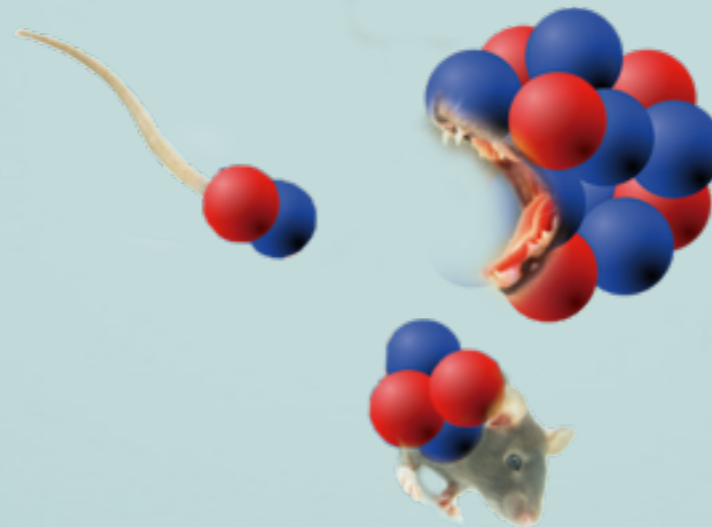




# Study of Inclusive Breakup Reactions Induced by Weakly Bound Nuclei



JIN LEI  
Ohio University  
Universidad de Sevilla

ANTONIO M. MORO  
Universidad de Sevilla





# Contents

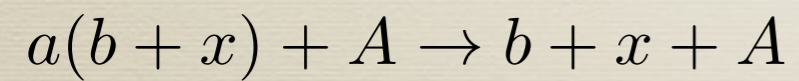
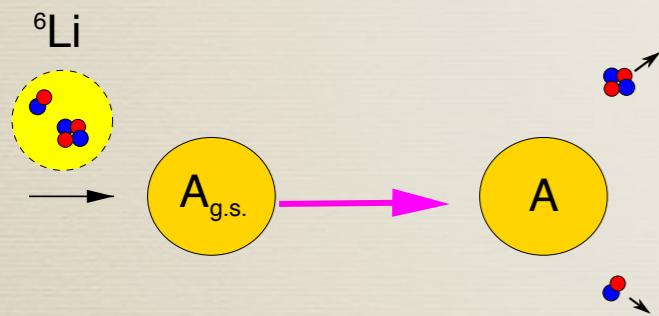
- ◆ Motivation
- ◆ The Ichimura, Austern and Vincent Model
- ◆ Applications
- ◆ Summary and Perspectives

# Motivation



# Introduction

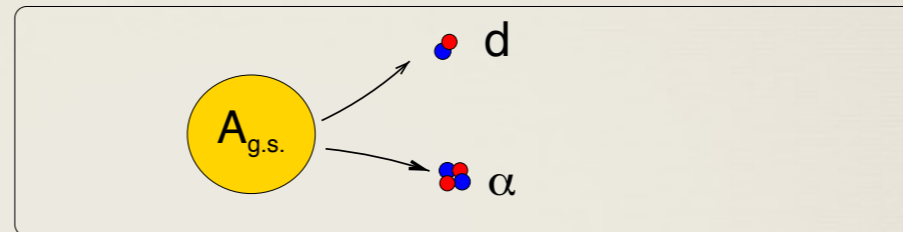
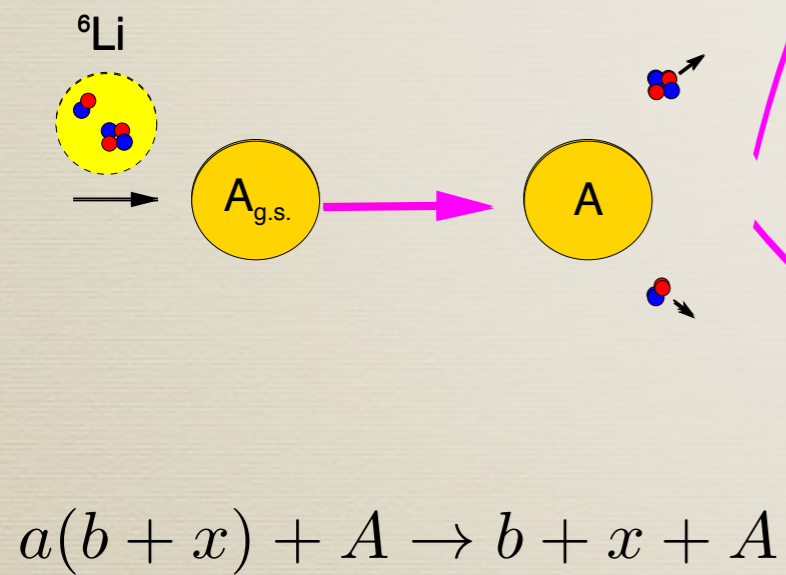
## Exclusive breakup



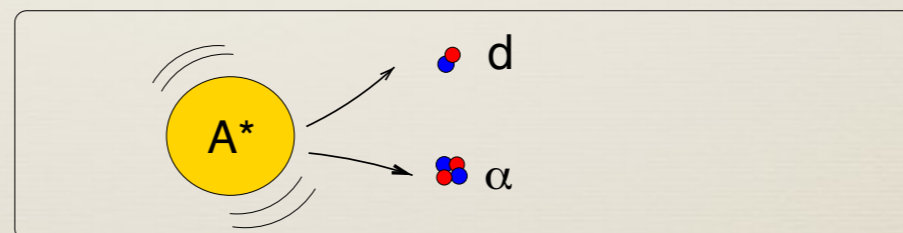


# Introduction

## Exclusive breakup



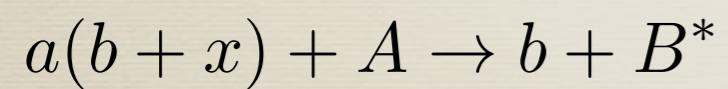
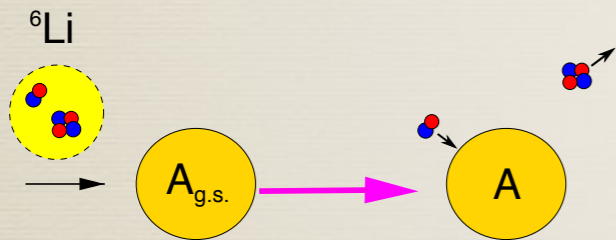
ELASTIC BREAKUP (EBU)  
("diffraction")



INELASTIC BREAKUP

# Introduction

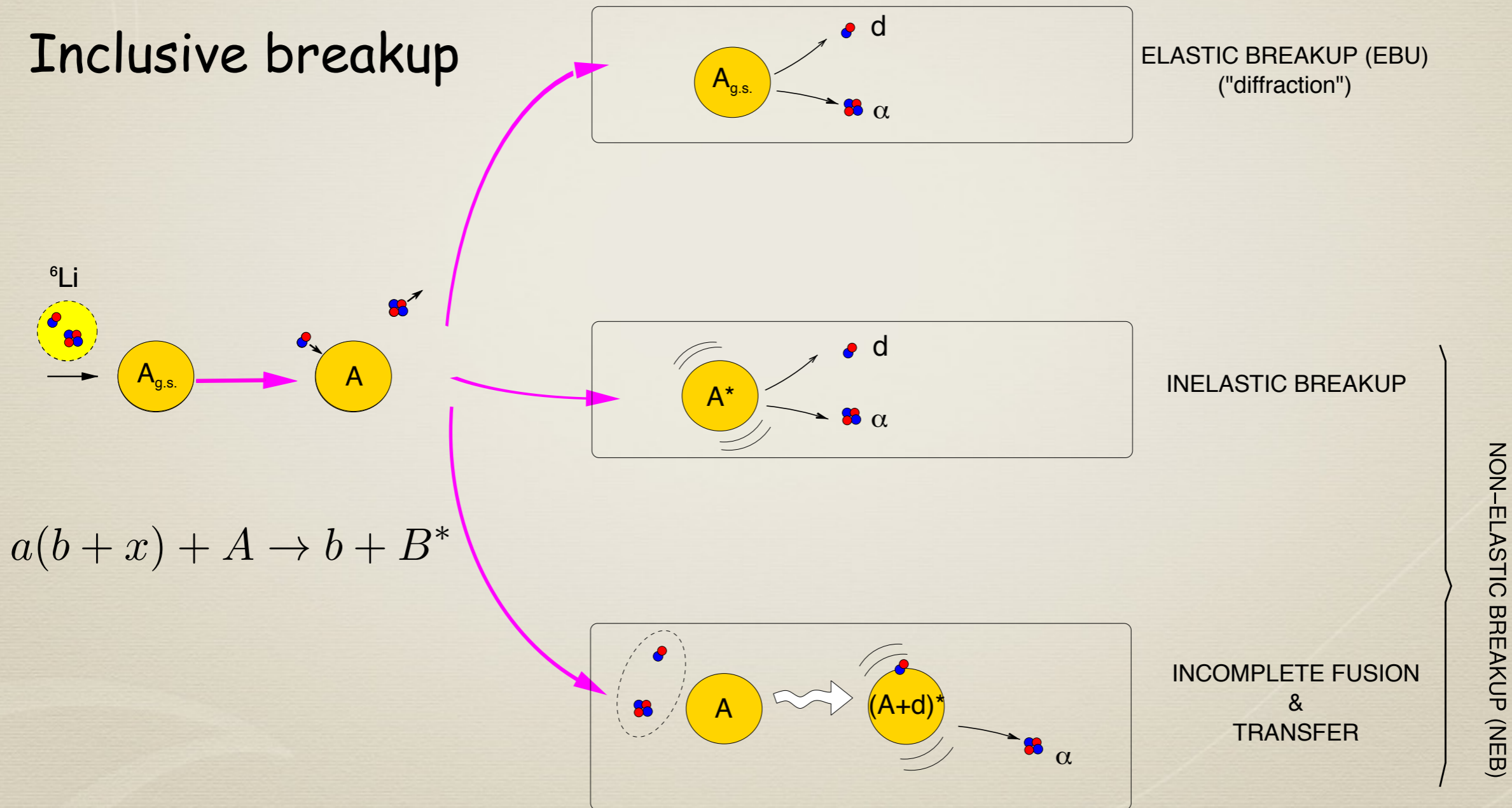
## Inclusive breakup





# Introduction

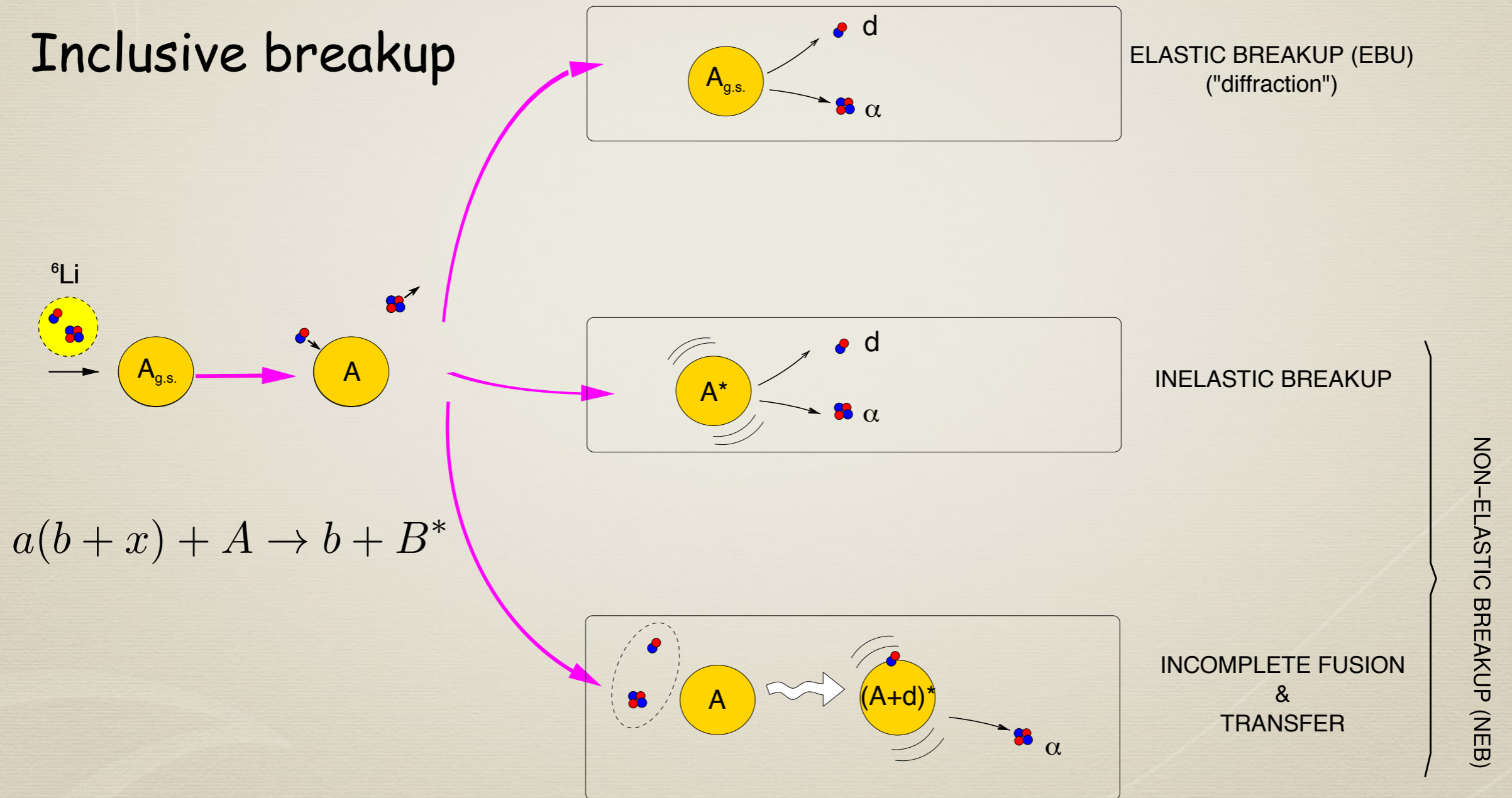
## Inclusive breakup



# Introduction

CDCC/Faddeev 😊

## Inclusive breakup

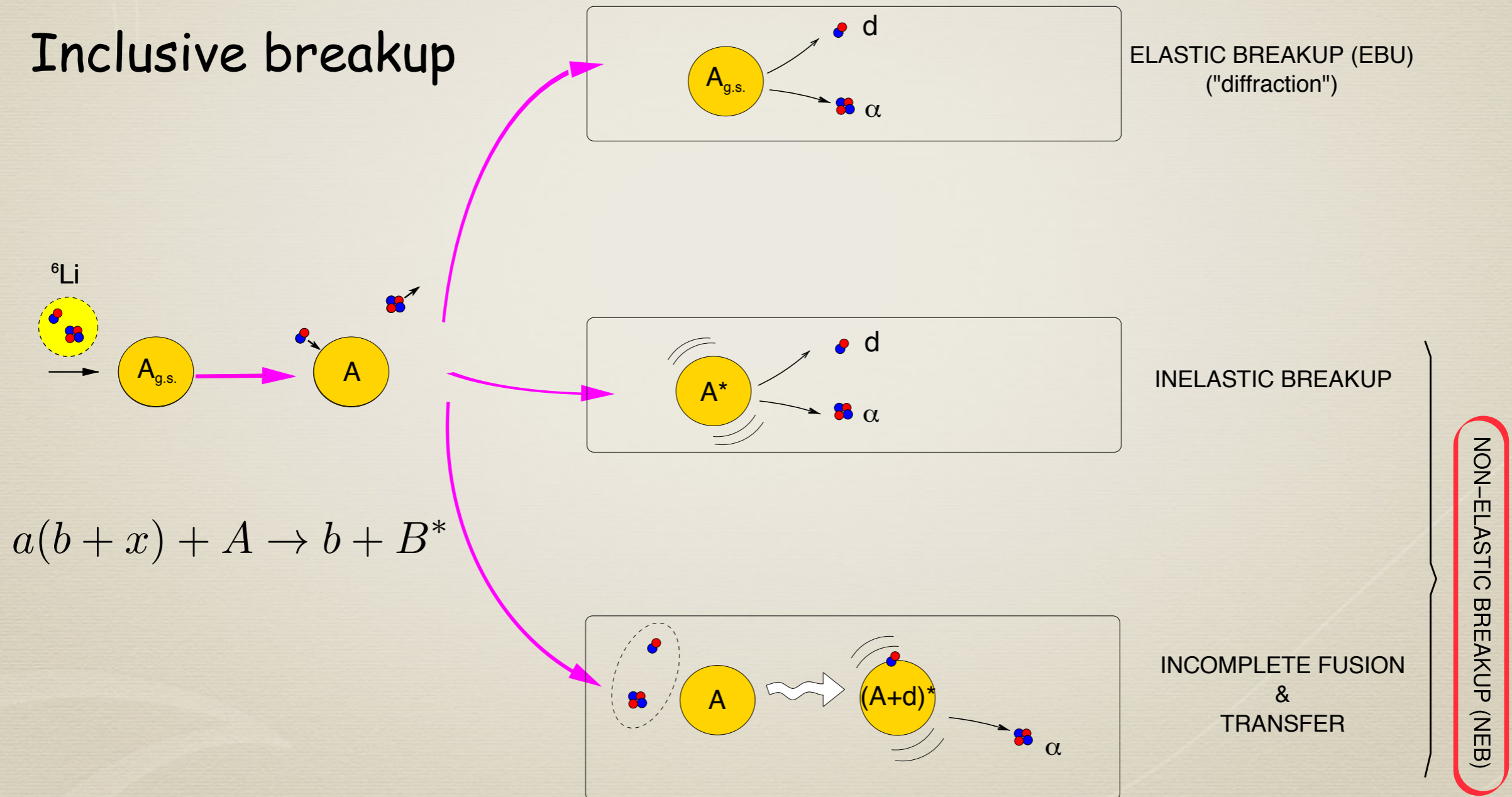




# Introduction

CDCC/Faddeev 😊

## Inclusive breakup



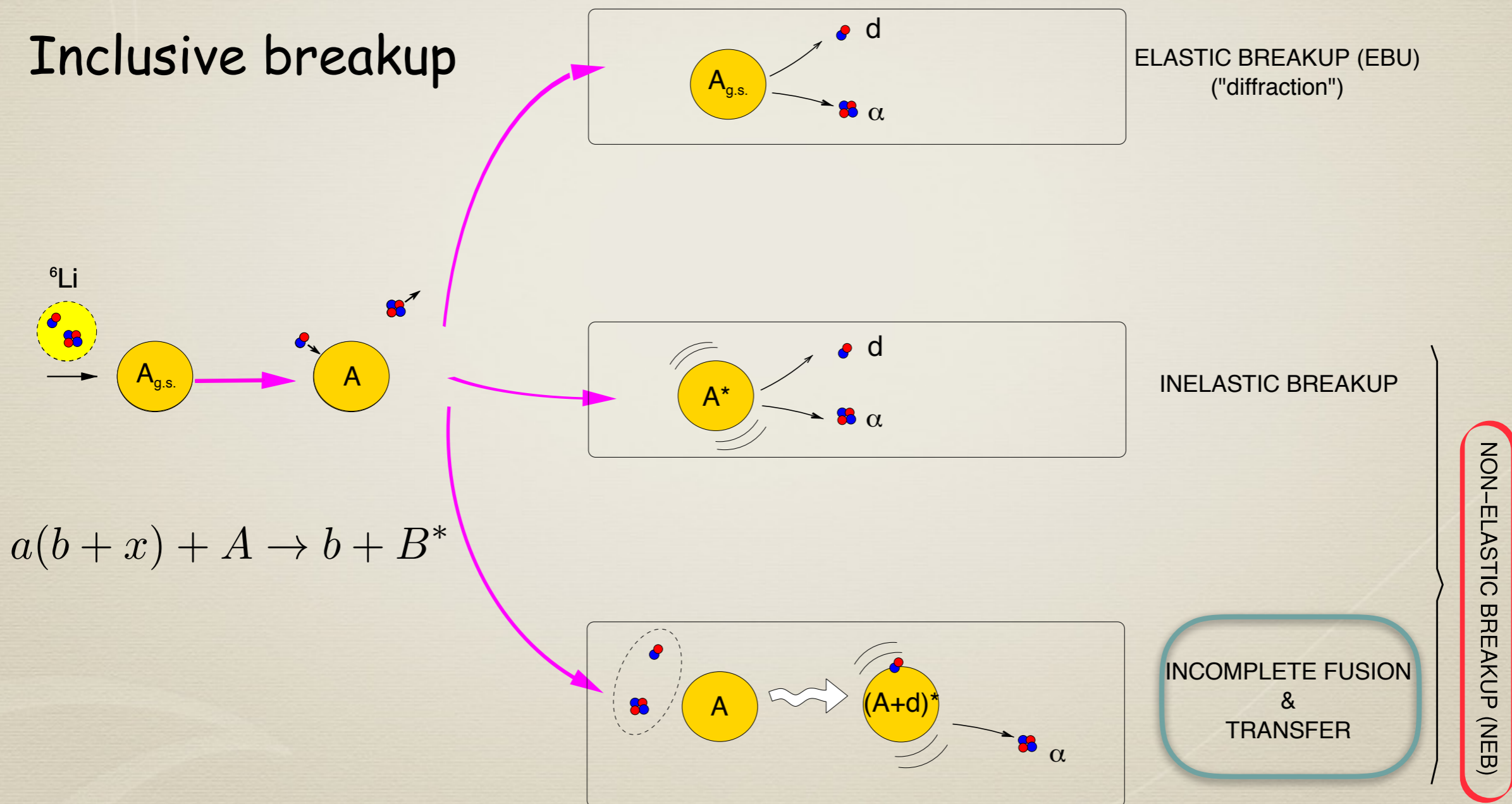
NON-ELASTIC BREAKUP (NEB)



# Introduction

CDCC/Faddeev 😊

## Inclusive breakup



NON-ELASTIC BREAKUP (NEB)

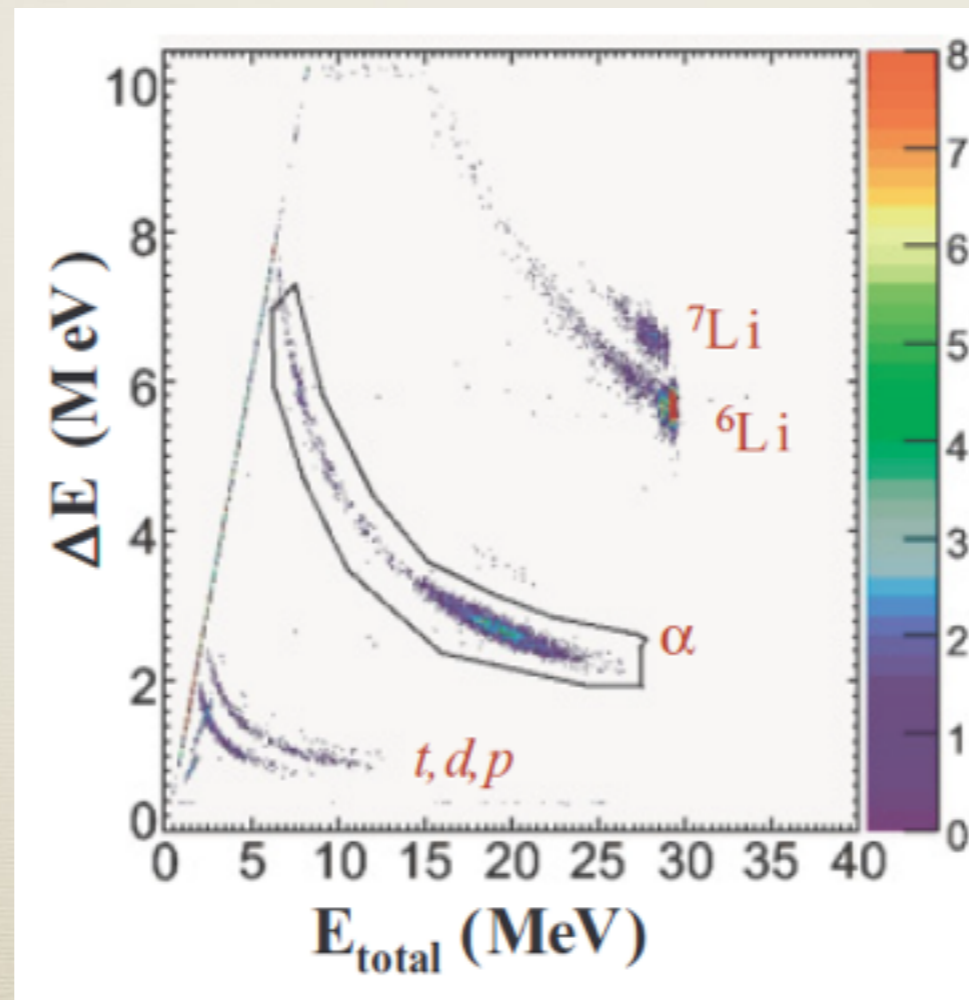




# Motivation

# Motivation

- \* Understanding of large inclusive alpha yields ( ${}^6\text{Li}$ ,  ${}^7\text{Be}$ ,  ${}^7\text{Li}$ ...).





# Motivation

- \* Understanding of large inclusive alpha yields ( ${}^6\text{Li}$ ,  ${}^7\text{Be}$ ,  ${}^7\text{Li}$ ...).
- \* Inclusive breakup reactions with halo nuclei ( ${}^{11}\text{Be}$ ,  ${}^6\text{He}$ ,  ${}^8\text{B}$ ...).

# Motivation

- \* Understanding of large
- \* Inclusive breakup react

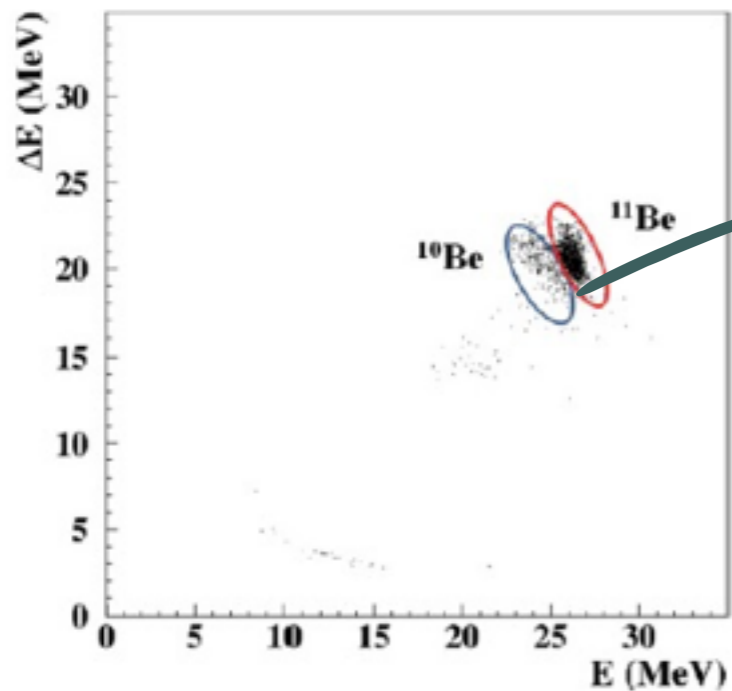


FIG. 12. (Color online)  $\Delta E$ - $E$  scatterplot for the collision  $^{11}\text{Be}+^{64}\text{Zn}$  at  $\theta = 39^\circ$ .

A. Di Pietro PRC 85, 054607 (2012)

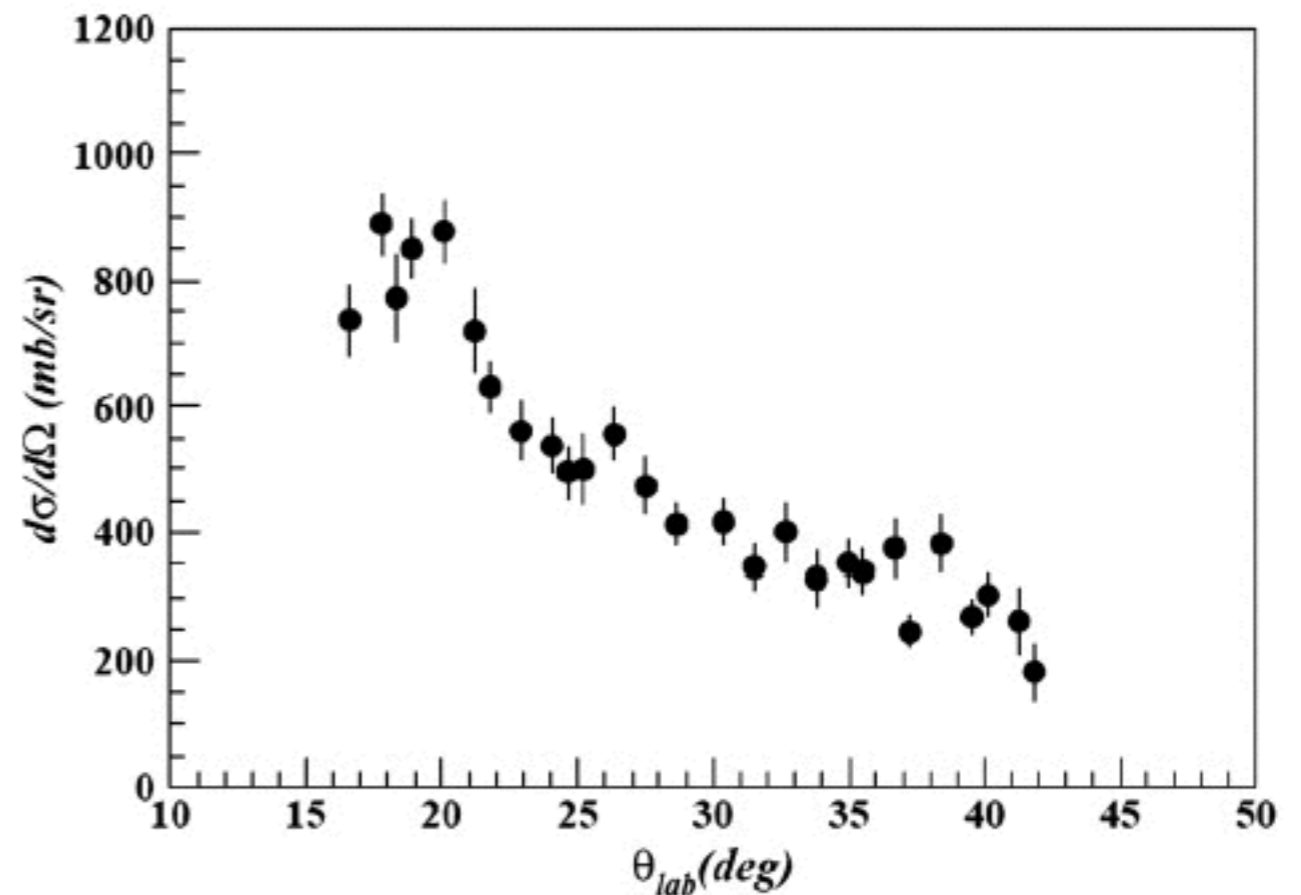
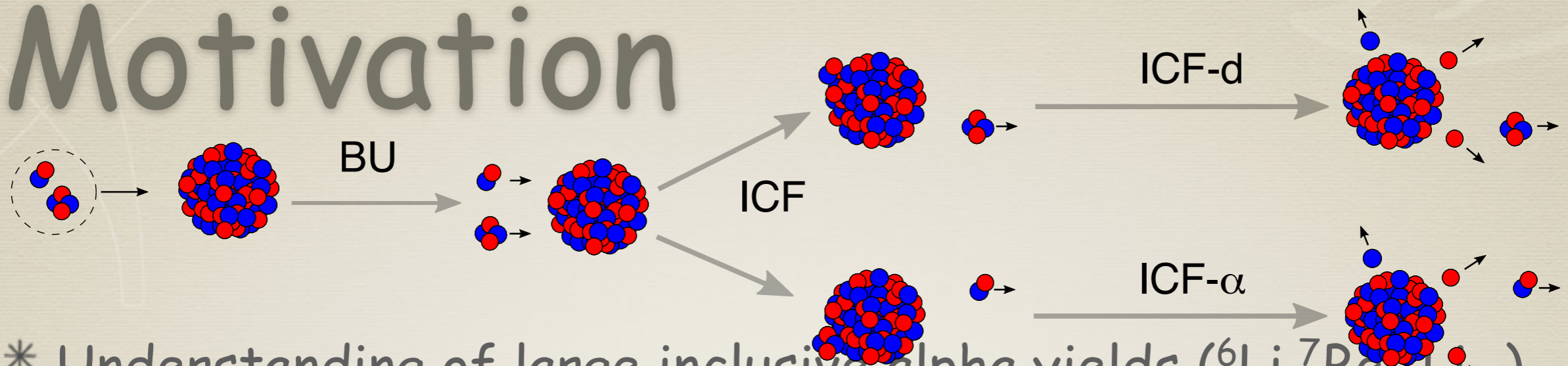


FIG. 3. AD of transfer or breakup events in  $^{11}\text{Be} + ^{64}\text{Zn}$  obtained by selecting  $^{10}\text{Be}$  events in the  $\Delta E$ - $E$  spectrum.

A. Di Pietro PRL 105, 022701 (2010)



# Motivation



\* Understanding of large inclusive alpha yields ( ${}^6\text{Li}$ ,  ${}^7\text{Be}$ ,  $\text{Li}\dots$ ).

\* Inclusive breakup reactions with halo nuclei ( ${}^{11}\text{Be}$ ,  ${}^6\text{He}$ ,  ${}^8\text{B}\dots$ ).

\* Incomplete fusion ( ${}^6\text{Li}$ ,  ${}^7\text{Li}$ ).

◆ Surrogate reactions (d,pf).

# Motivation

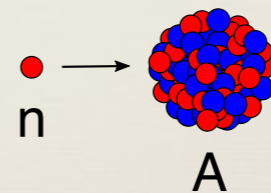
\* Understanding of large inclusive alpha yields ( ${}^6\text{Li}, {}^7\text{Be}, {}^7\text{Li}\dots$ ).

\* Inclusive breakup reactions with halo nuclei ( ${}^{11}\text{Be}, {}^6\text{He}, {}^8\text{B}\dots$ ).

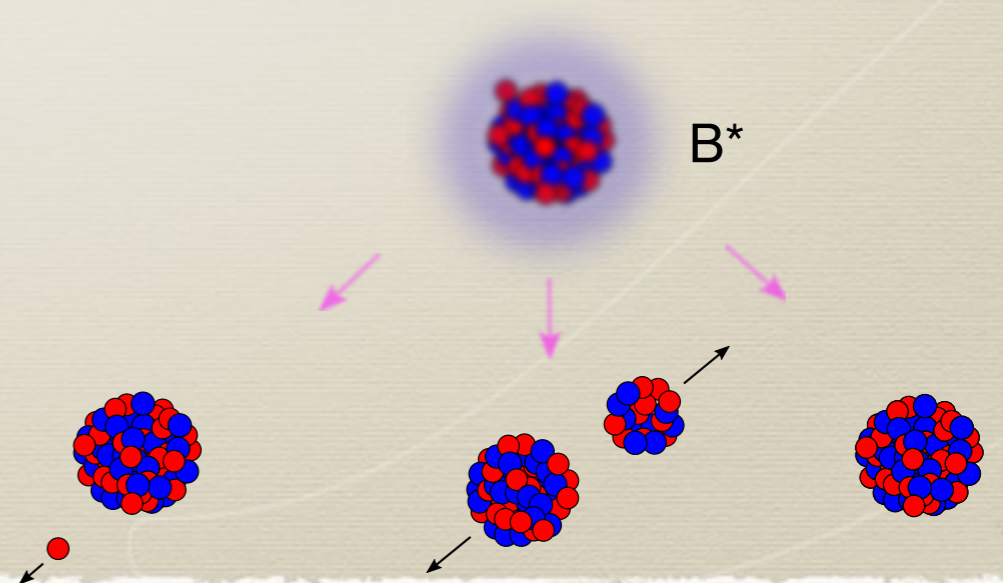
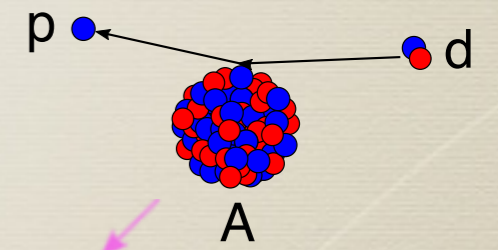
\* Incomplete fusion ( ${}^6\text{Li}, {}^7\text{Li}$ ).

◆ Surrogate reactions (d,pf).

Desired Reaction



Surrogate Reaction





# The Ichimura, Austern and Vincent Model

# Theories for inclusive breakup



# Theories for inclusive breakup

- ✿ **Prior Form**
  - ✿ Kerman, McVoy(KM)
  - ✿ Udagawa, Tamura(UT)

# Theories for inclusive breakup

## ★ Prior Form

- ★ Kerman, McVoy(KM)
- ★ Udagawa, Tamura(UT)

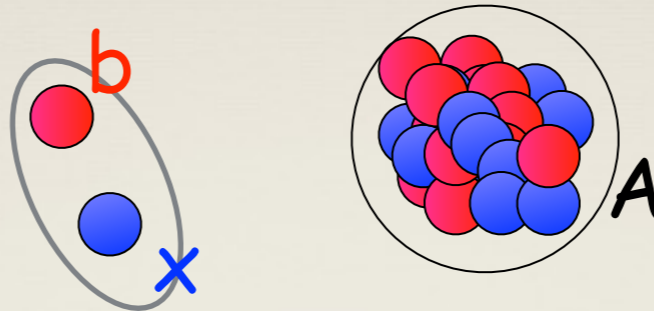
*vs*

## ★ Post Form

- ★ Baur & co: surface approximation
- ★ Ichimura, Austern,  
Vincent(IAV):sum rule



# Theories for inclusive breakup



## ✦ Prior Form

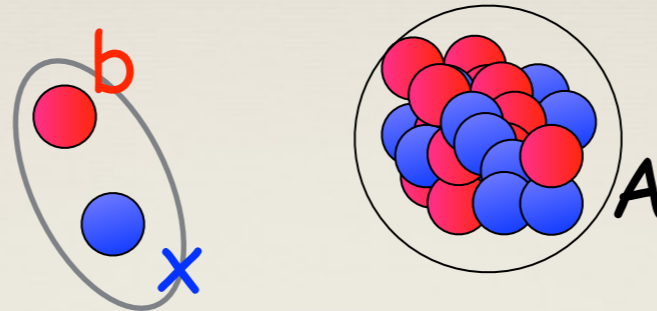
- ✦ Kerman, McVoy(KM)
- ✦ Udagawa, Tamura(UT)

*vs*

## ✦ Post Form

- ✦ Baur & co: surface approximation
- ✦ Ichimura, Austern, Vincent(IAV):sum rule

# Theories for inclusive breakup



## ★ Prior Form

- ★ Kerman, McVoy(KM)
- ★ Udagawa, Tamura(UT)

vs

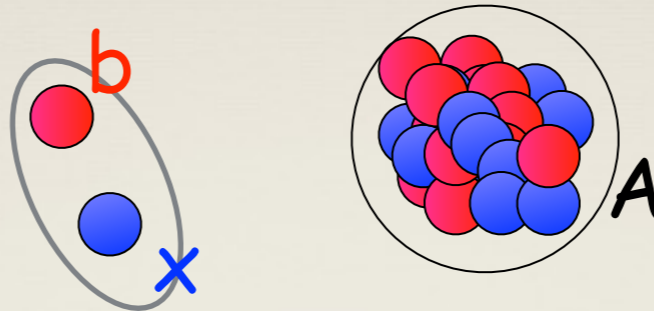
## ★ Post Form

- ★ Baur & co: surface approximation
- ★ Ichimura, Austern, Vincent(IAV):sum rule

$$\mathcal{H} = T + H_A + V_{bx} + U_{xA} + U_{bA}$$



# Theories for inclusive breakup



## ★ Prior Form

- ★ Kerman, McVoy(KM)
- ★ Udagawa, Tamura(UT)

vs

## ★ Post Form

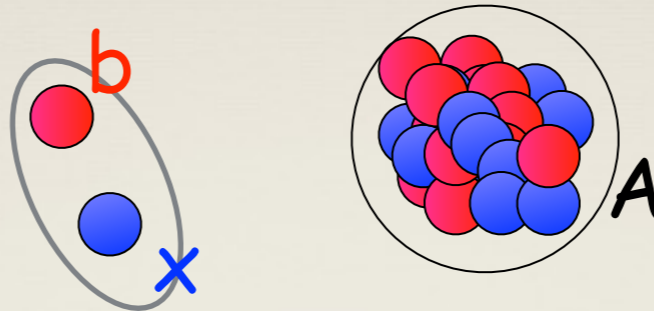
- ★ Baur & co: surface approximation
- ★ Ichimura, Austern, Vincent(IAV):sum rule

$$\mathcal{H} = T + H_A + V_{bx} + U_{xA} + U_{bA}$$

$$\mathcal{H} = T + H_A + V_{bx} + V_{xA} + U_{bA}$$



# Theories for inclusive breakup



## ★ Prior Form

- ★ Kerman, McVoy(KM)
- ★ Udagawa, Tamura(UT)

*vs*

## ★ Post Form

- ★ Baur & co: surface approximation
- ★ Ichimura, Austern, Vincent(IAV):sum rule

$$\mathcal{H} = T + H_A + V_{bx} + \underbrace{U_{xA}}_{\text{circled}} + U_{bA}$$

$$\mathcal{H} = T + H_A + V_{bx} + \underbrace{V_{xA}}_{\text{circled}} + U_{bA}$$



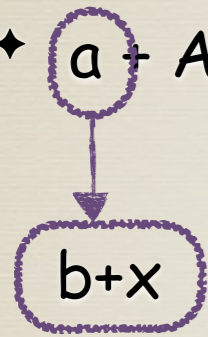
# The Ichimura, Austern, Vincent Model

- ✿ Inclusive breakup :
  - ✦  $a + A \longrightarrow b + \text{anything}$

# The Ichimura, Austern, Vincent Model

✿ Inclusive breakup :

✦  $a + A \longrightarrow b + \text{anything}$

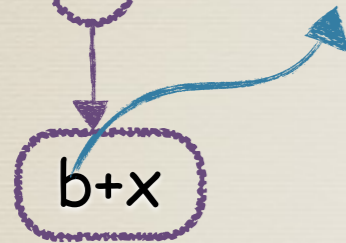




# The Ichimura, Austern, Vincent Model

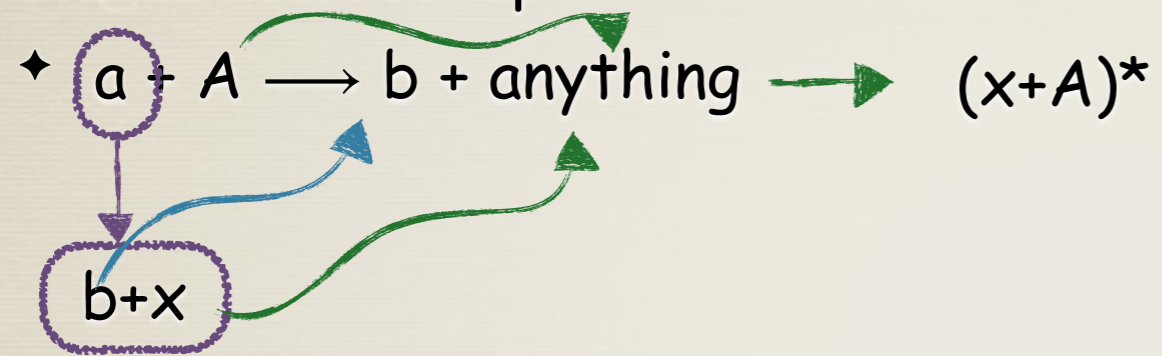
✿ Inclusive breakup :

✦  $a + A \longrightarrow b + \text{anything}$



# The Ichimura, Austern, Vincent Model

✿ Inclusive breakup :





# The Ichimura, Austern, Vincent Model

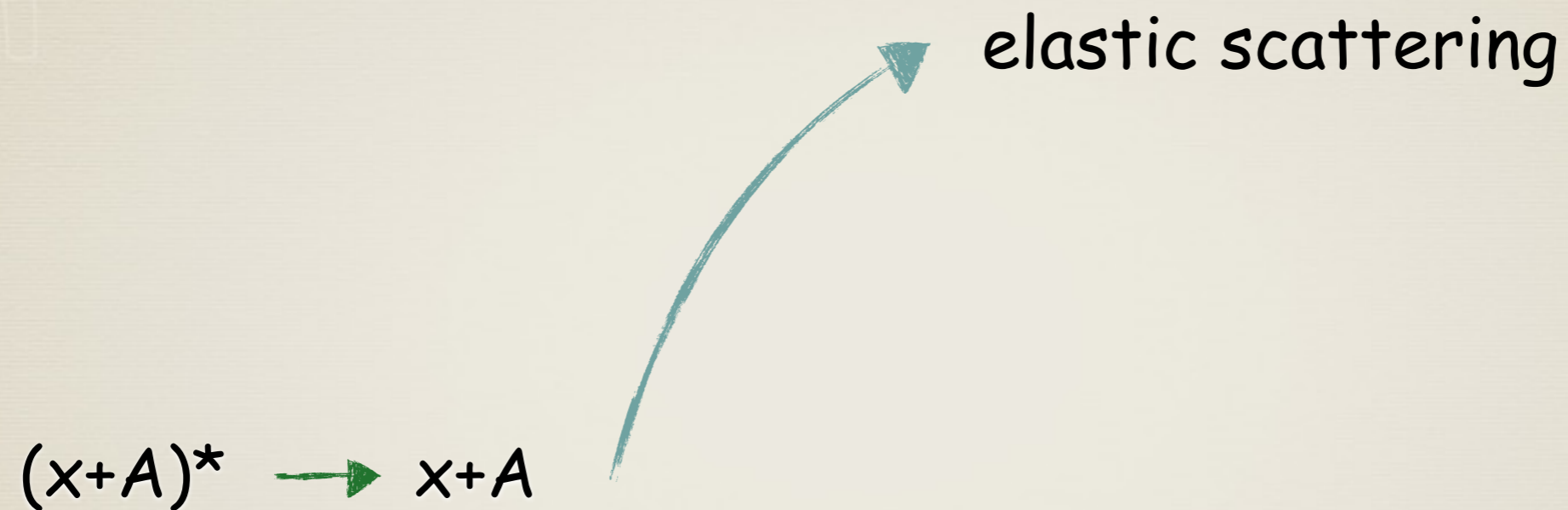
$$(x+A)^*$$

# The Ichimura, Austern, Vincent Model

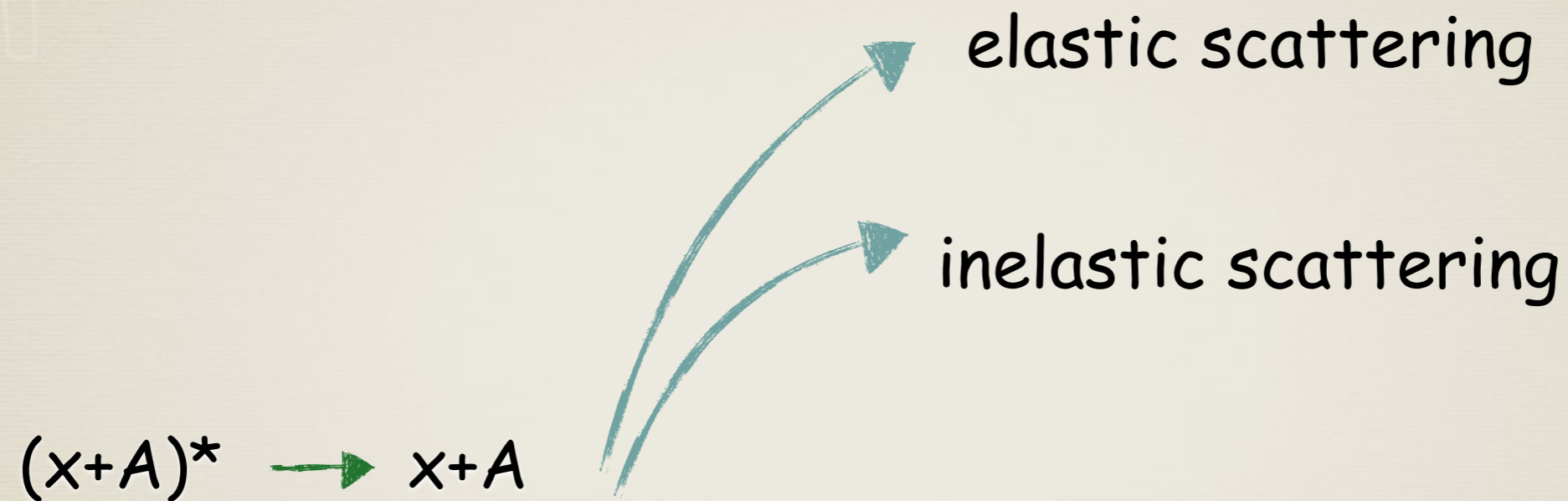
$$(x+A)^* \rightarrow x+A$$



# The Ichimura, Austern, Vincent Model

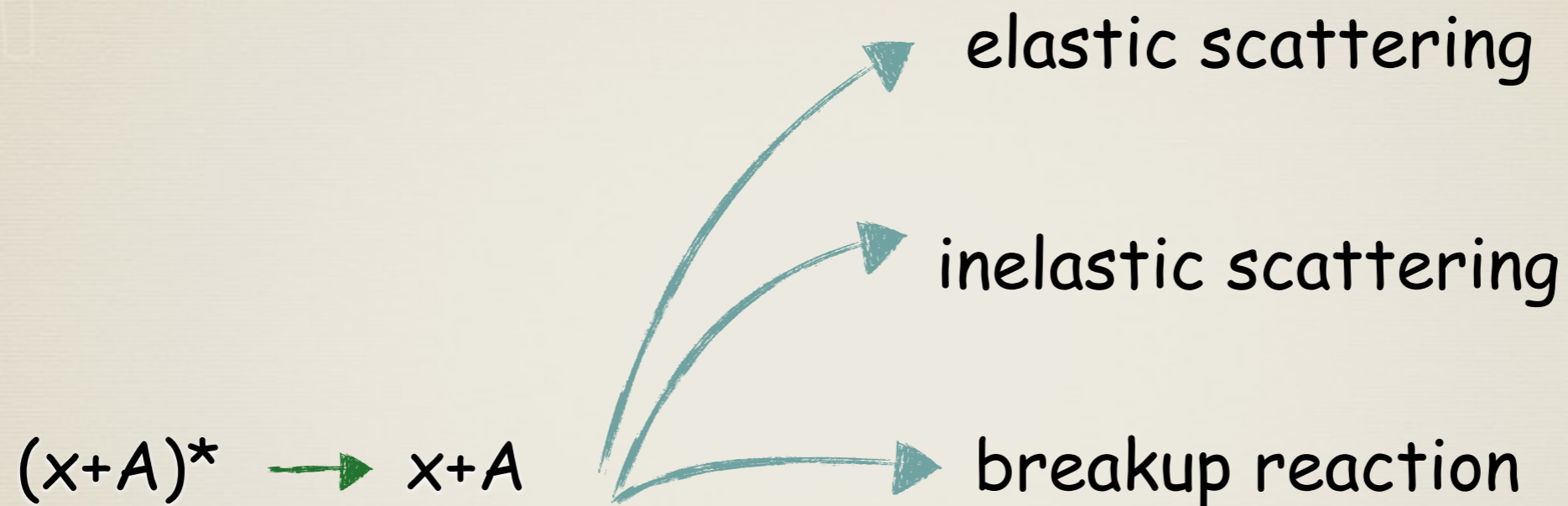


# The Ichimura, Austern, Vincent Model

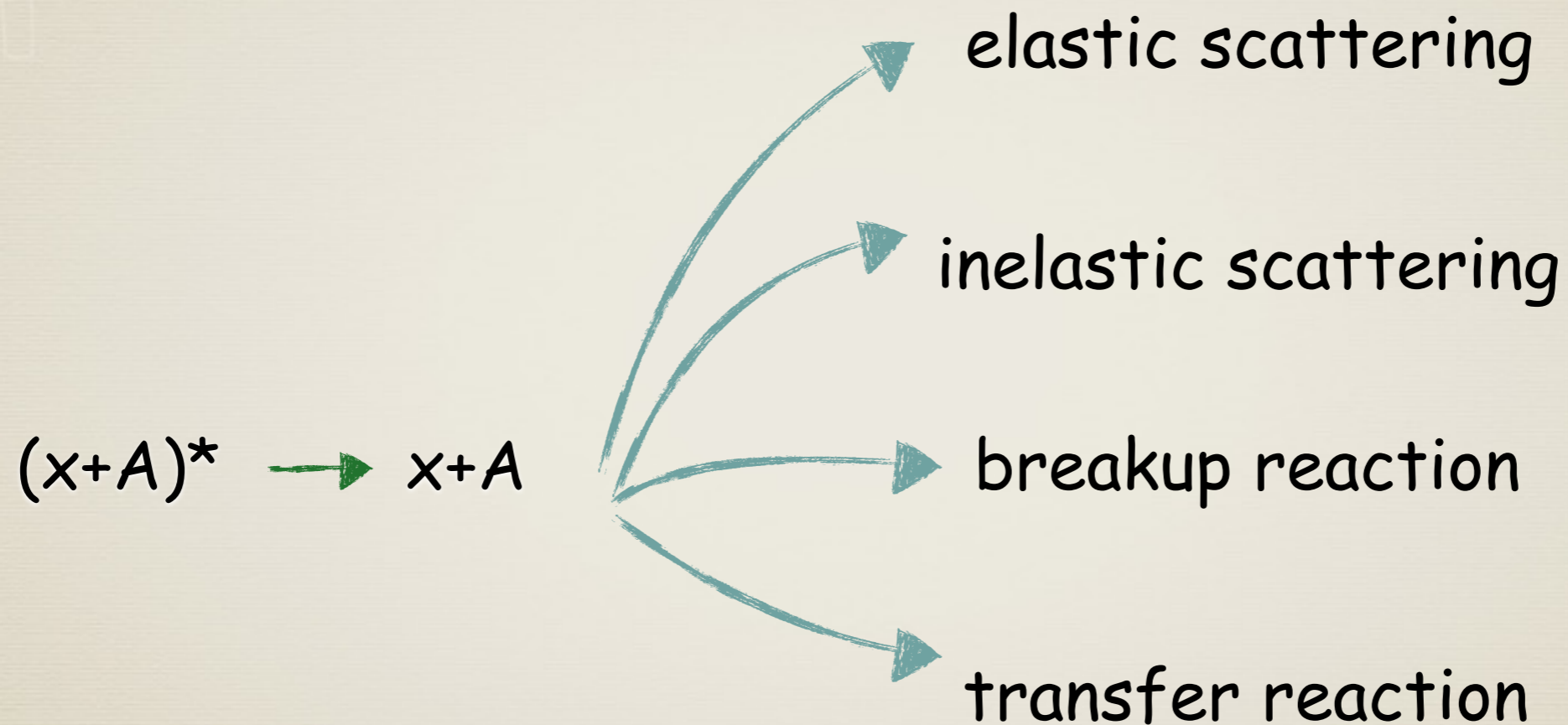




# The Ichimura, Austern, Vincent Model

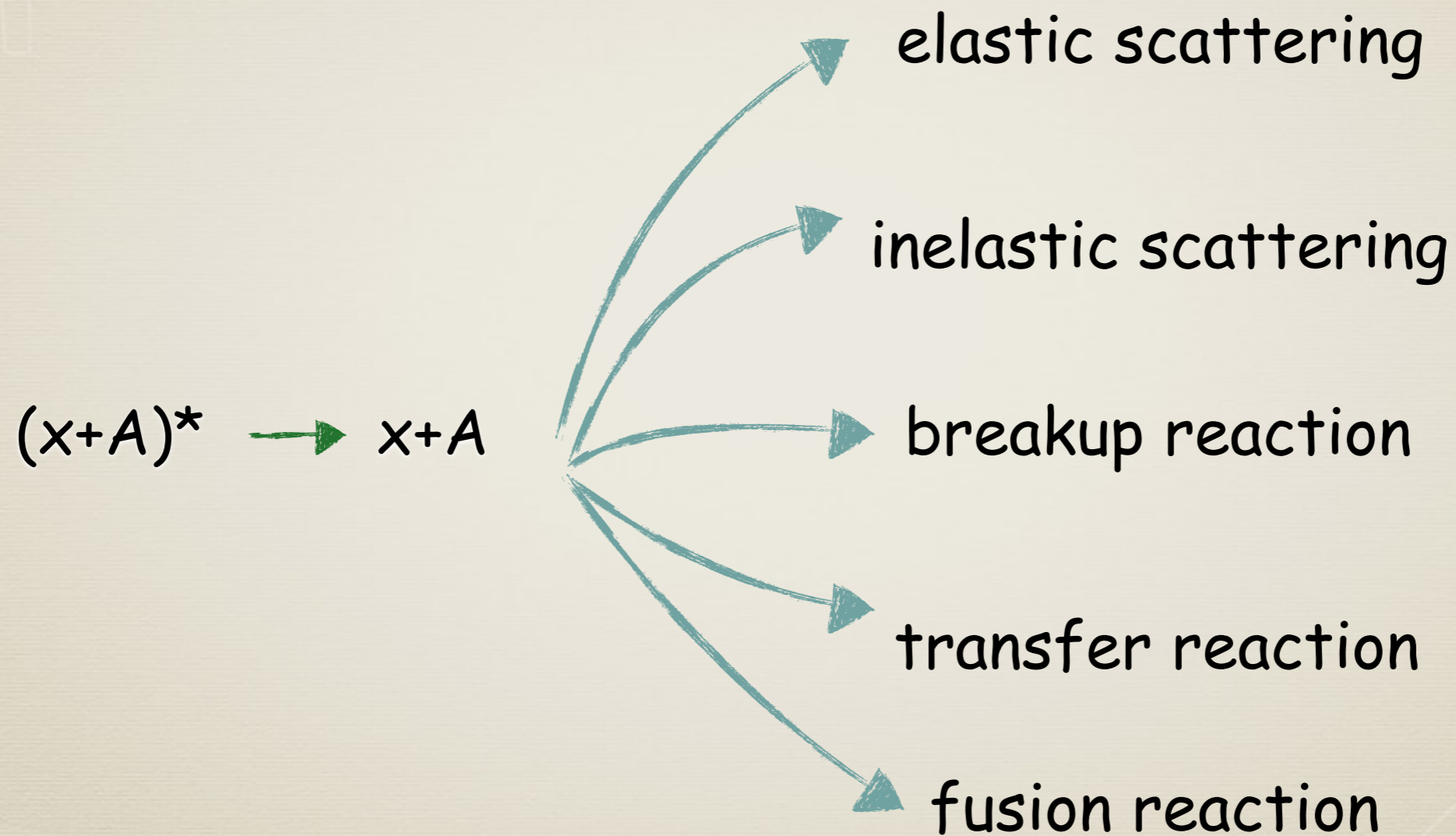


# The Ichimura, Austern, Vincent Model

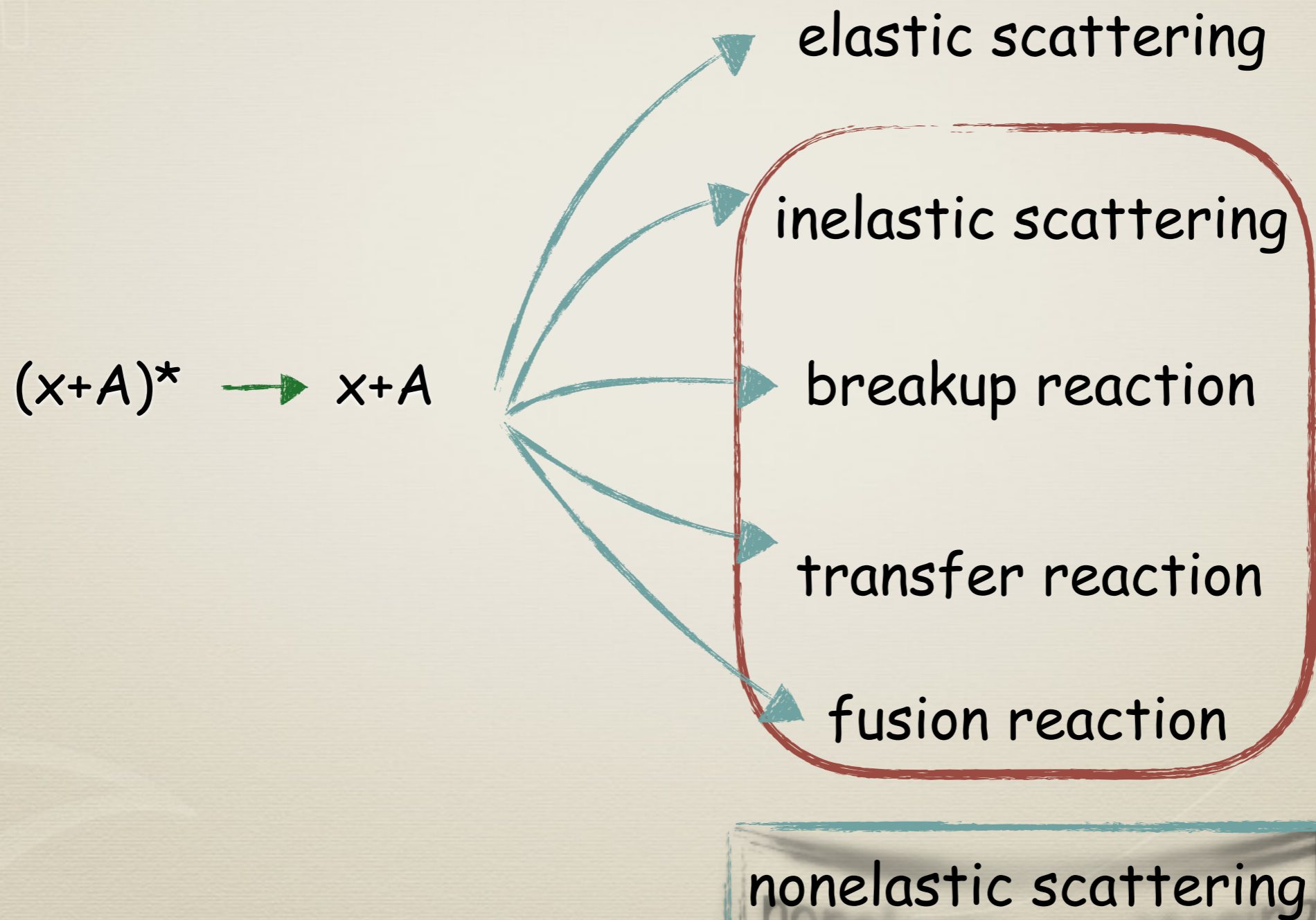




# The Ichimura, Austern, Vincent Model



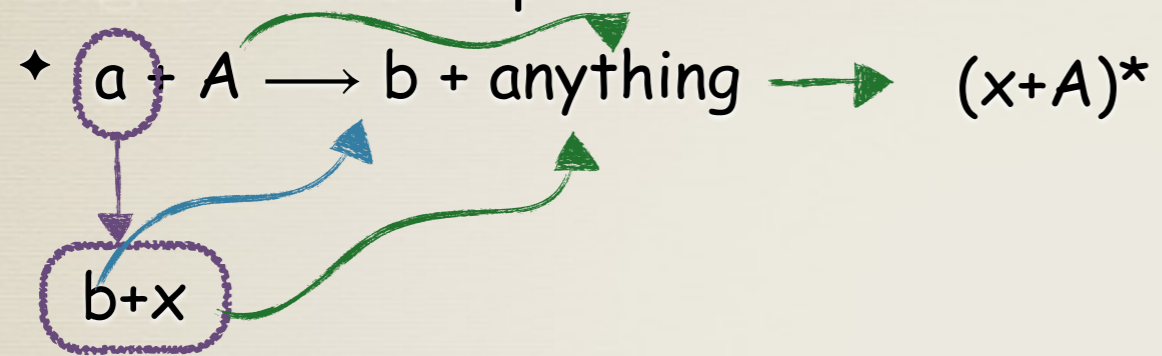
# The Ichimura, Austern, Vincent Model





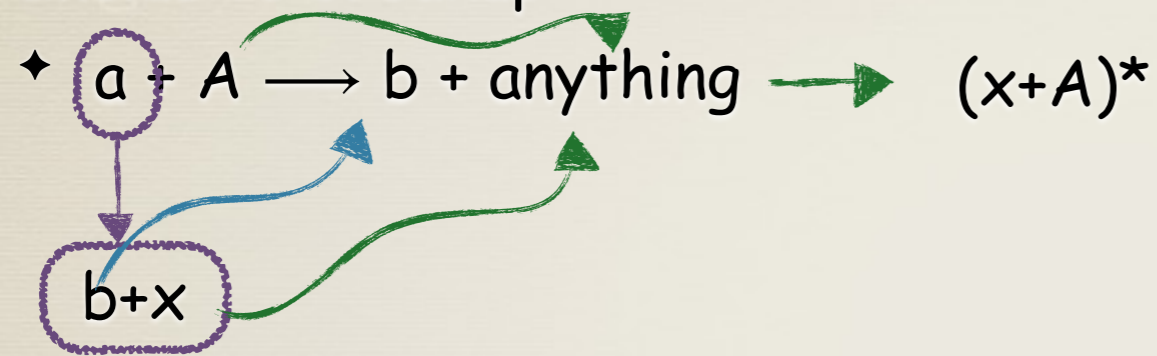
# The Ichimura, Austern, Vincent Model

✦ Inclusive breakup :



# The Ichimura, Austern, Vincent Model

✦ Inclusive breakup :

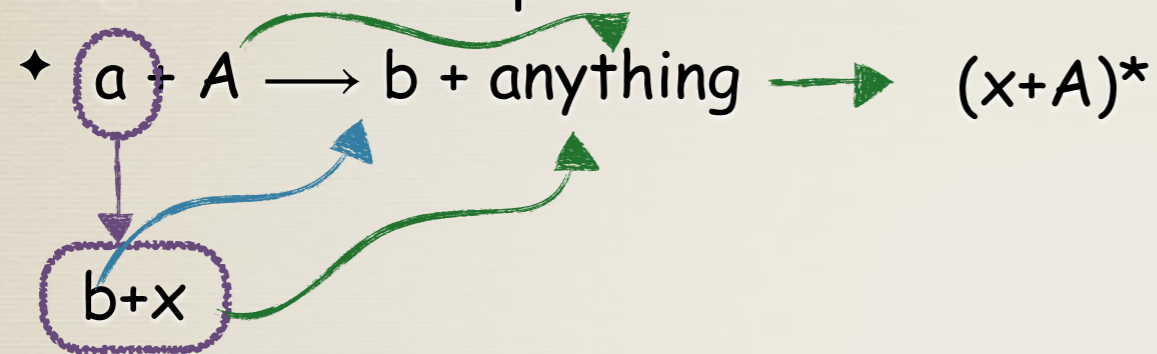


$x, A$  ground states  
Elastic Breakup



# The Ichimura, Austern, Vincent Model

✦ Inclusive breakup :

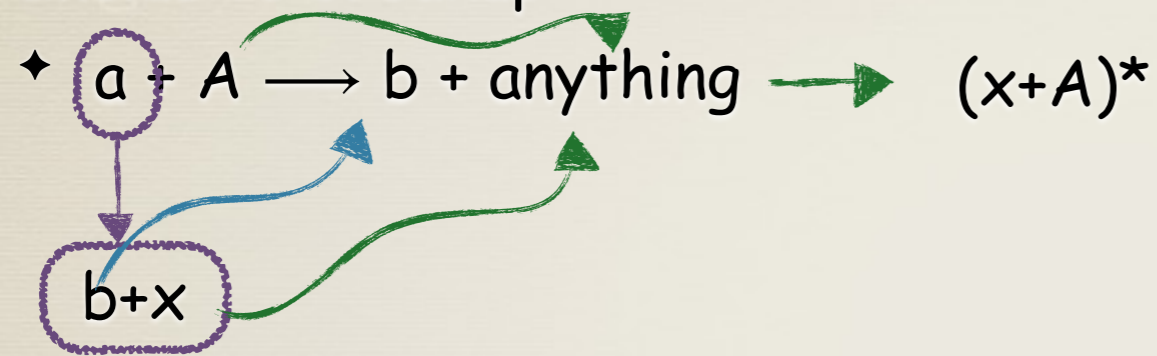


$x, A$  ground states  
Elastic Breakup

$x, A$  excited states  
Inelastic Breakup

# The Ichimura, Austern, Vincent Model

✦ Inclusive breakup :



$x, A$  ground states  
Elastic Breakup

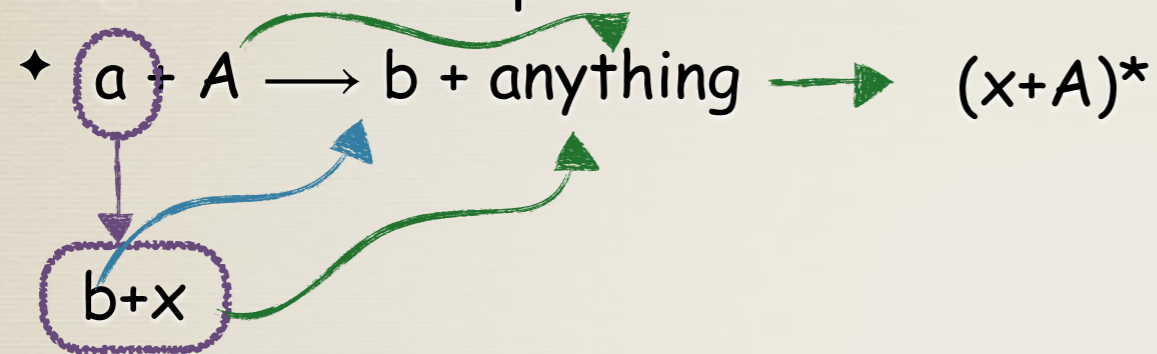
$x, A$  excited states  
Inelastic Breakup

sequential breakup



# The Ichimura, Austern, Vincent Model

✦ Inclusive breakup :



$x, A$  ground states  
Elastic Breakup

$x, A$  excited states  
Inelastic Breakup

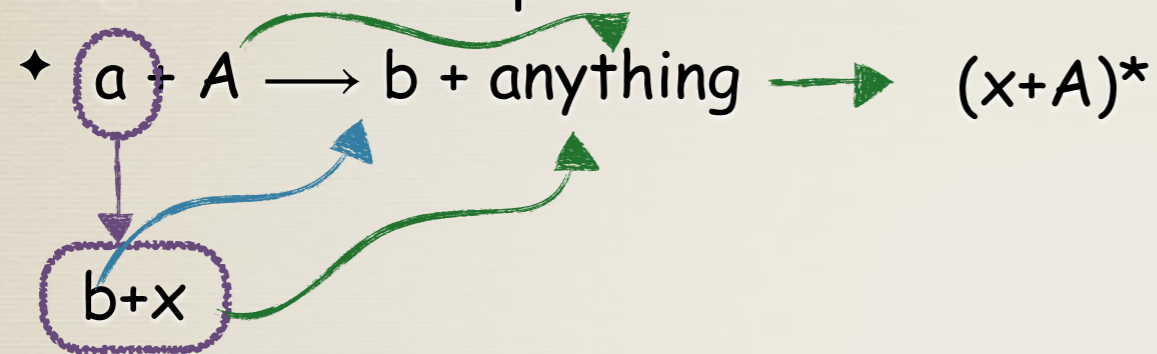
sequential breakup

particle transfer  
between  $x$  and  $A$



# The Ichimura, Austern, Vincent Model

✦ Inclusive breakup :



$x, A$  ground states  
Elastic Breakup

$x, A$  excited states  
Inelastic Breakup

sequential breakup

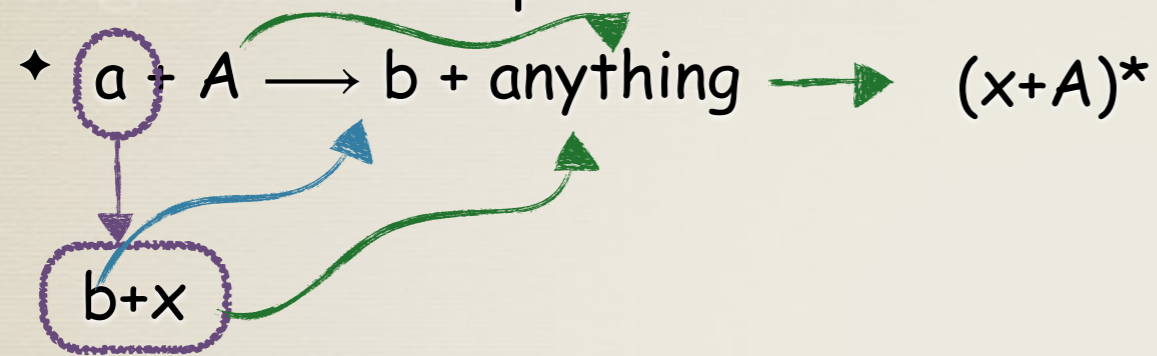
particle transfer  
between  $x$  and  $A$

$x$  absorbed by  $A$   
incomplete fusion



# The Ichimura, Austern, Vincent Model

✦ Inclusive breakup :



$x, A$  ground states  
Elastic Breakup

$x, A$  excited states  
Inelastic Breakup

sequential breakup

particle transfer  
between  $x$  and  $A$

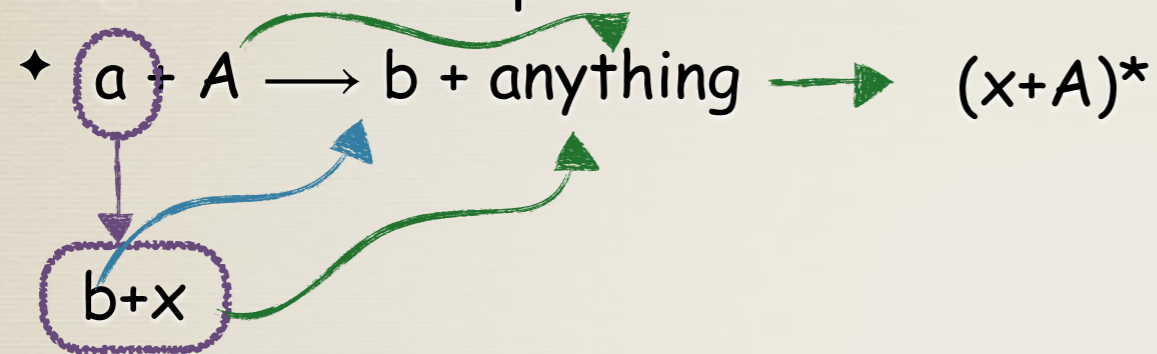
$x$  absorbed by  $A$   
incomplete fusion

Nonelastic breakup



# The Ichimura, Austern, Vincent Model

✦ Inclusive breakup :



✦ Inclusive differential cross sections :

$$\sigma_b^{TBU} = \sigma_b^{EBU} + \sigma_b^{NEB}$$

$x, A$  ground states  
Elastic Breakup

$x, A$  excited states  
Inelastic Breakup

sequential breakup

particle transfer  
between  $x$  and  $A$

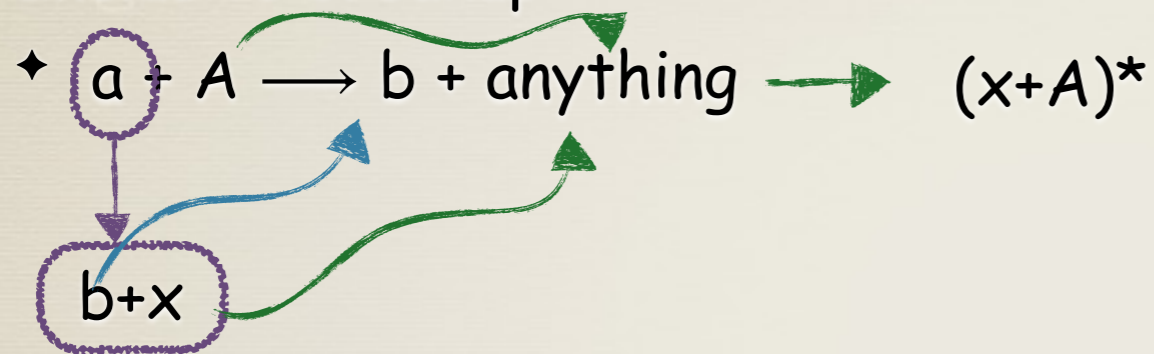
$x$  absorbed by  $A$   
incomplete fusion

Nonelastic breakup



# The Ichimura, Austern, Vincent Model

★ Inclusive breakup :



★ Inclusive differential cross sections :

$$\sigma_b^{TBU} = \sigma_b^{EBU} + \sigma_b^{NEB}$$

★ Post form expression for inclusive breakup

$$\frac{d^2\sigma}{d\Omega_b dE_b} = \frac{2\pi}{\hbar v_a} \rho(E_b) \sum_c \left| \langle \chi_b^{(-)} \Psi_{xA}^{c,(-)} | V_{bx} | \Psi^{(+)} \rangle \right|^2 \delta(E - E_b - E^c)$$

x, A ground states  
Elastic Breakup

x, A excited states  
Inelastic Breakup

sequential breakup

particle transfer  
between x and A

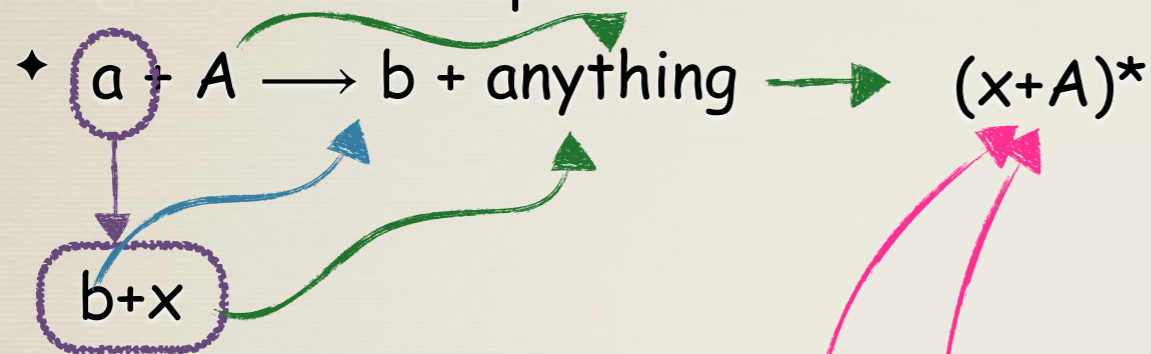
x absorbed by A  
incomplete fusion

Nonelastic breakup



# The Ichimura, Austern, Vincent Model

★ Inclusive breakup :



★ Inclusive differential cross sections :

$$\sigma_b^{TBU} = \sigma_b^{EBU} + \sigma_b^{NEB}$$

★ Post form expression for inclusive breakup

$$\frac{d^2\sigma}{d\Omega_b dE_b} = \frac{2\pi}{\hbar v_a} \rho(E_b) \sum_c \left| \langle \chi_b^{(-)} \Psi_{xA}^{c,(-)} | V_{bx} | \Psi^{(+)} \rangle \right|^2 \delta(E - E_b - E^c) \quad \text{Nonelastic breakup}$$

x, A ground states  
Elastic Breakup

x, A excited states  
Inelastic Breakup

sequential breakup

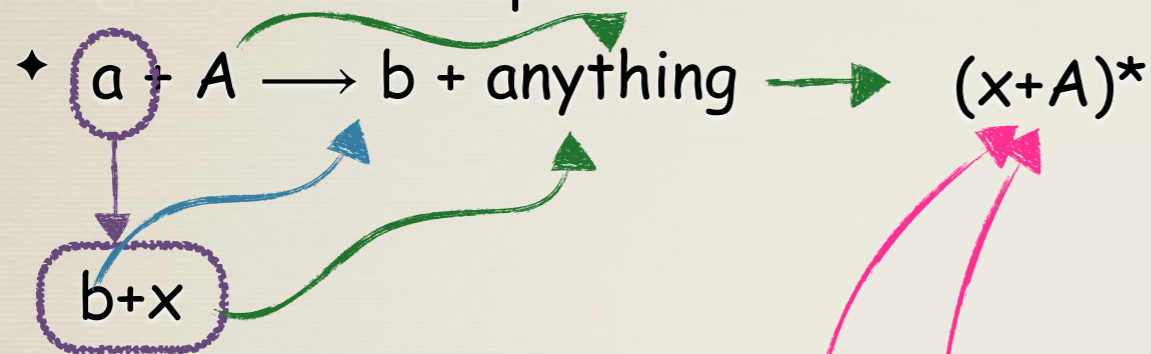
particle transfer  
between x and A

x absorbed by A  
incomplete fusion



# The Ichimura, Austern, Vincent Model

★ Inclusive breakup :



★ Inclusive differential cross sections :

$$\sigma_b^{TBU} = \sigma_b^{EBU} + \sigma_b^{NEB}$$

★ Post form expression for inclusive breakup

$$\frac{d^2\sigma}{d\Omega_b dE_b} = \frac{2\pi}{\hbar v_a} \rho(E_b) \sum_c \left| \langle \chi_b^{(-)} \Psi_{xA}^{c,(-)} | V_{bx} | \Psi^{(+)} \rangle \right|^2 \delta(E - E_b - E^c)$$

Nonelastic breakup

exact many body wave function

x, A ground states  
Elastic Breakup

x, A excited states  
Inelastic Breakup

sequential breakup

particle transfer  
between x and A

x absorbed by A  
incomplete fusion

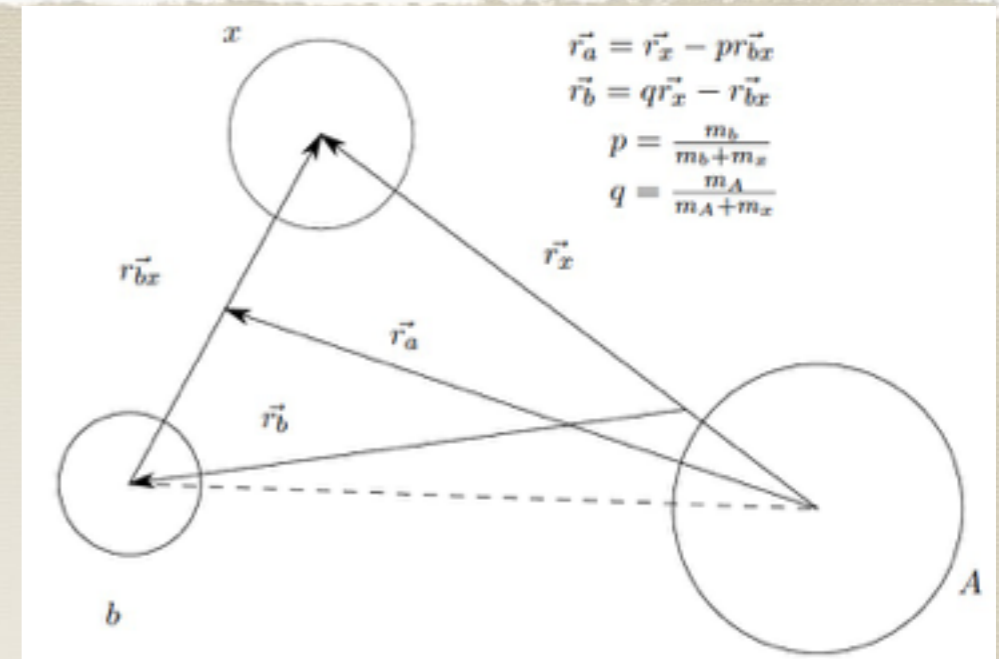


# IAV Model



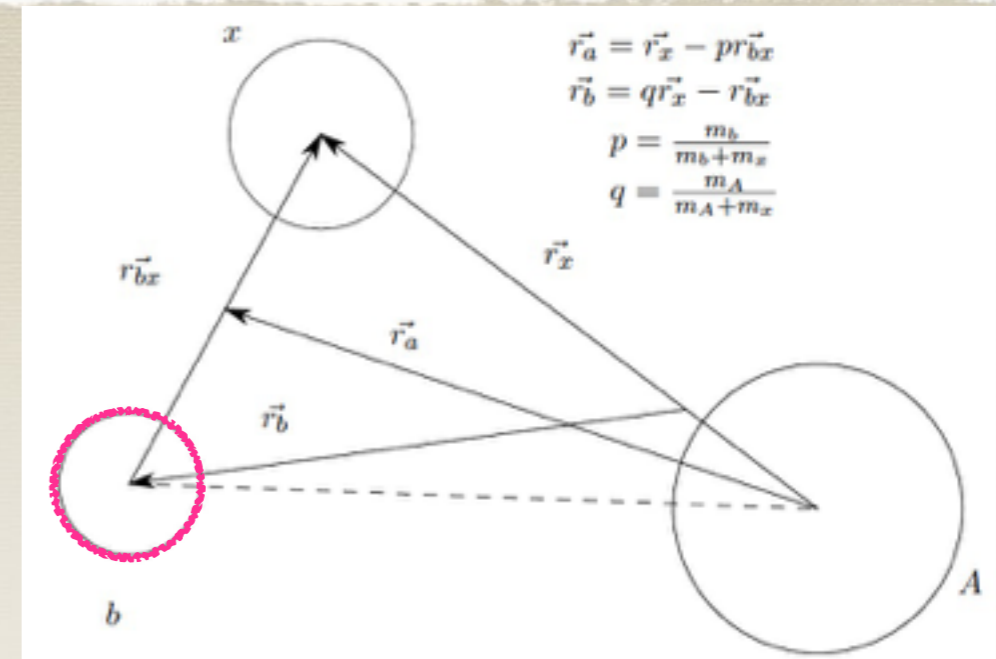
# IAV Model

- ✿ spectator/participant model:



# IAV Model

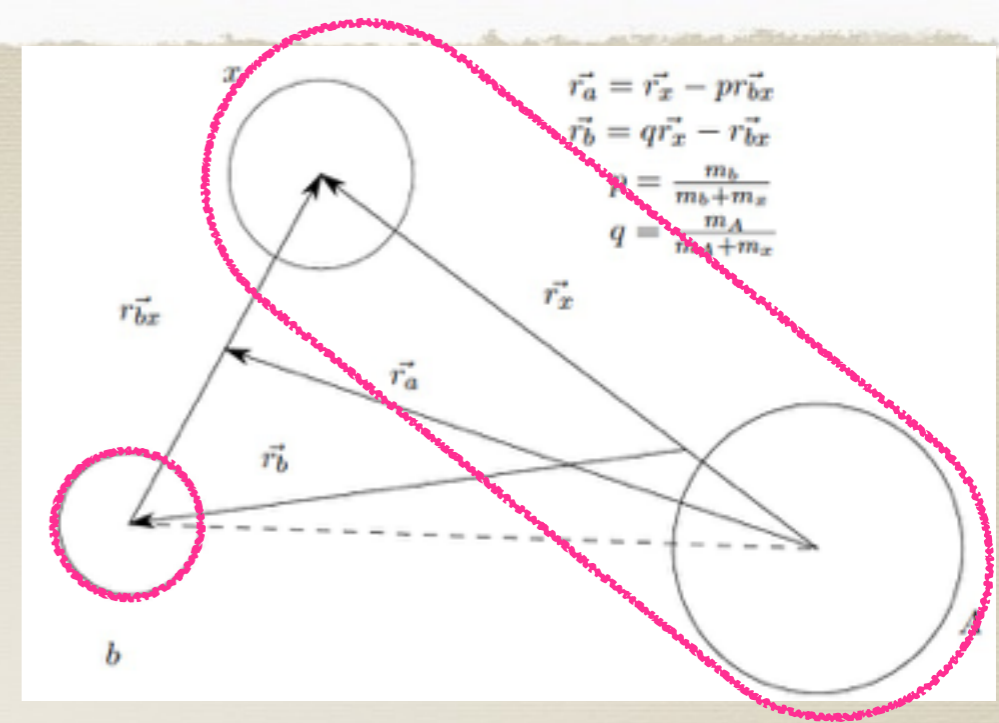
- spectator/participant model:
  - **b**: spectator;



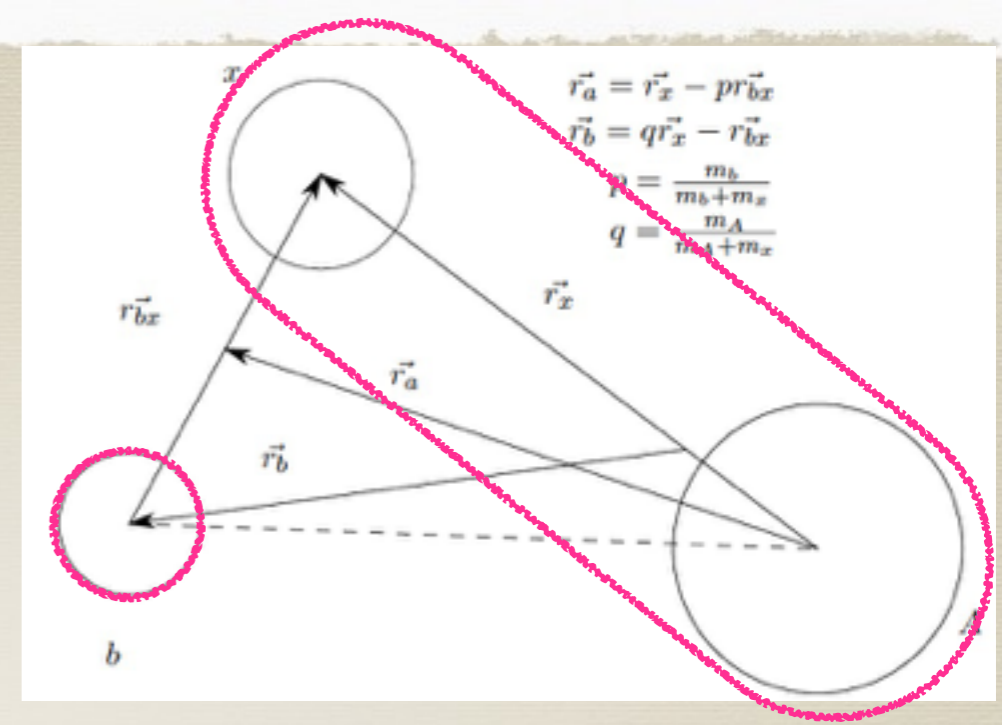


# IAV Model

- ✿ spectator/participant model:
  - ✿ **b**: spectator;
  - ✿ **x**: participant (not observed);



# IAV Model



- spectator/participant model:

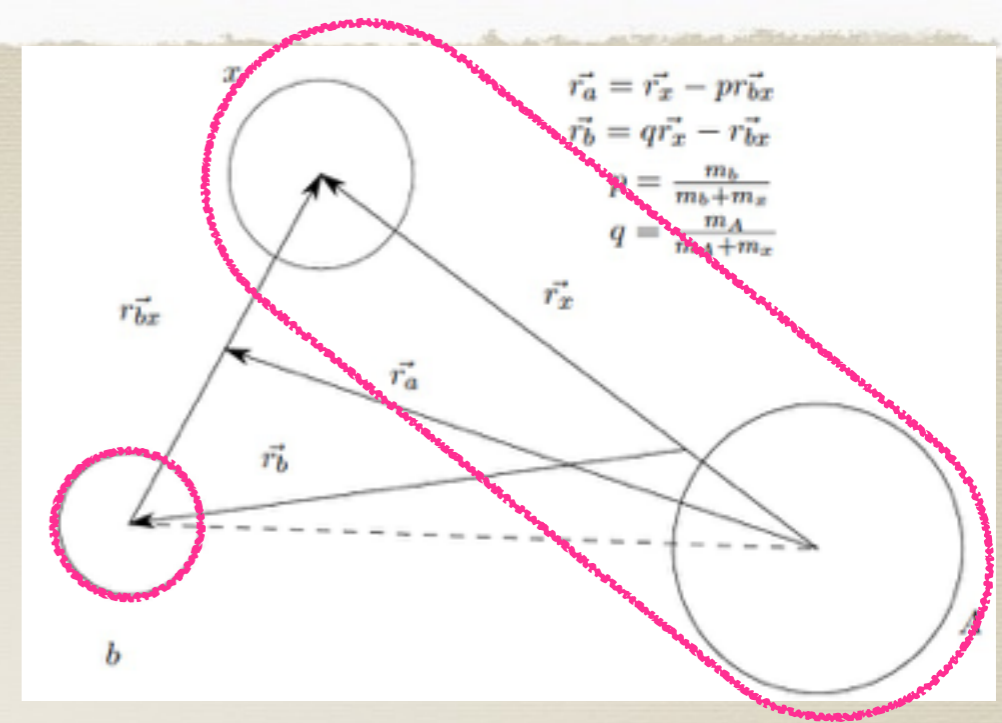
- **b**: spectator;

- **x**: participant (not observed);

- **x-A** wave function following breakup and projected on the  $A_{gs}$   $V_{xA} \rightarrow U_{xA}$



# IAV Model

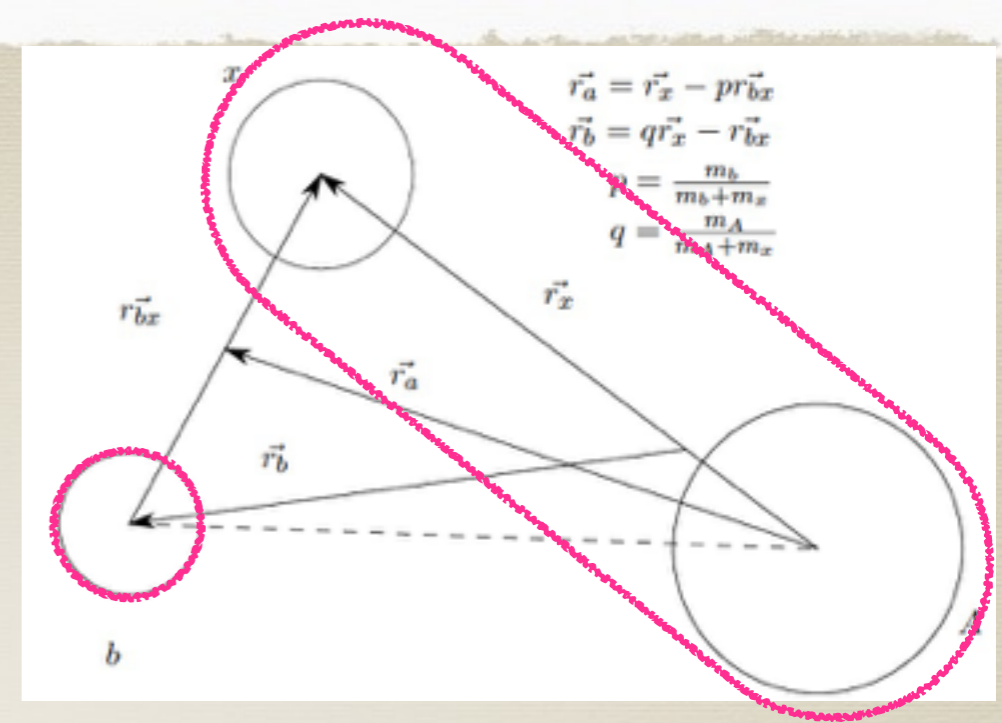


- ✦ spectator/participant model:
  - ✦ **b**: spectator;
  - ✦ **x**: participant (not observed);

✦ **x-A** wave function following breakup and projected on the  $A_{gs}$   $V_{xA} \rightarrow U_{xA}$

$$(E_x - K_x - U_x)\varphi_x^0(\vec{r}_x, \vec{k}_b) = (\chi_b^{(-)}(\vec{r}_b, \vec{k}_b) | V_{post} | \Psi^{3b} \rangle$$

# IAV Model



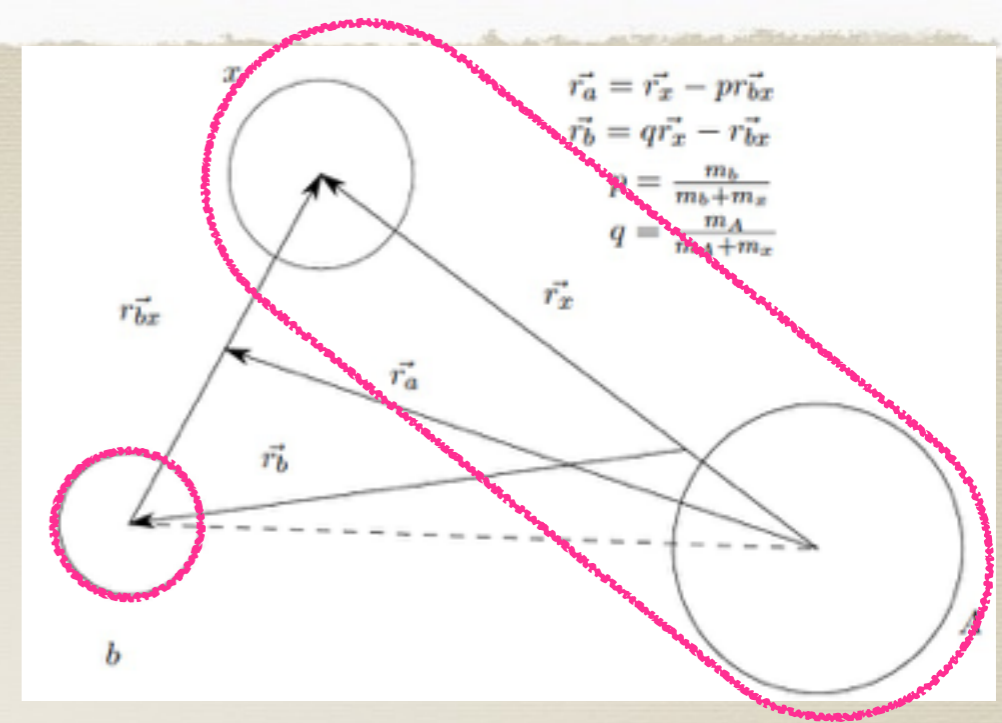
- ✦ spectator/participant model:
- ✦ **b**: spectator;
- ✦ **x**: participant (not observed);

✦ **x-A** wave function following breakup and projected on the  $A_{gs}$   $V_{xA} \rightarrow U_{xA}$

$$(E_x - K_x - U_x) \varphi_x^0(\vec{r}_x, \vec{k}_b) = (\chi_b^{(-)}(\vec{r}_b, \vec{k}_b) | V_{post} | \Psi^{3b} \rangle$$



# IAV Model

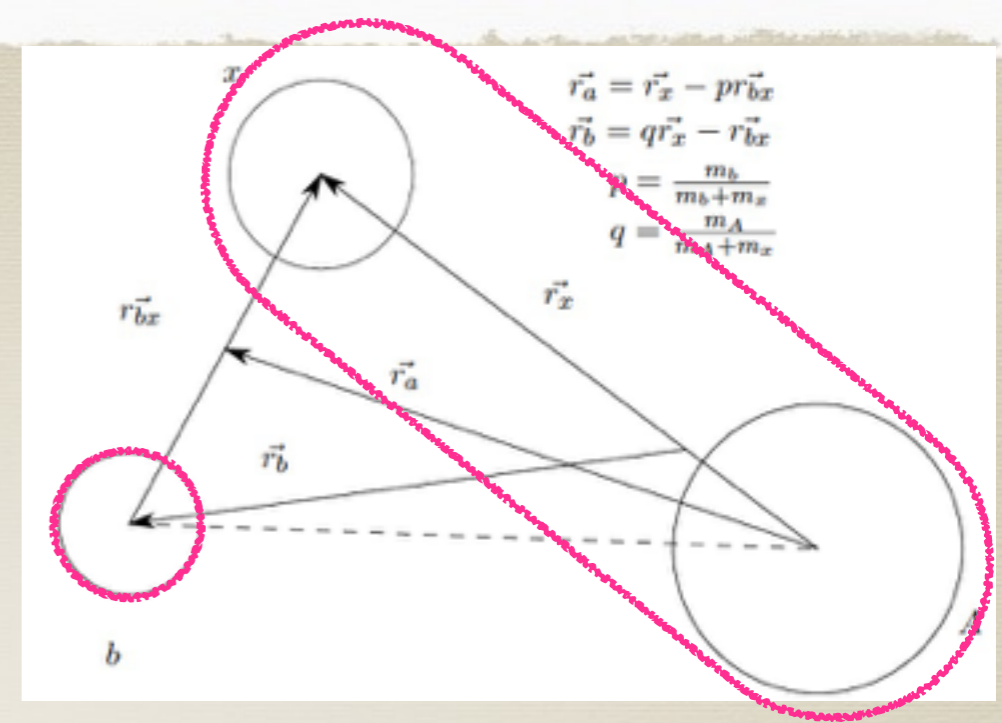


- spectator/participant model:
  - **b**: spectator;
  - **x**: participant (not observed);

• **x-A** wave function following breakup and projected on the  $A_{gs}$   $V_{xA} \rightarrow U_{xA}$

$$(E_x - K_x - U_x) \varphi_x^0(\vec{r}_x, \vec{k}_b) = (\chi_b^{(-)}(\vec{r}_b, \vec{k}_b) | V_{post} | \Psi^{3b} \rangle$$

# IAV Model



- spectator/participant model:
  - **b**: spectator;
  - **x**: participant (not observed);

• **x-A** wave function following breakup and projected on the  $A_{gs}$   $V_{xA} \rightarrow U_{xA}$

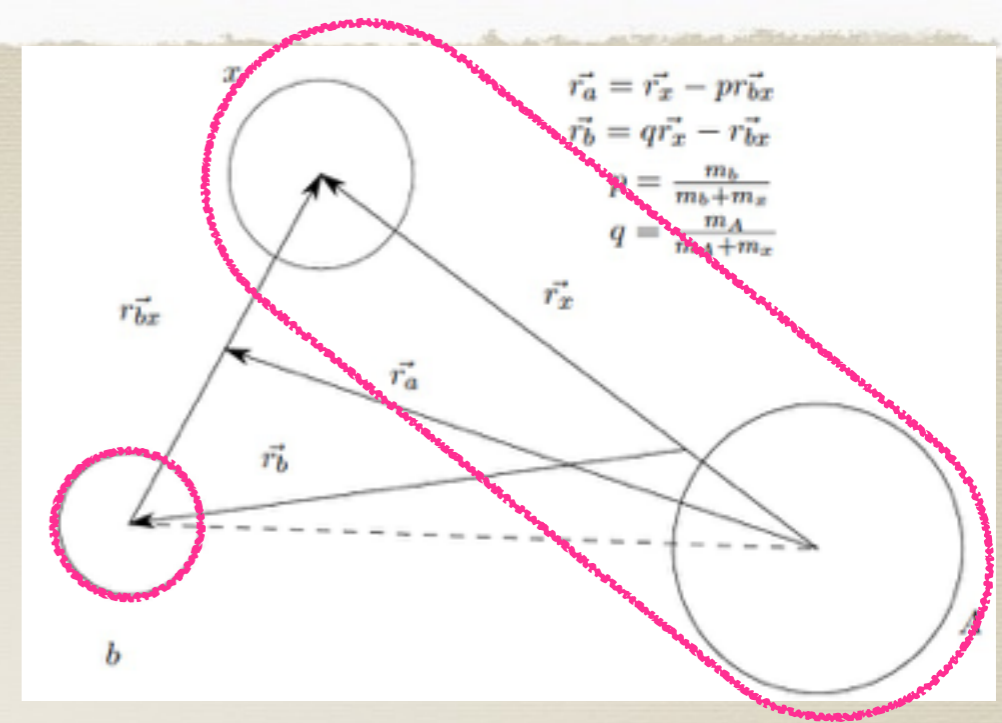
$$(E_x - K_x - U_x) \varphi_x^0(\vec{r}_x, \vec{k}_b) = (\chi_b^{(-)}(\vec{r}_b, \vec{k}_b) | V_{post} | \Psi^{3b} \rangle$$

DWBA

$$\Psi^{3b} \simeq \chi_a \varphi_a \Phi_A$$



# IAV Model



- spectator/participant model:
  - **b**: spectator;
  - **x**: participant (not observed);

• **x-A** wave function following breakup and projected on the  $A_{gs}$   $V_{xA} \rightarrow U_{xA}$

$$(E_x - K_x - U_x) \varphi_x^0(\vec{r}_x, \vec{k}_b) = (\chi_b^{(-)}(\vec{r}_b, \vec{k}_b) | V_{post} | \Psi^{3b} \rangle$$

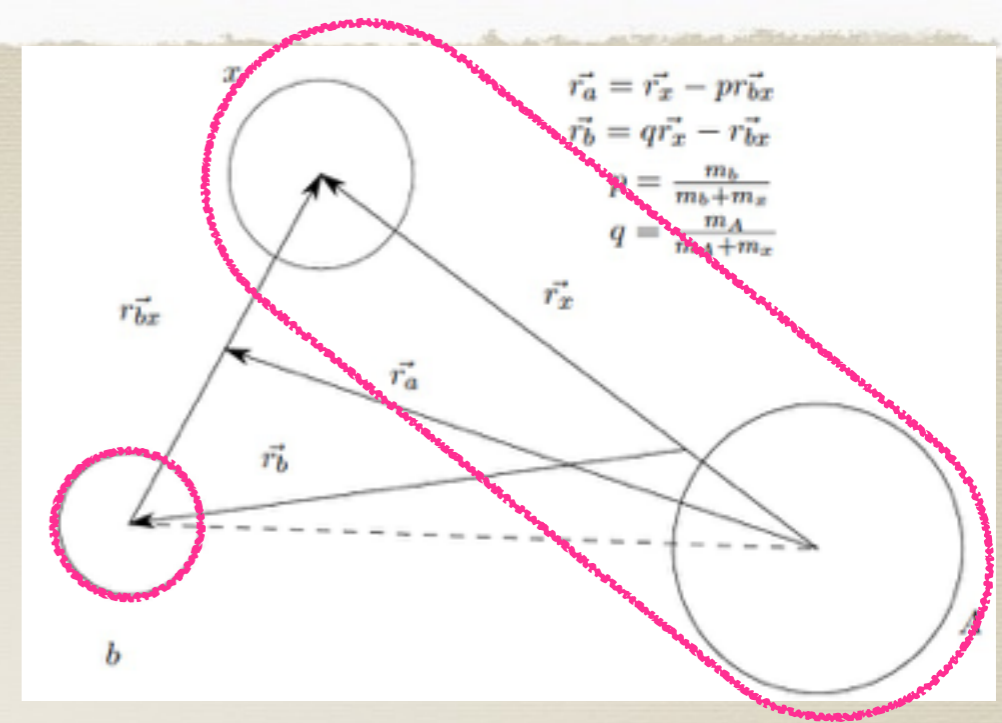
DWBA

$$\Psi^{3b} \simeq \chi_a \varphi_a \Phi_A$$

- Nonelastic breakup (NEB): loss of flux leaving the **x-A<sub>gs</sub>** channel



# IAV Model



- spectator/participant model:
  - **b**: spectator;
  - **x**: participant (not observed);

• **x-A** wave function following breakup and projected on the  $A_{gs}$   $V_{xA} \rightarrow U_{xA}$

$$(E_x - K_x - U_x) \varphi_x^0(\vec{r}_x, \vec{k}_b) = (\chi_b^{(-)}(\vec{r}_b, \vec{k}_b) | V_{post} | \Psi^{3b})$$

DWBA

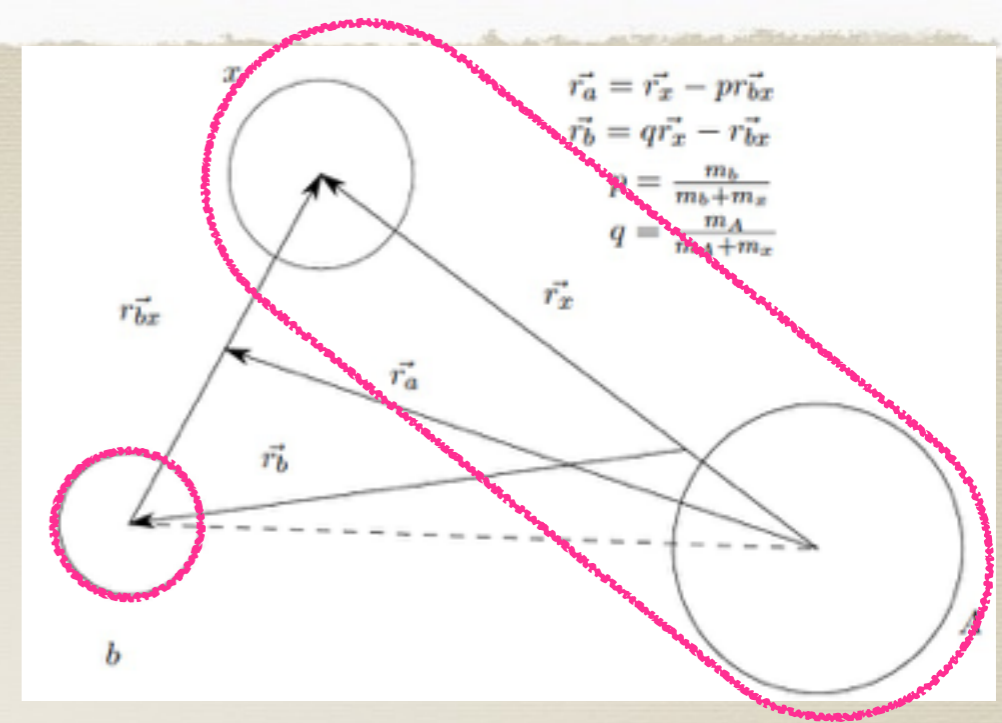
$$\Psi^{3b} \simeq \chi_a \varphi_a \Phi_A$$

- Nonelastic breakup (NEB): loss of flux leaving the **x-A<sub>gs</sub>** channel

$$\frac{d^2\sigma}{dE_b d\Omega_b} = -\frac{2}{\hbar v_a} \rho_b(E_b) \langle \varphi_x^0(\vec{r}_x, \vec{k}_b) | W_x | \varphi_x^0(\vec{r}_x, \vec{k}_b) \rangle$$



# IAV Model



- spectator/participant model:
  - **b**: spectator;
  - **x**: participant (not observed);

• **x-A** wave function following breakup and projected on the  $A_{gs}$   $V_{xA} \rightarrow U_{xA}$

$$(E_x - K_x - U_x) \varphi_x^0(\vec{r}_x, \vec{k}_b) = (\chi_b^{(-)}(\vec{r}_b, \vec{k}_b) | V_{post} | \Psi^{3b})$$

DWBA

$$\Psi^{3b} \simeq \chi_a \varphi_a \Phi_A$$

- Nonelastic breakup (NEB): loss of flux leaving the **x-A<sub>gs</sub>** channel

$$\frac{d^2\sigma}{dE_b d\Omega_b} = -\frac{2}{\hbar v_a} \rho_b(E_b) \langle \varphi_x^0(\vec{r}_x, \vec{k}_b) | \mathcal{W}_x | \varphi_x^0(\vec{r}_x, \vec{k}_b) \rangle$$

imaginary part of  $U_x$

# Analogy with two-body reaction

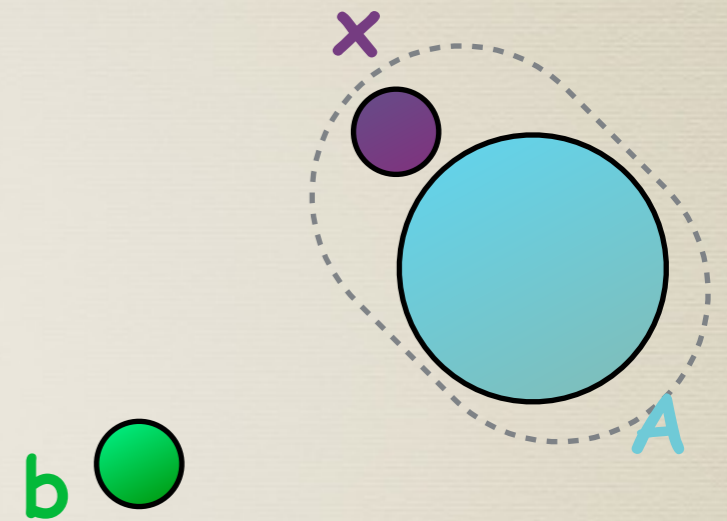
$$\frac{d^2\sigma}{dE_b d\Omega_b} = -\frac{2}{\hbar v_a} \rho_b(E_b) \langle \varphi_x^0(\vec{r}_x, \vec{k}_b) | W_x | \varphi_x^0(\vec{r}_x, \vec{k}_b) \rangle$$



# Analogy with two-body reaction

Absorption cross section in three body reaction  $b + (x + A)$

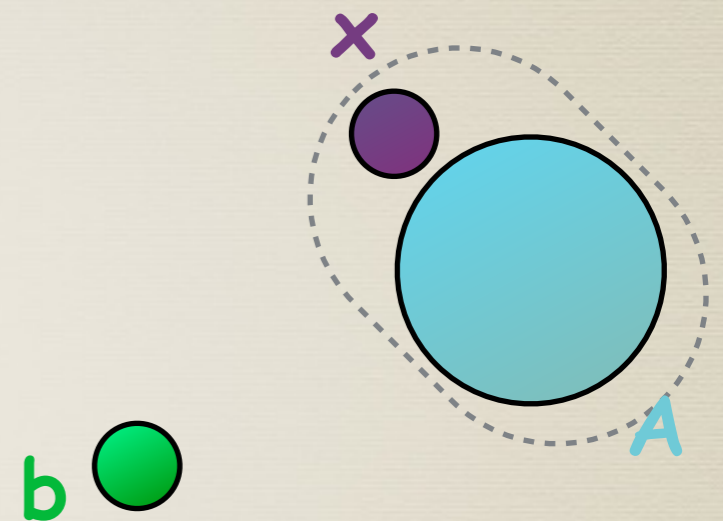
$$\frac{d^2\sigma}{dE_b d\Omega_b} = -\frac{2}{\hbar v_a} \rho_b(E_b) \langle \varphi_x^0(\vec{r}_x, \vec{k}_b) | W_x | \varphi_x^0(\vec{r}_x, \vec{k}_b) \rangle$$



# Analogy with two-body reaction

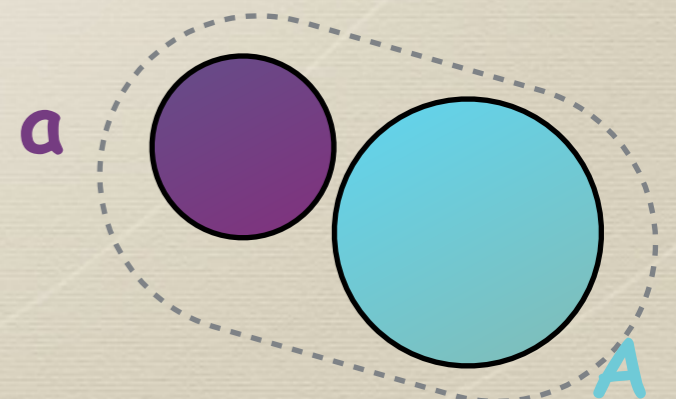
Absorption cross section in three body reaction  $b + (x + A)$

$$\frac{d^2\sigma}{dE_b d\Omega_b} = -\frac{2}{\hbar v_a} \rho_b(E_b) \langle \varphi_x^0(\vec{r}_x, \vec{k}_b) | W_x | \varphi_x^0(\vec{r}_x, \vec{k}_b) \rangle$$



Absorption cross section in binary reaction  $a+A$  (Optical Theorem)

$$\sigma_{\text{abs}} = -\frac{2}{\hbar v_a} \langle \chi_a | W_a | \chi_a \rangle$$

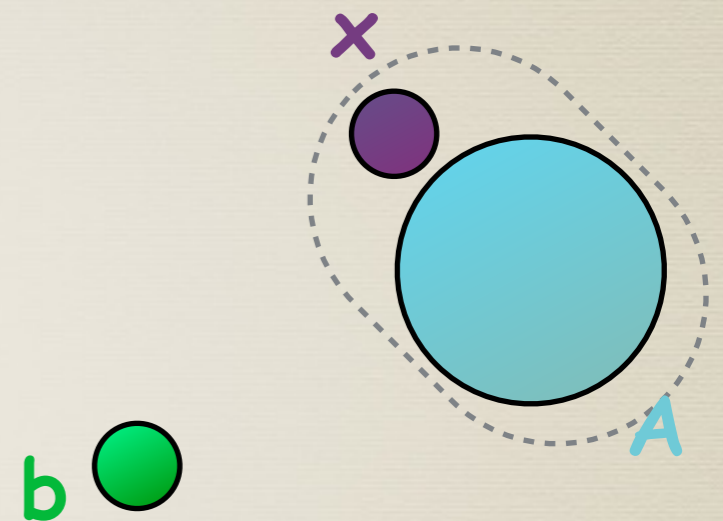




# Analogy with two-body reaction

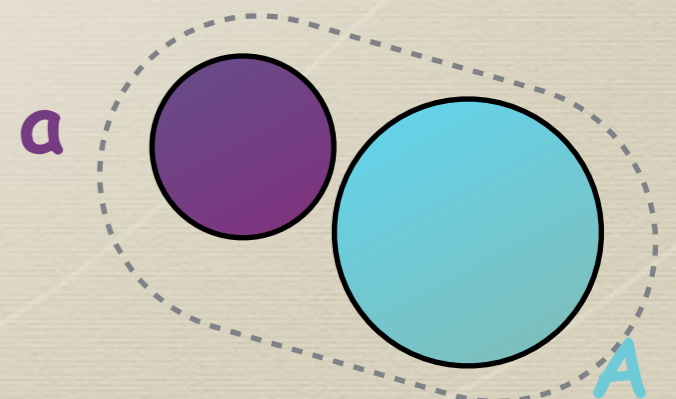
Absorption cross section in three body reaction  $b + (x + A)$

$$\frac{d^2\sigma}{dE_b d\Omega_b} = -\frac{2}{\hbar v_a} \rho_b(E_b) \langle \varphi_x^0(\vec{r}_x, \vec{k}_b) | W_x | \varphi_x^0(\vec{r}_x, \vec{k}_b) \rangle$$



Absorption cross section in binary reaction  $a+A$  (Optical Theorem)

$$\sigma_{\text{abs}} = -\frac{2}{\hbar v_a} \langle \chi_a | W_a | \chi_a \rangle$$



# Applications



# Deuteron Breakup

# Deuteron Breakup

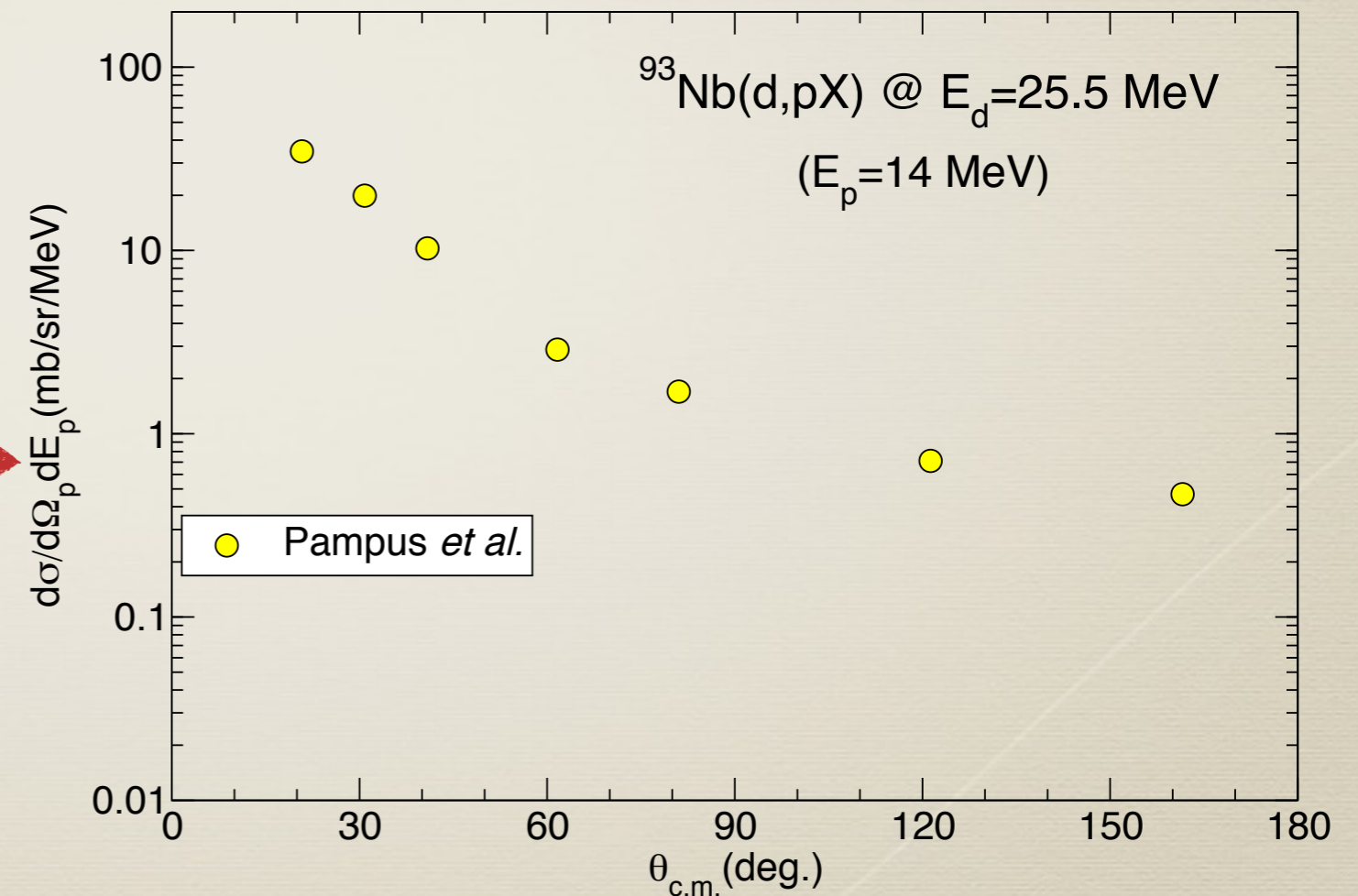
✦  $d \Rightarrow (n + p), S_p = 2.224 \text{ MeV}$



# Deuteron Breakup

- ✦  $d \Rightarrow (n + p)$ ,  $S_p = 2.224 \text{ MeV}$
- ✦ only **proton** is detected

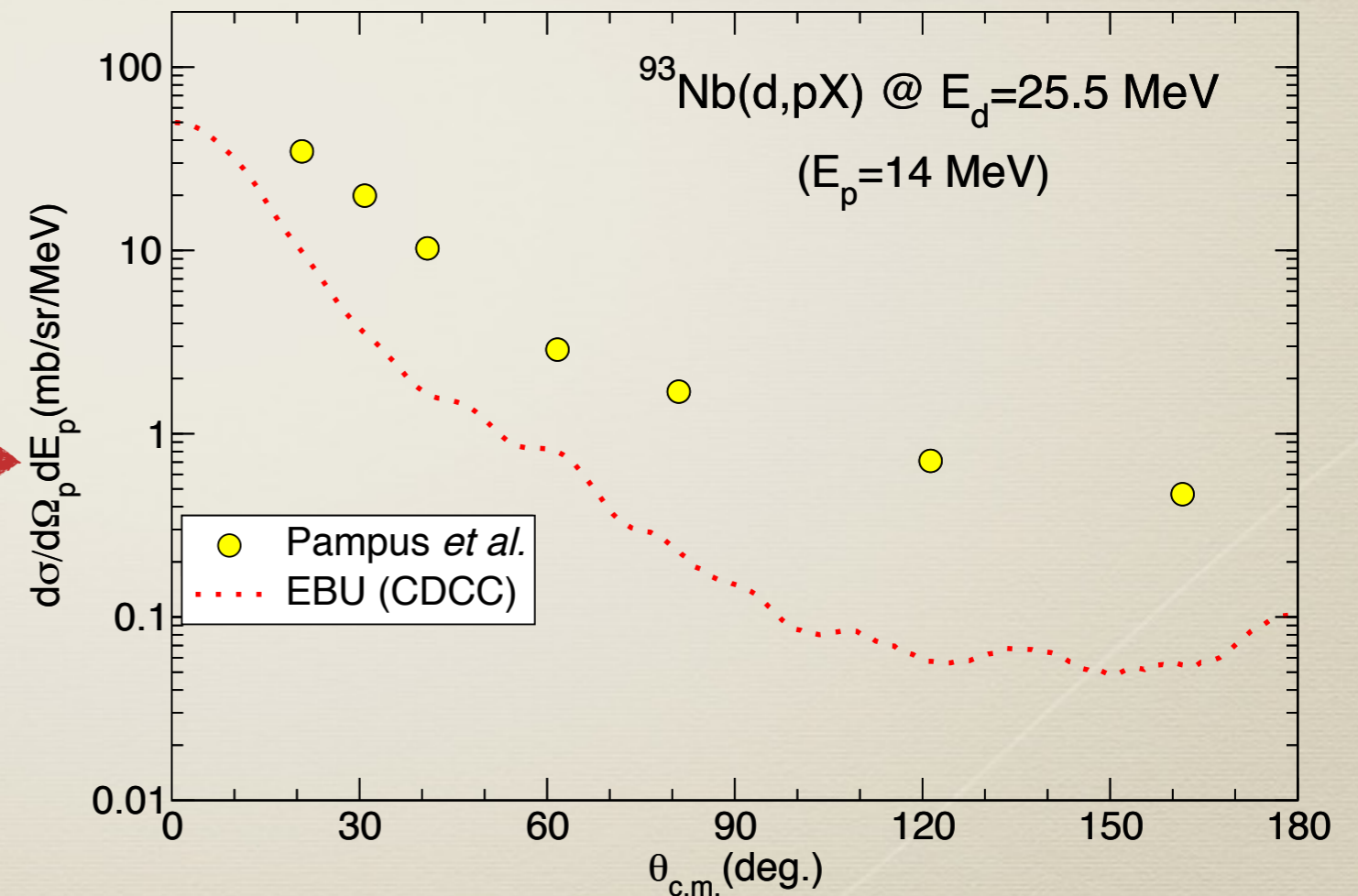
*J. Pampus et al, Nucl. Phys. A311, 141 (1978).*



# Deuteron Breakup

- ✦  $d \Rightarrow (n + p)$ ,  $S_p = 2.224 \text{ MeV}$
- ✦ only **proton** is detected
- ✦ EBU : CDCC (FRESCO)

*J. Pampus et al, Nucl. Phys. A311, 141 (1978).*

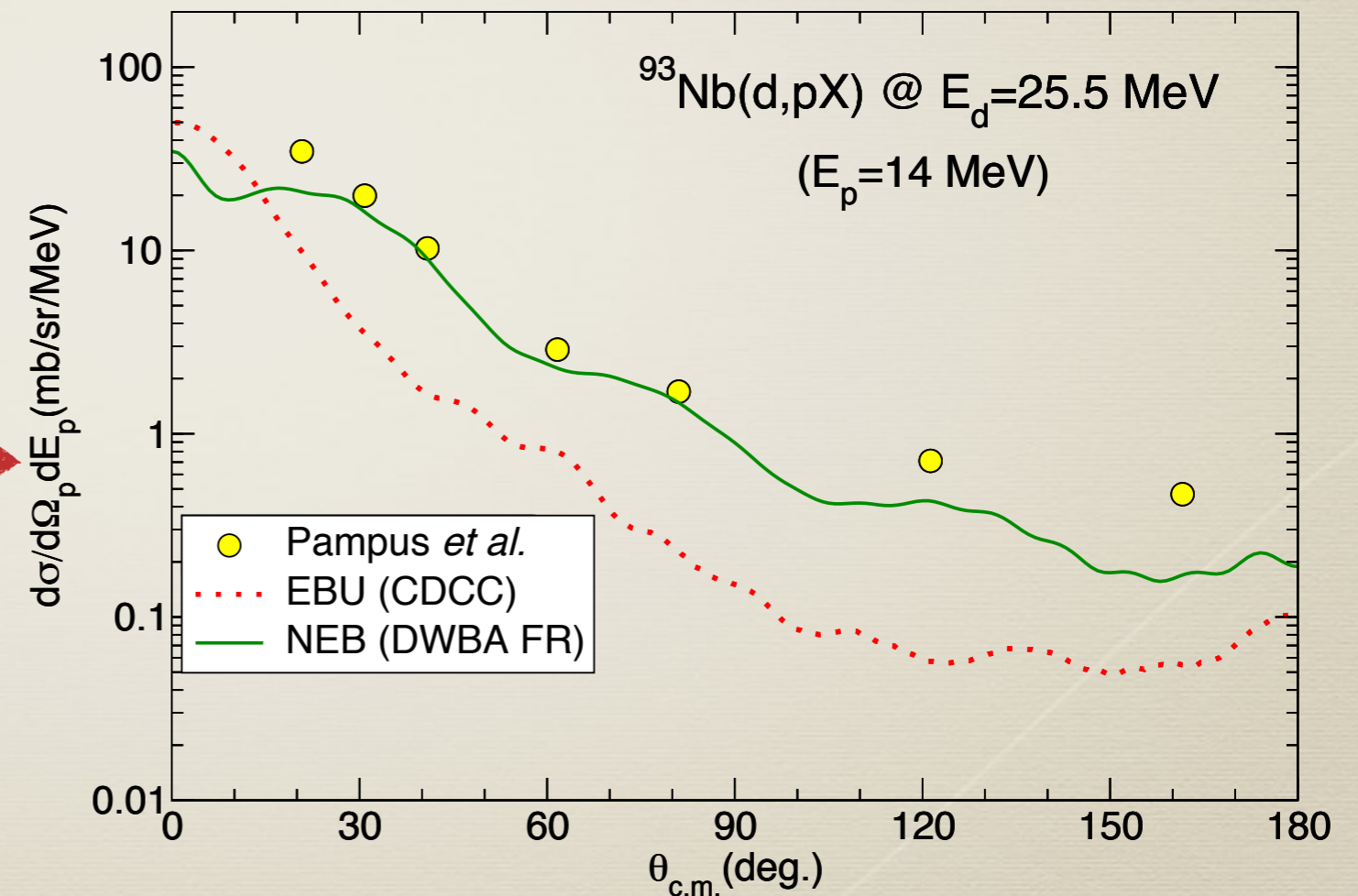




# Deuteron Breakup

- ✦  $d \Rightarrow (n + p)$ ,  $S_p = 2.224$  MeV
- ✦ only **proton** is detected
- ✦ EBU : CDCC (FRESCO)
- ✦ NEB : IAV model
- ✦ DWBA  $\Psi^{3b} \approx \chi_a \varphi_a \Phi_A$
- ✦ Exact Finite Range

*J. Pampus et al, Nucl. Phys. A311, 141 (1978).*

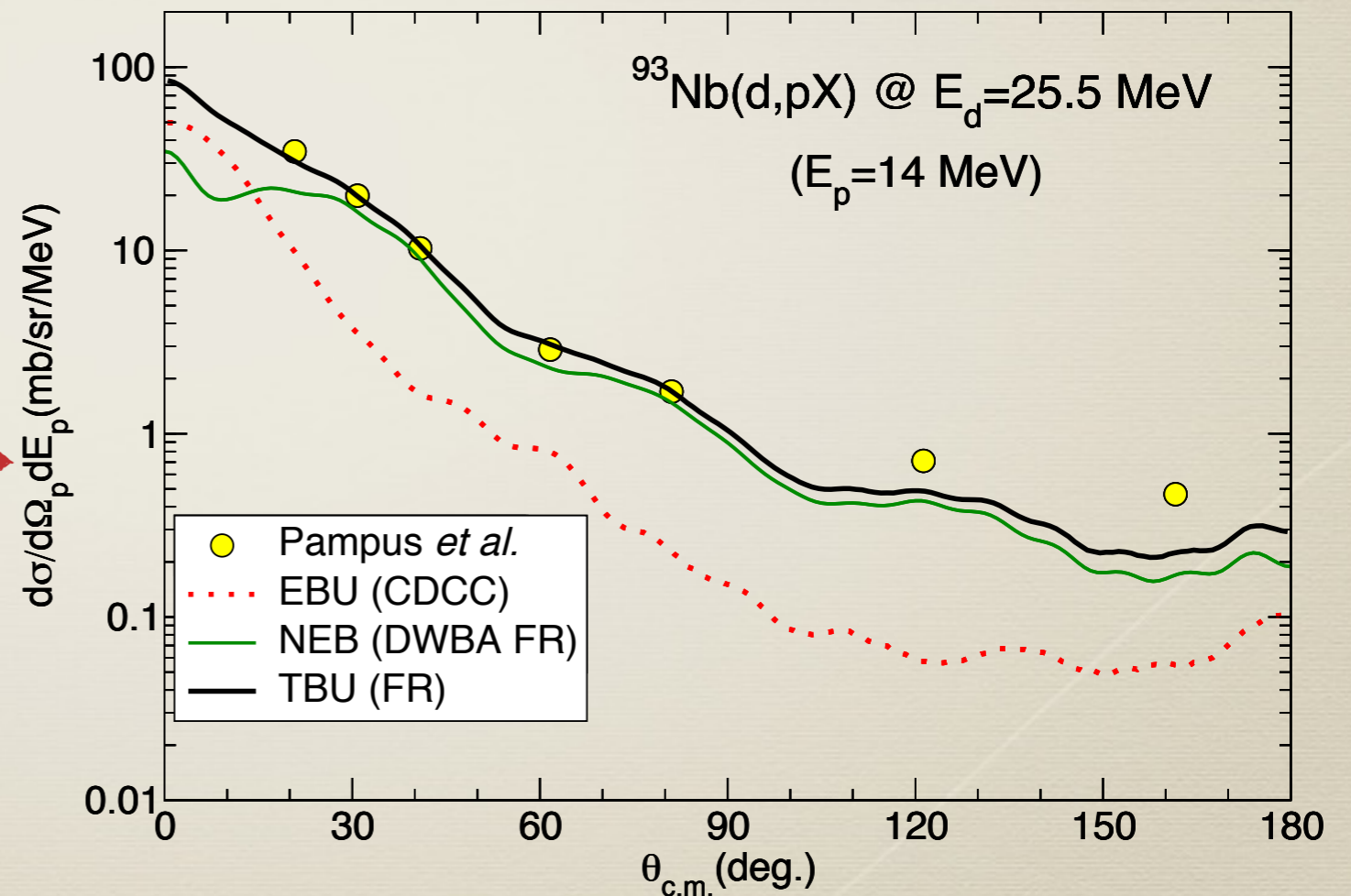




# Deuteron Breakup

- ✦  $d \Rightarrow (n + p)$ ,  $S_p = 2.224$  MeV
- ✦ only **proton** is detected
- ✦ EBU : CDCC (FRESCO)
- ✦ NEB : IAV model
- ✦ DWBA  $\Psi^{3b} \approx \chi_a \varphi_a \Phi_A$
- ✦ Exact Finite Range
- ✦ TBU = EBU + NEB 😊

*J. Pampus et al, Nucl. Phys. A311, 141 (1978).*





# Application to ${}^6\text{Li}$ breakup

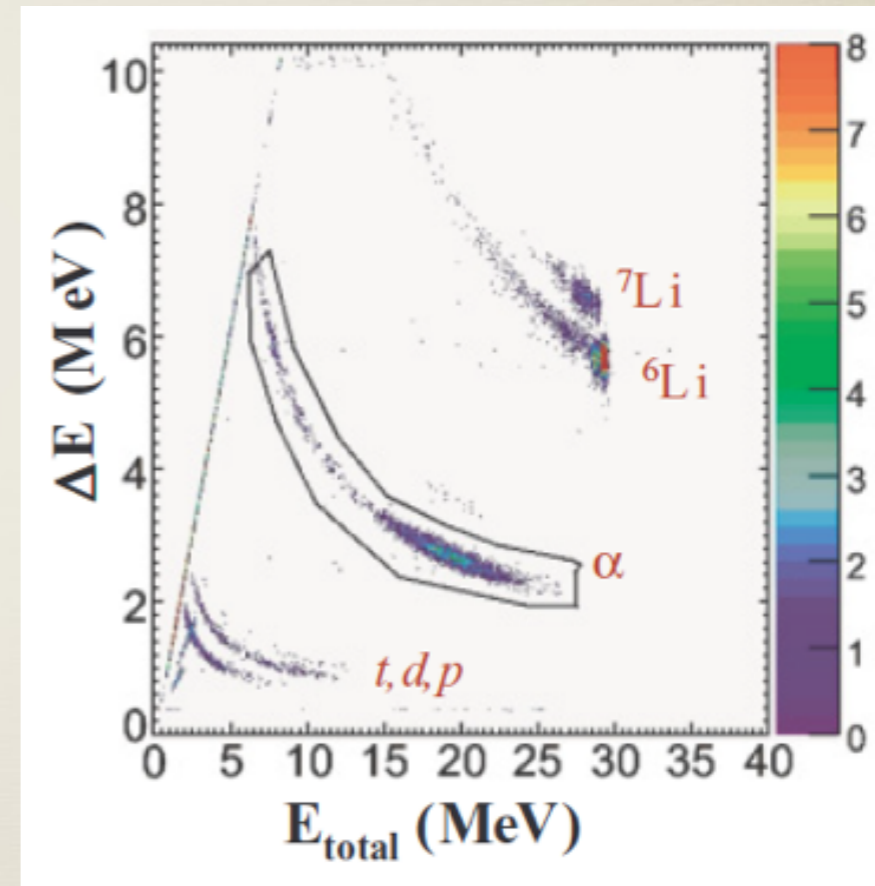
# Application to ${}^6\text{Li}$ breakup

★  ${}^6\text{Li} \Rightarrow (\alpha+d), Q_\alpha = -1.474 \text{ MeV}$



# Application to ${}^6\text{Li}$ breakup

✦  ${}^6\text{Li} \Rightarrow (\alpha+d)$ ,  $Q_\alpha = -1.474 \text{ MeV}$

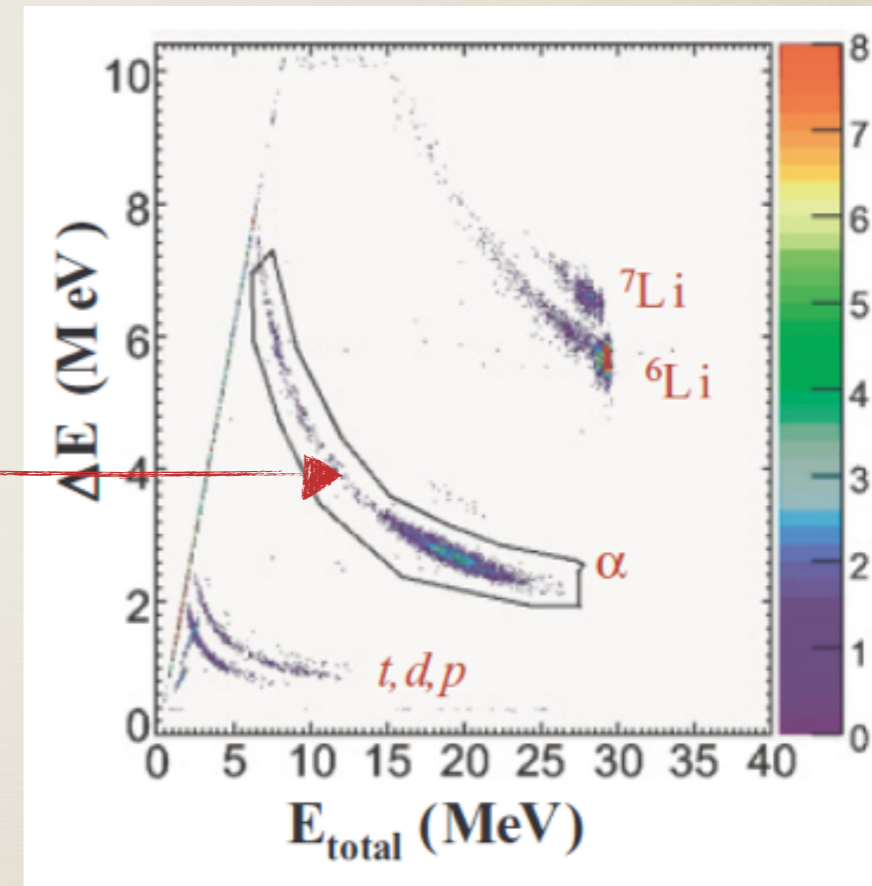


S. Santra et al, Phys. Rev. C 85, 014612 (2012).



# Application to ${}^6\text{Li}$ breakup

- ✦  ${}^6\text{Li} \Rightarrow (\alpha+d)$ ,  $Q_\alpha = -1.474 \text{ MeV}$
- ✦ large  $\alpha$  yields are detected

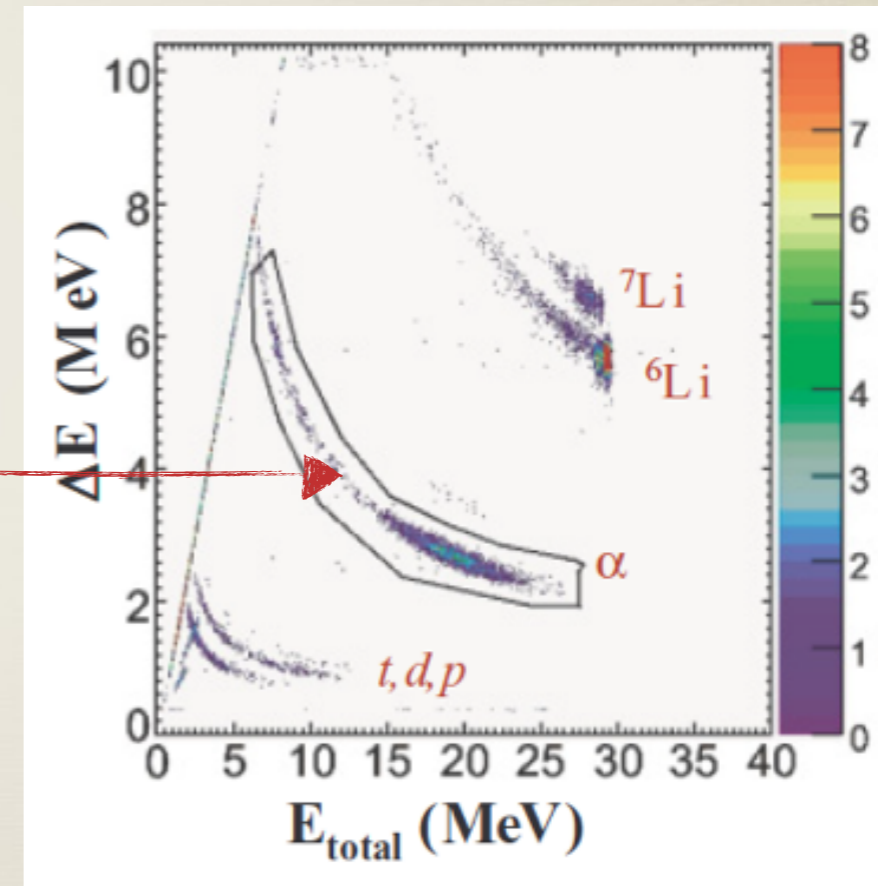


S. Santra et al, Phys. Rev. C 85, 014612 (2012).



# Application to ${}^6\text{Li}$ breakup

- ${}^6\text{Li} \Rightarrow (\alpha+d)$ ,  $Q_\alpha = -1.474 \text{ MeV}$
- large  $\alpha$  yields are detected
- $\sigma_\alpha \gg \sigma_d$  (EBU is not dominant)

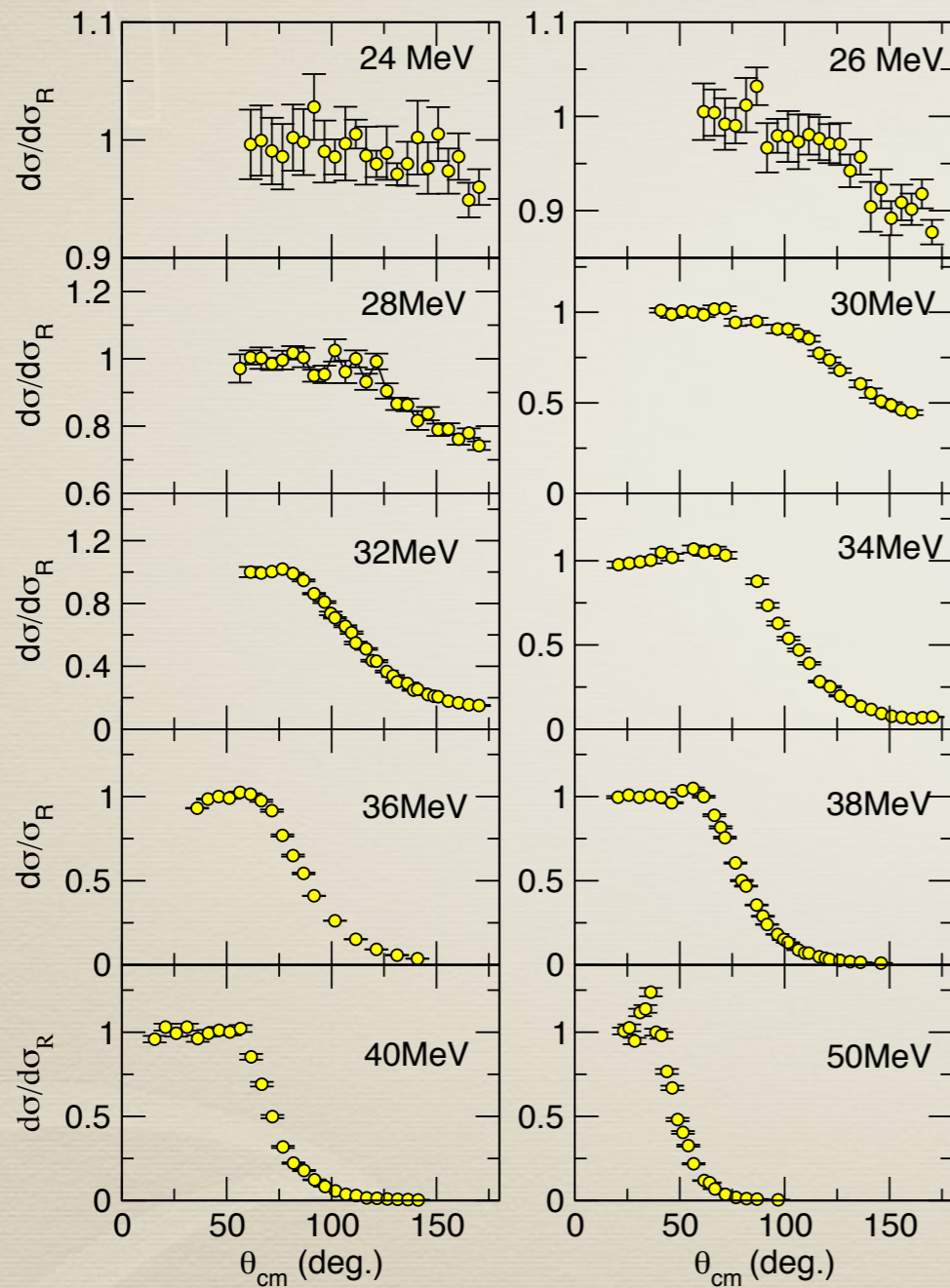


S. Santra et al, Phys. Rev. C 85, 014612 (2012).





# $^{209}\text{Bi}(^6\text{Li},^6\text{Li})^{209}\text{Bi}$

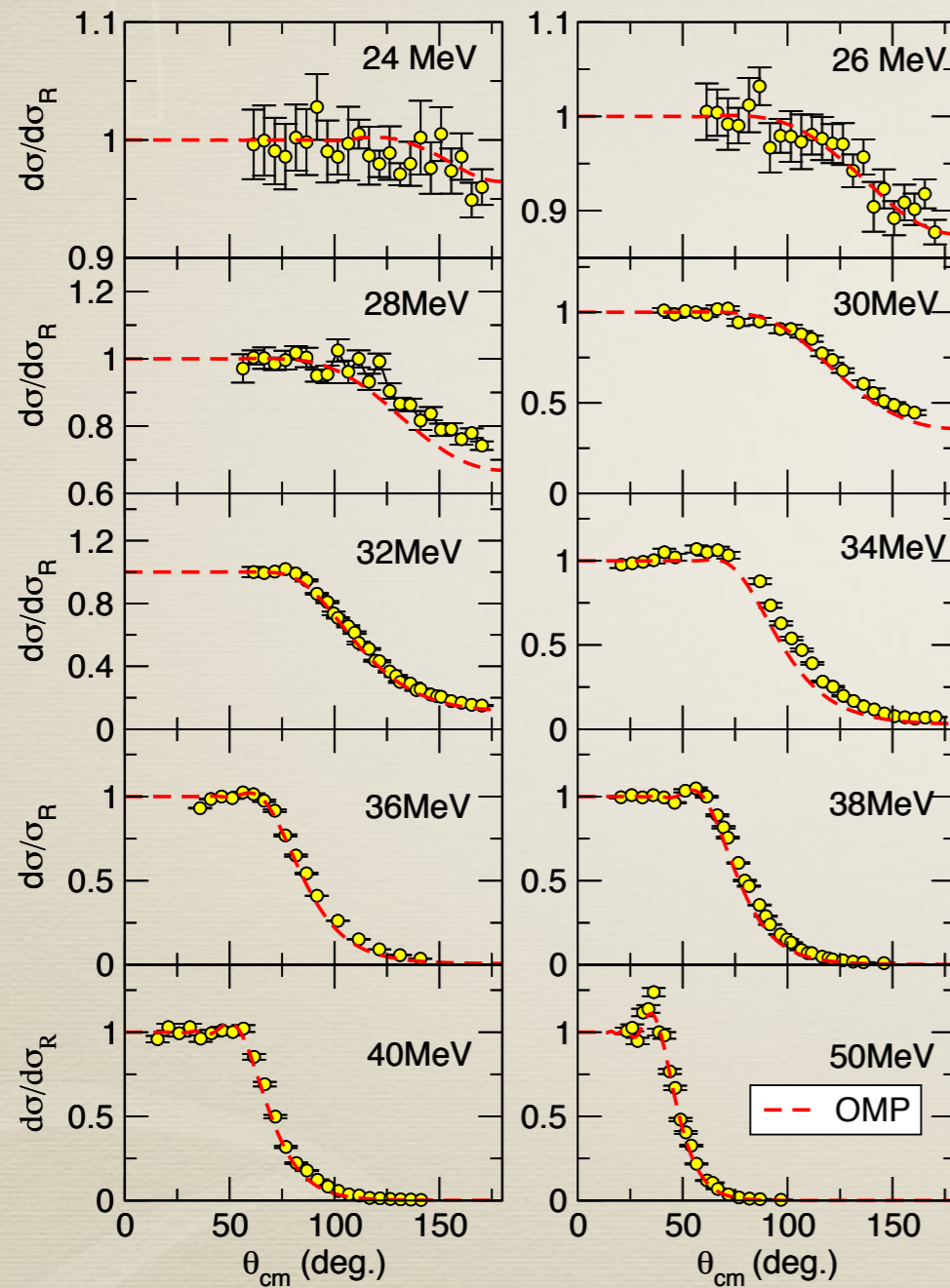


★ Elastic scattering

★ data : S. Santra et al



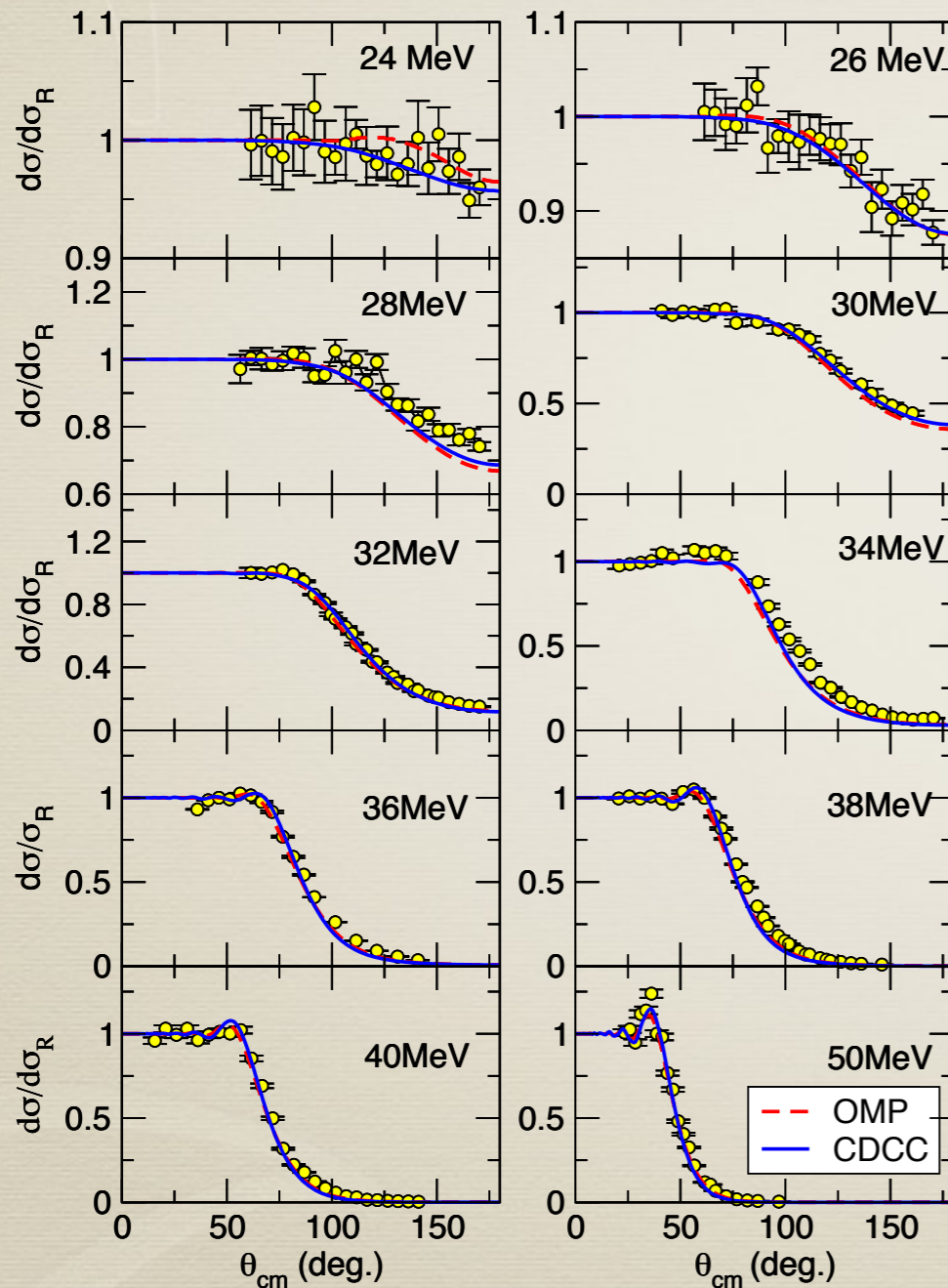
# $^{209}\text{Bi}(^6\text{Li}, ^6\text{Li})^{209}\text{Bi}$



- ★ Elastic scattering
- ★ data : S. Santra et al
- ★ J. Cook potential (global  $^{6,7}\text{Li}$  OMP)



# $^{209}\text{Bi}(^6\text{Li},^6\text{Li})^{209}\text{Bi}$



- ★ Elastic scattering
- ★ data : S. Santra et al
- ★ J. Cook potential (global  $^{6,7}\text{Li}$  OMP)
- ★ CDCC calculation
- ★  $d/\alpha+^{209}\text{Bi}$  : OMP
- ★  $d+^{209}\text{Bi}$  : requires reduction of imaginary part due to the limitation of 2-body model of  $^6\text{Li}$ .

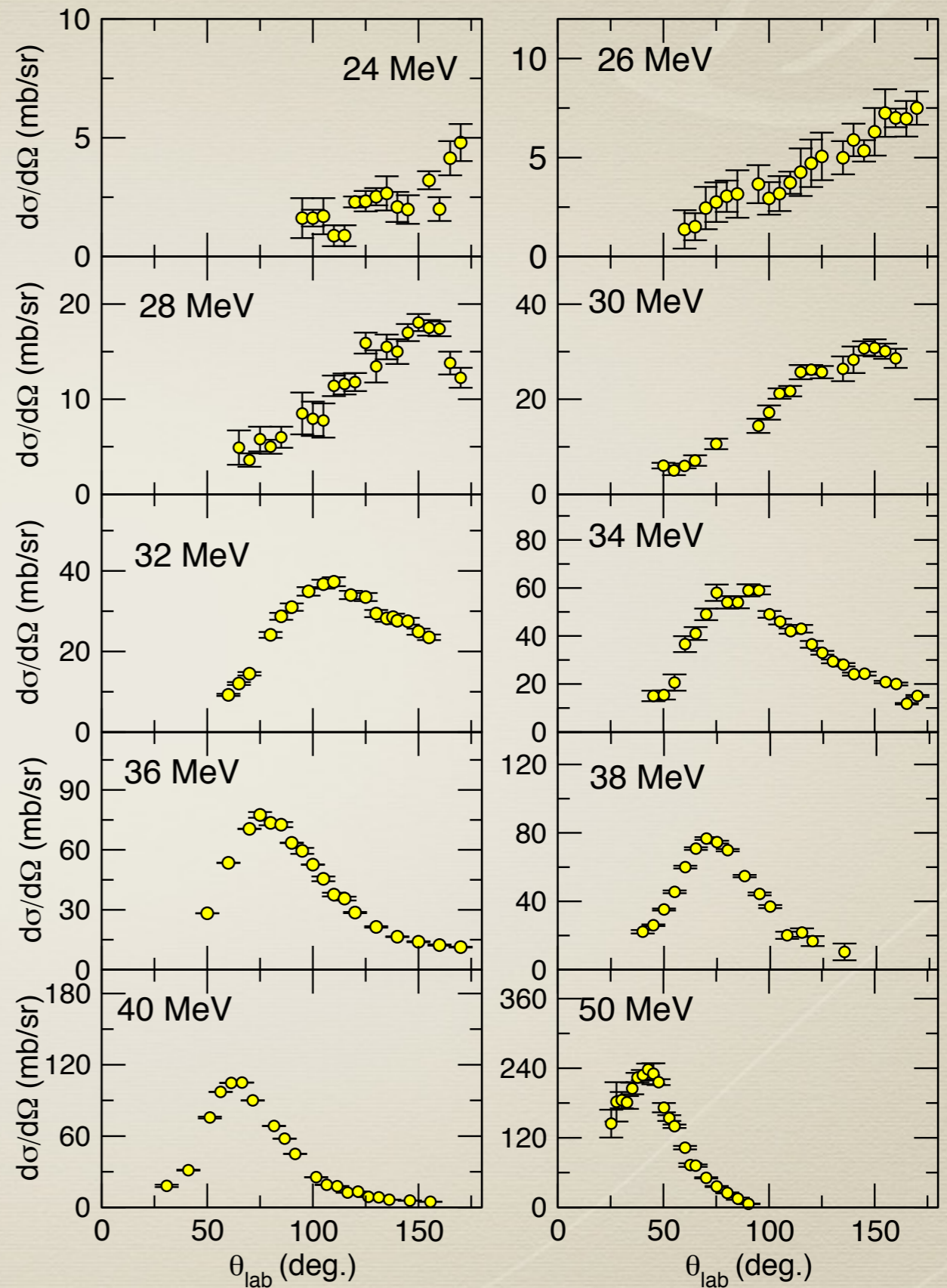
$^{209}\text{Bi}(^6\text{Li},\alpha X)$



# $^{209}\text{Bi}(^6\text{Li},\alpha X)$

✦ Inclusive  $\alpha$

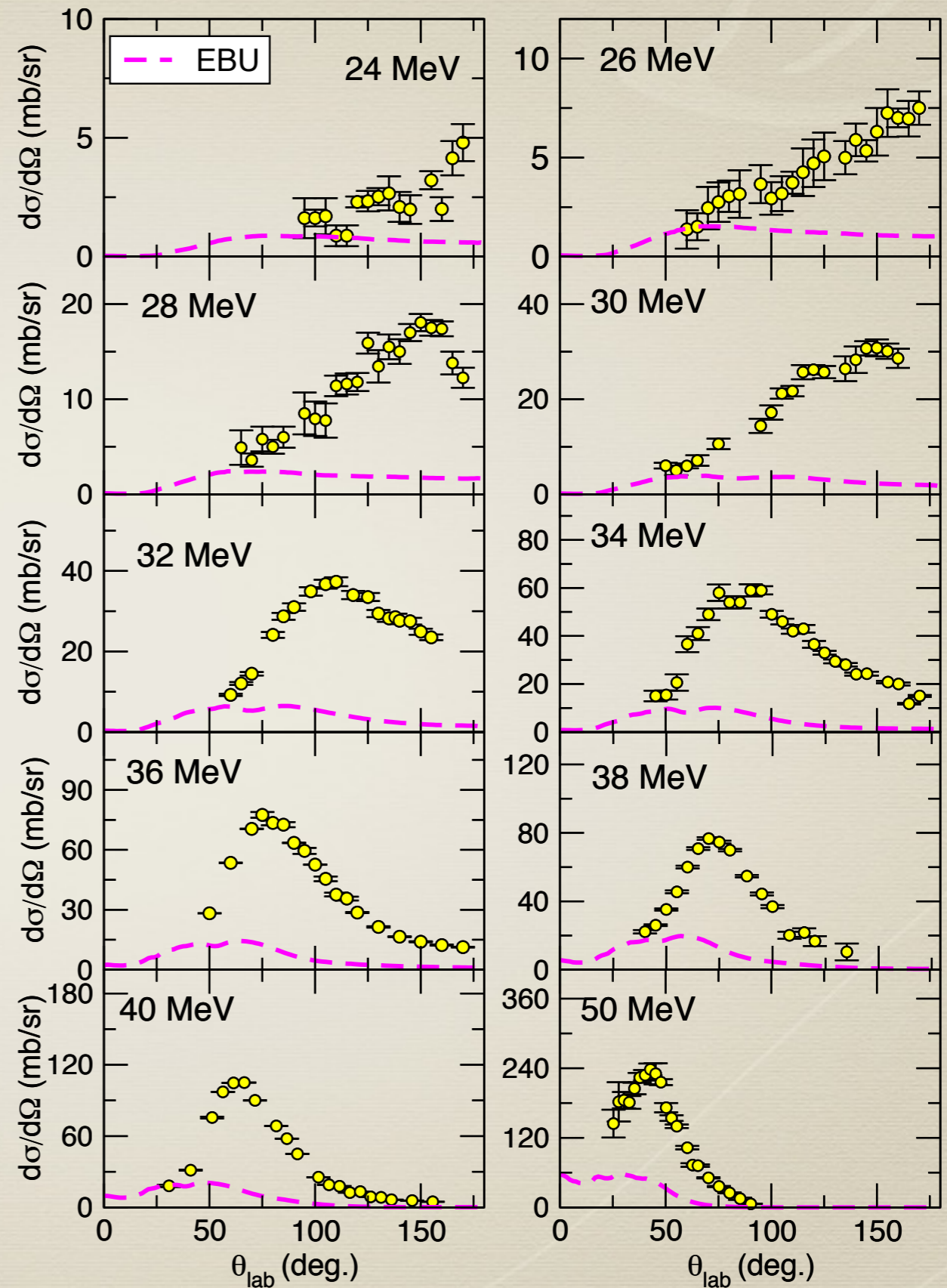
✦ data: S. Santra et al





# $^{209}\text{Bi}(^6\text{Li},\alpha X)$

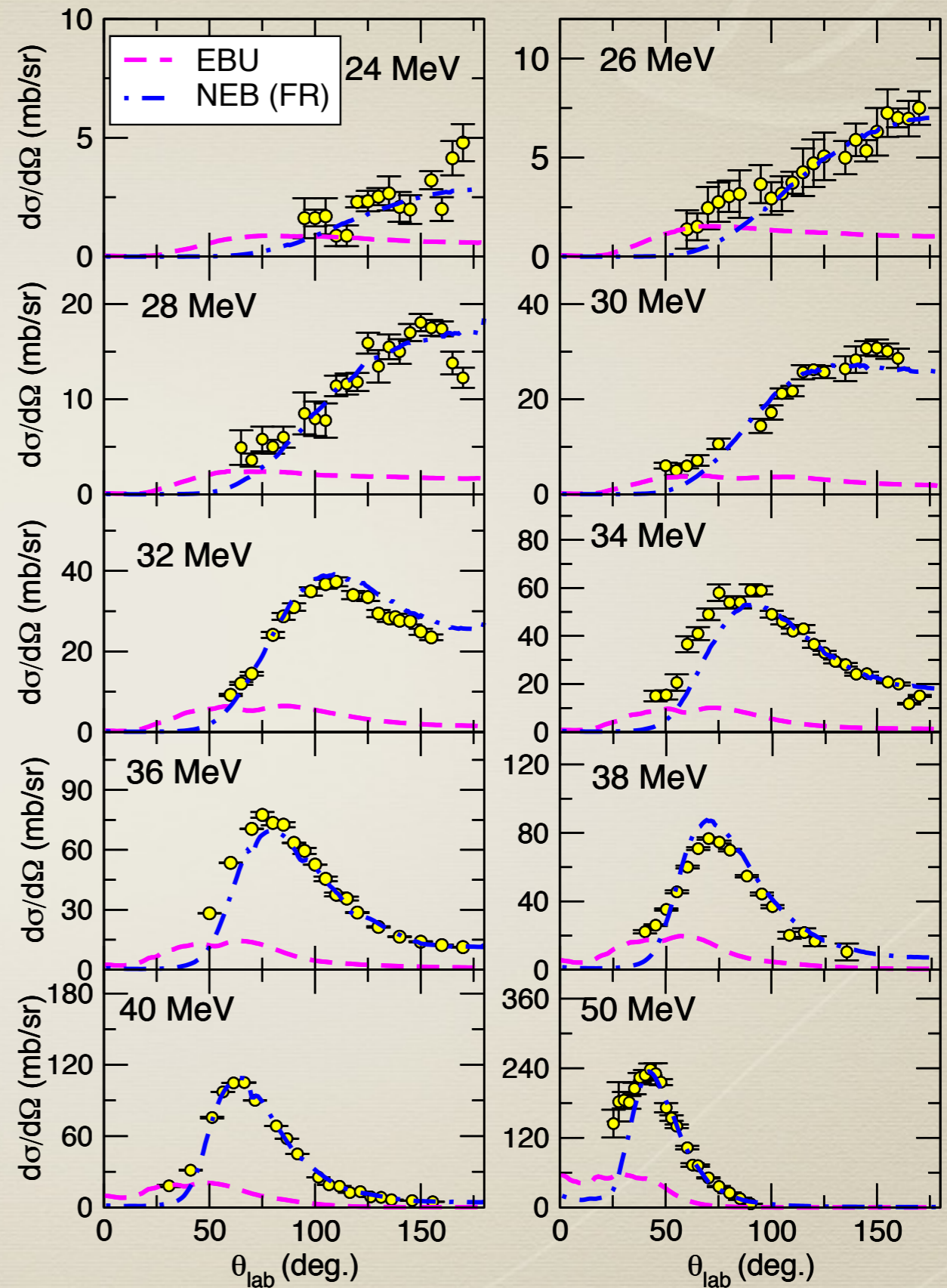
- Inclusive  $\alpha$
- data: S. Santra et al
- EBU : CDCC calculation





# $^{209}\text{Bi}(^6\text{Li},\alpha X)$

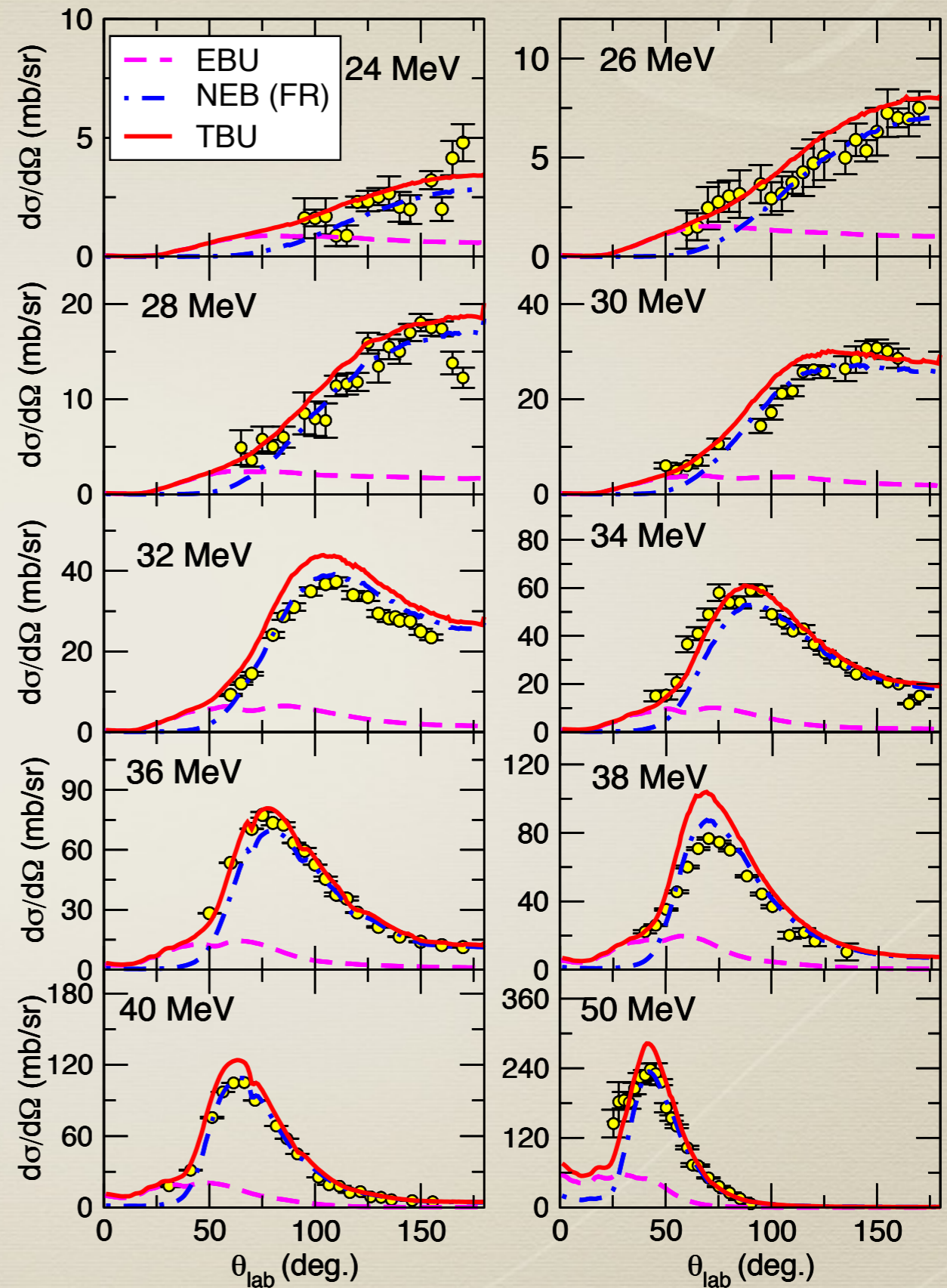
- ✦ Inclusive  $\alpha$
- ✦ data: S. Santra et al
- ✦ EBU : CDCC calculation
- ✦ NEB : IAV model (DWBA)
- ✦ dominate inclusive  $\alpha$





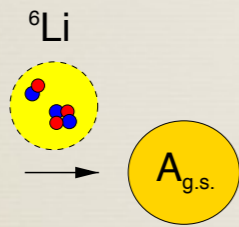
# $^{209}\text{Bi}(^6\text{Li},\alpha X)$

- Inclusive  $\alpha$
- data: S. Santra et al
- EBU : CDCC calculation
- NEB : IAV model (DWBA)
- dominate inclusive  $\alpha$
- TBU=EBU+NEB
- overall agreement with data

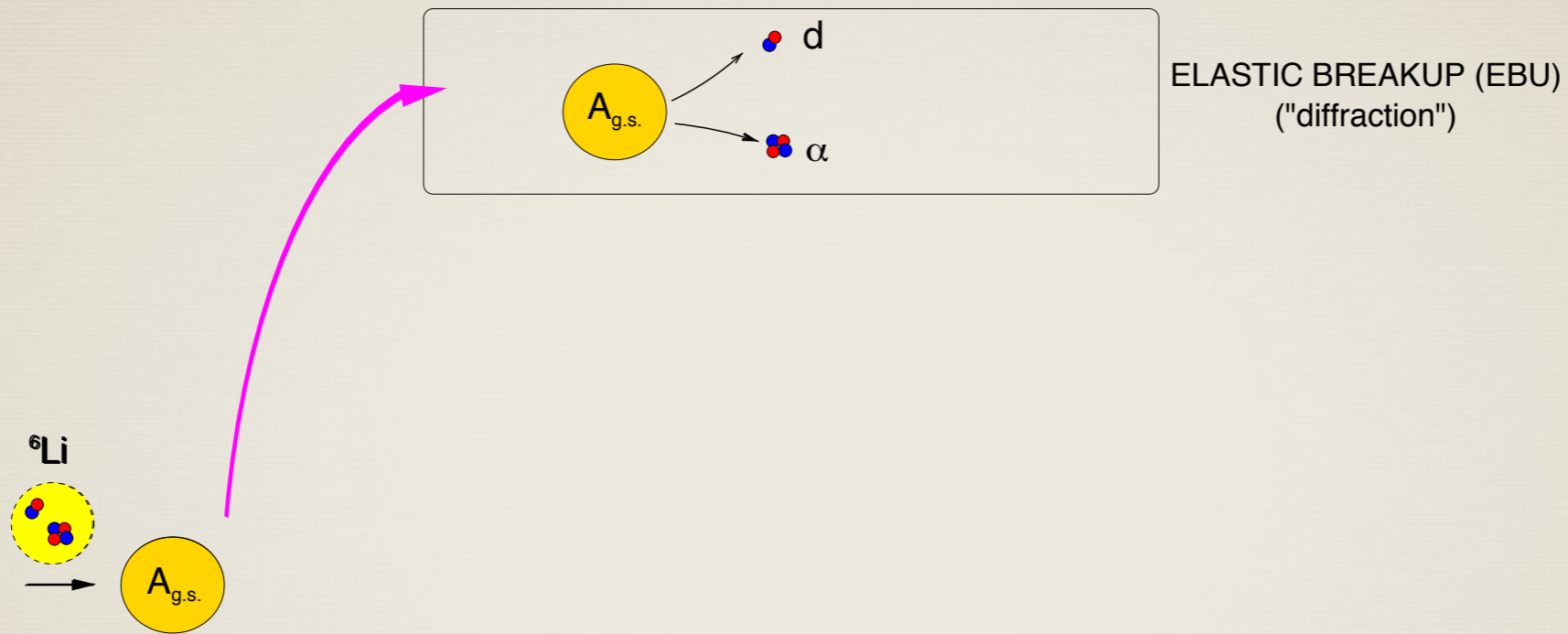




# Reaction cross section of ${}^6\text{Li}+{}^{209}\text{Bi}$

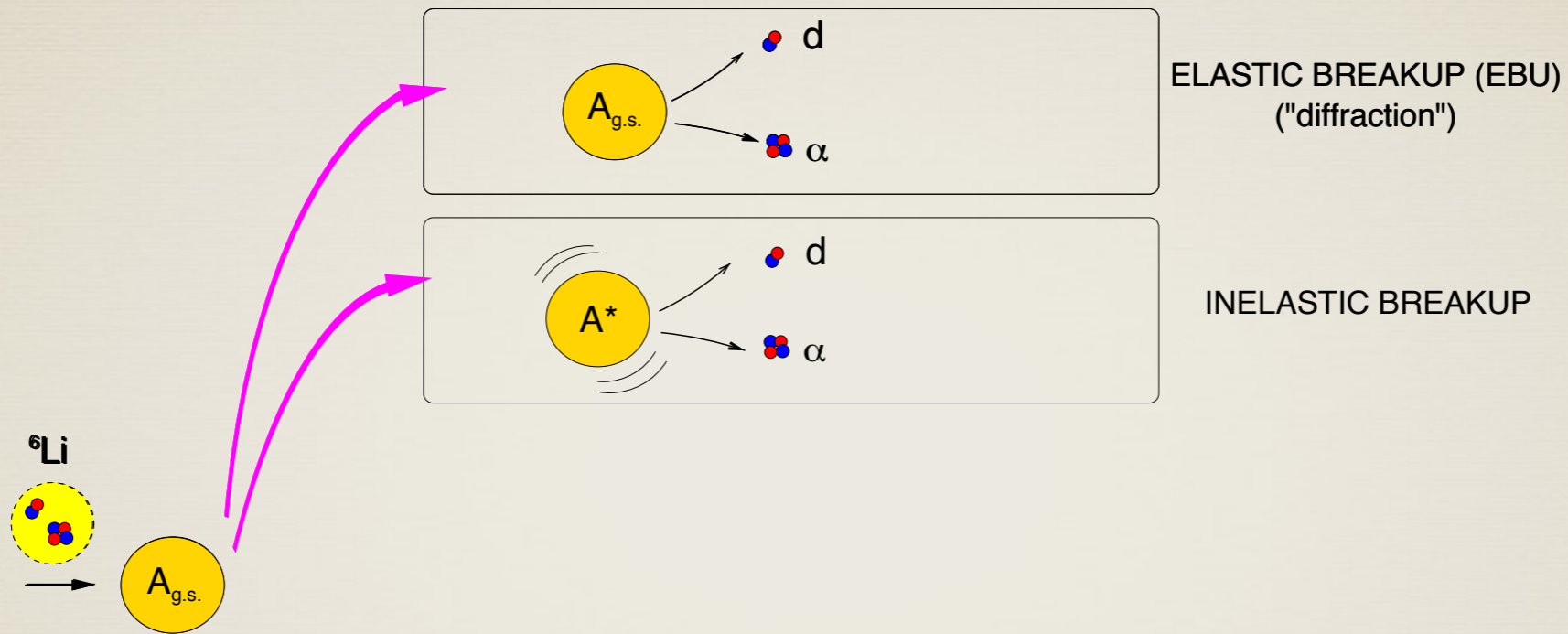


# Reaction cross section of ${}^6\text{Li}+{}^{209}\text{Bi}$

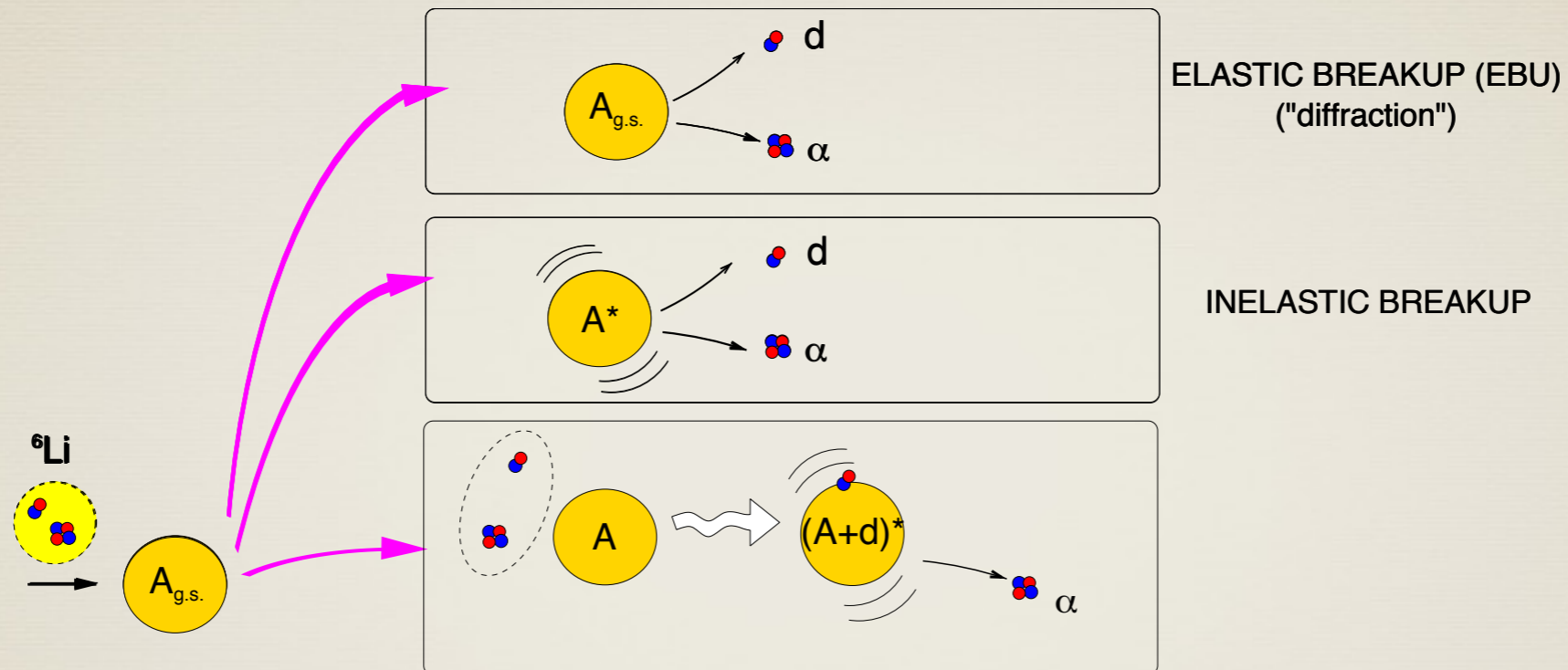




# Reaction cross section of ${}^6\text{Li}+{}^{209}\text{Bi}$

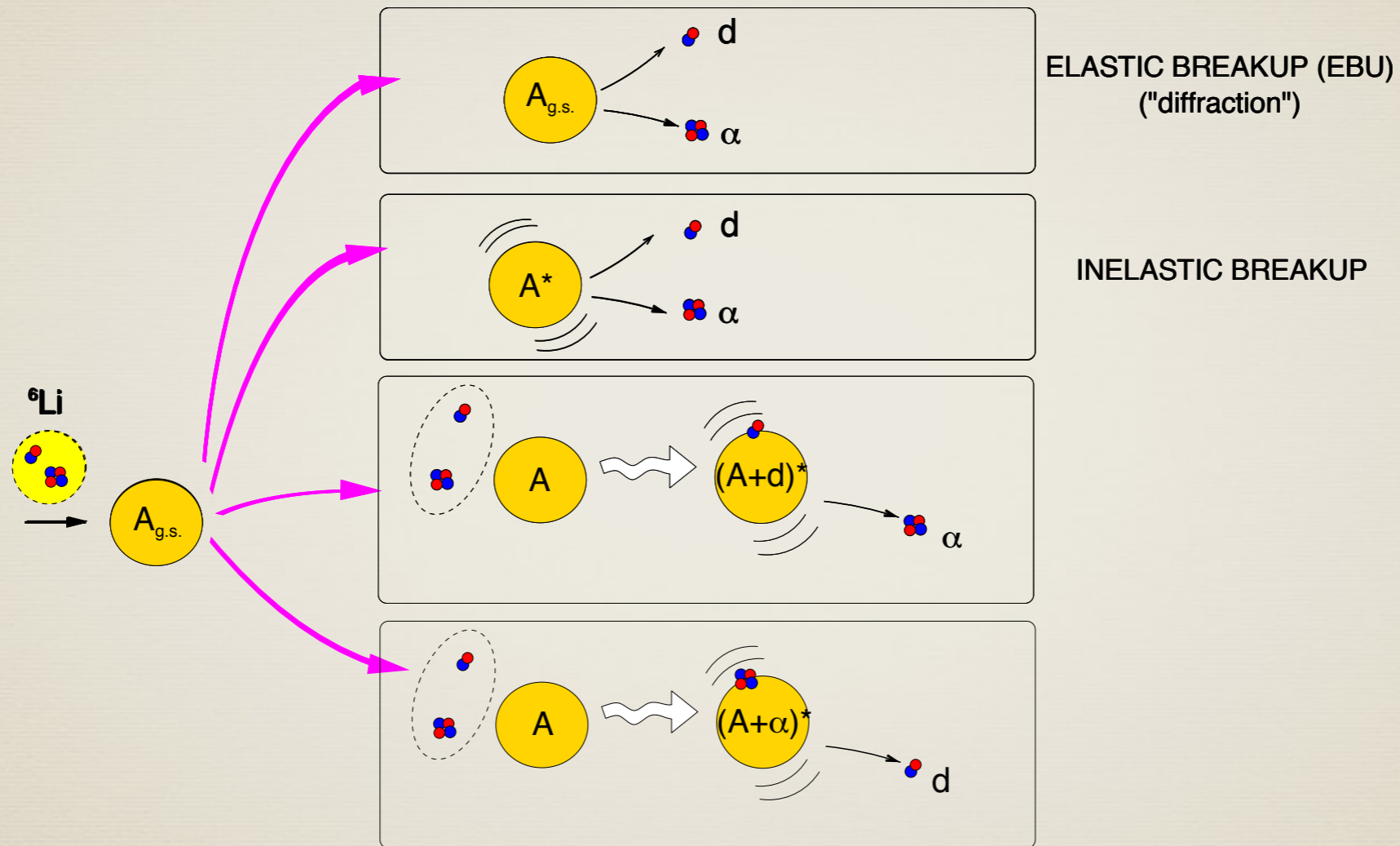


# Reaction cross section of ${}^6\text{Li}+{}^{209}\text{Bi}$

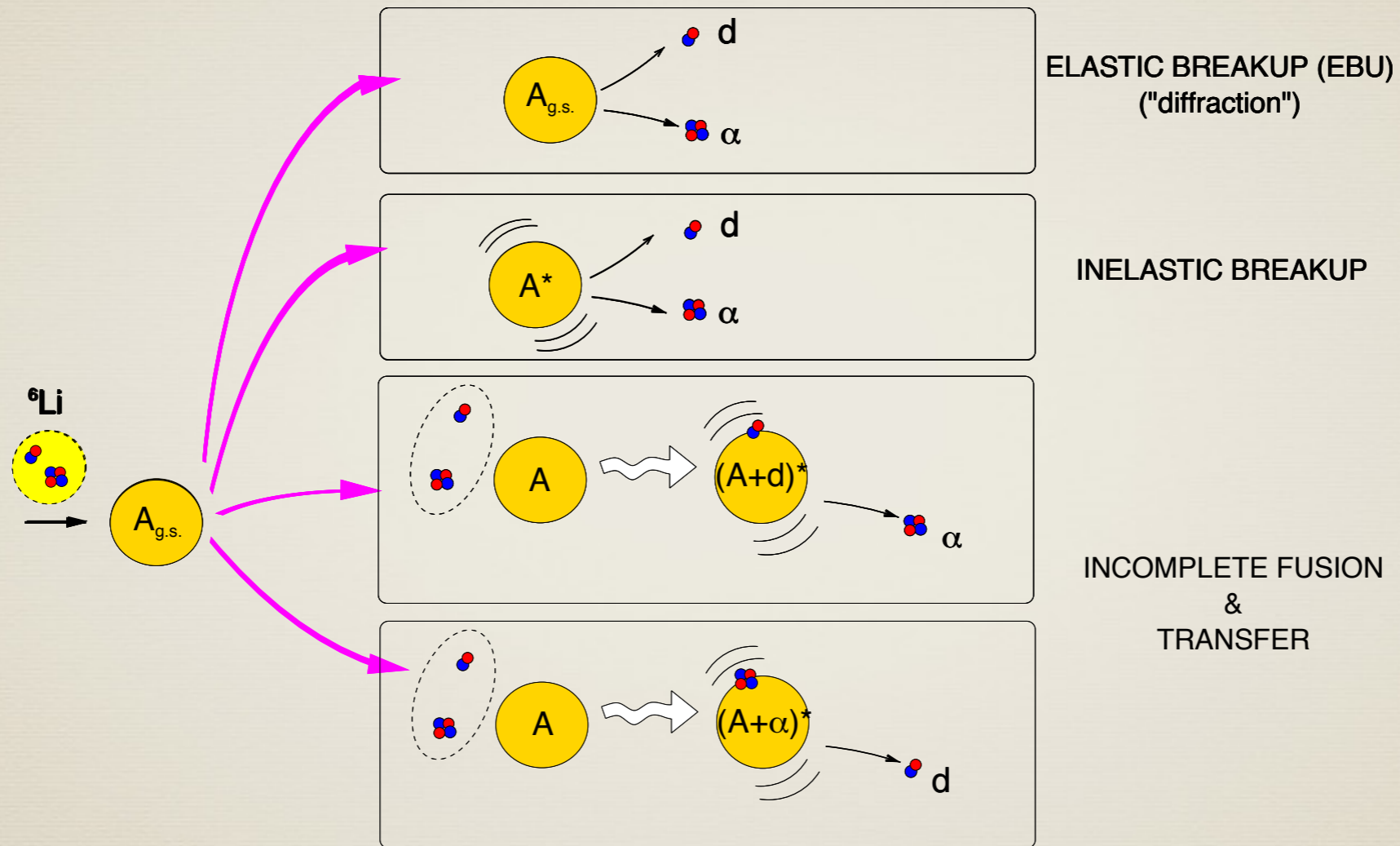




# Reaction cross section of ${}^6\text{Li}+{}^{209}\text{Bi}$

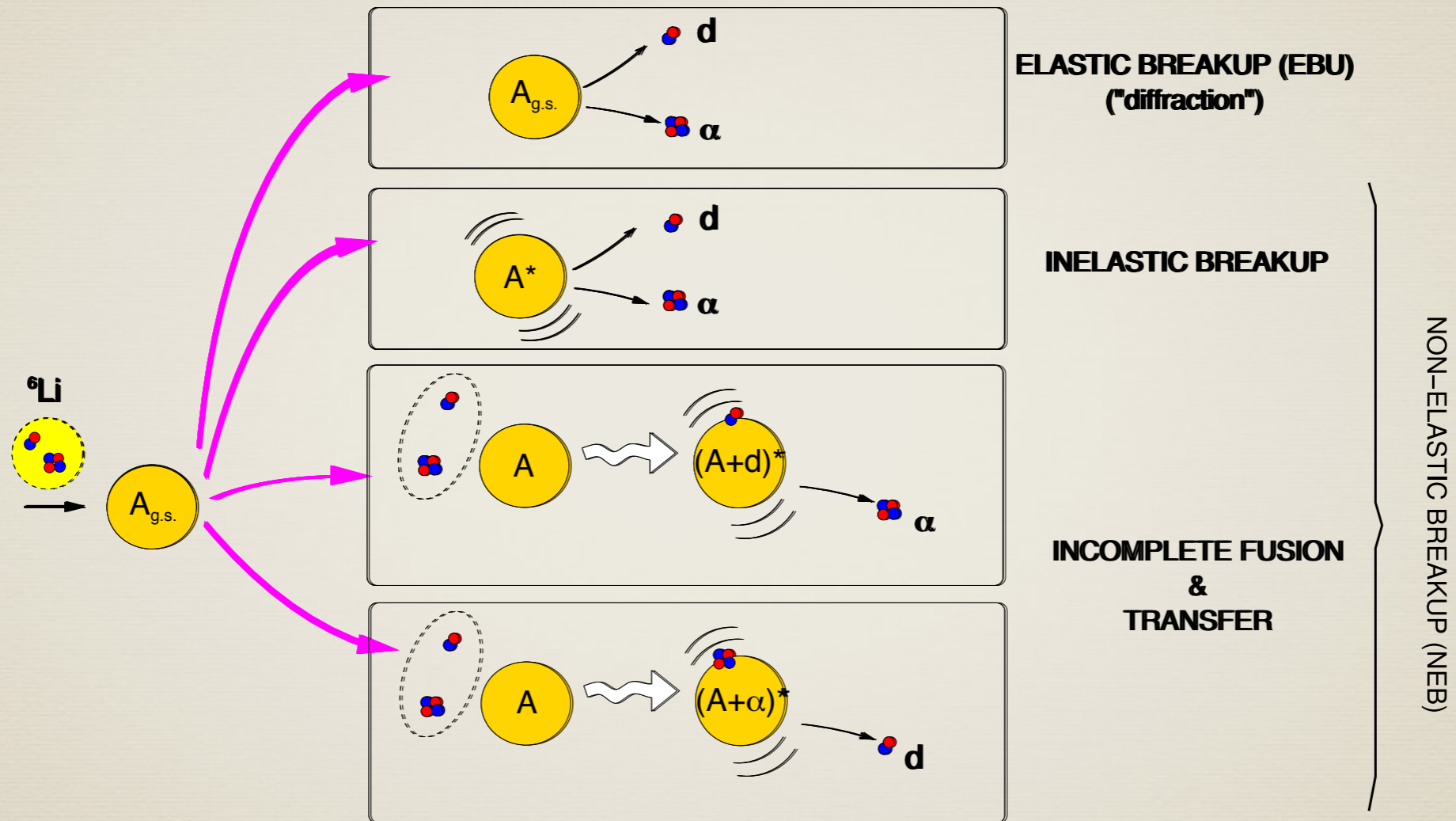


# Reaction cross section of ${}^6\text{Li}+{}^{209}\text{Bi}$





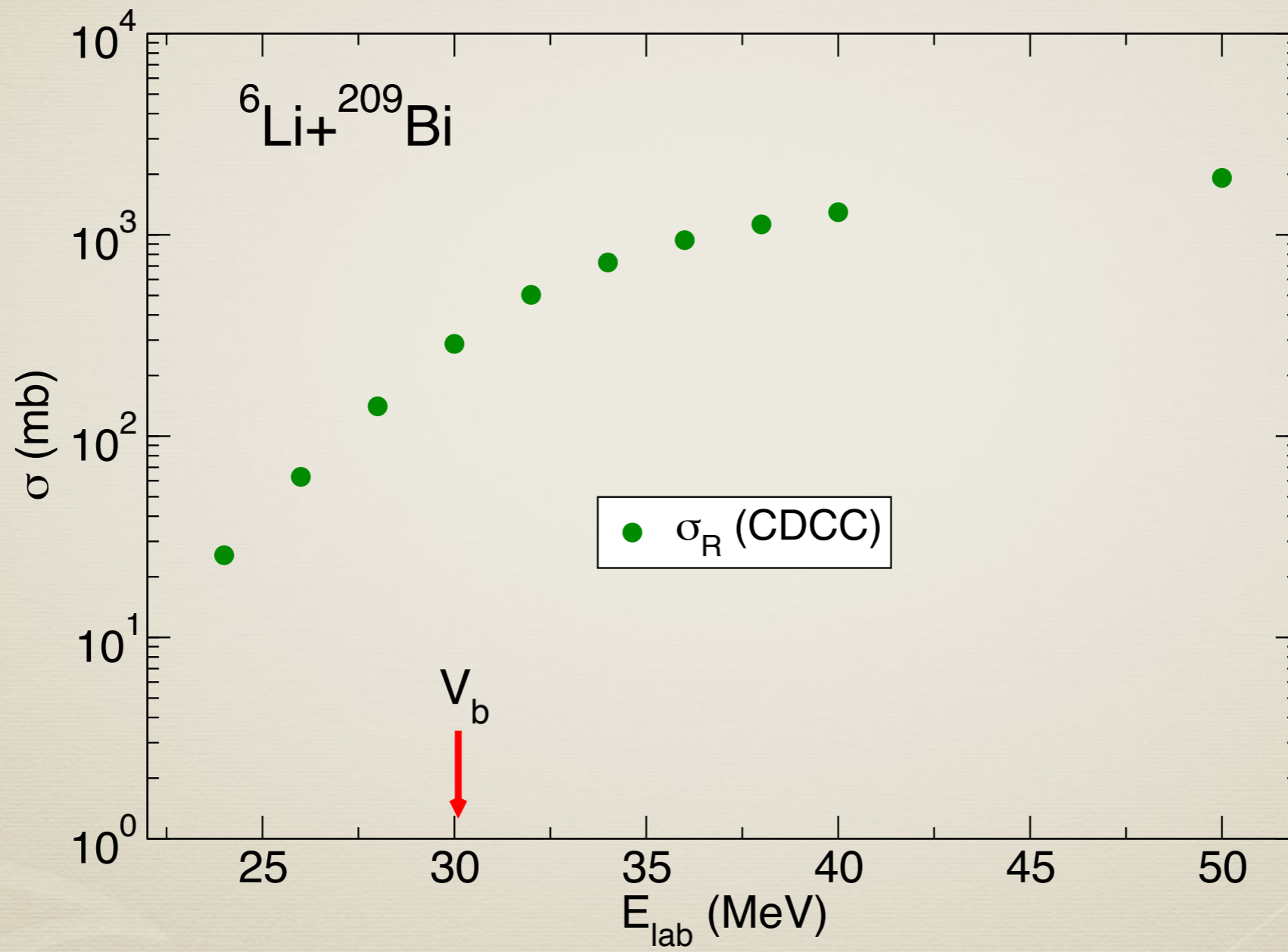
# Reaction cross section of ${}^6\text{Li}+{}^{209}\text{Bi}$



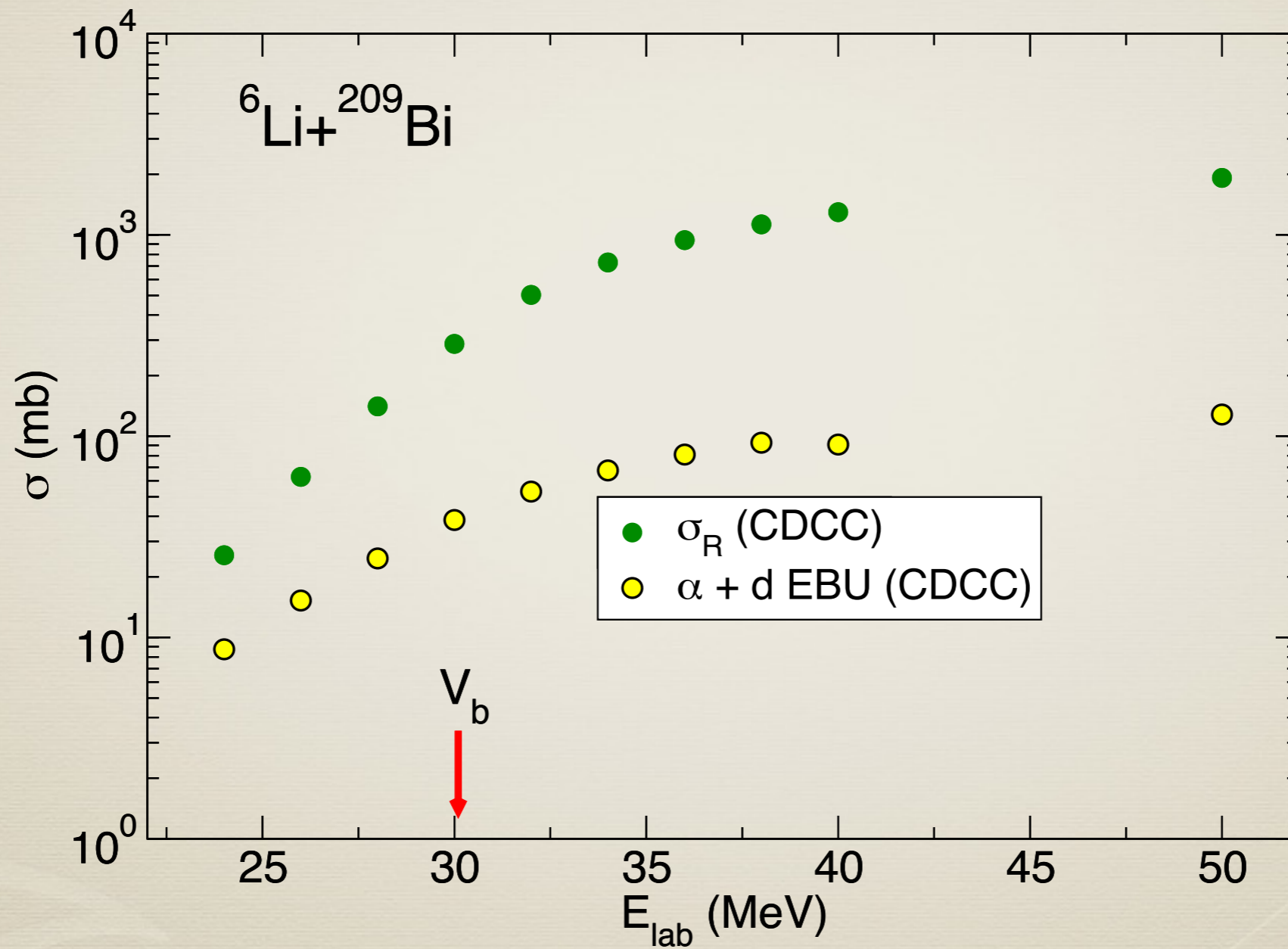




# ${}^6\text{Li} + {}^{209}\text{Bi}$

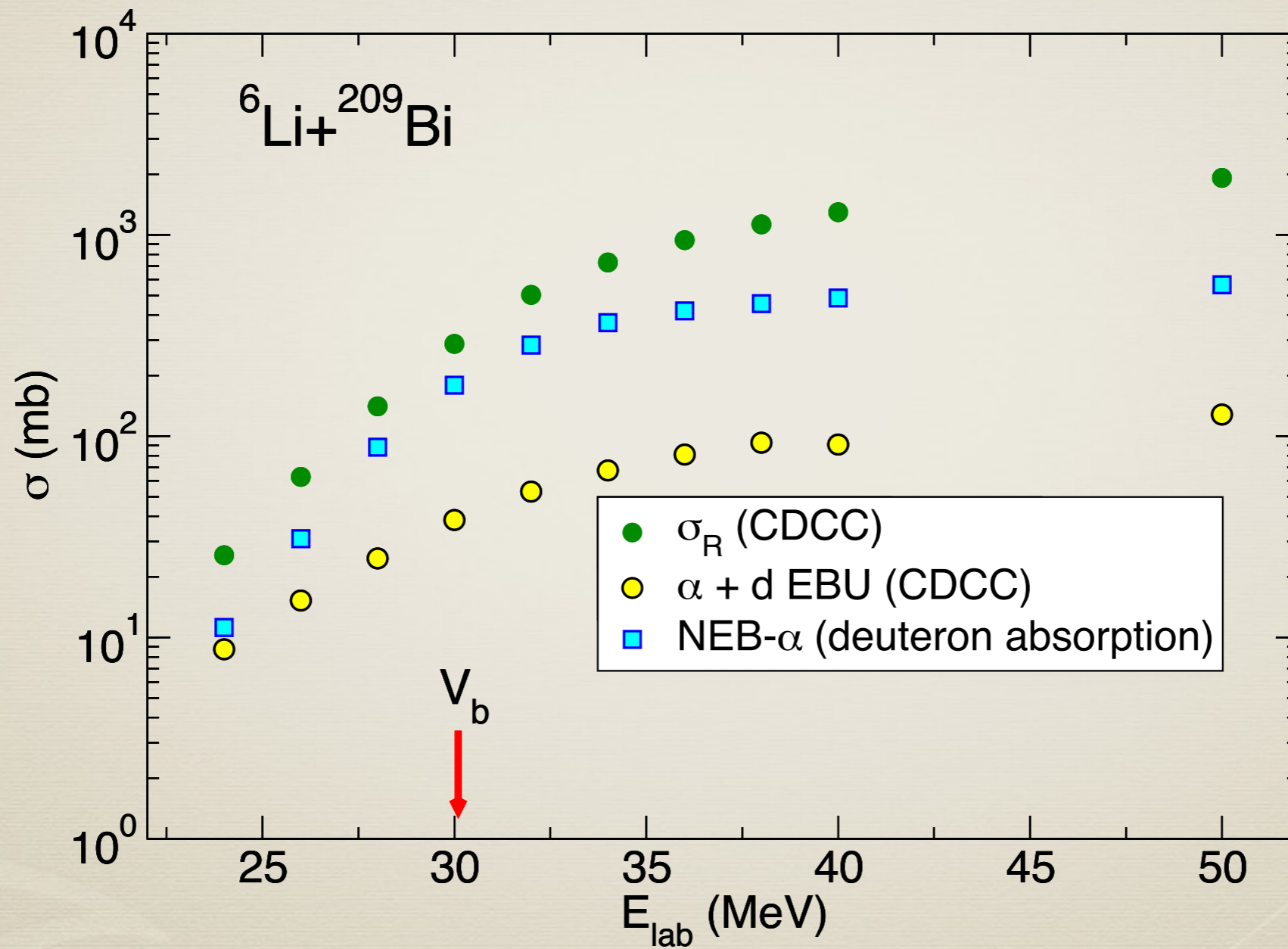


# ${}^6\text{Li} + {}^{209}\text{Bi}$

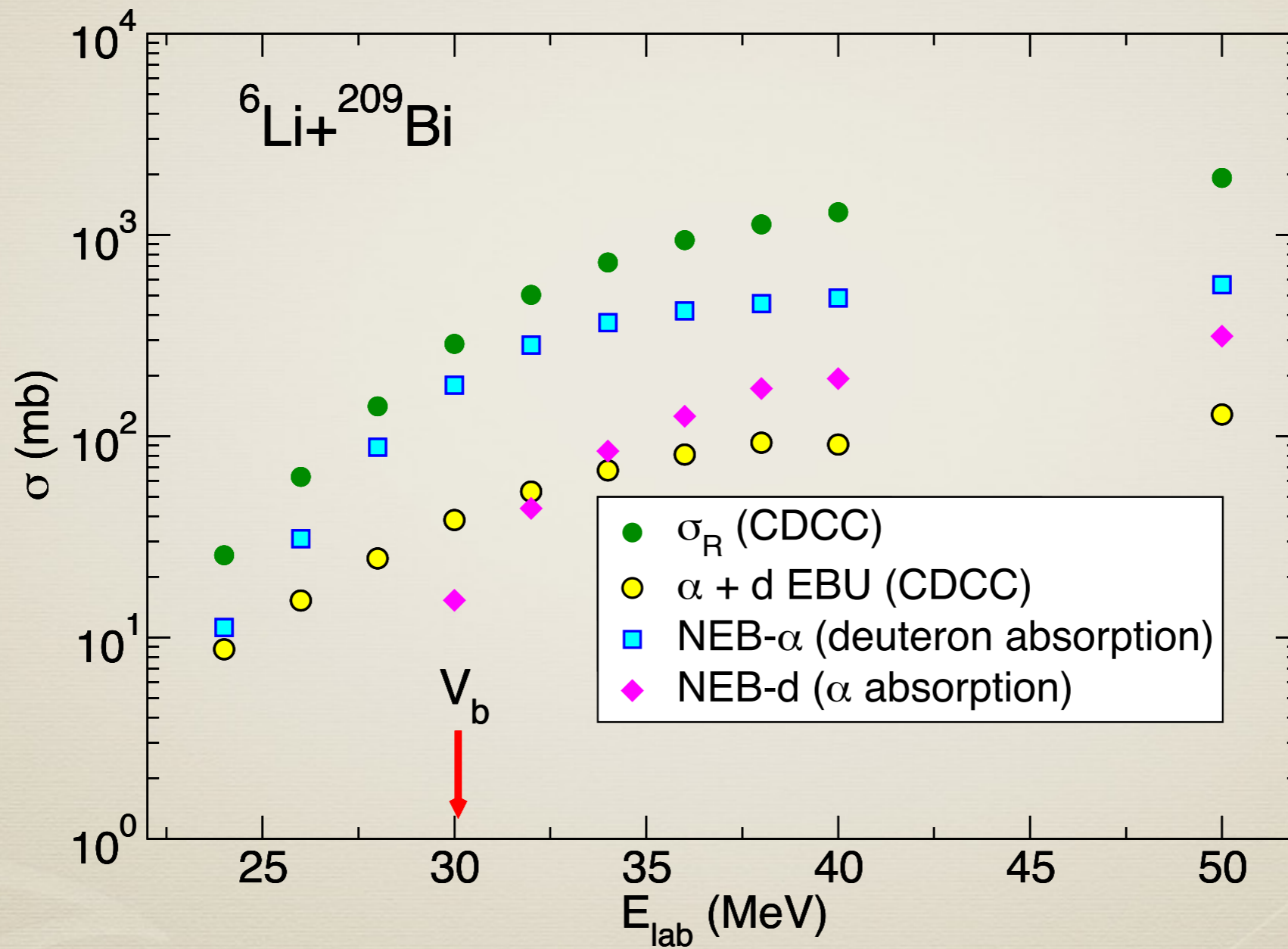




# ${}^6\text{Li} + {}^{209}\text{Bi}$



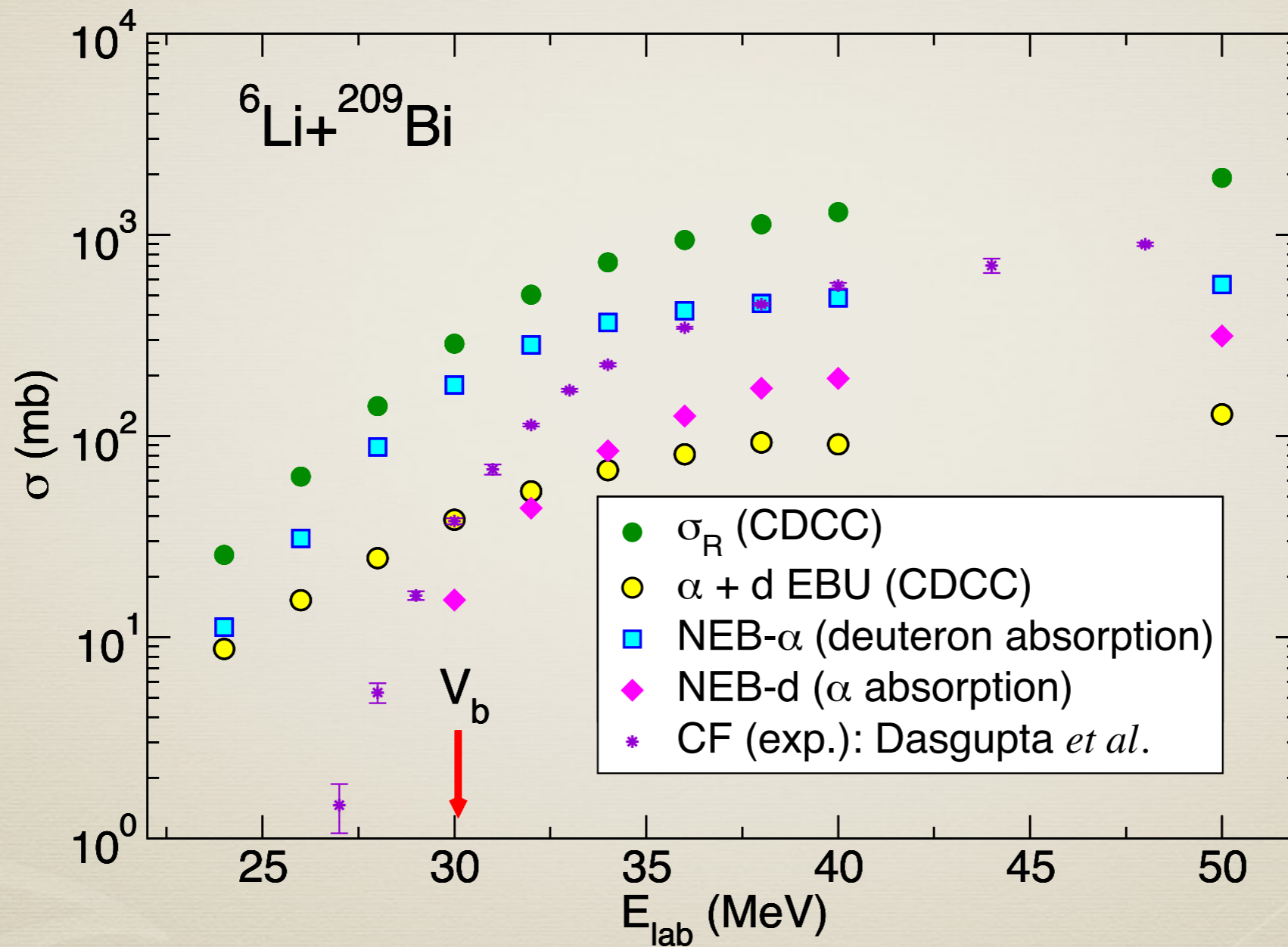
# ${}^6\text{Li} + {}^{209}\text{Bi}$





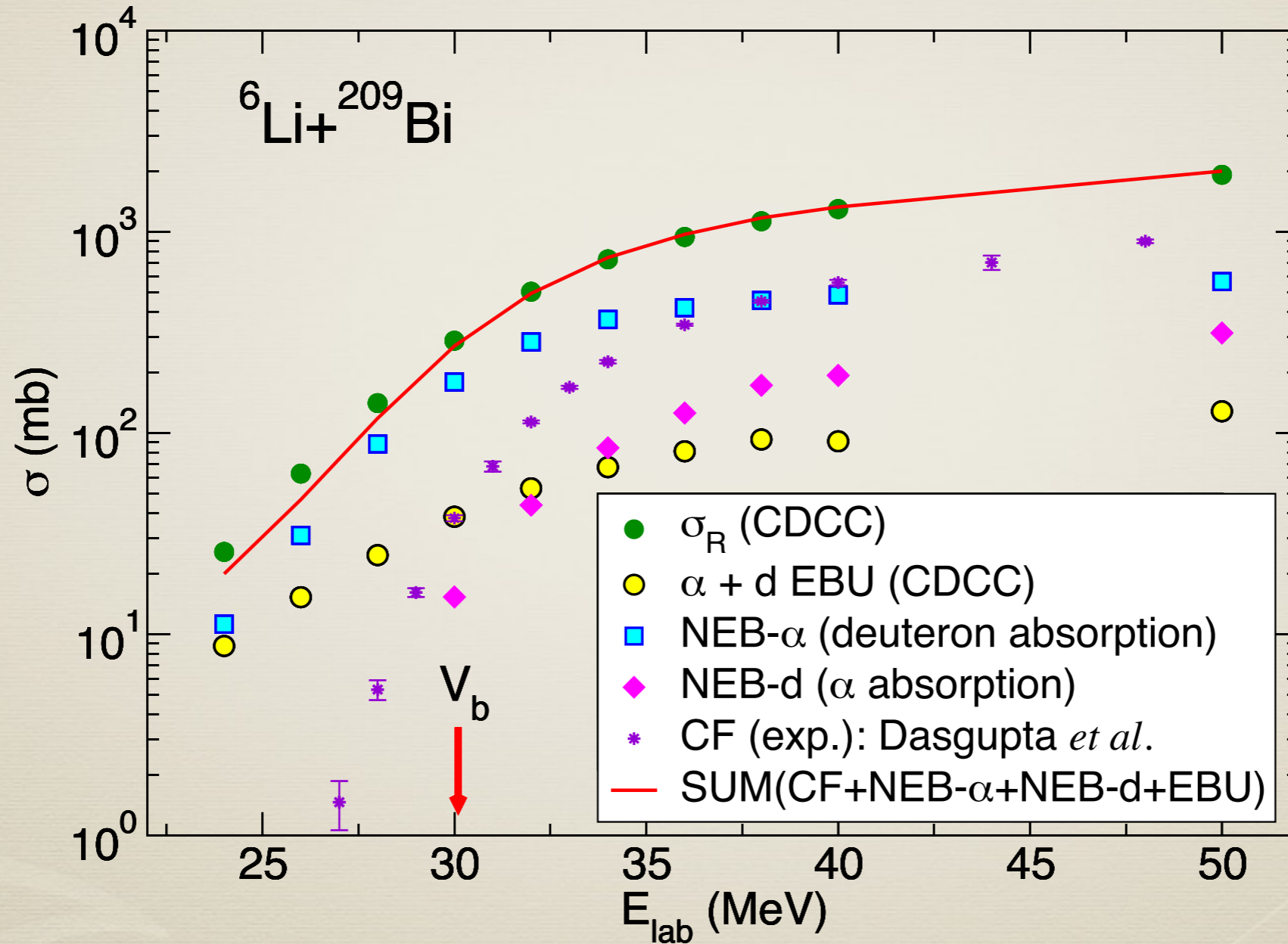
# ${}^6\text{Li} + {}^{209}\text{Bi}$

CF: M. Dasgupta et al, Phys. Rev. C 70, 024606 (2004).



# ${}^6\text{Li} + {}^{209}\text{Bi}$

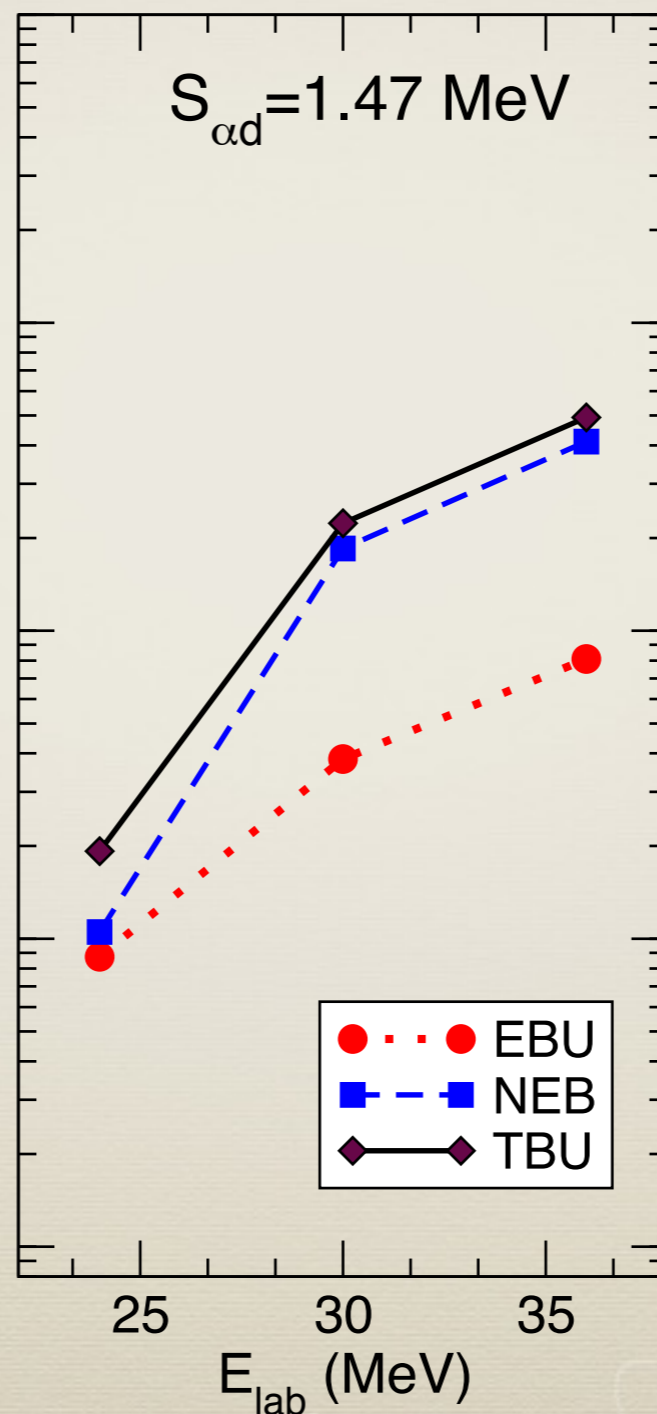
CF: M. Dasgupta et al, Phys. Rev. C 70, 024606 (2004).



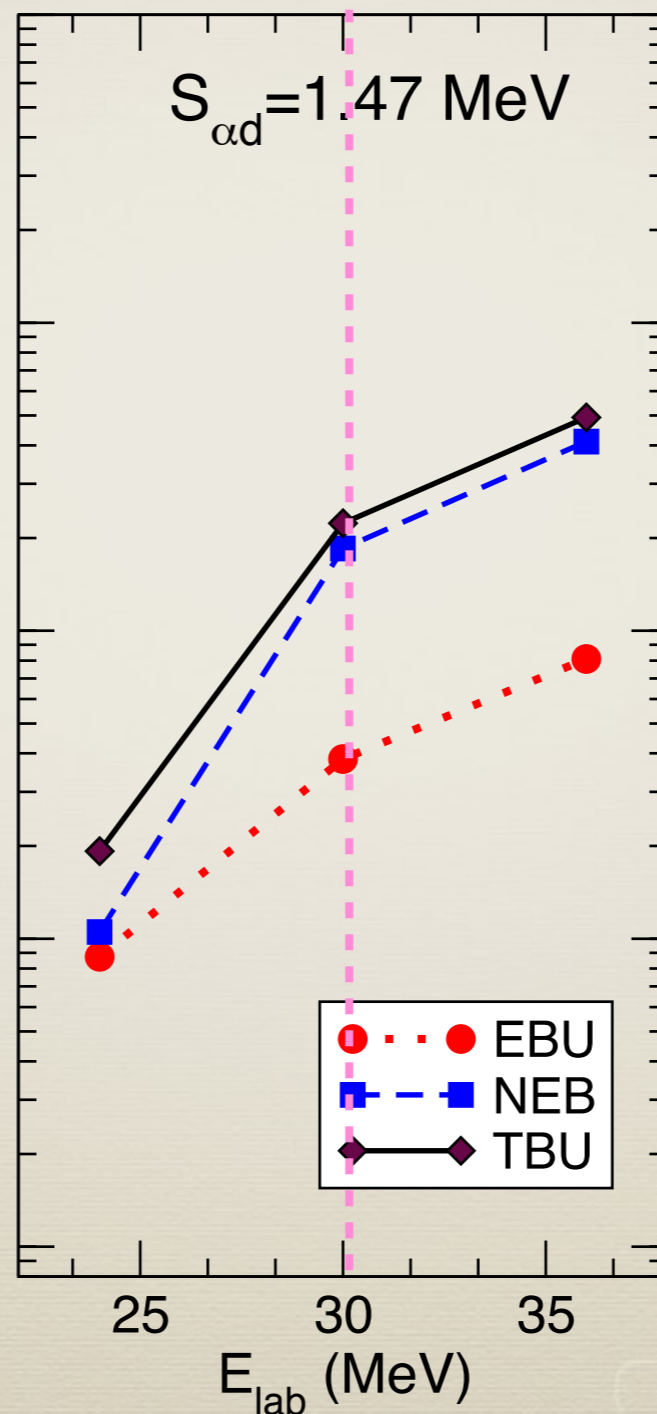
$$\sigma_R \approx \sigma_{\alpha+d}(\text{EBU}) + \sigma_{\alpha}(\text{NEB}) + \sigma_d(\text{NEB}) + \sigma(\text{CF})$$



# Influence of the separation energy and the incident energy on the EBU and NEB

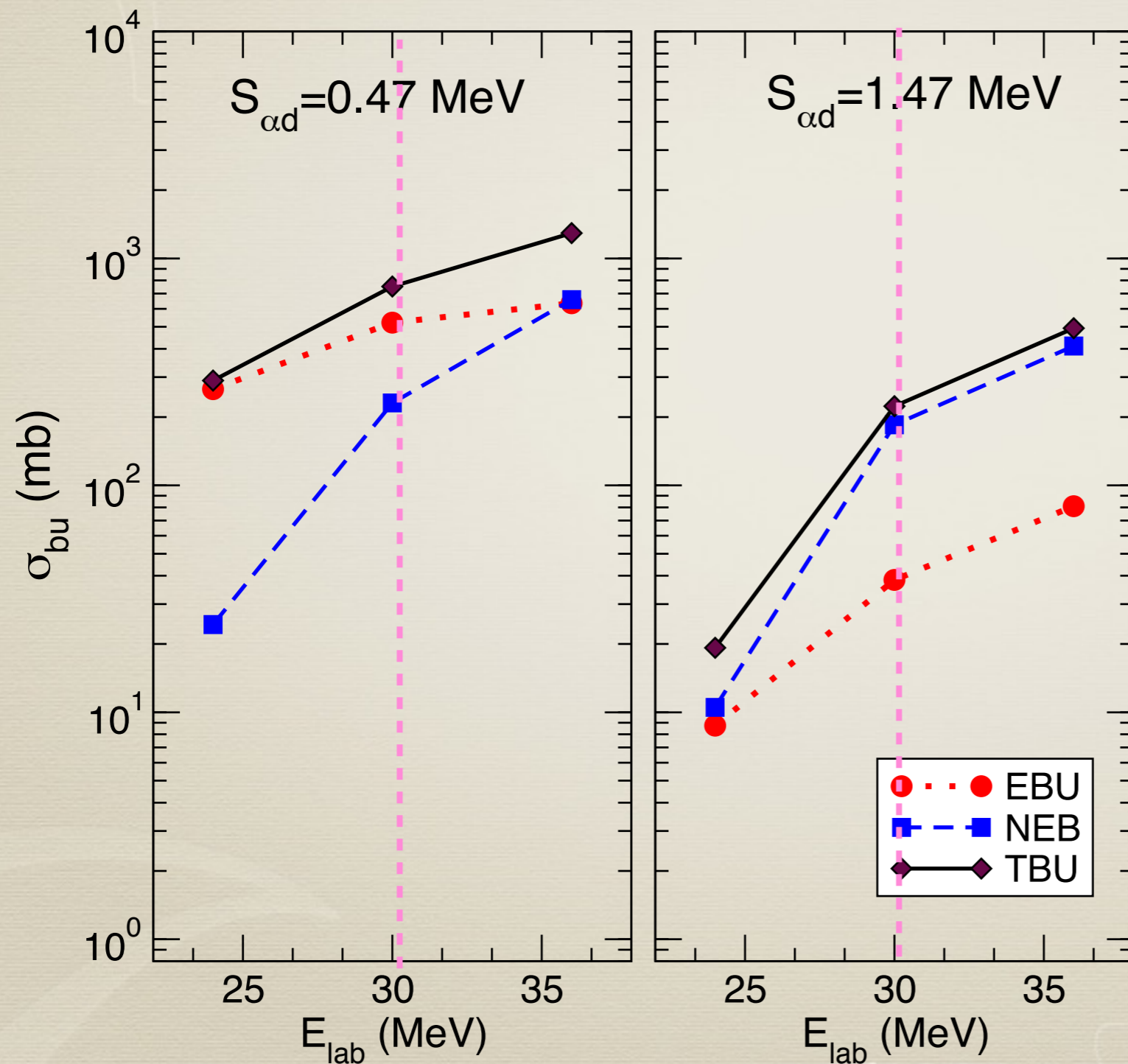


# Influence of the separation energy and the incident energy on the EBU and NEB

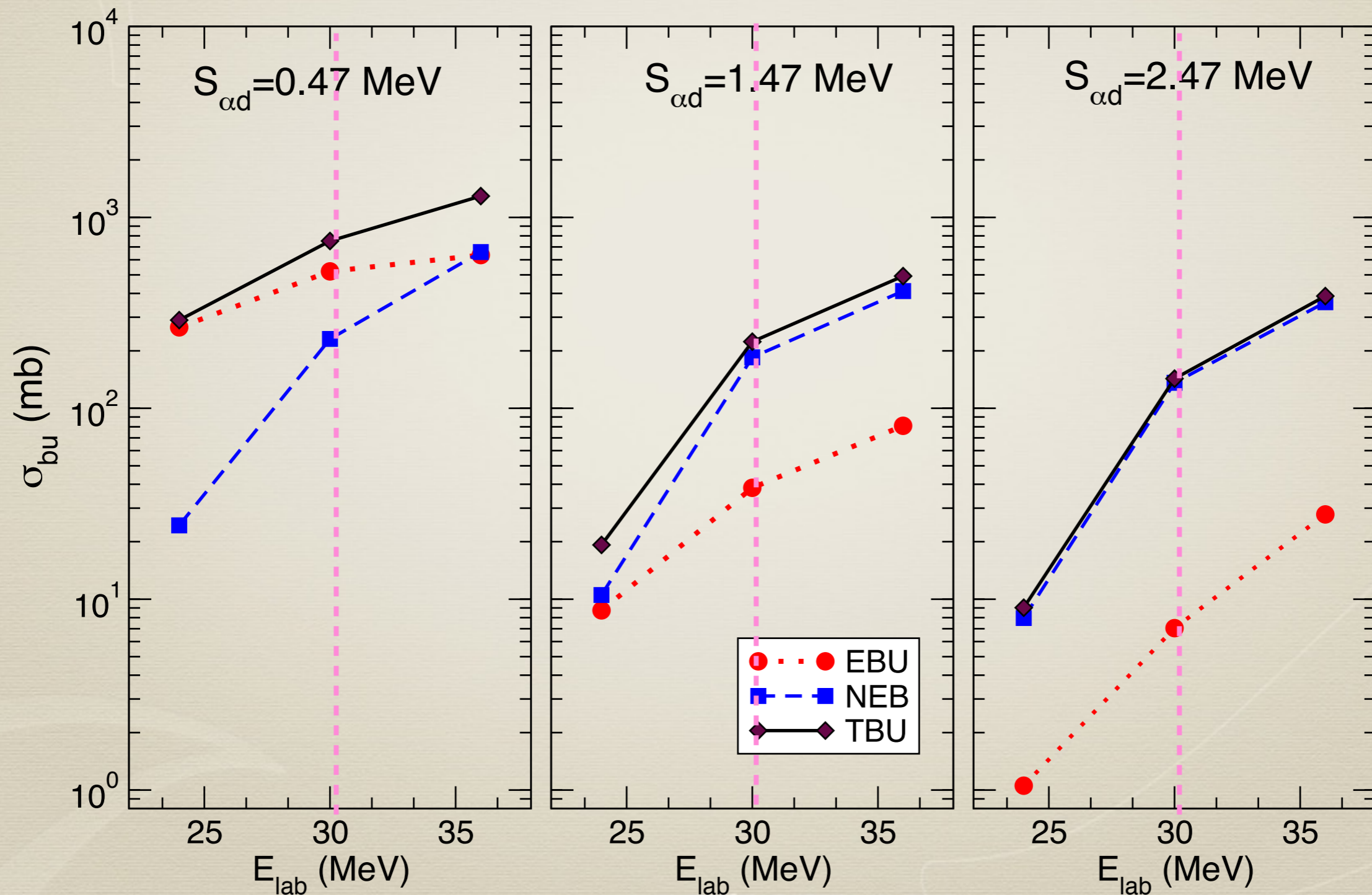




# Influence of the separation energy and the incident energy on the EBU and NEB

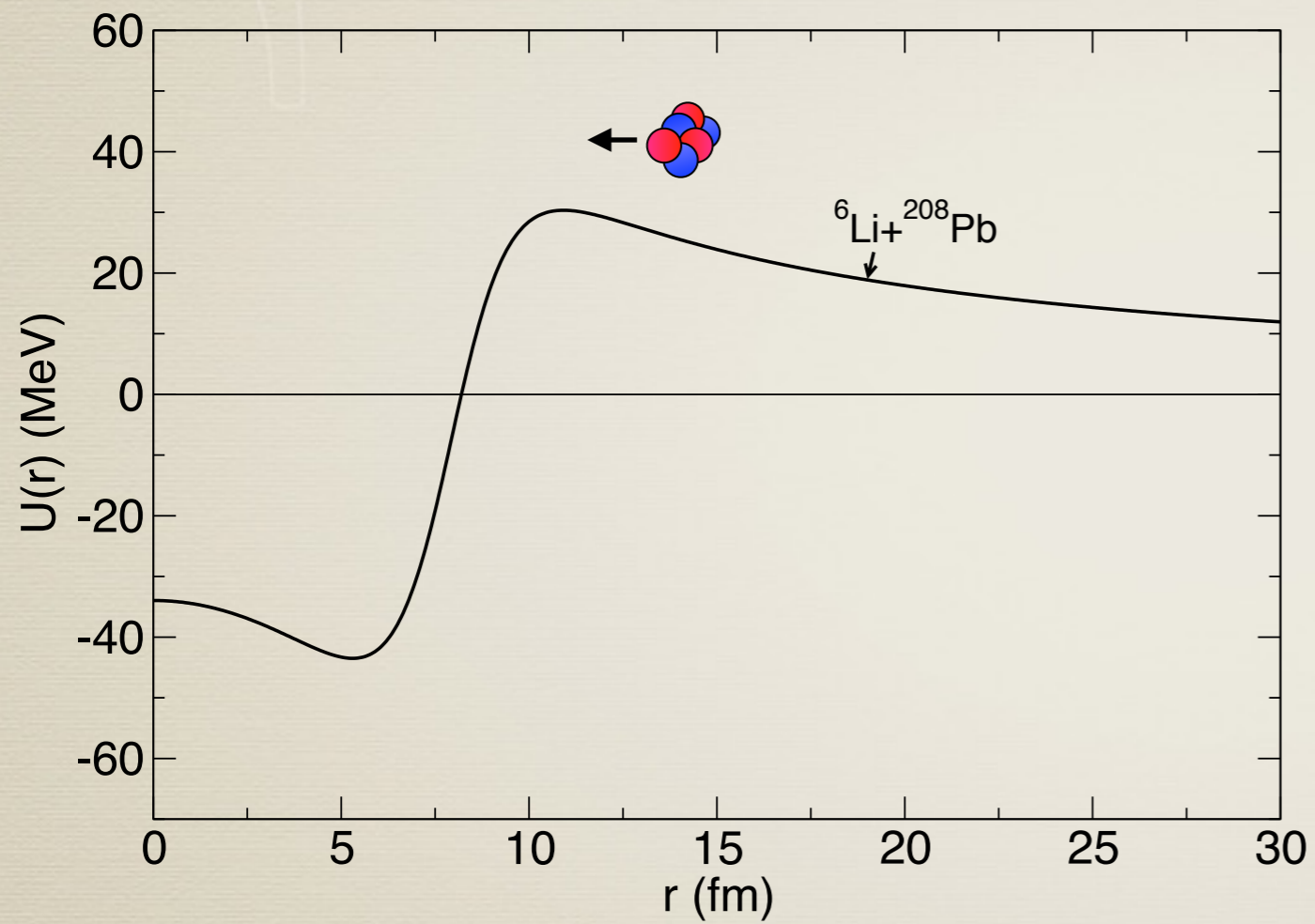


# Influence of the separation energy and the incident energy on the EBU and NEB

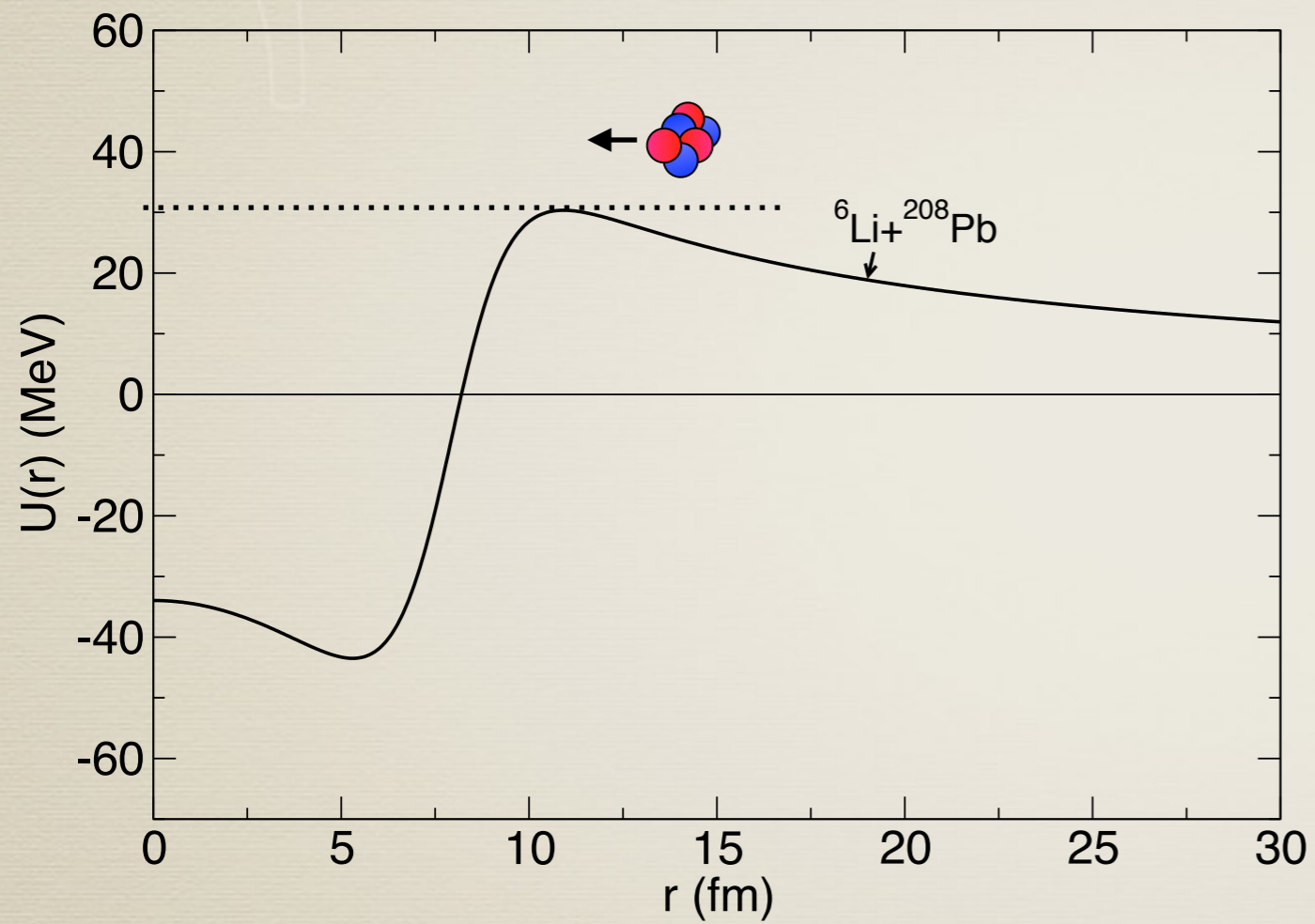




# Trojan Horse type process

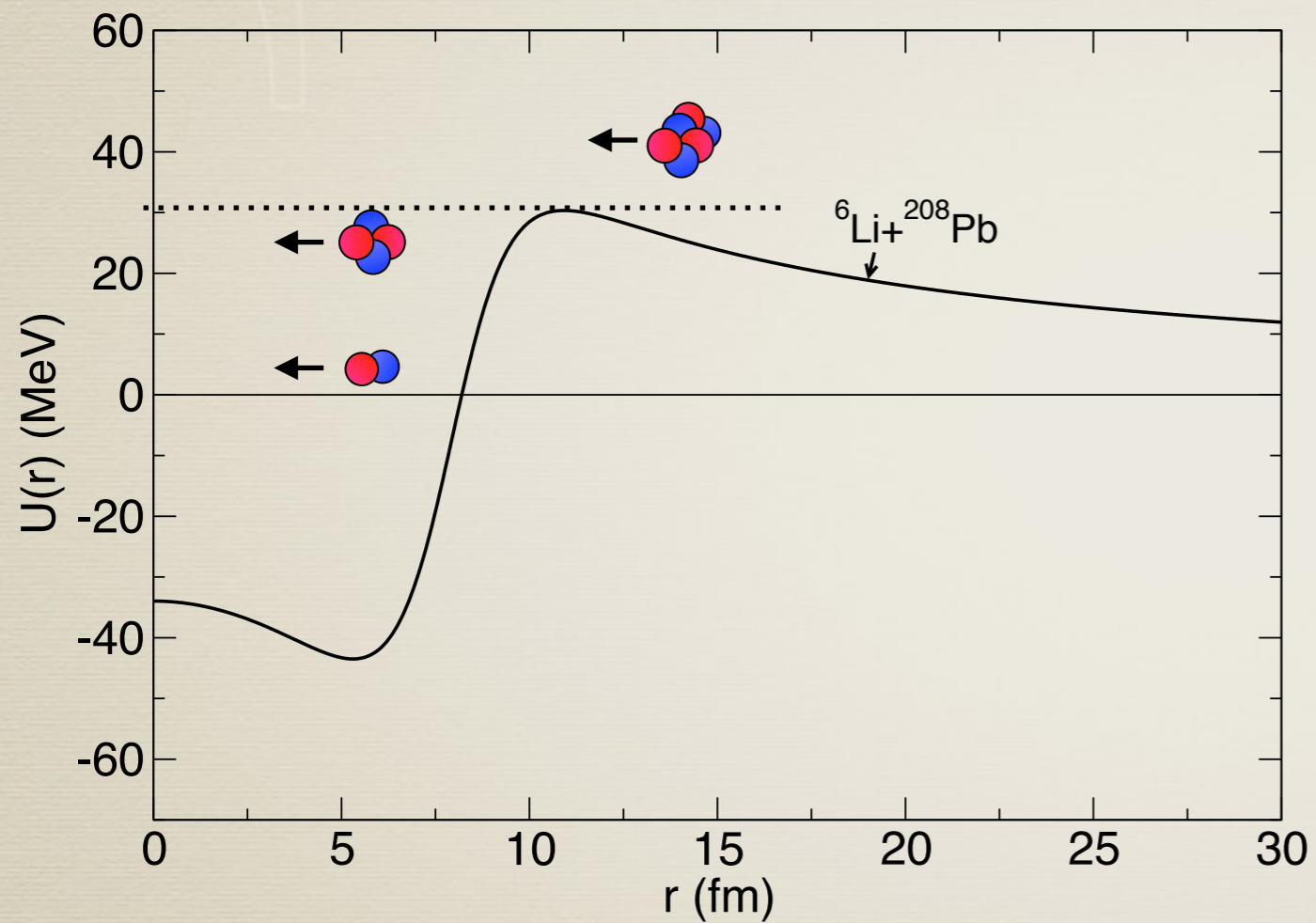


# Trojan Horse type process

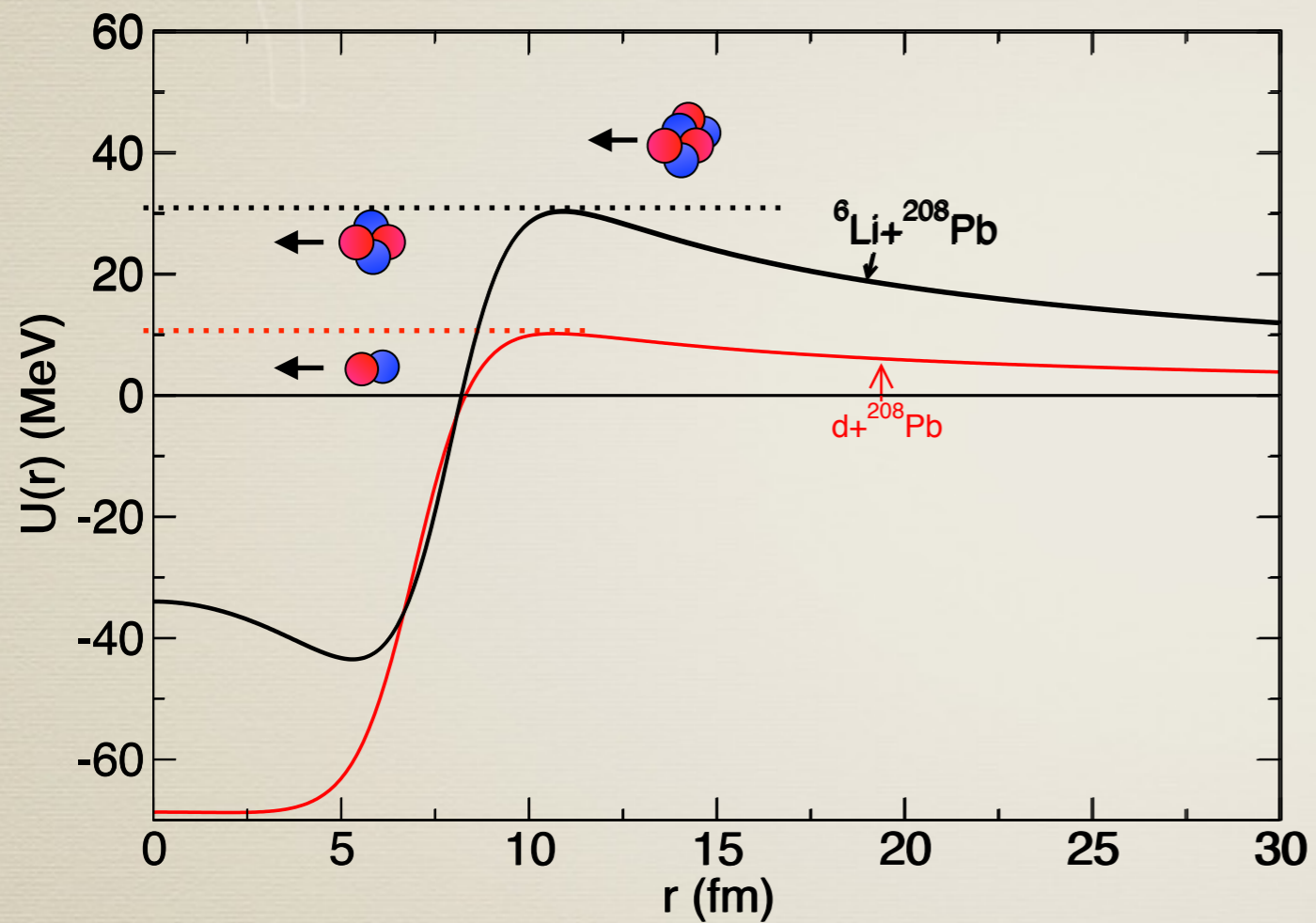




# Trojan Horse type process

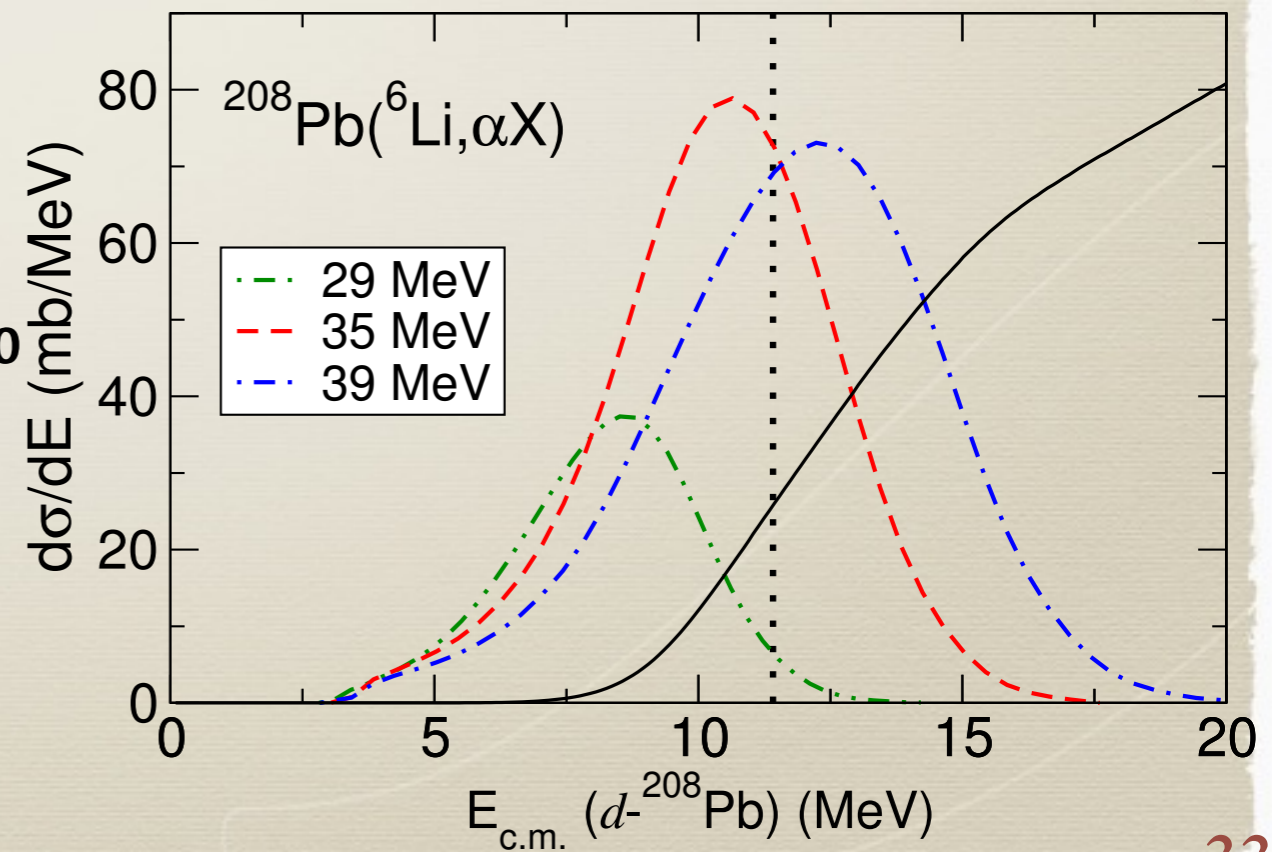
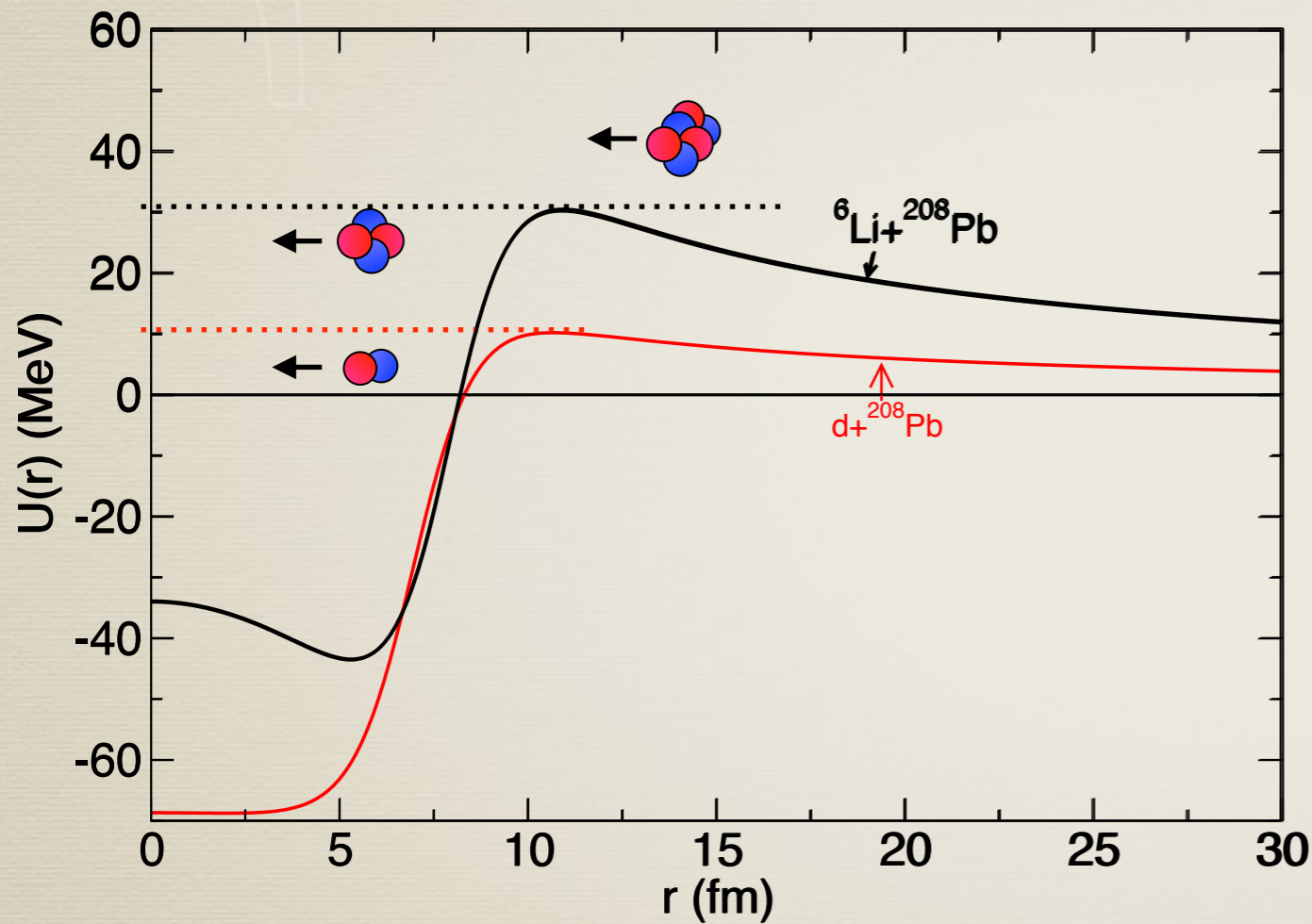


# Trojan Horse type process

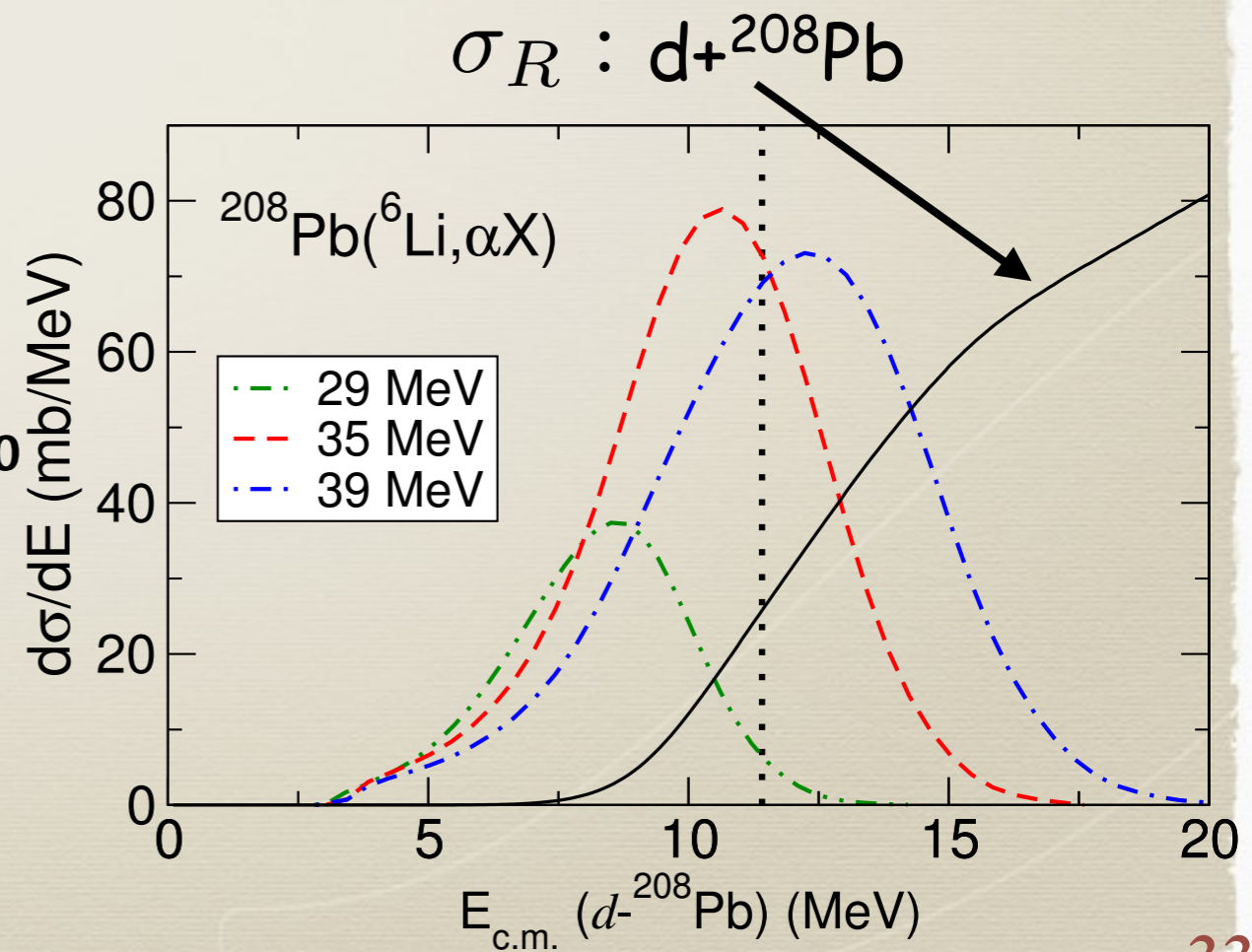
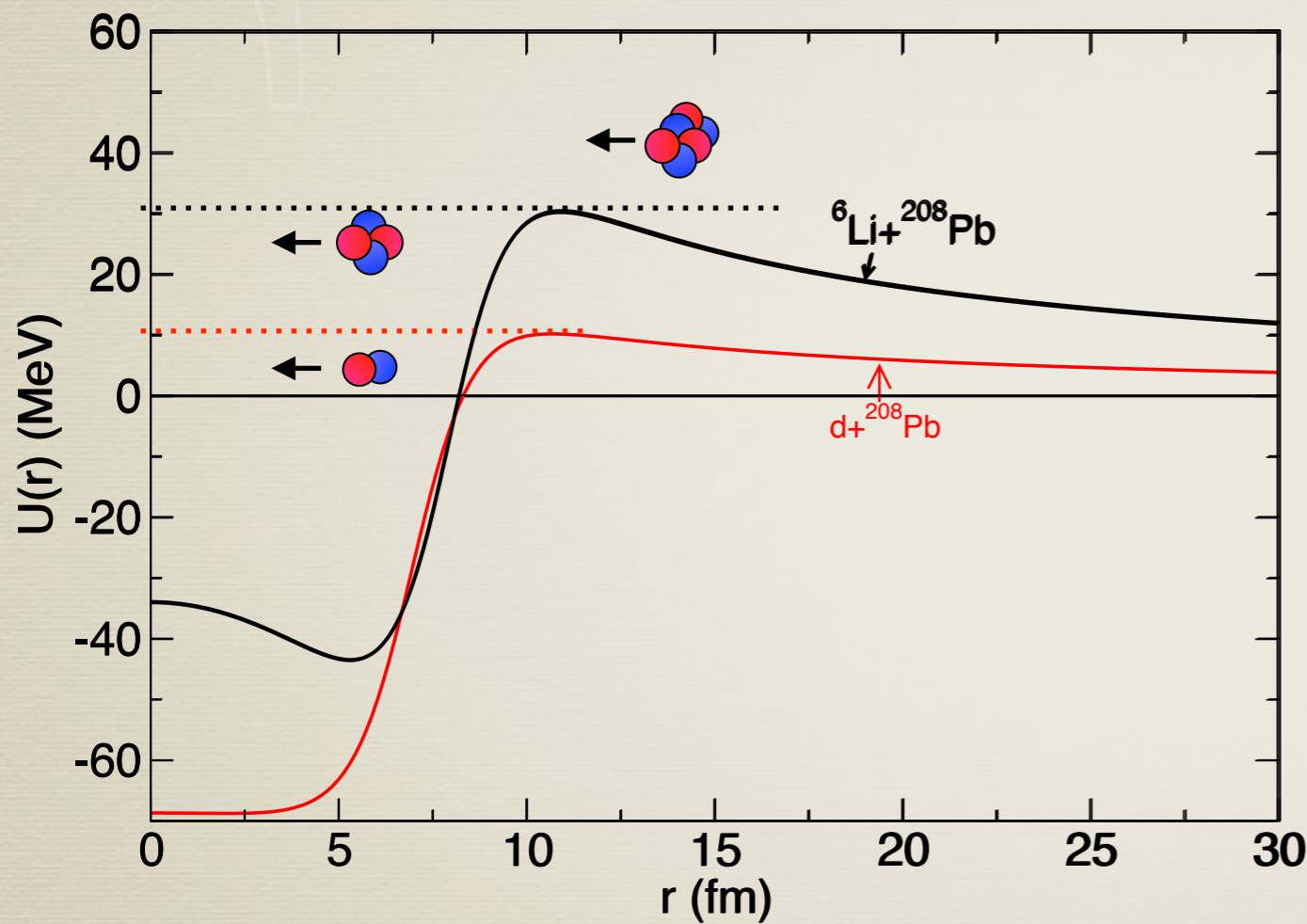




# Trojan Horse type process



# Trojan Horse type process





# Summary and Perspectives

# Summary



# Summary

- \* Our calculations show a overall agreement with the experimental data

# Summary

- \* Our calculations show a overall agreement with the experimental data
- \* For non-halo projectile ( $d, {}^6\text{Li}, {}^7\text{Li}, {}^7\text{Be}$ ), the inclusive breakup is dominated by NEB



# Summary

- \* Our calculations show a overall agreement with the experimental data
- \* For non-halo projectile ( $d, {}^6\text{Li}, {}^7\text{Li}, {}^7\text{Be}$ ), the inclusive breakup is dominated by NEB
- \* Relative importance between NEB and EBU depends on incident energy and projectile binding energy

# Summary

- \* Our calculations show a overall agreement with the experimental data
- \* For non-halo projectile ( $d, {}^6\text{Li}, {}^7\text{Li}, {}^7\text{Be}$ ), the inclusive breakup is dominated by NEB
- \* Relative importance between NEB and EBU depends on incident energy and projectile binding energy
- \* For halo nuclei ( ${}^{11}\text{Be}, {}^8\text{B}$ ), the EBU is found to be dominant.



# Perspectives

- \* Extend the model beyond DWBA
  - \* CDCC or Faddeev description of incident channel
- \* Inclusion of deformation of projectile ( $(^{10}\text{Be}^*)^{11}\text{Be}$ )
- \* Deep understanding of ICF and its application to surrogate reaction
- \* Extension to 3-body projectiles ( $^9\text{Be} \rightarrow \alpha + \alpha + n$ )

Thank you for your attention!!!

