

Consistency and Uniqueness  
of combined models of  
hard jet quenching and soft perfect fluid observables  
at RHIC and LHC

AND

Non-perturbative Lattice QCD data

Part 1: Perturbative and Nonperturbative Aspects of Jet Tomography  
In Ideal Event Averaged A+A Spacetime Geometries

Part 2: Jet Quenching Coupled to Event by Event Fluctuating  
Viscous Hydrodynamic “Perfect Fluids”

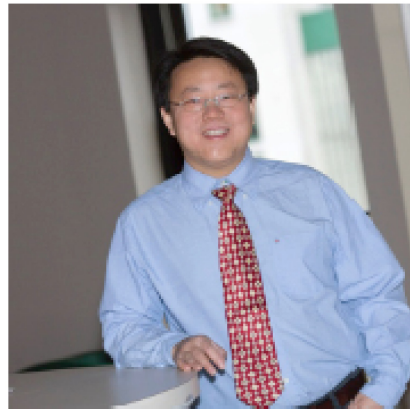
Miklos Gyulassy

*Nuclear Science Division, Lawrence Berkeley National Laboratory, Berkeley, CA 94720, USA  
Pupin Lab MS-5202, Department of Physics, Columbia University, New York, NY 10027, USA and  
Institute of Particle Physics, Central China Normal University, Wuhan, China*

This talk is based on work of many talented young collaborators. Special thanks to



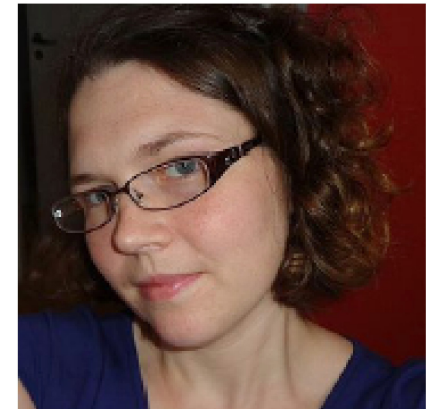
Jiechen Xu



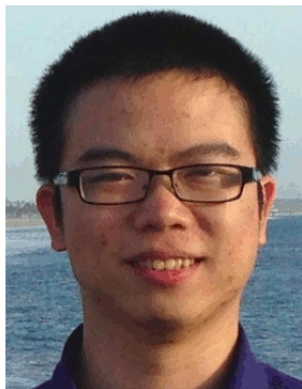
Jinfeng Liao



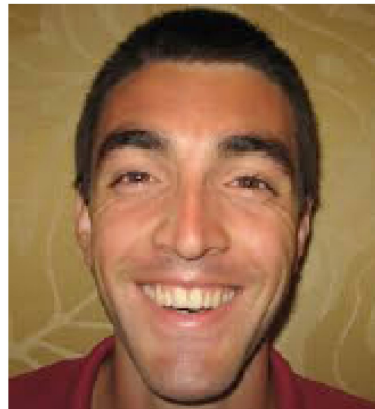
Jorge Noronha



Jaki Noronha-Hostler



Shuzhe Shi



Alessandro Buzzatti



Andrej Ficnar



Barbara Betz

And to more senior collaborators X.N.Wang, I.Vitev, P.Levai, W. Horowitz, ...

# Perturbative vs NonPerturbative Jet Tomography in 2+1D viscous hydrodynamic backgrounds

- 1) Data on (RAA and  $v_2$ ) at (RHIC&LHC) on high  $p_T$  ( $\pi$ , D,B) can be simultaneously “fit” with many different  $dE_{dx}$  models combined with different viscous hydrodynamic background models
- 2) CUJET3 with sQGMonopole plasma parameters constrained by lattice QCD provides a chromo-elec+mag quasi-parton model of  $q_{hat}(E,T)$  consistent with RHIC+LHC1+LHC2 data **as well as** perfect fluidity  $\eta/s \sim 1/q_{hat}(E \sim 3T, T) \sim 1/4\pi$  at least in smooth VISHNU fields  
[Consistency of Perfect Fluidity and Jet Quenching in semi-Quark-Gluon Monopole Plasmas, Jiechen Xu](#) , Jinfeng Liao, MG, CPL32 (2015),JHEP(2016); [Shuzhe Shi, et al in progress 2017](#)
- 3) There exists a pQCD/HTL  $dE_{dx}$  model coupled to **event by event** viscous hydro consistent with hard&soft data but with  **$q_{hat}(E \sim 3T, T)$  incompatible with perfect fluidity**  
**Event-by-event hydrodynamics + jet energy loss: A solution to the  $R_{AA} \otimes v_2$  puzzle**  
[Jacquelyn Noronha-Hostler \(Houston U.\)](#), [Barbara Betz \(Frankfurt U.\)](#), [Jorge Noronha \(Sao Paulo U.\)](#), [Miklos Gyulassy](#)  
PRL116 (2016), PRC95 (2017)
- 4) See other soft+hard model combinations this week workshop

The Existence of multiple incompatible microscopic descriptions that can account for hard and soft data (**at similar  $\chi^2/NDF < 4$  level of confidence**) remains an obstacle in drawing objective conclusions about the physics of the the new form(s) of matter produced in AA, pA, pp at RHIC and LHC. This talk outlines our strategy to proceed forward.

How to proceed ??

How can we converge on the physics ??

Can we utilize Soft-Hard Event Engineering (SHEE) to constrain quantitatively the model parameter-space iso- $\chi^2$  hypersurfaces(s)?

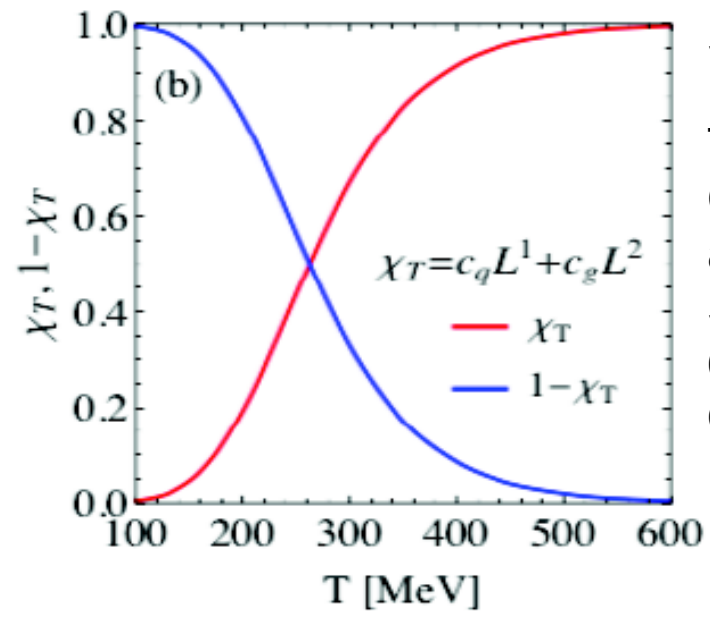
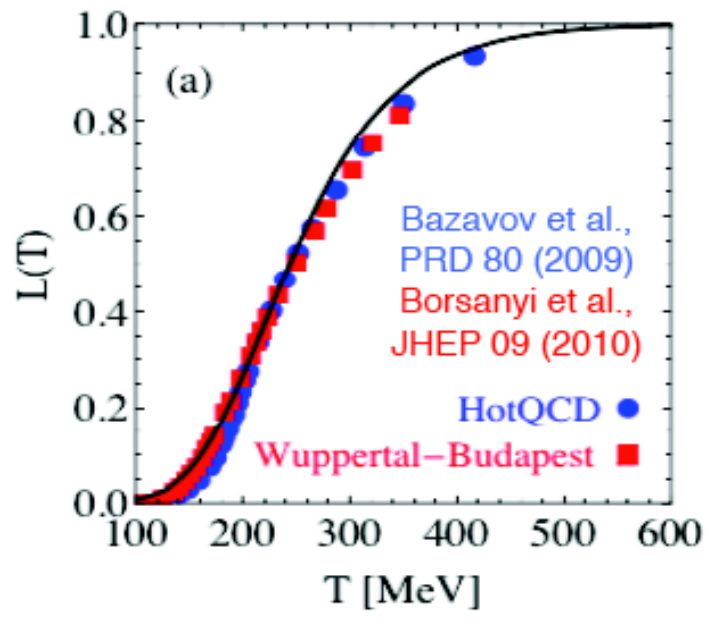
Goal is to put experimental constraint bands on top of Lattice QCD cyber-data !

Does there exist an internally consistent band of description(s) that can account with reasonable  $\chi^2 < 4$  or better for all RHIC & LHC data simultaneously on soft-soft, soft-hard, and hard-hard observed correlations AND that can predict falsifiable future observables ?

In this talk I review two such models in that band.

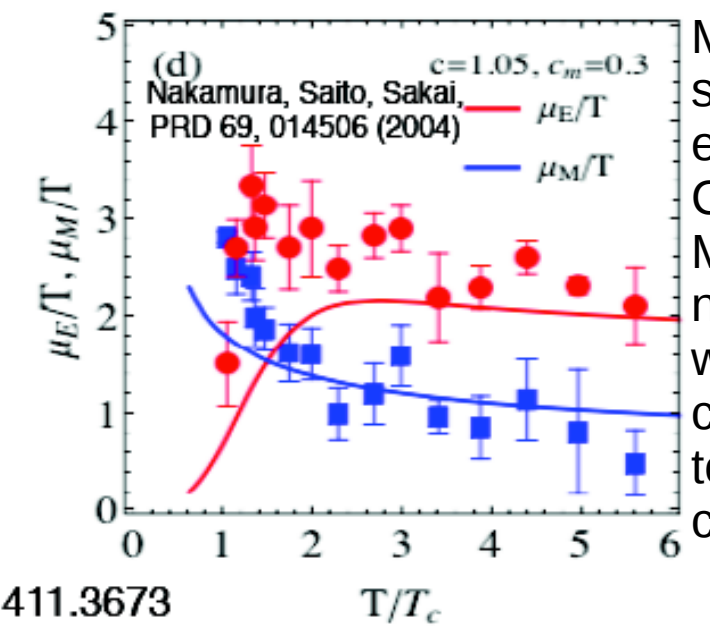
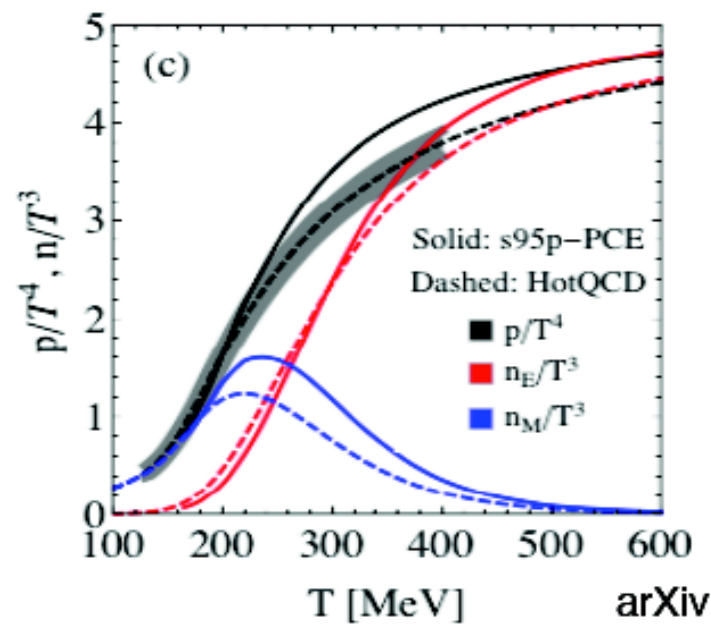
Can we eventually put exp.  $\chi^2$  constraint bands on these Thermal Lattice QCD data  
 And bridge heavy ion phenomenology with the fundamental physics of confinement ??

## Lattice Constraints: Polyakov Loop, EOS, E & M Screening Masses



Semi-QGP  
 The color elec  
 Q + G d.o.f.  
 are  
 Suppressed  
 due to semi  
 confinement

Pisarski et al



Magnetic screen  
 suggests  
 emergent  
 Chromo-Mag  
 Monopole d.o.f.  
 near  $T_c$   
 which could  
 condense  $T < T_c$   
 to explain  
 confinement

arXiv:1411.3673



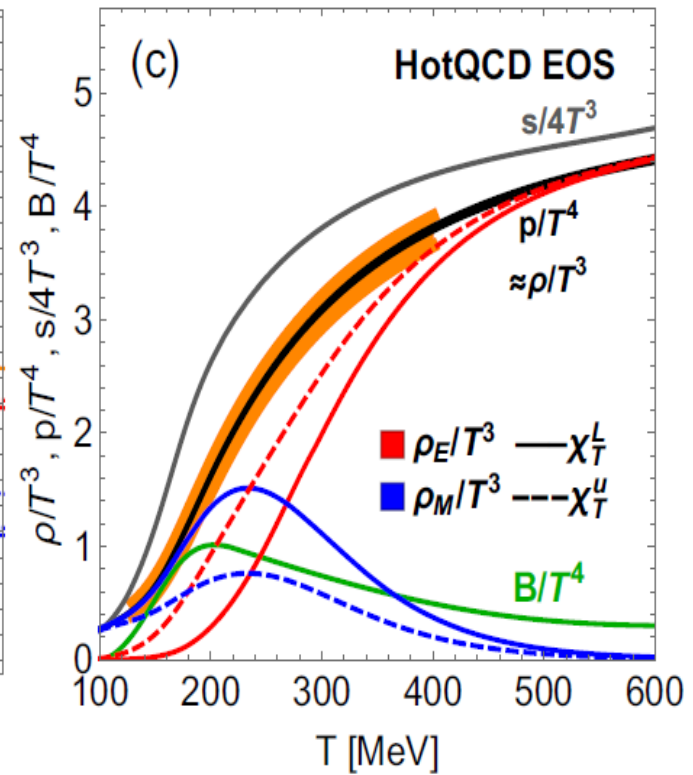
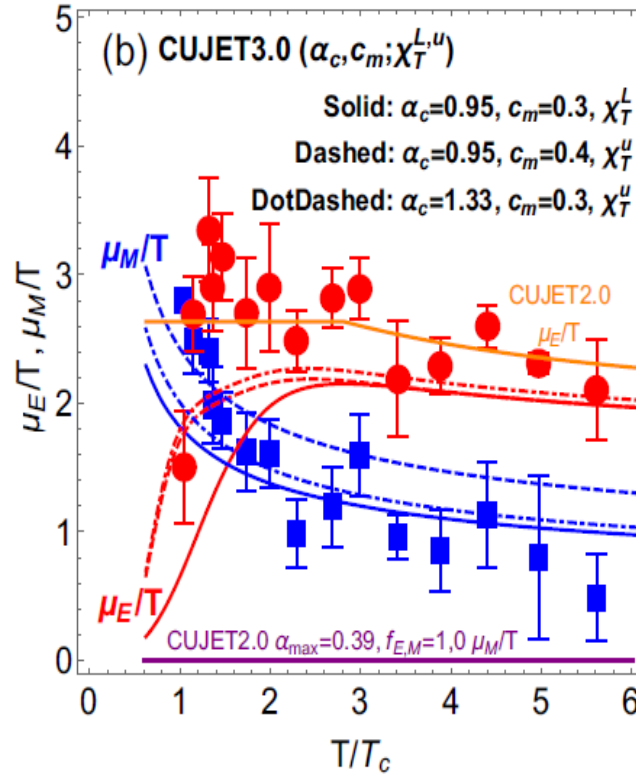
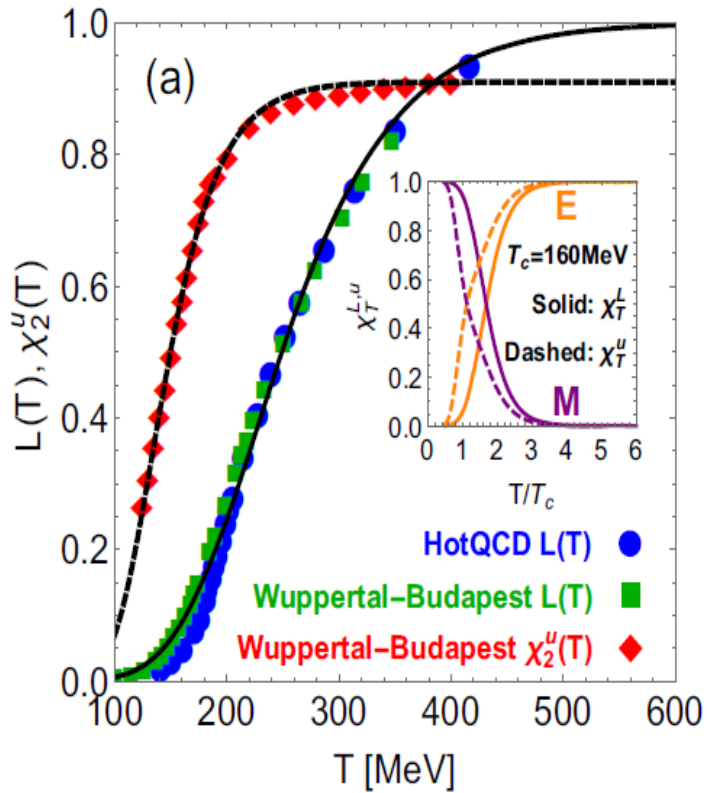
P.Petreczky proposed light quark susceptibility data => semi-Quark color elec dof may be liberated more quickly than suggested by Polyakov loop suppressed semi-Quarks

As a measure of the sensitivity CUJET3 fits to the assumed color structure of the sQGMP we compare results with Slow quark liberation

$$\chi_T^L = c_q L + c_g L^2$$

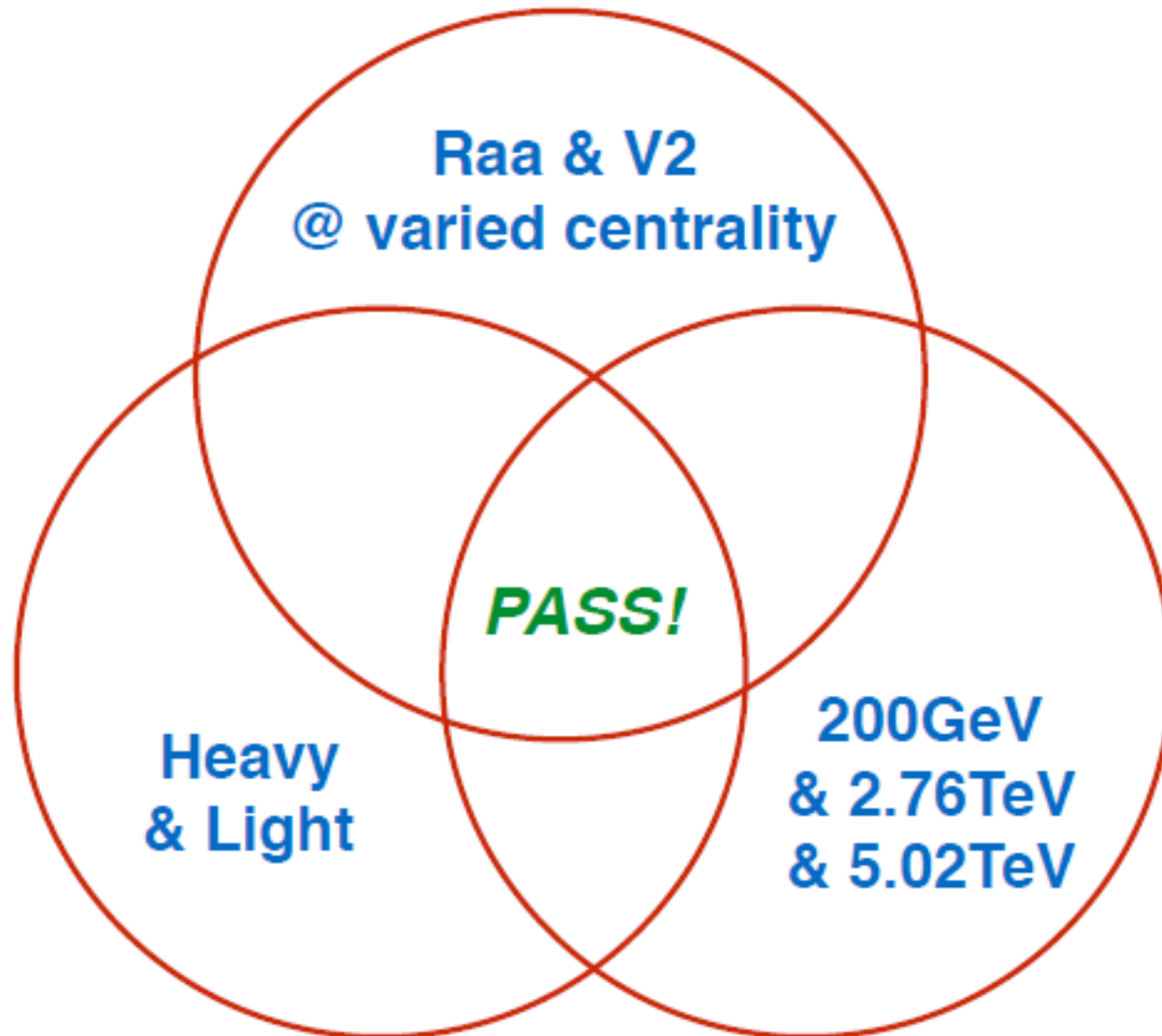
to Fast quark liberation

$$\chi_T^u = c_q \chi_2^u(T) / \chi_2^u(\infty) + c_g L^2$$

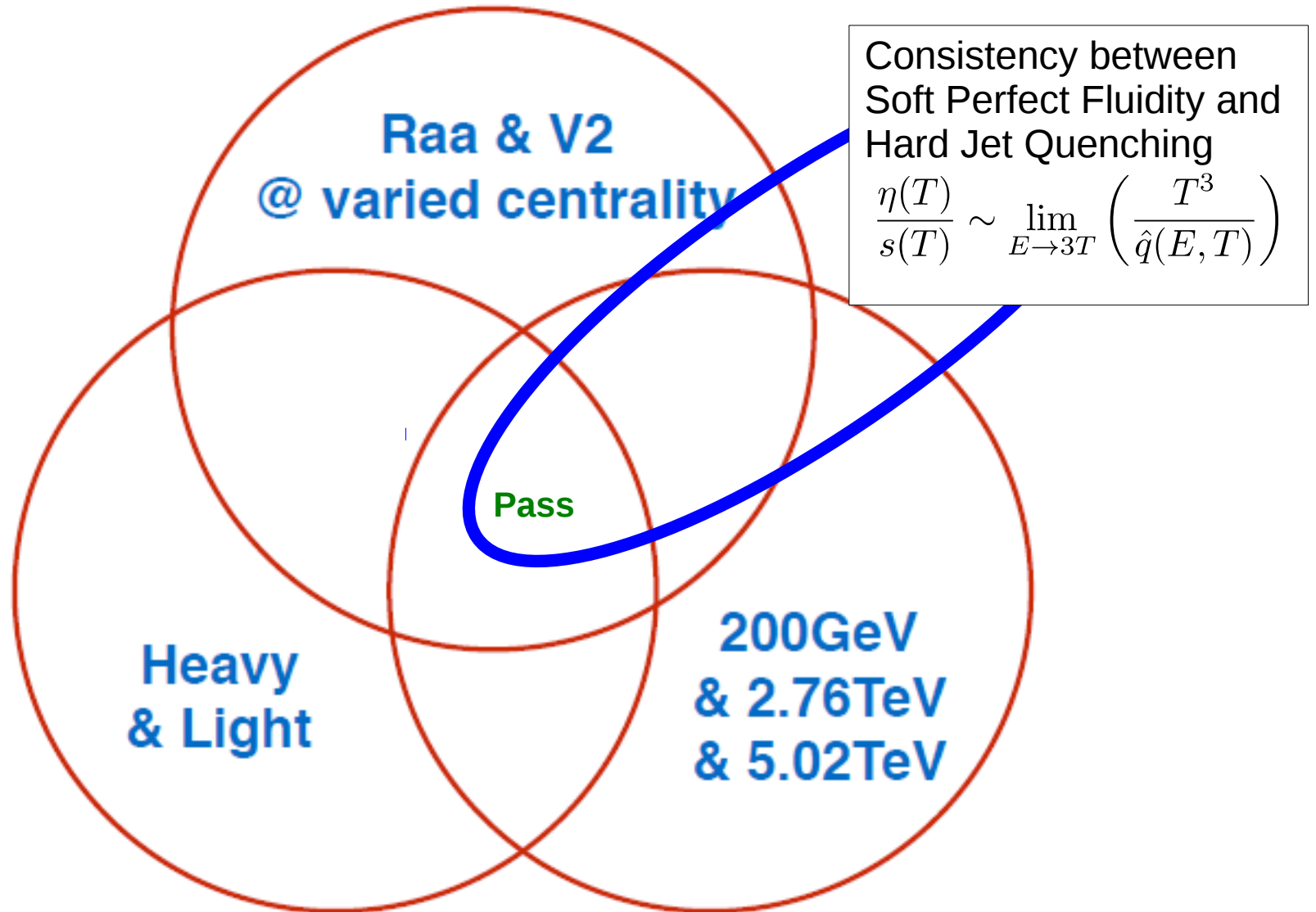


Our “greedy” goal with CUJET3 and future CUJET4= ebe CUJET3 and SHEE approaches is to try to put experimental (via RAA,v2,v3) Chi^2 constraint bands on the chromo composition/structure of sQGMP quark and gluon color electric quasi-monopoles dof and color magnetic quasi-monopoles dof consistent with (1) lattice EOS P(T) (2) screening masses, and (3) minimal eta/s~T^3/qhat soft-hard phenom.

# The Challenge to Every Model



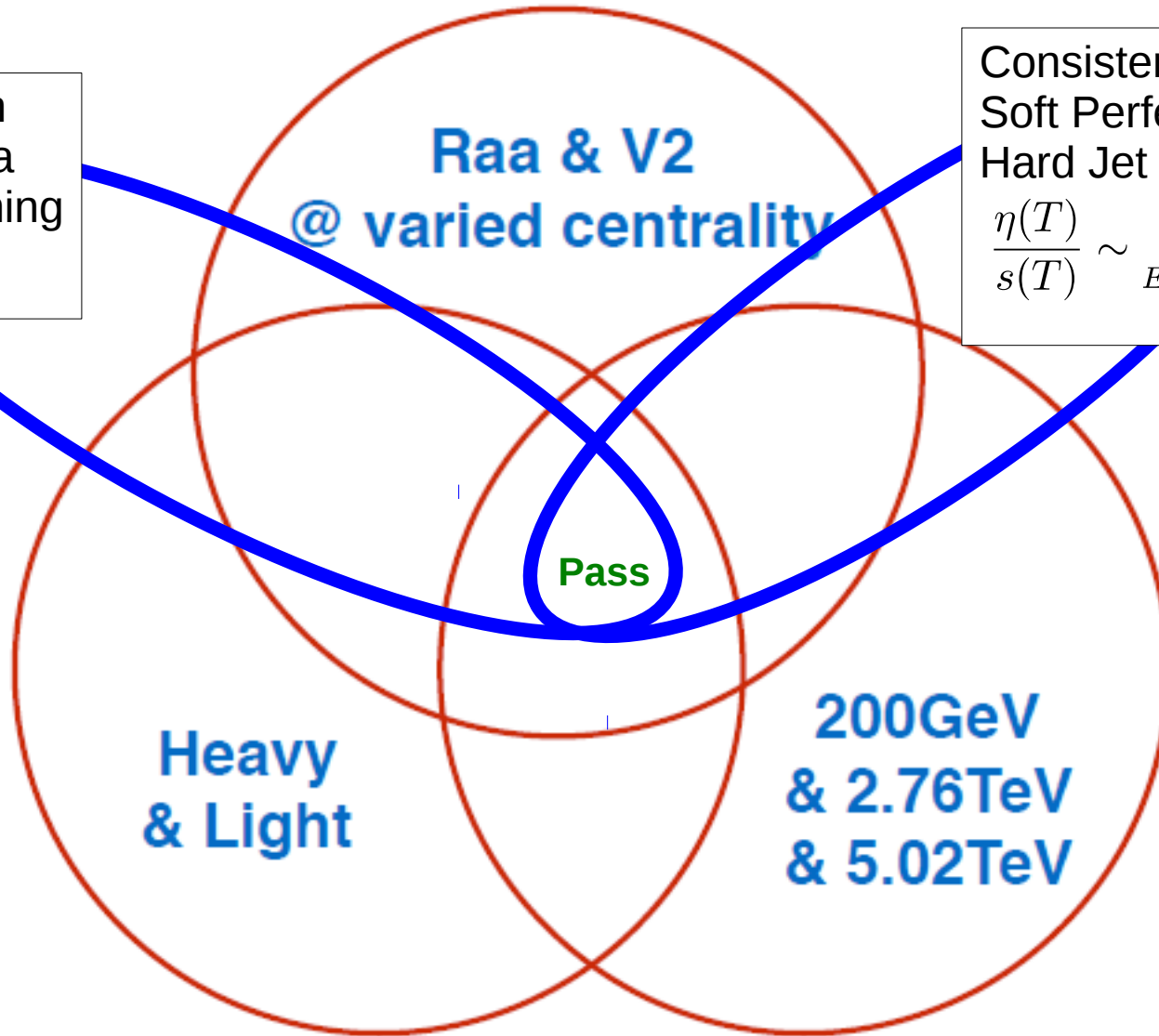
# The Challenge to Every Model





# The Challenge to Every Model

Consistency with Lattice QCD data On EOS, Screening Polyakov, ...



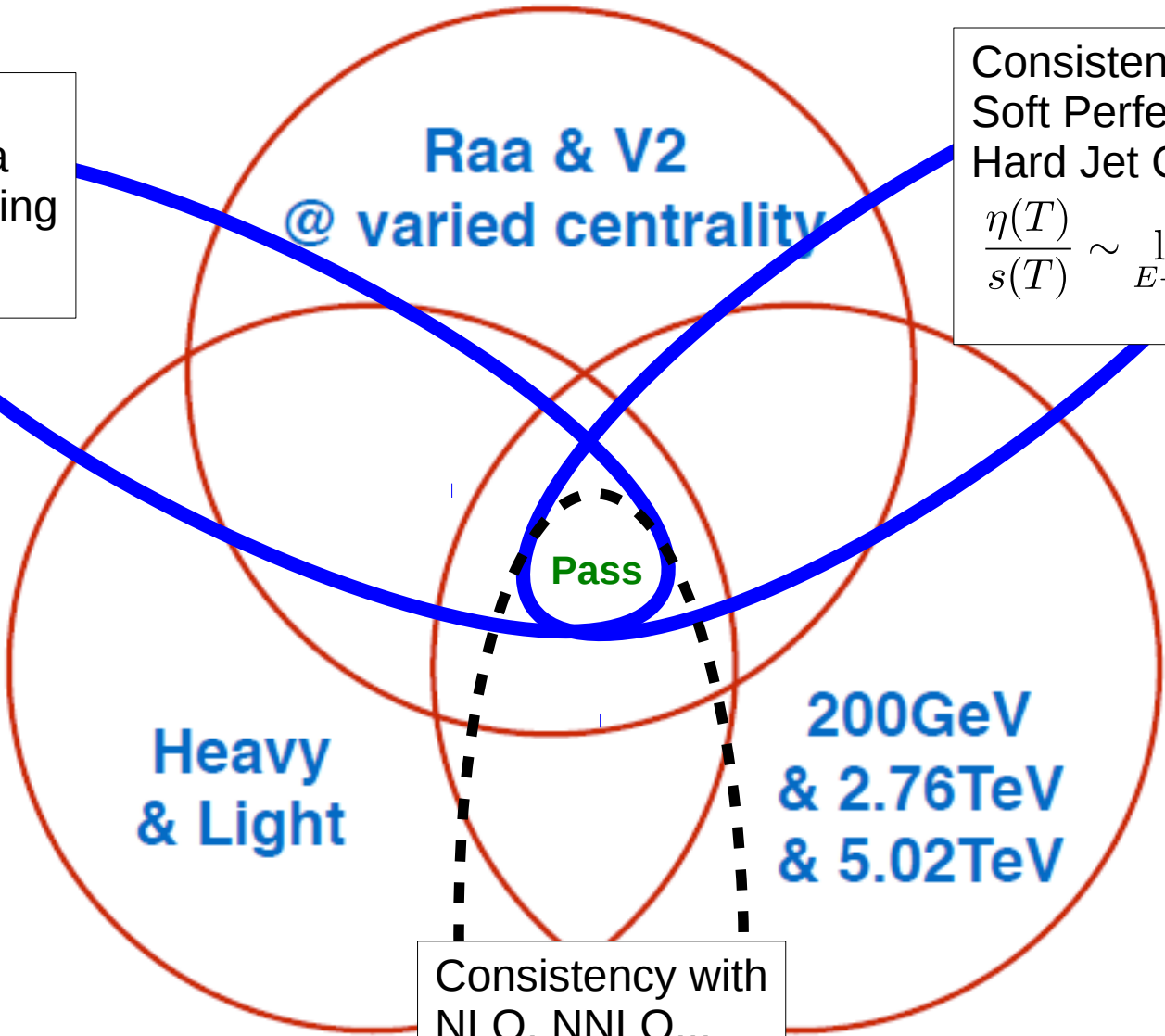
Consistency between Soft Perfect Fluidity and Hard Jet Quenching

$$\frac{\eta(T)}{s(T)} \sim \lim_{E \rightarrow 3T} \left( \frac{T^3}{\hat{q}(E, T)} \right)$$

# The Challenge to Every Model

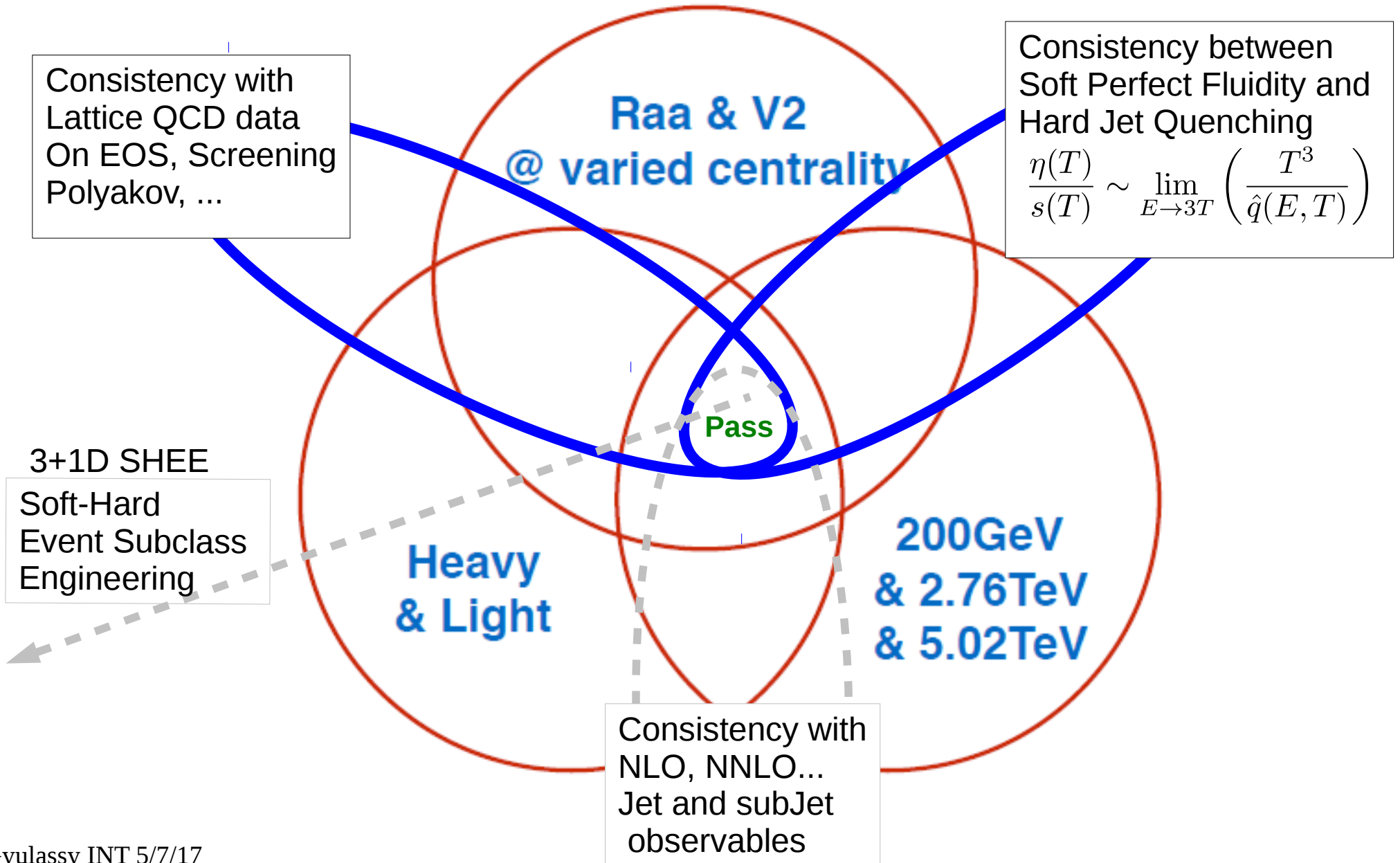
Consistency with Lattice QCD data On EOS, Screening Polyakov, ...

Consistency between Soft Perfect Fluidity and Hard Jet Quenching

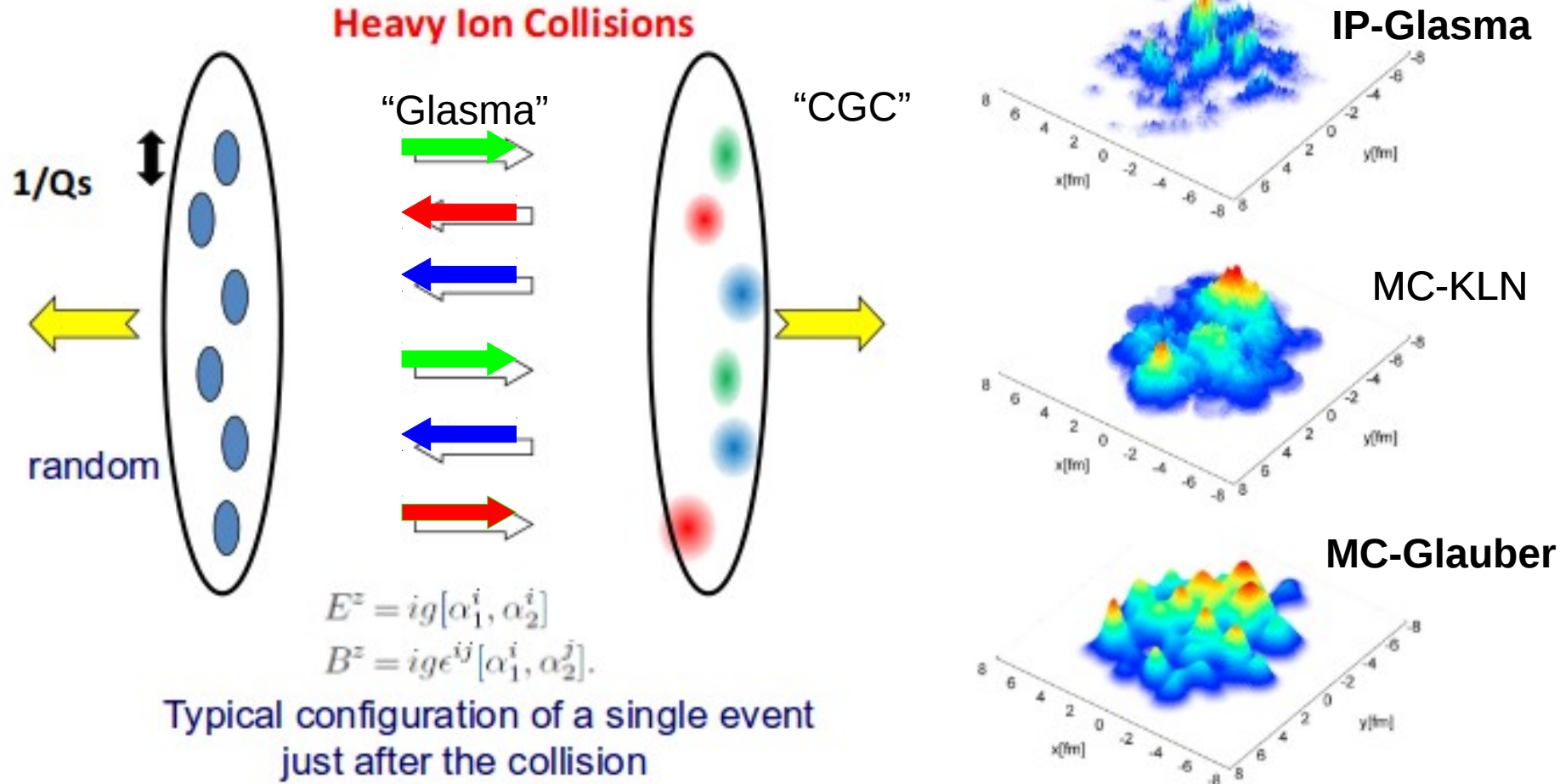
$$\frac{\eta(T)}{s(T)} \sim \lim_{E \rightarrow 3T} \left( \frac{T^3}{\hat{q}(E, T)} \right)$$


Consistency with NLO, NNLO... Jet and subJet observables

# The Challenge to Every Model



**A+B inhomogeneous fluctuating “perfect fluids” &/or “glasmas”:  
 ( L.McLerran, R.Venugopalan 1994. ...B.Schenke et al 2017 )**

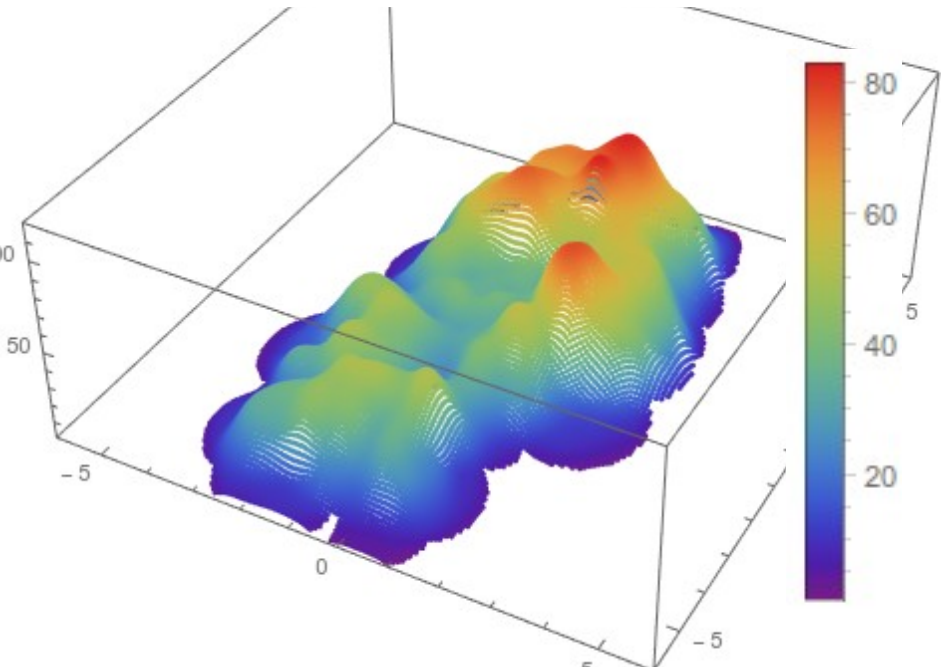


**Highly coherent colored fields:  
 Stringlike in longitudinal direction  
 Stochastic on scale of inverse saturation momentum in transverse direction  
 Multiplicity fluctuates as negative binomial distribution**

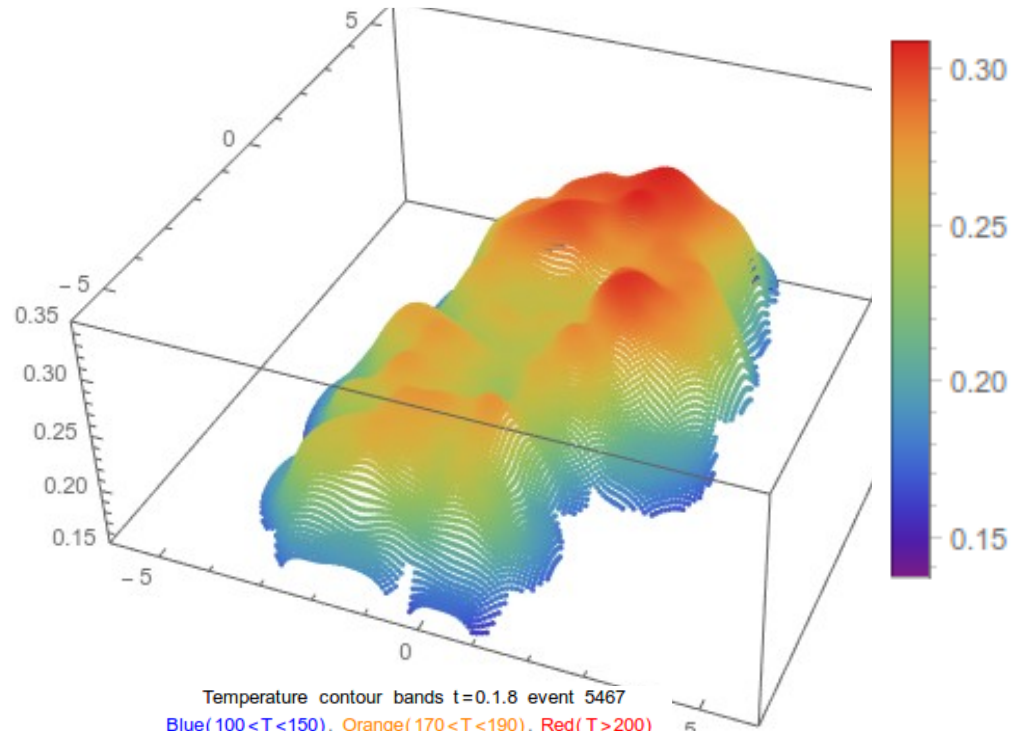
Longitudinal “Glasma” fields generalize  $\sim 1\text{fm}$  Lund strings in HIJING  
 To both electric and magnetic flux tubes of sub nucleon transverse scales  $1/Q_{\text{sat}} \sim 0.2 \text{ fm}$

Example of evolution of typical lumpy event with **disconnected isotherm surfaces**

Energy density profile event 5467



Temperature profile event 5467



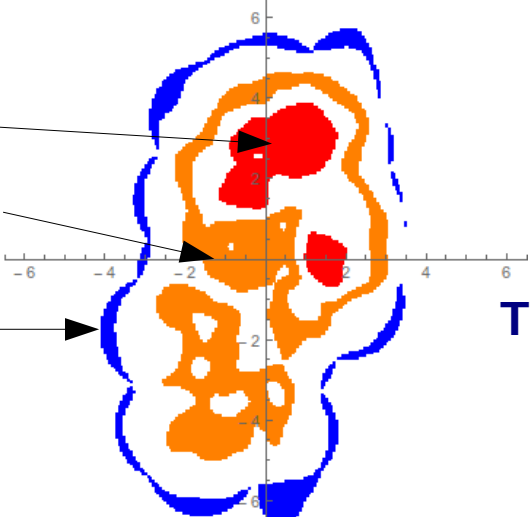
Temperature contour bands  $t=0.6$  event 5467  
Blue ( $150 < T < 190$ ), Orange ( $250 < T < 270$ ), Red ( $T > 290$ )

Temperature contour bands  $t=0.1.8$  event 5467  
Blue ( $100 < T < 150$ ), Orange ( $170 < T < 190$ ), Red ( $T > 200$ )

$t=0.6$   
 $T > 290$

$T=170-220$

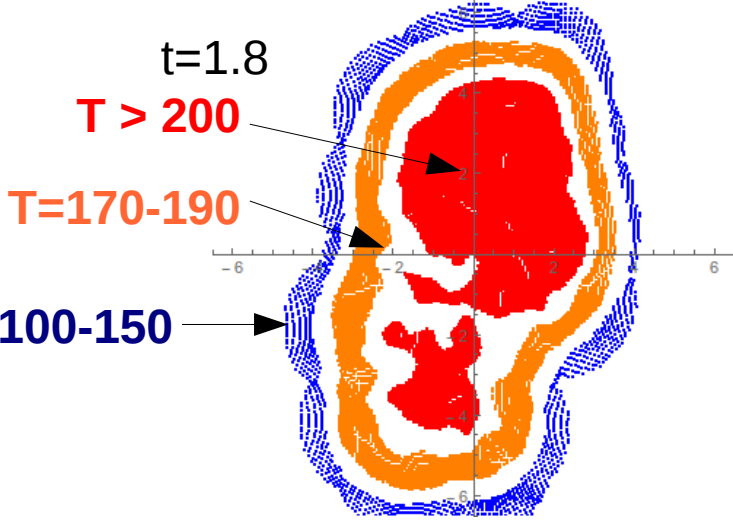
$T=150-190$



$t=1.8$   
 $T > 200$

$T=170-190$

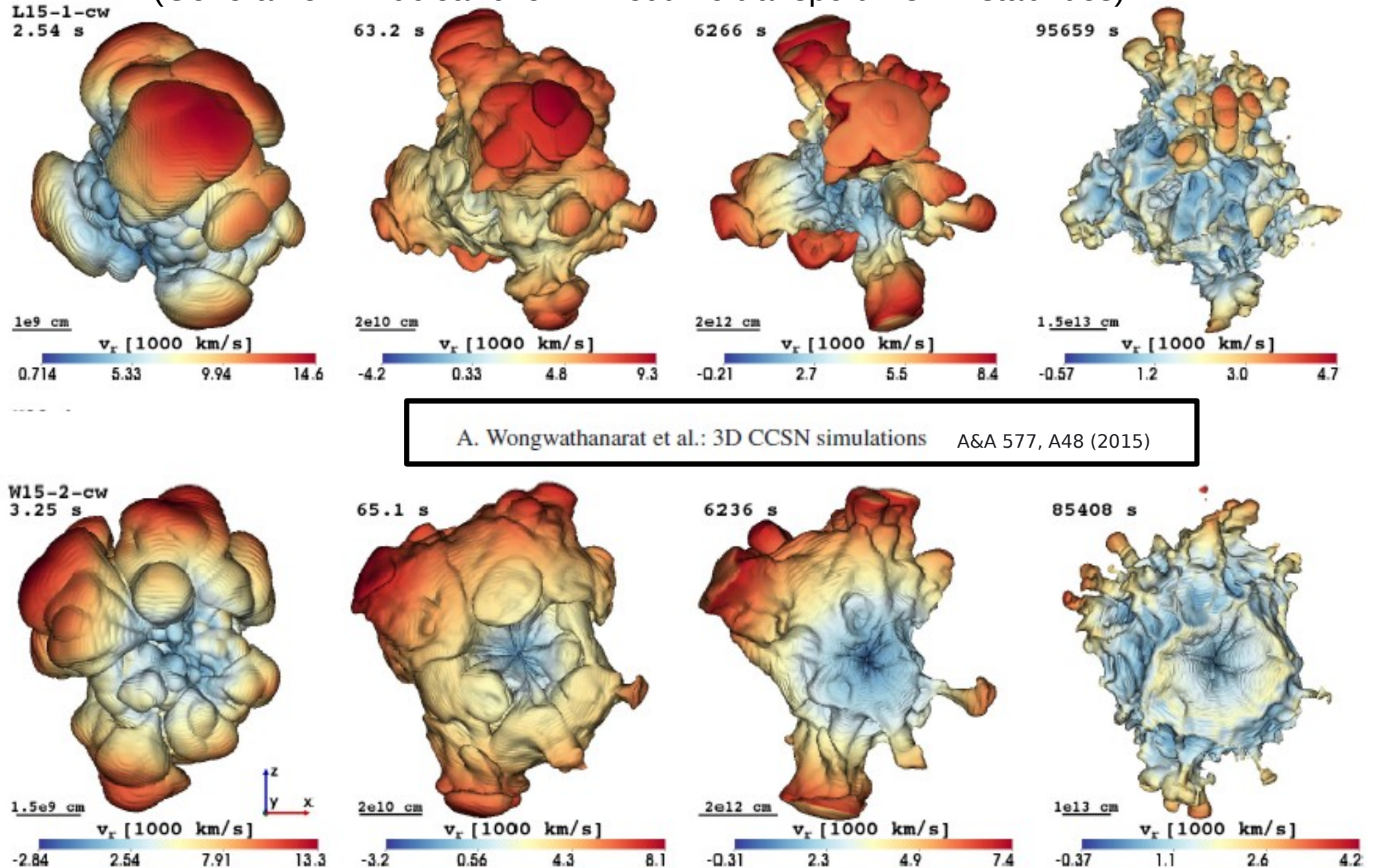
$T=100-150$



“Hard” jets probe  
Path Integrals  
of  $dE dx$   
through such  
Dynamic “Soft”  
 $pT < 2$  GeV  
Matter/Fields



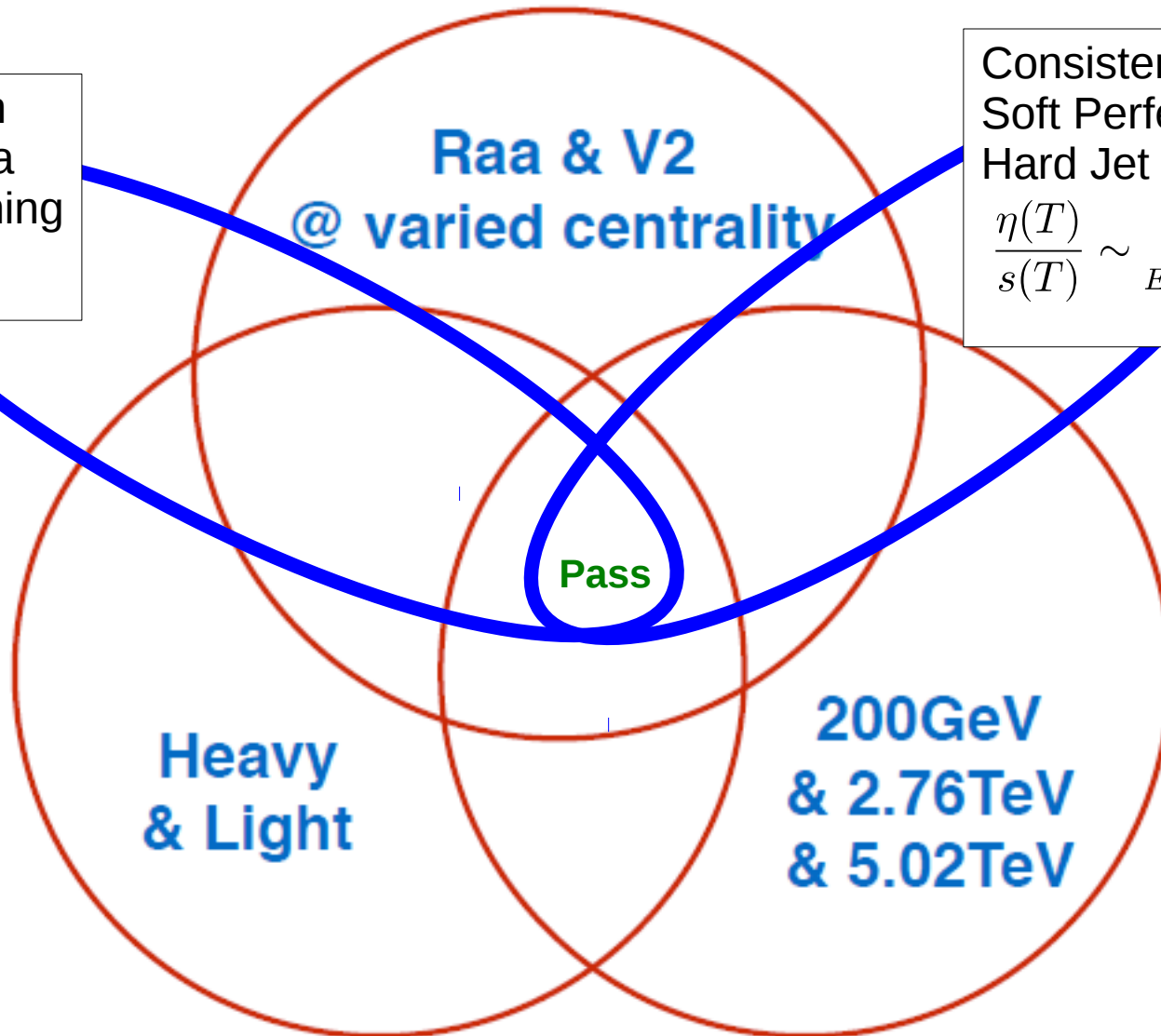
A+A ( $\eta, \phi$ ) problem similar to Multi Component problem of 3+1D Supernova Core Collapse  
 (General rel. + nuclear chem + neutrino transport + 3D instabilities)



**Fig. 7.** Snapshots displaying isosurfaces where the mass fraction of  $^{56}\text{Ni}$  plus n-rich tracer  $X$  equals 3% for model W15-2-cw (*top row*), L15-1-cw (*second row*), N20-4-cw (*third row*), and B15-1-pw (*bottom row*). The isosurfaces, which roughly coincide with the outermost edge of the neutrino-heated ejecta, are shown at four different epochs starting from shortly before the SN shock crosses the C+O/He composition interface in the progenitor star until the shock breakout time. The colors give the radial velocity (in units of  $\text{km s}^{-1}$ ) on the isosurface, with the color coding

# The Challenge to Every Model

Consistency with Lattice QCD data On EOS, Screening Polyakov, ...



Consistency between Soft Perfect Fluidity and Hard Jet Quenching

$$\frac{\eta(T)}{s(T)} \sim \lim_{E \rightarrow 3T} \left( \frac{T^3}{\hat{q}(E, T)} \right)$$

Review of current progress toward this level with CUJET3.1

## DGLV-CUJET framework for describing multi-parton scattering:

$$\begin{aligned}
 x_E \frac{dN_g^{n=1}}{dx_E} &= \frac{18C_R}{\pi^2} \frac{4 + N_f}{16 + 9N_f} \int d\tau n(\mathbf{z}) \Gamma(\mathbf{z}) \int d^2k \\
 &\times \alpha_s \left( \frac{\mathbf{k}^2}{x_+(1-x_+)} \right) \int d^2q \frac{\alpha_s^2(\mathbf{q}^2)}{\mu^2(\mathbf{z})} \frac{f_E^2 \mu^2(\mathbf{z})}{\mathbf{q}^2 (\mathbf{q}^2 + f_E^2 \mu^2(\mathbf{z}))} \\
 &\times \frac{-2(\mathbf{k} - \mathbf{q})}{(\mathbf{k} - \mathbf{q})^2 + \chi^2(\mathbf{z})} \left[ \frac{\mathbf{k}}{\mathbf{k}^2 + \chi^2(\mathbf{z})} - \frac{(\mathbf{k} - \mathbf{q})}{(\mathbf{k} - \mathbf{q})^2 + \chi^2(\mathbf{z})} \right] \\
 &\times \left[ 1 - \cos \left( \frac{(\mathbf{k} - \mathbf{q})^2 + \chi^2(\mathbf{z})}{2x_+ E} \tau \right) \right] \left( \frac{x_E}{x_+} \right) \left| \frac{dx_+}{dx_E} \right| \cdot (
 \end{aligned}$$

Original DGLV formalism has only quark/gluon scattering centers

We now include both color-electric and color-magnetic scattering centers.

$$x \frac{dN}{dx} \propto \dots \int_{q^2} \left[ \frac{n \alpha_s^2(q^2) f_E^2}{q^2 (q^2 + f_E^2 \mu^2)} \right] \dots \longrightarrow \left[ \frac{n_e (\alpha_s(q^2) \alpha_s(q^2)) f_E^2}{q^2 (q^2 + f_E^2 \mu^2)} + \frac{n_m (\alpha^e(q^2) \alpha^m(q^2)) f_M^2}{q^2 (q^2 + f_M^2 \mu^2)} \right]$$

Idea with CUJET3 is to *deform* DGLV HTL kernel with non-perturbative Lattice QCD data, fit (RAA,v2) data with min chi2 to fix max alpha and the ratio of magnetic/electric screen masses, and check if  $\hat{q}(E \rightarrow 3T, T)$  extrapolates near  $4 \pi T^3$  with

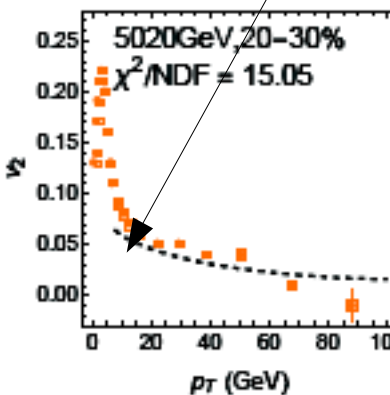
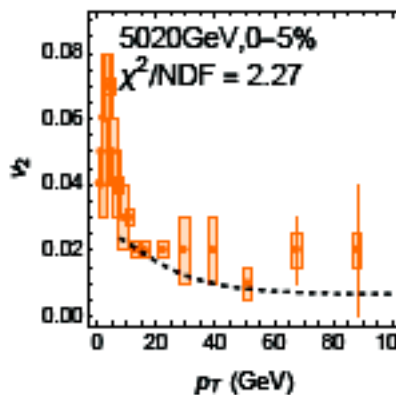
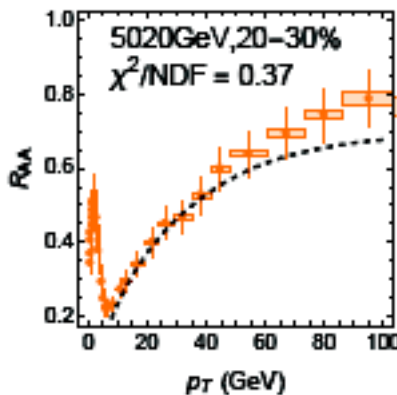
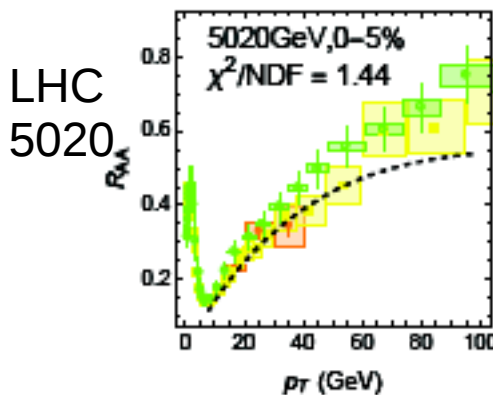
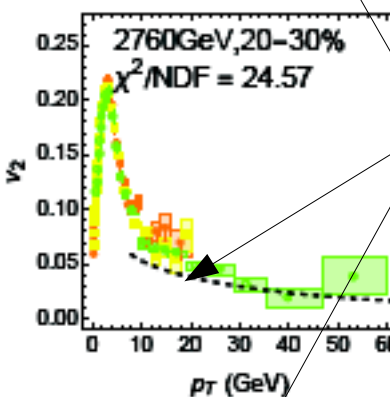
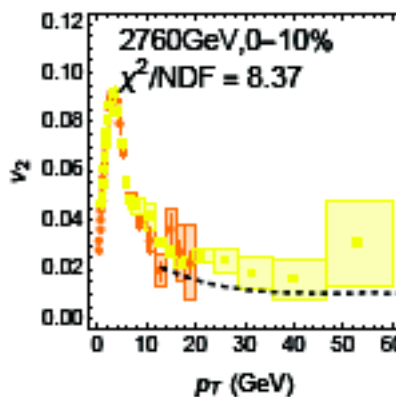
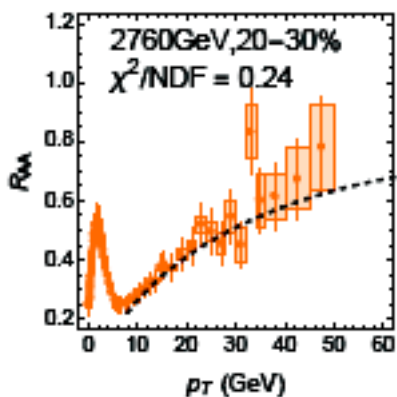
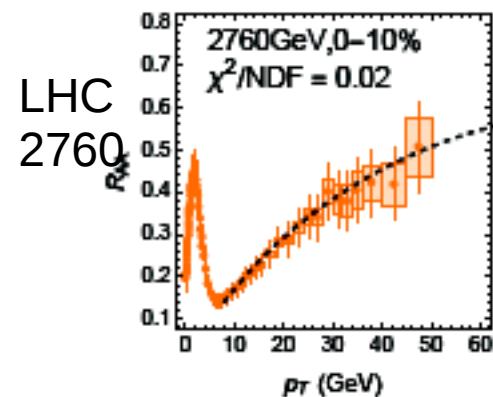
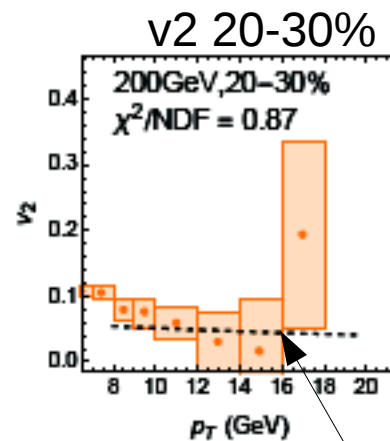
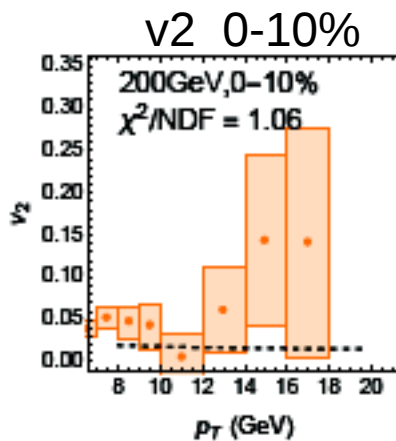
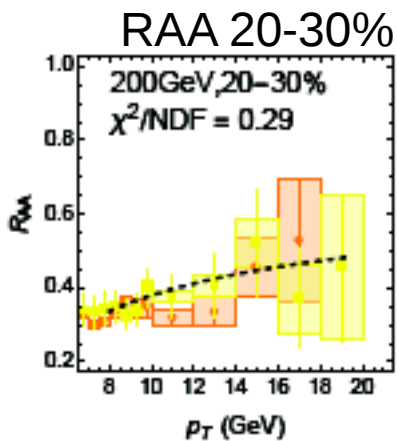
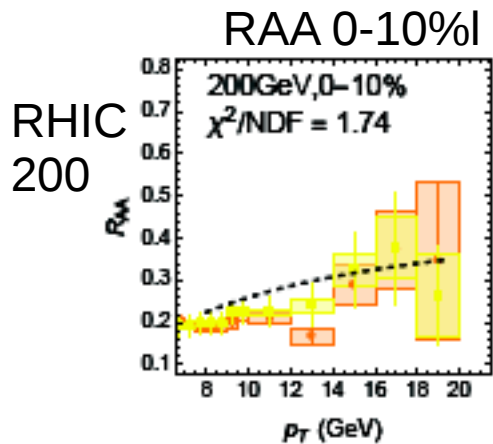
$$\frac{\eta(T)}{s(T)} \sim \lim_{E \rightarrow 3T} \left( \frac{T^3}{\hat{q}(E, T)} \right)$$



$\alpha_{\max} = 0.42$

$\chi^2/\text{d.o.f}$  for

VISH2+1  $\otimes$  CUJET2.1

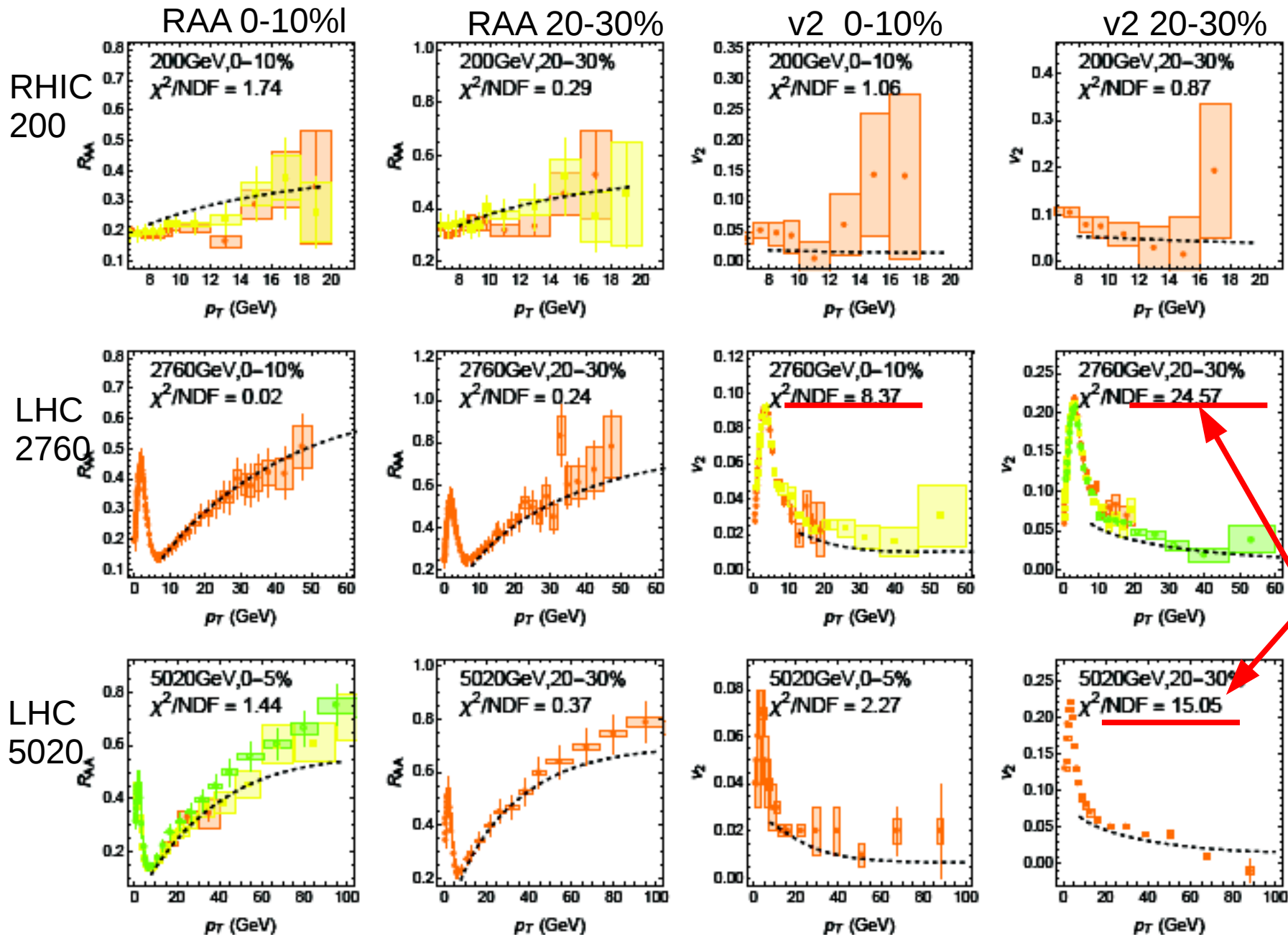


Looked Good by Eye Ball

$\alpha_{\max} = 0.42$

$\chi^2/\text{d.o.f}$  for

VISH2+1  $\otimes$  CUJET2.1



However  $\chi^2 > 15$   
Falsified Model !!



# CUJET3.0 status at QM15 (J.Xu, J Liao, mg, NPA956 (2016) ) improved

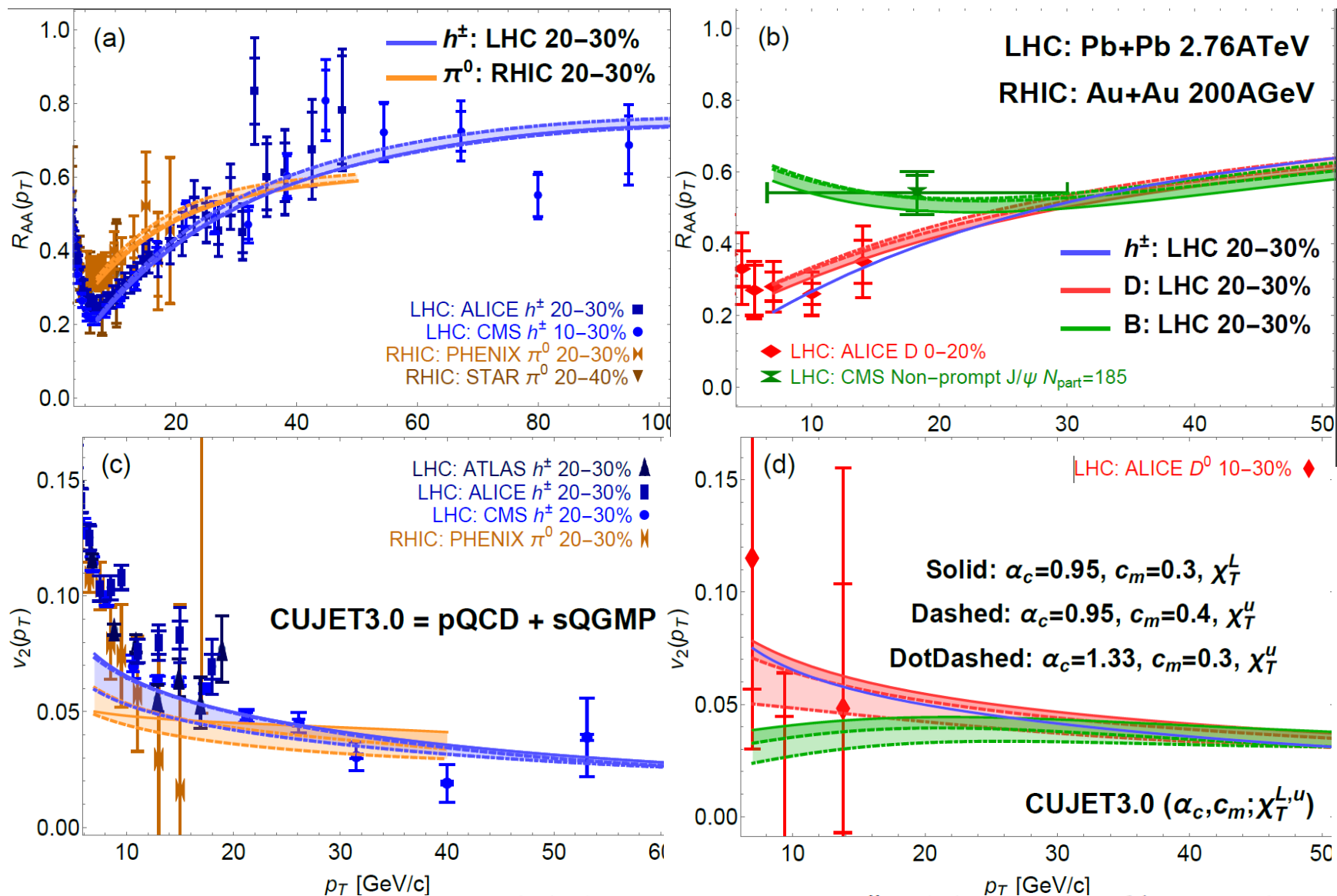


Fig. 2. (Color online) CUJET3.0 results of (a) light hadron (LH, neutral pion  $\pi^0$  and charge particle  $h^\pm$ )'s  $R_{AA}$ , (b) open heavy flavor (HF,  $B$  meson and prompt  $D$  meson)'s  $R_{AA}$ , (c) LH's  $v_2$ , and (d) HF's  $v_2$ , at high  $p_T > 8$  GeV in semi-peripheral A+A collisions, compared with data from RHIC and LHC [2]. The variations of predicted jet quenching observables from different schemes within CUJET3.0 suggest that data on high  $p_T$  leading hadron  $R_{AA}$  and  $v_2$  in heavy-ion collisions can rigorously constrain the nonperturbative chromo-electric and chromo-magnetic structure of the QCD matter near  $T_c$ , and provide critical information about color confinement.

CUJET3.0  $\hat{q}$  at QM15 was consistent with Perfect fluidity near  $T_c$  (J.Xu, J Liao, MG (2016) )

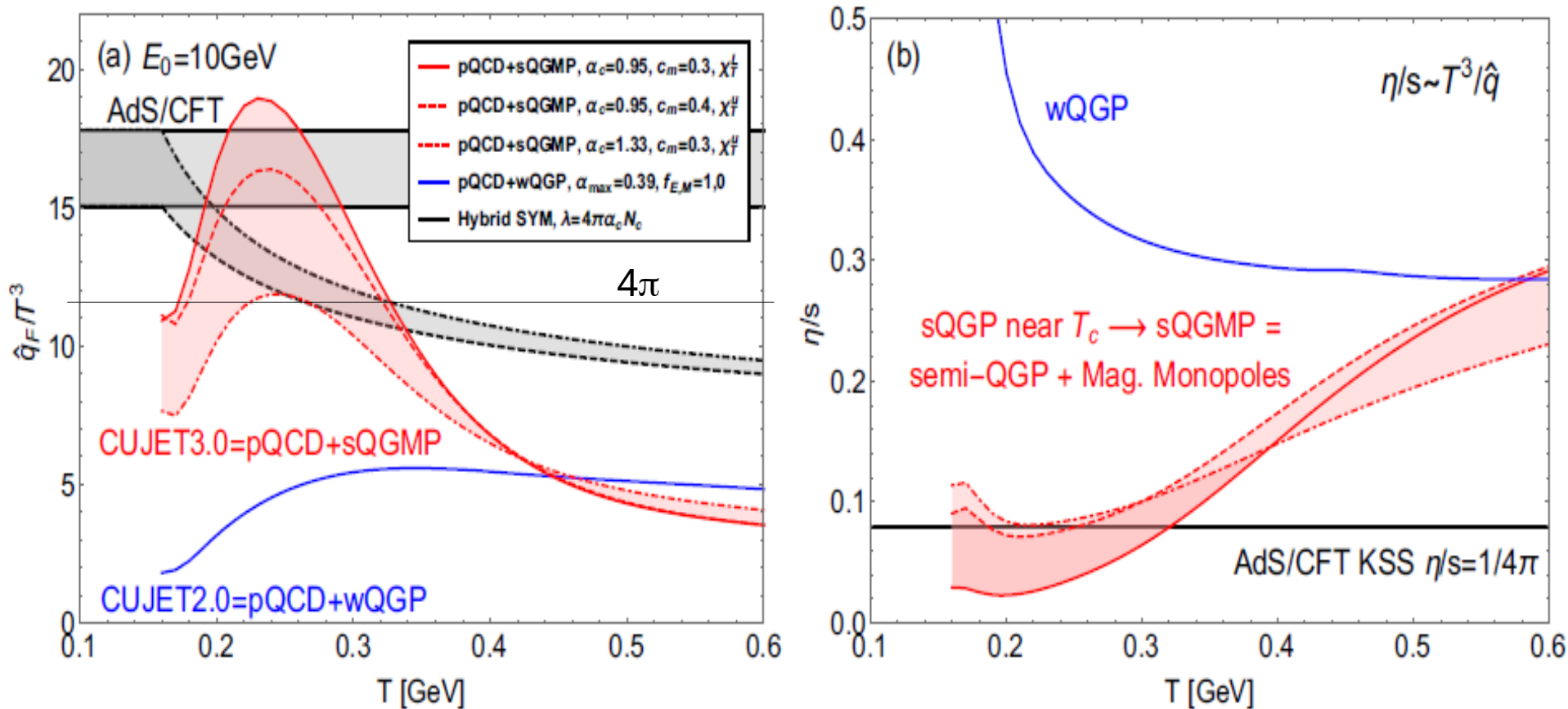
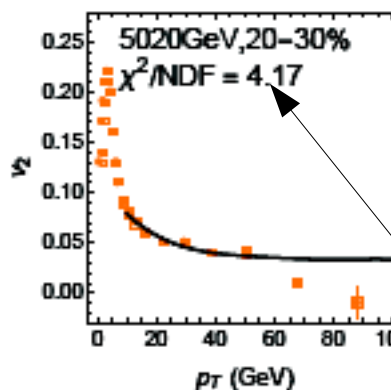
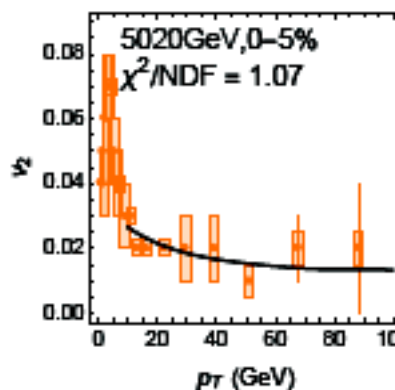
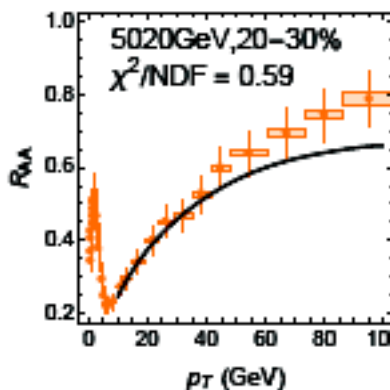
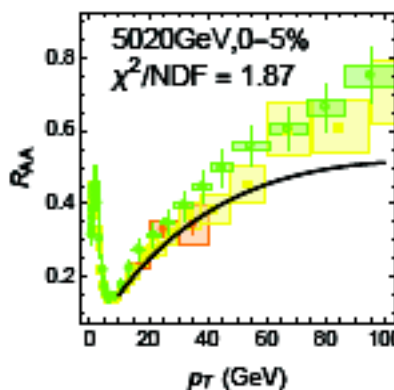
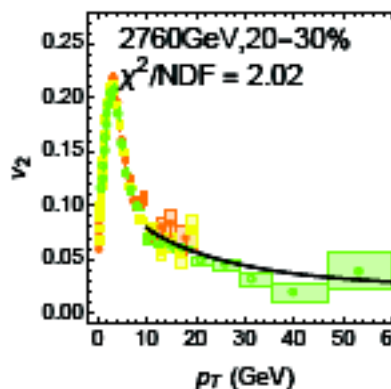
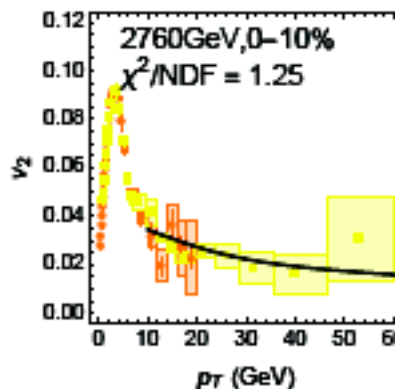
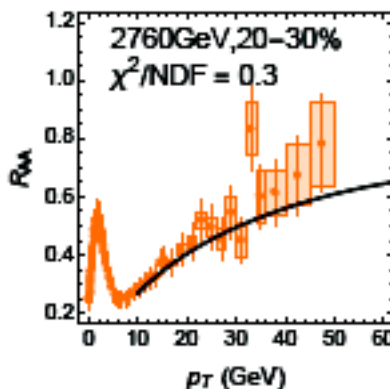
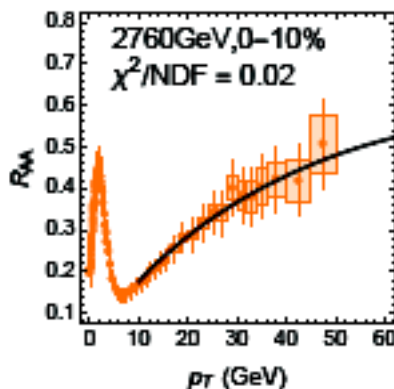
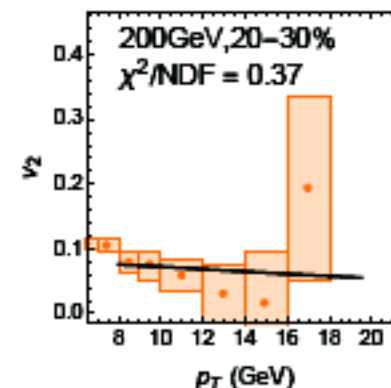
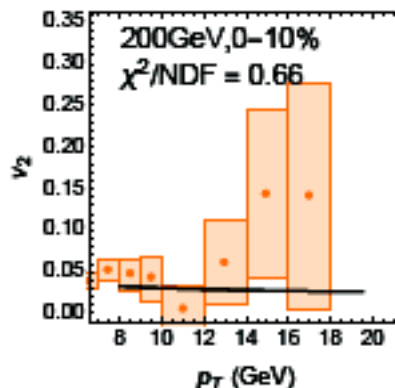
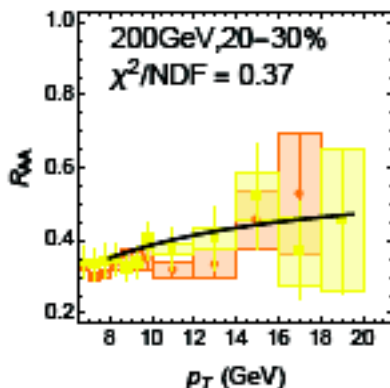
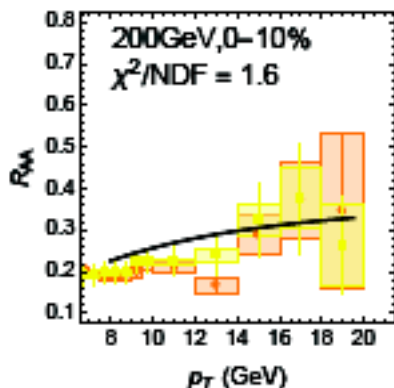


Fig. 3. (Color online) (a) The temperature dependence of the scaled jet transport parameter  $\hat{q}/T^3$  for a quark jet (in the fundamental representation  $F$  of  $SU(N_c=3)$ ) with initial energy  $E_0 = 10$  GeV in various schemes within the CUJET3.0 framework, compared with the CUJET2.0 counterpart, as well as  $N = 4$  Supersymmetric Yang-Mills (SYM)  $\hat{q}_{SYM}$  results from leading order (LO) AdS/CFT calculations ( $\hat{q}_{SYM} = [\pi^{3/2}\Gamma(3/4)/\Gamma(5/4)] \sqrt{\lambda} T_{SYM}^3$ ) [15]. Note that  $3T_{SYM}^3 \approx T^3$  because of different number of degrees of freedom in  $N_c = 3$  SYM and three-flavor QCD [16]. The gray band with dashed black edges corresponds to using 't Hooft coupling  $\lambda = 12\pi\alpha_s(Q^2)$ . (b) The shear viscosity to entropy density ratio  $\eta/s$  estimated in the kinetic theory extrapolation  $\eta/s \sim T^3/\hat{q}$  from jet quenching parameters in panel (a). Note that  $T_c = 160$  MeV. In CUJET3.0, a  $(\hat{q}_F/T^3)_{max}$  and  $(\eta/s)_{min}$  appear at  $T \sim 1.4T_c$  where the scaled number density of emergent chromo-magnetic monopoles near  $T_c$  peaks. The  $(\eta/s)_{min}$  is influenced by the EM fractions. Its value in both  $\chi_T^{L,u}$  schemes converge to approximately the KSS quantum bound  $\eta/s = 1/4\pi$  [4]. At high  $T$ , the  $\eta/s$  from sQGMP and weakly-coupled QGP (wQGP) coincide because of similar color screening structures.

$(\alpha_c, c_m) = (0.9, 0.25)$



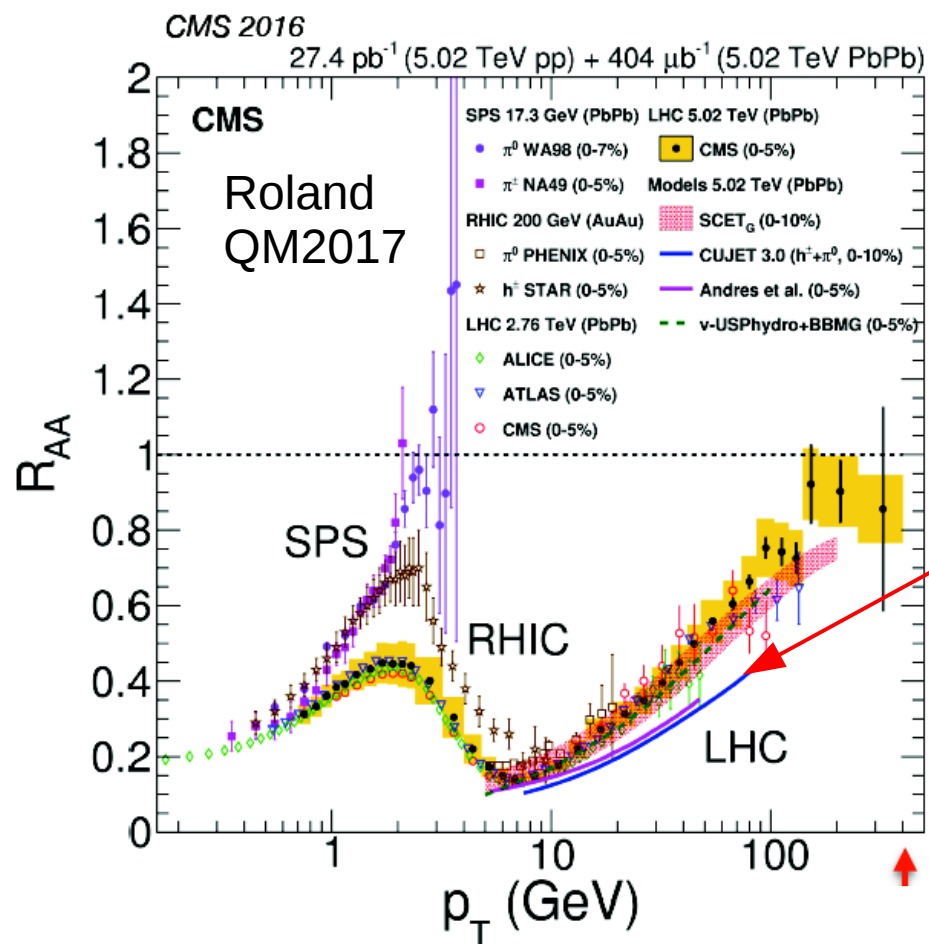
Note  
LHC2 data  
are much  
Higher  
Precision !

v2 CMS  
challenge  
now to 1%  
accuracy?!

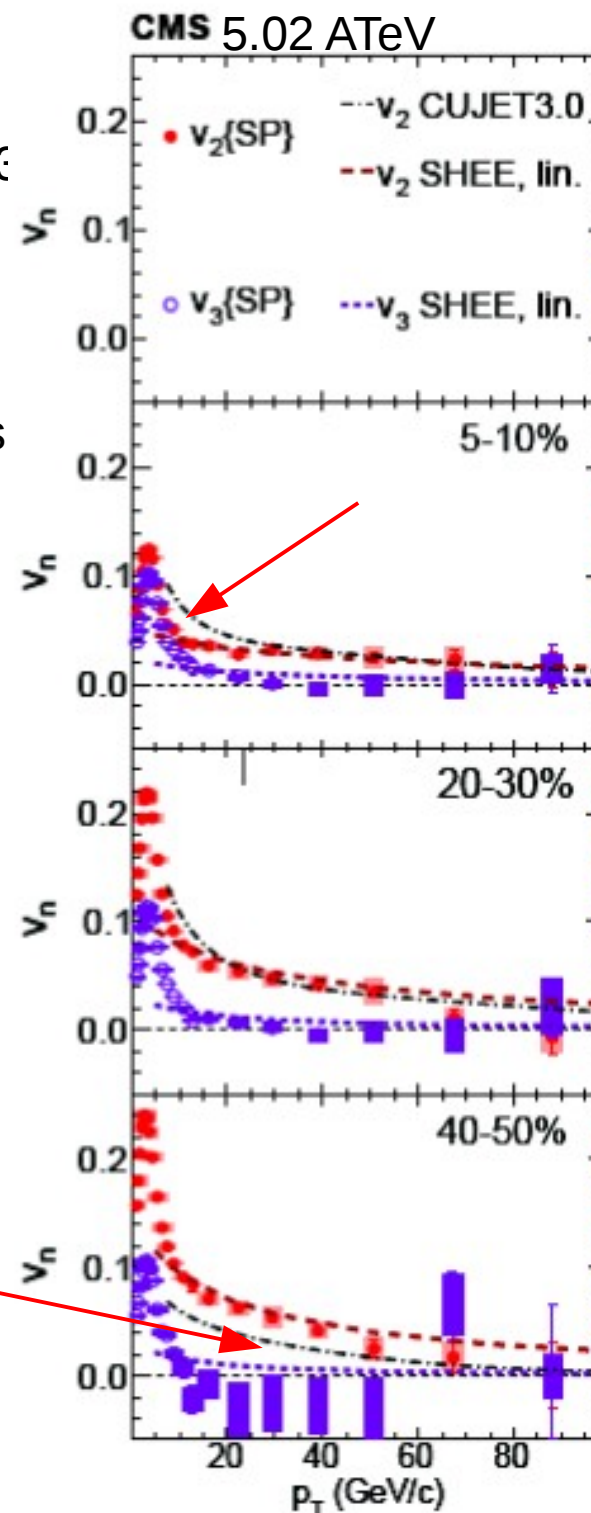
At IS16 and QM17 CMS discrepancies of CUJET3.0 reported for 5ATeV RAA and  $v_2$

**Shuzhe Shi** found 3 bugs in CUJET3.0 and corrected now in CUJET3.1

- 1) Initial parton spectra for 5.02 ATeV were erroneously read from a Pythia file rather than from pQCD Wang code used previously
- 2) VISHNU hydro fluid grid was misread into CUJET3.0 path integrals
- 3) Initial parton spectra cut off set at 200 instead of 400 GeV

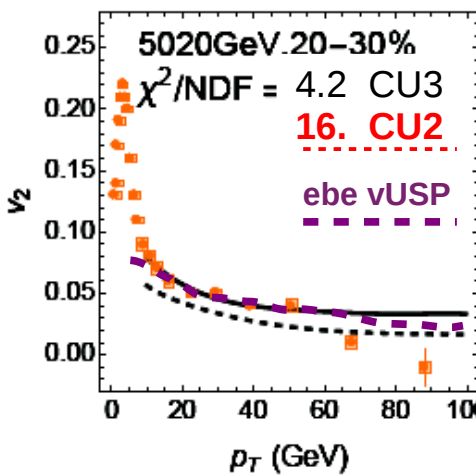
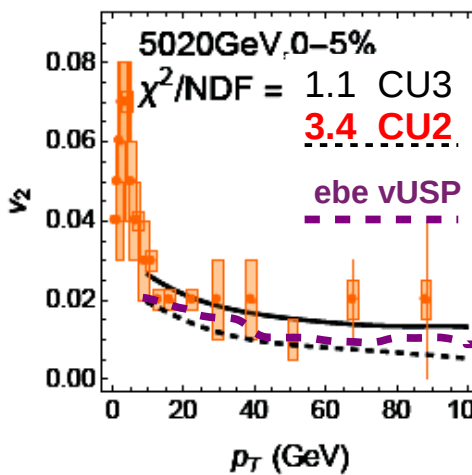
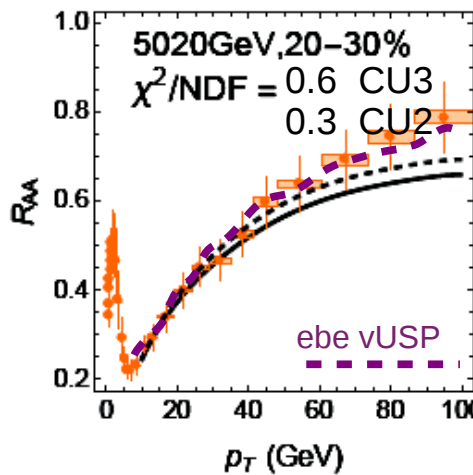
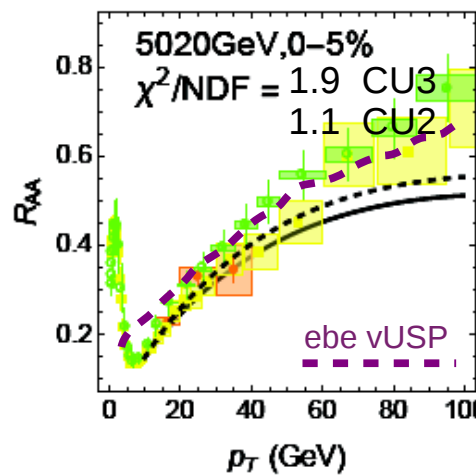
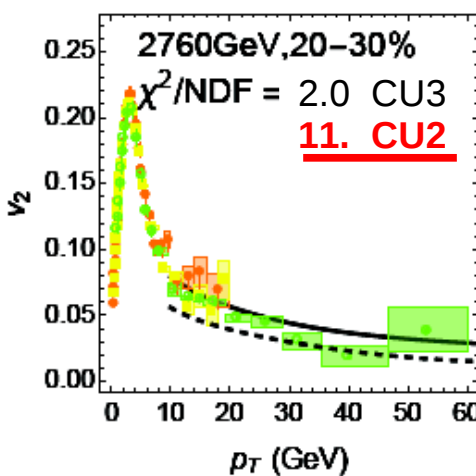
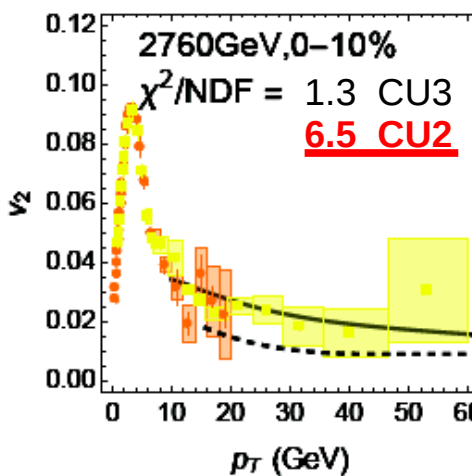
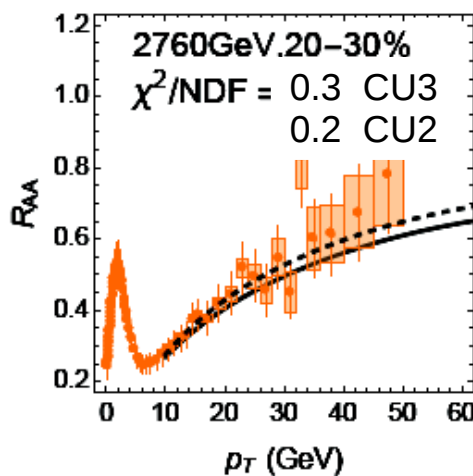
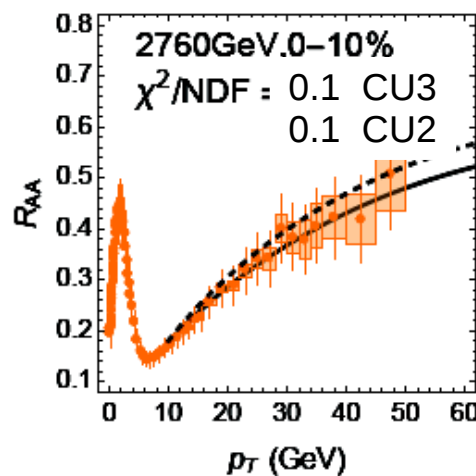
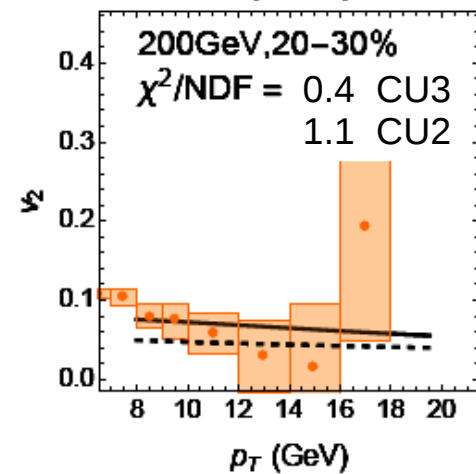
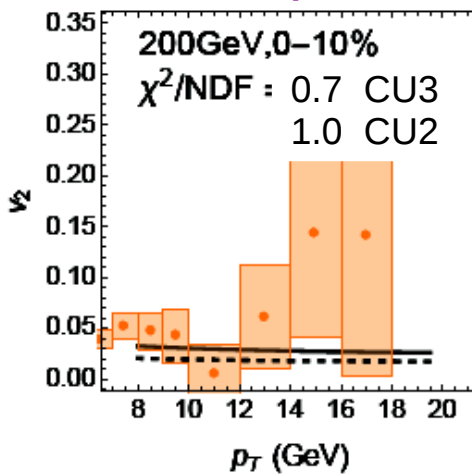
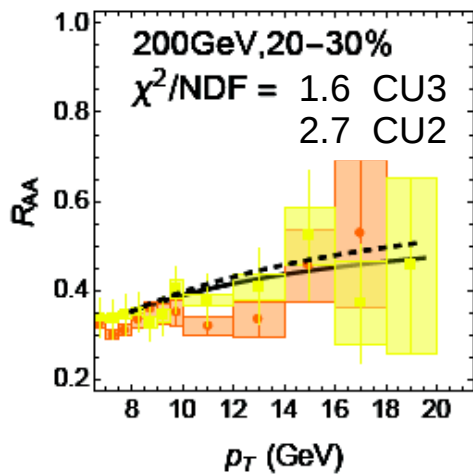
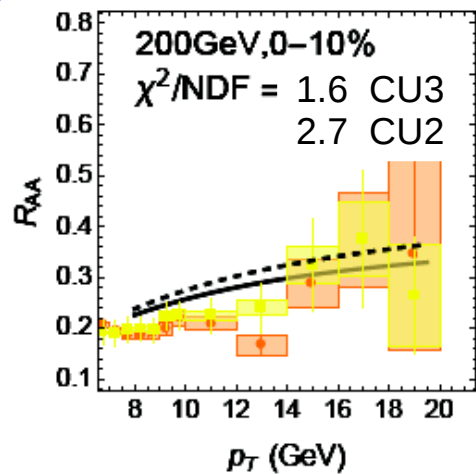


Bugs led at 5TeV to  
 1) overquench RAA  
 2) predict wrong  
 Centrality dep of  $v_2$





pQGP/CUJET2.1 vs sQGMP/CUJET3.1 vs RHIC&LHC vs ebe/vUSP+BBMG (J.Noronha-Hostler PRC95 (2017))

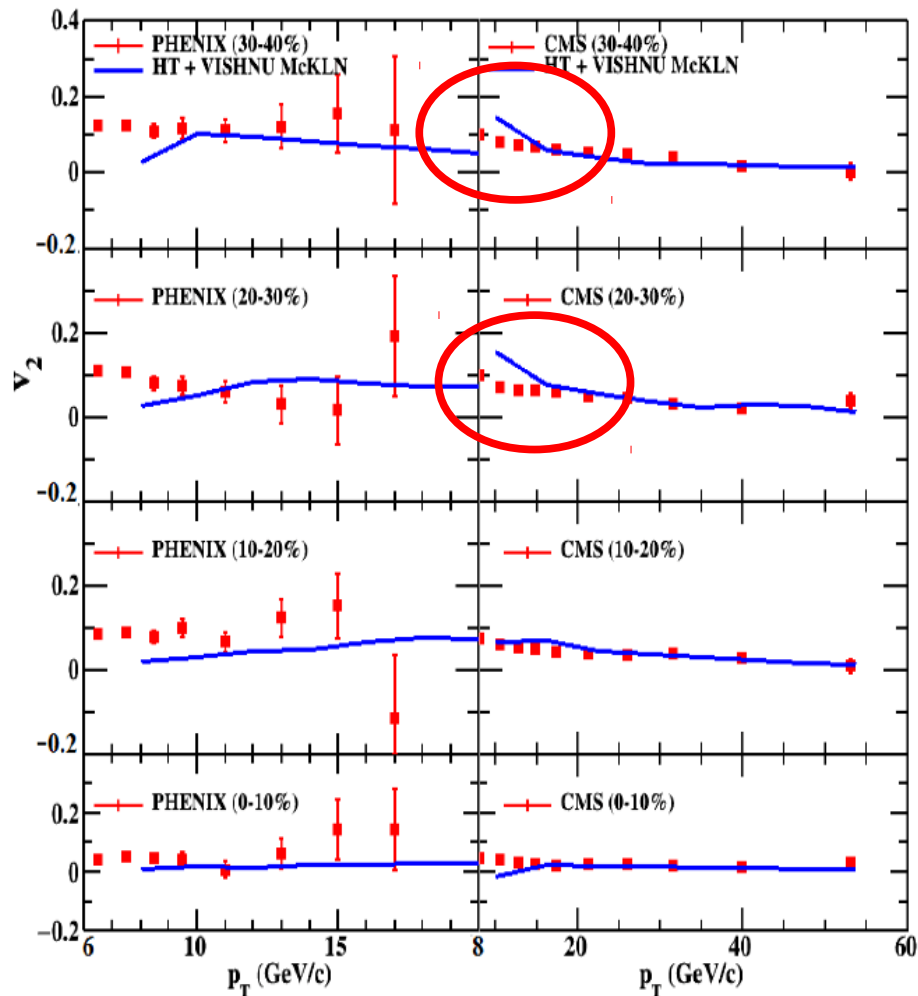
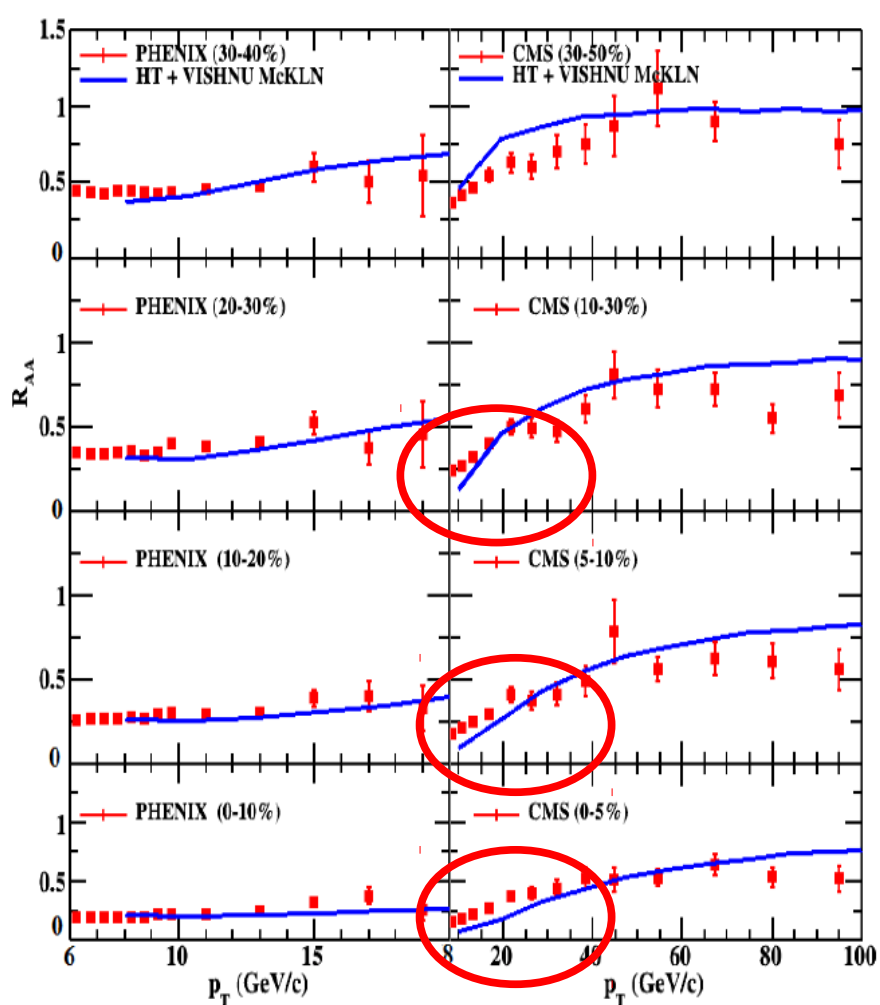




# Recent HigherTwist $xG(x, Q^2(L))$ model should also be compared via $\chi^2/\text{dof}$

E.Bianchi, J.Elledge, A.Kumar, A.Majumder, G.Y.Qin and C.Shen,

"The  $x$  and  $Q^2$  dependence of  $\hat{q}$ , quasi-particles and the JET puzzle" arXiv:1702.00481 [nucl-th]



Appears to over quench LHC  $R_{AA}(p_T < 40)$  in central

And over predict  $v_2(p_T < 20)$  in semi-central

Needs functional variation  $xG(x, Q)$  to minimize  $\chi^2(\text{LHC})$  ?

Combined RHIC+LHC1+LHC2 data RAA+v2 fit  $\chi^2(\alpha_c, c_m)$

Assuming slow Polyakov color electric semi-q+g liberation  $\chi_T^L = c_q L + c_g L^2$

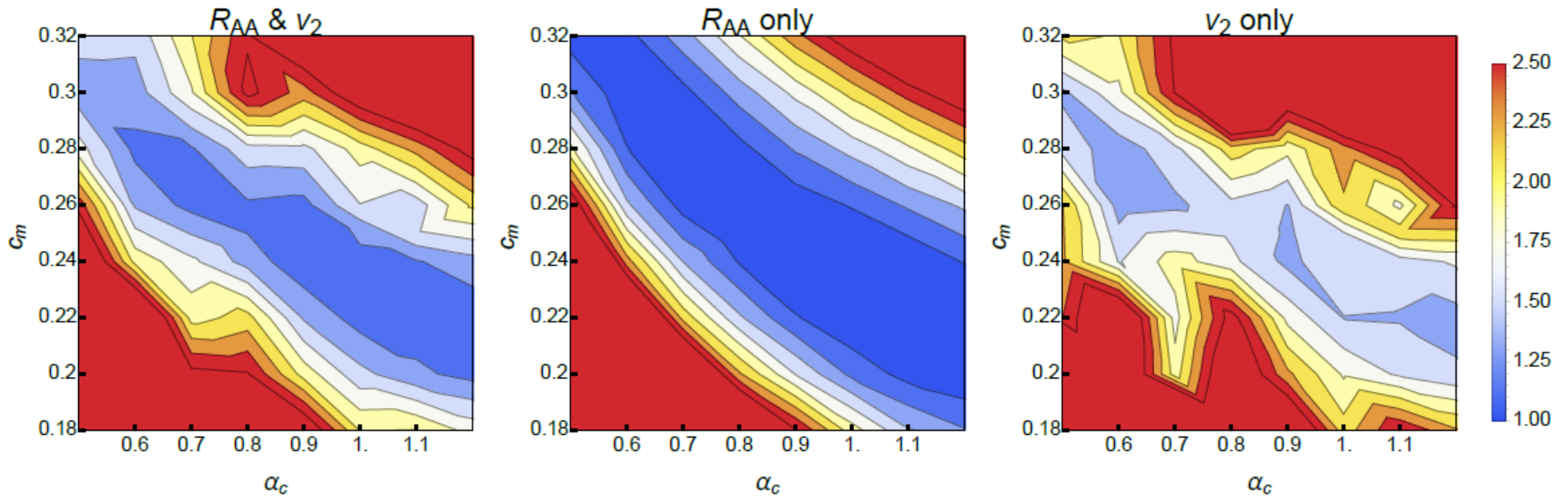
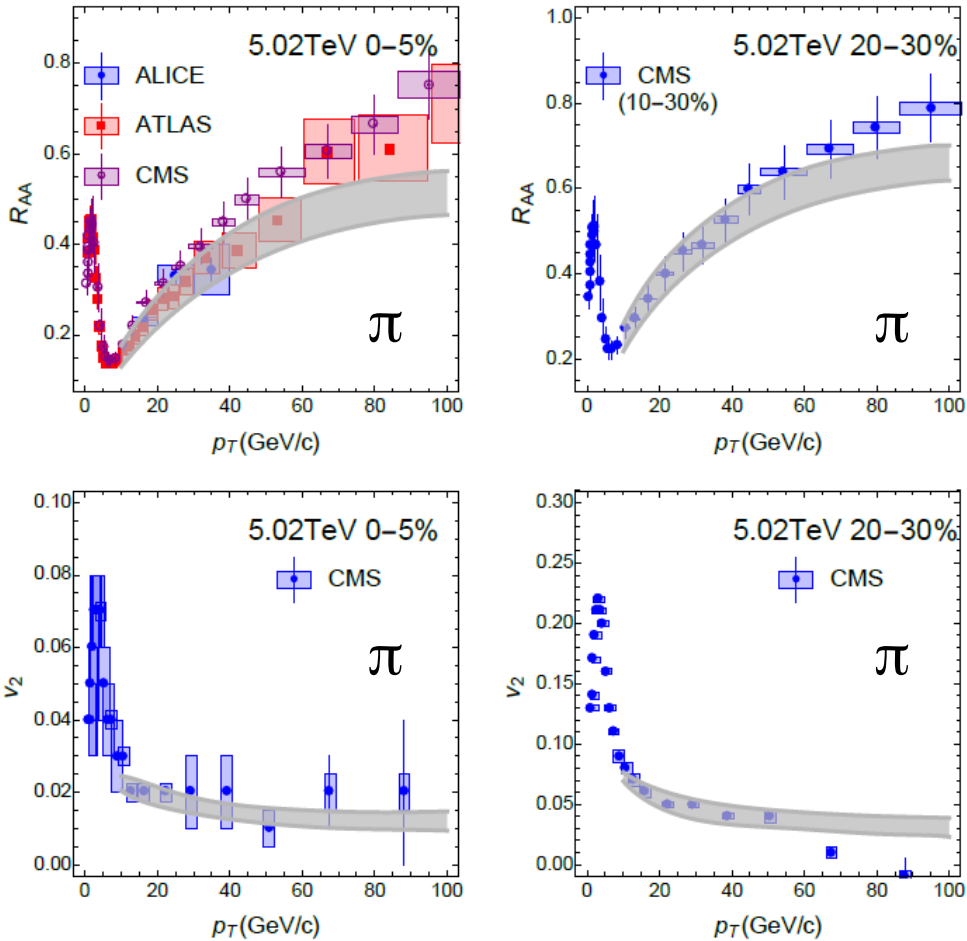


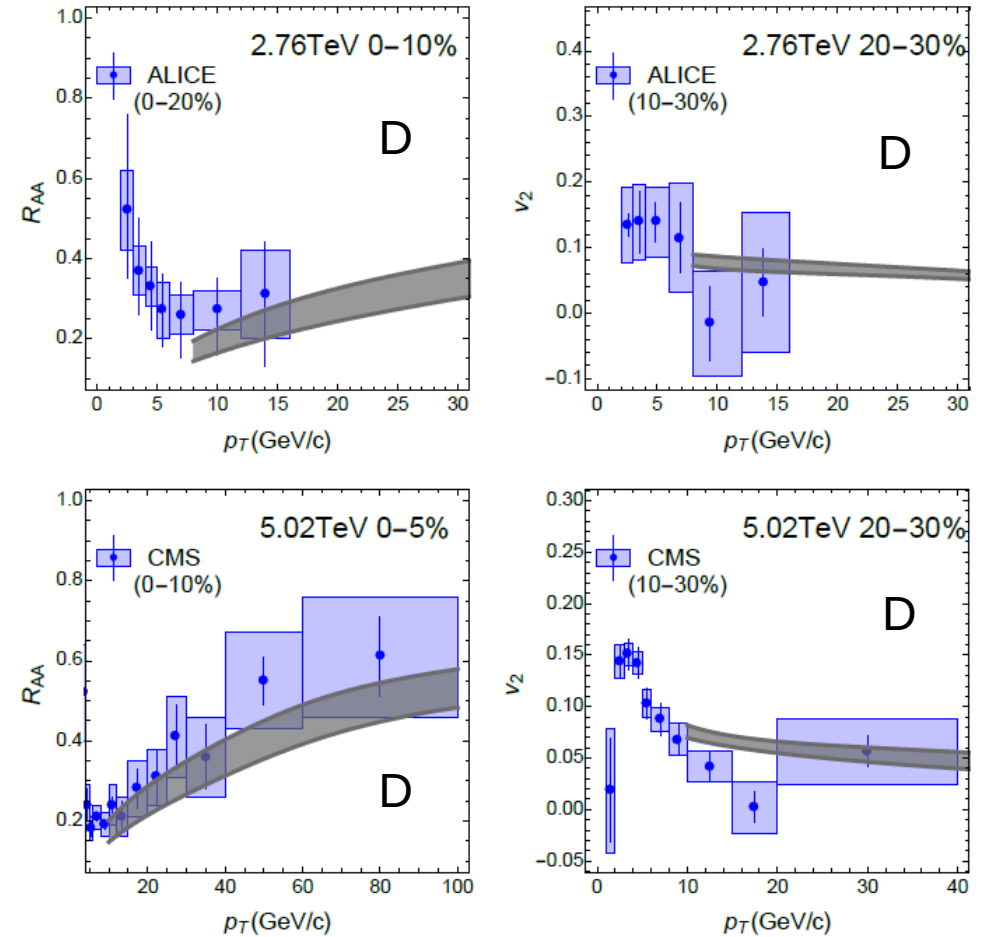
Fig. 1. (color online) The  $\chi^2/d.o.f$  distribution on  $(\alpha_c, c_m)$  parameter plane, from comparing CUJET3 results for pion high  $p_T$  observables with central and semi-central data from RHIC 200GeV, LHC 2.76TeV as well as 5.05TeV collisions: (left) including both  $R_{AA}$  and  $v_2$  data; (middle) including only  $R_{aa}$ ; (right) including only  $v_2$ .

The main next open question next is how will inclusion of event-by-event fluctuations Modify CUJET4.0 = ebe CUJET3.1 predictions ?

central and semi-central  $R_{AA}$  and  $v_2$  of high  $p_T$  pions

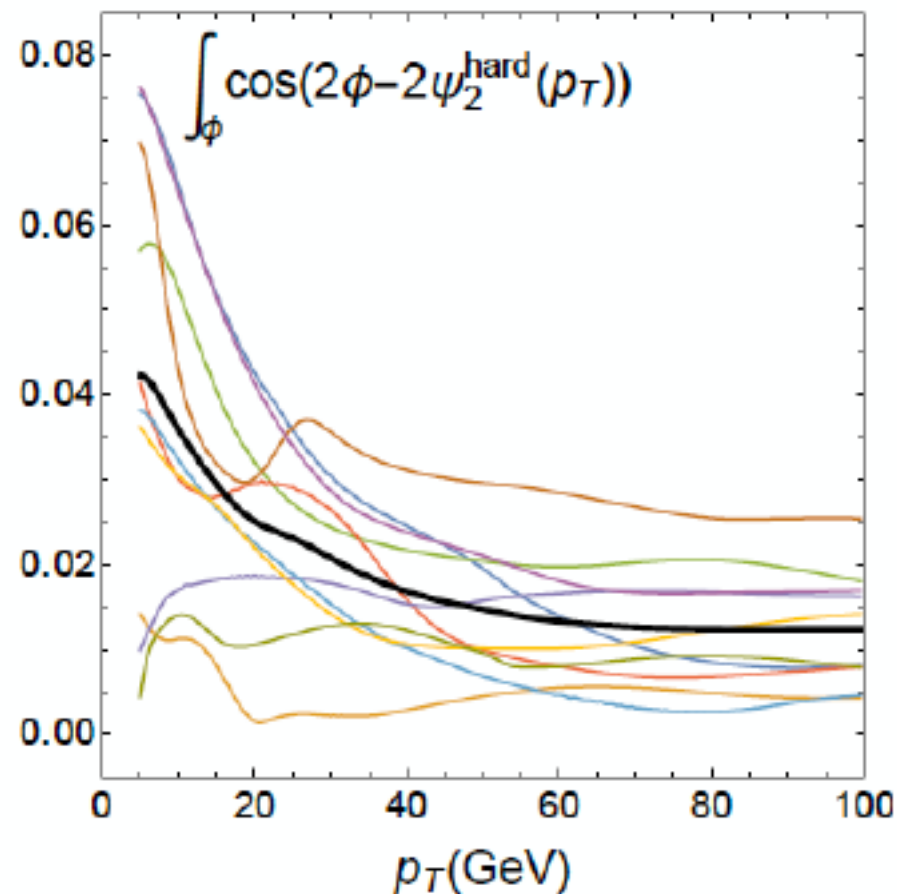
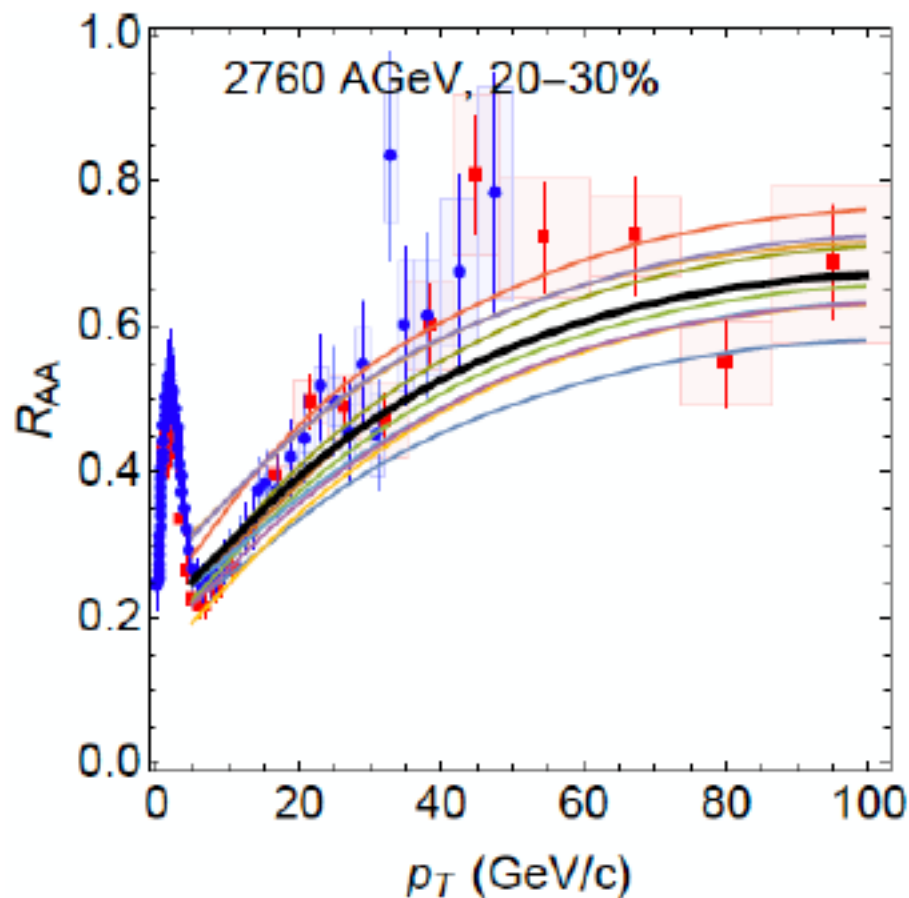


central and semi-central  $R_{AA}$  and  $v_2$  of high  $p_T$  D



# Event-By-Event Jet Quenching

*A first try of e-by-e CUJET3 exercise  
(for 10 events – computationally expensive!)*

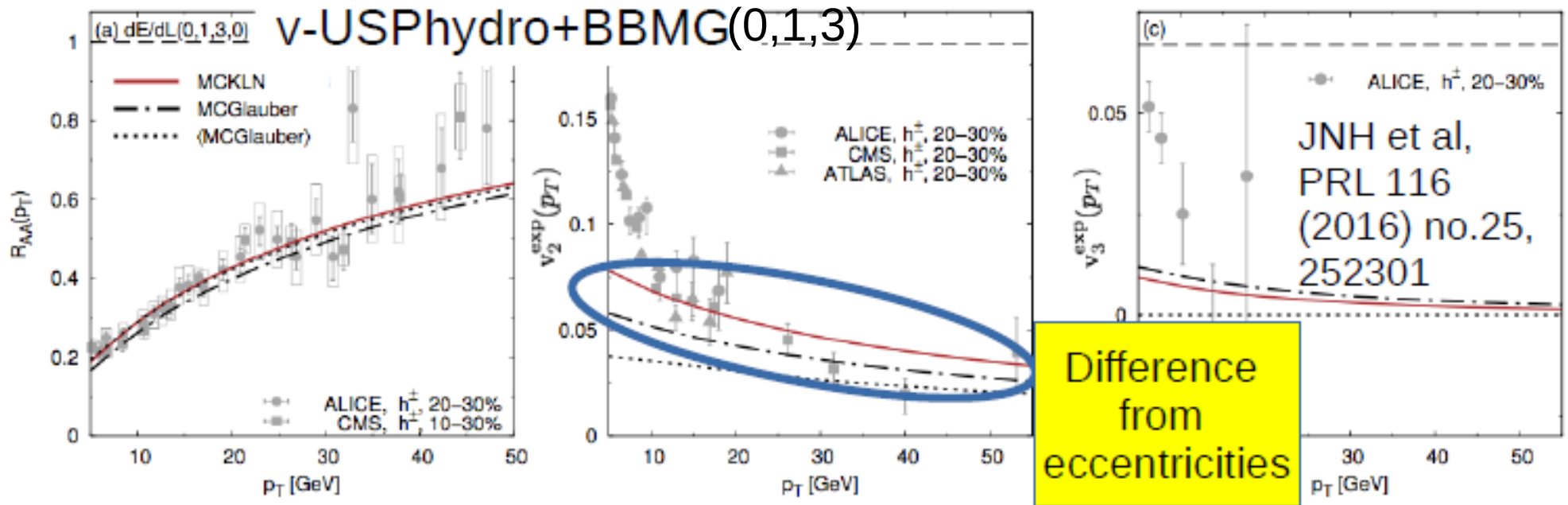


[Hydro background from Jaki Noronha-Holster]

# Event-by-event hydrodynamics + jet energy loss: A solution to the $R_{AA} \otimes v_2$ puzzle

Jacquelyn Noronha-Hostler (Houston U.), Barbara Betz (Frankfurt U.), Jorge Noronha (Sao Paulo U.), Miklos Gyulassy (LBNL, NSD & Columbia U. & CCNU, Wuhan, Inst. Part. Phys.). Feb 11, 2016. 6 pp.

Published in *Phys.Rev.Lett.* 116 (2016) no.25, 252301



Good fit to  $R_{AA}+v_2+v_3$ ! With simple perturbative QCD  $dE/dx = k L^1 T^3$  linear path depend

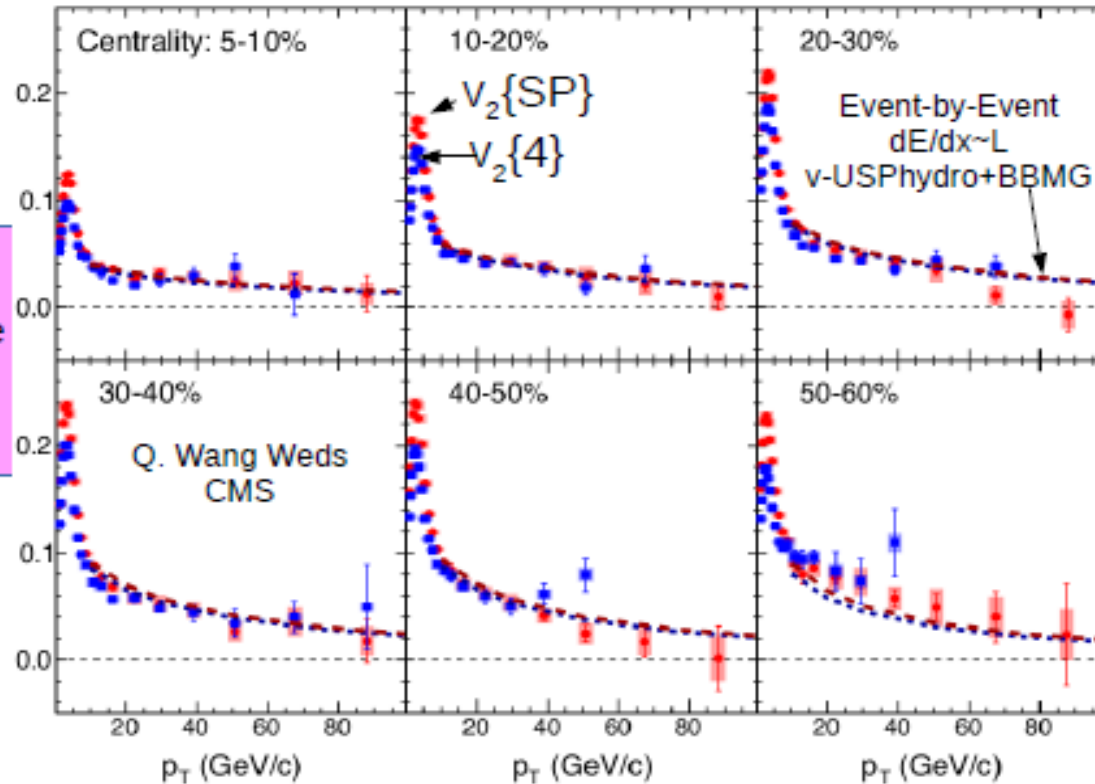
- Initial Conditions+Hydrodynamics that fit soft  $v_n$ 's  $\rightarrow$  match high  $p_T$  flow! But pQCD  $\hat{q}(3T_c, T_c)$  does not extrapolate to  $4 \pi T_c^3$
- Other groups currently checking: EKRT+Quenching Weights and v-USPhydro+CUJET3.0



# Predictions confirmed with CMS data for LHC Run 2

Over full range of centralities at 5ATeV

First multi-particle cumulants at high  $p_T$ !



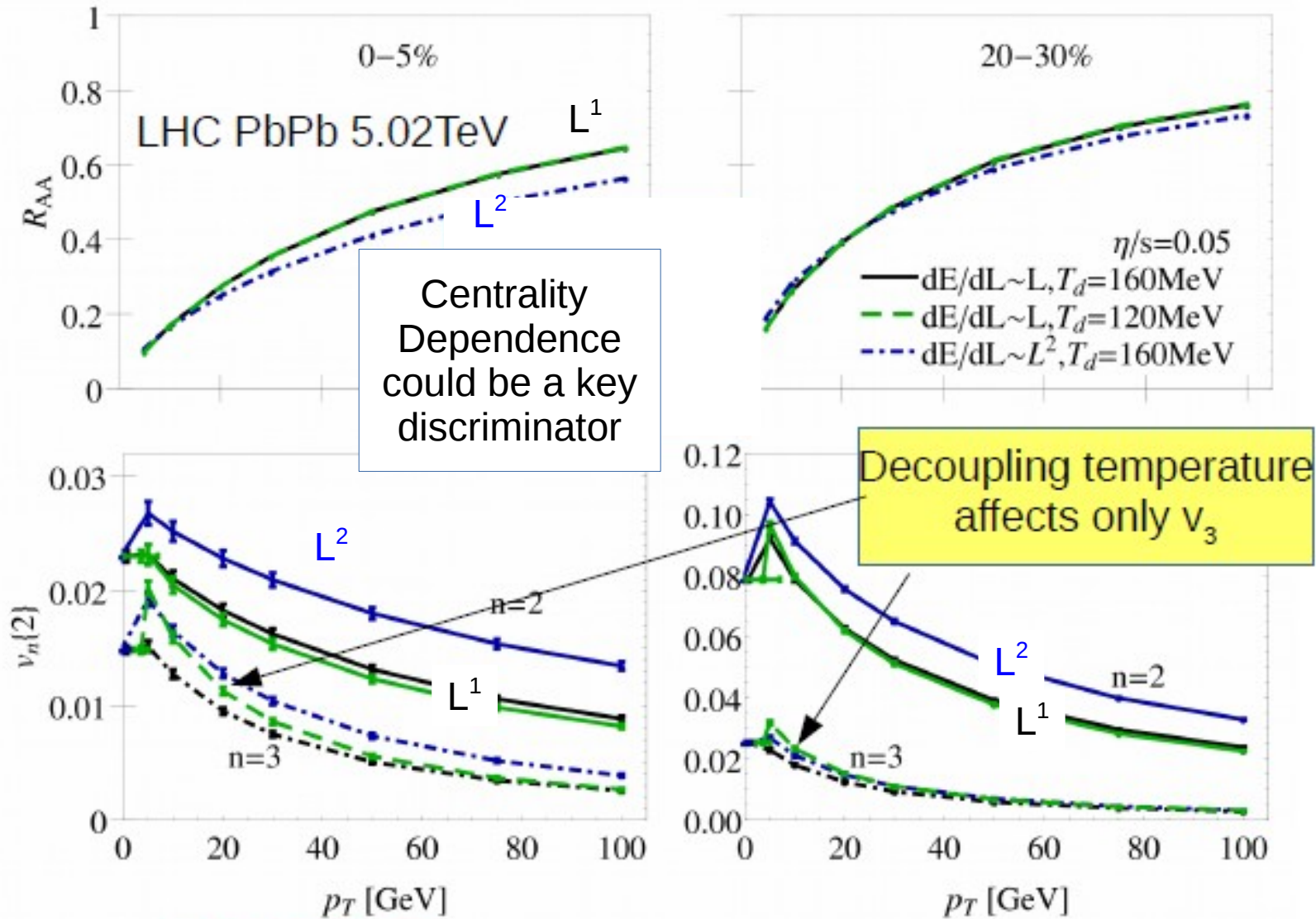
$\frac{v_2\{4\}(p_T)}{v_2\{SP\}(p_T)}$  encodes soft vs. hard fluctuations

## References

CMS  $v_n m(p_T)$  arXiv:1702.00630; v-USPhydro+BBMG JNH, Betz, Gyulassy, Luzum, Noronha, Portillo, Ratti arXiv:1609.05171

# What are $R_{AA}$ and $v_n$ 's sensitive to?

Test weak HTL pQCD like  $dE/dx \sim L^1 T^3$  versus infinitely coupled AdS like  $dE/dx \sim L^2 T^4$

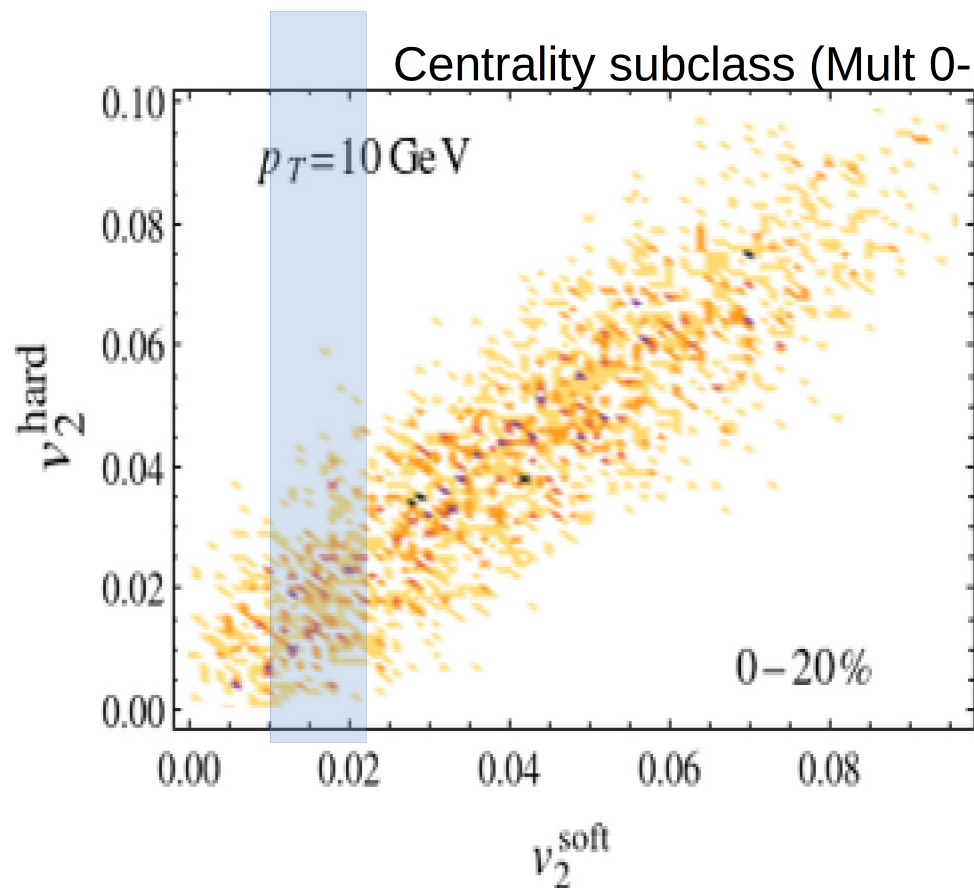


## SHEE : Soft-Hard Event Engineering

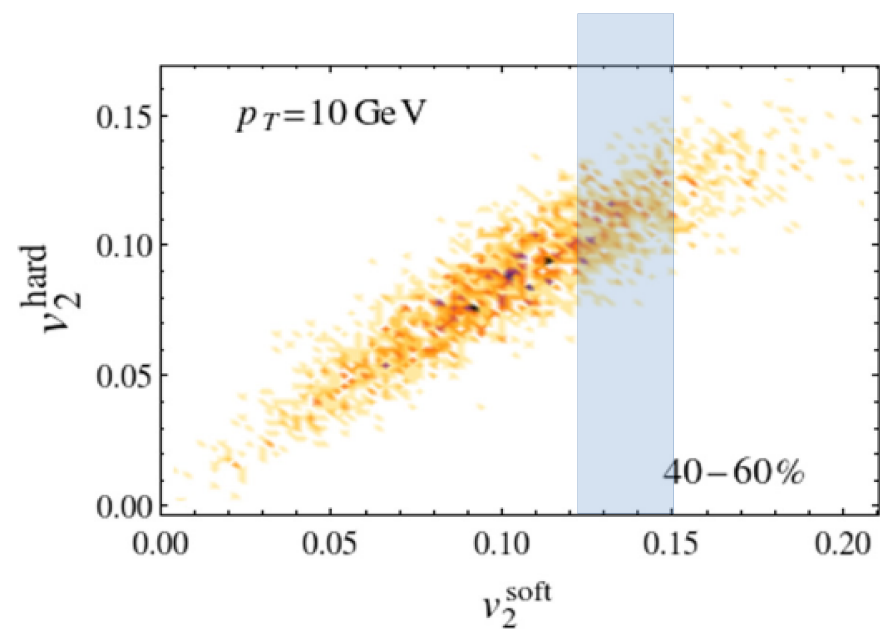
In addition to centrality bins based only on soft Multiplicity or ET binning more information could be extracted from subclasses of event based on soft  $v_2$ ,  $v_3$  .. bins  
In which hard jet response is tested subclasses of fluctuating geometries.

PHYSICAL REVIEW C **95**, 044901 (2017)

Centrality subclass (Mult 0-20%, less eccentric  $v_2^{\text{soft}}$  0.01-0.02)



Centrality subclass  
(Mult 40-60%, more eccentric  $v_2^{\text{soft}}$  0.12-0.15)



Status as of today:

There exists (at least) two combinations of Soft  $v_n$  + Hard RAA+ Hard  $v_n$  dynamical models

That are compatible at  $\chi^2 < 4$  level with RHIC+LHC1+LHC2 data sets at 0-10% and 20-30%

1) ebe MCKLN+vUSPH+BBMG(L<sup>1</sup>) : J.Noronha-Hostler et al, PRL116(2016),PRC95(2017)

2) ave MCKLN+VISH2+1 +CUJET3.1: S.Shi, et al QM17; arXiv:1704.04577;  
3.0 : J.Xu et al ; JHEP1602 (2016)

1) is compatible with aexp data including  $v_3$ , but the weak L<sup>1</sup> jet dynamics  $\hat{q}(E,T)$  does not extrapolate to the Perfect Fluidity limit near  $T_c$  as  $E \rightarrow 3T_c$ .  
The jet-medium interaction L<sup>1</sup> does not know about Lattice QCD physics near  $T_c$ .

The strong coupling AdS/CFT L<sup>2</sup> version is compatible to Perfect Fluidity but LHC2 CMS hints that maybe they can rule this out! Centrality dependence appears as key observable

2) sQGMP via corrected CUJET3.1 version is also compatible with present data  
And builds in all lattice QCD thermal data and does extrapolate near  $T_c$  to Perfect fluidity.  
However, 3.1 still has not taken into account ebe fluctuations and hence fails on odd  $v_n$ .  
Shuzhe Shi is developing CUJET4 = ebe-vUSPH/VISHNU + CUJET3.1 (numerically challenging)

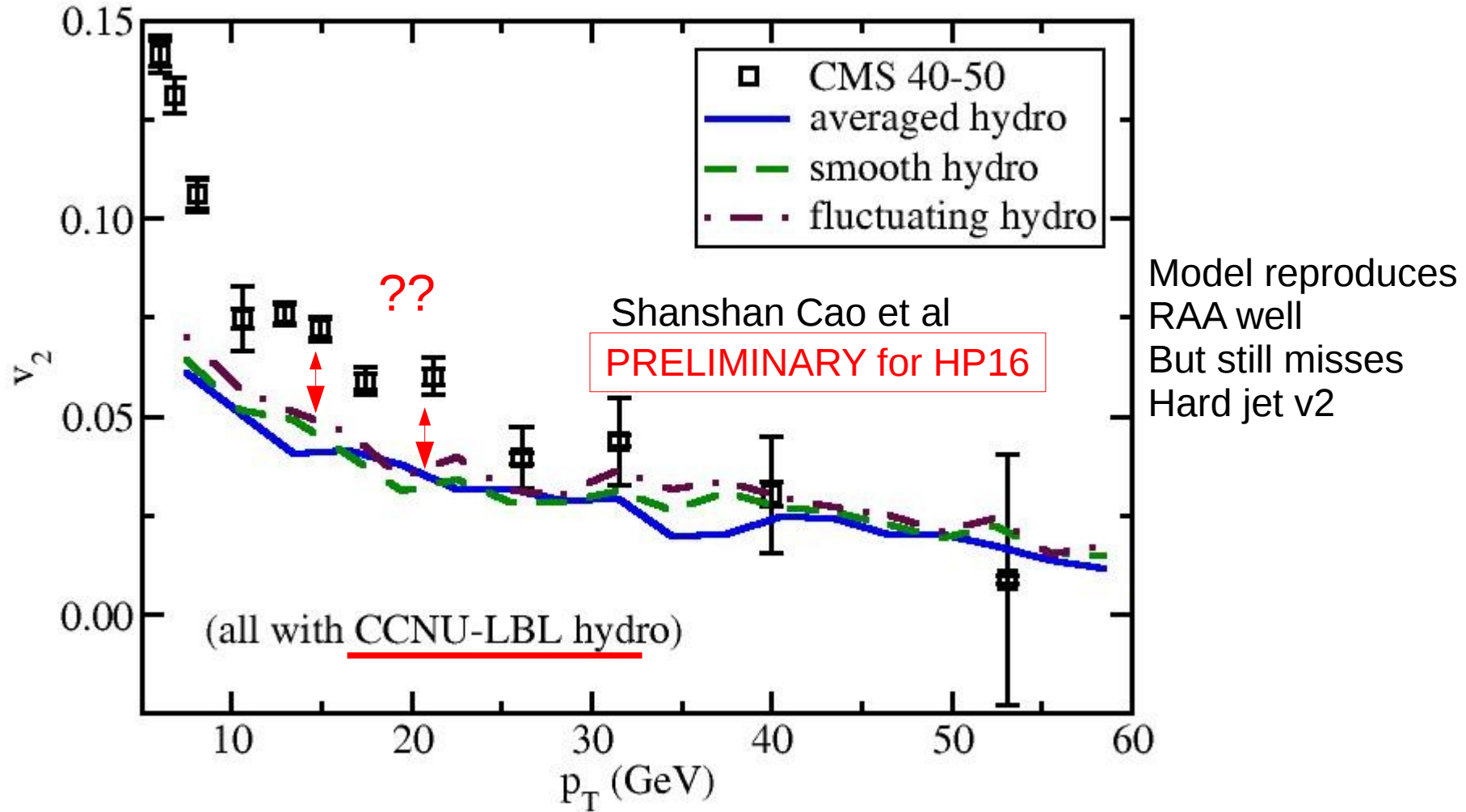
(Stay tuned )





Averaged: one hydro run on event average IC in 40-50% centrality  
 Smooth: 20 hydro runs in centrality bin on 20 different bins of soft v2(pT<2)  
 Fluctuating: Smooth times event fluctuation estimate

$\overline{v_2}$  linear response holds  $\frac{v_2(p_T)}{\langle v_2^{hard}(p_T) \rangle} \simeq 1 + \frac{1}{2} \left\langle \left( \frac{\delta v_2^{soft}}{\langle v_2^{soft} \rangle} \right)^2 \right\rangle - 2 \langle (\delta \psi_2(p_T))^2 \rangle$  (J.Noronga-Hostler et al PRL 2016)



Assuming linear hard-soft response:  $v_{2hard}(p_T) = \chi_{hs}(p_T) v_{2soft} = \chi_{hs}(p_T) \epsilon_2$

Ebe Fluctuations of soft v2 do not explain hard v2 data in 10-30 GeV range in this moswl

CUJET2.0 = rc DGLV + VISH2+1 at RHIC and LHC and

where  
 VISH is bulk flow  $p_T < 2$  GeV constrained viscous 2+1 D hydro UHeinz et al

$$\begin{aligned}
 x \frac{dN_{Q \rightarrow Q+g}}{dx}(\mathbf{x}, \phi) &= \int d\tau \rho_{QGP}(\mathbf{x} + \hat{\mathbf{n}}(\phi)\tau, \tau) \int \frac{d^2\mathbf{q}}{\pi} \frac{\alpha_s^2(q^2)}{(q^2 + f_E^2 \mu^2(\tau))(q^2 + f_M^2 \mu^2(\tau))} \int \frac{d^2\mathbf{k}}{\pi} \alpha_s(k_T^2/(x(1-x))) \\
 &\times \frac{12(\mathbf{k}+\mathbf{q})}{(\mathbf{k}+\mathbf{q})^2 + \chi(\tau)} \cdot \left( \frac{(\mathbf{k}+\mathbf{q})}{(\mathbf{k}+\mathbf{q})^2 + \chi(\tau)} - \frac{\mathbf{k}}{k^2 + \chi(\tau)} \right) \left( 1 - \cos \left[ \frac{(\mathbf{k}+\mathbf{q})^2 + \chi(\tau)}{2x_+ E} \tau \right] \right).
 \end{aligned}$$

where  $\mu^2(\tau) = 4\pi\alpha_s(4T^2)$  is the local HTL color electric Debye screening mass squared in a pure gluonic plasma with local temperature  $T(\tau) \propto \rho_{QGP}^{1/3}(\mathbf{x}, \tau)$  along the jet path  $\mathbf{x}(\tau)$  through the plasma. Here  $\chi(\tau) = M^2 x_+^2 + f_E^2 \mu^2(T(\tau))(1-x_+)/\sqrt{2}$  controls the “dead cone” and LPM destructive interference effects due to both the finite quark current mass  $M$ , and a thermal gluon  $m_g = f_E \mu(T)/\sqrt{2}$  mass.

Includes effects due to bulk Radial and Elliptic transverse flow of sQGP as well as boost invariant Bjorken longitudinal flow

These suppress jet  $v_2$  by factor of 2 (as in **D. Molnar and D.Sun**, NPA932 (2014) )