



# Linear Boltzmann Transport for Jet Propagation in the Quark Gluon Plasma

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*In collaboration with  
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and Yan Zhu*

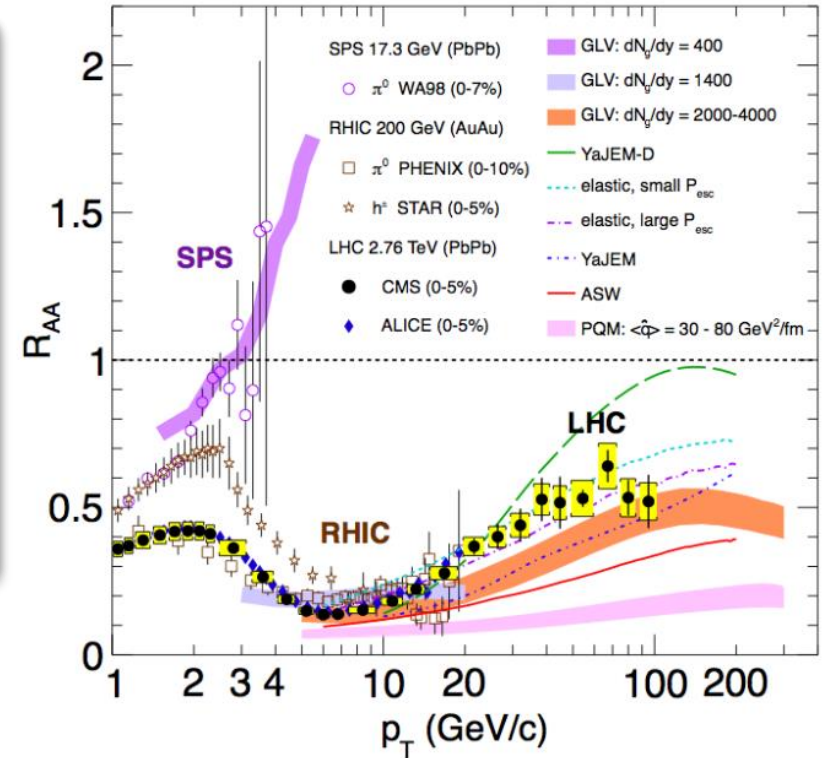
# Outline

- Introduction
- Linear Boltzmann Transport (LBT) model
- Jet modification in heavy-ion collisions
- Summary and Outlook

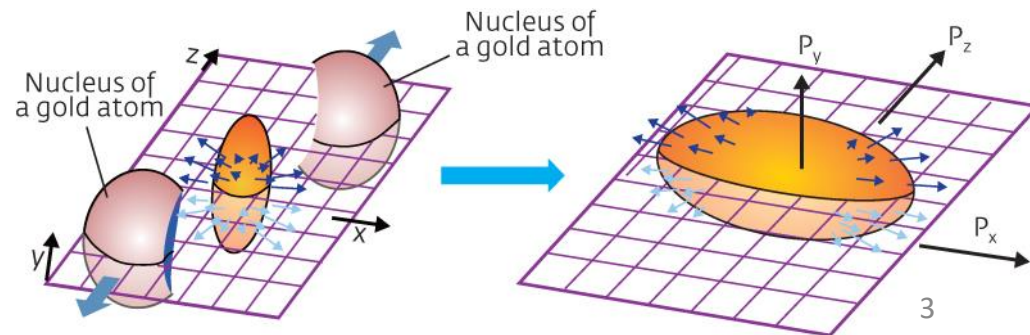
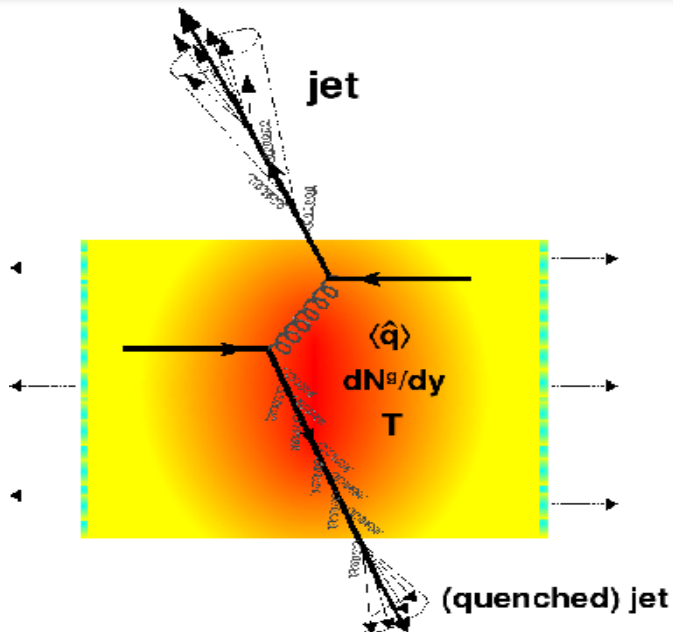
# Introduction

## Jet-Medium interaction

- Suppression of hadrons at high  $p_T$ . ( $R_{AA}$ )
- Path-length dependence of jet quenching. ( $v_2$ )

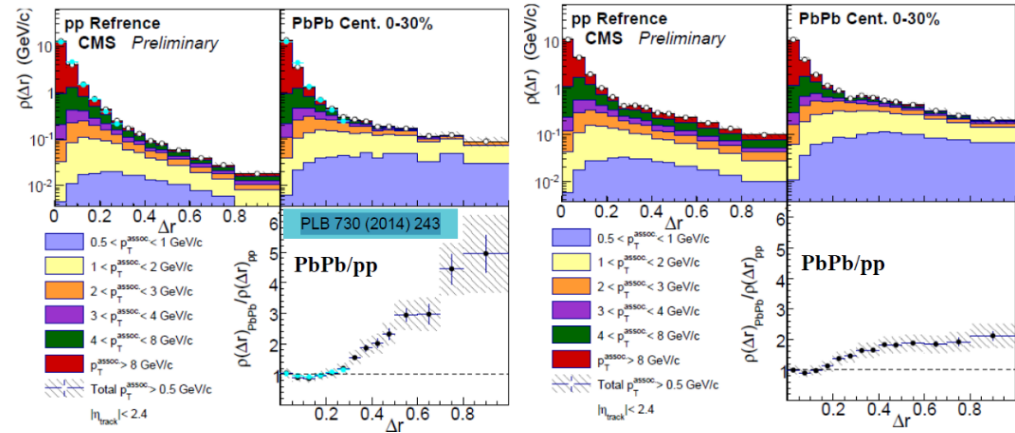
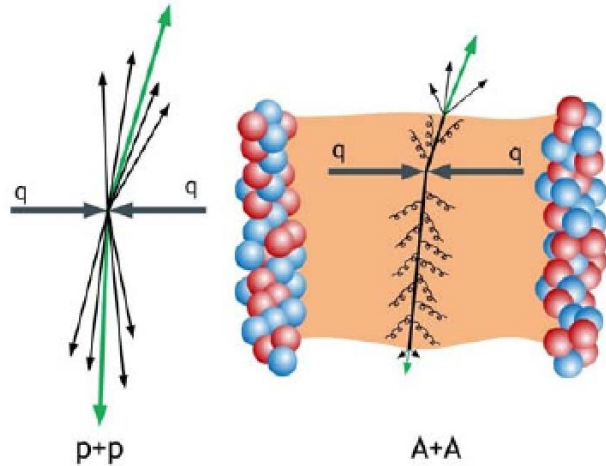


Betz, Barbara Eur.Phys.J. A48 (2012) 164  
 arXiv:1211.5897 [nucl-th]



# Introduction

## The jet shape and transverse momentum imbalance in *Dijet* events

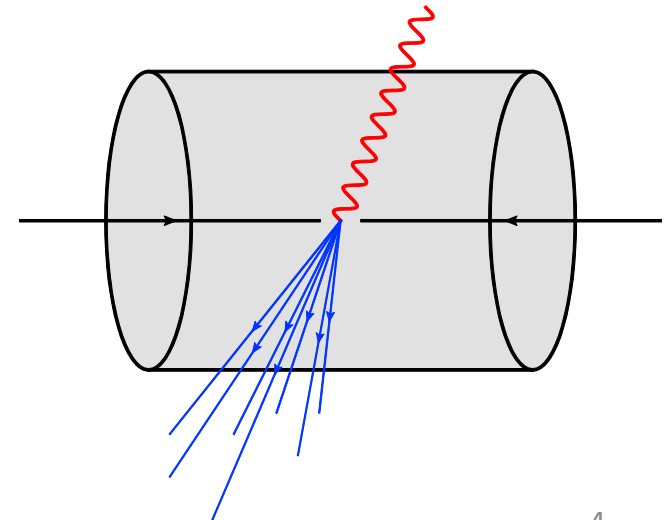


arXiv:1609.02466 CMS

**Gamma-jet** → *The golden channel*

XN Wang, Z Huang Phys. Rev. Lett. 77, 231 (1996)

- High  $p_T$  photons are unmodified by the medium
- No “surface bias” in triggered events which dijet events suffer



# A Linear Boltzmann Transport (LBT) Model

$$p_1 \cdot \partial f_1(x_1, p_1) = E_1 (C_{elastic} + C_{inelastic})$$

## Linear Boltzmann jet Transport

Elastic collision + Induced gluon radiation.

Follow the propagation of recoiled parton.

Include recoiled parton in jet reconstruction.

### Linear Approximation

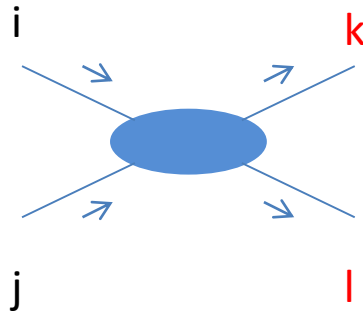
It works when the jet induced medium excitation  $\delta f \ll f$ .

Jet induced medium excitation

("Negative" parton for the **back reaction**)

# Complete set of elastic processes

## Single scattering



$$i, j = g, u, d, s, \bar{u}, \bar{d}, \bar{s}$$

Jussi Auvinen, Kari J. Eskola, Thorsten Renk

Phys.Rev. C82 024906

- Scattering rate for a process  $ij \rightarrow kl$  in the local rest frame of the fluid

$$\Gamma_{ij \rightarrow kl} = \frac{1}{2E_1} \int \frac{d^3 p_2}{(2\pi)^3 2E_2} \int \frac{d^3 p_3}{(2\pi)^3 2E_3} \int \frac{d^3 p_4}{(2\pi)^3 2E_4} \times f_j(p_2 \cdot u, T)$$

$$\times |M|_{ij \rightarrow kl}^2(s, t, u) \times S_2(s, t, u) \times (2\pi)^4 \delta^4(P_1 + P_2 - P_3 - P_4)$$

$$S_2(s, t, u) = \theta(s \geq 2\mu_D^2) \theta(-s + \mu_D^2 \leq t \leq -\mu_D^2) \quad \mu_D^2 = \left(\frac{3}{2}\right) 4\pi\alpha_s T^2$$

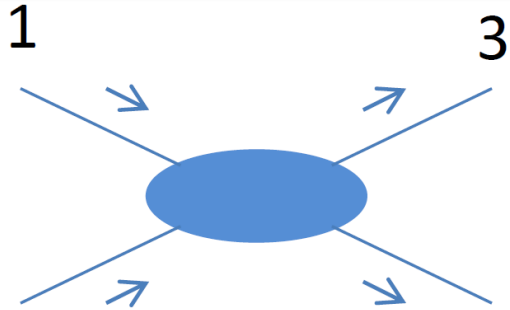
- The mean free path

$$\Gamma_i = \sum_{j,(kl)} \Gamma_{ij \rightarrow kl} = 1/\lambda_0$$

$$P(\Delta t) = 1 - e^{-\Gamma_i \Delta t}$$

$$P(ij \rightarrow kl) = \frac{\Gamma_{ij \rightarrow kl}}{\Gamma_i}$$

# Energy distribution of the recoiled parton



## Single scattering

Dominance of small angle scattering.

Switch of flavor and species of the leading parton.



$$gg \rightarrow gg$$

$$gq \rightarrow gq + g\bar{q} \rightarrow g\bar{q}$$

$$gg \rightarrow q\bar{q}$$

$$q_i \bar{q}_i \rightarrow gg$$

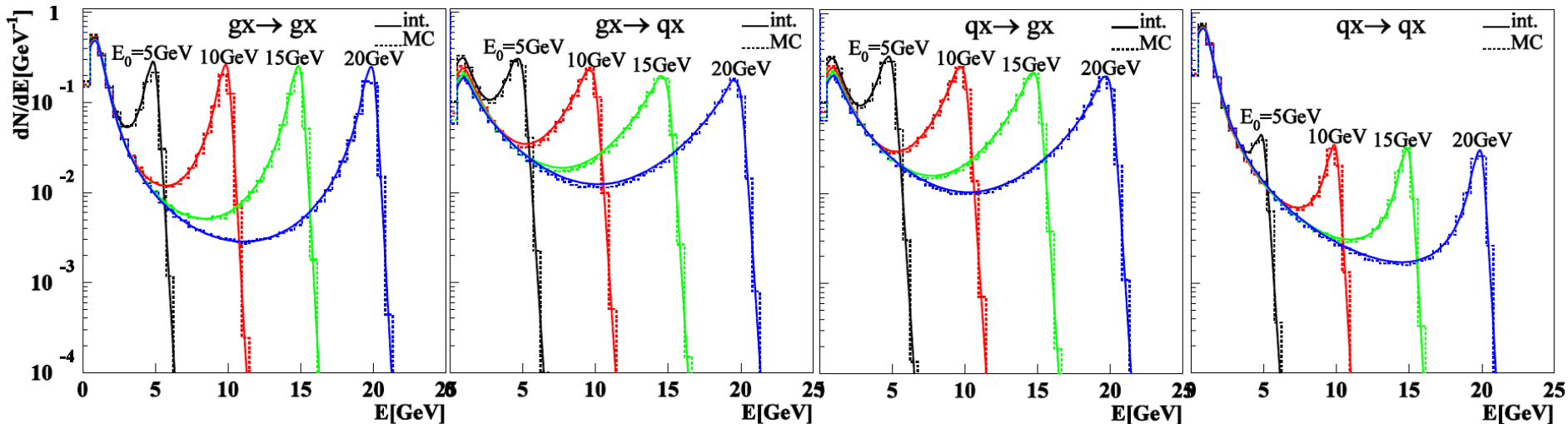
$$q_i g \rightarrow q_i g$$

$$q_i \bar{q}_i \rightarrow q_j \bar{q}_j$$

$$q_i q_j \rightarrow q_i q_j$$

$$q_i \bar{q}_i \rightarrow q_i \bar{q}_i$$

$$q_i q_i \rightarrow q_i q_i$$





# Medium-induced gluon radiations

## Radiated gluon distribution:

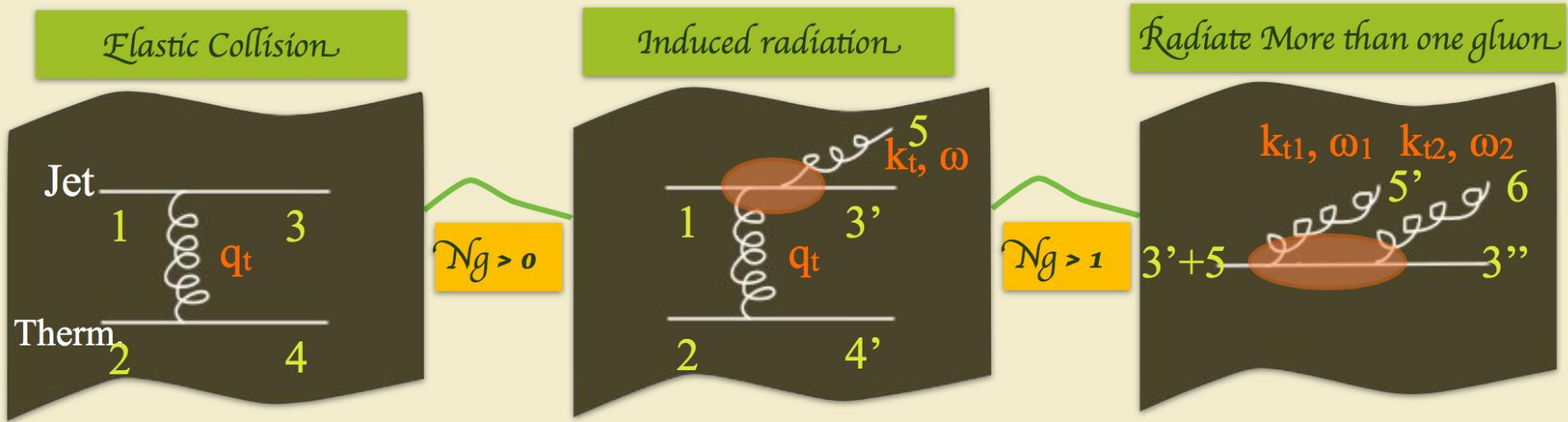
X. Guo, X. Wang PRL 85 (2000) Nucl.Phys. A696 (2001)

$$\frac{dN_g}{dxdk_{\perp}^2 dt} = \frac{2C_A \alpha_s P(x) \hat{q}}{\pi k_{\perp}^4} \sin^2 \frac{t-t_i}{2\tau_f} \quad \tau_f = 2Ex(1-x) / k_{\perp}^2$$

**Multiple gluon emissions:**  $P(N_g, \langle N_g \rangle) = \frac{\langle N_g \rangle^{N_g} e^{-\langle N_g \rangle}}{N_g!}$

**Induced radiations are accompanied by elastic collisions.**

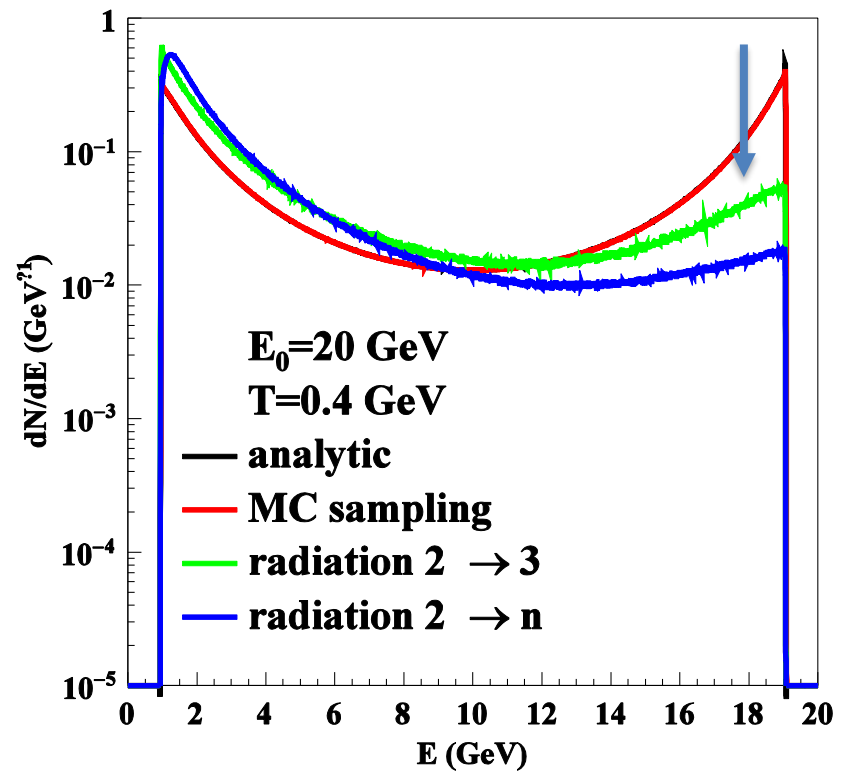
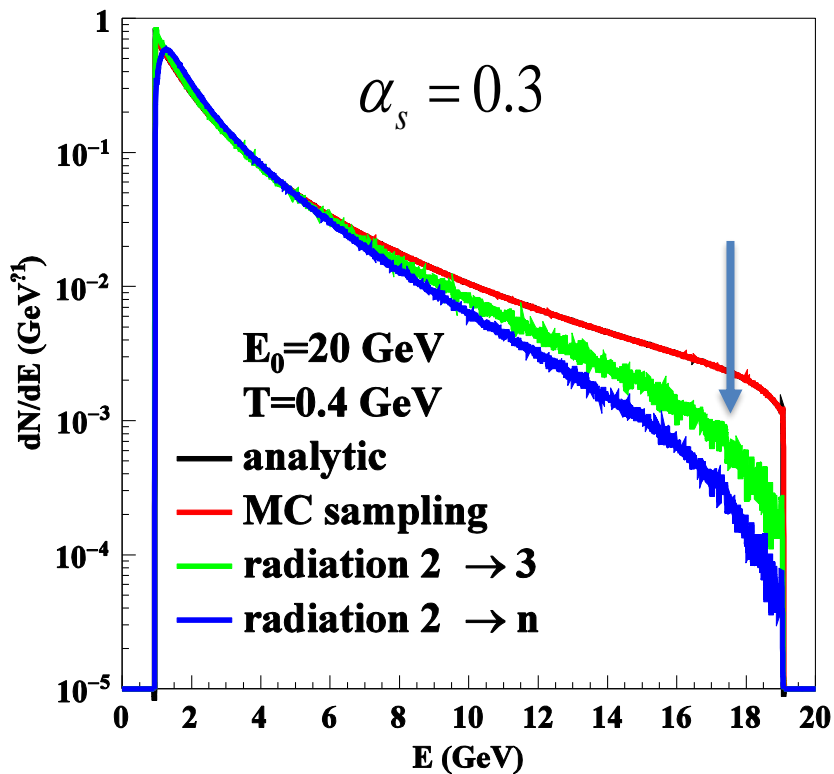
## Jet medium Interaction:





# Energy distribution of the radiated gluon

Global energy-momentum conservation in 2->3 and 2->n processes



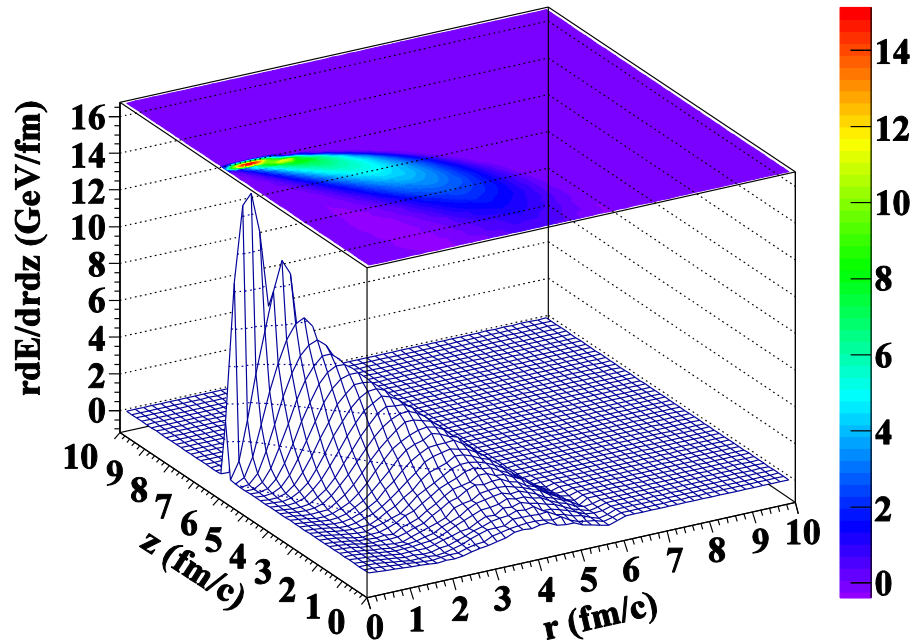
# Jet induced medium excitation (Energy distribution in space)

Initial jet parton: gluon  
 $E = 100 \text{ GeV}$   
 $T = 0.4 \text{ GeV}$        $\alpha_s = 0.3$

- Mach Cone like shock wave and the diffusion wake.

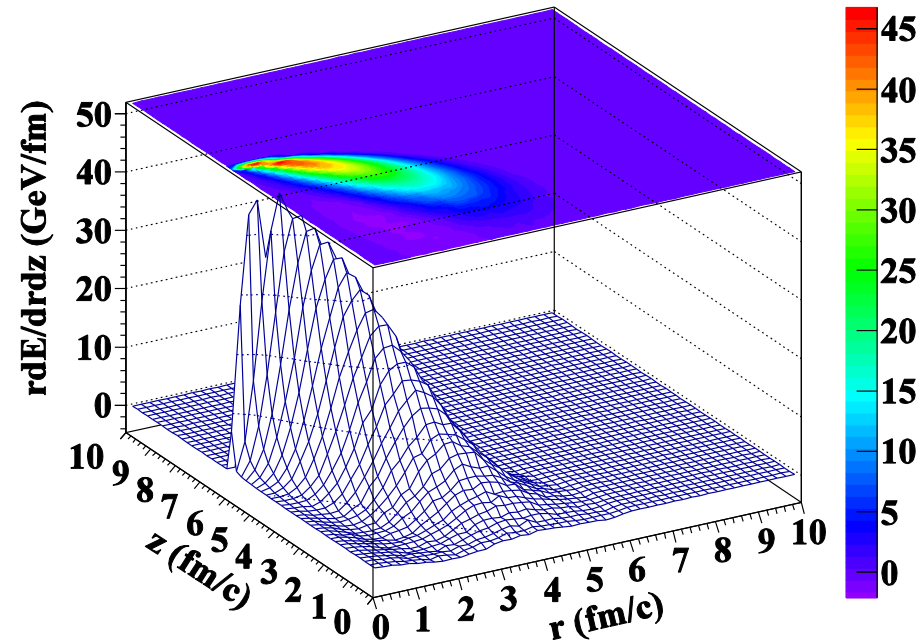
*Elastic only*

gluon: elastic only at  $t=6 \text{ fm/c}$



*Elastic + Radiation*

gluon: elastic + radiation at  $t=6 \text{ fm/c}$

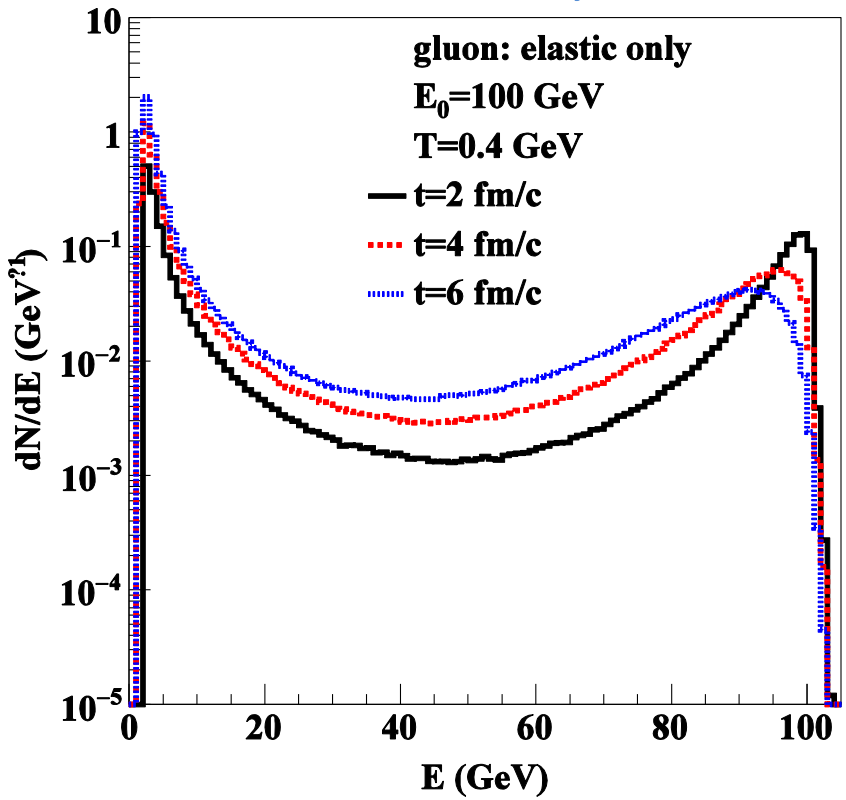


# Jet induced medium excitation (Energy distribution at different time)

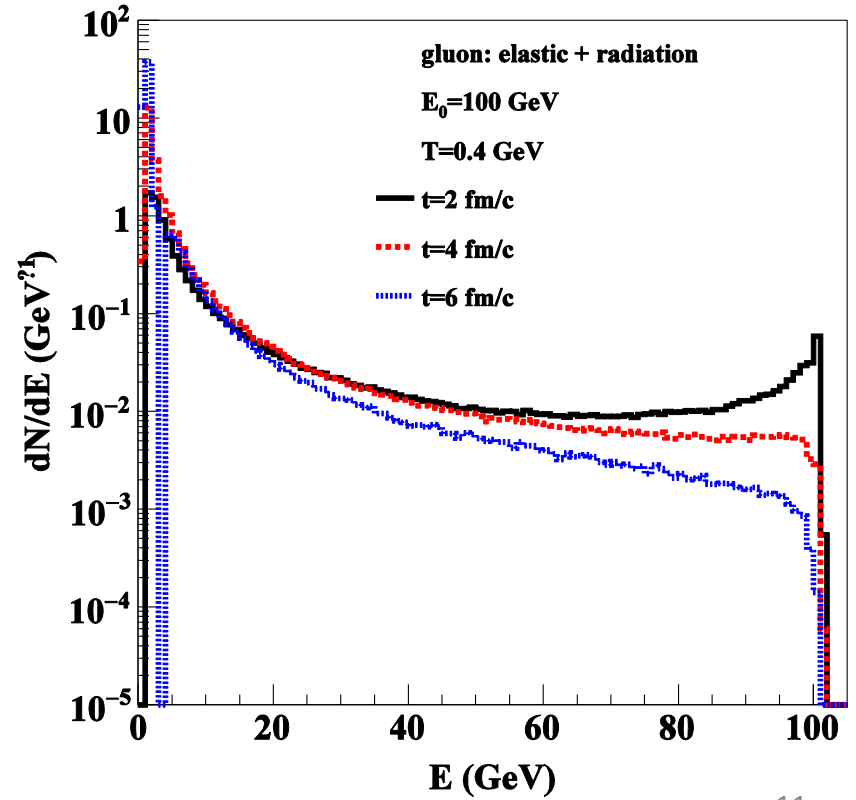
Initial jet parton: gluon  
 $E = 100 \text{ GeV}$   
 $T = 0.4 \text{ GeV}$        $\alpha_s = 0.3$

- Depletion of the energy of the leading parton.

*Elastic only*



*Elastic + Radiation*

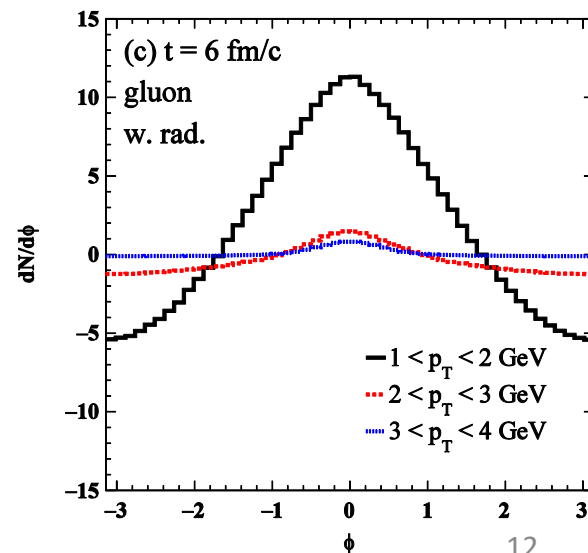
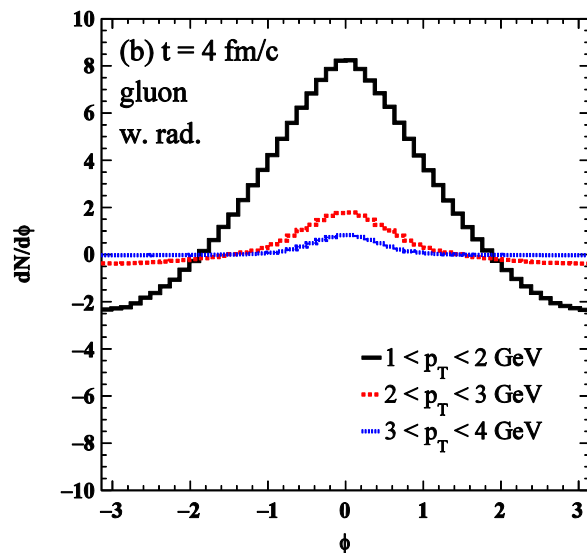
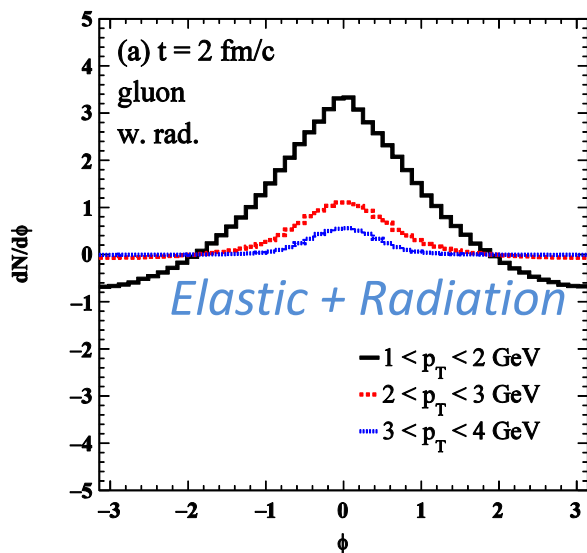
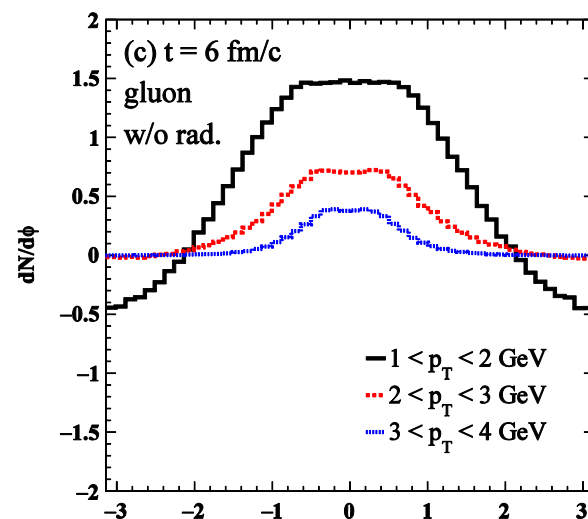
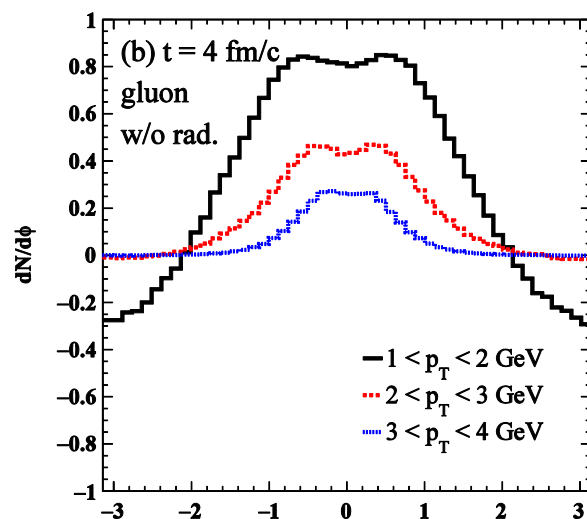
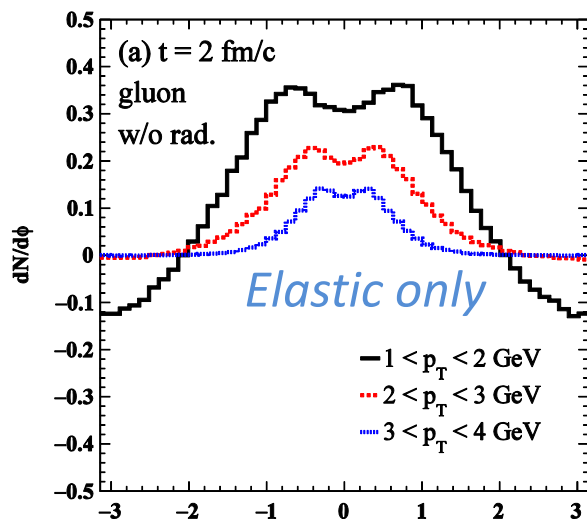


# Jet induced medium excitation (Angular distribution)

$t = 2 \text{ fm}$

$t = 4 \text{ fm}$

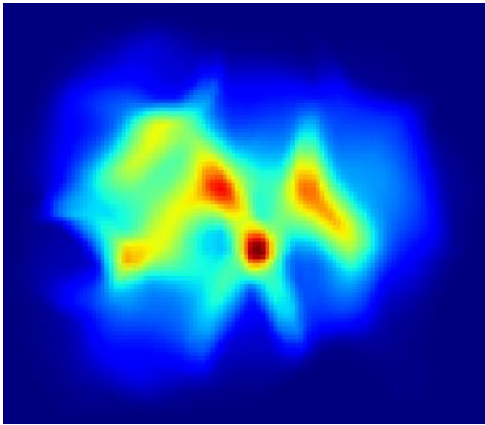
$t = 6 \text{ fm}$



# Jets in a 3+1D hydro

Initial jet shower partons from a p+p collision (Pythia or Hijing)

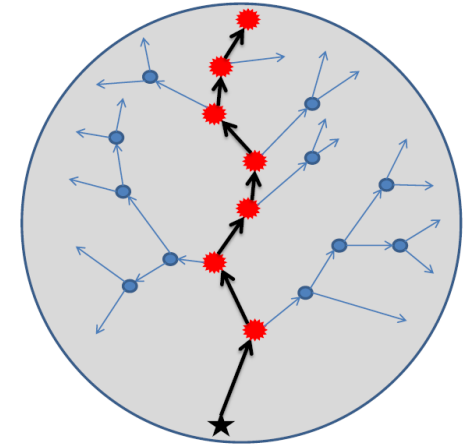
- 3+1D Ideal hydro



$\epsilon T u$

LBT Model

- Location of jets are decided according probability of binary collision.



L-G. Pang, Q. Wang, X-N. Wang  
Phys.Rev. C86 (2012) 024911

M. Cacciari, G. P. Salam and G. Soyez  
Eur. Phys. J. C 72, 1896 (2012).

Jet reconstruction (Fastjet)

# Inclusive jet in pp collisions

## pT distribution in pp collision within Pythia8

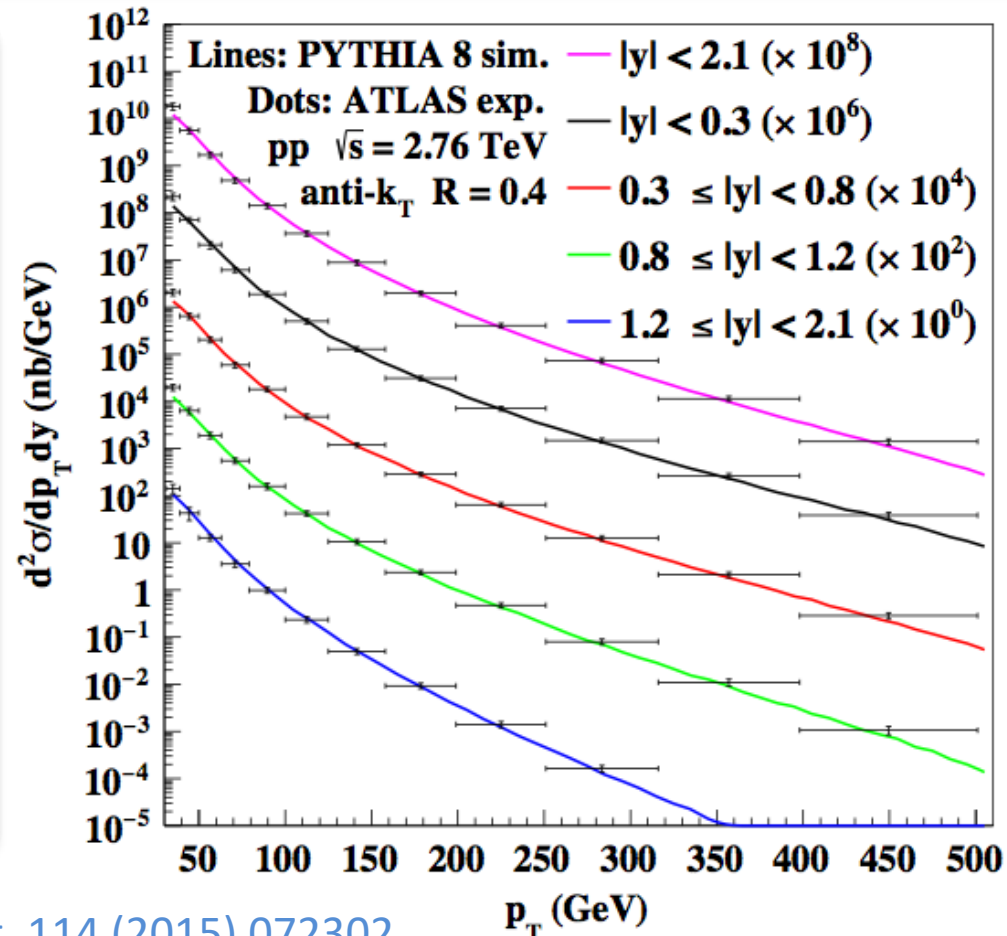
Weighted sampling in triggered p<sub>T</sub> bins to increase the efficiency of MC simulations

In PYTHIA 8 one can obtain the cross section for each triggered p<sub>T</sub> bin

$$\frac{d^2\sigma}{dp_T dy} = \sum_i \sigma_i \frac{1}{N_{events}} \frac{dN_i^{jets}}{dp_T \Delta y}$$

For each bin, the weight is

$$\omega_i = \sigma_i / \sum_i \sigma_i$$

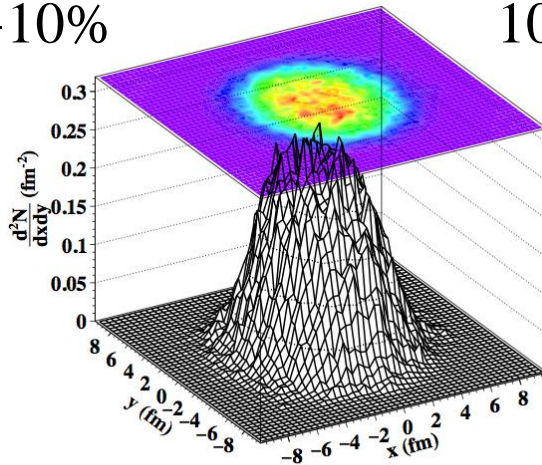




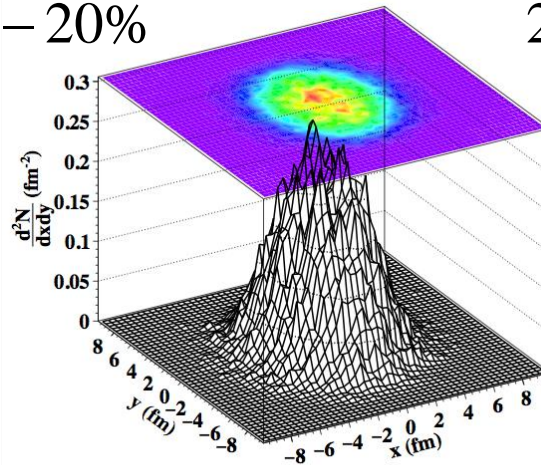
# Initial geometry

Averaged over 200 event-by-event hydro profiles

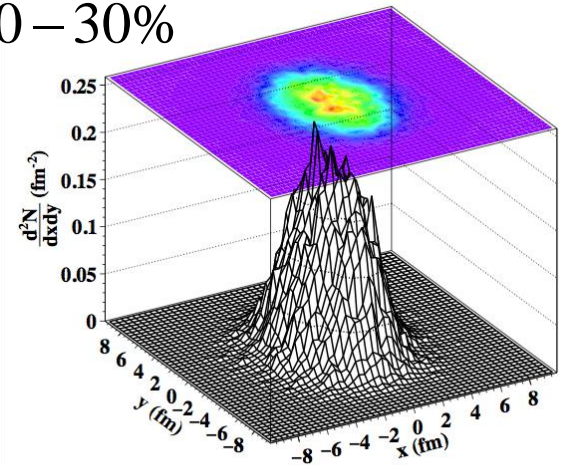
5–10%



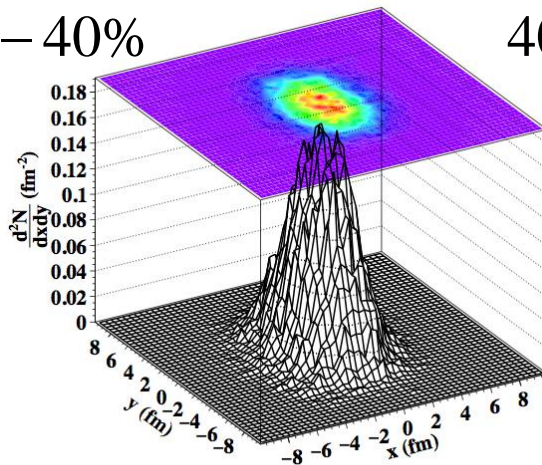
10–20%



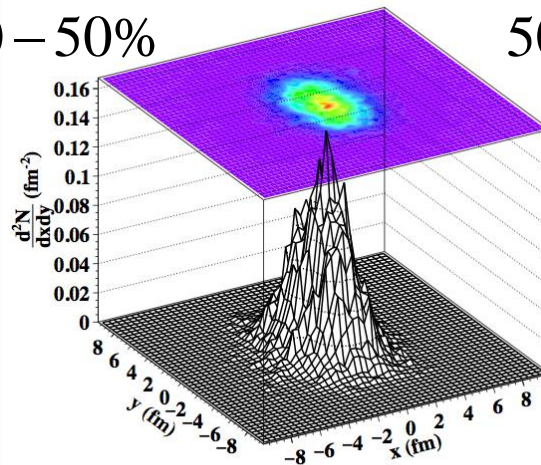
20–30%



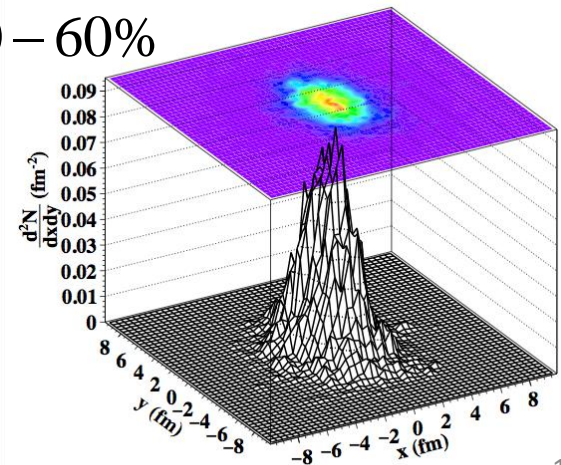
30–40%



40–50%



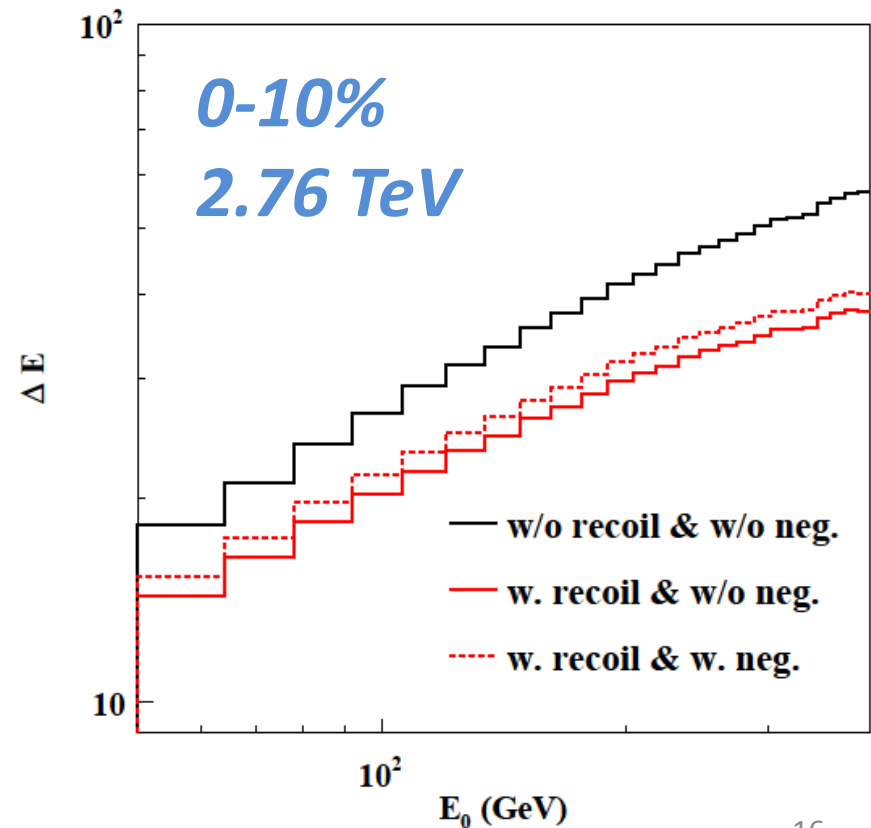
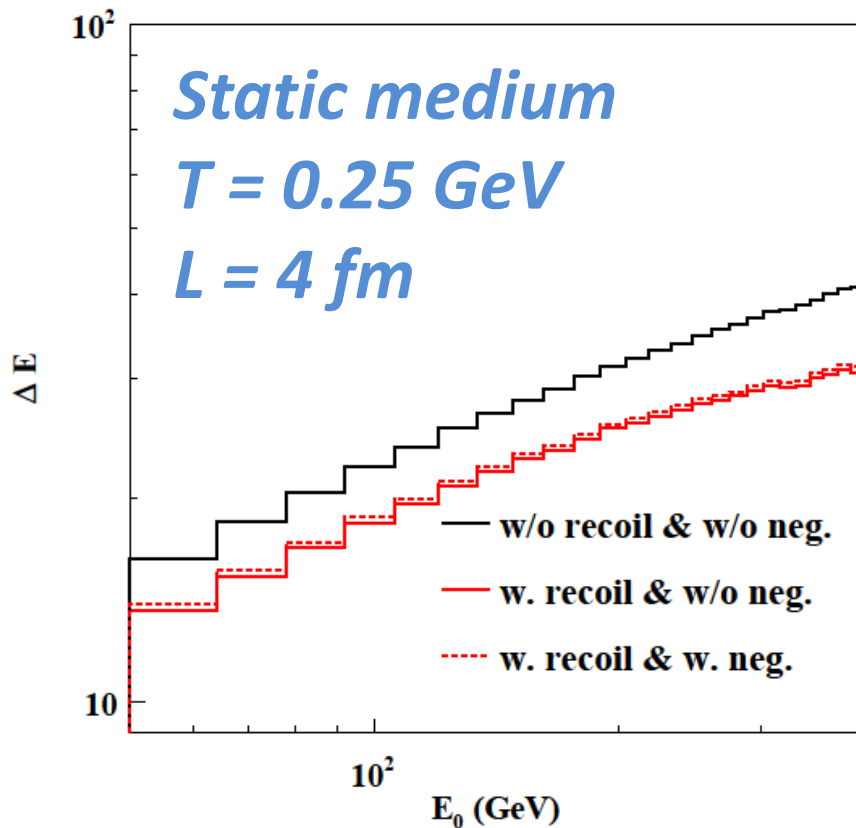
50–60%





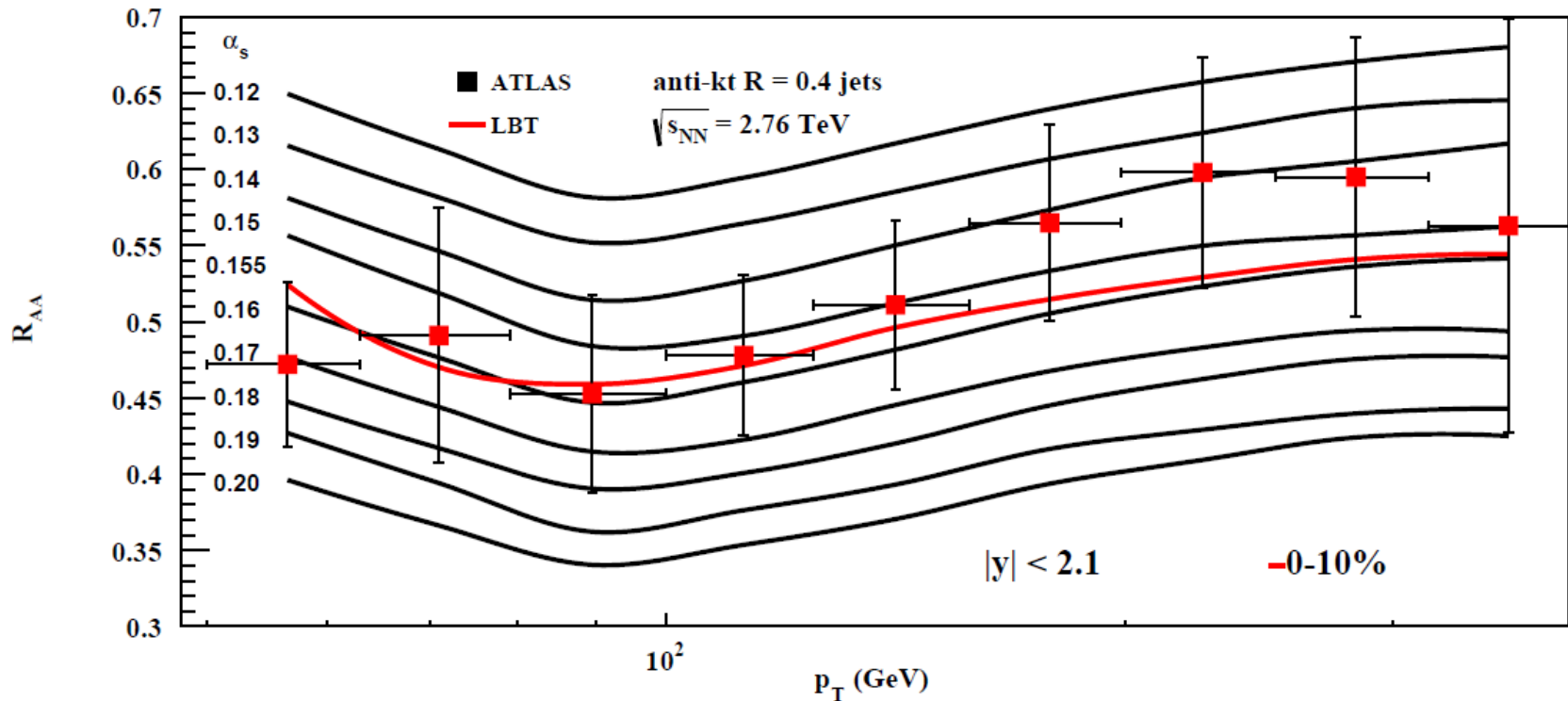
# Recoiled effect in the reconstructed jets

- The inclusion of the recoiled parton in the reconstructed jets will reduce the jet energy loss.
- The recoiled effect is more significant in the evolving medium.



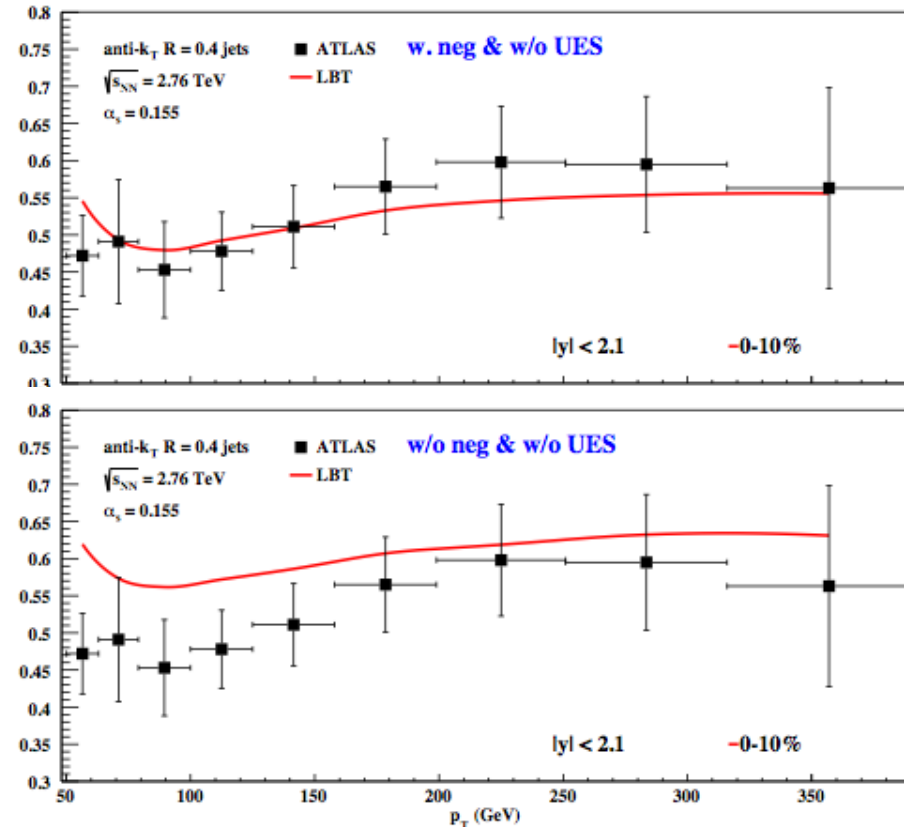
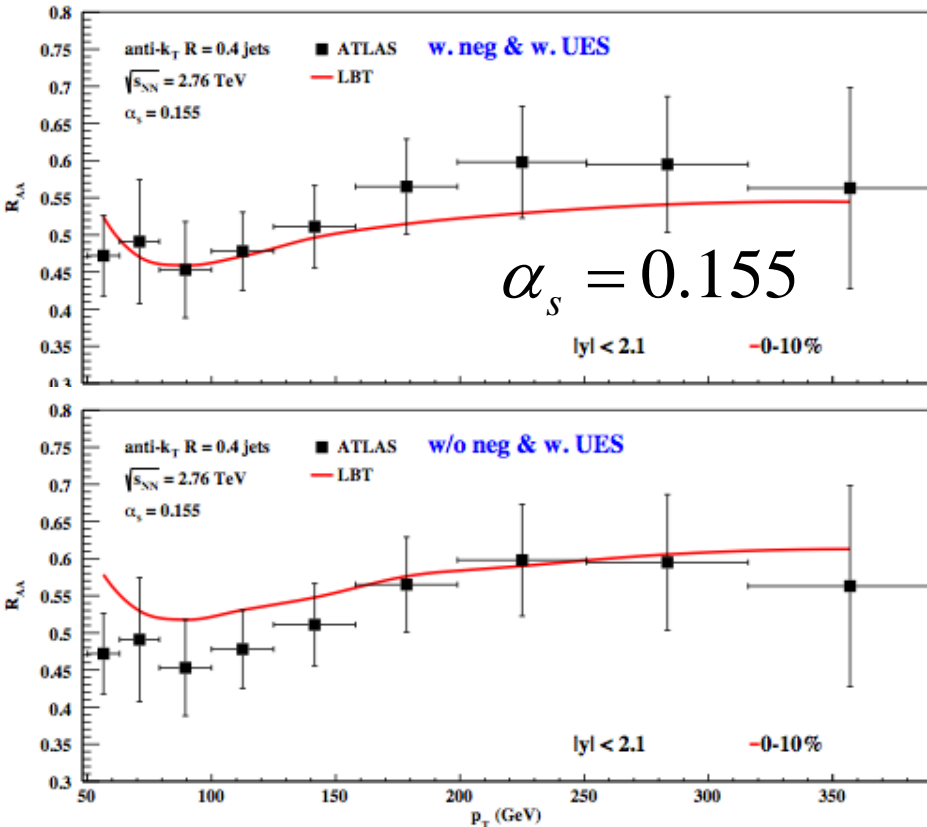
# Nuclear modification factor

- The only parameter strong coupling constant  $\alpha_s$  is fixed.
- We first calculate the single jet  $R_{AA}$  to extract the value of  $\alpha_s$ . (fix the strength of jet-medium interaction)



# Nuclear modification factor

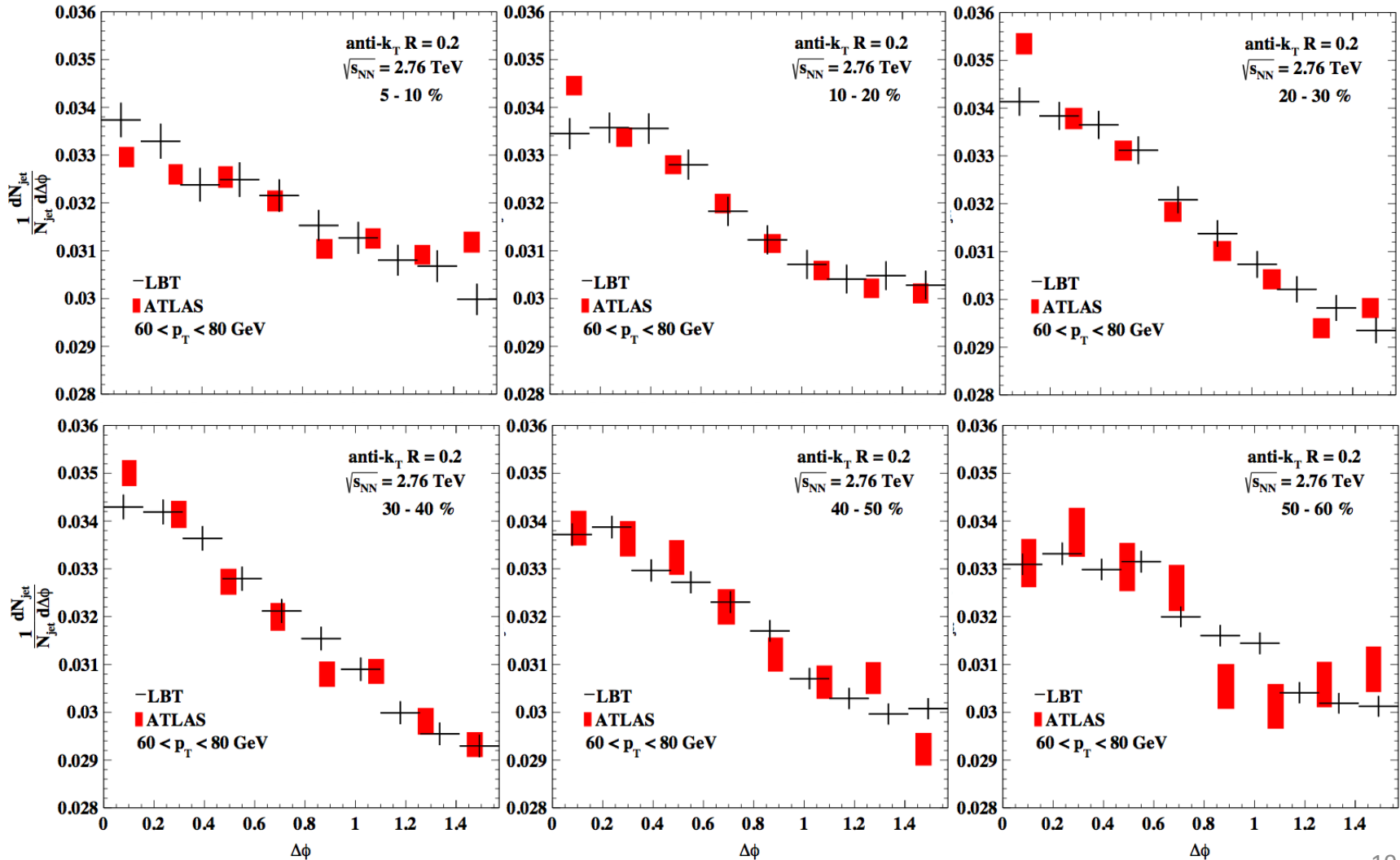
- The inclusion of back reaction (negative parton) will lead to suppression. (on the whole pT range)
- The Underlying Event Subtraction will lead to suppression. (on the low and intermediate pT range)



# Jet azimuthal distribution with different centralities

## Anisotropy shows up

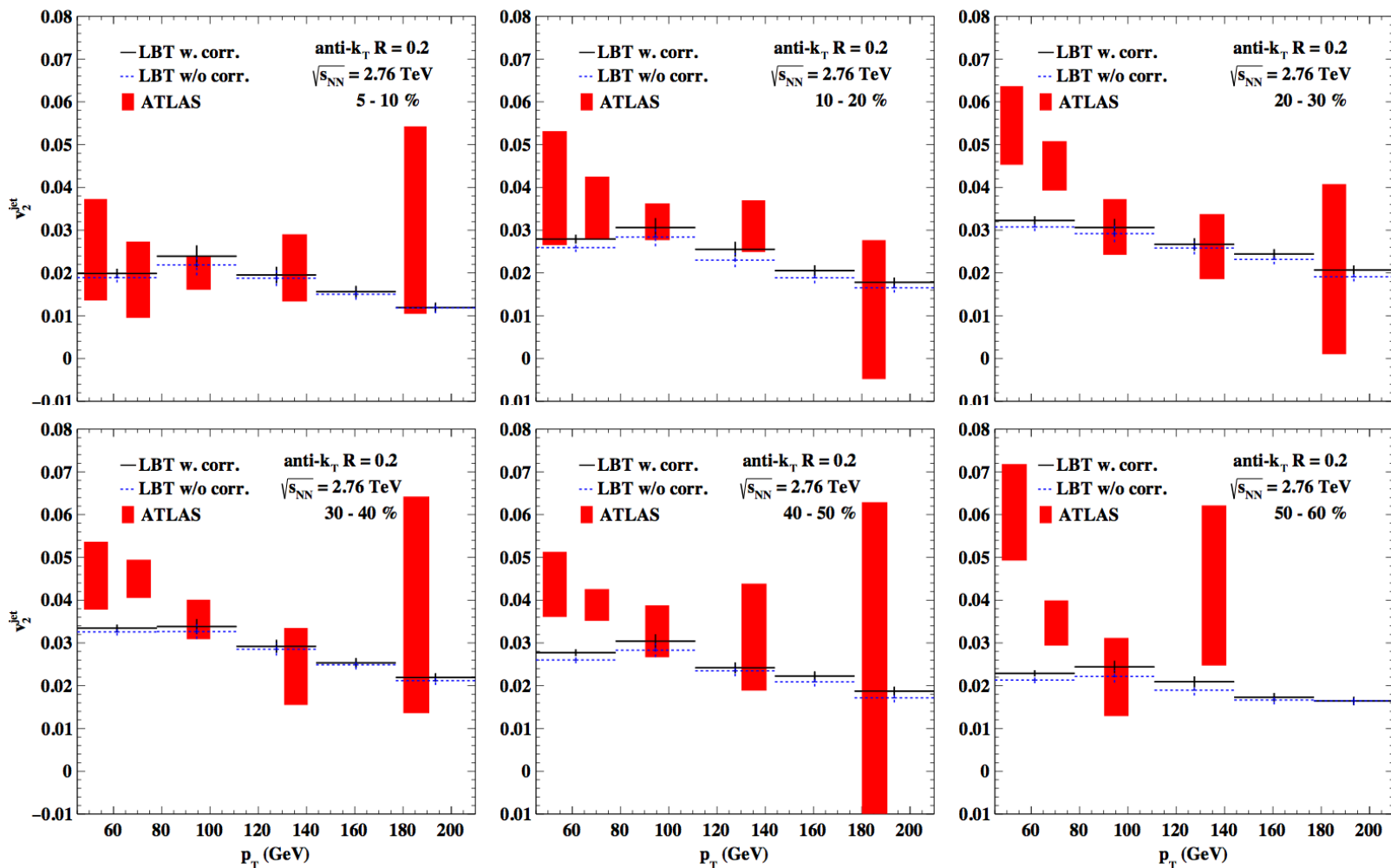
$$\Delta\phi = \phi^{jet} - \Psi_2$$



# Jet $v_2$ with different centralities

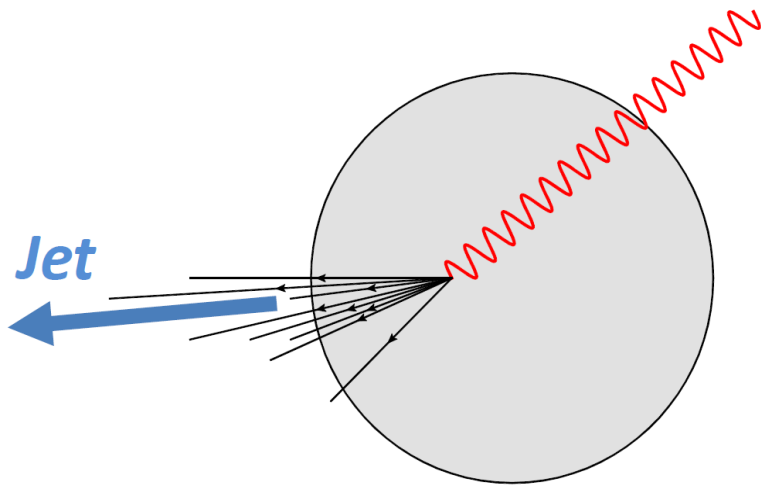
$$v_2^{jet} = \langle \cos(2[\phi^{jet} - \Psi_2]) \rangle$$

$$v_2^{jet} = \frac{\langle v_2^{soft} \cos(2[\phi^{jet} - \Psi_2]) \rangle}{\sqrt{\langle (v_2^{soft})^2 \rangle}}$$



# Asymmetry distribution of gamma-jet in heavy-ion collisions

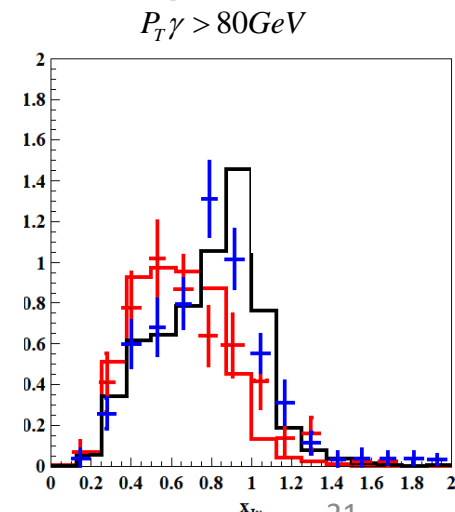
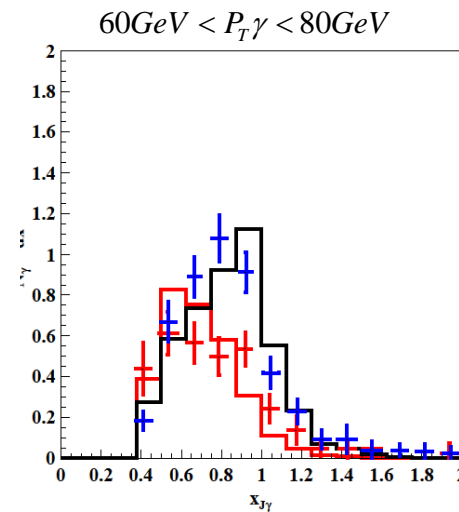
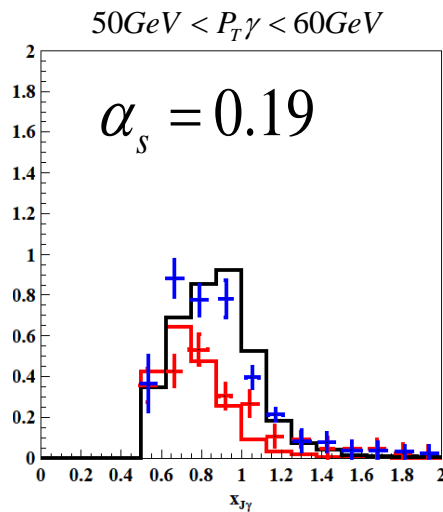
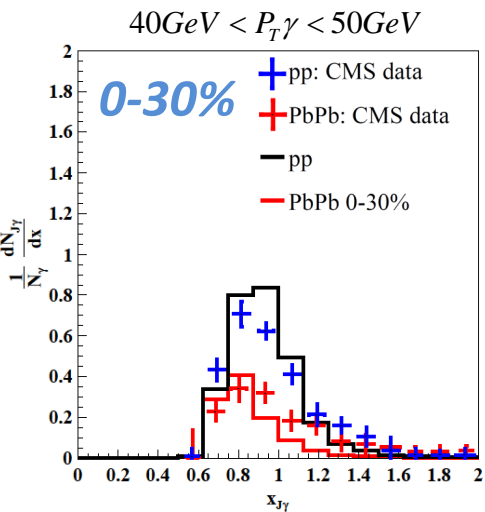
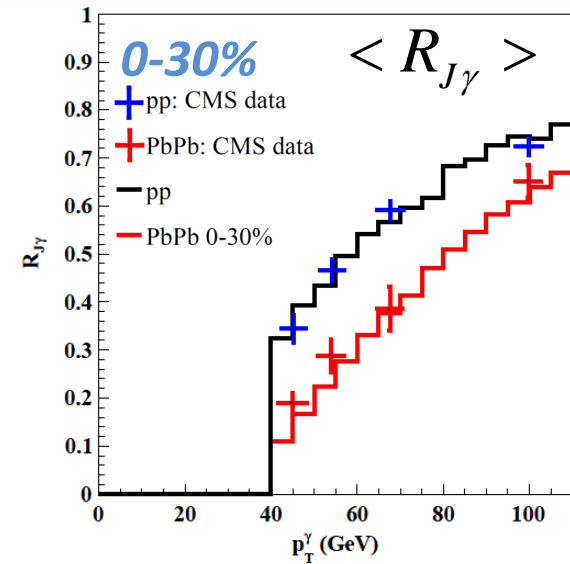
- fix the parameter  $\alpha_s$  via the comparison with the  $\gamma$ -jet asymmetry



$$|\eta_\gamma| < 1.44$$

$$P_{Tjet} > 30 GeV$$

$$|\eta_{jet}| < 1.6$$



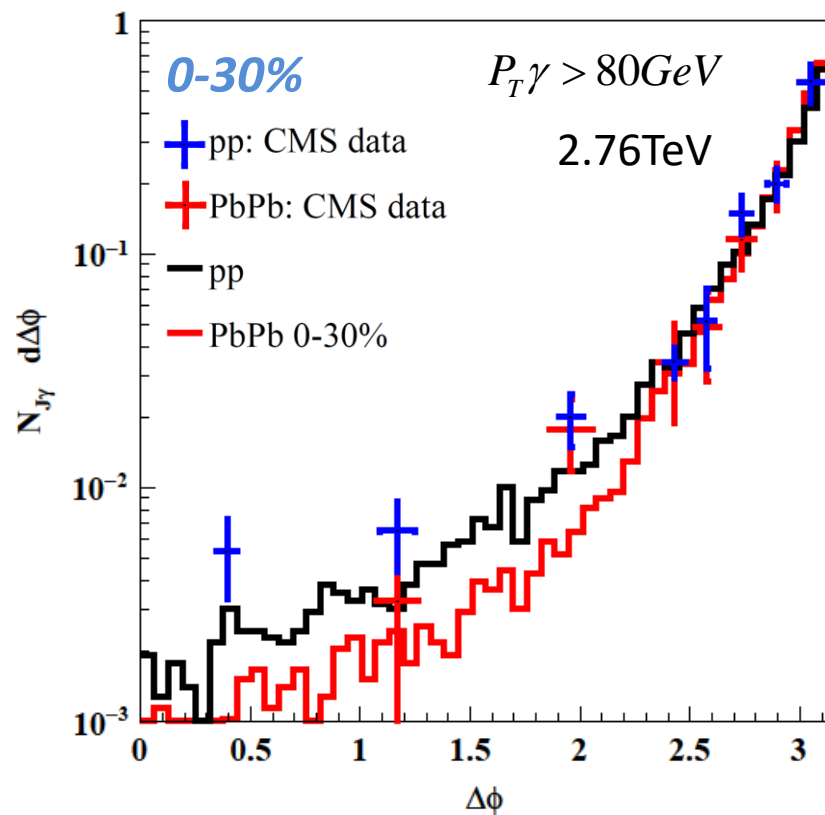
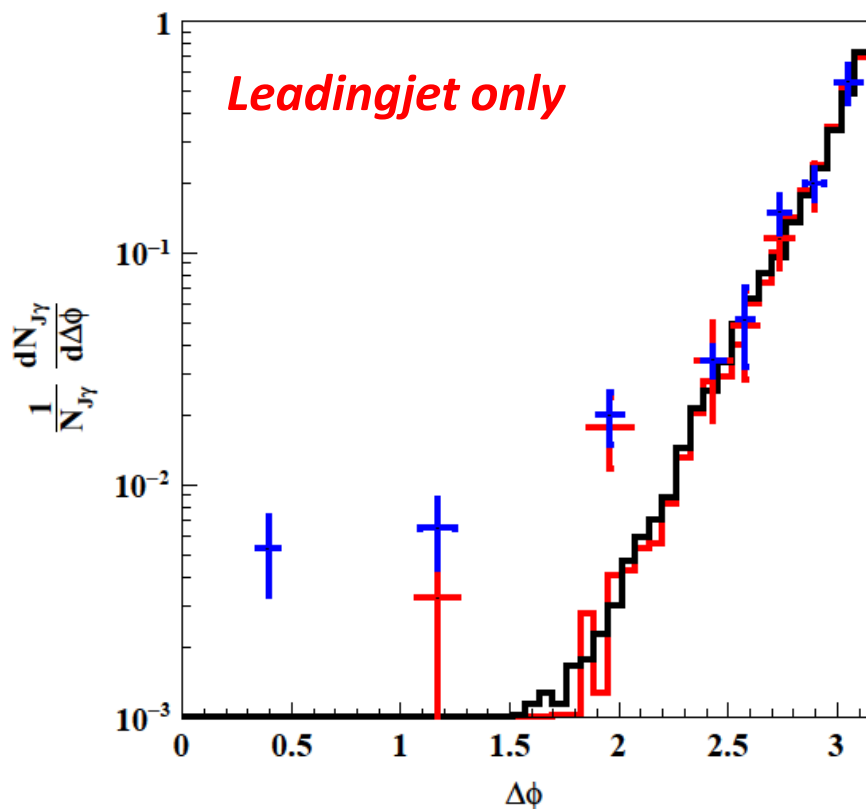
# Azimuthal distribution of gamma-jet in heavy-ion collisions

- Dominance of the initial state radiation in angular correlation

L Chen, GY Qin, SY Wei, BW Xiao, HZ Zhang [arXiv:1607.01932](#)

A. H. Mueller, B Wu, BW Xiao, F Yuan [arXiv:1604.04250](#)

- Multiple jets in gamma-jet events





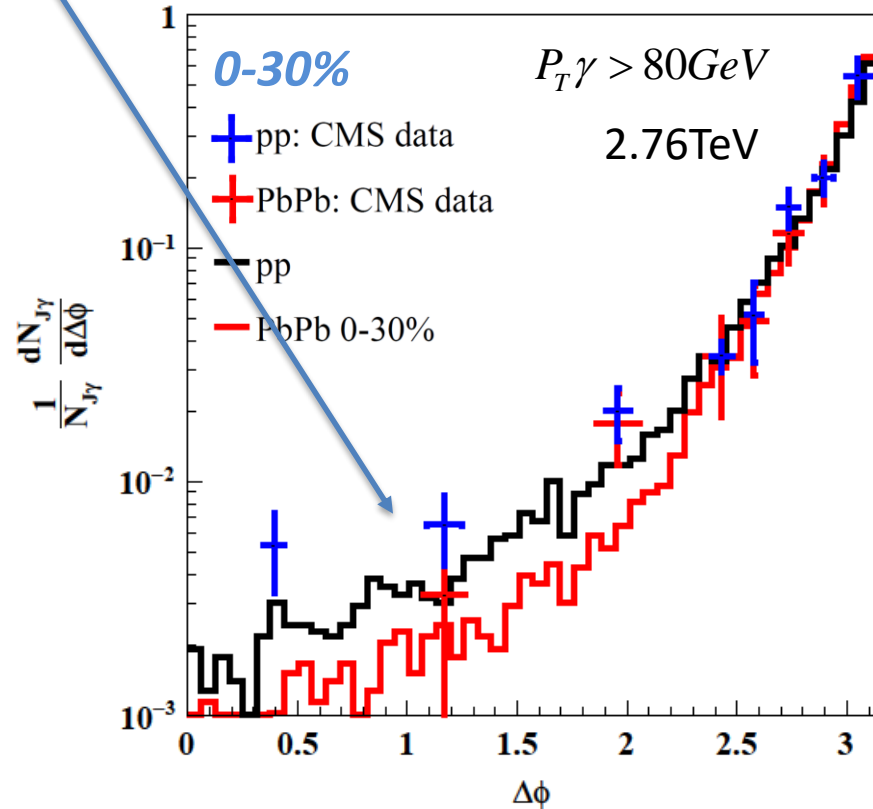
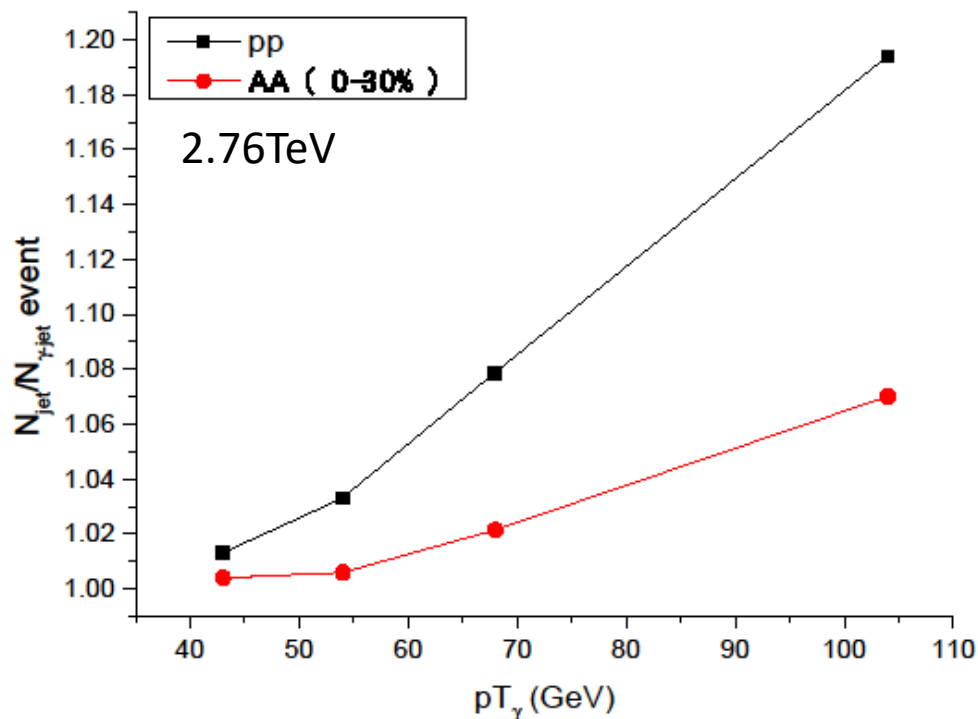
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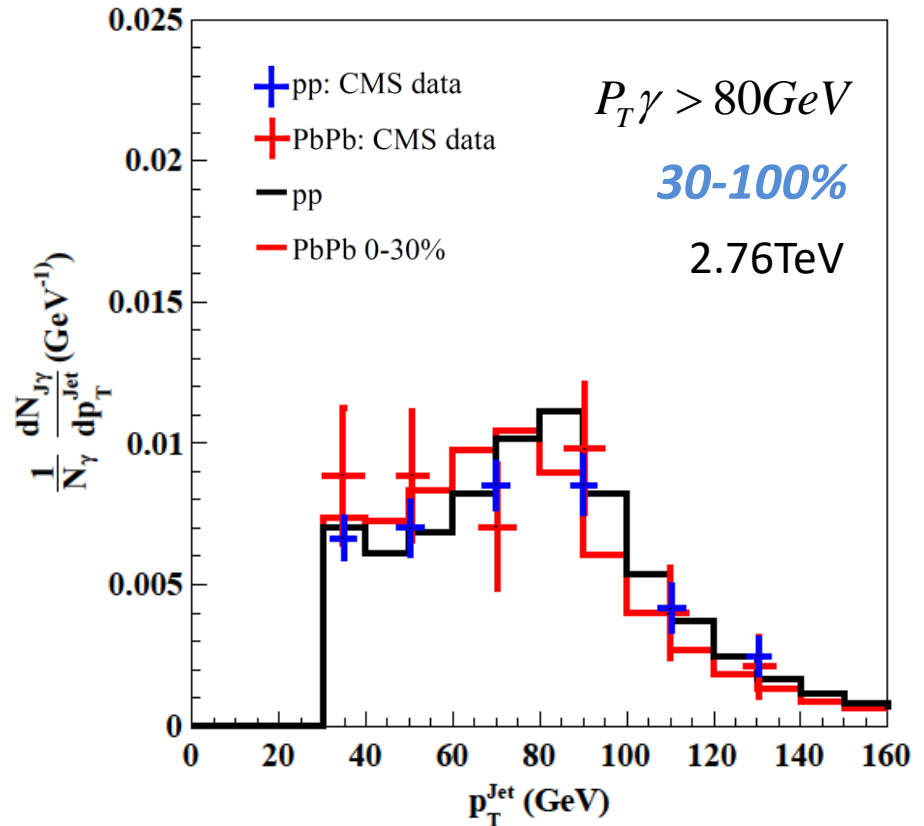
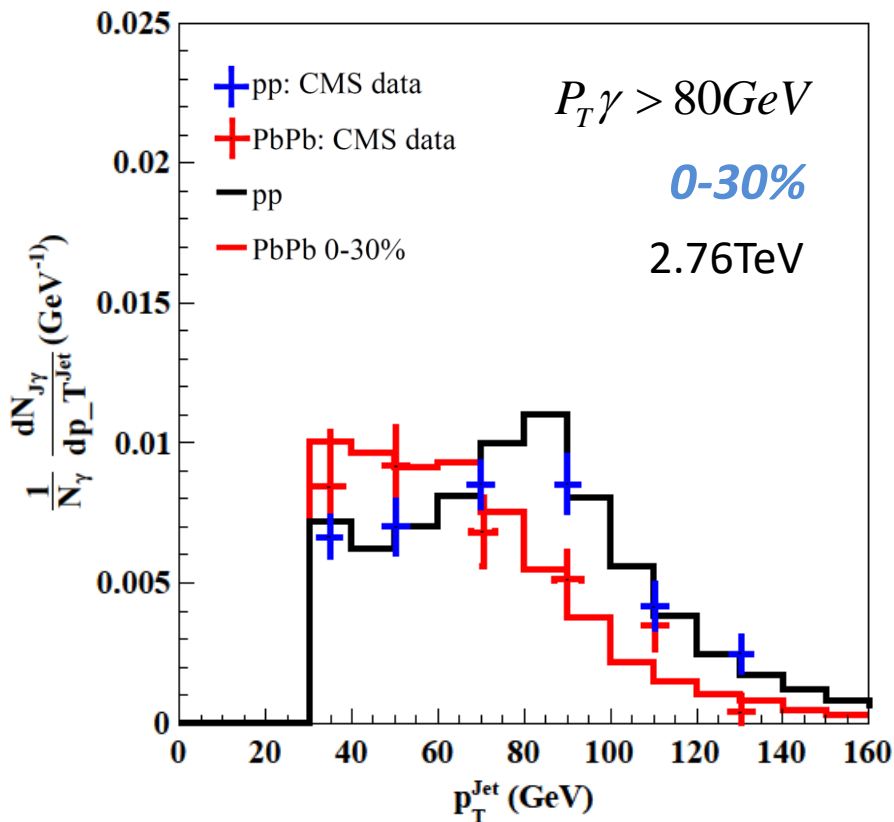
A. H. Mueller, B Wu, BW Xiao, F Yuan [arXiv:1604.04250](#)

- Multiple jets in gamma-jets events



# $p_T$ distribution of gamma-jet in heavy-ion collisions

- Shift of the peak of the  $p_T$  distribution
- Path length dependence of the energy loss

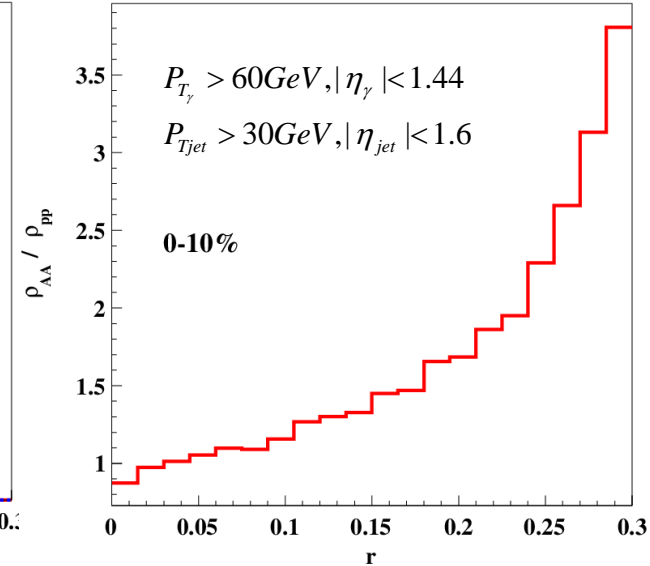
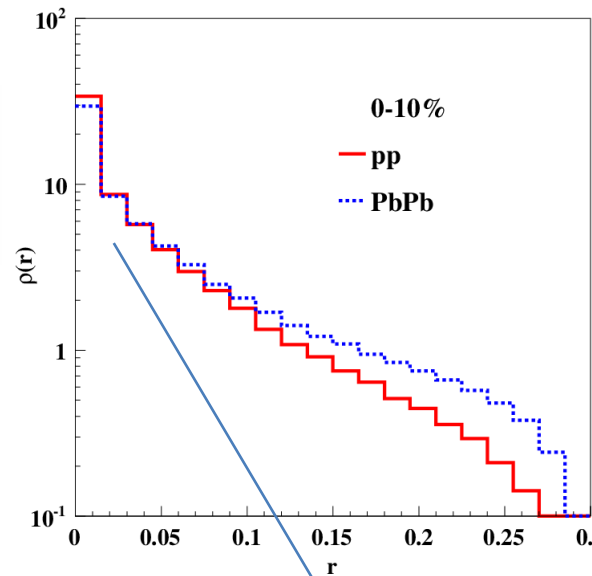
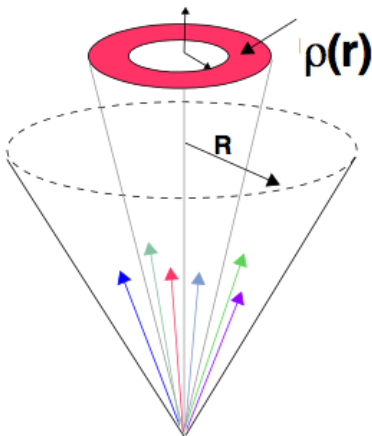


# Modification of gamma-jet structure

Jet shape

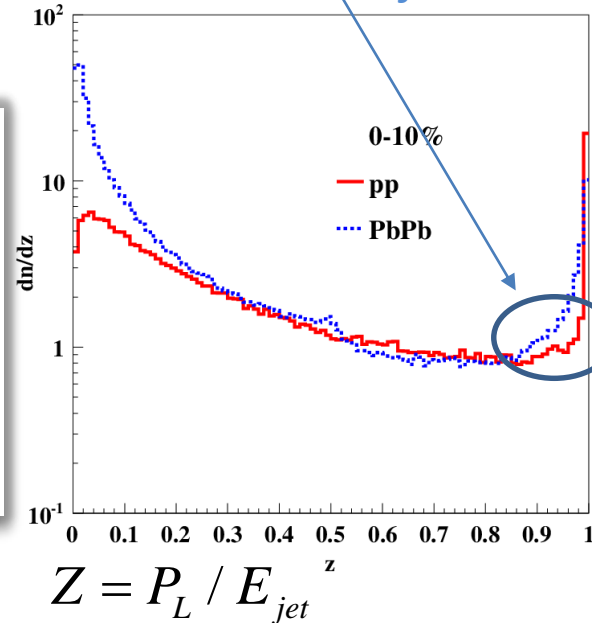
$$\rho(r) = \frac{1}{\Delta r} \frac{1}{N_{jet}} \sum_{jets} \frac{p_t(r - \frac{\Delta r}{2}, r + \frac{\Delta r}{2})}{p_t(0, R)}$$

P. Kurt

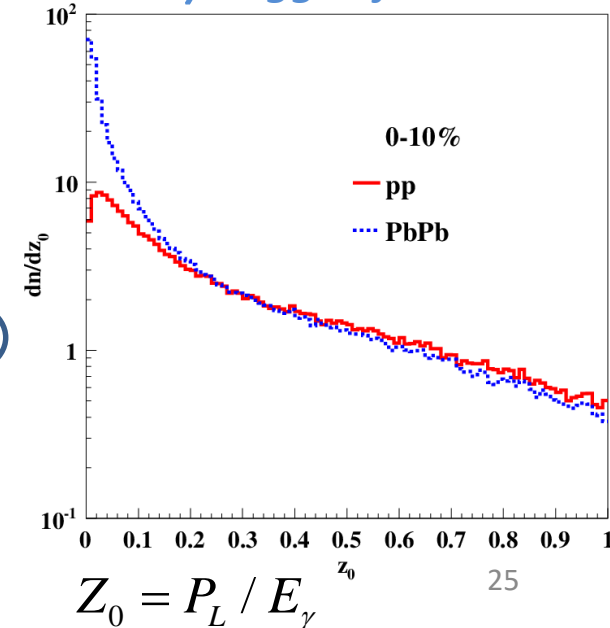


- The large energy fraction of leading particles in a reconstructed jet.
- $\gamma$ -tagged jet FF, a better probe for the  $\gamma$ -jet study.

Reconstructed jet FF



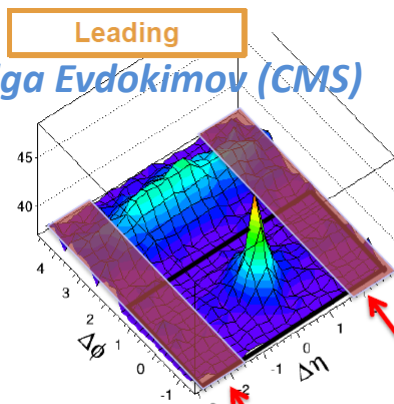
$\gamma$ -tagged jet FF



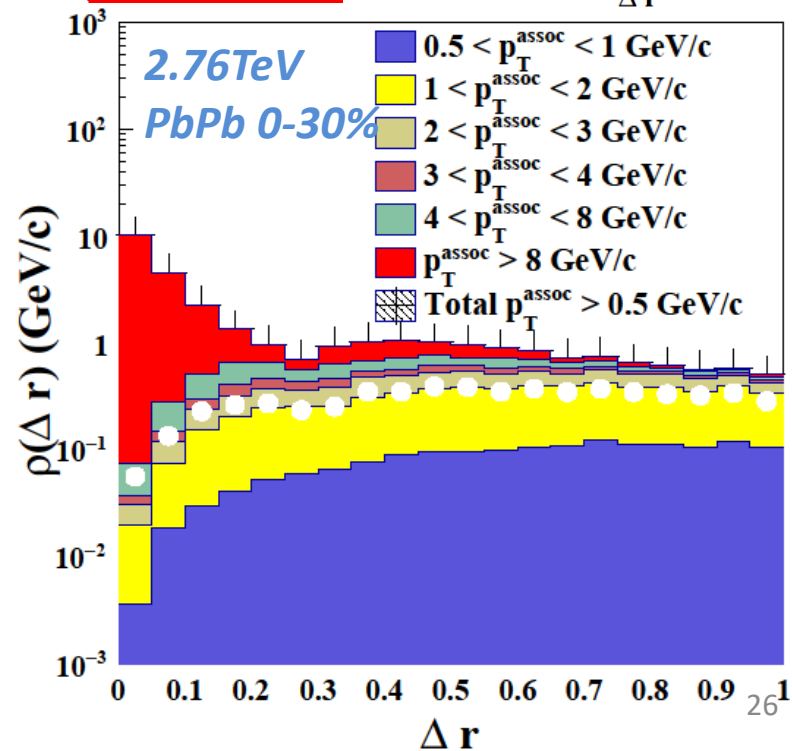
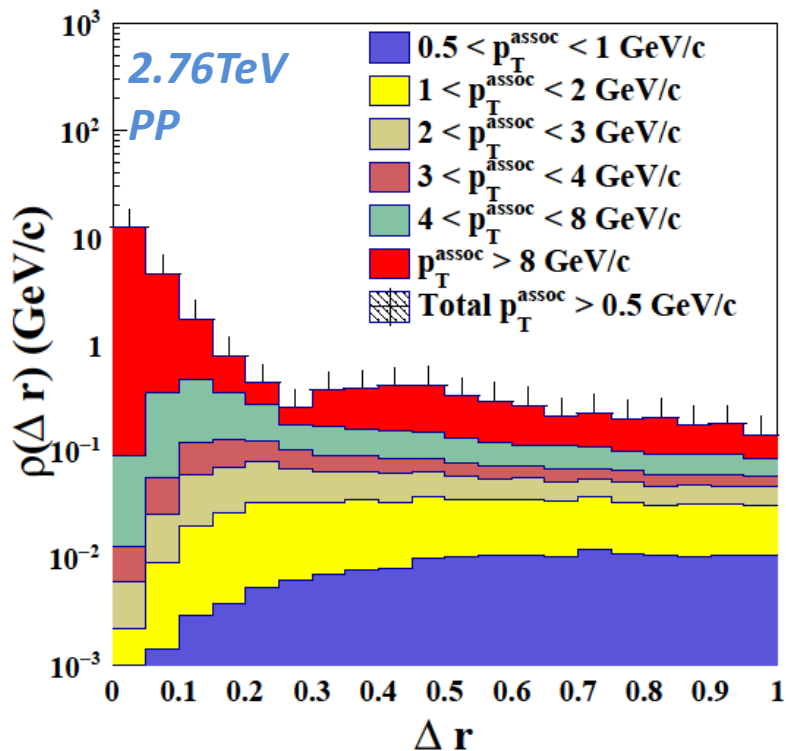
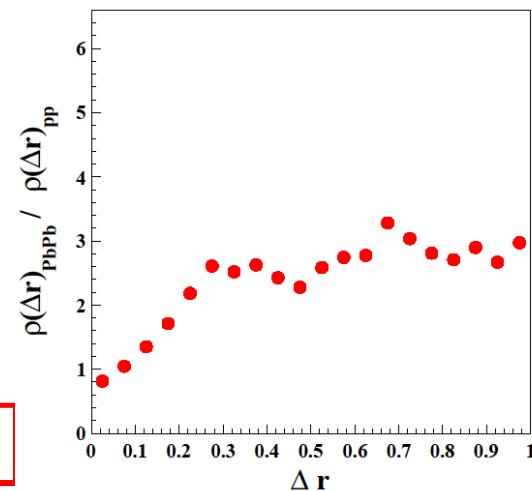
# Jet shape of gamma-jets in heavy-ion collisions

- Energy lost by the hard parton is transport out of the jet cone by the soft parton.

Leading  
Olga Evdokimov (CMS)



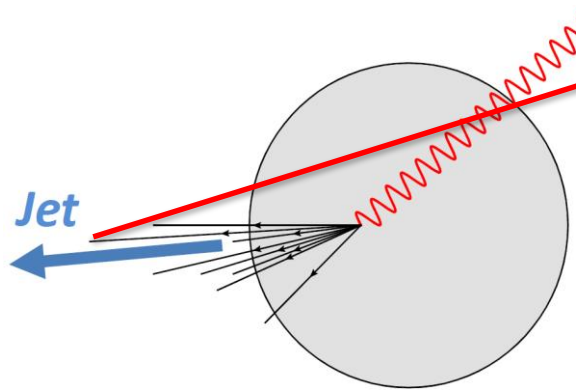
“Sideband” region  
 $1.5 < |\Delta\eta| < 2.5$



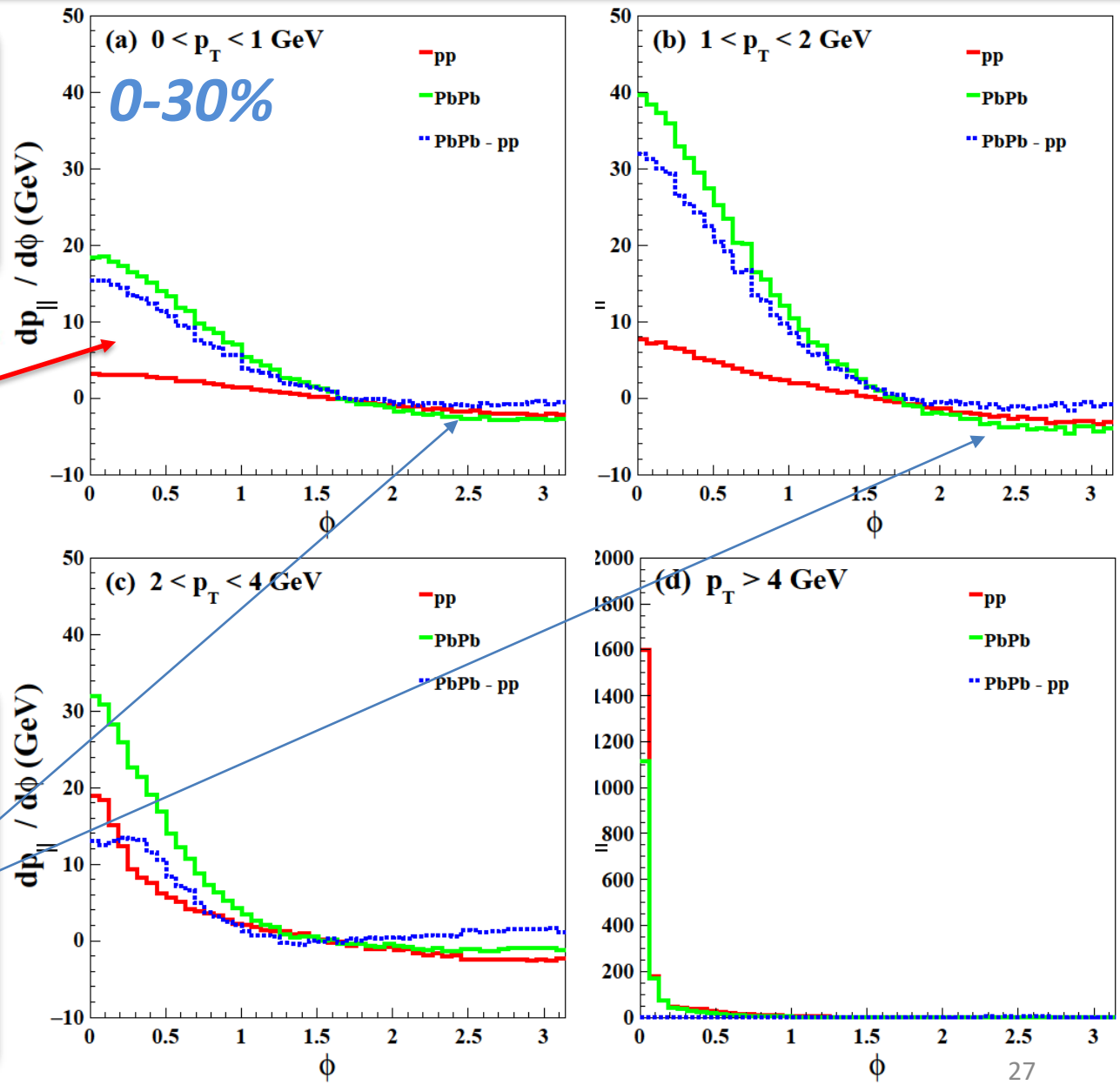
# Energy flow in gamma-jets events

$$P_{\parallel} = \sum_i P_{i(parton)} * \cos \theta_{i(parton-leadingjet)}$$

$$\phi = | \phi_{parton} - \phi_{leadingjet} |$$

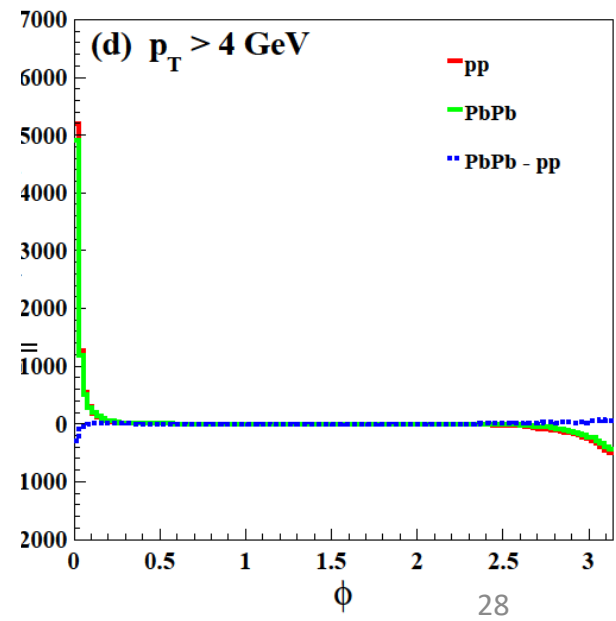
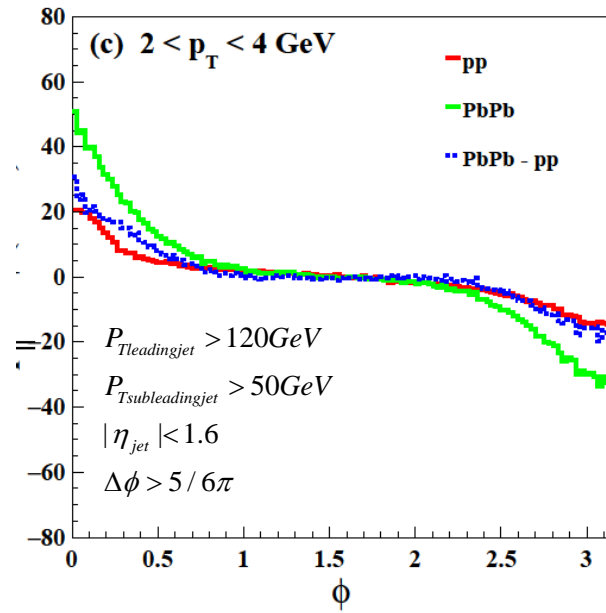
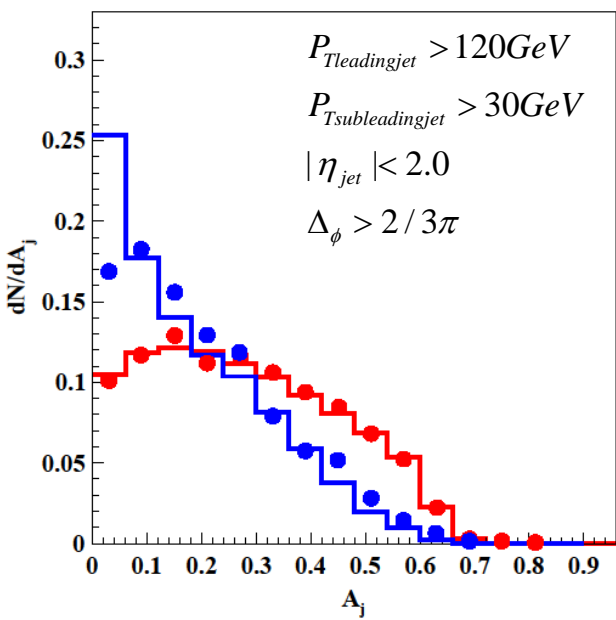
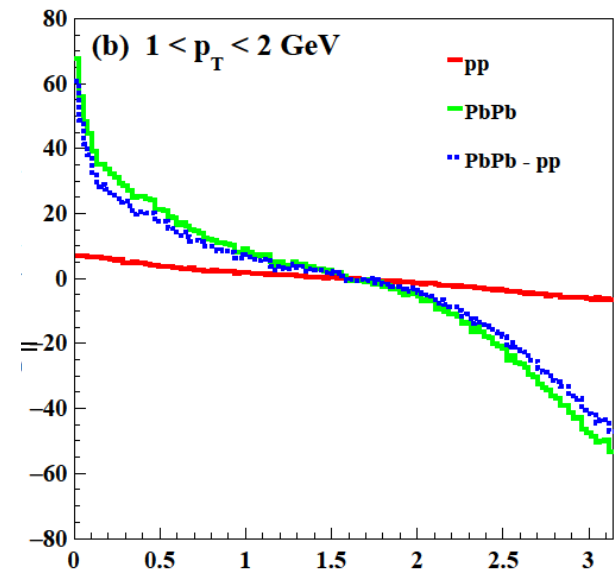
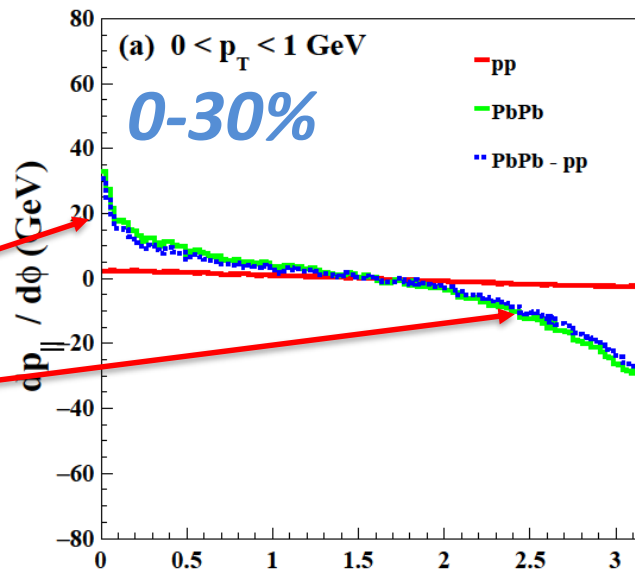
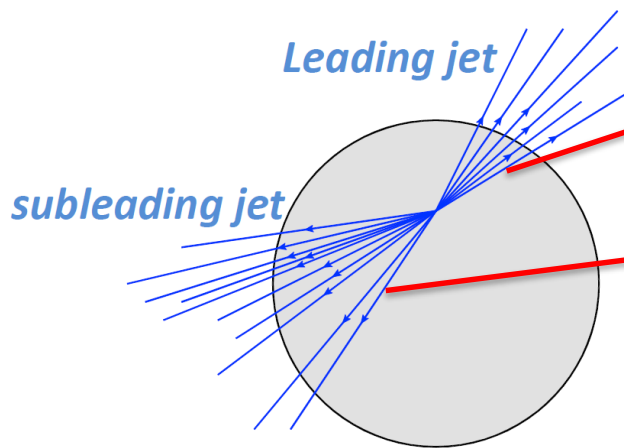


- Suppression of the hard parton, enhancement of the soft parton.
- Energy flow to the opposite direction of the jet



# Energy flow in dijet events

preliminary



# Jet shape of leading jet in heavy-ion collisions

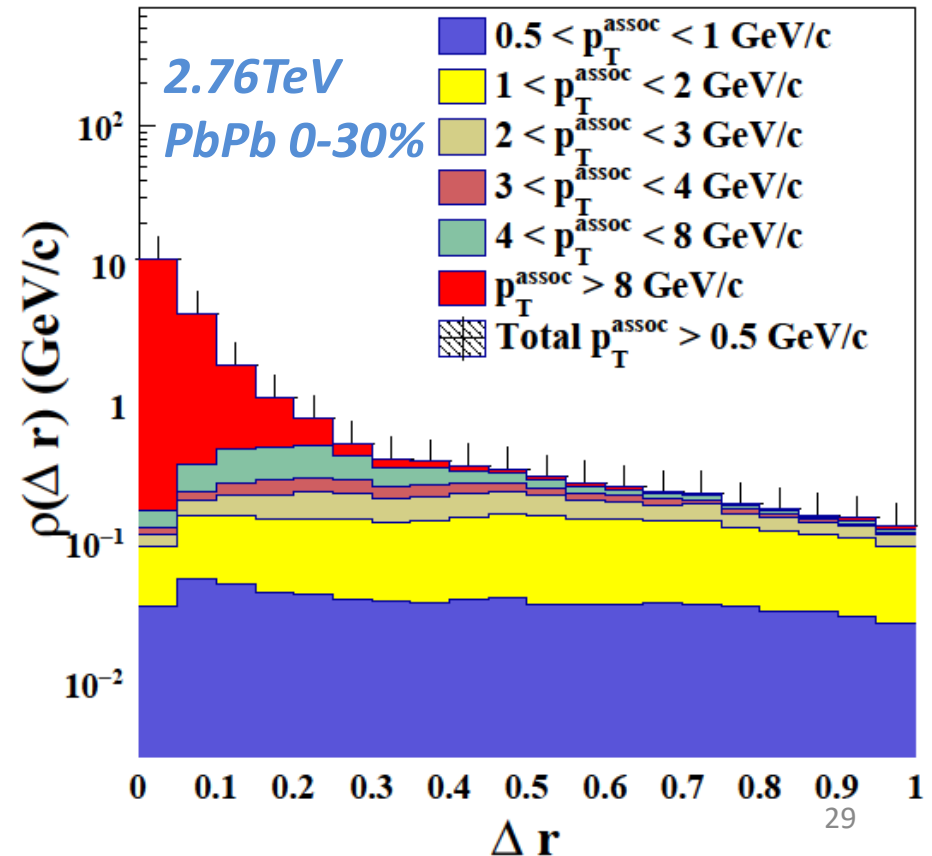
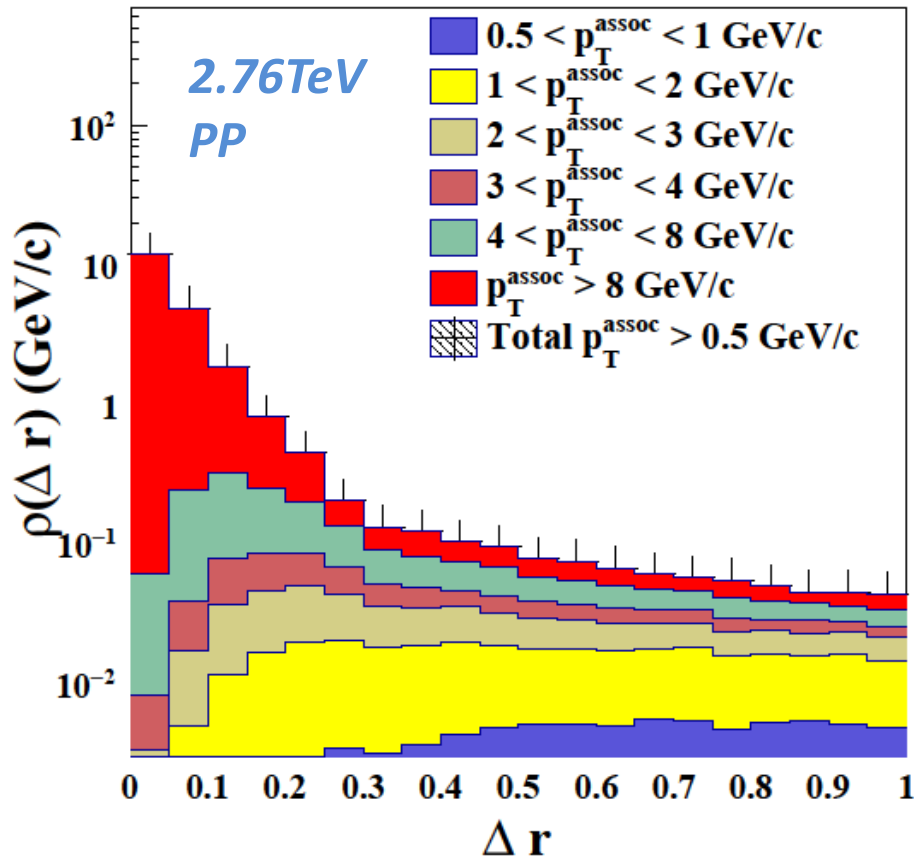
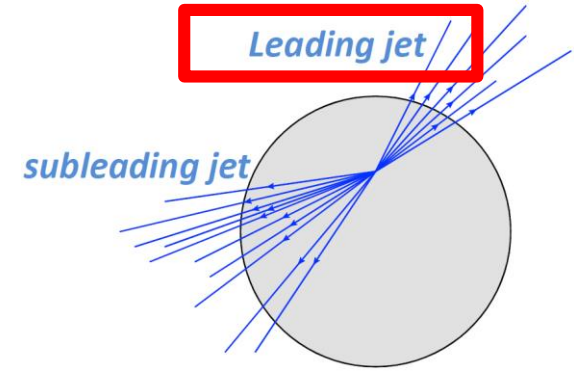
preliminary

$$P_{T\text{leadingjet}} > 120\text{GeV}$$

$$P_{T\text{subleadingjet}} > 50\text{GeV}$$

$$|\eta_{\text{jet}}| < 1.6$$

$$\Delta_\phi > 5/6\pi$$





# Jet shape of leading jet in heavy-ion collisions

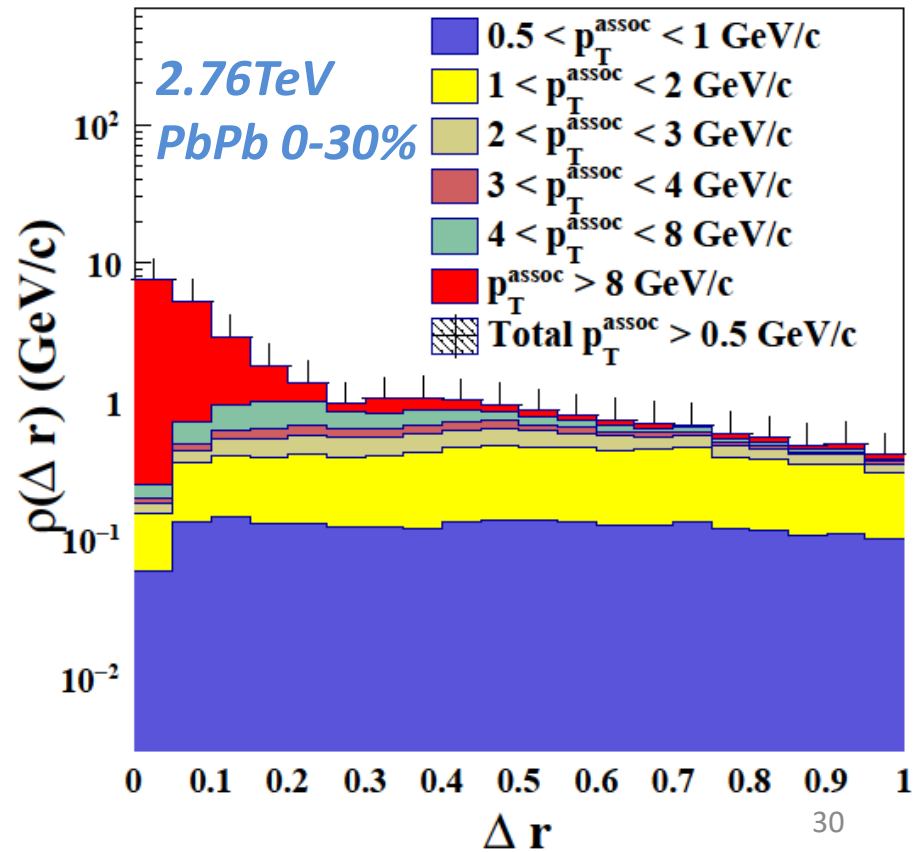
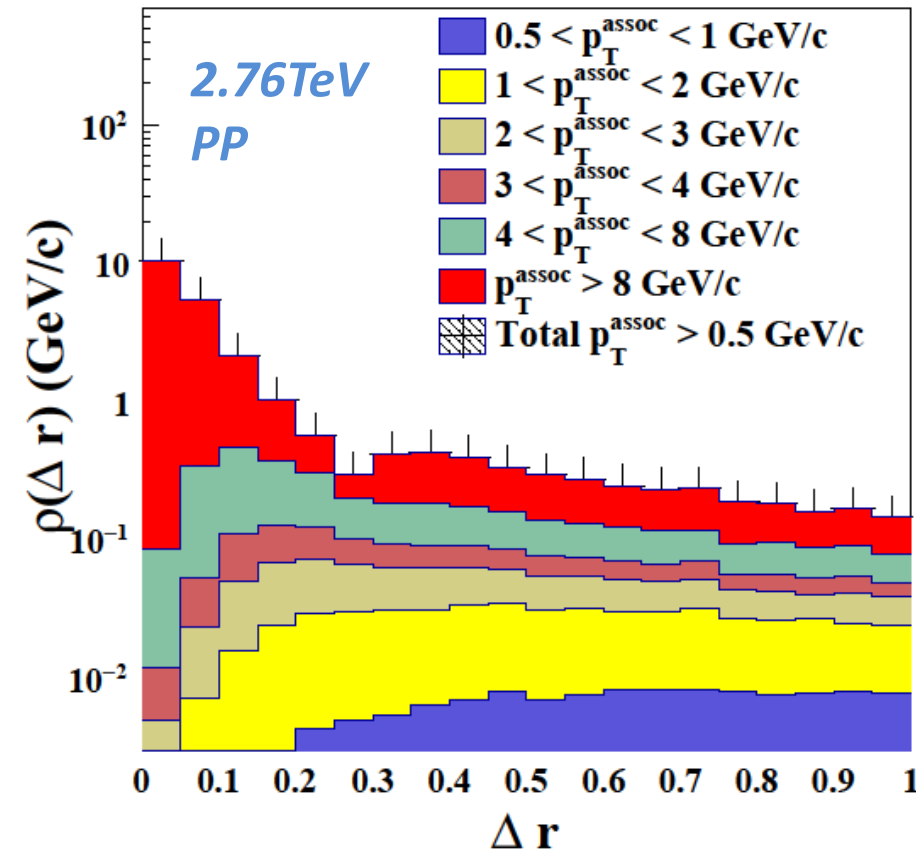
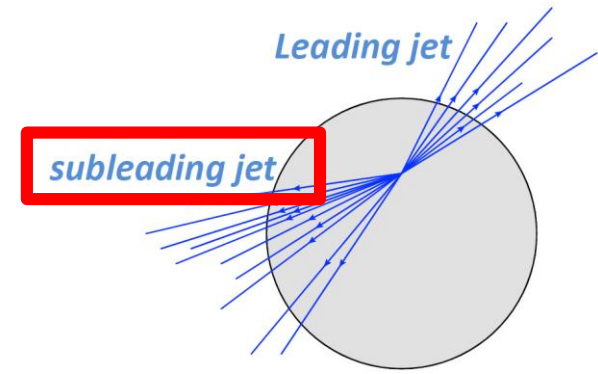
preliminary

$$P_{T\text{leadingjet}} > 120\text{GeV}$$

$$P_{T\text{subleadingjet}} > 50\text{GeV}$$

$$|\eta_{\text{jet}}| < 1.6$$

$$\Delta_\phi > 5/6\pi$$



# $p_T$ imbalance of dijet in heavy-ion collisions

$A_j$  inclusive

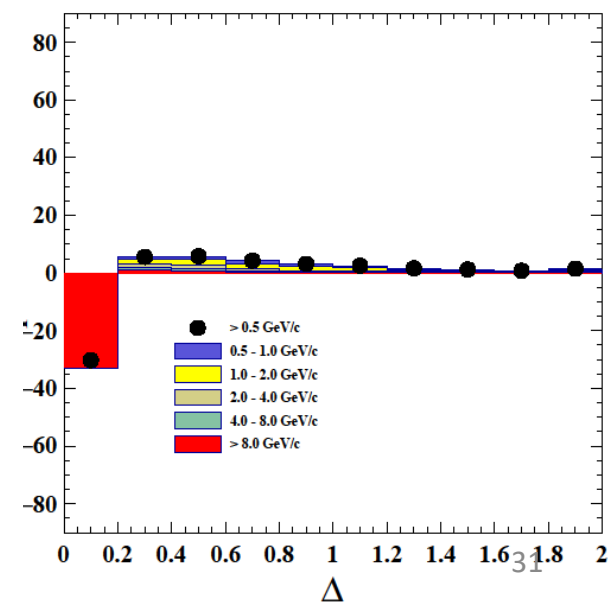
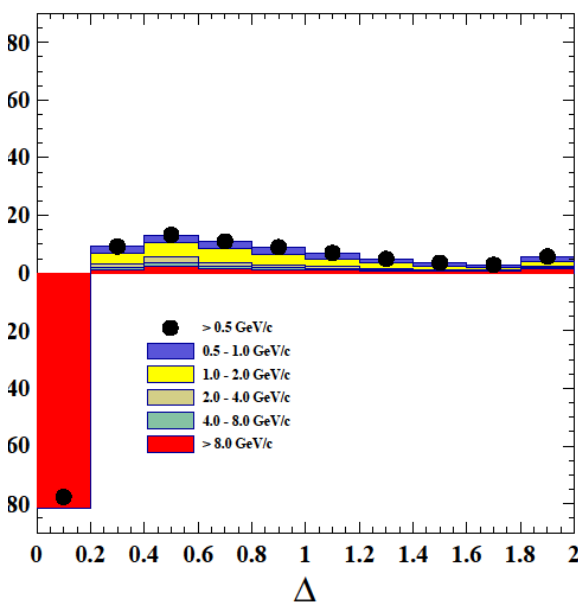
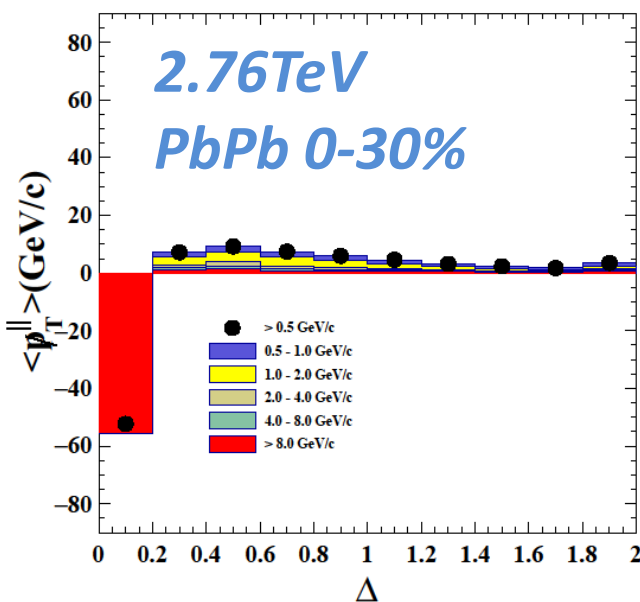
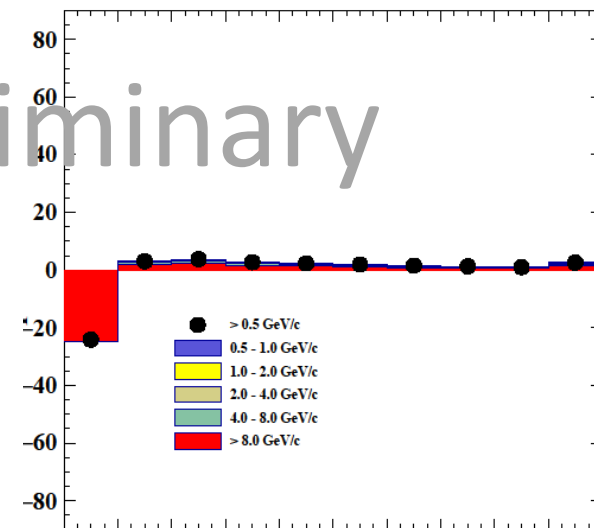
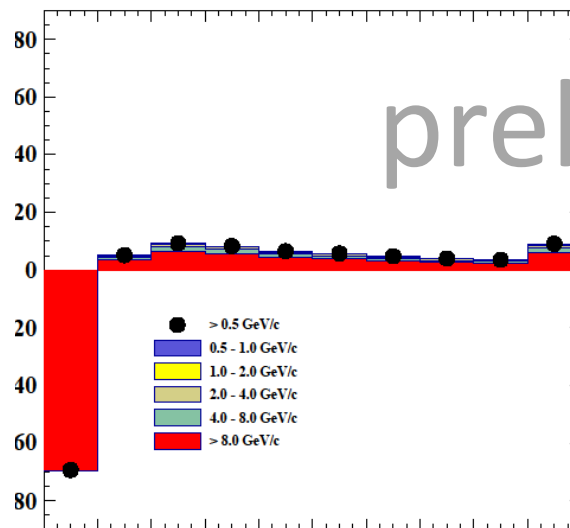
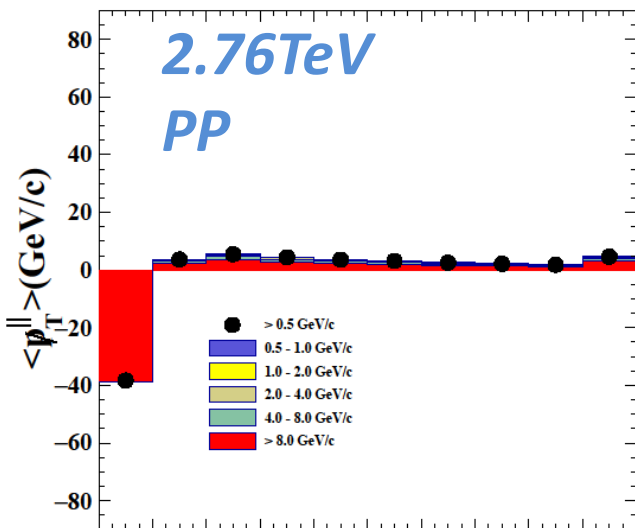
$A_j > 0.22$

$A_j < 0.22$

2.76TeV

PP

preliminary



# Summary

- We present a computation of jets modification in QGP within the Linear Boltzmann Transport model in which both the elastic and inelastic processes are included.

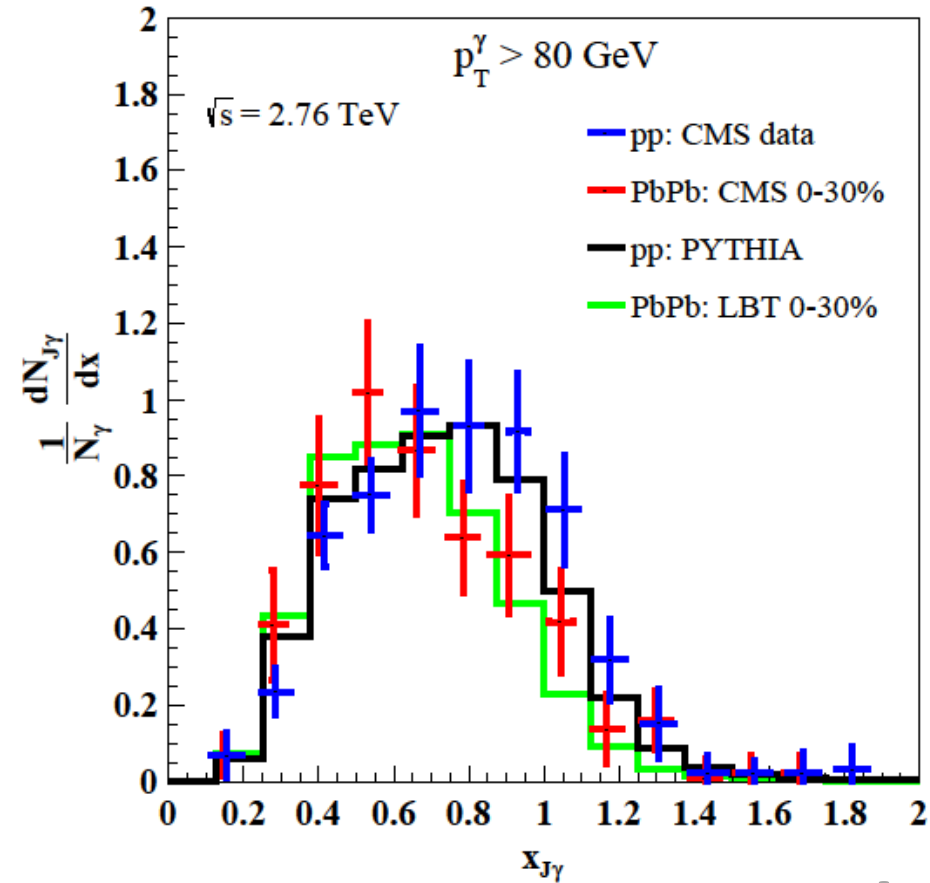
# Outlook

- *Hadron jet and Heavy quark jet*  
(with the *recombination model* developed by Texas A&M group)

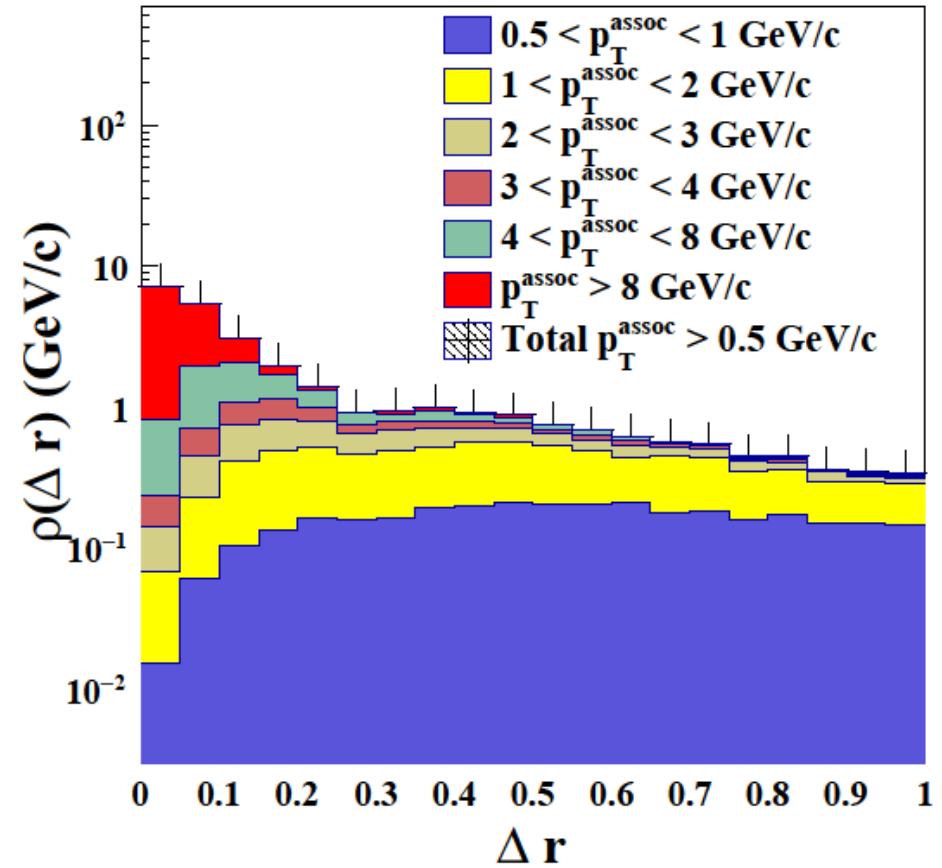
Rainer's talk

# Jet reconstruction with recombination model

## Gamma-jet asymmetry



## Jet shape

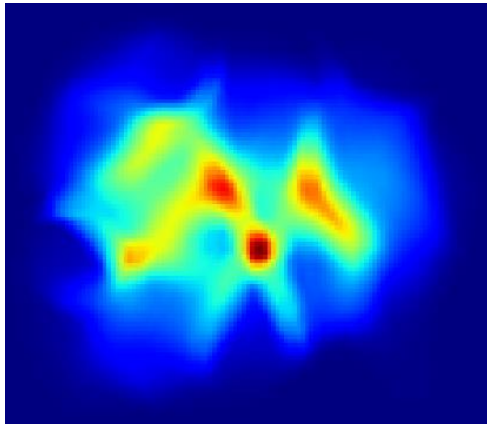


preliminary

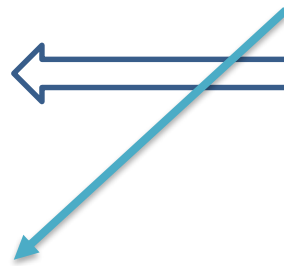
# Beyond LBT model (modified medium background)

- Linear approximation : jet induced medium excitation  $\delta f \ll f$ .
- Jet-Medium interaction : Where is the modification of the thermal background ?

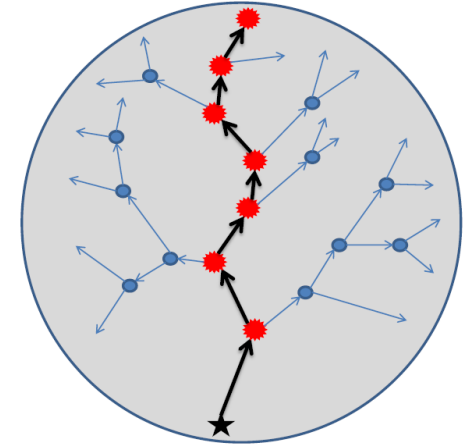
Modified medium background



$\epsilon T u$



JET

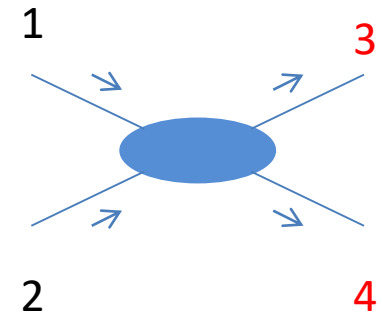
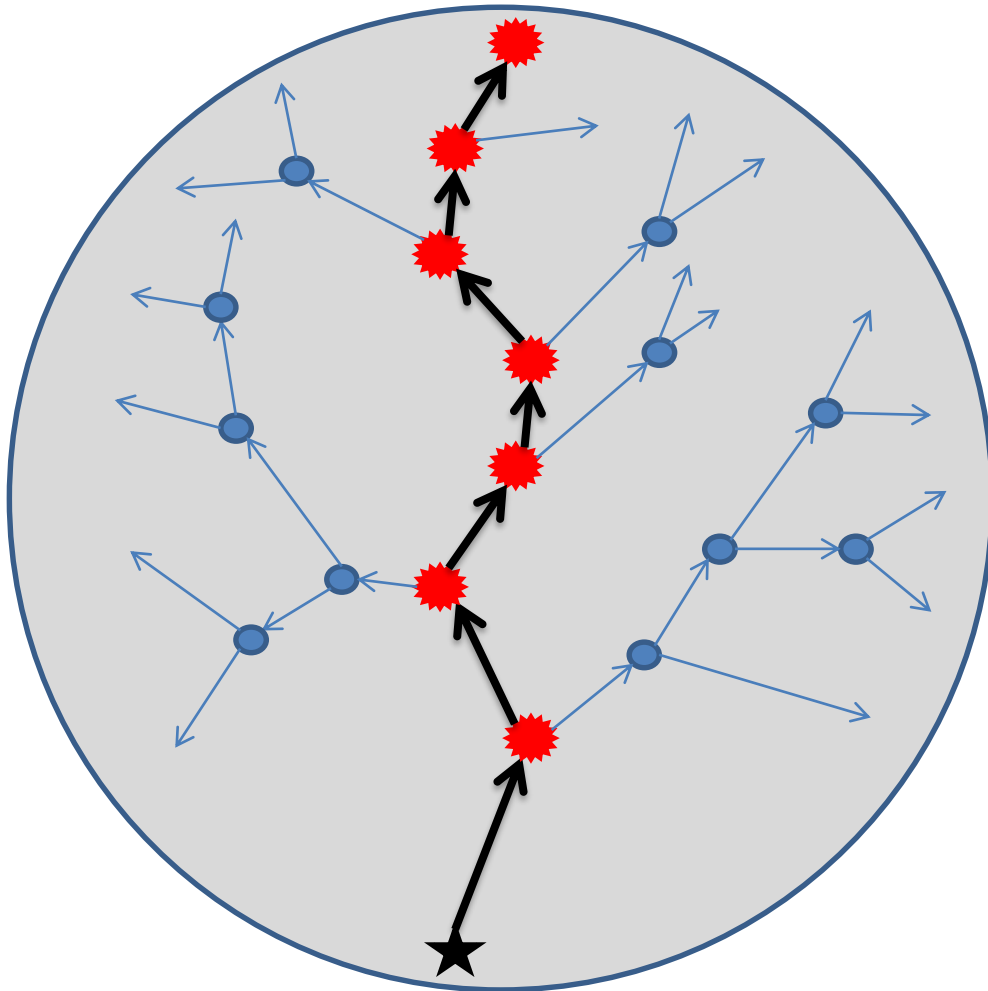




Energy and momentum deposited from the jets as source terms into hydro

CoLBT-Hydro model  
(A coupled LBT Hydro (3+1D) Model)

*Thanks*

## Positive particles : Medium Excitation



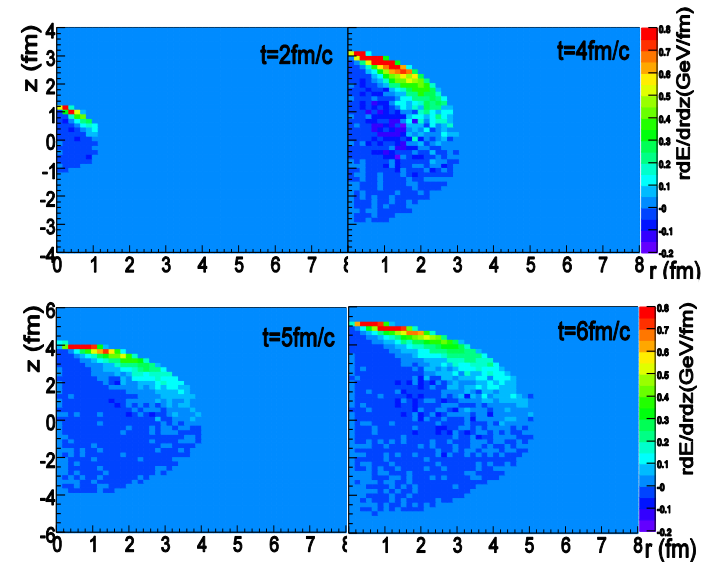
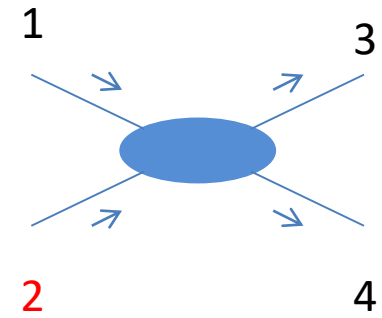
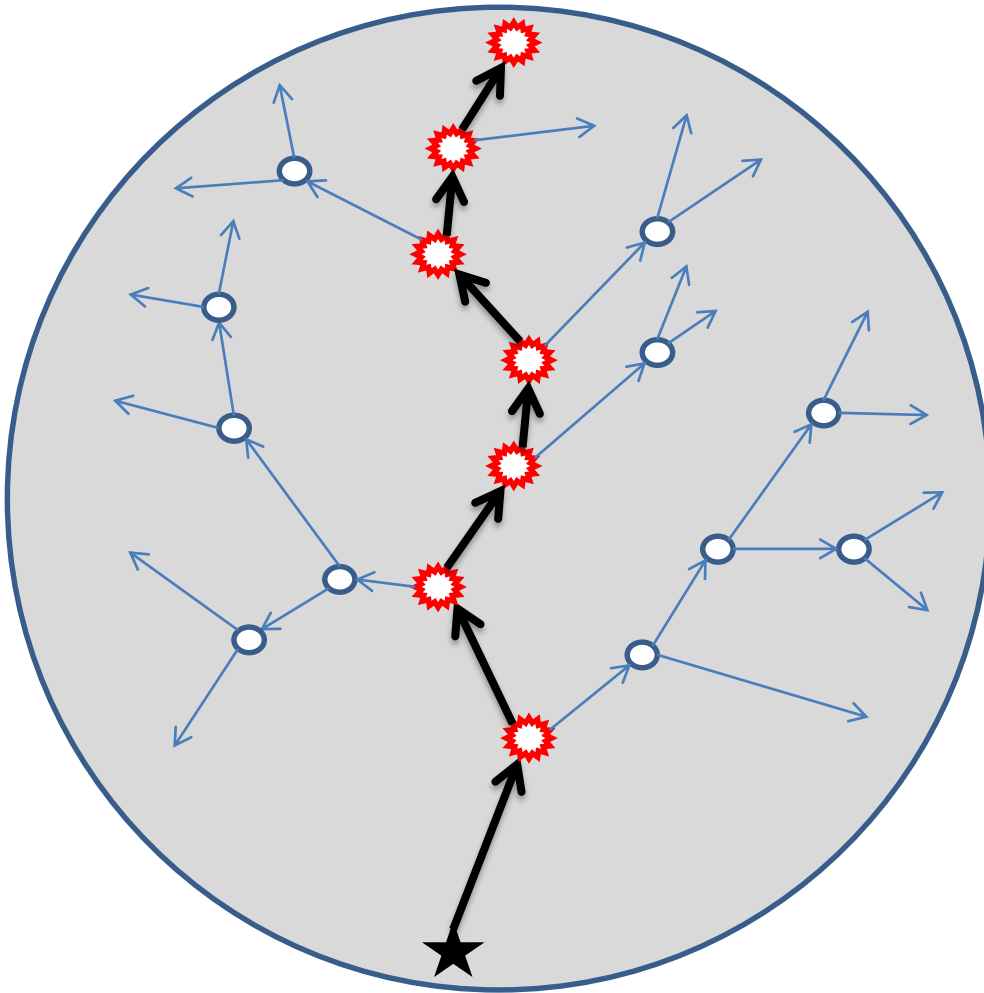
-  Leading parton-----thermal parton scattering
-  recoiled parton-----thermal parton scattering

*Linearized Boltzmann jet transport*  
neglect scatterings between recoiled medium partons.

It's a good approximation when the jet induced medium excitation  $\delta f \ll f$ .

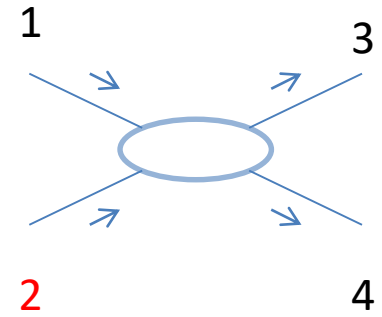
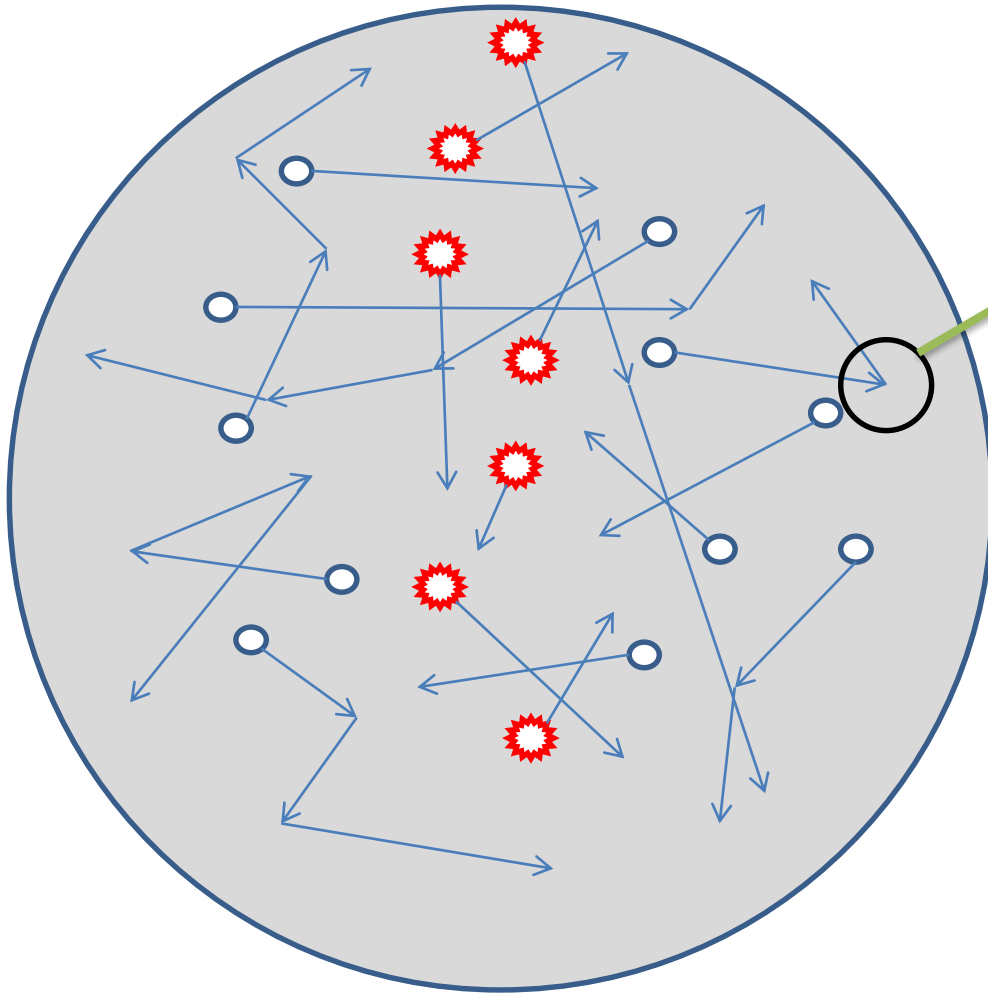


## Negative particles : the particle hole



One has to subtract the 4-momentum of negative particle when combine it to jet

# Negative particles : how do we deal with them?



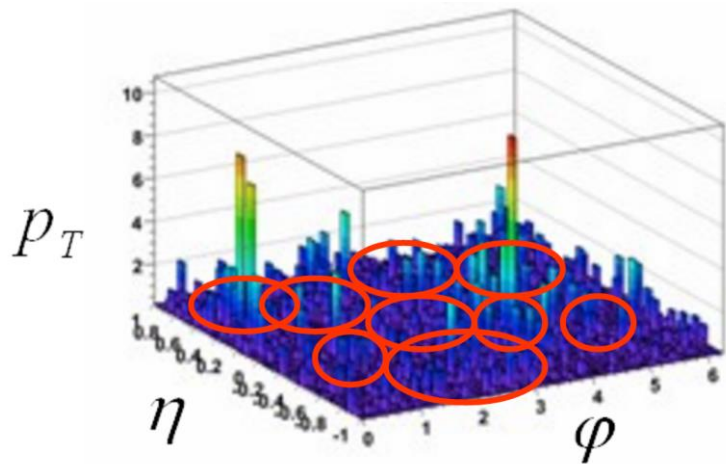
thermal parton-----thermal parton  
scattering

the negative particle is also traveling in the medium

One has to subtract the 4-momentum of negative particle when combine it to jet

# Underlying Event Subtraction (UES)

UE: collisions of beam remnant, fluctuation of the background, non-perturbative effects. Subtraction is needed to exclude the soft particles.



Seed jet:  $E_T > 3 \text{ GeV}$  for at least one parton, and

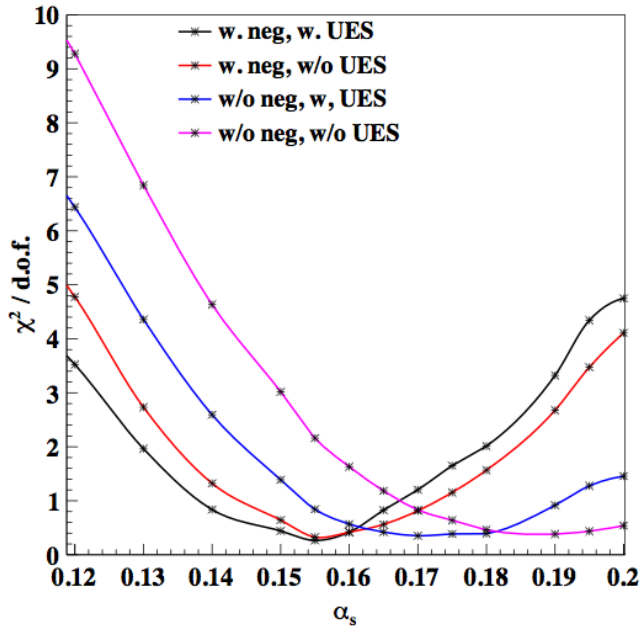
$$E_T^{max} / E_T^{ave} > 4$$

ATLAS Collaboration, Phys. Lett. B 719, 220 (2013).

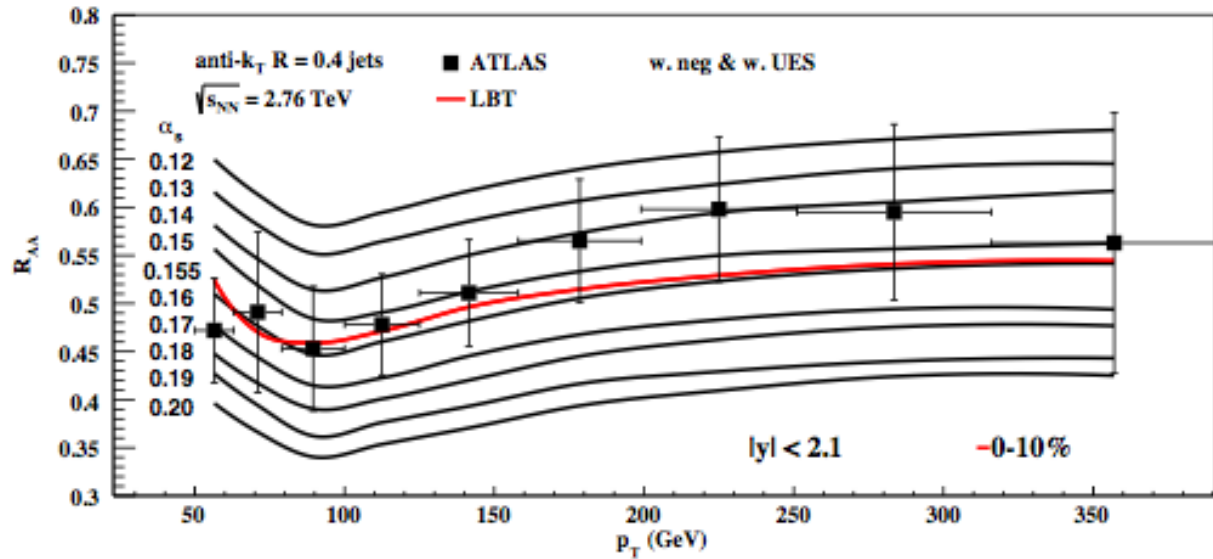
$$E_T^{UES} = E_T^{seedjet} - A^{seedjet} \rho (1 + 2v_2 \cos[2(\phi_{jet} - \Psi_2)])$$

We only subtract the energy of seed jets,  
and count all the final jets!

# Nuclear modification factor



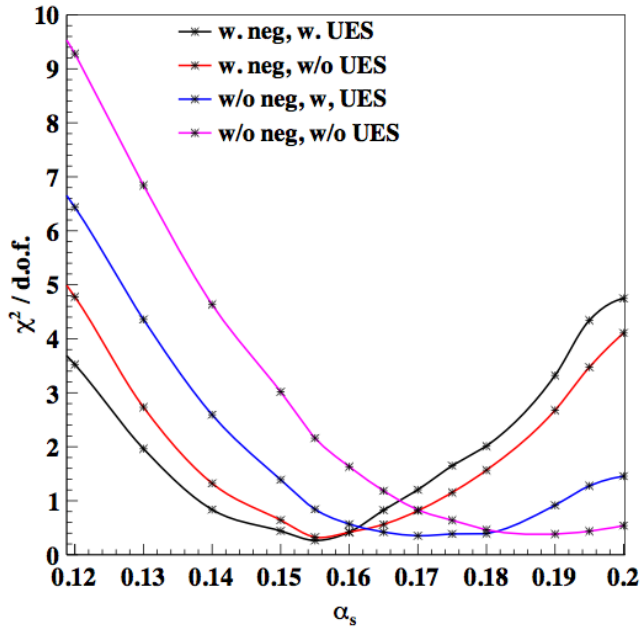
$$\chi^2 = \frac{(\text{Theo.} - \text{Exp.})^2}{(\delta \text{Exp.})^2}$$



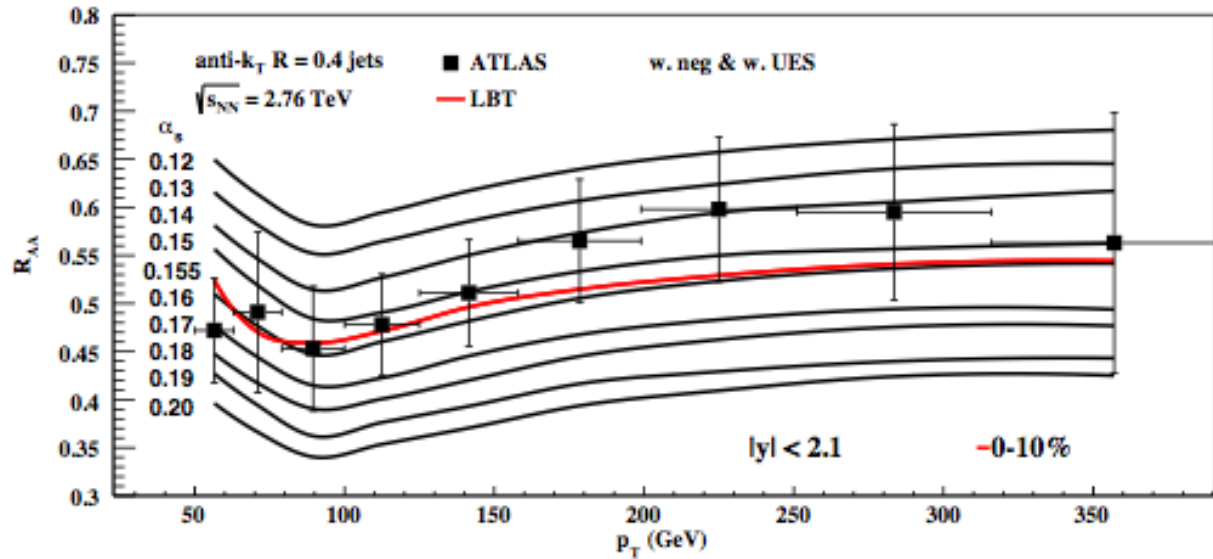
$$R_{AA} = \frac{\frac{1}{N_{evt}} \frac{d^2 N_{jet}^{AA}}{dp_T dy}}{\frac{1}{N_{evt}} \frac{d^2 N_{jet}^{pp}}{dp_T dy}}$$

We use the best  $\chi^2$  fit to extract the fixed value  $\alpha_s$   
in the LBT model

# Nuclear modification factor



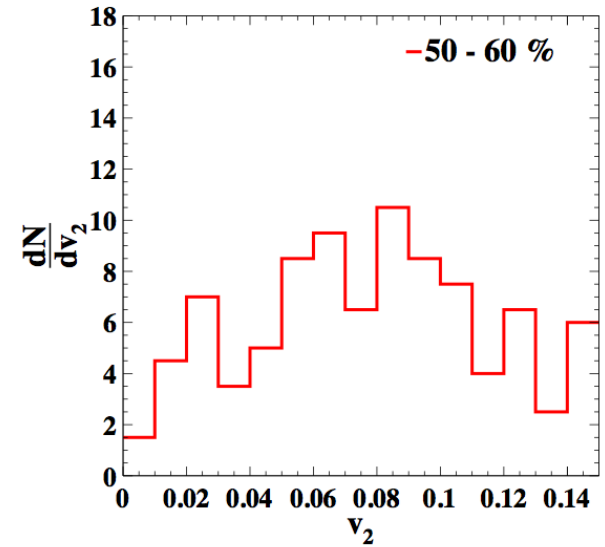
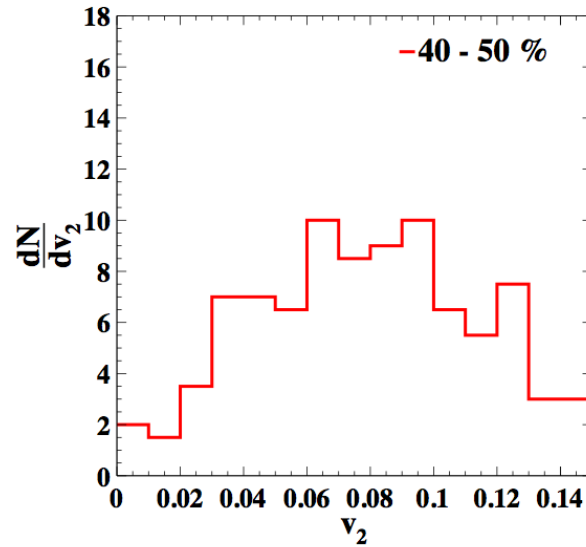
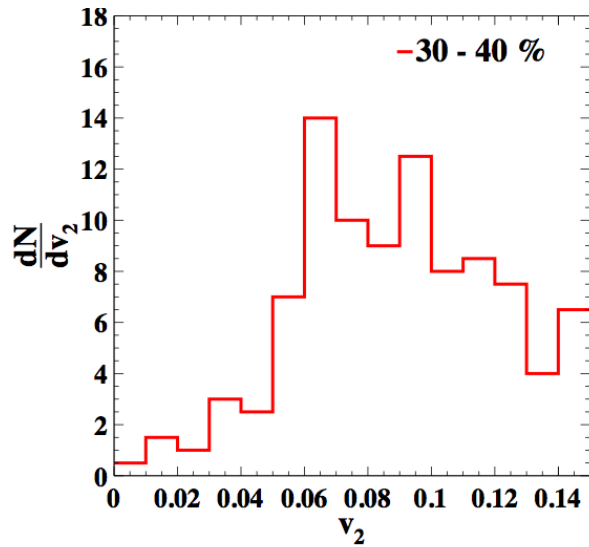
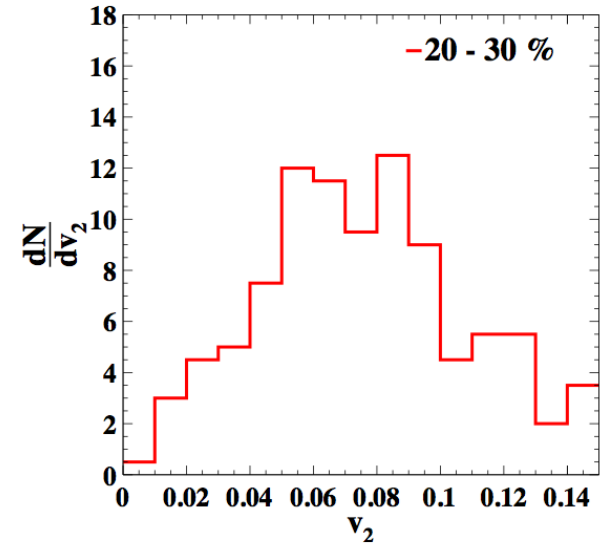
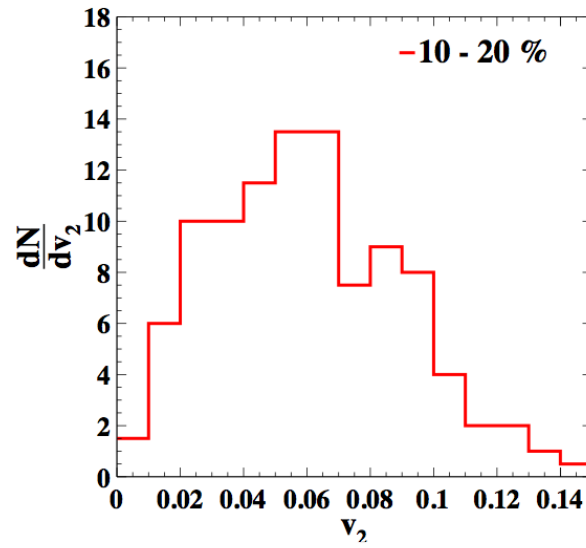
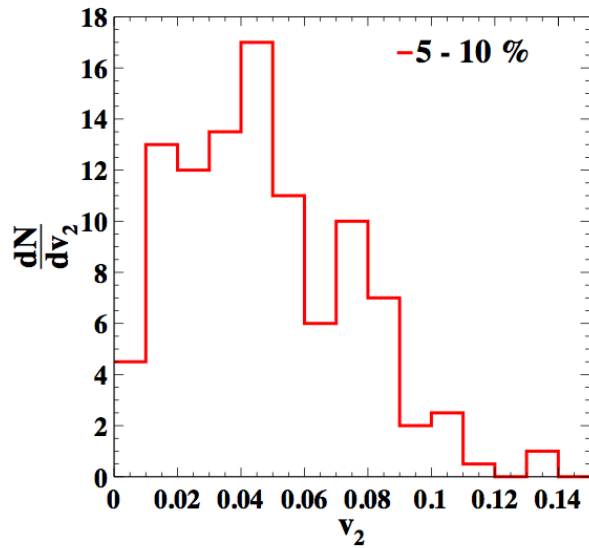
$$\chi^2 = \frac{(\text{Theo.} - \text{Exp.})^2}{(\delta \text{Exp.})^2}$$



$$R_{AA} = \frac{\sum_i w_i \frac{1}{N_{events}} \frac{dN_i^{jets}}{dp_T} |AA}{\sum_i w_i \frac{1}{N_{events}} \frac{dN_i^{jets}}{dp_T} |pp|}$$

We use the best  $\chi^2$  fit to extract the fixed value  $\alpha_s$  in the LBT model

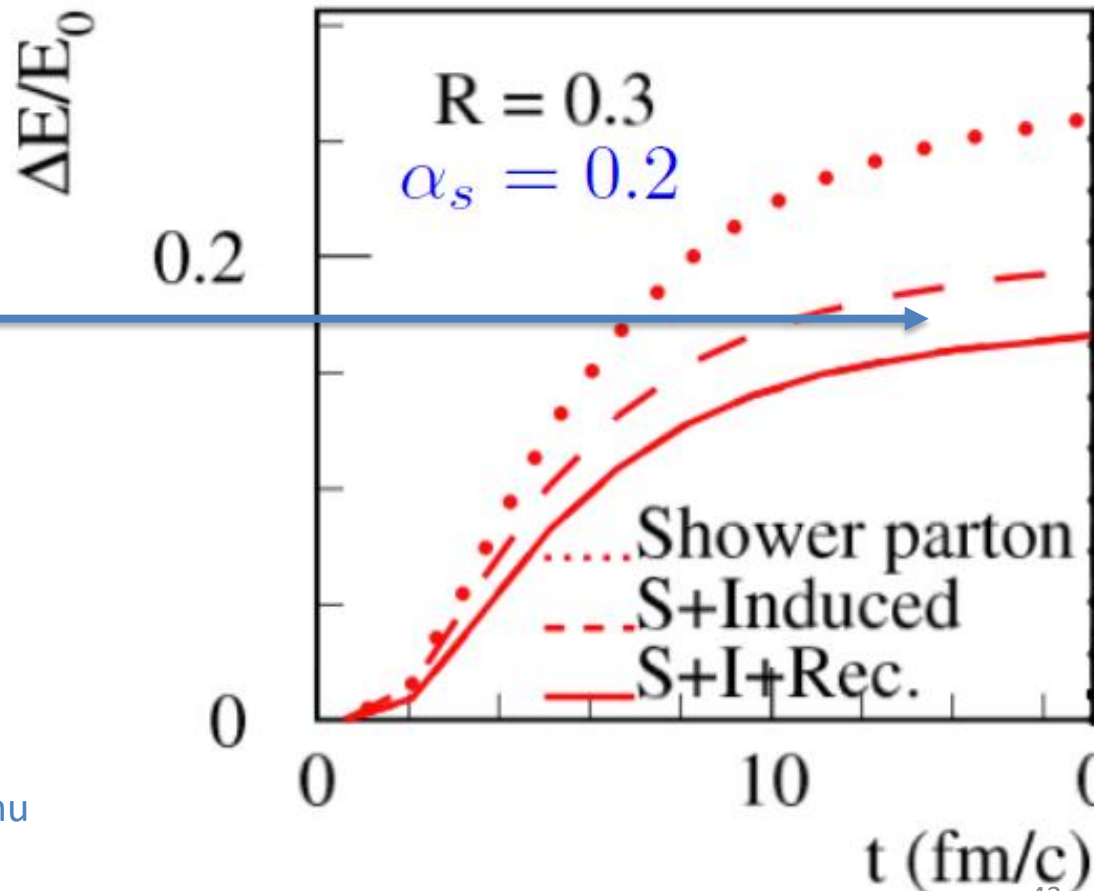
# $v_2$ of soft particles from hydro profiles



# Jets in a 3+1D hydro

- 3+1D Ideal hydro Longgang Pang, Qun Wang, Xin-Nian Wang Phys.Rev. C86 (2012) 024911
- Location of gamma-jet is decided according probability of binary collision.

## Recoiled effect in the reconstructed jets



The contribution of the recoiled parton in the reconstructed jets

HL Li, FM Liu, GL Ma, XN Wang, Y Zhu

Phys.Rev.Lett. 106, 012301

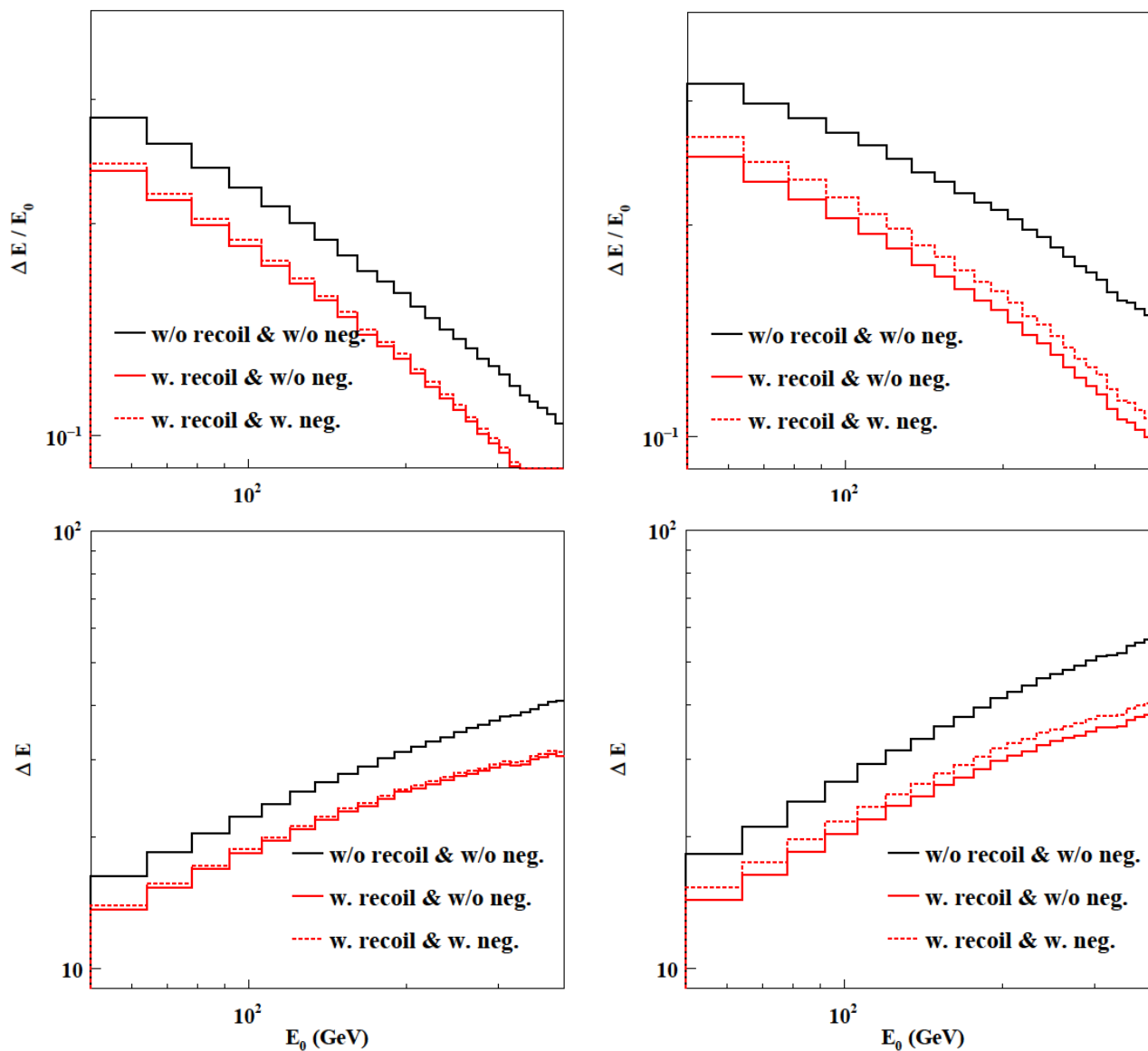
Xin-Nian Wang, Yan Zhu

Phys.Rev.Lett. 111, 062301

Yayun He, Tan Luo, Xin-Nian Wang, Yan Zhu

Phys.Rev. C91 (2015) 054908

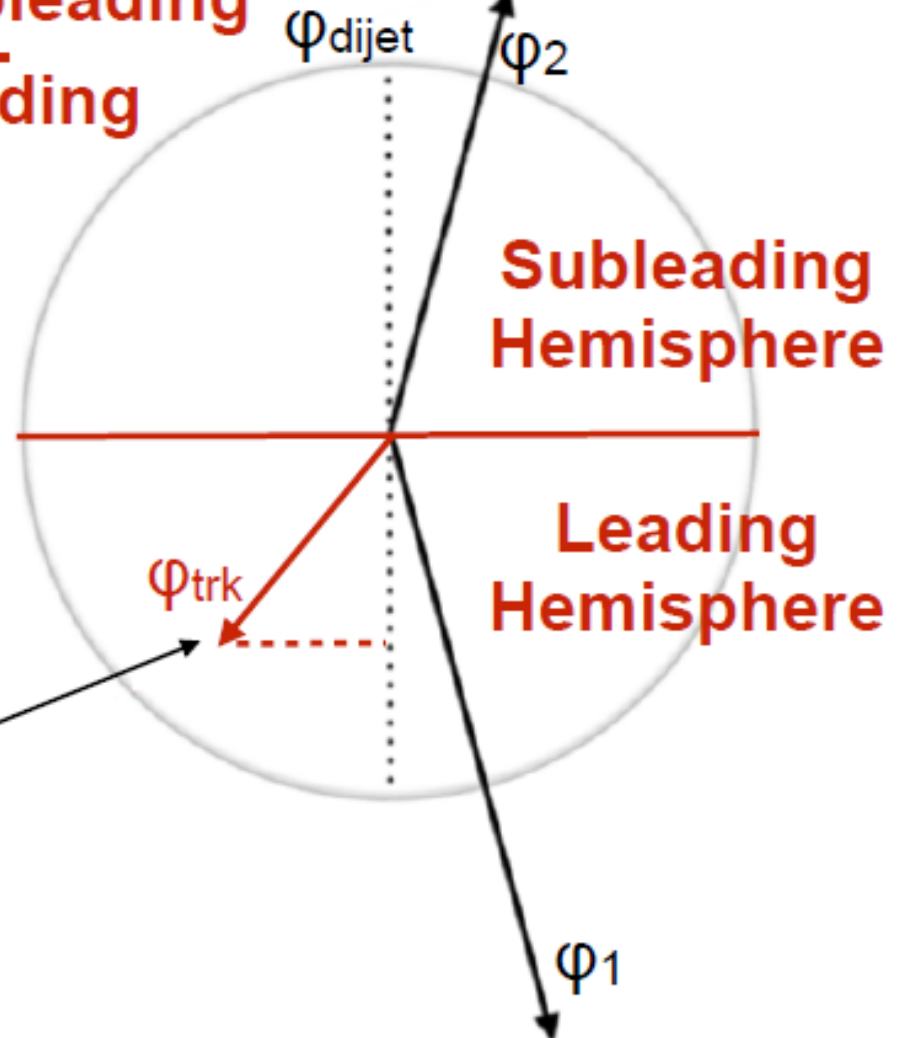
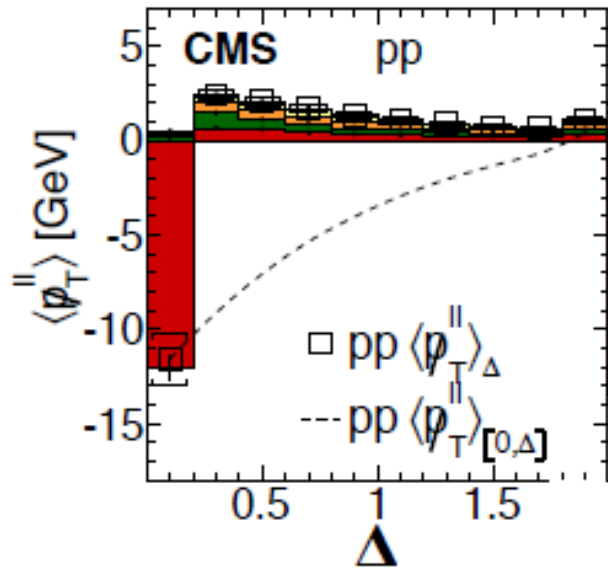
# Recoiled effect in the reconstructed jets





# $p_T$ imbalance of dijet in heavy-ion collisions

Christopher McGinn  
CMS collaboration

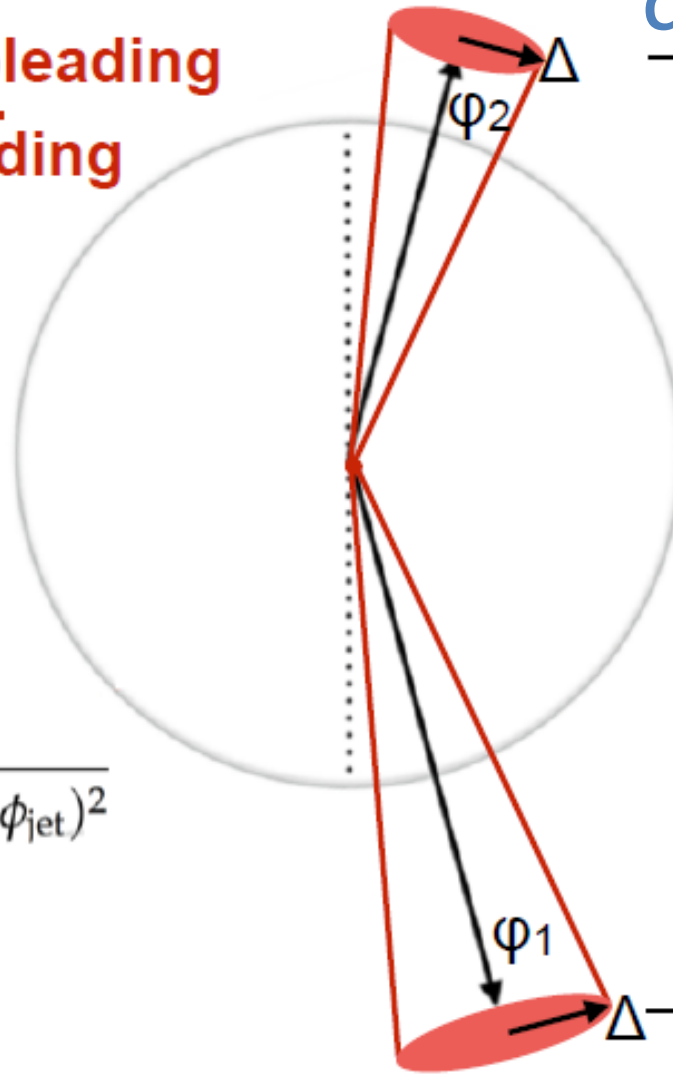
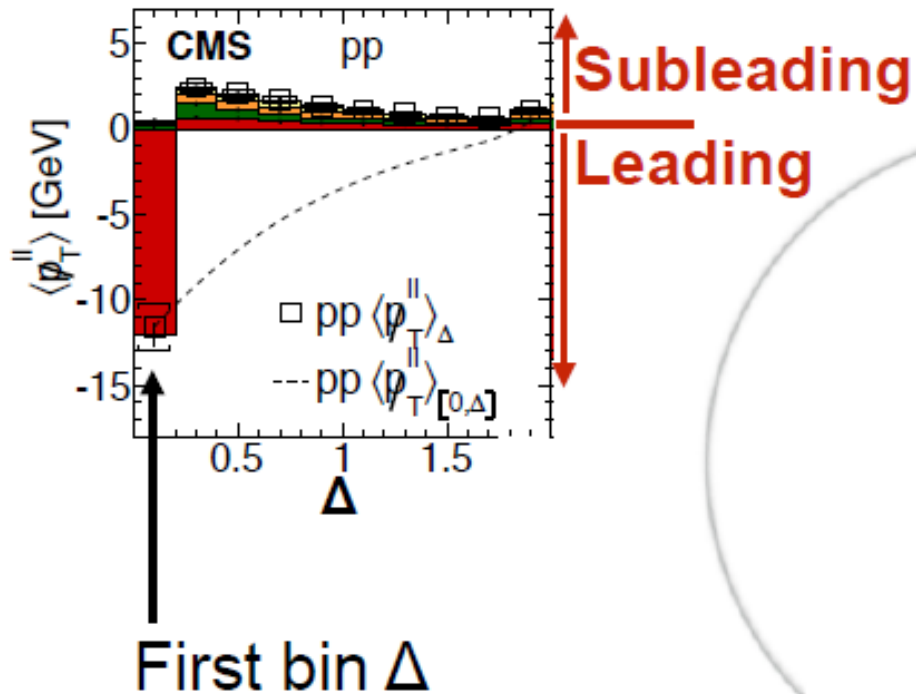


Track here  
contributes to  
Leading side

$$p_T^{\parallel} = -c^{\text{trk}} \times p_T^{\text{trk}} \times \cos(\phi_{\text{trk}} - \phi_{\text{dijet}})$$

# $p_T$ imbalance of dijet in heavy-ion collisions

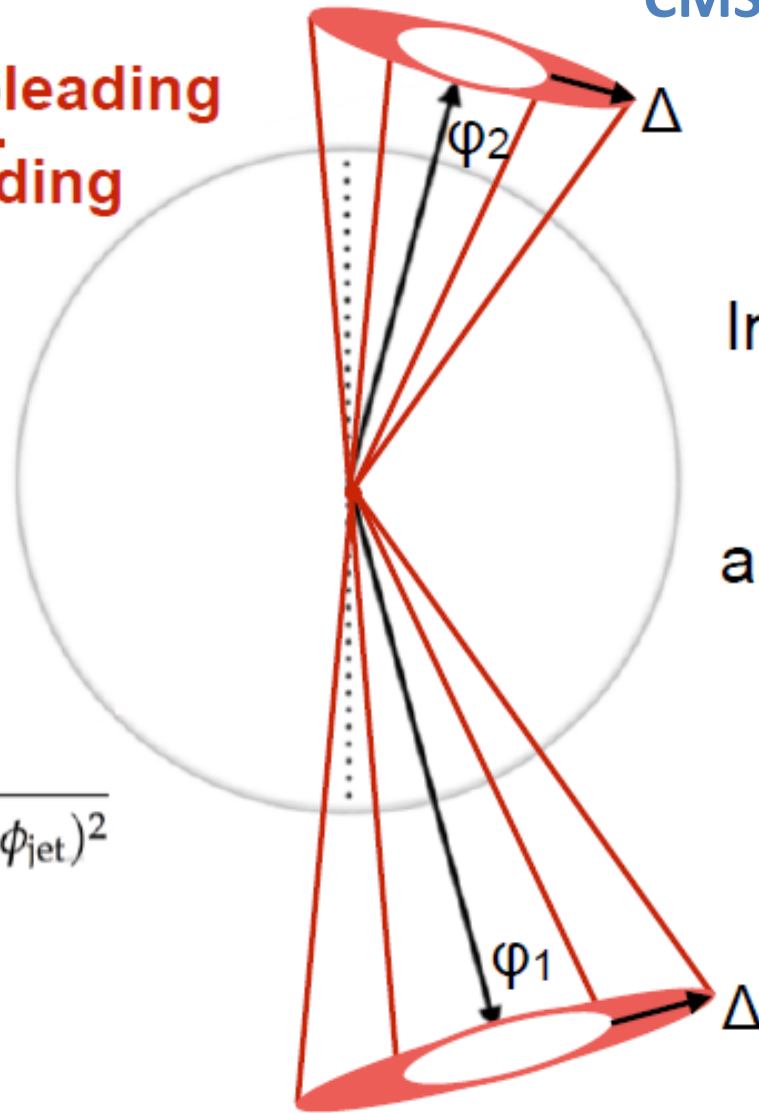
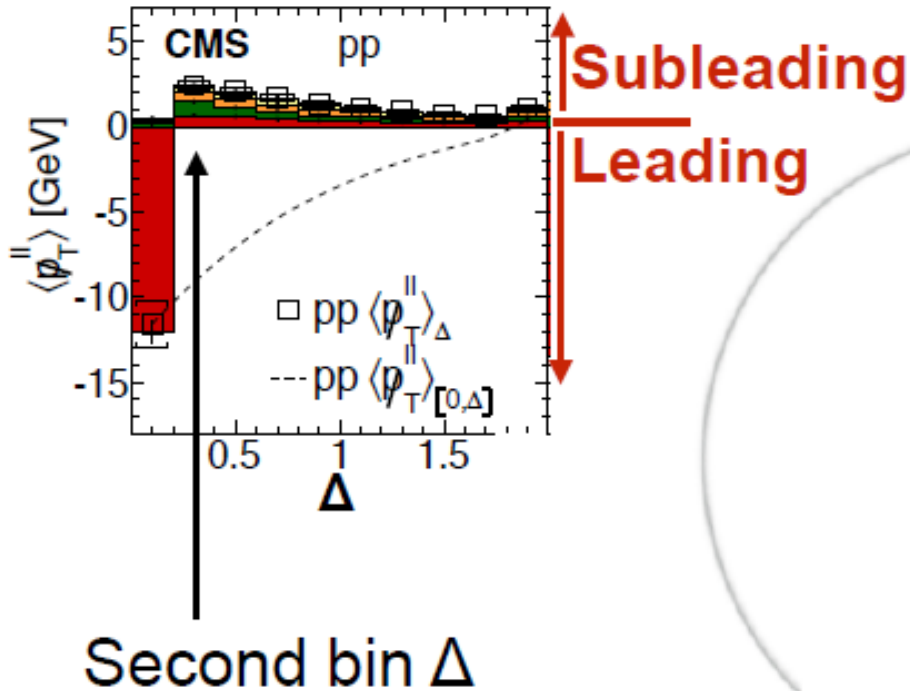
Christopher McGinn  
CMS collaboration



First bin  $\Delta$   
**NOT**  
same as jet  
cone

$$\Delta = \sqrt{(\eta_{\text{trk}} - \eta_{\text{jet}})^2 + (\phi_{\text{trk}} - \phi_{\text{jet}})^2}$$

Christopher McGinn  
CMS collaboration

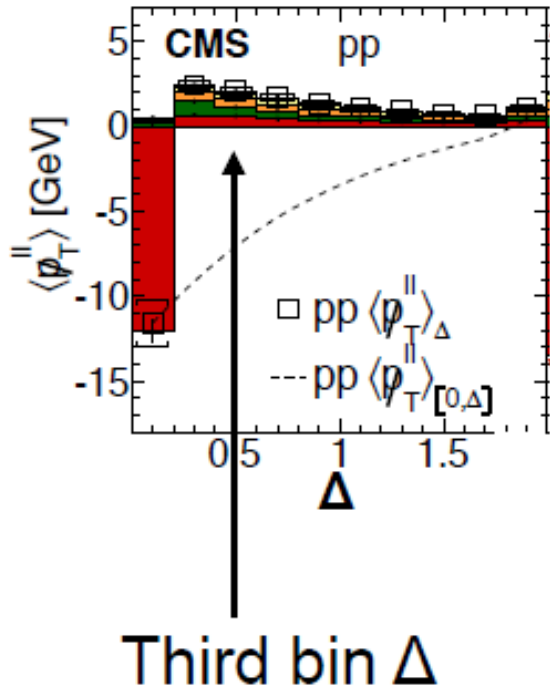


Increasing  $\Delta \rightarrow$   
Move away  
from leading  
and subleading  
jets

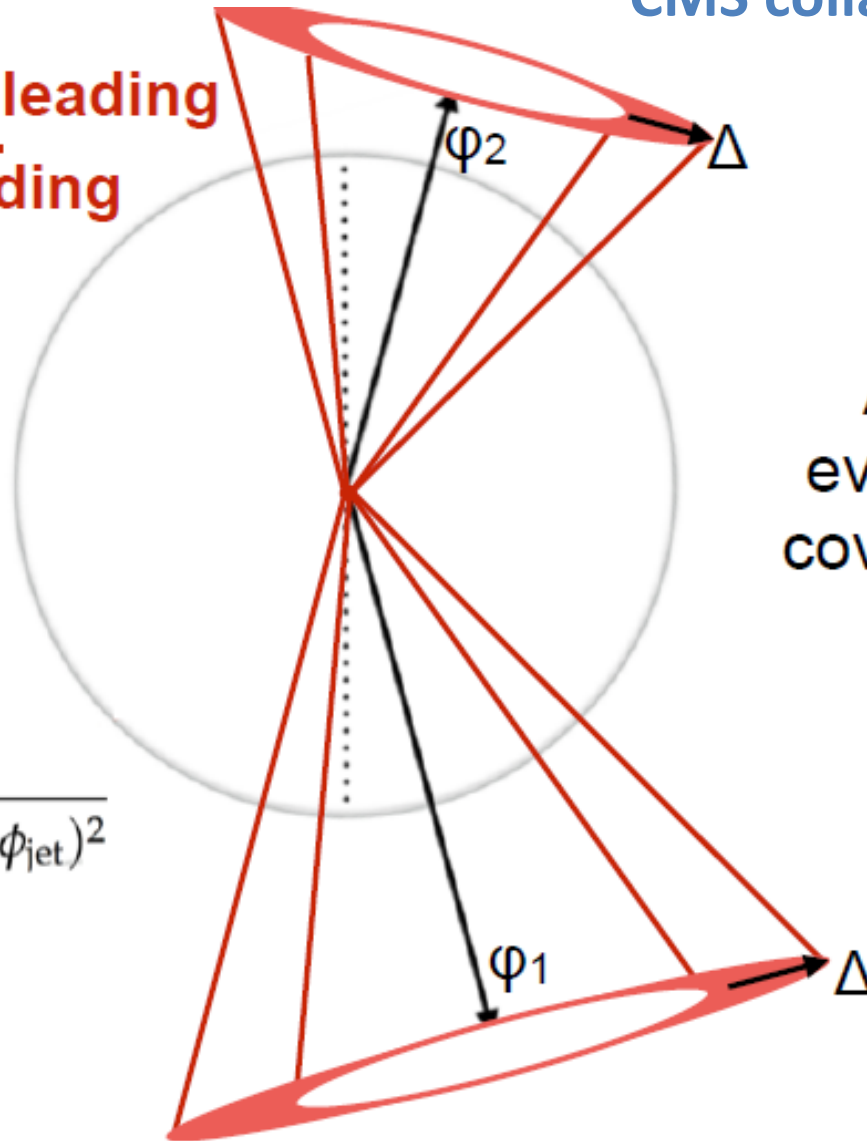
$$\Delta = \sqrt{(\eta_{\text{trk}} - \eta_{\text{jet}})^2 + (\phi_{\text{trk}} - \phi_{\text{jet}})^2}$$

# $p_T$ imbalance of dijet in heavy-ion collisions

Christopher McGinn  
CMS collaboration



Subleading  
Leading



Annuli  
eventually  
cover entire  
event

$$\Delta = \sqrt{(\eta_{\text{trk}} - \eta_{\text{jet}})^2 + (\phi_{\text{trk}} - \phi_{\text{jet}})^2}$$

## 5.02 TeV

$$|\eta_\gamma| < 1.44, P_{Tjet} > 30 \text{ GeV}, |\eta_{jet}| < 1.6$$

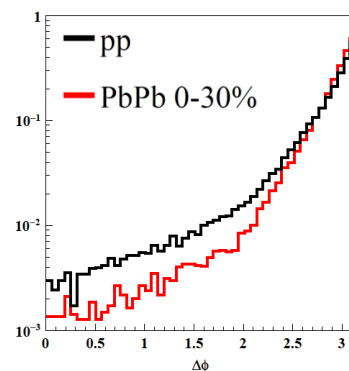
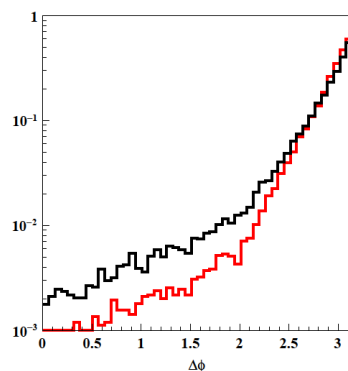
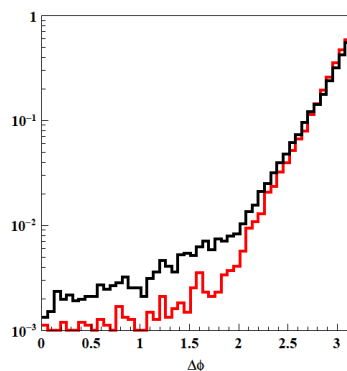
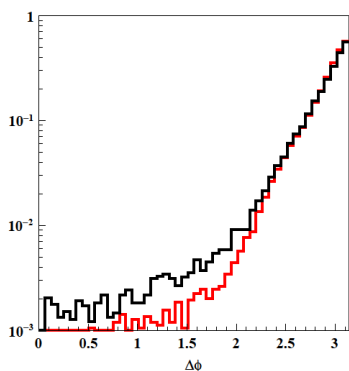
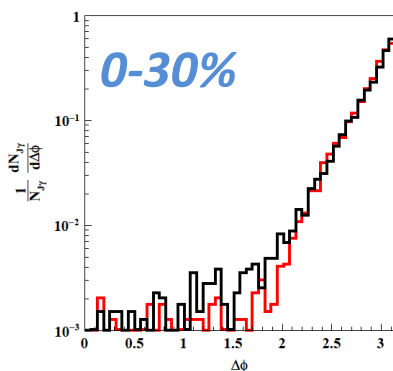
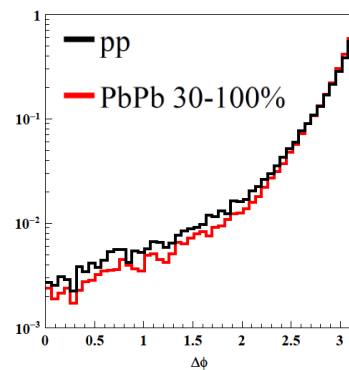
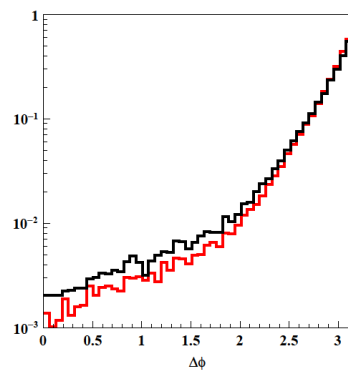
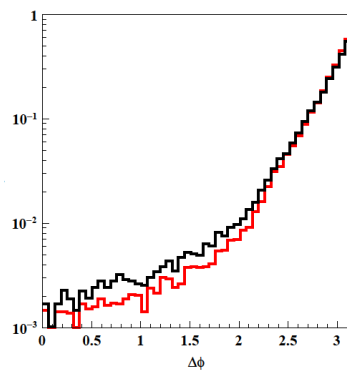
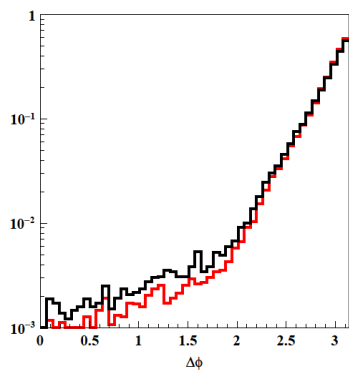
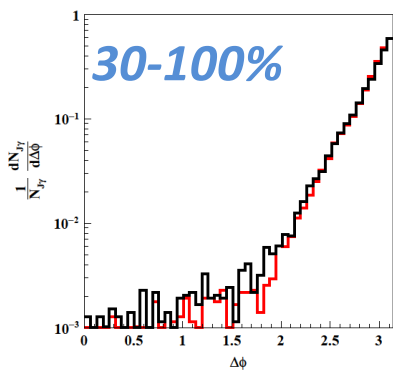
40 GeV <  $P_{T\gamma}$  < 50 GeV

50 GeV <  $P_{T\gamma}$  < 60 GeV

60 GeV <  $P_{T\gamma}$  < 80 GeV

80 GeV <  $P_{T\gamma}$  < 100 GeV

$P_{T\gamma} > 100 \text{ GeV}$

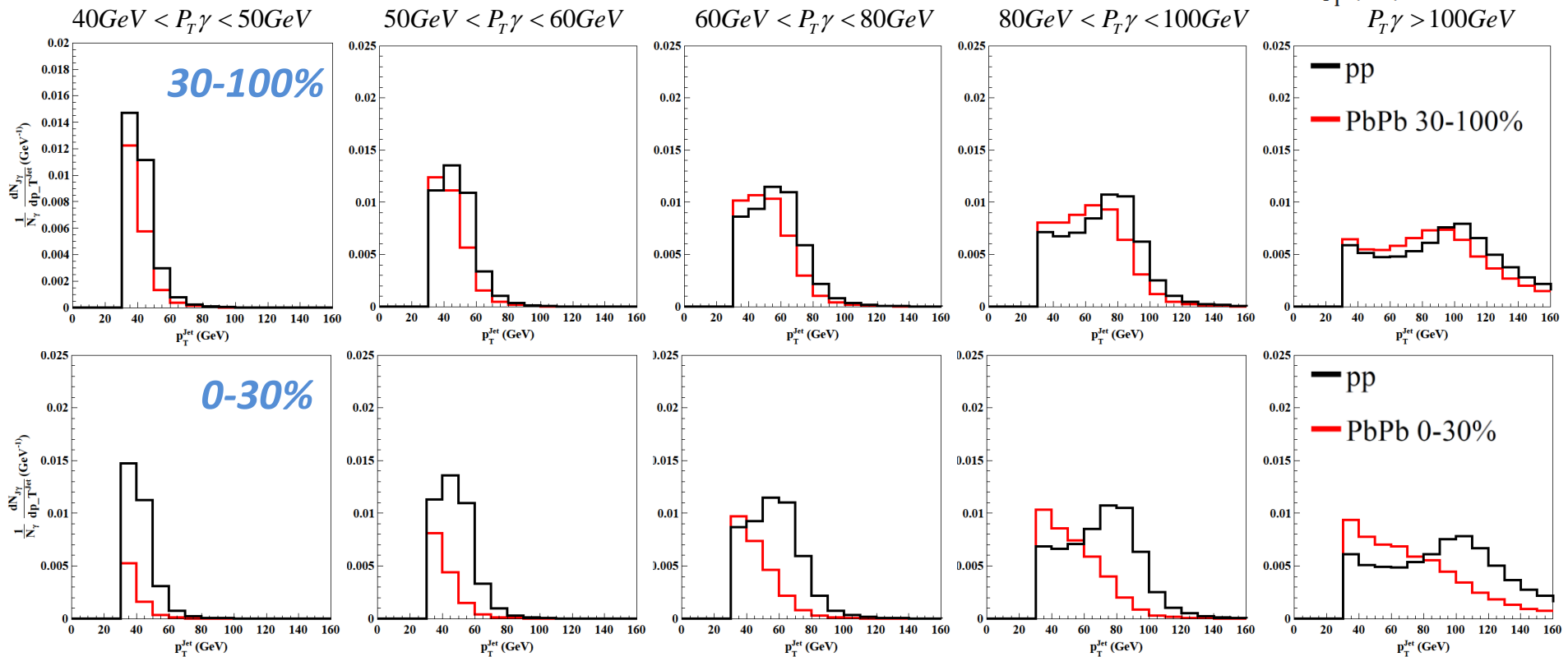
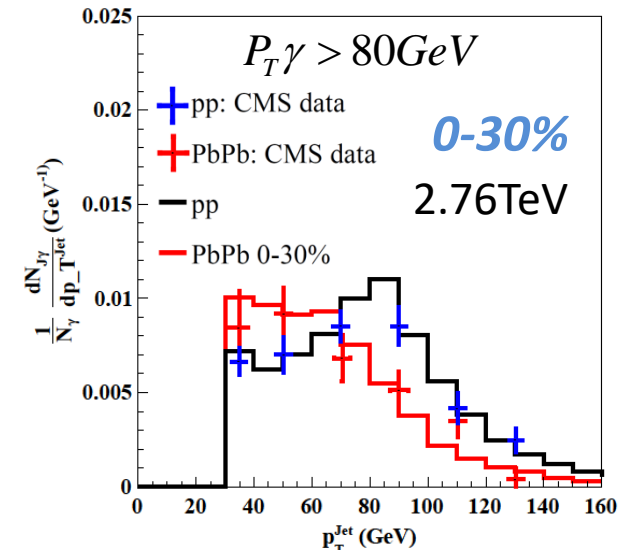


# $p_T$ distribution of gamma-jets in heavy-ion collisions

- Shift of the peak of the  $p_T$  distribution
- Path length dependence of the energy loss

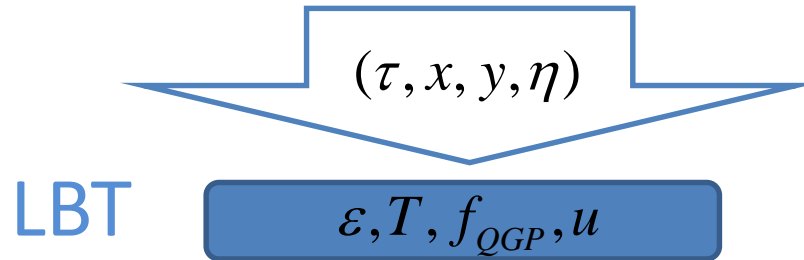
5.02 TeV

$$\Delta\phi_{J\gamma} > 7/8\pi$$

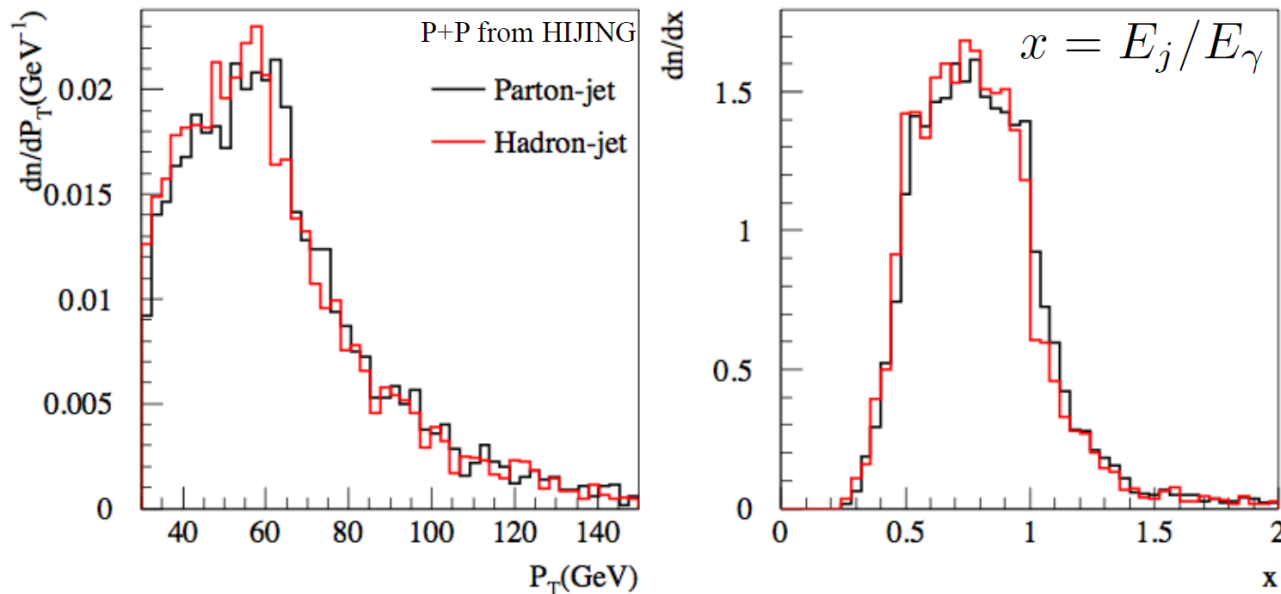


# Gamma-jets in a 3+1D hydro

- 3+1D Ideal hydro Longgang Pang, Qun Wang, Xin-Nian Wang Phys.Rev. C86 (2012) 024911

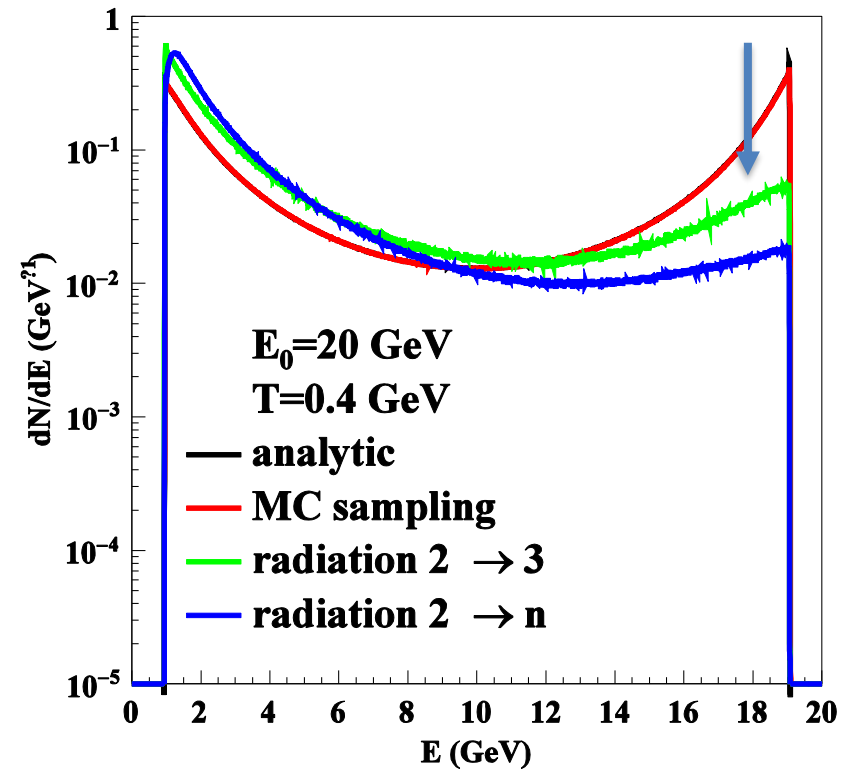
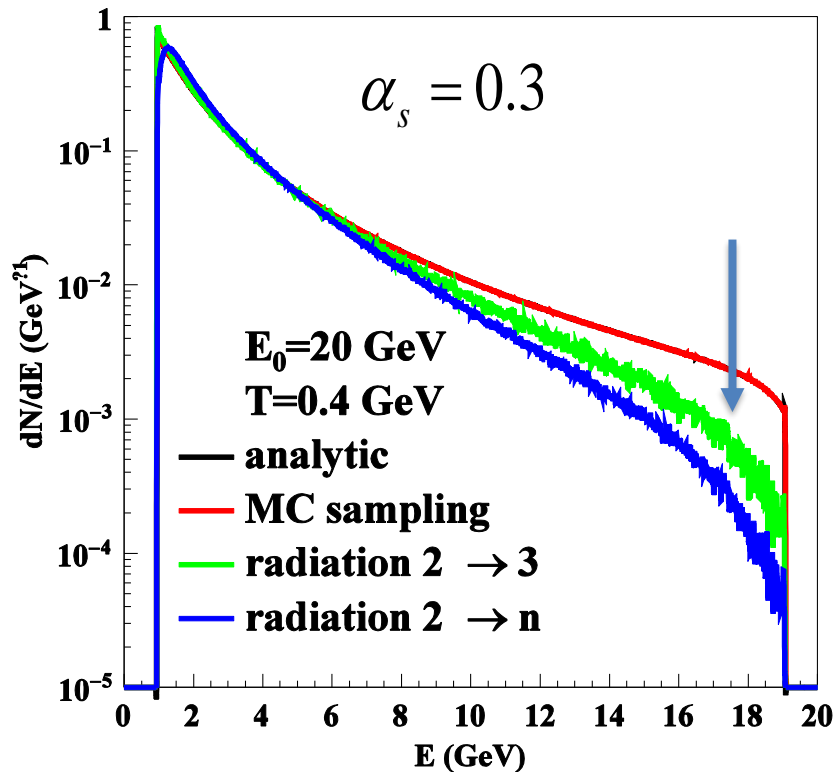


- Location of gamma-jet is decided according probability of binary collision.
- Small difference between parton-jet and hadron-jet.



# Energy distribution of the radiated gluon

Global energy-momentum conservation in 2->3 and 2->n processes



$$P_{q \rightarrow qg}(x) = C_A \frac{(1-x)(1+(1-x)^2)}{x}$$

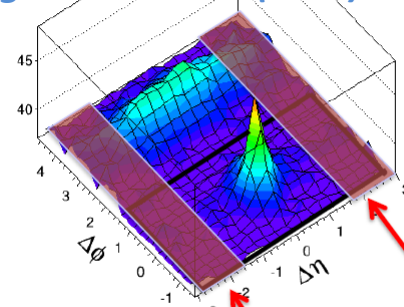
$$P_{g \rightarrow gg}(x) = 2N_C \frac{(1-x+x^2)^3}{x(1-x)}$$



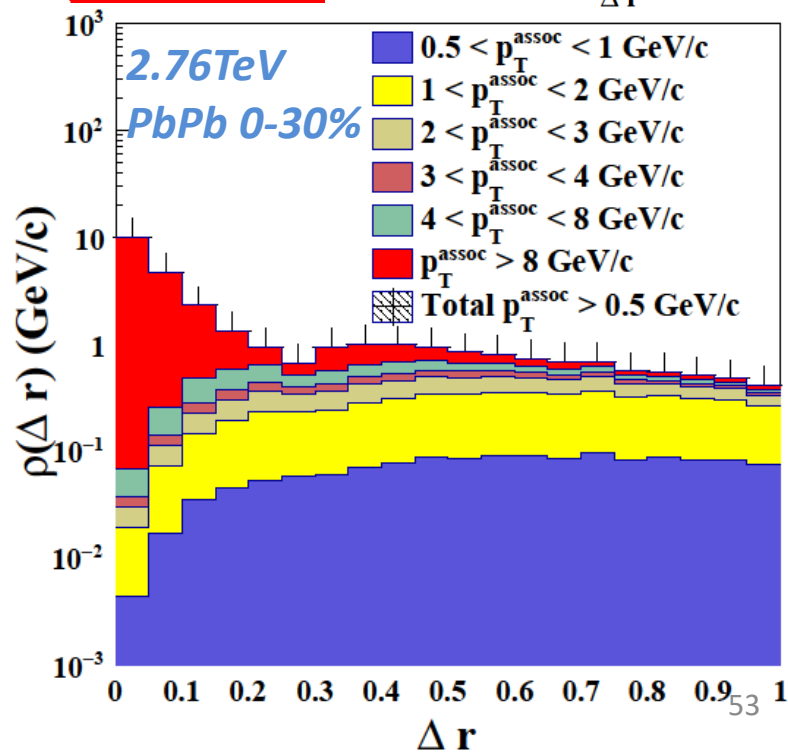
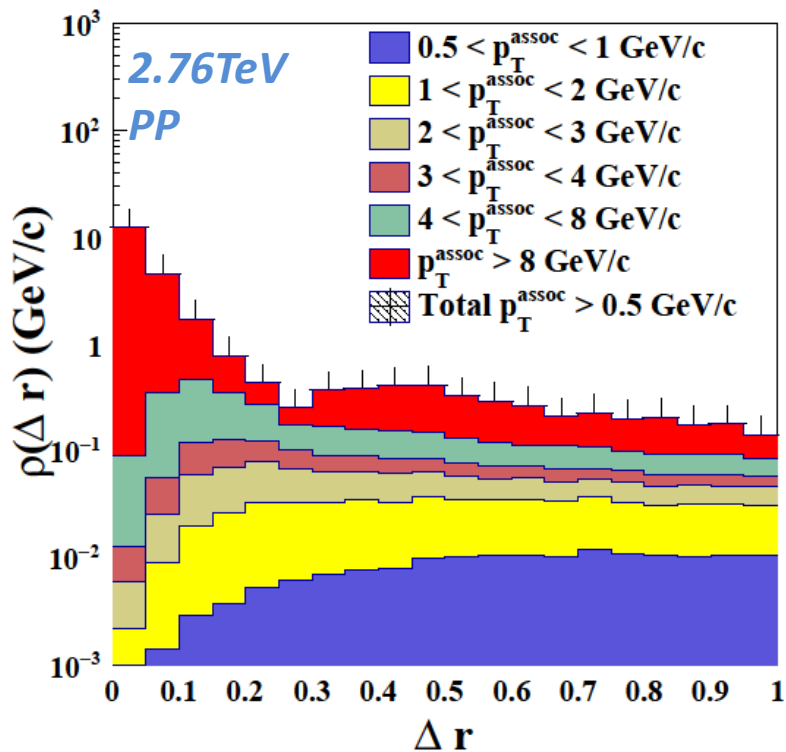
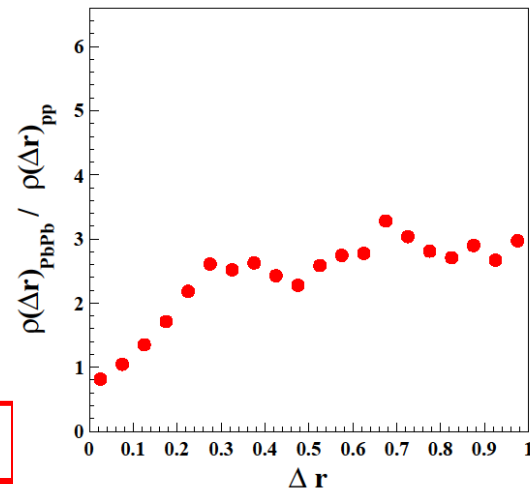
# Jet shape of gamma-jets in heavy-ion collisions

- Energy lost by the hard parton is transport out of the jet cone by the soft parton.

Leading  
Olga Evdokimov (CMS)



“Sideband” region  
 $1.5 < |\Delta\eta| < 2.5$



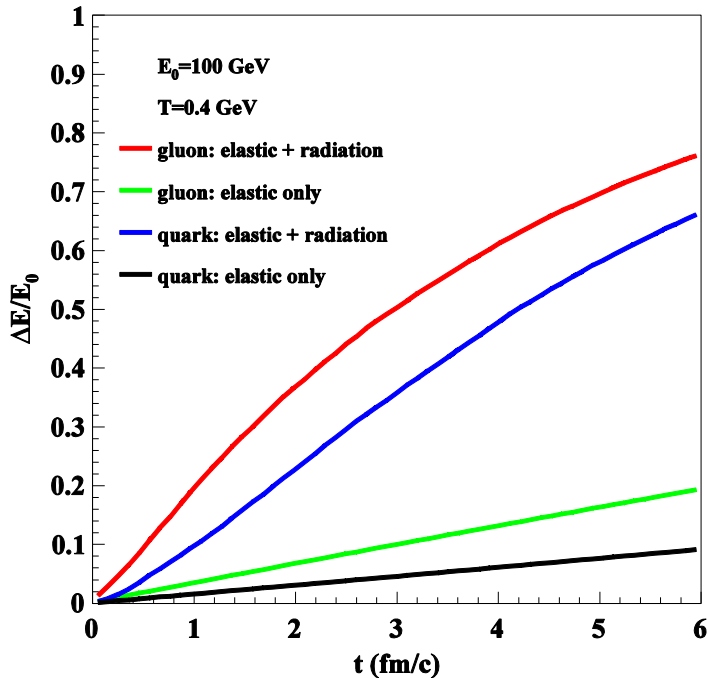
# Nontrivial path length dependence on parton energy loss

## Leading parton energy loss

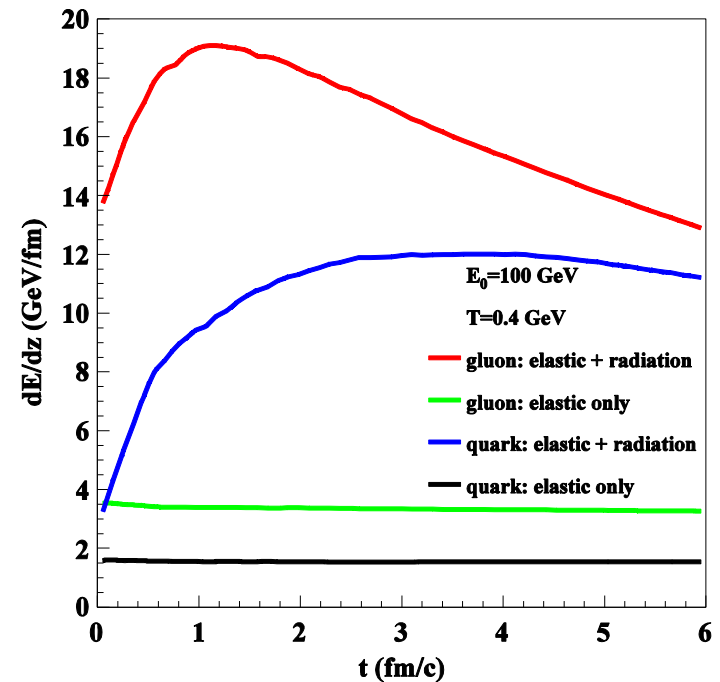
Propagation of a single initial jet parton in a uniform medium

$$\alpha_s = 0.3 \quad E = 100 \text{ GeV} \quad T = 0.4 \text{ GeV}$$

### Fractional energy loss



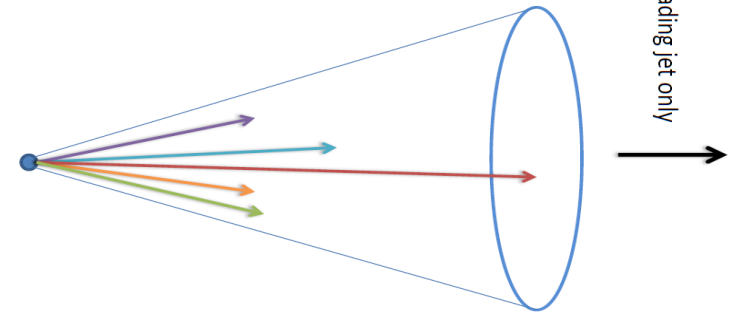
### Energy loss per unit length



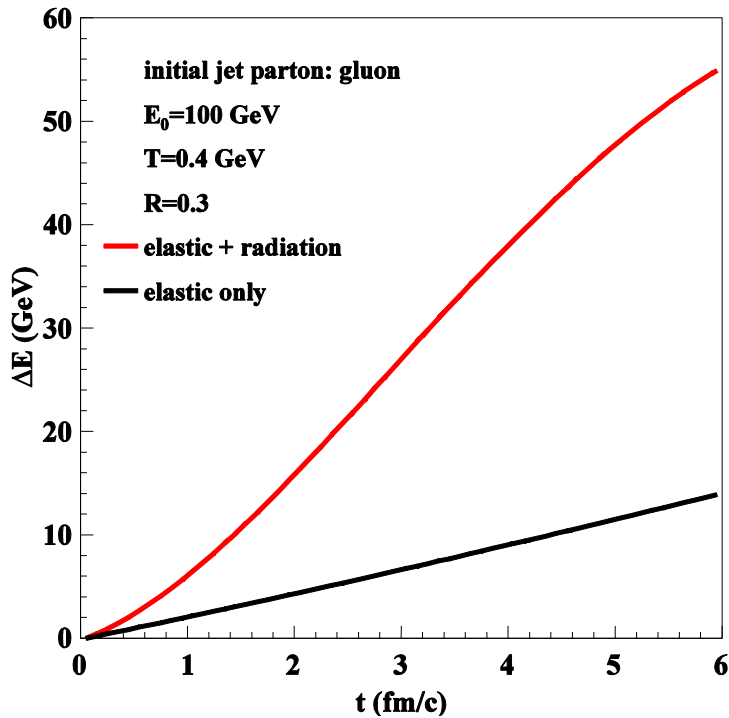
# Path length dependence on parton energy loss

## Leading jet energy loss

- Leading jet recover some of the energy lost by the leading parton.



## Initial jet parton: gluon



## Initial jet parton: quark

