

# Estimating saturation effects for dijet production in UPC

Piotr Kotko

Penn State University

based on:

P.K., K. Kutak, S. Sapeta,  
A. Stasto, M. Strikman, [arXiv:1702.03063](https://arxiv.org/abs/1702.03063)

A. van Hameren, P.K., K. Kutak,  
C. Marquet, E. Petreska, S. Sapeta,  
[JHEP 1612 \(2016\) 034](#), [JHEP 1509 \(2015\) 106](#)

supported by:  
DEC-2011/01/B/ST2/03643  
DE-FG02-93ER40771

# Motivation

## Why dijets in UPC?

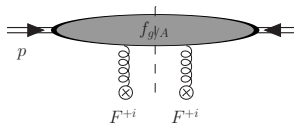
- $\gamma A \rightarrow 2 \text{ jets}$  is sensitive to the **Weizsacker-Williams (WW)** unintegrated gluon distribution (UGD), whereas other processes like  $J/\psi$  or inclusive jets are sensitive to the **dipole UGD**
- $pA \rightarrow 2 \text{ jets}$  is sensitive to both UGDs (directly to the dipole UGD and indirectly to WW)
- Dipole UGD for proton is relatively well constrained from HERA; this not the case for the WW UGD
- **Goal:** calculate nuclear modification ratios and see how much saturation one gets for dijets in UPC for the current LHC setup

# Plan

- 1 Introduction
  - nonuniversality of TMD gluon distributions
  - two basic TMDs
  - TMD 'factorization' and relation to Color Glass Condensate (CGC) (for  $pA \rightarrow 2$  jets to see the complications)
- 2 Saturation approach for hard dijets in  $pA$  and  $\gamma A$
- 3 Results for dijets in UPC
- 4 Summary

# Gluon distributions

Operator definition of collinear gluon distribution



$$f_{g/H}(x) = \int \frac{dz^-}{2\pi p^+} e^{-ixp^+ z^-} \langle p | \text{Tr} \{ F^{+i}(0, \vec{0}_T, z^-) U(z^-, 0; \vec{0}_T) F^{+i}(0) \} | p \rangle$$

$F^{+i}(x) = F_a^{+i}(x) t^a$  – gluon strength tensor in fundamental representation

$U(z^-, 0; \vec{0}_T) = \mathcal{P} \exp \left[ ig \int_0^{z^-} dy^- A_a^+(0, \vec{0}_T, y^-) t^a \right]$  – the Wilson line

# Gluon distributions

Transverse momentum dependent (TMD) gluon distributions

The position of one of the gluon operators is off the light-cone:

$$\mathcal{F}_{g;C_1,C_2}(x, k_T) = \int \frac{d\xi^- d^2\xi}{(2\pi)^3 p^+} e^{ixp^+ \xi^- - i\vec{k}_T \cdot \vec{\xi}_T} \langle p | \text{Tr} \left\{ F^{+i}(0, \xi_T, \xi^-) [\xi, 0]_{C_1} F^{+i}(0) [0, \xi]_{C_2} \right\} | p \rangle$$

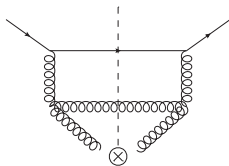
where  $[\xi, 0]_{C_i}$  are again Wilson lines which lie along some paths  $C_1$  and  $C_2$ .

The structure of Wilson lines depends on the particular hard process attached to the gluon distribution, more precisely its color structure.

# Gluon distributions

Example: TMD distribution for a particular subprocess in  $HH \rightarrow 2\text{jets}$

[C.J. Bomhof, P.J. Mulders, F. Pijlman, Eur.Phys.J.C. 47, 147 (2006)]



$$\mathcal{F}_{g;C_1,C_2} \sim \langle p | \text{Tr} \{ F^{+i}(\xi) \mathcal{U}^{[+] \dagger} F^{+i}(0) \left[ \frac{\text{Tr} \mathcal{U}^{[\square] \dagger}}{N_c} \mathcal{U}^{[+]} + \mathcal{U}^{[-]} \right] \} | p \rangle$$

where the Wilson lines (and loops) are defined as

$$\mathcal{U}^{[\pm]} = U(0, \pm\infty; 0_T) U_T(\pm\infty; 0_T, \xi_T) U(\pm\infty, \xi^-; \xi_T)$$

$$\mathcal{U}^{[\square]} = \mathcal{U}^{[+]} \mathcal{U}^{[-] \dagger} = \mathcal{U}^{[-]} \mathcal{U}^{[+] \dagger}$$

# Gluon distributions

Two most basic TMD distributions:

- 1  $\mathcal{F}_{g;++} \sim \langle p | \text{Tr} \{ F(\xi) \mathcal{U}^{[+] \dagger} F(0) \mathcal{U}^{[+]} \} | p \rangle$
- 2  $\mathcal{F}_{g;-+} \sim \langle p | \text{Tr} \{ F(\xi) \mathcal{U}^{[-] \dagger} F(0) \mathcal{U}^{[+]} \} | p \rangle$

It is possible to choose a gauge to eliminate Wilson lines in **1** so that it has an interpretation as a gluon number density.

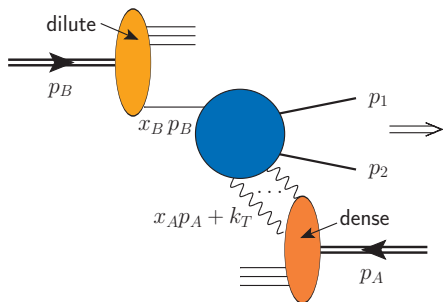
This is not possible for the distribution function **2**.

**Remark 1:** TMD gluon distributions are defined at leading power ('leading twist').

**Remark 2:** TMD gluon distributions are valid at any  $x$ .

⇒ there is a relation to Weizsacker-Williams (WW)  $xG_1$  and 'dipole'  $xG_2$  gluon distributions known at small  $x$ .

# Forward dijets in $pA$ collisions within CGC



forward dijets with transverse momentum imbalance:

$$|\vec{p}_{T1} + \vec{p}_{T2}| = |\vec{k}_T| = k_T$$

asymmetric kinematics:

$$x_B \gg x_A$$

Hybrid approach:

- large- $x$  parton in hadron  $B$  is treated as 'collinear' with standard PDFs
- small- $x$  partons within hadron  $A$  have internal transverse momentum  $k_T$

Three-scale problem (typically in CGC  $Q_s \sim k_T \sim P_T$ )

- 1 hard scale  $P_T$  (of the order of the average transverse momentum of jets)
- 2 transverse momentum imbalance  $k_T$
- 3 saturation scale  $\Lambda_{\text{QCD}} \ll Q_s$  (increasing with energy)



# Forward dijets in $pA$ collisions within CGC

Example:  $qA \rightarrow qg$  channel

[C. Marquet, Nucl. Phys. A 796 (2007) 41]

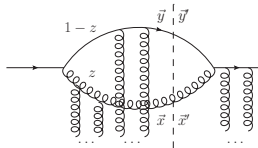
$$\frac{d\sigma_{qA \rightarrow 2j}}{d^3p_1 d^3p_2} \sim \int \frac{d^2x}{(2\pi)^2} \frac{d^2x'}{(2\pi)^2} \frac{d^2y}{(2\pi)^2} \frac{d^2y'}{(2\pi)^2} e^{-i\vec{p}_{T1} \cdot (\vec{x}_T - \vec{x}'_T)} e^{-i\vec{p}_{T2} \cdot (\vec{y}_T - \vec{y}'_T)} \psi_z^*(\vec{x}'_T - \vec{y}'_T) \psi_z(\vec{x}_T - \vec{y}_T) \left\{ S_{x_g}^{(6)}(\vec{y}_T, \vec{x}_T, \vec{y}'_T, \vec{x}'_T) - S_{x_g}^{(3)}(\vec{y}_T, \vec{x}_T, (1-z)\vec{y}'_T + z\vec{x}'_T) - S_{x_g}^{(3)}((1-z)\vec{y}_T + z\vec{x}_T, \vec{y}'_T, \vec{x}'_T) - S_{x_g}^{(2)}((1-z)\vec{y}_T + z\vec{x}_T, (1-z)\vec{y}'_T + z\vec{x}'_T) \right\}$$

$\psi_z(\vec{x}_T)$  – quark wave function

$S_{x_g}^{(i)}$  – correlators of Wilson line operators, e.g.

$$S_{x_g}^{(2)}(\vec{y}_T, \vec{x}_T) = \frac{1}{N_c} \langle \text{Tr} [U(\vec{y}_T) U^\dagger(\vec{x}_T)] \rangle_{x_g}$$

$$S_{x_g}^{(3)}(\vec{z}_T, \vec{y}_T, \vec{x}_T) = \frac{1}{2C_F N_c} \langle \text{Tr} [U(\vec{z}_T) U^\dagger(\vec{y}_T)] \text{Tr} [U(\vec{y}_T) U^\dagger(\vec{x}_T)] \rangle_{x_g} - S_{x_g}^{(2)}(\vec{z}_T, \vec{x}_T) \text{ etc.}$$



where  $U(\vec{x}_T) = U(-\infty, +\infty; \vec{x}_T)$  and  $\langle \dots \rangle_{x_g}$  denotes the average over color sources.

# CGC vs TMD

## Leading power limit of CGC vs small $x$ TMD factorization

[F. Dominguez, C. Marquet, B-W. Xiao, F. Yuan Phys.Rev. D 83 (2011) 105005]

- Take the limit  $k_T \sim Q_s \ll P_T$  of CGC expressions (back-to-back dijets)
- Replace the color averages by the hadronic ME:  $\langle \dots \rangle_{x_g} \rightarrow \langle p | \dots | p \rangle / \langle p | p \rangle$

$$\frac{d\sigma_{AB \rightarrow 2j}}{dy_1 d^2 p_{T1} dy_2 d^2 p_{T2}} \sim \sum_{a,c,d} f_{a/B}(x_B, P_T^2) \sum_i \mathcal{F}_{ag}^{(i)}(x_A, k_T^2) H_{ag \rightarrow cd}^{(i)}$$

$H^{(i)}$  – hard **on-shell** factors

$\mathcal{F}_{ag}^{(i)}$  – TMD gluon distributions:

$$\mathcal{F}_{qg}^{(1)} \sim \langle p_A | \text{Tr} \{ F^{+i}(\xi) \mathcal{U}^{[-]\dagger} F^{+i}(0) \mathcal{U}^{[+]} \} | p_A \rangle, \quad \mathcal{F}_{qg}^{(2)} \sim \langle p_A | \text{Tr} \{ F^{+i}(\xi) \frac{\text{Tr} \mathcal{U}^{[\square]}}{N_c} \mathcal{U}^{[+]\dagger} F^{+i}(0) \mathcal{U}^{[+]} \} | p_A \rangle,$$

$$\mathcal{F}_{gg}^{(1)} \sim \langle p_A | \text{Tr} \{ F^{+i}(\xi) \frac{\text{Tr} \mathcal{U}^{[\square]}}{N_c} \mathcal{U}^{[-]\dagger} F^{+i}(0) \mathcal{U}^{[+]} \} | p_A \rangle, \quad \mathcal{F}_{gg}^{(2)} \sim \frac{1}{N_c} \langle p_A | \text{Tr} \{ F^{+i}(\xi) \mathcal{U}^{[\square]\dagger} \} \text{Tr} \{ F^{+i}(0) \mathcal{U}^{[\square]} \} | p_A \rangle,$$

$$\mathcal{F}_{gg}^{(3)} \sim \langle p_A | \text{Tr} \{ F^{+i}(\xi) \mathcal{U}^{[+]\dagger} F^{+i}(0) \mathcal{U}^{[+]} \} | p_A \rangle, \quad \mathcal{F}_{gg}^{(4)} \sim \langle p_A | \text{Tr} \{ F^{+i}(\xi) \mathcal{U}^{[-]\dagger} F^{+i}(0) \mathcal{U}^{[-]} \} | p_A \rangle,$$

$$\mathcal{F}_{gg}^{(5)} \sim \langle p_A | \text{Tr} \{ F^{+i}(\xi) \mathcal{U}^{[\square]\dagger} \mathcal{U}^{[+]\dagger} F^{+i}(0) \mathcal{U}^{[\square]} \mathcal{U}^{[+]} \} | p_A \rangle, \quad \mathcal{F}_{gg}^{(6)} \sim \langle p_A | \text{Tr} \{ F^{+i}(\xi) \mathcal{U}^{[+]\dagger} F^{+i}(0) \mathcal{U}^{[+]} \} \left( \frac{\text{Tr} \mathcal{U}^{[\square]}}{N_c} \right)^2 | p_A \rangle$$

**Exact correspondence to the TMD factorization.**

# Improved TMD factorization (ITMD)

## Pros and cons of the TMD factorization

- Pros: usage of gluon distributions with operator definitions
- Cons: only back-to-back region
- Cons: cannot be easily implemented in a MC event generation

We can 'improve' the TMD factorization to be valid at  $P_T \gg Q_s$

[P.K., K. Kutak, C. Marquet, E. Petreska, S. Sapeta, A. van Hameren, JHEP 1509 (2015) 106]

- Use the dual decomposition of the hard sub-processes to simplify the structure: only two TMDs per channel
- Calculate the amplitudes **off-shell in a gauge invariant way**

$$\frac{d\sigma_{AB}}{dy_1 d^2 p_{T1} dy_2 d^2 p_{T1}} \sim \sum_{a,c,d} f_{a/B}(x_B, P_T^2) \sum_{i=1,2} \Phi_{ag \rightarrow cd}^{(i)}(x_A, k_T^2) K_{ag \rightarrow cd}^{(i)}(k_T^2)$$

- Two well defined limits:
  - ① leading power limit of CGC when  $P_T \gg k_T$  (saturation)
  - ② dilute limit of CGC when  $P_T \sim k_T$  (High Energy Factorization)

# ITMD for $\gamma A \rightarrow 2\text{jets}$

Similar procedure (but simpler) gives:

$$\frac{d\sigma_{\gamma A \rightarrow 2j}}{dy_1 d^2p_{T1} dy_2 d^2p_{T1}} \sim x_A G_1(x_A, k_T^2) \otimes K_{\gamma g^* \rightarrow q\bar{q}}(k_T)$$

$xG_1$  – the WW gluon distribution

$K_{\gamma g^* \rightarrow q\bar{q}}$  – off-shell hard factor for the  $\gamma g^* \rightarrow q\bar{q}$  process

- Formula is as simple as for e.g. inclusive DIS, but probes different gluon distribution
- For UPC the problem is that the photon flux dies out very fast above  $x_\gamma \sim 0.03$  for Pb, so there is not much 'space' for the asymmetric kinematics  $x_A \ll x_\gamma$  at current LHC energies with reasonable  $p_T$  cuts.

# Improved TMD factorization (ITMD)

## How to get gluon distributions?

- At large  $N_c$  and in Gaussian approximation all distributions can be calculated from the dipole UGD, which is known from HERA
- One can use JIMWLK equation to get gluon distributions from McLerran-Venugopalan (MV) model
- Direct renormalization group equation of operators, valid at any  $x$  and including hard scale dependence (very complicated, in progress)

[A. van Hameren, P.K., K. Kutak, C. Marquet, E. Petreska, S. Sapeta, JHEP 1612 (2016) 034]

[C. Marquet, E. Petreska, C. Roiesnel, JHEP 1610 (2016) 065]

[I. Balitsky, A. Tarasov, JHEP 1606 (2016) 164]

## Important result:

All gluon distributions have universal large  $k_T$  behavior (except one which vanishes very fast).

⇒ ITMD formalism recovers correct linear regime of High Energy factorization.

Checked in two first approaches (and also analytically for the MV model).

# The WW gluon distribution from data

Relation between  $xG_1$  and  $xG_2$  in gaussian approximation

$$\nabla_{k_T}^2 G^{(1)}(x, k_T) = \frac{4\pi^2}{N_c S_\perp} \int \frac{d^2 q_T}{q_T^2} \frac{\alpha_s}{(k_T - q_T)^2} G^{(2)}(x, q_T) G^{(2)}(x, |k_T - q_T|)$$

Realistic evolution equation for  $xG_2$

Nonlinear extension of the Kwiecinski-Martin-Stasto (KMS) evolution equation  
(below  $xG_2 \equiv \mathcal{F}$ ):

[K. Kutak, K. Kwiecinski, Eur. Phys. J. C 29 (2003) 521]  
[J. Kwiecinski, Alan D. Martin, A.M. Stasto, Phys.Rev. D56 (1997) 3991-4006]

$$\begin{aligned} \mathcal{F}(x, k_T^2) = & \mathcal{F}_0(x, k_T^2) + \frac{\alpha_s N_c}{\pi} \int_x^1 \frac{dz}{z} \int_{k_{T0}^2}^\infty \frac{dq_T^2}{q_T^2} \left\{ \frac{q_T^2 \mathcal{F}\left(\frac{x}{z}, q_T^2\right) \theta\left(\frac{k_T^2}{z} - q_T^2\right) - k_T^2 \mathcal{F}\left(\frac{x}{z}, k_T^2\right)}{|q_T^2 - k_T^2|} + \frac{k_T^2 \mathcal{F}\left(\frac{x}{z}, k_T^2\right)}{\sqrt{4q_T^4 + k_T^4}} \right\} \\ & + \frac{\alpha_s}{2\pi k_T^2} \int_x^1 dz \left\{ \left( P_{gg}(z) - \frac{2N_c}{z} \right) \int_{k_{T0}^2}^{k_T^2} dq_T^2 \mathcal{F}\left(\frac{x}{z}, q_T^2\right) + z P_{gq}(z) \Sigma\left(\frac{x}{z}, k_T^2\right) \right\} \\ & - \frac{2\alpha_s^2}{R^2} \left\{ \left[ \int_{k_T^2}^\infty \frac{dq_T^2}{q_T^2} \mathcal{F}(x, q_T^2) \right]^2 + \mathcal{F}(x, k_T^2) \int_{k_T^2}^\infty \frac{dq_T^2}{q_T^2} \ln\left(\frac{q_T^2}{k_T^2}\right) \mathcal{F}(x, q_T^2) \right\} \end{aligned}$$

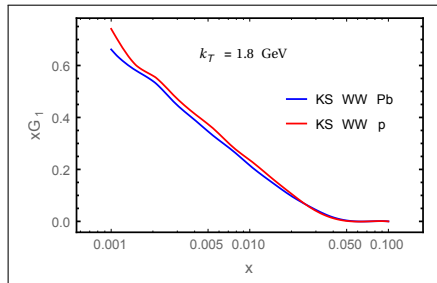
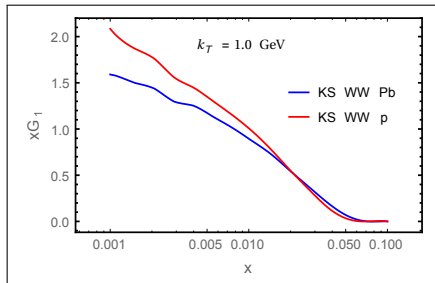
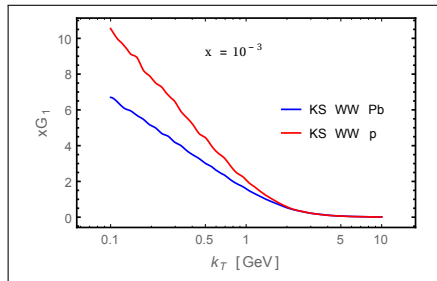
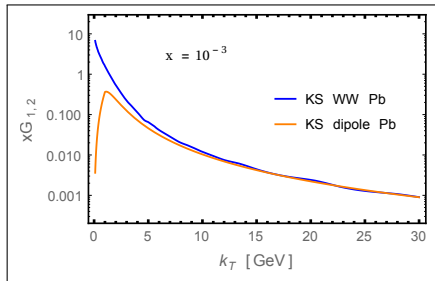
This equation was fitted to HERA data for proton by Kutak-Sapeta (KS).

[K. Kutak, S. Sapeta, Phys. Rev. D 86 (2012) 094043]

For nucleus  $R_A = RA^{1/3} / \sqrt{d}$  is used so the nonlinear term is enhanced by  $dA^{1/3}$ .

# The WW gluon distribution from data

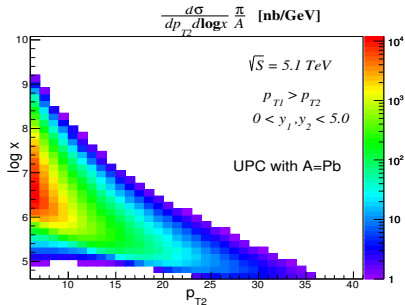
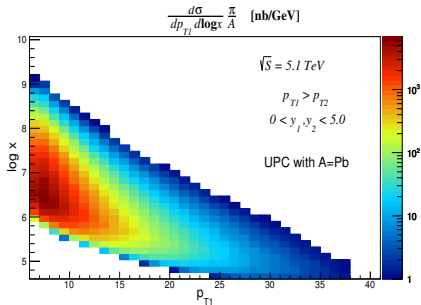
Results for  $Pb = 208$  and  $d = 0.5$



# Results for dijets in UPC

## Kinematic cuts

|   |                              |
|---|------------------------------|
| CM energy: 5.1 TeV  | rapidity: $0 < y_1, y_2 < 5$ |
| transverse momenta: $p_{T1} > p_{T2} > p_{T0}$ , $p_{T0} = 6 \div 25$ GeV | jet algorithm: $R = 0.5$     |

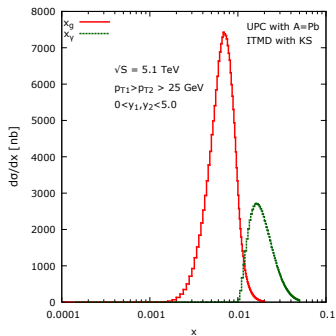
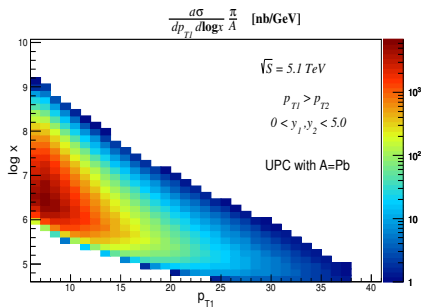




# Results for dijets in UPC

Kinematic cuts

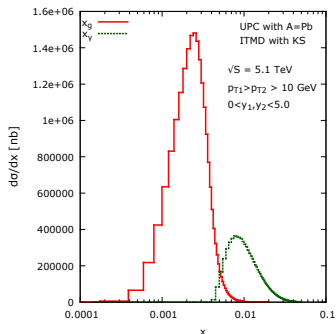
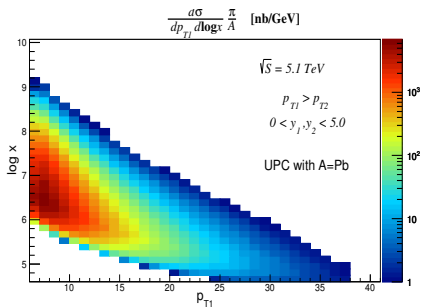
|   |                              |
|---|------------------------------|
| CM energy: 5.1 TeV  | rapidity: $0 < y_1, y_2 < 5$ |
| transverse momenta: $p_{T1} > p_{T2} > p_{T0}$ , $p_{T0} = 6 \div 25$ GeV | jet algorithm: $R = 0.5$     |



# Results for dijets in UPC

Kinematic cuts

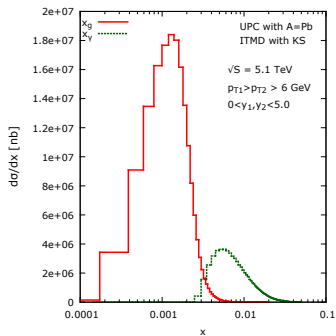
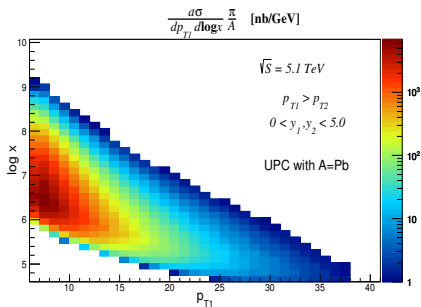
|   |                              |
|---|------------------------------|
| CM energy: 5.1 TeV  | rapidity: $0 < y_1, y_2 < 5$ |
| transverse momenta: $p_{T1} > p_{T2} > p_{T0}$ , $p_{T0} = 6 \div 25$ GeV | jet algorithm: $R = 0.5$     |



# Results for dijets in UPC

Kinematic cuts

|   |                              |
|---|------------------------------|
| CM energy: 5.1 TeV  | rapidity: $0 < y_1, y_2 < 5$ |
| transverse momenta: $p_{T1} > p_{T2} > p_{T0}$ , $p_{T0} = 6 \div 25$ GeV | jet algorithm: $R = 0.5$     |



# Results for dijets in UPC

Nuclear modification factor  $R_{\gamma A}$

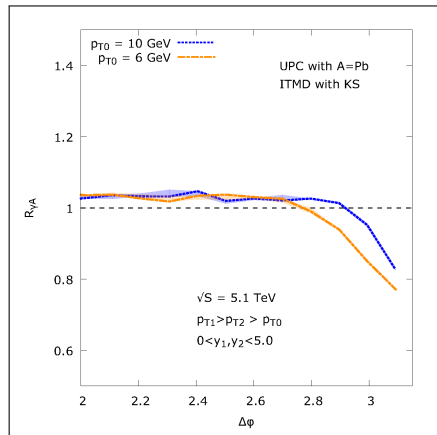
$$R_{\gamma A} = \frac{d\sigma_{AA}^{\text{UPC}}}{A d\sigma_{Ap}^{\text{UPC}}}$$

where  $A = \text{Pb}$  and the  $d\sigma_{Ap}^{\text{UPC}}$  is with jets going in the nucleus direction.

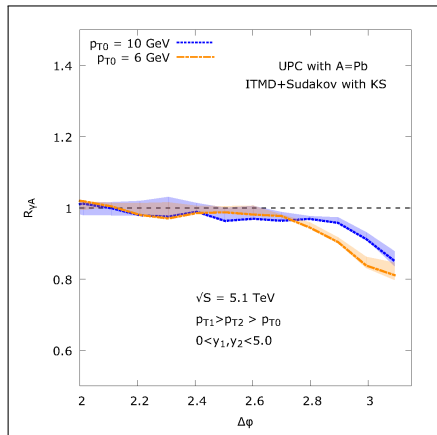
# Results for dijets in UPC

Nuclear modification factor  $R_{\gamma A}$

azimuthal imbalance



azimuthal imbalance with Sudakov

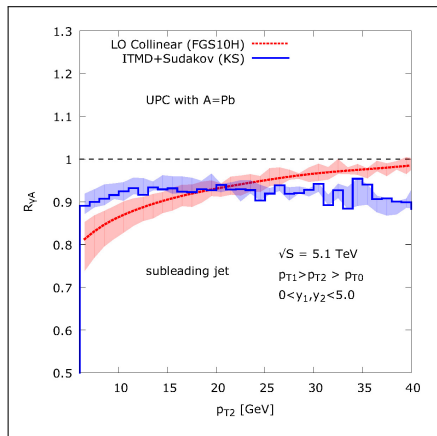
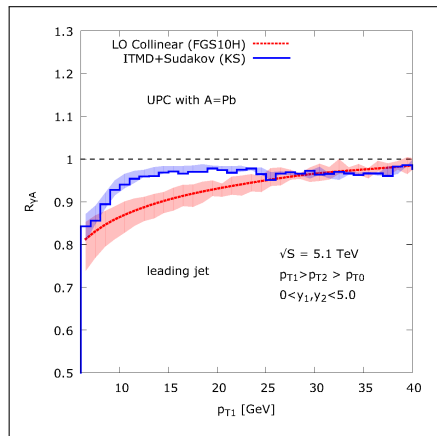


# Results for dijets in UPC

Nuclear modification factor  $R_{\gamma A}$

leading jet  $p_T$

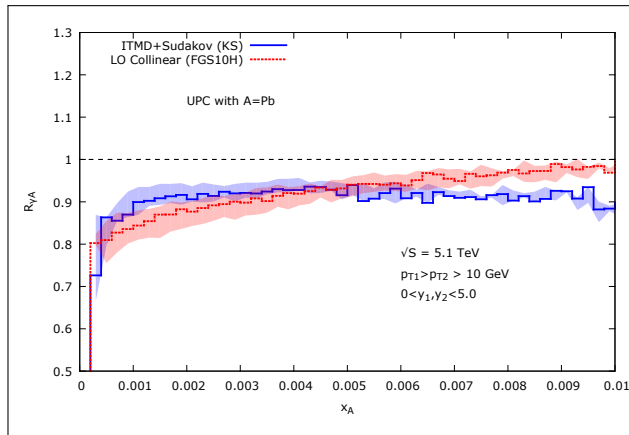
subleading jet  $p_T$



# Results for dijets in UPC

Nuclear modification factor  $R_{\gamma A}$

x spectrum



# Summary

- When  $P_T \gg Q_s$  the CGC expressions for dijet production can be reinterpreted in terms of small- $x$  TMD gluon distributions.
  - They are not universal, but can be calculated within certain approximations
  - The language of gluon distribution has practical advantages
- Direct component of dijet production in UPC is directly sensitive to Weizsacker-Williams (WW) gluon distribution; this is the only 'true' gluon distribution at small  $x$
- Present calculations use WW obtained from the 'dipole' gluon distribution fitted to data; no experimental information about WW is available
- Within the kinematics allowed by the present formalism the suppression factor is 10-20% depending on the transverse momentum cut
- Similar suppression is visible for leading twist shadowing, but it vanishes faster with increase of  $x$



**BACKUP**

# Improved TMD factorization (iTMD): $P_T \gg Q_s$

[P.K., K. Kutak, C. Marquet, E. Petreska, S. Sapeta, A. van Hameren, JHEP 1509 (2015) 106]

$$\frac{d\sigma_{AB}}{dy_1 d^2p_{T1} dy_2 d^2p_{T1}} \sim \sum_{a,c,d} f_{a/B}(x_B, P_T^2) \sum_{i=1,2} \Phi_{ag \rightarrow cd}^{(i)}(x_A, k_T^2) K_{ag \rightarrow cd}^{(i)}$$

$$\Phi_{qg \rightarrow gq}^{(1)} = \mathcal{F}_{qg}^{(1)}, \Phi_{qg \rightarrow gq}^{(2)} = \frac{1}{N_c^2 - 1} (N_c^2 \mathcal{F}_{qg}^{(2)} - \mathcal{F}_{qg}^{(1)}), \Phi_{gg \rightarrow q\bar{q}}^{(1)} = \frac{1}{N_c^2 - 1} (N_c^2 \mathcal{F}_{gg}^{(1)} - \mathcal{F}_{gg}^{(3)}), \Phi_{gg \rightarrow q\bar{q}}^{(2)} = \mathcal{F}_{gg}^{(3)} - N_c^2 \mathcal{F}_{gg}^{(2)}$$

$$\Phi_{gg \rightarrow gg}^{(1)} = \frac{1}{2N_c^2} (N_c^2 \mathcal{F}_{gg}^{(1)} - 2\mathcal{F}_{gg}^{(3)} + \mathcal{F}_{gg}^{(4)} + \mathcal{F}_{gg}^{(5)} + N_c^2 \mathcal{F}_{gg}^{(6)}), \Phi_{gg \rightarrow gg}^{(2)} = \frac{1}{N_c^2} (N_c^2 \mathcal{F}_{gg}^{(2)} - 2\mathcal{F}_{gg}^{(3)} + \mathcal{F}_{gg}^{(4)} + \mathcal{F}_{gg}^{(5)} + N_c^2 \mathcal{F}_{gg}^{(6)})$$

$$K_{qg \rightarrow gq}^{(1)} = -\frac{\bar{u}(\bar{s}^2 + \bar{u}^2)}{2\bar{t}\hat{s}} \left( 1 + \frac{\bar{s}\hat{s} - \bar{t}\hat{t}}{N_c^2 \bar{u}\hat{u}} \right), K_{qg \rightarrow gq}^{(2)} = -\frac{C_F}{N_c} \frac{\bar{s}(\bar{s}^2 + \bar{u}^2)}{\bar{t}\hat{t}\hat{u}}, K_{gg \rightarrow q\bar{q}}^{(1)} = \frac{1}{2N_c} \frac{(\bar{t}^2 + \bar{u}^2)(\bar{u}\hat{u} + \bar{t}\hat{t})}{\bar{s}\hat{s}\hat{t}\hat{u}}$$

$$K_{gg \rightarrow q\bar{q}}^{(2)} = \frac{1}{4N_c^2 C_F} \frac{(\bar{t}^2 + \bar{u}^2)(\bar{u}\hat{u} + \bar{t}\hat{t} - \bar{s}\hat{s})}{\bar{s}\hat{s}\hat{t}\hat{u}}, K_{gg \rightarrow q\bar{q}}^{(2)} = \frac{1}{4N_c^2 C_F} \frac{(\bar{t}^2 + \bar{u}^2)(\bar{u}\hat{u} + \bar{t}\hat{t} - \bar{s}\hat{s})}{\bar{s}\hat{s}\hat{t}\hat{u}},$$

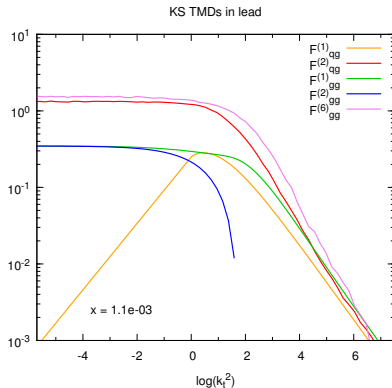
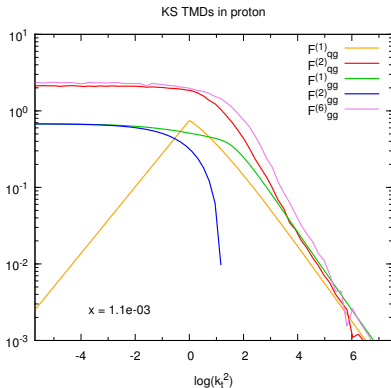
$$K_{gg \rightarrow gg}^{(1)} = \frac{N_c}{C_F} \frac{(\bar{s}^4 + \bar{t}^4 + \bar{u}^4)(\bar{u}\hat{u} + \bar{t}\hat{t})}{\bar{t}\hat{t}\hat{u}\hat{u}\bar{s}\hat{s}}, K_{gg \rightarrow gg}^{(2)} = -\frac{N_c}{2C_F} \frac{(\bar{s}^4 + \bar{t}^4 + \bar{u}^4)(\bar{u}\hat{u} + \bar{t}\hat{t} - \bar{s}\hat{s})}{\bar{t}\hat{t}\hat{u}\hat{u}\bar{s}\hat{s}}$$

$\hat{s}, \hat{t}, \hat{u}$  – ordinary Mandelstam variables,  $\hat{s} + \hat{t} + \hat{u} = k_T^2$

$\bar{s}, \bar{t}, \bar{u}$  off-shell momentum is replaced by its longitudinal component of off-shell momentum,  $\bar{s} + \bar{u} + \bar{t} = 0$

# Gluon distributions: realistic model

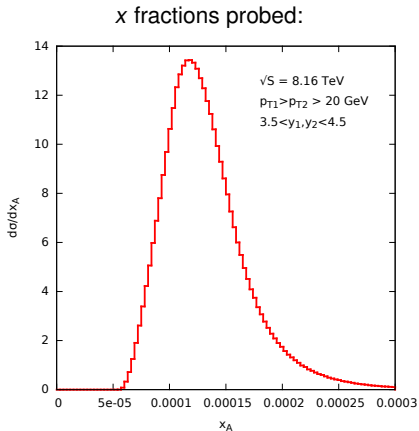
Five gluon distributions from KS fit



All gluons start to merge for large  $k_T$  (except  $\mathcal{F}_{gg}^{(2)}$  which vanishes)  $\Rightarrow$  consistent with HEF limit.

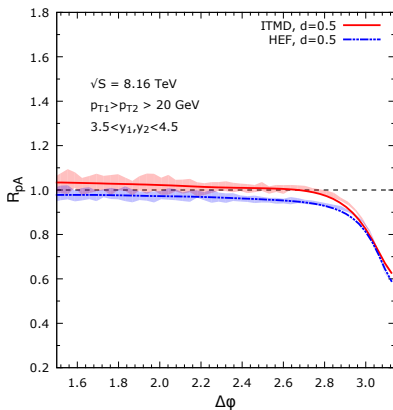
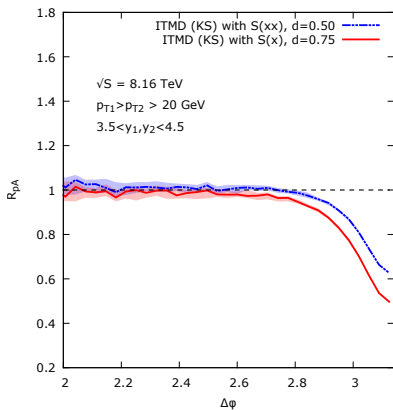
# $R_{pPb}$ for azimuthal disbalance in ITMD

Cuts:  $p_{T1} > p_{T2} > 20$  GeV,  $3.5 < y_1, y_2 < 4.5$ ,  $\sqrt{S} = 8.16$  TeV



# $R_{pPb}$ for azimuthal disbalance in ITMD

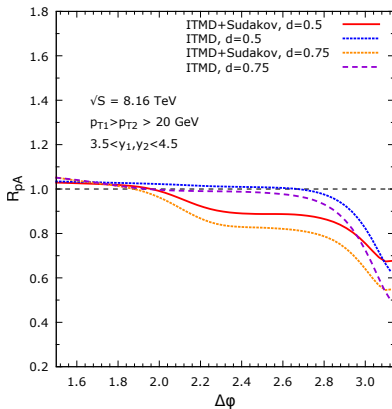
Cuts:  $p_{T1} > p_{T2} > 20$  GeV,  $3.5 < y_1, y_2 < 4.5$ ,  $\sqrt{S} = 8.16$  TeV



# $R_{pPb}$ for azimuthal disbalance in ITMD

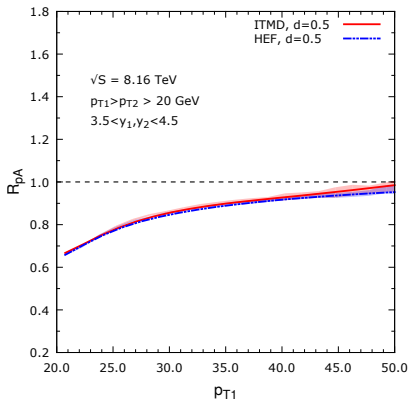
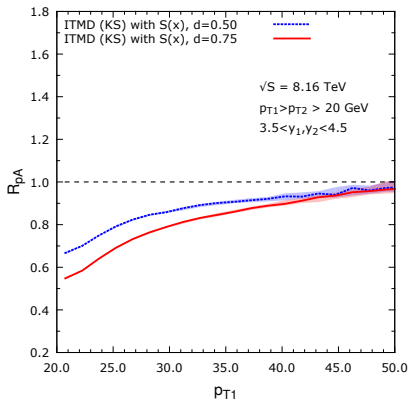
Cuts:  $p_{T1} > p_{T2} > 20 \text{ GeV}$ ,  $3.5 < y_1, y_2 < 4.5$ ,  $\sqrt{S} = 8.16 \text{ TeV}$

Including Sudakov resummation (a model of):



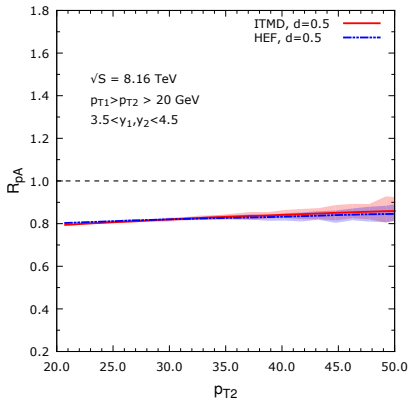
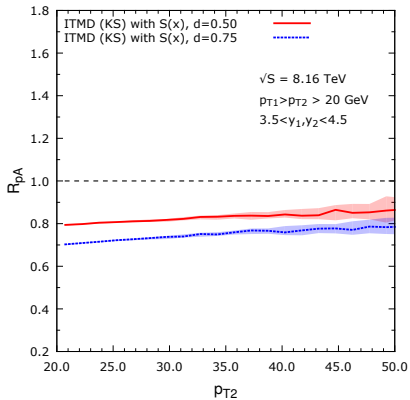
# $R_{pPb}$ for $p_T$ spectra in ITMD

leading jet spectrum:



# $R_{pPb}$ for $p_T$ spectra in ITMD

sub-leading jet spectrum:





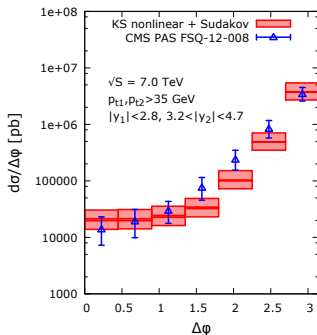
# High Energy Factorization

## Comparison with data

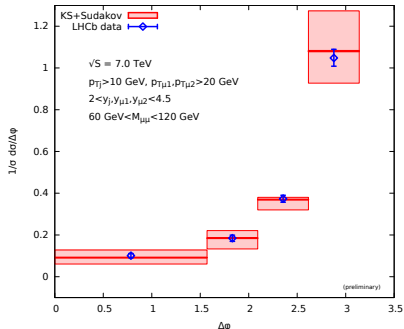
In reality, the forward jets are decorrelated  $\Rightarrow$  decorrelations are nicely described by the High Energy Factorization.

[A. van Hameren, PK, K. Kutak, S. Sapeta, Phys.Lett. B737 (2014) 335-340]

forward-central dijets



forward  $Z_0$  + jet



We can improve TMD factorization by introducing off-shellness to the hard factors.

# Constructing ITMD

## Main steps

[PK., K. Kutak, C. Marquet, E. Petreska, S. Sapeta, A. van Hameren, arXiv:150342]

- We revise the calculation of TMD gluon distributions using color decomposition of amplitudes

$$\mathcal{M}^{a_1 \dots a_N}(\varepsilon_1^{\lambda_1}, \dots, \varepsilon_N^{\lambda_N}) = \sum_{\sigma \in S_{N-1}} \text{Tr}(t^{a_1} t^{a_{\sigma_2}} \dots t^{a_{\sigma_N}}) \mathcal{M}(1^{\lambda_1}, \sigma_2^{\lambda_{\sigma_2}}, \dots, \sigma_N^{\lambda_{\sigma_N}})$$

$a_i$ - color indices,  $\varepsilon_i^{\lambda_i}$  - polarization vectors with helicity  $\lambda_i$ ,  $S_{N-1}$  - set of noncyclic permutations.

We conclude that there are only two independent TMDs  $\Phi^{(i)}$ ,  $i = 1, 2$  (being a combination of  $\mathcal{F}_{qg}^{(1)}$ 's) needed for each channel.

- We calculate off-shell gauge invariant color-ordered helicity amplitudes.

Methods for gauge invariant off-shell amplitudes:

[E. Antonov, L. Lipatov, E. Kuraev, I. Cherednikov, Nucl.Phys. B721 (2005) 111-135]

[A. van Hameren, PK, K. Kutak, JHEP 1212 (2012) 029; JHEP 1301 (2013) 078]

[A. van Hameren, JHEP 1407 (2014) 138],

[PK, JHEP 1407 (2014) 128]

[A. van Hameren, M. Serino, arXiv:1504.00315]

# Constructing ITMD

## Color-ordered off-shell helicity amplitudes

[A. van Hameren, PK, K. Kutak, JHEP 1212 (2012) 029]

In spinor formalism, the non-zero off-shell helicity amplitudes have the form of the MHV amplitudes with certain modification of spinor products:

$$\mathcal{M}_{g^*g \rightarrow gg}(1^*, 2^-, 3^+, 4^+) = 2g^2 \rho_1 \frac{\langle 1^*2 \rangle^4}{\langle 1^*2 \rangle \langle 23 \rangle \langle 34 \rangle \langle 41^* \rangle}$$

$$\mathcal{M}_{g^*g \rightarrow gg}(1^*, 2^+, 3^-, 4^+) = 2g^2 \rho_1 \frac{\langle 1^*3 \rangle^4}{\langle 1^*2 \rangle \langle 23 \rangle \langle 34 \rangle \langle 41^* \rangle}$$

$$\mathcal{M}_{g^*g \rightarrow gg}(1^*, 2^+, 3^+, 4^-) = 2g^2 \rho_1 \frac{\langle 1^*4 \rangle^4}{\langle 1^*2 \rangle \langle 23 \rangle \langle 34 \rangle \langle 41^* \rangle}$$

where  $\langle ij \rangle = \langle k_i - |k_j \rangle$  with spinors defined as  $|k_{i\pm} \rangle = \frac{1}{2} (1 \pm \gamma_5) u(k_i)$ . Modified spinor products involve only longitudinal component of the off-shell momentum  $\langle 1^*i \rangle = \langle p_A i \rangle$ . Similar expressions can be derived for quarks.