

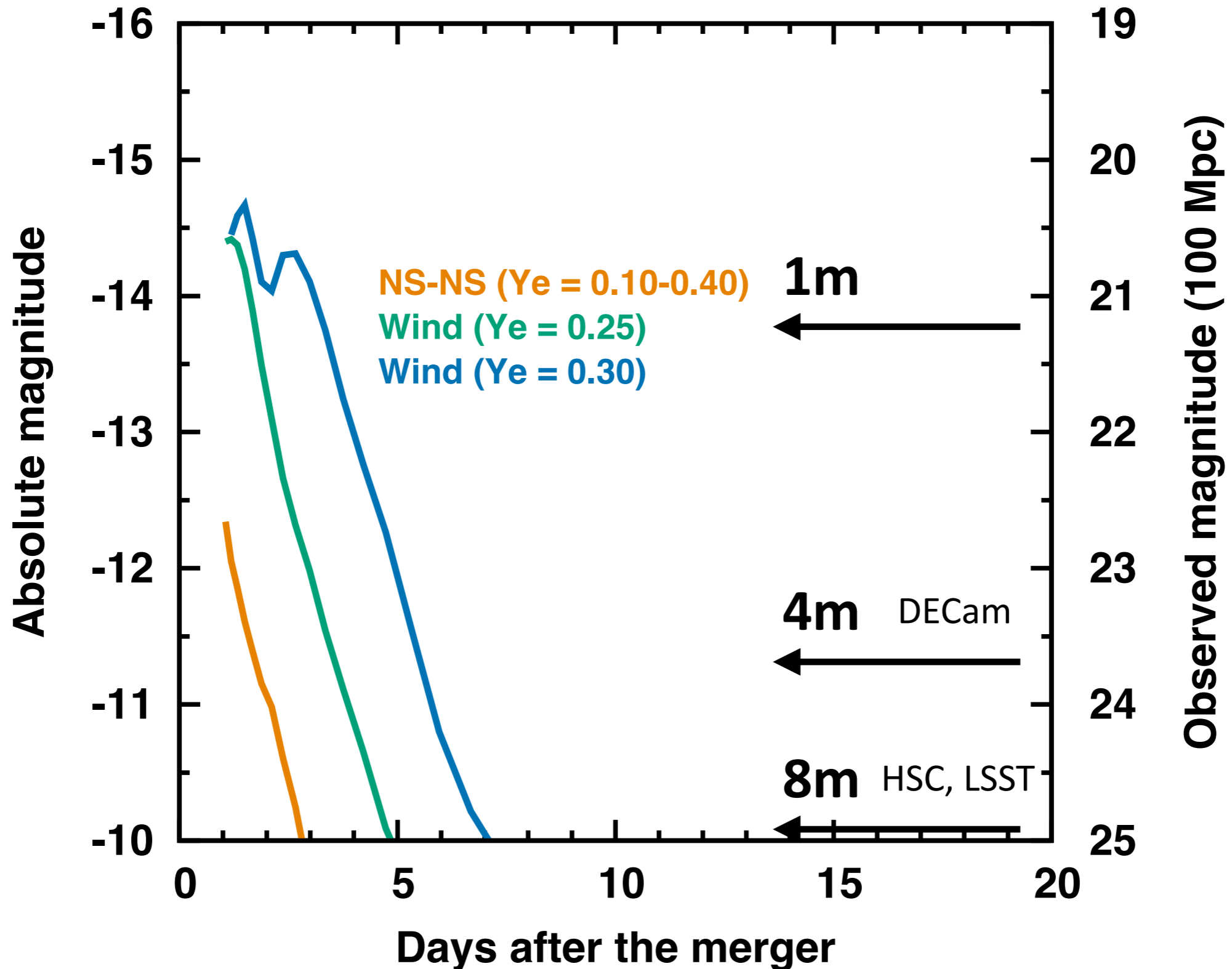
Opacities of and light curves of kilonovae

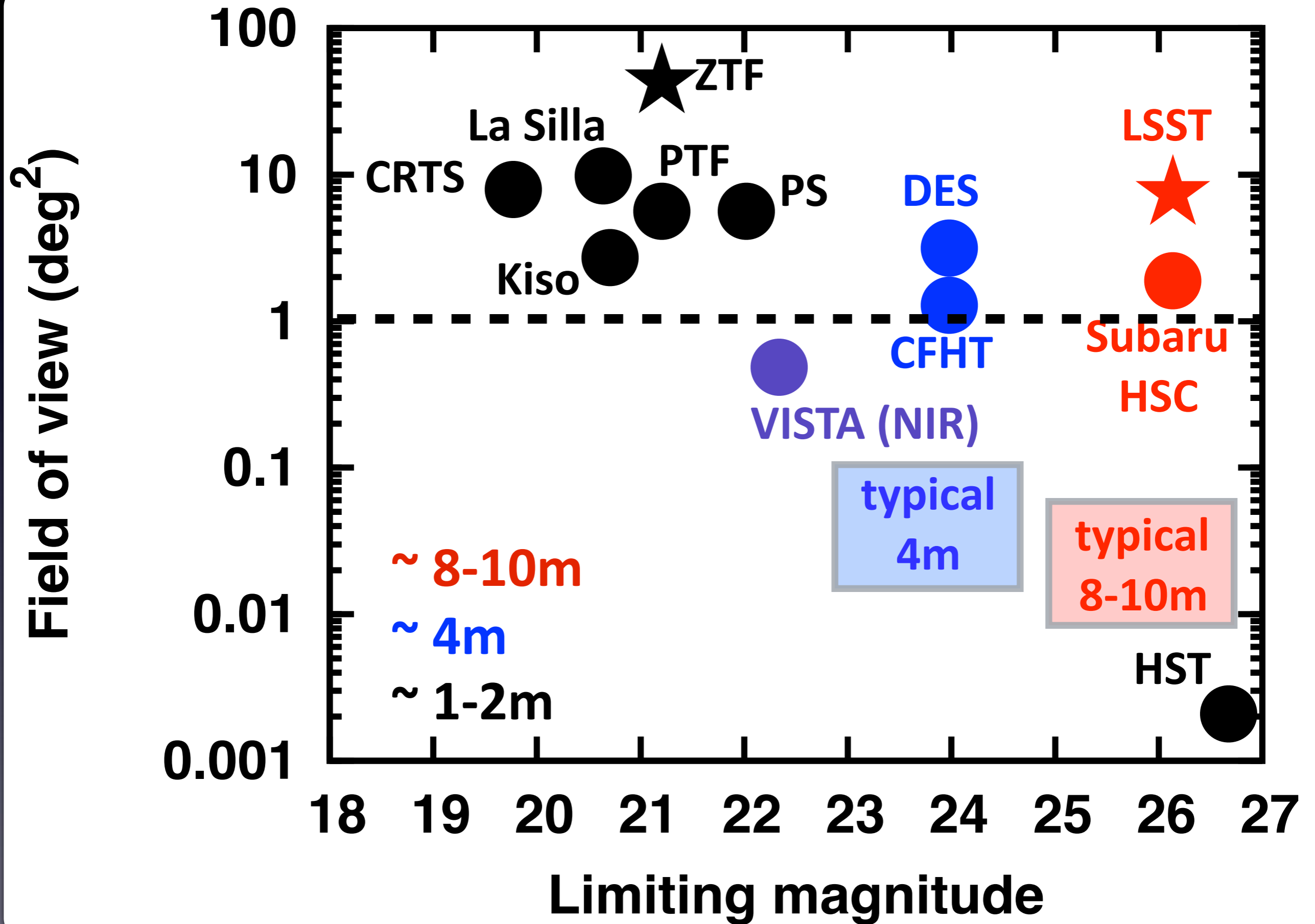
Masaomi Tanaka

(National Astronomical Observatory of Japan)

r-band magnitude @ 100 Mpc

$M_{ej} = 0.01 M_{\text{sun}}$





- Atomic and opacity calculations
- Kilonova light curves

Collaboration with

Daiji Kato (National Institute for Fusion Science, Japan),
Gediminas Gaigalas, Pavel Rynkun, Laima Radziute
(Vilnius University, Lithuania)

"Kilonova/Macronova"

Initial works: Li & Paczynski 98, Kulkarni 05, Metzger+10, Goriely+11, ...

High opacity: Kasen+13, Barnes & Kasen 13, MT & Hotokezaka 13, ...

Timescale

$$t_{\text{peak}} = \left(\frac{3\kappa M_{\text{ej}}}{4\pi c v} \right)^{1/2}$$
$$\simeq 8.4 \text{ days} \left(\frac{M_{\text{ej}}}{0.01 M_{\odot}} \right)^{1/2} \left(\frac{v}{0.1c} \right)^{-1/2} \left(\frac{\kappa}{10 \text{ cm}^2 \text{ g}^{-1}} \right)^{1/2}$$

Luminosity

$$L_{\text{peak}} = L_{\text{dep}}(t_{\text{peak}})$$
$$\simeq 1.3 \times 10^{40} \text{ erg s}^{-1} \left(\frac{M_{\text{ej}}}{0.01 M_{\odot}} \right)^{0.35} \left(\frac{v}{0.1c} \right)^{0.65} \left(\frac{\kappa}{10 \text{ cm}^2 \text{ g}^{-1}} \right)^{-0.65}$$

*assuming 50%
thermalization

Kasen+13: Sn II, Ce II-III, Nd I-IV, Os II

Fontes+17: Ce I-IV, Nd I-IV, Sm I-IV, U I-IV

Wollaeger+17: Se, Br, Zr, Pd, Te

MT+17: Se I-III, Ru I-III, Te I-III, Nd I-III, Er I-III

**open s shell
(l=1)**

**open p-shell
(l=2)**

**open d-shell
(l=3)**

**open f shell
(l=4)**

1 H																	2 He				
3 Li	4 Be															5 B	6 C	7 N	8 O	9 F	10 Ne
11 Na	12 Mg															13 Al	14 Si	15 P	16 S	17 Cl	18 Ar
19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr				
37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe				
55 Cs	56 Ba	57~71 La-Lu	72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn				
87 Fr	88 Ra	89~103 Ac-Lr	104 Rf	105 Db	106 Sg	107 Bh	108 Hs	109 Mt	110 Ds	111 Rg	112 Cn	113 Uut	114 Fl	115 Uup	116 Lv	117 Uus	118 Uuo				
			57 La	58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu				
			89 Ac	90 Th	91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk	98 Cf	99 Es	100 Fm	101 Md	102 No	103 Lr				

Atomic structure calculations

HULLAC code (relativistic, local radial potential, Bar-Shalom+99)

Se I-III

(Z=34, p)

Ru I-III

(Z=44, d)

Te I-III

(Z=52, p)

Nd I-III

(Z=60, f)

Er I-III

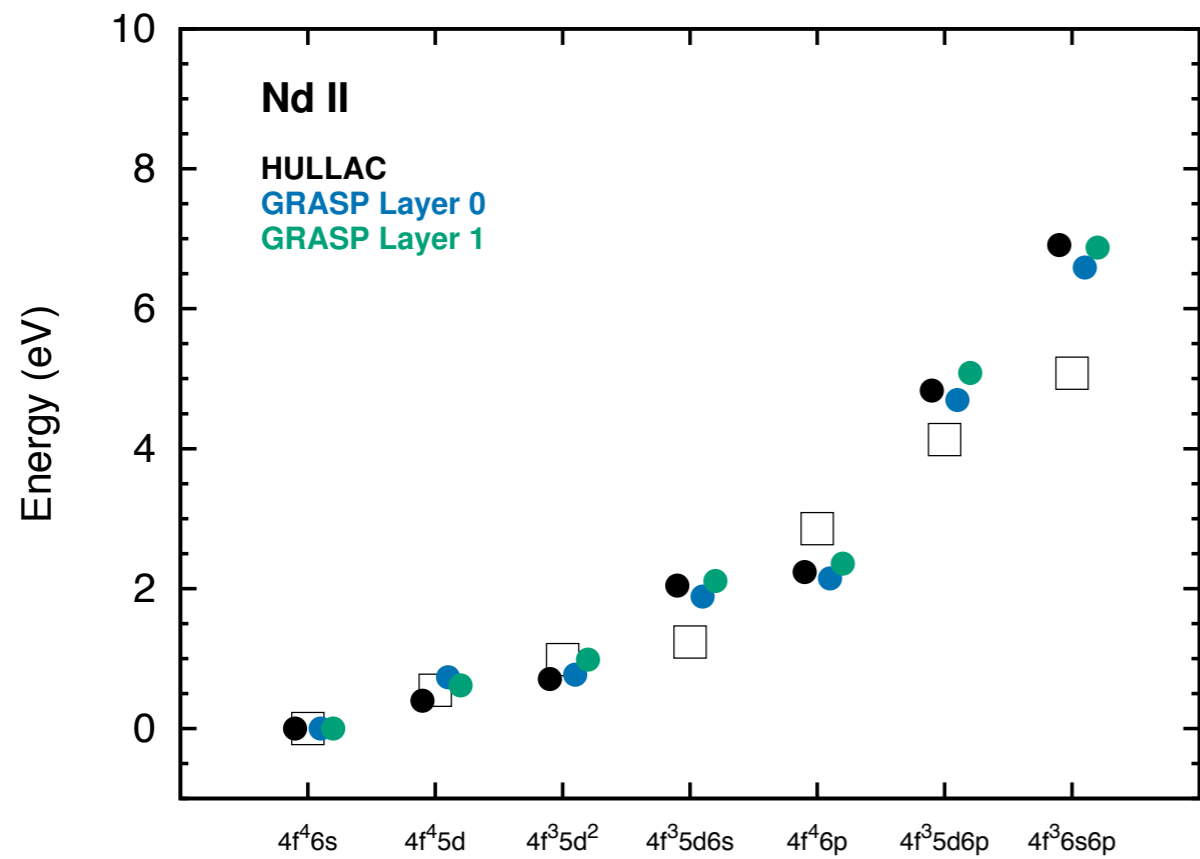
(Z=68, f)

Ion	Configurations	Number of levels	Number of lines
HULLAC			
Se I	$4s^2 4p^4$, $4s^2 4p^3(4d, 4f, 5 - 8l)$, $4s4p^5$, $4s4p^4(4d, 4f)$, $4s^2 4p^2(4d^2, 4d4f, 4f^2)$, $4s4p^3(4d^2, 4d4f, 4f^2)$	3076	973,168
Se II	$4s^2 4p^3$, $4s^2 4p^2(4d, 4f, 5 - 8l)$, $4s4p^4$, $4s4p^3(4d, 4f)$, $4s^2 4p(4d^2, 4d4f, 4f^2)$, $4s4p^2(4d^2, 4d4f, 4f^2)$	2181	511,911
Se III	$4s^2 4p^2$, $4s^2 4p(4d, 4f, 5 - 8l)$, $4s4p^3$, $4s4p^2(4d, 4f)$, $4s^2(4d^2, 4d4f, 4f^2)$, $4s4p(4d^2, 4d4f, 4f^2)$	922	92,132
Ru I	$4d^7 5s$, $4d^6 5s^6$, $4d^8$, $4d^7(5p, 5d, 6s, 6p)$, $4d^6 5s(5p, 5d, 6s)$	1,545	250,476
Ru II	$4d^7$, $4d^6(5s - 5d, 6s, 6p)$	818	76,592
Ru III	$4d^6$, $4d^5(5s - 5d, 6s)$	728	49,066
Te I	$5s^2 5p^4$, $5s^2 5p^3(4f, 5d, 5f, 6s - 6f, 7s - 7d, 8s)$, $5s5p^5$	329	14,482
Te II	$5s^2 5p^3$, $5s^2 5p^2(4f, 5d, 5f, 6s - 6f, 7s - 7d, 8s)$, $5s5p^4$	253	9,167
Te III	$5s^2 5p^2$, $5s^2 5p(5d, 6s - 6d, 7s)$, $5s5p^3$	57	419
Nd I	$4f^4 6s^2$, $4f^4 6s(5d, 6p, 7s)$, $4f^4 5d^2$, $4f^4 5d6p$, $4f^3 5d6s^2$, $4f^3 5d^2(6s, 6p)$, $4f^3 5d6s6p$	31,358	70,366,259
Nd II	$4f^4 6s$, $4f^4 5d$, $4f^4 6p$, $4f^3 6s(5d, 6p)$, $4f^3 5d^2$, $4f^3 5d6p$	6,888	3,951,882
Nd III	$4f^4$, $4f^3(5d, 6s, 6p)$, $4f^2 5d^2$, $4f^2 5d(6s, 6p)$, $4f^2 6s6p$	2252	458,161
Er I	$4f^{12} 6s^2$, $4f^{12} 6s(5d, 6p, 6d, 7s, 8s)$, $4f^{11} 6s^2(5d, 6p)$, $4f^{11} 5d^2 6s$, $4f^{11} 5d6s(6p, 7s)$	10,535	9,247,777
Er II	$4f^{12} 6s$, $4f^{12}(5d, 6p)$, $4f^{11} 6s^2$, $4f^{11} 6s(5d, 6p)$, $4f^{11} 5d^2$, $4f^{11} 5d6p$	5,333	2,432,665
Er III	$4f^{12}$, $4f^{11}(5d, 6s, 6p)$	723	42,671

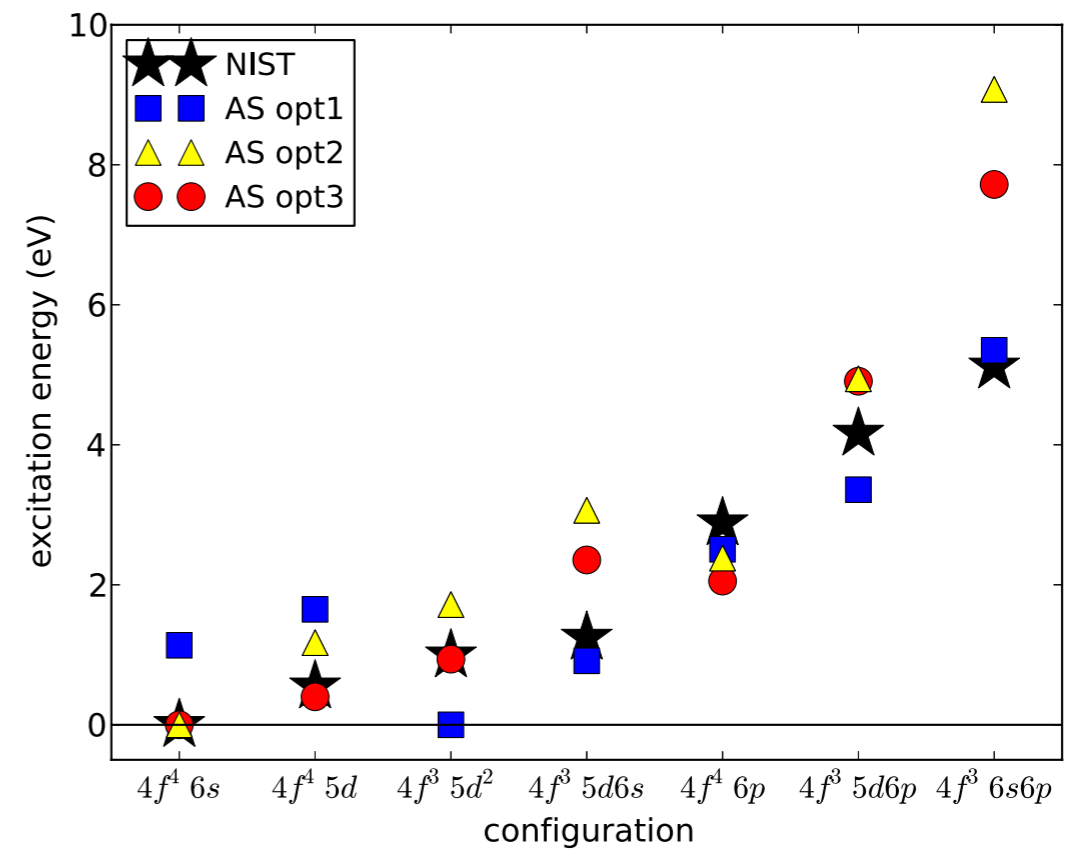
GRASP2K code (relativistic, e-e correlation, Jonsson+07)

Nd II-III, Er II-III

Energy levels of Nd II



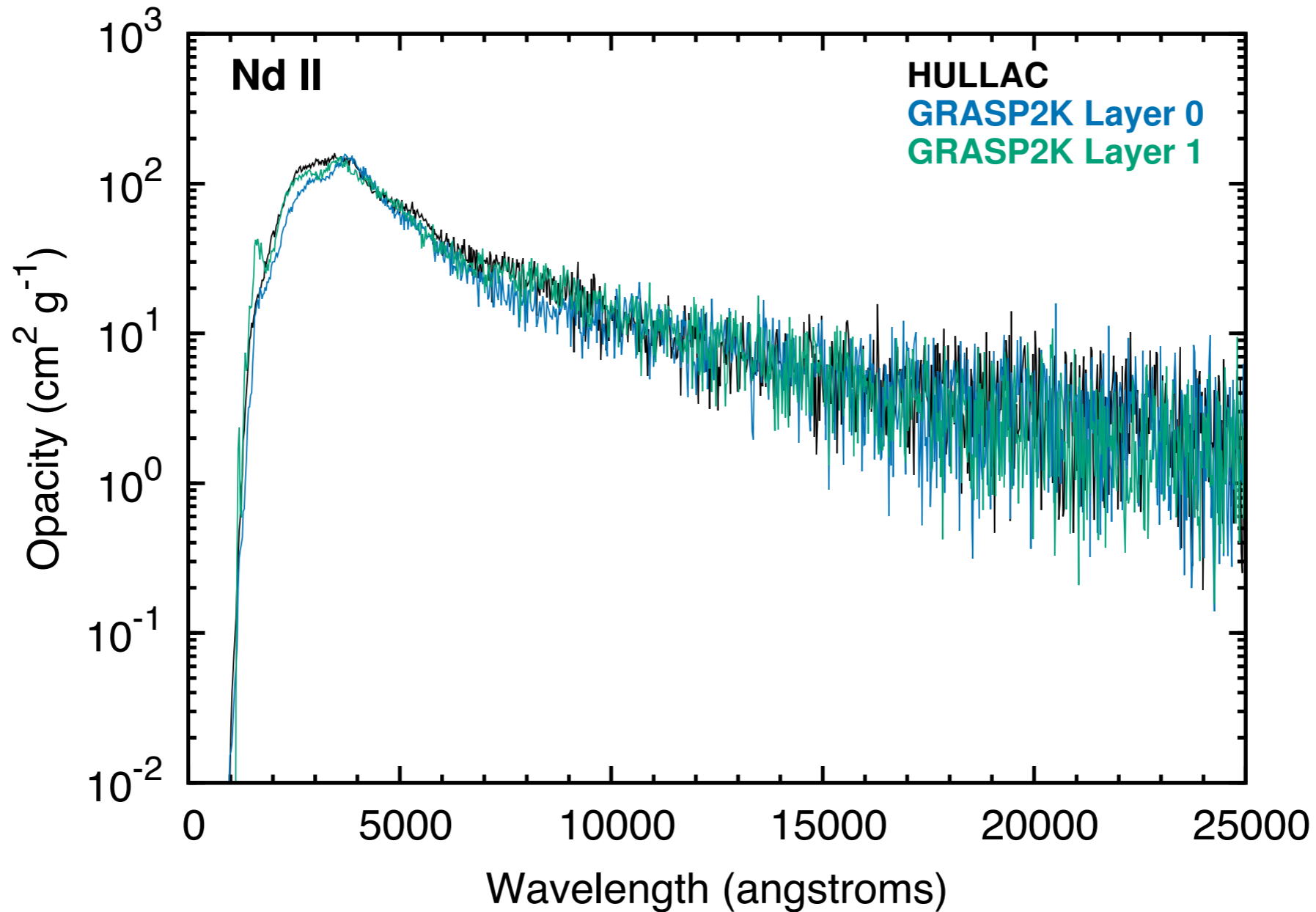
MT+ in prep



Kasen+13 (Autostructure code)

Line expansion opacity of Nd II

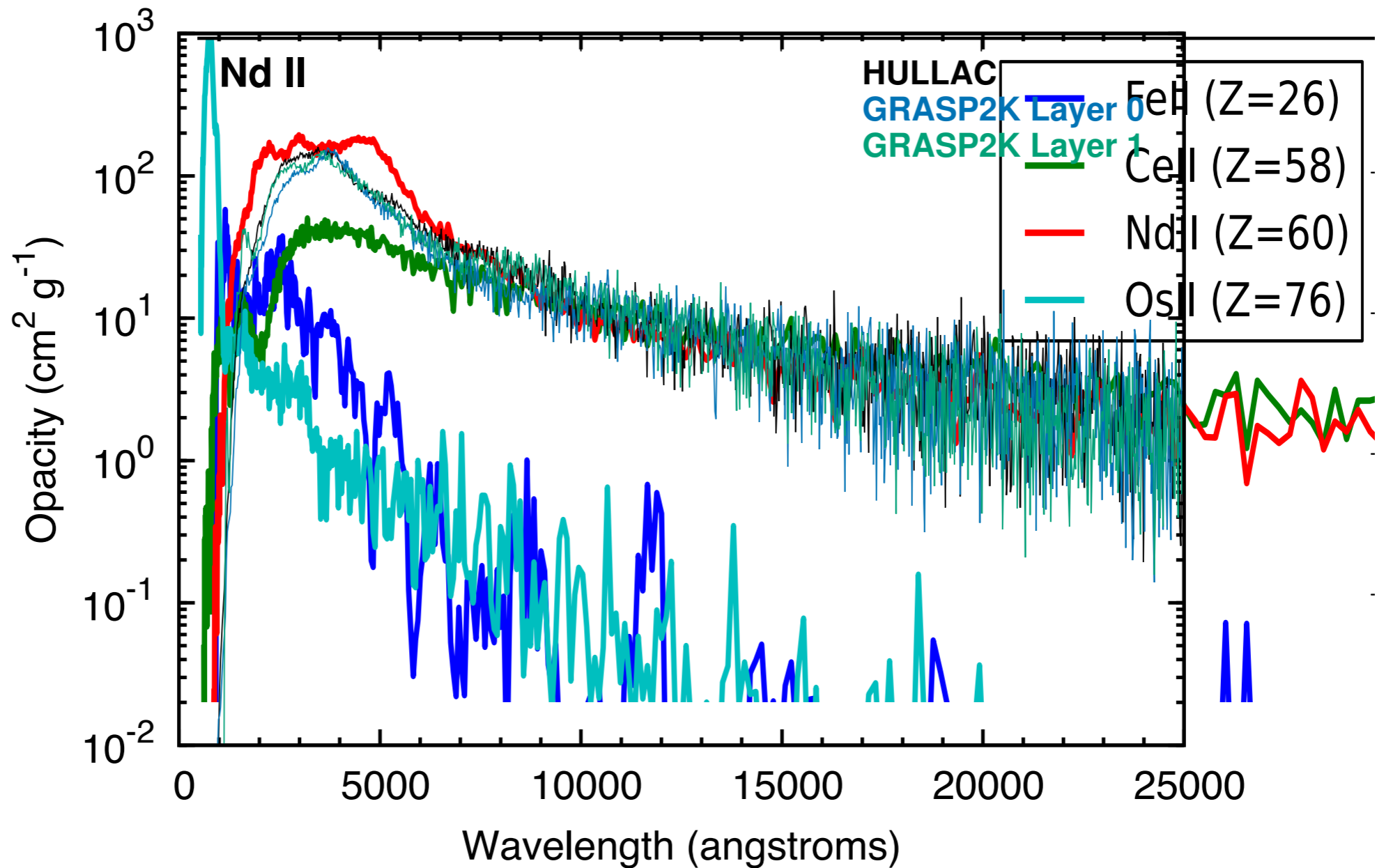
$T = 5,000 \text{ K}$, $\rho = 10^{-13} \text{ g cm}^{-3}$, $t = 1 \text{ day}$



Opacities from two codes agree very well

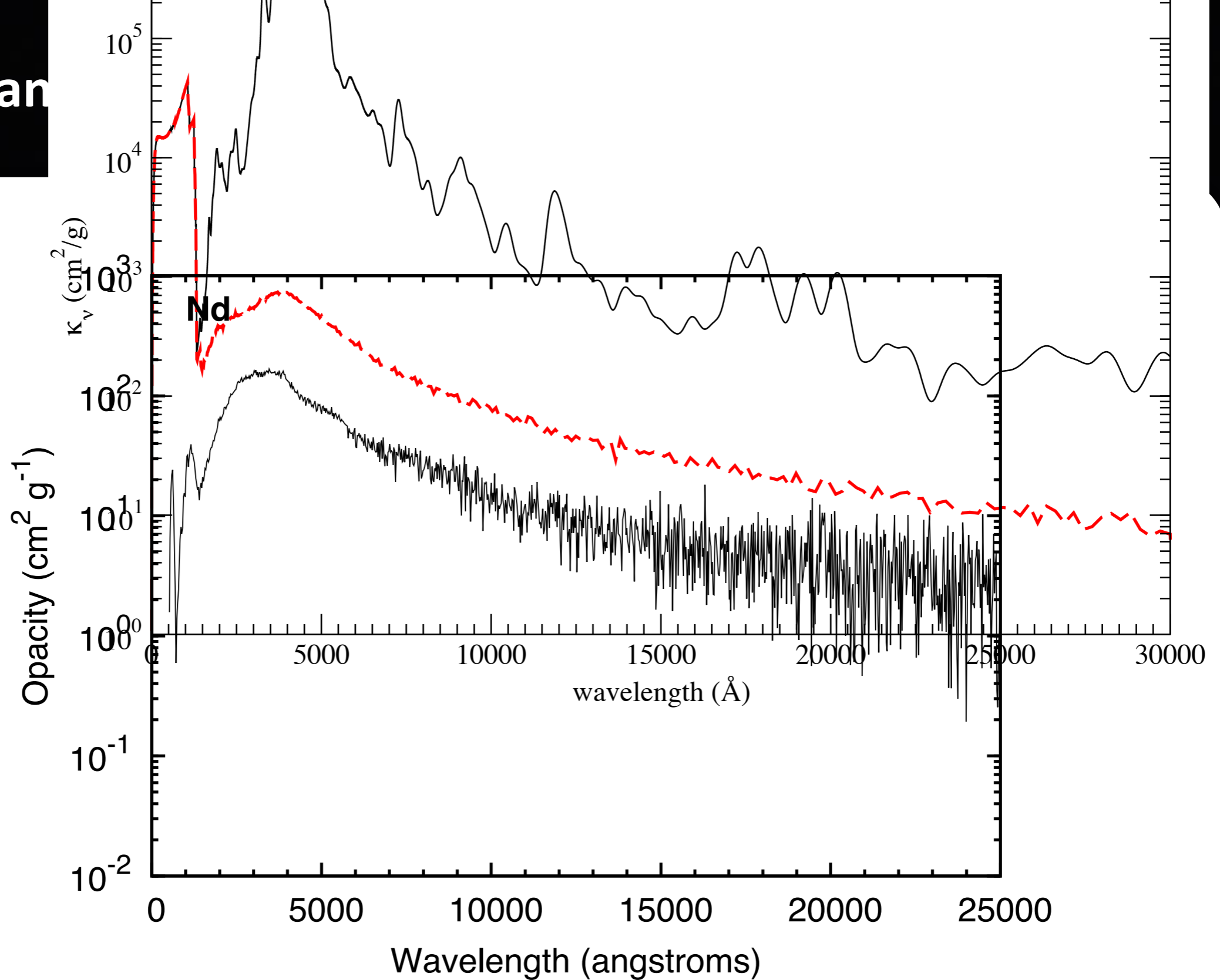
Line expansion opacity of Nd II

$T = 5,000 \text{ K}$, $\rho = 10^{-13} \text{ g cm}^{-3}$, $t = 1 \text{ day}$



Consistent with results by Kasen+13 (Autostruture code)

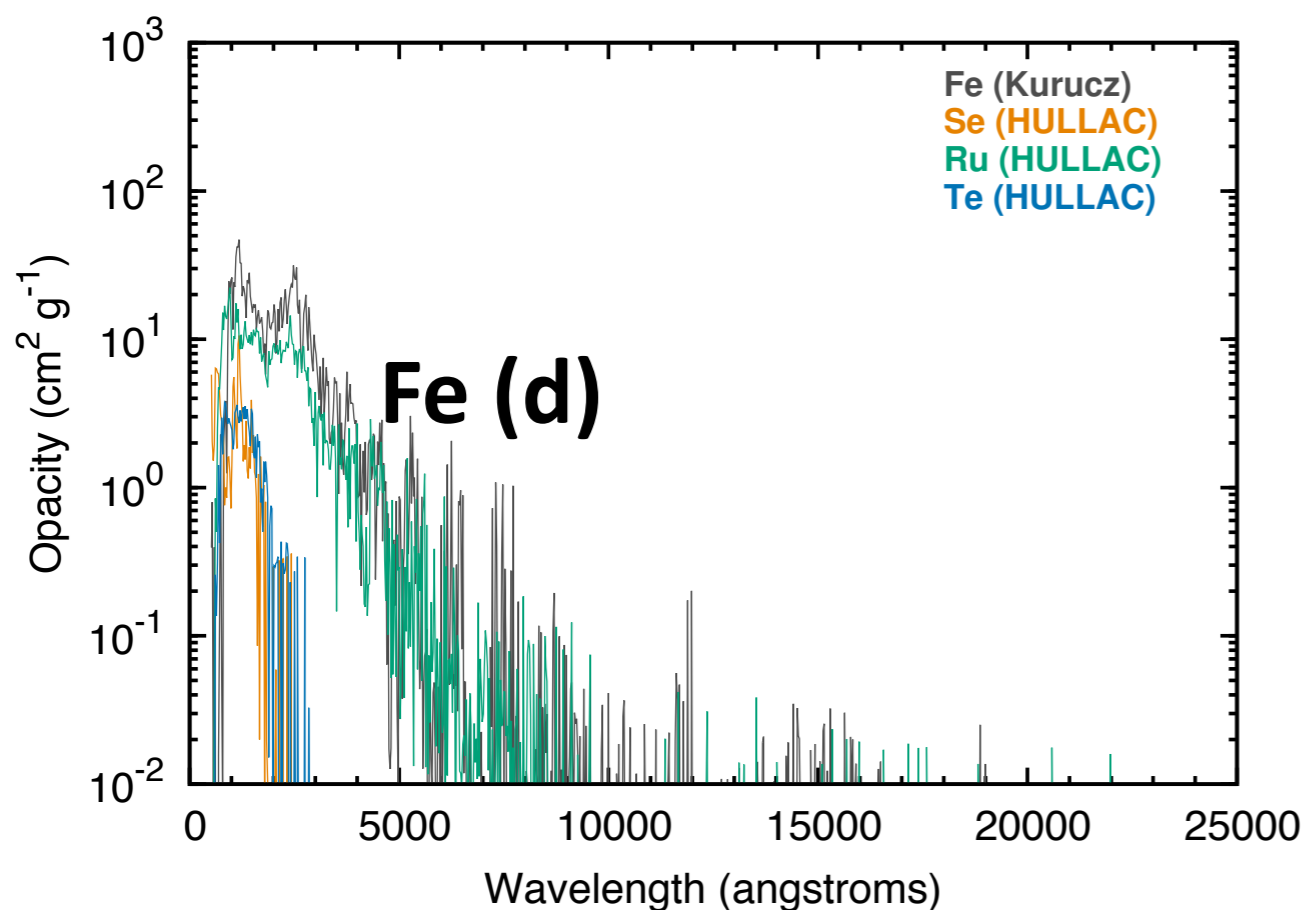
Line expansion



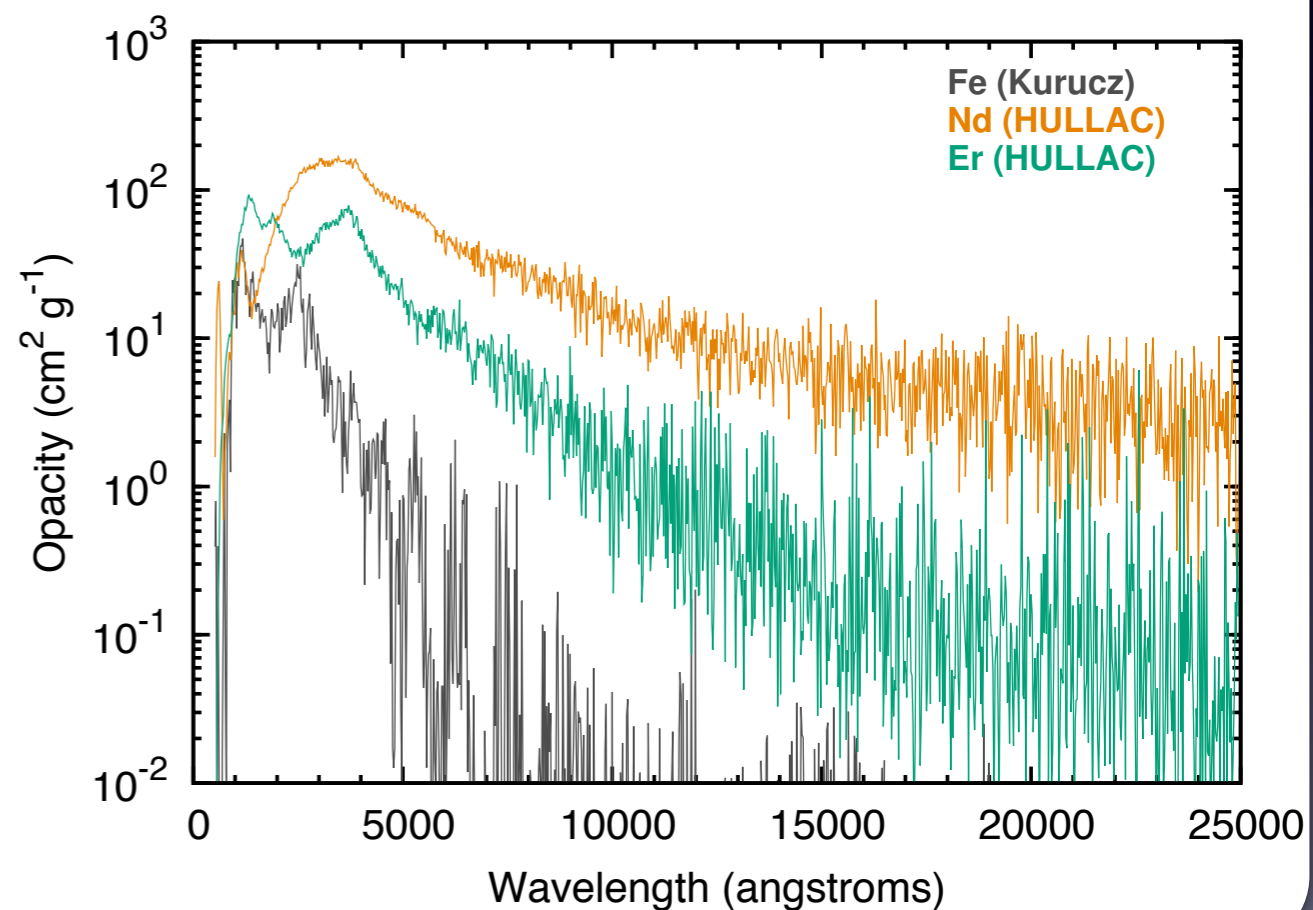
Expansion opacity of Fontes+17 is higher by a factor of 3-5

Line expansion opacity (for each element)

Se (p) Ru (d) Te (p)



Nd (f) Er (f)



MT+ in prep.

κ (p shell) \ll κ (d shell) \ll κ (f shell)

see Kasen+13, Fontes+17

Er (Z=68) Energy levels

NIST Atomic Spectra Database Levels Form

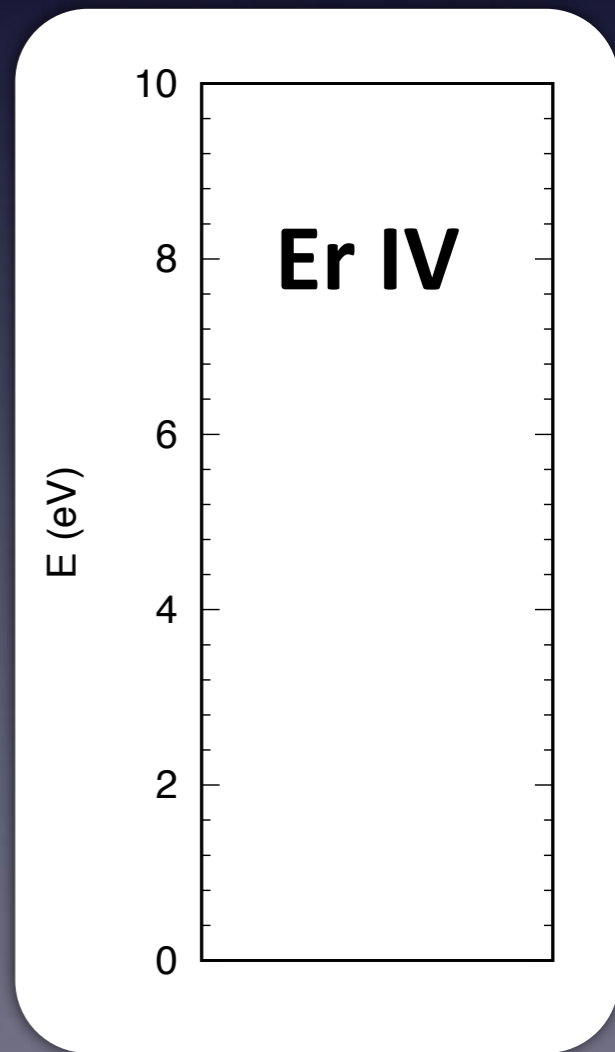
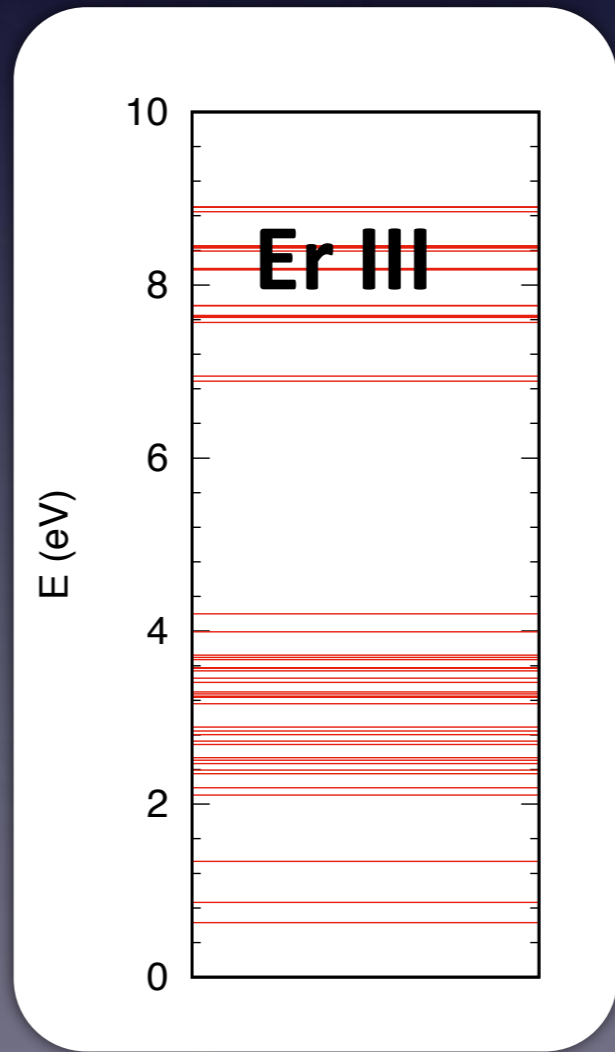
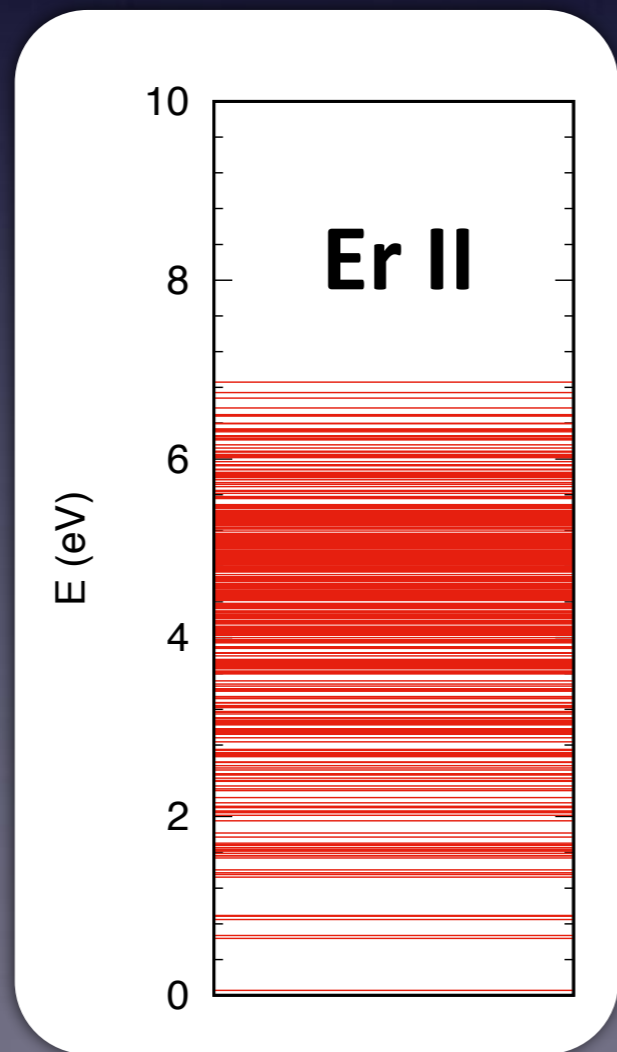
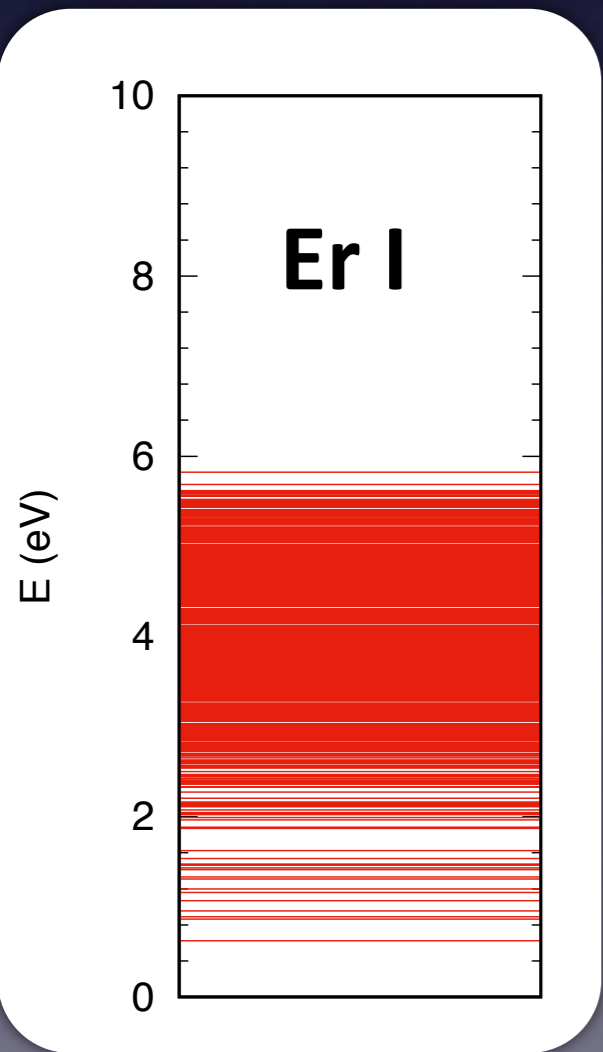
Best viewed with the latest versions of Web browsers and JavaScript enabled

This form provides access to NIST critically evaluated data on atomic energy levels.

Spectrum: e.g., Fe I or Mg Li-like or Z=59 II

Default Values

Retrieve Data



Spectroscopic experiments for Er (Z=68)

Collaboration with

**Nobuyuki Nakamura,
Hajime Tanuma,
Hiroyuki Sakaue, and
Izumi Murakami**

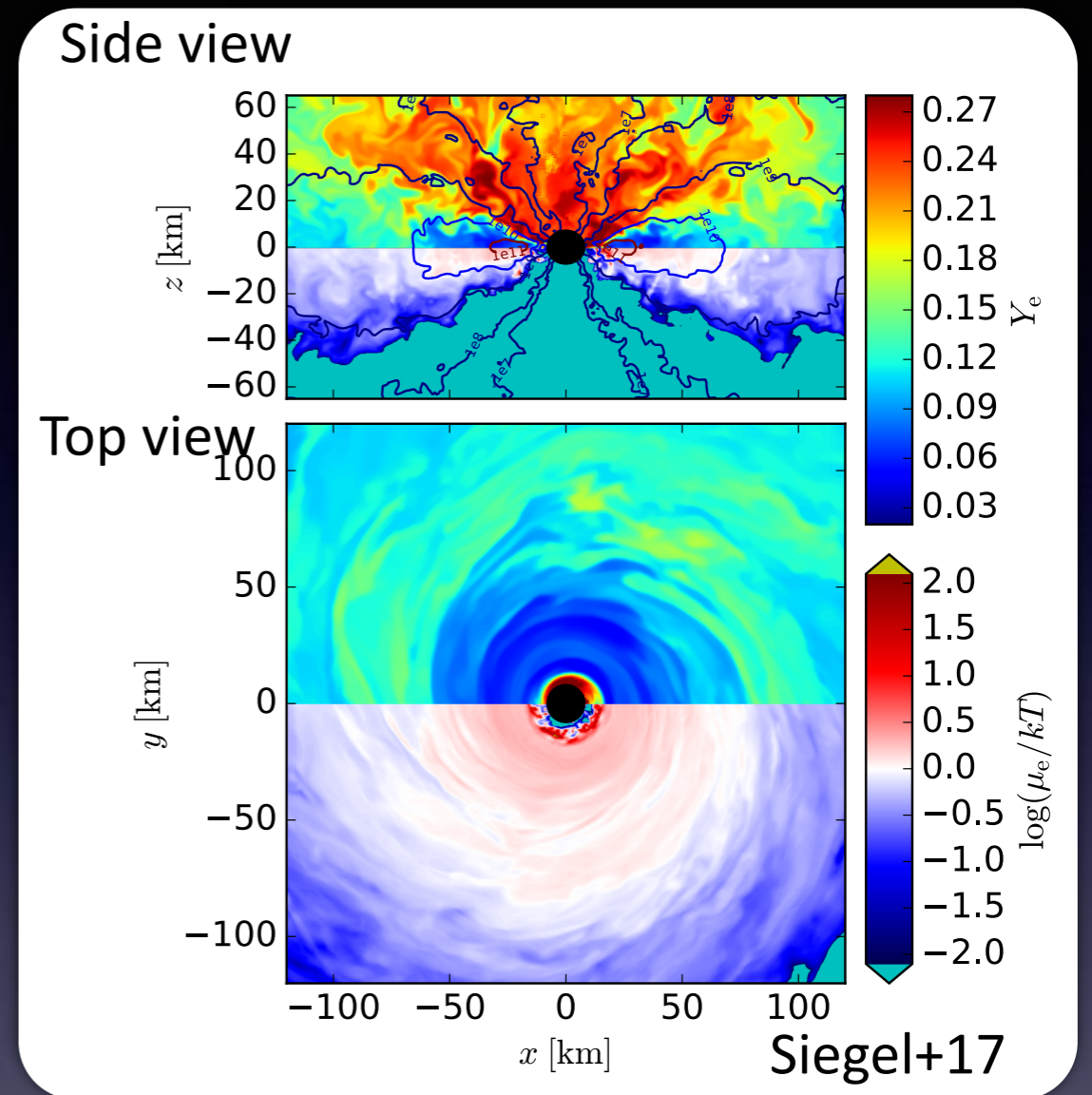
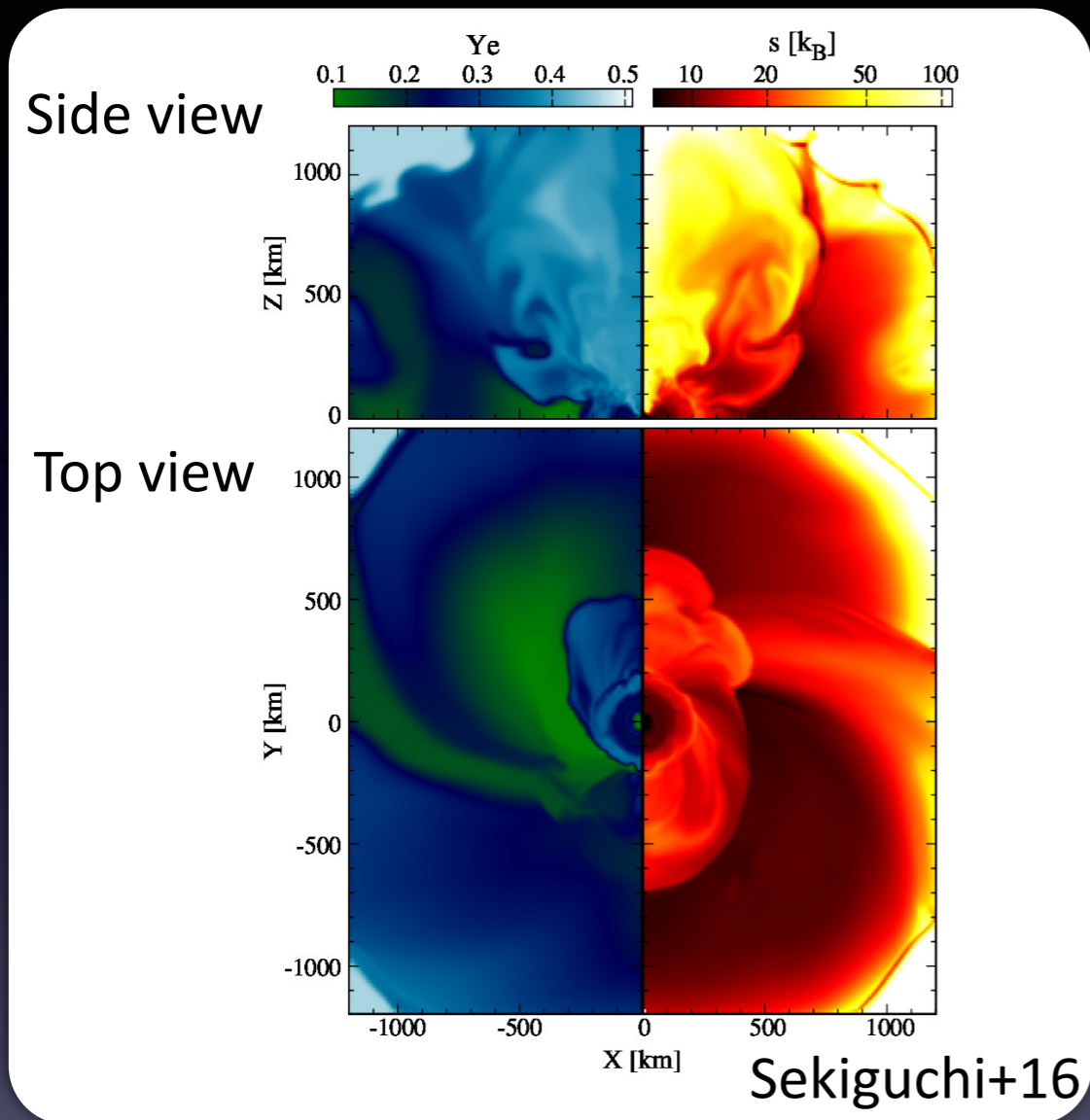
- Atomic and opacity calculations
- Kilonova light curves

Collaboration with

Shinya Wanajo (Sofia University, Japan) and
Yuichiro Sekiguchi (Toho University, Japan)

Dynamical ejecta ($\sim < 10$ ms)

Post-merger ejecta ($\sim < 100$ ms)



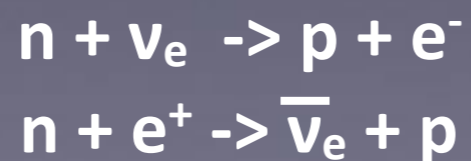
Rosswog+99, Lee+07, Goriely+11,
Hotokezaka+13, Bauswein+13, Radice+16...

Fernandez+13,15, Perego+14, Kiuchi+14,15,
Martin+15, Just+15, Wu+16, Siegel & Metzger 17...

- $M_{ej} \sim 10^{-3} - 10^{-2} M_{sun}$

- $v \sim 0.1-0.2 c$

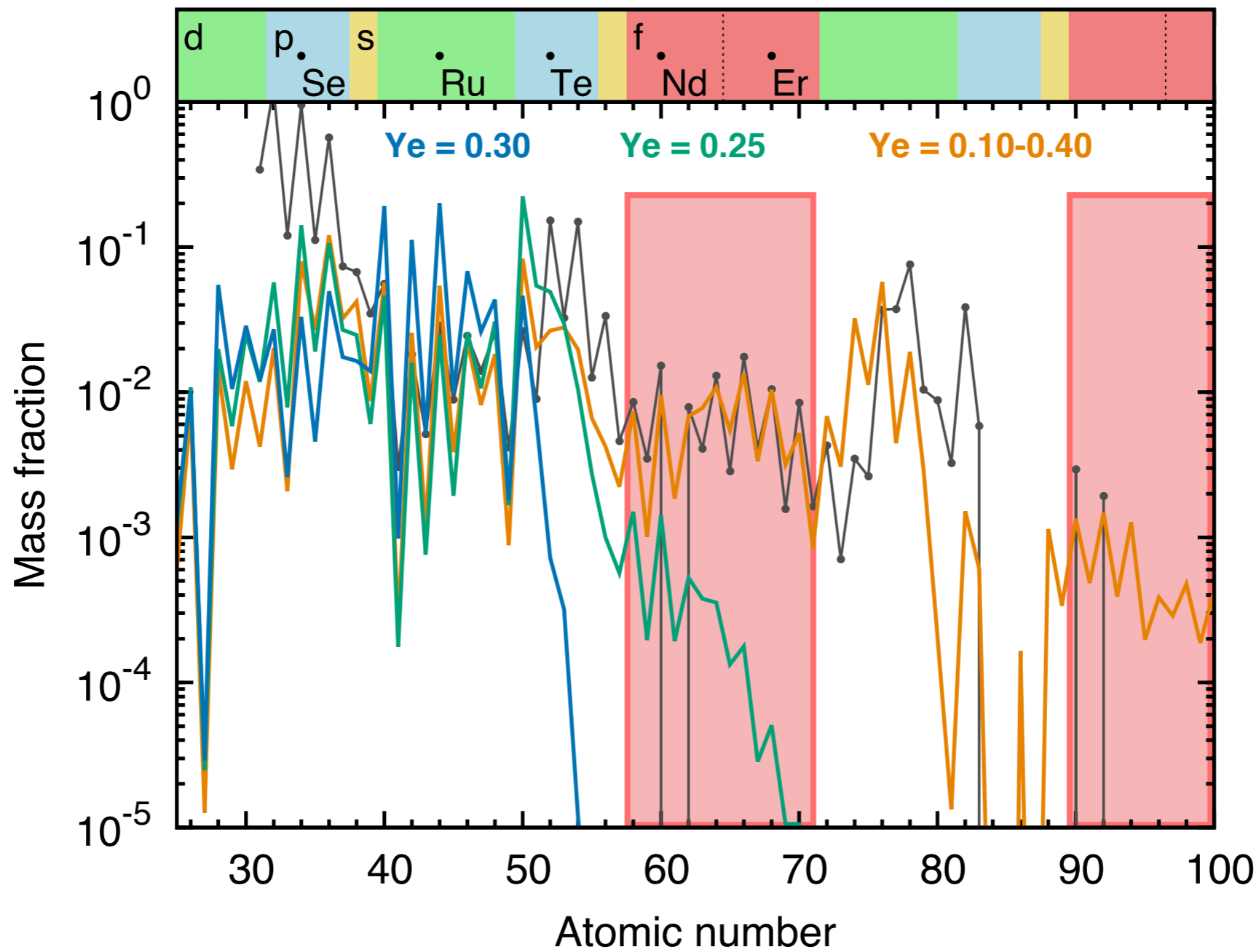
- wide Y_e



- $M_{ej} > \sim 10^{-3} M_{sun}$

- $v \sim 0.05 c$

- relatively high Y_e



“Blue” kilonova?

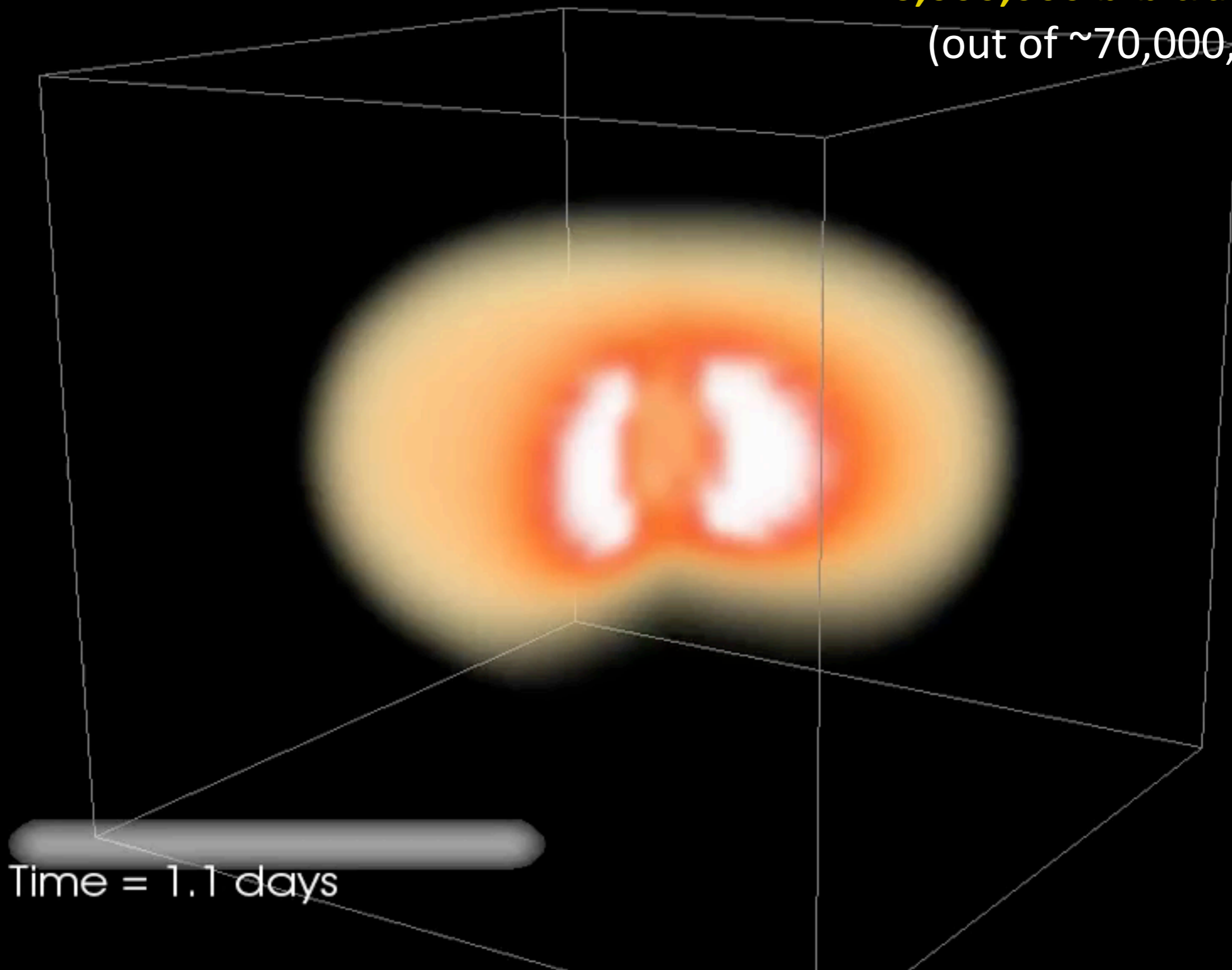
Simulations with Fe opacity or gray opacity
 Metzger+14, Kasen+15, Fernandez & Metzger 16, Metzger 16

3D Monte-Carlo frequency-dependent radiation transfer

(MT & Hotokezaka 13, MT+14, MT 16)

~6,000,000 b-b transitions

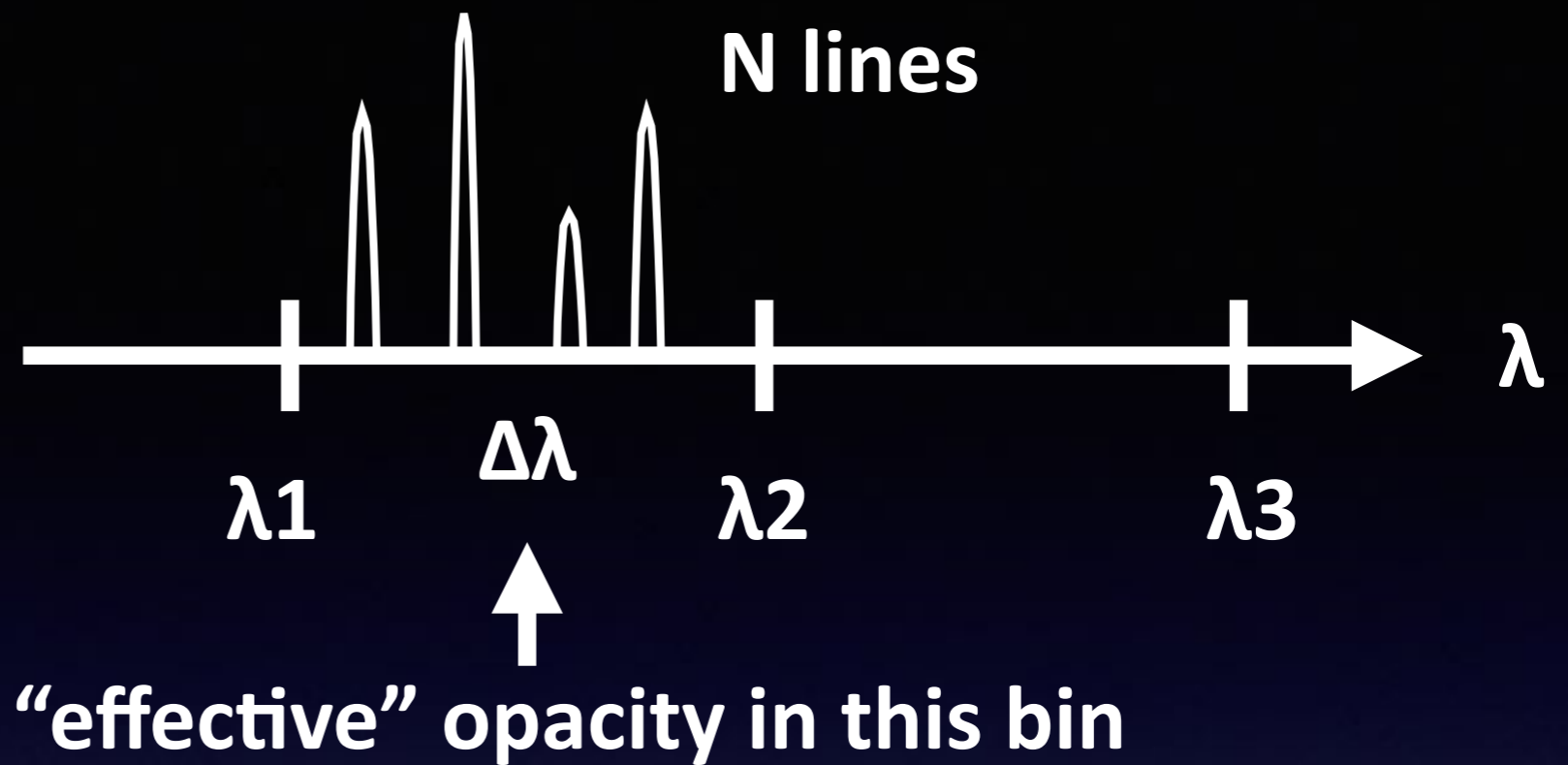
(out of ~70,000,000)



Time = 1.1 days

Expansion opacity

Pinto & Eastman 2000
Kasen+06, Kasen+13
MT+13



Line spacing

$$\frac{\Delta\lambda}{N}$$

"Effective" mean free path

$$l = \frac{\Delta\lambda}{N} \frac{1}{\lambda} ct$$

$$\tau_{\text{sob}} = \frac{\pi e^2}{mc} n_1 f_{\text{osc}} t \lambda$$

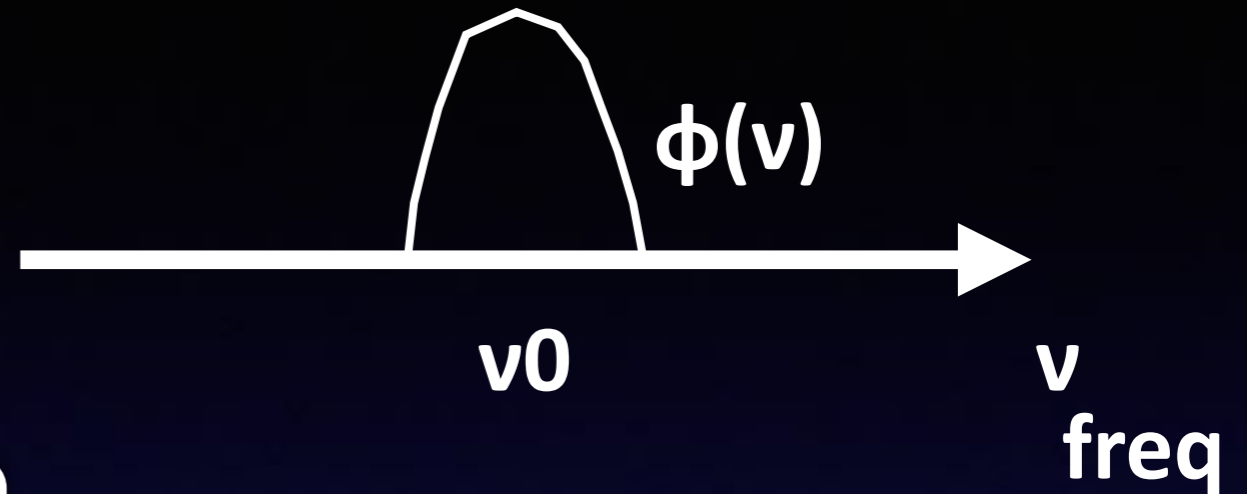
"Effective" absorption coefficient α_{exp} (cm^{-1})

$$\alpha_{\text{exp}} = \frac{1}{l} = \frac{\lambda}{\Delta\lambda} \frac{1}{ct} N$$

$$\alpha_{\text{exp}} = \frac{\lambda}{\Delta\lambda} \frac{1}{ct} \Sigma (1 - e^{-\tau_{\text{sob}}})$$

Sobolev optical depth

$$\alpha = \frac{\pi e^2}{mc} n_1 f_{\text{osc}} \phi(\nu)$$



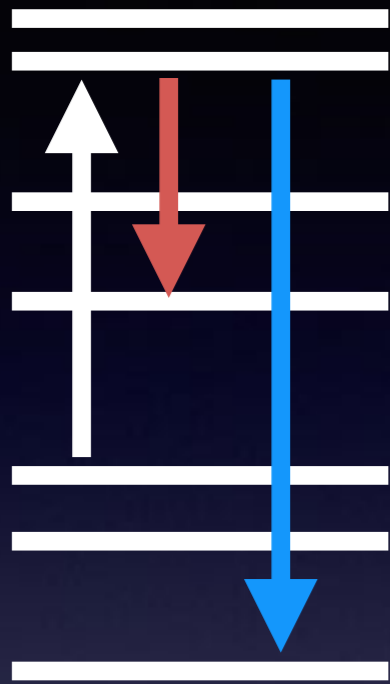
$$\begin{aligned} \tau_{\text{sob}} &= \int \alpha dr \\ &= \int \alpha \frac{dr}{d\nu} \frac{c}{\nu_0} d\nu \\ &= \int \frac{\pi e^2}{mc} n_1 f_{\text{osc}} \phi(\nu) \frac{dr}{d\nu} \frac{c}{\nu_0} d\nu \\ &= \frac{\pi e^2}{mc} n_1 f_{\text{osc}} \frac{dr}{d\nu} \frac{c}{\nu_0} \\ &= \frac{\pi e^2}{mc} n_1 f_{\text{osc}} t \lambda \end{aligned}$$

$$\frac{d\nu}{\nu_0} = \frac{d\nu}{c} = \frac{1}{c} \frac{d\nu}{dr} dr$$

if velocity dominated by
radial motion ($v_{\text{th}} \ll v_{\text{rad}}$)

$$\int \phi(\nu) d\nu = 1$$

Fluorescence



When photons interact with line,

* **Full treatment**

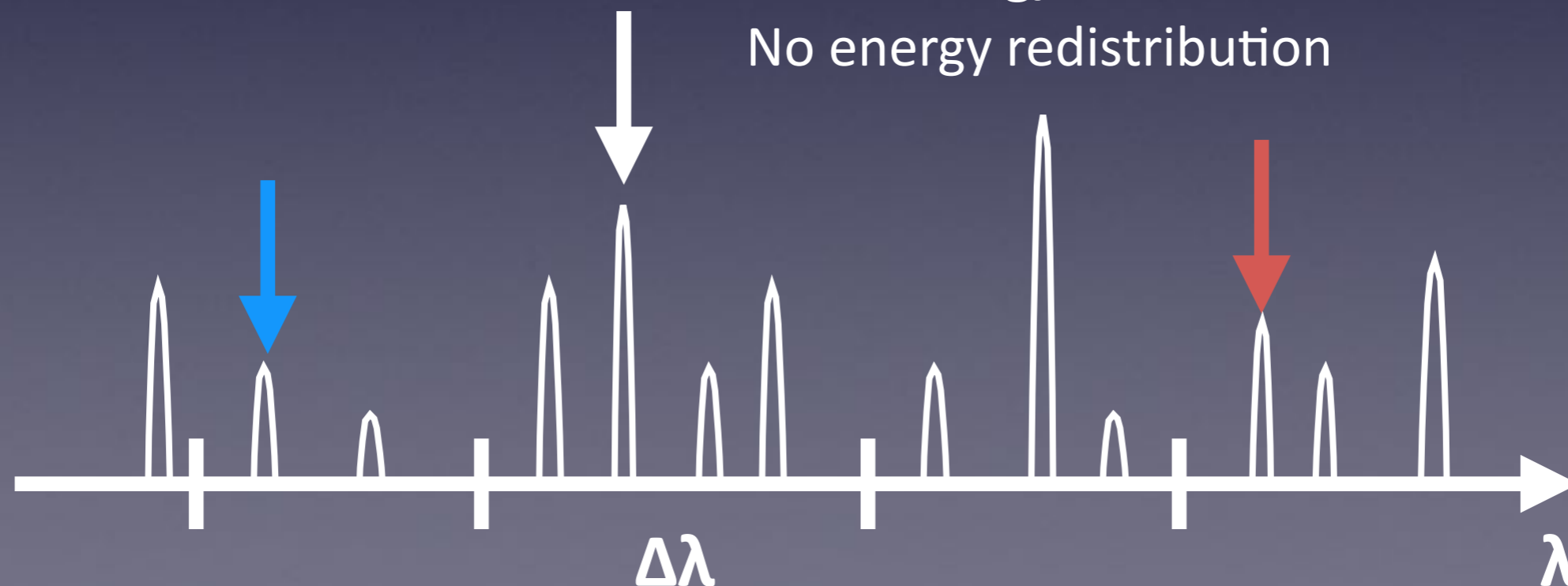
Redistribute photon energy according to branching ratios
(Lucy, Mazzali & Lucy, Kasen+06)

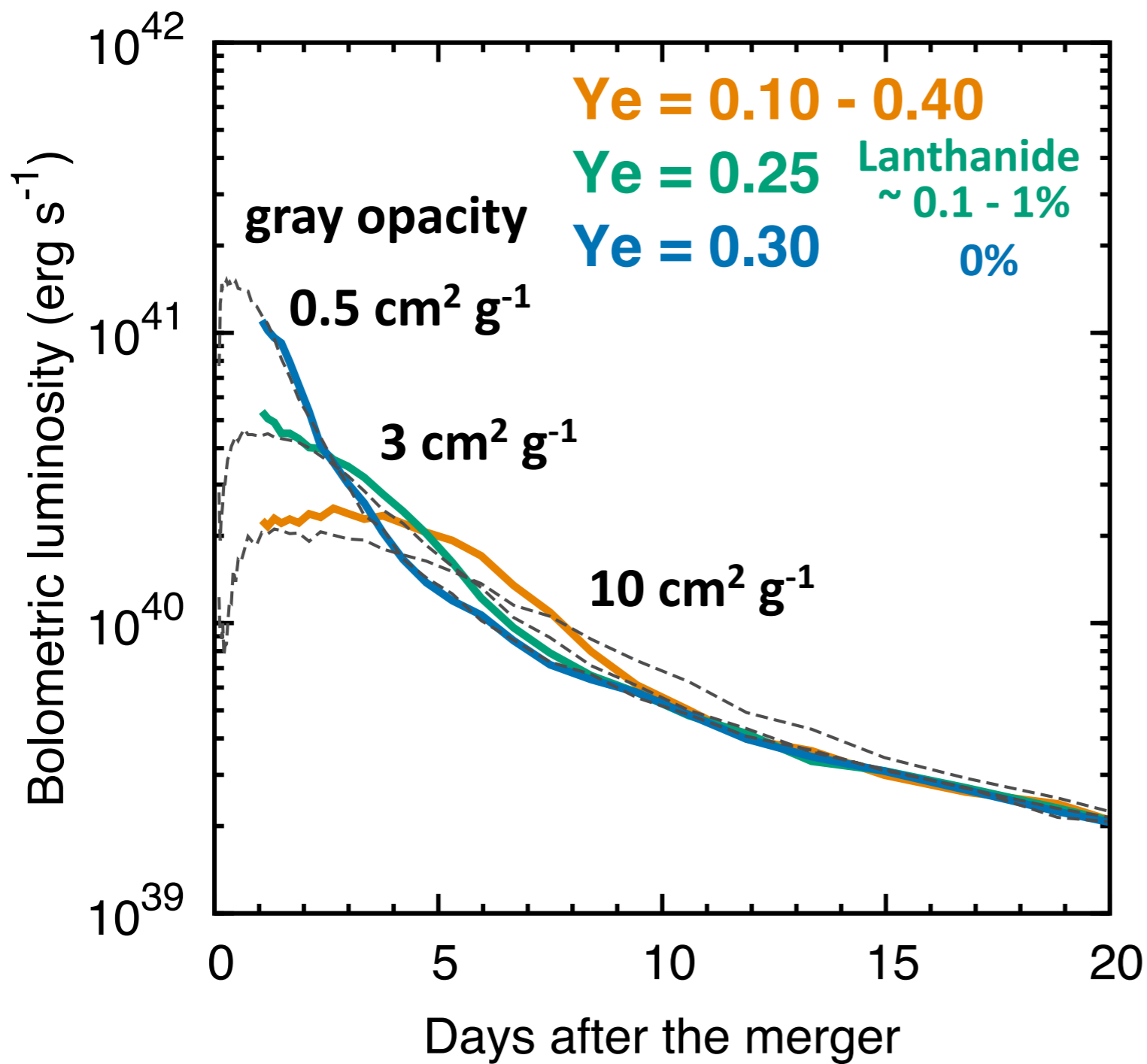
* **Absorptive**

Redistribute photon energy according to thermal distribution $j = \alpha B(T)$
(Kasen+13, Tanaka & Hotokezaka 13, Fontes+17, Wollaeger+17)

* **Scattering/resonance**

No energy redistribution



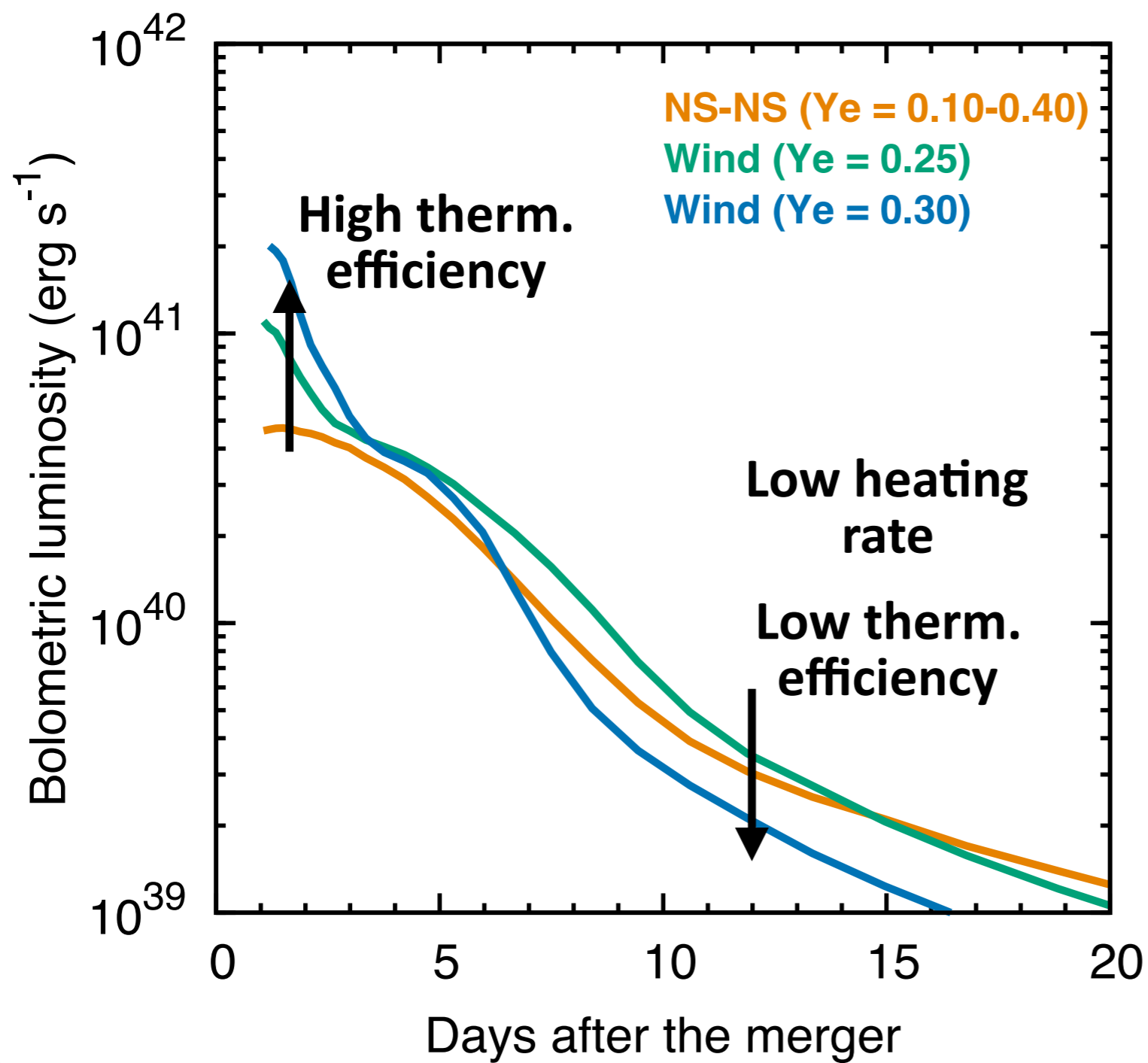


Simple model

- $M_{\text{ej}} = 0.01 M_{\text{sun}}$
- $v = 0.1c$
- Heating rate $\sim t^{-1.3}$
- Constant thermalization (0.25)

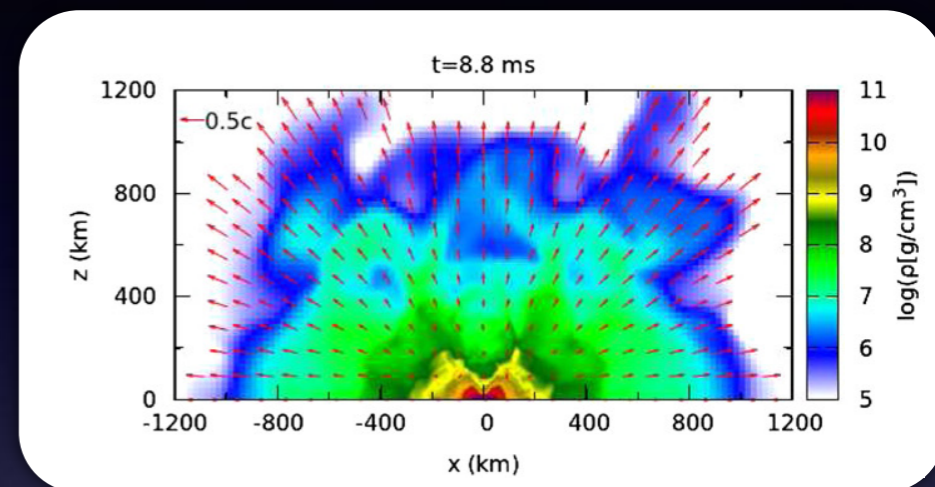
Depends sensitively on Ye

$\kappa \sim 0.5 \text{ cm}^2 \text{ g}^{-1}$ for Lanthanide-free ejecta (Ye ~ 0.3)



NS-NS

- $M_{\text{ej}} = 0.01 M_{\text{sun}}$
- $v = 0.2c$



Hotokezaka+13, Sekiguchi+15,16

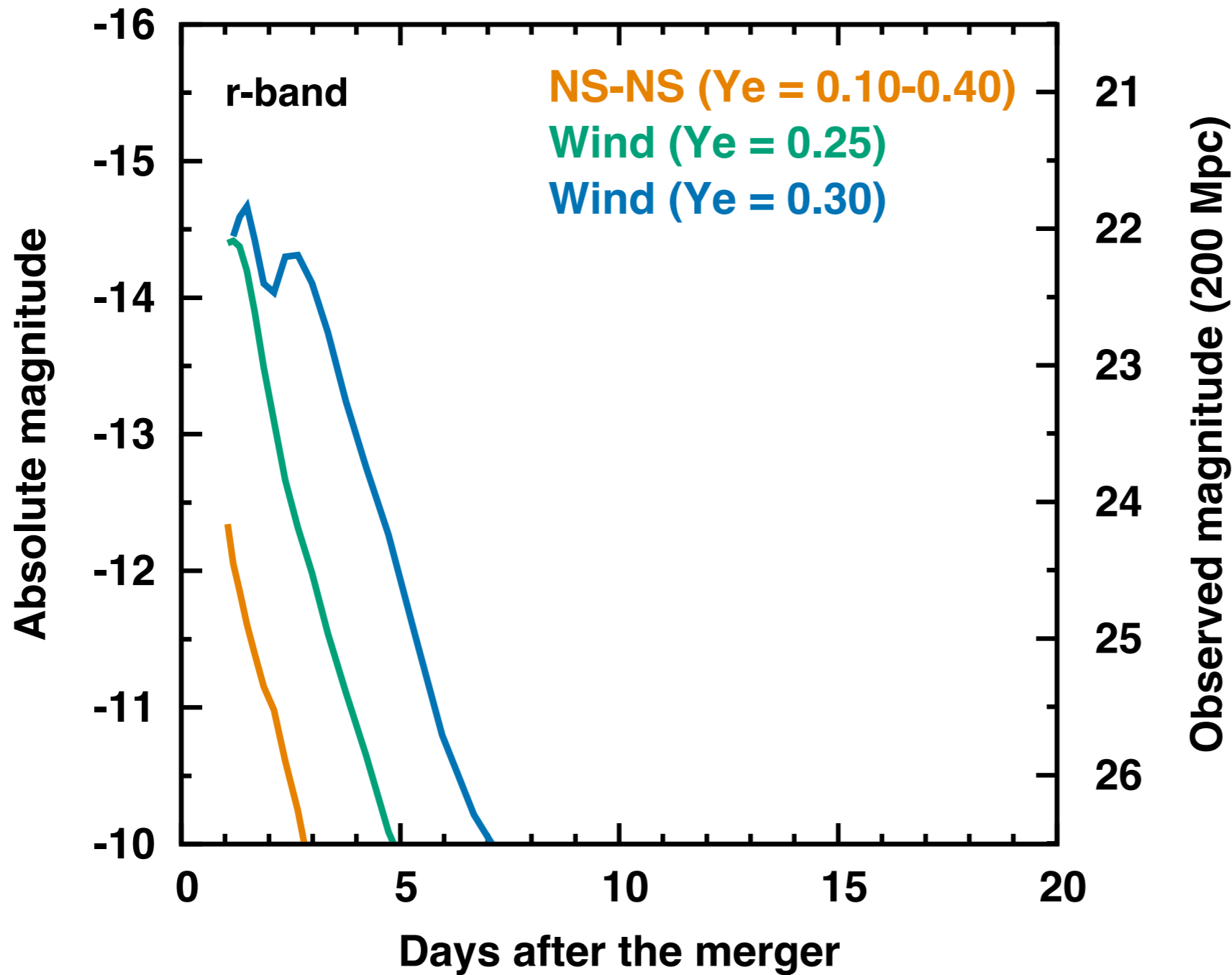
Wind

- $M_{\text{ej}} = 0.01 M_{\text{sun}}$
- $v = 0.05c$

- Heating rate from nucleosynthesis calc.
- Thermalization (Barnes+16)

Optical (r-band)

$M_{ej} = 0.01 M_{sun}$



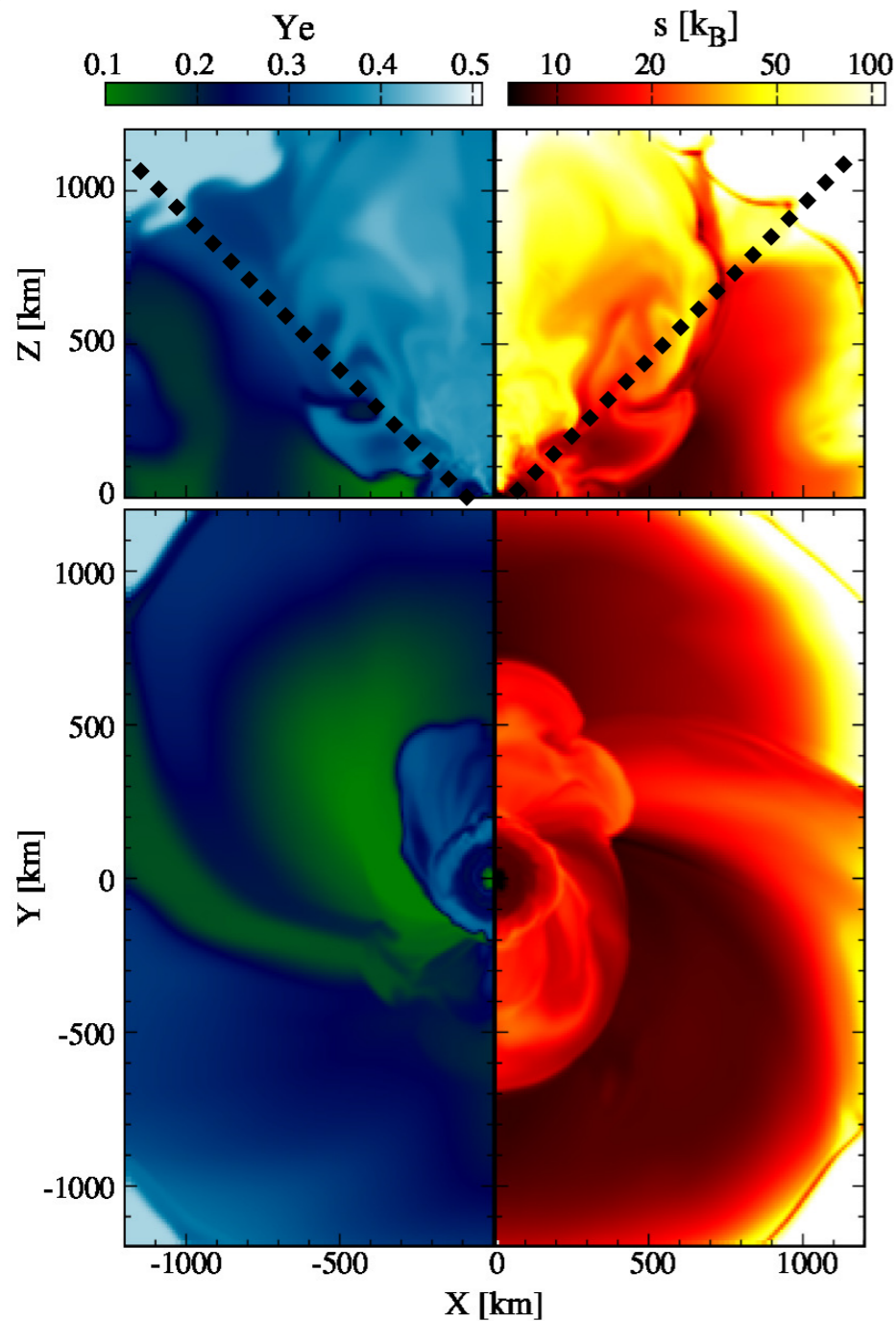
MT+ in prep.

Wide variety even for the same ejecta mass

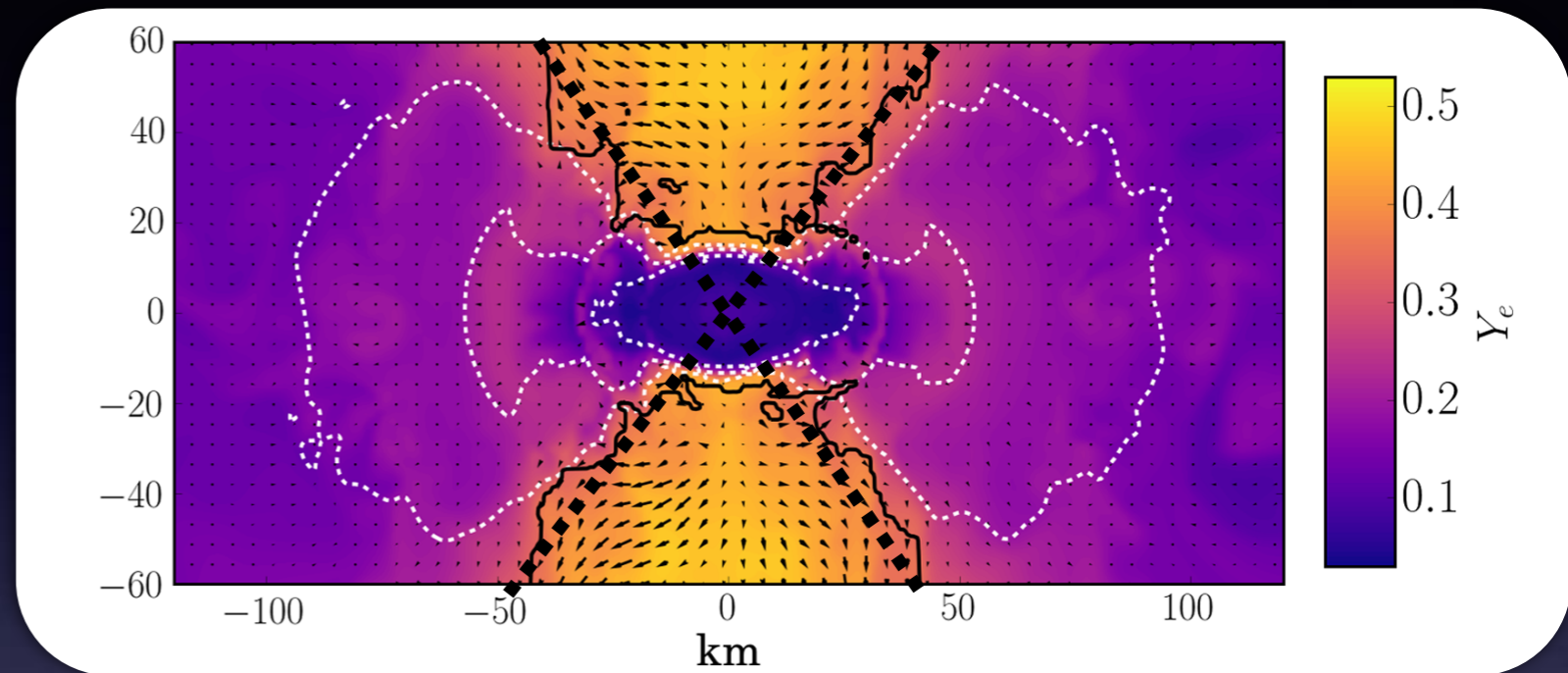
=> Accurate estimate of Y_e is crucial

Blue component may be absorbed by dynamical ejecta?

e.g., Kasen+15, Metzger 17



Sekiguchi+16

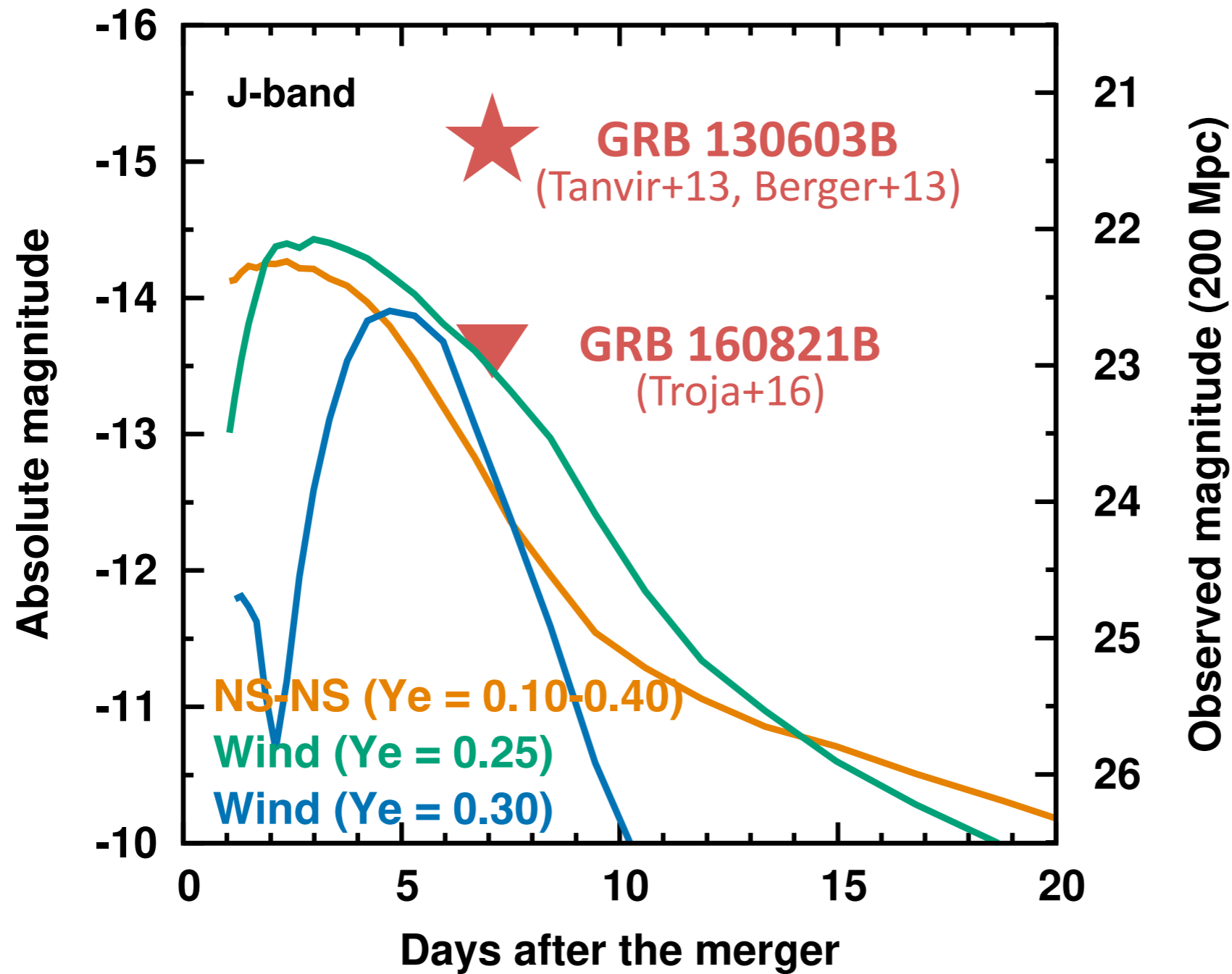


Foucart+16

High Y_e in the polar region ($< 30-45$ deg)
=> Blue emission may be able to escape

NIR (J-band)

$M_{ej} = 0.01 M_{sun}$



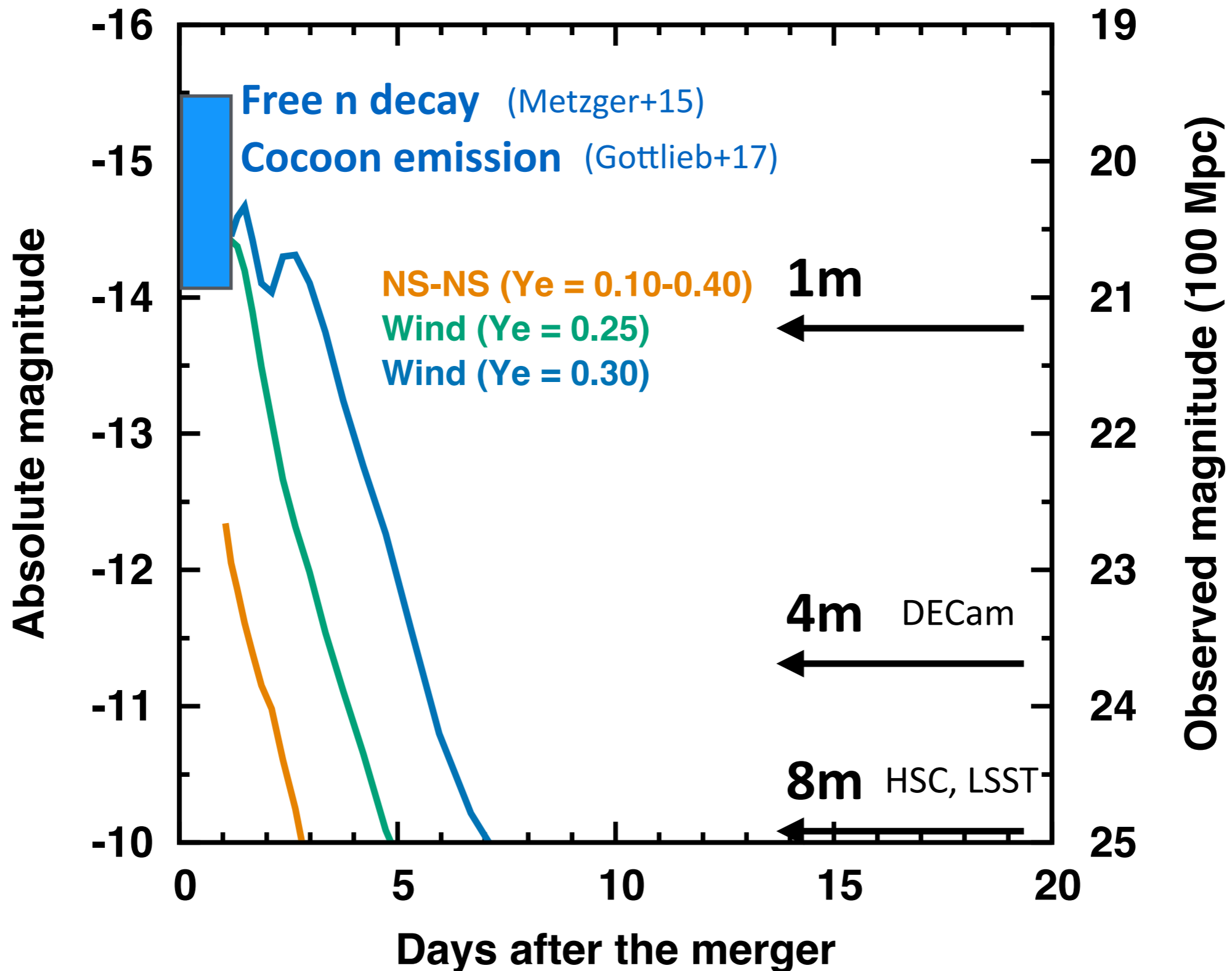
see also Kasliwal+17

$M \sim 0.06 M_{sun}$ for GRB 130603B

Barnes+16

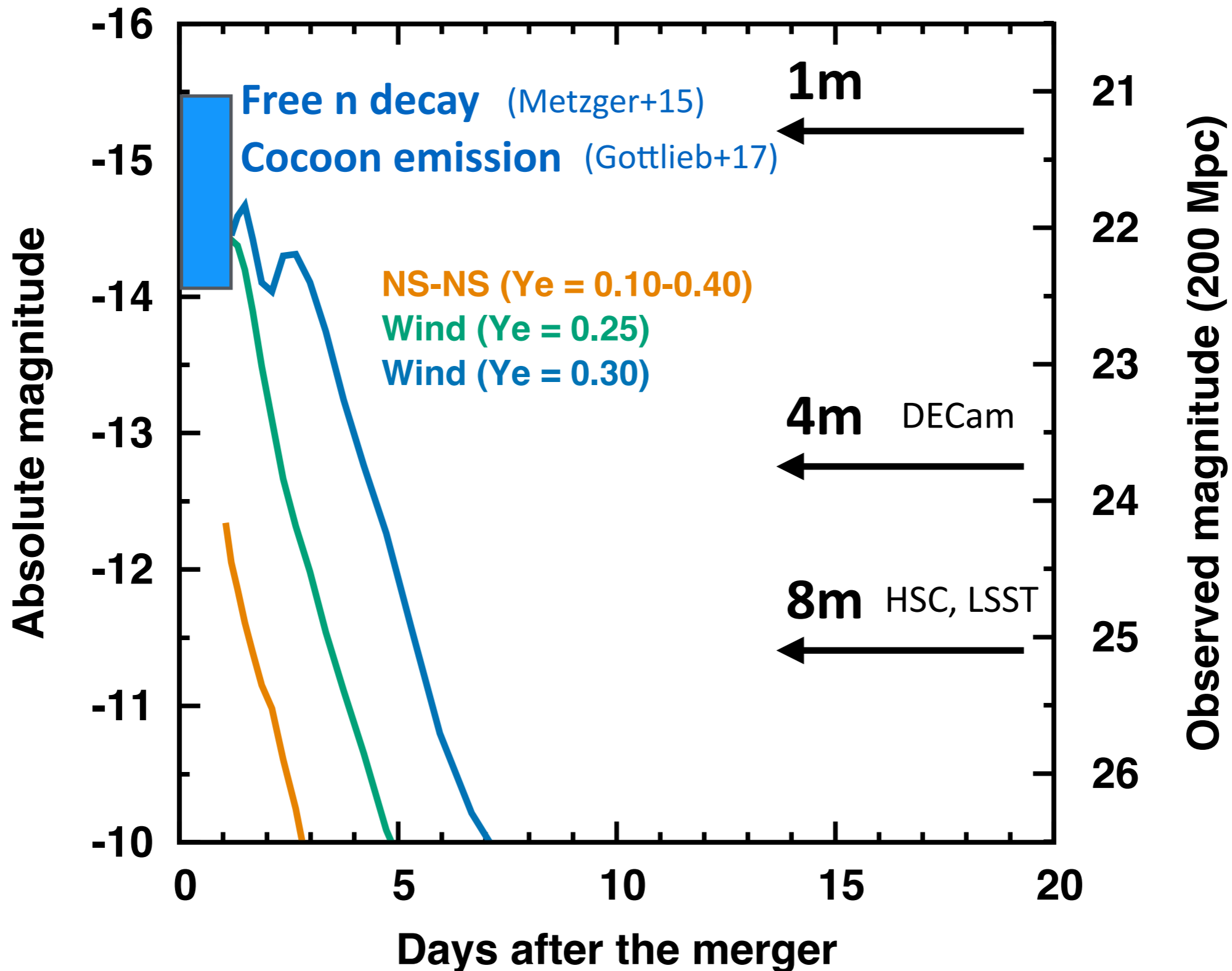
r-band magnitude @ 100 Mpc

$M_{ej} = 0.01 M_{\text{sun}}$



r-band magnitude @ 200 Mpc

$M_{ej} = 0.01 M_{\text{sun}}$



Summary

- **Guides from theory are important for observations**
- **New opacity calculations for Se, Ru, Te, Nd, and Er**
- **Opacity sensitively depends on compositions**
 - $\kappa \sim 0.5 \text{ cm}^2 \text{ g}^{-1}$ for $Y_e \sim 0.3$ (Lanthanide free)
 - $\kappa \sim 10 \text{ cm}^2 \text{ g}^{-1}$ for solar abundance
- **Kilonova brightness depends on compositions**
 - Optical: 22-25 mag for ~ 3 days @ 200 Mpc (0.01 Msun)
 - NIR: 22-24 mag for ~ 7 days @ 200 Mpc (0.01 Msun)
- **Accurate estimate of Y_e in merger simulations is critical**