Neutrino-nucleus reaction cross sections and e-capture rates based on recent advances in shell-model interactions

Toshio Suzuki Nihon University, NAOJ, Tokyo





INT, Seattle March 9, 2018 New shell-model Hamiltonians obtained due to the advances of studies of exotic nuclei and describe well the spin modes in nuclei

SFO (p-shell: p-sd); CK-MK-KB+monopole correction: GT in ¹²C, ¹⁴C Suzuki, Fujimoto, Otsuka, PR C69 (2003)

USDB (sd-shell); Brown, Richter, PR C74 (2006)

SDPF-M (sd-shell:sd- $f_{7/2}p_{3/2}$); USD+mon. cor.: Utsuno et al, PR C60 (1999)

GXPF1J (fp-shell): GT in Fe and Ni isotopes, M1 strengths Honma, Otsuka, Mizusaki, Brown, PR C65 (2002); C69 (2004)

VMU (monopole-based universal interaction)

Otsuka, Suzuki, Honma, Utsuno et al., PRL 104 (2010) 012501

Systematic improvements in energies, magnetic moments, GT strengths * important roles of tensor force

Monopole terms of V_{NN}

$$\mathbf{V}_{\mathbf{M}}^{\mathbf{T}}(\mathbf{j}_{1}\mathbf{j}_{2}) = \frac{\sum_{\mathbf{J}} (2\mathbf{J}+1) < \mathbf{j}_{1}\mathbf{j}_{2}; \mathbf{J}\mathbf{T} | \mathbf{V} | \mathbf{j}_{1}\mathbf{j}_{2}; \mathbf{J}\mathbf{T} >}{\sum_{\mathbf{J}} (2\mathbf{J}+1)}$$



$$j_{>}(=\ell + 1/2) - j_{<}(=\ell - 1/2)$$
: attractive

 $j_> - j_>$, $j_< - j_<$: repulsive

Otsuka, Suzuki, Fujimoto, Grawe, Akaishi, PRL 69 (2005)

Tensor forces due to $\pi + \rho$ meson exchanges



tensor force



Tensor component: renormalized ≈ **bare**

tensor = π + ρ meson exchange with short- range correlation

VMU: monopole-based universal interaction

Otsuka, Suzuki, Honma, Utsuno, Tsunoda, Tsukiyama, Hjorth-Jensen, RL 104 (2010) 012501

Monopole terms: New SM interactions vs. microscopic G matrix



v-nucleus reactions: $E_v \le 100 \text{ MeV}$

- $v^{-12}C$, $v^{-13}C$, $v^{-16}O$, $v^{-56}Fe$, $v^{-56}Ni$, $v^{-40}Ar$
- low-energy v-detection
 Scintillator (CH, ...), H₂O, Liquid-Ar, Fe
- nucleosynthesis of light elements in supernova explosion
 v-oscillation effects

e-capture rates in stellar environments

- sd-shell: cooling of O-Ne-Mg core in stars by nuclear URCA processes
 - USDB vs ab initio interactions (chiral effective int.)
- pf-shell: Type-Ia SNe and nucleosynthesis of iron-group elements
- sd-pf shell nuclei in the island of inversion EKK (extended Kuo-Krenciglowa method)





HT: Hayes-Towner, PR C62, 015501 (2000) CRPA: Kolb-Langanke-Vogel, NP A652, 91 (1999)

¹²C Neutral current reactions ¹²C



Nucleosynthesis processes of light elements in SNe





• v- ⁴⁰Ar reactions

Liquid argon = powerful target for SNv detection

VMU= Monopole-based universal interaction



Important roles of tensor force

Otsuka, Suzuki, Honma, Utsuno, Tsunoda, Tsukiyama, Hjorth-Jensen PRL 104 (2010) 012501 tensor force: bare≈renormalized



• v- ⁴⁰Ar reactions

Liquid argon = powerful target for SNv detection

sd-pf shell: 40 Ar (v, e⁻) 40 K (sd)⁻² (fp)² : 2hw SDPF-VMU-LS sd: SDPF-M (Utsuno et al.) fp: GXPF1 (Honma et al.) sd-pf: VMU + 2-body LS



Ormand et al. PL B345, 343 (1995): B-decay of ⁴⁰Ti

Various roles of v's in SN-nucleosynthesis



Spectrum with v-oscillations

With collective oscillation effects



With collective and MSW effects

 $F_{\nu_e}(E) = p(E)F_{\nu_e}^0(E) + [1 - p(E)]F_{\nu_x}^0(E),$

Survival probabilities including collective effects for the scenario described in the text,

Scenario	Hierarchy	$\sin^2 \Theta_{13}$	$p(E < E_{split})$	$p(E > E_{split})$	ρ (Ε)	Earth effects
A	Normal	$\gtrsim 10^{-3}$	0	0	$\cos^2 \Theta_{\odot}$	\overline{v}_e
B	Inverted	$\gtrsim 10^{-3}$	$\sin^2 \Theta_{\odot}$	0	$\cos^2 \Theta_{\odot}$	\overline{v}_e
C	Normal	$\lesssim 10^{-5}$	$\sin^2 \Theta_{\odot}$	sin² ⊖ _⊙	$\cos^2 \Theta_{\odot}$	v_e and \overline{v}_e
D	Inverted	$\lesssim 10^{-5}$	$\sin^2 \Theta_{\odot}$	0	0	-

Cross sections folded over	er the spectra	
• Target = ${}^{13}C$	$\langle E_{v_{e}} \rangle = 10, \langle E$	$\langle E_{\mu_{k}} \rangle = 14$ and $\langle E_{\mu_{k}} \rangle = 18$ MeV.
$E_v \leq 10 MeV E_v^{th}(^{12}C) \approx 13 MeV$		· · · · · · · · · · · · · · · · · · ·
Natural isotope abund. = 1.07%	A (normal)	B (inverted)
no oscillation	8.01	8.01 (10^{-42}cm^2)
collective osc.	8.01	39.44 (39.93)
collective +MSW	39.31	39.35 (39.53)
$-\mathbf{T}_{\text{advect}} = \frac{48}{2} \mathbf{C}_{\text{a}} = \mathbf{O}(48\mathbf{C}_{\text{a}})^{1/2}$		7(1+480) OFNIX

• Target = 4° Ca	$Q(^{48}Ca-^{48}Sc)=2.8 \text{ MeV}$	$E(1^+; {}^{48}Sc) = 2.5 \text{ MeV}$
	A (normal)	B (inverted)
no oscillation	73.56	$73.56 (10^{-42} \text{cm}^2)$
collective osc.	73.56	303.4
collective +MS	W 302.6	302.8

Cross sections are enhanced by oscillations. E_{split} is too small to distinguish the v-mass hierarchy in case of Collect.+MSW oscillations (): E_{split} =15 MeV



Weak Rates in sd-shell and Nuclear URCA process in O-Ne-Mg cores

 $M=8M_{\odot} \sim 10M_{\odot}$

C burning \rightarrow O-Ne-Mg core

 \rightarrow (1) O-Ne-Mg white dwarf (WD)

- \rightarrow (2) e-capture supernova explosion (collapse of O-Ne-Mg core induced by e-capture) with neutron star (NS) remnant
- → (3) core-collapse (iron-core collapse) supernova explosion with NS (neon burning shell propagates to the center)

Fate of the star is sensitive to its mass and nuclear e-capture and β -decay rates; Cooling of O-Ne-Mg core by nuclear URCA processes determines (2) or (3).

Nomoto and Hashimoto, Phys. Rep. 163, 13 (1988) Miyaji, Nomoto, Yokoi, and Sugimoto, Pub. Astron. Soc. Jpn. 32, 303 (1980) Nomoto, Astrophys. J. 277, 791 (1984); ibid. 322, 206 (1987) •URCA processes in sd-shell nuclei

 \rightarrow Cooling of O-Ne-Mg core in 8-10 M_{\odot} stars e-capture: ${}^{A}_{Z}X + e^{-} \rightarrow {}^{A}_{Z-1}Y + v$

 β -decay: ${}_{Z-1}^{A}Y \rightarrow {}_{Z}^{A}X + e^{-} + \overline{\nu}$

They occur simultaneously at certain stellar conditions and energy is lost from stars by emissions of v and $\overline{v} \rightarrow$ Cooling of stars How much star is cooled \rightarrow fate of the star after neon flash: $^{23}Na + e^- \rightarrow ^{23}Ne + \nu$ A=23: Q=4.376 MeV

•Beta-d	lecav	\mathbf{O})-va]	lues
Deta d	iccay	X	y u	luco

Odd-A sd-shell Nuclei (A=17-31)	$^{23}Ne \rightarrow ^{23}Na$ $^{25}Mg + e^{-} \rightarrow$	$e + e^{25}Na$	- + 1 + 1	\overline{v}	A A	=25 =27	5: Q 7: Q)=3.)=2.	.835 .61(5 M) M	eV eV
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$^{25}Na \rightarrow ^{25}Mg$ $^{27}Al + e^{-} \rightarrow ^{27}Al$ $^{27}Mg \rightarrow ^{27}Al$ $TABL$ $T_{J \times 10^{9}}$	$+e^{-7}Mg$ $+e^{-7}$	$\bar{r} + i$ $\bar{r} + i$ $+ \bar{i}$ lect	ntial μ_{ϵ} (in	units of Me	/) at high d emi	ensities, ργ. cal	= 10 ⁷ -10 ¹⁰ pot	g/cm ³ , and ent	high tempera ial	atures, T =
$\stackrel{\text{rs}}{\succ} \stackrel{10}{\longrightarrow} \stackrel{\text{Na}}{\longrightarrow} \stackrel{\text{Na}$	ρY_{ϵ} (g/cr	1 ³)					<i>T</i> 9				
$\mathcal{O}_{5} = \begin{bmatrix} \mathbf{N} \\ \mathbf{F} \end{bmatrix}$		1	2	3	4	5	6	7	8	9	10
O Ne Na Mg Al Si	10 ⁷	1.200	1.133	1.021	0.870	0.698	0.534	0.404	0.310	0.244	0.196
$0 1 \mathbf$	10 ⁹ 10 ¹⁰	2.437 5.176 11.116	2.400 5.162 11.109	2.555 5.138 11.098	2.283 5.105 11.083	2.192 5.062 11.063	2.081 5.010 11.039	4.948 11.011	1.808 4.877 10.978	1.055 4.797 10.940	1.493 4.708 10.898

- Nuclear weak rates in sd-shell
- (1) New shell-model Hamiltonian: USDB cf. Oda et al., USD
- (2) Fine meshes in both density and temperature

 $(\Delta \log_{10}(\rho Ye)=0.02, \Delta \log_{10}T=0.05)$

- cf. Interpolation problem in FFN (Fuller-Fowler-Newman) grids FFN grids are rather scarce, especially for the density
- (3) Effects of screening Suzuki, Toki and Nomoto, ApJ. 817, 163 (2016)





Ab-initio effective sd-shell interactions from chiral NN (N³LO) and 3N (N²LO)

•IM-SRG (in-medium similarity renormalization group)

Stroberg et al., PRC 93 (2016); Tsukiyama, Bogner and Schwenk, PRL 106 (2011)

Hamiltonian *H*, which is normal ordered with respect to a finite-density reference state $|\Phi\rangle$ (e.g., the Hartree-Fock ground state) is given as

$$H = E_0 + \sum_{ij} f_{ij} \{a_i^{\dagger} a_j\} + \frac{1}{2!^2} \sum_{ijkl} \Gamma_{ijkl} \{a_i^{\dagger} a_j^{\dagger} a_l a_k\} + \frac{1}{3!^2} \sum_{ijklmn} W_{ijklmn} \{a_i^{\dagger} a_j^{\dagger} a_k^{\dagger} a_n a_m a_l\},$$

$$H(s) = U(s)HU^{\dagger}(s) \equiv H^{d}(s) + H^{od}(s).$$
 (2)

Here, $H^{d}(s)$ is the diagonal part and $H^{od}(s)$ is the offiagonal part of the Hamiltonian. As $s \to \infty$, the off-diagonal natrix elements become zero.

$$\frac{dH(s)}{ds} = [\eta(s), H(s)], \quad \eta(s) \equiv \frac{dU(s)}{ds} U^{\dagger}(s).$$

where E_0 , f_{ij} , Γ_{ijkl} , and W_{ijklmn} are the normal-ordered zero-, one-, two-, and three-body terms, respectively [44]. The • CCEI (coupled-cluster effective interaction) Jansen et al, PRC 94 (2016)

$$\hat{H}_{A} = \sum_{i < j} \left(\frac{\left(\mathbf{p}_{i} - \mathbf{p}_{j}\right)^{2}}{2mA} + \hat{V}_{NN}^{(i,j)} \right) + \sum_{i < j < k} \hat{V}_{3N}^{(i,j,k)}.$$

$$H_{\text{CCEI}}^{A} = H_{0}^{A_{c}} + H_{1}^{A_{c}+1} + H_{2}^{A_{c}+2} + \cdots .$$
 (6)

Here the first term $H_0^{A_c}$ stands for the core, the second term $H_1^{A_c+1}$ for the valence one-body, and $H_2^{A_c+2}$ for the two-body Hamiltonian. The two-body term is derived from

$$[S^{\dagger}S]^{1/2}\hat{H}^{A}_{\text{CCEI}}[S^{\dagger}S]^{-1/2}.$$

GT strtength with ab initio interactions IM-SRG & CCEI vs USDB Saxena, Srivastava and Suzuki, PRC97, 024310 (2018)





 $B(GT)_{eff}$ vs $B(GT)_{exp}$ for beta-decays in T=1/2 mirror sd-shell nuclei



ESPE (neutron)

CCEI

USDB





•pf-shell: GT strength in ⁵⁶Ni: GXPF1J vs KB3G vs KBF



KBF: Table by Langanke and Martinez-Pinedo,

At. Data and Nucle. Data Tables 79, 1 (2001)

- fp-shell nuclei: KBF Caurier et al., NP A653, 439 (1999)
- Experimental data available are taken into account: Experimantal Q-values, energies and B(GT) values available
- Densities and temperatures at FFN (Fuller-Fowler-Newton) grids:



Type-Ia SNe and synthesis of iron-group nuclei

Accretion of matter to white-dwarf from binary star

- \rightarrow supernova explosion when white-dwarf mass \approx Chandrasekhar limit \rightarrow ⁵⁶Ni (N=Z)
- $\rightarrow {}^{56}\text{Ni}(e^-, \nu) {}^{56}\text{Co} \quad Y_e = 0.5 \rightarrow Y_e < 0.5 \text{ (neutron-rich)}$
- \rightarrow production of neutron-rich isotopes; more ⁵⁸Ni

Decrease of e-capture rate on ${}^{56}Ni \rightarrow less$ production of ${}^{58}Ni$ and larger Y_e

Problem of over-production of neutron-excess iron-group isotopes such as ⁵⁸Ni, ⁵⁴Cr ... compared with solar abundances



Iwamoto et al., ApJ. Suppl, 125, 439 (1999)

e-capture rates with FFN

(Fuller-Fowler-Newman)

Type-Ia SNe W7 model: fast deflagration WDD2: Slow deflagration + delayed detonation

Initial: C-O white dwarf, M=1.0M $_{\odot}$ central; ρ_9 =2.12, T_c=1x10⁷K

e-capture rates: GXP; GXPF1J ($21 \le Z \le 32$) and KBF (other Z)



GXP: WDD2 (slow deflagration + detonation)



Mori, Famiano, Kajino, Suzuki, Hidaka, Honma, Iwamoto, Nomoto, Otsuka, ApJ. 833, 179 (2016)

Weak rates for nuclei in the island of inversion

Nature 505, 65 (2014)

doi:10.1038/nature12/5/

Strong neutrino cooling by cycles of electron capture and β^- decay in neutron star crusts

H. Schatz^{1,2,3}, S. Gupta⁴, P. Möller^{2,5}, M. Beard^{2,6}, E. F. Brown^{1,2,3}, A. T. Deibel^{2,3}, L. R. Gasques⁷, W. R. Hix^{8,9}, L. Keek^{1,2,3}, R. Lau^{1,2,3}, A. W. Steiner^{2,10} & M. Wiescher^{2,6}

Electron-capture/β decay pair Parent Daughter*		Density†	Chemical potential†	Luminosity‡		
		(10 ¹⁰ gcm ⁻³)	(MeV)	(10 ³⁶ erg s ⁻¹⁾		
²⁹ Mg ⁵⁵ Ti ³¹ Al ³³ Al 56Ti ⁵⁷ Cr ⁵⁷ V ⁶³ Cr ¹⁰⁵ Zr ⁵⁹ Mn ¹⁰³ Sr ⁹⁶ Kr ⁶⁵ Fe ⁶⁵ Mp	²⁹ Na ⁵⁵ Sc, ⁵⁵ Ca ³¹ Mg ³³ Mg 56Sc ⁵⁷ V ⁵⁷ Ti, ⁵⁷ Sc ⁶³ V ¹⁰⁵ Y ⁵⁹ Cr ¹⁰³ Rb ⁹⁶ Br ⁶⁵ Mn ⁶⁵ Cr	4.79 3.73 3.39 5.19 5.57 1.22 2.56 6.82 3.12 0.945 5.30 6.40 2.34 3.55	13.3 12.1 11.8 13.4 13.8 8.3 10.7 14.7 11.2 7.6 13.3 14.3 10.3 11.7	24 11 8.8 8.3 3.5 1.6 1.6 1.6 0.97 0.92 0.88 0.65 0.65 0.65 0.60 0.46		
IVIII	UI	5.55	11.7	0.40		

Island of inversion

Z=10-12, N = 20-22

Table 1 Electron-capture/p -decay pairs with highest cooling rat	Table 1 El	ctron-capture/β [−] -deca	y pairs with highest	cooling rate
--	--------------	------------------------------------	----------------------	--------------

Rates evaluated by QRPA Shell-model evaluations are missing.



Figure 2 [Electron-capture/ β^- -decay pairs on a chart of the nuclides. The thick blue lines denote electron-capture/ β^- -decay pairs that would generate a strong neutrino luminosity in excess of $5 \times 10^{16} \text{ erg s}^{-1}$ at T = 0.51 GK for a composition consisting entirely of the respective electron-capture/ β^- -decay pair. They largely coincide with regions where allowed electron-capture and β^- -decay transitions are predicted to populate low-bying states and subsequent electron capture is blocked (shaded squares, see also the discussion

in ref. 3). These are mostly regions between the dosed neutron and proton shells (pairs of horizontal and vertical red lines), where nuclei are significantly deformed (see Supplementary Information section 4). Nuclides that are β^- -stable under terrestrial conditions are shown as squares bordered by thicker lines. Nuclear charge numbers are indicated in parentheses next to element symbols.





sd-pf shell

Non-degenerate treatment of sd and pf shells by EKK (extended Kuo-Krenciglowa) method Tsunoda, Takayanagi, Hjorth-Jensen and Otsuka, Phys. Rev. C 89, 024313 (2014)

Cf: monopoles with non-degenerate vs degenerate method



K. Takayanagi, Nucl. Phys. A 852, 61 (2011).
 K. Takayanagi, Nucl. Phys. A 864, 91 (2011).





Summary

v- nucleus reactions

- New v –induced cross sections based on new shell-model Hamiltonians with proper tensor forces
 ¹²C, ¹³C, ¹⁶O, ⁴⁰Ar, ⁵⁶Fe, ⁵⁶Ni
- Detection of low-energy reactor, solar v [¹³C] and SNv [¹²C, ¹⁶O, ⁴⁰Ar, ⁵⁶Fe]
- Nucleosynthesis elements by v-processes $v^{-12}C, v^{-4}He \rightarrow {}^{7}Li, {}^{11}B \text{ in CCSNe}$ $v^{-56}Ni \rightarrow {}^{55}Mn \text{ in Pop. III stars}$
- Effects of v-oscillations (MSW) in nucleosynthesis abundance ratio of $^7\text{Li}/^{11}\text{B} \rightarrow v$ mass hierarchy
- Cross sections are enhanced by oscillations. Distinguishing mass hierarchy by measurement on earth is not easy because of small E_{split} when both collective and MSW oscillations occur.

Summary

- 1. e-capture and β -decay rates for one-major shell nuclei
- New weak rates for sd-shell from USDB
 Nuclear URCA processes for A=23 and 25 nuclear pairs
 → Cooling of O-Ne-Mg core of 8-10 solar-mass stars and determines fate of stars with ~9M_☉ whether they end up with
 - e-capture SNe or core-collapse SNe.
 - ab initio interactions vs USDB
- New weak rates for pf-shell from GXPF1J
 - Nucleosynthesis of iron-group elements in Type Ia SNe.
- **Over-production problem in iron-group nuclei with FFN can be solved with smaller rates with GXPF1J**

2. Weak rates for two-major shell nuclei

sd-pf shell nuclei in the island of inversion, important for URCA processes in neutron star crusts, are evaluated with EKK method starting from chiral EFT interaction N3LO +3N (FM).
 e.g. ³¹Al (e⁻, v)³¹Mg, ³¹Mg(,e⁻v)³¹Al

Collaborators

T. Otsuka^m, T. Kajino ^{b,c}, S. Chiba^d,

M. Honma^e, T. Yoshida^c, K. Nomoto^f, H. Toki^g, S. Jones^h, R. Hirschiⁱ, K. Mori^{b,c}, M. Famiano^j, J. Hidaka^k, K. Iwamoto^l, N. Tsunodaⁿ, N. Shimizuⁿ, B. Balantekin^a,

^aRIKEN

^bNational Astronomical Observatory of Japan ^cDepartment of Astronomy, University of Tokyo ^dTokyo Institute of Technology ^eUniversity of Aizu ^fWPI, the University of Tokyo ^gRCNP, Osaka University ^hLANL, ⁱKeele University ^jWestern Michigan University, ^kMeisei University ¹Department of Physics, Nihon University ⁿCNS, University of Tokyo ^mUniv. of Wisconsin

Note added:

Difference between GXPF1J and KB3G

- 1. Shell gap $f_{5/2}$ - $f_{7/2}$ is larger for GXPF1J
- 2. Isoscalar pairing is larger for GXPF1J
- \rightarrow More spreading of GT strength for GXPF1J

Murchison Meteorite

SiC X-grains



- ${}^{12}C/{}^{13}C > Solar$
- ¹⁴N/¹⁵N < Solar
- Enhanced ²⁸Si

- Decay of ²⁶Al (t_{1/2}=7x10⁵yr), ⁴⁴Ti (t_{1/2}=60yr)

SiC X-grains are made of Supernova Dust !

W. Fujiya, P. Hoppe, and U. Ott (2011, ApJ 730, L7) discovered ¹¹B and ⁷Li isotopes in 13 SiC X-grains.

Grain	Size	${}^{12}C/{}^{13}C$	$\delta^{29}Si^a$	$\delta^{30}Si^{a}$	⁷ Li/ ⁶ Li	${}^{11}B/{}^{10}B$	Li/Si	B/Si
	(µm)	,	(‰)	(‰)		,	(10-5)	(10 ⁻⁵)
				Single X	grains			
X1	0.6	114 ± 2	-178 ± 11	-265 ± 9	11.87 ± 0.63	4.51 ± 0.77	9.69	3.33
X2	1.2	128 ± 2	-377 ± 11	-261 ± 10	12.06 ± 0.62	5.06 ± 0.58	23.8	18.8
X3	1.5	244 ± 5	-205 ± 10	-297 ± 7	11.48 ± 0.86	4.54 ± 0.63	1.76	1.92
X4	1.0	241 ± 6	-556 ± 10	-245 ± 9	12.00 ± 0.56	4.85 ± 1.19	24.8	3.31
X9	0.6	38 ± 1	-361 ± 10	-394 ± 8	11.20 ± 1.01	4.19 ± 0.70	10.8	11.4
X11	0.8	326 ± 14	-358 ± 12	-432 ± 11	11.78 ± 2.03	4.99 ± 1.88	3.66	3.00
X13	0.7	345 ± 6	-261 ± 10	-424 ± 7	11.59 ± 0.93	4.37 ± 2.04	10.7	1.14
Average					11.83 ± 0.29	4.68 ± 0.31		
			X grain	is + other nearby	/attached SiC grai	ns		
X5		34 ± 1	-226 ± 11	-120 ± 10	12.21 ± 0.41	4.36 ± 0.40	40.2	18.8
X6		88 ± 1	-236 ± 11	-189 ± 9	13.06 ± 1.36	3.83 ± 0.27	2.15	14.2
X7		78 ± 1	-281 ± 11	-208 ± 10	11.20 ± 2.40	11.47 ± 6.36	8.28	9.48
X8		76 ± 1	-223 ± 10	-266 ± 8	11.29 ± 0.64	4.27 ± 0.29	4.80	12.4
X12		83 ± 1	-271 ± 11	-242 ± 10	11.54 ± 0.52	4.13 ± 0.46	24.3	14.2
Average					11.90 ± 0.28	4.16 ± 0.17		
Solar		89	0	0	12.06	4.03	5.6	1.9

