

Connecting fundamental models with nuclear reaction evaluations

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*Nuclear Reactions: A Symbiosis between
Experiment, Theory and Applications*



U.S. DEPARTMENT OF
ENERGY

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Science

Summary

- What is a reaction evaluation?
- Importance of predictive theory in reaction evaluations
 - Extrapolation
 - Compensation of errors
- Soft-rotor optical potential applied to Iron evaluations
- Coupled-channels on interpolated Optical Potentials
 - Adiabatic principle: Separation of degrees of freedom
 - Rare-earth angular distributions
- Reaction observables from microscopic transition densities/potentials for nucleon-nucleus reactions
 - Reaction cross sections
 - Total cross sections
 - Angular distributions

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The Nuclear Data Community is the link between basic science and applications

Nuclear Science Community

- ◆ Experiments
- ◆ Theory



Nuclear Data Community

- ◆ Compilation
- ◆ Evaluation
- ◆ Dissemination
- ◆ Archival

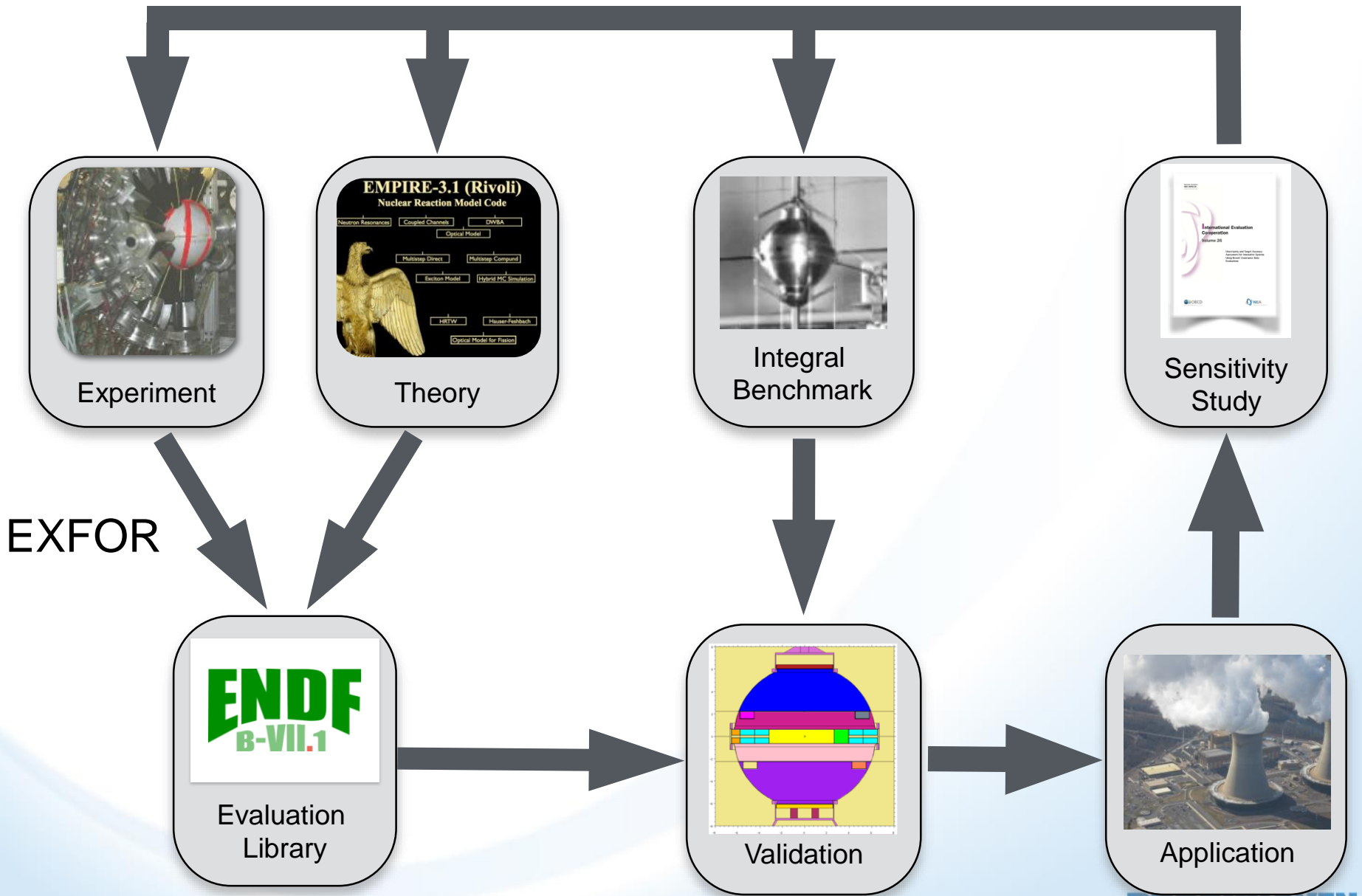


Application Community

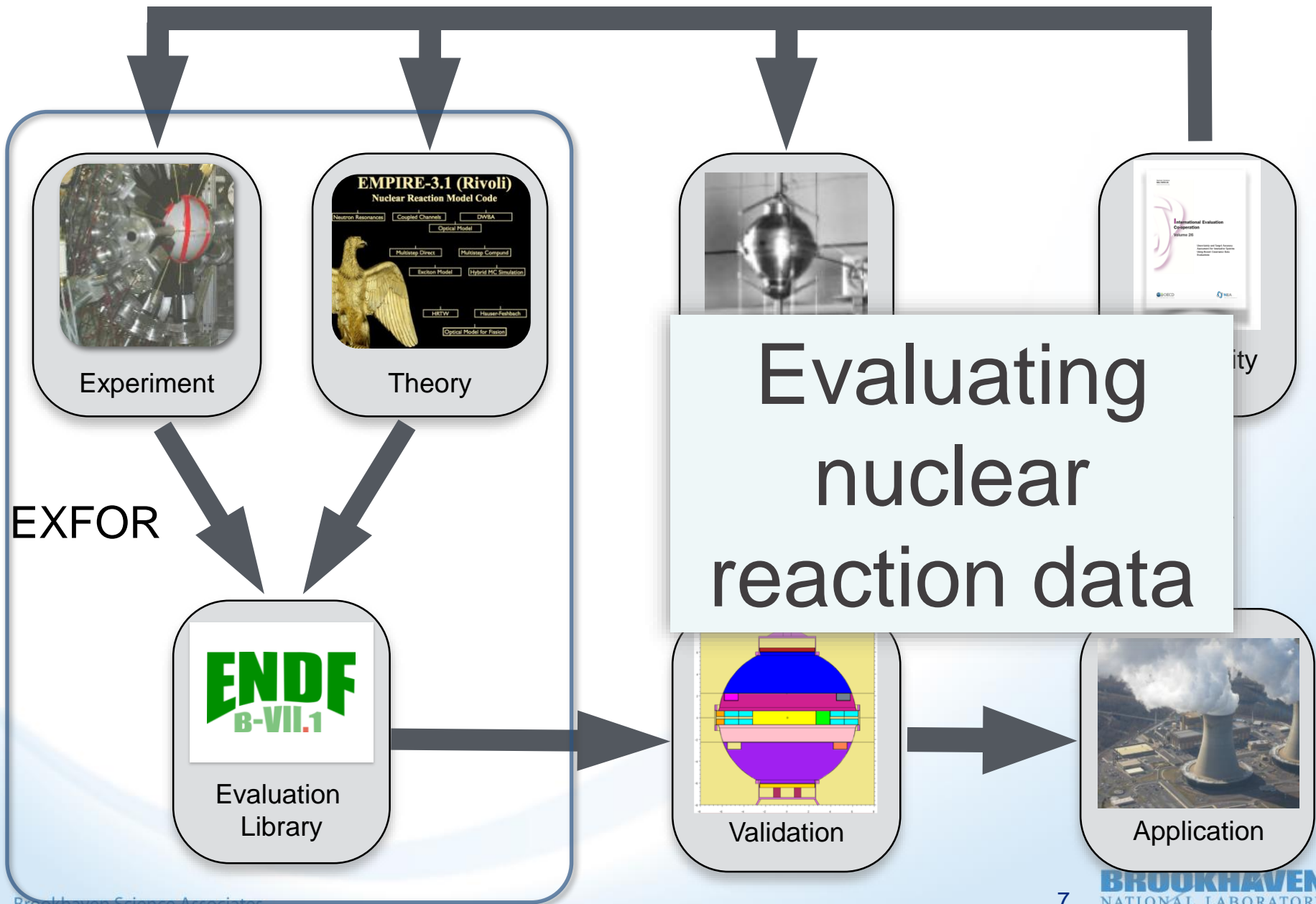
- needs data:
- ◆ Complete
 - ◆ Organized
 - ◆ Traceable
 - ◆ Readable

Reaction evaluations

- Goal: Provide best cross sections (integrated/differential)
- Used in applications: Nuclear power, astrophysics, medical isotope production, national security...
- Sub-libraries: neutron, proton, decay, ...
- Analysis of experimental data
 - Conflicting sets
 - Always be incomplete
- Modeling fills gaps
- Validation (integral testing)
 - Critical assemblies
 - Normally only one quantity is measured
 - Compensation of errors
 - Examples: minor Iron isotopes, Chromium issue in steel, etc.



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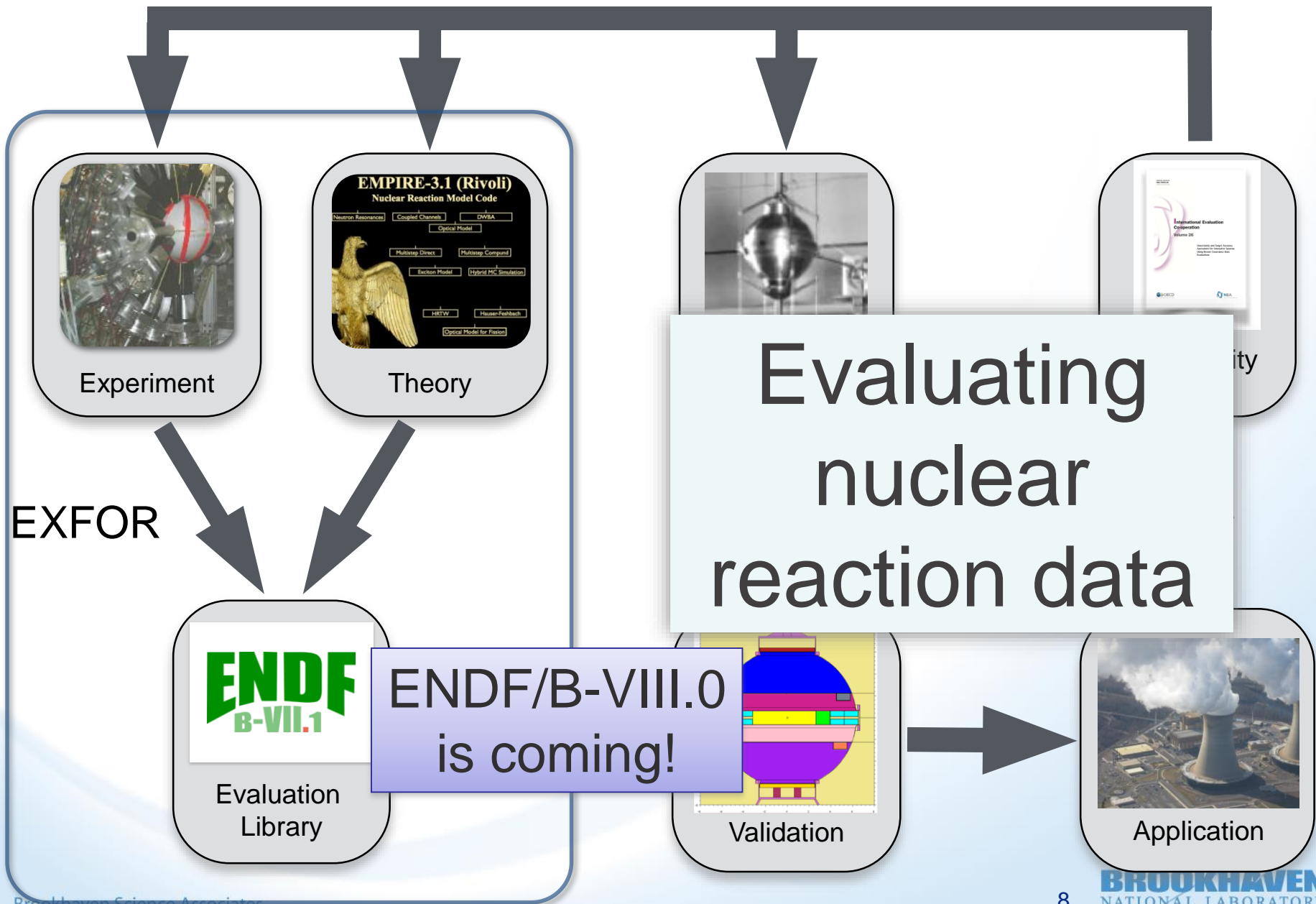
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Evaluation
Library

Evaluating
nuclear
reaction data

Validation

Application



Soft-Rotator Model (SRM)

1

- SRM used to obtain a dispersive OP: Fe evaluation
- Collective models are normally assumed either pure rotational or vibrational
- However, “centrifugal” forces in some rotating nuclei lead to displacement of nuclear matter within the nucleus
- Vibration within deformed matter: “Softness” parameter
- Applied to light, medium, and heavy nuclei, which are not pure vibrational nor pure rotors

$$R_i(\theta', \varphi') = R_{0i} \left\{ 1 + \sum_{\lambda=2,4,6,8} \beta_{\lambda 0} Y_{\lambda 0}(\theta') \right\} + R_{0i} \beta_{20} \left[\frac{\delta \beta_2}{\beta_{20}} \cos \gamma + \cos \gamma - 1 \right] Y_{20}(\theta') + R_{0i} (\beta_{20} + \delta \beta_2) \frac{\sin \gamma}{\sqrt{2}} [Y_{22}(\theta', \varphi') + Y_{2-2}(\theta', \varphi')] + R_{0i} \beta_3 \cos \eta Y_{30}(\theta') + R_{0i} \beta_3 \frac{\sin \eta}{\sqrt{2}} [Y_{32}(\theta', \varphi') + Y_{3-2}(\theta', \varphi')].$$

PRC 94, 064605 (2016)

Prediction of collective levels for $^{54,56,58}\text{Fe}$

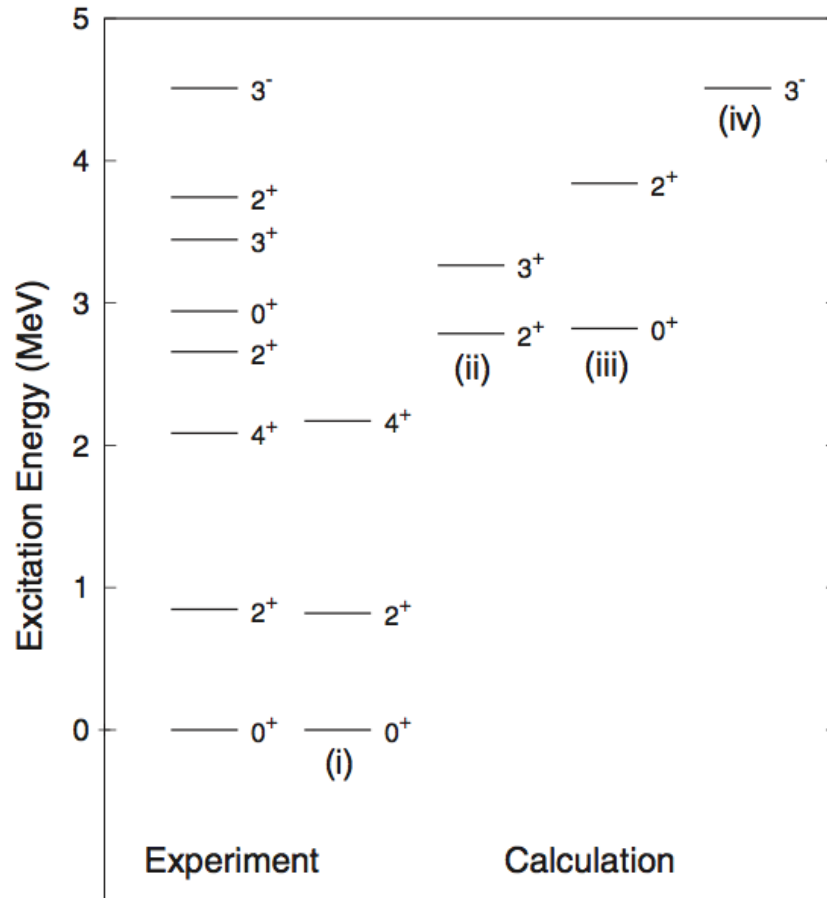


FIG. 1. Comparison of the experimental and predicted level schemes for the ^{56}Fe nucleus.

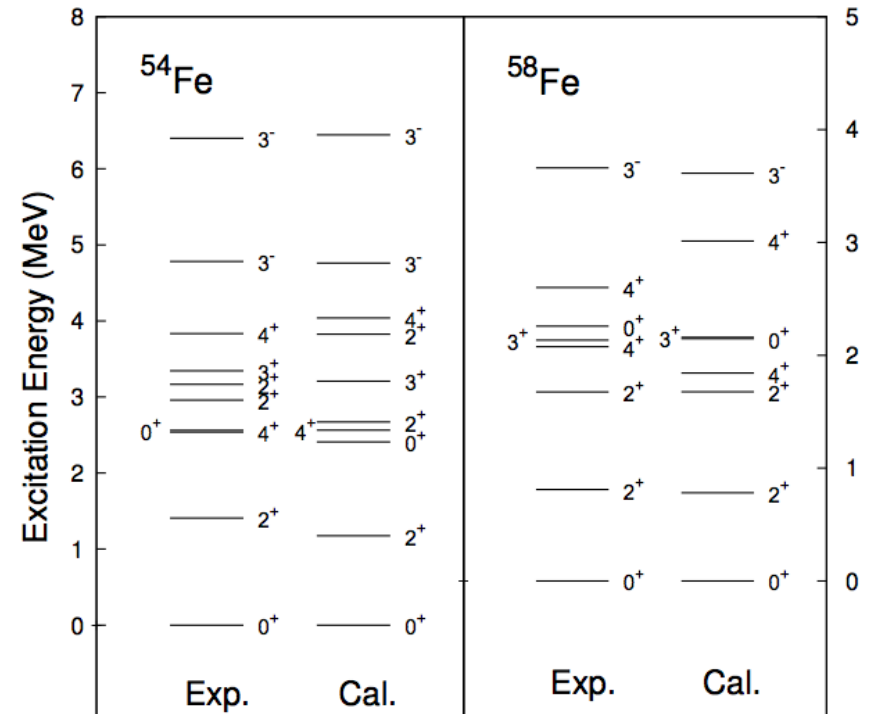
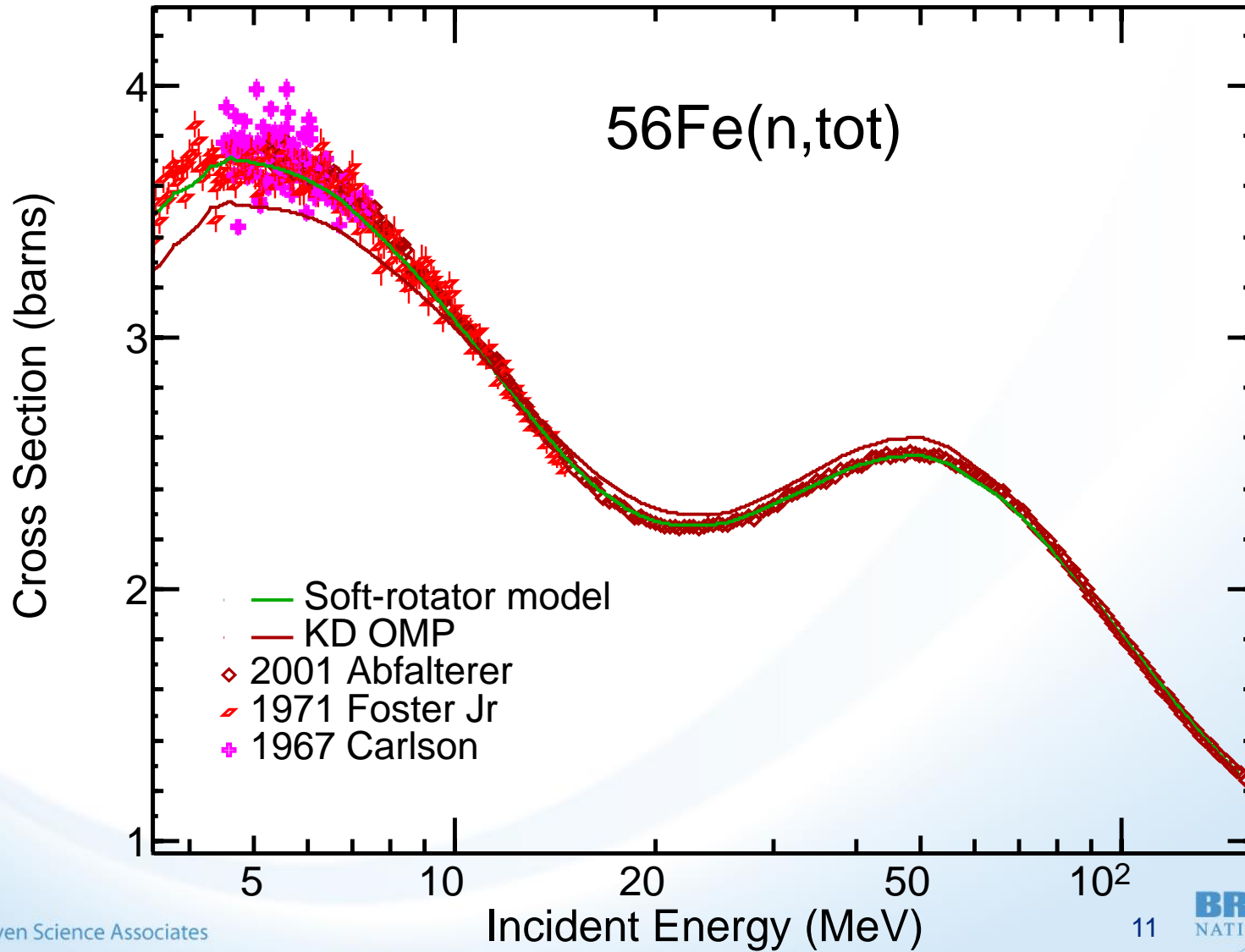


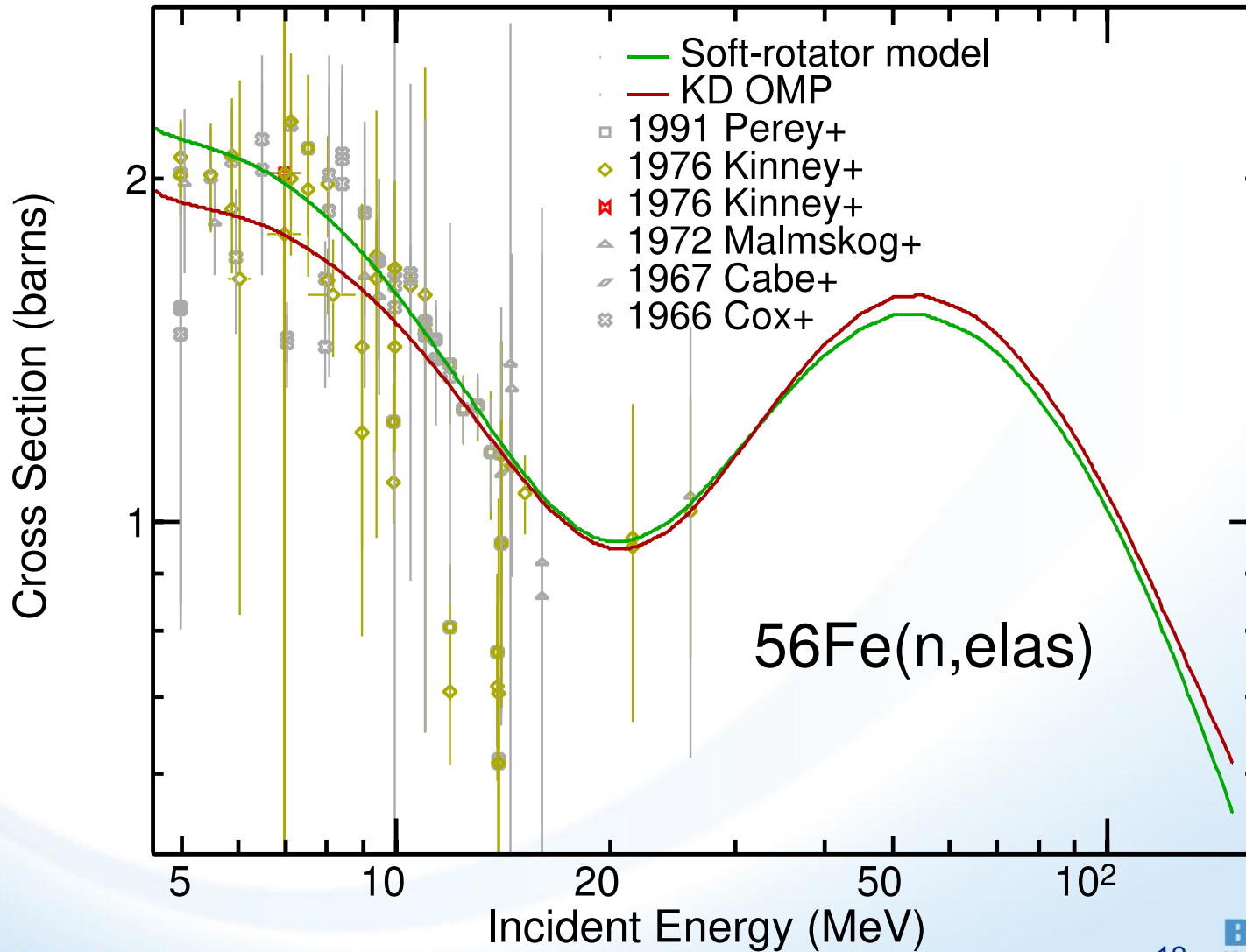
FIG. 1. Comparison of the experimental and SRM predicted collective level schemes for ^{54}Fe and ^{58}Fe nuclei.

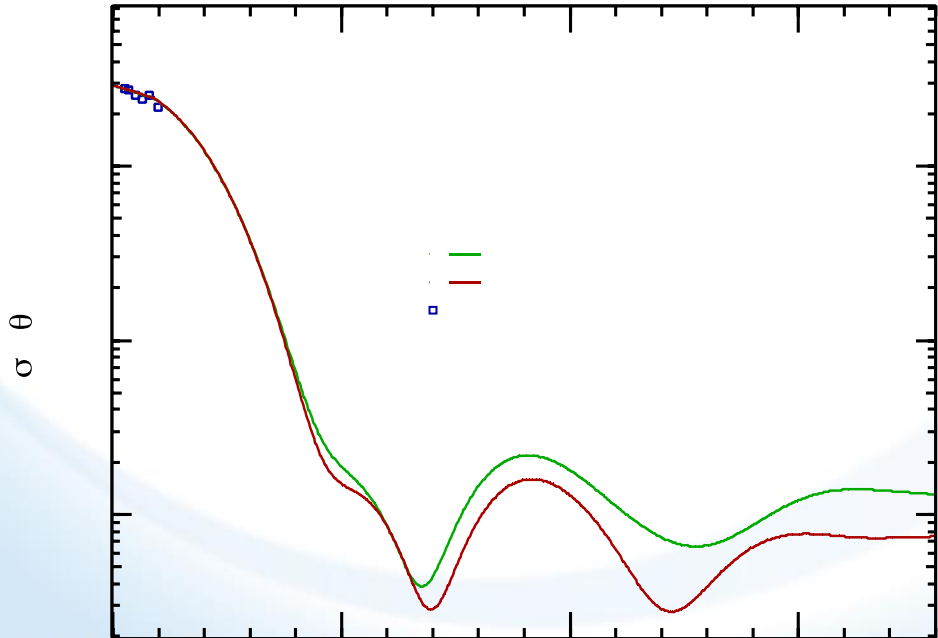
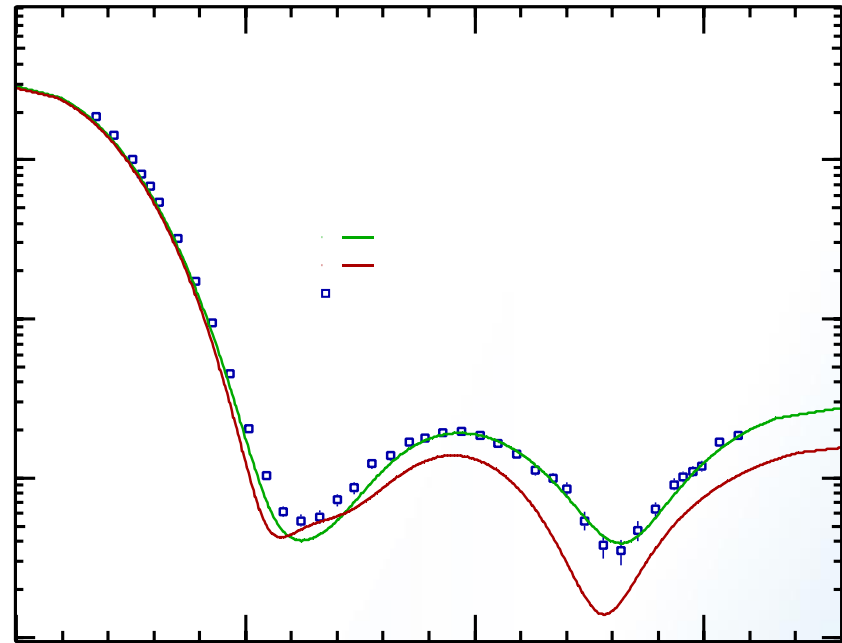
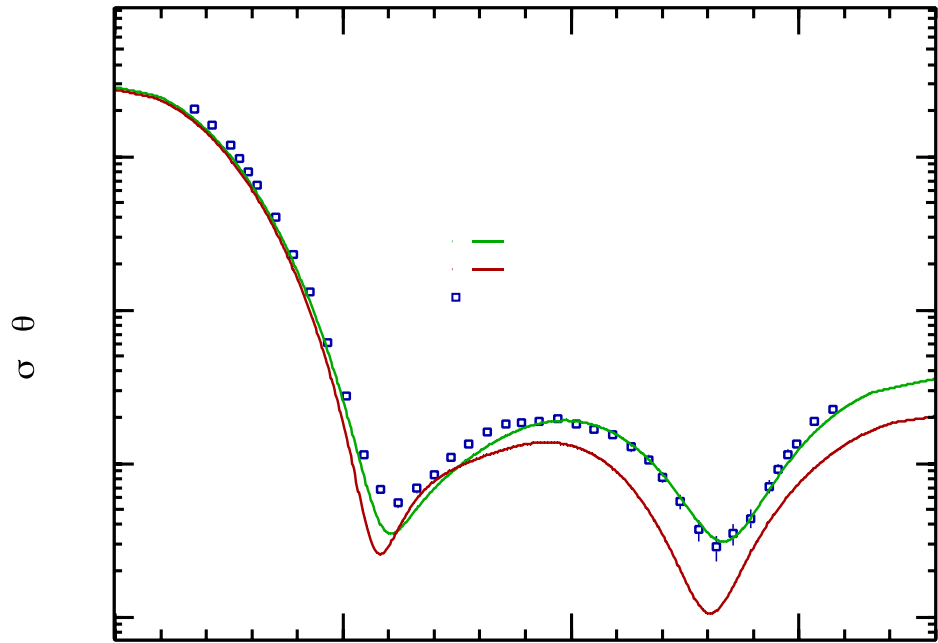
PRC 87, 054611 (2013)
NDS 118 (2014) 191-194

^{56}Fe



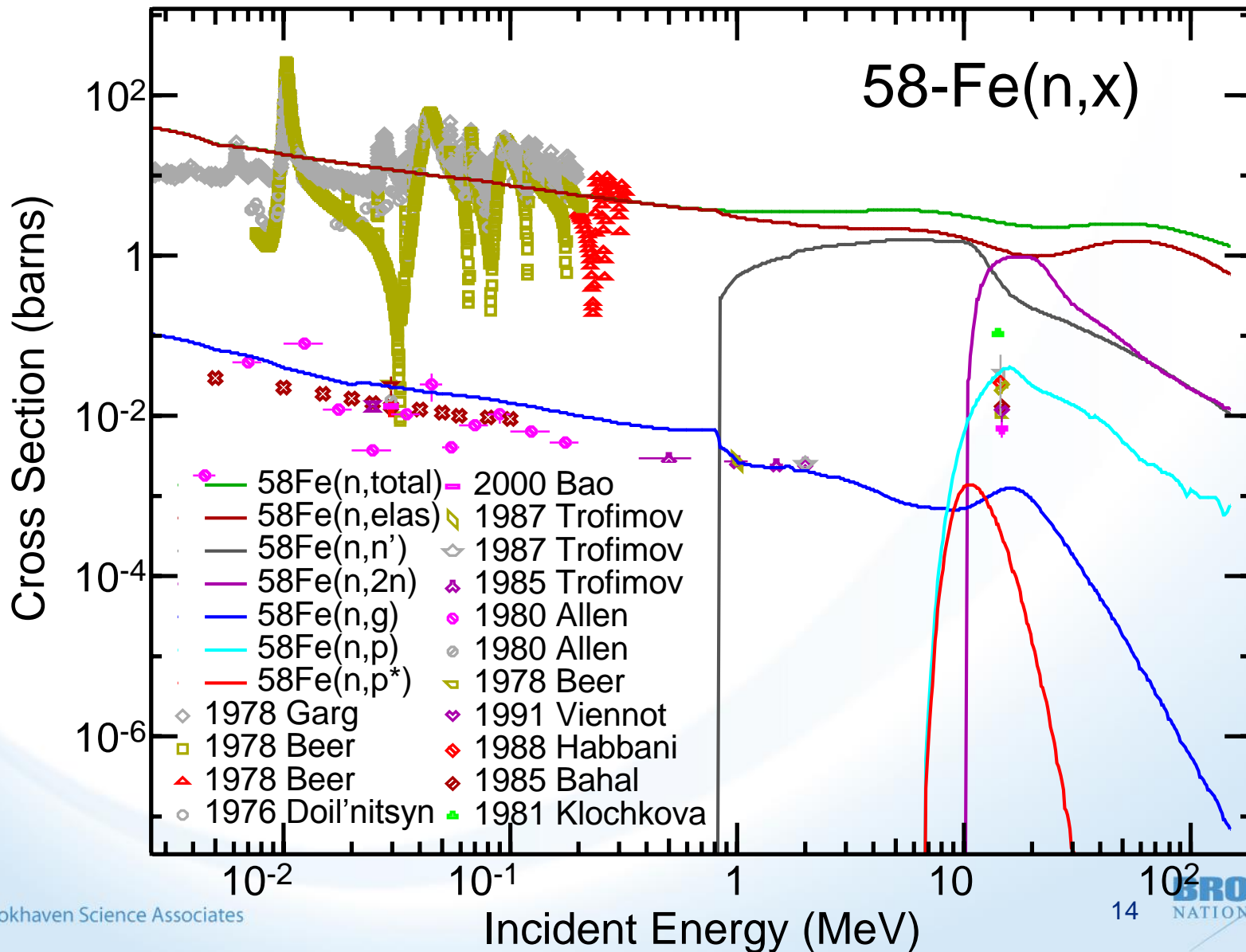
^{56}Fe





A more fundamental model lends reliability when there is little data available (or none whatsoever).

All data for ^{58}Fe

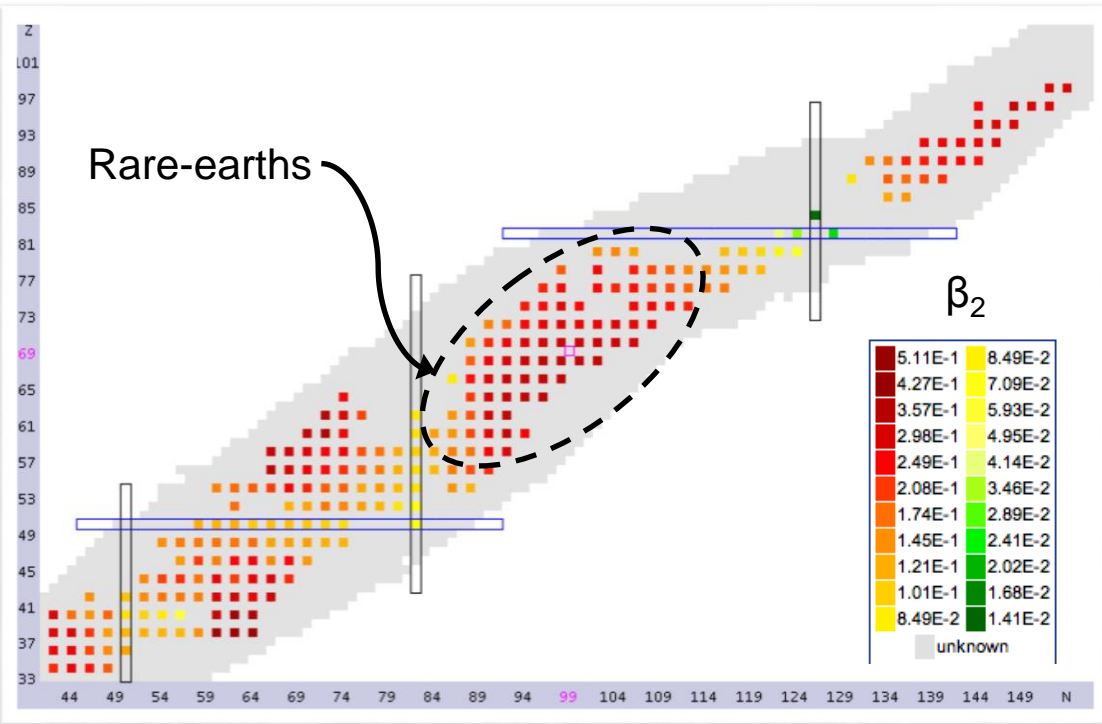


Development of an Optical Model Potential in the rare-earth region

Motivation

- Why seek an optical potential for the rare-earth region?
 - Lack of existing regional OP's for deformed nuclei
 - Recent work shows scattering from highly deformed nuclei is near adiabatic limit → deforming a spherical global potential may be suitable with only minor modifications

We deform the Koning-Delaroche spherical global potential and couple g.s. rotational band

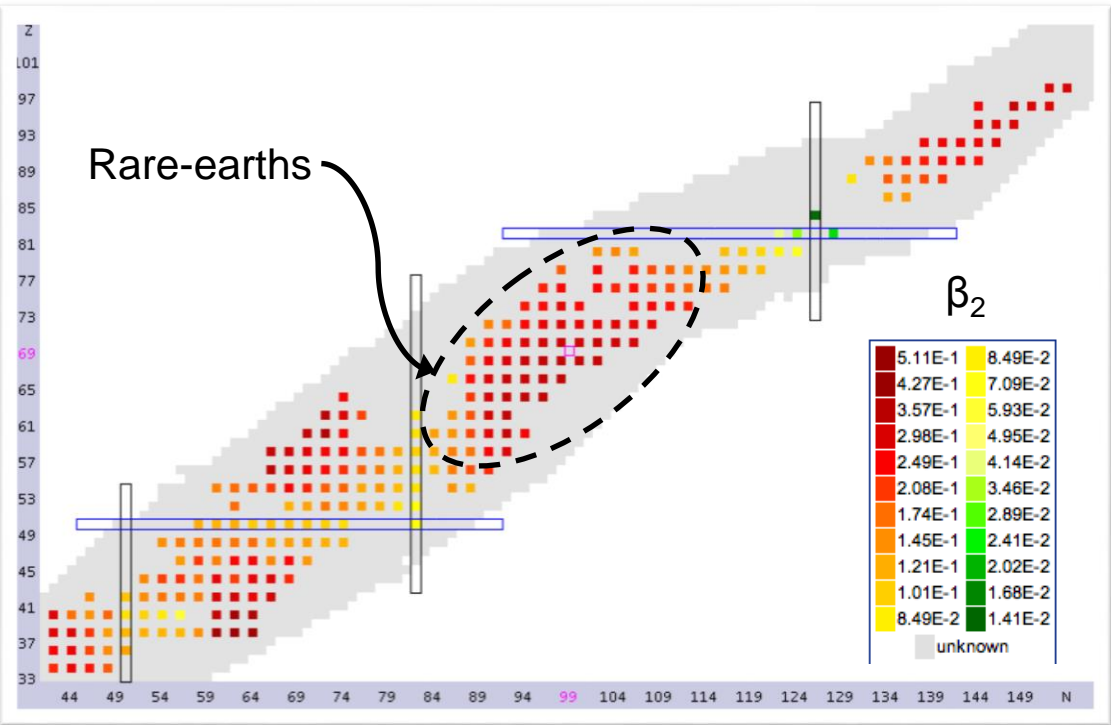


Development of an Optical Model Potential in the rare-earth region

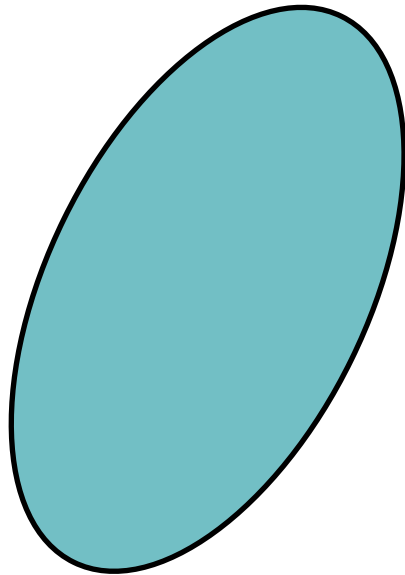
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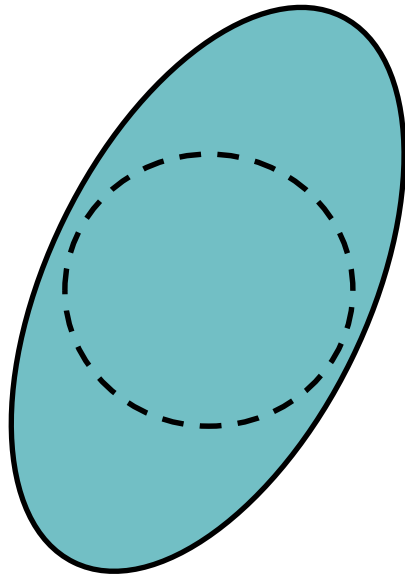


Very non-rigorous description



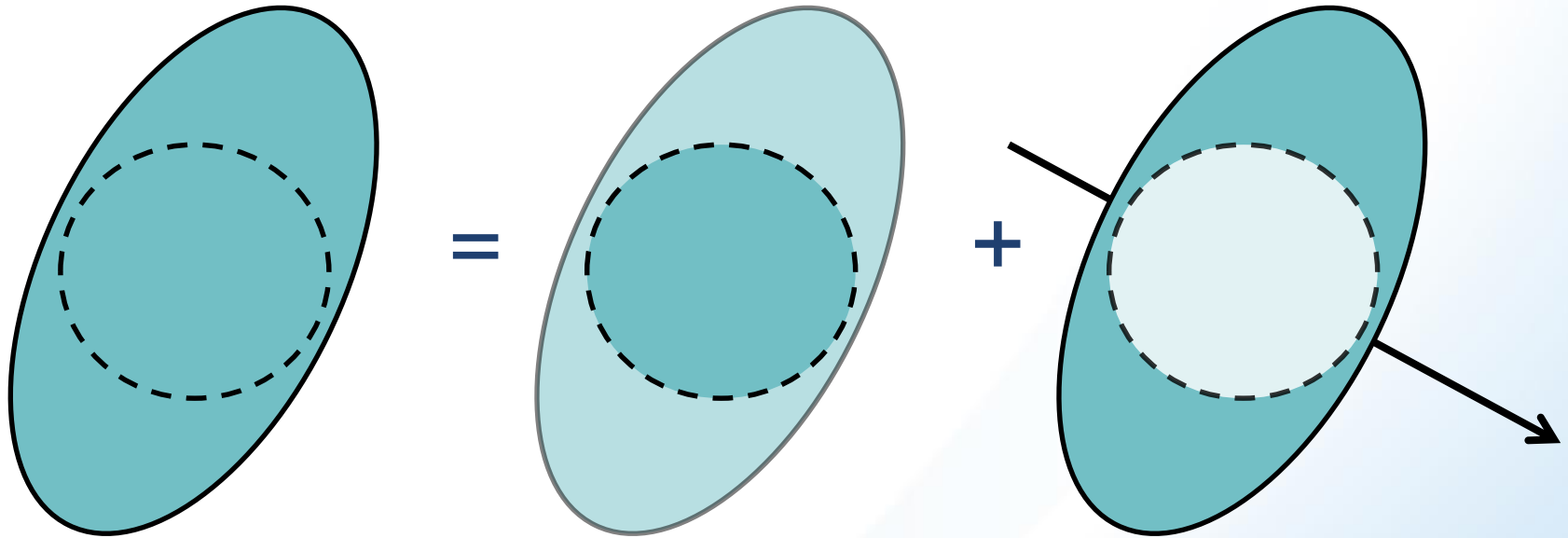
H_{deformed}

Very non-rigorous description



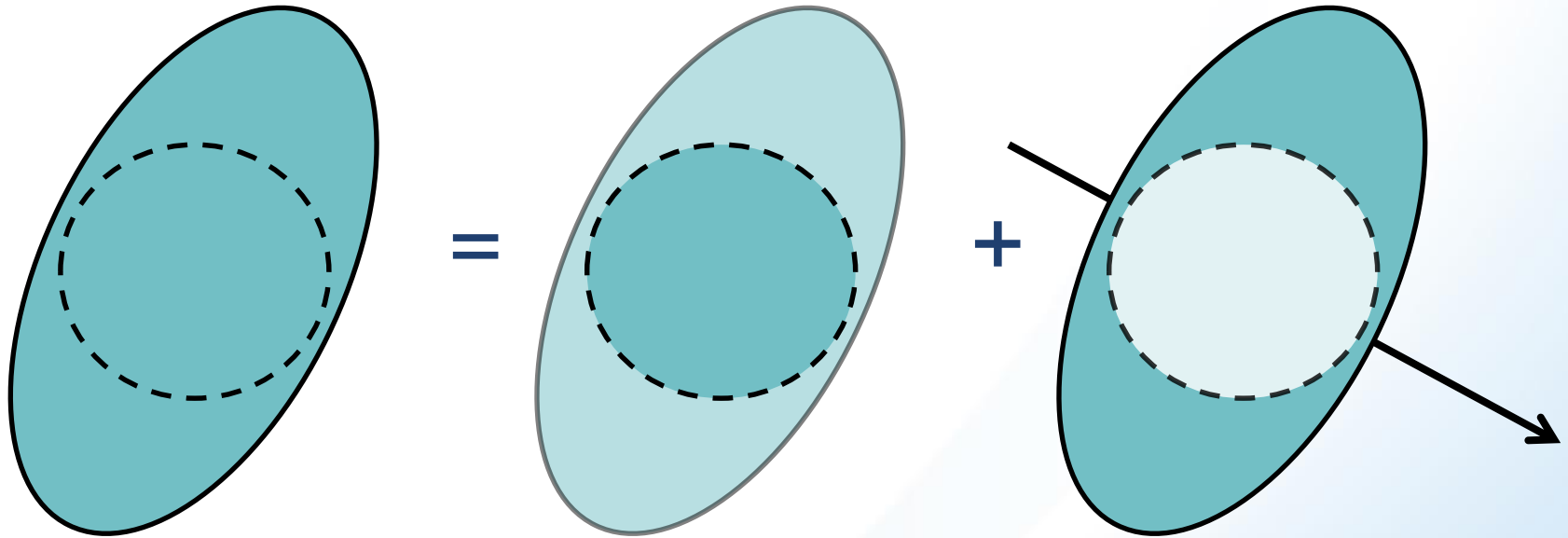
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$$H_{\text{deformed}} = H_{\text{spherical}} + H_{\text{rotational}}$$

Very non-rigorous description



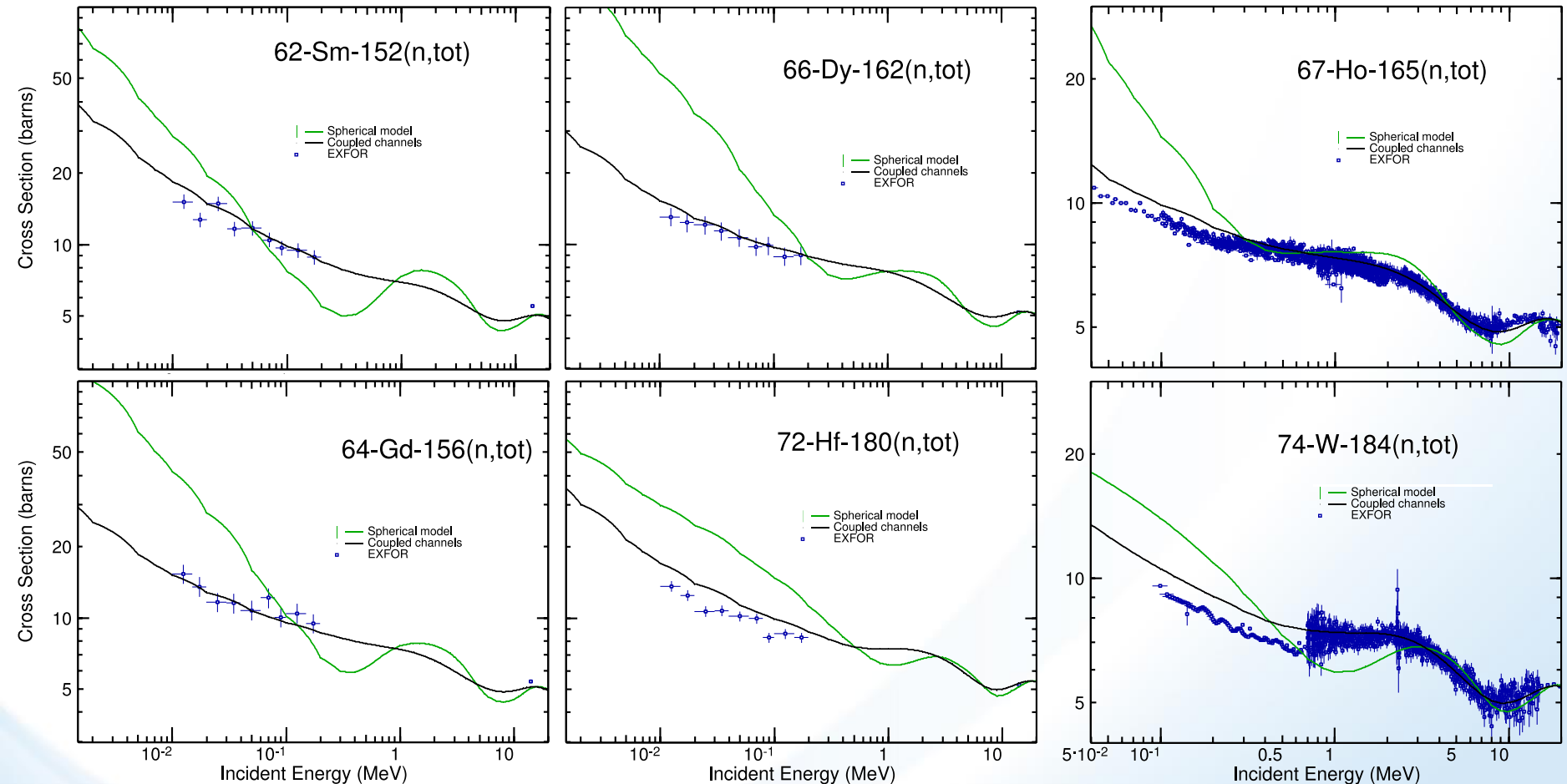
$$H_{\text{deformed}} = \underbrace{H_{\text{spherical}}}_{\text{Spher. OMP}} + \underbrace{H_{\text{rotational}}}_{\text{CC rot. band}}$$

Calculations done in rare-earths region

- CC calculations deforming spherical Koning-Delaroche OP
 - Full imaginary part of KD
 - Adiabatic limit
 - Experimental deformations
 - Coupled to g.s. rotational band
- Used EMPIRE code (Direct reaction part calculated by ECIS)
- 34 nuclei: $^{162,163,164}\text{Dy}$, $^{166,167,168,170}\text{Er}$, ^{153}Eu , $^{155,156,157,158,160}\text{Gd}$, $^{177,178,179,180}\text{Hf}$, ^{165}Ho , $^{175,176}\text{Lu}$, $^{152,154}\text{Sm}$, ^{181}Ta , ^{159}Tb , ^{169}Tm , $^{182,183,184,186}\text{W}$, $^{171,172,173,174,176}\text{Yb}$
- Tested convergence to the number of channels and correction for volume conservation
- Initially compared direct-reaction observables; then extended approach to test effect on compound nucleus quantities

$$R(q) = R_0 \left[1 + \frac{\hbar}{e} \sum_l b_l Y_{l,0}(q) \right]$$

Comparison between spherical and CC: Total cross sections

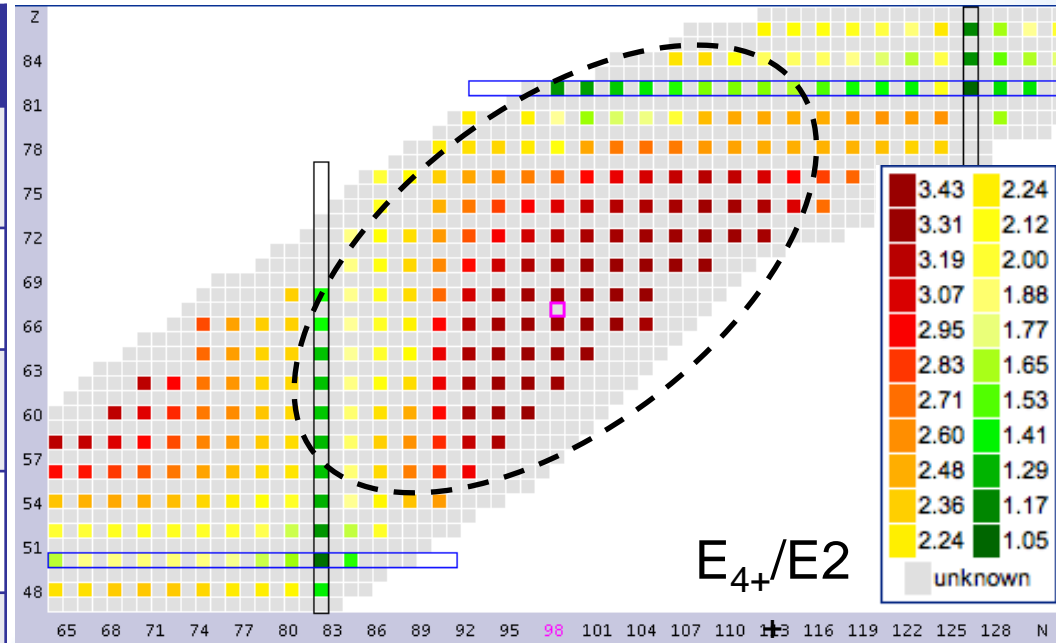


Spherical approach fails at low energy and its shape is often in disagreement with experimental data, while deforming KD potential provides a good description of the observed total cross sections

Angular distributions: Gd, Ho, W

- More detailed analysis on the experimental data sets
- Some elastic ang. dist. data actually contained inelastics
- Ensured convergence regarding number of rotational channels

nucleus	β_2^*	β_4^s	Δ_R	$\beta_2^{(sys)\dagger}$
^{158}Gd	0.34 8	0.056	0.990	0.362
^{160}Gd	0.35 3	0.056	0.990	0.372
^{165}Ho	0.29 3	-0.020	0.993	0.385
^{182}W	0.25 1	-0.080	0.995	0.268
^{184}W	0.23 6	-0.080	0.996	0.255
^{186}W	0.22 6	-0.080	0.998	0.226



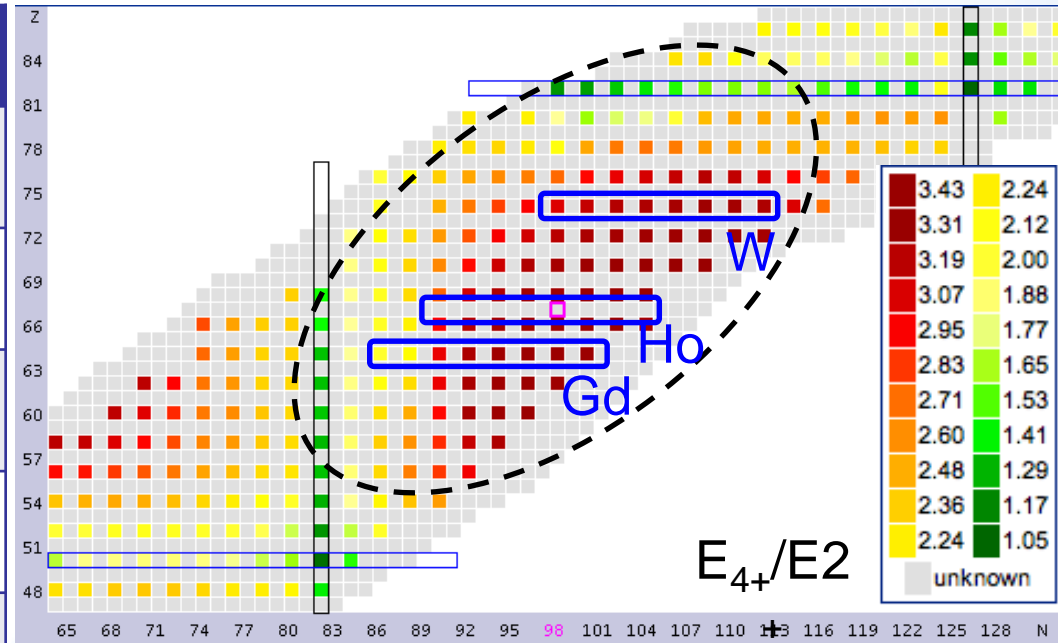
*At. Data. Nucl. & Data Tables, 78, (2001) 1
^s Ann. Nucl. Energy, 31 (2004) 1813;
 Phys. Lett. 26B (1968) 127;
 Ann. Nucl. Energy, 28 (2001) 1745

[†]Phys. Rev. C 70 (2004) 014604;
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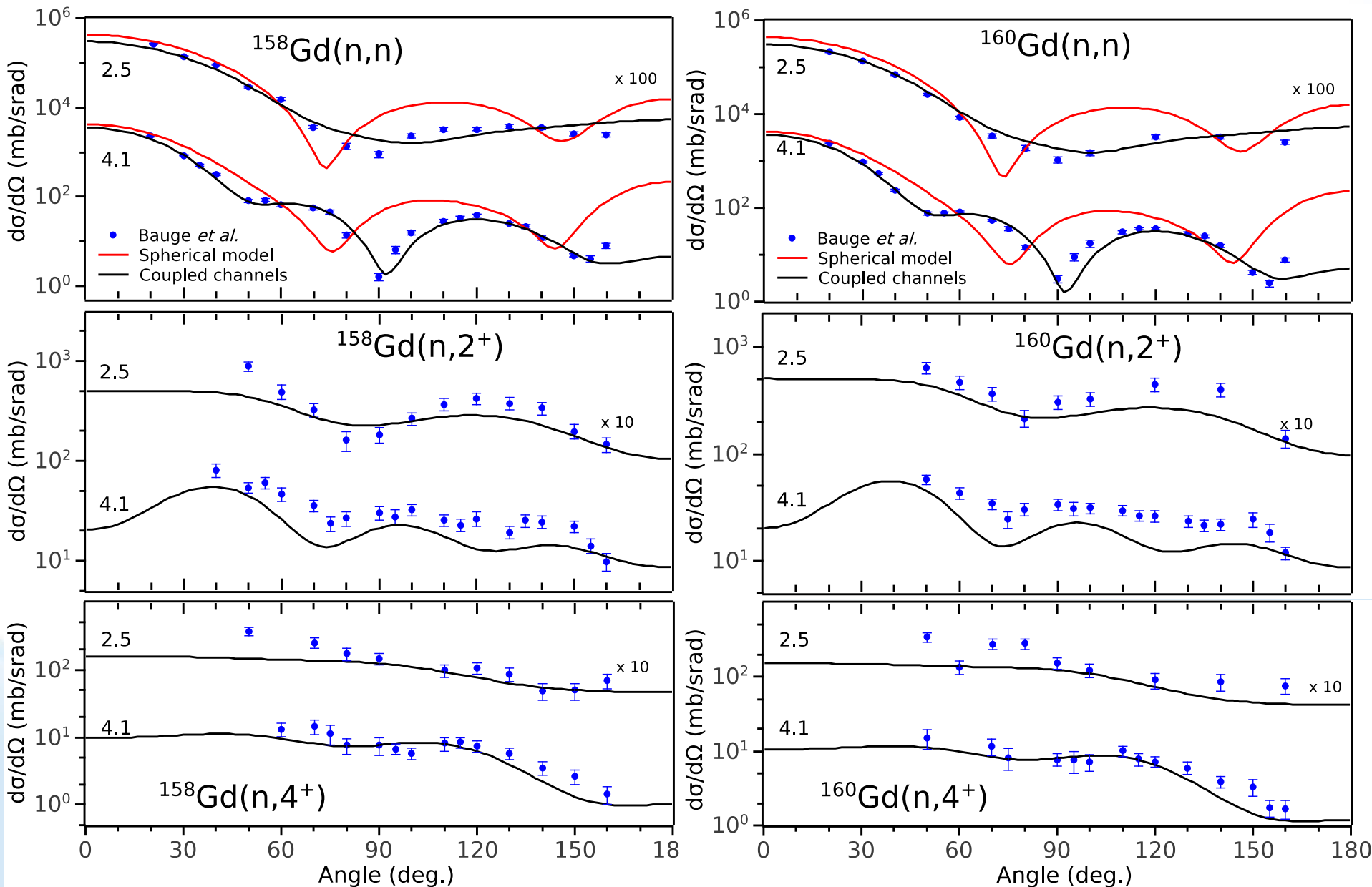


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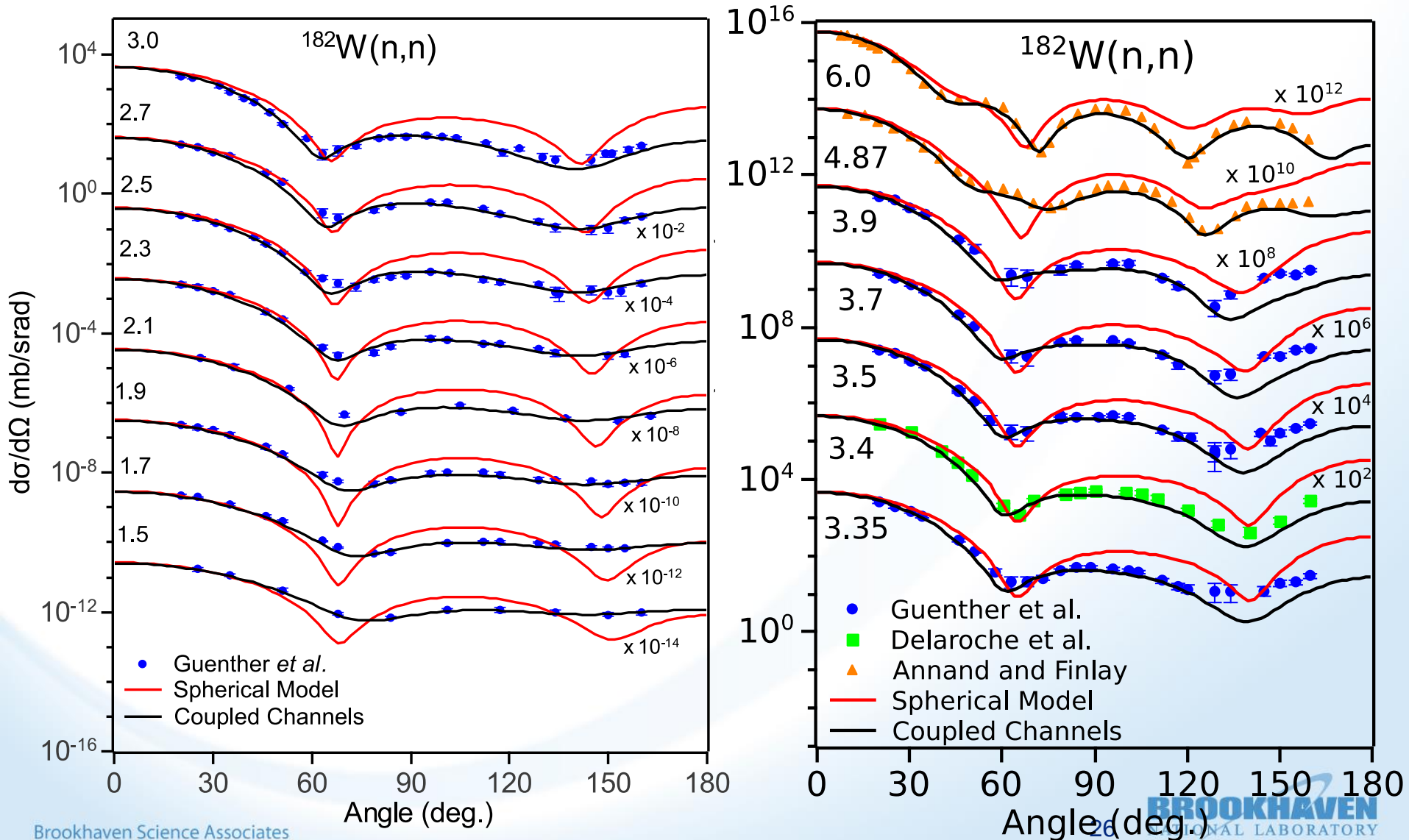
158, 160Gd Angular distributions

Good agreement with experimental data obtained by the model



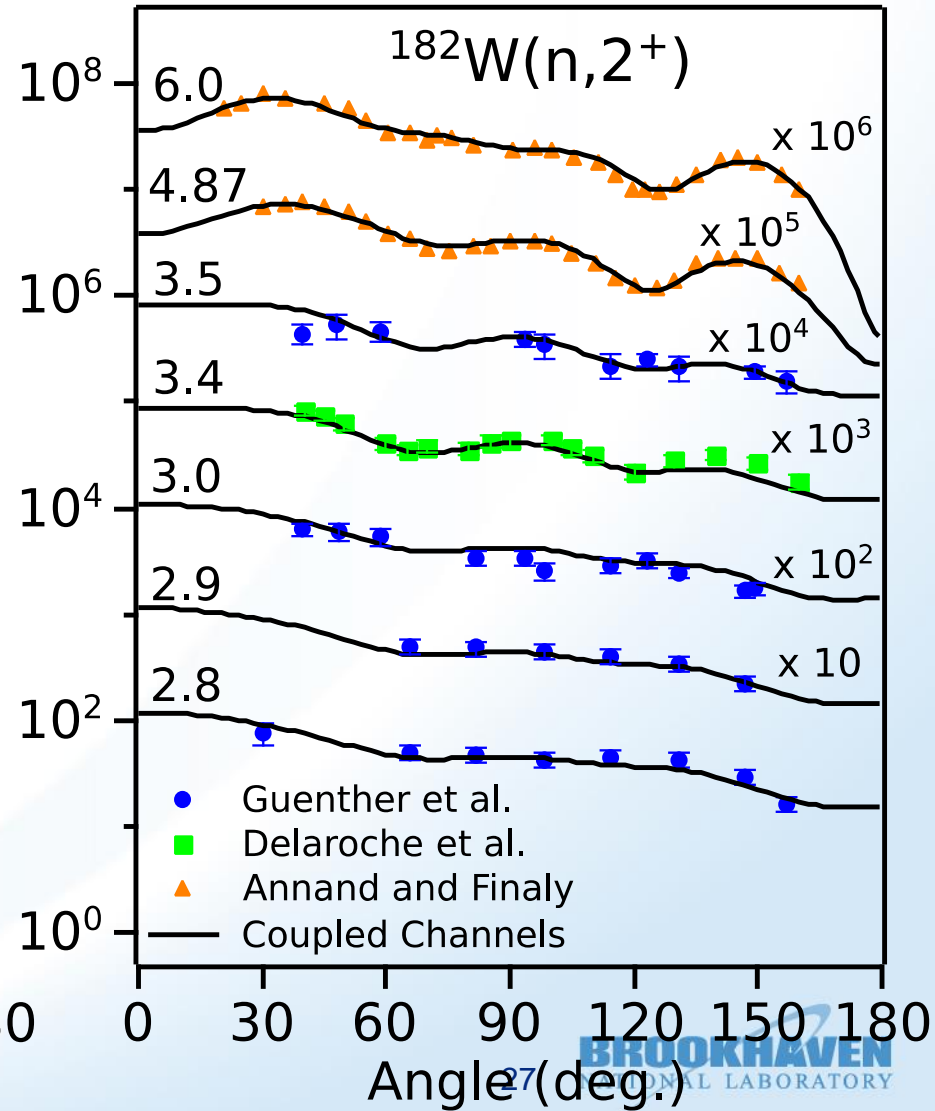
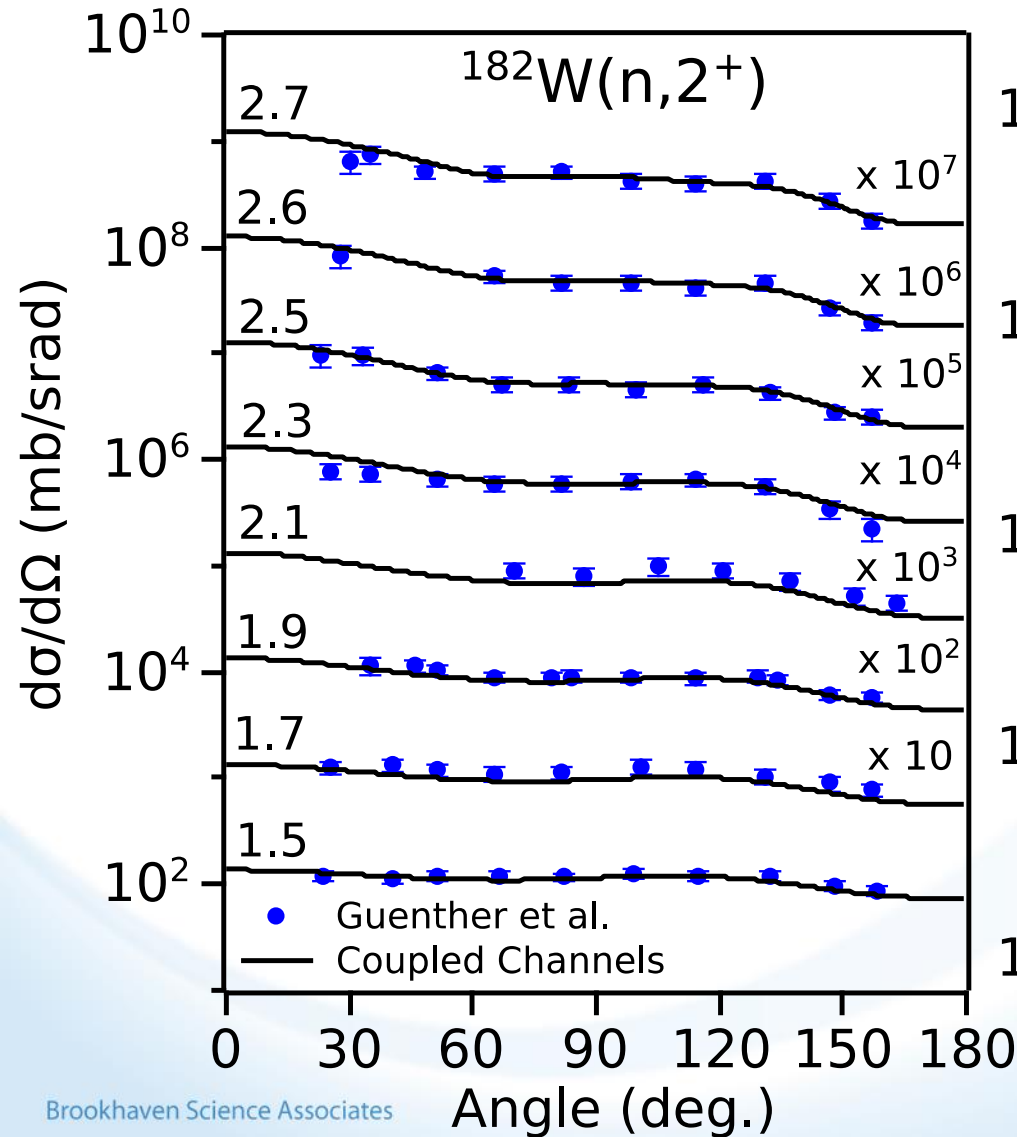
^{182}W – Elastic angular distributions

Good agreement with experimental data obtained by the model



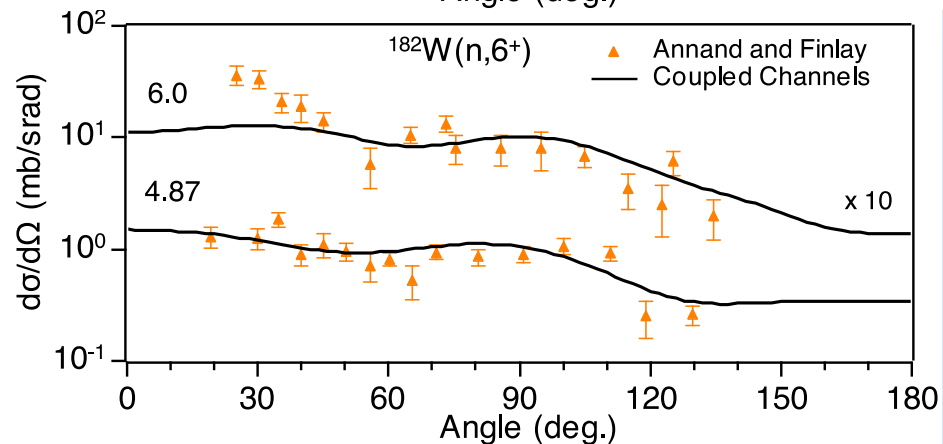
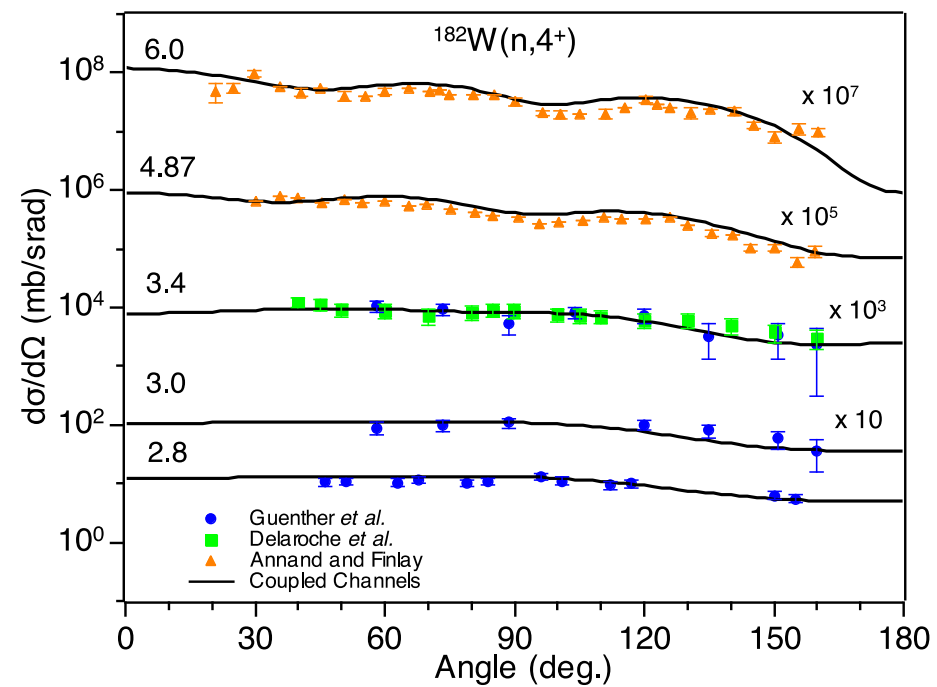
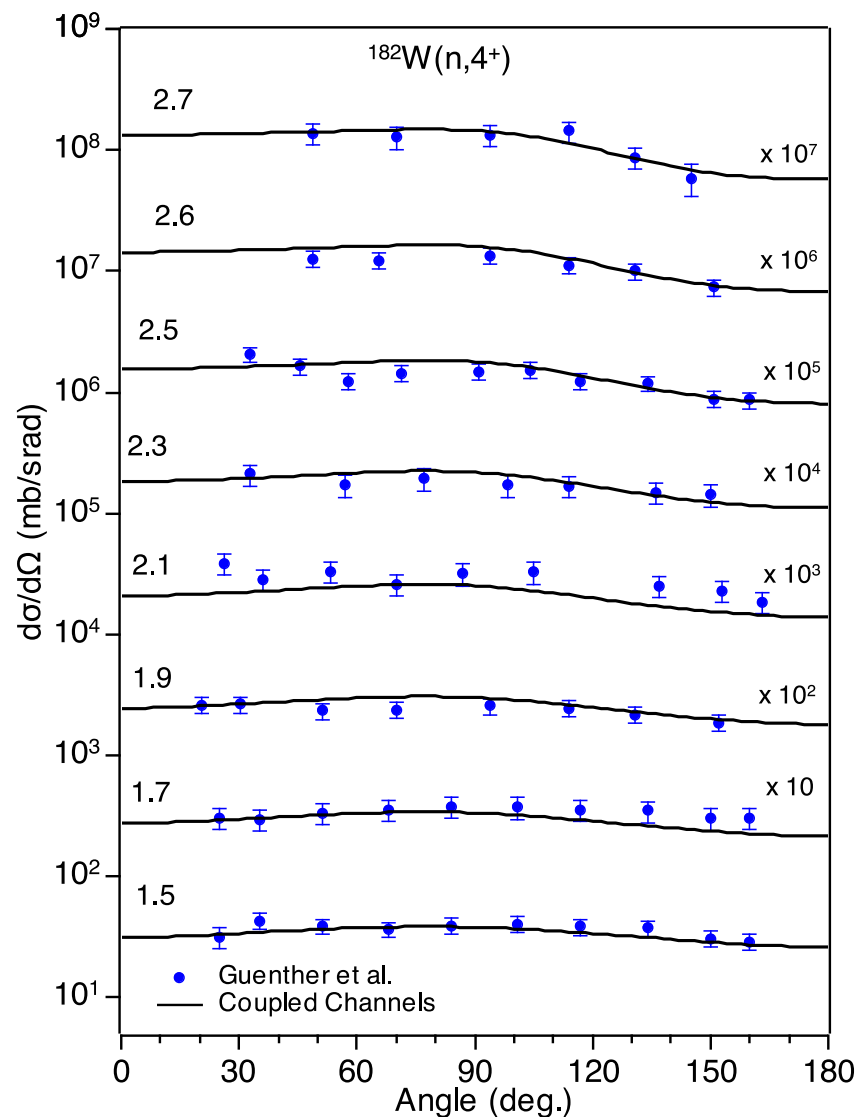
$^{182}\text{W} - 2^+$ Inelastic ang. dist. ($E_{2^+}=0.100\text{MeV}$)

Good agreement with experimental data obtained by the model

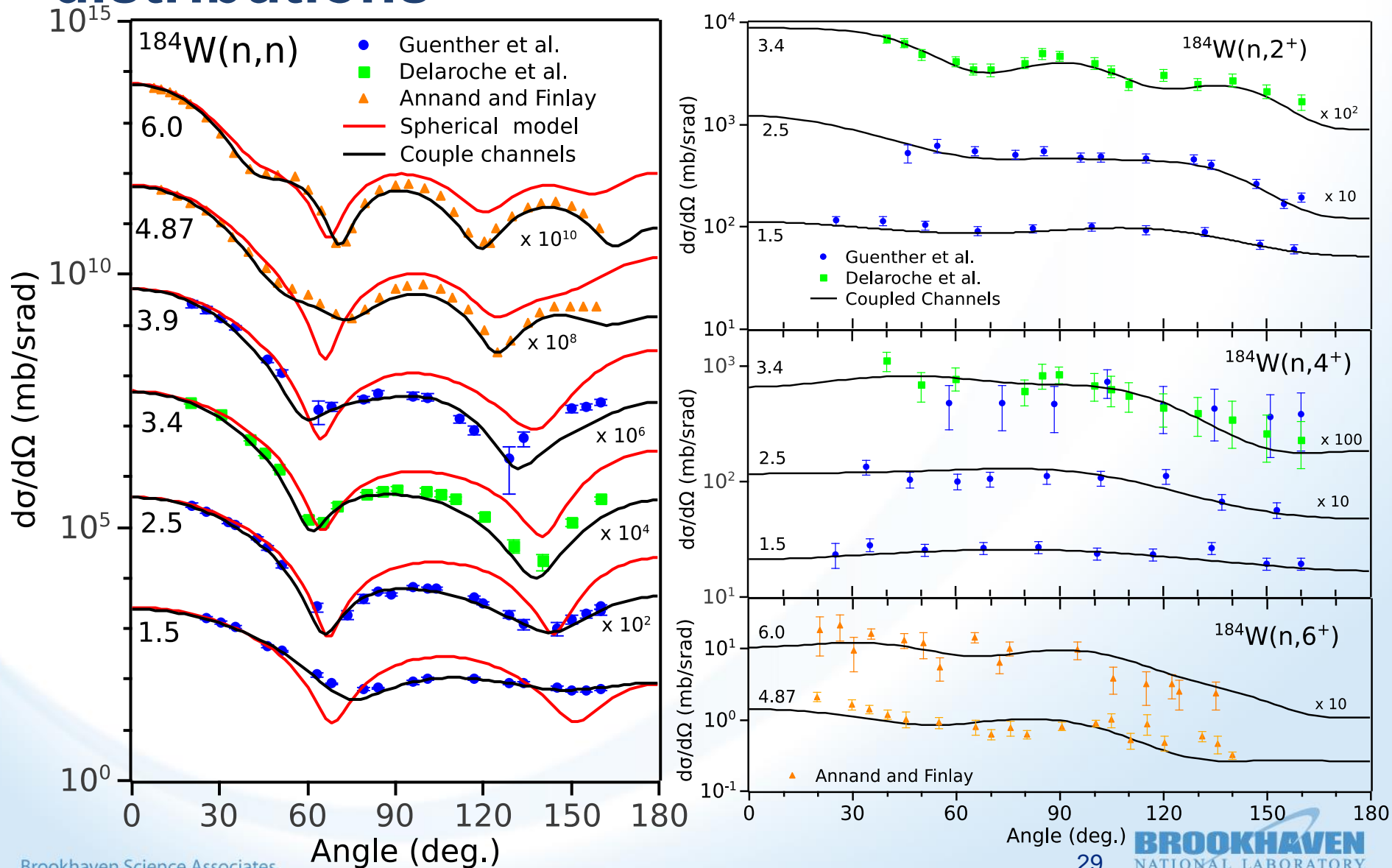


$^{182}\text{W} - 4^+$ Inelastic ang. dist. ($E_{4^+}=0.329\text{MeV}$)

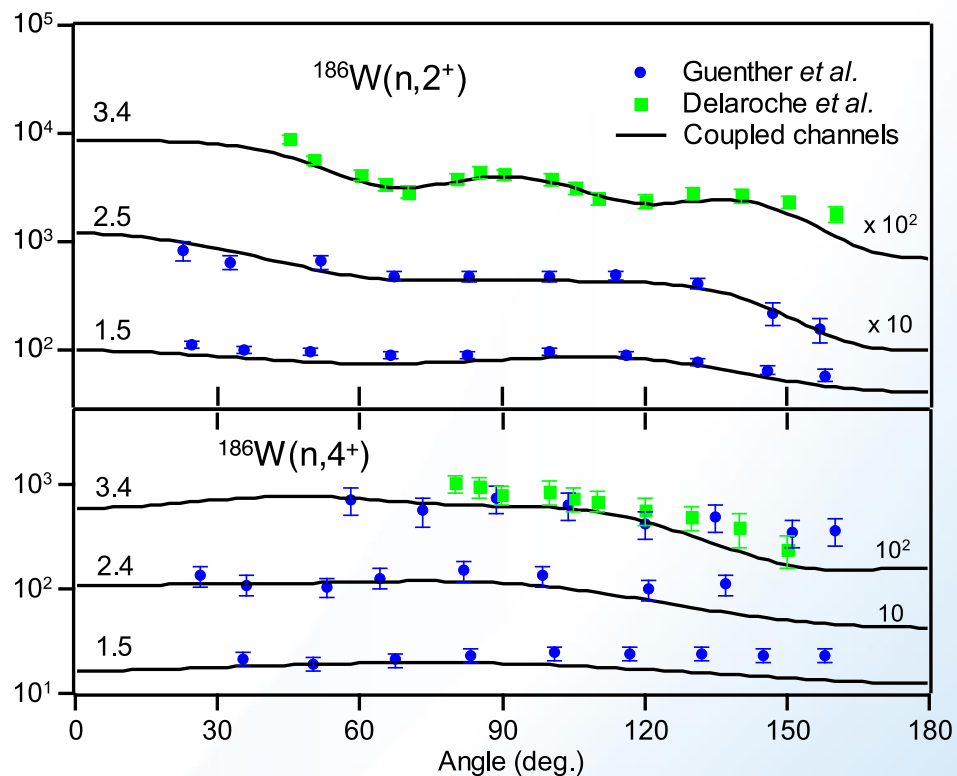
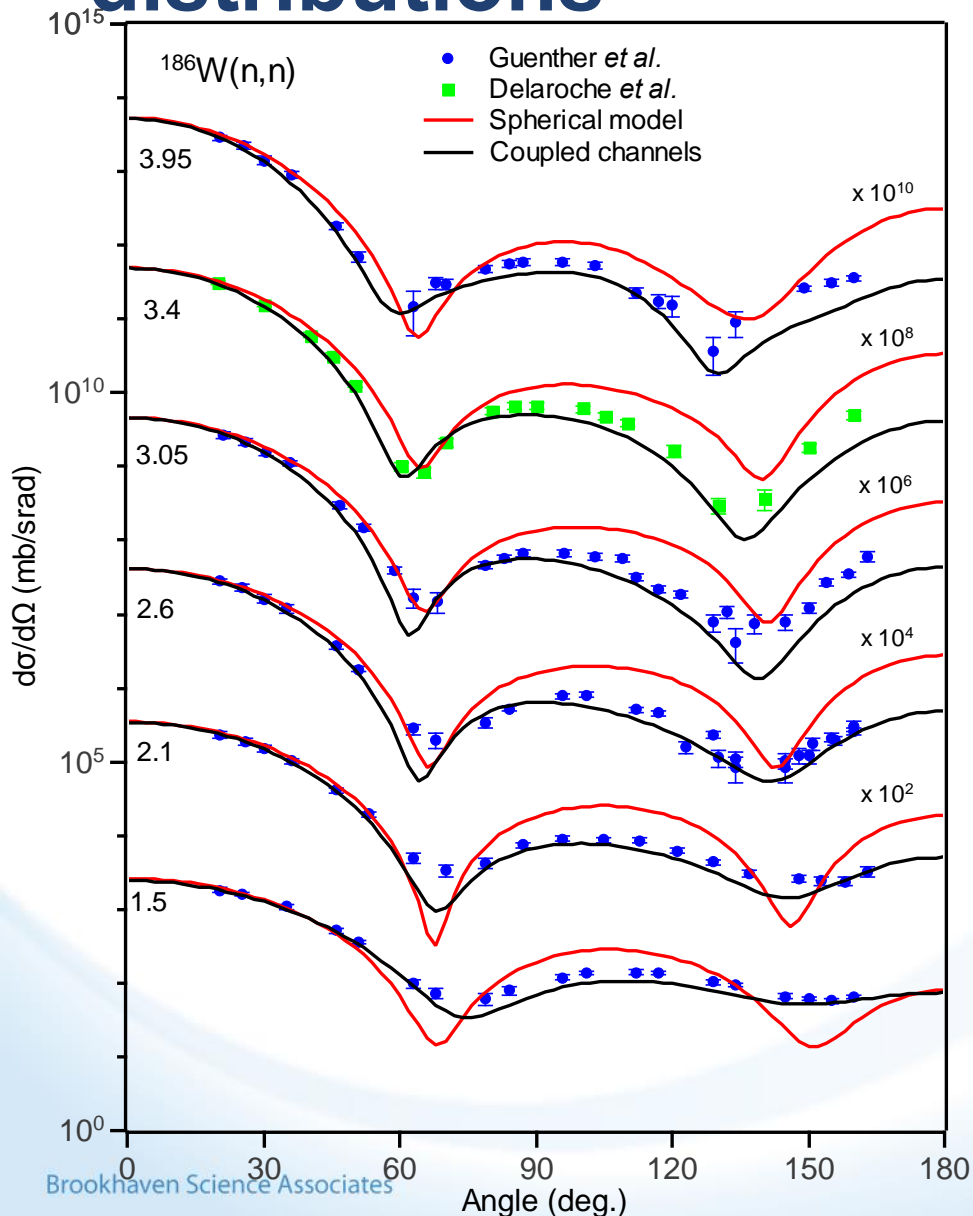
Good agreement with experimental data obtained by the model



^{184}W – Elastic and inelastic angular distributions



^{186}W – Elastic and inelastic angular distributions



The fact that deforming KD allows to consistently describe observed elastic and inelastic angular distributions remarkably well is very supportive of the model and of the adiabatic approximation.

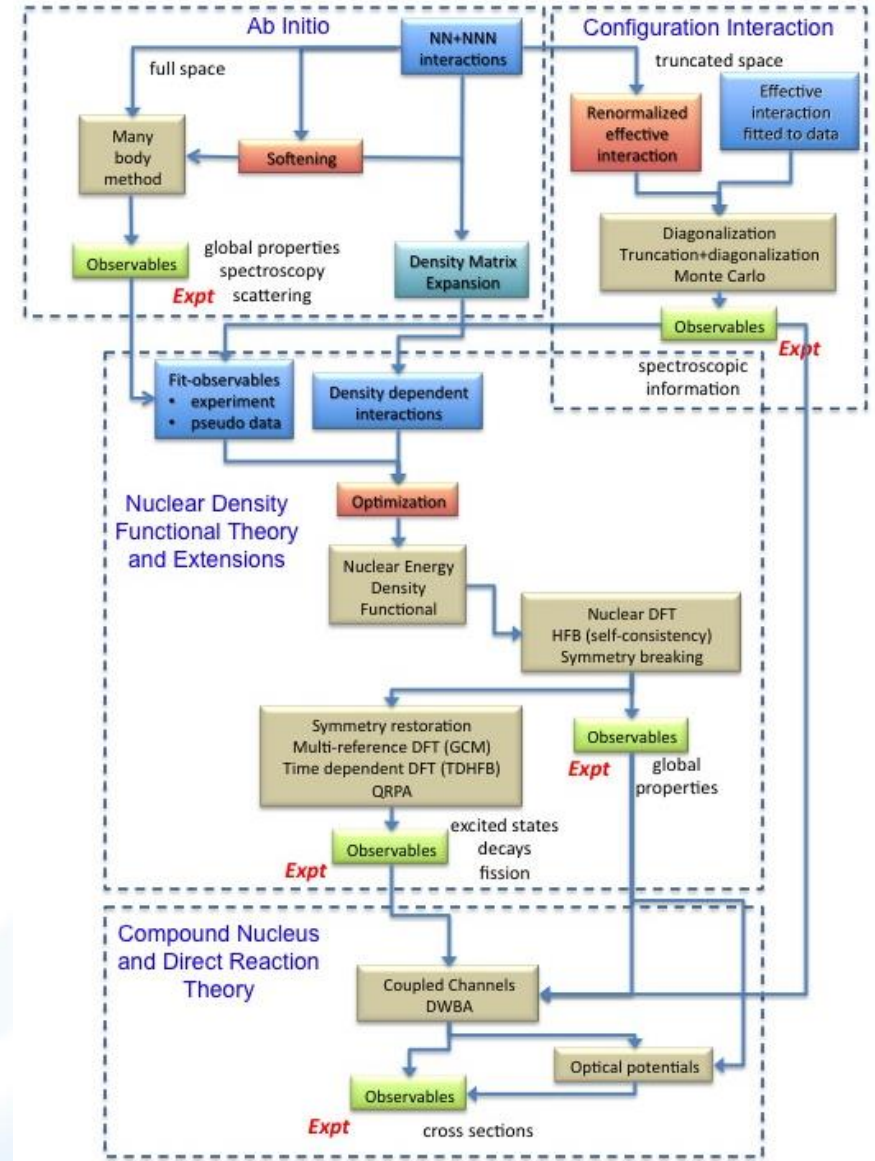
Reaction observables from Energy Density Functionals



UNEDF SciDAC Collaboration
Universal Nuclear Energy Density Functional

Main goals:

- To find an optimal energy density functional (EDF) using all our knowledge of the nucleonic Hamiltonian and basic nuclear properties.
- To apply the EDF theory and its extensions to validate the functional using all the available relevant nuclear structure data.
- To apply the validated theory to properties of interest that cannot be measured, in particular the transition properties needed for reaction theory.



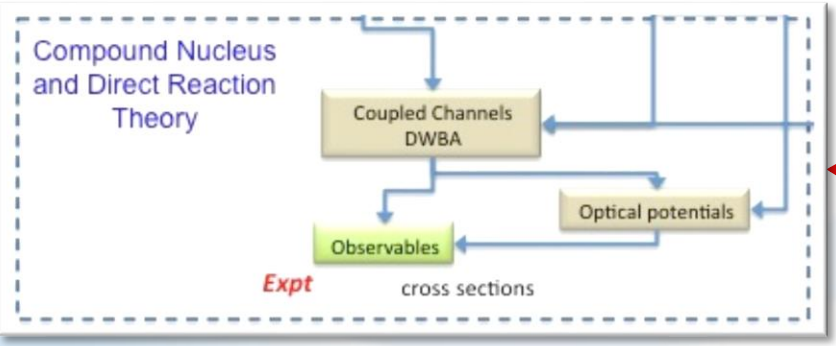
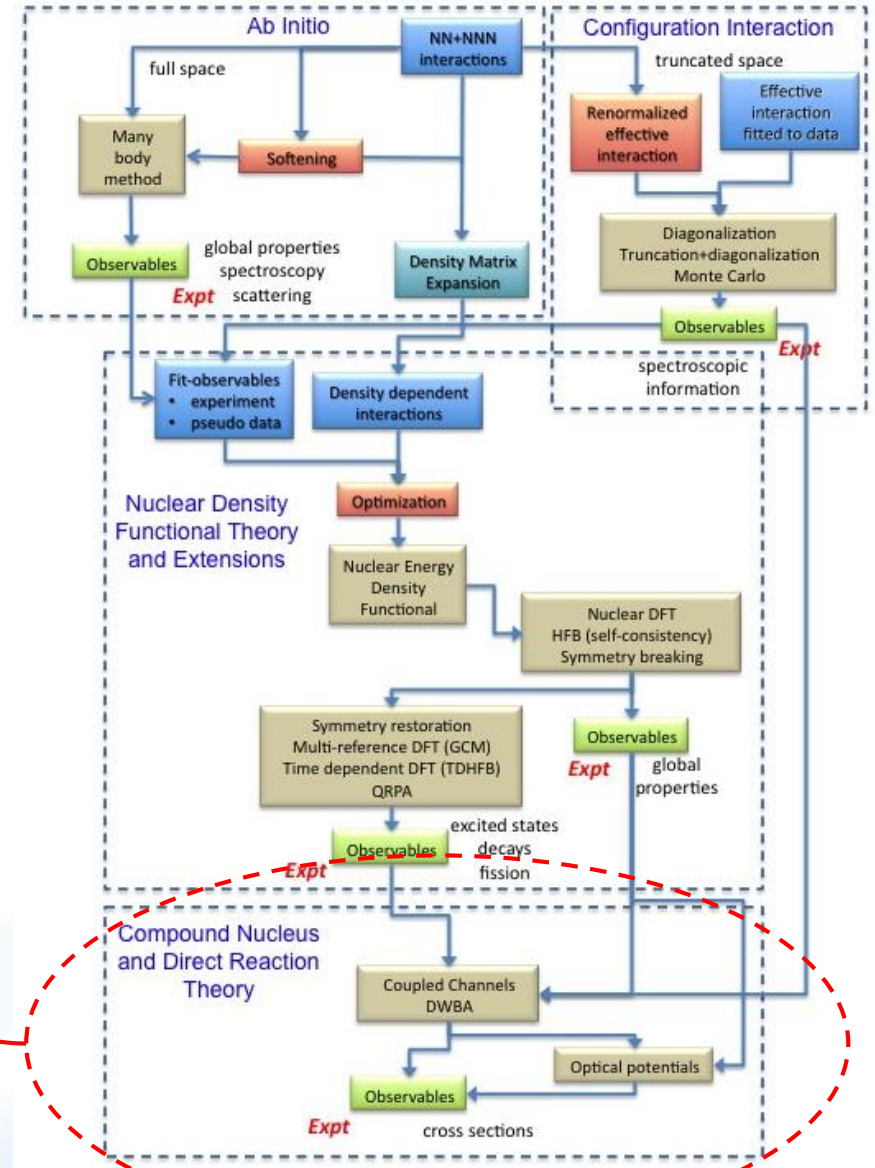
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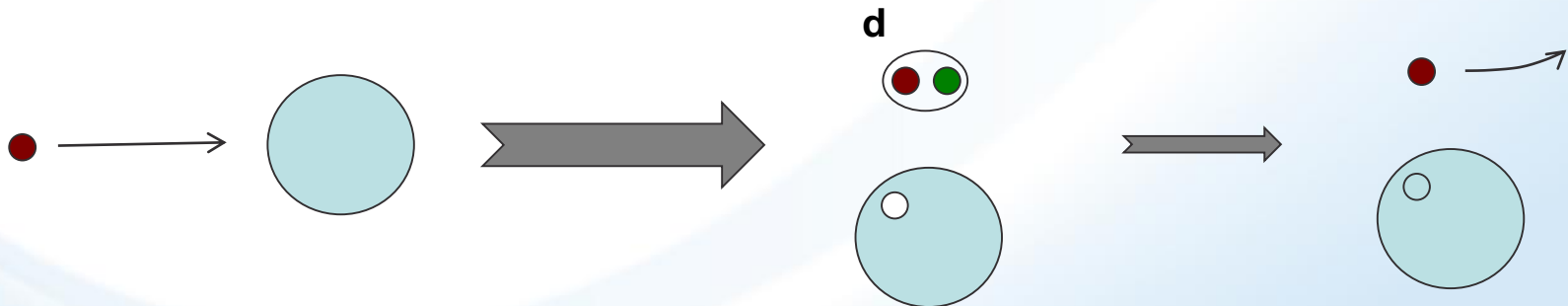


Outline of Coupled-Channels Calculations

- Mean-field HFB calculations using SLy4 Skryme functional
- Use (Q)RPA to find all levels E^* , with transition densities from the g.s.
- Structure calculations for $n,p + {}^{40,48}\text{Ca}$, ${}^{58}\text{Ni}$, ${}^{90}\text{Zr}$ and ${}^{144}\text{Sm}$
- Fold transition densities with effective n-n interaction: Transition Potentials
- Couple to all excited states, $E^* < 10, 20, 30, 40$ MeV
- Find what fraction of σ_R corresponds to inelastic couplings: **more states**, **larger σ_R** , until **all open channels** are coupled
- Couple to all pickup channels leading to deuteron formation

Outline of Coupled-Channels Calculations

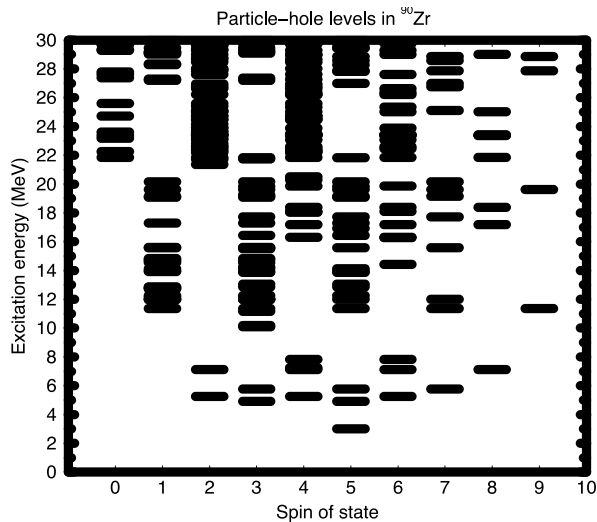
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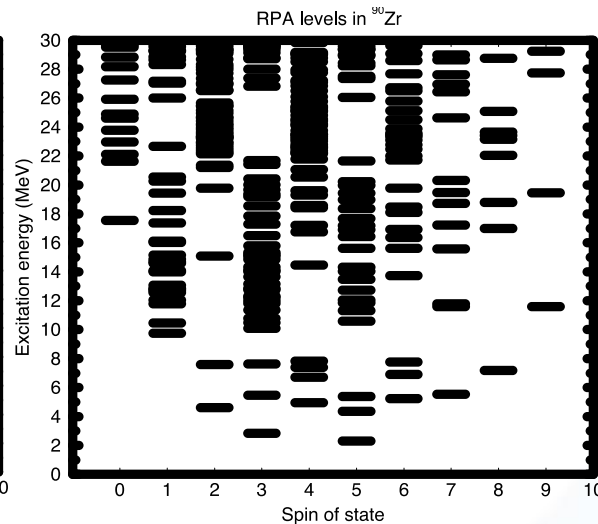
Nuclear Excited States from Mean-field Models

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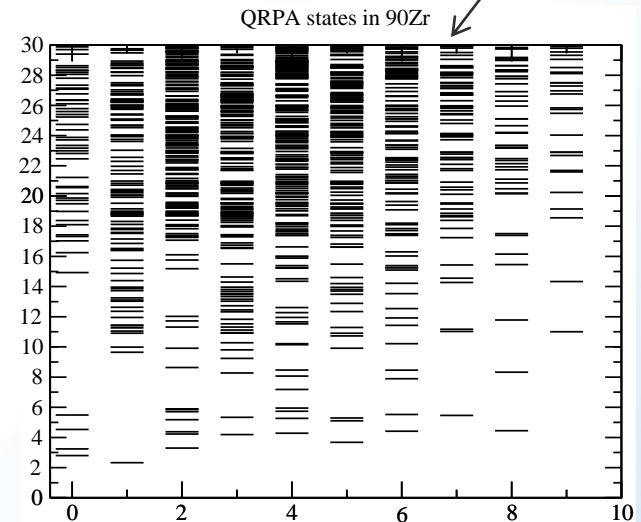
Collaboration with
Chapel Hill: Engel
& Terasaki



Uncorrelated
particle-hole states



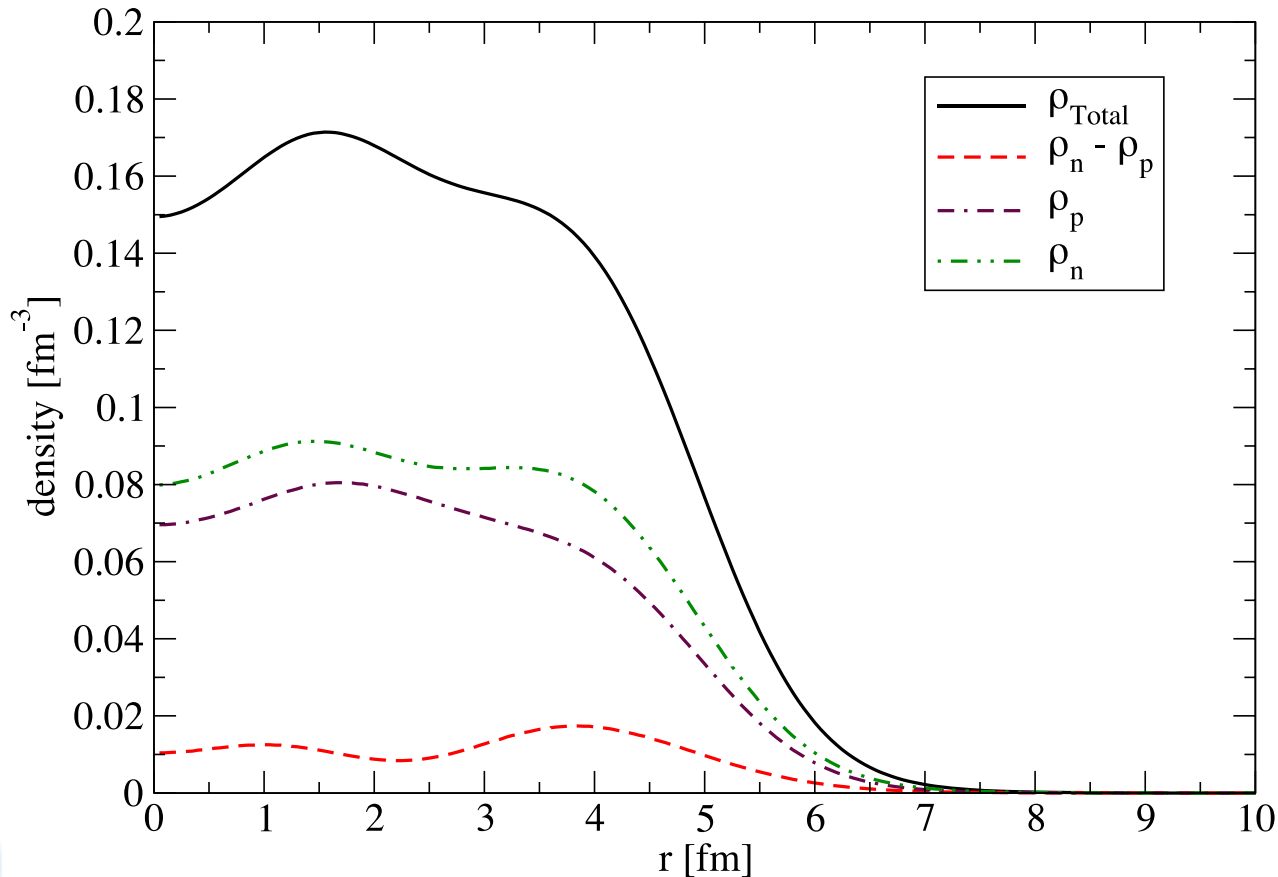
Correlated p-h
states in HO basis



Correlated p-h
states in 15 fm box

Neutron separation energy is 9.5 MeV.
Above this we have discretized continuum.

Diagonal Density



Example of diagonal
Density for ⁹⁰Zr

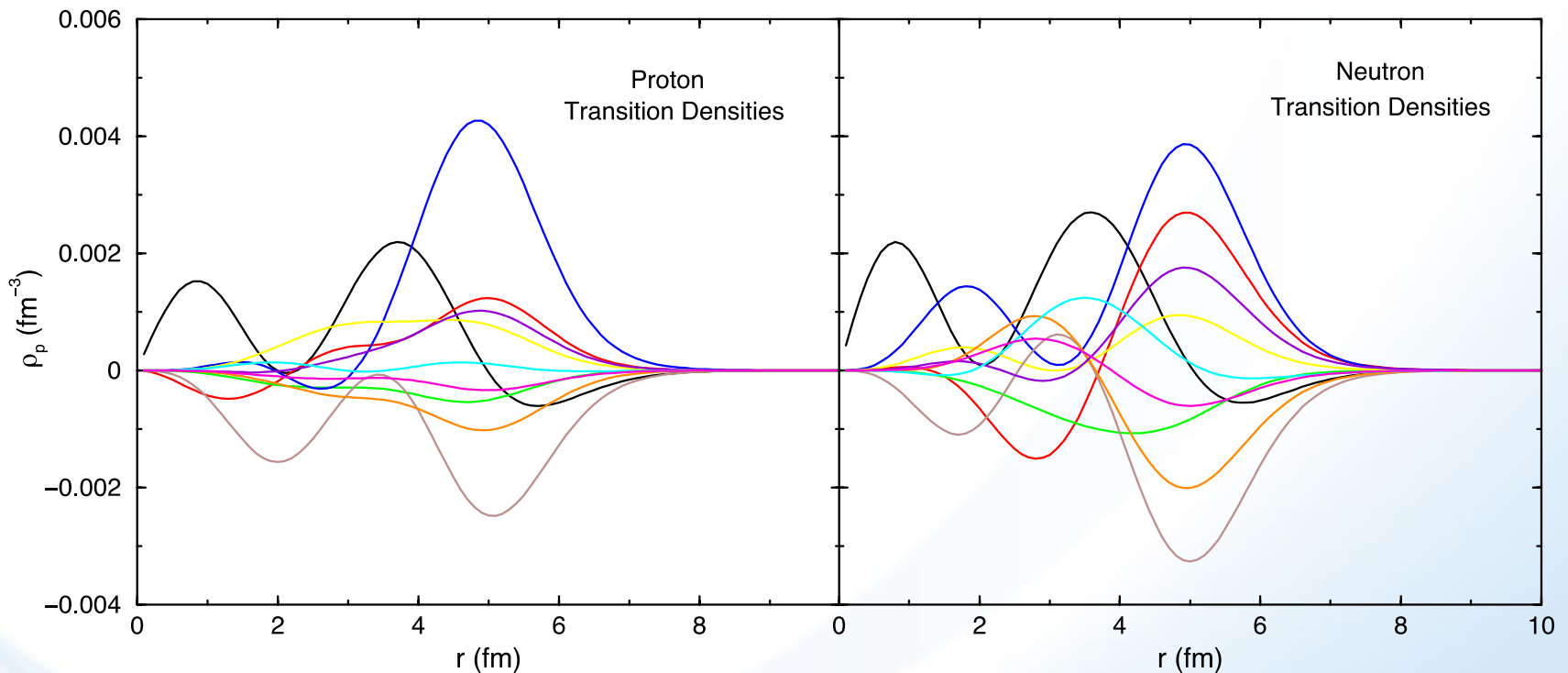
RPA

Folding of densities with n-n interaction Transition potentials

Off-Diagonal Densities

Example of off-diagonal
Transition densities for ^{90}Zr

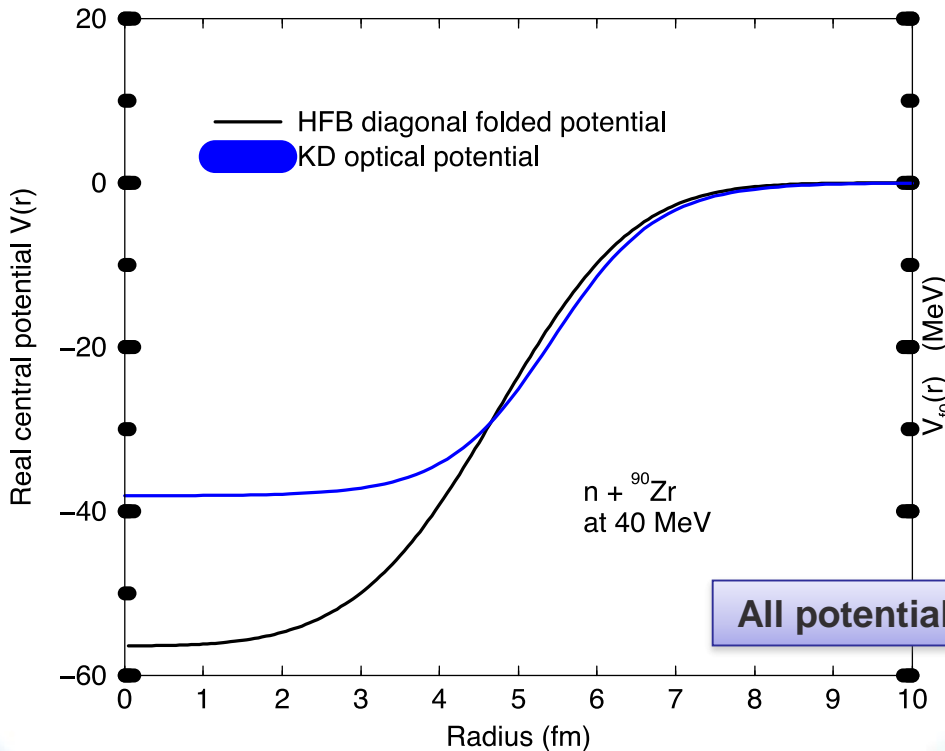
RPA
 $E^* < 10 \text{ MeV}; J_{\text{max}}^{\pi} = 4^+$



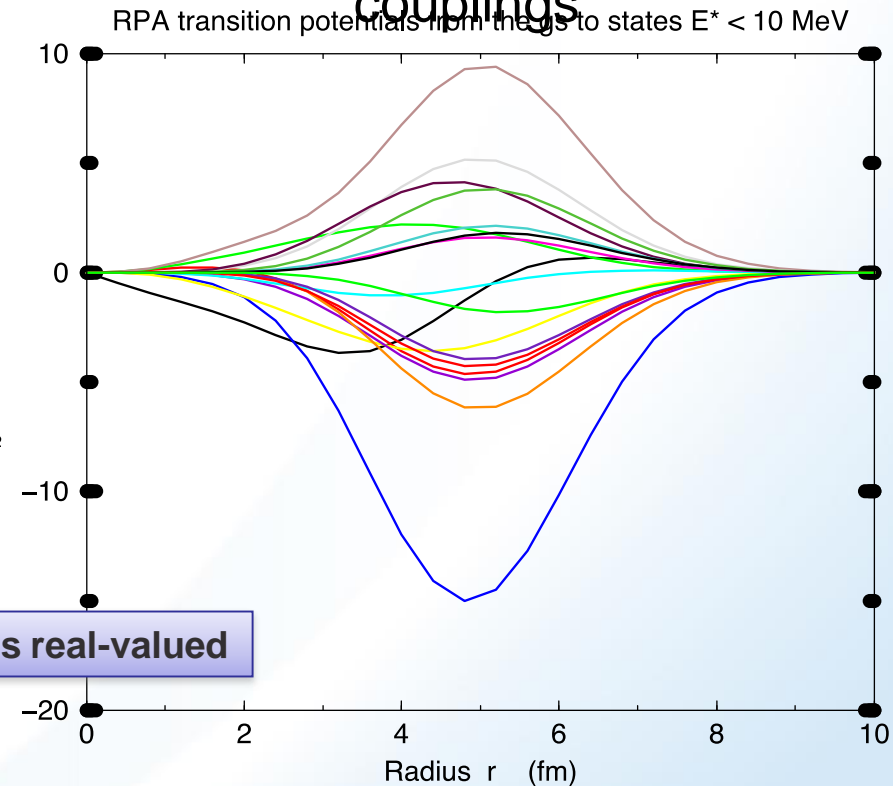
Folding of densities with n-n interaction Transition potentials

Transition densities to Transition potentials

Diagonal folded potential



Off-diagonal couplings



All potentials real-valued

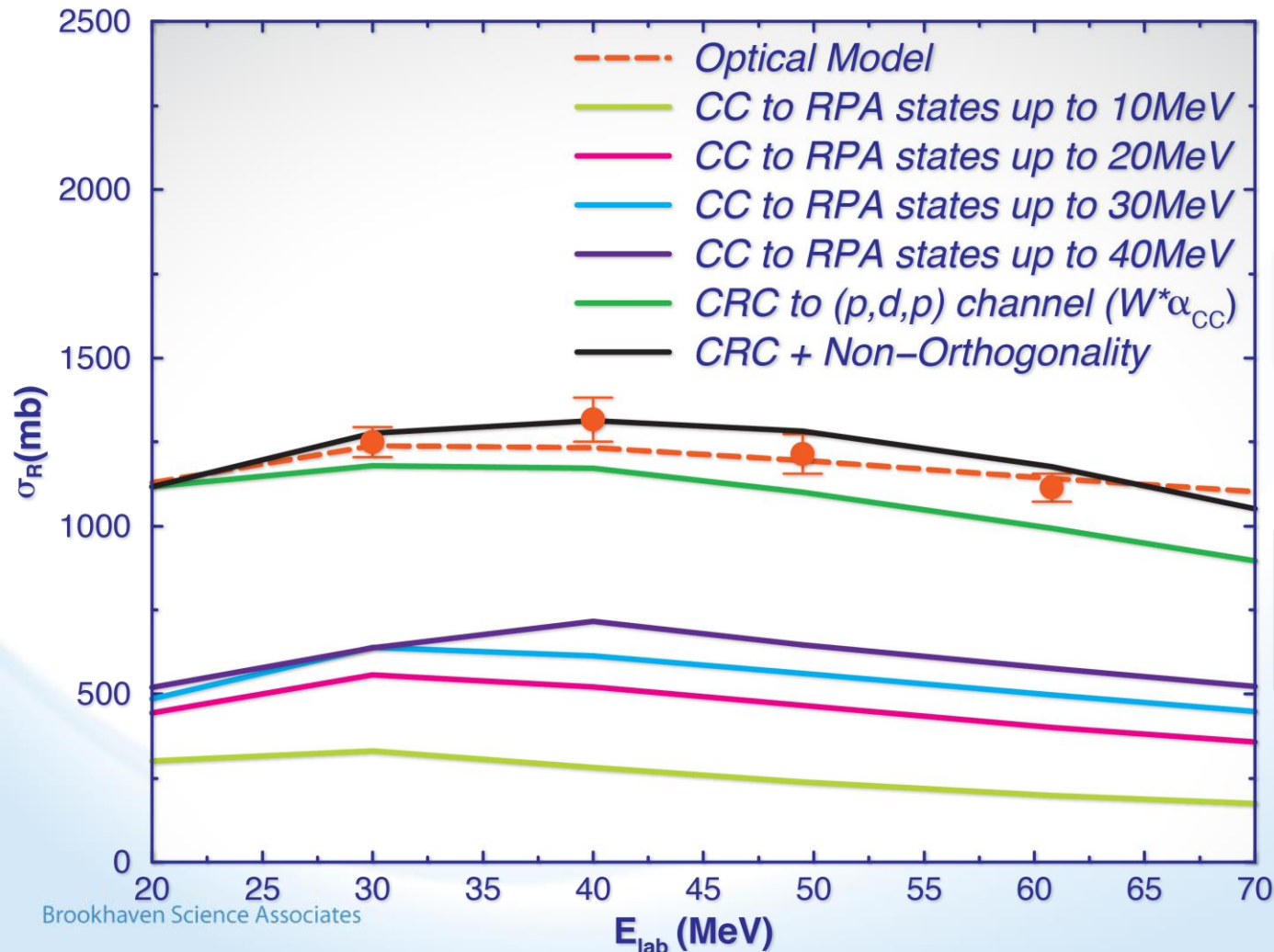
Natural parity states only: no spin-flip, so no spin-orbit forces generated.
No energy or density dependence. Exchange contributions included implicitly.

(So far...)

Comparison with Experimental Data

$p + {}^{90}\text{Zr}$

Total Reaction Cross-sections

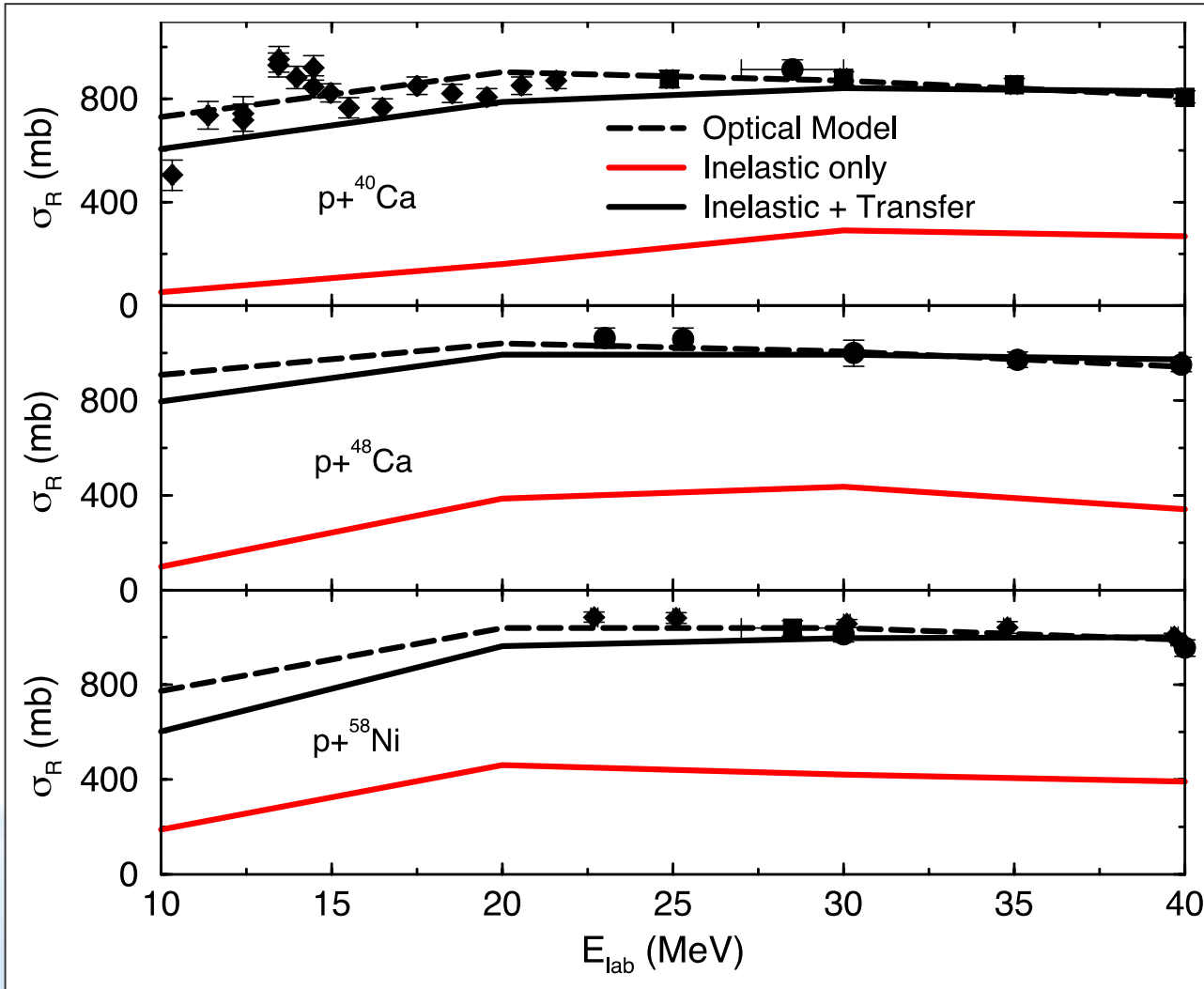


Inelastic convergence when coupling up to all open channels

Good description of experimental data!

Inelastic and pick-up channels account for all reaction cross sections

Comparison with Experimental Data



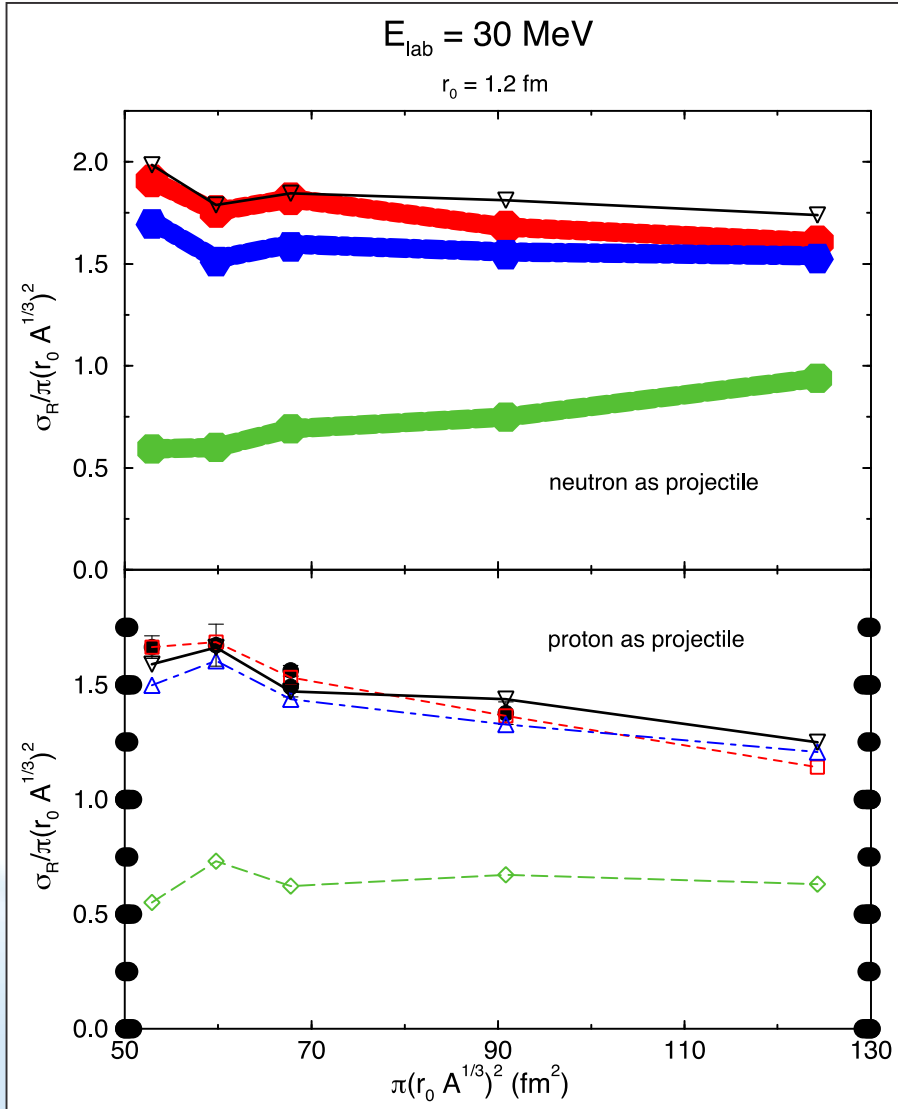
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Inelastic and pick-up channels account for all reaction cross sections

G. P. A. Nobre, F.S. Dietrich, J. E. Escher, I. J. Thompson, M. Dupuis, J. Terasaki and J. Engel

Phys. Rev. Lett. 105, 202502 (2010)

Summary of Results at $E_{\text{lab}} = 30 \text{ MeV}$



Targets

^{40}Ca , ^{48}Ca , ^{58}Ni , ^{90}Zr , ^{144}Sm

- Phenomenological Optical Model
- Inelastic couplings only
- · - Inelastic + Transfer
- Inelastic + Transfer with non-orthogonality

With all couplings, calculations agree with experimental data

Phys. Rev. Lett. 105, 202502 (2010)
Phys. Rev. C 84, 064609 (2011)

G. P. A. Nobre, F.S. Dietrich, J. E. Escher, I. J. Thompson, M. Dupuis, J. Terasaki and J. Engel

Two-Step Approximation

We found we need only two-step contributions

- These simply add for all $j=1, N$ inelastic & transfer states:

$$V_{\text{DPP}} = \sum_j^N V_{0j} G_j V_{j0}.$$

$G_j = [E_n - e_j - H_j]^{-1}$: channel- j Green's function

$V_{j0} = V_{0j}$: coupling from elastic channel to excited state j

- Gives $V_{\text{DPP}}(r, r', L, E_n)$: nonlocal, L - and E -dependent.

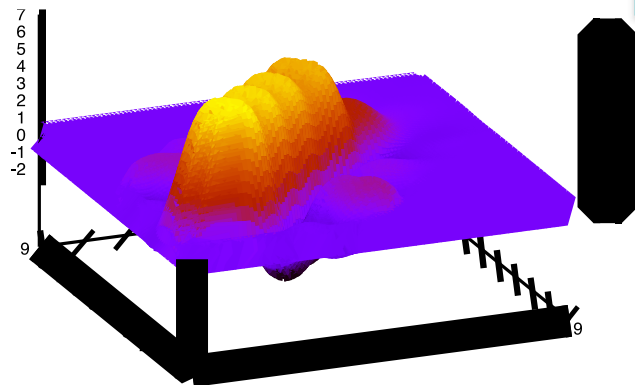
In detail: $V_{\text{DPP}}(r, r', L, E_n) = \sum_j^N V_{0j}(r) G_{jL}(r, r') V_{j0}(r') = V + iW$

- Quadratic in the effective interactions in the couplings V_{ij}
- Can be generalized to non-local $V_{ij}(r, r')$ more easily than CCh.
- Treat any higher-order couplings as a perturbative correction

Tried by Coulter & Satchler (1977), but only some inelastic states included

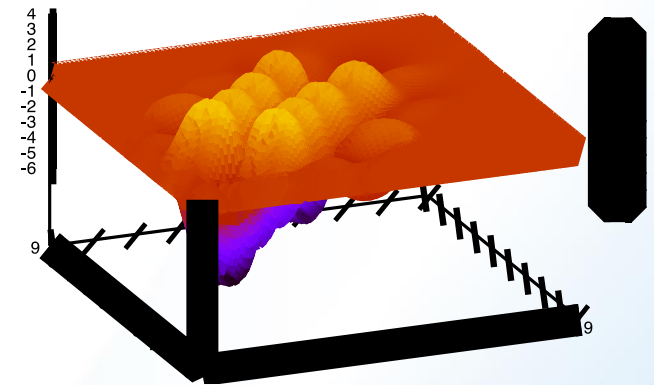
Calculated Nonlocal Potentials $V(r,r')$ now

Real

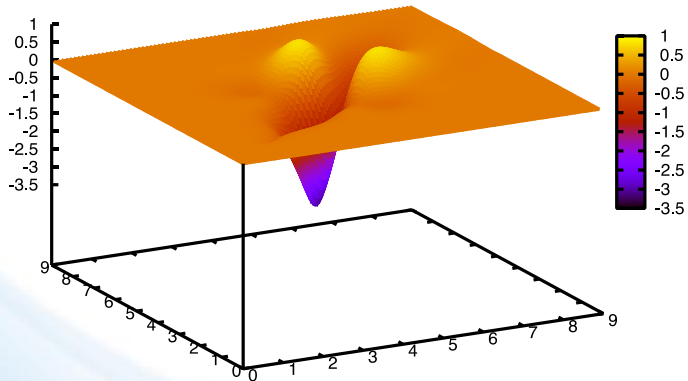


$n + {}^{90}\text{Zr}$
 $E_{\text{lab}} = 40 \text{ MeV}$
Inelastic + transfer

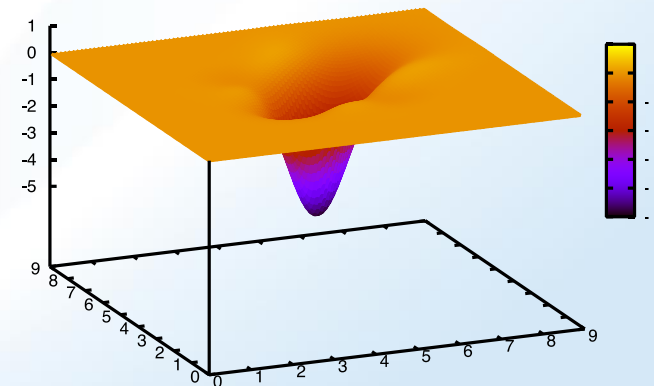
Imaginary



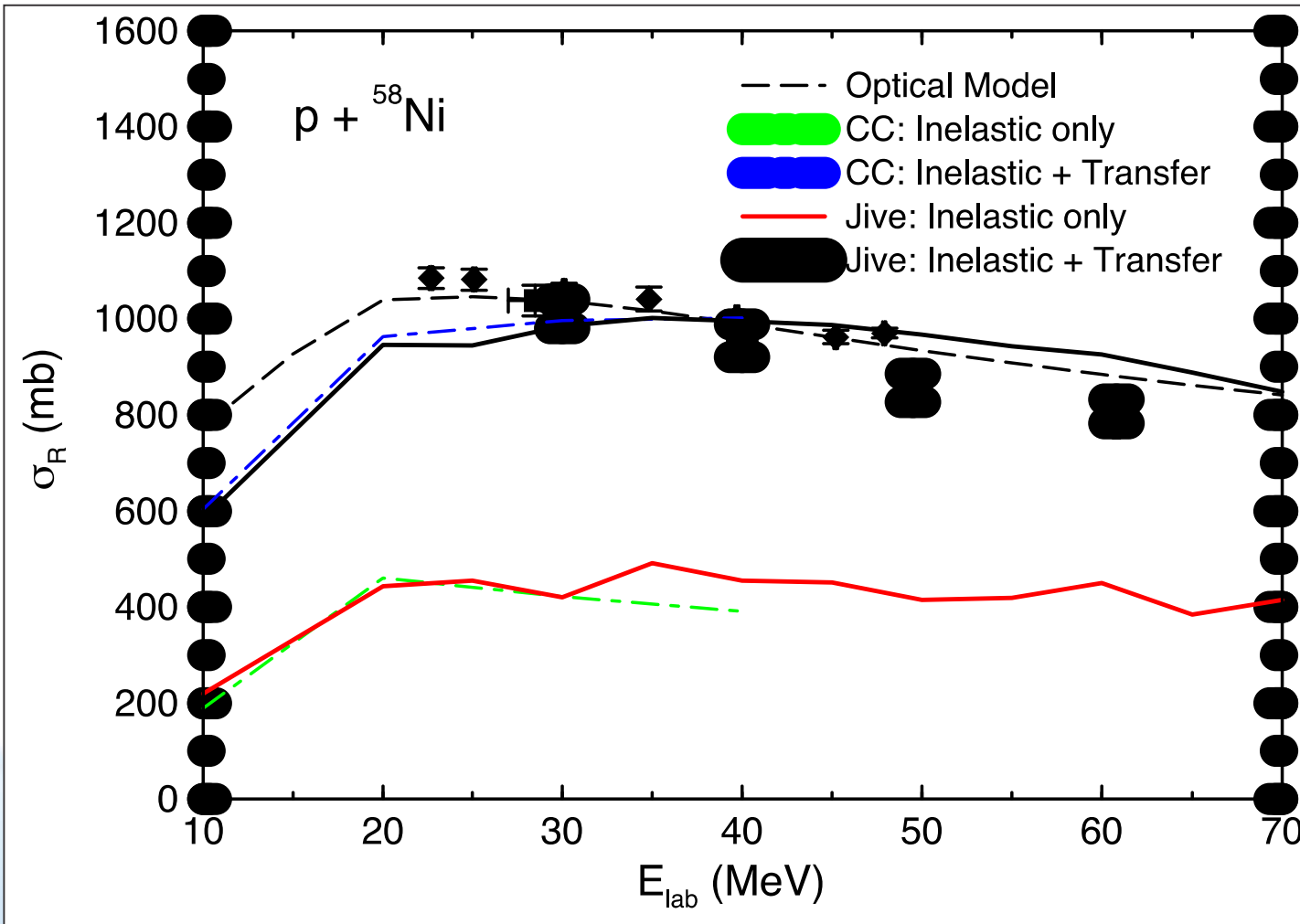
$L=0$



$L=9$
(~ grazing)



$p + {}^{58}\text{Ni}$ – Coupled Channels and Two-Step Approach



Two-step method allows to perform calculations at higher energies, coupling to higher states.

Conclusion

- Predictive models are crucial for progress of reaction evaluations
 - Evaluations are a link between nuclear science and applications
 - Collaboration with scientific community (both structure and reaction) is indispensable
 - Win-win: fundamental models will improve evaluations and allow for new ones; evaluations will point new ways to go that can directly impact applications
-
- Collaboration
 - Incorporate latest theoretical models
 - Benchmark our evaluations against most recent data

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