

Experimentally determined nuclear-structure properties of 0v2ß decay candidates

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Nuclear ab initio theories and neutrino physics INT-18-1a Week 5, 29 March 2018



Overview

- Basic premises (ground-state nucleon occupancies, pairing)
- Experiments (now a 10-year project, 4 candidates 'done')
- Analysis techniques
- Normalizations
- Quenching
- $\circ~$ An overview of results, compared with theory
- Comments on pairing







Connecting half-life and mass





Engel and Menéndez, Rep. Prog. Phys. 80, 046301 (2017)



Nuclear matrix elements

$$[T_{1/2}^{0\nu}]^{-1} = (\text{Phase Space Factor}) \times |\text{Nuclear Matrix Element}|^2 \times |\langle m_{\beta\beta} \rangle|^2$$

$$T_{1/2}^{0\nu} \propto a \cdot \epsilon \cdot \sqrt{\frac{M \cdot t}{B \cdot \Delta E}} \propto 1/|\text{NME}|^2$$

Experimental searches are often discussed in terms of their sensitivity to a given half life, accounting for enrichment, efficiency, backgrounds, resolution, and mass, though NP has a significant role ...



Figure taken from one of Jason Detwiler's talks found online



Mechanism, rationale



 76Se
 77Se
 78Se

 75As
 ββ
 77As

 74Ge
 75Ge
 76Ge

Ground states

- Single- and two-particle properties should be important:
 - How do the protons and neutrons rearrange themselves going from the initial to final state? (we can probe that)
 - Are the ground states 'simple' BCS like states? (we can probe that too) Bernadette Rebeiro talked about this earlier in the week
- Can knowledge of the above inform or constrain theoretical calculations?
- How well are the uncertainties (in the analysis of the experimental data) understood?
- (Are all these things not already known (after all, these are [essentially] stable isotopes?)



Series of experiments

Single-nucleon and two-nucleon transfer on nuclei involved in the $^{76}Ge \rightarrow ^{76}Se$, $^{100}Mo \rightarrow ^{100}Ru$, $^{130}Te \rightarrow ^{130}Xe$, and $^{136}Xe \rightarrow ^{136}Ba$ decays

Original works, including cross sections and analyzed data:

S. J. Freeman et al., Phys. Rev. C 75, 051301(R) (2007): A = 76 neutron pairing
J. P. Schiffer et al., Phys. Rev. Lett. 100, 112501 (2008): A = 76 neutron occupancies
B. P. Kay et al., Phys. Rev. C 79, 021301(R) (2009): A = 76 proton occupancies
T. Bloxham et al., Phys. Rev. C 82, 027308 (2010): A = 130 neutron (and proton) pairing
J. S. Thomas et al., Phys. Rev. C 86, 047304 (2012): A = 100 neutron pairing
B. P. Kay et al., Phys. Rev. C 87, 011302(R) (2013): A = 130 neutron occupancies
A. Roberts et al., Phys. Rev. C 87, 051305(R) (2013): A = 76 proton pairing
J. P. Entwisle et al., Phys. Rev. C 93, 064312 (2016): A = 130 and A = 136 proton occupancies
S. V. Szwec et al., Phys. Rev. C 94, 054314 (2016): A = 136 neutron occupancies
S. J. Freeman et al., Phys. Rev. C 96, 054325 (2017): A = 100 proton and neutron occupancies

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D. K. Sharp et al., upcoming works on A = 116, 124, and 150 neutron occupancies



Collaborators

Initiative led by Argonne and Manchester groups *Experiments at MLL (Munich), WNSL (Yale), RCNP (Osaka), and IPN (Orsay)* [Tandem facilities (except of RCNP), with beams around 10 MeV/u, high-resolution magnetic spectrographs. They are among the few facilities left in the world where these measurements are possible.]

J. P. Schiffer, S. J. Freeman, J. A. Clark, C. Deibel, C. R. Fitzpatrick, S. Gros, A. Heinz, D. Hirata, C. L. Jiang, B. P. Kay, A. Parikh, P. D. Parker, K. E. Rehm, A. C. C. Villari, V. Werner, C. Wrede, T. Adachi, H. Fujita, Y. Fujita, P. Grabmayr, K. Hatanaka, D. Ishikawa, H. Matsubara, Y. Meada, H. Okamura, Y. Sakemi, Y. Shimizu, H. Shimoda, K. Suda, Y. Tameshige, A. Tamii, T. Bloxham, S. A. McAllister, S. J. Freedman, K. Han, A. M. Howard, A. J. Mitchell, D. K. Sharp, J. S. Thomas, J. P. Entwisle, A. Tamii, S. Adachi, N. Aoi, T. Furuno, T. Hashimoto, C. R. Hoffman, E. Ideguchi, T. Ito, C. Iwamoto, T. Kawabata, B. Liu, M. Miura, H. J. Ong, G. Süsoy, T. Suzuki, S. V. Szwec, M. Takaki, M. Tsumura, T. Yamamoto T. E. Cocolios, L. P. Gaffney, V. Guimarães, F. Hammache, P. P. McKee, E. Parr, C. Portail, N. de Séréville, J. F. Smith, I. Stefan, ++

Now more 70 collaborators as participants in the various experiments



Focus of this talk

 $\pi = v$

⁷⁶ Se	⁷⁷ Se	⁷⁸ Se
⁷⁵ As	⁷⁶ As	⁷⁷ As
⁷⁴ Ge	⁷⁵ Ge	⁷⁶ Ge

$$\pi = v$$

¹³⁰ Xe	¹³¹ Xe	¹³² Xe
129	130J	131
¹²⁸ Te	¹²⁹ Te	¹³⁰ Te

$$\pi = v$$

¹³⁶Ba

¹³⁵Cs

¹³⁴Xe

¹³⁷Ba

¹³⁶Cs

¹³⁵Xe

¹³⁸Ba

¹³⁷Cs

¹³⁶Xe

π	≠	υ
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¹⁰⁰ Ru	¹⁰¹ Ru	¹⁰² Ru
⁹⁹ Tc	¹⁰⁰ Tc	¹⁰¹ Tc
⁹⁸ Mo	⁹⁹ Mo	¹⁰⁰ Mc









Transfer reactions (what is measured)

Around 10 MeV/u (direct reactions) Variety of reactions (momentum matching)



Spectra from BPK et al., Phys. Rev. C 87, 011302(R) (2013)

Transfer reactions (what is inferred)

Measure at several angles, shapes characteristic of *l*



Nuclear structure (a parameterized model)

- >50 years experience / refinement
- Parameterized (Wood-Saxon potentials, derivatives)
- Lots of logical check points (e.g., *parameters are consistent with those derived from electron scattering ... radii*, etc.), a wealth of nucleon-scattering data
- The spectroscopic factor is a 'reduced cross section' modest corrections to account for kinematics and spins



Distorted-wave Born Approximation, requires several ingredients and experimental consideration. ISPM cross sections.



Does it work? / model dependency? etc.

- Need a normalization
- Typical uncertainty is between +/-0.1-0.2 nucleons
- Demonstrated in many systems (groups of isotopes/isotones) across the chart of nuclides

$$S' \equiv \sigma_{\rm exp} / \sigma_{\rm DWBA}$$

$$N_j \equiv S'/S$$

$$N_j \equiv (\Sigma G_+ S'_{\text{adding}} + \Sigma G_- S'_{\text{removing}})/(2j+1)$$

• But is the normalization just arbitrary?

Ni occupancies from J. P. Schiffer et al., Phys. Rev. Lett. **108**, 022501 (2012)

REVIEWS OF MODERN PHYSICS

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Stripping Reactions and the Structure of Light and Intermediate Nuclei*

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AND

J. B. FRENCH

University of Rochester, Rochester, New York





JULY, 1960

Analysis, e.g., ⁷⁶Ge,Se







Analysis - sum rules and normalization

Е	l	S'	Е	l	(2 <i>j</i> +1)S
0	1	0.45	 160	4	0.44
191	4		100	l. I	0.44
248	1	0.12	225	4	
317	3		421	2	
457	3		505	2	
575	1	1.29	000	4	0.15
651	3		629		0.15
885	1	0.10	884	2	
1137	1	0.11	1021	1	0.12
1250	3		10/18	1	0.04
1410	0		10-0		0.04
1451	1	0.37	1250	0	
1580	3		1385	2	

$$N_j \equiv \left[\sum S'_{\text{removing}} + \sum (2j+1)S'_{\text{adding}}\right]/(2j+1)$$

 $N_j \equiv [(0.45 + 0.12 + 1.29 + 0.10 + 0.11 + 0.37) + (0.44 + 0.15 + 0.12 + 0.04)]/(2 + 4) = 0.53$



Analysis - sum rules and normalization

E	ł	S'	S		Е	l	(2 <i>j</i> +1)S'	(2 <i>j</i> +1)S
0	1	0.45	0.85		100	4	0.44	0.00
191	4				160	I	0.44	0.82
248	1	0.12	0.23		225	4		
317	3			-	421	2		
457	3				505	2		
575	1	1.29	2.43		000	-	0.15	0.00
651	3				629	I	0.15	0.28
885	1	0.10	0.19		884	2		
1137	1	0.11	0.21		1021	1	0.12	0.22
1250	3				10/18	1	0.04	0.07
1410	0				1040		0.04	0.07
1451	1	0.37	0.70		1250	0		
1580	3				1385	2		

$$N_j \equiv \left[\sum S'_{\text{removing}} + \sum (2j+1)S'_{\text{adding}}\right]/(2j+1)$$

 $N_j \equiv [(0.45 + 0.12 + 1.29 + 0.10 + 0.11 + 0.37) + (0.44 + 0.15 + 0.12 + 0.04)]/(2 + 4) = 0.53$



What's the significance of the normalization

The normalization appears meaningful, a *ubiquitous feature* of low-lying singleparticle strength, independent of *A*, *I*, nucleon type, reaction, *N-Z*.

Reaction, ℓ transfer	Number of determinations	F_q	rms spread
$(e,e'p)$, all ℓ	16	0.55	0.07
$(d,p), (p,d), \ell = 0-2$	40	0.53	0.09
$(d,p), (p,d), \ell = 0-3$	46	0.53	0.10
$(\alpha, {}^{3}\text{He}), ({}^{3}\text{He}, \alpha), \ell = 4-7$	26	0.50	0.09
$(\alpha, {}^{3}\text{He}), ({}^{3}\text{He}, \alpha), \ell = 3-7$	34	0.52	0.09
$({}^{3}\text{He},d), \ \ell = 0-2$	18	0.54	0.10
$({}^{3}\text{He},d), \ \ell = 0-4$	26	0.54	0.09
$(\alpha,t), \ell = 4-5$	14	0.64	0.04
$(\alpha,t), \ell = 3-5$	18	0.64	0.04
All transfer data ^a	124	0.55	0.10





Quenching of s. p. cross sections

"Thus at any time only 2/3 of the nucleons in the nucleus act as independent particles moving in the nuclear mean field. The remaining third of the nucleons are correlated."*

Key points:

- Academic in terms of change in occupancies
- Arguably essential in terms of trusting the data
- How does theory handle it?





Quenching factor (a bit more)

There are a handful of isotopes where reliable experimentally determined cross sections exist from numerous 'equivalent' probes, e.g., proton removal from ¹²C. A consistent picture emerges.



Evaluated Nuclear Structure Data File (www.nndc.bnl.gov)



Quenching factor, theory

- *Tempting* to conclude it is well understood
- Not captured in, e.g., shell model (SM does not explicitly include SRC)
- Ab initio calculations do capture it (in light nuclei)



Model	${S \atop 0^+}$	${S \over 2^+}$	${S \over 0^+ + 2^+}$
Expt. $(1p)$	0.42(4)	0.16(2)	0.58(5)
VMC $(1p)$	0.41	0.18	0.59
VMC $(1p + 1f)$	0.41	0.19	0.60

Lapikas, Wessling, and Wiringa, Phys. Rev. Lett. **82**, 4404 (1999)



Quenching factor (...)

- No obvious change with neutron excess (*np* dominates) or binding energy (at least near stability) [though new results about high mtm fractions ... and N/Z ratio]
- Note, there are very good (e,e'p) and (e,e'n) data on ⁴⁸Ca
- Arguably not necessary to explore (e,e'p) [no obvious facilities ... results agree with nucleon transfer]



 Does it relate to quenching of g_A? In the sense that there is missing physics / model space, and correlations, in the calculations

O. Hen et al., Science **346**, 614 (2014)



Aside: the g_A problem

(Shown earlier in the week)



FIG. 2. Ratios of GFMC to experimental values of the GT RMEs in the ³H, ⁶He, ⁷Be, and ¹⁰C weak transitions. Theory predictions correspond to the χ EFT axial current in LO (blue circles) and up to N4LO (magenta stars). Green squares indicate "unquenched" shell-model calculations from Ref. [17] based on the LO axial current.

PHYSICAL REVIEW C 97, 022501(R) (2018)

Rapid Communication

Quantum Monte Carlo calculations of weak transitions in A = 6-10 nuclei

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Ab initio calculations of the Gamow-Teller (GT) matrix elements in the β decays of ⁶He and ¹⁰C and electron captures in ⁷Be are carried out using both variational and Green's function Monte Carlo wave functions obtained from the Argome ν_{11} two-nucleon and Illinois's Three-nucleon interactions, and axial many-body currents derived from either meson-exchange phenomenology or chiral effective field theory. The agreement with experimental data is excellent for the electron captures in ⁷Be, while theory overestimates the ⁶He and ¹⁰C data by $\sim 2\%$ and $\sim 10\%$, respectively. We show that for these systems correlations in the nuclear wave functions are crucial to explaining the data, while many-body currents increase by $\sim 2-3\%$ the one-body GT contributions.

PHYSICAL REVIEW C 97, 014606 (2018)

Neutrinoless double- β decay matrix elements in light nuclei

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We present the first *ab initio* calculations of neutrinoless double- β decay matrix elements in A = 6-12 nuclei using variational Monte Carlo wave functions obtained from the Argonne v₁₈ two-nucleon potential and Illinois-7 three-nucleon interaction. We study both light Majorana neutrino exchange and potentials arising from a large class of multi-TeV mechanisms of lepton-number violation. Our results provide benchmarks to be used in testing many-body methods that can be extended to the heavy nuclei of experimental interest. In light nuclei we also study the impact of two-body short-range correlations and the use of different forms for the transition operators, such as those corresponding to different orders in chiral effective theory.



... old results

Isotope	0 <i>f</i> _{5/2}	1 <i>p</i> _{1/2,3/2}	0g _{9/2}	Sum	Expect
⁷⁴ Ge	1.8	1.1	4.3	7.2	8
⁷⁶ Ge	1.4	1.1	3.5	6.0	6
⁷⁶ Se	2.2	1.6	4.2	8.0	8
⁷⁸ Se	2.3	0.9	2.8	6.1	6
Isotope	0 <i>f</i> _{5/2}	1 <i>p</i> _{1/2,3/2}	0g _{9/2}	Sum	Expect
⁷⁴ Ge	1.89	1.52	0.37	3.78	4
⁷⁶ Ge	1.75	2.04	0.23	4.02	4
⁷⁶ Se	2.09	3.17	0.86	6.12	6
⁷⁸ Se	2.35	1.82	2.05	6.22	6

J. P. Schiffer et al., Phys. Rev. Lett. **100**, 112501 (2008) [neutrons] BPK et al., Phys. Rev. C **79**, 021301(R) (2009) [protons]



Change in occupancy



J. P. Schiffer et al., Phys. Rev. Lett. **100**, 112501 (2008) [neutrons] BPK et al., Phys. Rev. C **79**, 021301(R) (2009) [protons] Rodin et al., Nucl. Phys. A **766**, 107 (2006) [A] Suhonen et al., Phys. Lett. B **668**, 277 (2006) [B] Caurier et al., Phys. Rev. Lett.**100**, 052503 (2008) [C]



Error bars are dominated by the systematic uncertainties relating to the analysis (Does not include more recent IBM results)



Impact?



Yes, some. Much discussed. A 40-70% reduction in the well-known gap between QRPA and the ISM, resulted. This predated recent IBM work and newer calculations.

Šimkovic et al., Phys. Rev. C 79, 055501 (2009) [quote]





A = 100 occupancies

J. Suhonen and O. Civitarese, Nucl. Phys. A **924**, 1 (2014) [WS, WS ADJ] J. Kotila and J. Barea, Phys. Rev. C **94**, 034320 (2016) [IBM]

High level density, Munich Q3D (as good as 8-keV FWHM resolution





Freeman et al., Phys. Rev. C **96**, 054325 (2017)







A Neacsu and M. Horoi, Phys. Rev. C **91**, 024309 (2015) [SM1] J. Menéndez et al., Nucl. Phys. A **818**, 139 (2009) [SM2] J. Kotila and J. Barea, Phys. Rev. C **94**, 034320 (2016) [IBM] J. Suhonen and O. Civitarese, Nucl. Phys. A **847**, 207 (2010) [QRPA]









A = 136 occupancies

A. Neacsu and M. Horoi, Phys. Rev. C **91**, 024309 (2015) [SM1] J. Menéndez et al., Nucl. Phys. A **818**, 139 (2009) [SM2] J. Kotila and J. Barea, Phys. Rev. C **94**, 034320 (2016) [IBM]

Taking advantage of ¹³⁶Xe being a good closed shell for neutrons





Comment on occupancies

• The agreement is perhaps qualitatively okay, in some instances within the uncertainties (but not for both protons and neutrons), but quite poor on the whole

We can ask whether it matters? ... it does, regardless of how (in)sensitive the NME is to the change in occupancies

While likely challenging theoretically, it would be interesting to know what the consequence of 'shutting off' part of the model-space would be (e.g. the $g_{7/2}$ neutrons above tin, or comparing e.g. JUN45 and GXPF1A – or even more simplistic approaches)



Pairing properties

Can the ground states of the candidates be described as 'seas' of correlated 0⁺ paired protons and neutrons?



Pairing around A ~ 76

Pair-transfer reactions are a simple and effective probe of pairing correlations No evidence of 'pairing vibrations' in the A = 76 region



A. Roberts et al., Phys. Rev. C 87, 051305(R) (2013) [protons]



Pairing around A ~ 100



A transitional region with deformation playing a role in the nuclear structure:

- Reactions leading to and from ¹⁰⁰Ru show ~95% of the L=0(p,t) strength is in the g.s. (on the spherical side of the transitional region)
- For ¹⁰⁰Mo about 20% of the L=0(p,t) strength is an excited 0⁺, a shape-transitional nucleus
- No evidence for pairing vibrations, but structure is complicated (proton work remains to be done)

J. S. Thomas et al., Phys. Rev. C 86, 047304 (2012)



Pairing around A ~ 130, 136



From the proton-pair adding Te(³He,*n*) reactions by Alford *et al.*, significant strength is seen in $\ell = 0$ transitions to excited states ...

A classic case of pair vibration and likely a consequence of a sub-shell gap at Z = 64Consequences for QRPA? (Does the shell-model include this feature also?)

T. Bloxham et al., Phys. Rev. C **82**, 027308 (2010) [neutrons] W. P. Alford et al., Nucl. Phys. A **323**, 339 (**1979**) [protons]



Summary

Experimental nuclear-structure data is an essential part of the story of the NME challenge

The candidates are *not 'generically similar' systems* (pairing, e.g. Z = 64, closed shells, deformation, etc., all different in each case)

'Traditional' calculations do not reliably reproduce information extracted from experiments (what level of agreement should we expect?)

New ab initio calculations likely essential (model space, interactions, Hamiltonians, correlations, weak currents, *all still being worked on*)

*E*0 lifetimes, Ge and Se (approved exp. at TRIUMF) Revisiting two-proton transfer [Xe(³He,*n*) at ANL] Other programs (e.g. *RCNPs CE reactions*, Catania DCE) And ... many more (most covered this week)

