

# MICROSCOPIC OPTICAL POTENTIAL FROM NN CHIRAL POTENTIALS

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# OPTICAL POTENTIAL

The OP provides a suitable framework to describe elastic nucleon-nucleus scattering

Its use can be extended to inelastic scattering and to calculate the cross section of a wide variety of nuclear reactions

In our models for QE electron and neutrino-nucleus scattering the OP describes FSI between the emitted nucleon and the residual nucleus

# OPTICAL POTENTIAL

**PHENOMENOLOGICAL:** assume a form and a dependence on a number of adjustable parameters for the real and imaginary parts that characterize the shape of the nuclear density distribution and that vary with the nuclear energy and the nucleus mass number.

Parameters obtained through a fit to pA elastic scattering data

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Parameters obtained through a fit to  $pA$  elastic scattering data

**Global OP:** the adjustable parameters are fitted in a range of nuclei at many different energies with a dependence of the coefficients in terms of  $A$  and  $E$

**A independent OP:** given for a single target nucleus

# OPTICAL POTENTIAL

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Parameters obtained through a fit to pA elastic scattering data

**THEORETICAL:** microscopic calculations require the solution of the full many-body nuclear problem. Some approximations are needed.

We do not expect better description of experimental data (at least for data in the database used to generate phen. OP) but greater predictive power when applied to situations where exp. data not available

# OPTICAL POTENTIAL

- Complex
- $E$  dependent
- Non local

M. Vorabbi, P. Finelli, C. Giusti, PRC 93 034619 (2016)

Theoretical optical potential derived from nucleon-nucleon chiral potentials

M. Vorabbi, P. Finelli, C. Giusti, PRC 93 034619 (2017)

Optical potential derived from nucleon-nucleon chiral potentials at N<sup>4</sup>LO

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PHYSICAL REVIEW

VOLUME 89, NUMBER 3

FEBRUARY 1, 1953

**Multiple Scattering and the Many-Body Problem—Applications to Photomeson Production in Complex Nuclei\***

KENNETH M. WATSON

*Physics Department, Indiana University, Bloomington, Indiana*

(Received October 1, 1952)

PHYSICAL REVIEW

VOLUME 92, NUMBER 2

OCTOBER 15, 1953

**The Elastic Scattering of Particles by Atomic Nuclei\***

N. C. FRANCIS AND K. M. WATSON†

*Department of Physics, Indiana University, Bloomington, Indiana*

(Received June 1, 1953)

**The Scattering of Fast Nucleons from Nuclei**

A. K. Kerman

*Massachusetts Institute of Technology, Cambridge, Massachusetts*

H. McManus

*Chalk River Laboratory, Chalk River, Ontario, Canada*

and

R. M. Thaler

*Los Alamos Scientific Laboratory, Los Alamos, New Mexico*

Received May 27, 1959



M. Vorabbi, P. Finelli, C. Giusti, PRC 93 034619 (2016)

Theoretical optical potential derived from nucleon-nucleon chiral potentials

M. Vorabbi, P. Finelli, C. Giusti, PRC 93 034619 (2017)

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**Purpose: study the domain of applicability of microscopic two-body chiral potentials to the construction of an OP**

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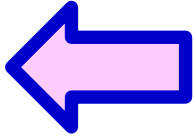
**Purpose: study the domain of applicability of microscopic two-body chiral potentials to the construction of an OP**

**Non relativistic optical potential**

**Comparison with elastic pA scattering data**

M. Vorabbi, P. Finelli, C. Giusti, PRC 93 034619 (2016)

Theoretical optical potential derived from nucleon-nucleon chiral potentials



# Theoretical framework for pA elastic scattering

We start from the full (A+1) body LS equation

$$T = T + VG_0(E)VT$$

Separation into two coupled integral equations

$$T = U + G_0(E)PT$$

$$U = V + VG_0(E)QU$$

T transition op. for  
elastic scattering,

U OP

Free propagator

$$G_0(E) = (E - H_0 + i\epsilon)^{-1}$$

Projection operators

$$P + Q = 1$$

Free Hamiltonian

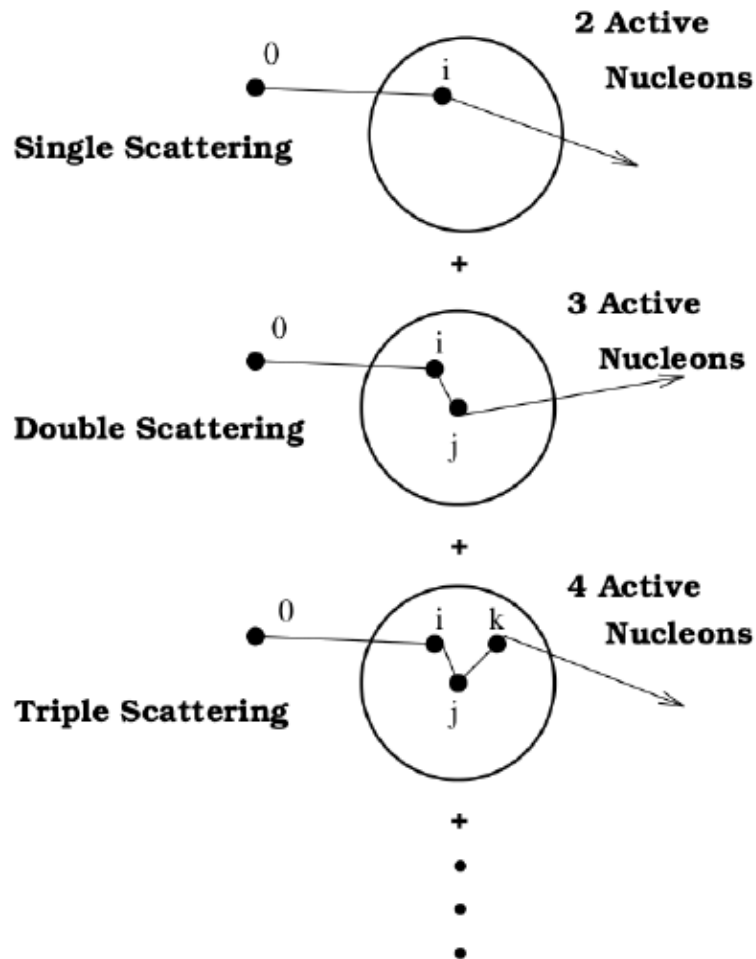
$$H_0 = h_0 + H_A$$

External interaction

$$V = \sum_{i=1}^A v_{0i}$$

# The spectator expansion

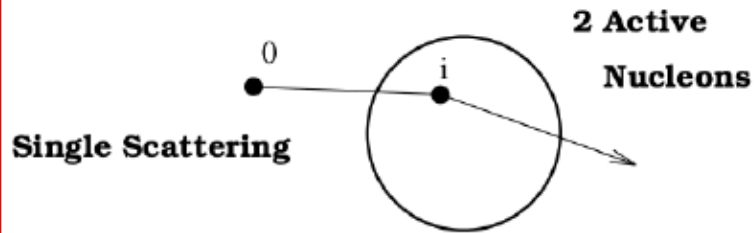
Consistent framework to calculate  $U$  and  $T$



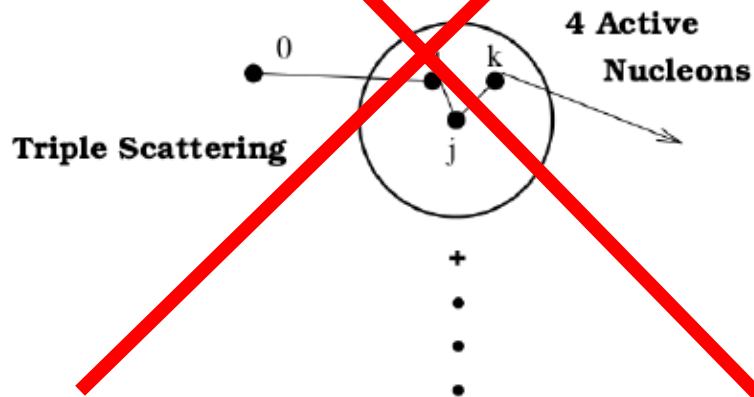
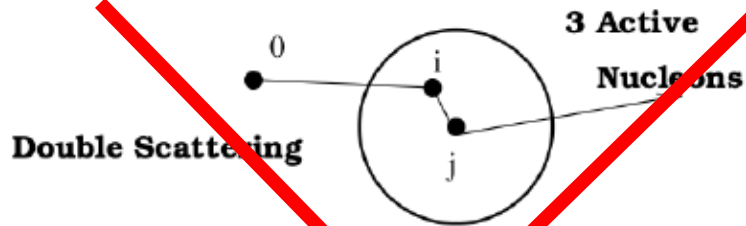
$$\begin{aligned}
 U &= \sum_{i=1}^A \tau_i \\
 &+ \sum_{i,j \neq i}^A \tau_{ij} \\
 &+ \sum_{i,j \neq i, k \neq i,j}^A \tau_{ijk} \\
 &+ \dots
 \end{aligned}$$

# The spectator expansion

Consistent framework to calculate U and T



$$U = \sum_{i=1}^A \tau_i$$



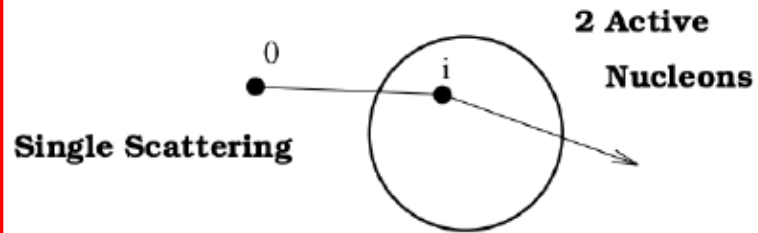
$$+ \sum_{i,j \neq i}^A \tau_{ij}$$

$$+ \sum_{i,j \neq i, k \neq i,j}^A \tau_{ijk}$$

$$+ \dots$$

# The spectator expansion

Consistent framework to calculate  $U$  and  $T$



$$U = \sum_{i=1}^A \tau_i$$

$$\tau_i = v_{0i} + v_{0i} G_0(E) Q \tau_i$$

# Impulse Approximation

$$\tau_i \approx t_{0i}$$

The free  $NN$   $t$  matrix

$$t_{0i} = v_{0i} + v_{0i}g_i t_{0i}$$

The free two-body propagator

$$g_i = \frac{1}{E - h_0 - h_i + i\epsilon}$$

$$U = \sum_{i=1}^A t_{0i}$$



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$$U = \sum_{i=1}^A t_{0i}$$

**We have to solve only 2-body equations**

# Optimum Factorization Approximation

$$U(\mathbf{q}, \mathbf{K}; \omega) = \frac{A-1}{A} \eta(\mathbf{q}, \mathbf{K}) \sum_{N=n,p} t_{pN} \left[ \mathbf{q}, \frac{A+1}{A} \mathbf{K}; \omega \right] \rho_N(\mathbf{q})$$


NN t-matrix  
NN interaction

n, p densities

$$\mathbf{q} = \mathbf{k}' - \mathbf{k}$$

$$\mathbf{K} = \frac{1}{2} (\mathbf{k}' + \mathbf{k})$$

# Optimum Factorization Approximation

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Moeller factor  
imposes the Lorentz invariance of  
the flux when passing from the  
NA to the NN frame in which the  
t matrices are evaluated

$$U(q, K; \omega) = U^c(q, K; \omega) + \frac{i}{2} \sigma \cdot q \times K U^{ls}(q, K; \omega)$$

**central**
**spin-orbit**

$$U^c(q, K; \omega) = \frac{A-1}{A} \eta(q, K) \sum_{N=n,p} t_{pN}^c \left[ q, \frac{A+1}{A} K; \omega \right] \rho_N(q)$$

$$U^{ls}(q, K; \omega) = \frac{A-1}{A} \eta(q, K) \frac{A+1}{2A} \sum_{N=n,p} t_{pN}^{ls} \left[ q, \frac{A+1}{A} K; \omega \right] \rho_N(q)$$

$$U(q, K; \omega) = \underbrace{U^c(q, K; \omega)}_{\text{central}} + \frac{i}{2} \sigma \cdot q \times K \underbrace{U^{ls}(q, K; \omega)}_{\text{spin-orbit}}$$


$$U^c(q, K; \omega) = \frac{A-1}{A} \eta(q, K) \sum_{N=n,p} t_{pN}^c \left[ q, \frac{A+1}{A} K; \omega \right] \rho_N(q)$$

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NN t-matrix  
NN interaction

n, p densities

# Optimum Factorization Approximation

$$U(\mathbf{q}, \mathbf{K}; \omega) = \frac{A-1}{A} \eta(\mathbf{q}, \mathbf{K}) \sum_{N=n,p} t_{pN} \left[ \mathbf{q}, \frac{A+1}{A} \mathbf{K}; \omega \right] \rho_N(\mathbf{q})$$


Moeller factor

NN t-matrix  
NN interaction

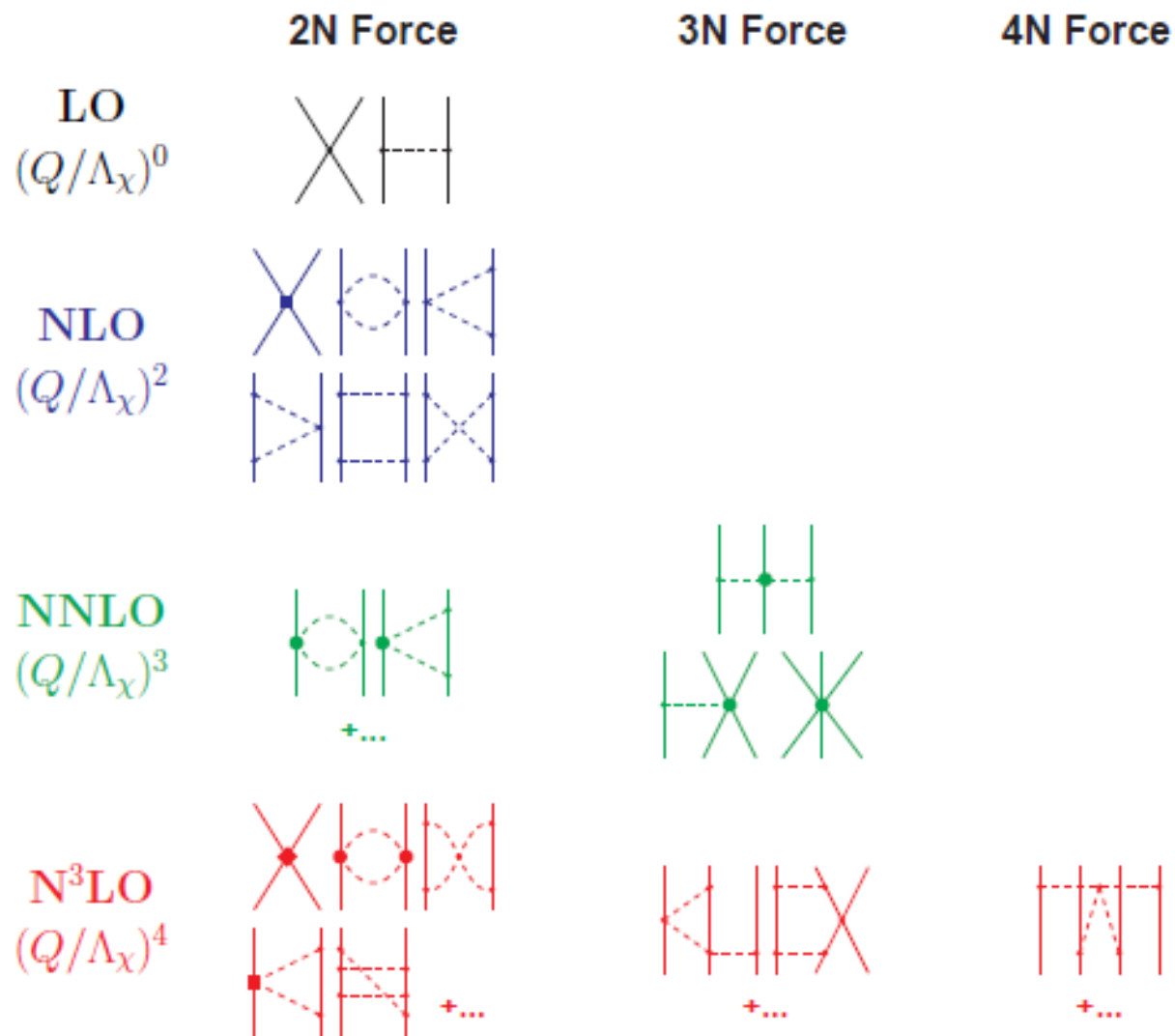
n, p densities

- **n, p densities** calculated within the RMF description of spherical nuclei using a DDME model
- **NN interaction** chiral potentials...

# CHIRAL POTENTIAL

- When the concept of EFT was applied to low-energy QCD, ChPT was developed
- Within ChPT it became possible to implement chiral symmetry consistently in a theory of pionic and nuclear interactions
- The theory is based on a perturbative expansion in powers of  $(Q/\Lambda_\chi)^n$  where  $Q$  is the magnitude of the three-momentum of the external particles or the pion mass and  $\Lambda_\chi$  is the chiral symmetry breaking scale of the chiral EFT
- From the perturbative expansion only a finite number of terms contribute at a given order

# CHIRAL POTENTIAL





# CHIRAL POTENTIAL

LO  
 $(Q/\Lambda_\chi)^0$



NLO  
 $(Q/\Lambda_\chi)^2$



NNLO  
 $(Q/\Lambda_\chi)^3$

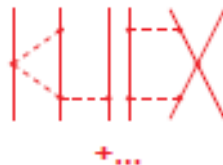
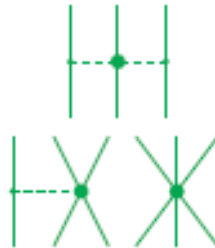


N<sup>3</sup>LO  
 $(Q/\Lambda_\chi)^4$

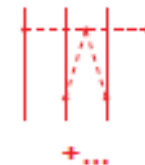


3N Force

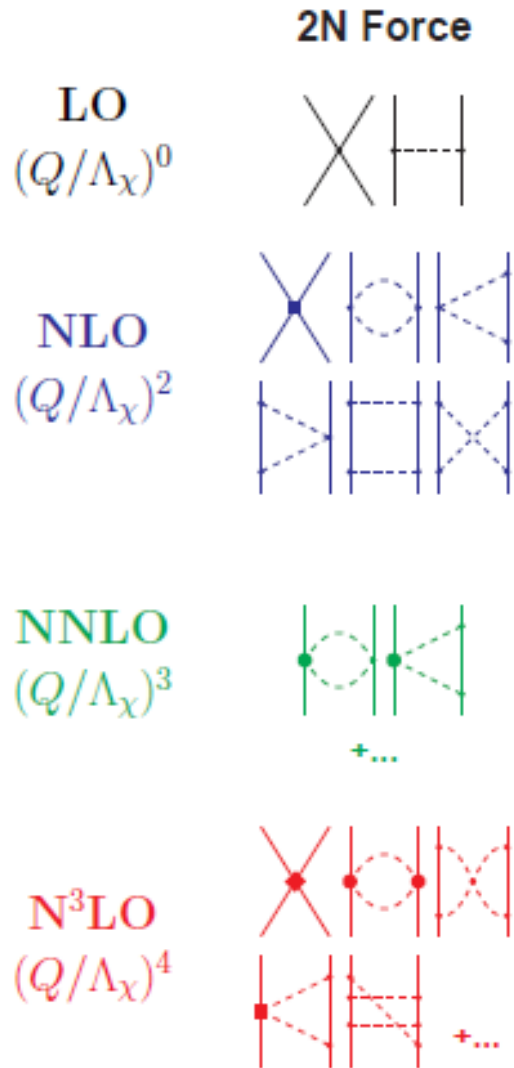
Graphs analyzed in terms of  $(Q/\Lambda_\chi)^n$   
 nuclear forces emerge as a hierarchy  
 controlled by the power n  
 Nuclear forces dominated by NN int.  
 many-body forces suppressed by  
 powers of the expansion parameters.



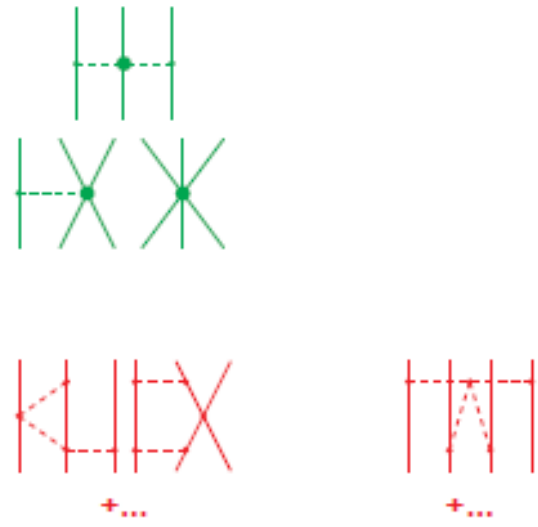
4N Force



# CHIRAL POTENTIAL



3N Force	4N Force
<p>3N forces start at 3<sup>rd</sup> order,            4N forces start at 4<sup>th</sup> order            2 and many-body forces are created on            an equal footing and emerge in            increasing order going to higher order</p>	



# CHIRAL POTENTIAL

	2N Force	3N Force	4N Force
LO $(Q/\Lambda_\chi)^0$			
NLO $(Q/\Lambda_\chi)^2$			
NNLO $(Q/\Lambda_\chi)^3$			
N <sup>3</sup> LO $(Q/\Lambda_\chi)^4$			

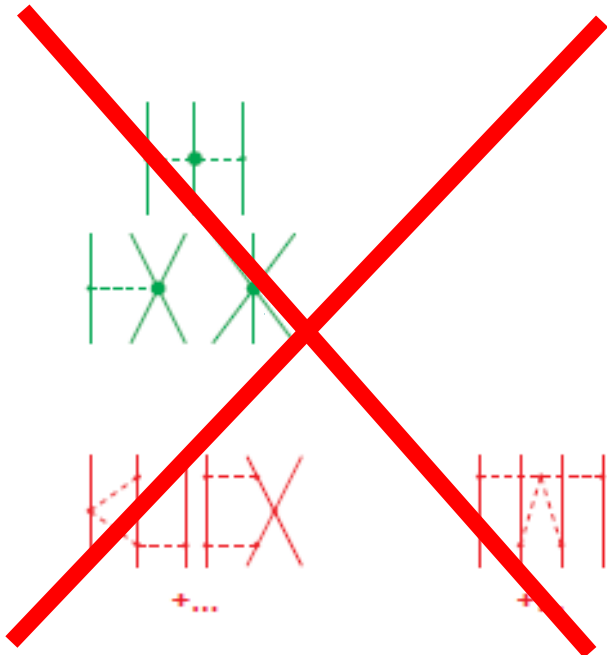
QCD symmetries are consistently respected order by order

Order by order uncertainties can be evaluated of the order  $(Q/\Lambda_\chi)^n$

# CHIRAL POTENTIAL

	2N Force	3N Force	4N Force
LO $(Q/\Lambda_\chi)^0$			
NLO $(Q/\Lambda_\chi)^2$			
NNLO $(Q/\Lambda_\chi)^3$			
N <sup>3</sup> LO $(Q/\Lambda_\chi)^4$			

CHIRAL POTENTIAL AT N<sup>3</sup>LO  
ONLY 2N



# CHIRAL POTENTIAL

Two different versions of chiral potentials at N<sup>3</sup>LO  
Entem and Machleidt (EM) , Epelbaum et al. (EGM)

In general the integral in the LS eq . is divergent and needs to be regularized

Usual procedure:  $V(k', k) \longmapsto V(k', k) e^{-(k'/\Lambda)^{2n}} e^{-(k/\Lambda)^{2n}}$

EM present results with  $\Lambda = 450, 500, 600$  MeV

EGM present results with  $\Lambda = 450, 550, 600$  MeV

and treat differently the short-range part of the 2PE contribution, that has an unphysically strong attraction.

EM dimensional regularization

EGM spectral function regularization introduces an additional cutoff  $\tilde{\Lambda}$  and give cut-off combinations:  $(\Lambda, \tilde{\Lambda}) = (450, 500), (450, 700), (550, 600), (600, 600), (600, 700)$

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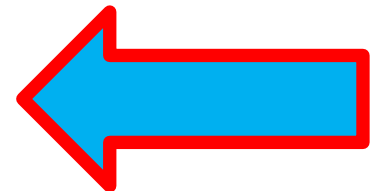
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**sensitivity to the cutoff parameters  
order by order convergence**



# NN transition matrix

NN elastic scatt. amplitude related to the antisymmetrized NN-t matrix elements

$$M(\boldsymbol{\kappa}', \boldsymbol{\kappa}, \omega) = \langle \boldsymbol{\kappa}' | M(\omega) | \boldsymbol{\kappa} \rangle = -4\pi^2 \mu \langle \boldsymbol{\kappa}' | t(\omega) | \boldsymbol{\kappa} \rangle$$

The most general form, consistent with invariance under rotation, time reversal, and parity

$$M = a + c(\boldsymbol{\sigma}_1 + \boldsymbol{\sigma}_2) \cdot \hat{\boldsymbol{n}} + m(\boldsymbol{\sigma}_1 \cdot \hat{\boldsymbol{n}})(\boldsymbol{\sigma}_2 \cdot \hat{\boldsymbol{n}}) \\ + (g + h)(\boldsymbol{\sigma}_1 \cdot \hat{\boldsymbol{l}})(\boldsymbol{\sigma}_2 \cdot \hat{\boldsymbol{l}}) + (g - h)(\boldsymbol{\sigma}_1 \cdot \hat{\boldsymbol{m}})(\boldsymbol{\sigma}_2 \cdot \hat{\boldsymbol{m}})$$

$$\hat{\boldsymbol{l}} = \frac{\boldsymbol{\kappa}' + \boldsymbol{\kappa}}{|\boldsymbol{\kappa}' + \boldsymbol{\kappa}|}, \quad \hat{\boldsymbol{m}} = \frac{\boldsymbol{\kappa}' - \boldsymbol{\kappa}}{|\boldsymbol{\kappa}' - \boldsymbol{\kappa}|}, \quad \hat{\boldsymbol{n}} = \frac{\boldsymbol{\kappa} \times \boldsymbol{\kappa}'}{|\boldsymbol{\kappa} \times \boldsymbol{\kappa}'|}$$

$a, c, m, g, h$  complex functions of  $\omega, \boldsymbol{\kappa}, \boldsymbol{\kappa}'$

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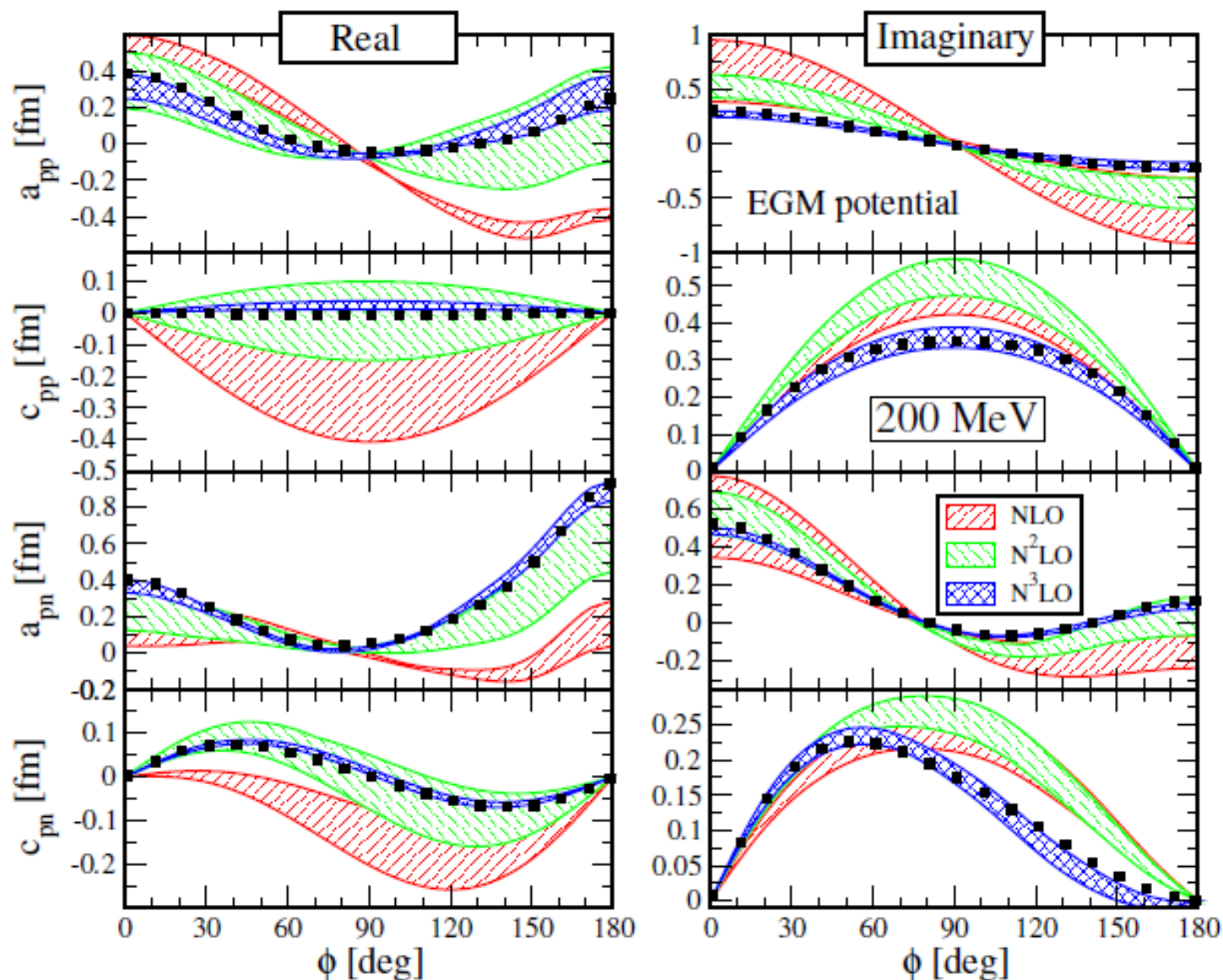
$$\hat{\boldsymbol{l}} = \frac{\boldsymbol{\kappa}' + \boldsymbol{\kappa}}{|\boldsymbol{\kappa}' + \boldsymbol{\kappa}|}, \quad \hat{\boldsymbol{m}} = \frac{\boldsymbol{\kappa}' - \boldsymbol{\kappa}}{|\boldsymbol{\kappa}' - \boldsymbol{\kappa}|}, \quad \hat{\boldsymbol{n}} = \frac{\boldsymbol{\kappa} \times \boldsymbol{\kappa}'}{|\boldsymbol{\kappa} \times \boldsymbol{\kappa}'|}$$

$a, c, m, g, h$  complex functions of  $\omega, \boldsymbol{\kappa}, \boldsymbol{\kappa}'$

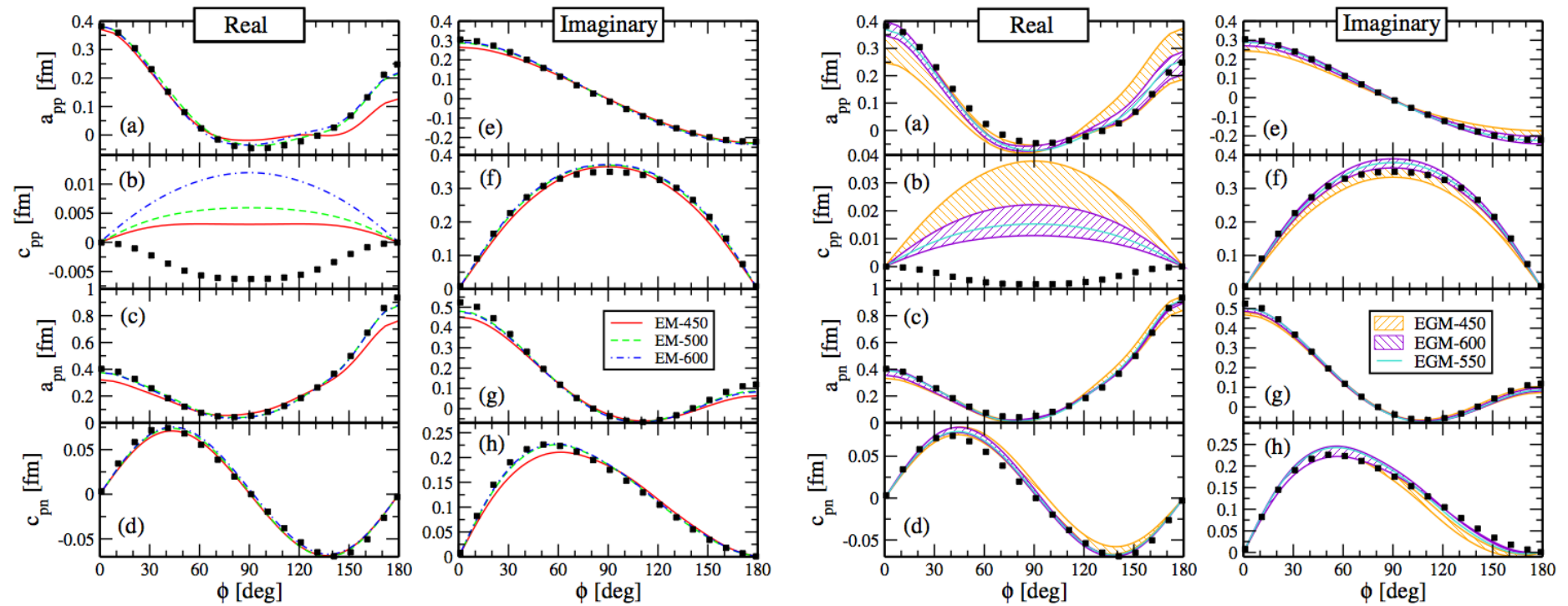
For even-even nuclei with  $J=0$  only  $a$  and  $c$  survive and they are connected to the central and spin-orbit part of the NN t-matrix



# THE NUCLEON-NUCLEON AMPLITUDES

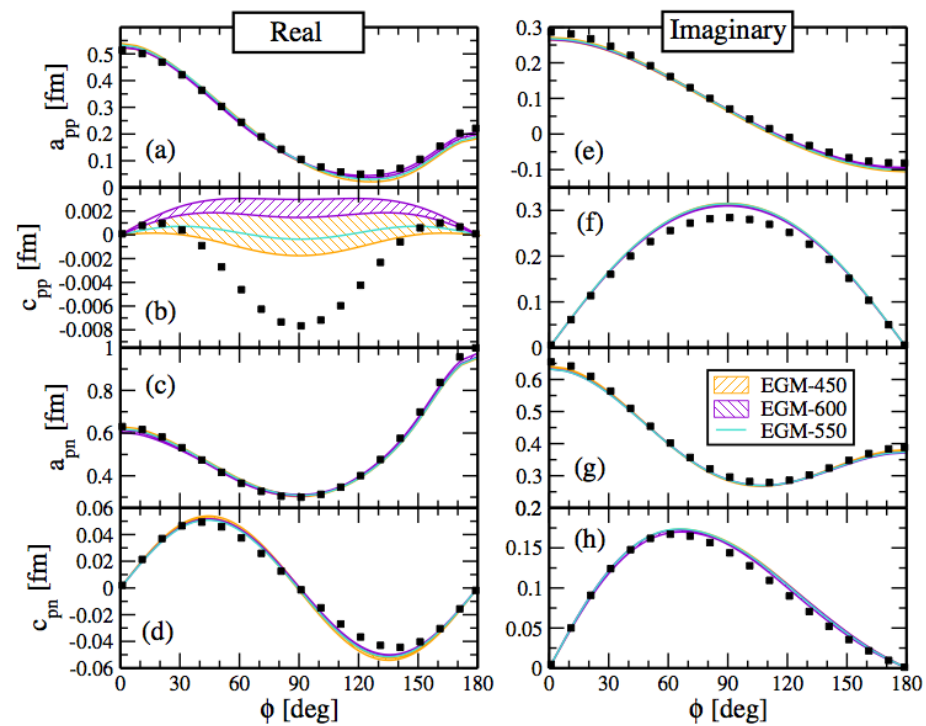
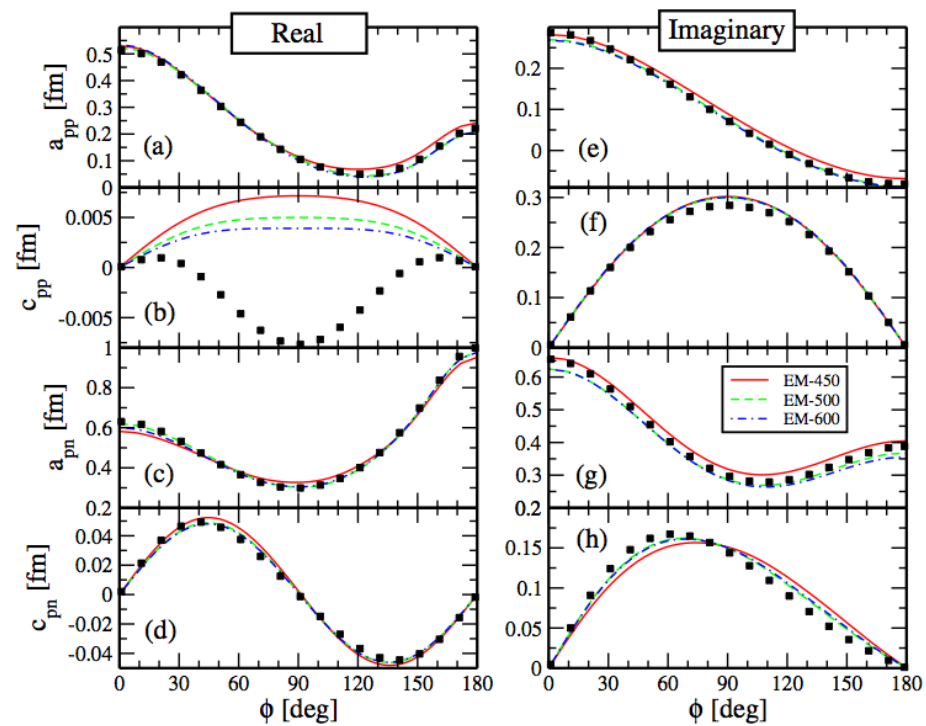


# NN AMPLITUDES 200 MeV



M. Vorabbi, P. Finelli, C. Giusti, PRC 93 034619 (2016)

# NN AMPLITUDES 100 MeV



## OP and scattering observables

The most general form of the amplitude for elastic p scattering from a spin 0 nucleus

$$M(k_0, \theta) = A(k_0, \theta) + \boldsymbol{\sigma} \cdot \hat{\mathbf{N}} C(k_0, \theta)$$

Scattering observables

$$\frac{d\sigma}{d\Omega}(\theta) = |A(\theta)|^2 + |C(\theta)|^2$$

unpolarized differential cross section

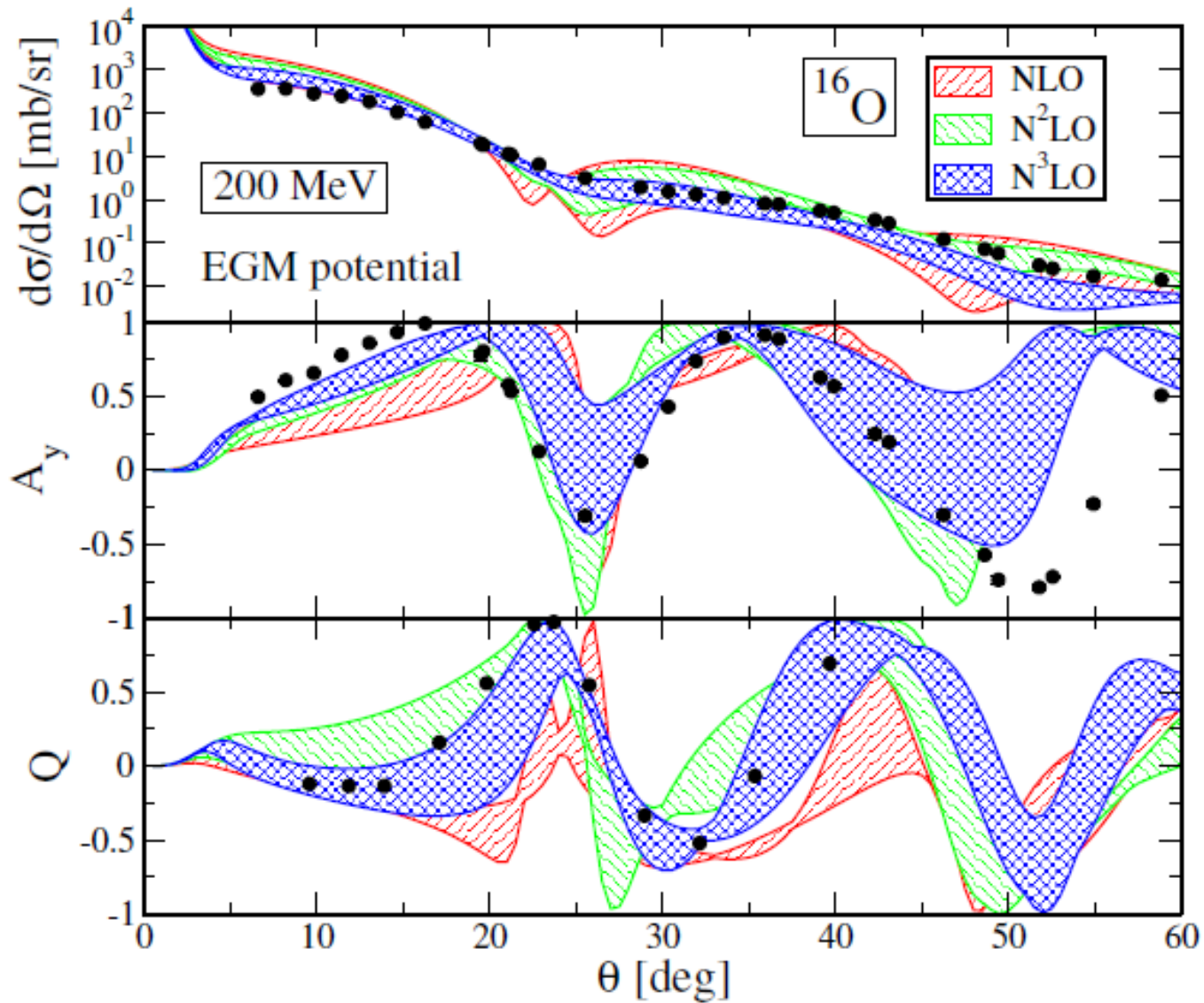
$$A_y(\theta) = \frac{2\text{Re}[A^*(\theta) C(\theta)]}{|A(\theta)|^2 + |C(\theta)|^2}$$

analyzing power

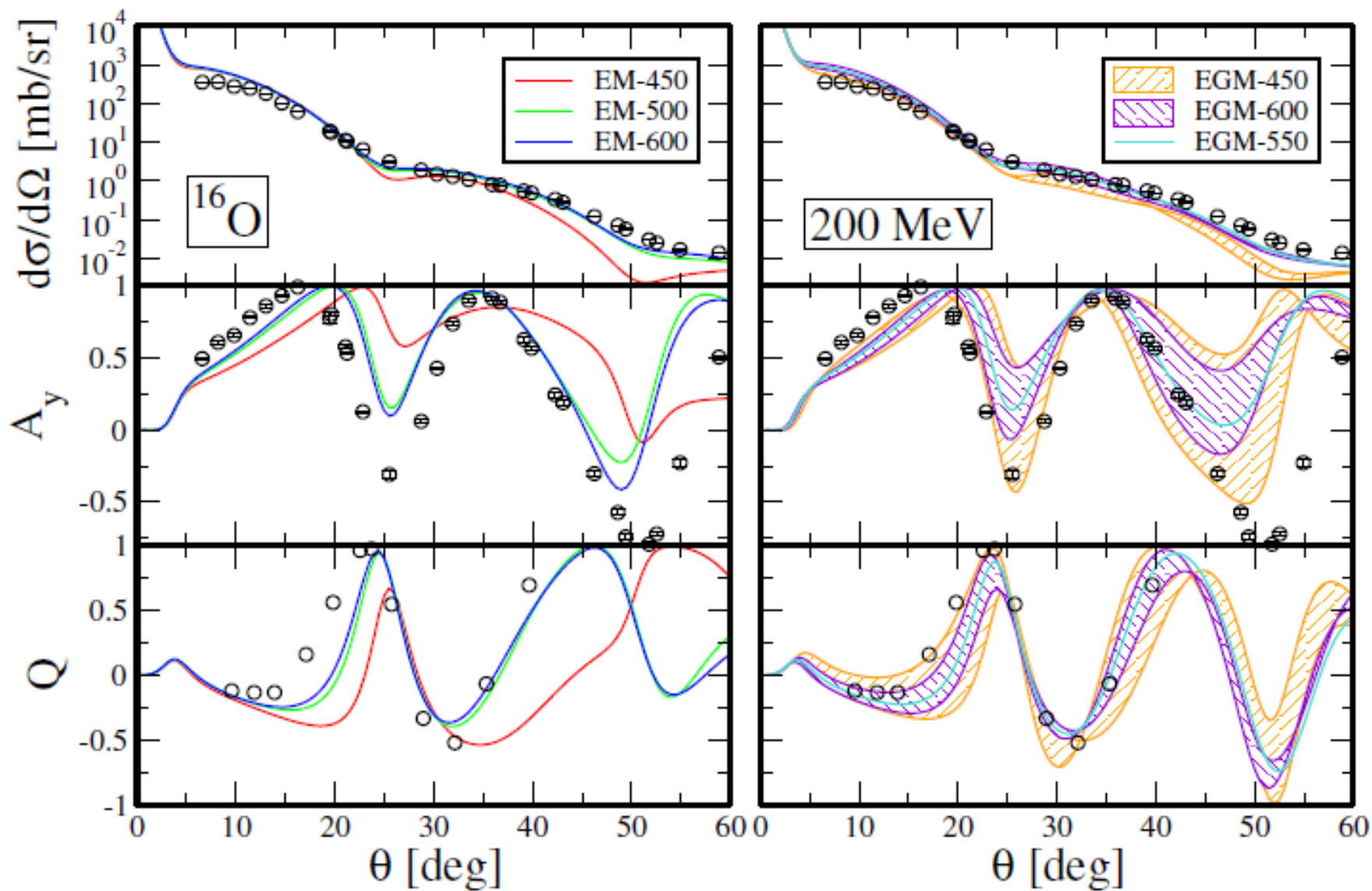
$$Q(\theta) = \frac{2\text{Im}[A(\theta) C^*(\theta)]}{|A(\theta)|^2 + |C(\theta)|^2}$$

spin rotation

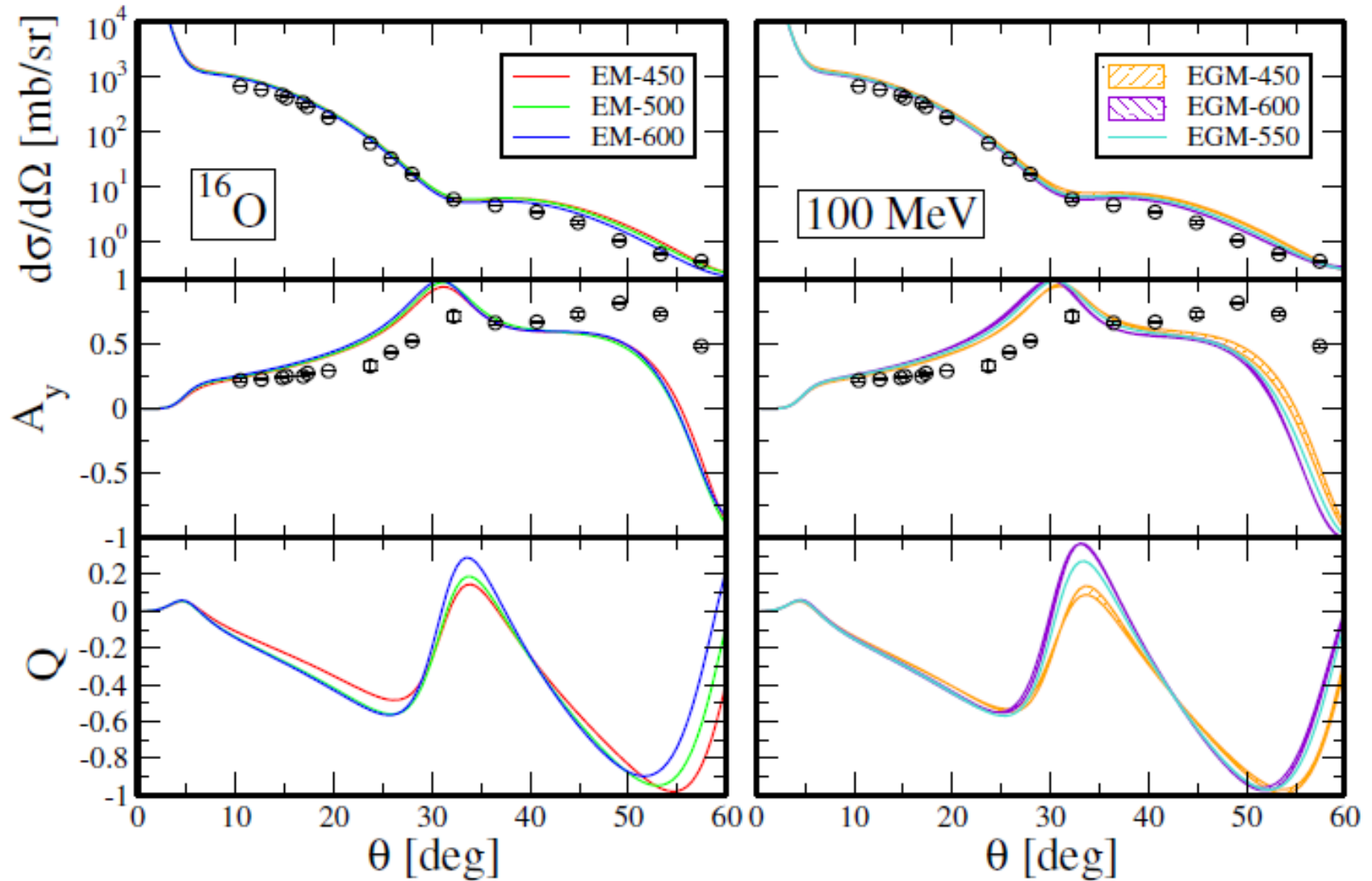
# ELASTIC PROTON SCATTERING



# ELASTIC P-A SCATTERING



# ELASTIC P-A SCATTERING

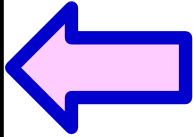


M. Vorabbi, P. Finelli, C. Giusti, PRC 93 034619 (2016)

Theoretical optical potential derived from nucleon-nucleon chiral potentials

M. Vorabbi, P. Finelli, C. Giusti, PRC 93 034619 (2017)

Optical potential derived from nucleon-nucleon chiral potentials at N<sup>4</sup>LO





# CHIRAL POTENTIAL AT N<sup>4</sup>LO

	Two-nucleon force	Three-nucleon force	Four-nucleon force
LO (Q <sup>0</sup> )		—	—
NLO (Q <sup>2</sup> )		—	—
N <sup>2</sup> LO (Q <sup>3</sup> )			—
N <sup>3</sup> LO (Q <sup>4</sup> )			
N <sup>4</sup> LO (Q <sup>5</sup> )			

E. Epelbaum et al. . PRL 115 122391 (2015), EPJA 51 53 (2015) **EKM**

D.R. Entem et al. PRC 91 014002 (2015), PRC 96 024004 (2017) **EMN**

# CHIRAL POTENTIAL AT N<sup>4</sup>LO

NN

	Two-nucleon force	Three-nucleon force	Four-nucleon force
LO ( $Q^0$ )		—	—
NLO ( $Q^2$ )		—	—
N <sup>2</sup> LO ( $Q^3$ )			—
N <sup>3</sup> LO ( $Q^4$ )			
N <sup>4</sup> LO ( $Q^5$ )			

E. Epelbaum et al. . PRL 115 122391 (2015), EPJA 51 53 (2015) **EKM**

D.R. Entem et al. PRC 91 014002 (2015), PRC 96 024004 (2017) **EMN**

M. Vorabbi, P. Finelli, C. Giusti, PRC 93 034619 (2017)

Optical potential derived from nucleon-nucleon chiral potentials at N<sup>4</sup>LO

**Purpose: check the convergence and assess the theoretical errors associated with the truncation of the chiral expansion in the construction of an OP**

# Regularization for EKM and EMN at N<sup>4</sup>LO

## EKM

Long-range part of the potential  
n=6 R=0.8, 0.9, 1., 1.1, 1.2 fm

$$f\left(\frac{r}{R}\right) = \left(1 - \exp\left(-\frac{r^2}{R^2}\right)\right)^n$$

Short-range part  
conventional mom. space

$$f_{\Lambda}(k', k) = \exp\left(-\left(\frac{k'}{\Lambda}\right)^{2m} - \left(\frac{k}{\Lambda}\right)^{2m}\right)$$

$\Lambda = 2R^{-1}$  and  $m=2$

## EMN

SFR with  $\tilde{\Lambda} \sim 700$  MeV to regularize the loop contribution and a conventional regulator function with  $\Lambda = 450, 500, 550$  MeV and  $m = 2, 4$  for multi-pion and single-pion exchange contribution

# Regularization for EKM and EMN at N<sup>4</sup>LO

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n=6 R=0.8, 0.9, 1., 1.1, 1.2 fm

$$f\left(\frac{r}{R}\right) = \left(1 - \exp\left(-\frac{r^2}{R^2}\right)\right)^n$$

Short-range part  
conventional mom. space

$$f_{\Lambda}(k', k) = \exp\left(-\left(\frac{k'}{\Lambda}\right)^{2m} - \left(\frac{k}{\Lambda}\right)^{2m}\right)$$

$$\Lambda = 2R^{-1} \text{ and } m=2$$

**all calculations performed  
with R=0.9 fm for EKM  
and  $\Lambda = 500$  MeV for EMN**

## EMN

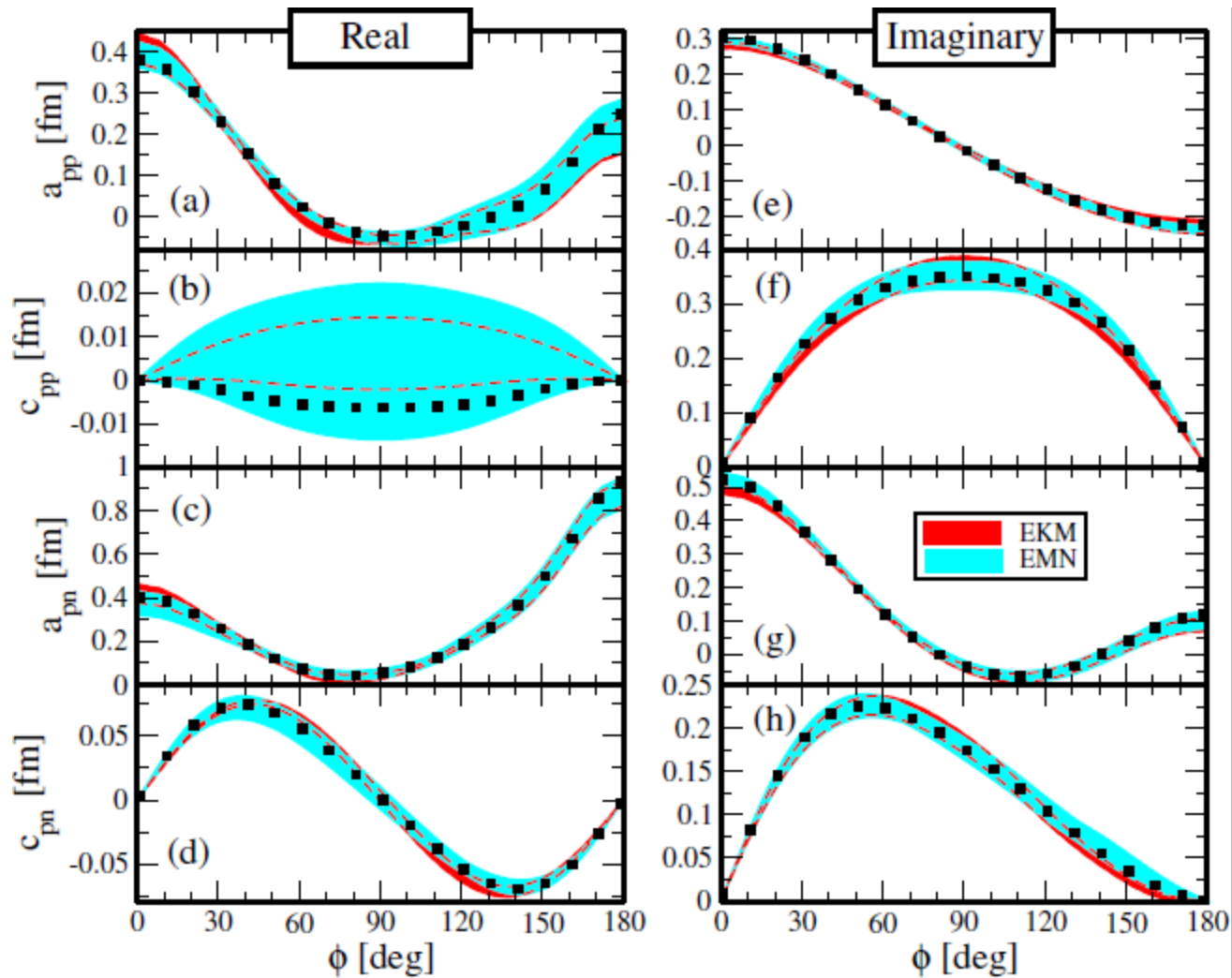
SFR with  $\tilde{\Lambda} \sim 700$  MeV to regularize the loop contribution  
and a conventional regulator function with  $\Lambda = 450, 500, 550$  MeV and  $m = 2, 4$  for multi-pion and single-pion exchange contribution

Assess theoretical errors associated to the truncation of the chiral expansion: given an observable  $\mathcal{O}(p)$  the uncertainty at order  $n$  is given by the size of neglected high-order terms. At N<sup>4</sup>LO:

$$\begin{aligned} \Delta \mathcal{O}^{\text{N}^4\text{LO}}(p) = & \max(Q^6 \times |\mathcal{O}^{\text{LO}}(p)|, \\ & \times Q^4 \times |\mathcal{O}^{\text{LO}}(p) - \mathcal{O}^{\text{NLO}}(p)|, \\ & \times Q^3 |\mathcal{O}^{\text{NLO}}(p) - \mathcal{O}^{\text{N}^2\text{LO}}(p)|, \\ & \times Q^2 \times |\mathcal{O}^{\text{N}^2\text{LO}}(p) - \mathcal{O}^{\text{N}^3\text{LO}}(p)|, \\ & \times Q |\mathcal{O}^{\text{N}^3\text{LO}}(p) - \mathcal{O}^{\text{N}^4\text{LO}}(p)|), \end{aligned}$$

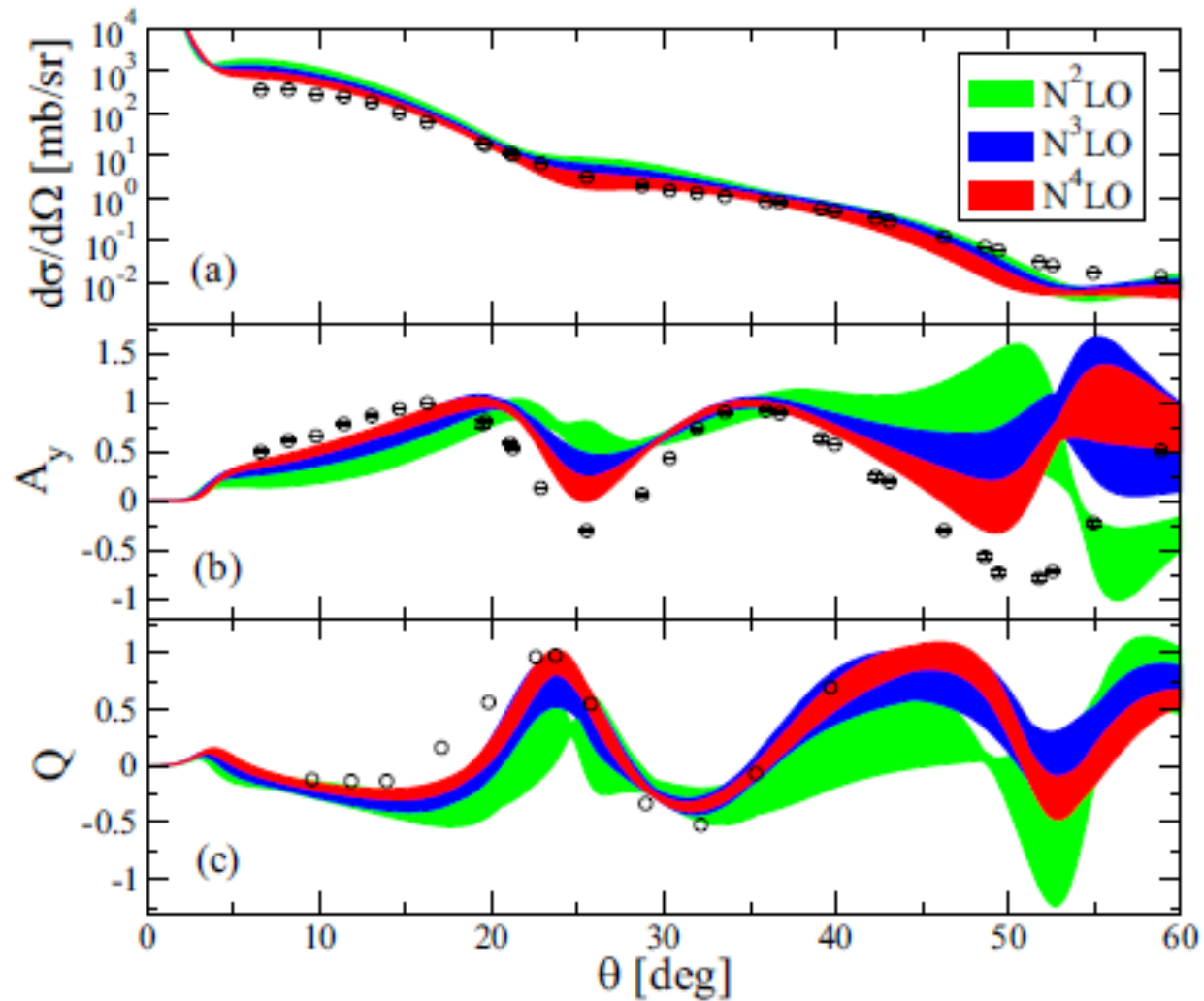
$$Q = \max\left(\frac{p}{\Lambda_b}, \frac{M_\pi}{\Lambda_b}\right) \quad \Lambda_b = 600 \text{ MeV}$$

# NN AMPLITUDES 200 MeV





$^{16}\text{O}$

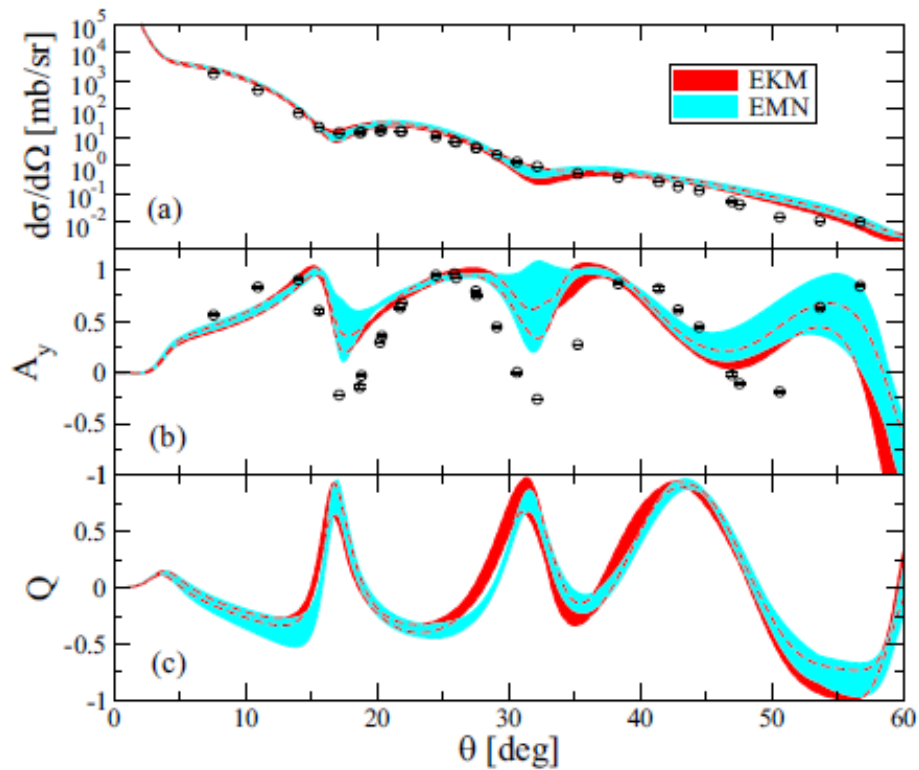
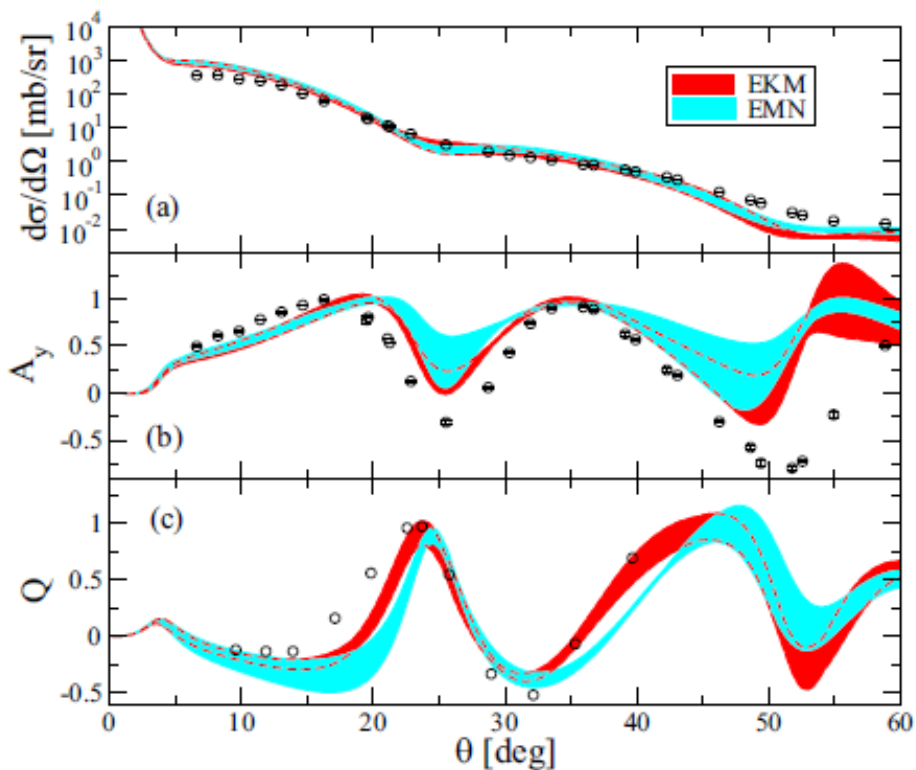


200 MeV

EKM

$^{16}\text{O}$ 

200 MeV

 $^{40}\text{Ca}$ 

# Comparison with phenomenological OP

- investigate and compare predictive power of our microscopic OP and of phenomenological OP in comparison with exp. data in a wider range of nuclei, including isotopic chains

## **PHENOMENOLOGICAL OP**

parameters fitted to data,  
data very well described in  
particular situations.

Investigate capability to  
describe data in different  
situations

## **MICROSCOPIC OP**

obtained from a model and  
approximations  
may be less able to describe  
specific data  
should have a greater  
predictive power for  
situations for which data not  
yet available

# Comparison phenomenological and microscopic NROP

## PHENOMENOLOGICAL OP

**GLOBAL** given in a wide range of nuclei and energies

**NROP** up to  $\sim 200$  MeV, for higher energies it is generally believed that the Schroedinger picture should be taken over by a Dirac approach. Global ROP available up to  $\sim 1$  GeV

**NROP Koning et al. NPA 713 231 (2003) (KON)** for nuclei  $24 \leq A \leq 209$  and energies from 1 keV to 200 MeV, recently extended to 1 GeV, to test at which energy the predictions of a phen. NROP fail

Calculations with TALYS (ECIS-06)

## MICROSCOPIC OP

chiral potentials at  $N^4$ LO describe NN scattering data up to 300 MeV and our OP can be used up to  $\sim 300$  MeV

# Comparison phenomenological and microscopic NROP

## PHENOMENOLOGICAL OP

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**NROP** Koning et al. NPA 713 231 (2003) (KON) for  $10 < A < 200$  and energies from 0 to 200 MeV recently extended to 300 MeV at which energy the phen. NROP fail

Calculations with TALYS (ECIS-06)

## MICROSCOPIC OP

chiral potentials at  $N^4$ LO describe NN scattering data up to 300 MeV and our OP can be used up to  $\sim 300$  MeV

Results of the comparison in the energy range 150-330 MeV

# Comparison phenomenological and microscopic NROP

## PHENOMENOLOGICAL OP

**GLOBAL** given in a wide range of nuclei and energies

**NROP** up to  $\sim 200$  MeV, for higher energies it is generally believed that the Schroedinger picture should be taken over by a Dirac approach. Global ROP available up to  $\sim 1$  GeV

**NROP Koning et al (2003) (KON)** and energies f recently exten at which energy the predictions of a phen. NROP fail

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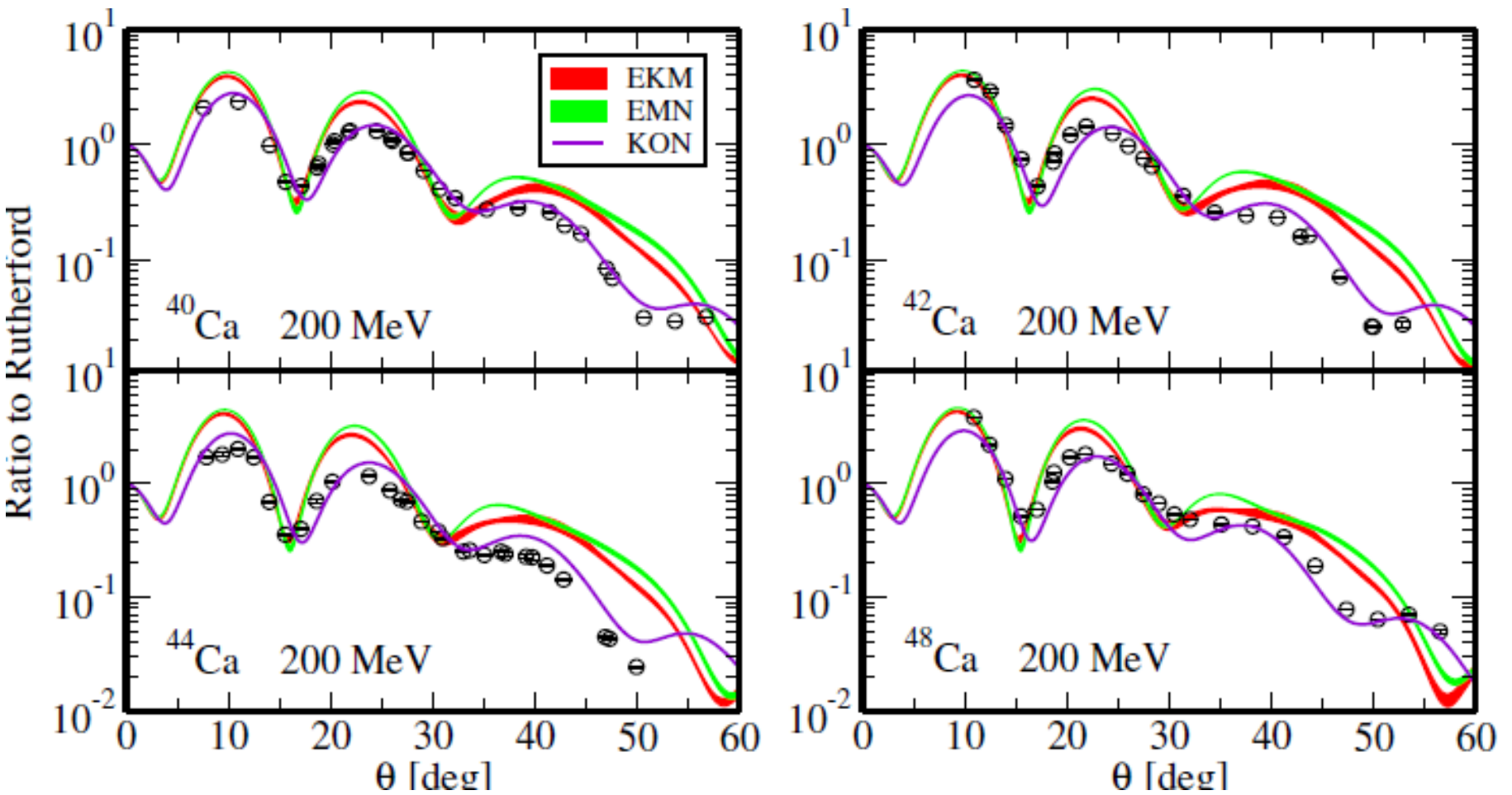
## MICROSCOPIC OP

chiral potentials at  $N^4$ LO describe NN scattering data up to 300 MeV and our OP can be used up to  $\sim 300$  MeV

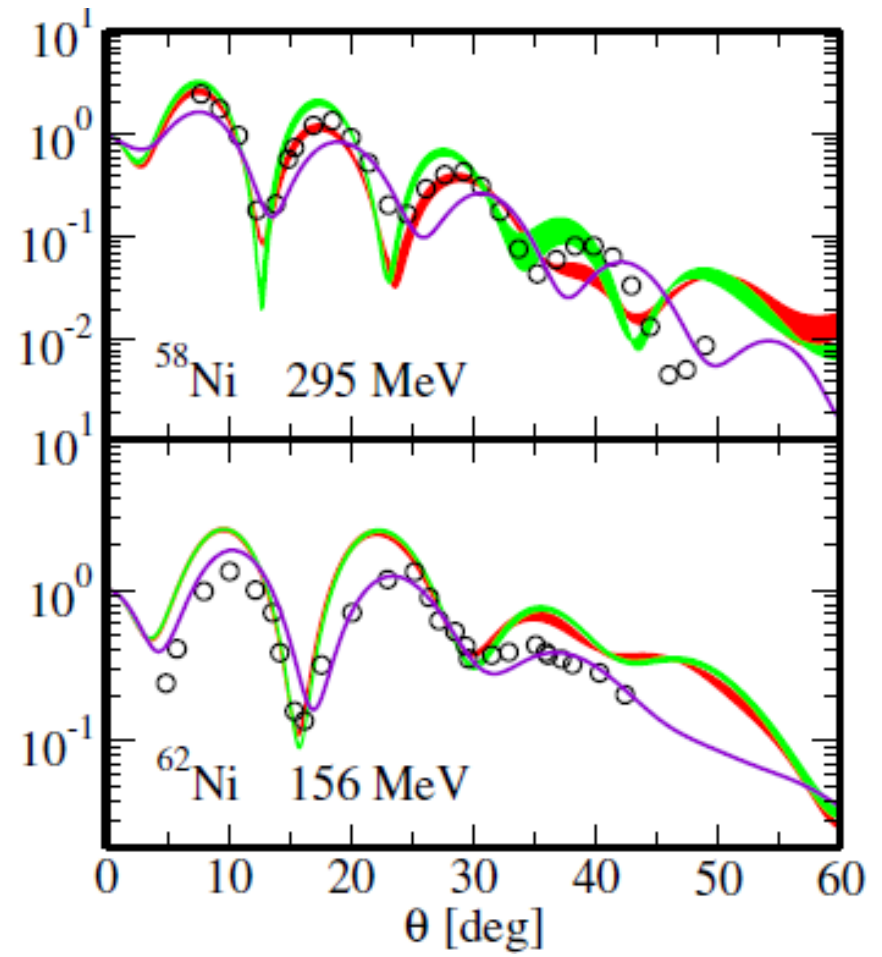
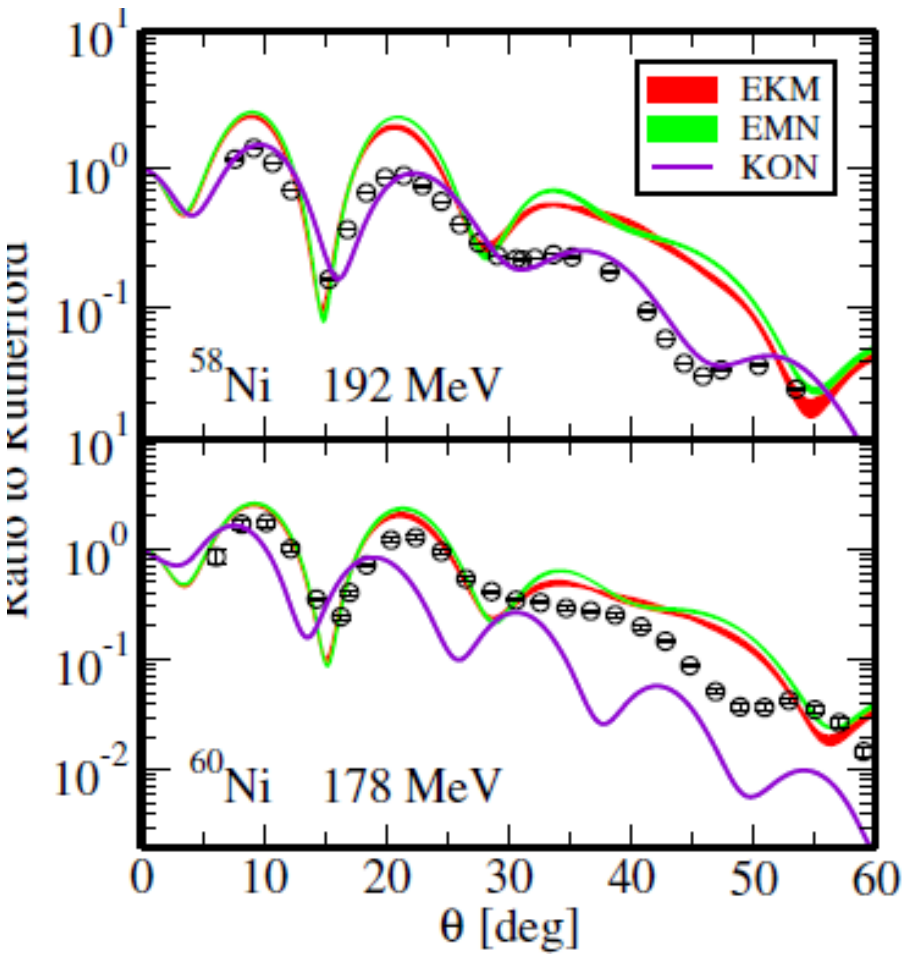
calculations with  $R=0,8,0.9,1.$  fm (EKM)  
 $\Lambda=500,550$  MeV (EMN )

The bands give the differences

# Comparison with phenomenological OP

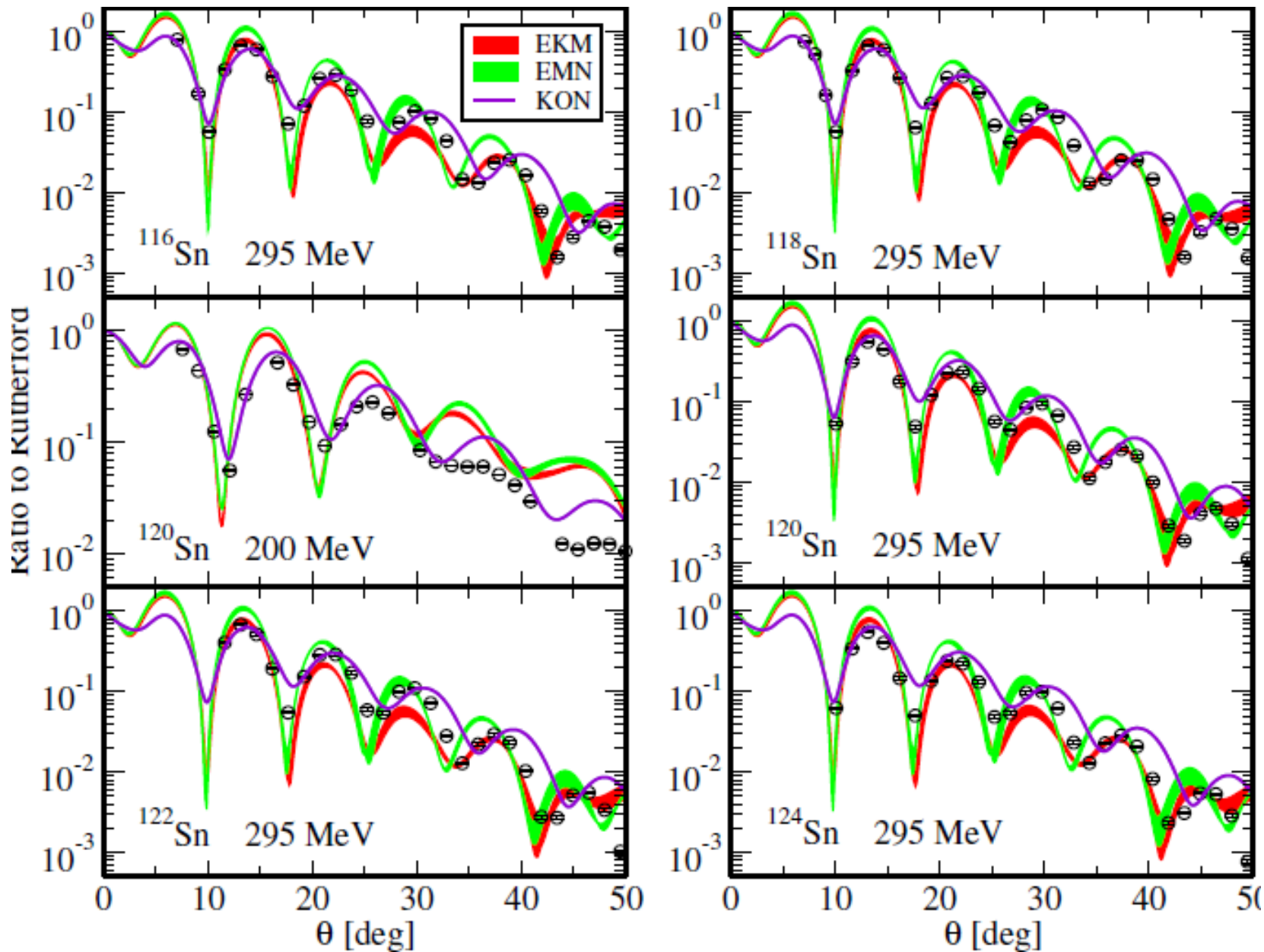


# Comparison with phenomenological OP

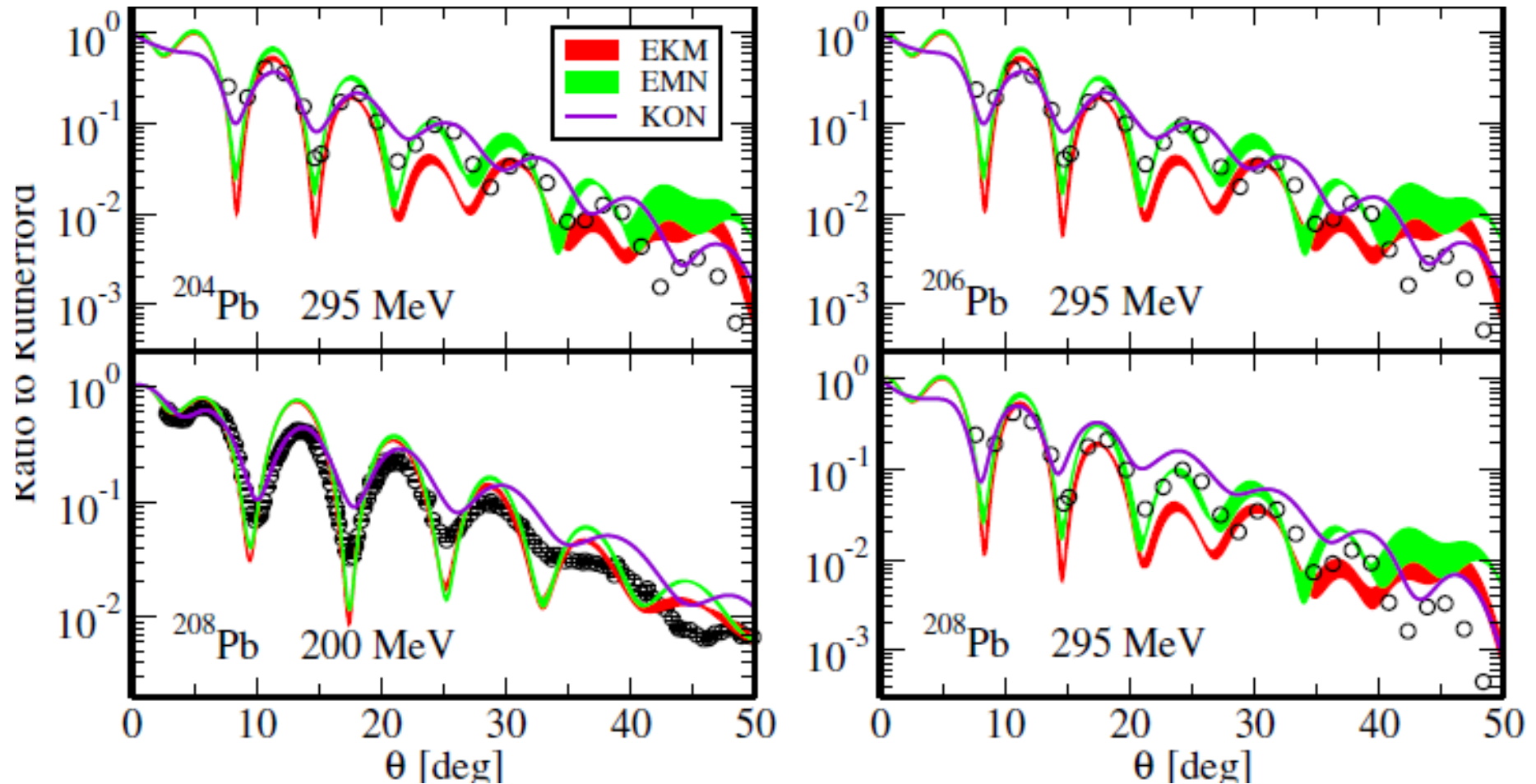




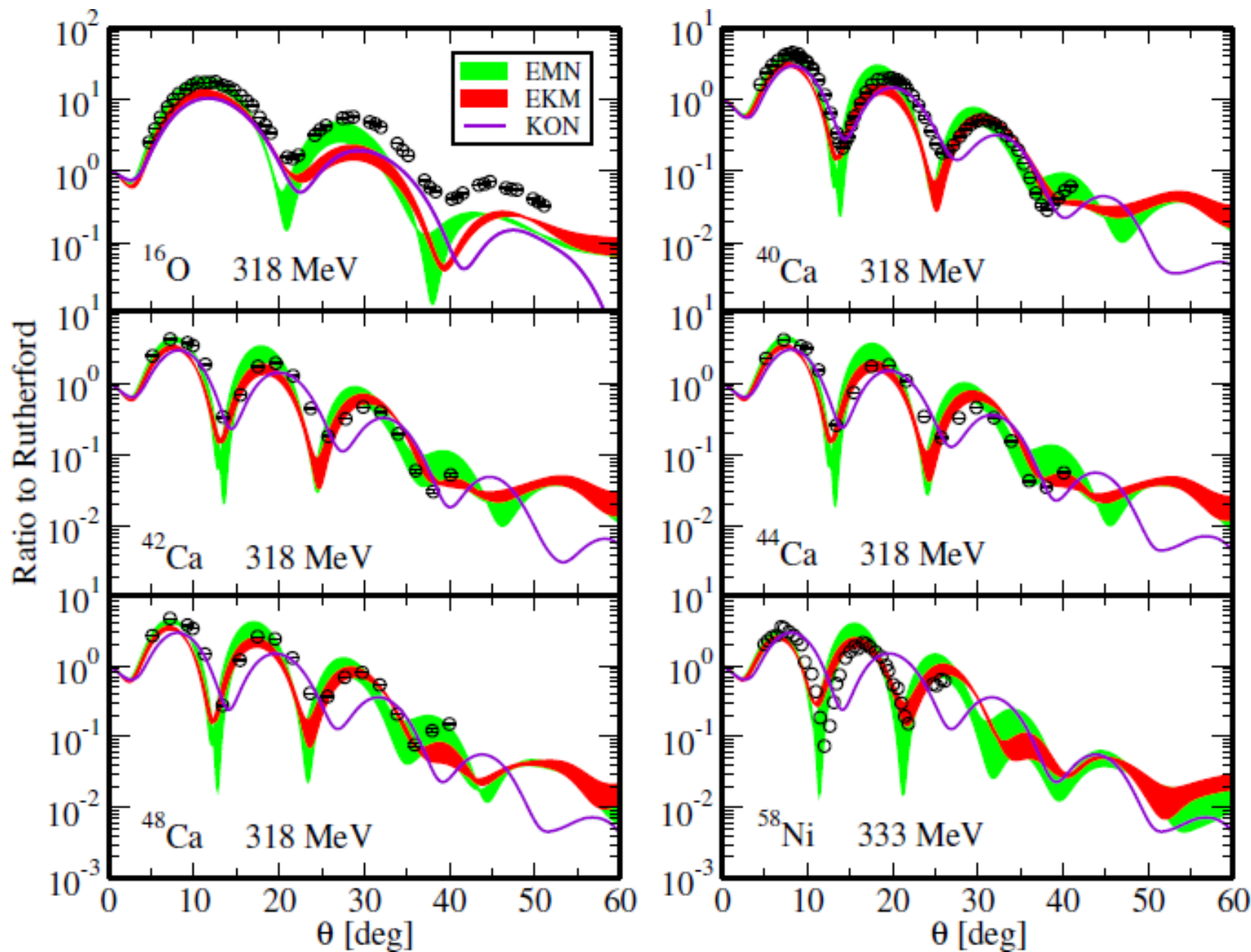
# Comparison with phenomenological OP



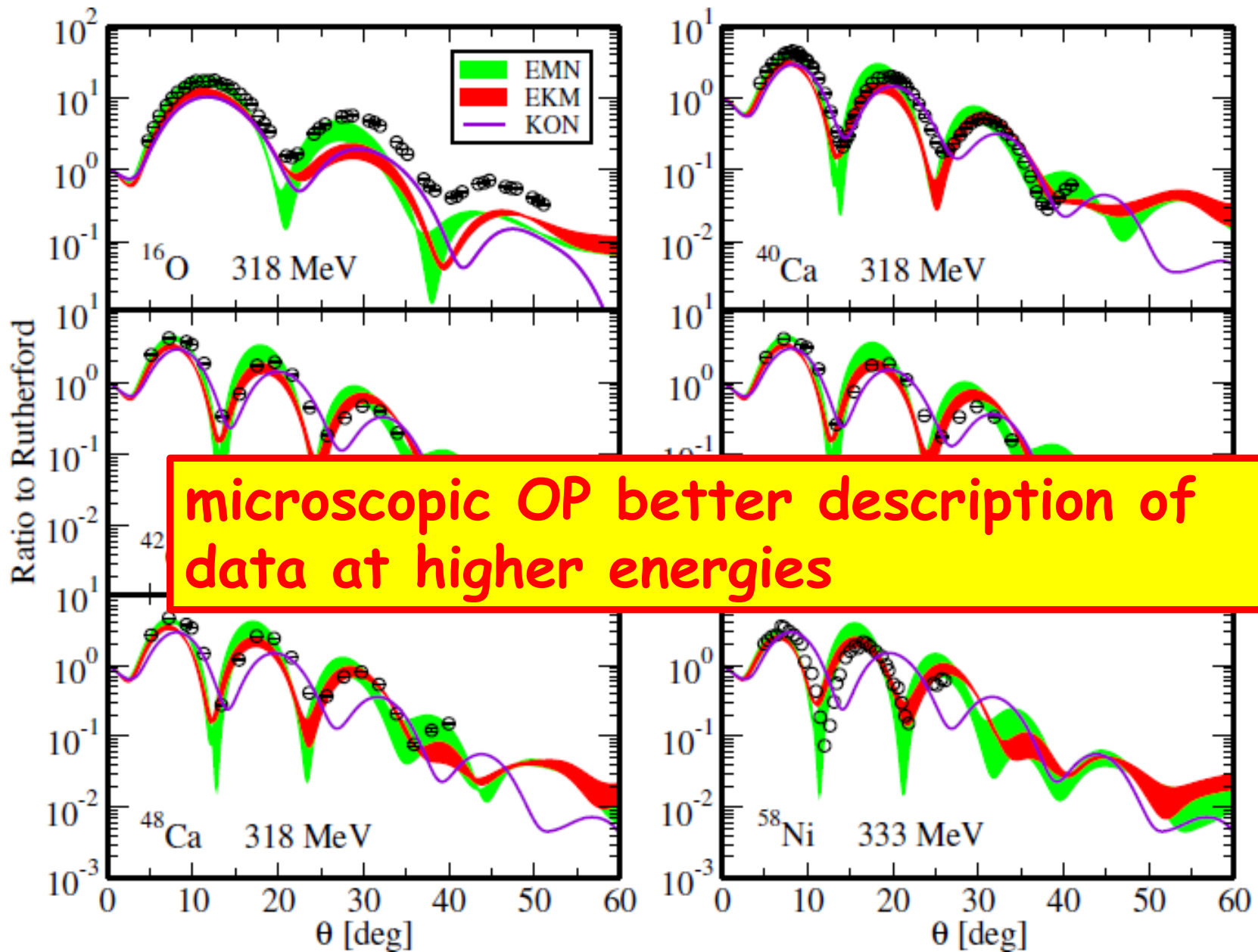
# Comparison with phenomenological OP



# Comparison with phenomenological OP



# Comparison with phenomenological OP



# PROSPECTS...

- model can be improved

# Microscopic optical potentials derived from *ab initio* translationally invariant nonlocal one-body densities

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(Dated: December 11, 2017)

**Background:** The nuclear optical potential is a successful tool for the study of nucleon-nucleus elastic scattering and its use has been further extended to inelastic scattering and other nuclear reactions. The nuclear density of the target nucleus is a fundamental ingredient in the construction of the optical potential and thus plays an important role in the description of the scattering process.

**Purpose:** In this work we derive a microscopic optical potential for intermediate energies using *ab initio* translationally invariant nonlocal one-body nuclear densities computed within the no-core shell model (NCSM) approach utilizing two- and three-nucleon chiral interactions as the only input.

**Methods:** The optical potential is derived at first-order within the spectator expansion of the non-relativistic multiple scattering theory by adopting the impulse approximation. Nonlocal nuclear densities are derived from the NCSM one-body densities calculated in the second quantization. The translational invariance is generated by exactly removing the spurious center-of-mass (COM) component from the NCSM eigenstates.

**Results:** The ground state local and nonlocal densities of  ${}^4,6,8\text{He}$ ,  ${}^{12}\text{C}$ , and  ${}^{16}\text{O}$  are calculated and applied to optical potential construction. The differential cross sections and the analyzing powers for the elastic proton scattering off of these nuclei are then calculated for different values of the incident proton energy. The impact of nonlocality and the COM removal is discussed.

**Conclusions:** The use of nonlocal densities has a substantial impact on the differential cross sections and improves agreement with experiment in comparison to results generated with the local densities especially for light nuclei. For the halo nuclei  ${}^6\text{He}$  and  ${}^8\text{He}$ , the results for the differential cross section are in a reasonable agreement with the data although a more sophisticated model for the optical potential is required to properly describe the analyzing powers.

PACS numbers: 24.10.-i; 24.10.Ht; 24.70.+s; 25.40.Cm; 21.60.De; 27.10.+h; 27.20.+n

M. Gennari, M. Vorabbi, A. Calci, P. Navratil, arXiv:  
1712.02879 (2017)

# PROSPECTS...

- the model can be improved
- folding integral
- 3N forces, medium effects
- application to nuclear reactions.... ? (e,e'p)