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Jets in SCET

Precision Spectroscopy of QGP with Jets and Heavy Quarks,

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Outline of the talk

- A brief introduction to effective field theories (EFTs). SCET
- Semi-inclusive jet cross sections in SCET and jet radius resummation.
- Consistent calculation of jet cross sections at NLO in heavy ion reactions
- Application of SCET to jet substructure, splitting and fragmentation
- Conclusions
- ... Toward heavy flavor jets



Thanks to the organizers for the invitation and for providing sunny weather on Sunday

Much of the credit for this work goes to my collaborators: Y.-T. Chien, Z.-B. Kang, G. Ovanesyan, F. Ringer

Introduction



The Fermi interaction

The first, probably best known, effective theory is the Fermi interaction





Holds for most relevant neutrino processes. First direct observation of the neutrino, Nov. 1970





E. Fermi (Nobel Prize)



- Effective theories are ubiquitous. The Standard Model is likely a low energy EFT of a theory at a much higher scale
- Particularly well suited to QCD, HEP and nuclear physics

Examples of effective field theories [EFTs]

DOF in FT DOF in EFT	Full Theory Effective	 Focus on the significant degrees of freedom [DOF]. Manifest power counting 			
	Theory	Q po	ower counting	DOF in F1	DOF in EFT
Chiral Perturbation Theory (ChPT)) Aqcd	p/Aqcd	q, g	Κ,π
Heavy Quark Effective Theory (HQET)		mb	Λ_{QCD}/m_b	ψ,A	h _v ,A _s
Soft Collinear Effective Theory (SCET)		Q	P⊥/Q	ψ,A	ξ_n, A_n, A_s

SCET formulation

Modes in SCET	C. Bauer et al. (2001)		D. Pirol et al. (2004)	
Collinear quarks, antiquarks	$\xi_n, \ \overline{\xi}_n$	Soft quarks are eliminated through the equations of motion		
Collinear gluons, soft gluons	A_n, A_s			
	modes	$p^{\mu} = (+, -, \bot$	$)$ p^2	fields
SCET	$\operatorname{collinear}$	$Q(\lambda^2,1,\lambda$	A) $Q^2\lambda^2$	ξ_n, A^{μ}_n
II	soft	$Q(\lambda,\lambda,\lambda)$	$) \qquad Q^2\lambda^2$	q_s,A^μ_s
D. Neill et al. (2012)				

Other formulations, e.g. SCET₁ and ultrasoft particles



Resummation, RG equations and Higgs production at the LHC

 SCET is very effective in resumming in large logarithms of ratios of energy/ mass scales using Renormalization Group equations

$$\ln \sigma(\tau) \sim \alpha_s (\ln^2 \tau + \ln \tau) + \ln \tau) + \alpha_s^2 (\ln^3 \tau + \ln^2 \tau + \ln \tau) + \alpha_s^3 (\ln^4 \tau + \ln^3 \tau + \ln^2 \tau + \ln \tau) + \frac{1}{2} (\ln^4 \tau + \ln^3 \tau + \ln^2 \tau + \ln \tau) + \frac{1}{2} (\ln^4 \tau + \ln^3 \tau + \ln^2 \tau + \ln \tau) + \frac{1}{2} (\ln^4 \tau + \ln^2 \tau + \ln^2 \tau) + \frac{1}{2} (\ln^4 \tau + \ln^2 \tau) + \frac{1}{2} (\ln^4 \tau + \ln^2 \tau + \ln^2 \tau) + \frac{1}{2} (\ln^4 \tau + \ln^2 \tau + \ln^2 \tau) + \frac{1}{2} (\ln^4 \tau + \ln^2 \tau + \ln^2 \tau) + \frac{1}{2} (\ln^4 \tau + \ln^2 \tau) + \frac{1}{2} (\ln^4 \tau + \ln^2 \tau + \ln^2 \tau) + \frac{1}{2} (\ln^4 \tau + \ln^4 \tau)$$

Traditional techniques such as CCS.
 SCET systematizes the approach and facilitates resummation

J. Collins



Semi-Inclusive Jet Calculations in SCET



Exclusive approach to jets in SCET



TASSO (1979)

PETRA at DESY 12 GeV < CM energy < 47 GeV



 Motivated by early e+ e- annihilation, SCET assumes that all energy goes into a well defined number of jets

Factorized expression

$$\sigma = \operatorname{Tr}(HS) \otimes \prod_{i=1}^{n_B} B_i \otimes \prod_{j=1}^N J_j$$

- Nomenclature: H hard function, S soft function, Bbeam function, J – jet function.
- Leads to multiplicative RG evolution

The exclusive view of a process in SCET summarized as $\frac{1}{\sigma_0} \frac{d\sigma}{dE_r dp_{T_i} dy_i} = H(p_{T_i}, y_i, \mu) J_{\omega_1}(E_r, \mu) J_{\omega_2}(\mu) \dots J_{\omega_N}(\mu) S_{n_1 n_2 \dots n_N}(\Lambda, \mu)$ $+ \mathcal{O}\left(\frac{\Lambda}{Q}\right) + \mathcal{O}(R) .$

Define a jet energy function

$$J_{\omega}(E_r,\mu) = \sum_{X_c} \langle 0|\bar{\chi}_{\omega}(0)|X_c\rangle \langle X_c|\chi_{\omega}(0)|0\rangle \delta(E_r - \hat{E}^{< r}(X_c))$$

Phase space for the jet energy distribution



Take as an example the jet shape (integral jet shape)

$$\Psi_{\omega}(r) = \frac{\langle E_r \rangle_{\omega}}{\langle E_R \rangle_{\omega}} = \frac{J_{\omega}^{E_r}(\mu)/J_{\omega}(\mu)}{J_{\omega}^{E_R}(\mu)/J_{\omega}(\mu)} = \frac{J_{\omega}^{E_r}(\mu)}{J_{\omega}^{E_R}(\mu)}$$

- To first non-trivial order, the phase space for the jet shape contributions is tractable
- Important to understand that in analytic calculations jet observables are calculated directly from their definition and the splitting kinematics at FO

Y.-T. Chien et al. (2014)

Integral jet function

$$\frac{2}{\omega}J_{\omega}^{qE_r}(\mu) = \alpha_s \left[a \ln^2 \frac{\omega^2 \tan^2 \frac{r}{2}}{\mu^2} + b \ln \frac{\omega^2 \tan^2 \frac{r}{2}}{\mu^2} + \text{finite} \right]$$

The idea is to eliminate the large logarithms from the fixed order (FO) expression by scale choice and put them in evolution

Need the distribution of the average energy

$$J^{E_r}_{\omega}(\mu) = \int dE_r E_r \ J_{\omega}(E_r,\mu)$$

NLL calculation of jet shapes

We use SCET resummation techniques and SCET_{G.}

We start form the natural scales that eliminate all large logarithms in the fixed order calculation and evolve to a common scale [resumming ln(r/R)]

Multiplicative RG evolution Logarithms of α_sln²X type

$$\frac{dJ_{\omega}^{qE_r}(\mu)}{d\ln\mu} = \left[-C_F \Gamma_{\text{cusp}}(\alpha_s) \ln \frac{\omega^2 \tan^2 \frac{R}{2}}{\mu^2} - 2\gamma^q(\alpha_s) \right] J_{\omega}^{qE_r}(\mu)$$
$$\frac{dJ_{\omega}^{gE_r}(\mu)}{d\ln\mu} = \left[-C_A \Gamma_{\text{cusp}}(\alpha_s) \ln \frac{\omega^2 \tan^2 \frac{R}{2}}{\mu^2} - 2\gamma^g(\alpha_s) \right] J_{\omega}^{gE_r}(\mu)$$

 $\mu_{j_R} \approx E_J \times R$

 $\mu_{j_r} \approx E_J \times r$

$$\Gamma_{\text{cusp}}(\alpha_s) = \left(\frac{\alpha_s}{4\pi}\right)\Gamma_0 + \left(\frac{\alpha_s}{4\pi}\right)^2\Gamma_1 + \cdots, \qquad \text{Order} \quad \Gamma_{\text{cusp}} \quad \gamma \quad \beta$$
$$\gamma(\alpha_s) = \left(\frac{\alpha_s}{4\pi}\right)\gamma_0 + \left(\frac{\alpha_s}{4\pi}\right)^2\gamma_1 + \cdots. \qquad \text{NLL} \quad 2\text{-loop} \quad 1\text{-loop} \quad 2\text{-loop}$$

 To resum the jet shape to NLL accuracy

NLL	1-loop	2-loop
β	$\beta_0 = \frac{11}{3}C_A - \frac{4}{3}T_F n_f$	$\beta_1 = \frac{34}{3}C_A^2 - \frac{20}{3}C_A T_F n_f - 4C_F T_F n_f$
$\Gamma_{\rm cusp}$	$\Gamma_0 = 4$	$\Gamma_1 = 4 \left[\left(\frac{67}{9} - \frac{\pi^2}{3} \right) C_A - \frac{20}{9} T_F n_f \right]$
γ	$\gamma_0^q = -3C_F, \ \gamma_0^g = -\beta_0$	

Numerical NLL results in p+p collisions

- We can study the algorithm dependence of the jet shapes (anti)k_T vs cone.
- Significant improvement over fixed order calculation
- Works reasonably well, but there can be room for improvement. Different evolution?



Why may we need inclusive SCET approach?

CERN energies 0.9 TeV < CM energy < 13 TeV

- It is certainly not the case in hadronic collisons (and even more energetic e+ e-) that all the energy goes into jets and beams
- Need to revisit the jet function evolution.
- Conjectured that a different type of evolution may hold, namely DGLAP evolution
 Dasgupta et al. (2014)
- Finally, experimental measurements are (semi) inclusive in nature



CMS (2015)

Experiments measure for example

$$A + B \rightarrow Jet + X$$

Typically no effort to determine what X is

Semi-inclusive jet function in SCET

• Allow for the jet to capture only a fraction of the parton shower energy $z=\omega_J/\omega$

Z. Kang et al. (2016)
$$J_q(z = \omega_J/\omega, \omega_J, \mu) = \frac{z}{2N_c} \operatorname{Tr} \begin{bmatrix} \frac{\pi}{2} \langle 0|\delta(\omega - \bar{n} \cdot \mathcal{P})\chi_n(0)|JX \rangle \langle JX|\bar{\chi}_n(0)|0 \rangle \\ \frac{1}{2N_c} \nabla F \begin{bmatrix} \frac{\pi}{2} \langle 0|\delta(\omega - \bar{n} \cdot \mathcal{P})\chi_n(0)|JX \rangle \langle JX|\bar{\chi}_n(0)|0 \rangle \\ \frac{1}{2N_c} \nabla F \begin{bmatrix} \frac{\pi}{2} \langle 0|\delta(\omega - \bar{n} \cdot \mathcal{P})\chi_n(0)|JX \rangle \langle JX|\bar{\chi}_n(0)|0 \rangle \\ \frac{\pi}{2N_c} \nabla F \end{bmatrix}$$
a At one loop order**b** At tree level $J_q^{(0)}(z, \omega_J) = \delta(1 - z)$ **b** At one loop order $\int_{\alpha}^{(1)}(z, \omega_J) = J_{q \to qg}(z, \omega_J) + J_{q \to q(g)}(z, \omega_J) + J_{q \to (q)g}(z, \omega_J)$ $E = \ln \frac{\mu^2}{\omega_J^2 \tan^2 \frac{\pi}{2}}$ $J_q^{(1)}(z, \omega_J) = J_{q \to qg}(z, \omega_J) + J_{q \to q(g)}(z, \omega_J) + J_{q \to (q)g}(z, \omega_J)$ $E = \ln \frac{\mu^2}{\omega_J^2 \tan^2 \frac{\pi}{2}}$ $= \frac{\alpha_s}{2\pi} \left\{ C_F \left[2 \left(1 + z^2 \right) \left(\frac{\ln(1 - z)}{1 - z} \right)_+ + (1 - z) \right] - \delta(1 - z) d_J^{q, \text{alg}}$ Logarithms and scales $+ P_{gq}(z) 2 \ln (1 - z) + C_F z \},$ $\mu_J = \omega_J \tan \frac{\pi}{2} = (2p_T \cosh \eta) \tan \left(\frac{R}{2 \cosh \eta} \right) \approx p_T R$

Renormalization and evolution of the SIJF

Renormalization matrix to one-loop order



Numerical implementation at NLO

Hard collinear factorization

F. Ringer et al. (2015)

Terms that we keep at NLO

$$\begin{aligned} d\sigma^{pp \to jetX} &\sim \left(d\hat{\sigma}_{ab}^{c,(0)} + d\hat{\sigma}_{ab}^{c,(1)} \right) \otimes \left(J_c^{(0)} + J_c^{(1)} \right) \\ &= \left(d\hat{\sigma}_{ab}^{c,(0)} + d\hat{\sigma}_{ab}^{c,(1)} \right) \otimes J_c^{(0)} + d\hat{\sigma}_{ab}^{c,(0)} \otimes J_c^{(1)} + \mathcal{O}(\alpha_s^2) \end{aligned}$$

We can perform LL_R resummation. Have generalized to NLL_R Z. Kang et al. (2016)

- Fixes the unphysical scale dependence of NLO jet
- Resummation can have up to 30% effect on the inclusive jet cross section for small R

$$\frac{d\sigma^{pp \to \text{jet}X}}{dp_T d\eta} = \frac{2p_T}{s} \sum_{a,b,c} \int_{x_a^{\min}}^1 \frac{dx_a}{x_a} f_a(x_a,\mu) \int_{x_b^{\min}}^1 \frac{dx_b}{x_b} f_b(x_b,\mu)$$
$$\times \int_{x_c^{\min}}^1 \frac{dz_c}{z_c^2} \frac{d\hat{\sigma}_{ab}^c(\hat{s},\hat{p}_T,\hat{\eta},\mu)}{dvdz} J_c(z_c,\omega_J,\mu).$$



Recent applications to inclusive jet production

Data/MC

Is it relevant?

CMS appears to see a difference difference between data and NLO calculations

 Resummation can explain large part of the discrepancy between data and NLO calculations





Jets in Soft Collinear Effective Theory with Glauber Gluons



The big picture for hard probes



The splitting kernels

- What is missing in the SCET Lagrangian is the interaction between the jet and the medium
- Background field approach

A. Idilbi et al. (2008)

G. Ovanesyan et al. (2011)

$$\mathcal{L}_{\mathcal{G}}(\xi_{n}, A_{n}, A_{\mathcal{G}}) = g \sum_{\tilde{p}, \tilde{p}'} e^{-i(\tilde{p} - \tilde{p}') \cdot x} \left(\bar{\xi}_{n, p'} T^{a} \frac{\not{n}}{2} \xi_{n, p} - i f^{abc} A^{\lambda c}_{n, p'} A^{\nu, b}_{n, p} g^{\perp}_{\nu \lambda} \bar{n} \cdot p \right) n \cdot A^{a}_{\mathcal{G}}$$



Gribov et al. (1972)

 Operator formulation for forward scattering / BFKL physics

I. Rothstein et al. (2016)

 Splitting functions are related to beam (B) and jet (J) functions in SCET

W. Waalewjin. (2014)

Y. Dokshitzer (1977)

G. Altarelli et al. (1977)

In-medium parton splittings and medium properties

Direct sum

$$\frac{dN(tot.)}{dxd^2k_{\perp}} = \frac{dN(vac.)}{dxd^2k_{\perp}} + \frac{dN(med.)}{dxd^2k_{\perp}}$$

- Derived using SCET_G
- Factorize form the hard part
- Gauge-invariant
- Depend on the properties of the medium

$$\begin{split} \left(\frac{dN}{dxd^{2}\boldsymbol{k}_{\perp}}\right)_{q \to qg} &= \frac{\alpha_{s}}{2\pi^{2}}C_{F}\frac{1+(1-x)^{2}}{x}\int\frac{d\Delta z}{\lambda_{g}(z)}\int d^{2}\mathbf{q}_{\perp}\frac{1}{\sigma_{el}}\frac{d\sigma_{el}^{\mathrm{medium}}}{d^{2}\mathbf{q}_{\perp}}\left[-\left(\frac{A_{\perp}}{A_{\perp}^{2}}\right)^{2}+\frac{B_{\perp}}{B_{\perp}^{2}}\cdot\left(\frac{B_{\perp}}{B_{\perp}^{2}}-\frac{C_{\perp}}{C_{\perp}^{2}}\right)\right.\\ &\times\left(1-\cos[(\Omega_{1}-\Omega_{2})\Delta z]\right)+\frac{C_{\perp}}{C_{\perp}^{2}}\cdot\left(2\frac{C_{\perp}}{C_{\perp}^{2}}-\frac{A_{\perp}}{A_{\perp}^{2}}-\frac{B_{\perp}}{B_{\perp}^{2}}\right)\left(1-\cos[(\Omega_{1}-\Omega_{3})\Delta z]\right)\\ &+\frac{B_{\perp}}{B_{\perp}^{2}}\cdot\frac{C_{\perp}}{C_{\perp}^{2}}\left(1-\cos[(\Omega_{2}-\Omega_{3})\Delta z]\right)+\frac{A_{\perp}}{A_{\perp}^{2}}\cdot\left(\frac{A_{\perp}}{A_{\perp}^{2}}-\frac{D_{\perp}}{D_{\perp}^{2}}\right)\cos[\Omega_{4}\Delta z]\\ &+\frac{A_{\perp}}{A_{\perp}^{2}}\cdot\frac{D_{\perp}}{D_{\perp}^{2}}\cos[\Omega_{5}\Delta z]+\frac{1}{N_{c}^{2}}\frac{B_{\perp}}{B_{\perp}^{2}}\cdot\left(\frac{A_{\perp}}{A_{\perp}^{2}}-\frac{B_{\perp}}{B_{\perp}^{2}}\right)\left(1-\cos[(\Omega_{1}-\Omega_{2})\Delta z]\right)\right]. \end{split}$$

N.B. $x \rightarrow 1-x$ A,...D, $\Omega_1 ... \Omega_5 - functions(x, k_{\perp}, q_{\perp})$

New physics – many-body quantum coherence effects



- Can be evaluated numerically
- Need numerical implementation

Calculating the jet cross section at NLO in the medium

- Master formula
- Modified jet function

$$\frac{d\sigma^{pp\to jet X}}{dp_T d\eta} = \sum_{a,b,c} f_a \otimes f_b \otimes H^c_{ab} \otimes J_c$$



The first diagram does not contribute to medium induced radiative corrections (included only once)

One needs to consider single and double Born interactions with the medium

$$|\mathcal{A}_{\mathrm{SB}}^{\mathrm{med}}|^2 + 2\mathfrak{Re}\left\{\mathcal{A}_{\mathrm{DB}}^{\mathrm{med}} \times \mathcal{A}^{\mathrm{vac}}
ight\}$$

M. Gyulassy et al. (2000)

Evaluating the in-medium jet function

(B)

 Can we formulate the evaluation of the jet function in a way suitable for numerical implementation

(B) =
$$\delta(1-z) \int_0^1 dx \int_0^{x(1-x)\omega \tan(R/2)} dq_\perp P_{qq}(x,q_\perp)$$

(C) = $-\delta(1-z) \int_0^1 dx \int_0^\mu dq_\perp P_{qq}(x,q_\perp)$ Sum
rules

(D) =
$$\int_{z(1-z)\omega \tan(R/2)} dq_{\perp} P_{qq}(z, q_{\perp})$$

(E) =
$$\int_{z(1-z)\omega \tan(R/2)}^{\mu} dq_{\perp} P_{gq}(z, q_{\perp})$$

$$J_q^{\mathrm{med},(1)}(z,\omega R,\mu) = \left[\int_{z(1-z)\omega \tan(R/2)}^{\mu} dq_{\perp} P_{qq}(z,q_{\perp}) \right]_+$$

 $+ \int_{z(1-z)\omega\tan(R/2)}^{\mu} dq_{\perp} P_{gq}(z,q_{\perp}) \,.$

- Stable in numerical implementation
- Similarly for gluon jets

Results for jet cross sections at NLO

In the medium it is strictly NLO

No multiple splittings, no collisional energy loss (to be revisited)

Possibilities: better evaluation of the splitting functions, collisional energy loss, larger jet-medium coupling, ...

One possibility is cold nuclear matter effects in the initial state (p+A)



$$d\sigma_{\rm PbPb}^{\rm jet} = d\sigma_{pp}^{\rm jet,vac} + d\sigma_{\rm PbPb}^{\rm jet,med}$$

$$d\sigma_{\rm PbPb}^{\rm jet,med} = \sum_{i=q,\bar{q},g} \sigma_i^{(0)} \otimes J_i^{\rm med}$$



Radius dependence of jet suppression

- For medium-induced radiative corrections
 smaller R jets more suppressed
- For collisional energy loss approx.
 constant with R (up to R~1)
- Strong coupling models have argued larger suppression with larger jet R





Consistent within error bars. But then any small separation ordering will be

Resolution deferred to earlier ATLAS measurements. Sees R ordering but weaker than predicted

Centrality dependence of jet suppression

Nuclei are macroscopic objects. One can define centrality of the collision

Changes the size of the medium

The temperature of the medium

The vacuum and medium contribution to jet functions

The overall level of suppression

(in the most peripheral collisions expected to disappear)



Z. Kang et al. (2017)

The centrality dependence appears to be well captured

Jet substructure observables in SCET



"I'm firmly convinced that behind every great man is a great computer."

Many observables to access jet substructure have emerged in SCET

Groomed jet distribution using "soft drop"





- Definition eliminates soft and collinear divergences to the observable
- probe the early time dynamics / splitting



 $\begin{aligned} & \operatorname{QGP\,size}\sim\operatorname{10fm}\\ & \tau_{\mathrm{br}}[\mathrm{fm}] = \frac{0.197~\mathrm{GeV}~\mathrm{fm}}{z_g(1-z_g)\,\omega[\mathrm{GeV}]\,\tan^2(r_g/2)} \end{aligned}$

Typical situation: E=200 GeV, $r_g = 0.1$ Branching time < 2 fm for z_g studied

Y. T. Chien et al . (2016)

Accessing the hardest branching in HIC – longitudinal modification

Calculating the soft dropped distribution with $\beta=0$



NB: data is preliminary, being reanalyzed, pints can change

Centrality and p_T dependence

(Collisional) energy loss of individual branches does not help

Evolution in pT is slowish theoretically . Experimental data fluctuates more but beware of error bars

Centrality dependence as expected – reduced effect for peripheral collisions

Y.T Chien et al . (2016)

Modification of the angular distribution of hardest branchings

New observable proposed – measures the typical splitting angle modification in HIC

$$p_i(r_g) = \frac{\int_{z_{cut}}^{1/2} dx \ p_T x (1-x) \overline{\mathcal{P}}_i(x, k_\perp(r_g, x))}{\int_{z_{cut}}^{1/2} dx \int_{k_\Delta}^{k_R} dk_\perp \overline{\mathcal{P}}_i(x, k_\perp)}$$

Y.-T. Chien et al . (2016)

Flexibility in selecting angular separation r_g

Found that inermediate values $r_g = 0.2$ give the strongest p_T dependence. Though not nearly as strong as preliminary data

Semi-inclusive fragmenting jet function

Generalize the definition to jet and a hadron, sequences of fractions

$$\mathcal{G}_{g}^{h}(z, z_{h}, \omega_{J}, \mu) = -\frac{z \,\omega}{(d-2)(N_{c}^{2}-1)} \delta\left(z_{h} - \frac{\omega_{h}}{\omega_{J}}\right) \langle 0|\delta\left(\omega - \bar{n} \cdot \mathcal{P}\right) \mathcal{B}_{n\perp\mu}(0)|(Jh)X\rangle$$

 $\times \langle (Jh)X | \mathcal{B}_{n+}^{\mu}(0) | 0 \rangle,$

Z. Kang et al . (2016)

Derive to one loop the SIFJF

 $NLO+NLL_B$

$$\begin{aligned}
\mathcal{G}_{q}^{q}(z, z_{h}, \omega_{J}, \mu) &= \delta(1-z)\delta(1-z_{h}) + \frac{\alpha_{s}}{2\pi} \left(-\frac{1}{\epsilon} - L\right) P_{qq}(z_{h})\delta(1-z) + \frac{\alpha_{s}}{2\pi} L P_{qq}(z)\delta(1-z_{h}) \\
&+ \delta(1-z)\frac{\alpha_{s}}{2\pi} \left[2C_{F}(1+z_{h}^{2})\left(\frac{\ln(1-z_{h})}{1-z_{h}}\right)_{+} + C_{F}(1-z_{h}) + 2P_{qq}(z_{h})\ln z_{h}\right] \\
&\times 10^{2} \\
&- \delta(1-z_{h})\frac{\alpha_{s}}{2\pi} \left[2C_{F}(1+z^{2})\left(\frac{\ln(1-z)}{1-z}\right)_{+} + C_{F}(1-z)\right], \quad (2.33a)
\end{aligned}$$

 z_h

 10^{5}

- Agrees with data within uncertainties. •
- However the central values can deviate by • 20% and small z even 40%
- Can be used to constrain FFs

Modification of the fragmentation function

One can carry through the calculation for the jet function for the semiinclusive jet function

+

$$\mathcal{G}_{q}^{q,(1)}(z, z_{h}, \omega R, \mu) = (B) + (C) + (D) = \\ \delta(1 - z_{h}) \left[\int_{z(1-z)\omega \tan(R/2)}^{\mu} P_{qq}(z, q_{\perp}) \right]_{+} \\ + \delta(1 - z) \left[\int_{\mu_{0}}^{z_{h}(1-z_{h})\omega \tan(R/2)} dq_{\perp} P_{qq}(z_{h}, q_{\perp}) \right]$$

- Out of cone contribution this is quenching –more quark jets
- In cone contribution enhance the soft particle, reduce hard

Still in the process of assessing the sensitivity, centrality dependence, etc

CNM-no effect (like on all other substructure observables)

Conclusions

- Effective theories of QCD have enabled important conceptual and breakthroughs in our understanding of strong interactions and very significant improvement in the accuracy of the theoretical predictions
- Only recently were semi-inclusive jet functions (and fragmenting jet functions) introduced and computed to one loop. Found that they satisfy standard time-like DGLAP evolution equations. Allowed to understand jet R resummation to NLL_R Appear to have immediate relevance to th small radius jet measurements at LHC
- Performed a consistent NLO calculation of jet production in SCET_G (an effective theory for jet propagation in matter). Allows us now to also look at jet substructure. Found that at high p_T only part of the suppression can be explained. CNM or collisional energy loss of the shower TBD.
- Progress in performing pQCD / SCET calculations of jet substructure connecting splitting functions through groomed soft-dropped momentum sharing distributions. Jet shapes discussed before and jet fragmentation functions.
- ... Recently extended to heavy flavor and NLO calculations

Open heavy flavor

Heavy quarks in the vacuum and the medium

SCET_{M,G} – for massive quarks with Glauber gluon interactions

$$\mathcal{L}_{\text{QCD}} = \bar{\psi}(i\not\!\!D - m)\psi \quad iD^{\mu} = \partial^{\mu} + gA^{\mu} \quad A^{\mu} = A^{\mu}_{c} + A^{\mu}_{s} + A^{\mu}_{G}$$

Feynman rules depend on the scaling of m. The key choice is $m/p^+ \sim \lambda$

I. Rothstein (2003)

A. Leibovich et al. (2003)

With the field scaling in the covariant gauge for the Glauber field there is no room for interplay with mass in the LO Lagrangian

$$\begin{pmatrix} \frac{dN}{dxd^2k_{\perp}} \end{pmatrix}_{Q \to Qg} = C_F \frac{\alpha_s}{\pi^2} \frac{1}{k_{\perp}^2 + x^2m^2} \left[\frac{1 - x + x^2/2}{x} - \frac{x(1 - x)m^2}{k_{\perp}^2 + x^2m^2} \right]$$
$$\begin{pmatrix} \frac{dN}{dxd^2k_{\perp}} \end{pmatrix}_{g \to Q\bar{Q}} = T_R \frac{\alpha_s}{2\pi^2} \frac{1}{k_{\perp}^2 + m^2} \left[x^2 + (1 - x)^2 + \frac{2x(1 - x)m^2}{k_{\perp}^2 + m^2} \right]$$

The process is not written Q to gQ

F. Ringer et al . (2016)

Result: $SCET_{M,G} = SCET_M \times SCET_G$

- You see the dead cone effects
 Dokshitzer et al. (2001)
- You also see that it depends on the process – it not simply x²m² everywhere: x²m², (1-x)²m², m²

Heavy quarks splitting functions in the medium

Kinematic variables

New physics – manybody quantum coherence effects

$$\begin{split} A_{\perp} &= k_{\perp}, \ B_{\perp} = k_{\perp} + xq_{\perp}, \ C_{\perp} = k_{\perp} - (1-x)q_{\perp}, \ D_{\perp} = k_{\perp} - q_{\perp}, \\ \Omega_{1} - \Omega_{2} &= \frac{B_{\perp}^{2} + \nu^{2}}{p_{0}^{+}x(1-x)}, \ \Omega_{1} - \Omega_{3} = \frac{C_{\perp}^{2} + \nu^{2}}{p_{0}^{+}x(1-x)}, \ \Omega_{4} = \frac{A_{\perp}^{2} + \nu^{2}}{p_{0}^{+}x(1-x)}, \\ \nu &= m \qquad (g \to Q\bar{Q}), \\ \nu &= xm \qquad (Q \to Qg), \\ \nu &= (1-x)m \qquad (Q \to gQ), \end{split}$$
F. Ringer et al. (2016)

$$\begin{split} & \left(\frac{dN^{\text{med}}}{dxd^{2}k_{\perp}}\right)_{Q \to Qg} = \frac{\alpha_{s}}{2\pi^{2}}C_{F}\int \frac{d\Delta z}{\lambda_{g}(z)}\int d^{2}q_{\perp}\frac{1}{\sigma_{el}}\frac{d\sigma_{el}^{\text{med}}}{d^{2}q_{\perp}}\left\{ \left(\frac{1+(1-x)^{2}}{x}\right)\left[\frac{B_{\perp}}{B_{\perp}^{2}+\nu^{2}}\right. \\ & \times \left(\frac{B_{\perp}}{B_{\perp}^{2}+\nu^{2}}-\frac{C_{\perp}}{C_{\perp}^{2}+\nu^{2}}\right)\left(1-\cos[(\Omega_{1}-\Omega_{2})\Delta z]\right)+\frac{C_{\perp}}{C_{\perp}^{2}+\nu^{2}}\cdot\left(2\frac{C_{\perp}}{C_{\perp}^{2}+\nu^{2}}-\frac{A_{\perp}}{A_{\perp}^{2}+\nu^{2}}\right) \\ & -\frac{B_{\perp}}{B_{\perp}^{2}+\nu^{2}}\right)\left(1-\cos[(\Omega_{1}-\Omega_{3})\Delta z]\right)+\frac{B_{\perp}}{B_{\perp}^{2}+\nu^{2}}\cdot\frac{C_{\perp}}{C_{\perp}^{2}+\nu^{2}}\left(1-\cos[(\Omega_{2}-\Omega_{3})\Delta z]\right) \\ & +\frac{A_{\perp}}{A_{\perp}^{2}+\nu^{2}}\cdot\left(\frac{D_{\perp}}{D_{\perp}^{2}+\nu^{2}}-\frac{A_{\perp}}{A_{\perp}^{2}+\nu^{2}}\right)\left(1-\cos[\Omega_{4}\Delta z]\right)-\frac{A_{\perp}}{A_{\perp}^{2}+\nu^{2}}\cdot\frac{D_{\perp}}{D_{\perp}^{2}+\nu^{2}}\left(1-\cos[\Omega_{5}\Delta z]\right) \\ & +\frac{1}{N_{c}^{2}}\frac{B_{\perp}}{B_{\perp}^{2}+\nu^{2}}\cdot\left(\frac{A_{\perp}}{A_{\perp}^{2}+\nu^{2}}-\frac{B_{\perp}}{B_{\perp}^{2}+\nu^{2}}\right)\left(1-\cos[(\Omega_{1}-\Omega_{2})\Delta z]\right)\right] \\ & +x^{3}m^{2}\left[\frac{1}{B_{\perp}^{2}+\nu^{2}}\cdot\left(\frac{1}{B_{\perp}^{2}+\nu^{2}}-\frac{1}{C_{\perp}^{2}+\nu^{2}}\right)\left(1-\cos[(\Omega_{1}-\Omega_{2})\Delta z]\right)+\ldots\right]\right\} \end{split}$$

- Full massive inmedium splitting functions now available
- Can be evaluated numerically

Heavy quark energy loss limit

In the soft gluon emission (x \rightarrow o) energy loss limit only the diagonal splittings survive (Q to Qg)

$$\begin{split} x \left(\frac{dN^{\text{SGA}}}{dxd^2k_{\perp}}\right)_{Q \to Qg} &= \frac{\alpha_s}{\pi^2} C_F \int d\Delta z \frac{1}{\lambda_g(z)} \int d^2 q_{\perp} \frac{1}{\sigma_{el}} \frac{d\sigma_{el}^{\text{med}}}{d^2 q_{\perp}} \\ \text{M. Djordjevic et al . (2003)} & \times \frac{2k_{\perp} \cdot q_{\perp}}{[k_{\perp}^2 + x^2m^2][(k_{\perp} - q_{\perp})^2 + x^2m^2]} \left[1 - \cos\frac{(k_{\perp} - q_{\perp})^2 + x^2m^2}{xp_0^+}\Delta z\right] \end{split}$$

ZMVFS open heavy flavor at NLO

- Typically assumed that only c to D, b to B fragment perturbatively
- Perform an NLO calculation

B. Jager et al . (2002)

$$\frac{d\sigma_{pp}^{H}}{lp_{T}d\eta} = \frac{2p_{T}}{s} \sum_{a,b,c} \int_{x_{a}^{\min}}^{1} \frac{dx_{a}}{x_{a}} f_{a}(x_{a},\mu) \int_{x_{b}^{\min}}^{1} \frac{dx_{b}}{x_{b}} f_{b}(x_{b},\mu)$$
$$\times \int_{z_{c}^{\min}}^{1} \frac{dz_{c}}{z_{c}^{2}} \frac{d\hat{\sigma}_{ab}^{c}(\hat{s},\hat{p}_{T},\hat{\eta},\mu)}{dvdz} D_{c}^{H}(z_{c},\mu),$$

When $p_T > m_c$, m_b

Factorization, non-perturbative physics is long distance

Implications for heavy flavor modification

• A very large contribution of gluon FF to heavy flavor ~50%

The important implication of this will affect the nuclear modification factor

Cross section calculation in the QCD medium

Medium contribution

$$\begin{split} D_q^{H,\mathrm{med}}(z,\mu) &= \int_z^1 \frac{dz'}{z'} D_q^H \left(\frac{z}{z'},\mu\right) \mathcal{P}_{q \to qg}^{\mathrm{med}}(z',\mu) - D_q^H(z,\mu) \int_0^1 dz' \mathcal{P}_{q \to qg}^{\mathrm{med}}(z',\mu) \\ &+ \int_z^1 \frac{dz'}{z'} D_g^H \left(\frac{z}{z'},\mu\right) \mathcal{P}_{q \to gq}^{\mathrm{med}}(z',\mu) \,, \\ D_g^{H,\mathrm{med}}(z,\mu) &= \int_z^1 \frac{dz'}{z'} D_g^H \left(\frac{z}{z'},\mu\right) \mathcal{P}_{g \to gg}^{\mathrm{med}}(z',\mu) - \frac{D_g^H(z,\mu)}{2} \int_0^1 dz' \left[\mathcal{P}_{g \to qg}^{\mathrm{med}}(z',\mu) \right. \\ &+ 2N_f \mathcal{P}_{g \to q\bar{q}}^{\mathrm{med}}(z',\mu) \right] + \int_z^1 \frac{dz'}{z'} \sum_{i=q,\bar{q}} D_i^H \left(\frac{z}{z'},\mu\right) \mathcal{P}_{g \to q\bar{q}}^{\mathrm{med}}(z',\mu) \,. \end{split}$$

For numerical implementation one can rewrite these expression in the + prescription and finds that the correction is negative

Can lead to larger cross section suppression at smaller $\ensuremath{p_{\text{T}}}$

Combined uncertainty

Includes both production mechanism and e-loss vs NLO

- The pure scale uncertainty largely cancels in the ratio
- At high pT there is at least 20% combined uncertainty. Did not increase much since gluon fragmenatation in H is softer and offsets the difference between quark-gluon enegry loss.
- At low PT th eucertainties can grow to 30% D and 50+% B.

Suppression of open heavy flavor in the medium

 For D mesons works reasonably well. Below 10 GeV room for some additional effects: collisional energy loss, dissociation

Z. Kang et al . (2016)

- B mesons there is improvement but not sufficient. Even more room for other nuclear effects
- Nice to extend the approach to include collisional energy losses

Medium-modified jet shapes at NLL

$$E_r(x,k_\perp) = \mathcal{M}_1 + \mathcal{M}_2 + \mathcal{M}_3 + \mathcal{M}_4$$

Measurement operator – tells us how the above configurations contribute energy to J (jet function) One can evaluate the jet energy functions from the splitting functions

$$J^{i}_{\omega,E_{r}}(\mu) = \sum_{j,k} \int_{PS} dx dk_{\perp} \mathcal{P}_{i \to jk}(x,k_{\perp}) E_{r}(x,k_{\perp})$$

$$J_{\omega,E_r}(\mu) = J_{\omega,E_r}^{vac}(\mu) + J_{\omega,E_r}^{med}(\mu).$$

First quantitative pQCD/SCET description of jet shapes in HI