



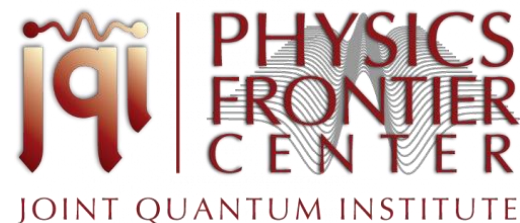
# Quantum simulations: advances in ion spin chains

**Jiehang Zhang**

Christopher Monroe group,

Joint Quantum Institute (JQI) and Department of Physics, University of Maryland

INT workshop, UW Seattle, 2017/11/14

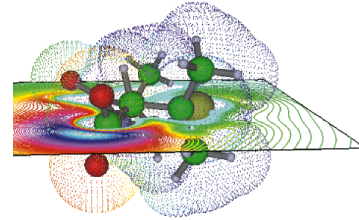


# Quantum Simulation

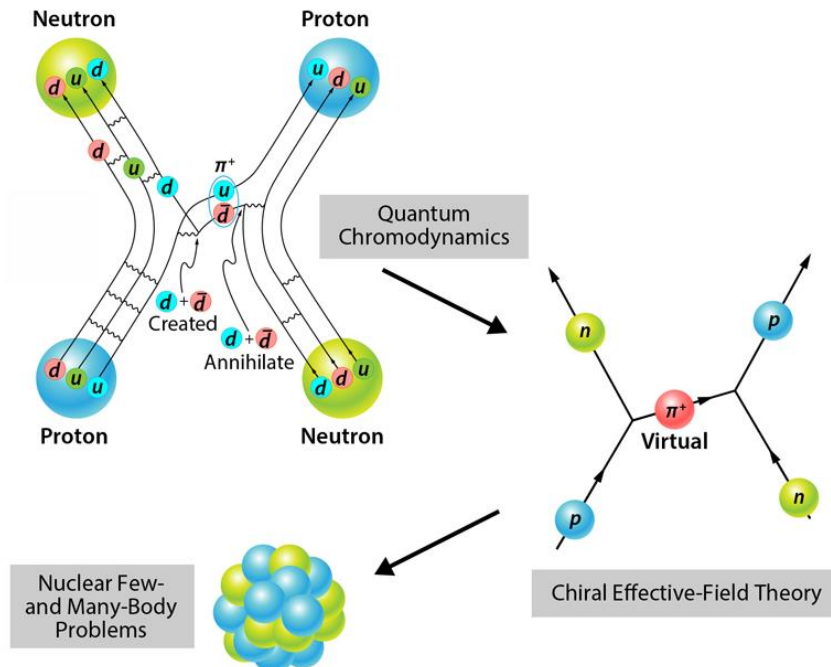
Study complex quantum many-body phenomena



High  $T_c$   
superconductivity



Quantum Chemistry



Nuclear many-body problems

# Quantum Simulation



*Classical Algorithms*

N spin  $\frac{1}{2}$  particles



$2^N$  complex amplitudes



# Quantum Simulation

*Classical Algorithms*

N spin  $\frac{1}{2}$  particles



$2^N$  complex amplitudes

*Quantum Simulation*

N spin  $\frac{1}{2}$  particles



N qubits

- **Toolbox**

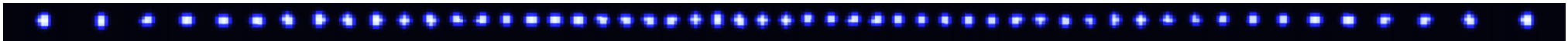
Quantum engineering with atomic ions

- **Non-equilibrium spin dynamics**

50+ qubit quantum simulator

- **Outlook**

Plenty of room at the bottom



- **Toolbox**

Quantum engineering with atomic ions

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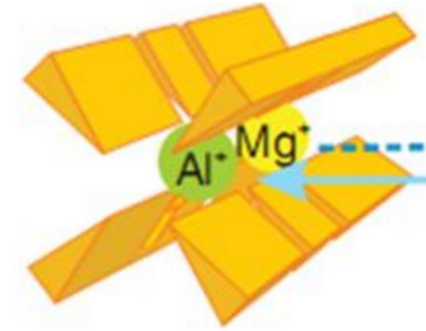
Plenty of room at the bottom

# Ion trap quantum information processing

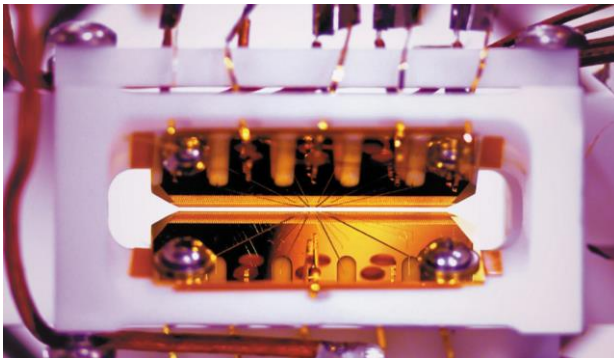


Ion clock  
 $3 \times 10^{-18}$   
accuracy

Precision measurements



Quantum logic spectroscopy



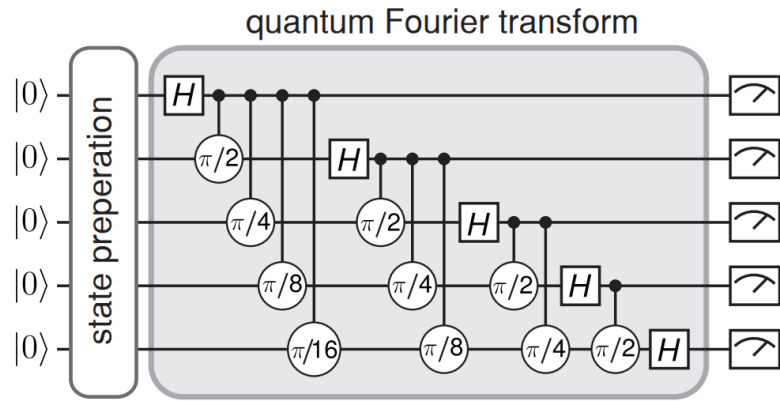
Program-  
mable  
quantum  
gates

Quantum computing:  
**digital**

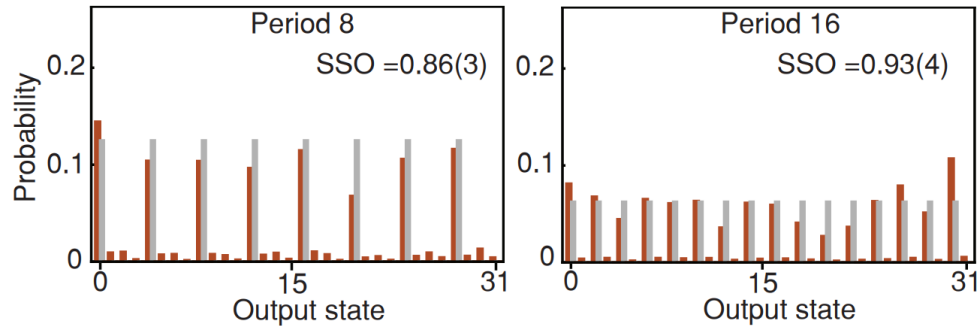


Synthetic quantum matter:  
**analog**

# Ion trap quantum information processing

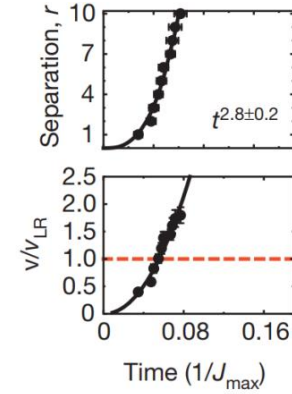
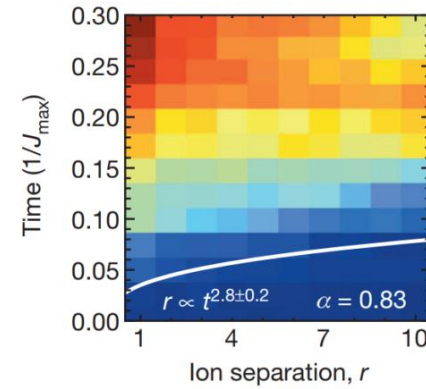


Quantum  
computing:  
digital

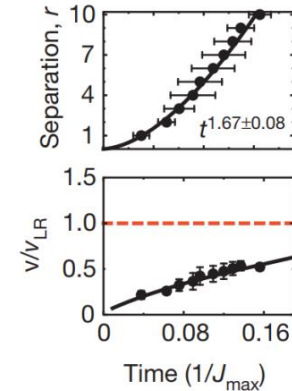
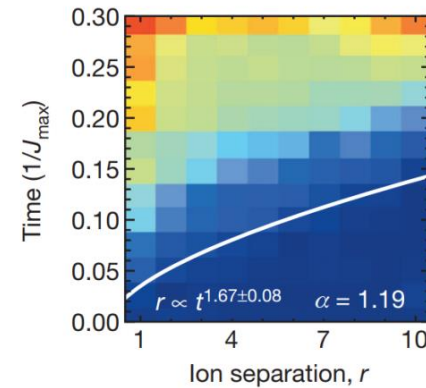


- Quantum algorithms

S. Debnath, *et al.*, *Nature* **536**, 63 (2016)



Synthetic  
quantum matter:  
analog



- Correlation propagation

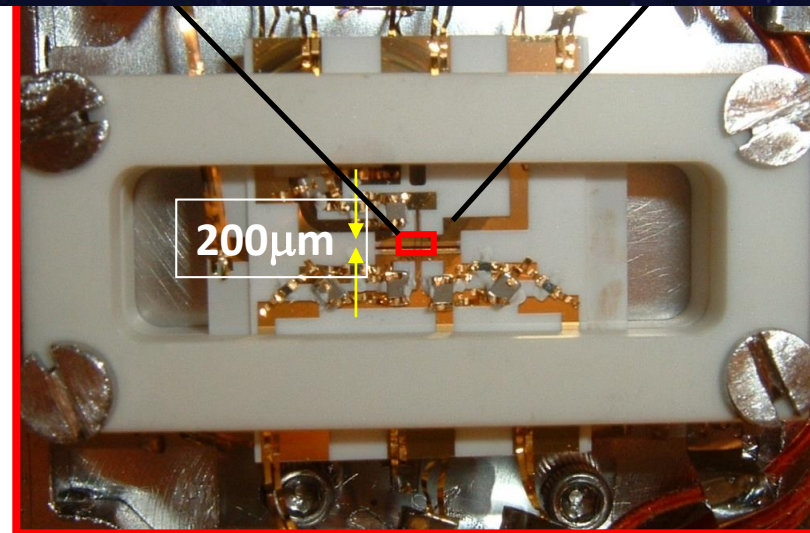
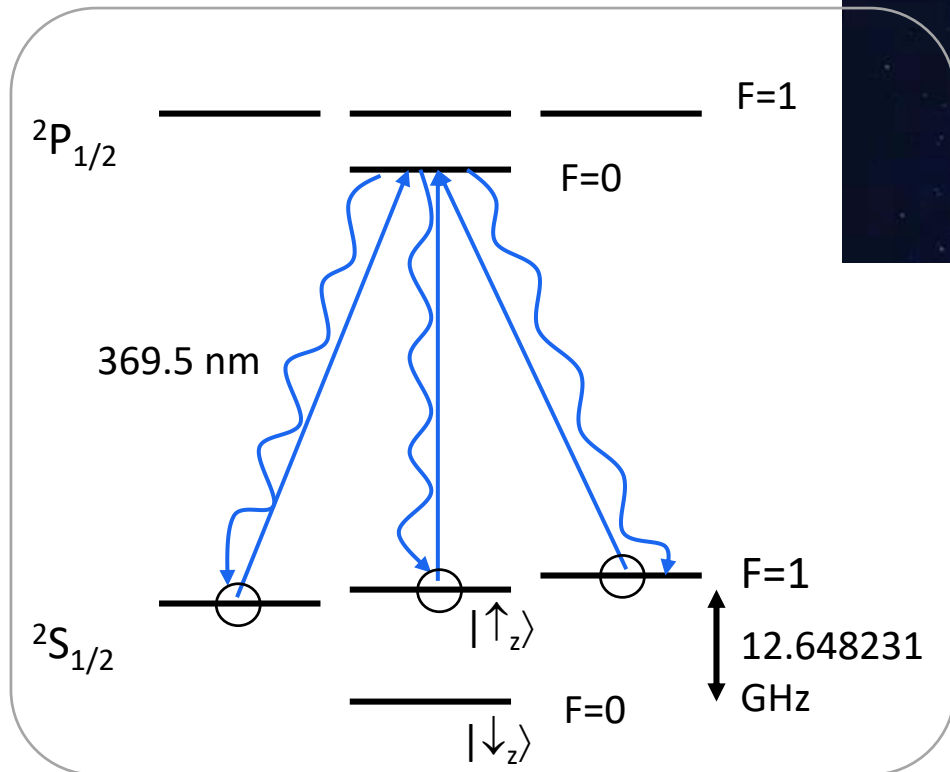
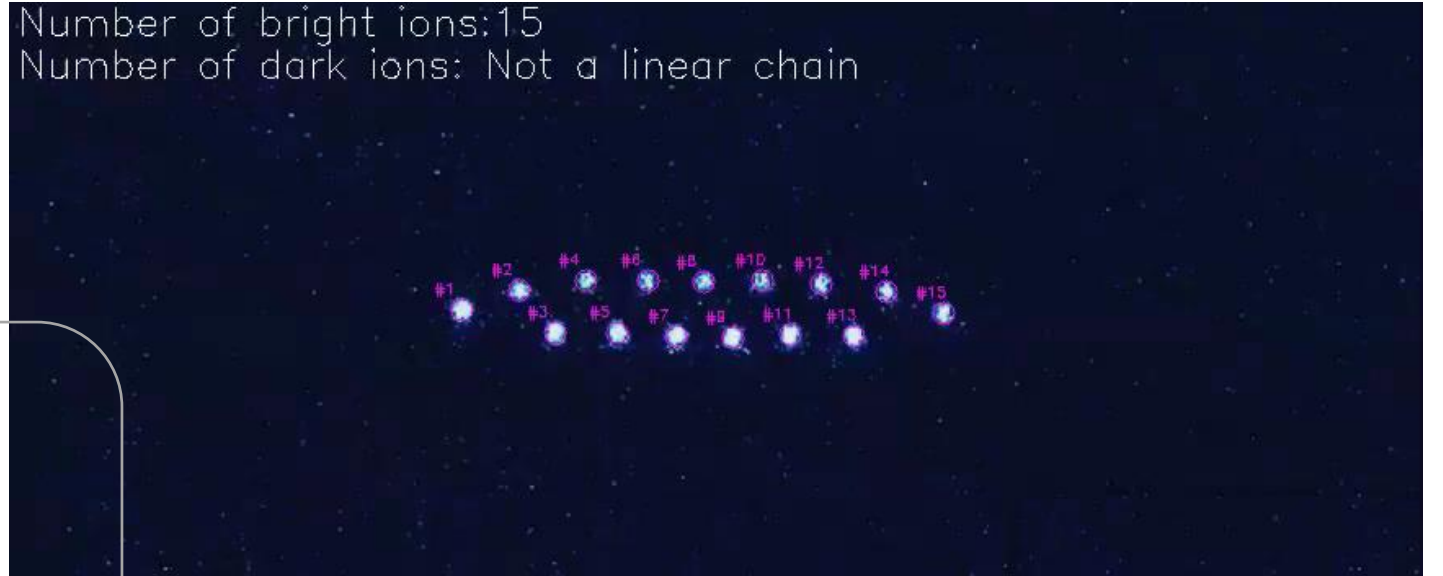
P. Richerme, *et al.*, *Nature* **511**, 198–201 (2014)

See also work by I. Bloch and R. Blatt groups

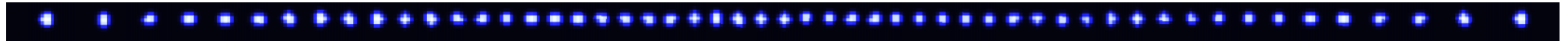


# $^{171}\text{Yb}^+$ hyperfine clock qubits.

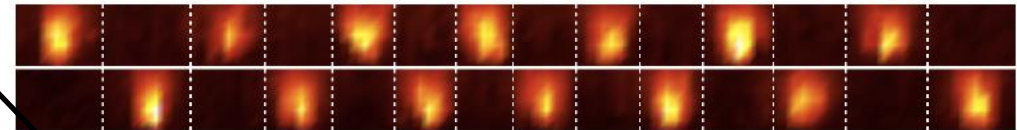
Number of bright ions: 15  
Number of dark ions: Not a linear chain



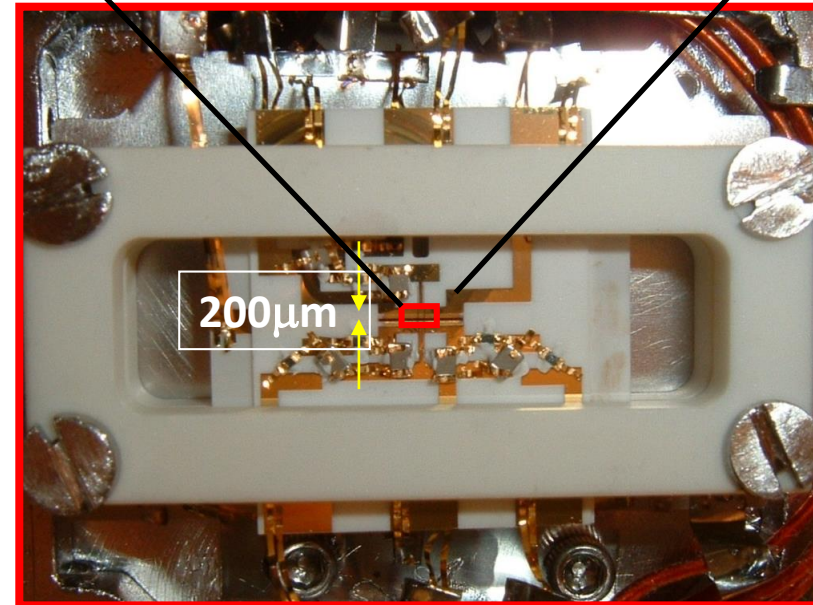
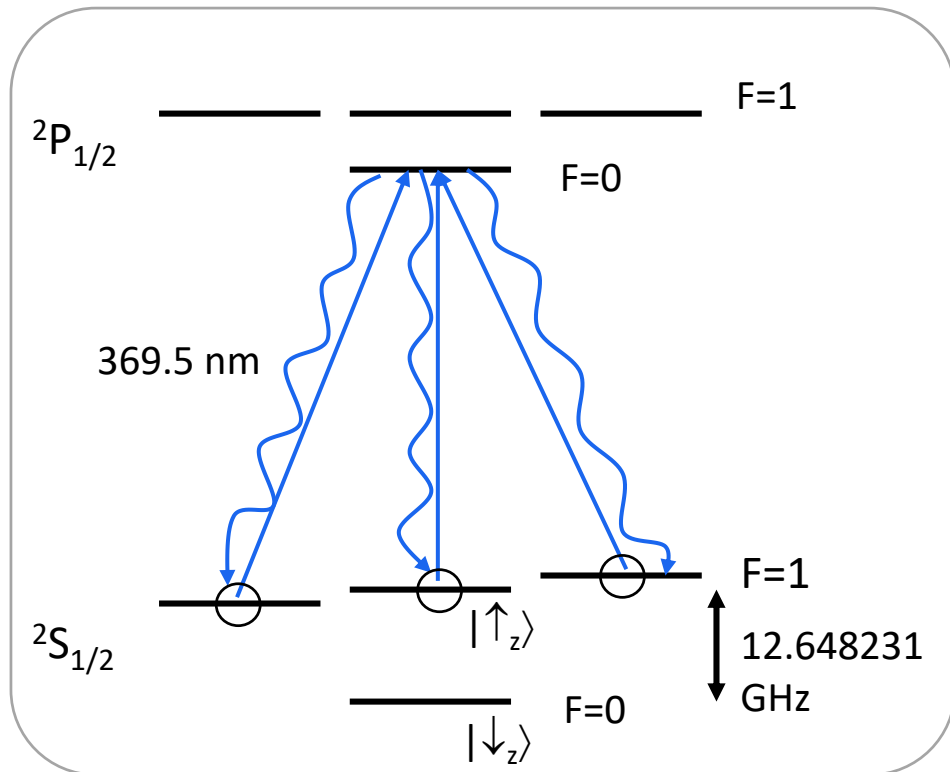
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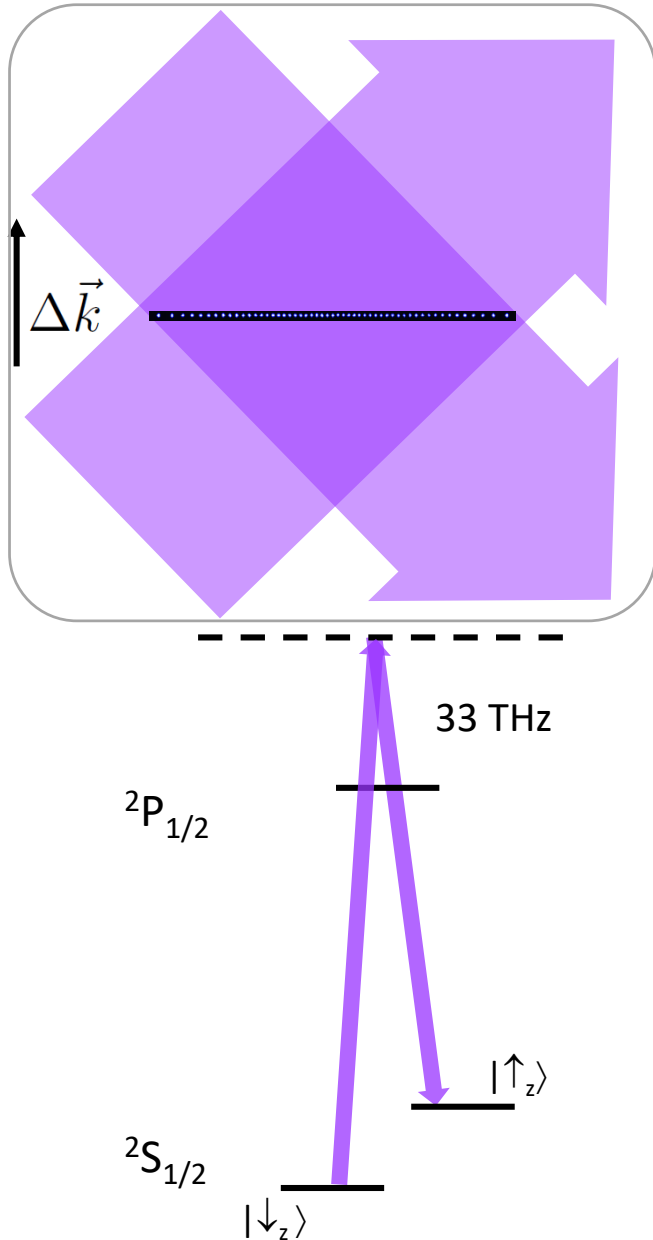


eg: AFM ordering of 14 spins



R. Islam, *et al.*, *Science* **340**, 583 (2013)





# Universal toolbox: Global interactions and individual addressing

## Transverse field Ising model

$$H_{\text{eff}} = \sum_{i < j} J_{ij} \sigma_i^x \sigma_j^x + B \sum_i \sigma_i^z + \sum_i D_i \sigma_i^z$$

- Long-range Ising interactions from spin-dependent dipole forces

$$J_{ij} \approx \frac{J_0}{|i - j|^\alpha} \quad (0 < \alpha < 3)$$

$J_0 \sim \text{kHz}$

- Transverse fields by asymmetric detuning of force
- Individual local field via Stark shifts:

A. C. Lee, *JZ, et al.*, Phys. Rev. A **94**, 042308 (2016)

- **Toolbox**

Quantum engineering with atomic ions

- **Non-equilibrium spin dynamics**

50+ qubit quantum simulator

- **Outlook**

Plenty of room at the bottom



# Non-equilibrium

- Correlation propagation [1]  
Lieb-Robinson bounds
- Failures of quantum thermalization [2,3]  
Localization and Prethermalization
- Dynamical phase transition [4]  
50+ qubit quantum simulator
- Discrete time crystal [5]  
A novel driven phase of matter

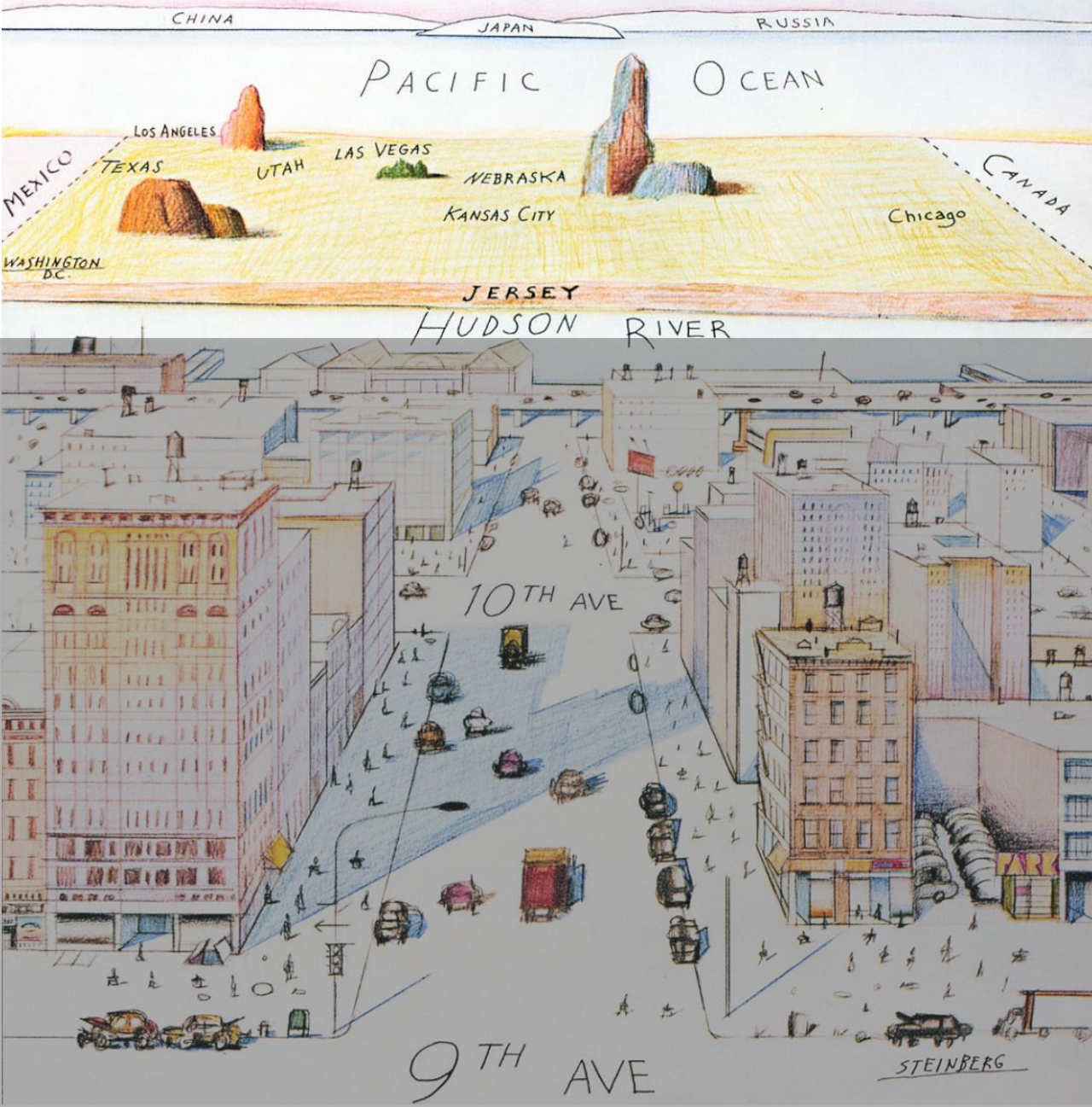
[1] P. Richerme, *et al.*, *Nature* **511**, 198–201 (2014)

[2] J. Smith, *et al.*, *Nat. Phys.* **12**, 907–911 (2016)

[3] B. Neyenhuis, JZ *et al.*, *Science Advances* **3**(8), e1700672 (2017)

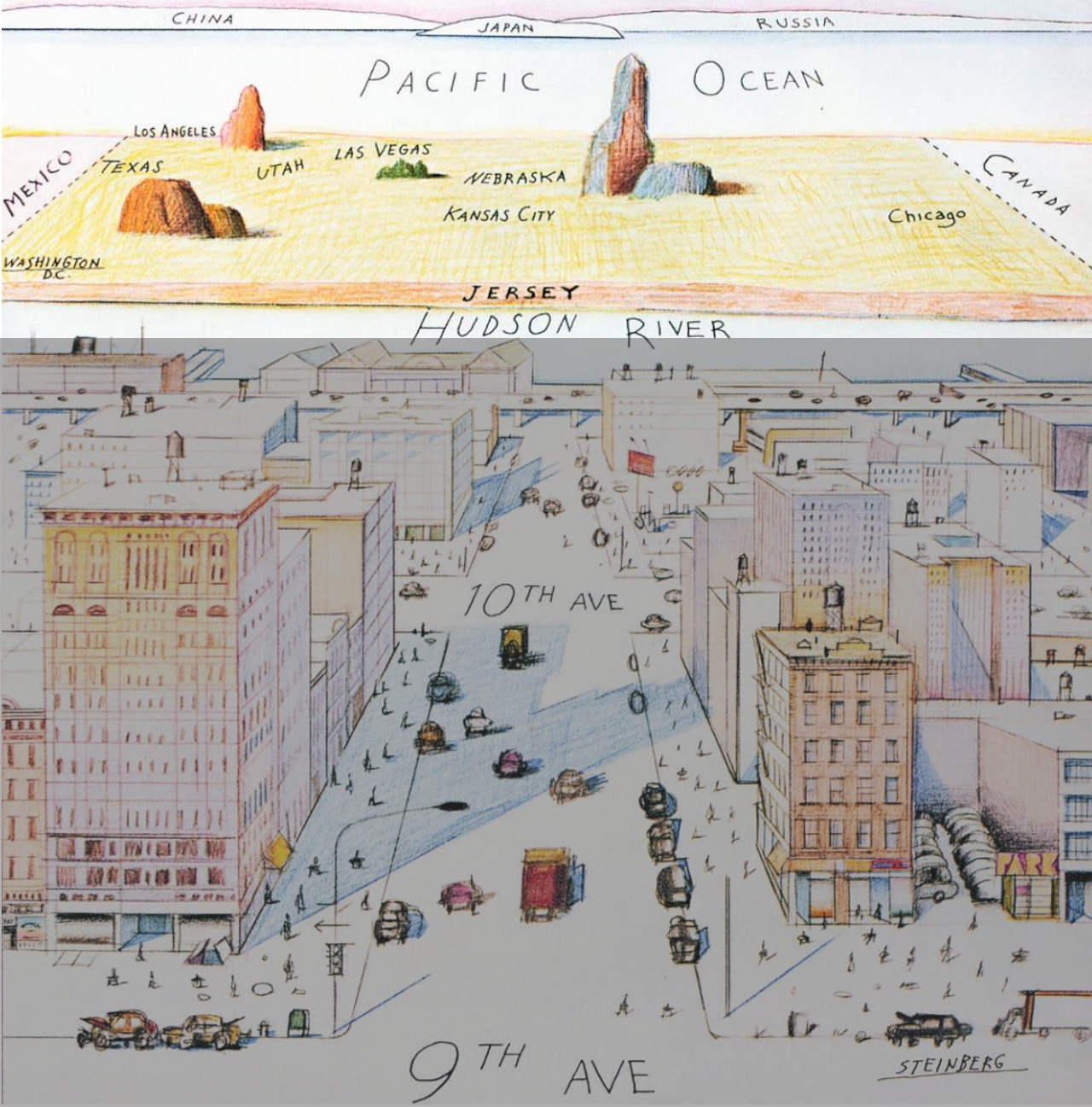
[4] JZ, *et al.*, arXiv 1708.01044 (2017), *Nature*, in press

[5] JZ *et al.*, *Nature* **543**, 217–220 (2017)





# Non-equilibrium



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A novel driven phase of matter

[1] P. Richerme, *et al.*, *Nature* **511**, 198–201 (2014)

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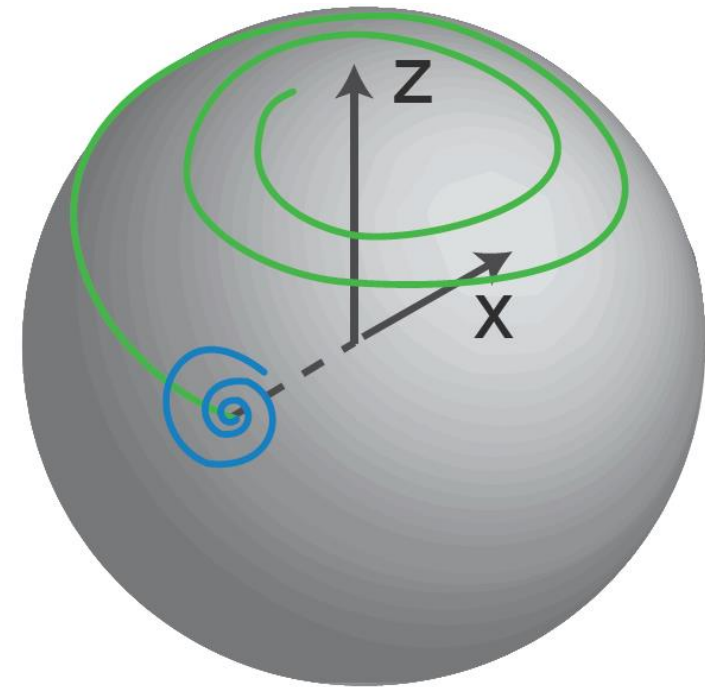
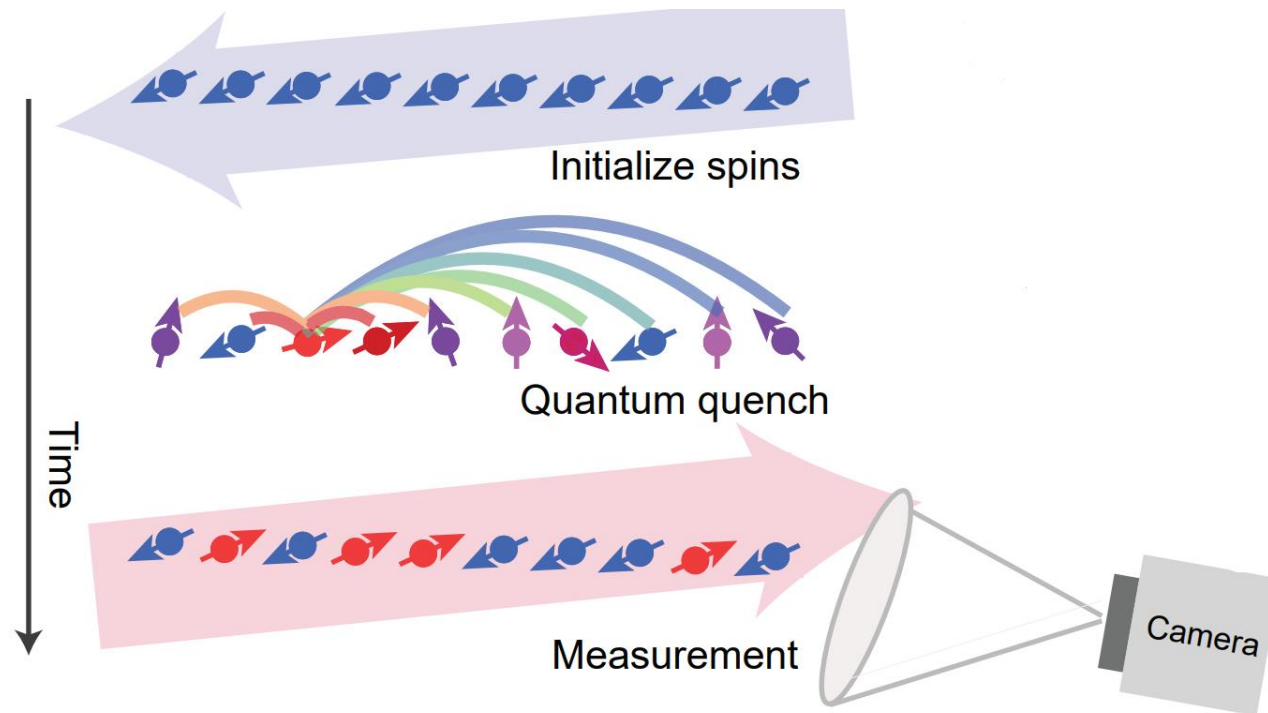
[3] B. Neyenhuis, *JZ et al.*, *Science Advances* **3**(8), e1700672 (2017)

[4] *JZ, et al.*, arXiv 1708.01044 (2017), *Nature*, in press

[5] *JZ et al.*, *Nature* **543**, 217–220 (2017)

# Dynamical phase transition

$$H = \sum_{i < j} J_{ij} \sigma_i^x \sigma_j^x + B \sum_i \sigma_i^z$$

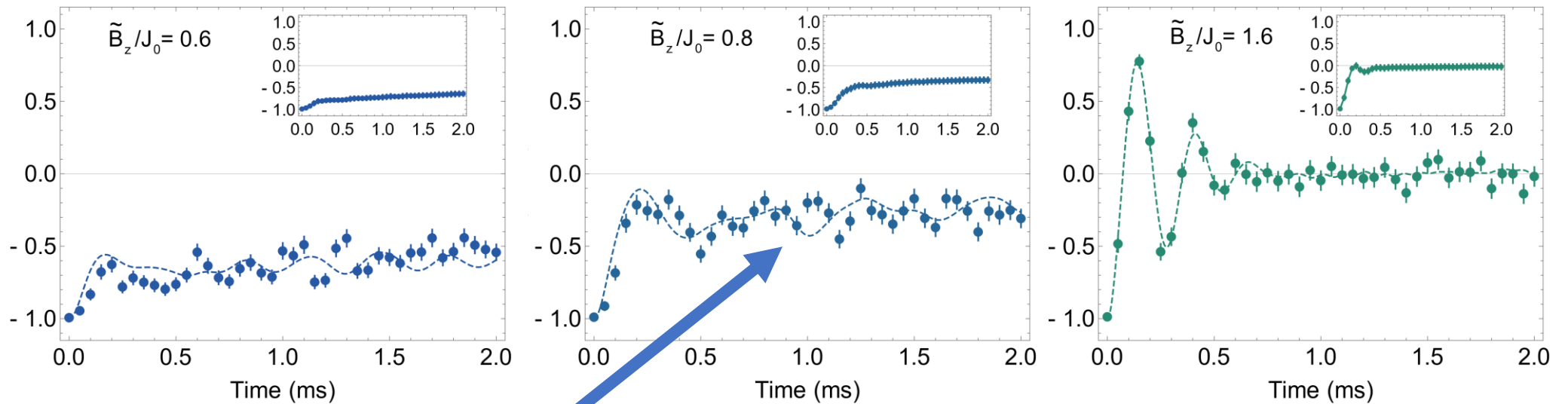


Evolution up to  $(2\pi J_0)t \sim 5$  for different transverse field strengths  
**(N=16 spins,  $\alpha \approx 0.8$ )**

$$H = \sum_{i<j} J_{ij} \sigma_i^x \sigma_j^x + B \sum_i \sigma_i^z$$

Average magnetization

$$\frac{1}{N} \sum_i \langle \sigma_i^x \rangle$$

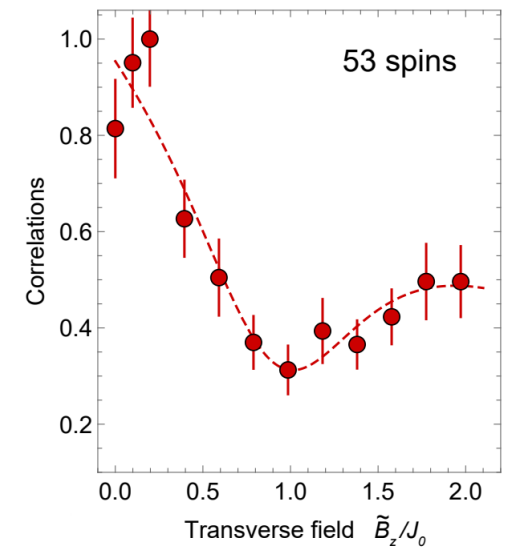
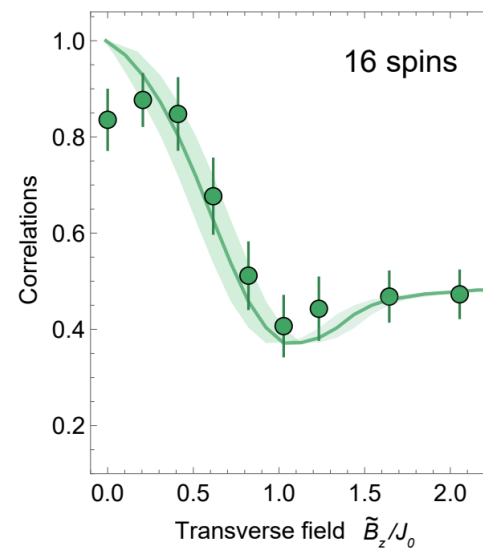
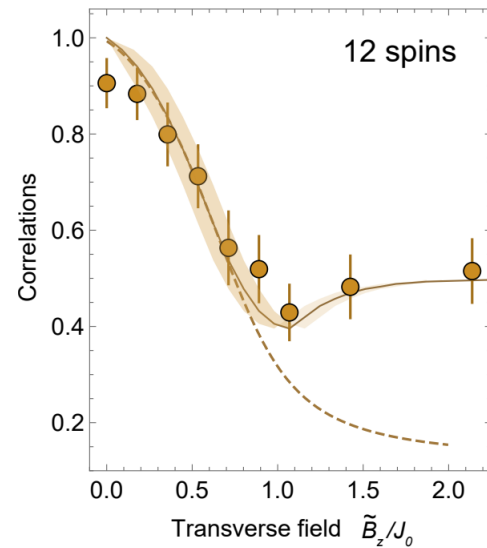
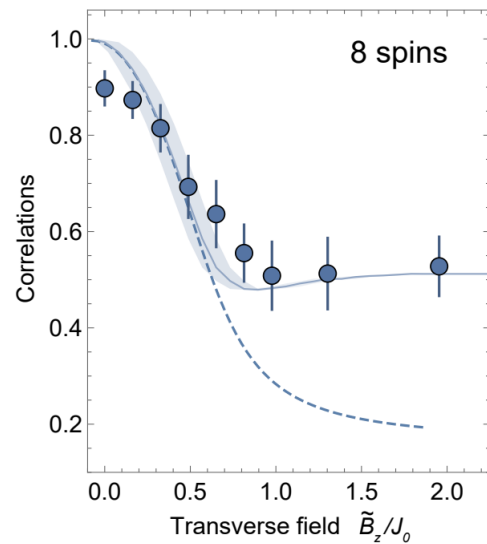


Plateau!



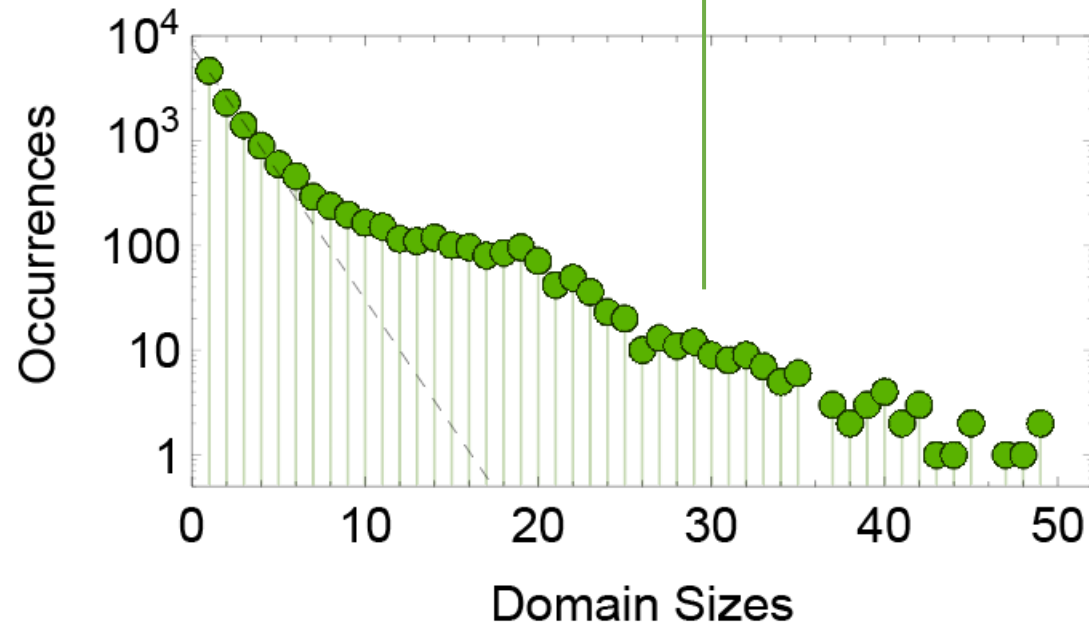
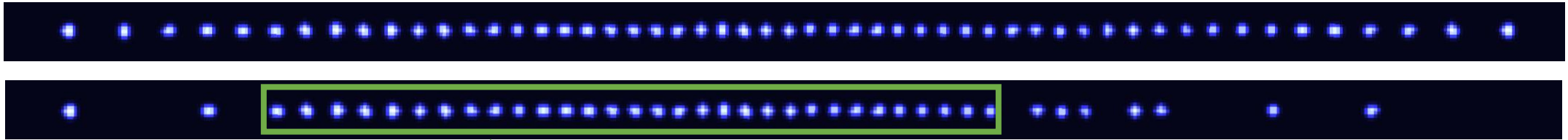
# Dynamical phase transitions:

Second order correlations  $\frac{1}{N^2} \sum_{i,j} \langle \sigma_i^x \sigma_j^x \rangle$



# Post-quench domain distributions.

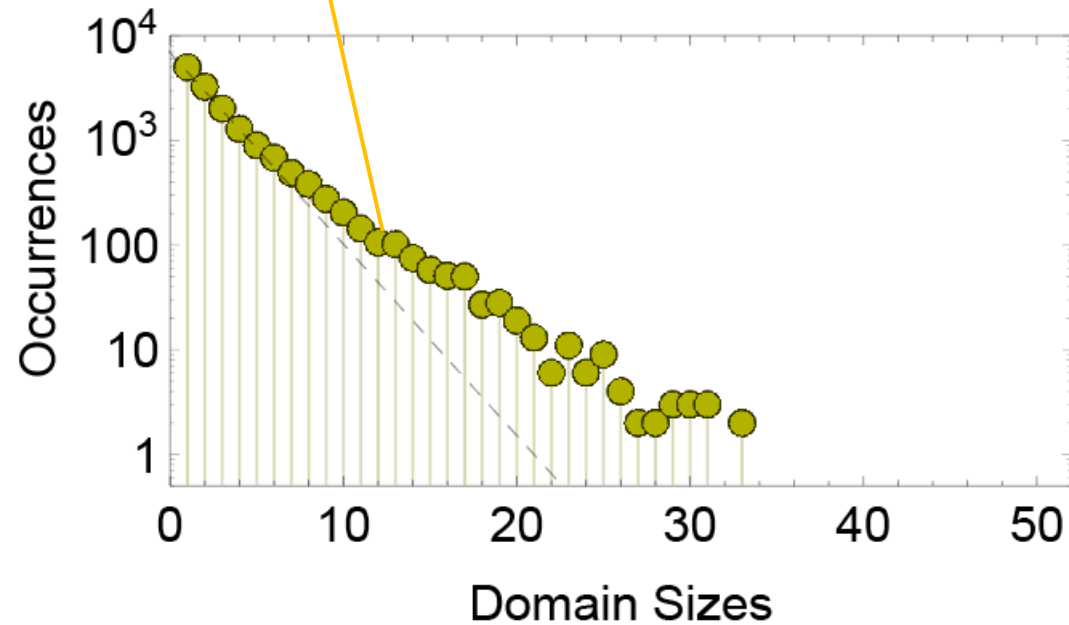
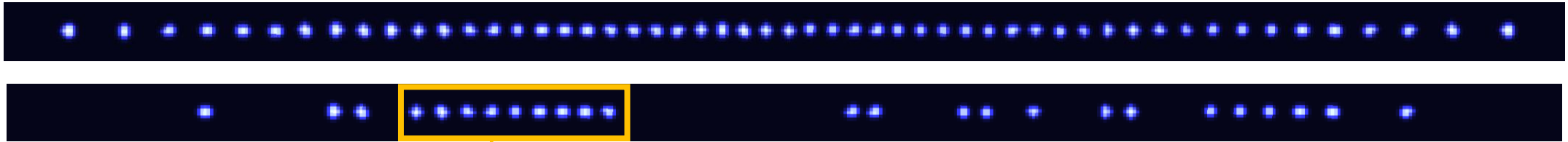
Initial state:



$$\tilde{B}_z/J_0 = 0.1$$

# Post-quench domain distributions.

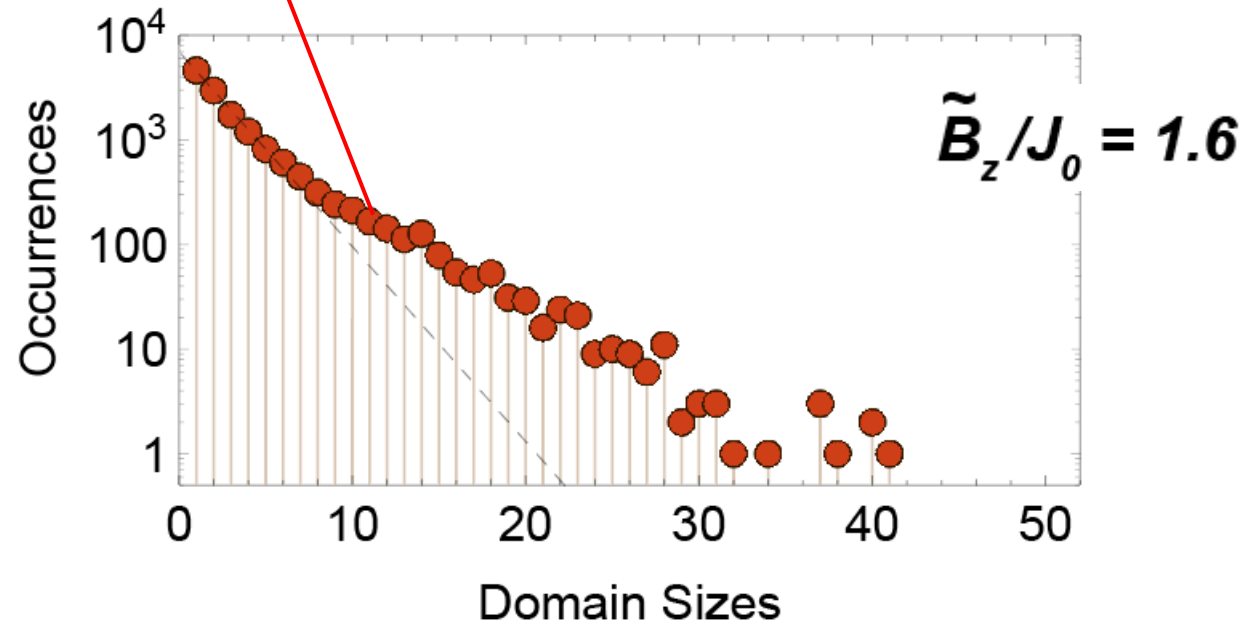
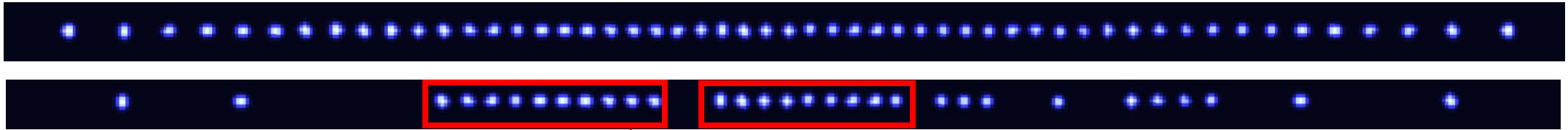
Initial state:



$$\tilde{B}_z/J_0 = 1.0$$

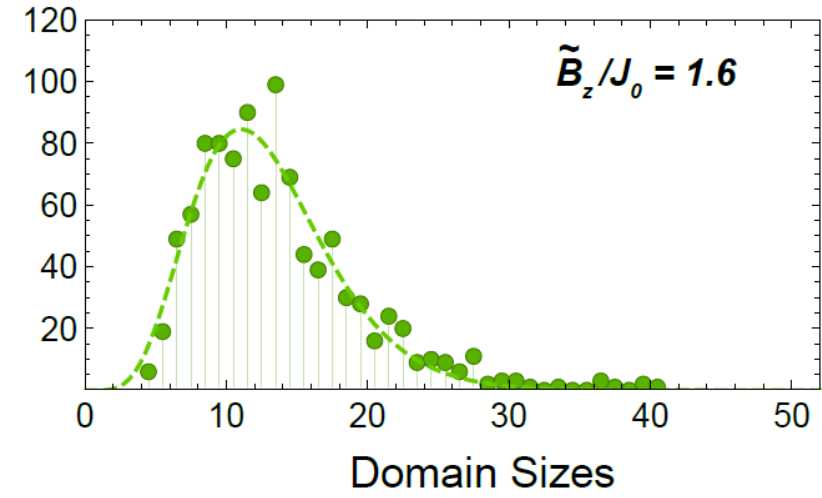
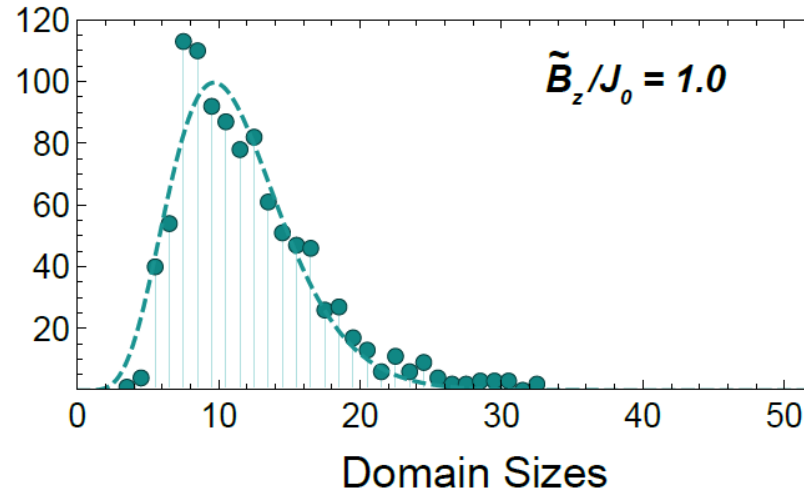
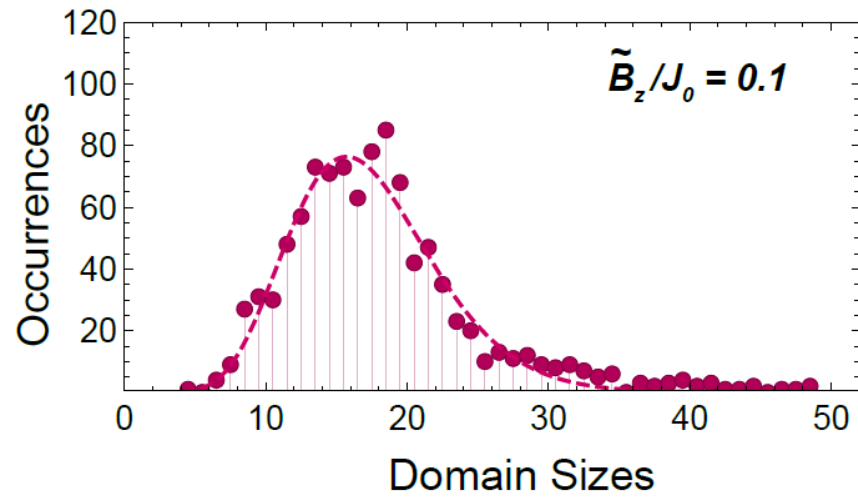
# Post-quench domain distributions.

Initial state:

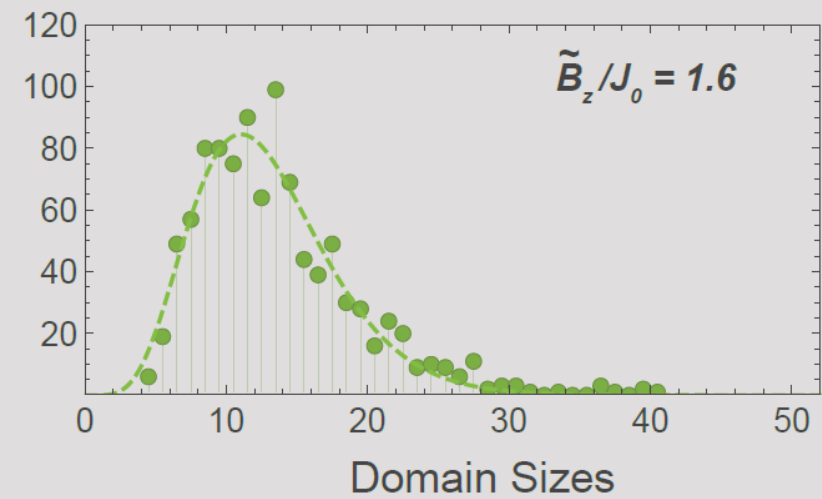
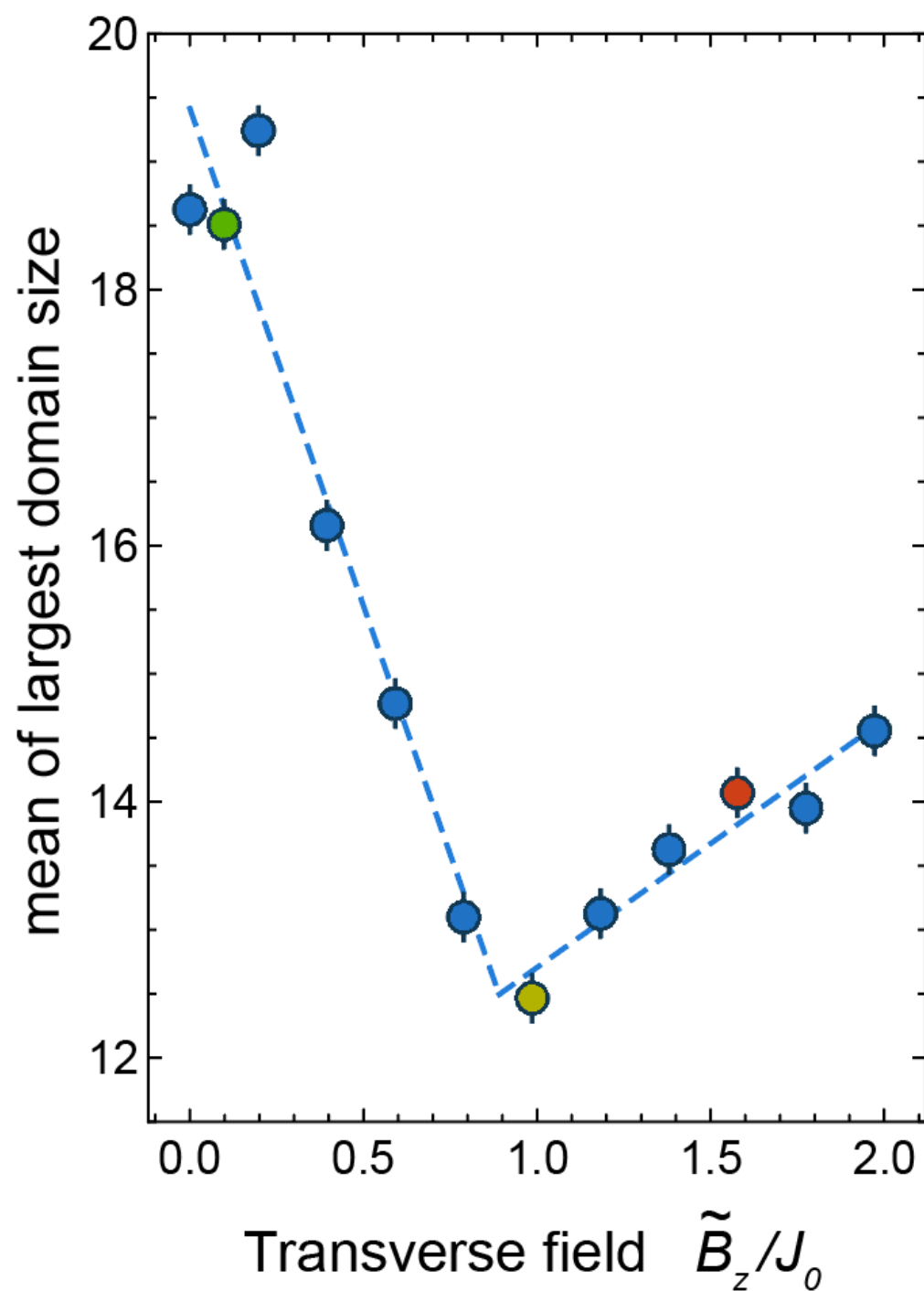
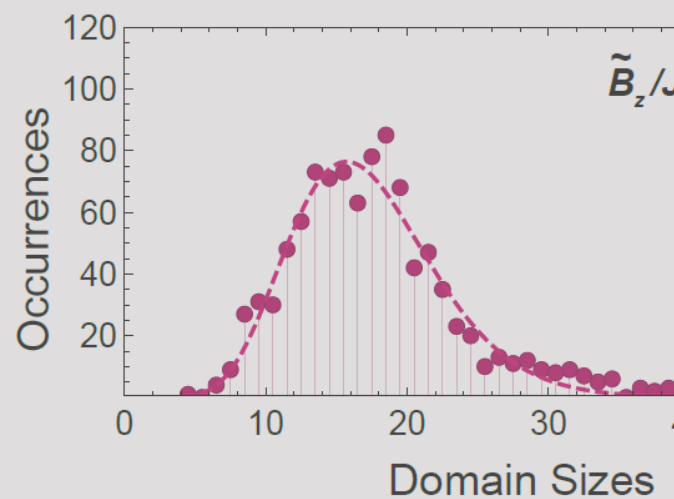




# Distribution of large domains



# Distribution

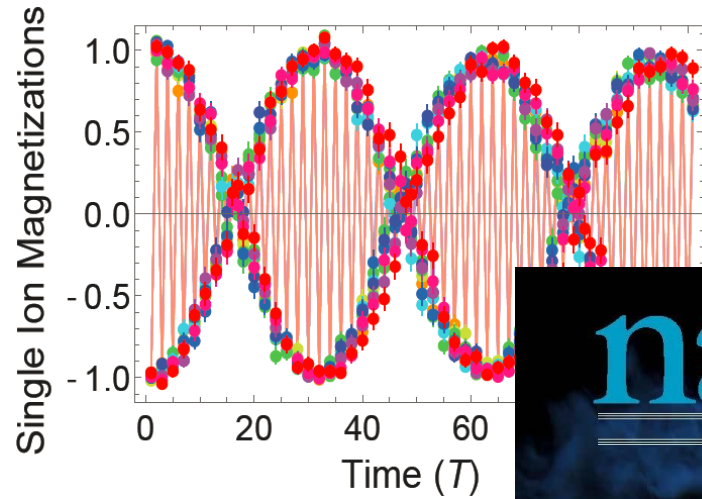


# Analog-digital mixed approach

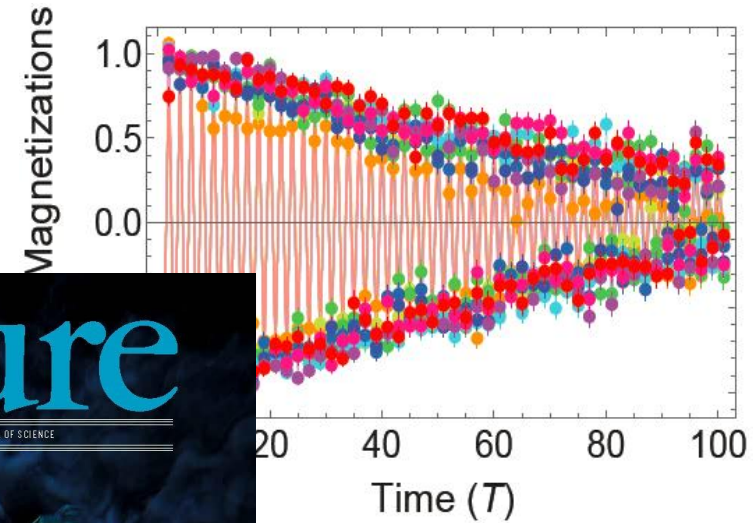
$$H = \begin{cases} H_1 = g(1 - \varepsilon) \sum_i \sigma_i^y, & \text{time } t_1 \\ H_2 = \sum_i J_{ij} \sigma_i^x \sigma_j^x, & \text{time } t_2 \\ H_3 = \sum_i D_i \sigma_i^x & \text{time } t_3 \end{cases}$$

# Analog-digital mixed approach

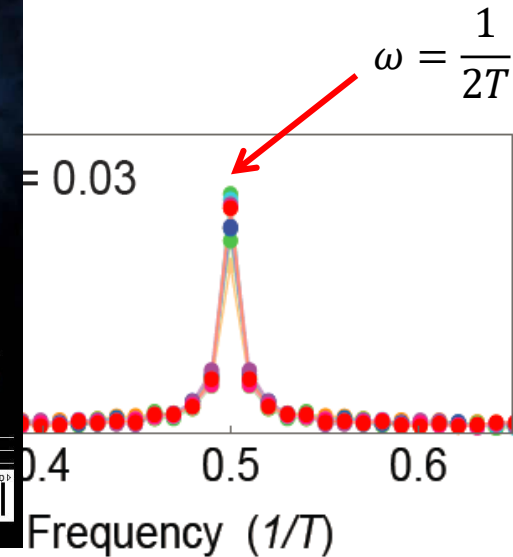
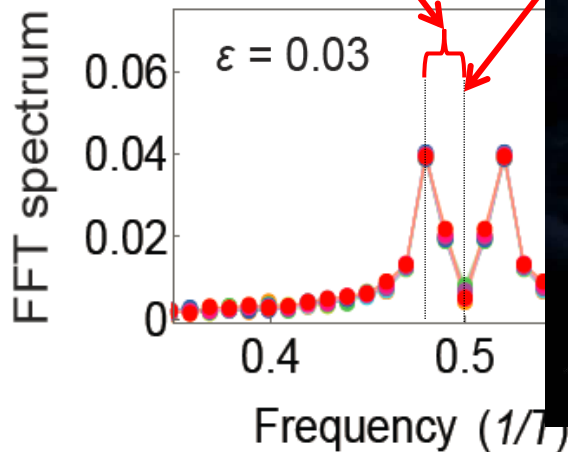
No Interactions ( $H_2$ ) or Disorder ( $H_3$ )



Many-body localization and interactions stabilizes time crystal



Fourier Peak Shifts by  $\epsilon$



- **Toolbox**

Quantum engineering with atomic ions

- **Non-equilibrium spin dynamics**

50+ qubit quantum simulator

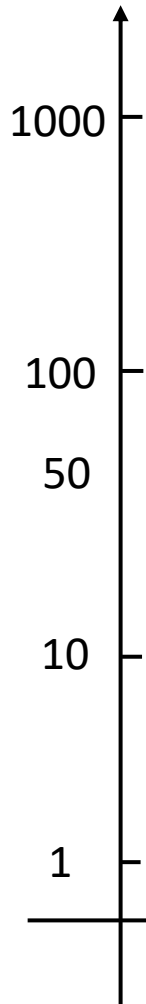
- **Outlook**

**Plenty of room at the bottom**



# Need both complexity and precision

# qubits



1000

100

50

10

1

90%

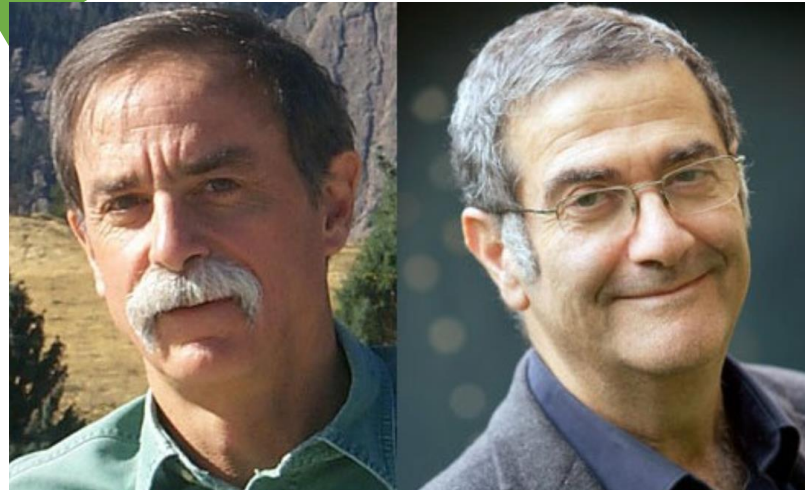
99%

99.9%

Entangling gate fidelity

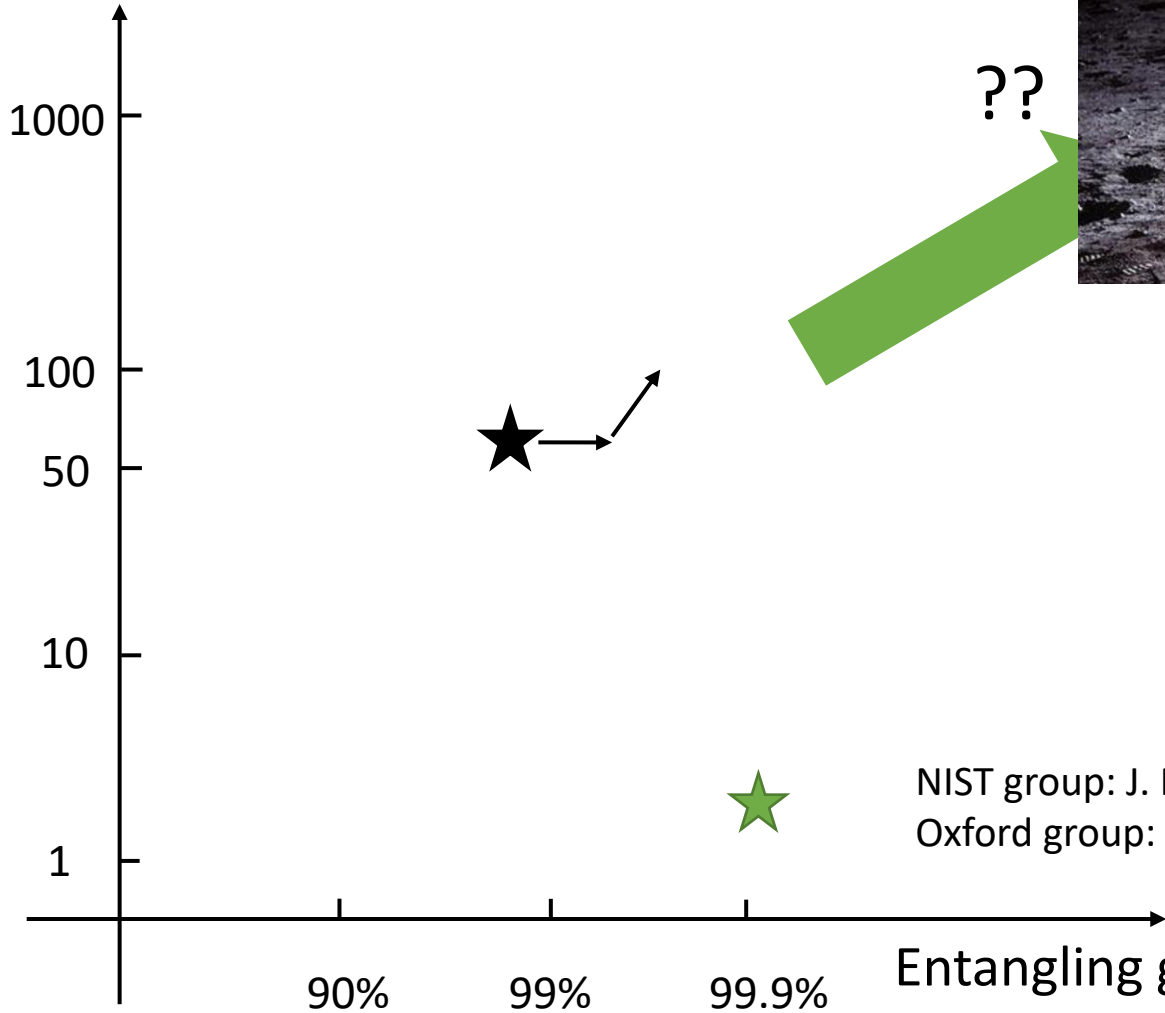


Nobel Prize 2012



# Need both complexity and precision

# qubits

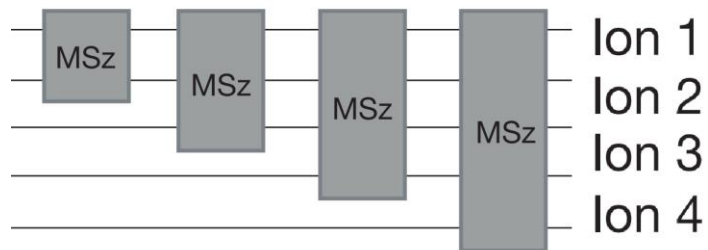
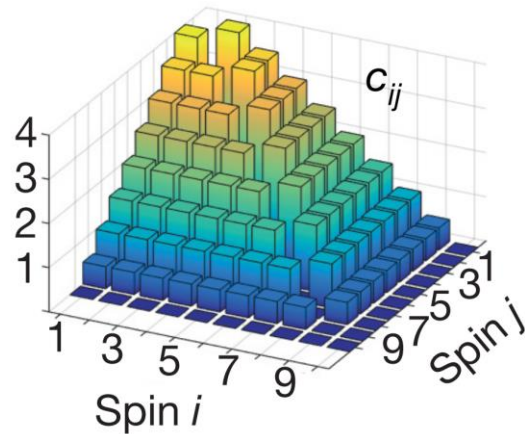


NIST group: J. P. Gaebler, *et al.*, Phys. Rev. Lett. **117**, 060505 (2016)  
Oxford group: C. J. Balance, *et al.*, Phys. Rev. Lett. **117**, 060504 (2016)

# How can we encode particle and nuclear physics?

Lattice gauge theories

Non-Abelian??



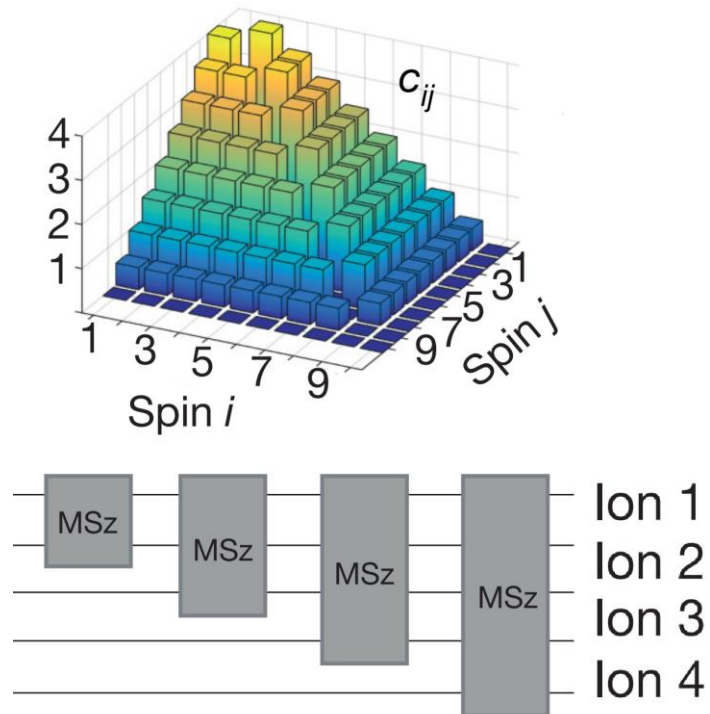
Blatt group: 1D QED

E. A. Martinez, et al., Nature **534**, 516 (2016)

# How can we encode particle and nuclear physics?

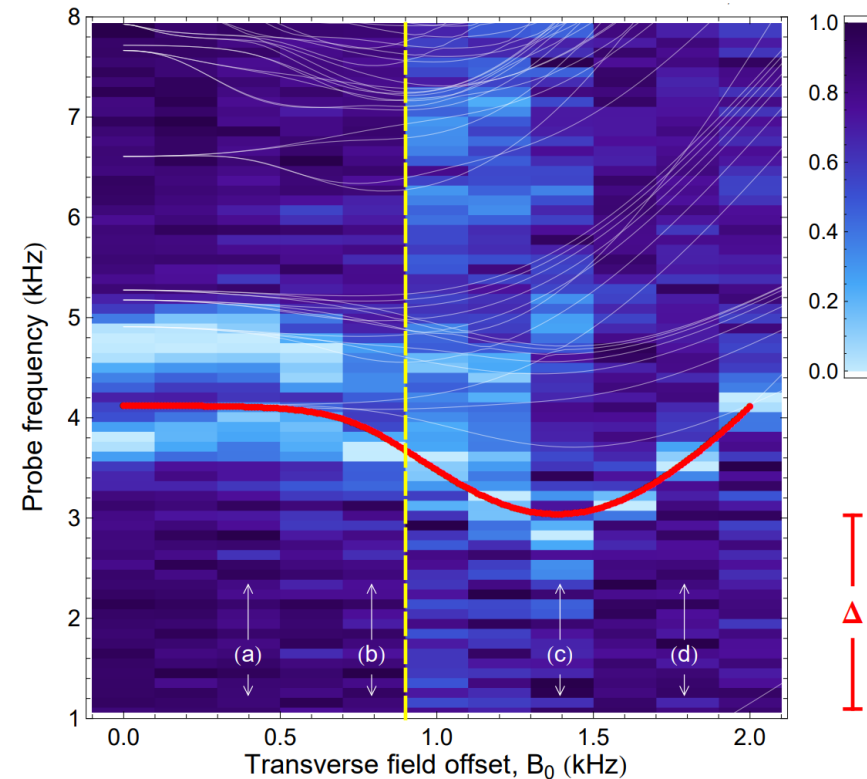
Lattice gauge theories

Non-Abelian??



Blatt group: 1D QED  
E. A. Martinez, et al., Nature **534**, 516 (2016)

Quantum advantage, sampling,  
connected to quantum chaos:  
Random matrix theory



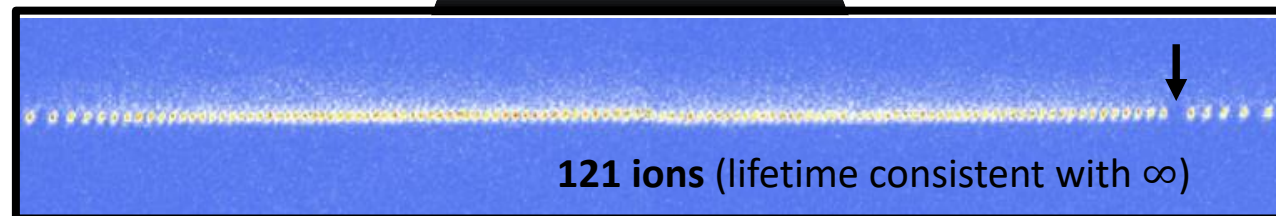
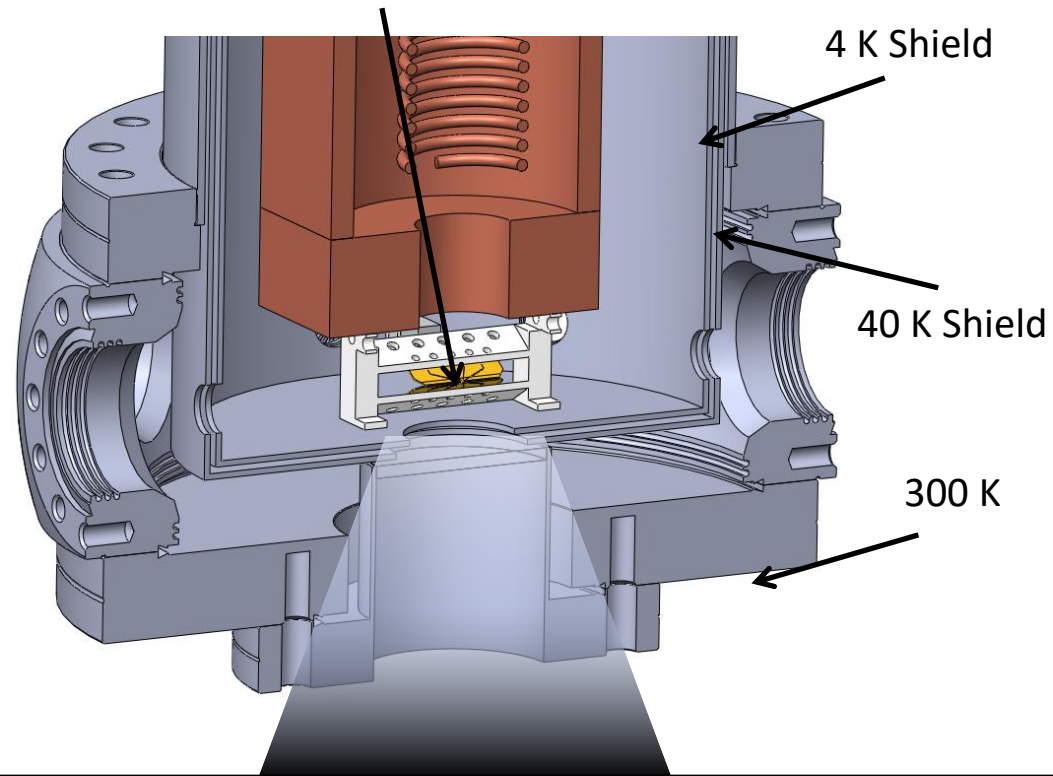
Many-body spectroscopy:  
C. Senko, et al., Science **345**, 430 (2014)

# Scaling Up: 4K to get lower pressure



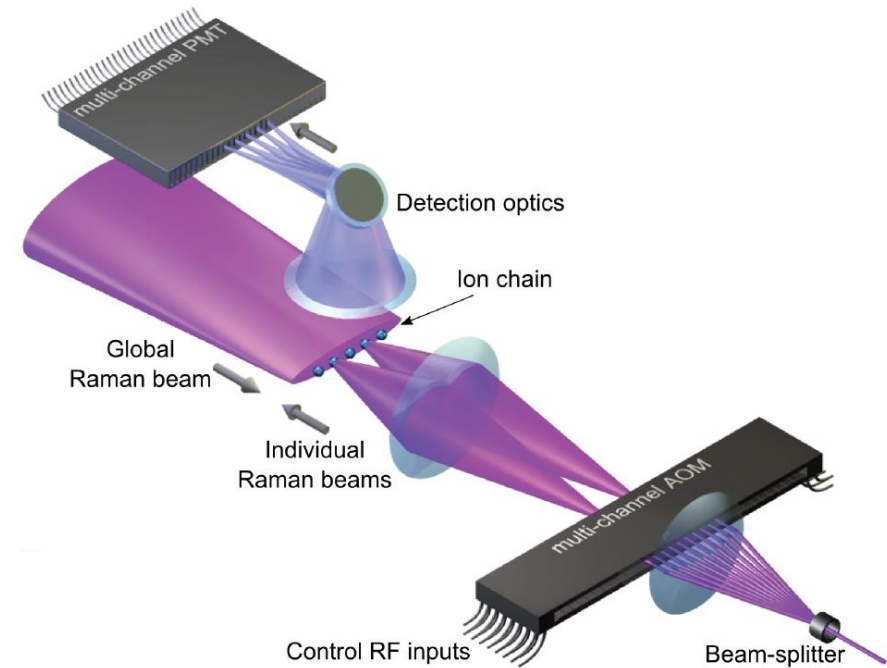
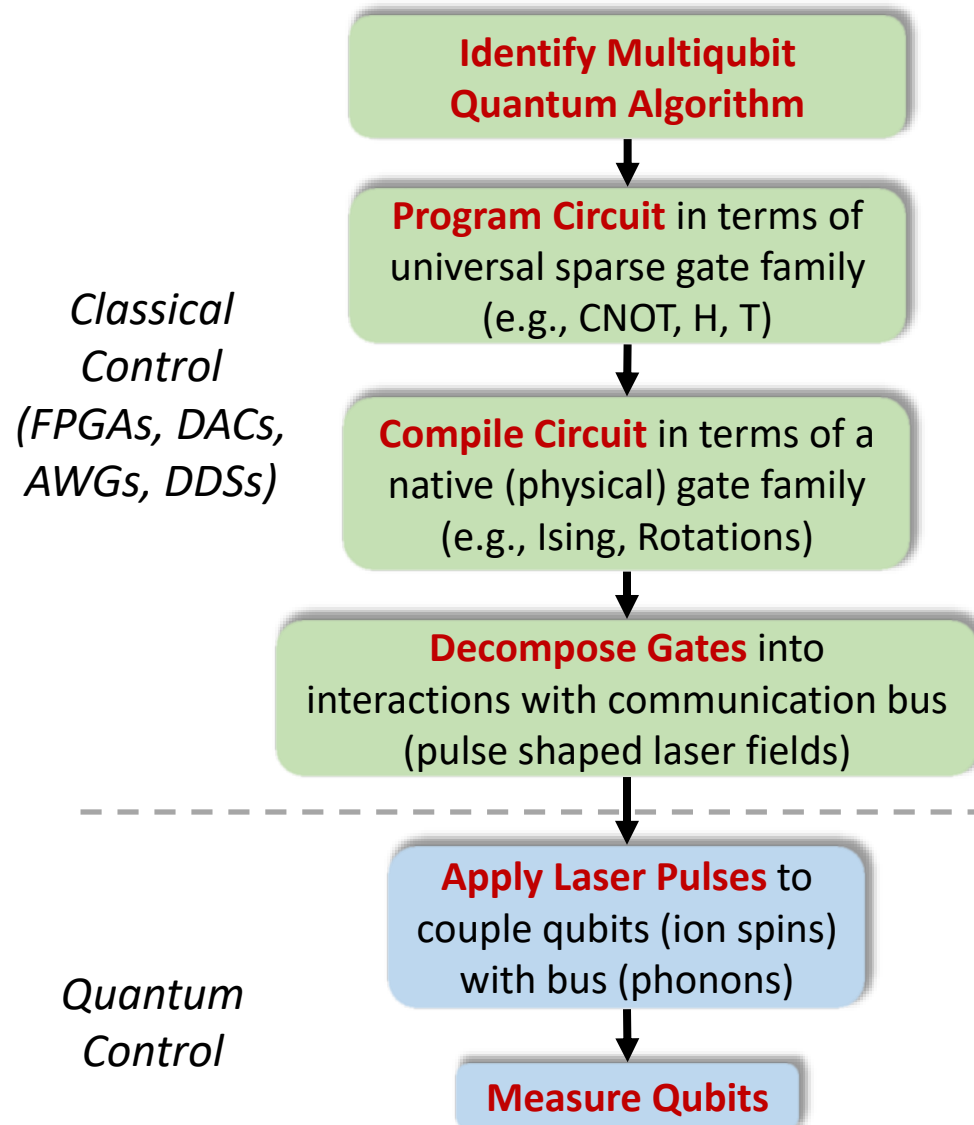
JANIS

5-segment linear rf ion trap  
(Au on  $\text{Al}_2\text{O}_3$  blades, 200mm)





# Qubit Control: Programmable/*Reconfigurable* Quantum Computer Module



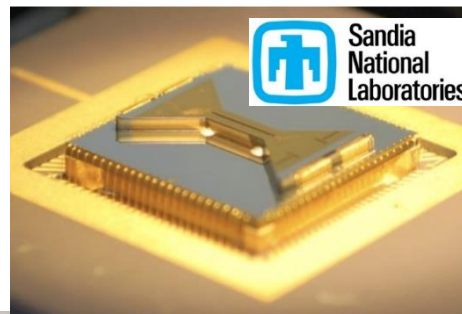
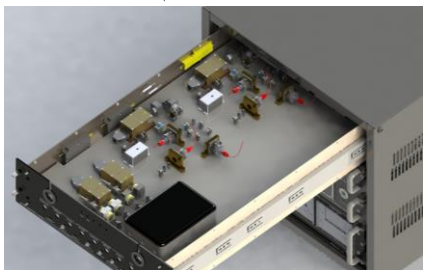
S. Debnath, *et al.*, Nature **536**, 63 (2016)  
N. Linke, *et al.*, PNAS **114**, 13 (2017)

# Engineering Meets Ion Traps

- Full control of up to 32 qubits
- Full connectivity/reconfigurability
- Dual species ( $^{171}\text{Yb}^+$ / $^{138}\text{Ba}^+$ )
- Room temperature chamber
- NA 0.6 optical access

*AO Sense* CW laser rack

- 6 wavelengths, all locked
- all modulators/switches
- fiber delivery



*AO Sense*

ColdQuanta

**HARRIS**

COHERENT



# Acknowledgements



## QSIM Team

PI: Chris Monroe

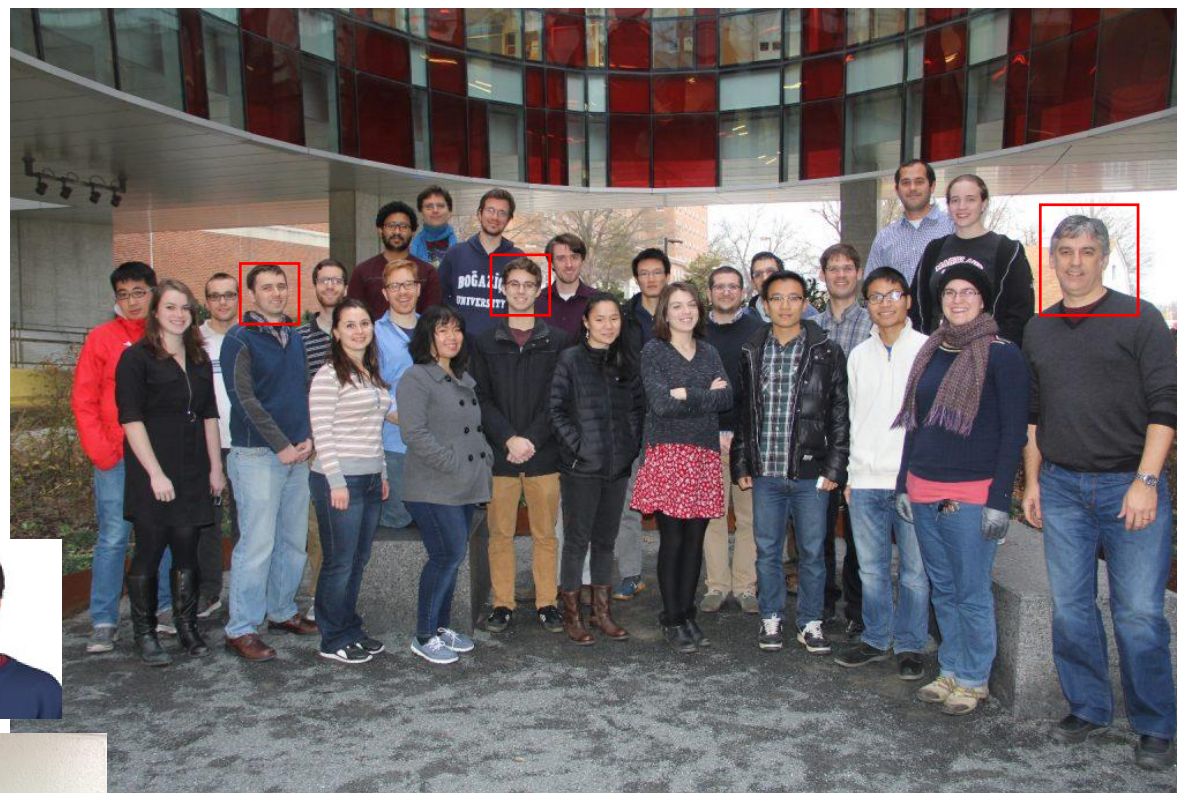
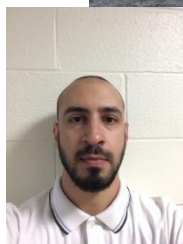
## Post-docs:

- Jiehang Zhang
- Paul Hess
- Guido Pagano



## Graduate Students:

- Antonis Kyprianidis
- Patrick Becker
- Harvey Kaplan
- Wen Lin Tan

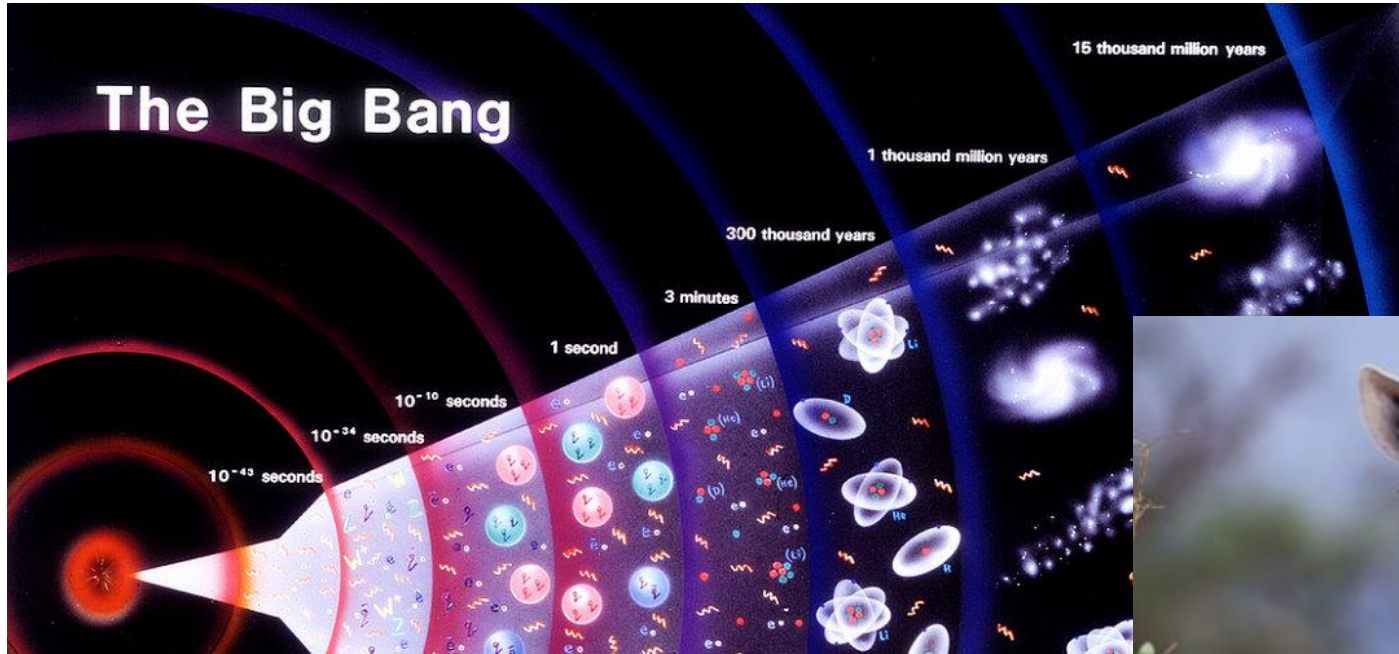


## Theory Collaborator:

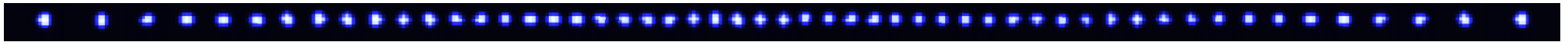
- Norman Yao
- Andrew Potter
- Ashvin Vishwanath
- Zhe-Xuan Gong
- Alexey Gorshkov



# Nature: the fastest quantum computer

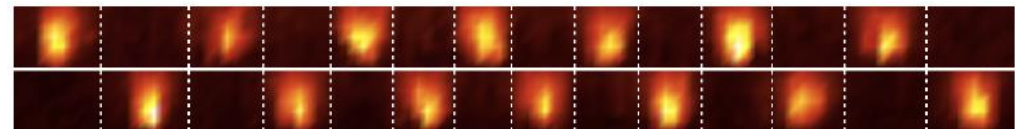


# Spin detection: High-resolution fluorescence imaging



- Ion positions are determined by illuminating the chain for less than 20 ms.
- State of *each spin* is then measured in 300  $\mu$ s detection time
- *All many-body correlations available in a single shot*

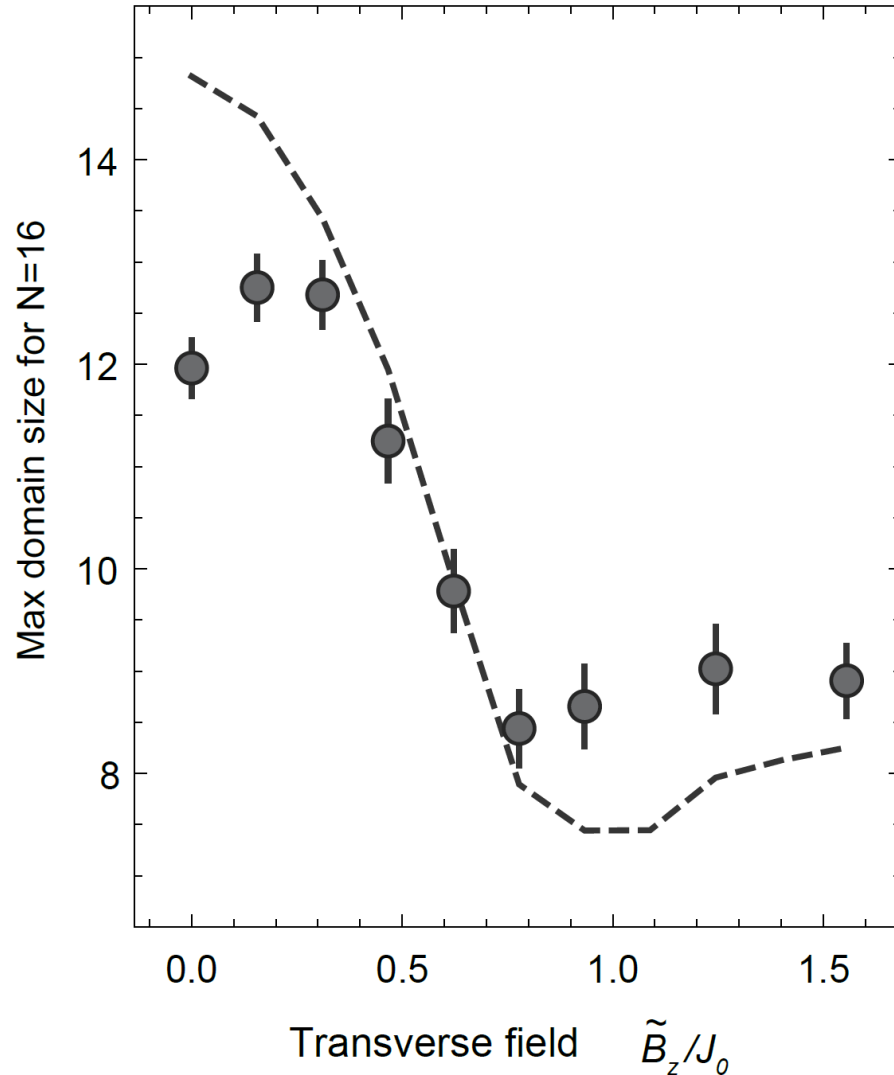
eg: AFM ordering of 14 spins



R. Islam, *et al.*, *Science* **340**, 583 (2013)

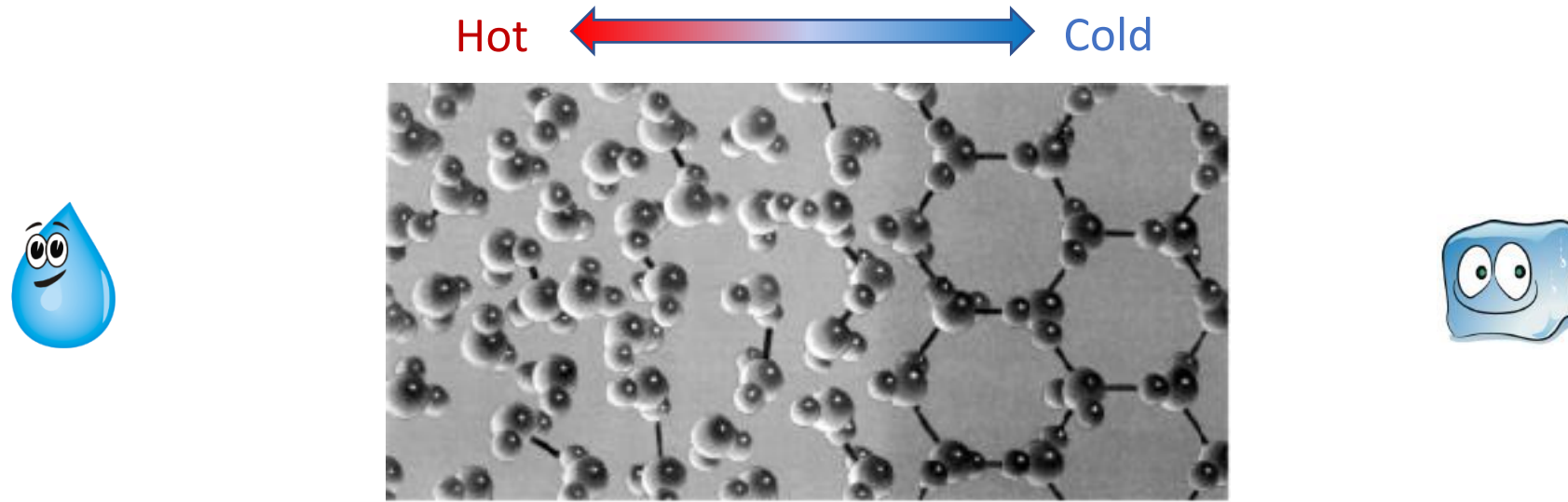


# Formation probabilities for 16 spins



K. Naja and M. A. Rajabpour, Phys. Rev. B 93, 125139 (2016).

# What are Time Crystals?



Time Translational Symmetry Breaking?

$$\hat{H} \quad \xrightarrow{?} \quad \langle \psi_0 | \hat{O} | \psi_0 \rangle = f(t)$$

Time independent

Time dependent

Wilczek (PRL 2012), Li *et al.*, (PRL 2012), Bruno (PRL 2013), Watanabe & Oshikawa (PRL 2015)

# Discrete Time Crystals

Periodically Driven (Floquet) Hamiltonian

$$\hat{H}(t) = \hat{H}(t + T) \quad \longrightarrow \quad \langle \hat{O}(t) \rangle = \langle \hat{O}(t + nT) \rangle$$

Khemani *et al.* (PRL 2016) ; Else, *et al.* (PRL 2016); N. Yao *et al.* (PRL 2016)  
von Keyserlingk, *et al.* (PRB 2016); Sacha PRA (2015)

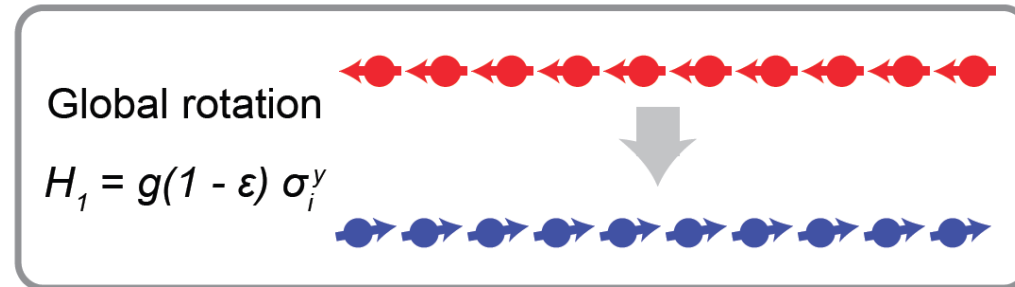
Requirements for Discrete Time Crystal definition:

- ✓ Periodic state dependence at sub-harmonic frequencies
- ✓ Robust to perturbations (no fine tuned parameters)
- ✓ Oscillations stabilized by many-body effects

Eliminates most  
“trivial” Discrete Time  
Crystals

# Spin chain Floquet evolution

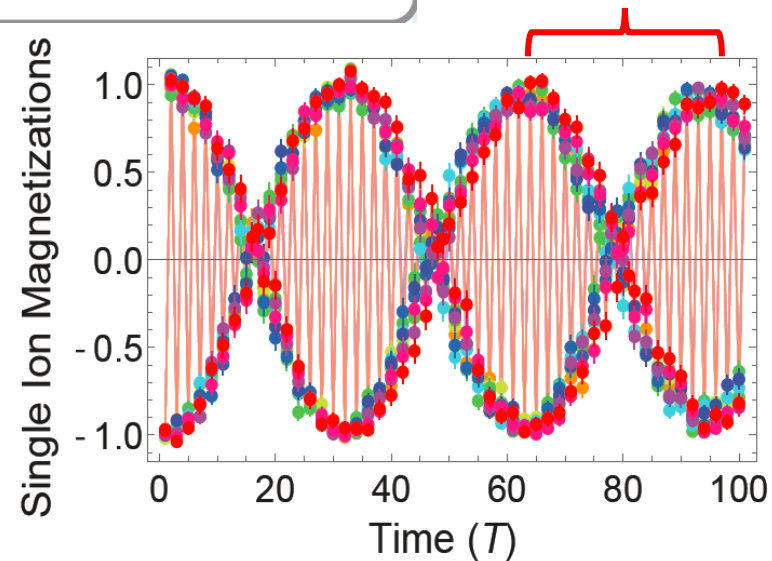
$$H = \begin{cases} H_1 = g(1 - \varepsilon) \sum_i \sigma_i^y, & \text{time } t_1 \\ H_2 = \sum_i J_{ij} \sigma_i^x \sigma_j^x, & \text{time } t_2 \\ H_3 = \sum_i D_i \sigma_i^x & \text{time } t_3 \end{cases}$$



Beatnote  
 Period  
 $1/\varepsilon$  (T)

Perturbed  
 $(1 - \varepsilon)\pi$  - pulses

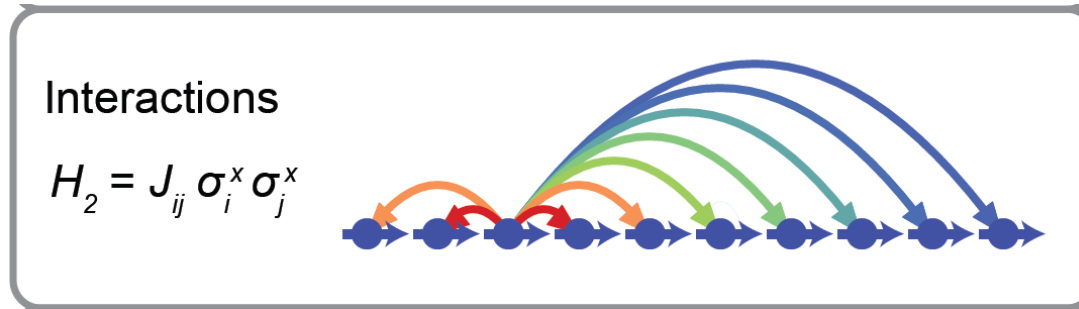
$$0 \leq \varepsilon \leq 15\%$$



J. Zhang *et al.*, Nature 543, 217-220 (2017).  
 See also work by M. Lukin group.

# Spin chain Floquet evolution

$$H = \begin{cases} H_1 = g(1 - \varepsilon) \sum_i \sigma_i^y, & \text{time } t_1 \\ H_2 = \sum_i J_{ij} \sigma_i^x \sigma_j^x, & \text{time } t_2 \\ H_3 = \sum_i D_i \sigma_i^x & \text{time } t_3 \end{cases}$$



$$J_{ij} \approx \frac{J_0}{|i - j|^\alpha}$$

$\alpha = 1.5$

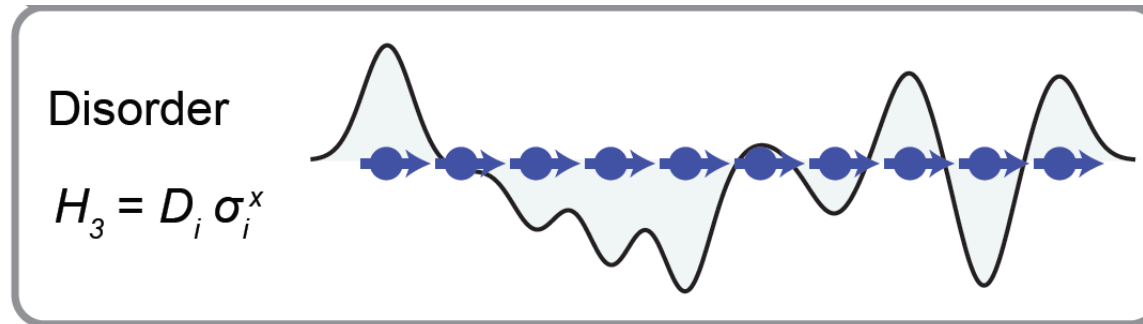
Interactions:

$$0.006 < J_0 t_2 < 0.04$$



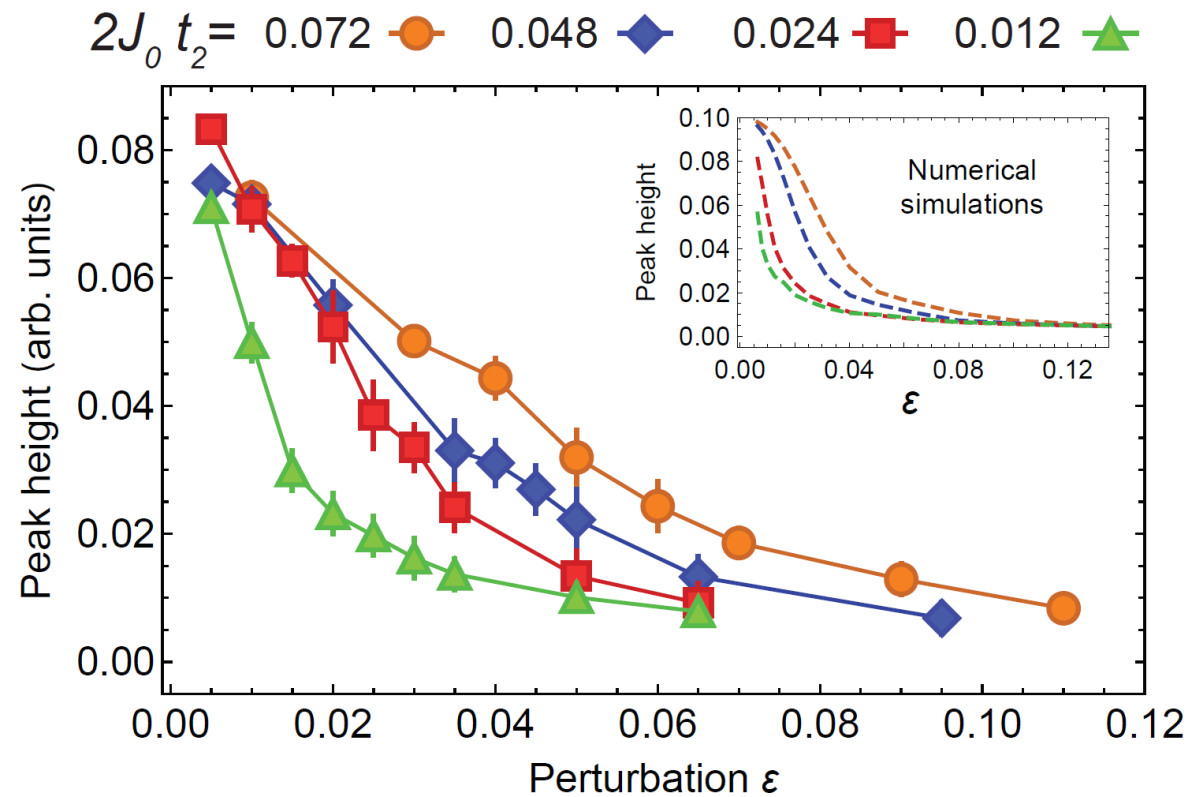
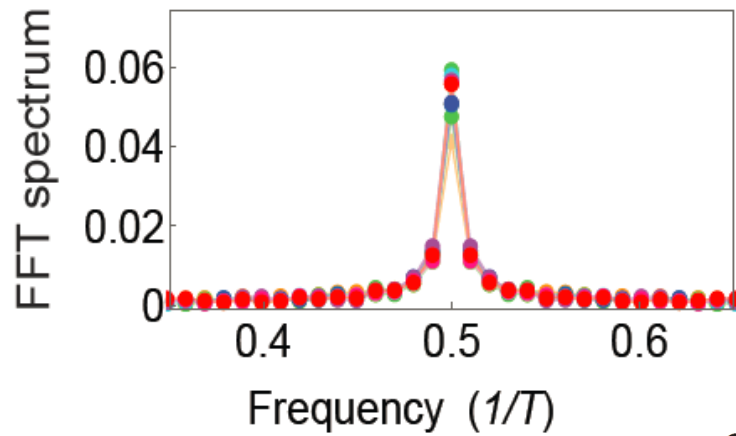
# Spin chain Floquet evolution

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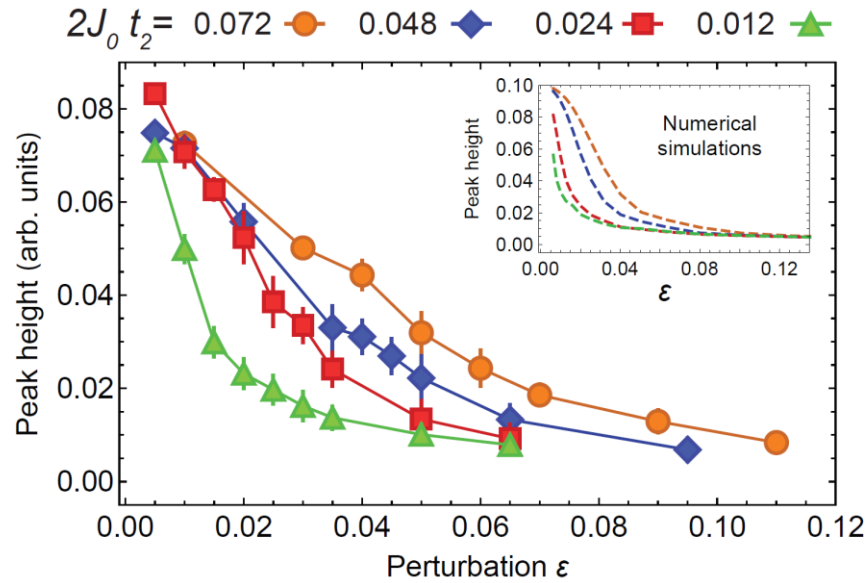


- Strong Disorder:  
 $D_i t_3 \in [0, \pi]$
- Localization prevents heating

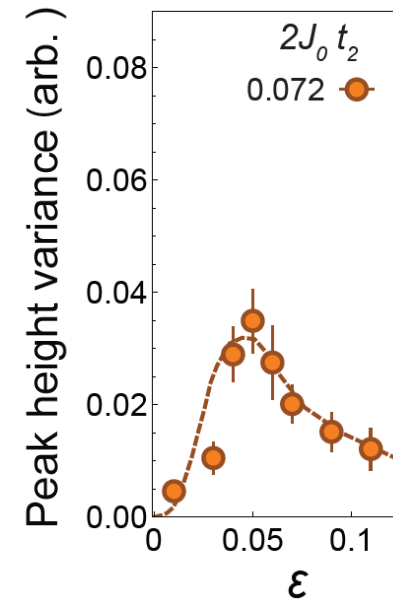
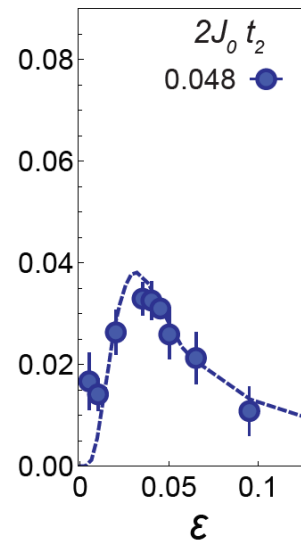
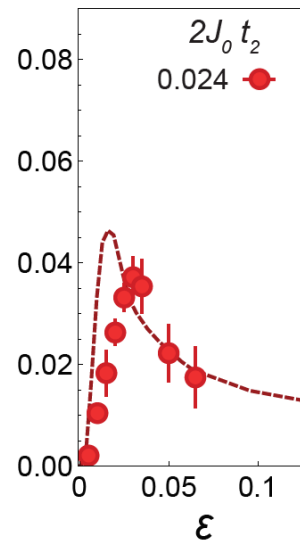
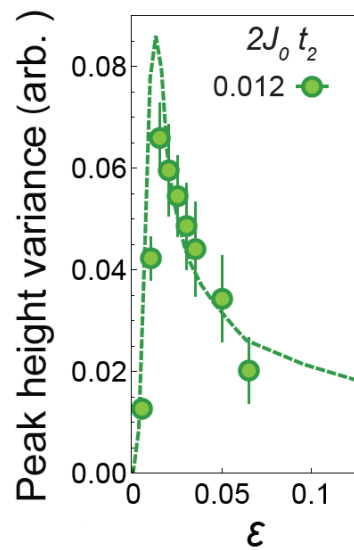
# Sub-harmonic peak heights: An order parameter



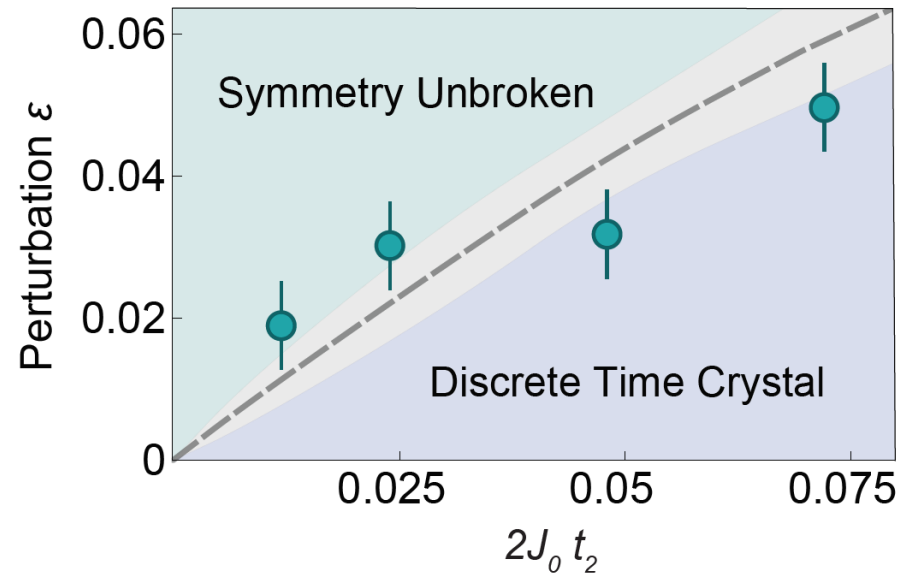
# Variance: signature of cross-over



Order parameter variance blows up at phase boundary



# “Phase diagram” and other signatures

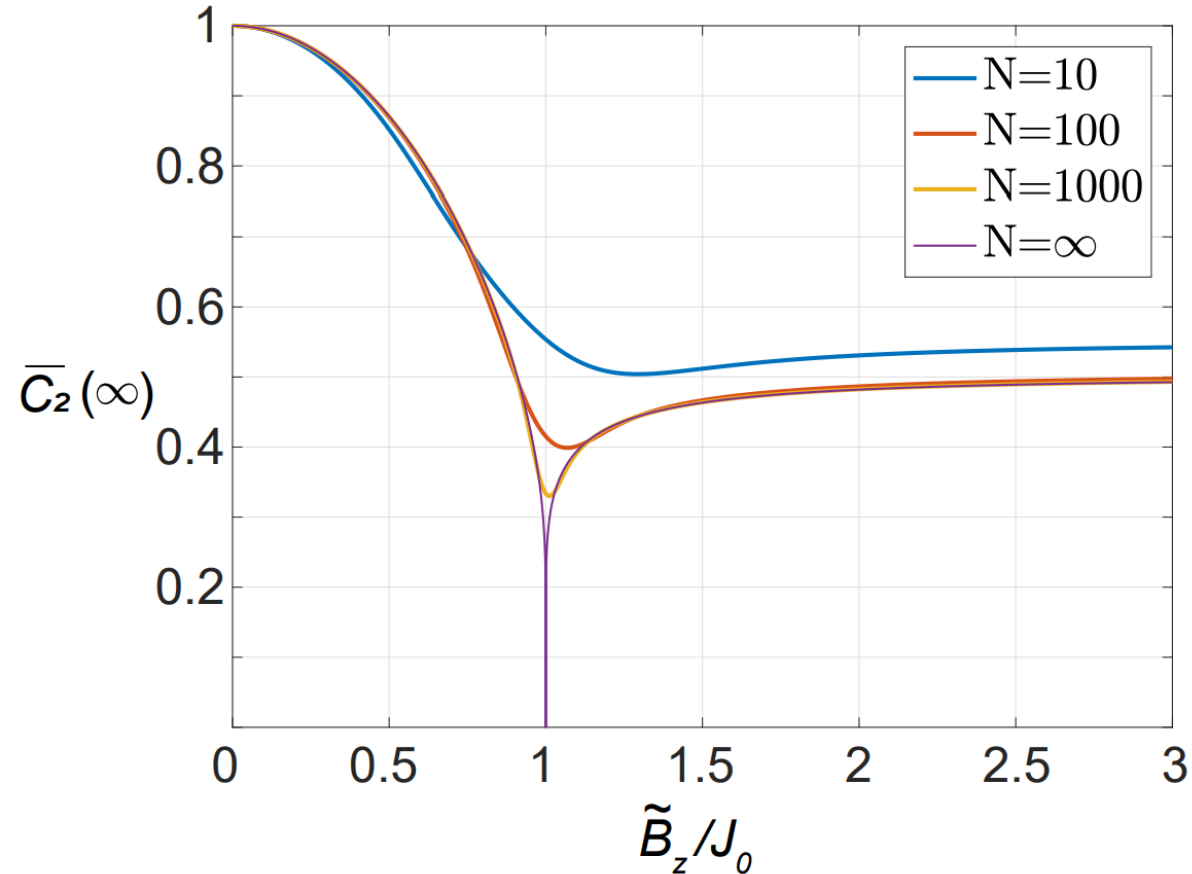


We've also checked:

- Finite-size scaling
- Different initial states
- Disorder vs clean systems (more to come)

- Highest variance correspond to the phase transition points, which is rounded into a cross-over with finite size systems
- Agrees well with numerical simulations (dashed line)

# Theory at the all-to-all limit ( $\alpha = 0$ )



- Special point where a permutation symmetry exist, i.e. all spins are interchangeable.
- Phase transition manifested in logarithmic “dip” in the second order correlation.
- $\alpha \neq 0$  remains an open question.



Possible connections to sampling experiments