

# QUARKONIUM PRODUCTION IN PROTON-PROTON AND PROTON-NUCLEUS COLLISIONS

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and Heavy Quarks

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# Part I

## Introduction

# Approaches to Quarkonium Production

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  - 3 COLOUR OCTET MECHANISM (encapsulated in NRQCD): higher Fock states of the mesons taken into account;  $Q\bar{Q}$  can be produced in octet states with different quantum # as the meson

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## 3 COLOUR OCTET MECHANISM

- one non-perturbative parameter per Fock States
- expansion in  $v^2$ ; series can be truncated
- the phenomenology partly depends on this
- HQSS relates some non-perturbative parameters to each others and to a specific quarkonium polarisation

## Part II

# Impact of QCD corrections to the C(S,E,O)M

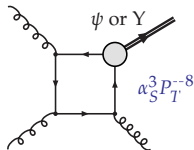
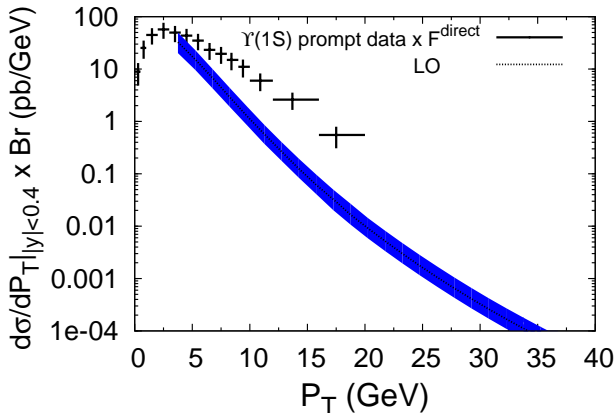
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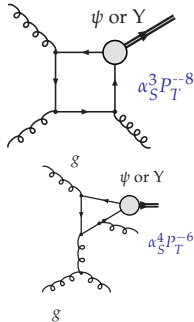
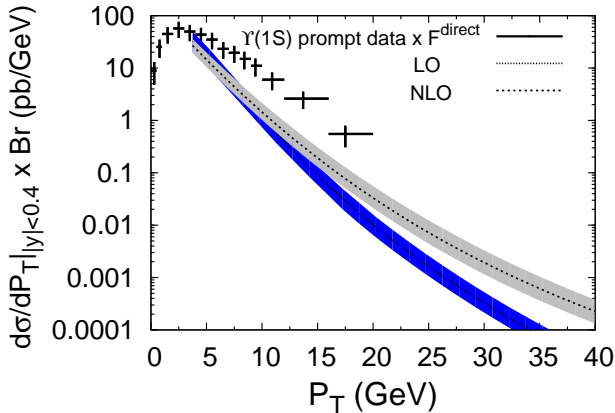


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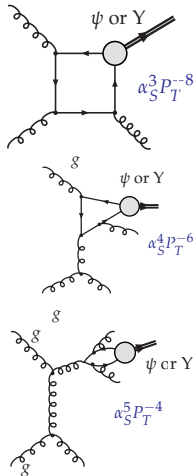
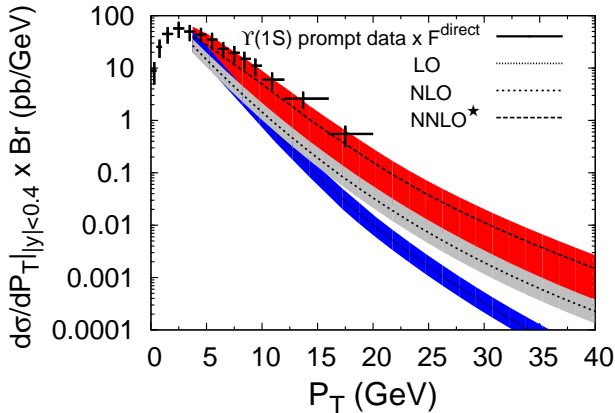


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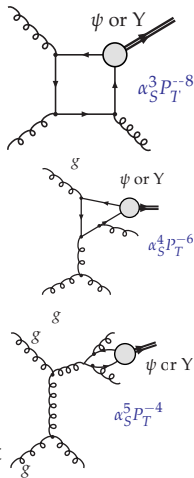
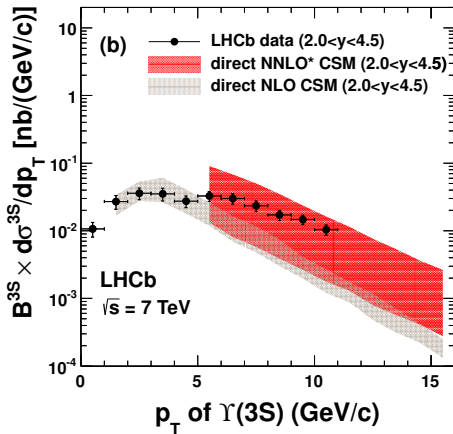
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+ double  $t$ -channel gluon exchange at  $\alpha_S^5$   
 Attention: the NNLO\* is not a complete NNLO

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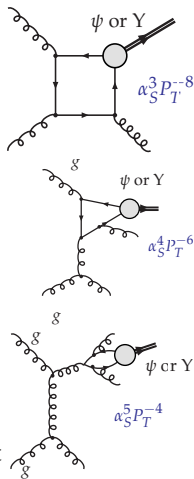
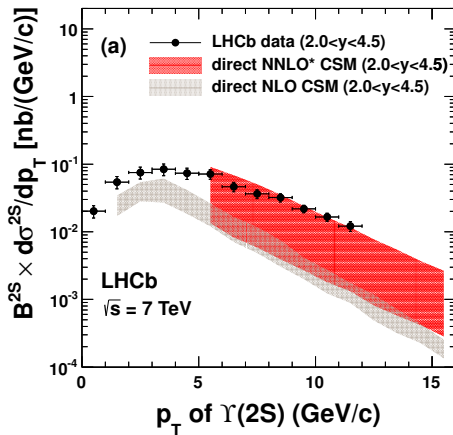
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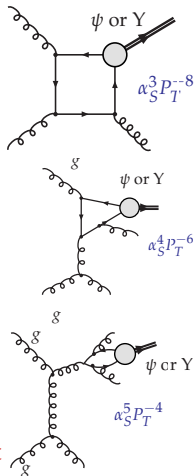
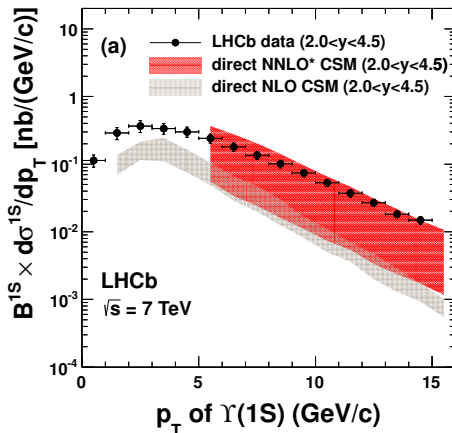
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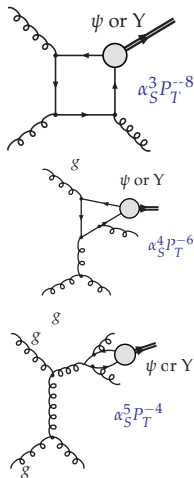
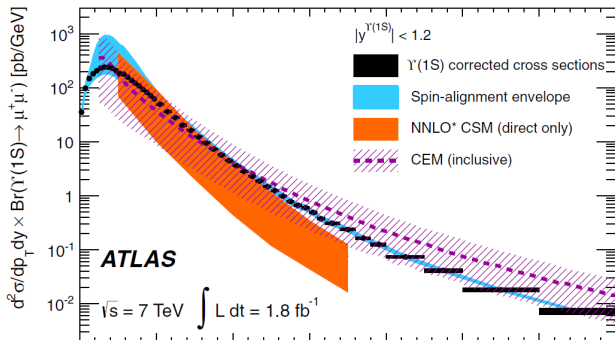
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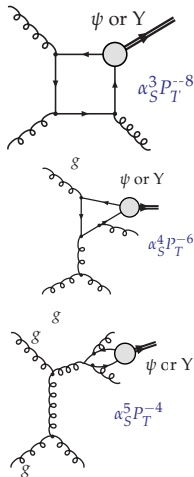
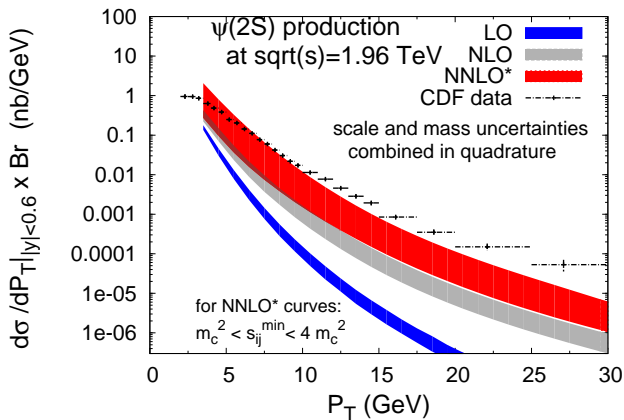
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 ATLAS PRD 87 052004



CSM theory curve extrapolated to prompt:  $\times 2$

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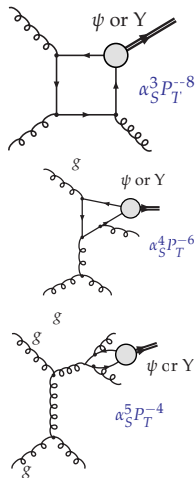
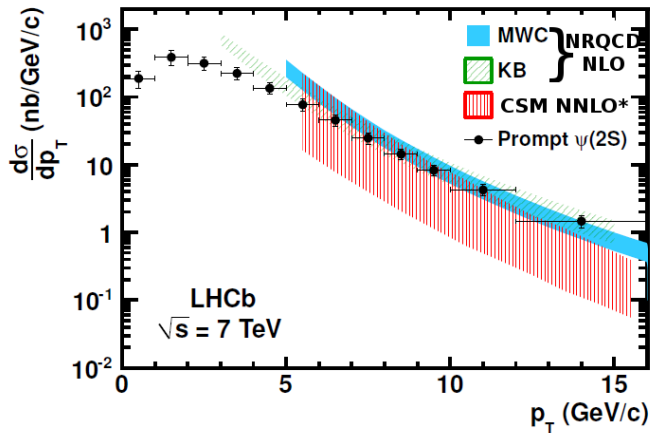


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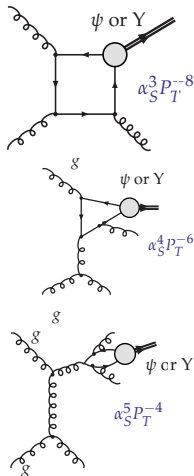
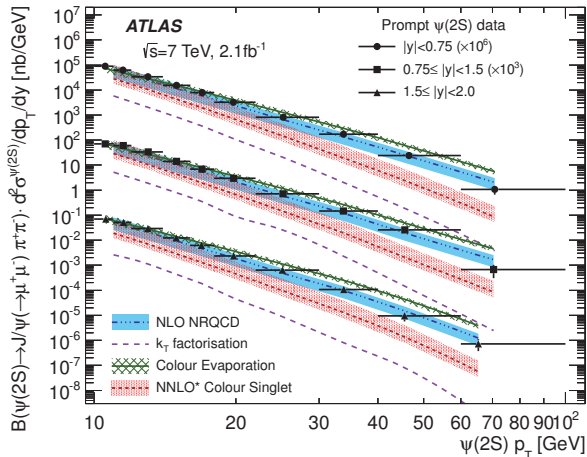


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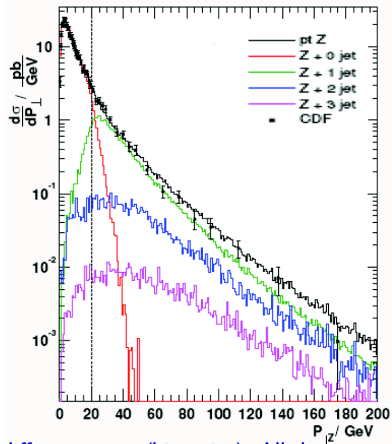
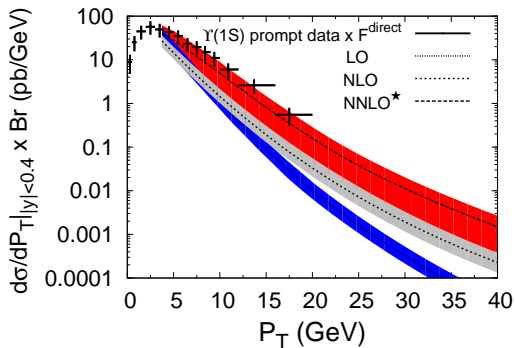
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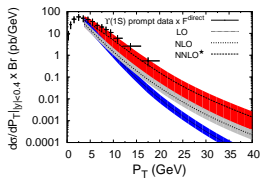
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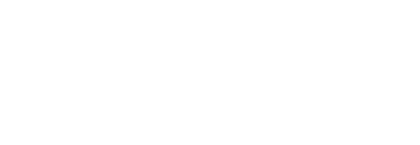
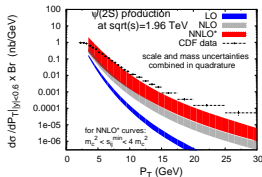
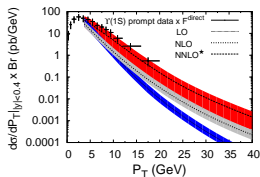
# Analogy with the $P_T$ spectrum for the $Z^0$ boson



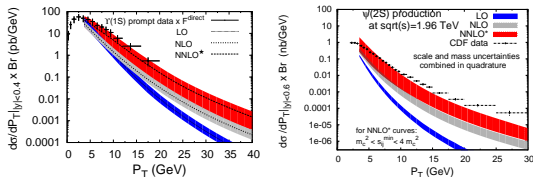
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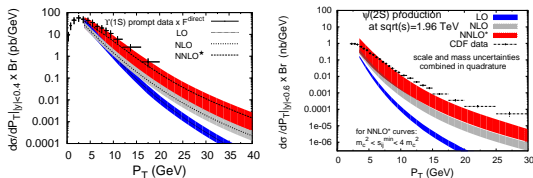
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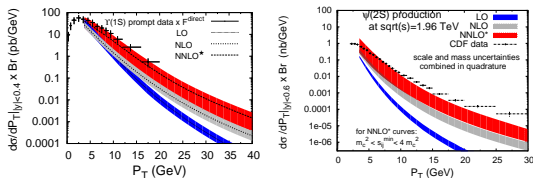
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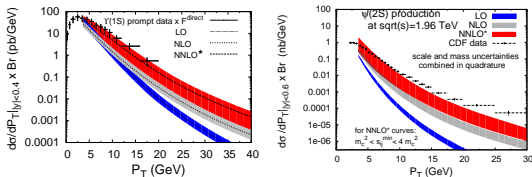
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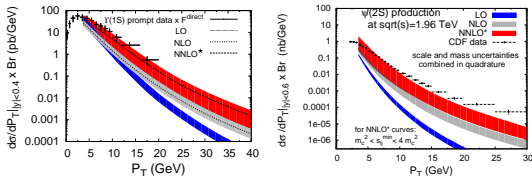
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**constraints** on  $^1S_0^{[8]}$  (&  $^3P_J^{[8]}$ ):  $e^+e^-$ , low  $P_T$   $pp$  and  $\eta_c$

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$k_T$  fact.  $\leftrightarrow$  NNLO Collinear fact. ?

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$\psi$  data: a little less hard than the blue curve

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- Tend to overshoot the  $\psi$  data at large  $P_T$

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- Since the 3 associated LDMEs are fit, the combination at NLO overall still describes the data; hence an **apparent stability** of NRQCD x-section at NLO
- What significantly changes is the size of the LDMEs



## 2 COLOUR EVAPORATION MODEL

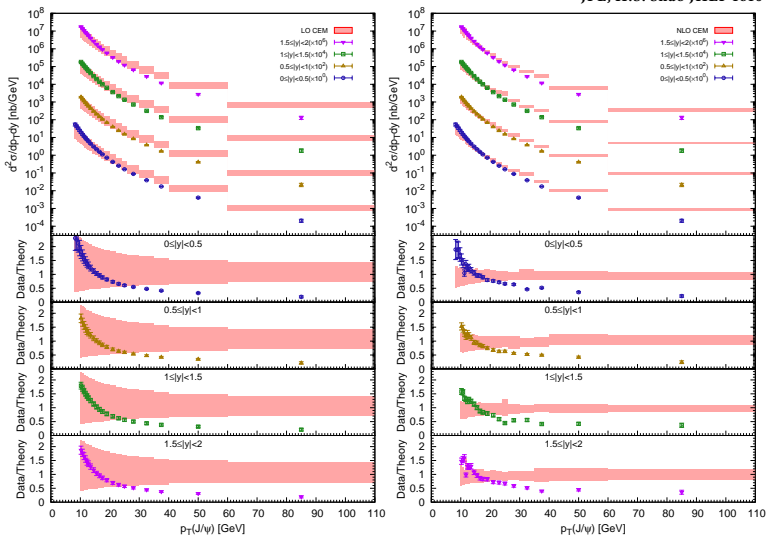
- All possible spin and colour combinations contribute
- By definition, the hardest ones (gluon fragment.  $\sim {}^3S_1^{[8]}$ ) dominant at large  $P_T$
- No reason for a change at NLO. The fit can yield another CEM parameter value but this will not modify the  $P_T$  spectrum

Confirmed by the first NLO study: JPL, H.S. Shao JHEP 1610 (2016) 153

- Tend to overshoot the  $\psi$  data at large  $P_T$
- The (LO) ICEM not significantly better at large  $P_T$

# QCD corrections (NLO) to the CEM $P_T$ dependence

JPL, H.S. Shao JHEP 1610 (2016) 153



# The current situation in one slide ...

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- Colour-Singlet Model (CSM) back in the game

[large NLO and NNLO correction to the  $P_T$  spectrum ; but not perfect → need a full NNLO]

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→ Especially keeping in mind a couple of lessons from past quarkonium studies

- Obviously, no consensus on the quarkonium production mechanism, at high, mid and low  $P_T$

The big question: how to treat quarkonium production in  $pA$  and  $AA$  collisions ?

# Part III

## 5 lessons from the past

# Photoproduction

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e.g. H1,EPJC 25, 2,2002; ZEUS, EPJC 27, 173, 2003

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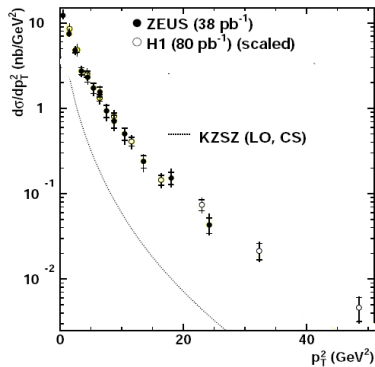
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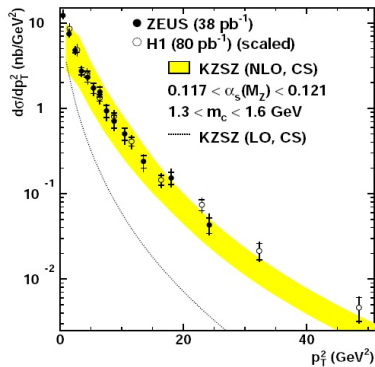
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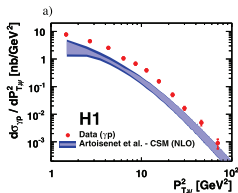
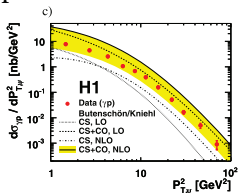
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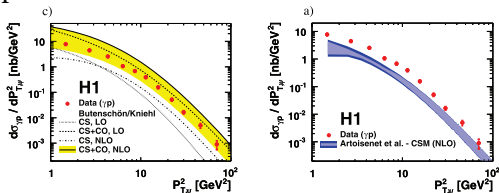
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As we say in French: "Tout ça pour ça ..."

# Photon-fusion production: from an evidence to a puzzle

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15 JULY 2002

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Michael Klasen, Bernd A. Kniehl, Luminița N. Mihaila, and Matthias Steinhauser

*II. Institut für Theoretische Physik, Universität Hamburg, Luruper Chaussee 149, 22761 Hamburg, Germany*

(Received 19 December 2001; published 28 June 2002)

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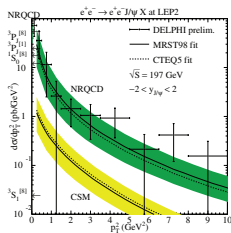
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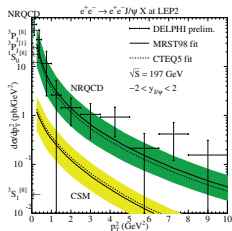
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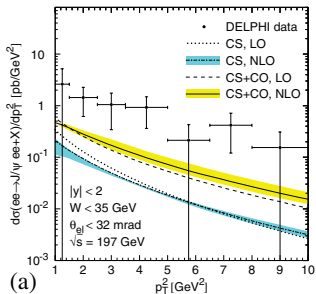
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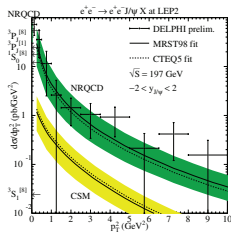
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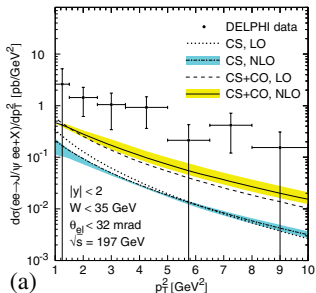
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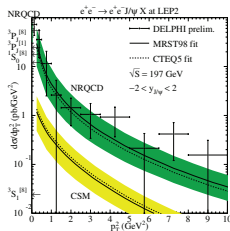
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Still an open issue ...

$J/\psi + W$

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V. D. Barger, S. Fleming and R. J. N. Phillips, *Phys. Lett. B* 371, 111 (1996)

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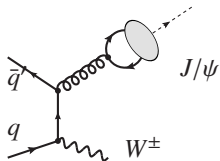
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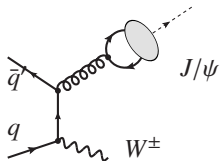
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- Usual conclusion:  
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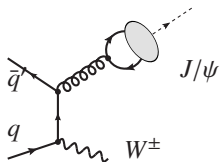
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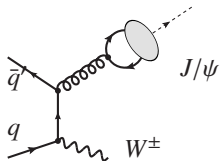
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J.P. Lansberg, C. Lorcé, PLB 7 26 (2013) 218

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- $\psi + W$  is not a clean test of CO contributions

# ”The” Smoking Gun: Polarisation

Quarkonium Working Group CERN Yellow Report, Dec. 2004, CERN-2005-005

*Despite these various diluting effects, a substantial polarization is expected at large  $p_T$ , and its detection would be a ”smoking gun” for the presence of the colour-octet production mechanism.*

*[..], it is difficult to see how there could not be substantial polarization in  $J/\psi$  or  $\psi(2S)$  production for  $p_T > 4m_c$ .”*

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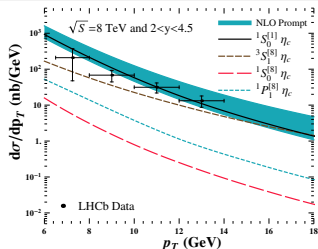
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- In about ten years, with the advent of NLO analyses, polarisation evolved from a NRQCD **smoking gun to a puzzle or a mere constraint ...**
- and this was **not anticipated** even after the NLO CSM corrections for  $\gamma p$  and  $pp$



## Part IV

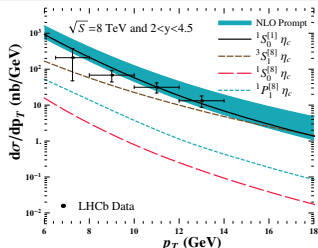
A last lesson from the (close) past:  
 $\eta_c$ : how not-so-precise data can matter much  
or  
The completely unexpected probe

# From exotic to essential



Data LHCb : EPJC 75 (2015) 311 (plot from H. Hanet *et al.* PRL 114 (2015) 092005)

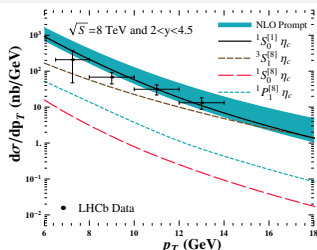
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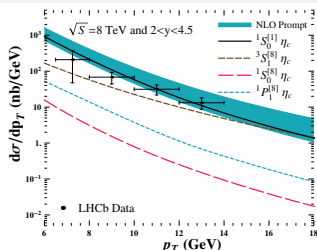
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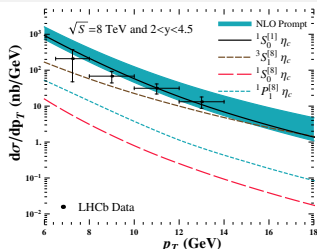


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## Part V

# Automating the computation of nuclear PDF effects

# An automated code to evaluate the impact of nuclear PDF on hard probes I

JPL, H.S. Shao *Eur.Phys.J. C77 (2017) 1*



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JPL, H.S. Shao Eur.Phys.J. C77 (2017) 1

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- Not yet interfaced to a Glauber model  
[no centrality and no combination with other nuclear effects]

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JPL, H.S. Shao *Eur.Phys.J. C77 (2017) 1*



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JPL, H.S. Shao Eur.Phys.J. C77 (2017) 1

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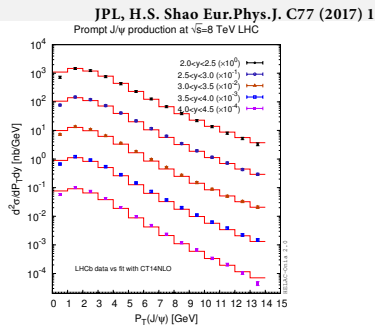
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- Last but not least: the automation of the evaluation allows one to study different nPDF sets AND the scale uncertainties: better control of the theory uncertainties

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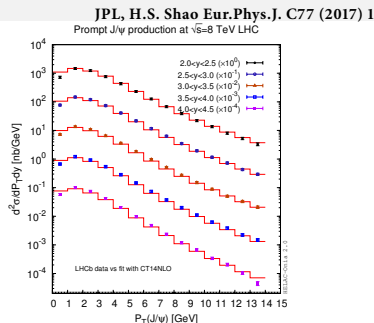
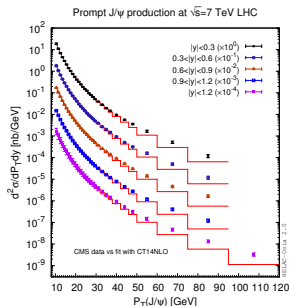
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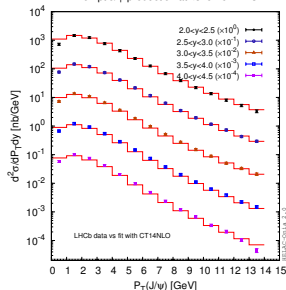


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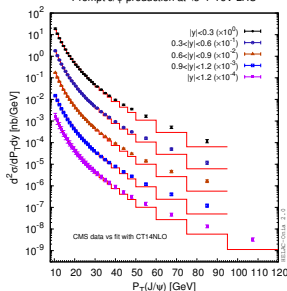
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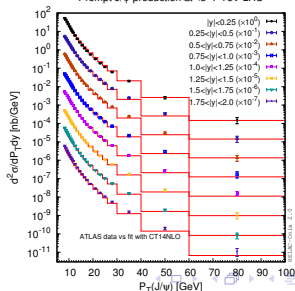
Prompt  $J/\psi$  production at  $\sqrt{s}=8$  TeV LHC



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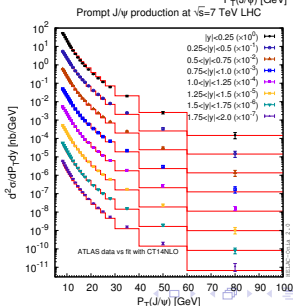
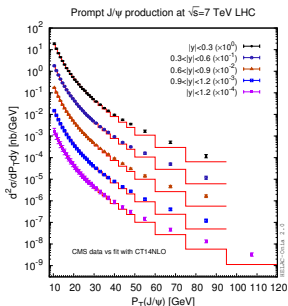
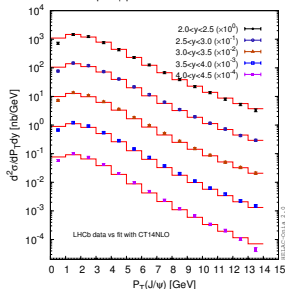




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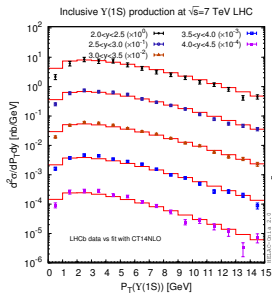


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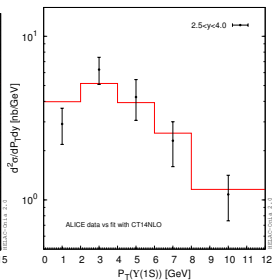
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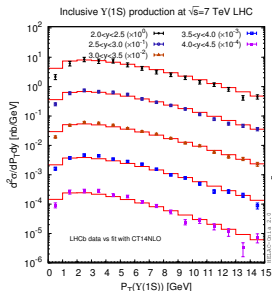


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Inclusive  $\Upsilon(1S)$  production at  $\sqrt{s}=7$  TeV LHC

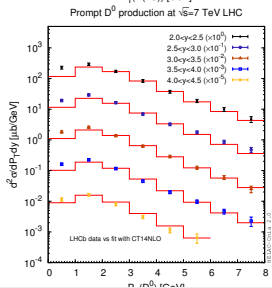
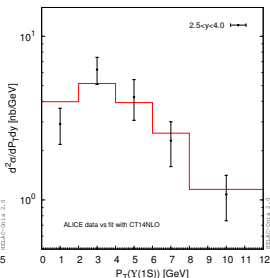


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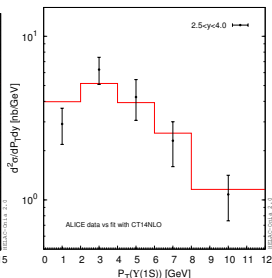
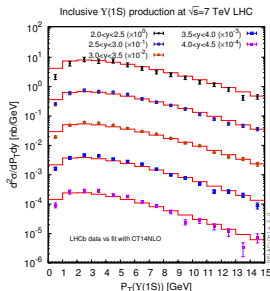


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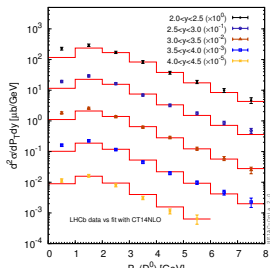
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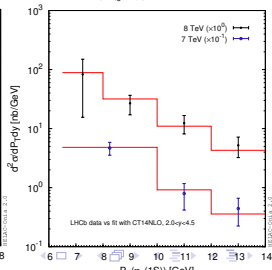
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Prompt  $D^0$  production at  $\sqrt{s}=7$  TeV LHC



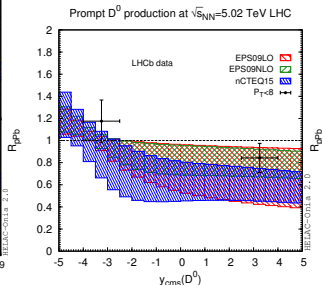
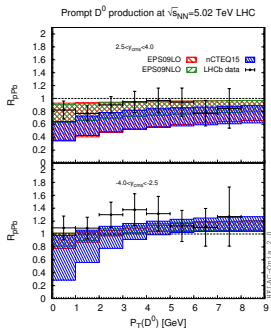
Prompt  $\eta_c(1S)$  production at the LHC



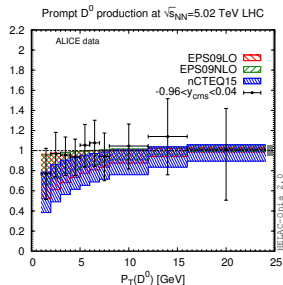
# Part VI

## Results for $pA$ collisions

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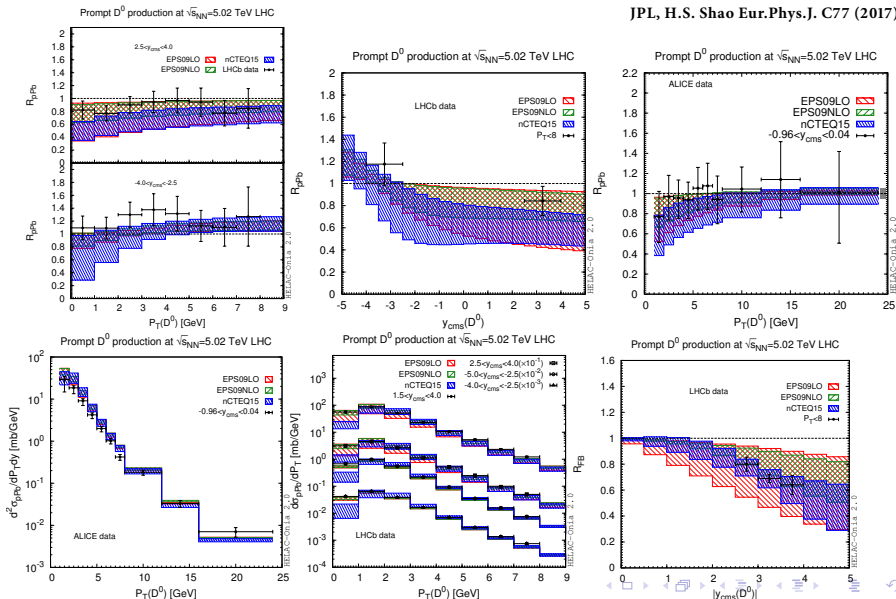


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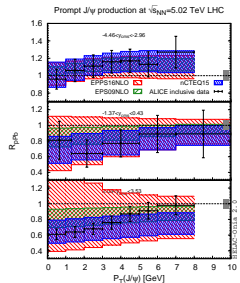
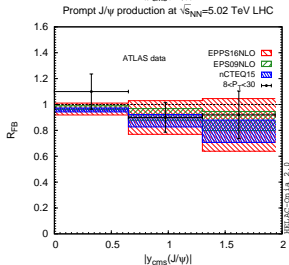
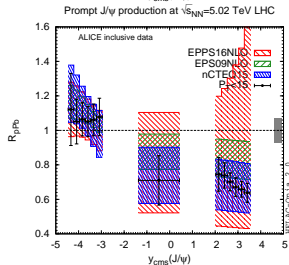
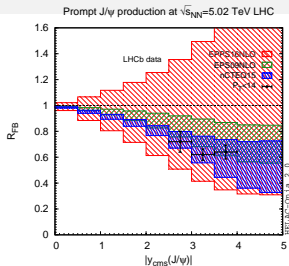
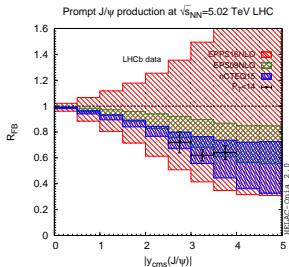
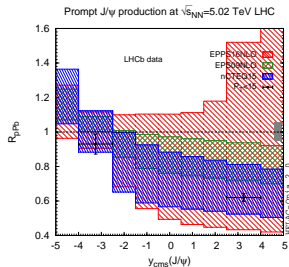
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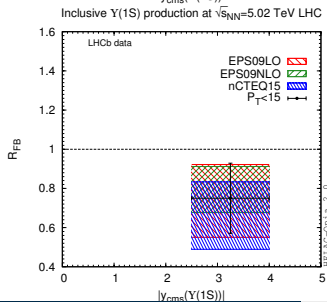
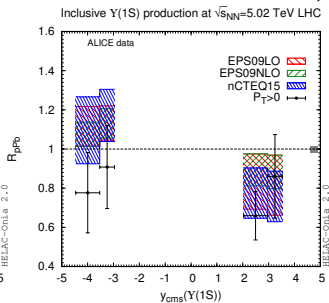
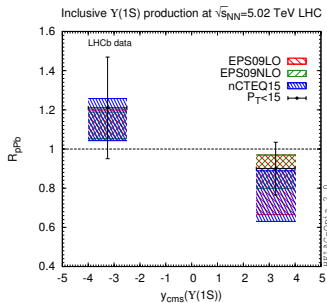


# Some $J/\psi$ comparisons (new plots with EPPS16)



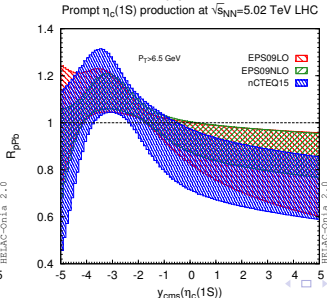
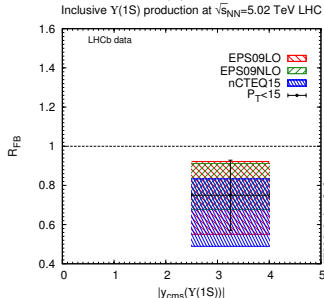
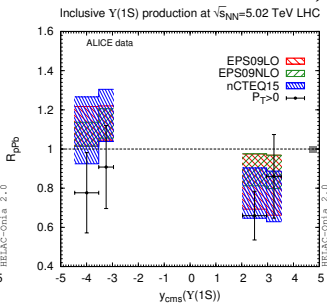
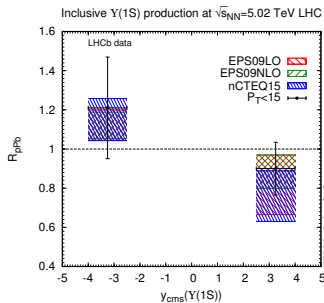
# More results: $\Upsilon(1S)$ and ... $\eta_c$

JPL, H.S. Shao Eur.Phys.J. C77 (2017) 1

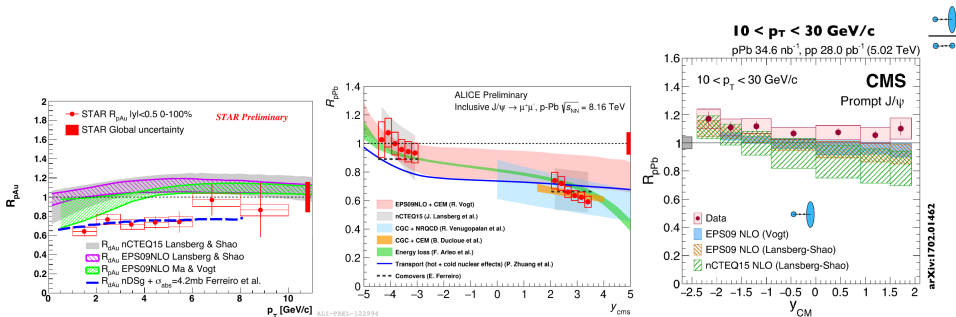


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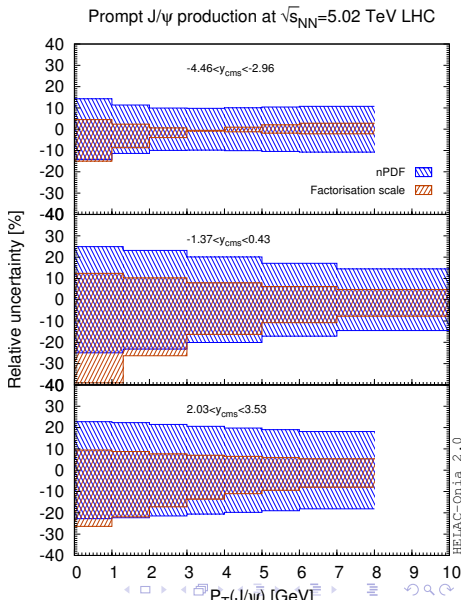
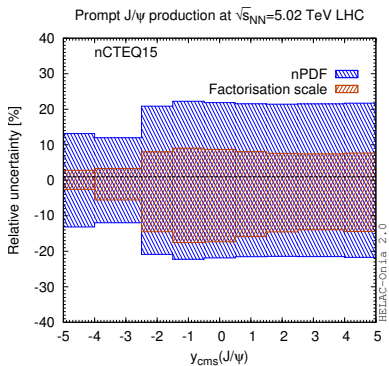


# Some recent comparisons [shown at QM2017]



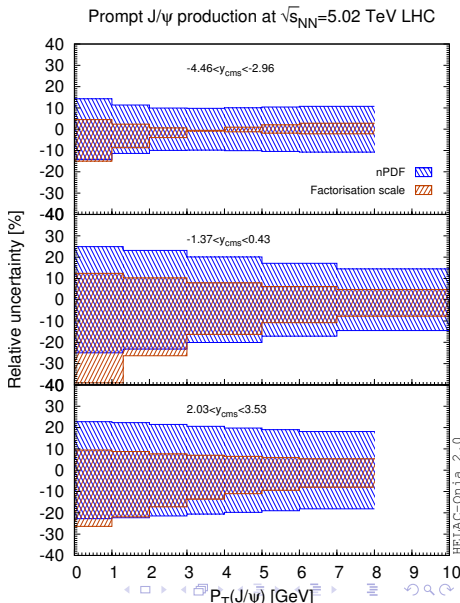
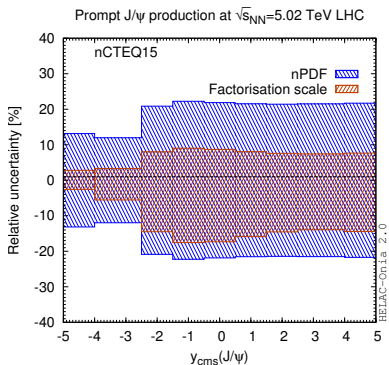
STAR: T.Todoroki; ALICE: M. Tarhini (ALICE-PUBLIC-2017-001); CMS: J. M. Blanco

# Uncertainties due to the factorisation scale



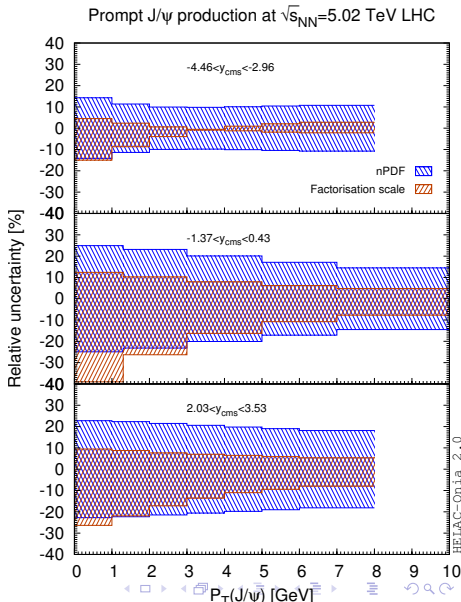
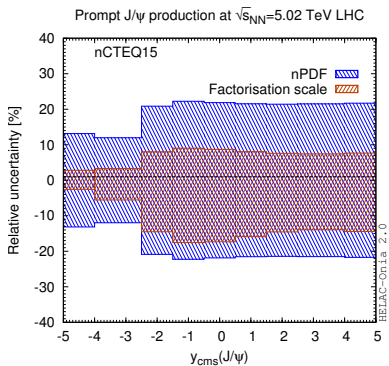
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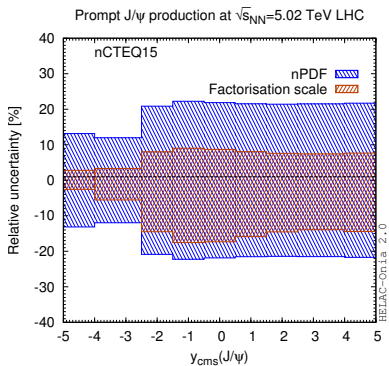
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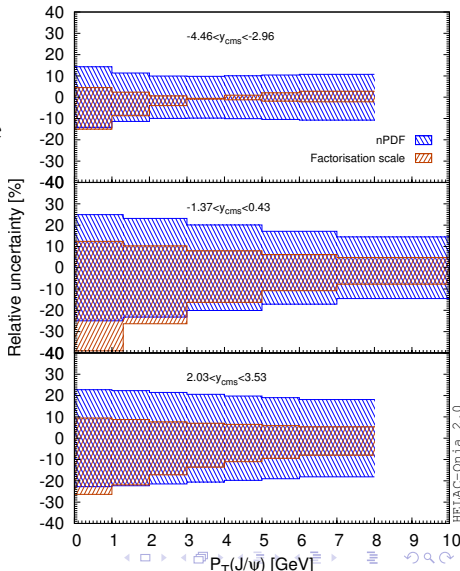


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- $\mu_F$  is on the order of  $m_T$
- The uncertainty due to  $\mu_F$  not negligible compared to the nPDF one [nCTEQ shown]



Prompt J/ $\psi$  production at  $\sqrt{s_{NN}}=5.02$  TeV LHC





## Fit step toward the inclusion of heavy-flavour data in a fit: reweighting

## REWEIGHTING FOR HESSIAN PDFS



Giele, Keller '98; Ball et al. '11; Sato, Owens, Prosper '14; Paukkunen, Zurita '14;

1. Convert Hessian error PDFs into replicas

$$f_k = f_0 + \sum_i^N \frac{f_i^{(+)} - f_i^{(-)}}{2} R_{ki},$$

2. Calculate weights for each replica

$$w_k = \frac{e^{-\frac{1}{2}\chi_k^2/T}}{\frac{1}{N_{\text{rep}}} \sum_i^{N_{\text{rep}}} e^{-\frac{1}{2}\chi_k^2/T}}, \quad \chi_k^2 = \sum_j^{N_{\text{data}}} \frac{(D_j - T_j^k)^2}{\sigma_j^2}$$

3. Calculate observables with new (reweighted) PDFs

$$\langle \mathcal{O} \rangle_{\text{new}} = \frac{1}{N_{\text{rep}}} \sum_{k=1}^{N_{\text{rep}}} w_k \mathcal{O}(f_k),$$
$$\delta \langle \mathcal{O} \rangle_{\text{new}} = \sqrt{\frac{1}{N_{\text{rep}}} \sum_{k=1}^{N_{\text{rep}}} w_k (\mathcal{O}(f_k) - \langle \mathcal{O} \rangle)^2}.$$

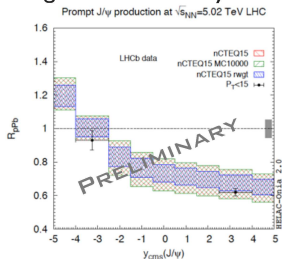
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Thanks to Kusina, Lansberg, Schienbein, Paukkunen etc

- We used only  $J/\psi$  production data from pPb collisions at the LHC
- Only the ratio  $R_{pPb}$  has been used here.
  - LHCb arXiv:1308.6729
  - ALICE arXiv:1503.07179, arXiv:1308.6726
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- Replicas reproduce the Hessian PDF
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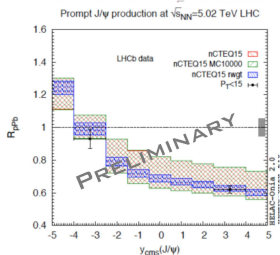
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- Reduction is more striking when including the yield data as well.

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- QCD corrections via new **NLO**, and perhaps **NNLO** topologies, **matter** much for some mechanisms and some observables
- Yet, this may not impact too much the kinematics of single quarkonium production such that  $J/\psi$  and  $\Upsilon$  (+ open HF) data might be of help to constrain nPDF

# Part VII

## Backup

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# The production mechanism(s) at low $P_T$ in proton-proton collisions

# Why is it important to know how low- $P_T$ quarkonia are produced

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- If color is bleaching at short distances (Color Singlet Model), low- $P_T$  quarkonia can be used to extract the distribution of **linearly polarised gluon in unpolarised protons**,  $h_1^{\perp g}(x, k_T, \mu)$

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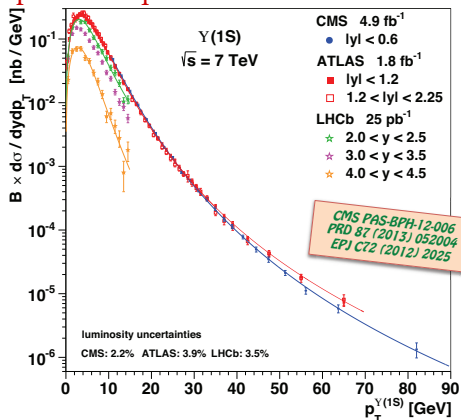
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- If regeneration is at work, how does it happen ? statistically ? according to the charm-quark distribution in the charmonium (wave-function) ?
- etc ...

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Also because, some very high  $P_T$  quarkonia which we study can be **as rare as a few millionth of the produced quarkonia**

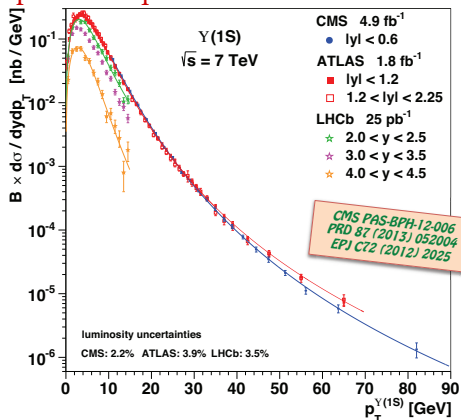
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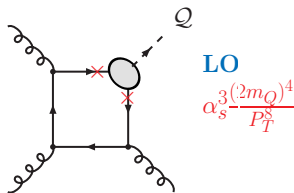


Most probably the production of a  $\Upsilon$  with  $P_T = 90 \text{ GeV}$ , even also  $20 \text{ GeV}$ , has very few things to do with the bulk of  $\Upsilon$

# Basic pQCD approach: the Colour Singlet Model (CSM)

C.-H. Chang, NPB172, 425 (1980); R. Baier & R. Rückl Z. Phys. C 19, 251(1983);

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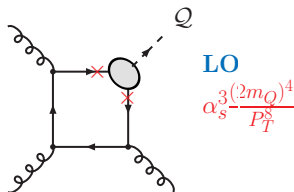


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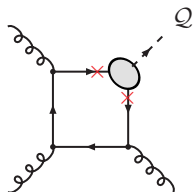
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→ Schrödinger wave function

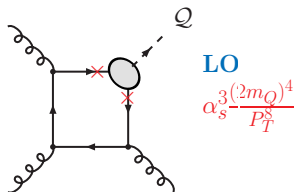


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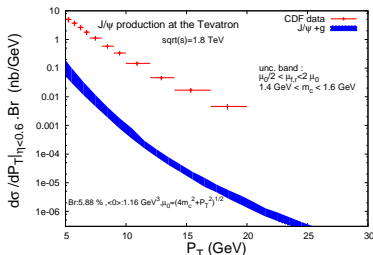
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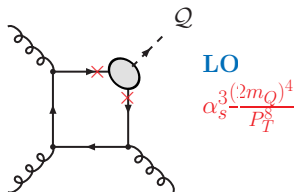
CDF, PRL 79:572 &amp; 578,1997

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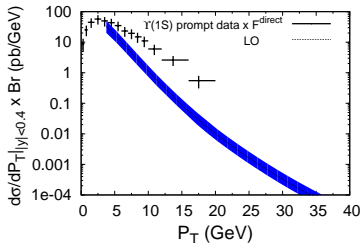
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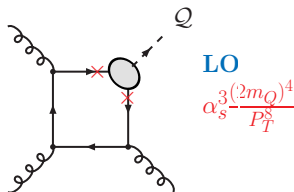
CDF, PRL 88:161802,2002

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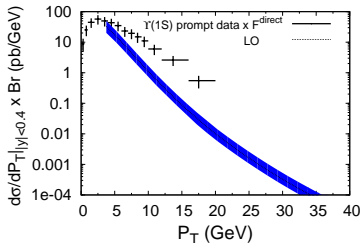
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⇒ Large QCD corrections from new topologies reduce the gap with data at mid and large  $P_T$

P.Artoisenet, J.Campbell, JPL, F.Maltoni, F. Tramontano, PRL 101, 152001 (2008)

# The LO CSM accounts for the $P_T$ -integrated yield

S. J. Brodsky and JPL, PRD 81 051502 (R), 2010; JPL, PoS(ICHEP 2010), 206 (2010); NPA 910-911 (2013) 470

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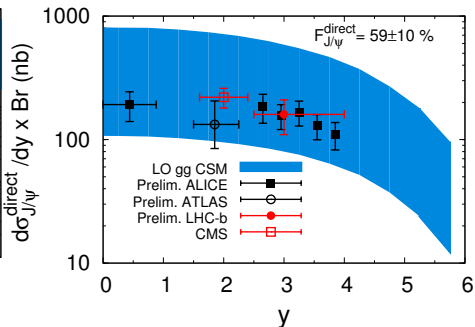
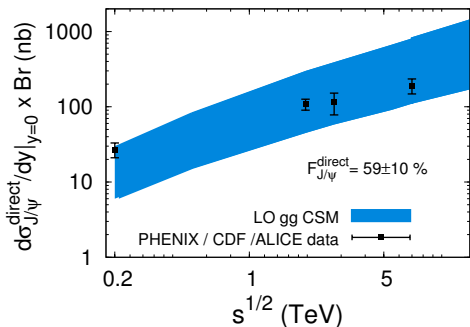
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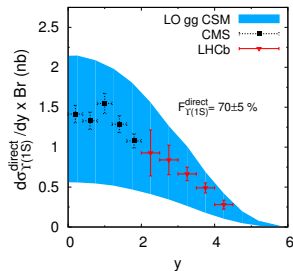


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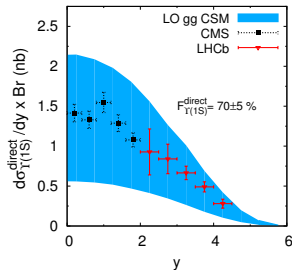
CMS PRD 83 (2011) 112004; LHCb EPJC 72 (2012) 2025

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CMS PRD 83 (2011) 112004; LHCb EPJC 72 (2012) 2025

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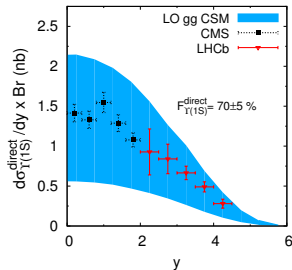


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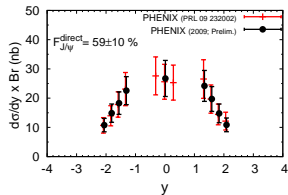
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- Earlier claims that CSM contribution to  $d\sigma/dy$  was small were based on the **incorrect assumption that  $\chi_c$  feed-down was dominant**

## NLO CSM at RHIC

 $\rightarrow J/\psi$ 

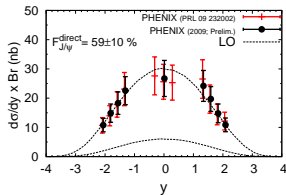
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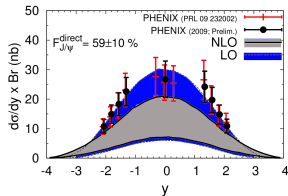
S. J. Brodsky and JPL, PRD 81 051502 (R), 2010.

LO:  $gg \rightarrow J/\psi g$  (see slide 5, **nothing new!**)

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S. J. Brodsky and JPL, PRD 81 051502 (R), 2010.



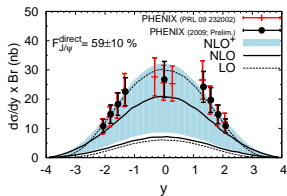
**NLO:**  $gg \rightarrow J/\psi gg, gq \rightarrow J/\psi gq, \dots$

using the matrix elements from J.Campbell, F. Maltoni, F. Tramontano, PRL 98:252002,2007

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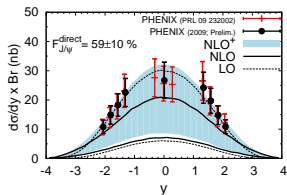
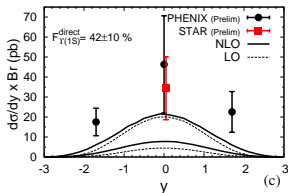
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NLO<sup>+</sup>: possible **new contribution** at LO  $cg \rightarrow J/\psi c$

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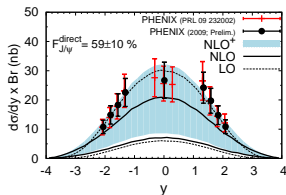
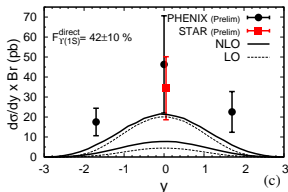
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\* Sorry: I should update these plots (updated data and fraction is about 60%)

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 $\rightarrow J/\psi$ NLO<sup>+</sup>: possible **new contribution** at LO  $cg \rightarrow J/\psi c$  $\rightarrow \Upsilon^*$ 

A priori, good convergence NLO w.r.t. LO

[I will come back to that later]

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## Analysis of charmonium production at fixed-target experiments in the NRQCD approach

F. Maltoni<sup>a</sup>, J. Spengler<sup>b</sup>, M. Bargiotti<sup>c</sup>, A. Bertin<sup>c</sup>, M. Bruschi<sup>c</sup>, S. De Castro<sup>c</sup>, L. Fabbri<sup>c</sup>,  
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- At  $\alpha_S^2$ , one only has CO contributions

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- At  $\alpha_S^3$ , one has in addition real emissions (including **one CS process**)  
 $g + g \rightarrow Q\bar{Q}[{}^1S_0^{[8]}, {}^3S_1^{[8]}, {}^3P_{J=0,2}^{[8]}] + g$ ,  $g + q(\bar{q}) \rightarrow Q\bar{Q}[{}^1S_8^{[0]}, {}^3S_1^{[8]}, {}^3P_{J=0,2}^{[8]}] + q(\bar{q})$   
 $q + \bar{q} \rightarrow Q\bar{Q}[{}^1S_0^{[8]}, {}^3S_1^{[8]}, {}^3P_{J=0,1,2}^{[8]}] + g$  and  **$g + g \rightarrow Q\bar{Q}[{}^3S_1^{[1]}] + g$**



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$$q + \bar{q} \rightarrow Q\bar{Q}[{}^1S_0^{[8]}, {}^3S_1^{[8]}, {}^3P_{J=0,1,2}^{[8]}] + g \quad \text{and} \quad \mathbf{g + g \rightarrow Q\bar{Q}[{}^3S_1^{[1]}] + g}$$

- Done with **NRQCD LDMEs fitted at LO on  $P_T$  spectra from CDF ( $\simeq 2$  TeV)**

Table 1

Reference NRQCD matrix elements for charmonium production. The color-singlet matrix elements are taken from the potential model calculation of [14, 15]. The color-octet matrix elements have been extracted from the CDF data [16] in Ref. [17]

$H$	$\langle\mathcal{O}_1^H\rangle$	$\langle\mathcal{O}_8^H[{}^3S_1]\rangle$	$\langle\mathcal{O}_8^H[{}^1S_0^{(8)}]\rangle = \langle\mathcal{O}_8[{}^3P_0^{(8)}]\rangle/m_c^2$
$J/\psi$	1.16 GeV <sup>3</sup>	$1.19 \times 10^{-2}$ GeV <sup>3</sup>	$1.0 \times 10^{-2}$ GeV <sup>3</sup>
$\psi(2S)$	0.76 GeV <sup>3</sup>	$0.50 \times 10^{-2}$ GeV <sup>3</sup>	$0.42 \times 10^{-2}$ GeV <sup>3</sup>
$\chi_{c0}$	0.11 GeV	$0.31 \times 10^{-2}$ GeV <sup>3</sup>	–

# NLO NRQCD up to RHIC II

---

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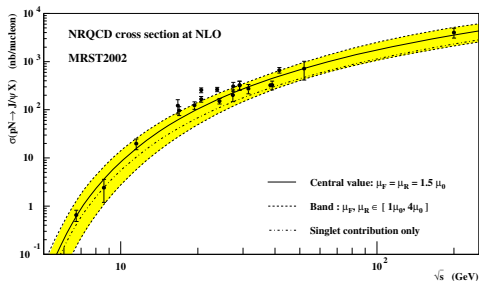
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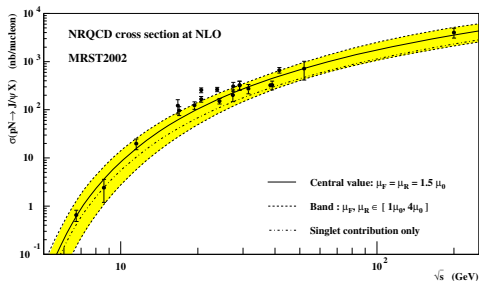


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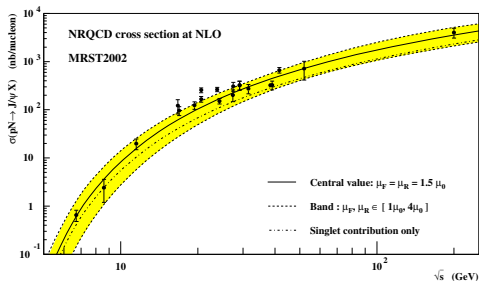
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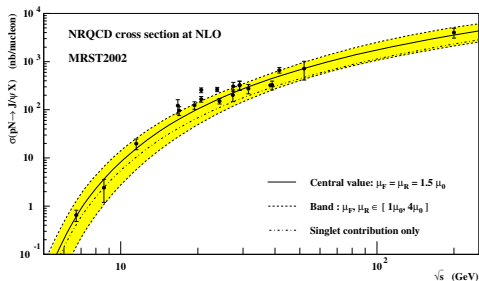


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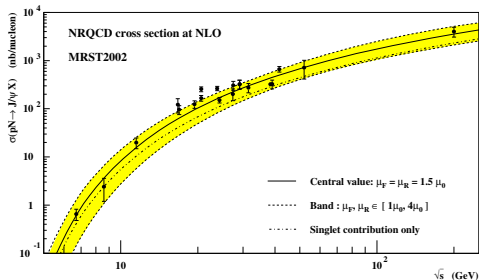
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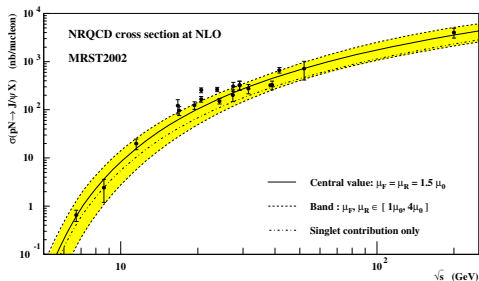
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- Never updated with LDMEs fitted at NLO

# What we did

[Y. Feng, JPL, J.X. Wang, EPJC (2015)75:313]

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  - CDF results after a small  $P_T$  extrapolation from 1.5 GeV to 0
  - LHC data
- **constant** feed-down (FD) fractions

- $F_{J/\psi}^{\text{direct}} = 60 \pm 10\%$

- $F_{\Upsilon(1S)}^{\text{direct}} = 66 \pm 10\%$

- $F_{\Upsilon(1S+2S+3S)}^{\text{direct}} = 60 \pm 10\%$

- Uncertainty on  $F^{\text{direct}}$  combined in quadrature with that of data

*Arguable but accounts for a possible energy dependence of the FD fraction*

# What we did II

We used LDMEs **fitted at NLO/one loop on the  $P_T$  spectra**

	Ref.	$\langle \mathcal{O}_{J/\psi}({}^3P_0^{[8]}) \rangle$ (in $\text{GeV}^5$ )	$\langle \mathcal{O}_{J/\psi}({}^1S_0^{[8]}) \rangle$ (in $\text{GeV}^3$ )	$\langle \mathcal{O}_{J/\psi}({}^3S_1^{[8]}) \rangle$ (in $\text{GeV}^3$ )
• $J/\psi$	Y.-Q. Ma, <i>et al.</i> PRL 106 (2011) 042002.	$-2.0 \times 10^{-3}$	$7.8 \times 10^{-2}$	0
		$2.1 \times 10^{-2}$	$3.5 \times 10^{-2}$	$5.8 \times 10^{-3}$
		$4.1 \times 10^{-2}$	0	$1.1 \times 10^{-2}$
	B. Gong, <i>et al.</i> PRL 110 (2013) 042002	$-2.2 \times 10^{-2}$	$9.7 \times 10^{-2}$	$-4.6 \times 10^{-3}$
M. Butenschoen, B. Kniehl. PRD (2011) 051501	$-9.1 \times 10^{-2}$	$3.0 \times 10^{-2}$	$1.7 \times 10^{-3}$	

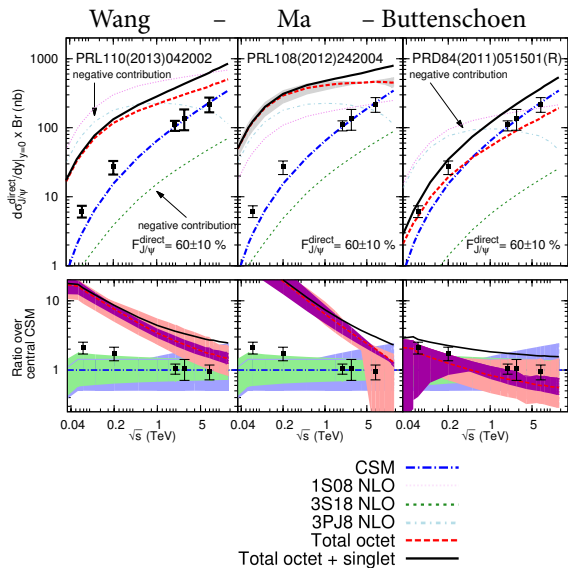
  

	Ref.	$\langle \mathcal{O}_{\psi(2S)}({}^3P_0^{[8]}) \rangle$ (in $\text{GeV}^5$ )	$\langle \mathcal{O}_{\psi(2S)}({}^1S_0^{[8]}) \rangle$ (in $\text{GeV}^3$ )	$\langle \mathcal{O}_{\psi(2S)}({}^3S_1^{[8]}) \rangle$ (in $\text{GeV}^3$ )
• $\psi'$	B. Gong, <i>et al.</i> PRL 110 (2013) 042002	$9.5 \times 10^{-3}$	$-1.2 \times 10^{-4}$	$3.4 \times 10^{-3}$
		$-4.8 \times 10^{-3}$	$2.9 \times 10^{-2}$	0
		$7.9 \times 10^{-3}$	$5.6 \times 10^{-3}$	$3.2 \times 10^{-3}$
Y.-Q. Ma, <i>et al.</i> PRL 106 (2011) 042002	$1.1 \times 10^{-2}$	0	$3.9 \times 10^{-3}$	

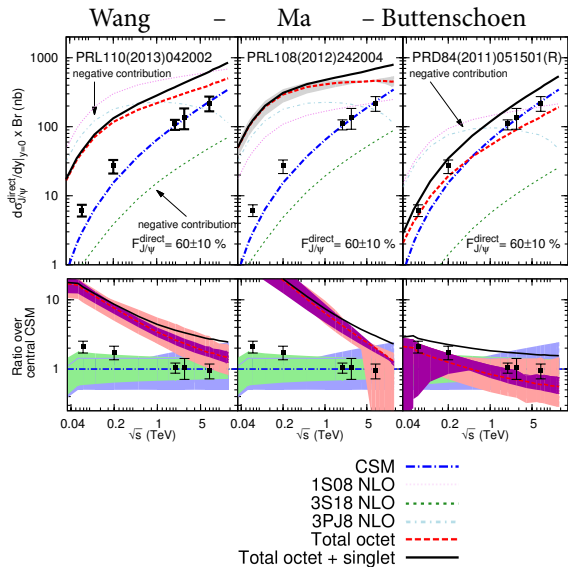
	Ref.	$\langle \mathcal{O}_{Y(1S)}({}^3P_0^{[8]}) \rangle$ (in $\text{GeV}^5$ )	$\langle \mathcal{O}_{Y(1S)}({}^1S_0^{[8]}) \rangle$ (in $\text{GeV}^3$ )	$\langle \mathcal{O}_{Y(1S)}({}^3S_1^{[8]}) \rangle$ (in $\text{GeV}^3$ )
• $Y(1S)$	B. Gong, <i>et al.</i> PRL 112 (2014) 3, 032001.	$-10.36 \times 10^{-2}$	$11.15 \times 10^{-2}$	$-4.1 \times 10^{-2}$

[We have also added the fit of G.T. Bodwin, *et al.*, PRL 113, 022001 (2014) even though it is based on a fragmentation function approach]

Results for the  $J/\psi$ 

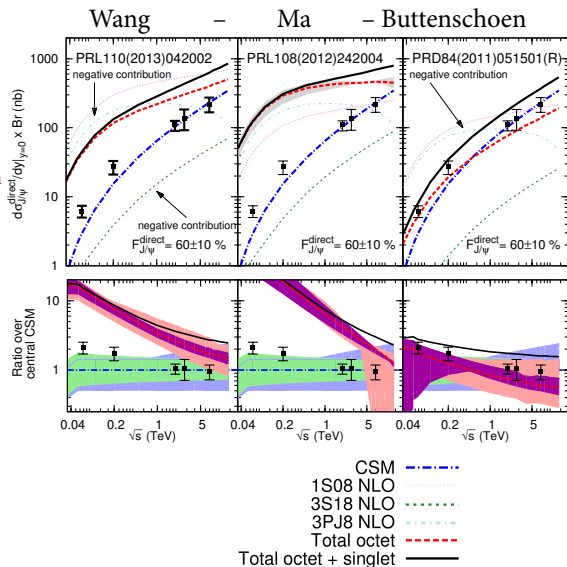
Results for the  $J/\psi$ 

- First 2 fits: **10 times above** the data around 200 GeV – as *Maltoni et al.*



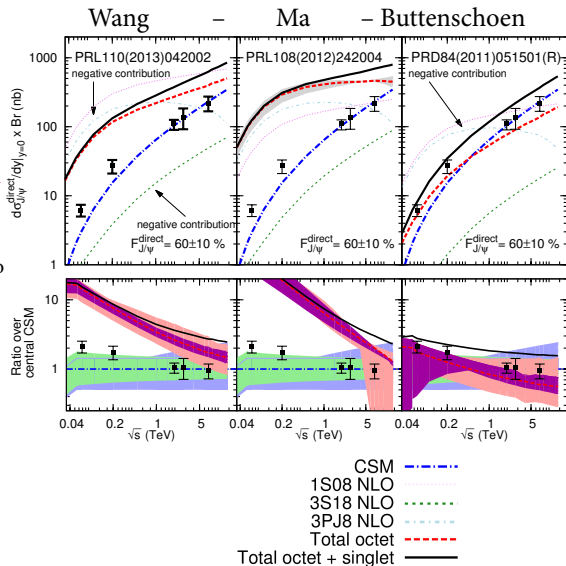
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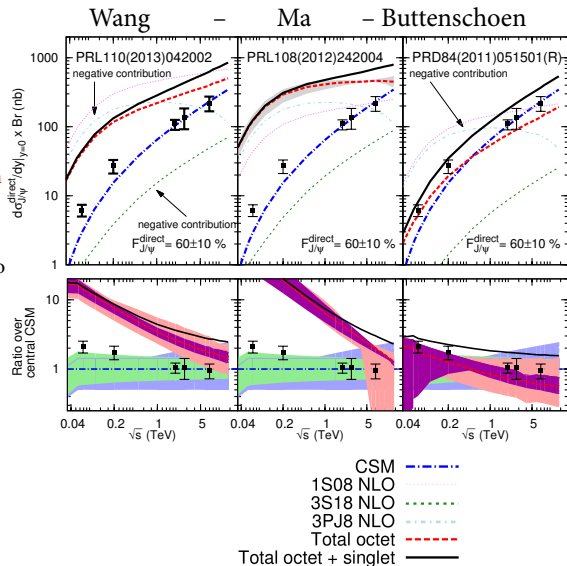
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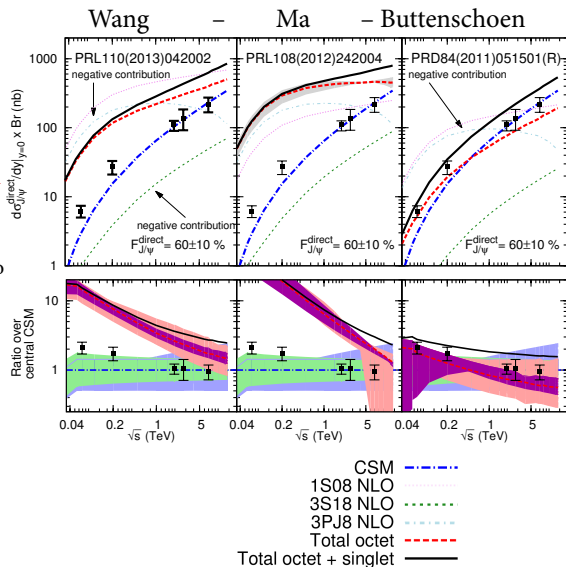
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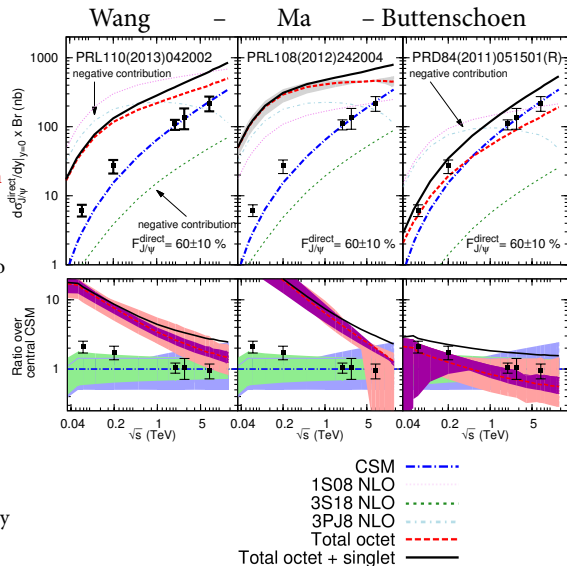
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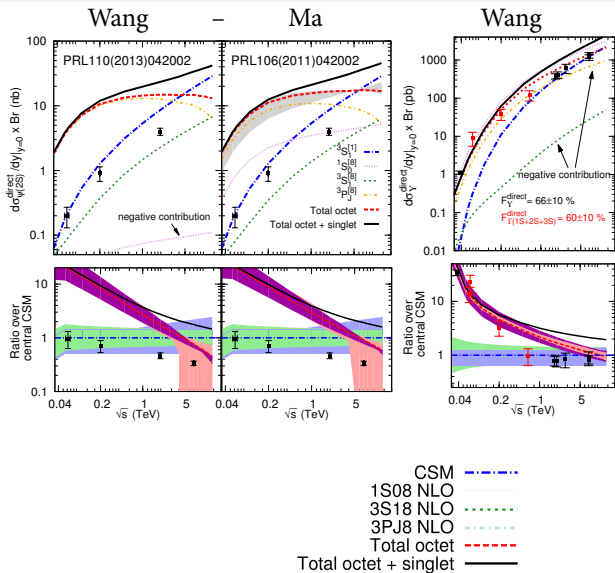




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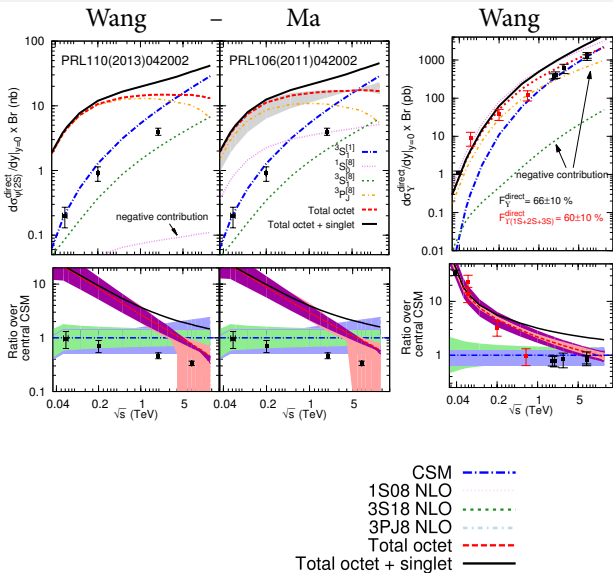
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- Not a surprise since **the CSM alone accounts well for the data**; adding any contribution creates a “surplus”



Results for the  $\psi'$  and  $\Upsilon$ 

Results for the  $\psi'$  and  $\Upsilon$ For  $\psi(2S)$ 

- Worse than for  $J/\psi$
- CSM even tends to overshoot at large  $\sqrt{s}$  – yet in agreement within uncertainties (lower panel)
- CO dominated by the  $^3P_J^{[8]}$  channel which nearly shows an unphysical behavior

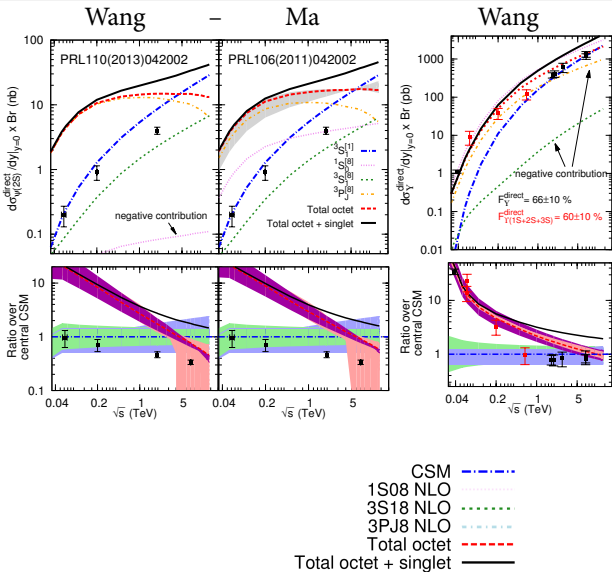


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For  $\Upsilon(1S)$ 

- Reasonable trend for  $\Upsilon$
- CSM is doing a perfect job in the TeV range – note that the RHIC points moved down
- On the other hand, CO needed at low  $\sqrt{s}$ ? High  $x$  gluon pdf underestimated?



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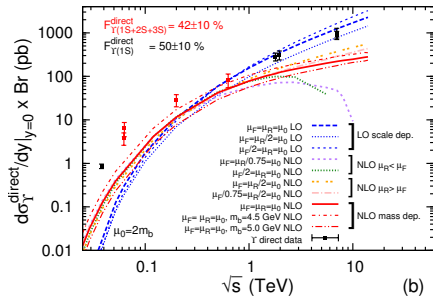
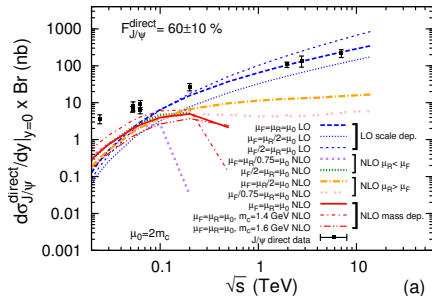
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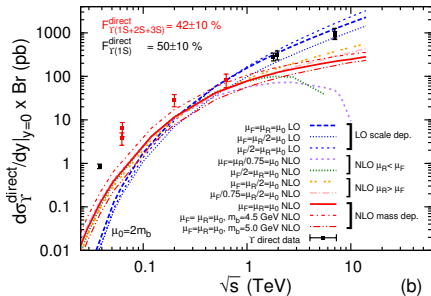
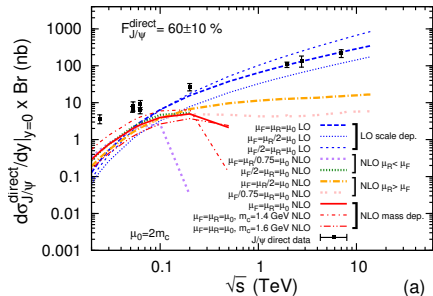
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We checked these with FDC

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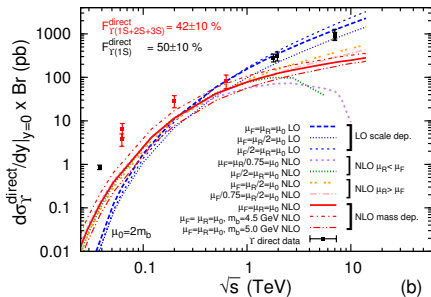
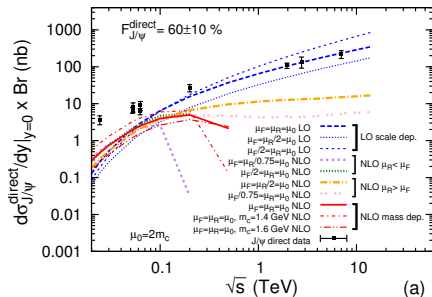


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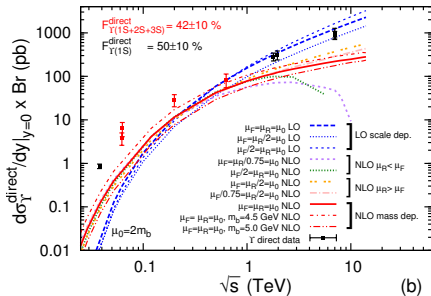
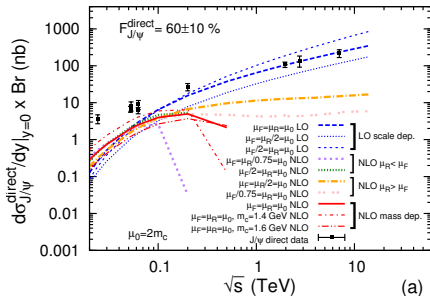
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Is it due to ISR, FSR ? Is NRQCD simply not holding at low  $P_T$  ?

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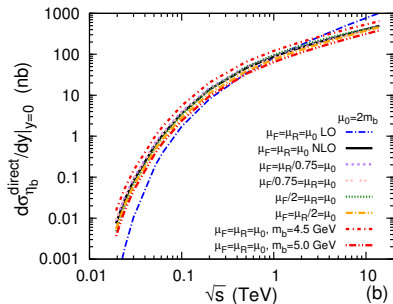
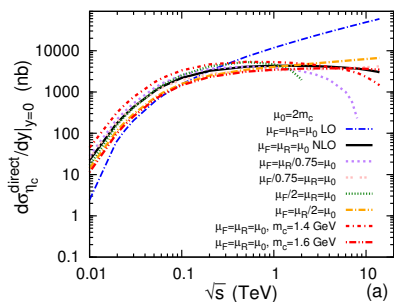


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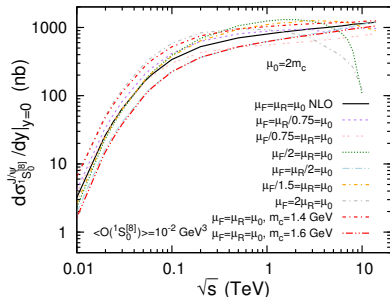
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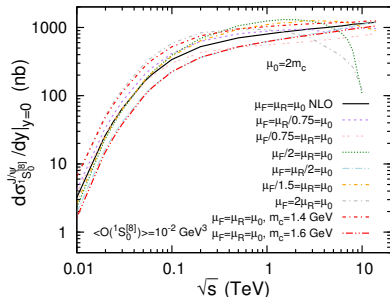
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M. Echevarria, T. Kasemets, JPL, C. Pisano A. Signori (in progress); J.P. Ma, J.X. Wang, S. Zhao, PRD 88 (2013) 014027



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LHCb, JHEP 10(2013)115 & JHEP 1410 (2014) 88 ; CMS, EPJC, 72, 2257 (2012); ATLAS, JHEP 07(2014)154

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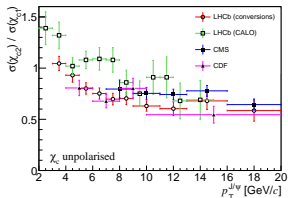
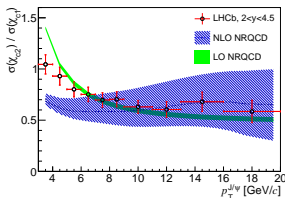
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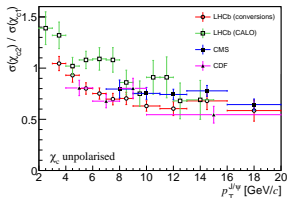
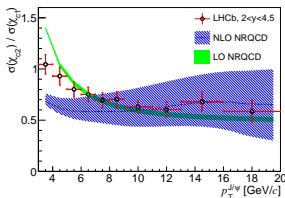


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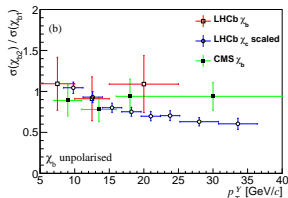
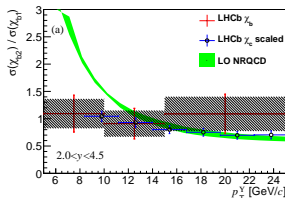
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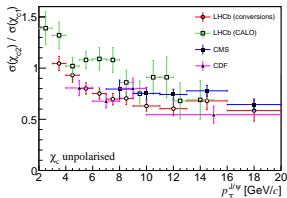
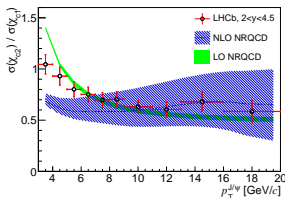


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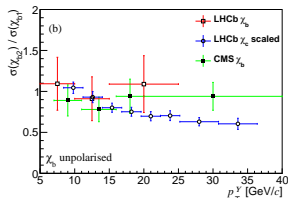
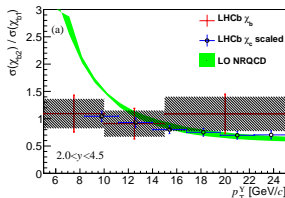
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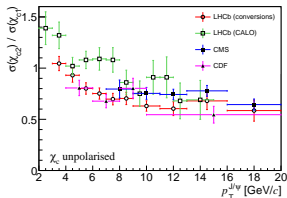
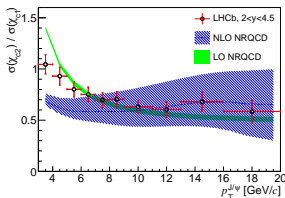
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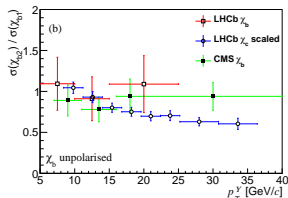
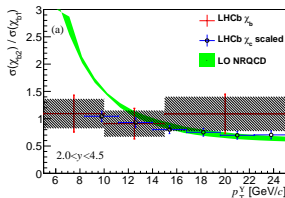
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- It can easily be check by MCFM at NLO for instance

<http://mcfm.fnal.gov/>

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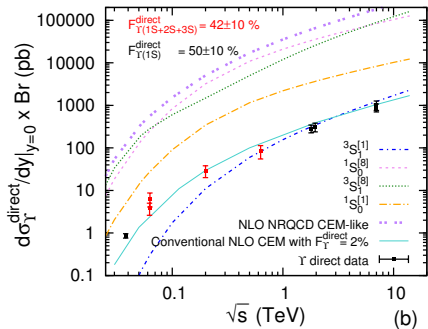
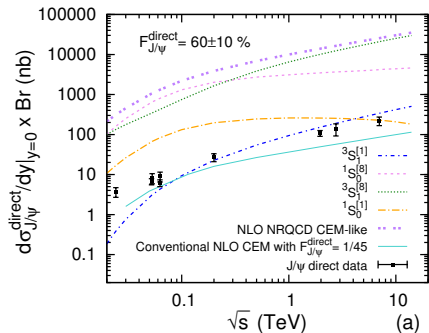
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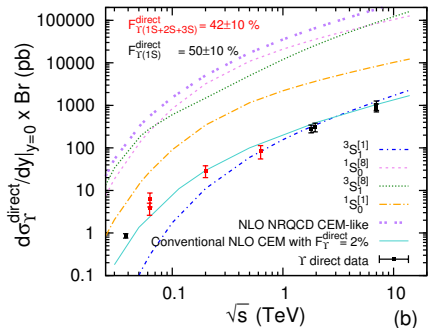
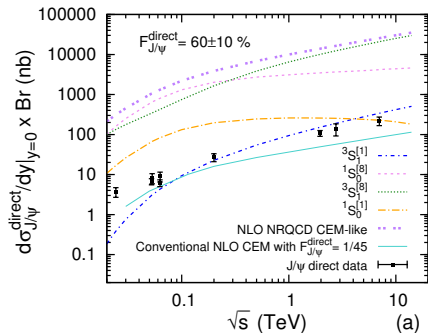
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 \langle \mathcal{O}_{3S_1}(^1S_0^{[8]}) \rangle &= \frac{4}{3} \times \langle \mathcal{O}_{3S_1}(^1S_0^{[1]}) \rangle, \\
 \langle \mathcal{O}_{3S_1}(^3S_1^{[8]}) \rangle &= 4 \times \langle \mathcal{O}_{3S_1}(^1S_0^{[1]}) \rangle.
 \end{aligned} \tag{1}$$

- If, as it should be in NRQCD,  $\langle \mathcal{O}_{3S_1}(^3S_1^{[1]}) \rangle$  is the usual CS LDME, *i.e.*  $\frac{2N_C}{4\pi} (2J+1) |R(0)|^2$ , everything is fixed

## CEM results

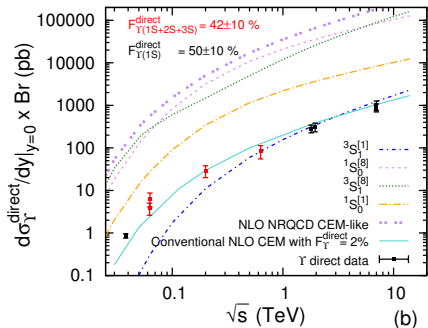
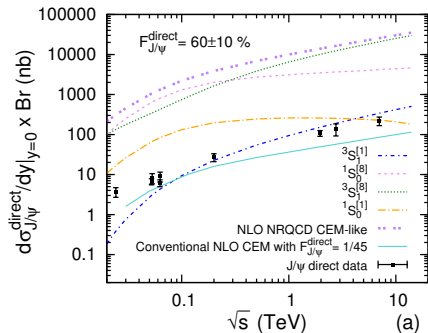


## CEM results



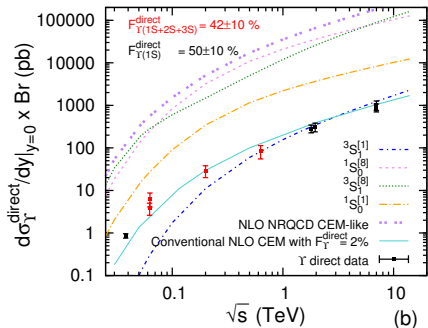
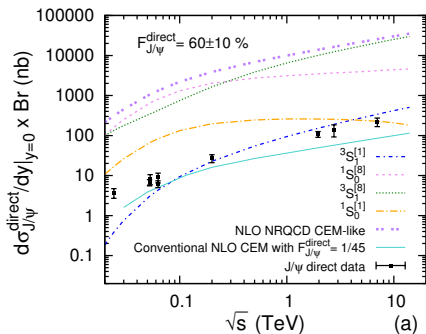
- NRQCD-like CEM badly overshoots the data

## CEM results



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  - Expected since CO LDMEs are as large as the CS, whereas the hard parts tend to be larger.

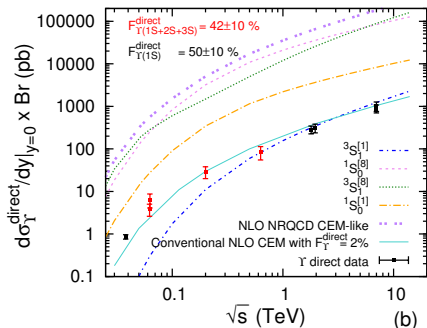
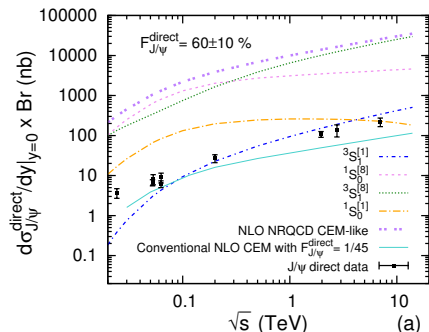
## CEM results



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## CEM results



- NRQCD-like CEM badly overshoots the data
  - Expected since CO LDMEs are as large as the CS, whereas the hard parts tend to be larger.
  - Weird energy behaviour
- **Conventional CEM does a pretty good job**
  - No th. uncertainty shown
  - “Natural” value of  $F_{J/\psi}^{\text{direct}}$  is ok