

Should neutrino-nucleon cross sections be (re)measured?

Luis Alvarez Ruso

A. H. Blin, K. Graczyk, E. Hernandez, J. Nieves,
E. Saúl Sala, M. J. Vicente Vacas, D. Yao



Introduction

- Do we want new more precise ν -nucleon cross section measurements?
 - Relevant input for ν MC and theoretical models
 - New info about the axial structure of nucleons and other baryons
 - Radiative corrections
 - ChPT LECs, non-pole corrections to Goldberger-Treiman relations
 - New physics (perhaps combining c.s. & lepton/baryon polarization)
 - ...

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 - ...
- ... but who pays for it?



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- Do we NEED new more precise ν -nucleon cross section measurements?
 - Our letter to Santa should be compelling



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- **Do we NEED new more precise ν -nucleon cross section measurements?**
 - Our letter to Santa should be compelling:
 - ν -nucleon cross section should be crucial for future oscillation measurements
 - Experimental projections: c.s. uncertainties \Rightarrow oscillation errors
- **Possible alternatives:**
 - LQCD
 - (Polarized) electron scattering
 - H₂ enriched targets
 - ...

Introduction

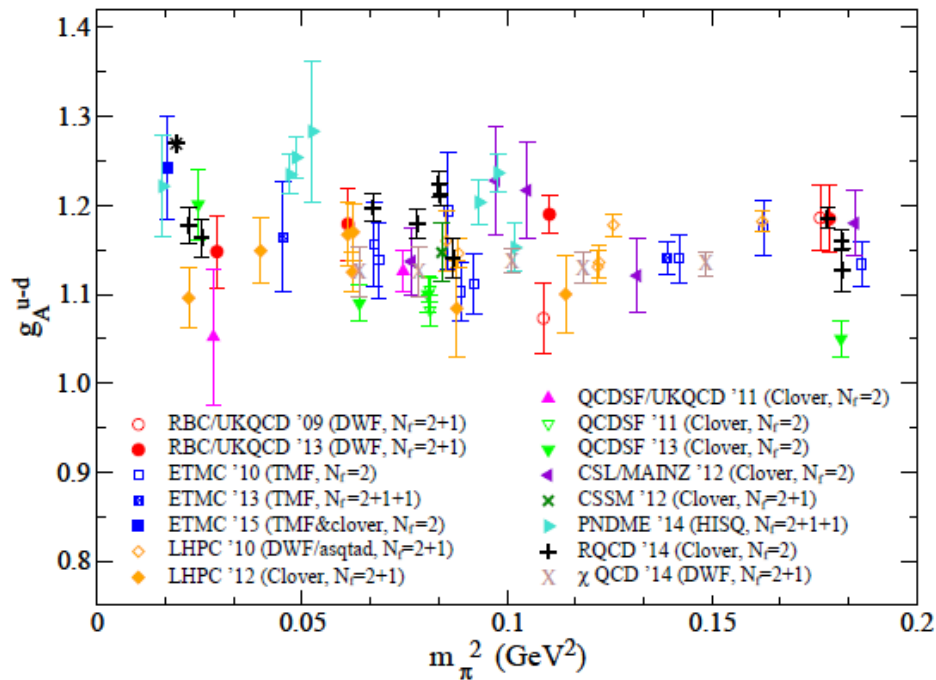
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- Do we NEED new more precise ν -nucleon cross section measurements?
 - Our letter to Santa should be compelling:
 - ν -nucleon cross section should be crucial for future oscillation measurements
 - Experimental projections: c.s. uncertainties \Rightarrow oscillation errors
- It is not just the nucleon $F_A(Q^2)$
- Our ignorance regarding the transition axial N-X ($X=N\pi, N\pi\pi, N K, \dots$) at $Q^2 \neq 0$ is **almost total**
- These processes will be (among) the **largest** at **DUNE**

Outline

- Introduction
- Extraction of F_A from LQCD results using BChPT
- Extraction of F_A from ν -nucleon data using neural networks
- Pion production and resonance excitation

F_A from LQCD

- g_A : lower than exp. values have been recurrently obtained



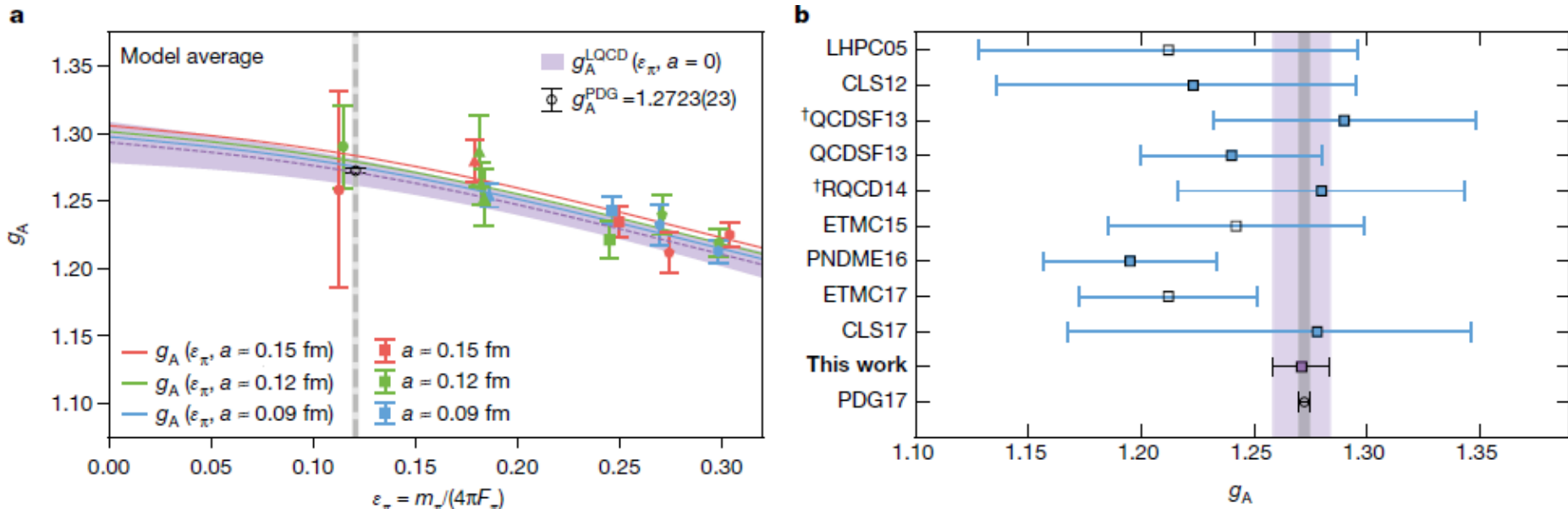
Constantinou, PoS CD15 (2015) 009

F_A from LQCD

- A per-cent-level determination of the nucleon axial coupling from quantum chromodynamics

Chang et al., Nature 558 (2018)

- unconventional method inspired by the Feynman–Hellmann theorem



F_A from LQCD

- Recent determinations of $F_A(Q^2, M_\pi)$:
 - improved algorithms for a careful treatment of **excited states**
 - **low pion masses**

Alexandrou et al., Phys. Rev. D 96 (2017)

Capitani et al., arXiv:1705.06186

Gupta, Phys.Rev. D96 (2017)

F_A in BChPT

$$A_\alpha^a = \bar{u}(p') \left[\gamma_\alpha \gamma_5 F_A + \frac{q_\alpha}{m_N} \gamma_5 F_P \right] \frac{\tau^a}{2} u(p)$$

- $F_A(Q^2, M_\pi)$ calculated using **covariant** ChPT
Yao, LAR, Vicente Vacas, PRD 96 (2017)
- up to leading one-loop $O(p^3)$
 - standard power counting
- with **explicit** $\Delta(1232)$
 - $\delta = m_\Delta - m_N \sim O(p)$
- **Power-counting breaking** (PCB) terms:
 - because of N, Δ with masses that **do not vanish in the χ limit**
 - **EOMS** (Extended on mass shell) scheme Gegelia & Scherer
 - PCB terms absorbed by low-energy constants (**LEC**)
 - Covariance and analytic properties of loops preserved.

F_A in BChPT

- Example: nucleon mass in SU(2)

$$O(p) \quad \mathcal{L}_1 = -\bar{\psi} M_0 \psi + \dots \quad M = M_0$$

$$O(p^2) \quad \mathcal{L}_2 = 4c_1 m_\pi^2 \bar{\psi} \psi + \dots \quad M = M_0 - 4c_1 m_\pi^2$$

$$O(p^3) \quad \text{Loops} \quad M = M_0 - 4c_1 m_\pi^2 + \frac{1}{16\pi^2} \left(\frac{g_A}{f_\pi} \right)^2 m_\pi^2 M_0 + \dots$$

$O(p^2)$!



$$\text{EOMS:} \quad c_1 \rightarrow c_1 + \frac{1}{64\pi^2} \left(\frac{g_A}{f_\pi} \right)^2 M_0$$

F_A in BChPT

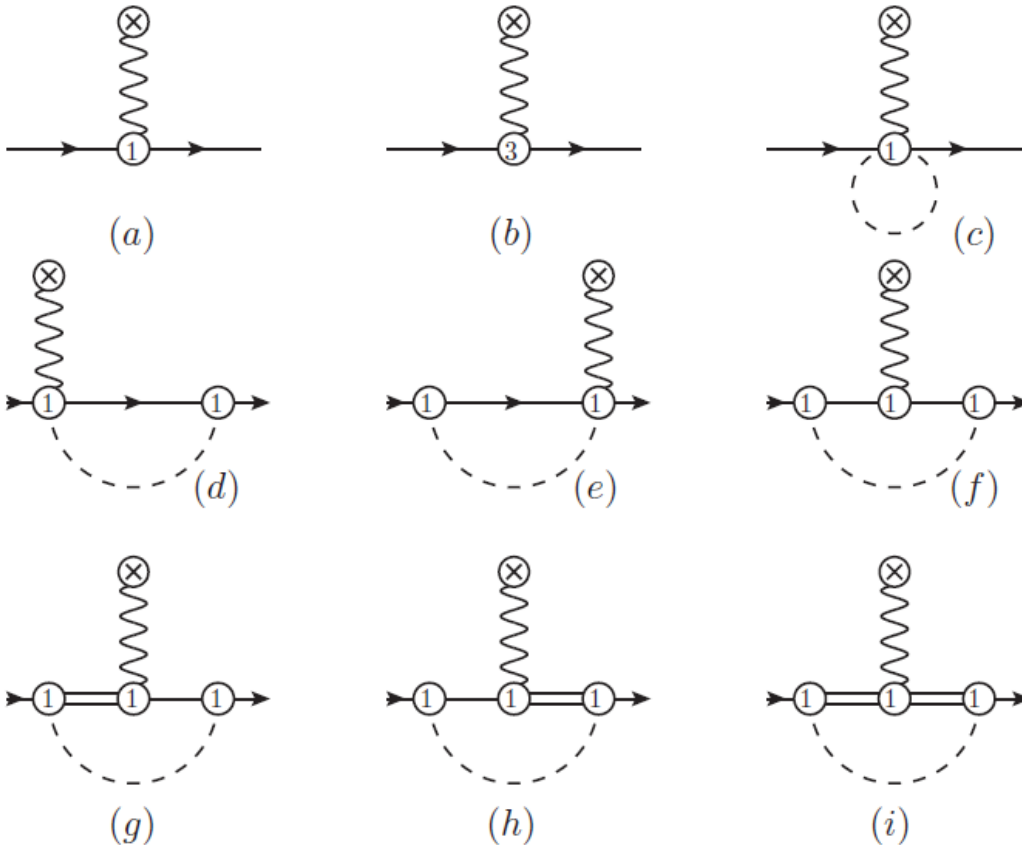
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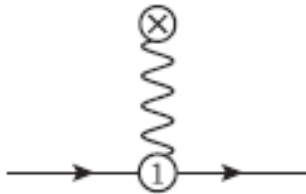
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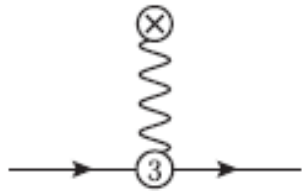
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$$\mathcal{L}_{\pi N}^{(1)} \supset \bar{\Psi} \left(\frac{1}{2} g u^\mu \gamma_\mu \gamma_5 \right) \Psi ,$$

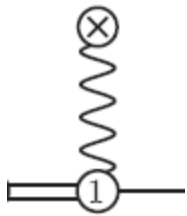


$$\mathcal{L}_{\pi N}^{(3)} \supset \bar{\Psi} \left\{ \frac{d_{16}}{2} \gamma^\mu \gamma_5 \langle \chi_+ \rangle u_\mu + \frac{d_{22}}{2} \gamma^\mu \gamma_5 [D_\nu, F_{\mu\nu}^-] \right\} \Psi ,$$

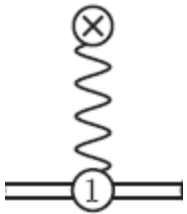
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$$\mathcal{L}_{\pi N \Delta}^{(1)} = h_A \bar{\Psi}_\mu^i \xi_{ij}^{\frac{3}{2}} \omega^{\mu,j} \Psi + h.c.$$

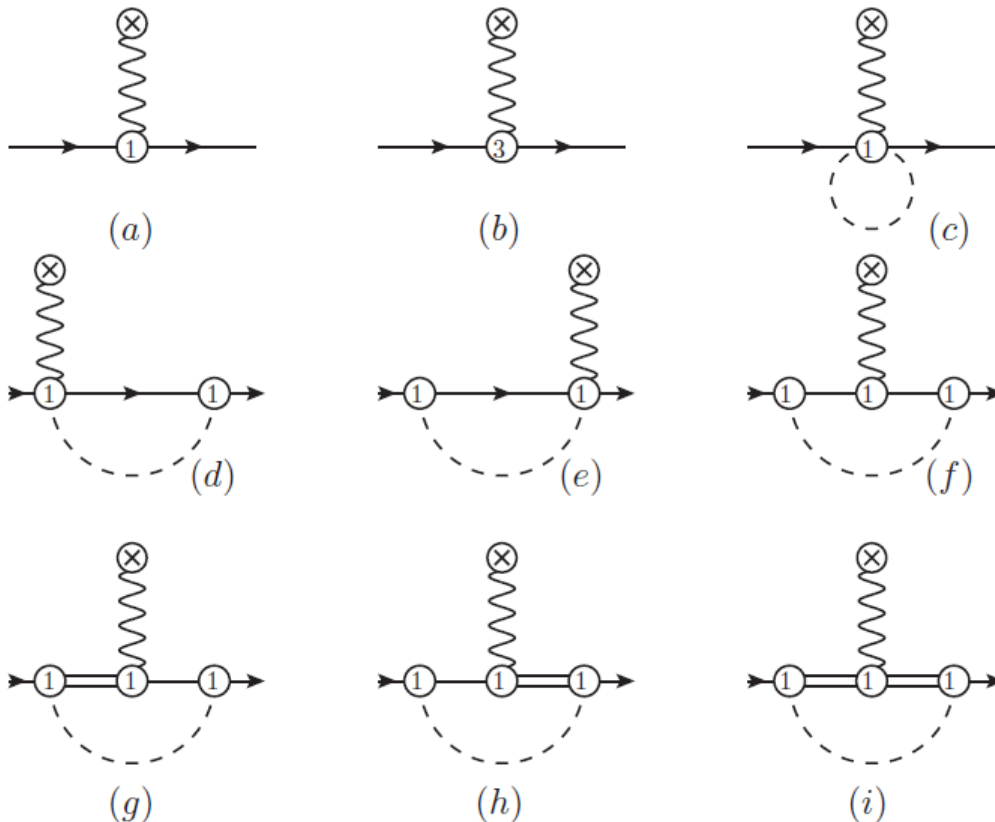


$$\mathcal{L}_{\pi \Delta}^{(1)} \supset -\bar{\Psi}_\mu^i \xi_{ij}^{\frac{3}{2}} \left\{ \frac{g_1}{2} \psi^{jk} \gamma_5 g^{\mu\nu} \right\} \xi_{kl}^{\frac{3}{2}} \Psi_\nu^l$$

- h_A , g_1 fixed in πN scattering Yao et al., JHEP 05 (2016)

F_A in BChPT

- $F_A(Q^2, M_\pi)$ calculated in **covariant** ChPT up to $O(p^3)$ with **explicit** $\Delta(1232)$
 Yao, LAR, Vicente Vacas, PRD 96 (2017)



$$F_A(Q^2, M_\pi^2) = g + 4d_{16}M_\pi^2 + d_{22}Q^2 + F_A^{(c)} + F_A^{(f)} + 2F_A^{(g)} + F_A^{(i)} + F_A^{(wf)}$$

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- g, d_{16}, d_{22} are determined from a **fit** to **LQCD data** in **both Q^2 and M_π**
Alexandrou et al., Phys. Rev. D 96 (2017)
Capitani et al., arXiv:1705.06186
Gupta, Phys.Rev. D96 (2017)

- **Fit range:**

- $M_\pi < ???$

- $Q^2 < ???$

- **Explicit** or **implicit $\Delta(1232)$?**

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Gupta, Phys.Rev. D96 (2017)

- **Fit range:**

- $M_\pi < 400$ MeV
 - reasonable
 - **LQCD ensembles** with $M_\pi > 400$ MeV **increase χ^2**
- $Q^2 < ???$

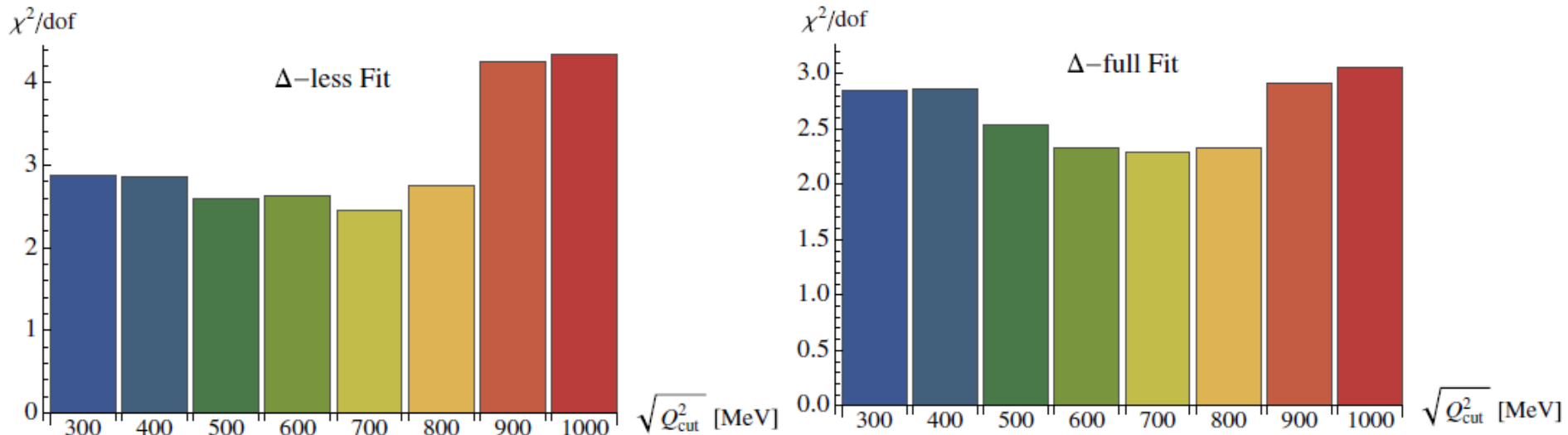
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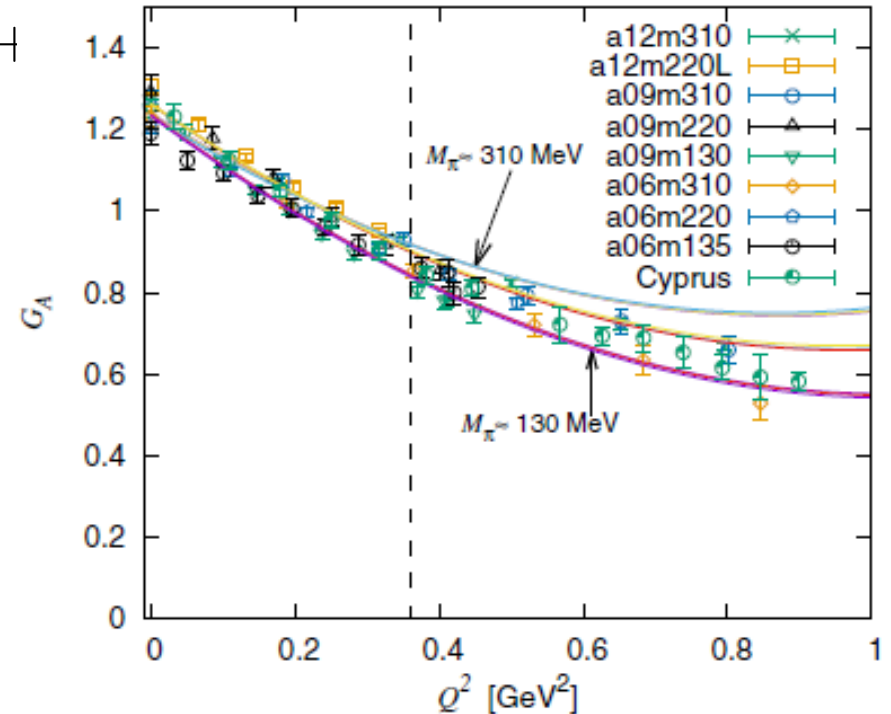
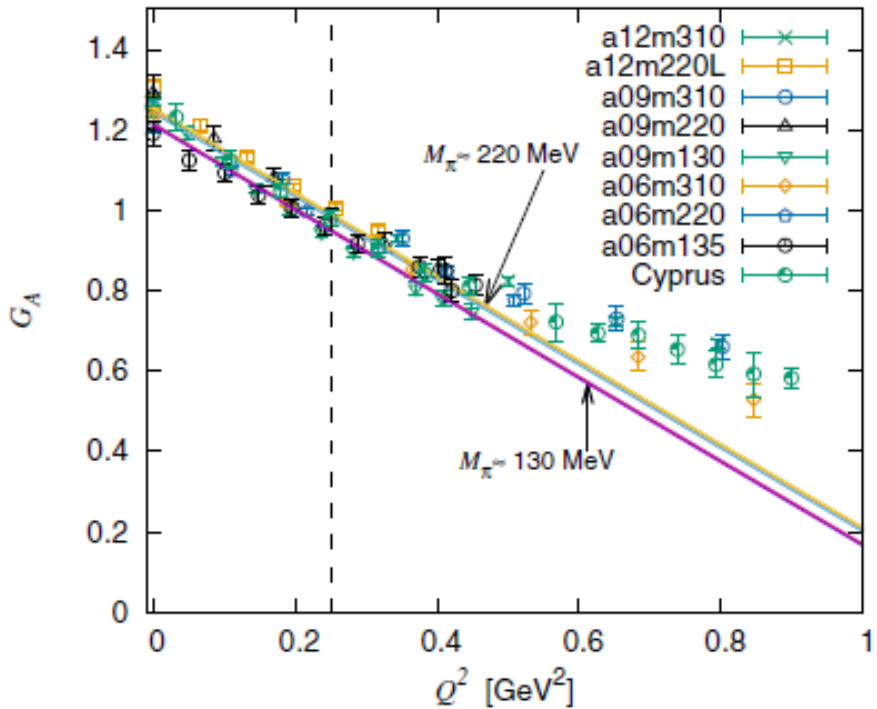
■ $Q^2 < 0.25$ (0.36) GeV^2

- **Explicit $\Delta(1232)$**

■ better χ^2/dof

F_A in BChPT

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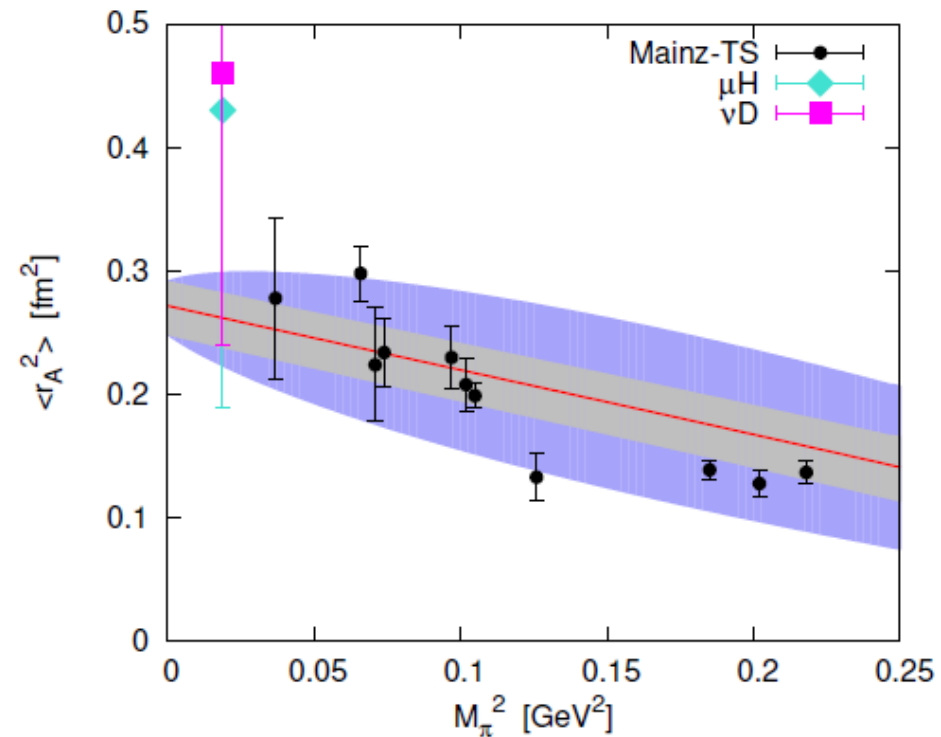
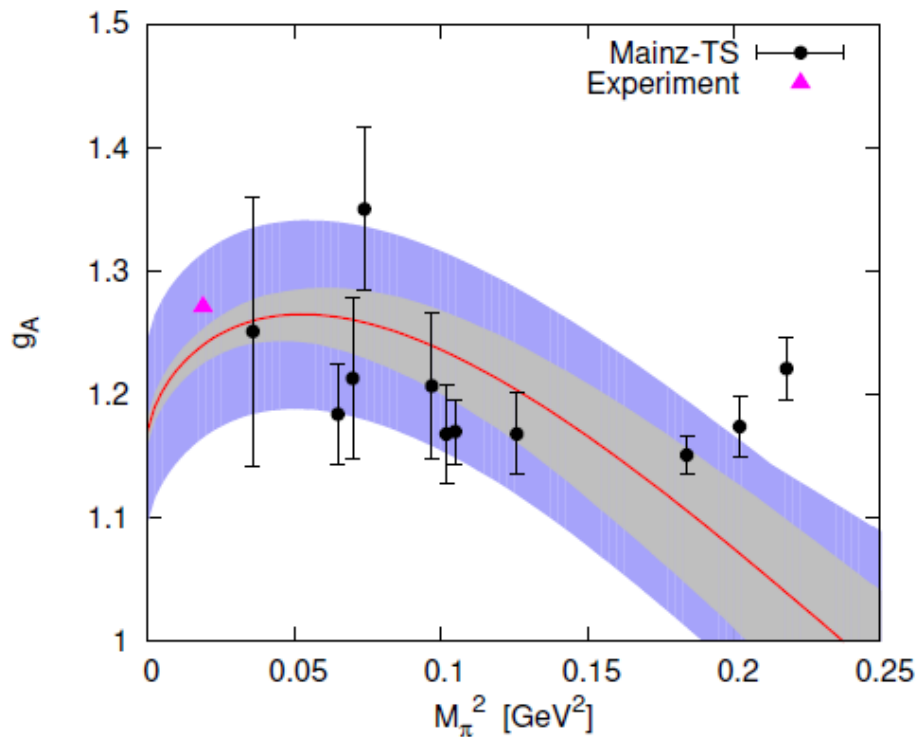
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F_A & LQCD

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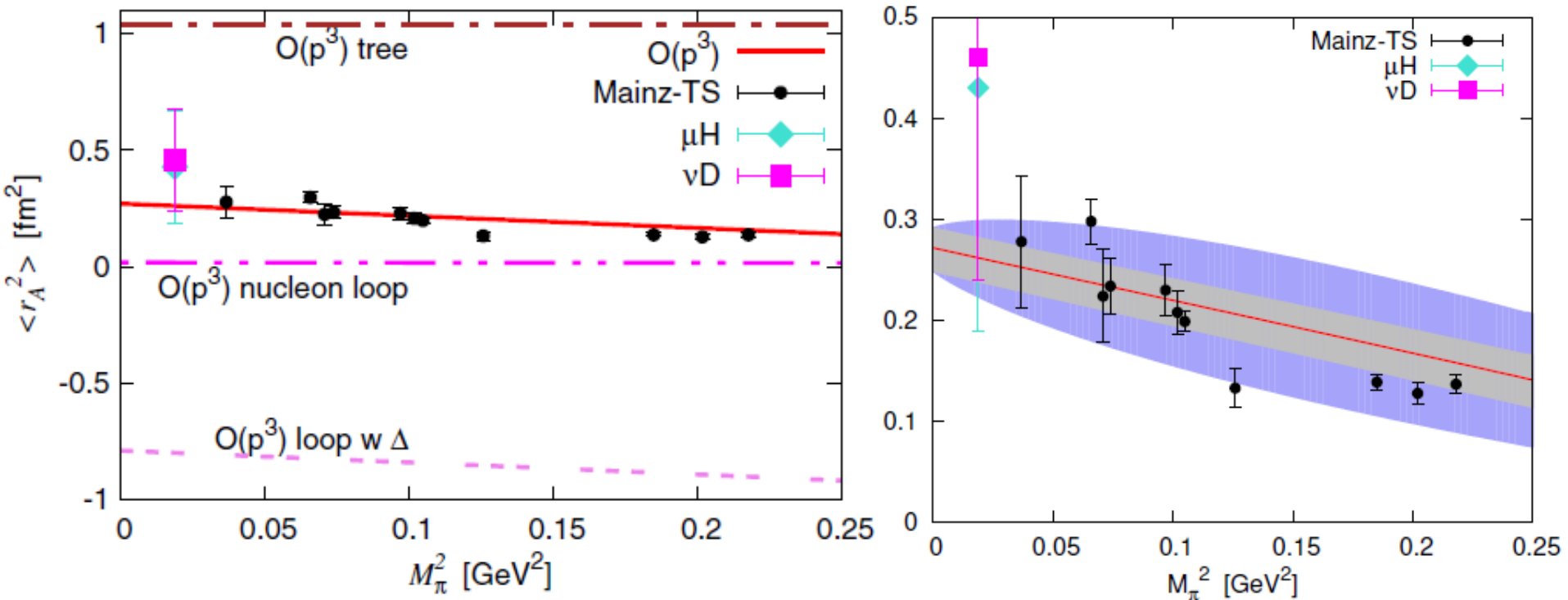


- At the **physical point**: $g_A = 1.237(74)$, $\langle r_A^2 \rangle = 0.263(38)$ fm²
- Mainz-TS points: z-expansion results from **Capitani et al.**, [arXiv:1705.06186](https://arxiv.org/abs/1705.06186), **not used in the fit.**

F_A & LQCD

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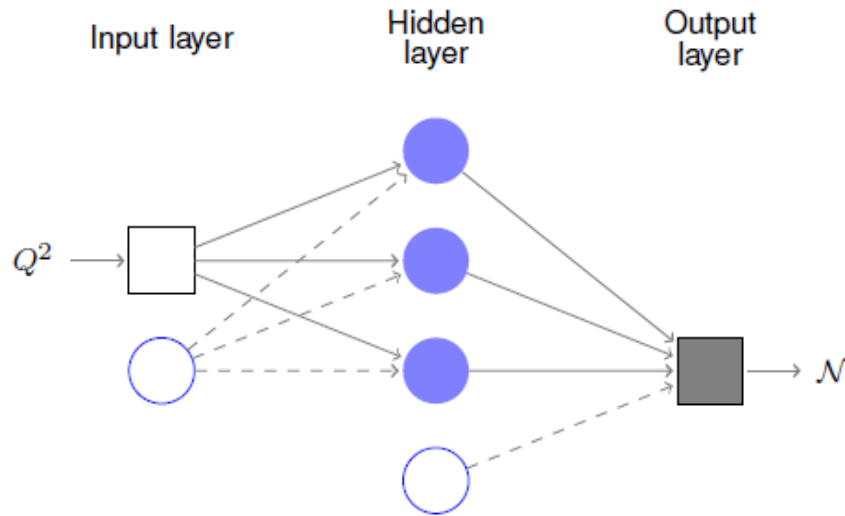
Yao, LAR, Vicente Vacas, PRD 96 (2017)



- At the **physical point**: $g_A = 1.237(74)$, $\langle r_A^2 \rangle = 0.263(38)$ fm²
- Loops with $\Delta(1232)$ significantly improve $\langle r_A^2 \rangle$
- $O(p^5)$ might be needed to improve M_π dependence of $\langle r_A^2 \rangle$

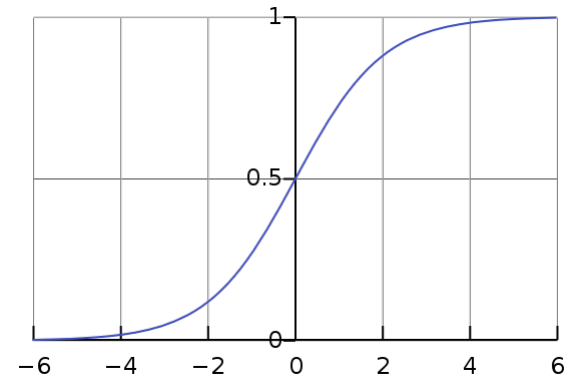
Neural Networks for F_A

- Feed-forward NN in multilayer perceptron (MLP) configurations
- Non-linear map $\mathcal{N}: \mathbb{R}^{\text{in}} \rightarrow \mathbb{R}^{\text{out}}$



- For every unit: $y = f_{\text{act}} \left(\sum_{i \in \text{prev. layer}} w_i y_i \right)$

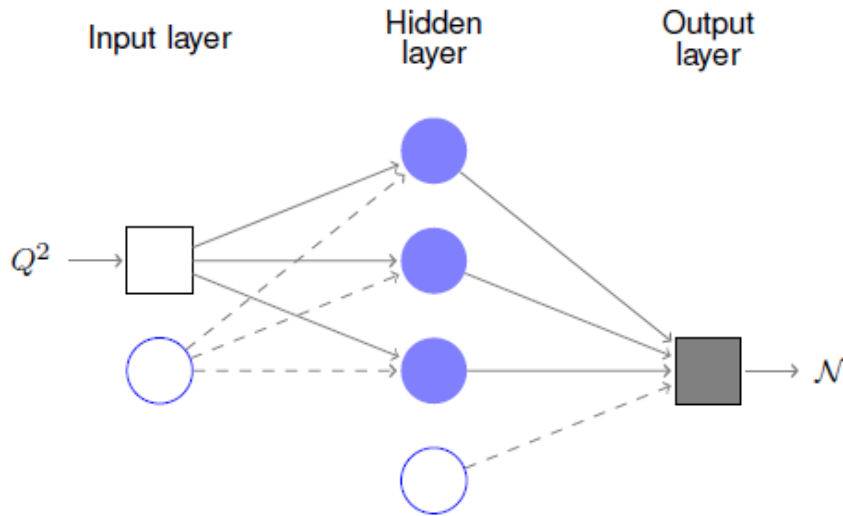
- Activation function: $f(x) = \frac{1}{1 + \exp(-x)}$



- except in bias units: $f(x) = 1$ and output: $f(x) = x$

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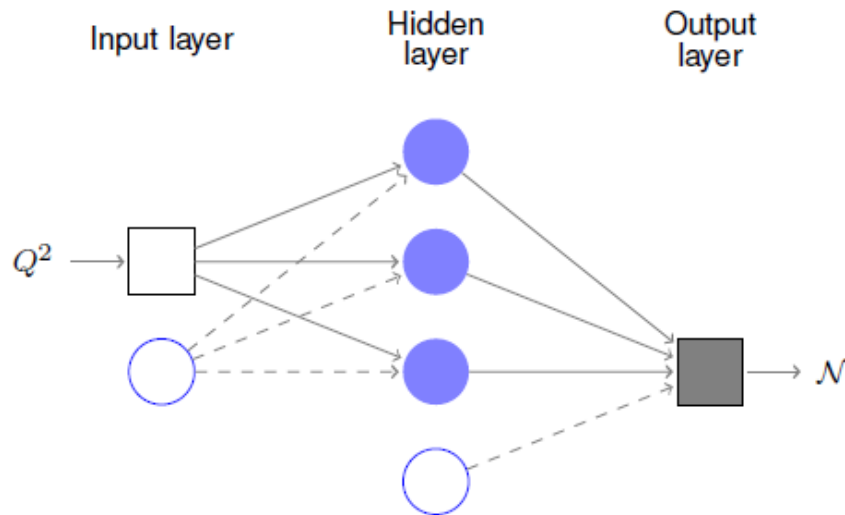
$$\mathcal{N}_M(Q^2; \{w_j\}) = \sum_{n=1}^M w_{2M+n} f(w_n Q^2 + w_{M+n}) + w_{3M+1}.$$

$$F_A(Q^2) = F_A^{\text{dipole}}(Q^2) \times \mathcal{N}_M(Q^2; \{w_i\}) \leftarrow \text{function of } W=3M+1 \text{ weights and } Q^2$$

- Cybenko's theorem: for large enough M , can map arbitrarily well any continuous function and its derivative

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- Bayesian inference to **train the network, avoiding overfitting**

Bayesian inference for NN

$$\text{posterior} = \frac{\text{likelihood} \times \text{prior}}{\text{evidence}}$$

1. For a given \mathcal{N} : $\mathcal{P}(\{w_j\} | \mathcal{D}, \mathcal{N}) = \frac{\mathcal{P}(\mathcal{D} | \{w_j\}, \mathcal{N})\mathcal{P}(\{w_j\} | \mathcal{N})}{\mathcal{P}(\mathcal{D} | \mathcal{N})}$,

- Likelihood in terms of χ^2 :

$$\mathcal{P}(\mathcal{D} | \{w_j\}, \mathcal{N}) = \frac{1}{N_L} \exp(-\chi^2)$$

- Prior: weights w_j are Gaussian distributed

$$\mathcal{P}(\{w_j\}, \mathcal{N}) = \frac{1}{N_w} \exp\left(-\alpha \frac{1}{2} \sum_{i=1}^W w_i^2\right) \quad \alpha \leftarrow \text{regularizer}$$

- Algorithm to find the optimal: $(\{w_j\}_{MP}, \alpha_{MP})$

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2. For \mathcal{N}_{1-M} : $\mathcal{P}(\mathcal{N} | \mathcal{D}) = \frac{\mathcal{P}(\mathcal{D} | \mathcal{N})\mathcal{P}(\mathcal{N})}{\mathcal{P}(\mathcal{D})}$

- Assuming all NN configurations are equally suited to describe data:

$$\mathcal{P}(\mathcal{N}_1) = \mathcal{P}(\mathcal{N}_2) = \dots = \mathcal{P}(\mathcal{N}_M) \quad \text{then} \quad \mathcal{P}(\mathcal{N} | \mathcal{D}) \propto \mathcal{P}(\mathcal{D} | \mathcal{N})$$

- In the Hessian approximation:

$$\mathcal{P}(\mathcal{D} | \mathcal{N}) = \int dw_1 \cdots dw_W \mathcal{P}(\mathcal{D} | \{w_j\}, \mathcal{N}) \mathcal{P}(\{w_j\} | \mathcal{N})$$

$$\ln \mathcal{P}(\mathcal{D} | \mathcal{N}) \approx -\chi^2 - \alpha_{MP} \frac{1}{2} \sum_{i=1}^W \{w_i\}_{MP}^2 - (\text{Occam's factor})$$

large for models with many parameters

Bayesian inference in hadronic and nuclear physics

- Resonance content of $\gamma p \rightarrow K^+ \Lambda$
De Cruz et al., PRL 108 (2012)
- Uncertainty Quantification in Nuclear Density Functional Theory
McDonnell et al., PRL 114 (2015)
- Halo effective field theories
Zhang et al., PLB 751 (2015)

- Bayesian neural-network analysis
 - Parametrization of EM nucleon form factors
Graczyk et al., JHEP 1009 (2010)
 - Proton radius
Graczyk & Juszczak, PRC 90 (2014)

 - Nucleon axial form factor from new ν -nucleon data
LAR, Graczyk, Saúl-Sala, arXiv:1805.00905

Bayesian inference in hadronic and nuclear physics

ional Theory



- Nucleon axial form factor from ~~new ν -nucleon data~~ ANL data

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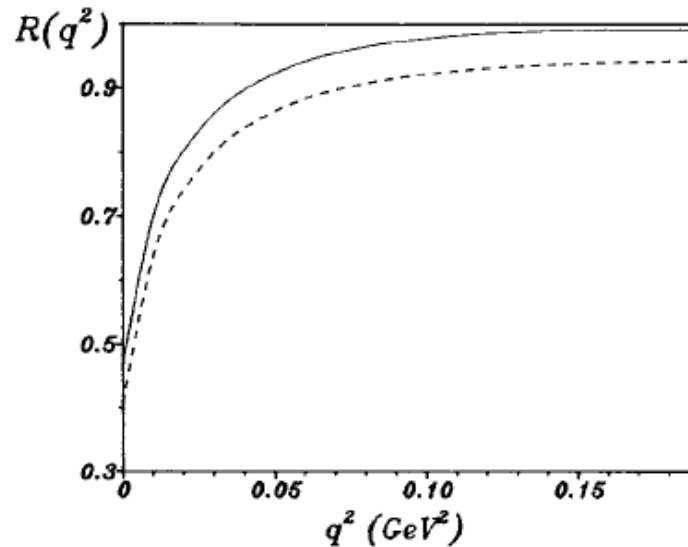
Bayesian NN analysis of ANL data

- LAR, Graczyk, Saúl-Sala, arXiv:1805.00905

$$\frac{d\sigma_{\nu n}}{dQ^2} = \frac{G_F^2 m_N^2}{8\pi E_\nu^2} \left[A(Q^2) + B(Q^2) \frac{(s-u)}{m_N^2} + C(Q^2) \frac{(s-u)^2}{m_N^4} \right]$$

- A, B, C are functions of $F_{1,2}^V$ and $F_{A,P}$
- $F_{1,2}^V$ assumed exact; F_P given in terms of F_A

$$\frac{d\sigma_{\nu d}}{dQ^2} = R(Q^2) \frac{d\sigma_{\nu n}}{dQ^2}$$



Singh, Arenhövel, Z. Phys. A 324 (1986)

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- A, B, C are functions of $F_{1,2}^V$ and $F_{A,P}$

- $F_{1,2}^V$ assumed exact; F_P given in terms of F_A

- Events: $N^{th}(Q^2) = \int_0^\infty dE_\nu \frac{d\sigma}{dQ^2}(E_\nu, F_A, Q^2) \phi(E_\nu)$

- Neutrino flux: $\phi(E_\nu) = p \frac{1}{\sigma(E_\nu, F_A)} \frac{dN}{dE_\nu}$

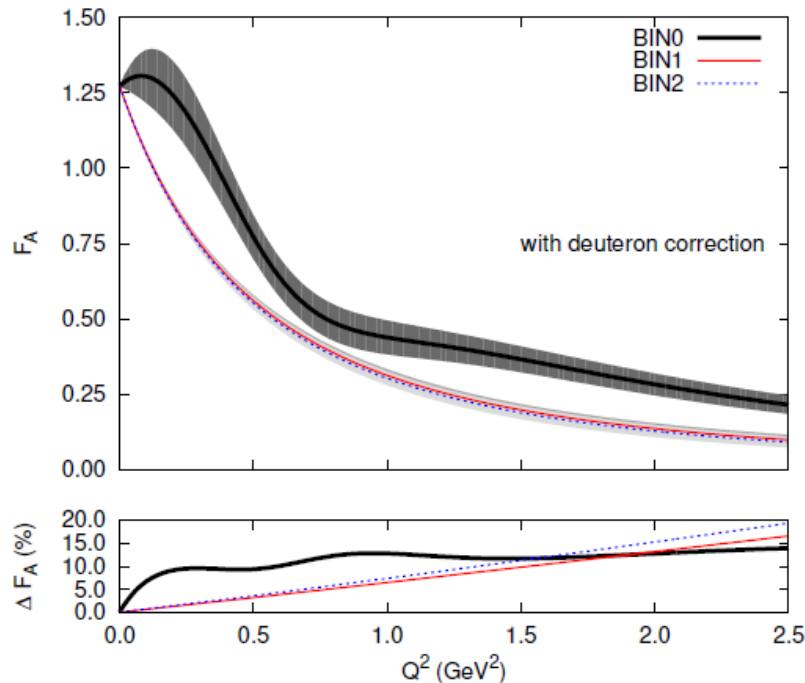
$$\frac{dN}{dE_\nu} \leftarrow \text{experimental } E_\nu \text{ distribution of observed events}$$

Barish et al., PRD19 (1979)

- $\chi^2 = \left(\frac{F_A(0) - g_A}{\Delta g_A} \right)^2 + \sum_{i=k}^{n_{ANL}} \frac{(N_i - N_i^{th})^2}{N_i} + \left(\frac{1-p}{\Delta p} \right)^2 \quad \Delta p = 20\%$

Bayesian NN analysis of ANL data

■ Results:



■ BIN0 results **inconsistent** with **z-exp** ones:

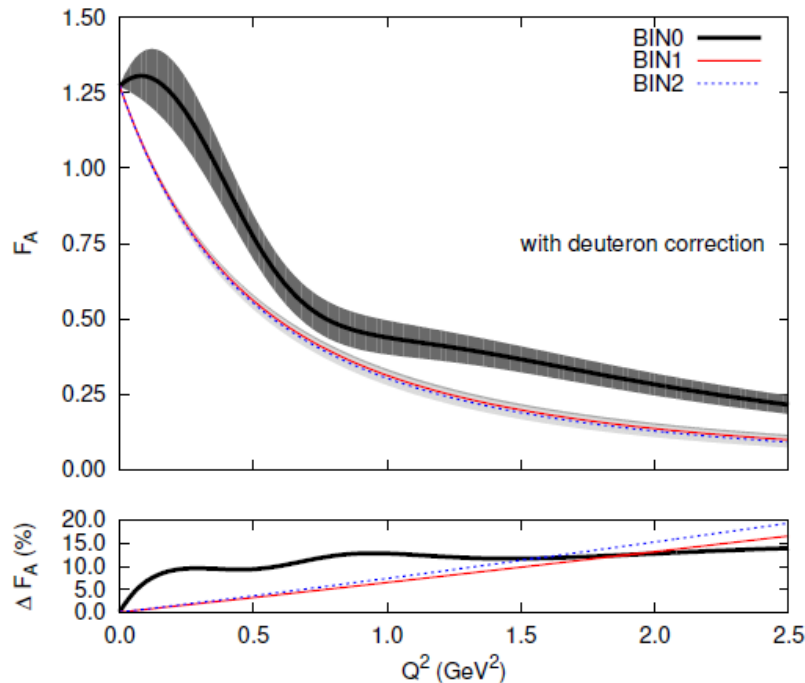
■ $r_A^2 = -1.61 \pm 0.24 \text{ fm}^2$ vs $0.46(22) \text{ fm}^2$ [νd] & $0.43(24) \text{ fm}^2$ [μ -capt.]

Meyer et al., PRD93 (2016)

Hill et al., arXiv:1708.08462

Bayesian NN analysis of ANL data

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■ BIN0 results **inconsistent** with **z-exp** ones:

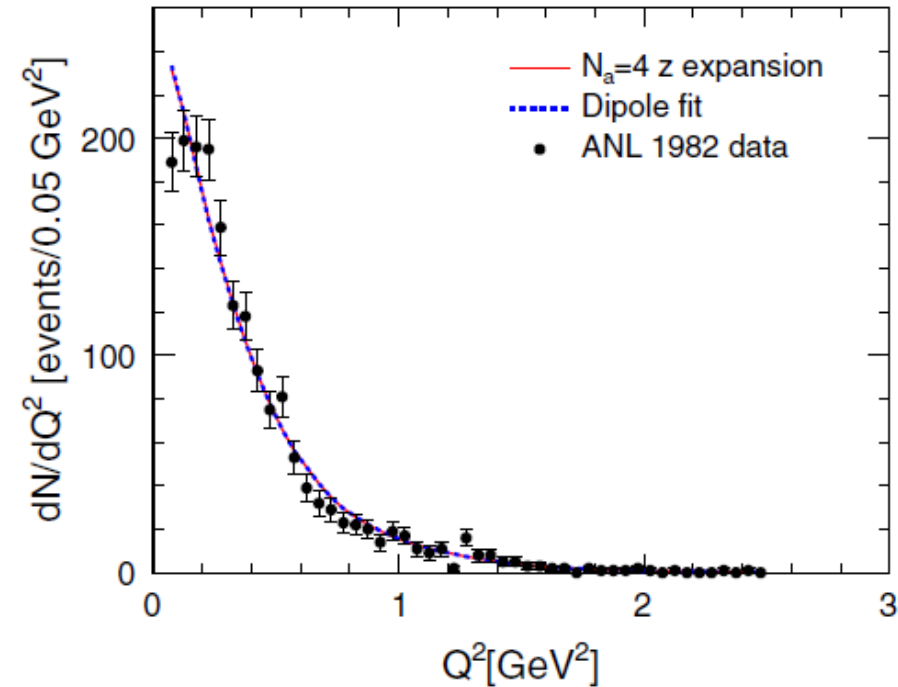
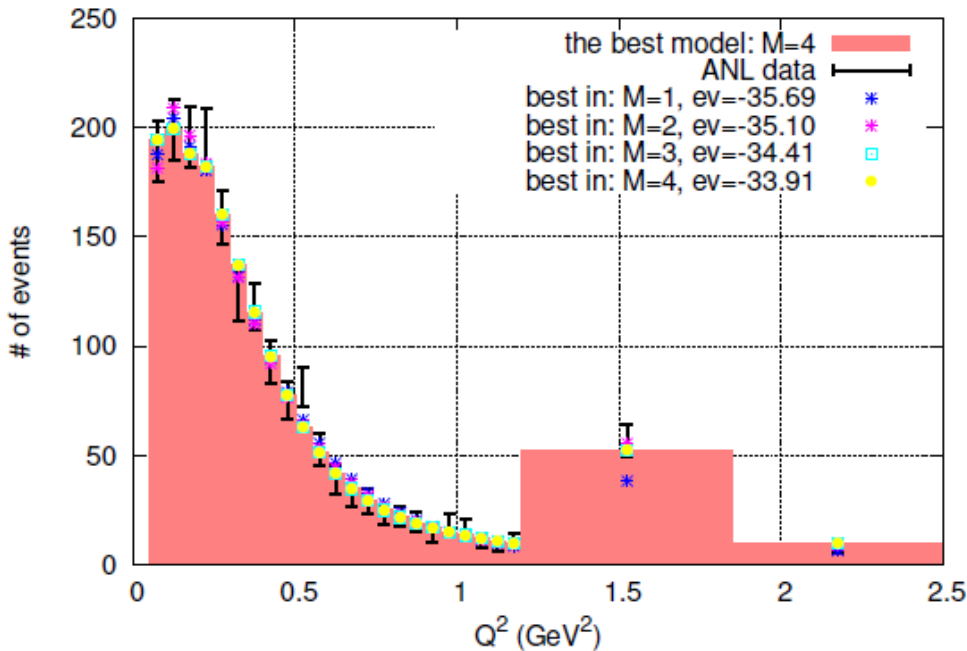
- $r_A^2 = -1.61 \pm 0.24 \text{ fm}^2$ vs $0.46(22) \text{ fm}^2$ [νd] & $0.43(24) \text{ fm}^2$ [μ -capt.]

■ In a similar study of the proton EM radii:

- $r_E^p = 0.899 \pm 0.003 \text{ fm}$ vs $0.870 \pm 0.023 \pm 0.012 \text{ fm}$

Bayesian NN analysis of ANL data

■ Results:



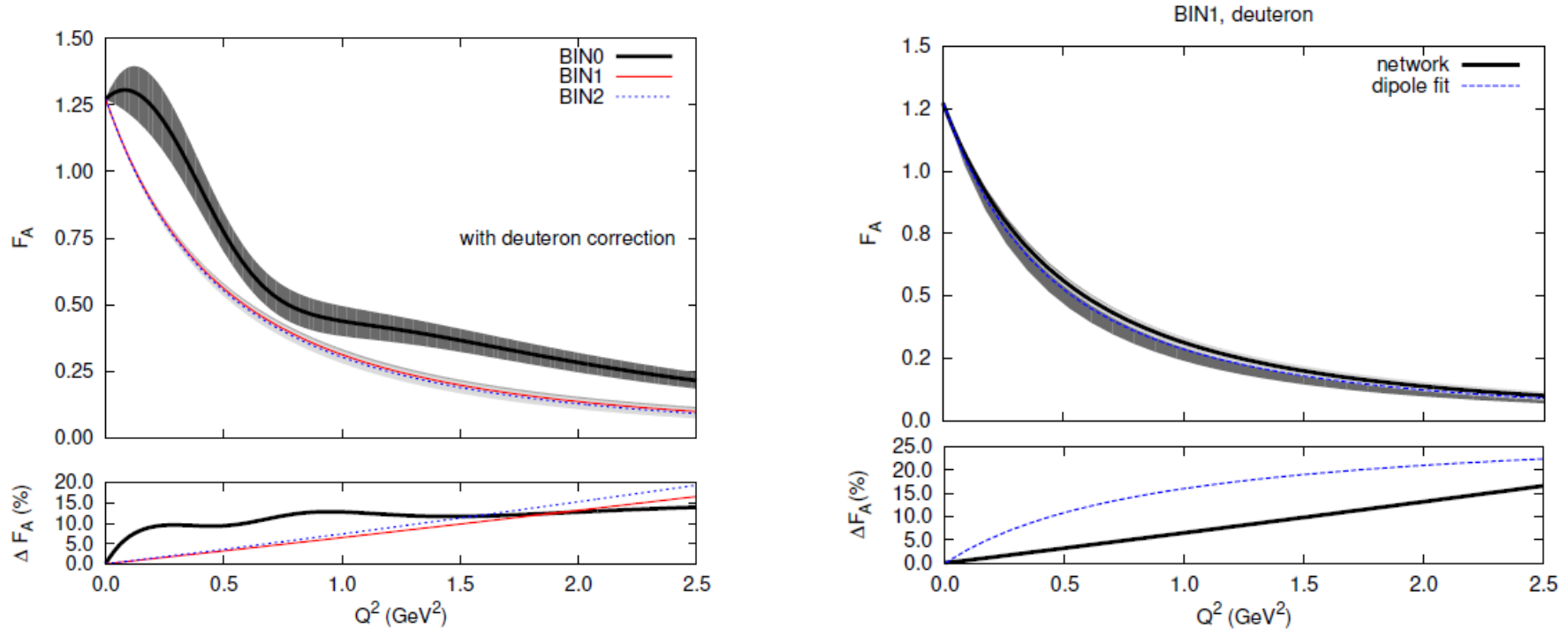
Meyer et al., PRD93 (2016)

■ BIN0 results **inconsistent** with **z-exp** ones:

- $r_A^2 = -1.61 \pm 0.24 \text{ fm}^2$ vs $0.46(22) \text{ fm}^2$ [νd] & $0.43(24) \text{ fm}^2$ [μ -capt.]
- **Deuteron** corrections (important in the 1st,2nd bins)
- Experimental **efficiency** issues at **low Q^2**

Bayesian NN analysis of ANL data

■ Results:



■ BIN1 results **consistent** with **z-exp** (and dipole) ones:

- $r_A^2 = 0.471 \pm 0.015 \text{ fm}^2$ vs $0.46(22) \text{ fm}^2$ [νd] & $0.43(24) \text{ fm}^2$ [μ -capt.]

Meyer et al., PRD93 (2016)

Hill et al., arXiv:1708.08462

Dipole nucleon form factors?

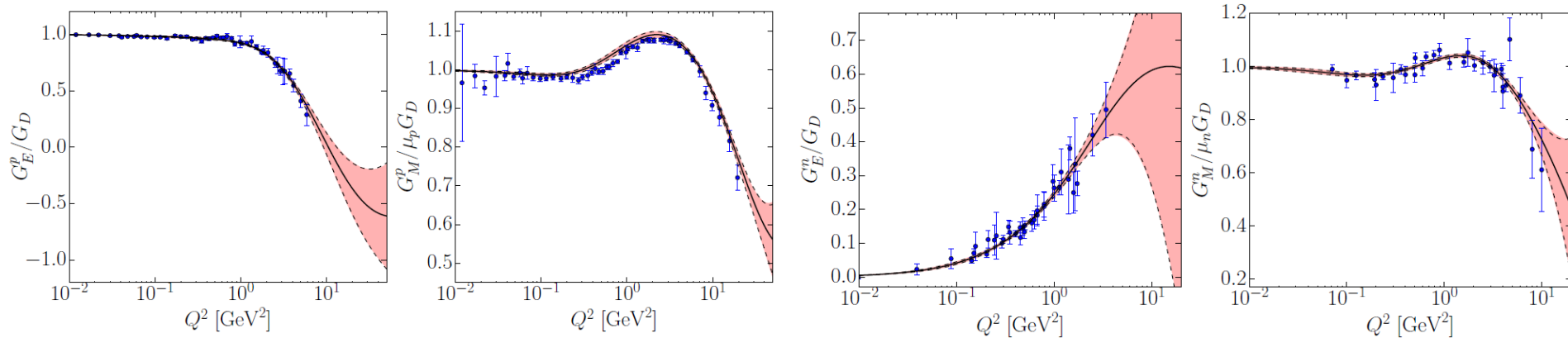
- A priori **not theoretically justified**
- z-expansion

$$F_A(q^2) = \sum_{k=0}^{\infty} a_k z(q^2)^k \quad z(t, t_{\text{cut}}, t_0) = \frac{\sqrt{t_{\text{cut}} - t} - \sqrt{t_{\text{cut}} - t_0}}{\sqrt{t_{\text{cut}} - t} + \sqrt{t_{\text{cut}} - t_0}}$$

$a_k \sim k^{-4}$ while for the dipole ansatz $a_k \sim k$ at **large k** Meyer et al., PRD93 (2016)

Dipole nucleon form factors?

EM form factors from (e,e') scattering

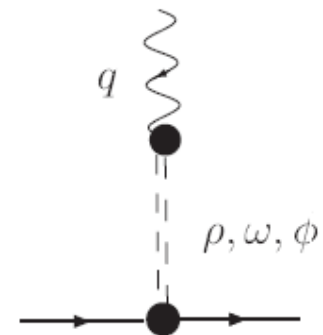


Ye et al., arXiv:1707.09063

Dipole behavior for $Q^2 \lesssim 1 \text{ GeV}^2$

$$G_D = \left(1 + \frac{Q^2}{0.71 \text{ GeV}^2} \right)^{-2}$$

- Exponential charge distributions (in the static limit)
- In the **VMD** picture, a dipole might arise from two mesons with similar masses and opposite couplings



Axial N-R transitions

- $\Delta(1232) J^P=3/2^+$

$$J_\alpha = \bar{u}^\mu(p') \left[\left(\frac{C_3^V}{M_N} (g_{\alpha\mu} \not{q} - q_\alpha \gamma_\mu) + \frac{C_4^V}{M_N^2} (g_{\alpha\mu} q \cdot p' - q_\alpha p'_\mu) + \frac{C_5^V}{M_N^2} (g_{\alpha\mu} q \cdot p - q_\alpha p_\mu) \right) \gamma_5 \right. \\ \left. + \frac{C_3^A}{M_N} (g_{\alpha\mu} \not{q} - q_\alpha \gamma_\mu) + \frac{C_4^A}{M_N^2} (g_{\alpha\mu} q \cdot p' - q_\beta p'_\mu) + C_5^A g_{\alpha\mu} + \frac{C_6^A}{M_N^2} q_\alpha q_\mu \right] u(p)$$

$$C_5^A(0) = \sqrt{\frac{2}{3}} g_{\Delta N \pi} \quad \leftarrow \text{off diagonal Goldberger-Treiman relation}$$

$$\mathcal{L}_{\Delta N \pi} = -\frac{g_{\Delta N \pi}}{f_\pi} \bar{\Delta}_\mu (\partial^\mu \vec{\pi}) \vec{T}^\dagger N \quad g_{\Delta N \pi} \Leftrightarrow \Gamma(\Delta \rightarrow N \pi)$$

- Deviations from GTR arise from chiral symmetry breaking
 - expected only at the few % level

Axial N-R transitions

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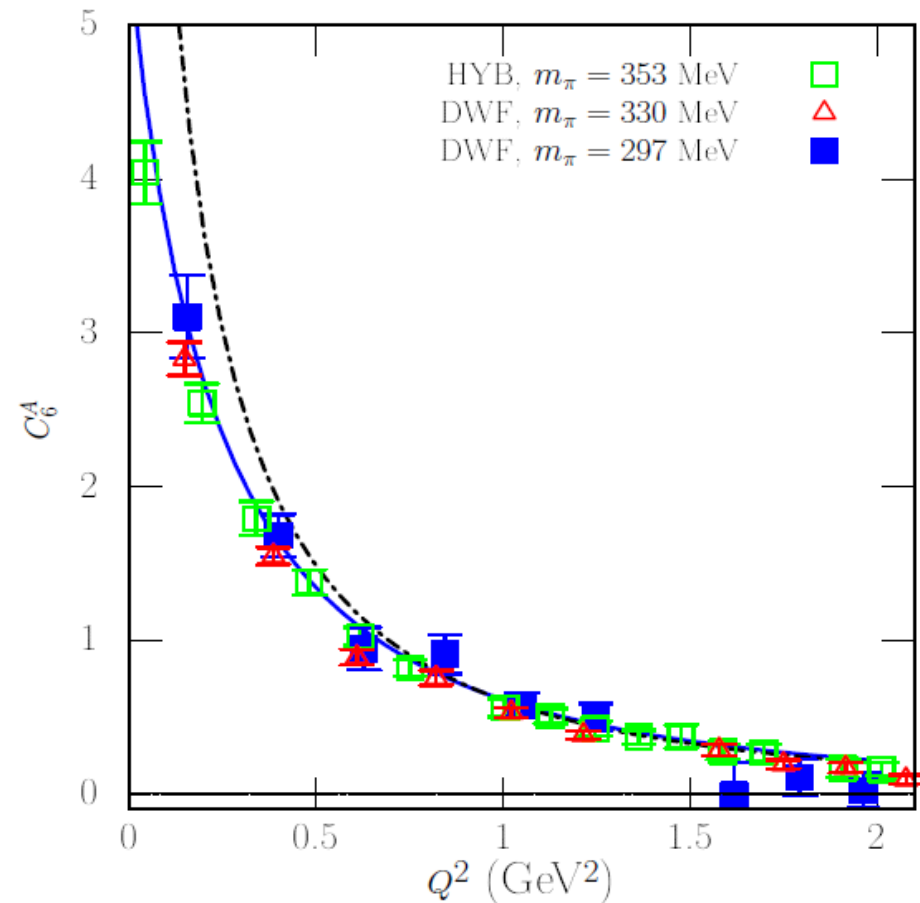
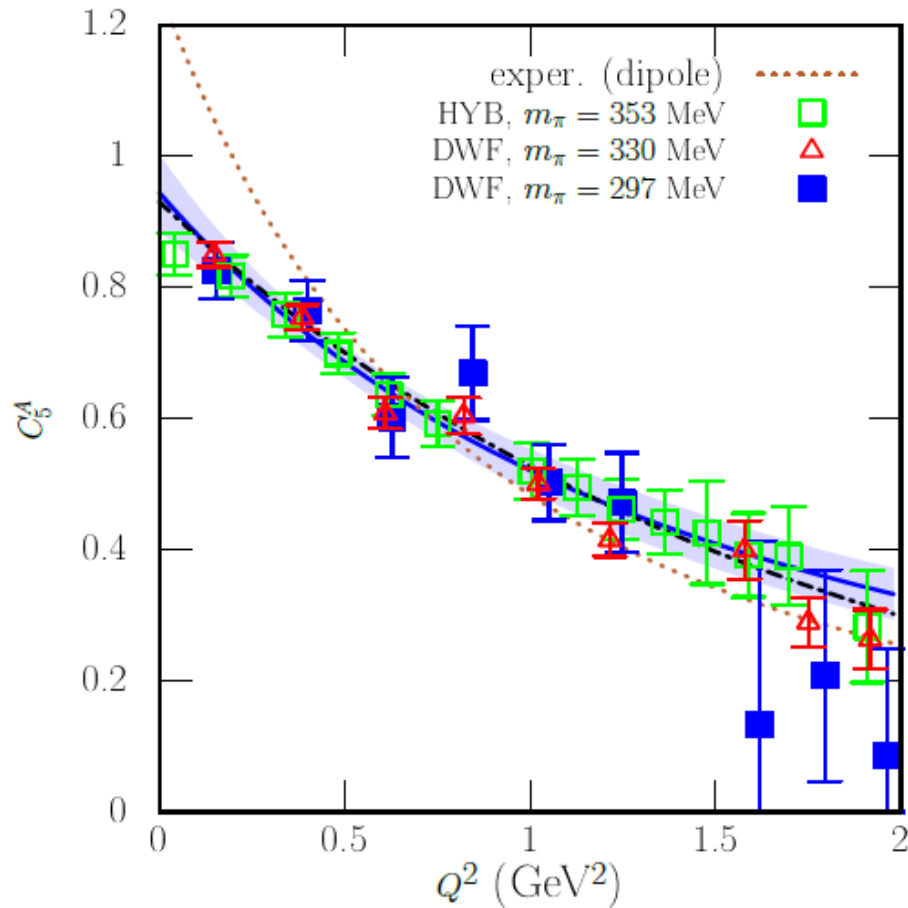
$$C_5^A = C_5^A(0) \left(1 + \frac{Q^2}{M_{A\Delta}^2} \right)^{-2} \quad \leftrightarrow \text{z-expansion for N-R transitions?}$$

- From ANL and BNL data on $\nu_\mu d \rightarrow \mu^- \pi^+ p n$
 - $M_{A\Delta} = 0.96 \pm 0.07 \text{ GeV}$ LAR, Hernandez, Nieves, Vicente Vacas, PRD 93 (2016)
 - ANL and BNL data do not constrain $C_{3,4}^A$: consistent with zero
Hernandez et al., PRD81(2010)

Axial N-R transitions

■ N- Δ axial form factors in LQCD

Alexandrou et al., PRD83 (2011)

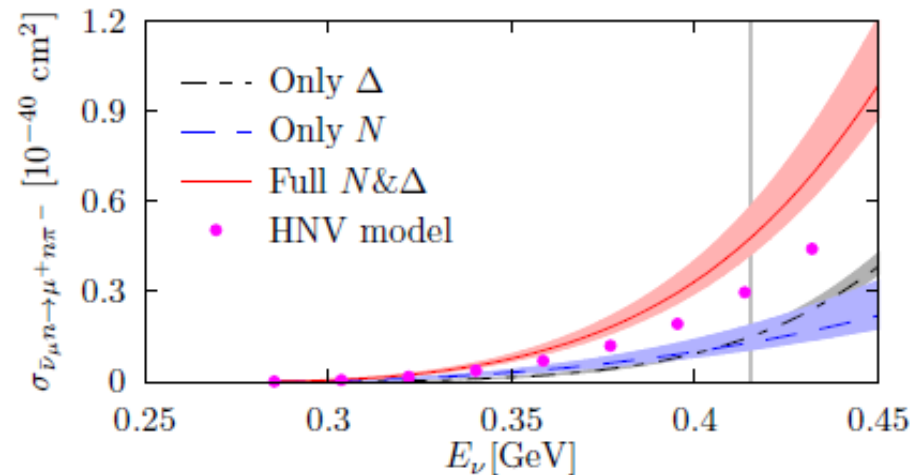
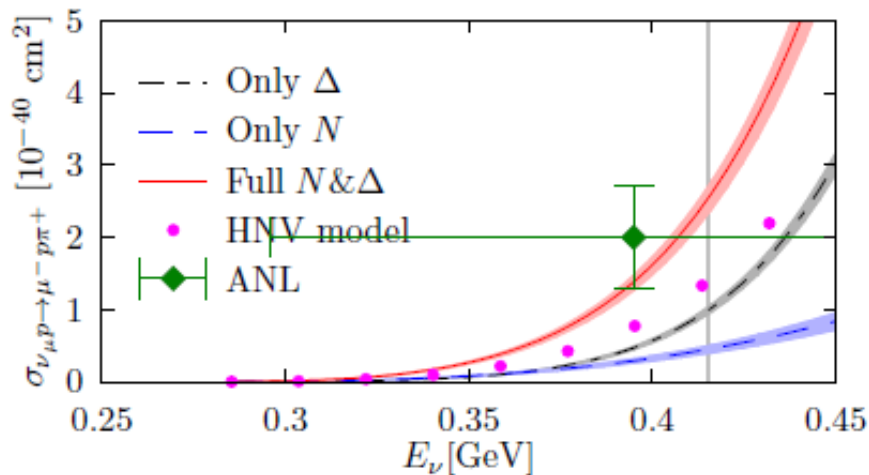


Axial N-R transitions

- Heavier resonances:
 - Goldberger-Treiman relations can be derived for leading couplings
 - No information about Q^2 dependence
 - Calculations assume dipole shapes with $M_A = 1$ GeV
 - No LQCD results

Weak pion production in BChPT

- Yao et al., arXiv:1806.09364
- First comprehensive study in ChPT
- EOMS
- Explicit $\Delta(1232)$
- $O(p^3)$
- $\delta = m_\Delta - m_N \sim O(p^{1/2})$
- Valid only close to threshold
- Benchmark for phenomenological models



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- Valid only close to threshold
- Benchmark for phenomenological models
- LECs :
 - 22 in total
 - 7 unknown (but not very relevant)
 - 4 of them can be extracted from pion electroproduction
 - information about remaining 3 LEC could be obtained from new close-to-threshold measurements of ν -induced π production on protons

Conclusions

- Do we want new more precise ν -nucleon cross section measurements?
 - Relevant input for ν MC and theoretical models in general
 - New info about the axial structure of nucleons and other baryons
 - Radiative corrections
 - ChPT LECs, non-pole corrections to Goldberger-Treiman relations
 - New physics (perhaps combining c.s. & lepton/baryon polarization)
 - ...
- Do we NEED new more precise ν -nucleon cross section measurements?
 - Our letter to Santa should be compelling:
 - ν -nucleon cross section should be crucial for future oscillation measurements
 - Experimental projections: c.s. uncertainties \Rightarrow oscillation errors
- Possible alternatives:
 - LQCD
 - (Polarized) electron scattering
 - H₂ enriched targets
 - ...