$ piece of EM having similar chiral properties
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Relation to electromagnetism

For non-standard cases?

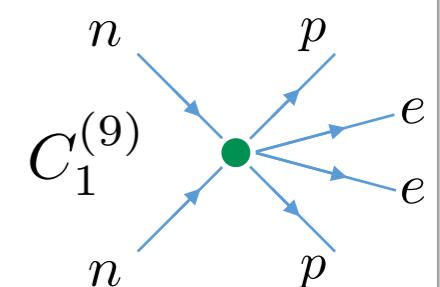
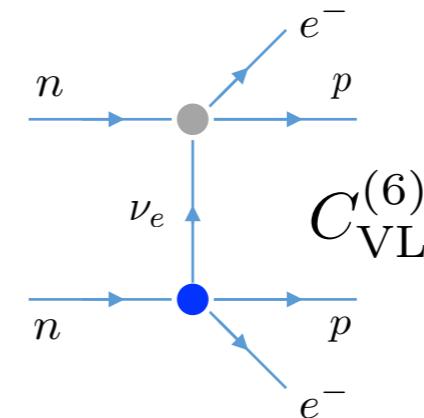
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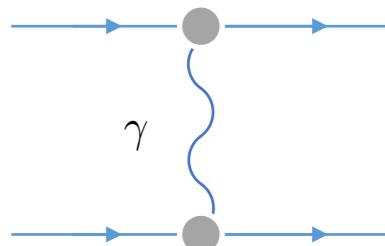
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- Several operators have the right chiral properties: $C_{\text{VL}}^{(6)}$ $C_1^{(9)}$

Relation to electromagnetism

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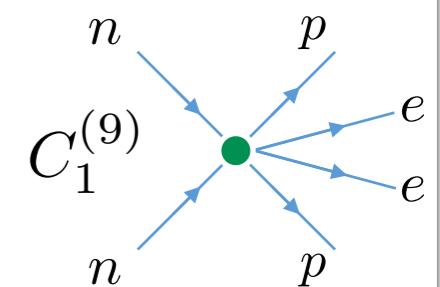
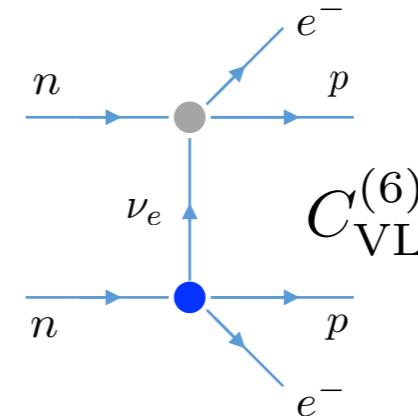
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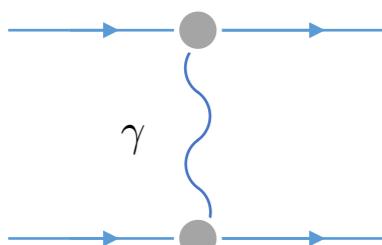
- Several operators have the right chiral properties: $C_{\text{VL}}^{(6)}$ $C_1^{(9)}$

- None of these give a photon propagator
 - $C_1^{(9)}$ Contact ~ 1
 - $C_{\text{VL}}^{(6)}$ Long distance, but wrong structure $\sim q^\alpha/q^2$

Relation to electromagnetism

For non-standard cases?

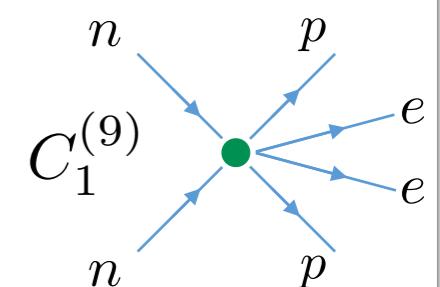
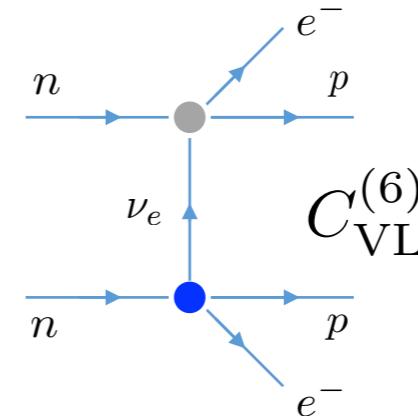
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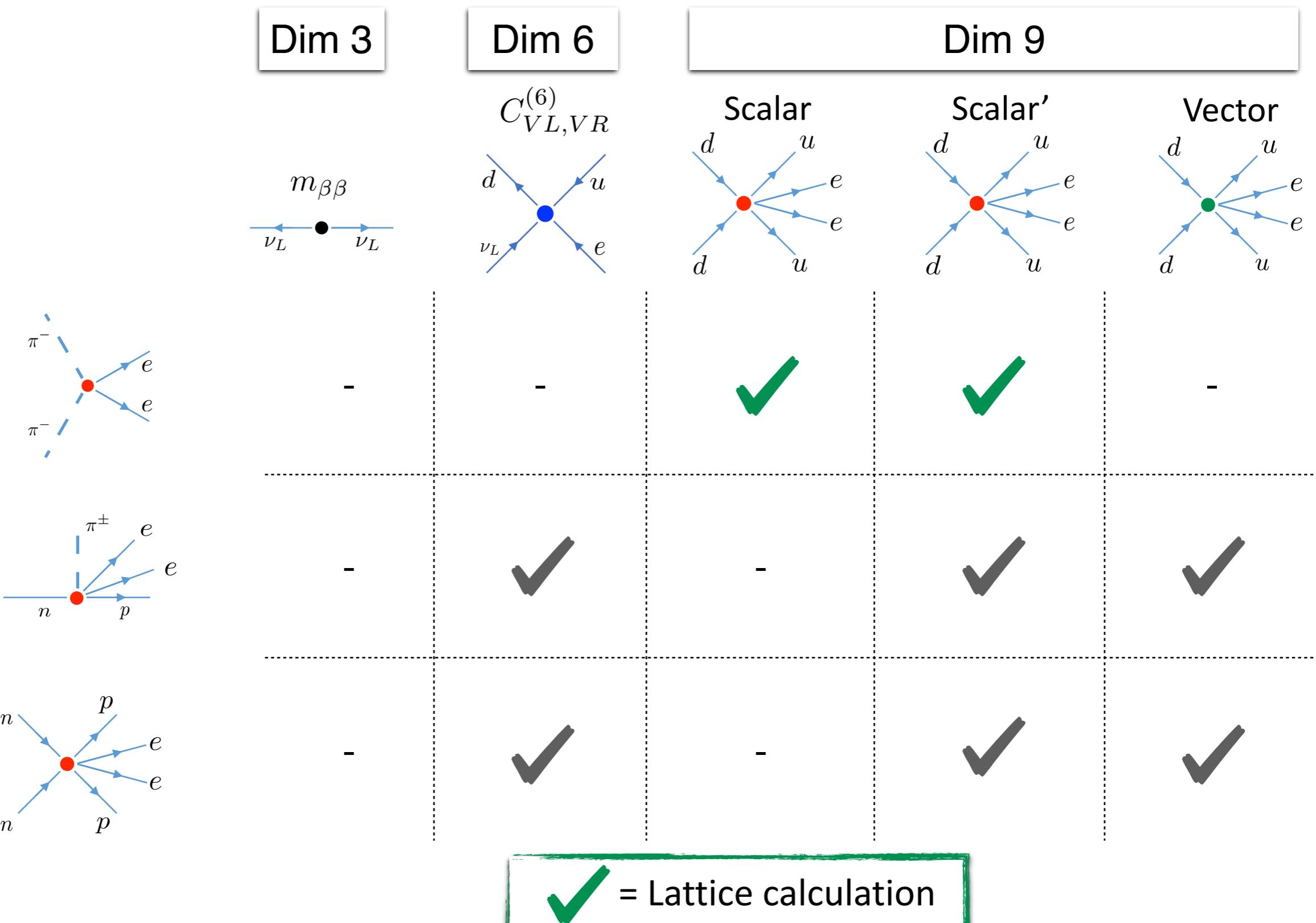
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Short-distance Counterterms

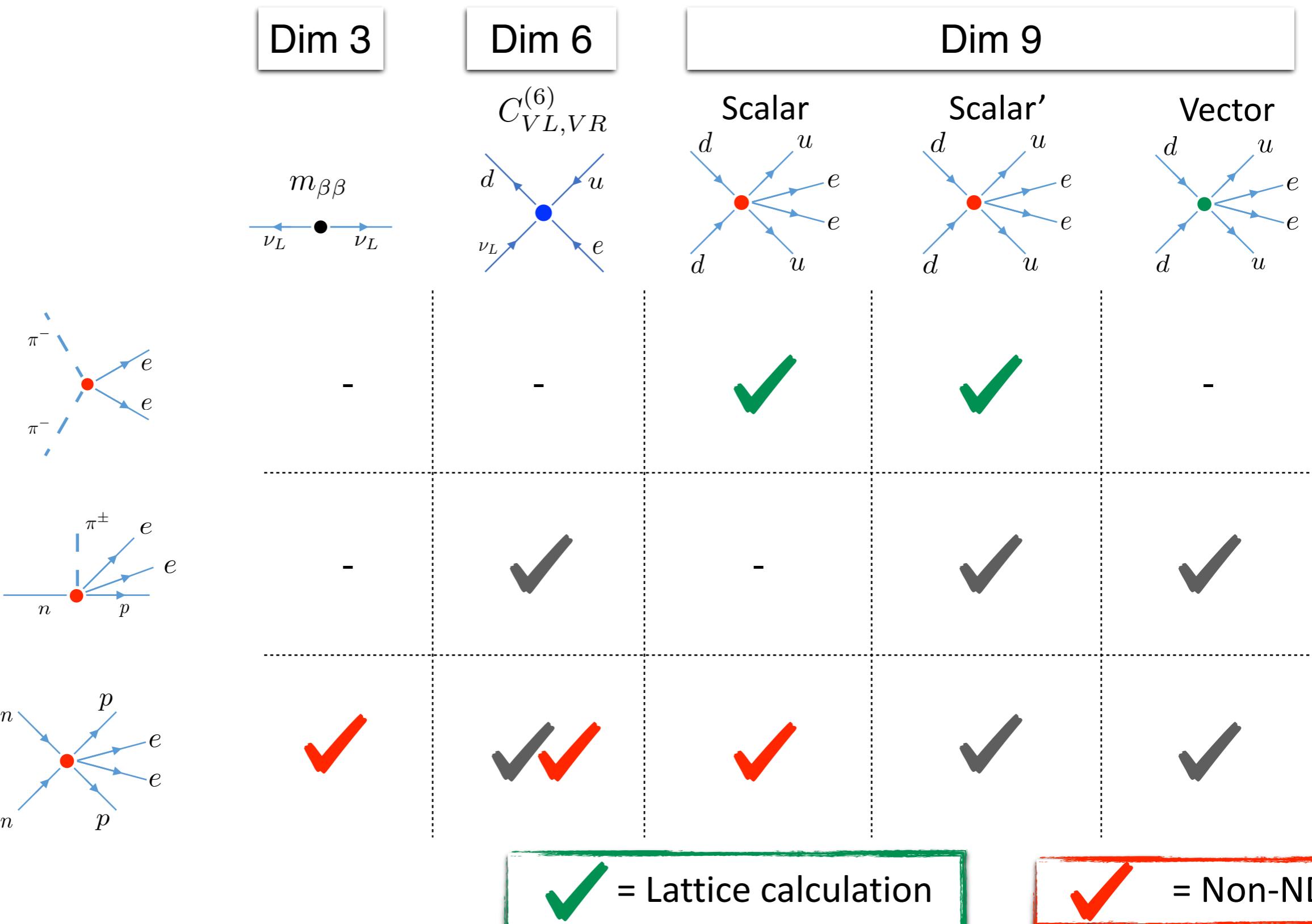
Chiral EFT

Short-range LECs



Chiral EFT

Short-range LECs



Ultrasoft contributions

$0\nu\beta\beta$ operators

Majorana-neutrino mass: N2LO

- N2LO Potential results from integrating out the ‘soft’ and ‘potential’

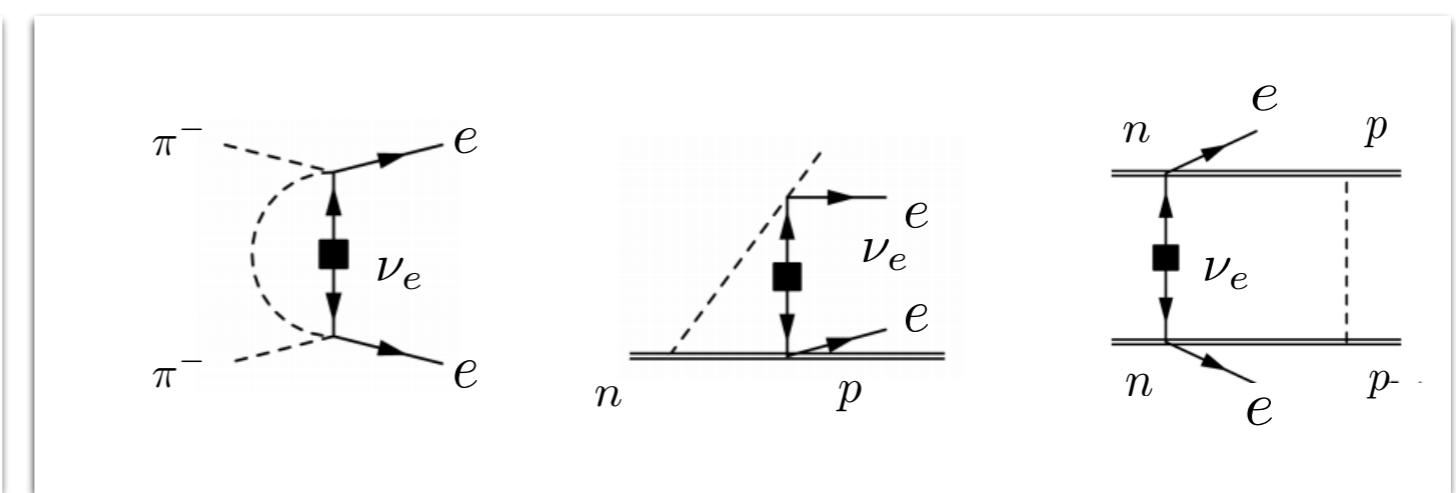
Full ChPT

Degrees of freedom:

Potential ν & π : $q^0 \ll k_F$, $\mathbf{q} \sim k_F$

Soft ν & π : $q^0 \sim \mathbf{q} \sim k_F$

Ultrasoft ν : $q^0 \sim \mathbf{q} \ll k_F$



$0\nu\beta\beta$ operators

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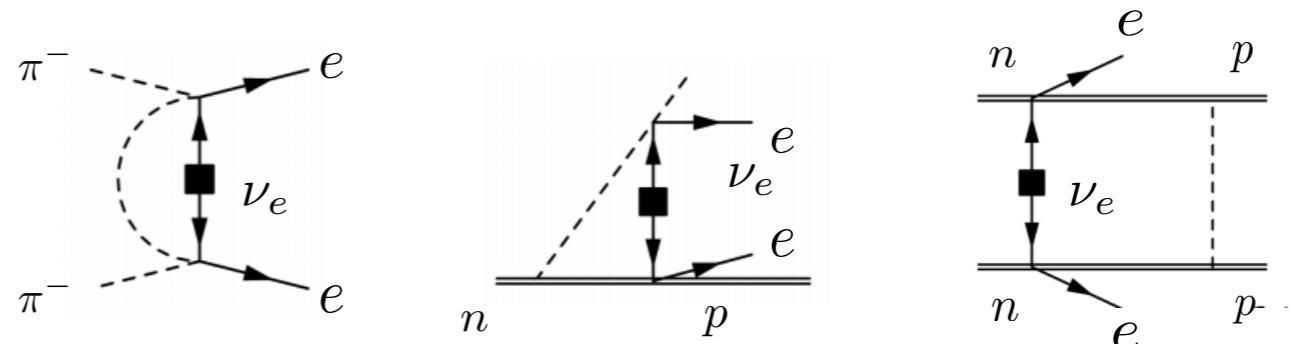
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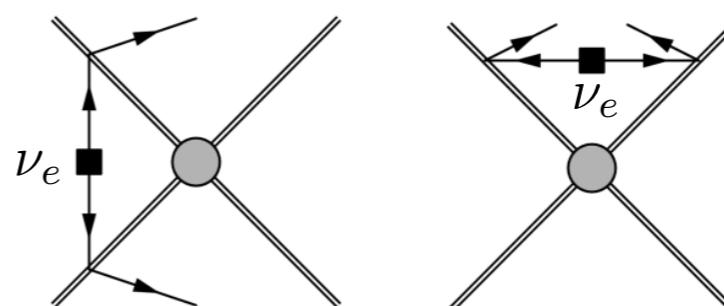
Ultrasoft ν : $q^0 \sim \mathbf{q} \ll k_F$



Low-energy EFT

Degrees of freedom:

Ultrasoft ν : $q^0 \sim \mathbf{q} \ll k_F$



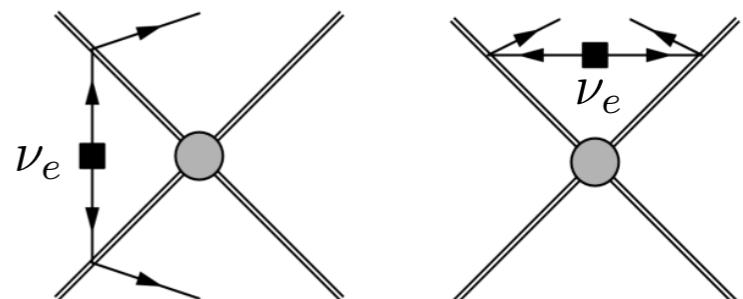
● = leading-order strong potential

$0\nu\beta\beta$ operators

Majorana-neutrino mass: N2LO

$$V_{\nu,2}^{(a,b)} = \tau^{(a)+} \tau^{(b)+} \left(\mathcal{V}_{VV}^{(a,b)} + \mathcal{V}_{AA}^{(a,b)} + \tilde{\mathcal{V}}_{AA}^{(a,b)} \log \frac{m_\pi^2}{\mu_{\text{us}}^2} + \mathcal{V}_{CT}^{(a,b)} \right)$$

- Piece that depends on the renormalization scale
 - Arises from loops with ultrasoft neutrinos
 - What cancels this μ_{us} dependence?



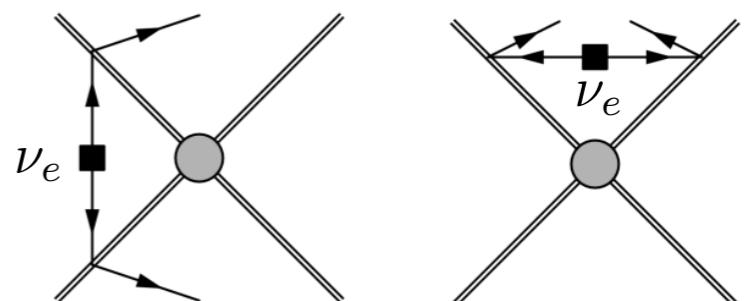
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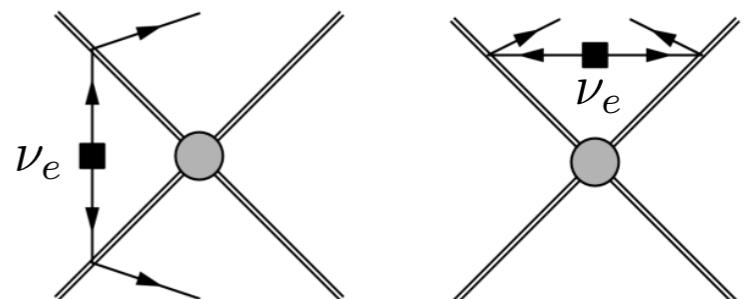
- Still have propagating ultrasoft neutrinos
- Have to add their contributions to the amplitude!

$0\nu\beta\beta$ operators

Majorana-neutrino mass: N2LO

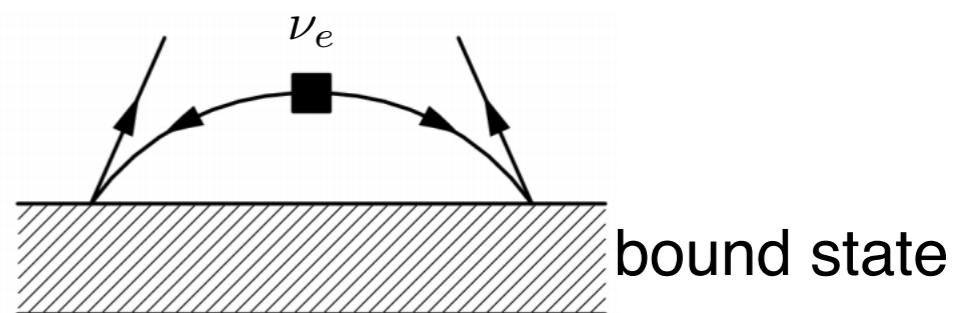
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- Piece that depends on the renormalization scale
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● = leading-order strong potential

- Still have propagating ultrasoft neutrinos
- Have to add their contributions to the amplitude!



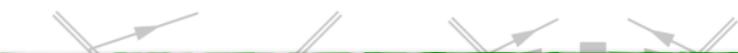
$0\nu\beta\beta$ operators

Majorana-neutrino mass: N2LO

$$V_{\nu,2}^{(a,b)} = \tau^{(a)+} \tau^{(b)+} \left(\mathcal{V}_{VV}^{(a,b)} + \mathcal{V}_{AA}^{(a,b)} + \tilde{\mathcal{V}}_{AA}^{(a,b)} \log \frac{m_\pi^2}{\mu_{\text{us}}^2} + \mathcal{V}_{CT}^{(a,b)} \right) - T'_{\text{usoft}}$$

- Piece that depends on the renormalization scale

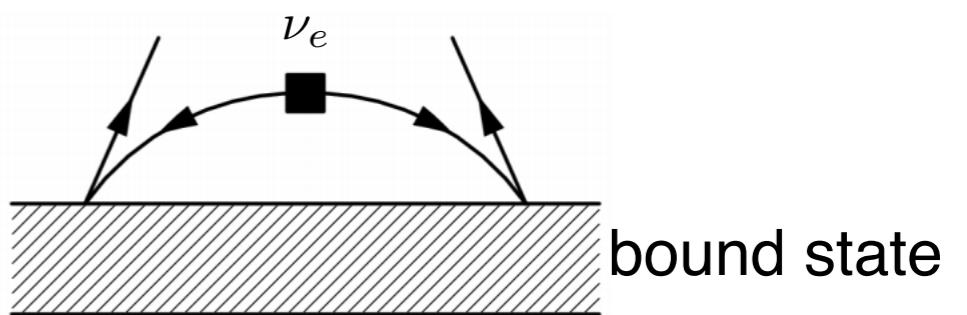
$$T'_{\text{usoft}} = \frac{1}{8\pi^2} \sum_n \langle f | J_\mu | n \rangle \langle n | J^\mu | i \rangle \left\{ (E_2 + E_n - E_i) \left(\log \frac{\mu_{\text{us}}}{2(E_2 + E_n - E_i)} + 1 \right) + (1 \leftrightarrow 2) \right\}$$



○ = leading-order strong potential

- Still have propagating ultrasoft neutrinos
- Have to add their contributions to the amplitude!

- Cancels the μ_{us} dependence of the potential
- Sensitive to the intermediate states
- Same matrix elements as in $2\nu\beta\beta$



bound state

$0\nu\beta\beta$ operators

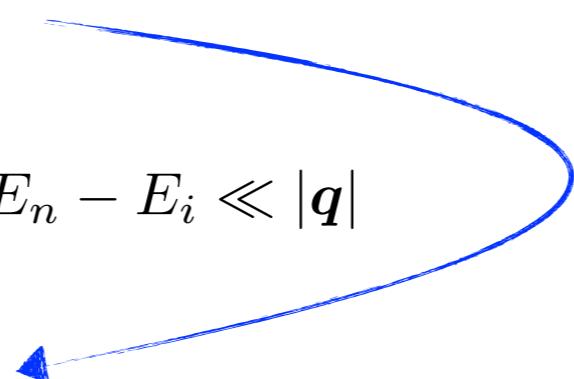
Majorana-neutrino mass: N2LO

- Standard approach
- At leading order
 - Use second order perturbation theory

$$\sum_n \frac{\langle f | J_L^\mu(\mathbf{q}) | n \rangle \langle n | J_L^\nu(-\mathbf{q}) | i \rangle}{|\mathbf{q}|(E_n + |\mathbf{q}| + E_{e2} - E_i)} .$$

- ‘Closure approximation’: $E_n - E_i \ll |\mathbf{q}|$

$$\frac{\langle f | J^\mu(\mathbf{q}) J_\mu(-\mathbf{q}) | i \rangle}{|\mathbf{q}|(|\mathbf{q}| + \bar{E} - (E_i + E_f)/2)}$$



$0\nu\beta\beta$ operators

Majorana-neutrino mass: N2LO

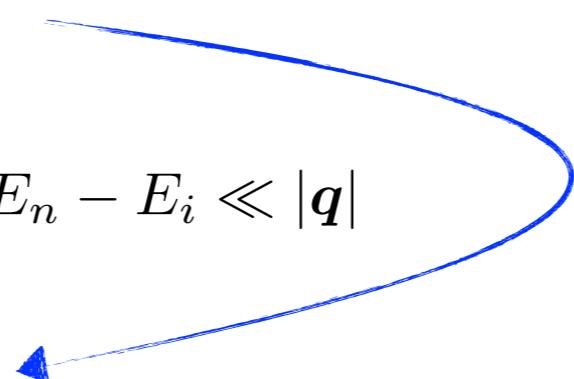
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- Chiral EFT

- At leading order:
 - No intermediate-state dependence
 - Agrees with standard approach for $\bar{E} - (E_i + E_f)/2 \rightarrow 0$

$0\nu\beta\beta$ operators

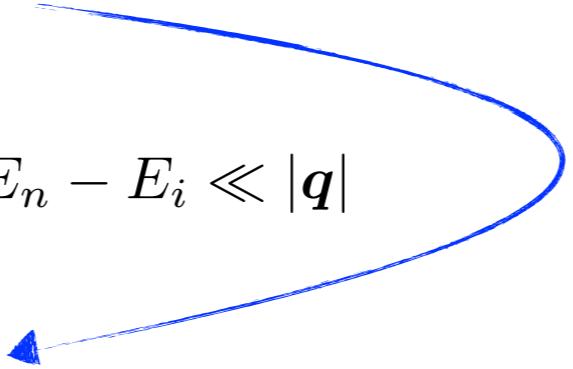
Majorana-neutrino mass: N2LO

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- At N²LO:
 - Include some effects through form factors

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- At N²LO:
 - Form factors

$0\nu\beta\beta$ operators

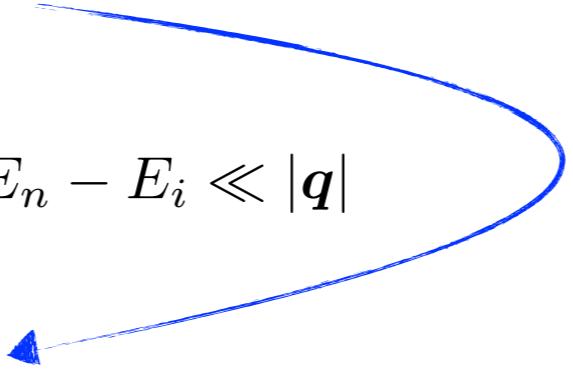
Majorana-neutrino mass: N2LO

- Standard approach

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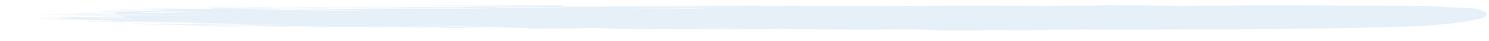
- At N²LO:
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- At N²LO:
 - Form factors
 - Ultrasoft contribution
 - Loops & Counterterms

Disentangling operators



Disentangling operators

What if a $0\nu\beta\beta$ signal is measured?

- Measurement in a single isotope could be due to any operator
- Could measure the rate in several nuclei, however
 - Different isotopes have similar sensitivity to LNV

Disentangling operators

What if a $0\nu\beta\beta$ signal is measured?

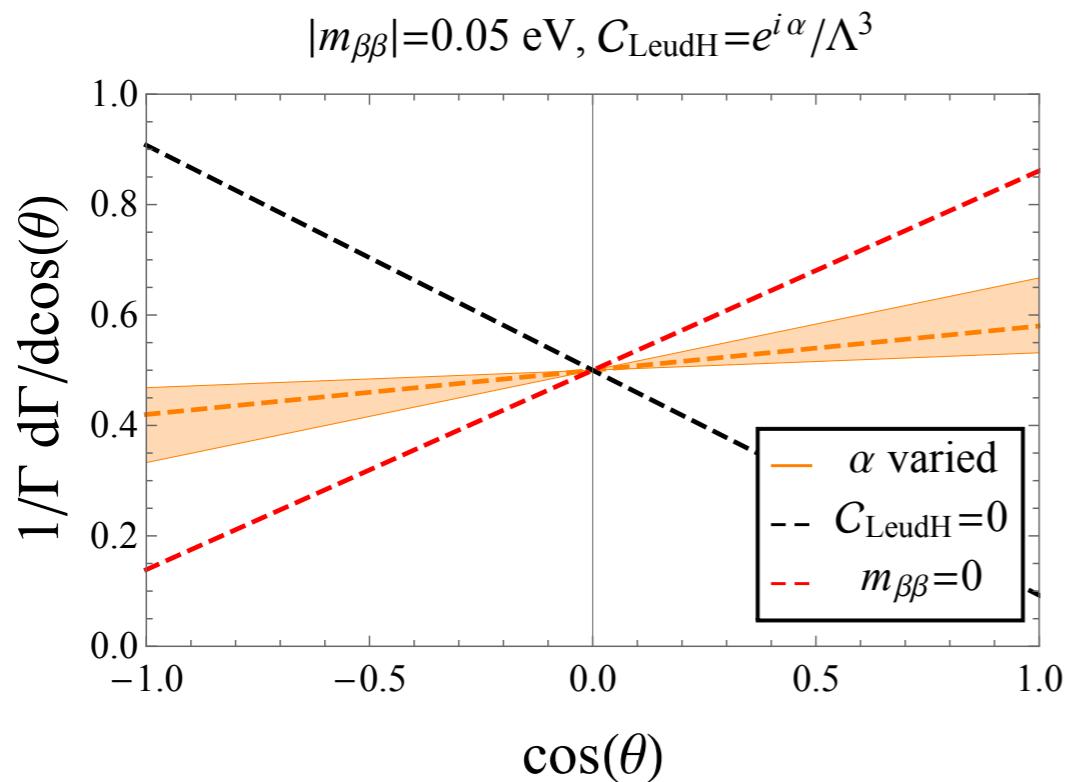
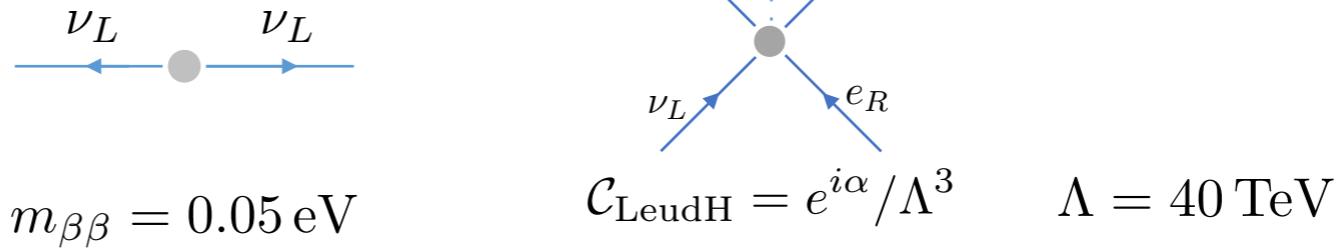
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- Instead look at angular & energy distributions of the

Disentangling operators

What if a $0\nu\beta\beta$ signal is measured?

- Picking the allowed values



Disentangling operators

What if a $0\nu\beta\beta$ signal is measured?

- Picking the allowed values

