

Sea Quark Flavor Asymmetries from Chiral Symmetry Breaking

Peter Schweitzer

University of Connecticut

Overview:

- QCD and dynamical chiral symmetry breaking
- practical tool: chiral quark soliton model
- examples: $M_N(m_\pi)$, GPDs, q PDFs
- sea quark flavor asymmetries
- what gives rise to them?
- conclusions

motivation

- **perturbative QCD** powerful tool!
establish factorization, provide definitions of non-perturbative objects
tells us how a non-perturbative object looks at $Q > \mu_0$ if it is known at μ_0

but how does a non-perturbative object look like at initial scale?
how to compute it? Beyond pQCD.

- **non-perturbative methods** needed

lattice QCD: great!

gives us the correct answer (42!)
but we do not know why (that's what QCD says)

models:

give an approximate result (41 ...) but we know exactly why we got it (because we did $\int_1^{10} dy \frac{N_c(N_c+2)}{N_c+1+y} - 1 = 41$)
can be **insightful** (if model well-motivated,
and if it provides predictions we can test)

global symmetries of QCD

- $\mathcal{L}_{\text{QCD}} = \mathcal{L}_{\text{QCD}}(\bar{\psi}_q, \psi_q, A_\mu)$

with $m_q \ll M_{\text{hadronic}}$ for $q = u, d, s$ $M_{\text{hadronic}} \sim \mathcal{O}(M_\rho, M_N) \sim (0.77\text{--}0.94) \text{ GeV} \sim 1 \text{ GeV}$

- chirality $\psi_{q,L} = \frac{1}{2}(1 - \gamma_5)\psi_q$ and $\psi_{q,R} = \frac{1}{2}(1 + \gamma_5)\psi_q$

vector symmetry $V = L + R$, axial symmetry $V = L - R$

global symmetry $U(3)_L \otimes U(3)_R = \underbrace{U(1)_V}_{\text{baryon number}} \otimes \underbrace{U(1)_A}_{\text{axial anomaly}} \otimes \underbrace{SU(3)_V}_{SU(n_f)} \otimes \underbrace{SU(3)_A}_{\text{spontaneous breaking}}$

$$J^\pi = \frac{1}{2}^+ p, n$$

$$J^\pi = 1^+ \rho^+, \rho^0, \rho^-$$

$$J^\pi = \frac{3}{2}^+ \Delta^{++}, \Delta^+, \Delta^0, \Delta^-$$

SU(3) octets and decuplets
small $m_q \neq 0 \rightarrow$ mass splittings



**symmetry is realized
in hadron spectrum**

$$J^\pi = \frac{1}{2}^+ N(940) \text{ vs}$$

$$J^\pi = \frac{1}{2}^- N(1535) \text{ so}$$

nucleon's chiral partner much heavier



**symmetry not realized
spontaneously broken**

spontaneous chiral symmetry breaking

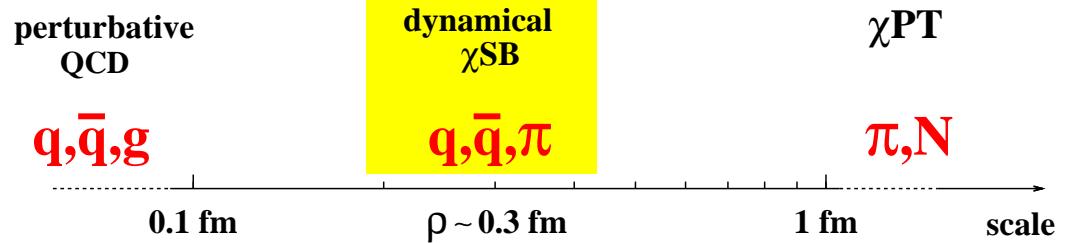
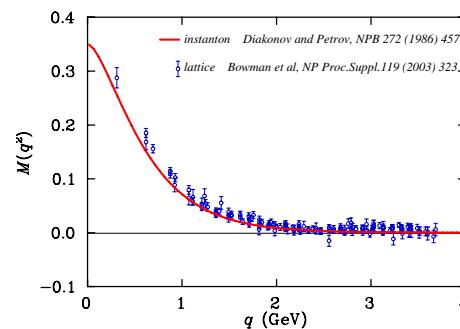
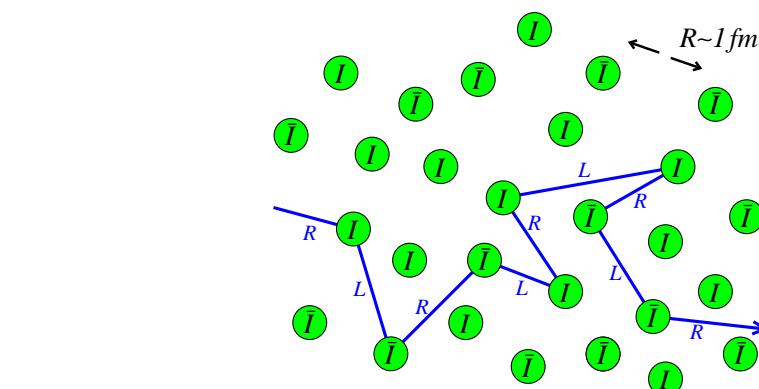
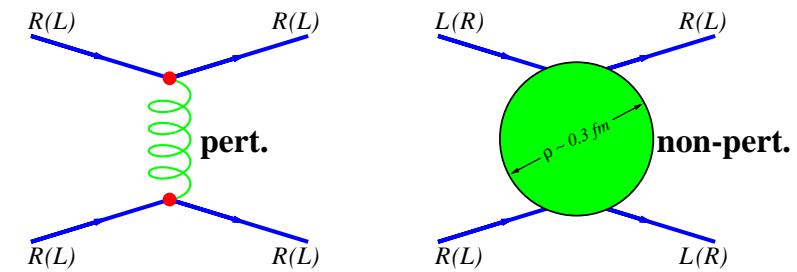
- $N_f^2 - 1$ Goldstone bosons
 π, K, η with $m_h \ll 1 \text{ GeV}$
- implemented in $\mathcal{L}_{\chi PT}$ with degrees of freedom N, Δ, π, \dots
powerful effective field theory
- **key feature of strong interaction**
fundamental for light hadron spectrum
crucial for structure of nucleon ∈ light hadron spectrum
- how to apply to parton structure of nucleon?
- **dynamical microscopic theory** needed which:
 - has partonic and Goldstone boson degrees of freedom
 - provides insights in non-perturbative regime(!)
 - is well-motivated, founded on QCD
 - consistent, effective, reliable
 - solvable*

* more easily than lattice QCD, otherwise just do lattice QCD

dynamical chiral symmetry breaking

Shuryak; Diakonov, Petrov (1980s)

- perturb. interactions preserve quark chirality
non-perturbative gluon fields can flip it
 topological gauge fields, instantons
- I, \bar{I} form dilute strongly-interacting medium which stabilizes at $\rho \sim 0.3 \text{ fm}$ and $R \sim 1 \text{ fm}$
 non-trivial small parameter $\sim c_0 (\rho/R)^4/N_c \sim \frac{1}{20}$
 instanton liquid model of QCD vacuum
- light quarks acquire momentum-dependent mass
 QCD vacuum structure (quark condensate)
 $\langle 0 | \bar{\psi} \psi | 0 \rangle = \langle 0 | \bar{\psi}_L \psi_R + \bar{\psi}_R \psi_L | 0 \rangle \neq 0$
 order parameter of symmetry breaking
- **Goldstone** boson π collective excitation
 $m_\pi^2 f_\pi^2 = -m_q \langle 0 | \bar{\psi} \psi | 0 \rangle$ Gell-Mann–Oakes–Renner
- **effective (“constituent”) q, \bar{q}** with dynamical mass $M(0) \sim 0.35 \text{ GeV}$
 for $p \ll \Lambda_{\text{cut}} = \rho^{-1} \sim 0.6 \text{ GeV}$
- chiral symmetry breaking occurs at **scale** $\rho \sim 0.3 \text{ fm}$

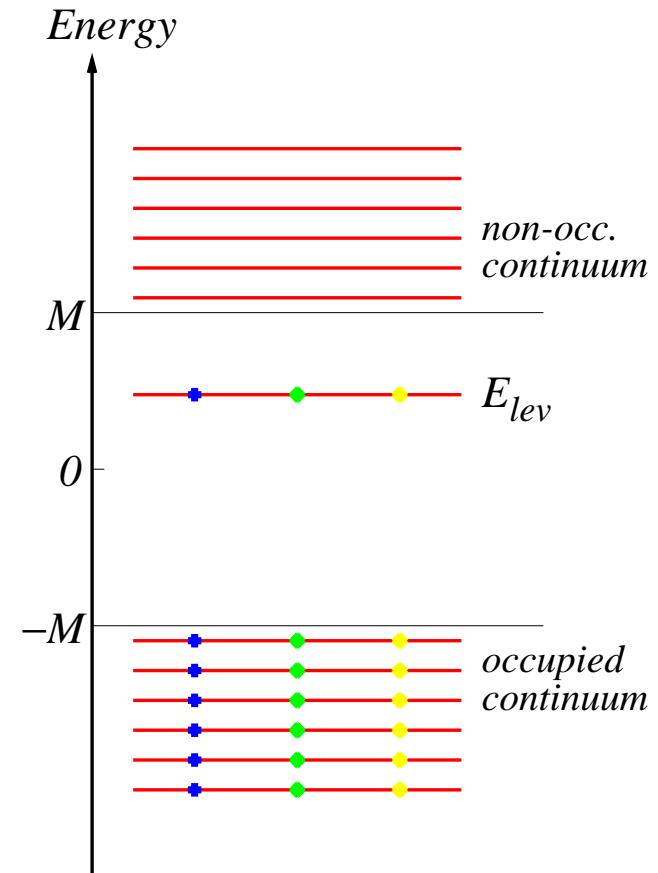


tool: chiral quark soliton model

Diakonov, Eides 1983; Diakonov, Petrov 1986

$$\mathcal{L}_{\text{eff}} = \bar{\Psi} (i \not{\partial} + M \not{U}^{\gamma_5}) \Psi$$

- constituent q, \bar{q} degrees of freedom with **dynamical mass** $M \sim 350 \text{ MeV}$ at energies $\lesssim \rho^{-1} \simeq 600 \text{ MeV}$ (cutoff)
- coupled to chiral field $\not{U}^{\gamma_5} = \exp(i\gamma_5 \tau^a \pi^a / F_\pi)$ coupling constant $g_{\pi q\bar{q}} = M/F_\pi \sim 4$ is large!
- $\langle N' | \dots | N \rangle = \int \mathcal{D}\bar{\Psi} \mathcal{D}\Psi \mathcal{D}U \langle 0 | J_N(\frac{T}{2}) \dots J_N^\dagger(-\frac{T}{2}) | 0 \rangle e^{-iS_{\text{eff}}}$
solve limit $T \rightarrow \infty$ on paper, integration over $\bar{\Psi}, \Psi$ exact path integral over U non-perturbatively in **$1/N_c$ expansion**
 $M_N = \min_U E_{\text{sol}}[U]$, quantize zero modes (large N_c picture, Witten 1979)
- **chiral quark-soliton model** (no free parameters!)
Diakonov, Petrov, Pobylitsa 1986; Kahana, Ripka 1984
- full Dirac sea, no Fock space truncation:
consistent, theoretically appealing!
(completeness, locality, analyticity)
- **successful phenomenology!** useful accuracy (10-30)%
systematic $1/N_c$ expansion: mass spectrum, form factors, PDFs, GPDs
TMDs (Goeke et al, Diakonov et al, Reinhardt et al, Wakamatsu et al)



$$H\psi_n = E_n\psi_n$$

$$\langle N' | \bar{\Psi} \dots \Psi | N \rangle = A \sum_n \bar{\psi}_n \dots \psi_n$$

applications of effective theory

- **vacuum sector:** $\frac{\langle F^2 \rangle}{32\pi^2} \simeq (200 \text{ MeV})^4$ **gluon condensate** QCD sum rules
= instanton density $\Rightarrow R \sim 1 \text{ fm}$

$$\begin{aligned}\langle \bar{\Psi} \Psi \rangle &\simeq -(250 \text{ MeV})^3 \text{ quark condensate} \\ &= \text{const } N_c / (\rho R^2) \Rightarrow \rho \sim \frac{1}{3} \text{ fm}\end{aligned}$$

- **meson sector:** **chiral Lagrangian** integrate out $\int \mathcal{D}\bar{\Psi} \mathcal{D}\Psi e^{-iS_{\text{eff}}} =$
 $\mathcal{L}_\pi(U) = \frac{1}{4} f_\pi^2 \partial^\mu U \partial_\mu U^\dagger + \text{Gasser-Leutwyler-terms} + \dots$
 $f_\pi^2 = \int \frac{d^4 p}{(2\pi)^4} \frac{4N_c M^2}{(p^2 + M^2)^2} = (93 \text{ MeV})^2 \Rightarrow \Lambda_{\text{cut}}$
low energy coefficients predicted, consistent
Schüren, Ruiz Arriola, Goeke 1991

- **baryon sector:** parameter-free results/predictions, no tuning!
 $M = 350 \text{ MeV}$ and $\Lambda_{\text{cut}} \sim \rho^{-1} \sim 600 \text{ MeV}$
determined in vacuum + meson sector
examples: M_N , GPDs, PDFs of q
main topic: asymmetries of \bar{q}

nucleon mass

$$M_N = N_c \sum_{\text{occ}} (E_n - E_n^{(0)})_{\text{reg}} + \mathcal{O}(N_c^0)$$

- at physical point: about 25% too large, spurious soliton center of mass motion ✓
 N_c^0 -correction $\sim -300 \text{ MeV}$ Pobylitsa et al. 1992
 \rightarrow model accuracy $\sim (10\text{--}30)\%$

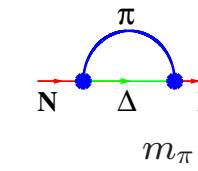
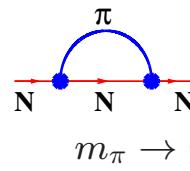
- in chiral limit: $M_N(m_\pi) = M_N(0) + A m_\pi^2 + k \times \frac{3 g_A^2}{32 \pi f_\pi^2} m_\pi^3 + \text{higher orders}$ ✓

$k = 1$ at finite N_c

$k = 3$ large- N_c limit

limits do not commute

the role of Δ -resonance
leading non-analytic terms

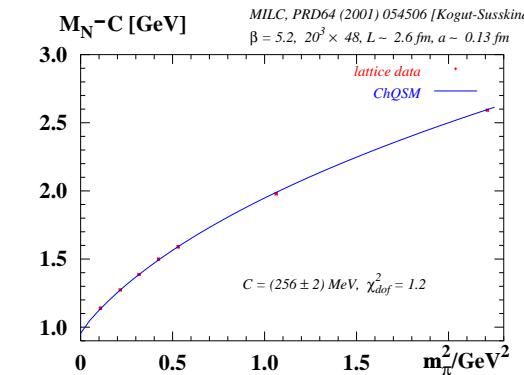
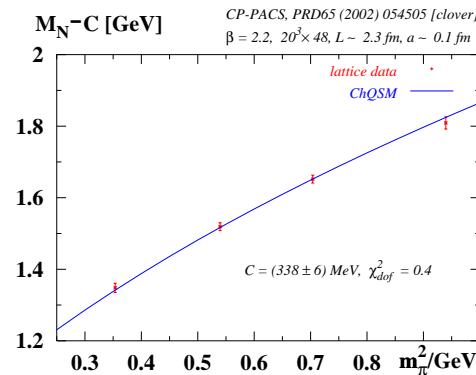
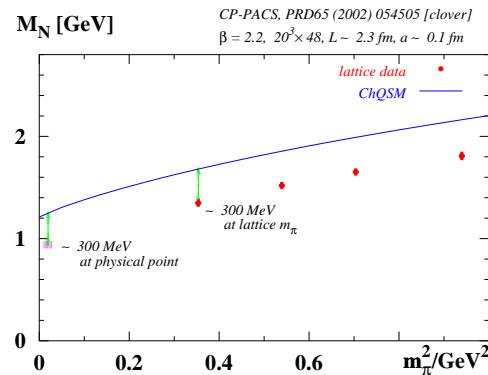


in large- N_c
Cohen, Broniowski 1992

- heavy quark limit: $\lim_{m_q \rightarrow M_Q} M_N = N_c M_Q$ formal proof ✓ Goeke et al, EPJA27 (2006) 77

- test with lattice ✓

⇒ no precision tool
but does what it
is expected:
chiral physics!



historical plot → model describes well variation of M_N with m_π (chiral physics)
EPJA (2006) see Tony Thomas et al, FRR approach

GPDs most demanding for models!

- (i) **forward limit** $H^q(x, \xi, t) \rightarrow f_1^q(x)$ ✓ all models
- (ii) **form factors** $\rightarrow \int dx H^q(x, \xi, t) = F_1^q(t) \neq F(\xi, t)$ ✓ not all models!
- (i) **positivity** $\rightarrow f_1^q(x) > 0$, Soffer bound ✓ certain models
- (iii) **polynomiality** Lorentz inv. + time-reversal, even N (if odd, highest power ξ^{N-1})

$$\int dx x^{N-1} H^q(x, \xi, t) = h_0^{q(N)}(t) + h_2^{q(N)}(t) \xi^2 + \dots + h_N^{q(N)}(t) \xi^N \quad \checkmark$$

$$\begin{aligned} \int dx x^{N-1} E^q(x, \xi, t) &= e_0^{q(N)}(t) + e_2^{q(N)}(t) \xi^2 + \dots + e_N^{q(N)}(t) \xi^N \quad \checkmark \\ -e_N^{q(N)}(t) &= h_N^{q(N)}(t) \quad \checkmark \text{ only ChQSM! (rigorous analytical proof)} \end{aligned}$$

- (iv) **D-term** \rightarrow even N highest powers ("Polyakov-Weiss terms") ✓ "discovered"
- (v) **form factors of EMT**

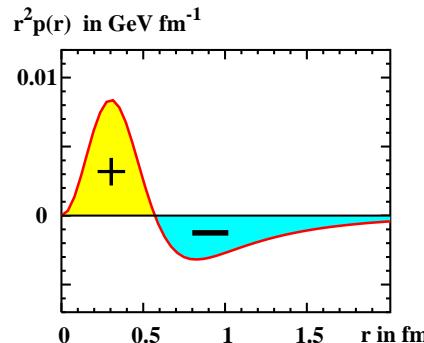
gravitational FFs, $N = 2$

$$T_{00}(r) \rightarrow \int d^3x T_{00}(r) = M_N \quad \checkmark$$

$$\varepsilon^{ijk} x_j T_{0k}(r) \rightarrow \text{Ji sum rule } J_N = \frac{1}{2} \quad \checkmark$$

$$T_{ij}(r) \rightarrow \int_0^\infty dr r^2 p(r) = 0 \quad \checkmark$$

→ forces



side remark:
insight from parton densities:
how are the quarks distributed?
here dynamics: **why** so distributed?
mechanical response function
grain of salt: $\sim 3\%$ rel. corr. proton

PDFs

What can we expect in effective theory?

- $xN_c = \mathcal{O}(1)$ applicable \rightarrow “non-exceptional x ” (no $x \rightarrow 0$, no $x \rightarrow 1$)
- small $x \leq (M\rho)^2/N_c \sim 0.1$ sensitive to **UV**-details of theory
- to leading order **model quark** = **QCD quark** + $\underbrace{\mathcal{O}(M^2\rho^2)}$ at low scale $\mu \sim \rho^{-1}$
 - suppressed in instanton vacuum*
- **gluons** not ignored, but (twist-2 gluons) suppressed by $\overbrace{\mathcal{O}(M^2\rho^2)} \sim 30\%$ at $\mu \sim \rho^{-1}$
- solve $\int \mathcal{D}U \dots$ in large- N_c : **PDF**(x) = $N_c^2 a_{\text{LO}}(xN_c) + N_c a_{\text{NLO}}(xN_c) + \dots$
- compare to meson-cloud models which “expand” to 1st order in $g_{\pi NN} = g_A M_N/f_\pi \sim 12.7$ in ChQSM **all orders** included in soliton field (non-perturbative method)
- **flavor structure:** $u \pm d$ leading vs $u \mp d$ subleading (general large N_c)

$$f_1: u + d \gg u - d$$

$$g_1: u - d \gg u + d$$

$$h_1: u - d \gg u + d \quad \text{analog for } \bar{q}$$

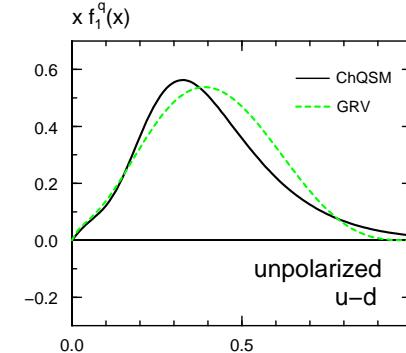
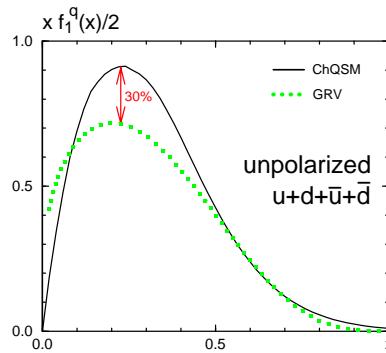
⇒ focus on “non-exceptional x ”
expect “precision” of 30 % or so

results for quarks

historical plots (GRV, GRSV, ...)

- unpolarized

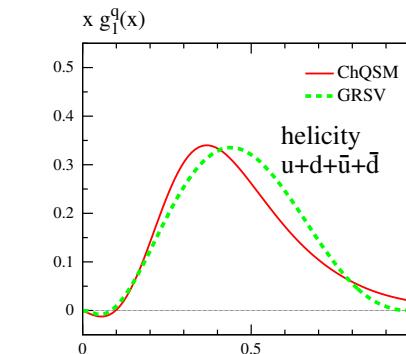
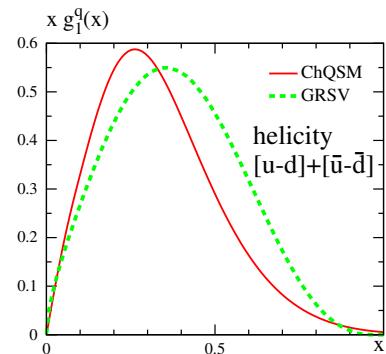
Diakonov et al, NPB 1996
Pobylitsa et al, PRD 1998



room for gluons in singlet
non-singlet fine, overall ✓

- helicity

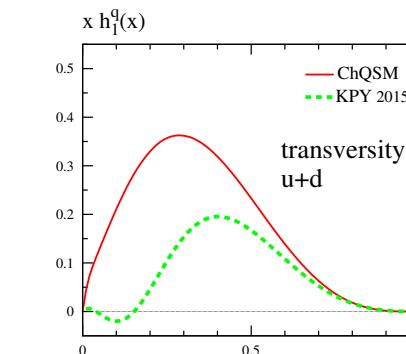
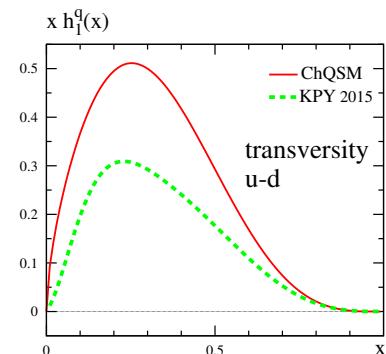
Diakonov et al, NPB 1996
Goeke et al, 2001



non-singlet, singlet within
what one can expect ✓

- transversity

PS, Urbano et al, PRD 2001



early stage of extractions
within model accuracy ✓

sea quarks

- model results:

flavor asymmetries in all twist-2 PDFs:

helicity Diakonov et al, NPB 1996

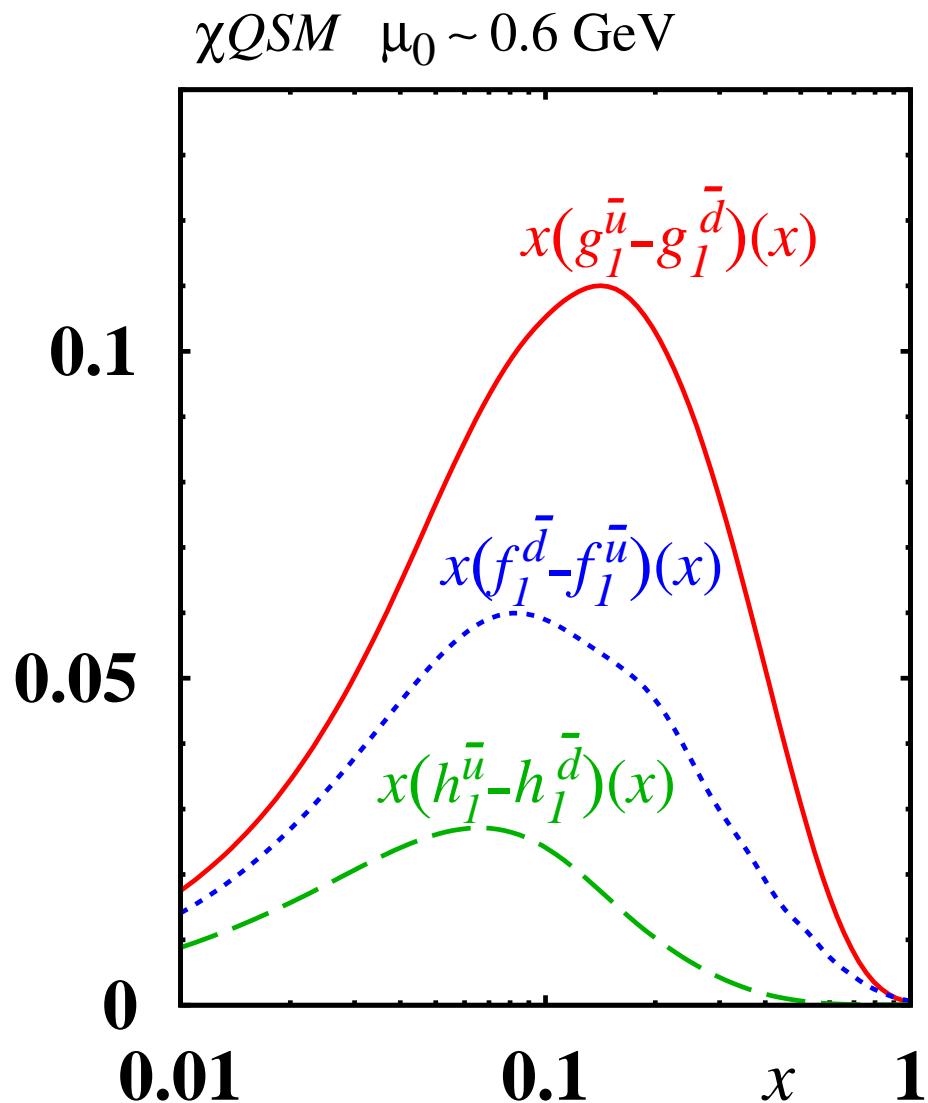
unpolarized Pobylitsa et al, PRD 1998

transversity PS et al, PRD 2001

$$(g_1^{\bar{u}} - g_1^{\bar{d}})(x) \sim N_c^2$$

$$(f_1^{\bar{d}} - f_1^{\bar{u}})(x) \sim N_c$$

$$(h_1^{\bar{u}} - h_1^{\bar{d}})(x) \sim N_c^2$$



unpolarized sea: $\bar{d} - \bar{u}$

- model result

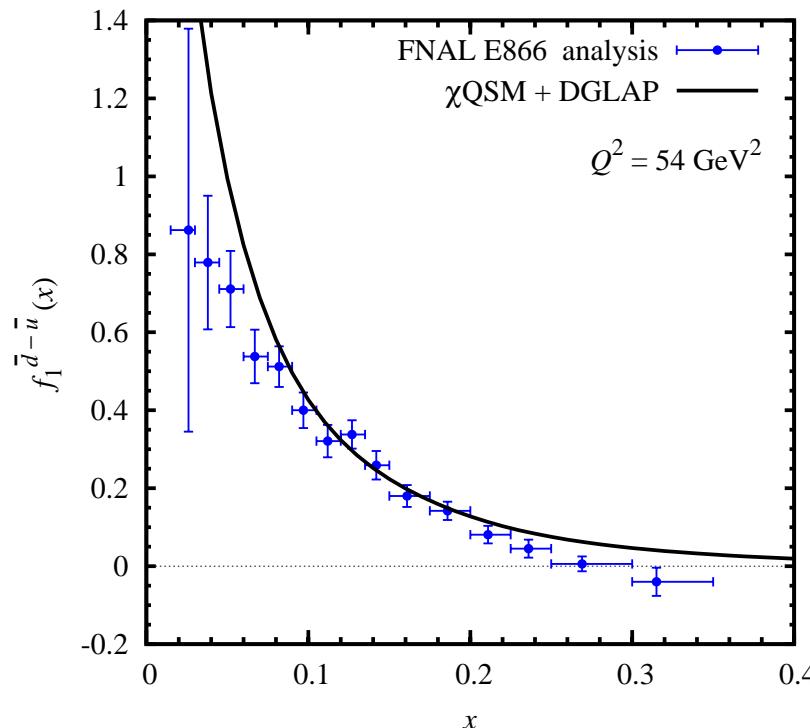
Pobylitsa et al, PRD 1998

LO non-singlet evolution VS

J. C. Peng et al, PRD 58 (1998)

Gottfried sum:

$$I_G = \frac{1}{3} + \frac{2}{3} \int dx (f_1^{\bar{u}} - f_1^{\bar{d}})(x) = 0.219$$

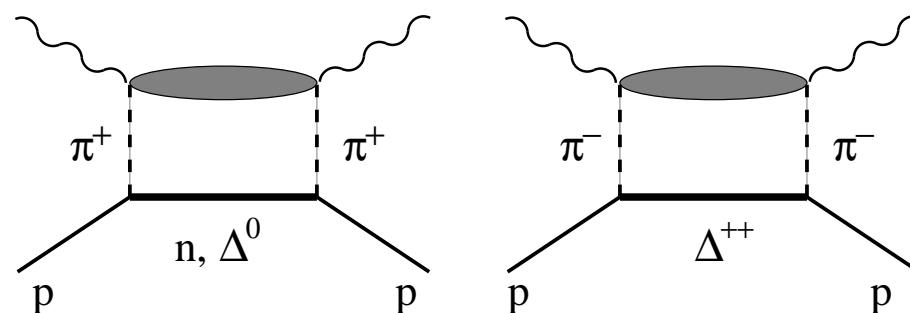


- why?

expand model expression in ∂U

\Leftrightarrow **Sullivan process** (\rightarrow Wally)

(no small parameter to justify
but gives a feeling about
involved quantum numbers)



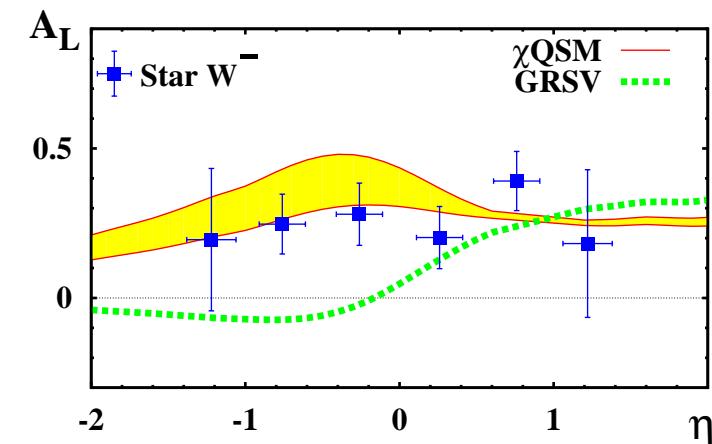
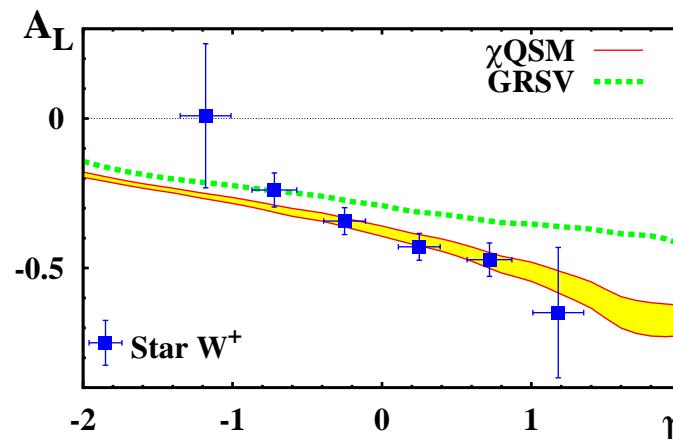
helicity sea: $\bar{u} - \bar{d}$

- model result

Diakonov et al, NPB 1996
 predictions for W^\pm in pp
 Dressler et al EPJC 2001
 (thanks to Werner)

L. Adamczyk et al.
 (STAR Collaboration),
 PRL 113, (2014) 072301
 → talks by Bernd Surrow
 and Elke Aschenauer

back in 2001: change of basis
 $u, d, \bar{u}, \bar{d}, \dots \rightarrow \underbrace{(u + \bar{u})}_{\text{DIS}}, \underbrace{(d + \bar{d})}_{\text{DIS}}, \underbrace{(\bar{u} + \bar{d})}_{\text{DIS}}, \underbrace{(\bar{u} - \bar{d})}_{\text{model}}, \dots$

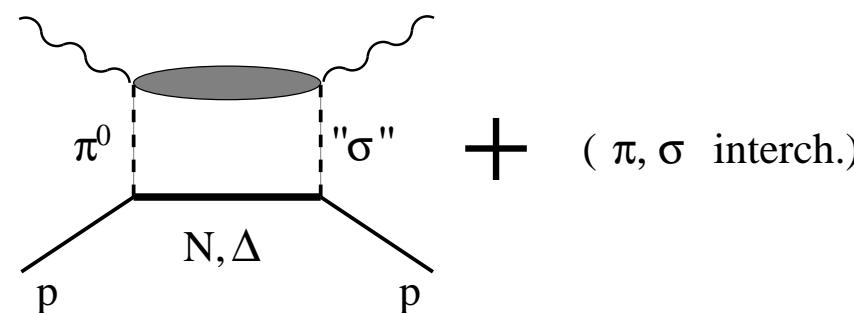


- why?

expand model expression in ∂U

↔ **σ - π interference**

(no small parameter to justify
 but gives a feeling about
 involved quantum numbers)



transversity sea: $\bar{u} - \bar{d}$

- model result

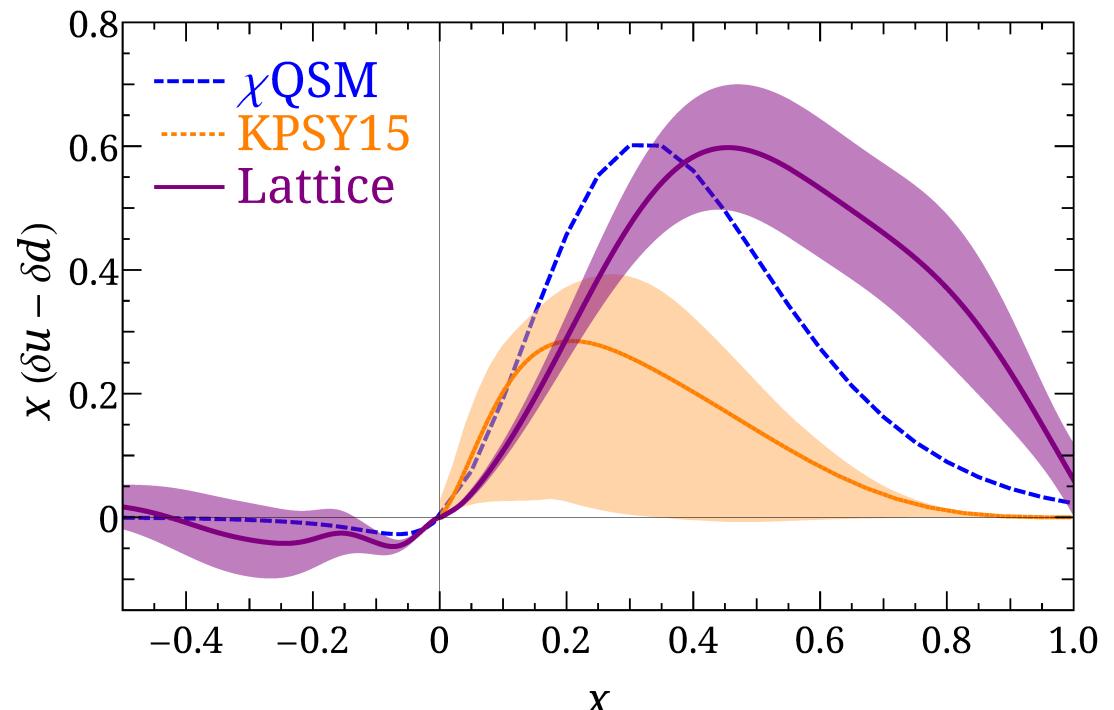
PS et al, PRD 2001

waiting for experimental test
meanwhile compare to lattice

Chen et al, NPB 911 (2016) 246

(→ Huey-Wen Lin's talk)

(+ Kang, Prokudin, Sun, Yuan PRD93)

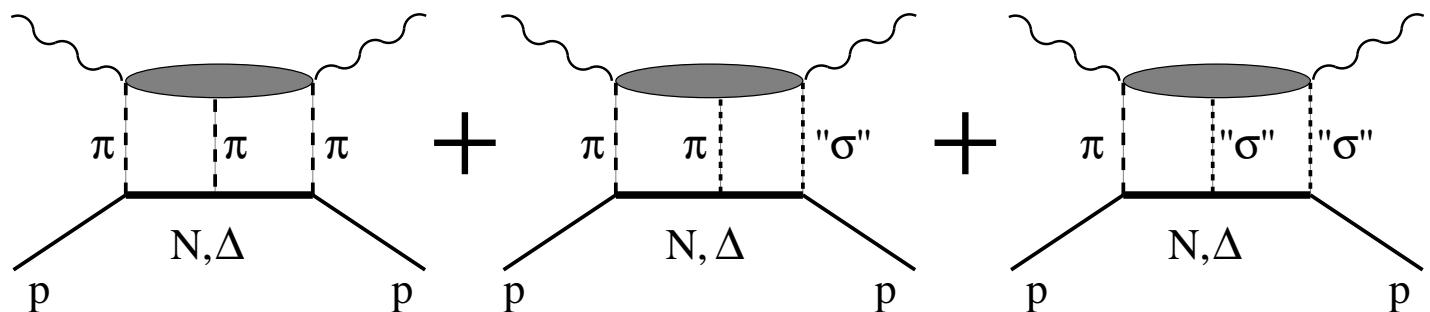


- why?

expand model expression in ∂U

↔ higher order chiral dynamics!

(no small parameter to justify)



emerging picture:

\bar{q} -asymmetry	experiment	χ QSM
$(f_1^{\bar{d}} - f_1^{\bar{u}})(x) \sim N_c$	✓	✓
$(g_1^{\bar{u}} - g_1^{\bar{d}})(x) \sim N_c^2$	✓	promising
$(h_1^{\bar{u}} - h_1^{\bar{d}})(x) \sim N_c^2$	future	waiting

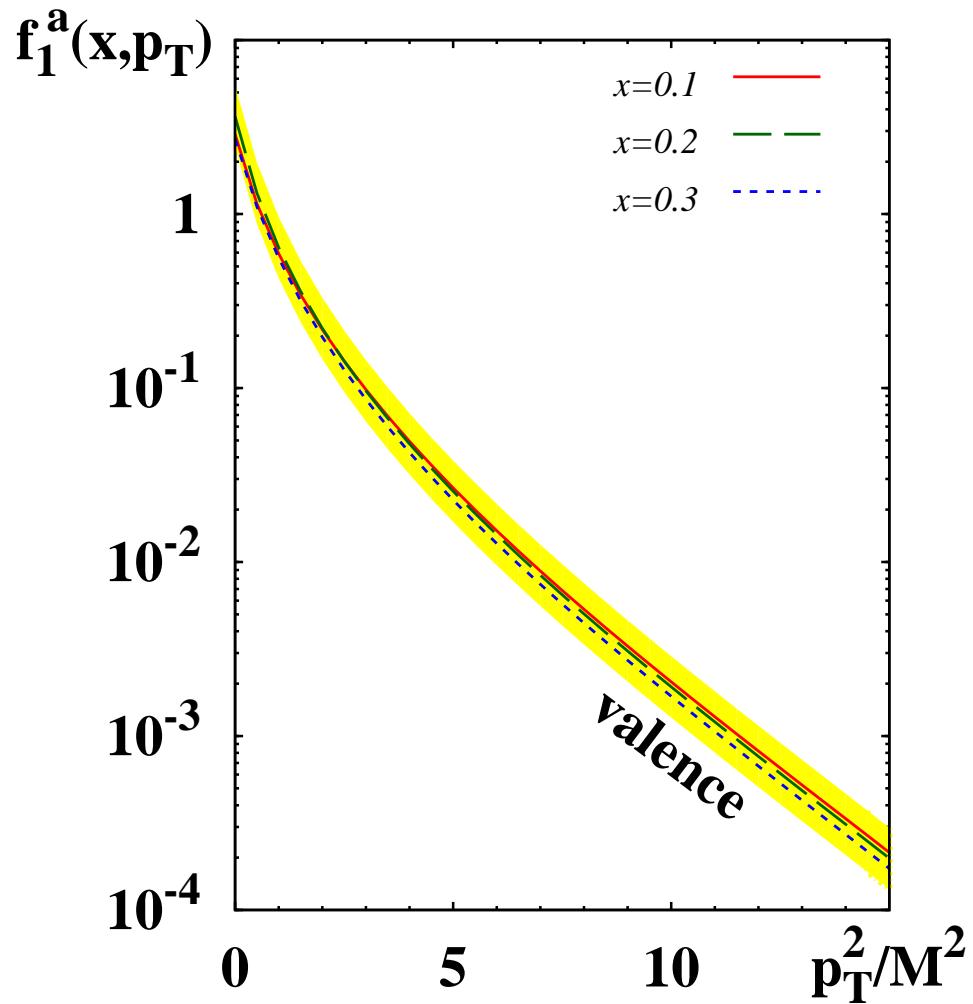
do we understand?

- $(g_1^{\bar{u}} - g_1^{\bar{d}})(x)$ sizable, perhaps larger than $(f_1^{\bar{d}} - f_1^{\bar{u}})(x)$. Why? Explanation: large- N_c
- but why should $(g_1^{\bar{u}} - g_1^{\bar{d}})(x)$ and $(f_1^{\bar{d}} - f_1^{\bar{u}})(x)$ be sizable in first place?
- and why should $(h_1^{\bar{u}} - h_1^{\bar{d}})(x)$ be less sizable?

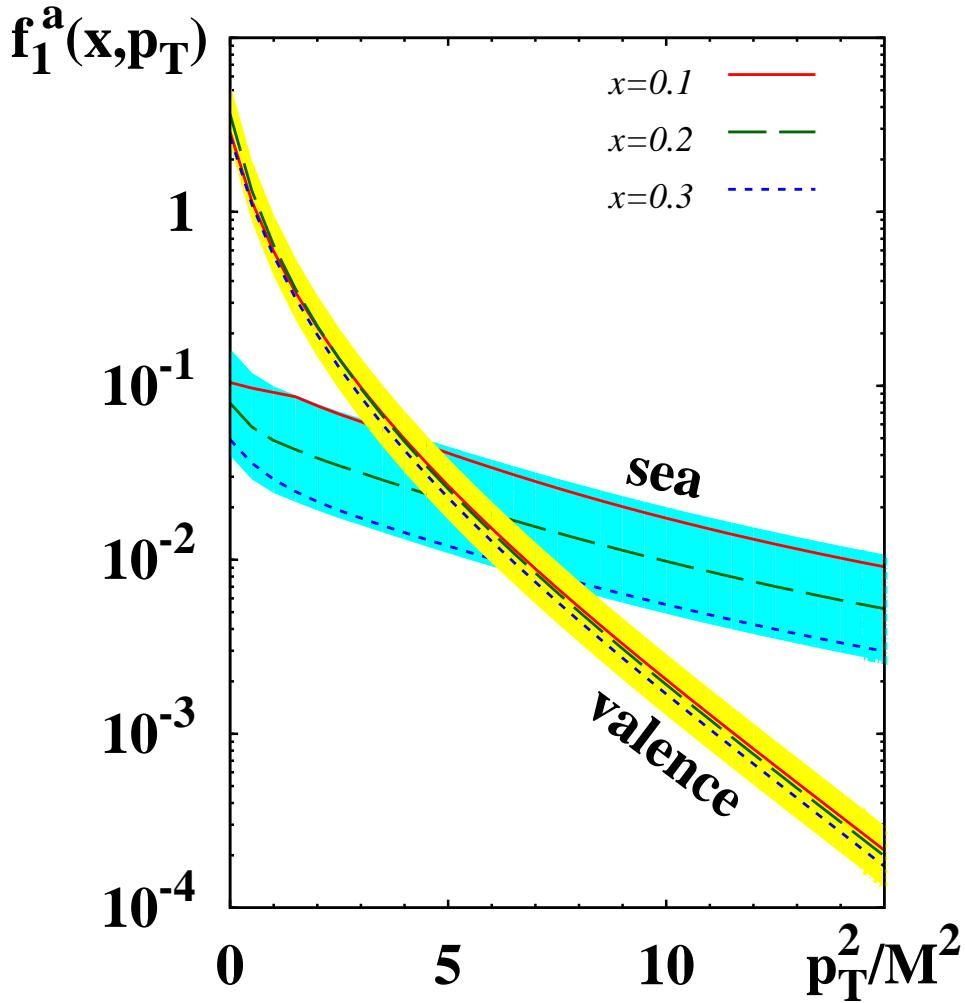
→ go beyond 1-D for new insights:
look at TMDs $f_1^{\bar{q}}(x, p_T)$, $g_1^{\bar{q}}(x, p_T)$, $h_1^{\bar{q}}(x, p_T)$

TMDs in ChQSM:

- **valence quarks** $\equiv (u + d) - (\bar{u} + \bar{d})$
 $\langle p_T^2 \rangle_{\text{val}} \sim 0.15 \text{ GeV}^2 \sim \mathcal{O}(M^2)$
 → bound state (similar: bag, spectator, LFCM)



TMDs in ChQSM:



- **valence quarks** $\equiv (u + d) - (\bar{u} + \bar{d})$
 $\langle p_T^2 \rangle_{\text{val}} \sim 0.15 \text{ GeV}^2 \sim \mathcal{O}(M^2)$
 → bound state (similar: bag, spectator, LFCM)

- **sea quarks** $\equiv \bar{q} \equiv (\bar{u} + \bar{d})$!
 $p_T \sim 1/\rho$ power-like behavior
 quasi model-independent:

$$f_1^{\bar{q}}(x, p_T) \approx f_1^{\bar{q}}(x) \frac{C_1 M^2}{M^2 + p_T^2}$$

$$C_1 = \frac{2N_c}{(2\pi)^3 F_\pi^2} \quad \leftarrow \text{chiral dynamics!}$$

- **valence vs sea: qualitatively different!!**
quantitatively different $\langle p_T^2 \rangle_{\text{sea}} \sim 3 \langle p_T^2 \rangle_{\text{val}} !!$

- $g_1^{\text{val}}(x, p_T)$ vs. $g_1^{\text{sea}}(x, p_T)$ **similar behavior !!!**
 here: $\text{val} \equiv (u - d) - (\bar{u} - \bar{d})$, $\text{sea} \equiv (\bar{u} - \bar{d})$

remarkable: $g_1^{\bar{q}}(x, p_T) \approx g_1^{\bar{q}}(x) \frac{C_1 M^2}{M^2 + p_T^2}$
 same coefficient $C_1 \leftarrow \text{chiral dynamics!!}$

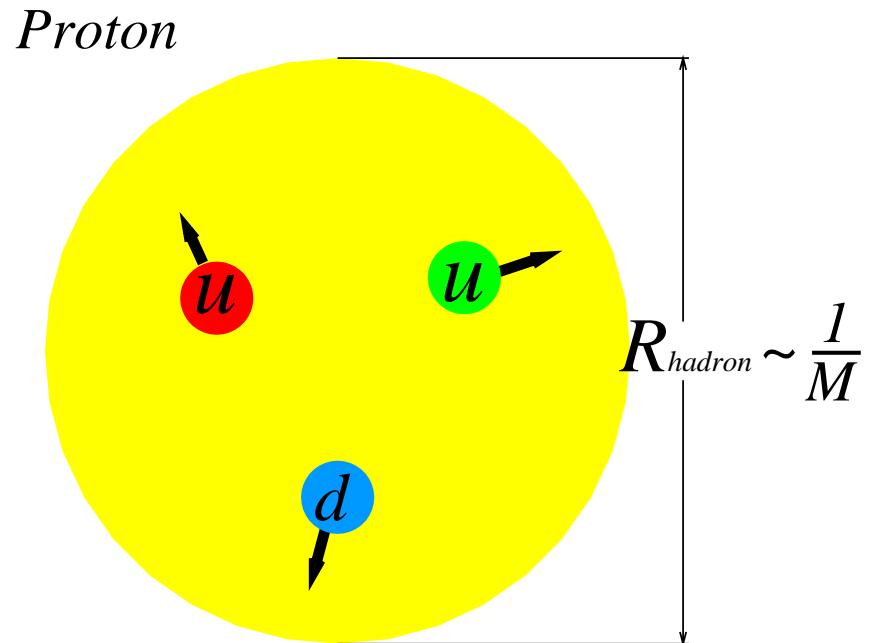
Why is that ...?

valence quark picture

realized in quark models: whether ChQSM,
spectator (Jakob et al), LFCM (Pasquini et al),
bag (Avakian et al), NJL-jet (Matevosyan et al),
details differ, but **bound-state** is bound-state

$$\langle p_T^2 \rangle_{\text{val}} \sim M^2$$

but what binds these valence quarks?
it's the **soliton field** due to χ SB,
strong coupling $f_{\pi q\bar{q}} = M/F_\pi \sim 4$
chiral field generates $\bar{q}q$ pairs
correlated at χ SB scale ρ !



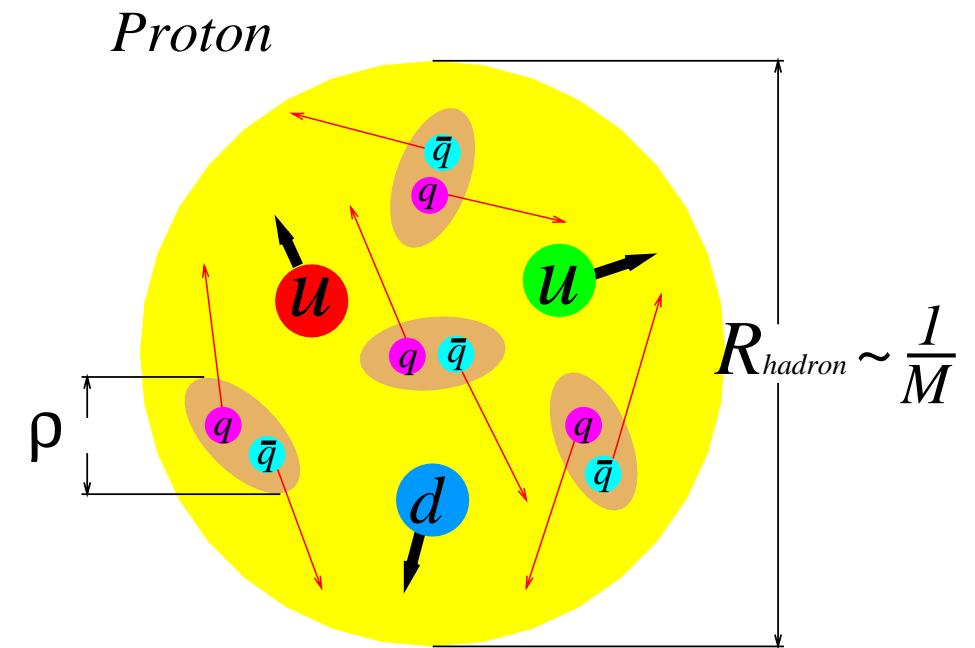
... signature of chiral symmetry breaking!

short-range correlations of q, \bar{q} pairs !!!

QCD vacuum structure
(“Dirac sea” in model)
PS, Strikman, Weiss 2013

$$\langle p_T^2 \rangle_{\text{val}} \sim M^2$$

$$\langle p_T^2 \rangle_{\text{sea}} \sim \rho^{-2}$$



$$\langle p_T^2 \rangle_{\text{val}} / \langle p_T^2 \rangle_{\text{sea}} \sim M^2 \rho^2 \sim M^2 / (\text{cutoff})^2 \ll 1$$

(‘diluteness’ of instanton medium) Diakonov, Petrov, Weiss 1996

transversity TMD (ongoing work)

- much different p_T -dependence:

$$h_1^q(x, p_T) \sim \frac{1}{(M^2 + p_T^2)^2}$$

vs. $f_1^q(x, p_T) \sim \frac{1}{(M^2 + p_T^2)}$ and $g_1^q(x, p_T) \sim \frac{1}{(M^2 + p_T^2)}$ for $M^2 \ll p_T^2 \ll \rho^{-2}$

- consequences:

p_T of transversity “of valence type” $\langle p_T^2 \rangle_{h_1} \ll \langle p_T^2 \rangle_{f_1}$ or $\langle p_T^2 \rangle_{g_1}$

clear: much different chiral mechanism

$f_1^{\bar{q}} \propto \sigma^* \sigma + \pi^* \pi \leftrightarrow$ Vector current

$g_1^{\bar{q}} \propto \sigma^* \pi + \pi^* \sigma \leftrightarrow$ Axial vector current

h_1^q and $h_1^{\bar{q}} \propto (\sigma \sigma^* \pi \pm \sigma \pi^* \pi \pm \pi \pi^* \pi) \mp$ c.c. \leftrightarrow “tensor current”

remarks

- sizable $f_1^{\bar{u}+\bar{d}}(x, p_T) \rightarrow$ sizable $f_1^{\bar{u}+\bar{d}}(x)$ (enhanced by chiral short range correlations)
- $f_1^{\bar{u}-\bar{d}}(x, p_T)$ suppressed by $1/N_c$ but the same chiral enhancement! So still large!
- sizable $g_1^{\bar{u}-\bar{d}}(x, p_T) \rightarrow$ sizable $g_1^{\bar{u}-\bar{d}}(x)$ feels chiral correlations & leading in large- N_c
- $g_1^{\bar{u}+\bar{d}}(x, p_T)$ also feels chiral short range correlations but suppressed by $1/N_c$
- $h_1^{\bar{q}}(x, p_T)$: higher order chiral dynamics, hence smallest flavor asymmetry

application for phenomenology:

CSS in b_T -space: $\tilde{f}_1^a(x, b_T) = \int d^2 p_T e^{i \vec{p}_T \cdot \vec{b}_T} f_1^a(x, p_T)$
 large- b_T : long-distance, non-perturbative physics, fit
 usual assumption: universal Gaussian- b_T fall-off
 Landry et al 2003; Konychev, Nadolsky 2006
 model: valence vs sea, exponential fall-off
 → Collins, Rogers 2014

experimental tests: ($q = \text{val} + \text{sea}$, $\bar{q} = \text{sea}$)

SIDIS (HERMES, COMPASS, JLab; JLab12, EIC)
 kinematic leverage, explore fragmentation (challenge)
 e.g.: $K^+ = u\bar{s} \sim (\text{val.} + \text{sea})$ vs $K^- = \bar{u}s \sim (\text{sea})$
 $(\pi^+ + \pi^-)$ vs $(\pi^+ - \pi^-)$

correlations in current \leftrightarrow target fragmentation

when correlated $q\bar{q}$ pair “split up”!

$Q^2 \sim$ few GeV 2 not too large
 (to avoid loss of correlation
 due to gluon radiation)

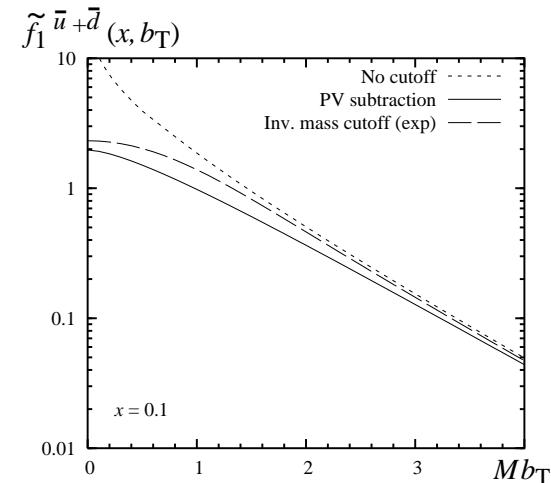
Kotzinian et al

hadron colliders

multi parton correlations (RHIC, Tevatron, LHC)

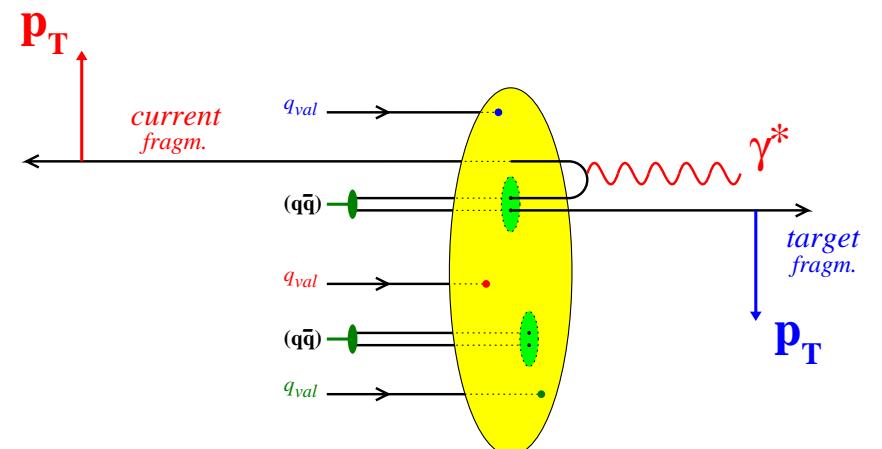
→ L. Frankfurt, M. Strikman, C. Weiss

Drell-Yan: pp vs $\bar{p}p$, RHIC, Fermilab, ...



large b_T -region

independent of UV-details (regularization)
 quasi model-independent → chiral-dynamics



short-range correlations $\sim \rho \ll R$

“opposite asymmetries” in fracture functions (?)

conclusions

- **χ SB key feature** of strong interactions, at $\rho \sim 0.3 \text{ fm} \ll R_{\text{hadron}}$
- realized in **chiral quark soliton model** (chiral, consistent, can do GPDs)
- predictions and good description of **sea quark flavor asymmetries**
- $(f_1^{\bar{d}} - f_1^{\bar{u}})(x) \checkmark \quad (g_1^{\bar{u}} - g_1^{\bar{d}})(x) \checkmark \quad (h_1^{\bar{u}} - h_1^{\bar{d}})(x)$
- underlying mechanism: **chiral symmetry breaking** at scale $\rho \ll R_{\text{hadron}}$
- more insight → **TMDs**: $\langle p_T^2 \rangle_{\text{sea}} > \langle p_T^2 \rangle_{\text{val}}$ interplay of ρ and R_{hadron} encouraging, more work and tests needed
- **chiral physics at $\mu_0 \sim \rho^{-1}$** of importance for non-perturbative parton properties

conclusions

- **χ SB key feature** of strong interactions, at $\rho \sim 0.3 \text{ fm} \ll R_{\text{hadron}}$
- realized in **chiral quark soliton model** (chiral, consistent, can do GPDs)
- predictions and good description of **sea quark flavor asymmetries**
- $(f_1^{\bar{d}} - f_1^{\bar{u}})(x) \checkmark \quad (g_1^{\bar{u}} - g_1^{\bar{d}})(x) \checkmark \quad (h_1^{\bar{u}} - h_1^{\bar{d}})(x)$
- underlying mechanism: **chiral symmetry breaking** at scale $\rho \ll R_{\text{hadron}}$
- more insight → **TMDs**: $\langle p_T^2 \rangle_{\text{sea}} > \langle p_T^2 \rangle_{\text{val}}$ interplay of ρ and R_{hadron} encouraging, more work and tests needed
- **chiral physics at $\mu_0 \sim \rho^{-1}$** of importance for non-perturbative parton properties

Thank you!