



皮影 Shadow play

Source: <http://www.cnhubei.com/ztmjys-pyts>

# Neutrino Shadow Play

– Neutrino interactions for oscillation measurements

Xianguo LU / 卢显国 University of Oxford

INT-18-1a: Nuclear ab initio Theories and Neutrino Physics  
Seattle, 9 March 2018

# *THE Universe*

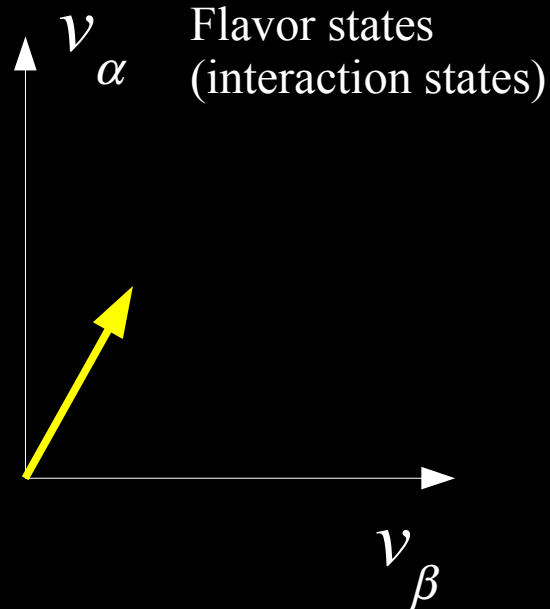
*– Matter & very little antimatter (matter-antimatter asymmetry)*



*CP-Symmetry violation (CP violation)*

# Neutrino

– Oscillation



## The Nobel Prize in Physics 2015



Photo: A. Mahmoud  
**Takaaki Kajita**  
Prize share: 1/2



Photo: A. Mahmoud  
**Arthur B. McDonald**  
Prize share: 1/2

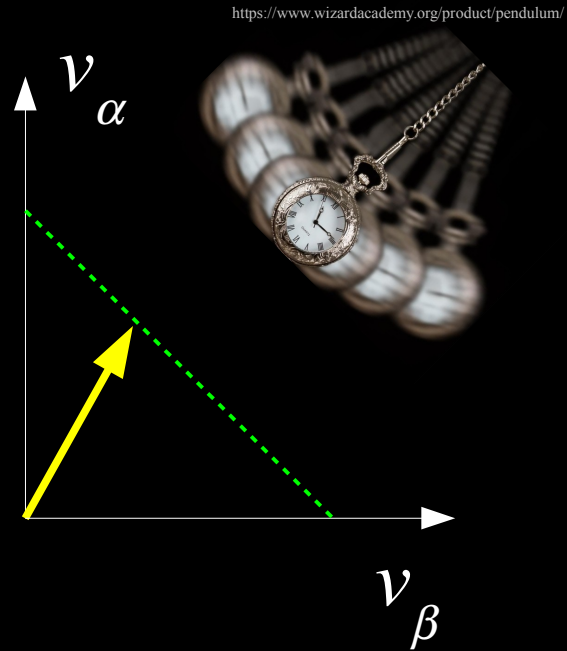
The Nobel Prize in Physics 2015 was awarded jointly to Takaaki Kajita and Arthur B. McDonald *"for the discovery of neutrino oscillations, which shows that neutrinos have mass"*

[https://www.nobelprize.org/nobel\\_prizes/physics/laureates/2015/](https://www.nobelprize.org/nobel_prizes/physics/laureates/2015/)

*Neutrino mass:*  
shift between interaction and propagation states

# Neutrino

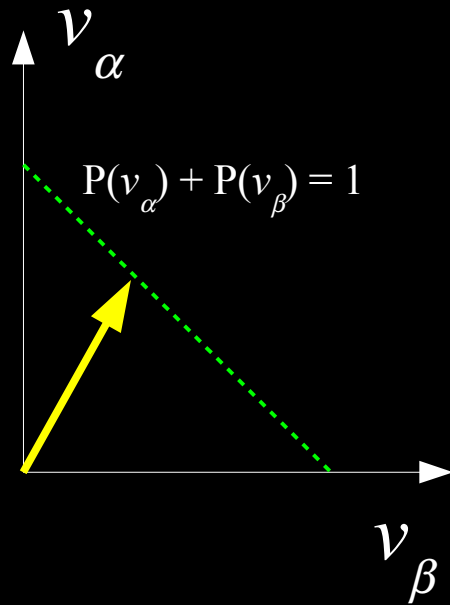
## – Oscillation



oscillation between flavor states as  
a function of time

# Neutrino

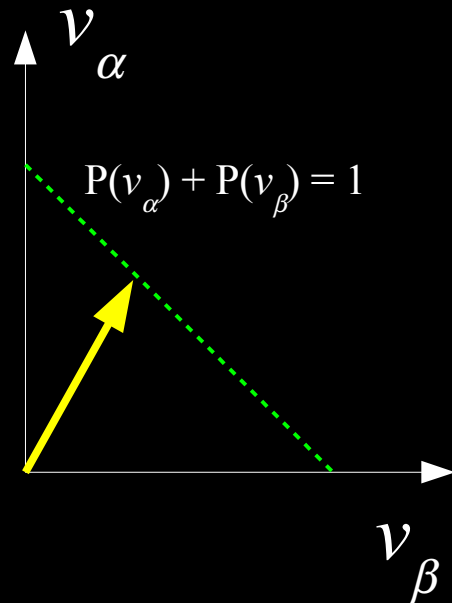
– Oscillation



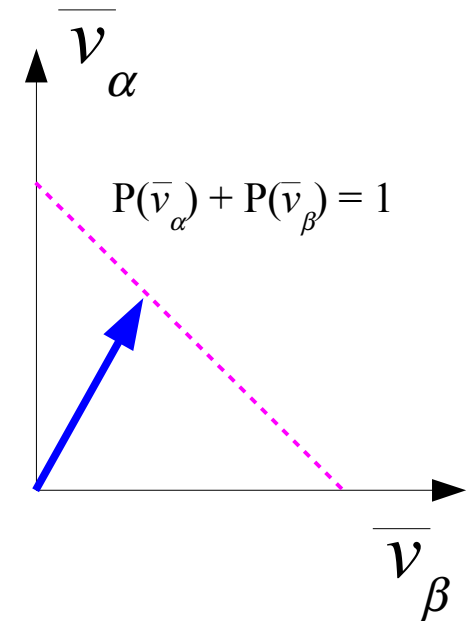
oscillation between flavor states as  
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# Neutrino

– Oscillation



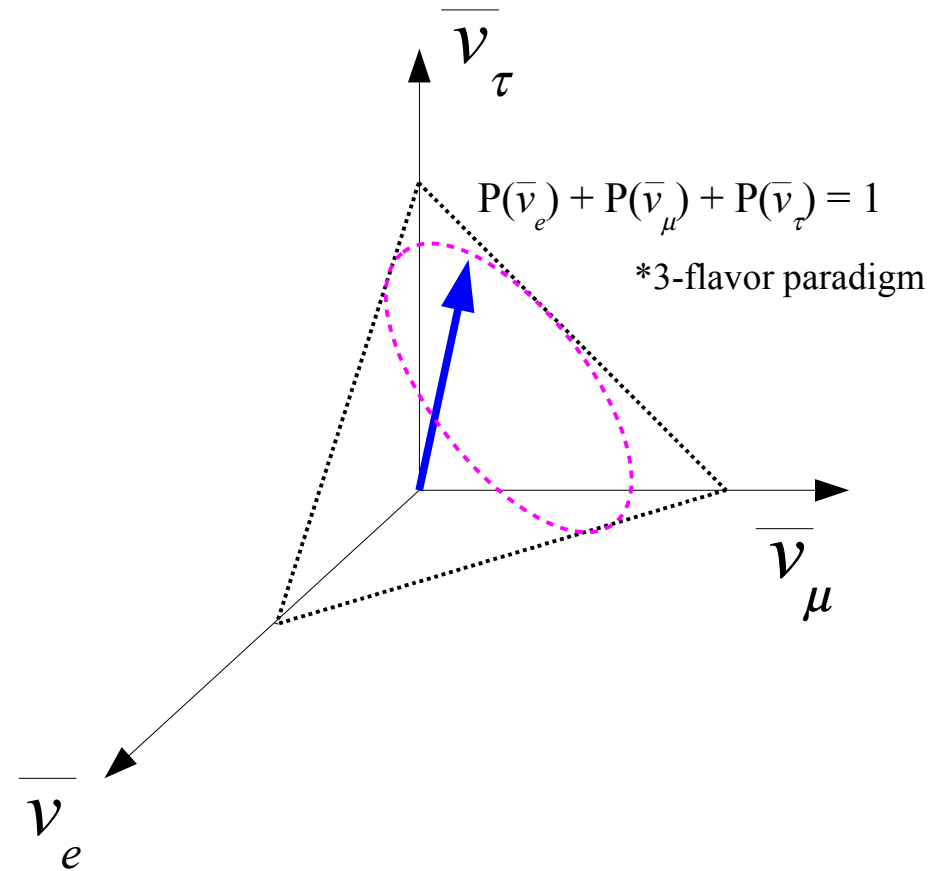
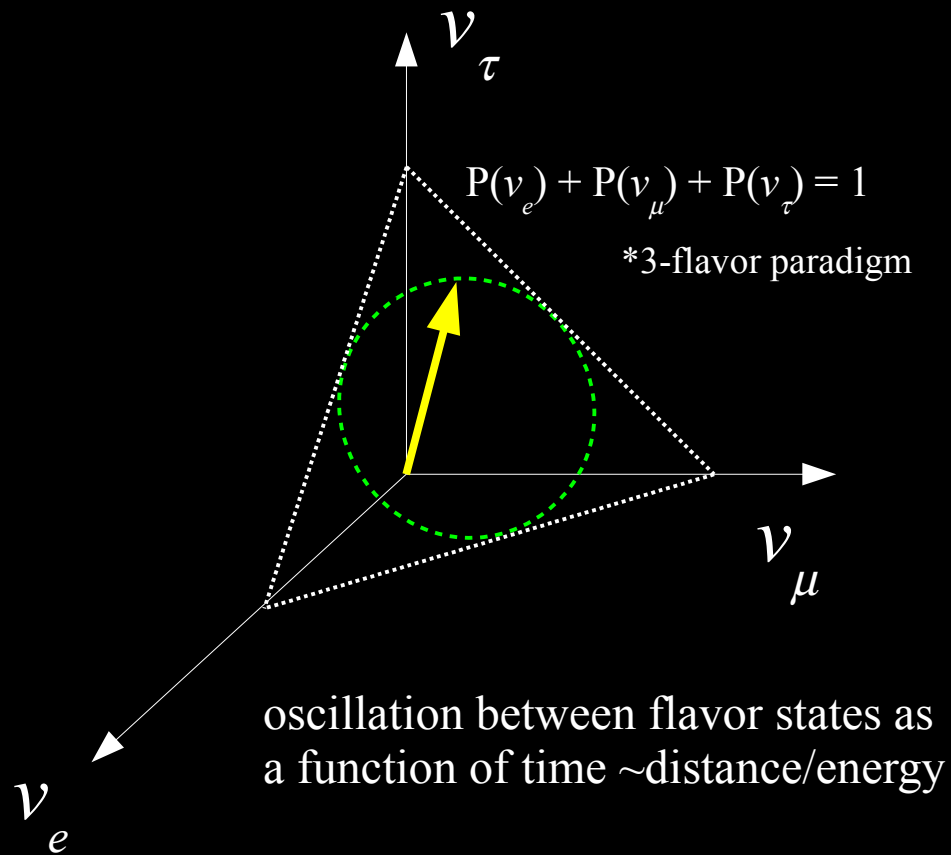
oscillation between flavor states as a function of time



*If only 2 flavors, same oscillation behavior  
→ CP violation not observed*

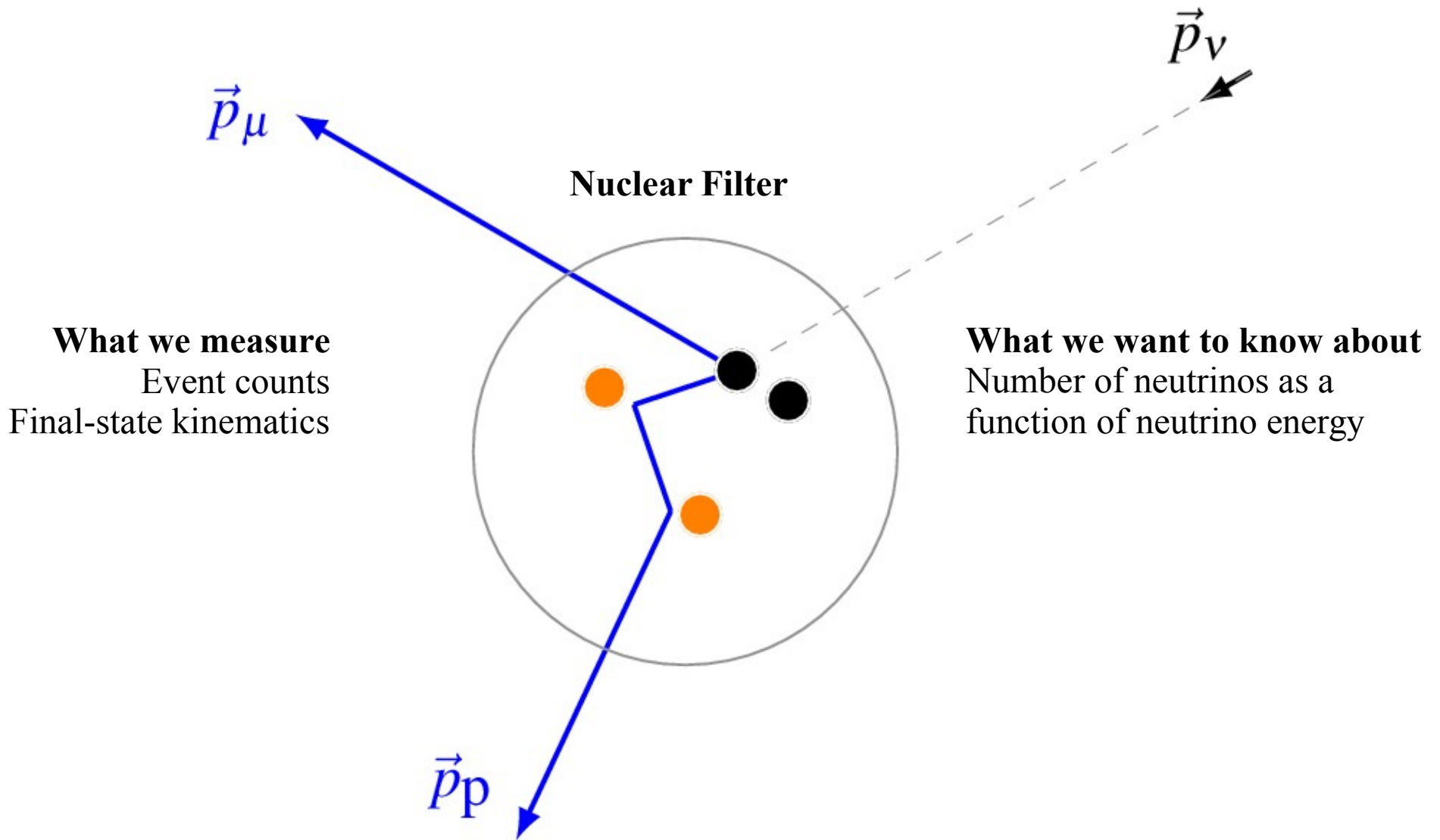
# Neutrino

– CP violation

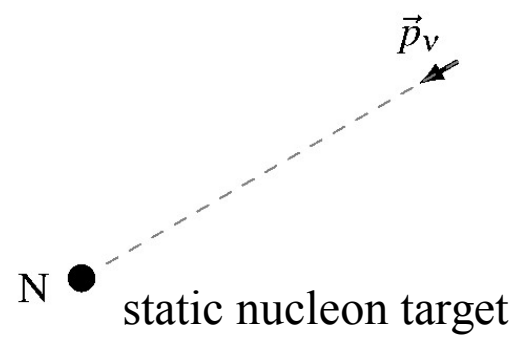


*Oscillation property difference*  
→ CP violation

# The big picture of neutrino detection in oscillation measurements







Neutrino energy in GeV regiem

Quasi-elastic scattering (QE)

$$\nu n \rightarrow \ell^- p$$

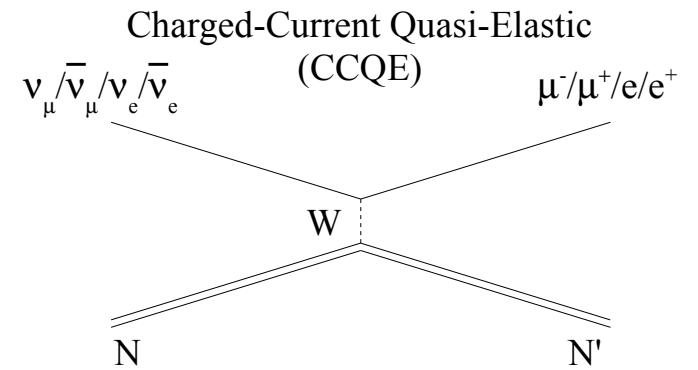
charged current (CC)  $\nu \rightarrow \ell'$

$\vec{p}_{\ell'}$

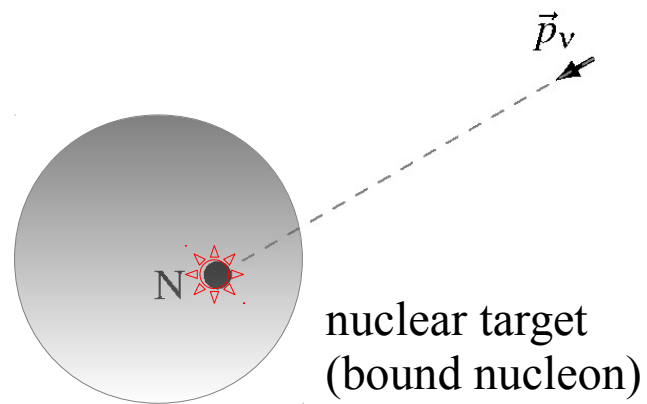
static nucleon target

$\vec{p}_{N'}$

quasi-elastic (QE)  $N \rightarrow N'$



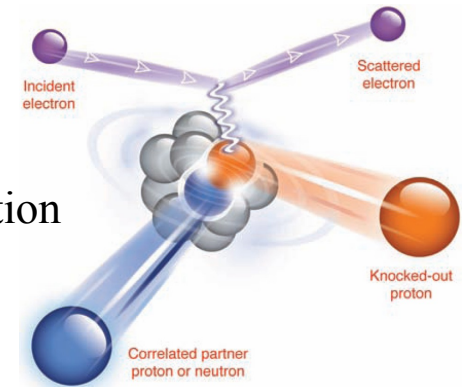
# Fermi motion biases $E_\nu$ reconstruction



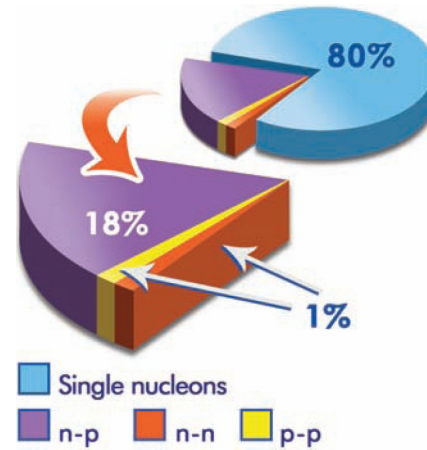
Fermi motion biases  $E_\nu$  reconstruction

Multinucleon correlations:

initial correlation  
large relative motion



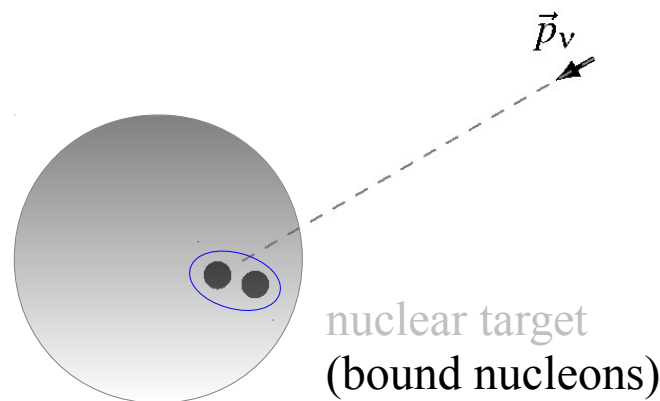
Science 320 (2008) 1476-1478



Fermi motion biases  $E_\nu$  reconstruction

Multinucleon correlations:

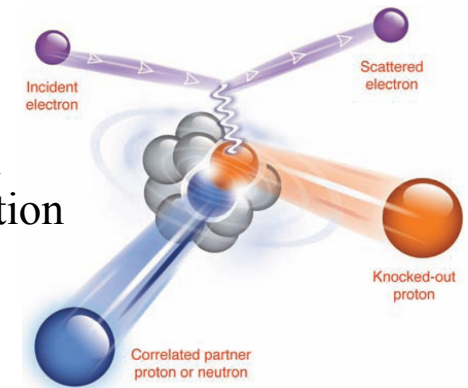
cross section unknown, strong bias to *all* final-state kinematics



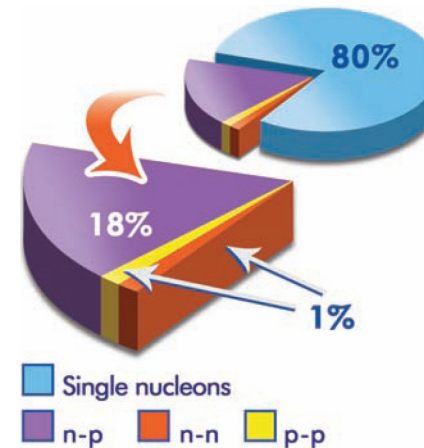
In **p**article-**h**ole excitation:

- Impulse approximation: independent particles (1p1h)
- RPA (random phase approximation): sum of 1p1h excitation (over all pairs) → “screening effect”
- npnh ( $n \geq 2$ ): sub-leading terms in ph expansion → short range correlations, meson exchange currents *etc.*

initial correlation  
large relative motion



Science 320 (2008) 1476-1478



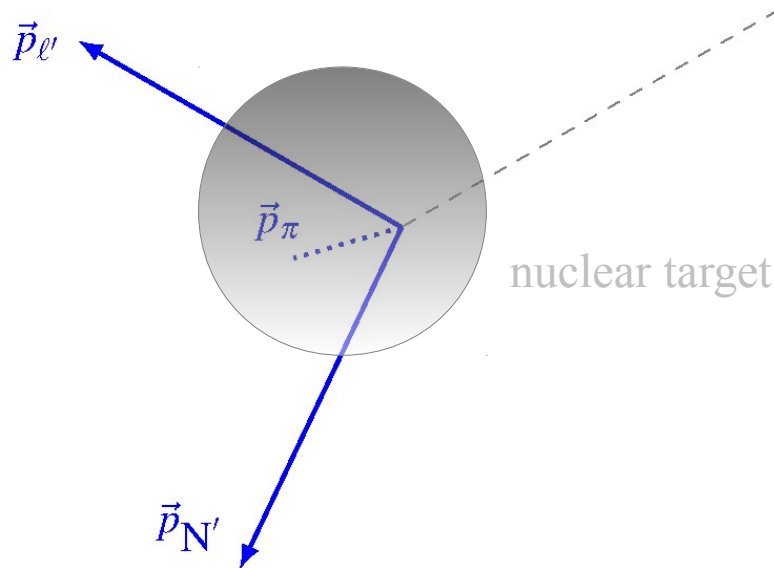
Fermi motion biases  $E_\nu$  reconstruction

Multinucleon correlations:

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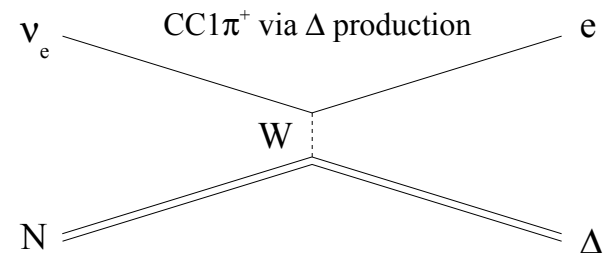
QE-like:  $\pi$  absorbed in nucleus  $\leftarrow$  final-state interaction (FSI)

charged current (CC)  $\nu \rightarrow l'$



Resonance production (RES)

$$\nu p \rightarrow l^- \Delta^{++} \rightarrow l^- p \pi^+$$



QE-like  $N \rightarrow N'$

including resonance production (RES)  $\Delta \rightarrow N'\pi$  followed by  $\pi$  absorption

Fermi motion biases  $E_\nu$  reconstruction

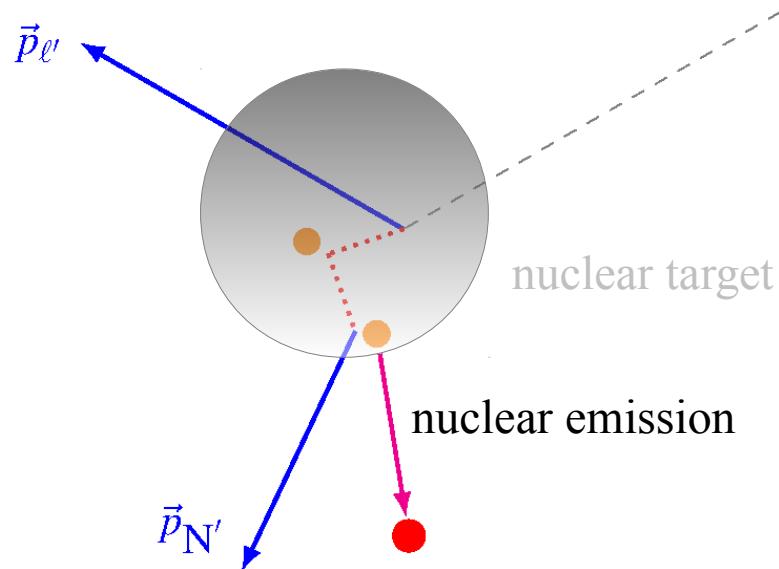
Multinucleon correlations:

cross section unknown, strong bias to *all* final-state kinematics

QE-like:  $\pi$  absorbed in nucleus  $\leftarrow$  final-state interaction (FSI)

FSI  $\rightarrow$  energy-momentum transferred in nucleus, possible nuclear emission

charged current (CC)  $\nu \rightarrow l'$



QE-like  $N \rightarrow N'$

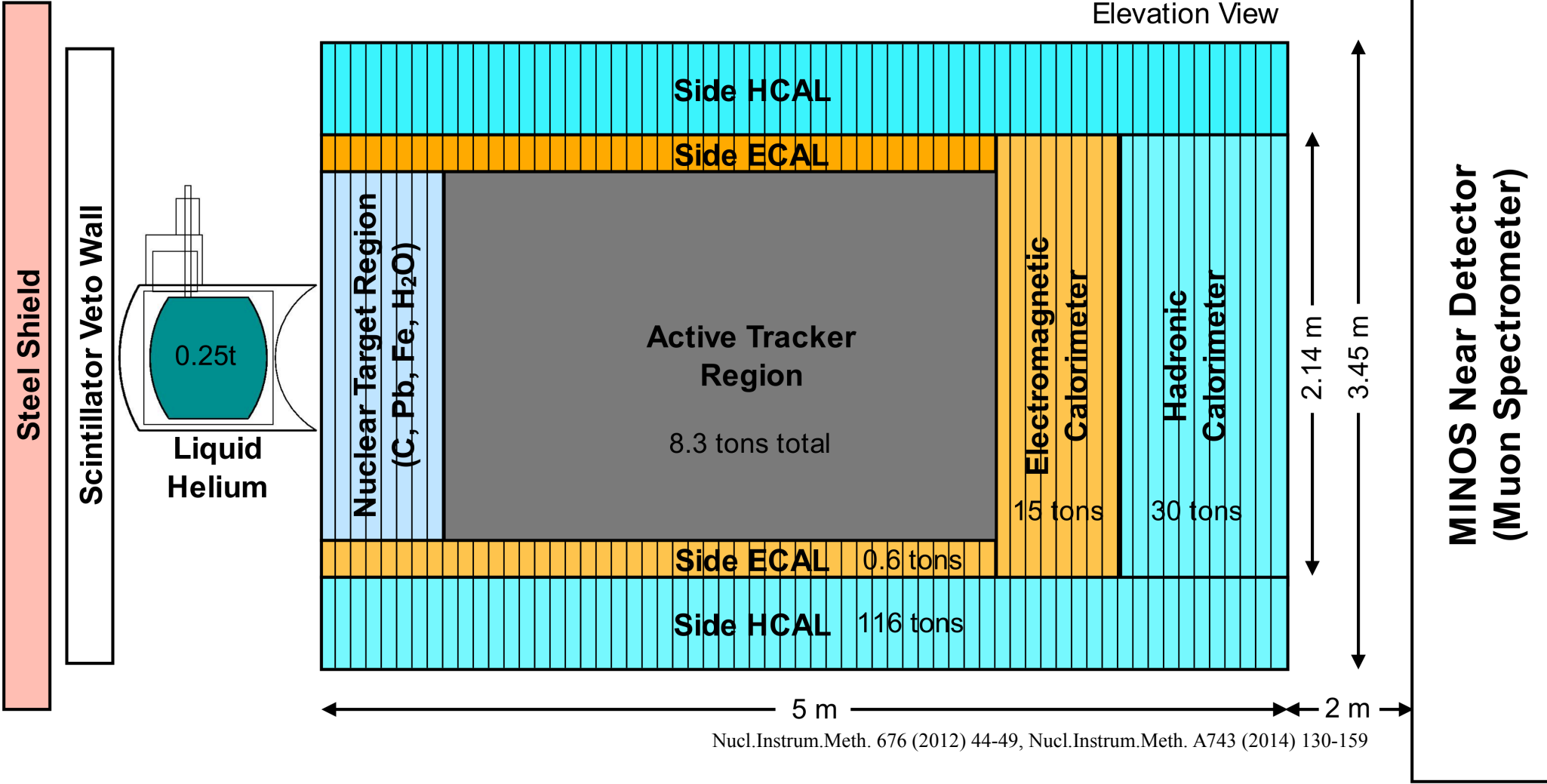
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# MINERvA



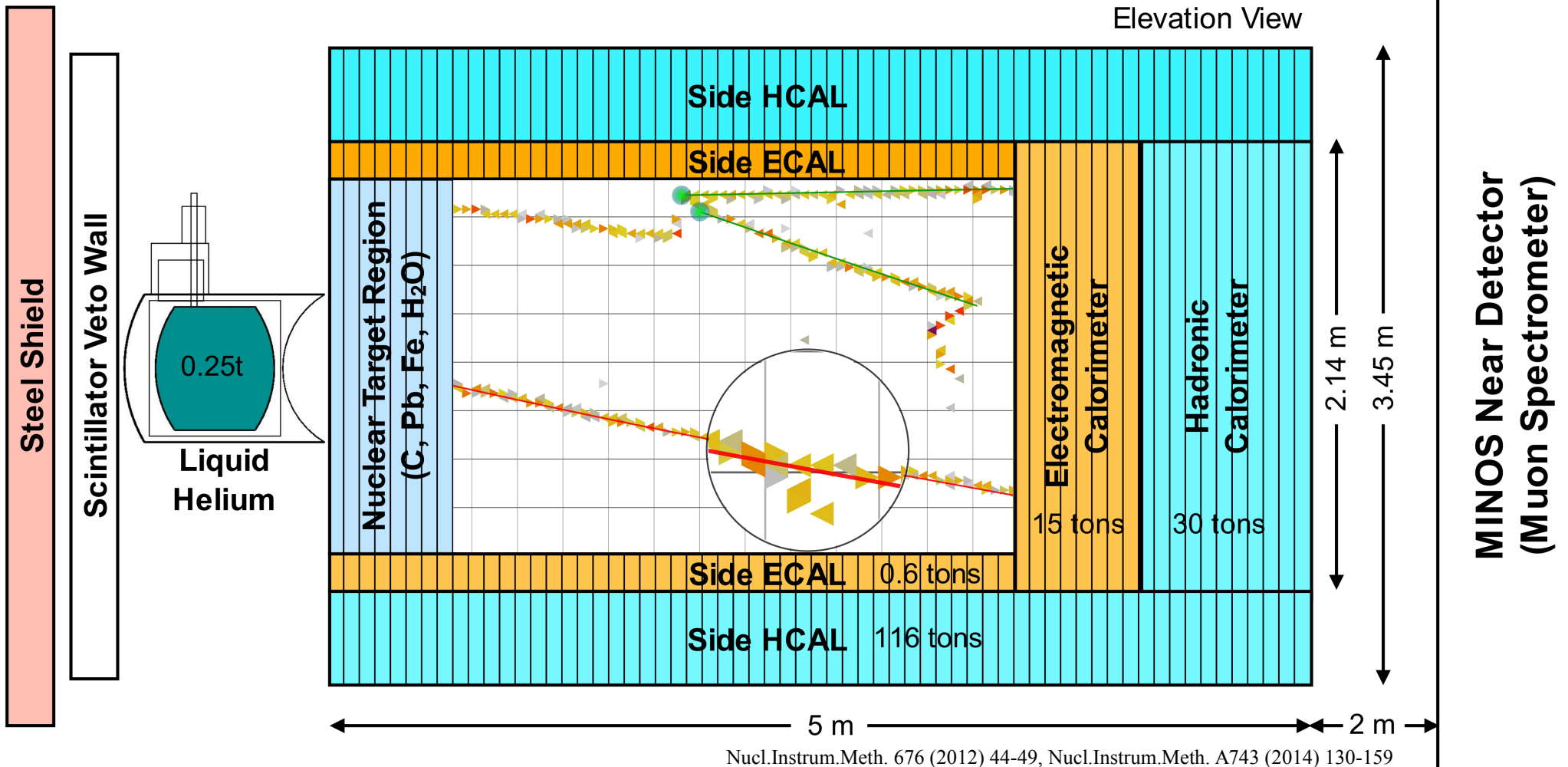


# MINERvA

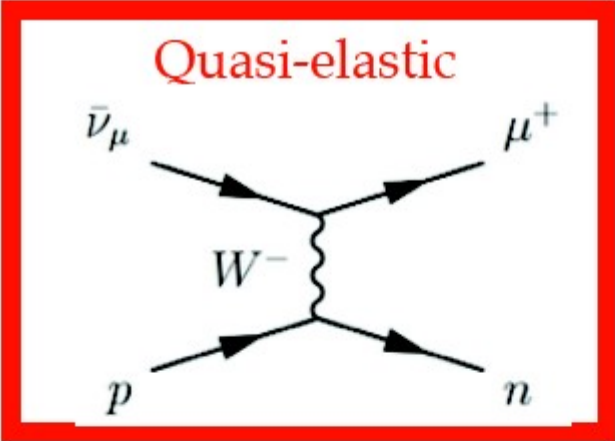


Scintillator tracker

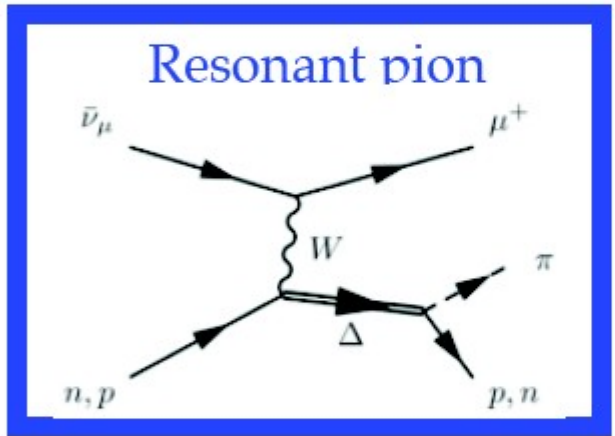
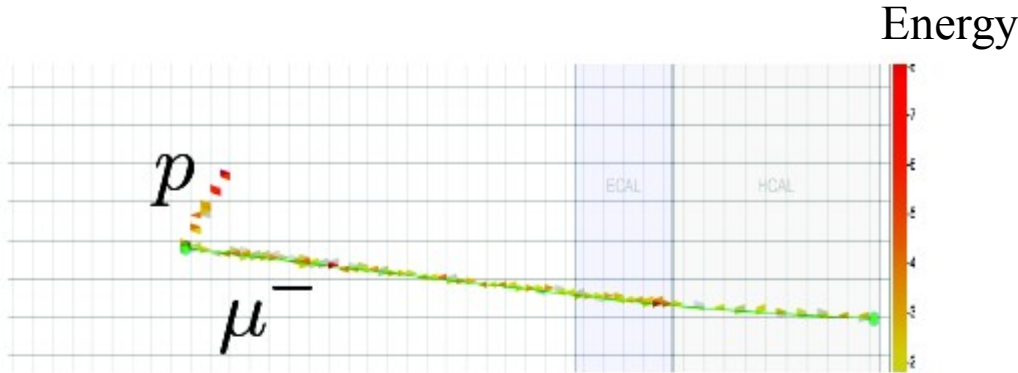
# MINERvA



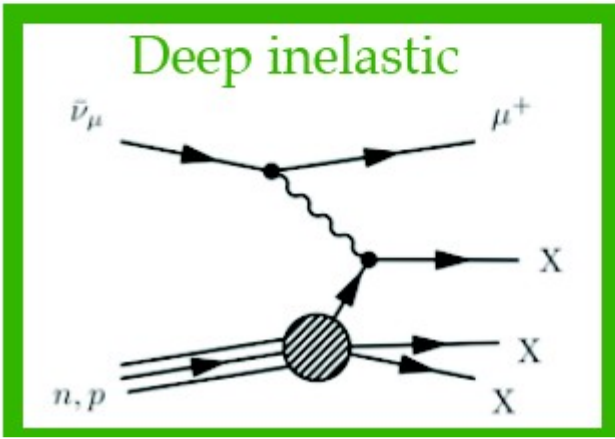
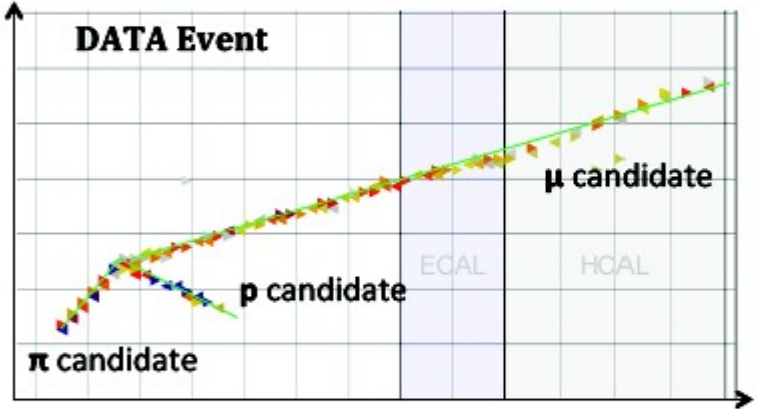
Scintillator tracker:  
Hydrocarbon (CH) target  
Homogeneous non-magnetized active tracker



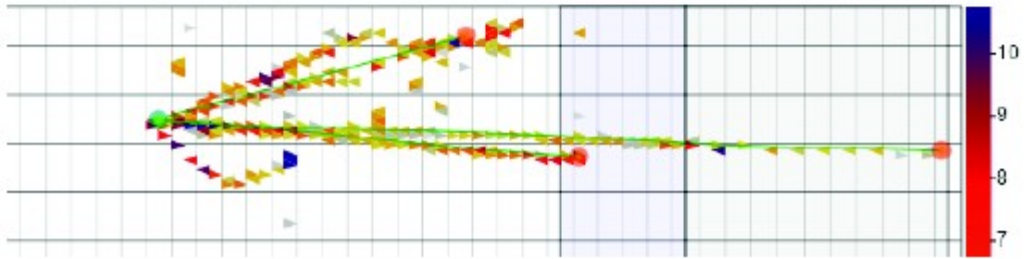
**QE**

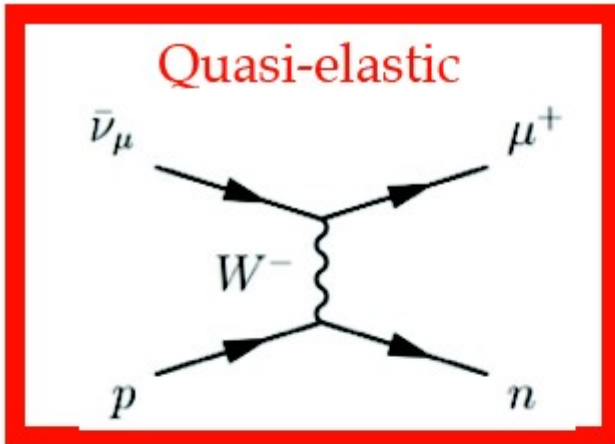


**RES**

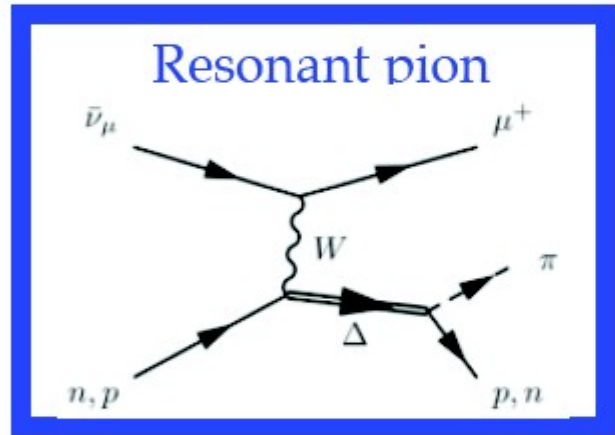


**DIS**

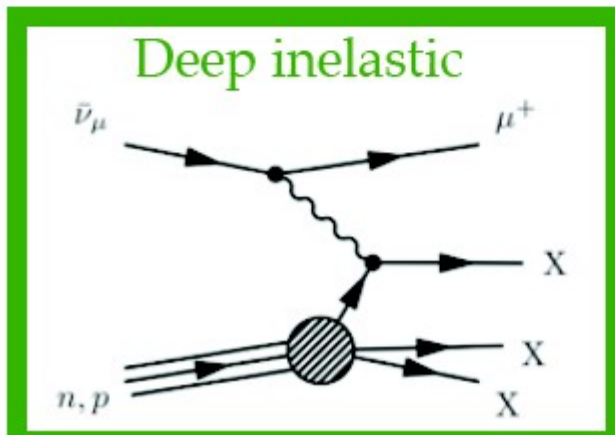




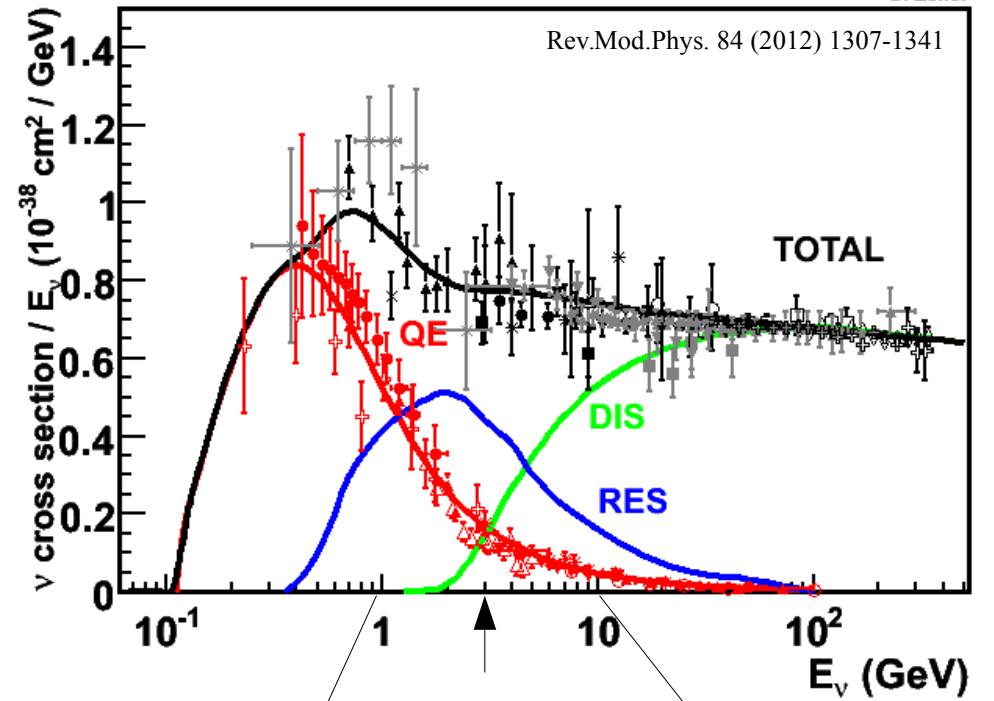
**QE**



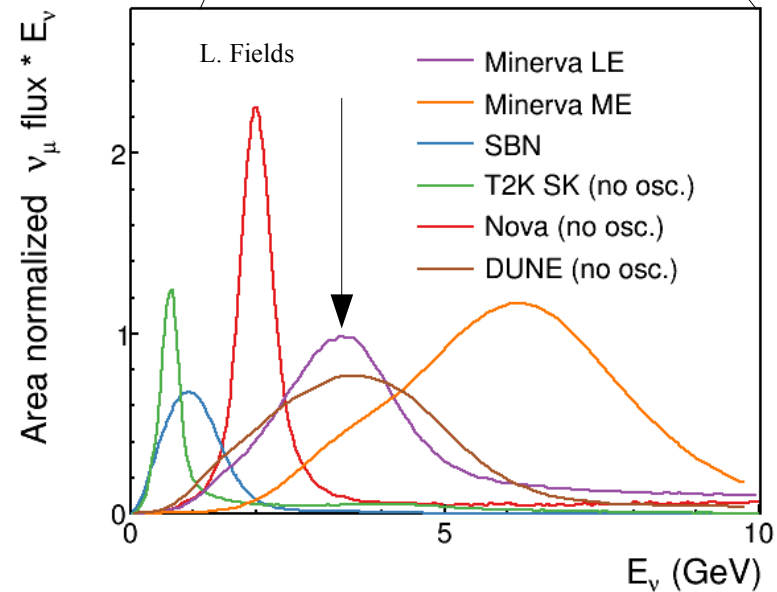
**RES**



**DIS**

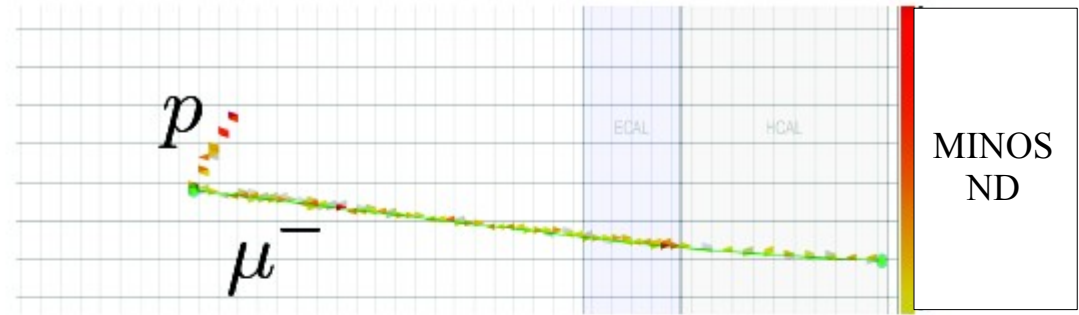


NuMI low energy beam  $\langle E_\nu \rangle \sim 3 \text{ GeV}$



Today's topic:

## $\mu$ -p mesonless production



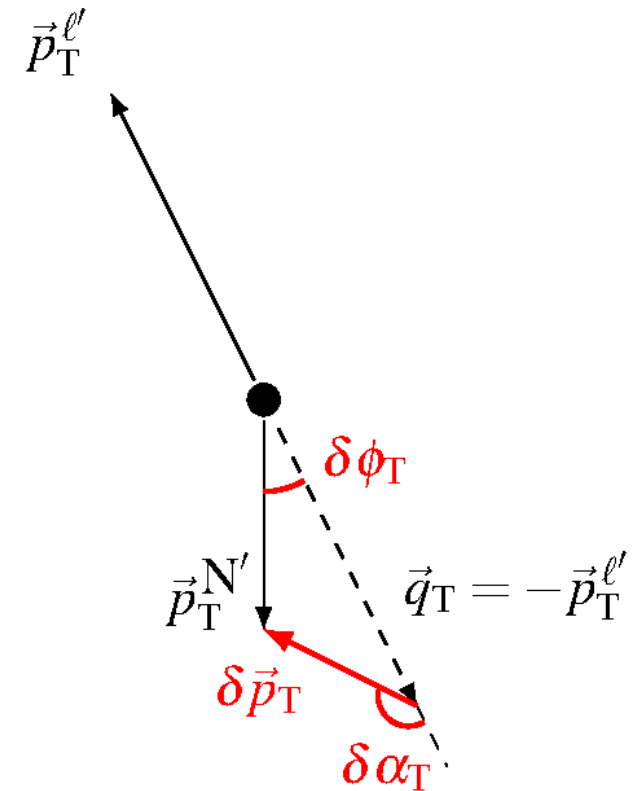
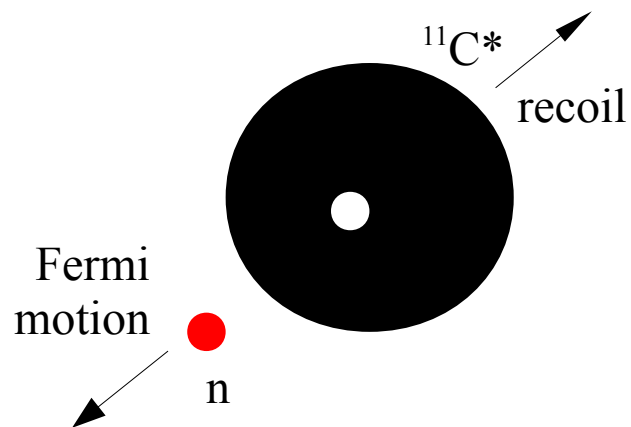
### Observables:

- **Transverse kinematics imbalances**

[XL, L. Pickering, S. Dolan *et al.*, Phys.Rev. C94 (2016) no.1, 015503]

- **Initial neutron momentum**

[A. Furmanski, J. Sobczyk, Phys.Rev. C95 (2017) no.6, 065501]



# *A brief history of Shadow Art*



[https://en.wikipedia.org/wiki/Cave\\_painting](https://en.wikipedia.org/wiki/Cave_painting)

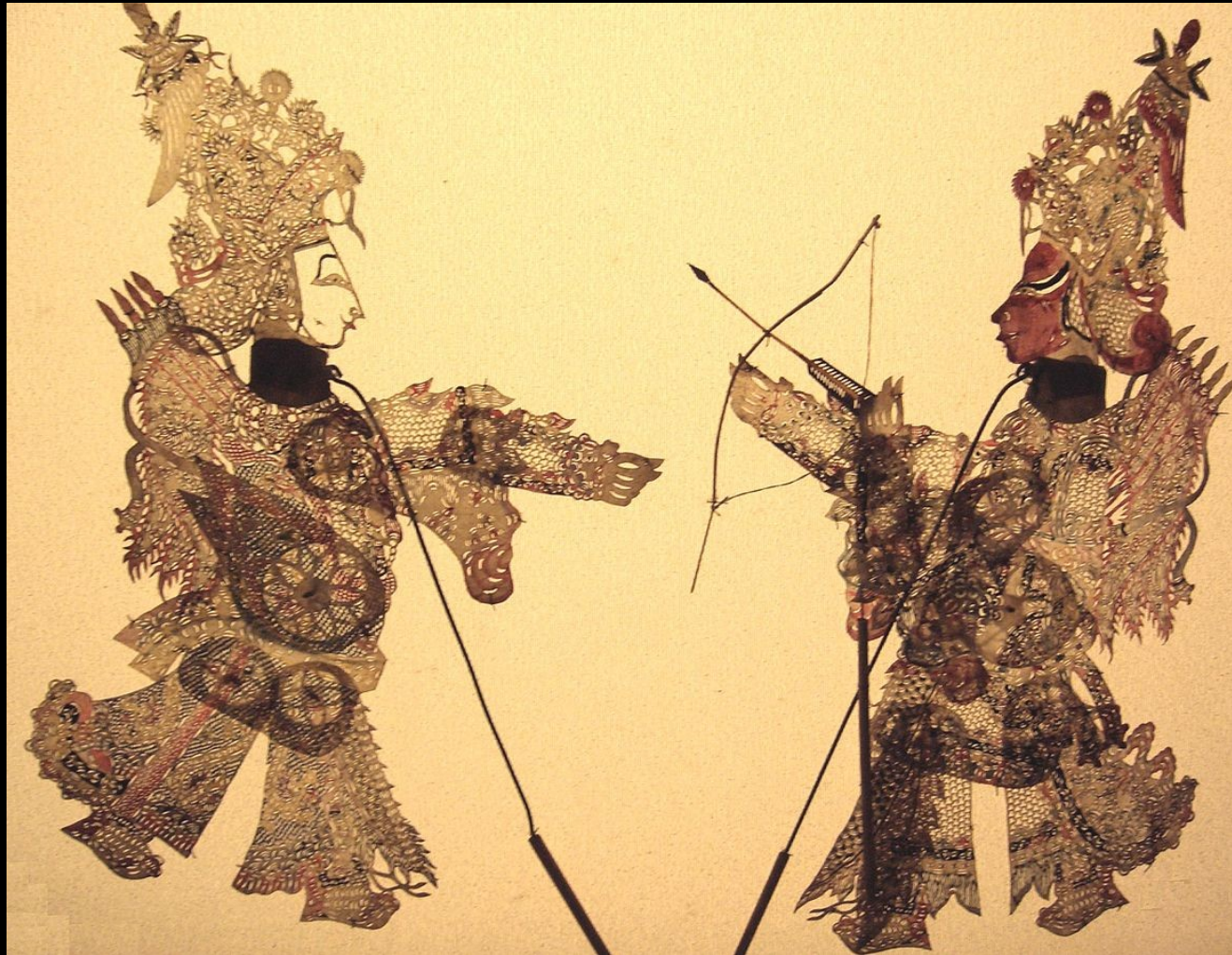
Cave of Pettakere, Bantimurung district (kecamatan), South Sulawesi,  
**Indonesia**. Hand stencils estimated between **35,000-40,000 BP**

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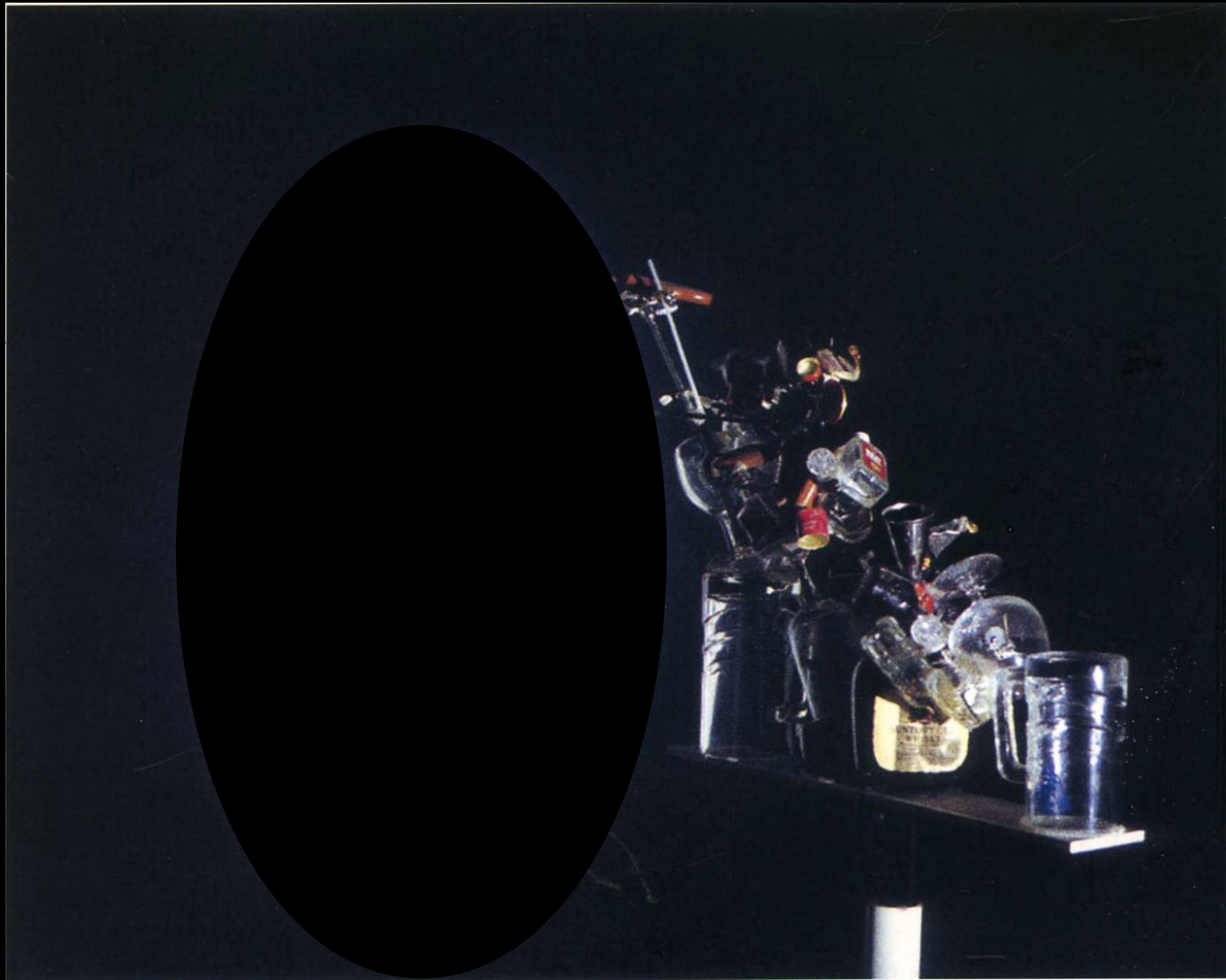


<https://zh.wikipedia.org/wiki/%E7%9A%AE%E5%BD%B1%E6%88%B2>

**Traditional Chinese “movie”**



# *A brief history of Shadow Art*



<http://www.spoon-tamago.com/2015/08/03/illusionistic-shadow-art-by-shigeo-fukuda/>

**Japanese modern art**

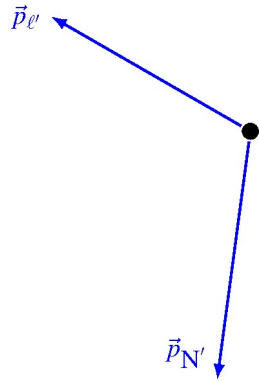
# *A brief history of Shadow Art*



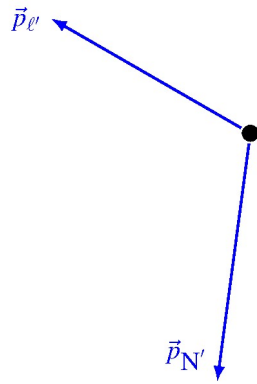
<http://www.spoon-tamago.com/2015/08/03/illusionistic-shadow-art-by-shigeo-fukuda/>

**Japanese modern art**

# Transverse kinematic imbalances – *a neutrino shadow play*



# Transverse kinematic imbalances – a neutrino shadow play



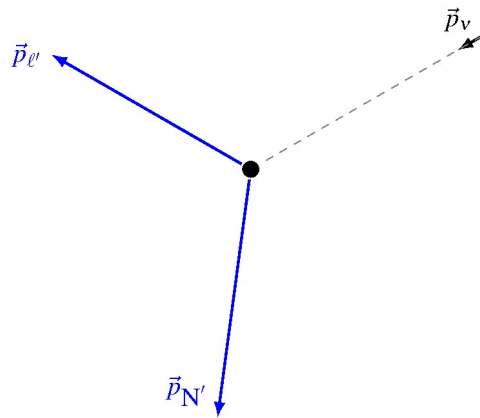
Source: <http://zhejiangpiying.sokutu.com/tupian.html>



To make *Neutrino Shadow Play*, we need

- ✓ beam of light
- ✓ screen

# Transverse kinematic imbalances – a neutrino shadow play



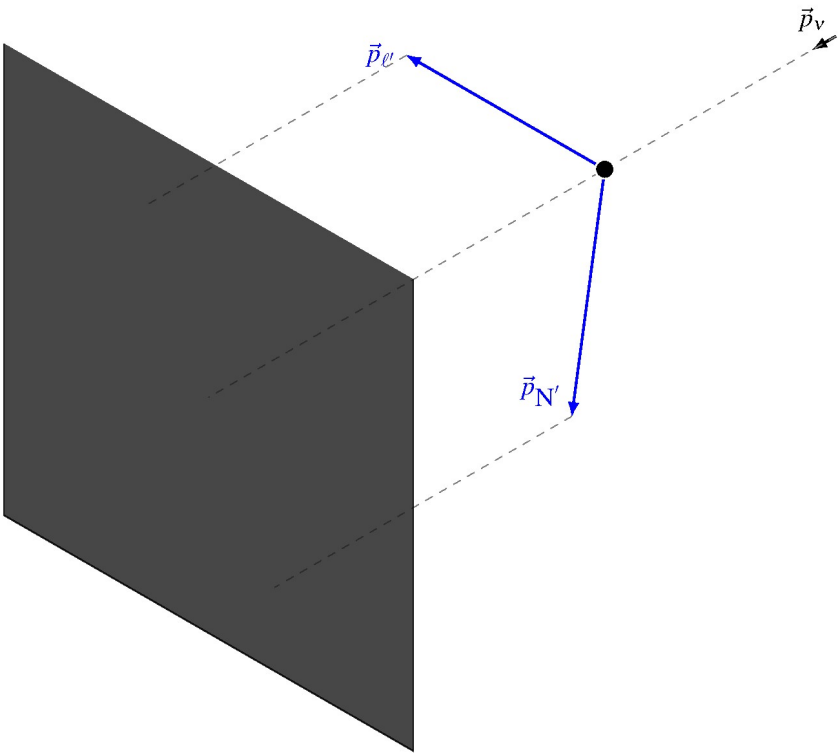
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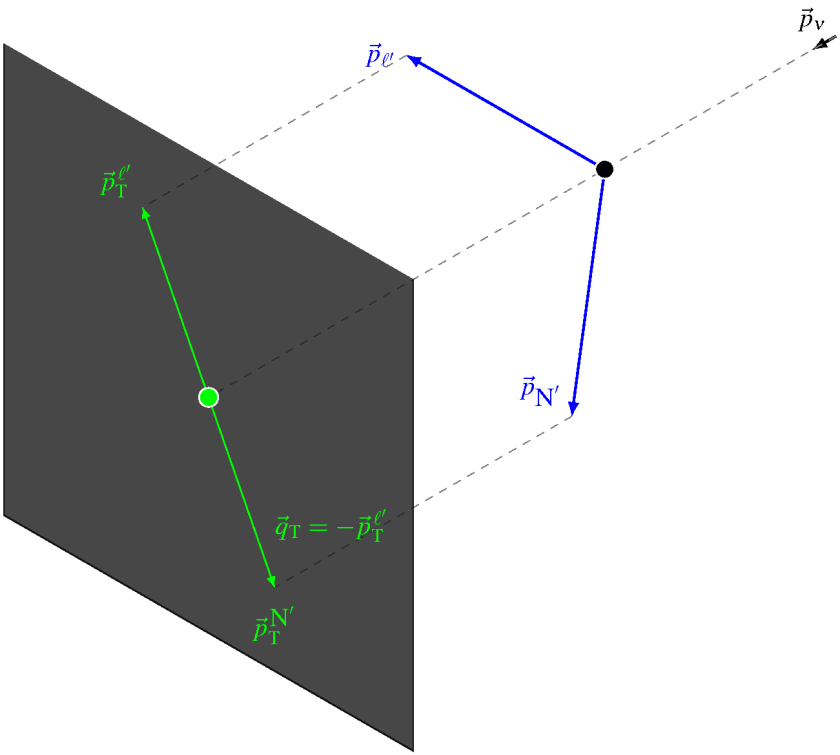


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- To make *Neutrino Shadow Play*, we need
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  - ✓ screen → transverse plane

# Transverse kinematic imbalances – a neutrino shadow play



Static nucleon target

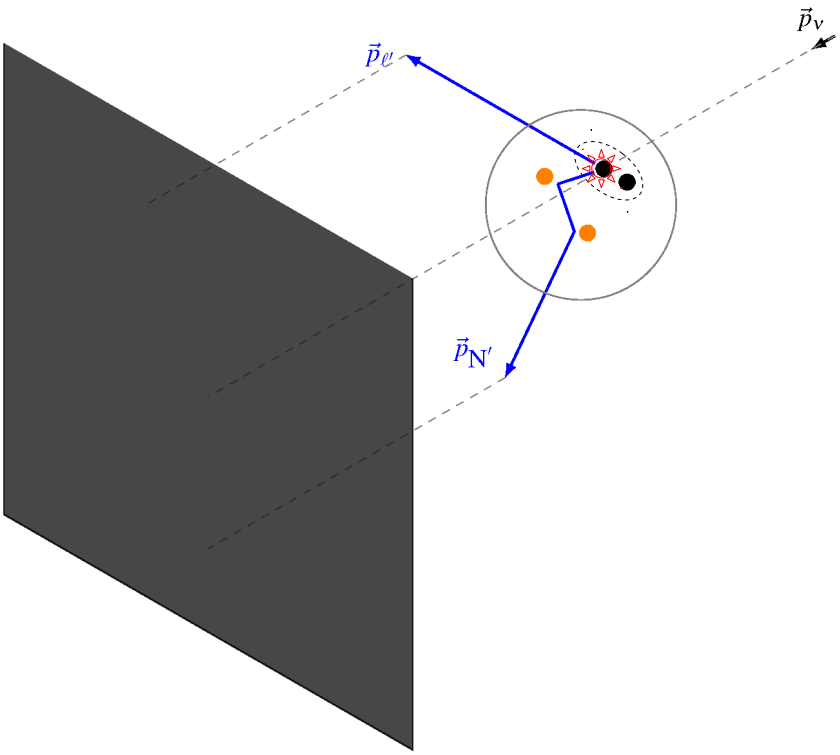


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# Transverse kinematic imbalances – a neutrino shadow play



Nuclear target



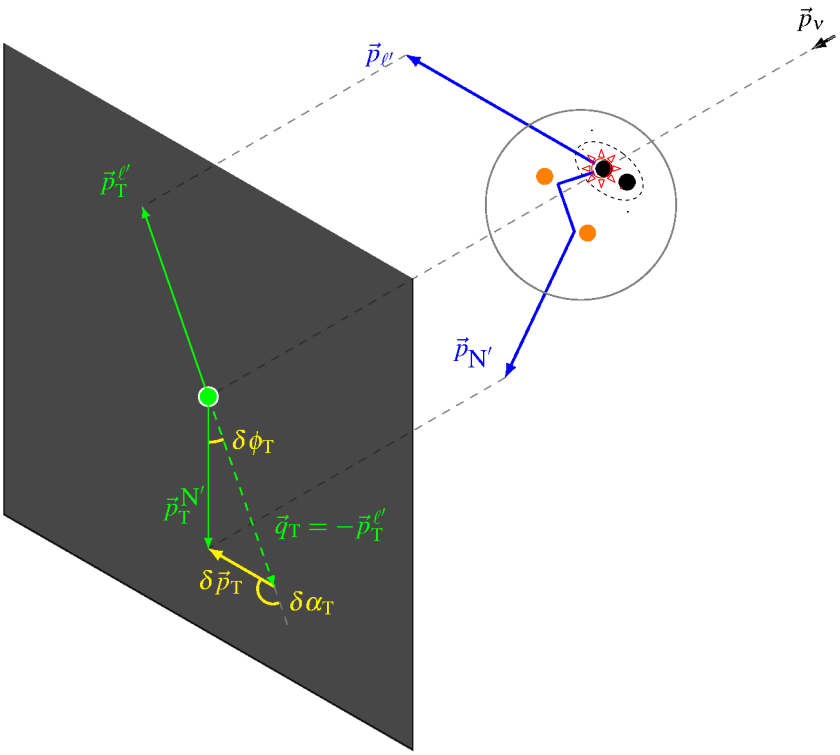
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To make *Neutrino Shadow Play*, we need  
✓ beam of light → accelerator  
✓ screen → transverse plane



# Transverse kinematic imbalances – a neutrino shadow play



Nuclear target



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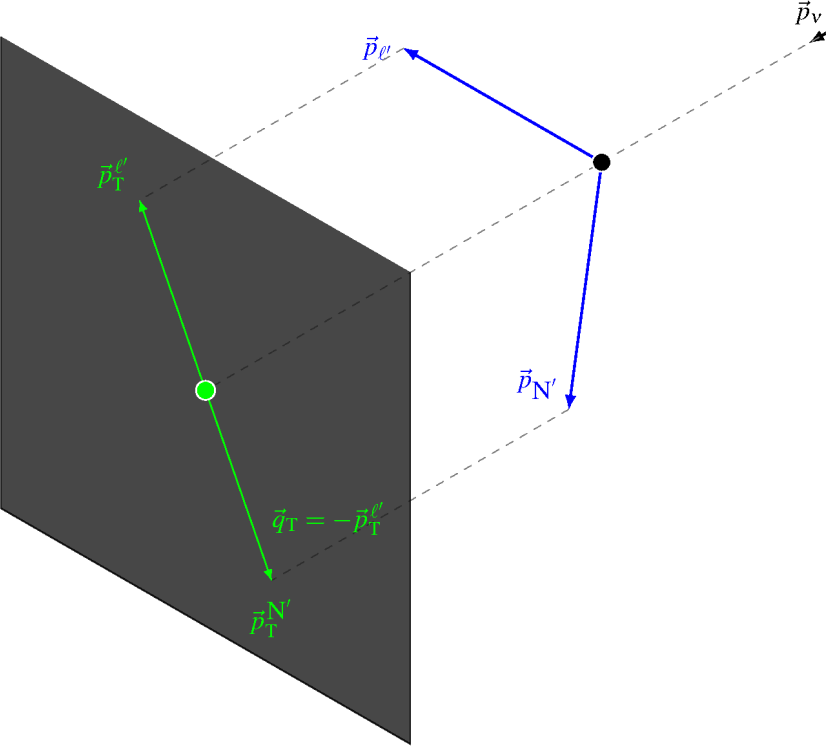


To make *Neutrino Shadow Play*, we need  
 ✓ beam of light → accelerator  
 ✓ screen → transverse plane

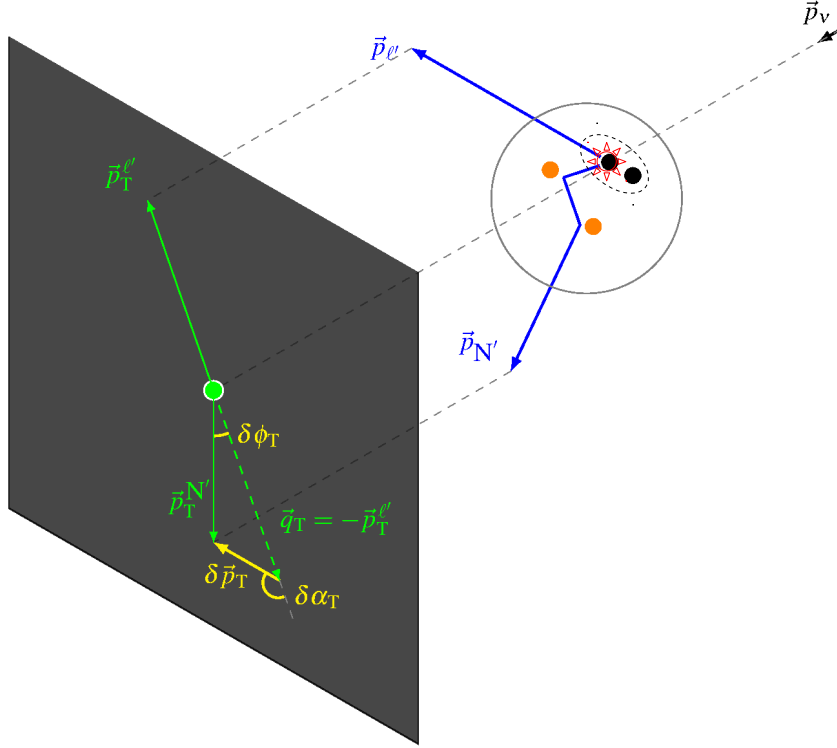
# Transverse kinematic imbalances – a neutrino shadow play

$$\delta \vec{p}_T = \vec{p}_T^N - \Delta \vec{p}_T$$

Convolution of Fermi motion and intra-nuclear momentum transfer due to FSI, resonance production, 2p2h etc.



Static nucleon target



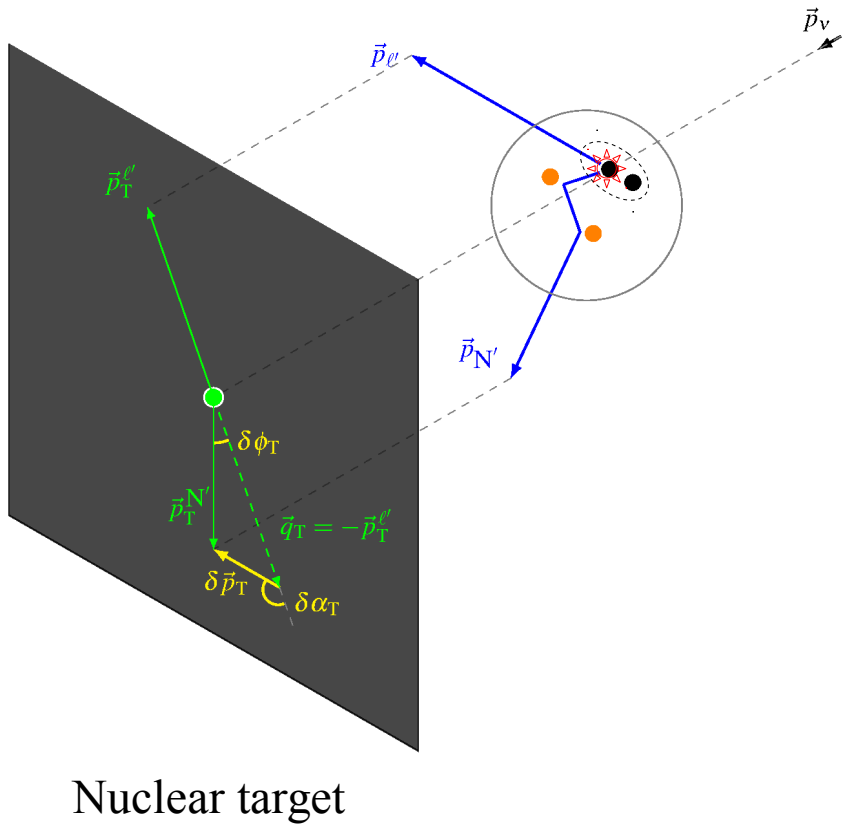
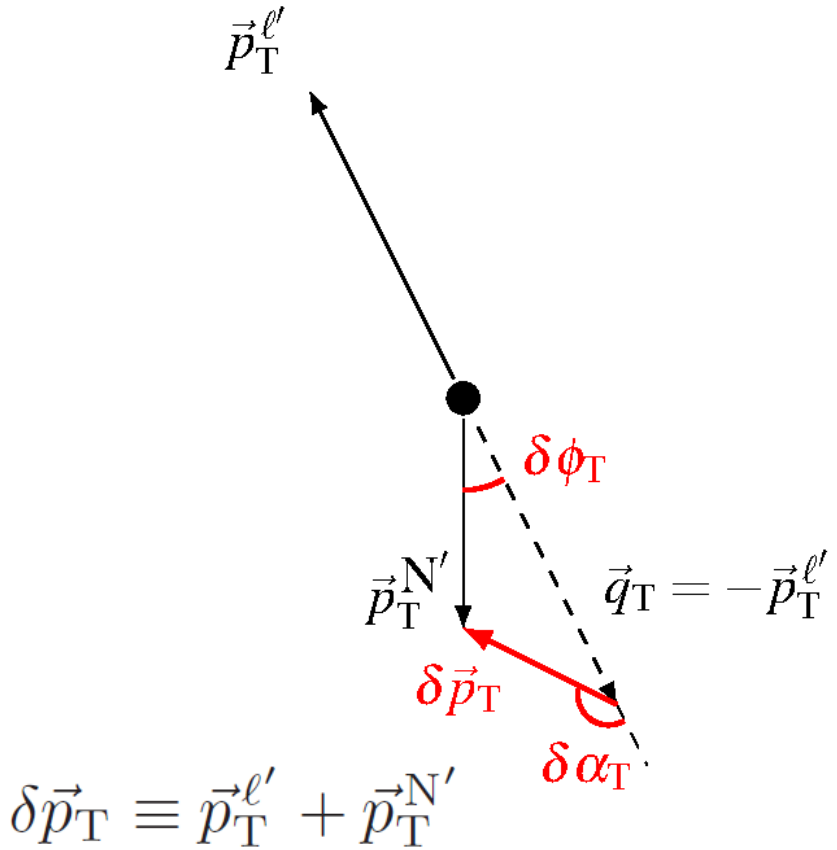
Nuclear target

XL, L. Pickering, S. Dolan *et al.*, Phys.Rev. C94 (2016) no.1, 015503

# Transverse kinematic imbalances – a neutrino shadow play

$$\delta \vec{p}_T = \vec{p}_T^N - \Delta \vec{p}_T$$

Convolution of Fermi motion and intra-nuclear momentum transfer due to FSI, resonance production, 2p2h etc.



XL, L. Pickering, S. Dolan *et al.*, Phys.Rev. C94 (2016) no.1, 015503

# EXTENSION: RADICAL SOLUTION TO NUCLEAR EFFECT PROBLEM

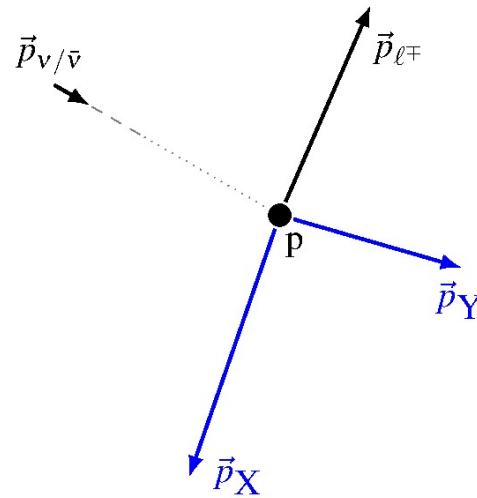
Lepton-proton interaction  $\rightarrow$  3 charged particles:  $l p \rightarrow l' X Y$

– Leading order realization in standard model:

$\{X, Y\}$

=  $\{p, \pi^+\}$  for  $\nu + p \rightarrow \ell^- + \Delta^{++}$

or  $\{p, \pi^-\}$  for  $\bar{\nu} + p \rightarrow \ell^+ + \Delta^0$



XL *et al.*, Phys.Rev. D92 (2015) no.5, 051302

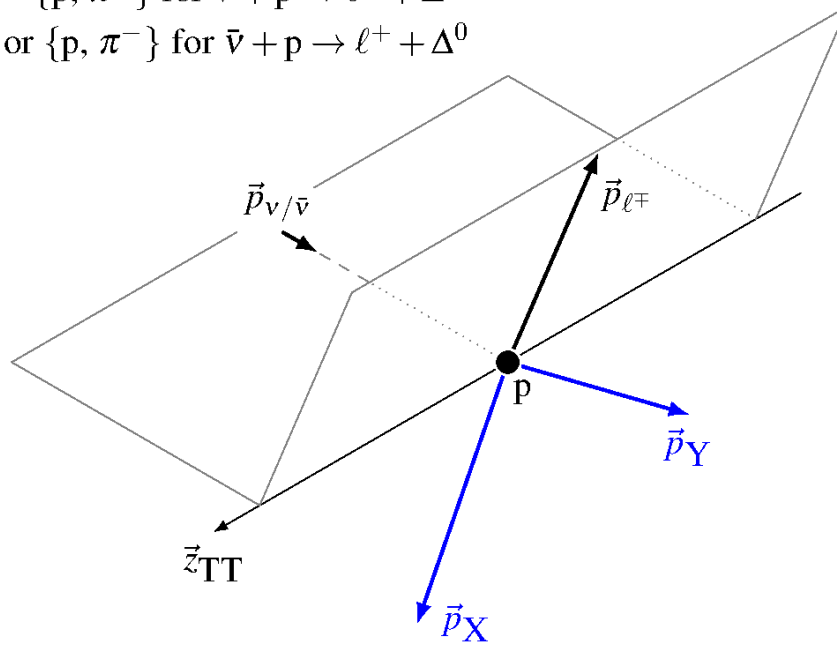
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XL *et al.*, Phys.Rev. D92 (2015) no.5, 051302

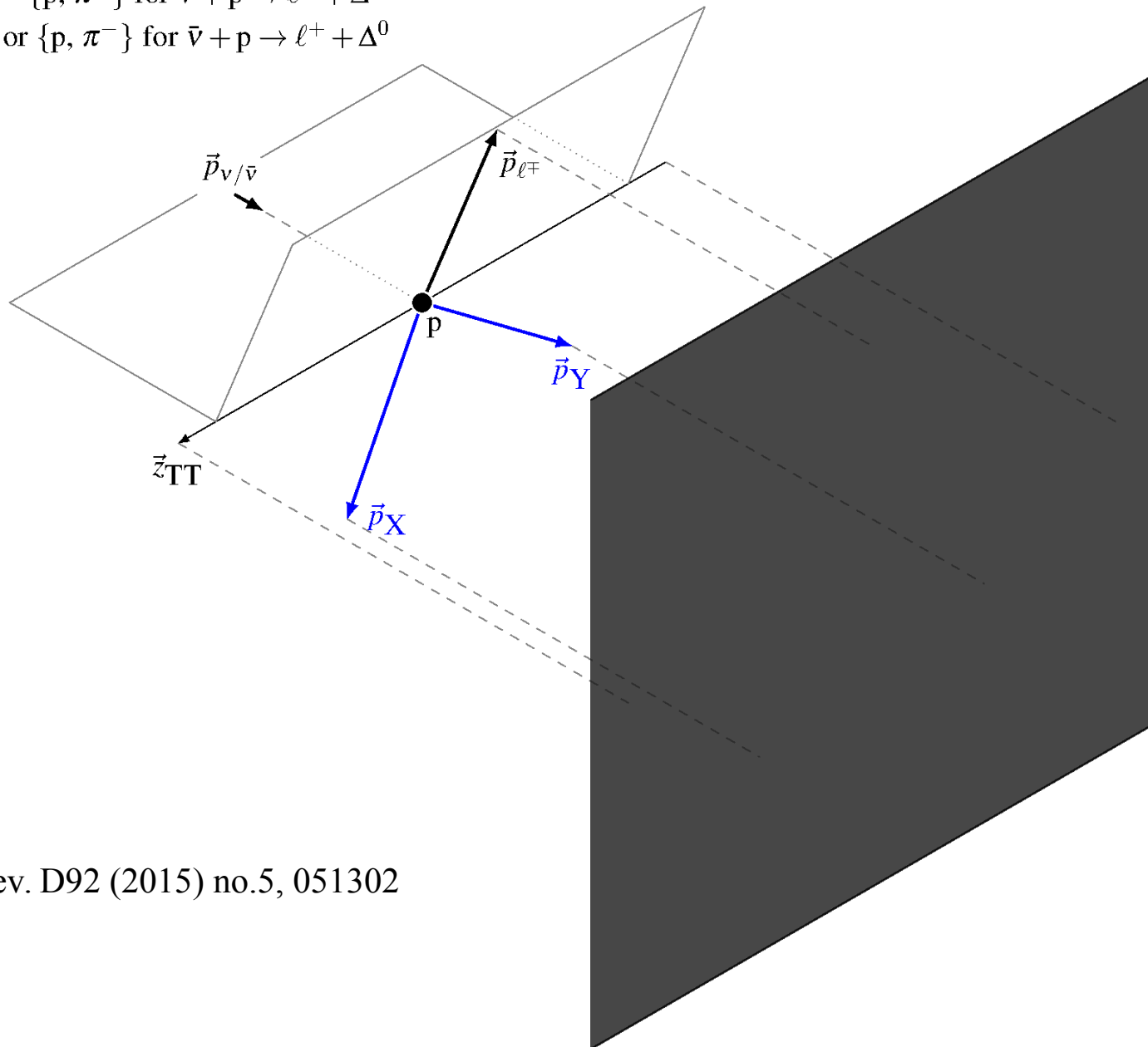
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XL *et al.*, Phys.Rev. D92 (2015) no.5, 051302

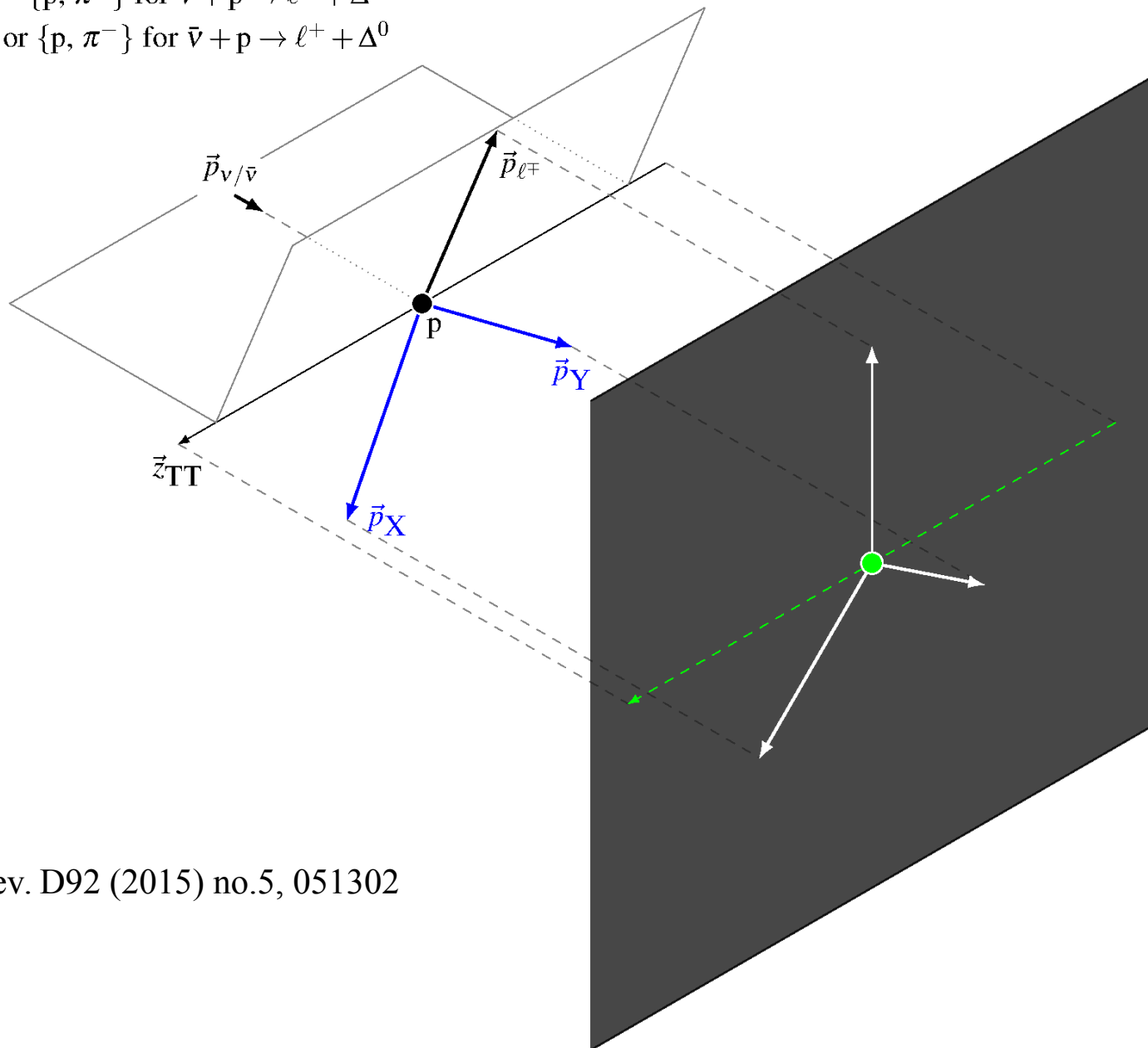
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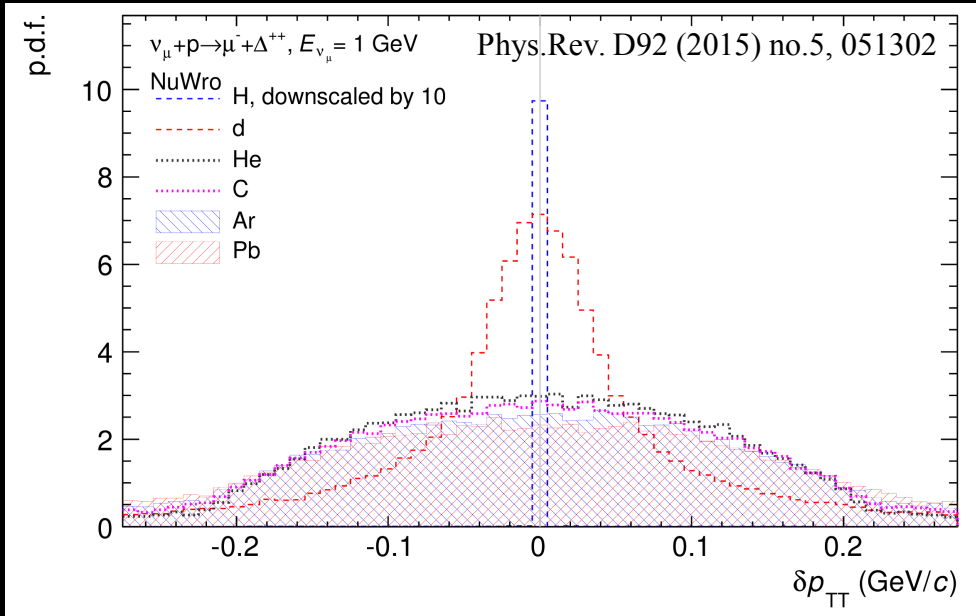
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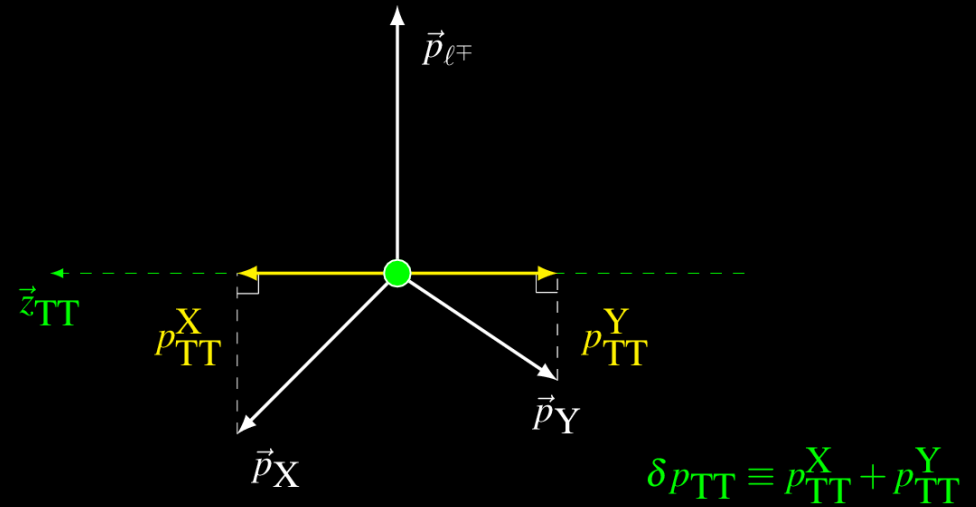


XL *et al.*, Phys.Rev. D92 (2015) no.5, 051302





$\{X, Y\}$   
 $= \{p, \pi^+\}$  for  $\nu + p \rightarrow \ell^- + \Delta^{++}$   
 or  $\{p, \pi^-\}$  for  $\bar{\nu} + p \rightarrow \ell^+ + \Delta^0$

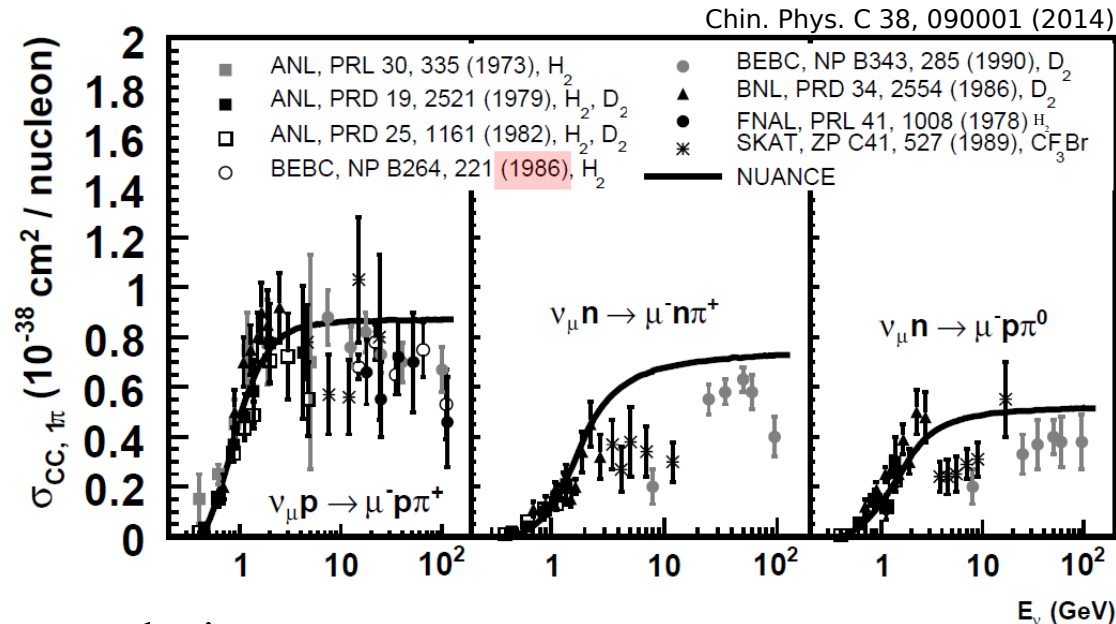


### Double-transverse momentum imbalance $\delta p_{TT}$

- H: 0
- Heavier nuclei: irreducible symmetric broadening
  - by Fermi motion  $O(200$  MeV)
  - further by FSI
- $CH_n$ : Hydrogen shape is only detector smearing.
  - With good detector resolution, hydrogen yield can be extracted.
  - With very good res., event-by-event selection of  $\nu$ -H interaction is possible.

- Pure hydrogen

- Technical requirement: bubble chamber (historical: 73, 79, 78, 82, 86)



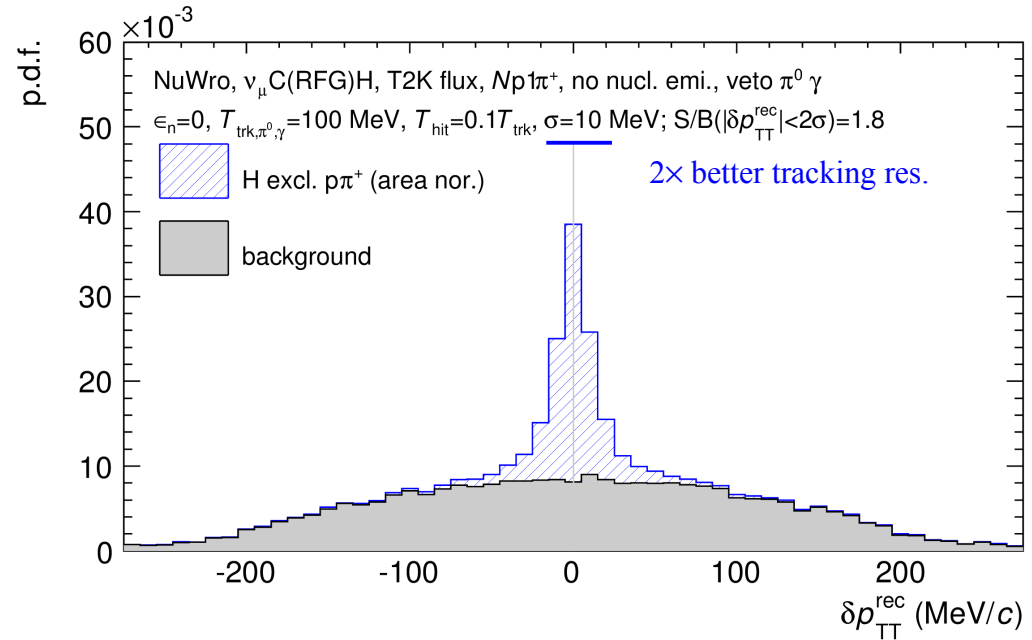
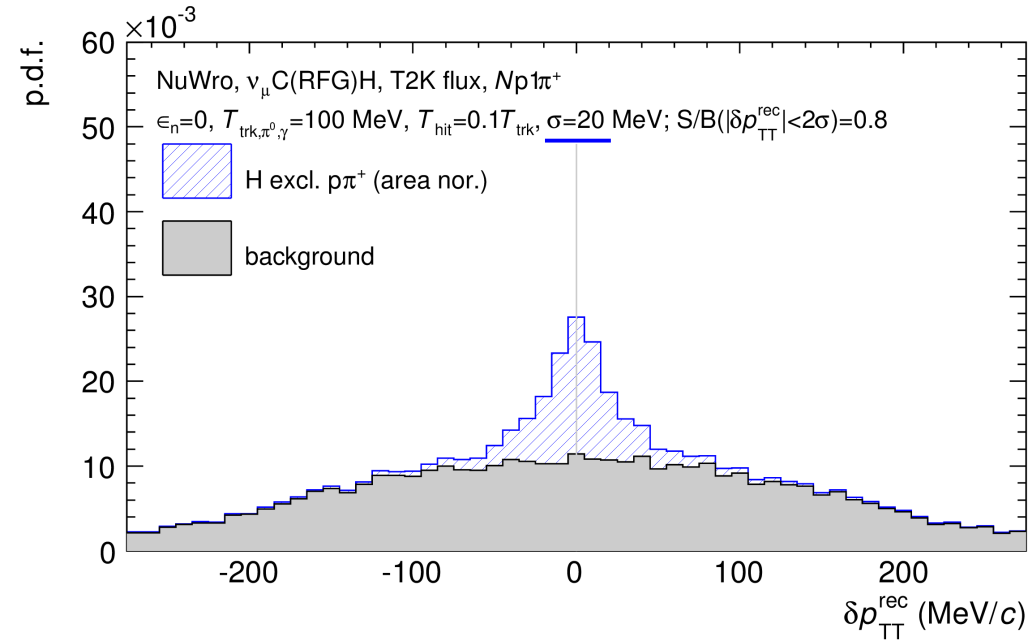
- Safety issue: explosive

- “Since the use of a liquid H<sub>2</sub> bubble chamber is excluded in the ND hall **due to safety concerns**, ...” [FERMILAB-PUB-14-022]

- Neutrino interactions on hydrogen:

- In the last ~30 years there has been no new measurement
- Nuclear-effect independent measurement of neutrino energy

# Extracting neutrino-hydrogen events from CH targets



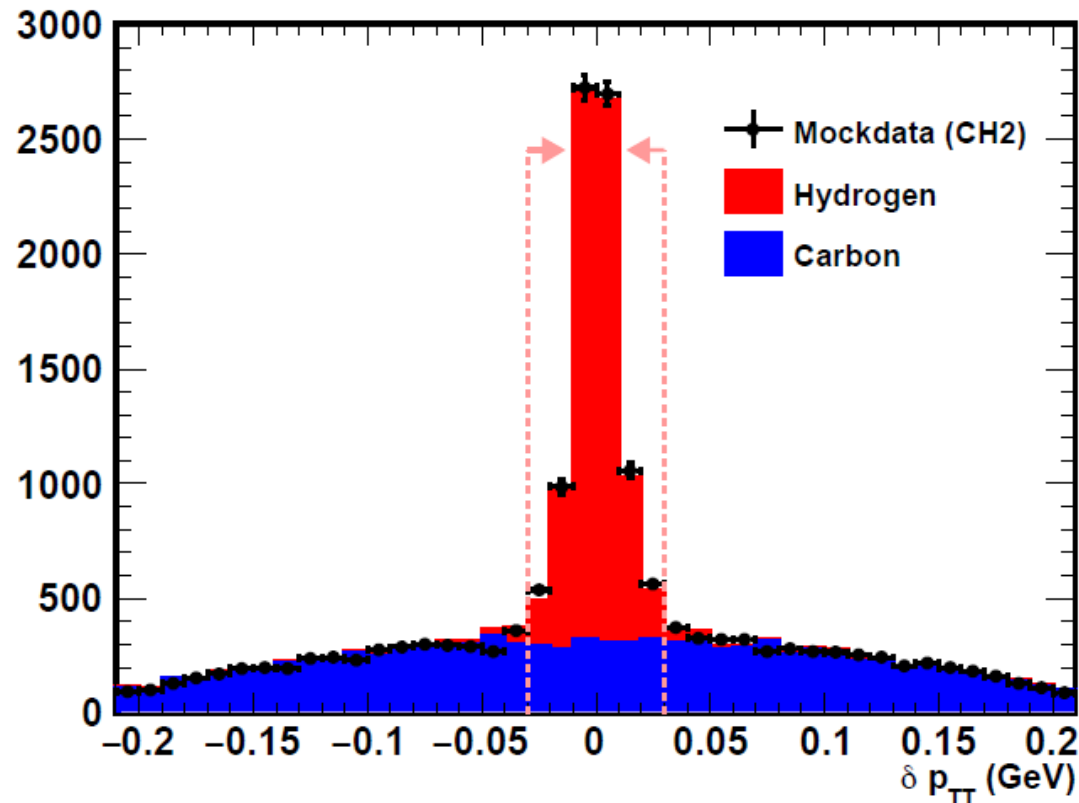
arXiv:1512.09042

Toy simulation of T2K performance

- T2K neutrino flux on CH target
- Realistic detector resolution

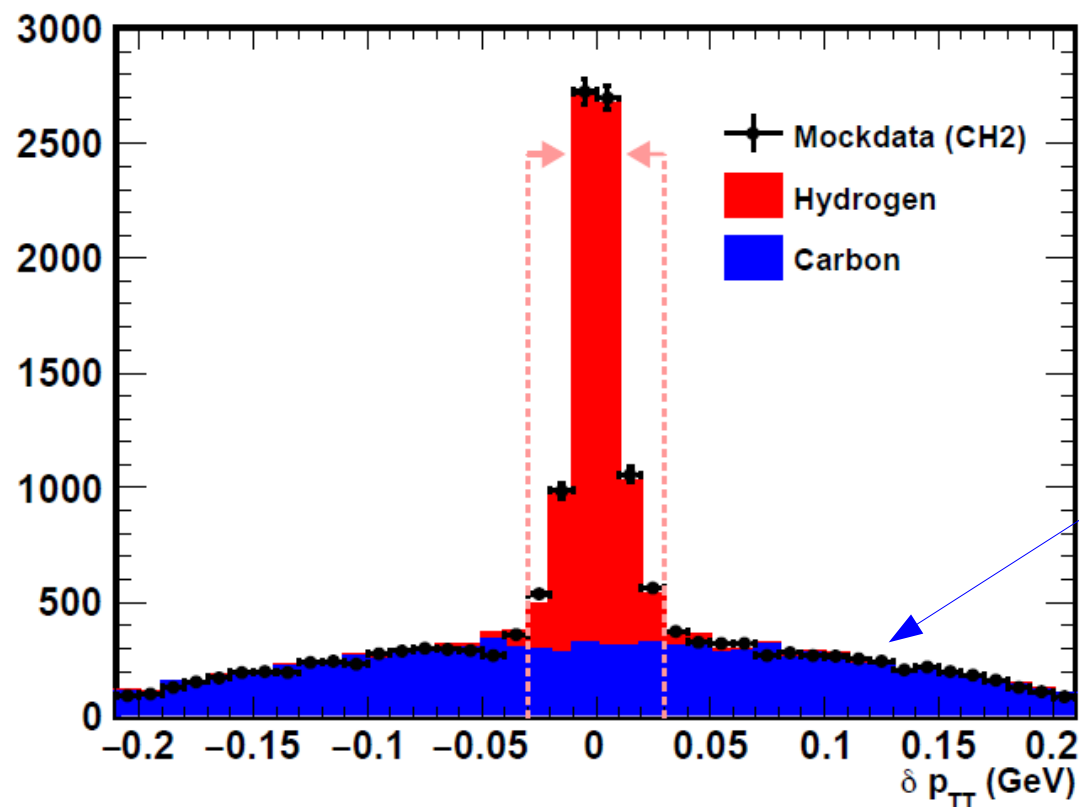
## Hydrogen Events Selection and Background Normalization

Slide from  
**Hongyue Duyang**  
 U. of South Carolina



- ▶ Select 3-track ( $\mu^- p \pi^+$ ) events with  $W_{rec} < 1.4$  GeV (RES region).
- ▶ Signal region:  $|\delta p_{TT}| < 0.03$  GeV. Background region:  $|\delta p_{TT}| > 0.03$  GeV.
- ▶ Normalize signal and background to mockdata.
- ▶ Purity is  $\sim 77\%$  in signal region.

## Hydrogen Events Selection and Background Normalization



Slide from  
**Hongyue Duyang**  
 U. of South Carolina

Background shape:  
 constrained by  
**multiple nuclear**  
**targets**, especially  
 carbon (graphite)

- ▶ Select 3-track ( $\mu^- p \pi^+$ ) events with  $W_{rec} < 1.4$  GeV (RES region).
- ▶ Signal region:  $|\delta p_{TT}| < 0.03$  GeV. Background region:  $|\delta p_{TT}| > 0.03$  GeV.
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END OF EXTENSION  
BACK TO  
NUCLEAR EFFECT MEASUREMENT

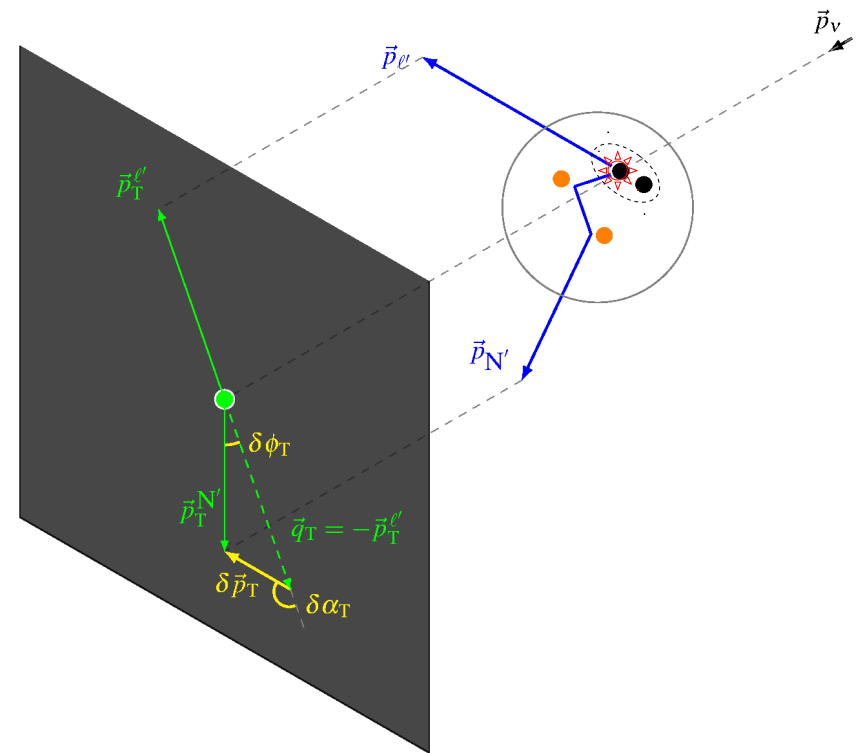
A more general analysis of kinematic imbalance

Transverse:  $0 = \vec{p}_T^{\ell'} + \vec{p}_T^{N'} - \delta\vec{p}_T$

Longitudinal:  $E_\nu = p_L^{\ell'} + p_L^{N'} - \delta p_L$

New variable:  $p_n \equiv \sqrt{\delta p_T^2 + \delta p_L^2}$

Neutrino energy is unknown (in the first place), equations are not closed.



A. Furmanski, J. Sobczyk, Phys.Rev. C95 (2017) no.6, 065501

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Assuming exclusive  $\mu$ -p-A' final states

Use energy conservation to close the equations

$$E_\nu + m_A = E_{\ell'} + E_{N'} + E_{A'}$$

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$p_n$ : recoil momentum of the nuclear remnant



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For CCQE,  $A' = {}^{11}\text{C}^*$   
 No more unknowns  
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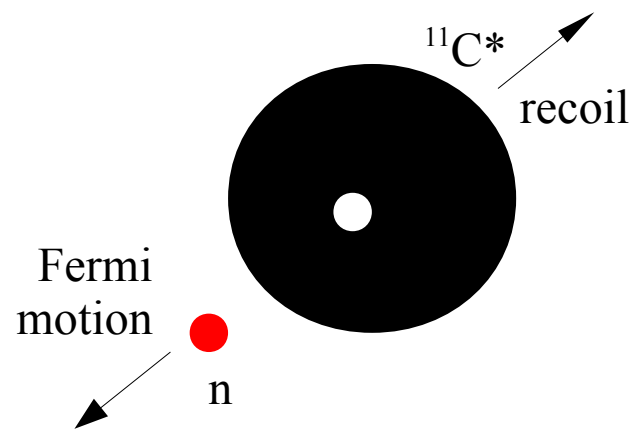
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$$p_L = \frac{1}{2}(M(A) + k'_L + p'_L - E' - E_{p'}) - \frac{p_T^2 + M^*(A-1)^2}{2(M(A) + k'_L + p'_L - E' - E_{p'})}$$

A. Furmanski, J. Sobczyk, Phys.Rev. C95 (2017) no.6, 065501

Xianguo Lu, Oxford

# Measurement of final-state correlations in neutrino charged-current muon-proton mesonless production on hydrocarbon at $\langle E_\nu \rangle = 3 \text{ GeV}$

## Signal definition:

- Charged current
- One muon and at least one proton in the restricted final-state phase space
- No mesons

$$1.5 \text{ GeV}/c < p_\mu < 10 \text{ GeV}/c, \theta_\mu < 20^\circ,$$
$$0.45 \text{ GeV}/c < p_p < 1.2 \text{ GeV}/c, \theta_p < 70^\circ$$

## Measurement:

Data sample: NuMI low energy neutrino data,  $3.28 \times 10^{20}$  POT

Interaction target: tracker (mostly CH)

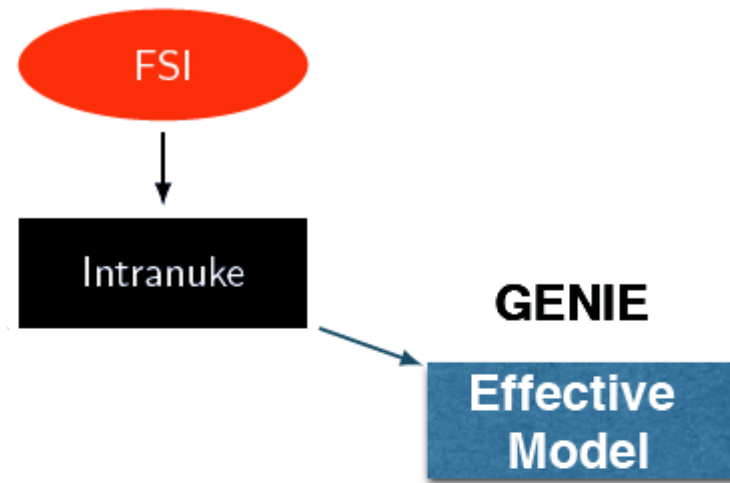
- Event selection
- Background estimation and subtraction
- Unfolding
- Efficiency correction

➤ Flux integrated cross section as results

➔ Focus today

# Simulation: GENIE [Nucl.Instrum.Meth. A614 (2010) 87-104]

- **Nominal:** version 2.8.4
  - ✓ global Fermi Gas (RFG) model with Bodek-Ritchie (BR) tail [Phys. Rev. D 23, 1070 (1981)]
  - ✓ hA FSI [AIP Conf.Proc. 1405 (2011) 213-218]
- **No-FSI:** Nominal without FSI

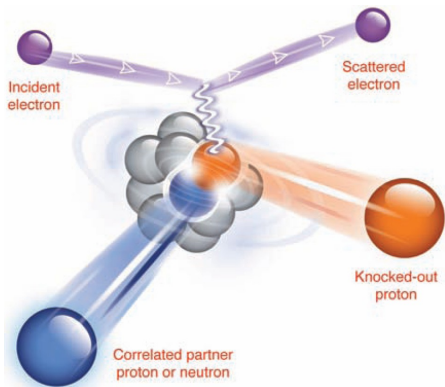


- INC-like with one “effective” interaction
- tuned do hadron-nucleus data
- easy to reweight

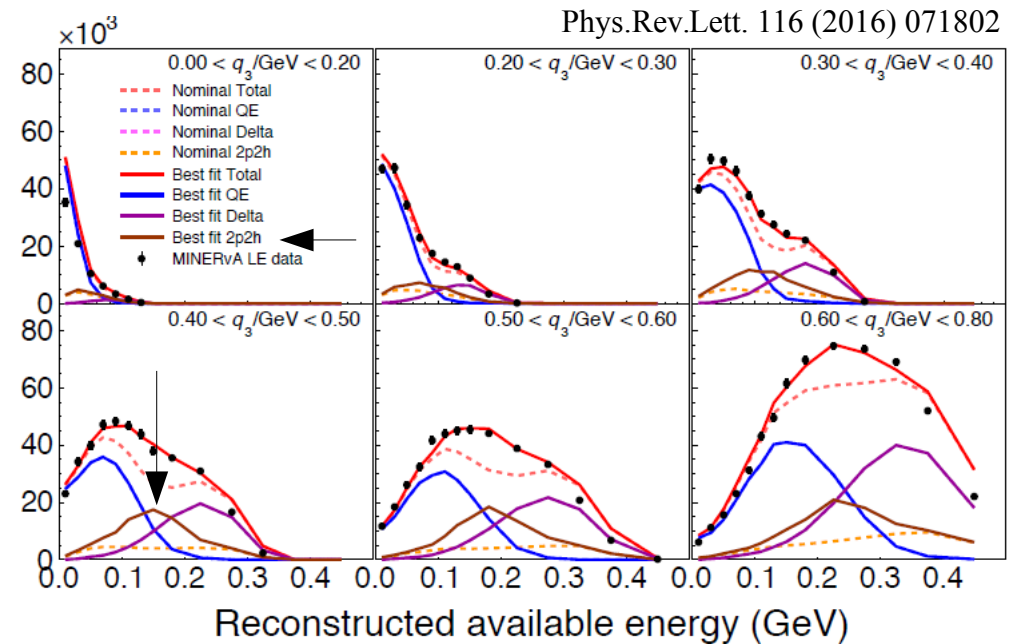
**courtesy of Tomasz Golan**

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  - Added Random Phase Approximation (RPA) [Phys.Rev. C70 (2004) 055503]
  - Non-resonance pion production scaled down by 75% [Phys.Rev. D90 (2014) no.11, 112017]
  - **Valencia 2p2h** [Nieves *et al.*, Phys.Lett. B707 (2012) 72-75, Phys. Rev. C 86, 015504 (2012), Phys.Rev. D88 (2013) no.11, 113007, arXiv:1601.02038]
  - ✓ **tuned to MINERvA inclusive data** → significant enhancement in small 4-momentum transfer region [Phys.Rev.Lett. 116 (2016) 071802]



Science 320 (2008) 1476-1478



→ representing energy transfer from the neutrino to the target

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  - ✓ global Fermi Gas (RFG) model with Bodek-Ritchie (BR) tail [Phys. Rev. D 23, 1070 (1981)]
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  - ✓ tuned to MINERvA inclusive data → significant enhancement in small 4-momentum transfer region [Phys.Rev.Lett. 116 (2016) 071802]

## Detector simulation: GEANT4 (4.9.2)

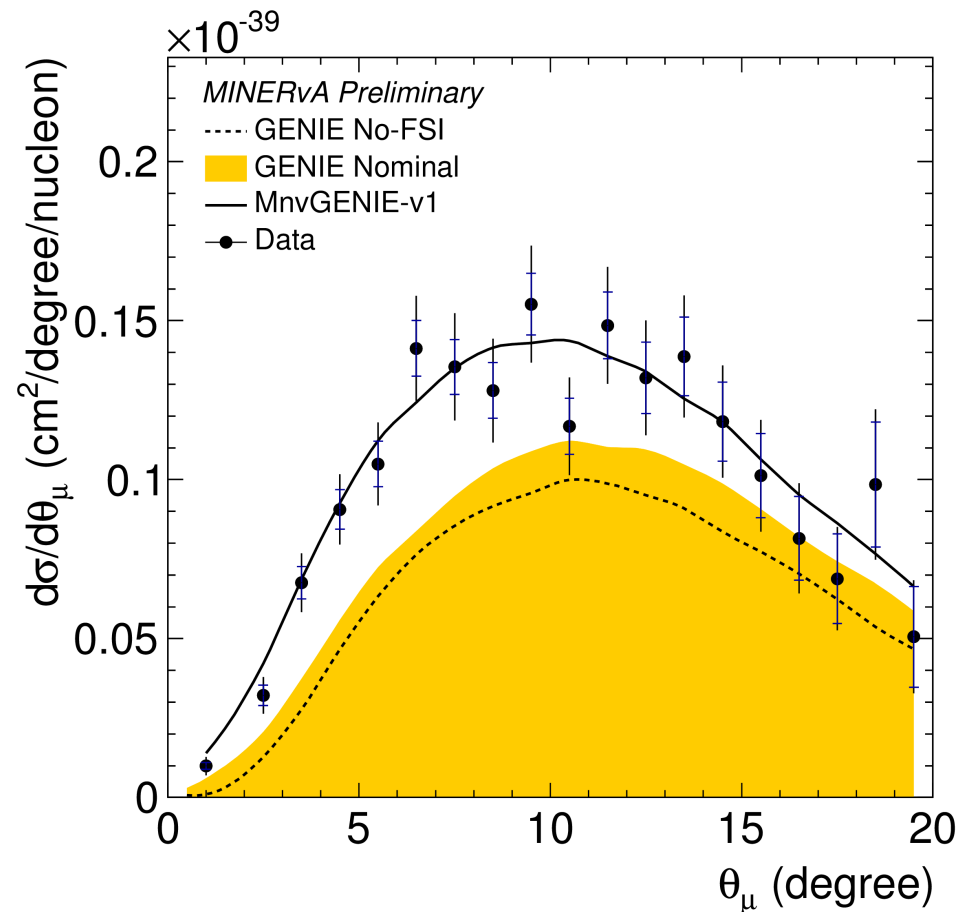
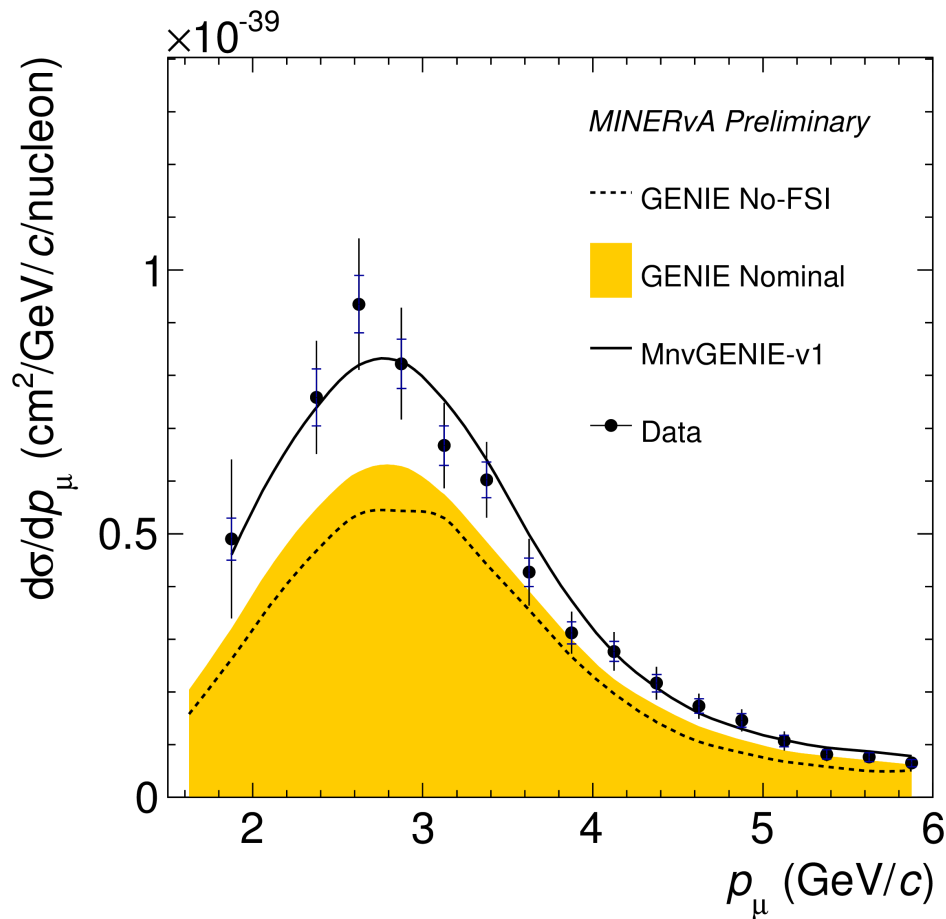
GENIE used in other experiments (e.g. NOvA, T2K,  $\mu$ BooNE, DUNE)

This analysis:  
GENIE MINERvA Tune (v1) used in cross section extraction

# RESULTS: Flux integrated cross section

# Single-Particle Kinematics

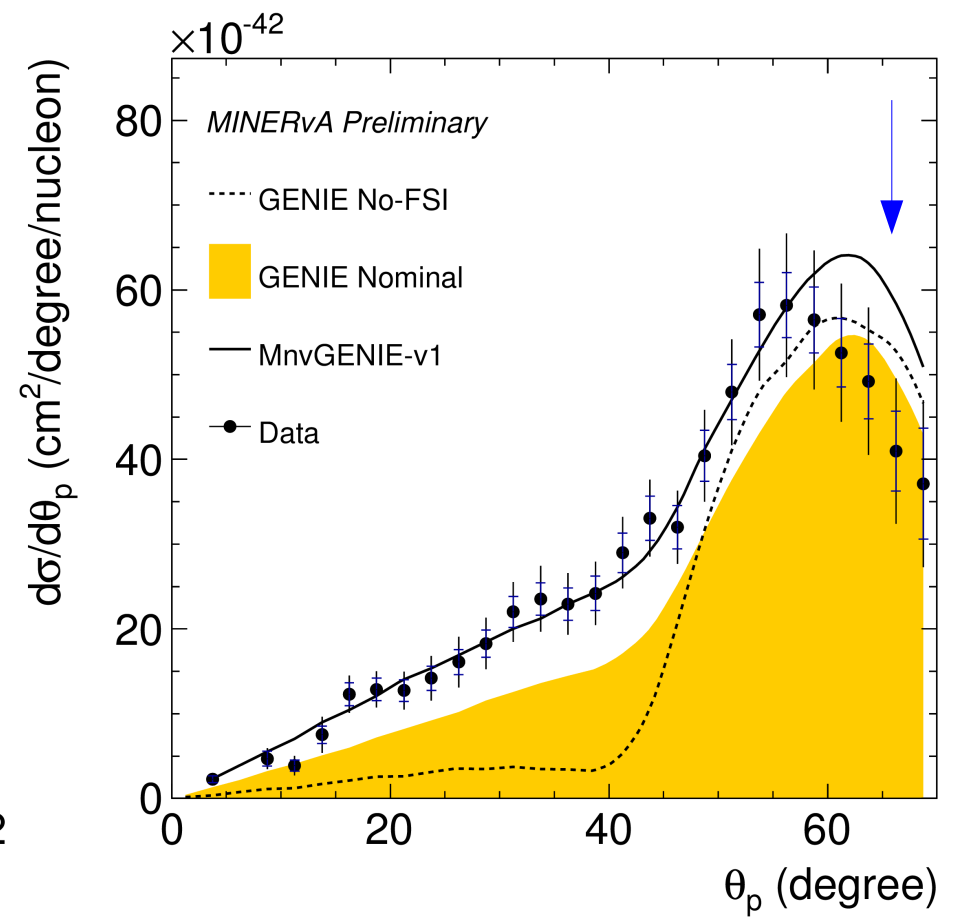
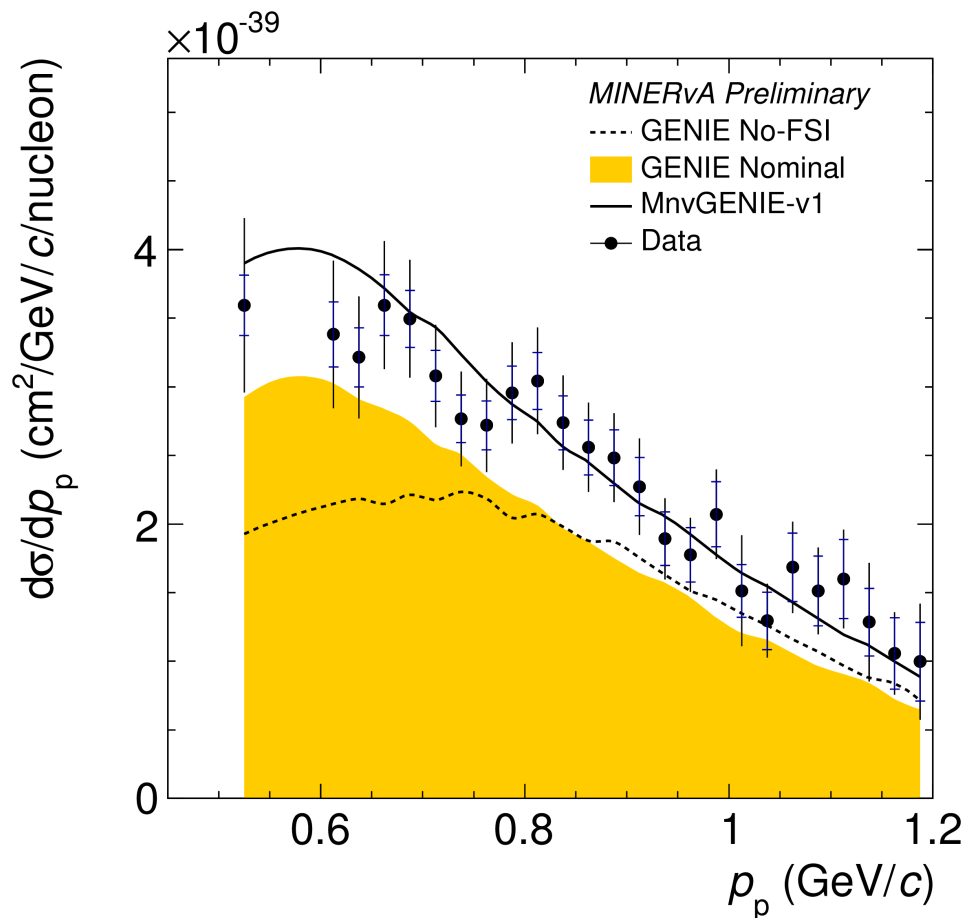
- Muon momentum, angle



- Good description by GENIE MINERvA Tune (v1)
- All predictions have same shape

# Single-Particle Kinematics

- Muon momentum, angle
- Proton momentum, angle



- GENIE Nominal and No-FSI have different shape
- GENIE MINERvA Tune (v1) excess at high angle



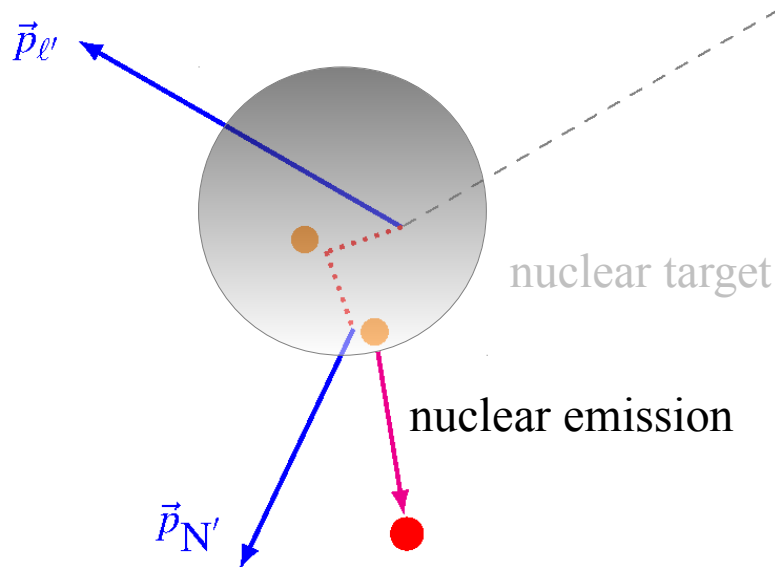
FSI decomposition in mesonless proton production:

**Proton FSI:**

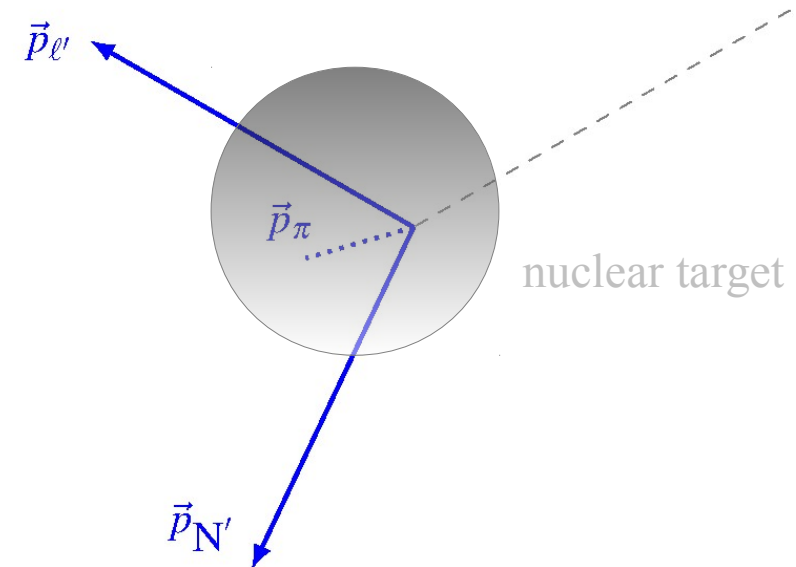
- Non-interacting (no change of energy and direction of the proton)
- **Acceleration:** energy of proton increased after FSI
- **Deceleration:** energy of proton decreased after FSI

**Pion FSI:** pion absorption

charged current (CC)  $\nu \rightarrow l'$

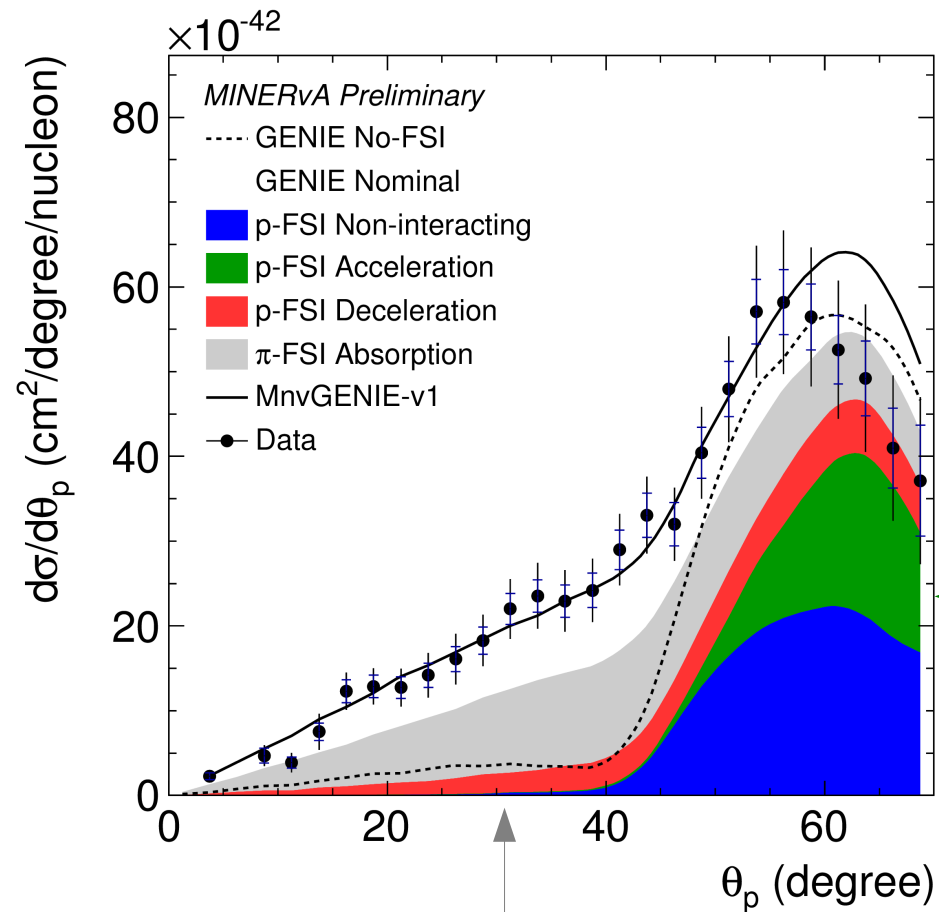


charged current (CC)  $\nu \rightarrow l'$



# Single-Particle Kinematics

- Muon momentum, angle
- Proton momentum, angle



Proton FSI acceleration  
localized at high angle

Pionless resonant production dominates low angle

# NUCLEAR EFFECT DIAGNOSTICS

A more general analysis of kinematic imbalance

Transverse:  $0 = \vec{p}_T^{\ell'} + \vec{p}_T^{N'} - \delta\vec{p}_T$

Longitudinal:  $E_\nu = p_L^{\ell'} + p_L^{N'} - \delta p_L$

New variable:  $p_n \equiv \sqrt{\delta p_T^2 + \delta p_L^2}$

Neutrino energy is unknown (in the first place), equations are not closed.

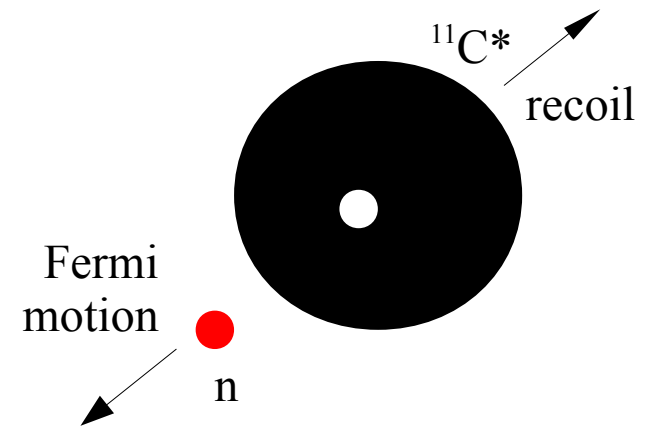
For CCQE,  $A' = {}^{11}\text{C}^*$   
 No more unknowns  
 $p_n$ : neutron Fermi motion

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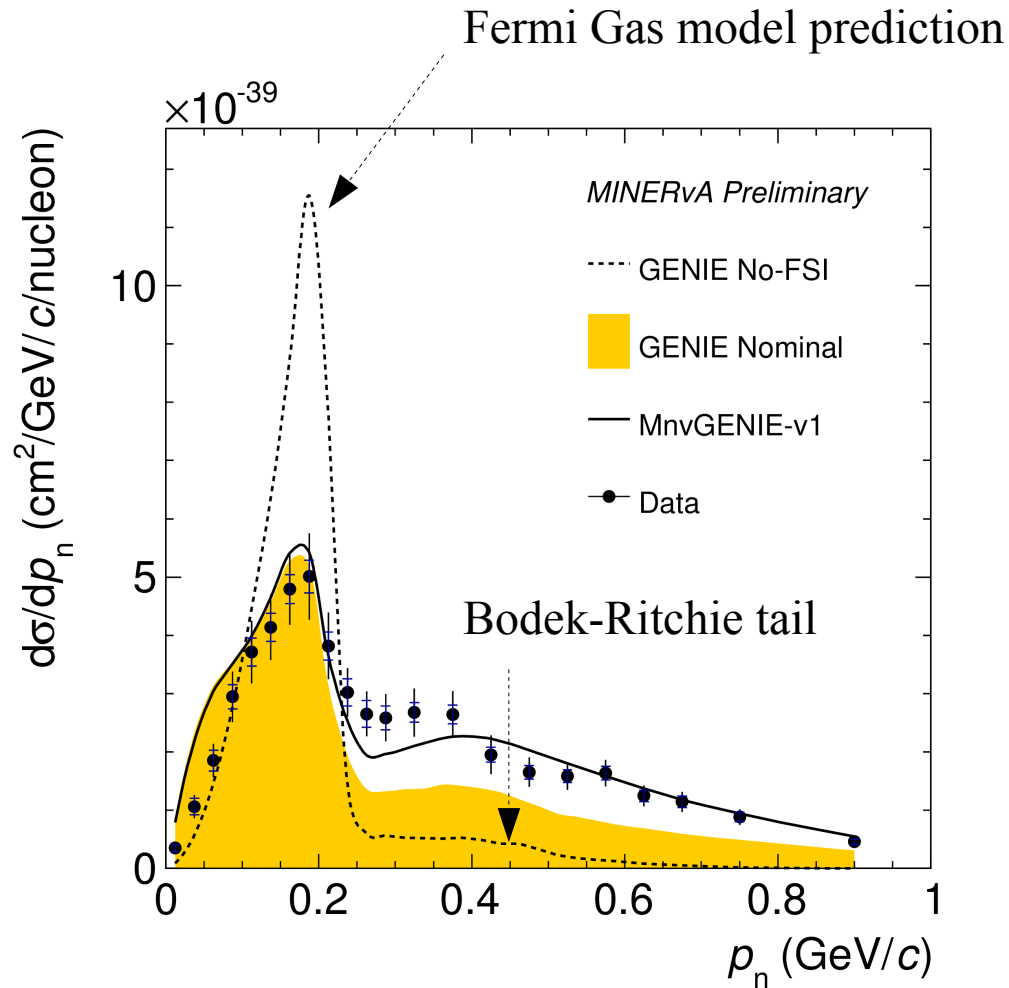


$$p_L = \frac{1}{2}(M(A) + k'_L + p'_L - E' - E_{p'}) - \frac{p_T^2 + M^*(A-1)^2}{2(M(A) + k'_L + p'_L - E' - E_{p'})}$$

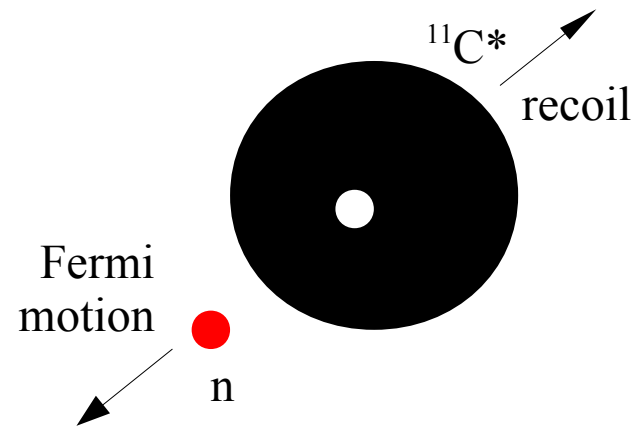
A. Furmanski, J. Sobczyk, Phys.Rev. C95 (2017) no.6, 065501

# Nuclear Effect Diagnostics

- CCQE with Fermi motion

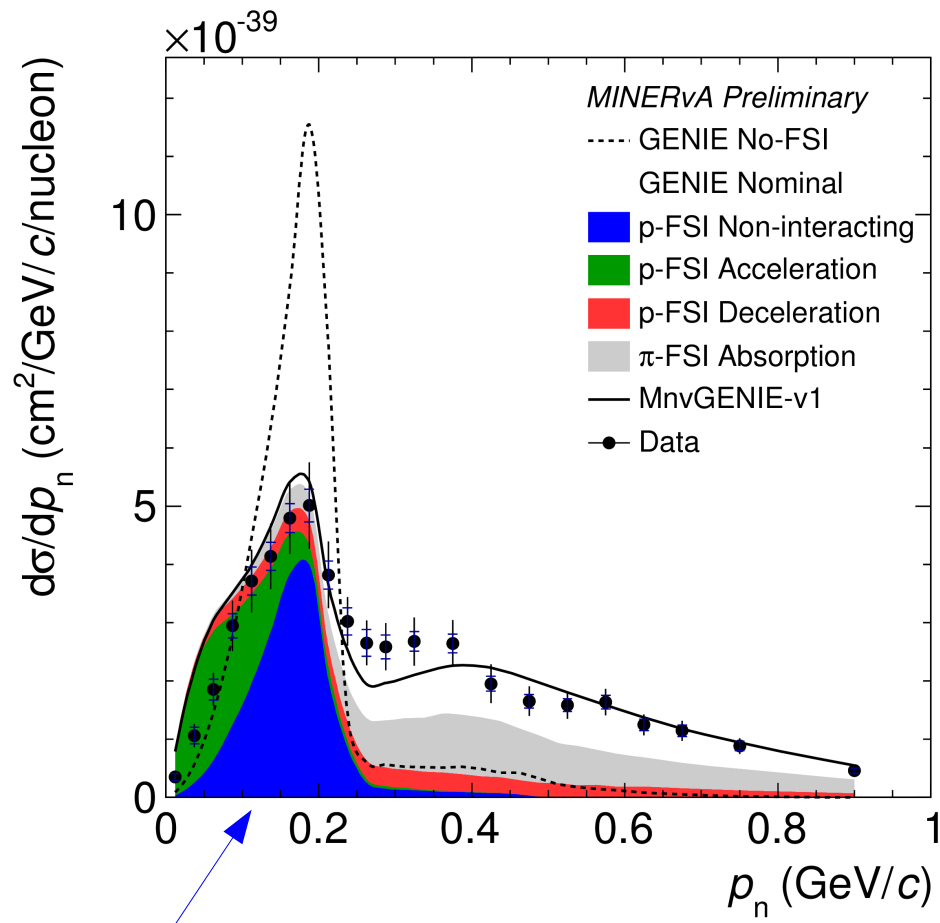


$p_n$  is Fermi motion magnitude  $\rightarrow$  “QE peak”  
 – GENIE No-FSI



# Nuclear Effect Diagnostics

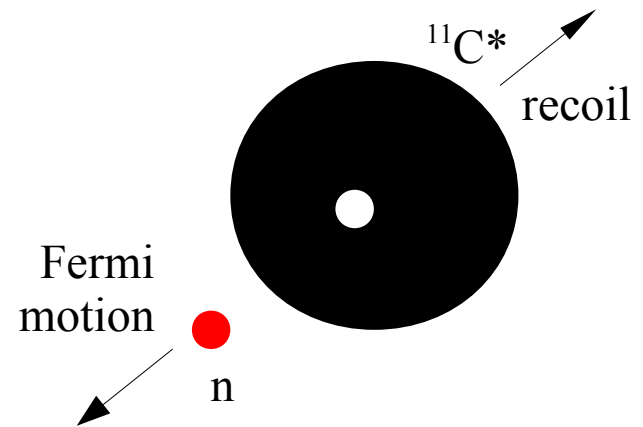
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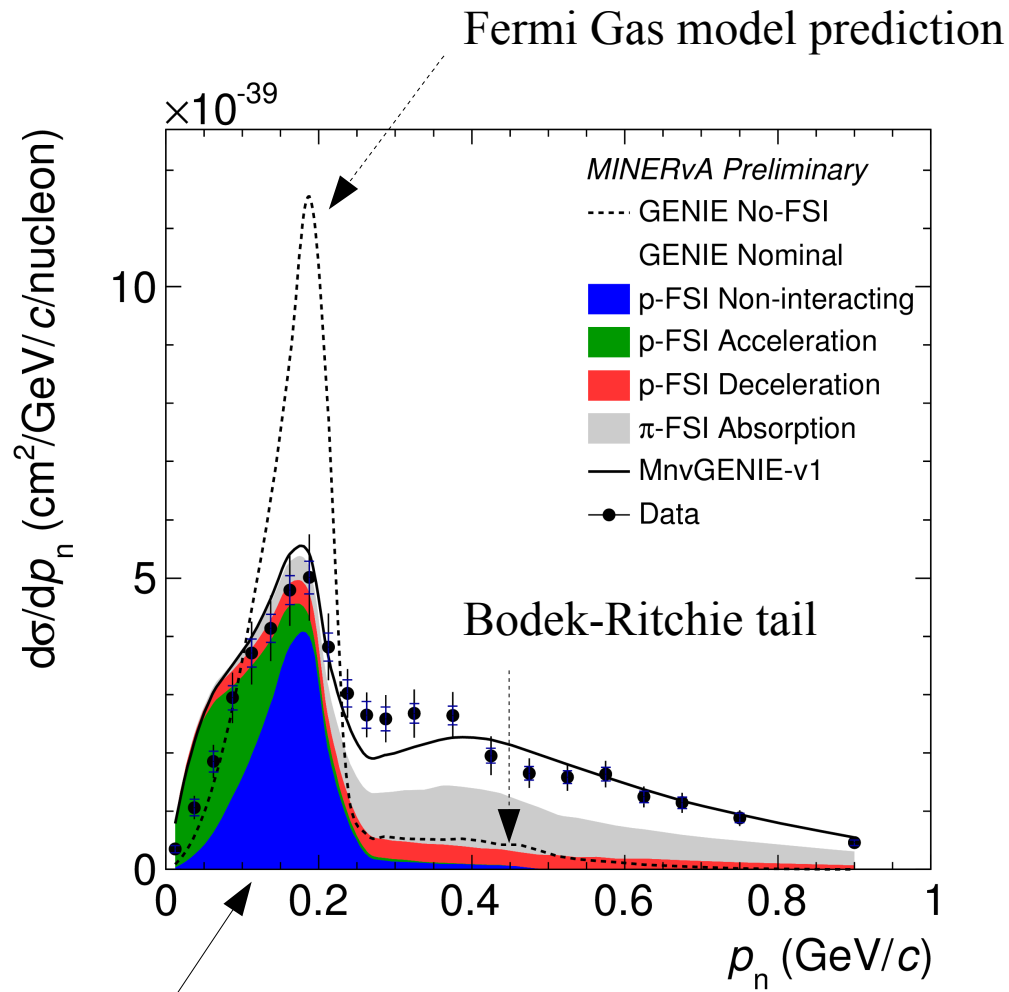
– GENIE No-FSI

– p-FSI Non-interacting



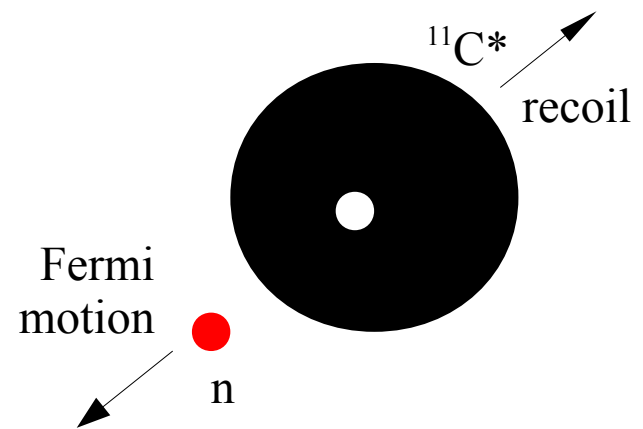
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- CCQE with Fermi motion

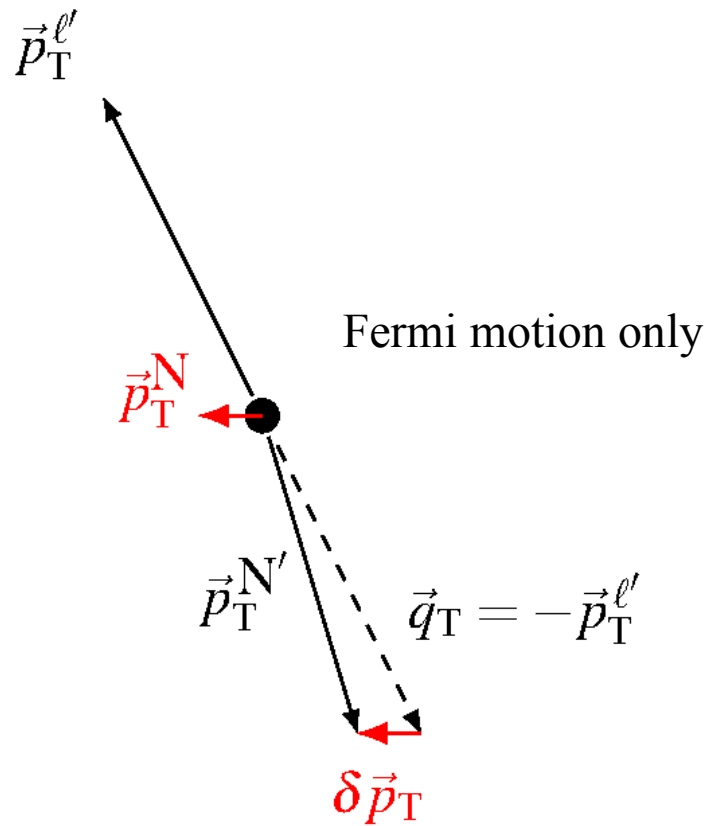


$p_n$  is Fermi motion magnitude → “QE peak”

- GENIE No-FSI
- p-FSI Non-interacting



QE peak dominated by CCQE without FSI  
Direct constraint of Fermi motion



For CCQE,  $A' = {}^{11}\text{C}^*$   
 No more unknowns  
 $\vec{p}_n$  : neutron Fermi motion

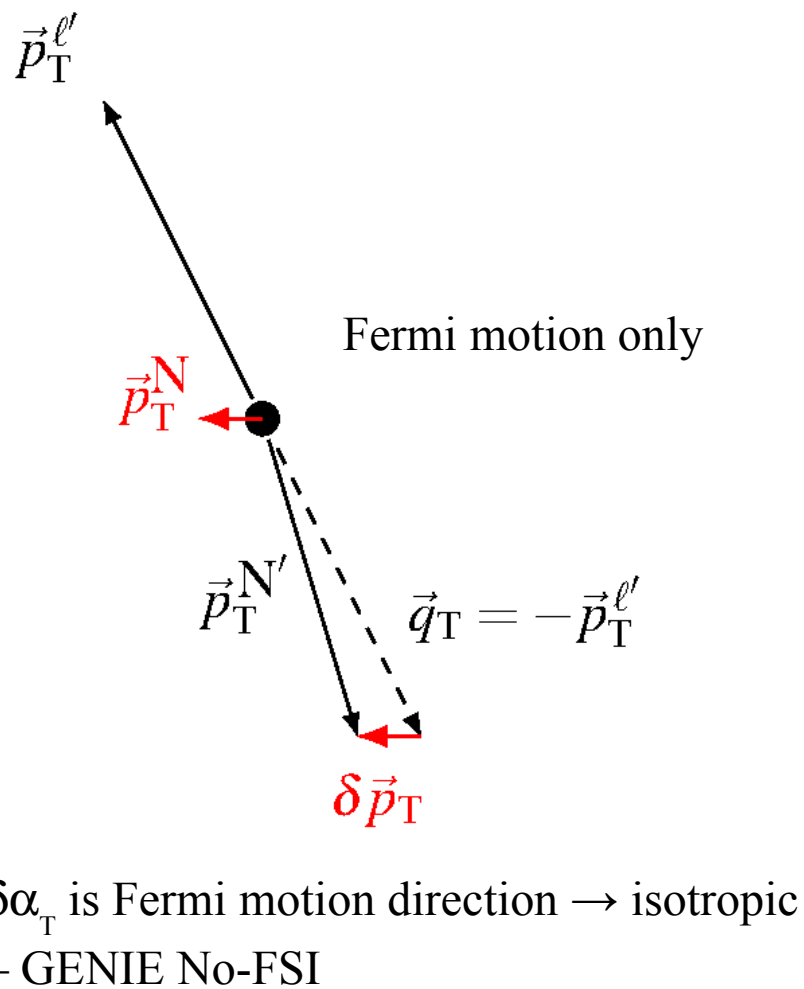
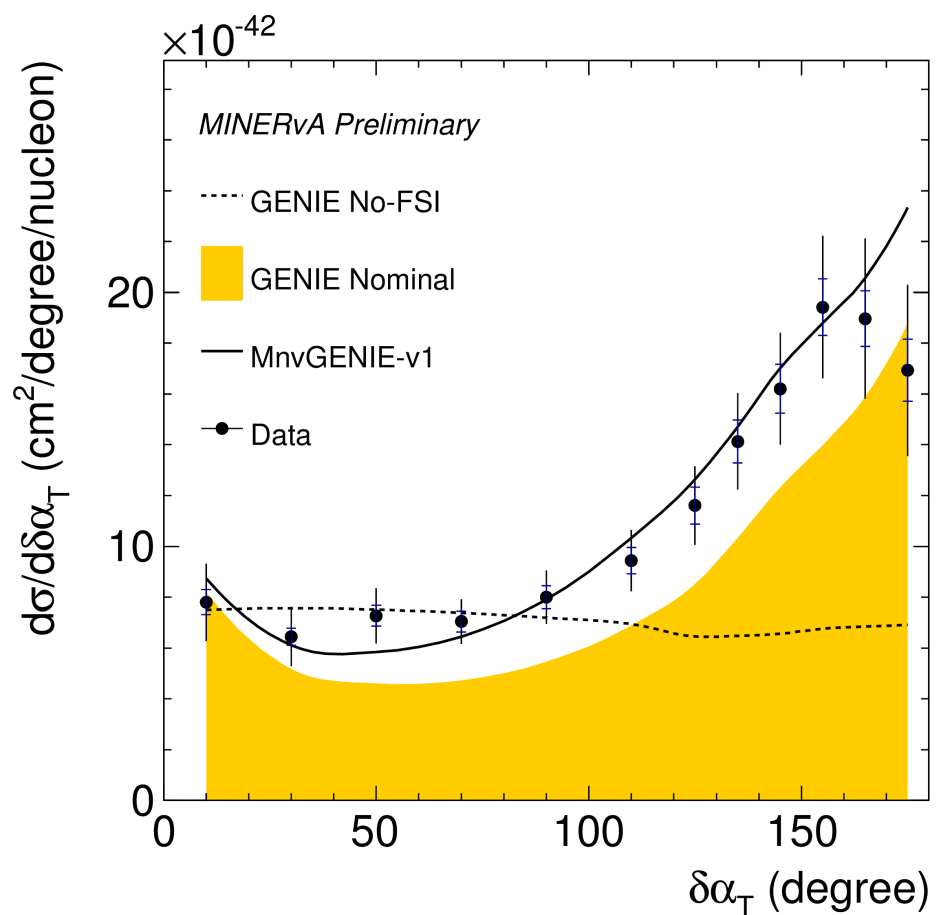
$$\delta\vec{p}_T = \vec{p}_T^N$$

$\delta\alpha_T$  is Fermi motion direction  $\rightarrow$  isotropic



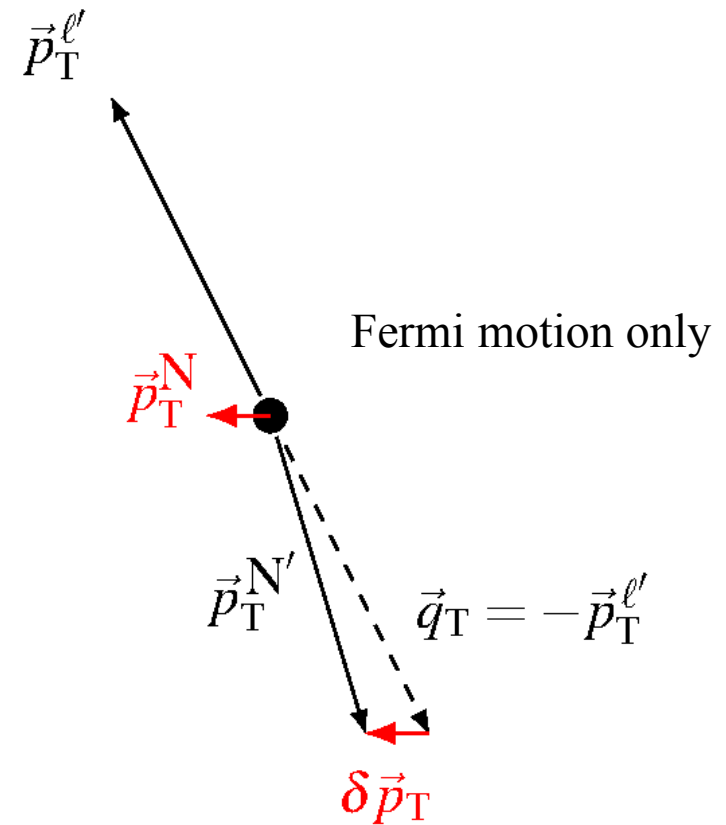
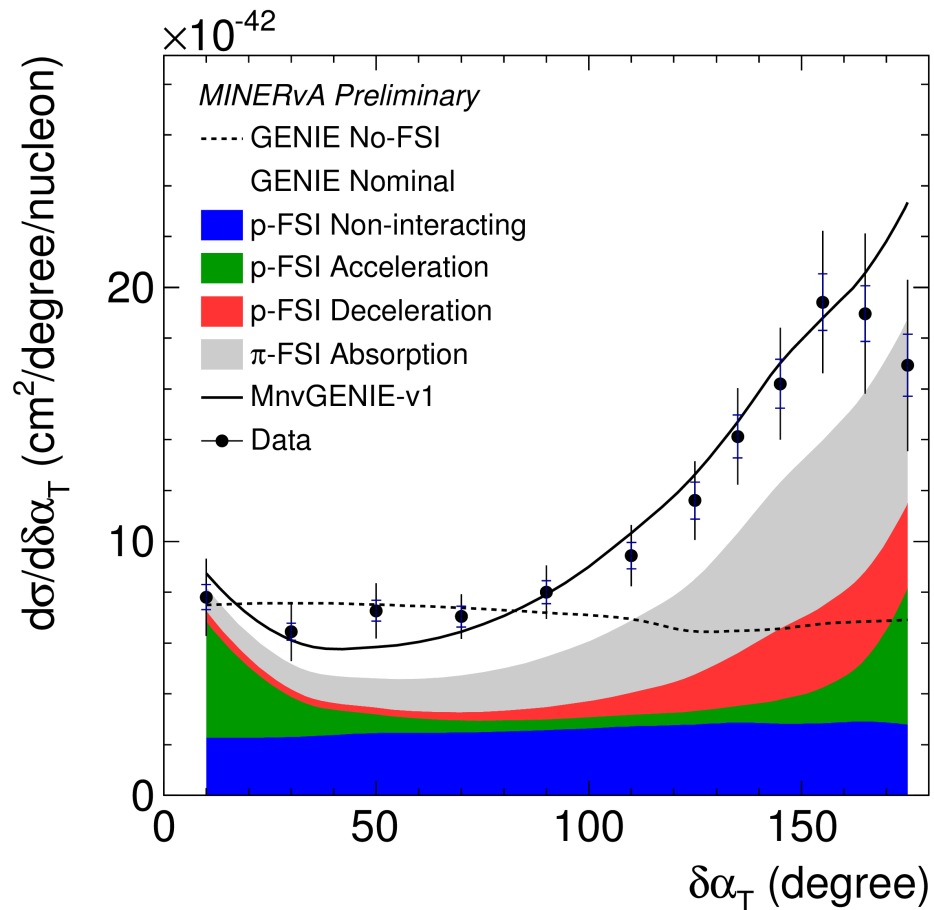
# Nuclear Effect Diagnostics

- CCQE with Fermi motion



# Nuclear Effect Diagnostics

- CCQE with Fermi motion



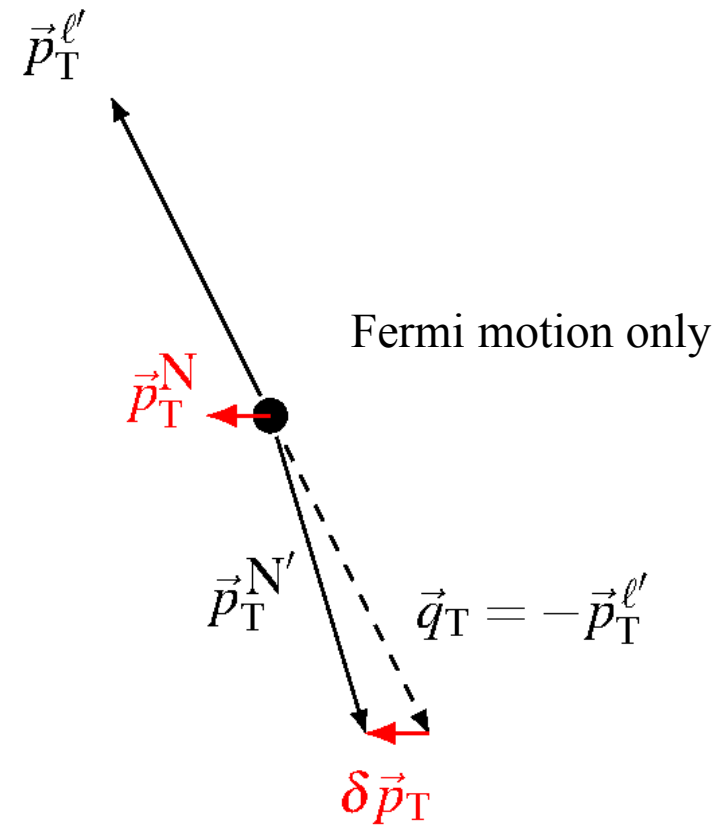
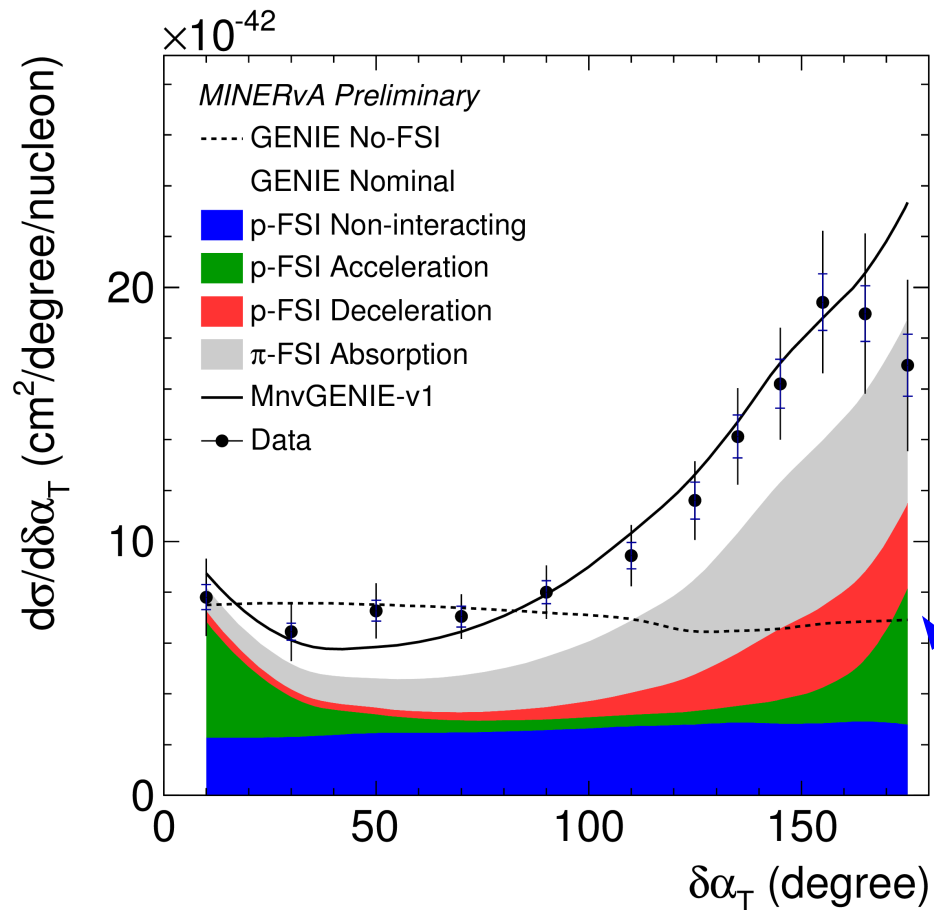
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– GENIE No-FSI

– p-FSI Non-interacting

# Nuclear Effect Diagnostics

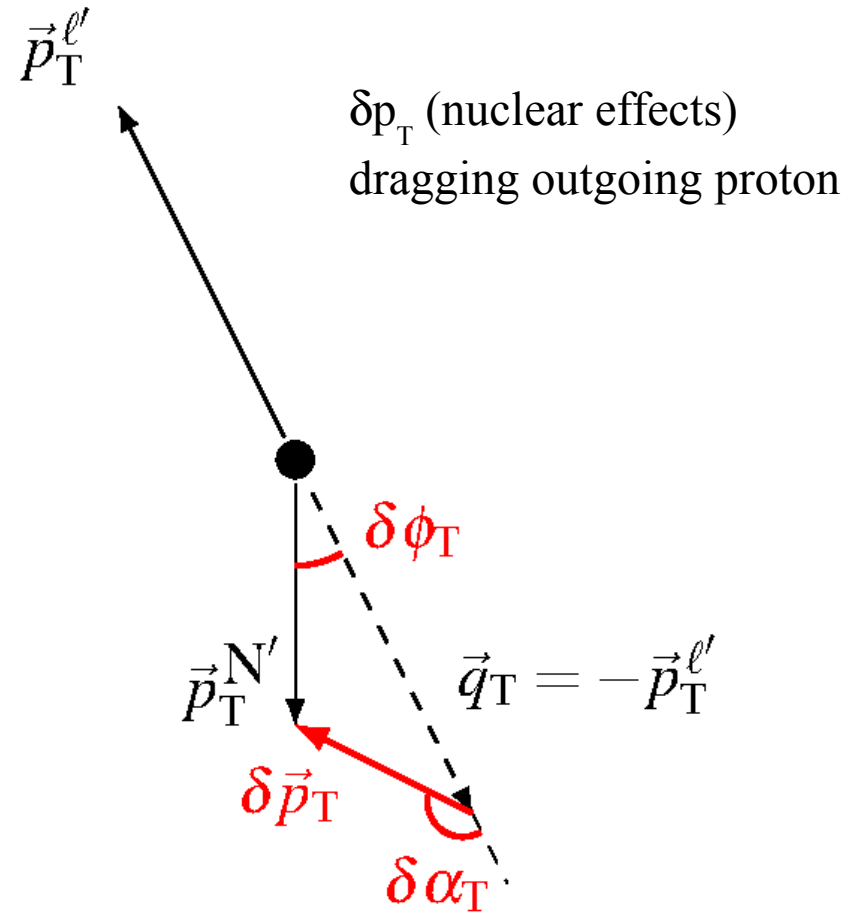
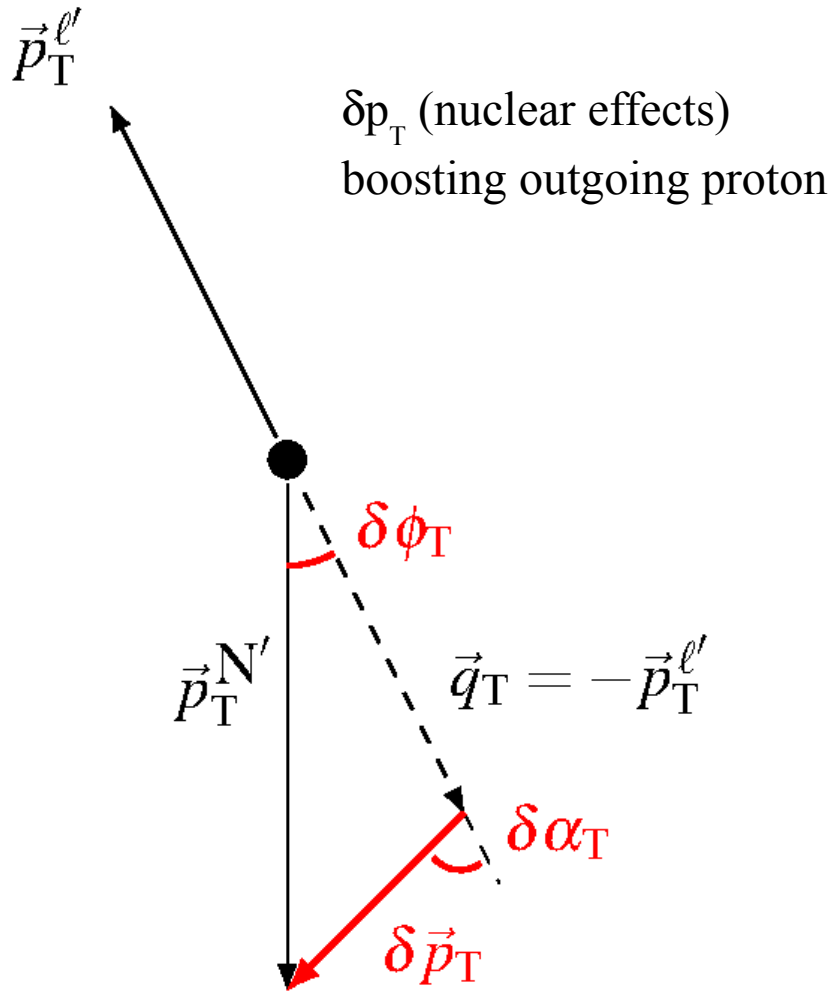
- CCQE with Fermi motion



$\delta\alpha_T$  is Fermi motion direction  $\rightarrow$  isotropic

- GENIE No-FSI
- p-FSI Non-interacting

Baseline for all non-Fermi motion effects  
 Factor out Fermi motion uncertainty  
 Complementary to  $p_n$



With full nuclear effects

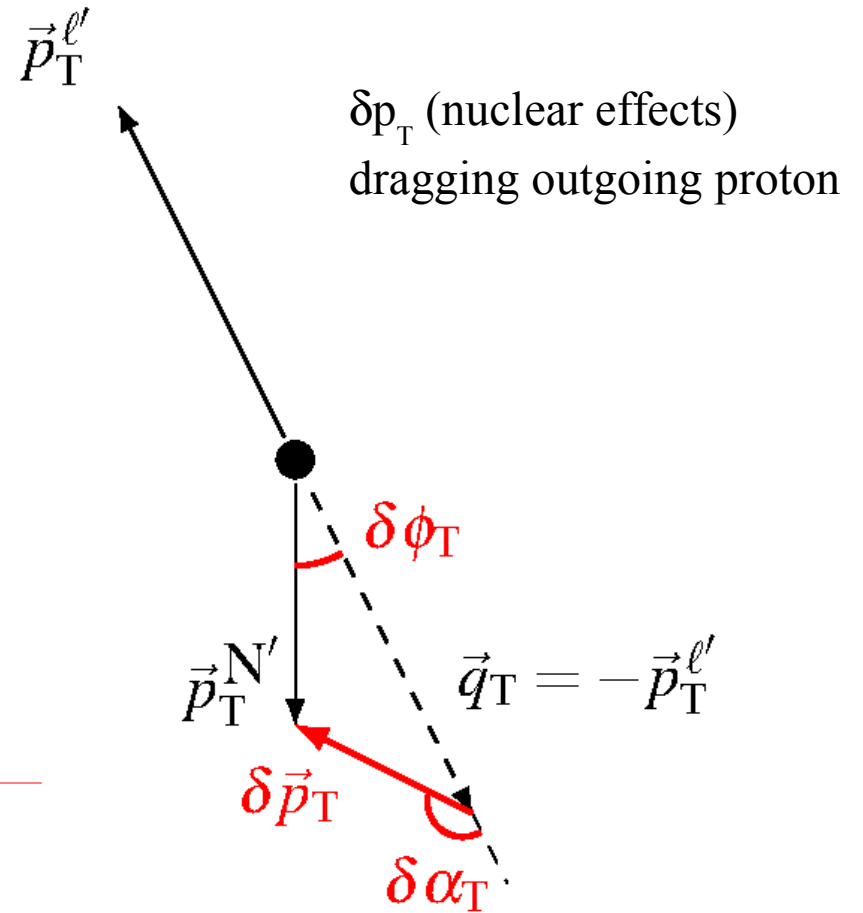
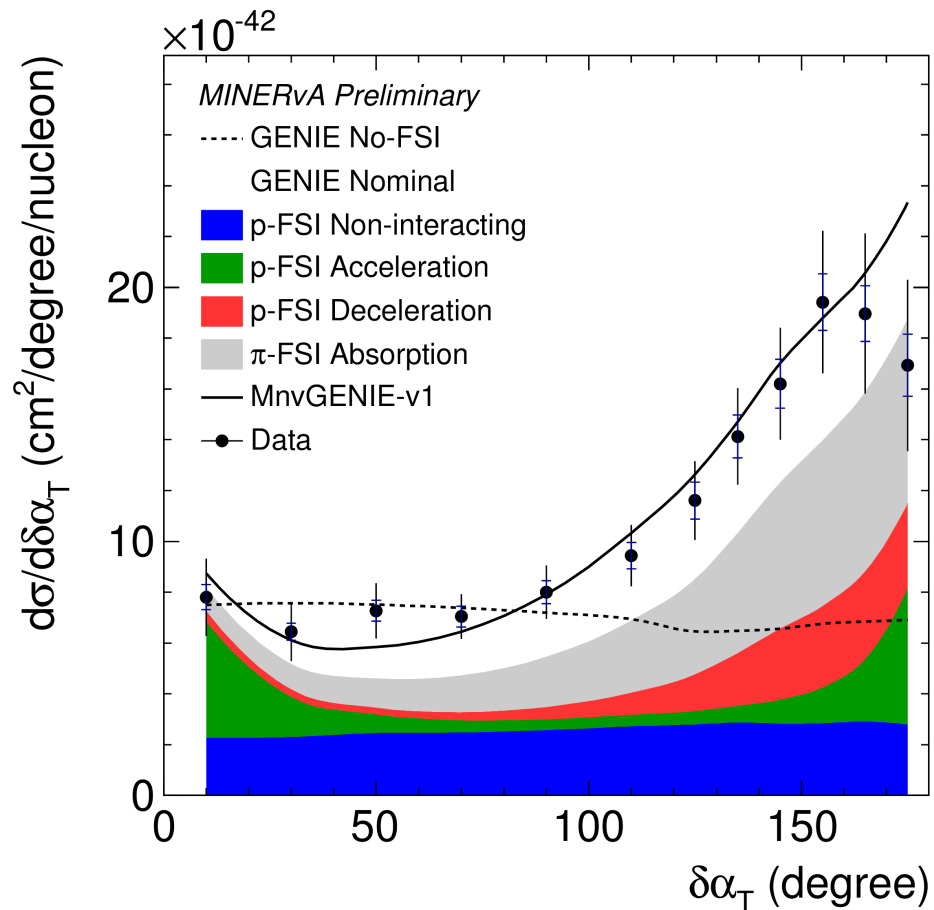
$$\delta\vec{p}_T = \vec{p}_T^N - \Delta\vec{p}_T$$

Intranuclear momentum transfer

Baseline for all non-Fermi motion effects  
 Factor out Fermi motion uncertainty  
 Complementary to  $p_n$

# Nuclear Effect Diagnostics

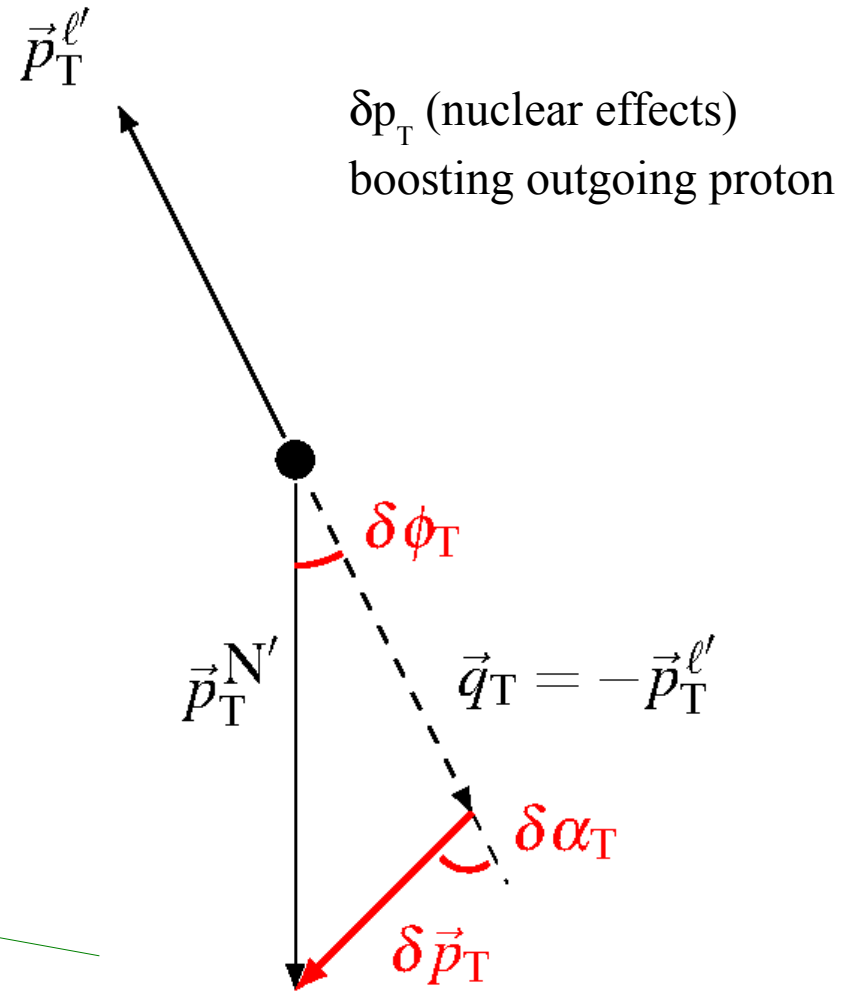
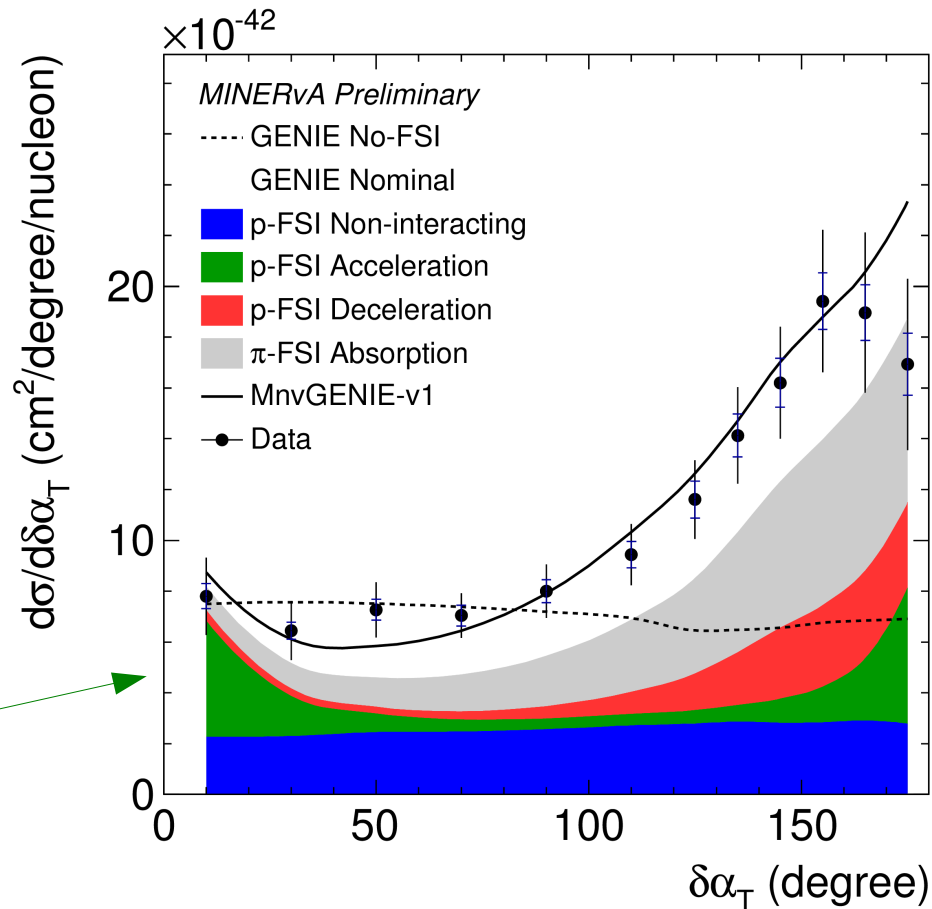
- CCQE with Fermi motion
- FSI deceleration vs. acceleration



Deceleration at large  $\delta\alpha_T$

# Nuclear Effect Diagnostics

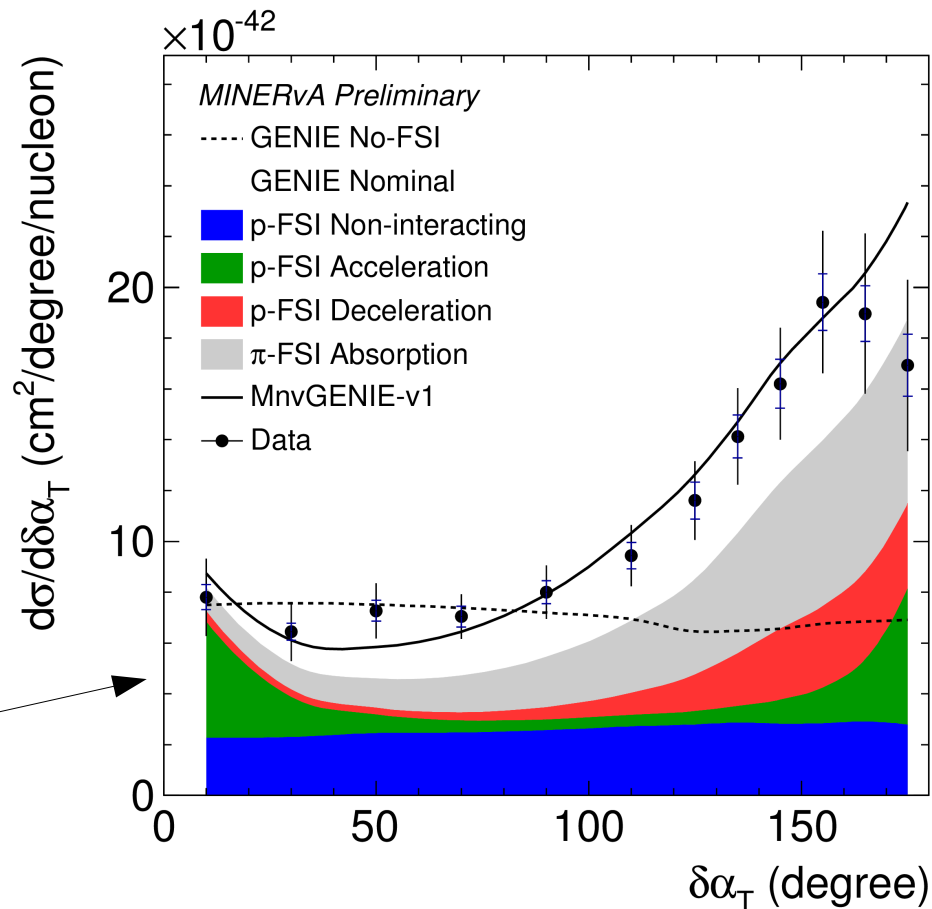
- CCQE with Fermi motion
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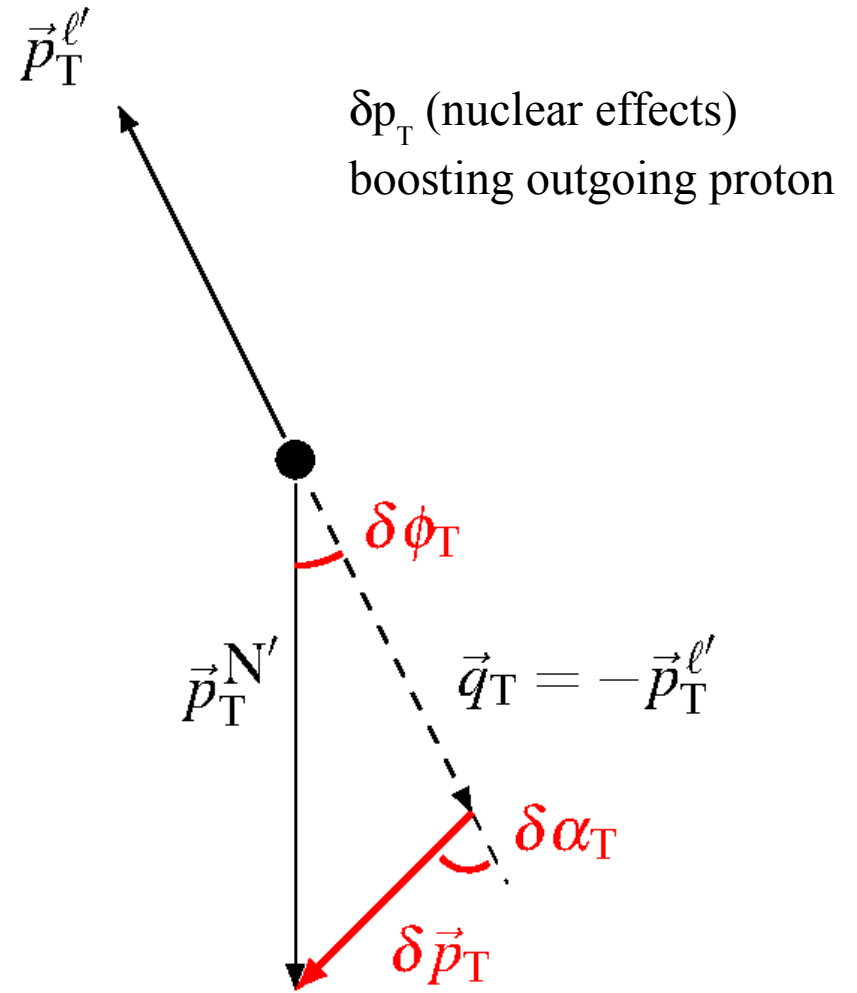
Deceleration at large  $\delta\alpha_T$   
 Acceleration at both small and (due to transverse projection) large  $\delta\alpha_T$

# Nuclear Effect Diagnostics

- CCQE with Fermi motion
- FSI deceleration vs. acceleration



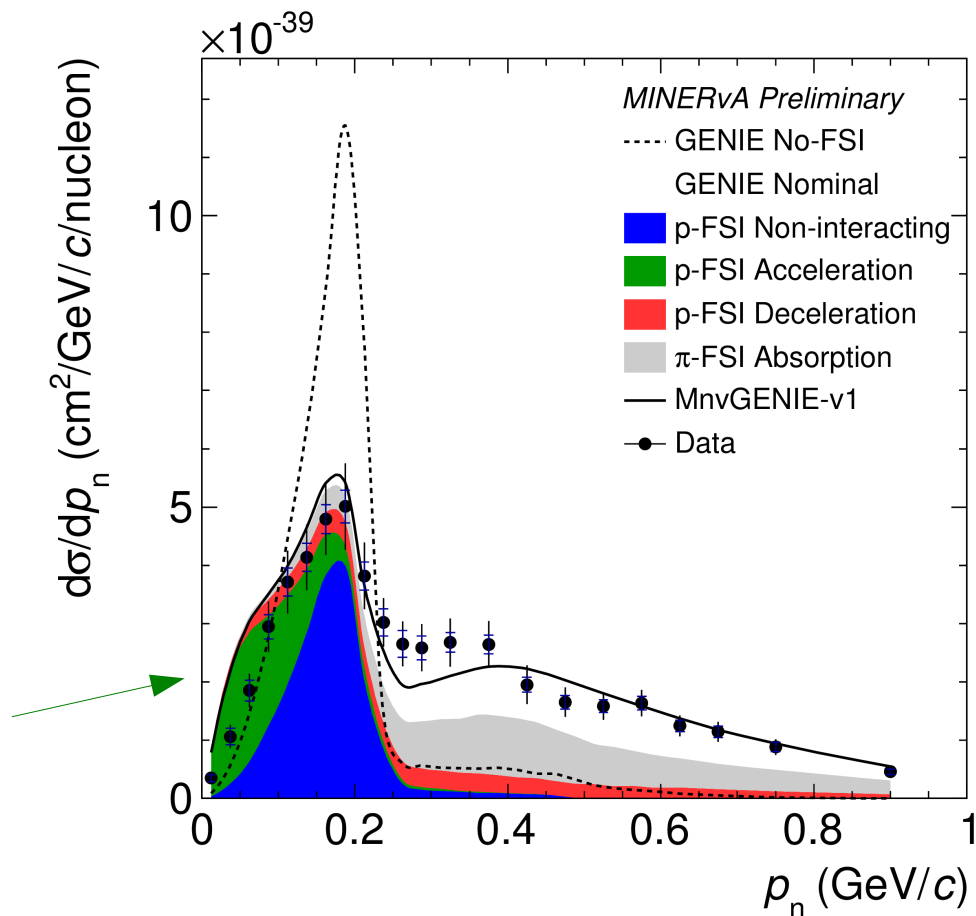
Only acceleration can enter small  $\delta\alpha_T$



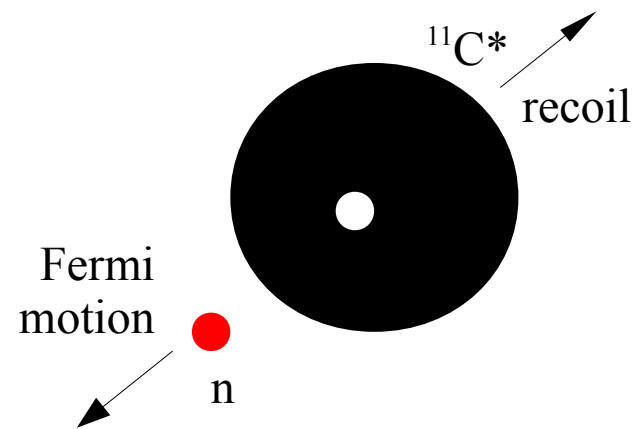
Deceleration at large  $\delta\alpha_T$   
Acceleration at both small and (due to transverse projection) large  $\delta\alpha_T$

# Nuclear Effect Diagnostics

- CCQE with Fermi motion
- FSI deceleration vs. acceleration



Acceleration to the left of QE peak  
Strongly distort QE peak





A more general analysis of kinematic imbalance

Transverse:  $0 = \vec{p}_T^{\ell'} + \vec{p}_T^{N'} - \delta\vec{p}_T$

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New variable:  $p_n \equiv \sqrt{\delta p_T^2 + \delta p_L^2}$

Neutrino energy is unknown (in the first place), equations are not closed.

For RES, DIS, 2p2h, no longer exclusive  $\mu$ -p-A' final states

$$p_n = |\vec{p}_N - \Delta\vec{p}|$$

Fermi motion

Intranuclear momentum transfer

A. Furmanski, J. Sobczyk, Phys.Rev. C95 (2017) no.6, 065501

Xianguo Lu, Oxford

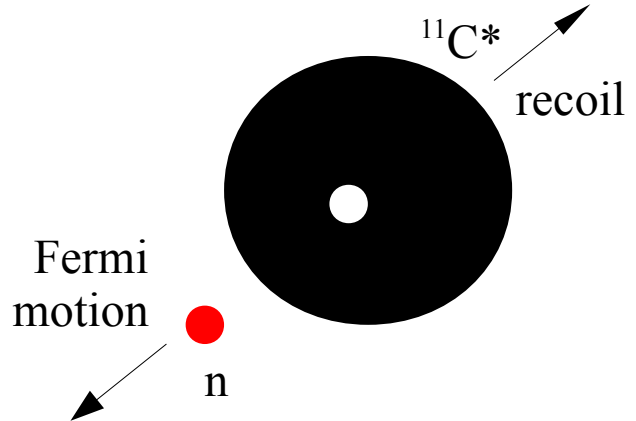
Assuming exclusive  $\mu$ -p-A' final states

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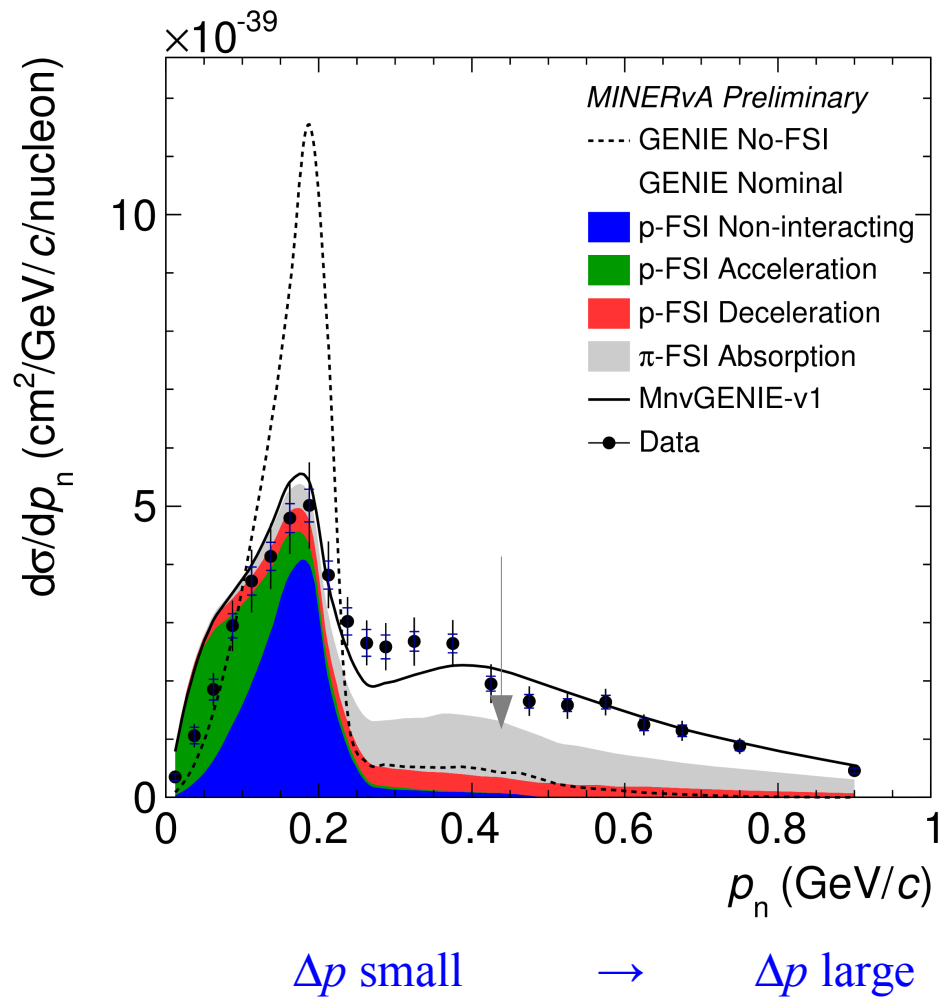
$p_n$ : recoil momentum of the nuclear remnant



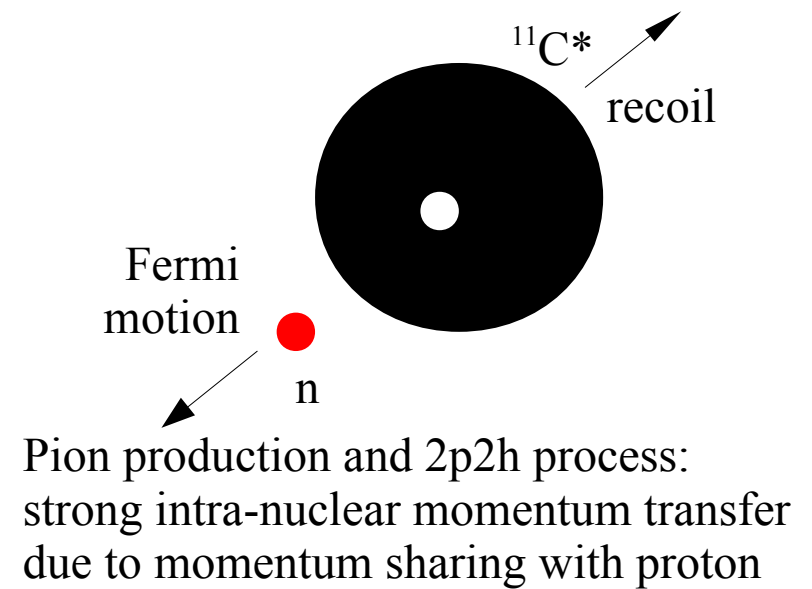
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# Nuclear Effect Diagnostics

- CCQE with Fermi motion
- FSI deceleration vs. acceleration
- Pionless resonant production, pion absorption FSI, and 2p2h

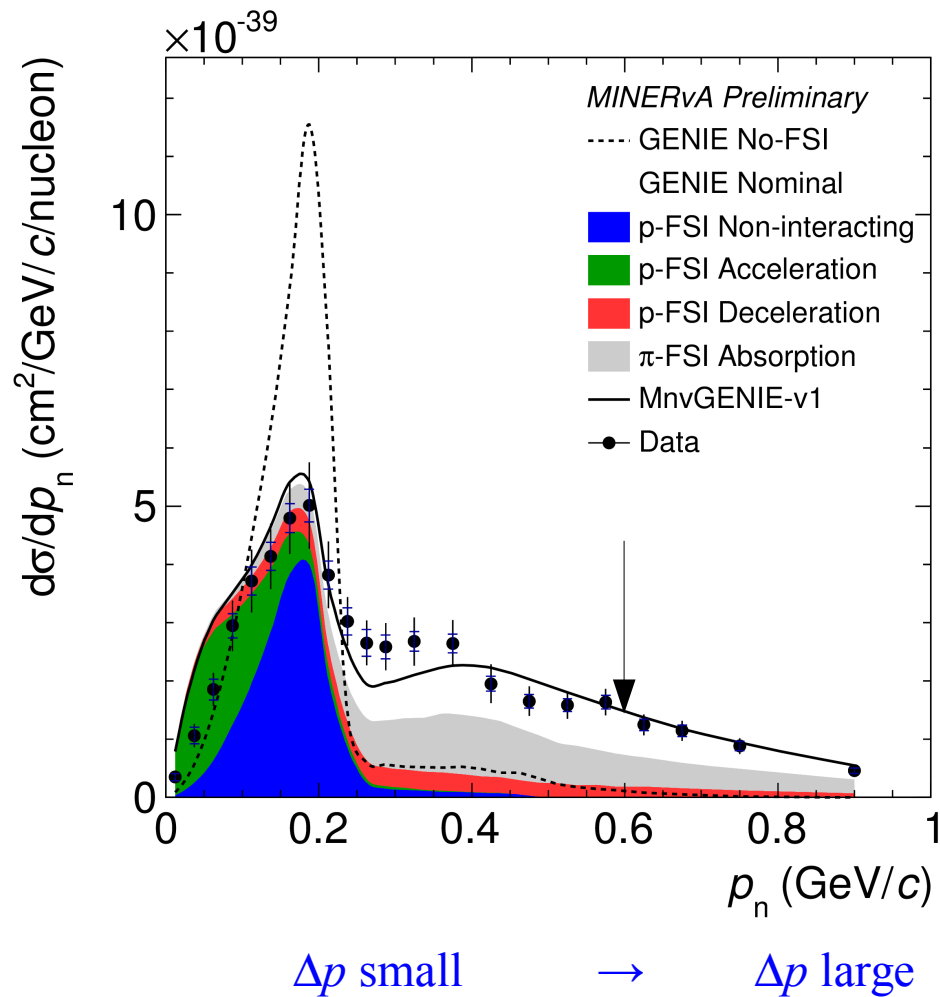


$p_n$ : smeared  $\delta p_T$  beyond QE peak  $\rightarrow$  tail  
 –  $\pi$ -FSI Absorption



# Nuclear Effect Diagnostics

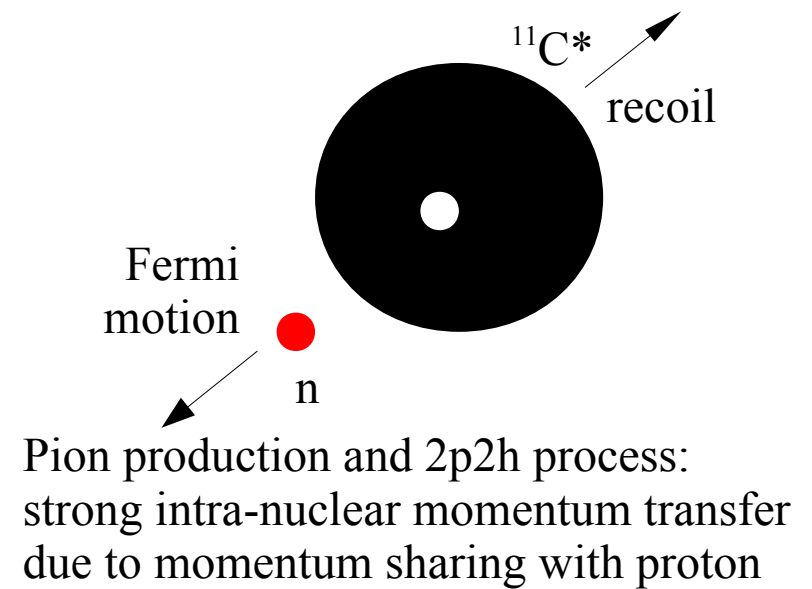
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$p_n$ : smeared  $\delta p_T$  beyond QE peak  $\rightarrow$  tail

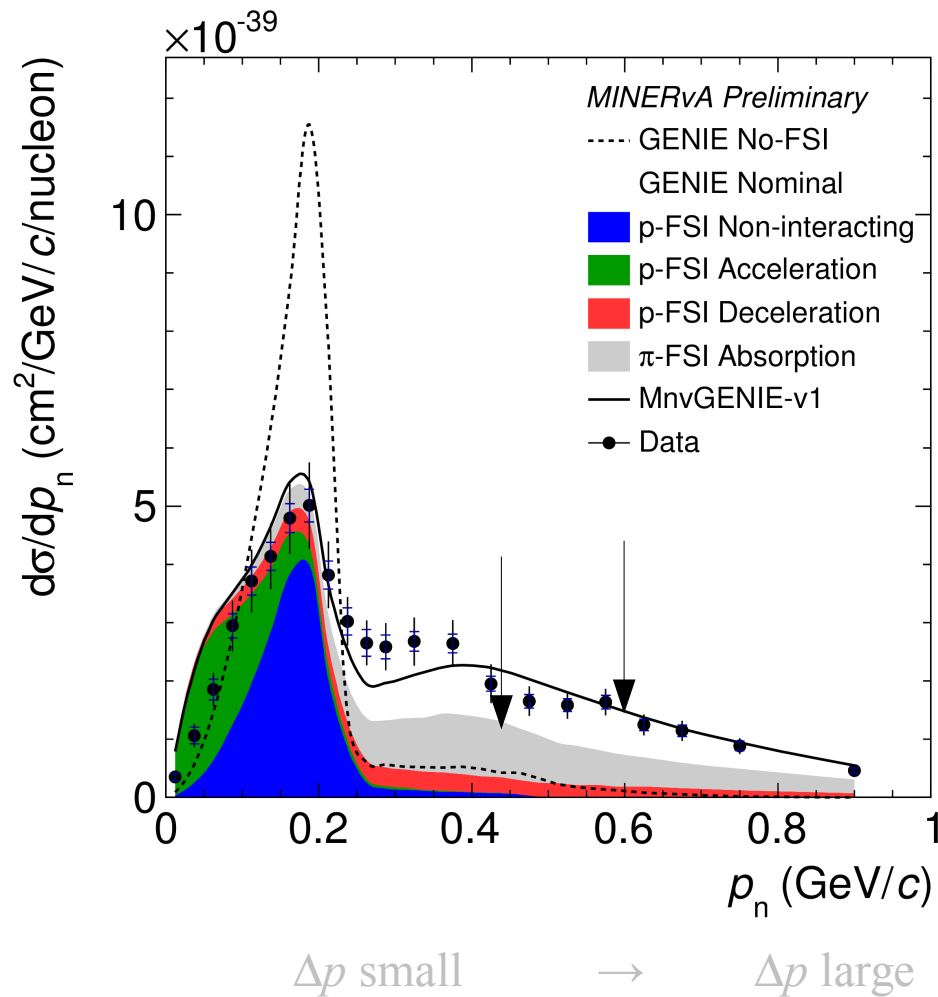
- π-FSI Absorption
- 2p2h

(= MnvGENIE-v1 – GENIE Nominal)



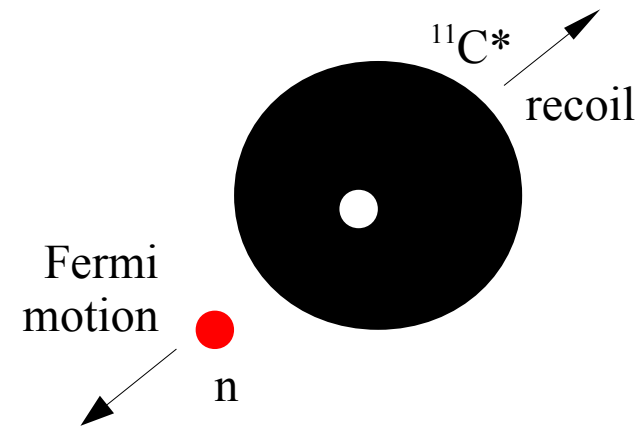
# Nuclear Effect Diagnostics

- CCQE with Fermi motion
- FSI deceleration vs. acceleration
- Pionless resonant production, pion absorption FSI, and 2p2h



GENIE describes the tail reasonably well due to large contribution from 2p2h tuned to MINERvA inclusive measurements

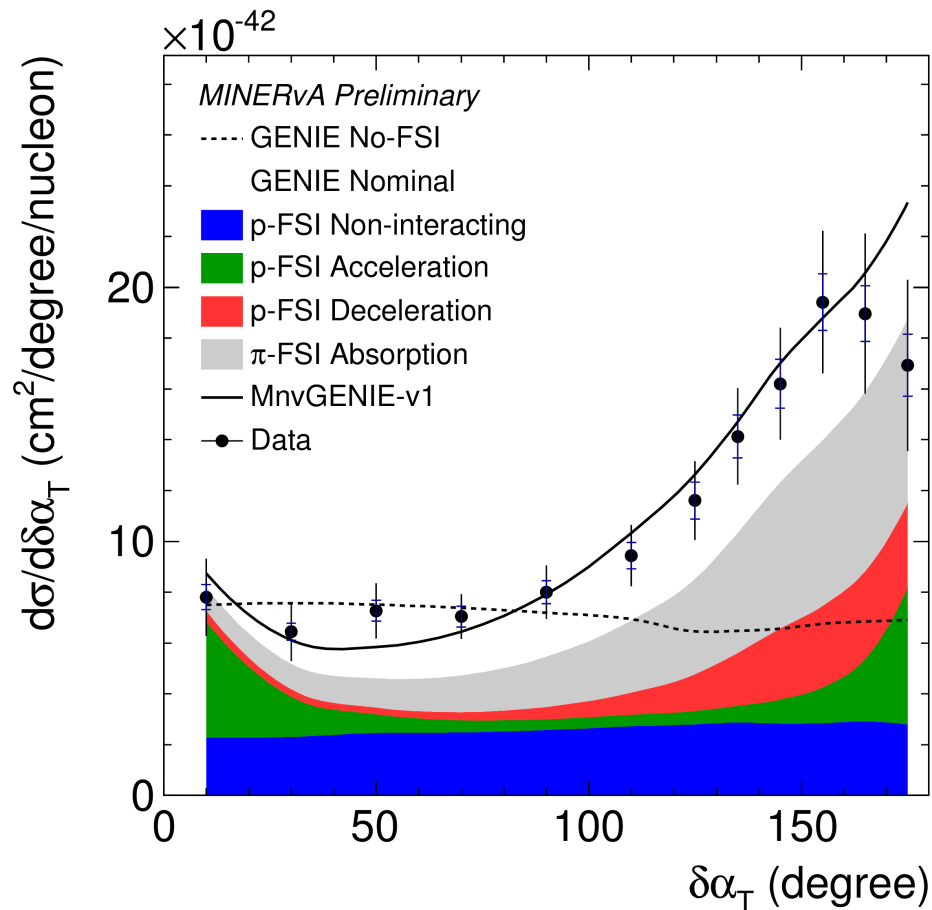
- $p_n$  : smeared  $\delta p_T$  beyond QE peak  $\rightarrow$  tail
- $\pi$ -FSI Absorption
- 2p2h  
(= MnvGENIE-v1 – GENIE Nominal)



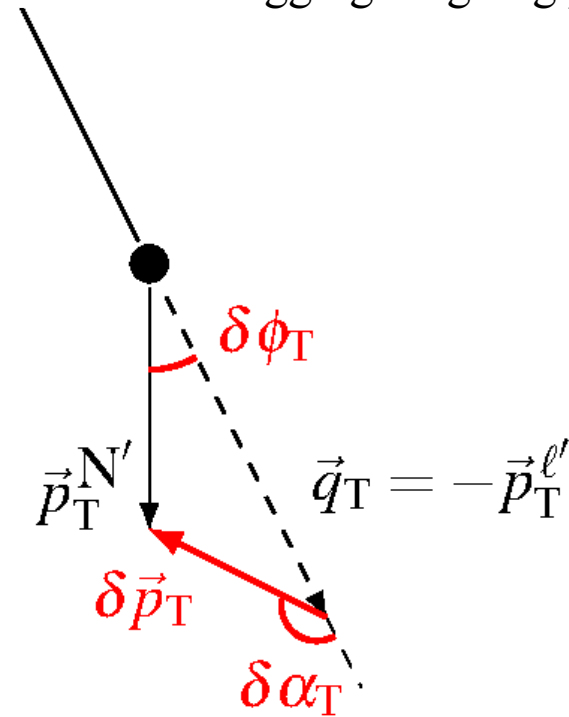
Pion production and 2p2h process: strong intra-nuclear momentum transfer due to momentum sharing with proton

# Nuclear Effect Diagnostics

- CCQE with Fermi motion
- FSI deceleration vs. acceleration
- Pionless resonant production, pion absorption FSI, and 2p2h



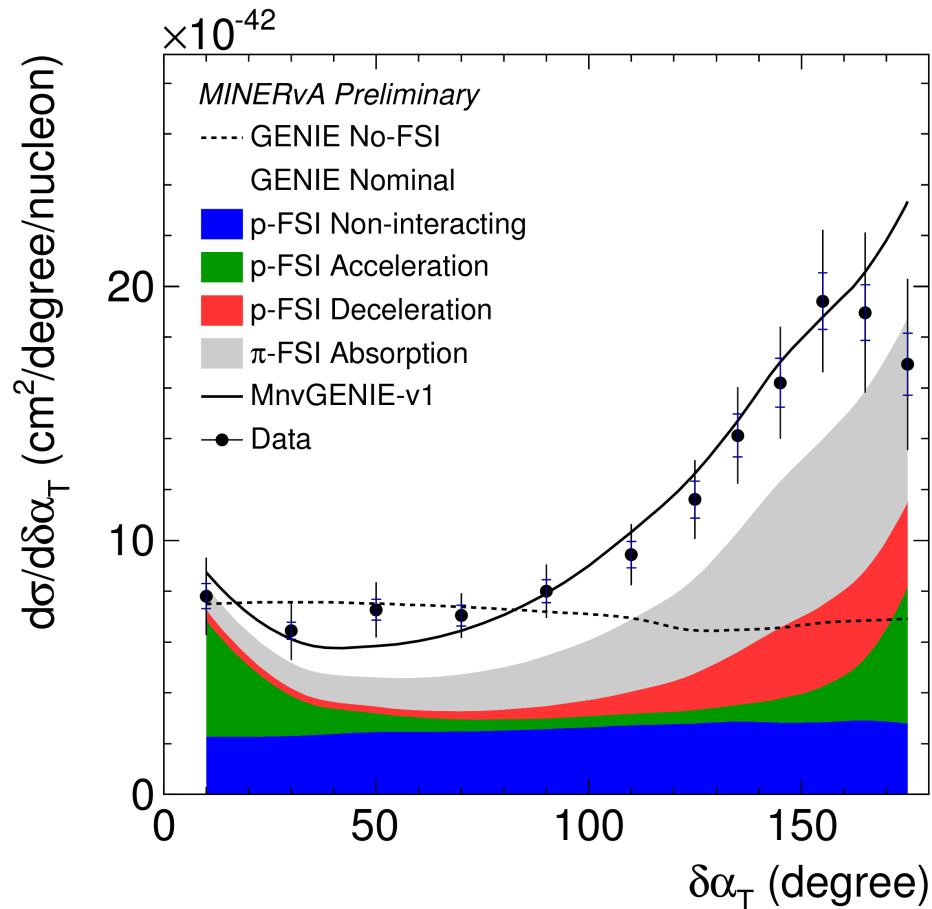
$\delta p_T$  (nuclear effects)  
dragging outgoing proton



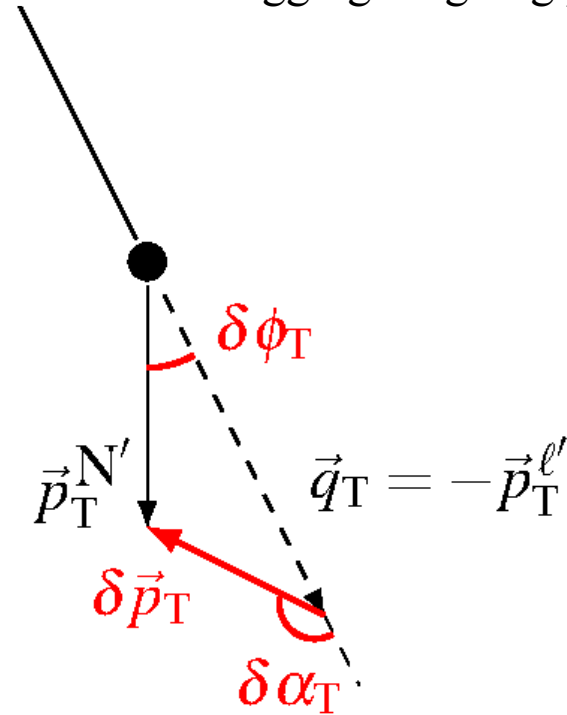
Proton momentum shared by others,  
decelerated → large  $\delta\alpha_T$  region  
–  $\pi$ -FSI Absorption

# Nuclear Effect Diagnostics

- CCQE with Fermi motion
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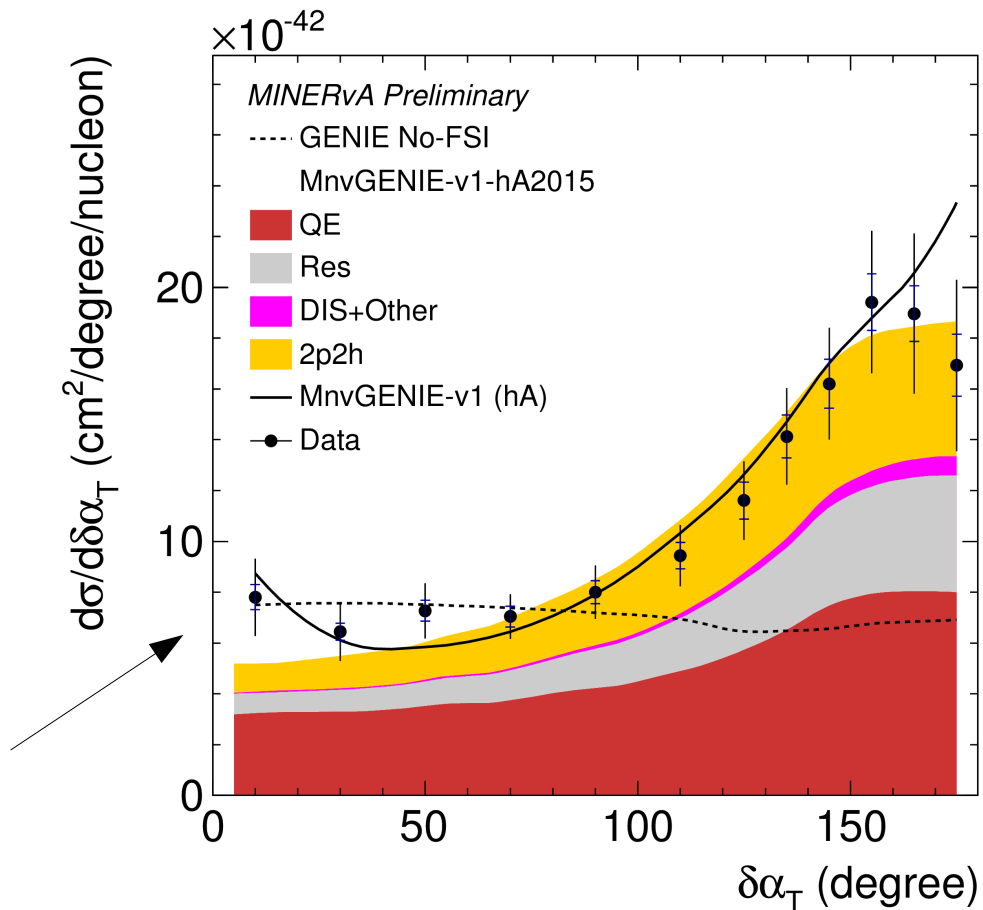
–  $\pi$ -FSI Absorption

– 2p2h (= MnvGENIE-v1 – GENIE Nominal)

# ADVANCED TOPICS: GENIE FSI<sub>s</sub>

# Advanced Topics: GENIE FSI

- (pre2015) hA: effective model, include “elastic component” in intranuclear scattering, used in GENIE MINERvA Tune (v1)
- hA2015: removed “elastic component”, replacing hA in MnvGENIE-v1-hA2015

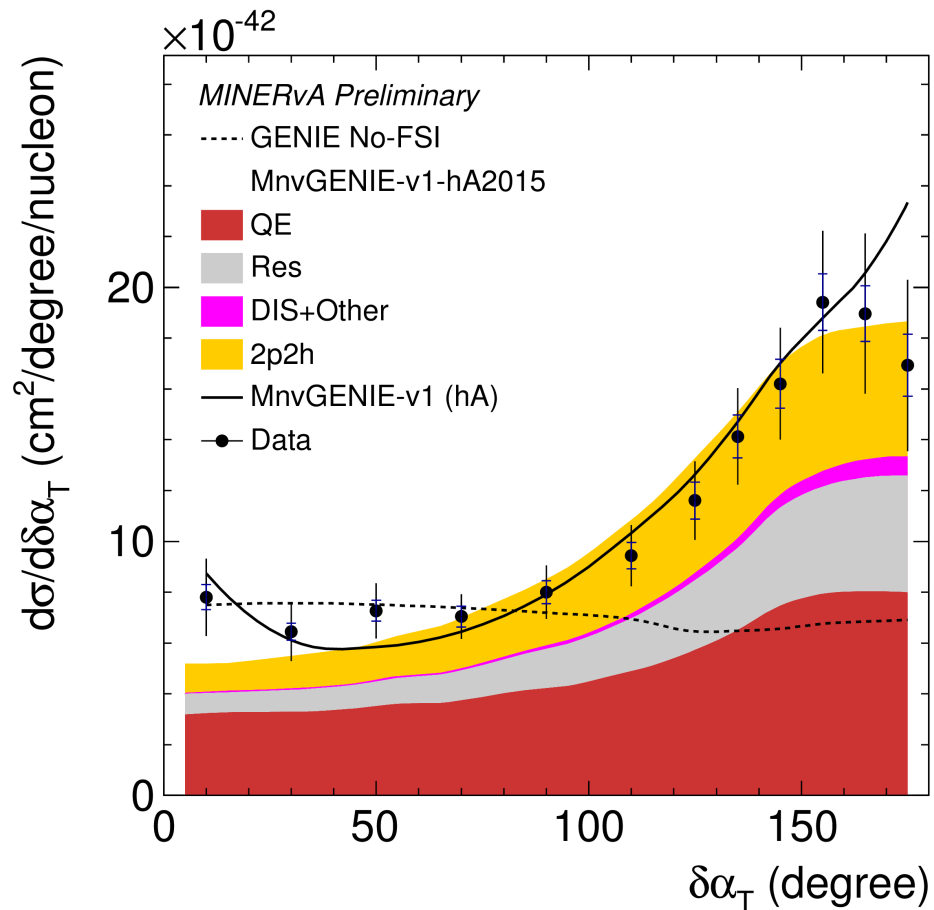


No p-FSI acceleration

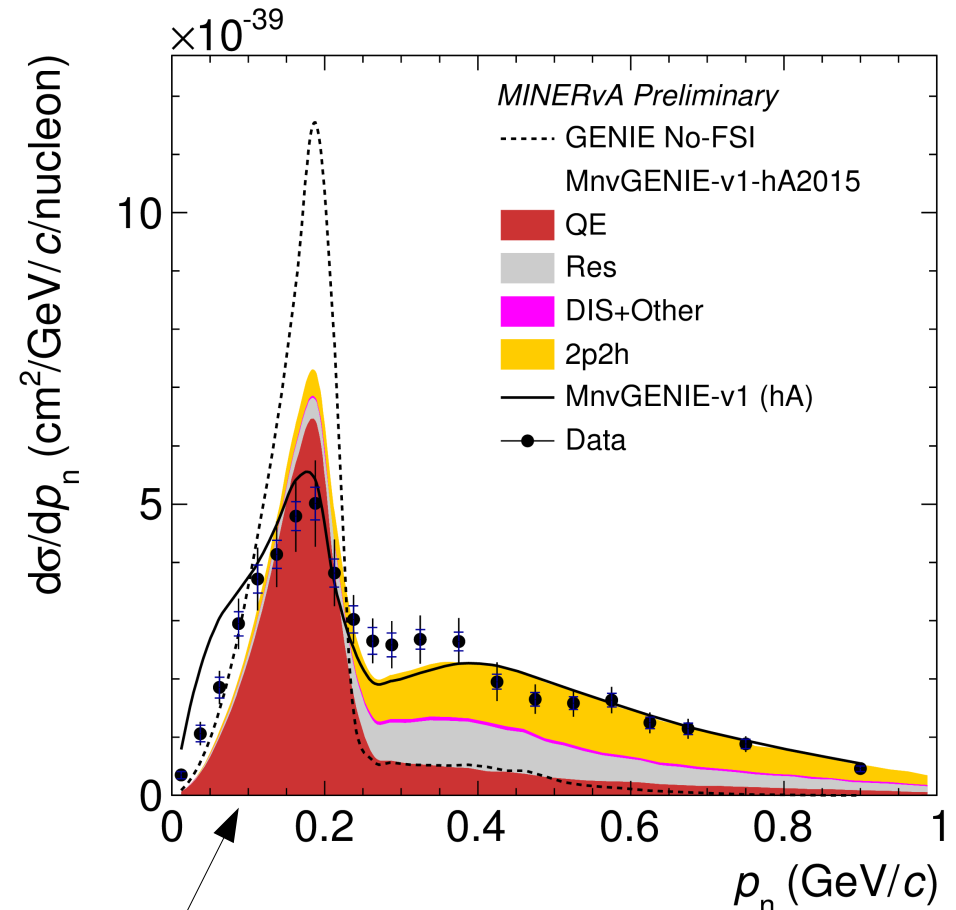


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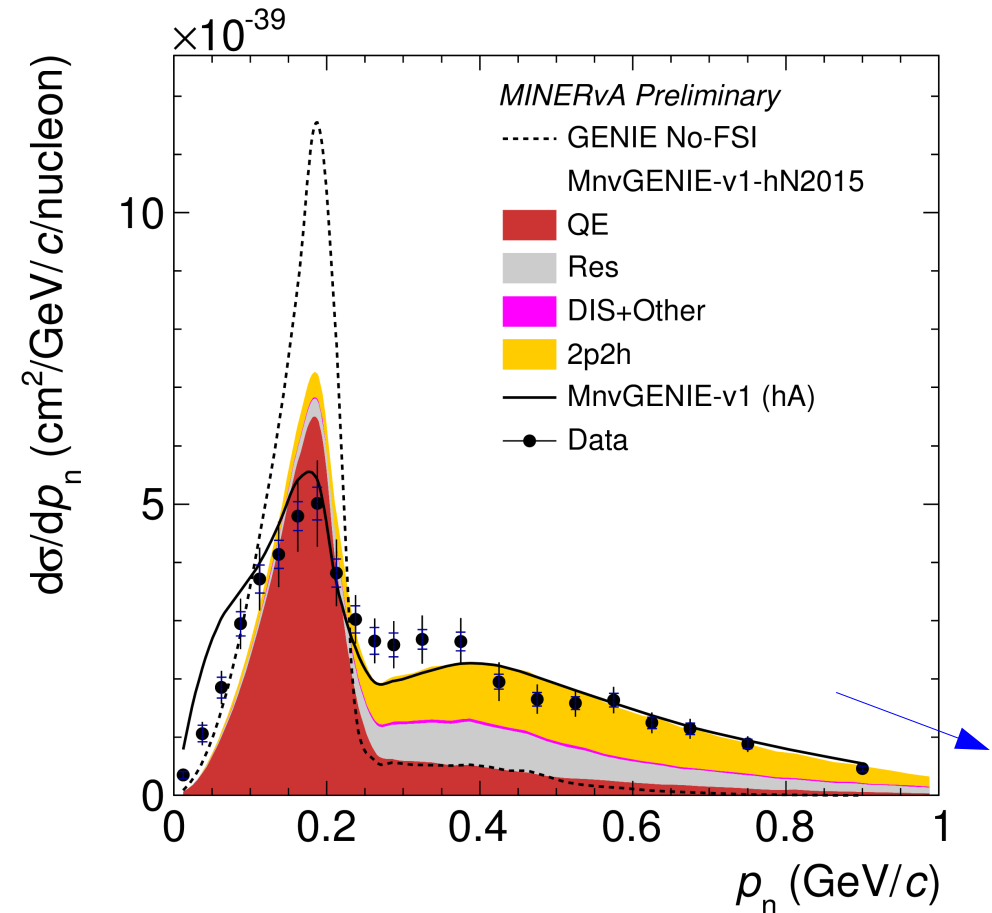
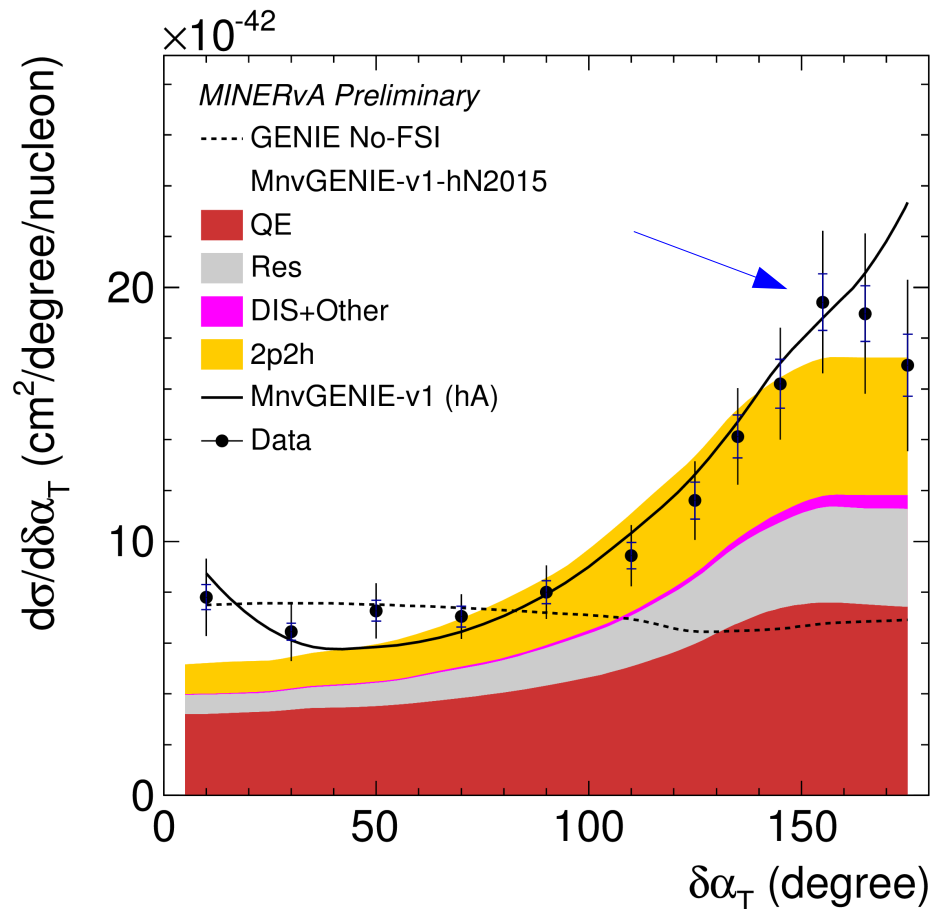
No p-FSI acceleration



QE peak not distorted, but much narrower

# Advanced Topics: GENIE FSI

- (pre2015) hA: effective model, include “elastic component” in intranuclear scattering, used in GENIE MINERvA Tune (v1)
- hA2015: removed “elastic component”, replacing hA in MnvGENIE-v1-hA2015
- hN2015: full cascades + Oset, replacing hA in MnvGENIE-v1-hN2015



hA2015 and hN2015 difference in

- Large  $\delta\alpha_T$  (concentrated)
- $p_n$  tail (diluted)

# ADVANCED TOPICS: NUWRO

# Simulation: GENIE [Nucl.Instrum.Meth. A614 (2010) 87-104]

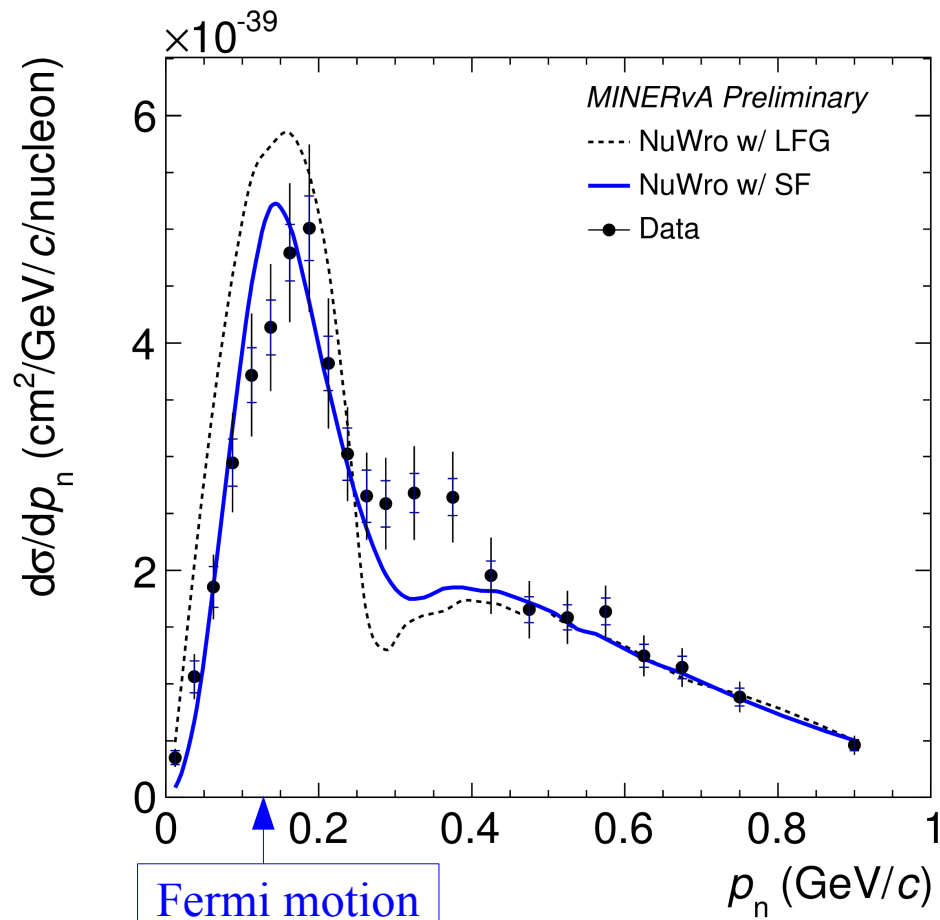
- **Nominal:** version 2.8.4
  - ✓ global Fermi Gas (RFG) model with Bodek-Ritchie (BR) tail [Phys. Rev. D 23, 1070 (1981)]
  - ✓ hA FSI [AIP Conf.Proc. 1405 (2011) 213-218]
- **No-FSI:** Nominal without FSI
- **MnvGENIE-v1: GENIE MINERvA Tune (v1) [only 2p2h relevant for this analysis]**
  - Added Random Phase Approximation (RPA) [Phys.Rev. C70 (2004) 055503]
  - Non-resonance pion production scaled down by 75% [Phys.Rev. D90 (2014) no.11, 112017]
  - Valencia 2p2h [Nieves *et al.*, Phys.Lett. B707 (2012) 72-75, Phys. Rev. C 86, 015504 (2012), Phys.Rev. D88 (2013) no.11, 113007, arXiv:1601.02038]
    - ✓ tuned to MINERvA inclusive data → significant enhancement in small 4-momentum transfer region [Phys.Rev.Lett. 116 (2016) 071802]

# Simulation: NuWro [Phys.Rev. C86 (2012) 015505]

- Version: 11q
  - ✓ Local Fermi Gas (LFG) or Spectral Function (SF) [Benhar *et al.*, Nucl.Phys. A579 (1994) 493-517]
  - ✓ FSI: intranuclear cascades of hadronic interactions + Oset model [Nucl.Phys. A484 (1988) 557-592]
- Valencia 2p2h [Nieves *et al.*, Phys.Lett. B707 (2012) 72-75, Phys. Rev. C 86, 015504 (2012)]

# Advanced Topics: NuWro

- Fermi motion

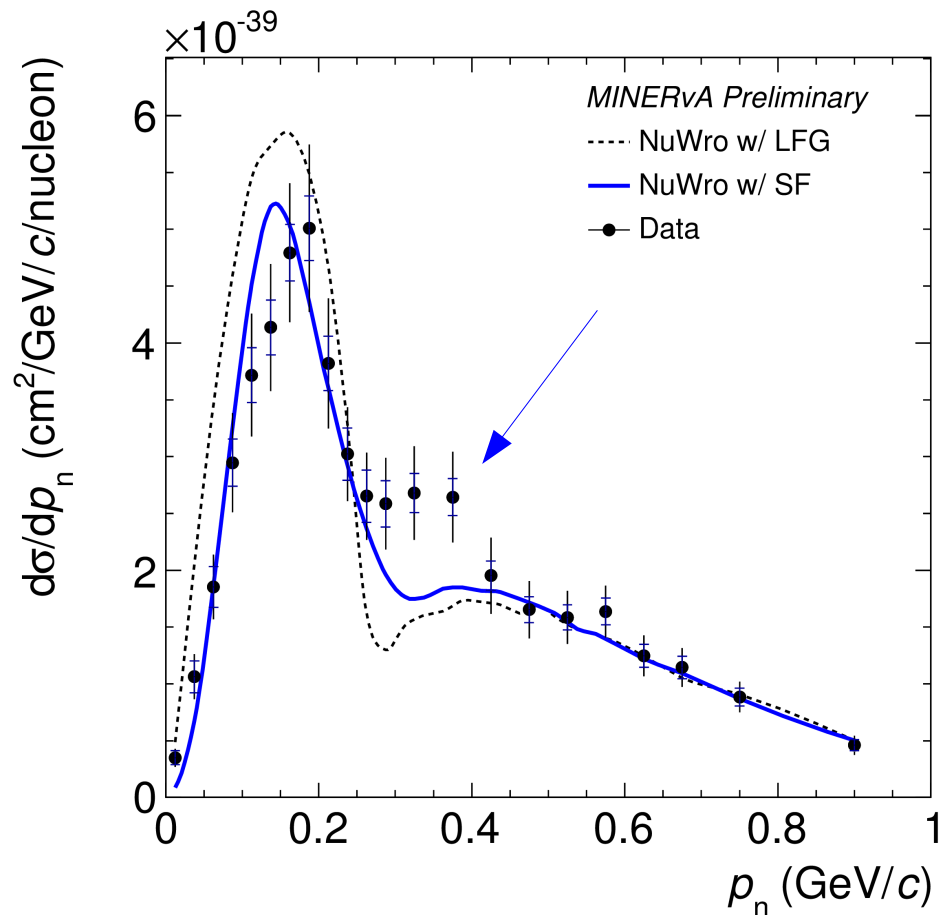


$\Delta p$  small  $\rightarrow$   $\Delta p$  large  
(intranuclear momentum transfer)

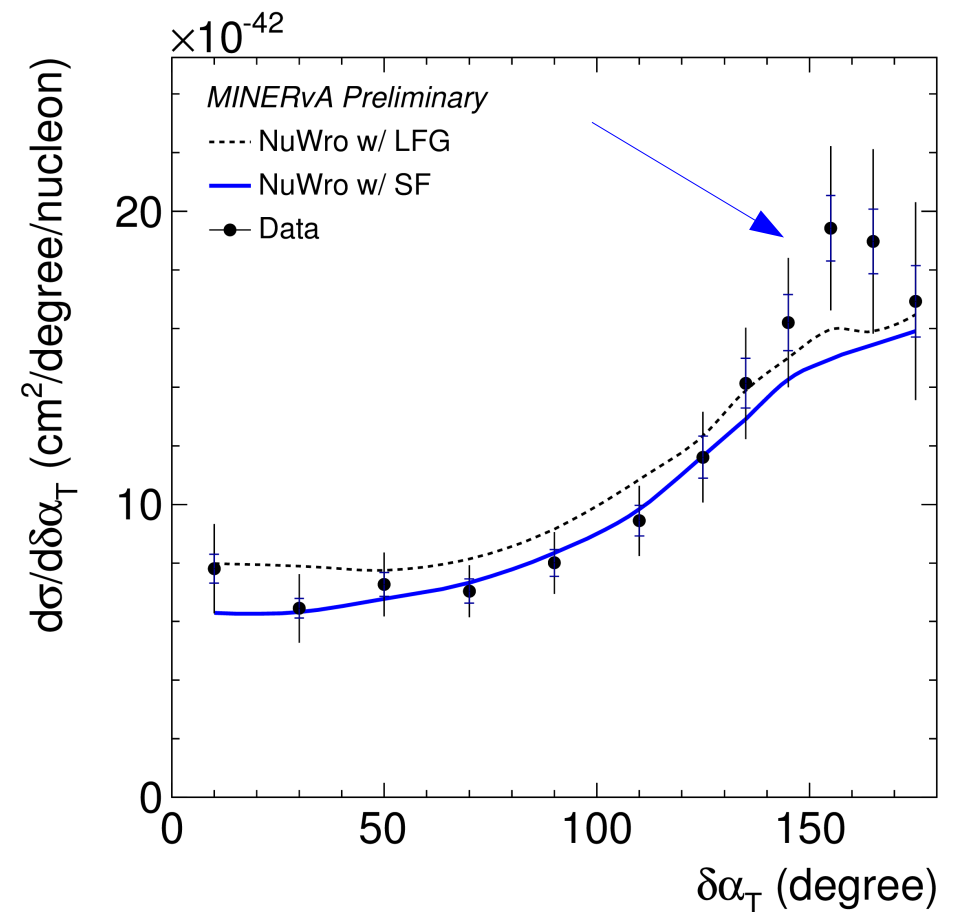
SF describes Fermi motion very well

# Advanced Topics: NuWro

- Fermi motion
- Resonance / 2p2h strength



$\Delta p$  small  $\rightarrow$   $\Delta p$  large  
(intranuclear momentum transfer)



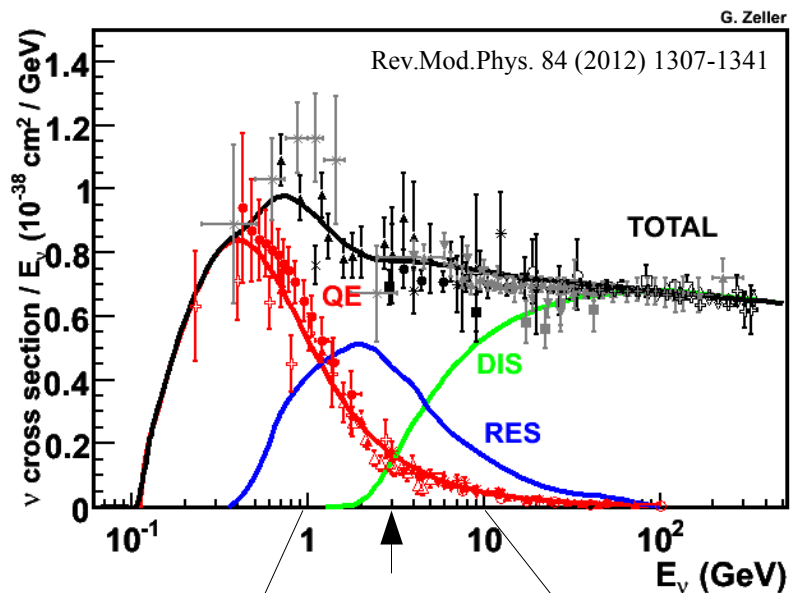
SF describes Fermi motion very well  
Resonance / 2p2h lacks of local strength

# ADVANCED TOPICS: COMPARISON TO T2K

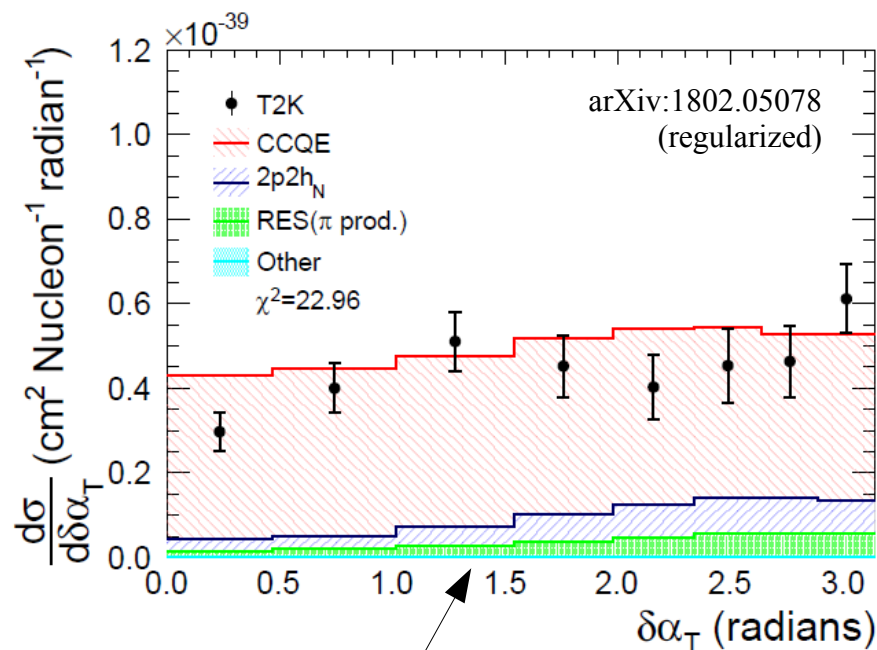
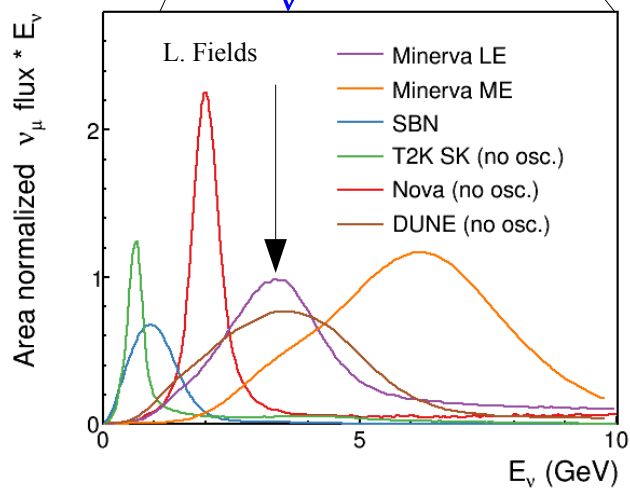
# Advanced Topics: Comparison to T2K

[arXiv:1802.05078] \*same target, slight difference in signal phase space definition

- $\delta\alpha_T$



NuMI LE  
 $\langle E_\nu \rangle \sim 3$  GeV



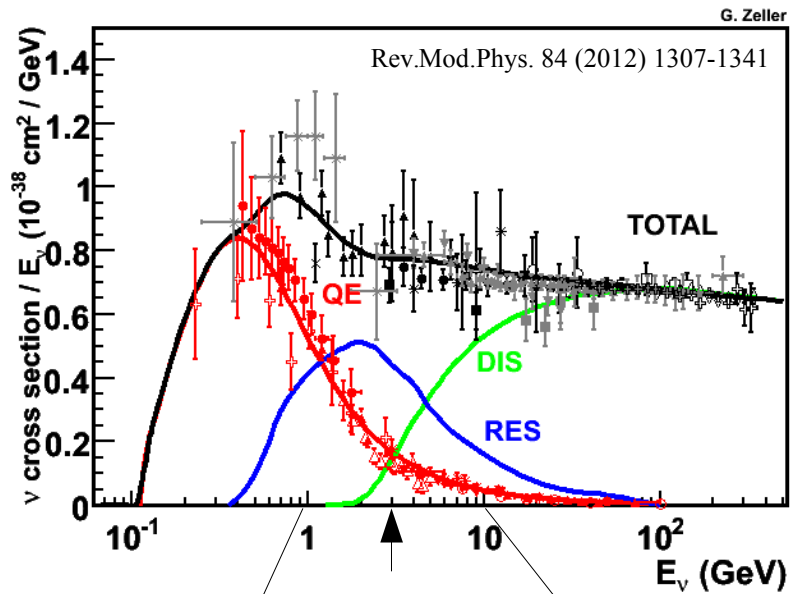
MINERvA-T2K difference mainly due to RES:  
Very small resonance contribution at T2K



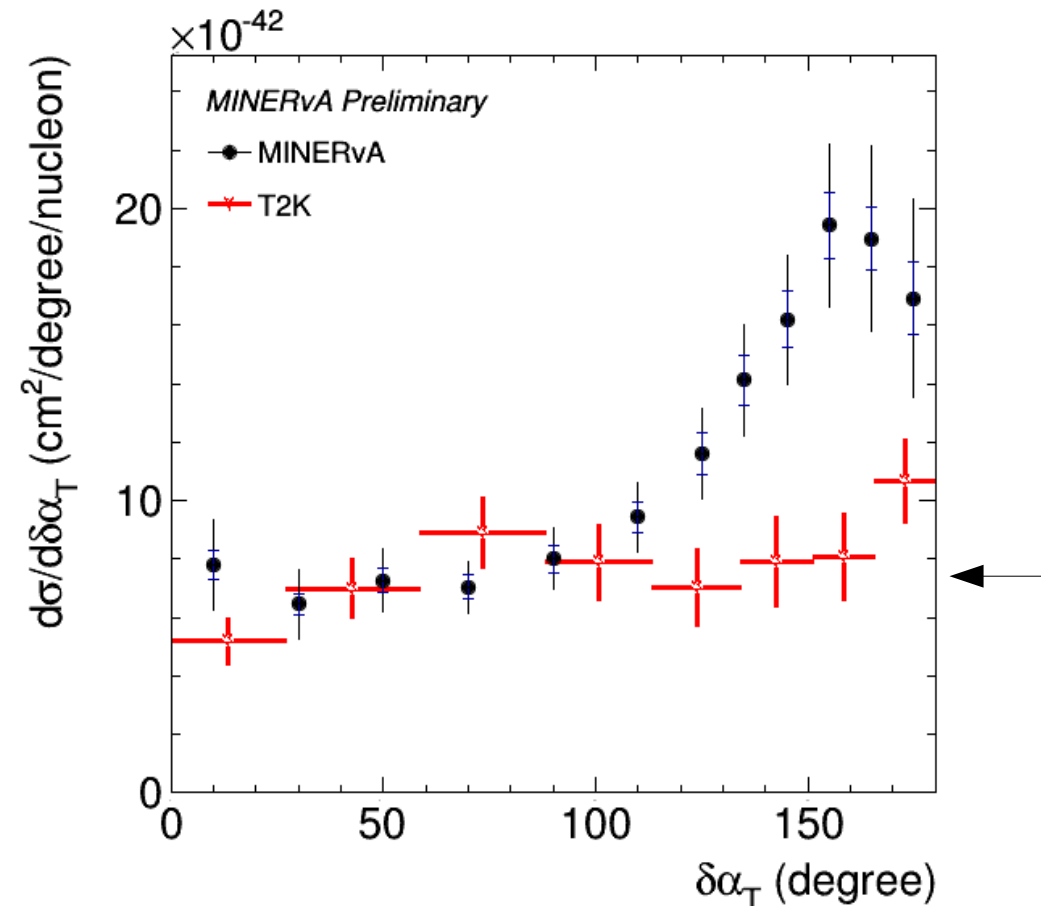
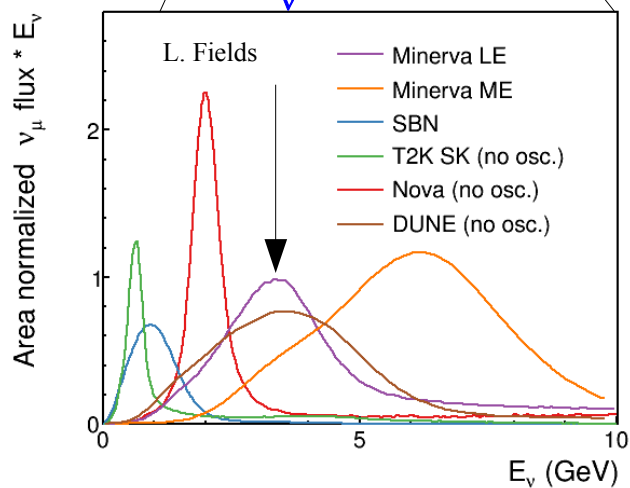
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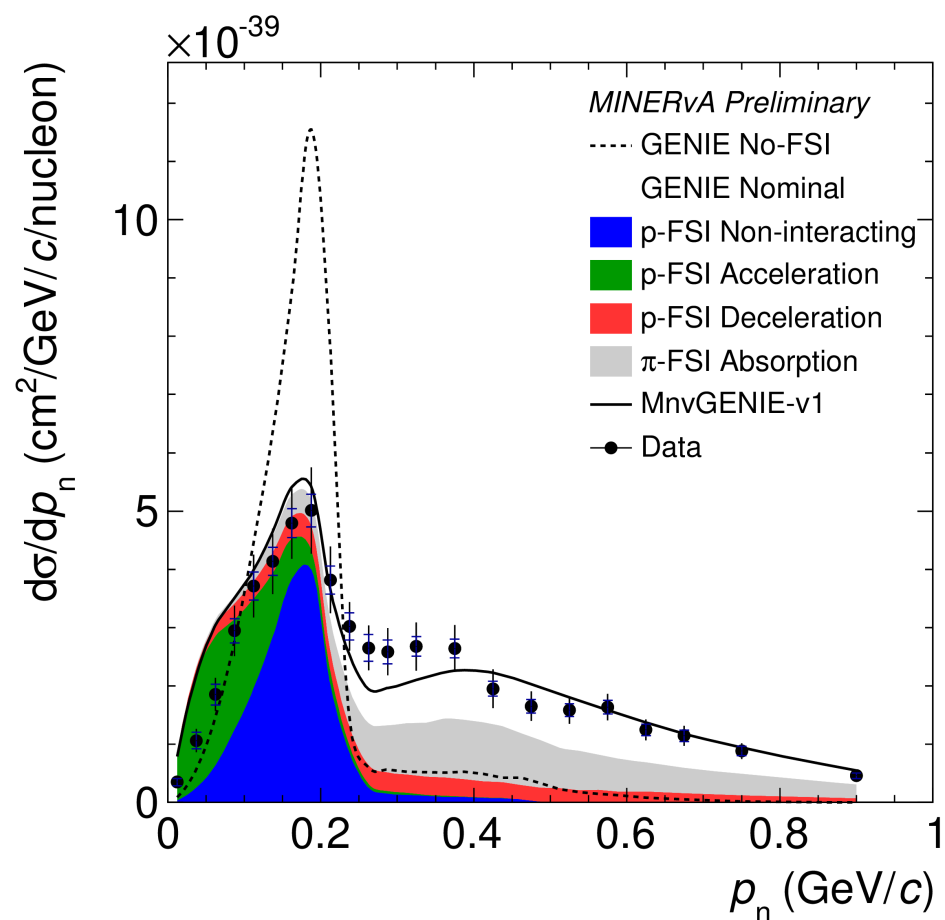
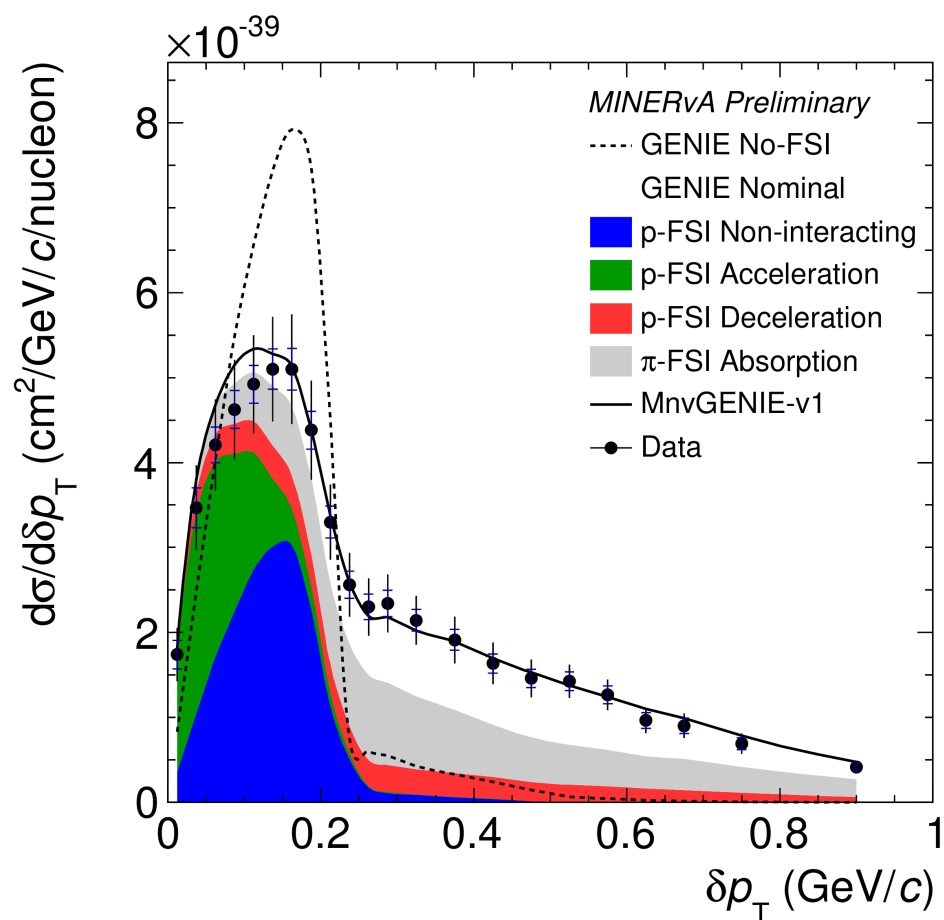


MINERvA-T2K difference mainly due to RES  
Fermi motion (isotropic) baseline consistent

# Advanced Topics: Comparison to T2K

[arXiv:1802.05078] \*same target, slight difference in signal phase space definition

- $\delta\alpha_T$
- $\delta p_T$



$$\delta\vec{p}_T = \vec{p}_T^N - \Delta\vec{p}_T$$

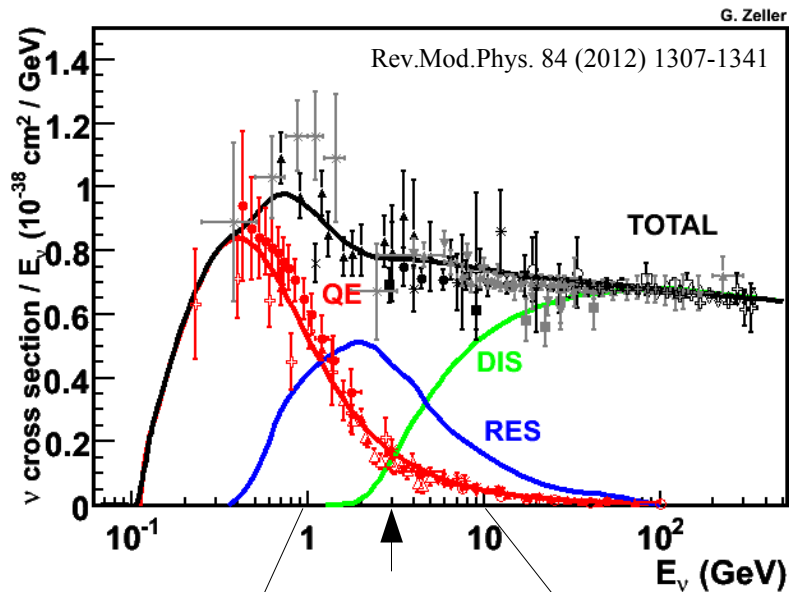
$$p_n \equiv \sqrt{\delta p_T^2 + \delta p_L^2}$$

Only differ by longitudinal momentum imbalance  
 $p_n$  has better resolution

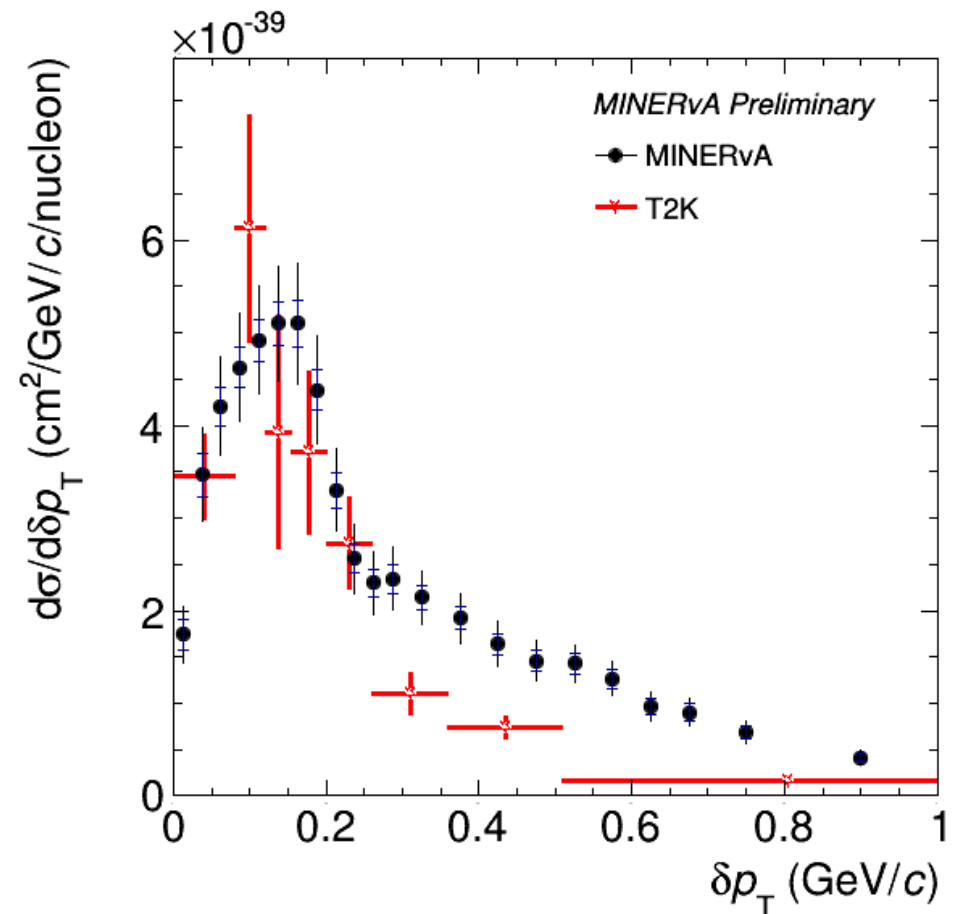
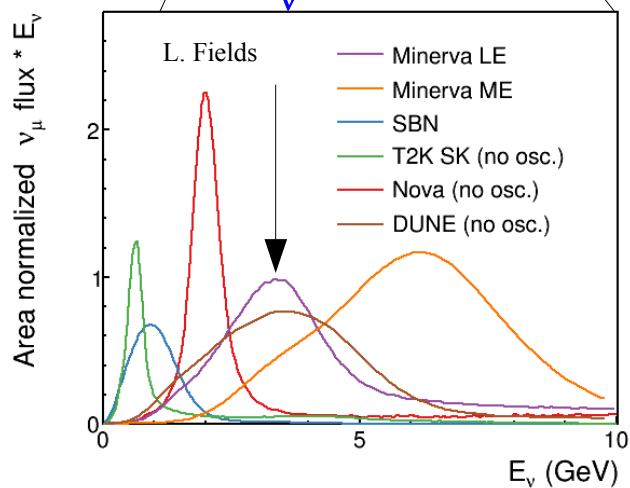
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- $\delta\alpha_T$
- $\delta p_T$

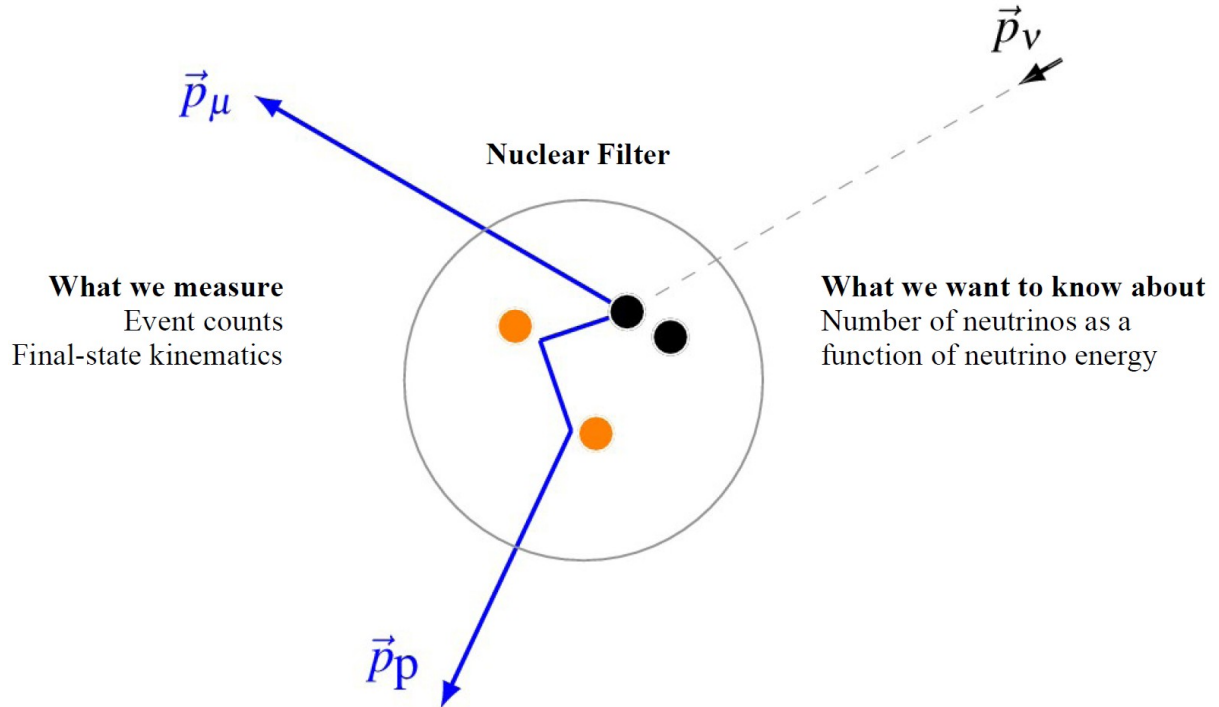
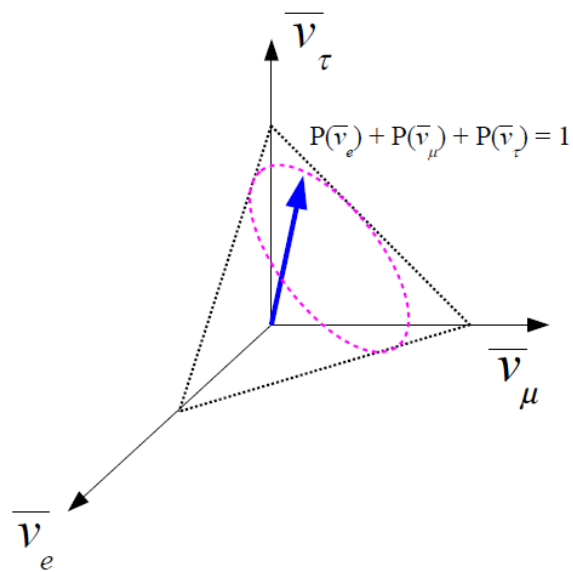
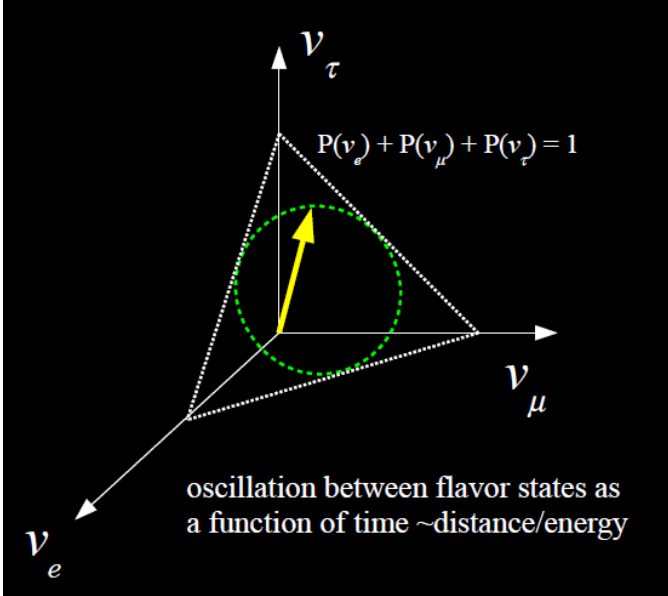


NuMI LE  
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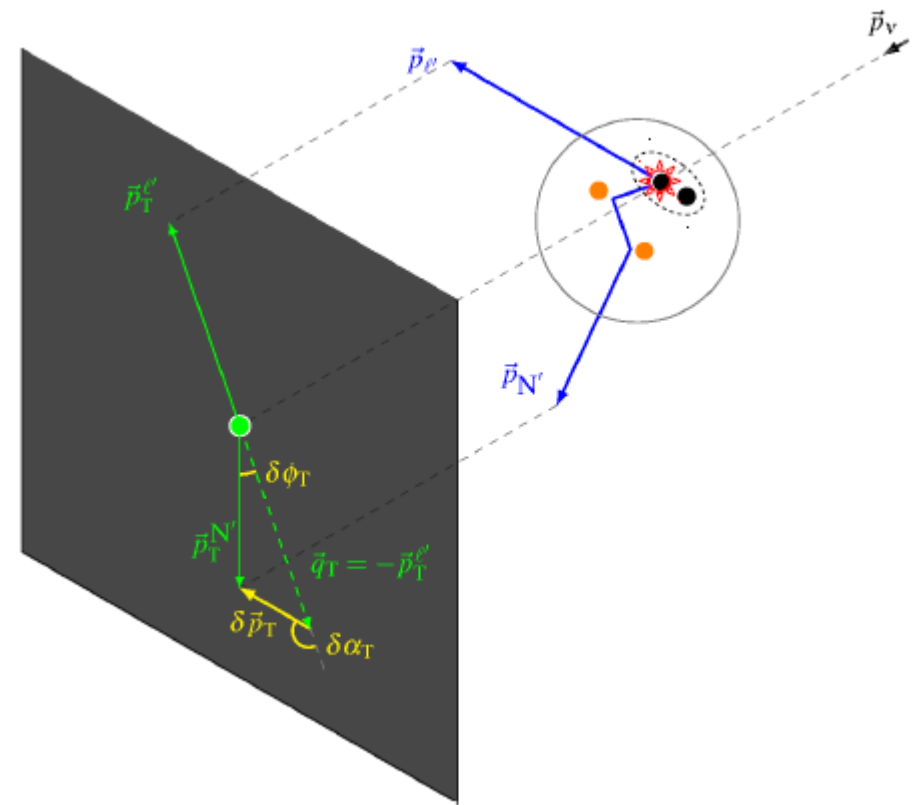


MINERvA-T2K difference mainly due to RES  
The QE peaks are consistent

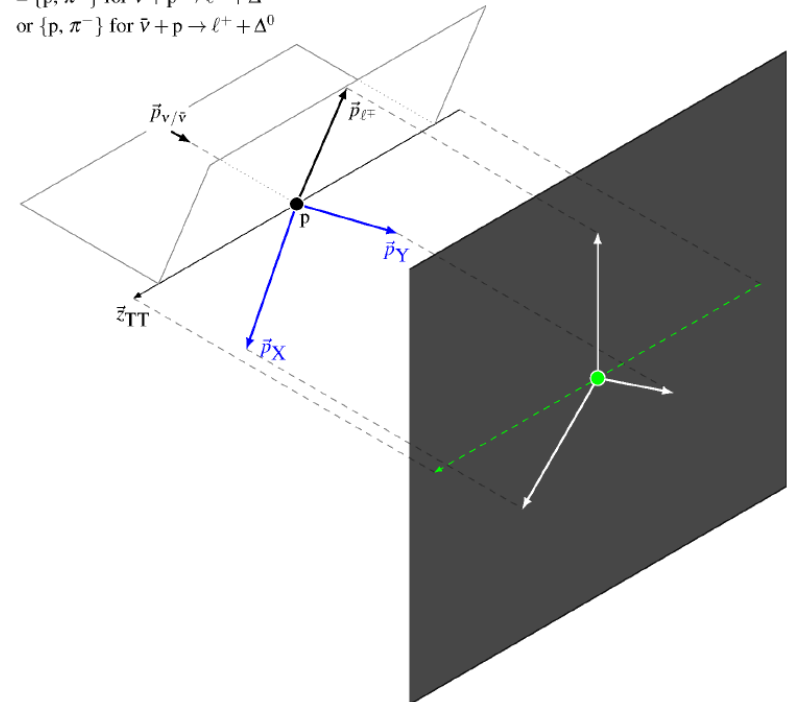
# Summary and Outlook



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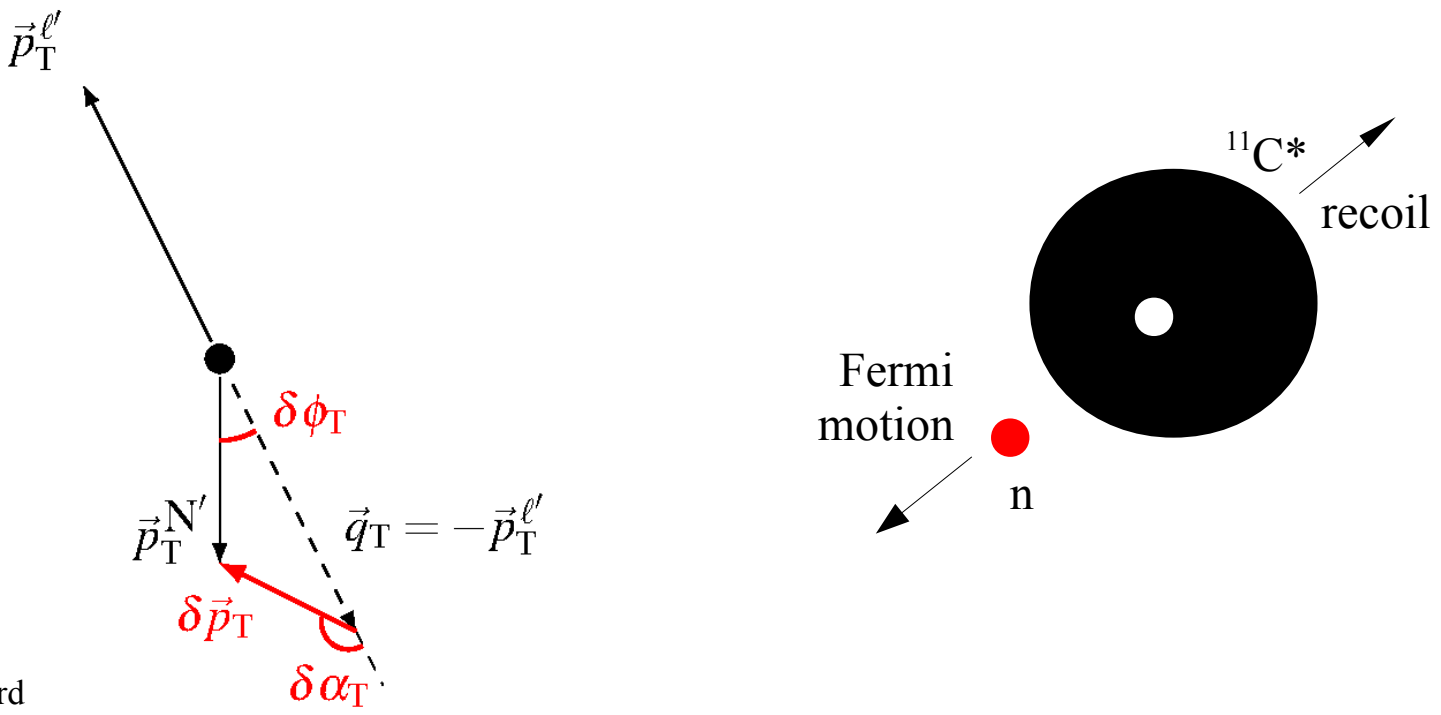


= {p,  $\pi^+$ } for  $v + p \rightarrow \ell^- + \Delta^{++}$   
 or {p,  $\pi^-$ } for  $\bar{v} + p \rightarrow \ell^+ + \Delta^0$



# Summary and Outlook

- Muon-proton mesonless production at MINERvA
  - 2014: LE neutrino beam, CH target
  - 2016: LE neutrino beam, CH + nuclear targets
  - **This analysis:** LE neutrino beam, CH ( $3.28 \times 10^{20}$  POT)
  - **Future: medium energy neutrino beam CH + nuclear targets** ( $E_\nu \sim 6$  GeV,  $12 \times 10^{20}$  POT)
- In this analysis, we have shown
  - ✓ Single-particle kinematics (muon and proton momentum and angle)
  - ✓ Transverse kinematic imbalances ( $\delta\alpha_T, \delta p_T$ )
  - ✓ Initial neutron momentum ( $p_n$ )

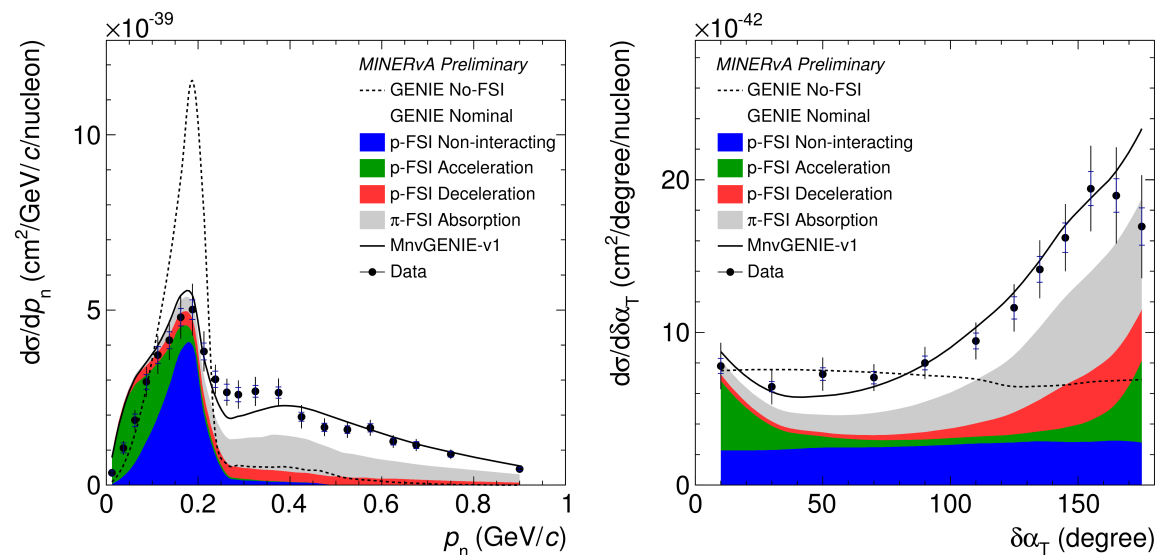


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By rearranging final-stat kinematics, nuclear effects can be diagnosed:

- ✓  $p_n$  strong constraint to Fermi motion
- ✓  $\delta\alpha_T$  factors out Fermi motion uncertainty and have direct sensitivity to FSI



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Interesting observation:

- GENIE MINERvA Tune (v1)
  - ✓ Describes data well to first order
  - ✓ Critical component is Valencia 2p2h tuned to MINERvA inclusive data
- NuWro
  - ✓ SF provides very good description of data



# Summary and Outlook

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  - ✓ Initial neutron momentum ( $p_n$ )
- **New developments**
  - Transverse kinematic imbalances
    - ✓ New system to solve the nuclear effect problem in neutrino interaction most relevant for oscillation measurements
    - ✓ Radical approach → double transverse kinematic imbalance [Phys. Rev. D 92, 051302(R)]
  - First measurement of Furmanski-Sobczyk initial neutron momentum
    - ✓ diagnostic power
    - Practically efficient way to select pure CCQE events (beyond the scope of this talk)

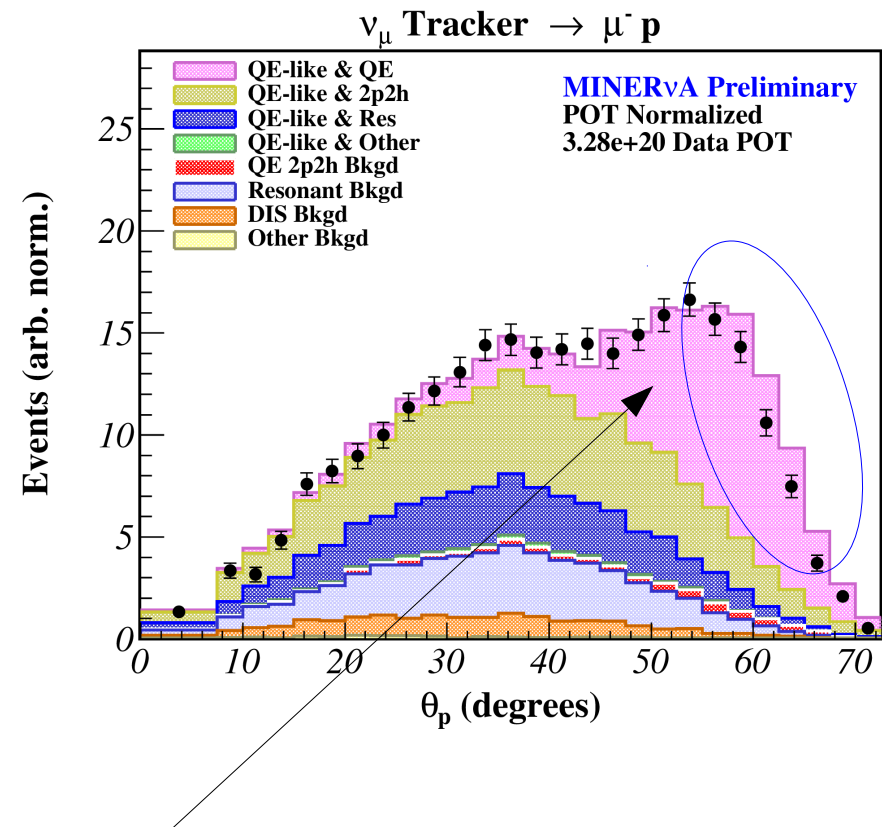


Source: <http://www.cnhubei.com/ztmjys-pyts>

# BACKUP

# Selected Sample

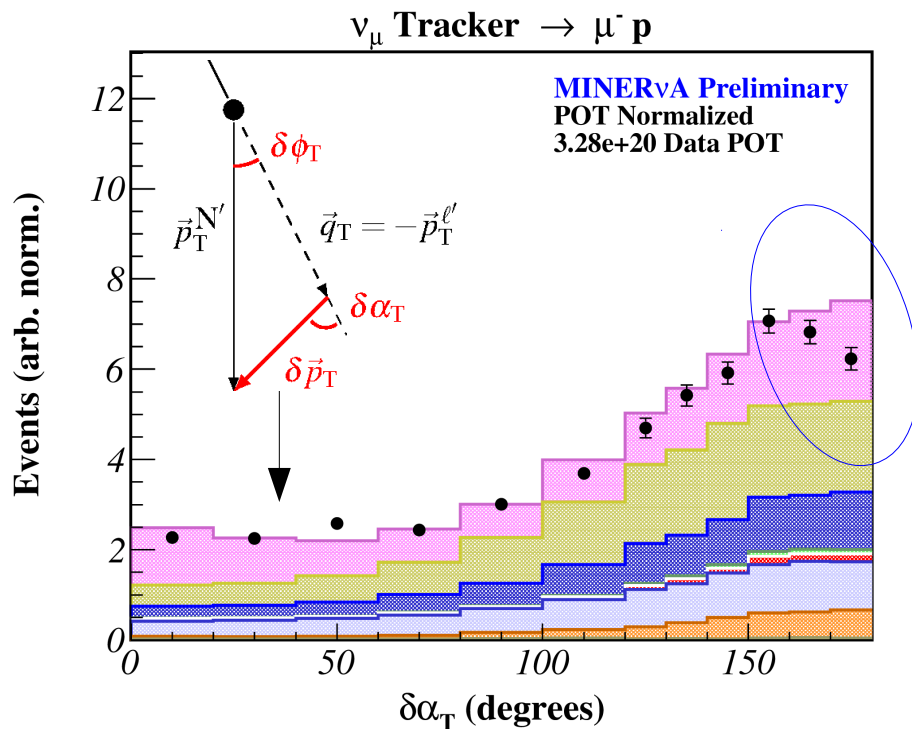
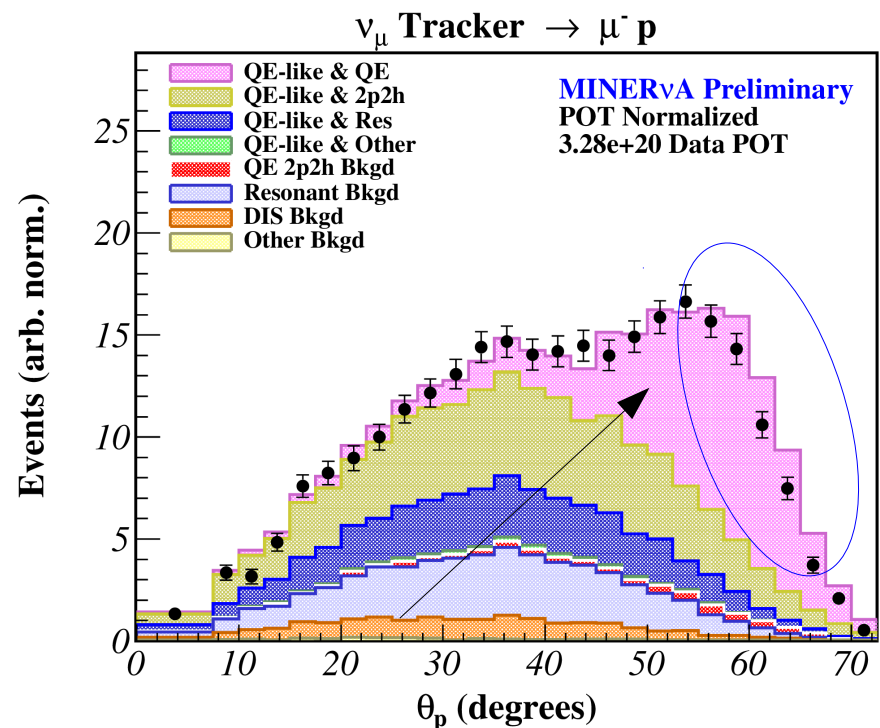
- Data-MC comparison at reconstructed level after sideband fit



GENIE MINERvA Tune (v1) describes data well (to first order)  
Large concentration of pure QE at high angle  
GENIE excess above data beyond 60 deg (see discussion later slides)

# Selected Sample

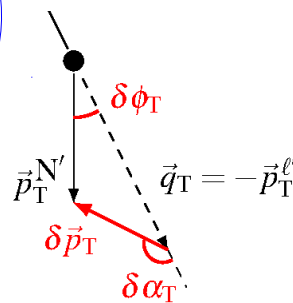
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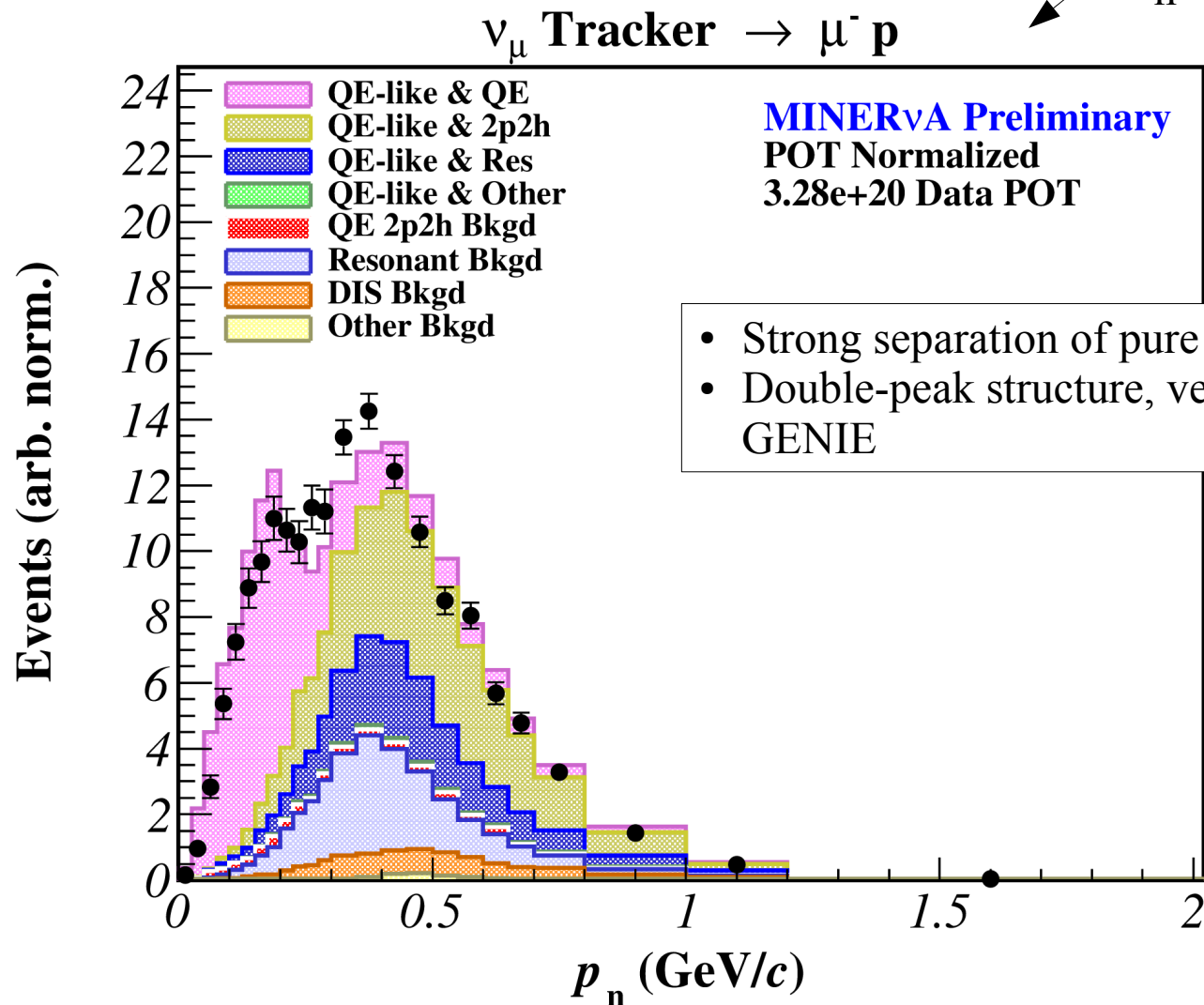
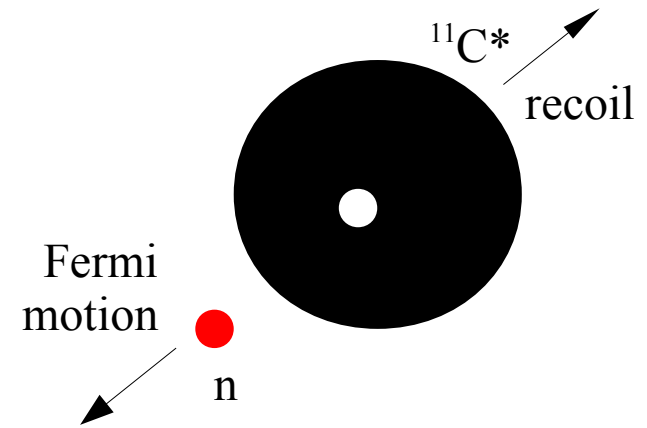
Depletion at small  $\delta\alpha_T$

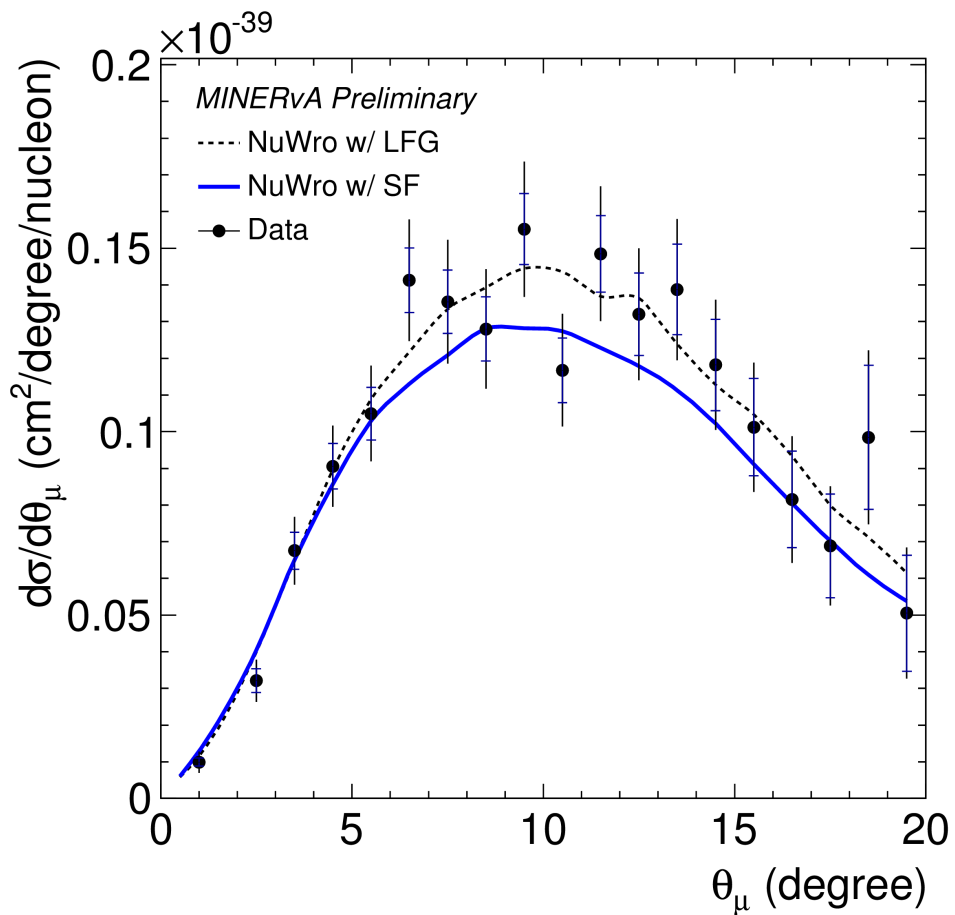
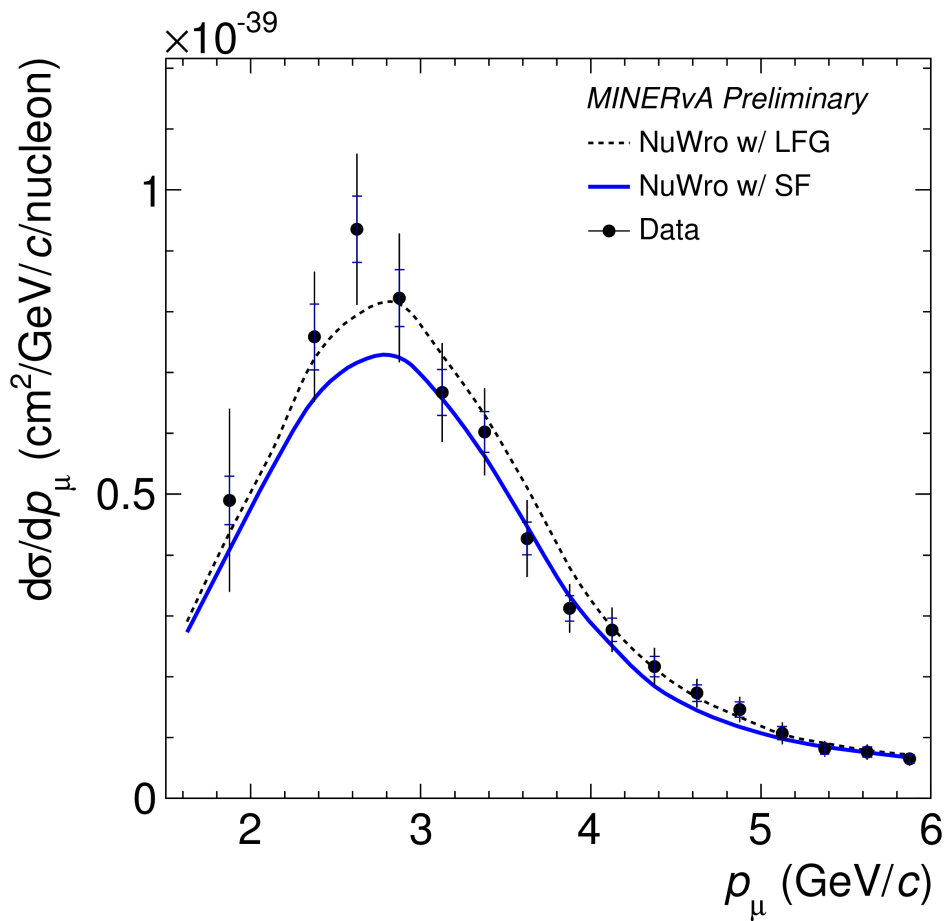
GENIE excess at  $\delta\alpha_T \rightarrow 180$  deg.

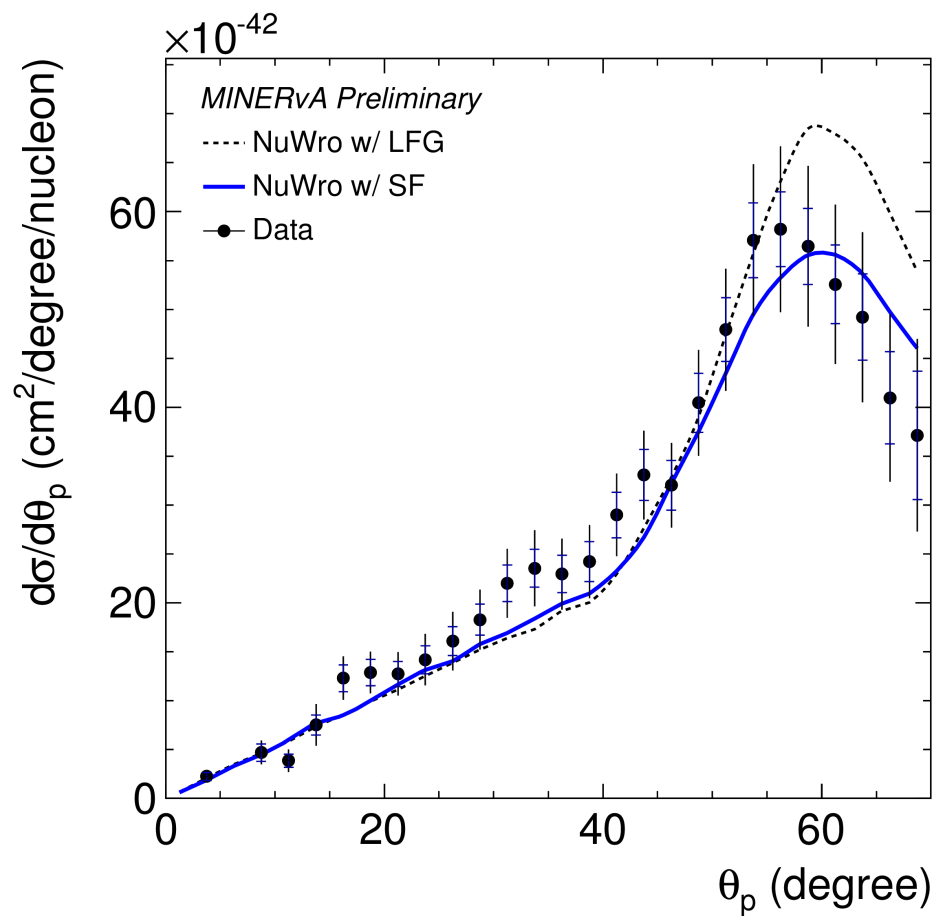
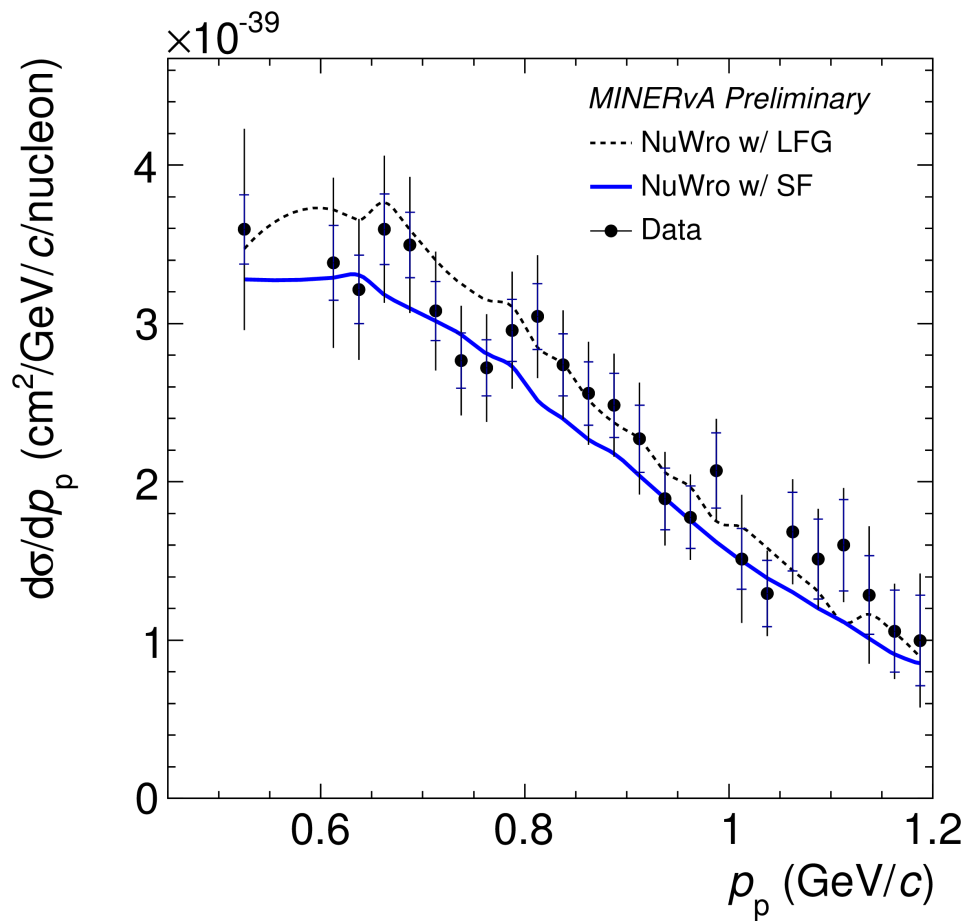


# Selected Sample

- Data-MC comparison at reconstructed level after sideband fit









66.4 deg



Analysis	$p_p$	$\cos\theta_p$	$p_\mu$	$\cos\theta_\mu$
Multi-dimensional	$> 500$ MeV	-	-	-
STV	450-1000 MeV	$> 0.4$	$> 250$ MeV	$> -0.6$
Inferred kinematics	$> 450$ MeV	$> 0.4$	-	-

TABLE I. Signal phase space restrictions for the three analyses.

[arXiv:1802.05078](https://arxiv.org/abs/1802.05078)

END