



INT Program INT-17-3

Spatial and Momentum Tomography of Hadrons and Nuclei

August 28 – September 29, 2017

Heavy Quarkonium Production at EIC Energies

- ✧ Why heavy quarkonium?
- ✧ Production mechanism?
- ✧ EIC: Inclusive DIS, SIDIS, Exclusive, ...
- ✧ Gluon distribution, imaging, threshold, ...
- ✧ Summary and outlook

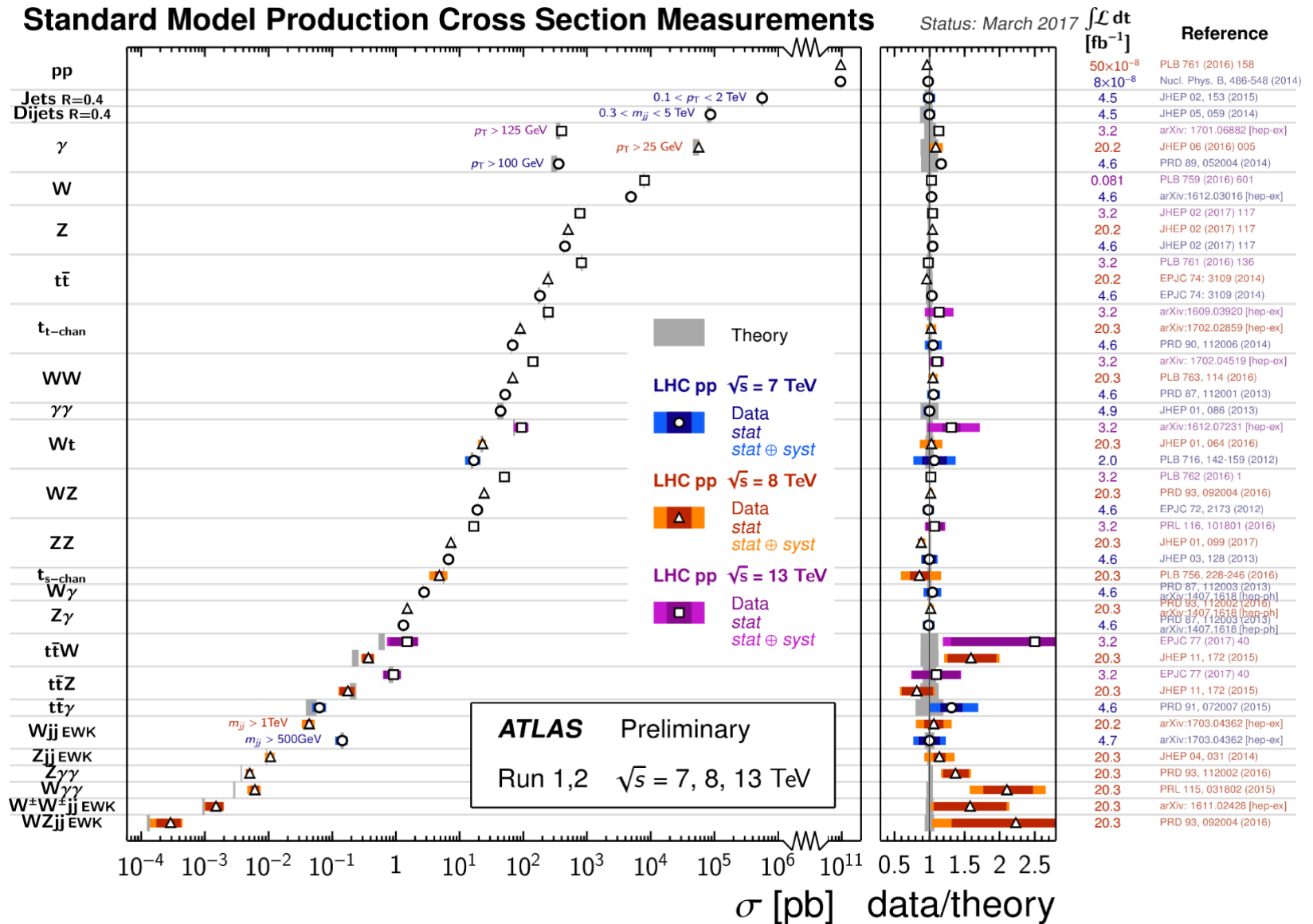


Theory Center

Jianwei Qiu

Jefferson Lab
EXPLORING THE NATURE OF MATTER

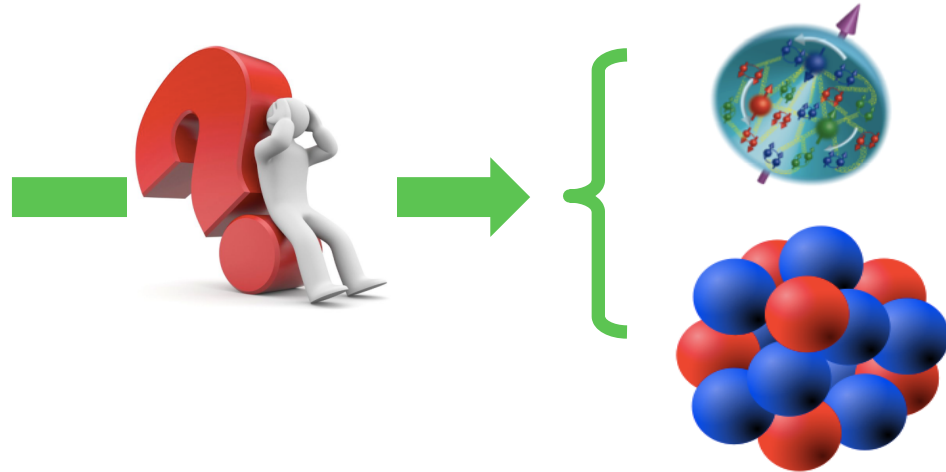
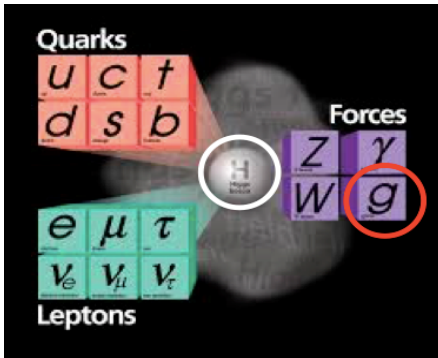
The great success of SM physics



SM: Electroweak processes + QCD perturbation theory works!

QCD – Final frontier of the SM physics

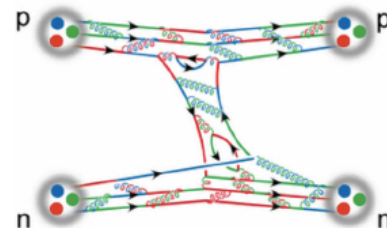
- How QCD works to get all of us? – the next QCD frontier!



- How hadrons are **emerged** from quarks and gluons?
- What is the quark/gluon **structure** of nucleon and nuclei?
- How does QCD make up the **properties** of hadrons?

Their mass, spin, magnetic moment, ...

- How does the **nuclear force** arise from QCD?
- ...



Why QCD is so hard to deal with?

- ❑ It is strongly coupled – nonlinear + nonperturbative!
- ❑ It is relativistic – nontrivial QCD vacuum!
- ❑ No localized heavy mass/charge center – nucleus in an atom!
- ❑ Gluons are “dark” and carry “color” – intellectual challenge!

How to probe the quark-gluon dynamics, quantify the hadron structure, study the emergence of hadrons, ..., if we cannot see quarks and gluons?

Heavy quarkonium:

- ✧ Heavy quark as relatively localized heavy mass/charge center
- ✧ Heavy quark in the pair’s rest frame is almost non-relativistic
- ✧ Production of heavy quark pair could be perturbative
- ✧ Top decays too quickly, strange is too light, ...



Charmonium ($c\bar{c}$) + Bottomonium ($b\bar{b}$)

c	1.0 – 1.4 GeV
b	4.0 – 4.5 GeV

Heavy quarkonium

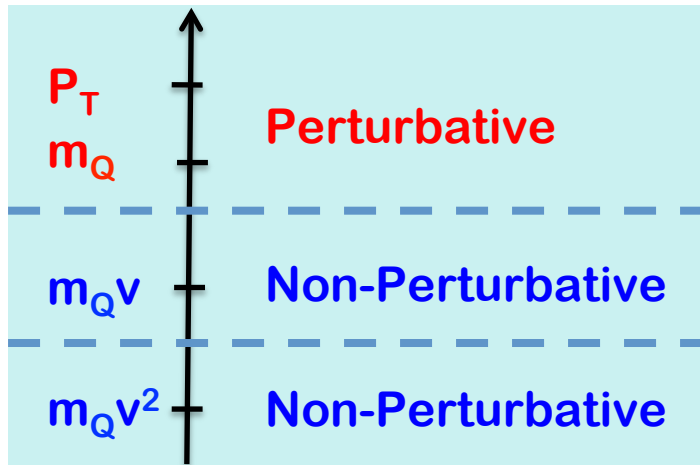
- One of the simplest QCD bound states:

Localized color charges (heavy mass), non-relativistic relative motion

Charmonium: $v^2 \approx 0.3$

Bottomonium: $v^2 \approx 0.1$

- Well-separated momentum scales – effective theory:



Hard — Production of $Q\bar{Q}$ [pQCD]

Soft — Relative Momentum [NRQCD]

← Λ_{QCD}

Ultrasoft — Binding Energy [pNRQCD]

- Cross sections and observed mass scales:

$$\frac{d\sigma_{AB \rightarrow H(P)X}}{dy dP_T^2} \quad \sqrt{S}, \quad P_T, \quad M_H,$$

PQCD is “expected” to work for the production of heavy quarks

Difficulty: Emergence of a quarkonium from a heavy quark pair?

Double $c\bar{c}$ production in e^+e^- collisions

□ Inclusive production:

$$\sigma(e^+e^- \rightarrow J/\psi c\bar{c})$$

Belle: $(0.87_{-0.19}^{+0.21} \pm 0.17)$ pb

NRQCD: : 0.07 pb

Kiselev, et al 1994,
Cho, Leibovich, 1996
Yuan, Qiao, Chao, 1997

□ Ratio to light flavors:

$$\sigma(e^+e^- \rightarrow J/\psi c\bar{c}) / \sigma(e^+e^- \rightarrow J/\psi X)$$

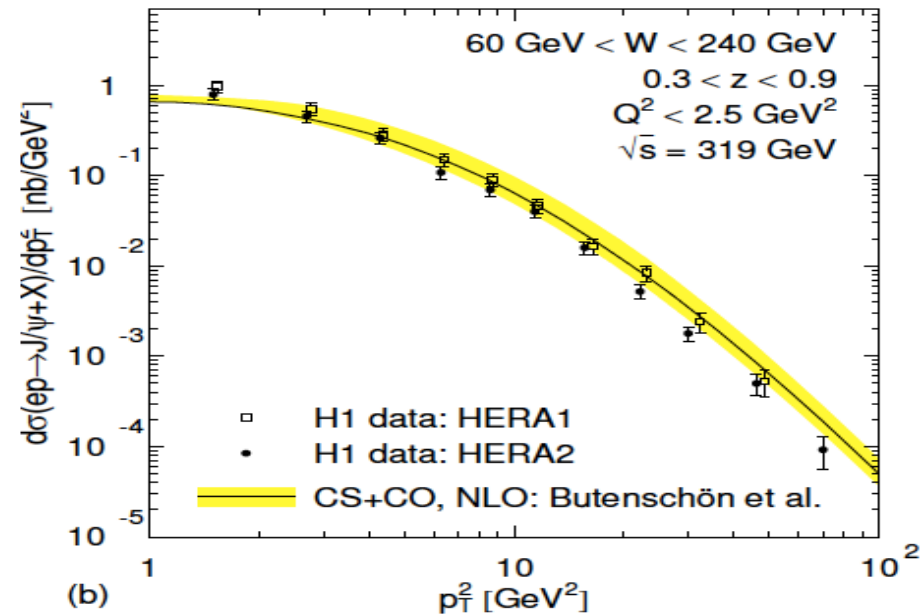
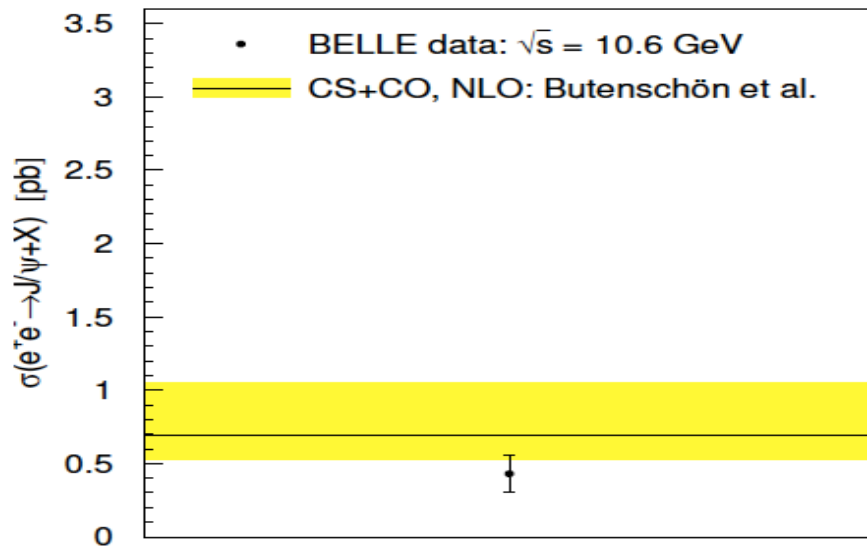
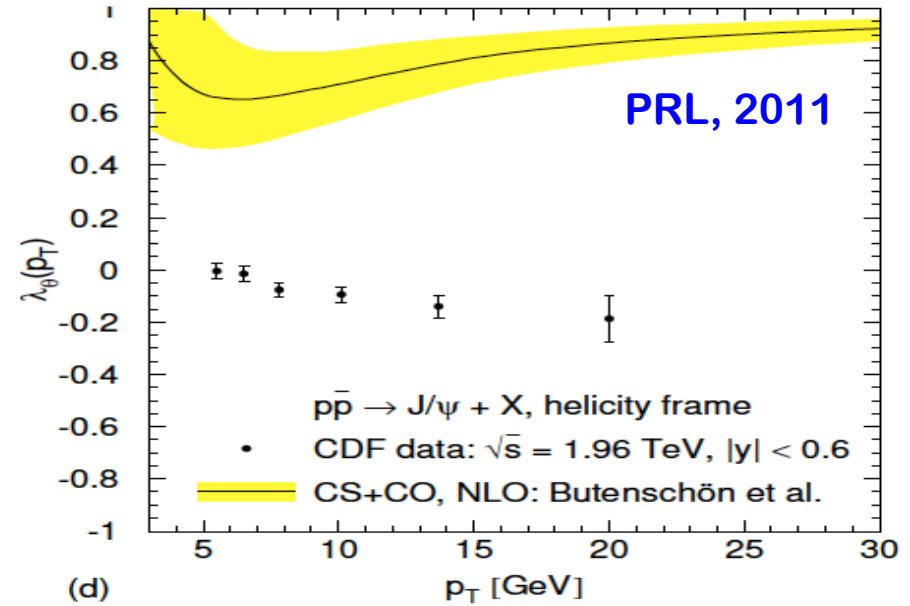
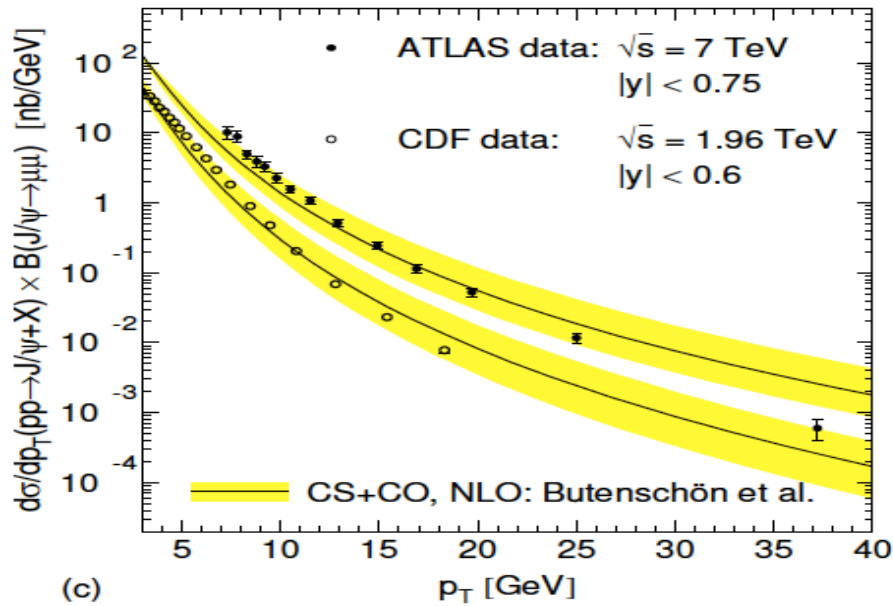
Belle: $0.59_{-0.13}^{+0.15} \pm 0.12$

Message:

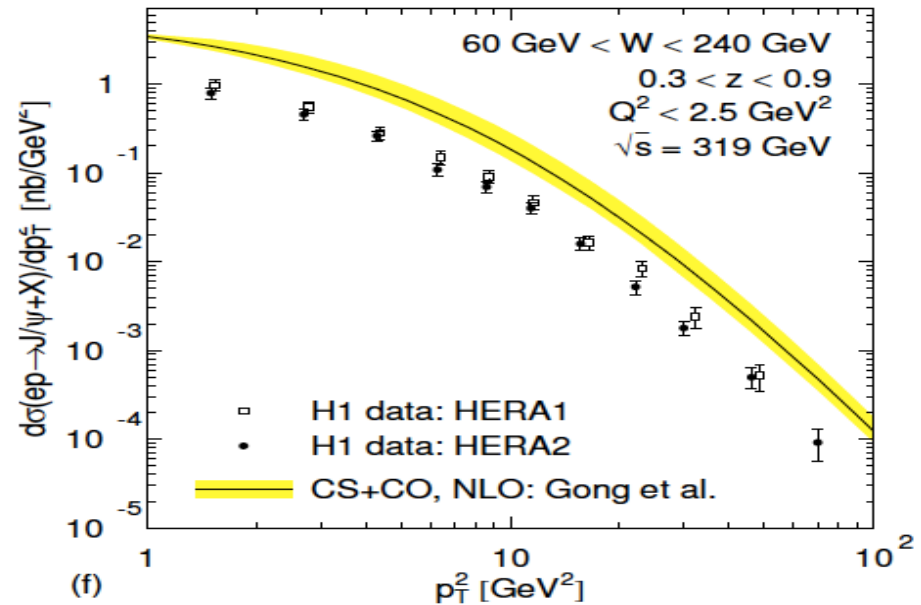
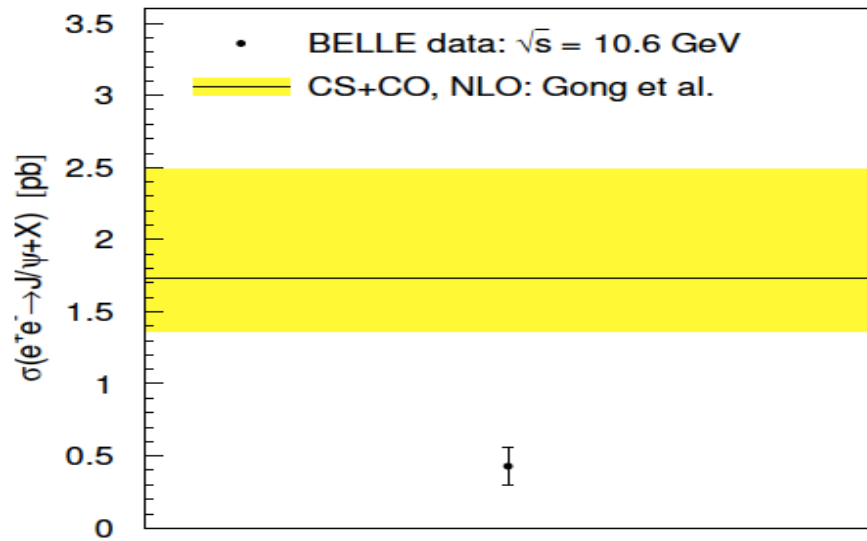
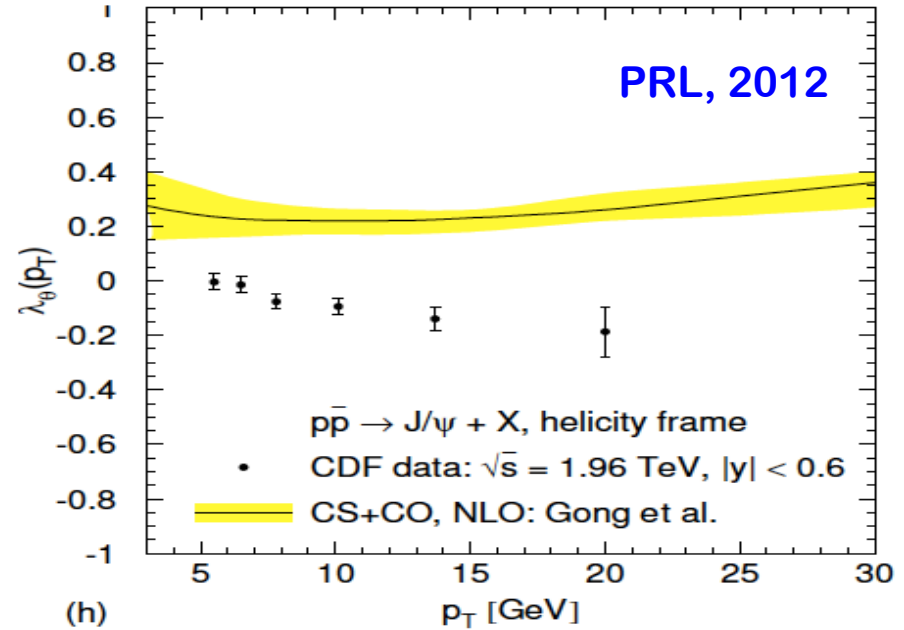
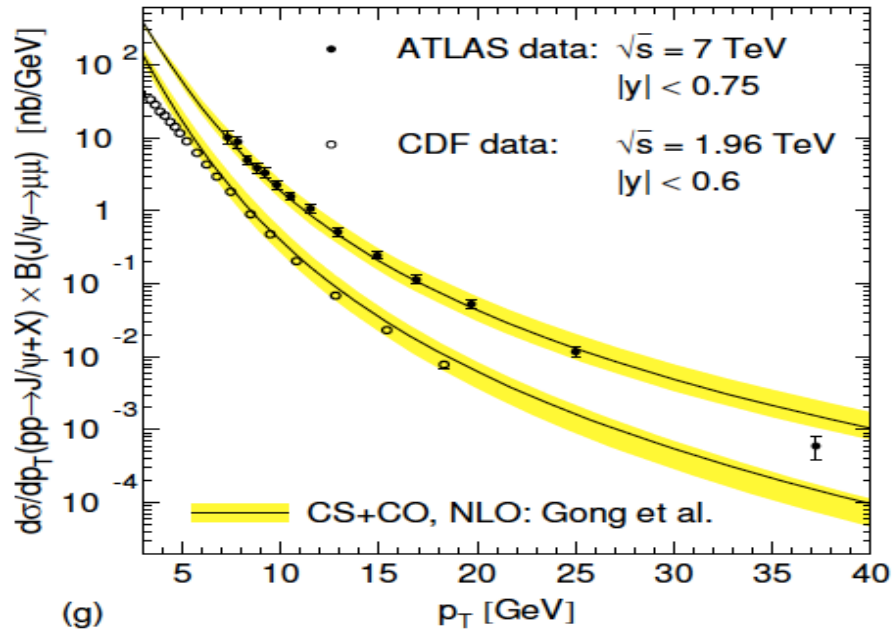
Production rate of $e^+e^- \rightarrow J/\psi c\bar{c}$ is larger than

all these channels: $e^+e^- \rightarrow J/\psi gg, e^+e^- \rightarrow J/\psi q\bar{q}, \dots$
combined ?

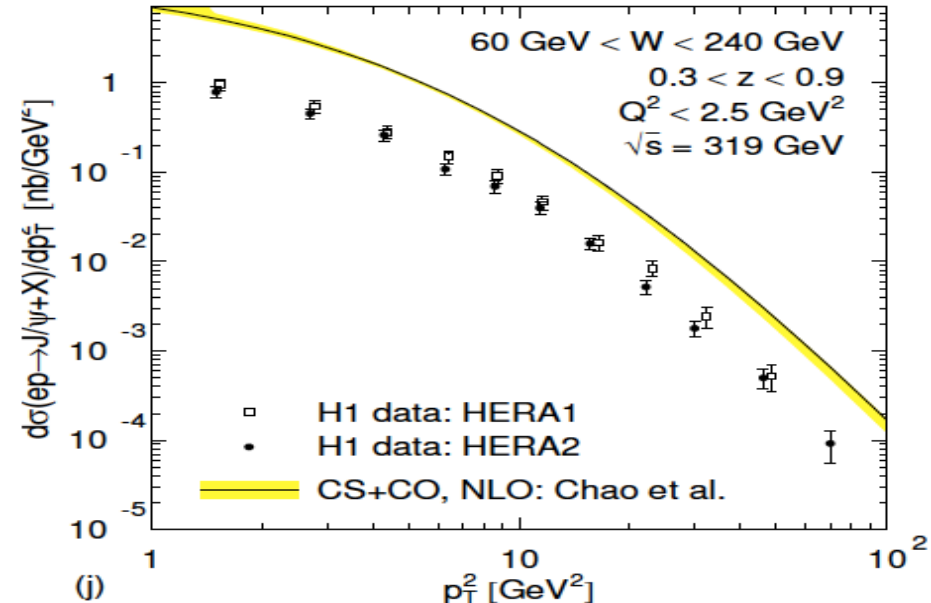
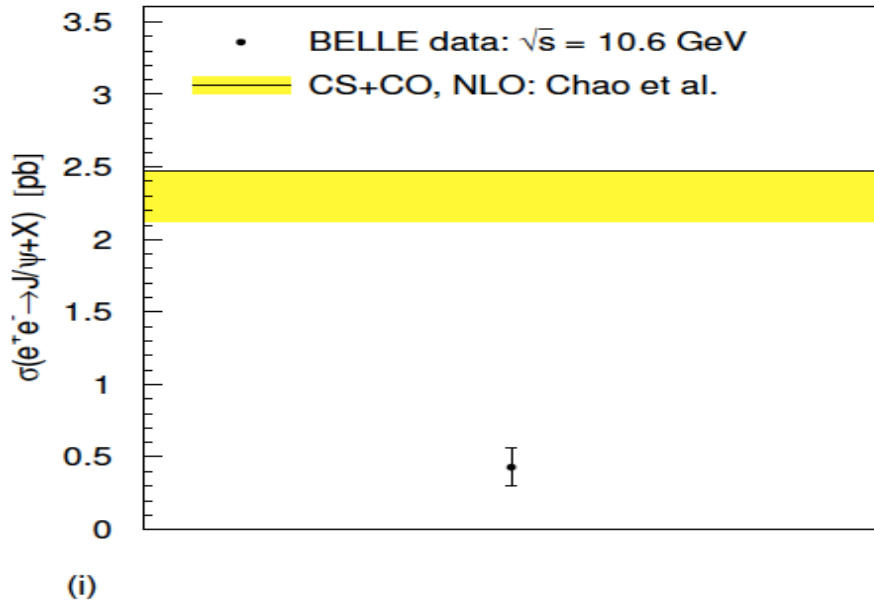
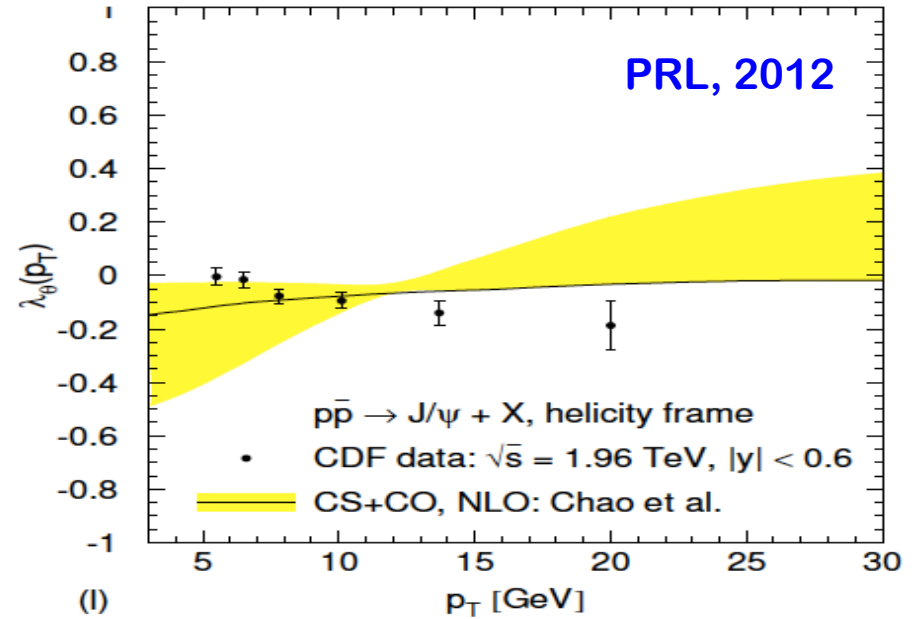
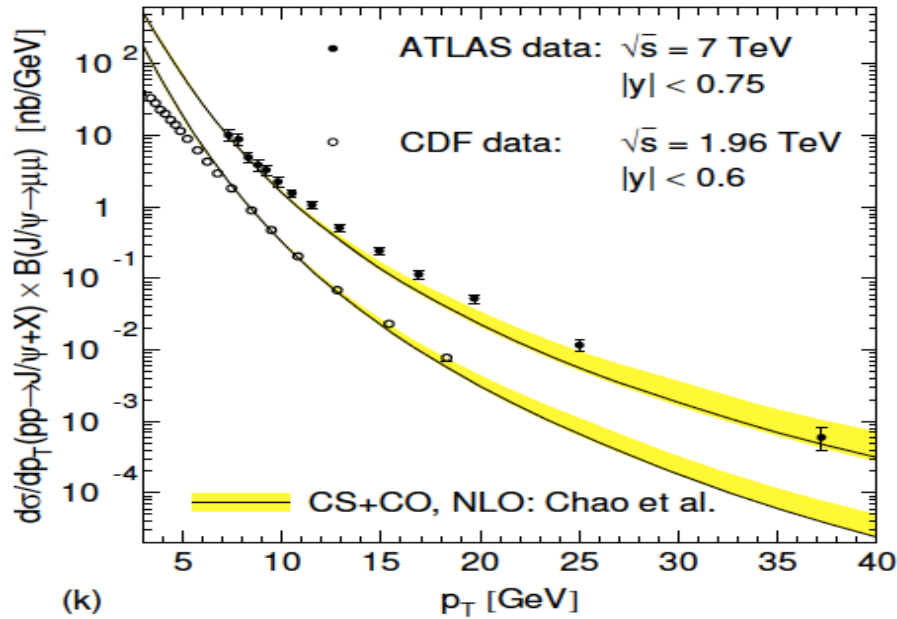
NLO theory fits – Butenschoen et al.



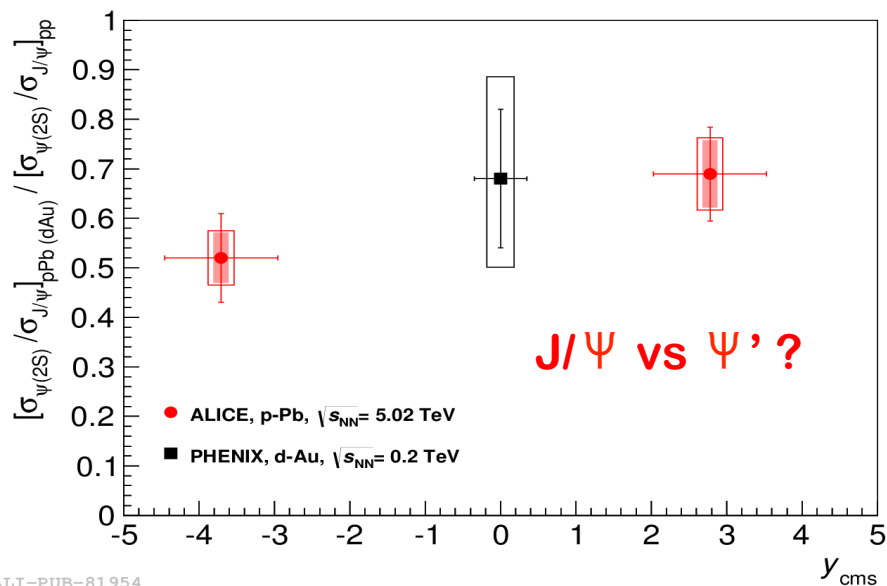
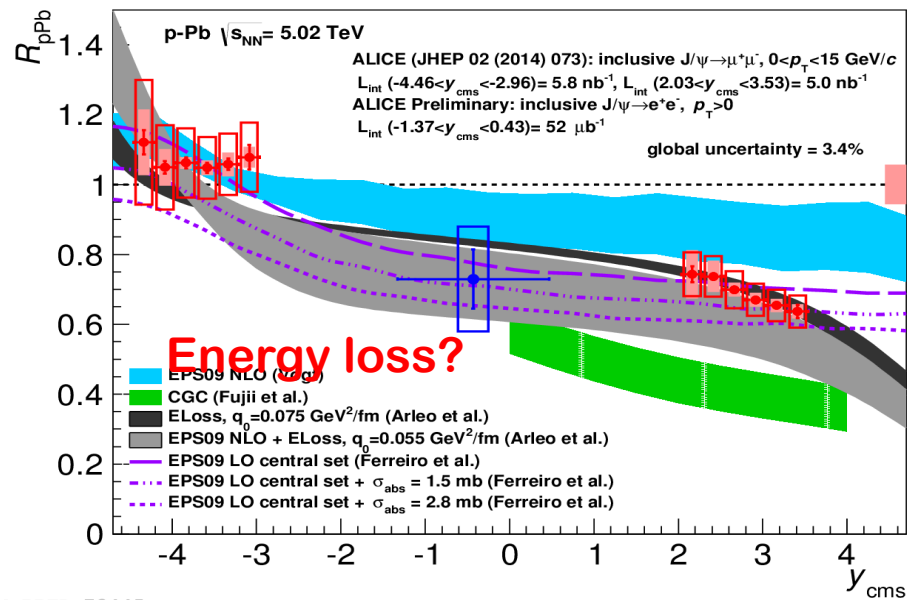
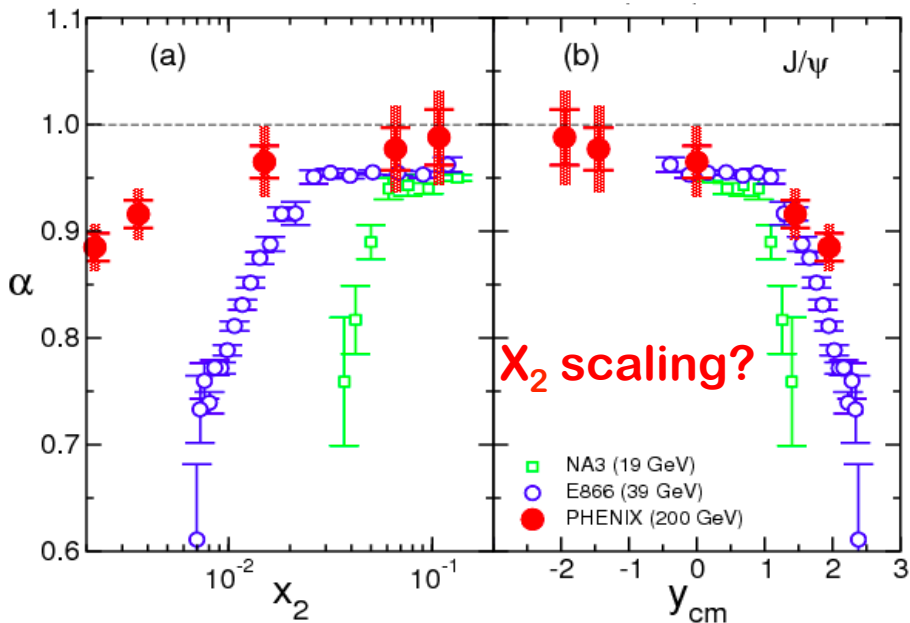
NLO theory fits – Gong et al.



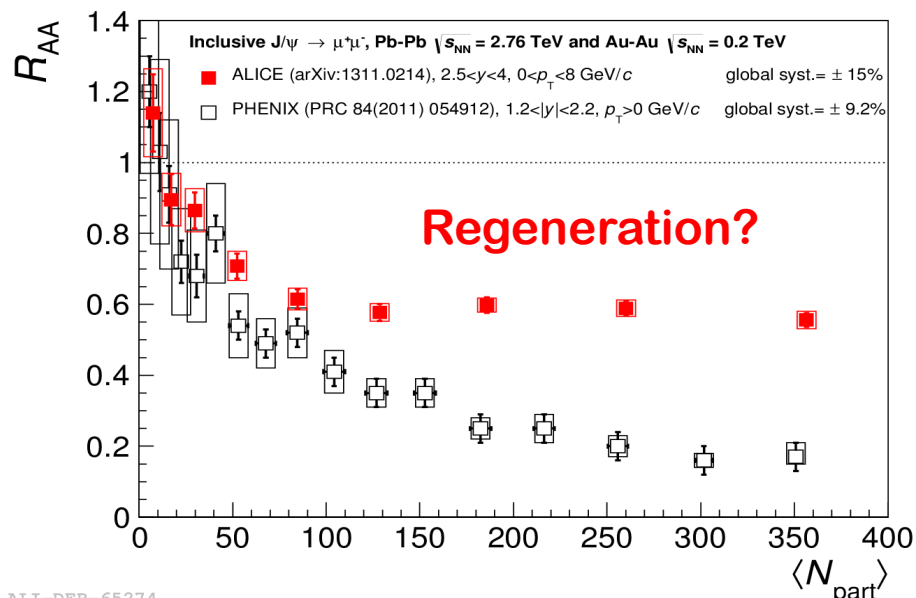
NLO theory fits – Chao et al.



Production in medium, cold or hot?



[--PREL-73445



ALI-PUB-81954

ALI-DER-65274

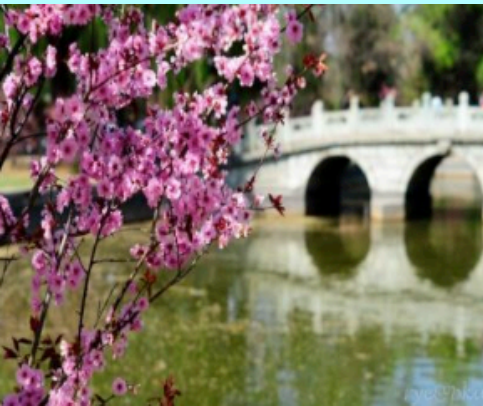
Quarkonium 2017

The 12th International Workshop on Heavy Quarkonium



November 6-10, 2017, PKU, Beijing, China
Organized by the Quarkonium Working Group

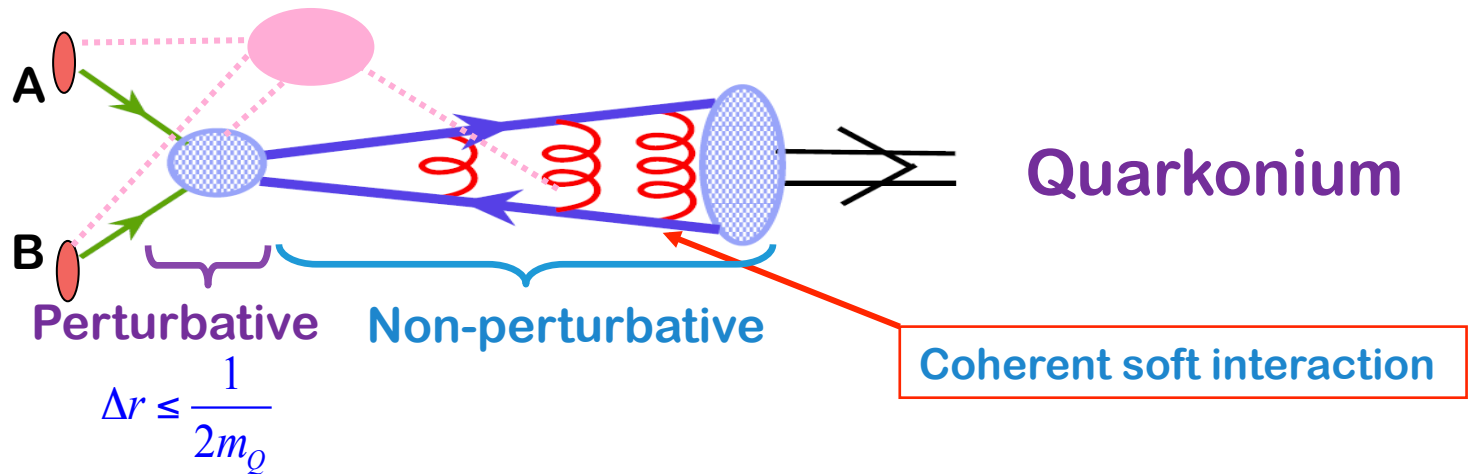
<http://itp.phy.pku.edu.cn/conference/qwg2017/>



Basic production mechanism

Factorization is likely to be valid for producing the pairs:

- Momentum exchange is much larger than $1/\text{fm}$
- Spectators from colliding beams are “frozen” during the hard collision



Approximation:

$$\sigma_{AB \rightarrow h} \propto \left| \begin{array}{c} A \rightarrow \text{H} \rightarrow Q \rightarrow \text{h} \\ B \rightarrow \text{H} \rightarrow \bar{Q} \rightarrow \text{h} \end{array} \right|^2$$

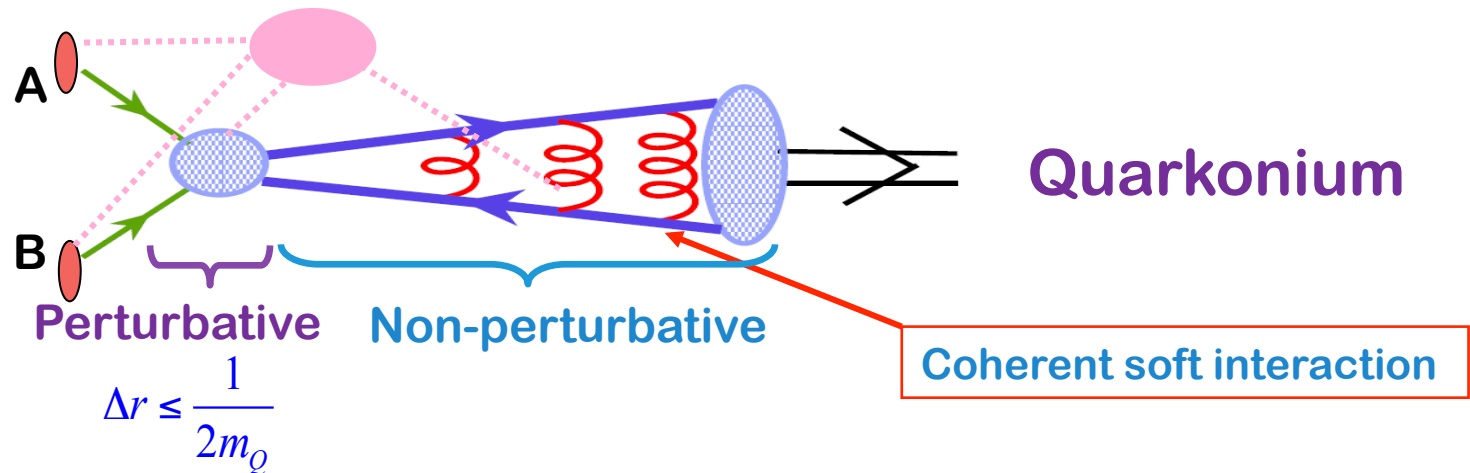
$$\propto \left| \begin{array}{c} A \rightarrow \text{H} \\ B \rightarrow \text{H} \end{array} \right|^2 \otimes \left| \begin{array}{c} Q \rightarrow \text{h} \\ \bar{Q} \rightarrow \text{h} \end{array} \right|^2 + \frac{\langle M_H^2 - 4m_Q^2 \rangle}{M_H^2}$$

$$\rightarrow \sigma_{AB \rightarrow h} = \int dq^2 \hat{\sigma}_{AB \rightarrow [Q\bar{Q}]}(m_Q^2, q^2) F_{[Q\bar{Q}] \rightarrow h}(q^2) + \dots$$

Basic production mechanism

□ Factorization is likely to be valid for producing the pairs:

- ✧ Momentum exchange is much larger than $1/\text{fm}$
- ✧ Spectators from colliding beams are “frozen” during the hard collision



□ Naïve factorization: on-shell pair + hadronization

$$\sigma_{AB \rightarrow J/\psi} = \sum_{[Q\bar{Q}(n)]} \int d\Gamma_{[Q\bar{Q}]} \hat{\sigma}_{AB \rightarrow [Q\bar{Q}(n)]}(p_Q, p_{\bar{Q}}) F_{[Q\bar{Q}(n)] \rightarrow J/\psi}(p_Q, p_{\bar{Q}}, P_{J/\psi})$$

Models & Debates

⇔ Different assumptions/treatments on $F_{[Q\bar{Q}(n)] \rightarrow J/\psi}(p_Q, p_{\bar{Q}}, P_{J/\psi})$
how the heavy quark pair becomes a quarkonium?

A long history for the production

□ Color singlet model: 1975 –

Only the pair with right quantum numbers

Effectively No free parameter!

Einhorn, Ellis (1975),
Chang (1980),
Berger and Jone (1981), ...

□ Color evaporation model: 1977 –

All pairs with mass less than open flavor heavy meson threshold

One parameter per quarkonium state

Fritsch (1977), Halzen (1977), ...

□ NRQCD model: 1986 –

All pairs with various probabilities – NRQCD matrix elements

Infinite parameters – organized in powers of v and α_s

Caswell, Lapage (1986)
Bodwin, Braaten, Lepage (1995)
QWG review: 2004, 2010

□ QCD factorization approach: 2005 –

$P_T \gg M_H$: M_H/P_T power expansion + α_s – expansion

Unknown, but universal, fragmentation functions – evolution

Nayak, Qiu, Sterman (2005), ...
Kang, Qiu, Sterman (2010), ...

□ Soft-Collinear Effective Theory + NRQCD: 2012 –

Fleming, Leibovich, Mehen, ...

NRQCD – most successful so far

Bodwin, Braaten, Lepage, PRD, 1995

NRQCD factorization:

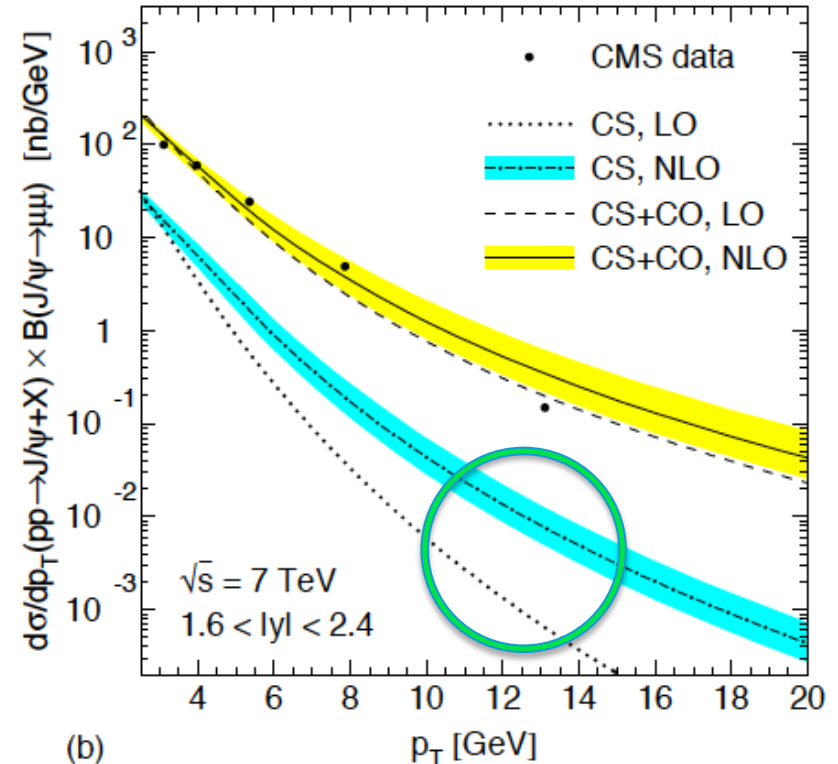
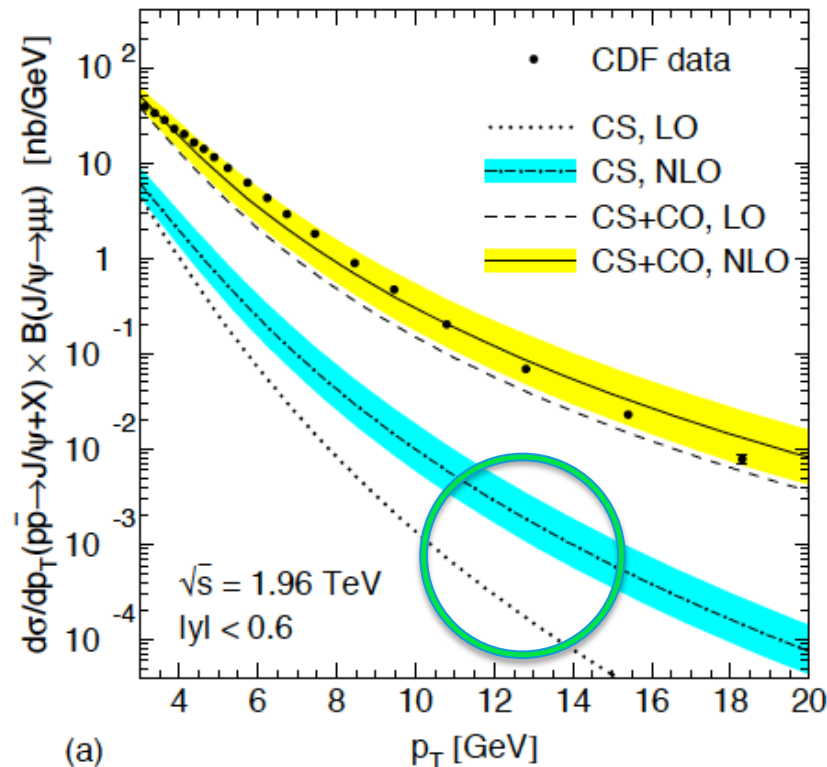
$$d\sigma_{A+B \rightarrow H+X} = \sum_n d\sigma_{A+B \rightarrow Q\bar{Q}(n)+X} \langle \mathcal{O}^H(n) \rangle$$

✧ 4 leading channels in v

$${}^3S_1^{[1]}, {}^1S_0^{[8]}, {}^3S_1^{[8]}, {}^3P_J^{[8]}$$

Phenomenology:

✧ Full NLO in α_s



Fine details – shape – high at large p_T ?

NRQCD model

□ **NRQCD Lagrangian:** $\mathcal{L}_{\text{NRQCD}} = \mathcal{L}_{\text{light}} + \mathcal{L}_{\text{heavy}} + \delta\mathcal{L}$

$$\mathcal{L}_{\text{light}} = -\frac{1}{2} \text{tr} G_{\mu\nu} G^{\mu\nu} + \sum_{n_F=1}^{3 \text{ or } 4} \bar{q} i \not{D} q$$

Caswell, Lepage, Phys. Lett. B, 1986
Bodwin, Braaten, Lepage, PRD, 1995

$$\mathcal{L}_{\text{heavy}} = \psi^\dagger \left(iD_t + \frac{\mathbf{D}^2}{2M} \right) \psi + \chi^\dagger \left(iD_t - \frac{\mathbf{D}^2}{2M} \right) \chi$$

Pauli spinor for antiquark

$$\begin{aligned} \delta\mathcal{L}_{\text{bilinear}} = & \frac{c_1}{8M^3} \left(\psi^\dagger (\mathbf{D}^2)^2 \psi - \chi^\dagger (\mathbf{D}^2)^2 \chi \right) \\ & + \frac{c_2}{8M^2} \left(\psi^\dagger (\mathbf{D} \cdot g\mathbf{E} - g\mathbf{E} \cdot \mathbf{D}) \psi + \chi^\dagger (\mathbf{D} \cdot g\mathbf{E} - g\mathbf{E} \cdot \mathbf{D}) \chi \right) \\ & + \frac{c_3}{8M^2} \left(\psi^\dagger (i\mathbf{D} \times g\mathbf{E} - g\mathbf{E} \times i\mathbf{D}) \cdot \boldsymbol{\sigma} \psi + \chi^\dagger (i\mathbf{D} \times g\mathbf{E} - g\mathbf{E} \times i\mathbf{D}) \cdot \boldsymbol{\sigma} \chi \right) \\ & + \frac{c_4}{2M} \left(\psi^\dagger (g\mathbf{B} \cdot \boldsymbol{\sigma}) \psi - \chi^\dagger (g\mathbf{B} \cdot \boldsymbol{\sigma}) \chi \right), \end{aligned}$$

Pauli spinor for heavy quark

□ **Limitation:**

Powerful for a process with available kinetic energy: $Mv^2 \ll Mc^2$

✧ Formalism is ideal for heavy quarkonium decay

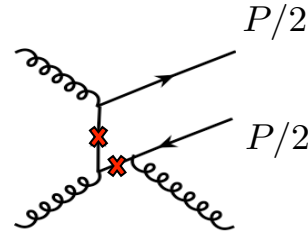
✧ Additional complications for production with $s \gg (2M)^2$

Why high orders in CSM are so large?

Kang, Qiu and Sterman, 2011

- LO in α_s but higher power in $1/p_T$:

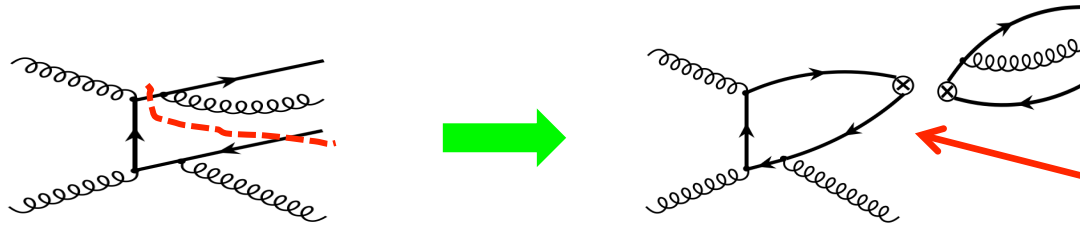
LO in α_s :



$$\hat{\sigma}^{\text{LO}} \propto \frac{\alpha_s^3(p_T)}{p_T^8}$$

CSM and NRQCD
spin-1 projection
NNLP in $1/p_T$!

- NLO in α_s but lower power in $1/p_T$:

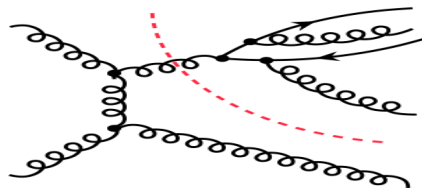


Relativistic
projection to
all
“spin states”

$$\hat{\sigma}^{\text{NLO}} \rightarrow \frac{\alpha_s^3(p_T)}{p_T^6} \otimes \alpha_s(\mu) \log(\mu^2 / \mu_0^2)$$

$$\mu_0 \gtrsim 2m_Q$$

- NNLO in α_s but leading power in $1/p_T$:



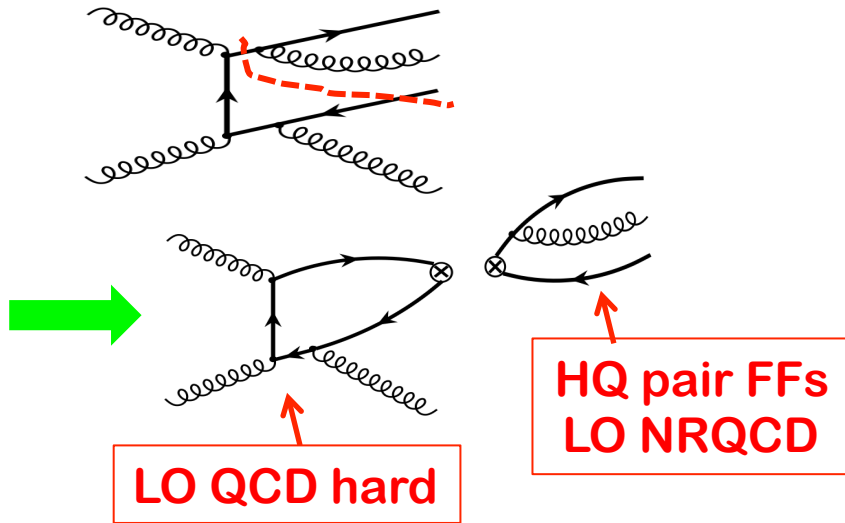
$$\hat{\sigma}^{\text{NNLP}} \rightarrow \frac{\alpha_s^2(p_T)}{p_T^4} \otimes \alpha_s^3(\mu) \log^m(\mu^2 / \mu_0^2)$$

Leading order in α_s -expansion \neq leading power in $1/p_T$ -expansion!

QCD factorization + NRQCD factorization

Kang, Qiu and Sterman, 2011

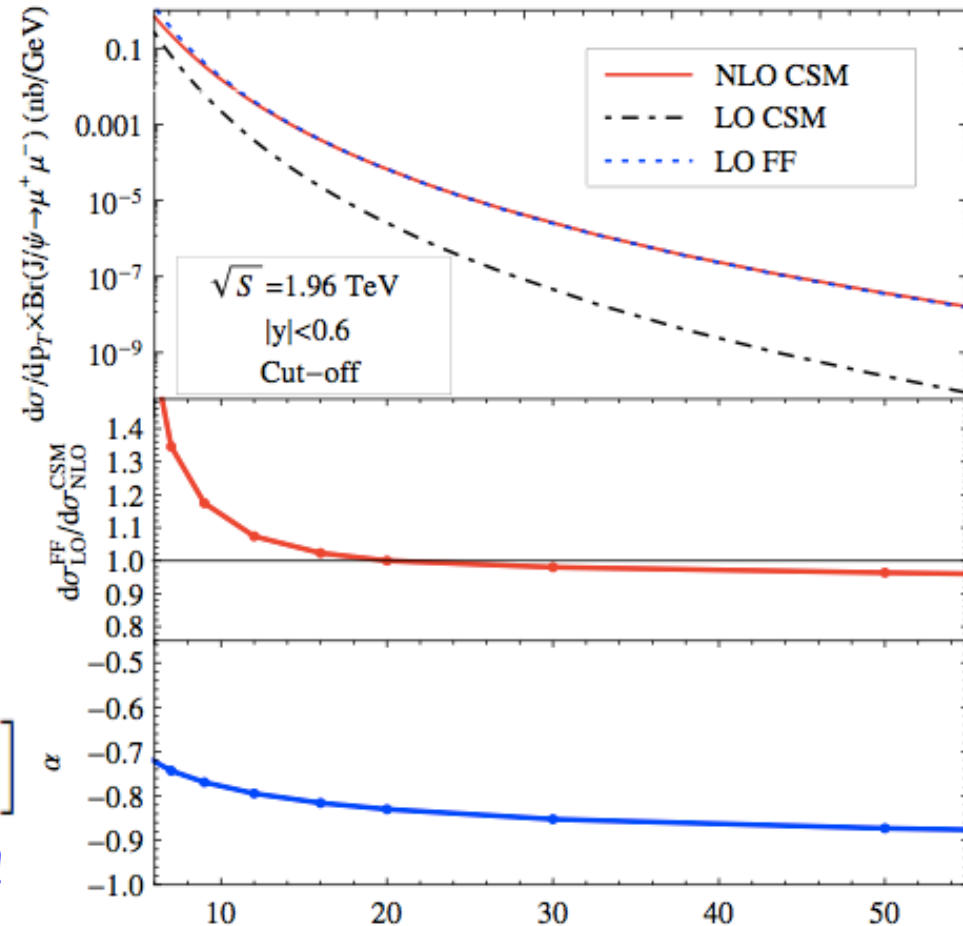
Color singlet as an example:



$$\sigma_{\text{NRQCD}}^{(\text{NLO})} \propto \left[d\hat{\sigma}_{ab \rightarrow [Q\bar{Q}(v8)]}^{A(\text{LO})} \otimes \mathcal{D}_{[Q\bar{Q}(v8)] \rightarrow J/\psi}^{(\text{LO})} + d\hat{\sigma}_{ab \rightarrow [Q\bar{Q}(a8)]}^{S(\text{LO})} \otimes \mathcal{D}_{[Q\bar{Q}(a8)] \rightarrow J/\psi}^{(\text{LO})} \right]$$

Reproduce NLO CSM for $p_T > 10$ GeV!

Cross section + polarization

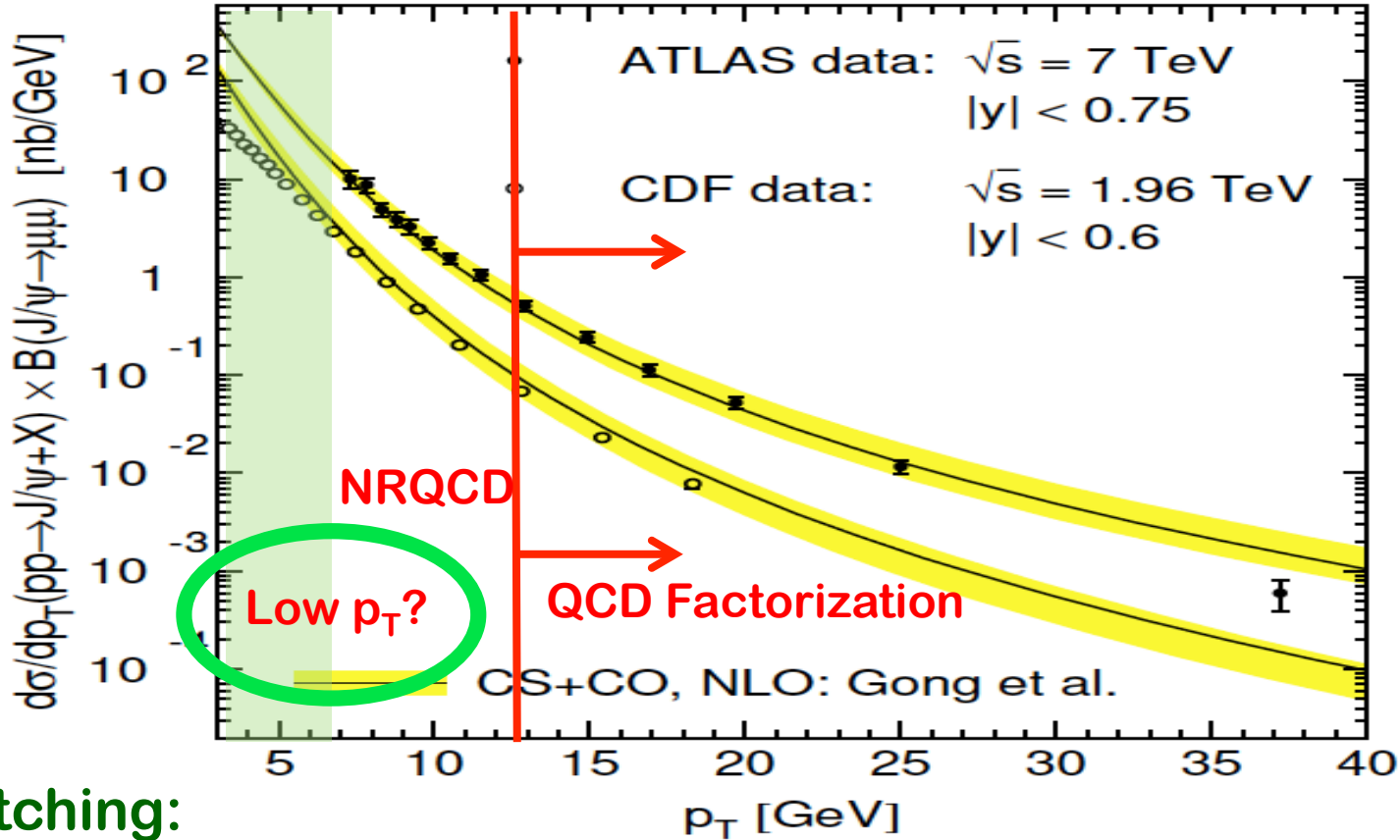


*Different kinematics, different approximation,
Dominance of different production channels!*

Matching between different approaches

Kang, Ma, Qiu and Sterman, 2014

Expectation:



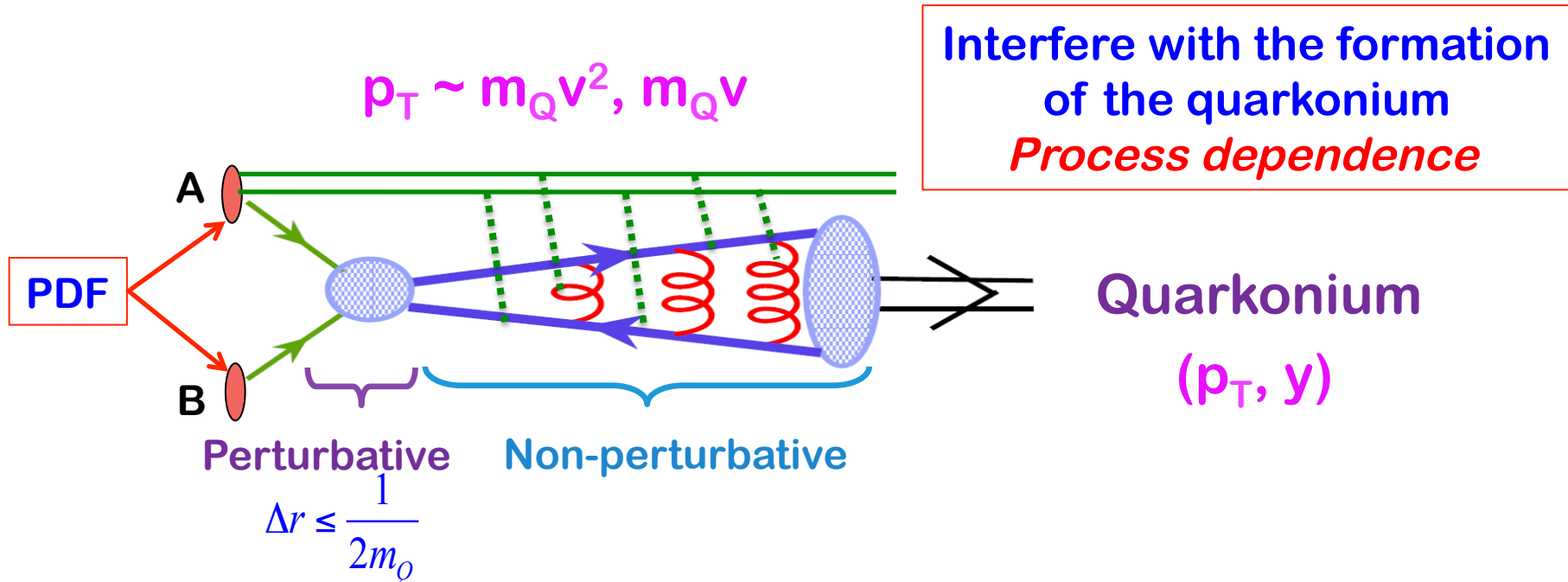
Matching:

$$E_P \frac{d\sigma_{A+B \rightarrow H+X}}{d^3P}(P, m_Q) \equiv E_P \frac{d\sigma_{A+B \rightarrow H+X}^{\text{QCD}}}{d^3P}(P, m_Q = 0) + E_P \frac{d\sigma_{A+B \rightarrow H+X}^{\text{NRQCD}}}{d^3P}(P, m_Q \neq 0) - E_P \frac{d\sigma_{A+B \rightarrow H+X}^{\text{QCD-Asym}}}{d^3P}(P, m_Q = 0)$$

Mass effect + expanded P_T region ($P_T \gtrsim m_Q$)

Production at low p_T ($< M_Q$)

- Spectator interaction – always there:



- The Challenge:

Break factorization – Process dependence – Alter p_T distribution, ...

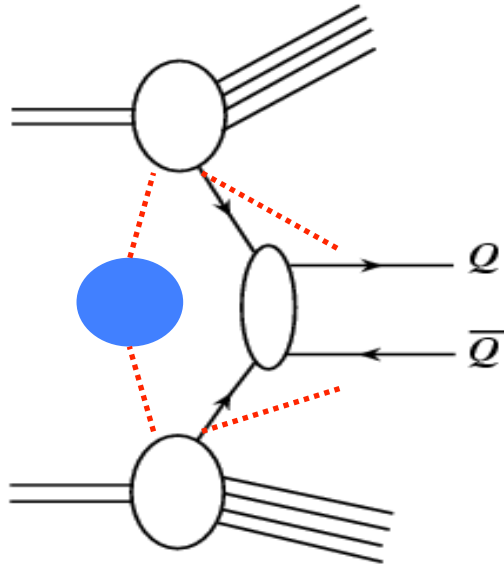
- Understand the factorization breaking:

If the breaking effect is controllable, we still have predictive power!

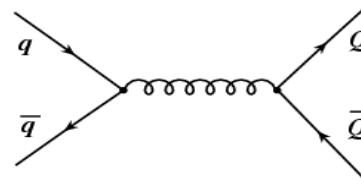
Even the Drell-Yan process is NOT fully factorizable!

Production at low p_T ($< M_Q$)

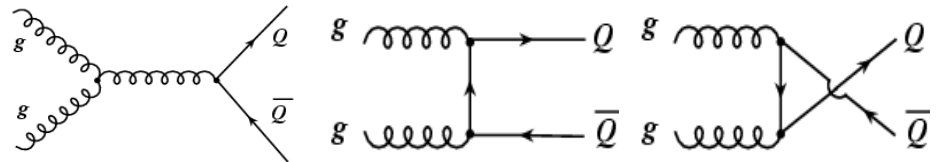
□ Gluon shower – Sudakov resummation dominated?



✧ Quark-antiquark channel:



✧ Gluon-gluon channel:



□ Assumption:

Leading double logarithms from the gluon shower are from initial-state active partons



Mimic the Drell-Yan type radiation pattern,
Resum the leading soft radiation into Sudakov form factor

Upsilon production at hadron colliders

□ CSS formalism (the b-space approach to low P_T region):

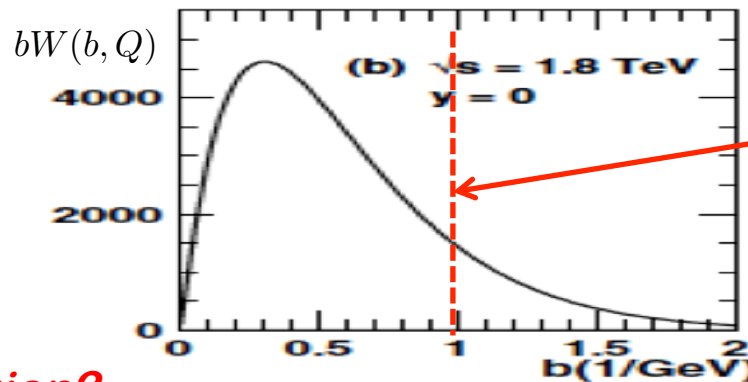
Use Drell-Yan as an example:

$$\begin{aligned} \frac{d\sigma_{AB}^{DY}}{dQ^2 dq_T^2}(Q, q_T, x_A, x_B) &= \hat{H}_{f\bar{f}}(Q) \otimes \Phi_{f/A}(x_A, k_{a\perp}) \otimes \Phi_{\bar{f}/B}(x_B, k_{b\perp}) \otimes \mathcal{S}(k_{s\perp}) + Y(Q, q_T) \\ &= \frac{1}{2\pi} \int_0^\infty db J_0(bq_T) b \widetilde{W}_{AB}(b, Q; x_A, x_B) + \left[\frac{d\sigma_{AB}^{(Pert)}}{dQ^2 dq_T^2} - \frac{d\sigma_{AB}^{(Asym)}}{dQ^2 dq_T^2} \right] \end{aligned}$$

The b-space distribution:

$$\widetilde{W}_{AB}^{Pert}(b, Q; x_A, x_B) = \hat{H}_{f\bar{f}}(Q) \left[C_{f/a} \otimes \Phi_{a/A}(x_A, 1/b) \right] \otimes \left[C_{\bar{f}/b} \otimes \Phi_{b/B}(x_B, 1/b) \right] e^{-S(b, Q)}$$

Predictive power:
very sensitive to
the role of
non-perturbative
contribution!



**Ratio of areas
large b vs. small b
Nonperturbative
Vs. perturbative**

The role of large-b region?

Good predictive power (not sensitive to the large-b region):

if the area under the b-space distribution is dominated by small-b region!

Upsilon production at hadron colliders

- Expect good predictive power:

Peak of p_T -distribution is around 4 GeV
 >> intrinsic p_T
 >> the Q_s at this energies

Shower is the dominant source to the observed large p_T

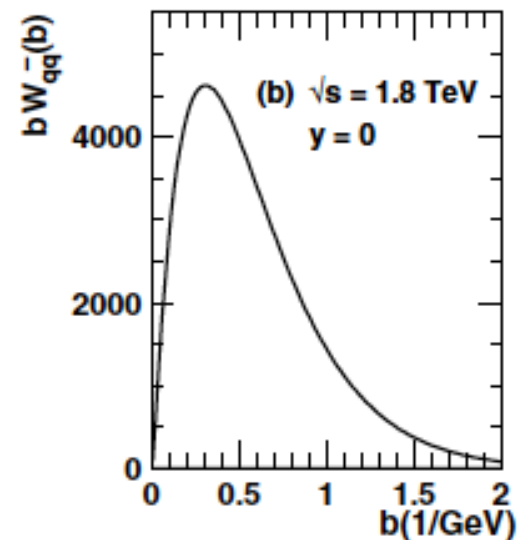
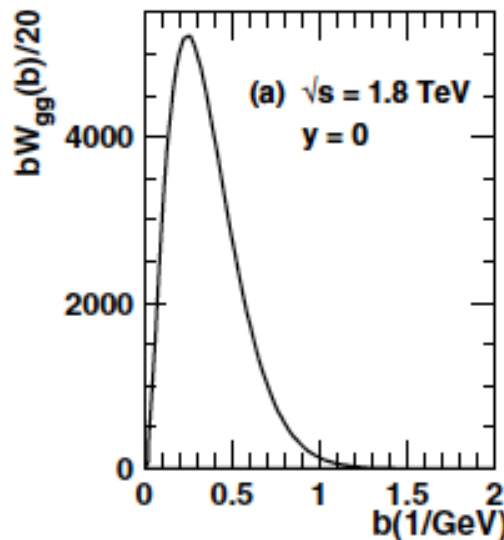
- Matching procedure to large- b region:

$$W_{ij}(b, Q, x_A, x_B) = \begin{cases} W_{ij}^{\text{pert}}(b, Q, x_A, x_B) & b \leq b_{\text{max}} \\ W_{ij}^{\text{pert}}(b_{\text{max}}, Q, x_A, x_B) F_{ij}^{\text{NRP}}(b, Q; b_{\text{max}}) & b > b_{\text{max}} \end{cases}$$

$$F_{ij}^{\text{NRP}} = \exp \left\{ - \ln \left(\frac{Q^2 b_{\text{max}}^2}{c^2} \right) \left\{ g_1 [(b^2)^\alpha - (b_{\text{max}}^2)^\alpha] + g_2 (b^2 - b_{\text{max}}^2) \right\} - \bar{g}_2 (b^2 - b_{\text{max}}^2) \right\}$$

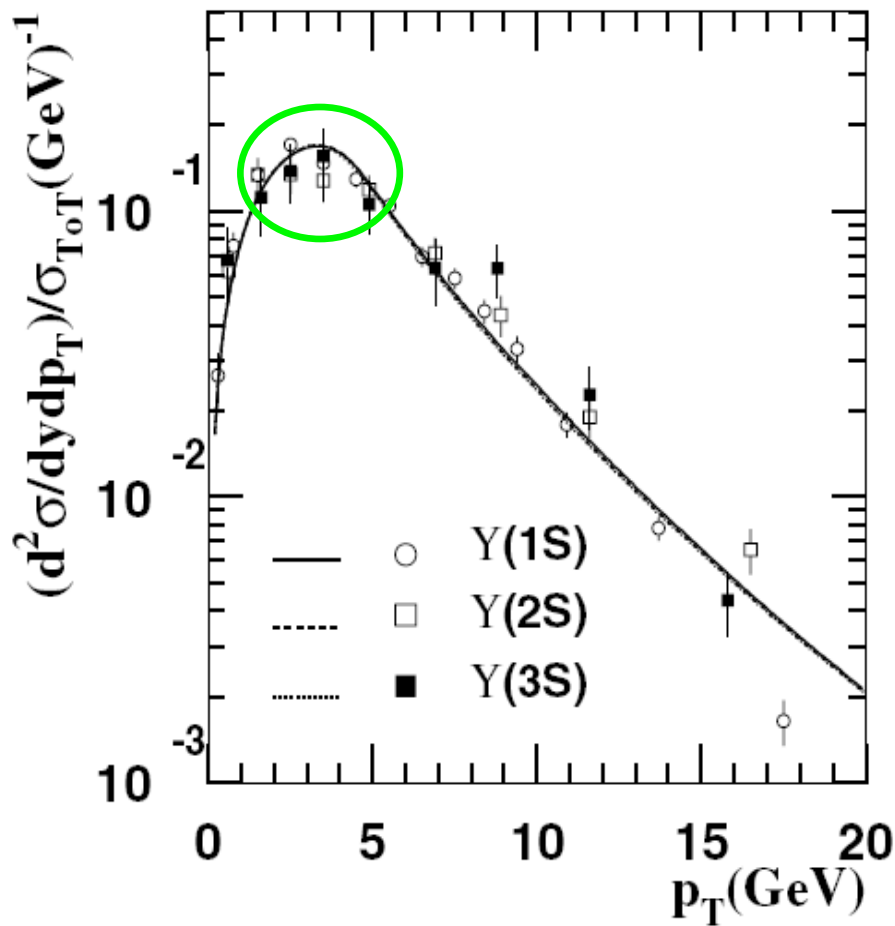
- b -space distribution for Upsilon production at Tevatron energy:

All parameters fixed by the derivatives to be continuous at $b = b_{\text{max}}$.

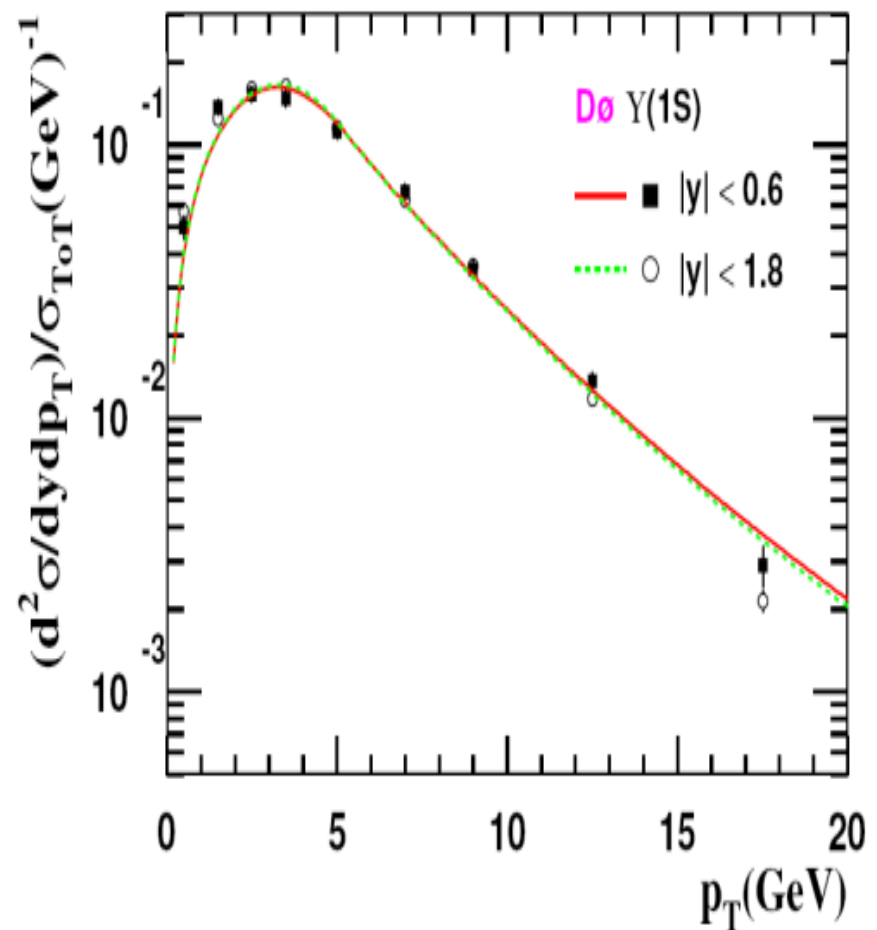


Upsilon production at hadron colliders

CDF Run-I



D0 Run-II



□ Strong gluon shower:

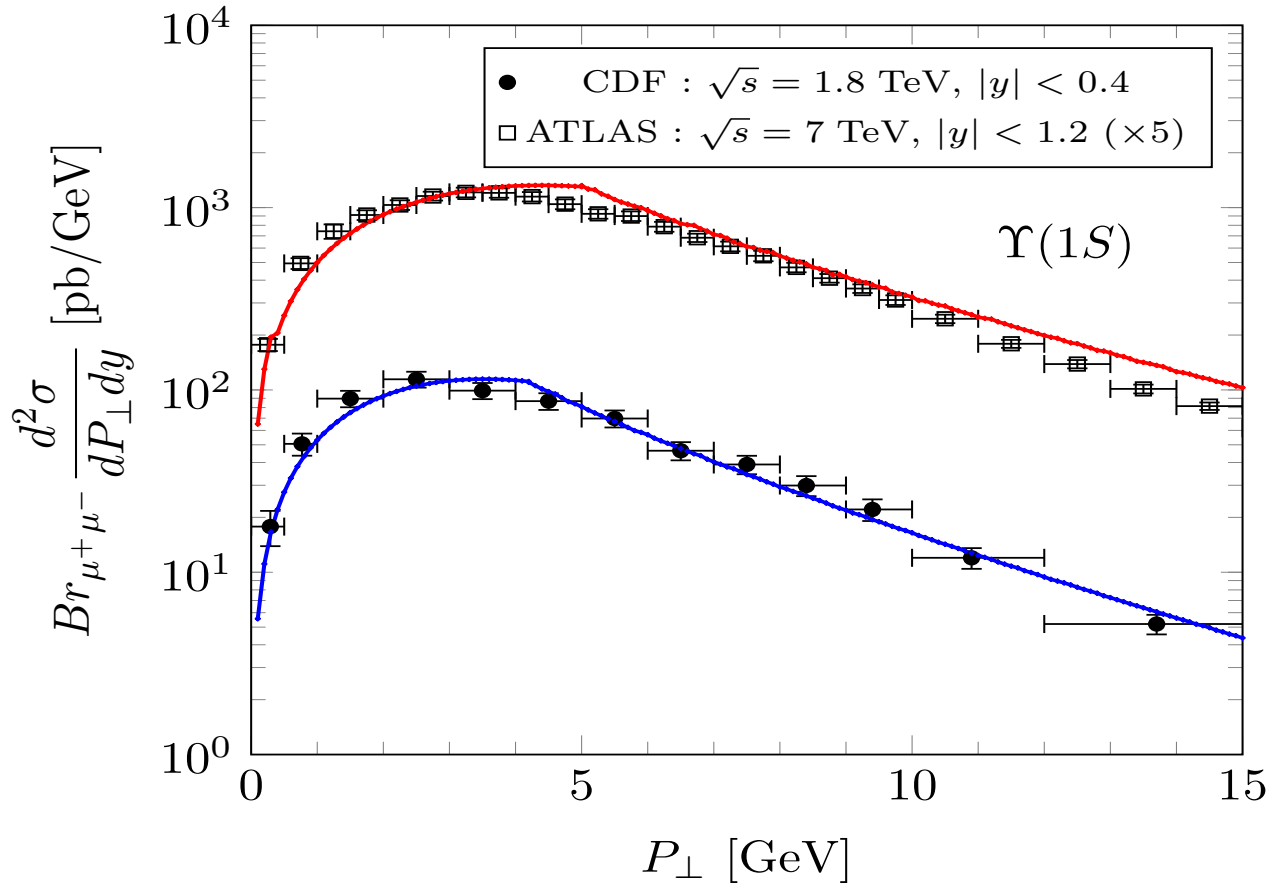
Berger, Qiu, Wang, 2005

Sufficiently large Q (Upsilon mass) + large shower phase space!

Predictive power – Upsilon

Qiu, Watanabe, 2017

□ Upsilon at the LHC:



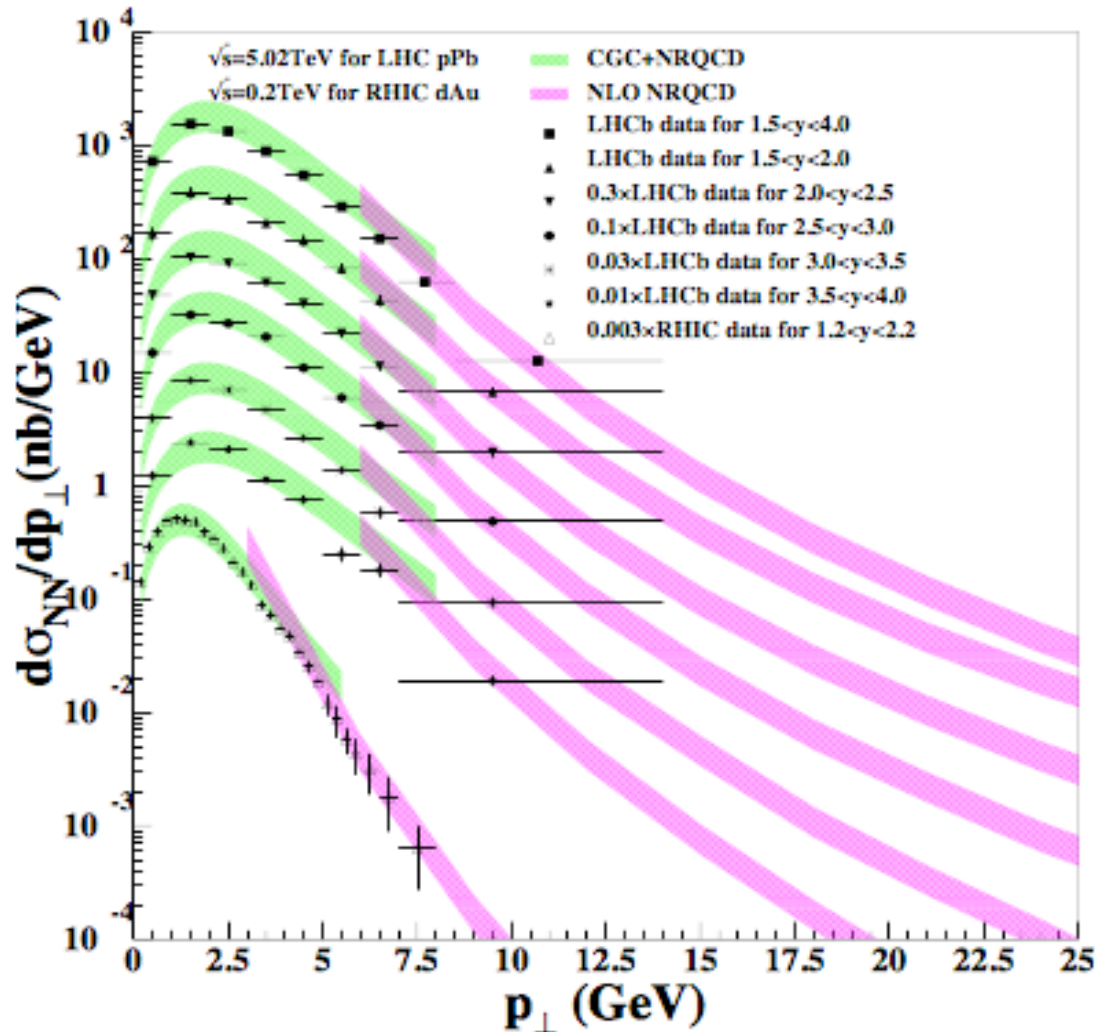
No adjustment on any parameter from Tevatron to the LHC!

BUT: this does not apply for J/ψ at low PT,
logarithmic contribution from the shower is not strong enough!

Forward quarkonium production in p(d)+A

CGC for low p_T region:

Ma et al. Phys.Rev. D92 (2015) 071901



Two free fitted parameters:
transverse overlap area,
saturation scale at initial
rapidities
seem reasonable

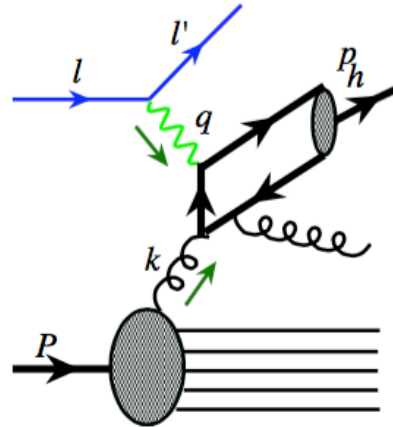
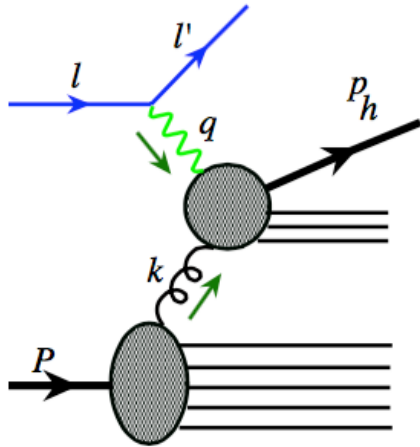
Matching to NLO NRQCD
calculation,
modulo small
shadowing effect,
seem to be smooth

Better agreement with
data than previous CGC
calculations

To understand what we could calculate, test, and learn at EIC energies!

Heavy quarkonium production at EIC

□ Semi-inclusive DIS:



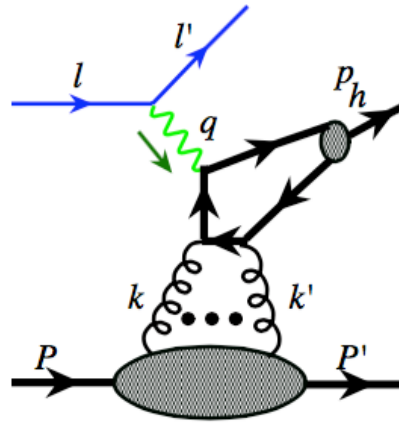
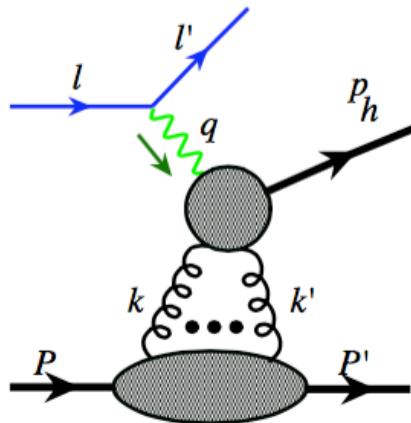
Low P_T : **Glue TMD ?**
CGC ?

Shower vs.
multiple scattering

$P_T \sim Q$: **Glueon PDF**

High P_T : **LP +NLP**
FFs

□ Exclusive / Gap:



$$\frac{d\sigma}{dt}(x_B, Q^2) \propto \text{GPDs}$$

Imaging gluon
density distribution

$$\frac{d\sigma}{dt}(x_B, Q^2)$$

Near threshold

\propto Trace Anomaly?

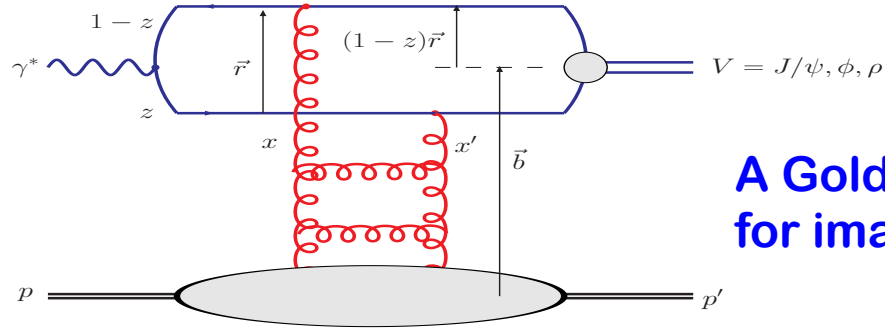
On-going effort, ...

One facility covers all issues of quarkonium production!

Critical role of J/ψ production at EIC

EIC WP, 1212.1701

❑ Exclusive:



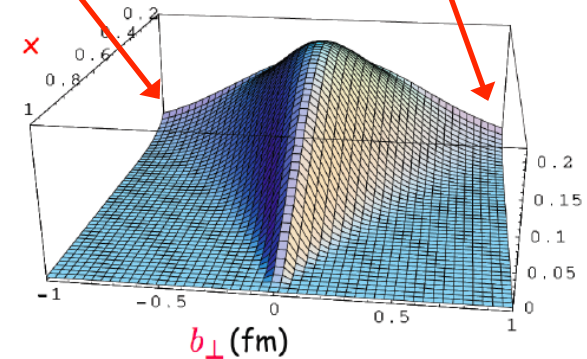
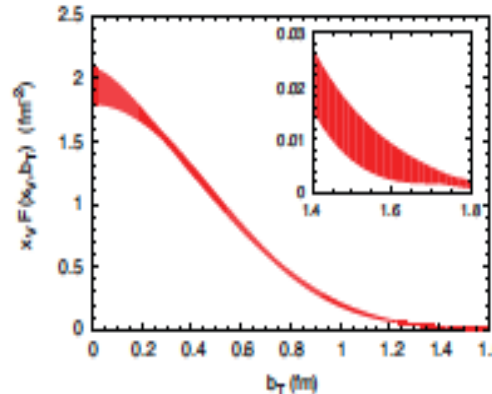
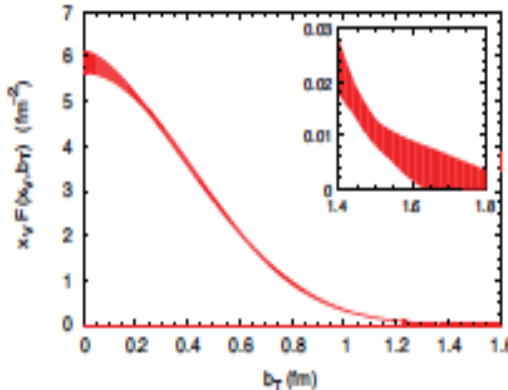
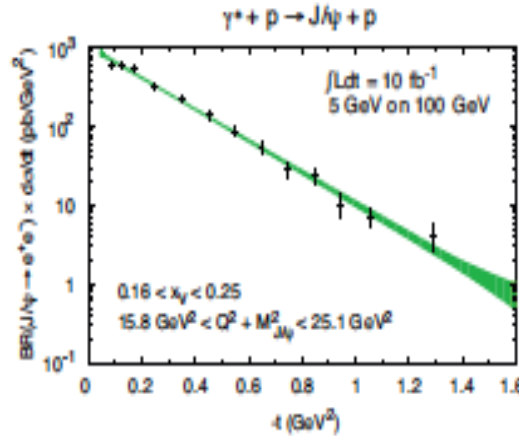
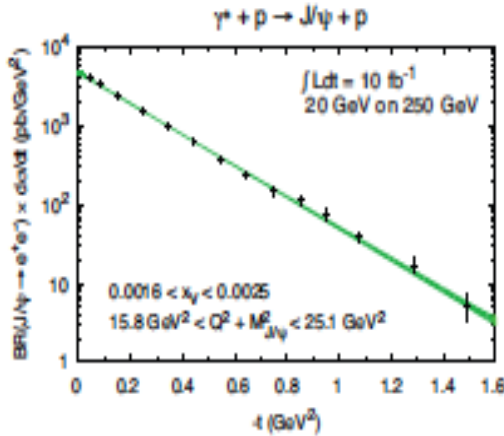
A Golden process for imagining gluon

Allow us to ask “new” fundamental questions:

Color confining radius?

How far does glue density spread?

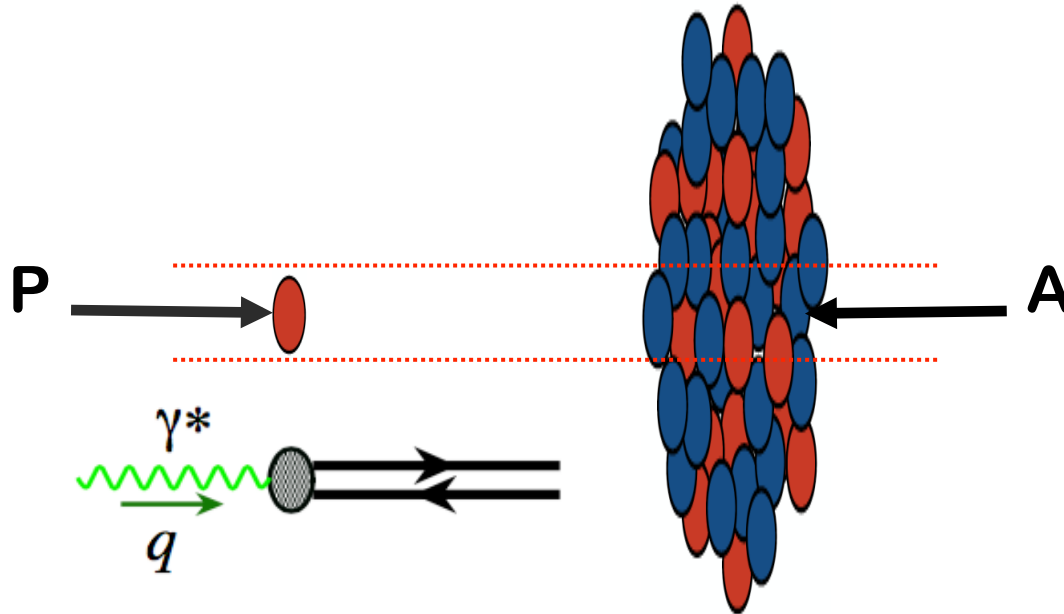
How fast does glue density fall?



Can A be a bigger P at small-x?

What have we learned from p+A collisions?

□ Proton (deuteron) – Nucleus Collisions:

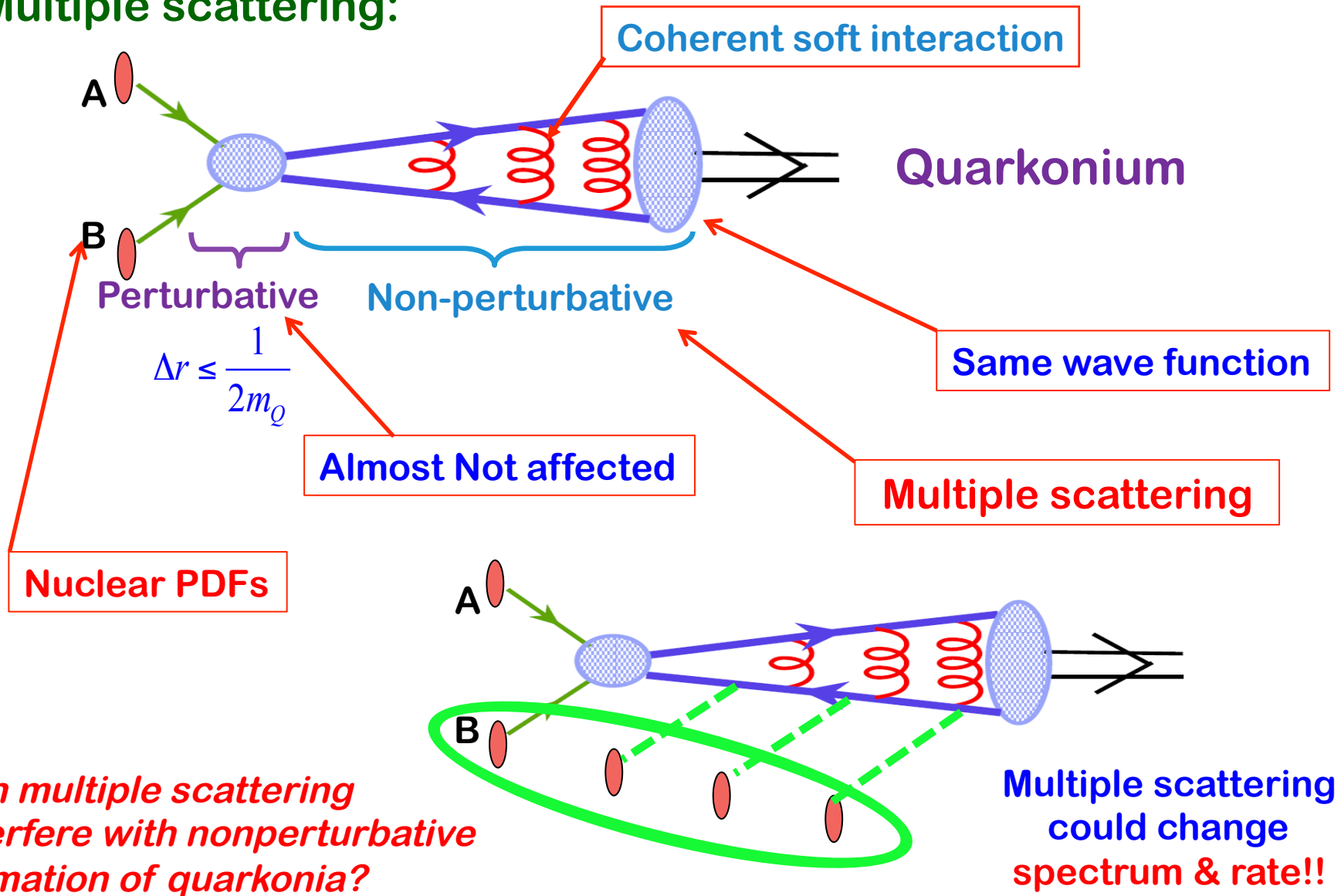


- ✧ NO QGP ($m_Q \gg T$)! → Cold nuclear effect for the “production”
- ✧ Nuclei as potential filters of production mechanisms
- ✧ Hard probe ($m_Q \gg 1/\text{fm}$) → quark-gluon structure of nucleus!

Nucleus is not a simple superposition of nucleons!

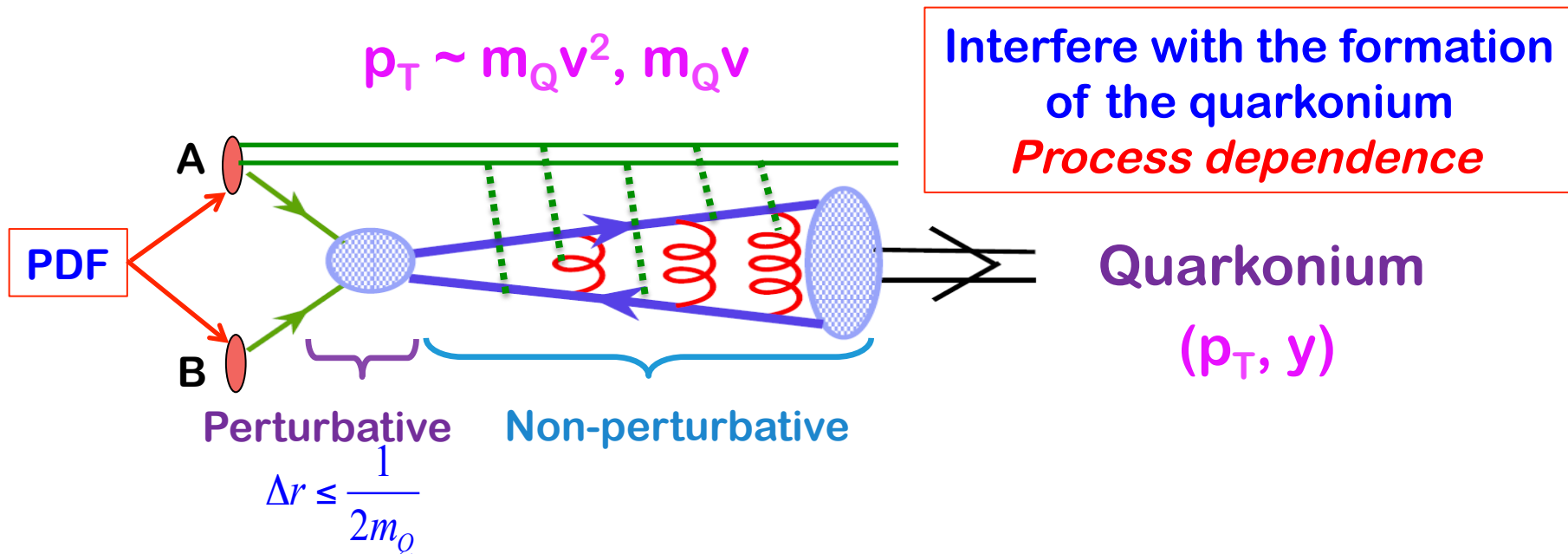
Production in p(d)+A collisions

Multiple scattering:



Production at low p_T ($< M_Q$)

- **Spectator interaction** – always there for $p+A$, but, not for $e+A$!



- **The Challenge:**

Process dependence – Break of factorization – No predictive power

- **The need:**

Controllable calculation of medium effect, extract medium properties, ...

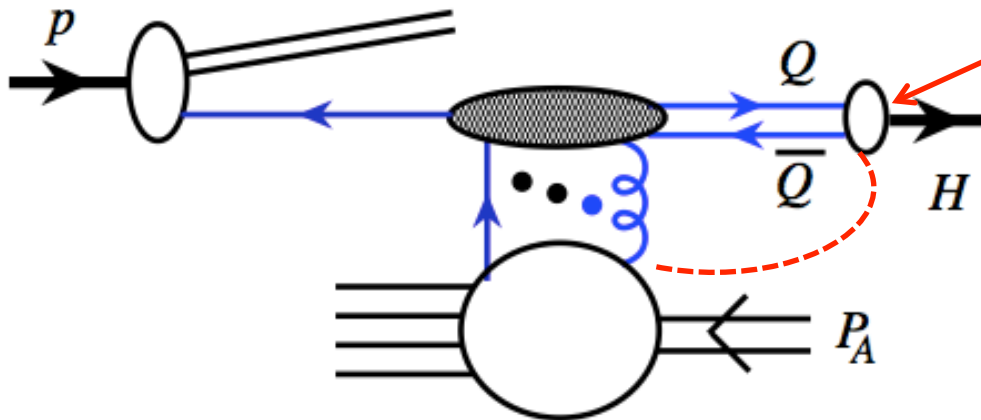
- **The Opportunities:**

Medium as a “detector” or “filter” to probe “color neutralization”, ...

Production with multiple scattering

Brodsky and Mueller, PLB 1988

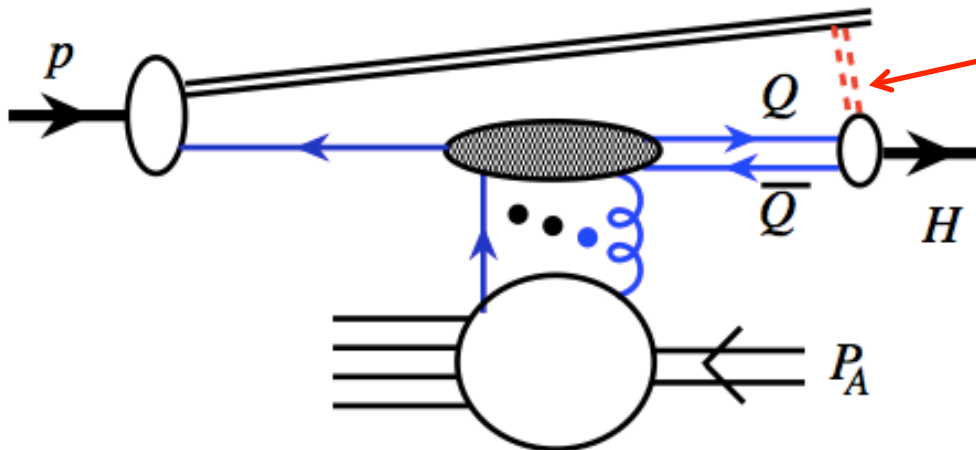
□ *Backward* production in p(d)+A collisions:



*J/ψ could be formed
Inside nucleus*

*Multiple scattering interfere
with the non-perturbative
hadronization
- no factorization!!*

□ Production at low $P_T (\rightarrow 0)$ in p(d)+A collisions:



Co-mover interaction

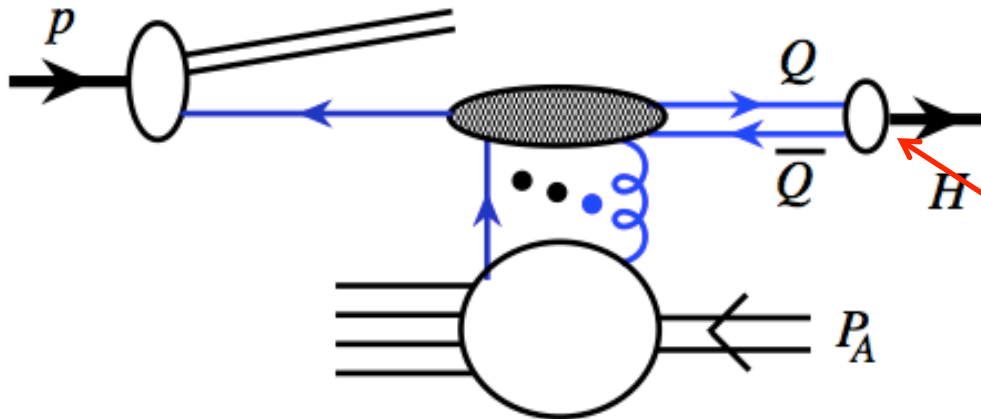
*to interfere with
quarkonium formation
- Break of factorization!!*

NOT a problem for e+A!

Production with multiple scattering

Brodsky and Mueller, PLB 1988

□ *Forward* production in p(d)+A collisions:



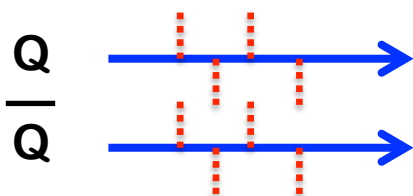
✧ Time dilation

Non-perturbative formation of J/ψ is far outside of nucleus

✧ SAME for e+A!

✧ Multiple scattering between partons & heavy quarks, not J/ψ

- ◆ Induced gluon radiation – energy loss – **suppression at large y**
- ◆ Modified P_T spectrum – **transverse momentum broadening**
- ◆ De-coherence of the pair – different $Q\bar{Q}$ state to hadronize – **lower rate**



Soft multiple scattering – “random walk”

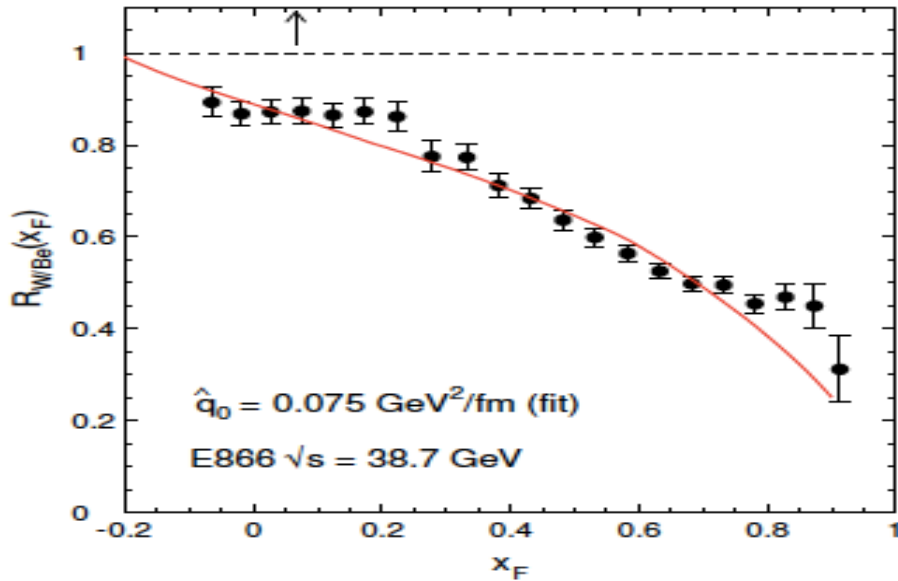


Momentum imbalance – larger invariant mass

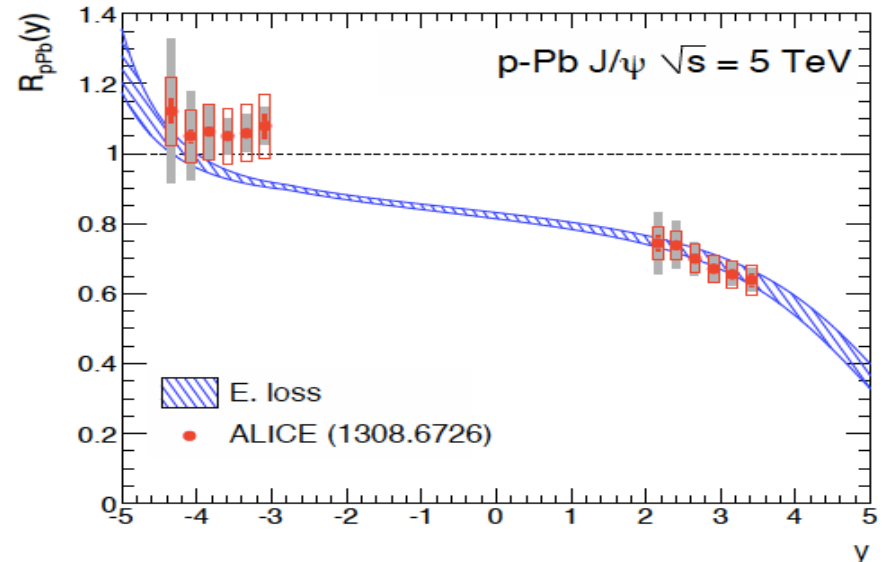
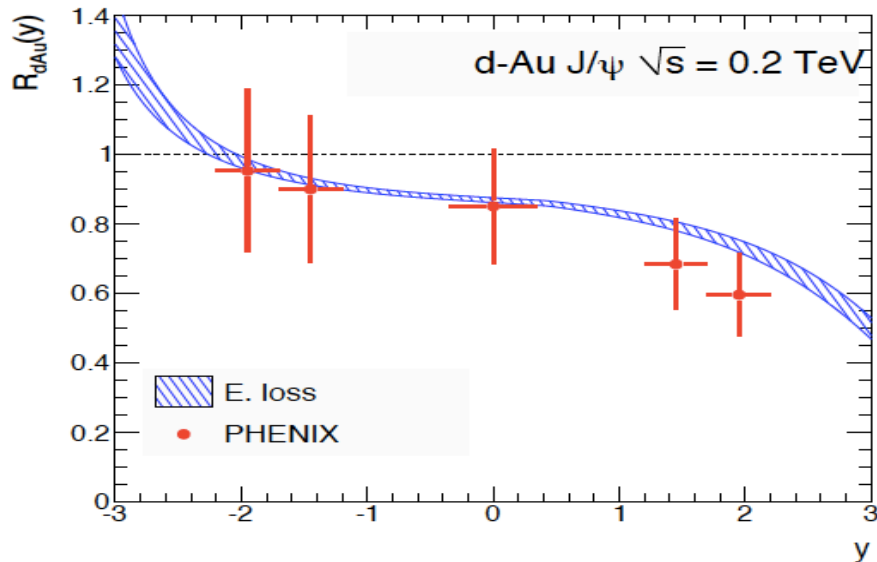
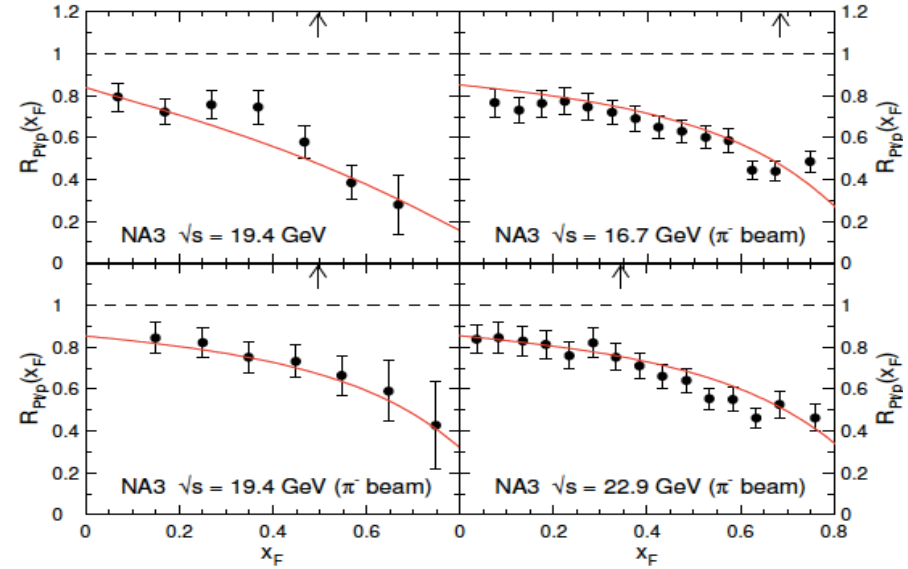


Match to the tail of wave function - “suppression”

A-dependence in rapidity y (x_F) in p+A



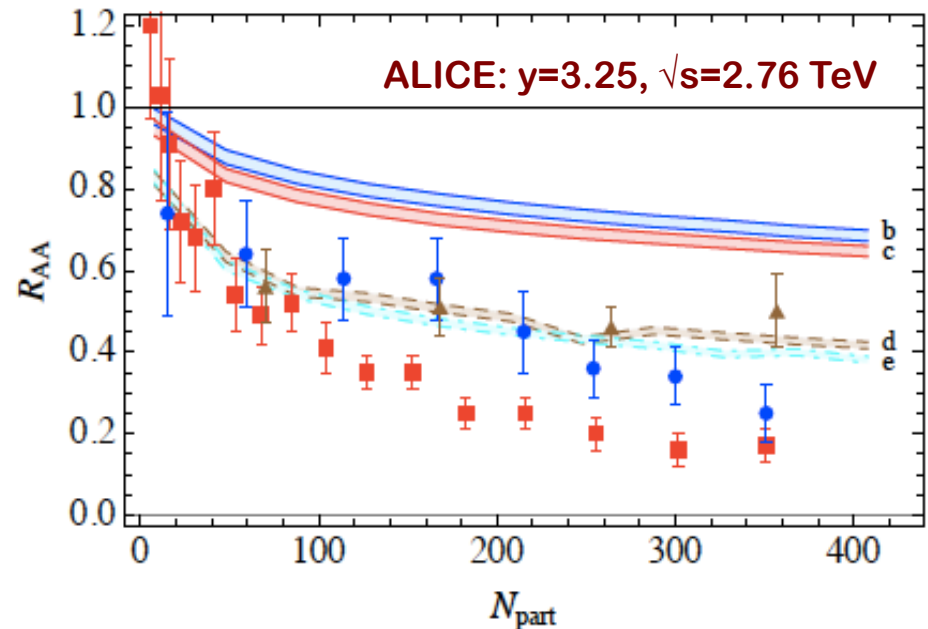
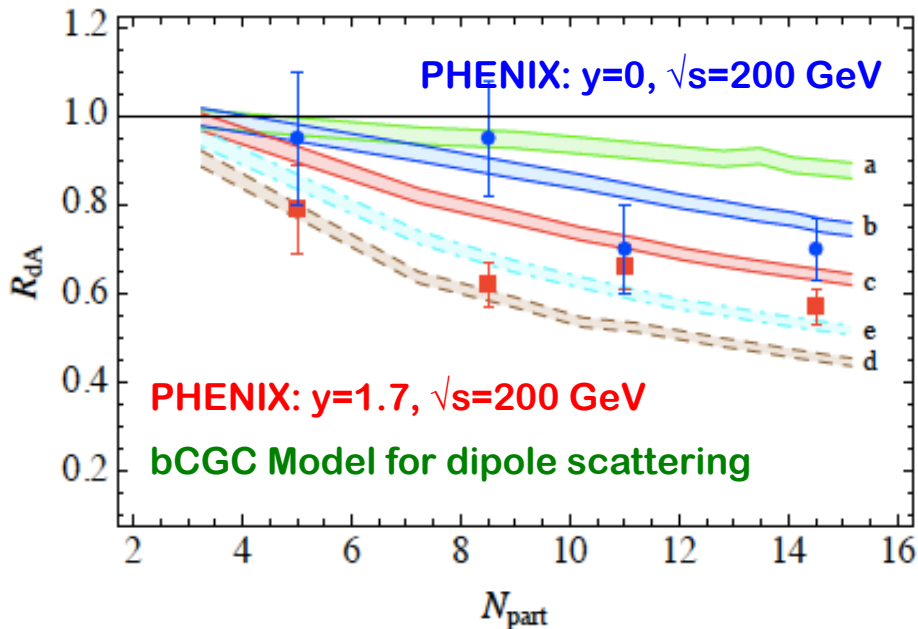
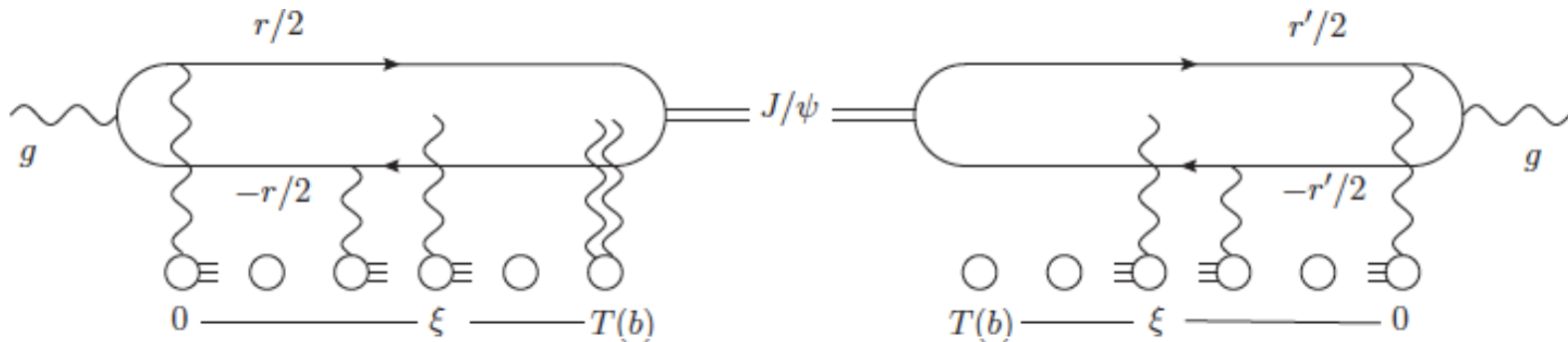
Arleo, Peigne, 2012, Arleo, Kolevatov, Peigne, 2014



Multiple scattering in pA collisions

Dominguez, Kharzeev, Levin, Mueller, and Tuchin, 2011

$$\frac{d\sigma_{pA \rightarrow J/\psi X}}{d^2b dy} = x_1 G(x_1, m_c^2) \frac{d\sigma_{gA \rightarrow J/\psi X}}{d^2b}$$

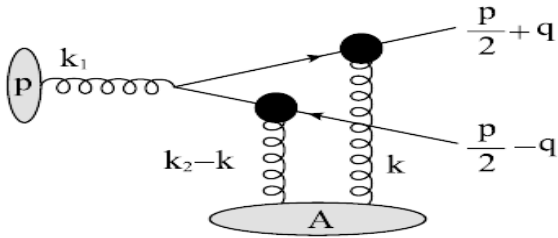


OK for pA, but, far off for AA – J/ψ melting in QGP (MS 1986)?

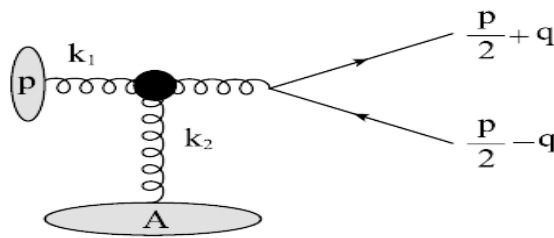
Forward quarkonium production in p(d)+A

□ Calculation of multiple scattering:

Kang, Ma, Venugopalan, JHEP (2014)
 Qiu, Sun, Xiao, Yuan PRD89 (2014)



(a)

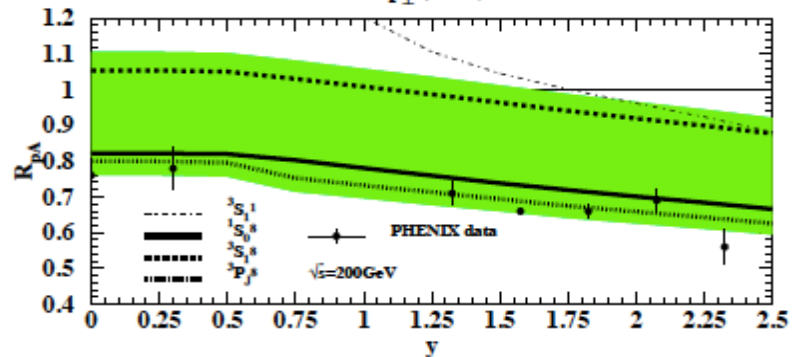
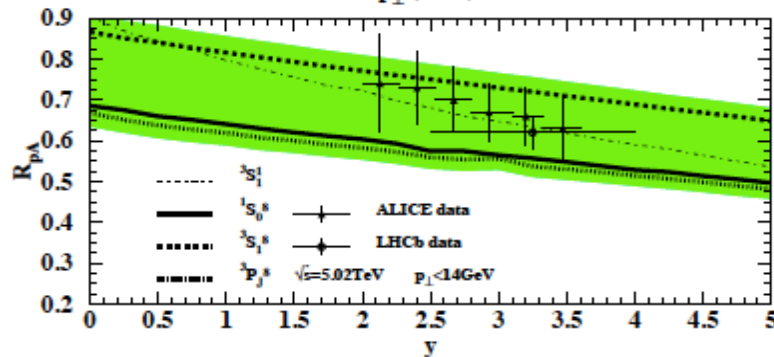
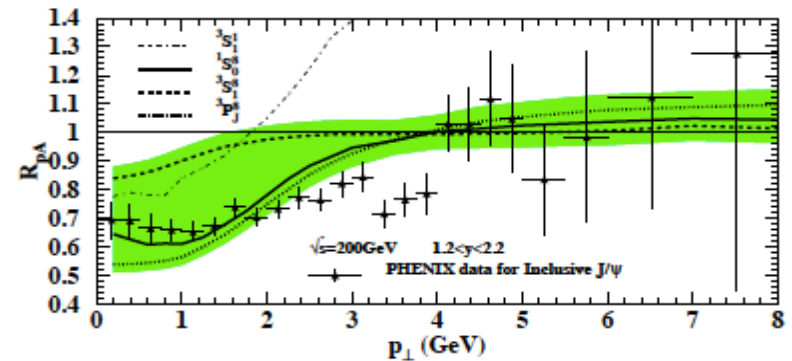
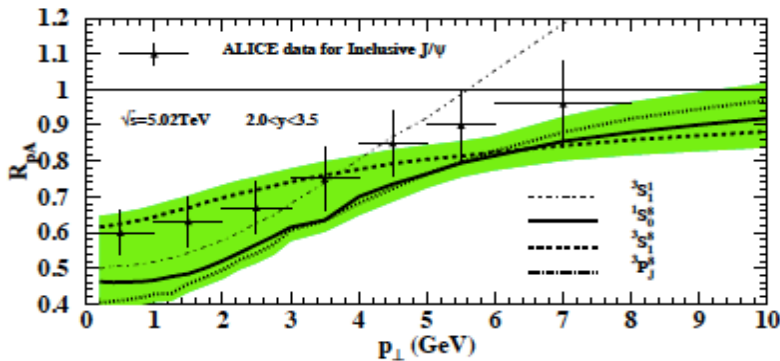


(b)

Coherent multiple scattering



suppression at large y



Ma, Venugopalan, Zhang, PRD92, 071901 (2015)

Quarkonium p_T distribution

□ Quarkonium production is dominated by low p_T region

□ Low p_T distribution at collider energies:

determined mainly by gluon shower of incoming partons

– initial-state effect

Qiu, Zhang, PRL, 2001

□ Final-state interactions suppress the formation of J/ψ :

Also modify the p_T spectrum – move low p_T to high p_T – broadening

– Final-state effect

□ Broadening:

✧ Sensitive to the medium properties

✧ Perturbatively calculable

$$\langle (q_T^2)^n \rangle = \frac{\int dq_T^2 (q_T^2)^n d\sigma/dq_T^2}{\int dq_T^2 d\sigma/dq_T^2}$$

$$\Delta \langle q_T^2 \rangle = \langle q_T^2 \rangle_{AB} - \langle q_T^2 \rangle_{NN}$$

□ R_{pA} at low q_T :

Guo, Qiu, Zhang, PRL, PRD 2002

$$R(A, q_T) \equiv \frac{1}{A} \frac{d\sigma^{hA}}{dQ^2 dq_T^2} \bigg/ \frac{d\sigma^{hN}}{dQ^2 dq_T^2} \equiv A^{\alpha(A, q_T) - 1} \approx 1 + \frac{\Delta \langle q_T^2 \rangle}{A^{1/3} \langle q_T^2 \rangle_{hN}} \left[-1 + \frac{q_T^2}{\langle q_T^2 \rangle_{hN}} \right]$$

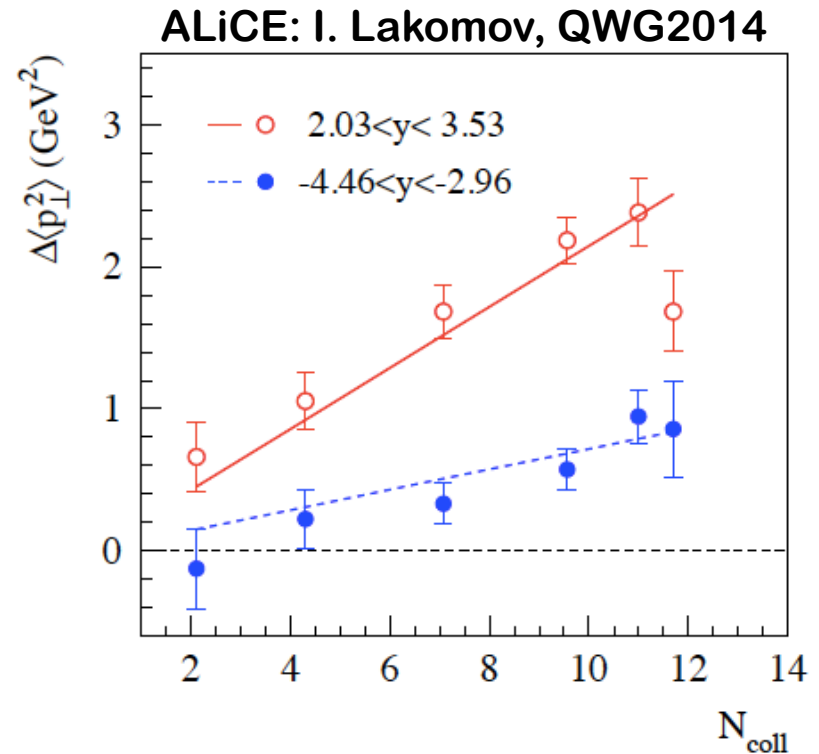
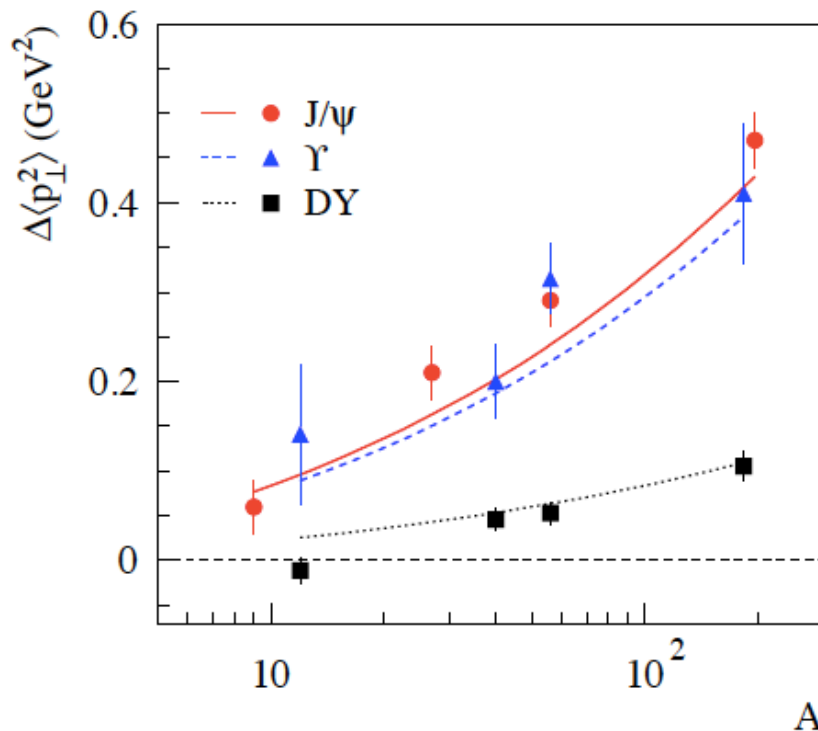
Quarkonium P_T -broadening in p(d)+A

Kang, Qiu, PRD77(2008)

□ Broadening:

$$\Delta \langle q_T^2 \rangle_{J/\psi}^{(I)} = C_A \left(\frac{8\pi^2 \alpha_s}{N_c^2 - 1} (A^{1/3} - 1) \lambda^2 \right) \approx \Delta \langle q_T^2 \rangle_{J/\psi}^{(F)} \quad \text{Calculated in both NRQCD and CEM}$$

$$\lambda^2 = \kappa \ln(Q) x^{-\delta} \propto \hat{q}, \quad \kappa = 3.51 \times 10^{-3} \text{ 1/GeV}^2, \quad \delta = 1.71 \times 10^{-1}$$

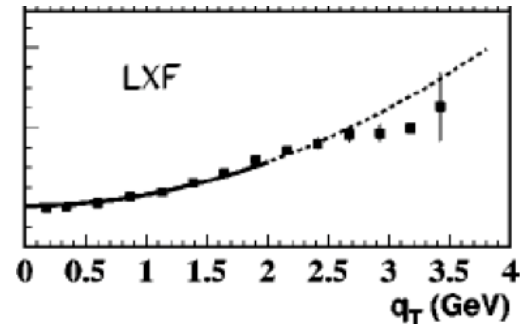
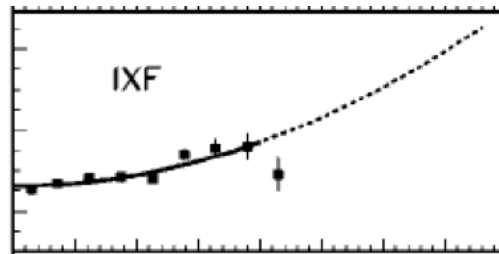
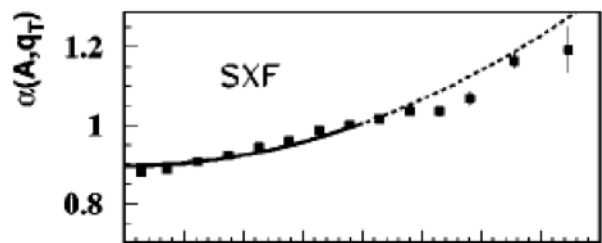


$$(A^{1/3} - 1) \rightarrow (A^{1/3} - 1) N_{\text{coll}} / N_{\text{coll}}^{\text{min.bias}}$$

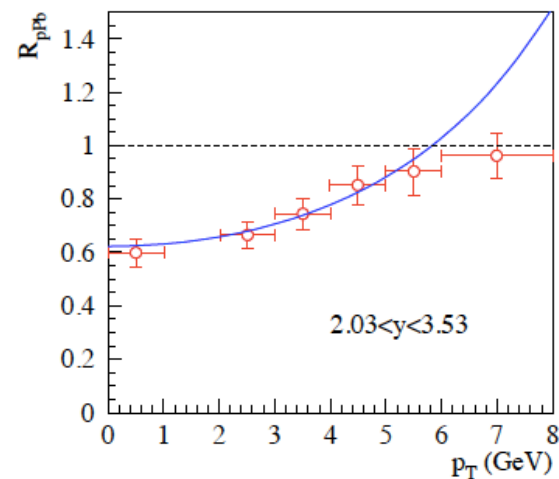
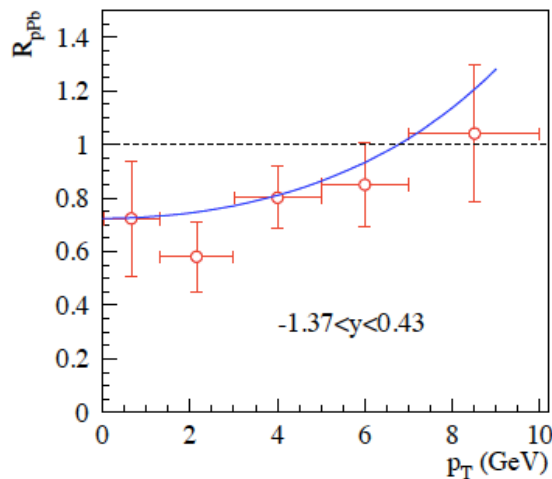
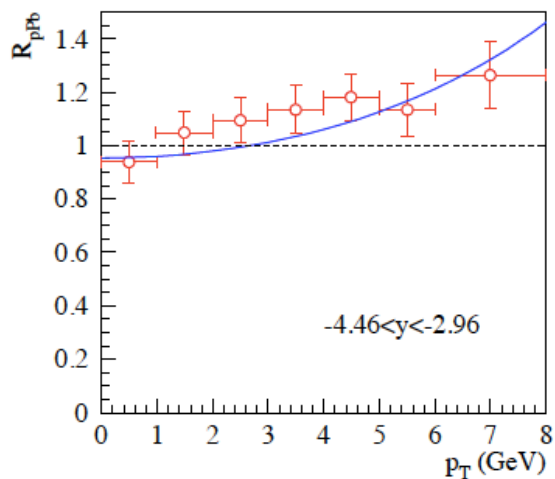
Quarkonium P_T -distribution in p(d)+A

□ Nuclear modification – low p_T region:

$$\frac{d\sigma_{AB}}{dyd^2p_T} \approx \frac{d\sigma_{AB}}{dy} \left[\frac{1}{\pi(\langle p_T^2 \rangle_{NN} + \Delta \langle p_T^2 \rangle_{AB})} e^{-p_T^2 / (\langle p_T^2 \rangle_{NN} + \Delta \langle p_T^2 \rangle_{AB})} \right]$$



E772 data – consistent with theory



ALICE data – Theory prediction

Summary

- ❑ It has been over 40 years since the discovery of J/ψ , but, still not completely sure about its production mechanism
- ❑ EIC kinematics covers all potential issues/physics of heavy quarkonium production + opportunity for the threshold production

Connection to the trace anomaly (proton mass), XYZ states, ...

- ❑ NRQCD factorization is expected to work for $P_T \sim Q$, and QCD factorization works for both LP and NLP at high P_T
Challenge for low P_T region
- ❑ Exclusive production could be a golden process for imagining glue
- ❑ Nuclear medium could be a good “filter” or a fermi-scale detector for studying how a heavy quarkonium is emerged from a pair of heavy quarks – special role of different rapidity regions

Thank you!