

HF Production and Dynamics in AMPT

Zi-Wei Lin
Department of Physics
East Carolina University



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Outline

- Where are heavy flavours in the AMPT model?
- Anisotropic parton escape: *review*
- Anisotropic parton escape: *flavour dependence*
- Future heavy flavour work with AMPT
- Summary

A Multi-Phase Transport AMPT

ZWL et al. PRC72 (2005)

was constructed as a comprehensive model for heavy ion collisions.

It aims to

evolve the system from initial condition to final observables;
conserve energy/momentum/flavour/charge of each event,
include particle productions of different flavours at different P_T & y ,
keep non-equilibrium features and dynamics
(e.g. intrinsic fluctuations and correlations).

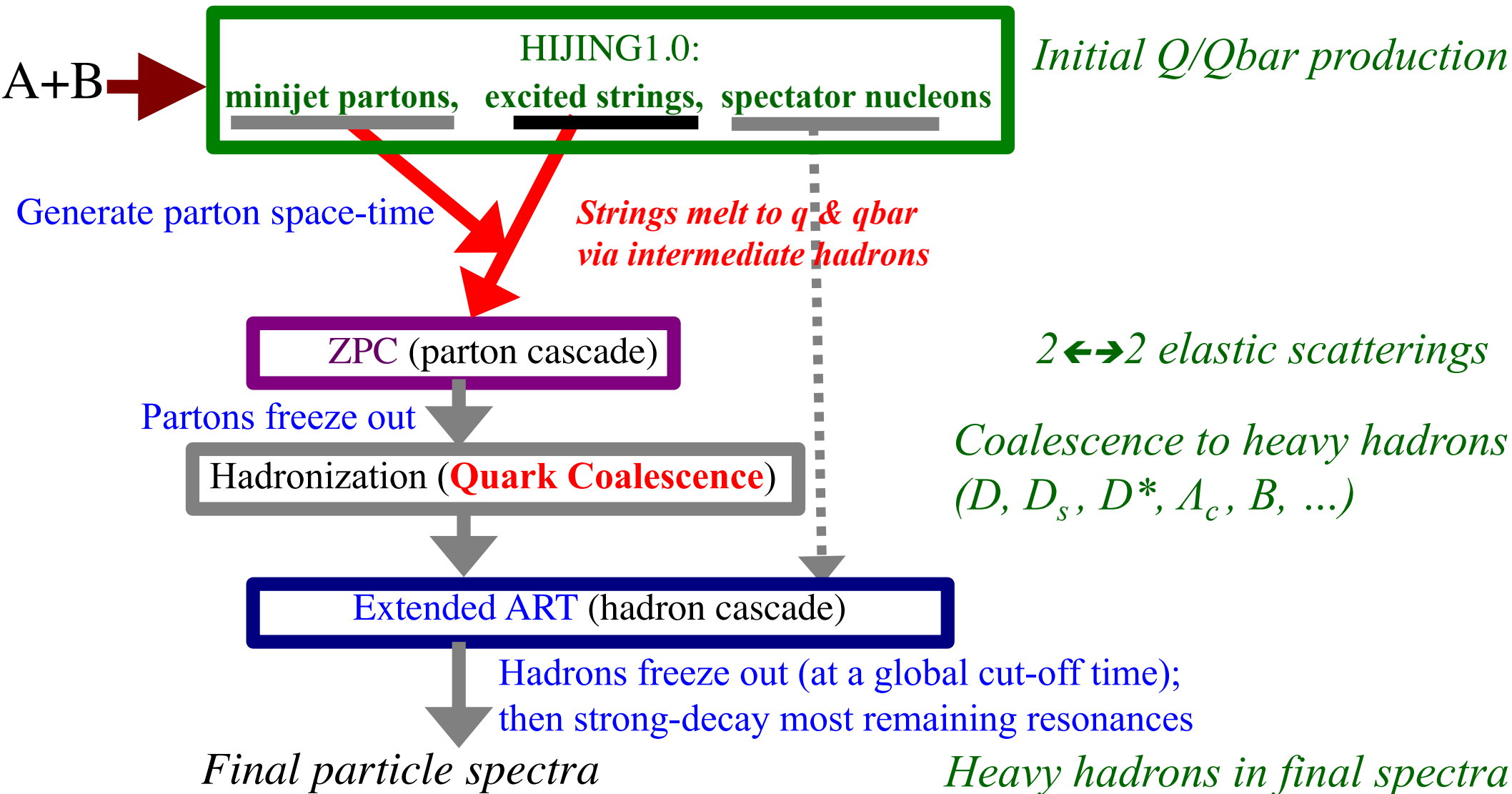
It is also a test-bed of different ideas:

- Discovery of the triangular flow v_3 Alver & Roland, PRC 81 (2010)
- Longitudinal (de)correlations of flows Pang et al. PRC 91 (2015), EPJA52 (2016)
- Flow may be dominated by anisotropic parton escape He et al. PLB753 (2016); ZWL et al. NPA 956 (2016)

So we are working to extend AMPT to heavy flavours, in order to simultaneously study light flavours, heavy flavours including their interactions.

Where are heavy flavours (Q) in the current AMPT model?

Structure of AMPT v2.xx (String Melting version)



The escape mechanism: review

Liang He, Terrence Edmonds, ZWL, Feng Liu, Denes Molnar, Fuqiang Wang: PLB 753 (2016):

Anisotropic parton escape is the dominant source of azimuthal anisotropy in transport models.

ZWL et al. NPA 956 (2016) for Quark Matter 2015:

Elliptic anisotropy v_2 may be dominated by particle escape instead of hydrodynamic flow.

Background:

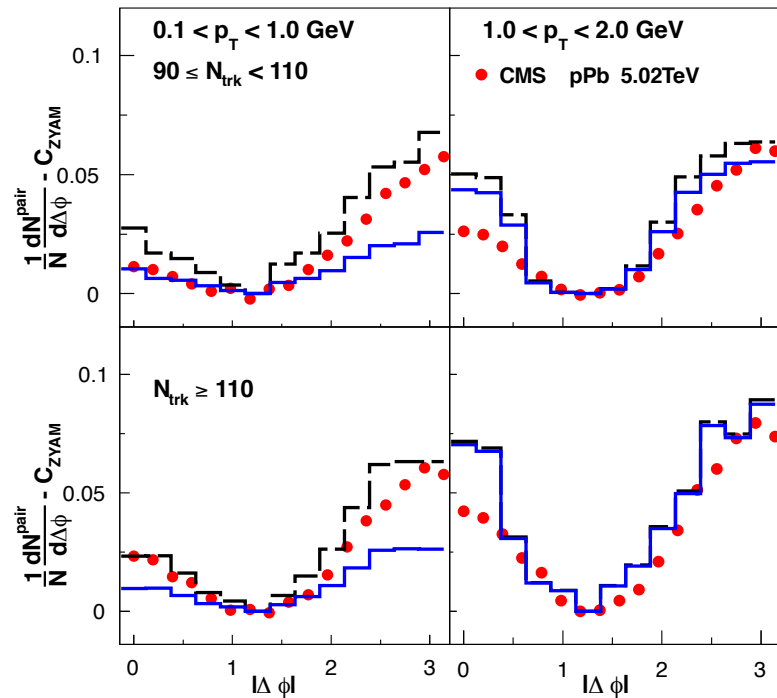
- **Transport models** at large-enough cross section will approach **hydrodynamics**.

It has been generally believed that:

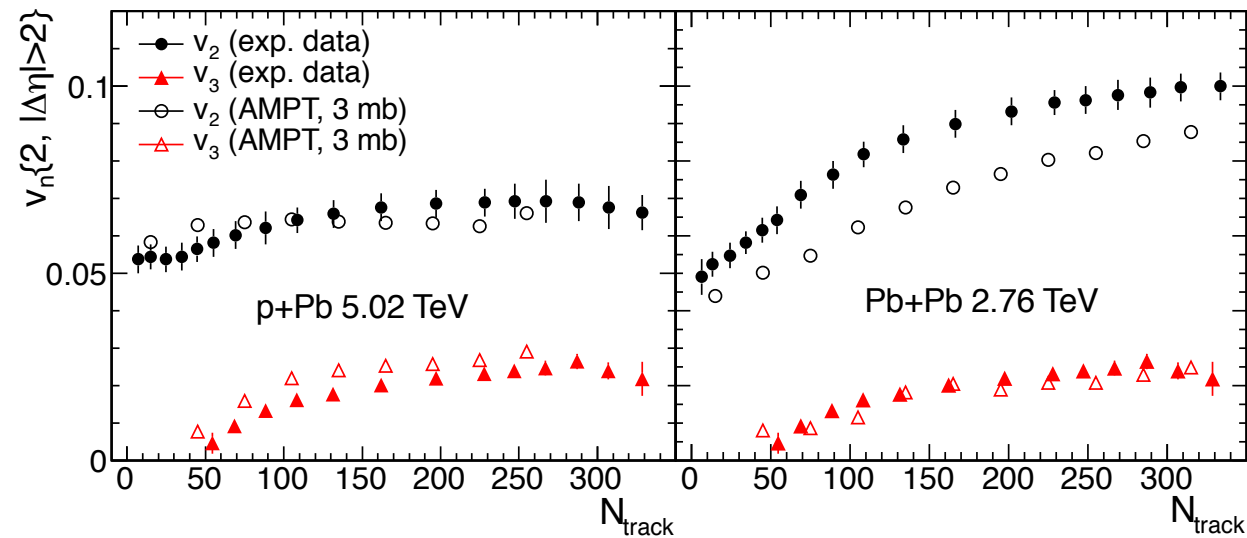
- Early hydro-type collective flow in sQGP converts initial spatial anisotropy into final momentum-space v_n
- For low- P_T particles in high-energy heavy ion collisions, since both **hydrodynamics** and **transport models** can describe v_n data, the mechanism of v_n development in **transport models** (*via particle interactions*) is in principle the same as in **hydrodynamics** (*via pressure gradients*).

The escape mechanism: review

Small systems: again, both **hydrodynamics** and **transport** can describe flow.



Bozek and Broniowski, PLB 718 (2013)
using e-by-e viscous hydrodynamics.



Bzdak and Ma, PRL 113 (2014)
using AMPT (String Melting version).

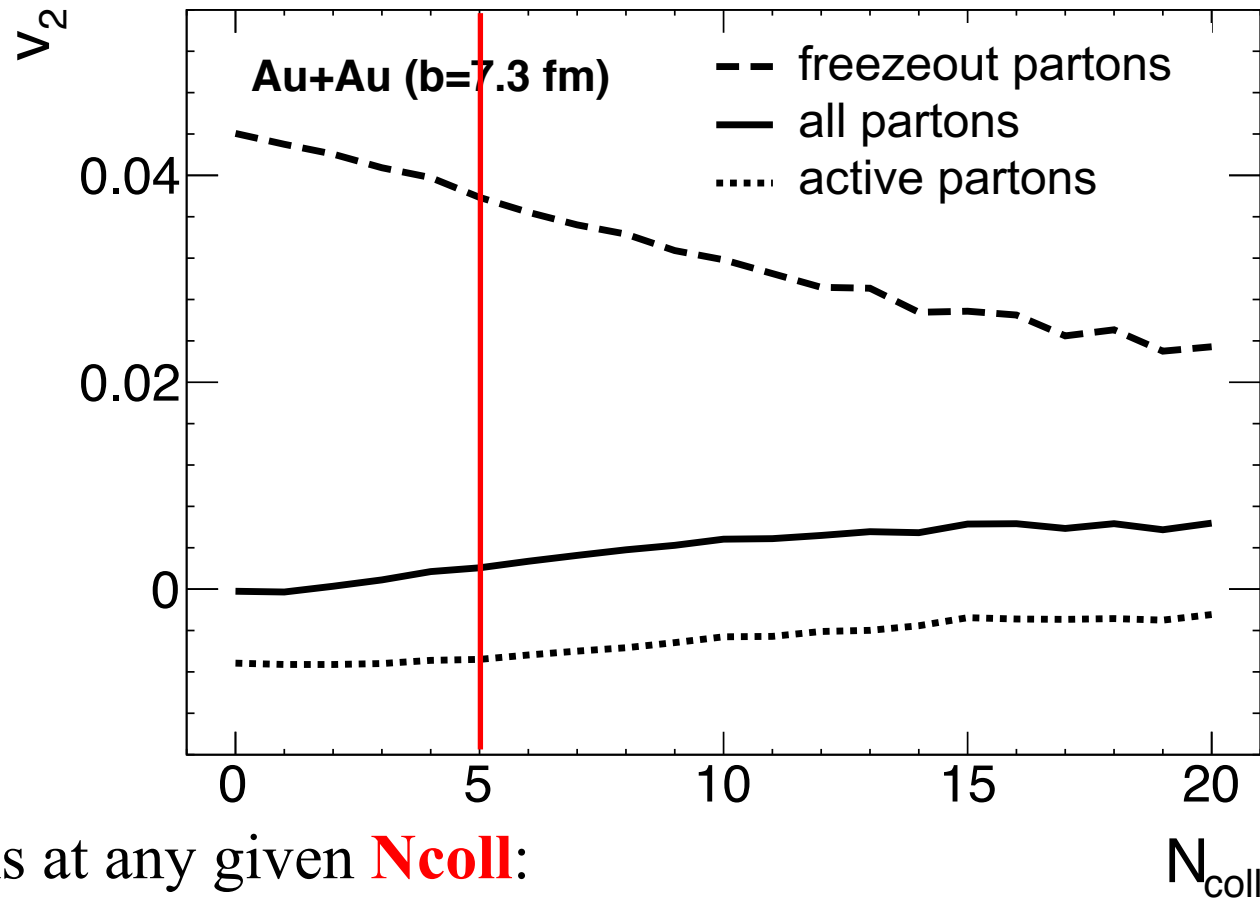
Puzzle for small systems such as p+Pb or d+Au:

- Mean free path may be comparable to the system size; is **hydrodynamics** still applicable to such small systems?
- Transport and hydrodynamics should be different here, could they also be different for large systems?

The escape mechanism: review

We have followed the complete parton collision history and evaluate its effect on parton v_2 in AMPT.

Ncoll: *number of collisions suffered by a parton*



He et al. PLB753 (2016)

3 parton populations at any given **Ncoll**:

- freezeout partons:** *freeze out after exactly N_{coll} collisions;*
- active partons:** *will collide further, freeze out after $>N_{\text{coll}}$ collisions;*
- all partons:** *sum of the above two populations (i.e. all partons that have survived N_{coll} collisions).*

The escape mechanism: review

At Ncoll=0:

all partons: $v_2=0$ by symmetry (*as they include all initial partons*);

they contain 2 parts:

escaped/freezeout: $v_2 \approx 4.5\%$,

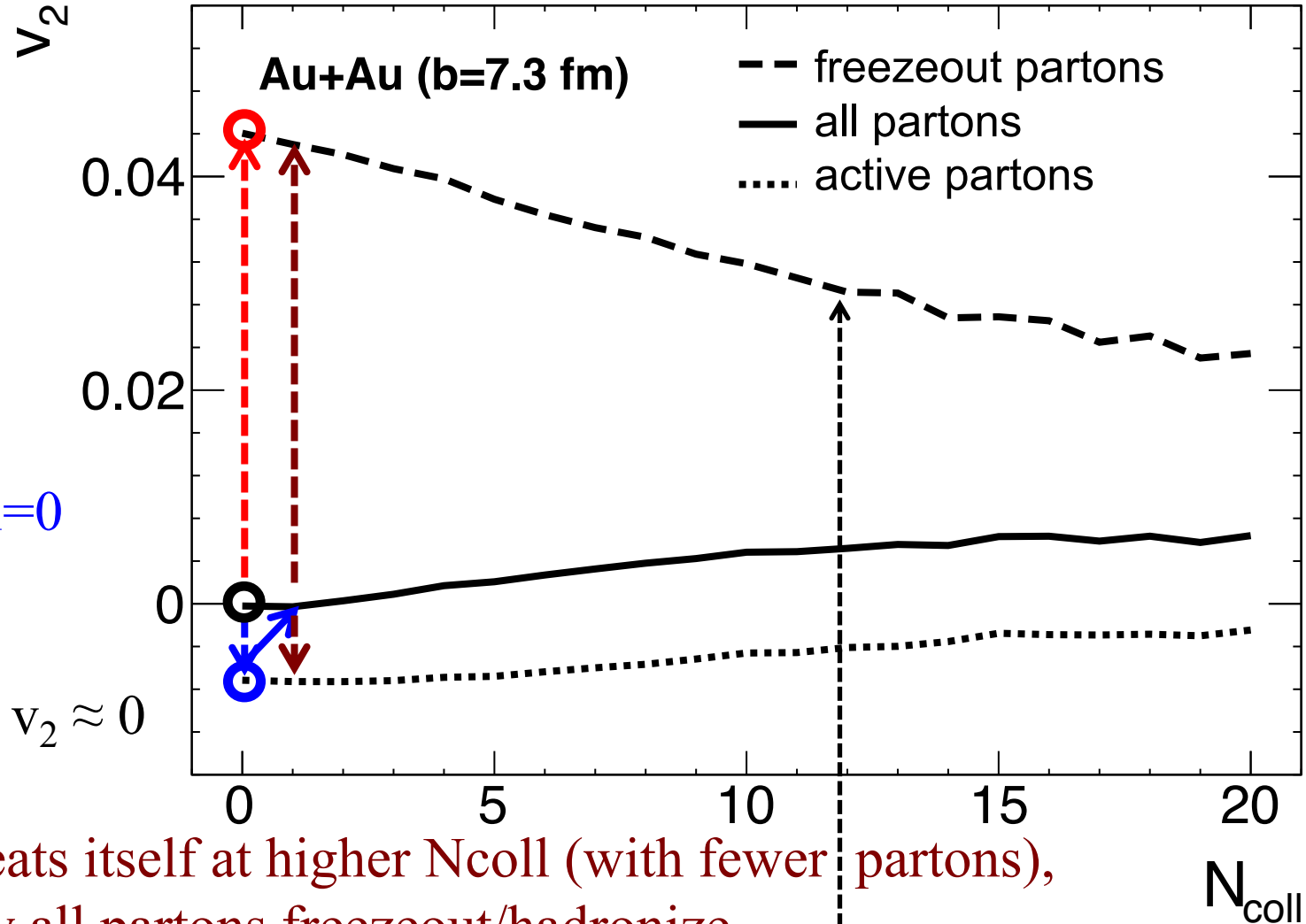
active: $v_2 < 0$.

At Ncoll=1:

active partons at Ncoll=0

collide once each
& become

all partons at Ncoll=1: $v_2 \approx 0$



This process repeats itself at higher Ncoll (with fewer partons),
eventually all partons freezeout/hadronize.

$\langle v_2 \rangle$ = weighed average of the freezeout partons' v_2 .

The escape mechanism: review

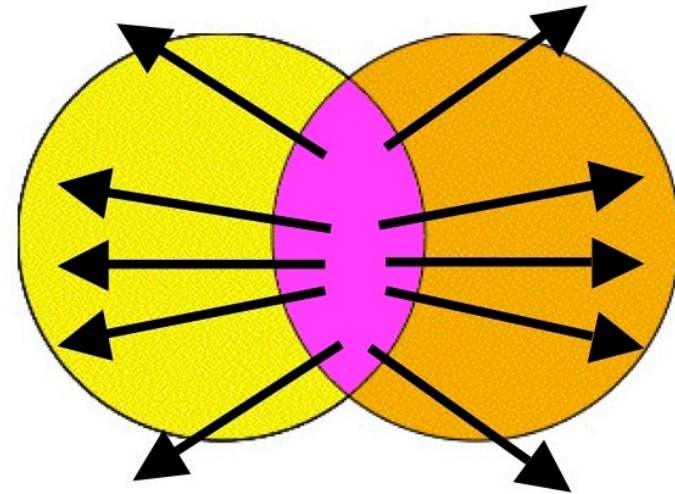
At $N_{\text{coll}}=0$:

escaped partons: $v_2 \approx 4.5\%$,
this is **purely** due to
anisotropic escape probability
(response to geometrical shape only,
no contribution from collective flow)

At $N_{\text{coll}} \geq 1$:

escaped partons: $v_2 > 0$
due to
anisotropic escape probability
& (anisotropic) **collective flow**.

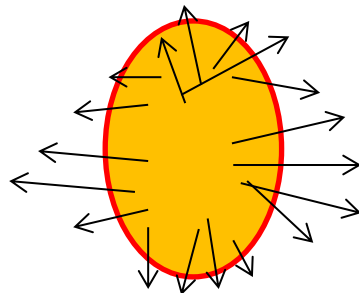
In event-averaged picture of elliptic flow:



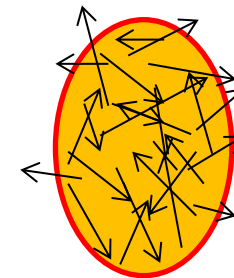
How to separate the two contributions?

We design a **Random- ϕ Test**

Normal:



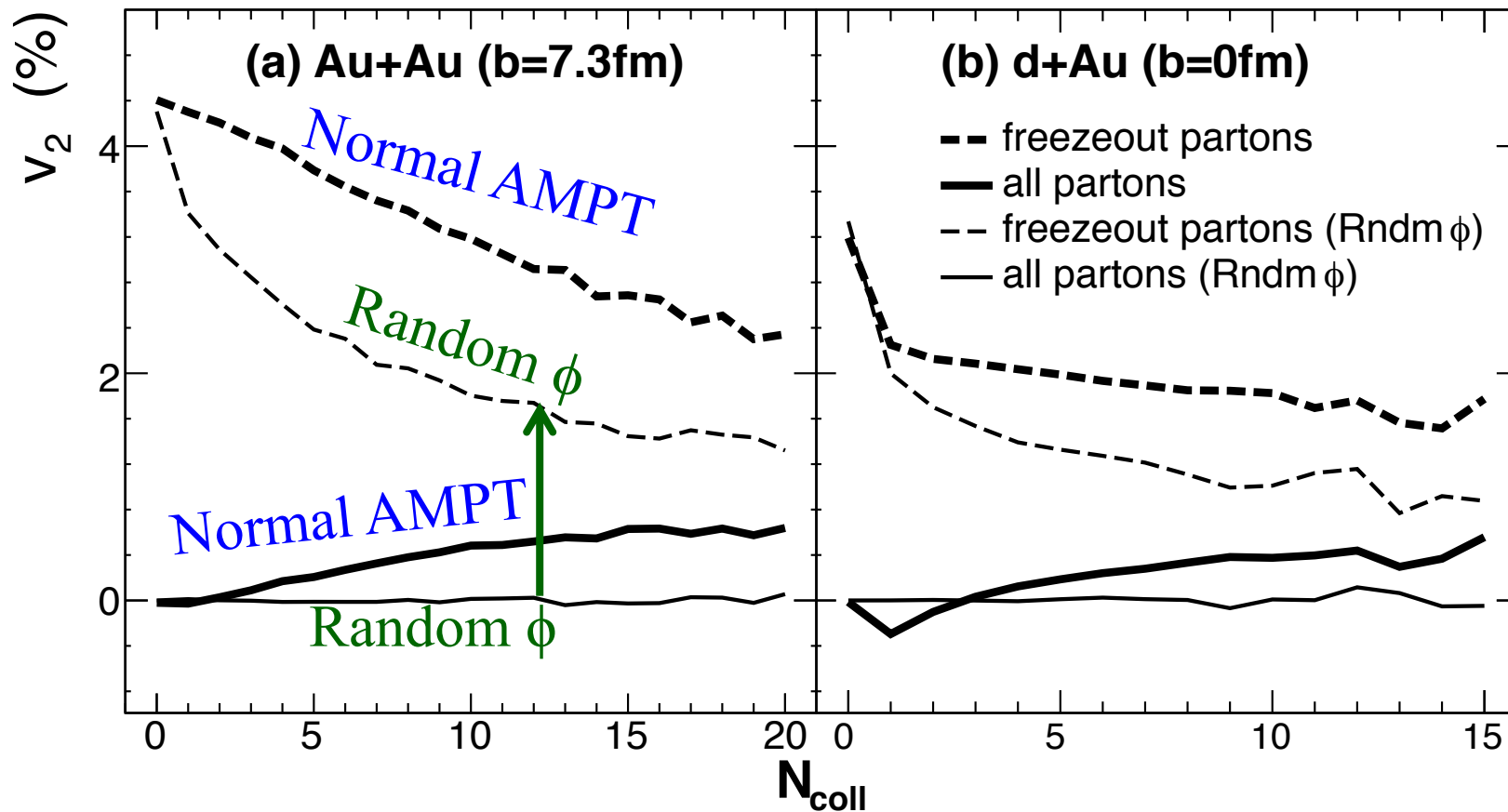
Random:



The escape mechanism: review

v_2 from the **Random- ϕ Test**: purely from the escape mechanism

He et al. PLB753 (2016)



$\langle v_2 \rangle_{\text{normal}}$

$\langle v_2 \rangle_{\text{random-}\phi}$

Ratio

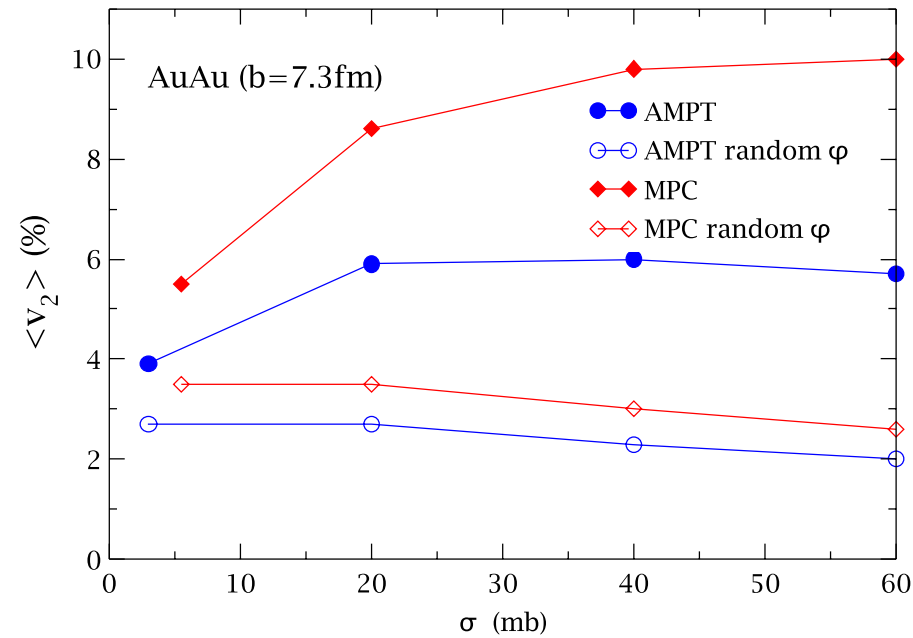
$\langle N_{\text{coll}} \rangle$

\sim fraction from pure escape

Au+Au	3.9%	2.7%	69%	4.6 (<i>modest</i>)
d+Au	2.7%	2.5%	93%	1.2 (<i>low</i>)

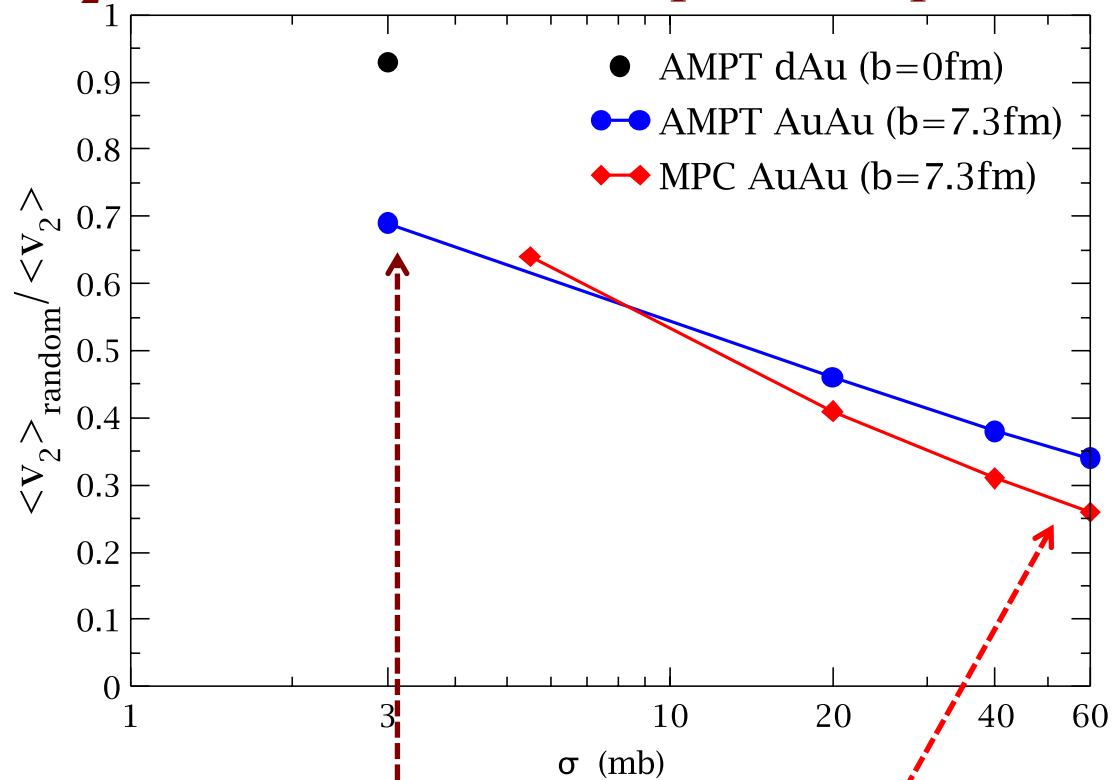
The escape mechanism: review

ZWL et al. NPA 956 (2016)



MPC: the same qualitative conclusion as AMPT despite many differences (*parton initial condition, cross section & $d\sigma/dt$, formation time, parton-subdivision*)

v_2 ratio \sim fraction from pure escape



Anisotropic particle escape is dominant for v_2 in small systems & even for v_2 in semi-central AuAu at RHIC.

At very large σ or $\langle N_{\text{coll}} \rangle$, hydrodynamic collective flow will be the dominant contribution of v_2 .

The escape mechanism: review

Implications:

- The escape mechanism helps to explain similar anisotropic flows observed in small and large systems:
since both are dominated by same mechanism (*anisotropic escape probability*)
- The driving force for v_2 at low & high P_T is qualitatively the same
since both are dominated by *anisotropic probability of interactions* before escape
(scatterings/kicks for low P_T & energy loss for high P_T)
- At low/modest opacity/ $\langle N_{\text{coll}} \rangle$: **transport and hydrodynamics are different.**

The escape mechanism dominates v_n at low to modest opacity/ $\langle N_{\text{coll}} \rangle$;
hydro-type collective flow dominates v_n at very high opacity/ $\langle N_{\text{coll}} \rangle$.

Which is the case for A+B collisions at RHIC & LHC?

The escape mechanism: flavour dependence

Our previous results are for ALL quarks @200 GeV.

**Does the escape mechanism work differently for different flavours?
or**

Does collective flow work differently for different flavours?

We now use string melting AMPT to analyze
light (u/d), strange, charm quarks
in p+Pb@5TeV, Au+Au@200GeV, Pb+Pb@2.76TeV.

H.L. Li, ZWL, F.Q. Wang, in preparation;
first result on pPb in H.L. Li, ZWL, F.Q. Wang, J Phys Conf Ser 779 (2017)

The escape mechanism: flavour dependence

Elastic parton scatterings only:

$$q_i q_j \rightarrow q_i q_j, \quad q_i \bar{q}_j \rightarrow q_i \bar{q}_j, \quad q Q \rightarrow q Q, \dots$$

Caveat: here we use the same cross section for all flavours:

Parton cross section
based on $gg \rightarrow gg$
in leading-order pQCD:

$$\begin{aligned} \frac{d\sigma_{gg}}{dt} &= \frac{9\pi\alpha_s^2}{2s^2} \left(3 - \frac{ut}{s^2} - \frac{us}{t^2} - \frac{st}{u^2} \right) \\ &\simeq \frac{9\pi\alpha_s^2}{2} \left(\frac{1}{t^2} + \frac{1}{u^2} \right) \simeq \frac{9\pi\alpha_s^2}{2t^2} \end{aligned}$$

A screening mass μ
regulates the divergence:

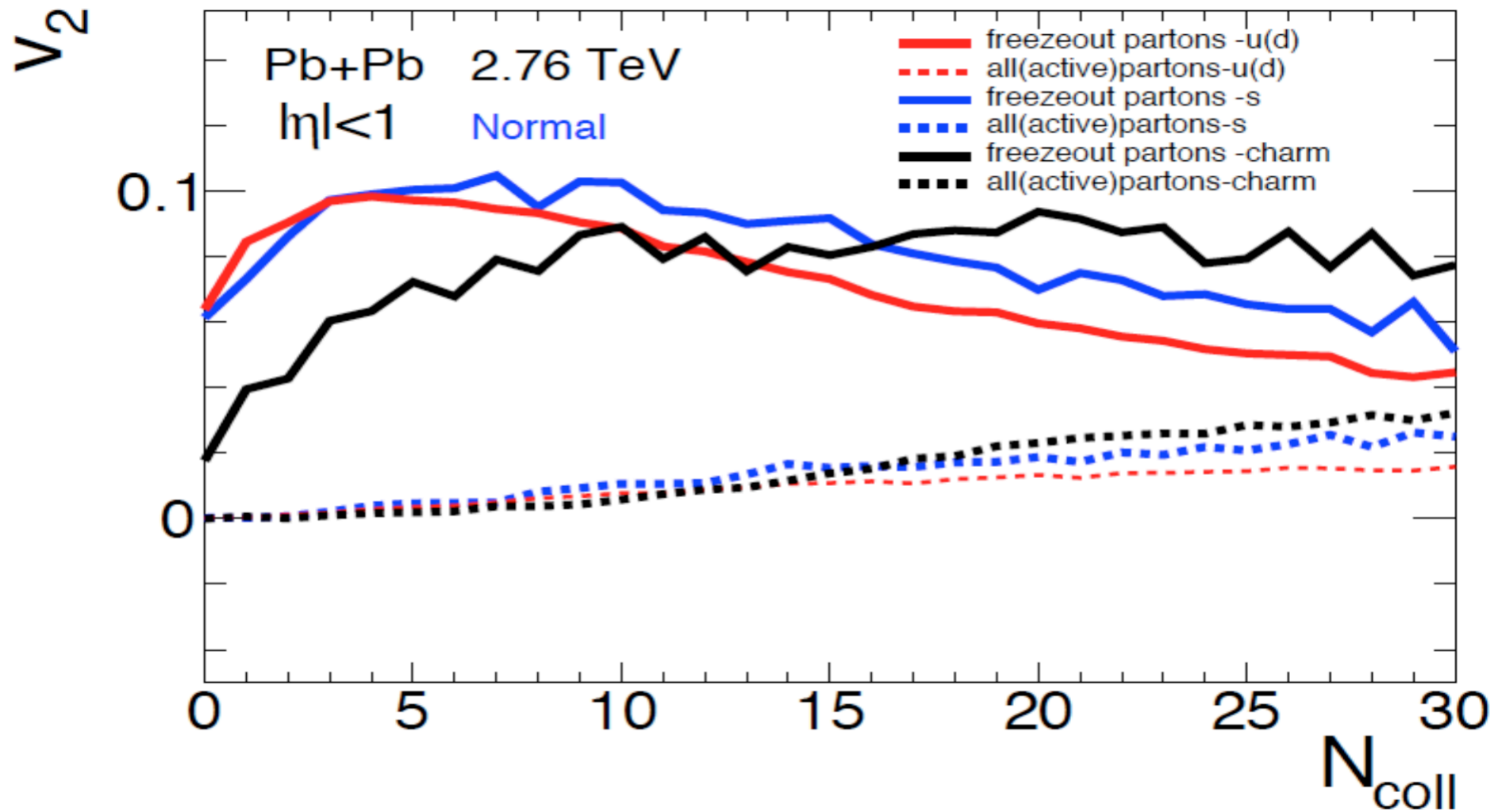
$$\begin{aligned} \frac{d\sigma_{gg}}{dt} &\simeq \frac{9\pi\alpha_s^2}{2(t - \mu^2)^2} \\ \rightarrow \sigma_{gg} &= \frac{9\pi\alpha_s^2}{2\mu^2} \frac{1}{1 + \mu^2/s} \end{aligned}$$

3mb cross section is used
since it reproduces $\pi/K/p$ $v_2(P_T)$

ZWL, PRC 90 (2014)

G.L. Ma & ZWL, PRC 93 (2016)

The escape mechanism: flavour dependence



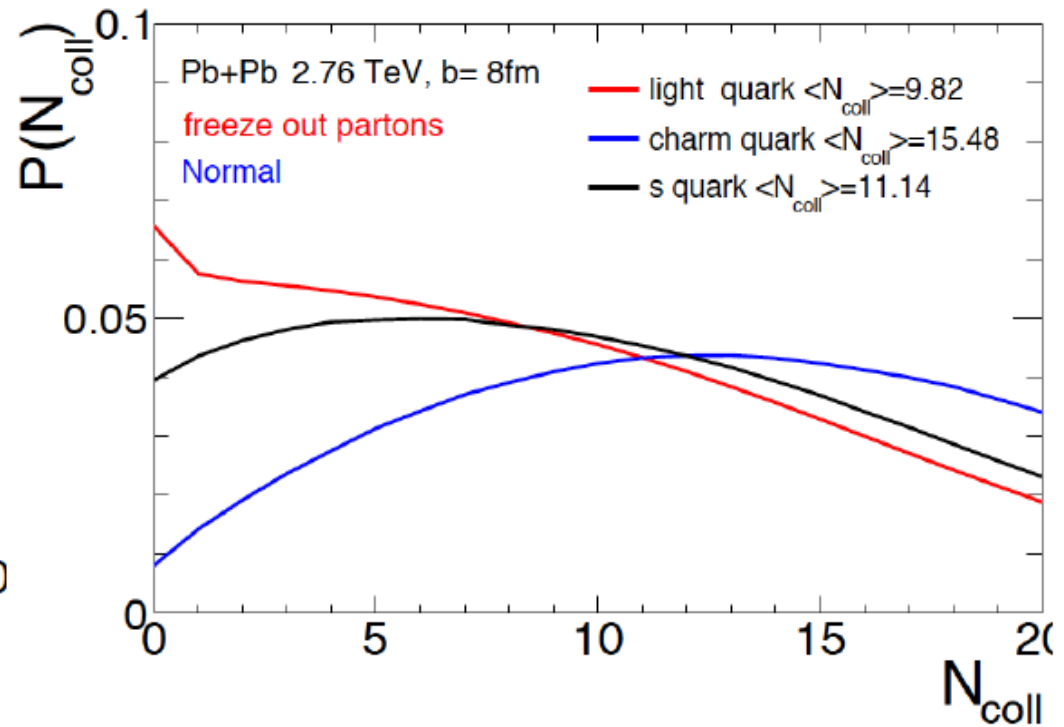
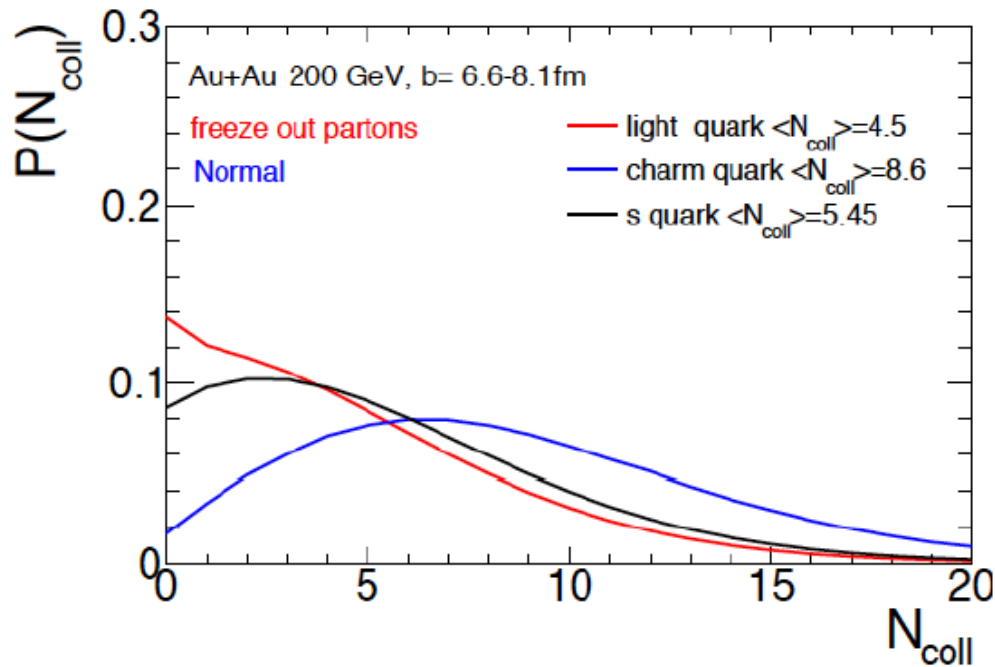
Pb+Pb
 2.76TeV
 8fm

Mass ordering in $v_2(N_{\text{coll}})$:

$v_{2c} < v_{2s} < v_{2ud}$
 reversed

at small N_{coll} ,
 at large N_{coll} .

The escape mechanism: flavour dependence



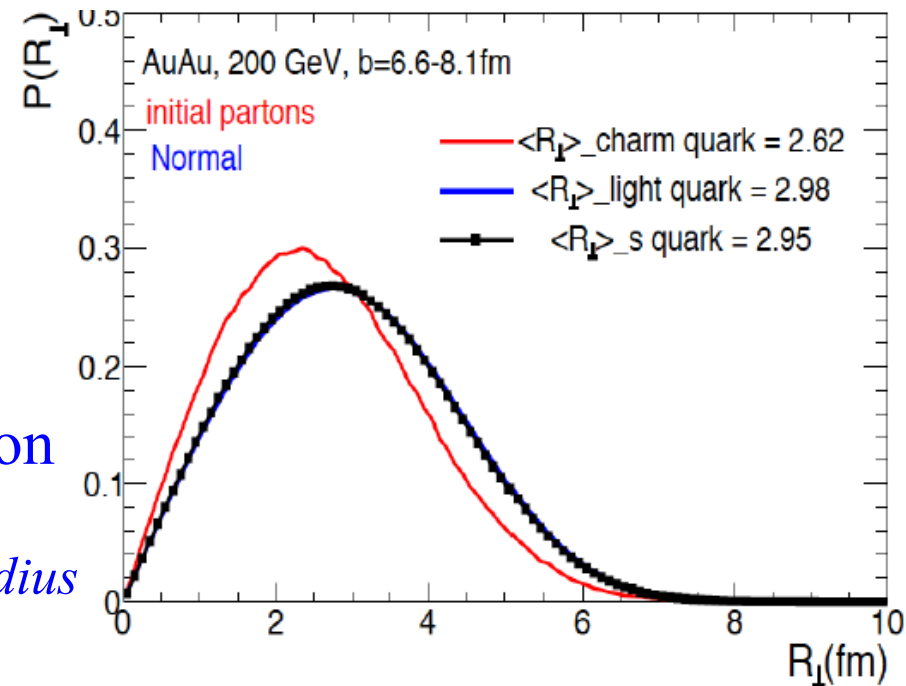
Mass ordering in the N_{coll} distribution

for all 3 systems:

$$\langle N_{\text{coll}} \rangle_c > \langle N_{\text{coll}} \rangle_s > \langle N_{\text{coll}} \rangle_{ud}$$

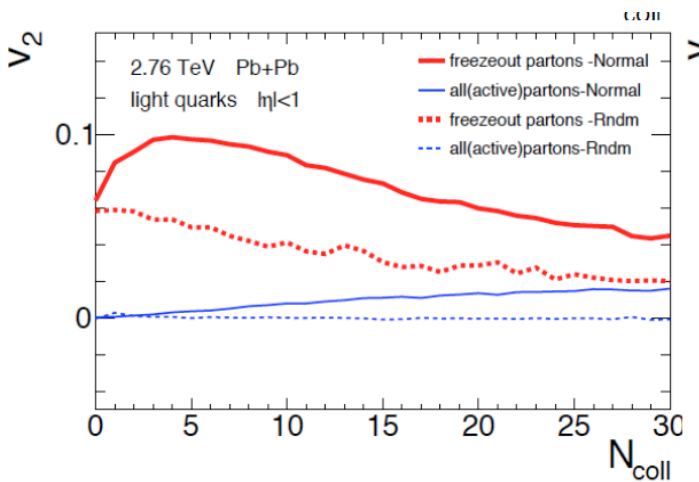
Related to the initial
(momentum &) spatial distribution

R_{\perp} : *transverse radius*

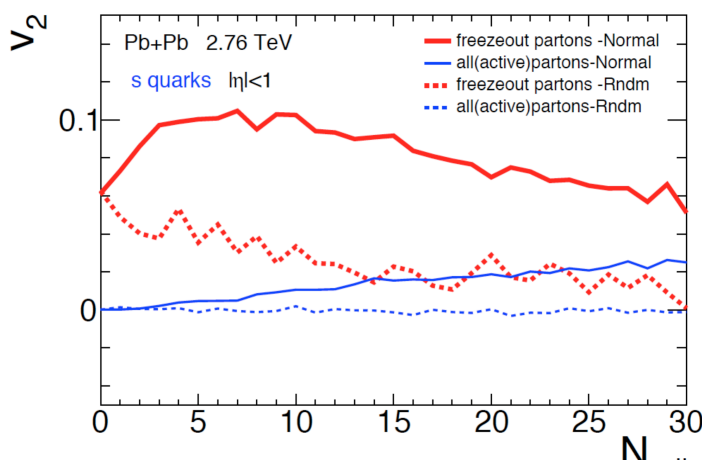


The escape mechanism: flavour dependence

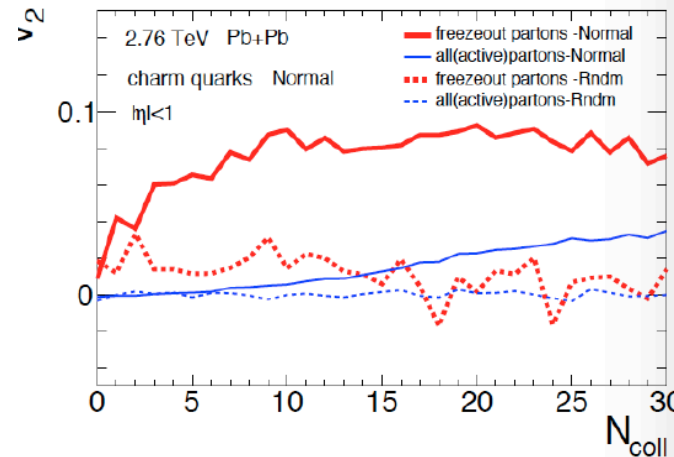
u/d



s



c



Pb+Pb
2.76TeV
8fm

Random- ϕ (for all quarks) test:
greater reduction of v_2 for heavier quarks.

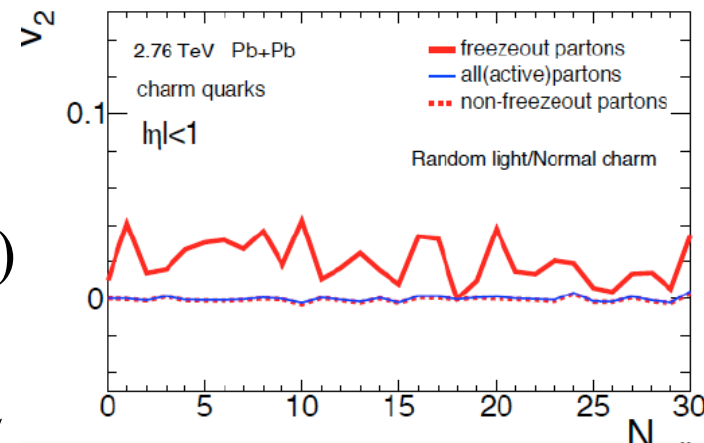
Random- ϕ for light quarks only

(Normal charm: they keep their collective flow):

large reduction of charm v_2 (like the random- ϕ test)



light quark collective flow is essential for charm v_2

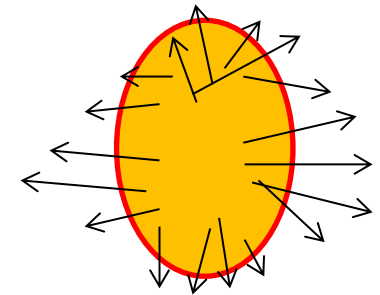
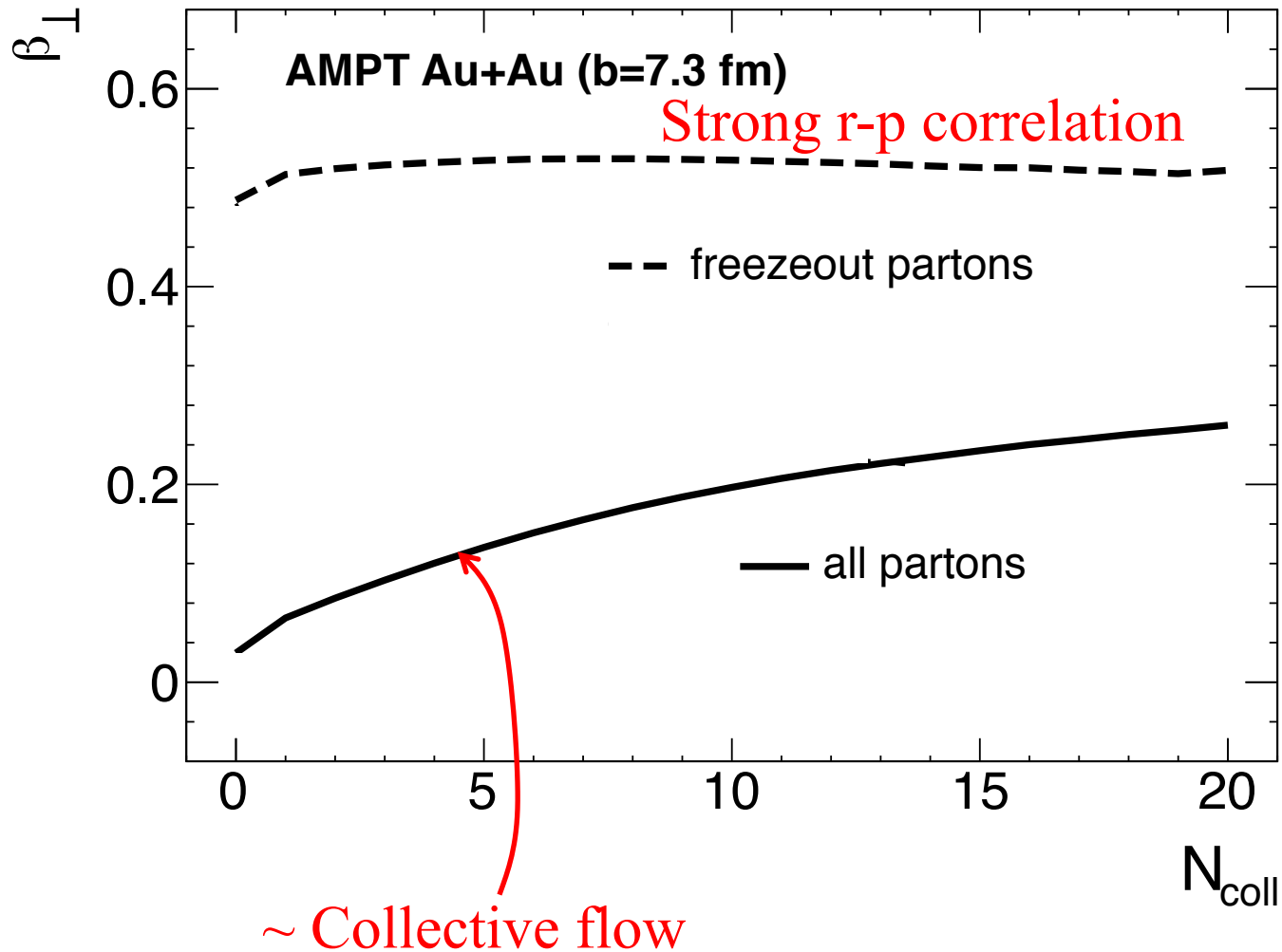


The escape mechanism: flavour dependence

Space-momentum correlation:
~ transverse flow velocity

$$\beta_{\perp} = \left\langle \frac{\vec{r}_{\perp} \cdot \vec{p}}{r_{\perp} p} \right\rangle$$

He et al. PLB753 (2016)

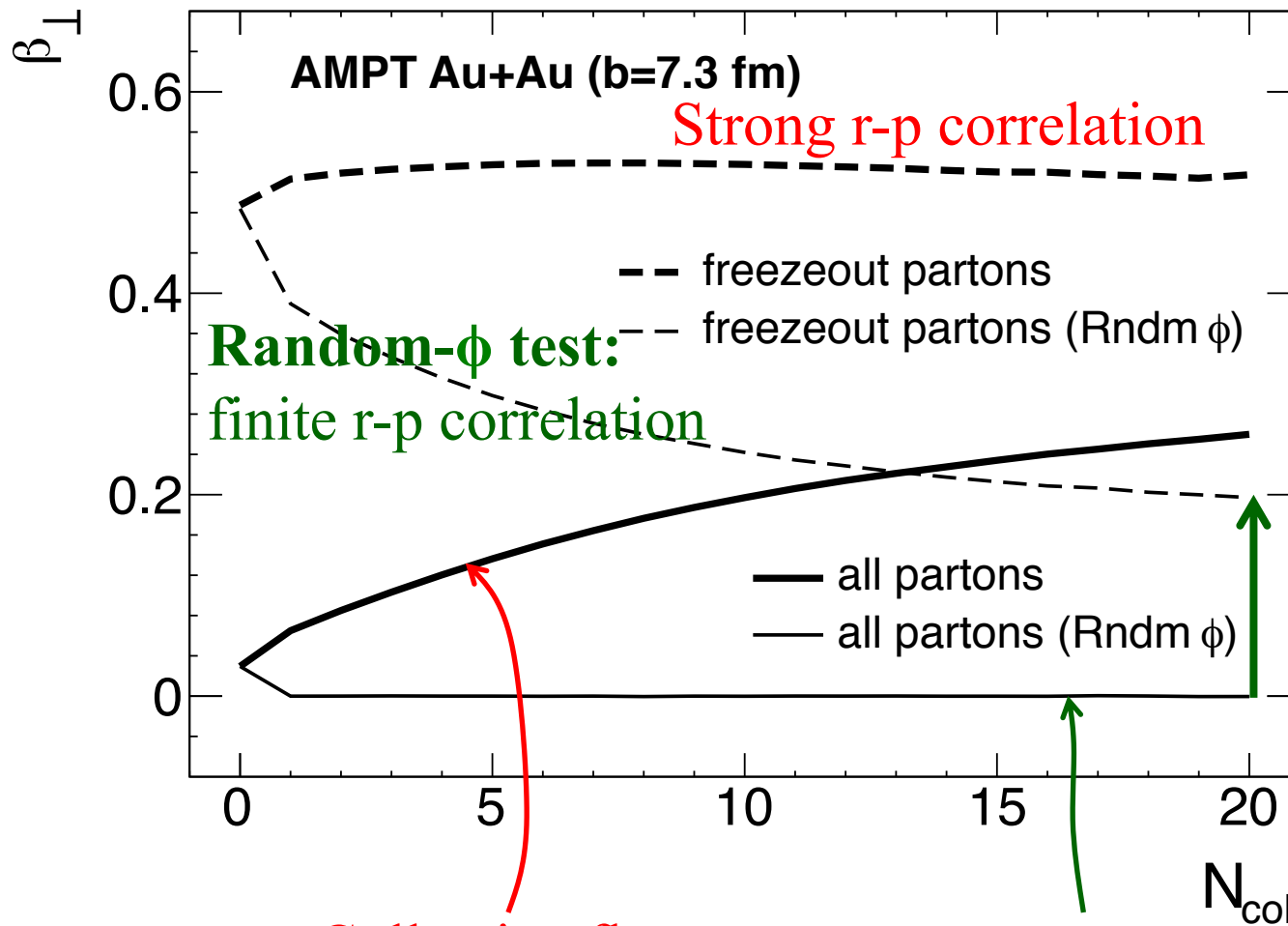


The escape mechanism: flavour dependence

Space-momentum correlation:
 \sim transverse flow velocity

$$\beta_{\perp} = \left\langle \frac{\vec{r}_{\perp} \cdot \vec{p}}{r_{\perp} p} \right\rangle$$

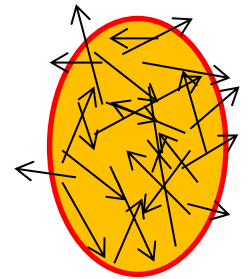
He et al. PLB753 (2016)



\sim Collective flow

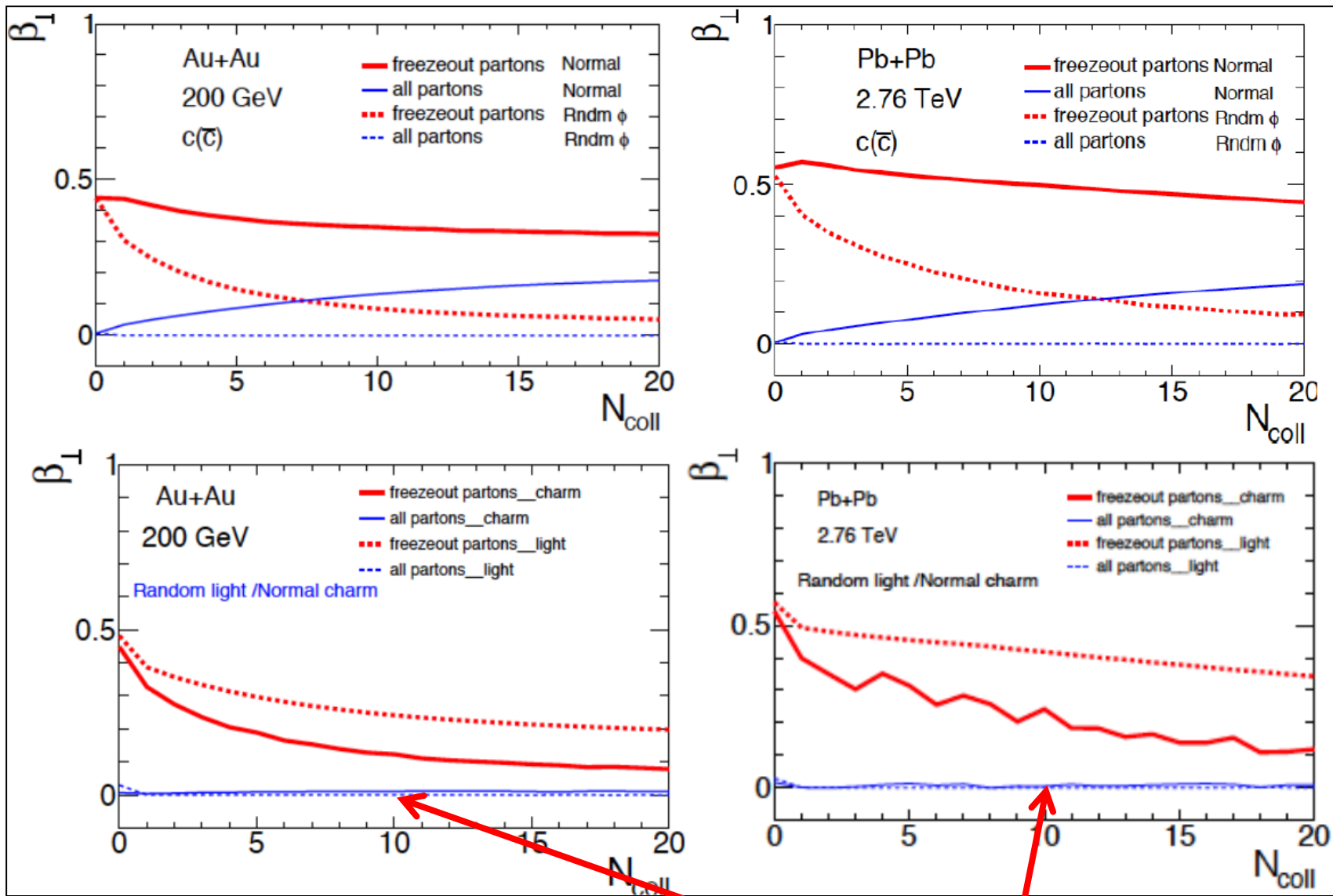
Collective flow is destroyed

r-p correlation
 purely from
 escape mechanism,
 not from collective flow



The escape mechanism: flavour dependence

Space-momentum correlation:



Random- ϕ light / Normal charm:

all partons_ charm's correlation ~ 0 :

➔ charm cannot “flow” without light quark flow

(although charm still interacts a lot with random- ϕ light quarks).

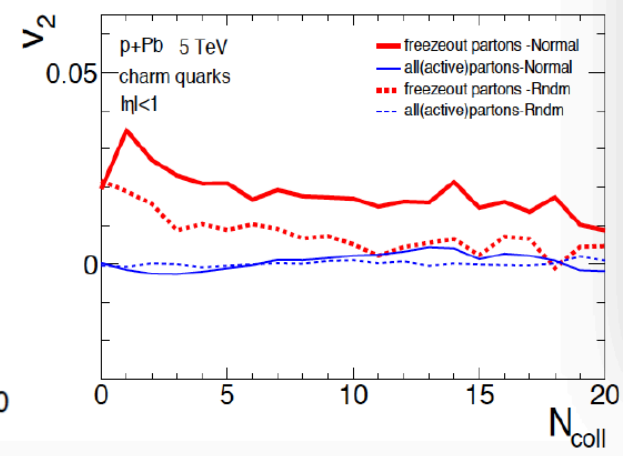
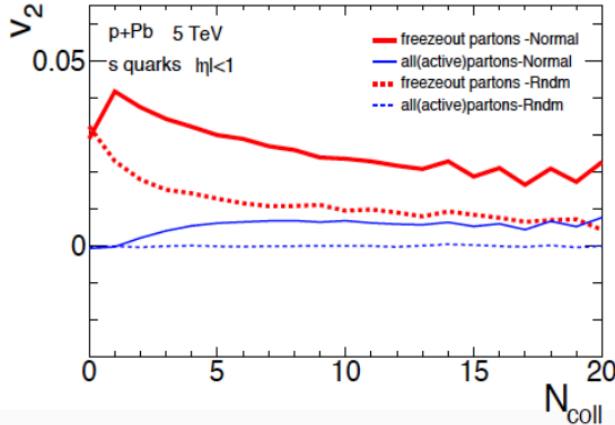
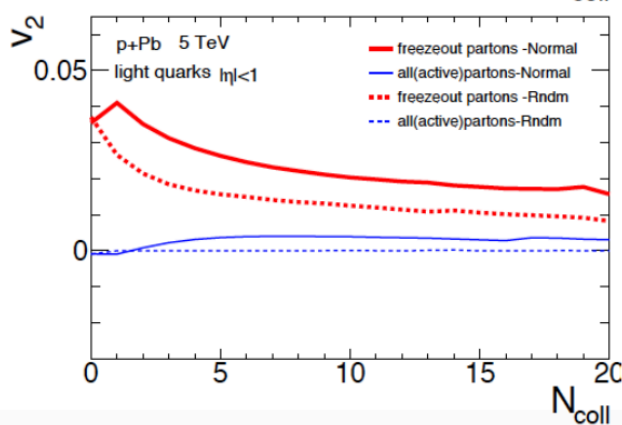
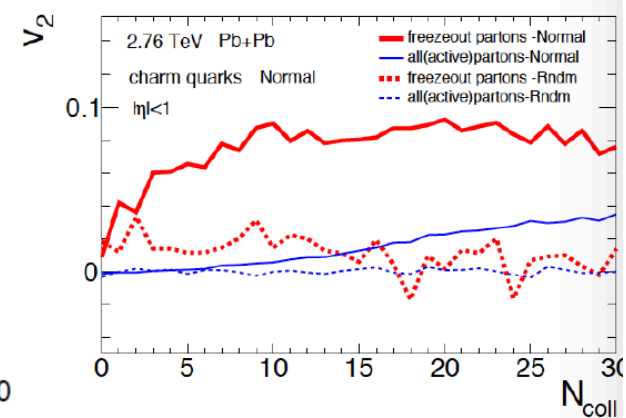
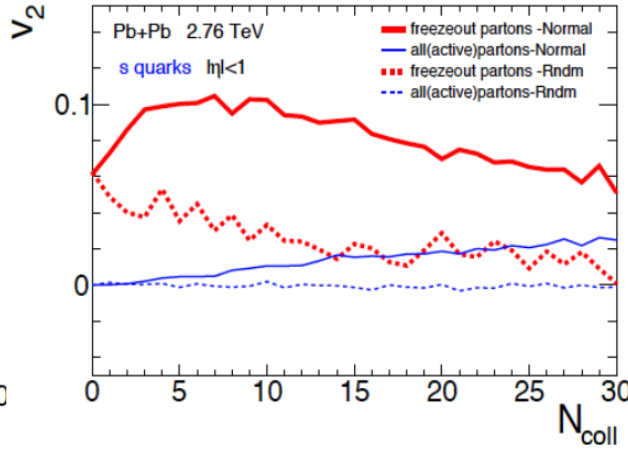
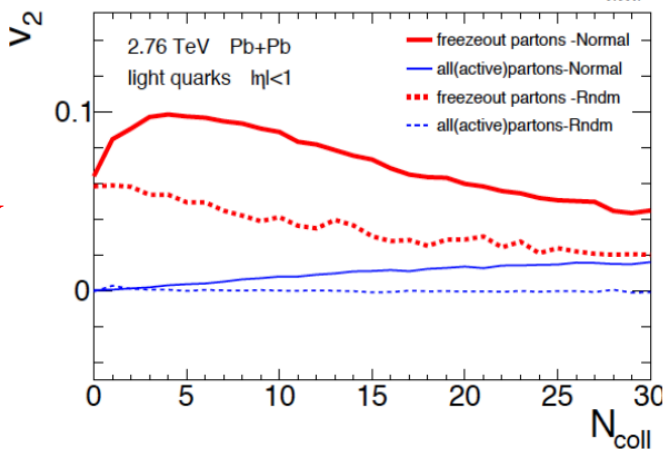
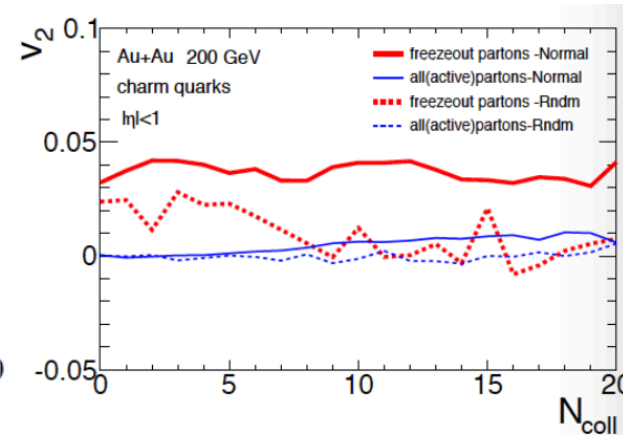
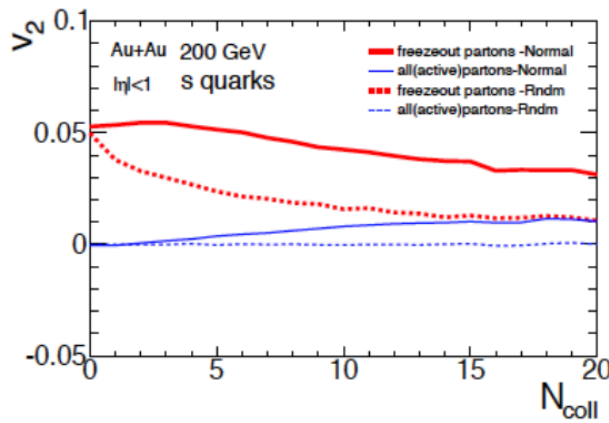
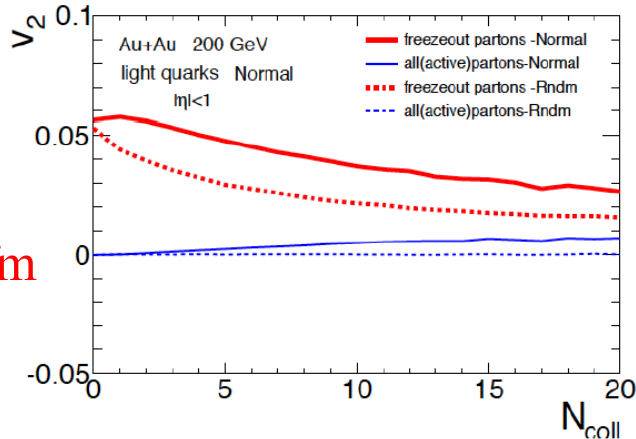
The escape mechanism: flavour dependence

Analysis is done for 3 systems:

u/d

s

c

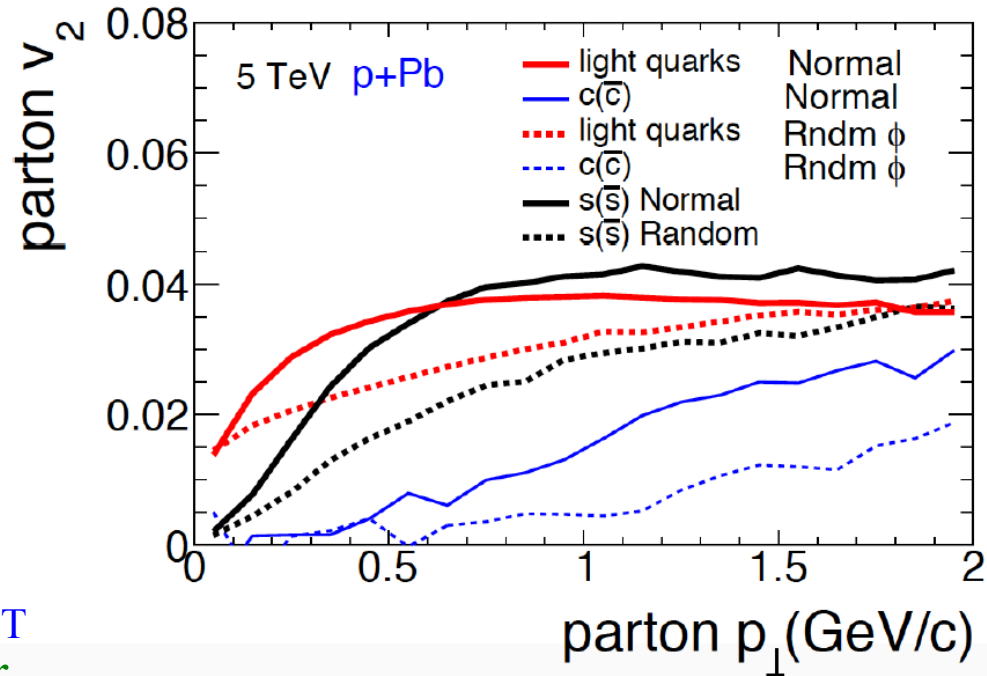
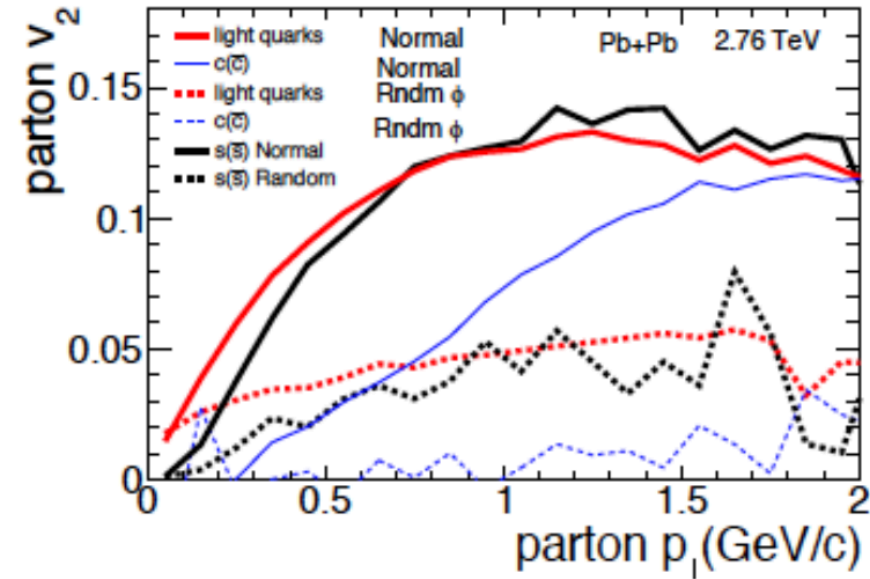
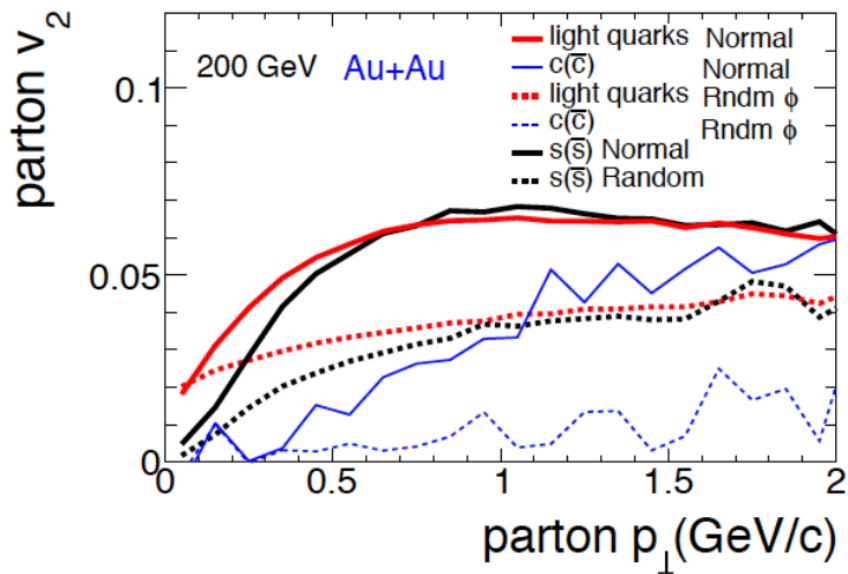


Au+Au
200GeV
b:6.6-8.1 fm

Pb+Pb
2.76TeV
8fm

p+Pb
5TeV
0fm

The escape mechanism: flavour dependence



$v_2(P_T)$:
 mass ordering at low P_T
 this is partly responsible for
 the mass ordering of hadron v_2

The escape mechanism: flavour dependence

No pt cut	pPb b=0fm	AuAu b=6.6-8.1fm	PbPb b=8fm
light	$\langle N_{\text{coll}} \rangle = 2.02$ $\langle v_2 \rangle_{\text{Rndm}} = 2.392\%$ $\langle v_2 \rangle_{\text{Norm}} = 3.279\%$ $\langle v_2 \rangle_{\text{Rndm}} / \langle v_2 \rangle_{\text{Norm}} = \mathbf{72.9\%}$	$\langle N_{\text{coll}} \rangle = 4.5$ $\langle v_2 \rangle_{\text{Rndm}} = 2.931\%$ $\langle v_2 \rangle_{\text{Norm}} = 4.468\%$ $\langle v_2 \rangle_{\text{Rndm}} / \langle v_2 \rangle_{\text{Norm}} = \mathbf{65.6\%}$	$\langle N_{\text{coll}} \rangle = 9.82$ $\langle v_2 \rangle_{\text{Rndm}} = 3.214\%$ $\langle v_2 \rangle_{\text{Norm}} = 7.562\%$ $\langle v_2 \rangle_{\text{Rndm}} / \langle v_2 \rangle_{\text{Norm}} = \mathbf{42.5\%}$
s-quark	$\langle N_{\text{coll}} \rangle = 2.54$ $\langle v_2 \rangle_{\text{Rndm}} = 1.894\%$ $\langle v_2 \rangle_{\text{Norm}} = 3.203\%$ $\langle v_2 \rangle_{\text{Rndm}} / \langle v_2 \rangle_{\text{Norm}} = \mathbf{59.1\%}$	$\langle N_{\text{coll}} \rangle = 5.45$ $\langle v_2 \rangle_{\text{Rndm}} = 2.266\%$ $\langle v_2 \rangle_{\text{Norm}} = 4.784\%$ $\langle v_2 \rangle_{\text{Rndm}} / \langle v_2 \rangle_{\text{Norm}} = \mathbf{47.4\%}$	$\langle N_{\text{coll}} \rangle = 11.14$ $\langle v_2 \rangle_{\text{Rndm}} = 2.23\%$ $\langle v_2 \rangle_{\text{Norm}} = 8.424\%$ $\langle v_2 \rangle_{\text{Rndm}} / \langle v_2 \rangle_{\text{Norm}} = \mathbf{26.5\%}$
c-quark	$\langle N_{\text{coll}} \rangle = 4.23$ $\langle v_2 \rangle_{\text{Rndm}} = 1.214\%$ $\langle v_2 \rangle_{\text{Norm}} = 2.139\%$ $\langle v_2 \rangle_{\text{Rndm}} / \langle v_2 \rangle_{\text{Norm}} = \mathbf{56.8\%}$	$\langle N_{\text{coll}} \rangle = 8.6$ $\langle v_2 \rangle_{\text{Rndm}} = 0.8455\%$ $\langle v_2 \rangle_{\text{Norm}} = 3.885\%$ $\langle v_2 \rangle_{\text{Rndm}} / \langle v_2 \rangle_{\text{Norm}} = \mathbf{22\%}$	$\langle N_{\text{coll}} \rangle = 15.48$ $\langle v_2 \rangle_{\text{Rndm}} = 0.6724\%$ $\langle v_2 \rangle_{\text{Norm}} = 7.923\%$ $\langle v_2 \rangle_{\text{Rndm}} / \langle v_2 \rangle_{\text{Norm}} = \mathbf{8.5\%}$

q

Q

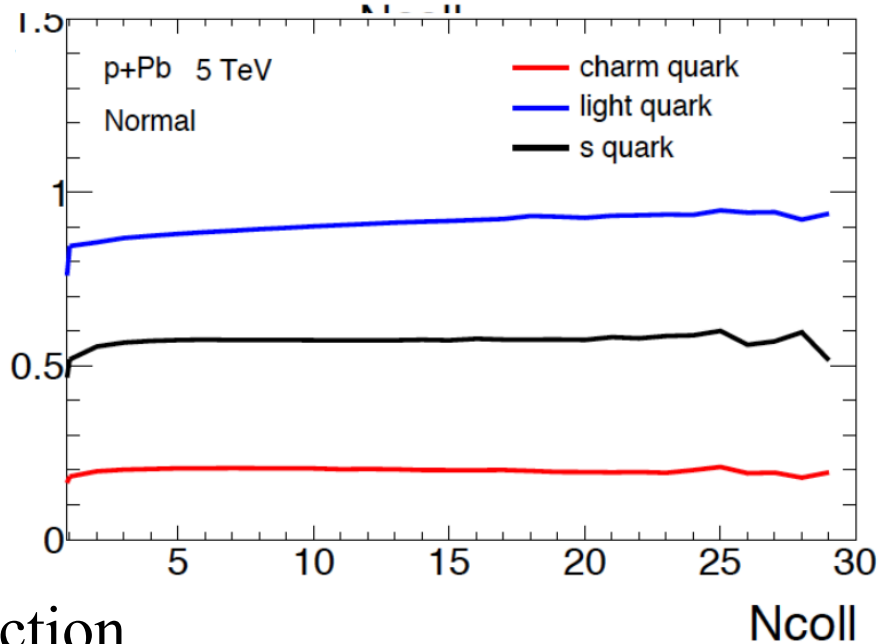
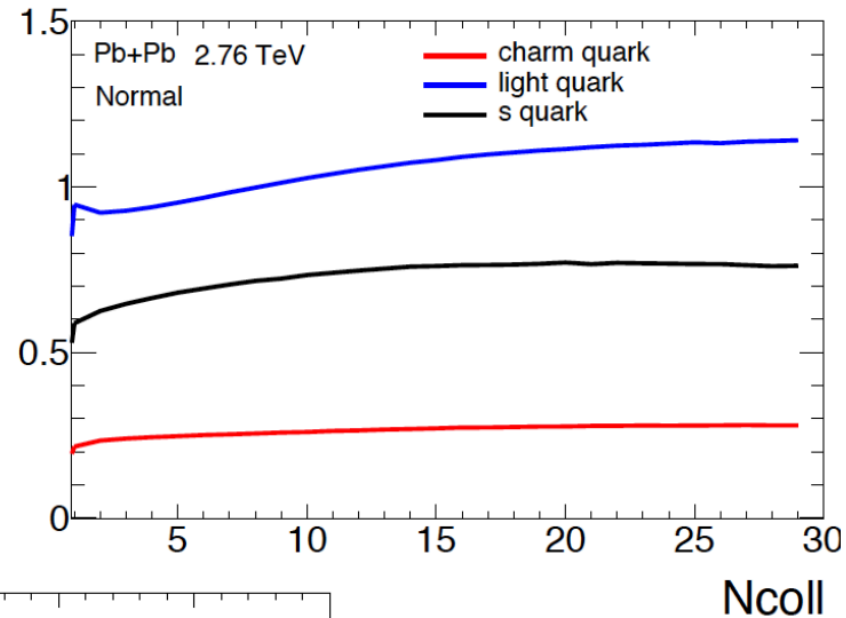
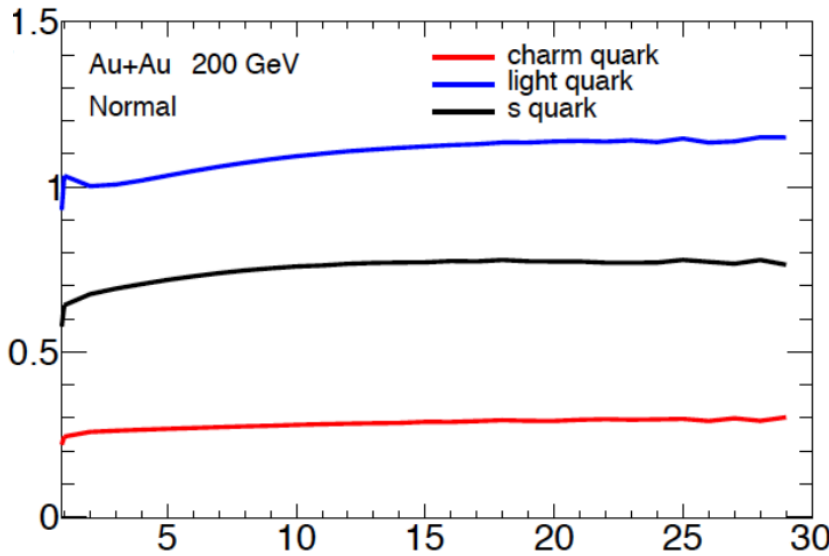
System size/energy

→ Less from escape /
more from collective flow

The escape mechanism: flavour dependence

$\Delta\phi$: change of azimuth due to one collision (the N_{coll} -th collision):

$\langle\Delta\phi\rangle$



Mass ordering on parton deflection angle: it takes more collisions to deflect a heavier quark, so light quark flow & strong light-charm interaction are essential to generate significant charm v_2 .

The escape mechanism: flavour dependence

$\langle v_2 \rangle_{\text{random-}\phi} / \langle v_2 \rangle_{\text{normal}}$ ratio
~ fraction from pure escape:

	dAu@200GeV b=0 fm	pPb@5TeV b=0 fm	AuAu@200GeV b=6.6-8.1 fm	PbPb@2.76TeV b=8 fm
u/d	93%(all quarks)	72.9%	65.6%	42.5%
s		59.1%	47.4%	26.5%
c		56.8%	21.8%	8.5%

v_2 of charm quarks in AuAu@RHIC-200GeV & PbPb@LHC:

mostly comes from collective flow (not the escape mechanism).

→ heavy quarks are more sensitive probes of collective flow & the medium.

Esha, Md. Nasim & Huang, JPG44 (2017)

v_2 of light quarks:

escape mechanism is more important for AuAu@RHIC, pPb@LHC
and smaller/lower-energy systems;

hydro-type collective flow is more important for PbPb@LHC

although with significant contribution from the escape mechanism.

Future heavy flavour work with AMPT

Up-to-date proton parton distribution function & nuclear shadowing
needed for heavy flavors and high- P_T

ongoing with L. Zheng, S.S. Shi, C. Zhang at CCNU

Include gluons & inelastic parton interactions

- Include gluons in string melting initial condition
in addition to quarks/antiquarks *planned*
- Include 2-2 inelastic parton reactions:
 $gg \leftrightarrow s\bar{s} / c\bar{c}, qq\bar{q} \leftrightarrow s\bar{s} / c\bar{c}, \dots$ *ongoing*
- Include gluons in a coalescence/recombination model
with energy momentum conservation *planned*

For high P_T :

- Parton radiative energy loss *planned*

Summary

AMPT aims to serve as a comprehensive transport model for heavy ion collisions:
event-by-event from initial condition to final observables;
include particle productions and interactions at different y & P_T ;
conserve energy/momentum/flavour/**charge (ongoing work)** of each event;
keep non-equilibrium dynamics & intrinsic fluctuations/correlations.

We have followed the complete parton collision history to study
 v_2 of light/strange/charm quarks in AMPT:

v_2 of charm quarks in AuAu@200GeV & PbPb@2.76TeV
mostly comes from collective flow (not the escape mechanism),
indicating that heavy quarks are more sensitive probes of the medium.

v_2 of light quarks at AuAu@200GeV & pPb@LHC

come mostly from the escape mechanism,

but at PbPb@2.76TeV comes more from collective flow

(although still with significant fraction from the escape mechanism).

We are working to improve AMPT on heavy flavours,
to simultaneously study light flavours, heavy flavours including their interactions.